K-Means

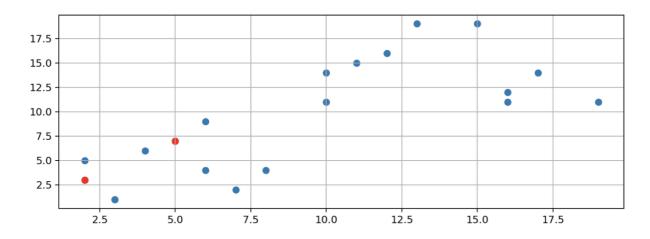
10185101210 陈俊潼

East China Normal University

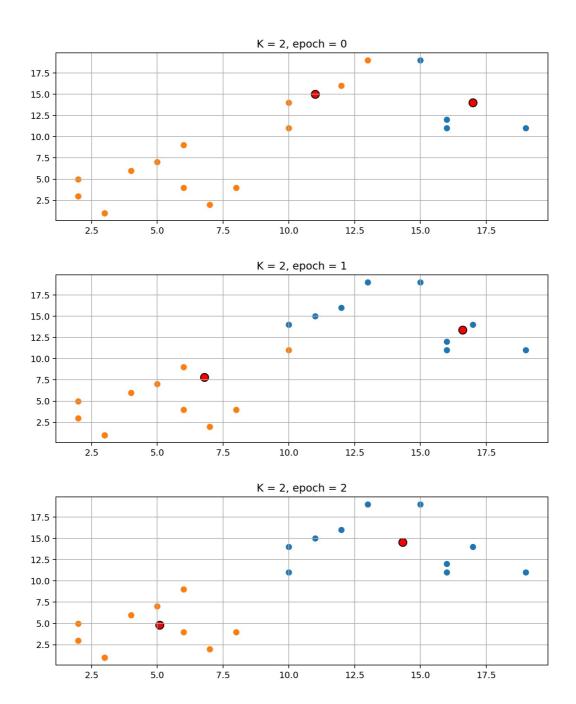
K-Means 均值聚类,主要代码位于 kmeans.ipynb 中。依次执行所有代码块即可。

K=2

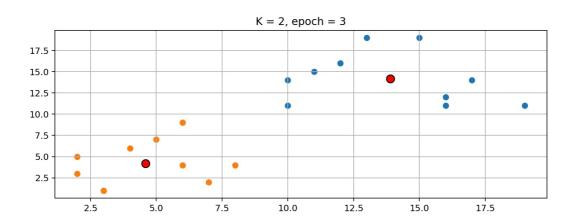
K=2时,随机选择两个点作为聚类起点(用红色标注):



经过了四次迭代后中心坐标不再改变。迭代过程如下图所示:



最终聚类结果:

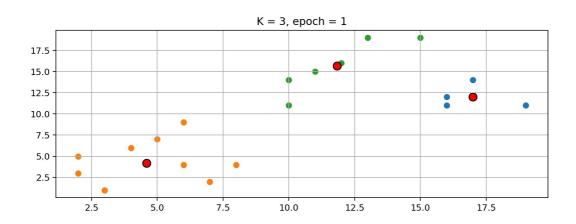


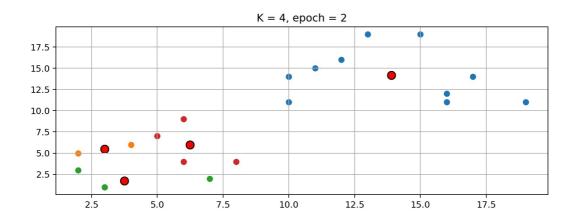
主要日志:

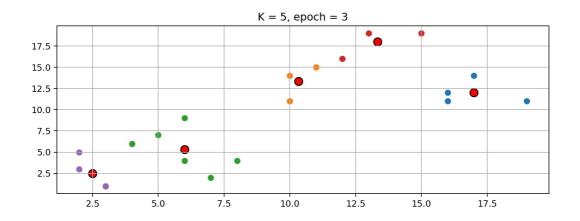
最终可以得到聚类中心的坐标为: (4.6, 4.2) (13.9, 14.2)

