CECS 444 Compiler Constructions

Seminar Notes

August 28, 2018

Syllabus

Things to cover:

Treewalking (binary)

Textbook:

Fisher, Cytron, Leblanc

- Crafting a Compiler (2009 ~720pg)

Grading:

Cumulative Exams

20% Exams I

20% Exams II

33% Final

20% Projects (Will build on each other)

7% Quiz, Paper, Participation

MGR Types: (Manager Types)

Good: 10% - Super people

Bad: 80% - Need people to do the job

They buy programmers "By the Yard"

Ugly: 10% - Backstab

Mini- SWE (Software Engineering) Rules

** Reasonable Person STD (Standard)

- Due Diligence (Everybody has their own view)

Pace yourself



- AIO: (Adapt, Improvise, and Overcome)
- ** "Smart" Person STD
 - Always be ready to show your work (Show your progress)
- ★ Most Important Things in SW(Software): MORALE

Rules:

0. Get to working Software Fast!

(Go ugly early)

. . . .

Why!



- 1. You can see it work
- * 2. Users can see it & tell you it sucks
 - Get users feedback faster

(MVP = Minimum Viable Product)

- 1. Never Pre-Optimize (Usually 1% of code is too slow)
 - Change this 1% and program increases more in speed
 - *** Optimize ONLY when proven needed
- 2. No "BUG HUNTS"
 - I. Compile-Time Errors \leq 5 mins to fix
 - II. Usually 90% of DEV Time spend on Run-Time Bugs
 - How to get rid of it?
 - Force all bugs into small box (look there!)
 - ★ Use "Add-A-Trick"
 - Add 1-N Lines, Compile, then Test
- 3. EIO (Expected Input/Output)
 - *** Build Before Coding (Slice it into Itty-Bitty Stepping Stones)
 - It focus design on what is important
 - *** Avoid "Gold-Platting"

Continued on August 30, but placed here since it

- Making things look nice with nothing to functionality

continue ---> 4. Clean The Page. (~ 50 to n lines of code per page)

- Usually one page for a Function so easy to read

August 30, 2018

Homework: Read Fischer

Chapter 1 Intro - 30pg

Chapter 2 Compiler Parts - 25pg

Chapter 3 Scanner/Lexer - 50pg

Mini Study Rules:

- 1. Textual Mean
 - Build/Use "Flash-Cards" (3x5)
- 2. Visual Memory

IE: Charts, Graphs, etc

- Draw it twice, looking
- Draw it Blind
 - win 3x include labels

TreeWalking:

- Consist of: Var

Post Pre order IN Left / Right / Lollypop = Var Var Var

Var

```
CLASS Node
```

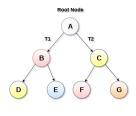
{

INT VAL;

NODE LKid;

NODE RKid;

}



Binary Tree

```
Void printTree(NODE root)
      # Basic Step
      If (NULL == root)
      {
             RGT; #Abbr. for returning nothing
      # Left Recur
      printTree(root.LKid);
      # Right Recur
      printTree(root.RKid);
      # Deal with LollyPOP
      System.out.println(root.VAL);
      # GLUE
      // None
}
Void countTree(NODE RP)
{
      # Basic Step
      If (NULL == root)
             RGT; #Abbr. for returning nothing
```

Left Recur

Right Recur

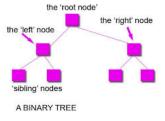
INT Lx = countTree(RP.LKid);

INT Rx = countTree(RP.RKid);

Deal with LollyPOP

To Do For TreeWalking:

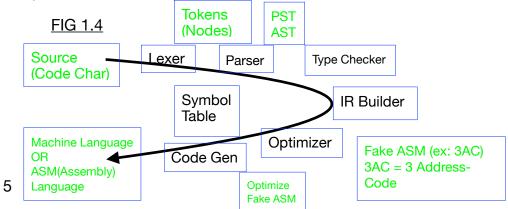
- 1. Header
- 2. Basic Step
 - Do manually
- 3. Left/Right Recur4. Deal with Lollypop
- 5. Glue



(c)www.leach-ict.or

```
Px = 1;
      # GLUE
      Return Lx + Rx + Px;
}
Void sumValTree(NODE RP)
      # Deal with LollyPOP
      Px = RP.VAL;
       . . .
}
Void sumValForKind(NODE RP, INT RK)
      # Left Recur
       .... RK
      # Right Recur
      ..... RK
      # Deal with LollyPOP
      Px = (RK == RP.kind)
             ? RP.VAL
             :\theta);
}
```

