

Autoencoders

Denote \mathbf{z} as encoded with encoder E input \mathbf{x}

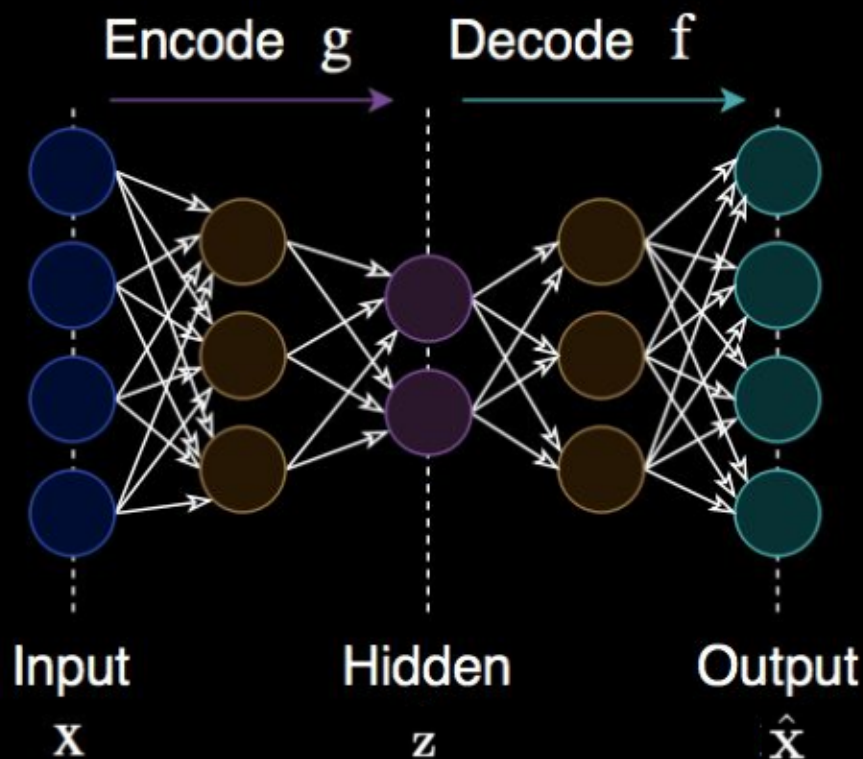
$$\mathbf{z} = E(\mathbf{x}, \boldsymbol{\theta}_E)$$

Decoder D recovers \mathbf{x} from latent representation

$$\hat{\mathbf{x}} = D(\mathbf{z}, \boldsymbol{\theta}_D)$$

Optimal parameters learned w.r.t. loss function L

$$[\boldsymbol{\theta}_E, \boldsymbol{\theta}_D] = \arg \min L(\hat{\mathbf{x}}, \mathbf{x})$$



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Simple example: PCA

Optimal parameters learned w.r.t. loss function L

$$[\boldsymbol{\theta}_E, \boldsymbol{\theta}_D] = \arg \min L(\hat{\mathbf{x}}, \mathbf{x})$$

PCA performance on MNIST



16 components

Convolutional performance on MNIST



7 x 7 latent space

- **One-hot vectors:**



Problems:

- Huge vectors
- VERY sparse
- No semantics or word similarity information included

Distributional semantics

Does vector similarity imply semantic similarity?

“You shall know a word by the company it keeps”

Firth, 1957

context input context

| | | | | | |
|-----|--------|-----|--------|----|----|
| The | fluffy | dog | barked | as | it |
|-----|--------|-----|--------|----|----|

chased a cat

context input context

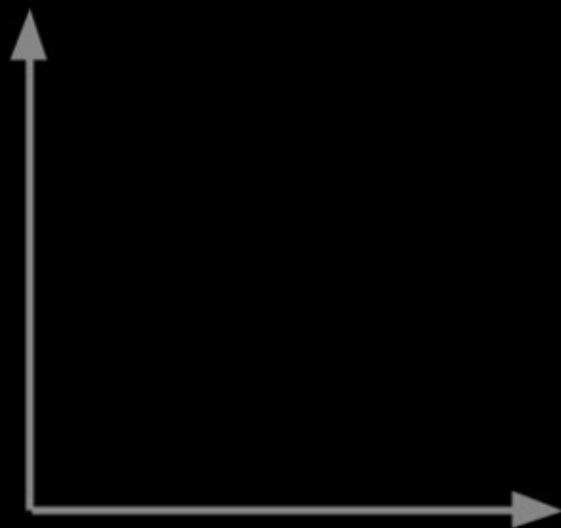
| | | | | |
|--------|-----|--------|----|----|
| fluffy | dog | barked | as | it |
|--------|-----|--------|----|----|

The chased a cat

Why not to learn word vectors?

