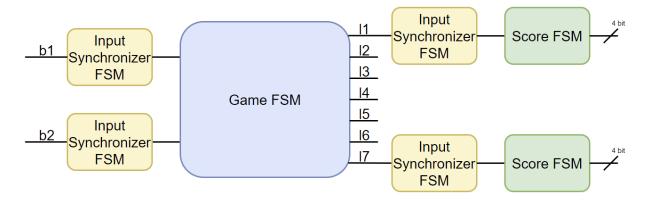
# CSE 232 SPRING 2020 PROJECT 1

## ABDULLAH CELIK 171044002

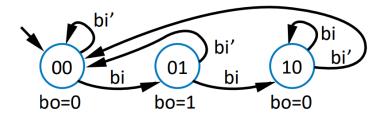
## **SYSTEM**



## **Input Synchronizer FSM**

#### **State Diagram**

FSM inputs: bi; FSM outputs: bo



#### **Truth Table**

|    | Inputs |    | (  | Dutput | S  |
|----|--------|----|----|--------|----|
| s1 | s0     | bi | n1 | n0     | bo |
| 0  | 0      | 0  | 0  | 0      | 0  |
| 0  | 0      | 1  | 0  | 1      | 0  |
| 0  | 1      | 0  | 0  | 0      | 1  |
| 0  | 1      | 1  | 1  | 0      | 1  |
| 1  | 0      | 0  | 0  | 0      | 0  |
| 1  | 0      | 1  | 1  | 0      | 0  |
| 1  | 1      | 0  | 0  | 0      | 0  |
| 1  | 1      | 1  | 0  | 0      | 0  |

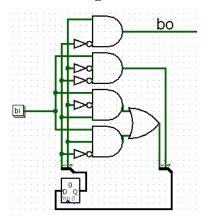
#### **Boolean Expressions**

$$n1 = s1$$
' $s0bi + s1s0$ ' $bi$ 

$$n0 = s1$$
's0'bi

$$bo = s1's0bi' + s1's0bi = s1's0$$

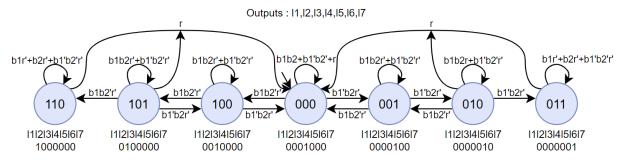
#### **Circuit on Logisim**



#### **Game FSM**

#### **State Diagram**

**Note :** Input b1 and b2 always output 1 clock timelength 1 output. Input synchronizer provides this. Inputs: b1,b2,r



**Truth Table** 

|           |    |               | G   | ame       | e C | oml | oina | tion | nal | Lo   | gic |    |    |           |    |
|-----------|----|---------------|-----|-----------|-----|-----|------|------|-----|------|-----|----|----|-----------|----|
|           |    | Inp           | uts |           |     |     |      |      | O   | utpu | ıts |    |    |           |    |
| <b>s2</b> | s1 | $\mathbf{s0}$ | b1  | <b>b2</b> | r   | n2  | n1   | n0   | 11  | 12   | 13  | 14 | 15 | <b>16</b> | 17 |
| 0         | 0  | 0             | 0   | 0         | 0   | 0   | 0    | 0    | 0   | 0    | 0   | 1  | 0  | 0         | 0  |
| 0         | 0  | 0             | 0   | 1         | 0   | 0   | 0    | 1    | 0   | 0    | 0   | 1  | 0  | 0         | 0  |
| 0         | 0  | 0             | 1   | 0         | 0   | 1   | 0    | 0    | 0   | 0    | 0   | 1  | 0  | 0         | 0  |
| 0         | 0  | 0             | 1   | 1         | 0   | 0   | 0    | 0    | 0   | 0    | 0   | 1  | 0  | 0         | 0  |
| 0         | 0  | 0             | X   | X         | 1   | 0   | 0    | 0    | 0   | 0    | 0   | 1  | 0  | 0         | 0  |
| 0         | 0  | 1             | 0   | 0         | 0   | 0   | 0    | 1    | 0   | 0    | 0   | 0  | 1  | 0         | 0  |
| 0         | 0  | 1             | 0   | 1         | 0   | 0   | 1    | 0    | 0   | 0    | 0   | 0  | 1  | 0         | 0  |
| 0         | 0  | 1             | 1   | 0         | 0   | 0   | 0    | 0    | 0   | 0    | 0   | 0  | 1  | 0         | 0  |
| 0         | 0  | 1             | 1   | 1         | 0   | 0   | 0    | 1    | 0   | 0    | 0   | 0  | 1  | 0         | 0  |
| 0         | 0  | 1             | X   | X         | 1   | 0   | 0    | 0    | 0   | 0    | 0   | 0  | 1  | 0         | 0  |
| 0         | 1  | 0             | 0   | 0         | 0   | 0   | 1    | 0    | 0   | 0    | 0   | 0  | 0  | 1         | 0  |
| 0         | 1  | 0             | 0   | 1         | 0   | 0   | 1    | 1    | 0   | 0    | 0   | 0  | 0  | 1         | 0  |
| 0         | 1  | 0             | 1   | 0         | 0   | 0   | 0    | 1    | 0   | 0    | 0   | 0  | 0  | 1         | 0  |
| 0         | 1  | 0             | 1   | 1         | 0   | 0   | 1    | 0    | 0   | 0    | 0   | 0  | 0  | 1         | 0  |
| 0         | 1  | 0             | X   | X         | 1   | 0   | 0    | 0    | 0   | 0    | 0   | 0  | 0  | 1         | 0  |
| 0         | 1  | 1             | X   | X         | 0   | 0   | 1    | 1    | 0   | 0    | 0   | 0  | 0  | 0         | 1  |

