2530. Maximal Score After Applying K Operations

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Medium Greedy Array Heap (Priority Queue)
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You are presented with an integer array nums and an integer k, and you start with a score of 0. In a single operation:

Choose an index i such that 0 <= i < nums.length.
 Increase your score by nums[i].

3. Replace nums[i] with ceil(nums[i] / 3).

Problem Description

greater than or equal to val.

Here's what you need to remember:

The goal is to find the maximum score you can achieve after exactly k operations. Note that ceil(val) is the smallest integer

You can apply operations only k times.
You want to maximize your score with these k operations.

- Intuition

should always choose the maximum number currently in the array because that will give you the highest possible addition to your

To efficiently track and extract the maximum number at every step, a max heap is ideal. A max heap is a data structure that always allows you to access and remove the largest element in constant time. In Python, you use a min heap by negating the values, as the standard library heapq module supports only min heap.

The intuition behind solving this problem comes from the need to maximize the score gained from each operation. To do this, you

Here's the step-by-step reasoning:

1. Negate all the values in the array and build a min heap, which simulates a max heap.

2. For k iterations, do the following:

Add the negation of the popped value to your total score (since the heap contains negatives, you negate again to get the original positive

- value).
- \circ Calculate ceil(v / 3) for the popped value v, negate it and then push it back to the heap.
 - By repeating this process k times, you are each time taking the current maximum value, getting the points from it, and then reducing its value before putting it back into the bean. This allows you to maximize the score at each of the k steps.

Pop the heap's top element (the smallest negative number, which is the max in the original array).

- reducing its value before putting it back into the heap. This allows you to maximize the score at each of the k steps.

 Solution Approach
 - The solution leverages a priority queue, particularly a max heap, to efficiently manage the elements while performing the

added to the heap so that retrieving the element with the maximum value (min heap for the negated values) can be done in constant time.

operations. Since Python's built-in heapq module provides a min heap implementation, the elements are negated before being

necessary because Python doesn't have a built-in max heap, so this workaround is used (h = [-v for v in nums]). Then, the

Here's a breakdown of the solution approach:

(heappush(h, -(ceil(v / 3)))).

heapify function converts the array into a heap (heapify(h)).

Iteration: Repeat the following steps k times, corresponding to the number of operations allowed:
 Extract (heappop) the root of the heap, which is the smallest negative number or the largest number before negation. Then negate it (v = - heappop(h)) to get back to the original value.
 Add this value to ans, which keeps track of the score after each operation.

Compute the new value to be inserted back into the heap. The new value is the ceiling of v / 3, negated to maintain the correct heap order

Scoring & Updating: Each iteration increases the score by the max element's value, and then the heap is updated to reflect

By following these steps, the solution ensures that we are always picking the maximum available element, thereby maximizing the

Initialization: Transform nums into a heap in-place by negating its values, effectively creating a max heap. The negative sign is

the change in the selected element's value post-operation.

exactly k operations.

Example Walkthrough

score with each operation. After k iterations, the score ans is returned, which is the maximum possible score after performing

Let's go through the process with a small example: Suppose nums = [4, 5, 6] and k = 2.

Before we start any operations, we will first negate all the values in nums to simulate a max heap: [-4, -5, -6]. Then we convert this array into a heap.

Step 1: Build a Heap

a. We pop the largest element (which is the smallest when negated): v = -heappop(h) => v = 6 (since heappop(h) gives -6).

c. We calculate the new value for the next heap insert, which is the ceiling of v / 3 and then negate it to maintain the max heap

b. We add this value to our score ans: ans = 0 + 6 = 6.

Step 3: Perform the Second Operation

a. Again, we pop the largest element from h: v = -heappop(h) => v = 5.

property: heappush(h, -(ceil(6/3))) => heappush(h, -2), so h becomes [-5, -2, -4].

We transform the array into a heap in-place: heapify(h) makes h = [-6, -5, -4].

c. We calculate the new value for the next heap insert: heappush(h, -(ceil(5/3))) => heappush(h, -2), and h now becomes [-4, -2, -2].

Solution Implementation

from math import ceil

from typing import List

from heapq import heapify, heappop, heappush

min_heap = [-value for value in nums]

Extract 'k' elements from the heap

value = -heappop(min_heap)

new_value = -(ceil(value / 3))

heappush(min_heap, new_value)

print(solution.maxKElements([4, 5, 6], 3))

heapify(min_heap) # Convert the list into a heap

and revert it to its original value

total_sum = 0 # Initialize the sum of the max 'k' elements

return total_sum # Return the sum of the extracted elements

// Function to calculate the sum of the max 'k' elements following a specific rule

// Retrieve the top element from the max heap (which is the current maximum)

// Creating a max priority queue using the elements of 'nums'

// This variable will store the sum of the max 'k' elements

sum += currentValue; // Add the current maximum to the sum

// Apply the rule: replace the extracted value with (value + 2) / 3

maxHeap.push(newValue); // Push the new value back into the max heap

priority_queue<int> maxHeap(nums.begin(), nums.end());

long long maxKelements(vector<int>& nums, int k) {

int currentValue = maxHeap.top();

k--: // Decrement the counter

maxHeap.pop(); // Remove the top element

int newValue = (currentValue + 2) / 3;

Python

b. We add the value to our score: ans = 6 + 5 = 11.