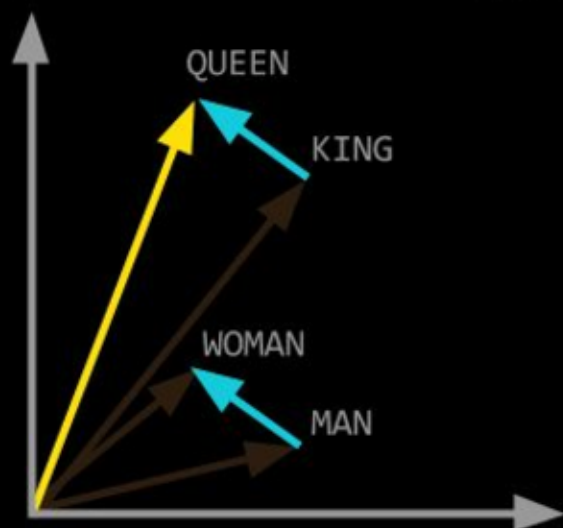
Embeddings: intuition

What is $\text{king} - \text{man} + \text{woman}$?

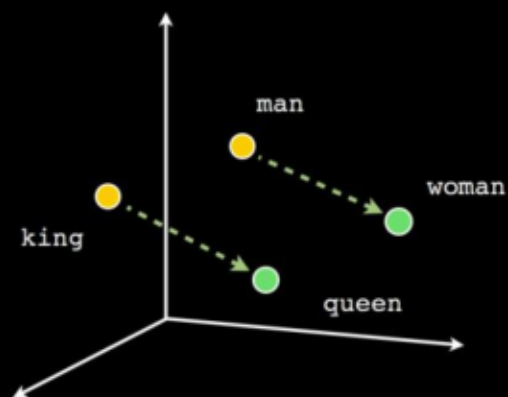


Embeddings: intuition

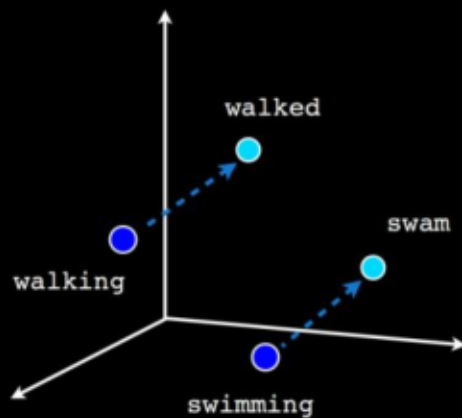
So $\text{king} - \text{man} + \text{woman} = \text{queen!}$



