



Study and development of a solidification model using CFD

MASTER FINAL THESIS

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UNIVERSITAT POLITÈCNICA DE
CATALUNYA

MASTER THESIS

**Study and development of a
solidification model using CFD**

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for the degree of Master Thesis*

in the

Research Group Name

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de Barcelona

June 20, 2022

Declaration of Authorship

I, Aitor BAZÁN ESCODA, declare that this thesis titled, "Study and development of a solidification model using CFD" and the work presented in it are my own. I confirm that:

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Abstract

Faculty Name

Escola Tècnica Superior d'Enginyeria de Camins, Canals i Ports de
Barcelona

Master Thesis

Study and development of a solidification model using CFD

by Aitor BAZÁN ESCODA

Phase change materials (PCMs) are of great interest within the automotive industry field. Not only when used in thermal management applications but also in different areas where these materials are of vital importance for both a safe and comfortable driving. For such objective, the present project arises from the idea of understanding solidification processes in windshield washer tanks. In this context, this master's thesis produces a comprehensive state of the art of some of the current numerical methods to effectively represent water solidification.

An OpenFOAM 21.12. solver based on a multi-phase solver, multi-component incompressible solver based on a volume of fluid method is adapted to deal with diffusive-convective phase change. So as to reach this goal, an implementation of the enthalpy-porosity technique is carried out. The work of Voller et al. is closely followed, and a detailed explanation of the used equations and the assumptions taken is given. Validation of the model is accomplished by comparing the results with the authors in Bourdillon and Kowaleski and Rebouw.

On a second stage, a 2D semi-empirical model based on the work of Lee is adapted to account for the nucleation characteristics during the process of the water phase change. Validation of the model is done by comparing the obtained results to Neumann solutions for classical Stefan problem.

Finally, the current work is extended to couple a fluid region in which the liquid undergoes a phase-change and a solid region. This is done in the context of a conjugate heat transfer environment.

Keywords: PCMs, multiphase, Enthalpy-porosity technique, Lee model, Stefan problem, conjugate heat transfer, OpenFOAM.

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Chapter 1

Introduction

1.1 Thesis Statement. Background and motivation

During the last decade, the use of phase change materials has been growing in the automotive industry.

These substances release or absorb large amounts of latent heat when they go through a change in their physical state, as the material reaches its specific phase change temperature. Thus, in the process of latent heat release or absorption, the temperature of the PCM remains constant. Therefore, PCMs are considered to be efficient in terms of thermal storage.

On the other hand, the use of these materials is not exclusive for thermal management. It is of relevant importance when used in conjunction with soap in the windshield wiper system of the car. In such zone, problems involving solidification are of considerable relevance. And this is mainly due to a volumetric expansion originated by the thermal effects within the PCM which at its turn, generates stresses in the polymeric tank in which is bottled up.

Therefore, this master's thesis main objective aims to study different numerical techniques to represent solidification process and, specially, pure water phase change. This is accomplished by first implementing an enthalpy-porosity technique within the frame of a multi-phase incompressible solver based on volume-of-fluid (VOF) method for interface tracking. The objective of this first stage is to apply sensible and latent heat as source terms in the energy equation. On a second term, a 2D semi-empirical model based on the work of Lee is adapted to account for the nucleation characteristics occurred during the water phase transition.

The final stage of this thesis is devoted to an implementation of a multiregion solver to calculate conjugate heat transfer problems between solid and fluid zones with the singularity of being, the fluid zone, capable of handling phase change materials.

So as to clarify the steps followed during the thesis, a *conceptual map* is presented below:



FIGURE 1.1: Workpath for buoyancy effects study.

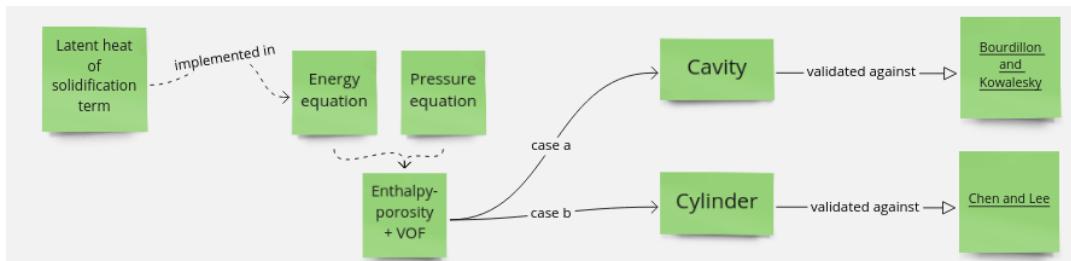


FIGURE 1.2: Workpath for latent heat implementation in Enthalpy-porosity model.

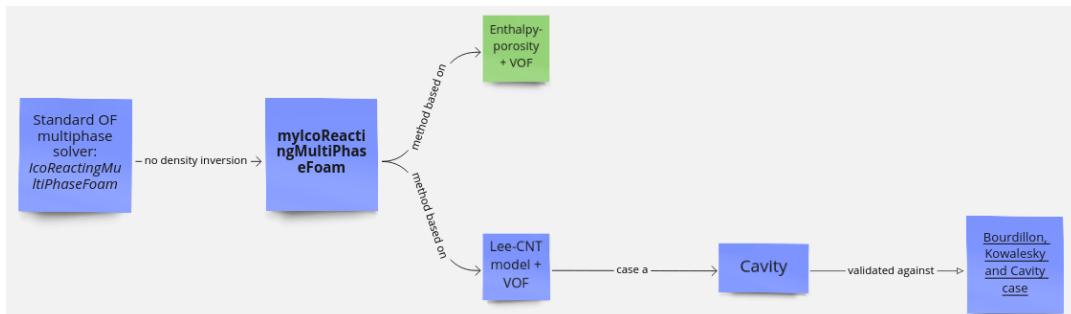


FIGURE 1.3: Workpath for nucleation theory implementation in Lee model.

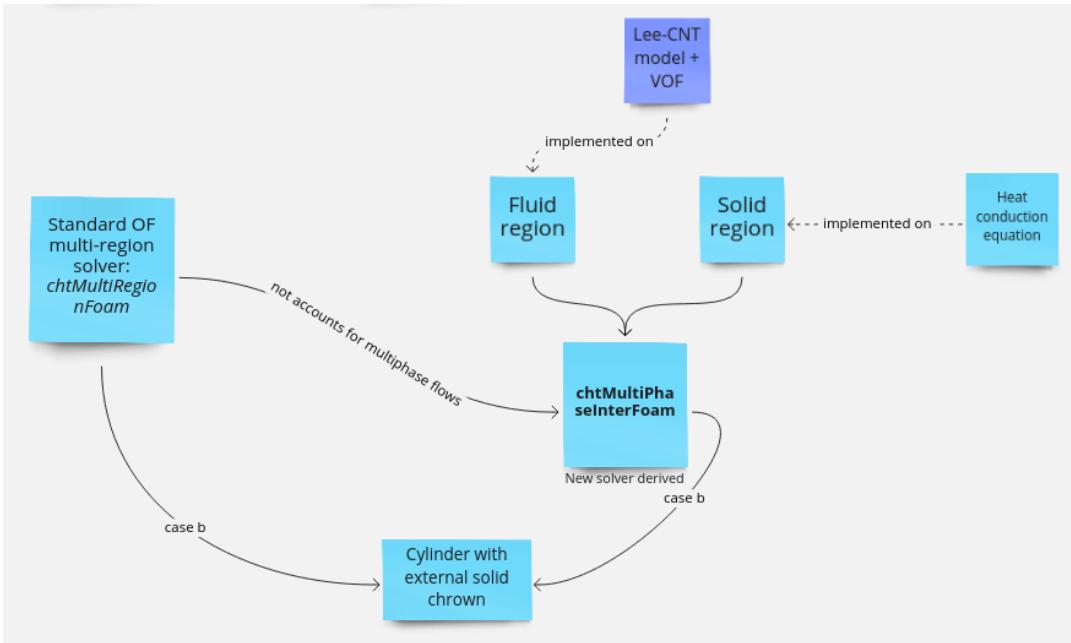


FIGURE 1.4: Workpath for conjugate heat transfer implementation.

The next chapters are mainly focused on describing phase-change phenomena and heat transfer mechanisms used along the completion of this master's thesis.

1.2 Phase-Change Process

The phase-change is usually modelled by a sudden change in enthalpy per unit of temperature generated within a narrow temperature range near the freezing point. Often, this process is assumed to behave in a characteristic temperature, as shown in Fig. 1.1, leading to a moving boundary problem. However, at a given critical temperature, both fluid and solid phases may coexist giving a state called mushy region. In this case, one speaks of a non-linear diffusion problem rather than a moving boundary problem [13].

As briefly introduced, two types of phase-change are used to describe the way the latent heat is released or absorbed during freezing or melting processes:

- **Non-isothermal phase-change:** the phase-change takes place within a temperature range yielding a transition zone between a solid and a liquid phase called mushy zone. Typically, the thickness of this region is straightfully proportional to the temperature range in which the phase-change occurs.
- **Isothermal phase-change:** the phase-change is arisen instantaneously at the melting temperature. The release or absorption of the latent heat occurs at this point in which, consequently, there is no transition zone between solid and liquid phases. At this point, there is a narrow line,

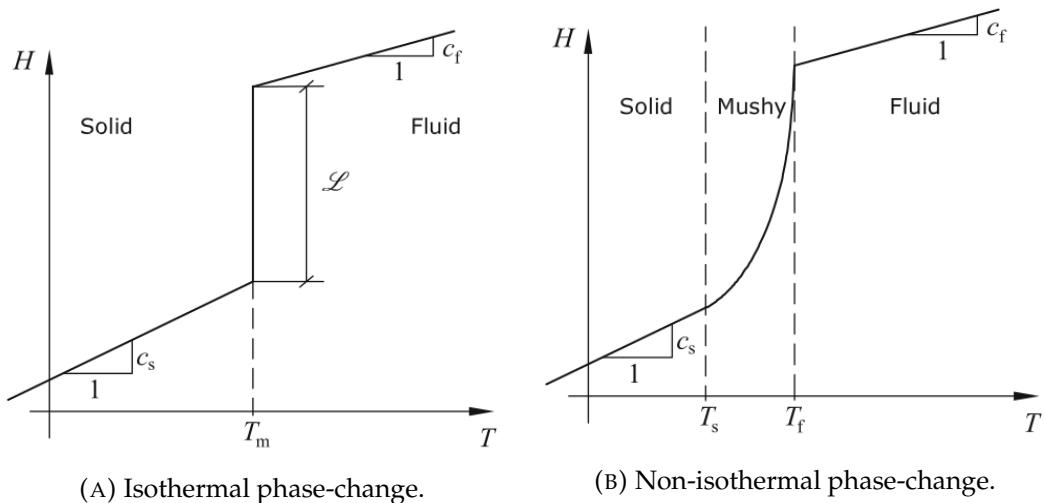


FIGURE 1.5: Phase-change comparison.

mainly derived from the discretization of the computational domain, characterizing the phase-change phenomena.

As an important remark, when the mushy region is sufficiently narrow, the isothermal assumption is usually a good approximation. However, despite of the fact of being a convenient approach it may lead to significant complication when it comes to numerical solution techniques.

Along the next chapters, a more detailed description on existing techniques that deal with such non-trivial phenomena will be given.

1.2.1 Water phase-change

In a similar manner, the water phase-change takes place. A complex interaction of the molecular forces generate water to behave in a curious way when it gets frozen into ice. The vast majority of substances, when they are cooled, become more dense in the frozen state than when liquid. However, when cooled under a specific temperature, water begins to expand and, once it starts freezing, it becomes less dense than water.

1.2.2 Phase diagram of ice

Ice crystals undergo different kinds of structures. Called ice Ih, in the form of hexagonal ice and, manifested in six cornered snow flakes, is the natural ice found in earth. However, at lower pressures below 2 kbar, many other ice structures may exist.

The ice phase diagram shown below, points out the conditions of stability for all ice phases. As it is cleared out, the line between the water and ice Ih is an equilibrium line with a negative slope, consequence of having, the solid, lower density than the liquid. These equilibrium lines extend in the form of metastable phase boundaries into the area of stability of other ice phases.

Although there are at least 11 crystalline ice shapes, the only which is found naturally on earth is the hexagonal form.

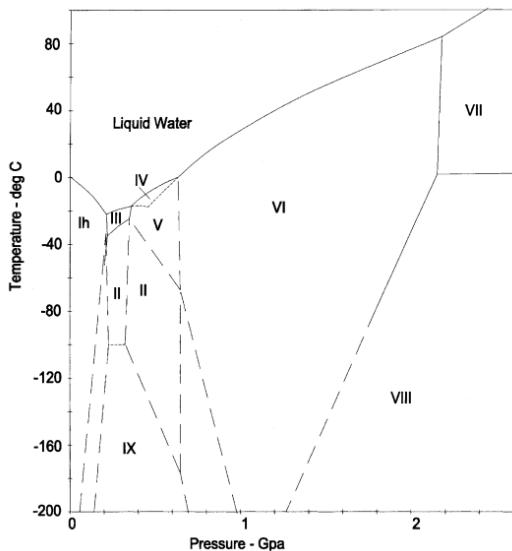


FIGURE 1.6: Phase diagram of ice.

As a remark, the implication that there is a rise on the pressure would not propitiate ice formation at 0°C, instead water would need to be cooled down.

1.2.3 Properties of ice

Ice, when subjected to visible light conditions, is transparent and has the lowest index of refraction for the sodium spectrum of any known crystalline material, as pointed out by Akyurt et al. [1].

Mechanically, ice behaves like a viscoelastic material with a non linear law. Polycrystalline ice subjected to stress, deforms elastically, followed by a transient creep and finally, a secondary creep in the form of steady viscous flow is obtained.

As pointed out in Akyurt et al. [1], the surface of ice Ih near the melting point has many dangling broken bonds that boost the presence of a liquid-like layer and as a consequence, low friction on such surface. Variation of density of ice with phase at 110 K is described in the table shown below.

1.2.4 Freezing phenomena

Time-temperature diagram for freezing of pure water (ABCDE) and aqueous solutions (AB'C'D'E') show the physical process that occurs during the solidification. The first stage, from A to B, belongs to undercooling, also called supercooling, and it is arisen below the freezing point T_f , which is equal to the melting point, T_m . This point is referred to a non equilibrium point and it is analogous to an activation energy necessary for the nucleation process. Before nucleation process, pure water may need to be cooled down several degrees. At point B, the system nucleates and releases its latent heat faster

Phase of ice	Density (Mg/cm^3)
Ih	0.93
II	1.18
III	1.15
IV	1.27
V	1.24
VI	1.33
VII	1.56
VII	1.56
IX	1.16
X	2.51

TABLE 1.1: Variation of ice density for every phase at 110K.

than the heat which is being removed from itself.

From C to D, the horizontal axis shows the evolution of the crystal growth in time. At C, there exists the nucleation point and, from there through D, latent heat gets removed out of the system at constant temperature. In this way, the mixture, which is in a partially frozen state, does not cool until all the potentially freezable water has crystallized.

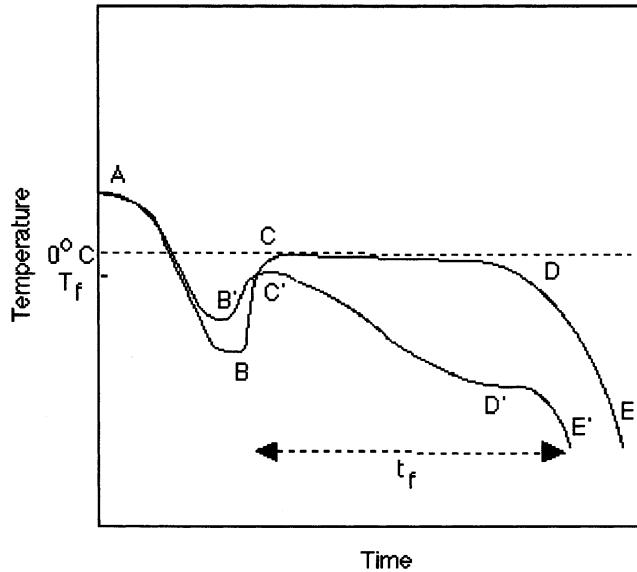


FIGURE 1.7: Process of crystallization of water.

1.3 Mechanisms of Heat Transfer. Heat convection

Convective heat transfer usually occurs in fluids due to the microscopic motion of the particles commonly understood as the bulk fluid motion.

Depending on the force originating such motion, one can distinguish two types of convection: natural convection and forced convection. Natural convection, the phenomena presented in this thesis, is originated due to differences of temperature gradients. These gradients, in the presence of the gravitational field, allow density to change within the fluid field. At the same time, the fact that density changes, enhance the rise of the colder liquid in contrast with the warmer which tends to sink thus, generating a motion in the fluid. On the other hand, the forced convection is driven by external sources which enforce the motion. In this case, buoyancy is not that relevant as it is for the first kind of convection.

In order to model the convection heat transfer in an object, the Newton's cooling law is typically used. As presented in Equation 1.1:

$$\frac{dQ}{dt} = hA (T_s(t) - T_\infty) \quad (1.1)$$

where Q is the heat source (thermal energy), T_s is the temperature on the surface of the object, T_∞ the temperature far away from the object, h is the heat transfer coefficient and A the heat transfer surface area.

The equation states that the rate of heat loss is proportional to the temperature difference between the object itself and the medium by which is surrounded.

The process of water freezing in enclosures is common in engineering. When there exist temperature gradients within the liquid phase in the process of

solidification, a natural buoyancy driven flow is initiated and such behavior is determined to affect the shape of the liquid/solid interface as well as the progress of solidification.

Indeed, these temperature differences in the liquid cause density variations so that the natural motion occurs. Boussinesq approximation can be validly used for fluids whose density varies linearly with temperature. However, pure water exhibits a maximum in its density when it ranges between 0°C and 4°C. Beyond this last temperature, and known as density inversion point, density decreases in a nonlinear manner as the temperature passes through the freezing point. In convective heat transfer, surroundings of the temperature where the aforementioned maximum happens to be, behave in a complex manner leading to fully control the process of growth of the solid phase.

1.4 Conjugate Heat Transfer. Heat conduction

The alternative heat transfer mechanism is heat conduction which usually happens at molecular level in where the energy is transferred from particles with high energetic levels to lower energetic particles. The equation driving the conductive heat transfer is commonly known as the Fourier's law and it reads as:

$$q = -k\nabla T \quad (1.2)$$

where q is the heat transfer per unit of area, κ is the thermal conductivity of the material and ∇T is the gradient of temperatures within the studied bodies.

Alongside, conjugate heat transfer, the phenomena studied in the last part of this thesis, is referred to the heat transfer between solids and fluids. Heat transfer in fluids is occurred mainly through a combination of two mechanisms: convection, due to a random motion of particles (diffusion) and advection, due to the bulk motion of the fluid. On the other hand, heat transfer in solids is mainly driven by conduction which accounts for the vibration and collision of the particles forming the solid.

Chapter 2

Numerical Methods for Phase-Change Phenomena

2.1 State of Art. Numerical Methods

Considering the PCM density as constant in the model might be thought as a reasonable assumption in some cases, in others where thermo-mechanical coupling between the fluid and its container is intended, it makes impossible to account for some physical behaviors which may result from expansion or contraction during the phase change of the material. However, the main goal of this thesis is not to present a method that represents thermo-mechanical coupling but a technique that ensures volume expansion due to density changes through the fluid domain. To reach this point, it is important to point some of the numerous researches that have been conducted in order to investigate the problem of solidification and melting.

At the present, the main used numerical methods representing the treatment of liquid-solid phase change are divided into these categories:

- **Front tracking method,**
- Volume-of-fluid method,**
- Level set method,**
- **Enthalpy method,**
- **Phase field method.**

2.1.1 Front tracking method

Several studies are carried out with this method. Juric et al. [11], presented a front-tracking method based on a finite difference approach of the heat equation and an explicit tracking of the fluid-solid interface to simulate time dependent two-dimensional dendritic solidification of pure substances. In similar fields, Al-Rawahi et al. [17] underwent also simulations of dendritic growth of pure substances by using front-tracking methods in which the

fluid-solid interface was tracked explicitly and the release of latent heat during solidification was calculated with the normal temperature gradient near the interface. Garimella et al. [14] proposed an explicit interface-tracking scheme involving reconstruction and advection of the moving interface in a fixed grid to solve moving-boundary problems associated with phase-change phenomena. As they describe, the movement of the interface is tackled first by advection and tracking of the interface, later by the calculation of normal velocities near the interface region and finally, by solving the governing equations for the existing phases.

Volume-of-fluid method

Initially introduced by Harlow et al. [7], a technique called the marker and cell method tracked the interface by weightless particles which were transported convectively by the velocity of the fluid. Cells that were filled with marked particles were considered occupied by the fluid while, contrarily, those which were not filled with marked particles were not occupied by fluid. Later in time, the idea was extended to track the interface based on phase fractions in the volume-of-fluid method which is discussed in detail below.

Level set method

In the field of the current technique, Tan et al. [21] conducted a level set method combining properties of both fixed domain and front-tracking methods to model the microstructure evolution in multi-component alloy solidification. Phase interface is tracked by solving the multi-phase level set equations. From this tracked interface, a diffused one is constructed by means of the level set functions. Volume-averaging methods are latter used to solve energy, species and momentum equations. Rauschenberger et al. [16] pursued a comparative assessment between a Level set approach and a volume-of-fluid method to track interfaces in the context of dendritic ice growth in supercooled water. The Level Set method is used as an implicit tracking of the moving boundary.

2.1.2 Enthalpy method

In 2004, Esen et al. [6] worked out an enthalpy method based on finite difference approximations applied to the Stefan problem. An enthalpy function is defined representing the total heat content per unit of mass of the material. The need of tracking the interface between the fluid and the solid phase is thereby removed when using such formulation. El Ganaoui et al. [5] presented an enthalpy-porosity formulation on a fixed grid framework for liquid-to-solid phase transition. The method is extended to solve time-dependent solutal convection in the melt during directional solidification that undergo the majority of alloys. Within the alloy research field, Voller et al. [24] developed an enthalpy fixed grid method for dendritic growth modeling in under-cooled binary alloys. This method is devoted to couple

explicit finite differences expressing the conservation of enthalpy and solute to an iterative scheme which enforces node-to-node consistency between solute, liquid-fraction, enthalpy and under-cooling interface.

2.1.3 Phase field method

Emerged as an approach to model and predict mesoscale morphological and microstructure evolution in materials, Chen et al. [4] reviews some phase-field models used to describe various materials processes including solidification, crack propagation and dislocation microstructures among others. This paper describes the capability of phase-field methods to predict the evolution of arbitrary morphologies and complex microstructures without explicitly tracking the evolution of the interface.

2.2 Solidification methods

The challenge of a numerical investigation of a solidification process is to capture the free surface for the flow of the phase change material and, at the same time, account for the moving boundary induced by the phase change within the PCM. The free surface may be handled by the volume-of-fluid (VOF), originally introduced by Hirt and Nichols [8]. VOF relies on the definition of a transport indicator function within the finite volume method's framework. Simultaneously, and in order to account for the phase changes, some of the used models are based on meso-scale. This is the phenomena occurring between microscopic and continuum length scales and, in the current context, the complex micro structure generated during the solidification is approximated as liquid, mushy (intermediate state), and solid regions. Mushy region is thereby described as an averaged value of the liquid and solid properties. One of the most used methods is the enthalpy-porosity technique, originally developed by Voller and Prakash [23], which uses the typical conservation equations on a fixed Eulerian grid. The main concepts underlying such method are: on the one side, an additional source term to the energy conservation equation is applied to describe the release of latent heat. On the other side, the solidification effects on the mass transport are modelled as a porosity variable and this is introduced as a Darcy-type source term to the momentum equation.

Some of the studies found on this topic, the coupling of both VOF and enthalpy-porosity methods are mainly related to casting processes. Rösler and Brügmann [19] introduced a numerical model for a solid-liquid phase change inside a latent heat thermal energy storage. Richter et al. [ref] worked out a method for the simultaneous mould filling and solidification process which settles the developing of free surface flow and the liquid-solid phase transition under the volume-of-fluid and enthalpy-porosity methods. However, no adaptation of these methods to purely solidification processes has been found. Therefore, and, the objectives of this research are:

- To introduce a new solver based on the coupling of VOF and enthalpy-porosity techniques which covers the relevant physical effects during the process of solidification.
- To validate simulation results by using benchmark cases found in the literature.

Numerical methods commented are briefly described next.

On the other hand, semi-empirical methods ...

2.2.1 Volume-of-Fluid Method: General Aspects

The Volume-of-fluid method (VOF) is a numerical method based on an Eulerian approach to track the free surface in a two-phase flow. The VOF method, developed by Hirt and Nichols in 1981, [8], takes relevance when fluids co-exist with other phases. An example could be the ice (solid phase) advancing front within the liquid phase. The surface in between both phases needs to be solved by means of the volume of fluid technique.

This is sometimes seen as the conservation of the mixture components along the path of a fluid region. The equation which allows that is described as:

$$\frac{\partial \alpha_{\text{phase}}}{\partial t} + \frac{\partial (\alpha_{\text{phase}} u_j)}{\partial x_j} = 0 \quad (2.1)$$

In which α_{phase} corresponds to the phase fraction and it applies

$$\alpha_{\text{phase}} = \begin{cases} 0 & = \text{solid PCM} \\ 0 < \alpha_{\text{phase}} < 1 & = \text{cell contains the interface} \\ 1 & = \text{liquid PCM} \end{cases} \quad (2.2)$$

As Eq. 2.1 exposes, the principle that lies behind the method is the definition of the phase field (α), which has a value between '0' and '1'. The value of '1' corresponds to any point filled with fluid and zero otherwise. Thus, the average value of α in a cell indicates the fractional volume of that cell occupied by the fluid. Consequently, if a cell has an average value of $\alpha = 1$ implies a fully filled cell of fluid and oppositely, a value of $\alpha = 0$ means that the fluid is not present in the cell. However, a cell presenting an average value between 0 and 1 would lead the presence of an interface in that region as it is clearly seen in Fig. 2.1. Near the interface, it clearly exists a jump in the fluid proper-

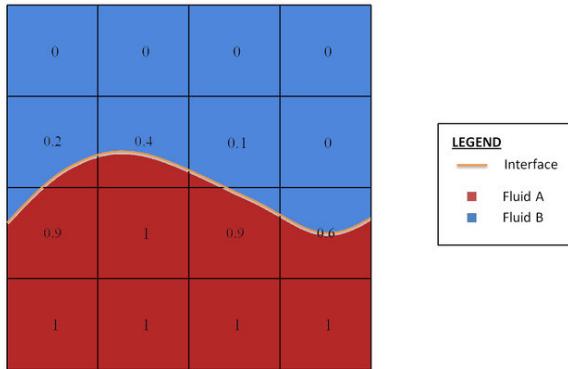


FIGURE 2.1: Volume-of-fluid approach.

ties that need to be corrected by properly averaging phase properties in that region.

In the present study, this method is used in conjunction with other techniques to carry out some cases undergoing phase-transition phenomena.

2.2.2 Enthalpy-Porosity Model. Governing Equations

The energy equation based on the enthalpy formulation for convective-diffusive heat transfer states that,

$$\frac{\partial \rho h}{\partial t} + \frac{\partial}{\partial x_j} (\rho u_j h) = \nabla \cdot (k_i \nabla T_i) \quad (2.3)$$

where u is the velocity component and κ_i is the thermal conductivity of the fluid. h can be expressed as a function of its latent heat and the specific sensible parts,

However, the enthalpy-porosity method describes the enthalpy h of the mixture by its sensible part and the latent heat of solidification. The release of the latent heat is dependent on the stage of the phase change, and must be restricted to the phase change material.

$$h = \int_{T_r}^T c_p dT + \alpha_l L \quad (2.4)$$

where the latent heat is driven by the evolution of the liquid α_l . The phase transition is modelled by expressing the liquid volume fraction as a function

of the temperature,

$$\alpha_l = \begin{cases} 1 & T > T_{liq} \\ \frac{T - T_{sol}}{T_{liq} - T_{sol} + \epsilon} & T_{sol} < T < T_{liq} \\ 0 & T < T_{sol} \end{cases} \quad (2.5)$$

For seek of brevity on the following expressions, it is adapted the term γ_{phase} to γ_l . If expression 2.4 is replaced in 2.3,

$$\begin{aligned} \frac{\partial (\rho c_p T + \gamma_l \alpha_l L)}{\partial t} + \frac{\partial (\rho u_j c_p T + u_j \gamma_l \alpha_l L)}{\partial x_j} \\ = \nabla \cdot (k_i \nabla T_i) \end{aligned} \quad (2.6)$$

Rearranging terms, it yields,

$$\begin{aligned} \frac{\partial (\rho C_p T)}{\partial t} + \nabla \cdot (u_j \rho C_p T) + L \left[\frac{\partial (\rho \alpha_l \gamma_l)}{\partial t} + \frac{\partial (u_j \rho \alpha_l \gamma_l)}{\partial x_j} \right] = \nabla \cdot (k_i \nabla T_i) \\ S = -L \left[\frac{\partial (\rho \alpha_l \gamma_l)}{\partial t} + \frac{\partial (u_j \rho \alpha_l \gamma_l)}{\partial x_j} \right] \end{aligned} \quad (2.7)$$

The momentum equation is discussed in detail in the sub-chapter *Interphase porosity models*.

2.2.3 Lee model

The Lee model is based in the liquid-vapour mass transfer. Governed by the vapour transport equation 2.7, this model is applicable during melting or solidification of a fluid.

$$\frac{\partial}{\partial t} (\alpha_i \rho_i) + \nabla (\alpha_i \rho_i u_i) = S_{m_i} \quad (2.8)$$

ρ_i and u_i are the fluid density and fluid velocity of the i th phase. Moreover, S_{m_i} is the mass source which takes on a zero value at the interface.

During melting, $T_l > T_{sat}$,

$$\frac{dm_{sl}}{dt} = C_f \rho_s \alpha_s \left(\frac{T_s - T_{sat}}{T_{sat}} \right) \quad (2.9)$$

During solidification, $T_l < T_{sat}$

$$\frac{dm_{ls}}{dt} = C_f \rho_l \alpha_l \left(\frac{T_{sat} - T_l}{T_{sat}} \right) \quad (2.10)$$

The coefficient C_f might be interpreted as a time rate and must be empirically tuned. Its magnitude is expressed in $\frac{1}{s}$. α represents the phase volume

fraction. $\frac{dm_i}{dt}$ are the mass transfer rates from one phase to another. The subscripts "s", "l", refer to solid and liquid phases respectively. T_{sat} , is the phase transition temperature which, in case of pure water would be 273.15 K. The source term of 2.7 is then calculated as,

$$S_{m_i} = \begin{cases} \frac{dm_{sl}}{dt} - \frac{dm_{ls}}{dt}, & \text{for water phase} \\ \frac{dm_{ls}}{dt} - \frac{dm_{sl}}{dt}, & \text{for ice phase} \end{cases} \quad (2.11)$$

2.2.3.1 Momentum Equation

In the momentum equation, the flow is modelled as,

$$\begin{aligned} \frac{\partial(\rho u_i)}{\partial t} + \frac{\partial(\rho u_i u_j)}{\partial x_j} \\ = -\alpha_i \nabla p + \frac{\partial}{\partial x_j} \left(\mu \frac{\partial u_i}{\partial x_j} \right) + F_{\sigma i} + S_{u_i} \end{aligned} \quad (2.12)$$

The source term for the momentum equation can be written as,

$$S_{u_i} = \begin{cases} \frac{dm_{sl}}{dt} u_l - \frac{dm_{ls}}{dt} u_s, & \text{for water phase} \\ \frac{dm_{ls}}{dt} u_s - \frac{dm_{sl}}{dt} u_l, & \text{for ice phase} \end{cases} \quad (2.13)$$

where u_l and u_s are the liquid and solid velocity components accordingly. The source terms related to interphase porosity (2.28) may be added to the momentum equation presented here for the Lee model 3.6.

