2771. Longest Non-decreasing Subarray From Two Arrays **Dynamic Programming** Medium Array

### **Problem Description** In this problem, you have two integer arrays nums1 and nums2, both containing n elements, indexed from 0. Your goal is to create a

fill nums3 such that it contains the longest non-decreasing subarray possible; basically, you want nums3 to have the longest sequence where elements from left to right are not in descending order. The desired output is the length of this longest non-decreasing subarray in nums3. A non-decreasing subarray is a contiguous sequence of elements that go from left to right without decreasing in value. In other words, every element is greater than or equal to the element that comes before it.

third array nums3, also with n elements, where each element at index i is either the element from nums1[i] or nums2[i]. You want to

**Leetcode Link** 

Intuition

# subproblems and using these solutions to construct an answer for the larger problem.

consider. However, we only need to keep track of the longest subarray lengths up to the current position for both potential choices. Here we define two states: f to represent the length of the longest non-decreasing subarray that ends with an element from nums1, and g to represent the length of the longest non-decreasing subarray that ends with an element from nums2.

The intuition behind the solution involves dynamic programming, a method that solves problems by combining solutions to

To arrive at the solution, we start by initializing f and g to 1, as the longest subarray at the start can only be of length 1. As we iterate through each index starting from 1, we determine the possible lengths of f and g by checking if the current elements in nums1 and nums2 can extend the non-decreasing subarrays ending at the previous index. For each element at index i, if nums1[i] is greater than or equal to the previous elements (nums1[i-1] or nums2[i-1]), we can extend

the non-decreasing subarray ending with nums1[i-1] or nums2[i-1]. The same applies for nums2[i]. At each step, we update f and g

Since for each index i, you can choose either nums1[i] or nums2[i] for the nums3 array, there can be many potential combinations to

to the longer of the current value of f or g and the length of the new non-decreasing subarray, which can be an extension of f or g from the previous step. Finally, the answer is the maximum value of f and g after traversing all elements. This dynamic approach ensures that we do not need to evaluate all possible combinations of elements from nums1 and nums2;

instead, we can efficiently calculate the length of the longest non-decreasing subarray by considering each position's optimal choice

The implementation of the solution makes use of a dynamic programming strategy. It involves tracking the potential longest nondecreasing subarray lengths dynamically as we iterate through the arrays. Here's a breakdown of how the algorithm works and the concepts it uses: 1. Initialization of States: We start with two variables, f and g, both set to 1 because, at the very beginning, the longest non-

2. Iteration through Arrays: We loop through the arrays starting from index 1, as the 0th index is already considered in our initial

3. State Transition: For each index i, we compute two temporary variables ff and gg which represent the potential new values of f

decreasing subarray that can be formed will just include the first element from either nums1 or nums2. The variable ans is also set

# state.

Example Walkthrough

decreasing subarray.

first elements.

based on the previous computations.

to 1, to track the length of the longest subarray found so far.

Let's walk through a small example to illustrate the solution approach.

Now we proceed to iterate through each index, starting from 1.

 $\max(ff, f + 1) => ff = \max(0, 1 + 1) => ff = 2.$ 

 $\max(ff, g + 1) \Rightarrow ff = \max(2, 1 + 1) \Rightarrow ff = 2.$ 

 $\max(gg, g + 1) => gg = \max(0, 1 + 1) => gg = 2.$ 

• We now perform the state update, f = ff and g = gg, setting both f and g to 2.

• nums1[2] (2) is smaller than nums1[i - 1] (4), so ff does not update based on f.

**Solution Approach** 

and g based on whether the current elements at index i can extend the longest non-decreasing subarray up to index i - 1. This involves four scenarios for updating ff and gg: ∘ If nums1[i] is not smaller than nums1[i - 1], the subarray ending with nums1[i - 1] can be extended, so we update ff to  $\max(ff, f + 1).$ 

max(ff, g + 1).∘ If nums2[i] is not smaller than nums1[i - 1], the subarray ending with nums1[i - 1] can be extended, so we update gg to max(gg, f + 1).∘ If nums2[i] is not smaller than nums2[i - 1], the subarray ending with nums2[i - 1] can be extended, so we update gg to

∘ If nums1[i] is not smaller than nums2[i - 1], the subarray ending with nums2[i - 1] can be extended, so we update ff to

max(gg, g + 1).4. State Update: After calculating ff and gg, we set f and g to these new values, as they represent the updated longest nondecreasing subarray lengths ending at index i for nums1 and nums2 respectively.

