

Network Summary

Для получения графа друзей я использую такие пакеты как: *igraph*, *rmarkdown*, *dplyr*, *vkR*. Мы используем пакет *vkR* для запроса и авторизации. С помощью OAuth мы получаем *access_token*. Теперь можно отправлять запросы используя *access_token* и получать информацию из приложения vk. Далее используем запрос *getFriends()*, чтобы получить граф друзей. Также удалим вершины, степень которых равна 0.

```
library(igraph)
library(rmarkdown)
library(dplyr)
library("vkR", lib.loc = "~/R/win-library/3.5" )
library(data.table)
#vkOAuth(6481300, 'friends')
```

```
setAccessToken(access_token = '458952d13d34de0037b043e41d2edf9cd98d45aeaf3802
111d86798b20a5208a050b642270da9183c1546')

my_friends <- getFriends(user_id = 182468682, fields = 'sex')
my_friends <- subset(my_friends$items, is.na(my_friends$items$deactivated))
n <- nrow(my_friends)
adjacency <- matrix(nrow = n, ncol = n)
dt <- data.table(my_friends$id)
l <- length(my_friends$id)
for (i in 1:l) {
  dt$num[i] <- i
}
for (i in 1:n) {
  user <- getFriends(user = my_friends$id[i])$items
  u <- length(user)
  for (j in 1:u) {
    if(is.na(match(user[j], dt$V1)) == F) {
      x <- match(user[j], dt$V1)
      adjacency[i,x] <- 1
      adjacency[x,i] <- 1
    }
  }
}
g <- graph_from_adjacency_matrix(adjacency, mode = "undirected")
V(g)
+ 190/190 vertices, from d857795:
```

```

[1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18
19 20 21 22 23 24 25 26

[27] 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44
45 46 47 48 49 50 51 52

[53] 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70
71 72 73 74 75 76 77 78

[79] 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96
97 98 99 100 101 102 103 104

[105] 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120 121 122
123 124 125 126 127 128 129 130

[131] 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 146 147 148
149 150 151 152 153 154 155 156

[157] 157 158 159 160 161 162 163 164 165 166 167 168 169 170 171 172 173 174
175 176 177 178 179 180 181 182

[183] 183 184 185 186 187 188 189 190

```

```

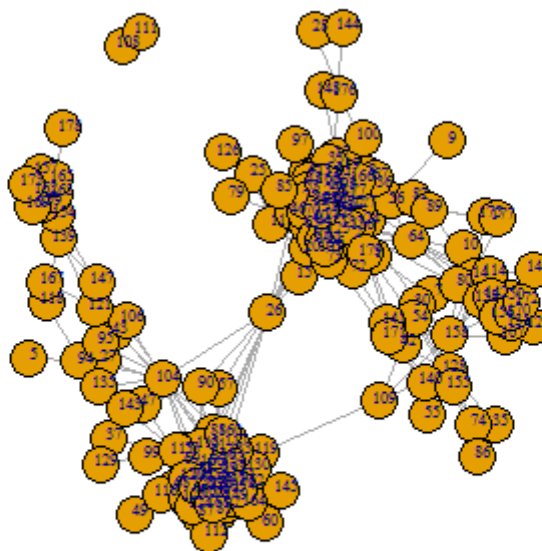
g <- delete.vertices(simplify(g), degree(g) == 0)
simplify(g)
IGRAPH 13ea479 U--- 179 1294 --
+ edges from 13ea479:
  [1] 1-- 2 1-- 7 1-- 21 1-- 38 1-- 64 1-- 72 1-- 83 1-- 96 1--125 2-- 3 2
  -- 20 2-- 21 2-- 22 2-- 32 2-- 44
  [16] 2-- 45 2-- 51 2-- 59 2-- 71 2-- 72 2-- 73 2-- 77 2-- 96 2--125 2--127 2
  --166 3-- 4 3-- 12 3-- 18 3-- 21
  [31] 3-- 22 3-- 23 3-- 31 3-- 32 3-- 34 3-- 39 3-- 40 3-- 44 3-- 45 3-- 48 3
  -- 51 3-- 56 3-- 59 3-- 70 3-- 71
  [46] 3-- 72 3-- 75 3-- 77 3-- 83 3-- 96 3-- 98 3--100 3--102 3--103 3--125 3
  --127 3--136 3--137 3--151 3--166
  [61] 3--168 3--179 4-- 12 4-- 22 4-- 23 4-- 39 4-- 45 4-- 46 4-- 51 4-- 59 4
  -- 63 4-- 67 4-- 70 4-- 75 4-- 97
  [76] 4--168 5-- 94 6-- 16 6-- 41 6-- 52 6-- 53 6-- 57 6-- 61 6-- 62 6-- 65 6
  -- 66 6-- 69 6-- 78 6-- 81 6-- 84
  [91] 6-- 87 6-- 92 6-- 93 6--101 6--105 6--110 6--113 6--117 6--123 6--132 6
  --134 6--149 6--150 6--152 6--153
  [106] 6--160 6--161 6--164 6--174 7-- 10 7-- 42 8-- 18 8-- 19 8-- 31 8-- 32 8
  -- 33 8-- 34 8-- 51 8-- 59 8-- 64
  [121] 8-- 67 8-- 77 8-- 98 8--151 9-- 56
+ ... omitted several edges

```

```

plot(g, vertex.label.font = 5, vertex.label.cex = 0.5, vertex.label.dist = 0.5)

```



```

ecount(g)
[1] 1294
vcount(g)
[1] 179
# the length of the "longest shortest path"
diameter(g)
[1] 10
get_diameter(g)
+ 11/179 vertices, from a062e4e:
[1] 86 155 30 32 34 26 104 121 139 165 178
graph.density(g)
[1] 0.08122528

```

Мы выяснили, что граф g имеет 179 вершин и 1294 ребер. Диаметр графа равен 10. В графе g диаметр может быть построен следующим образом: 86 155 30 32 34 26 104 121 139 165 178. Что касается плотности графа, то она равна ~ 0.08 .

