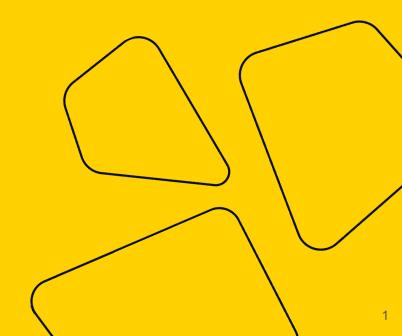
Machine Learning Lecture 1: intro to ML

Radoslav Neychev

MIPT, fall 2023





Outline

- 1. ML and AI overview
- 2. Thesaurus and notation
- 3. Maximum Likelihood Estimation
- 4. Some Machine Learning problems
 - a. Classification
 - o. Regression
 - c. Dimensionality reduction
- 5. Naïve Bayes classifier
- 5. k Nearest Neighbours (kNN)



ML and Al overview

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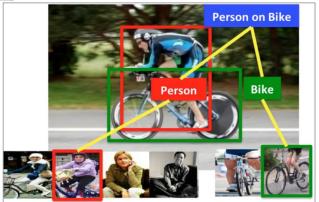
Machine Learning applications





- Object detection
- Action classification
- Image captioning
-





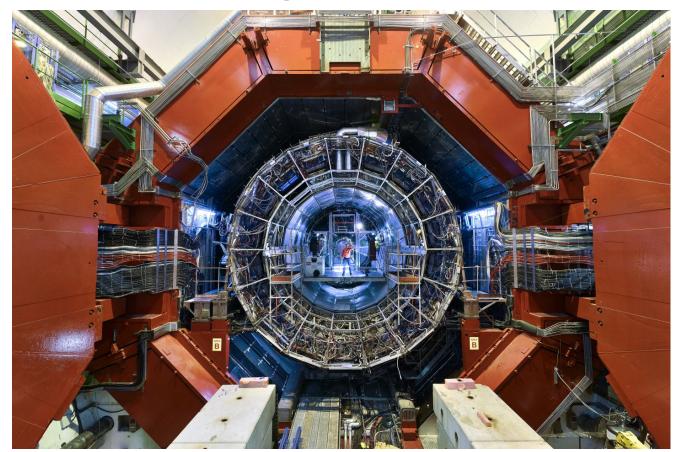
Machine Learning applications





Machine Learning applications



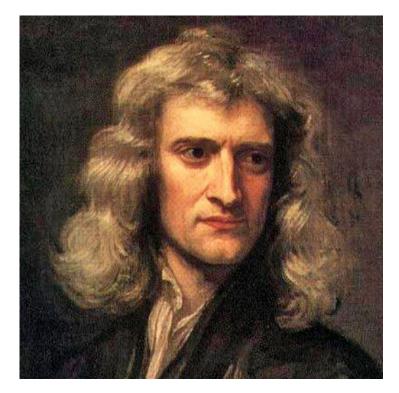




Data Knowledge

Long before the ML





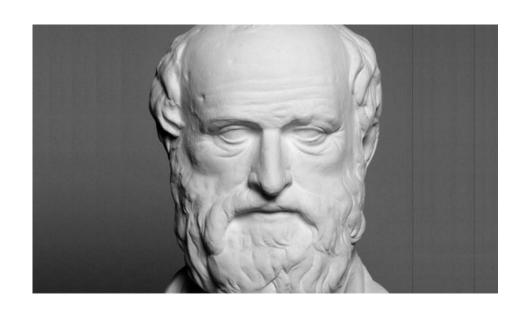
Isaac Newton



Johannes Kepler

Long before the ML





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Denote the **dataset**.

,	<u>, </u>							
/			Statistics	Python		Native	Target	Target
\	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(passed)
	John	22	5	4	Brown	English	5	TRUE
1	Aahna	17	4	5	Brown	Hindi	4	TRUE
	Emily	25	5	5	Blue	Chinese	5	TRUE
	Michael	27	3	4	Green	French	5	TRUE
	Some							
	student	23	3	3	NA	Esperanto	2	FALSE



Observation (or datum, or data point) is one piece of information.

,		-			•			
\langle			Statistics	Python		Native	Target	Target
	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(passed)
	John	22	5	4	Brown	English	5	TRUE
1	Aahna	17	4	5	Brown	Hindi	4	TRUE
	Emily	25	5	5	Blue	Chinese	5	TRUE
	Michael	27	3	4	Green	French	5	TRUE
	Some							
X	student	23	3	3	NA	Esperanto	2	FALSE

In many cases the observations are supposed to be *i.i.d.*

- independent
- identically distributed



Feature (or predictor) represents some special property.

