### 142. Linked List Cycle II

Medium Linked List Hash Table Two Pointers

# Problem Description

The problem presents a linked list and asks us to determine where a cycle begins within it. A cycle in a linked list happens when a node's next reference points back to a previous node in the list, causing a portion of the list to be traversed endlessly. We are given the head of the linked list, and we must find the node at which this cycle starts. If there is no cycle, our function should return null.

A linked list cycle is conceptually akin to a running track, where the entry point of the cycle is the "gate" to the track, and the cycle itself is the loop. Our goal is to figure out where this "gate" is located within the list.

## Intuition

require extra memory for storage. The intuition behind this algorithm involves a faster runner (the fast pointer) and a slower runner (the slow pointer), both starting at

To resolve the problem of finding out the cycle's starting point, we can use the two-pointer technique, which is efficient and doesn't

the head of the linked list. The fast pointer moves two steps at a time while the slow pointer moves only one. If a cycle exists, the fast pointer will eventually lap the slow pointer within the cycle, indicating that a cycle is present. Once they meet, we can find the start of the cycle. To do this, we set up another pointer, called ans, at the head of the list and move

it at the same pace as the slow pointer. The place where ans and the slow pointer meet again will be the starting node of the cycle. Why does this work? If we consider that the distance from the list head to the cycle entrance is x, and the distance from the

entrance to the meeting point is y, with the remaining distance back to the entrance being z, we can make an equation. Since the

fast pointer travels the distance of x + y + n \* (y + z) (where n is the number of laps made) and slow travels x + y, and fast is twice as fast as slow, then we can deduce that x = n \* (y + z) - y, which simplifies to x = (n - 1) \* (y + z) + z. This shows that starting a pointer at the head (x distance to the entrance) and one at the meeting point (z distance to the entrance) and moving them at the same speed will cause them to meet exactly at the entrance of the cycle. Solution Approach

#### speeds: slow and fast. slow moves one node at a time, while fast moves two nodes at a time.

The algorithm is divided into two main phases: 1. Detecting the cycle: Initially, both slow and fast are set to start at the head of the list. We then enter a loop in which fast

In this solution, we use the two-pointer technique, which involves having two iterators moving through the linked list at different

advances two nodes and slow advances one node at a time. If there is no cycle, the fast pointer will eventually reach the end of

- the list and we can return null at this point, as there is no cycle to find the entrance of. However, if there is a cycle, fast is guaranteed to meet slow at some point within the cycle. The meeting point is not necessarily the entrance to the cycle, but it indicates that a cycle does exist.
- list. Now, we move both ans and slow one node at a time. The node at which they conjoin is the start of the cycle. Why does the above approach lead us to the start of the cycle? We derive this from the fact that:

2. Finding the cycle starting node: When fast and slow meet, we introduce a new pointer called ans and set it to the head of the

The distance from the list's head to the cycle's entrance is denoted as x.

The remaining distance from the meeting point back to the entrance is z.

Using these variables, we know that when fast and slow meet, fast has traveled x + y + n \* (y + z) which is the distance to the

The distance from the cycle's entrance to the first meeting point is y.

meeting point plus n laps of the cycle. Since fast travels at twice the speed of slow, the distance slow has traveled (x + y) is half that of fast, leading us to the equation

2(x + y) = x + y + n \* (y + z). Simplifying this, we find x = (n - 1)(y + z) + z.

This equation essentially states that the distance from the head to the cycle entrance (x) is equal to the distance from the meeting point to the entrance (z) plus some multiple of the cycle's perimeter (y + z). This is why moving the ans pointer from the head and

slow from the meeting point at the same pace will lead them to meet at the cycle's entrance. The Python code provided implements this approach efficiently, using only two extra pointers (fast and slow) for detection and one

Example Walkthrough Let's consider a simple linked list example to walk through the solution approach:

Suppose we have the linked list 1 -> 2 -> 3 -> 4 -> 5 -> 2 (the last node points back to the second one, creating a cycle). Here,

### 1. Detecting the cycle:

extra (ans) for locating the cycle's entrance.

the node with the value 2 is the start of the cycle.

 Move slow to the next node (3) and fast two nodes forward (5). Continue this process until fast and slow meet. In our case, after few iterations, fast and slow both point to one of the

Initially, both slow and fast pointers are at the head of the list (node with value 1).

2. Finding the cycle starting node:

nodes inside the cycle (let's say they meet at node with value 4).

Move slow to the next node (2) and fast two nodes forward (3).

 Place the ans pointer at the head of the list (node with value 1). Move ans to the next node (2) and slow to the next node (5).

def detectCycle(self, head: Optional[ListNode]) -> Optional[ListNode]:

# Initialize two pointers, slow and fast

 Continue moving both ans and slow one node at a time. As the pointers move one step each turn, they will meet at the node that is the start of the cycle.

By following these steps and the reasonings behind the solution approach, we are able to find that the node with the value 2 is the

entry point of the cycle in the linked list without using any extra memory for storage, only the two pointer variables fast, slow, and

later the ans pointer.

In our case, ans and slow will both meet at the node with value 2, which is the correct entrance to the cycle.

