

MATH 3080 Lab Project 6

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- [Problem 1](#)

Remember: I expect to see commentary either in the text, in the code with comments created using `#`, or (preferably) both! **Failing to do so may result in lost points!**

Problem 1

As part of a study of its sheet metal assembly process, a major automobile manufacturer uses sensors that record the deviation from the nominal thickness (millimeters) at 4 locations on a car. Data on 30 cars are given in the file `car_body.csv` (Source: Data Courtesy of Darek Ceglarek).

STEP 1 (Data Preparation) Download the data file `car_body.csv` from our course webpage. Read the file into R, and reshape the data by using `stack()` function. You may use the variable names 'V1, V2, V3, V4' as treatment names. (Hint: see codes of previous lab.)

STEP 2 (ANOVA) Perform an ANOVA to test for the null hypothesis $H_0: \mu_1 = \mu_2 = \mu_3 = \mu_4$ vs. $H_A: H_0$ is not true at $(\alpha=0.05)$. Check all the appropriate assumptions.

STEP 3 (Tukey's method) Use Tukey's method to find which individual locations seem to show a cause for concern.

```
# Your code here
```

```
mydata = read.csv("car_body.csv", header = TRUE)
mydata
```

```
##      V1      V2      V3      V4
## 1 -0.12  0.36  0.40  0.25
## 2 -0.60 -0.35  0.04 -0.28
## 3 -0.13  0.05  0.84  0.61
## 4 -0.46 -0.37  0.30  0.00
## 5 -0.46 -0.24  0.37  0.13
## 6 -0.46 -0.16  0.07  0.10
## 7 -0.46 -0.24  0.13  0.02
## 8 -0.13  0.05 -0.01  0.09
## 9 -0.31 -0.16 -0.20  0.23
## 10 -0.37 -0.24  0.37  0.21
## 11 -1.08 -0.83 -0.81  0.05
## 12 -0.42 -0.30  0.37 -0.58
## 13 -0.31  0.10 -0.24  0.24
## 14 -0.14  0.06  0.18 -0.50
## 15 -0.61 -0.35 -0.24  0.75
## 16 -0.61 -0.30 -0.20 -0.21
## 17 -0.84 -0.35 -0.14 -0.22
## 18 -0.96 -0.85  0.19 -0.18
## 19 -0.90 -0.34 -0.78 -0.15
## 20 -0.46  0.36  0.24 -0.58
## 21 -0.90 -0.59  0.13  0.13
## 22 -0.61 -0.50 -0.34 -0.58
## 23 -0.61 -0.20 -0.58 -0.20
## 24 -0.46 -0.30 -0.10 -0.10
## 25 -0.60 -0.35 -0.45  0.37
## 26 -0.60 -0.36 -0.34 -0.11
## 27 -0.31  0.35 -0.45 -0.10
## 28 -0.60 -0.25 -0.42  0.28
## 29 -0.31  0.25 -0.34 -0.24
## 30 -0.36 -0.16  0.15 -0.38
```

```
stack_all <- stack(mydata)
stack_all
```

```
##      values ind
## 1    -0.12  V1
## 2    -0.60  V1
## 3    -0.13  V1
## 4    -0.46  V1
## 5     0.36  V2
```

