opticut: likelihood based optimal partitioning for indicator species analysis

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1 Introduction

General problem: find where species abundances are high vs. low in a way which leads to optimal classification by maximizing the contrast between the partitions.

Previous attempts: historical review, highlighting IndVal.

Issues with previous attempts:

- summary statistics & Monte Carlo randomization with p-values, no model,
- data types not always compatible with randomization (i.e. decimals),
- confounding effects to classification can impact power,
- assessing the ranking of partitions without inferential statements.

Goals:

- describe a general and extensible approach that addresses the above limitations,
- implement a computationally efficient algorithm,
- tools for exploring the results (i.e. summaries, plots) in a object oriented framework.

Why opticut?

- HPC is natively supported
- efficient for large number of partitions
- lots of models defined, extensible
- uncertainty and partitioning reliability

2 Theory

2.1 The quest for optimal binary partitioning

 Y_i 's are observations for a single species from n locations (i = 1, ..., n). g_i 's are known discrete descriptors of the locations with K levels (K > 2). $z^{(m)}$ is a binary reclassification of g taking values (0, 1). The superscript m = 1, ..., M indicates a possible combination of binary reclassification out of the total $M = 2^{K-1} - 1$ total combinations (excluding complements). See below for options for defining binary partitions. There can also be other site descriptors denoted as x_{ij} taking discrete or continuous values (j = 1, ..., p; number of predictors).

A suitable parametric model describes the relationship between the observations and the site descriptors through the probability density function $P(Y_i = y_i \mid z_i^{(m)}, x_{ij}, \theta)$ where θ is the vector of model parameters: $\theta = (\beta_0, \beta_1, \alpha_1, ..., \alpha_p)$. The choice of the parametric model depends on the nature of the observations. It can be Gaussian, Binomial, Poisson, ordinal, Beta regression, or zero-inflated models, with a suitable link function (f) for the mean: $f(\eta_i) = \beta_0^{(m)} + \beta_1^{(m)} z_i^{(m)} + \sum_{j=1}^p \alpha_j^{(m)} x_{ij}$.

 $\widehat{\theta^{(m)}}$ is the maximum likelihood estimate (MLE) of the model parameters given the data and classification m, with corresponding log-likelihood value $\widehat{l(\theta^{(m)};y)}$. Finding MLEs for all M candidate binary partitions leads to a set of log-likelihood values. One can compare the log-likelihood values to a null model (no binary partition is necessary) where $\beta_1 = 0$ leading to the MLE $\widehat{\theta^{(0)}}$ and corresponding log-likelihood value for the null model: $\widehat{l(\theta^{(0)};y)}$.

The log-likelihood ratio for each candidate partition can be calculated as $l(\widehat{\theta^{(m)}};y) - l(\widehat{\theta^{(0)}};y)$. The best supported binary partition is the model with the highest log-likelihood ratio value.

One way of calculating the indicator value for each candidate partition is based on expected values using the inverse link function as $\mu_0^{(m)} = f^{-1}(\beta_0^{(m)})$ and $\mu_1^{(m)} = f^{-1}(\beta_0^{(m)} + \beta_1^{(m)})$. $I = 1 - \min(\mu_0^{(m)}, \mu_1^{(m)})/\max(\mu_0^{(m)}, \mu_1^{(m)})$. Where $\mu_0^{(m)} = E[Y_i \mid z_i^{(m)} = 0, x_{ij} = 0]$ and $\mu_1^{(m)} = E[Y_i \mid z_i^{(m)} = 1, x_{ij} = 0]$ are expected values for the observations given the binary partition $z_i^{(m)}$ and at 0 value for all x_{ij} . This approach can be sensitive to the range of values supported by the link function. For example it works nicely with logarithmic or logistic link function where non-negativity of predicted values is ensured by definition. This is, however, not the case for the identity link in the Gaussian case, when negative values can

invaludate the indicator value calculations as described above. (This usually happens when confounding variables are not centered and the intercept then reflects that difference as part of the baseline.)

As an alternative, one can use the estimate $\beta_1^{(m)}$ itself to express the contrast between the two strata. This also makes the index more comparable when different link functions are used. We used the hyperbolic tangent function (or inverse Fisher's z transform) to scale the real valued $\beta_1^{(m)}$ into the unit range (0-1): $I = tanh(|\beta_1^{(m)}|) = \frac{exp(2|\beta_1^{(m)}|)-1}{exp(2|\beta_1^{(m)}|)+1}.$ Positive and negative cases are taken as absolute values, so that the index reflects only the contrast between strata, and not the direction of it. Negative value can happen when using all combinations.

2.2 Finding all possible binary partitions

Finding all combinations does not require a model or observed responses. It only takes a classification vector with K > 1 partitions.

kComb returns a 'contrast' matrix corresponding to all possible binary partitions of the factor with K levels. Complements are not counted twice, i.e. (0,0,1,1) is equivalent to (1,1,0,0). The number of such possible combinations is $M = 2^{K-1} - 1$.

Get the package and load it:

[3,]

[4,]

0

0

0

0

1

0

0

1

```
\#devtools::install\_github("psolymos/opticut")
#devtools::install("~/repos/opticut")
#devtools::check("~/repos/opticut")
#devtools::build("~/repos/opticut", binary=TRUE)
library(opticut)
## Loading required package: pbapply
## opticut 0.1-2
                      2016-09-14
kComb(k = 2)
##
        [,1]
## [1,]
## [2,]
kComb(k = 3)
        [,1] [,2] [,3]
##
## [1,]
           1
## [2,]
           0
                      0
                 1
## [3,]
           0
kComb(k = 4)
        [,1] [,2] [,3] [,4] [,5] [,6] [,7]
##
## [1,]
                 0
                      0
                           0
                                 1
                                      1
           1
## [2,]
           0
                 1
                      0
                           0
                                 1
                                      0
                                           0
```

0

1

0

0

allComb this takes a classification vector with at least 2 levels and returns a model matrix with binary partitions. checkComb checks if combinations are unique and non-complementary (misfits are returned as attributes).

```
(f <- rep(LETTERS[1:4], each=2))</pre>
## [1] "A" "A" "B" "B" "C" "C" "D" "D"
(mc <- allComb(f, collapse = "_"))</pre>
     A B C D A_B A_C A_D
## A 1 0 0 0
               1
## A 1 O O O
               1
                    1
                        1
## B O 1 O O
                        0
               1
                    0
## B O 1 O O
                   0
                        0
               1
## C O O 1 O
               0
                  1
                        0
## C O O 1 O
               0
## D O O O 1
               0
                    0
                        1
## D O O O 1
               0
## attr(,"collapse")
## [1] "_"
## attr(,"comb")
## [1] "all"
checkComb(mc)
## [1] TRUE
## attr(,"comp")
##
        iј
## attr(,"same")
##
        i j
mc2 \leftarrow cbind(z = 1 - mc[,1], mc[,c(1:ncol(mc), 1)])
colnames(mc2) <- 1:ncol(mc2)</pre>
mc2
     1 2 3 4 5 6 7 8 9
## A O 1 O O O 1 1 1 1
## A O 1 O O O 1 1 1 1
## B 1 O 1 O O 1 O O
## B 1 0 1 0 0 1 0 0 0
## C 1 0 0 1 0 0 1 0 0
## C 1 0 0 1 0 0 1 0 0
## D 1 0 0 0 1 0 0 1 0
## D 1 0 0 0 1 0 0 1 0
checkComb(mc2)
## [1] FALSE
## attr(,"comp")
##
        i j
```

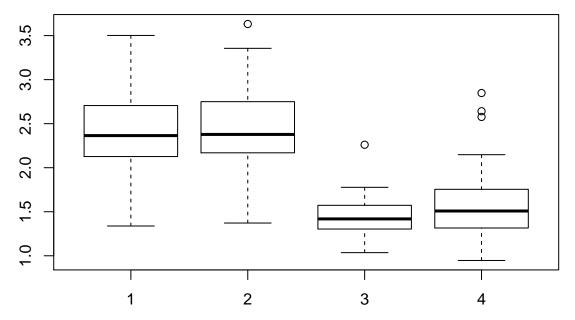
```
## [1,] 1 2
## [2,] 1 9
## attr(,"same")
## i j
## [1,] 9 2
```

2.3 Poisson count model example

```
set.seed(1234)
n <- 200
x0 <- sample(1:4, n, TRUE)
x1 <- ifelse(x0 %in% 1:2, 1, 0)
x2 <- rnorm(n, 0.5, 1)
table(x0,x1)</pre>
```

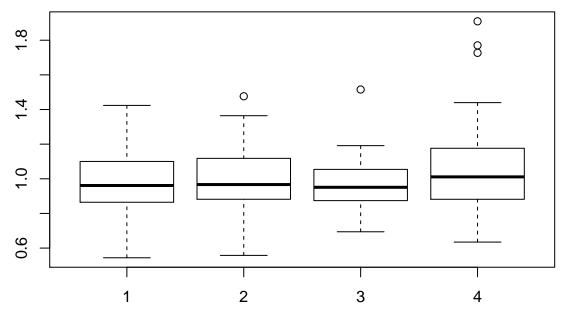
```
## x0 0 1
## 1 0 52
## 2 0 51
## 3 51 0
## 4 46 0
```

```
lam1 \leftarrow exp(0.5 + 0.5*x1 + -0.2*x2)
boxplot(lam1~x0)
```



```
Y1 <- rpois(n, lam1)
lam2 <- exp(0.1 + 0.5*ifelse(x0==4,1,0) + 0.2*x2)
boxplot(lam2~x0)
```

