# INTERNATIONAL TRANSACTIONS IN OPERATIONAL RESEARCH





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# Optimization of departure runway scheduling incorporating arrival crossings

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#### **Abstract**

The runway is a key airport resource and an efficient runway operation is critical to enhance the airport efficiency and to reduce delays. This paper addresses the problem of scheduling aircraft departures incorporating arrival crossings. Constraints for wake turbulence separations, flight time window restrictions, and holding queue capacity at runway threshold are explicitly considered. We present two integer linear programming models and a simulated annealing (SA) algorithm. Comparison tests are conducted for the south side of Paris Charles De Gaulle Airport and show that the three proposed methods can significantly improve the solutions based on the simple first-come-first-served rule. Moreover, SA has sufficiently small computation time for real-time deployment.

Keywords: aircraft sequencing problem; ILP; simulated annealing

# 1. Introduction

Continuous air traffic growth has led to congestion in many major airports. Limited capacity is the major cause of congestion. Surface congestion may result in significant delays and operational inefficiencies. Of all airport ground resources, the runway is the main bottleneck, as it is shared by all types of operations (arrivals, departures, and crossings) indicated by field observations (Anagnostakis, 2004). Efficient runway operations planning and control is critical to enhance the airport efficiency and to reduce delays while satisfying all system constraints. One important aspect of runway operations is the departure sequencing and scheduling termed as departure management (DMAN).

The DMAN is a tactical planning tool supporting the departure schedule. It assists in optimizing takeoff time while ensuring safety by taking into account several operational constraints: the minimum wake turbulence separation between successive aircraft, the time window of runway usage

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for individual flights, the interactions with landing runways with regard to airport layout, etc. The minimum separation requirement is a key factor for deciding the runway capacity. The International Civil Aviation Organization divides aircraft into four different wake turbulence weight categories (light, medium, heavy, and super heavy) based on the maximum certificated takeoff mass. Due to wake vortex, an aircraft is perturbed by the preceding one and a minimum separation must be respected to ensure safety. The separation time depends on the categories of the leading and trailing aircraft. For example, a heavy aircraft followed by a light aircraft generates longer separation than a light aircraft followed by a heavy aircraft. The time window constraint represents the earliest and latest time of arrival at the runway threshold. The time window can be applied to both flights with central flow management unit (CFMU) slots and the flights without CFMU slots to ensure fairness. CFMU slot is a takeoff slot that can be assigned to a departing flight in order to avoid congestion in some particular airspace. It is defined as the period between 5 minutes before and 10 minutes after the calculated takeoff times (CTOT). It can be transferred to the gate by subtracting the taxi time. For the flights without CFMU slots, the earliest and latest time of the time window represent the estimated off-block time (EOBT) and a maximum gate holding time with regard to the EOBT, respectively.

The EOBT is the estimated time when an aircraft will be ready after all doors are closed, boarding bridge removed, and is ready to push back upon receipt of clearance from the controller. Next, a target startup approval time (TSAT) is the time provided by controller when an aircraft can expect to receive pushback approval taking into account EOBT, and the traffic situation, etc. TSAT assignment is important to reduce aircraft waiting time with engine on. If many aircraft arrive at the runway threshold waiting for takeoff, a long queue is formed and leads to extra fuel burn. It is more efficient to delay departures before the engines start up so that the traffic arrives at the runway smoothly.

Air traffic controller officers are responsible for sequencing traffic and ensuring minimum separations for departures. In large airports, departure management is handled by three types of controllers: the apron controller (or ramp controller), the ground controller, and the local controller. The apron controller dictates aircraft pushback time from the gate and directs aircraft into gates after landing. They also coordinate with airline operators in implementing ground delays if necessary. The ground controller handles all intermediary taxiing routes to avoid conflicting movements of aircraft, and gives the pilot instructions on reaching the runway holding area via the appropriate taxiways. The local controller clears aircraft for takeoff or landing ensuring the prescribed runway separation.

Runway can be used in segregated mode (only landings or only takeoffs) or in mixed mode (both takeoffs and landings). The mixed mode can achieve higher runway throughput since separation between arrival and departure is shorter. Nevertheless, segregated mode is more often used due to airport layout. Departures and arrivals are highly coupled processes with complex interactions with regard to runway configurations, weather, mix of aircraft, etc. Departing and arrival flights may cross an active runway. Furthermore, controllers delay runway-crossing clearances until a group of aircraft has accumulated at various holding points (Anagnostakis, 2004). However, there is an upper limit on how many aircraft can hold at the same crossing point. For safety reasons, arrivals always have priority over departures and crossings.

Aircraft sequencing problem (ASP) has been studied intensively in the past decades. Research has been conducted both in the United States (Anagnostakis et al., 2000; Balakrishnan and Chandran, 2007; Gupta et al., 2010) and in Europe (Böhme, 2005; Atkin et al., 2007; Deau et al., 2009). Bennell

et al. (2011) presented an extensive overview on landing and takeoff scheduling problems. Lieder and Stolletz (2016) recently summarized different models and solution approaches on the ASP that considers heterogeneous or interdependent runways, featuring articles up to 2015.

ASP can be divided into aircraft landing problem (ALP), aircraft takeoff problem (ATP), and a combination of both problems. Numerous physical and operational constraints as well as the layout of runway system must be considered. Various exact and heuristic approaches have been proposed. The solution quality and the computational time of the approach are two important factors. In real situations, controllers can use only algorithms that can quickly find a good solution. Optimal solutions arising from lengthy computation times are of little practical use (Bennell et al., 2011).

In the rest of this section, we mainly review the ATP and its interactions with the arrival aircraft. Considering the exact approach, Balakrishnan and Chandran (2006, 2007, 2010) introduce a dynamic programming algorithm with constrained position shift that sets a limit on the number of positions an aircraft can occupy in the sequence for the ATP based on their model for the ALP. They also provide complexity analyses of their algorithms and extend their approach for multiple runways and active runway crossings. Montoya et al. (2014) formulate ATP as a multiobjective optimization problem with respect to total aircraft delay and runway throughput, and use dynamic programming to solve. Gupta et al. (2009) present a mixed integer linear program (MILP) to handle the departure queuing area. A following work by the same authors (Gupta et al., 2010) presented an MILP formulation for incorporating active runway crossings in departure scheduling. However, the computational performance was not good due to the lack of good lower bounds. Moreover, the MILP formulation only provides optimal solution for each short time frame (e.g., 15 minutes), which is addressed and improved in Bae et al. (2013).

Different heuristic approaches have been proposed. Atkin et al. (2008a) applied three different heuristic methods for the ATP taking into account some specific constraints concerning London Heathrow airport. Further work can be found in Atkin et al. (2007, 2008b, 2009). Anagnostakis and Clarke (2003) proposed a two-stage heuristic algorithm to solve the departure and runway-crossing problem. Mori (2017) applied a tabu search technique to develop a pushback time assignment algorithm in order to reduce takeoff delay.

Regarding comparative studies between exact and heuristic approaches, Furini et al. (2015) present two MILP models and a tabu search heuristic for finding solutions to the ASP in a short computation time. With a time limit of 15 seconds, the tabu search heuristic outperforms the two MILP models. Malik and Jung (2016) proposed one exact and two heuristic algorithms to solve the ATP, and they conclude that heuristics are more suitable than the exact approach to produce good-quality solutions in a relatively short computation time. D'Ariano et al. (2010) compare branch-and-bound (BB) and heuristic algorithms, setting a time limit of two minutes for the algorithm. Their results show that BB outperforms their heuristics for instances up to 60 minutes of traffic prediction.

In this paper, we focus on the departure sequencing problem incorporating arrival crossings. Different from the literature works, besides specific constraints such as wake turbulence separations, flight time window restrictions, etc., we consider explicitly the holding queue capacity at runway threshold. Moreover, holding point for arrivals is introduced as a decision variable to allow simultaneous crossings. Gate and runway threshold are two control points to hold departures. Two ILP models and a metaheuristic method are proposed to compare the solution quality and computational performance. The paper is organized as follows. In Section 2, the problem statement is

presented. In Section 3, two ILP formulations are proposed in detail, followed by the metaheuristic method in Section 4. Finally, computational results and conclusions are summarized in Sections 5 and 6, respectively.