2.2.3.2 Energy Equation

The energy equation for the Lee model can be described as,

$$\frac{\partial(\rho C_p T)}{\partial t} + \nabla \cdot (u_j \rho C_p T) = \nabla \cdot (k_i \nabla T_i) + S_{H_i} \quad (2.14)$$

where the heat source term due to mass transfer in the energy equation is calculated as,

$$S_{H_i} = \begin{cases} \frac{dm_{sl}}{dt} H_L, & \text{for water phase} \\ \frac{dm_{ls}}{dt} H_L & \text{for ice phase} \end{cases} \quad (2.15)$$

where H_l is the latent heat induced by the phase transition and k_i , the thermal conductivity.

2.2.3.3 Classical nucleation theory. The coefficient C_f .

The coefficient C_f that appears on Equations 3.2 and 3.3 is computed accordingly to the work of [9]. In these work, the Lee model is used and the nucleation rate is introduced for the calculation of mass transfer rate between phases.

The concept behind the *Classical Nucleation Theory*, CNT, as described in [10]

resides in the idea of droplet freezing. This is initiated in the fluctuation of molecules of a supercooled liquid due to thermal vibration which lead, at its turn, to spontaneous formation of ordered solid molecule clusters (ice embryos). The size of these embryos oscillates as individual water molecules are crystallized or lost from the liquid phase. When the size of the embryo reaches a critical value, it leads a faster and auspicious thermodynamic joining of further water molecules to the crystal lattice. This means the critical embryo enhancing the "parent phase", supercooled liquid, to undergo a macroscopic phase transition: droplet freezing.

And this is what CNT aims to describe; the freezing process in terms of temperature-dependent nucleation rate by joining two components: thermodynamic and kinetic. These components, briefly described in the following chapters, are based on the theory found at Lai et al. [25] and Huang et al. [9]. As a remark, in this thesis a brief introduction of this theory is given. However, for further details on the assumptions used refer to the literature.

Thermodynamic component

This thermodynamic component seeks for the number of critical embryos formed per unit of volume at a specific temperature. A decrease in the enthalpy, and consequently a change in Gibbs free energy required to form an ice embryo containing water molecules generates an energy barrier to nucleation. However, for ice embryo formation, this barrier needs to be overcome.

$$\Delta G_C = \underbrace{\Delta G_V}_{\text{volume term}} + \underbrace{\Delta G_S}_{\text{surface term}} \quad (2.16)$$

$$\Delta G_c = -\frac{4}{3} \cdot \frac{\pi r^3}{\Omega} \cdot \Delta g_v + 4\pi r^2 \gamma_{sf} \quad (2.17)$$

where r is the radius of a simplified spherical embryo, γ_{sf} the interfacial tension between phases Ω the volume of a single molecule ($\Omega = V_{m,w}/N_A$), $V_{m,w}$ is the molar volume and Δg_v represents the decrease in volume of the Gibbs free energy of a molecule and is defined as:

$$\Delta g_v = \frac{\Delta_m H_1}{N_A} \frac{\Delta T}{T^*} \quad (2.18)$$

where $\Delta_m H_1$ is the molar latent heat of crystallization, N_A is the Avogadro's number, T^* is the freezing temperature and $\delta T = T^* - T$, the degree of supercooling. The radius has an influence on the change in Gibbs free energy. This is when:

- $r < r_{crit} \Rightarrow \Delta G_c > 0 \parallel \Delta G_c \uparrow \Rightarrow r \uparrow \Leftarrow \text{endothermic process}$
- $r > r_{crit} \Rightarrow \Delta G_c < 0 \parallel \Delta G_c \downarrow \Rightarrow r \uparrow \Leftarrow \text{exothermic process}$

The critical radius exists when the global enthalpy variation gets negative.

By differentiating Eq. 3.10 and setting $\frac{d(\Delta G_c)}{dr} = 0$, the critical radius is defined

as:

$$r_{crit} = \frac{2\gamma_{sf} T^* V_{m,w}}{\Delta_m H_1 \Delta T} \quad (2.19)$$

Then, if substituting Eq. 3.11 and 3.12 in Eq. 3.10, it is obtained the energy barrier:

$$\Delta G_{crit} = \frac{16\pi}{3} \cdot \frac{\gamma_{sf}^3 V_{m,w}^2 T^2}{\Delta_m H_1^2 \Delta T^2} = \frac{1}{3} (4\pi r_{crit}^2 \gamma_{sf}) \quad (2.20)$$

In Huang et al. [9], the expression concerning the variation of Gibbs function for the phase change does not include the molar volume of water but a shape coefficient of nucleation. It involves the influence of the contact angle when going from a uniform state to an inhomogeneous. This shape factor is defined as:

$$\alpha_{ey} = \frac{2 - 3 \cos \theta + \cos \theta^3}{4} \quad (2.21)$$

Temperature and saturation dependent number of ice embryos per unit volume of water may be expressed in a Boltzmann distribution form using ΔG :

$$N_{embryo} \left[\text{m}^{-3} \right] = N_l \cdot \exp \left(-\frac{\Delta G}{k_B T} \right) \quad (2.22)$$

where N_l is a volume-based number density of water molecules in the liquid phase.

Kinetic component

The kinetic part of the nucleation rate is introduced in the form of water molecules flux. This is expressed as a Boltzmann distribution such that:

$$\Phi = \frac{k_B T}{h} \cdot \exp \left(-\frac{\Delta g}{k_B T} \right) \quad (2.23)$$

where h is the Planck's physical constant, and Δg the activation energy for the transfer of a water molecule across the phase boundary.

The rate at which the water molecules are transferred into an ice embryo is defined as:

$$K = n_s \cdot 4\pi r_{embryo}^2 \cdot Z \cdot \Phi \quad (2.24)$$

where n_s is the number of molecules and $4\pi r_{embryo}^2$ is the surface area of the critical embryo and Z a kinetic prefactor. For seek of simplification, the authors of the theory suggest that the product of these terms are close to unity. Thus, considering this change, the equation yields as:

$$K = \Phi \quad (2.25)$$

Nucleation rate

Combining the thermodynamic component Eq. 3.14 and the kinetic one 2.24, the formulation of the nucleation rate can be expressed as:

$$J_{\text{hom}} \left[\text{m}^{-3} \cdot \text{s}^{-1} \right] = \underbrace{K}_{\text{Kinetics}} \cdot \underbrace{N_1 \cdot \exp \left(-\frac{\Delta G}{k_B T} \right)}_{\text{Number of embryos}} \quad (2.26)$$

As a final step, inserting Eq. 3.17 into Eq. 3.18, the nucleation rate is expressed in the form of:

$$J_{\text{hom}} \left[\text{m}^{-3} \cdot \text{s}^{-1} \right] = \frac{k_B T}{h} \cdot \underbrace{\exp \left(-\frac{\Delta g^\#}{k_B T} \right)}_{\text{diffusion of molecules effect}} \cdot N_1 \cdot \underbrace{\exp \left(-\frac{\Delta G}{k_B T} \right)}_{\text{nucleation effect}} \quad (2.27)$$

Fig. ?? characterizes the variation of the crystallization rate in function of the temperature. In the image, the dotted line shows how the nucleation effect is 0 close to the cooling, and as the temperature values decrease, this lines tend to 1. Moreover, the dashed line shows how the effect of the diffusion of the molecules increases as the temperature does. This prompts out the ease of the embryo formation when at low temperatures since the molecules cannot overcome the energy barrier to enter the embryo. However, the crystal growth becomes harder. This may be seen as constant search of equilibrium among the nucleation and the crystal growth. Finally, the coefficient C_f that

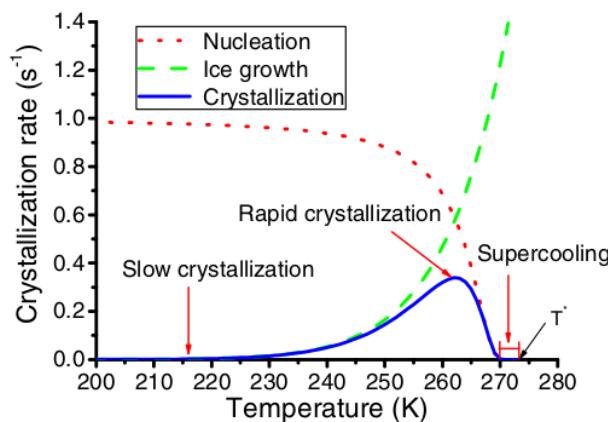


FIGURE 2.2: Crystallization rate versus temperature.

appears on Equations 3.2 and 3.3 as commented above, is defined for the Lee model as:

$$C_f = J_{\text{hom}} \cdot V_l \quad (2.28)$$

where V_l is the volume of water in each cell.

2.2.4 Interphase porosity models

Interphase porosity models add an artificial momentum source over the interface between phases to compute the sink of velocity in the solidified region. Therefore, influencing the behavior of the physics during the process of solidification or melting.

The model implemented in OpenFOAM is *Voller Prakash method* and it defines the source terms, S_y and S_z such that when along the fluid domain these terms take on a value of zero, the momentum equations are driven by the actual values of the velocities. On the other side, when it comes to treat the mushy region (i.e. porous region), the value of these source terms dominate convective, diffusive and transient terms and the momentum equation tends to approximate de Darcy law.

The two source terms as specified above,

$$\begin{cases} S_y = -Av \\ S_z = -Aw \end{cases} \quad (2.29)$$

Then, to specify a term for the function A, it is used the *Carman-Koseny equation*, which is derived from the Darcy law. The former expresses the gradient for the pressure as a combination of the velocity, \mathbf{u} , and the porosity, λ . The coefficient C depends on the morphology of the medium.

$$\text{grad}P = - \left(\frac{C(1-\lambda)^2}{\lambda^3} \right) \mathbf{u} \quad (2.30)$$

To avoid division by zero, q is added to the equations shown

$$A = - \left(\frac{C(1-\lambda)^2}{\lambda^3 + q} \right) \quad (2.31)$$

The source terms S_y and S_z are added in the Eq. 3.32 and 3.33. The source term S_b corresponds to the body forces of the fluid and will be discussed later on this thesis.

$$\frac{\partial(\rho v)}{\partial t} + \text{div}(\rho \mathbf{u} v) = \text{div}(\mu \text{grad } v) - \frac{\partial P}{\partial y} + S_y \quad (2.32)$$

$$\frac{\partial(\rho w)}{\partial t} + \text{div}(\rho \mathbf{u} w) = \text{div}(\mu \text{grad } w) - \frac{\partial P}{\partial z} + S_z + S_b \quad (2.33)$$

2.2.4.1 Surface tension model

The surface tension is only specified on a phase pair basis. In this version of OpenFOAM, it is present a constant model for a given σ .

Chapter 3

Numerical Simulation of Solidification Process

3.1 OpenFOAM. General Aspects

OpenFOAM is a free open-source software written in C++ and mainly conceived to perform computational fluid dynamics (CFD) simulations based on a finite volume discretization (FVM).

3.1.1 The finite volume method

Fluid equations usually take the form of non-linear partial differential equations and so, most of time, no analytical solution can be derived from them. In that context, different numerical techniques are employed to reach an approximation of the solution to these problems. These methods require a discretization of the domain in which the solution is going to be calculated. As aforementioned, OpenFOAM uses the finite volume method, which is, indeed, one of the most widely techniques used in computational fluid dynamics, and the one used in this thesis.

This technique turns the partial differential equations, which at their turn represent conservation laws over differential volumes, into discrete algebraic equations over finite volumes. Similarly to the finite element method, the FVM also needs a discretization of the geometric domain but in this numerical method, the elements used to integrate the algebraic equations representing the conservation partial differential equations are finite volumes or non-overlapping elements.

Some of the terms in the conservation equation are converted into face fluxes and evaluated in the discretized finite volumes. These face fluxes are strictly conservative. This is that the flux entering the volume is equal to the flux leaving the adjacent volume. This property makes the finite volume method the preferred technique for CFD [15].

Geometric domain discretization

The intrinsic properties of the finite volume method need the computational domain to be discretized in volume cells, known as control volumes (CV).

Each one of these volumes has a centroid or computational point in which the solution is obtained. Alongside with this idea, OpenFOAM follows a cell-centered approach in which the unknowns are defined at the center of these volumes or cells. The value of these are computed as an average value of the variable in that cell.

Moreover, the control volume is defined by the neighbours. This is, in the case the volume has an adjacent neighbour, an internal face is delimiting the separation of both. On the other hand, if the volume is not sharing a face with a neighbour volume, the face is considered to be a boundary.

Fluid dynamic equations discretization

The continuity equation, the Navier-Stokes equations and, the heat equation stated in section 2 can be stated in a more general form under the formulation of the Reynolds transport theorem:

$$\underbrace{\int_{V_p} \frac{\partial \rho \phi}{\partial t} dV}_{\text{Temporal term}} + \underbrace{\int_{V_p} \nabla \cdot (\rho \vec{u} \phi) dV}_{\text{Convective term}} = \underbrace{\int_{V_p} \nabla \cdot (\rho \Gamma_\phi \nabla \phi) dV}_{\text{Diffusive term}} + \underbrace{\int_{V_p} S_\phi dV}_{\text{Source term}} \quad (3.1)$$

where V_p is the control volume cell, ϕ may be any scalar or vectorial variable of the continuum, Γ_ϕ is the diffusivity of the variable and S_ϕ is a source term. In order to recover the continuity, momentum and energy equations, the parameters shown in table ?? need to be shaped in the transport equation.

Equation	ϕ	Γ_ϕ	S_ϕ
Continuity	1	0	0
Momentum	$\vec{u} u$	ν	$-\nabla p$
Energy	$C_p T$	κ	0

TABLE 3.1: Parameters to recover continuity, momentum and energy equations.

The fluid variable is defined as a ratio of itself integrated along the volume cell. Thus, it yields the following form,

$$\phi = \phi_P = \frac{1}{V_p} \int_{V_p} \phi(x) dV \quad (3.2)$$

Therefore, a complete discretization of the previous terms is needed to solve the physics regarding a general fluid dynamics problem.

3.1.2 OpenFOAM functioning

In this first section, a brief introduction on the structure and functioning of the OpenFOAM software is given. In the folder structure tree shown in Fig.

??, it is shown a typical case setup for a phase change problem using *icoReactingMultiphaseFoam* solver.

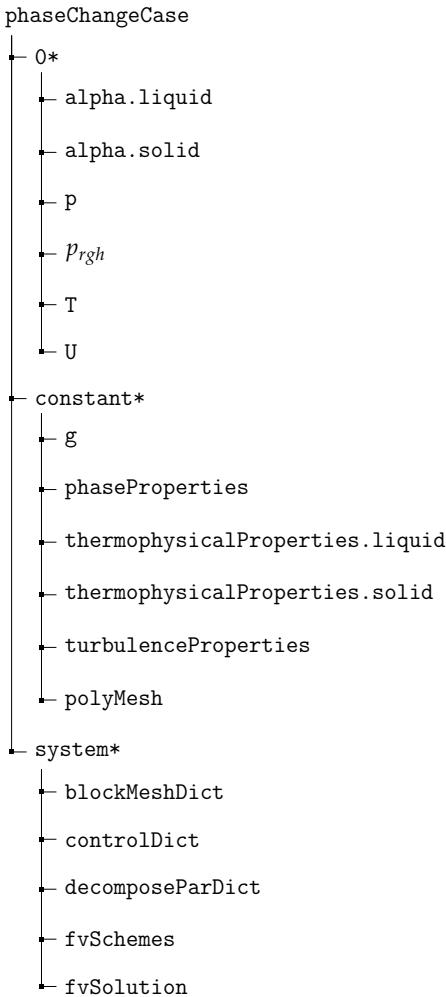


FIGURE 3.1: General structure of an OpenFOAM case.

3.1.2.1 Boundary Conditions Directory

The "0" directory gathers all the boundary conditions at time zero and the initial conditions to set up the case. As the simulation starts running, the information of these fields is saved in folders at every timestep.

3.1.2.2 Constant Properties Directory

The "constant" directory contains all the information typically regarding the physical properties which are kept constant through the simulation. Moreover, once the dictionary *blockMeshDict* is run, OpenFOAM creates a folder called *polyMesh* containing all the information relevant to the mesh (points, faces,...)

3.1.2.3 System Directory

This folder contains the files required by the control of the solver and the solution itself. The most common files are:

- **blockMeshDict:** in this file the parameters required to build up the computational domain, the mesh and the boundaries are found. The command **blockMesh** executes this dictionary creating the *polyMesh* folder commented above.
- **controlDict:** Time parameters associated to the computation are set in this file.
- **decomposeParDict:** In the realization of this thesis, the help of parallel computing is required. Thus, in this file, parameters regarding the decomposition of the mesh are configured. It is executed by means of the **decomposePar** application implicit in OF. The mesh is afterwards reconstructed by using **reconstructPar**
- **fvSchemes:** Schemes selected for the discretization of the derivative terms are defined. Among others, time schemes, gradient schemes, laplacian schemes, divergent schemes, interpolation schemes can be declared here.
- **fvSolution:** contains sub-dictionaries used to control the solvers and the solution algorithms. It also allows the definition of the fields resolution.

3.2 Solidification process. Methodology

A convection solver is used to represent the flow behavior generated by the density difference due to existing temperature gradients within the volume of control. A polynomial water density is implemented in the native OpenFOAM solver and compared with the standard Boussinesq approximation. The current model is validated against numerical results from the literature. The solution of this convection solver is later used as a boundary condition, before solidification phenomena plays a role.

3.3 OpenFOAM: BuoyantBoussinesqPimpleFOAM. Natural Convection solver

In a natural convection environment, the motion of the fluid is mainly driven by the density difference within the fluid volume of control. At its turn, the differences in the density, responsible for buoyancy forces, are generated by the existing temperature gradients. Within a physical context, the fluid near a hot heat source gets warmed up and, as a result, it becomes less dense moving up inside a domain. Consequently, the fluid in contact of the cold heat source is pushed from its zone to replace the hot fluid location. At this point, the cycle starts again repeating the physical phenomena.

3.3.1 Case Description

Within the context of natural convection, the current case aims to develop a comprehensive state of the capabilities that OpenFoam solvers brings to solve this phenomena. To reach the objective, and on purpose of controlling the physics generated on the simulation, a regular squared geometry of 0.038 mm side length is created:

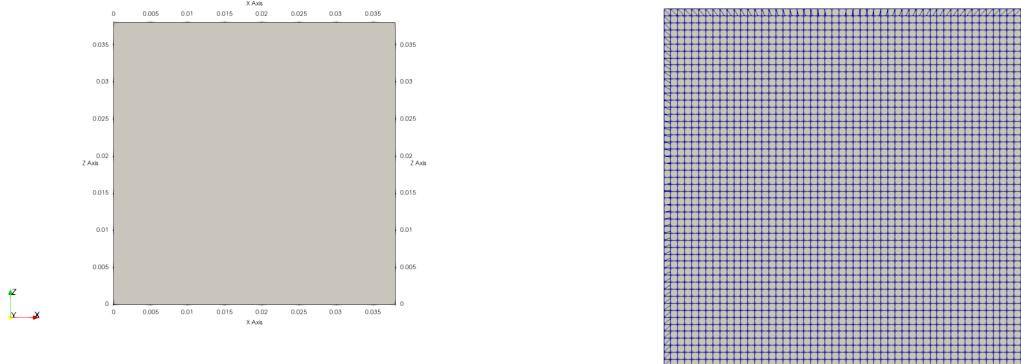


FIGURE 3.2: Geometric characteristics.

The mesh is structured and consists of 1971212 nodes.

3.3.2 Hypotheses And Assumptions

To carry out the current problem, a series of assumptions are taken into account in order to simplify the solving of the fluid equations involved.

Laminar regime: The Reynolds number, computed from the maximum velocity is not high enough to consider turbulent effects.

Convective heat transfer: To determine whether the heat transfer is assumed to be convective, the Prandtl number and the Rayleigh number should be assessed.

The Prandtl number, as the relation between the viscosity and the thermal

conductivity of a fluid or, in other words, the correlation between momentum transport and thermal transport capacity is calculated as:

$$\text{Pr} = \frac{\nu}{\alpha} = \frac{\eta}{\rho\alpha} = \frac{\eta c_p}{\lambda} = \frac{\text{momentum transport}}{\text{heat transport}} \quad (3.3)$$

where Thus, a small Prandtl number are owned by free-flowing flows with high thermal conductivity.

On the other hand, the Rayleigh number is referred to the time scale relation between the diffusive and the convective thermal transports. It is thus used to determine whether the buoyancy-driven natural convection plays an important role in the heat transfer. The dimensionless number is assessed in this context by this form:

$$\text{Ra}_x = \frac{g \cdot \beta}{\nu \cdot \alpha} \cdot (T_s - T_{\text{inf}}) \cdot x^3 \quad (3.4)$$

Being g , the gravity, β , the coefficient of thermal expansion, ν , the kinematic viscosity, α , the thermal diffusivity, and T_s and T_{inf} , the temperature on the wall surface and the temperature of the fluid far from the wall accordingly. In the current case-scenario, a Prandtl close to 7 and a Rayleigh of 2517629 determine a convective heat transfer. The values used to estimate the Rayleigh number calculation are: $\beta = 6.734e - 5K^{-1}$, $\nu = 1.003e - 6m^2.s^{-1}$, $\alpha = 1.435e - 7m^2.s^{-1}$, $T_s = 283K$, $T_{\text{inf}} = 273K$ and $x = 0.038m$. The values used for the laminar Prandtl number calculation are: $\mu = 0.001003Kg.m^{-1}.s^{-1}$, $\lambda = 0.6W.m^{-1}.K^{-1}$ and $C_p = 4182J.Kg.K^{-1}$.

Newtonian fluid: The viscosity of the fluid is assumed to be constant.

Thermophysical properties: specific heat, C_p , the thermal expansion coefficient, β , thermal conductivity, κ , kinematic viscosity, ν are assumed to be non-dependent of temperature. However, the density will be dependent of temperature so as it plays an important role in the buoyancy effects through the later explained in this section.

The conservative equations used to describe the motion of the fluid along time and space are described next.

3.3.3 Governing Equations

In this section, the governing equations for the used solver are described first.

The conservation of mass states that the mass flowing into the volume of control (CV) must be equal to the mass flowing out of such volume.

$$\frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \quad (3.5)$$

3.3.3.1 Momentum Equation

Throughout the CV the momentum of the fluid flow is preserved and here below it is expressed for the y-direction and z-direction.

$$\frac{\partial(\rho v)}{\partial t} + \operatorname{div}(\rho \mathbf{u}v) = \operatorname{div}(\mu \operatorname{grad} v) - \frac{\partial P}{\partial y} \quad (3.6)$$

$$\frac{\partial(\rho w)}{\partial t} + \operatorname{div}(\rho \mathbf{u}w) = \operatorname{div}(\mu \operatorname{grad} w) - \frac{\partial P}{\partial z} + S_b \quad (3.7)$$

where in the case of the *Boussinesq approximation* where the density variation is linear:

$$S_b = g \cdot \rho_r [1 - \beta(T - T_r)] \quad (3.8)$$

in the case of the implemented polynomial density which accounts for the inversion point as in [3]:

$$S_b = g \cdot [\rho_r - \rho(T)] \quad (3.9)$$

where the polynomial expression from ρ is:

$$\begin{aligned} \rho(T) = & 999.840281167108 + 0.0673268037314653 \times T \\ & - 0.00894484552601798 \times T^2 \\ & + 8.78462866500416.10^{-5} \times T^3 - 6.62139792627547.10^{-7} \times T^4 \end{aligned} \quad (3.10)$$

As it will be pointed out later, the native solver uses the Boussinesq approximation to account for the buoyancy effects. However, this linear assumption is only valid as the density variations meet:

$$\frac{\Delta\rho}{\rho_r} \ll 1 \quad (3.11)$$

Therefore, to account for the inversion points present during the freezing process, a density variation like the described in ?? is implemented in the solver.

3.3.3.2 Temperature Equation

The temperature equation representing the convection phenomena yields as:

$$\frac{\partial T}{\partial t} + \frac{\partial(u_j T)}{\partial x_j} = \frac{\partial}{\partial x_j} \left(\gamma \frac{\partial T}{\partial x_j} \right) \quad (3.12)$$

where the thermal diffusivity, γ , is defined as:

$$\gamma = \frac{\lambda}{\rho_r c_p} \quad (3.13)$$

All these equations are regarded by the solver *buoyantBoussinesqPimpleFoam*.

3.3.4 Solver descriptor. Control Loop

The *buoyantBoussinesqPimpleFoam* is a solver used to solve non-steady buoyancy-driven fluids by using the Boussinesq approximation as a coupling between density and temperature fields. It considers the fluid as incompressible and uses the PIMPLE algorithm for the pressure-velocity coupling. The flowchart of the integration procedure for the presented solvers *buoyantBoussinesqPimpleFoam* and *icoReactingMultiphaseInterFoam* is presented below:

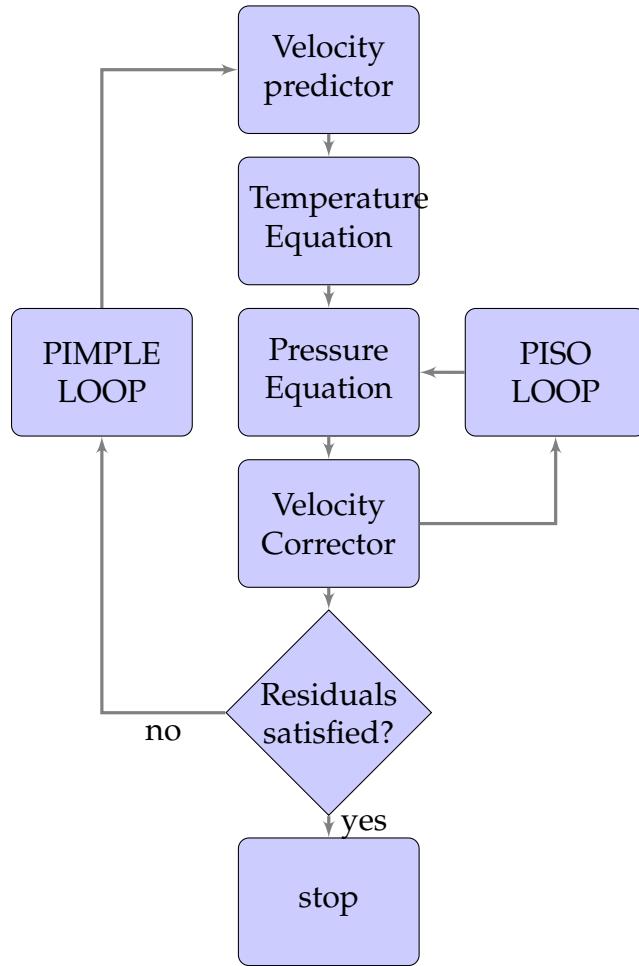


FIGURE 3.3: Flowchart of integration procedure. *buoyantBoussinesqPimpleFoam*

3.3.5 Code implementations

As described in the *Governing equations* section, the need for a polynomial density expression and a variation of the momentum source terms devoted to reflect the buoyancy effects is derived. To do so, a new equation of state is implemented within the OpenFoam framework. Now and, in order to take into account this buoyancy forces, the pressure equation is studied. This

is because in the context of a pressure-velocity corrector scheme, and in the case of ensuring stability and simplifying the boundary conditions definition, the modified pressure, p_{rgh} , within the pressure equation implementation, is the term that accounts for the gravity terms.

Here, it is presented a general form of a momentum equation with the continuity equation corresponding to an incompressible flow.

$$\begin{cases} \frac{\partial(\rho\mathbf{v})}{\partial t} + \nabla \cdot (\rho\mathbf{v} \otimes \mathbf{v}) = -\nabla p + \nabla \cdot (\mu(\nabla\mathbf{v} + \nabla\mathbf{v}^T)) \\ \nabla \cdot \mathbf{v} = 0 \end{cases} \quad (3.14)$$

From this general equation, it will be given the term $H(\mathbf{u})$, as later on will be needed for the pressure equation calculation.

Therefore, this term comes from considering the linearization of the advective term under the assumption of small Courant numbers ($\text{Co} < 1$). Leading the term $\mathbf{v}^0 \cong \mathbf{v}$.

$$\begin{aligned} \int_{\Omega} \nabla \cdot (\mathbf{v} \otimes \mathbf{v}^0) d\Omega &\cong \sum_f \mathbf{v}_f \mathbf{v}_f^0 \cdot \mathbf{s}_f \\ &= \sum_f F^0 \mathbf{v}_f \\ &= a_P \mathbf{v} + \sum_f a_N \mathbf{v}_N \end{aligned} \quad (3.15)$$

$$a_P \mathbf{v}_P = \mathbf{H}(\mathbf{v}) - \nabla p \quad (3.16)$$

$$\mathbf{H}(\mathbf{v}) = \underbrace{- \sum_f a_N \mathbf{v}_N}_{\text{Diagonal term}} + \underbrace{\frac{\mathbf{v}^0}{\Delta t}}_{\text{Off-diagonal term}} \quad (3.17)$$

where \mathbf{v}^0 is the velocity at previous time-step and F^0 is the face flux at the previous time-step.

In addition, by discretizing the continuity equation, it is possible to get the final form of the pressure equation.

So as to give stability to the solution and to simplify the boundary conditions definition [2], a modified pressure is defined as,

$$p_{rgh} = p - \rho_r \mathbf{g} \cdot \mathbf{x} + \rho(T) \mathbf{g} \cdot \mathbf{x} \quad (3.18)$$

being, the pressure gradient the next expression,

$$-\nabla p + \rho_r \mathbf{g} = -\nabla p_{rgh} - \mathbf{g} \cdot \mathbf{x} \nabla \rho_r + \mathbf{g} \cdot \mathbf{x} \nabla \rho(T) + \rho(T) \mathbf{g} \quad (3.19)$$

and rearranging terms,

$$-\nabla p + \rho_r \mathbf{g} + \mathbf{g} \cdot \mathbf{x} \nabla \rho_r - \mathbf{g} \cdot \mathbf{x} \nabla \rho(T) - \rho(T) \mathbf{g} = -\nabla p_{rgh} \quad (3.20)$$

If one tries to describe the discretized pressure equation in *buoyantBoussinesqPimpleFoam*, there is a first term called **phig**, which is,

$$\Phi_f^{\nu+1} = \Phi_u^{\nu+1} - \left[(\mathbf{g} \cdot \mathbf{x})_f \left(\nabla \rho_r^{n+1} \right)_f + (\mathbf{g} \cdot \mathbf{x})_f \left(\nabla \rho(T)^{n+1} \right)_f \right] \frac{|\mathbf{S}_f|}{(a_P)_f} \quad (3.21)$$

A face flux calculated by the term $\mathbf{H}(\mathbf{v})$, appearing in equation 3.16

$$\Phi_u^{\nu+1} = \Phi_f^{\nu+1} + \left(\frac{H(\mathbf{v}^\nu)}{a_P} \right)_f \cdot \mathbf{S}_f + \left(\frac{1}{a_P} \right)_f \text{ddtPhiCorr}(\mathbf{v}^\nu, \Phi^\nu) \quad (3.22)$$

where ddtPhiCorr is a flux adjustment due to the time-step. This is resolved by applying a *Rhie-Chow interpolation*, [18], the next term in the pressure equation, **phiHbyA**, reads as,

$$\Phi_f^{\nu+1} = \Phi_f^{\nu+1} - \left[\left(\frac{1}{a_P} \right)_f \left(\nabla p_{rgh} \right)_f \right] \cdot \mathbf{S}_f \quad (3.23)$$

The p_{rgh} term is thus assembled as,

$$\sum_f \left[\left(\frac{1}{a_P} \right)_f \left(\nabla p_{rgh}^{\nu+1} \right)_f \right] \cdot \mathbf{S}_f = \sum_f \Phi_f^{\nu+1} \quad (3.24)$$

The flux, ϕ , is adjusted by the p_{rgh} term yielding the following expression,

$$\Phi_f^{\nu+1} = \Phi_f^{\nu+1} - \left[\left(\frac{1}{a_P} \right)_f \left(\nabla p_{rgh} \right)_f \right] \cdot \mathbf{S}_f \quad (3.25)$$

$$\begin{aligned} \Phi_f^{\nu+1} = & \Phi_f^{\nu+1} + \left[\left(\frac{1}{a_P} \right)_f \left[(-\nabla p)_f + (\mathbf{g} \cdot \mathbf{x})_f \left(\nabla \rho_r^{n+1} \right)_f - (\mathbf{g} \cdot \mathbf{x})_f \left(\nabla \rho(T)^{n+1} \right)_f \right. \right. \\ & \left. \left. + (\rho_r^{n+1} \mathbf{g})_f - (\rho(T)^{n+1} \mathbf{g})_f \right] \right] \cdot \mathbf{S}_f \end{aligned} \quad (3.26)$$

Finally, the velocity calculated at the center of the volume reads as,

$$\mathbf{v}^{\nu+1} = \mathbf{v}^{\nu+1} + \frac{1}{a_P} \mathcal{R} \left[(\Phi_f^{\nu+1} - \Phi_u^{\nu+1}) (a_P)_f \right] \quad (3.27)$$

where \mathcal{R} is an operator used to recover cell-centered fields from fields given as fluxes at faces. Then, the static pressure, p , is reconstructed from p_{rgh} , leading the expression,

$$p = p_{rgh} + (\rho_r - \rho(T)) \mathbf{g} \cdot \mathbf{x} \quad (3.28)$$

3.3.6 Case Setup

Once the implementation is done, a first case is studied with the existing solver, *buoyantBoussinesqPimpleFoam*. The boundary conditions, thermophysical properties and some other solver parameters are described along the following subsections.

