## 1150. Check If a Number Is Majority Element in a Sorted Array

**Binary Search** Array Easy

## **Problem Description**

Given an integer array nums which is sorted in non-decreasing order, and an integer target, the task is to determine whether target is a "majority" element in <a href="majority">nums</a>. A majority element is one that appears more than <a href="majority">nums</a>. length / 2 times. The function should return true if target is indeed a majority element, and false otherwise.

Intuition

search to quickly find the first and last occurrences of the target element. In Python, this can be efficiently done using the bisect\_left and bisect\_right functions from the bisect module. • bisect\_left returns the index of the first occurrence of target in nums (or the index where target would be inserted to maintain the sorted

The intuition behind the solution comes from the property of the array being sorted in non-decreasing order. We can use binary

- order if it's not present). • bisect\_right returns the index of the first element greater than target (which would be one past the last occurrence of target if target is in nums).
- By subtracting the index returned by bisect\_left from the index returned by bisect\_right, we get the total number of times

target appears in nums. If this number is greater than nums.length / 2, then target is a majority element, and we return true. If not, we return false. Using binary search makes the solution very efficient even for large arrays, since we avoid scanning the whole array and operate

Solution Approach

The solution uses a binary search approach to find the first and last occurrences of the target element in the sorted array. The

### binary search algorithm is a well-known method that operates by repeatedly dividing the search interval in half. If the value of the search key is less than the item in the middle of the interval, narrow the interval to the lower half; otherwise, reduce it to the

with a time complexity of O(log n).

Here's how the bisect\_left and bisect\_right functions contribute to the solution: bisect\_left(nums, target): This line of code uses the bisect\_left function from Python's bisect module. Given the sorted array nums, it finds the leftmost position at which target should be inserted in order to maintain the sorted order. If

target is already in nums, bisect\_left will return the index of the first occurrence of target. This is effectively the start

bisect\_right(nums, target): Similarly, bisect\_right finds the rightmost position to insert target while keeping the array

sorted. If target exists in the array, bisect\_right will return the index directly after the last occurrence of target. This is

index of target in the array.

upper half. Repeatedly checking in this manner until the value is found or the interval is empty.

- essentially the index at which target would no longer appear in the array. With the indices from bisect\_left and bisect\_right, the code calculates the number of times target appears in the array by subtracting the left index from the right index (right - left). This gives us the total count of target in nums.
- To determine if target is a majority element, the code compares the count of target with half of the array's length (len(nums)) // 2). The integer division by two ensures that we have a threshold which target's count must exceed to be considered a majority element. If the count is greater than this threshold, the function returns true; otherwise, it returns false.

The data structure used here is the list <a href="mailto:nums">nums</a>, and the algorithm implemented is <a href="mailto:binary search">binary search</a> through the use of <a href="mailto:bisect\_left">bisect\_left</a>

and bisect\_right. No additional data structures are necessary. This approach is efficient because it minimizes the number of

elements inspected, and the binary search is performed in O(log n) time complexity, where n is the number of elements in nums. **Example Walkthrough** 

Let's consider a small example to illustrate the solution approach. Suppose we have the array nums and the target given as follows: nums = [1, 2, 2, 3, 3, 3, 3]target = 3

### The array nums is sorted, and we want to determine whether 3 is a majority element. The majority element must appear more

element. Let's apply the binary search approach using the bisect\_left and bisect\_right functions from the bisect module:

than len(nums) / 2 = 7 / 2 = 3.5 times. Since the array length is 7, the target must appear more than 3 times to be a majority

```
Find the left index for the target 3 using bisect_left:
from bisect import bisect left
```

This indicates that the first occurrence of 3 in the array nums is at index 3. Find the right index for the target 3 using bisect\_right:

right\_index = bisect\_right(nums, target) # right\_index is 7

is\_majority = count > len(nums) // 2 # is\_majority is True

count = right\_index - left\_index # count is 4

from bisect import bisect right

left\_index = bisect\_left(nums, target) # left\_index is 3

```
The variable count now holds the total number of times target appears in nums, and in this case, it is 4.
Finally, check if count is greater than len(nums) / 2 to determine if target is a majority element:
```

So, using this binary search approach, we have determined that the target element 3 is a majority element in the array with minimal computation compared to traversing the entire array. The example validates the solution's ability to efficiently solve the

# Check if the count of `target` in the list is greater than half the length of the list.

# This is done by comparing the difference between `right index` and `left index`, which

# gives the number of occurrences of `target`, to half the length of the list.

// Check if the count of the target value is more than half of the array's length

// Function to check if the target is the majority element in the sorted array

// Helper function to find the first occurrence of a value using binary search

// Check if the count of 'target' is more than half the size of the vector

// This function determines if a given target is the majority element in a sorted array.

bool isMajority = count > nums.size() / 2;

// index of a given number (x) in the sorted array.

const binarySearch = (x: number): number => {

let rightIndex = nums.length;

while (leftIndex < rightIndex) {</pre>

if (nums[midIndex] >= x) {

rightIndex = midIndex;

leftIndex = midIndex + 1;

// Perform a binary search.

function isMajorityElement(nums: number[], target: number): boolean {

// Helper function that performs a binary search to find the start

return isMajority;

let leftIndex = 0;

} else {

Since 4 is greater than 3.5, we can confirm that 3 is indeed a majority element in the array nums.

