

Problem Description

The problem is to find the smallest positive integer (x) that can be formed such that the product of all its digits equals a given positive integer (num). For instance, if num is 18, x could be 29 (since 2 * 9 = 18). We want to find the smallest such x if it exists.

However, there are a couple of constraints: if x does not exist or it is not a 32-bit signed integer (which means x must be less than 2^31), the function should return 0.

Intuition

1. To minimize x, we should try to use the largest digits possible (except for 0 and 1 since they don't change the product). Hence, we should start

To find the smallest integer x meeting our criteria, we need to consider a couple of key observations:

- checking from 9 down to 2. 2. Digits must multiply to num, so we'll repeatedly divide num by these digits, ensuring divisibility at each step.
- 3. We build x by appending digits to its right, meaning we first find the highest place-value digit and then move towards the lower ones.
- The approach works by iterating from 9 to 2 and checking if num can be evenly divided by these digits. When it can, the digit divides num, and itself is added to what will become x. This process repeats until num is reduced to 1 (if it can't be reduced to 1, x is

not possible under the problem constraints). After each division, we scale x up by a factor of 10 (to push previously added digits leftward) before adding the new digit. In the end, x must be within the 32-bit signed integer range, or else we return 0. **Solution Approach**

The implementation follows the intuition closely and uses a straightforward iterative method, with primary focus on the following

steps:

Early return for numbers less than 2: Given that our smallest possible positive integer that is not 1 must consist of multiple digits, the cases where num is 0 or 1 are special. The function returns the num itself since no multiplication is needed.

- if num < 2: return num Initializing variables: ans is initialized to 0 - it will hold the answer. mul is set to 1 and is our multiplying factor which helps in
- building the integer x from its least significant digit to the most significant digit. ans, mul = 0, 1
- Iterating from 9 down to 2: The loop runs backwards from 9 to 2, checking at each step if num can be divided by i without remainder (using the modulus operator %).

Dividing num by the digit if possible: When num is divisible by i, we divide num by i using integer division //= and update ans.

for i in range(9, 1, -1):

ans = mul * i + ans

return ans if num < 2 and ans <= 2**31 - 1 else 0

smallest positive integer x such that the product of its digits equals 26.

space for the next digit. while num % i == 0: num //= i

The new digit is placed in its correct position by the current value of mul. mul is then increased by a factor of 10 to make

Checking the final conditions: Once we break out of the loop, we check if num has been reduced to 1. If it's not, it means we could not fully factorize num using digits 2-9, so x cannot exist under our constraints. Moreover, we verify that the answer fits into a 32-bit signed integer by comparing it to 2**31 - 1. If either condition is not met, we return 0.

mul *= 10

The algorithm does not use any complex data structures, but it effectively leverages arithmetic operations and a simple for-loop to achieve the goal. This approach is efficient because it processes each digit in num at most once and avoids unnecessary computations or storage.

Let's walk through a small example to illustrate the solution approach using the number num = 26. We are tasked with finding the

if num < 2:

ans, mul = 0, 1

early return doesn't get triggered.

Example Walkthrough

return num Then, the variables ans and mul are initialized:

Firstly, the function would check if num is less than 2 and would return num itself if that's the case. Since 26 is greater than 1, this

Here, ans will be built up to form our final number x, and mul is the multiplying factor which helps place the found factors into their correct positions within x.

• ... Until we reach the digit 2:

• 2 does divide 26, leaving us with a quotient of 13 (26 // 2 = 13).

The loop starts at 9 and checks if num is divisible by any number from 9 down to 2. It proceeds as follows:

• num becomes 13 • ans is updated to mul * i + ans, which is 1 * 2 + 0 = 2

The current state of our variables is now:

• 9 does not divide 26, so it moves to the next digit.

• 8 does not divide 26, the algorithm continues to iterate.

mul is increased, multiplying by 10, becoming 10.

terminates.

for i in range(9, 1, −1):

Finally, we check:

• Is num now 1? No, it's 13, so we can't fully factorize num using digits 2-9.

function should return 0. return ans if num < 2 and ans <= 2**31 - 1 else 0

Since we couldn't reduce num to 1 by dividing by digits from 2 to 9, x does not exist within the problem constraints. Hence the

This example showed that the number 26 cannot be factorized into a product of digits between 2 and 9, which means there is no

• Would ans be within a 32-bit signed integer range if num was 1? We can't check this since the first condition has already failed.

Initialize the answer and the multiplier for the place value (ones, tens, etc.)

Add the current digit to the answer with the correct place value

// Append the digit to result, which is constructed from right to left.

// After we have tried all digits, num should be 1 if it was possible to factorize completely.

// If these conditions hold, cast the result to integer and return it. Otherwise, return 0.

Iterate over the digits from 9 to 2 since we want the smallest possible number after factorization

Increase the multiplier for the next place value (move to the left in the answer)

Now with num as 13, we continue to iterate. Our range is now exhausted since no digit between 2 to 9 divides 13. The loop

class Solution: def smallestFactorization(self, num: int) -> int: # If the number is less than 2, return the number itself as it's the smallest factorization

While the current digit i is a factor of num

answer = multiplier * i + answer

Divide num by i to remove this factor from num

such x that would satisfy the problem's conditions.