5. Answer Calculation: With each iteration, the ans variable is updated to reflect the maximum value among ans, f, and g. This

The code uses a simple for loop for iteration and max function calls for comparison to execute this algorithm effectively. By only

ensures that after traversing the entire array, ans holds the length of the longest non-decreasing subarray that can be formed.

maintaining the necessary states, we optimize space complexity while ensuring that the program runs in linear time relative to the size of the given arrays.

Assume our input arrays are nums1 = [3, 4, 2, 6] and nums2 = [1, 2, 3, 4], and we wish to construct nums3 with the longest non-

Initially, we set f = 1, g = 1, and ans = 1, since the longest non-decreasing subarray at the beginning can only include one of the

For i = 1: • We compute temporary variables ff and gg; at the start of every iteration, they are set to zero.

• Since nums1[1] (4) is not smaller than nums1[i - 1] (3), we can extend the subarray ending with nums1[i - 1]. Thus, ff =

• nums2[1] (2) is not smaller than nums1[i - 1] (3), so we cannot extend from nums1[i - 1] this time; gg remains the same.

• Since nums2[1] (2) is not smaller than nums2[i - 1] (1), we can extend the subarray ending with nums2[i - 1]. Thus, gg =

• Since nums1[1] (4) is also not smaller than nums2[i - 1] (1), we can extend the subarray ending with nums2[i - 1]. Thus, ff =

Now, ans is updated to be the max of ans, f, and g, which is max(1, 2, 2), so ans becomes 2. Repeating this process for the rest of the indices:

# For i = 2:

For i = 3:

gg = 4.

Python Solution

class Solution:

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from typing import List

n = len(nums1)

 $max_length = 1$ 

for i in range(1, n):

State update puts f = 4 and g = 4.

# Get the length of the input lists

if nums1[i] >= nums1[i - 1]:

if nums1[i] >= nums2[i - 1]:

if nums2[i] >= nums2[i - 1]:

# Update the global max\_length if necessary

max\_length\_end\_nums1 = max\_length\_end\_nums2 = 1

- nums2[2] (3) is not smaller than nums1[i 1] (4), so gg does not update based on f. • nums2[2] (3) is larger than nums2[i - 1] (2), so  $gg = max(gg, g + 1) \Rightarrow gg = max(0, 2 + 1) \Rightarrow gg = 3$ .
- Reset f and g to their new values ff and gg, respectively, both are now 3. • ans = max(ans, f, g) => ans = <math>max(2, 3, 3) => ans = 3.

• nums1[3] (6) is larger than both nums1[i - 1] (2) and nums2[i - 1] (3), so ff becomes max(0, f + 1) and max(0, g + 1),

In the end, the longest non-decreasing subarray that can be created (nums3) is of length 4, which is our answer. Thus, nums3 can be

resulting in ff = 4. • nums2[3] (4) is larger than nums1[i - 1] (2) but not nums2[i - 1] (3), so gg only updates from f, giving gg = max(0, f + 1) =>

# Initialize the lengths of non-decreasing sequences ending with the last element of nums1 and nums2

# Initialize the answer with 1, since the smallest non-decreasing sequence has at least one element

new\_max\_length\_end\_nums1 = max(new\_max\_length\_end\_nums1, max\_length\_end\_nums1 + 1)

new\_max\_length\_end\_nums1 = max(new\_max\_length\_end\_nums1, max\_length\_end\_nums2 + 1)

new\_max\_length\_end\_nums2 = max(new\_max\_length\_end\_nums2, max\_length\_end\_nums2 + 1)

max\_length = max(max\_length, max\_length\_end\_nums1, max\_length\_end\_nums2)

\* Computes the maximum length of a non-decreasing sequence from two arrays.

\* The non-decreasing sequence can switch between arrays at any point.

# Update the lengths of non-decreasing sequences ending with the last element of nums1 and nums2

max\_length\_end\_nums1, max\_length\_end\_nums2 = new\_max\_length\_end\_nums1, new\_max\_length\_end\_nums2

• But nums1[2] (2) is not smaller than nums2[i - 1] (2), so ff = max(ff, g + 1) => ff = max(0, 2 + 1) => ff = 3.

