663. Equal Tree Partition

Depth-First Search

Binary Tree

Problem Description

Medium

into two parts by removing exactly one edge, such that the sum of the nodes' values in both parts are equal. A binary tree is defined as a tree data structure where each node has at most two children, referred to as the left child and the right child. The constraint of removing exactly one edge means that we must find a sub-tree whose value equals half the sum of all node values in the entire tree.

The problem presents a scenario involving a binary tree, where the goal is to determine whether there is a way to split the tree

Intuition To solve this problem, we first think about the properties of the tree and its partitions. Since we want to split the tree into two

into two equal parts. Knowing this, we can first calculate the sum of the entire tree. To find a partition, we then perform a tree traversal (such as a depth-first search) and calculate the sum of each subtree as we go. Each subtree sum gives us a potential partition point—if the

with equal sums, the total sum of the tree's nodes must be even; otherwise, it's mathematically impossible to divide an odd sum

sum of a subtree is exactly half the total sum of the tree, then removing the edge above this subtree would indeed split the tree into two trees with equal sums.

The solution has a helper function sum which recursively computes the sum of the node values, while simultaneously constructing a list called seen that records the sum of each encountered subtree. With the total sum calculated (stored in variable s), the code checks if this sum is odd, in which case it returns False as no equal partition is possible.

Finally, before checking for the possibility of partitioning, the last element of the seen list (which is the sum of the entire tree) is removed, as the sum of the entire tree should not be considered for partitioning. This makes sure we are only considering subtrees for partitioning. The code then simply checks if half of the total sum s // 2 is found within the seen list. If it is present, it

indicates that there is a subtree whose sum is half the total sum, and thus the tree can be partitioned into two trees with equal sums by removing the edge connected to that subtree. **Solution Approach** The solution leverages a depth-first search (DFS) algorithm for recursively traversing the tree. During this traversal, the sum of each subtree is computed and stored in a list. DFS is a typical choice for tree problems, as it allows the exploration of all the

Here's a step-by-step breakdown of the implementation: A helper function named sum is defined within the Solution class to handle the DFS. This function takes a node of the tree

root.right.

(initially the root) as its argument.

partition the tree into two trees with equal sums.

If the input node is None (indicating a leaf's child), the function returns 0. Recursively calculate the sum of the left and right children of the current node by calling the sum function for root. Left and

The sum of the current subtree is the sum of the left and right subtrees plus the value of the current node (root.val). This value is appended to the list seen.

nodes and the computation of their aggregate values in a structured manner.

seen list with the subtree sums, including the total sum as the last element.

The helper function returns the last calculated sum (the sum of the current subtree). When the sum function is first called with the root of the tree, it computes the total sum of the tree's elements and populates the

The next step is to verify if the sum of the entire tree (s) is even. If it's not, we can already conclude that it's impossible to

Then, the total sum, which is the last element in the seen list, is removed because we only want to check if any subtree sum equals half of the total sum. Finally, the solution checks if half of the total sum (s // 2) is in the seen list. If it is, that means we have found a subtree sum that

is exactly half of the total, and the tree can be partitioned by removing the edge that leads to this subtree.

all subtrees encountered. The list is later used to determine if a valid partition exists. **Example Walkthrough**

Let's use a small binary tree example to illustrate the solution approach. Suppose we have the following binary tree:

This approach uses a recursive algorithm (DFS) to traverse the tree while using a list data structure to keep track of the sums of

10 10

The sum of all node values is first calculated. For our example tree, the sum is 5 + 10 + 10 + 2 + 3 = 30. Since the total sum 30 is even, it is possible for the tree to have a valid partition.

Tree 1:

Tree 2:

Python

class TreeNode:

class Solution:

Here's the walkthrough of the solution:

making the seen list [10, 15, 30].

original tree into two trees with equal sums:

Starting from the root:

• The function first calculates the sum of the left subtree which is 10. It stores this sum in the seen list. Next, it calculates the sum of the right subtree. The recursive call to sum goes to node (10), then to its left child (2), and right child (3),

combining their sums plus the node's own value (10 + 2 + 3 = 15). This sum is also recorded in the seen list.

The seen list now contains sums from the subtrees: [10, 15].

