



Scientific Computing with Python

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Outline

- Day 1 Basic Python Review
- Introducing Python Modules:
 - Numpy
 - Scipy
- > Examples
 - Calculate derivative of a function
 - Convert RGB image to Grayscale
 - Simple regression example
- > Exercise
 - Numpy warmup exercise





Day 1 Basic Python Recap

- Python is a general-purpose interpreted, interactive, object-oriented, and high-level programming language.
- ➤ It was created by Guido van Rossum during 1985-1990. Like Perl, Python source code is also available under the GNU General Public License (GPL).





Advantage of using Python

Python is:

- Interpreted:
 - Python is processed at runtime by the interpreter. You do not need to compile your program before executing it. This is similar to PERL and PHP.
- Interactive:
 - You can actually sit at a Python prompt and interact with the interpreter directly to write your programs.
- Object-Oriented:
 - Python supports Object-Oriented style or technique of programming that encapsulates code within objects.
- Beginner's Language:
 - Python is a great language for the beginner-level programmers and supports the development of a wide range of applications from simple text processing to browsers to games.





Directly Run into List/Array

```
#!/usr/bin/env python
# generate array from 0-4
a = list(range(5))
print(a)
# len(a)=5
for idx in range(len(a)):
    a[idx] += 5
print(a)
[fchen14@shelob001 python]$ ./loop_array.py
[0, 1, 2, 3, 4]
[5, 6, 7, 8, 9]
```





Python Tuples

A Python tuple is a sequence of immutable Python objects. Creating a tuple is as simple as putting different comma-separated values.

```
#!/usr/bin/env python
tup1 = ('physics', 'chemistry', 1997, 2000);
tup2 = (1, 2, 3, 4, 5);
tup3 = "a", "b", "c", "d";
# The empty tuple is written as two parentheses containing nothing
tup1 = ();
# To write a tuple containing a single value you have to include a comma,
tup1 = (50,);
# Accessing Values in Tuples
print("tup1[0]: ", tup1[0])
print("tup2[1:5]: ", tup2[1:5])
# Updating Tuples, create a new tuple as follows
tup3 = tup1 + tup2;
print(tup3)
# delete tuple elements
del tup3;
print("After deleting tup3 : ")
print(tup3)
```





Scientific Computing using Python

Introducing Numpy





Numpy Overview

- NumPy (Numeric Python) is the core package for scientific computing in Python.
- It is a Python library that provides a multidimensional array object, various derived objects (such as masked arrays and matrices)
- An assortment of routines for fast operations on arrays, including mathematical, logical, shape manipulation, sorting, selecting, I/O, discrete Fourier transforms, basic linear algebra, basic statistical operations, random simulation and much more.
- NumPy package provides basic routines for manipulating large arrays and matrices of numeric data.





Basic Array Operations

- Simple array math using np.array
- Note that NumPy array starts its index from 0, end at N-1 (C-style)

```
# To avoid module name collision inside package context
>>> import numpy as np
>>> a = np.array([1,2,3])
>>> b = np.array([4,5,6])
>>> a+b
array([5, 7, 9])
>>> a*b
array([ 4, 10, 18])
>>> a ** b
array([ 1, 32, 729])
```





Setting Array Element Values

```
>>> a[0]
1
>>> a[0]=11
>>> a
array([11, 2, 3, 4])
>>> a.fill(0) # set all values in the array with 0
>>> a[:]=1 # why we need to use [:]?
>>> a
array([1, 1, 1, 1])
>>> a.dtype # note that a is still int64 type !
dtype('int64')
>>> a[0]=10.6 # decimal parts are truncated, be careful!
>>> a
array([10, 1, 1, 1])
>>> a.fill(-3.7) # fill() will have the same behavior
>>> a
array([-3, -3, -3, -3])
```





Numpy Array Properties (1)

```
>>> a = np.array([0,1,2,3]) # create a from a list
# create evenly spaced values within [start, stop)
>>> a = np.arange(1,5)
>>> a
array([1, 2, 3, 4])
>>> type(a)
<type 'numpy.ndarray'>
>>> a.dtype
dtype('int64')
# Length of one array element in bytes
>>> a.itemsize
8
```





