

Fig 9

```
r = 1;
a = 0.09;
Omega = 50;
alpha = 2;
delta = 0.04;
f = 0.02;
K0 = 1;

B0 = 0.1;
I0 = 0.1;
P0 = 10;

tspan_total = [0 5000];
t_burn = 3000;

A_vec = 0:0.002:1;

bif_data = [];

% ODE
options = odeset('NonNegative', [1,2,3], 'RelTol', 1e-12, 'MaxStep', 0.1);

y0 = [B0; I0; P0];

for i = 1:length(A_vec)
    A = A_vec(i);
    fprintf('Running simulation for A = %.3f (%d/%d)\n', A, i, length(A_vec));

    [t, y] = ode15s(@(t,y) fluctuate_1B_nothre(t, y, A, f, r, K0, a, Omega, alpha, delta), tspan_total, y0);

    idx_steady = t > t_burn;
    t_steady = t(idx_steady);
    B_steady = y(idx_steady, 1) * 1e8;
    I_steady = y(idx_steady, 2) * 1e8;
    P_steady = y(idx_steady, 3) * 1e8;

    %Calculate the average value during the steady-state phase to use as the initial condition
    if ~isempty(B_steady)
        B0_next = mean(y(idx_steady, 1));
        I0_next = mean(y(idx_steady, 2));
        P0_next = mean(y(idx_steady, 3));
        y0 = [B0_next; I0_next; P0_next];
    end
end
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else
    fprintf('Warning: No steady state data for A = %.3f\n', A);
end

if length(B_steady) < 3
    continue;
end

[troughs, ~] = findpeaks(-B_steady);
troughs = -troughs;

if ~isempty(troughs)
    for j = 1:length(troughs)
        bif_data(end+1, :) = [A, troughs(j)];
    end
else
    bif_data(end+1, :) = [A, NaN];
end
end
end

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Running simulation for A = 0.992 (497/501)
Running simulation for A = 0.994 (498/501)
Running simulation for A = 0.996 (499/501)
Running simulation for A = 0.998 (500/501)
Running simulation for A = 1.000 (501/501)

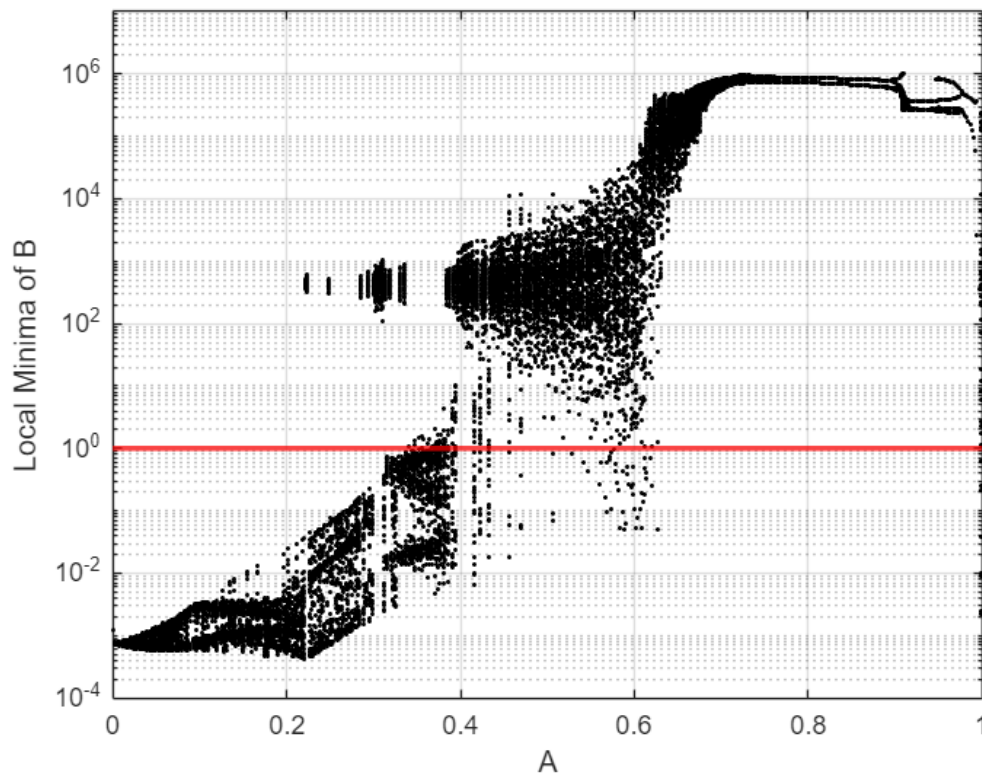
```