Chapter 1 Parts of Compiler:



Lexer = Lexical Analysis

- Lang. REGEXES

Parser = Syntactic Analysis

- CFG (Context Free Grammar) Rules

Type Checker & IR Builder = Semantic Analysis (Good meaning)

- IR Builder (Intermediate Representation Builder)
 - In each stages, since they are not source or final, they are
 IR
- AST + Decoration

Optimizer

Code Generation = Final representation (Emiter Phase)

- "Emits" Machine/ASM/Byte Code
 - Bytecode usually mean for JAVA since it is old
 - For interpreter/VM Architecture
- Machine Architecture Description

Symbol Table:

- Contains all user-define names (names = symbols)
- Are builded into debugger

Front End:

Between beginning to Syntactics Analysis

Back End:

- After Syntactics Analysis to end

PST (Parse Tree): Convert to AST (through Parser)

AST (Abstract Syntax Tree): In one simple operation from PST —> AST

September 4, 2018

Homework: Read Fisher

Chapter 3 Scanner (Lexer)

Chapter 3.2 REGEX (Regular Expression)

- Regular Lang
- 1. LITERALS: "3", "Hi"
- 2. Wildcard Character "operator".
 - Uses Period

IE: c.t

All matches of period wildcard -> {Cat, Cbt, C7t, C\$t, c t, c.t,...}

- 3. Escape (De-Opify)
 - Uses Backslash

IE:
$$c \cdot t -> \{c.t\}$$

IE:
$$c \setminus t \longrightarrow \{c \setminus t\}$$

- 4. Optional
 - Uses Question Mark

IE: Ca?t
$$\rightarrow$$
 {ct, cat}

- 5. Grouping
 - Uses Parenthesis

IE:
$$C(a)t \rightarrow \{Cat\}$$

IE:
$$(Ca)$$
?t $-> \{t, Cat\}$

- 6. Zero or More (AKA: Kleene Star)
 - Uses Astris

IE:
$$(Ca)^*t \rightarrow \{t, Cat, CaCat,...\}$$

7. 1 or more (AKA: Kleene Plus, Positive Closure)

- Uses Plus

- Give me one or more "wildcard char op"
- 8. Any 1 Char: From the set
 - Uses Brackets (Anything inside the bracket is auto escape)

- *9. Choose Sequence of (AKA "OR")
 - Uses Vertical Stroke

$$\label{eq:lem:coll} \mbox{IE: C(a|o+|u)LL } \longrightarrow \{\mbox{CaLL, CoLL, CuLL, Cooll}, \mbox{Cooll}\}$$

$$- a | o + | u = a \text{ or } o + \text{ or } u$$

- 10. In a Char Subset: A Range of..
 - Uses Hyphen

IE:
$$a[A-D]z \rightarrow \{aAz, aBz, aCz, aDz\}$$

y := x * 2 + 3

Lexer

Project 1 Lexer

Digits =
$$[0.9]$$
+

y = x * 2

FSM = Finite State Machine (AKA: DFA)

DFA = Deterministic(no choice) Finite Automaton

States

2 Types:

AS = Accept State(s) AKA Recognized

- Found a Match (Doesn't mean stop)

- Events (Words Event, Letters Event)
- Links/Moves (Labeled with Events)
 - moving from one state to another based on events

Input Event Sequence leading from SS to some AS

- A word/sentence in the "Language" of the Regex

IE: Regex,
$$R = C(a \mid o \mid u)t$$

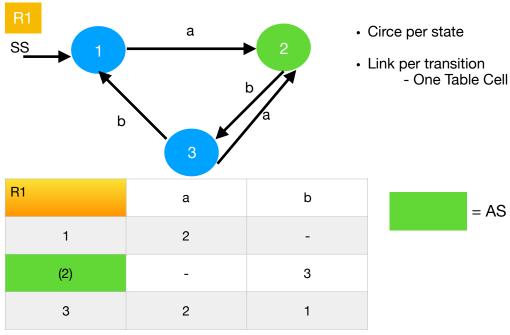
IE: R' = See the (cat|dog|bear)\?

