Evaluating Neural Network
Robustness against FGSM and PGD
Adversarial Attacks with \(\L \) Norms
Perturbations

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AGENDA

- 01 INTRODUCTION
- 02 RELATED WORK
- 03 METHODOLOGY
- 04 CONCLUSION
- 05 REFERENCES

INTRODUCTION

Artificial Intelligence (AI), with the integration of Deep Learning (DL) has resulted in notable and significant advancements in modern data-driven technologies, such as autonomous vehicle systems, image recognition and classification, and natural language processing,

Deep Learning Architectures

- Convolutional Neural Networks (CNNs)
- Recurrent Neural Networks (RNNs)
- Long Short-Term Memory Networks (LSTMs)
- Transformers
- DenseNet
- Autoencoders, etc.

Adversarial Attacks

INTRODUCTION CONT'D

| Attack Technique | Туре |
|---|------------------------------|
| FGSM (Fast Gradient Sign Method) | White-box, Non-targeted |
| PGD (Projected Gradient Descent) | Iterative White-box |
| Carlini-Wagner | Optimization-based White-box |
| DeepFool | White-box |
| JSMA (Jacobian-based Saliency Map Attack) | White-box |
| One-Pixel Attack | White-box |
| Boundary Attack | White-box |
| Spatial Transformation Attack | White-box or Black-box |
| Universal Adversarial Perturbations | White-box or Black-box |
| Data Poisoning Attack | White-box or Black-box |

Table 1: Adversarial Techniques and Types

INTRODUCTION CONT'D

Real-World Scenarios

Researchers tricked an autonomous driving Al into misreading fake signs and exceeding speed limits, showcasing adversarial attacks through physical means.



Figure 2: Attacked Microsoft Chatbot(Tay Bot) [2].



Figure 1: Autonomous Vehicle [1].

Microsoft's AI chatbot Tay began tweeting offensive content after a data-poisoning attack in 2016, revealing the vulnerability of AI to malicious inputs.

INTRODUCTION CONT'D

Problem Statement

- Neural networks show high error rates against adversarial attacks.
- Attacks can undermine safety-critical systems relying on AI.

Research Objectives

- Evaluate DenseNet-161 robustness against FGSM and PGD using L_1 , L_2 , L_∞ norms.
- Examine the impact of adversarial training on model resilience.

Research Questions

- How robust is DenseNet-161 against FGSM and PGD attacks with \(\alpha\) norms?
- Does adversarial training improve resilience?

COMPUTATIONAL AND DATA SCIENCE-MTSU

RELATED WORK

| Section | Key Themes | Findings and Contributions |
|--|--|---|
| The Inception and Evolution of Adversarial Machine Learning | Goodfellow et al. (2014) [3] discuss neural networks' vulnerability to adversarial examples, attributing it to their linear nature. They suggest adversarial training as a method to reduce error rates. | Pioneered the understanding of linearity in neural networks and its role in adversarial vulnerability; Developed adversarial training techniques. |
| | Madry et al., (2017) [4] investigate the vulnerability of deep neural networks to adversarial examples and propose a robust optimization framework | Introduced a methodology to enhance adversarial robustness in deep learning models. |
| | Huang et al., (2022) [5] enhance PGD and C&W algorithms for adversarial attacks targeting tram object detectors, demonstrating quick and effective attacks | Advanced the understanding of adversarial threats in public transportation safety. |
| Norm-Based Perturbations: A Spectrum of Attacks | Research on L∞ norm perturbations is predominant, but L1 and L2 norms offer different perspectives and attack strategies | Broadened the understanding of adversarial perturbations beyond the commonly focused L∞ norm |
| The Quest for Robustness Across Norms | Focus on L∞ norm defenses leaves gaps against L1 and L2 norm attacks, suggesting a false sense of security in models. | Identified a critical research gap in defending against diverse norm-based adversarial attacks |
| Gaps & Combined Approach | The research evaluates DenseNet161's defense against FGSM and PGD attacks (using L1, L2, and L∞ norms) on the Stanford Dogs dataset. | The study aims to enhance the understanding of adversarial robustness in detailed image classification, helping to create broader defense strategies against various adversarial attacks. |