### 2. The problem statement

Paris CDG airport is one of the busiest passenger airports in Europe, composed of four parallel runways (two for landings and two for departures) and three terminals. Figure 1 illustrates one-month runway throughput of CDG in July 2017; it handled more than 1400 flights per day. The southern pair of runways is in higher demand compared to the northern side due to the fact that it is closer to the main terminal (Terminal 2) of CDG. In this paper, we focus on the departure scheduling problem incorporating arrival crossings on the southern pair of runways: 26L for arrival and 26R for departure. As shown in Fig. 2, there are three main landing runway exits, V2, V3, and V4, and three holding points before crossing, S1, S2, and S3. In practice, the landing runway exit is chosen by the pilot with regard to the aircraft type and how fast it can brake after touching down. Controllers prefer to give priority to arrival aircraft to cross the departure runway without stopping when the departure runway is not fully occupied. When the departure traffic demand is high, controllers indicate arrival aircraft to wait at different holding points and to cross simultaneously. For departures, controllers can hold aircraft at the gate with engines off, or have them waiting at

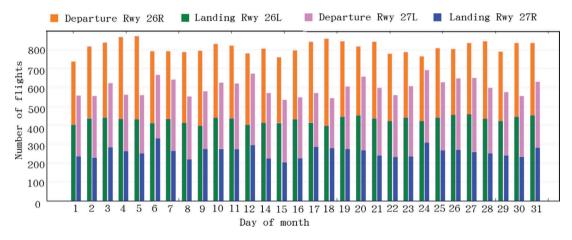


Fig. 1. Paris CDG airport runway throughput chart in July 2017. Southern pair of runways (26L/26R) is in higher demand compared to northern side (27L/27R). July 13 is excluded due to abnormal data record.

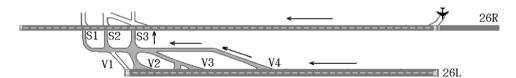


Fig. 2. CDG south-side runway layout. Runway 26L is for landing and 26R is for taking off. The arrival aircraft have to cross the departure runway to reach the taxi area. Three arrival holding points before crossing 26R: S1, S2, and S3.

Three main runway exits: V2, V3, and V4.

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To be more precise, let  $\mathcal{F} = \mathcal{A} \cup \mathcal{D}$  be the set of aircraft (arrivals and departures) that will use the runway during the time horizon  $\mathcal{T}$ , which is discretized into time intervals =  $\{1, \ldots T\}$ . Flight taking off/crossing at the time interval  $t \in \mathcal{T}$  refers that it occurs at the beginning of time interval t. We need to define the following notations for our problem formulation:

```
\mathcal{F}
             set of flights, \mathcal{F} = \mathcal{A} \cup \mathcal{D}
\mathcal{A}
             set of arrivals
\mathcal{D}
             set of departures
\mathcal{E}
             set of landing runway exits, \mathcal{E} = \{V2, V3, V4\}
\mathcal{H}
             set of holding points before crossing departure runway, \mathcal{H} = \{S1, S2, S3\}
\begin{array}{c} d_{e,h} \\ C_d \\ C_a \\ \rho \\ P_i \\ X_i^{0} \\ P_i^{0} \\ X_i^{0} \\ R_i^{p} \\ R_i^{p} \\ R_i^{p} \\ T_{ir} \\ C_i \\ C_i \\ T_{ih} \end{array}
             taxi time from runway exit e \in \mathcal{E} to holding point h \in \mathcal{H}, shown in Table 1
             departure capacity at the runway threshold
             arrival capacity at holding points
             time slot, which is a multiple of time intervals
             scheduled pushback time for flight i \in \mathcal{D}
             taxi time from spot to runway threshold for flight i \in \mathcal{D}
             initial runway usage time for flight i \in \mathcal{D}, T_i^0 = P_i + X_i
             maximum pushback delay (in number of slots) for departure flight i \in \mathcal{D}
             maximum holding time (in number of slots) for departure flight i \in \mathcal{D}
             maximum delay (in number of slots) for departure flight i \in \mathcal{D}, R_i = R_i^p + R_i^w
             set of possible pushback delays for flight i \in \mathcal{D}, \mathcal{R}_i^p = \{1, \dots, R_i^p\}
             set of possible total delays for flight i \in \mathcal{D}, \mathcal{R}_i = \{1, \dots, R_i\}
             time arriving at the runway threshold for flight i \in \mathcal{F}
             possible runway usage time for flight i \in \mathcal{D}, T_{ir} = T_i^0 + r\rho, r \in \mathcal{R}_i
             scheduled landing time for flight i \in A
             runway occupancy time for flight i \in A
             runway exit point for flight i \in A
             initial runway usage time for flight i \in A if i uses the holding point h, T_{ih}^0 = L_i + O_i + d_{e..h}
R_i^a
             maximum holding time (in number of slots) for flight i \in A
\mathcal{R}_{i}^{t}
             set of possible holding delays for flight i \in \mathcal{A}, \mathcal{R}_i^a = \{1, \dots, R_i^a\}
             possible runway usage time for flight i \in A if i uses the holding point h, T_{ihr} = T_{ih}^0 + r\rho, r \in \mathcal{R}_i
             minimum separation in runway usage time of two successive flights i and j with regard to their wake turbulence
                categories, as shown in Table 2
M
             large positive constant
```

Our aircraft runway scheduling consists in the following.

- Choosing a pushback delay  $d_i$ , that is, the difference between the EOBT and the modified pushback time, and a holding duration  $w_i$  at the runway threshold for each departure  $i \in \mathcal{D}$ . With these decisions, we know the arrival time at the runway threshold  $t_i^T = P_i + d_i + X_i$ , and the runway usage time  $t_i = t_i^T + w_i$ .
- Choosing a holding point  $h_i$  and a holding duration  $w_i$  for each arrival  $i \in A$ . With these decisions, we know the arrival time at holding point  $t_i^T = L_i + O_i + d_{e_i,h_i}$ , and the runway usage time  $t_i = t_i^T + w_i$ .

Table 1 Average time from runway exit of 26L to holding point,  $T_{eh}$  (in seconds)

	S1	S2	S3
V2	104	70	59
V3	118	102	75
V4	158	142	115

The average values are calculated based on one-month real traffic data.

Table 2 Single-runway separation requirements for departures and arrival crossings (in seconds)

		Trailing aircraft g						
Category		Heavy	Medium	Light	Crossing			
Leading aircraft f	Heavy	96	120	120	60			
	Medium	60	60	60	60			
	Light	60	60	60	60			
	Crossing	40	40	40	10			

In accordance with the operational practices, pushback delay and holding time are given as multiples of time slot  $\rho$ . A runway schedule is feasible if and only if for each pair of distinct flights  $(i, j) \in \mathcal{F} \times \mathcal{F}$  with  $t_i \leq t_i$ , we have

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- $t_j t_i \ge s_{ij}$  and  $t_j^T \ge t_i^T$  if  $(i, j) \in \mathcal{D} \times \mathcal{D}$ , that is, the minimum wake turbulence separation is respected, and the first aircraft arriving at the holding point departs first;
- $t_j t_i \ge s_{ij}$  and  $t_j^T \ge t_i^T$  if  $(i, j) \in \mathcal{A} \times \mathcal{A}$  and  $h_i = h_j$ , that is, two aircraft using the same holding point follow the FCFS order, and the minimum separation is respected;
- $t_j t_i \ge s_{ij}$  if  $(i, j) \in \mathcal{A} \times \mathcal{D} \cup \mathcal{D} \times \mathcal{A}$ , that is, the minimum separation is guaranteed between arrival and departure, *vice versa*.

Our problem consists of finding a feasible schedule while minimizing the total delay  $\sum_{i \in \mathcal{D}} (d_i + w_i) + \sum_{i \in \mathcal{A}} w_i$ .

The subproblem of scheduling aircraft takeoffs can be seen as a machine scheduling problem with release times, due dates, and sequence-dependent processing times (but zero setup times; Chaudhry and Khan, 2016). A related problem, the simple total tardiness problem (without sequence-dependent setup times), has been shown to be NP-hard (Du and Leung, 1990). Consequently, our runway scheduling problem is NP-hard too.

#### 3. The ILP formulations

Two ILP formulations are given in this section. First, we present Model A that uses the number of time slots as decision. This model involves many so called "big-M" constraints that makes the

LP relaxation rather weak. In order to reduce this number and to strengthen the formulation, we propose Model B termed as delay-indexed formulation.

