783. Minimum Distance Between BST Nodes **Breadth-First Search Binary Search Tree** 

## **Problem Description**

**Depth-First Search** 

The task is to find the minimum difference (also known as the minimum absolute difference) between the values of any two different nodes in a Binary Search Tree (BST). Remember, a BST has the property that all left descendants of a node have values less than the node's value, and all right descendants have values greater than the node's value. This property can be utilized to find the minimum

**Binary Tree** 

**Leetcode Link** 

## difference in an efficient way.

Intuition To solve this problem, we need to consider the properties of a BST and how they can help in finding the minimum difference. In a

The solution uses a recursive depth-first search (DFS) strategy to perform the in-order traversal. During the traversal: 1. Visit the left subtree.

BST, an in-order traversal results in a sorted sequence of values. The smallest difference between any two nodes is likely to be

2. Process the current node: Compare the current node's value with the value of the previous node (which is the closest smaller value since we are doing

between two adjacent nodes in this sorted order. So, the solution involves performing an in-order traversal of the tree.

in-order traversal). • Update the minimum difference (ans) if the current difference is less than the previously recorded minimum difference.

node's value we visited.

- 3. Visit the right subtree.
- The nonlocal keyword is used for the variables ans and prev inside the dfs helper function to update their values across recursive

calls. This is necessary because ans keeps track of the current minimum difference we have found, and prev keeps track of the last

Initially, we set ans to infinity (inf in Python) to ensure any valid difference found will be smaller and thus update ans. The prev variable is initialized to infinity as well since we have not encountered any nodes before the traversal. The algorithm starts by calling

minimum difference that it finds. By the time we are done with the in-order traversal, ans holds the minimum difference between any two nodes in the BST, and we

the dfs helper function with the root of the BST, which then recursively performs the in-order traversal and updates ans with the

return it as the result. **Solution Approach** 

The implementation of the solution is based on a Depth-First Search (DFS) algorithm performing an in-order traversal of the Binary

Search Tree (BST). A traversal is in-order if it visits the left child, then the node itself, and then the right child recursively. This

approach leverages the BST's property that an in-order traversal results in a sorted sequence of node values.

Here are the steps in the algorithm, along with how each is implemented in the solution:

# • A recursive method dfs(root) is defined, where root is the current node in the traversal. If root is None, the function returns

1. Depth-First Search (DFS):

immediately, as there's nothing to process (base case for the recursion). • The dfs function is called with the left child of the current node, dfs(root.left), to traverse the left subtree first. 2. Processing Current Node:

• The current node's value is compared with the last node's value stored in the variable prev (initialized at infinity to start

• A nonlocal variable ans is used to keep track of the minimum difference encountered throughout the traversal. If the current

with). The difference is calculated as abs(prev - root.val). 3. **Updating Minimum Difference:** 

difference is less than ans, we update ans with this new minimum.

structures are needed since the problem can be solved with the traversal alone.

any two nodes in the BST by leveraging its properties and an in-order DFS.

Let's say we have a Binary Search Tree (BST) with the following structure:

than infinity, so ans is updated to 1. Prev is now updated to 2.

-4 = 2, which is greater than ans. Thus, no update is made.

def \_\_init\_\_(self, val=0, left=None, right=None):

1. Since ans is already 1, it does not get updated.

Once we are at the leftmost node, which has no left child, the processing of nodes begins.

- The variable prev is updated with the current node's value, root.val, to ensure it's always set to the value of the last node visited.
- 4. Recursive Right Subtree Traversal: After processing the current node, the function calls itself with the right child of the current node, dfs(root.right), thus exploring the right subtree.
- values need to be retained across those calls. A Python class named Solution contains the method minDiffInBST which initiates the DFS with the first call to dfs(root). The inf

The use of the nonlocal keyword is key here, as ans and prev are updated by the recursive calls within the dfs function, and their

value is imported from Python's math module and represents infinity, used for comparison purposes to ensure the actual difference

The ans is initialized with inf so that the first computed difference (which will be finite) will become the new minimum. The prev

Data Structure: The recursive stack is the implicit data structure used here for the DFS implementation. No additional data

variable is also initialized outside the dfs function to inf in order to manage the case when the first node (the smallest value in the

Once the entire tree has been traversed, the ans variable will hold the smallest difference found between any two nodes.

always replaces the initial value.

