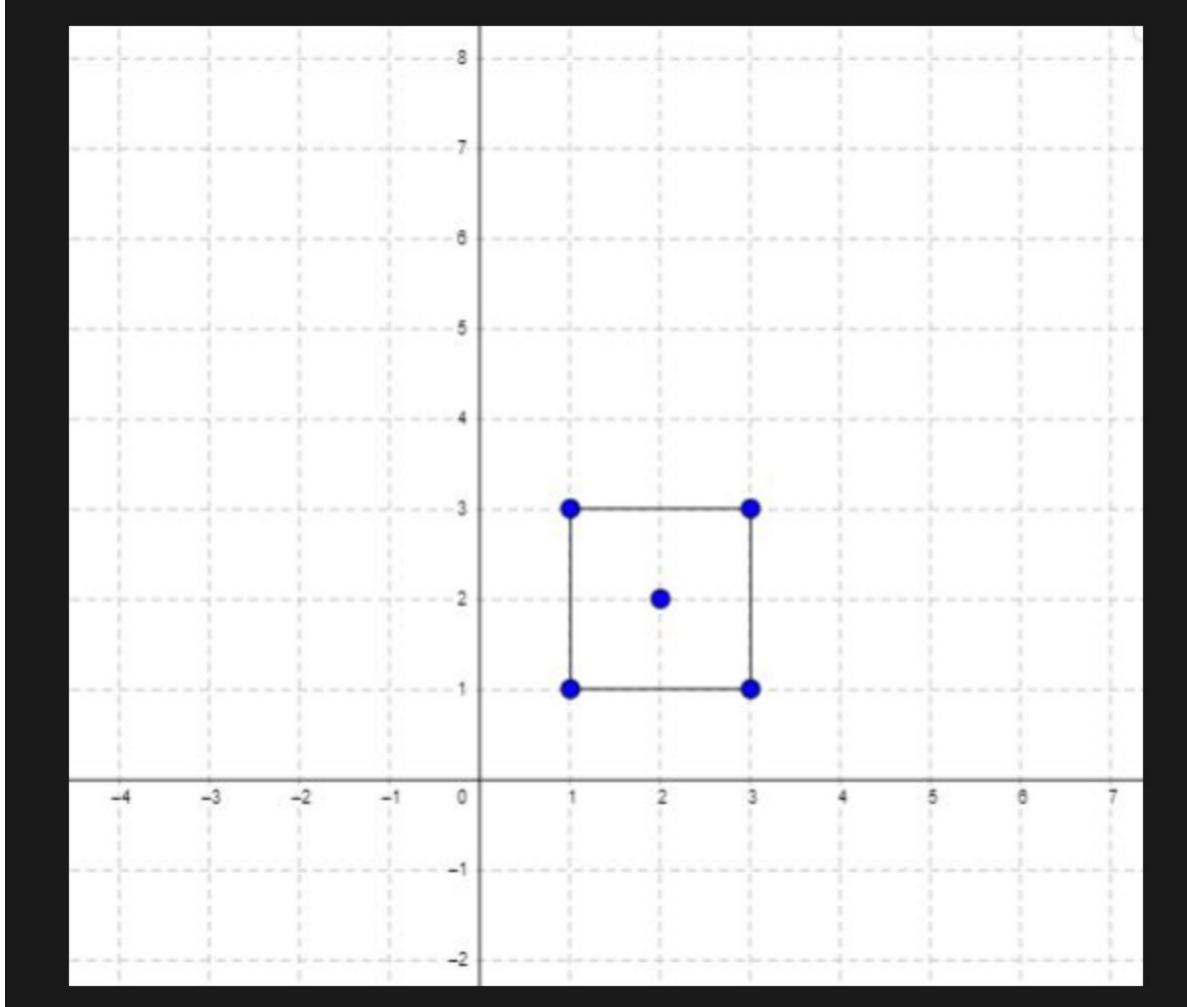
## 939. Minimum Area Rectangle

You are given an array of points in the X-Y plane points where points [i] =  $[x_i, y_i]$ .