| 0 | 1 | 1 | X | X | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | X | X | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | X | X | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | X | X | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | X | X | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 1 | X | X | X | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

#### **Boolean Expressions**

- n2

|           | Wh     | en n2 o       | utput is  | s 1       |   |  |  |  |  |
|-----------|--------|---------------|-----------|-----------|---|--|--|--|--|
|           | Inputs |               |           |           |   |  |  |  |  |
| <b>s2</b> | s1     | $\mathbf{s0}$ | <b>b1</b> | <b>b2</b> | r |  |  |  |  |
| 0         | 0      | 0             | 1         | 0         | 0 |  |  |  |  |
| 1         | 0      | 0             | 0         | 0         | 0 |  |  |  |  |
| 1         | 0      | 0             | 1         | 0         | 0 |  |  |  |  |
| 1         | 0      | 0             | 1         | 1         | 0 |  |  |  |  |
| 1         | 0      | 1             | 0         | 0         | 0 |  |  |  |  |
| 1         | 0      | 1             | 0         | 1         | 0 |  |  |  |  |
| 1         | 0      | 1             | 1         | 0         | 0 |  |  |  |  |
| 1         | 0      | 1             | 1         | 1         | 0 |  |  |  |  |
| 1         | 1      | 0             | X         | X         | 0 |  |  |  |  |

After some logical algebra

|           | When n2 output is 1 |    |    |           |   |  |  |  |  |  |
|-----------|---------------------|----|----|-----------|---|--|--|--|--|--|
| Inputs    |                     |    |    |           |   |  |  |  |  |  |
| <b>s2</b> | s1                  | s0 | b1 | <b>b2</b> | r |  |  |  |  |  |
| 0         | 0                   | 0  | 1  | 0         | 0 |  |  |  |  |  |
| 1         | 0                   | 0  | X  | 0         | 0 |  |  |  |  |  |
| 1         | 0                   | 0  | 1  | 1         | 0 |  |  |  |  |  |
| 1         | 0                   | 1  | X  | X         | 0 |  |  |  |  |  |
| 1         | 1                   | 0  | X  | X         | 0 |  |  |  |  |  |

```
\begin{array}{l} n2 = s2's1's0'b1b2'r' + s2s1's0'b2'r' + s2s1's0'b1b2r + s2s1's0r' + s2s1s0'r' \\ n2 = s1's0'b2'r'(s2'b1 + s2) + s2s1's0'b1b2r + s2s1's0r' + s2s1s0'r' \\ n2 = s2s1's0'b2'r' + s1's0'b1b2'r' + s2s1's0'b1b2r + s2s1's0r' + s2s1s0'r' \\ n2 = s2s1's0'r'(b2' + b1b2) + s1's0'b1b2'r' + s2s1's0r' + s2s1s0'r' \\ n2 = s2s1'b1s0'r' + s2s1's0'b2'r' + s1's0'b1b2'r' + s2s1's0r' + s2s1s0'r' \\ n2 = s2s0'r'(s1'b1 + s1) + s2s1'r'(s0'b2' + s0) + s1's0'b1b2'r' \\ n2 = s2s1s0'r' + s2s0'b1r' + s2s1's0r' + s2s1'b2'r' + s1's0'b1b2'r' \\ \end{array}
```

