1353. Maximum Number of Events That Can Be Attended Medium Sorting Heap (Priority Queue) Greedy Array

# **Problem Description**

during which the event takes place. We can choose to attend an event on any day from the start day to the end day inclusive. However, we can only attend one event at any given day. Our goal is to maximize the number of events that can be attended.

In this problem, we are given a list of events, where each event is represented by a start day and an end day, indicating the duration

**Leetcode Link** 

Intuition

The intuition behind the solution is to prioritize attending events based on their end dates because we want to ensure we do not miss out on events that are about to end. For this reason, a greedy algorithm works efficiently — sorting the events by their end times could help us attend as many as possible.

However, simply sorting by the end times is not adequate since we also have to consider the starting times. Therefore, we create a priority queue (min-heap) where we will keep the end days of events that are currently available to attend. We also use two variables to keep track of the minimum and maximum days we need to cover.

the number of events we can attend.

As we iterate through each day within the range, we do the following:

2. Add all events that start on the current day to the priority queue.

3. Attend the event that is ending soonest (if any are available).

1. Remove any events that have already ended.

- **Solution Approach**
- The solution uses a greedy approach combined with a priority queue (min-heap) to facilitate the process of deciding which event to

attend next. Specifically, it applies the following steps:

1. Initialization: A dictionary d is used to map each start day to a list of its corresponding end days. This enables easy access to events starting on a particular day.

Two variables, i and j, are initialized to inf and 0, respectively, to track the minimum start day and the maximum end day

By using a priority queue (min-heap), we ensure that we are always attending the event with the nearest end day, hence maximizing

# 2. Building the dictionary:

across all events.

 The solution iterates over each event and populates the dictionary d with the start day as the key and a list of end days as the value.

- It also updates i to the minimum start day and j to the maximum end day encountered. 3. Setting up a min-heap:
  - available events. 4. Iterating over each day:

■ If the min-heap is not empty, it means there is at least one event that can be attended. The event with the earliest end

A priority queue (implemented as a min-heap using a list h) is created to keep track of all the end days of the currently

∘ For each day s in the range from the minimum start day i to the maximum end day j inclusive: While there are events in the min-heap that have ended before day s, they are removed from the heap since they can no

• All events starting on day s are added to the min-heap with their end days.

day is attended (removed from the heap), and the answer count ans is incremented by one.

 After iterating through all the days, the ans variable that has been tracking the number of events attended gives us the maximum number of events that can be attended.

Example Walkthrough

2. Building the dictionary:

• We iterate over the events:

We initialize an empty min-heap list h.

1. Initialization:

can attend.

5. Returning the result:

longer be attended.

1 Events = [[1,4], [4,4], [2,2], [3,4], [1,1]]

Let's walk through an example to illustrate the solution approach. Suppose we are given the following list of events:

 $\circ$  We create a dictionary d, and two variables i = inf and j = 0.

■ For event [1,4], we update d with  $\{1: [4]\}$  and set i = 1 and j = 4.

In summary, by using a combination of a dictionary to map start days to events, a min-heap to efficiently find the soonest ending

event that can be attended, and iteration over each day, the solution efficiently computes the maximum number of events that one

■ For event [4,4], we update d with {1: [4], 4: [4]}. Variables i and j remain unchanged. ■ For event [2,2], we update d with {1: [4], 2: [2], 4: [4]}. Variables i and j remain unchanged. ■ For event [3,4], we update d with {1: [4], 2: [2], 3: [4], 4: [4]}. Variables i and j remain unchanged.

■ For event [1,1], we update d with {1: [4, 1], 2: [2], 3: [4], 4: [4]}. Variables i and j remain unchanged.

### 4. Iterating over each day: $\circ$ We have i = 1 and j = 4, so we iterate from day 1 to day 4.

○ On day 2:

∘ On day 4:

5. Returning the result:

**Python Solution** 

from math import inf

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});

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Typescript Solution

let maxDay: number = 0;

events.forEach(event => {

from collections import defaultdict

from heapq import heappush, heappop

earliest\_start, latest\_end = inf, 0

event\_dict[start].append(end)

for end in event\_dict[day]:

heappush(min\_heap, end)

max\_events\_attended += 1

# Return the total number of events attended

latest\_end = max(latest\_end, end)

earliest\_start = min(earliest\_start, start)

for start, end in events:

max\_events\_attended = 0

if min\_heap:

return max\_events\_attended

public int maxEvents(int[][] events) {

for (int[] event : events) {

int startDay = event[0];

int endDay = event[1];

 $min_heap = []$ 

3. Setting up a min-heap:

• On day 1:

■ We pop 1 from h as it's the earliest end day, attend this event, and increment ans to 1.

