334. Increasing Triplet Subsequence

Medium





Problem Description

The problem gives us an array of integers, nums, and asks us to determine if it is possible to find a sequence of three elements, where each element comes after the previous one in the order they appear in the array (i.e., they have increasing indices), and each element is greater than the one before it in this sequence. This sequence should satisfy the condition nums[i] < nums[j] < nums[k], where i, j, and k are the indices of these elements in the array, such that i < j < k. If such a sequence exists in nums, the function should return true, otherwise, it should return false.

This can be visualized as checking if there's an ascending subsequence of at least three numbers within the original array. It's essentially a question about identifying a pattern within a sequence without reordering it or changing the values.

Intuition

To arrive at the solution efficiently, instead of looking for the whole triplet right away, we can keep track of the smallest number we have encountered so far (mi) and a middle number that is greater than mi but smaller than any potential third number (mid). As we iterate through the array, we can update these two numbers whenever possible. The idea here is to maintain the lowest possible values for mi and mid as we move forward, giving us the best chance to find a number that would be greater than both, thus forming our triplet.

- If the current number (num) is less than or equal to mi, it becomes the new mi because we're always interested in the smallest starting point of the potential triplet.
- If num is greater than mi but less than mid, we have found a possible middle part of our triplet, so we set mid to this new number. • If num is greater than mid, this means we have successfully found a triplet (because num is greater than both mi and mid, which
- also implies that mi is less than mid), and we can return true. This efficient approach uses a greedy-like method to continuously look for the most optimal mi and mid with the hope of finding a

third number that could fit the sequence. It does so using a linear scan and constant extra space, without the need for sorting or extra arrays.

The Reference Solution Approach begins with the creation of two variables: mi and mid, both initialized to inf (infinity). Here's the

Solution Approach

reasoning for each line of code:

• mi and mid serve as placeholders to store the smallest and middle elements of the potential increasing triplet subsequence. By initializing them to infinity, it ensures that any number in the array will be smaller, allowing for proper updating of these variables.

A for loop iterates through the nums array.

The main algorithm unfolds within a single pass through the array of numbers (nums):

- For each num in nums, there is a series of checks and updates:
- if num > mid: This is the condition that tells us we have found a valid triplet. If the current num is greater than our mid value,
 - then we already have a mi which is less than mid, and hence, we have found a sequence where mi < mid < num. We return True immediately. o if num <= mi: If the current num is smaller than or equal to the current smallest value mi, it means that we can potentially
 - start a new triplet sequence with this num as the smallest element, thus we update mi with the value of num. • else: If the current num is greater than mi and not greater than mid, it fits between the mi and mid, so we update the mid to be
 - num since it could potentially be the middle element of a valid triplet.

—or the algorithm completes the array iteration without finding a triplet, resulting in a return value of False. It's important to note that the code uses a greedy approach to always maintain the smallest possible values for mi and mid as it

As the for loop continues, mi and mid are updated accordingly until either a valid triplet is found—causing the function to return True

iterates over nums. By consistently updating these with the smallest possible values at each step, it optimizes the chance of finding a valid triplet later in the array. No additional data structures are necessary, making this solution notably efficient with O(n) time complexity (due to single iteration through the array) and O(1) space complexity (using only two extra variables).

Let's illustrate the solution approach using a small example where our input nums array is [1, 2, 3, 4, 5].

Example Walkthrough

• We initialize mi and mid to infinity. Current state: mi = inf, mid = inf. We iterate over the array:

- We compare the first element, 1, with mid. Since 1 < inf, we cannot form a triplet yet, but 1 becomes our new mi. Updated
- - state: mi = 1, mid = inf. • We move to the next element, 2. Now, 2 is greater than mi but still less than mid. So, 2 becomes our new mid. Updated state:
 - mi = 1, mid = 2. Next element is 3. It is greater than both mi and mid. We now have a valid triplet: 1 < 2 < 3. Hence, according to our solution approach, we return True. There is no need to check the remaining elements (4 and 5) because we have successfully found
- an increasing triplet. In this example, the approach quickly identifies the increasing sequence with the satisfaction of the conditions outlined in the

Python Solution

problem description. The algorithm efficiently updates mi and mid and only stops when it confirms the existence of the increasing

def increasingTriplet(self, nums: List[int]) -> bool: # Initialize two variables with infinity which will # represent the smallest and middle numbers of the triplet.

