44. Wildcard Matching

Recursion

String

Problem Description

<u>Greedy</u>

Hard

characters. We need to determine if the pattern p matches the entire string s. The wildcard characters are defined as follows: A question mark ('?') matches any single character. • An asterisk ('*') matches any sequence of characters, including an empty sequence.

The problem is a classic example of pattern matching where we are given a string s and a pattern p that includes wildcard

The goal is to check if there is a complete match between the entire string and the pattern, not just a partial match.

into smaller subproblems and then build up the solution from these.

Dynamic Programming

Intuition

For solving this problem, dynamic programming is a common approach because it allows us to break down the complex problem

If the current character in the pattern is a ? or matches the current character in the string, we refer to previous states where the match has been progressing without the current character and pattern.

If the current character in the pattern is a *, it can be complex because * can match an empty sequence or any sequence of

characters. We need to consider multiple cases: either we use the * to match zero characters in the string (which means we

The key insight is to realize that we can make a decision at each character in the string based on two conditions:

look at the state of the match without the *), or we use the * to match at least one character in the string (which means we look at the state of the match without the current character in the string, but keep the *).

This method of breaking down the problem helps us to derive a solution using a 2D matrix dp where dp[i][j] represents

whether the first i characters of the string s can be matched with the first j characters of the pattern p. The final answer at

dp[m][n] (where m and n are the lengths of the string and pattern respectively) gives us the answer to whether the entire string matches the pattern. By filling up the matrix by iterating over the string and the pattern, we use the previously solved subproblems to inform the solution of the current subproblem. Eventually, we derive the solution to the entire problem.

The solution uses dynamic programming, a method where complex problems are broken into simpler subproblems and solved individually, with the solutions to the subproblems stored to avoid redundant calculations. Here is a breakdown of the implementation steps:

Initialize a 2D matrix dp with dimensions $(m + 1) \times (n + 1)$, where m is the length of the string s and n is the length of the

pattern p. Each element dp[i][j] in this matrix will store a boolean value indicating if s[0..i-1] matches p[0..j-1]. The

Pre-fill the first row of the matrix by setting dp[0][j] to True if p[j-1] is * and dp[0][j-1] is also True. This loop accounts

+1 offset allows us to easily handle the empty string and pattern cases. Set the first element dp[0][0] to True to represent that an empty string matches an empty pattern.

```python

initialization.

elif p[j - 1] == '\*':

**Solution Approach** 

for j in range(1, n + 1): if p[i - 1] == '\*': dp[0][j] = dp[0][j - 1]

Iterate through the matrix starting from i = 1 and j = 1, and calculate the dp[i][j] value based on the following rules:

If the current character of s[i - 1] matches the current character of p[j - 1] or p[j - 1] is a ? (which can match any

for the situation where the pattern starts with one or multiple \* characters, which can match the empty string.

- single character), then set dp[i][j] to the value of dp[i 1][j 1] since we can carry forward the match status from previous characters.
- dp[i][j] = dp[i 1][j 1]

```
If the current character of the pattern is *, there are two possibilities:
 ■ The * matches zero characters: carry forward the status from dp[i][j - 1].
 ■ The * matches one or more characters: carry forward the status from dp[i - 1][j].
Hence:
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from exponential (which would be the case with a naive recursive approach) to polynomial time. **Example Walkthrough** 

This approach ensures that each subproblem is only calculated once and then reused, dramatically reducing the time complexity

Initialize the 2D matrix dp: Since s has a length of 6 and p has a length of 5, our matrix dp will be a 7×6 matrix (including

• For all other cases where characters don't match and there is no wildcard, dp[i][j] will remain False, which is the default value after

After filling the entire matrix, the value at dp[m][n] will indicate whether the entire string s matches the pattern p.

First row pre-fill: We then iterate over the first row of dp to account for a pattern that starts with \*. In this case, p[0] is \*, so dp[0][1] should be set to True. Following that logic, here's how the first row will look after pre-filling:

the extra row and column for the empty string and pattern case). Initially, all values in dp are set to False.

First element dp[0][0]: We set dp[0][0] to True to denote that an empty pattern matches an empty string.

#### a. For i = 1 and j = 1, the pattern has \* which matches zero characters from s. So, dp[1][1] is True because dp[0][0]was true.