Degree distribution

```

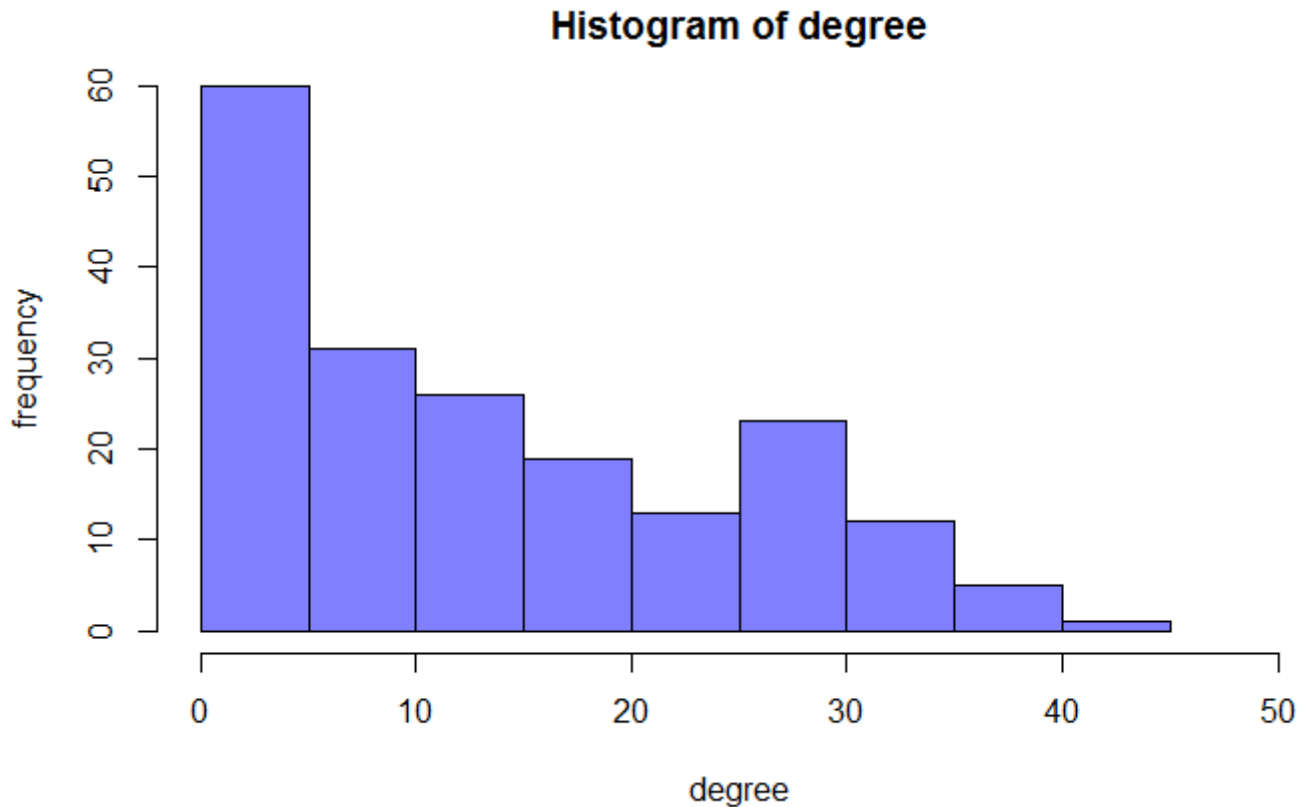
deg = degree(g)
summary(degrees)

```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
------	---------	--------	------	---------	------

```
1.00    4.00   12.00   14.46   24.00   43.00
```

```
hist(degree, col=rgb(0, 0, 1,.5), xlim=c(0, 50), xlab="degree", ylab="frequency")
```



Из гистограммы видно распределение степени вершин. Степенью узла называется количество узлов, связанных с данным узлом. Максимальная степень равна 43, а минимальная - 1. Медиана степеней вершин составляет 12, в то время как среднее значение равно 14.46. Из гистограммы видно, что большинство вершин имеет степень от 0 до 5, и только малая часть - выше 40.

Diameter

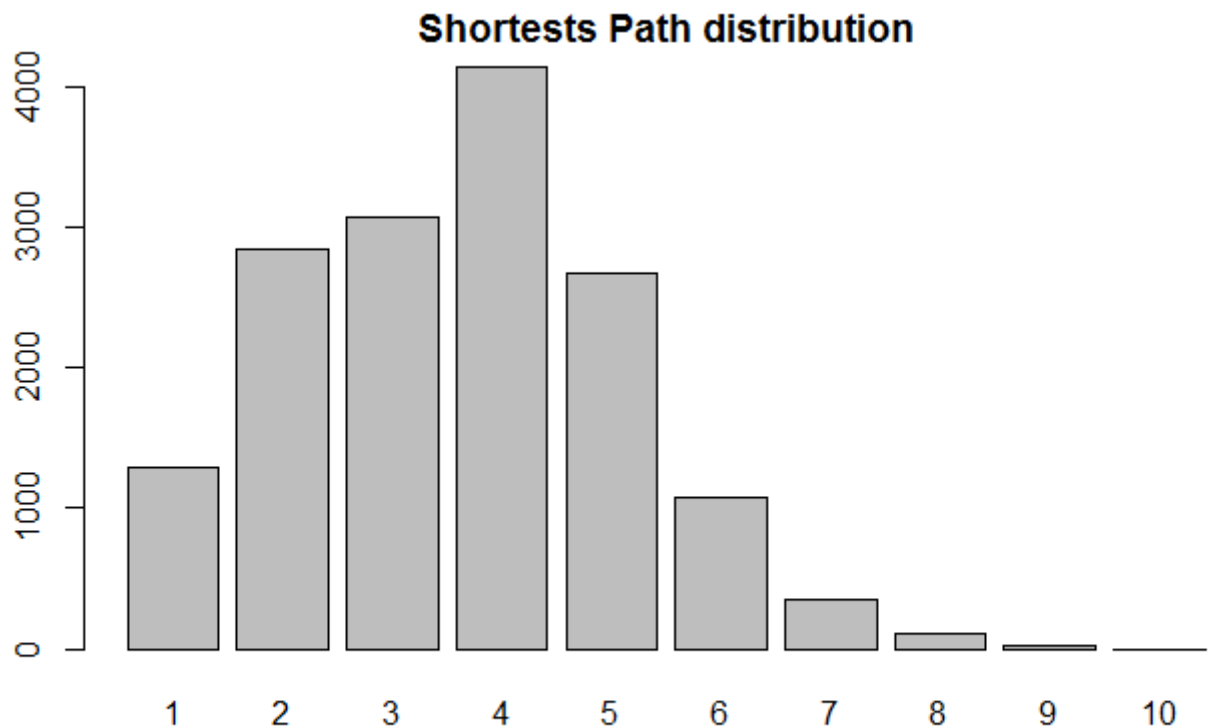
```
#the longest shortest path  
diameter(g)  
[1] 10
```

