

# 1846. Maximum Element After Decreasing and Rearranging

MediumGreedyArraySorting

Leetcode Link

## Problem Description

The problem presents an array of positive integers named `arr`. The objective is to apply certain operations to modify the array so that it meets the following criteria:

- The first element of the array should be `1`.
- The absolute difference between any two consecutive elements in the array should be less than or equal to `1`. That is, for each `i` (where `i` ranges from `1` to `arr.length - 1`), we have  $|arr[i] - arr[i - 1]| \leq 1$ , with  $|x|$  representing the absolute value of `x`.

We are allowed to perform two types of operations as many times as needed:

- Decrease the value of any element to a lower positive integer.
- Rearrange the elements in any order.

The goal is to return the maximum possible value of an element in `arr` after performing these operations to satisfy the given conditions.

## Intuition

The intuition behind the solution is based on the understanding that in order to minimize the absolute differences between adjacent elements, it makes sense to sort the array in non-decreasing order. Once sorted, the elements of the array should form a sequence where each element is either the same or 1 greater than its predecessor.

Here is the approach we can follow to arrive at a solution:

- Sort the array in non-decreasing order. This is because rearranging the elements can only help if they are sorted, which ensures that no two adjacent elements have an absolute difference greater than allowed after the operations.
- Set the first element of `arr` to `1`, since that's a mandatory requirement.
- Loop through the array starting from the second element. For each `i` from `1` to `arr.length - 1`, we need to ensure the absolute difference condition  $|arr[i] - arr[i - 1]| \leq 1$ . The best way to achieve this without violating the array's non-decreasing order is to check if `arr[i]` is more than `arr[i - 1] + 1` and if so, decrease it to `arr[i - 1] + 1`. This keeps the sequence in order and satisfies the adjacent element condition.
- After completing this process, the last element in the array would hold the maximum value possible while satisfying the required conditions.

The code provided gives us a straightforward implementation of this approach.

## Solution Approach

The provided solution utilizes a simple sorting-based approach with a single pass modification after sorting. Here's how the implementation works in detail:

### Algorithm:

- Sorting:** The first step is to sort the array `arr` in non-decreasing order. This is done with `arr.sort()`. Sorting is critical because it places elements in a sequence that makes it easier to minimize absolute differences between consecutive elements.
- Setting First Element:** Per the problem requirements, the first element must be set to `1`, so without considering its previous value, we directly assign `arr[0] = 1`.
- Loop Through Elements:** We then iterate over the array, starting from the second element (index `1`), since the first element is already set to `1`. For each element `arr[i]`, we want to ensure that it is not more than `1` greater than the previous element `arr[i - 1]`.

This is done by calculating the difference `d` between `arr[i]` and `arr[i - 1] + 1` and then checking if this is greater than `0`. If it is, it means that `arr[i]` is too large and needs to be reduced. The element `arr[i]` is then decreased by `d`, ensuring that the current element `arr[i]` is either equal to or one more than `arr[i - 1]`.

- Returning Result:** After the loop concludes, the array now satisfies all the given conditions. Since the array elements have been sorted and then properly adjusted, the maximum value that adheres to the constraints is located at the end of the array. Hence, `max(arr)` returns the maximum value from `arr`.

### Data Structures and Patterns:

- Array/Sorting:** The solution uses the given array `arr` as the primary data structure. No additional complex data structures are needed.
- The sorting algorithm used by Python's `sort()` function fundamentally determines the overall efficiency of this approach.**
- Iterative Loop:** An iterative loop is utilized to adjust the values of `arr` after the initial sort. This reduces the algorithm's complexity as it avoids recursive calls or additional passes through the array.
- In-Place Modifications:** All operations are performed in place, which means no additional arrays are created during the modification of `arr`. This is efficient both in terms of space and time.

### Computational Complexity:

- Time Complexity:**  $O(n \log n)$ , where `n` is the number of elements in `arr`. Sorting the array is the most computationally expensive operation in the provided solution.
- Space Complexity:**  $O(1)$ , as we are operating in-place and not using extra space that is dependent on the input size.

This implementation yields the desired result by sorting the array, adjusting its values while maintaining sorted order, and finally, retrieving the maximum possible element value.

## Example Walkthrough

Let's walk through a small example to illustrate the solution approach:

Given the input array `arr = [4, 7, 2]`, we want to modify it following our operation rules so that the first element is `1` and the absolute difference between consecutive elements is at most `1`. We will demonstrate each step of the algorithm with this array.

- Sorting:** First, we sort the array in non-decreasing order. Sort the array: `arr = [2, 4, 7]`.
- Setting First Element:** Next, we must set the first element to `1` to satisfy the problem's conditions. Set the first element: `arr = [1, 4, 7]`.
- Loop Through Elements:** Now, we start at the second element and iterate through the array to ensure the absolute difference between consecutive elements is at most `1`.
  - For the second element (`arr[1]`), the previous element is `1`, so the second element should not be greater than `2`. The value of `4` is too high, so we decrease it: `arr = [1, 2, 7]`.
  - For the third element (`arr[2]`), the previous element is `2`, so the third element should not be greater than `3`. The value of `7` is too high, so we decrease it: `arr = [1, 2, 3]`.
- Returning Result:** After modifying the array, the maximum value while satisfying the conditions is the last element. Return the max value: `max(arr) = 3`.

By following the steps above, we have successfully modified the original array `[4, 7, 2]` to `[1, 2, 3]` meeting the conditions that:

- The first element is `1`.
- Each element is at most `1` greater than the previous one.