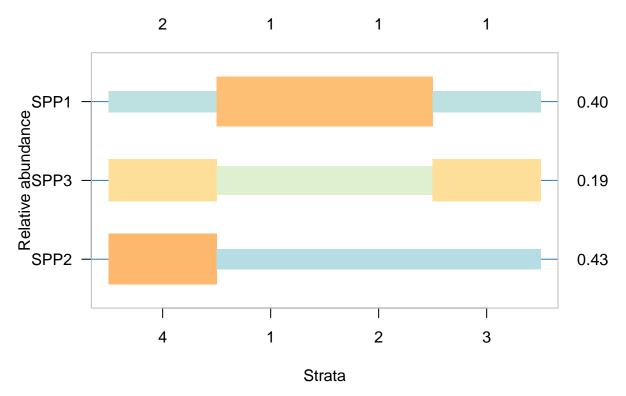
```
Y2 <- rpois(n, lam2)
lam3 <- exp(0.1 + -0.2*x2)
boxplot(lam3~x0)
```



```
Y3 <- rpois(n, lam3)
Y <- cbind(SPP1=Y1, SPP2=Y2, SPP3=Y3)
X <- model.matrix(~x2)
Z <- allComb(x0)
opticut1(Y1, X, Z, dist="poisson")
```

```
## Univariate opticut results, comb = all, dist = poisson
## I = 0.3972; w = 0.9842; H = 0.9687; logL_null = -343.8
##
## Best supported models with logLR >= 2:
```

```
assoc I mu0 mu1 logLR
## 1 2 +++ 0.3972 1.739 2.647 8.396 0.984200
         -- 0.3006 2.337 1.714 3.051 0.004694
## 4
         -- 0.3005 2.371 1.739 3.027 0.004583
## 2
         ++ 0.2505 2.048 2.645 2.633 0.003092
## 1
         ++ 0.2483 2.048 2.639 2.598 0.002987
## 7 binary splits (2 models not shown)
opticut1(Y2, X, Z, dist="poisson")
## Univariate opticut results, comb = all, dist = poisson
## I = 0.4326; w = 0.9254; H = 0.8584; logL_null = -315.6
##
## Best supported models with logLR >= 2:
##
      assoc
             I muO mu1 logLR
         ++ 0.4326 1.134 1.803 6.245 0.92545
## 1 3
         -- 0.2863 1.486 1.107 3.119 0.04063
         -- 0.2342 1.458 1.149 2.064 0.01415
## 7 binary splits (4 models not shown)
opticut1(Y3, X, Z, dist="poisson")
## Univariate opticut results, comb = all, dist = poisson
## I = 0.1899; w = 0.2205; H = 0.1562; logL_null = -244.4
##
## Best supported model:
      assoc
                 Ι
                     muO
                            mu1 logLR
          - 0.1899 1.096 0.9047 0.805 0.2205
## 7 binary splits (6 models not shown)
summary(m <- opticut(Y ~ x2, strata=x0, dist="poisson", comb="all"))</pre>
## Multivariate opticut results, comb = all, dist = poisson
##
## Call:
## opticut(formula = Y ~ x2, strata = x0, dist = "poisson", comb = "all")
##
## Best supported models with logLR >= 2:
##
       split assoc
                        I muO mu1 logLR
              +++ 0.3972 1.739 2.647 8.396 0.9842
## SPP1
        1 2
                ++ 0.4326 1.134 1.803 6.245 0.9254
## SPP2
           4
## 7 binary splits
## 1 species not shown
plot(m, cut=-Inf)
```



Describe here what is what in the output.

2.4 Not using all possible partitions

Blindly fitting a model to all possible partitions is wasteful use of resources. Instead, one can rank the K partitions based on expected response values $(\mu_1, ..., \mu_k, ..., \mu_K,$ where $\mu_k = E[Y_i \mid g_i = k, x_{ij} = 0])$. This way we have to explore only K - 1 partitions:

oComb(1:4)

```
##
     1 1 2 1 2 3
## 1 1
          1
                1
## 2 0
          1
                1
## 3 0
         0
                1
## 4 0
         0
## attr(,"rank")
## 1 2 3 4
## 1 2 3 4
```

oComb return the 'contrast' matrix based on the rank vector as input. Rank 1 means lowest expected value among the partitions.

The function rankComb fits the model with multiple (K > 2) factor levels to find out the ranking, and returns a binary classification matrix similarly to allComb:

```
head(rc <- rankComb(Y1, model.matrix(~x2), as.factor(x0), dist="poisson"))</pre>
```

```
## 2 1 2 1 2 4
## 1 0 1 1
```

```
## 3 0 0 0 0 ## 3 0 0 0 0 ## 4 0 0 1 ## 3 0 0 0
```

```
attr(rc, "est")
```

```
## 1 2 3 4
## 2.644132 2.650397 1.738868 1.738892
```

Note that the ranking varies from species to species, thus it is not possible to supply the resulting matrix as strata definition:

```
summary(opticut(Y ~ x2, strata=x0, dist="poisson", comb="rank"))
```

```
## Multivariate opticut results, comb = rank, dist = poisson
##
## Call:
## opticut(formula = Y ~ x2, strata = x0, dist = "poisson", comb = "rank")
##
## Best supported models with logLR >= 2:
                             mu0
##
        split assoc
                         Ι
                                   mu1 logLR
## SPP1
          1 2
                +++ 0.3972 1.739 2.647 8.396 0.9922
## SPP2
                 ++ 0.4326 1.134 1.803 6.245 0.9505
## 3 binary splits
## 1 species not shown
```

There is an overhead of fitting the model to calculate the ranking. But computing efficiencies can be still high compared to all partitions when the number of levels (k) is high.

A downside of this approach is that not all possible partitions are explored, thus the model weights do not represent all possible models, but only the top candidates. Thus model weight interpretation is different (i.e. cannot be used as a reliability matric, especially when support for the best model is not dominant).

3 Distributions

Currently available distributions:

- "gaussian": real valued continuous observations, e.g. biomass,
- "poisson": Poisson count data,
- "binomial": presence-absence type data,
- "negbin": overdispersed Negative Binomial count data,
- "beta": continuous response in the unit interval, e.g. percent cover,
- "zip", "zip2": zero-inflated Poisson counts (partitioning in count model: "zip", or in zero model: "zip2"),
- "zinb", "zinb": zero-inflated Negative Binomial counts (partitioning in count model: "zinb", or in zero model: "zinb2"),
- "ordered": response measured on ordinal scale, e.g. ordinal vegetation cover,
- "rsf", "rspf": presence-only data using resource selection and resource selection probability functions.

3.1 Gaussian

```
Y \leftarrow rnorm(n, log(lam1) + 10, 0.5)
(mod <- opticut(Y ~ x2, strata=x0, dist="gaussian"))</pre>
## Multivariate opticut results, comb = rank, dist = gaussian
##
## Call:
## opticut(formula = Y ~ x2, strata = x0, dist = "gaussian")
## 1 species, 3 binary splits
Legendre example
gr <- rep(1:5, each=5)
spp \leftarrow cbind(Sp1=rep(c(4,6,5,3,2), each=5),
   Sp2=c(rep(c(8,4,6), each=5), 4,4,2, rep(0,7)),
   Sp3=rep(c(18,2,0,0,0), each=5))
rownames(spp) <- gr</pre>
spp
##
    Sp1 Sp2 Sp3
## 1
      4
         8 18
          8 18
## 1
      4
## 1
      4
          8 18
## 1
      4 8 18
## 1
      4 8 18
## 2
      6
          4
## 2
      6
          4
              2
## 2
          4
             2
      6
## 2
      6
          4
             2
## 2
          4
              2
      6
## 3
      5
          6
             0
## 3
      5
          6
              0
## 3
      5
          6
              0
## 3
      5
          6
              0
## 3
      5
          6
              0
## 4
      3
              0
## 4
      3
          4
              0
## 4
      3
          2
              0
             0
## 4
      3 0
## 4
      3 0
             0
## 5
      2
         0
              0
## 5
      2 0
             0
## 5
      2 0
             0
## 5
      2
          0
              0
      2
## 5
          0
              0
summary(mod <- opticut(spp ~ 1, strata=gr, dist="gaussian", comb="all"))</pre>
```

Multivariate opticut results, comb = all, dist = gaussian

```
## opticut(formula = spp ~ 1, strata = gr, dist = "gaussian", comb = "all")
## Best supported models with logLR >= 2:
      split assoc
                       I muO mu1 logLR
## Sp2 1 3 +++ 0.9999 2.0 7.0 14.82 0.4995
## Sp1
        2 3 +++ 0.9866 3.0 5.5 17.33 0.4999
## Sp3
        1 +++ 1.0000 0.5 18.0 55.19 1.0000
## 15 binary splits
summary(mod <- opticut(spp ~ 1, strata=gr, dist="gaussian", comb="rank"))</pre>
## Multivariate opticut results, comb = rank, dist = gaussian
##
## Call:
## opticut(formula = spp ~ 1, strata = gr, dist = "gaussian", comb = "rank")
## Best supported models with logLR >= 2:
      split assoc I mu0 mu1 logLR
## Sp2 1 3 +++ 0.9999 2.0 7.0 14.82 0.4996
## Sp1 2 3 +++ 0.9866 3.0 5.5 17.33 0.4999
        1 +++ 1.0000 0.5 18.0 55.19 1.0000
## Sp3
## 4 binary splits
## DeCaceres & Legendre 2013 Oikos example from Fig 1
## Oikos 119: 1674-1684, 2010
## doi: 10.1111/j.1600-0706.2010.18334.x
Y \leftarrow c(0, 0, 3, 0, 2, 3, 0, 5, 5, 6, 3, 4)
z \leftarrow rep(1:3, each=4)
Z \leftarrow allComb(z)
Z \leftarrow cbind(Z, 1-Z)
colnames(Z) <- c("1", "2", "3", "2 3", "1 3", "1 2")
   1 2 3 2 3 1 3 1 2
## 1 1 0 0 0
                1
## 1 1 0 0 0
               1
                    1
## 1 1 0 0
           0 1
                    1
## 1 1 0 0
           0
               1
                    1
## 2 0 1 0
           1
               0
                    1
## 2 0 1 0 1 0
## 2 0 1 0 1 0
## 2 0 1 0 1
                0
                    1
## 3 0 0 1 1 1
                    0
## 3 0 0 1
## 3 0 0 1
            1
                1
                    0
## 3 0 0 1
           1
try(opticut1(Y, Z=Z))
oc <- ocoptions(check_comb=FALSE, cut=-Inf) # relax the checks
opticut1(Y, Z=Z) # identical results for complementary partitions
```

Call:

```
## Univariate opticut results, comb = NA, dist = gaussian
## I = 0.9937; w = 0.2871; H = 0.2463; logL_null = -25.93
## Best supported models with logLR >= -Inf:
##
      assoc
                 I muO
                           mu1
                                  logLR
## 3
         ++ 0.9937 1.625 4.500 3.232629 0.28708
       -- 0.9937 4.500 1.625 3.232629 0.28708
         -- 0.9919 3.500 0.750 2.878892 0.20154
## 2 3
         ++ 0.9919 0.750 3.500 2.878892 0.20154
          - 0.1244 2.625 2.500 0.004726 0.01138
## 2
## 1 3
          + 0.1244 2.500 2.625 0.004726 0.01138
## 6 binary splits
ocoptions(oc) # restore defaults
```