- **Word2vec** (Mikolov et al. 2013) - a framework for learning word embeddings



Male-Female



Verb tense

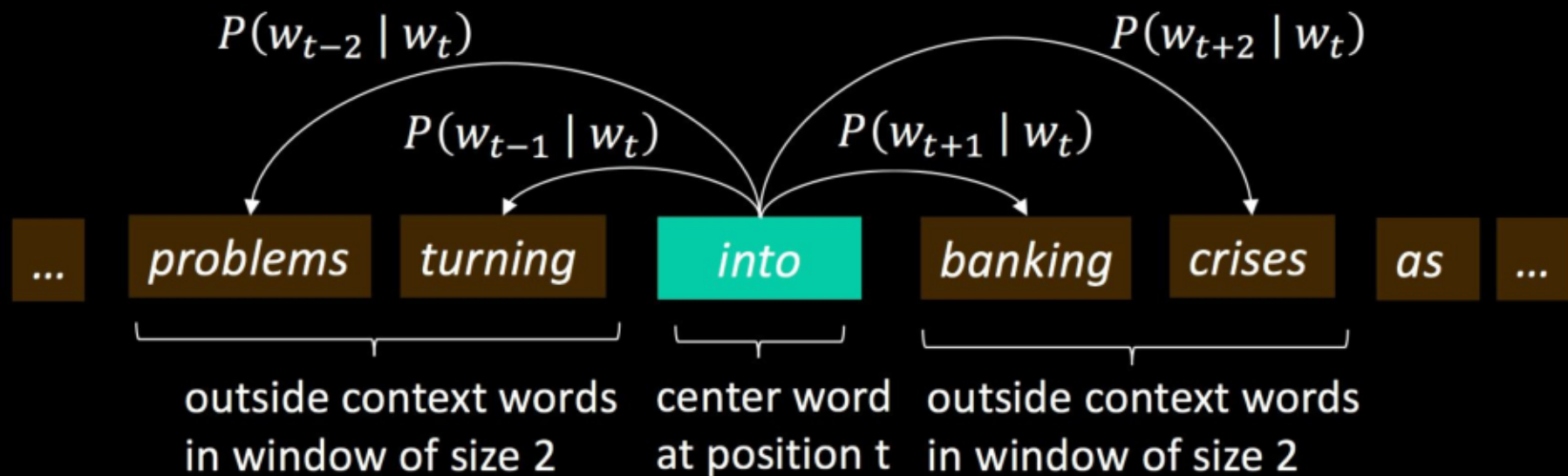


Country-Capital

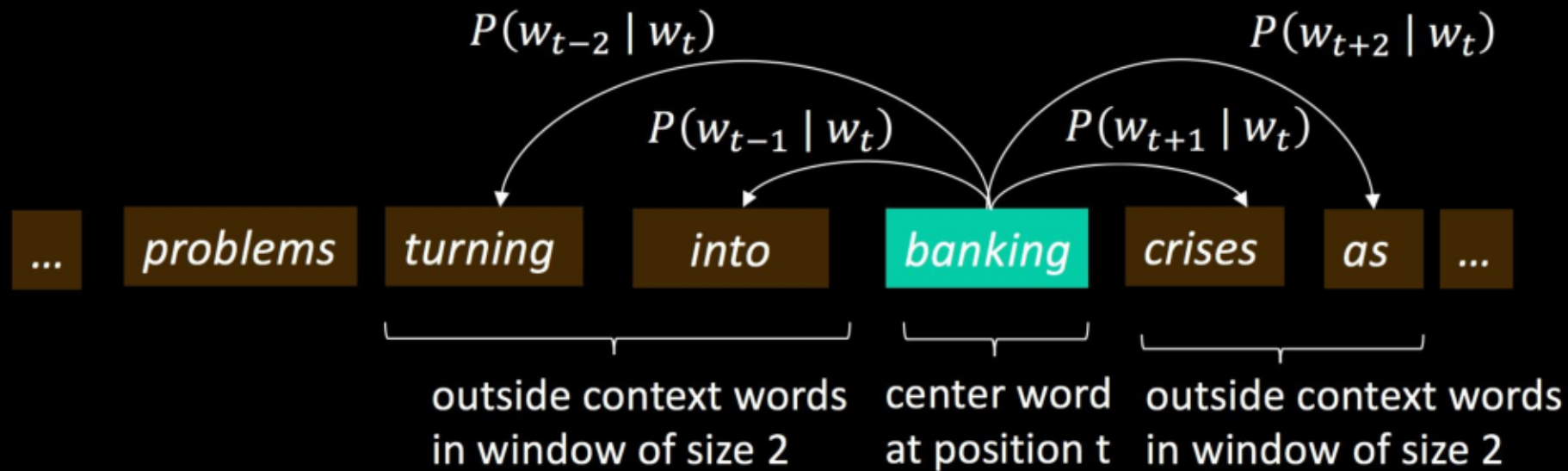
Embeddings: word2vec

| Source Text | Training Samples |
|--|--|
| <div>The quick brown fox jumps over the lazy dog.</div> <div>The quick brown</div> <div>→</div> | (the, quick) (the, brown) |
| <div>The quick brown fox jumps over the lazy dog.</div> <div>The quick brown fox</div> <div>→</div> | (quick, the) (quick, brown) (quick, fox) |
| <div>The quick brown fox jumps over the lazy dog.</div> <div>The quick brown fox jumps</div> <div>→</div> | (brown, the) (brown, quick) (brown, fox) (brown, jumps) |
| <div>The quick brown fox jumps over the lazy dog.</div> <div>The quick brown fox jumps over</div> <div>→</div> | (fox, quick) (fox, brown) (fox, jumps) (fox, over) |

