

Question 1:

Let G: $\langle \text{stmt} \rangle \rightarrow \langle \text{assignment} \rangle / \langle \text{if-stmt} \rangle$

$\langle \text{if-stmt} \rangle \rightarrow \text{if}(\langle \text{cond.} \rangle) \langle \text{stmt} \rangle / \text{if}(\langle \text{cond.} \rangle) \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$

$\langle \text{cond.} \rangle \rightarrow \langle \text{arth.E} \rangle \langle \text{relop} \rangle \langle \text{arth.E} \rangle$

$\langle \text{assignment} \rangle \rightarrow \langle \text{id} \rangle = \langle \text{arth.E} \rangle$

$\langle \text{arth.E} \rangle \rightarrow \langle \text{id} \rangle / \langle \text{const.} \rangle$

$\langle \text{relop} \rangle \rightarrow < / > / = =$

$\langle \text{id} \rangle \rightarrow \text{x} / \text{y}$

$\langle \text{const.} \rangle \rightarrow -1 / 1 / 2 / 0$

Construct the parse tree and left most derivation of the following string:

if (x >2) y=1

else if (x= =2) y=0

else y = -1

Answer

$\langle \text{stmt} \rangle \Rightarrow \langle \text{if-stmt} \rangle$

$\Rightarrow \text{if}(\langle \text{cond.} \rangle) \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$

$\Rightarrow \text{if}(\langle \text{arth.E} \rangle \langle \text{relop} \rangle \langle \text{arth.E} \rangle) \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$

$\Rightarrow \text{if}(\langle \text{id} \rangle \langle \text{relop} \rangle \langle \text{arth.E} \rangle) \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$

$\Rightarrow \text{if}(\text{x} \langle \text{relop} \rangle \langle \text{arth.E} \rangle) \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$

$\Rightarrow \text{if}(\text{x} > \langle \text{arth.E} \rangle) \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$

$\Rightarrow \text{if}(\text{x} > \langle \text{const.} \rangle) \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$

$\Rightarrow \text{if}(\text{x} > \text{2}) \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$

$\Rightarrow \text{if } (x > 2) <\text{assignment}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) <\text{id}> = <\text{arth.E}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = <\text{arth.E}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = <\text{const.}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else } <\text{if-stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else if } (<\text{cond.}>) <\text{stmt}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else if } (<\text{arth.E}> <\text{relop}> <\text{arth.E}>) <\text{stmt}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else if } (<\text{id}> <\text{relop}> <\text{arth.E}>) <\text{stmt}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else if } (x <\text{relop}> <\text{arth.E}>) <\text{stmt}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else if } (x == <\text{arth.E}>) <\text{stmt}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else if } (x == <\text{const.}>) <\text{stmt}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else if } (x == 2) <\text{stmt}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else if } (x == 2) <\text{assignment}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else if } (x == 2) <\text{id}> = <\text{arth.E}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else if } (x == 2) \text{ y} = <\text{arth.E}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \text{ y} = 1 \text{ else if } (x == 2) \text{ y} = <\text{const.}> \text{ else } <\text{stmt}>$

$\Rightarrow \text{if } (x > 2) \ y = 1 \text{ else if } (x == 2) \ y = \textcolor{red}{0} \text{ else } \langle \text{stmt} \rangle$

$\Rightarrow \text{if } (x > 2) \ y = 1 \text{ else if } (x == 2) \ y = 0 \text{ else } \langle \textcolor{red}{\text{assignment}} \rangle$

$\Rightarrow \text{if } (x > 2) \ y = 1 \text{ else if } (x == 2) \ y = 0 \text{ else } \langle \textcolor{red}{id} \rangle = \langle \textcolor{red}{arth.E} \rangle$

$\Rightarrow \text{if } (x > 2) \ y = 1 \text{ else if } (x == 2) \ y = 0 \text{ else } \textcolor{red}{y} = \langle \textcolor{red}{arth.E} \rangle$

$\Rightarrow \text{if } (x > 2) \ y = 1 \text{ else if } (x == 2) \ y = 0 \text{ else } y = \langle \textcolor{red}{const.} \rangle$

$\Rightarrow \text{if } (x > 2) \ y = 1 \text{ else if } (x == 2) \ y = 0 \text{ else } y = \textcolor{red}{-1}$
