Medium Array Hash Table

Problem Description

The problem deals with a set of points on a 2D plane and the goal is to determine if there is a line parallel to the y-axis that can reflect all points symmetrically. In essence, we have to find out whether we can draw a vertical line such that every point has a mirrored counterpart on the other side of the line. The set of points before and after reflecting them across this line should be identical, even if some points are repeated.

Intuition

To solve this problem, we must recognize that a reflection over a line parallel to the y-axis means that each point (x, y) will have a mirrored point (x', y) such that both points are equidistant from the line of reflection. This implies that the sum of the x-coordinates of the two points (x + x') will be equal to twice the x-coordinate of the reflection line.

reflection, if it exists, would be exactly halfway between these two values, so the sum s for the reflection condition would be min_x + max_x. Next, we store all given points in a set for constant-time lookups. Then, for every point in our input, we check if its symmetric

We approach the solution by first finding the minimal (min_x) and maximal (max_x) x-coordinates among all given points. The line of

counterpart with respect to the potential line of reflection ((s - x, y)) exists in our set. If all points satisfy this condition, the points are symmetric with respect to a line, and the function should return true. Otherwise, no such line exists and we return false.

To implement the solution, we use a set data structure to store the points for efficient querying, as well as simple variables to keep track of the minimum and maximum x-coordinates.

Solution Approach

The solution is straightforward in terms of algorithms and does not require any complex data structure manipulation or intricate

1. Initialize min_x to infinity and max_x to negative infinity. These will be used to track the minimum and maximum x-values of the given points.

- 2. Traverse all points in the input list. For each point (x, y), update min_x and max_x to keep track of the smallest and largest x-coordinates.
- Add the point (x, y) to the set point_set for efficient lookups later.

patterns. It essentially involves the following steps:

point_set for every (x, y) in the list of points.

- 3. Calculate the sum s which is the potential reflection line's x-coordinate times two ($s = min_x + max_x$). This is based on the
- principle that the line of reflection would be exactly in the middle of the leftmost and rightmost points. 4. Finally, confirm that each point (x, y) has its mirrored counterpart. This is done by checking if (s - x, y) is present in
- If all points have their mirrored counterparts in the set, return true. If there is even a single point without a mirrored counterpart, return false.

The use of a set is crucial here as it allows us to verify the existence of the mirrored pairs in constant time (0(1)), thus keeping the

- entire algorithm's time complexity to O(n), where n is the number of points.

For point (7, 1), min_x remains 1 and max_x is updated to 7.

For the last point (9, 1), min_x remains 1 and max_x is updated to 9.

point_set = set() # Create a set to store unique points.

// Using a set to store unique point representations.

pointSet.add(List.of(point[0], point[1]));

Set<List<Integer>> pointSet = new HashSet<>();

mathematical formulas involved, just the straightforward application of the definition of a reflection over a vertical line. Example Walkthrough

There are no particular algorithms used beyond basic iteration and set operations. Also, there are no complex logical patterns or

Let's consider an example with the following set of points on a 2D plane: [(1, 1), (3, 1), (7, 1), (9, 1)]. Our goal is to determine if there exists a line parallel to the y-axis that reflects all these points symmetrically.

points.

2. Now we traverse our points list:

 \circ For point (1, 1), we update min_x to 1 (as 1 < infinity) and max_x to 1 (as 1 > -infinity). For point (3, 1), min_x remains 1 and max_x is updated to 3.

1. First, we initialize min_x to infinity and max_x to negative infinity to keep track of the minimum and maximum x-coordinates of the

 Throughout the iteration, we also add each point to a set point_set for efficient lookups. 3. After the first traversal, we have $min_x = 1$ and $max_x = 9$. The sum s which represents twice the possible line of reflection's x-

coordinate is $s = min_x + max_x = 1 + 9 = 10$.

4. For the symmetry check, we traverse the list again:

 \circ Point (1, 1) has a counterpart (9, 1) because s - x = 10 - 1 = 9, and (9, 1) is in point_set.

that reflects all the points symmetrically. Therefore, the function should return true for this example.

Iterate over all points to find the min and max X values and add points to the set.

All points have a mirrored counterpart with respect to the line whose x-coordinate is s/2, which in this case is 5. Since each point (x, y) has a matching point (s - x, y) in the set, we can conclude that it's possible to draw a vertical line parallel to the y-axis at x = 5

Since points (7, 1) and (9, 1) have already been paired with their counterparts, the conditions are satisfied for all points.

 \circ Point (3, 1) should be mirrored with point (7, 1) because s - x = 10 - 3 = 7, and (7, 1) is indeed in point_set.