#### 3.1. Model A: time slot based formulation

The decision variables. We define the following decision variables:

 $d_i \equiv$  number of pushback delay slots for departure flight  $i \in \mathcal{D}$ ;

 $w_i \equiv$  number of holding time slots for flight  $i \in \mathcal{F}$ ;

 $t_i \equiv \text{runway}$  usage time for flight  $i \in \mathcal{F}$ ;

 $t_i^T \equiv \text{time arriving at the runway threshold for flight } i \in \mathcal{F};$ 

$$\delta_{ij} = \begin{cases} 1, & \text{if } i \text{ uses runway before } j \\ 0, & \text{otherwise;} \end{cases} \quad \text{for } i \in \mathcal{F}, j \in \mathcal{F}, i \neq j;$$

$$\alpha_{is} = \begin{cases} 1, & \text{if } i \text{ arrives at the runway threshold before time } s \\ 0, & \text{otherwise;} \end{cases} \quad \text{for } i \in \mathcal{D}, s \in \mathcal{T};$$

$$\beta_{is} = \begin{cases} 1, & \text{if } i \text{ uses runway after time } s \\ 0, & \text{otherwise;} \end{cases} \quad \text{for } i \in \mathcal{D}, \forall s \in \mathcal{T};$$

$$z_{ih} = \begin{cases} 1, & \text{if } i \text{ crosses runway via holding point } h \\ 0, & \text{otherwise;} \end{cases} \quad \text{for } i \in \mathcal{A}, h \in \mathcal{H};$$

$$\beta_{ihs} = \begin{cases} 1, & \text{if } i \text{ crosses via holding point } h \text{ after time } s \\ 0, & \text{otherwise;} \end{cases} \text{ for } i \in \mathcal{A}, \forall h \in \mathcal{H}, \forall s \in \mathcal{T}.$$

The objective function. Our objective is to minimize the total delay:

$$\min \sum_{i \in \mathcal{D}} (d_i + w_i) + \sum_{i \in A} w_i.$$

*The constraints.* 

$$\sum_{h \in \mathcal{H}} z_{ih} = 1, \qquad \forall i \in \mathcal{A},\tag{1}$$

$$t_i^T = T_i^0 + \rho d_i, \qquad \forall i \in \mathcal{D}, \tag{2}$$

$$t_i^T = \sum_{h \in \mathcal{H}} T_{ih}^0 z_{ih}, \qquad \forall i \in \mathcal{A}, \tag{3}$$

$$t_i = t_i^T + \rho w_i, \qquad \forall i \in \mathcal{F}, \tag{4}$$

$$\delta_{ij} + \delta_{ji} = 1, \quad \forall i, j \in \mathcal{F}, i < j,$$
 (5)

$$t_j^T - t_i^T \ge -M(1 - \delta_{ij}), \qquad \forall i, j \in \mathcal{D}, i \ne j,$$
 (6)

$$t_j - t_i \ge s_{ij} - M(1 - \delta_{ij}), \quad \forall i, j \in \mathcal{D}, i \ne j,$$
 (7)

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622 J. Ma et al. / Intl. Trans. in Op. Res. 28 (2021) 615–637

$$t_j^T - t_i^T \ge -M(3 - \delta_{ij} - z_{ih} - z_{jh}), \qquad \forall h \in \mathcal{H}, \forall i, j \in \mathcal{A}, i \ne j,$$
(8)

$$t_i - t_i \ge s_{ii} - M(3 - \delta_{ii} - z_{ih} - z_{ih}), \qquad \forall h \in \mathcal{H}, \forall i, j \in \mathcal{A}, i \ne j,$$

$$(9)$$

$$t_j - t_i \ge s_{ij} - M(1 - \delta_{ij}), \quad \forall (i, j) \in \mathcal{D} \times \mathcal{A} \cup \mathcal{A} \times \mathcal{D},$$
 (10)

$$\alpha_{is} \le \alpha_{i(s+1)}, \qquad \forall i \in \mathcal{D}, \forall s \in \mathcal{T} \setminus \{T\},$$

$$(11)$$

$$\beta_{is} \ge \beta_{i(s+1)}, \qquad \forall i \in \mathcal{D}, \forall s \in \mathcal{T} \setminus \{T\},$$
(12)

$$\beta_{ihs} \ge \beta_{ih(s+1)}, \quad \forall i \in \mathcal{A}, \forall h \in \mathcal{H}, \forall s \in \mathcal{T} \setminus \{T\},$$
(13)

$$t_i - \sum_{s \in \mathcal{T}} \beta_{is} = 0, \quad \forall i \in \mathcal{D},$$
 (14)

$$t_i^T - \sum_{s \in \mathcal{T}} (1 - \alpha_{is}) = 0, \qquad \forall i \in \mathcal{D},$$
(15)

$$\sum_{s \in \mathcal{T}} \beta_{ihs} \le M z_{ih}, \qquad \forall i \in \mathcal{A}, \forall h \in \mathcal{H},$$
(16)

$$t_i - \sum_{h \in \mathcal{H}} \sum_{s \in \mathcal{T}} \beta_{ihs} = 0, \qquad \forall i \in \mathcal{A},$$

$$(17)$$

$$\sum_{i \in \mathcal{D}} (\beta_{is} + \alpha_{is} - 1) \le C_d, \qquad \forall s \in \mathcal{T}, \tag{18}$$

$$\sum_{i \in \mathcal{A} \mid \mathcal{T}_{s}^{0} < s} \beta_{ihs} \le C_{a}, \qquad \forall s \in \mathcal{T}, \forall h \in \mathcal{H},$$

$$\tag{19}$$

$$0 \le d_i \le R_i^p$$
, integer,  $\forall i \in \mathcal{D}$ , (20)

$$0 \le w_i \le R_i^w$$
, integer,  $\forall i \in \mathcal{D}$ , (21)

$$0 \le w_i \le R_i^a$$
, integer,  $\forall i \in \mathcal{A}$ , (22)

$$t_i^T$$
, integer,  $\forall i \in \mathcal{F}$ , (23)

$$t_i$$
, integer,  $\forall i \in \mathcal{F}$ , (24)

$$\delta_{ij} \in \{0, 1\}, \qquad \forall i, j \in \mathcal{F}, i \neq j,$$
 (25)

$$\alpha_{is} \in \{0, 1\}, \qquad \forall i \in \mathcal{D}, \forall s \in \mathcal{T},$$
(26)

$$\beta_{is} \in \{0, 1\}, \qquad \forall i \in \mathcal{D}, \forall s \in \mathcal{T},$$
 (27)

$$z_{ih} \in \{0, 1\}, \qquad \forall i \in \mathcal{A}, \forall h \in \mathcal{H},$$
 (28)

$$\beta_{ihs} \in \{0, 1\}, \qquad \forall i \in \mathcal{A}, \forall h \in \mathcal{H}, \forall s \in \mathcal{T}.$$
 (29)

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arriving at runway threshold and the pushback delay for departures. Constraints (3) link the time arriving at holding point and the holding point decision variables for arrivals. Constraints (4) state the runway usage time as a sum of time to reach the holding point and the holding time. Constraints (5) guarantee that given any two aircraft, one leads the other. Constraints (6) and (7) ensure the first-come-first-served (FCFS) order at the runway threshold and for takeoff as well as the minimum separation for departures. There are two cases to consider here: if  $\delta_{ij} = 1$ , that is, i uses runway before j, then Constraints (6) and (7) become  $t_j^T \ge t_i^T$  and  $t_j - t_i \ge s_{ij}$ , respectively, ensuring that the FCFS order and the separation are respected. If  $\delta_{ij} = 0$ , j uses runway before i, then Constraints (6) and (7) become  $t_i^T - t_i^T \ge -M$  and  $t_j - t_i \ge s_{ij} - M$ , respectively, that is,  $t_i^T - t_i^T$  and  $t_i - t_i$  are bigger than some large negative values, thereby ensuring that this constraint is effectively inactive. Similarly, Constraints (8) and (9) guarantee that at the same holding point, the crossing order of two landing aircraft remains the same with the order they reach the holding point, and ensure the minimum separation while crossing. Constraints (10) guarantee the minimum separation between arrival and departure (vice versa). Constraints (11)–(13) ensure the connectivity in time. For example, if flight i arrives at the runway threshold before time s, then for all the time intervals  $s' \ge s$ ,  $\alpha_{is'}$  has to have a value of 1. Constraints (14) and (15) link the two binary variables to the runway usage time and the arrival time at runway threshold for departures. Constraints (16) ensure that  $\beta_{ihs} = 0$ , if flight i does not use holding point h. Constraints (17) are similar to Constraints (14) that link the binary variable  $\beta_{ihs}$  to the runway usage time for arrivals. Constraints (18) ensure that at every time the number of aircraft waiting at the departure runway threshold will not exceed the departure capacity. The term  $\beta_{is} + \alpha_{is} - 1$  is equal to 1 if and only if flight i is waiting at runway threshold during the time interval s. Likewise, Constraints (19) ensure that at every time the number of crossing aircraft waiting at the holding point will not exceed the holding capacity. Note that, contrary to the departures, we do not need to introduce variables  $\alpha_{ihs}$  for arrivals since the arrival time at runway threshold is known as soon as the holding point is given.

