# 1526. Minimum Number of Increments on Subarrays to Form a Target Array

**Dynamic Programming** Monotonic Stack

Array

## **Problem Description**

filled with zeros. The key objective is to transform the initial array into the target array. The only operation allowed to achieve this is to select a subarray from initial and increment each of its elements by one. The task is to determine the minimum number of such operations required to reach the target array configuration. It's also specified that the final answer will fit within a 32-bit integer, which means it won't be too huge for an int data type to store. To solve this problem, one needs to intuitively understand that the minimum number of operations needed is closely related to

The problem presents an integer array called target. We also have an array of the same size as target, named initial, which is

the differences between the heights (values) of adjacent elements in the target array.

#### Intuition behind the solution arises from looking at the problem in terms of "height differences". Imagine a graph where the value

ntuition

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of each element in the target array represents the height at that particular position. Incrementing a subarray by 1 is like raising the ground level of a terrain from one point to another by one unit. To minimize operations, we should always try to raise the terrain in the largest possible steps rather than incrementing little by little. The first insight is that we'll have to increment the first element of initial to the first element of target for sure since there are no previous elements to consider, which accounts for target [0] operations.

Following that, we move through the target array and look at the difference between each pair of adjacent elements (b - a for elements a and b). Each time we encounter a rise in height (where b > a), we need additional operations equivalent to the height

difference to "build up" our terrain to that new height. If the height decreases or remains equal (b - a is less than or equal to 0), we do not need extra operations since we can imagine that the previous increments have already covered that height. By summing up all necessary height differences, we can get the total number of increments required. Therefore, the number of operations can be given by the first element of the target array plus the sum of all positive differences between successive

adjacent pairs of elements and calculate the sum of the positive differences. **Solution Approach** The solution to this problem utilizes a straightforward Greedy algorithm approach and Python's built-in functionality to generate

elements in the target array. The given Python function pairwise from the itertools library can be used here to generate the

# Here's a brief walkthrough of the implementation:

adjacent pairs easily.

Initialization: We start by initializing the number of operations to the value of the first element in target, because the initial array is filled with zeros, and we must at least increment the first element 'target[0]' times to match the first element of the target array.

We then iterate over the target array, comparing each element to its predecessor to find the difference between them. The iteration of

**Calculating the Needed Operations:** 

Iterating through the array:

## pairs is done using the pairwise function, which neatly returns a tuple containing pairs of adjacent elements from the iterable target.

**Summation:** 

expression max(0, b - a) ensures that we only consider positive differences, which represent an increase in value from one element in target to the next. • The rationale behind this is that whenever b is greater than a, we need additional operations to raise initial[a] to initial[b]. If b is equal

to or less than a, no extra operations are needed because we assume initial[a] is already at least at height a, so we can effectively "carry

∘ For each pair (a, b) obtained from the pairwise, we add to our operations count the difference (b - a) if b is greater than a. The

## over" this height to initial[b].

computed using the built-in sum function, which takes an iterable. **Result:** • The final result is returned as the sum of the initial operations count and the accumulated extra operations needed. This sum represents the

• We sum up all the extra operations needed for each increase in the array, adding it to our initial count of target [0] operations. The sum is

- A List (target) to store the integer values we're working with,
  - pairwise utility from the itertools library to iterate through the array in adjacent element pairs. The beauty of this solution lies in its simplicity and efficiency. There are no complex data structures required, and the algorithm

Suppose we have a target array given as [1, 3, 2, 4]. Our goal is to transform an initial array from [0, 0, 0, 0] to match the

**Example Walkthrough** 

Let's walk through a small example to clearly understand how the solution approach works.

minimum number of operations required to form the target array from the initial array.

The data structures and patterns used in this approach are quite simple and consist of:

Python's built-in sum function to calculate the aggregate of operations needed,

runs in linear time, making it a very practical solution for this problem.

target array using the fewest number of operations.

Generate pairs using pairwise: (1, 3), (3, 2), (2, 4).

We combine the counted operations to get the total.

target [1, 3, 2, 4]. Thus, a total of 5 operations were needed.

for previous, current in pairwise(target):

**Calculating the Needed Operations:** 

• The Greedy algorithm pattern, where we take the optimal decision step-by-step based on the current and next element,

#### Start with operations count equal to the first element of target: operations = target[0] = 1. Iterating through the array:

**Summation:** 

**Initialization:** 

 $\circ$  Pair (3, 2): No increase (it's actually a decrease), so add 0: operations += max(0, 2 - 3) = 3.  $\circ$  Pair (2, 4): Increase is 2, so add 2 to operations: operations += max(0, 4 - 2) = 5.

 $\circ$  Pair (1, 3): Increase is 2, so add 2 to operations: operations +=  $\max(0, 3 - 1) = 3$ .

