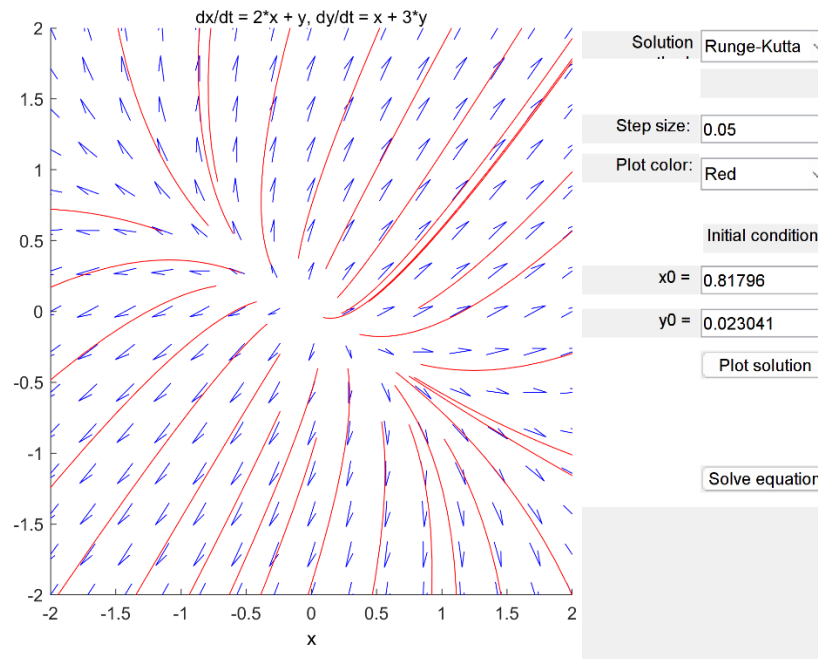


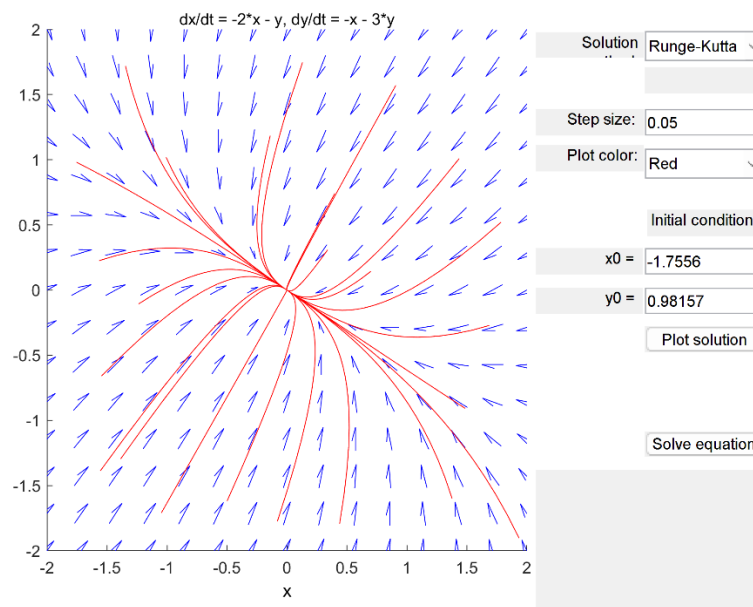
MAT 292 - Exercise 4

1. Plot



- 
- Unstable, Nodal Source, Motion N/A
- $\lambda_1 = (5+\sqrt{5})/2$ ;  $\lambda_2 = (5-\sqrt{5})/2$ . Since there're 2 distinct positive real eigenvalues, therefore, Unstable Node.