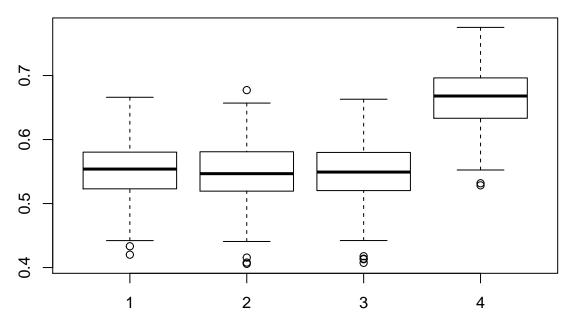
BCI data

3.2 Binomial

```
set.seed(1234)
n <- 1000
x0 <- sample(1:4, n, TRUE)</pre>
x1 <- ifelse(x0 %in% 1:2, 1, 0)
x2 <- rnorm(n, 0.5, 1)
table(x0,x1)
##
      x1
## x0
         0 1
##
       0 240
    1
##
     2 0 242
     3 260
##
     4 258
p1 \leftarrow plogis(0.5 + 0.5*x1 + -0.2*x2)
boxplot(p1~x0)
```

```
08:0 02:0 09:0 09:0 09:0 1 2 3 4
```

```
Y1 <- rbinom(n, 1, p1)
p2 <- plogis(0.1 + 0.5*ifelse(x0==4,1,0) + 0.2*x2)
boxplot(p2~x0)
```



```
Y2 <- rbinom(n, 1, p2)
Y <- cbind(SPP1=Y1, SPP2=Y2)
X <- model.matrix(~x2)
Z <- allComb(x0)
summary(opticut(Y ~ x2, strata=x0, dist="binomial"))</pre>
```

```
## Multivariate opticut results, comb = rank, dist = binomial
##
## Call:
```

```
## opticut(formula = Y ~ x2, strata = x0, dist = "binomial")
##
## Best supported models with logLR >= 2:
## split assoc I mu0 mu1 logLR w
## SPP1 1 2 ++ 0.4656 0.6301 0.7383 6.954 0.9222
## SPP2 4 ++ 0.4416 0.5415 0.6549 5.046 0.6378
## 3 binary splits
```

3.3 Poisson: Mite data set – high performance computing

See computing time diffs and plotting options.

ONOV

```
library(vegan)
## Loading required package: permute
## Loading required package: lattice
## This is vegan 2.4-1
data(mite)
data(mite.env)
mite.env$hab <- with(mite.env, interaction(Shrub, Topo, drop=TRUE))
summary(mod0 <- opticut(as.matrix(mite) ~ SubsDens, mite.env,</pre>
    strata=mite.env$hab, dist="poisson", comb="all"))
## Multivariate opticut results, comb = all, dist = poisson
##
## Call:
## opticut(formula = as.matrix(mite) ~ SubsDens, data = mite.env,
       strata = mite.env$hab, dist = "poisson", comb = "all")
## Best supported models with logLR >= 2:
##
                                split assoc
                                                  Ι
                                                          mu0
                                                                    m111
                                        --- 0.6920 3.500e+01 1.493e+01
## HPAV
                         Many.Hummock
## HMIN
                         None.Blanket
                                        --- 0.9990 1.880e+01 4.177e-01
## MEGR
                         None.Blanket
                                        --- 0.9969 9.729e-01 3.818e-02
                         None.Blanket
                                        --- 0.9574 1.637e+00 2.416e-01
## PWIL
## Eupelops
                         None.Blanket
                                         -- 0.9345 1.564e+00 2.878e-01
## NPRA
                          Few.Blanket
                                        --- 0.8206 1.425e+00 4.474e-01
## LCIL
            Many.Blanket Many.Hummock
                                        --- 0.9577 8.923e+00 1.312e+00
## PHTH
             None.Blanket Few.Blanket
                                        --- 1.0000 1.463e+00 2.525e-09
## RARD
             None.Blanket Few.Blanket
                                        --- 1.0000 2.546e+00 1.251e-08
## HMIN2
             None.Blanket Few.Blanket
                                        --- 1.0000 1.785e+00 5.504e-09
                                        --- 1.0000 1.523e+00 3.486e-09
## Galumna1 None.Blanket Few.Blanket
## PPEL
             None.Blanket Few.Blanket
                                         -- 1.0000 1.349e-01 6.501e-10
## SLAT
             None.Blanket Few.Blanket
                                        --- 1.0000 7.284e-01 4.062e-09
## Oribatl1 None.Blanket Few.Blanket
                                        --- 0.9986 1.311e+00 3.441e-02
## FSET
             None.Blanket Few.Blanket
                                        --- 0.9986 2.726e+00 7.211e-02
## TVEL
             None.Blanket Few.Blanket
                                        --- 0.9983 1.297e+01 3.759e-01
```

--- 0.8508 4.183e+01 1.188e+01

None.Blanket Few.Blanket

```
## SUCT
             None.Blanket Few.Blanket
                                         --- 0.7799 2.901e+01 1.020e+01
## Brachy
             None.Blanket Few.Blanket
                                         --- 0.7561 1.689e+01 6.294e+00
             Few. Hummock Many. Hummock
## PLAG2
                                         --- 0.8774 1.683e+01 4.300e+00
## Trhypch1
             Many.Blanket Few.Hummock
                                         --- 0.9364 7.493e-01 1.358e-01
## LRUG
             None.Blanket Few.Blanket
                                         +++ 0.9458 8.516e+00 5.100e+01
## Ceratoz3
             None.Blanket Few.Blanket
                                         +++ 0.8555 7.098e+00 2.543e+01
## Lepidzts
             Many.Blanket Few.Hummock
                                         +++ 1.0000 2.333e-09 8.547e-01
             Many.Blanket Few.Hummock
                                         +++ 0.9968 7.695e-01 1.916e+01
## Protopl
                                          ++ 0.8944 2.034e-01 8.614e-01
## MPRO
             Many.Blanket Few.Hummock
             Few. Hummock Many. Hummock
                                         +++ 0.9873 5.786e-03 7.230e-02
## Stgncrs2
## Oppiminu
            Few.Blanket Many.Blanket
                                         +++ 0.8348 2.243e+00 7.475e+00
## Miniglmn Many.Blanket Many.Hummock
                                         +++ 0.9975 2.716e-02 7.745e-01
## Trimalc2 None.Blanket Many.Hummock
                                         +++ 0.9997 6.359e-02 4.929e+00
## NCOR
                          Few.Blanket
                                          ++ 0.7181 4.238e+00 1.046e+01
## SSTR
                          Few.Hummock
                                         +++ 0.9971 1.561e-03 4.080e-02
## TVIE
                         None.Blanket
                                         +++ 0.8486 2.320e+00 8.106e+00
##
              logLR
## HPAV
             26.281 0.9944
## HMIN
             99.969 1.0000
## MEGR
             35.465 1.0000
## PWIL
             12.421 0.7564
## Eupelops
              6.536 0.3863
## NPRA
              8.523 0.8540
## LCIL
            540.701 1.0000
## PHTH
             56.766 1.0000
## RARD
             54.142 1.0000
## HMIN2
             87.196 1.0000
## Galumna1
             42.750 1.0000
## PPEL
              7.620 0.9359
## SLAT
             17.854 0.9399
## Oribatl1 69.712 1.0000
## FSET
             69.026 1.0000
## TVEL
            331.735 1.0000
## ONOV
            189.632 1.0000
## SUCT
            136.668 1.0000
## Brachy
             63.635 1.0000
## PLAG2
              9.162 0.9210
## Trhypch1 35.539 0.9998
## LRUG
            218.994 1.0000
## Ceratoz3 16.217 0.9392
## Lepidzts
            13.044 0.9912
## Protopl
             22.746 0.9936
## MPRO
              2.539 0.2639
## Stgncrs2
             29.557 0.9147
## Oppiminu
             12.310 0.9245
## Miniglmn
             12.918 0.9445
## Trimalc2
            83.215 1.0000
## NCOR
              6.241 0.4468
## SSTR
             23.076 0.9724
## TVIE
             11.050 0.9240
## 15 binary splits
## 2 species not shown
```

```
plot(mod0)
                   24
                               24
                                            21
                                                        12
                                                                     9
             Many.Blanket
                                     Many.Hummock
                                                               None.Blanket
                                          Strata
system.time(aa <- opticut(as.matrix(mite) ~ 1, strata=mite.env$hab, dist="poisson", comb="rank"))</pre>
      user system elapsed
##
##
     0.632
           0.015 0.650
system.time(bb <- opticut(as.matrix(mite) ~ 1, strata=mite.env$hab, dist="poisson", comb="all"))</pre>
##
      user system elapsed
     1.480
            0.042
                    1.531
##
## sequential
system.time(opticut(as.matrix(mite) ~ 1, strata=mite.env$hab, dist="poisson"))
      user system elapsed
           0.015
                    0.601
##
     0.584
## parallel -- compare system times
library(parallel)
cl <- makeCluster(3)</pre>
system.time(opticut(as.matrix(mite) ~ 1, strata=mite.env$hab, dist="poisson", cl=cl))
      user system elapsed
```

0.008

##

0.001

1.645

```
stopCluster(cl)
## forking -- will not work on Windows
if (!.Platform$0S.type == "windows")
system.time(opticut(as.matrix(mite) ~ 1, strata=mite.env$hab, dist="poisson", cl=3))
## user system elapsed
## 0.556 0.104 0.369
```

