

### Thermodynamics. Problems. Sheet 3.

1. A certain amount of ideal gas ( $c_{p,molar} = 7R/2$ ) at  $20^\circ\text{C}$  and 1 atm, has a volume of  $70\text{ m}^3$  and is heated at constant pressure to  $25^\circ\text{C}$  by heat transfer from a thermal reservoir at  $40^\circ\text{C}$ .
  - a) What is the heat transferred to the gas?
  - b) Is the process irreversible?
  - c) What is the change in entropy of the thermal reservoir?
  - d) What is the change in entropy of the gas?
2. A rigid container with a volume of  $50\text{ dm}^3$  contains an ideal gas ( $c_{v,molar} = 5R/2$ ) at  $500\text{ K}$  and 1 atm.
  - a) Compute the change in entropy of the gas if  $2870\text{ cal}$  are transferred to it as heat.
  - b) If the vessel has a stirrer that rotates such that the shaft's work delivered to the gas equals  $12.0\text{ kJ}$ , compute the entropy change of the gas if the process is adiabatic.
  - c) Compute the total entropy in stage b. Is the process irreversible?
3. Very pure liquid water can be subcooled at atmospheric pressure to temperatures well below  $0^\circ\text{C}$ . One kilogram of liquid water chilled to  $-6^\circ\text{C}$  partially freezes in an adiabatic process at atmospheric pressure.
  - a) What fraction of the system freezes?
  - b) What is its final temperature?
  - c) What is the  $\Delta S_{\text{total}}$  for the process?
  - d) Is the process reversible or irreversible?

$\Delta H_{\text{melting}}$  of water at  $0^\circ\text{C} = 333.4\text{ J g}^{-1}$ .  
 $c_p$  of subcooled liquid water  $= 4.226\text{ J g}^{-1} \text{ }^\circ\text{C}^{-1}$ .
4. Compute the entropy change that occurs when a 50-gram block of iron at a temperature of  $90^\circ\text{C}$  ( $c_p = 0.449\text{ J/g K}$ ) is placed in an insulated container containing  $100\text{ g}$  of water ( $c_p = 4180\text{ J kg}^{-1} \text{ K}^{-1}$ ) at  $25^\circ\text{C}$ . Is the process irreversible? Why? Consider the heat capacities to be constant within the working temperature range.
5. Compute the change in internal energy, enthalpy and entropy for the expansion of  $10\text{ mol}$  of oxygen from  $200$  to  $2000\text{ liters}$  at  $25^\circ\text{C}$ .
6. A plant operates with a source at  $300^\circ\text{C}$  and a sink at  $25^\circ\text{C}$ . If the thermal efficiency is equal to  $60\%$  of that of a Carnot engine for the same temperatures,
  - a) What is the thermal efficiency of the plant?
  - b) What increase must be given to the source temperature so that the thermal efficiency of the plant increases to  $40\%$ ? Again,  $\eta$  is equal to  $60\%$  of the value corresponding to the Carnot engine.

7. A heat engine works between a hot source at 900 K and a cold source at 300 K following a reversible Carnot cycle. The work produced is used in operating a crane. If 10% of the work of the heat engine is lost in the form of heat due to friction of the pulleys and the total amount of heat given off by the heat engine-pulleys assembly is 72 kJ, compute the heat absorbed from the hot source, the work done by the engine, and the heat transferred to the coolant.
8. The work obtained from a heat engine operating between  $1200^{\circ}\text{C}$  and  $25^{\circ}\text{C}$ , following a reversible Carnot cycle, is used to operate a Carnot refrigerating engine operating between  $0^{\circ}\text{C}$  and  $25^{\circ}\text{C}$ . Compute the relationship between the heat absorbed by the heat engine and the heat extracted from the refrigerating engine if it is assumed that both work reversibly.