2865. Beautiful Towers I Medium Stack Array Monotonic Stack

Problem Description

straight line where the i-th tower is positioned at coordinate i and may vary in height, up to a maximum height specified by maxHeights[i]. The goal is to build these towers in such a way that they form a beautiful configuration. A beautiful configuration is defined by two criteria: The height of each tower (heights[i]) must be at least 1 and at most maxHeights[i].

You are given an array maxHeights which consists of n integers. Imagine the responsibility of constructing n towers along a

- The height sequence of the towers (heights) must form a mountain array, meaning there exists an index i in heights such
- that: For any index j less than i, heights[j] is less than or equal to heights[j+1] (ascending order). For any index k greater than i, heights[k] is greater than or equal to heights[k+1] (descending order).
- The challenge is to find the configuration of towers that is beautiful and yields the maximal possible sum of heights across all

and condition checking. Here's a step-by-step breakdown of how the solution is implemented:

maintained with non-increasing tower heights. Each y value is added to the total sum t.

towers.

Intuition

The approach to solve this problem involves iterating through each possible peak of the mountain (the highest point where the towers will transition from ascending to descending heights). For each potential peak position i, we determine the maximum sum

of heights for a mountain configuration where the peak is at i. To achieve this, we initialize the peak tower's height with 'x' the value given by maxHeights[i]. We then expand this peak to the left and right to construct the ascending and descending parts of the mountain. While expanding to the left, we ensure that the heights of the towers are both less than or equal to maxHeights[j] and the height of the previous tower to maintain a non-decreasing slope. Similarly, when expanding to the right, we maintain heights that are less than or equal to maxHeights[j] and the previous tower to ensure a non-increasing slope. The total sum for this configuration

is computed by accumulating the heights as we expand from the peak to both the left and right ends. After exploring all potential peak positions, we keep track of the maximum sum of heights that we have encountered. This value represents the highest sum of tower heights for any beautiful configuration possible, and thus, is the answer we return.

Solution Approach The provided solution uses a straightforward brute force approach to simulate the construction of the mountain from each

potential peak position. The approach does not use complex data structures or advanced algorithms; it relies on basic iteration

The function maximumSumOfHeights begins with initializing variable ans to store the maximum sum found for any beautiful configuration, and variable n to store the number of towers (the length of the maxHeights array).

returned.

Example Walkthrough

directly to find the optimal configuration.

step by trying each position for the peak.

It then enters a loop to consider each element x in maxHeights as the peak of the mountain (tallest tower). The variable i refers to the index where the peak is located. Inside the loop, two additional loops are used:

maxHeights[j] to ensure that the tower heights are non-decreasing as we move towards the peak. We then add the height y to the total sum t. • The second inner loop increases from the peak's index i+1 to the end of the array, similarly initializing y to the height of the peak. As we

iterate to the right, we update y with the minimum of the current y and maxHeights[j] to ensure the mountain array condition is

the total sum starting with the peak. For every element left of the peak (j index), we update y to the minimum of the current y and

∘ The first inner loop decreases from the peak's index i-1 to the start of the array. We initialize y as the height of the peak tower and t as

with the current maximum ans, updating ans if t is greater. Finally, after all iterations, ans contains the maximum sum that can be achieved by a beautiful configuration of towers and is

After both loops, we have constructed the tallest possible mountain whose peak is at index i and we compare its total sum t

previous tower (to maintain a valid mountain shape), and the cumulative sum of the current configuration, respectively. No extra data structures are used; the solution operates directly on the input array, and no sorting or other modifications are needed. The simplicity of the problem allows for a direct brute force method, exploring every possibility and comparing sums

Throughout the implementation, variables ans, y, and t are used to keep track of the current best answer, the height of the

Let's walk through a small example to illustrate the solution approach using the following maxHeights array: maxHeights = [2, 1, 4, 3]

In this scenario, we have four positions to place towers, and we can set their heights with the constraints provided in the

maxHeights array. We need to build the towers such that they form a mountain array. Let's examine the construction step-by-

• To the right, we need to construct descending towers. However, given the height 1 at the next position, we cannot make a descending

Trying the first position as the peak (i = 0). The peak height x = 2. • To the left of the peak, there are no taller towers, so we can't extend in that direction.

sequence from 2. The sequence fails to form a mountain, and the sum here would simply be 2.

```
    Since the peak is the smallest possible tower, we cannot create a proper mountain.

• The sum for this peak would be 1.
Trying the third position as the peak (i = 2). The peak height x = 4.
```

• The sequence [2, 1, 3] is not a valid mountain as it lacks a descending part, making this an invalid peak position.

