

SWITCHING OVERVIEW

GENERAL AGENDA 1/2

- ▶ Introduction : Justification, quick history, main components ..
- ▶ Input output
- ▶ Transport, TDM technologie
- ▶ Switching matrix
- ▶ Signaling
- ▶ CPU
- ▶ Intelligent peripherals
- ▶ Traffic calculation

GENERAL AGENDA 2/2



Conclusion



Questions

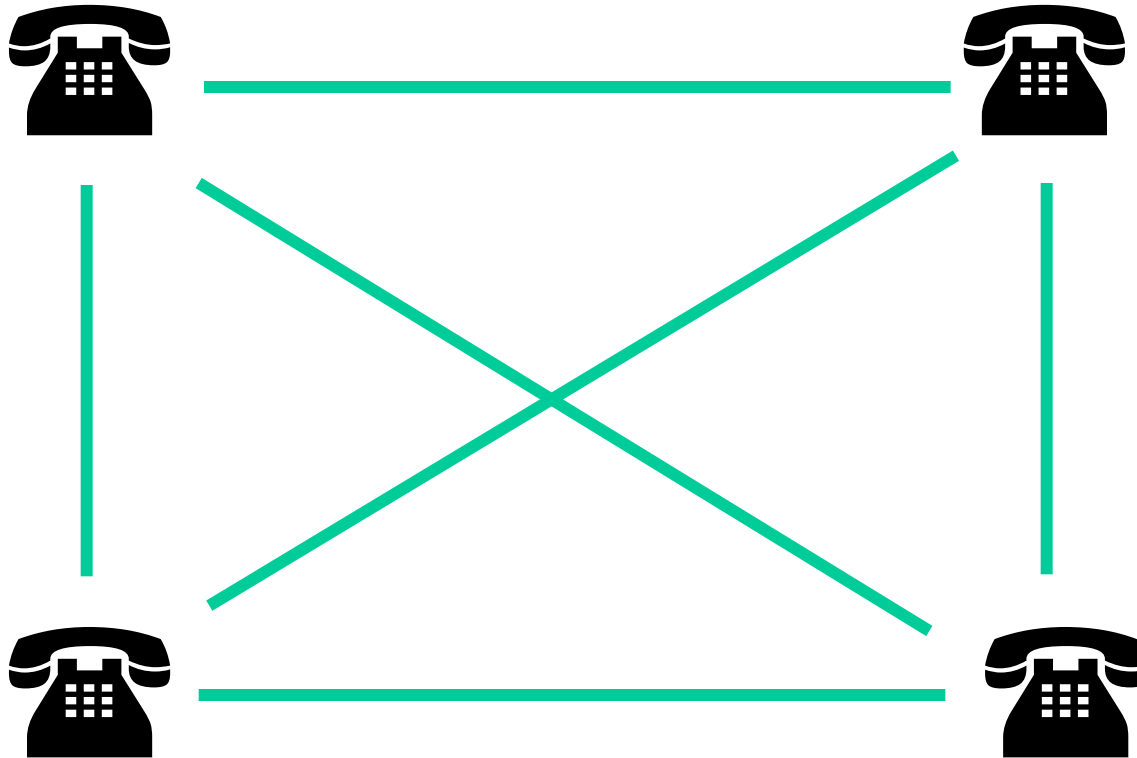
INTRODUCTION

Quick history, justification, main components ..

Quick history

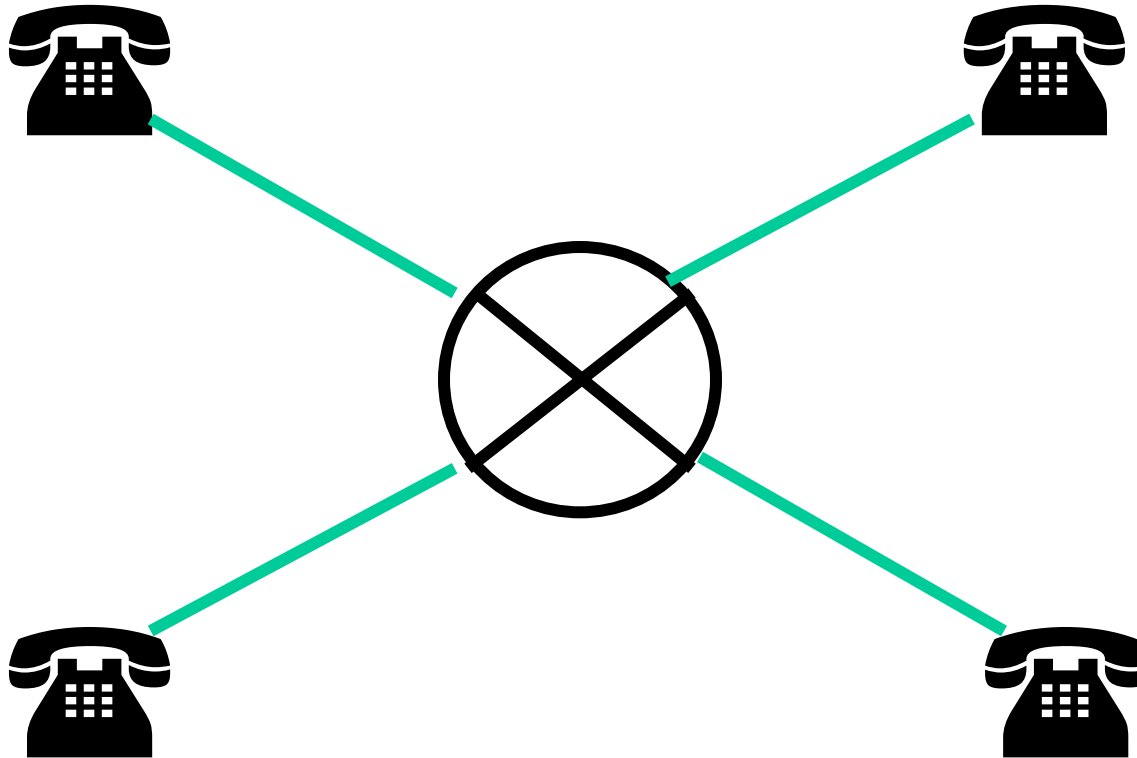
- ① The transmission was digital at the first step and analog
 - Morse transmission (Digital)
 - Voice transmission (Analog)
- ② Patent regarding the telephone has been registered by A.G Bell in 1876 :
 - Analog line and modulation,
 - Reversible Microphone/ Receiver
- ③ The switch introduction came quickly 1878 two years after the A.G Bell patent registration.

VOICE NETWORK WITHOUT SWITCH



6 links for a full meshed network

VOICE NETWORK WITH A SWITCH



4 links with a switch

BENEFIT WITH AN EXAMPLE

- ▶ N phones : $N(N-1)/2$ Links for a meshed network
- ▶ N phones: N Links and one switch
- ▶ Example 100 phones : 100 links instead 4950 links without a switch

QUICK HISTORY

The first switches were :

- ▶ Manual done by a human operator then,
- ▶ Mechanic then,
- ▶ Electromechanical and now
- ▶ Electronic.

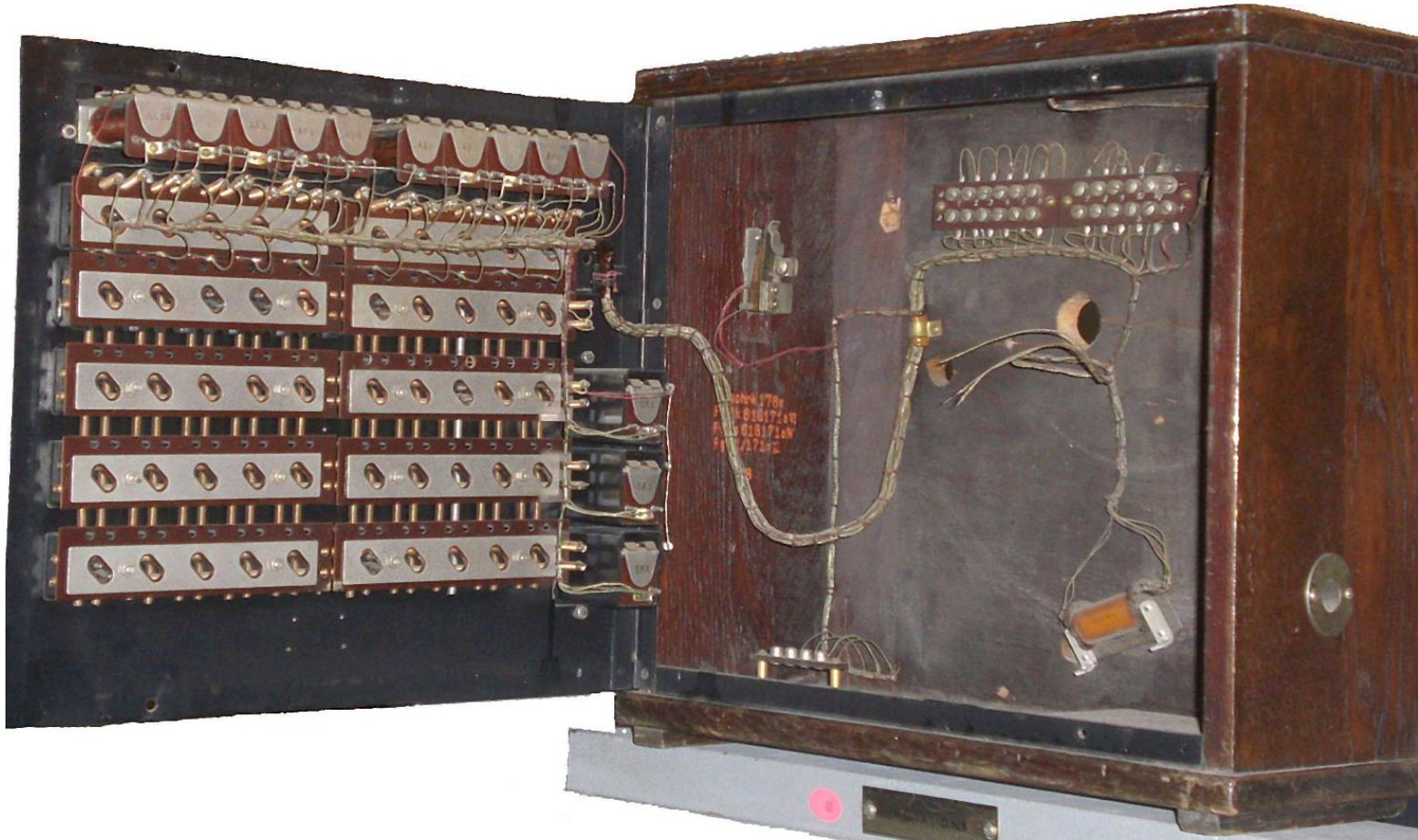
First type of phone

«Au début du téléphone, l'utilisateur, dit « abonné » car il possède un contrat avec le fournisseur du réseau téléphonique, actionne la manivelle de son poste téléphonique pour « sonner » ou appeler l'opératrice; l'opératrice rentre en contact phonique avec le demandeur pour lui demander qui il veut contacter puis connecte physiquement sa ligne à la ligne de destination pour atteindre le demandé. »



Subscriber side

Switch Manual done by a human operator



Switch board Inside View

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Manual done by a human operator



Switch board Inside View

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Manual done by a human operator



Switch board front View with the jack plug

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Manual done by a human operator

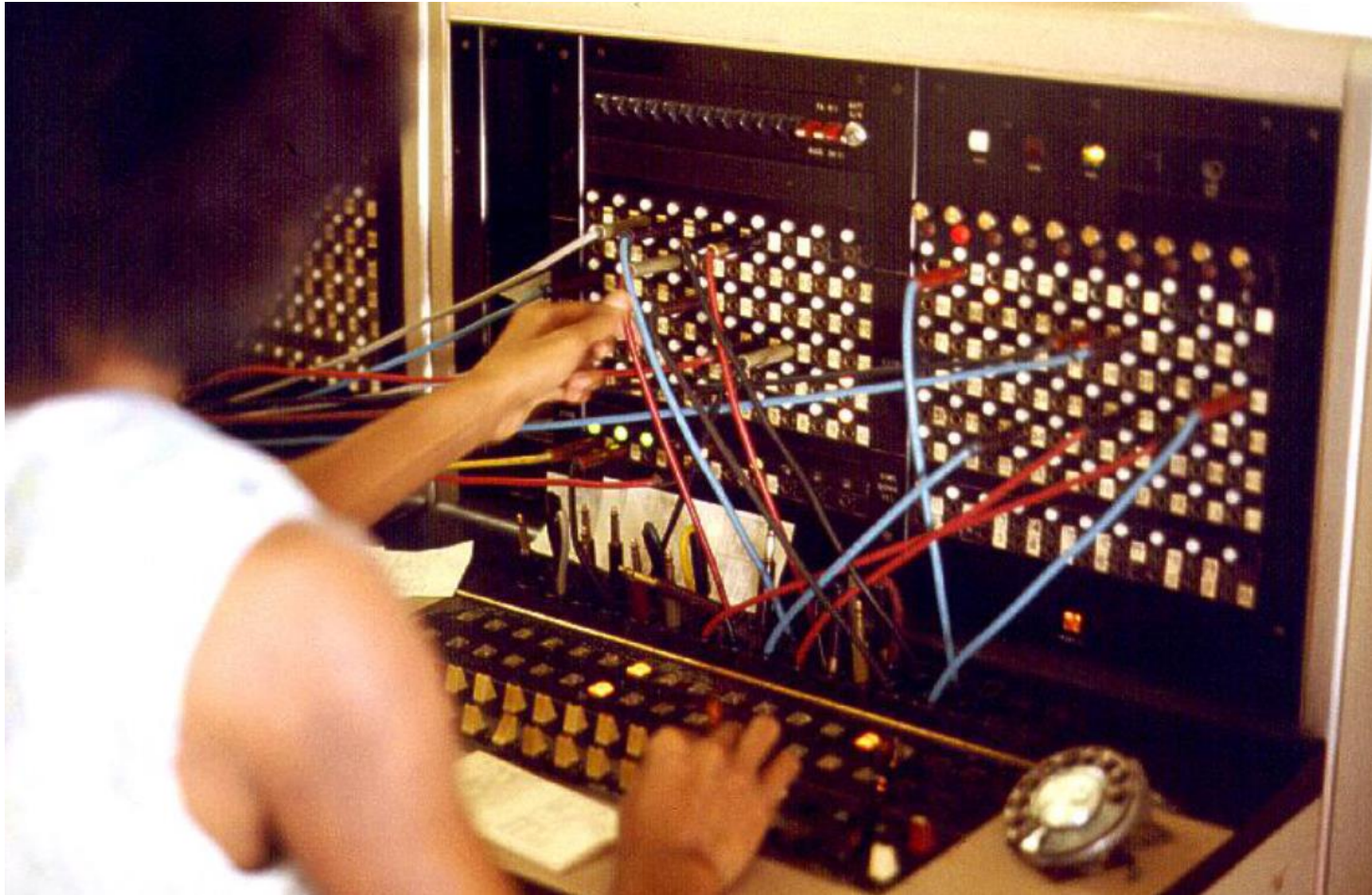


Switch Board operator

Manual done by a human operator



Manual done by a human operator



PBX 1975

Pentaconta switch 1950-1970

https://www.youtube.com/watch?v=Ahdd-r3Oq_o

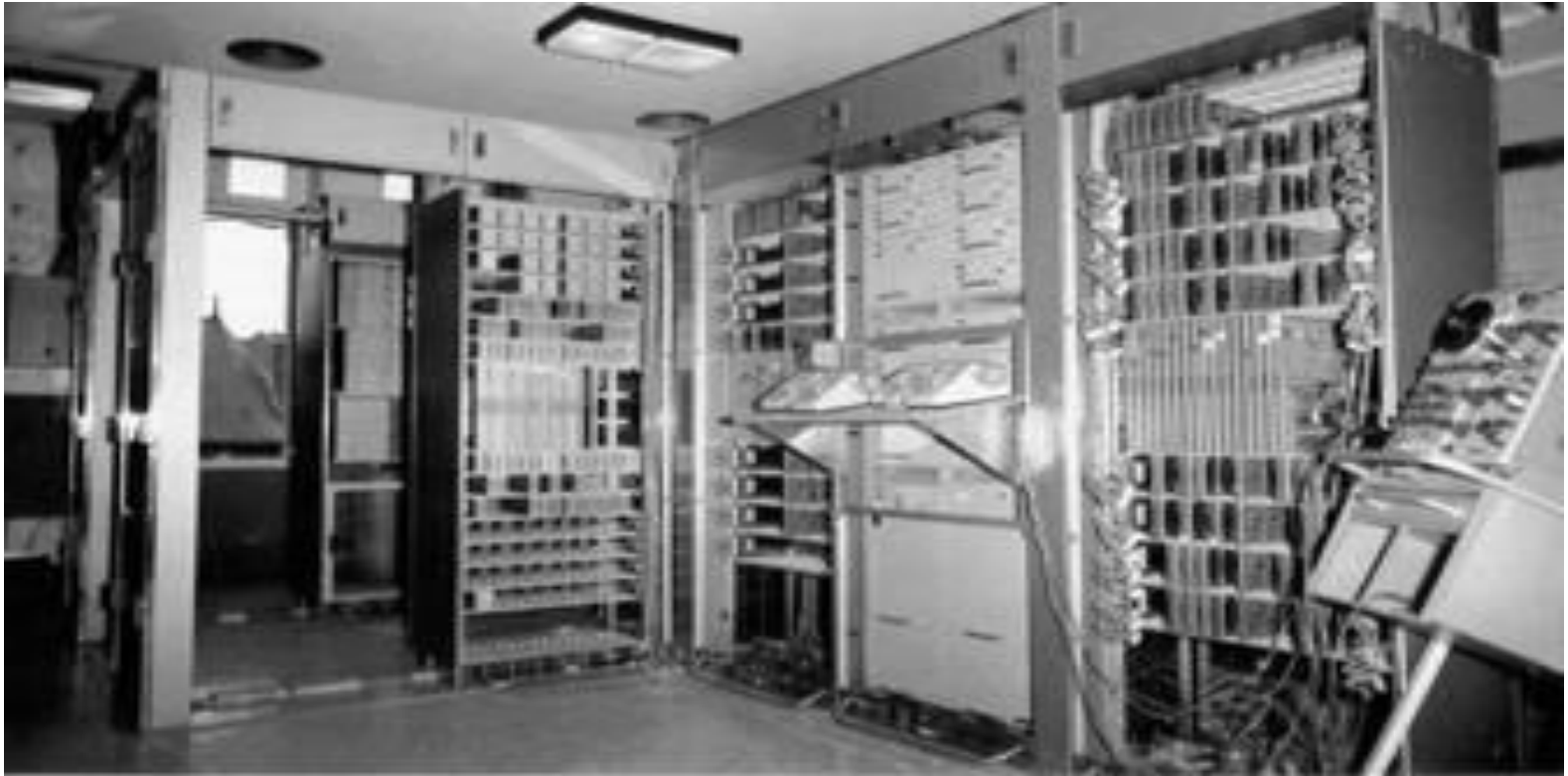
<https://www.youtube.com/watch?v=oM6OLeGOE6M>



Pentaconta switch 1000A Model



First Electronic TDM switch in France « The platon » in 1970 for 800 subscribers (Electronic Switch)



Nortel « DSM 100 » Local Switch (Electronic Switch) 2000 years



TYPE OF SWITCHES

We could consider that we have two type of switches :

- ▶ Private corporate switches (eg. PABX).
- ▶ Public Switches used by operators

MAIN SWITCH VENDOR

Today the market is shared by 5 vendors which propose 6 different public switches :

- ▶ SIEMENS : EWSD
- ▶ ALCATEL : E10 & S12.
- ▶ LUCENT TECHNOLOGIES : 5ESS
- ▶ ERICSSON : AXE 10.
- ▶ NORTEL : DMS

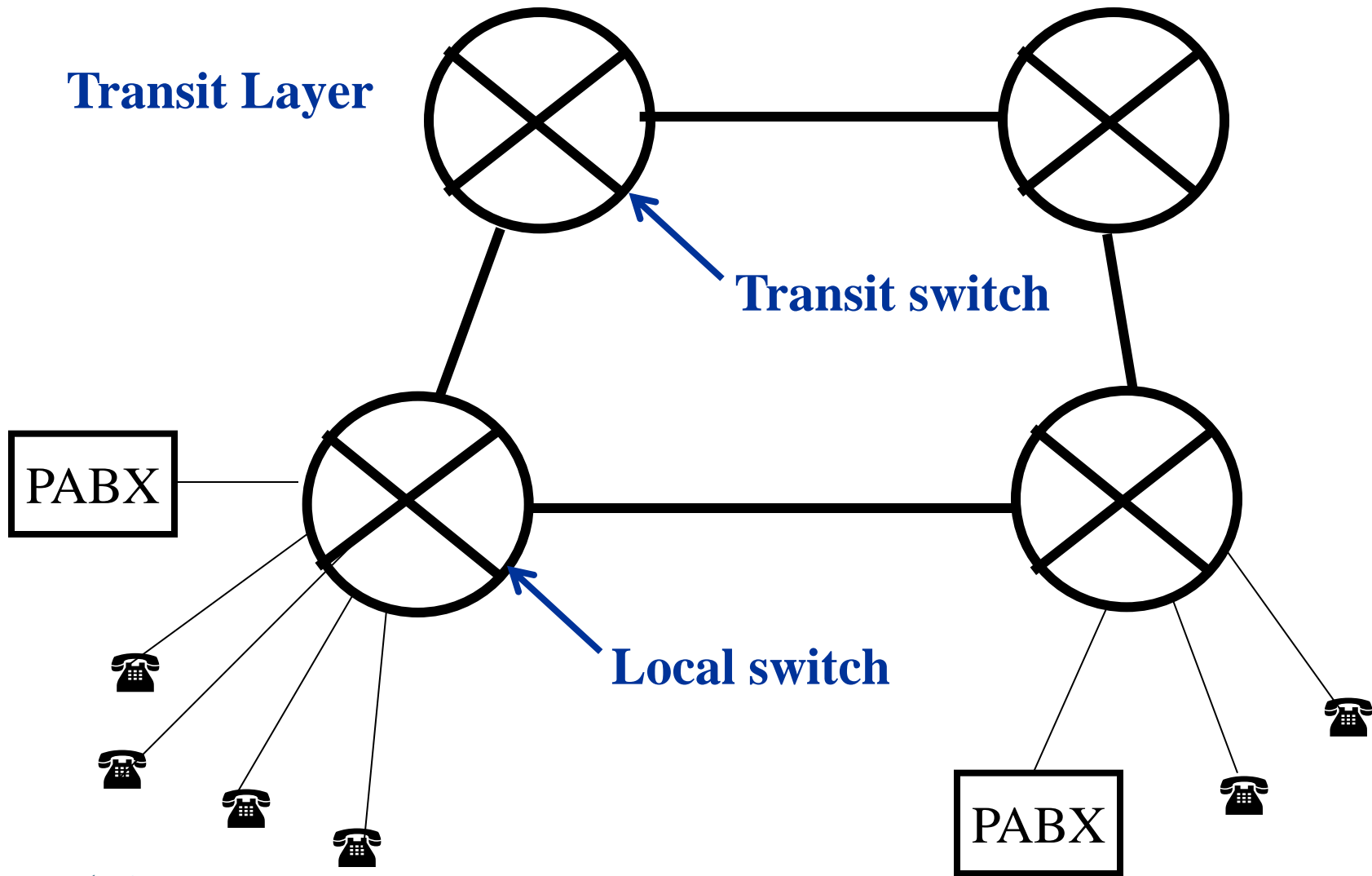
TYPE OF PUBLIC SWITCHES

There is 3 family of public switches

- ▶ LOCAL: used to connect customers and others switches
- ▶ TRANSIT : Used to interconnect switches
- ▶ “TRANS-LOCAL” : Which as the both functions generally used alternate operators which have not enough traffic for having a transit network.

