

Chapter 1

A simple fluid-structure interaction problem: Finite Reynolds number flow, driven by an oscillating ring.

This is a very simple fluid-structure interaction problem: We study the finite-Reynolds number internal flow generated by an oscillating ring. The wall motion only has a single degree of freedom: The ring's average radius, which needs to be adjusted to conserve mass. [This is a warm-up problem for the full fluid structure interaction problem discussed in the next example]. We compare the predictions for the flow field against asymptotic results.

The nodal positions in the fluid domain is updated by MacroElements.

```
//LIC// =====
//LIC// This file forms part of oomph-lib, the object-oriented,
//LIC// multi-physics finite-element library, available
//LIC// at http://www.oomph-lib.org.
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//LIC//
//LIC//=====
// Driver for 2D Navier Stokes flow, driven by oscillating ring
// with pseudo-elasticity: The mean radius of ring is adjusted to
// allow conservation of volume (area).
// Oomph-lib includes
#include "generic.h"
#include "navier_stokes.h"
//Need to instantiate templated mesh
#include "meshes/quarter_circle_sector_mesh.h"
//Include namespace containing Sarah's asymptotics
#include "osc_ring_sarah_asymptotics.h"
using namespace std;
using namespace oomph;
using namespace MathematicalConstants;

////////////////////////////////////
////////////////////////////////////
////////////////////////////////////

//=====
/// Namespace for physical parameters
//=====
namespace Global_Physical_Variables
{
```

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```
/// Reynolds number
double Re=100.0; // ADJUST_PRIORITY

/// Reynolds x Strouhal number
double ReSt=100.0; // ADJUST_PRIORITY
}

////////////////////////////////////
////////////////////////////////////
////////////////////////////////////

//=====
/// Driver for oscillating ring problem: Wall performs oscillations
/// that resemble eigenmodes of freely oscillating ring and drives
/// viscous fluid flow. Mean radius of wall is adjustable and
/// responds to a pressure value in the fluid to allow for
/// mass conservation.
//=====
template<class ELEMENT>
class OscRingNStProblem : public Problem
{
public:

    /// \short Constructor: Pass timestep and function pointer to the
    /// solution that provides the initial conditions for the fluid
    OscRingNStProblem(const double& dt,
        FiniteElement::UnsteadyExactSolutionFctPt IC_fct_pt);

    /// Destructor (empty)
    ~OscRingNStProblem(){}

    /// Get pointer to wall as geometric object
    GeomObject* wall_pt()
    {
        return Wall_pt;
    }

    /// Update after solve (empty)
    void actions_after_newton_solve(){}

    /// \short Update the problem specs before solve (empty)
    void actions_before_newton_solve(){}

    /// \short Update the problem specs before checking Newton
    /// convergence: Update the fluid mesh and re-set velocity
    /// boundary conditions -- no slip velocity on the wall means
    /// that the velocity on the wall is dependent.
    void actions_before_newton_convergence_check()
    {
        // Update the fluid mesh -- auxiliary update function for algebraic
        // nodes automatically updates no slip condition.
        fluid_mesh_pt()->node_update();
    }

    /// \short Update the problem specs after adaptation:
    /// Set auxiliary update function that applies no slip on all
    /// boundary nodes and choose fluid pressure dof that drives
    /// the wall deformation
    void actions_after_adapt()
    {
        // Ring boundary: No slip; this also implies that the velocity needs
        // to be updated in response to wall motion. This needs to be reset
        // every time the mesh is changed -- there's no mechanism by which
        // auxiliary update functions are copied to newly created nodes.
        // (that's because unlike boundary conditions, they don't
        // occur exclusively at boundaries)
        unsigned ibound=1;
        {
            unsigned num_nod= fluid_mesh_pt()->nboundary_node(ibound);
            for (unsigned inod=0;inod<num_nod;inod++)
            {
                fluid_mesh_pt()->boundary_node_pt(ibound,inod)->
                    set_auxiliary_node_update_fct_pt(
                        FSI_functions::apply_no_slip_on_moving_wall);
            }
        }

        // Set the reference pressure as the constant pressure in element 0
        dynamic_cast<PseudoBucklingRingElement*>(Wall_pt)
            ->set_reference_pressure_pt(fluid_mesh_pt()->element_pt(0)
                ->internal_data_pt(0));
    }

