2439. Minimize Maximum of Array Binary Search Medium Greedy Array Dynamic Programming Prefix Sum Leetcode Link

# Problem Description In this problem, you are given an array nums with n non-negative integers. The focus is on the array's integers' transformation through

a series of operations to minimize the value of the maximum integer in the array. Each operation includes three steps: Select an integer i where i is between 1 and n-1 (inclusive), and nums [i] is greater than 0.

- 2. Decrease nums [i] by 1.
- 3. Increase nums[i 1] by 1.

operations. Intuition

The objective is to find out the smallest possible value of the largest number in the array after performing any number of these

The intuition behind the solution is to use binary search to find the minimum possible value of the maximum integer in the array after all the operations. Since we are asked for the minimum possible maximum value, we can guess that there is some maximum value

that we cannot go below no matter how many operations we perform. We perform binary search between the lowest possible maximum value, which is 0, and the current maximum value in the array. For each guess (possible maximum value) in the binary search, we check if we can achieve that maximum value after performing the

operations. Here's the step-by-step reasoning: 1. Start with a binary search between 0 and the maximum value present in the array nums. Calculate the middle value between the current range as our guess for the possible maximum value.

- 4. In the check function, we work backwards from the end of the array towards the beginning (right to left). For each element, we
- calculate the surplus or deficit compared to our guessed maximum and carry this difference to the previous element.
- 5. The conditions that tell us if we can achieve the guessed maximum are: If at any point the required decrease is so great we cannot make up the difference with the carried surplus, the check fails.

3. Define a check function that will determine if it is possible to achieve the guessed maximum value with the array.

element does not exceed our guessed maximum. 6. If the check function returns true, it means we can achieve the guessed maximum or even lower, so we continue searching towards the lower half of the binary search range.

7. If the check function returns false, the guessed maximum is too low, and we have to adjust our range towards the higher values.

If we can carry the difference through to the first element, we then check if the total sum of increases needed for the first

condition (the left and right pointers converge). The solution uses the fact that after all possible optimizations, the array nums will become non-decreasing from the beginning to the

8. Repeat this process until the binary search narrows down to the smallest possible maximum integer value that satisfies the

end. This is because the maximum possible number in an optimal solution cannot be less than the average of the numbers in the array. Thus, binary search optimizes the process by eliminating the need to test each value sequentially.

The solution utilizes a binary search algorithm to narrow down the possible maximum value that can be achieved in the array after performing the operations. Here's an in-depth walkthrough of the algorithm, elaborating on the reference solution provided: 1. Binary Search Initialization: Define two pointers, left and right, which represent the range within which the final answer could

be. Initialize left to 0, assuming the minimum possible value in the array could be 0 after all operations, and initialize right to

# the maximum value in nums, which is the upper limit of the answer.

Solution Approach

2. Binary Search Loop: While left is less than right, calculate the middle of the current left and right boundary, mid = (left + right) >> 1. (>> 1 is a bitwise operation equivalent to dividing by 2, shifting the bits to the right once.)

allowed operations. It works as follows: Initialize a d variable to 0, which represents the cumulative difference needed to reach the guessed maximum mx from the end of the array.

3. Check Function: The check function is defined to test whether a certain maximum value mx can be attained after performing the

larger than mx, we need to 'push' some of its value to its left neighbor. Finally, add d to the first element nums [0] and check if it still does not exceed mx. If it does not, return True; otherwise, False.

4. Binary Search Logic: Use the result of the check function inside the binary search loop. If check(mid) returns True, the current

guess can be achieved, and perhaps a lower maximum value is possible, so we update right to mid. Conversely, if check(mid)

returns False, we must increase our guess and move the lower boundary up, setting left to mid + 1.

∘ Iterate in reverse (from the last element to the second, hence nums [:0:-1]) to calculate d. At each step, update d by adding

the difference between the current element x and mx only if that difference is positive. In other words, if the element x is

5. Binary Search Conclusion: The binary search concludes when left equals right, indicating that the search range has been narrowed down to a single element—this element is the minimum possible maximal value that can be achieved in the nums array after performing any number of operations. This solution effectively combines binary search with a greedy strategy in the check function to ensure that all potential operations

are taken into account from right to left, simulating the effect that the operations would have on an array and determining the

viability of a selected maximum value. The use of binary search drastically reduces the number of checks needed compared to a linear search and finds the optimal solution efficiently. Example Walkthrough

1. Initialize our binary search range with left = 0 and right = max(nums) = 8. 2. Conduct a binary search. The first mid value will be (0 + 8) / 2 = 4. 3. Run the check function with mx = 4:

Assume we have an array nums = [3, 1, 5, 6, 8, 7] with n = 6 non-negative integers. We need to minimize the value of the maximum

mid + 1, which is 5.

given problem.