As commented before, all studies are calculated on a computational domain of $38\text{mm} \times 38\text{mm}$.

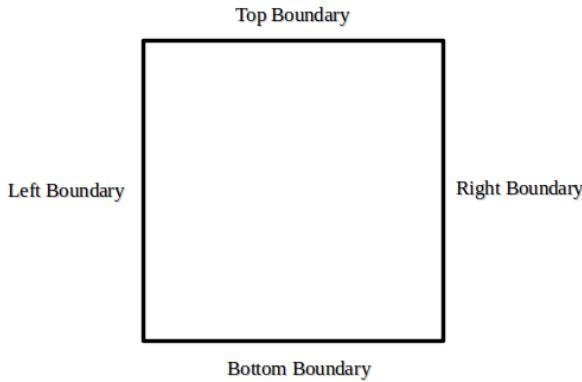


FIGURE 3.4: Setting of computational domain.

Boundary conditions

Five boundaries are defined in the current case:

Left: is considered a wall with a fixed value of temperature. This is the hot wall. No velocity is prescribed.

Right: considered to be the cold wall with a fixed temperature. No velocity is prescribed.

Top: this is considered the top wall and it is adiabatic, thus, no heat transfer is assumed and zero gradient is applied. No velocity is applied.

Bottom: This shares similar conditions as the top wall.

frontAndBack: this uses a symmetry plane condition in the z direction since the problem is considered to be 2-dimensional. For such boundary type, no more conditions need to be prescribed.

Boundary	Conditions
Left	$T_l = 283, v_l = 0$
Right	$T_r = 273, v_r = 0$
Top	$\frac{\partial T_u}{\partial n} = 0, v_u = 0$
Bottom	$\frac{\partial T_b}{\partial n} = 0, v_b = 0$

TABLE 3.2: Boundary conditions for natural convection case.

Thermophysical properties

Water properties	Symbol	Values	Units
Density	ρ_r	999.8	$kg.m^{-3}$
Dynamic viscosity	μ	0.001003	$kg.m^{-1}.s^{-1}$
Thermal conductivity	λ	0.6	$W.m^{-1}.K^{-1}$
Heat capacity	C_p	4182	$J.kg.K^{-1}$
Gravitational acceleration	g	9.81	$m.s^{-2}$
Thermal diffusivity	γ	1.435e-7	$m^2.s^{-1}$
Thermal expansion coefficient	β	6.734e-5	K^{-1}
Laminar Prandtl number	P_r	6.99	-
Reference temperature	T_r	6.734e-5	K

TABLE 3.3: Water properties for natural convection.

Modeling Term	Keyword	Scheme	Remarks
Time derivatives	ddtSchemes	Euler	First order, bounded, implicit
Divergence term	divSchemes		Second order, unbounded
Gradient term	gradSchemes	Gauss linear	Second order, unbounded
Laplacian term	laplacianSchemes	Gauss linear orthogonal	
Grad. normal to cell face	snGradSchemes	orthogonal	
Point to point interpolation	interpolationSchemes	linear	Central differencing

TABLE 3.4: Discretization schemes.

Equation	Linear Solver	Smoothening/Preconditioner	Tolerance
Pressure correction equation	PCG	DIC	1e-8
Momentum equation	PBiCGStab	DILU	1e-6
Temperature equation	PBiCGStab	DILU	1e-6

TABLE 3.5: Solvers for the discretised equations.

Parameter	Value
momentumPredictor	no
nOuterCorrectors	1
nNonOrthogonalCorrectors	0
nCorrectors	2

TABLE 3.6: Parameters for the discretised equations.

3.3.7 Validation of Results and Conclusions

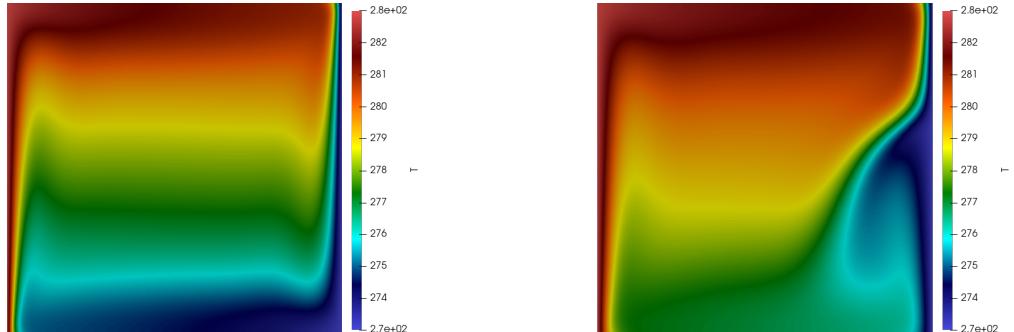
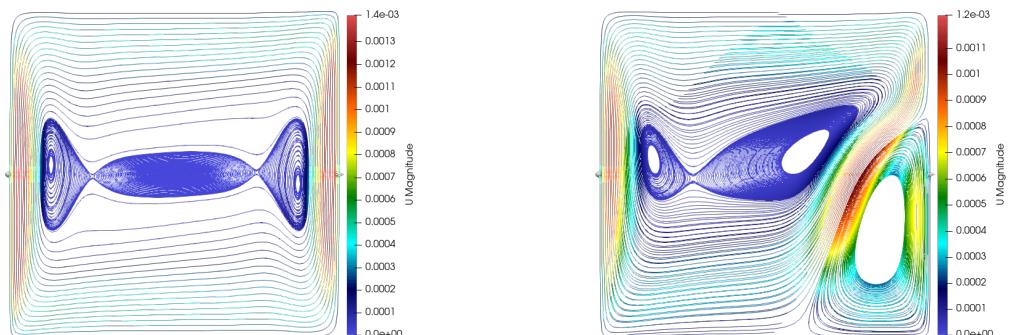
(A) Temperature magnitude comparison at $t = 1500$ s. Left: BuoyantBoussinesqPimpleFoam.
Right: NCMF(B) Velocity magnitude comparison at $t = 1500$ s. Left: BuoyantBoussinesqPimpleFoam.
Right: NCMF

FIGURE 3.5: Comparison between BuoyantBoussinesqPimpleFoam and NCMF*

NCMF*: Natural convection modified solver.

In order to compare consistently the obtained results with those of the literature, the following dimensionless values are pointed out:

$$\tilde{T} = \frac{T - T_{\text{cold}}}{T_{\text{hot}} - T_{\text{cold}}} = \frac{T - 273}{10} \quad (3.29)$$

$$\tilde{x} = \frac{x}{\ell} = \frac{x}{38 \times 10^{-3}} \quad (3.30)$$

$$\tilde{v} = \frac{v\ell}{\gamma} = \frac{v38 \times 10^{-3}}{1.435 \times 10^{-7}} \quad (3.31)$$

$$\tilde{u} = \frac{u\ell}{\gamma} = \frac{u38 \times 10^{-3}}{1.435 \times 10^{-7}} \quad (3.32)$$

$$\tilde{t} = \frac{t\gamma}{\ell^2} = \frac{t \times 1.435 \times 10^{-7}}{1.444 \times 10^{-6}} \quad (3.33)$$

$$\tilde{y} = \frac{y}{\ell} = \frac{y}{38 \times 10^{-3}} \quad (3.34)$$

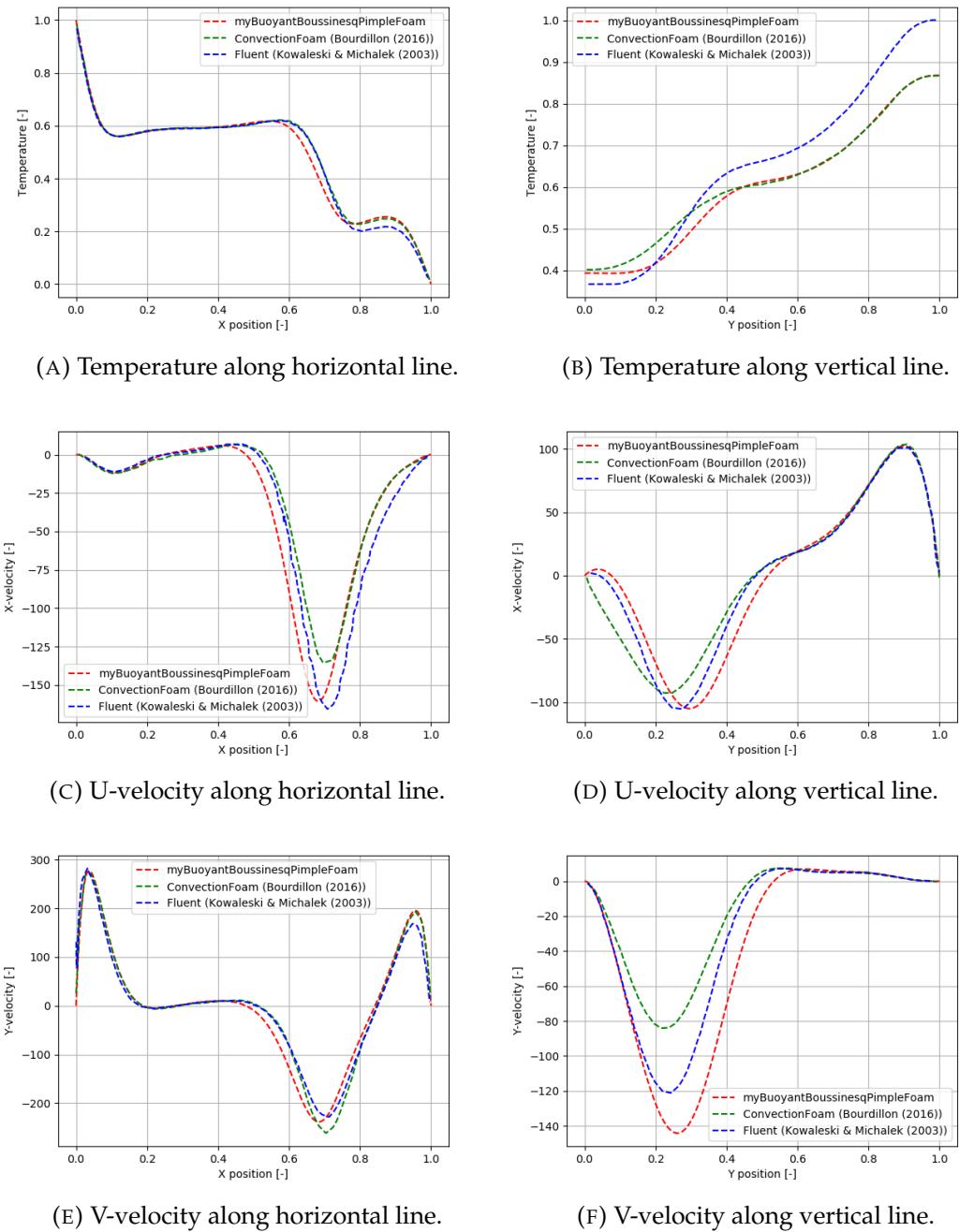


FIGURE 3.6: Adimensional magnitudes comparison.

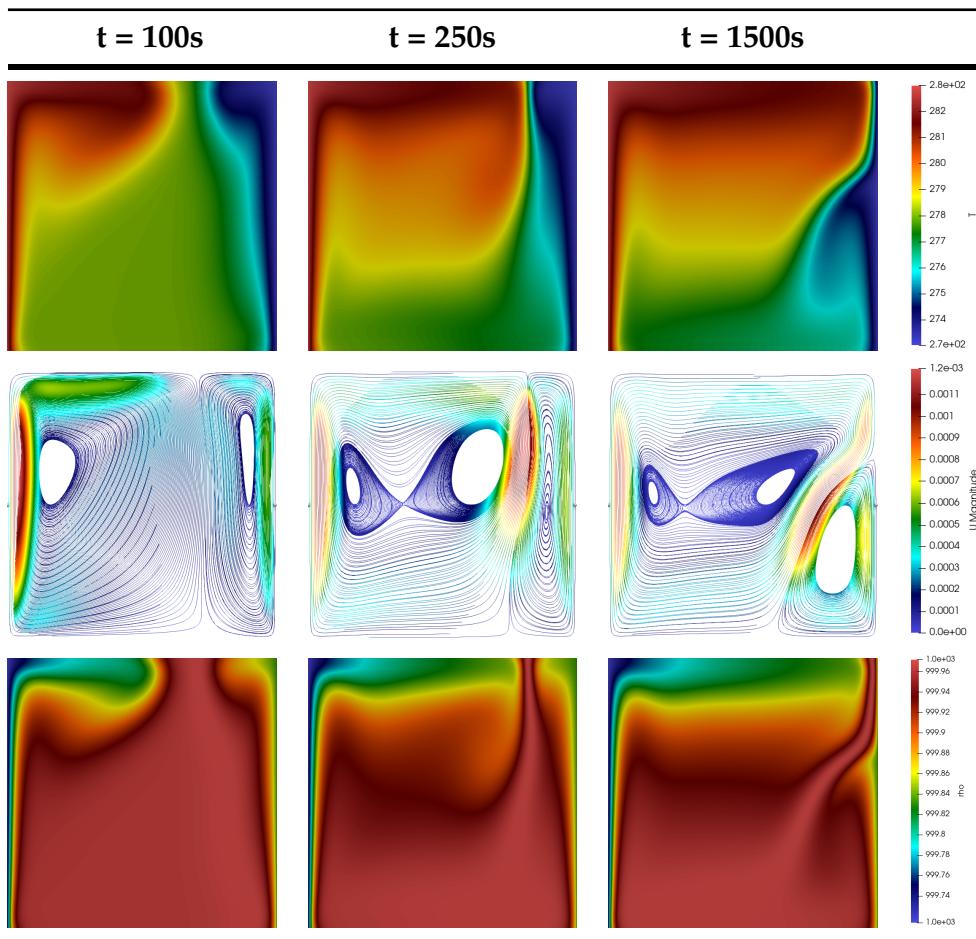


TABLE 3.7: Numerical results of Natural convection modified solver between $t = 100\text{s}$ and 1500s .

3.4 OpenFOAM: IcoReactingMultiphaseInterFOAM. Phase-Change Process

The solidification process is assessed in this section with two elaborated models. Both of the models are implemented within a multiphase solver based on the volume of fluid technique. This technique aims to capture interface and enhances contact angle and surface tension for each phase. Thus, the first model is based on the coupling of the VOF and the enthalpy-porosity method. To accomplish the inclusion of the enthalpy-porosity method, a library in which the latent heat is implemented as an explicit source term for the energy equation in the solver. On the other hand, the second model uses the VOF method combined with a semi-empirical model based on the work of Lee. The empirical constant is adapted here to be used in conjunction with the use of the *Classical Nucleation Theory*.

3.5 Case Description.

Two regular geometries are created: a squared cavity, used in the pure convection case and cylindrical plane geometry. Both geometries test both solidification models.

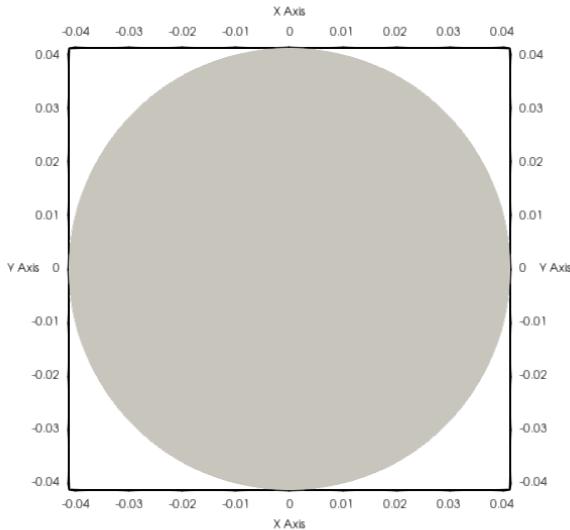


FIGURE 3.7: Cylinder.

3.5.1 Hypotheses And Assumptions

To carry out the phase-transition process, some assumptions are taken into account so as to simplify the multiphysics occurring during such arising phenomena.

Laminar regime: The Reynolds number, computed from the maximum velocity is not high enough to consider turbulent effects.

In the current case-scenario, a Prandtl close to 7. The values used for the laminar Prandtl number calculation are: $\mu = 0.001003 \text{Kg.m}^{-1}.\text{s}^{-1}$, $\lambda = 0.6 \text{W.m}^{-1}.\text{K}^{-1}$ and $C_p = 4182 \text{J.Kg.K}^{-1}$.

Newtonian fluid: The viscosity of the fluid is assumed to be constant. The thermophysical properties treatment is described below.

Two phase properties

Within a multiphase framework, a model reflects a jump in properties through the interphase. Thus, a smooth transition between phase properties must be achieved.

$$\lambda = \lambda_\ell \alpha_\ell + \lambda_s f_s \quad (3.35)$$

$$C_p = C_{p_\ell} \alpha_\ell + C_{p_s} f_s \quad (3.36)$$

$$\mu = \mu_\ell \alpha_\ell + \mu_s f_s \quad (3.37)$$

In the current case-scenario, $C_{p_s} = C_{p_l}$.

In the case of polynomial density variation it is settled in a similar manner. The polynomial is not thought to suit negative temperatures, and when the problem is within this range, the density should take ice's density.

$$\rho(T)' = \rho(T) \alpha_\ell + \rho_s f_s \quad (3.38)$$

3.5.2 Governing Equations

The solution of the system of equations given by the multiphase solver relies on a pressure-velocity coupling loop based on PISO (*Pressure-Implicit with Splitting of Operators*). In order to give more stability to the solution and to simplify the boundary conditions, the pressure is treated by using a modified pressure:

Therefore, due to the commented before, the buoyancy terms appearing on the RHS of the momentum equation, are implemented on the pressure equation.

3.5.2.1 Momentum Equation

The momentum equation has the same terms as per each one of the models. Here it is the equation recalled from previous section:

$$\begin{aligned} \frac{\partial(\rho u_i)}{\partial t} + \frac{\partial(\rho u_i u_j)}{\partial x_j} \\ = -\alpha_i \nabla p + \frac{\partial}{\partial x_j} \left(\mu \frac{\partial u_i}{\partial x_j} \right) + F_{\sigma i} + S_{u_i} \end{aligned} \quad (3.39)$$

3.5.2.2 Energy Equation

On the other side, the energy equation slightly differs from one model to the other. As pointed out before, here there are recalled both energy equations.

3.5.3 Solver description. Control Loop

IcoReactingMultiphaseInterFoam solver is a multiphase, multicomponent incompressible solver based on volume of fluid method. The solver captures the interfaces and includes contact angle and surface tension effects for each phase. Moreover, this solver supports mass and heat transfer across phases. The energy equation for the Enthalpy-porosity model:

$$\frac{\partial(\rho C_p T)}{\partial t} + \nabla \cdot (u_j \rho C_p T) + L \left[\frac{\partial(\rho \alpha_l \gamma_l)}{\partial t} + \frac{\partial(u_j \rho \alpha_l \gamma_l)}{\partial x_j} \right] = \nabla \cdot (k_i \nabla T_i) \quad (3.40)$$

The energy equation for the Lee model in conjunction with the nucleation theory:

$$\frac{\partial(\rho C_p T)}{\partial t} + \nabla \cdot (u_j \rho C_p T) = \nabla \cdot (k_i \nabla T_i) + S_{H_i} \quad (3.41)$$

3.5.4 Phase models

The solver allows for the use of three phase model types:

- **pureStaticSolidPhaseModel:** For pure static phase, like a solid.
- **pureMovingPhaseModel:** For pure moving phase, like a fluid.
- **multiComponentMovingPhaseModel:** For multi-component moving phase, like a multi-component fluid.

In the current case-scenario, the *pureStaticSolidPhaseModel* is selected for the solid phase and the *pureMovingPhaseModel* is used for the liquid phase.

3.5.5 Mass transfer models

For each pair of phases, two mass transfer models might be used:

- **Lee model:** Used for solid melting and liquid solidification.
- **KineticGasEvaporation:** Used for condensation and evaporation.

In this thesis, only the Lee model will be considered for further explanation.

3.5.6 Code implementations

Within the entrophy-porosity model, the source term belonging to the calculation of the latent heat is added within the OpenFOAM framework. The energy equation of the solver shown in [ref]. In the RHS of the equation, the solver calls the library *mySolidificationMeltingSource* that calculates the latent

```

fvScalarMatrix TEqn
(
    fvm::ddt(rhoCp, T)
    + fvm::div(rhoCpPhi, T, "div(phi,T)")
    - fvm::Sp(fvc::ddt(rhoCp) + fvc::div(rhoCpPhi), T)
    - fvm::laplacian(kappaEff, T, "laplacian(kappa,T)")
    ==
    fvOptions(rhoCp, T)
);

```

FIGURE 3.8: Energy equation of IcoReactingMultiphaseInterFoam.

heat source term as it appears in the Energy equation shown below. This li-

```

// contributions added to rhs of solver equation
if (eqn.psi().dimensions() == dimTemperature)
{
    eqn -= (L*alpha1_)/CpVoF*(fvc::ddt(rho, alphaC_) + fvc::div(rhoCpPhiVoF, alphaC_));
}
else
{
    //This option is not activated since fvOptions in TEqn does not enable this condition
    eqn -= L*alpha1_*(fvc::ddt(rho, alphaC_));
}

```

FIGURE 3.9: Latent heat source term present in mySolidificationMeltingSource library.

brary is adapted to be used in this solver. It exists in the context of being used for other solvers. Here, the alpha variable showing up in the calculation is obtained through a linear expression that gives the amount of energy contained in the fluid cell above the melting point. This is divided by the latent heat to obtain the liquid fraction. Then, this fraction is constained between 0 and 1.

The latent heat source term is afterwards weighted by the volume fraction calculated by means of the transport equation in the context of the volume of fluid method as it appears in Richter et al. [richter_turnow_kornev_hassel_2016].

The **rhoCpPhi** term, which is called in this library, is created in *createFields.H* as a variable field so that it can be called from everywhere within the code.

The implemented library can be found in the Appendix A.

The Lee model is already implemented in OpenFOAM. However, there is a parameter, C , devoted to act as a condensation rate. This is referred as an empirical coefficient used to speed-up or slow down the mass and heat transfer. Therefore, in favor of tunning this parameter in accordance with the characteristic behavior of the water when it freezes, the *Classical Nucleation theory* is followed.

In the function shown above, all of the parameters concerning the formulas required to calculate the nucleation rate of the water are user-defined parameters. In the Appendix A, the code related with the Lee model using this theory can be found.

```

surfaceScalarField rhoCpPhi
(
    IOobject
    (
        "rhoCpPhi",
        runTime.timeName(),
        mesh,
        IOobject::NO_READ,
        IOobject::NO_WRITE
    ),
    fvc::interpolate(fluid.Cp())*rhoPhi
);

rhoCpPhi.oldTime();

```

FIGURE 3.10: **rhoCpPhi** field in *createFields.H*

```

template<class Thermo, class OtherThermo>
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>::LeeCNT
(
    const dictionary& dict,
    const phasePair& pair
):
:
InterfaceCompositionModel<Thermo, OtherThermo>(dict, pair),
C_("C", inv(dimTime), dict),
Tactivate_("Tactivate", dimTemperature, dict),
planck_("planck", dimEnergy*dimTime, dict),
boltzmann_("boltzmann", dimEnergy/dimTemperature, dict),
deltag_("deltag", dimEnergy, dict),
nL_!("nL", inv(dimVolume), dict),
gammaYW_("gammaYW", dimEnergy/dimArea, dict),
hLV_("hLV", dimEnergy/dimVolume, dict),
alphaEY_("alphaEY", dict),
alphaMin_(dict.getOrDefault<scalar>("alphaMin", 0)),
interfaceVolume_
(
    IOobject
    (
        "cellVolume",
        this->mesh_.time().timeName(),
        this->mesh_,
        IOobject::NO_READ,
        IOobject::NO_WRITE
    ),
    this->mesh_,
    dimensionedScalar(dimVolume, Zero)
)
{}
```

FIGURE 3.11: Function used to ask for the required user inputs.

3.5.7 Case Setup

Boundary conditions

For the squared cavity: The initial conditions for the velocity and temperature fields are inherited from the last timestep of the natural convection case. frontAndBack boundary is set to *empty* to define a 2-dimensional case-scenario. For the cylinder: As in the previous geometry, there is an empty boundary called frontAndBack to define a planar case.

The thermophysical properties and solver parameters defined below are set-up for both geometries.

Boundary	Conditions
Left	$\frac{\partial \alpha_l}{\partial n} = 0, \frac{\partial \alpha_s}{\partial n} = 0$
Right	$\alpha_l = 1, \alpha_s = 0$
Upper	$\frac{\partial \alpha_l}{\partial n} = 0, \frac{\partial \alpha_s}{\partial n} = 0$
Bottom	$\frac{\partial \alpha_l}{\partial n} = 0, \frac{\partial \alpha_s}{\partial n} = 0$

TABLE 3.8: Boundary conditions for natural convection case.

Boundary	Conditions
Walls	$T = 255, v = 0, \frac{\partial \alpha_l}{\partial n} = 0, \frac{\partial \alpha_s}{\partial n} = 0$
Internal field	$T = 294, v = 0, \alpha_l = 1, \alpha_s = 0$

TABLE 3.9: Boundary conditions for natural convection case.

Thermophysical properties

Water properties	Symbol	Values	Units
Water density	ρ_l	999.8	$kg.m^{-3}$
Ice density	ρ_s	916.8	$kg.m^{-3}$
Water kinematic viscosity	ν_l	1.79e-6	$m^2.s^{-1}$
Ice kinematic viscosity	ν_s	2.0e-6	$m^2.s^{-1}$
Water thermal conductivity	λ_l	0.56	$W.m^{-1}.K^{-1}$
Ice thermal conductivity	λ_s	2.26	$W.m^{-1}.K^{-1}$
Heat capacity	$C_{p_l} = C_{p_s}$	4202	$J.kg.K^{-1}$
Gravitational acceleration	g	9.81	$m.s^{-2}$
Thermal diffusivity	γ	1.435e-7	$m^2.s^{-1}$
Thermal expansion coefficient	β	6.734e-5	K^{-1}
Latent heat	L	335000	$J.K^{-1}$
Laminar Prandtl number	P_r	6.99	-
Reference temperature	T_r	6.734e-5	K
Darcy's constant	D_c	10e8	-

TABLE 3.10: Water properties for natural convection.

The solver parameters used for the discretization of the different terms in the equations are pointed out next.

Solver parameters

3.5.8 Validation of Results and Conclusions

The validation of the phase change problem is achieved by different methodologies. First, the enthalpy-porosity method is compared with available data found in the thesis of [3] and [12].

Water nucleation properties	Symbol	Values	Units
Planck constant	h	6.63e-34	J.s
Boltzmann constant	k_B	1.38e-23	J.K ⁻¹
Gibbs free energy	Δ_{gv}	4e-20	J
Interfacial tension	γ_{yw}	2.91e-2	J.m ⁻²
Latent heat per volume	H_{lv}	3.10e8	J.m ⁻³
Shape coefficient of nucleation	α_{ey}	0.0001	-
Water molecule per volume	n_L	5.5e4	m ³

TABLE 3.11: Water properties for solidification.

Modeling Term	Keyword	Scheme	Remarks
Time derivatives	ddtSchemes	Euler	First order, bounded, implicit
Divergence term	divSchemes		Second order, unbounded
Gradient term	gradSchemes	Gauss linear	Second order, unbounded
Laplacian term	laplacianSchemes	Gauss linear orthogonal	
Grad. normal to cell face	snGradSchemes	orthogonal	
Point to point interpolation	interpolationSchemes	linear	Central differencing

TABLE 3.12: Discretization schemes.

Equation	Linear Solver	Smoother/Preconditioner	Tolerance
Pressure correction equation (P)	PCG	DIC	1e-5
Momentum equation (U)	smoothSolver	symGaussSeidel	1e-06
Volume fraction equation (alpha)	smoothSolver	symGaussSeidel	1e-8
Species equation (Y)	smoothSolver	symGaussSeidel	1e-09
Energy equation (T)	PBiCG 1e-08	DILU	

TABLE 3.13: Solvers for the discretised equations.

Parameter	Value
nAlphaCorr	1
nAlphaSubCycles	2
cAlpha	0
momentumPredictor	no
nOuterCorrectors	1
nNonOrthogonalCorrectors	0
nCorrectors	3

TABLE 3.14: Parameters for the discretised equations.

For the Lee model based on the *Classical Nucleation Theory*, the results are validated against the analytical solution given by the Neumann solutions of the Stefan problem.

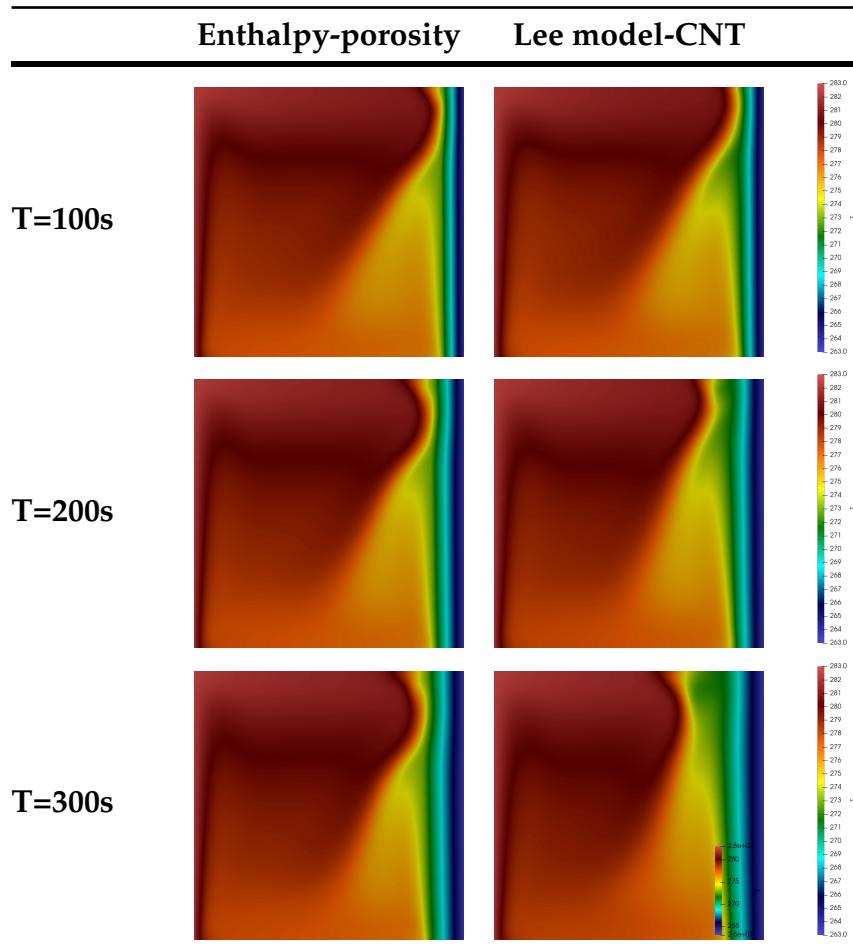


TABLE 3.15: Numerical results of temperature distributions for Enthalpy-porosity and Lee-CNT models at $t = 100, 200, 300\text{s}$.

