

# Lecture 15:

# Knowledge Distillation

**Radoslav Neychev**

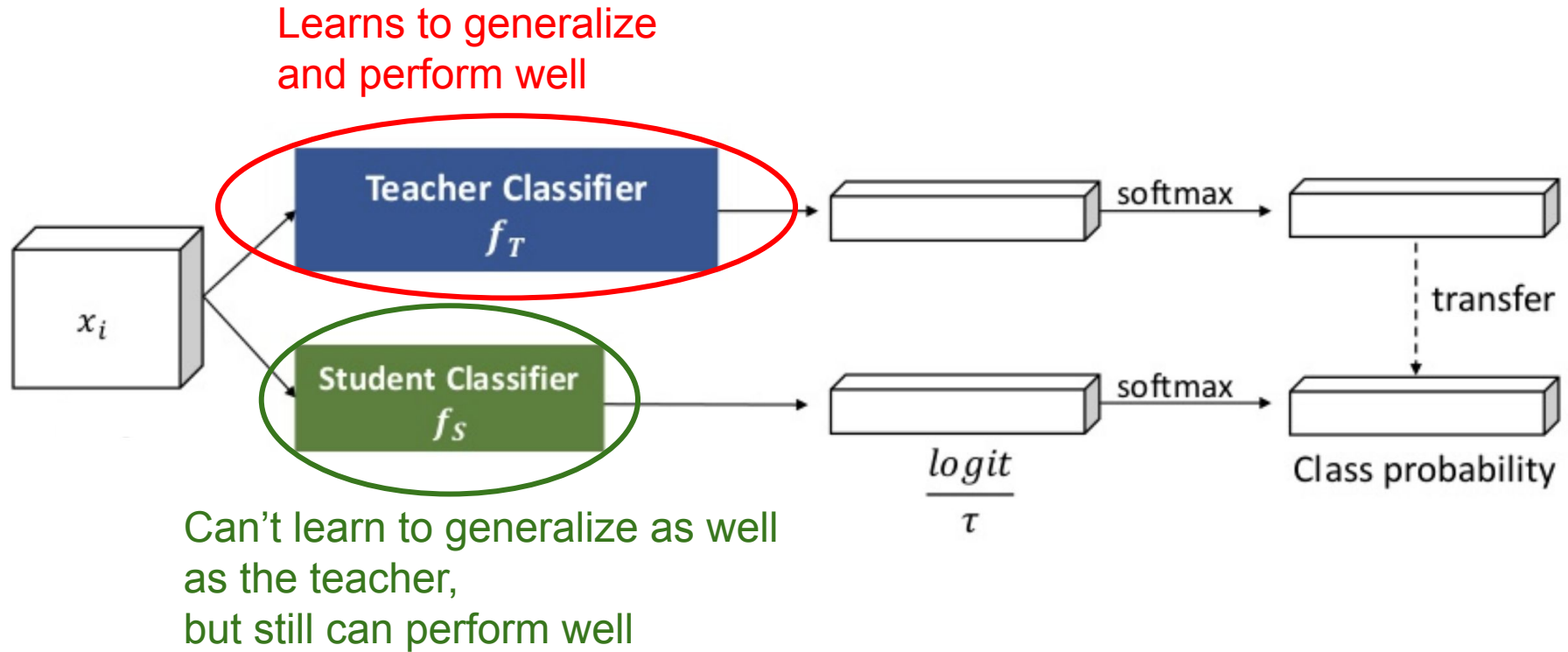
# Extra: Knowledge Distillation

# Cerura Vinula in caterpillar and butterfly forms



Do they have the same “life purpose”  
and solve the same problems?

# Knowledge distillation



# Knowledge distillation

Denote **teacher** and **student** models.

**Student** model has logits  $z_i$  and corresponding probabilities  $q_i$ , derived with the softmax operation:

$$q_i = \frac{\exp(z_i/T)}{\sum_j \exp(z_j/T)}$$

where  $T$  stays for the temperature.

