

Exercicis

1. Let $f(x, z) = e^{x+y}$.

- (a) Find the first-order Taylor formula for f at $(0, 0)$.
- (b) Find the second-order Taylor formula for f at $(0, 0)$.

In exercises 3 to 7, calculate the second-order Taylor formula for:

3. $f(x, y) = (x + y)^2$, where $x_0 = 0, y_0 = 0$

4. $f(x, y) = 1/(x^2 + y^2 + 1)$, where $x_0 = 0, y_0 = 0$

5. $f(x, y) = e^{x+y}$, where $x_0 = 0, y_0 = 0$

6. $f(x, y) = e^{-x^2-y^2} \cos(xy)$, where $x_0 = 0, y_0 = 0$

7. $f(x, y) = \sin(xy) + \cos(xy)$, where $x_0 = 0, y_0 = 0$

9. Calculate the second-order Taylor approximation to $f(x, y) = \cos x \sin y$ at the point $(\pi, \pi/2)$.

10. Let $f(x, y) = x \cos(\pi y) - y \sin(\pi x)$. Find the second-order Taylor approximation for f at the point $(1, 2)$.

11. Let $g(x, y) = \sin(xy) - 3x^2 \log y + 1$. Find the degree 2 polynomial which best approximates g near the point $(\pi/2, 1)$.