Numpy Array Properties (2)

```
# shape returns a tuple listing the length of the array
# along each dimension.
>>> a.shape # or np.shape(a)
>>> a.size # or np.size(a), return the total number of elements
4
# return the number of bytes used by the data portion of the array
>>> a.nbytes
32
# return the number of dimensions of the array
>>> a.ndim
1
```





Numpy Array Creation Functions (1)

```
# Nearly identical to Python's
                                     # specifying the dimensions of the
range(). Creates an array of values
                                     # array. If dtype is not specified,
in the range [start, stop) with the
                                     # it defaults to float64.
specified step value. Allows non-
                                     >>> a=np.ones((2,3))
integer values for start, stop, and
                                     >>> a
step. Default dtype is derived from
                                     array([[ 1., 1., 1.],
the start, stop, and step values.
                                            [1., 1., 1.]
>>> np.arange(4)
array([0, 1, 2, 3])
                                     >>> a.dtype
>>> np.arange(0, 2*np.pi, np.pi/4) dtype('float64')
array([0., 0.78539816, 1.57079633, >>> a=np.zeros(3)
2.35619449, 3.14159265, 3.92699082, >>> a
4.71238898, 5.49778714])
                                     array([ 0., 0., 0.])
>>> np.arange(1.5,2.1,0.3)
                                     >>> a.dtype
array([1.5, 1.8, 2.1])
                                     dtype('float64')
# ONES, ZEROS
# ones(shape, dtype=float64)
# zeros(shape, dtype=float64)
# shape is a number or sequence
```





Numpy Array Creation Functions (2)

```
# Generate an n by n identity >>> a = np.empty(2)
# array. The default dtype is
# float64.
>>> a = np.identity(4)
>>> a
array([[ 1., 0., 0., 0.],
      [0., 1., 0., 0.], array([5., 5.])
      [ 0., 0., 1., 0.], # alternative approach
      [0., 0., 0., 1.]
>>> a.dtype
dtype('float64')
>>> np.identity(4, dtype=int)
array([[1, 0, 0, 0],
      [0, 1, 0, 0],
      [0, 0, 1, 0],
      [0, 0, 0, 1]
# empty(shape, dtype=float64,
# order='C')
```

```
>>> a
     array([ 0., 0.])
     # fill array with 5.0
     >>> a.fill(5.0)
     >>> a
# (slightly slower)
     >>> a[:] = 4.0
     >>> a
array([ 4., 4.])
```





Numpy Array Creation Functions (3)

```
# Generate N evenly spaced elements between (and including)
# start and stop values.
>>> np.linspace(0,1,5)
array([ 0. , 0.25, 0.5 , 0.75, 1. ])
# Generate N evenly spaced elements on a log scale between
# base**start and base**stop (default base=10).
>>> np.logspace(0,1,5)
array([ 1., 1.77827941, 3.16227766, 5.62341325, 10.])
```





Array from/to ASCII files

- Useful tool for generating array from txt file
 - loadtxt
 - genfromtxt
- Consider the following example:

```
data.txt
Index
Brain Weight
Body Weight
#here is the training set
       3.385 44.500 abjhk
      0.480
               33.38 bc 00asdk
#here is the cross validation set
 6
      27.660 115.000 rk
     14.830 98.200 fff
 9
               58.000 kij
      4.190
```





Using loadtxt and genfromtxt

```
>>> a= np.loadtxt('data.txt',skiprows=16,usecols={0,1,2},dtype=None,comments="#")
>>> a
array([[ 1. , 3.385, 44.5 ],
        2. , 0.48 , 33.38 ],
      [3., 1.35, 8.1],
        4. , 465. , 423. ],
         5. , 36.33 , 119.5 ],
        6., 27.66, 115.],
        7. , 14.83 , 98.2 ],
      [ 8. , 1.04 , 5.5 ],
         9. , 4.19 , 58. ]])
# np.genfromtxt can guess the actual type of your columns by using dtype=None
>>> a= np.genfromtxt('data.txt',skip header=16,dtype=None)
>>> a
array([(1, 3.385, 44.5, 'abjhk'), (2, 0.48, 33.38, 'bc 00asdk'),
      (3, 1.35, 8.1, 'fb'), (4, 465.0, 423.0, 'cer'),
      (5, 36.33, 119.5, 'rg'), (6, 27.66, 115.0, 'rk'),
      (7, 14.83, 98.2, 'fff'), (8, 1.04, 5.5, 'zxs'),
      (9, 4.19, 58.0, 'kij')],
     dtype=[('f0', '<i8'), ('f1', '<f8'), ('f2', '<f8'), ('f3', 'S9')])
```