Radius

```
#the shortest shortest path  
radius(g)  
[1] 1
```

Shortest Path distribution

```
tab <- as.table(path.length.hist(g)$res)
names(tab) <- 1:length(tab)
barplot(tab, main = 'Shortests Path distribution')
```



Clustering Coefficients

```
transitivity(g, type="localaverage")
[1] 0.5903219
transitivity(g, type="global")
[1] 0.5597836
```

Коэффициент кластеризации является мерой степени, с которой узлы в графе стремятся сгруппироваться.

Structural Analysis

Degree/Closeness/Betweenness centralities. Top nodes interpretation

Нагрузка узла (Betweenness centrality) характеризует долю проходящих через узел кратчайших путей и узлы с высоким значением betweenness centrality являются наиболее загруженными. Эту величину можно считать индикатором наиболее общительных людей в

социальной сети. Узел под номером 26 имеет максимальное значение данной характеристики, отметим её на графе.

```
betw <- betweenness(g)
```

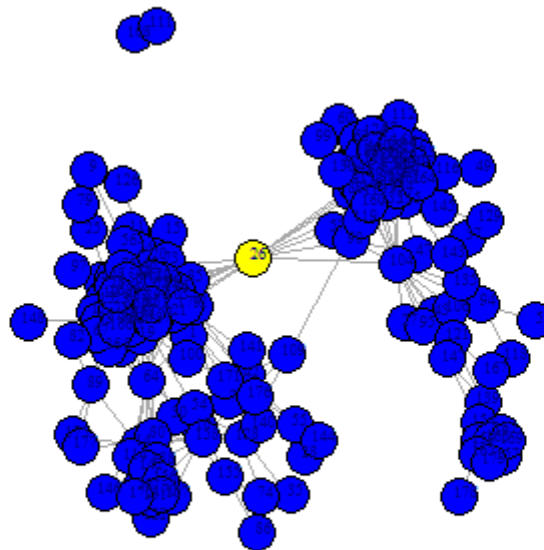
```
summary(betw)
```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
0.000	3.387	29.727	226.279	218.710	6384.425

```
V(g)$color <- ifelse(betw>=max(betw), "yellow", "blue")
```

```
plot(g, vertex.label.font = 5, vertex.label.cex = 0.5, vertex.label.dist = 0.5, main = "Top node Betweennees centralities")
```

Top node Betweennees centralities



Центральность по степени (Degree centrality) — это отношение количества связей определённого узла к общему количеству других узлов. Для центральности по степени мы имеем: минимальное = 1; медиана = 12; среднее значение = 14.46.

Closeness centrality — это средняя длина кратчайшего пути между узлом и всеми другими узлами графика. Таким образом, чем больше closeness centrality узла тем ближе он ко всем остальным узлам.

```
deg = degree(g)
```

```
summary(deg)
```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
1.00	4.00	12.00	14.46	24.00	43.00

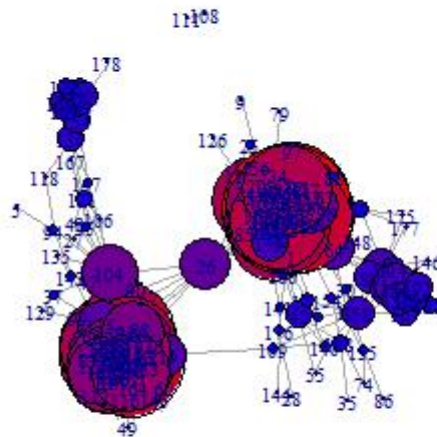
```
f = 500

palette = colorRampPalette(c('blue','red'))

degCol = palette(f)[as.numeric(cut(deg,breaks = fine))]

plot(g, layout=layout.fruchterman.reingold(g), vertex.color=degCol, vertex.size=deg*1.5, vertex.label.cex=0.6, main="Degree centrality")
```