 On day 3: ■ There's no event ending before day 3, so nothing is removed from h.

■ We add the end day of the event starting on day 3 to h, so h becomes [4, 4].

■ We add the end day of the event starting on day 2 to h, so h becomes [4, 2].

■ We add all end days of events starting on day 1 to h, so h becomes [4, 1].

■ There's no event ending before day 2, so nothing is removed from h.

We pop 2 from h, attend this event, and increment ans to 2.

We then attend this event and increment ans to 5.

that could be attended by ensuring we attend the ones ending soonest first.

# Initialize variables to track the earliest and latest event dates

# Initialize an empty min-heap to store active events' end dates

# Push all end dates of events starting today onto the heap

heappop(min\_heap) # Remove the event that was attended

// Create a map to associate start days with a list of their respective end days

dayToEventsMap.computeIfAbsent(startDay, k -> new ArrayList<>()).add(endDay);

int earliestStart = Integer.MAX\_VALUE; // Initialize earliest event start day

// Process the events to populate the map and find the range of event days

Map<Integer, List<Integer>> dayToEventsMap = new HashMap<>();

int latestEnd = 0; // Initialize latest event end day

// Map the start day to the end day of the event

// Iterate over each day within the range of event days

// Add new events that start on the current day

for (int endDay : eventsStartingToday) {

eventsEndingQueue.offer(endDay);

if (!eventsEndingQueue.isEmpty()) {

eventsEndingQueue.poll();

return attendedEventsCount;

if (!minHeap.empty()) {

minHeap.pop();

2 import { PriorityQueue } from 'typescript-collections';

const maxEvents = (events: number[][]): number => {

let minDay: number = Number.MAX\_SAFE\_INTEGER;

eventsByStartDay[startDay].push(endDay);

minDay = Math.min(minDay, startDay);

maxDay = Math.max(maxDay, endDay);

const [startDay, endDay] = event;

// A dictionary to hold events keyed by their start day

// Initialize minimum and maximum days for all events

const eventsByStartDay: { [key: number]: number[] } = {};

while (!minHeap.isEmpty() && minHeap.peek() < day) {</pre>

// Return the total number of events that can be attended

// Add new events that start on the current day to the heap

return maxEventsAttended;

maxEventsAttended++;

// Return the maximum number of events that can be attended

// Importing necessary functionalities from standard TypeScript library

eventsByStartDay[startDay] = eventsByStartDay[startDay] || [];

// Function to determine the maximum number of events that can be attended

// Populate the eventsByStartDay and define minimum and maximum days across all events

// Remove past events that have already ended

PriorityQueue<Integer> eventsEndingQueue = new PriorityQueue<>();

int attendedEventsCount = 0; // Initialize the count of events attended

// Attend the event that ends the earliest, if any are available

++attendedEventsCount; // Increment the count of events attended

for (int currentDay = earliestStart; currentDay <= latestEnd; ++currentDay) {</pre>

while (!eventsEndingQueue.isEmpty() && eventsEndingQueue.peek() < currentDay) {</pre>

List<Integer> eventsStartingToday = dayToEventsMap.getOrDefault(currentDay, Collections.emptyList());

// Create a min-heap to manage event end days

eventsEndingQueue.poll();

# If there are any events available to attend today, attend one and increment count

# Counter for the maximum number of events one can attend

# Populate event\_dict with events and update earliest\_start and latest\_end

 After iterating through all days, we find that ans = 5, which means we could attend a total of 5 events. In this example, by using the greedy approach outlined in the solution, we were methodically able to maximize the number of events

■ Since there is only one event with an end day of 4 left in h, we attend it and increment ans to 4.

■ We also check for more events starting today which is one [4, 4] and add it to the heap.

