2233. Maximum Product After K Increments Greedy Array Heap (Priority Queue) Medium

## **Problem Description**

all the elements in the array nums. After finding the maximum product, we need to return the result modulo 10^9 + 7 because the maximum product could be a very large number. The core of the problem lies in strategically choosing which numbers to increment to maximize the final product. Intuition

The problem provides us with a list of non-negative integers named nums and an integer k. The task is to increase any element

of nums by 1 during each operation, and you can perform this operation at most k times. The goal is to maximize the product of

With this in mind, we arrive at the solution approach:

pushed back into the heap, maintaining the heap order.

product of numbers that are closer together is generally higher than the product of the same numbers that are not evenly spread. For example, the product of [4, 4, 4] is 64, while the product of [2, 4, 6] is only 48, even though both sets have the same sum of 12.

In order to maximize the product of the numbers, we want to even out the values as much as possible. This is because the

- Use a min-heap (a data structure that allows us to always extract the smallest number efficiently) to manage the numbers. This ensures that we can always increment the smallest number available, which helps in balancing them as evenly as possible. Perform k operations of incrementing the smallest value in the min-heap. After each increment, the updated number is
- By following this approach, we effectively distribute the increments in a way that pushes the product to its maximum possible value before taking the modulo.

10^9 + 7 during this step by taking the modulo after each multiplication to prevent integer overflow.

Once all the operations are done, calculate the product of all the elements in the heap. We have to keep in mind the modulo

The solution to this problem is implemented in Python and makes use of the heap data structure, which allows us to easily and efficiently access and increment the smallest element in the <a href="nums">nums</a> list. Here is the step-by-step explanation of the

incremented in the next operation.

heappush(nums, heappop(nums) + 1)

**Return the Result**: Finally, we return the calculated ans as the result.

Let's walk through a small example to illustrate the solution approach.

**Perform Increment Operations**: We are allowed 3 increments.

Imagine we have nums = [1, 2, 3] and k = 3.

Heap after 1st increment: [2, 2, 3]

Heap after 2nd increment: [2, 3, 3]

Heap after 3rd increment: [3, 3, 3]

For last 3: ans = (9 \* 3) % 1000000007 = 27

So the final product modulo  $10^9 + 7$  is 27.

# Convert the list nums into a min-heap in-place

# Increment the smallest element in the heap k times

# Calculate the product of all elements mod 10^9 + 7

product = (product \* num) % modulo

private static final int MOD = (int) 1e9 + 7;

public int maximumProduct(int[] nums, int k) {

// incrementing any element 'k' times.

minHeap.offer(num);

smallest = heappop(nums) # Pop the smallest element

// Define the MOD constant to use for avoiding integer overflow issues.

// Function to calculate the maximum product of array elements after

// Increment the smallest element in the heap 'k' times.

// increment it and add it back to the heap.

int incrementedValue = minHeap.poll() + 1;

minHeap.offer(incrementedValue);

// Initialize a min-heap (PriorityQueue) to store the elements.

// Retrieve and remove the smallest element from the heap,

// Initialize the answer as a long to prevent overflow during the computation.

product = (product \* v) % mod; // Update the product with each element

return static\_cast<int>(product); // Cast to int to match return type

\* Calculates the maximum product of an array after incrementing any element "k" times.

let priorityQueue: MinPriorityQueue<number> = new MinPriorityQueue<number>();

// Note: This code assumes that MinPriorityQueue<number> is imported correctly and available.

heappush(nums, smallest + 1) # Increment the smallest element and push back onto heap

// Initialize the priority queue with all elements from the nums array

let minElement: number = priorityQueue.dequeue().element;

import { MinPriorityQueue } from '@datastructures-js/priority-queue';

Starting with ans = 1,

Solution Implementation

heapify(nums)

product = 1

for in range(k):

modulo = 10\*\*9 + 7

for num in nums:

return product

def maximumProduct(self, nums, k):

**Python** 

Java

class Solution {

Starting array: [1, 2, 3]

**Heapify the List**: We convert **nums** into a min-heap.

for in range(k):

mod = 10\*\*9 + 7

ans = (ans \* v) % mod

for v in nums:

implementation:

**Solution Approach** 

Heapify the List: The first step is to convert the list nums into a min-heap using the heapify function from Python's heapq module. In a min-heap, the smallest element is always at the root, which allows us to apply our increments as effectively as possible.

heapify(nums)

**Perform Increment Operations**: Next, we perform k increments. For each operation, we extract the smallest element from the heap using heappop(nums), increment it by 1, and then push it back into the heap using heappush(nums, heappop(nums) + 1). This ensures that our heap remains in a consistent state, with the smallest element always on top, ready to be

Because we're looking for the product modulo 10^9 + 7, we take the modulo after each multiplication to prevent integer overflow. We initialize the ans variable to 1 and iterate through each value v in nums, applying the modulo operation as we multiply: ans = 1

Calculate the Product: Once all increments are done, we iterate through all elements in the heap to calculate the product.

