

# Hyperbolic Graph Convolutional Networks for Aspect-Based Sentiment Analysis

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**Abstract**—Aspect-based sentiment analysis is a fine-grained sentiment analysis task that aims to predict the sentiment polarity of a specific aspect. Recent work adopts graph convolutional networks over dependency trees to capture the syntactic connections of aspects and opinion words while introducing the BiAffine to jointly refine syntax structures and semantic correlations. However, in the Euclidean space, the neural network models can't well capture the syntactic connections of aspects and opinion words due to the inaccurate dependency trees representation, and the original structures and correlations are affected due to the BiAffine exchange method. Fortunately, dependency trees can be represented well since hyperbolic space can be viewed as continuous simulations of trees, so we propose a hyperbolic graph convolutional networks (HyperGCN) model to handle these challenges. We employ hyperbolic graph convolution with the dependency tree to model syntactic connections between aspects and opinion words, additionally, we also capture the semantic correlations with a hyperbolic graph convolutional network incorporating self-attention mechanism. Particularly, to exchange the relevant features without original syntax structures and semantic correlations being affected, we leverage an attention mechanism with residual structure to exchange relevant features of syntactic and semantic information. The experimental results on three datasets verify the effectiveness of our model.

**Keywords**—HyperGCN, ABSA, attention mechanism, residual structure

## I. INTRODUCTION

Aspect-based sentiment analysis (ABSA) is an entity-oriented fine-grained sentiment analysis task that aims to determine the sentiment polarity of a given aspect in a sentence. In recent years, plenty of work begin to introduce dependency trees and apply neural networks to model the relations between sentences and aspects. Most of these methods apply graph convolutional network and graph attention network over

dependency trees. Among them, Li et al. [1] propose a dual graph convolutional network and employ a BiAffine module for the feature interchange between syntactic structures and semantic correlations to obtain a better representation respectively. But the dependency trees are tree-like structures, and in Euclidean space, the traditional neural network model can't effectively represent the complex tree-like hierarchies due to the limitation of the number of parameters [2]. At the same time, the BiAffine module has the problem that the original syntactic structures and semantic correlations will be affected during feature exchange, for example, the semantic correlations information is affected on account of the introduction of too many irrelevant syntactic features. Fortunately, hyperbolic geometry provides a perfect solution. The hyperbolic space can be viewed as a continuously simulated tree, so we can easily leverage hyperbolic geometry to embed the trees with low distortion [3]. Chami et al. [4] use hyperbolic graph convolutional networks for link prediction and node classification tasks and achieves good performance on multiple datasets.

Inspired by their work, we introduce the hyperbolic graph convolutional network into the ABSA task and propose a hyperbolic graph convolutional network model based on the dual graph convolutional network, and the experiment proves the effectiveness of our proposed model. Our contributions are summarized as follows:

- We effectively represent the hierarchies of dependency trees with hyperbolic geometry, thus modeling the syntactic connections between opinion words and aspects better.
- We design the residual attention mechanism for ensuring that the original syntactic structures and semantic correlations are not affected when exchanging features.

- We conduct extensive experiments on multiple datasets to verify the model's effectiveness.

