



Aaron P. Mills

Z-23547104

Dr. Ghoraani

CAP 4613

Intro to Deep Learning

Assignment 2

6 February 2022

<https://colab.research.google.com/drive/1FfbrSe5vSjtYv6rie2zYQanqzlvvS12D?usp=sharing>

Note: The code PDF is below, after the handwork solutions.

Problem 1)

a) Answer: ↓

	Fraudulent	Non-Fraudulent
Fraudulent	19	6
Non-Fraudulent	6	9

b) Answer: 70%

$$\text{Model Accuracy} = \frac{TP+TN}{\# \text{ of samples}} = \frac{19+9}{19+6+6+9} = \frac{28}{40} = 0.7 = 70\%$$

c) Answer: 76%

$$\text{Sensitivity} = \frac{TP}{TP+FN} = \frac{19}{19+6} = \frac{19}{25} = 0.76 = 76\%$$

d) Answer: 60%

$$\text{Specificity} = \frac{TN}{TN+FP} = \frac{9}{9+6} = \frac{9}{15} = 0.6 = 60\%$$

e) Answer: 76%

$$F1 \text{ Score} = 2 * \frac{\text{sensitivity} * \text{precision}}{\text{sensitivity} + \text{precision}} = 2 * \frac{0.76 * 0.76}{0.76 + 0.76} = 0.76 = 76\%$$

$$\text{Precision} = \frac{TP}{TP+FP} = \frac{19}{19+6} = \frac{19}{25} = 0.76 = 76\%$$

f) Answer: Recall = 76%, precision = 76%

$$\text{Recall} = \text{sensitivity} = \frac{TP}{TP+FN} = \frac{19}{19+6} = \frac{19}{25} = 0.76 = 76\%$$

$$\text{Precision} = \frac{TP}{TP+FP} = \frac{19}{19+6} = \frac{19}{25} = 0.76 = 76\%$$

## Problem 2)

a) Answer: ↓

	Class 1	Class 0
Class 1	7	2
Class 0	3	5

b) Answer: *Accuracy*  $\approx 70.59\%$ , *sensitivity*  $= 77.78\%$ , *specificity*  $\approx 62.5\%$

$$\text{Accuracy} = \frac{\sum \text{diagonal}}{\# \text{ of samples}} = \frac{TP+TN}{TP+TN+FP+FN} = \frac{7+5}{7+5+3+2} = \frac{12}{17} \approx 70.59\%$$

$$\text{Sensitivity} = \frac{TP}{TP+FN} = \frac{7}{7+2} = \frac{7}{9} \approx 77.78\%$$

$$\text{Specificity} = \frac{TN}{TN+FP} = \frac{5}{5+3} = \frac{5}{8} = 62.50\%$$

c) Answer:  $w_0 = -1$ ,  $w_1 = \frac{2}{3}$ ,  $w_2 = \frac{1}{3}$

$$v = w_1 x_1 + w_2 x_2 + w_0 = 0$$

$$0 = w_1(1.5) + w_2(0) + w_0 \quad \bullet \text{ Point 1: (1.5,0);}$$

$$0 = w_1(0) + w_2(3) + w_0 \quad \bullet \text{ Point 2: (0,3)}$$

$$0 = w_1(1.5) - 1 \rightarrow 1 = w_1(1.5) \rightarrow w_1 = \frac{1}{1.5} = \frac{2}{3} \quad \bullet \text{ let } w_0 = -1$$

$$0 = w_2(3) - 1 \rightarrow 1 = w_2(3) \rightarrow w_2 = \frac{1}{3} \quad \bullet \uparrow$$

d) Answer: New Sample 1:  $v = \frac{2}{3}$ ,  $y = 1$ , *Class Label* = *Class 1*;

New Sample 2:  $v = -\frac{7}{3}$ ,  $y = 0$ , *Class Label* = *Class 0*

$$v = \frac{2}{3}x_1 + \frac{1}{3}x_2 - 1 \quad \bullet v \text{ local field found in part (c)}$$

$$S_{i+1} \cdot v = \frac{2}{3}(2) + \frac{1}{3}(-1) - 1 = \frac{2}{3} \approx 0.67 \quad \bullet \text{ new sample 1's } v$$

$$S_{i+2} \cdot v = \frac{2}{3}(-0.5) + \frac{1}{3}(0.5) - 1 = -\frac{7}{6} \approx -1.17 \quad \bullet \text{ new sample 2's } v$$

$$y = \begin{cases} 1 & \text{if } v \geq 0 \\ 0 & \text{if } v < 0 \end{cases}$$