Python Solution

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def is\_valid(max\_value):

additional = 0

right = max(nums)

while left < right:

if is\_valid(mid):

for num in nums[:-1][::-1]:

mid = (left + right) // 2

integer in the array after performing our operations.

Start iterating from the end:

nums [4] = 8, d += 8 - 4 = 7 (total d becomes 10) • nums [3] = 6, d += 6 - 4 = 12 (total d becomes 12) nums [2] = 5, d += 5 - 4 = 13 (total d becomes 13)

5. With a new search range left = 5 and right = 8, we calculate a new mid value of (5 + 8) / 2 = 6 and repeat the check function.

Now, adding the total d (13) to nums [0] which is 3, we have 3 + 13 = 16, which is greater than mx = 4, so our check function

returns False. 4. Since the check function returned False, we can't attain a maximum with 4. We adjust our binary search range, setting left to

• nums [5] = 7, d += 7 - 4 = 3 (since 7 is greater than 4)

nums [1] does not contribute since 1 is not greater than 4

6. When we finally find the smallest mid for which the check function returns True, we have found the smallest possible value of the largest number in the array after performing the operations. For this example, let's assume through the binary search process, we find that the smallest maximum we can achieve is 5.

We keep iterating this process until we find the mid value for which the check function returns True.

# 'additional' keeps track of the value that needs to be distributed

# Check if the first element plus the distributable amount is less than

int maxValue = nums[0]; // Initialize with the first element of the array

// Iterate over the array to find the maximal value

maxValue = Math.max(maxValue, num);

return maxValue; // Return the found maximum

int minimizeArrayValue(std::vector<int>& nums) {

// by distributing values from right to left

auto canDistribute = [&](int maxValue) {

int minPossibleValue = 0;

long excess = 0;

// Initialize the search range for the minimum possible max value

// Define a lambda function to check if a given max value is possible

// Perform a binary search to find the minimum max value that satisfies

// If it doesn't work, we need to try a higher value

let mid: number = Math.floor((minPossibleValue + maxPossibleValue) / 2);

// The minPossibleValue will point to the smallest max value that works, so return it

// If the current midway value works, try to see if we can lower it

// Iterate over the array from the end to start (excluding the first element)

int maxPossibleValue = \*max\_element(nums.begin(), nums.end());

for (int num : nums) {

# Maximum possible value in the original array

# If the mid value is a valid maximum, we try to see if there's a smaller maximum.

# Iterating backwards to check if it's possible to reduce

additional = max(0, additional + num - max\_value)

# Minimum possible value

# to achieve the max\_value in the nums array.

# all values to at most max\_value by distribution.

# Perform binary search to find the minimum maximum value.

class Solution: def minimizeArrayValue(self, nums: List[int]) -> int: # Function to check if a given maximum value can be achieved # by distributing the values across the nums array.

7. The solution approach successfully minimizes the maximum value in the array with the optimal use of operations detailed in the

# or equal to the maximum value after distribution. 15 return nums[0] + additional <= max\_value 16 17 # Binary search to find the minimum possible maximum value in the array 18 19 # after redistribution.

