

CSE 232 SPRING 2020
PROJECT 2

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Editing C Code:

We will implement following C code with our machine.

```
mult = 0;
while(a > 0){
    mult = mult + b;
    a = a - 1;
}
```

However, this C code is insufficient for negative numbers. Because I will also implement negative number multiplication. First, let's edit the code above.

```
if(a < 0){
    a = -a;
    b = -b;
}
mult = 0;
while(a > 0){
    mult = mult + b;
    a = a - 1;
}
```

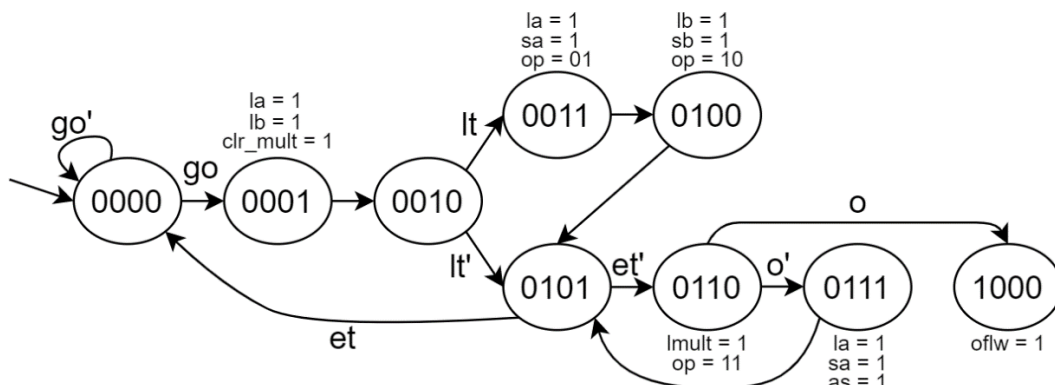
State Diagram

To simplify the diagram below, outputs that it's 0 are not shown in the diagram. And also the rst input is not shown in the diagram. If rst input is 1 in any state, state will be returned 0000.

- | | |
|---------------------------|---|
| - go = run (input) | - lb = load b (output) |
| - et = equal than (input) | - sb = select b (output) |
| - lt = less than (input) | - lmult = load mult (output) |
| - o = overflow (input) | - clr_mult = clear mult (output) |
| - rst = reset (input) | - op = operation (output) |
| - la = load a (output) | - as = addition or subtraction (output) |
| - sa = select a (output) | - oflw = overflow (output) |

Inputs: go,et,lt,o,rst

Outputs: la, sa, lb, sb, lmult, clr_mult
op, as, oflw



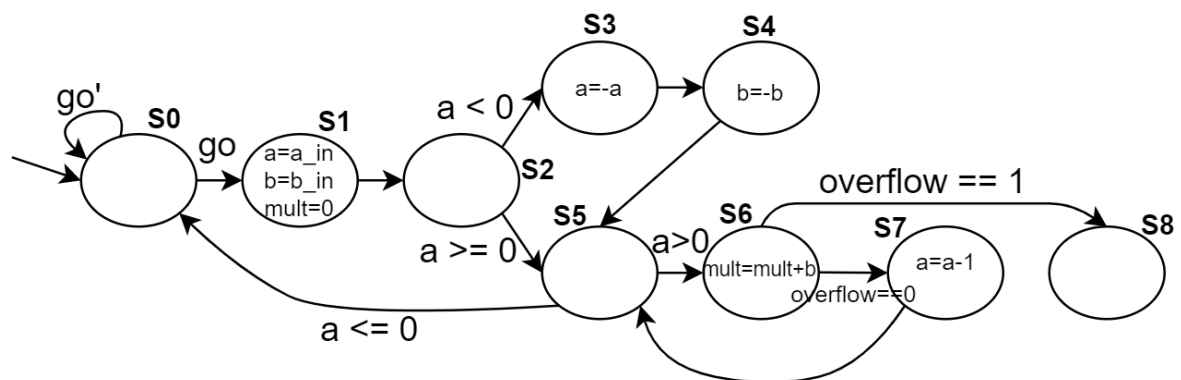
Draw Datapath

If rst input is 1 in any state, state will be returned S0 state. It is not drawn to simplify.

| Inputs | | Operation |
|--------|----|------------------|
| a | b | |
| >0 | >0 | Nothing |
| >0 | <0 | Nothing |
| <0 | >0 | $a = -a, b = -b$ |
| <0 | <0 | $a = -a, b = -b$ |

Inputs: go, a, b, rst

Outputs: mult



Draw Turth Table

[illegible]