Ascending from the left, we can have the first tower at height 2, next cannot exceed 1, so it stays 1.

• The mountain array [2, 1, 4, 3] forms a valid, beautiful configuration with a sum of 2 + 1 + 4 + 3 = 10.

Trying the fourth position as the peak (i = 3). The peak height x = 3. Ascending from the left, we start with 2, can increase to 1, but then we cannot go higher because the peak is at 3.

return 10 as the maximum sum for creating a beautiful tower configuration.

No towers to the right since this is the end of the array.

def maximumSumOfHeights(self, maxHeights: List[int]) -> int:

left min height = current height

right_min_height = current_height

temp_sum = current_height

Initialize the variable to hold the maximum sum of heights

encountered heights so far to the temporary sum

for left index in range(i - 1, -1, -1):

temp_sum += left_min_height

temp_sum += right_min_height

// Function to calculate the maximum sum of heights.

for (int i = 0; $i < sequenceLength; ++i) {$

minHeight = maxHeightSequence[i];

maxSum = max(maxSum, tempSum);

function maximumSumOfHeights(maxHeights: number[]): number {

// Return the maximum sum found

return maxSum;

long long maximumSumOfHeights(vector<int>& maxHeightSequence) {

long long maxSum = 0; // Initialize variable to hold the maximum sum

// Loop through the entire sequence to find the maximum sum of heights

// Extend to the left of position 'i' and accumulate heights

// Extend to the right of position 'i' and accumulate heights

// Update maxSum if the current temporary sum is greater

for (int leftIndex = i - 1; leftIndex >= 0; --leftIndex) {

// Reset minHeight for checking to the right of 'i'

int sequenceLength = maxHeightSequence.size(); // Get the length of the sequence

long long tempSum = maxHeightSequence[i]; // Start with the current height

tempSum += minHeight; // Add the minimum height to the temporary sum

for (int rightIndex = i + 1; rightIndex < sequenceLength; ++rightIndex) {</pre>

tempSum += minHeight; // Add the minimum height to the temporary sum

// This function calculates the maximum sum of heights based on the rules provided in the maxHeights array.

Initialize temporary variables for moving left and right from the current index

Temporary sum for current position including the current height itself

Move to the left of the current position and add the minimum of all

left min height = min(left min_height, maxHeights[left_index])

Move to the right of the current position and add the minimum of all

encountered heights so far to the temporary sum

encountered heights so far to the temporary sum

Return the maximum sum after considering all positions

for right index in range(i + 1, num heights):

for left index in range(i - 1, -1, -1):

temp_sum += left_min_height

// Initialize the answer variable that holds the maximum sum of heights encountered.

int minHeight = maxHeightSequence[i]; // Initialize the minimum height seen so far

minHeight = min(minHeight, maxHeightSequence[leftIndex]); // Update the min height

minHeight = min(minHeight, maxHeightSequence[rightIndex]); // Update the min height

max_sum = max(max_sum, temp_sum)

Descending from the peak to the right, the next and final tower can be up to 3.

Trying the second position as the peak (i = 1). The peak height x = 1.

Out of all the trials, the third position peak yields the highest sum of tower heights, which is 10. Therefore, the solution would

Temporary sum for current position including the current height itself

Move to the left of the current position and add the minimum of all

left min height = min(left min_height, maxHeights[left_index])

Update the maximum sum if the temporary sum is greater than the current maximum

the optimal construction.

Calculate the length of the maxHeights list once as it is used multiple times num_heights = len(maxHeights) # Iterate through each height in the maxHeights list for i. current height in enumerate(maxHeights): # Initialize temporary variables for moving left and right from the current index

The simple brute force approach worked effectively for this example by checking each possible peak and ensuring that all criteria

of a mountain array are met. By calculating the sums for each valid configuration and keeping track of the maximum, we identified

Move to the right of the current position and add the minimum of all # encountered heights so far to the temporary sum for right index in range(i + 1, num heights): right min height = min(right_min_height, maxHeights[right_index])

