1665. Minimum Initial Energy to Finish Tasks

Hard **Greedy** Array Sorting

Problem Description

represents a task where actual_i is the amount of energy needed to complete the i-th task and minimum_i is the minimum amount of energy required to start the task. The challenge is to figure out the least amount of energy we need initially to be able to complete all tasks, but what's unique is that we can tackle the tasks in any sequence we prefer. Imagine having some tasks that need a significant amount of energy to start but consume less upon completion, while others are

In this task, we are given an array called tasks, with each element being a pair of values [actual_i, minimum_i]. Each pair

easy to start but require a lot of energy to complete. The optimal sequence to complete these tasks will ensure that you never find yourself short of energy before starting a task. Given this, we are asked to calculate the minimum initial energy.

To arrive at an intuitive solution, consider that a task requiring a lot of energy to begin but not as much to finish should be tackled

Intuition

the minimum required will deplete the energy reserve, potentially preventing the start of tasks with high initial energy requirements. Hence, the solution sorts the tasks by the difference between actual_i and minimum_i. The tasks with the smallest difference (even potentially negative) are placed first, since completing these tasks either depletes the least energy from the reserve or can

later than a task that consumes more energy than it requires to start. This is because finishing tasks that spend more energy than

even recharge it. While iterating over the sorted tasks, the algorithm checks if the current energy level (cur) is sufficient to start the current task (m). If it's not enough, we need only increase our initial energy just enough to start the task (m - cur). We then deduct the actual energy spent to complete the task from cur. Throughout this process, ans tracks the total additional energy required, if any,

which ultimately will be the minimum initial energy needed to complete all tasks. **Solution Approach** The solution makes use of the sort function, a basic algorithm in Python, to arrange the tasks such that the task with the smallest

difference between the actual energy and the minimum required energy needed to start comes first. This is done to prioritize

To understand this, let's assume we have a list of tasks, each represented as [actual_i, minimum_i]. We apply the sorted

tasks that will either decrease our energy the least or could potentially increase it (if actual_i < minimum_i).

function with a custom sort key — the difference x[0] - x[1] (actual_i - minimum_i), which helps us to process tasks that are less energy-consuming first. The data structure used here is a simple list of lists, a common choice for representing a sequence of elements where each

The algorithm follows these steps: 1. Initialize ans and cur to zero. ans will hold our final answer, and cur tracks the current energy level. 2. Sort the tasks by the difference (x[0] - x[1]), which is calculated for each task using a lambda function as the key in the sorted method.

3. Iterate through the sorted tasks list. • For each task, check if our current energy cur is less than the minimum required energy m. ∘ If so, we update ans with the difference m - cur, as we need to boost our energy level up to the minimum required to start the task. We

 Deduct the actual amount of energy spent on the task a from cur. 4. The loop exits after all tasks have been processed, and ans now holds the minimum initial amount of energy we need to finish all the tasks

without running out of energy at any point.

and the current energy level (cur).

also update cur to reflect this new level of energy.

element itself contains multiple pieces of data.

energy only when necessary and by the smallest amount needed. After all tasks are completed, ans tells us the minimum energy we would need to reserve initially to accomplish this.

Using this approach allows us to guarantee that we always have enough energy to start each task by incrementing our initial

Let's say we're given the following array of tasks: [[3,1], [2,2], [1,2]]. Each task is represented as [actual_i, minimum_i]. We start by initializing ans and cur to zero. These variables will help us keep track of the additional energy needed (ans)

sorted method, the tasks are sorted as follows:

Example Walkthrough

[[1,2], [2,2], [3,1]] \rightarrow The task [1,2] has a difference of -1 (it actually gives us energy), [2,2] breaks even, and [3,1] requires 2 units more energy than it gives back.