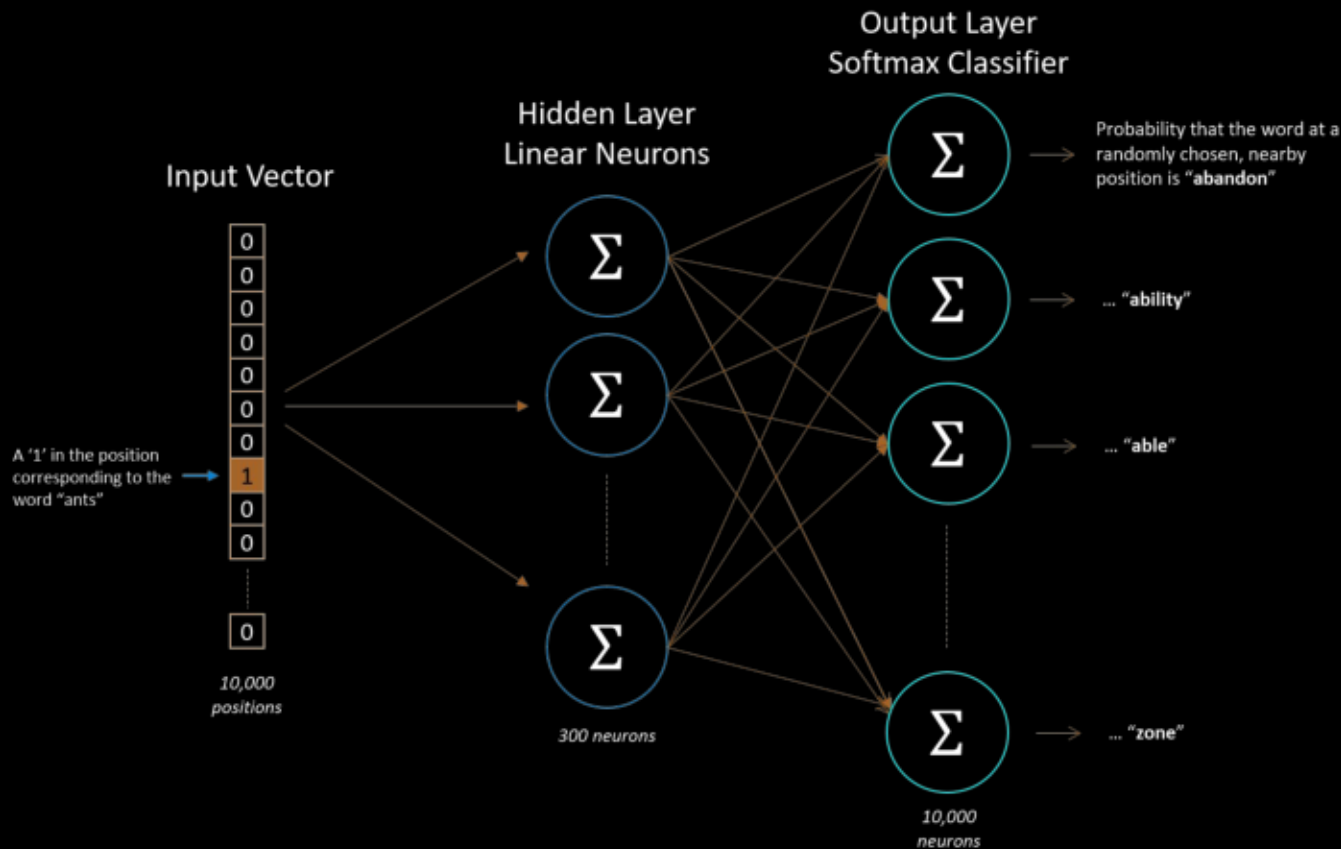
Embeddings: word2vec



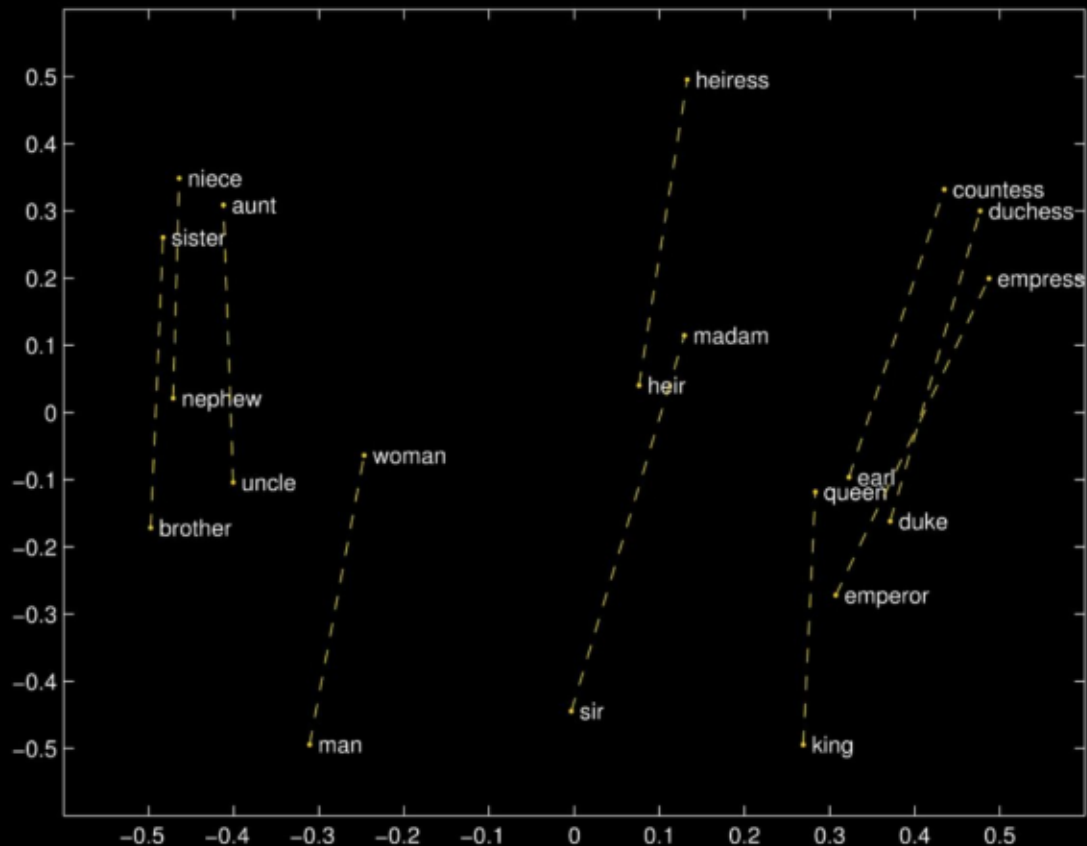
Embeddings: word2vec



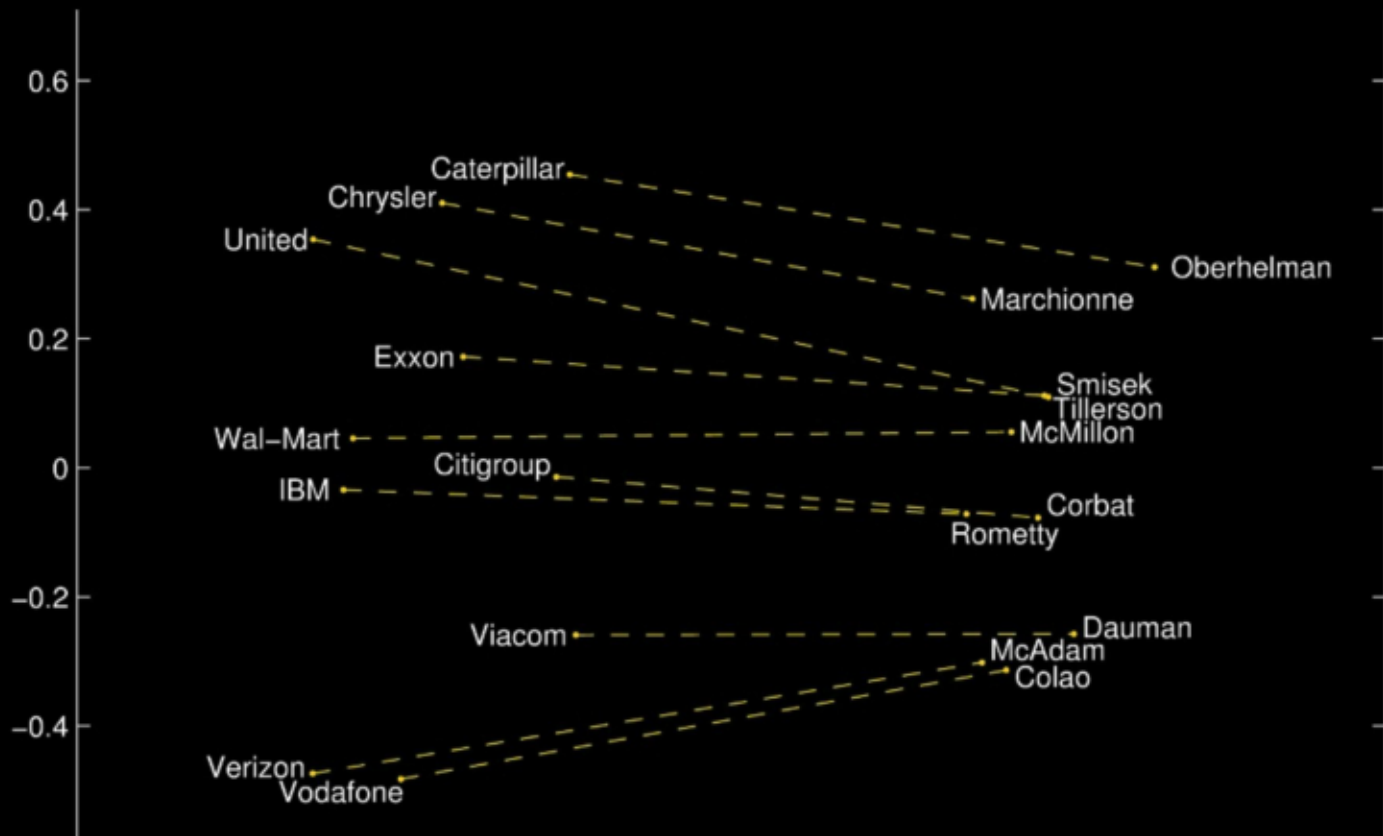
Embeddings: word2vec



GloVe Visualizations



GloVe Visualizations: Company - CEO



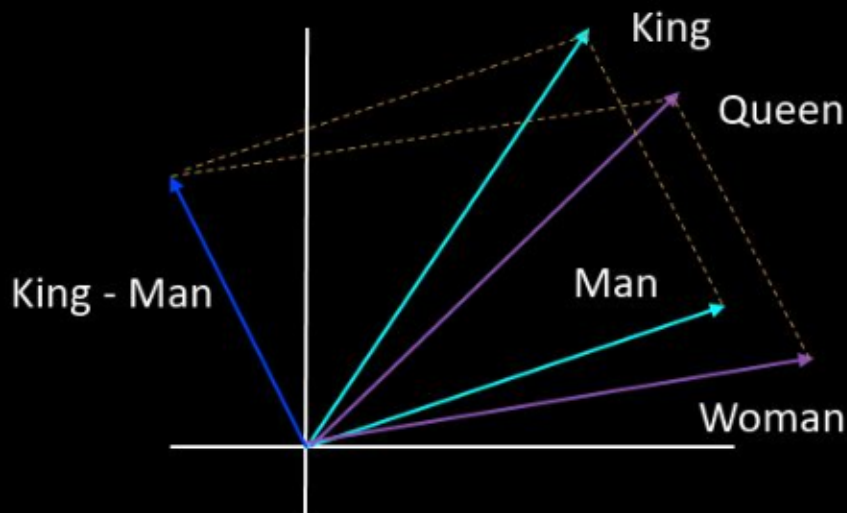
Word2vec: word analogies