Table 2: Related Work

METHODOLOGY

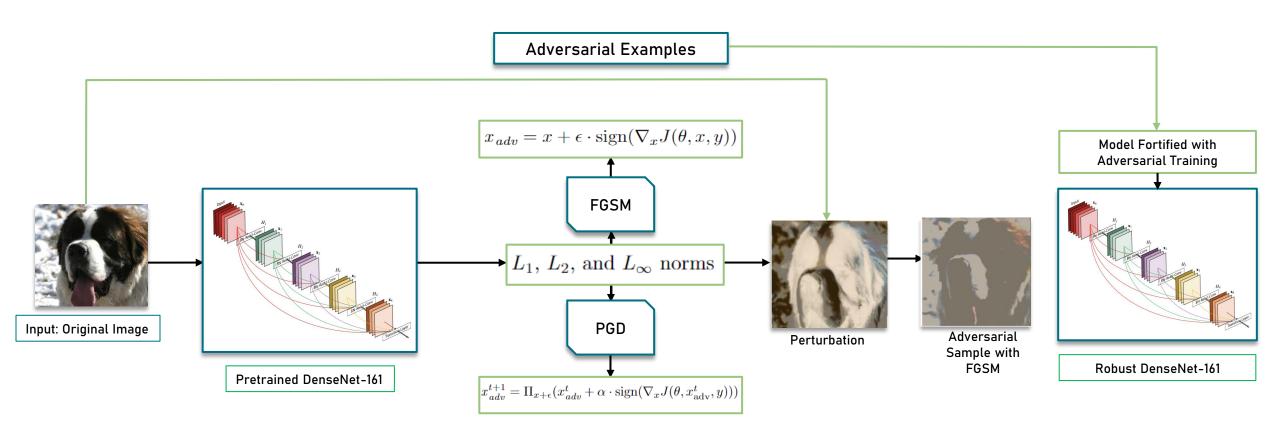


Figure 3: Research Process Design

DATA COLLECTION

Stanford Dogs Detail

The Stanford Dogs dataset provides a platform to evaluate the effectiveness of DenseNet-161 in a fine-grained visual categorization task and procedure.

| Aspect | Detail |
|----------------------|---------------------------------------|
| Dataset | Stanford Dogs |
| Number of Categories | 120 |
| Number of Images | 20,580 |
| Annotations | Class labels, Bounding boxes |
| Lists | Lists, with train/test splits (0.5MB) |
| Train Features | Train Features (1.2GB) |
| Test Features | Test Features (850MB) |

Table 3: Stanford Dogs Dataset Detail.



Figure 4: Stanford Dogs Image Samples [6].

MODEL ARCHITECTURE

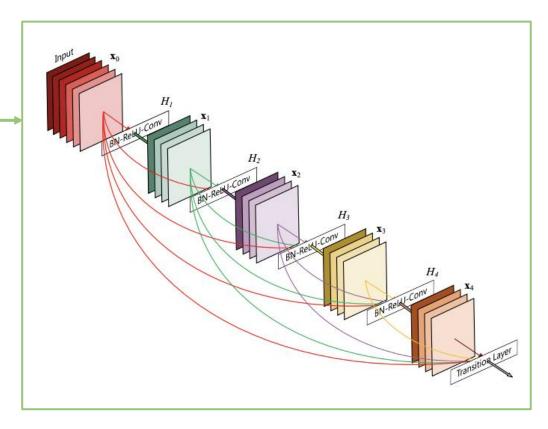
DenseNet-161: Architecture

DenseNet-161, a Dense Convolutional Network (DenseNet) variant, represents a significant advancement in deep learning architectures. DenseNet-161 is distinguished by its depth and complexity, incorporating 161 layers, and is specifically engineered to optimize parameter efficiency.