%Visualization

```

figure;
hold on;
plot(bif_data(:,1), bif_data(:,2), 'k.', 'MarkerSize', 5);
set(gca, 'Yscale', 'log');
xlabel('A');
ylabel('Local Minima of B');
xlim([min(A_vec), 1]);
ylim([10^-4, 10^7]);
yline(1, 'r-', 'LineWidth', 2, 'Color', 'red');
grid on;
box on;
hold off;

```



```

clear;
r = 1;
a = 0.09;
Omega = 50;
alpha = 2;
delta = 0.04;
A = 0.2;
K0 = 1;

B0 = 0.1;
I0 = 0.1;
P0 = 10;

y0 = [B0; I0; P0];

tspan_total = [0 5000];
t_burn = 3000;

bif_data = [];

% ODE
options = odeset('NonNegative', [1,2,3], 'RelTol', 1e-12, 'MaxStep', 0.1);
[t, y] = ode15s(@(t,y) fluctuate_1B_nothre(t, y, 0, 0, r, K0, a, Omega, alpha, delta), tspan_total, y0, options);
f0=PSD_max(y, t,tspan_total(2));

f_vec = logspace(log10(f0/1.5),log10(f0*5),500);

for i = 1:length(f_vec)
    f = f_vec(i);
    fprintf('Running simulation for f = %.5f (%d/%d)\n', f, i, length(f_vec));

    [t, y] = ode15s(@(t,y) fluctuate_1B_nothre(t, y, A, f, r, K0, a, Omega, alpha, delta), tspan_total, y0, options);

    idx_steady = t > t_burn;
    t_steady = t(idx_steady);
    B_steady = y(idx_steady, 1) * 1e8;

    if length(B_steady) < 3
        continue;
    end
end

```

```

end

[troughs, ~] = findpeaks(-B_steady);
troughs = -troughs;

if ~isempty(troughs)
    for j = 1:length(troughs)
        bif_data(end+1, :) = [f, troughs(j)];
    end
else
    bif_data(end+1, :) = [f, NaN];
end
end

```

```

Running simulation for f = 0.00886 (1/500)
Running simulation for f = 0.00889 (2/500)
Running simulation for f = 0.00893 (3/500)
Running simulation for f = 0.00896 (4/500)
Running simulation for f = 0.00900 (5/500)
Running simulation for f = 0.00904 (6/500)
Running simulation for f = 0.00907 (7/500)
Running simulation for f = 0.00911 (8/500)
Running simulation for f = 0.00915 (9/500)
Running simulation for f = 0.00918 (10/500)
Running simulation for f = 0.00922 (11/500)
Running simulation for f = 0.00926 (12/500)
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Running simulation for f = 0.00933 (14/500)
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Running simulation for f = 0.00941 (16/500)
Running simulation for f = 0.00945 (17/500)
Running simulation for f = 0.00949 (18/500)
Running simulation for f = 0.00952 (19/500)
Running simulation for f = 0.00956 (20/500)
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Running simulation for f = 0.00984 (27/500)
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Running simulation for f = 0.01008 (33/500)
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Running simulation for f = 0.01037 (40/500)
Running simulation for f = 0.01041 (41/500)
Running simulation for f = 0.01045 (42/500)
Running simulation for f = 0.01049 (43/500)
Running simulation for f = 0.01054 (44/500)