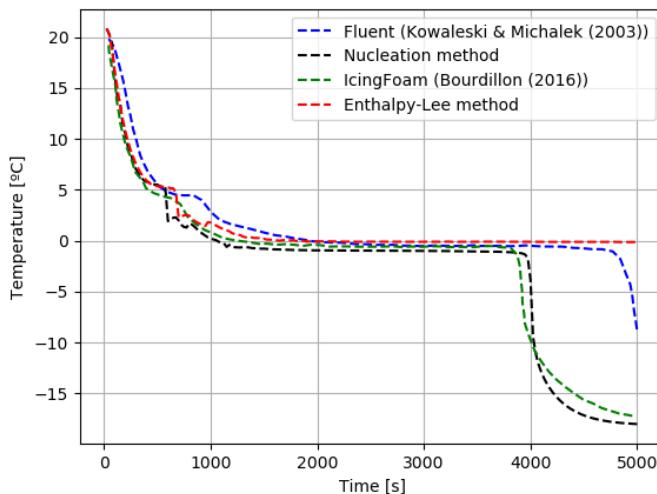


FIGURE 3.12: Numerical results of temperature profiles in center position of cylindrical geometry.

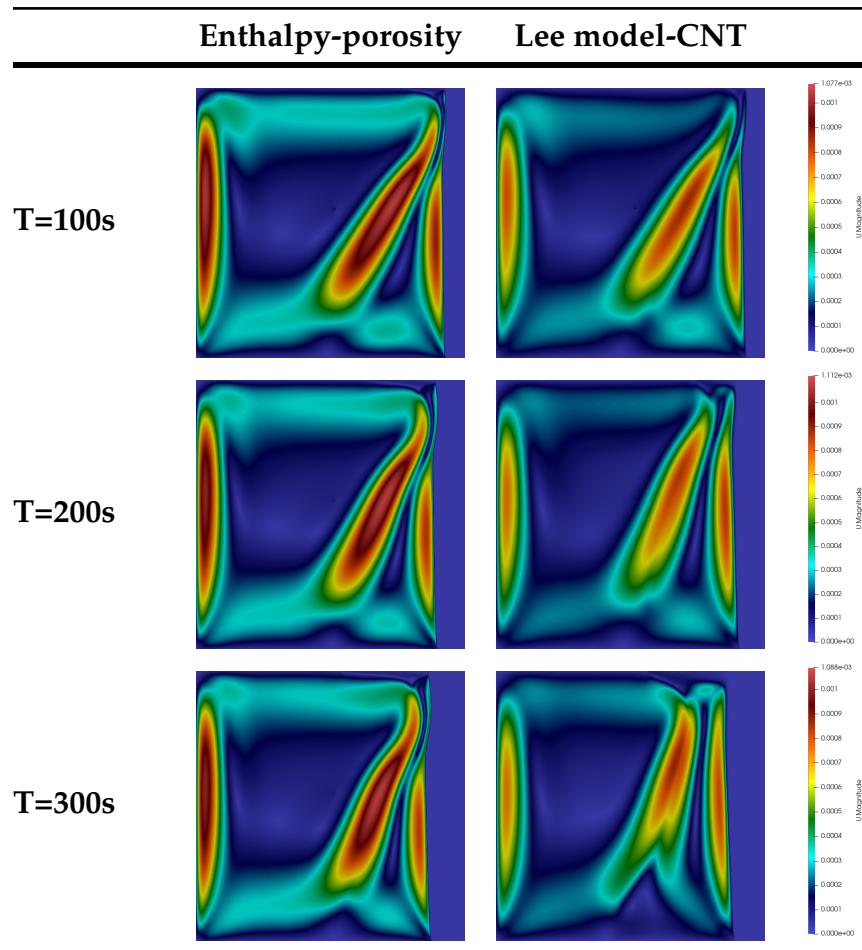


TABLE 3.16: Numerical results of velocity distributions for Enthalpy-porosity and Lee-CNT models at $t = 100, 200, 300s$.

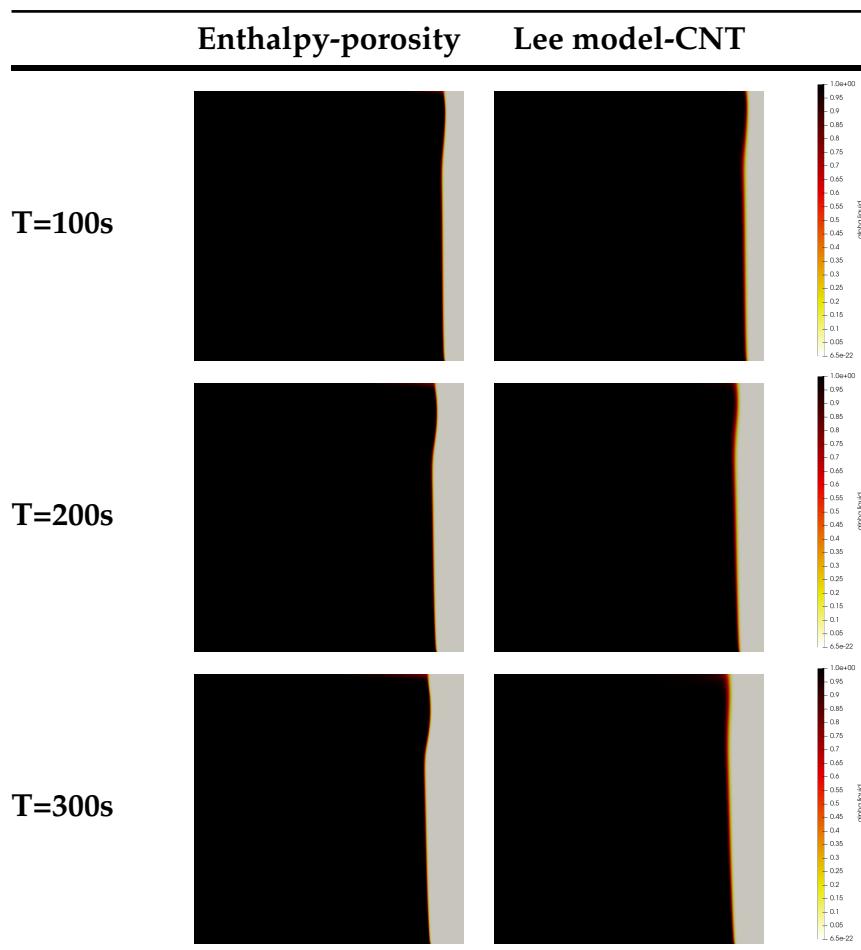


TABLE 3.17: Numerical results of fluid fraction distributions for Enthalpy-porosity and Lee-CNT models at $t = 100, 200, 300s$.

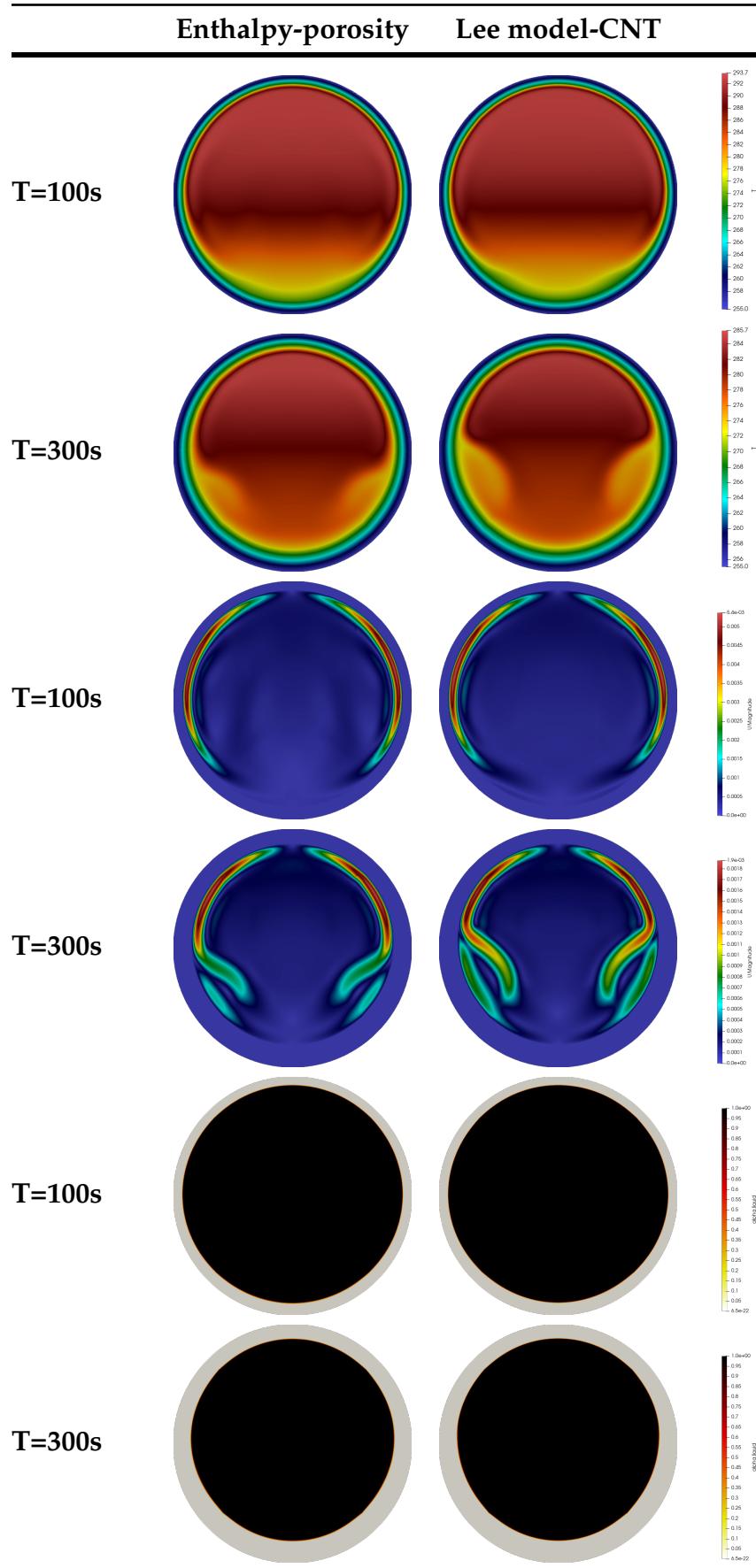


TABLE 3.18: Numerical results of Enthalpy-porosity and Lee-CNT models at $t = 100s$ and $300s$ in a cylinder.

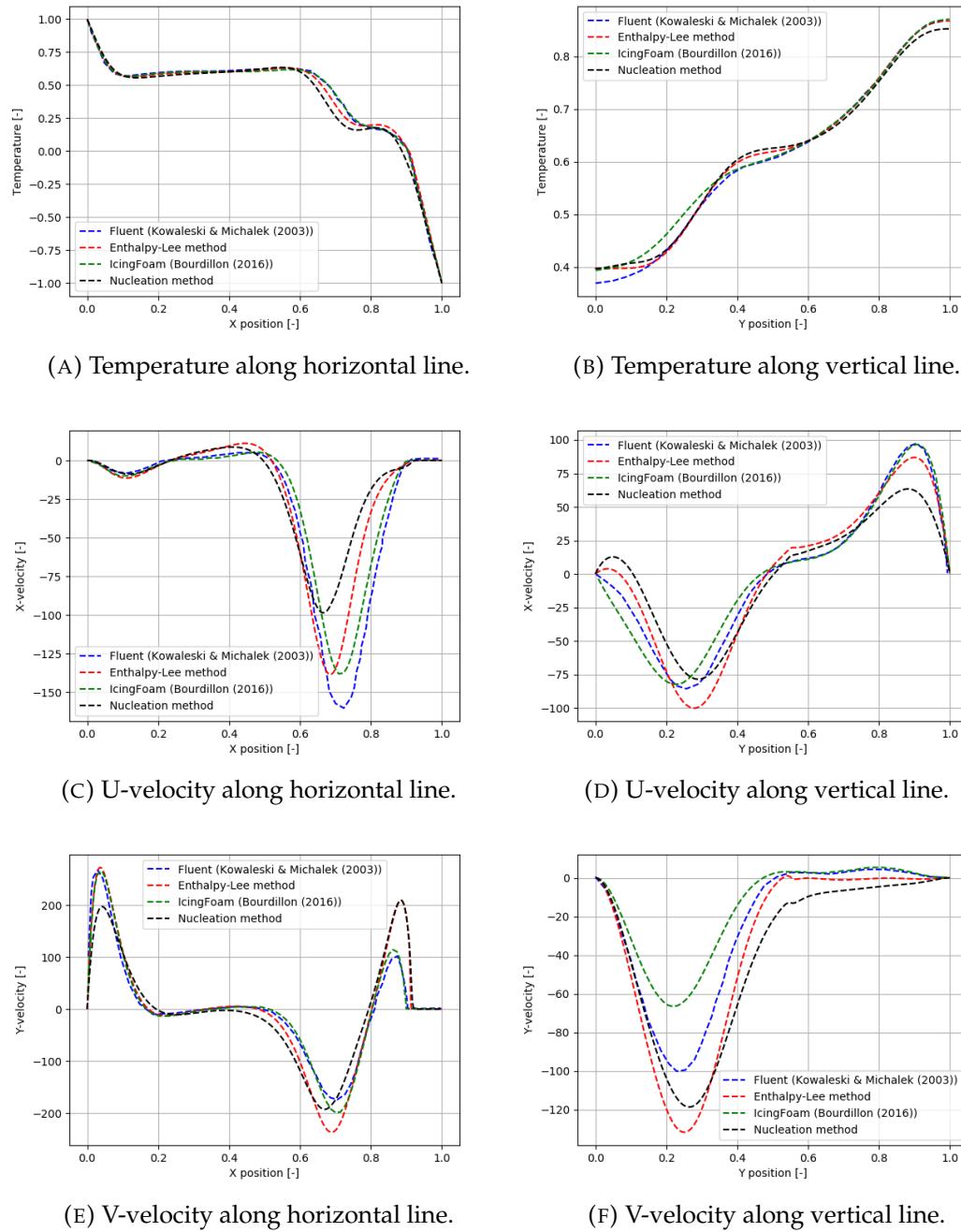


FIGURE 3.13: Adimensional magnitudes comparison.

3.5.8.1 Stefan Problem

The Stefan problem, is an initial boundary value problem of a parabolic differential equation with discontinuous coefficients on the phase transitions interfaces [[22]]. The analytical solution to the classical Stefan problem exists in a limited range of idealized situations. Some of them involve semi-infinite or infinite regions with simple and boundary conditions. Based on the work of [22] and [26], a two-region solidification process in a semi-infinite region is used to study the characteristics of the VOF-Lee model based on the Nucleation Theory.

One-dimensional problem

In seek of simplification, and recalling the 1D problem as shown in the figure: the initial conditions are expressed as:

$$u_0(x) = u_0, \quad t = 0, \quad x \in [0, L], \quad (3.42)$$

while the boundary conditions are the shown below:

$$u(0, t) = -20C, \quad \frac{\partial u}{\partial x}(L, t) = 0, \quad t > 0 \quad (3.43)$$

Boundary	Conditions
Left	$T_l = 253.15, \alpha_l = 1, \alpha_s = 0$
Right	$\frac{\partial T_r}{\partial n} = 0, \frac{\partial \alpha_l}{\partial n} = 0, \frac{\partial \alpha_s}{\partial n} = 0$
Upper	$\frac{\partial T_t}{\partial n} = 0, \frac{\partial \alpha_l}{\partial n} = 0, \frac{\partial \alpha_s}{\partial n} = 0$
Bottom	$\frac{\partial T_b}{\partial n} = 0, \frac{\partial \alpha_l}{\partial n} = 0, \frac{\partial \alpha_s}{\partial n} = 0$

TABLE 3.19: Boundary conditions for Stefan problem.

The internal field is initialized at 283.15 °C. The used thermophysical properties as well as the solver parameters are similar to the previous solidification cases.

The discontinuous exact solutions for the Stefan problem are:

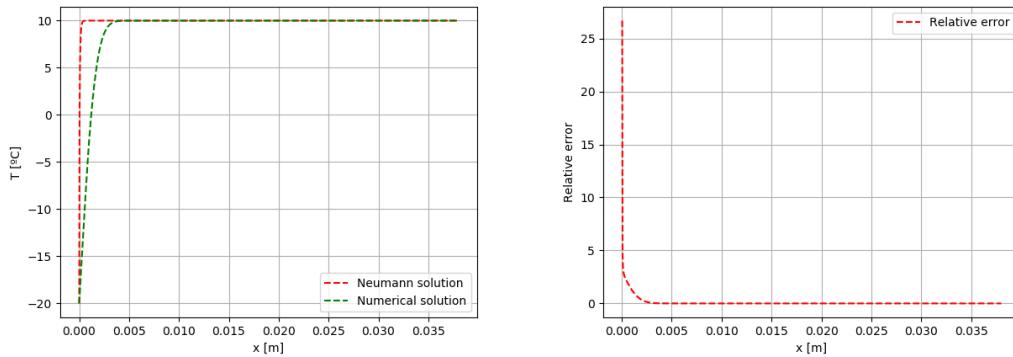
$$\begin{cases} T_l(x, t) = \frac{\operatorname{erfc}\left(\frac{x}{2\sqrt{a_1 t}}\right)}{\operatorname{erfc}\left(\lambda \sqrt{\frac{a_s}{a_1}}\right)} (T_m - T_0) + T_0, & x > \xi(t), \\ T_s(x, t) = \frac{\operatorname{erf}\left(\frac{x}{2\sqrt{a_s t}}\right)}{\operatorname{erf}} (T_m - T_b) + T_b, & x \leq \xi(t). \end{cases} \quad (3.44)$$

By using a phase change interface condition, a solution to the trascendental equation may be found:

$$\frac{e^{-\lambda^2}}{\operatorname{erf}(\lambda)} + \frac{k_l}{k_s} \sqrt{\frac{a_s}{a_1}} \frac{T_m - T_0}{T_m - T_b} \frac{e^{-\frac{a_s}{a_1} \lambda^2}}{\operatorname{erfc}\left(\lambda \sqrt{\frac{a_s}{a_1}}\right)} = \frac{\lambda L \sqrt{\pi}}{c_{ps} (T_m - T_b)} \quad (3.45)$$

The secant method is used as the iterative scheme to find the root of the given function with $tol < 1e - 12$. The root of γ is 0.2299545377262345.

In the following figures, the method is tested against the exact solutions of the Stefan problem.



(A) Neumann solution vs numerical solution. (B) Relative error of the numerical solution.

FIGURE 3.14: Numerical solutions of the Lee model-CNT vs Neumann analytical solutions.

The first key thing to point out is that the Stefan problem does not take into consideration the interface tensions and contact angles. The solution considers a planar interface so that the curvature κ vanishes and the effect of $\kappa\sigma$ on the interface is ignored. Another point to remark is the effect of the Stefan number properly. According to ...

The kinematic undercooling...

3.5.8.2 Interface height

The theoretical solution for the evolution of the interface is:

$$X(t) = 2\lambda\sqrt{a_s t} \quad (3.46)$$

Alongside, a post-process function to calculate the tracking of position of the interface is done. To do so, the values of the liquid fraction per timestep are first obtained. Thus, these values for each time are read to find the position in which alpha is 0.5. The python code is attached in Appendix A.

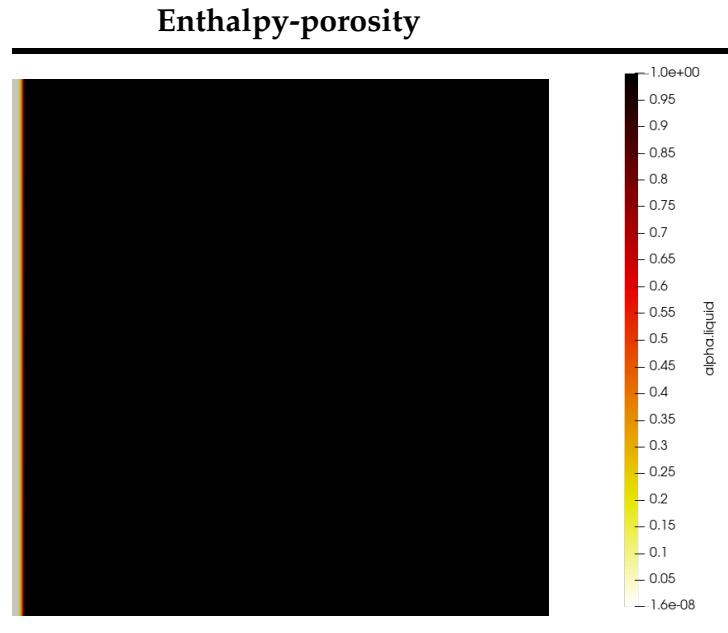


TABLE 3.20: Numerical results of alpha fraction for Enthalpy-porosity model at $t = 6\text{s}$.

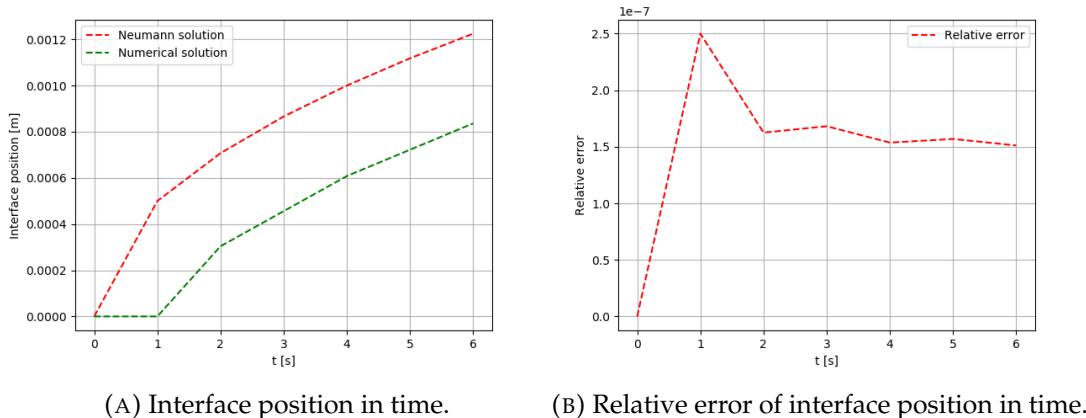


FIGURE 3.15: Numerical solutions of the Lee model-CNT vs Neumann analytical solutions for interface position.

Chapter 4

Numerical Simulation of Heat Transfer

4.1 OpenFOAM: chtMultiphaseInterFOAM. Conjugate Heat Transfer

The last objective of this thesis is to extend the multiphase solver of the previous section so it can account for multiregion purposes. To do so, a new solver derived from the concept of an existing multiregion solver is implemented. The existing solver, *chtMultiRegionFoam* is developed on the basis that the fluid it solves undergoes the compressible Navier-Stokes equations with buoyancy forces and the energy equation per unit mass with gravity terms as follows:

Continuity Equation

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0 \quad (4.1)$$

Momentum Equation

$$\begin{aligned} \frac{\partial \rho \mathbf{u}}{\partial t} + \nabla \cdot (\rho \mathbf{u} \otimes \mathbf{u}) = \\ - \nabla p_{\text{rgb}} + \nabla \cdot \left[\mu \left\{ \nabla \otimes \mathbf{u} + (\nabla \otimes \mathbf{u})^T \right\} \right] - \nabla \left(\frac{2}{3} \mu \nabla \cdot \mathbf{u} \right) - \mathbf{g} \cdot \mathbf{x} \nabla \rho \end{aligned} \quad (4.2)$$

Energy Equation

$$\frac{\partial \rho h}{\partial t} + \nabla \cdot (\rho \mathbf{u} h) + \nabla \cdot (\rho \mathbf{u} K) = \nabla \cdot \left(\frac{\lambda}{c_p} \nabla h \right) + \rho \mathbf{u} \cdot \mathbf{g} \quad (4.3)$$

where \mathbf{u} is the velocity vector, h is the enthalpy, $K = 0.5 * \mathbf{u} \cdot \mathbf{u}$ is the kinetic energy per unit mass, $p_{rgh} = p - \rho g \cdot \mathbf{x}$ the modified pressure so that the momentum equation accounts for the buoyancy terms, and the remaining thermophysical properties, μ , λ , C_p being the kinematic viscosity, the thermal conductivity and the specific heat accordingly. The energy equation does not include radiation, heat generation term and chemical reaction.

Therefore, the challenge of this part is to couple the multiphase solver (*IcoReactingMultiPhaseInterFoam*) that allows for the solving of a fluid undergoing phase-change with a solid region.

4.1.1 Case description

Within this new case, a mesh for the solid region is required. To do so, a second structured mesh region is implemented within the framework of a provided script which builds cylindrical computational meshes in OpenFOAM format. The script is attached in Appendix B. In the image shown above, a

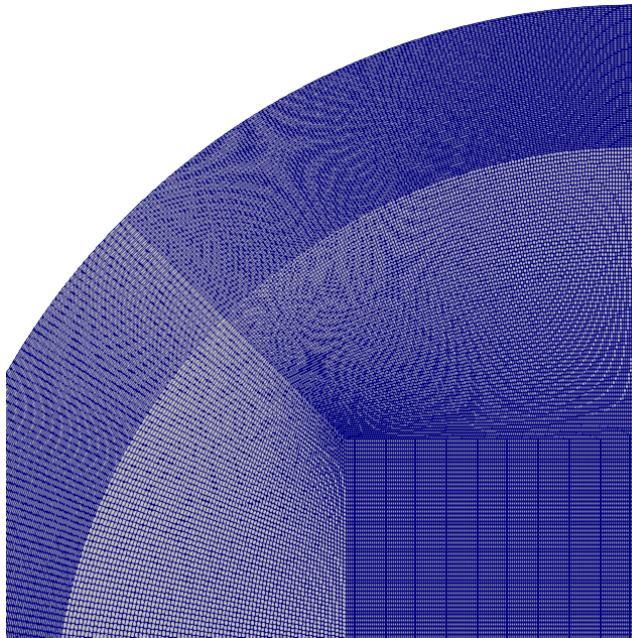


FIGURE 4.1: Computational mesh for the conjugate heat transfer case.

structured mesh of 731734 nodes is generated.

4.1.2 Hypotheses And Assumptions

Heat transfer: Conductive heat transfer is transferred throughout an isotropic material.

Laminar regime: The Reynolds number, computed from the maximum velocity is not high enough to consider turbulent effects.

In the current case-scenario, a Prandtl close to 7. The values used for the laminar Prandtl number calculation are: $\mu = 0.001003 \text{ Kg.m}^{-1}.\text{s}^{-1}$, $\lambda = 0.6 \text{ W.m}^{-1}.\text{K}^{-1}$

and $C_p = 4182 \text{ J.Kg.K}^{-1}$.

Newtonian fluid: The viscosity of the fluid is assumed to be constant. As per the solidification cases, the treatment of the thermophysical properties is performed in a similar manner.

4.1.3 Governing Equations of the Fluid Region

Momentum equation

The momentum equation is recalled here in terms of viscous stress tensor. The surface tension forces as the body forces and the Darcy term is added in the momentum equation as shown below.

$$\begin{aligned} \frac{\partial(\rho u_i)}{\partial t} + \frac{\partial(\rho u_i u_j)}{\partial x_j} \\ = -\alpha_i \nabla p + \nabla \cdot \tau + F_{\sigma i} + S_{u_i} + S_b \end{aligned} \quad (4.4)$$

Energy equation

The energy equation is also described here in terms of temperature and specific heat. Moreover, as for in the energy equation in the multiphase solver, the latent term here is also added, S_{H_i} but also the aforementioned terms concerning the buoyancy, the pressure and the viscous dissipation.

$$\frac{\partial(\rho C_p T)}{\partial t} + \nabla \cdot (u_j \rho C_p T) + \nabla \cdot (\mathbf{u} p) = \nabla \cdot (k_i \nabla T_i) + \nabla \cdot (\boldsymbol{\tau} \cdot \mathbf{u}) + \rho g \cdot \mathbf{u} + S_{H_i} \quad (4.5)$$

4.1.4 Governing Equations of the Solid Region

4.1.4.1 Energy Equation

The heat transfer in solids is mainly governed by the heat conduction equation:

$$\frac{\partial(\rho h)}{\partial t} - \nabla \cdot \left(\frac{\lambda}{\rho c_p} \nabla h \right) = 0 \quad (4.6)$$

chtMultiphaseInterFoam is a new solver derived from the existing solver cht-MultiRegionFoam. It is implemented to cope with transient fluid flow and solid heat conduction with conjugate heat transfer between regions. The solution follows a sequential strategy: equations of the fluid are first solved using the temperatures of the solid of the preceding loop to set the boundary conditions for the fluid part. Then, the equation for the solid is solved with the temperatures of the fluid to define lately the boundary conditions of the solid. This process is iteratively executed until convergence is reached.

4.1.5 Solver description. Control Loop

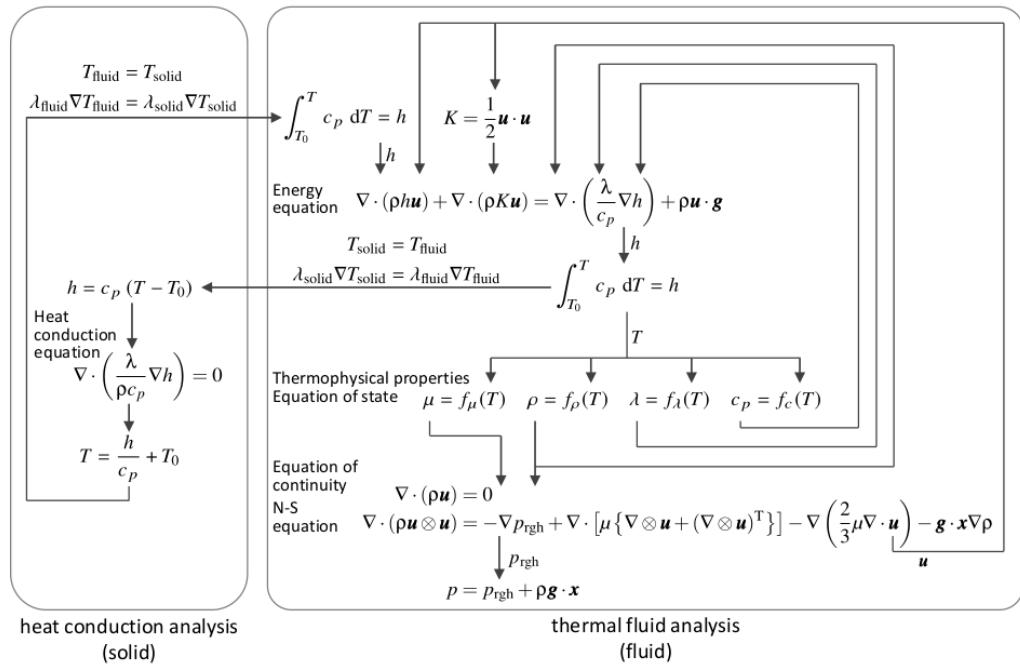


FIGURE 4.2: Flowchart of the conjugate heat transfer solver [20].

