

Contents

- [part 1](#)
- [part 4](#)
- [part 5](#)
- [part 2](#)
- [part 3](#)

```
% SPDX-License-Identifier: GPL-3.0-or-later
%
% ECE210 assignment04.m -- Func Off
% Copyright (C) 2024 Aidan Cusa <aidancusa@gmail.com>

clc;    % clear command window
clear; % clear all variables from current workspace
close all;
```

part 1

```
ip = @(x, y) x' * y;

% inner product norm for L2
ip_norm = @(x) sqrt(ip(x, x));
```

part 4

```
S = [1, 2 + 3j, -1 + 7j
      1j, 3j, 6 + 10j
      2 - 1j, 1 - 1j, 11 - 4j
      -1, 2j, 3 + 4j];

U = gram_schmidt(S, ip_norm)
```

part 5

```
orthogonal = isorthogonal(U(:, 1), U(:, 2), ip) & ...
              isorthogonal(U(:, 2), U(:, 3), ip) & ...
              isorthogonal(U(:, 1), U(:, 3), ip)
```

part 2

taken inspiration from <https://web.mit.edu/18.06/www/Essays/gramschmidtmat.pdf>

```
function gs = gram_schmidt(V, ip_norm)
    [m, n] = size(V);

    Q = zeros(m, n);
    R = zeros(n, n);
```

```

for j = 1:n
    v = V(:, j);

    for i = 1:j-1

        R(i, j) = Q(:, i)' * V(:, j);
        v = v - R(i, j) * Q(:, i);
    end

    R(j, j) = ip_norm(v);
    Q(:, j) = v / R(j, j);

    gs = Q;
end
end

```

U =

```

0.3536 + 0.0000i    0.2236 + 0.6708i   -0.5916 + 0.0845i
0.0000 + 0.3536i    0.0000 + 0.4472i    0.5071 + 0.1690i
0.7071 - 0.3536i   -0.2236 - 0.0000i    0.4226 + 0.0000i
-0.3536 + 0.0000i    0.2236 + 0.4472i    0.4226 + 0.0000i

```

part 3

```

function io = isorthogonal(u, v, ip)
    io = ip(u, v) < eps;
end

```

orthogonal =

logical

1