3.4 Percentages

3.4.1 Dune data, cover type data as ordinal

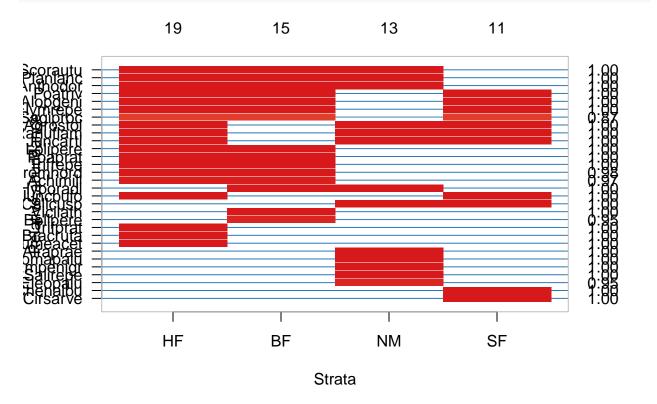
See http://www.davidzeleny.net/anadat-r/doku.php/en:data:dune

```
library(vegan)
data(dune)
data(dune.env)
dune.env$manure <- as.integer(dune.env$Manure) - 1</pre>
dune.env$moisture <- as.integer(dune.env$Moisture) - 1</pre>
oc <- ocoptions(collapse="+", cut=-Inf)</pre>
## ordinal regr
## (when nlevels() < 3 use logistic regression instead !!!</pre>
#Dune <- as.matrix(dune)</pre>
#Dune <- Dune[,apply(Dune, 2, function(z) length(unique(z)))>2]
#x1 <- opticut(Dune ~ 1, dune.env, strata=Management, dist="ordered")</pre>
#summary(x1)
\#plot(x1, mar=c(5,5,3,3))
## Binarizing data
Dune01 <- ifelse(as.matrix(dune)>0,1,0)
x2 <- opticut(Dune01 ~ 1, strata=dune.env$Management, dist="binomial")</pre>
summary(x2)
## Multivariate opticut results, comb = rank, dist = binomial
##
## Call:
```

```
## opticut(formula = Dune01 ~ 1, strata = dune.env$Management, dist = "binomial")
## Best supported models with logLR >= -Inf:
              split assoc
                                             mu1 logLR
                                       muO
                       ++ 1.0000 6.667e-01 1.0000 2.6826 0.7441
## Scorautu BF+HF+NM
## Planlanc BF+HF+NM
                     ++ 1.0000 8.647e-09 0.5000 3.2449 0.6890
                    ++ 1.0000 8.647e-09 0.4286 2.6566 0.6314
## Anthodor BF+HF+NM
## Poatriv BF+HF+SF +++ 1.0000 3.181e-09 0.9286 9.3465 0.7609
                     ++ 1.0000 8.647e-09 0.5714 3.8995 0.4732
## Alopgeni BF+HF+SF
                     ++ 1.0000 8.647e-09 0.4286 2.6566 0.6812
## Elymrepe BF+HF+SF
## Sagiproc BF+HF+SF
                      + 0.8672 1.667e-01 0.4286 0.6849 0.3726
## Agrostol HF+NM+SF
                     ++ 1.0000 8.647e-09 0.5882 2.3455 0.4403
## Ranuflam HF+NM+SF
                       + 1.0000 8.647e-09 0.3529 1.1801 0.3916
```

```
+ 1.0000 8.647e-09 0.2941 0.9481 0.3977
## Juncarti HF+NM+SF
## Lolipere
               BF+HF
                        ++ 1.0000 3.333e-01 1.0000 5.8221 0.8987
## Poaprat
                        ++ 1.0000 5.000e-01 1.0000 3.8995 0.7383
               BF+HF
## Trifrepe
               BF+HF
                        ++ 1.0000 6.667e-01 1.0000 2.3699 0.6700
                        ++ 0.9836 8.333e-02 0.5000 2.2595 0.4345
## Bromhord
               BF+HF
## Achimill
               BF+HF
                        ++ 0.9716 1.667e-01 0.6250 2.2497 0.6992
## Hyporadi
               BF+NM
                        ++ 1.0000 1.170e-09 0.3333 2.7256 0.7635
## Juncbufo
                        ++ 1.0000 3.181e-09 0.3636 2.7977 0.7960
               HF+SF
## Callcusp
               NM+SF
                         + 1.0000 3.181e-09 0.2500 1.7062 0.5054
## Vicilath
                  BF
                        ++ 0.9980 5.882e-02 0.6667 2.7414 0.4650
## Bellpere
                  BF
                         + 0.9538 2.353e-01 0.6667 1.0326 0.4286
## Trifprat
                  HF
                        ++ 1.0000 1.170e-09 0.6000 5.0891 0.8579
## Bracruta
                  HF
                         + 1.0000 6.667e-01 1.0000 1.6990 0.6935
                  HF
                        ++ 0.9994 6.667e-02 0.8000 5.0707 0.7703
## Rumeacet
## Airaprae
                  NM
                        ++ 1.0000 1.170e-09 0.3333 2.6826 0.7175
                        ++ 1.0000 1.170e-09 0.3333 2.6826 0.7516
## Comapalu
                  NM
## Empenigr
                  NM
                         + 1.0000 4.305e-10 0.1667 1.2669 0.4870
                        ++ 1.0000 1.170e-09 0.5000 4.2953 0.9007
## Salirepe
                         + 0.9459 1.429e-01 0.5000 1.3462 0.4330
## Eleopalu
                  NM
## Chenalbu
                         + 1.0000 4.305e-10 0.1667 1.2669 0.5523
                  SF
## Cirsarve
                  SF
                         + 1.0000 4.305e-10 0.1667 1.2669 0.5387
## 3 binary splits
```

plot(x2)



x3 <- opticut(DuneO1 ~ manure + moisture, dune.env, strata=dune.env\$Management, dist="binomial")

Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
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## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
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## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
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## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
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## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred

Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred

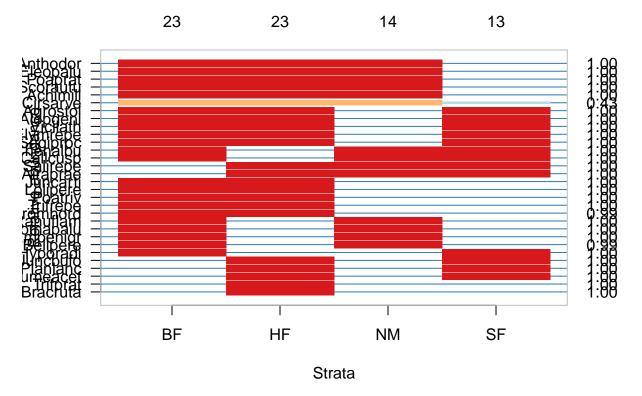
Warning: glm.fit: algorithm did not converge

.

```
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
summary(x3)
## Multivariate opticut results, comb = rank, dist = binomial
##
## Call:
## opticut(formula = DuneO1 ~ manure + moisture, data = dune.env,
##
       strata = dune.env$Management, dist = "binomial")
##
## Best supported models with logLR >= -Inf:
##
                                                           logLR
               split assoc
                                Ι
                                        mu0
                                                  mu1
## Anthodor BF+HF+NM
                         + 1.0000 3.690e-09 5.376e-01
                                                      1.629e+00 0.3705
                         + 1.0000 2.220e-16 2.220e-16 5.232e-01 0.4576
## Eleopalu BF+HF+NM
## Poaprat BF+HF+NM
                       ++ 1.0000 2.220e-16 1.000e+00
                                                      3.253e+00 0.7463
## Scorautu BF+HF+NM
                        + 1.0000 9.193e-01 1.000e+00 6.534e-01 0.3693
## Achimill BF+HF+NM
                        + 0.9987 3.591e-02 5.923e-01 9.259e-01 0.5420
                        + 0.4266 2.220e-16 2.220e-16 3.386e-11 0.3333
## Cirsarve BF+HF+NM
## Agrostol BF+HF+SF
                        + 1.0000 2.220e-16 2.220e-16 1.341e+00 0.3333
## Alopgeni BF+HF+SF
                        ++ 1.0000 6.724e-13 2.381e-02 3.298e+00 0.6809
## Vicilath BF+HF+SF
                        ++ 1.0000 1.000e+00 1.000e+00 3.998e+00 0.4954
                         + 1.0000 1.186e-08 2.227e-01 3.434e-01 0.4050
## Elymrepe BF+HF+SF
## Sagiproc BF+HF+SF
                        + 0.9993 1.261e-02 4.009e-01 1.782e+00 0.7077
## Chenalbu BF+NM+SF
                         + 1.0000 2.220e-16 2.220e-16 5.232e-01 0.3857
## Callcusp BF+NM+SF
                         + 1.0000 2.220e-16 2.220e-16 5.232e-01 0.4576
## Salirepe HF+NM+SF
                         + 0.9993 3.047e-02 6.221e-01 7.491e-10 0.3333
## Airaprae HF+NM+SF
                        + 0.9991 1.522e-02 4.159e-01 5.392e-10 0.3333
## Juncarti
              BF+HF
                        ++ 1.0000 2.220e-16 2.220e-16 2.660e+00 0.3857
## Lolipere
              BF+HF
                        ++ 1.0000 1.000e+00 1.000e+00 5.209e+00 0.4966
              BF+HF
                         + 1.0000 2.220e-16 2.220e-16
                                                      1.539e-09 0.3333
## Poatriv
              BF+HF
                       ++ 1.0000 5.906e-01 1.000e+00 2.284e+00 0.5479
## Trifrepe
## Bromhord
              BF+HF
                        + 0.9926 2.178e-02 2.672e-01 1.430e+00 0.4426
## Ranuflam
              BF+NM
                        + 1.0000 2.220e-16 2.220e-16 -4.704e-09 0.3333
## Comapalu
              BF+NM
                        + 1.0000 2.220e-16 1.837e-13 2.249e-09 0.3333
## Empenigr
              BF+NM
                        + 1.0000 2.220e-16 2.935e-13 2.062e-09 0.3333
## Bellpere
                        + 0.9931 5.142e-02 4.786e-01 9.237e-01 0.4039
              BF+NM
                        + 1.0000 5.289e-01 1.000e+00 7.921e-01 0.3811
## Hyporadi
              BF+SF
```

```
++ 1.0000 6.852e-10 9.064e-01 3.777e+00 0.8265
## Juncbufo
              HF+SF
## Planlanc
              HF+SF
                      + 1.0000 1.000e+00 1.000e+00 1.294e+00 0.3611
## Rumeacet
                      +++ 1.0000 4.887e-11 1.000e+00 1.033e+01 0.9961
              HF+SF
## Trifprat
                       ++ 1.0000 5.073e-12 1.000e+00 4.571e+00 0.4655
                 HF
## Bracruta
                 HF
                        + 1.0000 6.414e-01 1.000e+00 1.818e+00 0.5193
## 3 binary splits
```

plot(x3)

