

1429. First Unique Number

Medium

Design

Queue

Array

Hash Table

Data Stream

Leetcode Link

Problem Description

The problem at hand requires us to keep track of integers as they arrive in a sequence, so we can always query for the first unique integer in this sequence. To clarify, a unique integer is an integer that appears exactly once in the current sequence. We're given a sequence of integers as an array and need to do the following:

- Initialize our data structure with the array of integers.
- Be able to return the value of the first unique integer in the queue at any time.
- Be able to add new integers to the queue.

The problem specifies that if there isn't a unique integer, the `showFirstUnique` method should return `-1`. For the purpose of this problem, the 'queue' is a conceptual ordering of the integers; it's not necessarily a queue data structure in the traditional sense where elements are strictly processed in a FIFO (First-In-First-Out) manner, but rather a sequence where we can inspect and count occurrences of integers.

Intuition

Navigating to a solution requires us to address two key operations efficiently: query for the first unique integer, and add new integers to our dataset. A straightforward approach to find unique integers might involve iterating through our data and counting occurrences every time we want to find the first unique integer, but this would be inefficient, particularly as the amount of data grows. Instead, we're going to optimize this process.

The given solution takes advantage of two Python data structures—`Counter` and `deque`—to handle these operations efficiently:

- `Counter`: This is a special dictionary provided by Python's `collections` module that stores elements as keys and their counts as values. This allows us to efficiently keep track of the number of times each integer has been seen.
- `deque`: A double-ended queue that provides an efficient way to insert and remove elements from both ends, with $O(1)$ time complexity for these operations. It is important here for tracking the order of the integers as they appear and for quick removal of non-unique integers from the front.

For the `showFirstUnique` method, the implementation uses the `deque` to keep the integers in order and `Counter` to know the counts. It pops elements from the `deque` that are no longer unique (i.e., have a count higher than 1), until it finds an integer that is unique, or if the `deque` is empty, in which case it returns `-1`.

The `add` method needs to take an integer and add it to our data set, which consists of both the `Counter` and `deque`. It updates the count of the integer in the `Counter`, and appends the integer to the `deque`. This keeps our count accurate, and maintains the correct order for when we need to find the first unique integer.

In summary, the `Counter` keeps track of occurrences allowing for quick updates and checks, while the `deque` maintains the order of unique integers efficiently.

Solution Approach

The problem is addressed by implementing a class `FirstUnique` with two methods and an initializer:

- `__init__(self, nums: List[int])`: This is the initializer for our class. It takes a list of integers and initializes two attributes:
 1. `self.cnt`: A `Counter` object which records the number of occurrences of each integer in the list.
 2. `self.q`: A `deque` which represents our queue and stores the integers in the same order as they appear in the original list.
- `showFirstUnique(self) -> int`: This method is used to retrieve the value of the first unique integer in the queue. It does so by:
 1. Using a while loop to check the front element of the queue (using `self.q[0]`).
 2. If the count of the front element in the queue (as stored in `self.cnt`) is greater than 1, it is not unique; thus, it is removed from the `deque` using `popleft()`.
 3. This process repeats until a unique integer is found (an integer with a count of 1) or the `deque` becomes empty.
 4. The method returns `-1` if no unique integer is found; otherwise, it returns the first unique integer.
- `add(self, value: int) -> None`: This method handles adding a new integer to our data structure. When a new value is added:
 1. The `Counter` is updated to increment the count of the particular value (`self.cnt[value] += 1`).
 2. The value is appended to the end of the `deque` (using `self.q.append(value)`). This ensures the order of integers is maintained.

By maintaining a count of occurrences and the order of inserts, the class efficiently supports querying for unique values and extending the sequence with new values. The `Counter` allows for constant-time complexity for incrementing and checking counts, and the `deque` allows for constant-time complexity for adding and removing elements.

Together, these data structures enable the `FirstUnique` class to perform the necessary operations with an efficient time complexity that avoids the need for repeated scanning of the list of integers.

Example Walkthrough

Let's say we are given the following sequence of integers for our `FirstUnique` class: `[4, 10, 5, 3, 5, 4]`.

When the `FirstUnique` object is created with this sequence, the following operations occur during initialization:

- `self.cnt` is initialized as `Counter({4: 2, 10: 1, 5: 2, 3: 1})` showing the count of each number in the sequence.
- `self.q` is initialized as `deque([4, 10, 5, 3, 5, 4])` keeping the original order of numbers.