```

Running simulation for $f = 0.01058$ (45/500)
Running simulation for $f = 0.01062$ (46/500)
Running simulation for $f = 0.01066$ (47/500)
Running simulation for $f = 0.01071$ (48/500)
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Running simulation for $f = 0.04563$ (407/500)
Running simulation for $f = 0.04582$ (408/500)
Running simulation for $f = 0.04600$ (409/500)
Running simulation for $f = 0.04619$ (410/500)
Running simulation for $f = 0.04637$ (411/500)
Running simulation for $f = 0.04656$ (412/500)
Running simulation for $f = 0.04675$ (413/500)
Running simulation for $f = 0.04694$ (414/500)
Running simulation for $f = 0.04713$ (415/500)
Running simulation for $f = 0.04732$ (416/500)
Running simulation for $f = 0.04751$ (417/500)
Running simulation for $f = 0.04770$ (418/500)
Running simulation for $f = 0.04790$ (419/500)
Running simulation for $f = 0.04809$ (420/500)
Running simulation for $f = 0.04828$ (421/500)
Running simulation for $f = 0.04848$ (422/500)
Running simulation for $f = 0.04868$ (423/500)
Running simulation for $f = 0.04887$ (424/500)
Running simulation for $f = 0.04907$ (425/500)
Running simulation for $f = 0.04927$ (426/500)
Running simulation for $f = 0.04947$ (427/500)
Running simulation for $f = 0.04967$ (428/500)

Running simulation for $f = 0.04987$ (429/500)
Running simulation for $f = 0.05007$ (430/500)
Running simulation for $f = 0.05027$ (431/500)
Running simulation for $f = 0.05048$ (432/500)
Running simulation for $f = 0.05068$ (433/500)
Running simulation for $f = 0.05089$ (434/500)
Running simulation for $f = 0.05109$ (435/500)
Running simulation for $f = 0.05130$ (436/500)
Running simulation for $f = 0.05151$ (437/500)
Running simulation for $f = 0.05172$ (438/500)
Running simulation for $f = 0.05192$ (439/500)
Running simulation for $f = 0.05213$ (440/500)
Running simulation for $f = 0.05235$ (441/500)
Running simulation for $f = 0.05256$ (442/500)
Running simulation for $f = 0.05277$ (443/500)
Running simulation for $f = 0.05298$ (444/500)
Running simulation for $f = 0.05320$ (445/500)
Running simulation for $f = 0.05341$ (446/500)
Running simulation for $f = 0.05363$ (447/500)
Running simulation for $f = 0.05385$ (448/500)
Running simulation for $f = 0.05406$ (449/500)
Running simulation for $f = 0.05428$ (450/500)
Running simulation for $f = 0.05450$ (451/500)
Running simulation for $f = 0.05472$ (452/500)
Running simulation for $f = 0.05494$ (453/500)
Running simulation for $f = 0.05517$ (454/500)
Running simulation for $f = 0.05539$ (455/500)
Running simulation for $f = 0.05561$ (456/500)
Running simulation for $f = 0.05584$ (457/500)
Running simulation for $f = 0.05607$ (458/500)
Running simulation for $f = 0.05629$ (459/500)
Running simulation for $f = 0.05652$ (460/500)
Running simulation for $f = 0.05675$ (461/500)
Running simulation for $f = 0.05698$ (462/500)
Running simulation for $f = 0.05721$ (463/500)
Running simulation for $f = 0.05744$ (464/500)
Running simulation for $f = 0.05767$ (465/500)
Running simulation for $f = 0.05791$ (466/500)
Running simulation for $f = 0.05814$ (467/500)
Running simulation for $f = 0.05838$ (468/500)
Running simulation for $f = 0.05861$ (469/500)
Running simulation for $f = 0.05885$ (470/500)
Running simulation for $f = 0.05909$ (471/500)
Running simulation for $f = 0.05933$ (472/500)
Running simulation for $f = 0.05957$ (473/500)
Running simulation for $f = 0.05981$ (474/500)
Running simulation for $f = 0.06005$ (475/500)
Running simulation for $f = 0.06029$ (476/500)
Running simulation for $f = 0.06054$ (477/500)
Running simulation for $f = 0.06078$ (478/500)
Running simulation for $f = 0.06103$ (479/500)
Running simulation for $f = 0.06127$ (480/500)
Running simulation for $f = 0.06152$ (481/500)
Running simulation for $f = 0.06177$ (482/500)
Running simulation for $f = 0.06202$ (483/500)
Running simulation for $f = 0.06227$ (484/500)
Running simulation for $f = 0.06252$ (485/500)
Running simulation for $f = 0.06278$ (486/500)
Running simulation for $f = 0.06303$ (487/500)
Running simulation for $f = 0.06329$ (488/500)
Running simulation for $f = 0.06354$ (489/500)
Running simulation for $f = 0.06380$ (490/500)
Running simulation for $f = 0.06406$ (491/500)
Running simulation for $f = 0.06432$ (492/500)

```

Running simulation for f = 0.06458 (493/500)
Running simulation for f = 0.06484 (494/500)
Running simulation for f = 0.06510 (495/500)
Running simulation for f = 0.06536 (496/500)
Running simulation for f = 0.06563 (497/500)
Running simulation for f = 0.06589 (498/500)
Running simulation for f = 0.06616 (499/500)
Running simulation for f = 0.06643 (500/500)

