565. Array Nesting **Depth-First Search Array** Medium

Problem Description

In this problem, you are given an integer array nums with a length of n, where nums is a permutation of the numbers in the range [0, n - 1]. The goal is to create a unique set s[k] for each index k in the array. The set s[k] is formed by repeatedly applying the transformation nums[i] -> nums[nums[i]] starting with nums[k]. The transformation stops when it would add a duplicate element to s[k].

In other words:

- 1. Begin with an index k and the corresponding element nums [k], and add it to the set s[k]. 2. Find the next element by using the current element as the index to look up the next value in the array (nums [nums [k]]), and add that to the set.
- 3. Continue the process, each time using the latest element added to the set as the new index to look up. 4. Stop when you are about to add an element that is already in the set, because that would create a duplicate.
- The task is to determine the size of the largest set s[k] that can be created by following the above rules.

Intuition

exactly one cycle. Once you visit an element in nums, all subsequent elements that would be visited by following the transformation rule are part of the same cycle, and re-visiting them would just repeat the cycle without increasing the size of any set s[k]. The strategy, therefore, is to iterate through each element of nums and trace out the cycle, marking elements as visited by

To tackle the problem, note that since nums is a permutation of the numbers in [0, n - 1], every element in nums is part of

setting them to a value outside the range [0, n - 1] (for instance, n). Count the number of steps it takes to complete the cycle. This count represents the size of the set s[k] formed by starting at the index k. By doing this for each index k and keeping track of the maximum count found, we can identify the longest length of a set s[k].

The elements are marked as visited to avoid redundant computations and to ensure that once an element is a part of a set, it is

not counted again for subsequent indices. Solution Approach

each element, it tracks the formation of the set s[k] by following the chain of indices as described by the transformation rule

nums[i] -> nums[nums[i]]. Here is the step-by-step explanation of the process using the given code: 1. Initialize a variable ans to store the length of the largest set s[k] and set its initial value to zero (0). Initialize n to the length of nums.

The implemented solution follows a simple yet effective approach. It traverses through each element of the array nums, and for

4. Retrieve the number at the current index i (stored in j), then mark the element at i as visited by setting nums[i] to n.

2. Loop through each index i from 0 to n-1. The variable cnt is used to keep track of the length of the set s[k] starting at index i.

5. Set the current index i to j to move to the next number in the set. 6. Increment the counter cnt which reflects the size of the current set s[k].

3. Inside the loop, follow the cycle that starts at nums[i]. The while loop continues as long as the current element nums[i] has not been visited (a

- 7. Once a cycle is traced (and the while loop exits), compare the size of this set (cnt) with the previous maximum (ans) and update ans if cnt is
- larger. 8. Continue with the next index, marking elements and counting the size of each set until all indices are processed.

9. Return ans, which is the length of the longest set s[k].

visited element is marked by setting it to n).

- Through this algorithm, all sets are explored only once, since any index that has been visited and marked will not be considered
- again. The code effectively avoids duplicating work by marking the visited elements. This mechanism is key to ensuring the algorithm runs efficiently and the solution's time complexity is kept at O(n), where n is the size of the input array nums.
- Mathematically, you could view this as tracing cycles in a graph where nodes represent elements in the array and directed edges

more than once. **Example Walkthrough**

Let's take an example array nums with the permutation of numbers [1, 2, 0, 4, 5, 3]. Here's the step-by-step walkthrough to

connect node i to node nums[i]. The objective is to find the length of the longest cycle in this graph without visiting any node

Initialize the answer ans to 0. Since the length of nums is 6, initialize n to 6.

Start the loop with index i = 0. Here, nums[0] = 1. Initialize cnt = 0 which will count the size of set s[0]. Begin the transformation for set s [0]:

 \circ Now, i = 1 and nums[1] = 2, so the next index to visit is 2 and cnt becomes 2. We mark nums[1] as visited. Next, i = 2 and nums[2] = 0, but nums[0] has already been visited, so the cycle is complete, and we stop here.

nums[3] = 4 and cnt is reset to 1. We mark nums[3] as visited.

• Finally, nums [3] is already marked as visited, so we end the cycle.

with a linear time complexity relative to the size of the array nums.

The size of set s[0] is 2. We compare it with ans and since 2 > 0, we update ans to 2.

o nums [0] = 1, so the next index to visit is 1 and cnt becomes 1. We mark nums [0] as visited by setting it to n.

visited, so we move on to i = 3.

find the size of the largest set s[k].

 Next, i = 4 and nums[4] = 5. Increment cnt to 2 and mark nums[4] as visited. \circ Then, i = 5 and nums[5] = 3. cnt is incremented to 3 and mark nums[5] as visited.

Move to the next index i = 1, but we have already visited nums [1], so we skip to the next one, i = 2. This index is also

7. The size of the set formed starting at index 3 is 3. We compare it with $\frac{1}{2}$ and since $\frac{1}{2}$, we update $\frac{1}{2}$ and $\frac{1}{2}$.

larger than 3.

For i = 3, the process is:

- Continuing this process for the remaining unvisited indices (which are none in this case), we find that no other set has a size
- Having completed the cycle for each index, the largest set s[k] has size 3, so we return ans = 3.

