

Assignment No. 1
Calculus and Analytic Geometry

Name: _____ Id: _____ Program: _____

Last date to submit 7th April 2022

Max. Marks: 7

Q.No.1 List the following sets in descriptive form

- a. $A = \{n \in \mathbb{Z}^+ \mid n \text{ is a factor of } 6\}$
- b. $B = \{n \in \mathbb{Z} \mid n \text{ is a factor of } 6\}$

Q.No.2 List the following sets in tabular form

- a. Last four letters of English language
- b. Negative integer whose square root is a real number

Q.No.3 List the following sets in set builder form

- a. Positive integers between 10 and 20
- b. Negative integers whose squares are less than and equal to 25

Q.No.4 Let $A = \{w, x, y, z\}$ and $B = \{a, b\}$. Use the set-roster notation to write each of the following sets, and indicate the cardinal number of each set:

- a. $A \times B$
- b. $B \times A$
- c. are answers of part(a) and b same? (yes or No)

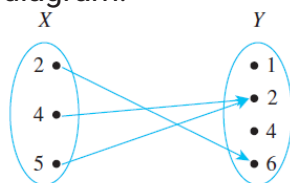
Q.No.5 Let A and B are the sets, defined by $A = \{1, 2, 3\}$ and $B = \{1, 3, 5\}$, and relation M is defined by $M = \{(1, 1), (1, 3), (2, 5), (2, 1), (3, 3)\}$ from A to B. Answer the following questions

- a. Draw the ray diagram of M, from A to B
- b. Is M a function? (Yes, No)
- b. in either case write a reason

Q.No.6 Let A and B are the sets, defined by $A = \{1, 2, 3\}$ and $B = \{1, 3, 5\}$ and define a relations $R = \{(1, 1), (2, 1), (3, 3)\}$ from A to B. Answer the following questions

- a. is R a function? (yes, No)
- b. in either case, draw the ray diagram of R, from A to B
- c. Write the domain, range and codomain of R

Q.No.7 Let $X = \{2, 4, 5\}$ and $Y = \{1, 2, 4, 6\}$. Define a function $F: X \rightarrow Y$ by the following arrow diagram:



- a. Write the domain, Range and co-domain of F.
- b. Find $F(-1)$, $F(0)$, and $F(1)$.

Q.No.8 Find inverse of the following functions

- a. $f(x) = 10/(2x-5)$, this function is not defined for $x = 5/2$
- b. $g(x) = 5/(x+9)$, this function is not defined for $x = -9$
- c. $k(x) = x/(2x-5)$, this function is not defined for $x = 5/2$

Q.No.9 Find the values of x where the following functions are undefined

- a. $f(x) = 2/(2-x)$
- b. $g(x) = (x-2)/(-3x+1)$
- c. $k(x) = (x-3)/(x^2+5x+6)$

Q.No.10 Find the natural domain for the following functions

- a. $f(z) = -2z^2 + 12z + 5$
- b. $f(t) = 2 - \sqrt{z^2+1}$

Q.No.11 Let a quadratic function $f(x) = x^2 + 3x - 4$. This function is defined for all real values of x . Find

- a. The vertex of $f(x)$
- b. The minimum value of $f(x)$
- c. The equation of line of symmetry
- d. The range of $f(x)$
- e. The values of x where $f(x) = 0$
- f. The domain of $f(x)$

Q.No.12 Let $f(x) = 2x^2 + 1$ and $g(x) = 2x - 1$ are functions. Find the following composition functions.

- a. $f \circ g(x)$
- b. $g \circ f(x)$