We initiate the depth-first search (DFS) with the root node (5). The helper function sum begins the traversal.

Since we do not consider the sum of the entire tree as a valid partition, the last element (30) is removed from the seen list. The final step is to check if the half of the total sum, which is 30 // 2 = 15, is found in the seen list. In our case, 15 is indeed

The function sum returns the total sum of the tree which here is 30, and this is initially appended to the seen list as well,

- in the list, corresponding to the right subtree of the root. By finding the value 15 in our seen list, we have determined that by removing the right edge of the root node, we can split the
- Both trees have a sum of 15, and thus the solution approach successfully finds a way to partition the tree into two parts with equal sums.

Recursively sum the left and the right subtrees left_sum = calculate_subtree_sum(node.left) right_sum = calculate_subtree_sum(node.right) # Update the cumulative sums we have seen subtree_sum = left_sum + right_sum + node.val cumulative_sums.append(subtree_sum) # Return the cumulative sum of the subtree rooted at the current node

Solution Implementation

Definition for a binary tree node.

 $self_val = val$

self.left = left

self.right = right

if node is None:

return 0

return subtree_sum

Calculate the total sum of the tree

total_sum = calculate_subtree_sum(root)

int nodeSum = leftSum + rightSum + node.val;

subtreeSums.add(nodeSum);

// Return the node sum

return nodeSum;

vector<int> subtreeSums;

bool checkEqualTree(TreeNode* root) {

int totalSum = sum(root);

subtreeSums.pop_back();

int sum(TreeNode* root) {

if (!root) return 0;

return subtreeSum;

// Definition for a binary tree node.

left: TreeNode | null;

right: TreeNode | null;

int leftSum = sum(root->left);

int rightSum = sum(root->right);

subtreeSums.push_back(subtreeSum);

// Return the sum of this subtree.

// Store the subtree sum in the vector.

this.val = (val === undefined ? 0 : val);

// Calculate the sum of the entire tree.

// Base case: if the node is null, return 0.

// Calculate the sum of the subtree rooted at 'root'.

int subtreeSum = leftSum + rightSum + root->val;

if (totalSum % 2 != 0) return false;

C++

public:

class Solution {

// Add the node sum to the list of subtree sums

// This vector stores the sum of all subtrees encountered.

// Function to check if a binary tree can be split into two trees with equal sum.

// Remove the sum of the entire tree as we can only split from non-root nodes.

// If the totalSum is odd, we can't split it into two equal parts.

// Check if there is a subtree with sum equal to half of the totalSum.

return count(subtreeSums.begin(), subtreeSums.end(), totalSum / 2);

// Recursive case: calculate the sum of the left and right subtrees.

constructor(val?: number, left?: TreeNode | null, right?: TreeNode | null) {

// Helper function to calculate the sum of a subtree rooted at 'root'.

cumulative_sums = []

if total_sum % 2 == 1:

def ___init___(self, val=0, left=None, right=None):

Base case: if the node is None, return 0

Helper function to calculate the sum of subtree node values

Initialize a list to store the cumulative sums of the subtrees

If the total sum is odd, there cannot be two equal subtree sums

def checkEqualTree(self, root: TreeNode) -> bool:

def calculate_subtree_sum(node):

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return False
       # The last element in cumulative_sums is the total sum of the tree
       # which must be removed before checking for an equal partition
       cumulative_sums.pop()
       # Check if there is a subtree whose sum is half of the total sum
       half_sum = total_sum // 2
       return half_sum in cumulative_sums
Java
class Solution {
   // This list will keep track of the sums of all seen subtrees
   private List<Integer> subtreeSums;
   // Main method to check if the tree can split into two
   // with the equals sum for both parts
    public boolean checkEqualTree(TreeNode root) {
       subtreeSums = new ArrayList<>();
       // Calculate the sum of the whole tree
       int totalSum = calculateSum(root);
       // If total sum of the tree is odd, it cannot be split into equal sum part
       if (totalSum % 2 != 0) {
           return false;
       // We remove the last element as it represents the
       // sum of the whole tree, which we don't want to consider as a split point
        subtreeSums.remove(subtreeSums.size() - 1);
       // Check if any subtree sum is equal to half of the total sum
       return subtreeSums.contains(totalSum / 2);
   // Helper method to calculate the sum of the tree or subtree
   // and store the sums in 'subtreeSums' list
   private int calculateSum(TreeNode node) {
       // If node is null, the sum is 0
       if (node == null) {
            return 0;
       // Recursively calculate the sum of left and right subtrees
       int leftSum = calculateSum(node.left);
       int rightSum = calculateSum(node.right);
       // Node sum is its value plus the sum of its left and right subtrees
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this.left = (left === undefined ? null : left);
this.right = (right === undefined ? null : right);
```

};

TypeScript

class TreeNode {

val: number;

