523. Continuous Subarray Sum

Math

Hash Table

Medium Array

Problem Description

The problem provides an integer array nums and an integer k. The task is to determine whether there exists at least one subarray within nums that is both of length two or more and whose sum of elements is a multiple of k. A subarray is defined as a contiguous sequence of elements within the parent array. It's important to note that any integer is considered a multiple of k if it can be expressed as n * k for some integer n. Zero is also considered a multiple of k by this definition (since 0 = k * 0).

Intuition

To solve this problem, we can utilize the properties of modular arithmetic. The key observation here is that if the sum of a subarray nums[i:j] (where i < j) is a multiple of k, then the cumulative sums sum[0:i-1] and sum[0:j] will have the same remainder when divided by k. This stems from the fact that if (sum[0:j] - sum[0:i-1]) is a multiple of k, then (sum[0:j] % k) = (sum[0:i-1] % k).

The algorithm proceeds as follows:

- 1. Iterate through the array, computing the cumulative sum s as we go.
- 2. At each step, calculate the remainder of the sum s divided by k (denoted as r = s % k). 3. Maintain a dictionary (mp) that maps each remainder to the earliest index where that remainder was seen.

Prefix Sum

- 4. For each calculated remainder r, check if we have seen this remainder before. If we have and the distance between the current
- index and the index stored in the dictionary mp[r] is at least two, this means we've found a good subarray, and we return True. 5. If the remainder has not been seen before, store the current index in the dictionary against the remainder r.
- 6. If no good subarray is found throughout the iteration, return False after the loop completes.
- whose sum is a multiple of k. The storage of the earliest index where each remainder occurs is crucial for determining the length of

By using this approach, we are effectively tracking the cumulative sums in such a way that we can efficiently check for subarrays

the subarray without having to store all possible subarrays.

The solution approach leverages the concept of prefix sums and modular arithmetic to identify a subarray sum that is a multiple of k.

iterate through the array.

Solution Approach

Here is the step-by-step explanation of how the solution is implemented: 1. Initialize a Variable to Store Cumulative Sum (s): We define a variable s that will hold the cumulative sum of the elements as we

- 2. Create a Dictionary (mp) to Store Remainders and Their Earliest Index: A Python dictionary mp is used to map each encountered remainder when dividing the cumulative sum by k to the lowest index where this remainder occurs. The dictionary is initialized
- with {0: -1} which handles the edge case wherein the cumulative sum itself is a multiple of k from the beginning of the array (i.e., the subarray starts at index 0). 3. Iterate Through the Array: Using a for-loop, we iterate through the array while keeping track of the current index i and the element value v.
- 4. Update Cumulative Sum: With each iteration, we update the cumulative sum s by adding the current element value v to it: s +=
- ٧. 5. Calculate Remainder: We calculate the remainder r of the current cumulative sum s when divided by k: r = s % k.
- 6. Check for a Previously Encountered Remainder: If the remainder r has been seen before, and the index difference i mp[r] is greater than or equal to 2, we have found a "good subarray." This is because the equal remainders signify that the sum of
- elements in between these two indices is a multiple of k. If such a condition is met, the function returns True. 7. Store the Remainder and Index If Not Already Present: If the remainder r has not been previously encountered, we store this remainder with its corresponding index i into the dictionary: mp[r] = i.
- 8. Return False If No Good Subarray Is Found: If the for-loop completes without returning True, it implies that no "good subarray" has been found. In this case, the function returns False.
- By using a hashmap to keep track of the remainders, the algorithm ensures a single-pass solution with O(n) time complexity and O(min(n, k)) space complexity, since the number of possible remainders is bounded by k.

Example Walkthrough Let's go through an example to illustrate the solution approach. Suppose we have an array nums = [23, 2, 4, 6, 7] and an integer k

= 6. We want to find out if there exists at least one subarray with a sum that is a multiple of k.

 \circ Calculate remainder r: r = 23 % 6 = 5.

 \circ Remainder 5 is not in mp, so we add it: mp = {0: -1, 5: 0}.

1. Initialize Cumulative Sum and Dictionary: s = 0. Dictionary mp is initialized as $\{0: -1\}$.

 \circ Index i = 0, Element v = 23. \circ Update s: s = 0 + 23 = 23.

subarray meets the criteria, thus the function would terminate early with a positive result.

A dictionary to keep track of the earliest index where

a particular modulus (prefix_sum % k) is found.

prefix_sum += value

for (int i = 0; i < nums.length; ++i) {</pre>

sum += nums[i];

int remainder = sum % k;

if (modIndexMap.count(mod)) {

modIndexMap[mod] = i;

} else {

return true;

// Add current number to the sum

// Calculate the remainder of the sum w.r.t k

// If the remainder is already in the map and the subarray is of size at least 2

// We found a subarray with a sum that is a multiple of k

// Put the remainder and index in the map if not already present

// If the distance between two same modulus is at least 2,

// If this modulus hasn't been seen before, record its index

// it indicates a subarray sum that is a multiple of k

if (i - modIndexMap[mod] >= 2) return true;

if (remainderIndexMap.containsKey(remainder) && i - remainderIndexMap.get(remainder) >= 2) {