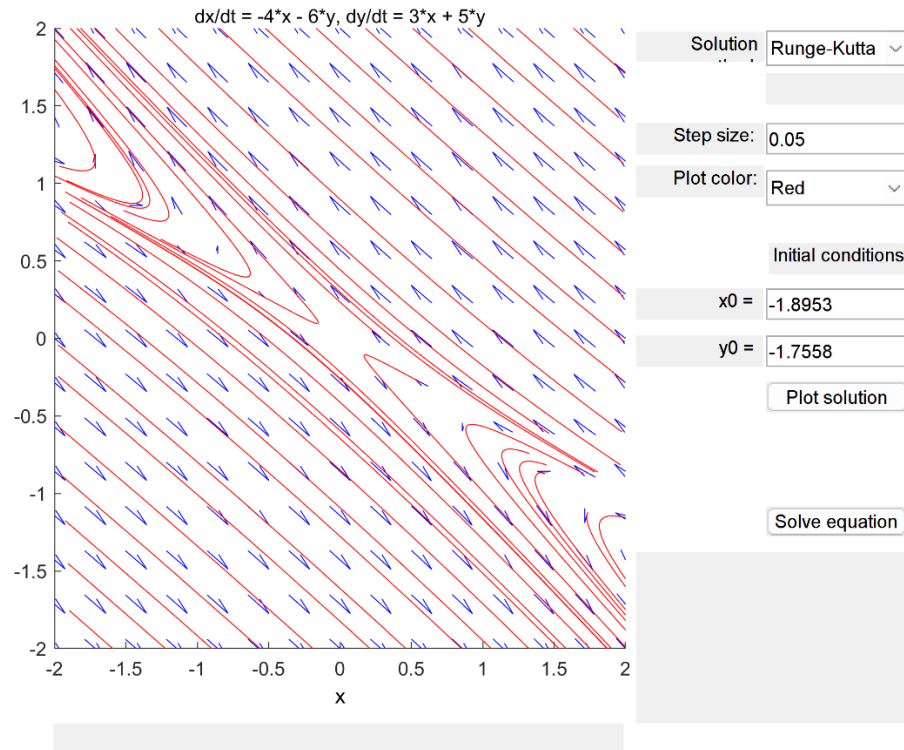
2. Plot



-

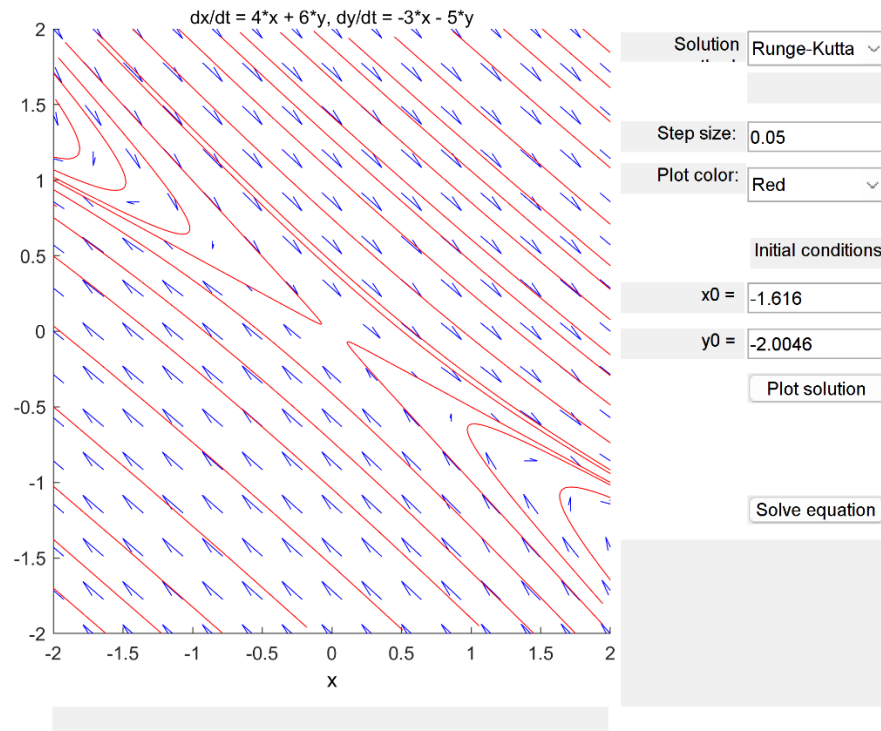
- b. Stable, Nodal Sink, Motion N/A
- c.  $\lambda_1 = (-5+\sqrt{5})/2$ ;  $\lambda_2 = (-5-\sqrt{5})/2$ . Since there're 2 distinct negative real eigenvalues, therefore, Stable Node.

