

## Database Homework 8

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### 12.1

First run: store first three element into the memory and sort, then next three element. Here I omit the second attribute of each tuples.

```
emu kangaroo wallaby || lion platypus warthog || hyena meerkat zebra || baboon hornbill
```

Second run: merge first two sections and last two sections:

```
emu kangaroo lion platypus wallaby warthog || baboon hornbill hyena meerkat zebra
```

Third run: merge two sections:

```
baboon emu hornibill hyena kangaroo lion meerkat platypus wallaby warthog zebra
```

### 12.2

The relational-algebra expression is shown as follows:

$$\begin{aligned} & \Pi_{T.branch\_name} \left( \Pi_{T.branch\_name, assets} (\rho_T(branch)) \bowtie_{T.assets > S.assets} \right. \\ & \left. \Pi_{assets} (\sigma_{S.branch\_city = "Brooklyn"} (\rho_S(branch))) \right) \end{aligned} \quad (1)$$

### 12.3

By calculating, there're  $20,000 / 25 = 800$  blocks for  $r_1$  and  $45,000 / 30 = 1500$  blocks for  $r_2$ .

Let relation  $r_1$  be the outer loop,  $r_2$  be the inner loop.

| Algorithm              | Block Transfers   | Seeks  |
|------------------------|---|--|
| Nested-loop join       | $800 + 20,000 * 1500 = 30,000,800$  | $800 + 20000 = 20,800$                                   |
| Block nested-loop join | $800 + 800 * 1500 = 1,200,800$ (Worst case, where memory can only store one block each time)<br>$800 + 1500 = 2300$ (Best case, where memory can store all inner relations) | $800 + 800 = 16,00$ (Worst case)<br>2 (Best case)        |
| Merge join             | $800 + 1500 = 2300$   | $\lceil 800/1500 \rceil + \lceil 1500/800 \rceil = 3$    |
| Hash join              | Assume there are n partitions.<br>$2 * (800 + 1500) + 800 + 1500 + 2 * 2 * n = 6900 + 4n$   | $2(\lceil 800/1500 \rceil + \lceil 1500/800 \rceil) = 6$ |

## • 12.10

### - a.

The cost of merge sort is <sup>1</sup> :

$$b_r(2\lceil \log_{M-1}(b_r/M) \rceil + 1) * \text{Block transfer time} + \left(2\lceil b_r/M \rceil + \lceil b_r/b_b \rceil(2\lceil \log_{M-1}(b_r/M) \rceil - 1)\right) * \text{Disk seek time} \quad (2)$$

Cost of a seek:  $5 * 10^{-3}$  s

Cost of a block transfer:  $4\text{KB} / 40(\text{MB/s}) = 1 * 10^{-4}$  s

Block count the memory can hold (M):  $40\text{MB} / 4\text{KB} = 1 * 10^4$

Block count in the relation ( $b_r$ ):  $40\text{GM} / 4\text{KB} = 10^7$

By calculating  $b_r(2\lceil \log_{M-1}(b_r/M) \rceil + 1)$ , the blocks to be transfered =  $3 * 10^7$ .

$$b_b = 1: \text{cost} = (1 * 10^{-4}) * (3 * 10^7) + (5 * 10^{-3}) * (2000 + 10^7 * 1) = 53010 \text{ s}$$

$$b_b = 100: \text{cost} = (1 * 10^{-4}) * (3 * 10^7) + (5 * 10^{-3}) * (2000 + 10^5 * 1) = 3510 \text{ s}$$

### - b.

There will be  $\lceil \log_{M-1}(b_r/M) \rceil$  runs.

When  $b_b = 1$  or  $100$ , the time of merge pass is the same, which  $\approx 1$ .

### - c.

The new cost for a seek:  $1 * 10^{-6}$  s.

$$b_b = 1: \text{cost} = (1 * 10^{-4}) * (3 * 10^7) + (1 * 10^{-6}) * (2000 + 10^7 * 1) = 3010.002\text{s}$$

$$b_b = 100: \text{cost} = (1 * 10^{-4}) * (3 * 10^7) + (1 * 10^{-6}) * (2000 + 10^5 * 1) = 3000.012 \text{ s}$$