

1) $I[\text{even}]$: beginning position of an interval $(i/2-1)$

$I[\text{odd}]$: ending

I is the set of intervals

$I[0]$ is the valid size of the memory of I .

$I[1]$ is the size of endpoints

$\text{indexB}, \text{indexE}$

bsearch_int64_t

if indexB is odd #, b is within the $\left\{ \frac{(\text{indexB}-1)}{2} \right\}^{\text{th}}$ interval

if indexB is even # & $b \in I$, b is within the $\left\{ \frac{(\text{indexB}-2)}{2} \right\}^{\text{th}}$ interval

else b is ~~not~~ out of any interval in I .

b, e inside some intervals in I

$$db = \begin{cases} \frac{\text{indexB}-1}{2} & \text{if indexB is odd.} \\ \frac{\text{indexB}-2}{2} & \text{if indexB is even.} \end{cases}$$

$$de = \begin{cases} \text{use indexE.} \end{cases}$$

$k = de - db.$

$bB - b - bE$ / $eB - e - eE$

~~$bB = I[db] + 2 * \text{indexB} + 2$~~ / ~~$eB = I[de] + 2 * \text{indexE} + 2$~~

~~$bE = I[db] + 2 * \text{indexB} + 3$~~ / ~~$eE = I[de] + 2 * \text{indexE} + 3$~~

Replace $\text{indexB}/\text{indexE}$ with db/de .

if $k = 0$, make sure that $*bB \leq b \leq *bE$

$*eB \leq e \leq *eE$ using assert.

else ~~$*bE = *eE$~~ $\text{tailSize} = \text{sizeI} - (de * 2 + 1)$

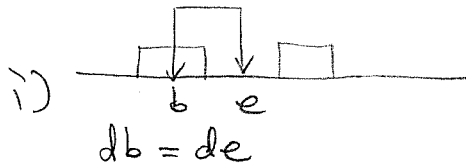
$\text{memmove}(bE, eE, \text{tailSize} * \text{sizeof}(\text{int64_t}))$

$I[1] -= k;$

after

②

II.



e is out of intervals.

even

$$de = \frac{(\text{index} E - 2)}{2}$$

~~$bB = I + 2 * \text{index} B + 2$~~

~~$bE = I + 2 * \text{index} B + 3$~~

~~$eE = I + 2 * \text{index} E + 3$~~

~~$eB = I + 2 * \text{index} E + 4$~~

if $2 * \text{index} E + 4 < \text{size} I + 2$,

else eB does not exist.

or $eB = \text{NULL}$

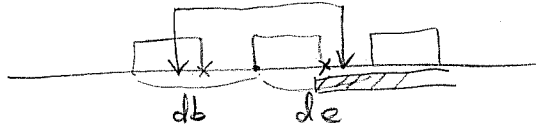
if $k=0$ if eB exists, $*bE = e$

Assert

$*bB \leq b \leq *bE$

$*eE < e < *eB$

if $k > 0$,



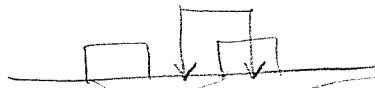
$\text{tailSize} = \text{size} I - (2 * de + 1)$

$\text{memmove}(bE, eE, \text{tailSize} * \text{sizeof}(\text{int64}_t))$

then $*bE = e$

$I[1] -- = k$

III.



~~$bE = I + 2 * \text{index} B + 1$~~

~~$bB = I + 2 * \text{index} B + 2$~~

~~$eB = I + 2 * \text{index} E + 2$~~

~~$eE = I + 2 * \text{index} E + 3$~~

if $k=0$, $*eB = b$

else, $\text{tailSize} = \text{size} I - (2 * de)$

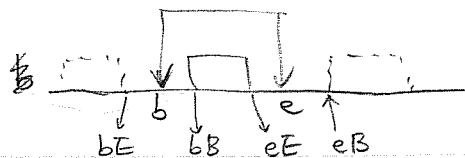
$\text{memmove}(bB, eB, \text{tailSize} * \text{sizeof}(\text{int64}_t))$

$I[1] -- = k$

if $2 * \text{index} B + 1 < 2$, $bE = \text{NULL}$

③

IV.