Solution Implementation

 $max_sum = 0$

Python

class Solution:

```
# Return the maximum sum after considering all positions
        return max_sum
Java
class Solution {
    // Method to calculate the maximum sum of heights, considering that each position
    // can act as a pivot, and the sum includes the minimum height from the pivot to each side.
    public long maximumSumOfHeights(List<Integer> maxHeightList) {
        long maxSum = 0: // This will store the maximum sum of heights we find
        int listSize = maxHeightList.size(); // The size of the provided list
        // Iterate through each element in the list to consider it as a potential pivot
        for (int i = 0; i < listSize; ++i) {</pre>
            int currentHeight = maxHeightList.get(i); // Height at the current pivot
            long tempSum = currentHeight; // Initialize temp sum with current pivot's height
            // Calculate the sum of heights to the left of the pivot
            for (int j = i - 1; j >= 0; --i) {
                currentHeight = Math.min(currentHeight, maxHeightList.get(i)); // Update to the smaller height
                tempSum += currentHeight; // Add this height to the running total for the pivot
            currentHeight = maxHeightList.get(i); // Reset height for current pivot
            // Calculate the sum of heights to the right of the pivot
            for (int j = i + 1; j < listSize; ++j) {</pre>
                currentHeight = Math.min(currentHeight, maxHeightList.get(i)); // Update to the smaller height
                tempSum += currentHeight; // Add this height to the running total for the pivot
            // Update maxSum if the sum for the current pivot is greater than the previous maximum
            maxSum = Math.max(maxSum, tempSum);
        // Return the maximum sum of heights found
        return maxSum;
C++
```

};

TypeScript

class Solution {

public:

```
let maximumSum = 0;
   // Get the total number of elements in the maxHeights array.
   const arrayLength = maxHeights.length;
   // Iterate over the maxHeights arrav.
   for (let currentIndex = 0; currentIndex < arrayLength; ++currentIndex) {</pre>
       // Get the height at the current index.
       const currentHeight = maxHeights[currentIndex];
       // Initialize the minimum height variables for left and right directions.
        let minHeightToLeft = currentHeight;
        let totalSum = currentHeight;
       // Iterate over the previous elements from the current index to calculate the sum.
        for (let leftIndex = currentIndex - 1; leftIndex >= 0; --leftIndex) {
           // Identify the new minimum height to the left.
           minHeightToLeft = Math.min(minHeightToLeft, maxHeights[leftIndex]);
           // Add the minimum height to the left to the total sum.
            totalSum += minHeightToLeft;
       // Reinitialize the minimum height to the current height for the right direction.
        let minHeightToRight = currentHeight;
       // Iterate over the next elements from the current index to calculate the sum.
        for (let rightIndex = currentIndex + 1; rightIndex < arrayLength; ++rightIndex) {</pre>
           // Identify the new minimum height to the right.
           minHeightToRight = Math.min(minHeightToRight, maxHeights[rightIndex]);
            // Add the minimum height to the right to the total sum.
            totalSum += minHeightToRight;
       // Compare the current total sum with the previous maximum sum and update maximumSum if necessary.
       maximumSum = Math.max(maximumSum, totalSum);
   // Return the maximum sum of heights after considering all possible positions.
   return maximumSum;
class Solution:
   def maximumSumOfHeights(self. maxHeights: List[int]) -> int:
       # Initialize the variable to hold the maximum sum of heights
       max_sum = 0
       # Calculate the length of the maxHeights list once as it is used multiple times
       num_heights = len(maxHeights)
       # Iterate through each height in the maxHeights list
       for i, current height in enumerate(maxHeights):
```

right min height = min(right_min_height, maxHeights[right_index]) temp_sum += right_min_height # Update the maximum sum if the temporary sum is greater than the current maximum max_sum = max(max_sum, temp_sum)

return max_sum

left min height = current height

right_min_height = current_height

temp_sum = current_height

Time Complexity

Time and Space Complexity

The time complexity of the provided code is $O(n^2)$, where n is the length of the maxHeights list. This is because for each element x in maxHeights, the code iterates over the elements to its left and then to its right in separate for-loops. Each of these nested loops runs at most n-1 times in the worst case, leading to roughly 2 * (n-1) operations for each of the n elements, thus the quadratic time complexity.

Space Complexity

The space complexity of the provided code is 0(1) as it only uses a constant amount of extra space. Variables ans, n, i, x, y, t, and j are used for computations, but no additional space that scales with the input size is used. Therefore, the space used does not depend on the input size and remains constant.