Reshaping arrays

```
>>> a = np.arange(6)
>>> a
array([0, 1, 2, 3, 4, 5])
>>> a.shape
(6,)
\Rightarrow a.shape = (2,3) # reshape array to 2x3
>>> a
array([[0, 1, 2],
       [3, 4, 5]]
>>> a.reshape(3,2) # reshape array to 3x2
array([[0, 1],
       [2, 3],
       [4, 5]
>>> a.reshape(2,5) # cannot change the number of elements in the array
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
ValueError: total size of new array must be unchanged
>>> a.reshape(2,-1) # numpy determines the last dimension
```





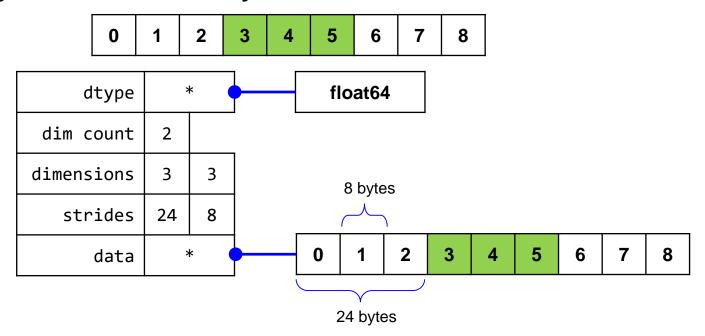
Numpy Array Data Structure

Numpy view of 2D array

```
>>> a=arange(9).reshape(3,-1)
>>> a.strides
(24, 8)
>>> a.ndim
2
```

0	1	2
4	5	6
7	8	9

Memory block of the 2D array







Flattening Multi-dimensional Arrays

```
# Note the difference between
# a.flatten() and a.flat
>>> a
array([[1, 2, 3],
       [4, 5, 6]]
# a.flatten() converts a
# multidimensional array into
# a 1-D array. The new array is a
# copy of the original data.
>>> b = a.flatten()
>>> h
array([1, 2, 3, 4, 5, 6])
>>> b[0] = 7
>>> b
array([7, 2, 3, 4, 5, 6])
>>> a
array([[1, 2, 3],
       [4, 5, 6]]
```

```
# a.flat is an attribute that
# returns an iterator object that
# accesses the data in the multi-
# dimensional array data as a 1-D
# array. It references the original
# memory.
>>> a.flat
<numpy.flatiter object at 0x1421c40>
>>> a.flat[:]
array([1, 2, 3, 4, 5, 6])
>>> b = a.flat
>>> b[0] = 7
>>> a
array([[7, 2, 3],
        [4, 5, 6]]
```





Principle of Using Numpy

- Write code without loops!
 - Easy
 - · Both read and write
 - Fast
 - Why loopless Numpy code is fast?
- How to write loopless code?





