

optimization problem

#### MPC OUTPUT AND INPUTS

FS-MPC algorithm accepts 7 input values: time ( $t$ ), filter currents ( $i_{\alpha}$ ,  $i_{\beta}$ ), capacitor voltage deviations ( $\Delta v_{c\alpha}$ ,  $\Delta v_{c\beta}$ ), optimum voltage vector from previous sampling period  $x(k-1)$ , load resistance ( $R_{load}$ ) and calculates 3 output values: reference values ( $v_{ref\alpha}$ ,  $v_{ref\beta}$ ), and future optimum switching combination  $x(k+1)$ . The reference values  $v_{ref\alpha\beta}$  are not used in the inputs because the two values are coupled and to keep this dependency it is more convenient to use time vector as an input value. They are calculated using two sine wave equations with a  $120^\circ$  phase shift and the input value of the time vector  $t$ . \cite{Imitation\_learning}

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#### COST FUNCTION

THEN, DERIVATIVES ARE NEEDED AND DRAWING, AND NEW COST FUNCTION WITH EVERYTHING AS IN 1))))))

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In [30], the conventional Euclidean distance-based CF in the  $\alpha\beta$  frame was used:

$$g_{con} = v_{f\alpha}^2 - v_{f\alpha}^2 + v_{f\beta}^2 - v_{f\beta}^2$$

It aims to minimize the Euclidean distance at every sampling instant.

\cite{Dragicevic2018}

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To determine which of the control actions is to be selected, a decision or cost function  $f_g$  can be defined, usually dependent on the desired reference

value and the predictions  $g_i = f_g\{x^*(t_{k+1}), x_{pi}(t_{k+1})\}$ , for  $i = 1, \dots, n$ . Note that the future reference value is needed  $x^*(t_{k+1})$ , which can be assumed to be equal to the actual value  $x^*(t_k)$ , since  $T_s$  is sufficiently small compared with the dynamic behavior of the system, and thus, the reference can be considered constant over  $T_s$ . If needed for highly dynamic systems, the future reference value  $x^*(t_{k+1})$  can be estimated via appropriate extrapolation methods. (as in ours) \cite{Kouro2009}

A typical example for would be the absolute error between the predictions and the reference  $g_i = |x^*(t_{k+1}) - x_{pi}(t_{k+1})|$  /IN OUR CASE IS NOT ABSOLUTE, IS SQUARED WHICH TAKES ABSOLUTE VALUE AND ALSO MAKES BIG DIFFERENCES BIGGER AND SMALL DIFFERENCES SMALLER). The evaluation of the cost function with the  $n$  predictions will lead to  $n$  different costs. Naturally, the control action leading to the minimum cost ( $\min\{g_i\}$ , for  $i = 1, \dots, n$ ) is selected to control the system \cite{Kouro2009}

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where  $v^*$   
 $f = v_f \alpha^* + j v_f \beta^*$  is the voltage reference vector,  $\omega$  is the reference frequency and  $\lambda_d$  is the weighting factor of the additional current reference term. This term was proposed in [16] for improving the steady state performance of the algorithm and the weighting factor can be selected using the ANN approach in [17]. Table I shows system parameters used in the control algorithm \cite{Imitation\_learning}.

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INTRO TO THIS FIGURE

A simplified control block diagram and the corresponding algorithm for the real-time implementation of FCS-MPC are shown in Figs. 2 and 3, respectively, considering a generic

system variable  $x(t)$ . It is worth mentioning that this control method is not limited to a single variable; on the contrary, multiple variables, system constraints, perturbations, saturations, and, basically, every characteristic that can be mathematically modeled and measured can be included in the predictive model and cost function. This is the basis of the great flexibility and control potential that can be achieved with FCS-MPC. Moreover, the fact that power converters have a reduced and limited number of switching states (or control set) makes this method feasible to implement with present-day available microprocessing resources. Since only a discrete model of the system is necessary, rather than approximated linear models together with control system design theory and modulation algorithms, a simpler and more direct design and implementation of the controller can be achieved. \cite{Kouro2009}

#### MPC EXPLANATION FIGURE

Based on the example shown in Fig. \ref{fig:MPC\_explanation}, the predicted value  $x$   $p_3(t_k+1)$  is the closest to the reference  $x^*(t_k+1)$ ; hence,  $S_3$  is selected and applied in  $t = t_k$ . Following the same criterion,  $S_2$  is selected and applied in  $t = t_k+1$ . However, the ideal theoretical case in which the variables can be measured, predicted, and controlled instantly in  $t = t_k$  is not realizable in real-time applications. Nevertheless, this problem can be overcome if a two-step-ahead prediction is considered, as shown in Fig. 1(b), in which the control action to be applied in the following sample time  $S(t_k+1)$  is determined. This way, a complete sample period  $T_s$  is available to perform the algorithm. Naturally, the sample period  $T_s$  has to be greater than the measurement, computation, and actuation times added together. Assume that on a sample time  $t_k$ , a measurement  $x(t_k)$

is made and the previously computed control action  $S(t_k)$  is applied. With this information and the system model, a first prediction can be made to obtain the future value  $x(t_{k+1})$  (this is the first step prediction). Now, from the predicted value

