3108. Minimum Cost Walk in Weighted Graph

Description

There is an undirected weighted graph with n vertices labeled from 0 to n - 1.

You are given the integer [n] and an array [edges], where $[edges[i] = [u_i, v_i, w_i]$ indicates that there is an edge between vertices $[u_i]$ and $[v_i]$ with a weight of $[w_i]$.

A walk on a graph is a sequence of vertices and edges. The walk starts and ends with a vertex, and each edge connects the vertex that comes before it and the vertex that comes after it. It's important to note that a walk may visit the same edge or vertex more than once.

The **cost** of a walk starting at node [u] and ending at node [v] is defined as the bitwise [AND] of the weights of the edges traversed during the walk. In other words, if the sequence of edge weights encountered during the walk is $[w_0, w_1, w_2, \ldots, w_k]$, then the cost is calculated as $[w_0, w_1, w_2, \ldots, w_k]$, where [a, b] denotes the bitwise [a, b] operator.

You are also given a 2D array query, where query[i] = [s i, t i]. For each query, you need to find the minimum cost of the walk starting at vertex s i and ending at vertex t i. If there exists no such walk, the answer is -1.

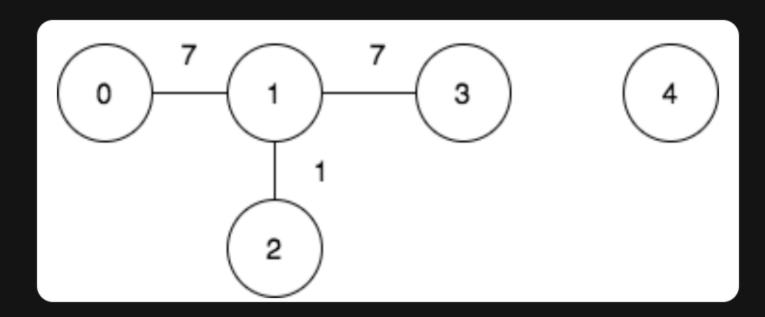
Return the array answer, where answer[i] denotes the minimum cost of a walk for query i.

Example 1:

Input: n = 5, edges = [[0,1,7],[1,3,7],[1,2,1]], query = [[0,3],[3,4]]

Output: [1,-1]

Explanation:



To achieve the cost of 1 in the first query, we need to move on the following edges: 0->1 (weight 7), 1->2 (weight 1), 2->1 (weight 1), 1->3 (weight 7).

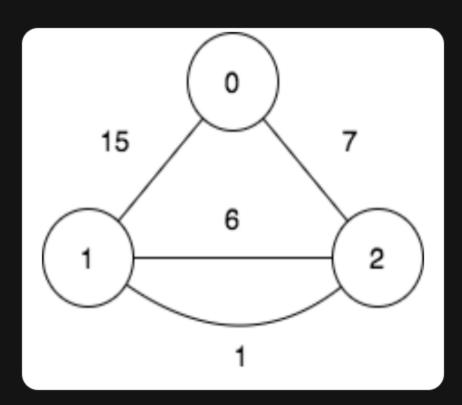
In the second query, there is no walk between nodes 3 and 4, so the answer is -1.

Example 2:

Input: n = 3, edges = [[0,2,7],[0,1,15],[1,2,6],[1,2,1]], query = [[1,2]]

Output: [0]

Explanation:



To achieve the cost of 0 in the first query, we need to move on the following edges: 1->2 (weight 1), 2->1 (weight 6), 1->2 (weight 1).

Constraints:

- 2 <= n <= 10 ⁵
- 0 <= edges.length <= 10^{5}
- edges[i].length == 3
- $0 \leftarrow u_i, v_i \leftarrow n-1$
- u i != v i
- $0 \ll w_i \ll 10^5$
- 1 <= query.length <= 10 ⁵
- query[i].length == 2
- $0 \ll s_i$, $t_i \ll n 1$
- s i != t i