Derive Boolean Expressions From The Truth Table

- n3 - when n3 output is 1

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 1 | 1 | 0 | X | X | X | 1 |
| 1 | 0 | 0 | 0 | X | X | X | X |

$$n3 = s3's2s1s0'o + s3s2's1's0'$$

- n2 - when n2 output is 1

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 0 | 1 | 0 | X | 0 | X | X |
| 0 | 0 | 1 | 1 | X | X | X | X |
| 0 | 1 | 0 | 0 | X | X | X | X |
| 0 | 1 | 0 | 1 | 0 | X | X | X |
| 0 | 1 | 1 | 0 | X | X | X | 0 |
| 0 | 1 | 1 | 1 | X | X | X | X |

$$n2 = s3's2's1s0'lt' + s3's2's1s0 + s3's2s1's0' + s3's2s1's0et' + s3's2s1s0'o' + s3's2s1s0$$

$$n2 = s3's2's1(s0'lt' + s0) + s3's2s1'(s0' + s0et') + s3's2s1(s0'o' + s0)$$

$$n2 = s3's2's1lt' + s3's2's1s0 + s3's2s1's0' + s3's2s1'et' + s3's2s1o' + s3's2s1s0$$

$$n2 = s3's2's1lt' + s3's1s0(s2' + s2) + s3's2s1's0' + s3's2s1'et' + s3's2s1o'$$

$$n2 = s3's2's1lt' + s3's1s0 + s3's2s1's0' + s3's2s1'et' + s3's2s1o'$$

- n1 - when n1 output is 1

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 0 | 0 | 1 | X | X | X | X |
| 0 | 0 | 1 | 0 | X | 1 | X | X |
| 0 | 1 | 0 | 1 | 0 | X | X | X |
| 0 | 1 | 1 | 0 | X | X | X | 0 |

$$n1 = s3's2's1's0 + s3's2's1s0'lt + s3's2s1's0et' + s3's2s1s0'o'$$

$$n1 = s3's1's0(s2' + s2et') + s3's2's1s0'lt + s3's2s1s0'o'$$

$$n1 = s3's2's1's0 + s3's1's0et' + s3's2's1s0'lt + s3's2s1s0'o'$$

- n0 - when n0 output is 1

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 0 | 0 | 0 | X | X | 1 | X |
| 0 | 0 | 1 | 0 | X | 0 | X | X |
| 0 | 0 | 1 | 0 | X | 1 | X | X |
| 0 | 1 | 0 | 0 | X | X | X | X |
| 0 | 1 | 1 | 0 | X | X | X | 0 |
| 0 | 1 | 1 | 1 | X | X | X | X |

$$n0 = s3's2's1's0'go + s3's2's1s0'lt' + s3's2's1s0'lt + s3's2s1's0' + s3's2s1s0'o' + s3's2s1s0$$

$$n0 = s3's1's0'(s2'go + s2) + s3's2's1s0'(lt' + lt) + s3's2s1s0'o' + s3's2s1s0$$

$$n0 = s3's1's0'go + s3's2s1's0' + s3's2's1s0' + s3's2s1s0'o' + s3's2s1s0$$

$$n0 = s3's1's0'go + s3's2s1's0' + s3's1s0'(s2' + s2o') + s3's2s1s0$$

$$n0 = s3's1's0'go + s3's2s1's0' + s3's2's1s0' + s3's1s0'o' + s3's2s1s0$$

- la - when la output is 1

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 0 | 0 | 1 | X | X | X | X |
| 0 | 0 | 1 | 1 | X | X | X | X |
| 0 | 1 | 1 | 1 | X | X | X | X |

$$la = s3's2's1's0 + s3's2's1s0 + s3's2s1s0$$

$$la = s3's2's0(s1' + s1) + s3's2s1s0$$

$$la = s3's2's0 + s3's2s1s0$$

$$la = s3's0(s2' + s2s1)$$

$$la = s3's0(s2' + s1)$$

- sa - when sa output is 1

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 0 | 1 | 1 | X | X | X | X |
| 0 | 1 | 1 | 1 | X | X | X | X |

$$sa = s3's2's1s0 + s3's2s1s0$$

$$sa = s3's1s0(s2' + s2)$$

$$sa = s3's1s0$$

- lb - when lb output is 1

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 0 | 0 | 1 | X | X | X | X |
| 0 | 1 | 0 | 0 | X | X | X | X |

$$lb = s3's2's1's0 + s3's2s1's0'$$

$$lb = s3's1'(s2's0 + s2s0')$$

$$lb = s3's1'(s2 \text{ XOR } s0)$$

- sb - when sb output is 1

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 1 | 0 | 0 | X | X | X | X |

$$sb = s3's2s1's0$$

- lmult - when lmult output is 1

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 1 | 1 | 0 | X | X | X | 0 |
| 0 | 1 | 1 | 0 | X | X | X | 1 |

