

Let  $X$  be amount bidden  
 $W$  be profit made.

$$W = X - 100 \text{ or } W = 0 \text{ (not lowest bid)} \quad f_Y(y) = \begin{cases} \frac{1}{140-70}, & 70 < x < 160 \\ 0, & \text{otherwise} \end{cases}$$

$$\begin{aligned} \therefore E(W) &= 0 \cdot \int_{70}^x f_Y(y) dy - (x - 100) \int_x^{160} f_Y(y) dy \\ &= 0 + (x - 100) \left( 2 - \frac{1}{70}x \right) \\ &= -\frac{1}{70}x^2 + \frac{24}{7}x - 200 \end{aligned}$$

$$\left( -\frac{\frac{24}{7}}{2 \cdot \left(-\frac{1}{70}\right)} = 120 \right)$$

symmetry axis of parabola

$\Rightarrow$  When  $x = 120$ , the expected profit will be maximized