PUBLIC VOICE NETWORK ARCHITECTURE

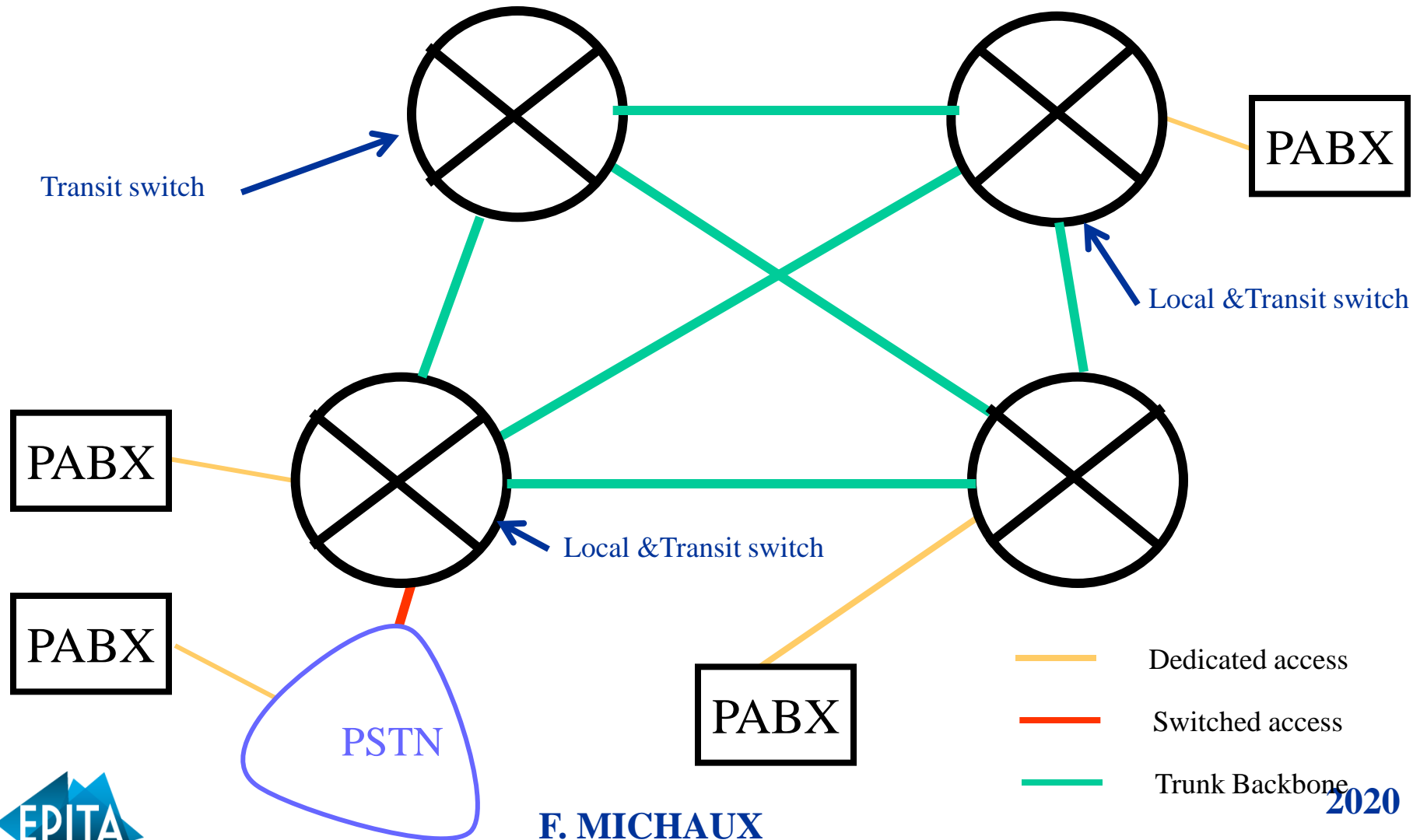
Transit Layer



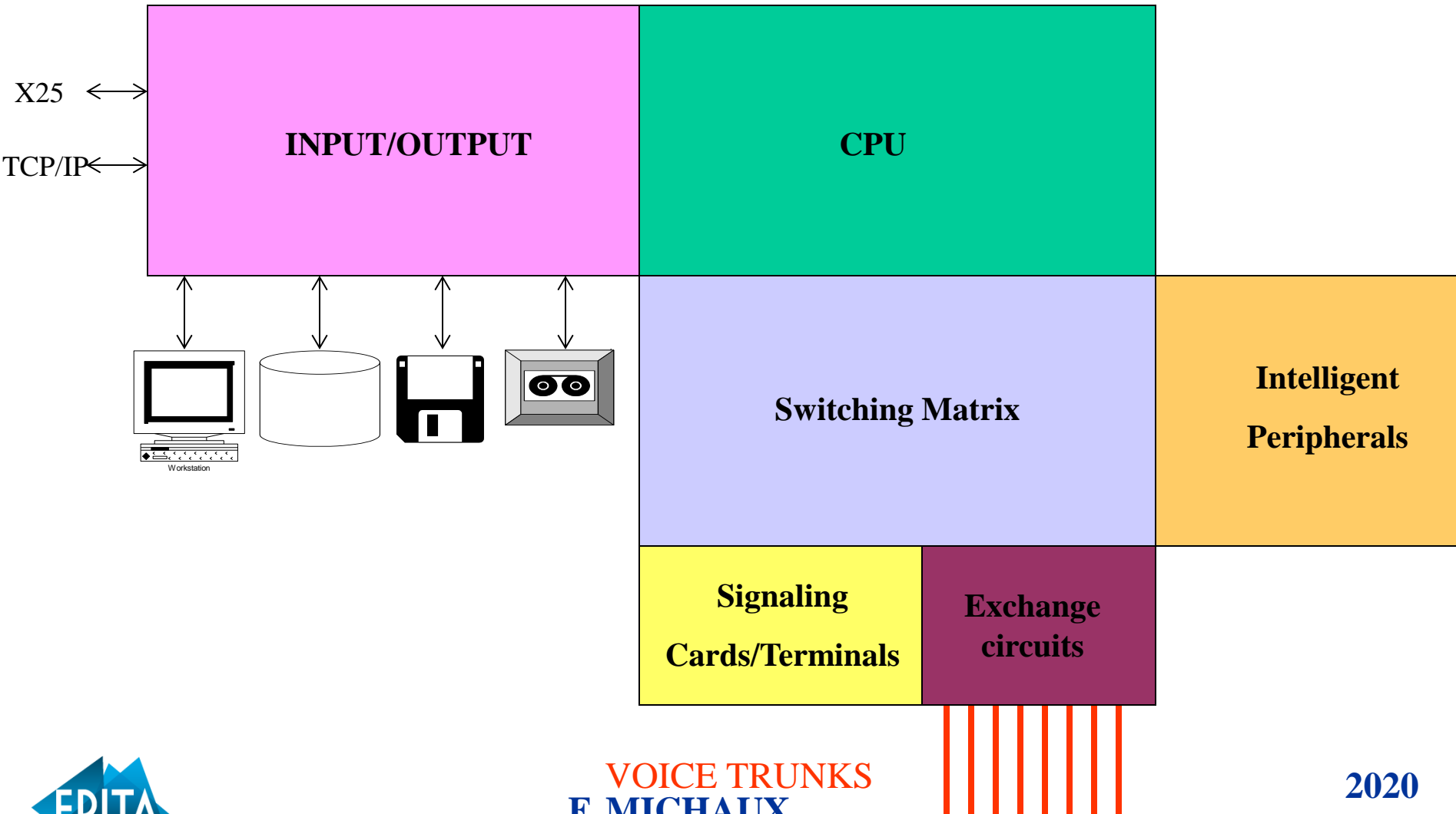
VOICE NETWORK ARCHITECTURE



The voice network architecture is flat no transit layer

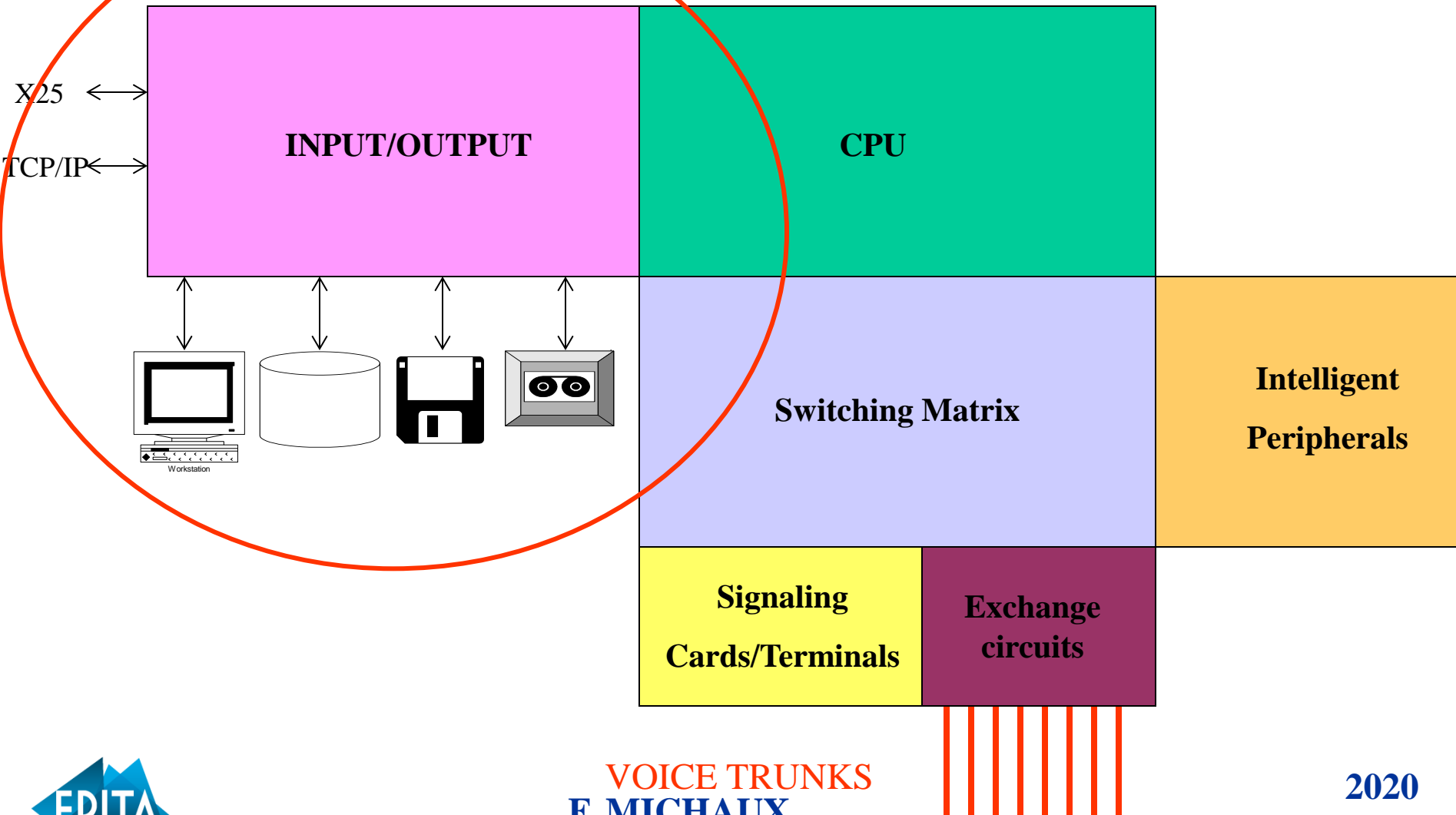


MAIN SWITCH COMPONENTS



INPUT/OUTPUT

MAIN SWITCH COMPONENTS



INPUT/OUTPUT

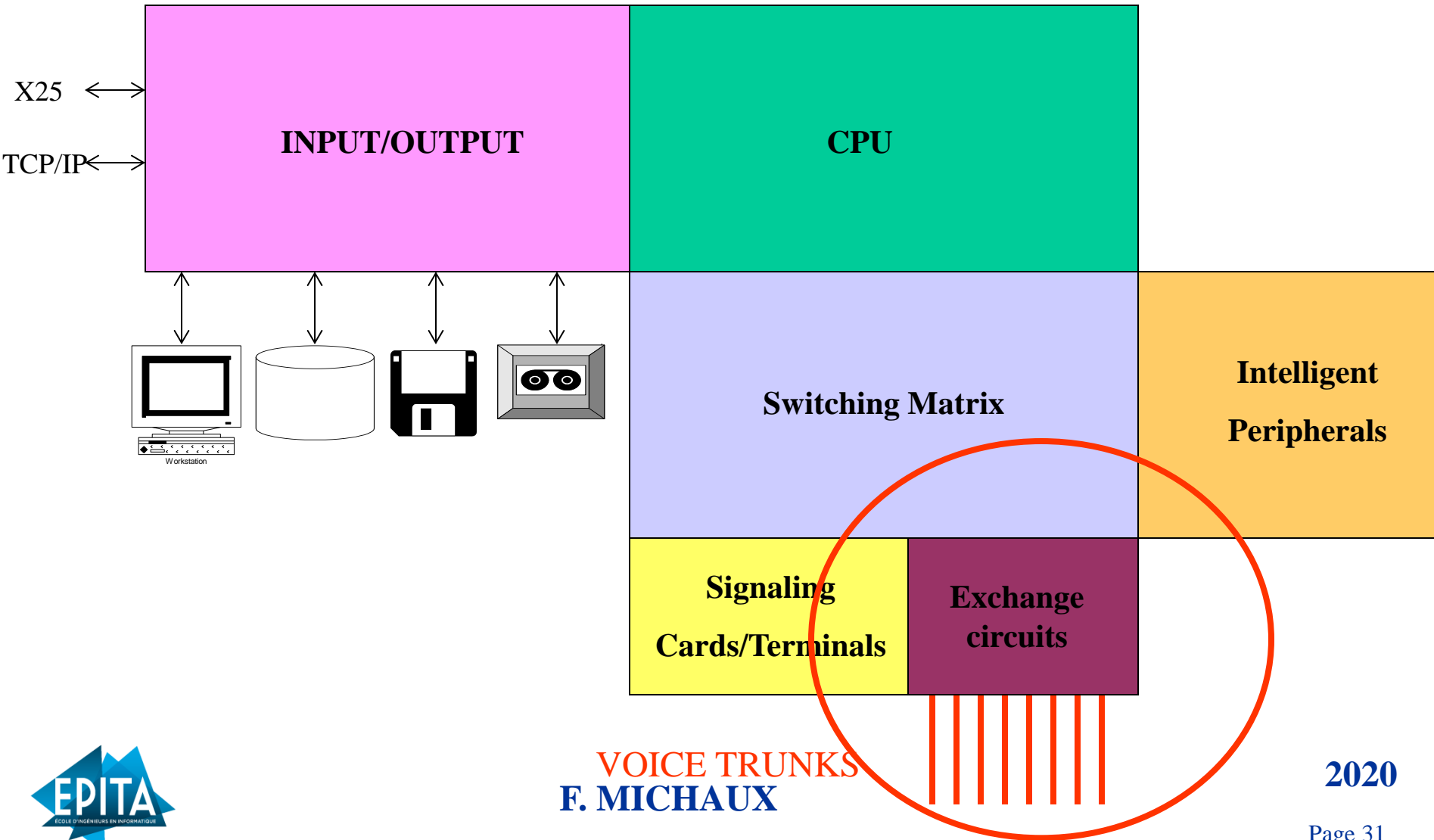
This device is the interface equipment between the switch and

- ▶ The billing system X25 or/and TCP/IP.
- ▶ Monitoring system remotely and locally.
- ▶ Saving system (Call detail records, translations
- ▶ The disks

TDM TECHNOLOGIE

Transport, PCM...

MAIN SWITCH COMPONENTS



TDM TECHNOLOGIE

TDM means Time Division Multiplexing

This technologie :

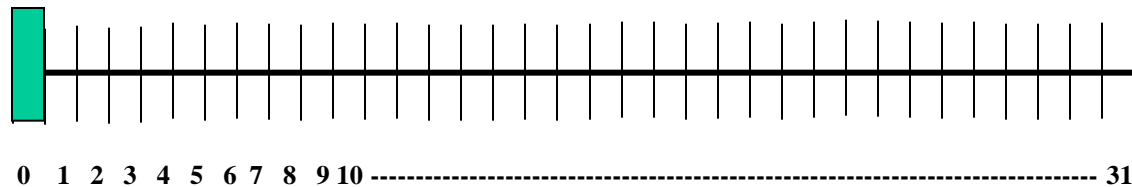


is known for more than 60 years, but deployed for 30 years. Patent dated before the second world war.



Consists of divided the time in order to carry in the same link different trafic stream

TDM TECHNOLOGIE



The time is divided in 32 time slots (E1) for the international standart and 24 (T1) for the american standart.

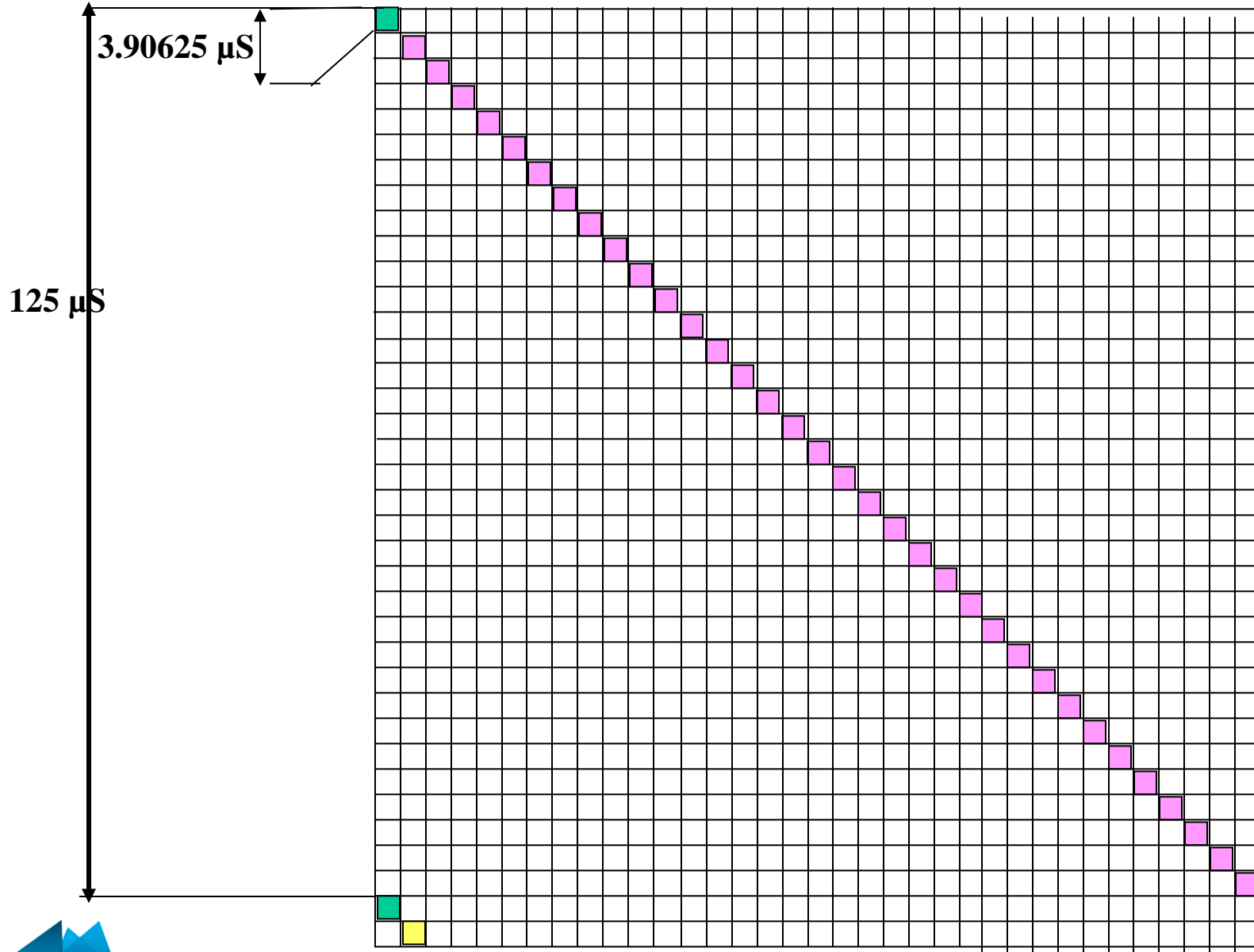
The total rate for the link is 2.048 Mb/s

The rate for the a time slot is $64 \text{ Kb/s} = 2048/32$

The time slot 0 is used for the synchronisation, the paylaod is not $32 \times 64 \text{ Kb/s}$ but $31 \times 64 \text{ Kb/s}$

TDM TECHNOLOGIE

0 1 2 3 4 5 6 7 8 9 10 31



TDM TECHNOLOGIE

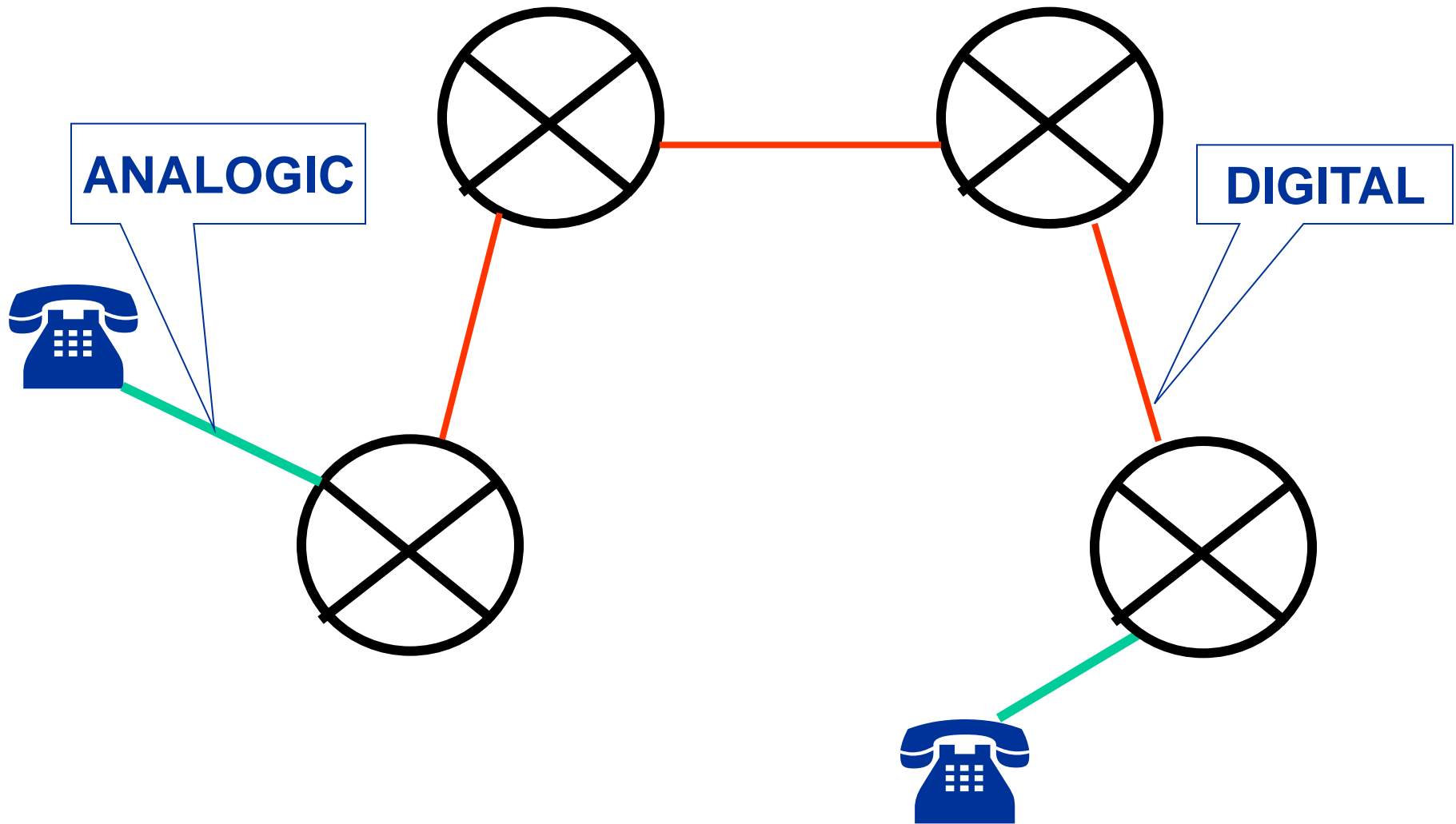
- Every 125 μ S each time slot has a window of $125 \mu\text{S} / 32 = 3.90625 \mu\text{S}$

- As the total rate of the link is 2.048 Mb/s therefore a time slot sends every 125 μ S.

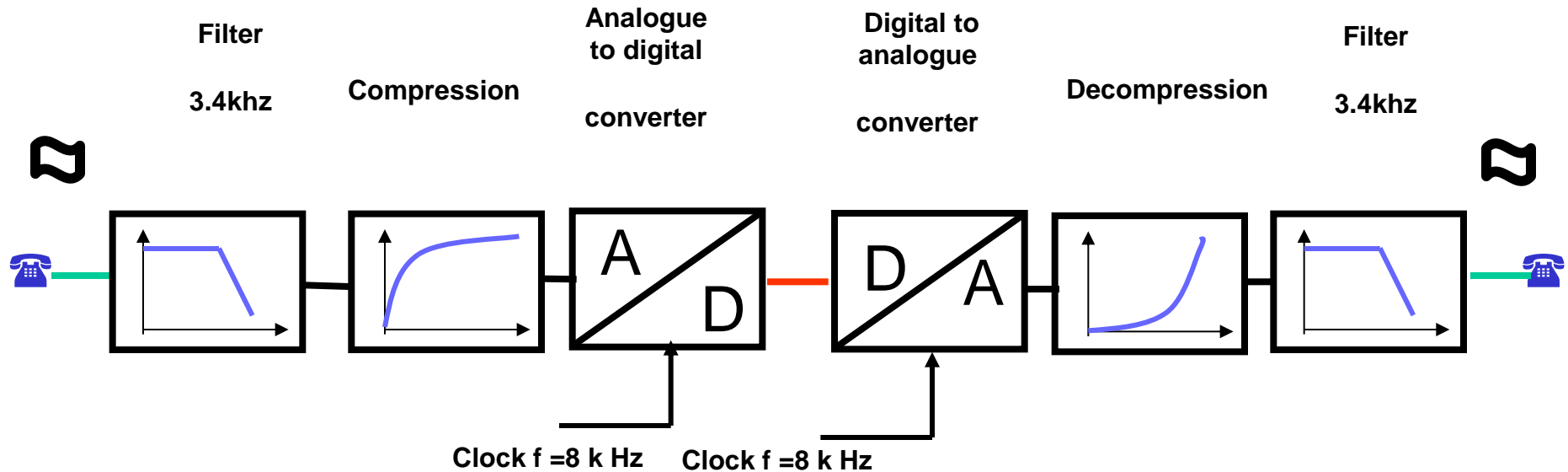
$$2\,048\,000 \text{ b/s} \times 3.90625 \mu\text{S} = \mathbf{8 \text{ bits}}$$

Conclusion: 1 Byte is sent every 125 μ S per time slot. It corresponds of 8000 Bytes/s or 64Kb/s.

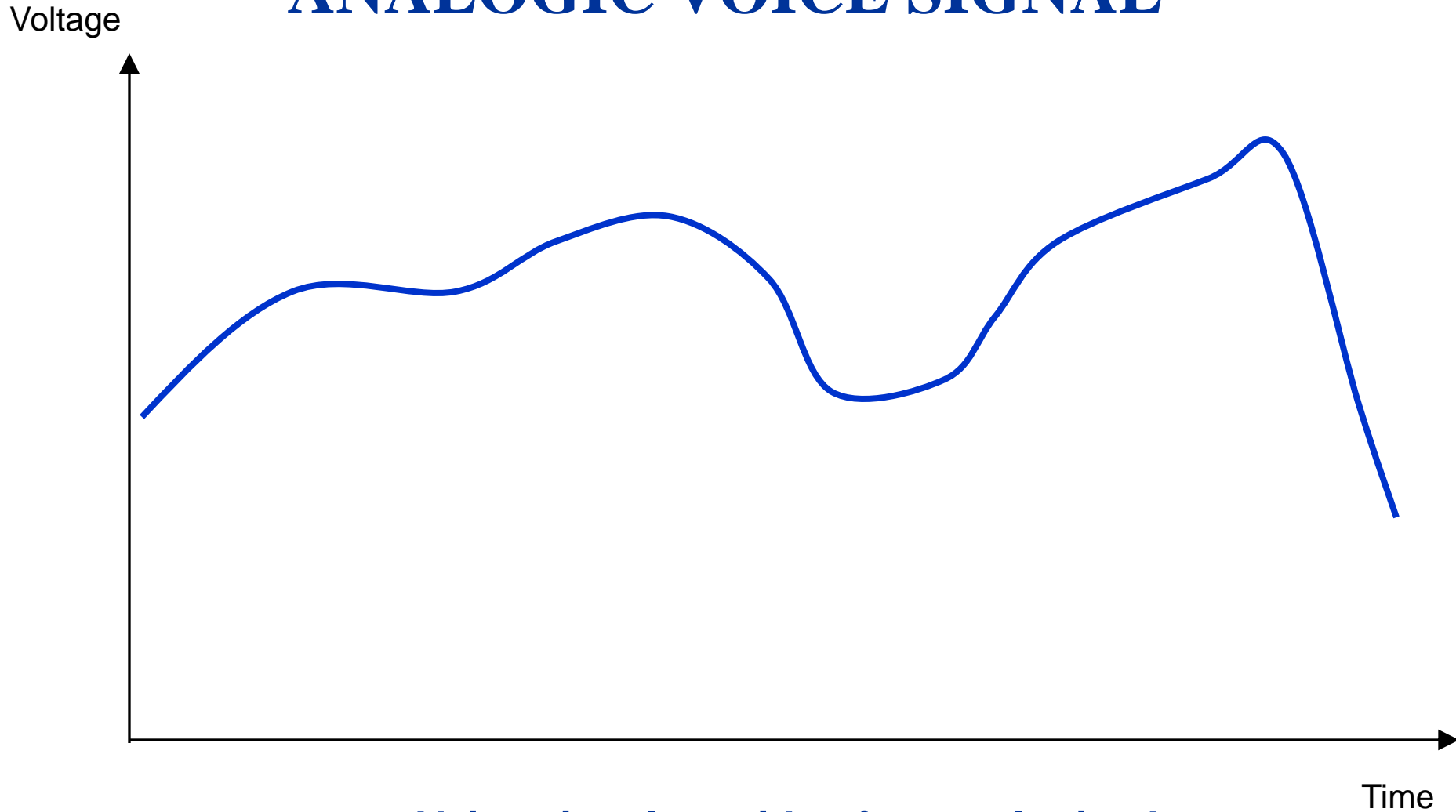
ANALOGIC & DIGITAL LINES



DIGITALIZATION PRINCIPLE

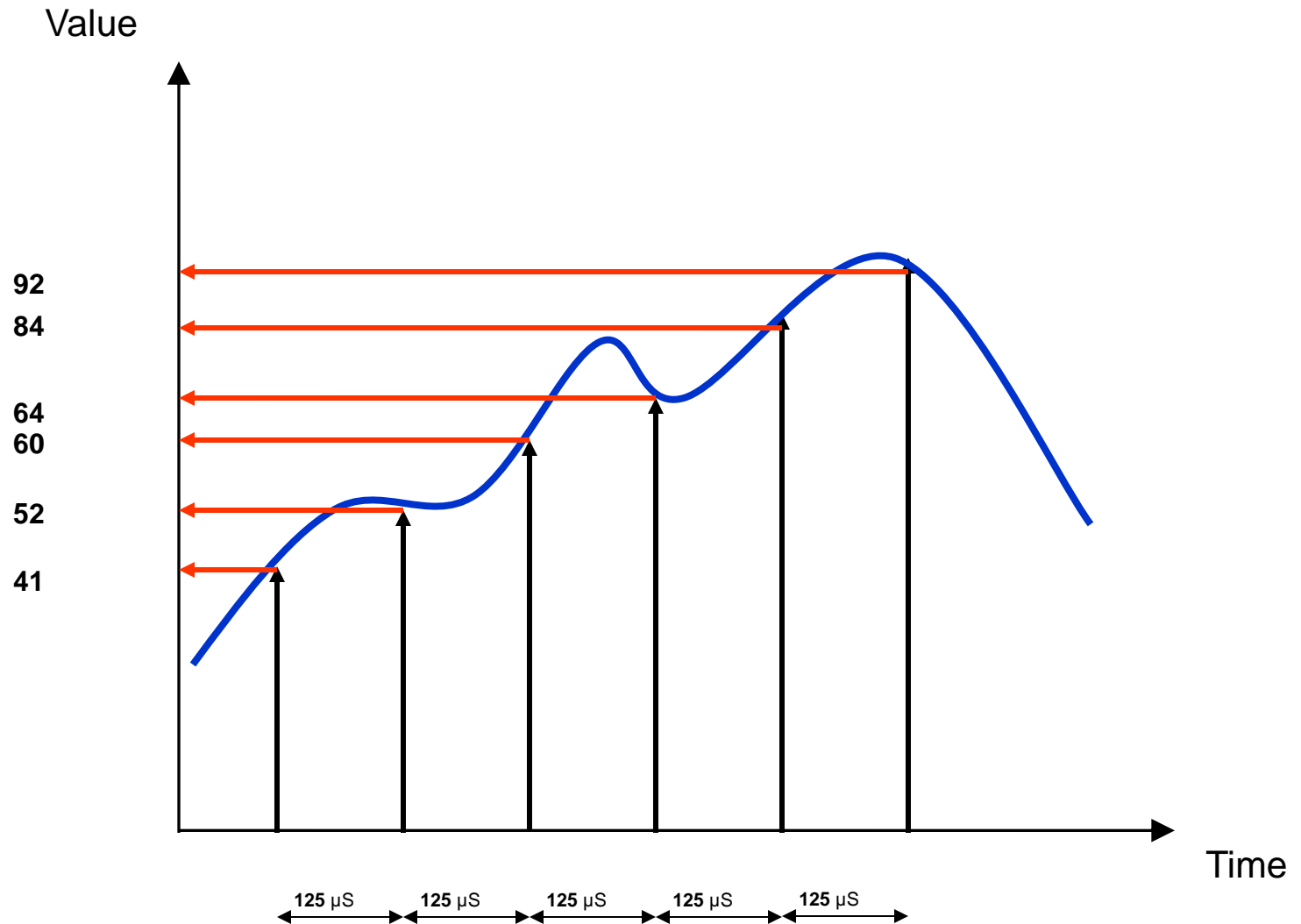


ANALOGIC VOICE SIGNAL



Voice signal outside of an analogic phone

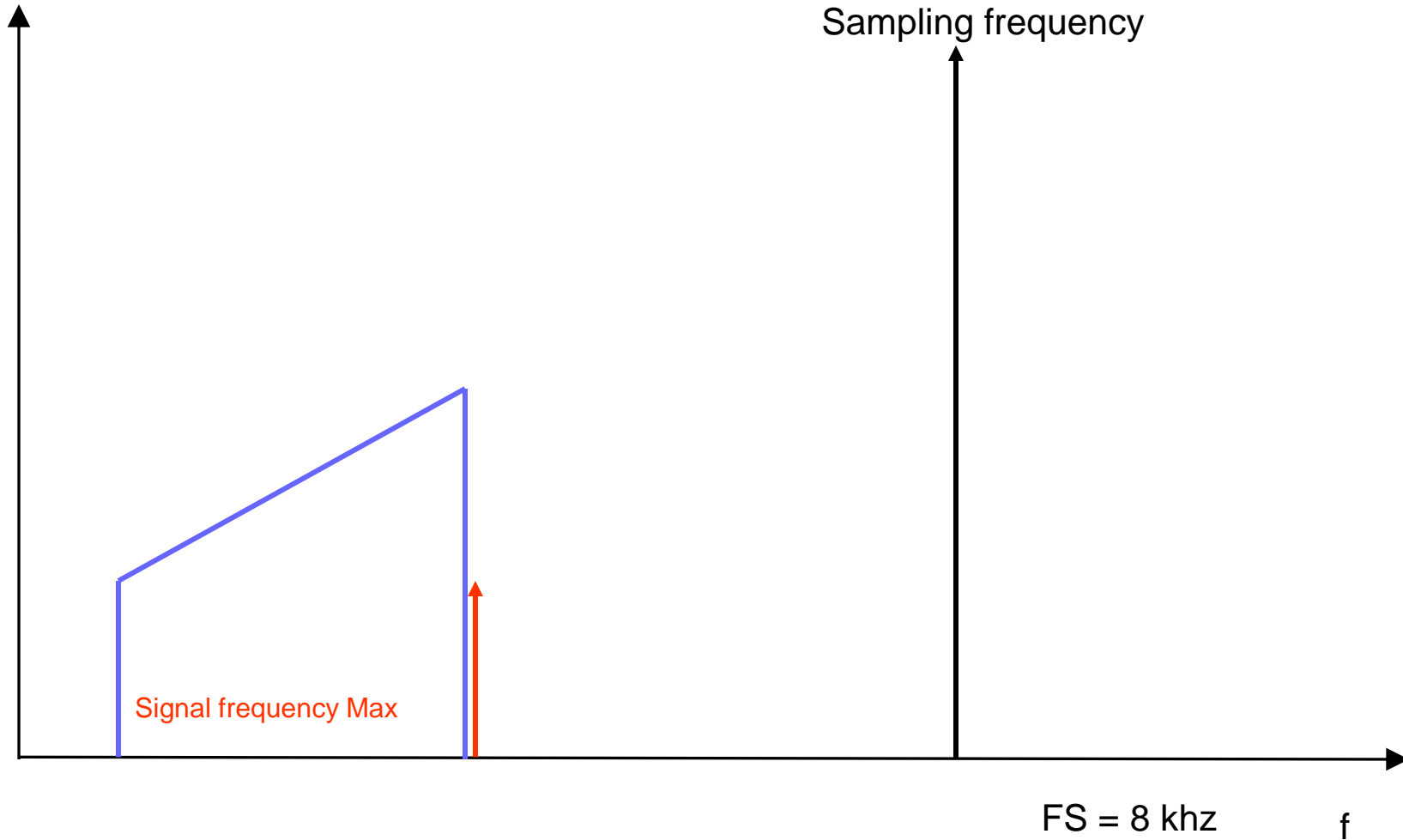
PULSE CODING MODULATION



DIGITALIZATION PRINCIPLE
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SIGNAL THEORY

