

# Bayesian Statistics & Bayes' Theorem

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$p(B|A)$  = Likelihood

$p(A|B)$  = Posterior Probability

$p(A)$  = Prior Probability

$p(B)$  = Bayesian Evidence  
(Marginalized Likelihood)

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A rare condition, affects 1 in 100,000 people of your demographic group. There is a test for the condition that is 98% accurate. This means that 98% of test takers who have the condition test positive (the other 2% get false negative results), and 98% of those who do not have the condition test negative (the other 2% get false positive results). You decide to take the test and receive a positive result. What is the probability you have the condition?

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$$p(+) = (0.98) \left( \frac{1}{100000} \right) + (0.02) \left( \frac{99999}{100000} \right) \approx \boxed{0.02}$$

$$p(c|+) = \frac{p(c) p(+|c)}{p(+)} \approx \boxed{0.0005}$$

# Battleship !



- You set up your ships, without seeing the other player's.
- Guess where the other player's ships are by calling out coordinates.
- Mark hits with red markers. Sink all the other player's ships!

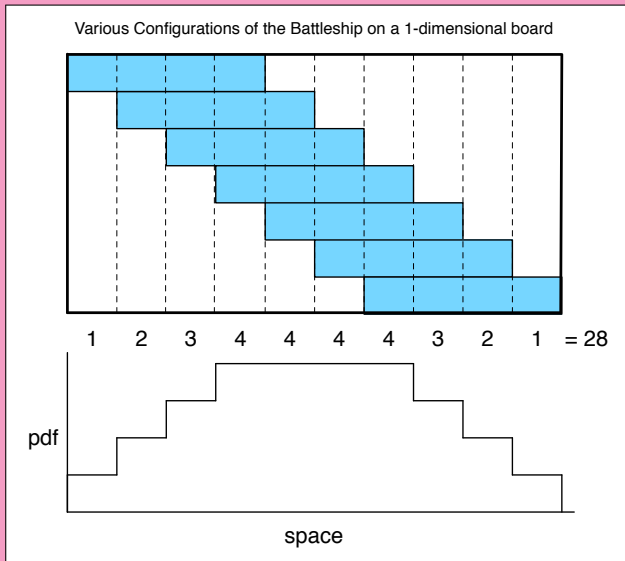


# 1-Dimensional game of Battleship

1-dimensional Battleship board

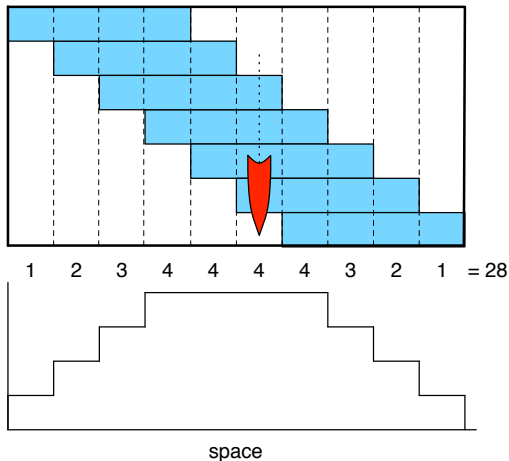


- A 1-dimensional board is simple enough to do all of the counting.
- There are only 7 configurations ( $\times 2$  if you allow flipping the battleship)



# 1-Dimensional game of Battleship

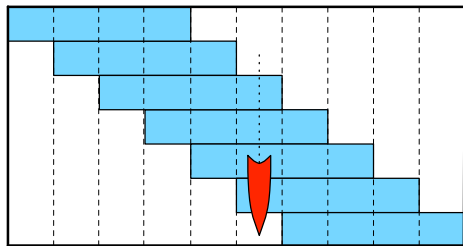
Various Configurations of the Battleship on a 1-dimensional board



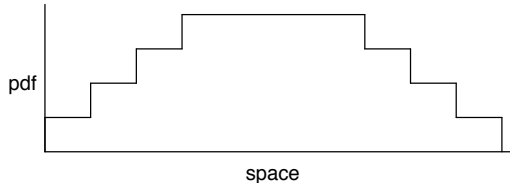


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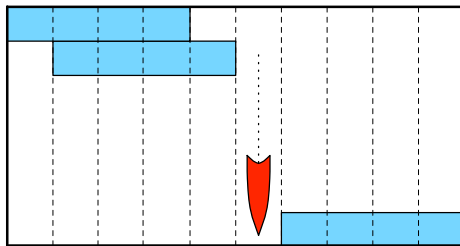
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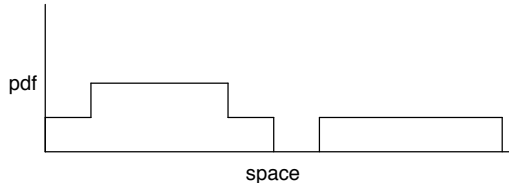
1 2 3 4 4 4 4 3 2 1 = 28



