Calibration with opticut

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Chapter 1

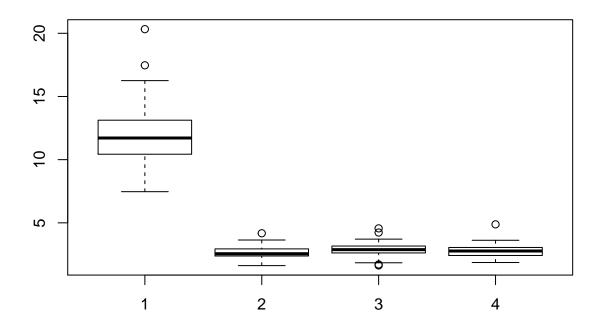
 $z \leftarrow ifelse(g == 1, 1, 0)$

Calibration with single species

This is not necessarily great. library(opticut) ## Loading required package: pbapply ## opticut 0.0-9 2016-10-30 library(dclone) ## Warning: package 'dclone' was built under R version 3.2.5 ## Loading required package: coda ## Loading required package: parallel ## Loading required package: Matrix ## Warning: package 'Matrix' was built under R version 3.2.5 ## dclone 2.1-2 2016-03-11 library(rjags) ## Linked to JAGS 4.2.0 ## Loaded modules: basemod, bugs source("~/repos/opticut/extras/calibrate.R") set.seed(234) n < -50*4K <- 4 g <- sample(1:K, n, replace=TRUE) $x \leftarrow rnorm(n, 0, 1)$

```
b0 <- 1
b1 <- 1.5
a < -0.2
mu \leftarrow b0 + z*b1 + x*a
#p <- plogis(mu)</pre>
#y \leftarrow rbinom(n, 1, p)
lam <- exp(mu)</pre>
y <- rpois(n, lam)
table(y, g)
##
      g
## y
       1 2 3 4
## 0 0 4 5 2
##
    1 0 10 12 12
##
    2 0 9 9 10
##
    3 1 8 13 7
    4 1 6 11 6
##
##
    5 0 7 8 5
    6 2 0 3 4
##
##
   7 0 1 0 1
##
    8 4 0 2 0
    9 7 0 0 0
##
    10 4 0 0 0
##
##
    11 4 0 0 0
##
    12 3 0 0 0
##
    13 4 0 0 0
##
    14 2 0 0 0
##
    15 1 0 0 0
##
    16 4 0 0 0
##
    17 4 0 0 0
##
    18 2 0 0 0
##
    20 1 0 0 0
##
    21 1 0 0 0
```

boxplot(lam ~ g)



```
df <- data.frame(y=y, x=x, g=g)</pre>
df \leftarrow df[-(1:5),]
\#o \leftarrow opticut(y \sim x, data=df, strata=g, dist="binomial")
o <- opticut(y ~ x, data=df, strata=g, dist="poisson")
summary(o)
## Multivariate opticut results, comb = rank, dist = poisson
##
## Call:
## opticut.formula(formula = y ~ x, data = df, strata = g, dist = "poisson")
##
## Best supported model with logLR >= 2:
        split assoc
                              muO
                          Ι
                                   mu1 logLR w
                +++ 0.6293 2.744 12.06 245.8 1
            1
## Sp 1
## 3 binary splits
co <- calibrate(o, cbind("Sp 1"=(y[1:5])), model.matrix(~x, data.frame(x=x[1:5])))
## Compiling model graph
##
      Resolving undeclared variables
      Allocating nodes
##
## Graph information:
```

```
##
      Observed stochastic nodes: 5
##
      Unobserved stochastic nodes: 6
##
      Total graph size: 70
##
## Initializing model
y[1:5]
## [1]
        4 2 10 4 10
g[1:5]
## [1] 3 4 1 4 1
co$gnew
## [1] "4" "3" "1" "2" "1"
round(co$pi, 2)
##
           1
                2
                     3
                          4
## [1,] 0.01 0.33 0.33 0.33
## [2,] 0.00 0.33 0.34 0.34
## [3,] 1.00 0.00 0.00 0.00
## [4,] 0.00 0.34 0.33 0.32
## [5,] 1.00 0.00 0.00 0.00
```

We get g=1 cases correctly classified (this is where Sp1 is to be found), But the rest is just all equally probable. All what we see is that it is not g=1. All makes sense, but not very useful. Luckily for us, we usually have >1 species.