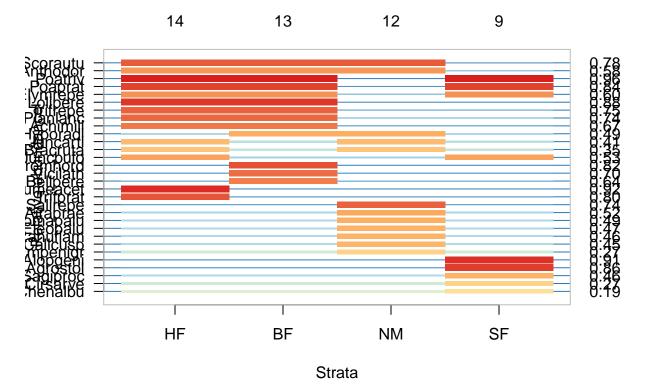


```
## Beta regression
Dune2 <- as.matrix(dune+0.5) / 10
x4 <- opticut(Dune2 ~ 1, strata=dune.env$Management, dist="beta")
summary(x4)</pre>
```

```
## Multivariate opticut results, comb = rank, dist = beta
##
## Call:
## opticut(formula = Dune2 ~ 1, strata = dune.env$Management, dist = "beta")
##
## Best supported models with logLR >= -Inf:
##
              split assoc
                               Ι
                                     mu0
                                             mu1 logLR
                       ++ 0.7794 0.17817 0.38107 5.0745 0.8647
## Scorautu BF+HF+NM
## Anthodor BF+HF+NM
                       + 0.5760 0.10484 0.18420 1.1481 0.4203
## Poatriv BF+HF+SF ++ 0.9620 0.12172 0.49912 7.3010 0.8074
## Poaprat BF+HF+SF
                       ++ 0.8433 0.13521 0.34908 4.3908 0.4868
## Elymrepe BF+HF+SF
                       + 0.5986 0.12205 0.21717 1.1230 0.4244
                      ++ 0.8840 0.21057 0.51807 4.1041 0.5739
## Lolipere
              BF+HF
## Trifrepe
              BF+HF ++ 0.7511 0.20483 0.40589 3.3954 0.6065
                      ++ 0.7389 0.12810 0.27492 2.4674 0.5496
## Planlanc
              BF+HF
```

```
## Achimill
               BF+HF
                        ++ 0.6717 0.09444 0.19051 2.5958 0.6056
## Hyporadi
               BF+NM
                         + 0.4898 0.07977 0.12901 1.1369 0.4604
## Juncarti
                         + 0.4131 0.11643 0.16976 0.6153 0.3946
               HF+NM
## Bracruta
                         + 0.3542 0.24927 0.32468 0.4567 0.3813
               HF+NM
## Juncbufo
               HF+SF
                         + 0.5259 0.08819 0.14786 1.2161 0.5040
## Bromhord
                  BF
                        ++ 0.8161 0.10488 0.26913 2.5352 0.6478
## Vicilath
                  BF
                        ++ 0.7049 0.05974 0.13249 4.3694 0.9287
                         + 0.6419 0.10238 0.19628 1.3851 0.5455
## Bellpere
                  BF
## Rumeacet
                  HF
                        ++ 0.9233 0.09043 0.33240 6.2240 0.9885
## Trifprat
                  HF
                        ++ 0.7962 0.07273 0.18889 3.8461 0.8910
## Salirepe
                  NM
                        ++ 0.7439 0.08105 0.18708 2.8623 0.8470
                  NM
                         + 0.5190 0.06399 0.10832 1.7093 0.6509
## Airaprae
                  NM
                         + 0.4882 0.05980 0.09784 1.8817 0.6948
## Comapalu
## Eleopalu
                  NM
                         + 0.4683 0.17312 0.25811 0.5215 0.3772
## Ranuflam
                  NM
                         + 0.4621 0.10558 0.16291 0.8663 0.3943
                         + 0.4476 0.09076 0.13910 0.7674 0.3972
## Callcusp
                  NM
## Empenigr
                  NM
                         + 0.2717 0.05575 0.07237 0.7740 0.4539
                  SF
                        ++ 0.9077 0.15803 0.46035 4.2254 0.8093
## Alopgeni
                        ++ 0.8612 0.20803 0.49026 3.0958 0.7098
## Agrostol
                  SF
                         + 0.4617 0.13397 0.20313 0.7063 0.3997
## Sagiproc
                  SF
## Cirsarve
                  SF
                         + 0.2717 0.05575 0.07237 0.7740 0.4539
## Chenalbu
                  SF
                         + 0.1918 0.05200 0.06245 0.9312 0.5111
## 3 binary splits
```

plot(x4)

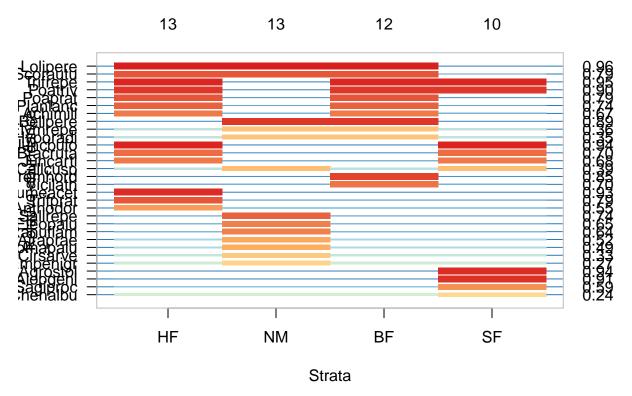


x5 <- opticut(Dune2 ~ manure, dune.env, strata=dune.env\$Management, dist="beta")
summary(x5)</pre>

Multivariate opticut results, comb = rank, dist = beta

```
##
## Call:
  opticut(formula = Dune2 ~ manure, data = dune.env, strata = dune.env$Management,
       dist = "beta")
##
## Best supported models with logLR >= -Inf:
               split assoc
                                Ι
                                      muO
                                                     logLR
                                               mu1
## Lolipere BF+HF+NM
                        ++ 0.9628 0.02503 0.15721 4.52994 0.6104
## Scorautu BF+HF+NM
                        ++ 0.7883 0.17329 0.37858 2.78625 0.6581
## Trifrepe BF+HF+SF
                        ++ 0.9473 0.21532 0.62509 3.90047 0.4742
## Poatriv BF+HF+SF
                        ++ 0.8963 0.11822 0.36436 2.00207 0.6594
## Poaprat
               BF+HF
                        ++ 0.7948 0.11196 0.27161 5.10107 0.6029
## Planlanc
               BF+HF
                        ++ 0.7433 0.14503 0.30657 2.53058 0.4590
                        ++ 0.6711 0.09329 0.18824 2.58564 0.4552
## Achimill
               BF+HF
## Bellpere
               BF+NM
                        ++ 0.8885 0.02647 0.10061 2.12610 0.5576
## Elymrepe
               BF+NM
                         + 0.3640 0.08561 0.12057 0.07552 0.3407
## Hyporadi
               BF+NM
                         + 0.3544 0.09572 0.13293 0.21056 0.3572
## Juncbufo
               HF+SF
                        ++ 0.9446 0.09242 0.37623 3.10402 0.8621
## Bracruta
               HF+SF
                         + 0.7044 0.31627 0.52623 0.92747 0.4554
## Juncarti
               HF+SF
                         + 0.6770 0.15362 0.29256 0.70062 0.3922
               NM+SF
## Callcusp
                         + 0.3886 0.09554 0.13733 0.63669 0.3964
## Bromhord
                  BF
                        ++ 0.8499 0.07911 0.23168 3.00961 0.7403
## Vicilath
                  BF
                        ++ 0.6987 0.06912 0.14988 4.62302 0.8194
## Rumeacet
                  HF
                        ++ 0.9302 0.09680 0.36044 6.26423 0.7311
                  HF
                        ++ 0.7931 0.07088 0.18342 3.76058 0.7219
## Trifprat
## Anthodor
                  HF
                         + 0.5504 0.16814 0.27289 0.87929 0.3494
## Salirepe
                  NM
                         + 0.7439 0.08105 0.18708 1.19959 0.5531
                  NM
                         + 0.6457 0.13865 0.25755 0.50249 0.3632
## Eleopalu
                  NM
## Ranuflam
                         + 0.6416 0.08310 0.16247 0.83466 0.3694
## Airaprae
                  NM
                         + 0.5190 0.06399 0.10832 0.66716 0.4815
## Comapalu
                  NM
                         + 0.4882 0.05980 0.09784 0.73272 0.4966
## Cirsarve
                  NM
                         + 0.3253 0.04022 0.05547 0.38506 0.3667
                  NM
## Empenigr
                         + 0.2717 0.05575 0.07237 0.29145 0.3942
## Agrostol
                  SF
                        ++ 0.9356 0.23871 0.63227 2.70445 0.7902
## Alopgeni
                  SF
                        ++ 0.9124 0.15916 0.46926 2.10605 0.7632
## Sagiproc
                  SF
                        + 0.5929 0.14226 0.24704 0.56757 0.4104
## Chenalbu
                  SF
                         + 0.2400 0.05312 0.06686 0.71117 0.4983
## 3 binary splits
```

plot(x5)