    /// Run the time integration for nsteps steps
    void unsteady_run(const unsigned &nsteps, const bool& restarted,
        DocInfo& doc_info);
}
```

```

/// \short Set initial condition (incl previous timesteps) according
/// to specified function.
void set_initial_condition();

/// Doc the solution
void doc_solution(DocInfo& doc_info);

/// Access function for the fluid mesh
MacroElementNodeUpdateRefineableQuarterCircleSectorMesh<ELEMENT>* fluid_mesh_pt()
{
    return Fluid_mesh_pt;
}

/// \short Dump problem data.
void dump_it(ofstream& dump_file, DocInfo doc_info);

/// \short Read problem data.
void restart(istream& restart_file);
private:

/// Write header for trace file
void write_trace_file_header();

/// Function pointer to set the initial condition
FiniteElement::UnsteadyExactSolutionFctPt IC_Fct_pt;

/// Pointer to wall
GeomObject* Wall_pt;

/// Pointer to fluid mesh
MacroElementNodeUpdateRefineableQuarterCircleSectorMesh<ELEMENT>* Fluid_mesh_pt;

/// Pointer to wall mesh (contains only a single GeneralisedElement)
Mesh* Wall_mesh_pt;

/// Trace file
ofstream Trace_file;

/// Pointer to node on coarsest mesh on which velocity is traced
Node* Veloc_trace_node_pt;

/// \short Pointer to node in symmetry plane on coarsest mesh at
/// which velocity is traced
Node* Sarah_veloc_trace_node_pt;
};
//=====
/// Constructor: Pass (constant) timestep and function pointer to the solution
/// that provides the initial conditions for the fluid.
//=====
template<class ELEMENT>
OscRingNStProblem<ELEMENT>::OscRingNStProblem(const double& dt,
FiniteElement::UnsteadyExactSolutionFctPt IC_fct_pt) : IC_Fct_pt(IC_fct_pt)
{
    // Period of oscillation
    double T=1.0;
    //Allocate the timestepper
    add_time_stepper_pt(new BDF<4>);
    // Initialise timestep -- also sets the weights for all timesteppers
    // in the problem.
    initialise_dt(dt);
    // Parameters for pseudo-buckling ring
    double eps_buckl=0.1; // ADJUST_PRIORITY
    double ampl_ratio=-0.5; // ADJUST_PRIORITY
    unsigned n_buckl=2; // ADJUST_PRIORITY
    double r_0=1.0;

    // Build wall geometric element
    Wall_pt=new PseudoBucklingRingElement(eps_buckl,ampl_ratio,n_buckl,r_0,T,
                                         time_stepper_pt());
    // Fluid mesh is suspended from wall between these two Lagrangian
    // coordinates:
    double xi_lo=0.0;
    double xi_hi=2.0*atan(1.0);
    // Fractional position of dividing line for two outer blocks in fluid mesh
    double fract_mid=0.5;
    // Build fluid mesh
    Fluid_mesh_pt=new MacroElementNodeUpdateRefineableQuarterCircleSectorMesh<ELEMENT>(
    Wall_pt,xi_lo,fract_mid,xi_hi,time_stepper_pt());
    // Set error estimator
    Z2ErrorEstimator* error_estimator_pt=new Z2ErrorEstimator;
    Fluid_mesh_pt->spatial_error_estimator_pt()=error_estimator_pt;