Now, when `showFirstUnique()` is called the first time, it performs the following steps:

1. The method starts a loop and examines `self.q[0]`, which is 4.
2. It then checks `self.cnt[4]`, which is 2. Since this is greater than 1, 4 is not unique, so it is removed from `self.q` using `popleft()`.
3. The next element at the front is 10. The count `self.cnt[10]` is checked and found to be 1. Therefore, 10 is the first unique number.
4. `showFirstUnique()` returns 10.

Later, if the `add()` method is called with the value 3, the following occurs:

- `self.cnt[3]` becomes 2 as 3 was already present in the sequence.
- 3 is added to `self.q`, which is now `deque([10, 5, 3, 5, 4, 3])`.

After this addition, calling `showFirstUnique()` again starts a check from the front:

1. The front element is 10 with `self.cnt[10]` still 1, so `showFirstUnique()` would again return 10.
2. If we had added another 10, then the count would change and the `showFirstUnique()` process would remove 10 from the queue since its count would be increased, and the next first unique number in the queue would be returned or `-1` if there are no unique numbers left.

Through this example, we understand how the `FirstUnique` class efficiently manages the data with `Counter` and `deque` to provide quick access to the first unique integer and accommodates additions to the sequence.

Python Solution

```
1 from collections import Counter, deque
2
3 class FirstUnique:
4     def __init__(self, nums: List[int]):
5         # Initialize a counter to keep the count of each number
6         self.counter = Counter(nums)
7         # Initialize a queue to store the unique numbers in order
8         self.queue = deque(nums)
9
10    def showFirstUnique(self) -> int:
11        # Loop until we find the first unique number or the queue is empty
12        while self.queue and self.counter[self.queue[0]] != 1:
13            # If the first element in the queue is not unique, remove it
14            self.queue.popleft()
15        # If the queue is empty return -1, otherwise return the first unique number
16        return -1 if not self.queue else self.queue[0]
17
18    def add(self, value: int) -> None:
19        # Increment the count of the added value
20        self.counter[value] += 1
21        # Add the value to the queue
22        self.queue.append(value)
23
24    # Usage of the FirstUnique class
25    # Create an object of FirstUnique with a list of numbers
26    # obj = FirstUnique(nums)
27    # Call showFirstUnique to get the first unique number
28    # param_1 = obj.showFirstUnique()
29    # Add a new value to the queue
30    # obj.add(value)
31
```

Java Solution

```
1 import java.util.Map;
2 import java.util.HashMap;
3 import java.util.Deque;
4 import java.util.ArrayDeque;
5
6 class FirstUnique {
7     // Maps each number to its occurrence count
8     private Map<Integer, Integer> countMap = new HashMap<>();
9     // Queue to maintain the order of elements
10    private Deque<Integer> queue = new ArrayDeque<>();
11
12    // Constructor that initializes the data structure with the given array of numbers
13    public FirstUnique(int[] nums) {
14        for (int num : nums) {
15            add(num); // Use the add method to handle the addition of numbers
16        }
17    }
18
19    // Returns the value of the first unique number
20    public int showFirstUnique() {
21        // While the queue is not empty and the front of the queue is not unique
22        while (!queue.isEmpty() && countMap.get(queue.peekFirst()) != 1) {
23            queue.pollFirst(); // Remove it from the queue
24        }
25
26        // Return the first element in the queue if the queue is not empty, else return -1
27        return queue.isEmpty() ? -1 : queue.peekFirst();
28    }
29
30    // Adds a new number into the data structure
31    public void add(int value) {
32        // Update the occurrence count of the value
33        countMap.put(value, countMap.getOrDefault(value, 0) + 1);
34        // If it is the first time the value is added, add it to the queue
35        if (countMap.get(value) == 1) {
36            queue.offer(value);
37        }
38    }
39 }
40
41 /**
42  * The FirstUnique class can be used by creating an instance with an array of integers
43  * and calling the instance methods to show the first unique number or add new numbers to the structure.
44  * Example:
45  * FirstUnique firstUnique = new FirstUnique(new int[]{2, 3, 5});
46  * System.out.println(firstUnique.showFirstUnique()); // outputs the first unique number
47  * firstUnique.add(5); // adds a number to the data structure
48  */
49
```