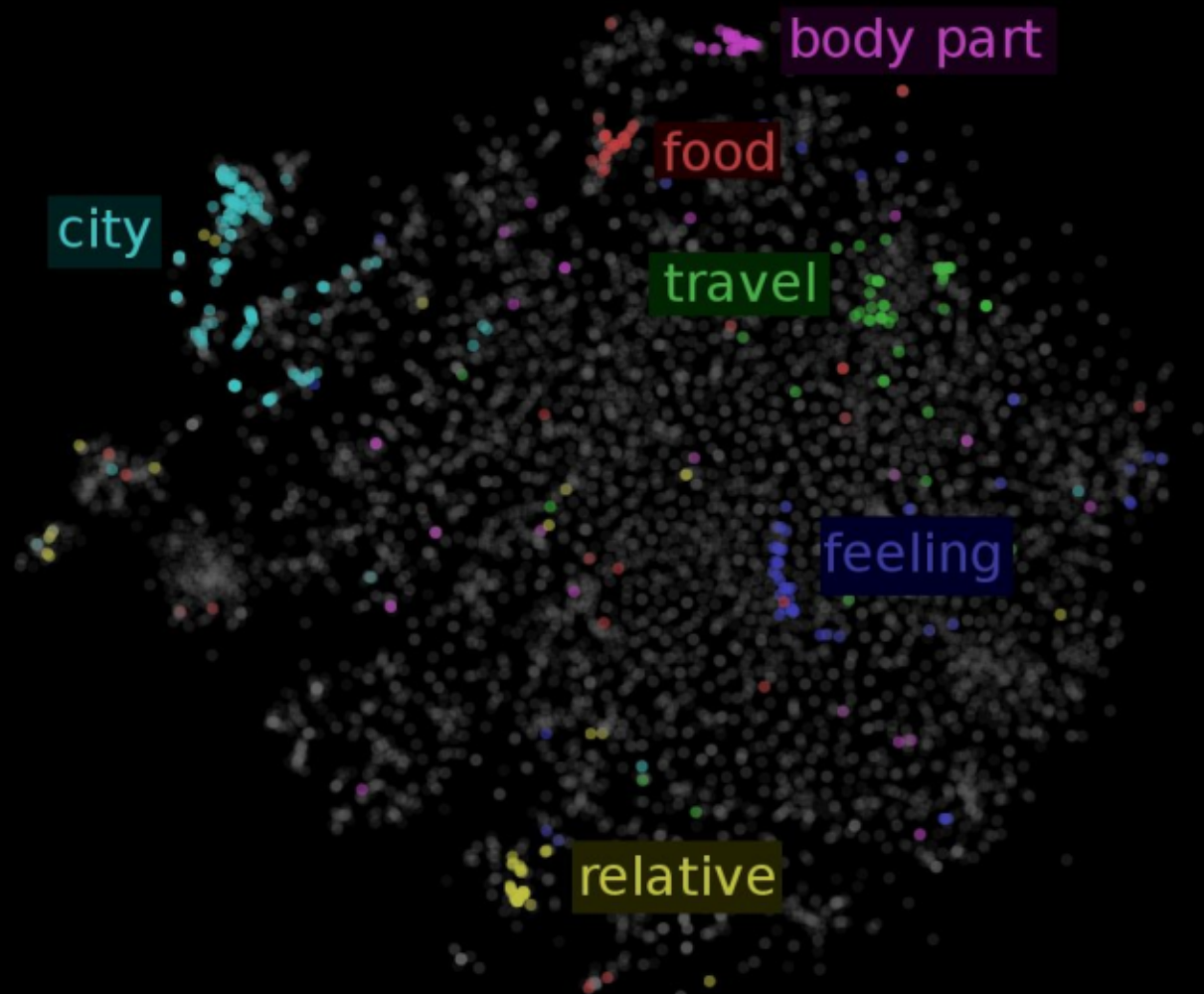
King - man + woman = queen

↓ ↓ ↓ ↓

x y y' $target$

$\cos(x - y + y', target) \rightarrow \max_{target}$





- Use statistics:
 - T-criterion

$$t = \frac{\overline{x} - \mu}{\sqrt{\frac{s^2}{N}}}$$

H_0 : 'social media' occurs with probability:

$$\mu = P(\text{social})P(\text{media}) = \frac{C(\text{social})(\text{media})}{N^2}$$

H_a : 'social media' does not occur with such a probability

- Use statistics:
 - Chi-squared

$$\chi^2 = \sum_{ij} \frac{(O_{ij} - E_{ij})^2}{E_{ij}}$$

$$E(\text{social media}) = \frac{C(\text{social})}{N} \cdot \frac{C(\text{media})}{N} \cdot N$$

O_{ij} from table

| | w1 = social | w1 != social |
|--------------------|---------------------------------------|---|
| w2 = media | C(social media) | C(x media) where x could be any word |
| w2 != media | C(social x) where x could be any word | C(any pair not starting with social or ending with media) |