```

%Visualization

```

figure;
hold on;

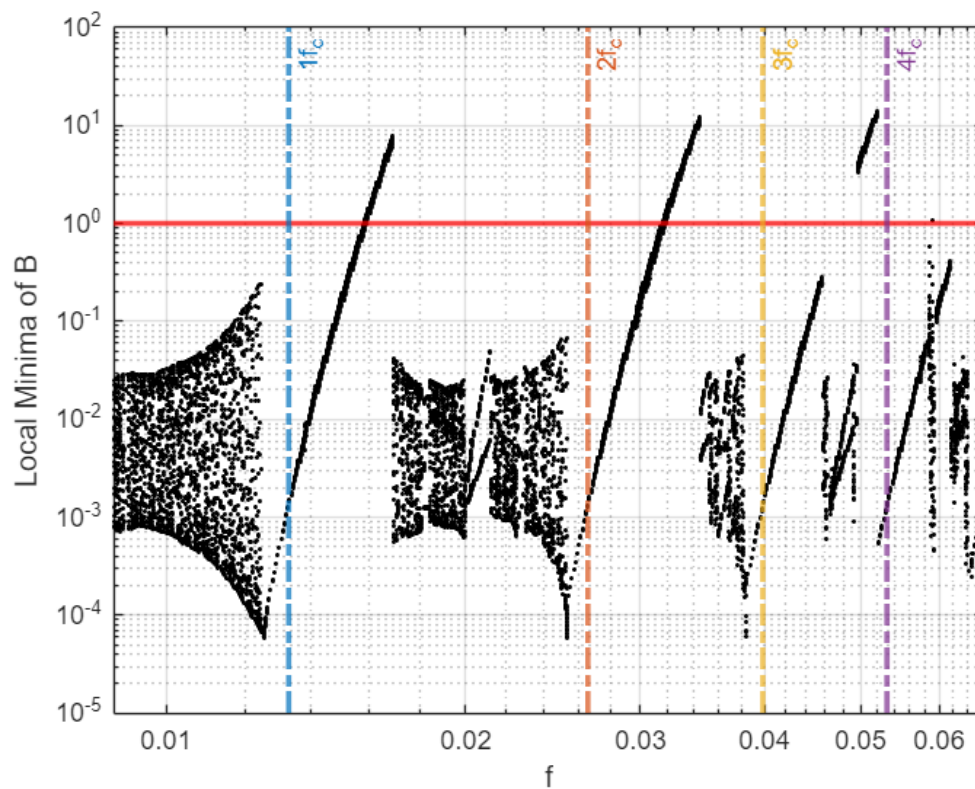
plot(bif_data(:,1), bif_data(:,2), 'k.', 'MarkerSize', 5);

set(gca, 'YScale', 'log', 'XScale', 'log');
xlabel('f');
ylabel('Local Minima of B');
xlim([min(f_vec), max(f_vec)]);
grid on;

n_list = [1, 2, 3, 4];
colors = lines(5);

yline(1, 'r-', 'LineWidth', 2, 'Color', 'red');
for n = n_list
    x2 = n * f0;
    if x2 >= min(f_vec) && x2 <= max(f_vec)
        xline(x2, '-.', sprintf('%df_c', n), 'Color', colors(n,:), 'LineWidth', 2);
    end
end
box on;
hold off;