The key algorithm used here is the heap (priority queue), which allows us to prioritize incrementing the smallest numbers. The pattern is simple yet effective: by giving priority to the smallest elements for incrementation, we use the operations to balance the numbers, aiming for a more uniform distribution which leads to a maximized product. The implementation is careful to take the product modulo 10^9 + 7 at each step, ensuring that the final result is within the correct range and doesn't overflow. **Example Walkthrough** 

After heapify: [1, 2, 3] (Note: Since the array is already a valid min-heap, there's no visible change)

2nd increment: Now we have two 2s at the top. We pop one out, increment to 3, and push back.

Calculate the Product: Now we calculate the product of the heap's elements modulo 10^9 + 7.

1st increment: Smallest is 1. We pop 1 out, increment to 2, and push back to heap.

3rd increment: One more increment to the remaining 2.

We've used our 3 increments to even out the numbers, as predicted by our intuition.

For 3: ans = (1 \* 3) % 1000000007 = 3For next 3: ans = (3 \* 3) % 1000000007 = 9

**Return the Result**: The result, 27, is returned as the final output.

from heapq import heapify, heappop, heappush class Solution:

heappush(nums, smallest + 1) # Increment the smallest element and push back onto heap

PriorityQueue<Integer> minHeap = new PriorityQueue<>(); // Add all the elements to the min-heap. for (int num : nums) {

while (k-- > 0) {

long answer = 1;

for (int v : nums) {

\* @param {number[]} nums An array of numbers.

priorityQueue.enqueue(nums[i]);

const n: number = nums.length;

for (let i = 0; i < n; i++) {

for (let i = 0; i < k; i++) {

const MODULO: number = 10 \*\* 9 + 7;

from heapq import heapify, heappop, heappush

def maximumProduct(self, nums, k):

let product: number = 1;

return product;

product = 1

modulo = 10\*\*9 + 7

Time and Space Complexity

for num in nums:

return product

\* @param {number} k The number of increments to perform.

\* @returns {number} The maximum product modulo 10^9 + 7.

function maximumProduct(nums: number[], k: number): number {

// Increment the smallest element in the queue k times

priorityQueue.enqueue(minElement + 1);

```
// Calculate the product of all elements now in the heap.
        while (!minHeap.isEmpty()) {
            // Take each element from the heap, multiply it with the current answer
            // and compute the modulus.
            answer = (answer * minHeap.poll()) % MOD;
        // Return the final product modulo MOD as an integer.
        return (int) answer;
C++
#include <vector>
#include <algorithm>
#include <functional> // for std::greater
class Solution {
public:
    int maximumProduct(std::vector<int>& nums, int k) {
        const int mod = 1e9 + 7; // Modulo value for the final result
        // Create a min-heap from the given vector nums
        std::make_heap(nums.begin(), nums.end(), std::greater<int>());
        // Iteratively increment the smallest element and then reheapify
        while (k-- > 0) {
            std::pop heap(nums.begin(), nums.end(), std::greater<int>());
            ++nums.back(); // Increment the smallest element
            std::push_heap(nums.begin(), nums.end(), std::greater<int>()); // Reheapify
        // Compute the product of all elements modulo mod
        long long product = 1; // Use long long to avoid integer overflow
```

```
// Calculate the product of all elements in the queue
for (let i = 0; i < n; i++) {
    product = (product * priorityQueue.dequeue().element) % MODULO;
```

class Solution:

**}**;

/\*\*

**TypeScript** 

heapify(nums) # Increment the smallest element in the heap k times for in range(k): smallest = heappop(nums) # Pop the smallest element

# Calculate the product of all elements mod 10^9 + 7

product = (product \* num) % modulo

# Convert the list nums into a min-heap in-place

```
Heapify Operation: Converting the nums array into a min-heap has a time complexity of O(n) where n is the number of
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**Time Complexity** 

elements in nums. **K Pop and Push Operations**: We pop the smallest element and then push an incremented value back onto the heap, k times.

The time complexity of this code is determined by the following parts:

Each such operation might take 0(log n) time since in the worst case, the element might need to sift down/up the heap which is a tree of height log n. Therefore, the time complexity for this part is 0(k log n).

Final Iteration to Calculate Product: We iterate over the heap of size n once and do a multiplication each time. Since the

heap is already a valid heap structure, and we are simply iterating over it, the iteration takes O(n) time. Thus, the overall time complexity is  $0(n + k \log n + n) = 0(n + k \log n)$ , assuming k pop and push operations dominate for

larger values of k. **Space Complexity** 

The space complexity is determined by: Heap In-Place: Since the heap is constructed in-place, it does not require additional space proportional to the input size

- Intermediate Variables: Only a constant amount of extra space is used for variables like ans and mod, which is also 0(1).

Therefore, the space complexity of the algorithm is 0(1).

beyond the initial list. Therefore, we consider this 0(1) additional space.