Various Configurations of the Battleship on a 1-dimensional board

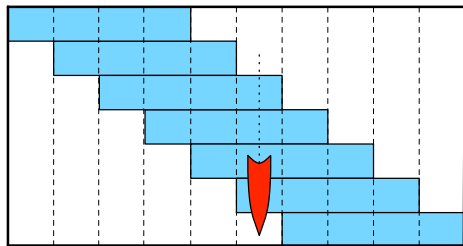


1 2 2 2 1 0 1 1 1 1 = 12

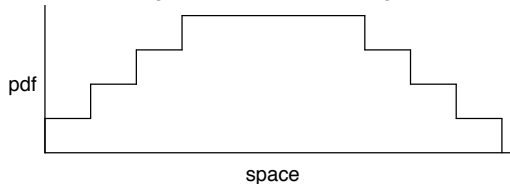


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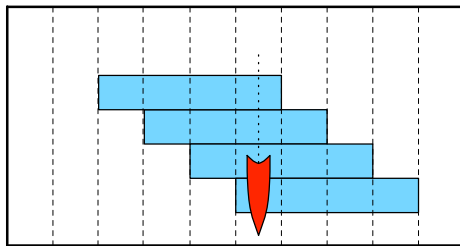
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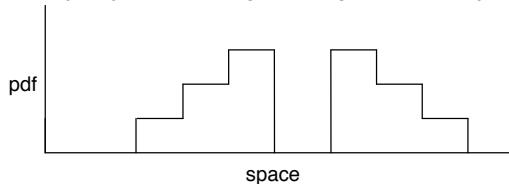
1 2 3 4 4 4 4 3 2 1 = 28



Various Configurations of the Battleship on a 1-dimensional board

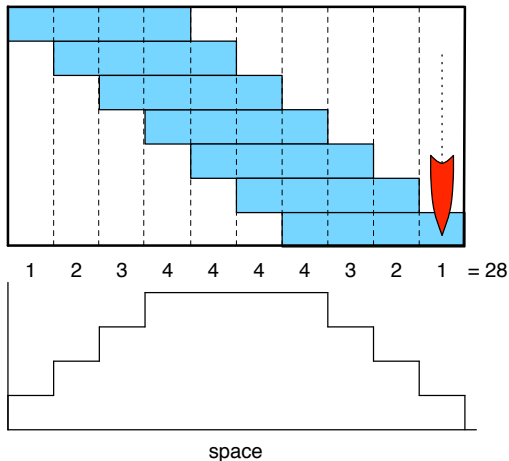


0 0 1 2 3 X 3 2 1 0 = 12



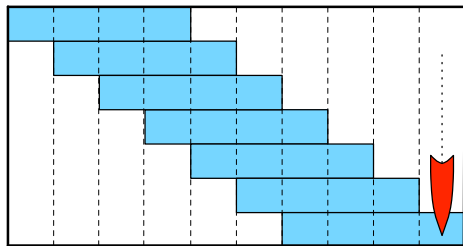
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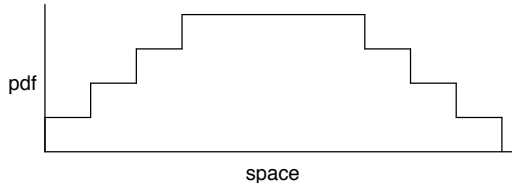


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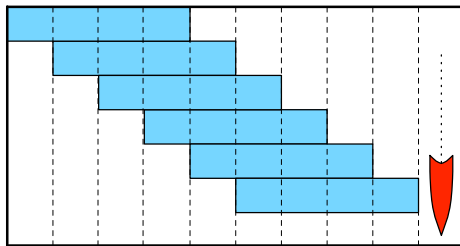
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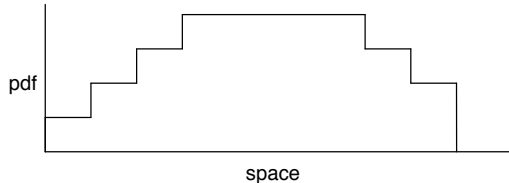
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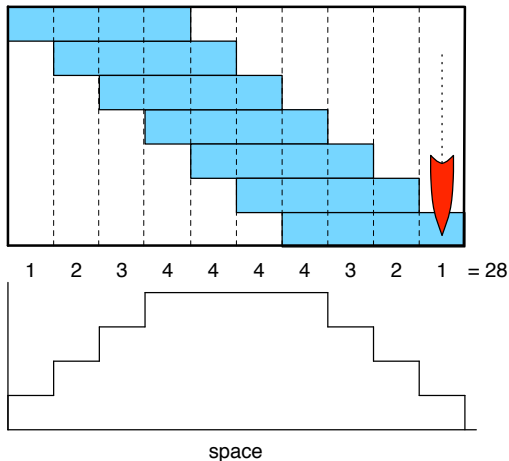


1 2 3 4 4 4 4 3 2 0 = 27



# 1-Dimensional game of Battleship Battleship Odds Website

Various Configurations of the Battleship on a 1-dimensional board



Various Configurations of the Battleship on a 1-dimensional board