Considering the LP relaxation of the problem, we would like M to be as small as possible, and this can be achieved by tailoring M for each constraint. For example, in Constraints (6), M can be set to  $\max(0, T_i^0 + R_i^p - T_i^0)$ . Moreover, as we know the time range where each aircraft can use the runway, we can strengthen the formulation by fixing the value of some variables:

$$\alpha_{is} = \begin{cases} 1, & \text{for } s \in \{T_{iR_i^p}, \dots, T\} \\ 0, & \text{for } s \in \{1, \dots, T_i^0 - 1\}; \end{cases} \quad \forall i \in \mathcal{D};$$

$$\beta_{is} = \begin{cases} 1, & \text{for } s \in \{1, \dots, T_i^0\} \\ 0, & \text{for } s \in \{T_{iR_i} + 1, \dots, T\}; \end{cases} \quad \forall i \in \mathcal{D};$$

$$\beta_{ihs} = 0, & \text{for } s \in \{0, \dots, T_{ih}^0 - 1\}; \quad \forall i \in \mathcal{A}, h \in \mathcal{H}.$$

### 3.2. Model B: delay-indexed formulation

The decision variables. We define the following binary decision variables:

$$x_{ir} = \begin{cases} 1, & \text{if the takeoff time of flight } i \text{ is delayed by } r \text{ slots} \\ 0, & \text{otherwise;} \end{cases}$$
 for  $i \in \mathcal{D}, r \in \mathcal{R}_i$ 

J. Ma et al. / Intl. Trans. in Op. Res. 28 (2021) 615-637

 $x_{ihr} = \begin{cases} 1, & \text{if } i \text{ crosses via holding point } h \text{ and is delayed by } r \text{ slots} \\ 0, & \text{otherwise;} \end{cases}$ for  $i \in \mathcal{A}$ ,  $h \in \mathcal{H}$ ,  $r \in \mathcal{R}_i^a$ 

 $y_{ir} = \begin{cases} 1, & \text{if the pushback time of flight } i \text{ is delayed by } r \text{ slots} \\ 0, & \text{otherwise;} \end{cases}$ for  $i \in \mathcal{D}$ ,  $r \in \mathcal{R}_i^p$ 

 $\delta_{ij} = \begin{cases} 1, & \text{if } i \text{ uses runway before } j \\ 0, & \text{otherwise;} \end{cases} \quad \text{for } i \in \mathcal{F}, j \in \mathcal{F}, i \neq j$ 

 $\alpha_{is} = \begin{cases} 1, & \text{if } i \text{ arrives at the runway threshold after time } s \\ 0, & \text{otherwise;} \end{cases}$ for  $i \in \mathcal{D}$ ,  $s \in \mathcal{T}$ 

 $\beta_{is} = \begin{cases} 1, & \text{if } i \text{ takes off before time } s \\ 0, & \text{otherwise;} \end{cases}$ 

 $\beta_{ihs} = \begin{cases} 0, & \text{otherwise;} \\ 0, & \text{otherwise;} \end{cases}$  for  $i \in \mathcal{D}, s \in \mathcal{T}$   $\beta_{ihs} = \begin{cases} 1, & \text{if } i \text{ crosses via holding point } h \text{ before time } s \\ 0, & \text{otherwise;} \end{cases}$ for  $i \in \mathcal{A}, h \in \mathcal{H}, s \in \mathcal{T}$ 

The objective function. Our objective is expressed by

$$\min \ \sum_{i \in \mathcal{D}} \sum_{r \in \mathcal{R}_i} r x_{ir} + \sum_{i \in \mathcal{A}} \sum_{h \in \mathcal{H}} \sum_{r \in \mathcal{R}_i^a} r x_{ihr}.$$

The constraints. In order to introduce the constraints, we define the following sets to represent some infeasible assignments pairs of delays (and crossing point for arrivals). Given two distinct flights  $i, j \in \mathcal{F}$ , we introduce

$$C_{ij} = \{(r, q) \in \mathcal{R}_i \times \mathcal{R}_j | T_{jq} - T_{ir} < s_{ij} \text{ and } T_{ir} - T_{jr} < s_{ji}\} \text{ if } (i, j) \in \mathcal{D} \times \mathcal{D},$$

the set of delay assignments that violate the separation requirements between two departure flights;

$$\mathcal{C}_{ijh} = \begin{cases} \{(r,q) \in \mathcal{R}_i \times \mathcal{R}_j^a | T_{jhq} - T_{ir} < s_{ij} \text{ and } T_{ir} - T_{jhq} < s_{ji} \} & \text{if } (i,j) \in \mathcal{D} \times \mathcal{A} \\ \{(r,q) \in \mathcal{R}_i^a \times \mathcal{R}_j^a | (T_{ih}^0 - T_{jh}^0) (T_{ihr} - T_{jhq}) < 0 \\ & \text{or } (T_{jhq} - T_{ihr} < s_{ij} \text{ and } T_{ihr} - T_{jhq} < s_{ji}) \} \end{cases} & \text{if } (i,j) \in \mathcal{A} \times \mathcal{A},$$

the set of delay assignments that violate the separation requirements between departure and arrival or between two arrivals using the same holding point. The first condition in the set definition expresses the violation of the FCFS order for arrival holding point. Note that it is not possible to express the FCFS order for departure queue directly in the set definition. It is ensured by Constraints (38) and (39).

$$\sum_{r \in \mathcal{R}_i} x_{ir} = 1, \qquad \forall i \in \mathcal{D}, \tag{30}$$

$$\sum_{h \in \mathcal{H}} \sum_{r \in \mathcal{R}_i^a} x_{ihr} = 1, \qquad \forall i \in \mathcal{A}, \tag{31}$$

$$\sum_{r \in \mathcal{R}_i} r x_{ir} - \sum_{r \in \mathcal{R}_i^p} r y_{ir} \ge 0, \qquad \forall i \in \mathcal{D},$$
(32)

$$\sum_{r \in \mathcal{R}_i} r x_{ir} - \sum_{r \in \mathcal{R}_i^p} r y_{ir} \le R_i^w, \qquad \forall i \in \mathcal{D},$$
(33)

$$x_{ir} + x_{iq} \le 1, \qquad \forall (r, q) \in \mathcal{C}_{ij}, \forall i, j \in \mathcal{D}, i < j,$$
 (34)

$$x_{ir} + x_{jhq} \le 1, \qquad \forall (r, q) \in \mathcal{C}_{ijh}, \forall h \in \mathcal{H}, \forall i \in \mathcal{D}, \forall j \in \mathcal{A},$$
 (35)

$$x_{ihr} + x_{jhq} \le 1, \qquad \forall (r, q) \in \mathcal{C}_{ijh}, \forall h \in \mathcal{H}, \forall i, j \in \mathcal{A}, i < j,$$
 (36)

$$\delta_{ij} + \delta_{ji} = 1, \quad \forall i, j \in \mathcal{D}, i < j,$$
 (37)

$$\sum_{r \in \mathcal{R}_j} T_{jr} x_{jr} - \sum_{r \in \mathcal{R}_i} T_{ir} x_{ir} \ge -M \delta_{ij}, \qquad \forall i, j \in \mathcal{D}, i \ne j,$$
(38)

$$\sum_{r \in \mathcal{R}_{j}^{p}} T_{jr} y_{jr} - \sum_{r \in \mathcal{R}_{i}^{p}} T_{ir} y_{ir} \ge -M \delta_{ij}, \qquad \forall i, j \in \mathcal{D}, i \ne j,$$

$$(39)$$

$$\alpha_{is} \le \alpha_{i(s+1)}, \quad \forall i \in \mathcal{D}, \forall s \in \mathcal{T} \setminus \{T\},$$