- n1

|    | When n1 output is 1 |    |    |           |   |  |  |  |  |  |
|----|---------------------|----|----|-----------|---|--|--|--|--|--|
|    | Inputs              |    |    |           |   |  |  |  |  |  |
| s2 | s1                  | s0 | b1 | <b>b2</b> | r |  |  |  |  |  |
| 0  | 0                   | 1  | 0  | 1         | 0 |  |  |  |  |  |
| 0  | 1                   | 0  | 0  | 0         | 0 |  |  |  |  |  |
| 0  | 1                   | 0  | 0  | 1         | 0 |  |  |  |  |  |
| 0  | 1                   | 0  | 1  | 1         | 0 |  |  |  |  |  |
| 0  | 1                   | 1  | X  | X         | 0 |  |  |  |  |  |
| 1  | 0                   | 1  | 1  | 0         | 0 |  |  |  |  |  |
| 1  | 1                   | 0  | X  | X         | 0 |  |  |  |  |  |

|           | Wh     | en n1 c | output is | 1         |   |  |  |  |
|-----------|--------|---------|-----------|-----------|---|--|--|--|
|           | Inputs |         |           |           |   |  |  |  |
| <b>s2</b> | s1     | s0      | b1        | <b>b2</b> | r |  |  |  |
| 0         | 0      | 1       | 0         | 1         | 0 |  |  |  |
| 0         | 1      | 0       | 0         | 0         | 0 |  |  |  |
| 0         | 1      | 0       | X         | 1         | 0 |  |  |  |
| 0         | 1      | 1       | X         | X         | 0 |  |  |  |
| 1         | 0      | 1       | 1         | 0         | 0 |  |  |  |
| 1         | 1      | 0       | X         | X         | 0 |  |  |  |

```
\begin{array}{l} n1 = s2's1's0b1'b2r' + s2's1s0'b1'b2'r' + s2's1s0'b2r' + s2's1s0r' + s2s1's0b1b2'r' + \\ s2s1s0'r' \\ n1 = s2's1's0b1'b2r' + s2's1s0'r'(b1'b2' + b2) + s2's1s0r' + s2s1's0b1b2'r' + s2s1s0'r' \\ n1 = s2's1's0b1'b2r' + s2's1s0'b1'r' + s2's1s0'b2r' + s2's1s0r' + s2s1's0b1b2'r' + s2s1s0'r' \\ n1 = s2's0r'(s1'b1'b2 + s1) + s1s0'r'(s2'b1' + s2) + s2's1s0'b2r' + s2s1's0b1b2'r' \\ n1 = s2's0b1'b2r' + s2's1s0r' + s2s1s0'r' + s1s0'b1'r' + s2's1s0'b2r' + s2s1's0b1b2'r' \\ n1 = s2's0b1'b2r' + s2's1r'(s0 + s0'b2) + s2s1s0'r' + s1s0'b1'r' + s2s1's0b1b2'r' \\ n1 = s2's0b1'b2r' + s2's1s0r' + s2's1b2r' + s2s1s0'r' + s1s0'b1'r' + s2s1's0b1b2'r' \\ \end{array}
```