Four Tools in Numpy

Removing loops using NumPy

- 1) Ufunc (Universal Function)
- 2) Aggregation
- 3) Broadcasting
- 4) Slicing, masking and fancy indexing





Why Numpy is fast? E.g.:

- Avoid type check overhead
- Vectorization
 - Vectorization (simplified): is the process of rewriting a loop so that instead of processing a single element of an array N times, it processes (say) 4 elements of the array simultaneously N/4 times.
- > Many of the built-in functions are implemented in compiled C code.
 - They can be much faster than the code on the Python level





A Ufunc experiment

Loop version

```
a=list(range(100000))
timeit [val+5 for val in a]
100 loops, best of 3: 4.94 ms per loop
```

Ufunc version

```
a=np.array(a)
timeit a+5
10000 loops, best of 3: 98 μs per loop
```

> Speedup

```
-4.94 \text{ ms} / 98 \mu \text{s} = 50!
```





Ufunc: Math Functions on Numpy Arrays

```
>>> x = np.arange(5.)
>>> X
array([ 0., 1., 2., 3., 4.])
>>> c = np.pi
>>> x *= c
array([ 0. , 3.14159265, 6.28318531, 9.42477796,
12.56637061])
>>> y = np.sin(x)
>>> V
array([ 0.00000000e+00, 1.22464680e-16, -2.44929360e-16,
        3.67394040e-16, -4.89858720e-16])
>>> import math
>>> y = math.sin(x) # must use np.sin to perform array math
Traceback (most recent call last):
 File "<stdin>", line 1, in <module>
TypeError: only length-1 arrays can be converted to Python scalars
```





Ufunc: Many ufuncs available

Arithmetic Operators: + - * / // (floor division) % **
 Bitwise Operators: & | ~ ^ >> <
 Comparison Oper's: < > <= >= == !=
 Trig Family: np.sin, np.cos, np.tan ...
 Exponential Family: np.exp, np.log, np.log10 ...
 Special Functions: scipy.special.*
 ... and many, many more.





Aggregation Functions

- Aggregations are functions which summarize the values in an array (e.g. min, max, sum, mean, etc.)
- Numpy aggregations are much faster than Python built-in functions

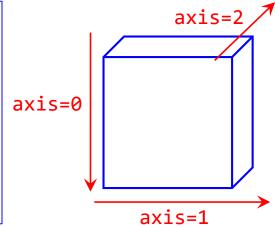


Numpy Aggregation - Array Calculation

```
>>> a=np.arange(6).reshape(2,-1)
>>> a
array([[0, 1, 2],
       [3, 4, 5]]
# by default a.sum() adds up all values array([ 3, 12])
>>> a.sum()
15
# same result, functional form
>>> np.sum(a)
15
# note this is not numpy's sum!
>>> sum(a)
array([3, 5, 7])
# not numpy's sum either!
>>> sum(a,axis=0)
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
TypeError: sum() takes no keyword
arguments
```

```
# sum along different axis
>>> np.sum(a,axis=0)
array([3, 5, 7])
>>> np.sum(a,axis=1)
>>> np.sum(a,axis=-1)
array([ 3, 12])
# product along different axis
>>> np.prod(a,axis=0)
array([ 0, 4, 10])
>>> a.prod(axis=1)
array([ 0, 60])
```

The axes of an array describe the order of indexing into the array, e.g., axis=0 refers to the first index coordinate. axis=1 the second, etc.







Numpy Aggregation – Statistical Methods

```
>>> np.set printoptions(precision=4) # variance
# generate 2x3 random float array >>> np.var(a, axis=1)
>>> a=np.random.random(6).reshape(2,3)
                                        array([ 0.0218, 0.0346])
>>> a
                                        >>> a.min()
array([[ 0.7639, 0.6408, 0.9969],
                                        0.17118969968007625
       [ 0.5546, 0.5764, 0.1712]]) >>> np.max(a)
>>> a.mean(axis=0)
                                        0.99691892655137737
array([ 0.6592, 0.6086, 0.5841])
                                       # find index of the minimum
>>> a.mean()
                                        >>> a.argmin(axis=0)
0.61730865425015347
                                        array([1, 1, 1])
>>> np.mean(a)
                                        >>> np.argmax(a,axis=1)
0.61730865425015347
                                        array([2, 1])
                                        # this will return flattened index
# average can use weights
>>> np.average(a,weights=[1,2,3],axis=1) >>> np.argmin(a)
array([ 0.8394, 0.3702])
# standard deviation
                                        >>> a.argmax()
>>> a.std(axis=0)
array([ 0.1046, 0.0322, 0.4129])
```





Numpy's Aggregation - Summary

All have the same call style.

```
- np.min() np.max() np.sum() np.prod()
- np.argsort()
- np.mean() np.std() np.var() np.any()
- np.all() np.median() np.percentile()
- np.argmin() np.argmax() . . .
- np.nanmin() np.nanmax() np.nansum(). . .
```





Array Broadcasting

- Broadcasting is a set of rules by which ufuncs operate on arrays of different sizes and/or dimensions.
- > Broadcasting allows NumPy arrays of different dimensionality to be combined in the same expression.
- Arrays with smaller dimension are broadcasted to match the larger arrays, without copying data.

