

GTU Department of Computer
Engineering

CSE 222 / 505 – Spring 2022

Homework 6

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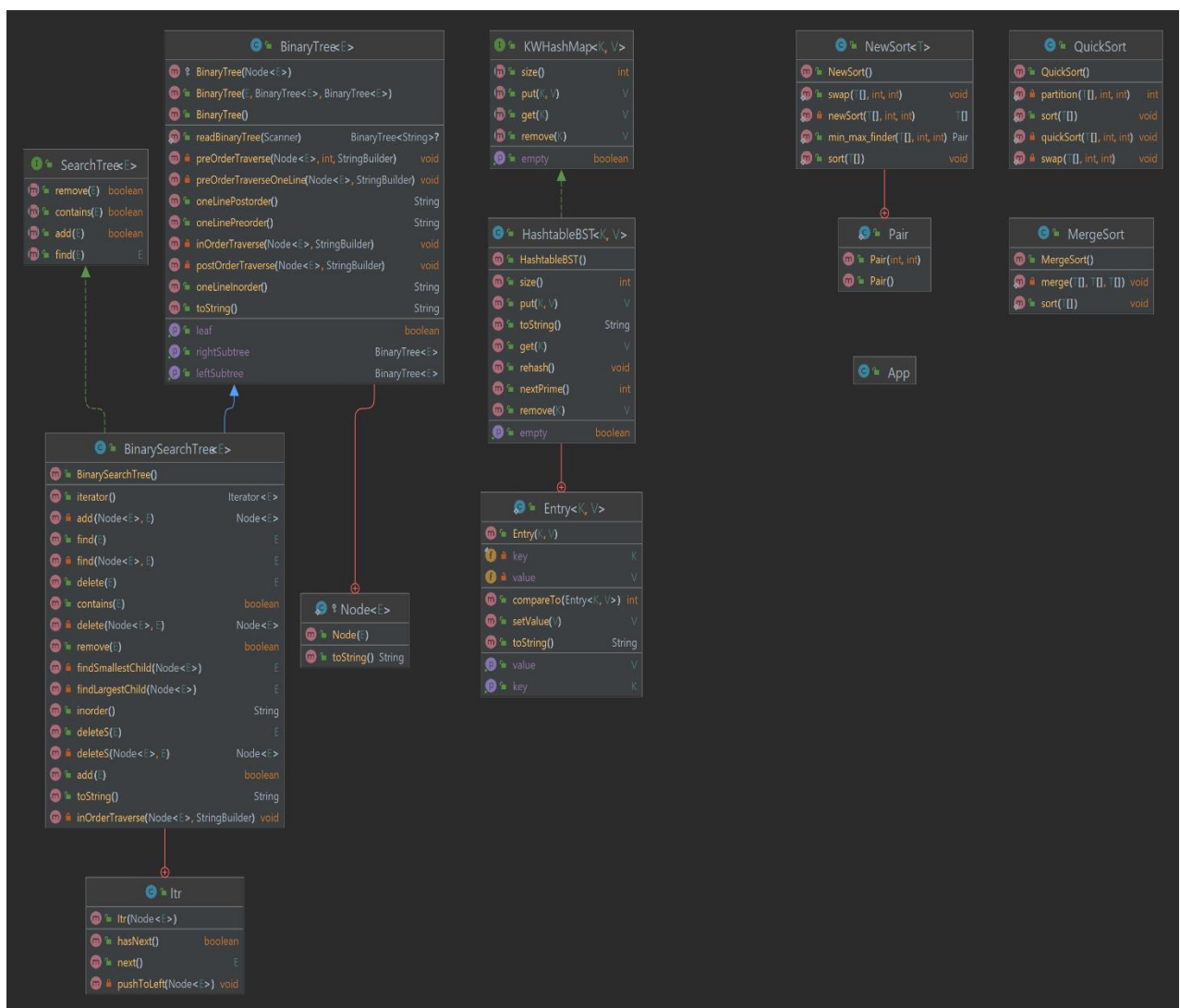
1 – System Requirement

Operating System must have JDK (Java Development Kit) 11 and JRE (Java RuntimeEnvironment) 11 or higher.