smallest = float('inf')

public boolean increasingTriplet(int[] nums) {

int smallest = Integer.MAX_VALUE;

int middle = Integer.MAX_VALUE;

middle = float('inf')

class Solution:

triplet.

```
# Iterate over the list of numbers.
           for num in nums:
9
10
               # If current number is greater than the middle number,
               # an increasing triplet exists.
11
               if num > middle:
12
13
                   return True
14
15
               # If current number is less than or equal to the smallest,
16
               # update the smallest number to be the current number.
               if num <= smallest:</pre>
                   smallest = num
ΤO
               # Otherwise, if the current number is between the smallest
               # and the middle, update the middle number.
21
               else:
22
                   middle = num
23
           # Return False if no increasing triplet is found.
24
25
            return False
26
Java Solution
   class Solution {
       // Method to check if there exists an increasing triplet in the array.
```

// Initialize two variables to hold the smallest and the middle value found so far.

// Iterate over each number in the array.

```
for (int num : nums) {
               // If the current number is greater than the middle value found,
11
               // an increasing triplet sequence exists.
               if (num > middle) {
                    return true;
14
15
16
               // If the current number is the smallest we've seen so far,
17
               // we update the smallest value.
18
19
               if (num <= smallest) {</pre>
20
                   smallest = num;
               } else {
                   // Otherwise, if it's between the smallest and the middle value,
23
                   // we update the middle value.
24
                   middle = num;
25
27
           // If we did not return true within the loop, then no increasing
29
           // triplet sequence was found.
           return false;
30
31
32 }
33
C++ Solution
 1 #include <vector>
 2 #include <climits> // Include for INT_MAX
   class Solution {
   public:
       // This function checks if there exists an increasing triplet subsequence
       // The sequence is increasing if nums[i] < nums[j] < nums[k] where i < j < k
```

13 // Iterate over the input vector 14 for (int num : nums) { // If we find a number greater than second smallest,

// Parameters:

nums - a vector of integers

bool increasingTriplet(std::vector<int>& nums) {

```
// this means we found a triplet; return true
               if (num > secondMin) {
19
                    return true;
20
21
               // If current number is less than or equal to firstMin,
               // update firstMin to the current number
24
               if (num <= firstMin) {</pre>
25
                   firstMin = num;
26
                } else {
                   // If current number is between firstMin and secondMin
                   // update secondMin to the current number
                   // This is because we want the smallest possible value for secondMin
                   // that is greater than firstMin
                    secondMin = num;
31
32
33
34
           // If we have reached this point, it means we did not find
35
           // an increasing triplet subsequence
37
           return false;
38
39 };
40
Typescript Solution
   /**
    * Checks whether there exists an increasing triplet subsequence within the array
    * @param nums - Array of numbers to check for the increasing triplet
    * @returns boolean - True if there is an increasing triplet, False otherwise
    */
   function increasingTriplet(nums: number[]): boolean {
        let length = nums.length;
       // If the array has fewer than 3 items, it can't have an increasing triplet
       if (length < 3) return false;</pre>
10
```

int firstMin = INT_MAX; // Store the smallest number encountered

int secondMin = INT_MAX; // Store the second smallest number encountered

```
// Initialize the smallest and middle values in the triplet
12
       let smallest = nums[0];
13
       let middle = Number.MAX_SAFE_INTEGER;
14
15
16
       // Iterate through the array to find the increasing triplet
       for (let number of nums) {
           if (number <= smallest) {</pre>
               // Current number becomes the new smallest if it's smaller or equal to the current smallest
                smallest = number;
           } else if (number <= middle) {</pre>
               // Current number is greater than smallest but smaller or equal to middle,
22
               // so it becomes the new middle
               middle = number;
25
           } else {
               // If we found a number greater than both smallest and middle, we found an increasing triplet
26
               return true;
28
29
30
       // If no increasing triplet is found, return false
31
       return false;
32
33 }
34
```

which consume a constant amount of space.

Time and Space Complexity The time complexity of the given code is O(n) where n is the number of elements in the nums list. This is because the code iterates

through the entire nums list once with a single loop, and within each iteration, it performs a constant number of operations. The space complexity of the given code is 0(1) regardless of the size of the input list. It uses only two extra variables, mi and mid,