4.1.6 Code implementations

As remarked in the previous section, in the context of multiregion solvers, OpenFOAM offers the possibility of solving a fluid representing the compressible Navier-Stokes equations. However, the purpose of this final part is to enhance the capability of this solver so it can handle multiphase fluids submitted to conjugate heat transfer conditions. To do so, and in favour of using the majority of possibilities that the solver brings, the energy equation in the solid part is kept without change. On the other side, the fluid part of the solver is implemented by integrating the multiphase solver used in the solidification section of this thesis. The implemented solver can be found in Appendix B but here are presented the main changes.

The first change is the way in which the fluid is solver. In figure ???. The loop in the fluid is corrected in such a way it incorporates the *IcoReactingMultiphaseInterFoam* solver.

```

if (finalIter)
{
    mesh.data::add("finalIteration", true);
}

#include "initCorrectPhi.H"

if (firstIter)
{
    thermol.correctMassSources(T);
    thermol.solve();
    rho = thermol.rho();
}

if (frozenFlow)
{
    #include "TEqnFluidPhase.H"
}
else
{

    #include "UEqnFluidPhase.H"
    #include "YEqnFluidPhase.H"
    #include "TEqnFluidPhase.H"
    // --- PISO loop

    for (int corr=0; corr<nCorr; corr++)
    {
        #include "pEqnFluidPhase.H"
    }
    if (pimple.turbCorr())
    {
        turbulence.correct();
    }
}

if (finalIter)
{
    rho = thermol.rho();
    mesh.data::remove("finalIteration");
}

```

FIGURE 4.3: Control loop for the fluid region in CHT.

On the other side, the energy equation is adapted so it can cope with multi-phase fluids in the scope of multi region solvers. In the way of building up the equation, some of the terms that are newly introduced are the buoyancy energy, $\rho(U \cdot g)$, and the pressure terms $\nabla \cdot (\mathbf{u} p)$ and the viscous dissipation term, $\nabla \cdot (\boldsymbol{\tau} \cdot \mathbf{u})$, where $\boldsymbol{\tau}$, the viscous stress tensor is calculated in the upper part of the code as the product of 2 by both the dynamic viscosity and the strain rate tensor.

$$\boldsymbol{\tau} = 2\mu \mathbf{D} \quad (4.7)$$

Where \mathbf{D} is the strain rate tensor:

$$\mathbf{D} = -\frac{1}{2} [\nabla \mathbf{u} + \nabla \mathbf{u}^\top] = -\frac{1}{2} \begin{pmatrix} 2\frac{\partial u_x}{\partial x} & \frac{\partial u_y}{\partial x} + \frac{\partial u_x}{\partial y} & \frac{\partial u_z}{\partial x} + \frac{\partial u_x}{\partial z} \\ \frac{\partial u_x}{\partial y} + \frac{\partial u_y}{\partial x} & 2\frac{\partial u_y}{\partial y} & \frac{\partial u_z}{\partial y} + \frac{\partial u_y}{\partial z} \\ \frac{\partial u_x}{\partial z} + \frac{\partial u_z}{\partial x} & \frac{\partial u_y}{\partial z} + \frac{\partial u_z}{\partial y} & 2\frac{\partial u_z}{\partial z} \end{pmatrix} \quad (4.8)$$

If substituting terms, it yields:

$$\boldsymbol{\tau} = -\mu \left[\nabla \mathbf{u} + \nabla \mathbf{u}^\top \right] \quad (4.9)$$

```
{
    rhoCp = rho*thermol.Cp();

    rhok = rho - rhoR;
    const surfaceScalarField rhoCpPhi(fvc::interpolate(thermol.Cp())*rhoPhi);
    volTensorField gradU = fvc::grad(U);
    volTensorField tau = turbulence.muEff() * (gradU + gradU.T());
    const volScalarField kappaEff
    (
        "kappaEff",
        thermol.kappa() + thermol.Cp()*turbulence.mut()/thermol.Prt()
    );

    fvScalarMatrix TEqn
    (
        fvm::ddt(rhoCp, T)
        + fvm::div(rhoCpPhi, T, "div(phi,T)")
        + fvc::div(rhoPhi/fvc::interpolate(rho), p, "div(phiv,p)")
        + fvc::ddt(rho, K) + fvc::div(rhoPhi, K)
        - fvm::laplacian(kappaEff, T, "laplacian(kappa,T)")
        ==
        thermol.heatTransfer(T)
        + fvc::div(tau & U, "div(tau,U)")
        + rho*(U&g)
        + fvOptions(rhoCp, T)
    );
    TEqn.relax();

    fvOptions.constrain(TEqn);

    TEqn.solve(mesh.solver(T.select(finalIter)));
    fvOptions.correct(T);
    thermol.correct();

    Info<< "min/max(T) = " << min(T).value() << ", " << max(T).value() << endl;
}
}
```

FIGURE 4.4: Energy equation for the fluid in CHT.

4.1.7 Case Setup

The case geometry is a plane cylinder, taking profit form the fluid mesh generated for the solidification case presented in the previous section. However, in this section, symmetry conditions are applied on the vertical axis (axis Y) so as to reduce the computational cost.

4.1.7.1 Boundary conditions

The boundary conditions are, in this case, setted up for both solid and fluid regions. Here it is shown a table summarizing the used ones.

For the fluid region: For the solid region:

Boundary	Conditions
Internal field	$T = 298, u = 0, \alpha_l = 1, \alpha_s = 0$
fluidFrontAndBack	empty
fluidSymmetryBC	symmetryPlane

TABLE 4.1: Boundary conditions for the fluid region in CHT problem.

Boundary	Conditions
Internal field	$T = 298$
solidWalls	$T = 258$
solidSymmetryBC	symmetryPlane
solidFrontAndBack	empty

TABLE 4.2: Boundary conditions for the solid region in CHT problem.

At the interface between solid and liquid regions, it is required to set an appropriate boundary condition which couples the energy equations in these areas.

Considering two cells at each side of the interface such as in the Figure where T_c and T_p is the temperature at the cell center and on the patch (2D boundary) accordingly. q_1 is the heat flux going out of the $cell_1$ and q_2 the heat flux entering the $cell_2$. The energy conservation in this zone constrains the temperature and heat fluxes to be equal at both sides of the interface. Then, temperature, in magnitude yields as

$$T_{p,1} = T_{p,2} = T_p, \quad (4.10)$$

and as well, for the fluxes

$$q''_1 = q''_2 = q'' \quad (4.11)$$

while the magnitude for the heat fluxes is derived from the one-dimensional expression for the Fourier's law and it gives

$$-k_1 \frac{\partial T}{\partial n} \Big|_{\text{side 1}} = -k_2 \frac{\partial T}{\partial n} \Big|_{\text{side 2}} \quad (4.12)$$

where κ is the thermal conductivity and n the direction normal to the patch. Discretizing linearly the temperature gradient of the previous equation, and with respect of the scheme of the Figure [], the differential equation that yields

$$k_1 \Delta_1 (T_{c,1} - T_p) = k_2 \Delta_2 (T_p - T_{c,2}) \quad (4.13)$$

where the temperatures and fluxes at the center of the patches are described as

$$\begin{aligned} T_p &= \frac{k_1\Delta_1 T_{c,1} + k_2\Delta_2 T_{c,2}}{k_1\Delta_1 + k_2\Delta_2} \\ q'' &= k_1\Delta_1 (T_{c,1} - T_p) = k_2\Delta_2 (T_p - T_{c,2}). \end{aligned} \quad (4.14)$$

This boundary condition is given in OpenFOAM under the name *turbulent-TemperatureCoupledBaffleMixed*. The required input is the temperature at the patch. Therefore, that temperature for the interface between the liquid and the solid regions is initially setted at 298°C.

4.1.7.2 Thermophysical properties

The thermophysical properties for the fluid are similarly applied as in previous solidification cases. For the solid region, the thermophysical properties are chosen as for the polyethylene.

Polyethylene properties	Symbol	Values	Units
Density	ρ	940	$kg.m^{-3}$
Thermal conductivity	λ	0.56	$W.m^{-1}.K^{-1}$
Heat capacity	C_p	1330	$J.kg.K^{-1}$
Latent heat	L	178600	$J.K^{-1}$

TABLE 4.3: Polyethylene properties for solind region definition.

4.1.8 Validation of Results and Conclusions

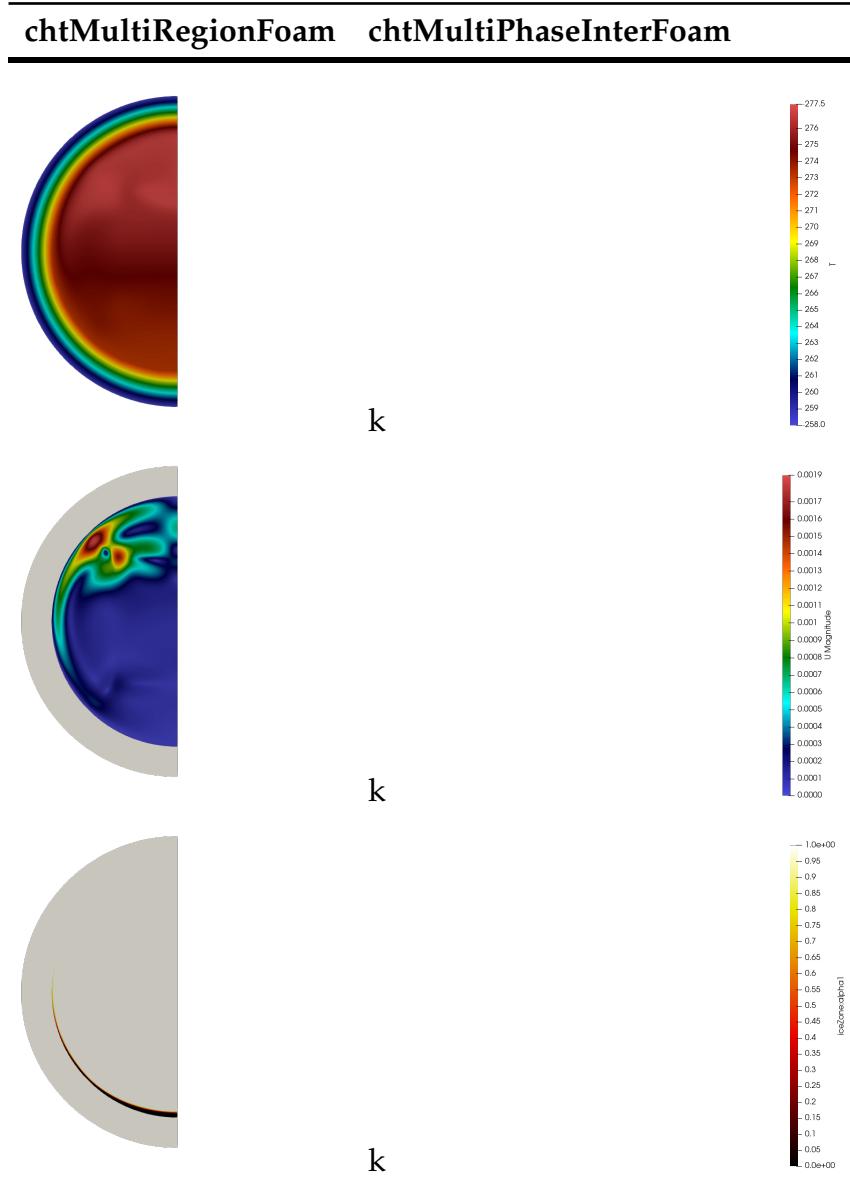


TABLE 4.4: Numerical results of Enthalpy-porosity and Lee-CNT models at $t = 100s$ and $300s$ in a cylinder.

Chapter 5

Conclusions

Chapter 6

Future Works

Bibliography

- [1] M. Akyurt, G. Zaki, and B. Habeebullah. "Freezing phenomena in ice-water systems". In: *Energy Conversion and Management* 43.14 (2002), pp. 1773–1789. DOI: [10.1016/s0196-8904\(01\)00129-7](https://doi.org/10.1016/s0196-8904(01)00129-7).
- [2] Edin Berberovic et al. "Drop impact onto a liquid layer of finite thickness: Dynamics of the cavity evolution". In: *Physical Review E* 79.3 (2009). DOI: [10.1103/physreve.79.036306](https://doi.org/10.1103/physreve.79.036306).
- [3] Arnaud Bourdillon. "Investigation towards a coupling between population balance and solidification models". PhD thesis. Cranfield University, 2016.
- [4] Long-Qing Chen. "Phase-Field Models for Microstructure Evolution". In: *Annual Review of Materials Research* 32.1 (2002), pp. 113–140. DOI: [10.1146/annurev.matsci.32.112001.132041](https://doi.org/10.1146/annurev.matsci.32.112001.132041).
- [5] M El Ganaoui et al. "Computational solution for fluid flow under solid/liquid phase change conditions". In: *Computers Fluids* 31.4-7 (2002), pp. 539–556. DOI: [10.1016/s0045-7930\(01\)00067-6](https://doi.org/10.1016/s0045-7930(01)00067-6).
- [6] A Esen and S Kutluay. "A numerical solution of the Stefan problem with a Neumann-type boundary condition by enthalpy method". In: *Applied Mathematics and Computation* 148.2 (2004), pp. 321–329. DOI: [10.1016/s0096-3003\(02\)00846-9](https://doi.org/10.1016/s0096-3003(02)00846-9).
- [7] H. Harlow and J. Welch. "Numerical Calculation of Time-Dependent Viscous Incompressible Flow of Fluid with Free Surface". In: *Physics of Fluids* 8.12 (1965), p. 2182. DOI: [10.1063/1.1761178](https://doi.org/10.1063/1.1761178).
- [8] C.W Hirt and B.D Nichols. "Volume of fluid (VOF) method for the dynamics of free boundaries". In: *Journal of Computational Physics* 39.1 (1981), pp. 201–225. DOI: [10.1016/0021-9991\(81\)90145-5](https://doi.org/10.1016/0021-9991(81)90145-5).
- [9] Chengyu Huang, Wenhua Wang, and Weizhong Li. "A Novel 2D Model for Freezing Phase Change Simulation during Cryogenic Fracturing Considering Nucleation Characteristics". In: *Applied Sciences* 10.9 (2020), p. 3308. DOI: [10.3390/app10093308](https://doi.org/10.3390/app10093308).
- [10] Luisa Ickes et al. "Classical nucleation theory of homogeneous freezing of water: thermodynamic and kinetic parameters". In: *Physical Chemistry Chemical Physics* 17.8 (2015), pp. 5514–5537. DOI: [10.1039/c4cp04184d](https://doi.org/10.1039/c4cp04184d).
- [11] Damir Juric and Gretar Tryggvason. "A Front-Tracking Method for Dendritic Solidification". In: *Journal of Computational Physics* 123.1 (1996), pp. 127–148. DOI: [10.1006/jcph.1996.0011](https://doi.org/10.1006/jcph.1996.0011).
- [12] T. A. KOWALEWSKI and M. REBOW. "Freezing of Water in a Differentially Heated Cubic Cavity". In: *International Journal of Computational Fluid Dynamics* 11.3-4 (1999), pp. 193–210. DOI: [10.1080/10618569908940874](https://doi.org/10.1080/10618569908940874).

- [13] K. Krabbenhoft, L. Damkilde, and M. Nazem. "An implicit mixed enthalpy-temperature method for phase-change problems". In: *Heat and Mass Transfer* 43.3 (2006), pp. 233–241. DOI: [10.1007/s00231-006-0090-1](https://doi.org/10.1007/s00231-006-0090-1).
- [14] Chin Li, Suresh Garimella, and James Simpson. "Fixed-grid front-tracking algorithm for solidification problems, part I: method and validation". In: *Numerical Heat Transfer, Part B: Fundamentals* 43.2 (2003), pp. 117–141. DOI: [10.1080/713836172](https://doi.org/10.1080/713836172).
- [15] Fadl Hassan Moukalled, L Mangani, and M Darwish. *The finite volume method in computational fluid dynamics*. Springer, 2016, pp. 4–5.
- [16] P. Rauschenberger et al. "Comparative assessment of Volume-of-Fluid and Level-Set methods by relevance to dendritic ice growth in super-cooled water". In: *Computers Fluids* 79 (2013), pp. 44–52. DOI: [10.1016/j.compfluid.2013.03.010](https://doi.org/10.1016/j.compfluid.2013.03.010).
- [17] Nabeel Al-Rawahi and Gretar Tryggvason. "Numerical Simulation of Dendritic Solidification with Convection: Two-Dimensional Geometry". In: *Journal of Computational Physics* 180.2 (2002), pp. 471–496. DOI: [10.1006/jcph.2002.7092](https://doi.org/10.1006/jcph.2002.7092).
- [18] C. M. Rhie and W. L. Chow. "Numerical study of the turbulent flow past an airfoil with trailing edge separation". In: *AIAA Journal* 21.11 (1983), pp. 1525–1532. DOI: [10.2514/3.8284](https://doi.org/10.2514/3.8284).
- [19] Fabian Rösler and Dieter Brüggemann. "Shell-and-tube type latent heat thermal energy storage: numerical analysis and comparison with experiments". In: *Heat and Mass Transfer* 47.8 (2011), pp. 1027–1033. DOI: [10.1007/s00231-011-0866-9](https://doi.org/10.1007/s00231-011-0866-9).
- [20] T. Sugimoto et al. "Thermal Fluid Coupled Analysis of Hydrothermal Destruction Reactor". In: *14th WCCM-ECCOMAS Congress* (2021). DOI: [10.23967/wccm-eccomas.2020.342](https://doi.org/10.23967/wccm-eccomas.2020.342).
- [21] Lijian Tan and Nicholas Zabaras. "A level set simulation of dendritic solidification of multi-component alloys". In: *Journal of Computational Physics* 221.1 (2007), pp. 9–40. DOI: [10.1016/j.jcp.2006.06.003](https://doi.org/10.1016/j.jcp.2006.06.003).
- [22] Vasily Vasilyev and Maria Vasilyeva. "An Accurate Approximation of the Two-Phase Stefan Problem with Coefficient Smoothing". In: *Mathematics* 8.11 (2020), p. 1924. DOI: [10.3390/math8111924](https://doi.org/10.3390/math8111924).
- [23] V. R. Voller and C. Prakash. "A fixed grid numerical modelling methodology for convection-diffusion mushy region phase-change problems". In: *International Journal of Heat and Mass Transfer* 30.8 (1987), pp. 1709–1719. DOI: [10.1016/0017-9310\(87\)90317-6](https://doi.org/10.1016/0017-9310(87)90317-6).
- [24] V.R. Voller. "An enthalpy method for modeling dendritic growth in a binary alloy". In: *International Journal of Heat and Mass Transfer* 51.3-4 (2008), pp. 823–834. DOI: [10.1016/j.ijheatmasstransfer.2007.04.025](https://doi.org/10.1016/j.ijheatmasstransfer.2007.04.025).
- [25] Daoyong Wu, Yuanming Lai, and Mingyi Zhang. "Heat and mass transfer effects of ice growth mechanisms in a fully saturated soil". In: *International Journal of Heat and Mass Transfer* 86 (2015), pp. 699–709. DOI: [10.1016/j.ijheatmasstransfer.2015.03.044](https://doi.org/10.1016/j.ijheatmasstransfer.2015.03.044).

- [26] Y. Zhao, C.Y. Zhao, and Z.G. Xu. "Numerical study of solid-liquid phase change by phase field method". In: *Computers Fluids* 164 (2018), pp. 94–101. DOI: [10.1016/j.compfluid.2017.05.032](https://doi.org/10.1016/j.compfluid.2017.05.032).

Appendix A

Appendix A: Solidification models

A.1 Enthalpy-porosity library

A.1.1 mySolidificationMeltingSource.H

```
/*
----- * \
=====
\\      / Field          / OpenFOAM: The Open Source CFD
     Toolbox
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```

```

Class
    Foam::fv::mySolidificationMeltingSource

Group
    grpFvOptionsSources

Description
    This source is designed to model the effect of
    solidification and
    melting processes, e.g. windshield defrosting, within a
    specified region.
    The phase change occurs at the melting temperature, \c Tmelt
    .

    The presence of the solid phase in the flow field is
    incorporated into the
    model as a momentum porosity contribution; the energy
    associated with the
    phase change is added as an enthalpy contribution.

References:
\verb+at+  

    Voller, V. R., & Prakash, C. (1987).
    A fixed grid numerical modelling methodology for
    convection-diffusion mushy region phase-change problems.
    International Journal of Heat and Mass Transfer, 30(8),
    1709-1719.  

    DOI:10.1016/0017-9310(87)90317-6

    Swaminathan, C. R., & Voller, V. R. (1992).
    A general enthalpy method for modeling solidification
    processes.
    Metallurgical transactions B, 23(5), 651-664.  

    DOI:10.1007/BF02649725

\verb+endat+  

The model generates a field \c \<name\>:alpha1 which can be
visualised to
to show the melt distribution as a fraction [0-1].  

Usage
Minimal example by using \c constant/fvOptions:  

\verb+at+  

mySolidificationMeltingSource1  

{  

    // Mandatory entries (unmodifiable)
    type           mySolidificationMeltingSource;  

    // Mandatory entries (runtime modifiable)
    Tmelt          273;
    L              334000;
    thermoMode    <thermoModeName>;
    rhoRef         800;
    beta           5e-6;  

    // Optional entries (runtime modifiable)
    relax          0.9;
}

```

```

T           < Tname >;
rho         < rhoName >;
U           < Uname >;
phi         < phiName >;
Cu          1e5;
q           1e-2;

// Conditional optional entries (runtime modifiable)

// when thermoMode=lookup
Cp          Cp;

// Conditional mandatory entries (runtime modifiable)

// when Cp=CpRef
CpRef      1000;

// Mandatory/Optional (inherited) entries
...
}

\endverbatim

```

where the entries mean:

\table

Property	/ Description	/ Type
Reqd	/ Dflt	
type	/ Type name: mySolidificationMeltingSource	/
word	/ yes / -	
Tmelt	/ Melting temperature [K]	/ scalar
yes	/ -	
L	/ Latent heat of fusion [J/kg]	/ scalar
yes	/ -	
thermoMode	/ Thermo mode	/ word
yes	/ -	
rhoRef	/ Reference (solid) density	/ scalar
yes	/ -	
beta	/ Thermal expansion coefficient [1/K]	/ scalar
yes	/ -	
relax	/ Relaxation factor [0-1]	/ scalar
no	/ 0.9	
T	/ Name of operand temperature field	/ word
no	/ T	
rho	/ Name of operand density field	/ word
no	/ rho	
U	/ Name of operand velocity field	/ word
no	/ U	
phi	/ Name of operand flux field	/ word
no	/ phi	
Cu	/ Mushy region momentum sink coefficient [1/s]	
<!--	-->	/ scalar
	no / 1e5	
q	/ Coefficient used in porosity calc	/ scalar
no	/ 1e-2	
Cp	/ Name of specific heat capacity field	/ word
cndtnl	/ Cp	

```

CpRef      / Specific heat capacity value           / scalar /
cndtnl    / -
\endtable

The inherited entries are elaborated in:
- \link fvOption.H \endlink
- \link cellSetOption.H \endlink

Options for the \c thermoMode entry:
\verbatim
thermo      / Access Cp information from database
lookup      / Access Cp information by looking up from
             dictionary
\endverbatim

SourceFiles
mySolidificationMeltingSource.C
mySolidificationMeltingSourceTemplates.C

/*
----- */

#ifndef mySolidificationMeltingSource_H
#define mySolidificationMeltingSource_H

#include "fvMesh.H"
#include "volFields.H"
#include "cellSetOption.H"
#include "Enum.H"

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
// * * * * * * //


namespace Foam
{
namespace fv
{

/*-----*/
/*-----*/
Class mySolidificationMeltingSource Declaration
/*-----*/
/*-----*/

class mySolidificationMeltingSource
:
public cellSetOption
{

// Private Data

//- Temperature at which melting occurs [K]
scalar Tmelt_;

//- Latent heat of fusion [J/kg]
scalar L_;

```

```

// Phase fraction under-relaxation coefficient
scalar relax_;

// Name of operand temperature field
word TName_;

// Name of specific heat capacity field
word CpName_;

// Name of operand velocity field
word UName_;

// Name of operand flux field
word rhoCpPhiName_;

// Calculated Phase fraction indicator field for PCM
volScalarField alphaC_;

// Phase fraction indicator field for VOF
volScalarField alpha1_;

// Current time index (used for updating)
label curTimeIndex_;

void update();

// Helper function to apply to the energy equation
template<class RhoFieldType>
void apply(const RhoFieldType& rho, fvMatrix<scalar>& eqn);

public:

// Runtime type information
TypeName("mySolidificationMeltingSource");

// Constructors

// Construct from explicit source name and mesh
mySolidificationMeltingSource
(
    const word& sourceName,
    const word& modelType,
    const dictionary& dict,
    const fvMesh& mesh
);

// No copy construct
mySolidificationMeltingSource
(
    const mySolidificationMeltingSource&
) = delete;

// No copy assignment

```

```

        void operator=(const mySolidificationMeltingSource&) =
            delete;

        // - Destructor
        ~mySolidificationMeltingSource() = default;

        // Member Functions

        // - Add explicit contribution to enthalpy equation
        virtual void addSup(fvMatrix<scalar>& eqn, const label
            fieldi);

        // - Add explicit contribution to compressible enthalpy
        //   equation
        virtual void addSup
        (
            const volScalarField& rho,
            fvMatrix<scalar>& eqn,
            const label fieldi
        );

        // - Read source dictionary
        virtual bool read(const dictionary& dict);
};

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
// * * * * * * // 

} // End namespace fv
} // End namespace Foam

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
// * * * * * * // 

#ifndef NoRepository
    #include "mySolidificationMeltingSourceTemplates.C"
#endif

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
// * * * * * * // 

#endif

// *****
// ****

```

A.1.2 mySolidificationMeltingSource.C

```

/*
----- * |
===== | 
\\ / Field | 
    Toolbox | 
\\ / Operation | 

```

```
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/*
-----*/



#include "mySolidificationMeltingSource.H"
#include "fvMatrices.H"
#include "basicThermo.H"
#include "gravityMeshObject.H"
#include "zeroGradientFvPatchFields.H"
#include "extrapolatedCalculatedFvPatchFields.H"
#include "addToRunTimeSelectionTable.H"
#include "geometricOneField.H"
#include <cmath>
// * * * * * * * * * * * * * * * * Static Member Functions * * * * *
* * * * * //



namespace Foam
{
namespace fv
{
defineTypeNamesAndDebug(mySolidificationMeltingSource, 0);
addToRunTimeSelectionTable(option,
    mySolidificationMeltingSource, dictionary);
}
}
```

```

// * * * * * * * * * * * * * * * * * * * * * * * * * * * Private Member Functions * * * * *
* * * * * * * //

void Foam::fv::mySolidificationMeltingSource::update()
{
    if (curTimeIndex_ == mesh_.time().timeIndex())
    {
        return;
    }

    if (debug)
    {
        Info<< type() << ":" << "alpha.liquid" << "updating"
            phaseIndicator" << endl;
    }

    // update old time alpha1 field
    alphaC_.oldTime();
    const auto& CpVoF = mesh_.lookupObject<volScalarField>(
        CpName_);

    const auto& T = mesh_.lookupObject<volScalarField>(TName_);
    scalar Tsol = Tmelt_-0.25;
    scalar Tliq = Tmelt_+0.75;
    scalar eps = 0.0001;
    forAll(cells_, i)
    {
        label celli = cells_[i];

        scalar Tc = T[celli];
        scalar Cpc = CpVoF[celli];
        scalar alpha1New = alphaC_[celli] + relax_*Cpc*(Tc -
            Tmelt_)/L_;
        // scalar alpha1New = 0.5 + 0.5*std::erf(4 * ((Tc -
        // Tliq + Tsol)/2)/(Tliq - Tsol + eps)));
        alphaC_[celli] = max(0, min(alpha1New, 1));
    }

    alpha1_.correctBoundaryConditions();

    curTimeIndex_ = mesh_.time().timeIndex();
}

// * * * * * * * * * * * * * * * * * * * * Constructors * * * * * * * *
* * * * * * * //

Foam::fv::mySolidificationMeltingSource::
mySolidificationMeltingSource
(
    const word& sourceName,
    const word& modelType,
    const dictionary& dict,
    const fvMesh& mesh
)
:

```

```

    cellSetOption(sourceName, modelType, dict, mesh),
    Tmelt_(coeffs_.get<scalar>("Tmelt")),
    L_(coeffs_.get<scalar>("L")),
    relax_(coeffs_.getOrDefault<scalar>("relax", 0.9)),
    TName_(coeffs_.getOrDefault<word>("T", "T")),
    CpName_(coeffs_.getOrDefault<word>("Cp", "Cp")),
    UName_(coeffs_.getOrDefault<word>("U", "U")),
    rhoCpPhiName_(coeffs_.getOrDefault<word>("rhoCpPhi", "
        rhoCpPhi")),
    alphaC_
(
    IOobject
(
    "alphaPCM",
    mesh.time().timeName(),
    mesh,
    IOobject::READ_IF_PRESENT,
    IOobject::NO_WRITE
),
    mesh,
    dimensionedScalar(dimless, Zero),
    zeroGradientFvPatchScalarField::typeName
),
    alpha1_
(
    IOobject
(
    "alpha.liquid",
    mesh.time().timeName(),
    mesh,
    IOobject::READ_IF_PRESENT,
    IOobject::AUTO_WRITE
),
    mesh,
    dimensionedScalar(dimless, Zero),
    zeroGradientFvPatchScalarField::typeName
),
    curTimeIndex_(-1)
{
    fieldNames_.resize(2);
    fieldNames_[0] = UName_;
    fieldNames_[1] = TName_;

    fv::option::resetApplied();
}

// * * * * * * * * * * * * * * * * Member Functions * * * * *
* * * * * //

void Foam::fv::mySolidificationMeltingSource::addSup
(
    fvMatrix<scalar>& eqn,
    const label fieldi
)
{
    apply(geometricOneField(), eqn);
}

```

```

}

void Foam::fv::mySolidificationMeltingSource::addSup
(
    const volScalarField& rho,
    fvMatrix<scalar>& eqn,
    const label fieldi
)
{
    apply(rho, eqn);
}

bool Foam::fv::mySolidificationMeltingSource::read(const
    dictionary& dict)
{
    if (cellSetOption::read(dict))
    {
        coeffs_.readEntry("Tmelt", Tmelt_);
        coeffs_.readEntry("L", L_);

        coeffs_.readIfPresent("relax", relax_);
        coeffs_.readIfPresent("T", TName_);
        coeffs_.readIfPresent("U", UName_);
        coeffs_.readIfPresent("Cp", CpName_);
        coeffs_.readIfPresent("rhoCpPhi", rhoCpPhiName_);

        return true;
    }

    return false;
}

// ****
// ****

```

A.1.3 mySolidificationMeltingSourceTemplates.C

```

/*
----- *
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/*
-----*/

```

```

#include "fvMatrices.H"
#include "fvcDdt.H"
#include "fvcDiv.H"
#include "basicThermo.H"

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *

template<class RhoFieldType>
void Foam::fv::mySolidificationMeltingSource::apply
(
    const RhoFieldType& rho,
    fvMatrix<scalar>& eqn
)
{
    if (debug)
    {
        Info<< type() << ": applying source to " << eqn.psi().
            name() << endl;
    }

    update();
    const auto& CpVoF = mesh_.lookupObject<volScalarField>(
        CpName_);
    const auto& rhoCpPhiVoF = mesh_.lookupObject<
        surfaceScalarField>(rhoCpPhiName_);
    dimensionedScalar L("L", dimEnergy/dimMass, L_);

    // contributions added to rhs of solver equation
    if (eqn.psi().dimensions() == dimTemperature)
    {

```

```

        eqn -= (L*alpha1_)/CpVoF*(fvc::ddt(rho, alphaC_) + fvc::
            div(rhoCpPhiVoF, alphaC_));

    }
else
{
    //This option is not activated since fvOptions in TEqn
    //does not enable this condition
    eqn -= L*alpha1_*(fvc::ddt(rho, alphaC_));
}
}

// ****
// ****

```

A.2 Lee-Nucleation library

A.2.1 LeeCNT.H

```

/*
----- * |
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      Toolbox
===== / O peration | 
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----- - 