Finally, we returned `3` as the maximum possible value after performing the allowed operations. The sorted array `arr` now satisfies the criteria, and no elements are more than `1` apart consecutively.

## Python Solution

```
1 from typing import List
2
3 class Solution:
4     def maximumElementAfterDecrementingAndRearranging(self, arr: List[int]) -> int:
5         # First, sort the array to make it easier to apply the decrementing rule.
6         arr.sort()
7
8         # The first element must be set to 1 according to the problem constraints.
9         arr[0] = 1
10
11         # Iterate over the sorted array starting from the second element.
12         for i in range(1, len(arr)):
13             # Calculate the maximum decrement for the current element so that
14             # it is not greater than the preceding element plus one.
15             decrement_value = max(0, arr[i] - arr[i - 1] - 1)
16
17             # Apply the calculated decrement to ensure each element is at most
18             # 1 greater than the previous element.
19             arr[i] -= decrement_value
20
21         # Return the last element in the modified array, which is the maximum.
22         return arr[-1] # Use -1 to access the last element for clarity.
23
```

## Java Solution

```
1 class Solution {
2
3     public int maximumElementAfterDecrementingAndRearranging(int[] arr) {
4
5         // Step 1: Sort the input array to check the difference between consecutive elements
6         Arrays.sort(arr);
7
8         // Step 2: The first element should be 1 as per problem's constraint
9         arr[0] = 1;
10
11         // Initialize the answer with the first element's value
12         int maximumElement = 1;
13
14         // Step 3: Iteratively check each element starting from the second one
15         for (int i = 1; i < arr.length; ++i) {
16
17             // Calculate the amount by which we can decrement the current element
18             // to ensure it's not more than 1 greater than its predecessor
19             // Ensure that we do not decrement the value into negatives by using Math.max with 0
20             int decrement = Math.max(0, arr[i] - arr[i - 1] - 1);
21
22             // Decrement the current element
23             arr[i] -= decrement;
24
25             // Update the maximumElement if current is greater
26             maximumElement = Math.max(maximumElement, arr[i]);
27         }
28
29         // Step 4: Return the highest value found which satisfies the given conditions
30         return maximumElement;
31     }
32 }
33
```

## C++ Solution

```
1 class Solution {
2 public:
3     int maximumElementAfterDecrementingAndRearranging(vector<int>& arr) {
4         // Step 1: Sort the array in non-decreasing order
5         sort(arr.begin(), arr.end());
6
7         // Step 2: The first element should be set to 1 according to the problem statement
8         arr[0] = 1;
9
10        // Initialize the answer with the first element's value
11        int maximumElement = 1;
12
13        // Step 3: Iterate over the sorted array starting from the second element
14        for (int i = 1; i < arr.size(); ++i) {
15            // Determine the maximum decrement needed to maintain non-decreasing order
16            // It should not be negative, hence max with 0
17            int decrement = max(0, arr[i] - arr[i - 1] - 1);
18
19            // Decrease the current element to make the sequence non-decreasing if needed
20            arr[i] -= decrement;
21
22            // Update the maximum element encountered so far
23            maximumElement = max(maximumElement, arr[i]);
24        }
25
26        // Return the largest possible element after performing the operations
27        return maximumElement;
28    }
29 };
30
```

## Typescript Solution

```
1 function maximumElementAfterDecrementingAndRearranging(arr: number[]): number {
2     // Sort the input array in non-decreasing order.
3     arr.sort((a, b) => a - b);
4
5     // The first element should always be set to 1.
6     arr[0] = 1;
7
8     // Initialize 'maxElement' to keep track of the maximum element after operations.
9     let maxElement = 1;
10
11    // Iterate over the array starting from the second element.
12    for (let i = 1; i < arr.length; ++i) {
13        // Calculate the decrement value needed while ensuring it's not negative.
14        // We subtract 1 to allow only increments by 1 from the previous number or remaining unchanged.
15        const decrementValue = Math.max(0, arr[i] - arr[i - 1] - 1);
16
17        // Decrement the current element by the calculated value.
18        arr[i] -= decrementValue;
19
20        // Update 'maxElement' to be the higher value between the current 'maxElement' and the new value of arr[i].
21        maxElement = Math.max(maxElement, arr[i]);
22    }
23
24    // Return the maximum element found after performing the operations.
25    return maxElement;
26 }
27
```

## Time and Space Complexity

### Time Complexity

The time complexity of the given code is determined by the main operations it performs:

- Sorting the Array:** The sort operation on the array is the most time-consuming part. Python uses TimSort, which is a hybrid sorting algorithm derived from merge sort and insertion sort. The worst-case time complexity of the sort operation is  $O(n \log n)$ , where `n` is the number of elements in the array.
- Iterating over the Sorted Array:** After sorting, the function iterates through the sorted array once to adjust the values. This is a linear operation with a time complexity of  $O(n)$ .

Since sorting the array dominates the overall time complexity, the final time complexity of the entire function is  $O(n \log n)$ .

### Space Complexity

The space complexity of the code is analyzed based on the extra space used in addition to the input array:

- Sorting the Array:** The in-place sorting does not require additional space, so it uses  $O(1)$  additional space.
- Iteration:** No additional data structures are used during iteration, so it only requires constant space.

From the above analysis, the space complexity of the function is  $O(1)$ , which means it only requires a constant amount of extra space.