Problem Description

Sliding Window Hash Table

subarray consists of consecutive elements from the given array, and a score is calculated by taking the sum of the unique elements within that subarray. We are looking for the subarray with the highest sum where all elements are unique. The challenge is to devise an efficient algorithm to perform this action rather than using brute-force, which could be very slow for large arrays.

The task is to find the maximum score you can obtain by erasing exactly one subarray from an array of positive integers nums. A

Intuition

of the most recent index of each number in the array. The sliding window allows us to consider a subarray of unique elements which we can dynamically resize as we traverse the array. Here's an outline of our approach:

1. Initialize a dictionary or hash table to store the most recent index where each element has appeared as we iterate through the

The intuition behind the solution is to utilize a sliding window approach along with a hash table (or dictionary in Python) to keep track

array.

- 2. Keep a cumulative sum array which will help in getting the sum of any subarray in constant time. 3. Set two pointers, j starting at the beginning of the array and i which we will move forward through the array. 4. For each element v at index i:
- Update j to be the maximum of it own current value or the index stored in the hash table for the current element v. This is

update the answer if this sum is greater than the previously recorded answer.

- required to ensure our window does not include duplicate values.
- Calculate the sum of elements in the current window (subarray without duplicates) using the cumulative sum array and
- 5. Return the maximum sum recorded during this process. The use of the cumulative sum and a hash table allows us to efficiently calculate the sum of each potential unique subarray and track
- the presence of duplicates respectively. The sliding window dynamically adjusts to skip over elements that would lead to duplication, thus ensuring that at all times, the subarray being considered is unique. The max operations ensure that the window only expands
- when needed and shrinks appropriately to exclude duplicates.

Update the hash table with the current index for the element v.

Solution Approach The implementation of the solution uses a sliding window approach to consider every possible subarray that contains unique elements. Here is the detailed walk-through:

A dictionary d with integer keys and integer values, which serves as a hash table to keep track of the last index at which each element has appeared.

The dictionary d starts off empty.

elements to its right, up to 1, are unique.

1. Data Structures used:

 An array s, which is a cumulative sum array, such that s[i] is the sum of the first i numbers in nums. 2. Initialization:

- The cumulative sum array s is initialized with 0 as the first element and the cumulative sums of nums after that. 3. Sliding Window:
- An ans variable is initialized to 0 for storing the maximum sum of subarrays encountered. 4. Iterating through nums:

Define two pointers: i represents the current position in nums, and j is the start index of the window which ensures all

 The outer loop goes through each element v at index i (1-indexed for simplicity, due to the initial 0 in s). For each element v, check for duplicates by looking up v in the hash table d. If v is found, update j to be the maximum of its

6. Return the Result:

Example Walkthrough

5. Maintaining the Maximum Score:

- current value or the one stored in d[v], the index after the last occurrence of v. While keeping j as the start of the unique window, compute the sum of the current window by subtracting s[j] from s[i]. If this sum is greater than ans, update ans.
- As the loop progresses, the ans variable keeps track of the maximum score seen so far, and it is updated accordingly when a larger sum of a unique subarray is found.

After the loop has finished iterating over all elements in nums, ans holds the maximum score attainable by erasing exactly one

subarray of unique elements. It is returned as the final answer.

the maximum sum of a subarray with unique elements after erasing exactly one subarray.

Update the hash table d[v] with the new index i to mark the most recent occurrence of v.

duplicate discovers that it has appeared previously in the window. The algorithm efficiently computes the maximum sum subarray with no duplicates with a time complexity of O(N), where N is the size of the array nums, since each element is processed exactly once.

Through the use of cumulative sums, we are able to tell the sum of the subarray nums [j+1...i] in constant time by a simple

subtraction: s[i] - s[j]. Using the hash map d, we can dynamically adjust our unique window's start position j whenever a

1. Using Data Structures: We initialize an empty dictionary d. We also create a cumulative sum array s=[0, 3, 5, 6, 8, 11, 14], representing the cumulative sum up to each index. 2. Initializing Variables:

Let's walk through an example to illustrate the solution approach. Consider the array nums as [3, 2, 1, 2, 3, 3]. We want to find

0 = 3.