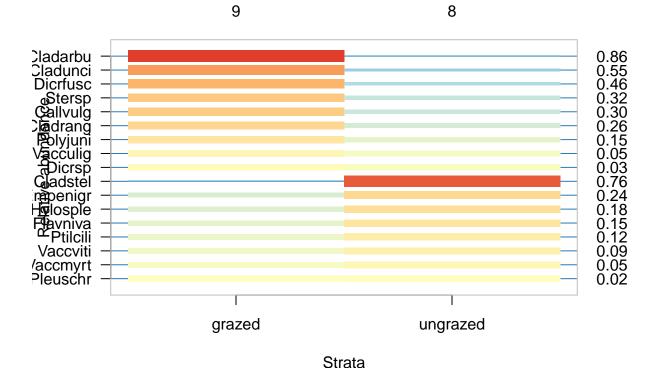


```
xx <- data.frame(#ord0=summary(x1)$summary$split,
   bin0=summary(x2)$summary$split,
   binx=summary(x3)$summary$split,
   bet0=summary(x4)$summary$split,
   betx=summary(x5)$summary$split)
rownames(xx) <- rownames(summary(x2)$summary)
xx</pre>
```

```
##
                bin0
                          binx
                                   bet0
                                            betx
               BF+HF BF+HF+NM
## Achimill
                                  BF+HF
                                           BF+HF
## Agrostol HF+NM+SF BF+HF+SF
                                     SF
                                              SF
## Airaprae
                  NM HF+NM+SF
                                     NM
                                              NM
## Alopgeni BF+HF+SF BF+HF+SF
                                     SF
                                               SF
## Anthodor BF+HF+NM BF+HF+NM BF+HF+NM
                                              HF
## Bellpere
                  BF
                         BF+NM
                                     BF
                                           BF+NM
## Bromhord
               BF+HF
                         BF+HF
                                     BF
                                              BF
## Chenalbu
                                     SF
                  SF BF+NM+SF
                                              SF
## Cirsarve
                  SF BF+HF+NM
                                     SF
                                              NM
## Comapalu
                                              NM
                  NM
                         BF+NM
                                     NM
## Eleopalu
                  NM BF+HF+NM
                                     NM
                                               NM
## Elymrepe BF+HF+SF BF+HF+SF
                                           BF+NM
## Empenigr
                  NM
                         BF+NM
                                     NM
                                              NM
## Hyporadi
               BF+NM
                         BF+SF
                                  BF+NM
                                           BF+NM
## Juncarti HF+NM+SF
                         BF+HF
                                  HF+NM
                                           HF+SF
## Juncbufo
               HF+SF
                         HF+SF
                                  HF+SF
                                           HF+SF
## Lolipere
               BF+HF
                         BF+HF
                                  BF+HF BF+HF+NM
## Planlanc BF+HF+NM
                         HF+SF
                                  BF+HF
                                           BF+HF
## Poaprat
               BF+HF BF+HF+NM BF+HF+SF
                                           BF+HF
## Poatriv BF+HF+SF
                         BF+HF BF+HF+SF BF+HF+SF
## Ranuflam HF+NM+SF
                         BF+NM
                                     NM
                                              NM
```

```
HF
## Rumeacet
             HF
                       HF+SF
                                   HF
## Sagiproc BF+HF+SF BF+HF+SF
                                   SF
                                            SF
## Salirepe
                 NM HF+NM+SF
                                  NM
                                            NM
## Scorautu BF+HF+NM BF+HF+NM BF+HF+NM
## Trifprat
              _{
m HF}
                         HF
                                _{
m HF}
## Trifrepe BF+HF BF+HF
                                BF+HF BF+HF+SF
## Vicilath BF BF+HF+SF
                               BF
                                            BF
## Bracruta
                _{
m HF}
                                HF+NM
                     _{
m HF}
                                         HF+SF
## Callcusp NM+SF BF+NM+SF
                                   NM
                                         NM+SF
ocoptions(oc)
3.4.2 Varespec data (% cover)
library(vegan)
data(varespec)
data(varechem)
y <- as.matrix(varespec / 100)
range(y[y>0])
## [1] 0.0002 0.8430
y[y \le 0] < 0.0001
y \leftarrow y[,apply(y, 2, max) > 0.05]
varechem$grazing <- as.factor(ifelse(rownames(varechem) %in% c(5,6,7,8,13,14,15,16,
    18,19,20,22,23,24,26), "grazed", "ungrazed"))
x <- opticut(y ~ 1, varechem, strata=grazing, dist="beta")</pre>
summary(x)
## Multivariate opticut results, comb = rank, dist = beta
## Call:
## opticut(formula = y ~ 1, data = varechem, strata = grazing, dist = "beta")
## Best supported models with logLR >= 2:
              split assoc
                               Ι
                                           mu1 logLR w
                       ++ 0.8616 0.04831 0.157 6.213 1
## Cladarbu grazed
## Cladstel ungrazed
                       ++ 0.7619 0.13055 0.290 2.091 1
## 1 binary split
## 15 species not shown
```

plot(x, cut=-Inf)



Implement ZI-Beta (quite unreliable for such small data set)

```
zi_beta_fun <- function(Y, X, linkinv, ...) {</pre>
    kx <- ncol(X)
    id1 <- Y > 0
    id0 <- !id1
    nll_ZIB_ML <- function(parms) {</pre>
        mu <- plogis(X %*% parms[1:kx])</pre>
         gamma <- exp(parms[kx + 1]) # precision</pre>
        phi <- plogis(parms[kx+2])</pre>
        alpha <- mu * gamma
        beta <- (1 - mu) * gamma
        loglik0 <- log(phi)</pre>
         loglik1 <- log(1 - phi) + suppressWarnings(dbeta(Y,</pre>
             alpha, beta, log = TRUE))
        loglik <- sum(loglik0[id0]) + sum(loglik1[id1])</pre>
         if (!is.finite(loglik) || is.na(loglik))
             loglik <- -.Machine$double.xmax^(1/3)</pre>
         -loglik
    }
    Yv <- Y
    Yv[Y \le 0.001] < 0.001
    ini <- c(coef(betareg::betareg(Yv ~ .-1, data=X)), zi=-5)</pre>
    X <- as.matrix(X)</pre>
    res <- optim(ini, nll_ZIB_ML, ...)</pre>
    list(coef=res$par,
         logLik=-res$value,
         linkinv=binomial("logit")$linkinv)
y <- as.matrix(varespec / 100)</pre>
```

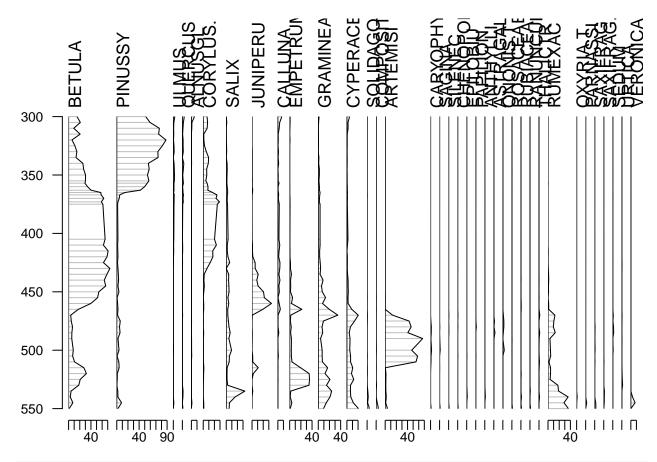
```
range(y[y>0])
y <- y[,apply(y, 2, max) > 0.05]
zi_beta_fun(y[,3], data.frame(matrix(1, nrow(y), 1)))
opticut1(y[,1], matrix(1, nrow(y), 1), varechem$grazing, dist=zi_beta_fun)
```

3.4.3 Stratigraphy example

```
library(rioja)

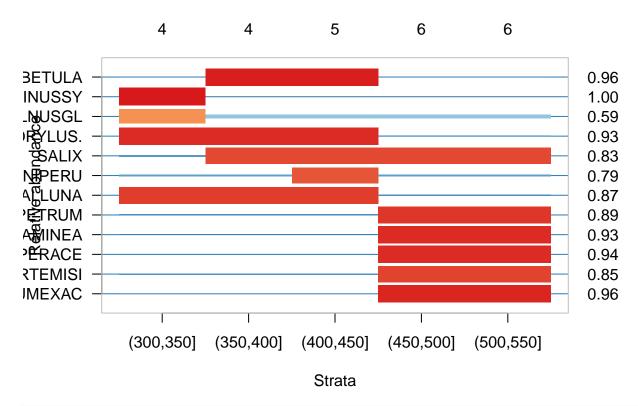
## This is rioja 0.9-9
```

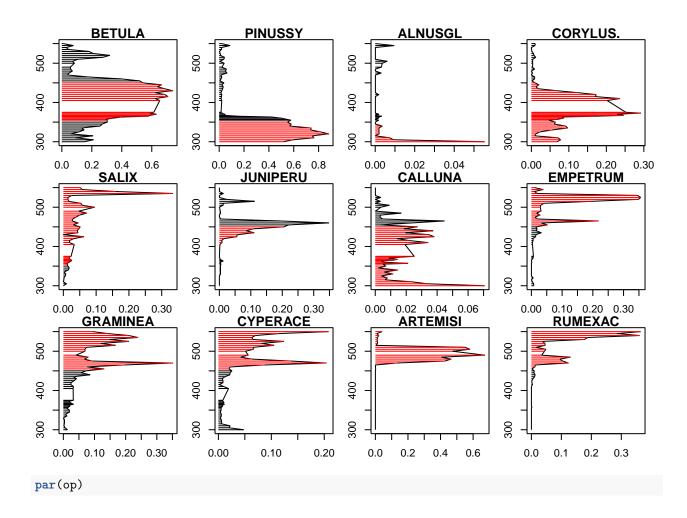
```
data(aber)
strat.plot(aber$spec, aber$ages$Depth, scale.percent=TRUE, y.rev=TRUE)
```



```
z <- as.factor(cut(aber$ages$Depth, 5))
ab <- as.matrix(aber$spec) / 100
ab[ab == 0] <- 0.0001
ab <- ab[,apply(ab, 2, max) > 0.05]
a <- opticut(ab ~ 1, strata=z, comb="rank", dist="beta")
summary(a)</pre>
```

```
## Multivariate opticut results, comb = rank, dist = beta
##
## Call:
## opticut(formula = ab ~ 1, strata = z, dist = "beta", comb = "rank")
## Best supported models with logLR >= 2:
                                              split assoc
                                                                Ι
                                                                       muO
## SALIX
            (350,400] (400,450] (450,500] (500,550]
                                                      +++ 0.8306 0.014015
## CORYLUS.
                      (300,350] (350,400] (400,450]
                                                      +++ 0.9341 0.019366
## CALLUNA
                      (300,350] (350,400] (400,450]
                                                      +++ 0.8682 0.005234
## BETULA
                                (350,400] (400,450]
                                                      +++ 0.9627 0.153662
## RUMEXAC
                                (450,500] (500,550]
                                                      +++ 0.9554 0.015648
## CYPERACE
                                (450,500] (500,550]
                                                      +++ 0.9353 0.015826
## GRAMINEA
                                (450,500] (500,550]
                                                      +++ 0.9299 0.028003
## EMPETRUM
                                (450,500] (500,550]
                                                      +++ 0.8857 0.020863
## ARTEMISI
                                (450,500] (500,550]
                                                       ++ 0.8515 0.046111
## PINUSSY
                                           (300,350]
                                                      +++ 0.9960 0.083196
## ALNUSGL
                                           (300,350]
                                                       ++ 0.5936 0.002089
## JUNIPERU
                                           (400, 450]
                                                       ++ 0.7935 0.025317
                 mu1 logLR
## SALIX
            0.044639 8.393 0.5344
## CORYLUS. 0.096616 17.133 0.9940
## CALLUNA 0.019421 12.719 0.5430
## BETULA
            0.568254 27.575 1.0000
## RUMEXAC 0.095248 15.892 0.9888
## CYPERACE 0.080857 24.351 1.0000
## GRAMINEA 0.131311 21.569 0.9914
## EMPETRUM 0.079641 10.171 0.6500
## ARTEMISI 0.145790 7.025 0.9708
## PINUSSY 0.669499 26.667 1.0000
## ALNUSGL 0.004128 2.081 0.4201
## JUNIPERU 0.071110 4.017 0.6459
## 4 binary splits
## 1 species not shown
plot(a, sort=FALSE)
```





3.5 Presence-only data

Describe $\ensuremath{\mathsf{RSF/RSPF}}$ differences especially related to covariates.

```
## presence-only data
## single species model only:
## because the used distr is different for
## each species by definition.
library(ResourceSelection)
```

ResourceSelection 0.2-6 2016-02-15

```
dd <- simulateUsedAvail(x, cfs, n.used, m, link="logit")</pre>
Y <- dd$status
X <- model.matrix(~ x1 + x2, dd)</pre>
Z <- allComb(as.integer(dd$x0))</pre>
mod1 <- opticut(Y ~ x1 + x2, dd, strata=x0, dist="rsf", m=0, B=0)</pre>
mod1$species
## $Species.1
## Univariate opticut results, comb = rank, dist = rsf
## I = 0.2344; w = 0.59; H = 0.5162; logL_null = -9184
## Best supported models with logLR >= 2:
       assoc
                  I mu0 mu1 logLR
##
## 3
         ++ 0.2344
                     1 1.270 6.649 0.59
## 1 3
        ++ 0.2397 1 1.277 6.285 0.41
## 2 binary splits
mod2 <- opticut(Y ~ x1 + x2, dd, strata=x0, dist="rspf", m=0, B=0)</pre>
mod2$species
## $Species.1
## Univariate opticut results, comb = rank, dist = rspf
## I = 0.5854; w = 0.73; H = 0.6058; logL_null = -9169
## Best supported model with logLR >= 2:
                     mu0
                            mu1 logLR
    assoc
                Τ
        ++ 0.5854 0.7359 0.8449 2.508 0.73
## 2 binary splits (1 model not shown)
```

4 Custom distributions

The distr argument accepts a function, so other parametric models can be supplied which are avoided due to package dependencies.

