2405. Optimal Partition of String

### Leetcode Link

# Problem Description

This problem asks to partition a given string s into the minimum number of substrings where each substring contains unique characters; no character is repeated within a single substring. All characters in the original string must be used exactly once in some substring, and no character can be in more than one substring. The goal is to find and return the smallest possible number of such unique-character substrings.

# The solution approach is to iterate over the characters of the string while keeping track of characters we have seen in the current

Intuition

substring. There are different strategies to keep track of the unique characters. For example, we could use a set, an array, or, as in the provided solution, a bit vector (which is an integer that represents a set of characters using bits). Here's the rundown of the intuition:

 We initialize a counter (ans) for the number of substrings to 1 because we need at least one substring. We also initialize a bit vector (v) to represent the characters we've seen in the current substring.

- We iterate through the string character by character.
- For each character, we convert it to a unique integer representing its position in the alphabet (i), where 'a' corresponds to 0, 'b'

current substring. Let's delve into the details of the algorithm and the data structures used:

1, where 0 would represent 'a' and 25 would represent 'z'.

- to 1, and so on. This is simply the ASCII value of the character minus the ASCII value of 'a'.
- We use bitwise operations to check if the bit at position in the bit vector v is already set, which would imply that the character has already appeared in the current substring. • If the character is already in the substring (i.e., the bit is set), we must start a new substring. So, we reset the bit vector to 0, and
- increment our substring counter (ans) by 1. Regardless of whether we've started a new substring, we now add the current character to the current substring by setting the bit at the corresponding position i in the bit vector v (using the bitwise OR operation).
- After processing all characters, the counter ans holds the minimum number of substrings needed, which we return.
- Using a bit vector is particularly efficient in terms of space since it replaces a potentially large set or array with a single integer and makes use of fast bitwise operations to manage the set of characters.

Solution Approach

The implementation of the solution involves a bit manipulation strategy to keep track of which characters have been seen in the

### • Bit Vector: A bit vector is the primary data structure used here. It is simple, yet powerful for tracking the presence of characters.

are performed:

A 32-bit integer can be used as a bit vector because the lower 26 bits can represent each letter of the English alphabet. Iterating Over the String: The solution iterates over each character in the given string . For each character, the following steps

- Convert the character to an index:
- 1 i = ord(c) ord('a')This uses the ord() function to get the ASCII value of c and then subtracts the ASCII value of 'a' to get a zero-based index
  - Check for Character's Presence:

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This checks if the bit at position i of the bit vector v is already set, which signifies that the character has been seen
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1 if (v >> i) & 1:

ans += 1

substring's character set.

 Update the Bit Vector: 1 v |= 1 << i After potentially starting a new substring, the bit at position i is set in v using a bitwise OR (1). The expression 1 << i creates an integer with only the i'th bit set, and then v is updated to include that bit, adding the character to the current

previously in the current substring. The solution uses bitwise right shift (>>>) to move the bit of interest to the least significant

bit position, and bitwise AND (&) with 1 to isolate that bit. If this results in a value of 1, indicating the character is a duplicate

in the current substring, the counter ans is incremented by 1, and v is reset to 0, signaling the start of a new substring.

Example Walkthrough

space-efficient and fast due to the nature of bitwise operations being low-level and quick on modern computer architectures.

This approach effectively utilizes bit manipulation to compactly track characters and manage substrings, making the solution both

• Returning the Final Answer: At the end of the loop, once all characters in s have been processed, the ans variable holds the

string into the minimum number of substrings with unique characters. 1. Initialize Counters: Let's initialize our substring counter ans to 1 and our bit vector v to 0.

To illustrate the solution approach, let's walk through a small example. Consider the string s = "abac". We want to partition this

### • We check if bit 0 in v is already set by checking (v >> 1) & 1. Since v is 0, the bit is not set.

 We then set bit 0 in v to mark 'a' as seen (v becomes 1 after v |= 1 << i).</li> 3. Process Second Character: Next is 'b':

 We check if bit 1 in v is set, which it's not. We set bit 1 in v (v becomes 3 after v |= 1 << i).</li>

2. Process First Character: Starting with the first character 'a':

The index i for 'a' is 0 (ord('a') - ord('a')).

The index i for 'b' is 1 (ord('b') - ord('a')).

4. Process Third Character: Now we encounter 'a' again:

We then set bit 0 in v again (v becomes 1).

5. Process Fourth Character: Lastly, we have 'c':

def partitionString(self, s: str) -> int:

char\_index = ord(char) - ord('a')

used\_characters = 0

bitMask |= 1 << bitNumber;

// Initialize a Set to store unique characters

// Initialize variable to count partitions

// Iterate over each character in the string

// Add the current character to the set

if (uniqueChars.has(char)) {

uniqueChars.clear();

// Return the total number of partitions

partitionCount++;

uniqueChars.add(char);

Time and Space Complexity

// If the character is already in the set, increment the partition count

// and clear the set to start a new partition with unique characters

const uniqueChars = new Set();

let partitionCount = 1;

for (const char of s) {

return partitionsCount;

// Return the total number of partitions needed

used\_characters |= 1 << char\_index</pre>

partitions += 1

number of substrings formed and is returned as the final answer.

