CS 181 HW6 2021 CS181

YIQIAO JIN

TOTAL POINTS

26.75 / 25

QUESTION 1

1 CFG 7/5

- $\sqrt{+2}$ pts Correct solution, and your CFG is unambiguous. You received 2 extra points.
- **0 pts** Correct solution, but your CFG is ambiguous, so you did not get the 2 bonus points.
- 1 pts Minor mistake, your grammar cannot generate some of the strings in the language. We use following strings to test your solution:
- \$\$\epsilon\$\$
- ab
- abbb
- b
- bbbb
- 1 pts Minor mistake, your grammar generates some strings that are not in the given language. We use following strings to test your solution:
- ล
- aa
- aab
- aaaabb
- ba
- bba
- baa
- 1 pts Correct solution, but no explanation provided. You expected a brief explanation that explains how your grammar is designed to correctly represent the language.
- 1 pts Did not define the start variable. You need to explicitly define which is the start variable.
 - 5 pts No answer provided.

QUESTION 2

2 CFL Pumping Lemma 8/8

- √ + 8 pts Correct or nearly correct
 - + 1 pts Appropriate string
 - + 1 pts Effective use of constraints on vxy
- **0.5 pts** Does not explicitly state how lvxyl \$\leq\$ p is used.
 - + 2 pts Clearly shows coverage of all cases
 - + 1 pts Partially shows coverage of all cases
 - + 1 pts Always pump down
 - + 3 pts Correct logic in every case
 - + 2 pts Partially correct logic in cases
 - + 1 pts Incorrect or weak logic in cases
 - + 0 pts No answer
 - + 0 pts Your string is not in the language.
- + **0 pts** Your string can be pumped and remain in the language.

QUESTION 3

Language Classification 12 pts

3.1 a R intersect L 2/2

- √ + 2 pts Correct and complete or nearly so.
 - + 1 pts Correct classification.
 - + 0.5 pts Partially correct classification.
 - + 1 pts Correct or nearly correct brief justification.
 - + 0.5 pts Partially correct brief justification.
 - + 0 pts Incorrect
 - + 0 pts No answer.

3.2 b A = Ambiguous Grammar 2/2

- √ + 2 pts Correct and complete or nearly so.
 - + 1 pts Correct classification.
 - + 0.5 pts Partially correct classification.
 - + 1 pts Correct or nearly correct brief justification.
 - + 0.5 pts Partially correct brief justification.
 - + **0 pts** Incorrect

+ 0 pts No answer.

3.3 c C\bar, C of PDA 2/2

√ + 2 pts Correct and complete or nearly correct.

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- + 0.5 pts Partially correct classification.
- + 1 pts Correct or nearly correct brief justification.
- + **0.5 pts** Partially correct brief justification.
- + 0 pts Incorrect
- + 0 pts No answer.

3.4 d G of Unambiguous CFG 2/2

√ + 2 pts Correct / Nearly Correct.

- + 1 pts Correct Classification.
- + 0.5 pts Partially Correct Classification.
- + 1 pts Correct Justification.
- + **0.5 pts** Partially Correct Justification.
- + **0 pts** Incorrect
- + 0 pts No answer.

3.5 e L\bar 1.75 / 2

√ + 2 pts Correct / Nearly Correct.

- + 1 pts Correct Classification.
- + **0.5 pts** Partially Correct Classification.
- + 1 pts Correct Justification.
- + 0.5 pts Partially Correct Justification.
- + 0 pts Incorrect.
- + 0 pts No Answer.
- √ 0.25 pts L and L\bar cannot be FSL.

3.6 f X 2 / 2

√ + 2 pts Correct / Nearly Correct.

- + 1 pts Correct Classification.
- + 0.5 pts Partially Correct Classification.
- + 1 pts Correct Justification.
- + **0.5 pts** Partially Correct Justification.
- + 0 pts Incorrect.
- + 0 pts No Answer.

Homework 6

Name: Yiqiao Jin UID: 305107551

1

Below is a CFG for this language

S is the start variable.