$x$

$p(t_{k+1})$ , the FCS-MPC algorithm is performed for  $n$  possible control actions, leading to one optimal selection  $S(t_{k+1})$

(this is the second step prediction). Both predictions are performed during the first sample period, and then, at  $t = t_{k+1}$ ,

the optimal selected control action  $S(t_{k+1})$  is applied, while

$x(t_{k+1})$  is measured to perform the algorithm again. As shown

in the example in Fig. 1(b), there is only one prediction for

the first step, given by the applied control action  $S(t_k) = S_3$

determined in the previous execution of the algorithm while  $S(t_{k+1}) = S_2$  is selected from the  $n$  predictions for the

second step. \cite{Kouro2009}

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1)))))) WHY DERIVATIVES

Although this may result in satisfactory performance for first order systems, coupling between the state variables makes it somewhat unsuitable for second order ones. The reason is that the controlled variable in first-order systems (i.e., converter side inductor current in the L filter) can be directly regulated by the control input, allowing an instantaneous change of its derivative at a particular sampling instant. On the contrary, capacitor voltage in the second-order LC filter configuration can only be regulated indirectly through the inductor current. As respective current cannot change instantaneously its value, the capacitor voltage correspondingly cannot change its derivative instantaneously.

Therefore, by involving exclusively the capacitor voltage error in the CF, as in (21), no respect is given to its derivative. The

result is that the minimal magnitude error will often be achieved

at a cost of having voltage trajectory pointing significantly away

from the reference trajectory. This causes intractable voltage deviations in intersampling periods which often lead to unfavorable starting points at future time instants, ultimately resulting

in high total harmonic distortion (THD) in the measured voltage

signal.

This phenomenon is illustrated in Fig. 4, where the exemplary propagation of capacitor voltage is shown. It can be seen

from the figure that, although the transition from the initial time

step  $t_1$  to step  $t_2$  with control input  $u = 2$  leads to the smallest

error at the sampling instance  $t_2$ , it also results in a significant

deviation of voltage trajectory heading from the reference heading. Therefore, the capacitor voltage will continue to decrease

rapidly regardless of the input applied at time instant  $t_2$ , resulting in a large oscillations around the reference and consequently

a large THD. \cite{Dragicevic2018}

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Assuming the model of the system to be accurate enough, FS-MPC often yields better stationary and transient response than linear closed-loop control structures.

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we do not need to use modulation this controller already creates the signals to the switches

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In addition, other converter topologies, drives, and applications are addressed to show the flexibility and potentiality of FCS-MPC

\cite{Kouro2009}

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%FS-MPC has, however, an important shortcoming. When predicting the values of states for more than a single step ahead, the number of calculations to be performed increases exponentially.

%The exponentially increasing computational requirements of FS-MPC means that it is often not possible to implement such an algorithm that is able to run in a time short enough to guarantee adequate performance while using a prediction window larger than very few steps ahead. For multi-level and multi-cell converters, for which many more possible states exist than for a six-switch inverter, this problem is further accentuated.

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MPC has several advantages, such as the easy inclusion of nonlinearities and constraints. This scheme has

few applications in power converter control and drives due to the high amount of calculations needed in order to solve the optimization problem online, which is incompatible with the small sampling times used in converter control. One solution in order to reduce the calculation time is to solve the optimization

problem offline, as presented in [27], where MPC is implemented as a search tree and the calculation time is reduced,

making it possible to use the MPC in drive control. Another

solution is the use of Generalized Predictive Control (GPC)

[28], where the optimization is solved analytically, obtaining

a linear controller. Nevertheless, with GPC, it is very difficult

to include system constraints and nonlinearities. \cite{Kouro2009}.

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MPC forces to commutate the optimal choice for each  $T_s$ , this sometimes means to continue with the previous state and do not commutate that sampling period, hence the average switching frequency is variable. drawback: spread current spectrum.

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#### COMPARACION SVM CON MPC

Fijando  $T_s$ , switchea menos que SVM porque SVM cambia 6 veces por  $T_s$ , sin embargo, MPC no elige la pata optima que cambiar, sino que elige el estado, de forma que cambiar de un estado a otro puede incluir cambiar varias ptas a la vez, un maximo de 3. de esta forma, MPC cambiaria de 0 a 3 switches respecto a los 6 que cambiar de forma continua por  $T_s$  SVM.