	Name	Age	Statistics (mark)	Python (mark)	Eye color	Native language	Target (mark)	Target (passed)
	John	22	5	4	Brown	English	5	TRUE
	Aahna	17	4	5	Brown	Hindi	4	TRUE
	Emily	25	5	5	Blue	Chinese	5	TRUE
	Michael	27	3	4	Green	French	5	TRUE
\ \	Some							
1	student	23	3	3	NA	Esperanto	2	FALSE



,								
\langle			Statistics	Python		Native	Target	Target
\	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(passed)
	John	22	5	4	Brown	English	5	TRUE
1	Aahna	17	4	5	Brown	Hindi	4	TRUE
	Emily	25	5	5	Blue	Chinese	5	TRUE
	Michael	27	3	4	Green	French	5	TRUE
	Some							
J	student	23	3	3	NA	Esperanto	2	FALSE



,								
/			Statistics	Python		Native	Target	Target
\	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(passed)
	John	22	5	4	Brown	English	5	TRUE
1	Aahna	17	4	5	Brown	Hindi	4	TRUE
	Emily	25	5	5	Blue	Chinese	5	TRUE
	Michael	27	3	4	Green	French	5	TRUE
	Some							
	student	23	3	3	NA	Esperanto	2	FALSE



,	<u>,</u>							
/			Statistics	Python		Native	Target	Target
\	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(passed)
	John	22	5	4	Brown	English	5	TRUE
1	Aahna	17	4	5	Brown	Hindi	4	TRUE
	Emily	25	5	5	Blue	Chinese	5	TRUE
	Michael	27	3	4	Green	French	5	TRUE
	Some							
	student	23	3	3	NA	Esperanto	2	FALSE



\langle			Statistics	Python		Native	Target	Target
\	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(passed)
	John	22	5	4	Brown	English	5	TRUE
1	Aahna	17	4	5	Brown	Hindi	4	TRUE
	Emily	25	5	5	Blue	Chinese	5	TRUE
	Michael	27	3	4	Green	French	5	TRUE
	Some							
	student	23	3	3	NA	Esperanto	2	FALSE



And even the name is a **feature**

,	<u>, </u>							
$\sqrt{}$			Statistics	Python		Native	Target	Target
\	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(passed)
	John	22	5	4	Brown	English	5	TRUE
1	Aahna	17	4	5	Brown	Hindi	4	TRUE
	Emily	25	5	5	Blue	Chinese	5	TRUE
	Michael	27	3	4	Green	French	5	TRUE
	Some							
	student	23	3	3	NA	Esperanto	2	FALSE



The **design matrix** contains all the features and observations.

,	<u>, </u>							
/			Statistics	Python		Native	Target	Target
	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(passed)
	John	22	5	4	Brown	English	5	TRUE
1	Aahna	17	4	5	Brown	Hindi	4	TRUE
	Emily	25	5	5	Blue	Chinese	5	TRUE
	Michael	27	3	4	Green	French	5	TRUE
	Some							
X	student	23	3	3	NA	Esperanto	2	FALSE

Features can even be multidimensional, we will discuss it later in this course.



Target represents the information we are interested in.

/	•							
\langle			Statistics	Python		Native	Target	Target
\	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(passed)
	John	22	5	4	Brown	English	5	TRUE
1	Aahna	17	4	5	Brown	Hindi	4	TRUE
· ·	Emily	25	5	5	Blue	Chinese	5	TRUE
	Michael	27	3	4	Green	French	5	TRUE
	Some							
X	student	23	3	3	NA	Esperanto	2	FALSE

Target can be either a **number** (real, integer, etc.) – for **regression** problem



Target represents the information we are interested in.

		Statistics	Python		Native	Target	Target
Name	Age	(mark)	(mark)	Eye color	language	(mark)	(passed)
John	22	5	4	Brown	English	5	TRUE
Aahna	17	4	5	Brown	Hindi	4	TRUE
Emily	25	5	5	Blue	Chinese	5	TRUE
 Michael	27	3	4	Green	French	5	TRUE
Some							
student	23	3	3	NA	Esperanto	2	FALSE

Or a **label** – for **classification** problem



Target represents the information we are interested in.

/								
\langle			Statistics	Python		Native	Target	Target
	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(passed)
	John	22	5	4	Brown	English	5	TRUE
1	Aahna	17	4	5	Brown	Hindi	4	TRUE
	Emily	25	5	5	Blue	Chinese	5	TRUE
	Michael	27	3	4	Green	French	5	TRUE
	Some							
Y	student	23	3	3	NA	Esperanto	2	FALSE

Mark can be treated as a label too (due to finite number of labels: 1 to 5). We will discuss it later.