We need to sort the tasks by the difference between actual_i and minimum_i. Using a lambda function as the key in the

- We iterate through the sorted tasks: The first task is [1, 2]. cur is 0 and is less than the minimum required energy 2 for the task. We need to increase it by 2-0=2, so ans becomes 2 and cur becomes 2. After completing the task that consumes 1 unit of energy, cur is now 2-
- 1=1. The next task is [2, 2]. cur is now 1 which is less than the 2 required to start the task. We must increase cur by 2-1=1, which means ans is updated from 2 to 2+1=3. After finishing the task that uses 2 units of energy, cur becomes 1-
- we reserved.) The final task is [3, 1]. cur is -1, and since the minimum energy to start is 1, we will boost cur by 1-(-1)=2, making

Having processed all tasks, ans holds the minimum initial amount of energy we need to complete all of them. In this case, we

By carefully selecting the sequence of the tasks and calculating the increments in our energy reserve only as needed, we find

ans now 3+2=5. We then complete the task by spending 3 units of energy, and cur is updated to -1-3=-4.

must start with at least 5 units of energy to ensure we can complete the tasks in this specific order.

that starting with 5 units of energy allows us to complete all tasks successfully.

Sort the tasks based on the difference between minimum energy needed

If current energy is less than the minimum energy needed for

the task, we need to increase our energy to at least the minimum.

and actual energy consumed (i.e., sort by actual effort required).

for actual, minimum in sorted(tasks, key=lambda x: x[0] - x[1]):

Set the current energy to the minimum required

After completing the task, decrease the current energy by

def minimumEffort(self, tasks: List[List[int]]) -> int:

energy_needed = current_energy = 0

We iterate through each sorted task.

current energy = minimum

current_energy -= actual

the amount of actual energy consumed.

#include <algorithm> // Needed to use the std::sort function

int minimumEffort(std::vector<std::vector<int>>& tasks) {

int currentEnergy = 0; // Current available energy

if (currentEnergy < minInitialEnergy) {</pre>

currentEnergy = minInitialEnergy;

// Iterate through the sorted tasks

for (auto& task : tasks) {

return (task1[0] - task1[1]) < (task2[0] - task2[1]);</pre>

totalEffort += minInitialEnergy - currentEnergy;

// current energy to represent the new state of current energy

int totalEffort = 0: // Accumulated effort required to start all tasks

// Sort the tasks based on the difference between the minimum initial energy required

// comes first because it requires less effort after completion to start the next task.

// and the actual energy consumed by the task. The task with the smallest difference

int actualEnergyConsumption = task[0]; // Actual energy consumed by the task

// then increase the totalEffort by the difference and update currentEnergy

// After the task is done, subtract the actual energy consumption from the

// If currentEnergy is less than the minimum required initial energy

int minInitialEnergy = task[1]; // Minimum initial energy required to start the task

std::sort(tasks.begin(), tasks.end(), [&](const auto& task1, const auto& task2) {

Return the total energy needed to complete all tasks.

Initialize the answer and the current energy to zero.

2=-1. (This indicates that we finished the task using not just the current energy we had, but also some of the initial energy

Python from typing import List

if current energy < minimum:</pre> # Update the total energy needed by adding the difference # between the minimum energy needed and the current energy. energy needed += minimum - current energy