• based on



$$S_{i+1} \cdot y = 1$$

$$\bullet S_{i+1} \cdot v = \frac{2}{3} \geq 0 \rightarrow y = 1$$

$$S_{i+2} \cdot y = 0$$

$$\bullet S_{i+2} \cdot v = -\frac{7}{6} < 0 \rightarrow y = 0$$

Predicted Classification Label = {Class 1} if  $y == 1$ , else {Class 0} if  $y == 0$

$$S_{i+1} \cdot \text{Classification Label} = \text{Class 1}$$

$$\bullet y = 1$$

$$S_{i+2} \cdot \text{Classification Label} = \text{Class 0}$$

$$\bullet y = 0$$



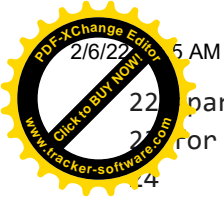
Aaron P. Mills / Z-23547104 / Dr. Ghoraani

Intro to Deep Learning / CAP 4613 / Assignment 2 / 6 February 2022

<https://colab.research.google.com/drive/1FfbrSe5vSjtYv6rie2zYQanqzIvyS12D?usp=sharing>

```
1 # Aaron P. Mills / Z-23547104 /
2 # Dr. Ghoraani
3 # Intro to Deep Learning / CAP 4613 /
4 # Assignment 2 / 6 February 2022
5 # Discription: In this assignment, I collect data, organize it into sets, display random s
6 # https://colab.research.google.com/drive/1FfbrSe5vSjtYv6rie2zYQanqzIvyS12D?usp=sharing
7 #####
8 #header block - includes heading, imports, functions, classes, ect.
9 import math as mth
10 import numpy as np
11 import matplotlib.pyplot as plt
12 from keras.datasets import mnist
13
14 #Problem 3)
15 #part b) write function which takes set of (image & label) as input and displays a figure
16 def plot_num(imgs=[0],labels=[0]): #takes set of images & corresponding label
17     plt.figure() #figure is the box that holds images, so it be
18     for i in range( len(imgs) ): #to print all images
19         plt.subplot(2,5,i+1) #2 rows, 5 cols, i+1 position in grid matrix
20         plt.imshow(imgs[i],cmap='gray') #needed for each image display
21         plt.title('Label: '+ str(labels[i]))#use corresponding label in tittle name
22     plt.show() #display entire figure

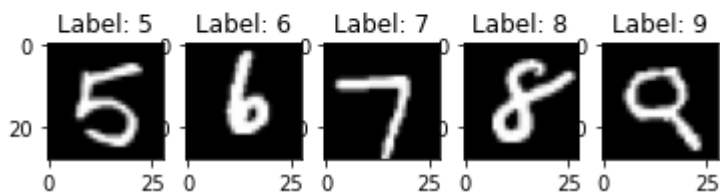
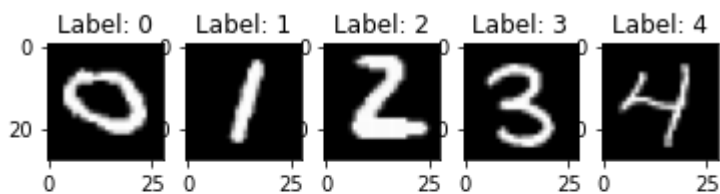
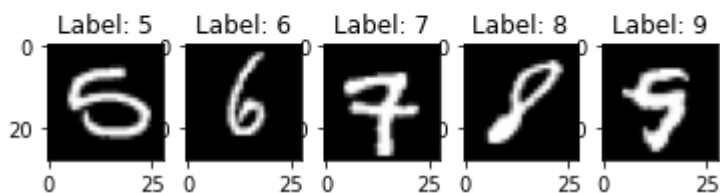
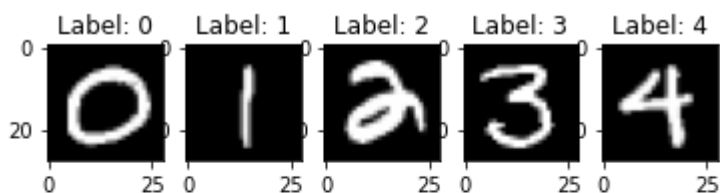
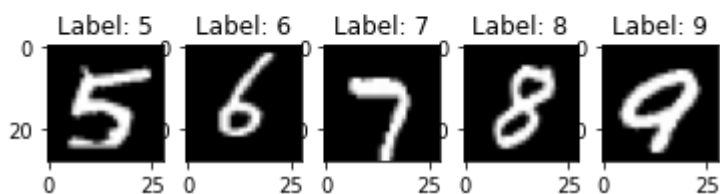
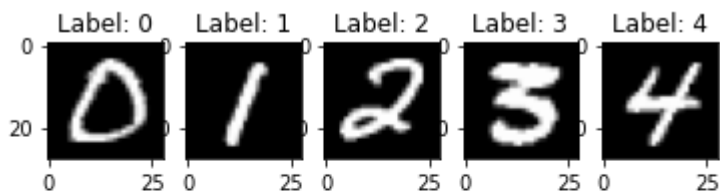
1 #part a) obtaining, splitting, and printing data from http://yann.lecun.com/exdb/mnist/
2 (x_train_all,y_train_all),(x_test_all,y_test_all) = mnist.load_data()
3 print(f"There exist {x_train_all.shape[0]} images of size {x_train_all.shape[1]}x{x_train_
4 print(f"There exist {x_test_all.shape[0]} images of size {x_test_all.shape[1]}x{x_test_all
5
6 #part b) write function which takes set of (image & label) as input and displays a figure
7 #NOTE: part b) may be found in the header (first code) block, because it is a function
8
9 #testing plot_num; this is NOT a requirement, so I commented it out
10 # print("Testing plot_num() function*****")
11 # xlist = [] #list for images
12 # ylist = [] #list for labels
13 # for digit in range(10): #10 images from 0-9
14 #     x_train_d = x_train_all[y_train_all==digit,:,:] #set of imgs with label==digit
15 #     x_train_i = x_train_d[0,:,:] #first img with label==digit
16 #     y_train_d = y_train_all[y_train_all==digit] #corresponding set of labels to img;
17 #     y_train_i = y_train_d[0] #corresponding label to img; first 1