## II. RELATED WORK

### A. Aspect-based sentiment analysis

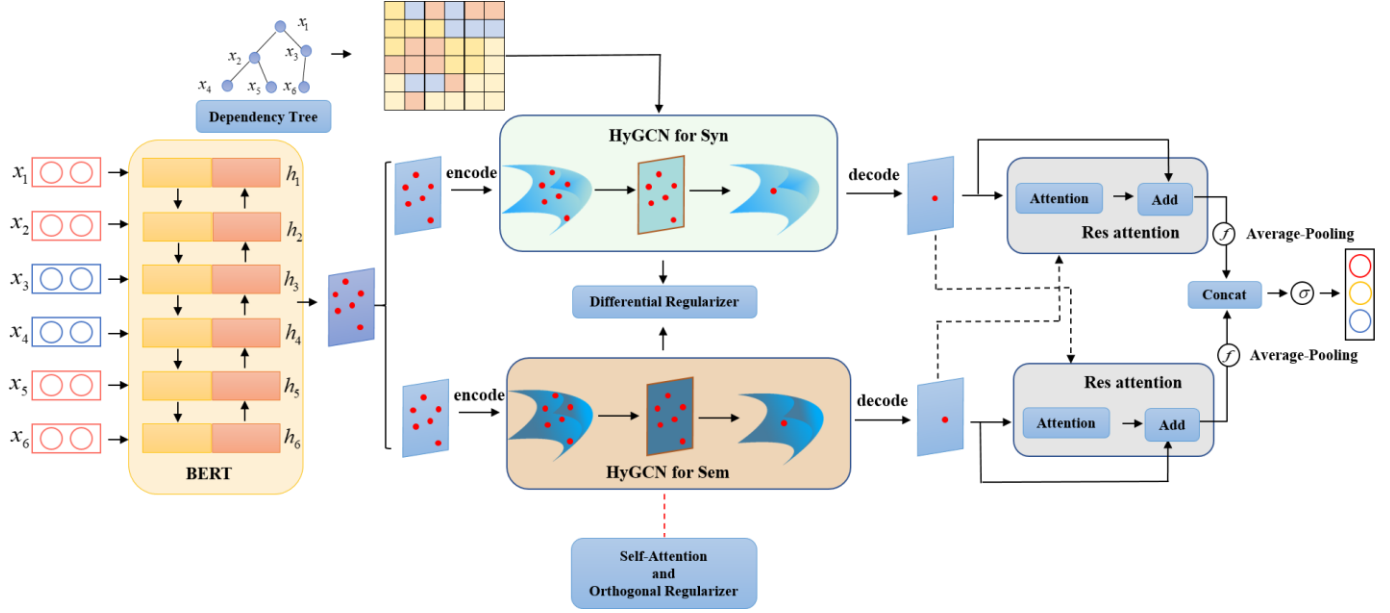


Fig. 1. The framework of HyperGCN. HyGCN for Syn is the hyperbolic graph convolutional networks for extracting syntactic structures and HyGCN for Sem is the hyperbolic graph convolutional networks for extracting semantic correlations. Res attention is the module of attention mechanism with residual structure.

In recent years, most of the recent methods have leverage neural networks to model the relations of the given aspects and the contexts. Among these methods, there are some outstanding works that have obtained relatively good results. For instance, Wang et al. [5] propose an Attention-based Long Short-Term Memory Network for aspect-level sentiment classification. However, the state-of-the-art model should be the graph neural networks over dependency trees. Chen et al. [6] propose a discrete latent opinion tree model as an alternative structure to explicit dependency trees.

### B. Hyperbolic Neural Networks

However, these methods over dependency trees only represent the dependency trees in the Euclidean space, ignoring the problem that the Euclidean space cannot represent the tree structure of the dependency trees well. Fortunately, hyperbolic space is a space similar to tree structure, so it can represent the dependency trees well. Thus, hyperbolic geometry becomes a good alternative. Meanwhile, a variety of hyperbolic neural networks have been proposed and widely used recently. Sonthalia and Gilbert. [7] explore a new method for learning hyperbolic representations, this method can preferentially learns the tree structure of the data. Chen et al. [8] design a hyperbolic capsule networks for multi-label classification, and applies the hyperbolic neural networks to text classification.

## III. PRELIMINARIES

We need to introduce some necessary knowledge of hyperbolic geometry in this section.

**Hyperbolic manifold.**  $L^n$  is a  $n$  dimension and continuous negative curvature  $-c(c > 0)$  hyperbolic manifold embedded in an  $n + 1$  dimension Minkowski space.

$$L^{n,c} = \{x = (x_0, x_1, \dots, x_n) \in R^{n+1} : \langle x, x \rangle_L = -\frac{1}{c}, x_0 > 0\} \quad (1)$$

where  $\langle, \rangle \in R^{n+1} \times R^{n+1}$  is the Minkowski inner product, it is defined as:

$$\langle x, y \rangle_L = -x_0 y_0 + \sum_{k=1}^n x_k y_k \quad (2)$$

**Tangent space.** The centered on point  $x$  tangent space can be defined as:

$$\tau_x L^{n,c} = \{v = (v_0, v_1, \dots, v_n) \in R^{n+1} : \langle v, x \rangle_L = 0\} \quad (3)$$

**Geodesic.** Geodesic is generally used to represent distances in manifold space, it can be expressed as:

$$d_L^c(x, y) = \frac{\arccosh(-\langle x, y \rangle_L c)}{\sqrt{c}} \quad (4)$$

**Exponential and logarithmic maps.** The mapping between tangent space and hyperbolic space generally adopts exponential map  $\exp_x^c(v)$  and logarithmic map  $\log_x^c(y)$ . They can be expressed as:

$$\exp_x^c(v) = \cosh(\sqrt{c} \|v\|_L)x + \frac{v \sinh(\sqrt{c} \|v\|_L)}{\|v\|_L \sqrt{c}} \quad (5)$$

$$\log_x^c(y) = d_L^c(x, y) \frac{y + c < x, y >_L x}{\|y + c < x, y >_L x\|_L} \quad (6)$$

#### IV. PROPOSED MODEL

In this section, we will introduce our HyperGCN model. Figure 1 shows the overall architecture of our model.