[3, 4, 3, 4] or [3, 4, 2, 4], both of which have the longest non-decreasing subarray of length 4.

def maxNonDecreasingLength(self, nums1: List[int], nums2: List[int]) -> int:

# Iterate through the lists starting from the second element

# Initialize new max lengths for the current iteration

new\_max\_length\_end\_nums1 = new\_max\_length\_end\_nums2 = 1

• ans updates to max(ans, f, g)  $\Rightarrow$  ans  $\Rightarrow$  max(3, 4, 4)  $\Rightarrow$  ans  $\Rightarrow$  4.

26 # Update the new\_max\_length\_end\_nums2 if the current nums2 element is not decreasing compared to the previous nums1 eleme 27 if nums2[i] >= nums1[i - 1]: 28 29 new\_max\_length\_end\_nums2 = max(new\_max\_length\_end\_nums2, max\_length\_end\_nums1 + 1)

# Update the new\_max\_length\_end\_nums1 if the current nums1 element is not decreasing compared to the previous one

# Update the new\_max\_length\_end\_nums1 if the current nums1 element is not decreasing compared to the previous nums2 eleme

# Update the new\_max\_length\_end\_nums2 if the current nums2 element is not decreasing compared to the previous nums2 eleme

### 41 # Return the length of the maximum non-decreasing sequence that can be made return max\_length 42 43

Java Solution

class Solution {

/\*\*

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        * @param nums1 The first input array.
        * @param nums2 The second input array.
        * @return The maximum length of a non-decreasing sequence.
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       public int maxNonDecreasingLength(int[] nums1, int[] nums2) {
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            int n = nums1.length; // Length of the input arrays.
12
            int maxLengthNums1 = 1; // Tracks max non-dec length ending with an element from nums1.
13
            int maxLengthNums2 = 1; // Tracks max non-dec length ending with an element from nums2.
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            int ans = 1; // Stores the overall maximum non-decreasing length.
16
           // Loop through both arrays starting from the second element.
17
           for (int i = 1; i < n; ++i) {
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19
                int tempMaxLengthNums1 = 1; // Temp variable for non-dec length ending with nums1[i].
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                int tempMaxLengthNums2 = 1; // Temp variable for non-dec length ending with nums2[i].
               // If the current element in nums1 is not smaller than the previous one in nums1,
               // update the temporary maximum for nums1.
24
               if (nums1[i] >= nums1[i - 1]) {
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                    tempMaxLengthNums1 = Math.max(tempMaxLengthNums1, maxLengthNums1 + 1);
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28
               // If the current element in nums1 is not smaller than the previous one in nums2,
               // update the temporary maximum for nums1.
               if (nums1[i] >= nums2[i - 1]) {
30
                    tempMaxLengthNums1 = Math.max(tempMaxLengthNums1, maxLengthNums2 + 1);
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34
               // If the current element in nums2 is not smaller than the previous one in nums1,
35
               // update the temporary maximum for nums2.
               if (nums2[i] >= nums1[i - 1]) {
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37
                    tempMaxLengthNums2 = Math.max(tempMaxLengthNums2, maxLengthNums1 + 1);
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39
               // If the current element in nums2 is not smaller than the previous one in nums2,
40
               // update the temporary maximum for nums2.
               if (nums2[i] >= nums2[i - 1]) {
43
                    tempMaxLengthNums2 = Math.max(tempMaxLengthNums2, maxLengthNums2 + 1);
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45
               // Update the lengths for the current element.
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                maxLengthNums1 = tempMaxLengthNums1;
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                maxLengthNums2 = tempMaxLengthNums2;
49
               // Calculate the maximum length considering both nums1 and nums2.
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51
                ans = Math.max(ans, Math.max(maxLengthNums1, maxLengthNums2));
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53
           // Return the overall maximum non-decreasing length found.
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55
            return ans;
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57 }
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C++ Solution
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// Method to find the length of the longest non-decreasing subsequence that can be obtained

// Initialize lengths for non-decreasing subsequences ending with nums1[i] and nums2[i]

// Loop through the array to compute the maximum length of non-decreasing subsequence

// If the current element of nums1 is not smaller than the previous element of nums1,

// If the current element of nums1 is not smaller than the previous element of nums2,

// If the current element of nums2 is not smaller than the previous element of nums1,

// Update the maxSequenceLength considering the lengths of both nums1 and nums2

maxSequenceLength = max(maxSequenceLength, max(lengthNums1, lengthNums2));

// update the new length for nums1. This indicates switching from nums2 to nums1.

