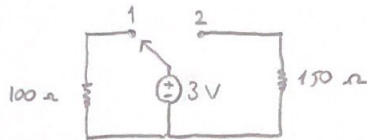


1. Question 2.4

(a) Calculate current i in Figure when the switch is in position 1.

(b) Find the current when the switch is in position 2.



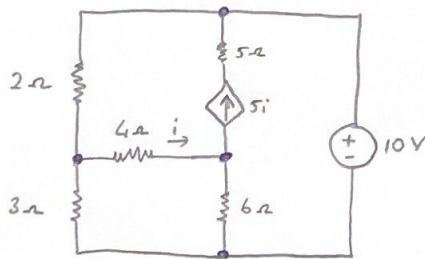
Solution:

a) $V = I \cdot R$ then $3V = I \cdot 100\ \Omega \Rightarrow I = 0.03\ A$

b) $3V = I \cdot 150\ \Omega \Rightarrow I = 0.02\ A$

2. Question 2.7

Determine the number of branches and nodes in the circuit in Figure.



Solution:

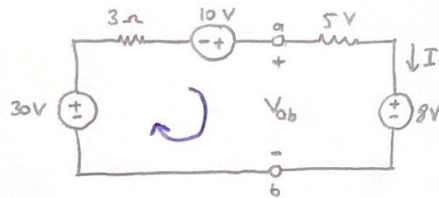
There are 4 nodes. The nodes are colored blue above.

The circuit above has 7 elements. Thus, it has seven branches.

- 2 Ω resistor
- 3 Ω resistor
- 4 Ω resistor
- 5 Ω resistor
- 6 Ω resistor
- 5A current source
- 10V voltage source

3. Question 2.15

Find I and V_{ab} in the circuit of figure.



Solution:

The cycle is colored blue above. Then equation

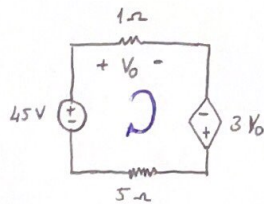
$$-30V + 3I - 10V + 5 \cdot I + 8V = 0$$

$$8I = 32V \Rightarrow I = 4A$$

$$V_{ab} = 5 \cdot 4 + 8V = 28V$$

4. Question 2.18

Calculate the power dissipated in the 5Ω resistor in the circuit of figure



Solution:

The cycle is colored blue above. Then equation

$$-45V + V_0 - 3V_0 + 5 \cdot I = 0, \quad V_0 = I \cdot 1\Omega$$

$$45V = 3V_0$$

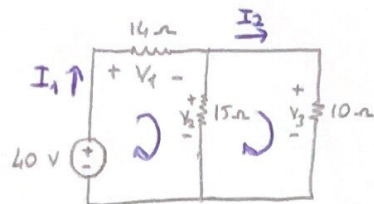
$$V_0 = 15V$$

$$I = 15A$$

$$P = I^2 \cdot R = 15^2 \cdot 5 = 1125W$$

5. Question 2.24

Find V_1 , V_2 and V_3 in the circuit in Figure.



Solution:

The cycles and currents are colored blue. So equations

$$-40V + 14 \cdot I_1 + 15 \cdot (I_1 - I_2) = 0$$

$$\textcircled{1} \quad 29I_1 - 15I_2 = 40$$

$$10 \cdot I_2 + 15 \cdot (I_2 - I_1) = 0$$

$$\textcircled{2} \quad -15I_1 + 25I_2 = 0$$

$$I_2 = \frac{3}{5} I_1$$

replace equation 1

$$29I_1 - 15 \cdot \frac{3}{5} I_1 = 40 \Rightarrow I_1 = 2A, \quad I_2 = \frac{6}{5}A$$

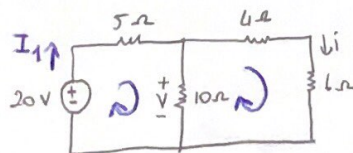
$$V_1 = 14 \cdot I_1 = 14 \cdot 2 = 28V$$

$$V_2 = 15 \cdot (I_1 - I_2) = 15 \cdot (2 - \frac{6}{5}) = 12V$$

$$V_3 = 10 \cdot I_2 = 10 \cdot \frac{6}{5} = 12V$$

6. Question 2.27

In the circuit in Figure, find V_i , and the power absorbed by the 4Ω resistor.