Python Solution 1 class Solution: def isReflected(self, points: List[List[int]]) -> bool: # Initialize minimum and maximum X to positive and negative infinity respectively. min_x, max_x = float('inf'), float('-inf')

for x, y in points: $min_x = min(min_x, x)$ 10 $max_x = max(max_x, x)$

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point_set.add((x, y))
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           # Calculate the sum of min and max X, which should be equal to twice the X value of the reflection line.
           reflection_sum = min_x + max_x
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15
16
           # Check if for each point (x, y), the reflected point across the Y-axis
           # given by (reflection_sum -x, y) exists in the point set.
17
           # The reflection across the Y-axis is defined by the line X = (min_x + max_x) / 2.
18
           return all((reflection_sum - x, y) in point_set for x, y in points)
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Java Solution
   class Solution {
       public boolean isReflected(int[][] points) {
           // Initialize the max and min X coordinates to extreme values.
           final int MAX_VALUE = Integer.MAX_VALUE;
           int minX = MAX_VALUE;
           int maxX = Integer.MIN_VALUE;
```

// Iterate over all points to find the minX and maxX values, // and add each point to the set. 12 13 for (int[] point : points) { minX = Math.min(minX, point[0]); 14 maxX = Math.max(maxX, point[0]); 15

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           // Calculate the sum of minX and maxX which is twice the X coordinate
20
           // of the line of reflection.
           int sum = minX + maxX;
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           // Check if each point has its reflected counterpart in the set.
           for (int[] point : points) {
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25
               // If the reflected point is not found in the set, return false.
26
               if (!pointSet.contains(List.of(sum - point[0], point[1]))) {
27
                   return false;
28
29
30
31
           // If all points have their reflected counterpart, return true.
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           return true;
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C++ Solution
  1 #include <vector>
  2 #include <set>
  3 #include <algorithm>
  4 using std::vector;
  5 using std::set;
  6 using std::min;
  7 using std::max;
    using std::pair;
 10 class Solution {
    public:
         // Function to determine if a set of points reflects across a single vertical axis.
 12
         bool isReflected(vector<vector<int>>& points) {
 13
 14
             // Constants to represent infinity and negative infinity.
 15
```

26 minX = min(minX, point[0]); // Update minX if current point's X is smaller. 27 28 29

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const int $INF = 1 \ll 30$;

int minX = INF, maxX = -INF;

set<pair<int, int>> pointSet;

for (auto& point : points) {

// Variables to store the minimum and maximum X-coordinates.

// A set to store unique points (pair of X and Y coordinates).

// Loop through all points to populate pointSet and find the minX and maxX.

```
maxX = max(maxX, point[0]); // Update maxX if current point's X is larger.
                 pointSet.insert({point[0], point[1]}); // Insert the point into the set.
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 31
             // Sum of minX and maxX is the total which, when halved, gives the X-coordinate of the reflection axis.
 32
             int sumOfMinAndMaxX = minX + maxX;
 33
 34
             // Iterate through all points to check if the reflected point exists.
 35
             for (auto& point : points) {
 36
                 // Calculate the reflection of the current point across the reflection axis.
 37
                 int reflectedX = sumOfMinAndMaxX - point[0];
 38
 39
                 // Check if the reflected point is not in the set. If it's not, the point array is not reflected.
                 if (!pointSet.count({reflectedX, point[1]})) {
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                     return false;
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             // Return true if all points have their reflected counterparts.
 46
             return true;
 47
 48
    };
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Typescript Solution
  1 // Importing arrays and sets from ECMAScript 6 (ES6) standard.
  2 import { Set } from "typescript-collections";
    // Function to determine if a set of points reflects across a single vertical axis.
    function isReflected(points: number[][]): boolean {
         // Constants to represent infinity and negative infinity.
         const INF: number = 1 << 30;</pre>
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  9
 10
         // Variables to store the minimum and maximum X-coordinates.
 11
         let minX: number = INF;
         let maxX: number = -INF;
 12
 13
         // A set to store unique points (tuple of X and Y coordinates).
 14
 15
         let pointSet: Set<string> = new Set();
 16
 17
         // Loop through all points to populate pointSet and find the minX and maxX.
         for (const point of points) {
 18
             minX = Math.min(minX, point[0]); // Update minX if current point's X is smaller.
 19
 20
             maxX = Math.max(maxX, point[0]); // Update maxX if current point's X is larger.
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 22
             // Insert the point into the set as a string to ensure uniqueness.
 23
             pointSet.add(JSON.stringify({x: point[0], y: point[1]}));
 24
 25
 26
         // Sum of minX and maxX is the total, which, when halved, gives the X-coordinate of the reflection axis.
```

36 return false; 37 38 39 40 // Return true if all points have their reflected counterparts.

return true;

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Time Complexity

The time complexity of the given code can be analyzed as follows:

const sumOfMinAndMaxX: number = minX + maxX;

for (const point of points) {

Time and Space Complexity

// Iterate through all points to check if the reflected point exists.

const reflectedX: number = sumOfMinAndMaxX - point[0];

// Calculate the reflection of the current point across the reflection axis.

if (!pointSet.contains(JSON.stringify({x: reflectedX, y: point[1]}))) {

// Check if the reflected point is not in the set. If it's not, the point array is not reflected.

point_set. This requires 0(n) time. • Then we check if each point has a reflected point in the point_set using the formula (s - x, y) where s is the sum of min_x and

max_x. This step also iterates over all n points and each lookup in a set is expected to be 0(1) on average, leading to another

We iterate over all n points once to find the minimum (min_x) and maximum (max_x) x-coordinates, and to add each point to the

O(n) time operation. Therefore, the overall time complexity is O(n) + O(n) = O(n) where n is the number of input points.

Space Complexity

The space complexity of the code can be considered as follows:

- We create a set, point_set, which in the worst case, will contain all input points if all points are unique. This leads to a space complexity of O(n).
- No additional significant space is used in the algorithm.

Hence, the overall space complexity of the algorithm is O(n) where n is the number of input points.