Features

- Dense Connectivity
- Efficient Feature Propagation
- Feature Concatenation
- Reduced Number of Parameters

MODEL HYPERPARAMETERS: Learning Rate = 0.001, Max-Epoch = 5, Batch-Size = 32, Optimizer = Adam



$$x_l = H_l([x_0, x_1, ..., x_{l-1}])$$

Here, x_l denotes the output feature maps of the lth layer.

Figure 5: A dense block comprising five layers [8].

ADVERSARIAL ATTACKS

Fast Gradient Sign Method (FGSM)

FGSM is an attack technique that generates adversarial examples by exploiting the gradients of the neural network. The goal is to create a new image, x_{adv} , that is visually similar to the original image, x, but is classified incorrectly by the network.

The adversarial image x_{adv} is computed as follows:

$$x_{\text{adv}} = x + \epsilon \cdot \text{sign}(\nabla_x J(\theta, x, y))$$

where:

- x: Original input image.
- x_{adv} : Adversarial image.
- ε: Perturbation magnitude, controlling how much the input is altered.
- $\nabla_x J(\theta, x, y)$: Gradient of the model's loss function concerning the input image.
- J: Loss function used by the neural network.
- θ : Parameters (weights) of the model.
- y: True label of the input image.
- $sign(\cdot)$: Sign function that extracts the sign of the gradient

The $sign(\cdot)$ function ensures that the perturbation is minimal but effective, causing the input to cross the decision boundary.

Projected Gradient Descent (PGD)

PGD is an iterative attack method that extends FGSM. PGD is often considered more powerful as it applies small perturbations iteratively, allowing for a more fine-grained search for adversarial examples. The adversarial image at each iteration t + 1 is calculated as:

$$x_{\text{adv}}^{t+1} = \Pi_{x+\epsilon}(x_{\text{adv}}^t + \alpha \cdot \text{sign}(\nabla_x J(\theta, x_{\text{adv}}^t, y)))$$

where:

- x_{adv}^{t+1} : Adversarial image at iteration t+1.
- $x_{\text{adv}}^{\overline{t}}$: Adversarial image at iteration t.
- α : Step size for each iteration.
- $\Pi_{x+\epsilon}(\cdot)$: Projection function ensuring the adversarial image remains within an ϵ -ball of the original image.

PARAMETERS USED: Epsilon = 0.003, Alpha = 0.01, Iteration = 10

THE L NORMS

The L norms, specifically L_1 , L_2 , and L_∞ , are crucial in defining the nature of perturbations applied in adversarial attacks like FGSM and PGD. Each norm provides a different way to measure the perturbations' magnitude, thereby shaping the characteristics of the adversarial examples generated.

L₁ Norm (Manhattan Norm)

Mathematically: $||\delta||_1 = \sum_i |\delta_i|$

The L_1 norm of a perturbation is the sum of the absolute values of its vector elements. In the context of images, it represents the sum of absolute differences across all pixels.

L₂ Norm (Euclidean Norm)

Mathematically: $||\delta||_2 = \sqrt{\sum_i \delta_i^2}$

The L_2 norm is the square root of the sum of the squares of the vector elements, equivalent to the Euclidean distance from the origin.

L_∞ Norm (Maximum Norm)

Mathematically: $||\delta||_{\infty} = \max_{i} |\delta_{i}|$

The L_{∞} norm is the maximum absolute value of the elements of the vector. In image perturbation, it limits the maximum change that can be applied to any pixel.

ADVERSARIAL TRAINING

Deep Learning Resilient Techniques

- Adversarial Training
- Defense Layers
- Randomization
- Ensemble Methods
- Feature Denoising
- Defensive Distillation
- Input Preprocessing
- Robust Optimizers