##### A. Hyperbolic Graph Convolutional Networks

**BERT encoding.** For the BERT encoding, given an aspect-sentence pair  $(a, s)$  where the sentence  $s = \{w_1, w_2, \dots, w_n\}$  contains  $a = \{a_1, a_2, \dots, a_m\}$ . We input "[CLS]sentence[SEP]aspect[SEP]" into the BERT model to obtain the hidden state representation  $H = \{h_1, h_2, \dots, h_n\}$ .

**Manifold encoding.** Let  $x^{0,E}$  to denote the representation encoded by BERT. Then we need to use exponential mapping to embed  $x^{0,E}$  from Euclidean space into hyperbolic space, we set the origin as:

$$o = (\frac{1}{\sqrt{c}}, 0, \dots, 0) \in L^{n,c}, \text{ and } \langle (0, x^{0,E}), o \rangle = 0 \quad (7)$$

Then the embedding after mapped  $x^{0,L}$  can be obtained:

$$x^{0,L} = \exp_o^c((0, x^{0,E})) \quad (8)$$

**Hyperboloid linear transform.** For the transformation, we first use the logarithmic mapping method to project the hyperbolic point  $x^L$  to the tangent space  $\tau_o L^{j,c}$ . Then we conduct hyperbolic matrix multiplication and hyperbolic paranoid addition, the two formulas are respectively defined as:

$$W \otimes^c x^L = \exp_o^c(W \log_o^c(x^H)) \quad (9)$$

$$x^H \oplus^c b = \exp_{x^L}^c(T_{0 \rightarrow x^L}^c(b)) \quad (10)$$

where  $W$  is weight matrix and  $b$  is bias.

**Hyperboloid neighborhood aggregation.** In hyperbolic space, for the hyperbolic embeddings  $(x_i^L, x_j^L)$  that have been obtained, we also first need to use logarithmic mapping to map  $x_i^L$  and  $x_j^L$  into the tangent space of the origin, then we adopts the hyperbolic aggregation to gain the nodes' representations.

$$AGG^c(x^L)_i = \exp_{x_i^L}^L(\sum_{j=1}^n A_{ij} \log_{x_i^L}^c(x_j^L)) \quad (11)$$

where  $A \in R^{n \times n}$  is the adjacency matrix input

**Hyperboloid non-linear activation.** Let  $c_{l-1}$  denotes the curvature of the layer  $l-1$  and  $c_l$  denotes the curvature of the layer  $l$ . We adopt a nonlinear activation function in the tangent space  $\tau_o L^{n, c_{l-1}}$ , and then map back to the hyperbolic manifold  $L^{n, c_l}$ , the formula is as follows:

$$\sigma^{\otimes^{c_{l-1}, c_l}}(x^L) = \exp_o^{c_l}(\sigma(\log_o^{c_{l-1}}(x^L))) \quad (12)$$

**Manifold decoding.** We embed the output into the tangent space of the origin by the logarithmic map for Euclidean space operations. The formula is defined as:

$$x^{0,\tau} = \log_o^{c_l}(x^{l,L}) \quad (13)$$

**Hyperboloid graph convolutional networks.** We have introduced all the components of the hyperbolic graph convolutional network in the previous content, so the structure of graph convolution operation is as follows:

$$\begin{aligned} h_i^{l,L} &= (W^l \otimes^{c_{l-1}} x_i^{l-1,L}) \oplus^{c_{l-1}} b^l \\ y_i^{l,L} &= AGG^{c_{l-1}}(h_i^{l,L}) \\ x_i^{l,L} &= \sigma^{\otimes^{c_{l-1}, c_l}}(y_i^{l,L}) \end{aligned} \quad (14)$$

Finally, we embed the last layer output of hyperbolic graph convolution into the tangent space of the origin by manifold decoding, and then we can do operations in Euclidean space.

##### B. Dual Hyperbolic Graph Convolutional Networks

We use two hyperbolic graph convolutional networks to capture semantic association and syntactic structure.