Value



Voice spectrum

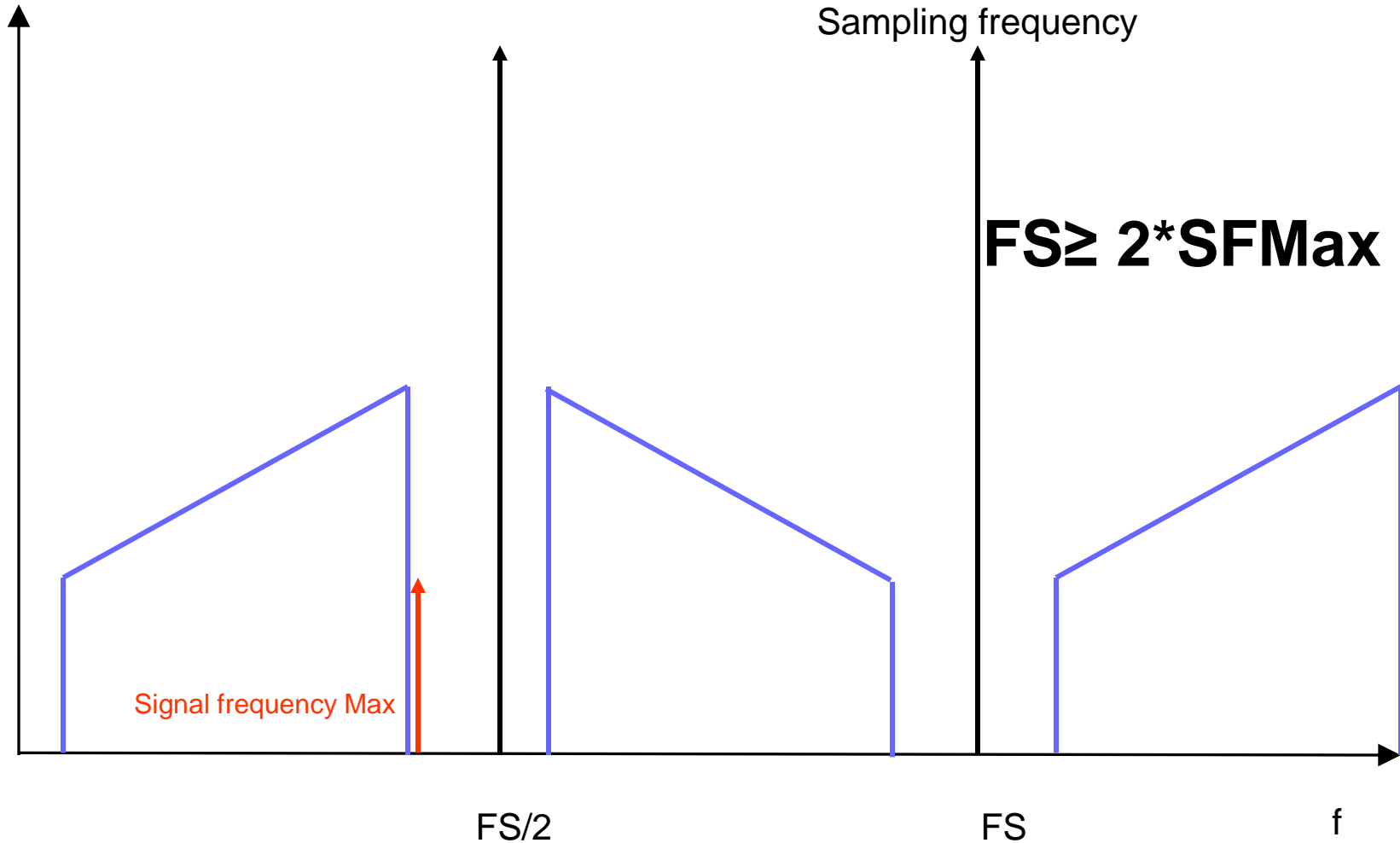
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SIGNAL THEORY

Value



Spectrum about turn effect due to the sampling

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SIGNAL THEORY

Value

Sampling frequency

$$FS < 2 * SF_{Max}$$

In this case the
spectrum is Changed

Signal frequency Max

$FS/2$

FS

f

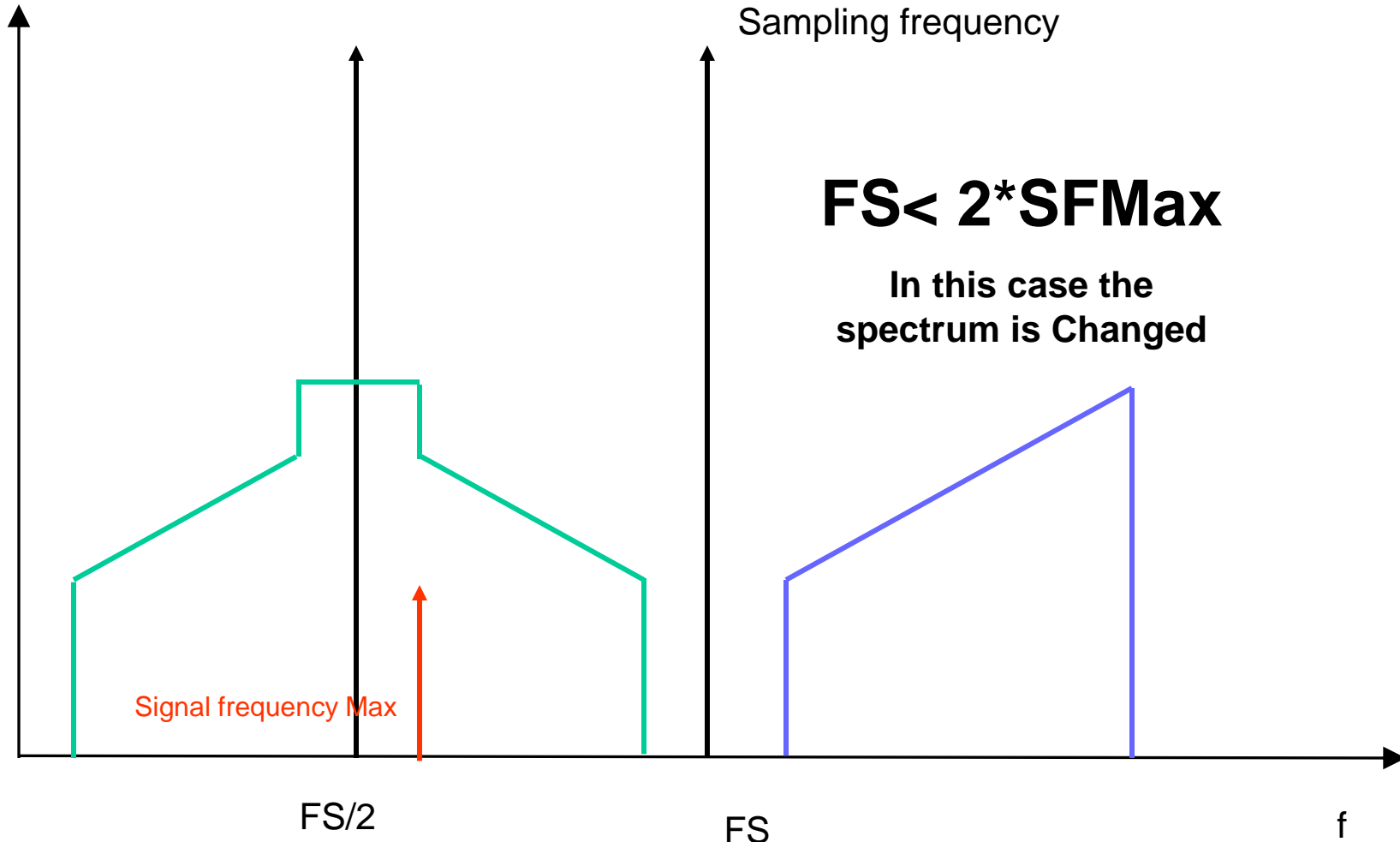
Spectrum about turn effect due to the sampling

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SIGNAL THEORY

Value



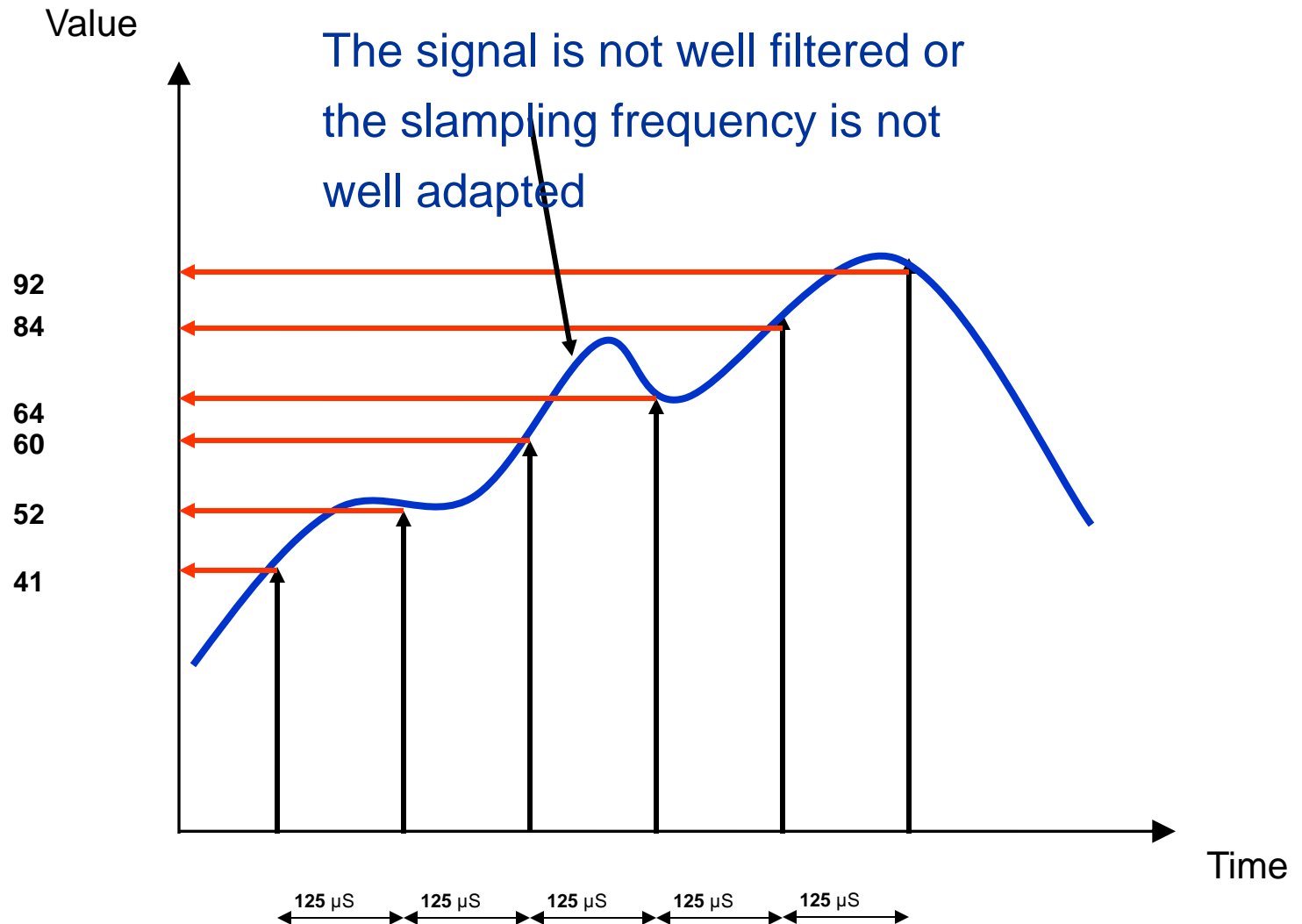
Spectrum about turn effect due to the sampling

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SIGNAL THEORY



DIGITALIZATION PRINCIPLE
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SIGNAL THEORIE

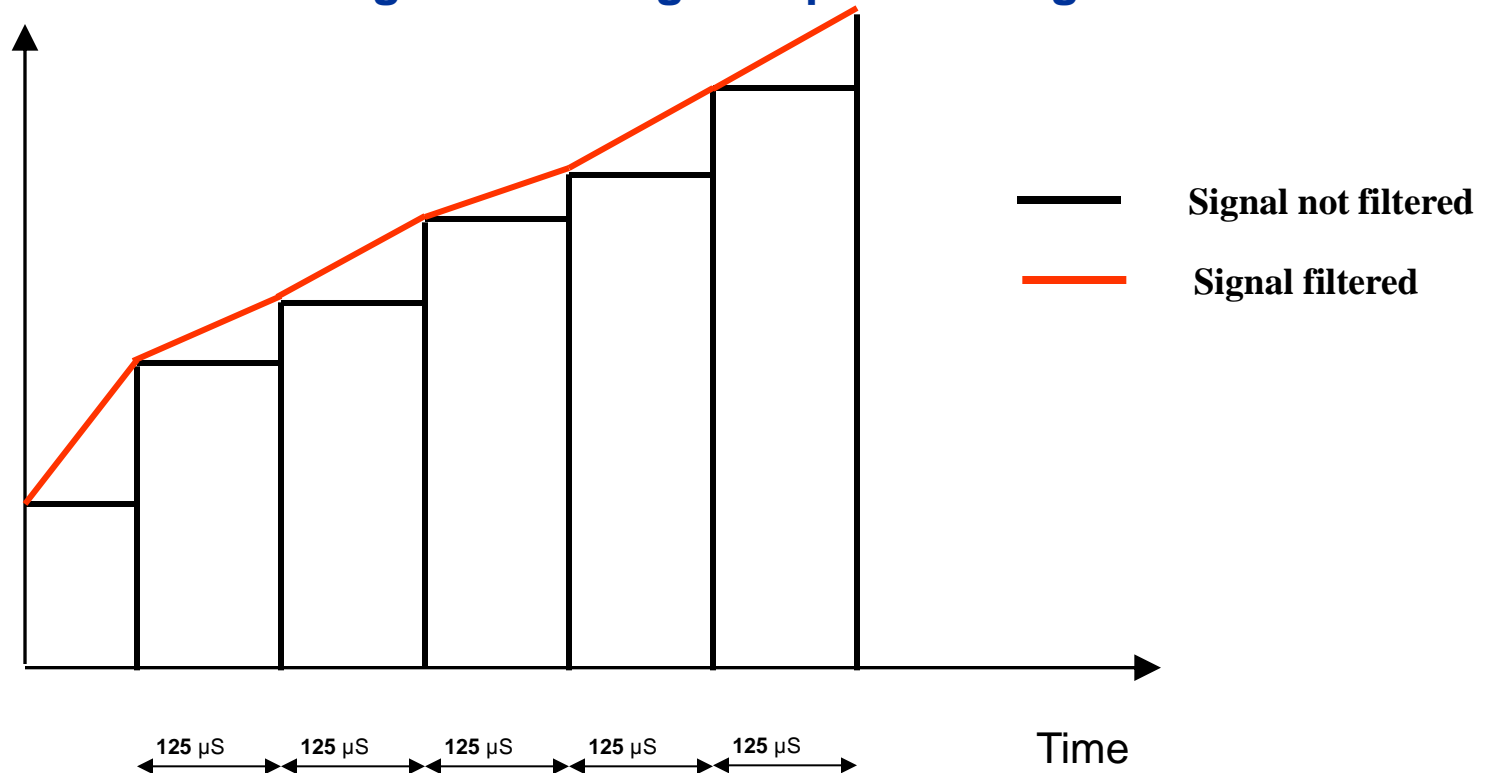
The Shannon theorem : the spectrum will be reproduced identically if the sampling frequency is superior or equal to $2 \cdot F_{\max}$ (of the voice signal) in telephony :

- ▶ The Sampling frequency is 8 KHz
- ▶ The voice spectrum is between 300-3400 hz
- ▶ Checking : $8000 \geq 2 * 3400 = 6800$
- ▶ This the reason why the voice signal is filtered

SIGNAL THEORIE

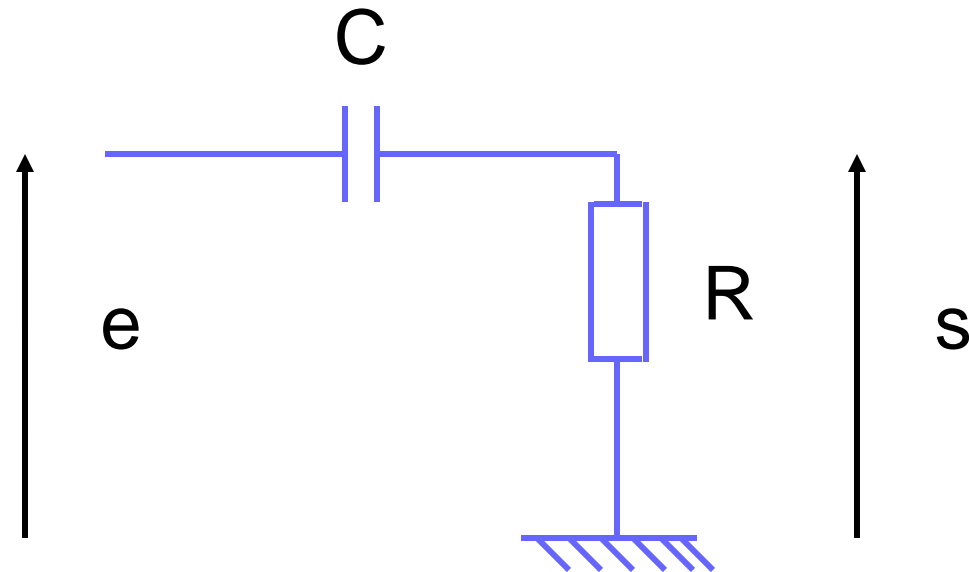
- ▶ The signal has to be filtered after the conversion digital to analog :

The conversion D to A generates high frequencies signal.



SIGNAL THEORIE

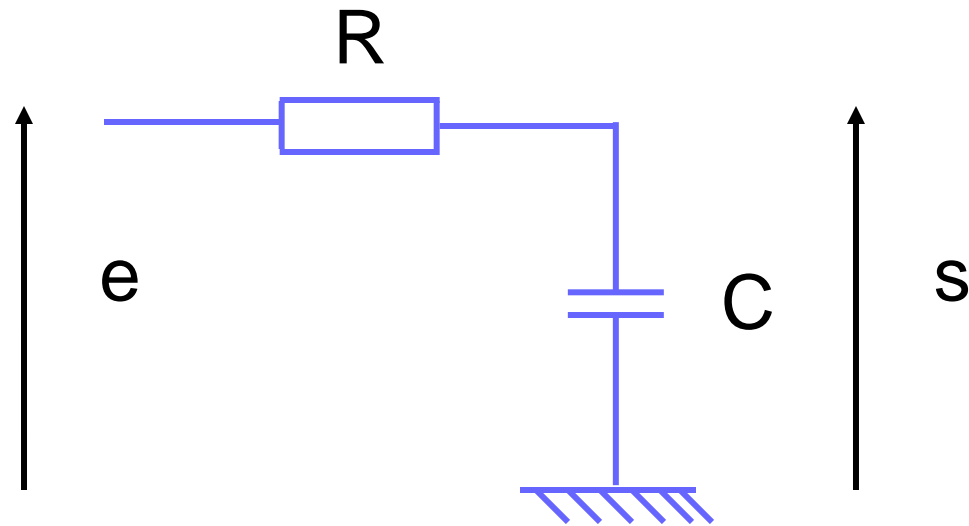
▶ Low frequencies suppressor



SIGNAL THEORIE

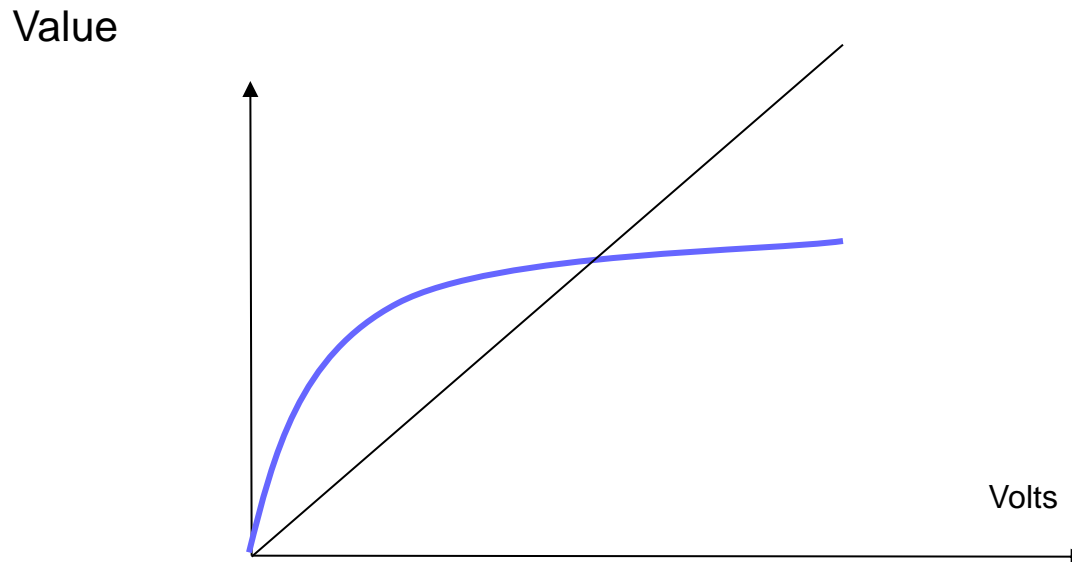


High frequencies suppressor



COMPRESSION 1/4

The conversion analogic to digital and the conversion digital to analogic is not linear. The reason is to extract the law signal from the noise and also to reduce the quantization noise.



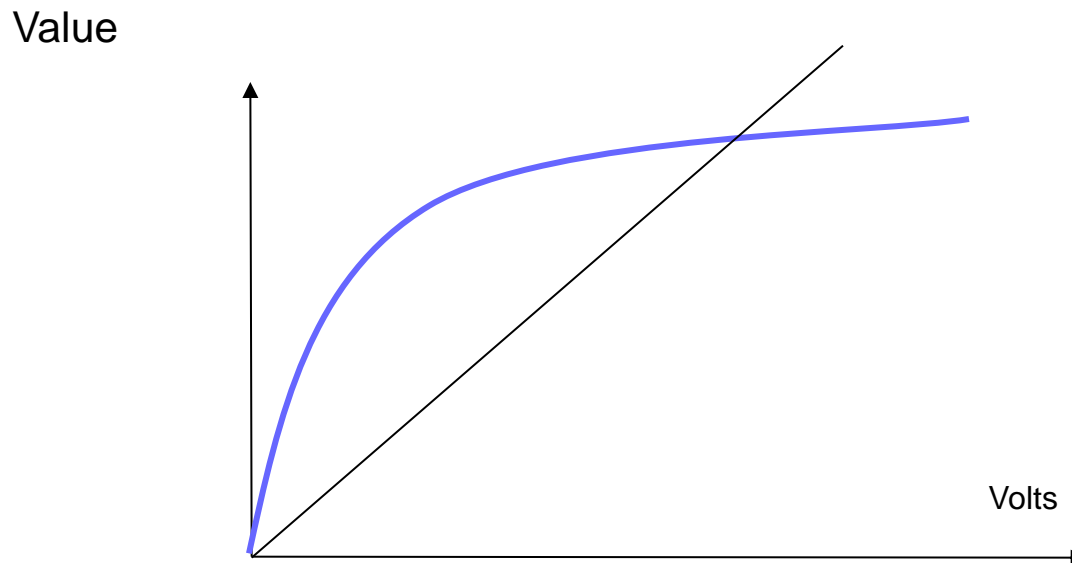
COMPRESSION 2/4

There is two kind of compression law :

- ▶ The law μ used in North America and Japan.
- ▶ The law A used for the rest of the world.
- ▶ The law A has priority

COMPRESSION 3/4

The law μ is a pure logarithmic curve.

