1372. Longest ZigZag Path in a Binary Tree

<u>Depth-First Search</u> <u>Dynamic Programming</u>

Problem Description

Medium

You are tasked with finding the longest ZigZag path in a binary tree. A ZigZag path is defined as follows: • You first pick any node as a starting point and choose a direction to move in (either left or right).

- Based on the chosen direction, you move to the corresponding child node (move to the right child if the direction is right, or to the left child if
- the direction is left). After moving to a child node, you switch the direction for the next move (from right to left or left to right).

Binary Tree

The ZigZag length is the number of nodes you have visited on the path minus one, since a path with a single node has a length of zero. Your objective is to find the length of the longest ZigZag path in the given binary tree.

You repeat the process of moving to the next child node and switching direction until there are no more nodes to visit.

ntuition To solve the problem, we employ depth-first search (DFS) to explore each possible path within the tree. The purpose of using

DFS is to traverse the tree in a manner where we check every possible ZigZag path starting from each node, considering both the left and right directions.

Here is the intuition behind the DFS approach: • We define a recursive DFS function that takes the current node and two integers, 1 and r, which represent the lengths of the ZigZag path when the last move was to the left (I) or to the right (r), respectively.

• We maintain a variable ans to keep track of the maximum length found so far. For each node, we update ans with the maximal value out of ans, l, and r.

• When we move to a left child (root.left), we increase the length of the ZigZag path for a move to the right (r + 1), and reset the left move length to zero. This is because moving to the left child is considered a right move for the parent node.

• At each call to the DFS function, if the current node is None (i.e., we can't move further), we return as we've reached the end of a path.

right move length to zero. • This recursive process continues until all nodes have been visited, and by then we will have recorded the maximum length of all ZigZag paths in the ans variable.

• Similarly, when moving to the right child (root.right), we increase the length of the ZigZag path for a move to the left (1 + 1), and reset the

- The solution uses a nonlocal declaration for the ans variable to ensure that its value is updated across different recursive calls. Each recursive call processes the current node and then makes two more recursive calls to the child nodes (if they exist), one for each possible direction (left or right) for the next move, continuing the ZigZag pattern.
- Solution Approach

referring to the Python code provided: We utilize the TreeNode class to represent the structure of the binary tree, where each node has a value (val), a pointer to the left child (left), and a pointer to the right child (right).

The solution uses a depth-first search (DFS) to explore each possible ZigZag path. Here's a breakdown of the implementation,

The Solution class has the method longestZigZag, which initiates the recursive DFS process to find the longest ZigZag

Inside longestZigZag, we define a nested function dfs which recursively processes each node of the tree. The dfs function

has parameters:

previous left move.

by the DFS traversal.

Example Walkthrough

paths as no moves have been made yet.

is returned as the final result.

 root: the current node being processed. ○ 1: an integer representing the ZigZag path length when the last move was to the left.

path. The method takes a TreeNode as an input, which is the root of the binary tree.

seen as a previous right move from the parent node's perspective.

To illustrate the solution approach, let us consider a small binary tree example:

We would like to find the longest ZigZag path in this binary tree.

- r: an integer representing the ZigZag path length when the last move was to the right. The dfs function begins by checking if the current node is None. If it is, that branch of recursion stops because we can't move further down the tree from this node.
- This ensures that ans can be updated across the different recursive calls and still maintains its most recent value. At each node, we update ans to be the maximum value between the current ans and the values of 1 and r. This ensures that as we move through the tree, any longer path lengths are captured and kept.

To keep track of the maximum ZigZag path length found at any point, we use a variable ans which is declared as nonlocal.

When the DFS explores the left subtree by calling dfs(root.left, r + 1, 0), it increments the ZigZag path length for a

direction switch to the right (r + 1) and resets the left path length to zero (0). This is because a move to the left child is

The initial call to the dfs function is made with dfs(root, 0, 0) starting at the root with lengths of 0 for both left and right

Once the DFS traversal is complete and all ZigZag paths have been computed, the longest path length is stored in lans, which

- Conversely, when exploring the right subtree with dfs(root.right, 0, l + 1), it increments the ZigZag path length for a direction switch to the left (1 + 1) and resets the right path length to zero (0). A move to the right child is considered as a
- In summary, the solution effectively utilizes recursive DFS to explore each path, alternating moves and updating the path length while maintaining a global maximum. This is an example of a modified DFS where additional parameters (1 and r) are used not only to keep track of the path length but also to encode the state of the ZigZag movement (direction change after each step). The complexity of the algorithm is O(n) where n is the number of nodes in the binary tree since every node is visited exactly once