Python

Solution Implementation

if num < 2:

return num

answer, multiplier = 0, 1

for i in range(9, 1, -1):

while num % i == 0:

num //= i

num /= i;

multiplier *= 10;

result = multiplier * i + result;

// Also, the result should fit into an integer.

// Increase the multiplier for the next digit.

return num == 1 && result <= Integer.MAX_VALUE ? (int) result : 0;</pre>

// If these conditions are not met, return 0 as specified.

function smallestFactorization(num: number): number {

return num < 2 && result <= INT MAX ? static cast<int>(result) : 0;

// If the number is less than 2, it is already the smallest factorization.

multiplier *= 10

```
# If num is fully factorized to 1 and the answer is within the 32-bit signed integer range, return answer
       # Else, return 0 because a valid factorization is not possible or the answer is too big
       return answer if num == 1 and answer <= 2**31 - 1 else 0
Java
class Solution {
   // Method to find the smallest integer that has the exact same set of digits as the input number when multiplied.
    public int smallestFactorization(int num) {
       // If the number is less than 2, return it as the smallest factorization of numbers 0 and 1 is themselves.
       if (num < 2) {
            return num;
       // Initialize result as a long type to avoid integer overflow.
        long result = 0;
       // Multiplier to place the digit at the correct position as we build the result number.
        long multiplier = 1;
       // Iterating from 9 to 2 which are the possible digits of the result.
        for (int i = 9; i >= 2; --i) {
           // If the current digit divides the number, we can use it in the factorization.
           while (num % i == 0) {
               // If so, divide the number by the digit to remove this factor from number.
```

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C++
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class Solution {
public:
   // This function returns the smallest integer by recombining the factors of the input 'num'.
    int smallestFactorization(int num) {
       // If the number is less than 2, it is already the smallest factorization.
       if (num < 2) {
            return num;
       // 'result' holds the smallest integer possible from the factorization.
       // 'multiplier' is used to construct the 'result' from digits.
        long long result = 0, multiplier = 1;
       // Iterate from 9 to 2 to check for factors.
       // We start from 9 because we want the smallest possible integer after factorization.
        for (int i = 9; i >= 2; --i) {
           // While 'i' is a factor of 'num', factor it out and build the result.
           while (num % i == 0) {
                num /= i;
                // Add the factor to the result, adjusting the position by 'multiplier'.
                result = multiplier * i + result;
                // Increase the multiplier by 10 for the next digit.
                multiplier *= 10;
```

// Check if remaining 'num' is less than 2 (fully factored into 2-9) and result fits into an int.

if (num < 2) {

TypeScript

};

```
return num;
      // 'result' holds the smallest integer possible from the factorization.
      // 'multiplier' is used to construct the 'result' from digits.
      let result: number = 0;
      let multiplier: number = 1;
      // Iterate from 9 to 2 to check for factors.
      // We start from 9 because we want the smallest possible integer after factorization.
      for (let i: number = 9; i >= 2; --i) {
          // While 'i' is a factor of 'num', factor it out and build the result.
          while (num % i === 0) {
              num /= i;
              // Add the factor to the result, adjusting the position by 'multiplier'.
              result = multiplier * i + result;
              // Check if the result is growing beyond the range of a 32-bit integer
              if (result > Number.MAX_SAFE_INTEGER) {
                  return 0;
              // Increase the multiplier by 10 for the next digit.
             multiplier *= 10;
      // Check if remaining 'num' is less than 2 (fully factored into 2—9) and result fits within a 32—bit signed integer.
      // If these conditions are not met, return 0 as specified.
      return num < 2 && result <= 2**31 - 1 ? result : 0;
class Solution:
   def smallestFactorization(self, num: int) -> int:
       # If the number is less than 2, return the number itself as it's the smallest factorization
       if num < 2:
            return num
       # Initialize the answer and the multiplier for the place value (ones, tens, etc.)
       answer, multiplier = 0, 1
       # Iterate over the digits from 9 to 2 since we want the smallest possible number after factorization
```

Else, return 0 because a valid factorization is not possible or the answer is too big return answer if num == 1 and answer <= 2**31 - 1 else 0**Time and Space Complexity**

multiplier *= 10

While the current digit i is a factor of num

answer = multiplier * i + answer

Divide num by i to remove this factor from num

Add the current digit to the answer with the correct place value

Increase the multiplier for the next place value (move to the left in the answer)

If num is fully factorized to 1 and the answer is within the 32-bit signed integer range, return answer

for i in range(9, 1, −1):

num //= i

while num % i == 0:

The time complexity of the given code is O(log(num)). This is because the while loop that reduces num by a factor of i will run at most O(log(num)) times. This is similar to how division works in terms of complexity while reducing the number digit by digit. Since the outer for loop is constant and only runs 8 times (from 9 to 2), it does not affect the time complexity significantly.

The space complexity of the code is 0(1). No additional space that grows with the input size num is used. We use a fixed number of variables (ans, mul, and i) that do not depend on the size of the input num.