There should be enough space for storing data's.

2 – Class Diagrams

*Higher Resolution Version of the Class Diagram is in the files.



3. Problem - Solution Approach

Problem:

1 -) Implement the chaining technique for hashing. Use binary search trees to chain items as underlying structure mapped on the same table slot.

2-) Compare the sorting algorithms Quick Sort, Merge Sort and New Sort both empirically and theoretically.

Solution:

1-) When implementing a hash table using chaining technique if the items stack over one index more than the others, searching for an item gets longer and it approaches to linear $O(n)$ complexity. To prevent this instead of using linked list as underlying structure, using Binary search trees makes searching time an average of $O(n \log n)$. Thus, gives us faster average but more complex space structure.

2-) Tested 3 sort algorithms by 100 time each with 100, 1000 and 10000 elements.

4 – Test Cases

a-) Testing the hash table for part1

- 1 – Adding 100 elements to the hash table and measuring time.
- 2 – Check the isEmpty with empty hash table.
- 3 – Check the isEmpty with filled hash table.
- 4 – Remove element from hashtable.
- 5 – Try removing unexisting element.
- 6 – Add an element with same key value to update it.

b-) Testing the sort algorithms for part2

- 1 -) Compare 3 algorithms 100 times with 100 sized arrays.
- 2 -) Compare 3 algorithms 100 times with 1000 sized arrays.
- 3 -) Compare 3 algorithms 100 times with 10000 sized arrays.

5 – Running Program and Results

a) Testing the hash table for part1

1 – Adding 100 elements to the hash table and measuring time

```
Added 100 elements to hashtable = 12 ms
```

2 – Check the isEmpty with empty hash table.

```
Creating new empty hashtable  
This hashtable is empty ==> true
```

3 – Check the isEmpty with filled hash table.

```
Added one to hashtable  
one  
This hashtable is empty ==> false
```

4 – Remove element from hashtable.

```
Removed one from hashtable  
This hashtable is empty ==> true
```

5 – Try removing unexisting element.

```
Trying to remove unexisting element from table
```

6 – Add an element with same key value to update it.

```
Added one to six to hashtable  
one two three four five six  
  
Added eight and nine to hashtable as 5 and 6 keys to update five and six  
one two three four eight nine
```

b-) Testing the sort algorithms for part2

1 -) Compare 3 algorithms 100 times with 100 sized arrays.

```
100 x 100
Merge Sort =5 ms
Quick Sort =7 ms
New Sort   =15 ms
```

2 -) Compare 3 algorithms 100 times with 1000 sized arrays.

```
100 x 1000
Merge Sort =49 ms
Quick Sort =14 ms
New Sort   =174 ms
```

3 -) Compare 3 algorithms 100 times with 10000 sized arrays.

```
100 x 10000
Merge Sort =169 ms
Quick Sort =102 ms
New Sort   =16390 ms
```

6 – Calculate Time complexity

--Example Hash Table functions implementations

```
1  /**
2      * If the key is in the table, remove it and return its value.
3      * Otherwise, return null
4      *
5      * @param key The key of the entry to remove.
6      * @return The value of the key that was removed.
7      */
8  public V remove(K key)
9  {
10     int index = Math.abs(key.hashCode()) % CAPACITY;
11     if (table[index] == null) {return null;}
12
13     var entry = table[index].find(new Entry<>(key, null));
14
15     if (entry == null) {return null;}
16
17     V oldValue = entry.getValue();
18     table[index].remove(entry);
19     numKeys--;
20     return oldValue;
21 }
```

```
1  public void rehash()
2  {
3      BinarySearchTree<Entry<K, V>>[] prevTable = table;
4
5      int NEWCAPACITY = nextPrime();
6      numKeys = 0;
7      table = new BinarySearchTree[NEWCAPACITY];
8
9      for (var bst : prevTable)
10     {
11         if (prevTable != null)
12         {
13             for (var element : bst)
14             {
15                 put(element.key, element.value);
16             }
17         }
18     }
19 }
```

```

1  @Override
2  public V put(K key, V value)
3  {
4      int index = key.hashCode() % table.length;
5
6      if (index < 0)
7          index += table.length;
8
9      if (table[index] == null)
10     {
11         // Create a new linked list at table[index].
12         table[index] = new BinarySearchTree<Entry<K,V>>();
13     }
14
15     // Search the list at table[index] to find the key.
16     for (Entry<K, V> nextItem : table[index])
17     {
18         // If the search is successful, replace the old value.
19         if (nextItem.getKey().equals(key))
20         {
21             // Replace value for this key.
22             V oldVal = nextItem.getValue();
23             nextItem.setValue(value);
24             return oldVal;
25         }
26     }
27
28     // assert: key is not in the table, add new item.
29     table[index].add(new Entry<>(key, value));
30     numKeys++;
31
32     if (numKeys > (LOAD_THRESHOLD * table.length))
33         rehash();
34
35     return null;
36 }