6. Returning Result:

Python Solution

class Solution:

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4. Iteration:

The dictionary d is {}.

3. Starting with a Sliding Window:

 Two pointers are set: i starts at 1 and j starts at 0. A variable ans is initialized to hold the maximum sum, starting at 0.

At i=1, nums[i] is 3. d does not contain 3, so no change to j. We add 3 to d with the value 1. ans becomes s[1] - s[j] = 3 -

At i=4, nums[i] is 2 again, but d does contain 2, so we update j to max(j, d[2] + 1) = max(0, 3) = 3. Update 2 in d with 4.

 At i=2, nums[i] is 2. No 2 in d, so j stays. Add 2 to d with value 2. ans becomes s[2] - s[j] = 5 - 0 = 5. At i=3, nums[i] is 1. No 1 in d, so j stays. Add 1 to d with value 3. ans becomes s[3] - s[j] = 6 - 0 = 6.

5. Maintaining Maximum Score:

elements from nums.

1 from collections import defaultdict

from itertools import accumulate

index_dict = defaultdict(int)

 \circ At i=5, nums[i] is 3. As 3 is in d, update j to max(j, d[3] + 1) = max(3, 2) = 3. Update 3 in d with 5. ans remains 6. • At i=6, nums[i] is 3. As 3 is in d, we update j to max(j, d[3] + 1) = max(3, 6) = 6. Update 3 in d with 6. ans remains 6.

def maximumUniqueSubarray(self, nums: List[int]) -> int:

prefix_sums = list(accumulate(nums, initial=0))

index_dict[value] = current_index

public int maximumUniqueSubarray(int[] nums) {

// Store the size of the nums vector

// Create an array to store the prefix sum of nums

prefixSum[i + 1] = prefixSum[i] + nums[i];

// Initialize the maximum sum of unique elements

// Initialize the start index of the current subarray

// Return the maximum sum of a unique element subarray

startIndex = max(startIndex, frequency[currentValue]);

// Iterate through the nums array to find the max sum of a unique-subarray

// Update the startIndex to be the maximum of the current startIndex or the

// Calculate the maxSum by considering the current unique subarray sum

// last index where currentValue was found (to ensure uniqueness in subarray)

prefixSum[0] = 0; // Initialize the first element as 0 for correct prefix sum calculation

int numsSize = nums.size();

int prefixSum[numsSize + 1];

int maxSum = 0;

return maxSum;

int startIndex = 0;

// Populate the prefixSum array

for (int i = 0; i < numsSize; ++i) {</pre>

for (int i = 1; i <= numsSize; ++i) {

int currentValue = nums[i - 1];

int length = nums.length; // Length of nums

Initialize a dictionary to store the most recent index of each number

Create a prefix sum array with an initial value of 0 for convenience

Update the dictionary with the current index of the value

int[] prefixSum = new int[length + 1]; // Array to store prefix sum

int[] lastIndex = new int[10001]; // Array to store the last index of each number

Return the maximum subarray sum containing unique elements

Initialize the maximum subarray sum and the start index for the subarray

ans is still 6 because s[4] - s[j] = 8 - 6 = 2.

The cumulative sum array s is [0, 3, 5, 6, 8, 11, 14].

- Each iteration considers whether the current unique window sum is greater than ans. The variable ans is kept up to date at all times.
- By employing this method, we have considered all subarrays with unique elements by dynamically adjusting the beginning of the subarray using the j pointer. Instead of calculating the sum each time, we utilized the cumulative sum array for quick calculations.

The dictionary d helped maintain indices of previous occurrences. Thus, we arrived at the maximum score efficiently.

