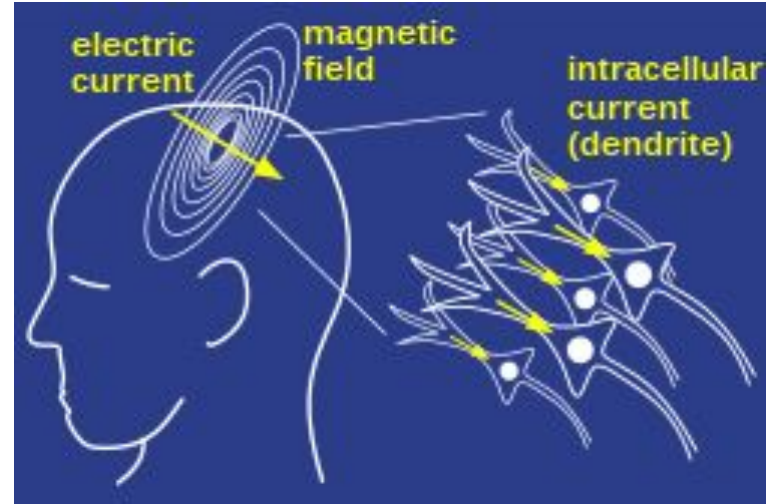


# Quantum Sensing: Magnetic Flux Detection

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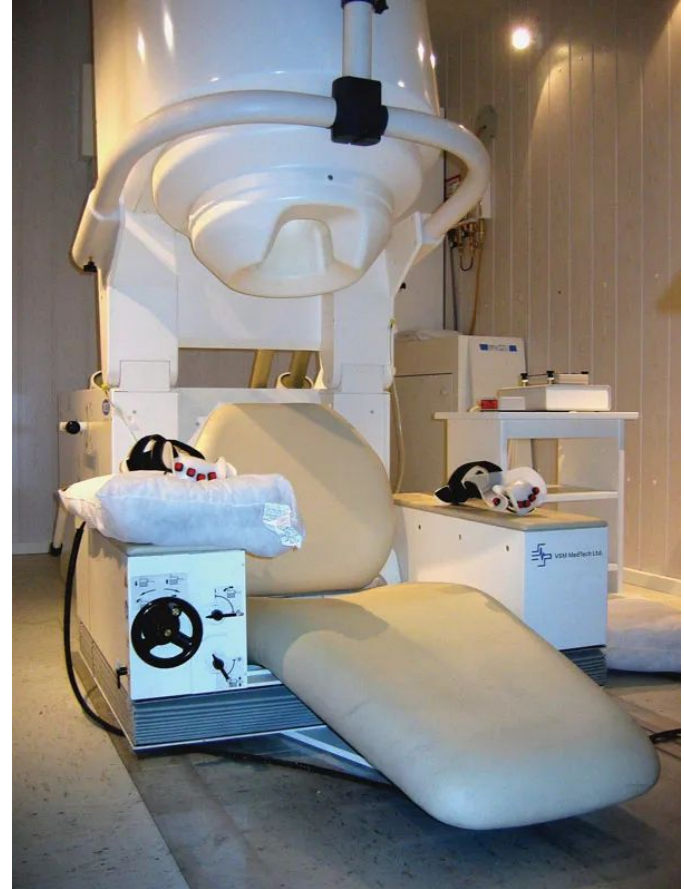
# Overview

- **Magnetoencephalography (MEG)**
  - Neuroimaging technique
  - used to measure magnetic fields produced by neuronal activity in the brain
- Neurons in the brain generate electrical currents when they communicate, resulting in tiny magnetic fields being produced



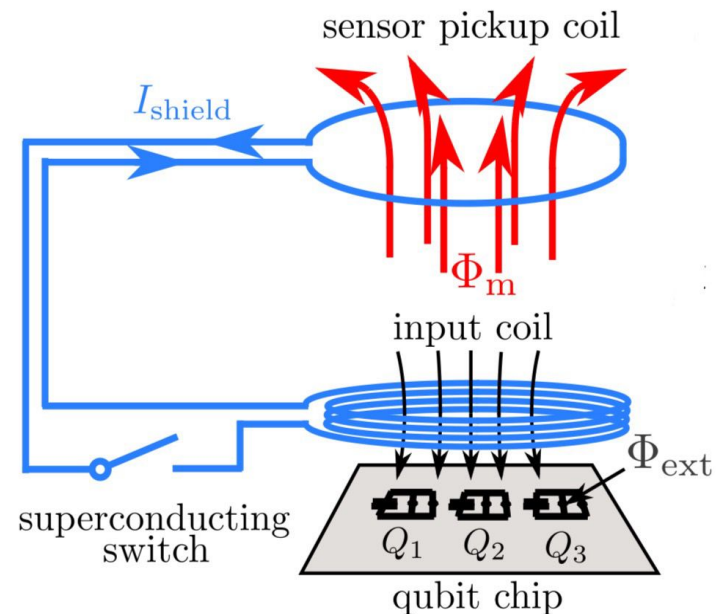
# SQUIDS

- **Superconducting Quantum Interference Device (SQUIDS)** is a magnetometer that detects magnetic fields from neural activity within the brain
  - Extremely sensitive to small magnetic fields