    // Fluid mesh is first sub-mesh
    add_sub_mesh(Fluid_mesh_pt);
    // Build wall mesh
    Wall_mesh_pt=new Mesh;

```

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```
// Wall mesh is completely empty: Add Wall element in its GeneralisedElement
// incarnation
Wall_mesh_pt->add_element_pt(dynamic_cast<GeneralisedElement*>(Wall_pt));
// Wall mesh is second sub-mesh
add_sub_mesh(Wall_mesh_pt);
// Combine all submeshes into a single Mesh
build_global_mesh();
// Extract pointer to node at center of mesh (this node exists
// at all refinement levels and can be used to doc continuous timetrace
// of velocities)
unsigned nnode=fluid_mesh_pt()->finite_element_pt(0)->nnode();
Veloc_trace_node_pt=fluid_mesh_pt()->finite_element_pt(0)->node_pt(nnode-1);
// Extract pointer to node in symmetry plane (this node exists
// at all refinement levels and can be used to doc continuous timetrace
// of velocities)
unsigned nnode_ld=dynamic_cast<ELEMENT*>(
    fluid_mesh_pt()->finite_element_pt(0))->nnode_ld();
Sarah_veloc_trace_node_pt=fluid_mesh_pt()->
    finite_element_pt(0)->node_pt(nnode_ld-1);
// The "pseudo-elastic" wall element is "loaded" by a pressure.
// Use the "constant" pressure component in Crouzeix Raviart
// fluid element as that pressure.
dynamic_cast<PseudoBucklingRingElement*>(Wall_pt)
    ->set_reference_pressure_pt(fluid_mesh_pt()->element_pt(0)
        ->internal_data_pt(0));
// Set the boundary conditions for this problem:
//-----
// All nodes are free by default -- just pin the ones that have
// Dirichlet conditions here.

// Bottom boundary:
unsigned ibound=0;
{
    unsigned num_nod= fluid_mesh_pt()->nboundary_node(ibound);
    for (unsigned inod=0; inod<num_nod; inod++)
    {
        // Pin vertical velocity
        {
            fluid_mesh_pt()->boundary_node_pt(ibound, inod)->pin(1);
        }
    }
}

// Ring boundary: No slip; this also implies that the velocity needs
// to be updated in response to wall motion
ibound=1;
{
    unsigned num_nod=fluid_mesh_pt()->nboundary_node(ibound);
    for (unsigned inod=0; inod<num_nod; inod++)
    {
        // Which node are we dealing with?
        Node* node_pt=fluid_mesh_pt()->boundary_node_pt(ibound, inod);
        // Set auxiliary update function pointer to apply no-slip condition
        // to velocities whenever nodal position is updated
        node_pt->set_auxiliary_node_update_fct_pt(
            FSI_functions::apply_no_slip_on_moving_wall);

        // Pin both velocities
        for (unsigned i=0; i<2; i++)
        {
            node_pt->pin(i);
        }
    }
}

// Left boundary:
ibound=2;
{
    unsigned num_nod=fluid_mesh_pt()->nboundary_node(ibound);
    for (unsigned inod=0; inod<num_nod; inod++)
    {
        // Pin horizontal velocity
        {
            fluid_mesh_pt()->boundary_node_pt(ibound, inod)->pin(0);
        }
    }
}

// Complete the build of all elements so they are fully functional
//-----
//Find number of elements in mesh
unsigned n_element = fluid_mesh_pt()->nelement();
// Loop over the elements to set up element-specific
// things that cannot be handled by constructor
for(unsigned i=0; i<n_element; i++)
{
    // Upcast from FiniteElement to the present element
    ELEMENT *el_pt = dynamic_cast<ELEMENT*>(fluid_mesh_pt()->element_pt(i));
```

```

//Set the Reynolds number, etc
el_pt->re_pt() = &Global_Physical_Variables::Re;
el_pt->re_st_pt() = &Global_Physical_Variables::ReSt;
}
//Attach the boundary conditions to the mesh
cout << "Number of equations: " << assign_eqn_numbers() << std::endl;

// Set parameters for Sarah's asymptotic solution
//-----
// Amplitude of the oscillation
SarahBL::epsilon=static_cast<PseudoBucklingRingElement*>(Wall_pt)->
    eps_buckl();
// Womersley number is the same as square root of Reynolds number
SarahBL::alpha=sqrt(Global_Physical_Variables::Re);
// Amplitude ratio
SarahBL::A=static_cast<PseudoBucklingRingElement*>(Wall_pt)->ampl_ratio();
// Buckling wavenumber
SarahBL::N=static_cast<PseudoBucklingRingElement*>(Wall_pt)->n_buckl_float();
// Frequency of oscillation (period is one)
SarahBL::Omega=2.0*MathematicalConstants::Pi;
}
//=====
/// Set initial condition: Assign previous and current values
/// of the velocity from the velocity field specified via
/// the function pointer.
///
/// Values are assigned so that the velocities and accelerations
/// are correct for current time.
//=====
template<class ELEMENT>
void OscRingNSTProblem<ELEMENT>::set_initial_condition()
{
    // Elastic wall: We're starting from a given initial state in which
    // the wall is undeformed. If set_initial_condition() is called again
    // after mesh refinement for first timestep, this needs to be reset.
    dynamic_cast<PseudoBucklingRingElement*>(Wall_pt)->set_R_0(1.0);
    // Backup time in global timestepper
    double backed_up_time=time_pt()->time();

    // Past history for velocities needs to be established for t=time0-deltat, ...
    // Then provide current values (at t=time0) which will also form
    // the initial guess for first solve at t=time0+deltat
    // Vector of exact solution values (includes pressure)
    Vector<double> soln(3);
    Vector<double> x(2);
    //Find number of nodes in mesh
    unsigned num_nod = fluid_mesh_pt()->nnode();
    // Get continuous times at previous timesteps
    int nprev_steps=time_stepper_pt()->nprev_values();
    Vector<double> prev_time(nprev_steps+1);
    for (int itime=nprev_steps;itime>=0;itime--)
    {
        prev_time[itime]=time_pt()->time(unsigned(itime));
    }
    // Loop over current & previous timesteps (in outer loop because
    // the mesh might also move)
    for (int itime=nprev_steps;itime>=0;itime--)
    {
        double time=prev_time[itime];

        // Set global time (because this is how the geometric object refers
        // to continuous time
        time_pt()->time()=time;

        cout << "setting IC at time =" << time << std::endl;

        // Update the fluid mesh for this value of the continuous time
        // (The wall object reads the continous time from the same
        // global time object)
        fluid_mesh_pt()->node_update();

        // Loop over the nodes to set initial guess everywhere
        for (unsigned jnod=0;jnod<num_nod;jnod++)
        {
            // Get nodal coordinates
            x[0]=fluid_mesh_pt()->node_pt(jnod)->x(0);
            x[1]=fluid_mesh_pt()->node_pt(jnod)->x(1);
            // Get intial solution
            (*IC_Fct_pt)(time,x,soln);

            // Loop over velocity directions (velocities are in soln[0] and soln[1]).
            for (unsigned i=0;i<2;i++)
            {
                fluid_mesh_pt()->node_pt(jnod)->set_value(itime,i,soln[i]);
            }
        }
    }
}

