710. Random Pick with Blacklist **Binary Search** Array Hash Table **Math** Sorting Randomized **Leetcode Link** Hard

Problem Description

keeping the process efficient.

The problem states that an integer n and an array blacklist are given. The task is to design an algorithm that can randomly choose an integer from 0 to n - 1 that is not included in the blacklist. Every valid integer within the range should have an equal chance of being picked. The algorithm should also minimize the number of calls to the random function provided by the programming language you are using. This means that we need to find an efficient way to track which numbers have been blacklisted and ensure that only non-blacklisted

numbers are considered when we want to pick a random number. All non-blacklisted numbers should be equally likely to be chosen. Intuition

The primary challenge lies in designing an algorithm that maintains the equal probability of picking a non-blacklisted number while

One intuitive way is to map all the blacklisted numbers within the range [0, k) to some non-blacklisted numbers in the range [k, n), where k is the count of non-blacklisted numbers. This is done because the random number selection will only happen within the [0,

k) range, thereby avoiding the blacklisted numbers. If a number within this range is not blacklisted, it maps to itself. If it is blacklisted, it maps to a non-blacklisted number outside the range. The intuition for the solution comes from the observation that picking a random number in the [0, n - len(blacklist)) range will

ensure that each pick is equally likely. Then we can 'remap' these picks if they are supposed to be a blacklisted value to some nonblacklisted value. This remapping is done using a dictionary that keeps track of the blacklisted numbers and their corresponding non-blacklisted 'replacement'. When picking a number, we first check if it needs to be remapped and get the corresponding value if needed.

The Solution class is initialized by creating the mapping of blacklisted numbers if they are within the [0, k) range to the first non-

blacklisted numbers outside of this range. As for the pick method, it randomly selects a number within [0, k) and returns the

corresponding value in the mapping if it exists, or itself if it is not blacklisted. **Solution Approach**

The solution to this problem employs a smart mapping strategy and a clever use of data structures to efficiently enable the random

selection of non-blacklisted numbers. By understanding that only those blacklisted numbers that fall within the range of [0, k) truly

interfere with our random pick, the solution avoids the need to deal with ones that are naturally excluded from the random range.

Here's a walk-through of the implementation details:

n).

1. Initialization (__init__ method): Compute k as n minus the size of the blacklist, which effectively represents the count of valid integers after excluding the

Loop through each number in the blacklist:

For each blacklisted number b that is less than k (and hence within the range of numbers we can randomly pick from),

blacklisted ones.

find a number i (starting from k) which is not in the blacklist. This determines the non-blacklisted number that b will map to.

The use of the dictionary data structure allows the algorithm to quickly access the remapped value, thereby minimizing the runtime

complexity for each pick operation to constant time (0(1)). Together with only initializing the mappings once in the constructor, this

By limiting the calls to the random function to the interval [0, k), the algorithm ensures that it minimizes the number of calls to this

Overall, this solution is both time and space-efficient, where space complexity is dictated by the number of blacklisted numbers

within [0, k), and the time complexity for the pick method is constant, irrespective of the size of the blacklist.

Update self.d[b] to i to keep the track of the mapping. Move to the next integer for mapping (increment i). 2. Random Pick (pick method):

Initialize a dictionary self.d that will hold the mapping from the blacklisted within [0, k) to the unblacklisted numbers in [k,

 Randomly select an integer x within the range [0, k). If x is a key in our mapping dictionary (which signifies that x is blacklisted), retrieve the mapped value (the substitute non-

blacklisted number). Otherwise, if x is not blacklisted, it can be returned as is.

makes the random pick operation very efficient.

potentially expensive operation.

Example Walkthrough

map:

To illustrate the solution approach, consider the following example:

need mapping to non-blacklisted numbers in [k, n).

The dictionary now looks like this: $self.d = \{3: 7, 5: 9\}$.

def __init__(self, n: int, blacklist: List[int]):

Iterate through each blacklisted number

for black_number in blacklist:

35 # Get a random number that's not on the blacklist

mapping_start_index = self.mapping_range_limit

find a non-blacklisted number to map it to

while mapping_start_index in blacklist_set:

if black_number < self.mapping_range_limit:</pre>

mapping_start_index += 1

random_pick = randrange(self.mapping_range_limit)

33 # Instantiate the Solution object with a length n and a blacklist

// Function to pick a random non-blacklisted number.

int randomNumber = random.nextInt(threshold);

* Your Solution object will be instantiated and called as such:

* Solution obj = new Solution(n, blacklist);

// Generate a random number within the range [0, threshold).

return mapping.getOrDefault(randomNumber, randomNumber);

// If the number is remapped, return the remapped number, otherwise return it as is.

return self.mapping_dict.get(random_pick, random_pick)

self.mapping_dict = {} # Dictionary to hold the mapping

Blacklisted 3 maps to 7, as 7 is the first non-blacklisted number available.

