

## Rules for Calculations in Code

### 1. Memory Usage Calculation

Rule Used: Memory is calculated based on the assumption that each element in the matrix (whether integer or float) takes 4 bytes.

Calculation:

- $\text{Memory Usage} = \text{Number of Rows} \times \text{Number of Columns} \times 4 \text{ bytes}$

This formula is used to estimate the total space used by the matrix.

### 2. Sparsity Calculation

Rule Used: Sparsity represents the percentage of elements in a matrix that are zero.

Calculation:

- $\text{Total Elements} = \text{Number of Rows} \times \text{Number of Columns}$
- $\text{Non-zero Elements} = \text{Count of elements} \neq 0$
- $\text{Sparsity} = (1 - (\text{Non-zero Elements} / \text{Total Elements})) \times 100\%$

This calculation helps measure how sparse the matrix is, indicating the proportion of zero entries.

### 3. User-User and Item-Item Similarity Calculation

Rule Used: Cosine similarity is used to calculate the similarity between users or items.

Calculation:

- $\text{Dot Product} = \sum(A[i][k] * A[j][k])$
- Norm Calculation:
  - $\text{Norm}_i = \sqrt{\sum((A[i][k])^2)}$
  - $\text{Norm}_j = \sqrt{\sum((A[j][k])^2)}$
- Similarity Score:
  - $\text{Similarity}[i][j] = \text{Dot Product} / (\text{Norm}_i * \text{Norm}_j)$

If either  $\text{Norm}_i$  or  $\text{Norm}_j$  is zero, similarity is set to 0 to avoid division by zero.

This calculation is repeated for all user pairs or item pairs to form the similarity matrix.

### 4. Time Complexity

Rule Used: The time taken to execute the similarity computation is measured using `time.time()`.

Calculation:

- $\text{Time Complexity} = \text{End Time} - \text{Start Time}$

This metric indicates the duration of the similarity matrix computation.

## **5. Space Complexity**

Rule Used: The space complexity refers to the memory used by the similarity matrix itself.

Calculation:

- Same as the memory usage rule explained above.

The space complexity indicates the storage required to hold the similarity matrix.

### **Explanation of Functions:**

`user_user_similarity()`: Computes similarity between users by iterating over each user-user pair and applying cosine similarity.

`item_item_similarity()`: Computes similarity between items by iterating over each item-item pair and applying cosine similarity.

Both functions return the similarity matrix along with time complexity, space complexity, and sparsity of the computed matrix.