Solution:

The cycles and I_1 are colored blue in Figure. So equations

$$-20 + 5I_1 + 10 \cdot (I_1 - i) = 0$$

$$15I_1 - 10i = 20$$

$$\textcircled{1} \quad 3I_1 - 2i = 4$$

$$4i + 6i + 10 \cdot (i - I_1) = 0$$

$$\textcircled{2} \quad -10I_1 + 20i = 0$$

$$I_1 = 2i$$

use in equation 1

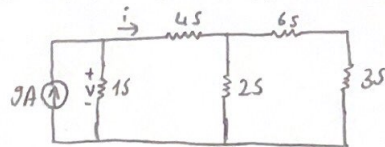
$$3 \cdot 2i - 2i = 4 \Rightarrow i = 1A, I_1 = 2A$$

$$V = 10 \cdot (I_1 - i) = 10 \cdot (2 - 1) = 10V$$

$$\text{Power absorbed by } 4\Omega \text{ resistor is } P = I^2 \cdot R = 1^2 \cdot 4 = 4W$$

7. Question 2.29

Obtain V and i in the circuit in Figure



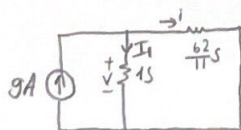
Solution:

Let's simplify the circuit. 6 ohm and 3 ohm resistors are series. Then equivalent and 25 resistors are parallel. Then equivalent and 4 ohm resistors are series.

$$6S + 3S = 9S$$

$$\frac{1}{R_{eq}} = \frac{1}{9S} + \frac{1}{25} \Rightarrow R_{eq} = \frac{18}{11} S$$

$$\frac{18}{11} S + 4S = \frac{62}{11} S \quad \text{The circuit}$$

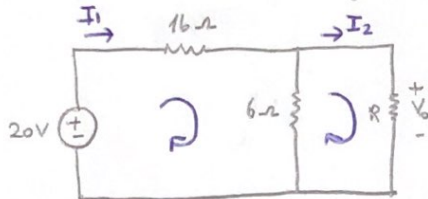


$$\begin{aligned} I_1 \cdot 15 &= i \cdot \frac{62}{11} \\ \textcircled{1} \quad I_1 &= \frac{62}{11} i \end{aligned} \quad \left. \begin{aligned} 9A &= I_1 + i \\ 9A &= \frac{62}{11} i + i \\ i &= 1.35 A \end{aligned} \right\}$$

$$V = 15 \cdot 1 = 15V$$

8. Question 2.33

In the circuit of Figure, find R if $V_0 = 4V$



Solution:

The cycles and currents are colored blue above so, equations

$$-20V + 16I_1 + 6 \cdot (I_1 - I_2) = 0$$

$$22I_1 - 6I_2 = 20$$

$$\textcircled{1} \quad 11I_1 - 3I_2 = 10$$

$$4V + 6 \cdot (I_2 - I_1) = 0$$

$$-6I_1 + 6I_2 = -4$$

$$\textcircled{2} \quad -3I_1 + 3I_2 = -2$$

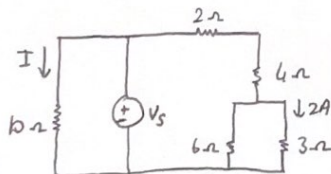
Add equation 1 and 2, then

$$8I_1 = 8 \Rightarrow I_1 = 1A, \quad I_2 = \frac{1}{3}A$$

$$I_2 \cdot R = 4V \Rightarrow R = 12\Omega$$

9. Question 2.34

Find I and V_S in the circuit of Figure if the current through the 3Ω resistor is $2A$

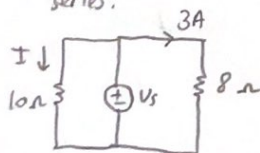


Solution:

6Ω branch and 3Ω branch voltages are should be equal.

$3 \cdot 2A = 6 \cdot I \Rightarrow I = 1A$, So the total voltage $3A$ on the 4Ω branch.

Then let's simplify circuit. 6Ω and 3Ω are parallel then 4Ω and 2Ω are series.



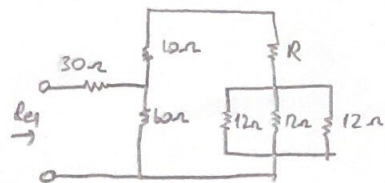
$$8 \cdot 3A = 10 \cdot I$$

$$I = 2.4A$$

$$V_S = \left(\frac{1}{6} + \frac{1}{8} \right)^{-1} \cdot 5.4 = 24V$$

10. Question 2.37

If $R_{eq} = 50 \Omega$ in the circuit in Figure, find R



Solution:

12 Ω resistors are parallel. The equivalent, R and 10 Ω resistors are series. Then equivalent and 60 Ω resistor are parallel. And last equivalent and 30 Ω resistor are series and the equivalent is 50 Ω .

$$1. \quad \frac{1}{R_{eq}} = \frac{1}{12} + \frac{1}{12} + \frac{1}{12} \Rightarrow R_{eq} = 4 \Omega$$

$$2. \quad 10 + R + 4 = 14 + R$$

$$3. \quad \frac{1}{R_{eq}} = \frac{1}{14+R} + \frac{1}{60} \Rightarrow R_{eq} = \left(\frac{1}{14+R} + \frac{1}{60} \right)^{-1}$$

$$4. \quad 30 + \left(\frac{1}{14+R} + \frac{1}{60} \right)^{-1} = 50$$

$$\left(\frac{1}{14+R} + \frac{1}{60} \right)^{-1} = 20$$

$$\frac{1}{14+R} + \frac{1}{60} = \frac{1}{20} \Rightarrow \frac{1}{14+R} = \frac{1}{30} \Rightarrow 14+R = 30$$

$$R = 16 \Omega$$