```



```

clear;
r = 1;
a = 0.09;
Omega = 50;
alpha = 2;
delta = 0.04;
K0 = 1;

B0 = 0.1;
I0 = 0.1;
P0 = 10;
y0 = [B0; I0; P0];

tspan_total = [0 5000];
t_burn = 3000;

% ODE

options = odeset('NonNegative', [1,2,3], 'RelTol', 1e-12, 'MaxStep', 0.1);
[t, y] = ode15s(@(t,y) fluctuate_1B_nothre(t, y, 0, 0, r, K0, a, Omega, alpha, delta), tspan_total, y0);
f0=PSD_max(y, t,tspan_total(2));

```

```

A_vec = 0:0.01:1;
f_vec = logspace(log10(f0/1.5), log10(f0*5), 100);

minB_matrix = zeros(length(A_vec), length(f_vec));

for i = 1:length(A_vec)
    A = A_vec(i);
    fprintf('Running simulations for A = %.4f (%d/%d)\n', A, i, length(A_vec));

    parfor j = 1:length(f_vec)
        f = f_vec(j);

        [t, y] = ode15s(@(t,y) fluctuate_1B_nothre(t, y, A, f, r, K0, a, Omega, alpha, delta),
            tspan_total, y0, options);

        idx_steady = t > t_burn;
        B_steady = y(idx_steady, 1)*10^8;

        if ~isempty(B_steady) && all(isfinite(B_steady))
            minB_matrix(i, j) = min(B_steady);
        else
            minB_matrix(i, j) = NaN;
        end
    end
end
end

```

```

Running simulations for A = 0.0000 (1/101)
Starting parallel pool (parpool) using the 'local' profile ...
Connected to the parallel pool (number of workers: 8).
Running simulations for A = 0.0100 (2/101)
Running simulations for A = 0.0200 (3/101)
Running simulations for A = 0.0300 (4/101)
Running simulations for A = 0.0400 (5/101)
Running simulations for A = 0.0500 (6/101)
Running simulations for A = 0.0600 (7/101)
Running simulations for A = 0.0700 (8/101)
Running simulations for A = 0.0800 (9/101)
Running simulations for A = 0.0900 (10/101)
Running simulations for A = 0.1000 (11/101)
Running simulations for A = 0.1100 (12/101)
Running simulations for A = 0.1200 (13/101)
Running simulations for A = 0.1300 (14/101)
Running simulations for A = 0.1400 (15/101)
Running simulations for A = 0.1500 (16/101)
Running simulations for A = 0.1600 (17/101)
Running simulations for A = 0.1700 (18/101)
Running simulations for A = 0.1800 (19/101)
Running simulations for A = 0.1900 (20/101)
Running simulations for A = 0.2000 (21/101)
Running simulations for A = 0.2100 (22/101)
Running simulations for A = 0.2200 (23/101)

```



```

Running simulations for A = 0.8700 (88/101)
Running simulations for A = 0.8800 (89/101)
Running simulations for A = 0.8900 (90/101)
Running simulations for A = 0.9000 (91/101)
Running simulations for A = 0.9100 (92/101)
Running simulations for A = 0.9200 (93/101)
Running simulations for A = 0.9300 (94/101)
Running simulations for A = 0.9400 (95/101)
Running simulations for A = 0.9500 (96/101)
Running simulations for A = 0.9600 (97/101)
Running simulations for A = 0.9700 (98/101)
Running simulations for A = 0.9800 (99/101)
Running simulations for A = 0.9900 (100/101)
Running simulations for A = 1.0000 (101/101)

```

```

% Visualization
figure;
set(gcf, 'Position', [100, 100, 800, 600]);
imagesc(f_vec, A_vec, log10(minB_matrix));
colormap hot;
axis xy;
colorbar;
hcb = colorbar;
hcb.Label.String = 'log_{10}(B_{min})';
xlabel('f');
ylabel('A');
set(gca, 'XScale', 'log');
ylabel('A');
xlabel('f ');

hold on;
n_list = [1, 2, 3, 4];
colors = lines(4);
for n = n_list
    f_n = n * f0;
    if f_n >= min(f_vec) && f_n <= max(f_vec)
        xline(f_n, 'k--', sprintf('%d f_c', n), 'LineWidth', 1.5);
    end
end
box on;
axis tight;
hold off;

```