838. Push Dominoes **Two Pointers** String ) Medium **Dynamic Programming Leetcode Link** 

# **Problem Description**

domino. A domino can either be standing vertically (.), pushed to the left (L), or pushed to the right (R). The string represents the initial configuration of the dominoes at time zero. When dominoes are pushed, they start falling and can cause adjacent dominoes to fall as well. If a domino is pushed to the left, it will

In this problem, we're given a line of dominoes represented by a string of characters, with each character indicating the state of a

make its left neighbor fall to the left in the next second, and similarly for the right. However, if dominoes are falling towards each other, they will make the domino in between them stand still (.) as the forces from both sides will cancel.

The objective is to determine the final state of all dominoes after all movements have stopped – which is when no further dominoes are being pushed over by their neighbors.

Intuition The solution approach deals with the propagation of the falling action among dominoes. A key observation is to keep track of the

time it takes for each domino to fall and the direction of the force applied to it. By initializing a queue to store the indices of dominoes

# that have been pushed, we can process each one by one.

We use Breadth-First Search (BFS) to simulate the domino effect. BFS is useful for problems where we need to propagate information (or in this case, force) level by level, from neighbor to neighbor. We start by adding indices with 'L' or 'R' to the queue and setting their time to 0 since these are the starting points of the falling process.

pushed (time[j] is -1) or at the same time from the opposite side (time[j] == t + 1). If a domino receives force from both sides at

the same time, it will remain standing - which is ensured by storing all forces in a force list and checking its length. When a domino

As we dequeue an index, we apply its force to its respective neighbor if the conditions allow - that is if the neighbor hasn't been

gets only one direction of force, we proceed with the domino effect in that direction, queuing up the next domino in line.

In the end, we join and return the resulted string, which is the final state of the dominoes. **Solution Approach** The implementation uses a combination of Breadth-First Search (BFS), a queue, a time array, and a force dictionary – each element

**Data Structures:** 

forces acting on it to the force dictionary. Also, each such domino's index is added to the q.

playing a specific role in simulating the domino effect.

## us to easily add new dominoes that start falling and process dominoes in the order they were pushed. • Time Array (time): An array that holds the time at which each domino falls. If a domino has not fallen, it is marked with -1. This

helps in determining if a neighboring domino should be pushed (if it is still untouched) or to detect simultaneous pushes (a domino pushed at the same time from both sides).

• Queue (q): A double-ended queue deque is used for BFS to store the indices of the dominoes that are currently falling. It allows

### • Force Dictionary (force): A defaultdict with list values used to track all forces acting on a domino. If a domino is pushed at the same time from both sides, this can be detected when the length of the list for that index is greater than 1.

**Algorithm:** 

1. Iterate through the dominoes string, and for each domino that is not upright ('.'), initialize the time at this index to 0 and add the

- 2. Start processing the queue until it's empty: Dequeue an index i and check the forces acting on it.
- o If there's only one force (len(force[i]) == 1): Set the ans array at position i to the current force f.

• If the neighbor is being pushed at the same time (time[j] == t + 1), add the force to it.

3. Once the queue is empty, join the ans array into a string representing the final state of the dominoes and return it.

■ Calculate the index j of the adjacent domino to push based on the current force's direction (j = i - 1 if f == 'L' and j

# ■ If the neighbor has not been pushed yet (time[j] == -1), update its time to t + 1, add its force, and enqueue index

= i + 1 if f == 'R').

If j is within bounds:

j.

arrangement of dominoes.

**Example Walkthrough** 

1. Initialize data structures:

∘ q: []

o dominoes: ..R...L..

 $\circ$  time: [-1, -1, 0, -1, -1, -1, 0, -1, -1]

Let's illustrate the solution approach with a small example, using the initial string of dominoes ..R...L... Here's how the algorithm processes this string:

By following this approach, the algorithm simulates the force propagation, domino interaction, and stabilization to output the final

o force: {2: ['R'], 6: ['L']} 2. Fill the queue with indices of pushed dominoes and their respective times and forces:

## Dequeue index 2, the force is ['R'], so we push the domino at index 3.

5. Resolve conflicts:

6. Output the final state:

..RR.L....

(previous time + 1).

3. Process the queue:

 Dequeue index 6, the force is ['L'], so we push the domino at index 5. 4. Continue the BFS: At index 3, since there was no push from the left, the domino falls to the right and we enqueue index 4 with a time of 1

At index 5, since there is no push from the right, the domino falls to the left and we enqueue index 4 with a time of 1.

