198. House Robber **Dynamic Programming** Medium Array

Problem Description

In this problem, you take on the role of a professional burglar who is aiming to rob houses lined up along a street. Every house has some money, but there's a twist: the houses are equipped with connected security systems. If you rob two adjacent houses on the same night, the security system will detect the break-ins and alert the police. Your goal is to figure out the maximum amount of money you can steal tonight without triggering any alarms.

So, you're presented with an array of integers nums, where nums [i] represents the amount of money stashed in the i-th house. The challenge is to find the optimal combination of houses to rob that will maximize your total loot, keeping in mind that you

cannot rob adjacent houses. It's a classic optimization problem that requires you to look for the best strategy to maximize your gains without breaking the constraint (the alarm system in this case).

To get to the heart of this problem, let's discuss the intuition behind the solution. The main idea here is dynamic programming, which involves breaking the problem down into smaller subproblems and building up

a solution from the answers to those subproblems.

dynamic programming solutions, and calculates the result in a bottom-up manner.

Now, consider the following choices at each house: either you rob it or you don't. If you decide to rob house i, you cannot rob house i-1, but you are free to rob house i-2 and before. If you decide not to rob house i, your best robbery amount up to house

i is the same as if you were standing at house i-1. Let's define two variables: f and g. We'll use f to track the maximum amount we can rob up to the current house if we don't rob

this house, and g to track the maximum amount if we do rob it.

We update f like this: We take the max between the previous f (not robbing the previous house) and g (robbing the previous house) because for the current house, we are not robbing it, so we are free to choose the maximum loot collected from the

On the other hand, we update g by adding the current house's money to the previous f, because if we decide to rob this house,

Lastly, we have to return the maximum amount we can rob including or excluding the last house, which means we return the max between f and g.

we can't rob the previous one, so we add to f (the max money robbed without including the previous house).

Solution Approach

The solution uses a dynamic programming approach, which is a method for solving complex problems by breaking them down

variables to store the results since we move through the nums array sequentially and only require information from the previous

Initialize two variables, f and g. f represents the maximum amount of money that can be robbed up to the current house

The elegance of this solution lies in its simplicity and the fact that it takes advantage of overlapping subproblems, typical in

into simpler subproblems. It computes solutions to these subproblems just once and stores their results—typically in an array—to avoid the need for redundant calculations. However, in this particular problem, we don't even need an array; we only use two

Here's a step-by-step explanation of the code that was provided:

f = max(f, g)

g = f + x

houses.

step.

previous two states.

f = g = 0Iterate over each amount x in the nums array representing the money at each house. for x in nums:

Within the for loop, this updates f and g at each house while maintaining the condition that we never rob two adjacent

It's important to note that f and g are being used to keep the space complexity of the solution at O(1), meaning it doesn't require

any extra space proportional to the input size. This algorithm overall has O(n) time complexity since it requires one pass through

In conclusion, the implementation keeps track of two possibilities at each house (to rob or not to rob) and makes decisions that

of is updated to the maximum of the previous f or g. This makes f the maximum amount of money we could have if we chose not to rob this

Update the values of f and g for each house:

the nums array, where n is the number of elements in the array.

without robbing it, and g represents the maximum amount with robbing it.

og is updated by adding the current house's stash x to the previous non-robbed maximum f. This is because if we rob the current house, we must skip the previous one, hence we add to the previous f.

house (i). We can use the maximum from the previous state since robbing the current house is out of the question.

- After the loop ends, the maximum amount of money that can be robbed will be the maximum of f and g. return max(f, g)
- ensure the highest amount of money robbed without ever triggering the alarm system.

Here's the step-by-step walkthrough: Initialize f and g to 0. These variables will hold the maximum money that can be robbed so far without and with robbing the

∘ For the first house (nums [0] = 2), we can only rob it since there's no previous house. Therefore, f remains 0 as we are not robbing this

To illustrate the solution approach, let's use a small example where the nums array representing money at each house is [2, 7, 9,

house, and g is updated to f + nums[0], which is also 2. Move to the second house (nums[1] = 7):

robbed is 12.

For the fifth house:

not robbing two adjacent houses.

def rob(self, nums: List[int]) -> int:

robbed without adjacent thefts:

prev_no_rob, prev_robbed = 0, 0

for current_house_value in nums:

the previous house or robbing it.

the previous one was not robbed.

temp = max(prev_no_rob, prev_robbed)

int temp = max(previous, beforePrevious);

// Update previous to the amount stored in temp

// The new robPrevious becomes the maximum of either

the previous house or robbing it.

the previous one was not robbed.

temp = max(prev_no_rob, prev_robbed)

prev_robbed = prev_no_rob + current_house_value

// robPrevious or robCurrent from the previous iteration.

beforePrevious = previous + num;

return max(previous, beforePrevious);

previous = temp;

prev_robbed = prev_no_rob + current_house_value

Iterate over all the houses

prev_no_rob = temp

int prevRob = 0;

was not robbed or if it was.

return max(prev_no_rob, prev_robbed)

Solution Implementation

• f remains 11, and

Python

current house, respectively.

Start iterating over the array nums.

At the fourth house (nums[3] = 3):

Example Walkthrough

3, 1].

At the third house (nums[2] = 9): Update f to max(2, 9), so f is now 9.

The loop has finished, and we now take the maximum of f and g. Both f and g are 12, so the maximum money that can be

If we map out the houses we chose to rob based on g's updates, we robbed the second and fourth houses - a total of 7 + 3 =

 Update f to max(9, 11), so f is now 11. Update g to f (previous f before updating which is 9) + nums[3], which is 9 + 3, so g is 12. Finally, at the fifth house (nums [4] = 1):

• f remains 11 since we're not adding the value of the current house.

