

Принцип расширения

$$A \widetilde{\subset} A, \quad B \widetilde{\subset} B, \quad C \widetilde{\subset} C$$

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$$\star : \mathbb{A} \times \mathbb{B} \rightarrow \mathbb{C}$$

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$$\mu_C(0) =$$

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$$\mu_C(c) = \max_{a,b : a+b=c} [\mu_A(a)\mu_B(b)]$$

$$\mu_C(0) = \max \left(\begin{array}{cc} 0.5 \cdot 0.1, & 0.9 \cdot 0.5, \\ 0.1 \cdot 0.9, & 0.1 \cdot 0.1 \end{array} \right) =$$

$$= \max(0.05, 0.45, 0.09, 0.01) = 0.45$$

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$$C = \frac{0.45}{0} +$$

$$\mu_C(1) = \max(0.05, 0.09, 0.05, 0.09)$$

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$$\mu_C(c) = \max_{a,b : a+b=c} [\mu_A(a)\mu_B(b)]$$

$$C = \frac{0.45}{0} + \frac{0.09}{1} +$$

$$\mu_C(2) = \max(0.45, 0.09, 0.01, 0.05)$$

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$$\mu_C(c) = \max_{a,b : a+b=c} [\mu_A(a)\mu_B(b)]$$

$$C = \frac{0.45}{0} + \frac{0.09}{1} + \frac{0.45}{2} +$$

$$\mu_C(3) = \max(0.25, 0.81, 0.01, 0.01)$$

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