## 5	-0.46	V1
## 6	-0.46	V1
## 7	-0.46	V1
## 8	-0.13	V1
## 9	-0.31	V1
## 10	-0.37	V1
## 11	-1.08	V1
## 12	-0.42	V1
## 13	-0.31	V1
## 14	-0.14	V1
## 15	-0.61	V1
## 16	-0.61	V1
## 17	-0.84	V1
## 18	-0.96	V1
## 19	-0.90	V1
## 20	-0.46	V1
## 21	-0.90	V1
## 22	-0.61	V1
## 23	-0.61	V1
## 24	-0.46	V1
## 25	-0.60	V1
## 26	-0.60	V1
## 27	-0.31	V1
## 28	-0.60	V1
## 29	-0.31	V1
## 30	-0.36	V1
## 31	0.36	V2
## 32	-0.35	V2
## 33	0.05	V2
## 34	-0.37	V2
## 35	-0.24	V2
## 36	-0.16	V2
## 37	-0.24	V2
## 38	0.05	V2
## 39	-0.16	V2
## 40	-0.24	V2
## 41	-0.83	V2
## 42	-0.30	V2
## 43	0.10	V2
## 44	0.06	V2
## 45	-0.35	V2
## 46	-0.30	V2
## 47	-0.35	V2
## 48	-0.85	V2
## 49	-0.34	V2
## 50	0.36	V2
## 51	-0.59	V2
## 52	-0.50	V2
## 53	-0.20	V2
## 54	-0.30	V2
## 55	-0.35	V2
## 56	-0.36	V2
## 57	0.35	V2
## 58	-0.25	V2
## 59	0.25	V2
## 60	-0.16	V2
## 61	0.40	V3
## 62	0.04	V3
## 63	0.84	V3
## 64	0.30	V3
## 65	0.37	V3
## 66	0.07	V3
## 67	0.13	V3
## 68	-0.01	V3
## 69	-0.20	V3
## 70	0.37	V3
## 71	-0.81	V3
## 72	0.37	V3
## 73	-0.24	V3
## 74	0.18	V3
## 75	-0.24	V3
## 76	-0.20	V3
## 77	-0.14	V3

```
## 78    0.19 V3
## 79   -0.78 V3
## 80    0.24 V3
## 81    0.13 V3
## 82   -0.34 V3
## 83   -0.58 V3
## 84   -0.10 V3
## 85   -0.45 V3
## 86   -0.34 V3
## 87   -0.45 V3
## 88   -0.42 V3
## 89   -0.34 V3
## 90    0.15 V3
## 91    0.25 V4
## 92   -0.28 V4
## 93    0.61 V4
## 94    0.00 V4
## 95    0.13 V4
## 96    0.10 V4
## 97    0.02 V4
## 98    0.09 V4
## 99    0.23 V4
## 100   0.21 V4
## 101   0.05 V4
## 102  -0.58 V4
## 103   0.24 V4
## 104  -0.50 V4
## 105   0.75 V4
## 106  -0.21 V4
## 107  -0.22 V4
## 108  -0.18 V4
## 109  -0.15 V4
## 110  -0.58 V4
## 111   0.13 V4
## 112  -0.58 V4
## 113  -0.20 V4
## 114  -0.10 V4
## 115   0.37 V4
## 116  -0.11 V4
## 117  -0.10 V4
## 118   0.28 V4
## 119  -0.24 V4
## 120  -0.38 V4
```

```
names(stack_all) <- c("body", "car")
stack_all
```

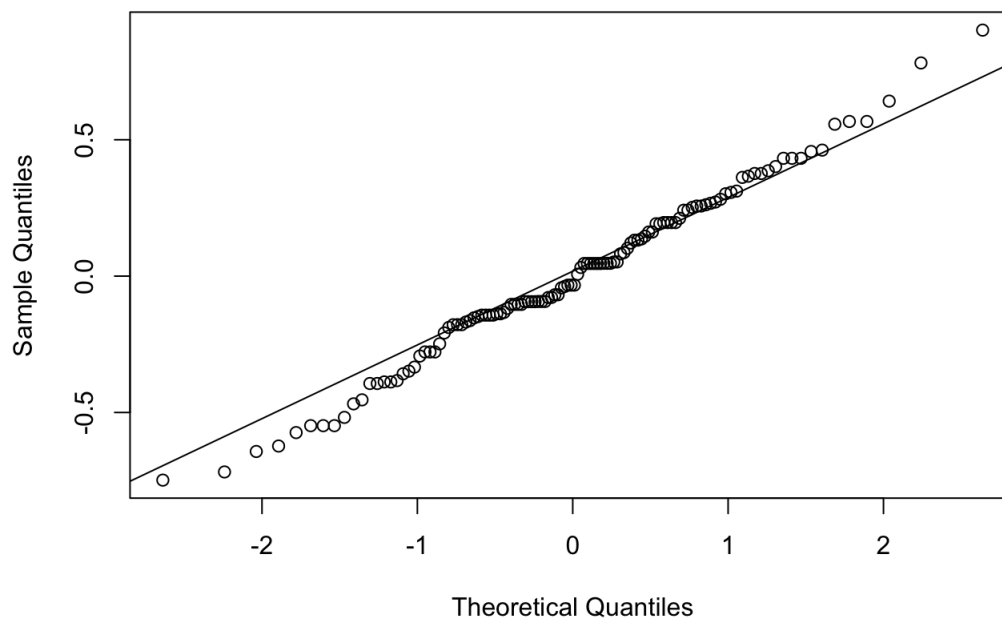
```
##      body car
## 1   -0.12 V1
## 2   -0.60 V1
## 3   -0.13 V1
## 4   -0.46 V1
## 5   -0.46 V1
## 6   -0.46 V1
## 7   -0.46 V1
## 8   -0.13 V1
## 9   -0.31 V1
## 10  -0.37 V1
## 11  -1.08 V1
## 12  -0.42 V1
## 13  -0.31 V1
## 14  -0.14 V1
## 15  -0.61 V1
## 16  -0.61 V1
## 17  -0.84 V1
## 18  -0.96 V1
## 19  -0.90 V1
## 20  -0.46 V1
## 21  -0.90 V1
## 22  -0.61 V1
## 23  -0.61 V1
## 24  -0.46 V1
```