# Quantum Sensors

- $\Phi_m$ : general flux to be measured
- $I_{\text{shield}}$ : Current representing  $\Phi_m$
- $\Phi_{\text{ext}}$ : magnetic flux representing  $\Phi_m$ 
  - They are exposed to the  $\Phi_{\text{ext}}$ 
    - This results in a phase shift depending on exposure time
      - Exposure time is determined by the superconducting switch
    - Phase shift is dependent on the strength of the flux and the time of exposure



# Ramsey Fringes Interferometry

- Technique used to measure phase evolution of qubits as it interacts with external fields
-

# Sensor Output Interpretation

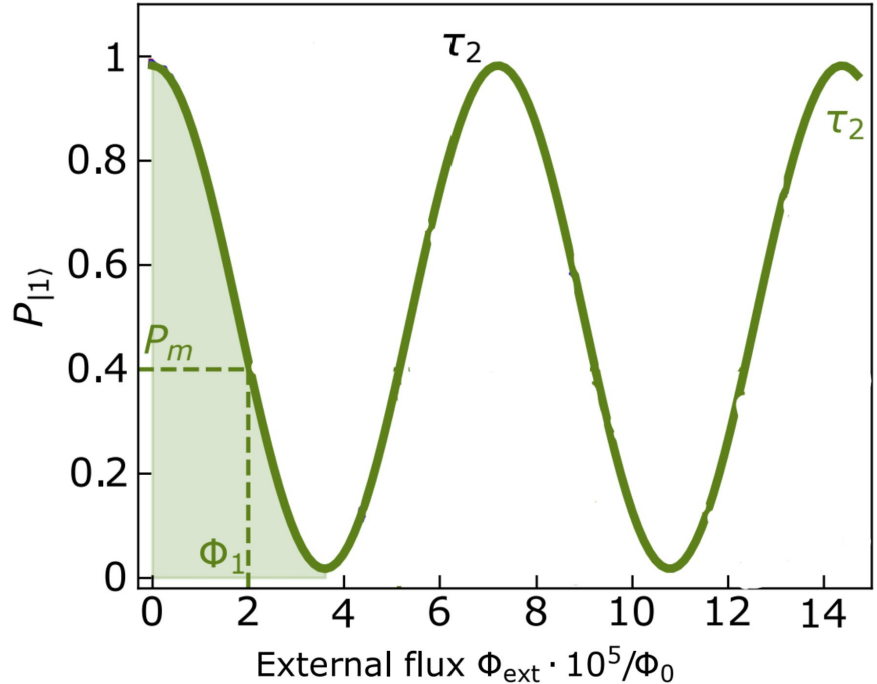
$P_m$  is an outcome from sensing procedure

