Problem Description

Array

Greedy

Hard

traversing these arrays according to a set of rules. A valid path through the arrays is defined by starting at the first element of either nums1 or nums2 and then moving from left to right. If, during your traversal, you encounter a value that exists in both nums1 and nums2, you are allowed to switch to the other array—but only once for each value. The score is the sum of all unique values that you encounter on this path. The goal is to find the maximum possible score for all valid paths. As the final score might be large, you should return the result modulo $10^9 + 7$.

You are presented with two distinct sorted arrays nums1 and nums2. Your task is to find the maximum score you can achieve by

Intuition

both arrays. Since you are allowed to switch between arrays at common elements, you should do so in a way that maximizes the score. The key is to walk through both arrays in parallel and track two sums: one for nums1 and another for nums2. As long as the numbers in

both arrays are distinct, keep adding them to their respective sums. When a common element is met, you have a choice to switch

To solve this problem, one needs to understand that the maximum score is obtained by traversing through the maximum values from

paths. You want to take the path with the greater sum up to this point since that gives you the maximum score. From that common element, reset both sums to the greater sum and continue the process. By doing this, you effectively collect the maximum values from both arrays and switch paths at the optimal times to ensure you are always on the path with the greatest potential score. When you reach the end of both arrays, the maximum sum at that point will be

the maximum score that can be obtained. **Solution Approach**

The solution is an elegant application of the two-pointer technique, which is well-suited for problems involving sorted arrays.

Because the two arrays are sorted and the problem description allows us to switch paths at common elements, the two-pointer

method allows us to efficiently compare elements from both arrays without needing additional space. Here's how the given solution works step by step:

1. Initialize two pointers, i and j, to start at the beginning of nums1 and nums2, respectively. 2. Initialize two sums, f and g, to keep track of the running sum for nums1 and nums2. These variables will also help decide when to switch paths.

- 3. Use a while loop to continue processing until both pointers have reached the end of their respective arrays (i < m or j < n).
- 4. Inside the loop, there are several cases to consider:
- a. If pointer i has reached the end of nums1, add the current element in nums2 to sum g, and increment j.
- c. If the current element in nums1 (nums1[i]) is less than the current element in nums2 (nums2[j]), add nums1[i] to sum f and
 - increment i.

b. If pointer j has reached the end of nums2, add the current element in nums1 to sum f, and increment i.

- d. If the current element in nums1 is greater than the current element in nums2, add nums2[j] to sum g and increment j.
- could end in either array. 6. Return this maximum value modulo 10⁹ + 7 as per the problem statement requirements to account for a potentially large score.

5. After the loop ends (both arrays have been fully traversed), the final answer is the maximum of the two sums, f and g, since you

e. If the current elements in both arrays are equal, a common element is encountered. The max of f and g (which represents the

best score up to this point from either array) is added to the common element, then this value is assigned to both f and g since

switching paths here is allowed and should yield the maximum score. Increment both i and j after this operation.

- In terms of data structures, no additional storage is needed apart from a few variables to keep track of the indices and the sums. This solution's space complexity is O(1), only requiring constant space, and the time complexity is O(m+n), where m and n are the lengths of the two input arrays. Because each element in the arrays is examined at most once by each pointer, the algorithm is highly
- This solution is a demonstration of cleverly optimizing the process of path selection in a way that continually maximizes the potential score at each step.

nums1 = [2, 4, 5, 8, 10]nums2 = [4, 6, 8, 9]

1. We initialize two pointers i = 0 for nums1 and j = 0 for nums2. We also initialize two sums f = 0 and g = 0. 2. Since nums1[0] < nums2[0], we add nums1[i] (which is 2) to f and increment i. Now, f = 2, g = 0.

Example Walkthrough

efficient.

3. Now we compare nums1[i] (which is 4) with nums2[j] (also 4). Since they are equal, we have a common element.

itself since it's much less than the modulo value.

Initialize variables

Following the proposed solution, here's the walkthrough:

Let's take two sorted arrays to illustrate the solution approach:

- b. We add the maximum of f and g to the common value and assign it to both f and g. Thus, f = g = 4 + 2 = 6. c. Increment both i and j. Now, i = 2, j = 1.
- 4. Now, nums1[i] is 5 and nums2[j] is 6. Since 5 < 6, we add nums1[i] to f and increment i. Now, f = 11, g = 6.
- 5. We have nums1[i] as 8 and nums2[j] also 8. Another common element encountered. a. We choose the path with the higher sum, which is f (11 > 6).