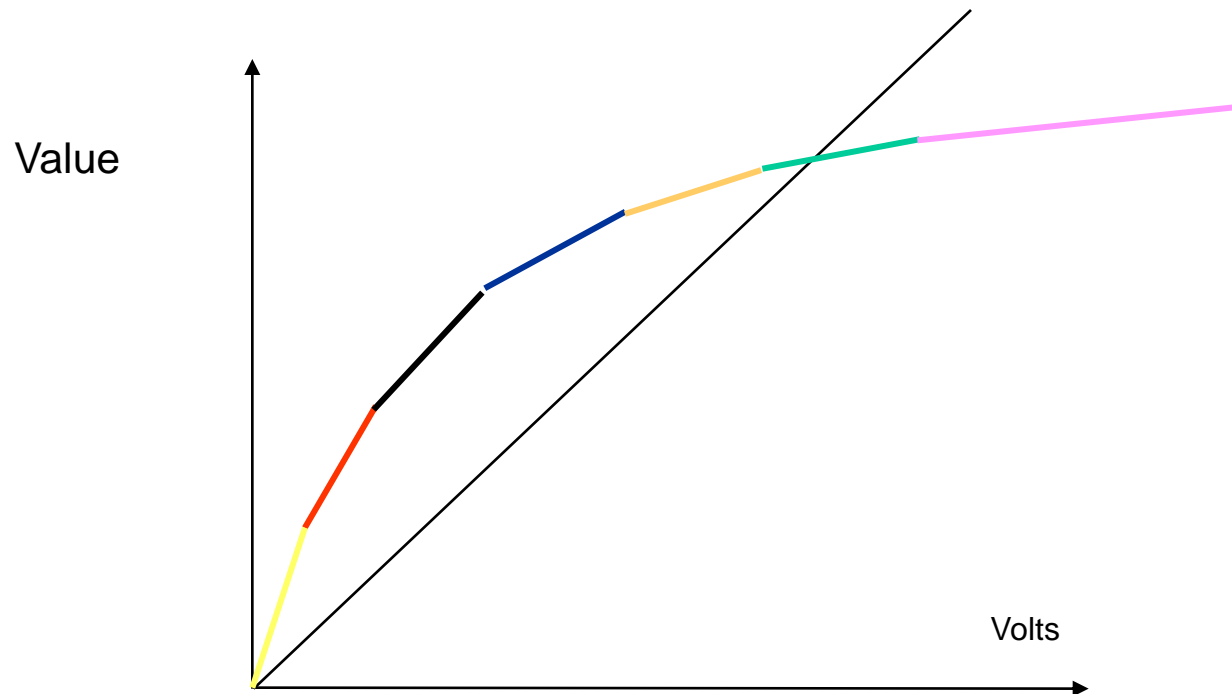


The law μ

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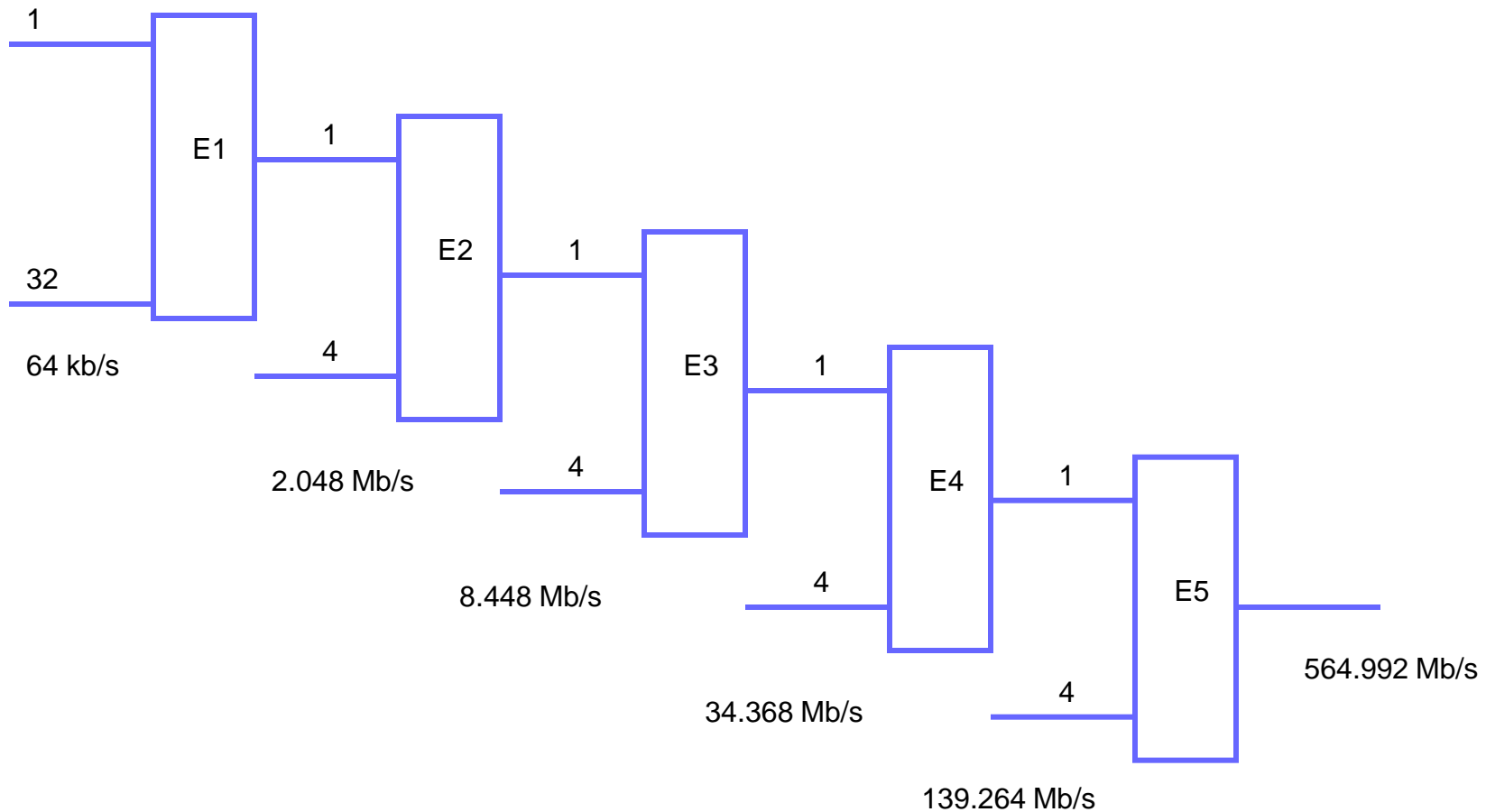
COMPRESSION 4/4

The law A is a sum of 7 linear segments



The law A
F. MICHAUX

PLESIOCHRON DATA HIERARCHY 1/2



PLESIOCHROME DATA HIERARCHY 2/2

This technology has some constraints :

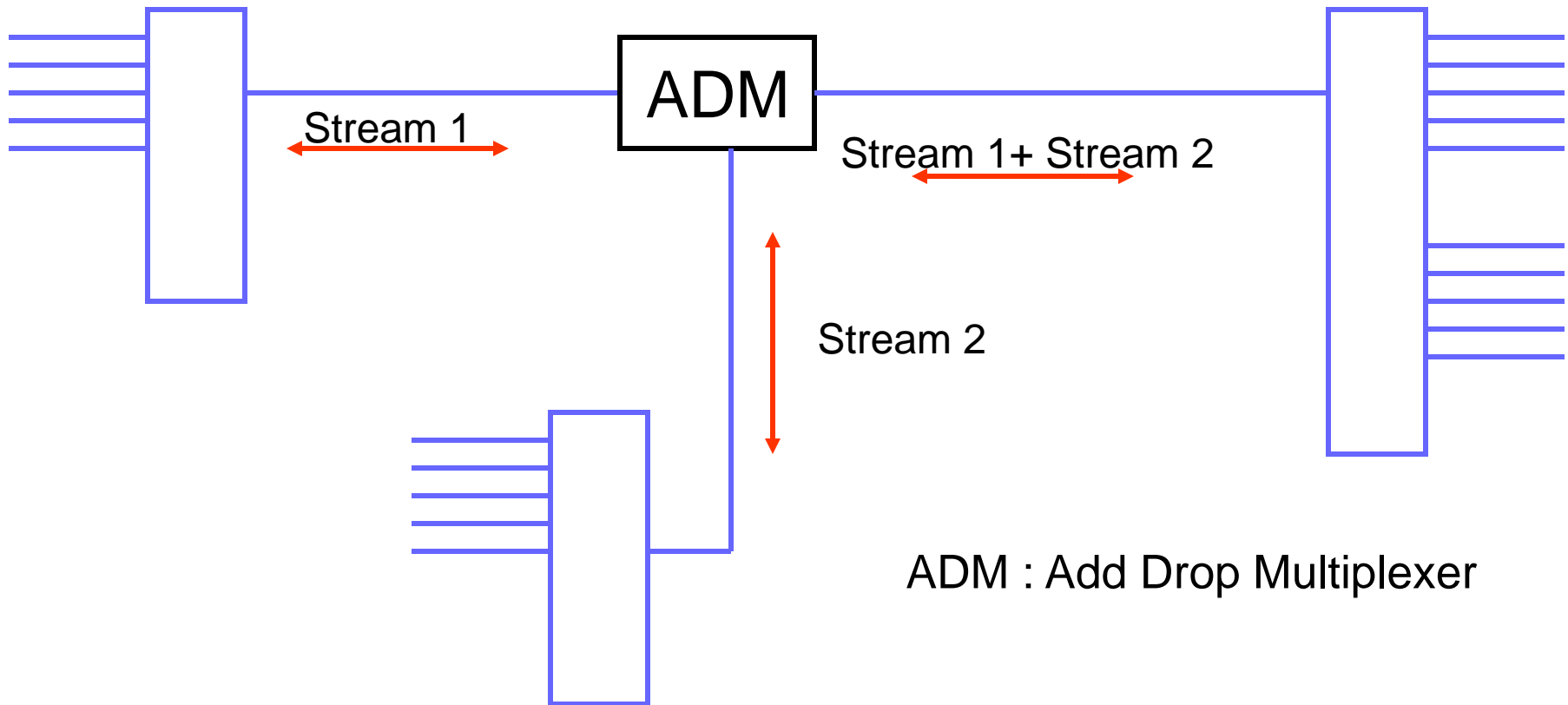
- ▶ The links have to be synchronized
- ▶ Impossible to drop one time slot or all of the traffic has to be de multiplexed.

Conclusion:

- ▶ Interesting for a point to point traffic

SYNCHRONOUS DATA HIERARCHY 1/6

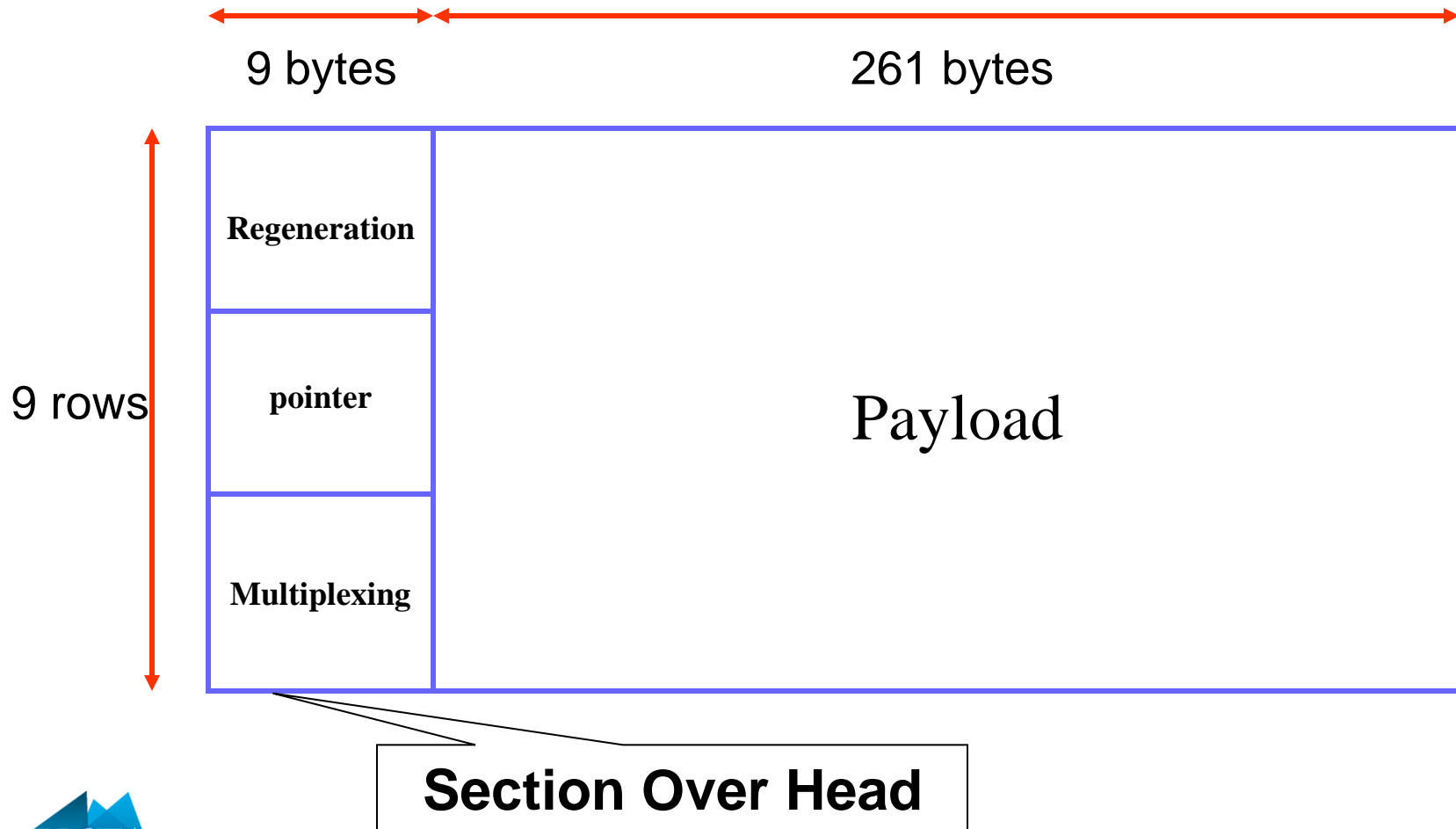
This technology is used in case of ring transport architecture



ADM : Add Drop Multiplexer




SYNCHRONOUS DATA HIERARCHY 2/6

STM1 Container description



SYNCHRONOUS DATA HIERARCHY 3/6

SOH DESCRIPTION

-  Overhead of regeneration : used for error correction
-  Overhead of position : used to synchronized the upstream traffic
-  Overhead of multiplexing : used to add and drop the traffic at the ADM level.

SYNCHRONOUS DATA HIERARCHY 4/6

There is 8000 containers per second :

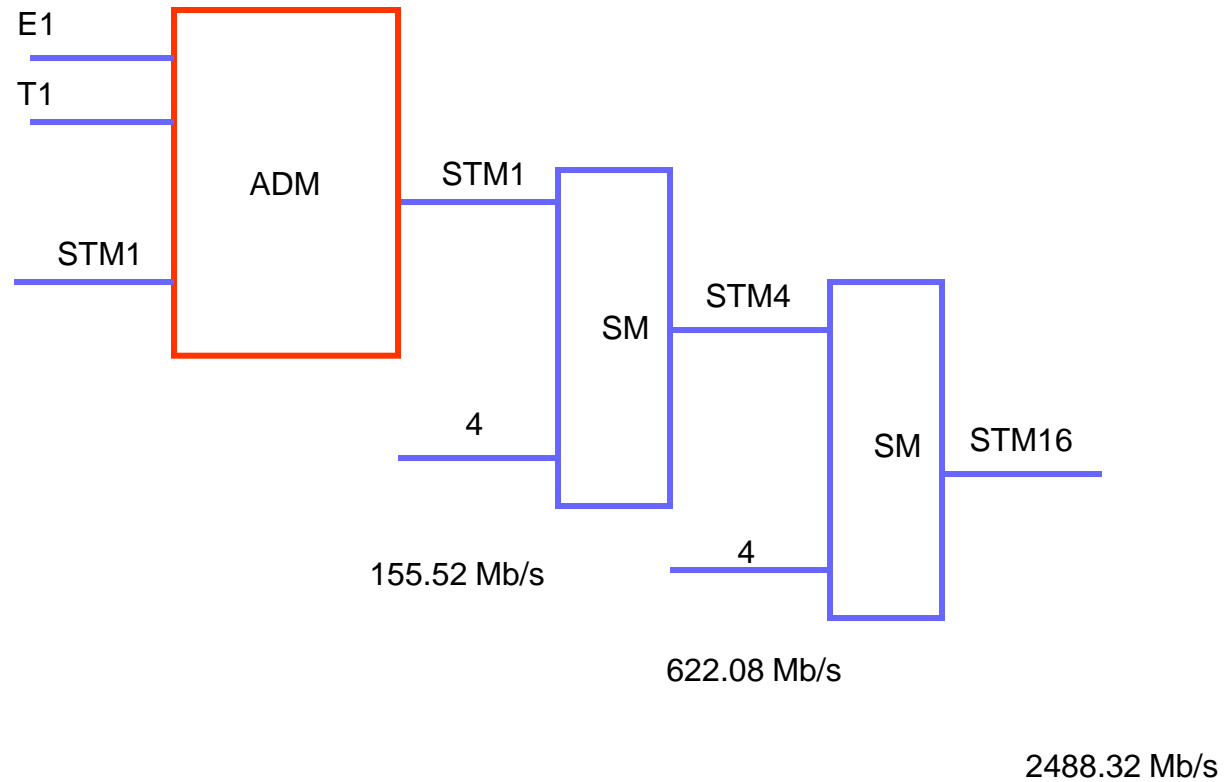
- ▶ The total rate is : $270 \times 9 \times 8000 \times 8 = 155.52 \text{ Mbit/s}$
- ▶ The payload is $261 \times 9 \times 8000 \times 8 = 150.336 \text{ Mbit/s}$
- ▶ STM4 rate is: 622.08 Mbit/s
- ▶ STM16 rate is: 2488.32 Mbit/s

SYNCHRONOUS DATA HIERARCHY 5/6

The benefit is :

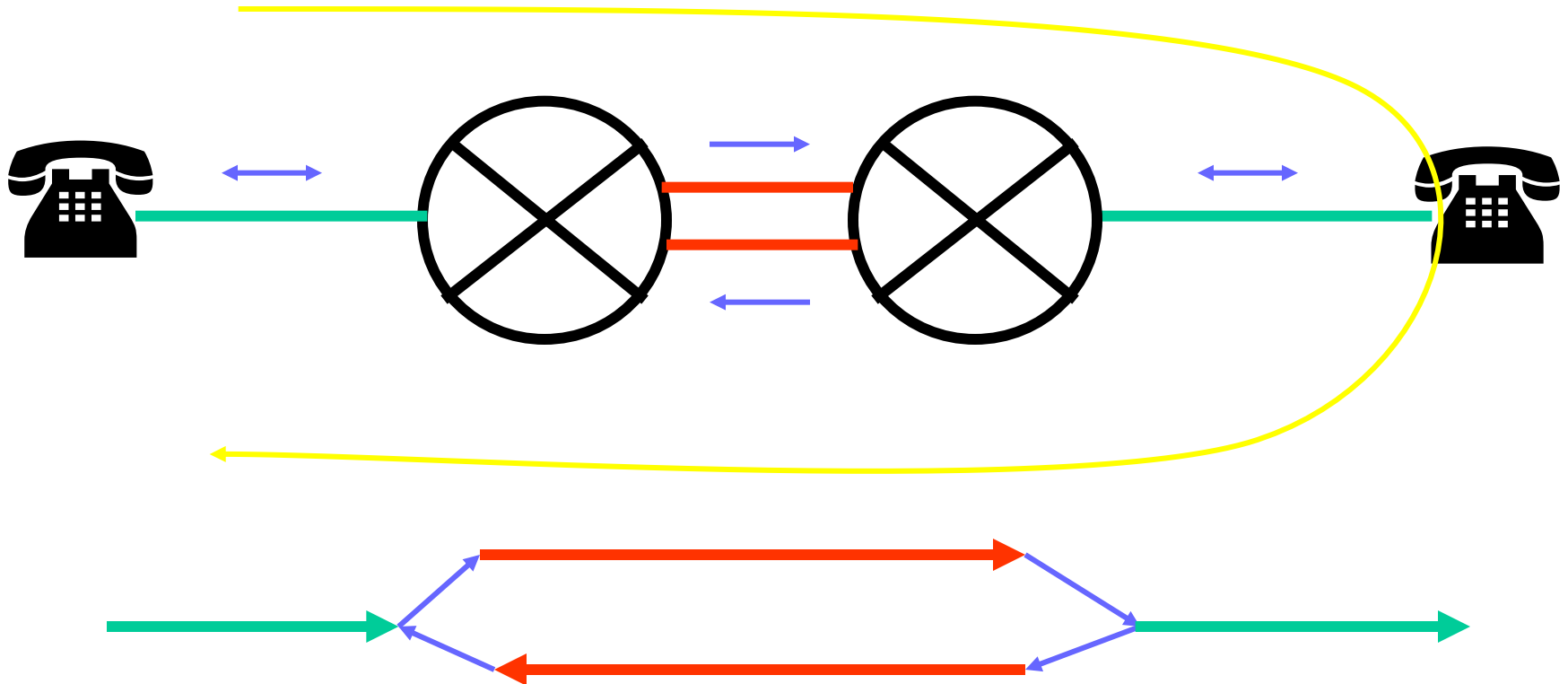
- ▶ to multiplex a plesiochronous and synchronous traffic
- ▶ to multiplex E1 and T1
- ▶ to extract an E1 in a STM16
- ▶ Very flexible

SYNCHRONOUS DATA HIERARCHY



ECHO EFFECT 1/2

In a long distance network a echo effect appears

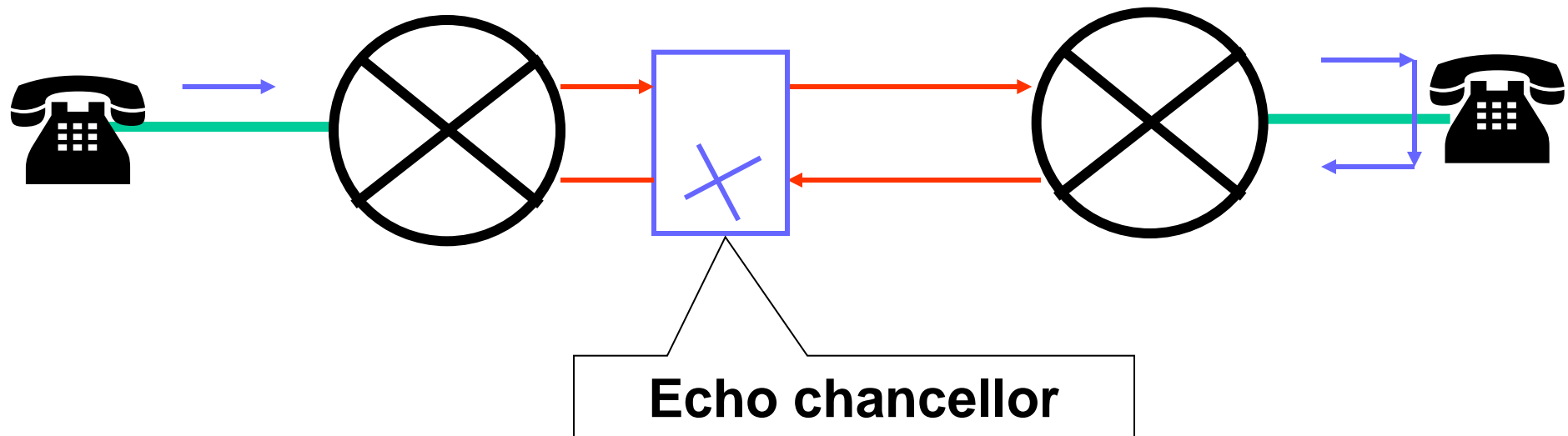


ECHO EFFECT 1/2

- ▶ **The voice signal is on one wire at the phone level**
- ▶ **When the voice signal arrives at the destination. It is returned to the origin and overlaid with the “normal” voice signal**

ECHO EFFECT 1/3

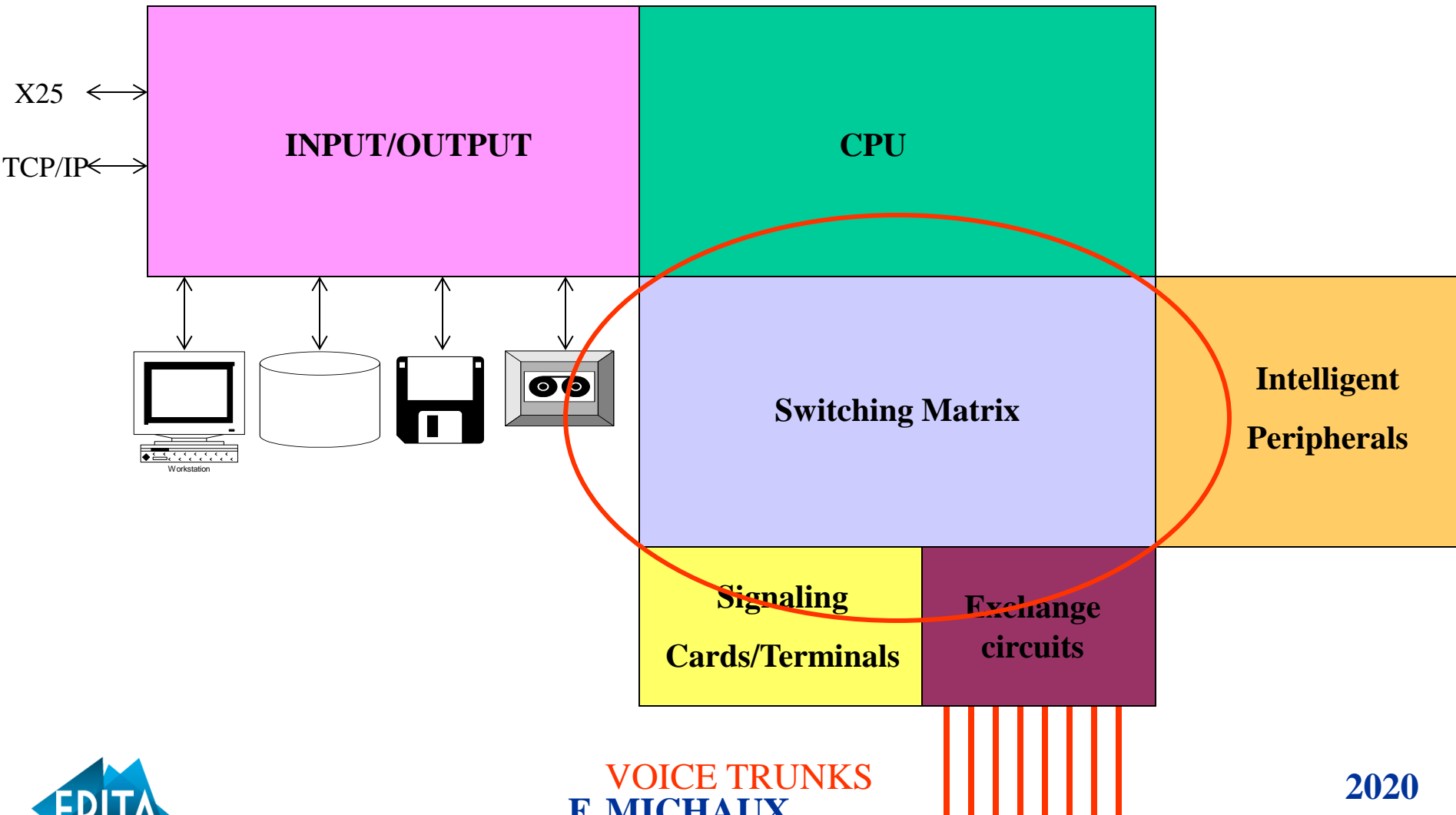
The solution consist of introducing an Echo cancellor



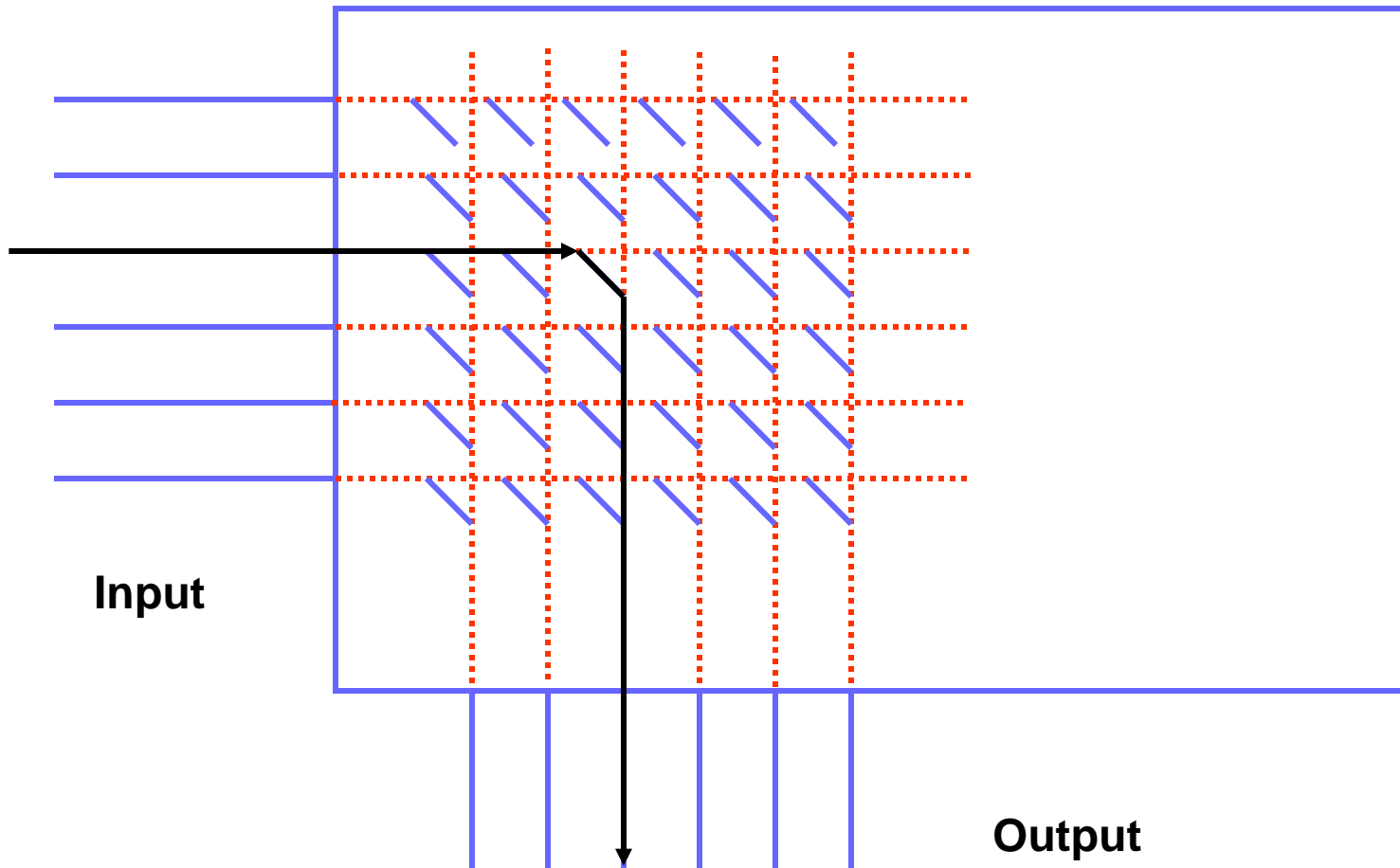
The echo cancellor memories the signal and cancels it at the return

Switching Matrix

MAIN SWITCH COMPONENTS



SWITCHING MATRIX



Switching Matrix Principle
F. MICHAUX

SWITCHING MATRIX



The switching matrix is controlled by the CPU



The switching matrix is named for the DMS “ENET” and “Group Switch or GSS” for the AXE 10.