4.1 Mixed models

x2 <- rnorm(n, 0.5, 1)

Here is an example using mixed models and the package lme4:

```
library(lme4)

## Loading required package: Matrix

set.seed(1234)
n <- 200
x0 <- sample(1:4, n, TRUE)
x1 <- ifelse(x0 %in% 1:2, 1, 0)</pre>
```

```
ee <- rnorm(n/5)
g \leftarrow rep(1:5, each=n/5)
lam1 \leftarrow exp(0.5 + 0.5*x1 + -0.2*x2 + ee[g])
Y1 <- rpois(n, lam1)
X <- model.matrix(~x2)</pre>
Z \leftarrow allComb(x0)
lmefun <- function(Y, X, linkinv, gr, ...) {</pre>
    X <- as.matrix(X)</pre>
    m <- glmer(Y ~ X-1 + (1|gr), family=poisson("log"), ...)
    list(coef=fixef(m),
        logLik=logLik(m),
        linkinv=family(m)$linkinv)
}
lmefun(Y1, X, gr=g)
## $coef
## X(Intercept)
##
      0.6880337 -0.1899153
## $logLik
## 'log Lik.' -345.1799 (df=3)
##
## $linkinv
## function (eta)
## pmax(exp(eta), .Machine$double.eps)
## <environment: namespace:stats>
opticut1(Y1, X, Z, dist=lmefun, gr=g)
## Univariate opticut results, comb = all, dist = lmefun
## I = 0.4736; w = 0.9985; H = 0.997; logL_null = -345.2
## Best supported models with logLR >= 2:
      assoc
                  I mu0 mu1 logLR
## 1 2 +++ 0.4736 1.480 2.476 13.582 0.9984969
         ++ 0.4057 1.745 2.683 6.864 0.0012072
## 4
          -- 0.3473 2.168 1.509 4.739 0.0001441
## 3
          -- 0.3495 2.134 1.482 4.620 0.0001279
          ++ 0.2447 1.858 2.386 2.813 0.0000210
## 7 binary splits (2 models not shown)
```

4.2 Imperfect detectability: N-mixture case

A single-visit based N-mixture is an example where detection error is estimated. Let us compare results based on naive GLM and N-mixture:

```
library(detect)
```

Loading required package: Formula

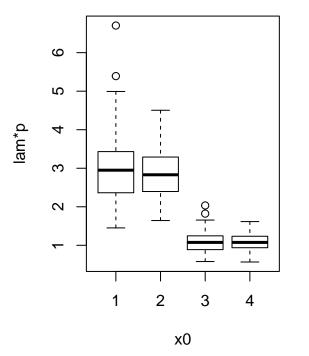
```
## Loading required package: stats4
```

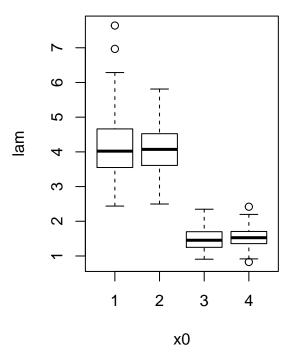
```
## detect 0.4-0 2016-03-02
```

```
set.seed(2345)
n <- 500
x0 <- sample(1:4, n, TRUE)
x1 <- ifelse(x0 %in% 1:2, 1, 0)
x2 <- rnorm(n, 0.5, 1)
x3 <- runif(n, 0, 1)
lam <- exp(0.5 + 1*x1 + -0.2*x2)
p <- plogis(2 + -2*x3)
Y <- rpois(n, lam*p)

X <- model.matrix(~x2)

op <- par(mfrow=c(1,2))
boxplot((lam*p) ~ x0, ylab="lam*p", xlab="x0")
boxplot(lam ~ x0, ylab="lam", xlab="x0")</pre>
```





\$coef

```
## X(Intercept)
##
      1.6746855
                 -0.2458261
##
## $logLik
## 'log Lik.' -884.583 (df=5)
##
## $linkinv
## function (eta)
## pmax(exp(eta), .Machine$double.eps)
## <environment: namespace:stats>
## naive GLM
print(opticut1(Y, X, as.factor(x0), dist="poisson"), cut=-Inf)
## Univariate opticut results, comb = rank, dist = poisson
## I = 0.7741; w = 1; H = 1; logL_null = -930
##
## Best supported models with logLR >= -Inf:
##
                    Ι
                      mu0
                             mu1 logLR
        assoc
## 1 2
          +++ 0.7741 1.139 3.193 115.16 1.000e+00
## 1 2 4 +++ 0.6998 1.078 2.566 52.38 5.383e-28
          +++ 0.5260 1.808 3.243 38.04 3.211e-34
## 3 binary splits
## N-mixture
print(opticut1(Y, X, as.factor(x0), dist=svfun), cut=-Inf)
## Univariate opticut results, comb = rank, dist = svfun
## I = 0.7876; w = 1; H = 0.9999; logL_null = -884.6
## Best supported models with logLR >= -Inf:
        assoc
                      mu0
##
                   Ι
                             mu1 logLR
          +++ 0.7876 2.409 6.989 26.239 1.000e+00
         +++ 0.7261 1.936 4.859 15.787 2.888e-05
            ++ 0.4664 4.142 6.866 3.284 1.073e-10
## 3 binary splits
```

4.3 Sampling differences: using offsets

Not accounting for unequal sampling effort can be quite misleading, especially if that is related to habitat classes. This example shows how to take advantage of the other arguments passed to the ... in the opticut function.

```
set.seed(1234)
n <- 50
x0 <- sample(1:4, n, TRUE)
x1 <- ifelse(x0 %in% 1:2, 1, 0)
x2 <- rnorm(n, 0.5, 1)
lam <- exp(0.5 + 1*x1 + -0.2*x2)
A <- ifelse(x0 %in% c(1,3), 1, 2)
Y <- rpois(n, lam*A)</pre>
```

```
op <- par(mfrow=c(1,2))
boxplot((lam*A) ~ x0, ylab="lam*A", xlab="x0")
boxplot(lam ~ x0, ylab="lam", xlab="x0")</pre>
```

```
10
                                                                             2
        \infty
lam*A
                                                                    <u>a</u>m
        9
                                                                             3
                                                                                          0
                               2
                                         3
                                                                                                    2
                                                                                                              3
                     1
                                                   4
                                                                                          1
                                                                                                                       4
                                   x0
                                                                                                        x0
```

```
par(op)
## no offset: incorrect
opticut(Y ~ x2, strata=x0, dist="poisson", comb="rank")$species
## $Species.1
## Univariate opticut results, comb = rank, dist = poisson
## I = 0.8354; w = 0.9895; H = 0.9792; logL_null = -154.2
##
## Best supported models with logLR >= 2:
##
         assoc
                    Ι
                      mu0
                              mu1 logLR
## 2
           +++ 0.8354 3.028 10.110 42.01 9.895e-01
           +++ 0.8412 2.192 7.464 37.46 1.049e-02
## 1 2 4
           +++ 0.8483 1.766 6.164 24.77 3.243e-08
## 3 binary splits
## with offsets: log Area
opticut(Y ~ x2, strata=x0, dist="poisson", offset=log(A), comb="rank")$species
## $Species.1
## Univariate opticut results, comb = rank, dist = poisson
## I = 0.8153; w = 1; H = 1; logL_null = -135.7
##
## Best supported models with logLR >= 2:
        assoc
                    Ι
                      muO
                            mu1 logLR
           +++ 0.8153 1.572 4.930 32.34 1.000e+00
## 1 2
```

```
## 1 2 3 +++ 0.7780 1.431 4.049 17.29 2.919e-07
## 2 +++ 0.6356 2.388 5.060 16.68 1.584e-07
## 3 binary splits
```