- n0

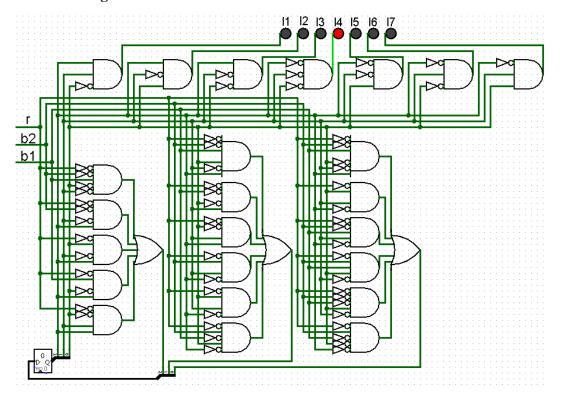
|           | Wh     | en n0 c | output is | s 1       |   |  |  |  |  |  |
|-----------|--------|---------|-----------|-----------|---|--|--|--|--|--|
|           | Inputs |         |           |           |   |  |  |  |  |  |
| <b>s2</b> | s1     | s0      | <b>b1</b> | <b>b2</b> | r |  |  |  |  |  |
| 0         | 0      | 0       | 0         | 1         | 0 |  |  |  |  |  |
| 0         | 0      | 1       | 0         | 0         | 0 |  |  |  |  |  |
| 0         | 0      | 1       | 1         | 1         | 0 |  |  |  |  |  |
| 0         | 1      | 0       | 0         | 1         | 0 |  |  |  |  |  |
| 0         | 1      | 0       | 1         | 0         | 0 |  |  |  |  |  |
| 0         | 1      | 1       | X         | X         | 0 |  |  |  |  |  |
| 1         | 0      | 0       | 1         | 0         | 0 |  |  |  |  |  |
| 1         | 0      | 1       | 0         | 0         | 0 |  |  |  |  |  |
| 1         | 0      | 1       | 1         | 1         | 0 |  |  |  |  |  |

|           | When n0 output is 1 |   |   |   |   |  |  |  |  |  |  |
|-----------|---------------------|---|---|---|---|--|--|--|--|--|--|
|           | Inputs              |   |   |   |   |  |  |  |  |  |  |
| <b>s2</b> | s2 s1 s0 b1 b2 r    |   |   |   |   |  |  |  |  |  |  |
| 0         | X                   | 0 | 0 | 1 | 0 |  |  |  |  |  |  |
| X         | 0                   | 1 | 0 | 0 | 0 |  |  |  |  |  |  |
| X         | 0                   | 1 | 1 | 1 | 0 |  |  |  |  |  |  |
| 0         | 1                   | 0 | 1 | 0 | 0 |  |  |  |  |  |  |
| 0         | 1                   | 1 | X | X | 0 |  |  |  |  |  |  |
| 1         | 0                   | 0 | 1 | 0 | 0 |  |  |  |  |  |  |

```
n0 = s2's0'b1'b2r' + s1's0b1'b2'r' + s1's0b1b2r' + s2's1s0'b1b2'r' + s2's1s0r' + s2s1's0'b1b2'r'
n0 = s2's0'b1'b2r' + s1's0b1'b2'r' + s1's0b1b2r' + s2's1r'(s0'b1b2' + s0) + s2s1's0'b1b2'r'
n0 = s2's0'b1'b2r' + s1's0b1'b2'r' + s1's0b1b2r' + s2's1b1b2'r' + s2's1s0r' + s2s1's0'b1b2'r'
```

- -11 = s2s1s0
- -12 = s2s1's0
- -13 = s2s1's0'
- 14 = s2's1's0'
- -15 = s2's1's0
- 16 = s2's1s0' - 17 = s2's1s0