1 and r initialized to zero since no moves have been made yet. Step 2: At the root node 1, since it is not None, we have two options to continue the ZigZag path: move to the left child or right child. We make two recursive calls to explore both options: dfs(root.left, r + 1, 0) which is dfs(node 3, 1, 0) dfs(root.right, 0, l + 1) which is dfs(node 2, 0, 1)

Step 3: Now in the subtree rooted at $\frac{3}{2}$, we have $\frac{1}{2} = \frac{1}{2}$, $\frac{1}{2} = \frac{1}{2}$. Since node $\frac{3}{2}$ has a left child $\frac{4}{2}$ and no right child, we make

another recursive call dfs(node 3.left, r + 1, 0) which becomes dfs(node 4, 1, 0). At this point, since node 4 is a leaf

node without children, the path ends here, and ans is potentially updated to the maximum of ans, 1, or r which in this case

Similarly, in the subtree rooted at 2, we have 1 = 0, r = 1. Node 2 has both a left and a right child, so two recursive calls are

In each of these calls, we are ZigZagging from the root now, so the appropriate path lengths 1 and r are updated.

Step 1: We start with the root of the tree which is the node with the value 1. A recursive call dfs(root, 0, 0) is made with both

would be 1.

made:

respectively.

Python

Java

/**

/**

class TreeNode {

int val;

class Solution {

/**

*/

TreeNode left;

TreeNode right;

class Solution:

At each leaf node (5 and 6), the same check for None occurs, and the ans is updated with the path lengths of 2 and 1,

• dfs(node 2.left, r + 1, 0) which is dfs(node 5, 2, 0)

• dfs(node 2.right, 0, l + 1) which is dfs(node 6, 0, 1)

through the tree to find the longest possible path.

def longestZigZag(self, root: TreeNode) -> int:

def dfs(node, left length, right length):

dfs(node.left, right length + 1, 0)

dfs(node.right, 0, left_length + 1)

Initialize the maximum length to 0 before starting DFS

Once DFS is complete, return the maximum zigzag length found

Helper function to perform DFS (Depth-First Search) on the tree

Recursively explore the right child, incrementing the "right length" as we are

making a zag (right direction) from the left side of the current node

Start DFS with the root of the tree, initial lengths are 0 as starting point

* Solution class contains methods to calculate the longest zigzag path in a binary tree.

* Method to find the length of the longest zigzag path starting from the root node.

* A recursive DFS method that traverses the tree to find the longest zigzag path.

* @param leftLength The current length of the zigzag path when coming from a left child.

* @param rightLength The current length of the zigzag path when coming from a right child.

The current node being visited.

private void dfs(TreeNode node, int leftLength, int rightLength) {

// Variable to store the length of the longest zigzag path found so far.

// Initialize with the assumption that there's no zigzag path.

If the node is None, we've reached the end of a path

Solution Implementation

if node is None:

max length = 0

dfs(root, 0, 0)

return max_length

* Definition for a binary tree node.

private int longestZigZagLength;

longestZigZagLength = 0;

return longestZigZagLength;

dfs(root, 0, 0);

* @param node

*/

};

TypeScript

interface TreeNode {

class Solution:

let longestPath: number = 0;

// Interface for a binary tree node

val: number; // Value of the node

left: TreeNode | null; // Reference to the left child

// Variable to store the longest ZigZag path length found

function longestZigZag(root: TreeNode | null): number {

def longestZigZag(self, root: TreeNode) -> int:

def dfs(node, left length, right length):

traverse(root, 0, 0); // Start the traversal from the root node

if (!node) return; // If we reach a null node, stop the traversal

// Update the maximum length of the ZigZag path seen so far

longestPath = Math.max(longestPath, leftSteps, rightSteps);

return longestPath; // Return the longest ZigZag path length found

right: TreeNode | null; // Reference to the right child

// Function to calculate the length of the longest ZigZag path in a binary tree

// Helper function to perform DFS and find the length of the longest ZigZag path

function traverse(node: TreeNode | null, leftSteps: number, rightSteps: number) {

// If we take a left child, we can move right on the next step; thus, increment rightSteps.

// Pass 0 for the opposite direction because the ZigZag path resets on turning twice in the same direction.