K = 2 - 5

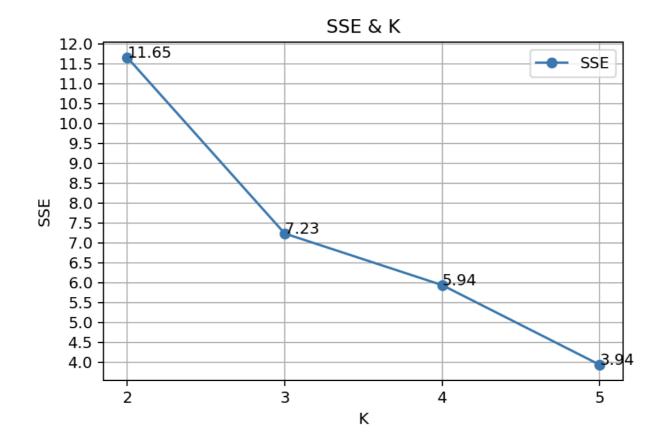
将 K 分别设置为 2、3、4、5, 并分别计算。得到分别的最终的聚类结果和聚类中心如下:







得到 SSE 和 K 的关系如下。可以看出随着 K 的增加,SSE 的值逐渐减小,可以认为分类效果更好。但当 K=5 时,分类簇相对数据点过多,每次的聚类效果会存在一定的随机性:

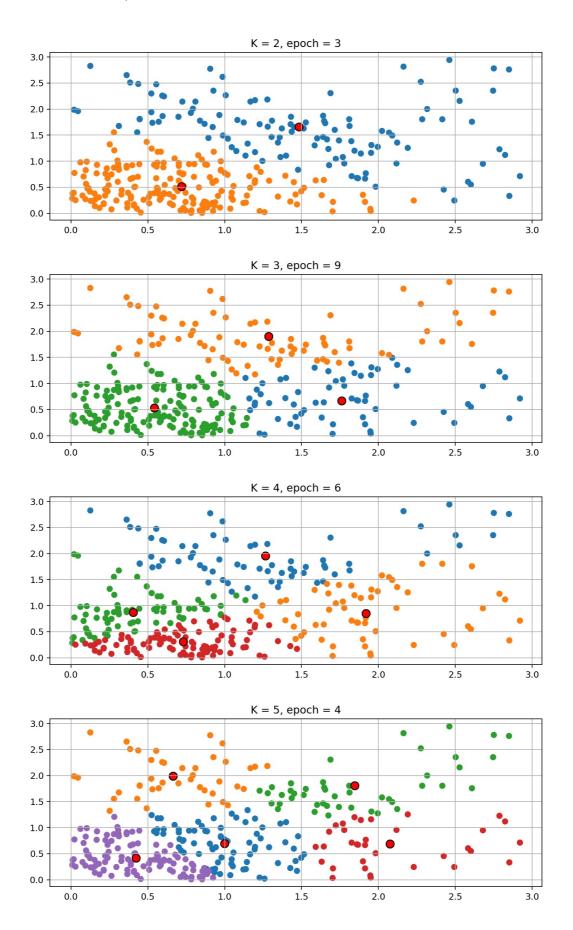


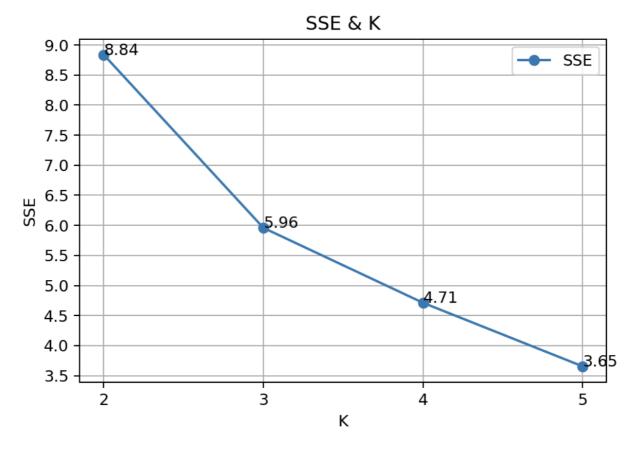
```
1 <2021-01-02 19:53:59 INFO>: K-Means started. K = 2, MAX_EPOCHS = 10
 2 <2021-01-02 19:54:00 INFO>: [EPOCH 0] Centroid updated: [[16.6 13.4] [ 6.8 7.8]]
 3 <2021-01-02 19:54:00 INFO>: [EPOCH 0] Current SSE: 16.695507816124437; Centroid
    offset: 8.366600265340756
4 <2021-01-02 19:54:00 INFO>: [EPOCH 1] Centroid updated: [[14.33 14.56] [ 5.09
    4.82]]
5 <2021-01-02 19:54:00 INFO>: [EPOCH 1] Current SSE: 12.57577169192891; Centroid
   offset: 4.276133513433808
6 <2021-01-02 19:54:00 INFO>: [EPOCH 2] Centroid updated: [[13.9 14.2] [ 4.6 4.2]]
7 <2021-01-02 19:54:00 INFO>: [EPOCH 2] Current SSE: 11.654674875992491; Centroid
   offset: 0.9681621903028267
8 <2021-01-02 19:54:01 INFO>: [EPOCH 3] Centroids are almost stable. Iterating
   stopped.
9 <2021-01-02 19:54:01 INFO>: [EPOCH 3] Current SSE: 11.654674875992491; Centroid
   offset: 0.0
10 <2021-01-02 19:54:01 INFO>: Centroid coordinates: [[13.9 14.2] [ 4.6 4.2]]
11 <2021-01-02 19:56:29 INFO>: K-Means started. K = 2, MAX_EPOCHS = 10
12 <2021-01-02 19:56:30 INFO>: [EPOCH 0] Centroid updated: [[13.9 14.2] [ 4.6 4.2]]
13 <2021-01-02 19:56:30 INFO>: [EPOCH 0] Current SSE: 11.654674875992491; Centroid
    offset: 5.123475382979798
14 <2021-01-02 19:56:30 INFO>: [EPOCH 1] Centroids are almost stable. Iterating
    stopped.
15 <2021-01-02 19:56:30 INFO>: [EPOCH 1] Current SSE: 11.654674875992491; Centroid
   offset: 0.0
16 <2021-01-02 19:56:30 INFO>: Centroid coordinates: [[13.9 14.2] [ 4.6 4.2]]
17 <2021-01-02 19:56:45 INFO>: K-Means started. K = 2, MAX_EPOCHS = 10
18 <2021-01-02 19:56:45 INFO>: [EPOCH 0] Centroid updated: [[ 4.6 4.2] [13.9 14.2]]
19 <2021-01-02 19:56:45 INFO>: [EPOCH 0] Current SSE: 11.654674875992491; Centroid
   offset: 4.695742752749558
20 <2021-01-02 19:56:46 INFO>: [EPOCH 1] Centroids are almost stable. Iterating
    stopped.
21 <2021-01-02 19:56:46 INFO>: [EPOCH 1] Current SSE: 11.654674875992491; Centroid
   offset: 0.0
22 <2021-01-02 19:56:46 INFO>: Centroid coordinates: [[ 4.6 4.2] [13.9 14.2]]
23 <2021-01-02 19:56:46 INFO>: K-Means started. K = 3, MAX_EPOCHS = 10
[11.83 15.67]]
25 <2021-01-02 19:56:46 INFO>: [EPOCH 0] Current SSE: 7.232632038258262; Centroid
