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Homework 3

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1. $G_0 = A_0 * B_0$.

Both A_0 and B_0 are available at OT

Delay = 2T, the delay of 1 AND gate

2. $P_0 = A_0 \oplus B_0$.

Delay = 2T, the delay of 1 XOR gate

3. $G_{\alpha} = G_0 * P_1 * P_2 * P_3 + G_1 * P_2 * P_3 + G_2 * P_3 + G_3$

Delay = Delay of 4-input OR gate + maximum delay of the 4 inputs = 5T + max(5T+2T, 3T+2T, 2T+2T, 2T) = 12T

4. $P_{\alpha} = P_0 * P_1 * P_2 * P_3$

Delay = Delay of 4-input AND gate = 7T

5. $C_{12} = G_{\gamma} + G_{\beta} * P_{\gamma} + G_{\alpha} * P_{\beta} * P_{\gamma} + C_{0} * P_{\alpha} * P_{\beta} * P_{\gamma}$

The output OR gate has delay 5T

Each Propagator P has delay 7T

Each Generator G has delay 12T

Delay = 5T + max(12T, 2T + max(12T, 7T), 3T + max(12T, 7T, 7T), 5T + max(0T, 7T, 7T, 7T)) = <math>5T + 15T = 20T

- 6. $C_{15} = G_{14} + G_{13} * P_{14} + G_{12} * P_{13} * P_{14} + C_{12} * P_{12} * P_{13} * P_{14}$ Delay = 5T + max(2T, 2T + max(2T, 2T), 3T + max(2T, 2T, 2T), 5T + max(20T, 2T, 2T, 2T)) = 30T
- 7. $C_{16} = G_{\delta} + G_{\gamma} * P_{\delta} + G_{\beta} * P_{\gamma} * P_{\delta} + G_{\alpha} * P_{\beta} * P_{\gamma} * P_{\delta} + C_{0} * P_{\alpha} * P_{\beta} * P_{\gamma} * P_{\delta}$ Delay = 7T + max(12T, 2T + max(12T, 7T), 3T + max(12T, 7T, 7T), 5T + max(12T, 7T, 7T, 7T), 7T + max(0T, 7T, 7T, 7T, 7T)) = 7T + max(12T, 14T, 15T, 17T, 14T) = 24T
- 8. $S_{15} = A_{15} \oplus B_{15} \oplus C_{15}$ Delay = 3T + 30T = 33T
- 9.

 $C_{20} = G_{19} + G_{18} * P_{19} + G_{17} * P_{18} * P_{19} + G_{16} * P_{17} * P_{18} * P_{19} + C_{16} * P_{16} * P_{17} * P_{18} * P_{19}$

For the CSA, C_{16} has delay 0T. The output is generated by a 5-input OR gate.

Delay = 7T + max(2T, 2T+2T, 3T+2T, 5T+2T, 7T+2T) = 7T + 9T = 16T

10. $C_{19} = G_{18} + G_{17} * P_{18} + G_{16} * P_{17} * P_{18} + C_{16} * P_{16} * P_{17} * P_{18}$ For the CSA, C_{16} has delay 0T. The output is generated by a 4-input OR gate.

Delay = 5T + max(2T, 2T+2T, 3T+2T, 5T+2T) = 5T+7T = 12T

$$S_{19} = A_{19} \oplus B_{19} \oplus C_{19}$$

Delay = 3T + max(0T, 0T, 12T) = 15T

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11.

$$C_{24} = G_{23} + G_{22} * P_{23} + G_{21} * P_{22} * P_{23} + G_{20} * P_{21} * P_{22} * P_{23} + C_{20} * P_{20} * P_{21} * P_{22} * P_{23}$$
 Delay = 7T + max(2T, 2T+2T, 3T+2T, 5T+2T, 7T+16T) = 7T + 23T = 30T

12.
$$C_{31} = G_{30} + G_{29} * P_{30} + G_{28} * P_{29} * P_{30} + C_{28} * P_{28} * P_{29} * P_{30}$$

$$C_{28} = G_{27} + G_{26} * P_{27} + G_{25} * P_{26} * P_{27} + G_{24} * P_{25} * P_{26} * P_{27} + C_{24} * P_{24} * P_{25} * P_{26} * P_{27}$$

Delay of
$$C_{28} = 7T + max(2T, 2T+2T, 3T+2T, 5T+2T, 7T+30T) = 44T$$

Delay of
$$C_{31} = 5T + \max(2T, 2T+2T, 3T+2T, 5T+44T) = 54T$$

13. Before MUX:

$$C_{32} = G_{31} + G_{30} * P_{31} + G_{29} * P_{30} * P_{31} + G_{28} * P_{29} * P_{30} * P_{31} + C_{28} * P_{28} * P_{29} * P_{30} * P_{31}$$

Delay = 7T + max(2T, 2T+2T, 3T+2T, 5T+2T, 7T+44T) = 58T

The selection bit C_{16} has delay 24T

After MUX:
$$C_{32} = 4T + \max(58T, 58T, 24T) = 62T$$

14. Before MUX:

$$S_{31} = A_{31} \oplus B_{31} \oplus C_{31} = 3T + \max(0T, 0T, 54T) = 57T$$

After MUX:

$$S_{31} = 4T + \max(57T, 57T, 24T) = 61T$$

15. The maximal delay is the max latency of these 3 outputs:

 S_0-S_{15} from the 16-bit HCLA. Max latency is 33T from S_{15} $S_{16}-S_{31}$ from MUX of the 16-bit CSA. Max latency is 61T from S_{31} C_{31} from MUX of the 16-bit CSA. Latency is 62T

So Maximal Delay = max(33T, 61T, 62T) = 62T