A is the variable for generating a at the beginning and b at the end of the new string. It either generates a pair of a and b, or only b. This ensures that $i \leq j$, the number of a's generated is always less than or equal to that of b's. When A finishes its generation, it generates ε .

An equivalent unambiguous language is:

This language also ensures that $i \leq j$. This language is unambiguous because every a must be paired with a b when A is generating. For example, for abb, the prefix ab is generated by A, and suffix b is generated by B.

Example strings that can be accepted by $L: abb, ab, b, \varepsilon, aaabbb$

2

Note: I use w instead of x in the original question so that it won't be confused with the x in the Pumping Lemma.

We assume that L_2 is a **CFL** and obtain a contradiction. Let p be the pumping length given by the pumping lemma. We can use the string $w = 0^p 1^p$ and let

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$$s=ww^Rw=\underbrace{0^p1^p1^p0^p0^p1^p}_{w^R}=0^p1^{2p}0^{2p}1^p\in L$$

According to the pumping lemma for CFL, since $|s| \ge p$, s may be divided into five pieces s = uvxyz satisfying the conditions

- 1. for each $i \geq 0$, $uv^i xy^i z \in L_2$
- 2. $|vy| \ge 1$
- $3. |vxy| \leq p$

We consider the following 4 cases:

1) The substrings v and y contain some symbols from the 0^p in the first half of s

Since $|vxy| \leq p$, v and y CANNOT contain 0's from the 0^{2p} in the second half of s

Consider $s' = uxz = 0^i 1^j 0^{2p} 1^p$, where $i < p, j \le 2p$. Since $|vxy| \le p$, pumping down on s will still yield $|s'| \ge 5p$.

Since $s' = uxz \in L$, it must be of the form tt^Rt . The first t must begin with the block of i < p 0's followed by some number of 1's. Thus, t^Rt must contain a block of at most 2i < 2p 0's.

However, uxz contains 0^{2p} (a continuous block of 0's with length 2p), a contradiction.

2) The substrings v and y contain some symbols from the 1^{2p} in the first half of s

Since $|vxy| \leq p$, v and y CANNOT contain 1's from the 1^p in the second half of s

Consider $s'=uxz=0^i1^j0^k1^p$, where $i\leq p, j<2p, k\leq 2p$. Since $s'=uxz\in L$, it must be of the form tt^Rt .

Since $|vxy| \le p$, pumping down on s will still yield $|s'| \ge 5p$. The last t must end with the block of 1^p preceded by some number of 0's. $t = 0..0 \underbrace{1^p}_{}$

So
$$tt^R=0..0\underbrace{1^p1^p}_{2p}0..0$$

Thus, tt^R must contain a continuous block of 2p 1's, whereas uxz contains a block of only j < 2p 1's, a contradiction.

3) The substrings v and y contain some symbols from 0^{2p} in the second half of s

Since $|vxy| \leq p$, v and y CANNOT contain 0's from the 0^p in the first half of s

However, s' = uxz contains a block of only j < 2p 0's, a contradiction.

4) The substrings v and y contain some symbols from 1^p in the second half of s

Since $|vxy| \leq p$, v and y CANNOT contain 1's from the 1^{2p} in the first half of s

Consider $s' = uxz = 0^p 1^{2p} 0^i 1^j$, where $i \le 2p, j < p$. Assume $s' \in L$, s' must be of the form $tt^R t$. Since $|vxy| \le p$, pumping down on s will yield $|s'| \ge 5p$. The second t must end with the block of $1^j, j < p$ preceded by some number of 0's:

Thus, tt^R must contain a continuous block of at most 2j < 2p 1's, whereas uxz actually contains a block of 2p 1's, a contradiction.

From 1-4, the Pumping Lemma does NOT apply under all these cases. So we prove that this language L_2 is NOT a **CFL**.

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1) $R \cap L$

This can be (1) (2) (3) (4). R is an FSL means R is also a CFL. Since L is non-CFG, no closure can be applied.