$$bE = I + 2 * indexB + 1 \text{ if } 2 * indexB + 1 > 2, \text{ otherwise NULL}$$

$$bB = I + 2 * indexB + 2$$

$$eE = I + 2 * indexE + 2$$

$$eB = I + 2 * indexE + 3 \text{ if } 2 * indexE + 3 < sizeI + 2, \text{ otherwise NULL}$$

compute db, de

$$k = de - db \quad \text{tailSize} = sizeI - (2 * de + 2)$$

if $k = 0$, memmove(eB, bB, tailSize * sizeof(int - 64 - t))

$$*bB = b$$

$$*eE = e$$

$$I[1] += 1.$$

if $k = 1$, $*bB = b$

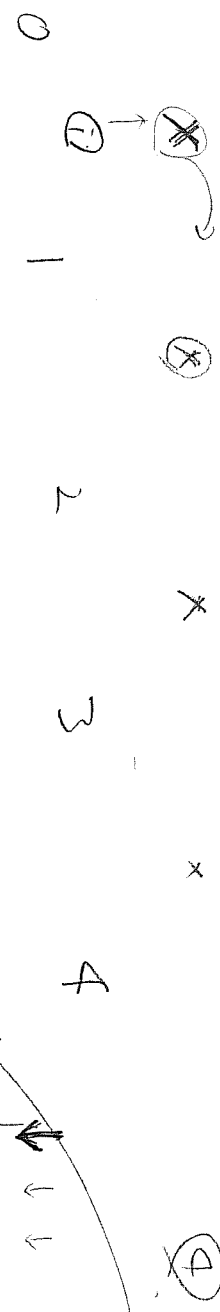
$$*eE = e$$

if $k > 1$, tailSize = sizeI - (2 * de + 1)

memmove($\begin{matrix} \text{bB} \\ \text{bB} + 1 \end{matrix}$, eE, tailSize * (sizeof))

$$I[1] -= (k - 1);$$

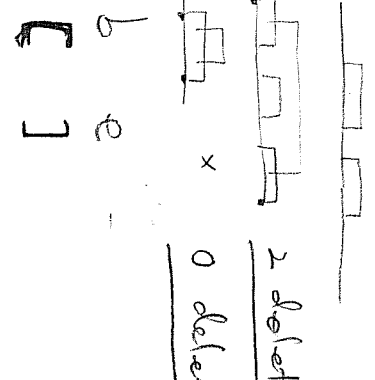
1 2 3 4



$V[r-1] \leq key < V[r]$

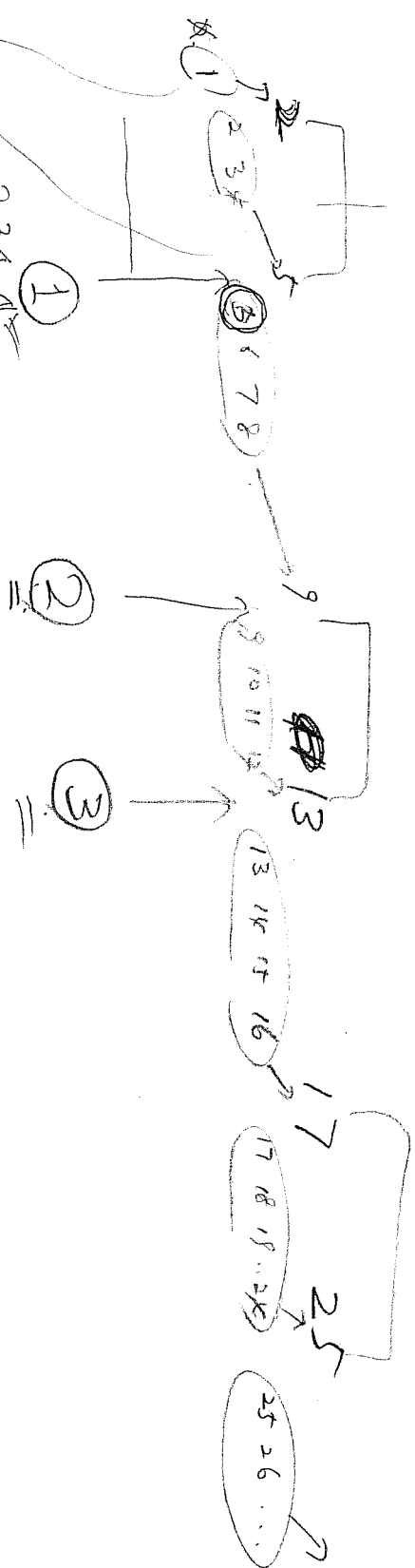
if $r < \text{nel}$

I. $[b, e]$



II. $[b, e]$

if $key < \min(V)$, $r = 0$
if $key \geq \max(V)$, $r = \text{nel}$.



odd#

if odd # index,

within an interval $(\text{index} - 1) / 2$

index

if ~~odd~~ # index &

key \in endpoints,

with an interval $(\text{index} - 2) / 2$

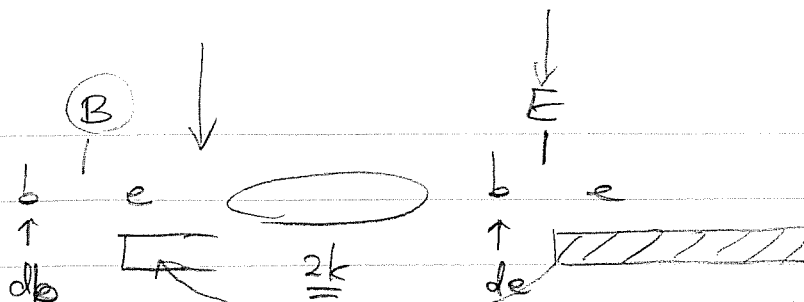
even

else

$(\text{index} - 2) / 2$

index

I.