   offset: 4.2354325503883175
26 <2021-01-02 19:56:46 INFO>: [EPOCH 1] Centroids are almost stable. Iterating
    stopped.
```

```
27 <2021-01-02 19:56:46 INFO>: [EPOCH 1] Current SSE: 7.232632038258262; Centroid
   offset: 0.0
28 <2021-01-02 19:56:46 INFO>: Centroid coordinates: [[17. 12. ] [ 4.6 4.2 ]
    [11.83 15.67]]
29 <2021-01-02 19:56:46 INFO>: K-Means started. K = 4, MAX_EPOCHS = 10
30 <2021-01-02 19:56:47 INFO>: [EPOCH 0] Centroid updated: [[13.18 13.73] [ 4. 5. ]
    [ 3.75 1.75] [ 6.5 5.5 ]]
31 <2021-01-02 19:56:47 INFO>: [EPOCH 0] Current SSE: 6.5849737413632425; Centroid
   offset: 8.974999712240148
32 <2021-01-02 19:56:47 INFO>: [EPOCH 1] Centroid updated: [[13.9 14.2 ] [ 3. 5.5 ]
    [ 3.75 1.75] [ 6.25 6. ]]
33 <2021-01-02 19:56:47 INFO>: [EPOCH 1] Current SSE: 5.93599494586555; Centroid
   offset: 1.5171539797749958
34 <2021-01-02 19:56:48 INFO>: [EPOCH 2] Centroids are almost stable. Iterating
35 <2021-01-02 19:56:48 INFO>: [EPOCH 2] Current SSE: 5.93599494586555; Centroid
   offset: 0.0
36 <2021-01-02 19:56:48 INFO>: Centroid coordinates: [[13.9 14.2 ] [ 3. 5.5 ] [
   3.75 1.75] [ 6.25 6. ]]
37 <2021-01-02 19:56:48 INFO>: K-Means started. K = 5, MAX_EPOCHS = 10
38 <2021-01-02 19:56:48 INFO>: [EPOCH 0] Centroid updated: [[16.6 13.4 ] [10. 12.5 ]
    [ 6. 5.33] [12. 16.67] [ 2.5 2.5 ]]
39 <2021-01-02 19:56:48 INFO>: [EPOCH 0] Current SSE: 4.53122887111425; Centroid
   offset: 3.8503968049482324
40 <2021-01-02 19:56:49 INFO>: [EPOCH 1] Centroid updated: [[17. 12. ] [10. 12.5]
          5.33] [12.75 17.25] [ 2.5 2.5 ]]
41 <2021-01-02 19:56:49 INFO>: [EPOCH 1] Current SSE: 4.023086665782328; Centroid
   offset: 1.7386137517510254
42 <2021-01-02 19:56:49 INFO>: [EPOCH 2] Centroid updated: [[17. 12. ] [10.33 13.33]
    [ 6. 5.33] [13.33 18. ] [ 2.5 2.5 ]]
43 <2021-01-02 19:56:49 INFO>: [EPOCH 2] Current SSE: 3.9356681049237885; Centroid
   offset: 1.3070322617798442
44 <2021-01-02 19:56:49 INFO>: [EPOCH 3] Centroids are almost stable. Iterating
45 <2021-01-02 19:56:49 INFO>: [EPOCH 3] Current SSE: 3.9356681049237885; Centroid
46 <2021-01-02 19:56:49 INFO>: Centroid coordinates: [[17. 12. ] [10.33 13.33] [ 6.
      5.33] [13.33 18. ] [ 2.5 2.5 ]]
```