After completing the loop, we have ans = 6, which is the maximum score obtainable by erasing one subarray of unique

max_sum = start_index = 0 11 12 13 # Iterate over the numbers alongside their indices (starting from 1) for current_index, value in enumerate(nums, 1): 14 # Update the start index to the maximum of the current start_index and the next index 15

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# after the previous occurrence of the current value
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               start_index = max(start_index, index_dict[value])
               # Update the maximum sum if the current subarray sum is greater
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               current_subarray_sum = prefix_sums[current_index] - prefix_sums[start_index]
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               max_sum = max(max_sum, current_subarray_sum)
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Java Solution

1 class Solution {

return max_sum

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// Calculate prefix sum array
           for (int i = 0; i < length; ++i) {
               prefixSum[i + 1] = prefixSum[i] + nums[i];
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           int maxSum = 0; // Initialize the maximum sum of a unique subarray
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           int windowStart = 0; // Initialize the start of the current window
14
           // Iterate over the nums array
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           for (int i = 1; i <= length; ++i) {
16
               int value = nums[i - 1]; // Current value
17
               windowStart = Math.max(windowStart, lastIndex[value]); // Update the start of the window to be after the last occurrence
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               // Calculate the current sum of unique subarray and compare it with the maximum sum found so far
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               maxSum = Math.max(maxSum, prefixSum[i] - prefixSum[windowStart]);
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               lastIndex[value] = i; // Update the last index of the current value
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           return maxSum; // Return the maximum sum of a unique subarray
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26 }
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C++ Solution
1 class Solution {
2 public:
       int maximumUniqueSubarray(vector<int>& nums) {
           // Create a frequency array initialized to zero for the possible range of values in nums
           int frequency[10001]{};
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maxSum = max(maxSum, prefixSum[i] - prefixSum[startIndex]); 32 33 // Update the index in frequency array to the current position for currentValue frequency[currentValue] = i; 34 35 36

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Typescript Solution
1 // Define the array of frequencies with a default value of zero for a range of possible values in nums array
2 let frequency: number[] = new Array(10001).fill(0);
   // Function to calculate the maximum sum of unique-elements subarray
   function maximumUniqueSubarray(nums: number[]): number {
       // Store the size of the nums array
       const numsSize: number = nums.length;
       // Create an array to store the prefix sum of nums
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       let prefixSum: number[] = new Array(numsSize + 1);
10
       prefixSum[0] = 0; // Initialize the first element as 0 for correct prefix sum calculation
11
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13
       // Populate the prefixSum array
       for (let i = 0; i < numsSize; ++i) {</pre>
14
           prefixSum[i + 1] = prefixSum[i] + nums[i];
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       // Initialize the maximum sum of unique elements
       let maxSum: number = 0;
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       // Initialize the start index of the current subarray
22
       let startIndex: number = 0;
23
24
       // Iterate through the nums array to find the max sum of a unique-element subarray
25
       for (let i = 1; i <= numsSize; ++i) {</pre>
           let currentValue = nums[i - 1];
26
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28
           // Update the startIndex to be the maximum of the current startIndex or the
           // last index where currentValue was found (to maintain uniqueness in subarray)
           startIndex = Math.max(startIndex, frequency[currentValue]);
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           // Calculate the maxSum by considering the current unique subarray sum
33
           maxSum = Math.max(maxSum, prefixSum[i] - prefixSum[startIndex]);
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return maxSum;

frequency[currentValue] = i;

// Return the maximum sum of a unique element subarray

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Time and Space Complexity **Time Complexity**

The time complexity of the code is O(n), where n is the length of the nums array. This is because the code involves a single loop that

// Update the index in frequency array to the current position for currentValue

iterates over nums, and within this loop, the operations performed (accessing the dictionary d, updating the sliding window's sum using the prefix sum s, and calculating the maximum ans) are all constant time operations.

Space Complexity The space complexity of the code is also O(n) due to the following reasons:

1. The d dictionary stores each unique value encountered in the nums array with its latest index position. In the worst case, if all elements are unique, the dictionary could hold up to n key-value pairs.

2. The s list is a prefix sum array which contains a cumulative sum of the nums array, and it has n + 1 elements (including the initial

Combining the above, the total space complexity remains O(n).

0). Thus, it also consumes O(n) space.