L(R') = {"See the cat?", "See the dog?", "See the bear?"}

DFA Format/"Coding"

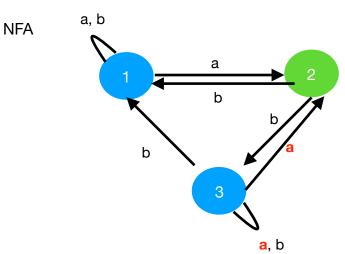
State transition

- Table/(Matrix)
- Diagram/(Graph)



- Row per state
- Column per event

• Empty Cell = no possible match



- Because of a, we have choice so NFA

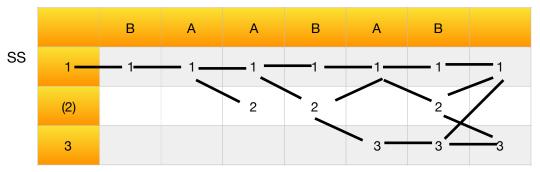
R2	а	b
1	1,2	1
(2)	-	1,3
3	2,3	1,3

- NFA Choice, 2 Ways:
 - 1. Choice of Moves (From State, on Event)
 - 2. "Epsilon Move" Greek E (ϵ) for empty

*(FISCHER uses Lambda, λ)

★ Convert NFA to DFA:

"Path Graph": BAABAB\$ (\$ = end of input)

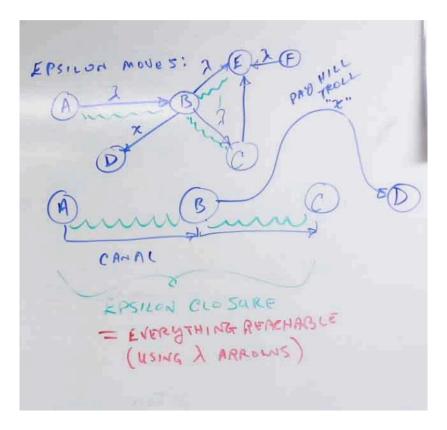


To DFA	а	b
{1}	{1,2}	{1}
{1,2}	{1,2}	{1,3}
{1,3}	{1,2,3}	{1,3}
{1,2,3}	{1,2,3}	{1,3}
{2,3}	{2,3}	

Q: How many DFA States from "N" NFA States max?

Ans: $2^n - 1$

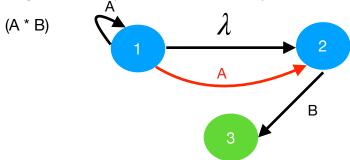
Epsilon Moves:



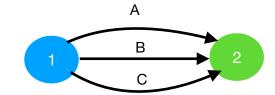
September 6, 2018

Why NFA Bother?

Regex to FSM (Finite State Machine)



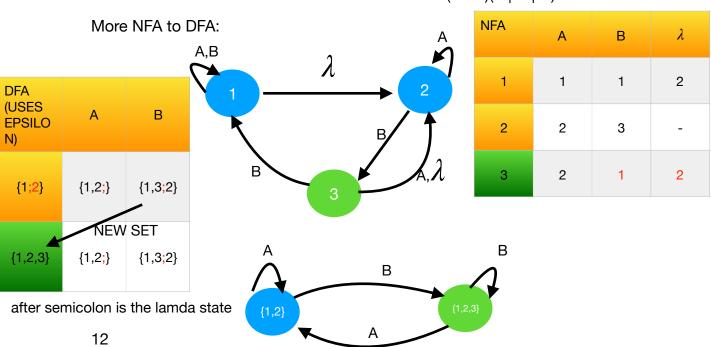




(A . B)



- These Scenario can be combined: (A . B)(A | B | C)



- The red semi colon is there even though on cell {1;2}A the lamda doesn't go anywhere beside 1 and 2
- On cell {1;2}B, we got a new set, {1,3,2} so we start a new row for {1,2,3}.
 - After that row, no more new set, so we stop
- Since 3 is the accept state, anything with a 3 will be green, aka accepted

READ FISHER

Chapter 4

Chapter 5.1 - 5.4

September 11, 2018

History: High-Level Langs

Java - 16%

Python - 5%

C - 14% C++ - 8%

Read Chapter 3: 1957: FORTRAN (FTN)

Skip 3.5 Lex 1958: LISP (A.I)

Read Chapter 4:

1960: Cobol
1960: Algol 60

then 4.4
- Algol 68 (Euro ver.)