随机数据

使用大量生成的随机数据可以更好地展示聚类效果。例如,随机生成主要集中在左下角的 300 个点并再次分别使用 K=2-5 聚类,得到如下结果:





主要日志如下:

```
1 <2021-01-02 19:53:59 INFO>: K-Means started. K = 2, MAX_EPOCHS = 10
 2 <2021-01-02 19:54:00 INFO>: [EPOCH 0] Centroid updated: [[16.6 13.4] [ 6.8 7.8]]
3 <2021-01-02 19:54:00 INFO>: [EPOCH 0] Current SSE: 16.695507816124437; Centroid
  offset: 8.366600265340756
4 <2021-01-02 19:54:00 INFO>: [EPOCH 1] Centroid updated: [[14.33 14.56] [ 5.09
  4.82]]
5 <2021-01-02 19:54:00 INFO>: [EPOCH 1] Current SSE: 12.57577169192891; Centroid
  offset: 4.276133513433808
6 <2021-01-02 19:54:00 INFO>: [EPOCH 2] Centroid updated: [[13.9 14.2] [ 4.6 4.2]]
 7 <2021-01-02 19:54:00 INFO>: [EPOCH 2] Current SSE: 11.654674875992491; Centroid
  offset: 0.9681621903028267
8 <2021-01-02 19:54:01 INFO>: [EPOCH 3] Centroids are almost stable. Iterating
9 <2021-01-02 19:54:01 INFO>: [EPOCH 3] Current SSE: 11.654674875992491; Centroid
  offset: 0.0
10 <2021-01-02 19:54:01 INFO>: Centroid coordinates: [[13.9 14.2] [ 4.6 4.2]]
11 <2021-01-02 19:56:29 INFO>: K-Means started. K = 2, MAX_EPOCHS = 10
12 <2021-01-02 19:56:30 INFO>: [EPOCH 0] Centroid updated: [[13.9 14.2] [ 4.6 4.2]]
13 <2021-01-02 19:56:30 INFO>: [EPOCH 0] Current SSE: 11.654674875992491; Centroid
  offset: 5.123475382979798
```

```
14 <2021-01-02 19:56:30 INFO>: [EPOCH 1] Centroids are almost stable. Iterating
  stopped.
15 <2021-01-02 19:56:30 INFO>: [EPOCH 1] Current SSE: 11.654674875992491; Centroid
16 <2021-01-02 19:56:30 INFO>: Centroid coordinates: [[13.9 14.2] [ 4.6 4.2]]
17 <2021-01-02 19:56:45 INFO>: K-Means started. K = 2, MAX_EPOCHS = 10
18 <2021-01-02 19:56:45 INFO>: [EPOCH 0] Centroid updated: [[ 4.6 4.2] [13.9 14.2]]
19 <2021-01-02 19:56:45 INFO>: [EPOCH 0] Current SSE: 11.654674875992491; Centroid
  offset: 4.695742752749558
20 <2021-01-02 19:56:46 INFO>: [EPOCH 1] Centroids are almost stable. Iterating
21 <2021-01-02 19:56:46 INFO>: [EPOCH 1] Current SSE: 11.654674875992491; Centroid
  offset: 0.0
22 <2021-01-02 19:56:46 INFO>: Centroid coordinates: [[ 4.6 4.2] [13.9 14.2]]
23 <2021-01-02 19:56:46 INFO>: K-Means started. K = 3, MAX_EPOCHS = 10
[11.83 15.67]]
25 <2021-01-02 19:56:46 INFO>: [EPOCH 0] Current SSE: 7.232632038258262; Centroid
  offset: 4.2354325503883175
26 <2021-01-02 19:56:46 INFO>: [EPOCH 1] Centroids are almost stable. Iterating
  stopped.
27 <2021-01-02 19:56:46 INFO>: [EPOCH 1] Current SSE: 7.232632038258262; Centroid
28 <2021-01-02 19:56:46 INFO>: Centroid coordinates: [[17. 12. ] [ 4.6 4.2 ]
  [11.83 15.67]]
29 <2021-01-02 19:56:46 INFO>: K-Means started. K = 4, MAX_EPOCHS = 10
30 <2021-01-02 19:56:47 INFO>: [EPOCH 0] Centroid updated: [[13.18 13.73] [ 4.
   [ 3.75 1.75] [ 6.5 5.5 ]]
31 <2021-01-02 19:56:47 INFO>: [EPOCH 0] Current SSE: 6.5849737413632425; Centroid
  offset: 8.974999712240148
32 <2021-01-02 19:56:47 INFO>: [EPOCH 1] Centroid updated: [[13.9 14.2 ] [ 3. 5.5 ]
   [ 3.75 1.75] [ 6.25 6. ]]
33 <2021-01-02 19:56:47 INFO>: [EPOCH 1] Current SSE: 5.93599494586555; Centroid
  offset: 1.5171539797749958