• g doesn't change since we can't rob this house directly after the third house.

Update g to f + nums[1], which is 2 + 7, so g becomes 9.

 Update f to max(11, 12), so f is now 12. • Update g to f (previous f before updating which is 11) + nums[4], which is 11 + 1, so g becomes 12.

• Update g to f (previous f before updating which is 2) + nums[2], which is 2 + 9, so g is 11.

Update f to max(f, g), which was from the previous iteration. Here f becomes max(0, 2) so f is now 2.

10, and not the third and fifth as the walk through suggests. Let's correct the steps for the fourth and fifth houses. For the fourth house, since we can't rob it (because we robbed the third house):

• g is updated with 11 + 1 (the previous f plus the current house's value), resulting in g being 12.

Initialize two variables to store the maximum amount of money that can be

prev_no_rob denotes the max amount considering the previous house wasn't robbed

prev_robbed denotes the max amount considering the previous house was robbed

Calculate the new value for prev_no_rob by choosing the max between

The value for prev_robbed is updated to the sum of prev_no_rob and

prev_no_rob and prev_robbed. This is because if the current house is not

being robbed, then the maximum amount is the best of either not robbing

the value of the current house, as we can only rob the current house if

Return the max amount that can be robbed - either the amount if the last house

// g represents the max profit we can get if we rob the current house

In this case, we robbed the third and fifth houses (2nd house was not actually robbed), getting a total of 9 + 1 = 10. Hence, the final maximum amount we could rob is 12, updating our final g with the amount from the fifth house and maintaining the rule of

from typing import List class Solution:

```
class Solution {
   public int rob(int[] nums) {
       // f represents the max profit we can get from the previous house
       int prevNoRob = 0;
```

Java

```
// Iterate over all the houses in the array
        for (int currentHouseValue : nums) {
            // Store max profit of robbing/not robbing the previous house
            int tempPrevNoRob = Math.max(prevNoRob, prevRob);
           // If we rob the current house, we cannot rob the previous one
            // hence our current profit is previous house's no-rob profit + current house value
            prevRob = prevNoRob + currentHouseValue;
            // Update the previous no-rob profit to be the best of robbing or not robbing the last house
            prevNoRob = tempPrevNoRob;
       // Return the max profit we can get from the last house,
       // regardless of whether we rob it or not
       return Math.max(prevNoRob, prevRob);
C++
#include <vector>
#include <algorithm> // For std::max
class Solution {
public:
    // Function to calculate the maximum amount of money that can be robbed
    int rob(vector<int>& nums) {
       // Initialize previous and beforePrevious to store the max rob amounts
       // at two adjacent houses we may potentially skip or rob
       int previous = 0, beforePrevious = 0;
       // Loop through each house represented in the nums vector
        for (int num : nums) {
            // Temporarily hold the maximum amount robbed so far
```

```
};
TypeScript
// Function to determine the maximum amount of money that can be robbed
// without robbing two adjacent houses.
function rob(nums: number[]): number {
   // Initialize two variables:
    // robPrevious - the maximum amount robbed up to the previous house
   // robCurrent — the maximum amount robbed up to the current house
    let [robPrevious, robCurrent] = [0, 0];
    for (const currentHouseValue of nums) {
       // Compute the new maximum excluding and including the current house:
```

// robCurrent is updated with the sum of robPrevious (excludes the previous house)

// and the value of the current house, representing the choice to rob this house.

prev_no_rob and prev_robbed. This is because if the current house is not

being robbed, then the maximum amount is the best of either not robbing

the value of the current house, as we can only rob the current house if

Return the max amount that can be robbed — either the amount if the last house

The value for prev_robbed is updated to the sum of prev_no_rob and

// Update beforePrevious to the new amount robbed including the current house

// which is the maximum of previous and beforePrevious after considering all houses

// Return the maximum amount that can be robbed without alerting the police

```
// Return the maximum amount robbed between the last two houses considered
      return Math.max(robPrevious, robCurrent);
from typing import List
class Solution:
   def rob(self, nums: List[int]) -> int:
       # Initialize two variables to store the maximum amount of money that can be
       # robbed without adjacent thefts:
       # prev_no_rob denotes the max amount considering the previous house wasn't robbed
       # prev_robbed denotes the max amount considering the previous house was robbed
        prev_no_rob, prev_robbed = 0, 0
       # Iterate over all the houses
        for current_house_value in nums:
           # Calculate the new value for prev_no_rob by choosing the max between
```

[robPrevious, robCurrent] = [Math.max(robPrevious, robCurrent), robPrevious + currentHouseValue];

Time and Space Complexity **Time Complexity**

prev_no_rob = temp

was not robbed or if it was.

return max(prev_no_rob, prev_robbed)

The given code consists of a single for-loop that iterates through every element in the input list nums. Inside this loop, the calculations involve simple arithmetic operations and a single max function call which both have a constant time complexity (0(1)).

Since these operations are performed once for each element in the list, the time complexity is directly proportional to the length of the list. Thus, the time complexity of the code is O(n), where n is the number of elements in nums. **Space Complexity**

The algorithm uses two variables (f and g) to keep track of the calculations at each step. No additional data structures that grow with the input size are used. This means that the space complexity is not dependent on the size of the input and is, therefore, constant. Hence, the space complexity of the code is 0(1).