549. Binary Tree Longest Consecutive Sequence II Depth-First Search Binary Tree Medium Tree

Leetcode Link

This problem provides us with the root of a binary tree and asks us to find the length of the longest consecutive path in that tree.

Problem Description

nodes in this path should have values that differ by exactly one. To clarify, paths such as [1,2,3,4] (increasing) and [4,3,2,1] (decreasing) are valid. However, a path like [1,2,4,3] is invalid as the values do not differ by one. Additionally, it's important to note that the path does not need to follow parent-child relationships and could include a 'bounce', going from child to parent to another child (child-parent-child pattern). Intuition

The consecutive path we are looking for can be either increasing or decreasing in terms of node values, and every two consecutive

The intuition behind this solution lies in using a recursive depth-first search (DFS) algorithm to traverse the tree and compute the increasing and decreasing consecutive paths. For every node, there can be four kinds of consecutive paths: Paths that only include this node.

To track these paths, for each node, we calculate two values: incr and decr, which represent the lengths of the longest increasing and decreasing paths ending at this node, respectively.

path. Here's a step-by-step walkthrough of the implementation:

there are no consecutive paths beyond this point.

or one more than the current node's value, respectively.

consecutive paths ending at this node (both increasing and decreasing).

Let's walk through an example to illustrate the solution approach. Consider the following binary tree:

as the result of the longestConsecutive function.

Here's how the recursive DFS would process this tree:

"bounces" between children, we ensure no possible paths are missed.

When we visit a node, we check its children. If either child's value is one more than the current node's value, we increment incr; if it's

2. Paths that start from this node and extend to any node in the left subtree.

Paths that start from this node and extend to any node in the right subtree.

one less, we increment decr. We take these two values from both children and use them to update the incr and decr values of the current node. The magic happens by considering not only the deepest path from this node to each child but also the possibility of continuing the

4. Paths that go through this node, meaning they start from the left subtree, include this node, and go to the right subtree.

path by "bouncing" from one child to the other through the current node, which effectively can increase the overall length of the consecutive path.

As we compute the incr and decr values for each node, we keep track of the global maximum length (ans) found so far. To get the maximum consecutive path that can pass through a node, we add the incr and decr values of this node but subtract 1 because the node itself is counted twice (once in each path). After the DFS traverses the whole tree, ans will store the length of the longest consecutive path.

Solution Approach The solution uses a recursive depth-first search (DFS) to explore the binary tree and calculate the length of the longest consecutive

1. Recursive Function Definition: A function dfs is defined, which takes a node of the tree as an argument and returns a tuple

[incr, decr]. incr holds the maximum length of an increasing consecutive path ending at that node, and decr is the same for

2. Base Case: When dfs encounters a None (indicating the node being visited is non-existent or a leaf's child), it returns [0, 0] as

3. State Variables: The solution introduces a nonlocal variable ans to track the maximum length found during traversal.

4. Child Nodes Analysis: Each call to dfs considers the current node's left and right child nodes. For each child, the function computes i1/d1 and i2/d2 which are tuples returned by the recursive dfs call on the left and right children, respectively.

counted once.

Example Walkthrough

decreasing paths.

5. Update Increments/Decrements: □ It then checks the value of the left child (if it exists), updating incr or decr based on whether the left child's value is one less

current node. 6. Global Maximum Update: After calculating the incr and decr for both the left and right children, and is updated by taking the sum of the current node's incr and decr minus one — as the current node is counted in both incr and decr and should only be

7. Return Values: Finally, the function returns a tuple [incr, decr] for the current node, which signifies the maximum lengths of

8. Result: After dfs is called on the root, ans contains the length of the longest consecutive path in the tree, which is then returned

Similarly, checks are performed on the right child, updating incr and decr by comparing the values of the right child and the

- The algorithm effectively scans the entire tree only once, ensuring an efficient solution with a time complexity of O(n), where n is the number of nodes in the tree. By considering each node and its potential paths (both increasing and decreasing), as well as potential

1. Starting at the Root (Node 3): The initial call to DFS is made on the root (node 3). At this point, ans is initialized to 0.

• The right child has the value 4, which is more by 1 than its parent (node 3), so for node 3, incr = 2.

2. Recursive Calls: The dfs function will make recursive calls to the left (node 2) and right (node 4) children: ◦ Left Child (Node 2): ■ The left child has the value 2, which is less by 1 than its parent (node 3), so for node 3, decr = 2. It recursively calls dfs on node 2's left child (node 1).

■ The decr from node 2 is now combined with node 3's decr to update ans, if necessary, to ans = decr_2 + decr_3 - 1.