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```

```

Class
  Foam::meltingEvaporationModels::LeeCNT

Description
  Mass transfer LeeCNT model. Simple model driven by field
  value difference as:


$$\dot{m} = C \rho \alpha (T - T_{\text{activate}}) / T_{\text{activate}}$$


where  $C$  is a model constant.

if  $C > 0$ :

$$\dot{m} = C \rho \alpha (T - T_{\text{activate}}) / T_{\text{activate}}$$

for  $T > T_{\text{activate}}$ 

and


$$\dot{m} = 0.0 \quad \text{for } T < T_{\text{activate}}$$


if  $C < 0$ :

$$\dot{m} = -C \rho \alpha (T_{\text{activate}} - T) / T_{\text{activate}}$$

for  $T < T_{\text{activate}}$ 

and

Based on the reference:
-# W. H. LeeCNT. "A Pressure Iteration Scheme for Two-Phase
Modeling".
Technical Report LA-UR 79-975. Los Alamos Scientific
Laboratory,
Los Alamos, New Mexico. 1979.

Usage
Example usage:
\verbatim
massTransferModel
(
    (solid to liquid)
    {
        type          LeeCNT;
        C             40;
        Tactivate     302.78;
    }
);
\endverbatim

Where:

```

```


|                  |                                |                 |   |
|------------------|--------------------------------|-----------------|---|
| <i>Property</i>  | <i>Description</i>             | <i>Required</i> | / |
| Default value    |                                |                 |   |
| Tactivate        | Activation temperature         | yes             |   |
| C                | Model constant                 | yes             |   |
| includeVolChange | Volumen change                 | no              | / |
| species          | Specie name on the other phase | no              | / |
| none             |                                |                 |   |


SourceFiles
LeeCNT.C

/*
-----*/
#ifndef meltingEvaporationModels_LeeCNT_H
#define meltingEvaporationModels_LeeCNT_H

#include "InterfaceCompositionModel.H"

// * * * * *
// */

namespace Foam
{
namespace meltingEvaporationModels
{

/*
-----*
Class LeeCNT Declaration
*/
/*
-----*/
template<class Thermo, class OtherThermo>
class LeeCNT
:
public InterfaceCompositionModel<Thermo, OtherThermo>
{
// Private Data

//- Condensation coefficient [1/s]
dimensionedScalar C_;

volScalarField interfaceVolume_;
//- Phase transition temperature
const dimensionedScalar Tactivate_;

//- Phase minimum value for activation
scalar alphaMin_;

//- Planck constant [J.s]
const dimensionedScalar planck_;

//- Boltzmann constant [J/K]

```

```

    const dimensionedScalar boltzmann_ ;

    //- Activation energy of water molecules passing through
    water-ice interface [J]
    const dimensionedScalar deltag_ ;

    //- Number of water molecule in a water volume [m3]
    const dimensionedScalar NL_ ;

    //- Superficial free energy of the water-ice interface [
    J/m2]
    const dimensionedScalar gammaYW_ ;

    //- Latent heat per volume [J/m3]
    const dimensionedScalar hLV_ ;

    //- Shape coefficient of nucleation
    const dimensionedScalar alphaEY_ ;

public:

    //- Runtime type information
    TypeName("LeeCNT") ;

// Constructors

    //- Construct from components
    LeeCNT
    (
        const dictionary& dict,
        const phasePair& pair
    ) ;

    //- Destructor
    virtual ~LeeCNT() = default;

// Member Functions

    //- Explicit total mass transfer coefficient
    virtual tmp<volScalarField> Kexp
    (
        const volScalarField& field
    ) ;

    //- Implicit mass transfer coefficient
    virtual tmp<volScalarField> KSp
    (
        label modelVariable,
        const volScalarField& field
    ) ;

    //- Explicit mass transfer coefficient
    virtual tmp<volScalarField> KSu

```

```

(
    label modelVariable,
    const volScalarField& field
);

// - Return T transition between phases
virtual const dimensionedScalar& Tactivate() const;

// - Add/subtract alpha*div(U) as a source term
// - for alpha, substituting div(U) = mDot(1/rho1 - 1/
// rho2)
virtual bool includeDivU();

virtual const dimensionedScalar& planck() const;

virtual const dimensionedScalar& boltzmann() const;

virtual const dimensionedScalar& deltag() const;

virtual const dimensionedScalar& nL() const;

virtual const dimensionedScalar& gammaYW() const;

virtual const dimensionedScalar& hLV() const;

virtual const dimensionedScalar& alphaEY() const;

};

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
* * * * * * // 

} // End namespace meltingEvaporationModels
} // End namespace Foam

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
* * * * * * // 

#ifndef NoRepository
#   include "LeeCNT.C"
#endif

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
* * * * * * // 

#endif

// ****
***** * //

```

A.2.2 LeeCNT.C

```

/*
----- -* \
===== / 

```

```

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  Toolbox
\\      / Operation      |
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/*
----- */

#include "LeeCNT.H"
#include "addToRunTimeSelectionTable.H"
#include "mathematicalConstants.H"

// * * * * * Constructors * * * * *
// * * * * *

template<class Thermo, class OtherThermo>
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>::
LeeCNT
(
    const dictionary& dict,
    const phasePair& pair
)
:
    InterfaceCompositionModel<Thermo, OtherThermo>(dict, pair),
    C_("C", inv(dimTime), dict),
    Tactivate_("Tactivate", dimTemperature, dict),
    planck_("planck", dimEnergy*dimTime, dict),

```

```

boltzmann_("boltzmann", dimEnergy/dimTemperature, dict),
deltag_("deltag", dimEnergy, dict),
nL_("nL", inv(dimVolume), dict),
gammaYW_("gammaYW", dimEnergy/dimArea, dict),
hLV_("hLV", dimEnergy/dimVolume, dict),
alphaEY_("alphaEY", dict),
alphaMin_(dict.getOrDefault<scalar>("alphaMin", 0)),
interfaceVolume_
(
    IOobject
    (
        "cellVolume",
        this->mesh_.time().timeName(),
        this->mesh_,
        IOobject::NO_READ,
        IOobject::NO_WRITE
    ),
    this->mesh_,
    dimensionedScalar(dimVolume, Zero)
)
{}

// * * * * * * * * * * * * * * * * Member Functions * * * * * * * *
* * * * * * //


template<class Thermo, class OtherThermo>
Foam::tmp<Foam::volScalarField>
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>::
    Kexp
(
    const volScalarField& refValue
)
{
    {
        const fvMesh& mesh = this->mesh_;
        const volScalarField deltaG
        (
            (16.0 * (constant::mathematical::pi) * pow(gammaYW_,
                3.0) * pow(Tactivate_, 2.0) * alphaEY_)/(3.0 *
                pow(hLV_, 2.0) * pow((Tactivate_ - refValue), 2.0)
            )
        );
        const volScalarField J
        (
            (boltzmann_*refValue)/(planck_) * (exp(-deltag_/
                boltzmann_*refValue)) * nL_ * exp(-deltaG/(
                boltzmann_*refValue)))
        );
        forAll(interfaceVolume_, celli)
        {
            interfaceVolume_[celli] = mesh.V()[celli];
        }
    }
}

```

```

    const volScalarField lambda
    (
        J*interfaceVolume_
    );

    const volScalarField from
    (
        min(max(this->pair().from(), scalar(0)), scalar(1))
    );

    const volScalarField coeff
    (
        C_*from*this->pair().from().rho()*pos(from -
            alphaMin_)
        *(refValue - Tactivate_)
        /Tactivate_
    );

    const volScalarField coeff1
    (
        -lambda*from*this->pair().from().rho()*pos(from -
            alphaMin_)
        *(refValue - Tactivate_)
        /Tactivate_
    );

    if (sign(C_.value()) > 0)
    {
        return
        (
            coeff*pos(refValue - Tactivate_)
        );
    }
    else
    {
        return
        (
            coeff1*pos(Tactivate_ - refValue)
        );
    }
}

template<class Thermo, class OtherThermo>
Foam::tmp<Foam::volScalarField>
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>::KSp
(
    label variable,
    const volScalarField& refValue
)
{
    if (this->modelVariable_ == variable)
    {
        const fvMesh& mesh = this->mesh_;

```

```

const volScalarField deltaG
(
    (16.0 * (constant::mathematical::pi) * pow(gammaYW_
        ,3.0) * pow(Tactivate_ ,2.0) * alphaEY_)
    /(3.0 * pow(hLV_ ,2.0) * pow((Tactivate_ - refValue)
        ,2.0))
);

const volScalarField J
(
    (boltzmann_*refValue)/(planck_) * (exp(-deltag_/( 
        boltzmann_*refValue)) * nL_ * exp(-deltaG/( 
        boltzmann_*refValue)))
);

forAll(interfaceVolume_ , celli)
{
    interfaceVolume_[celli] = mesh.V()[celli];
}
const volScalarField lambda
(
    J*interfaceVolume_
);

volScalarField from
(
    min(max(this->pair().from() , scalar(0)), scalar(1))
);

const volScalarField coeff
(
    C_*from*this->pair().from().rho()*pos(from -
        alphaMin_)
    /Tactivate_
);

const volScalarField coeff1
(
    -lambda*from*this->pair().from().rho()*pos(from -
        alphaMin_)
    /Tactivate_
);

if (sign(C_.value()) > 0)
{
    return
    (
        coeff*pos(refValue - Tactivate_)
    );
}
else
{
    return
    (
        coeff1*pos(Tactivate_ - refValue)
    );
}

```

```

        }
    }
    else
    {
        return tmp<volScalarField> ();
    }
}

template<class Thermo, class OtherThermo>
Foam::tmp<Foam::volScalarField>
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>::KSu
(
    label variable,
    const volScalarField& refValue
)
{
    if (this->modelVariable_ == variable)
    {
        const fvMesh& mesh = this->mesh_;

        const volScalarField deltaG
        (
            (16.0 * (constant::mathematical::pi) * pow(gammaYW_
                ,3.0) * pow(Tactivate_,2.0) * alphaEY_)
            /(3.0 * pow(hLV_,2.0) * pow((Tactivate_ - refValue)
                ,2.0))
        );

        const volScalarField J
        (
            (boltzmann_*refValue)/(planck_) * (exp(-deltag_/
                boltzmann_*refValue)) * nL_ * exp(-deltaG/(
                    boltzmann_*refValue)))
        );

        forAll(interfaceVolume_, celli)
        {
            interfaceVolume_[celli] = mesh.V()[celli];
        }
        const volScalarField lambda
        (
            J*interfaceVolume_
        );

        volScalarField from
        (
            min(max(this->pair().from(), scalar(0)), scalar(1))
        );

        const volScalarField coeff
        (
            C_*from*this->pair().from().rho()*pos(from -
                alphaMin_)
        );
    }
}

```

```

        const volScalarField coeff1
    (
        -lambda*from*this->pair().from().rho()*pos(from -
            alphaMin_)
    );

    if (sign(C_.value()) > 0)
    {
        return
        (
            -coeff*pos(refValue - Tactivate_)
        );
    }
    else
    {
        return
        (
            -coeff1*pos(Tactivate_ - refValue)
        );
    }
}
else
{
    return tmp<volScalarField> ();
}

template<class Thermo, class OtherThermo>
const Foam::dimensionedScalar&
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>:::
Tactivate() const
{
    return Tactivate_;
}

template<class Thermo, class OtherThermo>
const Foam::dimensionedScalar&
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>:::
planck() const
{
    return planck_;
}

template<class Thermo, class OtherThermo>
const Foam::dimensionedScalar&
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>:::
boltzmann() const
{
    return boltzmann_;
}

template<class Thermo, class OtherThermo>
const Foam::dimensionedScalar&
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>:::
deltag() const
{

```

```

        return deltag_;
    }

template<class Thermo, class OtherThermo>
const Foam::dimensionedScalar&
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>::nL
    () const
{
    return nL_;
}

template<class Thermo, class OtherThermo>
const Foam::dimensionedScalar&
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>::gammaYW() const
{
    return gammaYW_;
}

template<class Thermo, class OtherThermo>
const Foam::dimensionedScalar&
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>::hLV
    () const
{
    return hLV_;
}

template<class Thermo, class OtherThermo>
const Foam::dimensionedScalar&
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>::alphaEY() const
{
    return alphaEY_;
}

template<class Thermo, class OtherThermo>
bool
Foam::meltingEvaporationModels::LeeCNT<Thermo, OtherThermo>::includeDivU()
{
    return true;
}

// ****
// ****

```

A.2.3 Library header files

```

/*
-----*|
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\ \ / O peration |
\ \ / A nd |
\ \ / M anipulation |

```

```
-----  
-----  
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-----  
-----  
/*-----  
-----*/  
  
#include "addToRunTimeSelectionTable.H"  
  
// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *  
* * * * * * //  
  
#include "interfaceCompositionModel.H"  
#include "InterfaceCompositionModel.H"  
//#include "thermoPhysicsTypes.H"  
#include "myThermoPhysicsTypes.H"  
  
#include "bPolynomial.H"  
  
#include "pureMixture.H"  
  
#include "rhoThermo.H"  
  
#include "heRhoThermo.H"  
  
#include "solidThermo.H"  
#include "heSolidThermo.H"  
#include "solidThermoPhysicsTypes.H"  
  
#include "Lee.H"  
#include "LeeCNT.H"
```

```

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
* * * * * * * //



#define makeInterfacePureType(Type, Thermo, Comp, Mix, Phys,
    OtherThermo, OtherComp, OtherMix, OtherPhys) \
\\

    typedef Thermo<Comp, Mix<Phys>>
    \
    Type##Thermo##Comp##Mix##Phys;
    \
    \
\\

    typedef OtherThermo<OtherComp, OtherMix<OtherPhys>>
    \
    Type##Other##OtherThermo##OtherComp##OtherMix##OtherPhys
    ;
    \
    \
\\

    addInterfaceCompositionToRunTimeSelectionTable
    \
(
    \
    \
    \
    Type,
    \
    \
    \
    Type##Thermo##Comp##Mix##Phys,
    \
    Type##Other##OtherThermo##OtherComp##OtherMix##OtherPhys
    \
)
\\

// Addition to the run-time selection table
#define addInterfaceCompositionToRunTimeSelectionTable(Type,
    Thermo, OtherThermo) \
\\

    typedef Type<Thermo, OtherThermo>
    \
    Type##Thermo##OtherThermo;
    \
    \
\\

    defineTemplateNameAndDebugWithName
    \
(
    \
    \
    Type##Thermo##OtherThermo,
    \
    \
    \
    word(Type##Thermo##OtherThermo::typeName_()) + "<" \
)
\\

```

```

+ word(Thermo::typeName) + ", "
+
+ word(OtherThermo::typeName) + ">"
    \\
).c_str(),
\\
0
\\
);

\\

addToRunTimeSelectionTable
(
\\
interfaceCompositionModel,
\\
Type##Thermo##OtherThermo,
\\
dictionary
\\
)

// * * * * *
* * * * */
namespace Foam
{
    using namespace meltingEvaporationModels;

    //NOTE: First thermo (from) and second otherThermo (to)

    // Lee model definitions

    // From pure phase (poly) to phase (solidThermo)
makeInterfacePureType
(
    Lee,
    heRhoThermo,
    rhoThermo,
    pureMixture,
    constbPolFluidHThermoPhysics,
    heSolidThermo,
    solidThermo,
    pureMixture,
    hConstSolidThermoPhysics
);
makeInterfacePureType
(
    LeeCNT,

```

```

        heRhoThermo ,
        rhoThermo ,
        pureMixture ,
        constbPolFluidHThermoPhysics ,
        heSolidThermo ,
        solidThermo ,
        pureMixture ,
        hConstSolidThermoPhysics
    ) ;

    makeInterfacePureType
    (
        Lee ,
        heRhoThermo ,
        rhoThermo ,
        pureMixture ,
        polybPolFluidHThermoPhysics ,
        heSolidThermo ,
        solidThermo ,
        pureMixture ,
        hConstSolidThermoPhysics
    ) ;

    makeInterfacePureType
    (
        LeeCNT ,
        heRhoThermo ,
        rhoThermo ,
        pureMixture ,
        polybPolFluidHThermoPhysics ,
        heSolidThermo ,
        solidThermo ,
        pureMixture ,
        hConstSolidThermoPhysics
    ) ;
    // interfaceHeatResistance model definitions

    // From pure phase (poly) to phase (solidThermo)
    // makeInterfacePureType
    // (
    //     interfaceHeatResistance ,
    //     heRhoThermo ,
    //     rhoThermo ,
    //     pureMixture ,
    //     constbPolFluidHThermoPhysics ,
    //     heSolidThermo ,
    //     solidThermo ,
    //     pureMixture ,
    //     hConstSolidThermoPhysics
    // );
}

// ****
// ****

```

```

/*
----- * |
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*/
----- */



#include "rhoThermo.H"
#include "makeThermo.H"

#include "specie.H"
#include "bPolynomial.H"

#include "hConstThermo.H"
#include "sensibleEnthalpy.H"
#include "thermo.H"

#include "constTransport.H"
#include "polynomialTransport.H"
#include "heRhoThermo.H"
#include "pureMixture.H"

```

```

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
// * * * * * * * //

namespace Foam
{

/* * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
 * * * * * * * * */

makeThermos
(
    rhoThermo,
    heRhoThermo,
    pureMixture,
    constTransport,
    sensibleEnthalpy,
    hConstThermo,
    bPolynomial,
    specie
);
makeThermos
(
    rhoThermo,
    heRhoThermo,
    pureMixture,
    polynomialTransport,
    sensibleEnthalpy,
    hConstThermo,
    bPolynomial,
    specie
);
// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
// * * * * * * * //

} // End namespace Foam

// *****
***** //



/*
-----* \
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/*
-----*/

```

```

#include "makeReactionThermo.H"

#include "rhoReactionThermo.H"
#include "heRhoThermo.H"

#include "specie.H"
// #include "perfectGas.H"
// #include "incompressiblePerfectGas.H"
#include "hConstThermo.H"
// #include "janafThermo.H"
#include "sensibleEnthalpy.H"
#include "thermo.H"
// #include "rhoConst.H"
// #include "rPolynomial.H"
// #include "perfectFluid.H"
// #include "adiabaticPerfectFluid.H"
// #include "Boussinesq.H"

#include "constTransport.H"
#include "polynomialTransport.H"
// #include "homogeneousMixture.H"
// #include "inhomogeneousMixture.H"
// #include "veryInhomogeneousMixture.H"
// #include "multiComponentMixture.H"
// #include "reactingMixture.H"
// #include "singleStepReactingMixture.H"
#include "singleComponentMixture.H"

#include "myThermoPhysicsTypes.H"

// * * * * *
* * * * */

```

```

namespace Foam
{
// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
// * * * * * * * //

makeReactionThermo
(
    rhoReactionThermo ,
    heRhoThermo ,
    singleComponentMixture ,
    constTransport ,
    sensibleEnthalpy ,
    hConstThermo ,
    bPolynomial ,
    specie
);

makeReactionThermo
(
    rhoReactionThermo ,
    heRhoThermo ,
    singleComponentMixture ,
    polynomialTransport ,
    sensibleEnthalpy ,
    hConstThermo ,
    bPolynomial ,
    specie
);

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
// * * * * * * * //

} // End namespace Foam

// ****
// ****

```

A.3 equationOfState

equationOfState

```

/*
-----*|
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```

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```
\*-----*/
#include "bPolynomial.H"
#include "IOstreams.H"

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
// * * * * * * */

namespace Foam
{

// * * * * * * * * * * * * Constructors * * * * * * * *
// * * * * * * */

template<class Specie, int PolySize>
bPolynomial<Specie, PolySize>::bPolynomial(const dictionary&
    dict)
:
    Specie(dict),
    rhoRef_(dict.subDict("equationOfState").get<scalar>("rhoRef")),
    Tref_(dict.subDict("equationOfState").get<scalar>("Tref")),
    rhoCoeffs_(dict.subDict("equationOfState").lookup(coeffsName
        ("rho")))
{};

// * * * * * * * * * * * * Member Functions * * * * * * *
// * * * * * * */


```


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Class
Foam::bPolynomial

Group
grpSpecieEquationOfState

Description
Incompressible, polynomial form of equation of state, using a polynomial function for density.

Usage
\table
Property / Description
rhoCoeffs<8> / Density polynomial coefficients
\endtable

Example of the specification of the equation of state:
\verbatim
equationOfState
{
rhoCoeffs<8> (1000 -0.05 0.003 0 0 0 0 0);
}
\endverbatim

The polynomial expression is evaluated as so:

```
\f[
    \rho = 1000 - 0.05 T + 0.003 T^2
\f]
```

Note
Input in [kg/m³], but internally uses [kg/m³/kmol].

SourceFiles
bPolynomialI.H
bPolynomial.C

See also
Foam::Polynomial

```
/*
----- */

#ifndef bPolynomial_H
#define bPolynomial_H

#include "autoPtr.H"
#include "Polynomial.H"

// * * * * *
// */

namespace Foam
{

// Forward Declarations

template<class Specie, int PolySize>
class bPolynomial;

template<class Specie, int PolySize>
bPolynomial<Specie, PolySize> operator+
(
    const bPolynomial<Specie, PolySize>&,
    const bPolynomial<Specie, PolySize>&
);

template<class Specie, int PolySize>
bPolynomial<Specie, PolySize> operator*
(
    const scalar,
    const bPolynomial<Specie, PolySize>&
);

template<class Specie, int PolySize>
bPolynomial<Specie, PolySize> operator==
(
    const bPolynomial<Specie, PolySize>&,
    const bPolynomial<Specie, PolySize>&
);

template<class Specie, int PolySize>
Ostream& operator<<
(
    Ostream&,
    const bPolynomial<Specie, PolySize>&
);

/*
----- */
                         Class bPolynomial Declaration
/*
----- */
----- */
```

template<class Specie, int PolySize=8>

```

class bPolynomial
:
    public Specie
{
    // Private Data

        // Reference density
        scalar rhoRef_;

        // Reference temperature
        scalar Tref_;

        // Density polynomial coefficients
        Polynomial<PolySize> rhoCoeffs_;

    // Private Member Functions

        // Coeffs name. Eg, "rhoCoeffs<10>"
        inline static word coeffsName(const char* name)
        {
            return word(name + ("Coeffs<" + std::to_string(
                PolySize) + '>'));
        }

public:

    // Generated Methods: copy construct, copy assignment

    // Constructors

        // Construct from components
        inline bPolynomial
        (
            const Specie& sp,
            const scalar rhoRef,
            const scalar Tref,
            const Polynomial<PolySize>& rhoPoly
        );

        // Construct from dictionary
        explicit bPolynomial(const dictionary& dict);

        // Construct as named copy
        inline bPolynomial(const word& name, const bPolynomial&)
        ;

        // Construct and return a clone
        inline autoPtr<bPolynomial> clone() const;

        // Selector from dictionary
        inline static autoPtr<bPolynomial> New(const dictionary&
            dict);

    // Member Functions

```

```

//- Return the instantiated type name
static word typeName()
{
    return "bPolynomial<" + word(Specie::typeName_()) +
           '>';
}

// Fundamental properties

//- Is the equation of state is incompressible i.e.
    rho != f(p)
static const bool incompressible = true;

//- Is the equation of state is isochoric i.e. rho =
    const
static const bool isochoric = false;

//- Return density [kg/m^3]
inline scalar rho(scalar p, scalar T) const;

//- Return enthalpy departure [J/kg]
inline scalar H(const scalar p, const scalar T)
    const;

//- Return Cp departure [J/(kg K)]
inline scalar Cp(scalar p, scalar T) const;

//- Return internal energy departure [J/kg]
inline scalar E(const scalar p, const scalar T)
    const;

//- Return Cv departure [J/(kg K)]
inline scalar Cv(scalar p, scalar T) const;

//- Return entropy [J/(kg K)]
inline scalar S(const scalar p, const scalar T)
    const;

//- Return compressibility rho/p [s^2/m^2]
inline scalar psi(scalar p, scalar T) const;

//- Return compression factor []
inline scalar Z(scalar p, scalar T) const;

//- Return (Cp - Cv) [J/(kg K)]
inline scalar CpMCv(scalar p, scalar T) const;

// IO

//- Write to Ostream
void write(Ostream& os) const;

// Member Operators

```

```

        inline void operator+=(const bPolynomial&);
        inline void operator*=(const scalar);

// Friend Operators

        friend bPolynomial operator+ <Specie, PolySize>
        (
            const bPolynomial&,
            const bPolynomial&
        );

        friend bPolynomial operator* <Specie, PolySize>
        (
            const scalar s,
            const bPolynomial&
        );

        friend bPolynomial operator== <Specie, PolySize>
        (
            const bPolynomial&,
            const bPolynomial&
        );

// Iostream Operators

        friend Ostream& operator<< <Specie, PolySize>
        (
            Ostream&,
            const bPolynomial&
        );
    };

/* * * * * */

} // End namespace Foam

/* * * * * */

#define makebPolynomial(PolySize)
    \
    defineTemplateNameAndDebugWithNamespace
    \
    \
    \
    \
    bPolynomial<Specie, PolySize>, \
    \
    "bPolynomial<"#PolySize">", \
    \

```



```

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licenses/>.

/*
-----*
----- */

#include "bPolynomial.H"

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
* * * * * * * //


template<class Specie, int PolySize>
inline Foam::bPolynomial<Specie, PolySize>::bPolynomial
(
    const Specie& sp,
    const scalar rhoRef,
    const scalar Tref,
    const Polynomial<PolySize>& rhoCoeffs
)
:
    Specie(sp),
    rhoRef_(rhoRef),
    Tref_(Tref),
    rhoCoeffs_(rhoCoeffs)
{}


// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
* * * * * * * //


template<class Specie, int PolySize>
inline Foam::bPolynomial<Specie, PolySize>::bPolynomial
(
    const word& name,
    const bPolynomial<Specie, PolySize>& ip
)
:
    Specie(name, ip),
    rhoRef_(ip.rhoRef_),
    Tref_(ip.Tref_),
    rhoCoeffs_(ip.rhoCoeffs_)
{}


template<class Specie, int PolySize>
inline Foam::autoPtr<Foam::bPolynomial<Specie, PolySize>>
Foam::bPolynomial<Specie, PolySize>::clone() const
{
    return autoPtr<bPolynomial<Specie, PolySize>>::New(*this);
}

template<class Specie, int PolySize>
inline Foam::autoPtr<Foam::bPolynomial<Specie, PolySize>>
Foam::bPolynomial<Specie, PolySize>::New(const dictionary& dict)

```

```
{  
    return autoPtr<bPolynomial<Specie, PolySize>>::New(dict);  
}  
  
// * * * * * * * * * * * * * * * * Member Functions * * * * *  
* * * * * //  
  
template<class Specie, int PolySize>  
inline Foam::scalar Foam::bPolynomial<Specie, PolySize>::rho  
(  
    scalar p,  
    scalar T  
) const  
{  
    return rhoCoeffs_.value(T-Tref_);  
}  
  
template<class Specie, int PolySize>  
inline Foam::scalar Foam::bPolynomial<Specie, PolySize>::H  
(  
    scalar p,  
    scalar T  
) const  
{  
    return 0;  
}  
  
template<class Specie, int PolySize>  
inline Foam::scalar Foam::bPolynomial<Specie, PolySize>::Cp  
(  
    scalar p,  
    scalar T  
) const  
{  
    return 0;  
}  
  
template<class Specie, int PolySize>  
inline Foam::scalar Foam::bPolynomial<Specie, PolySize>::E  
(  
    scalar p,  
    scalar T  
) const  
{  
    return 0;  
}  
  
template<class Specie, int PolySize>  
inline Foam::scalar Foam::bPolynomial<Specie, PolySize>::Cv  
(  
    scalar p,  
    scalar T
```

```

) const
{
    return 0;
}

template<class Specie, int PolySize>
inline Foam::scalar Foam::bPolynomial<Specie, PolySize>::S
(
    scalar p,
    scalar T
) const
{
    return 0;
}

template<class Specie, int PolySize>
inline Foam::scalar Foam::bPolynomial<Specie, PolySize>::psi
(
    scalar p,
    scalar T
) const
{
    return 0;
}

template<class Specie, int PolySize>
inline Foam::scalar Foam::bPolynomial<Specie, PolySize>::Z
(
    scalar p,
    scalar T
) const
{
    return 0;
}

template<class Specie, int PolySize>
inline Foam::scalar Foam::bPolynomial<Specie, PolySize>::CpMCv
(
    scalar p,
    scalar T
) const
{
    return 0;
}

// * * * * * * * * * * * * * * * * Member Operators * * * * *
* * * * * * // 

template<class Specie, int PolySize>
inline void Foam::bPolynomial<Specie, PolySize>::operator+=
(
    const bPolynomial<Specie, PolySize>& ip

```

```

)
{
    scalar Y1 = this->Y();
    Specie::operator+=(ip);

    if (mag(this->Y()) > SMALL)
    {
        Y1 /= this->Y();
        const scalar Y2 = ip.Y()/this->Y();
        rhoRef_ = Y1*rhoRef_ + Y2*ip.rhoRef_;
        Tref_ = Y1*Tref_ + Y2*ip.Tref_;
        rhoCoeffs_ = Y1*rhoCoeffs_ + Y2*ip.rhoCoeffs_;
    }
}

template<class Specie, int PolySize>
inline void Foam::bPolynomial<Specie, PolySize>::operator*=(const scalar s)
{
    Specie::operator*=(s);
}

// * * * * * * * * * * * * * * * * * * * Friend Operators * * * * *
// * * * * * * //

template<class Specie, int PolySize>
Foam::bPolynomial<Specie, PolySize> Foam::operator+(
(
    const bPolynomial<Specie, PolySize>& ip1,
    const bPolynomial<Specie, PolySize>& ip2
)
{
    Specie sp
    (
        static_cast<const Specie&>(ip1)
        + static_cast<const Specie&>(ip2)
    );

    if (mag(sp.Y()) < SMALL)
    {
        return bPolynomial<Specie, PolySize>
        (
            sp,
            ip1.rhoRef_,
            ip1.Tref_,
            ip1.rhoCoeffs_
        );
    }
    else
    {
        const scalar Y1 = ip1.Y()/sp.Y();
        const scalar Y2 = ip2.Y()/sp.Y();

        return bPolynomial<Specie, PolySize>
        (

```

```

        sp,
        Y1*ip1.rhoRef_ + Y2*ip2.rhoRef_,
        Y1*ip1.Tref_ + Y2*ip2.Tref_,
        Y1*ip1.rhoCoeffs_ + Y2*ip2.rhoCoeffs_
    );
}
}

template<class Specie, int PolySize>
Foam::bPolynomial<Specie, PolySize> Foam::operator*
(
    const scalar s,
    const bPolynomial<Specie, PolySize>& ip
)
{
    return bPolynomial<Specie, PolySize>
    (
        s*static_cast<const Specie&>(ip),
        ip.rhoRef_,
        ip.Tref_,
        ip.rhoCoeffs_
    );
}

template<class Specie, int PolySize>
Foam::bPolynomial<Specie, PolySize> Foam::operator==
(
    const bPolynomial<Specie, PolySize>& ip1,
    const bPolynomial<Specie, PolySize>& ip2
)
{
    Specie sp
    (
        static_cast<const Specie&>(ip1)
        ==
        static_cast<const Specie&>(ip2)
    );

    const scalar Y1 = ip1.Y()/sp.Y();
    const scalar Y2 = ip2.Y()/sp.Y();

    return bPolynomial<Specie, PolySize>
    (
        sp,
        Y2*ip2.rhoRef_ - Y1*ip1.rhoRef_,
        Y2*ip2.Tref_ - Y1*ip1.Tref_,
        Y2*ip2.rhoCoeffs_ - Y1*ip1.rhoCoeffs_
    );
}

// ****
// ****