Chapter 2

Calibration with multiple species

This should work much better in principle.

```
set.seed(234)
n < -50*4
K <- 4
g <- sample(1:K, n, replace=TRUE)
g[1:K] \leftarrow 1:K
x \leftarrow rnorm(n, 0, 1)
z <- ifelse(g %in% 1:2, 1, 0)
b0 <- 1
b1 <- 1.5
a < -0.2
mu \leftarrow b0 + z*b1 + x*a
lam <- exp(mu)</pre>
y1 <- rpois(n, lam)
z <- ifelse(g %in% 2:3, 1, 0)
b0 <- 1
b1 <- 1.5
a < -0.2
mu \leftarrow b0 + z*b1 + x*a
lam <- exp(mu)</pre>
y2 <- rpois(n, lam)
y \leftarrow cbind(y1=y1, y2=y2)
df <- data.frame(x=x, g=g)</pre>
df \leftarrow df[-(1:5),]
yy <- y[-(1:5),]
o <- opticut(yy ~ x, data=df, strata=g, dist="poisson")</pre>
summary(o)
```

```
## Multivariate opticut results, comb = rank, dist = poisson
##
## Call:
## opticut.formula(formula = yy ~ x, data = df, strata = g, dist = "poisson")
## Best supported models with logLR >= 2:
      split assoc
                       I
                           mu0 mu1 logLR w
       1+2
              +++ 0.6344 2.823 12.62 331.6 1
## y1
              +++ 0.6502 2.499 11.79 314.5 1
## y2
        2+3
## 3 binary splits
co <- calibrate(o, y[1:5,], df[1:5,])</pre>
## Compiling model graph
      Resolving undeclared variables
##
##
      Allocating nodes
## Graph information:
##
      Observed stochastic nodes: 10
      Unobserved stochastic nodes: 7
##
##
      Total graph size: 122
##
## Initializing model
y[1:5,]
       y1 y2
## [1,] 14 3
## [2,] 14 17
## [3,] 3 6
## [4,] 4 2
## [5,] 5 1
g[1:5]
## [1] 1 2 3 4 1
co$gnew
## [1] "1" "2" "3" "4" "4"
round(co$pi, 2)
                     3
           1
                2
##
## [1,] 0.98 0.02 0.00 0.00
## [2,] 0.00 1.00 0.00 0.00
## [3,] 0.00 0.05 0.88 0.07
## [4,] 0.08 0.00 0.01 0.91
## [5,] 0.07 0.00 0.00 0.93
```