**Iterate and fill the matrix:** 

F

F

X

а

a

b

**Pytnon** 

Java

C++

public:

#include <vector>

#include <string>

class Solution {

// characters of p.

dp[0][0] = true;

// Fill the DP table.

class Solution {

class Solution:

b. When j = 2 and i = 1, the pattern is a but our string is x. Since they don't match and the pattern is not a ?, dp[1][2] stays False.

F

def isMatch(self, string: str, pattern: str) -> bool:

length\_s, length\_p = len(string), len(pattern)

# Create a DP table with default values False

# The empty pattern matches the empty string

for j in range(1, length p + 1):

for i in range(1, length s + 1):

return dp[length\_s][length\_p]

if pattern[i - 1] == '\*':

dp[0][j] = dp[0][j - 1]

for i in range(1, length p + 1):

public boolean isMatch(String str, String pattern) {

// Lengths of the input string and the pattern

int strLen = str.length(), patternLen = pattern.length();

// The value in the bottom right corner will be our answer

bool isMatch(const std::string& s, const std::string& p) {

// Create a DP table with dimensions  $(m+1) \times (n+1)$  initialized to false.

// dp[i][i] will be true if the first i characters of s match the first j

// Initialize the first row of the DP table. If we find '\*', it can match

// If the characters match or the pattern character is '?',

// If the pattern character is '\*', it can either match zero characters,

// meaning we transition from dp[i][i-1], or it can match one character,

// we can transition from the state dp[i-1][i-1].

if  $(s[i-1] == p[i-1] || p[i-1] == '?') {$ 

dp[i][j] = dp[i][j - 1] || dp[i - 1][j];

// The final state dp[m][n] gives us the answer to whether the entire

std::vector<std::vector<bool>> dp(strSize + 1, std::vector<bool>(patternSize + 1, false));

int strSize = s.size(), patternSize = p.size();

// The empty pattern matches the empty string.

for (int j = 1; j <= patternSize; ++j) {</pre>

dp[0][j] = dp[0][j - 1];

for (int i = 1; i <= strSize; ++i) {</pre>

if (p[i - 1] == '\*') {

// an empty string, which is the state of dp[0][j-1].

for (int i = 1; i <= patternSize; ++i) {</pre>

else if (p[i - 1] == '\*') {

// strings s and p match with each other.

return dp[strSize][patternSize];

function isMatch(s: string, p: string): boolean {

let strLen: number = s.length;

dp[i][j] = dp[i - 1][j - 1];

// meaning we transition from dp[i-1][j].

return dp[strLen][patternLen];

// dp[i][i] will be true if the first i characters in given string

# Get the lengths of the input string and the pattern

dp = [[False] \* (length\_p + 1) for \_ in range(length\_s + 1)]

# Initialize first row of the DP table, considering the pattern starting with '\*'

if string[i - 1] == pattern[j - 1] or pattern[j - 1] == '?':

dp[i][j] = dp[i - 1][j] or dp[i][j - 1]

# Return the value at the bottom-right corner of the DP table

if s[i-1] == p[i-1] or p[i-1] == '?':

dp[i][j] = dp[i - 1][j] or dp[i][j - 1]

Let's illustrate the solution approach using a small example:

Assume s = "xaabyc" and p = "\*a?b\*".

- c. Eventually, by following the iteration rules while filling out the matrix, we will have:

```
matches the pattern p.
 By processing the dp matrix according to the dynamic programming approach, we've avoided redundant calculations and
 determined the match between s and p efficiently.
Solution Implementation
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dp[0][0] = True

# Fill the DP table

dp[i][i] = dp[i - 1][i - 1]# If pattern has '\*', we check two cases: # 1. '\*' matches no character: move left in the table # 2. '\*' matches at least one character: move up in the table elif pattern[i - 1] == '\*':

# If characters match or pattern has '?', we can move back diagonally in the table (match found)

Final Check: Our final cell dp[6][5] contains True. Therefore, we can deduce that with the given example, the string s