Degree centrality



```
close = closeness(g)
```

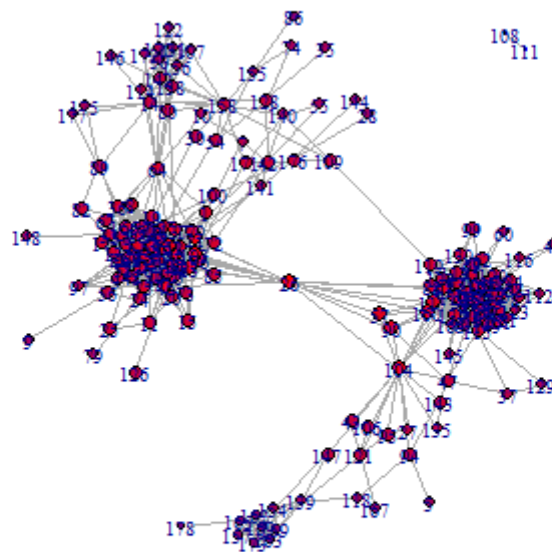
```
summary(close)
```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
3.156e-05	9.565e-04	1.041e-03	1.010e-03	1.090e-03	1.280e-03

```
closn = palette(f)[as.numeric(cut(close,breaks = f))]

plot(g,layout =layout.fruchterman.reingold(g) , vertex.color=closn, vertex.size=close*5000, vertex.label.cex=0.6, main="Closeness centrality")
```

Closeness centrality

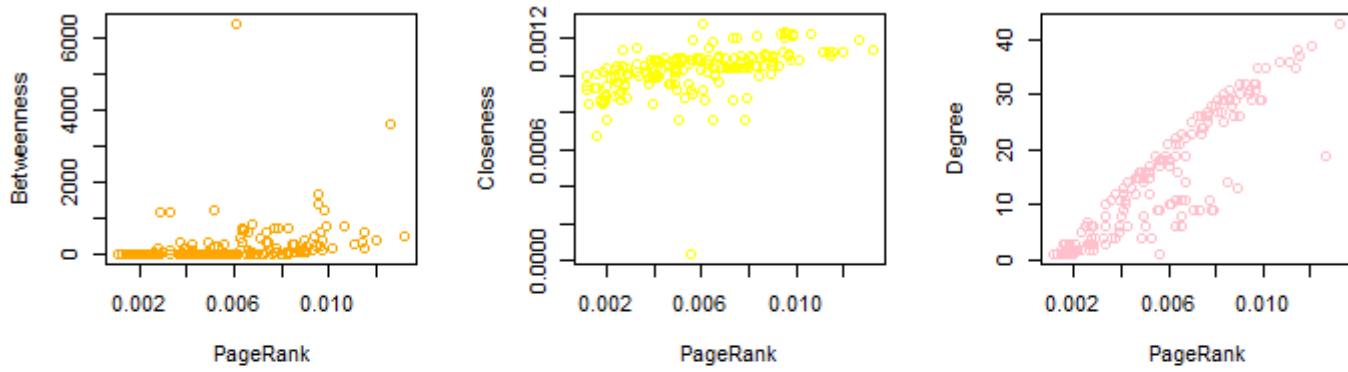


Page-Rank. Comparison with centralities

```
pr=page.rank(g)$vector
```

```
op <- par(mfrow = c(2, 3))  
plot(pr, betw, xlab = 'PageRank' , ylab = 'Betweenness' , col = 'orange' )  
plot(pr, close, xlab = 'PageRank' , ylab = 'Closeness' , col = 'yellow' )
```

```
plot(pr, deg, xlab = 'PageRank' , ylab = 'Degree' , col = 'pink' )
```

Из первого графика видно, что переменная PageRank принимает значения больше, чем betweenness. Из этих графиков можно сделать вывод, что, чем больше PageRank тем больше степень узла.

Assortative Mixing according to node attributes

Hide

```
assortativity(g, types1 = (V(g)))
[1] 0.2009739
```

Hide

```
assortativity.degree(g, directed = F)
[1] 0.2612559
```

Ассортативное смешивание (assortative mixing) – тенденция узлов сети формировать связи с аналогичными узлами. В сети возможна ситуация, когда узлы, имеющие большую степень, преимущественно связаны с узлами, имеющими большую степень. При такой сети коэффициент ассортативности $r > 0$. А отрицательное значение r показывает о взаимодействии узлов, имеющих разные степени.

Node structural equivalence/similarity

Используем функцию `similarity()`, которая вычисляет схожесть узлов на основе их соединений.

Hide

```
sim <- similarity(g, vids = V(g))
summary(sim)
```

V5	V1	V6	V2	V3	V4
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.03977	Mean :0.08061	Mean :0.1127	Mean :0.07552	Mean :0.1128	Mean :0.01007
3rd Qu.:0.06573	3rd Qu.:0.17446	3rd Qu.:0.2000	3rd Qu.:0.15000	3rd Qu.:0.1402	3rd Qu.:0.00000
V11	V7	V12	V8	V9	V10
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.01498	Mean :0.07187	Mean :0.00774	Mean :0.01193	Mean :0.03194	Mean :0.103
3rd Qu.:0.00000	3rd Qu.:0.08514	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.03322	3rd Qu.:0.164
V17	V13	V18	V14	V15	V16
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.09768	Mean :0.0349	Mean :0.03177	Mean :0.1090	Mean :0.08938	Mean :0.1071
3rd Qu.:0.13485	3rd Qu.:0.0000	3rd Qu.:0.00000	3rd Qu.:0.1101	3rd Qu.:0.12772	3rd Qu.:0.1802
V23	V19	V20	V21	V22	V24
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.06822	Mean :0.05167	Mean :0.09644	Mean :0.1031	Mean :0.1140	Mean :0.04400
3rd Qu.:0.12019	3rd Qu.:0.08167	3rd Qu.:0.17108	3rd Qu.:0.1766	3rd Qu.:0.1968	3rd Qu.:0.07825