BST) has no predecessor.

5. Result:

Example Walkthrough

Considering the algorithm and pattern applied, the solution efficiently finds and returns the minimum absolute difference between

1. We initiate a Depth-First Search (DFS) from the root of the BST, which is the node with value 4. 2. The DFS will first go to the left subtree (value 2). Since 2 also has a left child, the DFS will go further left, reaching all the way to node 1, which is the leftmost node and has no children.

3. Node 1 is processed, and since it's the first node, there's no previous node to compare with, so prev is set to this node's value

4. The DFS backtracks to node 2, and 2 is compared with the previous node 1. The absolute difference is 2 - 1 = 1, which is less

6. DFS backtracks to the root node 4, but we've already processed its left subtree. Now, we compare 4 with the previous node 3.

7. The DFS proceeds to the right child of root, node 6. We calculate the difference between the previous node 4 and 6, giving us 6

The absolute difference is 4 - 3 = 1, which is the same as ans, so no update to ans is made. Prev is updated to 4.

The process concludes by returning 1 as the minimum difference between the values of any two different nodes in the BST.

## 5. The DFS then moves to the right child of node 2, which is node 3. The difference between 3 and the previous node 2 is 3 - 2 =

(1). The ans is still infinity at this point.

# Definition for a binary tree node.

self.val = val

self.left = left

self.right = right

return

in\_order\_traversal(root)

TreeNode(int val) { this.val = val; }

private void dfs(TreeNode node) {

if (node == null) {

prevValue = node.val;

// Definition for a binary tree node.

minDifference = INF;

previousValue = -INF;

return minDifference;

inOrderTraversal(root);

// compute the minimum difference.

void inOrderTraversal(TreeNode\* node) {

// If the node is null, return immediately.

dfs(node.right);

return;

dfs(node.left);

// Base case: if the node is null, just return

TreeNode(int val, TreeNode left, TreeNode right) {

return min\_difference

# Traverse the left subtree

# Process the current node

previous\_value = node.val

# Traverse the right subtree

in\_order\_traversal(node.right)

# Return the minimum difference found

in\_order\_traversal(node.left)

nonlocal min\_difference, previous\_value

# Update the smallest difference and the previous value

min\_difference = min(min\_difference, node.val - previous\_value)

# Call the helper function to start in-order traversal from the root

class TreeNode:

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C++ Solution

struct TreeNode {

- 8. The traversal ends as there are no more nodes to visit. Our minimum difference ans is 1, which is the minimum absolute difference between any two nodes in this BST.
- Python Solution
- class Solution: def minDiffInBST(self, root: TreeNode) -> int: 9 # Helper function for depth-first search traversal of the binary tree 10 def in\_order\_traversal(node): 11 if node is None:

27 # Initialize the minimum difference as infinity 28 # The prev variable is used to keep track of the previous node's value 29 # Because the initial "previous value" is not defined, we use infinity 30 min\_difference, previous\_value = float('inf'), float('-inf') 31

Java Solution // Definition for a binary tree node.

2 class TreeNode {

int val;

TreeNode left;

TreeNode() {}

TreeNode right;

this.val = val;

this.left = left; 10 this.right = right; 11 12 13 14 class Solution { // Variable to store the minimum difference 16 private int minDifference; 17 // Variable to keep track of the previously visited node's value in in-order traversal 18 private int prevValue; // A large value to initialize minDifference and prevValue. It signifies "infinity". 20 private final int INF = Integer.MAX\_VALUE; 21 22 23 // Public method to find the minimum difference between values of any two nodes in a BST public int minDiffInBST(TreeNode root) { 24 25 // Initialize minDifference to "infinity" as we look for the minimum value 26 minDifference = INF; // Initialize prevValue to "infinity" to handle the edge case of the first node 28 prevValue = INF; 29 // Call the helper method to do a depth-first search starting from the root 30 dfs(root); 31 // Return the minimum difference found return minDifference;