18 #     xlist.append(x_train_i) #add to list of imgs
19 #     ylist.append(y_train_i) #add to corresponding list of labels
20 # plot_num(xlist,ylist) #plot all imgs from 0-9
21
```



```
22 part c) create loop to call plot function from part b) for 3 times, and ensure each digit is represented
23 for i in range(3):
24     img_list = []
25     label_list = []
26     for digit in range(10):
27         x_train_d = x_train_all[y_train_all==digit] #matrix of ONLY imgs that are of c
28         y_train_d = y_train_all[y_train_all==digit] #corresponding label for digits
29         num_imgs_d = x_train_d.shape[0] #get number of image of digit
30         train_ind_d = np.arange(0,num_imgs_d) #use that number in creating indic
31         train_ind_ds = np.random.permutation(train_ind_d)#randomize the order of the indic
32         x_train_dshuffle = x_train_d[train_ind_ds,:,:] #shuffled data = original_data@[ra
33         y_train_dshuffle = y_train_d[train_ind_ds] #corresponding label for shuffled
34         ind_ds = np.random.randint(0,num_imgs_d) #randomized index for more randomi
35         x_train_dimg = x_train_dshuffle[ind_ds,:,:] #randomized img of digit = shuffle
36         y_train_dimg = y_train_dshuffle[ind_ds] #corresponding label for such imag
37         img_list.append(x_train_dimg) #add random img of digit to list
38         label_list.append(y_train_dimg) #and its label
39     plot_numb(img_list,label_list) #display each random img of all di
40
41 #part d) split the training data so that a random 20% is allocated to validation, while th
42 num_train_imgs = x_train_all.shape[0] #get number of training images
43 train_ind_all = np.arange(0,num_train_imgs) #get indices representing entire s
44 train_ind_all_s = np.random.permutation(train_ind_all) #randomized set indices
45 x_train_all_s = x_train_all[train_ind_all_s,:,:] #randomized_set = data@[randomized
46 y_train_all_s = y_train_all[train_ind_all_s] #^with corresponding labels
47
48 x_valid = x_train_all_s[0:int(0.20*num_train_imgs),:,:] #validity set is 20% of random set
49 y_valid = y_train_all_s[0:int(0.20*num_train_imgs)] #same for label
50 x_train = x_train_all_s[(int(0.20*num_train_imgs)):num_train_imgs,:,:] #training set is t
51 y_train = y_train_all_s[(int(0.20*num_train_imgs)):num_train_imgs] #same for label
52
53 print("|Number of Samples per Set|")
54 print(f"x_valid: {x_valid.shape[0]}\nty_valid: {y_valid.shape[0]}") #shape returns [ca
55 print(f"x_train: {x_train.shape[0]}\nty_train: {y_train.shape[0]}") #^
56 print(f"The validation set holds {x_valid.shape[0]} images, while training holds {x_train.
```

↳

Downloading data from <https://storage.googleapis.com/tensorflow/tf-keras-datasets/mnist/train-images-idx3-ubyte.gz>  
11493376/11490434 [=====] - 0s 0us/step  
11501568/11490434 [=====] - 0s 0us/step  
There exist 60000 images of size 28x28 in the training set.  
There exist 10000 images of size 28x28 in the testing set.



|Number of Samples per Set|

x\_valid: 12000 y\_valid: 12000

x\_train: 48000 y\_train: 48000

The validation set holds 12000 images, while training holds 48000