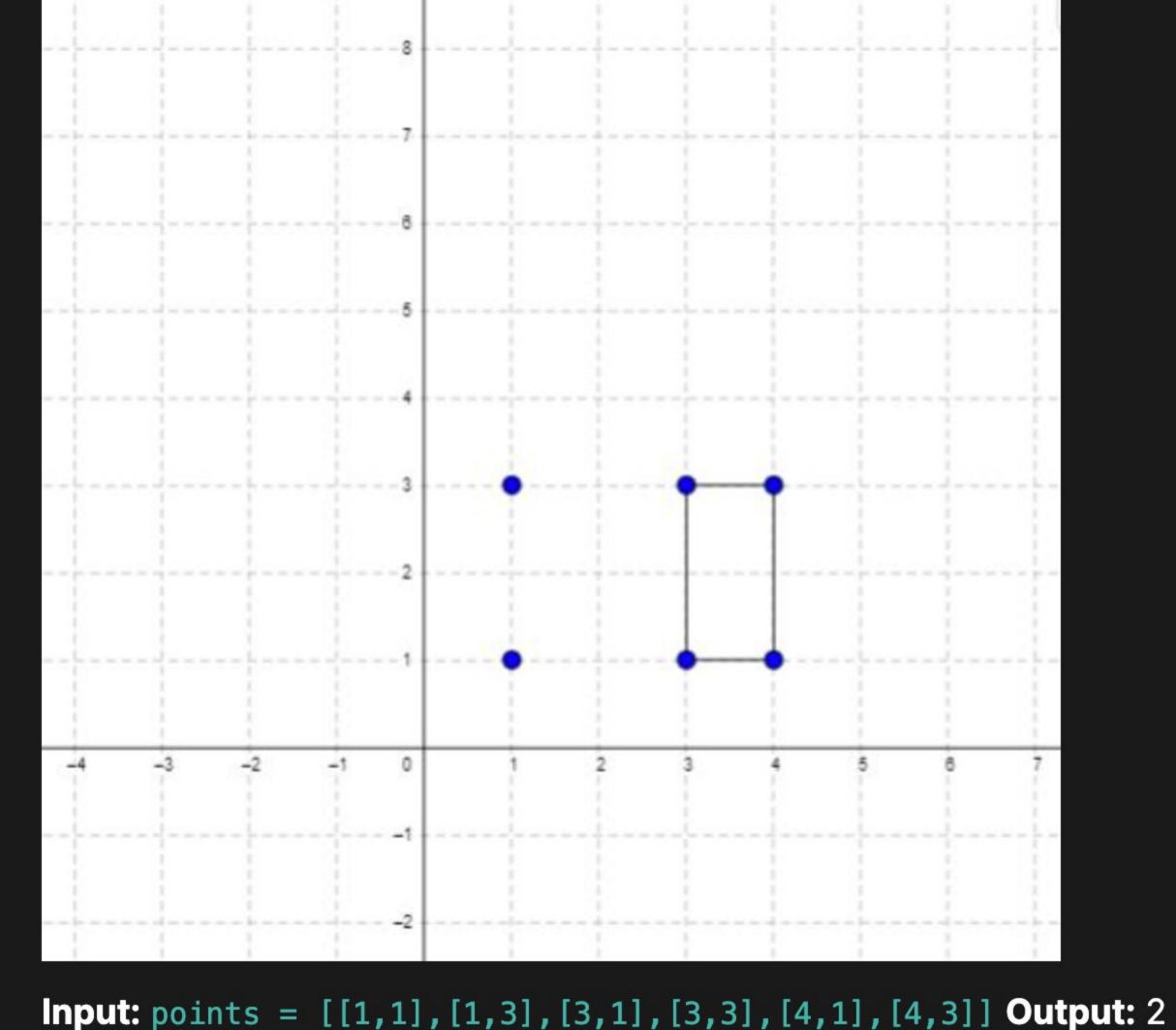
Return the minimum area of a rectangle formed from these points, with sides parallel to the X and Y axes. If there is not any such rectangle, return 0.

### Example 1:



Example 2:

Input: points = [[1,1],[1,3],[3,1],[3,3],[2,2]] Output: 4



Constraints:  $1 \leq {\tt points.length} \leq 500 \ {\tt points[i].length} == 2 \ 0 \leq x_i, y_i \leq 4*10^4 \ {\tt All the given points are unique}.$ 

### T > bothes.

Solution

### Since we need to form a rectangle from 4 different points, we can check all combinations of 4 points to see if it forms a rectangle.

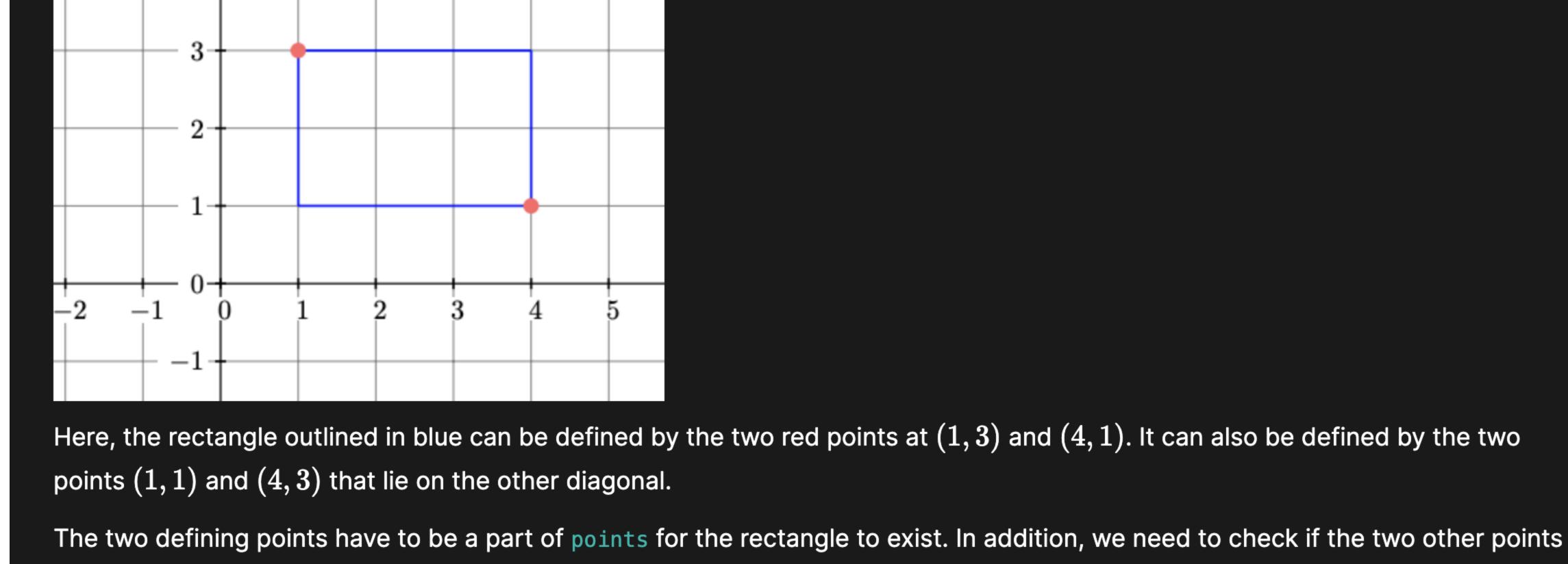
rectangle has positive area. Let N denote the size of points. This algorithm runs in  $\mathcal{O}(N^4)$ .