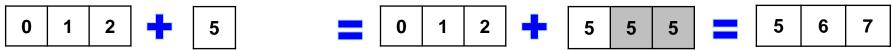




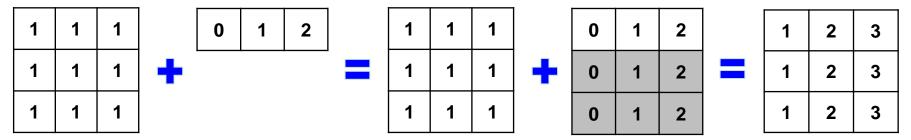
Broadcasting Rules

- 1. If array shapes differ, left-pad the smaller shape with 1s
- 2. If any dimension does not match, broadcast the dimension with size=1
- 3. If neither non-matching dimension is 1, raise an error.

$$np.arange(3) + 5$$



np.ones((3,3)) + np.arange(3)



np.arange(3).reshape(3,1) + np.arange(3)

0		0	1	2	0	0	0		0	1	2	0	1	2
1	+				1	1	1	+	0	1	2	1	2	3
2					2	2	2		0	1	2	2	3	4





Broadcasting Rules – 1D array

$$np.arange(3) + 5$$

0	1	2



- 1. If array shapes differ, left-pad the smaller shape with 1s
 - 1) shape=(3,) shape=()
 - 2) shape=(3,) shape=(1,)
 - 3) shape=(3,) shape=(3,)
 - 4) final shape=(3,)
- 2. If any dimension does not match, broadcast the dimension with size=1
- 3. If neither non-matching dimension is 1, raise an error.

0	1	2	+	5	5	5	=	5	6	7
	•	-	•	•		•				•





Broadcasting Rules – 2D array (1)

np.o	np.ones((3,3)) + np.arange(3)										
1	1	1		0	1	2		1	2	3	
1	1	1	+	0	1	2		1	2	3	
1	1	1		0	1	2		1	2	3	

- 1) shape=(3,3) shape=(3,)
 2) shape=(3,3) shape=(1,3)
 3) shape=(3,3) shape=(3,3)
- final shape=(3,3)
- 1. If array shapes differ, left-pad the smaller shape with 1s
- 2. If any dimension does not match, broadcast the dimension with size=1
- 3. If neither non-matching dimension is 1, raise an error.





Broadcasting Rules – 2D array (2)

np.arrange(3).reshape(3,1) + np.arange(3)

0	0	0		0	1	2	0	1	2
1	1	1	+	0	1	2	1	2	3
2	2	2		0	1	2	2	3	4

- 1) shape=(3,1) shape=(3)
- 2) shape=(3,1) shape=(1,3)
- 3) shape=(3,3) shape=(3,3)

final shape=(3,3)

- 1. If array shapes differ, left-pad the smaller shape with 1s
- 2. If any dimension does not match, broadcast the dimension with size=1
- 3. If neither non-matching dimension is 1, raise an error.





Broadcasting Rules – Error

➤ The trailing axes of either arrays must be 1 or both must have the same size for broadcasting to occur. Otherwise, a "ValueError: operands could not be broadcast together with shapes" exception is thrown.

```
>>> a=np.arange(6).reshape(3,2)
                                                      mismatch!
>>> a
array([[0, 1],
                                              3x2
       [2, 3],
       [4, 5]]
                                              0
>>> b=np.arange(3)
>>> h
                                              2
                                                  3
array([0, 1, 2])
>>> a+b
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
ValueError: operands could not be broadcast together with shapes (3,2) (3,)
```



Slicing, Masking and Fancy Indexing

See next few slides...