$$(40)$$

$$\beta_{is} \ge \beta_{i(s+1)}, \quad \forall i \in \mathcal{D}, \forall s \in \mathcal{T} \setminus \{T\},$$

$$(41)$$

$$\beta_{ihs} \ge \beta_{ih(s+1)}, \quad \forall i \in \mathcal{A}, \forall h \in \mathcal{H}, \forall s \in \mathcal{T} \setminus \{T\},$$

$$(42)$$

$$\sum_{r \in \mathcal{R}_{i}} T_{ir} x_{ir} - \sum_{s \in \mathcal{T}} \beta_{is} = 0, \qquad \forall i \in \mathcal{D},$$
(43)

$$\sum_{r \in \mathcal{R}_i^p} T_{ir} y_{ir} - \sum_{s \in \mathcal{T}} (1 - \alpha_{is}) = 0, \qquad \forall i \in \mathcal{D},$$

$$(44)$$

$$\sum_{r \in \mathcal{R}_{a}^{a}} T_{ihr} x_{ihr} - \sum_{s \in \mathcal{T}} \beta_{ihs} = 0, \qquad \forall i \in \mathcal{A}, \forall h \in \mathcal{H},$$
(45)

$$\sum_{i \in \mathcal{D}} (\beta_{is} + \alpha_{is} - 1) \le C_d, \qquad \forall s \in \mathcal{T}, \tag{46}$$

$$\sum_{i \in A} \beta_{ihs} \le C_a, \qquad \forall s \in \mathcal{T}, \forall h \in \mathcal{H}, \tag{47}$$

$$x_{ir} \in \{0, 1\}, \qquad \forall i \in \mathcal{D}, \forall r \in \mathcal{R}_i,$$
 (48)

$$x_{ihr} \in \{0, 1\}, \qquad \forall i \in \mathcal{A}, \forall h \in \mathcal{H}, \forall r \in \mathcal{R}_i^a$$
 (49)

$$y_{ir} \in \{0, 1\}, \qquad \forall i \in \mathcal{D}, \forall r \in \mathcal{R}_i^p,$$
 (50)

$$\delta_{ij} \in \{0, 1\}, \qquad \forall i, j \in \mathcal{D}, i \neq j, \tag{51}$$

$$\alpha_{is} \in \{0, 1\}, \qquad \forall i \in \mathcal{D}, \forall s \in \mathcal{T},$$
 (52)

J. Ma et al. / Intl. Trans. in Op. Res. 28 (2021) 615-637

$$\beta_{is} \in \{0, 1\}, \qquad \forall i \in \mathcal{D}, \forall s \in \mathcal{T},$$
 (53)

$$\beta_{ihs} \in \{0, 1\}, \quad \forall i \in \mathcal{A}, \forall h \in \mathcal{H}, \forall s \in \mathcal{T}.$$
 (54)

Constraints (30) and (31) require exactly one time period of runway usage for departure and arrival flights. Constraints (32) guarantee that for departures, the arrival time at the runway threshold is always smaller than the takeoff time. Constraints (33) state the maximum holding time for departures. Constraints (34)–(36) ensure the separation criteria between two departures, arrival and departure, and two arrival crossings, respectively. Constraints (37) guarantee that given any two aircraft, one leads the other. Constraints (38) and (39) guarantee the same order waiting at the runway threshold and for takeoff for departures. Constraints (40)–(42) are similar to Constraints (11)–(13) in Model A. Constraints (43) and (44) link the binary variables for departures. Constraints (45) is similar to Constraints (43), which link the binary variables for arrivals. Constraints (46)–(47) are the similar to Constraints (18) and (19) in Model A.

One disadvantage of this discrete time formulation is a relatively large number of variables (in particular, Constraints (34)–(36)). In order to reduce the number of variables, we reformulate Constraints (34) and (35) to Constraints (55), and Constraints (36) to Constraints (56).

$$x_{ir} + \sum_{j \in \mathcal{D}, j \neq i} \sum_{q \mid (r,q) \in \mathcal{C}_{ii}} x_{jq} + \sum_{h \in \mathcal{H}} \sum_{j \in \mathcal{A}} \sum_{q \mid (r,q) \in \mathcal{C}_{iih}} x_{jhq} \le 1 + M(1 - x_{ir}), \qquad \forall r \in \mathcal{R}_i, \forall i \in \mathcal{D}, \quad (55)$$

$$x_{ihr} + \sum_{j \in \mathcal{A}, j \neq i} \sum_{q \mid (r,q) \in \mathcal{C}_{ijh}} x_{jhq} \le 1 + M(1 - x_{ihr}), \qquad \forall r \in \mathcal{R}_i^a, \forall h \in \mathcal{H}, \forall i \in \mathcal{A}.$$
 (56)

There are two cases to consider: if  $x_{ir}=1$ , then the takeoff time of flight i is delayed by r slots, Constraints (55) become  $\sum_{j\in\mathcal{D},j\neq i}\sum_{q\mid (r,q)\in\mathcal{C}_{ij}}x_{jq}+\sum_{h\in\mathcal{H}}\sum_{j\in\mathcal{A}}\sum_{q\mid (r,q)\in\mathcal{C}_{ijh}}x_{jhq}\leq 0$ , ensuring that i is separated with respect to all the other flights. If  $x_{ir}=0$ , then Constraints (55) become  $\sum_{j\in\mathcal{D},j\neq i}\sum_{q\mid (r,q)\in\mathcal{C}_{ij}}x_{jq}+\sum_{h\in\mathcal{H}}\sum_{j\in\mathcal{A}}\sum_{q\mid (r,q)\in\mathcal{C}_{ijh}}x_{jhq}\leq 1+M$ , which inactivates the constraints. The same reasoning applies to Constraints (56).

The decision variables of Model A can be linked to the decision variables of Model B using the following equations (57)–(60):

$$w_i = \sum_{r \in \mathcal{R}_i} i x_{ir}, \qquad \forall i \in \mathcal{D}, \tag{57}$$

$$d_i = \sum_{r \in \mathcal{R}_i^p} i y_{ir}, \qquad \forall i \in \mathcal{D}, \tag{58}$$

$$w_i = \sum_{h \in \mathcal{H}} \sum_{r \in \mathcal{R}_i^a} i x_{ihr}, \qquad \forall i \in \mathcal{A},$$
(59)

$$z_{ih} = \sum_{r \in \mathcal{R}_i^a} x_{ihr}, \qquad \forall i \in \mathcal{A}, \forall h \in \mathcal{H}.$$

$$(60)$$

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626

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x_{irq} = \begin{cases} 1, & \text{if the pushback time of flight } i \text{ is delayed by } r \text{ slots} \\ & \text{and flight } i \text{ holds } q \text{ slots at the runway threshold} \end{cases} \quad \text{for } i \in \mathcal{D}, r \in \mathcal{R}_i^p, q \in \mathcal{R}_i^w.
0, \quad \text{otherwise;}
```

However, experimental tests showed that the benefit is counterbalanced by the large increase in the number of variables and constraints.

After describing our two ILP formulations, in the next section we consider also the metaheuristic method to tackle the aircraft runway scheduling problem.

# 4. Simulated annealing

In this section, we present a simulated annealing (SA) algorithm to solve our aircraft runway scheduling problem.

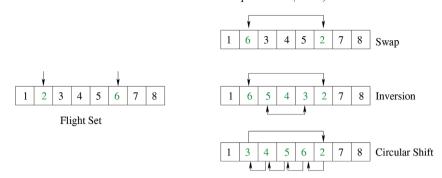
# Algorithm 1. Simulated annealing

