

TUTORIAL 3

① Pseudocode for linear search

for (i=0 to n)

 if (arr[i] == value) // found
 {

② void insertion(int arr[], int n) // recursive

 if (n <= 1)

 return;

 insertion(arr, n-1);

 int nh = arr[n-1];

 int j = n-2;

 while (j >= 0 && arr[j] > nh)

{

 arr[j+1] = arr[j];

 j--;

}

 arr[j+1] = nh;

}

 for (i=1 to n) // iterative

 key = A[i];

 j ← i - 1

 while (j >= 0 and A[j] > key)

 A[j+1] ← A[j];

 j ← j - 1;

}

$A[j+1] \leftarrow \text{key}$

3

Insersion sort is online sorting
because it doesn't know the
whole input, more input can be
inserted with the insertion sorting
is running.

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Q3 Complexity

Name	Best	worse	Average
Selection	$O(n^2)$	$O(n^2)$	$O(n^2)$
Bubble	$O(n)$	$O(n^2)$	$O(n^2)$
Insrtion	$O(n)$	$O(n^2)$	$O(n^2)$
Heap	$O(n \log(n))$	$O(n \log(n))$	$O(n \log(n))$
Quick	$O(n \log(n))$	$O(n^2)$	$O(n \log(n))$
Merge	$O(n \log(n))$	$O(n \log(n))$	$O(n \log(n))$

Q4

Inplace sorting stable sorting Online sorting

Bubble

Mergesort

Insertion

Selection

Bubble

Insrtion

Insertion

Quick sort

Count

Heapsort

Q5
int binary (int arr[], int l, int r, int x)

{
if (r >= l)

{
int mid = l + (r - l) / 2;

if (arr[mid] == x)

return mid;

else if (arr[mid] > x)

return binary (arr, l, m - 1, x);

else

return binary (arr, m + 1, r, x);

}

return -1;

}

int binary (int arr[], int l, int r, int x)

{
while (l <= r)

{
int m = l + (r - l) / 2;

if (arr[m] == x)

return m;

else if (arr[m] > x)

x = m - 1;

else

l = m + 1;

}

return -1;

}

Time complexity of binary search
 $= O(\log n)$
 Linear search $\rightarrow O(n)$

(6) Recurrence relation for binary recursive search

$$T(n) = T(n/2) + 1$$

where $T(n)$ is the time required for binary search in an array of size n .

(7) int find(A[], n, k)

E

sort(A, n)

for (i=0 to n-1)

E n = binary search(A, 0, n-1, k-a[i])
 i.e. (n)

return 1

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return -1

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Time complexity: $O(n \log n) + n \cdot O(\log n)$
 $= O(n \log n)$



(d) Quicksort is the fastest general purpose sort.

- In most practical situations, quick sort is the method of choice. If stability is important and space is available, merge sort might be best.

(e) A pair $a[i:j], a[l:j]$ is said to be inversion if $a[i:j] > a[l:j]$.

(f) The worst case time complexity of quicksort is $O(n^2)$. This case occurs when the picked pivot is always an extreme (smallest or largest) element. This happens when input array is sorted or reverse sorted. The best case of quicksort is when we will select pivot as a mean element.

(ii) Recurrence Relation of

$$\text{Mergesort} \rightarrow T(n) = 2T(n/2) + n$$

$$\text{Quicksort} \rightarrow T(n) = 2T(n/2) + n.$$

Merge sort is more efficient & works faster than good quick sort in case of larger array size or datasets.

Worst case complexity for quick sort is $\mathcal{O}(n^2)$ whereas $\mathcal{O}(n \log n)$ for merge sort.

OR Stable Selection Sort

```
void stable_selection(int arr[], int n)
    for (int i=0; i<n-1; i++)
        E int min = i;
```

```
        for (int j=i+1; j<n; j++)
            E if (arr[min] > arr[j])
                min=j;
```

}

```
    int key = arr[min];
    while (min > i)
```

```
        E arr[min] = arr[min-1];
        min--;
    }
```

```
    arr[i] = key;
}
```

}

Q3. Modified bubble sorting.

void bubble (int a[], int n)

{ for (int i=0; i<n; i++)

{ int swaps = 0;

for (int j=0; j<n-1-i; j++)

{ if (a[j] > a[j+1])

int t = a[j];

a[j] = a[j+1];

a[j+1] = t;

swaps++;

}

}

if (swaps == 0)

break;

}

}