34 <2021-01-02 19:56:48 INFO>: [EPOCH 2] Centroids are almost stable. Iterating
35 <2021-01-02 19:56:48 INFO>: [EPOCH 2] Current SSE: 5.93599494586555; Centroid
  offset: 0.0
36 <2021-01-02 19:56:48 INFO>: Centroid coordinates: [[13.9 14.2 ] [ 3. 5.5 ] [
  3.75 1.75] [ 6.25 6. ]]
37 <2021-01-02 19:56:48 INFO>: K-Means started. K = 5, MAX_EPOCHS = 10
38 <2021-01-02 19:56:48 INFO>: [EPOCH 0] Centroid updated: [[16.6 13.4 ] [10. 12.5 ]
   [ 6. 5.33] [12. 16.67] [ 2.5 2.5 ]]
```

```
39 <2021-01-02 19:56:48 INFO>: [EPOCH 0] Current SSE: 4.53122887111425; Centroid
  offset: 3.8503968049482324
40 <2021-01-02 19:56:49 INFO>: [EPOCH 1] Centroid updated: [[17. 12. ] [10. 12.5]
   [ 6. 5.33] [12.75 17.25] [ 2.5 2.5 ]]
41 <2021-01-02 19:56:49 INFO>: [EPOCH 1] Current SSE: 4.023086665782328; Centroid
   offset: 1.7386137517510254
5.33] [13.33 18. ] [ 2.5 2.5 ]]
43 <2021-01-02 19:56:49 INFO>: [EPOCH 2] Current SSE: 3.9356681049237885; Centroid
   offset: 1.3070322617798442
44 <2021-01-02 19:56:49 INFO>: [EPOCH 3] Centroids are almost stable. Iterating
45 <2021-01-02 19:56:49 INFO>: [EPOCH 3] Current SSE: 3.9356681049237885; Centroid
46 <2021-01-02 19:56:49 INFO>: Centroid coordinates: [[17. 12. ] [10.33 13.33] [ 6.
      5.33] [13.33 18. ] [ 2.5 2.5 ]]
47 <2021-01-02 20:00:27 INFO>: K-Means started. K = 2, MAX_EPOCHS = 10
48 <2021-01-02 20:00:28 INFO>: [EPOCH 0] Centroid updated: [[1.35 1.7 ] [0.8 0.48]]
49 <2021-01-02 20:00:28 INFO>: [EPOCH 0] Current SSE: 9.084632833500144; Centroid
   offset: 1.0783800944922404
50 <2021-01-02 20:00:28 INFO>: [EPOCH 1] Centroid updated: [[1.44 1.7 ] [0.75 0.5 ]]
51 <2021-01-02 20:00:28 INFO>: [EPOCH 1] Current SSE: 8.946377149429686; Centroid
   offset: 0.1007166547161402
52 <2021-01-02 20:00:28 INFO>: [EPOCH 2] Centroid updated: [[1.48 1.66] [0.72 0.51]]
53 <2021-01-02 20:00:28 INFO>: [EPOCH 2] Current SSE: 8.884159078981497; Centroid
   offset: 0.07103114142885013
54 <2021-01-02 20:00:29 INFO>: [EPOCH 3] Centroids are almost stable. Iterating
55 <2021-01-02 20:00:29 INFO>: [EPOCH 3] Current SSE: 8.836643983084578; Centroid
  offset: 0.043257381258992034
56 <2021-01-02 20:00:29 INFO>: Centroid coordinates: [[1.48 1.66] [0.72 0.51]]
57 <2021-01-02 20:00:29 INFO>: K-Means started. K = 3, MAX_EPOCHS = 10
58 <2021-01-02 20:00:29 INFO>: [EPOCH 0] Centroid updated: [[1.09 0.27] [1.36 1.38]
   [0.26 0.89]]
59 <2021-01-02 20:00:29 INFO>: [EPOCH 0] Current SSE: 7.24164583345518; Centroid
   offset: 0.7790249329727592
60 <2021-01-02 20:00:30 INFO>: [EPOCH 1] Centroid updated: [[1.06 0.33] [1.52 1.64]
   [0.36 0.76]]
61 <2021-01-02 20:00:30 INFO>: [EPOCH 1] Current SSE: 6.352441733742936; Centroid
   offset: 0.3493782817722399
62 <2021-01-02 20:00:30 INFO>: [EPOCH 2] Centroid updated: [[1.16 0.36] [1.51 1.71]
   [0.39 0.71]]
63 <2021-01-02 20:00:30 INFO>: [EPOCH 2] Current SSE: 6.296660431436018; Centroid
   offset: 0.1406256889944029
```

```
64 <2021-01-02 20:00:30 INFO>: [EPOCH 3] Centroid updated: [[1.28 0.39] [1.47 1.76] [0.41 0.66]]
```