V29	V25	V30	V26	V27	V28
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Q
Median :0.00000	Median :0.05000	Median :0.00000	Median :0.00000	Median :0.00000	Media
Mean :0.02287	Mean :0.06892	Mean :0.02450	Mean :0.0227	Mean :0.01276	Mean
3rd Qu.:0.00000	3rd Qu.:0.09524	3rd Qu.:0.02598	3rd Qu.:0.0000	3rd Qu.:0.00000	3rd Q
5	V31	V36	V32	V33	V34
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median
Mean :0.1039	Mean :0.1137	Mean :0.06110	Mean :0.09329	Mean :0.1178	Mean
3rd Qu.:0.1633	3rd Qu.:0.1827	3rd Qu.:0.08333	3rd Qu.:0.11966	3rd Qu.:0.1879	3rd Qu.
V42	V37	V44	V38	V39	V40
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :
Mean :0.01233	Mean :0.1044	Mean :0.01848	Mean :0.109	Mean :0.1165	Mean :
3rd Qu.:0.00000	3rd Qu.:0.1673	3rd Qu.:0.00000	3rd Qu.:0.200	3rd Qu.:0.1811	3rd Qu.:
V47	V43	V48	V44	V45	V46
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Q
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Media
Mean :0.03104	Mean :0.08255	Mean :0.07639	Mean :0.1077	Mean :0.09329	Mean
3rd Qu.:0.00000	3rd Qu.:0.14352	3rd Qu.:0.15000	3rd Qu.:0.1766	3rd Qu.:0.16667	3rd Q

V49		V50		V51		V52	
V53	V54						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.01709	Mean :0.04218	Mean :0.1109	Mean :0.11634	Mean :0.07867	Mean :0.02996	Mean :0.1898	Mean :0.07806
3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.1898	3rd Qu.:0.07806	3rd Qu.:0.11513	3rd Qu.:0.03125	3rd Qu.:0.11513	3rd Qu.:0.03125
V55		V56		V57		V58	
V59	V60						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.01561	Mean :0.04258	Mean :0.03592	Mean :0.08125	Mean :0.1158	Mean :0.02766	Mean :0.05263	Mean :0.15476
3rd Qu.:0.00000	3rd Qu.:0.07692	3rd Qu.:0.05263	3rd Qu.:0.15476	3rd Qu.:0.1807	3rd Qu.:0.00000	3rd Qu.:0.05263	3rd Qu.:0.15476
V61		V62		V63		V64	
V65	V66						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.09680	Mean :0.07767	Mean :0.09774	Mean :0.04509	Mean :0.1086	Mean :0.1090	Mean :0.16398	Mean :0.07500
3rd Qu.:0.09839	3rd Qu.:0.13393	3rd Qu.:0.16398	3rd Qu.:0.07500	3rd Qu.:0.1202	3rd Qu.:0.1166	3rd Qu.:0.16398	3rd Qu.:0.07500
V67		V68		V69		V70	
V71	V72						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.05498	Mean :0.06405	Mean :0.08035	Mean :0.0811	Mean :0.1139	Mean :0.04859	Mean :0.12250	Mean :0.1583
3rd Qu.:0.08514	3rd Qu.:0.08893	3rd Qu.:0.12250	3rd Qu.:0.1583	3rd Qu.:0.2082	3rd Qu.:0.07846	3rd Qu.:0.12250	3rd Qu.:0.1583

V73		V74		V75		V76	
V77	V78						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.05205	Mean :0.01744	Mean :0.07784	Mean :0.11111	Mean :0.1036	Mean :0.1144	Mean :0.08392	Mean :0.1040
3rd Qu.:0.08392	3rd Qu.:0.00000	3rd Qu.:0.12702	3rd Qu.:0.1154	3rd Qu.:0.1647	3rd Qu.:0.1040	3rd Qu.:0.08392	3rd Qu.:0.1040
V79	V80	V81	V82				
V83	V84						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.01388	Mean :0.04728	Mean :0.1034	Mean :0.02074	Mean :0.09197	Mean :0.09935	Mean :0.01388	Mean :0.04728
3rd Qu.:0.00000	3rd Qu.:0.02857	3rd Qu.:0.1145	3rd Qu.:0.00000	3rd Qu.:0.16905	3rd Qu.:0.09214	3rd Qu.:0.00000	3rd Qu.:0.02857
V85	V86	V87	V88				
V89	V90						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.04722	Mean :0.01164	Mean :0.08719	Mean :0.08635	Mean :0.02717	Mean :0.03715	Mean :0.04722	Mean :0.01164
3rd Qu.:0.09233	3rd Qu.:0.00000	3rd Qu.:0.10263	3rd Qu.:0.14550	3rd Qu.:0.04712	3rd Qu.:0.05635	3rd Qu.:0.09233	3rd Qu.:0.00000
V91	V92	V93	V94				
V95	V96						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.1052	Mean :0.11272	Mean :0.1175	Mean :0.01941	Mean :0.02631	Mean :0.08441	Mean :0.1052	Mean :0.11272
3rd Qu.:0.1176	3rd Qu.:0.09203	3rd Qu.:0.1051	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.16065	3rd Qu.:0.1176	3rd Qu.:0.09203

V97		V98		V99		V100	
V101	V102						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.03531	Mean :0.1113	Mean :0.02457	Mean :0.03289	Mean :0.03531	Mean :0.0711	Mean :0.1062	Mean :0.1099
3rd Qu.:0.03750	3rd Qu.:0.1909	3rd Qu.:0.00000	3rd Qu.:0.05480	3rd Qu.:0.1099	3rd Qu.:0.1319	3rd Qu.:0.1062	3rd Qu.:0.1099
V103		V104		V105		V106	
V107	V108						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.09152	Mean :0.04028	Mean :0.11433	Mean :0.03104	Mean :0.04127	Mean :0.005587	Mean :0.16173	Mean :0.06822
3rd Qu.:0.16173	3rd Qu.:0.06822	3rd Qu.:0.08973	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.000000	3rd Qu.:0.00000	3rd Qu.:0.000000
V109		V110		V111		V112	
V113	V114						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.02521	Mean :0.1049	Mean :0.005587	Mean :0.04222	Mean :0.07965	Mean :0.0423	Mean :0.15395	Mean :0.1140
3rd Qu.:0.00000	3rd Qu.:0.1140	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.15395	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000
V115		V116		V117		V118	
V119	V120						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.06585	Mean :0.03339	Mean :0.09821	Mean :0.01557	Mean :0.06785	Mean :0.08022	Mean :0.11765	Mean :0.03994
3rd Qu.:0.11765	3rd Qu.:0.03994	3rd Qu.:0.13636	3rd Qu.:0.00000	3rd Qu.:0.10620	3rd Qu.:0.10317	3rd Qu.:0.10620	3rd Qu.:0.10317

