274. H-Index

Given an array of integers citations where {" "} citations [i] is the number of citations a researcher received for their {" "} ith {" "} paper, return compute the researcher's h -index.

According to the {" "} definition of h-index on Wikipedia: A scientist has an index h if h of their {" "} n papers have at least h

If there are several possible values for h, the maximum one is taken as the h -index.

citations each, and the other n - h papers have no more than h citations each.

```
Example 1:
```

```
Input: citations = [3,0,6,1,5]{"\n"}
Output: 3{"\n"}
Explanation: [3,0,6,1,5] means the researcher has 5 papers
in total and each of them had received 3, 0, 6, 1, 5 citations respectively.
{"\n"}Since the researcher has 3 papers with at least 3 citations each and
the remaining two with no more than 3 citations each, their h-index is 3.
{"\n"}
```

Example 2:

```
Input: citations = [1,3,1]{"\n"}
Output: 1{"\n"}
```

Constraints:

- n == citations.length
- 1 <= n <= 5000 • 0 <= citations[i] <= 1000

Solution

We can try all possible values of h from 0to n. For each h, loop through citations to see if h is a possible h-index, using the condition we are given:

A scientist has an index h if h of their n papers have at least h citations each, and the other n-h papers have no more than h citations each.

The answer is the highest h for which this is true. This takes $\mathcal{O}(n^2)$ time because for each of the n+1 possible h values, we have to loop through n citations.

Create a function hasAtLeastHPapersWithHCitations with a parameter h to check if there are at least h papers with >= h citations.

When has At Least HP apers With HC itations (x) is true, has At Least HP apers With HC itations (x-1) is also true. This means that

hasAtLeastHPapersWithHCitations is a monotonic function, so we can binary search for the highest h for which it return true. This

h is our h-index.

Time Complexity

Binary searching the range [0, n] takes $\mathcal{O}(\log n)$.

Each call to hasAtLeastHPapersWithHCitations checks all n papers, taking $\mathcal{O}(n)$.

Multiplying these together, we take $\mathcal{O}(n \log n)$.

Space Complexity

couple of variables, so the space complexity is $\mathcal{O}(1)$.

citations is passed by reference, so we aren't allocating any memory for it. We allocate a constant amount of memory for a

```
class Solution {
public:
   bool hasAtLeastHPapersWithHCitations(int h, vector<int>& citations) {
        int count = 0;
        for (int cite_count : citations) {
            if (cite_count >= h)
                count++;
        return count >= h;
    int hIndex(vector<int>& citations) {
        int low = 0, high = citations.size();
        while (low <= high) {</pre>
            int mid = (low + high) / 2;
            if (hasAtLeastHPapersWithHCitations(mid, citations))
                low = mid + 1;
            else
                high = mid - 1;
        return high;
};
class Solution {
    static boolean hasAtLeastHPapersWithHCitations(int h, int[] citations) {
        int count = 0;
        for (int cite_count : citations) {
            if (cite_count >= h)
                count++;
        return count >= h;
   public int hIndex(int[] citations) {
        int low = 0, high = citations.length;
        while (low <= high) {</pre>
            int mid = (low + high) / 2;
            if (hasAtLeastHPapersWithHCitations(mid, citations))
                low = mid + 1;
            else
                high = mid - 1;
        return high;
class Solution:
   def hIndex(self, citations: List[int]) -> int:
        def hasAtLeastHPapersWithHCitations(h, citations):
            return sum(cite_count >= h for cite_count in citations) >= h
        low = 0
        high = len(citations)
        while low <= high:</pre>
            mid = (low + high) // 2;
            if hasAtLeastHPapersWithHCitations(mid, citations):
                low = mid + 1;
```