- The index for 'a' is still 0.
- current substring. Since 'a' is a repeating character, we increment ans to 2 and reset v to 0.

needs to be started, ensuring that each substring contains unique characters.

# Initialize 'partitions' as the counter for required partitions and

# 'used\_characters' to keep track of the characters used in the current partition.

# Check if the character has already been used in the current partition.

# Set the bit at the character's index to 1 to mark it as used for the current partition.

# Return the number of partitions needed such that no two partitions have any characters in common.

The index i for 'c' is 2 (ord('c') - ord('a')). We check if bit 2 in v is set, which it's not.

unique characters, which are "ab" and "ac".

 We set bit 2 in v (v becomes 5 after v |= 1 << i).</li> After processing all characters in s, we have an ans of 2, indicating the given string "abac" can be partitioned into 2 substrings with

This example demonstrates how the solution efficiently tracks characters using bit manipulation to ascertain when a new substring

Checking (v >> i) & 1, we find that the bit is set since v is 3 (binary 11), which means 'a' was already included in the

used\_characters = 0 # Iterate over each character in the string. for char in s: 9 # Calculate the bit index corresponding to the character.

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# (v >> i) & 1 checks if the ith bit in 'used_characters' is set to 1,
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               # meaning that character was already used.
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               if (used_characters >> char_index) & 1:
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                   # If so, we need a new partition. Reset 'used_characters' and
                   # increment the 'partitions' counter.
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Python Solution

partitions = 1

class Solution:

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           return partitions
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Java Solution
   class Solution {
       public int partitionString(String s) {
           // 'bitMask' is used to keep track of the characters seen in the current partition
           int bitMask = 0;
           // 'partitionsCount' represents the number of partitions needed
           int partitionsCount = 1;
8
           // Iterate over each character in the string
9
           for (char character : s.toCharArray()) {
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               // Calculate the bit number corresponding to 'character'
               int bitNumber = character - 'a';
12
               // 'bitMask >> bitNumber' shifts the bitMask 'bitNumber' times to the right
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15
               // '& 1' checks if the bit at position 'bitNumber' is set to 1, i.e., if character is already seen
               if (((bitMask >> bitNumber) & 1) == 1) {
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                   // If the character has been seen, reset bitMask for a new partition
                   bitMask = 0;
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                   // Increment partition count as we're starting a new partition
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                   ++partitionsCount;
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               // '|=' is the bitwise OR assignment operator. It sets the bit at position 'bitNumber' in bitMask to 1
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               // '1 << bitNumber' creates a bitmask with only bitNumber'th bit set
               // This indicates that character is included in the current partition
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C++ Solution

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1 class Solution {
2 public:
       // Function to determine the number of substrings without repeating characters
       int partitionString(string s) {
           int numPartitions = 1; // Initialize the count of partitions to 1
           int charBitset = 0;  // Use a bitset to track the occurrence of characters
           // Iterate through each character in the string
           for (char c : s) {
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               int charIndex = c - 'a'; // Convert character to its corresponding bit index
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               // Check if the character has already been seen in the current partition
               // by checking the corresponding bit in the bitset
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               if ((charBitset >> charIndex) & 1) {
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                   // If the character is repeated, start a new partition
                   charBitset = 0; // Reset the bitset for the new partition
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                   ++numPartitions; // Increment the count of partitions
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               // Mark the current character as seen in the bitset for the current partition
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               charBitset |= 1 << charIndex;</pre>
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24
           // Return the total number of partitions found
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           return numPartitions;
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27 };
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Typescript Solution
1 // Function that calculates the minimum number of partitions
2 // of a string such that each letter appears in at most one part
   function partitionString(s: string): number {
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## 25 } 26

return partitionCount;

Time Complexity The time complexity of the algorithm is primarily determined by the loop through the string s. Since each character in the string is checked exactly once, the time complexity is O(n), where n is the length of the string s.

characters.

During each iteration, the operations performed include basic bitwise operations (>>, &, |, and <<), which are O(1) operations, and thus do not affect the linear nature of the time complexity.

Therefore, the time complexity of the code is O(n). Space Complexity

The space complexity of the algorithm is due to the storage required for the variable v, which serves as a mask to track the unique

Since v is a single integer and its size does not grow with the size of the input string s, the space complexity of storing this integer is constant O(1), regardless of the length of the string.

Additionally, since there are no other data structures used that scale with the input size, the overall space complexity remains constant.

Hence, the space complexity of the code is 0(1).

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