V121		V122		V123		V124	
V125		V126					
Min.	:0.00000	Min.	:0.00000	Min.	:0.00000	Min.	:0.00000
:0.00000	Min.	:0.00000					Min.
1st Qu.:	:0.00000	1st Qu.:	:0.00000	1st Qu.:	:0.00000	1st Qu.:	:0.00000
Qu.:	:0.00000	1st Qu.:	:0.00000				1st
Median	:0.00000	Median	:0.00000	Median	:0.00000	Median	:0.00000
an	:0.00000	Median	:0.00000				Medi
Mean	:0.02044	Mean	:0.03425	Mean	:0.08323	Mean	:0.07878
:0.08507	Mean	:0.01542					Mean
3rd Qu.:	:0.00000	3rd Qu.:	:0.00000	3rd Qu.:	:0.11806	3rd Qu.:	:0.08995
Qu.:	:0.16954	3rd Qu.:	:0.00000				3rd
V127		V128		V129		V130	
V131		V132					
Min.	:0.00000	Min.	:0.00000	Min.	:0.00000	Min.	:0.00000
:0.00000	Min.	:0.00000					Min.
1st Qu.:	:0.00000	1st Qu.:	:0.00000	1st Qu.:	:0.00000	1st Qu.:	:0.00000
Qu.:	:0.00000	1st Qu.:	:0.00000				1st
Median	:0.00000	Median	:0.00000	Median	:0.00000	Median	:0.00000
an	:0.00000	Median	:0.00000				Medi
Mean	:0.08809	Mean	:0.01901	Mean	:0.01302	Mean	:0.06714
:0.04151	Mean	:0.1141					Mean
3rd Qu.:	:0.16333	3rd Qu.:	:0.00000	3rd Qu.:	:0.00000	3rd Qu.:	:0.12698
Qu.:	:0.00000	3rd Qu.:	:0.1094				3rd
V133		V134		V135		V136	
V137		V138					
Min.	:0.00000	Min.	:0.00000	Min.	:0.00000	Min.	:0.00000
:0.00000	Min.	:0.00000					Min.
1st Qu.:	:0.00000	1st Qu.:	:0.00000	1st Qu.:	:0.00000	1st Qu.:	:0.00000
u.:	:0.00000	1st Qu.:	:0.00000				1st Q
Median	:0.00000	Median	:0.00000	Median	:0.00000	Median	:0.00000
n	:0.00000	Median	:0.00000				Media
Mean	:0.07351	Mean	:0.10795	Mean	:0.02348	Mean	:0.0768
:0.1052	Mean	:0.04615					Mean
3rd Qu.:	:0.12019	3rd Qu.:	:0.09934	3rd Qu.:	:0.00000	3rd Qu.:	:0.1519
u.:	:0.2064	3rd Qu.:	:0.00000				3rd Q
V139		V140		V141		V142	
V143		V144					
Min.	:0.00000	Min.	:0.00000	Min.	:0.00000	Min.	:0.00000
:0.00000	Min.	:0.00000					Min.
1st Qu.:	:0.00000	1st Qu.:	:0.00000	1st Qu.:	:0.00000	1st Qu.:	:0.00000
Qu.:	:0.00000	1st Qu.:	:0.00000				1st
Median	:0.00000	Median	:0.00000	Median	:0.00000	Median	:0.00000
an	:0.00000	Median	:0.00000				Medi
Mean	:0.03156	Mean	:0.02043	Mean	:0.01804	Mean	:0.04597
:0.02666	Mean	:0.01276					Mean
3rd Qu.:	:0.00000	3rd Qu.:	:0.00000	3rd Qu.:	:0.00000	3rd Qu.:	:0.00000
Qu.:	:0.02857	3rd Qu.:	:0.00000				3rd

V145		V146		V147		V148	
V149	V150						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.02895	Mean :0.0221	Mean :0.02952	Mean :0.01528	Mean :0.01528	Mean :0.01528	Mean :0.01528	Mean :0.01528
3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000
u.:0.10428	u.:0.1154						
V151		V152		V153		V154	
V155	V156						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.1148	Mean :0.1119	Mean :0.1153	Mean :0.03546	Mean :0.03546	Mean :0.03546	Mean :0.03546	Mean :0.03546
3rd Qu.:0.1731	3rd Qu.:0.1351	3rd Qu.:0.1001	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000
u.:0.000000	u.:0.000000						
V157		V158		V159		V160	
V161	V162						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.03453	Mean :0.03217	Mean :0.03797	Mean :0.09569	Mean :0.09569	Mean :0.09569	Mean :0.09569	Mean :0.09569
3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.13665	3rd Qu.:0.13665	3rd Qu.:0.13665	3rd Qu.:0.13665	3rd Qu.:0.13665
u.:0.09936	u.:0.000000						
V163		V164		V165		V166	
V167	V168						
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.03797	Mean :0.07381	Mean :0.03459	Mean :0.09109	Mean :0.09109	Mean :0.09109	Mean :0.09109	Mean :0.09109
3rd Qu.:0.00000	3rd Qu.:0.06905	3rd Qu.:0.00000	3rd Qu.:0.15476	3rd Qu.:0.15476	3rd Qu.:0.15476	3rd Qu.:0.15476	3rd Qu.:0.15476
u.:0.000000	u.:0.1640						

