

# Outline



1. Previous lecture recap: backpropagation, activations, intuition.
2. Optimizers.
3. Data normalization.
4. Regularization.

# Once again: nonlinearities

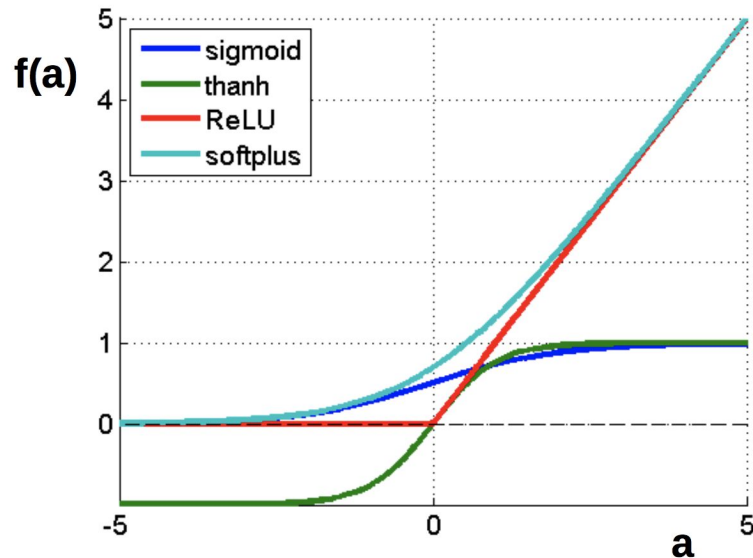


$$f(a) = \frac{1}{1 + e^{-a}}$$

$$f(a) = \tanh(a)$$

$$f(a) = \max(0, a)$$

$$f(a) = \log(1 + e^a)$$



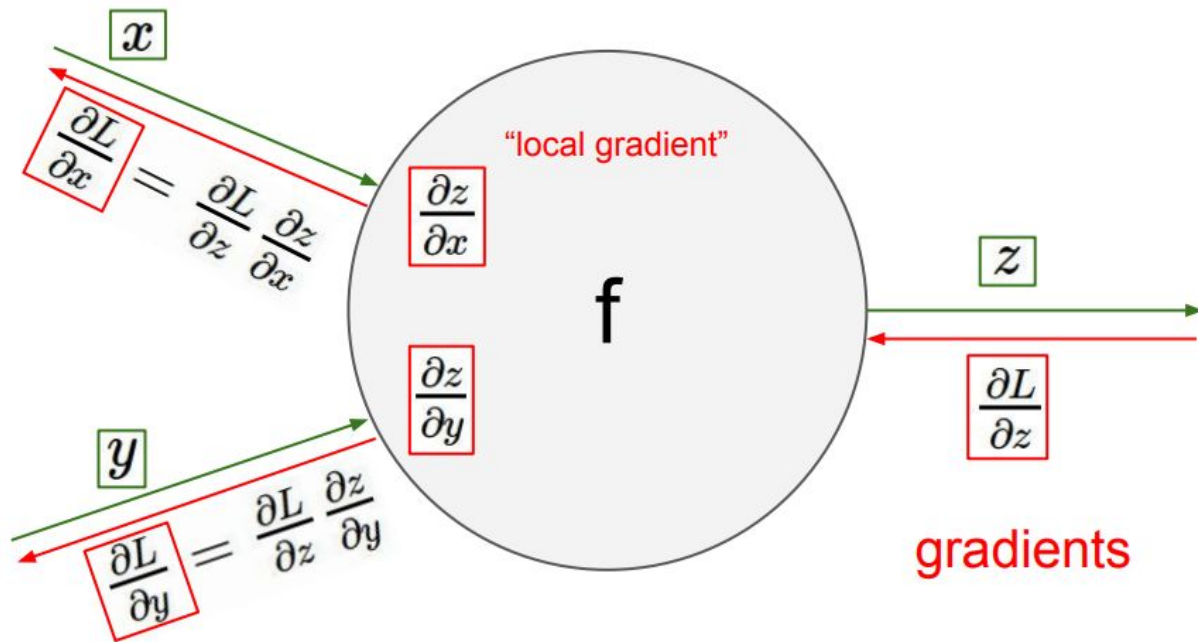


# Backpropagation and chain rule

Chain rule is just simple math:

$$\frac{\partial L}{\partial x} = \frac{\partial L}{\partial z} \frac{\partial z}{\partial x}$$

Backprop is just way to use it in NN training.