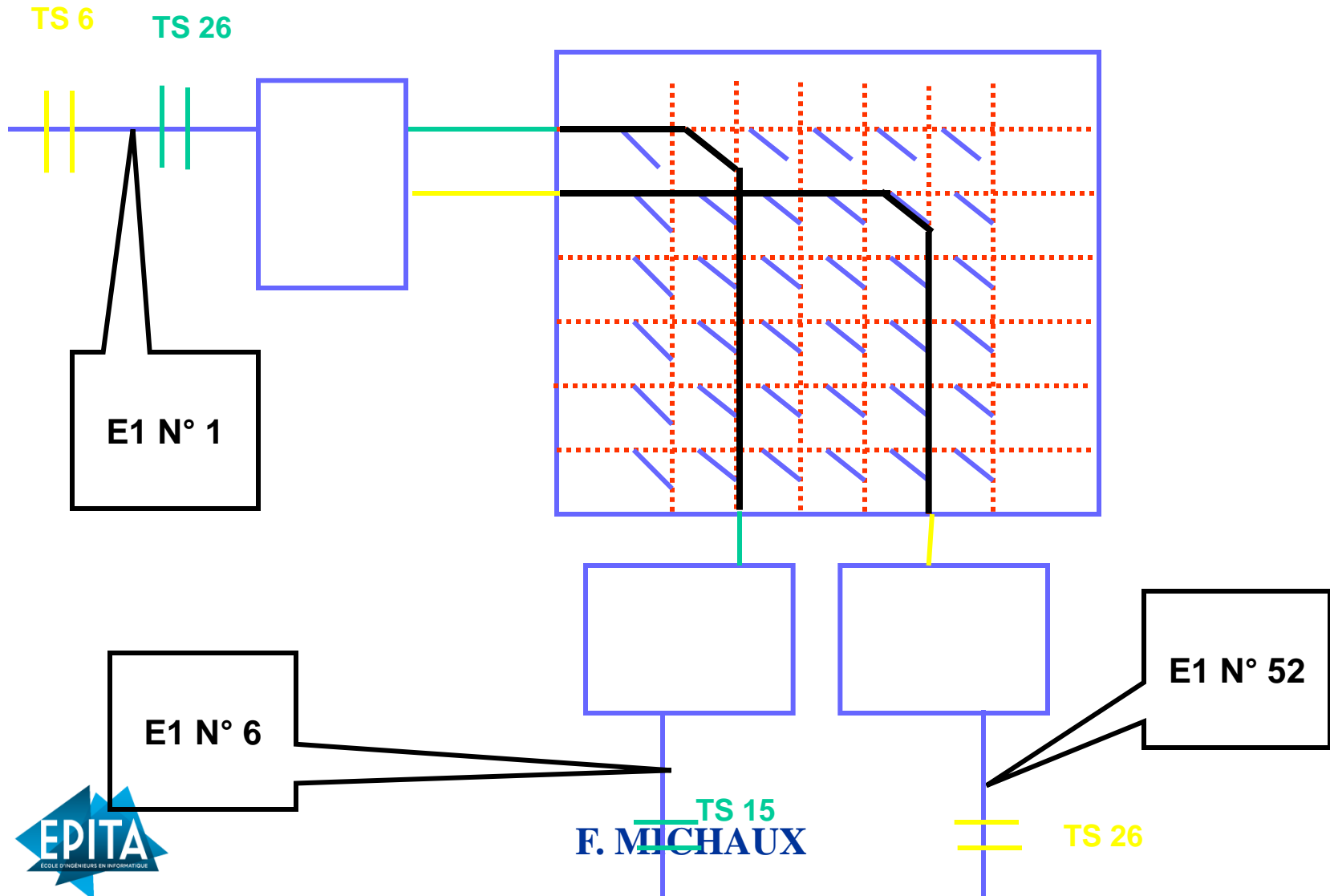
SWITCHING MATRIX

The size of a switching is calculated as the following:

- ▶ 1 E1 = 32 Time slot
- ▶ With 32 E1 you have $32 \times 32 = 1024$ cross connections
- ▶ 32 E1 per 1K of Switching Matrix
- ▶ Example a switch with 16 k will have a maximum of $16 \times 32 = 512$ E1.

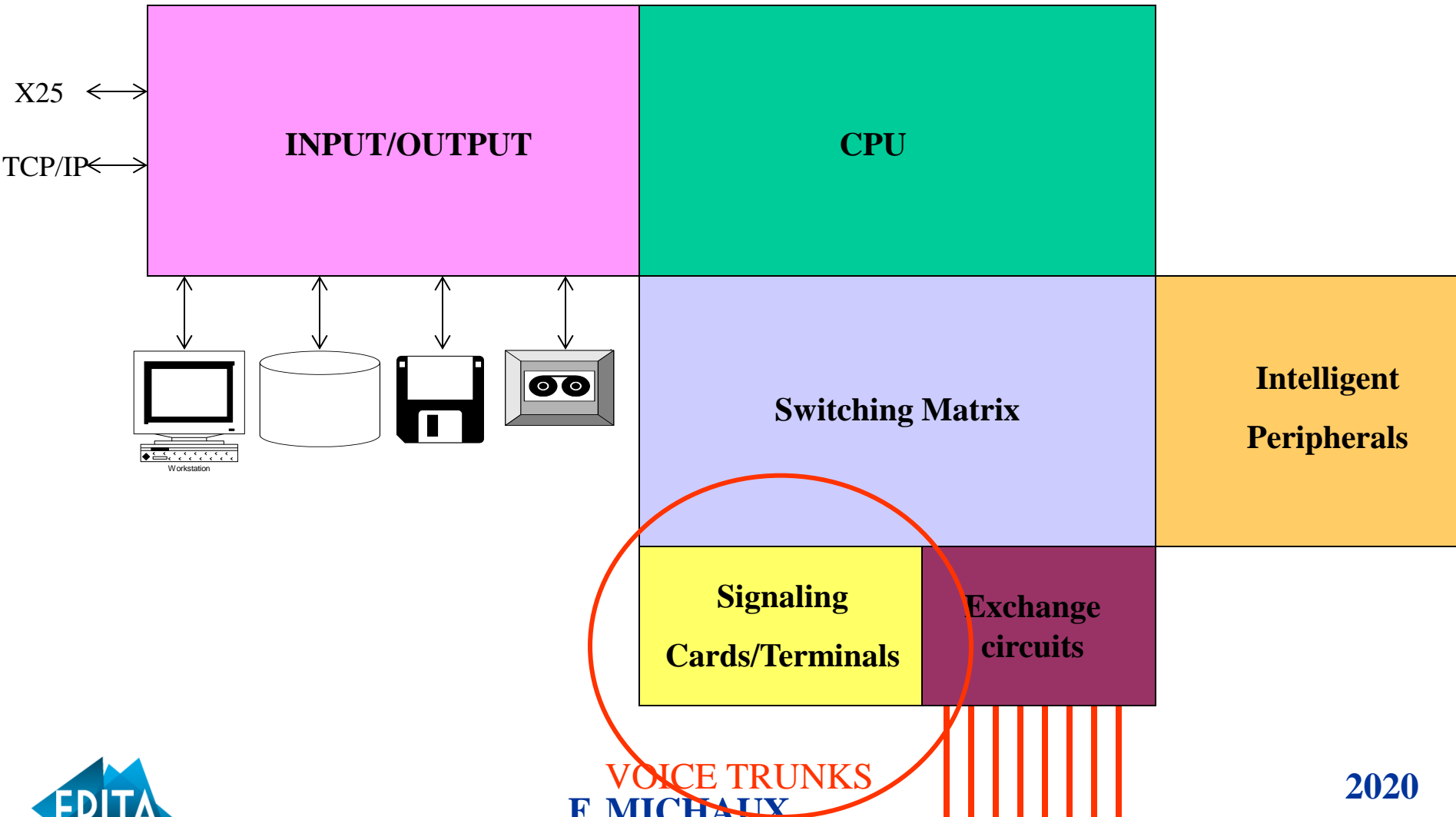
SWITCHING MATRIX PROBLEMATIC

The E1 links have to be synchronised between them.



Signaling

MAIN SWITCH COMPONENTS



SIGNALING

The signaling allow to exchange information between nodes.

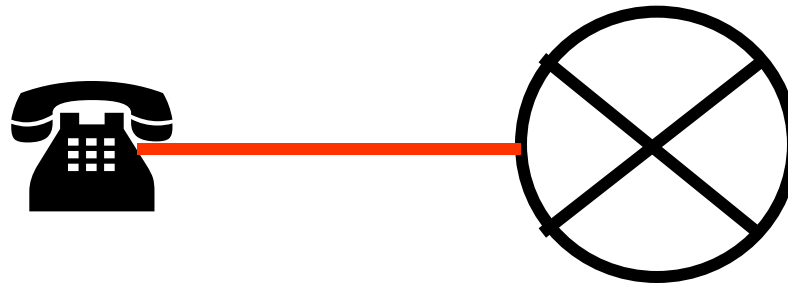
There is several kind of signaling

- ▶ Signaling circuit associated : eg : ISUP, ISDN, R2...
- ▶ Signaling non circuit associated : eg : INAP (for added value services IN), MAP (for mobility GSM or PCS network).

CIRCUIT SIGNALING ASSOCIATED

User to Network Interface

- ▶ USER signaling UNI (User to Network Interface) :
(eg DTMF) between a analogic phone and a public switch



CIRCUIT SIGNALING ASSOCIATED

User to Network Interface

- ▶ USER Signaling UNI (User to Network Interface) : between public and private switch PABX e.g. ISDN, R2.



CIRCUIT SIGNALING ASSOCIATED

User to User Interface

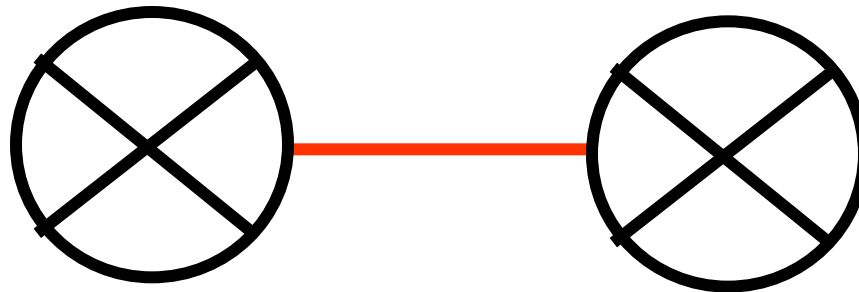
- ▶ User to User Interface: (eg QSIG, DPNSS,..) between two PABX.



CIRCUIT SIGNALING ASSOCIATED

Network to Network Interface

- ▶ Network Signaling : NNI (Network to Network Interface) between public switch e.g. R2, TUP, ISUP..



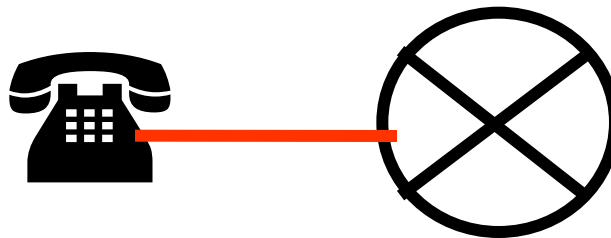
CIRCUIT SIGNALING ASSOCIATED

Signaling between an analogic phone and a public switch



Two Signaling exists

- by pulse
- by dual tone multi frequency **DTMF**



CIRCUIT SIGNALING ASSOCIATED

Signaling by pulse



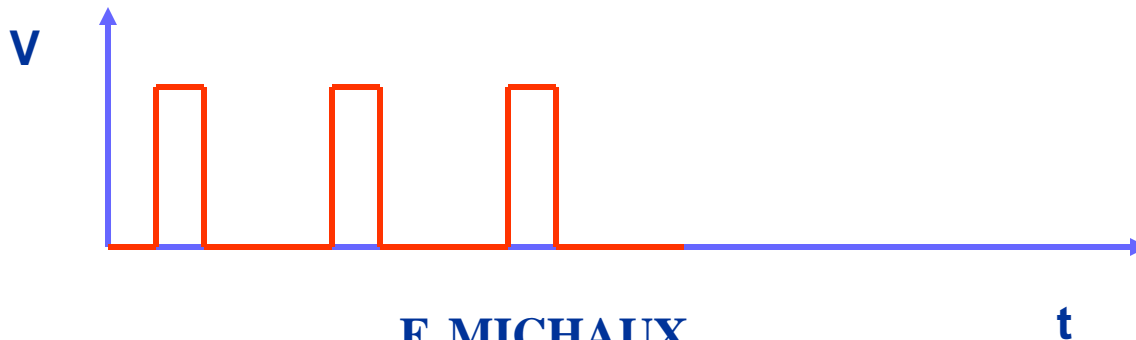
Used in the past when the phone was mechanic

Dial 10 => 10 pulse on the line

Dial 9 => 9 pulse on the line

Dial 1 => 1 pulse on the line.

Example 3 is dialled



CIRCUIT SIGNALING ASSOCIATED

Signaling by pulse

- ▶ This solution was used when the phones were mechanic
- ▶ Very slow 1s per digit
- ▶ It was possible to dial only digits and not (*,#,..)

CIRCUIT SIGNALING ASSOCIATED

Signaling by Dual Tone MultiFrequency



The phone has a kind of modem which is able to generate 8 different frequencies. 2 among 8 are chosen to dial a digit

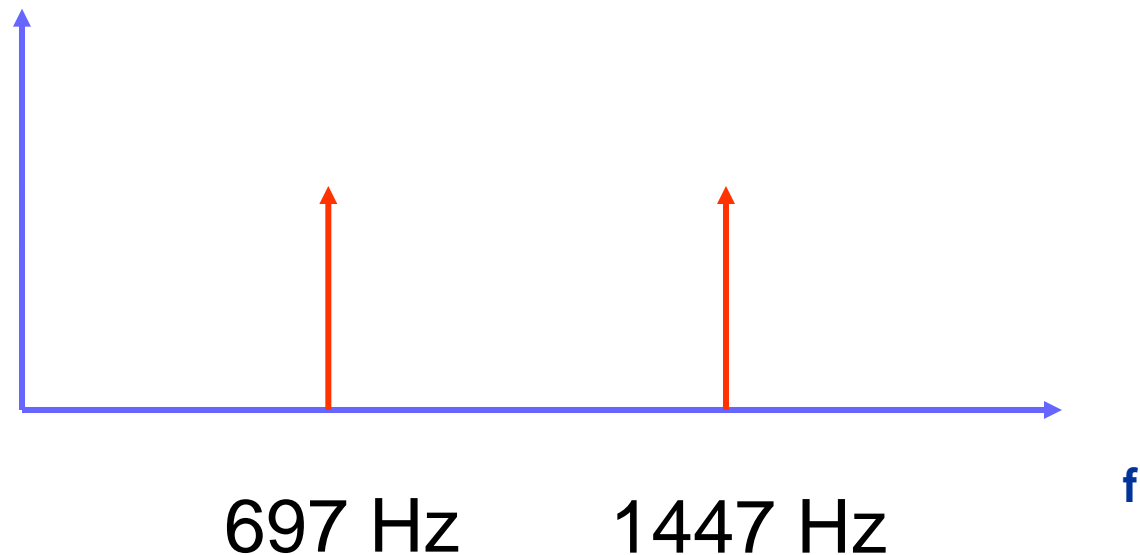
	1 209 Hz	1 336 Hz	1 447 Hz	1 633 Hz
697 Hz	1	2	3	A
770 Hz	4	5	6	B
852 Hz	7	8	9	C
941 Hz	*	0	#	D

CIRCUIT SIGNALING ASSOCIATED

Signaling by Dual Tone MultiFrequency

- ▶ The both frequencies are sent simultaneously

Example 3 is dialled



CIRCUIT SIGNALING ASSOCIATED

Signaling by Dual Tone MultiFrequency

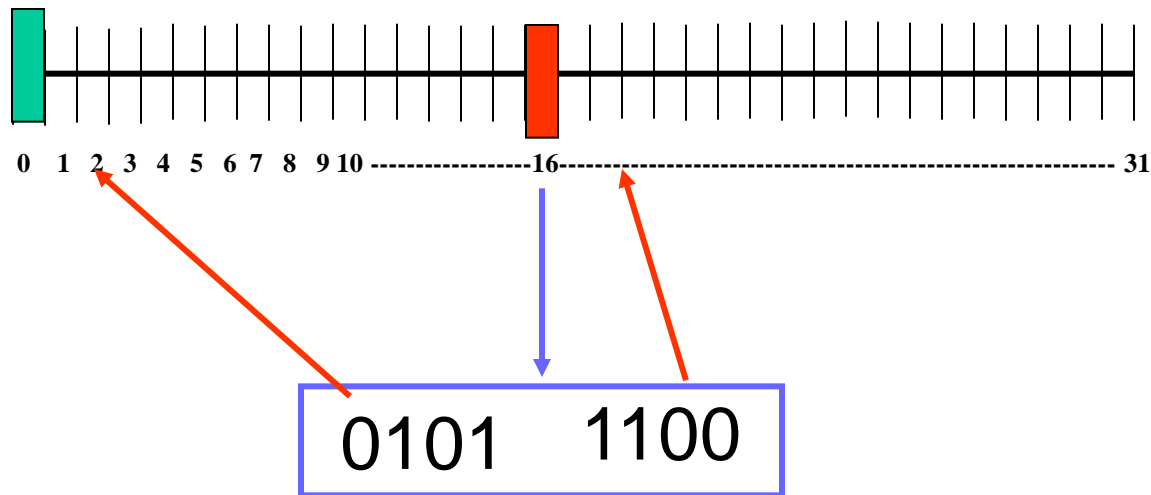
- ▶ This solution is quicker than the previous one
- ▶ It's possible to dial other character (*,#,A,B..)
- ▶ This solution is better but is still very poor

CIRCUIT SIGNALING ASSOCIATED

CAS Signaling



CAS Means Channel Associated Signaling



CIRCUIT SIGNALING ASSOCIATED

CAS Signaling

- ▶ The 4 highest bits of the time slot 16 are used for signaling the time slot 1 to 15
- ▶ The 4 lowest bits of the time slot 16 are used is used for signaling the time slot 17 to 31
- ▶ At the time the TS 16 give the signaling of the TS 1 and TS 17. 125 μ s later the TS 16 give the signaling of the TS 2 and TS 18

CIRCUIT SIGNALING ASSOCIATED

CAS Signaling

- ▶ The TS 16 give the state of the circuit e.g. : sleep, hang up..
- ▶ The numbering is sent by frequencies inside the circuit as the DTMF but the frequencies are different

CIRCUIT SIGNALING ASSOCIATED

CAS Signaling

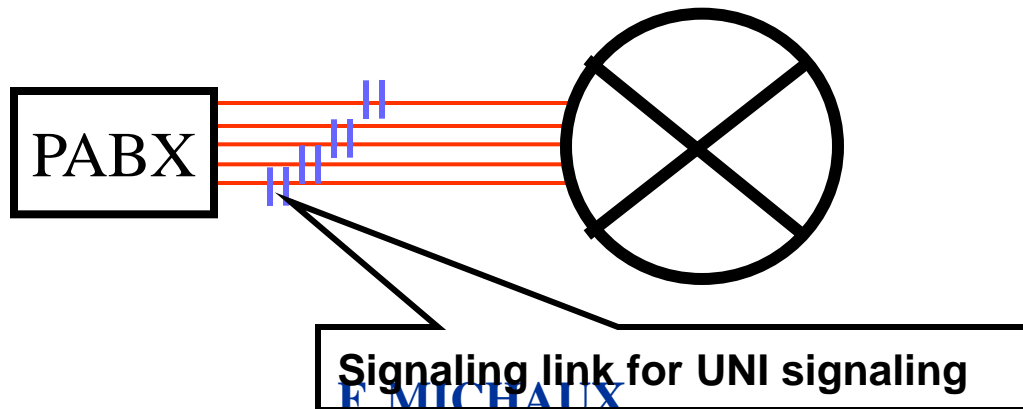
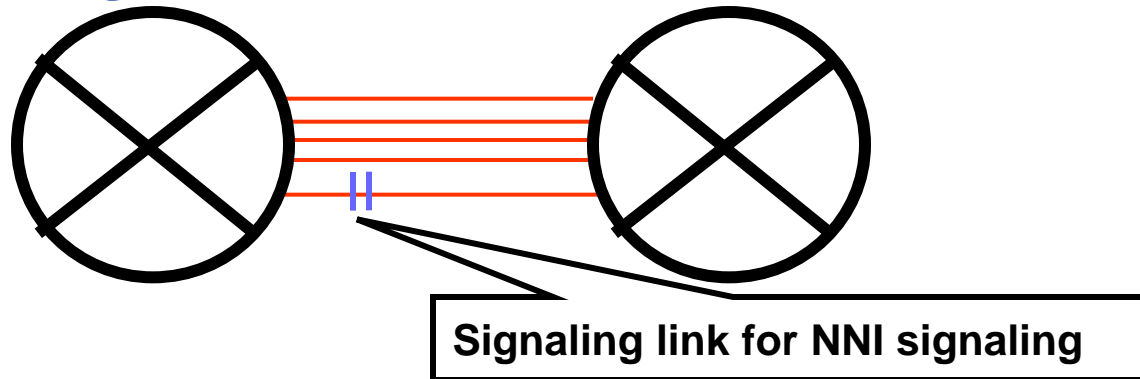
- ▶ **This signaling is a UNI and NNI signaling**
- ▶ **This signaling is very rich**
- ▶ **R1, R2 are an example of CAS signaling**
- ▶ **Only one default very slow**

CIRCUIT SIGNALING ASSOCIATED

CCS Signaling

▶ CCS Means Common channel signaling

▶ A signaling link has a rate of 64 Kb/S



CIRCUIT SIGNALING ASSOCIATED

CCS Signaling

- ▶ **The signaling channel is common for several circuit.**
- ▶ **The CCS signaling is in message mode: ISDN for UNI signaling, TUP, ISUP.. For the NNI signaling**
- ▶ **In the UNI signaling one signaling link per E1 in the timeslot 16 named D channel.**

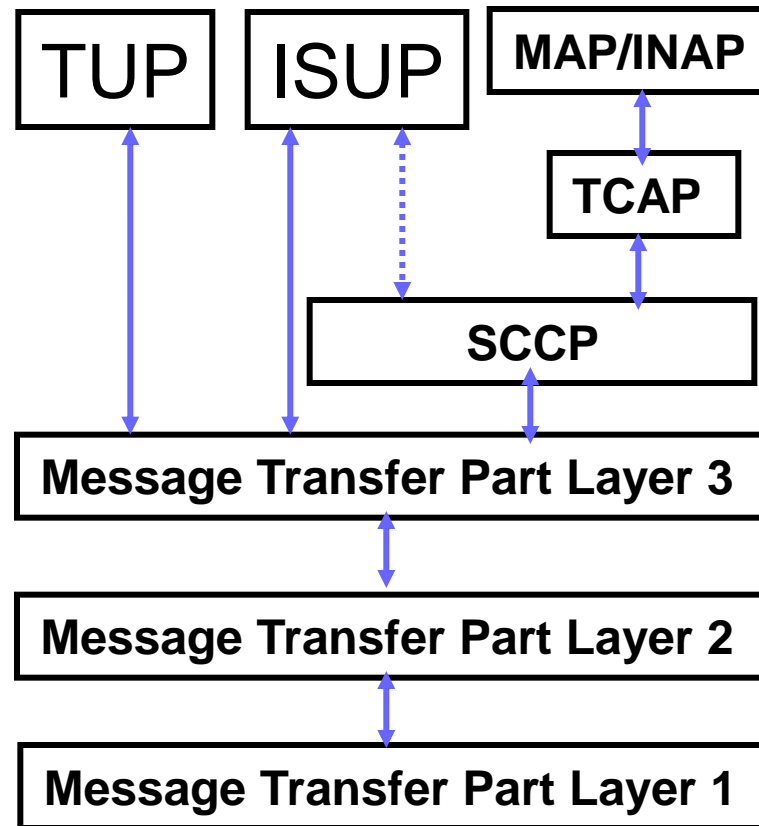
CIRCUIT SIGNALING ASSOCIATED

CCS Signaling

- ▶ **The CCS Signaling is named signaling N°7, it's a message mode signaling.**
- ▶ **The protocols are different at UNI and NNI level**
UNI : ISDN
NNI : ISUP
- ▶ **The benefits of the SS7 signaling are :**
 - **A better efficiency, the Post Dial Delay (PDD) decreases from 10/20 s in CAS signaling to 2/4 s consequence economy of ressources.**
 - **Mandatory for added value services and supplementary services.**