#### **Circuit on Logisim**

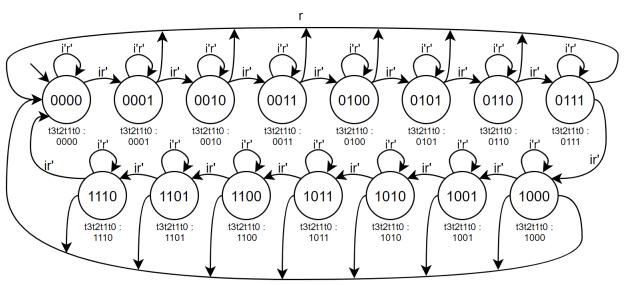


#### **Score FSM**

#### **State Diagram**

**Note:** Input i always output 1 clock timelength 1 output. Input synchronizer provides this.

Inputs: i,r Outputs: t3,t2,t1,t0



**Truth Table** 

| So | core | e Co | mb         | ina | ati | ona     | al L | лоg | ic |
|----|------|------|------------|-----|-----|---------|------|-----|----|
|    |      | Inpu | its        |     |     | Outputs |      |     |    |
| р3 | p2   | p1   | <b>p</b> 0 | i   | r   | t3      | t2   | t1  | t0 |
| 0  | 0    | 0    | 0          | 0   | 0   | 0       | 0    | 0   | 0  |
| 0  | 0    | 0    | 0          | 1   | 0   | 0       | 0    | 0   | 1  |
| 0  | 0    | 0    | 1          | 0   | 0   | 0       | 0    | 0   | 1  |
| 0  | 0    | 0    | 1          | 1   | 0   | 0       | 0    | 1   | 0  |
| 0  | 0    | 1    | 0          | 0   | 0   | 0       | 0    | 1   | 0  |
| 0  | 0    | 1    | 0          | 1   | 0   | 0       | 0    | 1   | 1  |
| 0  | 0    | 1    | 1          | 0   | 0   | 0       | 0    | 1   | 1  |
| 0  | 0    | 1    | 1          | 1   | 0   | 0       | 1    | 0   | 0  |
| 0  | 1    | 0    | 0          | 0   | 0   | 0       | 1    | 0   | 0  |
| 0  | 1    | 0    | 0          | 1   | 0   | 0       | 1    | 0   | 1  |
| 0  | 1    | 0    | 1          | 0   | 0   | 0       | 1    | 0   | 1  |
| 0  | 1    | 0    | 1          | 1   | 0   | 0       | 1    | 1   | 0  |
| 0  | 1    | 1    | 0          | 0   | 0   | 0       | 1    | 1   | 0  |
| 0  | 1    | 1    | 0          | 1   | 0   | 0       | 1    | 1   | 1  |
| 0  | 1    | 1    | 1          | 0   | 0   | 0       | 1    | 1   | 1  |
| 0  | 1    | 1    | 1          | 1   | 0   | 1       | 0    | 0   | 0  |
| 1  | 0    | 0    | 0          | 0   | 0   | 1       | 0    | 0   | 0  |
| 1  | 0    | 0    | 0          | 1   | 0   | 1       | 0    | 0   | 1  |
| 1  | 0    | 0    | 1          | 0   | 0   | 1       | 0    | 0   | 1  |
| 1  | 0    | 0    | 1          | 1   | 0   | 1       | 0    | 1   | 0  |
| 1  | 0    | 1    | 0          | 0   | 0   | 1       | 0    | 1   | 0  |
| 1  | 0    | 1    | 0          | 1   | 0   | 1       | 0    | 1   | 1  |
| 1  | 0    | 1    | 1          | 0   | 0   | 1       | 0    | 1   | 1  |
| 1  | 0    | 1    | 1          | 1   | 0   | 1       | 1    | 0   | 0  |
| 1  | 1    | 0    | 0          | 0   | 0   | 1       | 1    | 0   | 0  |
| 1  | 1    | 0    | 0          | 1   | 0   | 1       | 1    | 0   | 1  |
| 1  | 1    | 0    | 1          | 0   | 0   | 1       | 1    | 0   | 1  |
| 1  | 1    | 0    | 1          | 1   | 0   | 1       | 1    | 1   | 0  |
| 1  | 1    | 1    | 0          | 0   | 0   | 1       | 1    | 1   | 0  |
| 1  | 1    | 1    | 0          | 1   | 0   | 1       | 1    | 1   | 1  |
| 1  | 1    | 1    | 1          | 0   | 0   | 1       | 1    | 1   | 1  |
| 1  | 1    | 1    | 1          | 1   | 0   | 0       | 0    | 0   | 0  |
| X  | X    | X    | X          | X   | 1   | 0       | 0    | 0   | 0  |

#### **Boolean Expressions**

- t3

|    | When | t3 outp   | uts is 1  | Į. |   |
|----|------|-----------|-----------|----|---|
|    |      | Inputs    |           |    |   |
| р3 | p2   | <b>p1</b> | <b>p0</b> | i  | r   |
| 0  | 1    | 1         | 1         | 1  | 0   |
| 1  | 0    | 0         | 0         | 0  | 0   |
| 1  | 0    | 0         | 0         | 1  | 0   |
| 1  | 0    | 0         | 1         | 0  | 0   |
| 1  | 0    | 0         | 1         | 1  | 0   |
| 1  | 0    | 1         | 0         | 0  | 0   |
| 1  | 0    | 1         | 0         | 1  | 0   |
| 1  | 0    | 1         | 1         | 0  | 0   |
| 1  | 0    | 1         | 1         | 1  | 0   |
| 1  | 1    | 0         | 0         | 0  | 0   |
| 1  | 1    | 0         | 0         | 1  | 0   |
| 1  | 1    | 0         | 1         | 0  | 0   |
| 1  | 1    | 0         | 1         | 1  | 0<br>0<br>0<br>0<br>0<br>0<br>0<br>0<br>0 |
| 1  | 1    | 1         | 0         | 0  | 0   |
| 1  | 1    | 1         | 0         | 1  | 0   |
| 1  | 1    | 1         | 1         | 0  | 0   |