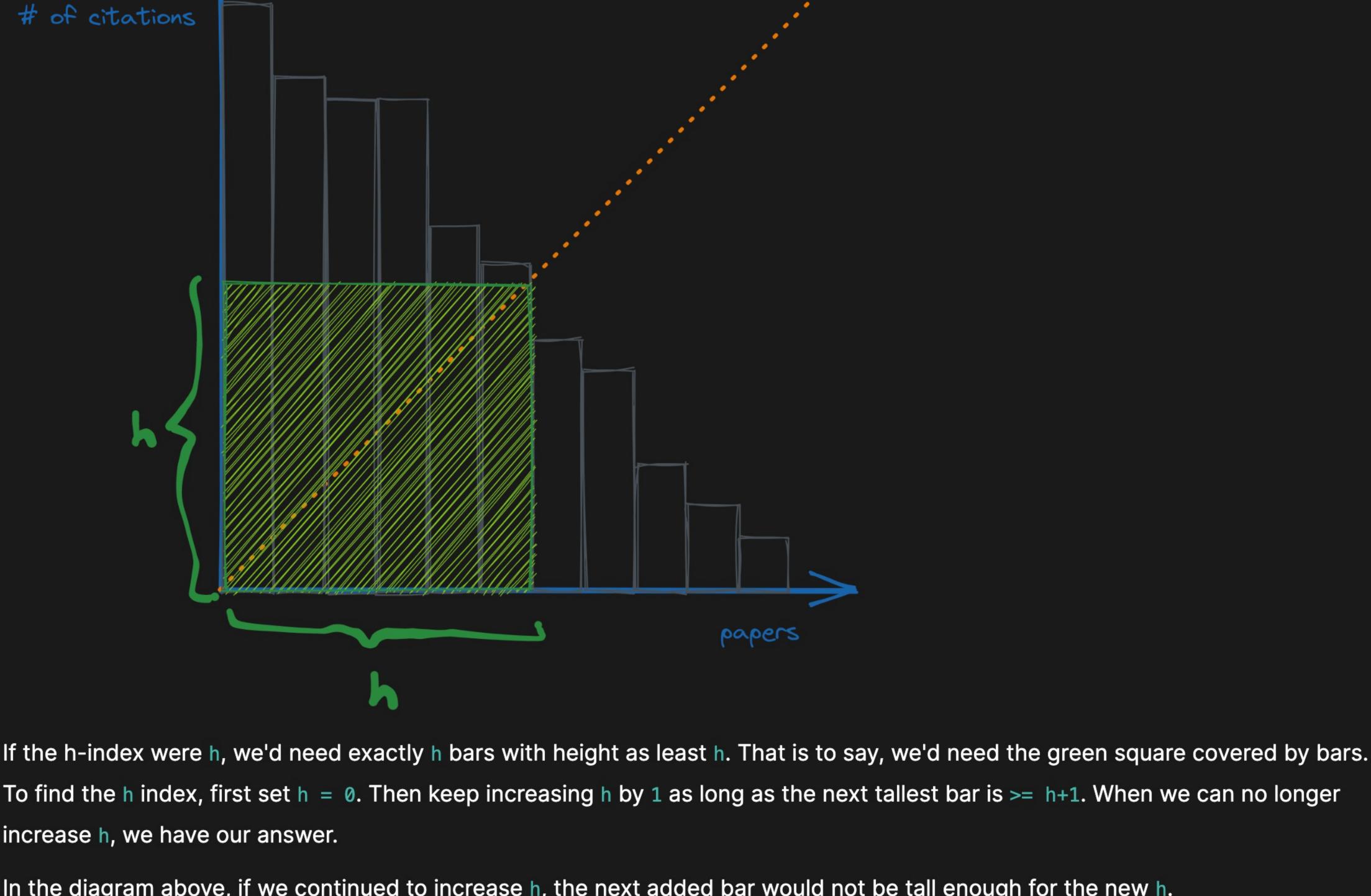

First we sort the papers by decreasing # of citations. Imagine a histogram where each bar represents a paper and its height is the

else:

return high

of citations it has.

high = mid - 1;



In the diagram above, if we continued to increase h, the next added bar would not be tall enough for the new h. **Time Complexity**

Sorting is $\mathcal{O}(n\log n)$. Looping h is $\mathcal{O}(n)$. So the time complexity is $\mathcal{O}(n\log n)$.

Space Complexity

class Solution { public: int hIndex(vector<int>& citations) {

The only memory we allocate is the integer h, so the space complexity is $\mathcal{O}(1)$.

```
sort(citations.rbegin(), citations.rend());
        int h = 0;
        while (h < citations.size() and citations[h] >= h+1) {
            h++;
        return h;
class Solution {
    public int hIndex(int[] citations) {
        // Sorting an int[] in reverse in Java is annoying
        // We first sort normally then reverse the array
        Arrays.sort(citations);
        for (int i = 0; i < citations.length/2; i++) {</pre>
            int tmp = citations[i];
            citations[i] = citations[citations.length-1-i];
            citations[citations.length-1-i] = tmp;
        int h = 0;
        while (h < citations.length && citations[h] >= h+1) {
            h++;
        return h;
class Solution:
   def hIndex(self, citations: List[int]) -> int:
```

while h < len(citations) and citations[h] >= h+1:

citations.sort(reverse=True)

h = 0

return h

h += 1