Further we will work with the numerical target (mark)

Name	Age	Statistics (mark)	Python (mark)	Eye color	Native language	Target (mark)
John	22	,	,	Brown	English	5
Aahna	17	4	5	Brown	Hindi	4
Emily	25	5	5	Blue	Chinese	5
Michael	27	3	4	Green	French	5
Some						
student	23	3	3	NA	Esperanto	2



The **prediction** contains values we predicted using some **model**.

\langle			Statistics	Python		Native	Target	Predicted
	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(mark)
	John	22	5	4	Brown	English	5	4.5
1	Aahna	17	4	5	Brown	Hindi	4	4.5
	Emily	25	5	5	Blue	Chinese	5	5
	Michael	27	3	4	Green	French	5	3.5
	Some							
7	student	23	3	3	NA	Esperanto	2	3

One could notice that prediction just averages of Statistics and Python marks. So our **model** can be represented as follows:



The **prediction** contains values we predicted using some **model**.

\langle			Statistics	Python		Native	Target	Predicted
	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(mark)
	John	22	5	4	Brown	English	5	4.5
/	Aahna	17	4	5	Brown	Hindi	4	4.5
	Emily	25	5	5	Blue	Chinese	5	5
	Michael	27	3	4	Green	French	5	3.5
	Some							
	student	23	3	3	NA	Esperanto	2	3

Different models can provide different predictions:



The **prediction** contains values we predicted using some **model**.

			Statistics	Python		Native	Target	Predicted
	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(mark)
	John	22	5	4	Brown	English	5	1
	Aahna	17	4	5	Brown	Hindi	4	5
	Emily	25	5	5	Blue	Chinese	5	2
	Michael	27	3	4	Green	French	5	4
	Some							
1	student	23	3	3	NA	Esperanto	2	3

Different models can provide different predictions:

$$\operatorname{mark}_{ML} = \operatorname{random}(\operatorname{integer from} [1; 5])$$



The **prediction** contains values we predicted using some **model**.

			Statistics	Python	_	Native	Target	Predicted
	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(mark)
	John	22	5	4	Brown	English	5	1
	Aahna	17	4	5	Brown	Hindi	4	5
	Emily	25	5	5	Blue	Chinese	5	2
_	Michael	27	3	4	Green	French	5	4
	Some							
1	student	23	3	3	NA	Esperanto	2	3

Different models can provide different predictions.

Usually some hypothesis lies beneath the model choice.



Loss function measures the error rate of our model.

Square	Target	Predicted
deviation	Target (mark)	(mark)
16	5	1
1	4	5
9	5	2
1	5	4
1	2	3

• **Mean Squared Error** (where **y** is vector of targets):

$$MSE(\mathbf{y}, \hat{\mathbf{y}}) = \frac{1}{N} ||\mathbf{y} - \hat{\mathbf{y}}||_2^2 = \frac{1}{N} \sum_i (y_i - \hat{y}_i)^2$$



Loss function measures the error rate of our model.

Absolute deviation	Target (mark)	Predicted (mark)
4	5	1
1	4	5
3	5	2
1	5	4
1	2	3

• **Mean Absolute Error** (where **y** is vector of targets):

$$MAE(\mathbf{y}, \hat{\mathbf{y}}) = \frac{1}{N} ||\mathbf{y} - \hat{\mathbf{y}}||_1 = \frac{1}{N} \sum_{i} |y_i - \hat{y}_i|$$



To learn something, our **model** needs some degrees of freedom:

	Name	Age	Statistics (mark)	Python (mark)	Eye color		Target (mark)	Predicted (mark)
	John	22	5	4	Brown	English	5	4.5
	Aahna	17	4	5	Brown	Hindi	4	4.5
	Emily	25	5	5	Blue	Chinese	5	5
	Michael	27	3	4	Green	French	5	3.5
	Some							
1	student	23	3	3	NA	Esperanto	2	3

$$\operatorname{mark}_{ML} = w_1 \cdot \operatorname{mark}_{Statistics} + w_2 \cdot \operatorname{mark}_{Python}$$



To learn something, our **model** needs some degrees of freedom:

			Statistics	Python		Native	Target	Predicted
	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(mark)
	John	22	5	4	Brown	English	5	4.447
	Aahna	17	4	5	Brown	Hindi	4	4.734
	Emily	25	5	5	Blue	Chinese	5	5.101
	Michael	27	3	4	Green	French	5	3.714
	Some							
1	student	23	3	3	NA	Esperanto	2	3.060

$$\operatorname{mark}_{ML} = w_1 \cdot \operatorname{mark}_{Statistics} + w_2 \cdot \operatorname{mark}_{Python}$$



To learn something, our **model** needs some degrees of freedom:

			Statistics	Python		Native	Target	Predicted
	Name	Age	(mark)	(mark)	Eye color	language	(mark)	(mark)
	John	22	5	4	Brown	English	5	1
	Aahna	17	4	5	Brown	Hindi	4	5
	Emily	25	5	5	Blue	Chinese	5	2
	Michael	27	3	4	Green	French	5	4
	Some							
1	student	23	3	3	NA	Esperanto	2	3

$$\operatorname{mark}_{ML} = \operatorname{random}(\operatorname{integer from} [1; 5])$$



Last term we should learn for now is **hyperparameter**.

Hyperparameter should be fixed before our model starts to work with the data.

We will discuss it later with kNN as an example.



Recap:

- Dataset
- Observation (datum)
- Feature
- Design matrix
- Target
- Prediction
- Model
- Loss function
- Parameter
- Hyperparameter

Machine Learning problems overview

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Supervised learning problem statement

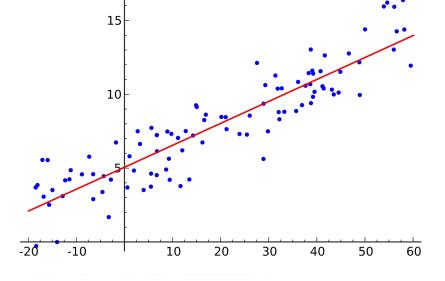


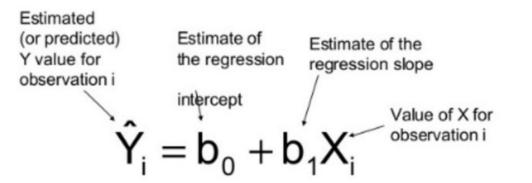
Let's denote:

- ullet Training set $\mathcal{L} = \{\mathbf{x}_i, y_i\}_{i=1}^n$, where
 - $\circ (\mathbf{x} \in \mathbb{R}^p, y \in \mathbb{R})$ for regression
 - $\mathbf{x}_i \in \mathbb{R}^p$, $y_i \in \{+1, -1\}$ for binary classification
- ullet Model $f(\mathbf{X})$ predicts some value for every object
- ullet Loss function $Q(\mathbf{x},y,f)$ that should be minimized



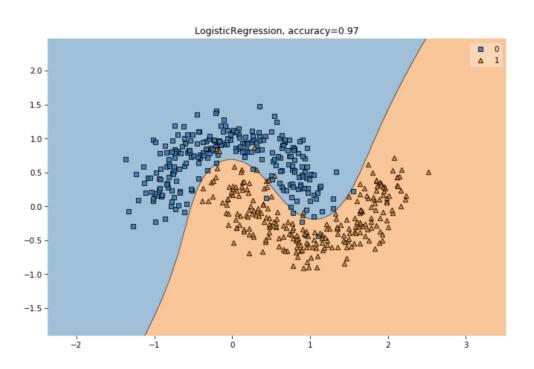
• Regression problem





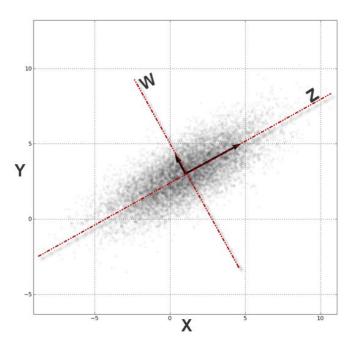


- Regression problem
- Classification problem





- Regression problem
- Classification problem
- Dimensionality reduction



kNN – k Nearest Neighbors

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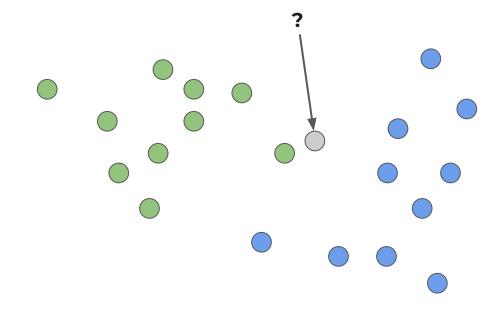


kNN - k Nearest Neighbours



kNN - k Nearest Neighbours





k Nearest Neighbors Method



Given a new observation:

- 1. Calculate the distance to each of the samples in the dataset.
- 2. Select samples from the dataset with the minimal distance to them.
- 3. The label of the new observation will be the most frequent label among those nearest neighbors.