Chapter 3

Dolina and calibration

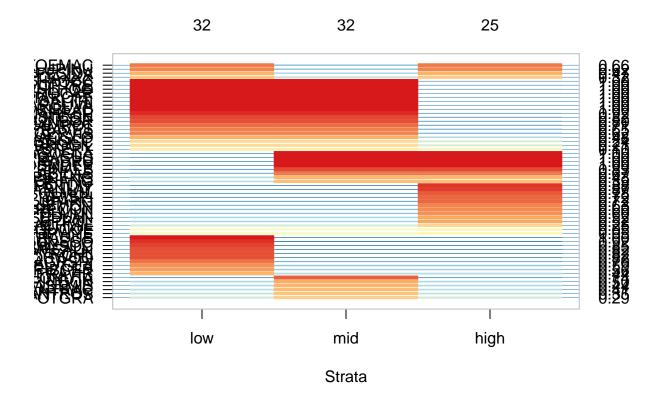
```
data(dolina)
dolina$samp$stratum <- as.integer(dolina$samp$stratum)</pre>
Y <- dolina$xtab#[dolina$samp$method=="Q",]
X <- dolina$samp#[dolina$samp$method=="Q",]
inew <- 1:nrow(Y) %in% sample(nrow(Y), 10)</pre>
Y \leftarrow Y[,colSums(Y[!inew,] > 0) >= 20]
\#Y \leftarrow ifelse(Y > 0, 1, 0)
x \leftarrow X[!inew,]
xnew <- dolina$samp[inew,]</pre>
y <- Y[!inew,]</pre>
ynew <- Y[inew,]</pre>
o <- opticut(y ~ stratum + lmoist + method, data=x, strata=mhab, dist="poisson")
#o <- opticut(y ~ 1, data=x, strata=mhab, dist="poisson")
## binary calibration
cal <- calibrate(o, ynew, xnew)</pre>
## Compiling model graph
##
      Resolving undeclared variables
##
      Allocating nodes
## Graph information:
##
      Observed stochastic nodes: 190
##
      Unobserved stochastic nodes: 29
##
      Total graph size: 1901
##
## Initializing model
#cal <- calibrate(o, ynew)</pre>
round(cal$pi,2)
##
            LI
                       TL
                            R.O
                 DW
```

```
## 11R3T 0.05 0.83 0.04 0.08
## 12A4Q 0.00 0.12 0.87 0.00
## 13A2T 0.46 0.05 0.47 0.03
## 1A1T 0.44 0.07 0.45 0.04
## 1A6T 0.43 0.05 0.44 0.08
## 3H2T 0.00 0.09 0.00 0.90
## 4A7T 0.38 0.07 0.38 0.18
## 4R3Q 0.00 0.00 0.00 1.00
## 7R1Q 0.00 0.00 0.00 1.00
## 9L3T 0.81 0.00 0.18 0.00
round(cor(cal$pi),2)
##
         LI
               DW
                     TL
                            RO
      1.00 -0.29
                  0.23 - 0.63
## LI
## DW -0.29
            1.00 -0.18 -0.25
## TL 0.23 -0.18 1.00 -0.70
## RO -0.63 -0.25 -0.70 1.00
data.frame(predicted=cal$gnew,
    truth=dolina$samp[inew,"mhab"],
    OK=cal$gnew == dolina$samp[inew,"mhab"])
##
      predicted truth
                         OK
## 1
             DW
                   RO FALSE
## 2
             TL
                   LI FALSE
## 3
             TL
                   LI FALSE
## 4
             TL
                   LI FALSE
## 5
             TL
                   LI FALSE
## 6
             RO
                   DW FALSE
                       TRUE
## 7
             LI
                   LI
## 8
             RO
                       TRUE
                   RO
## 9
             RO
                   R.O
                       TRUE
             LI
                   TL FALSE
## 10
cm <- table(pred=cal$gnew, true=X[inew,"mhab"])</pre>
cm <- cm[rownames(cm),rownames(cm)]</pre>
cm
##
       true
## pred DW LI RO TL
##
     DW
         0
            0
               1
                  0
           1
##
     LI
        0
               0
                  1
##
     RO
        1
            0
               2
                  0
     TL
         0
            4 0 0
##
```

```
sum(diag(cm)) / sum(cm)
## [1] 0.3
## multinomial calibration using calibrate.default
oo <- lapply(1:ncol(y), function(i) {</pre>
    glm(y[,i] ~ mhab + stratum + lmoist + method, x, family=poisson)
})
xnew <- model.matrix(~ stratum + lmoist + method, xnew)</pre>
cal <- calibrate(oo, ynew, xnew, K=4)
## Compiling model graph
      Resolving undeclared variables
##
      Allocating nodes
## Graph information:
##
      Observed stochastic nodes: 190
##
      Unobserved stochastic nodes: 29
##
      Total graph size: 2187
##
## Initializing model
round(cal$pi,2)
         [,1] [,2] [,3] [,4]
## 11R3T 0.07 0.66 0.11 0.16
## 12A4Q 0.00 0.02 0.98 0.00
## 13A2T 0.60 0.04 0.35 0.01
## 1A1T 0.64 0.03 0.31 0.02
## 1A6T 0.44 0.04 0.48 0.04
## 3H2T 0.00 0.60 0.00 0.40
## 4A7T 0.49 0.04 0.39 0.09
## 4R3Q 0.00 0.00 0.00 1.00
## 7R1Q 0.00 0.00 0.00 1.00
## 9L3T 0.82 0.01 0.18 0.00
round(cor(cal$pi),2)
         [,1] [,2] [,3] [,4]
##
## [1,] 1.00 -0.41 0.12 -0.63
## [2,] -0.41 1.00 -0.36 -0.04
## [3,] 0.12 -0.36 1.00 -0.62
## [4,] -0.63 -0.04 -0.62 1.00
data.frame(predicted=levels(x$mhab)[cal$gnew],
    truth=dolina$samp[inew,"mhab"],
    OK=levels(x$mhab)[cal$gnew] == dolina$samp[inew,"mhab"])
```

```
##
      predicted truth
                          ŊΚ
## 1
                   RO FALSE
             DW
## 2
             TL
                   LI FALSE
## 3
             LI
                   LI
                       TRUE
## 4
             LI
                   LI
                       TRUE
             TL
                   LI FALSE
## 5
## 6
             DW
                   DW
                       TRUE
## 7
             LI
                   LI
                       TRUE
## 8
             R.O
                   R.O
                       TRUE
## 9
             RO
                   RO
                       TRUE
## 10
             LI
                   TL FALSE
cm <- table(pred=levels(x$mhab)[cal$gnew], true=X[inew,"mhab"])</pre>
cm <- cm[rownames(cm),rownames(cm)]</pre>
cm
##
       true
## pred DW LI RO TL
##
     DW
         1
            0
               1
##
     LI
        0
            3
              0
                  1
##
     RO
         0
            0
               2
                  0
     TL
        0
           2 0 0
sum(diag(cm)) / sum(cm)
## [1] 0.6
library(optpart)
## Warning: package 'optpart' was built under R version 3.2.5
## Loading required package: cluster
## Warning: package 'cluster' was built under R version 3.2.5
## Loading required package: labdsv
## Loading required package: mgcv
## Warning: package 'mgcv' was built under R version 3.2.5
## Loading required package: nlme
## Warning: package 'nlme' was built under R version 3.2.5
## This is mgcv 1.8-15. For overview type 'help("mgcv-package")'.
## Loading required package: MASS
##
## Attaching package: 'labdsv'
```

```
## The following object is masked from 'package:stats':
##
##
       density
## Loading required package: plotrix
## Warning: package 'plotrix' was built under R version 3.2.5
##
## Attaching package: 'optpart'
## The following object is masked from 'package:labdsv':
##
##
       clustify
data(shoshsite)
data(shoshveg)
#elev <- cut(shoshsite$elevation, breaks=c(0, 7200, 8000, 9000, 20000))
#levels(elev) <- c("low", "mid1", "mid2", "high")
elev <- cut(shoshsite$elevation, breaks=c(0, 7800, 8900, 20000))
levels(elev) <- c("low", "mid", "high")</pre>
sveg <- as.matrix(shoshveg)</pre>
sveg[sveg > 0] <- 1
set.seed(1)
ss <- seq_len(nrow(sveg)) %in% sample.int(nrow(sveg), floor(nrow(sveg) * 0.9))
sveg1 <- sveg[ss,]</pre>
sveg1 <- sveg1[,colSums(sveg1) > 5]
elev1 <- elev[ss]</pre>
dim(sveg)
## [1] 150 368
dim(sveg1)
## [1] 135 85
sveg2 <- sveg[!ss, colnames(sveg1)]</pre>
elev2 <- elev[!ss]</pre>
o <- opticut(sveg1 ~ 1, strata=elev1, dist="binomial")</pre>
plot(o, sort=1)
```



```
co <- calibrate(o, sveg2)</pre>
## Compiling model graph
##
      Resolving undeclared variables
##
      Allocating nodes
## Graph information:
      Observed stochastic nodes: 1275
##
##
      Unobserved stochastic nodes: 100
##
      Total graph size: 7586
##
## Initializing model
data.frame(predicted=co$gnew,
    truth=elev2,
    OK=co$gnew == elev2,
    round(co$pi,2))
##
             predicted truth
                                 OK low mid high
## X1V90L019
                         mid FALSE 0.00 0.01 0.99
                  high
## X1V90P002
                   low
                         low TRUE 0.89 0.11 0.00
## X1V90L031
                   low
                         low TRUE 0.95 0.05 0.00
```