4.4 GAM models

```
library(mgcv)
## Loading required package: nlme
## Attaching package: 'nlme'
## The following object is masked from 'package:lme4':
##
       lmList
## This is mgcv 1.8-15. For overview type 'help("mgcv-package")'.
library(detect)
data(oven)
oven$veg <- factor(NA, c("agr","open","decid","conif", "mix"))</pre>
oven$veg[oven$pforest < 0.5] <- "open"</pre>
oven$veg[oven$pagri > 0.5 & oven$pforest < 0.5] <- "agr"</pre>
oven$veg[oven$pforest >= 0.5] <- "mix"</pre>
oven$veg[oven$pforest >= 0.5 & oven$pdecid >= 0.8] <- "decid"</pre>
oven$veg[oven$pforest >= 0.5 & oven$pdecid < 0.2] <- "conif"</pre>
table(oven$veg, useNA="always")
##
##
     agr open decid conif
                               mix <NA>
                  78
                               220
##
     530
            33
                         30
oven$xlat <- scale(oven$lat)</pre>
oven$xlong <- scale(oven$long)</pre>
gamfun <- function(Y, X, linkinv, Data, ...) {</pre>
    X <- as.matrix(X)</pre>
    m <- mgcv::gam(Y ~ X-1 + s(xlat) + s(xlong), Data, ...)</pre>
    list(coef=coef(m),
        logLik=logLik(m),
        linkinv=family(m)$linkinv)
}
x <- ifelse(oven$veg=="agr",1,0)
X <- model.matrix(~x)</pre>
gamfun(oven$count, X, Data=oven, family=poisson)
## $coef
## X(Intercept)
                                  s(xlat).1
                                                s(xlat).2
                                                              s(xlat).3
                           Xx
## -0.306661304 -1.382449156 -0.555089095 -0.890381109 0.306380012
```

```
##
     s(xlat).4 s(xlat).5
                             s(xlat).6 s(xlat).7
                                                         s(xlat).8
  1.122776013 0.132117780 -0.052077672 0.036702449 -3.041886993
##
     s(xlat).9 s(xlong).1
                                          s(xlong).3 \quad s(xlong).4
##
                             s(xlong).2
## 0.955525315 -1.090347031 1.922368963 -0.004724731 -0.428722334
##
    s(xlong).5 s(xlong).6
                              s(xlong).7
                                           s(xlong).8
                                                        s(xlong).9
## 0.369410432 0.241421901 -0.228281375 -0.857581486 0.995878919
##
## $logLik
## 'log Lik.' -730.8404 (df=16.34444)
##
## $linkinv
## function (eta)
## pmax(exp(eta), .Machine$double.eps)
## <environment: namespace:stats>
print(opticut1(oven$count, X=X[,1,drop=FALSE], oven$veg, dist=gamfun,
   Data=oven, family=poisson), cut=-Inf)
## Univariate opticut results, comb = rank, dist = gamfun
## I = 0.8815; w = 0.9985; H = 0.997; logL_null = -777.7
## Best supported models with logLR >= -Inf:
                       assoc
                                  Ι
                                       mu0
                                              mu1 logLR
## open decid conif mix +++ 0.8815 0.1847 0.7359 46.906 9.985e-01
## decid conif mix
                        +++ 0.8681 0.2049 0.7712 40.373 1.451e-03
## decid mix
                        +++ 0.8196 0.2298 0.7298 37.182 5.973e-05
## decid
                         ++ 0.4631 0.3462 0.5714 6.942 4.396e-18
## 4 binary splits
o <- opticut(count ~ 1, oven, strata=veg, dist=gamfun, Data=oven, family=poisson)
summary(o)
## Multivariate opticut results, comb = rank, dist = gamfun
##
## opticut(formula = count ~ 1, data = oven, strata = veg, dist = gamfun,
##
      Data = oven, family = poisson)
##
## Best supported model with logLR >= 2:
                                         I muO
                           split assoc
                                                      mu1 logLR
## Species.1 open decid conif mix +++ 0.8815 0.1847 0.7359 46.91 0.9985
## 4 binary splits
o <- opticut(count ~ 1, oven, strata=veg, dist="poisson")
summary(o)
## Multivariate opticut results, comb = rank, dist = poisson
##
## Call:
## opticut(formula = count ~ 1, data = oven, strata = veg, dist = "poisson")
## Best supported model with logLR >= 2:
```

```
##
                            split assoc I mu0 mu1 logLR
## Species.1 open decid conif mix +++ 0.935 0.1868 1.019 142.7 0.9998
## 4 binary splits
oven$pa <- ifelse(oven$count > 0, 1, 0)
o <- opticut(pa ~ 1, oven, strata=veg, dist=gamfun, Data=oven, family=binomial)
summary(o)
## Multivariate opticut results, comb = rank, dist = gamfun
##
## Call:
## opticut(formula = pa ~ 1, data = oven, strata = veg, dist = gamfun,
      Data = oven, family = binomial)
##
## Best supported model with logLR >= 2:
                                          I
                            split assoc
                                                 mu0
                                                        mu1 logLR
## Species.1 open decid conif mix +++ 0.9388 0.1421 0.4824 28.84 0.919
## 4 binary splits
o <- opticut(pa ~ 1, oven, strata=veg, dist="binomial")</pre>
summary(o)
## Multivariate opticut results, comb = rank, dist = binomial
##
## Call:
## opticut(formula = pa ~ 1, data = oven, strata = veg, dist = "binomial")
## Best supported model with logLR >= 2:
                            split assoc
                                            Ι
                                                 muO
                                                        mu1 logLR
## Species.1 open decid conif mix +++ 0.9629 0.1377 0.5374 82.37 0.6569
## 4 binary splits
```

5 Finding best partitions

It is useful to access the best binary partition

Call:

```
set.seed(2345)
n <- 50
x0 <- sample(1:4, n, TRUE)
x1 <- ifelse(x0 %in% 1:2, 1, 0)
x2 <- rnorm(n, 0.5, 1)
lam <- exp(0.5 + 1*x1 + -0.2*x2)
Y <- rpois(n, lam)
o <- opticut(Y ~ x2, strata=x0, dist="poisson", comb="rank")
summary(o)
## Multivariate opticut results, comb = rank, dist = poisson</pre>
```

opticut(formula = Y ~ x2, strata = x0, dist = "poisson", comb = "rank")

```
##
## Best supported model with logLR >= 2:
             split assoc
                               I muO
                                         mu1 logLR
              1 2
                     +++ 0.7037 1.819 4.361 12.46 0.9918
## Species.1
## 3 binary splits
bp <- bestpart(o)</pre>
head(bp)
##
     Species.1
## 1
## 1
## 3
## 1
             1
## 2
             1
## 2
```

The model based on the best partition can be returned as:

```
bestmodel(o, which=1)
## $Species.1
##
## Call: stats::glm(formula = Y ~ . - 1, family = Family, data = XX)
##
## Coefficients:
## `(Intercept)`
                             Z1
                                            x2
                        0.8747
##
                                       -0.1246
##
## Degrees of Freedom: 50 Total (i.e. Null); 47 Residual
## Null Deviance:
                        180.3
## Residual Deviance: 46.98
                                AIC: 184.8
```

the which argument can be used to subset the species.

6 Uncertainty

Uncertainty in I values might be of interest. The type argument for the uncertainty method can take the following values:

- "asymp": asymptotic distribution of I, μ_0 and μ_1 based on best partition found for the input object.
- "boot": non-parametric bootstrap distribution of I, μ_0 and μ_1 based on best partition found for the input object.
- "multi": non-parametric bootstrap distribution of I, μ_0 and μ_1 based on best partition found for the bootstrap data (i.e. the model ranking is re-evaluated each time).

```
uc1 <- uncertainty(o, type="asymp", B=5000)
uc2 <- uncertainty(o, type="boot", B=200)
uc3 <- uncertainty(o, type="multi", B=200)
uc1$uncertainty[[1]]</pre>
```

```
## Univariate opticut uncertainty results, type = asymp, B = 5000
##
##
    best
                                   mu0
  1 2:5001
                    :0.2381 Min.
                                     :1.120
                                                     :2.863
##
                                              Min.
              Min.
##
              1st Qu.:0.5299
                              1st Qu.:1.640
                                              1st Qu.:4.022
##
              Median :0.5846 Median :1.814
                                            Median :4.356
              Mean :0.5764 Mean :1.835
                                             Mean :4.387
##
              3rd Qu.:0.6319 3rd Qu.:2.001
                                              3rd Qu.:4.727
##
                                    :3.401
##
              Max.
                    :0.7970 Max.
                                              Max.
                                                     :6.587
uc2$uncertainty[[1]]
## Univariate opticut uncertainty results, type = boot, B = 200
##
##
    best
                   Ι
                                  mu0
                                                  mu1
## 1 2:201
             Min.
                    :0.3206
                            Min. :1.244
                                             Min. :3.178
##
             1st Qu.:0.5356
                            1st Qu.:1.651
                                            1st Qu.:4.014
             Median :0.5801
                             Median :1.801
##
                                            Median :4.408
##
             Mean
                   :0.5780
                            Mean :1.819
                                            Mean :4.365
##
             3rd Qu.:0.6270
                             3rd Qu.:1.986
                                             3rd Qu.:4.685
##
             Max.
                    :0.7412
                             Max. :2.522
                                             Max. :5.930
uc3$uncertainty[[1]]
## Univariate opticut uncertainty results, type = multi, B = 200
##
##
      best
                     Ι
                                    muO
                                                     mu1
## 1
        : 1
                     :0.4628
                               Min. :0.7104 Min.
                                                      :3.137
             Min.
## 1 2 :183
              1st Qu.:0.6463
                               1st Qu.:1.6341
                                               1st Qu.:4.046
## 1 2 4: 2
              Median :0.7165
                               Median :1.8144
                                               Median :4.532
## 2
        : 15
              Mean
                    :0.7132
                               Mean :1.8115
                                               Mean :4.530
##
               3rd Qu.:0.7833
                               3rd Qu.:1.9957
                                                3rd Qu.:4.915
##
               Max.
                      :0.9322
                               Max. :2.6809
                                                Max. :6.141
## performance comparisons for 10 species
YYY <- cbind(Y, Y, Y, Y, Y, Y, Y, Y, Y)
colnames(YYY) <- LETTERS[1:10]</pre>
o <- opticut(YYY ~ x2, strata=x0, dist="poisson", comb="rank")</pre>
library(parallel)
cl <- makeCluster(2)</pre>
system.time(uncertainty(o, type="asymp", B=5000))
##
     user system elapsed
##
    0.090
           0.001 0.091
system.time(uncertainty(o, type="asymp", B=5000, cl=cl))
##
     user system elapsed
##
    0.011
           0.002
                   1.038
```

```
system.time(uncertainty(o, type="boot", B=100))
     user system elapsed
##
##
     2.890 0.065 2.963
system.time(uncertainty(o, type="boot", B=100, cl=cl))
##
     user system elapsed
##
    0.009 0.001 1.447
system.time(uncertainty(o, type="multi", B=100))
##
     user system elapsed
## 13.622 0.250 13.898
system.time(uncertainty(o, type="multi", B=100, cl=cl))
##
     user system elapsed
           0.001 6.912
##
    0.009
stopCluster(cl)
```

7 Opticut logo

```
y <- matrix(c(</pre>
   1, 1, 1, 1, 1, 1, 1, 1, 1,
   1, 1, 0, 0, 1, 1, 1,
                             0, 0,
   1, 0, 1, 1, 0, 1, 0,
                            1,
   1, 0, 1, 1,
                  0, 1, 0,
                            1,
   1, 0, 1, 1, 0, 1, 0, 1, 1, 1,
   1, 1, 0, 0, 1, 1, 1, 0, 0, 1,
      1, 1, 1, 1, 1, 1, 1, 1),
   7, 10, byrow=TRUE)
yy \leftarrow t(1-y*0.85)
colnames(yy) <- paste0("Spp", 1:7)</pre>
x <- opticut(yy ~ 1, strata=0:9)</pre>
plot(x, sort=FALSE, cut=-Inf, xlab="", ylab="")
```