$$\text{lmult} = s3's2s1s0'o' + s3's2s1s0'o$$

$$\text{lmult} = s3's2s1s0'(o' + o)$$

$$\text{lmult} = s3's2s1s0'$$

- clr_mult - when clr_mult output is 1

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 0 | 0 | 1 | X | X | X | X |

$$\text{clr_mult} = s3's2's1's0$$

- op - when any of the bits of op output are 1

0.bit

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 0 | 1 | 1 | X | X | X | X |
| 0 | 1 | 1 | 0 | X | X | X | 0 |
| 0 | 1 | 1 | 0 | X | X | X | 1 |

$$\text{op } 0.\text{bit} = s3's2's1s0 + s3's2s1s0'o' + s3's2s1s0'o$$

$$\text{op } 0.\text{bit} = s3's2's1s0 + s3's2s1s0'(o' + o)$$

$$\text{op } 0.\text{bit} = s3's2's1s0 + s3's2s1s0'$$

$$\text{op } 0.\text{bit} = s3's1(s2's0 + s2s0')$$

$$\text{op } 0.\text{bit} = s3's1(s2 \text{ XOR } s0)$$

1.bit

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 1 | 0 | 0 | X | X | X | X |
| 0 | 1 | 1 | 0 | X | X | X | 0 |
| 0 | 1 | 1 | 0 | X | X | X | 1 |

$$\text{op } 1.\text{bit} = s3's2s1's0' + s3's2s1s0'o' + s3's2s1s0'o$$

$$\text{op } 1.\text{bit} = s3's2s1's0' + s3's2s1s0'(o' + o)$$

$$\text{op } 1.\text{bit} = s3's2s1's0' + s3's2s1s0'$$

$$\text{op } 1.\text{bit} = s3's2s0'(s1' + s1)$$

$$\text{op } 1.\text{bit} = s3's2s0'$$

- as - when as output is 1

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 0 | 1 | 1 | 1 | X | X | X | X |

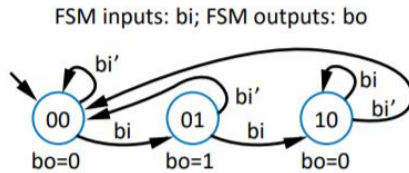
$$\text{as} = s3's2s1s0$$

- oflw - when oflw output is 1

| s3 | s2 | s1 | s0 | et | lt | go | o |
|----|----|----|----|----|----|----|---|
| 1 | 0 | 0 | 0 | X | X | X | X |

$$\text{oflw} = s3s2's1's0'$$

Button Press Synchronizer State Diagram



Button Press Synchronizer Truth Table and Boolean Expressions

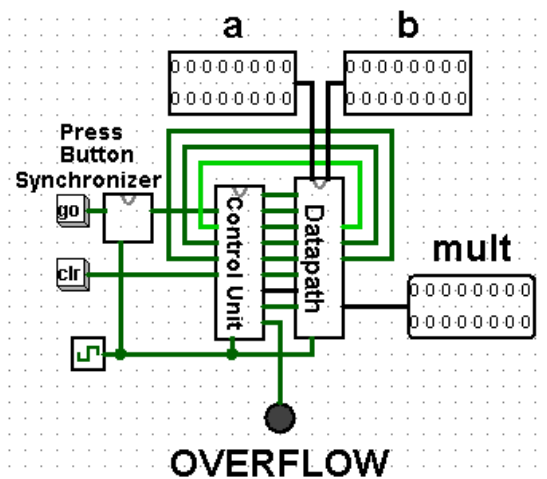
| Combinational logic | | | |
|---------------------|----|----|----------|
| Inputs | | | Outputs |
| s1 | s0 | bi | n1 n0 bo |
| 0 | 0 | 0 | 0 0 0 |
| 0 | 0 | 1 | 0 1 0 |
| 0 | 1 | 0 | 0 0 1 |
| 0 | 1 | 1 | 1 0 1 |
| 1 | 0 | 0 | 0 0 0 |
| 1 | 0 | 1 | 1 0 0 |
| 1 | 1 | 0 | 0 0 0 |
| 1 | 1 | 1 | 0 0 0 |

$$n1 = s1's0bi + s1s0'bi$$

$$n0 = s1's0'bi$$

$$bo = s1's0bi' + s1's0bi = s1's0(bi' + bi) = s1's0$$

Overview



Optimization

In some parts, I did not take any parenthesis because the critical path will increase, so I reduced the critical paths. Apart from that, I created an overflow state to prevent the process from continuing when there was overflow and prevented the process from continuing unnecessarily. I added a button press synchronizer to the go button of the user and no matter how long the user held it, I made the control unit work once.