```

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```
// Loop over coordinate directions
for (unsigned i=0; i<2; i++)
{
    fluid_mesh_pt()->node_pt(jnod)->x(itime,i)=x[i];
}
}
// Reset backed up time for global timestepper
time_pt()->time()=backed_up_time;
}
//=====
/// Doc the solution
///
//=====
template<class ELEMENT>
void OscRingNSTProblem<ELEMENT>::doc_solution(DocInfo& doc_info)
{
    cout << "Doc-ing step " << doc_info.number()
          << " for time " << time_stepper_pt()->time_pt()->time() << std::endl;
    ofstream some_file;
    char filename[100];
    // Number of plot points
    unsigned npts;
    npts=5;
    // Output solution on fluid mesh
    //-----
    sprintf(filename,"%s/soln%i.dat",doc_info.directory().c_str(),
            doc_info.number());
    //some_file.precision(20);
    some_file.open(filename);
    unsigned nelem=fluid_mesh_pt()->nelement();
    for (unsigned ielem=0; ielem<nelem; ielem++)
    {
        dynamic_cast<ELEMENT*>(fluid_mesh_pt()->element_pt(ielem))->
            full_output(some_file,npts);
    }
    some_file.close();

    // Plot wall posn
    //-----
    sprintf(filename,"%s/Wall%i.dat",doc_info.directory().c_str(),
            doc_info.number());
    some_file.open(filename);

    unsigned nplot=100;
    Vector<double> > xi_wall(1);
    Vector<double> > r_wall(2);
    for (unsigned iplot=0; iplot<nplot; iplot++)
    {
        xi_wall[0]=0.5*Pi*double(iplot)/double(nplot-1);
        Wall_pt->position(xi_wall,r_wall);
        some_file << r_wall[0] << " " << r_wall[1] << std::endl;
    }
    some_file.close();
    // Doc Sarah's asymptotic solution
    //-----
    sprintf(filename,"%s/exact_soln%i.dat",doc_info.directory().c_str(),
            doc_info.number());
    some_file.open(filename);
    fluid_mesh_pt()->output_fct(some_file,npts,
                               time_stepper_pt()->time_pt()->time(),
                               SarahBL::full_exact_soln);