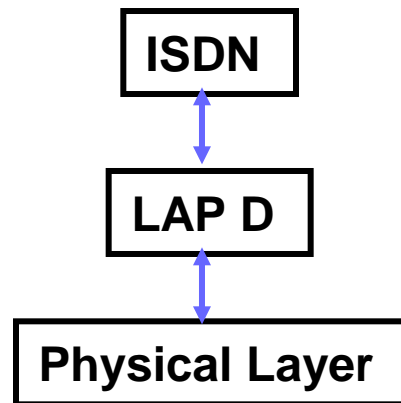
SIGNALING SS7

NNI Signaling N°7 layers description



SIGNALING SS7

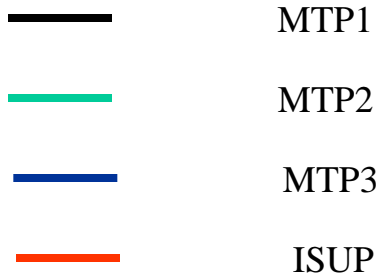
UNI Signaling N°7 layers description



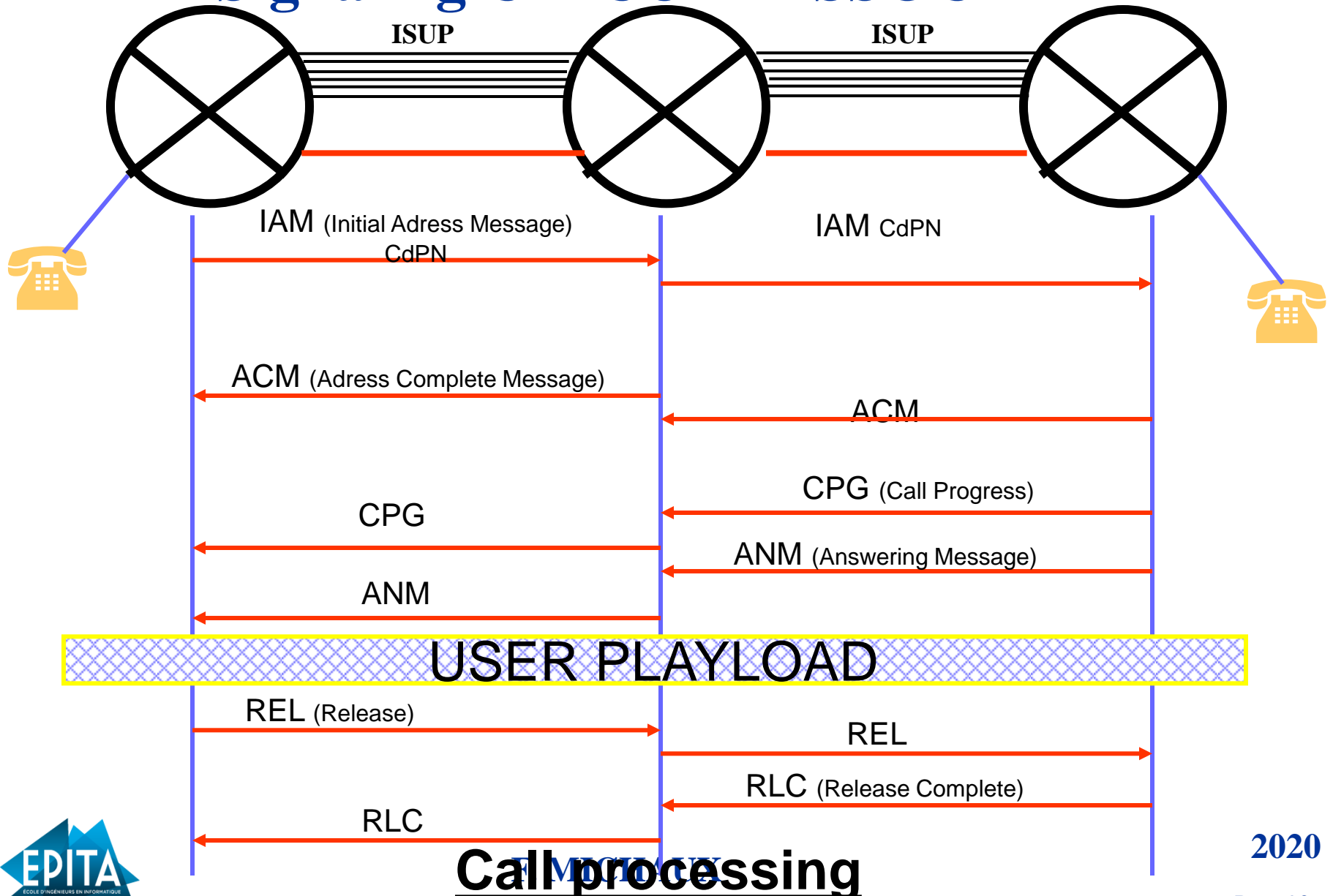
SIGNALING SS7

EXAMPLE OF ISUP MESSAGE

CIC 12 bits

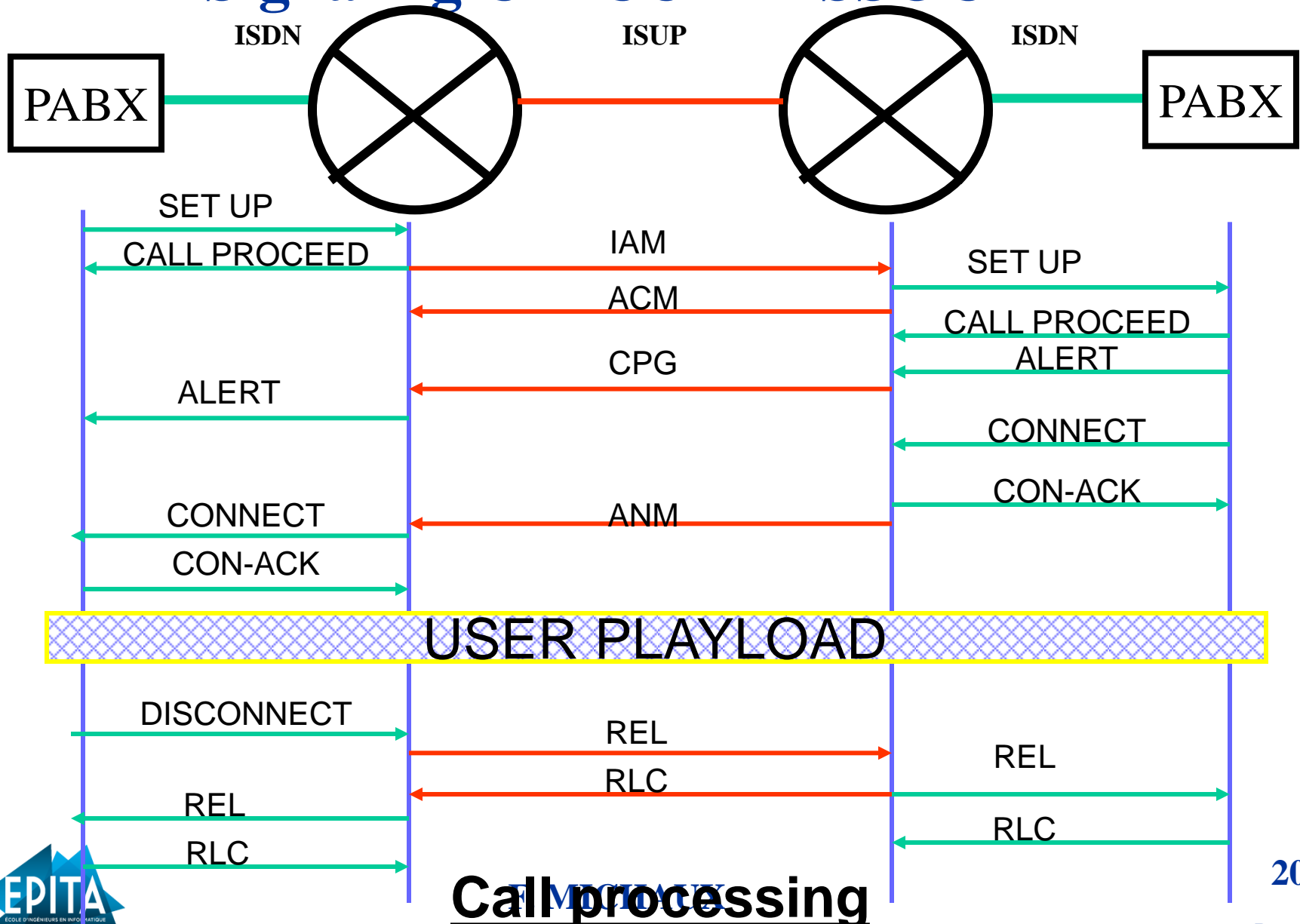


Signaling CIRCUIT ASSOCIATED

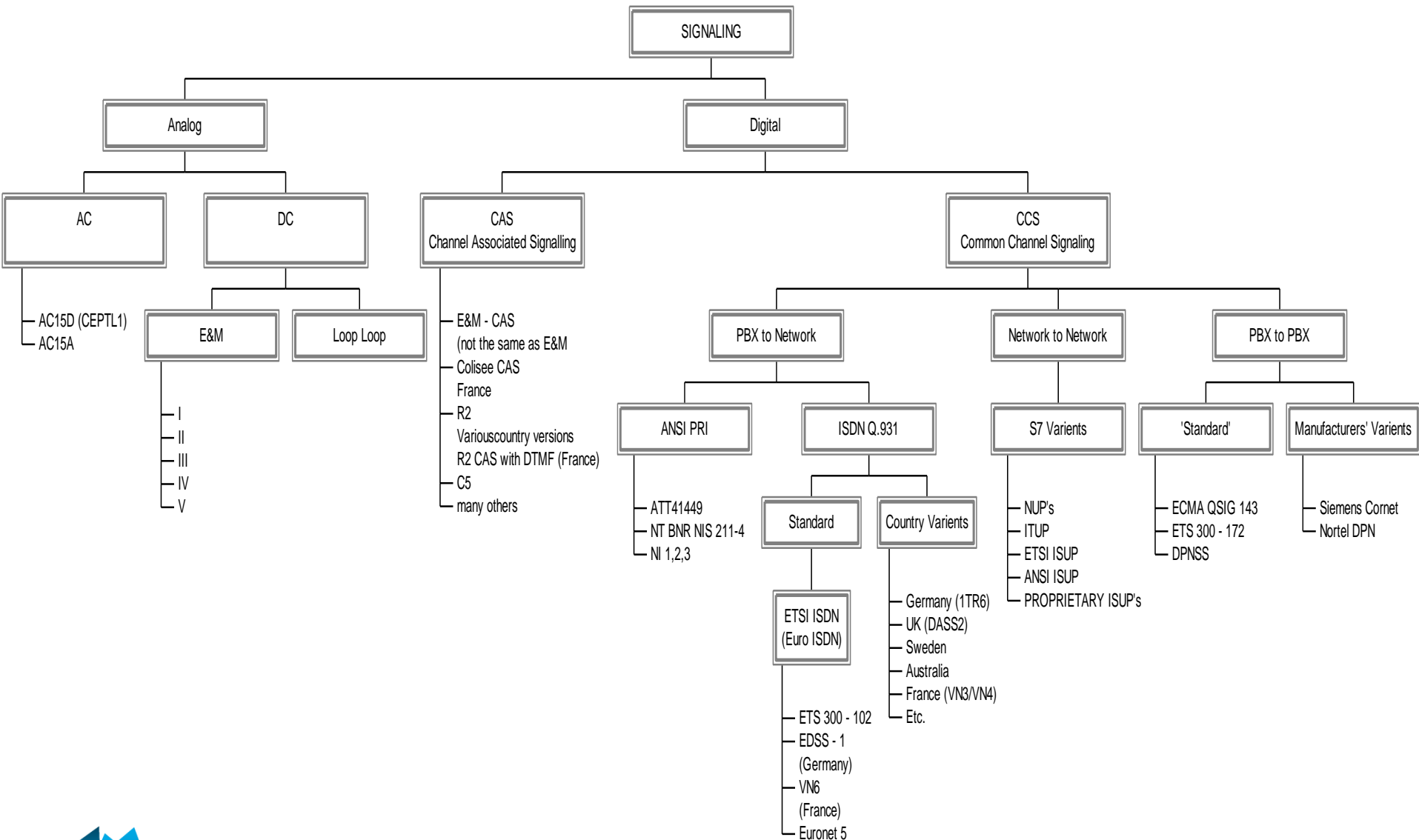


Call processing

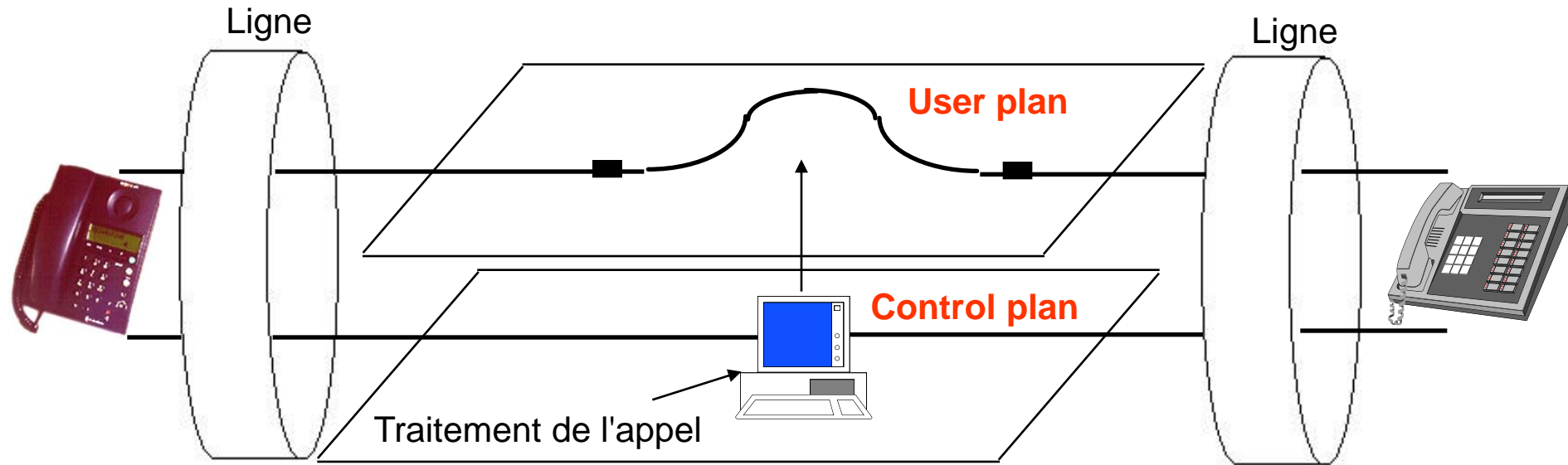
Signaling CIRCUIT ASSOCIATED



Signaling CIRCUIT ASSOCIATED



Control plan / User plan 1/7

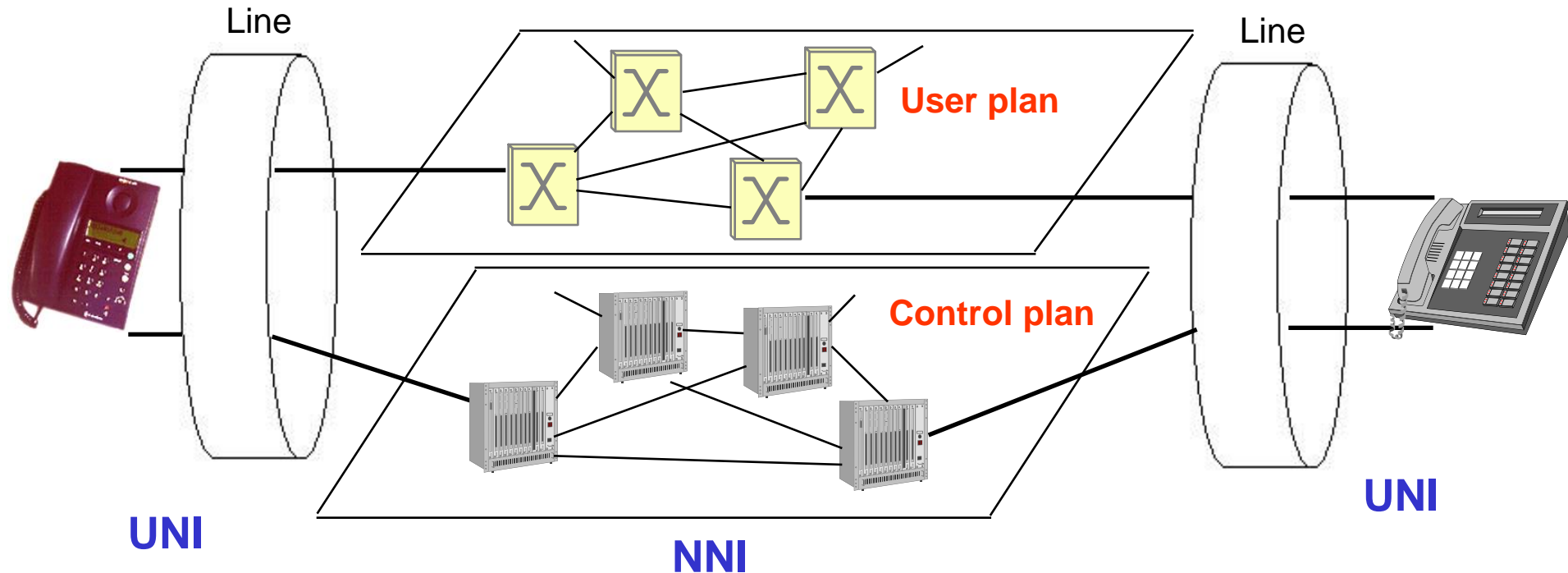


Control Plan : In charge to establish the connexion

User Plan : In charge to connect the voice ressources

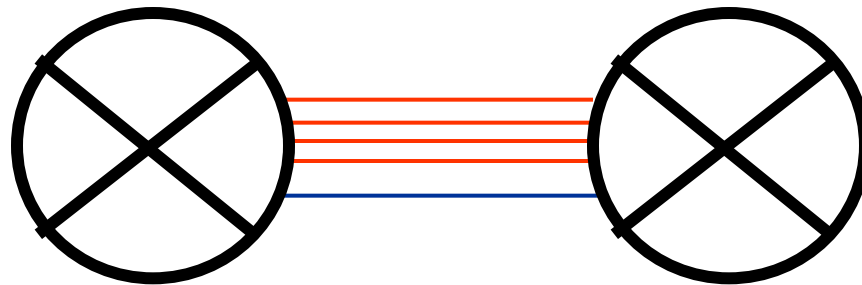
➡ **the both networks are parrallele**

Control plan / User plan 2/7



It's a logical separation which can be also physical
with an overlay network

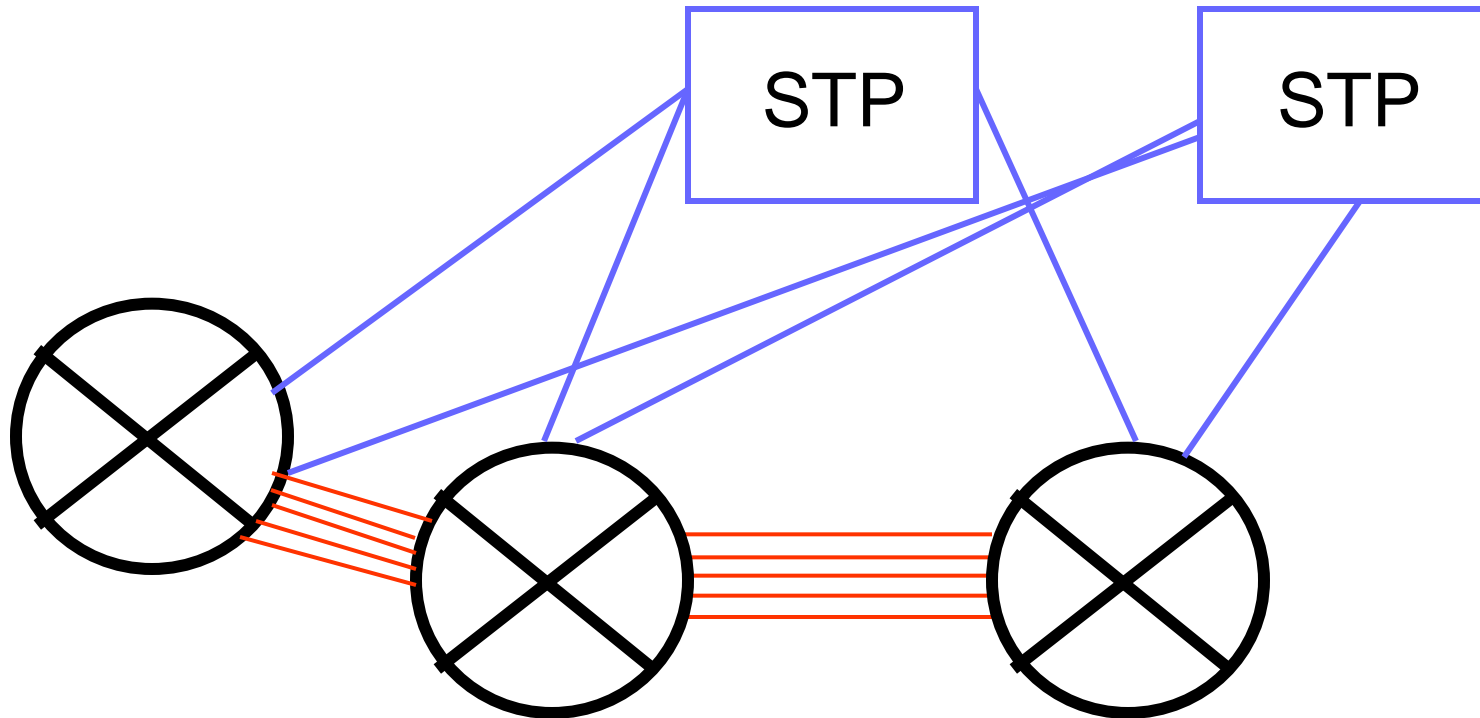
Control plan / User plan 3/7



Associated mode

The Signaling link is dedicated to one voice trunk

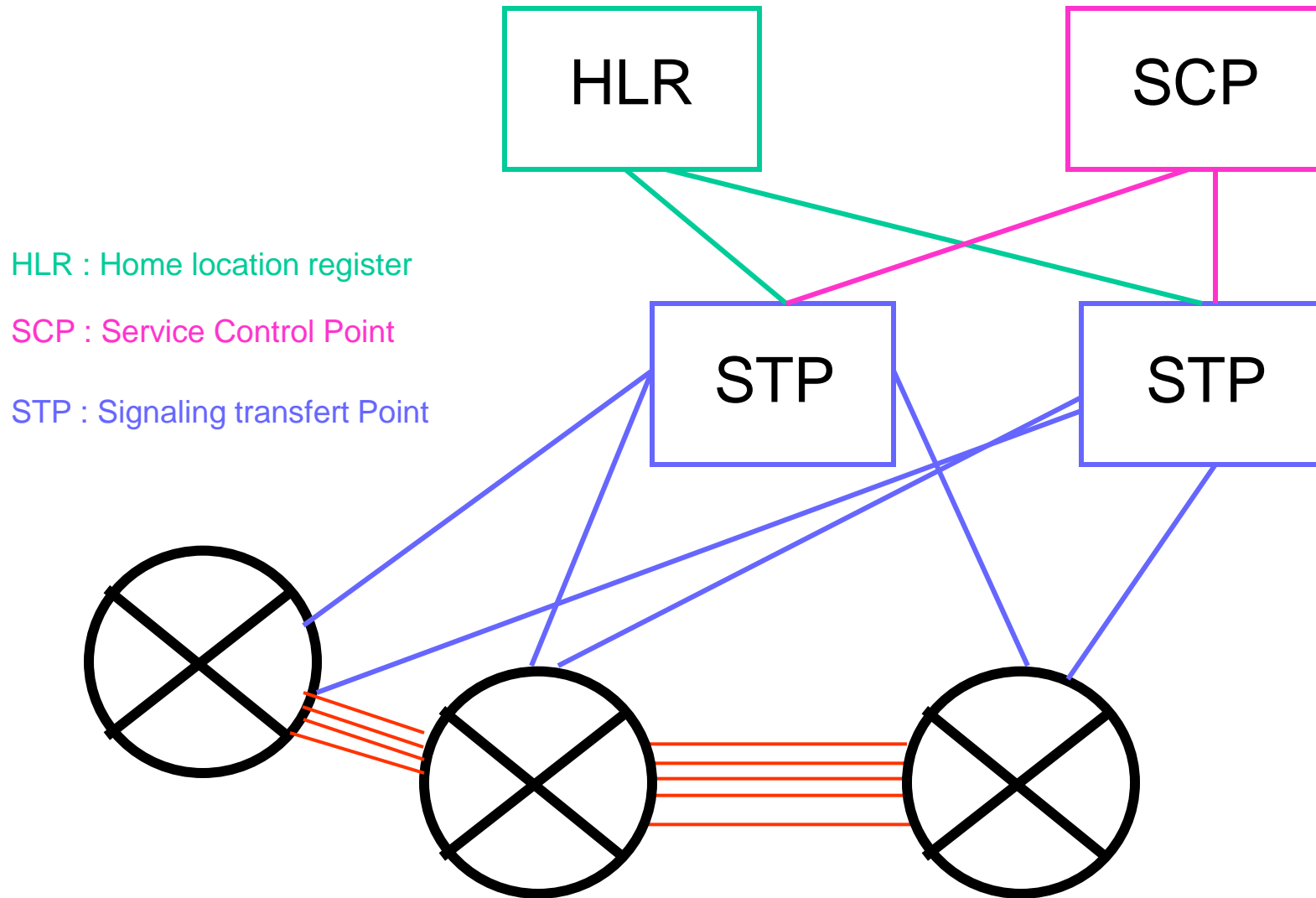
Control plan / User plan 4/7



Quasi Associated mode

The Signaling link is not dedicated to one voice trunk

Control plan / User plan 5/7




Control plan / User plan 6/7

link set dimensioning

 A link set dimensioning is a set of signaling links connected to the same signaling address.

 The link set dimensioning depends of the trunk group size. One signaling per 2000 circuits, they are duplicated for security reason.

 Example : 2000 circuits 2 signaling links
1000 circuits 2 signaling links
4000 circuits 4 signaling links

Control plan / User plan 7/7

Signaling link dimensioning

- ▶ **Signaling link economy.**
- ▶ **The traffic is centralized in the STP interesting for the monitoring.**
- ▶ **Mandatory to plug service added value platforms**

Free customer call in Roaming

HLR : Home location register

MSC : Mobile Switch Centre

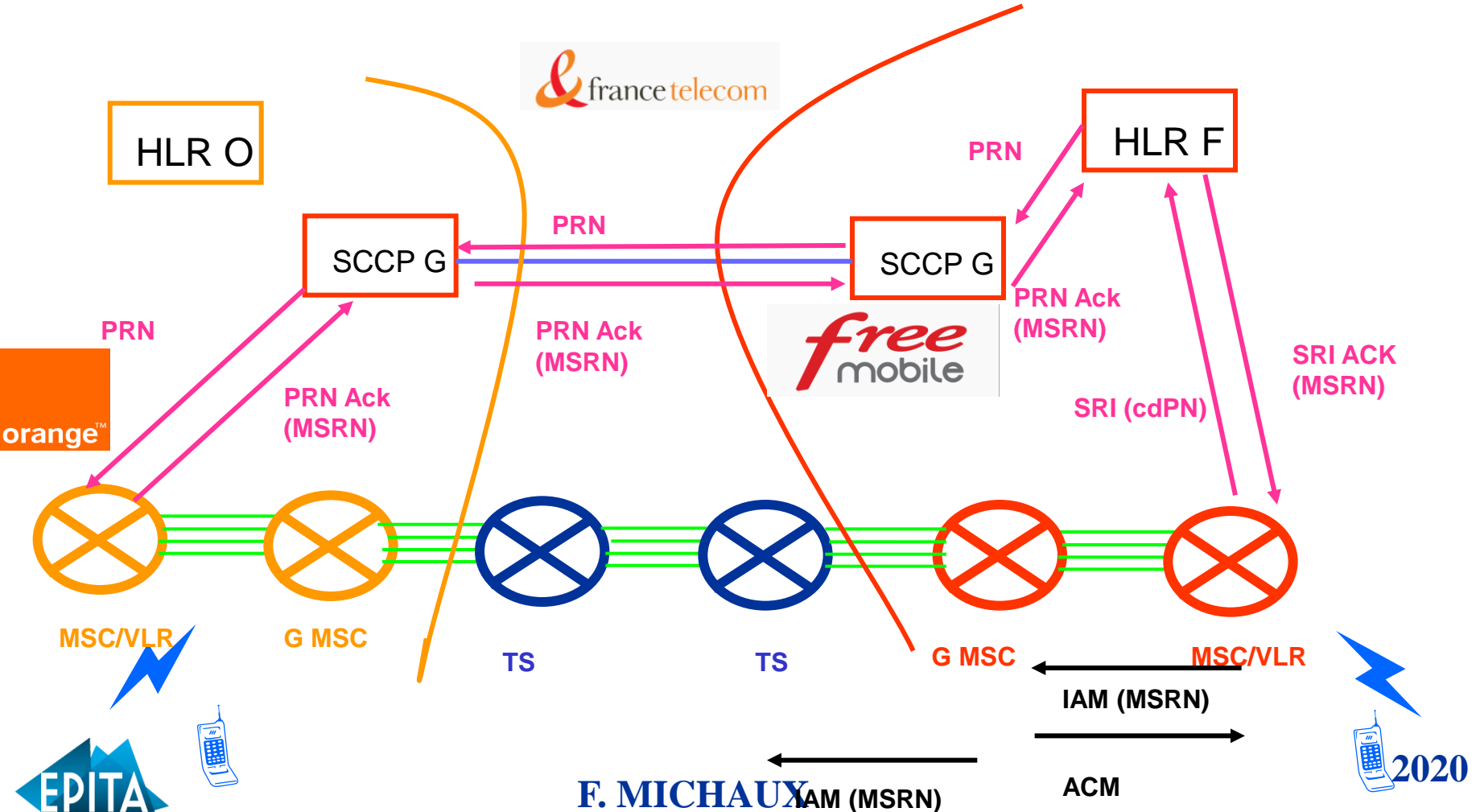
G MSC : Gateway MSC

SCCP G : Signalling Connection Control Part Gateway:

— SS7 : Signaling N° 7

SRI : Send Routing Information

PRN : Provide Roaming Number



F. MICHAUX

Free customer call in Roaming

HLR : Home location register

MSC : Mobile Switch Centre

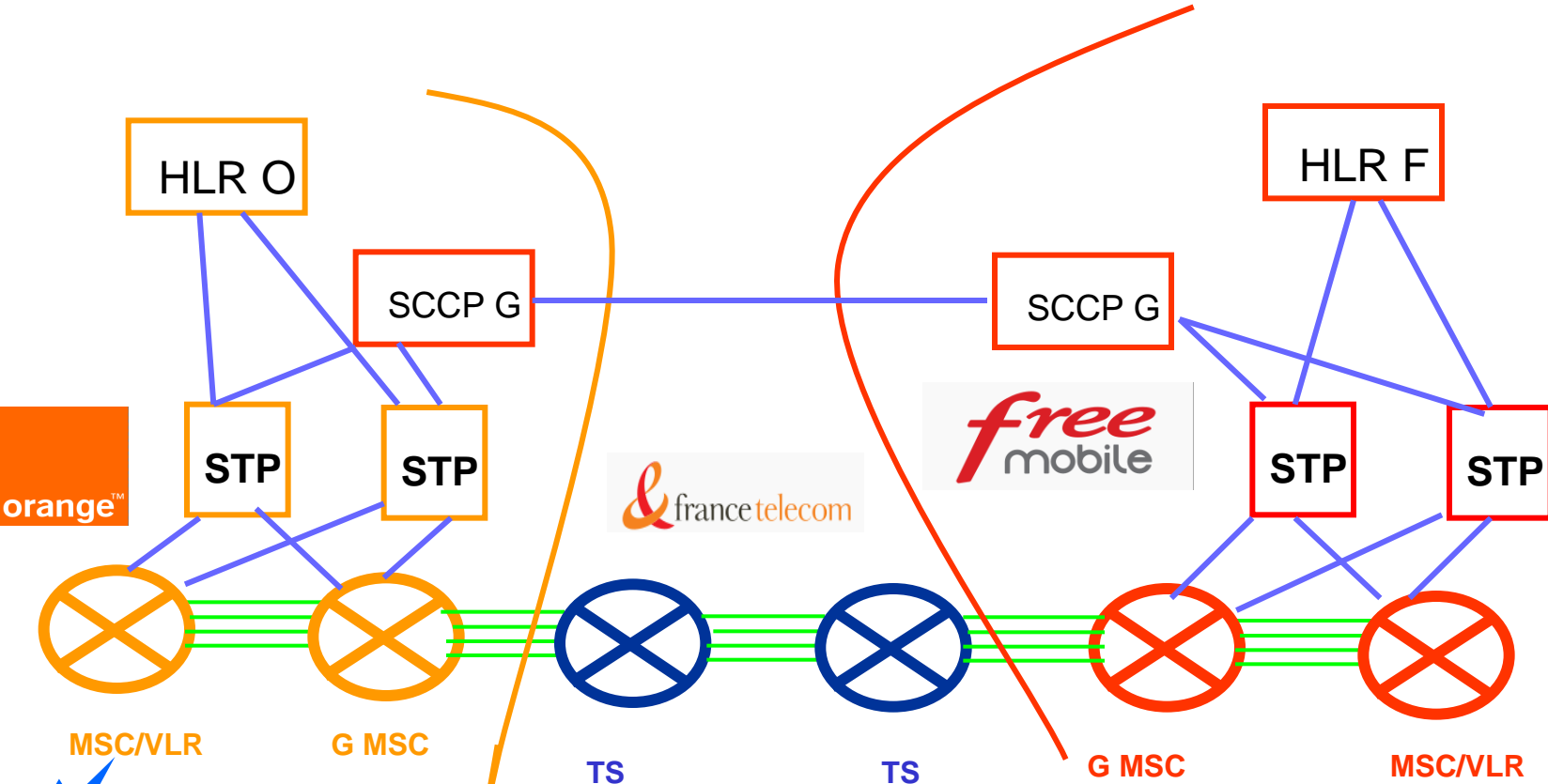
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Free customer call in Roaming

HLR : Home location register

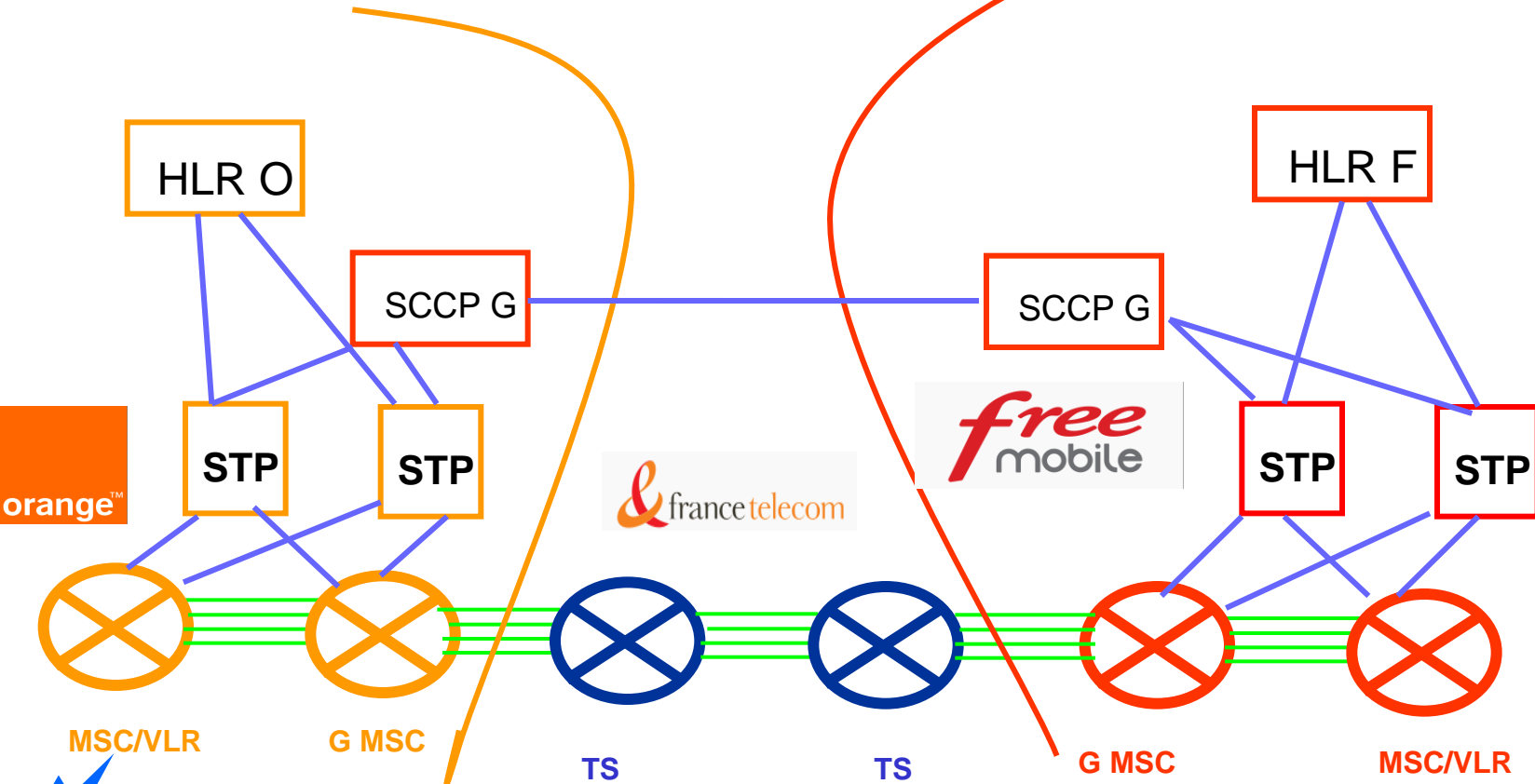
MSC : Mobile Switch Centre

G MSC : Gateway MSC

SCCP G : Signalling Connection Control Part Gateway:

SRI : Send Routing Information

PRN : Provide Roaming Number



“Les villes de Lyon, Grenoble, Angers et bien sûr Paris ont ont été touchées, entre autres. Hier soir, Orange a tenu à réagir en affirmant ne pas être à l’origine du problème : « Vu de notre fenêtre, tout est au vert. On pense savoir que Free a un problème sur un de ses équipements. Il y a eu un incident il y a déjà trois semaines. **Un équipement de signalisation de Free Mobile était en cause. On constate les mêmes symptômes aujourd'hui** », a expliqué un représentant de l’opérateur historique à 20 Minutes.”

Free customer call in Roaming

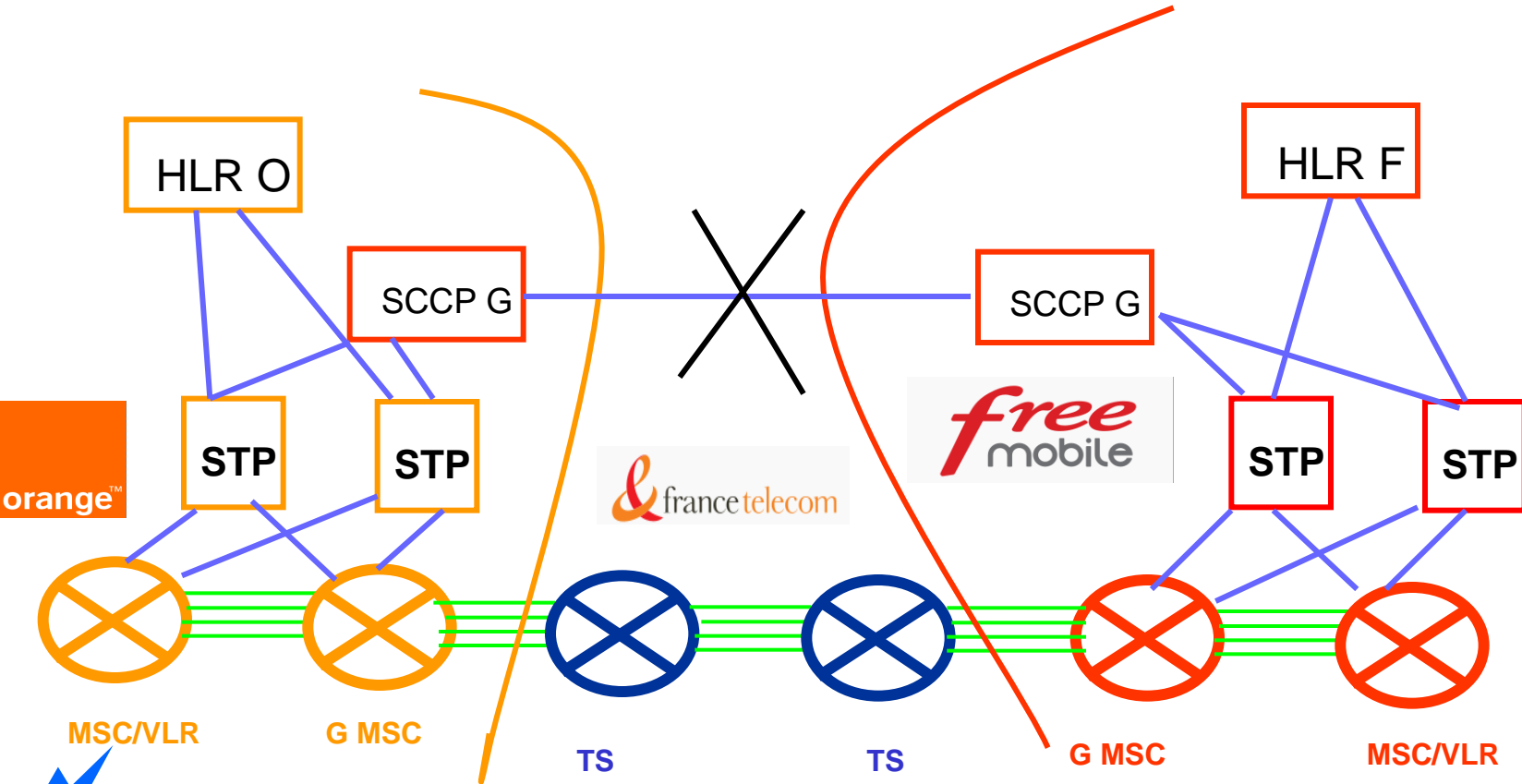
HLR : Home location register

MSC : Mobile Switch Centre

G MSC : Gateway MSC

SCCP G : Signalling Connection Control Part Gateway:

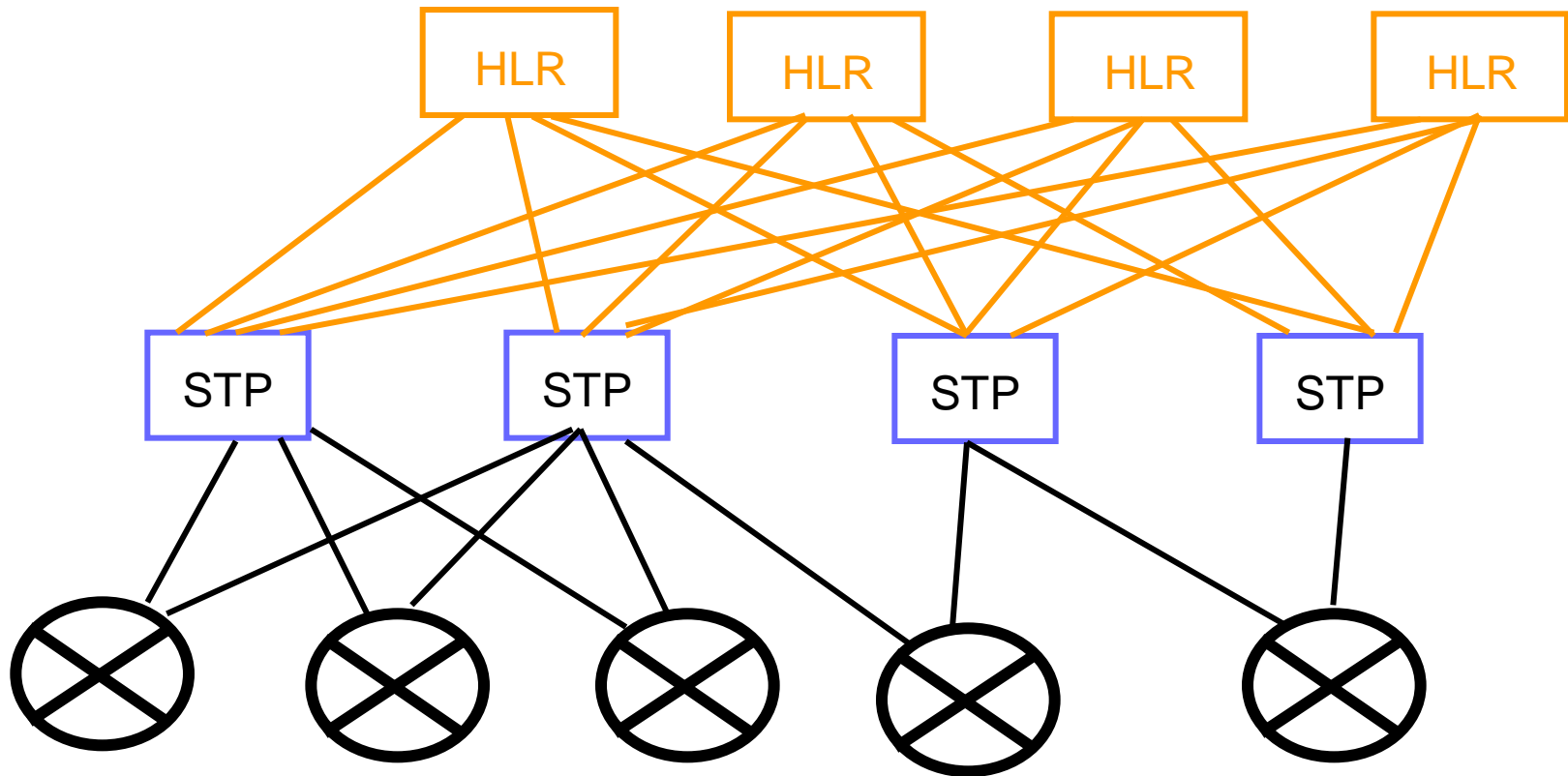
— SS7 : Signaling N° 7



HLR classi connection to the STP 's

HLR : Home location register

STP : Signalling Transfer Point

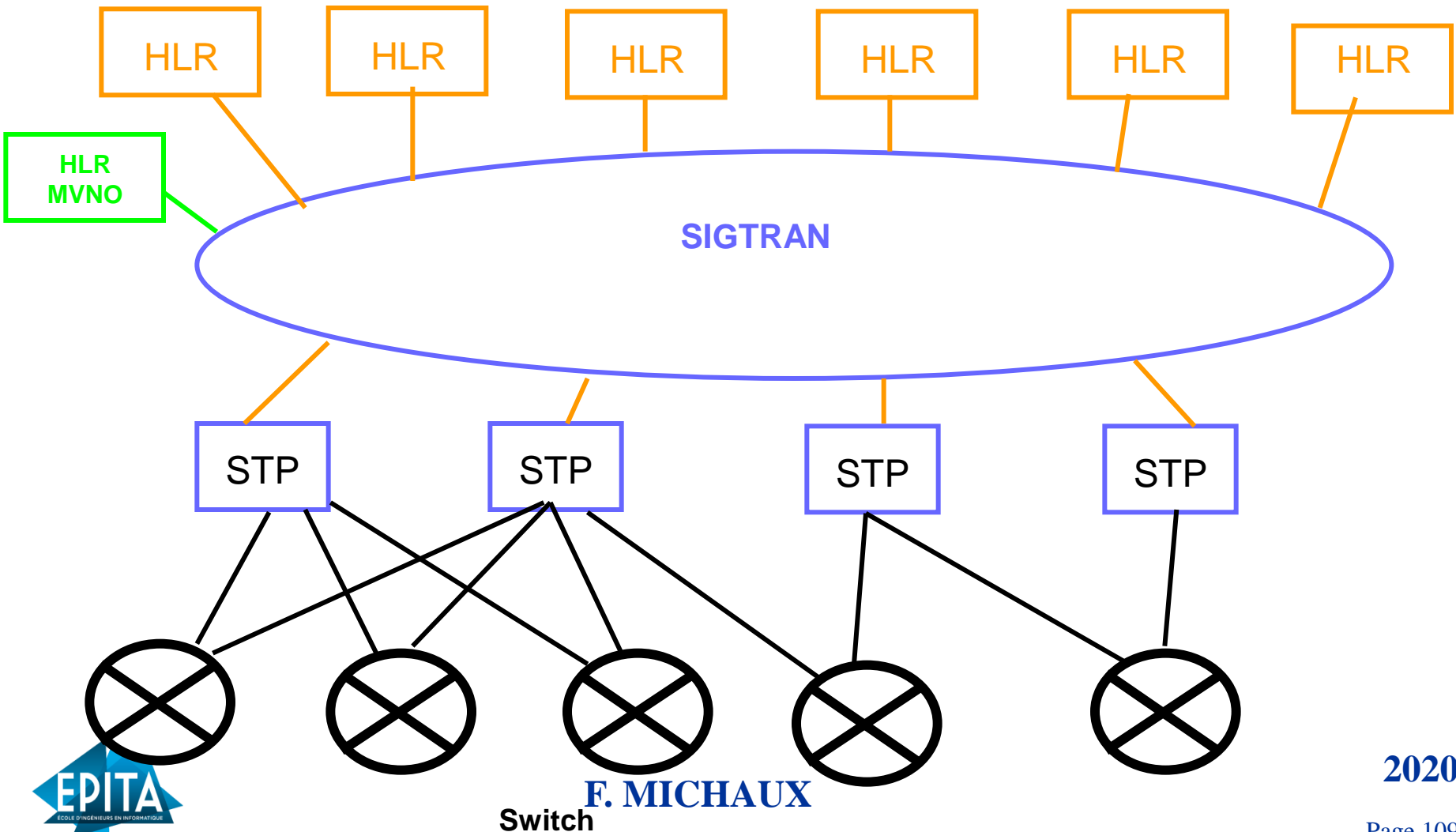


HLR connection to the STP's via Sigtran

HLR : Home location register

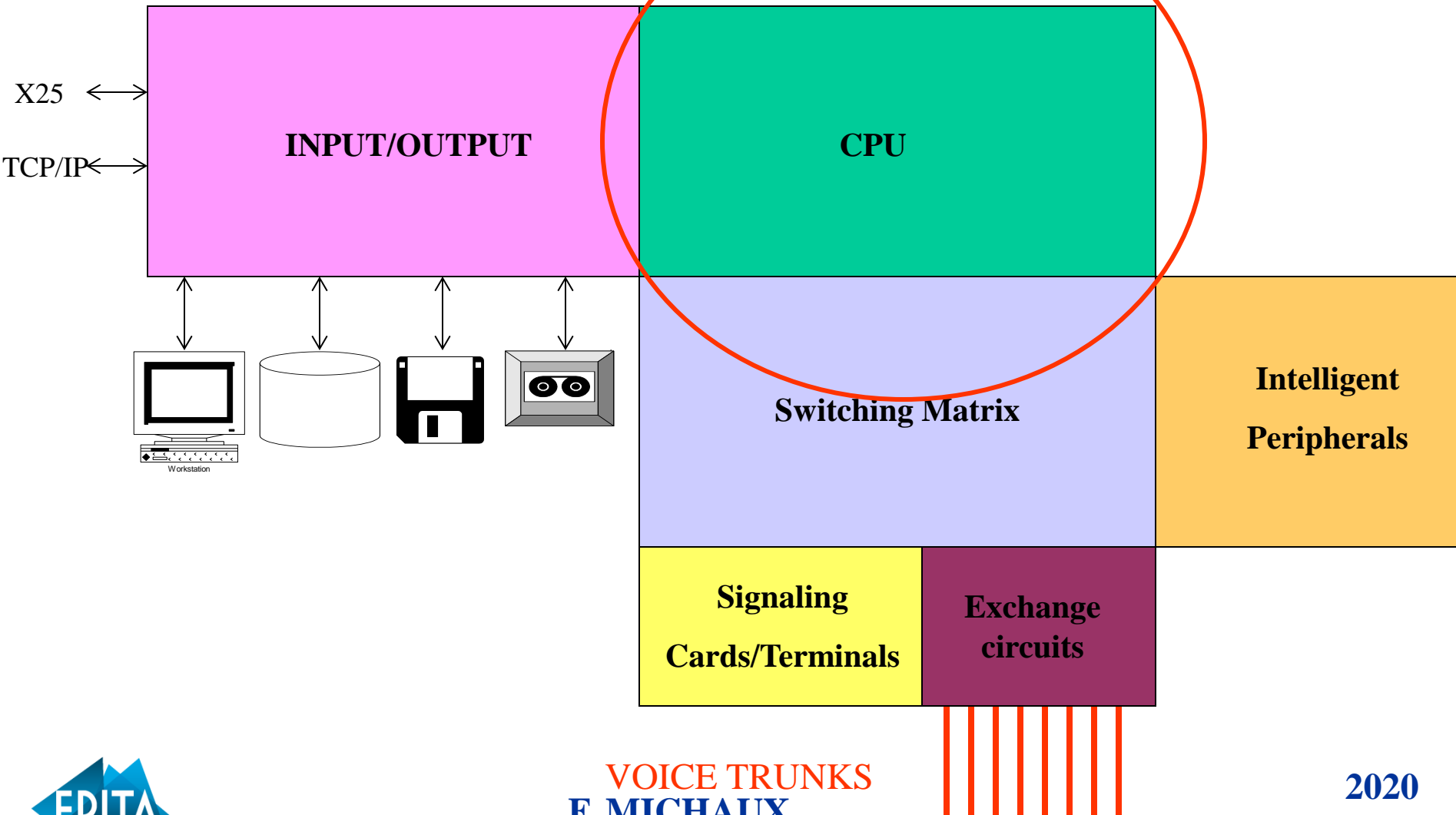
STP : Signalling Transfer Point

Sigtran : **Signaling transport** (infrastructure to carry SS7 signaling on an IP network)



CPU

MAIN SWITCH COMPONENTS



CPU

The CPU is the Central Processor Unit. It is the main switch component

The CPU :

- ▶ handles the call processing
- ▶ Controls the switching matrix
- ▶ Controls the intelligent peripherals
- ▶ Handles the translations
- ▶ Handles the signaling protocol from the network layer to the application layer.

CPU

- ▶ There is 2 CPU's in a switch in order to Increase the reliability.
- ▶ One active and one standby in case of failure
- ▶ There is no loss of call in case of channel change over from the active to the stand by
- ▶ The size of the software is huge
- ▶ It's a real time software each call launches a task.

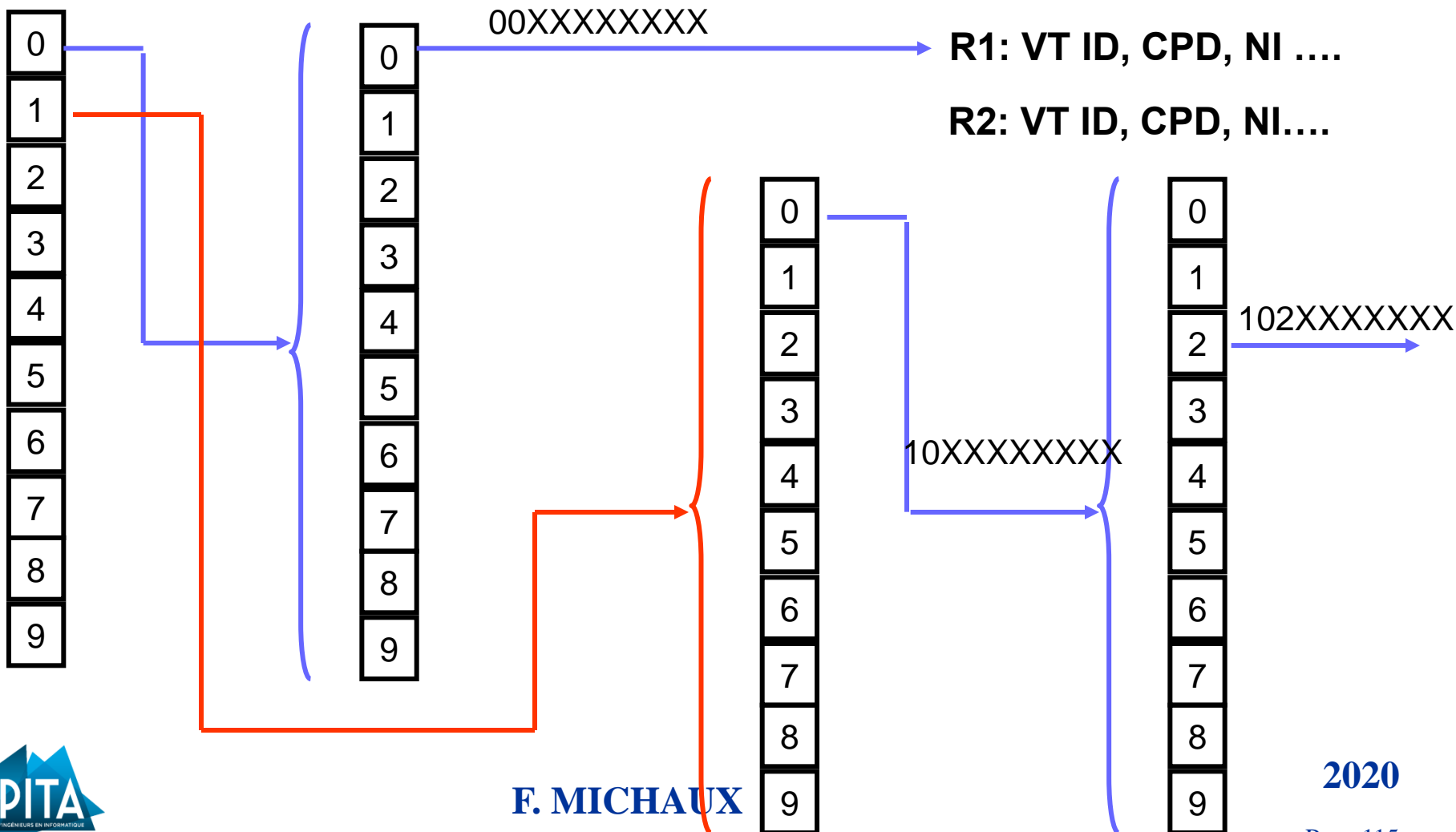
CPU

The CPU is dimensioned by the traffic handles by the switch at the peak hour

- ▶ The BHCA is the unity
- ▶ BHCA : Busy Hour Call Attempt
- ▶ The CPU size is linked to the switching matrix size and the type of traffic. IN traffic

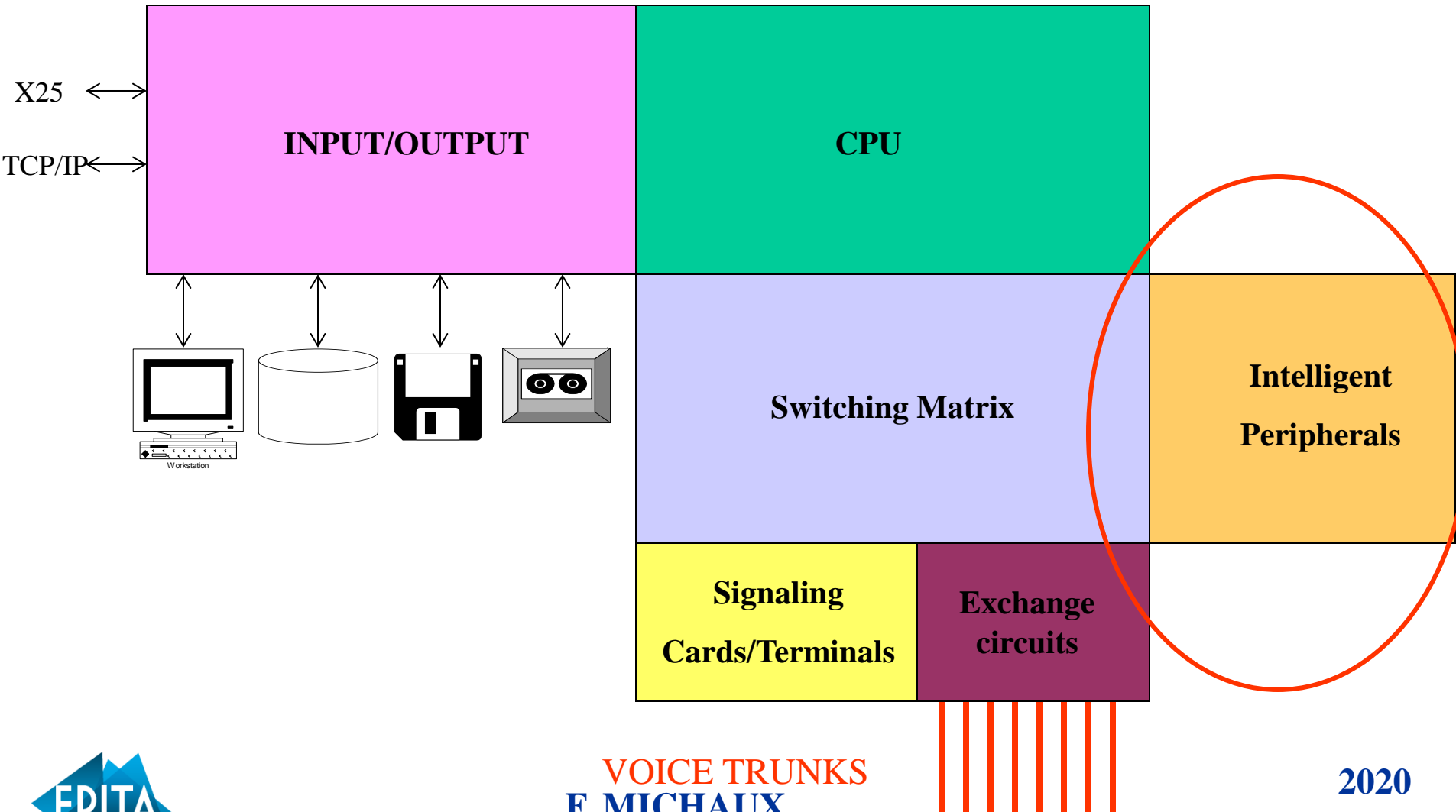
Translation principle

The called party number is analysed by the translation



INTELLIGENT PERIPHERALS

MAIN SWITCH COMPONENTS



INTELLIGENT PERIPHERALS

The intelligent peripherals provide additional services for the basic calls :