○ From left child's decr (2 from node 2) and right child's incr (2 from node 4), we get 2 + 2 - 1 = 3 for node 3, which means

We've also computed ans at each node, which is the maximum value obtained by adding incr and decr and subtracting 1 (to

Since the tree was recursively traversed, ans holds the maximum length of the longest consecutive path after taking all

Based on our example, the longest consecutive path is 3 (which is the path [2, 3, 4] or [4, 3, 2]), and this is output by the

longestConsecutive function as the DFS is executed from the root of the tree to all its children and their subsequent descendants.

Node 5 is more by 1 than node 4, so for node 4, incr = 2. ■ The incr from node 4 is now combined with node 3's incr to update ans, if necessary, to ans = incr_4 + incr_3 - 1.

Right Child (Node 4):

4. Finalizing the Result: After the full traversal,

nodes into consideration.

1 # Definition for a binary tree node.

def dfs(node):

if node is None:

if node.left:

def longestConsecutive(self, root: TreeNode) -> int:

Perform DFS on the left and right children

left_incr, left_decr = dfs(node.left)

right_incr, right_decr = dfs(node.right)

if node.left.val + 1 == node.val:

incr_length = left_incr + 1

elif node.left.val - 1 == node.val:

decr_length = left_decr + 1

return max_length # Return the maximum length found

if (node.right.val - 1 == node.val) {

return new int[] {incrementing, decrementing};

TreeNode() : val(0), left(nullptr), right(nullptr) {}

TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}

decrementing = Math.max(decrementing, rightSubtree[1] + 1);

longestLength = Math.max(longestLength, incrementing + decrementing - 1);

// -1 is to not double count the current node in both incrementing and decrementing sequences

// Return the length of the longest incrementing and decrementing sequence ending at this node

TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}

// Function that starts the process and returns the longest consecutive sequence length

// Helper function to perform DFS and calculate the consecutive sequence length

// Base case: if the node is null, return {0, 0} as there is no sequence

// Initialize the length of the increasing and decreasing sequences to 1 (the root itself)

if (root->left->val + 1 == root->val) increaseLength = leftSequence[0] + 1;

if (root->left->val - 1 == root->val) decreaseLength = leftSequence[1] + 1;

if (root->right->val + 1 == root->val) increaseLength = max(increaseLength, rightSequence[0] + 1);

if (root->right->val - 1 == root->val) decreaseLength = max(decreaseLength, rightSequence[1] + 1);

// Update longestLength if the current sequence is the longest

return [incr_length, decr_length]

dfs(root) # Start DFS from the root

Recursive depth-first search to find the longest consecutive path

Check for consecutive increments or decrements on the left child

Check for consecutive increments or decrements on the right child

Update the max_length considering both increasing and decreasing paths

max_length = max(max_length, incr_length + decr_length - 1)

max_length = 0 # Initialize the maximum length of consecutive sequence

Python Solution

2 class TreeNode:

class Solution:

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65 }

* };

public:

12 class Solution {

*/

C++ Solution

* struct TreeNode {

int val;

TreeNode *left;

int longestStreak;

dfs(root);

longestStreak = 0;

return longestStreak;

vector<int> dfs(TreeNode* root) {

if (!root) return {0, 0};

// Process left child

// Process right child

if (root->right) {

if (root->left) {

TreeNode *right;

* Definition for a binary tree node.

int longestConsecutive(TreeNode* root) {

int increaseLength = 1, decreaseLength = 1;

vector<int> leftSequence = dfs(root->left);

vector<int> rightSequence = dfs(root->right);

// Check if it's consecutively increasing

// Check if it's consecutively decreasing

// Check if it's consecutively increasing

// Check if it's consecutively decreasing

// Recursively call dfs for the left and right subtrees

3. Update Global Maximum (ans): Since both left and right children of node 3 form consecutive sequences, we calculate the maximum sum of decr and incr.

including node 3, there is a path of length 3 that goes from node 5 to node 3 to node 2.

Node 1 is also less by 1 than node 2, so now for node 2, decr = 2.

Node 1 has no children, so the recursive call would return [0, 0].

It recursively calls dfs on node 4's right child (node 5).

account for the current node being included in both sequences).

- We have computed incr and decr for all nodes.
- def __init__(self, val=0, left=None, right=None): self.val = val self.left = left self.right = right

return [0, 0] # Base case: return 0's for the length of increasing and decreasing sequences

nonlocal max_length # Use nonlocal keyword to modify the non-local max_length variable

incr_length = decr_length = 1 # Initialize lengths of increasing and decreasing paths

if node.right: if node.right.val + 1 == node.val: 32 incr_length = max(incr_length, right_incr + 1) 33 34 elif node.right.val - 1 == node.val: decr_length = max(decr_length, right_decr + 1)