    some_file.close();
    // Get position of control point
    //-----
    Vector<double> r(2);
    Vector<double> xi(1);
    xi[0]=MathematicalConstants::Pi/2.0;
    wall_pt()->position(xi,r);
    // Get total volume (area) of computational domain, energies and average
    //-----
    // pressure
    //-----
    double area=0.0;
    double press_int=0.0;
    double diss=0.0;
    double kin_en=0.0;
    nelem=fluid_mesh_pt()->nelement();
    for (unsigned ielem=0; ielem<nelem; ielem++)
    {
        area+=fluid_mesh_pt()->finite_element_pt(ielem)->size();
        press_int+=dynamic_cast<ELEMENT*>(fluid_mesh_pt()->element_pt(ielem))
            ->pressure_integral();
        diss+=dynamic_cast<ELEMENT*>(fluid_mesh_pt()->element_pt(ielem))->
            dissipation();
        kin_en+=dynamic_cast<ELEMENT*>(fluid_mesh_pt()->element_pt(ielem))->
            kin_energy();
    }
}
```

```

    }
    // Total kinetic energy in entire domain
    double global_kin=4.0*kin_en;
    // Max/min refinement level
    unsigned min_level;
    unsigned max_level;
    fluid_mesh_pt()->get_refinement_levels(min_level,max_level);
    // Total dissipation for quarter domain
    double time=time_pt()->time();
    double diss_asympt=SarahBL::Total_Diss_sarah(time)/4.0;
    // Asymptotic predictions for velocities at control point
    Vector<double> x_sarah(2);
    Vector<double> soln_sarah(3);
    x_sarah[0]=Sarah_veloc_trace_node_pt->x(0);
    x_sarah[1]=Sarah_veloc_trace_node_pt->x(1);
    SarahBL::exact_soln(time,x_sarah,soln_sarah);
    // Doc
    Trace_file << time_pt()->time()
        << " " << r[1]
        << " " << global_kin
        << " " << SarahBL::Kin_energy_sarah(time_pt()->time())
        << " " << static_cast<PseudoBucklingRingElement*>(Wall_pt)->r_0()
        << " " << area
        << " " << press_int/area
        << " " << diss
        << " " << diss_asympt
        << " " << Veloc_trace_node_pt->x(0)
        << " " << Veloc_trace_node_pt->x(1)
        << " " << Veloc_trace_node_pt->value(0)
        << " " << Veloc_trace_node_pt->value(1)
        << " " << fluid_mesh_pt()->nelement()
        << " " << ndof()
        << " " << min_level
        << " " << max_level
        << " " << fluid_mesh_pt()->nrefinement_overruled()
        << " " << fluid_mesh_pt()->max_error()
        << " " << fluid_mesh_pt()->min_error()
        << " " << fluid_mesh_pt()->max_permitted_error()
        << " " << fluid_mesh_pt()->min_permitted_error()
        << " " << fluid_mesh_pt()->max_keep_unrefined()
        << " " << doc_info.number()
        << " " << Sarah_veloc_trace_node_pt->x(0)
        << " " << Sarah_veloc_trace_node_pt->x(1)
        << " " << Sarah_veloc_trace_node_pt->value(0)
        << " " << Sarah_veloc_trace_node_pt->value(1)
        << " " << x_sarah[0]
        << " " << x_sarah[1]
        << " " << soln_sarah[0]
        << " " << soln_sarah[1]
        << " "
        << static_cast<PseudoBucklingRingElement*>(Wall_pt)->r_0()-1.0
        << std::endl;
    // Output fluid solution on coarse-ish mesh
    //-----
    // Extract all elements from quadtree representation
    Vector<Tree*> all_element_pt;
    fluid_mesh_pt()->forest_pt()->
        stick_all_tree_nodes_into_vector(all_element_pt);
    // Build a coarse mesh
    Mesh* coarse_mesh_pt = new Mesh();
    //Loop over all elements and check if their refinement level is
    //equal to the mesh's minimum refinement level
    nelem=all_element_pt.size();
    for (unsigned ielem=0;ielem<nelem;ielem++)
    {
        Tree* el_pt=all_element_pt[ielem];
