## **Chapter 1**

## Demo problem: Boundary-driven elastic deformation of a fish-shaped domain

Detailed documentation to be written. Here's a plot of the result and the already fairly well documented driver code...

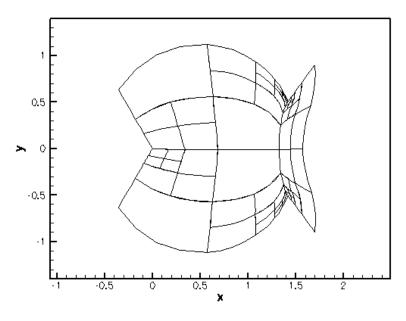


Figure 1.1 Boundary-driven elastic deformation of a fish-shaped domain.

```
//LIC// This file forms part of oomph-lib, the object-oriented,
//LIC// multi-physics finite-element library, available
//LIC// multi-physics finite-element library, available
//LIC// at http://www.oomph-lib.org.
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//LIC// 02110-1301 USA.
//LIC// The authors may be contacted at oomph-lib@maths.man.ac.uk.
// Driver for elastic deformation of a fish-shaped domain with
// adaptivity -- deformation is driven by displacement of
// GeomObject-based boundary!
// Generic oomph-lib headers
#include "generic.h"
// Solid mechanics
#include "solid.h"
// The fish mesh
#include "meshes/fish_mesh.h"
using namespace std;
using namespace oomph;
/// Refineable fish mesh upgraded to become a solid mesh
template<class ELEMENT>
class ElasticFishMesh : public virtual RefineableFishMesh<ELEMENT>,
                         public virtual SolidMesh
public:
 /// \ short Constructor: Build underlying adaptive fish mesh and then
 /// set current Eulerian coordinates to be the Lagrangian ones.
/// Pass pointer to geometric objects that specify the
/// fish's back in the "current" and "undeformed" configurations,
 /// and pointer to timestepper (defaults to Static)
 // Note: FishMesh is virtual base and its constructor is automatically
 // called first! --> this is where we need to build the mesh;
 // the constructors of the derived meshes don't call the // base constructor again and simply add the extra functionality. ElasticFishMesh(GeomObject* back_pt, GeomObject* undeformed_back_pt,
                  TimeStepper* time_stepper_pt=&Mesh::Default_TimeStepper) :
  FishMesh<ELEMENT>(back_pt,time_stepper_pt),
  RefineableFishMesh<ELEMENT>(back_pt,time_stepper_pt)
   // Mesh has been built, adaptivity etc has been set up -->
   // assign the Lagrangian coordinates so that the current
   // configuration becomes the stress-free initial configuration
   set_lagrangian_nodal_coordinates();
   // Build "undeformed" domain: This is a "deep" copy of the
   // Domain that we used to create set the Eulerian coordinates
   // in the initial mesh -- the original domain (accessible via
   // the private member data Domain_pt) will be used to update // the position of the boundary nodes; the copy that we're
   // creating here will be used to determine the Lagrangian coordinates
   // of any newly created SolidNodes during mesh refinement
   double xi_nose = this->Domain_pt->xi_nose();
double xi_tail = this->Domain_pt->xi_tail();
   Undeformed_domain_pt=new FishDomain(undeformed_back_pt,xi_nose,xi_tail);
   // Loop over all elements and set the undeformed macro element pointer
   unsigned n_element=this->nelement();
   for (unsigned e=0;e<n_element;e++)</pre>
    {
     // Get pointer to full element type
     ELEMENT* el_pt=dynamic_cast<ELEMENT*>(this->element_pt(e));
     // Set pointer to macro element so the curvlinear boundaries
     // of the undeformed mesh/domain get picked up during adaptive
     // mesh refinement
     el_pt->set_undeformed_macro_elem_pt(
      Undeformed_domain_pt->macro_element_pt(e));
     // Use MacroElement representation for
     // Lagrangian coordinates of newly created
     el_pt->enable_use_of_undeformed_macro_element_for_new_lagrangian_coords();
 /// Destructor: Kill "undeformed" Domain
 virtual ~ElasticFishMesh()
   delete Undeformed_domain_pt;
private:
```

```
/// Pointer to "undeformed" Domain -- used to determine the
/// Lagrangian coordinates of any newly created SolidNodes during
 /// Mesh refinement
Domain* Undeformed_domain_pt;
/// Global variables
namespace Global_Physical_Variables
 /// Pointer to strain energy function
StrainEnergyFunction* Strain_energy_function_pt;
 /// Pointer to constitutive law
ConstitutiveLaw* Constitutive_law_pt;
 /// Elastic modulus
double E=1.0;
 /// Poisson's ratio
double Nu=0.3;
 /// "Mooney Rivlin" coefficient for generalised Mooney Rivlin law
double C1=1.3;
 /// Body force
double Gravity=0.0;
 /// Body force vector: Vertically downwards with magnitude Gravity
void body_force(const double& t,
              const Vector<double>& xi,
