

$$aX + bY + cZ + d = 0$$

$$\vec{AB} = \begin{vmatrix} Bx - Ax \\ By - Ay \\ Bz - Az \end{vmatrix} \quad \vec{AC} = \begin{vmatrix} Cx - Ax \\ Cy - Ay \\ Cz - Az \end{vmatrix}$$

$$\begin{aligned} a &= \vec{AB}_2 * \vec{AC}_3 - \vec{AB}_3 * \vec{AC}_2 \\ b &= \vec{AB}_3 * \vec{AC}_1 - \vec{AB}_1 * \vec{AC}_3 \\ c &= \vec{AB}_1 * \vec{AC}_2 - \vec{AB}_2 * \vec{AC}_1 \\ d &= -(aAx + bAy + cAz) \end{aligned}$$

$$\begin{aligned} A &= -5, 1, -4 \\ B &= -5, 1, 1 \\ C &= -5, -1, 1 \\ D &= -5, -1, -4 \end{aligned}$$

$$\vec{AB} = \begin{vmatrix} -5 & -5 \\ 1 & 1 \\ 1 & -4 \end{vmatrix} \quad \vec{AC} = \begin{vmatrix} -5 & -5 \\ -1 & 1 \\ 1 & -4 \end{vmatrix}$$

$$\vec{AB} = \begin{vmatrix} 0 \\ 0 \\ -5 \end{vmatrix} \quad \vec{AC} = \begin{vmatrix} 0 \\ -2 \\ -5 \end{vmatrix}$$

$$\begin{aligned} a &= (0 * -5) - (-5 * -2) = 10 \\ b &= (-5 * 0) - (0 * -5) = 0 \\ c &= (0 * -2) - (0 * 0) = 0 \\ d &= -(10 * -5 + 0 * 1 + 0 * -4) = 50 \end{aligned}$$

$$10x + 50 = 0$$

$$\sqrt{a^2+b^2+c^2}$$

$$\sqrt{10^2}=10$$

$$\frac{ax+by+cz+d}{\sqrt{a^2+b^2+c^2}}< r$$

$$\sqrt{(x_2-x_1)^2+(y_2-y_1)^2+(z_2-z_1)^2}<r_2+r_1$$