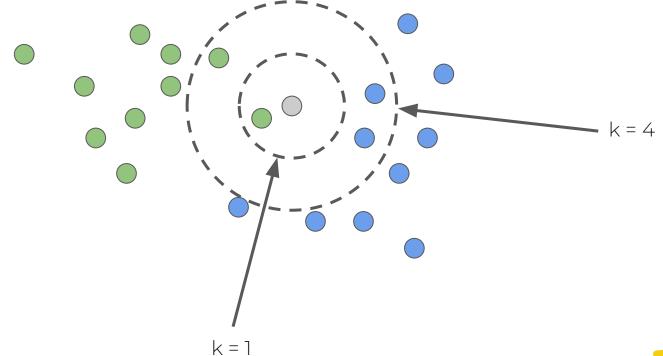
How to make it better?



• The number of neighbors k (it is a **hyperparameter**)

kNN - k Nearest Neighbours



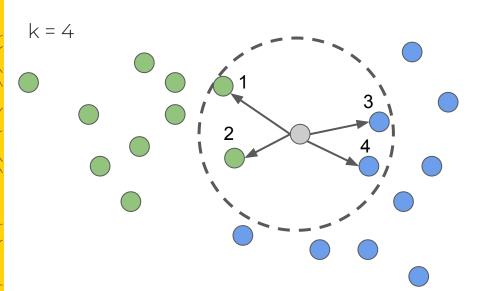


How to make it better?

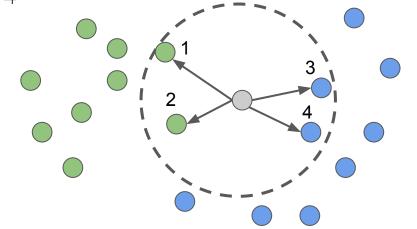


- The number of neighbors k (it is a **hyperparameter**)
- The distance measure between samples
 - a. Hamming
 - b. Euclidean
 - c. cosine
 - d. Minkowski distances
 - e. etc.
- Weighted neighbours







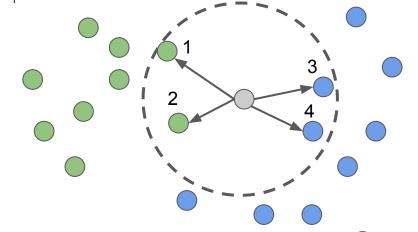


 Weights can be adjusted according to the neighbors order,

$$w(\mathbf{x}_{(i)}) = w_i$$



$$k = 4$$



 Weights can be adjusted according to the neighbors order,

$$w(\mathbf{x}_{(i)}) = w_i$$

or on the distance itself

$$w(\mathbf{x}_{(i)}) = w(d(\mathbf{x}, \mathbf{x}_{(i)}))$$



 Weights can be adjusted according to the neighbors order,

$$w(\mathbf{x}_{(i)}) = w_i$$

or on the distance itself $w(\mathbf{x}_{(i)}) = w(d(\mathbf{x}, \mathbf{x}_{(i)}))$

$$p_{\text{green}} = \frac{w(\mathbf{x}_1) + w(\mathbf{x}_2)}{w(\mathbf{x}_1) + w(\mathbf{x}_2) + w(\mathbf{x}_3) + w(\mathbf{x}_4)}$$



 Weights can be adjusted according to the neighbors order,

$$w(\mathbf{x}_{(i)}) = w_i$$

or on the distance itself $w(\mathbf{x}_{(i)}) = w(d(\mathbf{x}, \mathbf{x}_{(i)}))$

$$p_{\text{blue}} = \frac{w(\mathbf{x}_3) + w(\mathbf{x}_4)}{w(\mathbf{x}_1) + w(\mathbf{x}_2) + w(\mathbf{x}_3) + w(\mathbf{x}_4)}$$

Outro



- Remember the i.i.d. property
- Usually the first dimension corresponds to the batch size, the second (and so on) to the features/time/...
- Even the naïve assumptions may be suitable in some cases
- Simple models provide great baselines

Revise

- 1. ML and AI overview
- 2. Thesaurus and notation
- 3. Maximum Likelihood Estimation
- 4. Some Machine Learning problems
 - a. Classification
 - b. Regression
 - c. Dimensionality reduction
- 5. Naïve Bayes classifier
- 5. k Nearest Neighbours (kNN)



A&Q

Thanks for attention!