Previous: Regular Langs Popular Langs: (TIOBE website)

- REGEX Market Shares:

CFG: Context-Free Grammar

CFG Rules

• LHS = RHS (left hand side = right hand side)

1 Symbol = Sequence 0 or more Symbols

C# - 4%
VB - 4%
PHP
Javascript
SQL
RUBY

::=

<- = LHS "expands to" RHS in A "Derivation"</pre>

GMR "G":

IE: $S = X \mid Y$ is an example of Combo - Rule

- Rule 1: S = X is Simple Rule OR
- Rule 2: S = Y

IE:
$$X = a \mid yxy$$

- RHS = Terminal Symbol
 - 1. Can't expand
 - 2. Not on LHS
- LHS = Non-Terminal Symbol

Lang "G": All "sentence" described by GMR "G"

Q: is "bab" in L(G)?

Try to derive from Starting Symbol

A: * We can only "->" into something that is rule in GMR "G"

yxy // second y
$$\rightarrow$$
 b

- Right-Most Derivation

yxb
$$//X \rightarrow a$$

yab
$$// Y \rightarrow b$$

Parse Tree (PST):

S

Χ

y x y

b a b

LR = Left-To-Right Scan & Right-Most Derivation

LL = Left-To-Right Scan & Left-Most Derivation

```
S
                                              AST = Abstract-Syntax-Tree
                                              Subj
                                                    Verb
                                                          Obj
IE: I See The Red Truck
                                              1
                                                          S = Subj Verb Obj
                                              Man
                                                    SEE
                                                          Adj Adj Noun
      Person = I | You | Fred | ....
                                                          the red truck
```

"GE": Arith Expr GMR

PIC GOES HERE

```
"Recursive Descent" Parser
- Uses Depth First Search (DFS)
REG:
• Each Non-T gets a Function
• Each Rule gets a "Trial" in that function
- to match next input Sequence
BOOL E() // Match the first E = ... rule
{
Input_Pos = Current;
if (match (E) && match('+') && match('T'))
```

```
{
                                 return True;
                           }
                           Else (E() && match('-') && T())
                           {
                                 return True;
                          }
                           Else (T()) return True;
                           return False;
      Cons:
             - Most Tries Fail

    Very Slow

             - If Error, tries everything first
LL Parse Machine
                 + Table +
                                               Stack
      Machine
      4 Steps
                           Predict the rules
                                               Partial Derivation
```

September 13, 2018

LL Parser:

Machine, Table, Stack

Table: (LHS, TERM) — LHS = top of stack TERM = Front of input

	Terminal 1	Terminal 2	
LHS 1	###	-	
LHS 2	-	-	R#2
LHS 3	-	R#16	

$$N = N A B C --> Left Recursion$$

$$X = A B X C$$
 —-> Also recursion

Things we need to do:

- 1. Need simple rules
- 2. Get rid of left recursion

Combo —> Simple:

$$E = E + T \mid E - T$$

- Breaking it down : E = E + T

E = E - T

$$A = B [C-DF]G$$

- Breaking it down: A = B C G

A = BDG

A = B F G

- The F is there as extra step

A = B ? C

- Breaking it Down: A = B C

A = C

A = X * Y

- Breaking it down: A = N Y

N = X N - Right Recursion

- As much X as I want with N since *

 $N = \lambda$

$$A = B(X|Y)?C$$

- Breaking it Down: A = B X C

A = B Y C

$$A = B C$$

$$A = B X + Y \text{ or } A = B X X * Y (C.F Ex: p 138 #3, 7)$$

- A = B X X * Y is similar to A = X * Y so just pretend B X is the front

LRE = Left Recursion Elimination

Direct LRE = N = N - Directly calling itself, NOT foo calls bar and bar calls foo.

GE: * In GE, lowercase are TERM and uppercase are Non-TERM

$$E = E + T | E - T | T$$

$$T = T * F | T / F | F$$

$$F = i | K | '(' E ')'$$

- 9 Rules

- 3 Rules to do LRE for one NON-TERMINAL, N:
 - 1. Add a new NON-TERMINAL (EX: "X")
 - Which means X goes to nothing AKA $X = \lambda$
 - 2. Append X to all N right hand sides.
 - 3. Replace "Lefty Part" (N = N) with (X =)