Then, we return the minimum area from a rectangle formed with these points. One key point is that we need to make sure the

Let's try to optimize our algorithm to find all possible rectangles faster. One observation we can make is that a rectangle can be

defined by two points that lie on one of the two diagonals.

Example



combinations, this algorithm runs in  $\mathcal{O}(N^2)$ .

int minAreaRect(vector<vector<int>>& points) {

for (int index1 = 0; index1 < points.size();</pre>

unordered\_map<int, unordered\_map<int, bool>> hashMap;

in the rectangle exist in points. Specifically, let's denote the two defining points as  $(x_1, y_1)$  and  $(x_2, y_2)$ . We'll need to check if  $(x_1, y_2)$  and  $(x_2, y_1)$  exist in points. This is where we can use a <u>hashmap</u> to do this operation in  $\mathcal{O}(1)$ . We'll also need to make sure the rectangle has positive area (i.e.  $x_1 \neq x_2, y_1 \neq y_2$ ).

Now, instead of trying all combinations of 4 different points from points, we'll try all combinations of 2 different points from points to be the two defining points of the rectangle.

Time Complexity

In our algorithm, we check all combinations of 2 different points in points. Since each check runs in  $\mathcal{O}(1)$  and there are  $\mathcal{O}(N^2)$ 

# Space Complexity

class Solution {

public:

Time Complexity:  $\mathcal{O}(N^2)$ .

Space Complexity:  $\mathcal{O}(N)$ .

Since we store  $\mathcal{O}(N)$  integers in our <code>hashmap</code>, our space complexity is  $\mathcal{O}(N)$ .

```
for (vector<int> point : points) { // add all points into hashmap
    hashMap[point[0]][point[1]] = true;
}
```

return ans;

solution.

int ans = INT MAX;

```
index1++) { // iterate through first defining point
            int x1 = points[index1][0];
            int y1 = points[index1][1];
            for (int index2 = index1 + 1; index2 < points.size();</pre>
                 index2++) { // iterate through second defining point
                int x2 = points[index2][0];
                int y2 = points[index2][1];
                if (x1 == x2 ||
                    y1 == y2) { // rectangle doesn't have positive area
                    continue;
                if (hashMap[x1].count(y2) &&
                    hashMap[x2].count(
                        y1)) { // check if other points in rectangle exist
                    ans = min(ans, abs(x1 - x2) * abs(y1 - y2));
        if (ans == INT_MAX) { // no solution
            return 0;
        return ans;
class Solution {
   public int minAreaRect(int[][] points) {
        HashMap<Integer, HashMap<Integer, Boolean>> hashMap = new HashMap<>();
        for (int[] point : points) { // add all points into hashmap
            if (!hashMap.containsKey(point[0])) {
                hashMap.put(point[0], new HashMap<>());
            hashMap.get(point[0]).put(point[1], true);
        int ans = Integer.MAX_VALUE;
        for (int index1 = 0; index1 < points.length;</pre>
             index1++) { // iterate through first defining point
            int x1 = points[index1][0];
            int y1 = points[index1][1];
            for (int index2 = index1 + 1; index2 < points.length;</pre>
                 index2++) { // iterate through second defining point
                int x2 = points[index2][0];
                int y2 = points[index2][1];
                if (x1 == x2 || y1 == y2) { // rectangle doesn't have positive area
                    continue;
                if (hashMap.get(x1).containsKey(y2)
                    && hashMap.get(x2).containsKey(y1)) { // check if other points in rectangle exist
                    ans = Math.min(ans, Math.abs(x1 - x2) * Math.abs(y1 - y2));
        if (ans == Integer.MAX_VALUE) { // no solution
            return 0;
```

}
Small note: You can use a set in python which acts as a hashset and essentially serves the same purpose as a hashmap for this