```
// match the first i characters of the pattern
boolean[][] dp = new boolean[strLen + 1][patternLen + 1];
// Empty string and empty pattern are a match
dp[0][0] = true;
// Initialize the first row for the cases where pattern contains st
// as they can match the empty string
for (int i = 1; i <= patternLen; ++i) {</pre>
 if (pattern.charAt(j - 1) == '*') {
 dp[0][j] = dp[0][j - 1];
// Build the dp matrix in bottom-up manner
for (int i = 1; i <= strLen; ++i) {</pre>
 for (int i = 1; i <= patternLen; ++i) {</pre>
 // If the current characters match or pattern has '?',
 // we can propagate the diagonal value
 if (str.charAt(i - 1) == pattern.charAt(j - 1) || pattern.charAt(j - 1) == '?') {
 dp[i][j] = dp[i - 1][j - 1];
 // If pattern contains '*', it can either match zero characters
 // in the string or it can match one character in the string
 // and continue matching
 else if (pattern.charAt(i - 1) == '*') {
 dp[i][j] = dp[i - 1][j] || dp[i][j - 1];
 // If the current pattern character is not a wildcard and the characters
 // don't match, dp[i][j] remains false, which is the default value.
```

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let patternLen: number = p.length;
// Create a DP table with dimensions (strLen+1) x (patternLen+1) initialized to false.
// dp[i][i] will be true if the first i characters of s match the first j characters of p.
let dp: boolean[][] = Array.from({ length: strLen + 1 },
```

**}**;

**TypeScript** 

// The empty pattern matches the empty string. dp[0][0] = true;// Initialize the first row of the DP table. If we find '\*', it can match // an empty string, thereby adopting the value from dp[0][j-1]. for (let j = 1; j <= patternLen; j++) {</pre> if (p[i - 1] === '\*') { dp[0][j] = dp[0][j - 1];// Fill the DP table. for (let i = 1; i <= strLen; i++) {</pre> for (let i = 1;  $i \le patternLen$ ; i++) { // If the characters match or the pattern character is '?', // we can transition from the state dp[i-1][i-1]. if  $(s[i-1] === p[i-1] || p[i-1] === '?') {$ dp[i][j] = dp[i - 1][j - 1];// If the pattern character is '\*', it can either match zero characters, // meaning we transition from dp[i][i-1], or it can match one or more characters, // meaning we transition from dp[i-1][j]. else if (p[i - 1] === '\*') { dp[i][j] = dp[i][j - 1] || dp[i - 1][j];// The final state dp[strLen][patternLen] gives us the answer to whether the entire // strings s and p match with each other. return dp[strLen][patternLen]; class Solution: def isMatch(self, string: str, pattern: str) -> bool: # Get the lengths of the input string and the pattern length\_s, length\_p = len(string), len(pattern) # Create a DP table with default values False dp = [[False] \* (length\_p + 1) for \_ in range(length\_s + 1)] # The empty pattern matches the empty string dp[0][0] = True# Initialize first row of the DP table, considering the pattern starting with '\*' for j in range(1, length p + 1): if pattern[i - 1] == '\*': dp[0][j] = dp[0][j - 1]

() => Array<boolean>(patternLen + 1).fill(false));

### Time and Space Complexity The time complexity of the provided code is 0(m \* n), where m is the length of the string s and n is the length of the pattern p. This is because the code involves a nested loop structure that iterates through the lengths of s and p. Each cell in the DP table

# Fill the DP table

for i in range(1, length s + 1):

return dp[length\_s][length\_p]

for i in range(1, length p + 1):

elif pattern[i - 1] == '\*':

dp[i][i] = dp[i - 1][i - 1]

# If pattern has '\*', we check two cases:

dp[i][j] computes whether the first i characters of s match the first j characters of p, and the computation of each cell is constant time. The space complexity of the code is also 0(m \* n). This is due to the use of a two-dimensional list dp, which has (m + 1) \* (n + 1)elements, to store the states of substring matches. Each element of this list represents a subproblem, with extra rows and columns to handle empty strings.

# If characters match or pattern has '?', we can move back diagonally in the table (match found)

if string[i - 1] == pattern[i - 1] or pattern[j - 1] == '?':

# 2. '\*' matches at least one character: move up in the table

# 1. '\*' matches no character: move left in the table

dp[i][j] = dp[i - 1][j] or dp[i][j - 1]

# Return the value at the bottom-right corner of the DP table