V173	V169	V174	V170	V171	V172
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.03797	Mean :0.04159	Mean :0.02478	Mean :0.04325	Mean :0.03453	Mean :0.1025
3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.1202
V179	V175	V176	V177	V178	
Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000	Min. :0.00000
1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000	1st Qu.:0.00000
Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000	Median :0.00000
Mean :0.02048	Mean :0.01285	Mean :0.02048	Mean :0.01148	Mean :0.05470	Mean :0.09307
3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000	3rd Qu.:0.00000
[reached getOption("max.print") -- omitted 1 row]					

Community Detection

Клика — группа, в которой все пользователи имеют «прямые» связи (узлы соединены ребром) друг к другу

```
largest = largest.cliques(g)
op = par(mfrow = c(1, 2))
labels = rep(0, vcount(g))
labels[largest[[1]]] = 2
plot(g, vertex.color = labels, layout = layout.kamada.kawai(g))
labels = rep(0, vcount(g))
labels[largest[[2]]] = 2
plot(g, vertex.color = labels, layout = layout.kamada.kawai(g))
```



```
largest
```

```
[[1]]
```

```
+ 14/179 vertices, from 13ca955:
```

```
[1] 59 51 32 34 98 151 31 23 71 38 13 33 168 77
```

```
[[2]]
```

```
+ 14/179 vertices, from 13ca955:
```

```
[1] 59 51 32 34 98 151 31 23 71 38 13 33 168 17
```

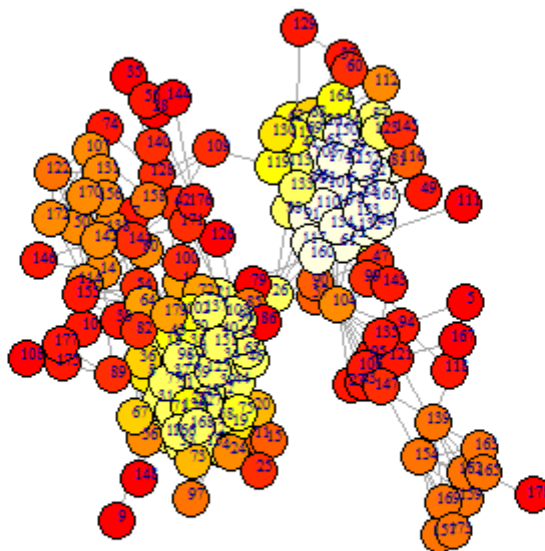
k-cores *k*-core – ядро степени *k* – означает, что степень всех входящих в него узлов не меньше *k*. (*k*+1)-core всегда является подграфом *k*-core

```
coreness <- graph.coreness(g)
```

```
max_cor <- max(coreness)
```

```
color_bar <- heat.colors(max_cor)
```

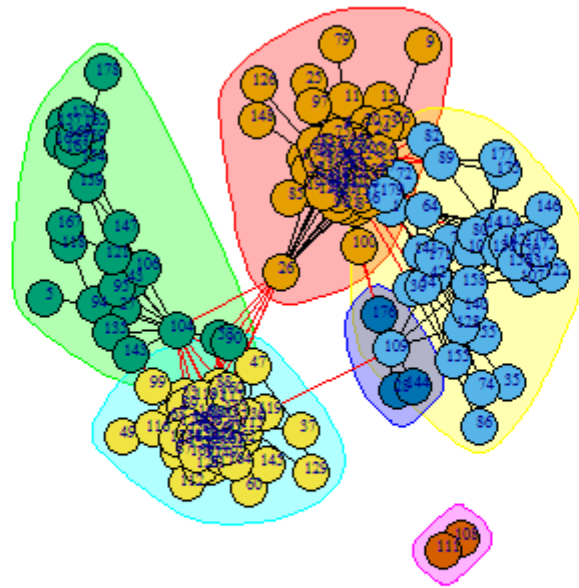
```
plot(g, vertex.label.font = 5, vertex.label.cex = 0.5, vertex.label.dist = 0.5, vertex.color = color_bar[coreness], layout = layout.kamada.kawai(g))
```



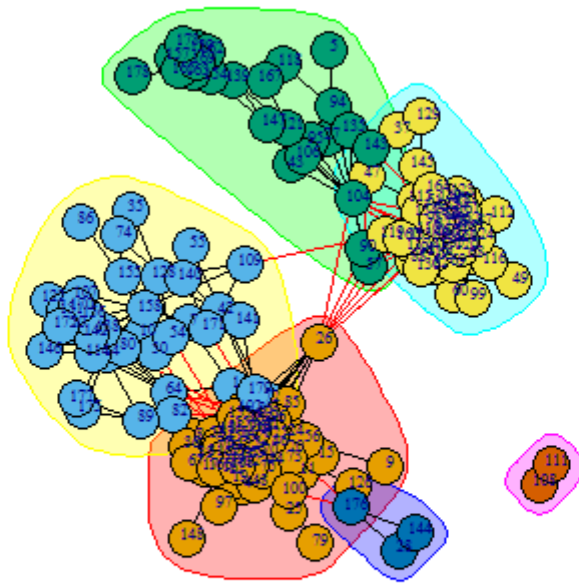
Fast greedy algorithm for cluster

```
o <- cluster_fast_greedy(g)
mm <- fastgreedy.community(g)
length(o)
[1] 6
```