low TRUE 0.99 0.01 0.00

X1V891031

low

```
## X5V96I296
                   high
                         high
                               TRUE 0.00 0.00 1.00
## X5V96M122
                   high
                         high
                               TRUE 0.00 0.00 1.00
## X4V93R081
                    low
                          mid FALSE 1.00 0.00 0.00
## X1V901051
                   high
                         high
                               TRUE 0.00 0.00 1.00
## X1V891022
                               TRUE 0.01 0.99 0.00
                    mid
                          mid
## X4V89P048
                         high FALSE 0.02 0.93 0.04
                    mid
## X4V95S079
                          mid
                               TRUE 0.01 0.99 0.00
                    mid
## X2V95S211
                   high
                         high
                               TRUE 0.00 0.00 1.00
## X1V90L024
                   high
                         high
                              TRUE 0.00 0.00 1.00
## X5V96K201
                               TRUE 0.00 0.00 1.00
                   high
                         high
## X5V96I014
                    mid
                          \mbox{mid}
                               TRUE 0.04 0.96 0.00
sum(co$gnew == elev2) / nrow(sveg2)
```

[1] 0.8

3.1 Conclusions

- More species, merrier results (see simple simulation)
- Binary partitions might not be the best, especially for count models
- Multinomial models (K levels in g) are more eficient (see dolina example)
- Many species in binomial context work quite well, if K is not unreasonably high.

3.2 Todo

- OK use notation: j=1...p & r=1...S
- OK implement test cases for lm/glm
- OK write internal function (.calibrate)
- OK implement user interface: calibrate, calibrate.opticut(object, ynew, xnew, ...)
- add NB, beta, ZI cases (ZI: inits!) [drop all the 1-species models!]
- gaussian needs sig²