3. Plot

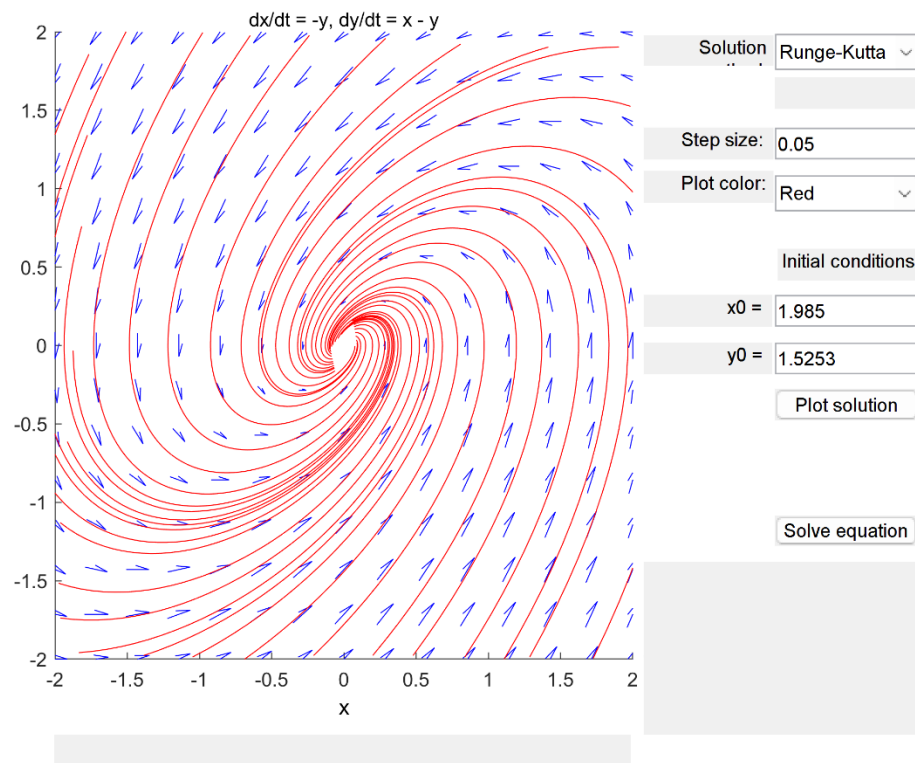


- a.
- b. Unstable, Saddle Point, Motion N/A
- c.  $\lambda_1 = -1$ ;  $\lambda_2 = 2$ . Since eigenvalues are real, distinct, and  $\lambda_1 = -k(\lambda_2)$ . Thus, Saddle Point

4. Plot



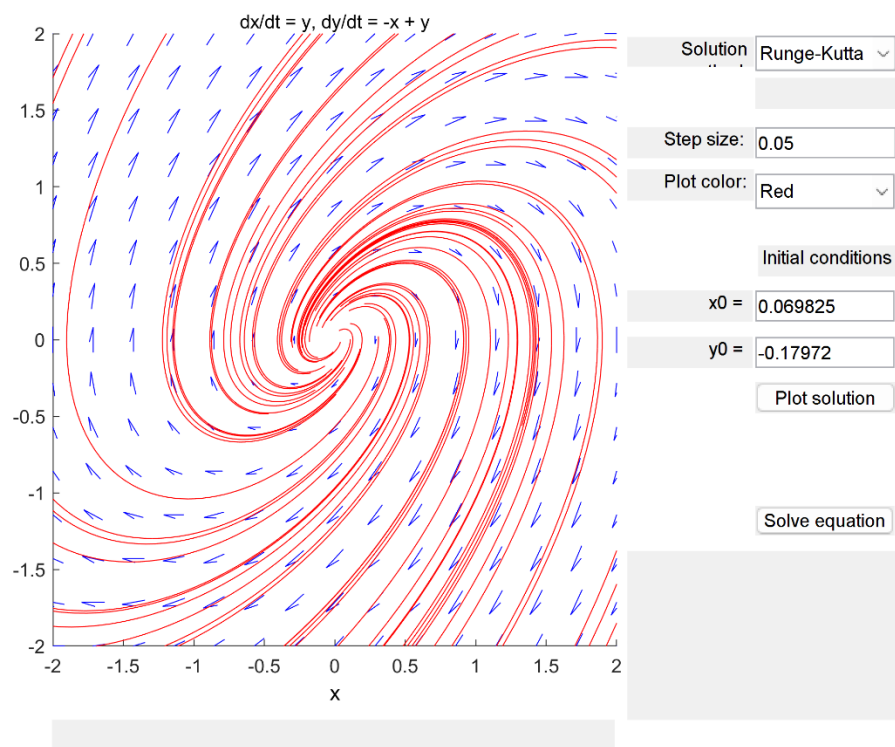
- - Unstable, Saddle Point, Motion N/A
  - $\lambda_1 = -2; \lambda_2 = 1$ . Since eigenvalues are real, distinct, and  $\lambda_1 = -k(\lambda_2)$ . Thus, Saddle Point
5. Plot