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                   right = mid
               # If the mid value is not valid, we search for a larger value that might be valid.
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               else:
                    left = mid + 1
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           # The binary search loop exits when left == right, which is the minimum maximum value.
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left = 0

return left

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Java Solution
    class Solution {
         private int[] nums; // Array to store the input numbers
         // Method to find the minimum possible max value of the array after modifications
         public int minimizeArrayValue(int[] nums) {
             this.nums = nums; // Initialize the global array with the input array
  6
             int left = 0; // Start of the search range
             int right = findMaxValue(nums); // End of the search range, which is the max value in nums
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             // Binary search to find the minimum possible value
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             while (left < right) {</pre>
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                 int mid = (left + right) / 2; // Middle value of the current search range
 12
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                 if (canBeMinimizedTo(mid)) {
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                     right = mid; // If can minimize to `mid`, continue search on the left half
 15
                 } else {
 16
                     left = mid + 1; // Otherwise, search on the right half
 17
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             return left; // The minimum possible max value after minimization
 21
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         // Method to check if we can minimize the array to a certain max value
 24
         private boolean canBeMinimizedTo(int maxVal) {
 25
             long deficit = 0; // Tracks the required decrease to achieve maxVal
 26
             // Iterate backward through the array
 27
             for (int i = nums.length - 1; i > 0; --i) {
 28
                 // Accumulate the deficit from the end of the array to the start
                 deficit = Math.max(0, deficit + nums[i] - maxVal);
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             // Check if we can minimize the first element with the accumulated deficit
 32
             return nums[0] + deficit <= maxVal;</pre>
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         // Helper method to find the maximum value in an array
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         private int findMaxValue(int[] nums) {
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# for (int $i = nums.size() - 1; i > 0; --i) {$ 16 // Calculate the excess that needs to be distributed to the left 17 excess = std::max(0l, excess + nums[i] - maxValue); 18 19 // The first element plus any excess should not exceed the max value 20

C++ Solution

1 #include <vector>

class Solution {

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#include <algorithm>

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return nums[0] + excess <= maxValue;</pre>
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           };
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           // Perform a binary search to find the minimum max value that satisfies
           // the distribution criteria
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           while (minPossibleValue < maxPossibleValue) {</pre>
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                int mid = (minPossibleValue + maxPossibleValue) / 2;
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29
               // If the current midway value works, try to see if we can lower it
30
               if (canDistribute(mid))
                   maxPossibleValue = mid;
31
32
               // If it doesn't work, we need to try a higher value
33
               else
34
                   minPossibleValue = mid + 1;
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36
37
           // The left pointer will point to the smallest max value that works, so return it
           return minPossibleValue;
39
40 };
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Typescript Solution
    // TypeScript code equivalent of the provided C++ code
    // Import array related utilities
    import { max } from 'lodash';
    // Define a method to minimize the array value
     function minimizeArrayValue(nums: number[]): number {
         // Initialize the search range for the minimum possible max value
         let minPossibleValue: number = 0;
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         let maxPossibleValue: number = max(nums) as number;
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         // Define a lambda function to check if a given max value is possible
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 13
         // by distributing values from right to left
         const canDistribute = (maxValue: number): boolean => {
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 15
             let excess: number = 0;
 16
             // Iterate over the array from the end to start (excluding the first element)
 17
             for (let i: number = nums.length - 1; i > 0; --i) {
                 // Calculate the excess that needs to be distributed to the left
 18
                 // If positive, add it to the current excess, otherwise keep the current excess
 19
 20
                 excess = Math.max(0, excess + nums[i] - maxValue);
 21
 22
             // The first element plus any excess should not exceed the max value
 23
             return nums[0] + excess <= maxValue;</pre>
 24
         };
```

Time and Space Complexity

return minPossibleValue;

// the distribution criteria

if (canDistribute(mid)) {

maxPossibleValue = mid;

minPossibleValue = mid + 1;

operation. Here's the analysis of its time and space complexity:

while (minPossibleValue < maxPossibleValue) {</pre>

44 // Example usage: // const nums: number[] = [10, 20, 30]; // const minimizedValue: number = minimizeArrayValue(nums); // console.log(minimizedValue); // Output will vary based on function implementation

The given code implements a binary search algorithm to minimize the maximum value in the array after applying the specified

# The while loop in the code is running a binary search over the range 0 to max(nums), which has at most log(max(nums)) iterations

since we're halving the search space in every step. The check function is called inside the loop and it iterates through the array in reverse, which takes O(n) time. Therefore, the time complexity of the code is O(n \* log(max(nums))).

**Space Complexity:** 

**Time Complexity:** 

The space complexity of the code is 0(1). The algorithm uses a constant number of variables (d, mx, left, right, mid) and the space occupied by these does not depend on the size of the input array nums. The function check also does not use any additional space that scales with the size of the input, as it works in place.