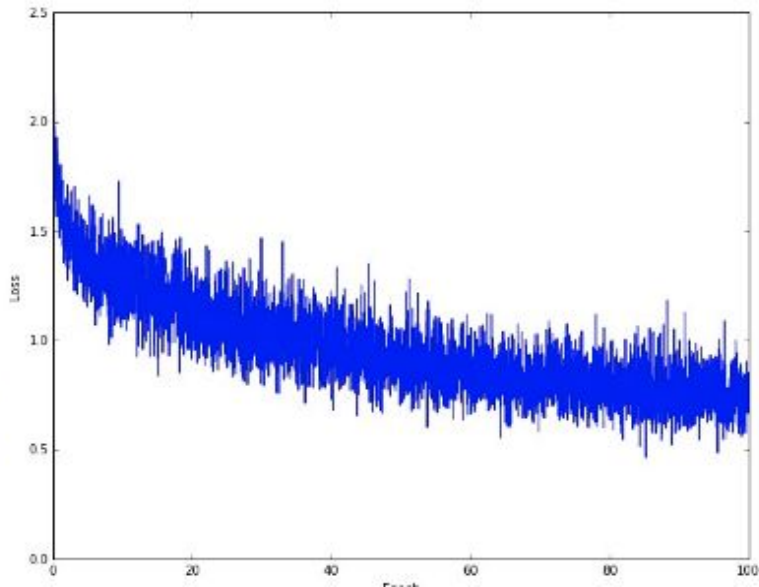
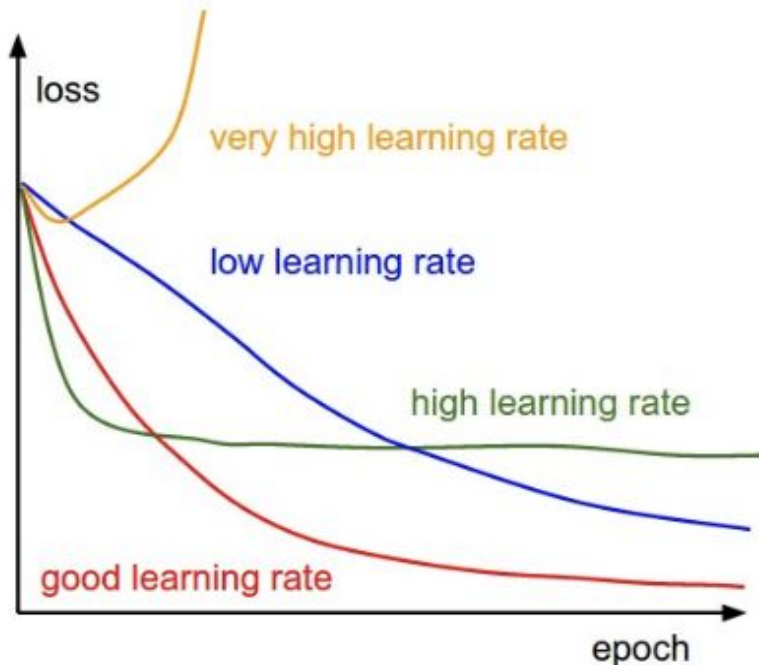


# Optimizers



Stochastic gradient descent is used to optimize NN parameters.

$$x_{t+1} = x_t - \text{learning rate} \cdot dx$$

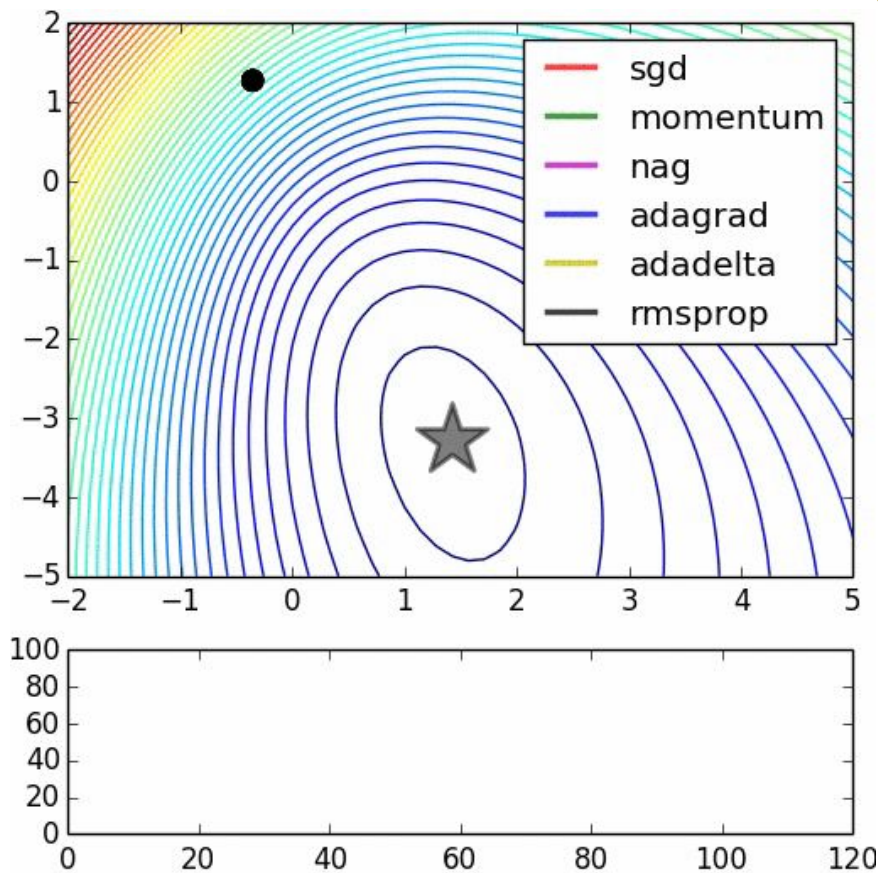


source: <http://cs231n.github.io/neural-networks-3/>

# Optimizers

There are much more optimizers:

- Momentum
- Adagrad
- Adadelata
- RMSprop
- Adam
- ...
- even other NNs



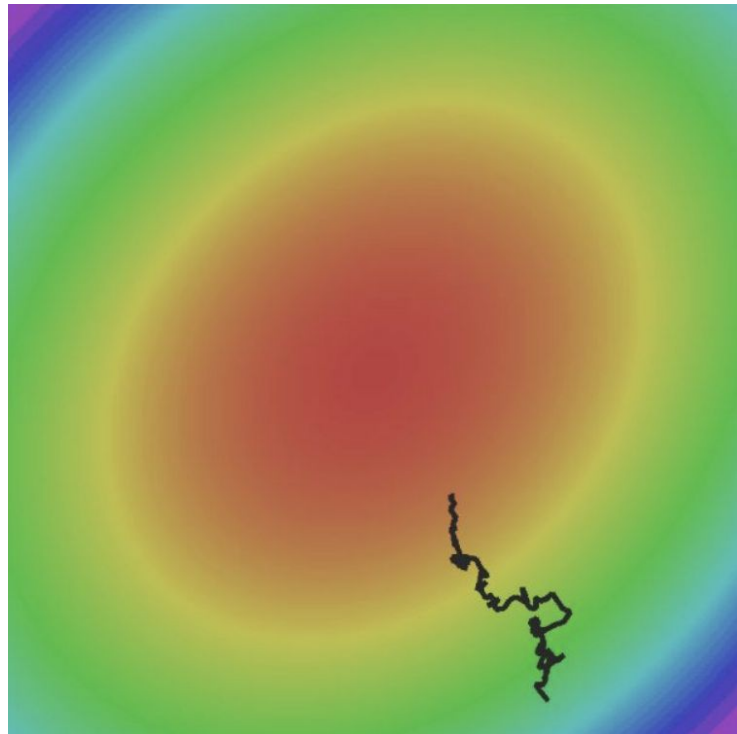
# Optimization: SGD



$$L(W) = \frac{1}{N} \sum_{i=1}^N L_i(x_i, y_i, W)$$

$$\nabla_W L(W) = \frac{1}{N} \sum_{i=1}^N \nabla_W L_i(x_i, y_i, W)$$

Averaging over mini batches => noisy gradient



# First idea: momentum



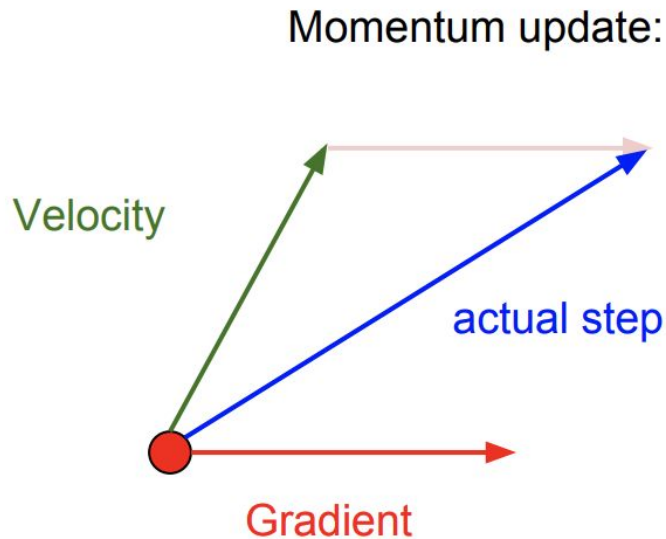
Simple SGD

$$x_{t+1} = x_t - \alpha \nabla f(x_t)$$

SGD with momentum

$$v_{t+1} = \rho v_t + \nabla f(x_t)$$

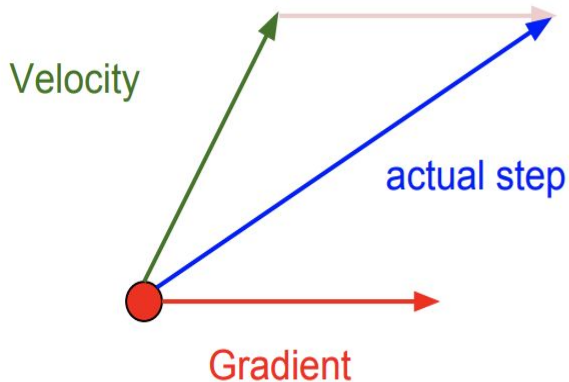
$$x_{t+1} = x_t - \alpha v_{t+1}$$





# Nesterov momentum

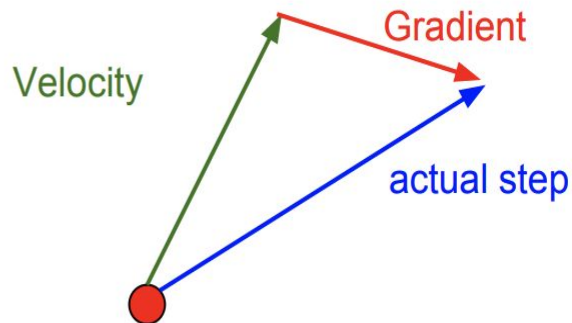
Momentum update:



$$v_{t+1} = \rho v_t + \nabla f(x_t)$$

$$x_{t+1} = x_t - \alpha v_{t+1}$$

Nesterov Momentum

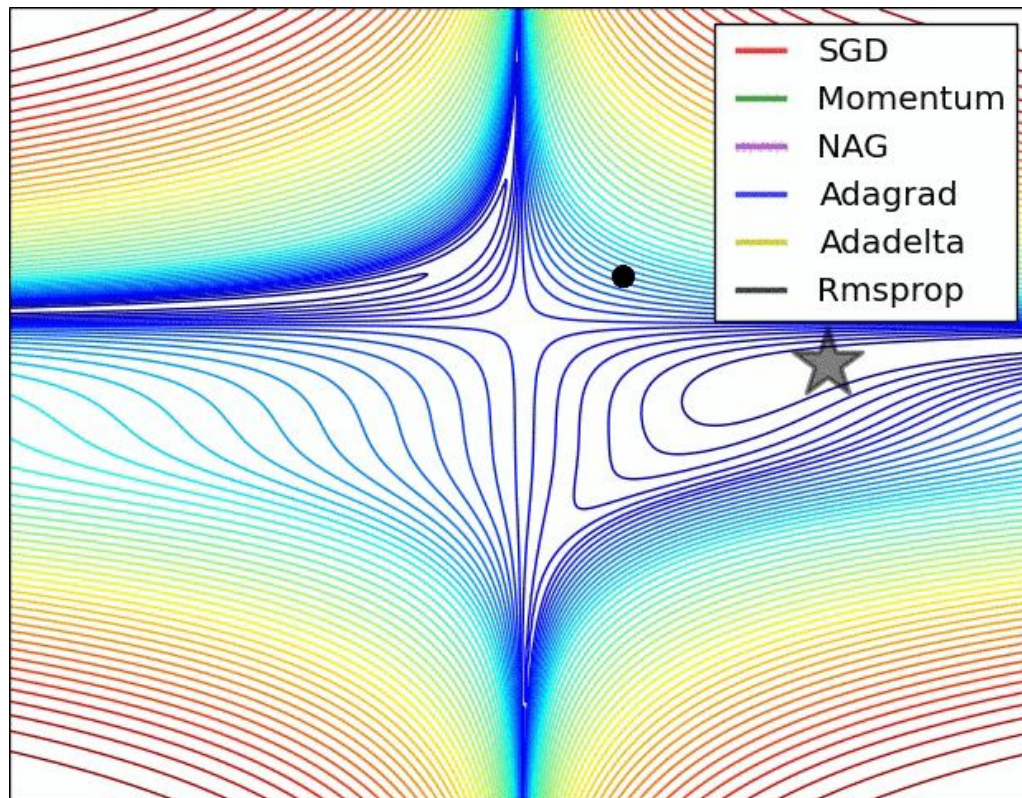


$$v_{t+1} = \rho v_t - \alpha \nabla f(\boxed{x_t + \rho v_t})$$

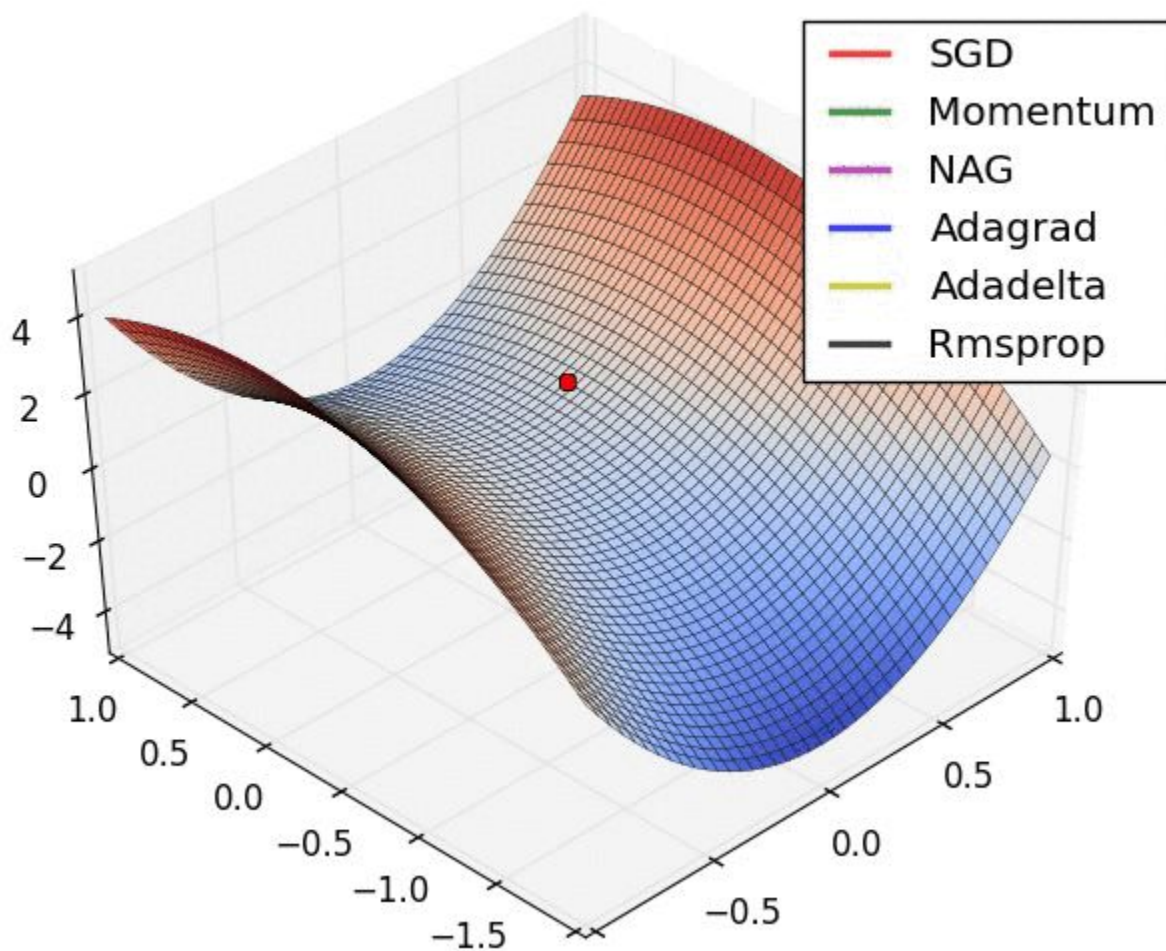
$$x_{t+1} = x_t + v_{t+1}$$



# Comparing momentums



source:



source:

[https://ruder.io/content/images/2016/09/saddle\\_point\\_evaluation\\_optimizers.gif](https://ruder.io/content/images/2016/09/saddle_point_evaluation_optimizers.gif)

# Second idea: different dimensions are different



Adagrad: SGD with cache

$$\text{cache}_{t+1} = \text{cache}_t + (\nabla f(x_t))^2$$

$$x_{t+1} = x_t - \alpha \frac{\nabla f(x_t)}{\text{cache}_{t+1} + \varepsilon}$$



# Second idea: different dimensions are different

Adagrad: SGD with cache

$$\text{cache}_{t+1} = \text{cache}_t + (\nabla f(x_t))^2$$

$$x_{t+1} = x_t - \alpha \frac{\nabla f(x_t)}{\text{cache}_{t+1} + \varepsilon}$$

Problem: gradient fades with time



# Second idea: different dimensions are different

Adagrad: SGD with cache

$$\text{cache}_{t+1} = \text{cache}_t + (\nabla f(x_t))^2$$

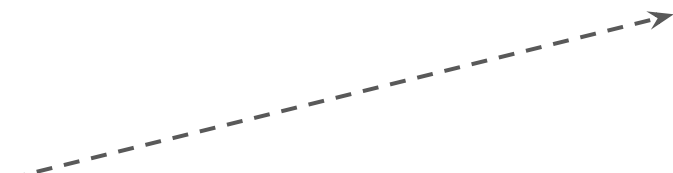
$$x_{t+1} = x_t - \alpha \frac{\nabla f(x_t)}{\text{cache}_{t+1} + \varepsilon}$$



RMSProp: SGD with cache with exp. Smoothing

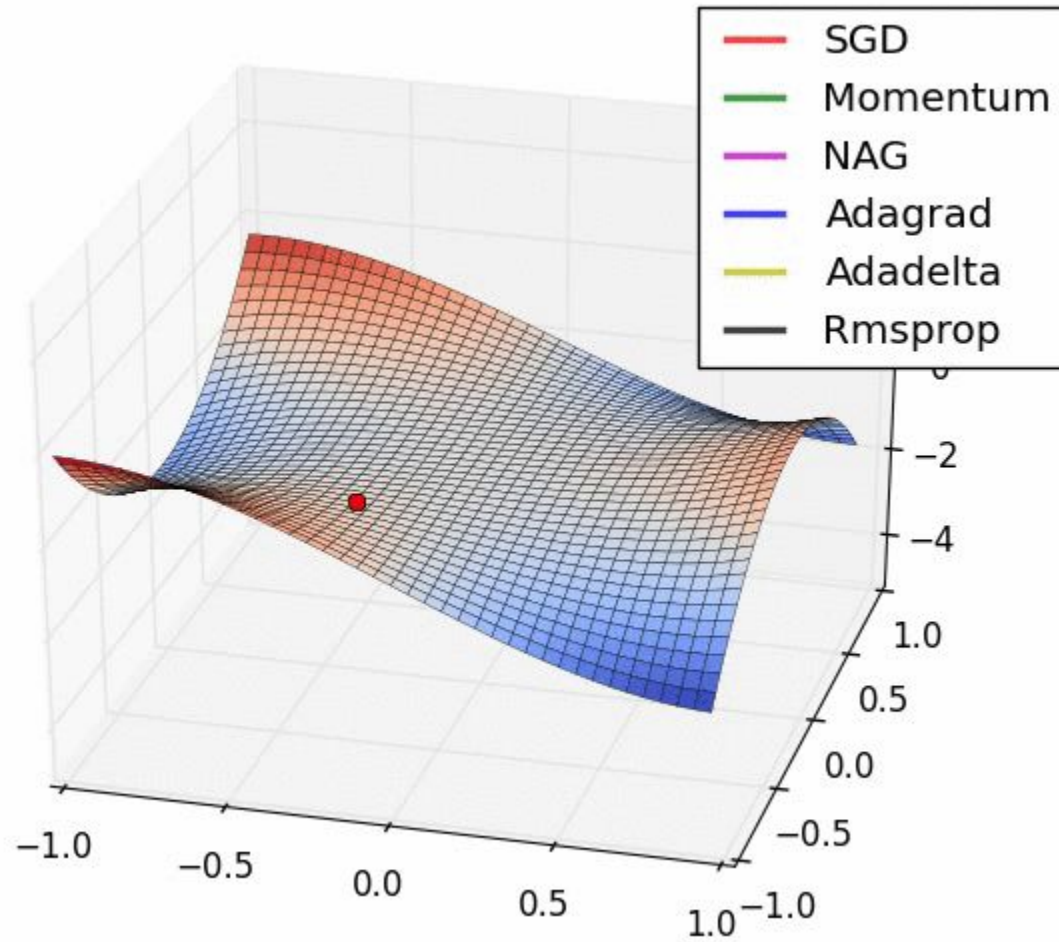
$$\text{cache}_{t+1} = \beta \text{cache}_t + (1 - \beta)(\nabla f(x_t))^2$$

$$x_{t+1} = x_t - \alpha \frac{\nabla f(x_t)}{\text{cache}_{t+1} + \varepsilon}$$