For semantic association extraction, we use the self-attention matrix as the adjacency matrix for input. Let  $A^{se} \in R^{n \times n}$  denote the self-attention matrix:

$$A^{se} = \text{soft max}(\frac{QW_1 \times (KW_2)^T}{\sqrt{n}}) \quad (15)$$

where  $Q$  and  $K$  are both BERT encoded representations,  $W_1$  and  $W_2$  are learnable weight matrices,  $n$  is the input dimension. Then we employ orthogonal regularizer [1] for orthogonality among the attention score vectors of all words and make it as a part of the loss.

$$L_{ort} = \|A^{se} A^{seT} - I\|_F \quad (16)$$

where  $I$  is an identity matrix.

Finally, we will get the semantic correlations hidden representations  $H^{se} = (h_1^{se}, h_2^{se}, \dots, h_n^{se})$ , and  $h_i^{se} \in R^n$  denotes hidden representation of node  $i$ . We will also do the same operations for aspect nodes to get aspect semantic correlations hidden representation  $H_a^{se} = (h_{a_1}^{se}, h_{a_2}^{se}, \dots, h_{a_n}^{se})$ . For syntactic structures, we adopt LAL-Parser [9] as the dependency parsing model and input the obtained dependency probability matrix  $A^{sy} \in R^n \times R^n$  to the hyperbolic graph convolutional network. The hyperbolic graph convolutional networks can perfectly represent dependency trees with low distortion because of the tree-like structure of hyperbolic spaces. For learning different semantic correlations and syntactic structures information with hyperbolic graph convolutional network, we employ differential regularizer [1] and make it as a part of the loss.

$$L_{dif} = \frac{1}{\|A^{se} - A^{sy}\|_F} \quad (17)$$

We also get syntactic structures hidden representation  $H^{sy} = (h_1^{sy}, h_2^{sy}, \dots, h_n^{sy})$  and aspect syntactic hidden representation  $H_a^{sy} = (h_{a_1}^{sy}, h_{a_2}^{sy}, \dots, h_{a_n}^{sy})$ .

### C. Attention Mechanism with Residual Structure

We leverage attention mechanism with residual structure to exchange the relevant features without original syntax structures and semantic correlations being affected. We process semantic correlations hidden representation and syntactic structures hidden representation as follows:

$$H^{se'} = \text{soft max}\left(\frac{H^{se}W_3(H^{sy}W_4)^T}{\sqrt{n}}\right)H^{sy}W_5 \quad (18)$$

$$H^{se'} = H^{se'} + H^{se}$$

$$H^{sy'} = \text{soft max}\left(\frac{H^{sy}W_6(H^{se}W_7)^T}{\sqrt{n}}\right)H^{se}W_8 \quad (19)$$

$$H^{sy'} = H^{sy'} + H^{sy}$$

where  $W_3, W_4, W_5, W_6, W_7$  and  $W_8$  are trainable weight matrix.

Finally, we apply average pooling on  $H_a^{se}$  and  $H_a^{sy}$ :

$$\begin{aligned} h_a^{se} &= \text{AveragePooling}(H_a^{se}) \\ h_a^{sy} &= \text{AveragePooling}(H_a^{sy}) \end{aligned} \quad (20)$$

For BERT encoding, we concat  $h_a^{se}, h_a^{sy}$  and  $[CLS]$  after pooling:

$$f = \text{Concat}(h_a^{se}, h_a^{sy}, h_{CLS}) \quad (21)$$

We compute the probability contribution of sentiment applying a linear layer and a softmax function:

$$p(a) = \text{soft max}(W_p f + b_p) \quad (22)$$

where  $W_p$  and  $b$  are trainable weight matrix and bias.

### D. Loss Function

We norm all trainable model parameters as part of the loss function:

$$L_{par} = \sqrt{\theta_1^2 + \theta_2^2 + \dots + \theta_t^2} \quad (23)$$

where  $\theta_i$  is trainable model parameter and  $t$  is the number of trainable model parameters.

We also apply the cross entropy loss function as part of the loss function:

$$L_{cross} = - \sum_{(s,a) \in D} \sum_{c \in C} \log p(a) \quad (24)$$

where  $D$  is a collection of aspect-sentence pairs,  $C$  is the collection of distinct sentiment classes.

Finally, we combine all the loss function parts as our final loss function to train the model better:

$$L_{total} = L_{cross} + \lambda_1 L_{ort} + \lambda_2 L_{dif} + \lambda_3 L_{par} \quad (25)$$

where  $\lambda_1, \lambda_2$  and  $\lambda_3$  are regularization coefficient.

