$mowitone\ tinurfirm otith.$

$$x = \ln y. : y = e^{x} \quad (y^{-1}(y))$$

$$f_{X}(x) = f_{Y}(e^{x}) e^{x} \quad \frac{d}{dx}(y) = e^{x}$$

$$= e^{-e^{x}} e^{x}$$

$$= e^{x-e^{x}}$$

$$\therefore f_{x}(x) = e^{x-e^{x}} \quad \text{for } x \in \mathbb{R}.$$

$$F_{\gamma}(y) = \int_{0}^{\infty} e^{-y} dy.$$

$$F_{x}(x) = p(x \le x) = p(\ln Y \le x)$$

$$= p(y \le e^{x})$$

$$= F_{Y}(e^{x})$$

$$f_{x}(x) = \frac{d}{dx} F_{y}(e^{x})$$

$$1 = e^{x} f_{Y}(e^{x})$$

$$= e^{x} e^{-e^{x}}$$

 $=e^{x-e^x}$