        if (el_pt->level()==min_level)
        {
            coarse_mesh_pt->add_element_pt(el_pt->object_pt());
        }
    }
    // Output fluid solution on coarse mesh
    sprintf(filename,"%s/coarse_soln%i.dat",doc_info.directory().c_str(),
        doc_info.number());
    some_file.open(filename);
    nelem=coarse_mesh_pt->nelement();
    for (unsigned ielem=0;ielem<nelem;ielem++)
    {
        dynamic_cast<ELEMENT*>(coarse_mesh_pt->element_pt(ielem))->
            full_output(some_file,npts);
    }
    some_file.close();
    // Write restart file
    sprintf(filename,"%s/restart%i.dat",doc_info.directory().c_str(),
        doc_info.number());
    some_file.open(filename);
    dump_it(some_file,doc_info);

```

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```
some_file.close();
}
//=====
/// Dump the solution
//=====
template<class ELEMENT>
void OscRingNSTProblem<ELEMENT>::dump_it(ofstream& dump_file, DocInfo doc_info)
{
    // Dump refinement status of mesh
    //fluid_mesh_pt()->dump_refinement(dump_file);
    // Call generic dump()
    Problem::dump(dump_file);
}
//=====
/// Read solution from disk
//=====
template<class ELEMENT>
void OscRingNSTProblem<ELEMENT>::restart(istream& restart_file)
{
    // Refine fluid mesh according to the instructions in restart file
    //fluid_mesh_pt()->refine(restart_file);
    // Rebuild the global mesh
    //rebuild_global_mesh();
    // Read generic problem data
    Problem::read(restart_file);
    // // Complete build of all elements so they are fully functional
    // finish_problem_setup();

    //Assign equation numbers
    //cout << "\nNumber of equations: " << assign_eqn_numbers()
    //      << std::endl << std::endl;
}
//=====
/// Driver for timestepping the problem: Fixed timestep but
/// guaranteed spatial accuracy. Beautiful, innit?
///
//=====
template<class ELEMENT>
void OscRingNSTProblem<ELEMENT>::unsteady_run(const unsigned& nsteps,
                                              const bool& restarted,
                                              DocInfo& doc_info)
{
    // Open trace file
    char filename[100];
    sprintf(filename, "%s/trace.dat", doc_info.directory().c_str());
    Trace_file.open(filename);
    // Max. number of adaptations per solve
    unsigned max_adapt;
    // Max. number of adaptations per solve
    if (restarted)
    {
        max_adapt=0;
    }
    else
    {
        max_adapt=1;
    }

    // Max. and min. error for adaptive refinement/unrefinement
    fluid_mesh_pt()->max_permitted_error()= 0.5e-2;
    fluid_mesh_pt()->min_permitted_error()= 0.5e-3;
    // Don't allow refinement to drop under given level
    fluid_mesh_pt()->min_refinement_level()=2;
    // Don't allow refinement beyond given level
    fluid_mesh_pt()->max_refinement_level()=6;
    // Don't bother adapting the mesh if no refinement is required
    // and if less than ... elements are to be merged.
    fluid_mesh_pt()->max_keep_unrefined()=20;
    // Get max/min refinement levels in mesh
    unsigned min_refinement_level;
    unsigned max_refinement_level;
    fluid_mesh_pt()->get_refinement_levels(min_refinement_level,
                                          max_refinement_level);
    cout << "\n Initial mesh: min/max refinement levels: "
         << min_refinement_level << " " << max_refinement_level << std::endl << std::endl;
    // Doc refinement targets
    fluid_mesh_pt()->doc_adaptivity_targets(cout);
    // Write header for trace file
    write_trace_file_header();
    // Doc initial condition
    doc_solution(doc_info);