3. Iteration 2:

2. Iteration 1:

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\circ Index i = 1, Element v = 2.
     \circ Update s: s = 23 + 2 = 25.
     \circ Calculate remainder r: r = 25 % 6 = 1.
     \circ Remainder 1 is not in mp, so we add it: mp = {0: -1, 5: 0, 1: 1}.
4. Iteration 3:
    \circ Index i = 2, Element v = 4.
     \circ Update s: s = 25 + 4 = 29.
     \circ Calculate remainder r: r = 29 % 6 = 5.
     \circ Remainder 5 is already in mp, and i - mp[5] = 2 - 0 = 2 which is equal to or greater than 2, hence we have found a "good"
      subarray" [23, 2, 4] with sum 29 which is a multiple of k (since 29 - 23 = 6 which is 6*1).
     • Return True.
```

class Solution: def checkSubarraySum(self, nums: List[int], k: int) -> bool: # Initialize the prefix sum as zero prefix_sum = 0

In this example walkthrough, we found a "good subarray" in the third iteration and therefore returned True. This means at least one

$mod_index_map = \{0: -1\}$ # The modulus 0 is at the "imaginary" index -1 9 # Iterate over the list of numbers 10 11 for index, value in enumerate(nums): 12 # Update the prefix sum with the current value

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Python Solution

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               # Get the modulus of the prefix sum with 'k'
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               modulus = prefix_sum % k
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17
               # If the modulus has been seen before and the distance between
18
               # the current index and the earlier index of the same modulus
19
20
               # is at least 2, we found a subarray sum that's multiple of k
               if modulus in mod_index_map and index - mod_index_map[modulus] >= 2:
21
22
                   return True
23
24
               # Store the index of this modulus if it's not seen before
25
               if modulus not in mod_index_map:
26
                   mod_index_map[modulus] = index
27
           # No subarray found that sums up to a multiple of k
28
           return False
29
30
Java Solution
   class Solution {
       public boolean checkSubarraySum(int[] nums, int k) {
           // HashMap to store the remainder of the sum encountered so far and its index
           Map<Integer, Integer> remainderIndexMap = new HashMap<>();
           // To handle the case when subarray starts from index 0
           remainderIndexMap.put(0, -1);
           // Initialize the sum to 0
           int sum = 0;
 9
10
           // Iterate through the array
```

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remainderIndexMap.putIfAbsent(remainder, i);
22
23
24
           // If we reach here, no valid subarray was found
25
           return false;
26
27 }
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C++ Solution
1 #include <vector>
2 #include <unordered_map>
   using namespace std;
   class Solution {
   public:
       // Function to check if the array has a contiguous subarray of size at least 2
       // that sums up to a multiple of k
       bool checkSubarraySum(vector<int>& nums, int k) {
9
           // Create a map to store the modulus occurrence with their index
10
11
           unordered_map<int, int> modIndexMap;
12
           modIndexMap[0] = -1; // Initialize with a special case to handle edge case
13
           int sum = 0; // Accumulated sum
14
15
           // Iterate through the numbers in the vector
           for (int i = 0; i < nums.size(); ++i) {</pre>
16
               sum += nums[i]; // Add current number to sum
17
               int mod = sum % k; // Current modulus of sum by k
18
19
20
               // Check if the modulus has been seen before
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           // If no qualifying subarray is found, return false
32
           return false;
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34 };
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Typescript Solution
 1 // Importing necessary utilities
 2 import { HashMap } from 'hashmap';
   // Function to check if the array has a contiguous subarray of size at least 2
  // that sums up to a multiple of k
   function checkSubarraySum(nums: number[], k: number): boolean {
       // Create a map to store the modulus occurrence with their index
       let modIndexMap: Map<number, number> = new Map();
 8
       modIndexMap.set(0, -1); // Initialize with a special case to handle edge case
 9
       let accumulatedSum = 0; // Accumulated sum
10
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12
       // Iterate through the numbers in the array
13
       for (let i = 0; i < nums.length; ++i) {</pre>
           accumulatedSum += nums[i]; // Add current number to the accumulated sum
14
           let mod = accumulatedSum % k; // Current modulus of the accumulated sum by k
16
           // Check if the modulus has been seen before
17
           if (modIndexMap.has(mod)) {
18
19
               // If the distance between two same modulus is at least 2,
               // it indicates a subarray sum that is a multiple of k
20
               if (i - modIndexMap.get(mod)! >= 2) return true;
           } else {
               // If this modulus hasn't been seen before, record its index
               modIndexMap.set(mod, i);
```

Time and Space Complexity

22 23 24 25 26 27 28 // If no qualifying subarray is found, return false 29 return false; 30 } 31

The provided code consists of a single loop that iterates over the list nums once. For each element of nums, it performs constant-time operations involving addition, modulus, and dictionary access (both lookup and insert). Therefore, the time complexity is determined by the loop and is O(n), where n is the number of elements in nums.

Time Complexity

Space Complexity The space complexity of the code is primarily dependent on the dictionary mp that is used to store the remainders and their respective indices. In the worst case, each element could result in a unique remainder when taken modulo k. Therefore, the

maximum size of mp could be n (where n is the number of elements in nums). Thus, the space complexity is also O(n).