- so
$$E = E -> X =$$

GE:

$$E = E + T | E - T | T$$

$$T = T * F | T / F | F$$

$$Q = \lambda$$

$$R = \lambda$$

$$T = T * F R$$

 $T = T / F R$

$$E = TQ$$

$$Q = + T Q$$
$$Q = - T Q$$

GE2:

$$E = TQ$$

$$Q = + TQ | - TQ | \lambda$$

$$T = F R$$

$$R = *FR|/FR|\lambda$$

$$L(GE2) == L(GE)$$

Next Chapter: 4.5.2

September 18, 2018

Disappearing Non-T's

Direct Epsilon Rule: $N = \lambda$ <- 0th step

Indirect Epsilon Rule: N = AB | fg

$$A = \lambda$$
 <- 0th step

$$B = C \mid h$$

$$C = \lambda$$
 <- 0th step

Consult Further (CF) Fig 4.7, p 129

ALT: KEY: Bottom Up

ALGO - Direct Epsilon, First

1 Step Indirect, Next

2 Step ,

ETC

Disappearing Set of Non-Ts:

```
"Dirty Bit"
                                                                                  Simple Rules:
                                                                                         (N, -) < - go to DS
                                                                                         (N, AB)
                                                                                         (N, fg) <- RHS, only Terms
                                                                                         (A, -) < - go to DS
                                   Step:
                                                                                         (B,C)
                                                                                         (B,h) <- Take out
                                         0: (N, A, C) -> Disappearing Set
                                                                                         (C,-) < - go to DS
                                                 - Look at right hand side for N, A, C and eliminate
Setup:
                                                 - Red = take out based on NAC
       DS < - Empty
       SR < - All Simple Rules
                                                 - for (B,C), right hand side became empty so add B
       Dirty = True;
                                          1: (N, A, C, B) -> DS
       while (Dirty)
       { // One Step
                                               Point:
              Dirty = False
                                                      Add direct Epsilon Rule
              For each Pair in SR
                                                      For each indirect
                     RHS = Pair.RHS
                                                      Disappearing Non-T:
                     For each N,A,C in DS
                                                      Simplify Table Build
                            RHS -= N,A,C
                     IF RHS is Empty
                            DS += Pair.LHS
                            Dirty = True
       }
             First Sets:

    Let RHS
```

- Look at L(RHS) RHS = "Reduced Grammar"
 - Set of all Terms that start a sentence in L(RHS)

$$F(\lambda) = \{ \}$$
 $F(h) = \{ h \}$
 $F(fg) = \{ f \}$
 $F(C) = \{ \}$
Union $F(C=RHS)$
 $F(AB) = A = F(\lambda) = \{ \}$

September 20, 2018

No Class

September 25, 2018

Exam Review:

NOX (not in exam): MINI - SWE Rules, PST

In exam:

- Treewalking
 - · not just binary tree
- Spiderweb Diagram

EX:

- What is it?
- What are the parts?
- What are the links?
 - · Leads to glossary terms
- Front-End
- · Back-End

What Parts?

Glossary Items:

- Bytecode
- (PST) = parse tree
 - non standard, but mirrors AST
- AST = abstract syntax tree

AST vs PST

• PST = every node and its kids are

- Non terminal = shows on left and right side
- Terminal doesn't expanse so it on only right
- AST = contains only Terminal symbol

Why AST?

- Twice as many nodes
- Messing with tree, mom and kids in PST will change
- LEXER
- Scanner
- Tokens
- ASM
 - Assembly language
- CFG
- Context Free Grammar
- IR
- Intermediate Representation
 - Source code is NOT IR
 - PST and AST are IR
 - Code coming out are NOT IR
- 3AC
- 3 Address Code
- Semantic Analysis
 - Checking on meaning
 - Making well form sentences with reasonable meaning

EX: The Bread ate the cat: Bad

The Mouse ate the bread: good

Syntax Analysis

- Check on Sentence Form by Grammar (part of speech)
- Glue words together to form proper sentence
- Well form coded
 - Ex: a statements, assignment, etc

The Bread ate the cat: works here

- Since Semantic will check meaning

- Lexical Analysis
 - Check if word exist in Dictionary

IE: Is word in "Lexicon"

- Glueing letters together to form word
- Deals with stuff from below the level of words
 - EX: words are "+=" which are tokens

- REGEX

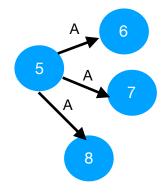
- · What is t?
- What are the Operations?
- · What are their actions?
- What are legal tokens/words in L(R)
 - L(R) = Language of Regex

- DFA

- · What is it?
- What Parts?
- SS,(AS) = Start state, Accepted State
- L(G) = language of grammar
- State transition
 - TABLE (Matrix)
 - Diagram (Graph)

• Convert from Diagram to Table?