Through the above example, we were able to find the longest cycle in the permutation graph, which represents the size of the

largest set s[k]. The algorithm efficiently marks visited nodes to avoid redundant calculations, leading to an optimized solution

Solution Implementation **Python**

Mark the current element as visited by setting it to num_elements.

from typing import List # We need to import List from typing to use it as a type hint.

class Solution: def arrayNesting(self, nums: List[int]) -> int: # Initialize the max size of the nesting to 0. max nesting size = 0# Get the length of the input list.

current set size = 0 # Continue traversing the set until we find an element that is marked as visited. while nums[i] != num elements: # Fetch the next index from the current element.

num_elements = len(nums)

for i in range(num elements):

next index = nums[i]

Iterate through each element in the list.

Initialize count for the current set.

return maxNestSize; // Return the size of the largest nest

```
nums[i] = num elements
                # Move to the next index.
                i = next index
                # Increment the size count for the current set.
                current set size += 1
            # Update the maximum nesting size if the current set size is larger.
            max_nesting_size = max(max_nesting_size, current_set_size)
        # Return the maximum size of nesting found.
        return max_nesting_size
Java
class Solution {
    public int arrayNesting(int[] nums) {
        int maxNestSize = 0; // Variable to keep the size of the largest nest
        int arrayLength = nums.length; // Get the length of the array
        for (int start = 0: start < arrayLength: ++start) { // Loop through each element in the array</pre>
            int size = 0; // Initialize size for the current nest
            int currentIndex = start; // Starting index for the current nest
            // Iterate through the nest starting at currentIndex until a visited element is found
            while (nums[currentIndex] < arrayLength) { // Visited elements are marked with value equal or greater than arrayLength
                int nextIndex = nums[currentIndex]; // Get the next index in the nest
                nums[currentIndex] = arrayLength; // Mark the current index as visited
                currentIndex = nextIndex; // Move to the next index
                ++size; // Increase the size of the current nest
            maxNestSize = Math.max(maxNestSize, size); // Update the size of the largest nest found so far
```

// This will hold the maximum size of the nest

int tempIndex = nums[currentIndex]; // Store next index from the current element's value

// Increment the nest size

int numElements = nums.size(); // Get the number of elements in the array

int currentIndex = i; // Start nesting from the current index

// Loop to find the nest size starting from the current index

int nestSize = 0;
// Initialize the size for the current nest

nums[currentIndex] = numElements: // Mark the current element as visited

currentIndex = tempIndex; // Move to the next index in the nest

C++

public:

class Solution {

int arrayNesting(vector<int>& nums) {

++nestSize;

// Iterate through each element in the array

while (nums[currentIndex] < numElements) {</pre>

maxNestSize = max(maxNestSize, nestSize);

def arrayNesting(self, nums: List[int]) -> int:

Get the length of the input list.

 \max nesting size = \emptyset

 $num_elements = len(nums)$

Initialize the max size of the nesting to 0.

// Update maxNestSize if the current nest is bigger

for (int i = 0; i < numElements; ++i) {</pre>

int maxNestSize = 0;

```
return maxNestSize;
                                             // Return the largest nest size found
TypeScript
function arrayNesting(nums: number[]): number {
    let maxNestSize: number = 0; // This will hold the maximum size of the nest
    let numElements: number = nums.length; // Get the number of elements in the array
    // Iterate through each element in the array
    for (let i = 0; i < numElements; ++i) {</pre>
        let nestSize: number = 0; // Initialize the size for the current nest
        let currentIndex: number = i; // Start nesting from the current index
        // Loop to find the nest size starting from the current index
        while (nums[currentIndex] < numElements) {</pre>
            let tempIndex: number = nums[currentIndex]; // Store the next index from the current element's value
            nums[currentIndex] = numElements; // Mark the current element as visited
            currentIndex = tempIndex; // Move to the next index in the nest
            nestSize++; // Increment the nest size
        // Update maxNestSize if the current nest is larger
        maxNestSize = Math.max(maxNestSize, nestSize);
    return maxNestSize; // Return the largest nest size found
from typing import List # We need to import List from typing to use it as a type hint.
```

class Solution:

```
# Iterate through each element in the list.
for i in range(num elements):
    # Initialize count for the current set.
    current set size = 0
    # Continue traversing the set until we find an element that is marked as visited.
   while nums[i] != num elements:
        # Fetch the next index from the current element.
        next index = nums[i]
        # Mark the current element as visited by setting it to num_elements.
        nums[i] = num elements
        # Move to the next index.
        i = next index
        # Increment the size count for the current set.
        current set size += 1
   # Update the maximum nesting size if the current set size is larger.
   max_nesting_size = max(max_nesting_size, current_set_size)
# Return the maximum size of nesting found.
return max_nesting_size
```

Time and Space Complexity

linear time complexity relative to the size of the input array.

Space Complexity

Time Complexity The time complexity of the code is O(n). This is because each element is visited only once. The while loop marks visited elements by setting their value to n, ensuring that each element can become the start of a set at most once. Since the input array has n elements, and we are doing constant time operations per element, traversing and marking all elements results in a

The space complexity of the code is 0(1) (ignoring the input size). This is due to the fact that no additional space proportional to

the input size is used. The variables ans, n, cnt, i, and j only use a constant amount of extra space.