    doc_info.number()++;
    // Switch off doc during solve
    doc_info.disable_doc();
    // If we set first to true, then initial guess will be re-assigned
    // after mesh adaptation. Don't want this if we've done a restart.
```



```

bool first;
bool shift;
if (restarted)
{
    first=false;
    shift=false;
    // Move time back by dt to make sure we're re-solving the read-in solution
    time_pt()->time()-=time_pt()->dt();
}
else
{
    first=true;
    shift=true;
}

//Take the first fixed timestep with specified tolerance for Newton solver
double dt=time_pt()->dt();
unsteady_newton_solve(dt,max_adapt,first,shift);
// Switch doc back on
doc_info.enable_doc();
// Doc initial solution
doc_solution(doc_info);
doc_info.number()++;
// Now do normal run; allow for one mesh adaptation per timestep
max_adapt=1;
//Loop over the remaining timesteps
for(unsigned t=2;t<=ntsteps;t++)
{
    // Switch off doc during solve
    doc_info.disable_doc();
    //Take fixed timestep
    first=false;
    unsteady_newton_solve(dt,max_adapt,first);
    // Switch doc back on
    doc_info.enable_doc();
    // Doc solution
    //if (icount%10==0)
    {
        doc_solution(doc_info);
        doc_info.number()++;
    }
}
// Close trace file
Trace_file.close();
}
//=====
/// Write trace file header
//=====
template<class ELEMENT>
void OscRingNSTProblem<ELEMENT>::write_trace_file_header()
{
    // Doc parameters in trace file
    Trace_file << " # err_max " << fluid_mesh_pt()->max_permitted_error() << std::endl;
    Trace_file << " # err_min " << fluid_mesh_pt()->min_permitted_error() << std::endl;
    Trace_file << " # Re " << Global_Physical_Variables::Re << std::endl;
    Trace_file << " # St " << Global_Physical_Variables::ReSt/
        Global_Physical_Variables::Re << std::endl;
    Trace_file << " # dt " << time_stepper_pt()->time_pt()->dt() << std::endl;
    Trace_file << " # initial # elements " << mesh_pt()->nelement() << std::endl;
    Trace_file << " # min_refinement_level "
        << fluid_mesh_pt()->min_refinement_level() << std::endl;
    Trace_file << " # max_refinement_level "
        << fluid_mesh_pt()->max_refinement_level() << std::endl;
    Trace_file << "VARIABLES=\"time\", \"V_c_t_r_l\", \"e_k_i_n\"";
    Trace_file << ", \"e_k_i_n_(a_s_y_m_p_t)\", \"R_0\", \"Area\"";
    Trace_file << ", \"Average pressure\", \"Total dissipation (quarter domain)\"";
    Trace_file << ", \"Asymptotic dissipation (quarter domain)\"";
    Trace_file << ", \"x<sub>1</sub><sup>(track)</sup>\"";
    Trace_file << ", \"x<sub>2</sub><sup>(track)</sup>\"";
    Trace_file << ", \"u<sub>1</sub><sup>(track)</sup>\"";
    Trace_file << ", \"u<sub>2</sub><sup>(track)</sup>\"";
    Trace_file << ", \"N<sub>element</sub>\"";
    Trace_file << ", \"N<sub>dof</sub>\"";
    Trace_file << ", \"max. refinement level\"";
    Trace_file << ", \"min. refinement level\"";
    Trace_file << ", \"# of elements whose refinement was over-ruled\"";
    Trace_file << ", \"max. error\"";
    Trace_file << ", \"min. error\"";
    Trace_file << ", \"max. permitted error\"";
    Trace_file << ", \"min. permitted error\"";
    Trace_file << ", \"max. permitted # of unrefined elements\"";
    Trace_file << ", \"doc number\"";
    Trace_file << ", \"x<sub>1</sub><sup>(track2 FE)</sup>\"";
    Trace_file << ", \"x<sub>2</sub><sup>(track2 FE)</sup>\"";
    Trace_file << ", \"u<sub>1</sub><sup>(track2 FE)</sup>\"";
    Trace_file << ", \"u<sub>2</sub><sup>(track2 FE)</sup>\"";
    Trace_file << ", \"x<sub>1</sub><sup>(track2 Sarah)</sup>\"";