Adversarial Training Algorithm

```
Result: Train the model with enhanced robustness using adversarial
        training
Initialize: Model parameters;
while training do
   Get a batch of data (x, y);
   Forward Pass: Compute logits logits = model(x);
   Compute Loss: loss = CrossEntropyLoss(logits, y);
   Log training loss;
   Calculate and log training accuracy;
   if current \ epoch \ge adv\_training\_start\_epoch then
       Adversarial Training:
         1. Compute gradient w.r.t input data: data\_grad = \nabla_x loss;
         2. Generate adversarial examples: x_{adv} = fgsm\_attack(x, \epsilon, data\_grad);
         3. Forward pass with adversarial examples: logits_{adv} = model(x_{adv});
         4. Compute loss for adversarial examples:
            loss_{adv} = CrossEntropyLoss(logits_{adv}, y);
         Log adversarial training loss;
         6. Compute combined loss: combined\_loss = loss + loss_{adv};

    Backward pass and update model parameters using combined_loss;

   else
       Standard Training:

    Backward pass and update model parameters using loss;

   end
   Algorithm 3: Adversarial Training for Dog Breed Classifier
```

RESULTS

The research shows DenseNet-161, trained on the Stanford Dogs dataset, achieving optimal performance in the second epoch with high precision and accuracy, indicating its strong capability in fine-grained image classification of dog breeds.

Metric Performance without Adversarial Attacks

| Epoch | Validation Loss | Accuracy | F1 Score | Precision |
|-------|-----------------|----------|----------|-----------|
| 1 | 0.7362 | 0.7840 | 0.7798 | 0.8127 |
| 2 | 0.6460 | 0.8020 | 0.7971 | 0.8230 |
| 3 | 0.6998 | 0.7932 | 0.7858 | 0.8206 |
| 4 | 0.6884 | 0.7928 | 0.7859 | 0.8180 |
| 5 | 0.6914 | 0.7959 | 0.7920 | 0.8159 |

Table 4: Model Metric Performance

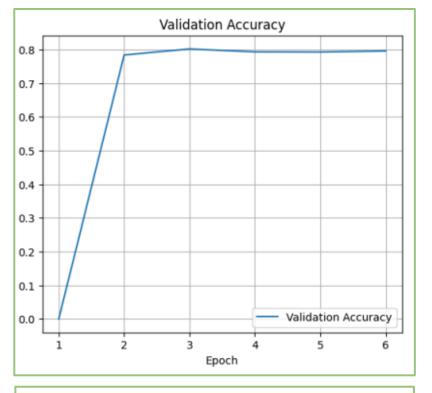
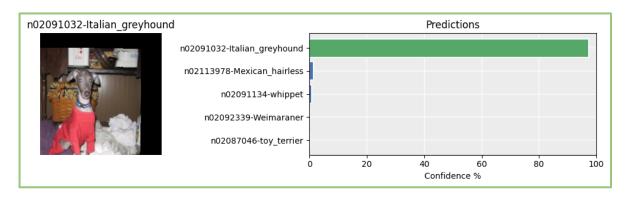
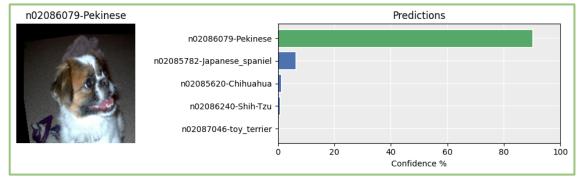


Figure 5: Graph of Model's Validation Accuracy

Model Prediction without Adversarial Attacks with Confidence Score in Percentage





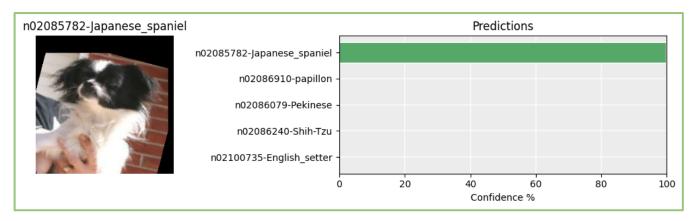


Figure 6 : Dog Image Prediction Confidence Scores

Model Prediction with FGSM Adversarial Attacks with Confidence Score in Percentage