- 65 <2021-01-02 20:00:30 INFO>: [EPOCH 3] Current SSE: 6.223448294655537; Centroid offset: 0.14565255864462445
- 66 <2021-01-02 20:00:31 INFO>: [EPOCH 4] Centroid updated: [[1.35 0.41] [1.44 1.78] [0.42 0.64]]
- 67 <2021-01-02 20:00:31 INFO>: [EPOCH 4] Current SSE: 6.232771335317366; Centroid offset: 0.08361889313321569
- 68 <2021-01-02 20:00:31 INFO>: [EPOCH 5] Centroid updated: [[1.41 0.46] [1.43 1.81] [0.44 0.62]]
- 69 <2021-01-02 20:00:31 INFO>: [EPOCH 5] Current SSE: 6.231241594598399; Centroid offset: 0.09348551773401224
- 70 <2021-01-02 20:00:31 INFO>: [EPOCH 6] Centroid updated: [[1.48 0.48] [1.4 1.83] [0.48 0.59]]
- 71 <2021-01-02 20:00:31 INFO>: [EPOCH 6] Current SSE: 6.158039505450404; Centroid offset: 0.09843152231474
- 72 <2021-01-02 20:00:32 INFO>: [EPOCH 7] Centroid updated: [[1.65 0.57] [1.34 1.86] [0.52 0.55]]
- 73 <2021-01-02 20:00:32 INFO>: [EPOCH 7] Current SSE: 6.062791253276619; Centroid offset: 0.20894904002053158
- 74 <2021-01-02 20:00:32 INFO>: [EPOCH 8] Centroid updated: [[1.76 0.67] [1.29 1.9] [0.54 0.53]]
- 75 <2021-01-02 20:00:32 INFO>: [EPOCH 8] Current SSE: 5.970752114170463; Centroid offset: 0.1622267864028703
- 76 <2021-01-02 20:00:33 INFO>: [EPOCH 9] Centroid updated: [[1.79 0.72] [1.27 1.92] [0.55 0.53]]
- 77 <2021-01-02 20:00:33 INFO>: [EPOCH 9] Current SSE: 5.957964970912589; Centroid offset: 0.07071241626807692
- 78 <2021-01-02 20:00:33 INFO>: Centroid coordinates: [[1.79 0.72] [1.27 1.92] [0.55 0.53]]
- $79 < 2021-01-02 \ 20:00:33 \ INFO>: K-Means started. K = 4, MAX_EPOCHS = 10$
- 80 <2021-01-02 20:00:33 INFO>: [EPOCH 0] Centroid updated: [[1.28 1.66] [1.35 0.68] [0.22 0.77] [0.87 0.22]]
- 81 <2021-01-02 20:00:33 INFO>: [EPOCH 0] Current SSE: 5.450719950948322; Centroid offset: 1.1258711743598417
- 82 <2021-01-02 20:00:33 INFO>: [EPOCH 1] Centroid updated: [[1.37 1.86] [1.62 0.69] [0.31 0.75] [0.75 0.26]]
- 83 <2021-01-02 20:00:33 INFO>: [EPOCH 1] Current SSE: 4.72262510112004; Centroid offset: 0.39057378065049275
- 84 <2021-01-02 20:00:34 INFO>: [EPOCH 2] Centroid updated: [[1.34 1.92] [1.81 0.72] [0.37 0.81] [0.74 0.3]]
- 85 <2021-01-02 20:00:34 INFO>: [EPOCH 2] Current SSE: 4.653745415605375; Centroid offset: 0.22042674272586063

```
86 <2021-01-02 20:00:34 INFO>: [EPOCH 3] Centroid updated: [[1.32 1.93] [1.86 0.76]
[0.37 0.84] [0.74 0.31]]

87 <2021-01-02 20:00:34 INFO>: [EPOCH 3] Current SSE: 4.66324215468795; Centroid offset: 0.07678847887676
```