Step 2: Perform the First Operation

At this point, we have performed 2 operations, which is our limit k, so we are done.

Result:

The maximum score that can be achieved after exactly k = 2 operations is 11. This result comes from choosing the operations

- that maximize the score at each step, using the heap to efficiently select these operations.
- class Solution:
 def maxKElements(self, nums: List[int], k: int) -> int:
 # Invert the values of the nums array to use the heapq as a min-heap,

Pop the smallest (inverted largest) element from the heap

since Python's heapq module implements a min-heap instead of a max-heap.

total_sum += value # Add the element to the sum # Calculate the new value by taking the ceiling division by 3 # and push its inverted value onto the heap

Example usage:

solution = Solution()

for _ in range(k):

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Java
class Solution {
   // Method to find the maximum sum of k elements with each element replaced by a third of its value.
    public long maxKelements(int[] nums, int k) {
       // Create a max heap using PriorityQueue to store the elements in descending order.
       PriorityQueue<Integer> maxHeap = new PriorityQueue<>((a, b) -> b - a);
       // Add all elements from the array to the max heap.
        for (int value : nums) {
           maxHeap.offer(value);
       // Initialize a variable to store the sum of the maximum k elements.
       long sum = 0;
       // Iterate k times to get the sum of the maximum k elements.
       while (k-- > 0) {
           // Poll the top element from the max heap (the maximum element).
           int maxElement = maxHeap.poll();
           // Add the maximum element to the sum.
            sum += maxElement;
           // Replace the maximum element with a third of its value and add it back to the max heap.
           maxHeap.offer((maxElement + 2) / 3);
       // Return the sum of the maximum k elements.
       return sum;
```

public:

C++

#include <vector>

#include <queue>

class Solution {

long long sum = 0;

// Iterate 'k' times

from heapq import heapify, heappop, heappush

def maxKElements(self, nums: List[int], k: int) -> int:

heapify(min heap) # Convert the list into a heap

and revert it to its original value

total sum = 0 # Initialize the sum of the max 'k' elements

min_heap = [-value for value in nums]

Extract 'k' elements from the heap

value = -heappop(min heap)

print(solution.maxKElements([4, 5, 6], 3))

Time and Space Complexity

within the loop that runs k times.

space, without the input.

for _ in range(k):

from math import ceil

class Solution:

from typing import List

solution = Solution()

while (k > 0) {

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// Return the calculated sum
       return sum;
};
TypeScript
import { MaxPriorityQueue } from '@datastructures-js/priority-queue'; // assuming required package is imported
/**
* Function to compute the sum of the 'k' maximum elements after each is replaced
 * with the flooring result of that element plus two, divided by three.
 * @param nums Array of numbers from which we are finding the max 'k' elements.
 * @param k The number of maximum elements we want to sum.
 * @return The sum of the 'k' maximum elements.
 */
function maxKElements(nums: number[], k: number): number {
    // Initialize a priority queue to store the numbers.
    const priorityQueue = new MaxPriorityQueue<number>();
    // Iterate over the array of numbers and enqueue each element into the priority queue.
    nums.forEach(num => priorityQueue.enqueue(num));
    // Initialize the answer variable to accumulate the sum of max 'k' elements.
    let sum = 0;
    // Loop to process 'k' elements.
    while (k > 0) {
       // Dequeue the largest element from the priority queue.
       const currentValue = priorityQueue.dequeue().element;
       // Add the value to the sum.
       sum += currentValue;
       // Compute the new value using the specified formula and enqueue it back to the priority queue.
       priorityQueue.enqueue(Math.floor((currentValue + 2) / 3));
       // Decrement 'k' to move to the next element.
        k--;
    // Return the accumulated sum.
    return sum;
```

```
total_sum += value # Add the element to the sum

# Calculate the new value by taking the ceiling division by 3
# and push its inverted value onto the heap
new_value = -(ceil(value / 3))
heappush(min_heap, new_value)

return total_sum # Return the sum of the extracted elements

# Example usage:
```

Invert the values of the nums array to use the heapq as a min-heap,

Pop the smallest (inverted largest) element from the heap

since Python's heapq module implements a min-heap instead of a max-heap.

The heapify(h) function takes O(n) time to create a heap from an array of n elements.
 Inside the loop, each heappop(h) and heappush(h, -(ceil(v / 3))) operation has a time complexity of O(log n) because both operations involve maintaining the heap invariant, which requires a restructuring of the heap. Since these operations are called k times, the complexity

within the loop is 0(k * log n).

So, the total time complexity of the function is 0(n + k * log n), where n is the length of the nums list.

The time complexity of this function primarily comes from two operations: the heapification of the nums list and the operations

Now, let's consider the space complexity. The function uses additional memory for the heap, which is h in the code. This copy of the list adds a space complexity of O(n). If we consider auxiliary space complexity (i.e., not counting space taken up by the input itself), it could be argued that the space complexity is O(1) because we are rousing the space of the given input list nume to

itself), it could be argued that the space complexity is 0(1) because we are reusing the space of the given input list nums to create the heap h.

Thus, the space complexity can be 0(n) considering the total space used, including input, or 0(1) if considering only auxiliary