

## Problem Set 2

2.14 First of all, we need to merge-sort the array  $a1$  ( $O(n \log n)$ ) so as to group duplicates. Then we create another array  $a2$  to store the non-duplicates. Finally, we set up a loop:

```
for i = 1 to a1.length()  
  If  $a1[i] == a1[i+1]$   
    i++
```

copy  $a1[i]$  to  $a2$

return  $a2$ ;

2.15 In order to split the set into 3 subset without allocating new memory, we need two loops to sort the array. The first loop arranges all elements smaller than  $v$  at the front of the array. The second loop arranges all elements equal to  $v$  right behind the first subset. In this case, the remaining part of the array contains elements larger than  $v$ . In each loop, the functionalities of  $s$  and  $i$  are pretty much the same.  $s$  points to the latest position of the subset while  $i$  is used for iterating the whole loop to find the corresponding value.

An array  $t$  is given

```
Integer  $s = 1$  //used for swap elements  
for i = 1 to n  
  If  $t[i] < v$   
    swap  $t[s]$  and  $t[i]$   
  s++
```

for i = s to n //the second loop is used for arrange the elements equal to  $v$

```
  If  $t[i] == v$   
    swap  $t[s]$  and  $t[i]$   
  s++
```

3. Approach 1: Merge-sort the array first and the number at the  $n/2$  position is always the majority number because the list is guaranteed to have a number which appears more than  $n/2$  times in the list. In this case, the number indexed at  $n/2$  in a sorted list is always the majority number. And time complexity is  $O(n \log n)$ .

Approach 2: Creating two loops to count each number in the array and check if the count of each number is larger than  $n/2$ .

In this approach, the worst case is that the majority number is all positioned at the second half of the array. Therefore, the time complexity is  $O(n/2 * n) = O(n^2)$

To recap, the first approach is better since it got a lower time complexity.