```
Require: Initial state S_0, T_0;
S_c \leftarrow S_0, T \leftarrow T_0, i \leftarrow 0;
while T > T_f do
\text{for } i = 0 \text{ to } N_T \text{ do}
Generate a neighborhood solution, S_N;
\text{if } E(S_N) \leq E(S_C) \text{ then}
S_C \leftarrow S_N;
\text{else if } \text{random}(0,1) < \exp{\frac{-(E(S_N) - E(S_C))}{T}} \text{ then}
S_C \leftarrow S_N;
\text{end if}
\text{end for}
T \leftarrow \beta T;
\text{end while}
\text{return} S_c
```

SA (Kirkpatrick et al., 1983) is a metaheuristic that simulates the annealing of a metal, in which the metal is heated up and slowly cooled down to move toward an optimal energy state. SA is applied to many optimization problems, in particular the job shop scheduling problem (Cruz-Chávez et al., 2017). In SA, the objective function to be minimized is analogous to the energy of the physical problem. Algorithm 1 illustrates the SA procedure, where the parameters are as follows:

- $S_0$ : the initial solution;
- $S_C$ : the current solution;
- $S_N$ : the neighborhood solution generated from  $S_C$ ;
- $T_0$ : the initial temperature;





J. Ma et al. / Intl. Trans. in Op. Res. 28 (2021) 615-637

Fig. 3. Illustration of three neighborhood generation methods: swap, that is, exchanging the positions of two aircraft; inversion, that is, inverting the order of aircraft between two positions; circular shift, that is, moving the first aircraft to the final position, while shifting all other aircraft to the previous position.

- T: the current temperature;
- $T_f$ : the final temperature;
- $\vec{E}$ : the SA fitness function;
- $N_T$ : the total number of transitions in each temperature step;
- $\beta$ : the geometrical temperature reduction coefficient.

A global parameter T is used to simulate the cooling process. A current solution may be replaced by a random "neighborhood" solution with a probability. We start the cooling process from a high initial temperature  $T_0$  (which can be determined by a heating process or defined by user), the current solution changes almost randomly at a high temperature, thus the algorithm is able to escape from local minima. The decrease in temperature may follow different laws such as linear law, geometric law, etc. At each temperature step, a number of transitions are executed. The probability to accept a degrading solution becomes smaller and smaller when T decreases. Therefore, at the final stages of the annealing process, the system will converge to a near-global or global optimum.

In order to apply SA to our problem, the neighborhood generation is critical and needs to be defined precisely. Our neighborhood choice is similar to a traveling salesman problem with a constrained search space. The algorithm starts with an initial sequence sorted by the earliest runway usage time. First, we randomly choose one flight, and we search for a list of sequence positions that can be used by the current chosen flight without exceeding the maximum delay. Then, we choose one flight in the list and apply three exchange strategies with the current one: *swap, inversion*, and *circular shift*. As shown in Fig. 3, swap move exchanges the positions of two aircraft, inversion move inverts the order of aircraft between two positions, and circular shift move changes the first aircraft to the final position, while shifting all other aircraft to the previous position. Note that it is necessary to relax the maximum pushback delay and maximum holding time constraints in order to allow SA to search more freely in the state space. Nevertheless, a penalty coefficient is added if one aircraft cannot meet the maximum delay constraints. At the end of the procedure, SA can always find a solution satisfying the maximum delay requirement. A comparison test with one-hour traffic is made to find the most efficient neighborhood generation method. As indicated in Fig. 4, the strategy combining circular shift move and swap move can achieve less delay than other

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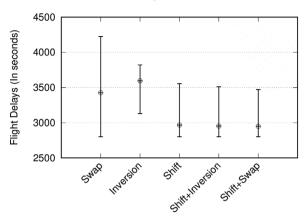


Fig. 4. Comparison of different neighborhood methods on solution qualities. We run the proposed SA algorithm 10 times with the same input parameters for each method. The error bar represents the minimum delay, the average delay, and the maximum delay, respectively.

Table 3
Empirically set parameter values of SA

Parameter	Value
Geometrical temperature reduction coefficient, $\delta$	0.95
Number of transitions at each temperature step, $N_T$	100
Initial temperature, $T_0$	0.1
Final temperature, $T_f$	$0.0001 \times T_0$

strategies. Thus, in the remaining part of the paper, we choose circular shift move and swap move as our neighborhood generation method.

After the previous step, we obtained a new sequence, and we now have to update the flight schedules: First, we set the earliest runway usage time of the first flight in the sequence as its actual runway usage time. Then, for each aircraft, its runway usage time is set with respect to its earliest available time and the minimum separation with its precedent aircraft. Moreover, the best holding point for arrivals is determined. More precisely, we calculate for each holding point the required waiting time for the flight and choose the holding point with the shortest waiting time. Table 3 lists some SA parameters related to our problem.

#### 5. Computational results

In this section, we present the results of some computational experiments. We test our methodology on both real data cases at Paris CDG Airport and randomly generated data. Numerical results with different settings of (user-defined) algorithm parameters are presented and discussed. The overall process is run on a 2.50 GHz core i7 CPU, PC under Linux operating system, implemented in the Java programming language. The ILP models were solved with GUROBI solver (Gurobi Optimization, 2018) with the default parameters settings. Table 4 lists some parameters related to our mathematical

Table 4
Chosen parameter values specifying the optimization problem

Parameter	Value
Departure capacity at runway threshold, $C_d$	5
Arrival capacity at holding points, $C_a$	2
Time slot, $\rho$	5 seconds
Maximum pushback delay (in number of slots), $R_i^p$	120
Maximum holding time (in number of slots) for departures, $R_i^w$	120
Maximum holding time (in number of slots) for arrivals, $R_i^a$	36

formulation. The actual pushback time from historical data is considered as the EOBT in this paper. In our test cases, all the flights are without CFMU slots due to data unavailability.

In the current system, controllers schedule aircraft takeoffs in an FCFS order with regard to their earliest arrival time at runway threshold. In this study, we set an FCFS sequence as the baseline based on the earliest arrival time at runway threshold. We assume that all the arrival flights use the closest holding point after they land, that is, S3. There is no limit on the maximum holding number and the maximum waiting time at the runway threshold. Moreover, a landing aircraft is assumed to cross the departure runway without any holding time. In a real-world case, arrivals do have priority on departures, as departures can be held on the ground. The arrival holding area is limited in terms of capacity and should be vacated as early as possible.

To illustrate how we calculate the FCFS sequence and compare with the optimized sequence, we give an example by generating a random instance consisting of 15 aircraft (5 arrivals and 10 departures). As shown in Table 5, given the initial landing time or initial pushback time, we calculate the earliest arrival time at runway threshold,  $t_i^T$ . For departures,  $t_i^T = P_i + X_i$ ; for arrivals,  $t_i^T = L_i + O_i + T_{e,h}$ . We assume that all the arrival flights use the closest holding point after they land, that is, S3. Then, we build an FCFS sequence by sorting  $t_i^T$  and we obtain the runway usage time  $t_i$  with regard to the separation requirements. After that, the optimized sequence is presented in Table 5. We observed a decrease in total delay from 4340 seconds in the baseline case to 2950 seconds in the optimized case.

We chose a heavy traffic summer day, July 11, 2017, as our test case. An optimization time window of one hour is applied from 8:00 to 20:00; the rest of the periods involve only a few flights. As illustrated in Table 6, real traffic data provide various mixes of arrivals and departures: three fully loaded periods of 8:00–9:00, 11:00–12:00, and 19:00–20:00 with more than 30 departures per hour per runway, and 14:00–15:00 with 30 arrivals per hour per runway are observed.

Table 6 shows the comparison of optimization results for four cases: FCFS, Model A, Model B, and SA. We list the gap, that is, the percent increase in total delay over the optimal solution. The computation time in seconds is listed in the last four columns. For SA, the gap and the computation time are averaged over 10 times random runs. In order to be fair and practical in the real-world application, we set the computational time limit to be 10 seconds for all the algorithms. As shown in Table 6, first we can see a significant reduction of delays from Model A and SA compared to FCFS sequence. Model B cannot find a feasible solution in most of the cases within the time limit. Model A can find a near-optimal solution. Nevertheless, it is difficult to prove the