- 88 <2021-01-02 20:00:35 INFO>: [EPOCH 4] Centroid updated: [[1.29 1.94] [1.9 0.81] [0.39 0.86] [0.73 0.31]]
- 89 <2021-01-02 20:00:35 INFO>: [EPOCH 4] Current SSE: 4.684047289306287; Centroid offset: 0.07242621504329899
- 90 <2021-01-02 20:00:35 INFO>: [EPOCH 5] Centroid updated: [[1.26 1.96] [1.92 0.85] [0.41 0.87] [0.73 0.31]]
- 91 <2021-01-02 20:00:35 INFO>: [EPOCH 5] Current SSE: 4.702882296202382; Centroid offset: 0.05958200898169935
- 92 <2021-01-02 20:00:35 INFO>: [EPOCH 6] Centroids are almost stable. Iterating stopped.
- 93 <2021-01-02 20:00:35 INFO>: [EPOCH 6] Current SSE: 4.7118083155550705; Centroid offset: 0.04844511252831861
- 94 <2021-01-02 20:00:35 INFO>: Centroid coordinates: [[1.26 1.96] [1.92 0.85] [0.41 0.87] [0.73 0.31]]
- 95 <2021-01-02 20:00:35 INFO>: K-Means started. K = 5, MAX_EPOCHS = 10
- 96 <2021-01-02 20:00:36 INFO>: [EPOCH 0] Centroid updated: [[0.97 0.72] [0.31 1.98] [1.36 1.92] [2.02 0.8] [0.42 0.41]]
- 97 <2021-01-02 20:00:36 INFO>: [EPOCH 0] Current SSE: 3.8977596033449764; Centroid offset: 0.5643413862150298
- 98 <2021-01-02 20:00:36 INFO>: [EPOCH 1] Centroid updated: [[0.99 0.7] [0.47 1.98] [1.57 1.89] [2.06 0.81] [0.43 0.41]]
- 99 <2021-01-02 20:00:36 INFO>: [EPOCH 1] Current SSE: 3.7565910073650803; Centroid offset: 0.2697654559890776
- 100 <2021-01-02 20:00:37 INFO>: [EPOCH 2] Centroid updated: [[1. 0.7] [0.58 2.] [1.75 1.84] [2.06 0.74] [0.42 0.41]]
- 101 <2021-01-02 20:00:37 INFO>: [EPOCH 2] Current SSE: 3.6897836128881876; Centroid offset: 0.22950402065172437
- 102 <2021-01-02 20:00:37 INFO>: [EPOCH 3] Centroid updated: [[1. 0.7] [0.66 1.99] [1.85 1.81] [2.08 0.69] [0.42 0.42]]
- 103 <2021-01-02 20:00:37 INFO>: [EPOCH 3] Current SSE: 3.656776268252373; Centroid offset: 0.14171336542501425
- 104 <2021-01-02 20:00:38 INFO>: [EPOCH 4] Centroids are almost stable. Iterating stopped.
- 105 <2021-01-02 20:00:38 INFO>: [EPOCH 4] Current SSE: 3.654811106661147; Centroid offset: 0.03564353575472734
- 106 <2021-01-02 20:00:38 INFO>: Centroid coordinates: [[1. 0.7] [0.66 1.99] [1.85 1.81] [2.08 0.69] [0.42 0.42]]