Since there are no more dominoes to process, we concatenate our finalized ans array to get the final state of the dominoes:

 At index 4, we have enqueued this index twice (once from the right and once from the left) both with time 1. When dequeued, the force dictionary shows two forces acting on this domino, ['R', 'L'], so it stays upright.

arrived at the final arrangement without any iterative comparison.

def pushDominoes(self, dominoes: str) -> str:

# Queue to hold the indices of dominoes to process

# Array to hold the time when each dominoe falls

# Initialize the queue, fall\_time, and forces

for index, force in enumerate(dominoes):

forces[index].append(force)

queue.append(index)

fall\_time[index] = 0

current\_idx = queue.popleft()

if len(forces[current\_idx]) == 1:

resultant\_force = forces[current\_idx][0]

current\_time = fall\_time[current\_idx]

fall\_time[next\_idx] = current\_time + 1

elif fall\_time[next\_idx] == current\_time + 1:

forces[next\_idx].append(resultant\_force)

forces[next\_idx].append(resultant\_force)

# Additionally, the comments provide a clear explanation of each part of the algorithm.

// If only one force is affecting the index, update the result

int nextIdx = force == 'L' ? idx - 1 : idx + 1;

times[nextIdx] = currentTime + 1;

} else if (times[nextIdx] == currentTime + 1) {

int numDominoes = dominoes.size(); // Get the size of the string representing the dominoes.

// Vector to store the time at which each domino is tipped. Initialize with -1 (untipped).

// Queue to keep track of indices of dominoes which have been tipped or will be tipped.

// Multiple forces can only act during the same time unit, hence using strings.

if (dominoes[i] == '.') continue; // Skip if the domino has not been tipped.

forces[i].push\_back(dominoes[i]); // Record the initial force ('L' or 'R')

int index = waitingQueue.front(); // Get the current index to be processed.

// Calculate the adjacent index. Left for 'L', Right for 'R'.

char forceDirection = forces[index][0]; // Get the force direction 'L' or 'R'.

finalState[index] = forceDirection; // Tip the domino in the final state.

int adjacentIndex = (forceDirection == 'L') ? (index - 1) : (index + 1);

forces[nextIdx].add(force);

forces[nextIdx].add(force);

// Vector of strings to store the forces acting on each domino.

waitingQueue.emplace(i); // Add the index to the queue.

// If only one force is acting on the domino, process it.

tipTime[i] = 0; // Tipped at time 0 (initial state)

// String to store the final state of the dominoes.

if (nextIdx >= 0 && nextIdx < length) {</pre>

int currentTime = times[idx];

queue.offer(nextIdx);

if (times[nextIdx] == -1) {

next\_idx = current\_idx - 1 if resultant\_force == 'L' else current\_idx + 1

result[current\_idx] = resultant\_force

if fall\_time[next\_idx] == -1:

queue.append(next\_idx)

if 0 <= next\_idx < num\_dominoes:</pre>

# Return the final dominoes state as a string

46 # The code now uses more standard and descriptive variable names.

int idx = queue.poll();

if (forces[idx].size() == 1) {

// Convert char array to string and return

return new String(result);

string pushDominoes(string dominoes) {

vector<int> tipTime(numDominoes, -1);

vector<string> forces(numDominoes);

string finalState(numDominoes, '.');

// Process each domino in the queue.

if (forces[index].size() == 1) {

while (!waitingQueue.empty()) {

waitingQueue.pop();

for (int i = 0; i < numDominoes; i++) {</pre>

queue<int> waitingQueue;

result[idx] = force;

char force = forces[idx].get(0);

# Length of the dominoes string

 $fall_time = [-1] * num_dominoes$ 

**if** force != '.':

# Resultant dominoes state

# Process the queue

return ''.join(result)

while queue:

result = ['.'] \* num\_dominoes

num\_dominoes = len(dominoes)

queue = deque()

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C++ Solution

public:

class Solution {

The domino at index 2 is pushed to the right, so we add 2 to q.

• The domino at index 6 is pushed to the left, so we add 6 to q.

**Python Solution** from collections import deque, defaultdict class Solution:

In this way, using BFS and the associated data structures, we've efficiently simulated the entire domino chain-reaction and have

13 14 # Dictionary to hold the force(s) acting on each dominoe 15 forces = defaultdict(list) 16