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Java Solution

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class Solution {
        private int longestLength;
       // Function to start the longest consecutive sequence process
        public int longestConsecutive(TreeNode root) {
            longestLength = 0;
           dfs(root);
            return longestLength;
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       // Perform a Depth First Search on the tree
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       private int[] dfs(TreeNode node) {
            if (node == null) {
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14
                return new int[] {0, 0};
15
16
            int incrementing = 1; // Length of incrementing sequence ending at this node
17
            int decrementing = 1; // Length of decrementing sequence ending at this node
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20
           // Recurse left
21
            int[] leftSubtree = dfs(node.left);
22
           // Recurse right
23
            int[] rightSubtree = dfs(node.right);
24
           // Check left child
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26
            if (node.left != null) {
27
                if (node.left.val + 1 == node.val) {
28
                    incrementing = leftSubtree[0] + 1;
29
                if (node.left.val - 1 == node.val) {
30
                    decrementing = leftSubtree[1] + 1;
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32
33
34
            // Check right child
35
            if (node.right != null) {
36
37
                if (node.right.val + 1 == node.val) {
                    incrementing = Math.max(incrementing, rightSubtree[0] + 1);
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```

49 50 51 // Update the longest streak result by taking the maximum sum of increasing and // decreasing lengths from the current node minus 1 (to avoid double-counting the node itself) 52 53 longestStreak = max(longestStreak, increaseLength + decreaseLength - 1);

```
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             // Return a pair of the longest increasing and decreasing sequences starting from the current node
 56
             return {increaseLength, decreaseLength};
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 58 };
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Typescript Solution
  1 // Definition for a binary tree node.
  2 class TreeNode {
        val: number;
         left: TreeNode | null;
         right: TreeNode | null;
  6
         constructor(val: number = 0, left: TreeNode | null = null, right: TreeNode | null = null) {
             this.val = val;
  8
             this.left = left;
  9
 10
             this.right = right;
 11
 12 }
 13
     let longestStreak: number;
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 15
 16 // Function that starts the process and returns the longest consecutive sequence length
    function longestConsecutive(root: TreeNode | null): number {
         longestStreak = 0;
 18
        dfs(root);
 19
 20
         return longestStreak;
 21 }
 22
    // Helper function to perform DFS and calculate the consecutive sequence length
    function dfs(root: TreeNode | null): number[] {
        // Base case: if the node is null, return [0, 0] as there is no sequence
 25
 26
         if (!root) return [0, 0];
 27
 28
         // Initialize the length of the increasing and decreasing sequences to 1 (the root itself)
 29
         let increaseLength: number = 1, decreaseLength: number = 1;
 30
 31
         // Recursively call dfs for the left and right subtrees
 32
         const leftSequence: number[] = dfs(root.left);
 33
         const rightSequence: number[] = dfs(root.right);
 34
 35
        // Process left child
 36
        if (root.left) {
 37
             // Check if it's consecutively increasing
 38
             if (root.left.val + 1 === root.val) {
 39
                 increaseLength = leftSequence[0] + 1;
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 41
             // Check if it's consecutively decreasing
             if (root.left.val - 1 === root.val) {
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 43
                 decreaseLength = leftSequence[1] + 1;
 44
 45
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 47
         // Process right child
 48
         if (root.right) {
```

Time and Space Complexity **Time Complexity**

// Check if it's consecutively increasing

// Check if it's consecutively decreasing

increaseLength = Math.max(increaseLength, rightSequence[0] + 1);

decreaseLength = Math.max(decreaseLength, rightSequence[1] + 1);

// Update the longest streak result by taking the maximum sum of increasing and

longestStreak = Math.max(longestStreak, increaseLength + decreaseLength - 1);

reset it, is done at every node. This leads to each node being visited exactly once.

// decreasing lengths from the current node minus 1 (to avoid double-counting the node)

// Return a pair of the longest increasing and decreasing sequences starting from the current node

if (root.right.val + 1 === root.val) {

if (root.right.val - 1 === root.val) {

return [increaseLength, decreaseLength];

Therefore, the time complexity of the DFS is O(N), where N is the number of nodes in the tree. This is because the function processes each node a single time without revisiting anything.

space used for storing the variables in each recursive call.

to an average case space complexity of O(log N).

Space Complexity The space complexity of the algorithm includes the space used by the recursive call stack during the DFS traversal as well as the

The provided code executes a depth-first search (DFS) on a binary tree. For every node, it calculates the longest consecutive

sequence that can be formed both increasing and decreasing. The decision to increment or decrement the consecutive count, or to

In the worst case, the height of the binary tree may be O(N) (in case of a skewed tree where each node has only one child), which would imply O(N) recursive calls stack space would be used. For balanced trees, the average case height would be O(log N) leading

The ans variable used to store the maximum length of the consecutive sequence doesn't significantly affect the space complexity as it is a single integer value.

Hence, the space complexity is O(N) in the worst case, but in the average case for a balanced tree, it would be $O(\log N)$.