// If we take a right child, we can move left on the next step; thus, increment leftSteps.

if (node.left) traverse(node.left, rightSteps + 1, 0); // Traverse the left child

Helper function to perform DFS (Depth-First Search) on the tree

If the node is None, we've reached the end of a path

max length = max(max length, left length, right length)

Initialize the maximum length to 0 before starting DFS

Once DFS is complete, return the maximum zigzag length found

if (node.right) traverse(node.right, 0, leftSteps + 1); // Traverse the right child

Update the global answer by taking the maximum value found so far

making a zig (left direction) from the right side of the current node

Start DFS with the root of the tree, initial lengths are 0 as starting point

Recursively explore the left child, incrementing the "left length" as we are

* @param root The root node of the binary tree.

public int longestZigZag(TreeNode root) {

* @return The length of the longest zigzag path in the tree.

// Start Depth First Search traversal from the root.

// Return the length of the longest zigzag path found.

that was kept up to date in each step now contains the value 2, which is the longest ZigZag path length in the binary tree (from 1 to 2 to 5).

The longest ZigZag path in this binary tree is therefore of length 2, which corresponds to two moves: one move from root (1) to

the right child (2), and another move from the right child (2) to its left child (5). This illustrates how the DFS algorithm zigzags

Step 4: Once all leaves have been reached, and None returned for each childless call, the recursion unwinds. The ans variable

return # Update the global answer by taking the maximum value found so far nonlocal max length max length = max(max length, left length, right length) # Recursively explore the left child, incrementing the "left length" as we are # making a zig (left direction) from the right side of the current node

TreeNode() {} TreeNode(int val) { this.val = val; } TreeNode(int val, TreeNode left, TreeNode right) { this.val = val; this.left = left; this.right = right;

```
// If the node is null, we have reached beyond leaf, so return.
       if (node == null) {
            return;
       // Update the longestZigZagLength with the maximum path length seen so far at this node.
        longestZigZagLength = Math.max(longestZigZagLength, Math.max(leftLength, rightLength));
       // Traverse left — the zigzag is coming from the right so add 1 to rightLength.
       dfs(node.left, rightLength + 1, 0);
       // Traverse right - the zigzag is coming from the left so add 1 to leftLength.
       dfs(node.right, 0, leftLength + 1);
C++
#include <algorithm> // For using max()
// Definition for a binary tree node.
struct TreeNode {
               // Value of the node
   int val;
   TreeNode *left: // Pointer to the left child
   TreeNode *right; // Pointer to the right child
   // Constructors
   TreeNode() : val(0), left(nullptr), right(nullptr) {}
   TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
   TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}
class Solution {
public:
    int longestPath = 0; // Variable to store the longest ZigZag path length found
   // Function to calculate the length of the longest ZigZag path in a binary tree.
   int longestZigZag(TreeNode* root) {
       traverse(root, 0, 0); // Start the traversal from the root node
        return longestPath; // Return the longest ZigZag path length found
   // Helper function to perform DFS and find the length of the longest ZigZag path
   void traverse(TreeNode* node, int leftSteps, int rightSteps) {
        if (!node) return; // If we reach a null node, stop the traversal
       // Update the maximum length of ZigZag path seen so far
        longestPath = std::max(longestPath, std::max(leftSteps, rightSteps));
       // If we take a left child, we can move right the next step; thus, increment rightSteps.
       // If we take a right child, we can move left the next step; thus, increment leftSteps.
       // Pass 0 for the opposite direction because ZigZag path resets on turning twice in the same direction.
       if (node->left) traverse(node->left, rightSteps + 1, 0); // Traverse the left child
```

if (node->right) traverse(node->right, 0, leftSteps + 1); // Traverse the right child

dfs(node.left, right length + 1, 0) # Recursively explore the right child, incrementing the "right length" as we are # making a zag (right direction) from the left side of the current node dfs(node.right, 0, left_length + 1)

max length = 0

dfs(root, 0, 0)

return max_length

Time and Space Complexity

if node is None:

nonlocal max length

return

Time Complexity The time complexity of the given code is O(n) where n is the number of nodes in the binary tree. The reason for this is that the function dfs visits every node in the tree exactly once. During each call, it performs a constant amount of work, regardless of the

Space Complexity

size of the subtree it is working with.

The space complexity of the code is O(h), where h is the height of the binary tree. This space is used by the call stack due to recursion. In the worst case, when the binary tree becomes a skewed tree (like a linked list), the height h can be equal to n, which means the space complexity in the worst case would be O(n). However, for a balanced tree, the height h will be log(n), resulting in a space complexity of O(log(n)).