Array Slicing (1)

- arr[lower:upper:step]
- Extracts a portion of a sequence by specifying a lower and upper bound. The lower-bound element is included, but the upper-bound element is not included. Mathematically: [lower, upper). The step value specifies the stride between elements.

```
# indices: 0 1 2 3 4
# negative indices:-5 -4 -3 -2 -1
>>> a = np.array([10,11,12,13,14])
# The following slicing results are the same
>>> a[1:3]
array([11, 12])
>>> a[1:-2]
array([11, 12])
>>> a[-4:3]
array([11, 12])
```





Array Slicing (2)

Omitting Indices: omitted boundaries are assumed to be the beginning or end of the list, compare the following results

```
>>> a[:3] # first 3 elements
array([10, 11, 12])
>>> a[-2:] # last 2 elements
array([13, 14])
>>> a[1:] # from 1st element to the last
array([11, 12, 13, 14])
>>> a[:-1] # from 1st to the second to last
array([10, 11, 12, 13])
>>> a[:] # entire array
array([10, 11, 12, 13, 14])
>>> a[::2] # from 1st, every other element (even indices)
array([10, 12, 14])
>>> a[1::2] # from 2nd, every other element (odd indices)
array([11, 13])
```





Multidimensional Arrays

> A few 2D operations similar to the 1D operations shown above

```
>>> a = np.array([[ 0, 1, 2, 3],[10,11,12,13]], float)
>>> a
array([[ 0., 1., 2., 3.],
      [ 10., 11., 12., 13.]])
>>> a.shape # shape = (rows, columns)
(2, 4)
>>> a.size # total elements in the array
8
>>> a.ndim # number of dimensions
2
>>> a[1,3] # reference a 2D array element
13
>>> a[1,3] = -1 \# set value of an array element
>>> a[1] # address second row using a single index
array([10., 11., 12., -1.])
```





2D Array Slicing

```
\Rightarrow a = np.arange(1,26)
>>> a = a.reshape(5,5) # generate the 2D array
\Rightarrow \Rightarrow a[0,3:5]
array([4, 5])
\Rightarrow \Rightarrow a[0,3:4]
array([4])
>>> a[4:,4:]
array([[25]])
>>> a[3:,3:]
array([[19, 20],
        [24, 25]])
>>> a[:,2]
array([ 3, 8, 13, 18, 23])
>>> a[2::2,::2]
array([[11, 13, 15],
        [21, 23, 25]])
```

1	2	3	4	5	
6	7	8	9	10	
11	12	13	14	15	
16	17	18	19	20	
21	22	23	24	25	
	11 16	6 7 11 12 16 17	6 7 8 11 12 13 16 17 18	6 7 8 9 11 12 13 14 16 17 18 19	6 7 8 9 10 11 12 13 14 15 16 17 18 19 20





Slices Are References

- Slices are references to memory in the original array
- Changing values in a slice also changes the original array!

```
>>> a = np.arange(5)
>>> a
array([0, 1, 2, 3, 4])
>>> b = a[2:4]
>>> b
array([2, 3])
>>> b[0]=7
>>> a
array([0, 1, 7, 3, 4])
```





Masking

```
>>> a=np.arange(10)
>>> a
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
                                                     3
                                                               6
                                                                     8
# creation of mask using ufunc
>>> mask=np.abs(a-5)>2
                                     mask
>>> mask
array([ True, True, True, False, False, False, False, True,
True], dtype=bool)
>>> a[mask]
                                     mask
array([0, 1, 2, 8, 9])
>>> mask=np.array([0,1,0,1],dtype=bool)
# manual creation of mask
>>> mask
array([False, True, False, True], dtype=bool)
>>> a[mask]
array([1, 3])
```





Masking and where

```
\Rightarrow a=np.arange(8)**2
>>> a
array([ 0, 1, 4, 9, 16, 25, 36, 49])
>>> mask=np.abs(a-9)>5
>>> mask
array([ True, True, False, False, True, True, True],
dtype=bool)
# find the locations in array where expression is true
>>> np.where(mask)
(array([0, 1, 4, 5, 6, 7]),)
>>> loc=np.where(mask)
>>> a[loc]
array([ 0, 1, 16, 25, 36, 49])
```