|    | When      | t3 outp   | uts is    | 1 |   |  |  |  |  |  |
|----|-----------|-----------|-----------|---|---|--|--|--|--|--|
|    | Inputs    |           |           |   |   |  |  |  |  |  |
| р3 | <b>p2</b> | <b>p1</b> | <b>p0</b> | i | r |  |  |  |  |  |
| 0  | 1         | 1         | 1         | 1 | 0 |  |  |  |  |  |
| 1  | X         | X         | 0         | X | 0 |  |  |  |  |  |
| 1  | X         | X         | 1         | 0 | 0 |  |  |  |  |  |
| 1  | 0         | X         | 1         | 1 | 0 |  |  |  |  |  |
| 1  | 1         | 0         | 1         | 1 | 0 |  |  |  |  |  |

```
t3 = p3'p2p1p0ir2' + p3p0'r2' + p3p0i'r2' + p3p2'p0ir2' + p3p2p1'p0ir2'
t3 = p3'p2p1p0ir2' + p3r2'(p0' + p2'p0i) + p3p0r2'(i' + p2p1'i)
t3 = p3'p2p1p0ir2' + p3p0'r2' + p3p2'ir2' + p3p0i'r2' + p3p2p1'p0r2'
t3 = p3'p2p1p0ir2' + p3r2'(p0' + p2p1'p0) + p3p2'ir2' + p3p0i'r2'
t3 = p3'p2p1p0ir2' + p3p0'r2' + p3p2p1'r2' + p3p2'ir2' + p3p0i'r2'
t3 = p3'p2p1p0ir2' + p3p0'r2' + p3p2p1'r2' + p3p2'ir2' + p3p0i'r2'
t3 = p3'p2p1p0ir2' + p3r2'(p0' + p0i') + p3p2p1'r2' + p3p2'ir2'
t3 = p3'p2p1p0ir2' + p3p0'r2' + p3i'r2' + p3p2p1'r2' + p3p2'ir2'
t3 = p3'p2p1p0ir2' + p3p0'r2' + p3r2'(i' + p2'i) + p3p2p1'r2'
t3 = p3'p2p1p0ir2' + p3p0'r2' + p3i'r2' + p3p2'r2' + p3p2p1'r2'
t3 = p3'p2p1p0ir2' + p3p0'r2' + p3i'r2' + p3p2'r2' + p3p2p1'r2'
t3 = p3'p2p1p0ir2' + p3p0'r2' + p3i'r2' + p3p2'r2' + p3p2p1'r2'
t3 = p3'p2p1p0ir2' + p3p0'r2' + p3i'r2' + p3p2'r2' + p3p1'r2'
```

After some logical algebra

- t2

| When t2 outputs is 1 |           |           |            |   |   |
|----------------------|-----------|-----------|------------|---|---|
|                      | Inputs    |           |            |   |   |
| р3                   | <b>p2</b> | <b>p1</b> | <b>p</b> 0 | i | r |
| 0                    | 0         | 1         | 1          | 1 | 0 |
| 0                    | 1         | 0         | 0          | 0 | 0 |
| 0                    | 1         | 0         | 0          | 1 | 0 |
| 0                    | 1         | 0         | 1          | 0 | 0 |
| 0                    | 1         | 0         | 1          | 1 | 0 |
| 0                    | 1         | 1         | 0          | 0 | 0 |
| 0                    | 1         | 1         | 0          | 1 | 0 |
| 0                    | 1         | 1         | 1          | 0 | 0 |
| 1                    | 0         | 1         | 1          | 1 | 0 |
| 1                    | 1         | 0         | 0          | 0 | 0 |
| 1                    | 1         | 0         | 0          | 1 | 0 |
| 1                    | 1         | 0         | 1          | 0 | 0 |
| 1                    | 1         | 0         | 1          | 1 | 0 |