■ We pop 4 from h (either one, as both have the same end day), attend this event, and increment ans to 3.

class Solution: def maxEvents(self, events: List[List[int]]) -> int: # Create a default dictionary to hold events keyed by start date event\_dict = defaultdict(list)

24 25 # Iterate over each day within the range of event dates for day in range(earliest\_start, latest\_end + 1): 26 27 # Remove events that have already ended 28 while min\_heap and min\_heap[0] < day:</pre> 29 heappop(min\_heap)

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               // Update earliest start and latest end
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                earliestStart = Math.min(earliestStart, startDay);
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                latestEnd = Math.max(latestEnd, endDay);
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Java Solution

1 class Solution {

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C++ Solution
  1 #include <vector>
  2 #include <queue>
    #include <unordered_map>
    #include <algorithm>
    #include <climits>
     using namespace std;
    class Solution {
     public:
         int maxEvents(vector<vector<int>>& events) {
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             // Map to hold the events on each day
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             unordered_map<int, vector<int>> eventsByStartDay;
             // Initialize the minimum and maximum days across all events
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             int minDay = INT_MAX;
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             int maxDay = 0;
 17
             // Iterate through all the events
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             for (auto& event : events) {
                 int startDay = event[0];
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                 int endDay = event[1];
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                 // Map the end day of each event to its start day
 23
                 eventsByStartDay[startDay].push_back(endDay);
 24
                 // Update the minimum and maximum days
 25
                 minDay = min(minDay, startDay);
                 maxDay = max(maxDay, endDay);
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             // Min-heap (priority queue) to keep track of the events' end days, prioritised by earliest end day
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             priority_queue<int, vector<int>, greater<int>> minHeap;
 31
             // Counter to hold the maximum number of events we can attend
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             int maxEventsAttended = 0;
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 34
             // Iterate through each day from the earliest start day to the latest end day
 35
             for (int day = minDay; day <= maxDay; ++day) {</pre>
 36
                 // Remove events that have already ended
                 while (!minHeap.empty() && minHeap.top() < day) {</pre>
 37
                     minHeap.pop();
 38
 39
                 // Add all events starting on the current day to the min-heap
 40
                 for (int endDay : eventsByStartDay[day]) {
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 42
                     minHeap.push(endDay);
```

// If we can attend an event, remove it from the heap and increase the count

### eventsByStartDay[day].forEach(endDay => { 38 minHeap.enqueue(endDay); }); 39 40 // Attend the event that ends the earliest 41 42 if (!minHeap.isEmpty()) {

Time Complexity:

run O(j - i) times.

**Space Complexity:** 

minHeap.dequeue();

if (eventsByStartDay[day]) {

maxEventsAttended++;

minHeap.dequeue();

return maxEventsAttended;

Time and Space Complexity

Let's analyze the time complexity step by step:

2. Populating the min-heap h on each day has a variable complexity. In the worst case, we could be adding all events to the heap on a single day which will be O(N log N) due to N heap insertions (heappush operations), each with O(log N) complexity. 3. The outer loop runs from the minimum start time i to the maximum end time j. Therefore, in the worst-case scenario, it would

4. Inside this loop, we perform a heap pop operation for each day that an event ends before the current day. Since an event end

5. We also perform a heap pop operation when we can attend an event, and this happens at most N times (once for each event).

can only be popped once, all these operations together sum up to O(N log N), as each heappop operation is O(log N) and there

1. Building the dictionary d has a complexity of O(N), where N is the number of events since we iterate through all the events once.

The given Python code aims to find the maximum number of events one can attend, given a list of events where each event is

represented by a start and end day. The code uses a greedy algorithm with a min-heap to facilitate the process.

### Adding these complexities, we have: • For the worst case, a complexity of O(N log N + (j - i)) for the loop, with O(N log N) potentially dominating the overall time

In conclusion, the time complexity of the code is  $0(N \log N + (j - i))$ . However, (j - i) may be considered negligible compared to N  $\log N$  for large values of N, yielding an effective complexity of  $O(N \log N)$ .

consideration, which is standard in space complexity analysis.

complexity when (j - i) is not significantly larger than N.

are at most N such operations throughout the loop.

- complexity due to the heap is O(N). The min-heap h and the dictionary d represent the auxiliary space used by the algorithm. Since they both have O(N) space

complexity, the overall space complexity is also O(N), assuming that the space required for input and output is not taken into

Let's analyze the space complexity: 1. The dictionary d can hold up to N entries in the form of lists, with each list containing at least one element, but potentially up to N end times in the worst case. Therefore the space required for d is O(N). 2. The min-heap h also requires space which in the worst-case scenario may contain all N events at once. Thus, the space

22 23 // Using a TypeScript priority queue to manage events' end days 24 const minHeap: PriorityQueue<number> = new PriorityQueue<number>((a, b) => a - b); 25 26 // Counter for the maximum number of events attended 27 let maxEventsAttended: number = 0; 28 29 // Iterate from the minimum start day to the maximum end day for (let day = minDay; day <= maxDay; day++) {</pre> 30 // Remove events that have already ended 31

Typescript doesn't have a built-in PriorityQueue, but you can use the 'typescript-collections' library to match the desired functi