Masking in 2D

```
>>> a=np.arange(25).reshape(5,5)+10
>>> a
array([[10, 11, 12, 13, 14],
       [15, 16, 17, 18, 19],
       [20, 21, 22, 23, 24],
       [25, 26, 27, 28, 29],
       [30, 31, 32, 33, 34]])
>>> mask=np.array([0,1,1,0,1],dtype=bool)
>>> a[mask] # on rows, same as a[mask,:]
array([[15, 16, 17, 18, 19],
       [20, 21, 22, 23, 24],
       [30, 31, 32, 33, 34]])
>>> a[:,mask] # on columns
array([[11, 12, 14],
                                        a[mask]
       [16, 17, 19],
       [21, 22, 24],
       [26, 27, 29],
       [31, 32, 34]])
```

a[:,mask]

0 1	1	0	1
-----	---	---	---

10	11	12	13	14
15	16	17	18	19
20	21	22	23	24
25	26	27	28	29
30	31	32	33	34





Fancy Indexing - 1D

- NumPy offers more indexing facilities than regular Python sequences.
- In addition to indexing by integers and slices, arrays can be indexed by arrays of integers and arrays of Booleans (as seen before).

```
\Rightarrow a=np.arange(8)**2
>>> a
array([ 0, 1, 4, 9, 16, 25, 36, 49])
# indexing by position
>>> i=np.array([1,3,5,1])
>>> a[i]
array([ 1, 9, 25, 1])
>>> b=(np.arange(6)**2).reshape(2,-1)
>>> b
array([[ 0, 1, 4],
       [ 9, 16, 25]])
\Rightarrow \Rightarrow i = [0,1,0]
>>> j=[0,2,1]
>>> b[i,j] # indexing 2D array by position
array([ 0, 25, 1])
```





Fancy Indexing - 2D

```
>>> b=(np.arange(12)**2).reshape(3,-1)
>>> b
array([[ 0, 1, 4, 9],
       [ 16, 25, 36, 49],
       [ 64, 81, 100, 121]])
\Rightarrow i = [0, 2, 1]
>>> j=[0,2,3]
# indexing 2D array
>>> b[i,j]
array([ 0, 100, 49])
# note the shape of the resulting array
>>> i=[[0,2],[2,1]]
>>> j=[[0,3],[3,1]]
# When an array of indices is used,
# the result has the same shape as the indices;
>>> b[i,j]
array([[ 0, 121],
       [121, 25]]
```

idx	0	1	2	3
0	0	1	4	9
1	16	25	36	49
2	64	81	100	121





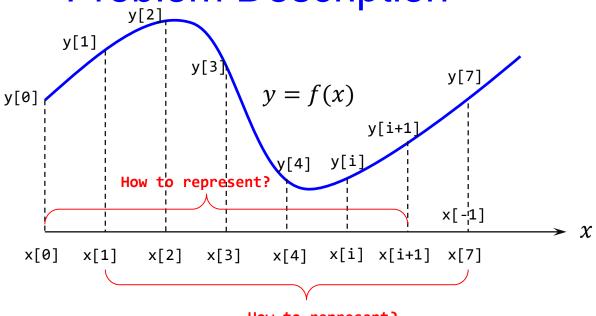
Scientific Computing with Python

Calculate Derivative





Problem Description



How to represent?

Numerical Derivative and Integration:

$$y' = \frac{dy}{dx} \approx \frac{\Delta y}{\Delta x} = \frac{y_{i+1} - y_i}{x_{i+1} - x_i}$$

$$\int_{a}^{b} f(x)dx = \sum_{i=1}^{N} \frac{1}{2} (y_{i} + y_{i+1}) \cdot \Delta x$$
y[1]-y[0]

y[1] y[2] y[3] y[4]

y[0] y[1] y[2] y[3]

y[1]-y[0] y[2]-y[1] y[3]-y[2] y[4]-y[3]

► How to get a vector of Δy and Δx ?