6. Now nums1[i] is 10 and nums2[j] is 9. Since 9 < 10, we add nums2[j] to g and increment j. Now, g = 19 + 9 = 28.

a. We switch to the array with the higher sum, which are equal at this moment (f = g = 2), so the path doesn't change.

c. Increment both i and j. Now, i = 4, j = 3.

b. We add the max of f and g to the common value, which gives f = g = 8 + 11 = 19.

7. We add nums1[i] to f (since j has reached the end of nums2) and increment i. Now, f = 19 + 10 = 29. 8. Both pointers have reached the end of their arrays. We take the maximum of f and g, which in this case is f = 29.

def maxSum(self, nums1: List[int], nums2: List[int]) -> int:

Process both arrays until we reach the end of one of them

while index_nums1 < len_nums1 or index_nums2 < len_nums2:</pre>

sum_nums2 += nums2[index_nums2]

sum_nums1 += nums1[index_nums1]

sum_nums2 += nums2[index_nums2]

else: # Elements in both arrays are equal

sumNums1 += nums1[indexNums1++];

sumNums2 += nums2[indexNums2++];

// and move forward in both arrays

// Calculate max of both sums and apply modulo

} else if (nums1[indexNums1] > nums2[indexNums2]) {

int result = (int) (Math.max(sumNums1, sumNums2) % MODUL0);

// If current element in nums2 is smaller, add it to sumNums2

// If elements are the same, add the max of the two running sums to both sums

sumNums1 = sumNums2 = Math.max(sumNums1, sumNums2) + nums1[indexNums1];

index_nums2 += 1

index_nums2 += 1

Python Solution

if index_nums1 == len_nums1: # nums1 is exhausted, continue with nums2

elif index_nums2 == len_nums2: # nums2 is exhausted, continue with nums1

MOD = 10**9 + 7 # The modulo value for the result len_nums1, len_nums2 = len(nums1), len(nums2) # Lengths of the input arrays index_nums1 = index_nums2 = 0 # Index pointers for nums1 and nums2 sum_nums1 = sum_nums2 = 0 # Running sums for nums1 and nums2 10

So, the maximum score that can be achieved is 29, and we will return this value modulo 10^9 + 7 to get the final answer which is 29

18 index_nums1 += 1 elif nums1[index_nums1] < nums2[index_nums2]: # Current element of nums1 is smaller</pre> 19 20 sum_nums1 += nums1[index_nums1] index nums1 += 1 21 22 elif nums1[index_nums1] > nums2[index_nums2]: # Current element of nums2 is smaller

from typing import List

class Solution:

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                    # Update both sums to the maximum of the two sums plus the current element
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                    sum_nums1 = sum_nums2 = max(sum_nums1, sum_nums2) + nums1[index_nums1]
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                   # Move past this common element in both arrays
29
                    index_nums1 += 1
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                    index_nums2 += 1
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           # Return the maximum of the two sums modulo MOD
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           return max(sum_nums1, sum_nums2) % MOD
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Java Solution
   class Solution {
       public int maxSum(int[] nums1, int[] nums2) {
            final int MODULO = (int) 1e9 + 7; // Define the modulo value as a constant
           int lengthNums1 = nums1.length; // Length of the first array
            int lengthNums2 = nums2.length; // Length of the second array
            int indexNums1 = 0; // Current index in nums1
            int indexNums2 = 0; // Current index in nums2
            long sumNums1 = 0; // Running sum of segments from nums1
            long sumNums2 = 0; // Running sum of segments from nums2
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           // While there are elements left to consider in either array
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           while (indexNums1 < lengthNums1 || indexNums2 < lengthNums2) {</pre>
               if (indexNums1 == lengthNums1) {
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                   // If nums1 is exhausted, add remaining nums2 elements to sumNums2
                    sumNums2 += nums2[indexNums2++];
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                } else if (indexNums2 == lengthNums2) {
                    // If nums2 is exhausted, add remaining nums1 elements to sumNums1
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                    sumNums1 += nums1[indexNums1++];
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               } else if (nums1[indexNums1] < nums2[indexNums2]) {</pre>
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                   // If current element in nums1 is smaller, add it to sumNums1
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40 } 41

