2317. Maximum XOR After Operations

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Medium
         Bit Manipulation
                        Array
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In this problem, we are given an array of integers nums, and our objective is to maximize the bitwise XOR of all elements of the array after performing a certain operation any number of times. The operation defined allows us to:

- 1. Choose any non-negative integer x.
- 2. Select any index i.

Problem Description

3. Update nums[i] to nums[i] AND (nums[i] XOR x).

Here AND and XOR are bitwise operations. Bitwise AND results in a bit being 1 if both bits at the same position are 1, otherwise it's 0. Bitwise XOR results in a bit being 1 if the bits at the same position differ, otherwise it's 0.

The main challenge is to figure out what x and t we should choose to maximize the final XOR of all elements.

Intuition

behavior of AND when combined with XOR: for any integer n, n AND (n XOR x) equals n. Armed with this knowledge, we can simplify the problem significantly. Since applying the given operation does not change the value of any element in the array (because for any given i and x, nums [i]

To solve this problem, we should understand the properties of the XOR and AND operations. An important fact to consider is the

(nums[i] XOR x) will always equal nums[i]), the elements of nums can be left as they are. Thus, the operation has no effect on the outcome of maximizing the bitwise XOR of all array elements. This leads us to the conclusion that the maximum possible bitwise XOR can be obtained by simply computing the bitwise XOR of all elements in the array without modifying them. To implement the solution, we use a reduce function from Python's functools module with or_, which is a function that performs

the bitwise OR operation (imported from the operator module). By performing a bitwise OR between all numbers in nums, we effectively combine all the bits set in any number in the array. Since XOR of identical bits is 0 and 1 otherwise, the bitwise OR accumulates all the 1 bits across all the numbers, yielding the maximum XOR value achievable. **Solution Approach**

The solution employs the reduce function, a Python technique that cumulatively applies an operation to all elements of an

Here's a step-by-step breakdown of the algorithm used in the solution: 1. Import the reduce function from the functools module and the or_ function from the operator module (this import is not shown in the given

iterable. The specific operation used here is the bitwise OR, provided by the or_ function from the operator module.

2. Initialize the maximumXOR method, which takes nums, the list of integers.

- 3. Within the method, call reduce with two arguments:
- The first argument is or_, the function that will be applied to the elements of nums.
- The second argument is the nums list itself. 4. reduce then applies the or_ function cumulatively to the items of nums, from left to right. This means that it starts with the first two elements a
 - and b of nums, computes a | b, then applies the or_ operation to this result and the next element, and so on until all elements have been

code, but is required for or_ to be used).

- included. 5. Since the bitwise OR accumulates all bits set in any number in nums, the final result represents the maximum possible XOR that can be obtained, as each bit position in the final result is set to 1 if it's set in at least one number in the array.
- 6. The result of the reduce operation is the maximum XOR value, which is returned by the maximumXOR method.

In summary, the given solution cleverly sidesteps the need to perform any complex calculations by realizing that the maximum

XOR is simply the accumulation of all the unique bits set in the original nums list, and it uses reduce with bitwise OR to calculate this result efficiently.

Example Walkthrough

Suppose we have the following array of integers nums:

nums = [3, 10, 5]

Let's walk through a small example to illustrate the solution approach.

Based on the provided content, our goal is to maximize the bitwise XOR of all elements in the array by performing defined operations. However, since we know that the operations won't change any value (as n AND (n XOR x) equals n), the process

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simplifies to finding the XOR of all numbers as they are.
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The binary representations of the numbers in nums are as follows: **->** 101

based on the explanation) of all elements in nums:

Start with the first two numbers: 3 (011) | 10 (1010) = 11 (1011).

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Now let's compute the bitwise OR (not XOR, as incorrectly mentioned in the content, but it's intended to be the OR operation
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The result of 15 (1111) in binary indicates that all bit positions have been set to 1. This is the maximum value we can obtain from a bitwise XOR of any subsequence of these numbers because all possible 1 bits are included in the result.