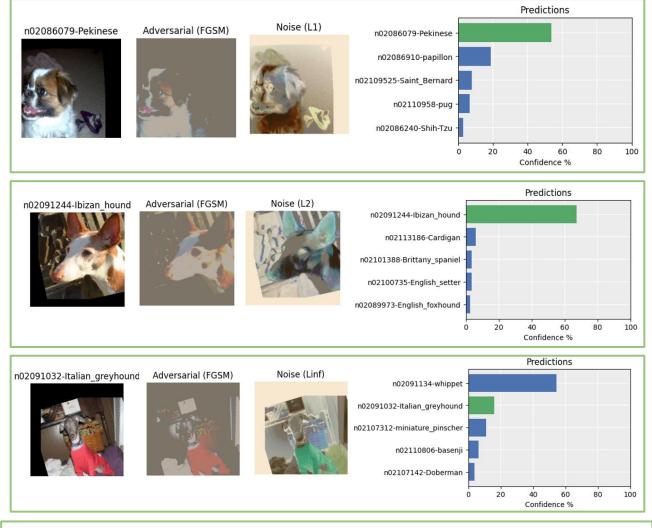


Figure 7: Dog Image Prediction Confidence Scores with FGSM Adversarial Attacks

Model Prediction with PGD Adversarial Attacks with Confidence Score in Percentage

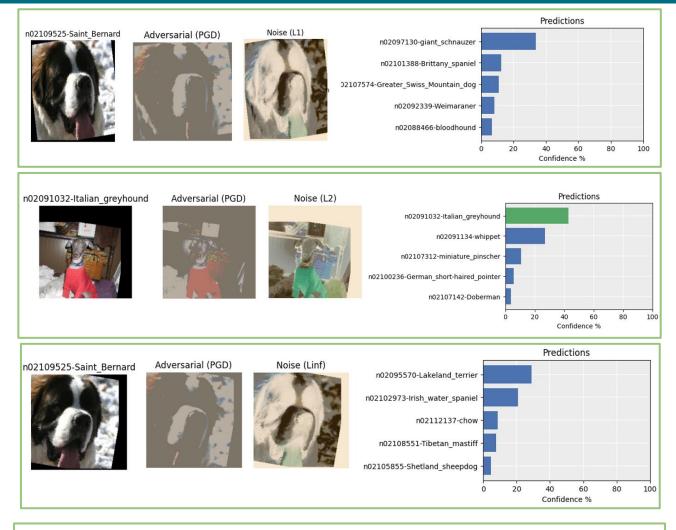


Figure 8: Dog Image Prediction Confidence Scores with PGD Adversarial Attacks

Model Metric Performance After Adversarial Training with Adversarial Attacks Implementation

| Attack Type | Norm | Accuracy |
|-------------|--------------|----------|
| Clean | None | 79.37% |
| FGSM | L_{∞} | 17.78% |
| PGD | L_1 | 19.61% |
| PGD | L_2 | 16.06% |
| PGD | L_{∞} | 4.03% |

Table 5: FGSM & PGD Adversarial Attacks on Model Before Training

| Attack Type | Norm | Accuracy |
|-------------|--------------|----------|
| Clean | None | 79.59% |
| FGSM | L_{∞} | 31.05% |
| PGD | L_1 | 34.11% |
| PGD | L_2 | 29.32% |
| PGD | L_{∞} | 9.79% |

Table 6: FGSM & PGD Adversarial Attacks on Model After Training

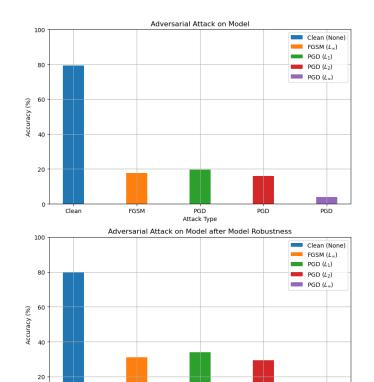


Figure 8: Distribution of Adversarial Attacks Before and After Training

CONCLUSION

The study shows DenseNet161's vulnerability to adversarial attacks, notably PGD, with accuracy dropping from 79% to 4%. Adversarial training did make the model somewhat more robust, yet significant gaps remain, especially against L^{∞} norm attacks, highlighting the urgent need for more advanced security in AI for real-world resilience.

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