} else {

indexNums1++;

indexNums2++;

return result; // Return the result

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C++ Solution
   #include <vector>
2 #include <algorithm>
   class Solution {
   public:
       int maxSum(std::vector<int>& nums1, std::vector<int>& nums2) {
            const int MODUL0 = 1e9 + 7; // Define the modulo constant.
           int size1 = nums1.size(), size2 = nums2.size();
           int index1 = 0, index2 = 0; // Initialize pointers for the two arrays.
            long long sum1 = 0, sum2 = 0; // Initialize sums to 0 as long long to prevent overflow.
           // Iterate through both arrays simultaneously.
           while (index1 < size1 || index2 < size2) {</pre>
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               if (index1 == size1) {
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                   // If nums1 is exhausted, add remaining elements of nums2 to sum2.
                   sum2 += nums2[index2++];
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               } else if (index2 == size2) {
                   // If nums2 is exhausted, add remaining elements of nums1 to sum1.
                    sum1 += nums1[index1++];
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               } else if (nums1[index1] < nums2[index2]) {</pre>
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                   // If the current element in nums1 is less than in nums2, add it to sum1.
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                   sum1 += nums1[index1++];
                } else if (nums1[index1] > nums2[index2]) {
                   // If the current element in nums2 is less than in nums1, add it to sum2.
24
                    sum2 += nums2[index2++];
25
               } else {
26
                   // When both elements are equal, move to the next elements and add the maximum
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                   // of sum1 and sum2 to both sums.
                    sum1 = sum2 = std::max(sum1, sum2) + nums1[index1];
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                    index1++;
                   index2++;
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           // Calculate the maximum sum encountered, modulo the defined number.
           return std::max(sum1, sum2) % MODULO;
36
37
38 };
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nums1MaxSum += nums1[nums1Index++]; 24 25 } else if (nums1[nums1Index] < nums2[nums2Index]) {</pre> 26 // If the current element in nums1 is less than in nums2, 27 // add it to the max sum path of nums1. nums1MaxSum += nums1[nums1Index++]; 28

} else {

Typescript Solution

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const mod = 1e9 + 7;

let nums1MaxSum = 0;

let nums2MaxSum = 0;

let nums1Index = 0;

let nums2Index = 0;

function maxSum(nums1: number[], nums2: number[]): number {

// Initialize two pointers for traversing through the arrays.

// Iterate over the arrays until the end of both is reached.

} else if (nums1[nums1Index] > nums2[nums2Index]) {

// add it to the max sum path of nums2.

nums2MaxSum += nums2[nums2Index++];

nums1MaxSum = maxOfBoth;

nums2MaxSum = max0fBoth;

nums1Index++;

nums2Index++;

// If the current element in nums2 is less than in nums1,

// and increment both pointers as the path merges.

nums2MaxSum += nums2[nums2Index++];

} else if (nums2Index === nums2Length) {

while (nums1Index < nums1Length || nums2Index < nums2Length) {</pre>

// Store the lengths of the input arrays.

if (nums1Index === nums1Length) {

const nums1Length = nums1.length;

const nums2Length = nums2.length;

// Define the modulo value as per the problem's constraint to avoid overflow.

// Initialize two variables to keep track of the maximum sum path for each of the arrays.

// If nums1 is exhausted, continue adding the elements from nums2 to nums2's max sum.

// If nums2 is exhausted, continue adding the elements from nums1 to nums1's max sum.

// If the elements are equal, add the maximum of the two paths plus the current element,

const maxOfBoth = Math.max(nums1MaxSum, nums2MaxSum) + nums1[nums1Index];

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      // Return the maximum sum path lesser array modulo the defined mod value.
45
       return Math.max(nums1MaxSum, nums2MaxSum) % mod;
46 }
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Time and Space Complexity
The given code aims to find the maximum sum of two non-decreasing arrays where the sum includes each number exactly once, and
where an element present in both arrays can only be counted in one of the arrays at any intersection point.
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algorithm uses two pointers i and j to traverse both arrays simultaneously. In the worst case, each pointer goes through the entirety

Time Complexity

of its corresponding array, resulting in a complete traversal of both arrays. Since the traversal involves constant-time checks and updates, no element is visited more than once, and there are no nested loops, the time complexity is linear with respect to the total number of elements in both arrays. **Space Complexity**

The time complexity of the code is 0(m + n), where m is the length of nums1 and n is the length of nums2. This is because the

The space complexity of the code is 0(1). Aside from the input arrays nums1 and nums2, we only use a constant amount of extra space for the variables i, j, f, g, and mod. No additional space is allocated that is dependent on the input size, hence the constant space complexity.