```

10 A simple fluid-structure interaction problem: Finite Reynolds number flow, driven by an oscillating ring.

```
Trace_file << " , \"x<sub>2</sub><sup>(track2 Sarah)</sup>\"";
Trace_file << " , \"u<sub>1</sub><sup>(track2 Sarah)</sup>\"";
Trace_file << " , \"u<sub>2</sub><sup>(track2 Sarah)</sup>\"";
Trace_file << " , \"R<sub>0</sub><sup>-1</sup>\"";
Trace_file << std::endl;
}

////////////////////////////////////
////////////////////////////////////
////////////////////////////////////

//=====
/// Demonstrate how to solve OscRingNSt problem in deformable domain
/// with mesh adaptation
//=====
int main(int argc, char* argv[])
{
    // Store command line arguments
    CommandLineArgs::setup(argc, argv);
    //Do a certain number of timesteps per period
    unsigned nstep_per_period=40; // 80; // ADJUST_PRIORITY
    unsigned nperiod=3;
    // Work out total number of steps and timestep
    unsigned nstep=nstep_per_period*nperiod;
    double dt=1.0/double(nstep_per_period);
    // Set up the problem: Pass timestep and Sarah's asymptotic solution for
    // generation of initial condition
    OscRingNStProblem<MacroElementNodeUpdateElement<RefineableQCrouzeixRaviartElement<2> > >
    problem(dt, &SarahBL::full_exact_soln);
    // Restart?
    //-----
    bool restarted=false;
    // Pointer to restart file
    ifstream* restart_file_pt=0;
    // No restart
    //-----
    if (CommandLineArgs::Argc!=2)
    {
        cout << "No restart" << std::endl;
        restarted=false;
        // Refine uniformly
        problem.refine_uniformly();
        problem.refine_uniformly();
        // Set initial condition on uniformly refined domain (if this isn't done
        // then the mesh contains the interpolation of the initial guess
        // on the original coarse mesh -- if the nodal values were zero in
        // the interior and nonzero on the boundary, then the waviness of
        // of the interpolated i.g. between the nodes on the coarse mesh
        // gets transferred onto the fine mesh where we can do better
        problem.set_initial_condition();
    }

    // Restart
    //-----
    else if (CommandLineArgs::Argc==2)
    {
        restarted=true;
        // Open restart file
        restart_file_pt=new ifstream(CommandLineArgs::Argv[1], ios_base::in);
        if (restart_file_pt!=0)
        {
            cout << "Have opened " << CommandLineArgs::Argv[1] <<
                " for restart. " << std::endl;
        }
        else
        {
            std::ostringstream error_stream;
            error_stream << "ERROR while trying to open "
                << CommandLineArgs::Argv[2]
                << " for restart." << std::endl;
            throw OomphLibError(error_stream.str(),
                                OOMPH_CURRENT_FUNCTION,
                                OOMPH_EXCEPTION_LOCATION);
        }
        // Do the actual restart
        problem.restart(*restart_file_pt);
    }
    // Two command line arguments: do validation run
    if (CommandLineArgs::Argc==3)
    {
        nstep=3;
        cout << "Only doing nstep steps for validation: " << nstep << std::endl;
    }
    // Setup labels for output
    DocInfo doc_info;

    // Output directory
```

```

doc_info.set_directory("RESULT");
// Do unsteady run of the problem for nstep steps
//-----
problem.unsteady_run(nstep, restarted, doc_info);
// Validate the restart procedure
//-----
if (CommandLineArgs::Argc==3)
{
    // Build problem and restart

    // Set up the problem: Pass timestep and Sarah's asymptotic solution for
    // generation of initial condition
    OscRingNSStProblem<MacroElementNodeUpdateElement<
    RefineableQCrouzeixRaviartElement<2> > >
    restarted_problem(dt, &SarahBL::full_exact_soln);

    // Setup labels for output
    DocInfo restarted_doc_info;

    // Output directory
    restarted_doc_info.set_directory("RESULT_restarted");

    // Step number
    restarted_doc_info.number()=0;

    // Copy by performing a restart from old problem
    restart_file_pt=new ifstream("RESULT/restart2.dat");

    // Do the actual restart
    restarted_problem.restart(*restart_file_pt);

    // Do unsteady run of the problem for one step
    unsigned nstep=2;
    bool restarted=true;
    restarted_problem.unsteady_run(nstep, restarted, restarted_doc_info);
}
}

```

1.1 PDF file

A [pdf version](#) of this document is available.