Result:

Solution Implementation

**Python** 

Java

class Solution {

In this example, we increment the first element (index 0) of the initial array 1 time to match the first element of the target array,

# sum up the differences between consecutive elements if they are positive

# The total number of operations to match the target array is returned

 $\circ$  The result is operations = 1 + 2 + 0 + 2 = 5. So, it takes a minimum of 5 operations to transform initial into target.

then we perform another operation on the subarray from index 0 to index 1 to increment both elements (making the array [1, 1,

transition from 3 to 2, as the previous operations have already covered this. Finally, we perform two more operations from index 2

to index 3 to increment the last two elements by 1 each time, resulting in [2, 3, 1, 1] and then [2, 3, 2, 2], and finally our

0, 0]). Next, we perform a third operation on the same subarray, resulting in [2, 2, 0, 0]. No operation is needed for the

from itertools import pairwise # Python 3 function from the itertools module class Solution: def minNumberOperations(self, target: List[int]) -> int: # The function calculates the minimum number of operations needed to form the target array # from a starting array of zeros. Each operation increments a contiguous subarray by 1. # The first operation will increment the contiguous subarray from the start to set the first element # Thus, the number of operations for the first element is equal to its value operations = target[0]

# as these represent the additional operations needed for increasing the array to match the target

operations += max(0, current - previous) # Only positive differences are added

#### public int minNumberOperations(int[] target) { // Initialize minimum operations with the first element // since that's the minimum number of operations needed // to increase from 0 to the first element's value.

int minOperations = target[0];

\* An operation is incrementing a subarray by 1.

\* @return The minimum number of operations required.

int minNumberOperations(std::vector<int>& target) {

for (int i = 1; i < target.size(); ++i) {</pre>

if (target[i] > target[i - 1]) {

def minNumberOperations(self, target: List[int]) -> int:

for previous, current in pairwise(target):

return totalOperations;

\* @param target Vector of integers representing the target array.

// Iterate through the target array starting from the second element.

// If the current target value is greater than the previous,

// Return the total number of operations needed to form the target array.

totalOperations += target[i] - target[i - 1];

return operations

```
// Iterate through the array starting from the second element
        for (int i = 1; i < target.length; ++i) {</pre>
            // If the current element is greater than the previous one,
            // it means we need additional operations to increase from
            // the previous element's value to the current element's value.
            if (target[i] > target[i - 1]) {
                minOperations += target[i] - target[i - 1];
            // If not, no additional operations are needed because the
            // operations required to reach the previous element are adequate.
        // Return the total minimum number of operations required.
        return minOperations;
C++
#include <vector>
class Solution {
public:
    /**
```

```
};
  TypeScript
  // Function to calculate the minimum number of operations needed to
  // raise a series of values to match the heights specified in the 'target' array.
  // Each operation increments a subarray's elements by 1.
  function minNumberOperations(target: number[]): number {
      // Initialize the number of operations with the first element of the target array,
      // since we start with an array of zeros, the first element itself will be
      // the number of operations needed to reach its value.
      let operations = target[0];
      // Loop through the target array starting from the second element.
      for (let index = 1; index < target.length; ++index) {</pre>
          // If the current element is greater than the previous one,
          // we need additional operations for the difference between
          // the current and the previous elements.
          if (target[index] > target[index - 1]) {
              operations += target[index] - target[index - 1];
      // Return the total number of operations calculated.
      return operations;
from itertools import pairwise # Python 3 function from the itertools module
```

# The function calculates the minimum number of operations needed to form the target array

# The first operation will increment the contiguous subarray from the start to set the first element

# as these represent the additional operations needed for increasing the array to match the target

# from a starting array of zeros. Each operation increments a contiguous subarray by 1.

operations += max(0, current - previous) # Only positive differences are added

# Thus, the number of operations for the first element is equal to its value

# sum up the differences between consecutive elements if they are positive

# The total number of operations to match the target array is returned

\* Calculate the minimum number of operations to form a target array from a zero array.

// this signifies a need for additional operations to increment the subarray.

int totalOperations = target[0]; // Start with the first value as the initial number of operations.

```
The code provided calculates the minimum number of operations to form a target array where each operation increments a
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space proportional to the input size.

Time and Space Complexity

operations = target[0]

return operations

subarray by 1. The function minNumberOperations does this by summing the differences between consecutive elements where the second element is larger than the first, plus the value of the first element in the target array. Let's analyze both the time complexity and space complexity: Time Complexity:

# The time complexity for this operation is O(n), where n is the length of the target array, because it goes through the list once.

class Solution:

The pairwise utility itself, which is presumably a wrapper around a simple loop-like construct that yields successive pairs of elements, does not add any significant time overhead as it just creates a tuple of the current and next elements in the array. Therefore, the overall time complexity of the code is O(n).

The function iterates once over the list of target elements using the pairwise utility to consider pairs of consecutive elements.

**Space Complexity:** 

The function is a one-liner without the use of additional data structures that depend on the size of the input. It relies on generator

expressions which yield one item at a time. The max function is applied in a generator expression, so it does not require additional

The space complexity is not affected by the size of the input array, as the sum function processes the generator expression iteratively. The pairwise utility is expected to yield one pair at a time and doesn't store the entire list of pairs in memory.

As a result, the overall space complexity of the code is 0(1), reflecting constant space usage.