              Vector<double>& b)
 b[0]=0.0;
 b[1]=-Gravity;
}
/// Boundary-driven elastic deformation of fish-shaped domain.
template<class ELEMENT>
class ElasticFishProblem : public Problem
public:
 /// Constructor:
ElasticFishProblem();
/// Run simulation.
void run();
 /// Access function for the mesh
ElasticFishMesh<ELEMENT>* mesh_pt()
 {return dynamic_cast<ElasticFishMesh<ELEMENT>*>(Problem::mesh_pt());}
/// Doc the solution
void doc_solution(DocInfo& doc_info);
 /// Update function (empty)
void actions_after_newton_solve() {}
/// \short Update before solve: We're dealing with a static problem so /// the nodal positions before the next solve merely serve as
 /// initial conditions. For meshes that are very strongly refined
 /// near the boundary, the update of the displacement boundary
 /// conditions (which only moves the SolidNodes *on* the boundary),
 /// can lead to strongly distorted meshes. This can cause the
 /// Newton method to fail --> the overall method is actually more robust
 /// if we use the nodal positions as determined by the Domain/MacroElement-
 /// based mesh update as initial guesses.
 void actions_before_newton_solve()
  bool update_all_solid_nodes=true;
  mesh_pt()->node_update(update_all_solid_nodes);
```

```
/// Update after adapt: Pin all redundant pressure nodes (if required)
 void actions after adapt()
   // Pin the redundant solid pressures (if any)
  {\tt PVDE} quations {\tt Base} < 2 {\tt >::pin\_redundant\_nodal\_solid\_pressures} \ (
   mesh_pt()->element_pt());
 // Geometric object that represents the deformable fish back
Circle* Fish_back_pt;
};
/// Constructor:
template<class ELEMENT>
ElasticFishProblem<ELEMENT>::ElasticFishProblem()
 // Set coordinates and radius for the circle that will become the fish back
double x_c=0.5;
double y_c=0.0;
double r_back=1.0;
 // Build geometric object that will become the deformable fish back
 // \texttt{GeomObject} \star \ \texttt{fish\_back\_pt=new ElasticFishBackElement} \ (\texttt{x\_c,y\_c,r\_back}) \ ;
Fish_back_pt=new Circle(x_c,y_c,r_back);
 // Build geometric object that specifies the fish back in the
 // undeformed configuration (basically a deep copy of the previous one)
GeomObject* undeformed_fish_back_pt=new Circle(x_c,y_c,r_back);
 // Build fish mesh with geometric objects that specify the deformable
 // and undeformed fish back
Problem::mesh_pt()=new ElasticFishMesh<ELEMENT>(Fish_back_pt,
                                                   undeformed fish back pt);
  / Set error estimator
 Z2ErrorEstimator* error_estimator_pt=new Z2ErrorEstimator;
mesh_pt()->spatial_error_estimator_pt()=error_estimator_pt;
 // Change/doc targets for mesh adaptation
mesh pt()->max permitted error()=0.05;
mesh_pt()->min_permitted_error()=0.005;
mesh_pt()->doc_adaptivity_targets(cout);
 // Pin all nodal positions apart from those on the tail
 unsigned num_bound = mesh_pt()->nboundary();
 for(unsigned ibound=0;ibound<num_bound;ibound++)</pre>
   if (ibound!=2)
     unsigned num_nod=mesh_pt()->nboundary_node(ibound);
     for (unsigned inod=0;inod<num_nod;inod++)</pre>
       for (unsigned i=0:i<2:i++)
         mesh_pt()->boundary_node_pt(ibound,inod)->pin_position(i);
      }
   }
 //Loop over the elements in the mesh to set parameters/function pointers
 unsigned n_element =mesh_pt()->nelement();
 for (unsigned i=0;i<n_element;i++)</pre>
   //Cast to a solid element
   ELEMENT *el_pt = dynamic_cast<ELEMENT*>(mesh_pt()->element_pt(i));
   // Set the constitutive law
   el_pt->constitutive_law_pt() =
    Global_Physical_Variables::Constitutive_law_pt;
   // Set the body force
   el_pt->body_force_fct_pt()=Global_Physical_Variables::body_force;
 // Pin the redundant solid pressures (if any)
PVDEquationsBase<2>::pin_redundant_nodal_solid_pressures(
 mesh\_pt() \rightarrow element\_pt());
 //Attach the boundary conditions to the mesh
cout « assign_eqn_numbers() « std::endl;
 // Refine the problem uniformly (this automatically passes the
 // function pointers/parameters to the finer elements
 refine_uniformly();
 // The non-pinned positions of the newly SolidNodes will have been
 // determined by interpolation. Update all solid nodes based on
 // the Mesh's Domain/MacroElement representation.
 bool update_all_solid_nodes=true;
mesh_pt()->node_update(update_all_solid_nodes);
 // Now set the Eulerian equal to the Lagrangian coordinates
mesh_pt()->set_lagrangian_nodal_coordinates();
}
```