##	24	-0.46	V1
##	25	-0.60	V1
##	26	-0.60	V1
##	27	-0.31	V1
##	28	-0.60	V1
##	29	-0.31	V1
##	30	-0.36	V1
##	31	0.36	V2
##	32	-0.35	V2
##	33	0.05	V2
##	34	-0.37	V2
##	35	-0.24	V2
##	36	-0.16	V2
##	37	-0.24	V2
##	38	0.05	V2
##	39	-0.16	V2
##	40	-0.24	V2
##	41	-0.83	V2
##	42	-0.30	V2
##	43	0.10	V2
##	44	0.06	V2
##	45	-0.35	V2
##	46	-0.30	V2
##	47	-0.35	V2
##	48	-0.85	V2
##	49	-0.34	V2
##	50	0.36	V2
##	51	-0.59	V2
##	52	-0.50	V2
##	53	-0.20	V2
##	54	-0.30	V2
##	55	-0.35	V2
##	56	-0.36	V2
##	57	0.35	V2
##	58	-0.25	V2
##	59	0.25	V2
##	60	-0.16	V2
##	61	0.40	V3
##	62	0.04	V3
##	63	0.84	V3
##	64	0.30	V3
##	65	0.37	V3
##	66	0.07	V3
##	67	0.13	V3
##	68	-0.01	V3
##	69	-0.20	V3
##	70	0.37	V3
##	71	-0.81	V3
##	72	0.37	V3
##	73	-0.24	V3
##	74	0.18	V3
##	75	-0.24	V3
##	76	-0.20	V3
##	77	-0.14	V3
##	78	0.19	V3
##	79	-0.78	V3
##	80	0.24	V3
##	81	0.13	V3
##	82	-0.34	V3
##	83	-0.58	V3
##	84	-0.10	V3
##	85	-0.45	V3
##	86	-0.34	V3
##	87	-0.45	V3
##	88	-0.42	V3
##	89	-0.34	V3
##	90	0.15	V3
##	91	0.25	V4
##	92	-0.28	V4
##	93	0.61	V4
##	94	0.00	V4
##	95	0.13	V4
##	96	0.10	V4

```
## 97 0.02 V4
## 98 0.09 V4
## 99 0.23 V4
## 100 0.21 V4
## 101 0.05 V4
## 102 -0.58 V4
## 103 0.24 V4
## 104 -0.50 V4
## 105 0.75 V4
## 106 -0.21 V4
## 107 -0.22 V4
## 108 -0.18 V4
## 109 -0.15 V4
## 110 -0.58 V4
## 111 0.13 V4
## 112 -0.58 V4
## 113 -0.20 V4
## 114 -0.10 V4
## 115 0.37 V4
## 116 -0.11 V4
## 117 -0.10 V4
## 118 0.28 V4
## 119 -0.24 V4
## 120 -0.38 V4
```

```
# STEP 2 (ANOVA) Perform an ANOVA to test for the null hypothesis Ho:
# mu1=mu2=mu3=mu4 vs. Ha: Ho is not true at alpha=0.05. Check all the
# appropriate assumptions.
attach(mydata)
dev = c(V1 - mean(V1), V2 - mean(V2), V3 - mean(V3), V4 - mean(V4))
dev = sort(dev)
qqnorm(dev) # a built-in function to generate qq-plots
qqline(dev) # add a straight line to the qq-plots
```