- 
- Stable, Spiral Sink, Motion: CCW

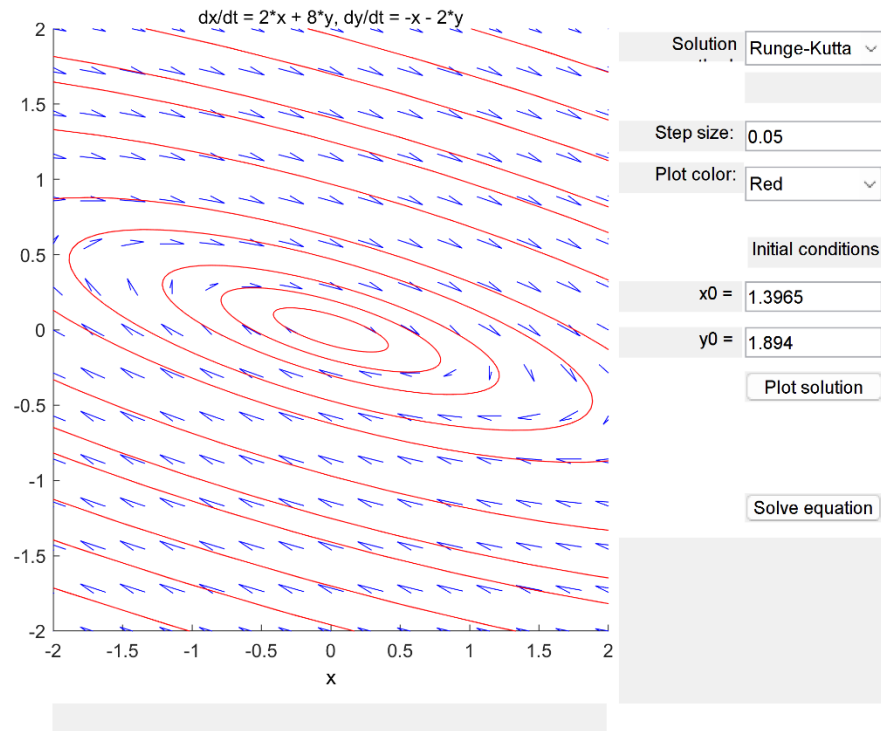
- c.  $\lambda_1 = -1/2 + i\sqrt{3}/2$ ;  $\lambda_2 = -1/2 - i\sqrt{3}/2$ . Since distinct and complex eigenvalues with negative real parts. Thus, Spiral Sink

6. Plot



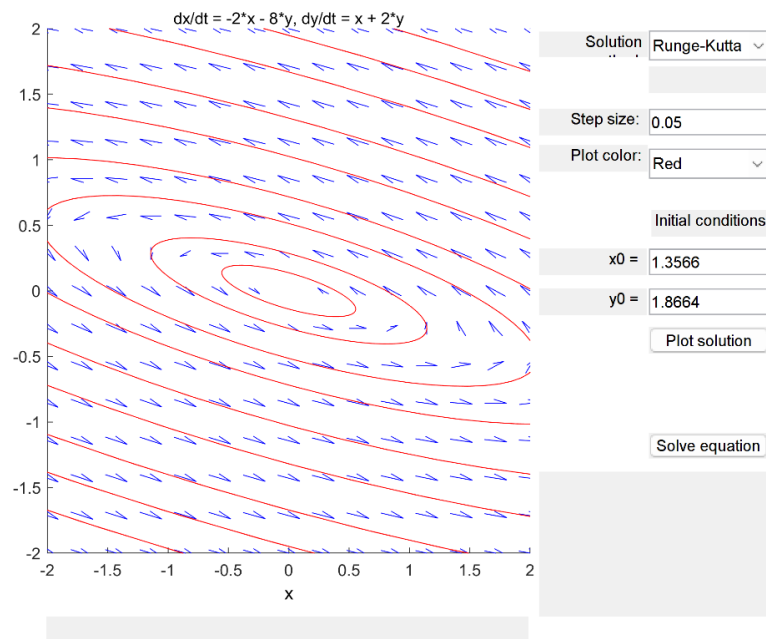
- a.
- b. Unstable, Spiral Source, Motion: CW
- c.  $\lambda_1 = 1/2 + i\sqrt{3}/2$ ;  $\lambda_2 = 1/2 - i\sqrt{3}/2$ . Since distinct and complex eigenvalues with positive real parts. Thus, Spiral source.

