#### 1526. Minimum Number of Increments on Subarrays to Form a Target Array Dynamic Programming

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Leetcode Link



Array

The problem presents an integer array called target. We also have an array of the same size as target, named initial, which is filled with zeros. The key objective is to transform the initial array into the target array. The only operation allowed to achieve this is to select a subarray from initial and increment each of its elements by one. The task is to determine the minimum number of such operations required to reach the target array configuration. It's also specified that the final answer will fit within a 32-bit integer, which means it won't be too huge for an int data type to store.

differences between the heights (values) of adjacent elements in the target array.

To solve this problem, one needs to intuitively understand that the minimum number of operations needed is closely related to the

Intuition

### Intuition behind the solution arises from looking at the problem in terms of "height differences". Imagine a graph where the value of

ground level of a terrain from one point to another by one unit. To minimize operations, we should always try to raise the terrain in the largest possible steps rather than incrementing little by little. The first insight is that we'll have to increment the first element of initial to the first element of target for sure since there are no previous elements to consider, which accounts for target [0] operations.

each element in the target array represents the height at that particular position. Incrementing a subarray by 1 is like raising the

Following that, we move through the target array and look at the difference between each pair of adjacent elements (b - a for elements a and b). Each time we encounter a rise in height (where b > a), we need additional operations equivalent to the height

do not need extra operations since we can imagine that the previous increments have already covered that height. By summing up all necessary height differences, we can get the total number of increments required. Therefore, the number of operations can be given by the first element of the target array plus the sum of all positive differences between successive

difference to "build up" our terrain to that new height. If the height decreases or remains equal (b - a is less than or equal to 0), we

adjacent pairs of elements and calculate the sum of the positive differences. Solution Approach The solution to this problem utilizes a straightforward Greedy algorithm approach and Python's built-in functionality to generate

elements in the target array. The given Python function pairwise from the itertools library can be used here to generate the

#### Here's a brief walkthrough of the implementation:

adjacent pairs easily.

1. Initialization:

2. Iterating through the array:

the iterable target. 3. Calculating the Needed Operations: For each pair (a, b) obtained from the pairwise, we add to our operations count the difference (b - a) if b is greater than

a. The expression max(0, b - a) ensures that we only consider positive differences, which represent an increase in value

We then iterate over the target array, comparing each element to its predecessor to find the difference between them. The

iteration of pairs is done using the pairwise function, which neatly returns a tuple containing pairs of adjacent elements from

We start by initializing the number of operations to the value of the first element in target, because the initial array is filled

with zeros, and we must at least increment the first element 'target[0]' times to match the first element of the target array.

 The rationale behind this is that whenever b is greater than a, we need additional operations to raise initial[a] to initial[b]. If b is equal to or less than a, no extra operations are needed because we assume initial[a] is already at least

from one element in target to the next.

- at height a, so we can effectively "carry over" this height to initial[b]. 4. Summation: We sum up all the extra operations needed for each increase in the array, adding it to our initial count of target [0]
- 5. Result: The final result is returned as the sum of the initial operations count and the accumulated extra operations needed. This sum represents the minimum number of operations required to form the target array from the initial array.

 Python's built-in sum function to calculate the aggregate of operations needed, pairwise utility from the itertools library to iterate through the array in adjacent element pairs.

The data structures and patterns used in this approach are quite simple and consist of:

A List (target) to store the integer values we're working with,

in linear time, making it a very practical solution for this problem.

The beauty of this solution lies in its simplicity and efficiency. There are no complex data structures required, and the algorithm runs

The Greedy algorithm pattern, where we take the optimal decision step-by-step based on the current and next element,

Let's walk through a small example to clearly understand how the solution approach works.

Start with operations count equal to the first element of target: operations = target[0] = 1.

Pair (3, 2): No increase (it's actually a decrease), so add 0: operations += max(0, 2 - 3) = 3.

operations. The sum is computed using the built-in sum function, which takes an iterable.

Suppose we have a target array given as [1, 3, 2, 4]. Our goal is to transform an initial array from [0, 0, 0, 0] to match the target array using the fewest number of operations.

• The result is operations = 1 + 2 + 0 + 2 = 5. So, it takes a minimum of 5 operations to transform initial into target.

In this example, we increment the first element (index 0) of the initial array 1 time to match the first element of the target array, then

to 2, as the previous operations have already covered this. Finally, we perform two more operations from index 2 to index 3 to

# The function calculates the minimum number of operations needed to form the target array

increment the last two elements by 1 each time, resulting in [2, 3, 1, 1] and then [2, 3, 2, 2], and finally our target [1, 3, 2,

### Generate pairs using pairwise: (1, 3), (3, 2), (2, 4).

2. Iterating through the array:

1. Initialization:

4. Summation:

Example Walkthrough

3. Calculating the Needed Operations:

Pair (1, 3): Increase is 2, so add 2 to operations: operations += max(0, 3 - 1) = 3.