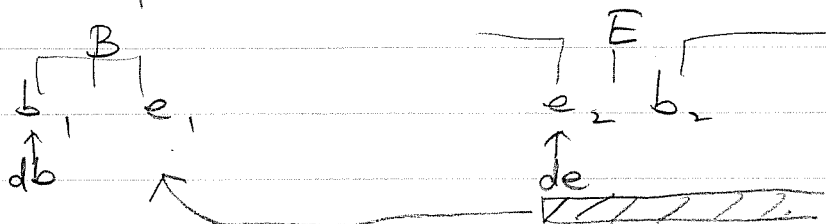
$$de - db = 2k$$

$$k \geq 0$$

Size Endpoint $\Rightarrow 2k$.

if $k=0$, Nothing.
if $k=1$, delete.

II.

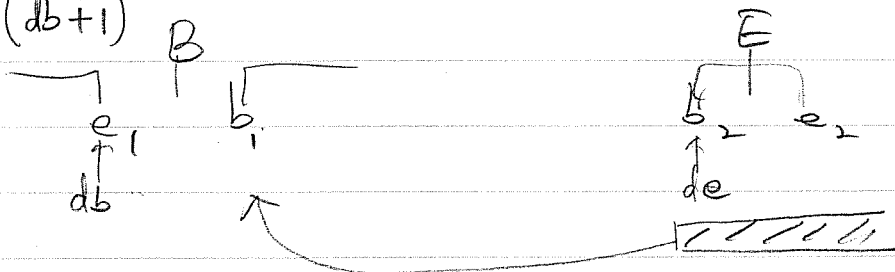


$$de - db = 2k + 1 \quad k \geq 0$$

if $k=0$, $e_1 = e_2$
if $k \geq 1$, delete.

$B \setminus e \in E$
 $*(db+1)$

III.



$$de - db = 2k + 1 \quad k \geq 0$$

if $k=0$, Nothing. $b_1 = b_2$
if $k=1$, delete

$B \setminus b \in B$

$*(db+1)$

IV.



$$de - db = 2k \quad k \geq 0$$

$*(db+1) \in B$

$*(de) \in E$

if $k=0$ insert two points
if $k=1$ use the two points
if $k \geq 2$ delete

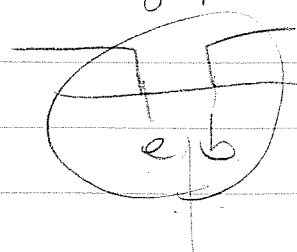
I. No left special, No right special

II. No left special, $de \rightarrow$ last element

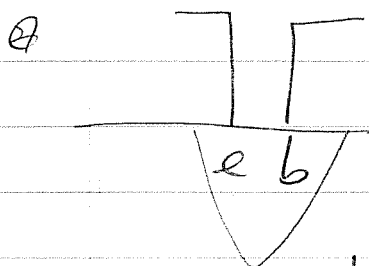
III. $db = -1$, No right special

IV.

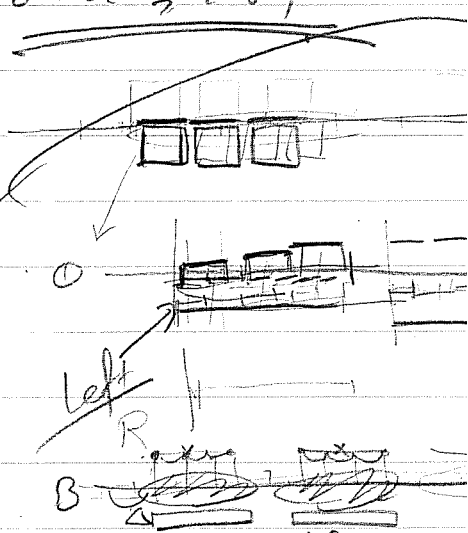
except $0_{n-1} 0_{n-2} \dots 0_1$ point



④ $(db) (de) \Rightarrow$ $0_{n-1} 0_{n-2} \dots 0_1$ or $\text{search } 2, 3, \dots, n$



two intervals
diff.



- ① Use R to build interval
- ② Build tree using B interval
- ③ Periodic points in R are used as queries to the interval tree



single diff