2580. Count Ways to Group Overlapping Ranges

Description

You are given a 2D integer array ranges where ranges[i] = [start $_i$, end $_i$] denotes that all integers between $start_i$ and $start_i$ and $start_i$ are contained in the $start_i$ range.

You are to split ranges into two (possibly empty) groups such that:

- Each range belongs to exactly one group.
- Any two overlapping ranges must belong to the same group.

Two ranges are said to be overlapping if there exists at least one integer that is present in both ranges.

• For example, [1, 3] and [2, 5] are overlapping because 2 and 3 occur in both ranges.

Return the total number of ways to split ranges into two groups. Since the answer may be very large, return it modulo 109 + 7.

Example 1:

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Input: ranges = [[6,10],[5,15]]
Output: 2
Explanation:
The two ranges are overlapping, so they must be in the same group.
Thus, there are two possible ways:
- Put both the ranges together in group 1.
- Put both the ranges together in group 2.
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Example 2:

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Input: ranges = [[1,3],[10,20],[2,5],[4,8]]
Output: 4
Explanation:
Ranges [1,3], and [2,5] are overlapping. So, they must be in the same group.
Again, ranges [2,5] and [4,8] are also overlapping. So, they must also be in the same group.
Thus, there are four possible ways to group them:
    All the ranges in group 1.
    All the ranges in group 2.
    Ranges [1,3], [2,5], and [4,8] in group 1 and [10,20] in group 2.
    Ranges [1,3], [2,5], and [4,8] in group 2 and [10,20] in group 1.
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Constraints:

- 1 <= ranges.length <= 10^{5}
- ranges[i].length == 2
- 0 <= start $_i$ <= end $_i$ <= 10 9