

Test Functions for Single-Objective Optimization Problems

	FORMULA	SEARCH DOMAIN
1	$f(x, y) = -20 \exp \left(-0.2 \sqrt{0.5 (x^2 + y^2)} \right) - \exp (0.5 (\cos (2\pi x) + \cos (2\pi y))) + e + 20$	$-5 \leq x, y \leq 5$
2	$f(\mathbf{x}) = \sum_{i=1}^n x_i^2$	$-\infty \leq x_i \leq \infty, 1 \leq i \leq n$
3	$f(\mathbf{x}) = \sum_{i=1}^{n-1} \left[100 (x_{i+1} - x_i^2)^2 + (x_i - 1)^2 \right]$	$-\infty \leq x_i \leq \infty, 1 \leq i \leq n$
4	$f(x, y) = (1.5 - x + xy)^2 + (2.25 - x + xy^2)^2 + (2.625 - x + xy^3)^2$	$-4.5 \leq x, y \leq 4.5$
5	$f(x, y) = (1 + (x + y + 1)^2 (19 - 14x + 3x^2 - 14y + 6xy + 3y^2)) (30 + (2x - 3y)^2 (18 - 32x + 12x^2 + 48y - 36xy + 27y^2))$	$-2 \leq x, y \leq 2$
6	$f(x, y) = (x + 2y - 7)^2 + (2x + y - 5)^2$	$-10 \leq x, y \leq 10$
7	$f(x, y) = 100 \sqrt{ y - 0.01x^2 } + 0.01 x + 10 .$	$-15 \leq x \leq -5, -3 \leq y \leq 3$
8	$f(x, y) = 0.26 (x^2 + y^2) - 0.48xy$	$-10 \leq x, y \leq 10$
9	$f(x, y) = \sin^2 (3\pi x) + (x - 1)^2 (1 + \sin^2 (3\pi y)) + (y - 1)^2 (1 + \sin^2 (2\pi y))$	$-10 \leq x, y \leq 10$
0	$f(x, y) = 2x^2 - 1.05x^4 + \frac{x^6}{6} + xy + y^2$	$-5 \leq x, y \leq 5$