```

- Hash table searching complexity average = $O(\log n)$.
- Hash table searching complexity worst case = $O(n)$.
- Hash table searching complexity best case = $O(1)$.

--Example Merge Sort functions implementations

```
1 public static <T extends Comparable<T>> void sort(T[] table)
2 {
3     // A table with one element is sorted already.
4     if (table.length > 1)
5     {
6         // Split table into halves.
7         int halfSize = table.length / 2;
8         T[] leftTable = (T[]) new Comparable[halfSize];
9         T[] rightTable = (T[]) new Comparable[table.length - halfSize];
10        System.arraycopy(table, 0, leftTable, 0, halfSize);
11        System.arraycopy(table, halfSize, rightTable, 0, table.length - halfSize);
12        // Sort the halves.
13        sort(leftTable);
14        sort(rightTable);
15        // Merge the halves.
16        merge(table, leftTable, rightTable);
17    }
18 }
```

-- Merge Sort Average Complexity = $O(n \log n)$

-- Merge Sort Worst Case Complexity = $O(n \log n)$

-- Merge Sort Best Case Complexity = $O(n \log n)$

```
100 x 100
Merge Sort =5 ms
Quick Sort =7 ms
New Sort   =15 ms

100 x 1000
Merge Sort =49 ms
Quick Sort =14 ms
New Sort   =174 ms

100 x 10000
Merge Sort =165 ms
Quick Sort =107 ms
New Sort   =16405 ms
```

--Example Quick Sort functions implementations

```
1 private static <T extends Comparable<T>> void quickSort(T[] table, int first, int last) {
2     if (first < last) { // There is data to be sorted.
3         // Partition the table.
4         int pivIndex = partition(table, first, last);
5         // Sort the left half.
6         quickSort(table, first, pivIndex - 1);
7         // Sort the right half.
8         quickSort(table, pivIndex + 1, last);
9     }
10 }
```

- Quick Sort Average Complexity = $O(n \log n)$
- Quick Sort Worst Case Complexity = $O(n^2)$
- Quick Sort Best Case Complexity = $O(n \log n)$

```
100 x 100
Merge Sort =5 ms
Quick Sort =7 ms
New Sort   =15 ms

100 x 1000
Merge Sort =49 ms
Quick Sort =14 ms
New Sort   =174 ms

100 x 10000
Merge Sort =165 ms
Quick Sort =107 ms
New Sort   =16405 ms
```

-- Example Quick Sort functions implementations

```
1 private static <T extends Comparable<T>> T[] newSort(T[] table, int head, int tail)
2     {
3         if(head > tail)
4             return table;
5         else
6         {
7             Pair min_max = min_max_finder(table,head, tail);
8
9             swap(table, tail, min_max.max);
10            min_max = min_max_finder(table,head, tail);
11            swap(table, head, min_max.min);
12            return newSort(table, head+1,tail-1);
13        }
14    }
```

-- New Sort Average Complexity = $O(n^2)$
-- New Sort Worst Case Complexity = $O(n^2)$
-- New Sort Best Case Complexity = $O(n^2)$

```
100 x 100
Merge Sort =5 ms
Quick Sort =7 ms
New Sort   =15 ms

100 x 1000
Merge Sort =49 ms
Quick Sort =14 ms
New Sort   =174 ms

100 x 10000
Merge Sort =165 ms
Quick Sort =107 ms
New Sort   =16405 ms
```