**Teacher** model has logits  $v_i$  and corresponding probabilities  $p_i$ .

# Knowledge distillation

Let's derive the cross-entropy gradient on **student** logits using the **teacher** predictions as targets:

$$\frac{\partial C}{\partial z_i} = \frac{1}{T} (q_i - p_i) = \frac{1}{T} \left( \frac{e^{z_i/T}}{\sum_j e^{z_j/T}} - \frac{e^{v_i/T}}{\sum_j e^{v_j/T}} \right)$$

If the temperature is high, the following equation takes place:

$$\frac{\partial C}{\partial z_i} \approx \frac{1}{T} \left( \frac{1 + z_i/T}{N + \sum_j z_j/T} - \frac{1 + v_i/T}{N + \sum_j v_j/T} \right)$$


# Knowledge distillation

Logits can be centered, so

$$\sum_j z_j = \sum_j v_j = 0$$

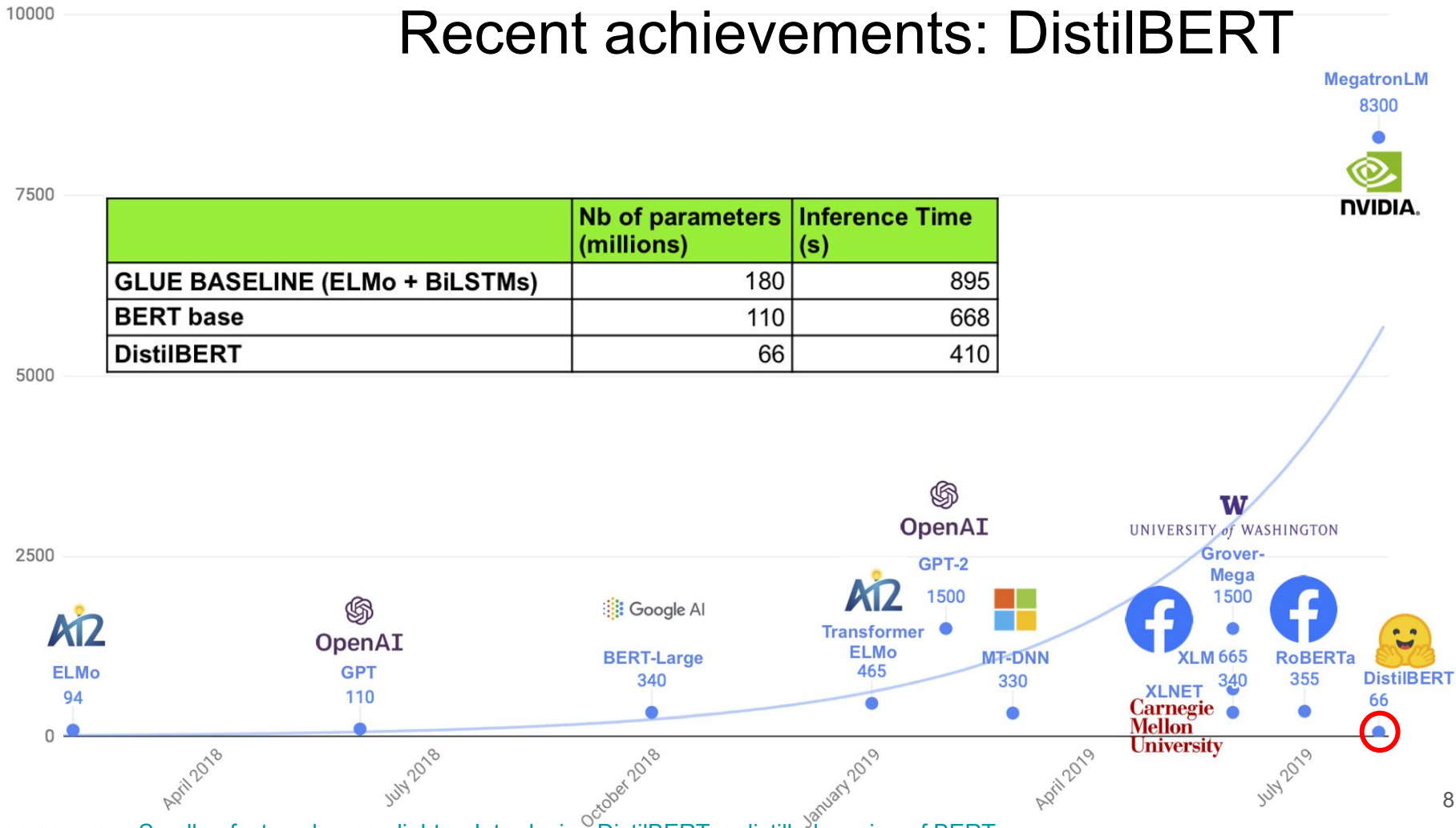
Then the gradient takes form:

$$\frac{\partial C}{\partial z_i} \approx \frac{1}{T} \left( \frac{1 + z_i/T}{N + \sum_j z_j/T} - \frac{1 + v_i/T}{N + \sum_j v_j/T} \right) \approx \frac{1}{NT^2} (z_i - v_i)$$

$$\frac{dC}{dz_i} = \frac{1}{NT^2} (z_i - v_i) \sim (z_i - v_i) = \overset{\text{Constant}}{M} \frac{d(z_i - v_i)^2}{dz_i}$$


# Recent achievements: DistilBERT

number of parameters, millions





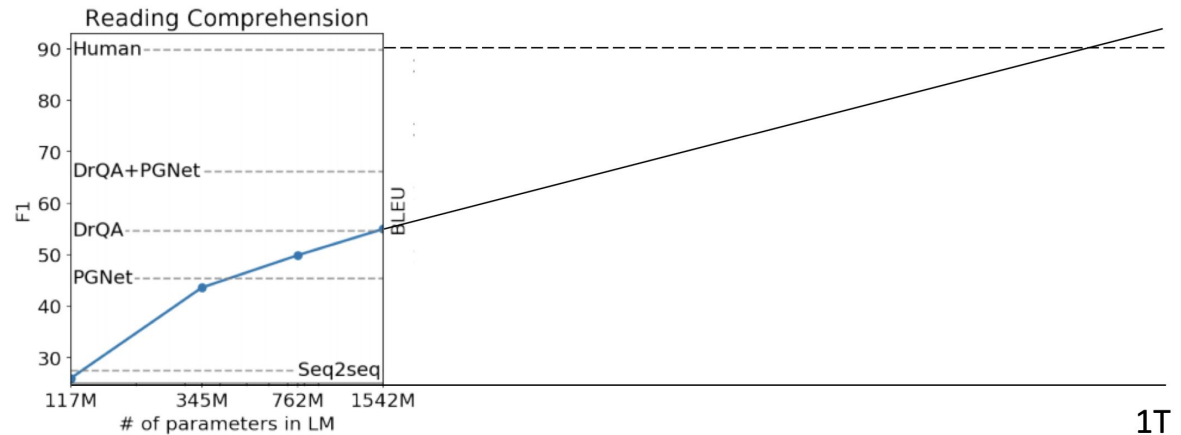
# Main ideas

- DistilBERT is initialized from its teacher, BERT, by taking one layer out of two, leveraging the common hidden size.
  - *Comment: Training a sub-network is not only about the architecture. It is also about finding the right initialization for the sub-network to converge.*
- DistilBERT is trained on very large batches leveraging gradient accumulation (up to 4000 examples per batch), with dynamic masking and removed the next sentence prediction objective.
  - *Comment: the way BERT is trained is crucial for its final performance.*
- DistilBERT was trained on eight 16GB V100 GPUs for approximately three and a half days using the concatenation of Toronto Book Corpus and English Wikipedia (same data as original BERT).



# Recent achievements: GPT-3

GPT-3, May 2020  
175B parameters  
(proportions are incorrect for visual sake)



Hypothesis from Stanford CS224n (2019) lecture 20

number of parameters, millions