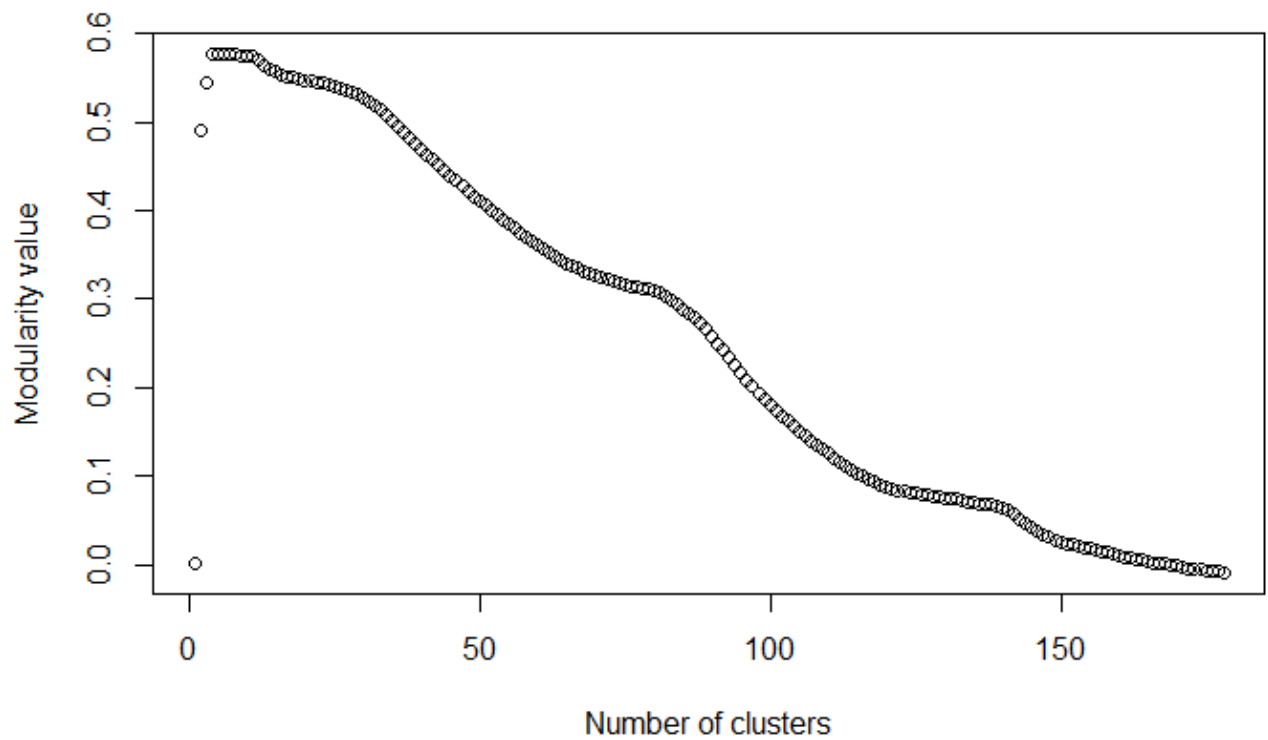
```
plot(mm, g, vertex.label.font = 5, vertex.label.cex = 0.5, vertex.label.dist = 0.5)
```



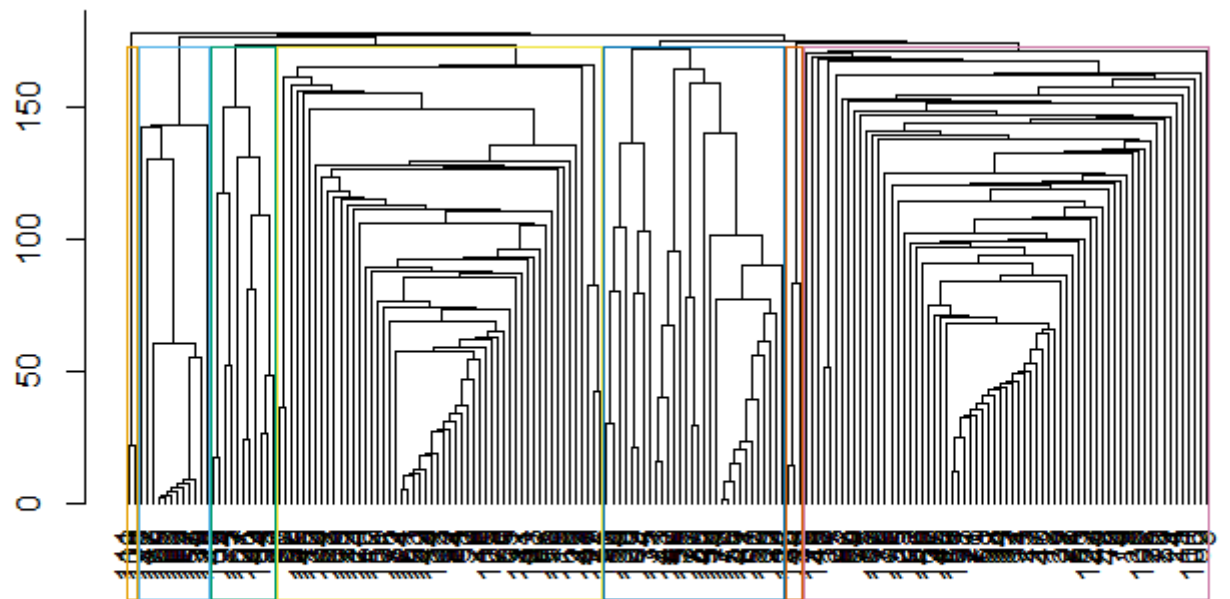
```
plot(o,g,vertex.label.font = 5, vertex.label.cex = 0.5, vertex.label.dist = 0
.5)
```



```
plot(rev(mm$modularity), xlab = 'Number of clusters' , ylab = 'Modularity value' )
```



```
edge_betw <- edge.betweenness.community(g)  
cluster_edge_betw <- cluster_edge_betweenness(g)  
dendPlot(cluster_edge_betw, mode="hclust")
```



```
plot(cluster_edge_betw, g, vertex.label.font = 5, vertex.label.cex = 0.5, vertex.label.dist = 0.5)
```