- NFA
- · What is it?
- · How to tell if NFA vs DFA?
 - Choice move?



- Epsilon move λ
- Extra Column in table for λ
- Convert NFA to DFA
 - Know how
 - Path graph + fill in
 - All subset of NFA states
 - Start with DFA SS. and use Reachability (row by row)
 - Epsilon Closure
 - CANALS
 - WETNESS
 - HILL TROLLS

Glossary Items:

• REGEX

Recognized

• DFA

Accepted

FSM

- Recognized vs Accepted = SAME

- NFA
- EPS Closure

- ·SS
- Why bother with NFA?
 - REGEX operations give NFA

- History
 - 1957 Fortran Math Equation
 - 1958 LISP Lambda Calc
 - 1960 ALGOL Fortran-killer
 - 1960 COBOL Don't need Programmers
- Arithmetic Expression Grammar
 - · How to use it to build
 - A PST from an input Expression

Recalls:

PST mom + kids

GMR: LHS + RHS

Glossary:

- LHS RHS
 - L_1 = Left-To-Right Scan of Input Tokens
 - L_2 = Left-Most Derivation
 - R_2 = Right-Most Derivation

EX:

a b X c F a Y Z p Q a - Cap = Non Terminal

- LL expands the Capitalized Letter from left to right
- RR expands the Capitalized Letter from right to left

- Recursive Descent Parser
 - · What is it?
 - How to build (given GMR)
 - It is LL (Left Recursion)
 - Mutual Function Call Recursion
 - A calls B and B calls A (Has to be a loop)
 - PROS
 - Rewind the input
 - Real simple to build the functions
 - CONS
 - Checking all possible Derivations
 - Could take a long time because it tries and fail to check
 - Very SLOW
- LL Parse Machine
 - · What is it?
 - · What parts?
 - Machines
 - Tables
 - · What is it?
 - Parts?
 - Row Headers
 - Has LHS Symbol
 - Column Headers
 - Has Event/Terminal Symbol
 - Cells
 - One Simple Rules in a Cell

- LHS is Row headers
- How does it index?
 - (LHS,Token) = (Row, Column)
- Runtime Stack
- Any LL parser can't handle Left Recursion
- Left Recursion in a Simple Rule
 - · What is it?
 - A = A ...
 - Convert Combo Rules to Simple Rules

Glossary:

- LRE (Left-Recursion Elimination)
 - Removes Left Recursion in Grammar
- Disappearing Non-Terminals
 - Direct (easy)
 - Indirect
 - · How to find them all

Glossary:

- Terminal Symbol
- Non-Terminal Symbol

What is a Epsilon Rule?

- Rule where Terminal goes to nothing

September 27, 2018

MIDTERM

October 2, 2018

GE2: (LRE'd)
$$E = {}^{1}TQ$$

$$Q = {}^{2}+TQ | {}^{3}-TQ | {}^{4}esp$$

$$T = {}^{5}FR < - IF "F" has an esp, then there is a ghost rule for T goes to R$$

$$R = {}^{6}*FR | {}^{7}\div FR | {}^{8}esp$$

$$F = {}^{9}i | {}^{10}k | {}^{11}("E")"$$

* Build First Step, Each simple rule (RHS)

LL Table

only terminal ->	i	k	+	-	*	÷	()	\$ (EOF)	T (F,i) E	i
E											
Q										\$	\$
Т										stack	input stream
R											
F	R#9 or F=i										
			E/D#6							•	