$\tau$  is the delay time

Amount of time the sensor has been

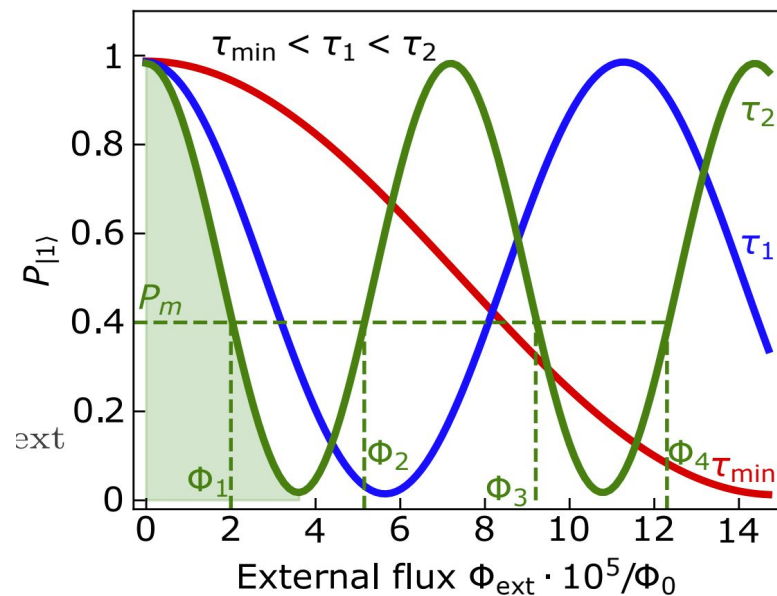
Influenced by the magnetic flux

$\Phi$  is the external flux we are measuring



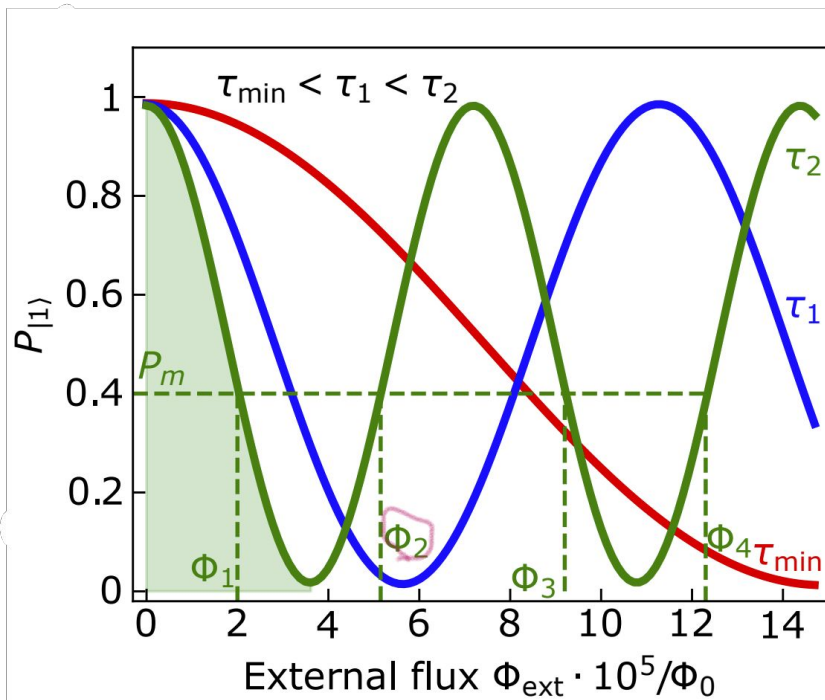
# Issues

- Selecting the optimal delay time for unknown flux value.
  - $\tau_{\text{opt}}$  as large as possible
  - Larger delay times are more sensitive to flux



# Issues

- For longer delay times, it is not possible to unambiguously determine the measured flux based on a single outcome
  - $\Phi_1, \Phi_2, \Phi_3, \Phi_4$ ?
  - Coherence time
    - Time qubit can maintain its state
      - Decoherence occur after
        - Energy relaxation
        - Dephasing
    - Depends on qubit





# Coherence only if asked.

how long a qubit can maintain its quantum state before it is disrupted by decoherence mechanisms, such as energy relaxation and dephasing.

# Solution

- For this we use PEA(Phase Estimation Algorithms) to find the optimal delay time
- One common approach is using Kitaev algorithm
- Using Kitaev's algorithm provides both a higher accuracy and a faster runtime as will be shown next

# Kitaev's Algorithm

# Simulation

Create  $n$  ancilla qubits

Apply the Hadamard gate to ancilla qubits

Apply the  $U$  gate to the qubit being controlled

```
home > tai > Desktop > qiskit2.py > ...
1  from qiskit import QuantumCircuit
2  from qiskit_aer import AerSimulator
3  from qiskit.circuit.library import QFT
4  from qiskit.visualization import plot_histogram
5  from qiskit.utils import QuantumInstance
6  import numpy as np
7
8  # Define the phase for the U gate
9  theta = 0.5
10 U = QuantumCircuit(1)
11 U.rz(2 * np.pi * theta, 0) # U = Rz(2*pi*theta)
12 U = U.to_gate()
13 U.name = "U"
14
15 # Kitaev Phase Estimation Circuit
16 tabnine:test|explain|document|ask
17 def kitaev_phase_estimation(U, n_bits):
18     qc = QuantumCircuit(n_bits + 1, n_bits)
19
20     # Apply H-gates to all ancilla qubits
21     for i in range(n_bits):
22         qc.h(i)
23
24     # Controlled-U operations
25     for i in range(n_bits):
26         qc.append(U.control(), [i, n_bits])
27
28     # Inverse Quantum Fourier Transform
29     qc.append(QFT(num_qubits=n_bits, inverse=True).to_gate(), range(n_bits))
30
31     # Measure the ancilla qubits
32     qc.measure(range(n_bits), range(n_bits))
33     return qc
34
35 # Number of bits for phase estimation (try increasing this value)
36 n_bits = 1
37
38 # Create the phase estimation circuit
39 qc = kitaev_phase_estimation(U, n_bits)
40
41 # Set up the AerSimulator
42 simulator = AerSimulator()
43
44 # Run the simulation using the QuantumInstance
45 quantum_instance = QuantumInstance(backend=simulator, shots=1024)
46 result = quantum_instance.execute(qc)
47 # print(result)
48 counts = result.get_counts(qc)
49
50 # Plot the results
51 plot_histogram(counts)
52
53 # Estimate the phase from the most frequent result
54 max_count = max(counts, key=count.get)
55 estimated_phase = int(max_count, 2) / 2**n_bits
56 print(f"Estimated Phase: {estimated_phase}")
```

# References

[1] Matthew J. Brookes (2022)

Magnetoencephalography with optically pumped magnetometers (OPM-MEG): the next generation of functional neuroimaging  
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Optically pumped magnetometers: From quantum origins to multi-channel magnetoencephalography  
(<https://www.sciencedirect.com/science/article/pii/S1053811919304550>)

[3] Tengyue Long (2023)

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(<https://ieeexplore.ieee.org/document/10352347>)

[4] Sergey Danilin (2024)

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(<https://arxiv.org/abs/2211.08344>)