Calculate Derivative - Solution

Using Numpy slicing:

```
import numpy as np
import matplotlib.pyplot as plt
# calculate the sin() function on evenly spaced data.
x = np.linspace(0, 2*np.pi, 101)
y = np.sin(x)
# use slicing to get dy and dx
dy=y[1:]-y[:-1]
dx=x[1:]-x[:-1]
dy dx = dy/dx
```





Scientific Computing with Python

Change RGB Image to Grayscale





Using Numpy to Process Image

- RGB to Grayscale Conversion:
 - Using simple average

$$V_{Gray} = (V_{Red} + V_{Green} + V_{Blue})/3$$

Using weighted average (https://en.wikipedia.org/wiki/Grayscale

$$V_{Gray} = 0.299V_{Red} + 0.587V_{Green} + 0.114V_{Blue}$$

Loading and Displaying Images





Load Image

```
# import necessary images
import numpy as np
from scipy.misc import imread, imresize
import matplotlib.pyplot as plt
# To load an image, we use imread method from scipy's misc modules:
img = imread('cat.jpg')
print img.shape
                                                            axis=2
Shape of the loaded image in ipython:
In [2]: imread('cat.jpg')
Out[2]:
                                             axis=0
array([[132, 128, 117],
       [155, 151, 139],
       [181, 175, 161],
       [ 91, 76, 57],
       [89, 74, 55],
                                                         axis=1
       [ 86, 71, 50]]], dtype=uint8)
```





Averaging The RGB Channel Values

```
# This is simple average along axis=2
# img tinted = np.average(img,axis=2)
# This is weighted average along axis=2
img tinted = np.average(img, weights=[0.299, 0.587, 0.114], axis=2)
print img_tinted.shape
print img.shape
# plot the original image on the left
                                         plt.subplot(1, 2, 1)
plt.imshow(img)
# plot the grayscale image on the left
                                            100
plt.subplot((1, 2, 2))
                                            150
plt.imshow(np.uint8(img_tinted)
                                            200
    cmap='gray')
                                            250
                                                           250
plt.show()
                                            350
```





Scientific Computing with Python

Introducing Scipy





Numerical Methods with Scipy

- Scipy package (SClentific PYthon) provides a multitude of numerical algorithms built on Numpy data structures
- Organized into subpackages covering different scientific computing areas
- A data-processing and prototyping environment almost rivaling MATLAB





Major modules from scipy

Available sub-packages include:

- constants: physical constants and conversion factors
- cluster: hierarchical clustering, vector quantization, K-means
- integrate: numerical integration routines
- interpolate: interpolation tools
- io: data input and output
- linalg: linear algebra routines
- ndimage: various functions for multi-dimensional image processing
- optimize: optimization algorithms including linear programming
- signal: signal processing tools
- sparse: sparse matrix and related algorithms
- spatial: KD-trees, nearest neighbors, distance functions
- special: special functions
- stats: statistical functions
- weave: tool for writing C/C++ code as Python multiline strings





Scipy Example: Integration

$$\int_{1}^{3} x^{2} dx = \frac{1}{3} x^{3} \Big|_{1}^{3}$$

```
#!/usr/bin/env python
import scipy.integrate as integrate
import scipy.special as special
result_integ, err = integrate.quad(lambda x: x**2, 1, 3)
result_real = 1./3.*(3.**3-1**3)

print "result_real=", result_real
print "result_integ=", result_integ
```





Scipy Example: Regression

```
#!/usr/bin/env python

from scipy import stats
import numpy as np
import matplotlib.pyplot as plt
```

```
x = np.array([1, 2, 5, 7, 10, 15])
y = np.array([2, 6, 7, 9, 14, 19])
slope, intercept, r_value, p_value, std_err = stats.linregress(x,y)

plt.plot(x,y,'or')
yh = x*slope + intercept
plt.plot(x, yh, '-b')
plt.show()
```

```
♠ ○ ○ | ← ☞ | ❷ 圖 ✓
```