For example, let $\Sigma = \{0,1\}$, $R = (00)^*$ and $L = \{ww | w \in \{0,1\}^*\}$. $R \cap L = R$, a regular language (1)

Let $\Sigma=\{a,b,c\}$, $R=\{b,c\}^*$ and $L=\{a^ib^jc^k|0\leq i\leq j\leq k\}$. $R\cap L=\{b^jc^k|0\leq j\leq k\}$, which is (2) CFL but not FSL . If $R=\{a,b,c\}^*$, then $R\cap L=L\}$. This is (4) non-CFL.

2) A

A can be (1) FSL, OR (2) CFL and NOT FSL, OR (3) Inherently Ambiguous CFL.

A can be (1) since finite state language is a subset of CFL.

For example, the language S o Sa|aS|a|arepsilon is an ambiguous CFL. But it represents a^*

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A can also be (3) if it is inherently ambiguous.

3) \bar{C} , the complement of C with respect to Σ

 \bar{C} can be (1) (2) (3) (4). A language that can be represented by a PDA is a CFL. But CFL is NOT closed under complement.

4) G

G can be (1) FSL, or (2) CFL.

The class of FSL is a subclass of CFG and every regular language is naturally context-free. Since G can be represented by an unambiguous CFG, it can either be a FSL (CFG can simulate any FSL), or it can be a CFG that is NOT an FSL.

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6) *X*

3.1 a R intersect L 2/2

- √ + 2 pts Correct and complete or nearly so.
 - + 1 pts Correct classification.
 - + **0.5 pts** Partially correct classification.
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3.5 e L\bar 1.75 / 2

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- ✓ 0.25 pts L and L\bar cannot be FSL.

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Consider $s' = uxz = 0^p 1^{2p} 0^i 1^j$, where $i \le 2p, j < p$. Assume $s' \in L$, s' must be of the form $tt^R t$. Since $|vxy| \le p$, pumping down on s will yield $|s'| \ge 5p$. The second t must end with the block of $1^j, j < p$ preceded by some number of 0's:

Thus, tt^R must contain a continuous block of at most 2j < 2p 1's, whereas uxz actually contains a block of 2p 1's, a contradiction.

From 1-4, the Pumping Lemma does NOT apply under all these cases. So we prove that this language L_2 is NOT a **CFL**.

3

1) $R \cap L$

This can be (1) (2) (3) (4). R is an FSL means R is also a CFL. Since L is non-CFG, no closure can be applied.

For example, let $\Sigma = \{0,1\}$, $R = (00)^*$ and $L = \{ww | w \in \{0,1\}^*\}$. $R \cap L = R$, a regular language (1)

Let $\Sigma=\{a,b,c\}$, $R=\{b,c\}^*$ and $L=\{a^ib^jc^k|0\leq i\leq j\leq k\}$. $R\cap L=\{b^jc^k|0\leq j\leq k\}$, which is (2) CFL but not FSL . If $R=\{a,b,c\}^*$, then $R\cap L=L\}$. This is (4) non-CFL.

2) A

A can be (1) FSL, OR (2) CFL and NOT FSL, OR (3) Inherently Ambiguous CFL.

A can be (1) since finite state language is a subset of CFL.

For example, the language S o Sa|aS|a|arepsilon is an ambiguous CFL. But it represents a^*

A can also be (3) if it is inherently ambiguous.

3) \bar{C} , the complement of C with respect to Σ

 \bar{C} can be (1) (2) (3) (4). A language that can be represented by a PDA is a CFL. But CFL is NOT closed under complement.

4) G

G can be (1) FSL, or (2) CFL.

The class of FSL is a subclass of CFG and every regular language is naturally context-free. Since G can be represented by an unambiguous CFG, it can either be a FSL (CFG can simulate any FSL), or it can be a CFG that is NOT an FSL.

5) \bar{L} , the complement of L with respect to Σ

 \bar{L} can be (1) (2) (3) (4). Since L is non-CFG, no closure can be applied to determine the class of \bar{L} .

6) *X*

3.6 f X 2/2

- √ + 2 pts Correct / Nearly Correct.
 - + 1 pts Correct Classification.
 - + **0.5 pts** Partially Correct Classification.
 - + 1 pts Correct Justification.
 - + **0.5 pts** Partially Correct Justification.
 - + **0 pts** Incorrect.
 - + 0 pts No Answer.