```
// This array stores the sum of all subtrees encountered.
  let subtreeSums: number[] = [];
  // Function to check if a binary tree can be split into two trees with equal sum.
  function checkEqualTree(root: TreeNode | null): boolean {
      // Calculate the sum of the entire tree.
      let totalSum = sum(root);
      // If the total sum is odd, it cannot be split into two equal parts.
      if (totalSum % 2 !== 0) return false;
      // Remove the sum of the entire tree as we can only split from non-root nodes.
      subtreeSums.pop();
      // Check if there is a subtree with sum equal to half of the total sum.
      return subtreeSums.includes(totalSum / 2);
  // Helper function to calculate the sum of a subtree rooted at 'root'.
  function sum(node: TreeNode | null): number {
      // Base case: if the node is null, return 0.
      if (!node) return 0;
      // Recursive case: calculate the sum of the left and right subtrees.
      let leftSum = sum(node.left);
      let rightSum = sum(node.right);
      // Calculate the sum of the subtree rooted at 'root'.
      let subtreeSum = leftSum + rightSum + node.val;
      // Store the subtree sum in the array.
      subtreeSums.push(subtreeSum);
      // Return the sum of this subtree.
      return subtreeSum;
# Definition for a binary tree node.
# class TreeNode:
     def __init__(self, val=0, left=None, right=None):
         self.val = val
         self.left = left
         self.right = right
class Solution:
   def checkEqualTree(self, root: TreeNode) -> bool:
       # Helper function to calculate the sum of subtree node values
        def calculate_subtree_sum(node):
            # Base case: if the node is None, return 0
            if node is None:
                return 0
            # Recursively sum the left and the right subtrees
            left_sum = calculate_subtree_sum(node.left)
            right_sum = calculate_subtree_sum(node.right)
            # Update the cumulative sums we have seen
            subtree_sum = left_sum + right_sum + node.val
            cumulative_sums.append(subtree_sum)
            # Return the cumulative sum of the subtree rooted at the current node
            return subtree_sum
       # Initialize a list to store the cumulative sums of the subtrees
        cumulative_sums = []
       # Calculate the total sum of the tree
        total_sum = calculate_subtree_sum(root)
       # If the total sum is odd, there cannot be two equal subtree sums
       if total_sum % 2 == 1:
            return False
       # The last element in cumulative_sums is the total sum of the tree
       # which must be removed before checking for an equal partition
        cumulative_sums.pop()
       # Check if there is a subtree whose sum is half of the total sum
        half_sum = total_sum // 2
        return half_sum in cumulative_sums
Time and Space Complexity
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Time Complexity

sum is called recursively for each node of the binary tree. Therefore, in the worst-case scenario, which is when the binary tree is either completely unbalanced or is a complete tree, the function sum will be called once for each node. Given that there are n nodes in the binary tree, the time complexity of the algorithm is O(n), where n is the number of nodes in the tree. This is because each node is processed exactly once to compute its sum and store it in the seen list. **Space Complexity**

The given Python function entails a depth-first traversal of the binary tree to compute the sum of the tree nodes. The function

The space complexity is determined by the storage required for the recursive function calls (the call stack) and the additional space used by the list seen that keeps track of the sum of each subtree. In the worst-case scenario (in a completely unbalanced tree), the maximum depth of the recursive call stack can be O(n). The list seen will also store n-1 different sums (since the last total sum isn't included, as observed from seen.pop()), contributing O(n) space complexity. Therefore, the overall space complexity of the function is O(n), considering both the recursion call stack and the seen list together.