Slide 29 Lecture 6 of Geoff Hinton's Coursera class

[http://www.cs.toronto.edu/~tijmen/csc321/slides/lecture\\_slides\\_lec6.pdf](http://www.cs.toronto.edu/~tijmen/csc321/slides/lecture_slides_lec6.pdf)



source: <https://imgur.com/a/Hqolp#NKsFHJb>



# Adam

Let's combine the momentum idea and RMSProp normalization:

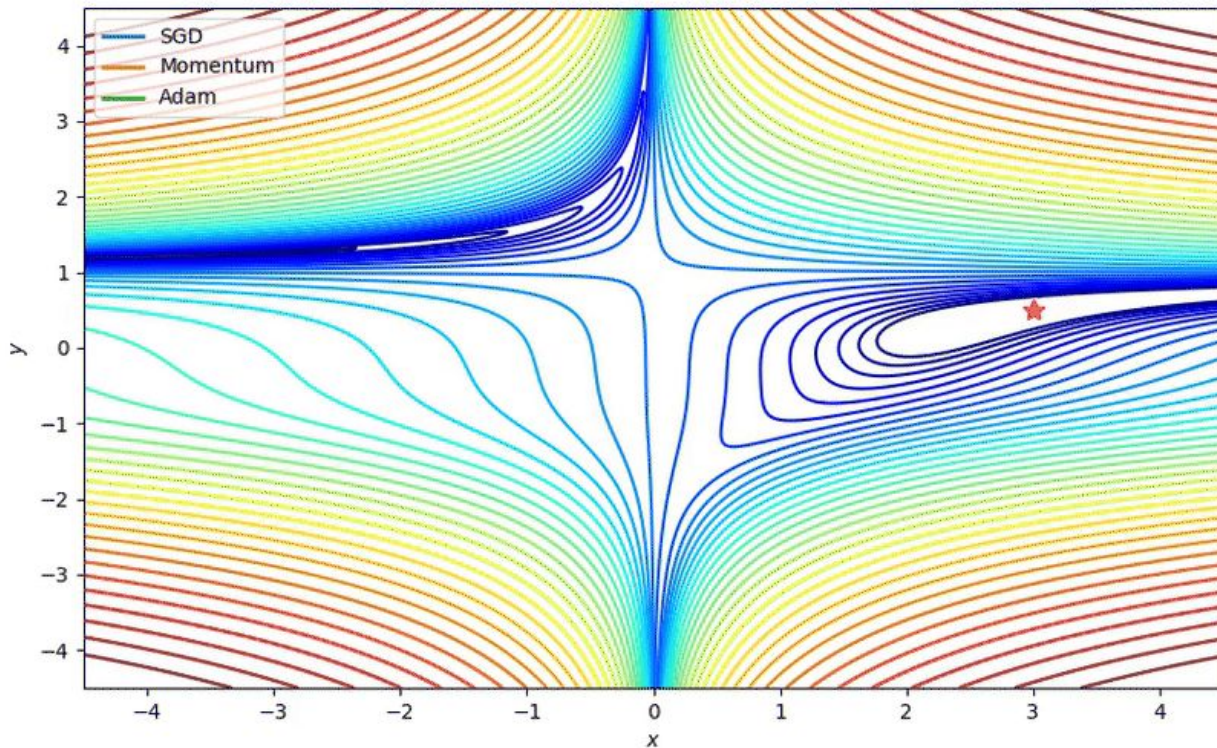
$$\begin{aligned}v_{t+1} &= \gamma v_t + (1 - \gamma) \nabla f(x_t) \\ \text{cache}_{t+1} &= \beta \text{cache}_t + (1 - \beta) (\nabla f(x_t))^2 \\ x_{t+1} &= x_t - \alpha \frac{v_{t+1}}{\text{cache}_{t+1} + \varepsilon}\end{aligned}$$

Actually, that's not quite Adam.

Adam full form involves bias correction term. See <http://cs231n.github.io/neural-networks-3/> for more info.



# Comparing optimizers



source:

<https://joshvarty.com/2018/02/27/ltn-7-a-quick-look-at-tensorflow-optimizers/>





**Andrej Karpathy** ✓

@karpathy



3e-4 is the best learning rate for Adam, hands down.

6:01 AM · Nov 24, 2016 · [Twitter Web Client](#)

**108** Retweets **461** Likes



**Andrej Karpathy** ✓ @karpathy · Nov 24, 2016



Replying to [@karpathy](#)

(i just wanted to make sure that people understand that this is a joke...)



