Model Exercises

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HW link

Import packages

```
library(tidyverse)
## -- Attaching packages -----
                                              ----- tidyverse 1.3.1 --
## v ggplot2 3.3.6
                 v purrr
v dplyr
                            0.3.4
## v tibble 3.1.7
                            1.0.9
## v tidyr
          1.2.0 v stringr 1.4.0
## v readr
         2.1.2 v forcats 0.5.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                  masks stats::lag()
library(modelr)
```

Familiarize yourself with the heights data set provided with the modelr package.

Solution

```
data(heights)
heights
```

```
## # A tibble: 7,006 x 8
     income height weight
##
                            age marital sex
                                               education afqt
##
      <int> <dbl> <int> <int> <fct>
                                                   <int> <dbl>
                                        <fct>
   1 19000
                                                      13 6.84
##
                60
                      155
                             53 married female
## 2 35000
                70
                      156
                             51 married female
                                                      10 49.4
  3 105000
##
                65
                      195
                             52 married male
                                                      16 99.4
## 4 40000
                63
                      197
                             54 married female
                                                      14 44.0
## 5 75000
                66
                      190
                            49 married male
                                                      14 59.7
## 6 102000
                      200
                68
                             49 divorced female
                                                     18 98.8
## 7
                74
                      225
                             48 married male
                                                     16 82.3
## 8 70000
                64
                      160
                             54 divorced female
                                                      12 50.3
## 9 60000
                69
                      162
                             55 divorced male
                                                      12 89.7
## 10 150000
                69
                      194
                             54 divorced male
                                                      13 96.0
## # ... with 6,996 more rows
```

?heights

Create a list of formulas for modeling income with:

- height
- height · weight
- linear combination of all variables

Solution

```
concat_col <- paste(colnames(heights)[-1], collapse=" + ")
formulas <- paste0("income ~ ", c("height", "height * weight", concat_col))
formulas</pre>
```

```
## [1] "income ~ height"
## [2] "income ~ height * weight"
## [3] "income ~ height + weight + age + marital + sex + education + afqt"
```

From the data, remove rows containing NA's. Fit the linear model with the formulas from exercise 2.

Solution

```
heights <- heights %>%
  drop_na()
model_height <- lm(formula = formulas[1], data = heights)</pre>
model_height_times_weight <- lm(formula = formulas[2], data = heights)</pre>
model_all <- lm(formula = formulas[3], data = heights)</pre>
summary(model_height)
##
## Call:
## lm(formula = formulas[1], data = heights)
## Residuals:
     Min
              1Q Median
                            3Q
## -92970 -31753 -11225 14620 320574
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -161639.1 11215.0 -14.41 <2e-16 ***
## height
                  3031.1
                             166.8
                                    18.18
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 55500 on 6643 degrees of freedom
## Multiple R-squared: 0.04737,
                                   Adjusted R-squared: 0.04723
## F-statistic: 330.3 on 1 and 6643 DF, p-value: < 2.2e-16
summary(model_height_times_weight)
##
## Call:
## lm(formula = formulas[2], data = heights)
##
## Residuals:
       Min
                1Q Median
                               ЗQ
                                      Max
## -100812 -31099 -11073
                            14835 322415
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                -2.164e+05 4.652e+04 -4.652 3.36e-06 ***
                 4.079e+03 7.000e+02
                                       5.827 5.90e-09 ***
## height
## weight
                  1.393e+02
                            2.369e+02
                                       0.588
                                                 0.557
## height:weight -3.286e+00 3.510e+00 -0.936
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 55420 on 6641 degrees of freedom
## Multiple R-squared: 0.0507, Adjusted R-squared: 0.05028
## F-statistic: 118.2 on 3 and 6641 DF, p-value: < 2.2e-16
```

summary(model_all)

```
##
## Call:
## lm(formula = formulas[3], data = heights)
## Residuals:
##
      Min
               1Q Median
                              3Q
                                     Max
## -115521 -25139
                   -5477
                          14904 326890
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                              20565.27 -2.159 0.03085 *
                   -44409.17
                                        1.288 0.19796
## height
                     293.26
                               227.77
## weight
                     -22.62
                                15.41 -1.468 0.14227
## age
                    -401.81
                               270.53 -1.485 0.13753
## maritalmarried
                   14204.65
                               1754.67
                                        8.095 6.74e-16 ***
## maritalseparated 3364.49
                               3055.37
                                        1.101 0.27086
                             1990.67
## maritaldivorced
                     5586.83
                                         2.807 0.00502 **
## maritalwidowed
                  10663.36
                               4290.03
                                         2.486 0.01296 *
## sexfemale
                               1744.56 -14.225 < 2e-16 ***
                   -24815.77
                   5944.87
## education
                               289.14 20.561 < 2e-16 ***
## afqt
                     389.42
                                26.52 14.685 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 49100 on 6634 degrees of freedom
## Multiple R-squared: 0.2556, Adjusted R-squared: 0.2545
## F-statistic: 227.8 on 10 and 6634 DF, p-value: < 2.2e-16
```

For each fit, calculate RMSE.

Solution

```
rmse(model_height, heights)

## [1] 55496.35

rmse(model_height_times_weight, heights)

## [1] 55399.18

rmse(model_all, heights)
```

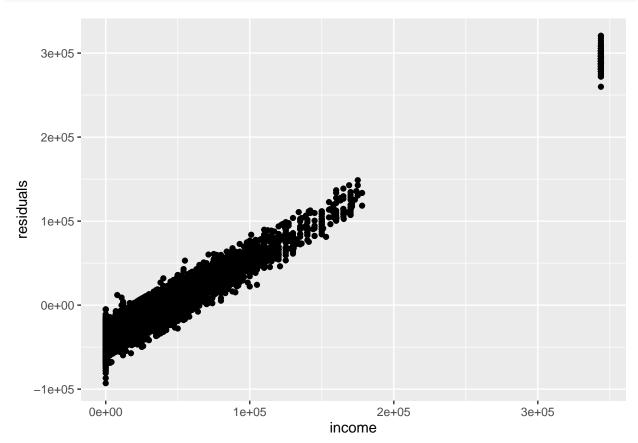
[1] 49056.82

For each model, add residuals to the data and plot their distribution. (Hint: use lift_dl().)

Solution

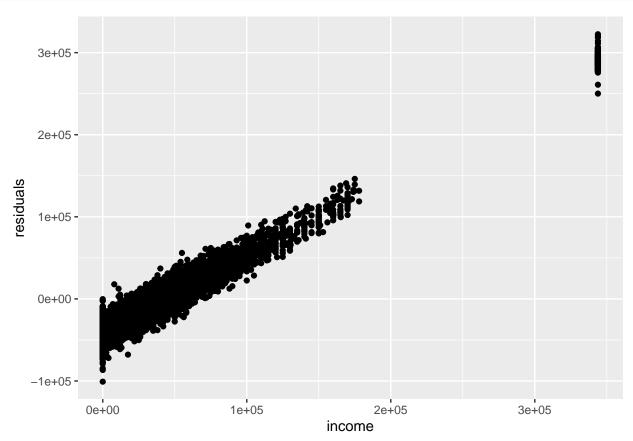
```
residuals <- resid(model_height)

ggplot(data = heights, aes(x = income, y = residuals)) +
   geom_point()</pre>
```



```
residuals <- resid(model_height_times_weight)

ggplot(data = heights, aes(x = income, y = residuals)) +
    geom_point()</pre>
```



```
residuals <- resid(model_all)

ggplot(data = heights, aes(x = income, y = residuals)) +
  geom_point()</pre>
```