|    | When t2 outputs is 1 |           |           |   |   |  |
|----|----------------------|-----------|-----------|---|---|--|
|    |                      | Inputs    | S         |   |   |  |
| р3 | p2                   | <b>p1</b> | <b>p0</b> | i | r |  |
| X  | 0                    | 1         | 1         | 1 | 0 |  |
| X  | 1                    | X         | 0         | X | 0 |  |
| X  | 1                    | X         | 1         | 0 | 0 |  |
| X  | 1                    | 0         | 1         | 1 | 0 |  |

```
t2 = p2'p1p0ir2' + p2p0'r2' + p2p0i'r2' + p2p1'p0ir2'

t2 = p2'p1p0ir2' + p2p0'r2' + p2p0r2'(i' + p1'i)

t2 = p2'p1p0ir2' + p2p0'r2' + p2p0i'r2' + p2p1'p0r2'

t2 = p2'p1p0ir2' + p2r2'(p0' + p0i') + p2p1'p0r2'

t2 = p2'p1p0ir2' + p2p0'r2' + p2i'r2' + p2p1'p0r2'

t2 = p2'p1p0ir2' + p2r2'(p0' + p1'p0) + p2i'r2'

t2 = p2'p1p0ir2' + p2p0'r2' + p2p1'r2' + p2i'r2'

t2 = p2'p1p0ir2' + p2p0'r2' + p2p1'r2' + p2i'r2'
```

- t1

|                  | When      | t1 outp   | uts is 1  |   |   |
|------------------|-----------|-----------|-----------|---|---|
|                  |           | Inputs    |           |   |   |
| р3               | <b>p2</b> | <b>p1</b> | <b>p0</b> | i | r |
| 0                | 0         | 0         | 1         | 1 | 0 |
| 0                | 0         | 1         | 0         | 0 | 0 |
| 0<br>0<br>0      | 0         | 1         | 0         | 1 | 0 |
| 0                | 0         | 1         | 1         | 0 | 0 |
| 0<br>0<br>0<br>0 | 1         | 0         | 1         | 1 | 0 |
| 0                | 1         | 1         | 0         | 0 | 0 |
| 0                | 1         | 1         | 0         | 1 | 0 |
| 0                | 1         | 1         | 1         | 0 | 0 |
| 1                | 0         | 0         | 1         | 1 | 0 |
| 1                | 0         | 1         | 0         | 0 | 0 |
| 1                | 0         | 1         | 0         | 1 | 0 |
| 1                | 0         | 1         | 1         | 0 | 0 |
| 1                | 1         | 0         | 1         | 1 | 0 |
| 1                | 1         | 1         | 0         | 0 | 0 |
| 1                | 1         | 1         | 0         | 1 | 0 |
| 1                | 1         | 1         | 1         | 0 | 0 |

After some logical algebra

|   |    | When      | t1 out    | outs is   | 1 |   |
|---|----|-----------|-----------|-----------|---|---|
|   |    |           | Input     | S         |   |   |
|   | р3 | <b>p2</b> | <b>p1</b> | <b>p0</b> | i | r |
| ı | X  | X         | 0         | 1         | 1 | 0 |
|   | X  | X         | 1         | 0         | X | 0 |
|   | X  | X         | 1         | 1         | 0 | 0 |

```
t1 = p1'p0ir2' + p1p0'r2' + p1p0i'r2'
t1 = p1'p0ir2' + p1r2'(p0' + p0i')
t1 = p1'p0ir2' + p1p0'r2' + p1i'r2'
```

- t0

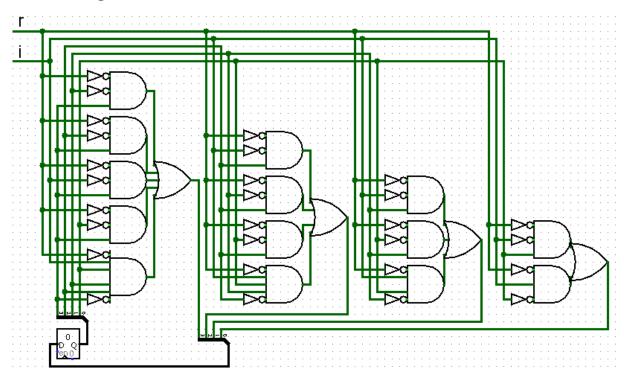
|    | When      | t0 outp   | uts is 1  |   |   |
|----|-----------|-----------|-----------|---|---|
|    |           | Inputs    |           |   |   |
| р3 | <b>p2</b> | <b>p1</b> | <b>p0</b> | i | r |
| 0  | 0         | 0         | 0         | 1 | 0 |
| 0  | 0         | 0         | 1         | 0 | 0 |
| 0  | 0         | 1         | 0         | 1 | 0 |
| 0  | 0         | 1         | 1         | 0 | 0 |
| 0  | 1         | 0         | 0         | 1 | 0 |
| 0  | 1         | 0         | 1         | 0 | 0 |
| 0  | 1         | 1         | 0         | 1 | 0 |
| 0  | 1         | 1         | 1         | 0 | 0 |
| 1  | 0         | 0         | 0         | 1 | 0 |
| 1  | 0         | 0         | 1         | 0 | 0 |