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Table 5 Example of FCFS sequence and optimized sequence with a random instance of 5 arrivals and 10 departures

			-	-								-		
D01	D02	D03	D04	D05	D06	D07	D08	D09	D10	A01	A02	A03	A04	A05
H	M	M	H	M	M	M	M	M	M	C	C	C	C	C
0	10	20	30	40	50	60	70	80	90	_	_	_	_	_
300	300	300	300	300	300	300	300	300	300	_	_	_	_	_
_	_	_	_	_	_	_	_	_	_	0	100	200	300	400
_	_	_	_	_	_	_	_	_	_	60	60	60	60	60
_	_	_	_	_	_	_	_	_	_	V4	V4	V4	V4	V4
A01	A02	D01	A03	A04	D02	A05	D03	<b>D04</b>	D05	D06	<b>D07</b>	<b>D08</b>	D09	D10
175	275	300	375	475	310	575	320	330	340	350	360	370	380	390
0	0	15	0	0	205	0	295	345	455	505	555	605	655	705
175	275	315	375	475	515	575	615	675	795	855	915	975	1035	1095
<b>S</b> 3	S3	_	S3	S3	_	S3	_	_	_	_	_	_	_	_
115	115	_	115	115	_	115	_	_	_	_	_	_	_	_
							4340							
A01	A02	D02	D08	D10	D01	A03	A04	A05	D09	D05	D06	D07	D03	D04
_	_					_	_	_						580
_	_	10				_	_	_				490		610
175	275		370	420	490	419	519	575	610	670	730	790	855	910
0	0	5	5	15	5	140	50	0	5	5	5	5	0	5
175	275	315	375	435	495	559	569	575	615	675	735	795	855	915
<b>S</b> 3	<b>S</b> 3	_	_	_	_	<b>S</b> 1	S1	<b>S</b> 3	_	_	_	_	_	_
115	115	_	_	_	_	158	158	115	_	_	_	_	_	_
							2950							
	H 0 300 175	H         M           0         10           300         300           -         -           -         -           -         -           -         -           175         275           0         0           175         275           S3         S3           115         115    A01 A02	H         M         M           0         10         20           300         300         300           -         -         -           -         -         -           -         -         -           -         -         -           -         -         -           -         0         15           175         275         315           S3         S3         -           115         115         -           A01         A02         D02           -         -         0           -         -         10           175         275         310           0         0         5           175         275         315           S3         S3         -	H         M         M         H           0         10         20         30           300         300         300         300           -         -         -         -           -         -         -         -           -         -         -         -           -         -         -         -           -         -         -         -           -         0         0         15         0           175         275         315         375         S3           S3         S3         -         S3           115         -         115           A01         A02         D02         D08           -         -         0         0           -         -         10         70           175         275         310         370           0         0         5         5           175         275         315         375           S3         S3         -         -	H         M         M         H         M           0         10         20         30         40           300         300         300         300         300           -         -         -         -         -           -         -         -         -         -           -         -         -         -         -           -         -         -         -         -           A01         A02         D01         A03         A04           175         275         300         375         475           0         0         15         0         0         0           175         275         315         375         475           S3         S3         -         S3         S3           115         115         115         115           115         115         115         115           A01         A02         D02         D08         D10           -         -         0         0         30           -         -         0         0         30           -         -	H         M         M         H         M         M           0         10         20         30         40         50           300         300         300         300         300           300         300         300         300           300         300         300         300           300         300         300         300           300         300         300         300           401         402         D01         A03         A04         D02           175         275         300         375         475         310           0         0         15         0         0         205           175         275         315         375         475         515           S3         S3         -         S3         S3         -           115         115         -         115         115         -           A01         A02         D02         D08         D10         D01           -         -         0         0         30         190           -         -         0         0         30	H         M         M         H         M         M         M           0         10         20         30         40         50         60           300         300         300         300         300         300         300           300         300         300         300         300         300         300           300         300         300         300         300         300         300           300         300         300         300         300         300         300           401         A02         D01         A03         A04         D02         A05           175         275         300         375         475         310         575           0         0         15         0         0         205         0           175         275         315         375         475         515         575           S3         S3         -         S3         S3         -         S3           115         115         -         115         -         115           A01         A02         D02         D08         D10	H         M         M         H         M         M         M         M           0         10         20         30         40         50         60         70           300         300         300         300         300         300         300         300           300         300         300         300         300         300         300         300           300         300         300         300         300         300         300         300           300         300         300         300         300         300         300         300           401         A02         D01         A03         A04         D02         A05         D03           175         275         300         375         475         310         575         320           0         0         15         0         0         205         0         295           175         275         315         375         475         515         575         615           S3         S3         -         S3         S3         -         S3         -         S3         -	H         M         M         H         M	H         M         M         H         M	H         M	H         M         M         M         M         M         M         M         M         M         M         M         M         M         M         C         C           300         60         30         30	H         M         M         H         M         M         M         M         M         M         M         M         C         C         C           300         200         200         -         -         -         0         0         100         200         200         200         200         200         200         300         340         350         360         370         370         300         375         475         310         575         615         675         795         855         915         975         83         33         -         83         83	H         M         M         H         M         M         M         M         M         M         M         M         C         C         C         C           300         300         300         300         300         300         300         300         300         300         300         300         300         200         300 <t< td=""></t<>

H, heavy; M, medium; C, crossing. All the times are in seconds. The FCFS sequence and the optimized sequence as well as their total delays are in bold.

Table 6 Comparison of heuristics for solving one-hour real traffic on July 11, 2017

	Nur	nber of flight	.s	Gap (%	(o)			Computational time (seconds)				
Time window	All	Departure	Arrival	FCFS	Model A	Model B	SA	Model B optimum	Model A	Model B	SA	
8:00–9:00	54	31	23	69.59	_	_	2.35	113.13	10.00	10.00	3.35	
9:00-10:00	49	23	26	84.43	3.92	_	6.34	43.98	10.00	10.00	3.60	
10:00-11:00	34	16	18	66.16	0.00	19.44	0.00	12.31	2.02	10.00	1.57	
11:00-12:00	55	30	25	82.64	12.08	_	2.15	58.35	10.00	10.00	3.82	
12:00-13:00	40	22	18	84.04	0.00	_	4.62	20.15	4.37	10.00	1.94	
13:00-14:00	25	20	5	33.31	4.89	_	4.37	22.47	10.00	10.00	0.41	
14:00-15:00	46	16	30	79.18	7.32	_	5.04	27.51	10.00	10.00	3.31	
15:00-16:00	41	18	23	67.31	0.00	18.68	0.00	13.51	2.22	10.00	2.44	
16:00-17:00	39	24	15	68.82	0.00	_	7.81	26.82	10.00	10.00	1.52	
17:00-18:00	45	19	26	81.02	10.84	_	2.06	29.34	10.00	10.00	2.94	
18:00-19:00	47	23	24	43.12	10.25	45.27	0.12	64.87	10.00	10.00	3.00	
19:00-20:00	54	32	22	76.23	28.87	_	5.55	156.80	10.00	10.00	3.21	

Best results are in bold.

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Table 7