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```
/// Doc the solution
template<class ELEMENT>
void ElasticFishProblem<ELEMENT>::doc solution(DocInfo& doc info)
ofstream some_file;
char filename[100];
 // Number of plot points
unsigned npts = 5;
// Output shape of deformed body sprintf(filename, "%s/soln%i.dat", doc_info.directory().c_str(),
         doc_info.number());
 some_file.open(filename);
mesh_pt()->output(some_file,npts);
 some_file.close();
 // removed until Jacobi eigensolver is re-instated
// Output principal stress vectors at the centre of all elements // SolidHelpers::doc_2D_principal_stress<ELEMENT>(doc_info,mesh_pt());
/// Run the problem
template<class ELEMENT>
void ElasticFishProblem<ELEMENT>::run()
 // Output
DocInfo doc_info;
 // Set output directory
doc_info.set_directory("RESLT");
 // Step number
doc_info.number()=0;
// Initial parameter values
 // Gravity:
Global_Physical_Variables::Gravity=0.1;
 //Parameter incrementation
unsigned nstep=5;
 for(unsigned i=0;i<nstep;i++)</pre>
   //Solve the problem with Newton's method, allowing for up to 5
   //rounds of adaptation
   newton_solve(5);
   // Doc solution
   doc_solution(doc_info);
  doc_info.number()++;
   // Increment width
   Fish_back_pt->y_c()+=0.03;
/// Driver for simple elastic problem
int main()
 //Initialise physical parameters
Global_Physical_Variables::E = 2.1;
Global_Physical_Variables::Nu = 0.4;
Global_Physical_Variables::C1 = 1.3;
 // Define a strain energy function: Generalised Mooney Rivlin
Global_Physical_Variables::Strain_energy_function_pt =
 &Global_Physical_Variables::E);
 // Define a constitutive law (based on strain energy function)
Global_Physical_Variables::Constitutive_law_pt
 \verb"new IsotropicStrainEnergyFunctionConstitutiveLaw" (
  Global_Physical_Variables::Strain_energy_function_pt);
 //Set up the problem with pure displacement formulation
 ElasticFishProblem<RefineableQPVDElement<2,3> > problem;
problem.run();
```

## 1.1 PDF file

A pdf version of this document is available.