// Helper method to perform in-order traversal and find the minimum difference

// Recursively call dfs for the left subtree to visit nodes in in-order

// between the current node's value and the previous node's value

#include <algorithm> // Include algorithm header for std::min function

// Update the minimum difference with the smallest difference found so far

// Update the prevValue to the current node's value for subsequent iterations

// Recursively call dfs for the right subtree to continue in-order traversal

minDifference = Math.min(minDifference, Math.abs(node.val - prevValue));

int val; TreeNode \*left; TreeNode \*right; TreeNode() : val(0), left(nullptr), right(nullptr) {} 8 TreeNode(int x) : val(x), left(nullptr), right(nullptr) {} 9 TreeNode(int x, TreeNode \*left, TreeNode \*right) : val(x), left(left), right(right) {} 10 11 }; 12 13 class Solution { 14 public: // Initialize the maximum possible value for an integer as infinity. // This will be used to calculate the minimum difference. static const int INF = INT MAX; 17 18 19 // Variable to hold the current minimum difference found in the BST. 20 int minDifference; 21 // Variable to keep track of the previous node's value during in-order traversal. 22 23 int previousValue; 24 25 // Constructor initializes member variables. 26 Solution() : minDifference(INF), previousValue(-INF) {} 27 28 // Function to find the minimum difference between any two nodes in the BST. int minDiffInBST(TreeNode\* root) { 29

// Start the depth-first search (in-order traversal) of the tree.

// Helper function to perform in-order traversal on the BST and

// After the traversal, minDifference will hold the minimum difference.

// Reset the minDifference and previousValue before reusing the solution instance.

43 if (!node) return; 44 45 // Traverse the left subtree first. 46 inOrderTraversal(node->left); 47 48 // If previousValue is not set to the initial value (which is —INF here), // update the minDifference with the minimum of current minDifference and 49 50 // the difference between the current node's value and previousValue. if (previousValue != -INF) { 51 52 minDifference = std::min(minDifference, abs(node->val - previousValue)); 53 // Update previousValue to hold the current node's value for the next comparison. 54 55 previousValue = node->val; 57 // Traverse the right subtree. inOrderTraversal(node->right); 59 60 }; 61

constructor(val: number = 0, left: TreeNode | null = null, right: TreeNode | null = null) {

// Note that we don't have to reset minDifference and previousValue here // because they're not part of a class instance anymore. function minDiffInBST(root: TreeNode | null): number { // Initialize minDifference and previousValue for a new computation. minDifference = INFINITY;

Typescript Solution

left: TreeNode | null;

this.val = val;

this.left = left;

this.right = right;

let minDifference: number;

let previousValue: number;

previousValue = -INFINITY;

inOrderTraversal(node.left);

previousValue = node.val;

// Traverse the right subtree.

Time and Space Complexity

if (previousValue !== -INFINITY) {

inOrderTraversal(root);

right: TreeNode | null;

class TreeNode {

val: number;

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// Definition for a binary tree node.

const INFINITY = Number.MAX\_SAFE\_INTEGER;

// The maximum possible value for a number in JavaScript.

// Variable to hold the current minimum difference found in the BST.

// Variable to keep track of the previous node's value during in-order traversal.

// Function to find the minimum difference between any two nodes in the BST.

// Start the depth-first search (in-order traversal) of the tree.

34 // After the traversal, minDifference will hold the minimum difference. 35 return minDifference; 36 } 37 // Helper function to perform in-order traversal on the BST and // compute the minimum difference. function inOrderTraversal(node: TreeNode | null) { // If the node is null, return immediately. if (node === null) return; 43 // Traverse the left subtree first.

// If previousValue is not set to the initial value (which is —INFINITY here),

minDifference = Math.min(minDifference, Math.abs(node.val - previousValue));

// Update previousValue to hold the current node's value for the next comparison.

// update the minDifference with the minimum of current minDifference and

// the difference between the current node's value and previousValue.

inOrderTraversal(node.right);

in-order traversal visits each node exactly once.

Here's the analysis of its complexity: • Time Complexity: The time complexity of the function is O(n), where n is the number of nodes in the BST. This is because the

The given code performs an in-order traversal of a binary search tree (BST) to find the minimum difference between any two nodes.

- Space Complexity: The space complexity of the recursive in-order traversal is O(h), where h is the height of the BST. This accounts for the call stack during the recursive calls. In the worst case of a skewed BST, the height h can become n, which
- would make the space complexity O(n). In a balanced BST, however, the space complexity would be  $O(\log n)$ .

Tree

Easy