```

A.4 Python code for Stefan Problem

```

1 import os
2 import re
3 from tkinter import Tk
4 from tkinter.filedialog import askdirectory
5 import csv
6 import matplotlib.pyplot as plt
7 import numpy as np
8 from glob import iglob
9 from cmath import pi, sqrt, exp
10
11 path = askdirectory(title='Select Folder')
12 for root, dirs, files in os.walk(path):
13     numL2 = []
14     denL2 = []
15     L2 = []
16     numL2_sol2 = []
17     denL2_sol2 = []
18     L2_sol2 = []
19     dir = []
20     n = 0
21     for i in files:
22         with os.scandir(root) as it:
23             alphaField = []
24             posField = []
25             t = []
26
27         j = 0
28         for entry in it:
29             if entry.name.endswith(".csv") and entry.is_file():
30
31                 t = np.append(t, int(re.search(r'\d+', entry.
name).group()))
32                 with open(entry.path, 'r') as f:
33                     fields = []
34                     alpha = []
35                     x = []
36                     csvreader = csv.reader(f)
37                     fields = next(csvreader)
38                     for row in csvreader:
39                         alpha = np.append(alpha, float(row[0]))
40                         x = np.append(x, float(row[1]))
41                     idx = (np.abs(alpha - 0.5)).argmin()
42                     alp = alpha[idx]
43                     loc = x[idx]
44                     # if alp == 1:
45                     #     loc = 0.0
46                     #     alp = 1
47
48                     posField = np.append(posField, loc)
49                     alphaField = np.append(alphaField, alp)
50
51                     j = j + 1
52                     m = t.argsort()
53                     alphaField = alphaField[m]
54                     posField = posField[m]
```

```

55      # Analytical Interface position
56      cps = 2050
57      k1 = 2.22
58      rho1 = 916.2
59      a1 = k1/(rho1*cps)
60      lambd = 0.00032622525325939834
61      lambd1 = 0.2299545377262345
62      psi = []
63      psi2 = []
64      t = np.sort(t)
65      for x in range(0,len(t)):
66          psi = np.append(psi, lambd*sqrt(t[x]))
67          psi2 = np.append(psi2, 2*lambd1*sqrt(a1*t[x]))
68
69      numL2 = []
70      denL2 = []
71      L2 = []
72      for k in range(0,len(t)):
73          numL2 = np.append(numL2, np.sum(np.power((posField[k]-
74          psi2[k]),2)))
75      L2 = numL2
76
77      f1 = plt.figure()
78      f2 = plt.figure()
79
80      ax1 = f1.add_subplot(111)
81      ax1.plot(t, psi2.real, 'r--', label='Neumann solution')
82      ax1.plot(t, posField, 'g--', label='Numerical solution')
83      ax1.set(xlabel='t [s]', ylabel= 'Interface position [m]')
84      ax1.grid(True)
85      ax1.legend()
86      L2 = L2.real
87      ax2 = f2.add_subplot(111)
88      ax2.plot(t, L2, 'r--', label='Relative error')
89      ax2.set(xlabel='t [s]', ylabel= 'Relative error')
90      ax2.grid(True)
91
92      ax2.legend()
93      plt.show()

```

```

1 from scipy import optimize
2 from scipy.special import erfc
3 from scipy.special import erf
4 from cmath import pi, sqrt, exp
5
6 # Roots of "An Accurate Approximation of the Two-Phase Stefan
7 # Problem with Coefficient Smoothing"
8 g = -20
9 u0 = 10
10 k1 = 2.26
11 k2 = 0.59
12 c1 = 4.182E6
13 c2 = 4.182E6
14 D = 3.35E8
15 a1 = sqrt(k1/c1)
16 a2 = sqrt(k2/c2)

```

```

17 def func(x):
18     return (((k1/a1) * g * exp(-(x/(2*a1))**2)) / erf(x/(2*a1))) +
19         ((k2/a2) * u0 * (exp(-(x/(2*a2))**2)) / (1.0-erf(x/(2*a2)))) +
20         ((x * D * sqrt(pi)) / 2))
21
22 sol = optimize.root_scalar(func, rtol=1E-12, method='secant', x0
23     =-0.1, x1=0.0005)
24 lambd = sol.root.real
25 print("An Accurate Approximation of the Two-Phase Stefan Problem
26       with Coefficient Smoothing: ", lambd)
27
28
29 tm = 0.15
30 t0 = 10
31 tb = -20
32 L = 335000
33 cps = 4182
34 k1 = 2.26
35 k2 = 0.59
36 rho1 = 916.8
37 rho2 = 999.8
38 a1 = k1/(rho1*cps)
39 a2 = k2/(rho2*cps)
40
41 def f(x):
42     return ((exp(-(x**2))/erf(x)) + (k2/k1) * sqrt(a1/a2) * ((tm-t0)
43         /(tm-tb)) * (exp(-(a1/a2)*(x**2))/erfc(x*sqrt(a1/a2))) - (x*L*
44         sqrt(pi))/(cps*(tm-tb)))
45
46 sol1 = optimize.root_scalar(f, rtol=1E-12, method='secant', x0=0.1,
47     x1=0.5)
48 lambd1 = sol1.root.real
49
50 import os
51 import re
52 from tkinter import Tk
53 from tkinter.filedialog import askdirectory
54 import csv
55 import matplotlib.pyplot as plt
56 import pandas as pd
57 import numpy as np
58 path = askdirectory(title='Select Folder')
59
60 for root, dirs, files in os.walk(path):
61     for i in files:
62         if i == 'mesh1_TX_950s.xlsx':
63             dfs1 = pd.read_excel(root+'/'+i)
64             T = []
65             x = []
66             idx1 = np.where(dfs1.columns == "T")[0][0]
67             T = dfs1.values[:,idx1]
68             T = T - 273.15
69             idx2 = np.where(dfs1.columns == "X")[0][0]
70             x = dfs1.values[:,idx2]
71
72             t = np.linspace(0,50,len(x))
73             g = -20

```

```

67      u0 = 10
68      k1 = 2.26
69      k2 = 0.59
70      c1 = 4.182E6
71      c2 = 4.182E6
72      D = 3.33E8
73      a1 = (sqrt(k1/c1))
74      a2 = (sqrt(k2/c2))
75      fxt = []
76      den = []
77      psi = []
78      fyvt = []

79
80      j = 0
81      for i in x:
82          psi = np.append(psi, lambd*sqrt(t[j]))
83          if i <= psi[j]:
84              den = np.append(den, 2*a1*sqrt(t[j]))
85              if (t[j]==0.0):
86                  fxt = g
87              else:
88                  fxt = np.append(fxt, (g * (erf(psi[j]/den[j])
89                  ])-erf(x[j]/den[j]))/(erf(psi[j]/den[j])))
90
91          else:
92              den = np.append(den, 2*a2*sqrt(t[j]))
93              if (t[j]==0.0):
94                  fxt = 0.0
95              else:
96                  fxt = np.append(fxt, (u0 * (erf(x[j]/den[j]
97                  ])-erf(psi[j]/den[j])))/(1-erf(psi[j]/den[j])))
98
99
100     tm = 0.15
101     t0 = 10
102     tb = -20
103     L = 335000
104     cps = 4182
105     k1 = 2.26
106     k2 = 0.59
107     rho1 = 916.8
108     rho2 = 999.8
109     a1 = k1/(rho1*cps)
110     a2 = k2/(rho2*cps)

111
112     j = 0
113     for i in x:
114         psi = np.append(psi, 2*lambd1*sqrt(a1*x[j]))
115         if i <= psi[j]:
116             if (t[j]==0.0):
117                 fyvt = tb
118             else:
119                 fyvt = np.append(fyvt, (erf(x[j]/(2*sqrt(a1*t
120                 [j])))/erf(lambd1)) * (tm-tb) + tb)
121             else:

```

```

121             if (t[j]==0.0):
122                 fyt = 0.0
123             else:
124                 fyt = np.append(fyt, (erfc(x[j]/(2*sqrt(a2*t[j])))/erfc(lambd1*sqrt(a1/a2))) * (tm-t0) + t0)
125
126             j = j + 1
127
128         else:
129             continue
130
131     num_solution = T
132     ana_solution1 = fxt
133     ana_solution2 = fyt
134     numL2 = []
135     denL2 = []
136     L2 = []
137     for k in range(0,len(T)):
138         numL2 = np.append(numL2, abs(num_solution[k]-
139             ana_solution2[k])/ana_solution2[k])
140
141 dydx = np.gradient(fyt.real, x)
142 dydxT = np.gradient(T,x)
143
144 f1 = plt.figure()
145 f2 = plt.figure()
146 f3 = plt.figure()
147
148 ax1 = f1.add_subplot(111)
149 ax1.plot(x, fyt.real, 'r--', label='Neumann solution')
150 ax1.plot(x, T, 'g--', label='Numerical solution')
151 ax1.set(xlabel='x [m]', ylabel= 'T [C]')
152 ax1.grid(True)
153 ax1.legend()
154 L2 = L2.real/len(T)
155 ax2 = f2.add_subplot(111)
156 ax2.plot(x[1:], L2[1:], 'r--', label='Relative error')
157 ax2.set(xlabel='x [m]', ylabel= 'Relative error')
158 ax2.grid(True)
159 ax2.legend()
160
161 ax3 = f3.add_subplot(111)
162 ax3.plot(x,dydx, 'r--', label='Neumann solution')
163 ax3.plot(x,dydxT, 'g--', label='Numerical solution')
164 ax3.set(xlabel='x [m]', ylabel= 'dy/dx')
165 ax3.grid(True)
166 ax3.legend()
167
168 plt.show()

```


Appendix B

Appendix B: Solver implementations

B.1 Computational Mesh script

```

1 from ofblockmeshdicthelper import BlockMeshDict, Vertex, Point,
2   SimpleGrading
3 import numpy as np
4 import os
5
6 from tkinter import Tk
7 from tkinter.filedialog import askdirectory
8 path = askdirectory(title='Select Folder')
9
10 bmd = BlockMeshDict()
11 r = 41.4
12 Hp = 1
13 Nx_pipe = 300
14 Ny_pipe = 300
15 Nz_pipe = 1
16 r2 = r + 10
17 rati = r/r2
18
19 bmd.add_vertex(-r/2,-r/2,-Hp, 'v0')
20 bmd.add_vertex(0,-r/2,-Hp, 'v1')
21 bmd.add_vertex(0,r/2,-Hp, 'v2')
22 bmd.add_vertex(-r/2,r/2,-Hp, 'v3')
23 bmd.add_vertex(-r/2,-r/2,0, 'v4')
24 bmd.add_vertex(0,-r/2,0, 'v5')
25 bmd.add_vertex(0,r/2,0, 'v6')
26 bmd.add_vertex(-r/2,r/2,0, 'v7')
27 bmd.add_vertex(-r*np.sin(np.pi/4),-r*np.cos(np.pi/4),-Hp, 'v8')
28 bmd.add_vertex(0,-r,-Hp, 'v9')
29 bmd.add_vertex(-r*np.sin(np.pi/4),r*np.cos(np.pi/4),-Hp, 'v10')
30 bmd.add_vertex(0,r,-Hp, 'v11')
31 bmd.add_vertex(-r*np.sin(np.pi/4),-r*np.cos(np.pi/4),0, 'v12')
32 bmd.add_vertex(0,-r,0, 'v13')
33 bmd.add_vertex(-r*np.sin(np.pi/4),r*np.cos(np.pi/4),0, 'v14')
34 bmd.add_vertex(0,r,0, 'v15')
35
36
37

```

```

38 bmd.add_vertex(-r2*np.sin(np.pi/4), -r2*np.cos(np.pi/4), -Hp, 'v16')
39 bmd.add_vertex(0, -r2, -Hp, 'v17')
40 bmd.add_vertex(-r2*np.sin(np.pi/4), r2*np.cos(np.pi/4), -Hp, 'v18')
41 bmd.add_vertex(0, r2, -Hp, 'v19')
42 bmd.add_vertex(-r2*np.sin(np.pi/4), -r2*np.cos(np.pi/4), 0, 'v20')
43 bmd.add_vertex(0, -r2, 0, 'v21')
44 bmd.add_vertex(-r2*np.sin(np.pi/4), r2*np.cos(np.pi/4), 0, 'v22')
45 bmd.add_vertex(0, r2, 0, 'v23')
46 bmd.add_arcedge(( 'v8' , 'v9' ), 'arc1' , Vertex(-r*np.sin(np.pi/8), -r*np.cos(np.pi/8), -Hp, 'v_arc1'))
47 bmd.add_arcedge(( 'v12' , 'v13' ), 'arc2' , Vertex(-r*np.sin(np.pi/8), -r*np.cos(np.pi/8), 0, 'v_arc2'))
48 bmd.add_arcedge(( 'v8' , 'v10' ), 'arc3' , Vertex(-r, 0, -Hp, 'v_arc3'))
49 bmd.add_arcedge(( 'v12' , 'v14' ), 'arc4' , Vertex(-r, 0, 0, 'v_arc4'))
50 bmd.add_arcedge(( 'v10' , 'v11' ), 'arc5' , Vertex(-r*np.sin(np.pi/8), r*np.cos(np.pi/8), -Hp, 'v_arc5'))
51 bmd.add_arcedge(( 'v14' , 'v15' ), 'arc6' , Vertex(-r*np.sin(np.pi/8), r*np.cos(np.pi/8), 0, 'v_arc6'))
52 bmd.add_arcedge(( 'v16' , 'v17' ), 'arc7' , Vertex(-r2*np.sin(np.pi/8), -r2*np.cos(np.pi/8), -Hp, 'v_arc7'))
53 bmd.add_arcedge(( 'v20' , 'v21' ), 'arc8' , Vertex(-r2*np.sin(np.pi/8), -r2*np.cos(np.pi/8), 0, 'v_arc8'))
54 bmd.add_arcedge(( 'v16' , 'v18' ), 'arc9' , Vertex(-r2, 0, -Hp, 'v_arc9'))
55 bmd.add_arcedge(( 'v20' , 'v22' ), 'arc10' , Vertex(-r2, 0, 0, 'v_arc10'))
56 bmd.add_arcedge(( 'v18' , 'v19' ), 'arc11' , Vertex(-r2*np.sin(np.pi/8), r2*np.cos(np.pi/8), -Hp, 'v_arc11'))
57 bmd.add_arcedge(( 'v22' , 'v23' ), 'arc12' , Vertex(-r2*np.sin(np.pi/8), r2*np.cos(np.pi/8), 0, 'v_arc12'))
58
59
60 prism_pipe = bmd.add_hexblock(( 'v0' , 'v1' , 'v2' , 'v3' , 'v4' , 'v5' , 'v6' , 'v7' ), (int(Nx_pipe/2), int(Ny_pipe/2), Nz_pipe), 'prims_pipe', grading=SimpleGrading(1,1,1))
61 south_pipe = bmd.add_hexblock(( 'v8' , 'v9' , 'v1' , 'v0' , 'v12' , 'v13' , 'v5' , 'v4' ), (int(Nx_pipe/2), int(Ny_pipe/4), Nz_pipe), 'south_pipe', grading=SimpleGrading(1,1,1))
62 east_pipe = bmd.add_hexblock(( 'v8' , 'v0' , 'v3' , 'v10' , 'v12' , 'v4' , 'v7' , 'v14' ), (int(Ny_pipe/4), int(Ny_pipe/2), Nz_pipe), 'east_pipe', grading=SimpleGrading(1,1,1))
63 north_pipe = bmd.add_hexblock(( 'v3' , 'v2' , 'v11' , 'v10' , 'v7' , 'v6' , 'v15' , 'v14' ), (int(Nx_pipe/2), int(Ny_pipe/4), Nz_pipe), 'north_pipe', grading=SimpleGrading(1,1,1))
64
65 #Region #2
66 south_pipe_region2 = bmd.add_hexblock(( 'v16' , 'v17' , 'v9' , 'v8' , 'v20' , 'v21' , 'v13' , 'v12' ), (int(Nx_pipe/2), int(Ny_pipe/4), Nz_pipe), 'south_pipe_region2', grading=SimpleGrading(1,1,1))
67 east_pipe_region2 = bmd.add_hexblock(( 'v16' , 'v8' , 'v10' , 'v18' , 'v20' , 'v12' , 'v14' , 'v22' ), (int(Ny_pipe/4), int(Ny_pipe/2), Nz_pipe), 'east_pipe_region2', grading=SimpleGrading(1,1,1))
68 north_pipe_region2 = bmd.add_hexblock(( 'v10' , 'v11' , 'v19' , 'v18' , 'v14' , 'v15' , 'v23' , 'v22' ), (int(Nx_pipe/2), int(Ny_pipe/4), Nz_pipe), 'north_pipe_region2', grading=SimpleGrading(1,1,1))
69
70
71
72
73
74
75
76

```

```

77 bmd.add_boundary('wall','solidWall',[south_pipe_region2.face('s'),
    east_pipe_region2.face('w'),north_pipe_region2.face('n')])
78 bmd.add_boundary('empty','fluidFrontAndBack',[prism_pipe.face('b'),
    south_pipe.face('b'),east_pipe.face('b'),north_pipe.face('b'),
    prism_pipe.face('t'),south_pipe.face('t'),east_pipe.face('t'),
    north_pipe.face('t')])
79 bmd.add_boundary('empty','solidFrontAndBack',[south_pipe_region2.
    face('b'),east_pipe_region2.face('b'),north_pipe_region2.face('b'),
    south_pipe_region2.face('t'),east_pipe_region2.face('t'),
    north_pipe_region2.face('t')])
80 bmd.add_boundary('symmetryPlane','fluidSymmetryBC',[prism_pipe.face
    ('e'),south_pipe.face('e'),north_pipe.face('e')])
81 bmd.add_boundary('symmetryPlane','solidSymmetryBC',[

    south_pipe_region2.face('e'),north_pipe_region2.face('e')])
82
83
84 bmd.set_metric('mm')
85 bmd.assign_vertexid()
86 print(bmd.format())
87
88 print(bmd.format())
89
90 filetxt = bmd.format()
91 nameOfFile = 'blockMeshDict'
92 completeName = os.path.join(path, nameOfFile)
93 with open(completeName,'w') as f:
94     f.writelines(filetxt)
95
96 f.close()

```

B.2 *chtMultiphaseInterFoam* solver

```

/*
----- * \
=====
\\      / F ield           / OpenFOAM: The Open Source CFD
      Toolbox
\\      / O peration        /
\\  / A nd                / www.openfoam.com
\\/  M anipulation        /
----- -
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```

```

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Application
    chtMultiPhaseInterFoam

Group
    grpHeatTransferSolvers

/*-----*
-----*/

#include "fvCFD.H"
#include "subCycle.H"
#include "multiphaseSystem.H"
#include "turbulentFluidThermoModel.H"
#include "pimpleControl.H"
#include "CombustionModel.H"
#include "fixedGradientFvPatchFields.H"
#include "regionProperties.H"
#include "alphaCourantNo.H"
#include "ddtAlphaNo.H"
#include "compressibleCourantNo.H"
#include "solidRegionDiffNo.H"
#include "solidThermo.H"
#include "radiationModel.H"
#include "fvOptions.H"
#include "coordinateSystem.H"
#include "loopControl.H"
#include "pressureControl.H"
#include "CorrectPhi.H"

// * * * * *
* * * * */

int main(int argc, char *argv[])
{
    argList::addNote
    (
        "Transient solver for buoyant, turbulent fluid flow and
         solid heat
        " conduction with conjugate heat transfer
        " between solid and fluid regions."
    );
}

```

```

#define NO_CONTROL
#define CREATE_MESH createMeshesPostProcess.H
#include "postProcess.H"
#include "setRootCaseLists.H"
#include "createTime.H"
#include "createMeshes.H"
#include "createFields.H"
#include "createFieldRefs.H"
#include "initContinuityErrs.H"
#include "createTimeControls.H"
#include "readFluidTimeControls.H"
#include "readSolidTimeControls.H"
#include "ddtAlphaMultiRegionNo.H"
#include "compressibleMultiRegionCourantNo.H"
#include "solidRegionDiffusionNo.H"
#include "setInitialMultiRegionDeltaT.H"
#include "validateTurbulenceModel.H"

Info<< "\nStarting time loop\n" << endl;

while (runTime.run())
{
    #include "readTimeControls.H"
    #include "readFluidTimeControls.H"
    #include "readSolidTimeControls.H"
    #include "readPIMPLEControls.H"

    #include "alphaCourantMultiRegionNo.H"
    #include "ddtAlphaMultiRegionNo.H"
    #include "compressibleMultiRegionCourantNo.H"
    #include "solidRegionDiffusionNo.H"
    #include "setMultiRegionDeltaT.H"

    ++runTime;

    Info<< "Time = " << runTime.timeName() << nl << endl;

    // --- PIMPLE loop
    for (int oCorr=0; oCorr<nOuterCorr; ++oCorr)
    {
        const bool firstIter = (oCorr == 0);
        const bool finalIter = (oCorr == nOuterCorr-1);

        forAll(fluidRegions, i)
        {
            Info<< "\nSolving for fluid region "
                << fluidRegions[i].name() << endl;
            #include "setRegionFluidFields.H"
            #include "readFluidMultiRegionPIMPLEControls.H"
            #include "solveFluid.H"
        }

        forAll(solidRegions, i)
        {
            Info<< "\nSolving for solid region "
                << solidRegions[i].name() << endl;
        }
    }
}

```

```

        #include "setRegionSolidFields.H"
        #include "readSolidMultiRegionPIMPLEControls.H"
        #include "solveSolid.H"
    }

        // Additional loops for energy solution
        only
    if (!oCorr && nOuterCorr > 1)
    {
        loopControl looping(runTime, pimpleCHT, "
            energyCoupling");

        while (looping.loop())
        {
            Info<< nl << looping << nl;

            forAll(fluidRegions, i)
            {
                Info<< "\nSolving for fluid region"
                    << fluidRegions[i].name() << endl;
                #include "setRegionFluidFields.H"
                #include "
                    readFluidMultiRegionPIMPLEControls.H"
                frozenFlow = true;
                #include "solveFluid.H"
            }

            forAll(solidRegions, i)
            {
                Info<< "\nSolving for solid region"
                    << solidRegions[i].name() << endl;
                #include "setRegionSolidFields.H"
                #include "
                    readSolidMultiRegionPIMPLEControls.H"
                    "
                #include "solveSolid.H"
            }
        }
    }

    runTime.write();

    runTime.printExecutionTime(Info);
}

Info<< "End\n" << endl;

return 0;
}

// ****
***** //

```

createFields

```
#include "createFluidFields.H"
#include "createSolidFields.H"
```

createMeshes

```
regionProperties rp(runTime);

#include "createFluidMeshes.H"
#include "createSolidMeshes.H"
```

createMeshesPostProcess

```
#include "createMeshes.H"

if (!fluidRegions.size() && !solidRegions.size())
{
    FatalErrorIn(args.executable())
        << "No_region_meshes_present" << exit(FatalError);
}

fvMesh& mesh = fluidRegions.size() ? fluidRegions[0] :
solidRegions[0];
```

readPIMPLEControls

```
// We do not have a top-level mesh. Construct the fvSolution
// for
// the runTime instead.
fvSolution solutionDict(runTime);

const dictionary& pimpleCHT = solutionDict.subDict("PIMPLE")
;

const int nOuterCorr =
    pimpleCHT.getOrDefault<int>("nOuterCorrectors", 1);
```

B.2.1 Fluid region**createFluidMeshes**

```
const wordList fluidNames(rp["fluid"]);

PtrList<fvMesh> fluidRegions(fluidNames.size());
// PtrList<dynamicFvMesh> fluidRegions(fluidNames.size());
forAll(fluidNames, i)
{
    Info<< "Create fluid mesh for region " << fluidNames[i]
        << " for time = " << runTime.timeName() << nl <<
        endl;

    fluidRegions.set
    (
        i,
        new fvMesh
        // dynamicFvMesh::New
        (
            IOobject
            (
```

```

        fluidNames[i],
        runTime.timeName(),
        runTime,
        IOobject::MUST_READ
    )
)
);
}
}

alphaCourantNo

/*
----- * -----
===== / Field | OpenFOAM: The Open Source CFD
\| Toolbox |
\| / Operation |
\| / And | www.openfoam.com
\|/ Manipulation |

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Global
alphaCourantNo

Description
Calculates and outputs the mean and maximum alpha Courant
Numbers.

```

```

/*
-----*/
#ifndef alphaCourantNo_H
#define alphaCourantNo_H

#include "fvMesh.H"
#include "multiphaseSystem.H"

namespace Foam
{
    scalar alphaCourantNo
    (
        const fvMesh& mesh,
        const Time& runTime,
        const multiphaseSystem& thermol,
        const surfaceScalarField& phi
    );
}

#endif

// ****
***** */

```

ddtAlphaNo.H

```

/*
-----*/
=====
||   / F ield           | OpenFOAM: The Open Source CFD
Toolbox
||   / O peration       |
||   / A nd              | www.openfoam.com
||/  M anipulation      |

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Global
alphaCourantNo

Description
Calculates and outputs the mean and maximum alpha Courant
Numbers.

/*-----*
-----*/

#ifndef ddtAlphaNo_H
#define ddtAlphaNo_H

#include "fvMesh.H"
#include "multiphaseSystem.H"

namespace Foam
{
    scalar ddtAlphaNo
    (
        const fvMesh& mesh,
        const Time& runTime,
        const multiphaseSystem& thermol,
        const surfaceScalarField& phi
    );
}

#endif

```

ddtAlphaNo.C

```

/*-----*
=====
\ \ / F i e l d \ / OpenFOAM: The Open Source CFD
\ \ / T o o l b o x \ /
\ \ / O p e r a t i o n \ /
\ \ / A n d \ / w w w . o p e n f o a m . c o m
\ \ / M a n i p u l a t i o n \ /
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```
/*
-----*/
#include "ddtAlphaNo.H"
#include "fvcom.H"

Foam::scalar Foam::ddtAlphaNo
(
    const fvMesh& mesh,
    const Time& runTime,
    const multiphaseSystem& thermol,
    const surfaceScalarField& phi
)
{
    scalar maxAlphaDdt
    (
        runTime.controlDict().getOrDefault("maxAlphaDdt", GREAT)
    );
    scalar ddtAlphaNum = 0.0;
    if (mesh.nInternalFaces())
    {
        ddtAlphaNum = thermol.ddtAlphaMax().value()*runTime.
            deltaTValue();
    }
    return ddtAlphaNum;
}
```

compressibleCourantNo.H

```
/*
-----*/
===== /
||      /   F ield           / OpenFOAM: The Open Source CFD
||      /   T oolbox
||      /   O peration       /
||      /   A nd             / www.openfoam.com
||      /   M anipulation    /
```

```

-----+
-----+
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Description
Calculates and outputs the mean and maximum Courant Numbers
for the fluid
regions

/*
-----*/
#ifndef compressibleCourantNo_H
#define compressibleCourantNo_H

#include "fvMesh.H"

namespace Foam
{
    scalar compressibleCourantNo
    (
        const fvMesh& mesh,
        const Time& runTime,
        const volScalarField& rho,
        const surfaceScalarField& phi
    );
}

#endif

// ****
// ****

```

compressibleCourantNo.C

```
/*
-----*|
=====| / Field | OpenFOAM: The Open Source CFD
      | Toolbox |
=====| / Operation | |
      | | / And | www.openfoam.com
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*/
-----*/
```

```
#include "compressibleCourantNo.H"
#include "fvvc.H"

Foam::scalar Foam::compressibleCourantNo
(
    const fvMesh& mesh,
    const Time& runTime,
    const volScalarField& rho,
    const surfaceScalarField& phi
)
{
    scalar CoNum = 0.0;
    scalar meanCoNum = 0.0;
```

```

{
    scalarField sumPhi
    (
        fvc::surfaceSum(mag(phi))().primitiveField()
    );

    CoNum = 0.5*gMax(sumPhi/mesh.V().field())*runTime.
        deltaTValue();

    meanCoNum =
        0.5*(gSum(sumPhi)/gSum(mesh.V().field()))*runTime.
            deltaTValue();
}

Info<< "Region:" << mesh.name() << " Courant Number mean:"
<< meanCoNum
<< " max:" << CoNum << endl;

return CoNum;
}

// ****
***** */

```

correctPhi

```

CorrectPhi
(
    U,
    phi,
    p_rgh,
    surfaceScalarField("rAUf", fvc::interpolate(rAU())),
    geometricZeroField(),
    pimple
);

// #include "continuityErrs.H"

```

createFluidFields

```

// Initialise fluid field pointer lists

PtrList<multiphaseSystem> thermoFluid(fluidRegions.size());
PtrList<volScalarField> rhoFluid(fluidRegions.size());
PtrList<volScalarField> TFluid(fluidRegions.size());
PtrList<volVectorField> UFluid(fluidRegions.size());
PtrList<uniformDimensionedScalarField> hRefFluid(fluidRegions.
    size());
PtrList<volScalarField> ghFluid(fluidRegions.size());
PtrList<surfaceScalarField> ghfFluid(fluidRegions.size());
PtrList<volScalarField> kappaLK(fluidRegions.size());
PtrList<CompressibleTurbulenceModel<multiphaseSystem>>
    turbulenceFluid(fluidRegions.size());
PtrList<volScalarField> p_rghFluid(fluidRegions.size());
PtrList<volScalarField> KFluid(fluidRegions.size());
PtrList<volScalarField> dpdtFluid(fluidRegions.size());

```

```

PtrList<multivariateSurfaceInterpolationScheme<scalar>>::  

    fieldTable>  

    fieldsFluid(fluidRegions.size());  

List<scalar> initialMassFluid(fluidRegions.size());  

List<bool> frozenFlowFluid(fluidRegions.size(), false);  

List<bool> correctPhiFluid(fluidRegions.size(), true);  

List<bool> ddtCorrFluid(fluidRegions.size(), true);  

PtrList<fv::options> fluidFvOptions(fluidRegions.size());  

List<label> pRefCellFluid(fluidRegions.size());  

List<scalar> pRefValueFluid(fluidRegions.size());  

PtrList<dimensionedScalar> rhoMinFluid(fluidRegions.size());  

PtrList<dimensionedScalar> rhoMaxFluid(fluidRegions.size());  

PtrList<dimensionedScalar> rhoRFluid(fluidRegions.size());  

PtrList<volScalarField> rhokFluid(fluidRegions.size());  

PtrList<volScalarField> CpFluid(fluidRegions.size());  

PtrList<volScalarField> rhoCpFluid(fluidRegions.size());  

PtrList<volScalarField> pFluid(fluidRegions.size());  

PtrList<surfaceScalarField> rhoPhiFluid(fluidRegions.size());  

PtrList<pimpleControl> pimpleFluid(fluidRegions.size());  
  

PtrList<pressureControl> pressureControls(fluidRegions.size());  
  

const uniformDimensionedVectorField& g = meshObjects::gravity::  

    New(runTime);  
  

// Populate fluid field pointer lists  

forAll(fluidRegions, i)  

{  

    Info<< "***_Reading fluid mesh thermophysical properties for  

    _region "  

    << fluidRegions[i].name() << nl << endl;  

    pimpleFluid.set  

    (  

        i,  

        new pimpleControl(fluidRegions[i])  

    );  
  

    p_rghFluid.set  

    (  

        i,  

        new volScalarField  

        (  

            IOobject  

            (  

                "p_rgh",  

                runTime.timeName(),  

                fluidRegions[i],  

                IOobject::MUST_READ,  

                IOobject::AUTO_WRITE  

            ),  

            fluidRegions[i]
        )
    );
    Info<< " Adding to UFluid\n" << endl;
    UFluid.set
    (
        i,

```

```

    new volVectorField
    (
        IOobject
        (
            "U",
            runTime.timeName(),
            fluidRegions[i],
            IOobject::MUST_READ,
            IOobject::AUTO_WRITE
        ),
        fluidRegions[i]
    )
);

Info<< "Adding to TFluid\n" << endl;
TFluid.set
(
    i,
    new volScalarField
    (
        IOobject
        (
            "T",
            runTime.timeName(),
            fluidRegions[i],
            IOobject::MUST_READ,
            IOobject::AUTO_WRITE
        ),
        fluidRegions[i]
    )
);

Info<< "Adding to hRefFluid\n" << endl;
hRefFluid.set
(
    i,
    new uniformDimensionedScalarField
    (
        IOobject
        (
            "hRef",
            runTime.constant(),
            fluidRegions[i],
            IOobject::READ_IF_PRESENT,
            IOobject::NO_WRITE
        ),
        dimensionedScalar("hRef", dimLength, Zero)
    )
);