- Let n be 10, so the valid range of numbers is [0, 9]. • Let the blacklist be [3, 5, 8]. In the initialization step of our solution, we perform the following actions:
- we want to avoid picking a blacklisted number directly. 2. Initialize an empty dictionary self.d to hold the mappings. Since 3 and 5 are the only blacklisted numbers within [0, k), they will

3. We map blacklisted numbers within [0, k] to the first available non-blacklisted numbers starting from k. Starting at k = 7, we

1. Compute k as n - len(blacklist), which is 10 - 3 = 7. Therefore, k is 7, and our random pick range becomes [0, 6], because

Let's proceed with the random pick method: 1. We invoke the pick method to randomly select a number. Let's say the random function returns 5.

This process ensures that numbers are only picked from the valid set [0, 6], and if a blacklisted number is picked, it is properly

mapped to a non-blacklisted number hence maintaining equal probability of picking any non-blacklisted number. The pick operation remains efficient as it involves a constant-time dictionary lookup and a random choice within the reduced range.

self.mapping_range_limit = n - len(blacklist) # The upper limit for the mapping

If the blacklisted number is within the range of mappable values,

blacklist_set = set(blacklist) # Convert the blacklist to a set for efficient lookup

Skip all numbers that are in the blacklist until a valid one is found

Pick a random number from 0 to the upper exclusive limit (mapping_range_limit)

Return the mapped value if it exists, otherwise return the random_pick itself

Initialize an index to start mapping from blacklist numbers less than the mapping range limit

2. We check if 5 is in our mapping dictionary self.d. Since 5 is a key in self.d, we return self.d[5], which is 9.

3. If the random function returned 4, since 4 is not in self.d, 4 is not blacklisted, and we would return 4 directly.

• Blacklisted 5 maps to 9, as 8 is blacklisted and 9 is the next available non-blacklisted number.

Python Solution

20 # Map the blacklisted number within range to a non-blacklisted number 22 self.mapping_dict[black_number] = mapping_start_index 23 # Move on to the next possible number for mapping 24 mapping_start_index += 1

32 # Example usage:

def pick(self) -> int:

34 # obj = Solution(n, blacklist)

36 # param_1 = obj.pick()

from random import randrange

from typing import List

class Solution:

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C++ Solution

public int pick() {

* int param_1 = obj.pick();

```
Java Solution
1 import java.util.HashMap;
2 import java.util.HashSet;
  import java.util.Map;
  import java.util.Random;
   import java.util.Set;
   class Solution {
       // A map to keep the mapping of blacklisted numbers to the safe numbers.
 8
       private Map<Integer, Integer> mapping = new HashMap<>();
9
       // Instance of Random to generate random numbers.
10
       private Random random = new Random();
11
       // The threshold for picking a safe number.
12
       private int threshold;
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15
       // Constructor that takes the total number of elements (n) and the list of blacklisted elements (blacklist).
       public Solution(int n, int[] blacklist) {
16
           threshold = n - blacklist.length;
17
           // Convert the blacklist into a set for faster lookup.
18
           Set<Integer> blacklistSet = new HashSet<>();
19
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            for (int b : blacklist) {
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               blacklistSet.add(b);
22
23
           // Initialize a variable to the start of the possible non-blacklisted numbers above the threshold.
24
           int nextSafeNumber = threshold;
25
            for (int b : blacklist) {
26
               // Only remap blacklisted numbers below the threshold.
               if (b < threshold) {</pre>
27
28
                   // Find the next non-blacklisted number to map to.
29
                   while (blacklistSet.contains(nextSafeNumber)) {
                        ++nextSafeNumber;
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31
32
                   // Add the mapping from the blacklisted number to the safe number.
33
                   mapping.put(b, nextSafeNumber++);
34
35
```