|    | wnen      | to outp   | uts is I   | L |   |
|----|-----------|-----------|------------|---|---|
|    |           | Inputs    |            |   |   |
| р3 | <b>p2</b> | <b>p1</b> | <b>p</b> 0 | i | r |
| X  | X         | X         | 0          | 1 | 0 |
| X  | X         | X         | 1          | 0 | 0 |

| 1 | 0 | 1 | 0 | 1 | 0 |
|---|---|---|---|---|---|
| 1 | 0 | 1 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 | 0 | 0 |
| 1 | 1 | 1 | 0 | 1 | 0 |
| 1 | 1 | 1 | 1 | 0 | 0 |

$$t0 = p0$$
'ir2' +  $p0$ i'r2'

## **Circuit on Logisim**



## **System Simulate Results**

| Scenerio  | Expected Result  | Actual<br>Result | Pass/Fail |
|---|--|------------------|-----------|
| When stage is 000, just press b1 button   | Successfully went next<br>stage(stage 100 is next<br>stage for button b1)              | As expected      | Pass      |
| When stage is 000, just press b2 button   | Successfully went next<br>stage(stage 001 is next<br>stage for button b2)              | As expected      | Pass      |
| When stage is 000, just<br>press b1 and b2 buttons<br>or don't press any<br>buttons | Successfully kept<br>current stage   | As expected      | Pass      |
| When stage is 001, just press b1 button   | Successfully turned<br>previous stage(stage 000<br>is previous stage for<br>button b1) | As expected      | Pass      |

| When stage is 001, just press b2 button   | Successfully went next<br>stage(stage 010 is next<br>stage for button b2)     | As expected | Pass |
|---|---|-------------|------|
| When stage is 001, just<br>press b1 and b2 buttons<br>or don't press any<br>buttons       | Successfully kept<br>current stage  | As expected | Pass |
| When stage is 010, just press b1 button   | Successfully turned previous stage(stage 001 is previous stage for button b1) | As expected | Pass |
| When stage is 010, just press b2 button   | Successfully went next<br>stage(stage 011 is next<br>stage for button b2)     | As expected | Pass |
| When stage is 001, just<br>press b1 and b2 buttons<br>or don't press any<br>buttons       | Successfully kept<br>current stage  | As expected | Pass |
| When stage is 011,<br>press button b1 or press<br>button b2 or press b1<br>and b2 buttons | Successfully kept<br>current stage  | As expected | Pass |
| When stage is 100, just press button b1   | Successfully went next<br>stage(stage 101 is next<br>stage for button b1)     | As expected | Pass |
| When stage is 100, just press button b2   | Successfully turned previous stage(stage 000 is previous stage for button b2) | As expected | Pass |
| When stage is 100, just<br>press b1 and b2 buttons<br>or don't press any<br>buttons       | Successfully kept<br>current stage  | As expected | Pass |
| When stage is 101, just press button b1   | Successfully went next<br>stage(stage 110 is next<br>stage for button b1)     | As expected | Pass |
| When stage is 101, just press button b2   | Successfully turned previous stage(stage 100 is previous stage for button b2) | As expected | Pass |
| When stage is 101, just press b1 and b2 buttons or don't press any buttons                | Successfully kept<br>current stage  | As expected | Pass |

| When stage is 110, press button b1 or press button b2 or press b1 and b2 buttons          | Successfully kept<br>current stage | As expected | Pass |
|---|------------------------------------|-------------|------|
| When stage is any stage, press the r button regardless of the status of the other buttons | Successfully turned 000 stage      | As expected | Pass |
| When stage is 011, scoreboard increased.  | Succeesfully increased             | As expected | Pass |
| When stage is 110, scoreboard increased.  | Succeesfully increased             | As expected | Pass |
| When press reset button of scoreboard   | Successfully reseted               | As expected | Pass |