1 # Definition for singly-linked list. class ListNode: def \_\_init\_\_(self, value=0, next=None): self.value = value self.next = next class Solution:

#### 12 # Traverse the linked list with two pointers moving at different speeds 13 while fast and fast.next: slow = slow.next # Slow pointer moves one step 14 fast = fast.next.next # Fast pointer moves two steps 15

slow = fast = head

ListNode fast = head;

ListNode slow = head;

slow = slow.next;

fast = fast.next.next;

if (slow == fast) {

// Loop until the fast pointer reaches the end of the list

// Move both pointers at the same pace

// Move each pointer by one step

// Initialize another pointer to the start of the list

// If the loop exits without the pointers meeting, there is no cycle.

while (fast != null && fast.next != null) {

// Move the slow pointer by one step

// Move the fast pointer by two steps

// If they meet, a cycle is detected

ListNode start = head;

while (start != slow) {

start = start.next;

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**Python Solution** 

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# Check if the slow and fast pointers meet, indicating a cycle
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               if slow == fast:
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                   # Initialize another pointer to the head of the linked list
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                   start = head
21
22
                   # Move both pointers at the same speed until they meet at the cycle's start node
23
                   while start != slow:
24
                        start = start.next
25
                       slow = slow.next
26
27
                   # Return the node where the cycle begins
28
                   return start
29
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           # If no cycle is detected, return None
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           return None
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Java Solution
 1 // Definition for singly-linked list.
  class ListNode {
       int val;
       ListNode next;
       ListNode(int x) {
           val = x;
           next = null;
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   public class Solution {
       // This method detects the node where the cycle begins in a linked list
13
       public ListNode detectCycle(ListNode head) {
14
           // Two pointers initialized to the start of the list
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```

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                       slow = slow.next;
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                   // When they meet again, it's the start of the cycle
36
                   return start;
37
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39
           // If we reach here, no cycle was detected
           return null;
41
42 }
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C++ Solution
1 // Definition for singly-linked list.
2 struct ListNode {
       int val;
       ListNode *next;
       ListNode(int x) : val(x), next(nullptr) {}
6 };
   class Solution {
   public:
       // This function detects a cycle in a linked list and returns the node
10
       // where the cycle begins. If there is no cycle, it returns nullptr.
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       ListNode* detectCycle(ListNode* head) {
12
           ListNode* fastPointer = head; // Fast pointer will move two steps at a time
13
           ListNode* slowPointer = head; // Slow pointer will move one step at a time
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15
           // Loop until the fast pointer reaches the end of the list,
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           // or until the fast and slow pointers meet, indicating a cycle.
           while (fastPointer && fastPointer->next) {
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               slowPointer = slowPointer->next;
                                                           // Move slow pointer one step
19
20
               fastPointer = fastPointer->next->next;
                                                           // Move fast pointer two steps
21
               // Check if the slow and fast pointers have met, indicating a cycle.
               if (slowPointer == fastPointer) {
23
24
                   ListNode* entryPoint = head; // Start from the head
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26
                   // Loop until the entry point of the cycle is found.
27
                   while (entryPoint != slowPointer) {
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                                                            // Move entry point one step
                       entryPoint = entryPoint->next;
29
                       slowPointer = slowPointer->next;
                                                            // Move slow pointer one step
30
32
                   // The entry point is where the slow pointer and entry point meet.
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                   return entryPoint;
```

# val: number;

return nullptr;

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Typescript Solution
1 // Definition for singly-linked list node.
   interface ListNode {
       next: ListNode | null;
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   /**
    * Detects a cycle in a linked list and returns the node where the cycle begins.
    * If there is no cycle, it returns null.
    * @param head - The head of the singly-linked list.
    * @returns The node where the cycle begins or null if no cycle exists.
12
    */
   function detectCycle(head: ListNode | null): ListNode | null {
       // Initialize two pointers, slow and fast.
14
       let slow: ListNode | null = head;
15
       let fast: ListNode | null = head;
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18
       // Traverse the list with two pointers moving at different speeds.
       while (fast !== null && fast.next !== null) {
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           slow = slow!.next; // Move slow pointer one step.
           fast = fast.next.next; // Move fast pointer two steps.
           // If slow and fast pointers meet, a cycle exists.
           if (slow === fast) {
               // Initialize another pointer to the beginning of the list.
25
               let startPoint: ListNode | null = head;
               // Move the startPoint and slow pointer at the same speed.
               while (startPoint !== slow) {
                   startPoint = startPoint!.next;
                   slow = slow!.next;
               // The node where both pointers meet is the start of the cycle.
               return startPoint;
       // If no cycle is detected, return null.
       return null;
```

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Time and Space Complexity

intersection which is also linear in time.

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The space complexity of the code is 0(1). This is due to the fact that no additional space proportional to the size of the input linked list is being allocated; only a fixed number of pointer variables fast, slow, and ans are used, irrespective of the size of the linked list.

The time complexity of the code is O(n), where n is the number of nodes in the linked list. This is because in the worst case, both

fast and slow pointers traverse the entire list to detect a cycle, and then a second pass is made from the head to the point of