13 14 15 16

```
1 #include <unordered_map>
 2 #include <unordered set>
   #include <vector>
   class Solution {
   private:
       std::unordered_map<int, int> whitelistMapping;
       int whitelistSize;
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10 public:
       // Constructor takes the size of the array (n) and a list of blacklisted indices (blacklist).
11
       Solution(int n, std::vector<int>& blacklist) {
12
           // Calculate the effective size of the whitelist (array size minus the size of the blacklist).
           whitelistSize = n - blacklist.size();
           // Set an index pointing to the start of the upper range which is outside of the whitelist.
           int upperIndex = whitelistSize;
17
           std::unordered_set<int> blacklistSet(blacklist.begin(), blacklist.end());
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20
           // Iterate over each number in the blacklist.
21
           for (int& blackNumber : blacklist) {
22
               // Only process blacklisted numbers that would have been chosen otherwise.
23
               if (blackNumber < whitelistSize) {</pre>
                   // Find the next number not in the blacklist past the initial whitelist range.
24
                   while (blacklistSet.count(upperIndex)) {
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                        ++upperIndex;
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                   // Establish a mapping from the blacklisted number to a whitelisted number from the upper range.
29
                   whitelistMapping[blackNumber] = upperIndex++;
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       // Function to randomly pick an index from the available whitelisted indices
       int pick() {
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           // Choose a random index from the initial range of whitelisted indices.
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37
           int randomIndex = rand() % whitelistSize;
38
           // If the index has been remapped due to being blacklisted, fetch the remapped index.
39
           // Otherwise, return it as is because it's not blacklisted.
40
            return whitelistMapping.count(randomIndex) ? whitelistMapping[randomIndex] : randomIndex;
41
42 };
43
   /**
    * Your Solution object will be instantiated and called as such:
    * Solution* obj = new Solution(n, blacklist);
    * int result = obj->pick();
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    */
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Typescript Solution
   // TypeScript lacks `unordered_map` and `unordered_set` but has the `Map` and `Set` classes.
   let whitelistMapping: Map<number, number>;
    let whitelistSize: number;
   // Initialize necessary structures and perform calculations as would be performed in the constructor.
```

25 }); 26 27 } 28 // Function to select a random whitelisted index.

// Usage example:

function pick(): number {

// initialize(100, [1, 2, 3]);

// let randomPick: number = pick();

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function initialize(n: number, blacklist: number[]): void {

let blacklistSet: Set<number> = new Set(blacklist);

// Iterate over each item in the blacklist array.

while (blacklistSet.has(upperIndex)) {

whitelistMapping.set(blackNumber, upperIndex++);

// Generate a random index within the initial whitelist range.

return whitelistMapping.get(randomIndex) ?? randomIndex;

let randomIndex: number = Math.floor(Math.random() * whitelistSize);

// Convert the blacklist array into a Set for O(1) lookups.

// Focus on blacklisted numbers within the initial whitelist range.

// Locate a non-blacklisted number beyond the initial whitelist range.

// Check and return the mapped index if originally blacklisted, else return the original.

// Create a mapping for the blacklisted number to the identified whitelisted number.

whitelistMapping = new Map<number, number>();

whitelistSize = n - blacklist.length;

let upperIndex: number = whitelistSize;

if (blackNumber < whitelistSize) {</pre>

blacklist.forEach(blackNumber => {

upperIndex++;

Time Complexity

Time and Space Complexity

- _init_ method: The initialization method initializes the mapping of a blacklist to new values. For each value in the blacklist, there is a possibility of a while loop running if the value is less than self.k. Considering that i is incremented each time to find a non-blacklisted value, and assuming the worst-case scenario where all the blacklisted values are less than k, the while loop has to iterate over all values from self.k to n-1 in the worst case. However, since each value from the blacklist requires only one mapping operation, and we do not revisit already mapped values, the time complexity would be O(B), where B is the length of the blacklist, assuming set membership test operations are O(1) which is the average case for Python sets. • pick method: This method generates a random number and looks up the value in the dictionary (if it is a blacklisted value that
- **Space Complexity** • The space complexity of the <u>init</u> method is O(B). The dictionary self.d used to store the remapped values will at most

has been remapped). Generating a random number is O(1), and dictionary lookup is on average O(1). In the worst case (not likely

in average scenarios) due to hash collisions, it could be O(k) but we generally do not consider this for average-case analysis,

have B entries, where B is the length of the blacklist. The set black also takes O(B) space. • The pick method does not use any additional space that scales with the input size, so its space complexity is O(1).

particularly because Python dictionaries are well optimized. Hence, the time complexity of pick is O(1).