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Java Solution 1 public class Solution { public String pushDominoes(String dominoes) { int length = dominoes.length(); // Queue to keep track of indices in the dominoes string that are affected by forces Deque<Integer> queue = new ArrayDeque<>(); // Array to keep track of the time when each force reaches an index 6 int[] times = new int[length]; // Initialize all times to -1 (indicating no force has reached the index) 8 Arrays.fill(times, -1); 9 10 // List to store forces affecting each index (as multiple forces can affect the same index) 11 List<Character>[] forces = new List[length]; 12 for (int i = 0; i < length; ++i) {</pre> 13 forces[i] = new ArrayList<>(); 14 15 16 // Initialize the forces and times with the initial state. Also add indices to queue to process for (int i = 0; i < length; ++i) {</pre> 17 18 char force = dominoes.charAt(i); **if** (force != '.') { 19 20 queue.offer(i); 21 times[i] = 0;22 forces[i].add(force); 23 24 25 26 // Array to store the final state of the dominoes 27 char[] result = new char[length]; 28 Arrays.fill(result, '.'); 29 30 // Process the queue until it is empty while (!queue.isEmpty()) { 31

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// Check if the adjacent index is within bounds. 40 if (adjacentIndex >= 0 && adjacentIndex < numDominoes) {</pre> int currentTime = tipTime[index]; // Get the current time. 41 42 43 // Tip the next domino if it hasn't been tipped yet. 44 if (tipTime[adjacentIndex] == -1) { 45 waitingQueue.emplace(adjacentIndex); // Add index to the queue. 46 tipTime[adjacentIndex] = currentTime + 1; // Update the time. 47 forces[adjacentIndex].push\_back(forceDirection); // Apply the force. 48 // If the next domino is tipped at the same time, it means forces are colliding. } else if (tipTime[adjacentIndex] == currentTime + 1) 49 50 forces[adjacentIndex].push\_back(forceDirection); // Forces collide. 51 52 53 // Collision case is implicitly handled by not tipping the domino in the final state. 54 55 return finalState; // Return the final state of the dominoes 56 57 58 }; 59 **Typescript Solution** function pushDominoes(dominoes: string): string { const length = dominoes.length; // Mapping the input characters to numerical values for easy processing const dominoMap = { 'L': -1, 'R': 1, '.': 0, 8 **}**; // Initialize the result array with numerical values 9 let result = new Array(length).fill(0); 10 11 // Track visited positions with their propagation depth 12 let visited = new Array(length).fill(0); 13 // Queue for BFS (Breadth-First Search) to track dominos to process let queue: number[] = []; 14 15 // Start with depth 1 (first level of BFS) let currentDepth = 1; 16 17 18 // Set up the queue with initial domino positions for (let index = 0; index < length; index++) {</pre> 19 20 let dominoValue = dominoMap[dominoes.charAt(index)]; 21 if (dominoValue) { 22 queue.push(index); 23 visited[index] = currentDepth; 24 result[index] = dominoValue; 25 26 27 28 // Process the queue using BFS 29 while (queue.length) { 30 currentDepth++; 31 let nextLevel: number[] = []; 32 for (let position of queue) { 33 const direction = result[position]; 34 let newPosition = position + direction; // If not out of bounds and not visited at current level or blocked 35 if (newPosition >= 0 && newPosition < length && [0, currentDepth].includes(visited[newPosition])) {</pre> 36 result[newPosition] += direction; 37 38 visited[newPosition] = currentDepth;

## space complexity analysis are as follows: **Time Complexity:**

Time and Space Complexity

queue = nextLevel;

.map(value => {

.join('');

else return 'R';

return result

})

nextLevel.push(newPosition);

if (value === 0) return '.';

else if (value < 0) return 'L';</pre>

// Convert the numerical result back into domino state characters

2. The while loop processes each domino at most twice - once for each possible push direction ('L' or 'R'). The main processing within the while loop executes in constant time for each element, except for the deque operations. 3. The popleft operation from deque q is O(1) amortized per element.

4. Checking and updating the force at index j is also O(1) for each element since list append and length check are constant time

The overall time complexity of the loop is O(n), because each element is dealt with in constant time and the queue ensures that each

1. The initialization of time and force, as well as the enumeration of dominoes to populate the queue q: O(n), since every domino is

The given code simulates the process of pushing dominoes. Let n be the length of the string dominoes. The time complexity and

### operations. 5. Hence, every element can be inserted into the queue at most twice, once for being pushed to the left, and once for being pushed to the right.

processed once.

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**Space Complexity:** 1. The time list, force dictionary, and ans list each require O(n) space.

3. The force dictionary has lists, but each index i in force will have at most two forces (pushed from left and right) if dominoes at index i falls due to being pushed by both sides. So, space required by force values (lists) still remains within O(n) overall.

Thus, the space complexity is O(n) + O(n) + O(n) = O(n).

2. The q can have at most n elements in the worst case when all dominoes are getting pushed.

element is processed at most twice. Therefore, the total time complexity is O(n) + O(n) = O(n).