return energy_needed

Solution Implementation

class Solution:

```
# Example usage:
\# tasks = [[1, 2], [2, 4], [4, 8]]
# solution = Solution()
# print(solution.minimumEffort(tasks)) # Output will be the total minimum energy needed
Java
import java.util.Arrays; // Import Arrays utility for sorting
class Solution {
    // Calculates the minimum initial energy required to complete all tasks
    public int minimumEffort(int[][] tasks) {
        // Sort the tasks by the difference between the minimum energy to start and actual energy consumed
        Arrays.sort(tasks, (a, b) \rightarrow (b[1] - b[0]) - (a[1] - a[0]));
        int totalEnergyNeeded = 0; // Total initial energy needed to start all tasks
        int currentEnergy = 0;  // Current energy level while performing tasks
        // Iterate over each task to calculate the total initial energy required
        for (int[] task : tasks) {
            int actualEnergy = task[0]; // Actual energy spent to complete the task
            int minimumEnergyToStart = task[1]; // Minimum energy required to initiate the task
            // If current energy is less than the minimum required to start the task,
            // increase the total energy needed accordingly and update the current energy
            if (currentEnergy < minimumEnergyToStart) {</pre>
                totalEnergyNeeded += minimumEnergyToStart - currentEnergy;
                currentEnergy = minimumEnergyToStart;
            // After task completion, reduce the current energy by the actual energy spent
            currentEnergy -= actualEnergy;
        // Return the calculated total initial energy needed
        return totalEnergyNeeded;
```

C++

public:

#include <vector>

class Solution {

});

```
currentEnergy -= actualEnergyConsumption;
        // Return the accumulated totalEffort required to start all tasks
        return totalEffort;
};
TypeScript
function minimumEffort(tasks: number[][]): number {
    // Sort the tasks based on the difference between minimum initial energy and actual energy consumption
    // This helps to start with tasks that require less extra energy after considering their actual energy use
    tasks.sort((task1, task2) => (task1[0] - task1[1]) - (task2[0] - task2[1]));
    let totalMinimumEnergy = 0; // The accumulated energy needed to complete all tasks
    let currentEnergy = 0; // Current energy level
    // Iterate over each task to calculate the minimum initial energy required to complete them
    for (const [actualEnergy, minimumInitialEnergy] of tasks) {
        // If the current energy is less than the task's minimum initial required energy
        if (currentEnergy < minimumInitialEnergy) {</pre>
            // Need to add the extra energy required to meet the minimum initial energy
            totalMinimumEnergy += minimumInitialEnergy - currentEnergy;
            // Update the current energy to match the minimum initial requirement
            currentEnergy = minimumInitialEnergy;
        // After completing the task, the actual energy used is subtracted from the current energy
        currentEnergy -= actualEnergy;
    // Return the accumulated minimum initial energy needed to complete all tasks
    return totalMinimumEnergy;
from typing import List
class Solution:
    def minimumEffort(self, tasks: List[List[int]]) -> int:
        # Initialize the answer and the current energy to zero.
        energy_needed = current_energy = 0
        # Sort the tasks based on the difference between minimum energy needed
        # and actual energy consumed (i.e., sort by actual effort required).
```

tasks = [[1, 2], [2, 4], [4, 8]] solution = Solution() print(solution.minimumEffort(tasks)) # Output will be the total minimum energy needed

Time Complexity

Example usage:

We iterate through each sorted task.

if current energy < minimum:</pre>

current_energy -= actual

return energy_needed

Time and Space Complexity

current energy = minimum

the amount of actual energy consumed.

for actual, minimum in sorted(tasks, key=lambda x: x[0] - x[1]):

Set the current energy to the minimum required

After completing the task, decrease the current energy by

energy needed += minimum - current energy

Return the total energy needed to complete all tasks.

If current energy is less than the minimum energy needed for

the task, we need to increase our energy to at least the minimum.

between the minimum energy needed and the current energy.

Update the total energy needed by adding the difference

The time complexity of the solution is dominated by the sorting of the tasks array and the subsequent iteration through the sorted tasks.

The sorting function uses the Timsort algorithm in Python, which has a time complexity of 0(n log n) in the average and worst case, where n is the number of tasks. After sorting, the function goes through the tasks one by one, which takes 0(n) time.

Therefore, combining both steps, the total time complexity of the function is 0(n log n) due to the sorting step being the most significant factor.

Space Complexity

The space complexity of the solution can be considered as 0(1) because the sorting is done in-place and no additional data structures that grow with the input size are used. The variables ans, cur, a, and m are all constant in space, requiring a fixed amount of memory regardless of the number of tasks.