9



3



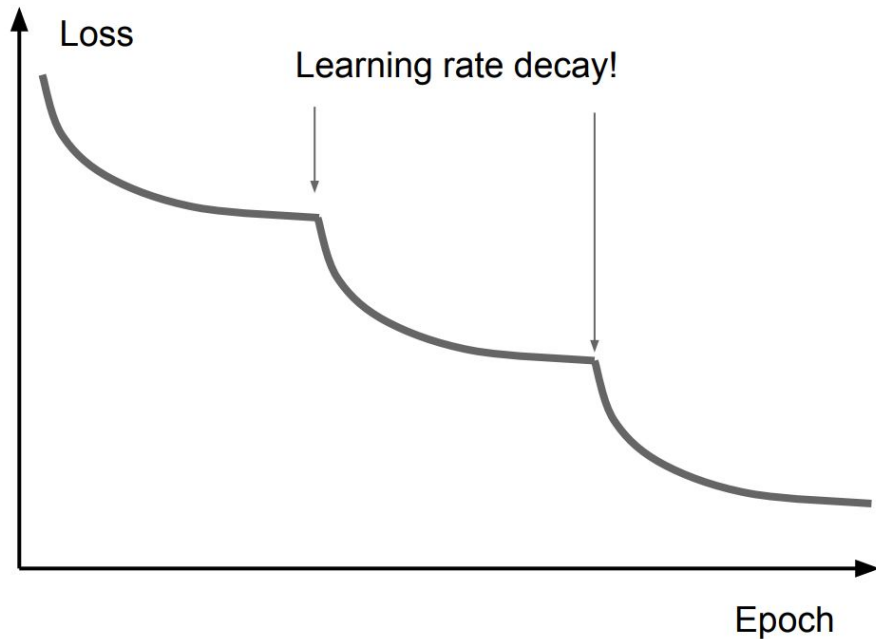
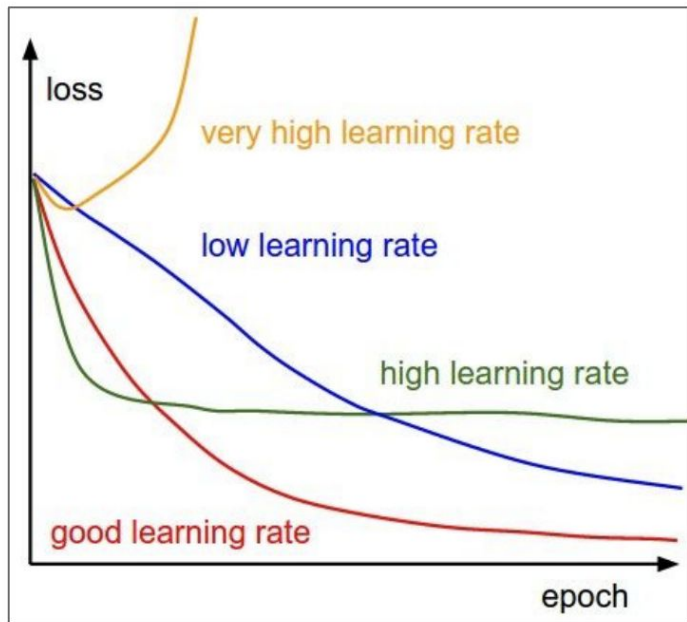
119



source: <https://twitter.com/karpathy/status/801621764144971776>



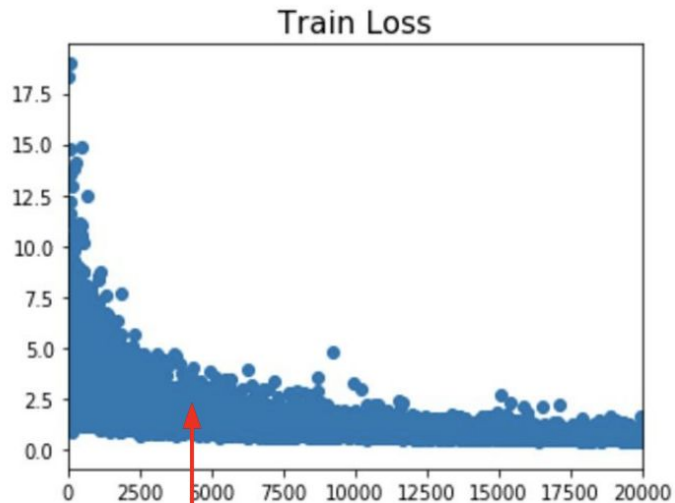
# Once more: learning rate



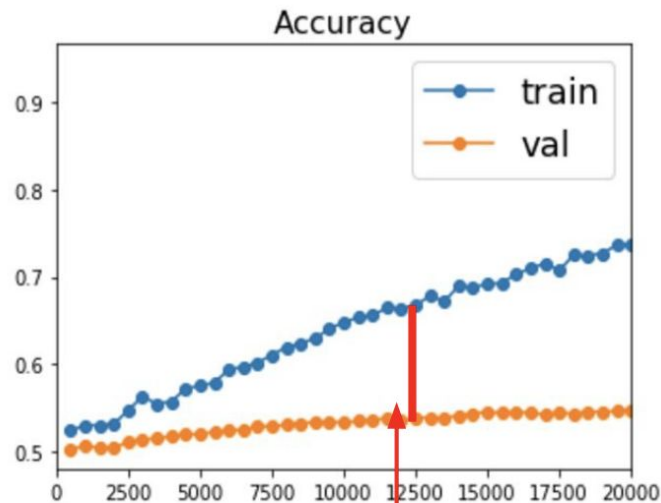
# Sum up: optimization



- Adam is great basic choice
- Even for Adam/RMSProp learning rate matters
- Use learning rate decay
- Monitor your model quality