// Temporary variables to hold possible new lengths for the current index

newLengthNums1 = max(newLengthNums1, lengthNums1 + 1);

newLengthNums1 = max(newLengthNums1, lengthNums2 + 1);

newLengthNums2 = max(newLengthNums2, lengthNums1 + 1);

newLengthNums2 = max(newLengthNums2, lengthNums2 + 1);

// Update the lengths with the new computed values

// by choosing elements either from nums1 or nums2 at each step, under the constraint

int maxNonDecreasingLength(vector<int>& nums1, vector<int>& nums2) {

int n = nums1.size(); // Get the size of the input vectors

// Initialize the answer with a subsequence of length 1

int newLengthNums1 = 1, newLengthNums2 = 1;

// update the new length for nums1.

if (nums1[i] >= nums1[i - 1]) {

if (nums1[i] >= nums2[i - 1]) {

// update the new length for nums2.

if (nums2[i] >= nums1[i - 1]) {

lengthNums1 = newLengthNums1;

lengthNums2 = newLengthNums2;

// that we can't switch from nums2 back to nums1.

int lengthNums1 = 1, lengthNums2 = 1;

int maxSequenceLength = 1;

for (int i = 1; i < n; ++i) {

#### // If the current element of nums2 is not smaller than the previous element of nums2, 38 39 // update the new length for nums2. if (nums2[i] >= nums2[i - 1]) { 40 41 43

1 class Solution {

public:

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48 }

complexity.

return maxLength;

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 52
             // Return the computed maximum length of the non-decreasing subsequence
 53
             return maxSequenceLength;
 54
 55 };
 56
Typescript Solution
   /**
    * Calculates the maximum length of a non-decreasing sequence
    * that can be formed by elements taken from either nums1 or nums2
    * at each position while maintaining the order.
    * @param nums1 - The first array of numbers.
    * @param nums2 - The second array of numbers.
    * @returns The maximum length of a non-decreasing sequence from nums1 or nums2.
    */
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   function maxNonDecreasingLength(nums1: number[], nums2: number[]): number {
       const n: number = nums1.length;
10
       // Initialize lengths of non-decreasing subsequences for nums1 and nums2
11
       let nums1Length: number = 1;
12
13
       let nums2Length: number = 1;
       // Initialize the global maximum length
14
       let maxLength: number = 1;
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17
       // Iterate through the arrays to determine the non-decreasing subsequences
       for (let i = 1; i < n; ++i) {
18
19
           // Temporary variables to store the subsequence lengths at the current iteration
           let nextNums1Length: number = 1;
20
           let nextNums2Length: number = 1;
22
23
           // Check and update the non-decreasing subsequence length for nums1
           if (nums1[i] >= nums1[i - 1])
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25
               nextNums1Length = Math.max(nextNums1Length, nums1Length + 1);
26
           if (nums1[i] >= nums2[i - 1]) {
27
28
               nextNums1Length = Math.max(nextNums1Length, nums2Length + 1);
29
30
           // Check and update the non-decreasing subsequence length for nums2
31
           if (nums2[i] >= nums1[i - 1]) {
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33
               nextNums2Length = Math.max(nextNums2Length, nums1Length + 1);
34
35
           if (nums2[i] >= nums2[i - 1]) {
               nextNums2Length = Math.max(nextNums2Length, nums2Length + 1);
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38
           // Update the current lengths of the subsequences for nums1 and nums2
39
           nums1Length = nextNums1Length;
40
           nums2Length = nextNums2Length;
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43
           // Update the global maximum length
           maxLength = Math.max(maxLength, nums1Length, nums2Length);
44
```

# Time and Space Complexity

The time complexity of this code is O(n), where n is the length of the input arrays nums1 and nums2. The code consists of a single loop that iterates from 1 to n-1, performing a constant amount of work for each element with no nested loops, resulting in a linear time

The space complexity of the code is 0(1), as it uses a fixed number of integer variables (f, g, ff, gg, ans, and n). No additional space that grows with the input size is utilized, resulting in constant space complexity.