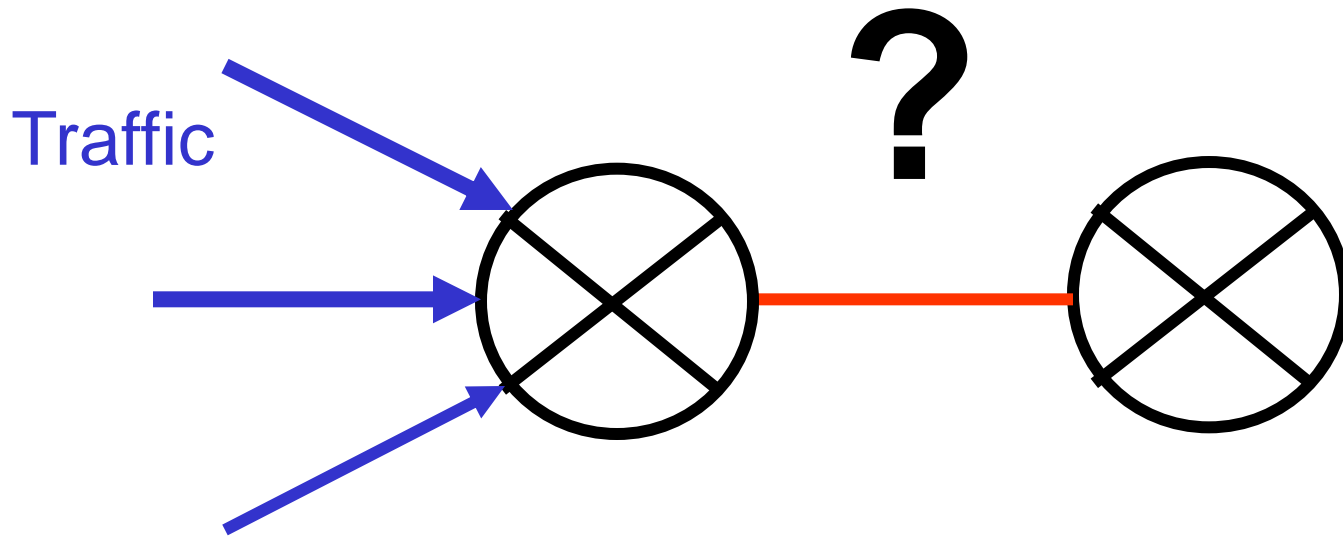
DTMF receivers



Announcement machines

Traffic calculation

Traffic calculation



Problematic :

if the trunk group is too small the consequence is an important lost of traffic => lost of Money

if the trunk group is too big the capacity is paid but not used => lost of Money

Traffic calculation

The size of the link between 2 switches depends of the traffic between the both switches

- ① it's based on : A stochastic process which means that It's **partially** due to the luck, that's why it's possible to define a model.
- ① A formula which is named the Erlang law.
- ① The calculation is generally done at the busy hour

Traffic calculation

An erlang (*) is :



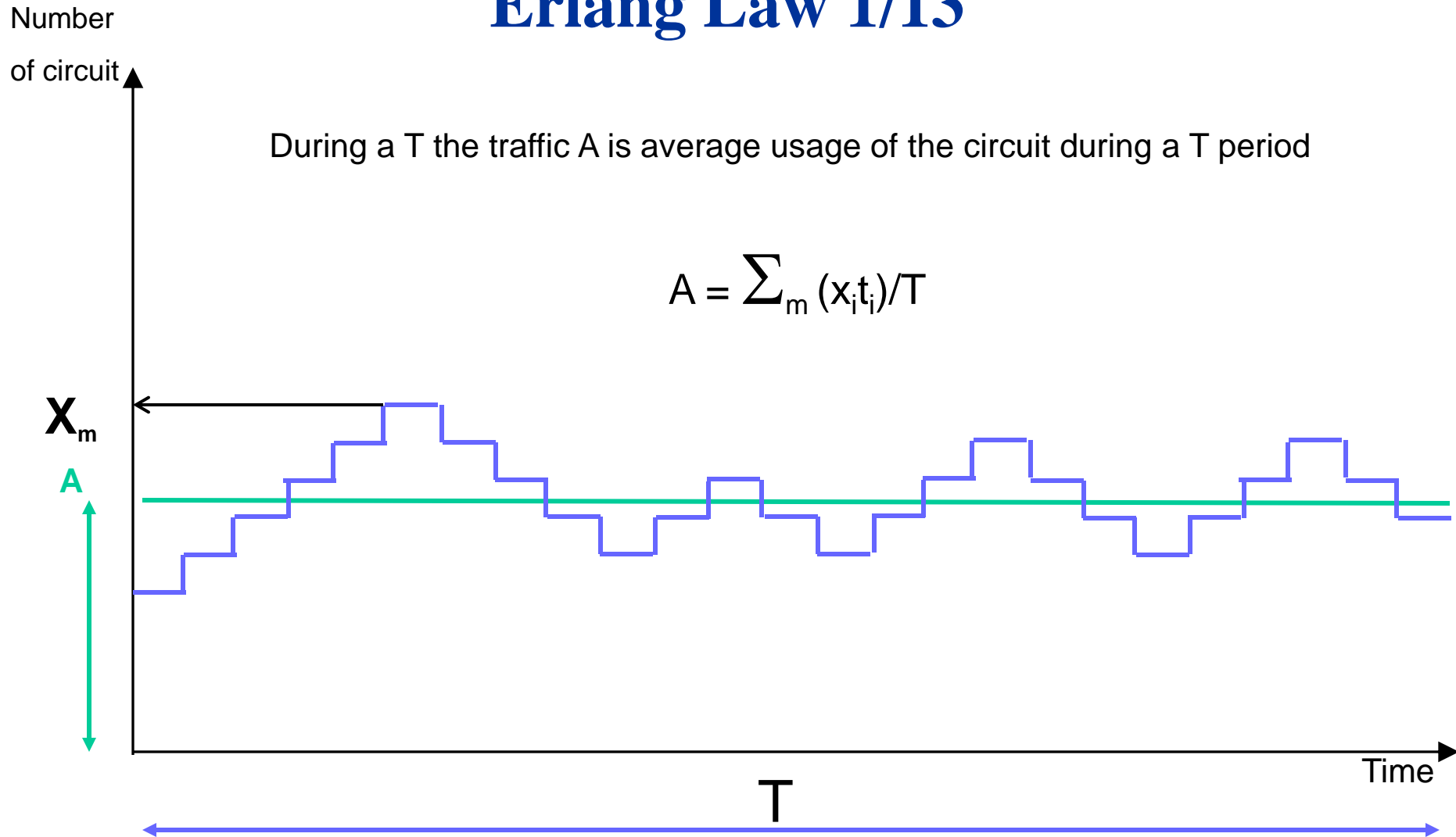
the utilization of the resources in percentage

The resources are the circuits

Example : if the average circuit traffics at 12%. The traffic is 0.12 E / circuit

(*) Mister Agner Krarup Erlang (1878-1929) was Danish

Erlang Law 1/13



Erlang Law 2/13

Generally the traffic is given per minutes

Example : 20 000 calls / hour and the average time per call is 3 minutes

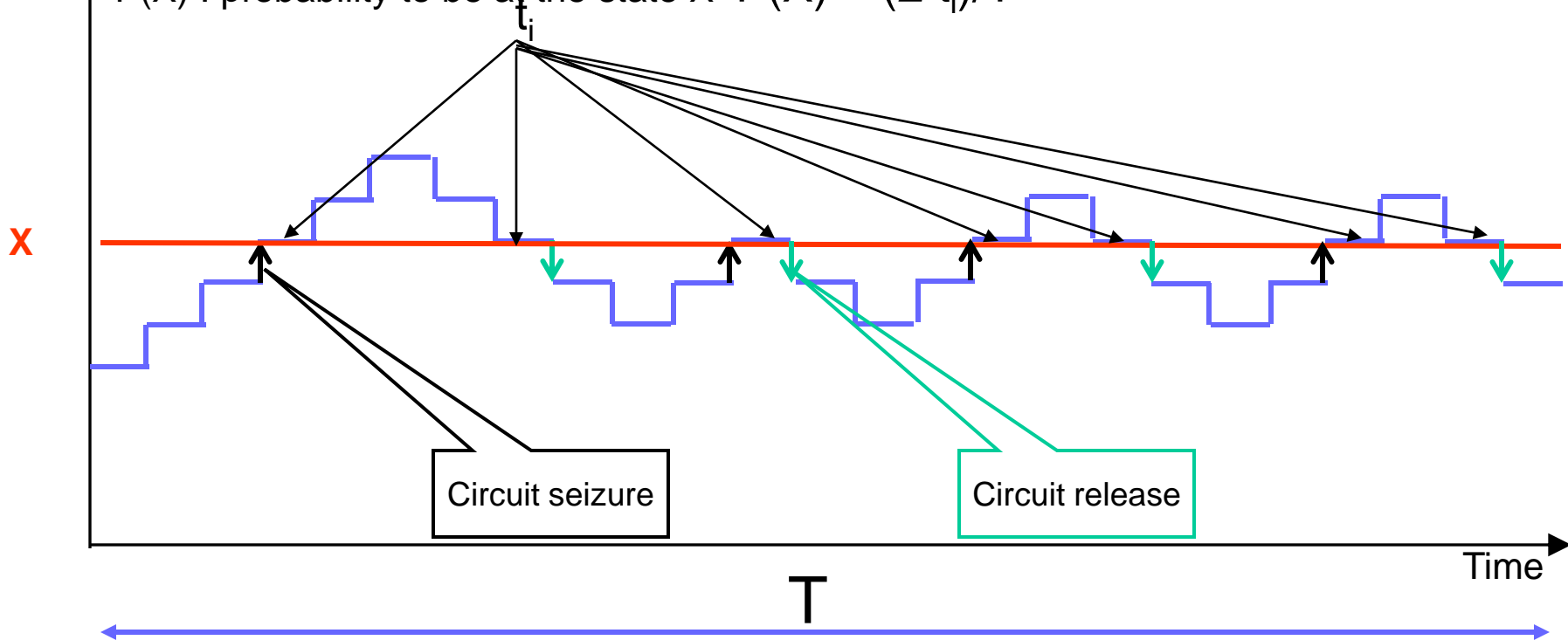
Result : $3/60 * 20\ 000 = 1000$ Erlangs

Erlang Law 3/13

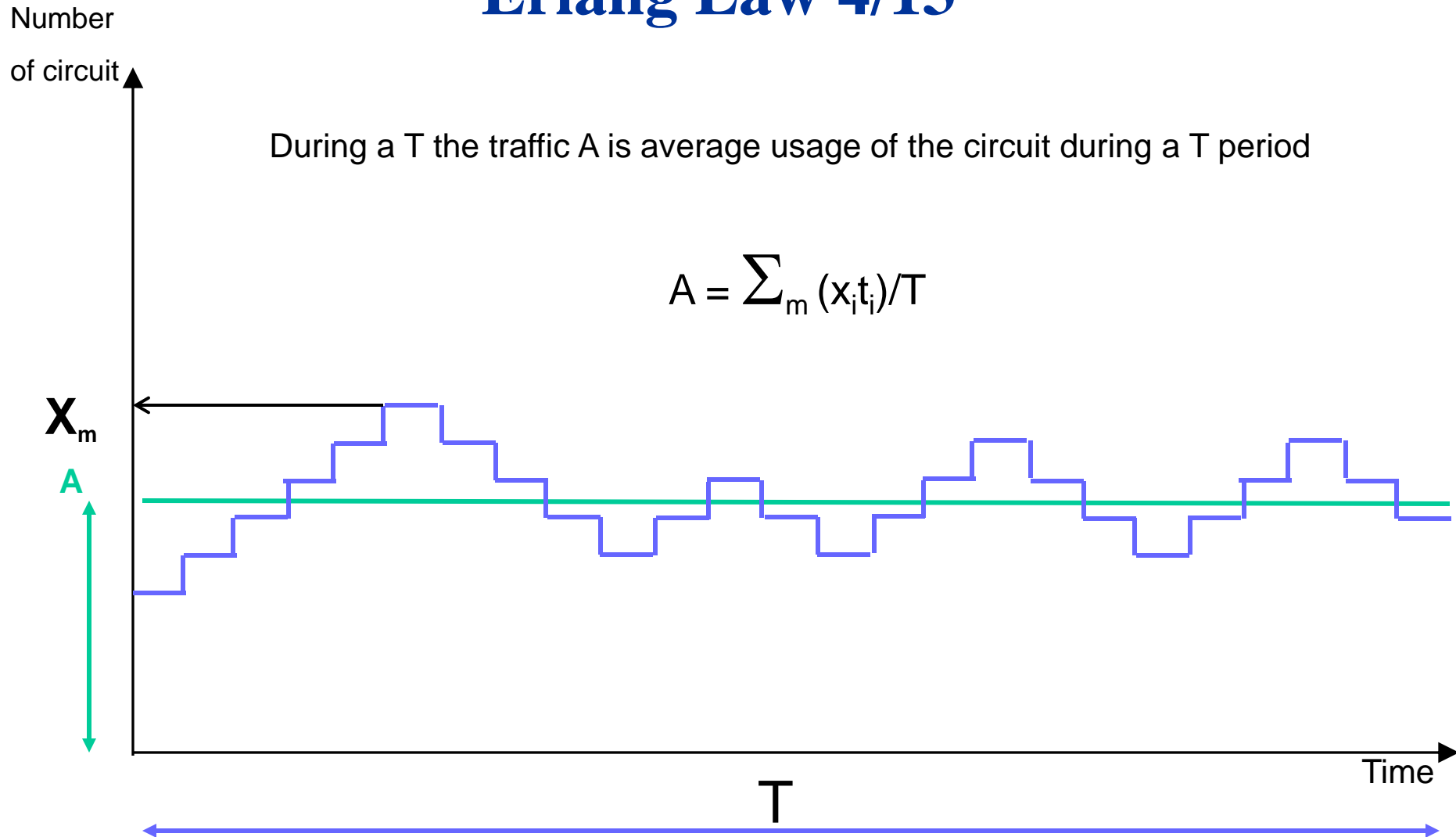
Number
of circuit

During a T period the number of transition from the $(X-1)$ state to the (X) state is equal to the number of transition from the (X) state to the $(X-1)$

$P(X)$: probability to be at the state X $P(X) = (\sum t_i)/T$



Erlang Law 4/13



Erlang Law 5/13



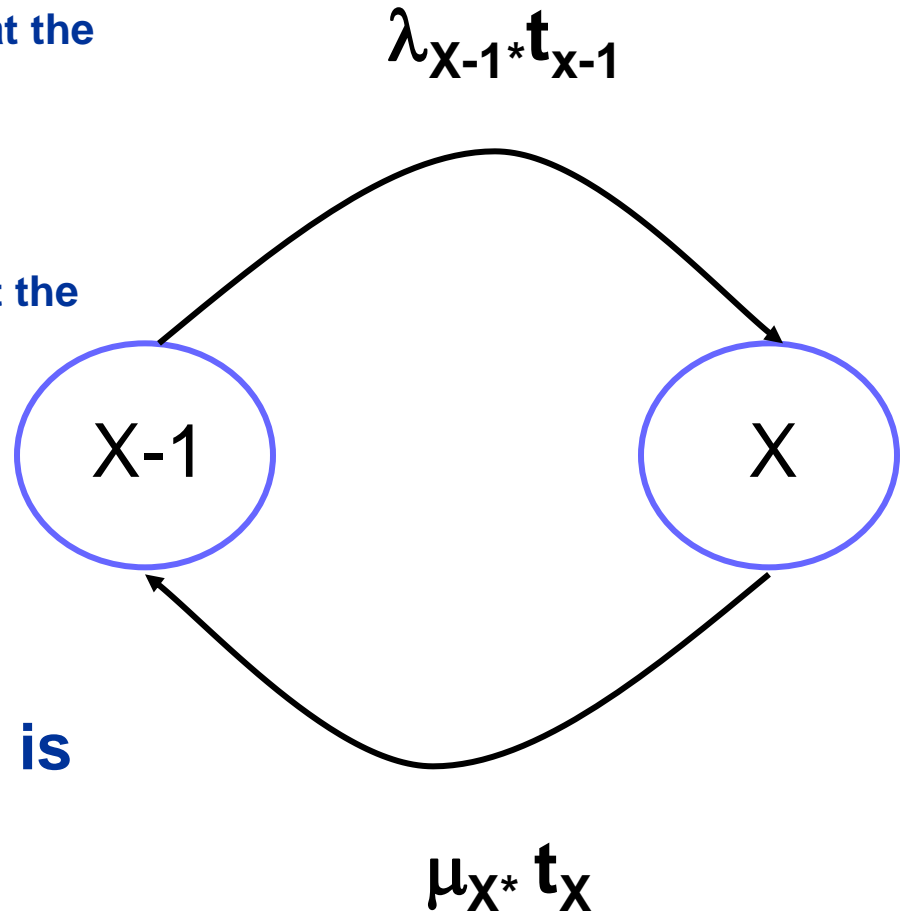
λ_{X-1} is the rate of circuit seizure at the (X-1) state



μ_X is the rate of circuit release at the (X) state



The balance equation is
 $\lambda_{X-1} P(X-1) = \mu_X P(X)$



Transition between the states (X) and (X-1)

Erlang Law 6/13



λ_{X-1} does not depend of the circuit already seized but depends only of the traffic A



μ_X is proportional to the circuit seized. More the circuit are seized more the circuit could be released



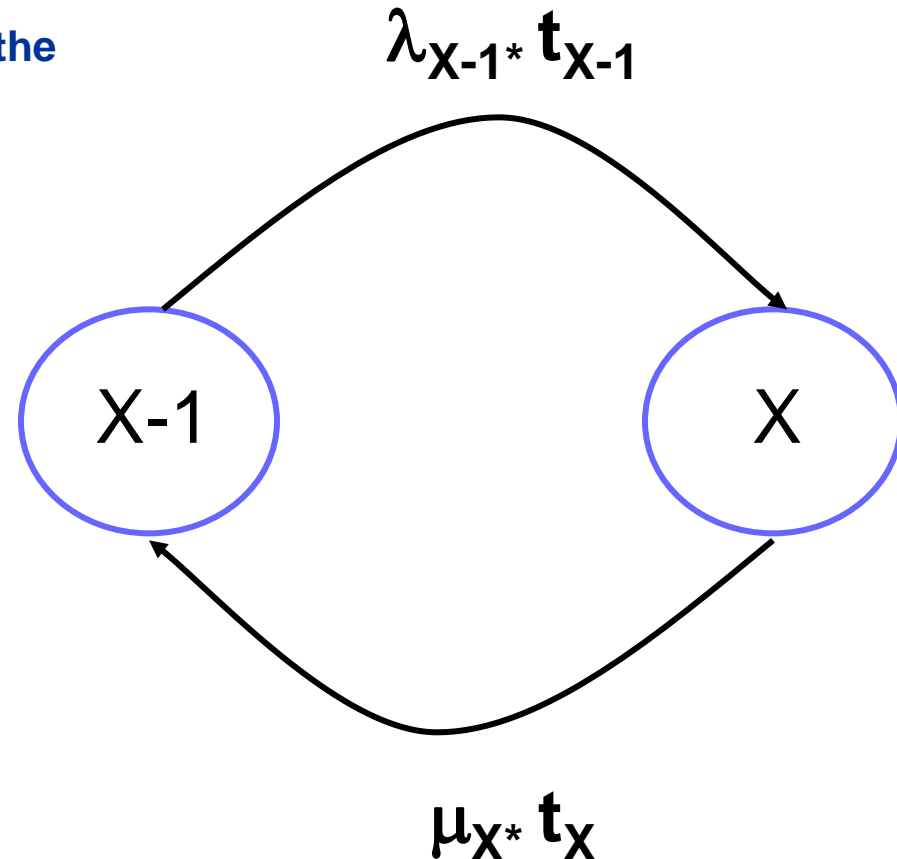
$$\lambda_{X-1} = \lambda = n/T = \mathbf{A/\tau}$$



$$\mu_X = \mathbf{X/\tau}$$



The balance equation is
 $\mathbf{A * P(X-1)/\tau = (X) * P(X)/\tau}$



Transition between the states (X) and (X-1)

Erlang Law 7/13



$$P(X) = A/X P(X-1) = A/X * A/(X-1) * A/(X-2) * \dots * P(0)$$

$$P(X) = (A^X / X!) * P(0)$$

$$\sum_0^N P(X) = 1 \quad N \text{ is the number of circuit of the trunk}$$



$$P(0) * \sum_0^N (A^i / i!) = 1 \Rightarrow P(0) = 1 / \sum_0^N (A^i / i!)$$



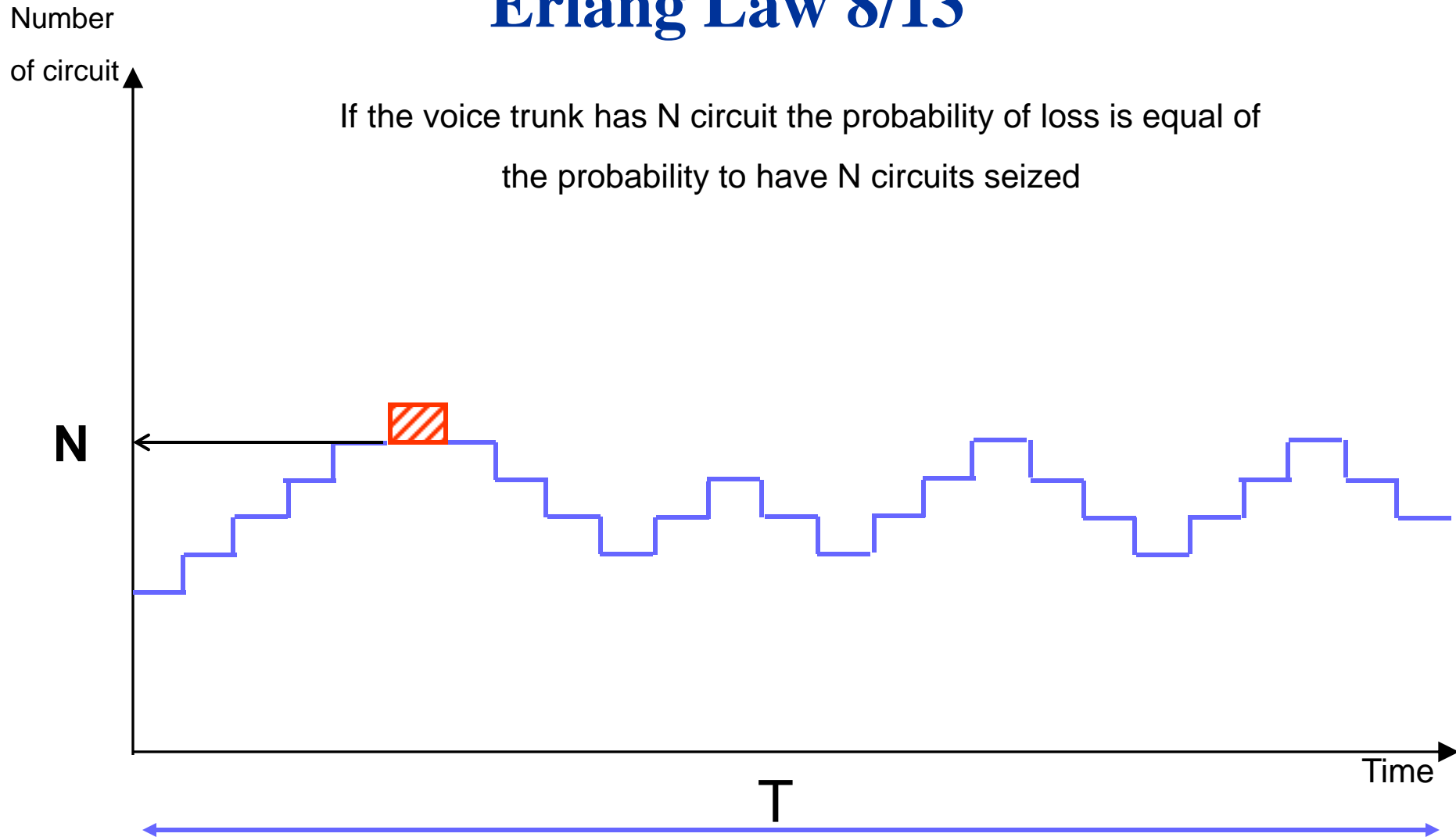
$P(X) = (A^X / X!) / \sum_0^N (A^i / i!)$ This is the Erlang distribution probability to have X circuit engaged when the traffic is A and the voice trunk has N circuits.



NOTA : The Erlang Law is very close to the Poisson Law

$$\sum_0^\infty P(X) = 1 \Rightarrow P(0) = 1 / \sum_0^\infty (A^i / i!) = e^{-A} \Rightarrow P(X) = A^X / X! * e^{-A}$$

Erlang Law 8/13



Erlang Law 9/13

- ▶ $P(X) = (A^X/X!) / \sum^N (A^i/i!)$
Probability to have X circuit engaged when the traffic is A and the voice trunk has N circuits.

- ▶ $1/P(N) = \sum^N (A^i/i!) / (A^N/N!)$
- ▶ $1/P(N) = (N!/A^N) * (1 + A + A^2/2 + ... + A^N/N!)$
- ▶ $1/P(N) = N/A * ((N-1!)/A^{N-1}) * (1 + A + A^2/2 + ... + A^{N-1}/(N-1)! + A^N/N!)$
- ▶ $1/P(N) = N/A * 1/P(N-1) + N!/A^N * A^N/N!$
- ▶ $1/P(N) = N/A * 1/P(N-1) + 1$ with $P(0)=1$

Erlang Law 10/13

The first Erlang law is the following :

$$1/E_{(1,N)}(A) = 1 + N/A * 1/E_{(1,N-1)}(A) \quad \text{with } E_{(1,0)}(A) = 1$$

N : is the Number of circuits

A : is the traffic in Erlang

$E_{(1,N)}(A)$: is the probability of loss with A Erlangs and N circuits

$E_{(1,0)}(A) = 1$ because with 0 circuit the probability of loss is 1

Erlang Law 11/13

$$1/E_{(1,N)}(A) = 1 + N/A * 1/E_{(1,N-1)}(A) \text{ with}$$

$$E_{(1,0)}(A) = 1$$

$$E_{(1,0)}(A) = 1.000000 \quad A = 100$$

$$E_{(1,1)}(A) = 0.990099$$

$$E_{(1,2)}(A) = 0.980200$$

$$E_{(1,3)}(A) = 0.970303$$

$$E_{(1,4)}(A) = 0.960408$$

$$E_{(1,5)}(A) = 0.950515$$

$$E_{(1,100)}(A) = 0.075700$$

$$1/E_{(1,100)}(A) = 13.209960$$

$$E_{(1,140)}(A) = 0.000028$$

$$1/E_{(1,140)}(A) = 36185.150291$$

Conclusion : as much as the circuit are important the probability of loss is small

Erlang Law 12/13



Conclusion :

As much as the circuit are important as the probability of loss is small.



Problematic :

Generally the inputs are the probability of loss and the traffic. N has to be found !

The probability of loss for n circuits depends the probability of loss for $(n-1)$ circuits.

Very long to calculate before the computer the people used Palm table.

Erlang Law 13/13



It's not easy to calculate the number of circuit
A formula which gives a good approximation is

$$E_{(1,N)}(A) = 10^{-k}$$

$$k = -\text{LOG}_{10}[E_{(1,N)}(A)]$$

$$\underline{N \# A + k * A^{1/2}}$$

CONCLUSION

Conclusion



This switching overview shows the experience required is very large as :

- **Electronic : Modulation, filtering, digitalization**
- **Signal theory, compression,**
- **Protocol (Signaling),**
- **Real time software knowledge,**
- **Probability (traffic calculation).**
- **.....**

QUESTIONS

?

QUESTIONS



Questions regarding the presentation ?



Questions regarding the Telecommunication World ?

How is the business ?

What is the future ?

Thank you for your attention