This suggests that the index directly after the last appearance of 3 in the array nums is 7.

Now we calculate the total count of target by subtracting the left index from the right index:

def isMajorityElement(self, nums: List[int], target: int) -> bool: # Find the leftmost index where `target` should be inserted to keep the list sorted. left\_index = bisect\_left(nums, target) # Find the rightmost index where `target` should be inserted to keep the list sorted. right\_index = bisect\_right(nums, target)

### public boolean isMajoritvElement(int[] nums, int target) { // Find the start index of the target value int startIndex = findFirstOccurrence(nums, target); // Find the start index of the value immediately after the target

int left = 0;

given problem.

**Python** 

Java

class Solution {

class Solution:

Solution Implementation

from bisect import bisect\_left, bisect\_right

return right\_index - left\_index > len(nums) // 2

int endIndex = findFirstOccurrence(nums, target + 1);

return (endIndex - startIndex) > nums.length / 2;

private int findFirstOccurrence(int[] nums, int value) {

```
int right = nums.length;
        while (left < right) {</pre>
            // Compute the middle index
            int mid = left + (right - left) / 2;
            // Narrow down to the left half if the middle element is greater than or equal to the value
            if (nums[mid] >= value) {
                right = mid;
            } else {
                // Otherwise, narrow down to the right half
                left = mid + 1;
        // Return the starting index where the target value would be or is located
        return left;
C++
#include <vector>
#include <algorithm> // Required for std::lower_bound and std::upper_bound
class Solution {
public:
    bool isMajorityElement(vector<int>& nums, int target) {
        // Use lower bound to find the first occurrence of 'target'
        auto firstOccurrence = std::lower_bound(nums.begin(), nums.end(), target);
        // Use upper bound to find the position immediately after the last occurrence of 'target'
        auto lastOccurrence = std::upper_bound(nums.begin(), nums.end(), target);
        // Calculate the number of times 'target' appears in the vector
        int count = lastOccurrence - firstOccurrence;
```

**TypeScript** 

```
return leftIndex;
    };
    // Using the helper function to find the first occurrence of the target.
    const firstTargetIndex = binarySearch(target);
    // Finding the first index past the last occurrence of the target
    // using the next number (target + 1).
    const firstIndexPastTarget = binarySearch(target + 1);
    // Determine if the target is the majority element by comparing the
    // number of occurrences to more than half the size of the array.
    return firstIndexPastTarget - firstTargetIndex > nums.length >> 1; // Equivalent to Math.floor(nums.length / 2)
from bisect import bisect_left, bisect_right
class Solution:
    def isMajorityElement(self, nums: List[int], target: int) -> bool:
        # Find the leftmost index where `target` should be inserted to keep the list sorted.
        left_index = bisect_left(nums, target)
        # Find the rightmost index where `target` should be inserted to keep the list sorted.
        right_index = bisect_right(nums, target)
        # Check if the count of `target` in the list is greater than half the length of the list.
        # This is done by comparing the difference between `right index` and `left index`, which
        # gives the number of occurrences of `target`, to half the length of the list.
        return right_index - left_index > len(nums) // 2
Time and Space Complexity
Time Complexity
  The time complexity of the provided code is determined by the functions bisect_left and bisect_right from Python's bisect
```

let midIndex = (leftIndex + rightIndex) >> 1; // Equivalent to Math.floor((leftIndex + rightIndex) / 2)

# module. Both functions perform binary search to find the leftmost and rightmost positions of target in the sorted array nums,

respectively.

The binary search algorithm has a time complexity of O(log n), where n is the number of elements in the array. Since the code performs two binary searches, one for bisect\_left and one for bisect\_right, the total time complexity is:

This simplifies to  $O(\log n)$  because the constants are dropped in Big O notation.

# **Space Complexity**

 $2 * 0(\log n) = 0(\log n)$ 

The space complexity of the code is 0(1) since it uses only a fixed amount of extra space. The variables left and right are used to store the indices found by the binary search, and no additional data structures are created that depend on the size of the input array nums. Therefore, the space requirements of the algorithm do not scale with the input size.