7. Plot



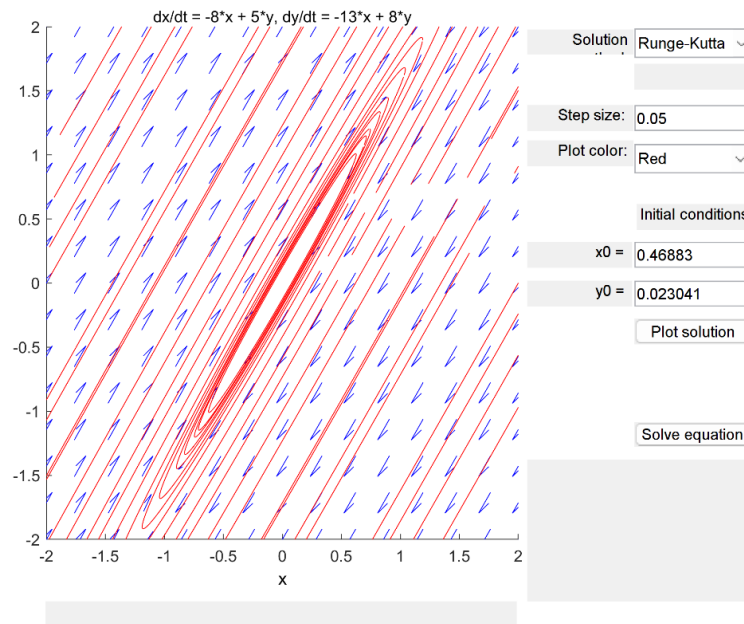
- 
- Stable, Center, Motion: CW
- $\lambda_1 = -2i; \lambda_2 = 2i$ . Since distinct, opposite signs, complex without real parts. Thus, clockwise stable center.

## 8. Plot



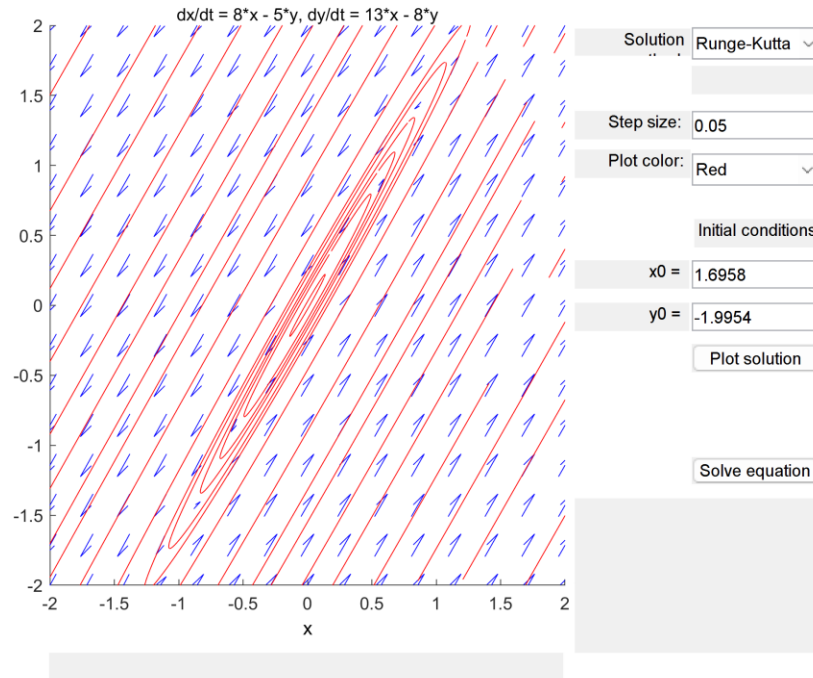
- 
- Stable, Center, Motion: CCW
- $\lambda_1 = -2i; \lambda_2 = 2i$ . Since distinct, opposite signs, complex without real parts. Thus, counterclockwise stable center.

## 9. Plot



- 
- Stable, Center, Motion: CW
- $\lambda_1 = -i$ ;  $\lambda_2 = i$ . Since distinct, opposite, complex with no real parts. Thus, clockwise stable center.

## 10. Plot



- 
- Stable, Center, Motion: CCW
- $\lambda_1 = -i$ ;  $\lambda_2 = i$ . Since distinct, opposite, complex with no real parts. Thus, counterclockwise stable center.