## V. EXPERIMENTS

### A. Datasets

We do experiments on some public datasets including Restaurant14, Laptop14 and Twitter. Both Restaurant and Laptop are from SemEval 2014 [14] that are comments on Laptop and Restaurant. Following [10], we delete instances using the ‘‘conflict’’ label. The Twitter dataset [15] is also a very important dataset for us, which is mainly composed of some tweets.

### B. Implementation and Parameter Settings

Our initial word embeddings, dependency parser, and input to BERT all follow [1]. Furthermore, following [16], we set up a self-loop for each node in the hyperbolic graph convolutional network.

### C. Baselines

To verify the performance of our proposed model (HyperGCN), we compare HyperGCN with multiple baselines, including DGEDT+BERT [11], DualGCN+BERT [1], BERT[12], T-GCN+BERT [13], dotGCN+BERT [6].

TABLE I. THE COMPARISON PERFORMANCE BETWEEN HYPERGCN AND BASELINES

Models	Restaurant14		Laptop 14		Twitter	
	Accuracy	Macro-F1	Accuracy	Macro-F1	Accuracy	Macro-F1
BERT [12]	86.15	80.29	81.01	76.69	75.18	74.01
DGEDT+BERT [11]	86.30	80.00	79.80	75.60	77.90	75.40
DualGCN+BERT [1]	87.13	81.16	<b>81.80</b>	78.10	77.40	76.02
T-GCN+BERT [13]	86.16	79.95	80.88	77.03	76.45	75.25
dotGCN+BERT [6]	86.16	80.49	81.03	78.10	78.11	77.00
Our HyperGCN+BERT	<b>87.49</b>	<b>82.19</b>	80.85	<b>78.18</b>	<b>78.14</b>	<b>77.16</b>

TABLE II. ABLATION EXPERIMENT RESULTS

Models	Restaurant14		Laptop14		Twitter	
	Accuracy	Macro-F1	Accuracy	Macro-F1	Accuracy	Macro-F1
w/o attention	86.51	80.96	80.06	76.68	77.40	76.11
w/o hyperbolic	85.70	79.73	78.96	74.36	76.66	75.21
Our HyperGCN +BERT	<b>87.49</b>	<b>82.19</b>	<b>80.85</b>	<b>78.18</b>	<b>78.14</b>	<b>77.16</b>

#### D. Results

Table I shows the comparison results between our model(HyperGCN) and all Baselines. We evaluate all models with Accuracy and Macro-F1. In the experiment, we use BERT as the encoding method. The analyses of the results are as follows:

Compared with the BERT model[12], we obtain an improvements of 3.15, 1.9 and 1.49 Macro-F1 score on Twitter, Restaurant and Laptop datasets respectively. We also have an improvements on the accuracy score, particularly, 2.96 accuracy score is improved on Twitter dataset. At the same time, in the Restaurant and Laptop datasets, the dimension of our final representation (below 80 dimensions) is much lower than the 768 dimensions of other baselines, which verifies the high efficiency of hyperbolic neural network representation in low-dimensional space. In addition, our model also performs better than the baselines (DGEDT+BERT [11] , DualGCN+BERT [1] ) that employ BiAffine for feature interchange, it shows that the attention mechanism with residual structure we adopt is more effective than BiAffine.

#### E. Ablation Study

We conduct extensive ablation experiments for verifying the effectiveness of each module, and the experiment results are shown in Table II. We conduct ablation experiments on BERT encoding, we first ablate the attention mechanism, which causes the syntactic structures and semantic associations without exchanging features, and we can see a significant drop in BERT encoding experiment. We also use Euclidean GCN instead of hyperbolic GCN module, which will cause the dependency tree to not be well represented. This directly leads to a large drop in performance on all datasets, such as a drop of 2.85 accuracy score and 3.59 Macro-F1 score on Laptop

#### VI. CONCLUSION

In this paper, we propose a HyperGCN model which can represent the dependency trees with low distortion in the hyperbolic space, overcoming the problem that the traditional neural network can't represent the complex dependency trees well due to the parameter number limitation in the Euclidean space. Syntactic structures and semantic correlations are well extracted by two hyperbolic graph convolutional networks. Furthermore, we use a residual-structured Attention mechanism to exchange syntactic structures and semantic correlations relevant features without destroying the original information. Extensive experimental results show that our model is effective and outperforms graph convolutional networks in Euclidean space.

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