Info<< "Calculating field g.h\n" << endl;
#include "readGravitationalAcceleration.H"

dimensionedScalar ghRef
(
    mag(g.value()) > SMALL
    ? g & (cmptMag(g.value()) / mag(g.value())) * hRefFluid[i]

```

```

    : dimensionedScalar("ghRef", g.dimensions()*dimLength, 0)
);

Info<< "Adding toUGHFluid\n" << endl;
ghFluid.set
(
    i,
    new volScalarField
    (
        "gh",
        (g & fluidRegions[i].C()) - ghRef
    )
);

Info<< "Adding toUGHfFluid\n" << endl;
ghfFluid.set
(
    i,
    new surfaceScalarField
    (
        "ghf",
        (g & fluidRegions[i].Cf()) - ghRef
    )
);

pFluid.set
(
    i,
    new volScalarField
    (
        IOobject
        (
            "p",
            runTime.timeName(),
            fluidRegions[i],
            IOobject::NO_READ,
            IOobject::AUTO_WRITE
        ),
        p_rghFluid[i]
    )
);
Info<< "Adding toUthermoFluid\n" << endl;
thermoFluid.set(i, multiphaseSystem::New(fluidRegions[i]).ptr());
Info<< "Adding toUrhoFluid\n" << endl;
rhoFluid.set
(
    i,
    new volScalarField
    (
        IOobject
        (
            "rho",
            runTime.timeName(),
            fluidRegions[i],
            IOobject::NO_READ,
            IOobject::AUTO_WRITE
        )
    )
);

```

```

        ) ,
        thermoFluid[i].rho()
    )
);
rhoFluid[i].oldTime();

const dictionary& thermophysicalPropertiesFluid =
    fluidRegions[i].lookupObject<IOdictionary>(
        "thermophysicalProperties.liquid");

rhoRFluid.set
(
    i,
    new dimensionedScalar
    (
        "rhoRef",
        dimDensity,
        thermophysicalPropertiesFluid.subDict("mixture").subDict
            ("equationOfState")
    )
);
Info<< "uuuuCalculating_rhoK\n" << endl;
rhokFluid.set
(
    i,
    new volScalarField
    (
        IOobject
        (
            "rhok",
            runTime.timeName(),
            fluidRegions[i],
            IOobject::NO_READ,
            IOobject::AUTO_WRITE
        ),
        thermoFluid[i].rho() - rhoRFluid[i]
    )
);
rhokFluid[i].oldTime();

Info<< "uuuuAdding_to_rhoPhiFluid\n" << endl;
rhoPhiFluid.set
(
    i,
    new surfaceScalarField
    (
        IOobject
        (
            "rhoPhi",
            runTime.timeName(),
            fluidRegions[i],
            IOobject::NO_READ,
            IOobject::NO_WRITE
        ),
        thermoFluid[i].rhoPhi()
    )
);
rhoPhiFluid[i].oldTime();

```

```
        )
    );

Info<< "Adding to CpFluid\n" << endl;
CpFluid.set
(
    i,
    new volScalarField
    (
        IOobject
        (
            "Cp",
            runTime.timeName(),
            fluidRegions[i],
            IOobject::NO_READ,
            IOobject::AUTO_WRITE
        ),
        thermoFluid[i].Cp()
    )
);

Info<< "Adding to Kappa Lookup\n" << endl;
kappaLK.set
(
    i,
    new volScalarField
    (
        IOobject
        (
            "kappa",
            runTime.timeName(),
            fluidRegions[i],
            IOobject::NO_READ,
            IOobject::AUTO_WRITE
        ),
        thermoFluid[i].kappa()
    )
);

Info<< "Adding to rhoCpFluid\n" << endl;
rhoCpFluid.set
(
    i,
    new volScalarField
    (
        IOobject
        (
            "rhoCp",
            runTime.timeName(),
            fluidRegions[i],
            IOobject::NO_READ,
            IOobject::NO_WRITE
        ),
        thermoFluid[i].rho()*thermoFluid[i].Cp()
    )
);
rhoCpFluid[i].oldTime();
```

```

Info<< "Adding to turbulenceFluid\n" << endl;
turbulenceFluid.set
(
    i,
    CompressibleTurbulenceModel<multiphaseSystem>::New
    (
        rhoFluid[i],
        UFluid[i],
        rhoPhiFluid[i],
        thermoFluid[i]
    )
);

pFluid[i] = p_rghFluid[i] + rhokFluid[i]*ghFluid[i];

Info<< "Adding to KFluid\n" << endl;
KFluid.set
(
    i,
    new volScalarField
    (
        "K",
        0.5*magSqr(UFluid[i])
    )
);

Info<< "Adding to dpdtFluid\n" << endl;
dpdtFluid.set
(
    i,
    new volScalarField
    (
        IObject
        (
            "dpdt",
            runTime.timeName(),
            fluidRegions[i]
        ),
        fluidRegions[i],
        dimensionedScalar(thermoFluid[i].p().dimensions()/
            dimTime, Zero)
    )
);

pimpleFluid[i].dict().readIfPresent("correctPhi",
    correctPhiFluid[i]);
pimpleFluid[i].dict().readIfPresent("ddtCorr", ddtCorrFluid[i]);
const dictionary& pimpleDict =
    fluidRegions[i].solutionDict().subDict("PIMPLE");

pimpleDict.readIfPresent("frozenFlow", frozenFlowFluid[i]);

rhoMaxFluid.set
(
    i,

```

```

        new dimensionedScalar("rhoMax", dimDensity, GREAT,
                               pimpleDict)
    );

rhoMinFluid.set
(
    i,
    new dimensionedScalar("rhoMin", dimDensity, Zero,
                           pimpleDict)
);

pressureControls.set
(
    i,
    new pressureControl(thermoFluid[i].p(), rhoFluid[i],
                         pimpleDict, false)
);

Info<< "uuuuAdding fvOptions\n" << endl;
fluidFvOptions.set
(
    i,
    new fv::options(fluidRegions[i])
);

pRefCellFluid[i] = 0;
pRefValueFluid[i] = 0.0;

setRefCell
(
    pFluid[i],
    p_rghFluid[i],
    pimpleDict,
    pRefCellFluid[i],
    pRefValueFluid[i]
);

if (p_rghFluid[i].needReference())
{
    pFluid[i] += dimensionedScalar
    (
        "p",
        pFluid[i].dimensions(),
        pRefValueFluid[i] - getRefCellValue(pFluid[i],
                                            pRefCellFluid[i])
    );
    p_rghFluid[i] = pFluid[i] - rhokFluid[i]*ghFluid[i];
}
}

}
```

createFieldRefs

```

PtrList<surfaceScalarField> phiFluid(fluidRegions.size());
forAll(fluidRegions, i)
{
```

```

Info<< "Adding to phiFluid\n" << endl;
phiFluid.set
(
    i,
    new surfaceScalarField
    (
        IOobject
        (
            "phi",
            runTime.timeName(),
            fluidRegions[i],
            IOobject::READ_IF_PRESENT,
            IOobject::AUTO_WRITE
        ),
        thermoFluid[i].phi()
    )
);
}

```

initContinuityErrs

```

PtrList<uniformDimensionedScalarField> cumulativeContErrIO(
    fluidRegions.size());
forAll(cumulativeContErrIO, i)
{
    const fvMesh& mesh = fluidRegions[i];

    cumulativeContErrIO.set
    (
        i,
        new uniformDimensionedScalarField
        (
            IOobject
            (
                "cumulativeContErr",
                runTime.timeName(),
                "uniform",
                mesh,
                IOobject::READ_IF_PRESENT,
                IOobject::AUTO_WRITE
            ),
            dimensionedScalar(dimless, Zero)
        )
    );
}

UPtrList<scalar> cumulativeContErr(cumulativeContErrIO.size());
forAll(cumulativeContErrIO, i)
{
    cumulativeContErr.set(i, &cumulativeContErrIO[i].value());
}

```

ddtAlphaMultiRegionNo

```

scalar ddtAlphaNum = -GREAT;
forAll(fluidRegions, regioni)
{
    ddtAlphaNum = max

```

```

    (
        ddtAlphaNo
        (
            fluidRegions[regioni],
            runTime,
            thermoFluid[regioni],
            phiFluid[regioni]
        ),
        ddtAlphaNum
    );
}

```

compressibleMultiRegionCourantNo

```

scalar CoNum = -GREAT;

forAll(fluidRegions, regioni)
{
    CoNum = max
    (
        compressibleCourantNo
        (
            fluidRegions[regioni],
            runTime,
            rhoFluid[regioni],
            phiFluid[regioni]
        ),
        CoNum
    );
}

```

validateTurbulenceModel

```

forAll(fluidRegions, i)
{
    turbulenceFluid[i].validate();
}

```

readFluidTimeControls

```

/*
----- * \
=====
\\ / F ield           / OpenFOAM: The Open Source CFD
   Toolbox
\\ / O peration        /
\\ / A nd               / www.openfoam.com
\\/ M anipulation      /
----- -
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```

```

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Global
   readTimeControls

Description
   Read the control parameters used by setDeltaT

/*-----*
-----*/

scalar maxAlphaCo =
   runTime.controlDict().get<scalar>("maxAlphaCo");

scalar maxAlphaDdt =
   runTime.controlDict().getOrDefault<scalar>("maxAlphaDdt",
      GREAT);

// *****
***** */ //

```

setRegionFluidFields

```

fvMesh& mesh = fluidRegions[i];

multiphaseSystem& thermol = thermoFluid[i];
volScalarField& kappa = kappaLK[i];
volScalarField& rho = rhoFluid[i];
volVectorField& U = UFluid[i];
volScalarField& T = TFluid[i];
surfaceScalarField& phi = phiFluid[i];
volScalarField& Cp = CpFluid[i];
volScalarField& rhoCp = rhoCpFluid[i];
surfaceScalarField& rhoPhi = rhoPhiFluid[i];
volScalarField& rhok = rhokFluid[i];
dimensionedScalar& rhoR = rhoRFluid[i];
CompressibleTurbulenceModel<multiphaseSystem>& turbulence =
turbulenceFluid[i];

```

```

volScalarField& K = KFluid[i];
volScalarField& dpdt = dpdtFluid[i];
volScalarField& p = pFluid[i];
volScalarField& p_rgh = p_rghFluid[i];

const volScalarField& gh = ghFluid[i];
const surfaceScalarField& ghf = ghfFluid[i];

fv::options& fvOptions = fluidFvOptions[i];

bool frozenFlow = frozenFlowFluid[i];

const label pRefCell = pRefCellFluid[i];
const scalar pRefValue = pRefValueFluid[i];

const dimensionedScalar rhoMax = rhoMaxFluid[i];
const dimensionedScalar rhoMin = rhoMinFluid[i];

const pressureControl& pressureControl = pressureControls[i];
};

pimpleControl& pimple = pimpleFluid[i];

bool correctPhi = correctPhiFluid[i];
bool ddtCorr = ddtCorrFluid[i];

```

readFluidMultiRegionPIMPLEControls

```

const dictionary& pimpleCHT = mesh.solutionDict().subDict("PIMPLE");

const int nCorr =
    pimpleCHT.getOrDefault<int>("nCorrectors", 1);

const int nNonOrthCorr =
    pimpleCHT.getOrDefault<int>("nNonOrthogonalCorrectors",
    0);

const bool momentumPredictor =
    pimpleCHT.getOrDefault("momentumPredictor", false);

// correctPhi = pimple.getOrDefault("correctPhi", true);

// ddtCorr = pimple.getOrDefault("ddtCorr", true);

```

solveFluid

```

if (finalIter)
{
    mesh.data::add("finalIteration", true);
}

#include "initCorrectPhi.H"

if (firstIter)
{
    thermol.correctMassSources(T);
    thermol.solve();
}

```

```

    rho = thermol.rho();

}

if (frozenFlow)
{
    #include "TEqnFluidPhase.H"
}
else
{

    #include "UEqnFluidPhase.H"
    #include "YEqnFluidPhase.H"
    #include "TEqnFluidPhase.H"
        // --- PISO loop

    for (int corr=0; corr<nCorr; corr++)
    {
        #include "pEqnFluidPhase.H"
    }
    if (pimple.turbCorr())
    {
        turbulence.correct();
    }

}

if (finalIter)
{
    rho = thermol.rho();
    mesh.data::remove("finalIteration");
}

```

initCorrectPhi

```

tmp<volScalarField> rAU;

if (correctPhi)
{
    rAU = new volScalarField
    (
        IOobject
        (
            "rAU",
            runTime.timeName(),
            mesh,
            IOobject::READ_IF_PRESENT,
            IOobject::AUTO_WRITE
        ),
        mesh,
        dimensionedScalar("rAU", dimTime/dimDensity, 1)
    );

    #include "correctPhi.H"
}
else
{

```

```

    CorrectPhi
    (
        U,
        phi,
        p_rgh,
        dimensionedScalar("rAUf", dimTime/rho.dimensions(), 1),
        geometricZeroField(),
        pimple
    );
}

```

createFluidMeshes

```

{
    rhoCp = rho*thermol.Cp();

    rhok = rho - rhoR;
    const surfaceScalarField rhoCpPhi(fvc::interpolate(thermol.
        Cp())*rhoPhi);
    volTensorField gradU = fvc::grad(U);
    volTensorField tau = turbulence.muEff() * (gradU + gradU.T())
        );
    const volScalarField kappaEff
    (
        "kappaEff",
        thermol.kappa() + thermol.Cp()*turbulence.mut()/thermol.
            Prt()
    );

    fvScalarMatrix TEqn
    (
        fvm::ddt(rhoCp, T)
        + fvm::div(rhoCpPhi, T, "div(phi,T)")
        + fvc::div(rhoPhi/fvc::interpolate(rho), p, "div(phiv,p)")
        + fvc::ddt(rho, K) + fvc::div(rhoPhi, K)
        - fvm::laplacian(kappaEff, T, "laplacian(kappa,T)")
        ==
        thermol.heatTransfer(T)
        + fvc::div(tau & U, "div(tau,U)")
        + rho*(U&g)
        + fvOptions(rhoCp, T)
    );
    TEqn.relax();

    fvOptions.constrain(TEqn);

    TEqn.solve(mesh.solver(T.select(finalIter)));

    fvOptions.correct(T);
    thermol.correct();

    Info<< "min/max(T)= " << min(T).value() << ", " << max(T).
        value() << endl;
}

```

UEqnFluidPhase

```

rhok = rho - rhoR;

fvVectorMatrix UEqn
(
    fvm::ddt(rho, U)
    + fvm::div(rhoPhi, U)
    + turbulence.divDevRhoReff(U)
    ==
    fvOptions(rho, U)
);

UEqn.relax();

thermol.addInterfacePorosity(UEqn);

if (momentumPredictor)
{
    solve
    (
        UEqn
        ==
        fvc::reconstruct
        (
            (
                thermol.surfaceTensionForce()
                - ghf*fvc::snGrad(rhok)
                - fvc::snGrad(p_rgh)
            ) * mesh.magSf()
        ),
        mesh.solver(U.select(finalIter))
    );

    fvOptions.correct(U);
    K = 0.5*magSqr(U);
}

```

YEqnFluidPhase

```

{
    for (phaseModel& phase : thermol.phases())
    {
        PtrList<volScalarField>& Y = phase.Y();

        if (!Y.empty())
        {
            // Su phase source terms
            PtrList<volScalarField::Internal> Sus(Y.size());
            // Sp phase source terms
            PtrList<volScalarField::Internal> Sps(Y.size());

            forAll(Sus, i)
            {
                Sus.set
                (
                    i,

```

```

        new volScalarField::Internal
        (
            IOobject
            (
                "Su" + phase.name(),
                mesh.time().timeName(),
                mesh
            ),
            mesh,
            dimensionedScalar(dimless/dimTime, Zero)
        )
    );
    SpS.set
    (
        i,
        new volScalarField::Internal
        (
            IOobject
            (
                "Sp" + phase.name(),
                mesh.time().timeName(),
                mesh
            ),
            mesh,
            dimensionedScalar(dimless/dimTime, Zero)
        )
    );
}

forAll(Y, i)
{
    // Calculate mass exchange for species
    // consistent with
    // alpha's source terms.
    thermol.massSpeciesTransfer(phase, Sus[i], SpS[i],
        Y[i].name());
}
phase.solveYi(Sus, SpS);
}
}
}

```

TEqnFluidPhase

```

{
    rhoCp = rho*thermol.Cp();

    rhok = rho - rhoR;
    const surfaceScalarField rhoCpPhi(fvc::interpolate(thermol.
        Cp())*rhoPhi);
    volTensorField gradU = fvc::grad(U);
    volTensorField tau = turbulence.muEff() * (gradU + gradU.T())
    );
    const volScalarField kappaEff
    (
        "kappaEff",

```

```

        thermol.kappa() + thermol.Cp()*turbulence.mut()/thermol.
        Prt()
    );

fvScalarMatrix TEqn
(
    fvm::ddt(rhoCp, T)
    + fvm::div(rhoCpPhi, T, "div(phi,T)")
    + fvc::div(rhoPhi/fvc::interpolate(rho), p, "div(phiv,p)")
    + fvc::ddt(rho, K) + fvc::div(rhoPhi, K)
    - fvm::laplacian(kappaEff, T, "laplacian(kappa,T)")
    ==
    thermol.heatTransfer(T)
    + fvc::div(tau & U, "div(tau,U)")
    + rho*(U&g)
    + fvOptions(rhoCp, T)
);
TEqn.relax();

fvOptions.constrain(TEqn);

TEqn.solve(mesh.solver(T.select(finalIter)));

fvOptions.correct(T);
thermol.correct();

Info<< "min/max(T)= " << min(T).value() << ", " << max(T).
value() << endl;
}

```

pEqnFluidPhase

```

{
    bool closedVolume = p_rgh.needReference();
    rho = thermol.rho();

    rhok = rho - rhoR;

    if (correctPhi)
    {
        rAU.ref() = 1.0/UEqn.A();
    }
    else
    {
        rAU = 1.0/UEqn.A();
    }

    surfaceScalarField rAUf("rAUf", fvc::interpolate(rAU()));

    volVectorField HbyA("HbyA", U);

    HbyA = rAU()*UEqn.H();

    surfaceScalarField phiHbyA
    (

```

```

    "phiHbyA",
    (fvc::interpolate(HbyA) & mesh.Sf())
    + fvc::interpolate(rho*rAU())*fvc::ddtCorr(U, phi)
);

if (p_rgh.needReference())
{
    fvc::makeRelative(phiHbyA, U);
    adjustPhi(phiHbyA, U, p_rgh);
    fvc::makeAbsolute(phiHbyA, U);
}

surfaceScalarField phig
(
(
    thermol.surfaceTensionForce()
    - ghf*fvc::snGrad(rhok)
)*rAUf*mesh.magSf()
);

phiHbyA += phig;

// Update the fixedFluxPressure BCs to ensure flux consistency
constrainPressure(p_rgh, U, phiHbyA, rAUf);

for (int nonOrth=0; nonOrth<=nNonOrthCorr; nonOrth++)
{
    fvScalarMatrix p_rghEqn
    (
        fvc::div(phiHbyA)
        - fvm::laplacian(rAUf, p_rgh)
    );

    if (thermol.includeVolChange())
    {
        p_rghEqn += thermol.volTransfer(p_rgh);
    }

    p_rghEqn.setReference(pRefCell, pRefValue);

    p_rghEqn.solve
    (
        mesh.solver
        (
            p_rgh.select
            (
                (
                    oCorr == nOuterCorr -1
                    && corr == nCorr -1
                    && nonOrth == nNonOrthCorr
                )
            )
        )
    );
}

```

```

) ;

if (nonOrth == nNonOrthCorr)
{
    phi = phiHbyA + p_rghEqn.flux();

    p_rgh.relax();

    U = HbyA + rAU()*fvc::reconstruct((phig + p_rghEqn.
        flux()) / rAUf);

    U.correctBoundaryConditions();

    fvOptions.correct(U);

    K = 0.5 * magSqr(U);

}

}

#include "incompressibleContinuityErrors.H"

fvc::makeRelative(phi, U);
p == p_rgh + rhok*gh;

// For closed-volume cases adjust the pressure and density
// levels
// to obey overall mass continuity
if (p_rgh.needReference())
{
    p += dimensionedScalar
    (
        "p",
        p.dimensions(),
        pRefValue - getRefCellValue(p, pRefCell)
    );
    p_rgh = p - rhok*gh;
}

if (!correctPhi)
{
    rAU.clear();
}
rho = thermol.rho();

// Update pressure time derivative if needed
if (thermol.dpdt())
{
    dpdt = fvc::ddt(p);
}
}

```

B.2.2 Solid region

createSolidMeshes

```

const wordList solidNames(rp["solid"]);

PtrList<fvMesh> solidRegions(solidNames.size());

forAll(solidNames, i)
{
    Info<< "Create_solid_mesh_for_region " << solidNames[i]
        << " for time = " << runTime.timeName() << nl <<
            endl;

    solidRegions.set
    (
        i,
        new fvMesh
        (
            IOobject
            (
                solidNames[i],
                runTime.timeName(),
                runTime,
                IOobject::MUST_READ
            )
        )
    );
}

// Force calculation of geometric properties to prevent
// it being done
// later in e.g. some boundary evaluation
//(void)solidRegions[i].weights();
//(void)solidRegions[i].deltaCoeffs();
}

```

createSolidFields

```

// Initialise solid field pointer lists
PtrList<coordinateSystem> coordinates(solidRegions.size());
PtrList<solidThermo> thermos(solidRegions.size());
PtrList<radiation::radiationModel> radiations(solidRegions.size());
PtrList<fv::options> solidHeatSources(solidRegions.size());
// PtrList<volScalarField> rhos(solidRegions.size());
// PtrList<volScalarField> cps(solidRegions.size());
// PtrList<volScalarField> rhoCpSolid(solidRegions.size());
// PtrList<volScalarField> Ks(solidRegions.size());
// PtrList<volScalarField> Ts(solidRegions.size());
PtrList<volScalarField> betavSolid(solidRegions.size());
PtrList<volSymmTensorField> aniAlphas(solidRegions.size());

// Populate solid field pointer lists
forAll(solidRegions, i)
{
    Info<< "***_Reading_solid_mesh_thermophysical_properties
        _for_region "
        << solidRegions[i].name() << nl << endl;
}

```

```

// Info<< "      Adding to Ts\n" << endl;
// Ts.set
// (
//   i,
//   new volScalarField
//   (
//     IOobject
//     (
//       "T",
//       runTime.timeName(),
//       solidRegions[i],
//       IOobject::MUST_READ,
//       IOobject::AUTO_WRITE
//     ),
//     solidRegions[i]
//   )
// );
Info<< "uuuuAdding to thermos\n" << endl;
thermos.set(i, solidThermo::New(solidRegions[i]));

Info<< "uuuuAdding to radiations\n" << endl;
radiations.set(i, radiation::radiationModel::New(thermos
[i].T()));

Info<< "uuuuAdding fvOptions\n" << endl;
solidHeatSources.set
(
  i,
  new fv::options(solidRegions[i])
);

if (!thermos[i].isotropic())
{
  Info<< "uuuuAdding coordinateSystems\n" << endl;
  coordinates.set
  (
    i,
    coordinateSystem::New
    (
      solidRegions[i],
      thermos[i],
      coordinateSystem::typeName_()
    )
  );

  tmp<volVectorField> tkappaByCp =
    thermos[i].Kappa()/thermos[i].Cp();

  aniAlphas.set
  (
    i,
    new volSymmTensorField
    (
      IOobject
      (
        "Anialpha",

```

```

        runTime.timeName(),
        solidRegions[i],
        IOobject::NO_READ,
        IOobject::NO_WRITE
    ),
    solidRegions[i],
    dimensionedSymmTensor(tkappaByCp().
        dimensions(), Zero),
    zeroGradientFvPatchSymmTensorField::typeName
)
);

aniAlphas[i].primitiveFieldRef() =
    coordinates[i].transformPrincipal
(
    solidRegions[i].cellCentres(),
    tkappaByCp()
);
aniAlphas[i].correctBoundaryConditions();

}

IOobject betavSolidIO
(
    "betavSolid",
    runTime.timeName(),
    solidRegions[i],
    IOobject::MUST_READ,
    IOobject::AUTO_WRITE
);

if (betavSolidIO.typeHeaderOk<volScalarField>(true))
{
    betavSolid.set
    (
        i,
        new volScalarField(betavSolidIO, solidRegions[i])
    );
}
else
{
    betavSolid.set
    (
        i,
        new volScalarField
        (
            IOobject
            (
                "betavSolid",
                runTime.timeName(),
                solidRegions[i],
                IOobject::NO_READ,
                IOobject::NO_WRITE
            ),
            solidRegions[i],
            dimensionedScalar("1", dimless, scalar(1))
        )
    );
}

```

```

        )
    );
}

// Info << "      Adding to rhos\n" << endl;
// rhos.set
// (
//     i,
//     new volScalarField
//     (
//         IOobject
//         (
//             "rho",
//             runTime.timeName(),
//             solidRegions[i],
//             IOobject::NO_READ,
//             IOobject::AUTO_WRITE
//         ),
//         thermos[i].rho()
//     )
// );

// Info << "      Adding to Cps\n" << endl;
// cps.set
// (
//     i,
//     new volScalarField
//     (
//         IOobject
//         (
//             "cp",
//             runTime.timeName(),
//             solidRegions[i],
//             IOobject::NO_READ,
//             IOobject::AUTO_WRITE
//         ),
//         thermos[i].Cp()
//     )
// );

// Info << "Calculating field rhoCps\n" << endl;
// rhoCpSolid.set
// (
//     i,
//     new volScalarField
//     (
//         IOobject
//         (
//             "rhoCp",
//             runTime.timeName(),
//             solidRegions[i],
//             IOobject::NO_READ,
//             IOobject::NO_WRITE
//         ),
//         thermos[i].rho()*thermos[i].Cp()
//     )
// );

```

```

// Info << "      Adding to Ks\n" << endl;
// Ks.set
// (
//     i,
//     new volScalarField
//     (
//         IOobject
//         (
//             "K",
//             runTime.timeName(),
//             solidRegions[i],
//             IOobject::NO_READ,
//             IOobject::AUTO_WRITE
//         ),
//         thermos[i].kappa()
//     )
// );
// }

}
```

solidRegionDiffusionNo

```

scalar DiNum = -GREAT;

forAll(solidRegions, i)
{
    // Note: do not use setRegionSolidFields.H to avoid double
    // registering Cp
    //#include "setRegionSolidFields.H"
    const solidThermo& therms = thermos[i];

    tmp<volScalarField> magKappa;
    if (therms.isotropic())
    {
        magKappa = therms.kappa();
    }
    else
    {
        magKappa = mag(therms.Kappa());
    }

    tmp<volScalarField> tcp = therms.Cp();
    const volScalarField& cp = tcp();

    tmp<volScalarField> trho = therms.rho();
    const volScalarField& rho = trho();

    DiNum = max
    (
        solidRegionDiffNo
        (
            solidRegions[i],
            runTime,
            rho*cp,

```

```

        magKappa()
),
DiNum
);

}

```

solidRegionDiffNo.H

```

/*
-----*/
===== / Field | OpenFOAM: The Open Source CFD
      Toolbox
===== / Operation | www.openfoam.com
===== / And | www.openfoam.com
===== / Manipulation | www.openfoam.com

-----|
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licenses/>.

Description
Calculates and outputs the mean and maximum Diffusion
Numbers for the solid
regions

/*
-----*/
#ifndef solidRegionDiffNo_H
#define solidRegionDiffNo_H

```

```
#include "fvMesh.H"

namespace Foam
{
    scalar solidRegionDiffNo
    (
        const fvMesh& mesh,
        const Time& runTime,
        const volScalarField& Cprho,
        const volScalarField& kappa
    );
}

#endif

// ****
// ****
// ****
```

solidRegionDiffNo.C

```
/*
   - *
=====
   \ \ / F ield           / OpenFOAM: The Open Source CFD
     Toolbox
   \ \ / O peration       /
   \ \ / A nd              / www.openfoam.com
   \ \ / M anipulation    /
-----
   -
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-----
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```

```

/*
-----*/
#include "solidRegionDiffNo.H"
#include "surfaceInterpolate.H"

// * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
* * * * * * * //



Foam::scalar Foam::solidRegionDiffNo
(
    const fvMesh& mesh,
    const Time& runTime,
    const volScalarField& Cprho,
    const volScalarField& kappa
)
{
    surfaceScalarField kapparhoCpbyDelta
    (
        sqr(mesh.surfaceInterpolation::deltaCoeffs())
        *fvc::interpolate(kappa)
        /fvc::interpolate(Cprho)
    );

    const scalar DiNum = max(kapparhoCpbyDelta).value()*runTime.
        deltaTValue();
    const scalar meanDiNum =
        average(kapparhoCpbyDelta).value()*runTime.deltaTValue()
        ;

    Info<< "Region:" << mesh.name() << "DiffusionNumber" << mean:
        << "max:" << DiNum << endl;

    return DiNum;
}

// ****
***** */

```

setRegionSolidFields

```

fvMesh& mesh = solidRegions[i];
solidThermo& therms = thermos[i];

// volScalarField& rho = rhos[i];
// volScalarField& cp = cps[i];
// volScalarField& rhoCps = rhoCpSolid[i];
// volScalarField& K = Ks[i];
// volScalarField& T = Ts[i];

tmp<volScalarField> trho = therms.rho();
const volScalarField& rhosol = trho();

tmp<volScalarField> tcp = thermos.Cp();
const volScalarField& cpsol = tcp();

```

```

// tmp<volScalarField> tkappa = thermo.kappa();
// const volScalarField& kappa = tkappa();

// volScalarField& Tsol = Ts[i];

tmp<volSymmTensorField> taniAlpha;
if (!therms.isotropic())
{
    volSymmTensorField& aniAlpha = aniAlphas[i];
    tmp<volVectorField> tkappaByCp = therms.Kappa()/cpsol;
    const coordinateSystem& coodSys = coordinates[i];

    aniAlpha.primitiveFieldRef() =
        coodSys.transformPrincipal
    (
        mesh.cellCentres(),
        tkappaByCp()
    );

    aniAlpha.correctBoundaryConditions();

    taniAlpha = tmp<volSymmTensorField>
    (
        new volSymmTensorField(aniAlpha)
    );
}

const volScalarField& betav = betavSolid[i];

fv::options& fvOptions = solidHeatSources[i];
volScalarField& h = therms.he();

```

readSolidMultiRegionPIMPLEControls

```

const dictionary& pimpleCHT = mesh.solutionDict().subDict("PIMPLE");

int nNonOrthCorr =
    pimpleCHT.getOrDefault<int>("nNonOrthogonalCorrectors", 0);

```

solveSolid

```

if (finalIter)
{
    mesh.data::add("finalIteration", true);
}

{
    for (int nonOrth=0; nonOrth<=nNonOrthCorr; ++nonOrth)
    {
        fvScalarMatrix hEqn
        (
            fvm::ddt(betav*rhosol, h)
            - (
                therms.isotropic()
                ? fvm::laplacian(betav*therms.alpha(), h, "laplacian(alpha,h)")

```

```

        : fvm::laplacian(betaV*taniAlpha(), h, "laplacian(
            alpha,h)")
    )
    ==
    fvOptions(rhosol, h)
);

hEqn.relax();

fvOptions.constrain(hEqn);

hEqn.solve(mesh.solver(h.select(finalIter)));

fvOptions.correct(h);
}

therms.correct();

Info<< "Min/max_T:" << min(therms.T()).value() << ' '
<< max(therms.T()).value() << endl;
}

if (finalIter)
{
    mesh.data::remove("finalIteration");
}

```

readSolidTimeControls

```

/*
 *-----*
=====
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 \|      / Operation       /
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-----*
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```

Global

```
readSolidTimeControls
```

Description

```
Read the control parameters used in the solid
```

```
\*-----*/
```

```
scalar maxDi = runTime.controlDict().getOrDefault<scalar>("maxDi  
", 10);
```

```
// ***** //  
***** */
```