Pratical work: EM algorithm

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Simulation

We first generate:

- 1. A sample of n = 100 observations with a Poisson law using $\lambda = 3$.
- 2. A sample of n = 200 observations with a Poisson law using $\lambda = 15$.
- 3. A vectgor of 300 coordinates, which the 100 first are 1 and the others are 2.

```
sample3 <- rpois(100, 3)</pre>
print(sample3)
             \begin{smallmatrix} 1 \end{smallmatrix} \begin{smallmatrix} 1 \end{smallmatrix} \begin{smallmatrix} 3 \end{smallmatrix} \begin{smallmatrix} 8 \end{smallmatrix} \begin{smallmatrix} 5 \end{smallmatrix} \begin{smallmatrix} 5 \end{smallmatrix} \begin{smallmatrix} 0 \end{smallmatrix} \begin{smallmatrix} 0 \end{smallmatrix} \begin{smallmatrix} 3 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 0 \end{smallmatrix} \begin{smallmatrix} 7 \end{smallmatrix} \begin{smallmatrix} 7 \end{smallmatrix} \begin{smallmatrix} 8 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 5 \end{smallmatrix} \begin{smallmatrix} 3 \end{smallmatrix} \begin{smallmatrix} 5 \end{smallmatrix} \begin{smallmatrix} 6 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 7 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 3 \end{smallmatrix} \begin{smallmatrix} 7 \end{smallmatrix} \begin{smallmatrix} 3 \end{smallmatrix} \begin{smallmatrix} 5 \end{smallmatrix} \begin{smallmatrix} 0 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 5 \end{smallmatrix} \begin{smallmatrix} 3 \end{smallmatrix} \begin{smallmatrix} 5 \end{smallmatrix} 
          [38] 3 3 4 2 1 1 2 4 1 0 1 4 2 4 4 4 1 3 0 2 1 4 3 5 5 4 1 3 3 0 5 1 3 7 2 2 7
         [75] 0 4 3 3 4 1 2 1 6 6 4 4 2 3 1 5 2 2 2 8 4 3 4 2 1 3
sample15 <- rpois(200, 15)</pre>
print(sample15)
            [1] 13 9 13 12 12 16 21 8 25 17 13 23 11 13 11 10 6 10 14 11 18 14 15 15 16
          [26] 10 16 22 16 17 18 18 15 16 17 11 14 15 9 8 18 18 18
                    9 18 8 15 13 12 23 22 19 14 12 14 8 10 16 17 13 18 16 16 16 13 15 10 17
      [76] 19 16 20 10 9 14 16 15 15 11 15 15 17 21 21 21 7 23 12 10 10 12 14
## [101] 18 16 13 18 19 15 16 15 19 12 14 19 15 11 19 15 21 13 17 13 13  9 12
## [126] 14 16 8 14 14 11 16 16 15 12 12 13 17 11 12 9 15 18 12 14 15 16 19 16 17
## [151] 25 15 15 19 9 11 14 15 15 15 19 15 14 17 11 11 13 13 14 21 13 19 19 15 15
## [176] 15 12 15 8 21 21 23 18 14 13 26 10 15 19 18 13 14 16 26 9 13 7 15 17
v <- c()
for (i in 1:100)
{
    v <- c(v, 1, recursive = TRUE)</pre>
}
for (i in 1:200)
    v <- c(v, 2, recursive = TRUE)</pre>
}
```

Now, we are going to generate a Poisson law using two components:

```
#Settings constants
pi1 <- 0.4
pi2 <- 0.4
lambda1 <- 3
```

lambda2 <- 15
#Computing sample</pre>