Now, take the previous OR result and apply it to the next number: $11 (1011) \mid 5 (0101) = 15 (1111)$.

from functools import reduce from operator import or_ nums = [3, 10, 5]

Indeed, the maximum possible bitwise XOR value for this array is 15, which is the result we obtained by applying the bitwise OR

print(max_xor_value) # Output should be 15

The reduce function iteratively applies the binary OR operation (or_)

value can be achieved by performing a bitwise OR on all numbers, since

XORing a bit with 0 keeps the original bit, and XOR of all different

// Function to calculate the maximum XOR of all elements in the given vector

int result = 0; // Initialize result to 0, the identity element for XOR

int maximumXOR(vector<int>& nums) {

to all elements of the nums list. This is because the maximum XOR

bits set in the numbers will be reflected in the OR operation.

Thus, using the solution approach, we would simply call reduce with the or_ function:

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operation to all elements of nums using the reduce function. The computation of the result agrees perfectly with our manual
  calculation, illustrating the correctness and efficiency of the solution approach.
Solution Implementation
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max_xor_value = reduce(or_, nums)

Python from functools import reduce # Import the reduce function from the functools module from operator import or_ # Import the or_ function from the operator module from typing import List # Import the List type from the typing module for type hints

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class Solution:
   def maximum_xor(self, nums: List[int]) -> int:
       # Compute the maximum XOR value of all elements in the nums list.
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# Args:
              nums (List[int]): A list of integers.
        # Returns:
              int: The maximum XOR value of all elements in nums.
        return reduce(or_, nums)
# Example usage:
# Instantiate the Solution class.
solution = Solution()
# Call the maximum_xor method with a list of integers.
max_xor = solution.maximum_xor([1, 2, 3])
# The returned value would be 1 \mid 2 \mid 3 which is 3 (in binary: 01 \mid 10 \mid 11 = 11)
print(max_xor) # Output will be 3
Java
class Solution {
    // Method to calculate the maximum XOR of all elements in the array
    public int maximumXOR(int[] nums) {
        int maxXor = 0; // Initialize the variable to store the maximum XOR result
        // Loop through each number in the array
        for (int num : nums) {
            // Perform bitwise OR operation with current number and store the result
            // This will set maxXor to the union of bits set in any of the numbers
            maxXor |= num;
        // Return the maximum XOR value obtained
        return maxXor;
C++
#include <vector>
class Solution {
public:
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// Iterate over all the numbers in the vector
        for (int num : nums) {
           // Perform bitwise OR on the result with the current number
           // This ensures that any bit set in any number will be set in the final result
            result |= num;
       // The result now contains the maximum XOR possible with the given numbers
       return result;
};
TypeScript
// Function to calculate the maximum XOR of an array of numbers
function maximumXOR(nums: number[]): number {
   // Initialize answer with 0
   let answer = 0;
   // Iterate through each number in the array
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for (const number of nums) {
         // Perform bitwise OR between the current answer and the number
         // This accumulates the set bits across all numbers in the array
          answer |= number;
      // Return the final answer which is the maximum XOR value
      return answer;
from functools import reduce # Import the reduce function from the functools module
from operator import or_ # Import the or_ function from the operator module
                             # Import the List type from the typing module for type hints
from typing import List
class Solution:
   def maximum_xor(self, nums: List[int]) -> int:
       # Compute the maximum XOR value of all elements in the nums list.
       # The reduce function iteratively applies the binary OR operation (or_)
       # to all elements of the nums list. This is because the maximum XOR
       # value can be achieved by performing a bitwise OR on all numbers, since
       # XORing a bit with 0 keeps the original bit, and XOR of all different
       # bits set in the numbers will be reflected in the OR operation.
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# Args:
      nums (List[int]): A list of integers.
# Returns:
      int: The maximum XOR value of all elements in nums.
return reduce(or_, nums)
```

max_xor = solution.maximum_xor([1, 2, 3]) # The returned value would be $1 \mid 2 \mid 3$ which is 3 (in binary: $01 \mid 10 \mid 11 = 11$) print(max_xor) # Output will be 3

Call the maximum_xor method with a list of integers.

Instantiate the Solution class.

Example usage:

solution = Solution()

each pair of integers.

Time and Space Complexity The time complexity of the code is O(N), where N is the number of elements in the list nums. This is because the function reduce applies the or_operator (|) sequentially to the elements of the list, and applying the or_operator takes constant time 0(1) for

The space complexity of the function is 0(1), as it reduces all the elements to a single integer without using any additional space that grows with the input size.