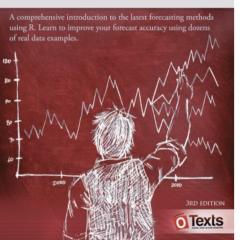
Rob J Hyndman George Athanasopoulos

FORECASTING PRINCIPLES AND PRACTICE



10. Dynamic regression models

10.5 Dynamic harmonic regression OTexts.org/fpp3/

Dynamic harmonic regression

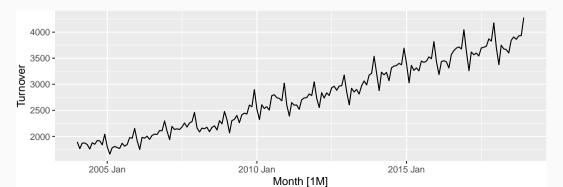
Combine Fourier terms with ARIMA errors

Advantages

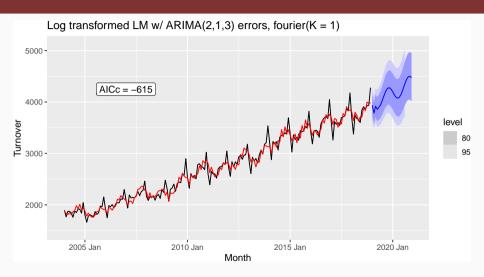
- it allows any length seasonality;
- for data with more than one seasonal period, you can include Fourier terms of different frequencies;
- the seasonal pattern is smooth for small values of K (but more wiggly seasonality can be handled by increasing K);
- the short-term dynamics are easily handled with a simple ARMA error.

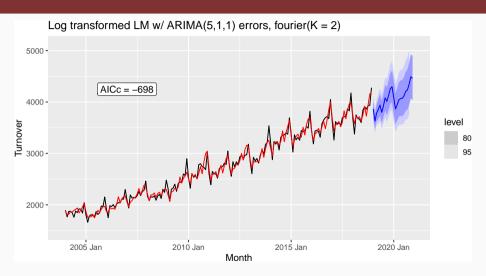
Disadvantages

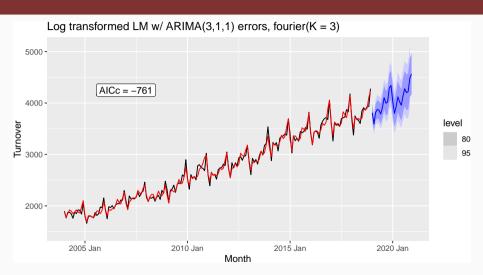
seasonality is assumed to be fixed

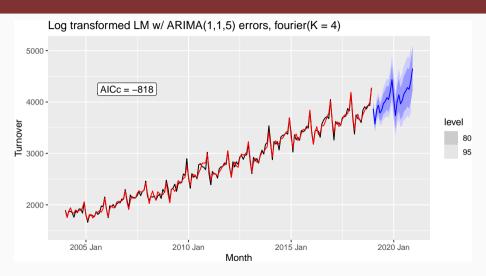


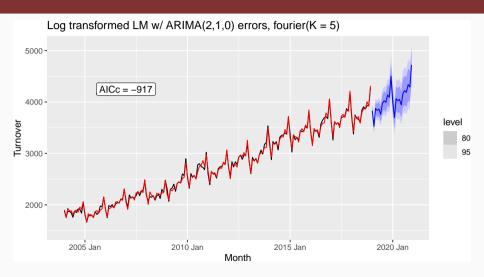
model	sigma2	log_lik	AIC	AICc	BIC
Κ = 1	0.002	317	-616	-615	-588
K = 2	0.001	362	-700	-698	-661
K = 3	0.001	394	-763	-761	-725
K = 4	0.001	427	-822	-818	-771
K = 5	0.000	474	-919	-917	-875
K = 6	0.000	474	-920	-918	-875

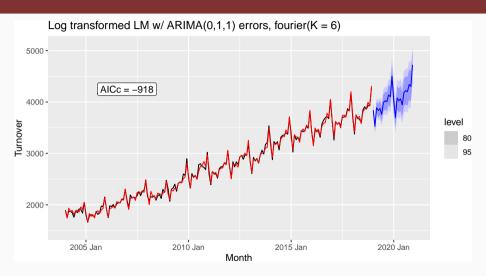












Example: weekly gasoline products

```
fit <- us gasoline |>
 model(K06 = ARIMA(Barrels \sim fourier(K = 6) + PDO(0, 0, 0)))
report(fit)
## Series: Barrels
## Model: LM w/ ARIMA(0,1,1) errors
##
## Coefficients:
  mal fourier(K = 6)C1 52 fourier(K = 6)S1 52 fourier(K = 6)C2 52 fourier(K = 6)S2 52
##
## -0.895
          -0.1121 -0.2299
                                              0.0419
                                                           0.0316
## s.e. 0.013
                  0.0123 0.0122 0.0099
                                                           0.0099
  ##
##
            0.0832 0.0345
                                         0.0186 0.0398
        0.0094
                        0.0094
                                         0.0093
                                                      0.0092
## s.e.
  fourier(K = 6)C5_52 fourier(K = 6)S5_52 fourier(K = 6)C6_52 fourier(K = 6)S6_52 intercept
##
##
           -0.0314 0.0010 -0.0522
                                                0.0002
                                                             0.0014
## s.e.
            0.0092
                    0.0092 0.0091
                                                      0.0091
                                                             0.0007
##
## sigma^2 estimated as 0.06205: log likelihood=-33.1
## ATC=96 2 ATCC=96 6
                BTC=174
                                                                11
```

Example: weekly gasoline products

```
forecast(fit, h = "3 years") |>
autoplot(us_gasoline)
```