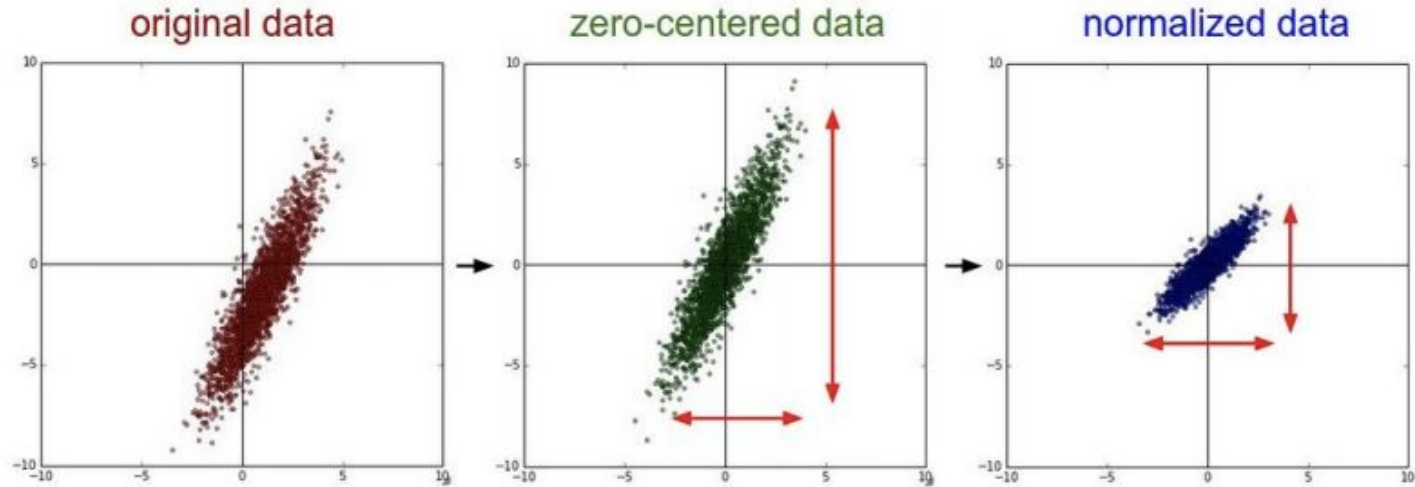


Better optimization algorithms  
help reduce training loss



But we really care about error on new  
data - how to reduce the gap?

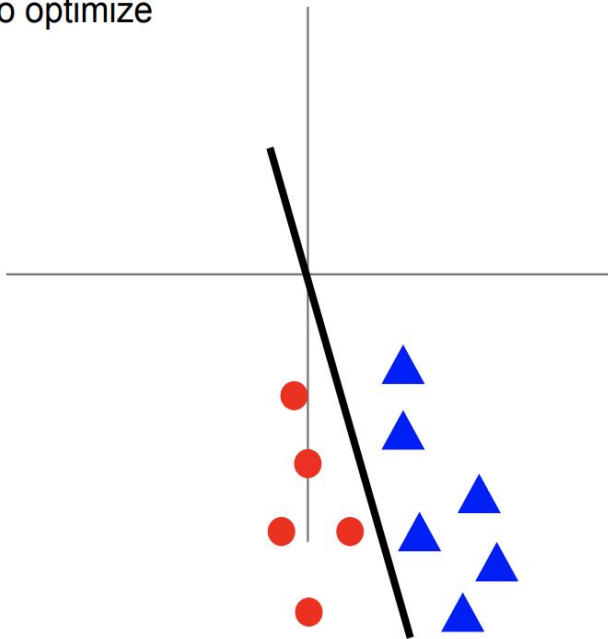
# Data normalization



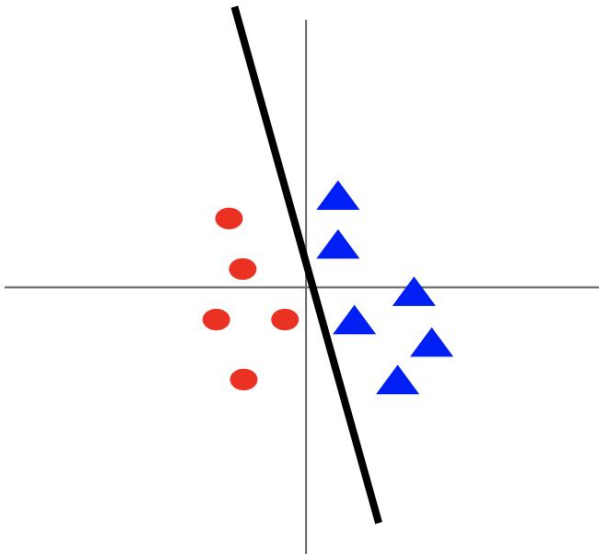


# Data normalization

**Before normalization:** classification loss  
very sensitive to changes in weight matrix;  
hard to optimize



**After normalization:** less sensitive to small  
changes in weights; easier to optimize



# Weights initialization



- Pitfall: all zero initialization.

# Weights initialization



- Pitfall: all zero initialization.
- Small random numbers.





# Weights initialization

- Pitfall: all zero initialization.
- Small random numbers.
- Calibrated random numbers.

$$\text{Var}(s) = \text{Var}\left(\sum_i^n w_i x_i\right)$$

$$= \sum_i^n \text{Var}(w_i x_i)$$

$$= \sum_i^n [E(w_i)]^2 \text{Var}(x_i) + E[(x_i)]^2 \text{Var}(w_i) + \text{Var}(x_i) \text{Var}(w_i)$$

$$= \sum_i^n \text{Var}(x_i) \text{Var}(w_i)$$

$$= (n \text{Var}(w)) \text{Var}(x)$$

# Thanks for attention!

Questions?

