

Homework 8

*Assigned: Thursday 20 May**Due: Thursday 27 May 3:00pm PDT***Problem 1**

Let $\Sigma = \{a, b\}$. Show two different left-most reductions of the string “baabba” in the following context-free grammar:

$$S \longrightarrow AB \mid BA$$

$$A \longrightarrow AS \mid BC \mid a$$

$$B \longrightarrow BS \mid AD \mid b$$

$$C \longrightarrow AA$$

$$D \longrightarrow BB$$

Here, the variable set is $\{S, A, B, C, D\}$, and the start variable is S .

Problem 2

Let L_P be a Recursively Enumerable (R.E.) language, and let L_A be a Recursive language.

- a. Prove that $L_P \cup L_A$ is R.E. by showing a construction using the Universal TM (UTM) for a TM procedure that recognizes the union.
- b. *Briefly* explain why we cannot say that the union is Recursive. You may use the style of argument discussed in class. You do *not* have to prove it.