C++ Solution

```
1 #include <vector>
2 #include <deque>
3 #include <unordered_map>
4
5 class FirstUnique {
6 public:
7     // Constructor that takes a vector of integers and initializes the object.
8     // @param nums - The vector of integers to process.
9     FirstUnique(std::vector<int>& nums) {
10         for (int num : nums) {
11             ++frequencyCount[num]; // Increment the frequency count of each number
12             uniqueQueue.push_back(num); // Add the number to the deque
13         }
14     }
15
16     // Returns the value of the first unique integer of the current list.
17     // @return - The first unique integer in the list, or -1 if there isn't one.
18     int showFirstUnique() {
19         while (!uniqueQueue.empty() && frequencyCount[uniqueQueue.front()] != 1) {
20             uniqueQueue.pop_front(); // Remove non-unique elements from the front
21         }
22         if (!uniqueQueue.empty()) {
23             return uniqueQueue.front(); // Return the first unique number
24         }
25         return -1; // Return -1 if there's no unique number
26     }
27
28     // Adds value to the stream of integers the class is tracking.
29     // @param value - The integer to add to the list.
30     void add(int value) {
31         ++frequencyCount[value]; // Increment the frequency count of the added number
32         uniqueQueue.push_back(value); // Add the new number to the back of the deque
33     }
34
35 private:
36     std::unordered_map<int, int> frequencyCount; // Maps each number to its frequency count in the stream
37     std::deque<int> uniqueQueue; // A deque maintaining the order of incoming numbers
38 };
39
40 /**
41  * Your FirstUnique object will be instantiated and called as such:
42  * FirstUnique* obj = new FirstUnique(nums);
43  * int firstUniqueNumber = obj->showFirstUnique();
44  * obj->add(value);
45  */
46
```

Typescript Solution

```
1 let frequencyCount: { [key: number]: number } = {}; // Maps each number to its frequency count in the stream
2 let uniqueQueue: number[] = []; // An array representing a queue maintaining the order of incoming numbers
3
4 // Function that initializes the object with an array of integers.
5 // @param nums - The array of integers to process.
6 function initializeFirstUnique(nums: number[]) {
7     frequencyCount = {}; // Reset frequency count
8     uniqueQueue = []; // Reset the unique queue
9 }
10
11 nums.forEach(num => {
12     frequencyCount[num] = (frequencyCount[num] || 0) + 1; // Increment the frequency count of each number
13     uniqueQueue.push(num); // Add the number to the queue
14 });
15
16 // Function that returns the value of the first unique integer of the current list.
17 // @return - The first unique integer in the list, or -1 if there isn't one.
18 function showFirstUnique(): number {
19     while (uniqueQueue.length > 0 && frequencyCount[uniqueQueue[0]] != 1) {
20         uniqueQueue.shift(); // Remove non-unique elements from the front
21     }
22     if (uniqueQueue.length > 0) {
23         return uniqueQueue[0]; // Return the first unique number
24     }
25     return -1; // Return -1 if there's no unique number
26 }
27
28 // Function that adds a value to the stream of integers the functions are tracking.
29 // @param value - The integer to add to the list.
30 function add(value: number) {
31     frequencyCount[value] = (frequencyCount[value] || 0) + 1; // Increment the frequency count of the added number
32     uniqueQueue.push(value); // Add the new number to the back of the queue
33 }
34
35 // Example usage:
36 // initializeFirstUnique([2, 3, 5]);
37 // console.log(showFirstUnique()); // Outputs the first unique number
38 // add(5); // Add number 5 to the queue
39 // console.log(showFirstUnique()); // Outputs the new first unique number
40
```

Time and Space Complexity

Time Complexity

For the `__init__` method:

- Constructing the `Counter` from the `nums` list involves counting the frequency of each integer in the list, which has a time complexity of $O(n)$ where n is the number of elements in `nums`.
- Initializing the `deque` with `nums` has a time complexity of $O(n)$ for copying all elements into the deque.

For the `showFirstUnique` method:

- The while loop in this method can be deceiving, but in the amortized analysis, each element gets dequeued only once due to the nature of the "first unique" constraint. Although in the worst case of a single `showFirstUnique` call, it could be $O(n)$ where n is the number of elements in the deque, the total operation across all calls is bounded by the number of `add` operations. Therefore, we consider the amortized time complexity to be $O(1)$.

For the `add` method:

- Incrementing the counter for a value is $O(1)$.
- Appending the value to the deque is also $O(1)$.

Space Complexity

- The space complexity is $O(n)$ for storing the elements in both the `Counter` and the `deque`, where n is the total number of elements that have been added (including duplicates). There is no extra space used that grows with respect to the input size or operations other than what is used to store the numbers and their counts.