$$----> F(R#9) = \{i\}$$

$$L(F=i \& GE2) = \{"i"\}$$

$$F(f=i) = \{i\} \qquad F = First Set \qquad f=i = GE2 Non-T$$

$$F(\#9) = \{i\}$$

$$F(\#10) = \{k\}$$

$$F(\#11) = \{'(') < -- \text{ every thing has to start with (for rule 11)}$$

$$F(\#6) = \{*\}$$

$$F(\#7) = \{\div\}$$

$$F(\#2) = \{+\}$$

$$F(\#3) = \{-\}$$

$$F(\#4) = \{ \} < -\text{ eps goes to nothing (eps } = \lambda)$$

$$F(\#8) = \{ \} < -\lambda$$

$$F(\#5) = \{F(f)\} = \{i,k,'(')\}$$

$$-F(f) = F(\#9) + F(\#10) + F(\#11) = \{i,k,'(')\}$$

$$F(\#1) = \{F(T)\} = \{i,k,'(')\}$$

$$-F(T) = \{F(\#5)\} = \{i,k,'(')\}$$

New Table: to get rule, look at equation and see what rule applies

- EX:
$$Q = \text{rule } 2 \mid 3 \mid 4 \longrightarrow \text{we we put } 2 \text{ and } 3 \text{ under } (Q, +) \& (Q, -)$$

only terminal	i	k	+	•	*	÷	()	\$ (EOF)
E	1	1					1		
Q			2	3					
Т	5	5					5		
R					6	7			
F	9						11		

First Set Algorithm:

- 1. If RHS starts with sym X, Add F(x) to F(RHS)
- 2. If X has an esp rule A = XYZ, then Add F(A=YZ) —> Ghost Rule
 And keep going with Y, etc
- 3. If like A = ... Y & Y has eps rule

-> Ignore it (Handle in Follow Set)

Continuing from Set of Rules

$$W(E) = \{\$, ')'\}$$

$$W(Q) = \{W(E), W(Q), W(Q)\} < - \text{Recursion } W(Q)$$

$$W(E) = \text{Rule 1}$$

$$W(Q) = \{\$, ')'\}$$

$$W(Q) = \text{Rule 2}$$

$$W(T) = \{F(Q), W(E), F(Q), W(Q), F(Q), W(Q)\}$$

$$F(Q) \& W(E) = R#1$$

$$F(Q) \& W(Q) = R#2$$

$$F(Q) \& W(Q) = R#3$$

$$= \{+, -, \$, ')'\}$$

$$W(R) = \{W(T), W(R), W(R)\}$$

$$W(R) = \{+, -, \$, ')'\}$$

$$W(R) = BUT WAIT!!!$$

$$Done for 2 reasons:$$

$$1. No F = \lambda \text{ Rule}$$

2. No Further worry about other λ Rules

LL TABLE:

only terminal	i	k	+	•	*	÷	()	\$ (EOF)
E	1	1					1		
Q			2	3				4	4
Т	5	5					5		
R			8	8	6	7		8	8
F	9	10					11		

- NO two rules in a single cell
 - It means Grammar Bug (Or your bug)

October 4, 2018

LL Table

Cell Conflict:

Left Factoring: (Direct)

$$S = {}^{1} i eq T$$
 $F(S) = { i }$ $T = {}^{3} inp | {}^{4} E$ $F(\# 4) = F(E) = { i,k,'(') }$

LL Table	 i	 iNP	K	('
S	1			
Т	4	3	4	4

```
F(E) = \{i,k,'(') \text{ from previous set } E
                    • inp = INPUT
                    • E = expression
                    • eq = equals
                          - SO S = i eq (inp | E)
                          <sup>3</sup> = Input Statement
                          <sup>4</sup> = Assignment Statement
LL MECH:
      - Setup: Push $, Symbols
             // Stack Element is a Symbol
      While STACK
             Let TOP, FRONT.....
             M1: IF TOP == FRONT
                          IF $ == TOP, Success (We're done)
                           ELSE, POP & Advance the STACK
             M2E: (Error)
                    IF TOP is a TERM, ERROR (We're done)
                    // TOP is a non-TERM
             Let Cell == LLT[TOP _{ID}, FRONT _{ID}] LLT = LL Table
             M3E: IF Cell is Empty, ERROR
             M4: POP //No Advance
                    PUSH (Reversed(RHS))
             MP: Print TOP, FRONT, STACK
In Lab:
```

Stack: : \$ E : \$ Q T

X + Y \$

 $i_x + i_y$ \$

E =
1
 TQ
Q = 2 +TQ | 3 -TQ | 4 λ
T = ${}^{5}FR$
R = 6 *FR | 7 ÷FR | 8 λ
F = 9 i | 10 k | 11 '(' E ')'

LL Table	i	k	+	_	×	÷	()	\$
Е	1	1					1		
Q			2	3				4	4
T	5	5					5		
R			8	8	6	7		8	8
F	9	10					11		

I GAVE UP!!!

October 9, 2018

October 11, 2018