Normal Q-Q Plot



```
shapiro.test(V1)
```

```
##
##  Shapiro-Wilk normality test
##
## data:  V1
## W = 0.94164, p-value = 0.1007
```

```
shapiro.test(V2) ## we don't sure how to determine this group if the Normality by step by step test.
```

```
##
## Shapiro-Wilk normality test
##
## data: V2
## W = 0.93309, p-value = 0.05934
```

```
shapiro.test(V3)
```

```
##
## Shapiro-Wilk normality test
##
## data: V3
## W = 0.97856, p-value = 0.7862
```

```
shapiro.test(V4)
```

```
##
## Shapiro-Wilk normality test
##
## data: V4
## W = 0.97124, p-value = 0.5737
```

```
# it is Normality. If it is not normality, we can not to do anova
```

```
detach(mydata)
bartlett.test(body ~ car, data = stack_all)
```

```
##
## Bartlett test of homogeneity of variances
##
## data: body by car
## Bartlett's K-squared = 5.0695, df = 3, p-value = 0.1668
```

```
# P-value is larger than  $\alpha=0.05$ , so the null that the variances in each of
# the groups (samples) are the same
```

```
# if the variances are the same, we can use anova to analysis the data.
# Then, we can use Tukey for more detail.
```

```
anova <- aov(body ~ car, data = stack_all)
summary(anova)
```

```
##              Df Sum Sq Mean Sq F value    Pr(>F)
## car           3  4.238   1.4126    13.84 8.94e-08 ***
## Residuals    116 11.841   0.1021
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
# The p-value is less than  $\alpha=0.05$ , so we reject  $H_0$ .
```

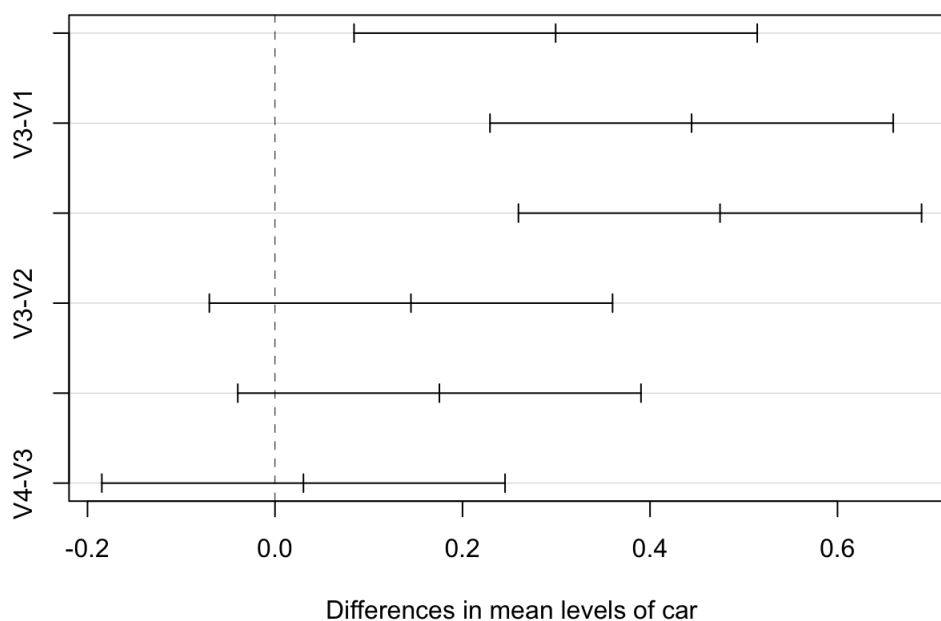
```
# STEP 3 (Tukey's method) Use Tukey's method to find which individual
# locations seem to show a cause for concern
```

```
tk <- TukeyHSD(anova, ordered = T)
tk
```

```
## Tukey multiple comparisons of means
## 95% family-wise confidence level
## factor levels have been ordered
##
## Fit: aov(formula = body ~ car, data = stack_all)
##
## $car
##          diff          lwr          upr      p adj
## V2-V1 0.29933333 0.08429847 0.5143682 0.0023727
## V3-V1 0.44433333 0.22929847 0.6593682 0.0000023
## V4-V1 0.47466667 0.25963180 0.6897015 0.0000004
## V3-V2 0.14500000 -0.07003486 0.3600349 0.2990726
## V4-V2 0.17533333 -0.03970153 0.3903682 0.1511715
## V4-V3 0.03033333 -0.18470153 0.2453682 0.9829339
```

```
plot(tk)
```

95% family-wise confidence level



```
# V1 ~ v2, v3 and v4 are significant difference. V2 ~ v3 and v4 are
# significant. V3 ~ v4 is significant.
```