Comparison of heuristics for solving two-hour real traffic on July 11, 2017

	Num	ber of fl	ights	Gap (%	<u>5</u> )			Computation time (s)				
Time Window	All	Dep.	Arr.	FCFS	Model A	Model B	SA	Model B Optimum	Model A	Model B	SA	
8:00–10:00	103	54	49	84.15	_	_	3.92	378.90	20.00	20.00	15.68	
10:00-12:00	89	46	43	81.51	11.35	_	0.46	99.67	20.00	20.00	10.35	
12:00-14:00	65	42	23	68.74	12.26	_	2.65	83.40	20.00	20.00	3.91	
14:00-16:00	87	34	53	77.13	6.97	_	4.21	53.78	20.00	20.00	11.22	
16:00-18:00	84	43	41	77.56	22.13	_	3.42	83.79	20.00	20.00	8.81	
18:00-20:00	101	55	46	81.88	39.31	_	5.12	383.93	20.00	20.00	13.14	

Best results are in bold.

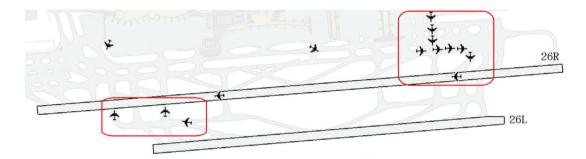


Fig. 5. Departure queues at 9:30 at runway 26R at CDG Airport on February 18, 2016. Visualization of actual surface surveillance data.

optimality due to the poor lower bound when the number of aircraft is large and the traffic scenario is dense. Therefore, we still use Model B to find the optimal solution with a reasonable time from 12 seconds up to 156 seconds, as shown in the first column of computational times in Table 6. In contrast, SA can find good-quality solutions with most of the gaps less than 10% within five seconds.

In order to test the performance of algorithms facing large instances, we set our time window to be two hours and the algorithm running time limit to be 20 seconds. The number of flights ranges from 65 to 103, which is challenging to find a good solution in a short period of time. As shown in Table 7, first we observe a large gap between FCFS solution and optimal solution. After optimization, SA can still find a near-optimal solution within the time limit compared to other models. In 18:00–20:00, the computational time is 384 seconds for Model B, even Model A has a gap of 39% compared to optimality. This proves that SA is more suitable and more practical for dealing with large instances.

We test another heavy traffic day on February 18, 2016. A departure queue of nine aircraft with three arrivals waiting at the holding point at 9:30 is illustrated in Fig. 5. As shown in Table 8, in 9:00–10:00, there are 58 aircraft with 35 departures and 23 arrivals.

The optimization results are listed in Table 8. SA still keeps a similar performance compared to the first test. Model A also shows very good performance to find the optimal solution within

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Table 8 Comparison of heuristics for solving one-hour real traffic on February 18, 2016

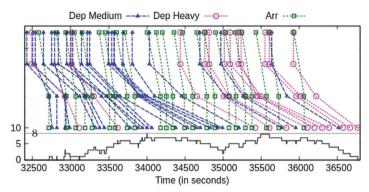
	Nur	nber of flight	.s	Gap (%	(o)			Computation time (seconds)				
Time window	All	Departure	Arrival	FCFS	Model A	Model B	SA	Model B optimum	Model A	Model B	SA	
6:00-7:00	41	19	22	61.23	11.79	_	0.64	86.73	10.00	10.00	1.51	
7:00-8:00	48	13	35	71.16	0.00	53.67	3.81	14.57	5.35	10.00	2.31	
8:00-9:00	34	17	17	57.49	0.00	0.00	0.00	8.20	1.25	8.20	1.05	
9:00-10:00	58	35	23	85.31	41.09	_	6.55	353.74	10.00	10.00	3.28	
10:00-11:00	48	21	27	79.81	8.46	_	1.81	106.17	10.00	10.00	2.40	
11:00-12:00	42	20	22	26.98	1.57	_	0.00	51.01	10.00	10.00	1.68	
12:00-13:00	42	30	12	33.09	7.31	_	8.48	124.70	10.00	10.00	1.35	
13:00-14:00	37	14	23	89.82	0.00	0.00	1.96	6.22	1.36	6.22	1.33	
14:00-15:00	41	23	18	47.05	0.00	69.09	2.54	24.38	6.80	10.00	1.40	
15:00-16:00	40	20	20	45.77	0.00	_	0.99	16.02	5.39	10.00	1.47	
16:00-17:00	38	10	28	58.86	0.00	4.21	0.00	11.51	4.76	10.00	1.49	
17:00-18:00	46	25	21	84.14	9.09	_	0.00	25.20	10.00	10.00	1.99	
18:00-19:00	45	19	26	69.45	0.47	-	0.61	80.24	10.00	10.00	2.02	
19:00-20:00	46	26	20	73.77	5.26	_	2.17	34.19	10.00	10.00	1.89	
20:00-21:00	41	21	20	74.54	0.00	_	2.36	28.71	10.00	10.00	1.54	

Best results are in bold.

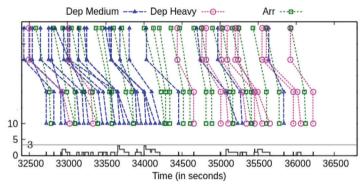
10 seconds, except in 9:00–10:00 with a gap of 41%. Note that 9:00–10:00 is the period in the highest demand of the day. Next, we analyze in detail the optimization results of time window 9:00–10:00. Figure 6 shows the sequencing results in 9:00–10:00 for three cases: the FCFS sequence, the optimal sequence with a preference to wait at the holding point, and the optimal sequence with a preference to wait at the gate. One can observe a large departure delay as well as a long departure queue for FCFS case illustrated at the bottom of the Fig. 6a. While in Fig. 6b, much less departure delays are achieved with slight modification of arrival holding time. The departure queue is reduced to three aircraft. In Fig. 6c, with a preference of holding at gate, aircraft taxi to the runway threshold and take off smoothly.

Next, we generate some random data set to check if our methods can be suitable for dense traffic scenarios. The mix of arrivals and departures, and the fleet mix of medium and heavy aircraft are two important factors in departure scheduling. Thus, we generate 15 random high traffic demand scenarios in a time window of 30 minutes. The number of arrivals/departures is set to be 10/20, 15/15, and 15/20. A mix of heavy aircraft from 0% to 40% is set. Results are shown in Table 9: the solution quality decreases when the number of departures increases; SA keeps the shortest computational time; Model A is more suitable for cases with low departure rate.

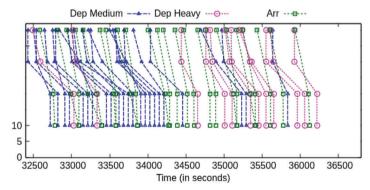
In conclusion, Model B is suitable for finding an optimal solution while Model A is suitable for finding a feasible solution within a short computation time. In fact, by imposing a time limit, Model A solves most instances and sometimes reaches optimality. However, when the runway is in high demand, Model A is not able to find a good-quality solution. The SA is suitable for finding a near-optimal solution in a short computational time.



(a) FCFS sequence. Each line represents one flight, the four points from top to bottom for departures indicate respectively initial pushback time, actual pushback time, arriving time at the runway threshold, and take-off time; the three points from top to bottom for arrivals indicate respectively landing time, arriving time at the runway threshold, and crossing time. The departure waiting queue is shown at the bottom of the figure.



(b) Optimal sequence with a preference to wait at the holding point.



(c) Optimal sequence with preference to wait at the gate.

Fig. 6. Comparison of the FCFS sequence, optimal sequence with a preference to wait at the holding point, and optimal sequence with preference waiting at the gate.

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Table 9
Comparison of heuristics for solving random data with different fleet mix

	Gap (%	)			Computation time (s)					
$Arr\!-\!Dep\!-\!H\%\!-\!M\%$	FCFS	Model A	Model B	SA	Model B Optimum	Model A	Model B	SA		
10-20-0-100	68.36	15.14	_	8.01	97.07	10.00	10.00	0.58		
10-20-10-90	74.54	27.99	_	5.99	80.35	10.00	10.00	0.57		
10-20-20-80	81.77	0.00	_	1.41	31.93	10.00	10.00	0.56		
10-20-30-70	64.55	28.23	_	8.80	601.98	10.00	10.00	0.59		
10-20-40-60	85.78	3.57	_	3.57	36.80	10.00	10.00	0.57		
15-15-0-100	59.00	0.00	_	1.51	25.68	10.00	10.00	0.63		
15-15-10-90	91.28	0.00	_	11.45	13.03	4.06	10.00	0.70		
15-15-20-80	59.55	19.15	_	4.78	146.53	10.00	10.00	0.67		
15-15-30-70	93.73	0.00	_	7.53	15.40	8.59	10.00	0.73		
15-15-40-60	89.47	0.00	_	5.99	13.60	10.00	10.00	0.74		
15-20-0-100	70.74	40.16	_	15.54	52.63	10.00	10.00	0.96		
15-20-10-90	36.28	15.40	_	6.21	86.23	10.00	10.00	1.01		
15-20-20-80	25.94	5.71	_	0.32	154.06	10.00	10.00	1.02		
15-20-30-70	32.39	0.64	_	1.77	48.41	10.00	10.00	1.11		
15-20-40-60	54.74	22.68	_	9.03	2194.23	10.00	10.00	1.05		

A time window of 30 minutes is considered, "10–20–0–100" means 10 arrivals and 20 departures with a fleet mix of 0% heavy and 100% medium. Best results are in bold.

#### 6. Conclusions

The runway system is a major source of delay in the departure process. It is critical to achieve efficient scheduling of aircraft taking into account specific operational constraints. In this paper, we have developed two ILP models and one metaheuristic algorithm for departure runway scheduling incorporating arrival crossings. Specific constraints such as wake turbulence separations, flight time window restrictions, and holding queue capacity at runway threshold are explicitly considered. Different comparison tests on real and random data were launched and demonstrate that the time slot based formulation can find an optimal or near-optimal solution quickly, but it is hard to prove optimality facing high demand periods; the delay-indexed formulation can prove optimality in a reasonable time; SA is a good candidate for having a near-optimal solution to reduce flight delays, and the run times are sufficiently small for real-time application. The runway sequencing algorithm can be implemented as a decision support tool for controllers in actual operations. However, the benefits of the runway sequencing algorithm may be limited by the uncertainty arising from real operations. For real-time application, flight information needs to be updated frequently and accurately as time passes. For example, the taxi time to the runway threshold can be varied with regard to the current aircraft position at the airport after pushback. A proper prediction of the travel time on the surface can help the tactical runway sequencing algorithms better organize the sequence and decrease flight delays. Future extensions of the model could develop a robust algorithm facing uncertain pushback time and taxi time changes.

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