• Pair (2, 4): Increase is 2, so add 2 to operations: operations += max(0, 4-2) = 5.

- We combine the counted operations to get the total. 5. Result:
- we perform another operation on the subarray from index 0 to index 1 to increment both elements (making the array [1, 1, 0, 0]). Next, we perform a third operation on the same subarray, resulting in [2, 2, 0, 0]. No operation is needed for the transition from 3

from itertools import pairwise # Python 3 function from the itertools module

def minNumberOperations(self, target: List[int]) -> int:

# from a starting array of zeros. Each operation increments a contiguous subarray by 1. # The first operation will increment the contiguous subarray from the start to set the first element # Thus, the number of operations for the first element is equal to its value 10 operations = target[0] 11 12 # sum up the differences between consecutive elements if they are positive # as these represent the additional operations needed for increasing the array to match the target 13 for previous, current in pairwise(target): 14 operations += max(0, current - previous) # Only positive differences are added 15 16 17 # The total number of operations to match the target array is returned 18 return operations

# **Java Solution**

public int minNumberOperations(int[] target) {

for (int i = 1; i < target.length; ++i) {

int minNumberOperations(std::vector<int>& target) {

for (int i = 1; i < target.size(); ++i) {</pre>

if (target[i] > target[i - 1]) {

1 // Function to calculate the minimum number of operations needed to

// Each operation increments a subarray's elements by 1.

function minNumberOperations(target: number[]): number {

return totalOperations;

// Iterate through the target array starting from the second element.

// If the current target value is greater than the previous,

// Return the total number of operations needed to form the target array.

totalOperations += target[i] - target[i - 1];

// raise a series of values to match the heights specified in the 'target' array.

// since we start with an array of zeros, the first element itself will be

// Initialize the number of operations with the first element of the target array,

int minOperations = target[0];

// Initialize minimum operations with the first element

// since that's the minimum number of operations needed

// Iterate through the array starting from the second element

// If the current element is greater than the previous one,

// it means we need additional operations to increase from

// the previous element's value to the current element's value.

// to increase from 0 to the first element's value.

4]. Thus, a total of 5 operations were needed.

**Python Solution** 

class Solution:

class Solution {

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25 };

```
if (target[i] > target[i - 1]) {
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15
                   minOperations += target[i] - target[i - 1];
16
               // If not, no additional operations are needed because the
17
               // operations required to reach the previous element are adequate.
19
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21
           // Return the total minimum number of operations required.
22
           return minOperations;
25
C++ Solution
   #include <vector>
   class Solution {
   public:
       /**
        * Calculate the minimum number of operations to form a target array from a zero array.
        * An operation is incrementing a subarray by 1.
        * @param target Vector of integers representing the target array.
9
        * @return The minimum number of operations required.
10
11
```

int totalOperations = target[0]; // Start with the first value as the initial number of operations.

// this signifies a need for additional operations to increment the subarray.

# **Typescript Solution**

```
// the number of operations needed to reach its value.
       let operations = target[0];
 8
 9
       // Loop through the target array starting from the second element.
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       for (let index = 1; index < target.length; ++index) {</pre>
11
           // If the current element is greater than the previous one,
           // we need additional operations for the difference between
13
           // the current and the previous elements.
14
           if (target[index] > target[index - 1]) {
15
               operations += target[index] - target[index - 1];
16
17
18
19
       // Return the total number of operations calculated.
20
21
       return operations;
22 }
23
Time and Space Complexity
The code provided calculates the minimum number of operations to form a target array where each operation increments a subarray
by 1. The function minNumberOperations does this by summing the differences between consecutive elements where the second
element is larger than the first, plus the value of the first element in the target array. Let's analyze both the time complexity and
```

The function iterates once over the list of target elements using the pairwise utility to consider pairs of consecutive elements. The

Therefore, the overall time complexity of the code is O(n).

Space Complexity:

## The function is a one-liner without the use of additional data structures that depend on the size of the input. It relies on generator

space complexity: Time Complexity: time complexity for this operation is O(n), where n is the length of the target array, because it goes through the list once.

The pairwise utility itself, which is presumably a wrapper around a simple loop-like construct that yields successive pairs of

elements, does not add any significant time overhead as it just creates a tuple of the current and next elements in the array.

space proportional to the input size. The space complexity is not affected by the size of the input array, as the sum function processes the generator expression

expressions which yield one item at a time. The max function is applied in a generator expression, so it does not require additional

iteratively. The pairwise utility is expected to yield one pair at a time and doesn't store the entire list of pairs in memory. As a result, the overall space complexity of the code is 0(1), reflecting constant space usage.