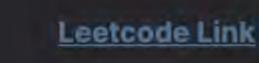
1013. Partition Array Into Three Parts With Equal Sum



### Problem Description The problem asks us to determine whether it's possible to partition a given array of integers arr into three contiguous, non-empty

Greedy

Easy

Array

parts such that the sum of the numbers in each part is equal. This is akin to cutting the array at two points to create three subarrays, where each subarray sums up to the same value. The constraints are quite simple: we need to find two indices i and j, with i + 1 < j, that satisfy the partitioning condition.

# To tackle this problem, we need to consider that if we can partition the array into three parts with equal sums, the sum of the whole

Intuition

False, because no such partitioning will be possible. If, on the other hand, s is divisible by 3, we then look for the two cut points by trying to find a subarray from the start and from the end that each sum up to s // 3 (which represents one-third of the array's total sum).

array must be divisible by 3. That's our starting point. If the entire sum s does not satisfy this condition, we can immediately return

We iterate from the start of the array, accumulating a sum a until a equals 5 // 3. This represents the end of the first part of the array. We do a similar process from the end of the array, accumulating another sum b until b equals 5 // 3. This loop runs in reverse

and represents the start of the third part of the array. If we find such indices 1 and j where a and b each equal s // 3, and 1 is strictly less than j - 1 (which ensures that the middle part is non-empty), we can conclude that it is indeed possible to partition the array into three parts with equal sums, and return True. Otherwise, the function returns False. Solution Approach

1. Initially, the algorithm calculates the sum s of all elements in the array. Since we aim to partition the array into three parts with

# equal sum, we first check if the total sum is divisible by 3. If not, we return False.

loop.

2. To find the partitioning of the array, we maintain two pointers i and j representing the boundaries of the first and last section of the partitioned array, respectively. We also maintain two accumulator variables a and b for the sums of the respective sections.

To implement the solution, the algorithm takes the following steps, leveraging simple iteration and summation:

- 3. We start a while loop that runs as long as i has not reached the end of the array. Within this loop, we increment a with the current element arr [1] and check if a has reached s // 3. If it has, we break the loop, as we have found the sum for the first
- part. 4. Similarly, we start a while loop that runs in reverse as long as j has not reached the start of the array (vj checks for this since vj

will be -1 when j is 0). We increment b with the current element arr[j] and check if b has reached s // 3. If it has, we break the

5. After finding the two potential cut points i and j, we check if i < j - 1. This ensures that there is at least one element between the two parts that we have found, fulfilling the non-empty middle section requirement. If this condition is true, we return True, indicating that the array can be partitioned into three parts with equal sums.

The algorithm mainly uses two pointers with a linear pass from both ends of the array, making the time complexity O(n), where n is

the number of elements in the array. The space complexity is O(1) since it only uses a fixed number of extra variables.

Example Walkthrough Let's say we have the following array of integers:

Now, let's walk through the solution approach step by step with this example:

1. First, we calculate the sum s of all elements in the array arr. We get s = 1 + 3 + 4 + 2 + 2 = 12. Since 12 is divisible by 3, we

2. We then initialize two pointers i with the value 0 and j with the value len(arr) - 1. Also, we initialize two accumulator variables

### can proceed. If the sum were not divisible by 3, we would return False as it would be impossible to partition the array into three parts with an equal sum.

3.

[4], and [2, 2].

total\_sum = sum(arr)

if total\_sum % 3 != 0:

return False

break

while (start < arr.length) {</pre>

endSum += arr[end];

break;

++start;

while (end >= 0) {

--end;

break;

startSum += arr[start];

if (startSum == totalSum / 3) {

if (endSum == totalSum / 3) {

indeed possible.

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1 arr = [1, 3, 4, 2, 2]

a and b to 0, which we will use to store the sums of the parts as we loop through arr. 3. The target sum for each part is s // 3, which is 12 // 3 = 4. We start looping through the array from the start, adding each

def can\_three\_parts\_equal\_sum(self, arr: List[int]) -> bool:

# Calculate the total sum of all elements in the array

# Initialize pointers for the left and right partitions

left\_index, right\_index = 0, len(arr) - 1

left\_sum += arr[left\_index]

if left\_sum == total\_sum // 3:

- element to a until a equals 4. Adding the first element 1, a becomes 1. Adding the next element 3, a becomes 4. We have found the end of the first part at i = 1. 4. Similarly, we loop through the array from the end, decrementing j and adding each element to b. Adding the last element 2, b
- 5. We then check if i < j 1. In this case, i = 1, and j = 3, so 1 < 3 1 which is 1 < 2. This inequality holds, meaning there is at least one element for the middle part, and we can confirm that the array can be split into three parts with equal sums [1, 3],

Since all checks pass, the function would return True for this array, indicating that partitioning into three parts with equal sums is

becomes 2. Decrementing j, we add the next last element 2, b becomes 4. We have found the beginning of the third part at j =

Python Solution from typing import List class Solution:

# If the total sum is not divisible by 3, it's not possible to partition the array into three parts with equal sums

left\_sum, right\_sum = 0, 0 13 14 15 # Increase the left partition until we find a partition with a sum that's a third of the total sum while left\_index < len(arr):</pre> 16

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                left_index += 1
21
22
           # Similarly, decrease the right partition to find a partition with a sum that's a third of the total sum
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23
           while right_index >= 0:
24
                right_sum += arr[right_index]
               if right_sum == total_sum // 3:
25
26
                    break
27
                right_index -= 1
28
29
           # Check if there is at least one element between the two partitions
           # i + 1 < j ensures there's room for a middle partition
30
           return left_index < right_index - 1
31
32
33 # Example usage:
34 # solution = Solution()
35 # arr = [0, 2, 1, -6, 6, -7, 9, 1, 2, 0, 1]
36 # print(solution.can_three_parts_equal_sum(arr)) # Output: True
37
Java Solution
   class Solution {
       public boolean canThreePartsEqualSum(int[] arr) {
           // Calculate the total sum of the elements in the array
           int totalSum = 0;
            for (int num : arr) {
                totalSum += num;
 6
           // If the total sum is not divisible by 3, we cannot split the array into 3 parts with equal sum
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           if (totalSum % 3 != 0) {
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               return false;
12
13
14
           // Initialize two pointers for traversing the array from both ends
15
           int start = 0, end = arr.length - 1;
16
17
           // Initialize sums for the segments from the start and end of the array
18
           int startSum = 0, endSum = 0;
19
```

// Find the first segment from the start that sums up to a third of the total sum

// Find the first segment from the end that sums up to a third of the total sum

// Check if there is a middle segment between the two previously found segments

### 39 // The condition `start < end - 1` ensures there is at least one element in the middle segment return start < end - 1; 41 42 }

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C++ Solution
   #include <vector>
  2 using namespace std;
    class Solution {
    public:
         // This function checks whether we can partition the array into three parts with equal sum
         bool canThreePartsEqualSum(vector<int>& arr) {
  8
             int totalSum = 0;
  9
 10
             // Calculate the sum of all elements in the array
 11
             for (int value : arr) {
 12
                 totalSum += value;
 13
 14
 15
             // If the total sum is not divisible by 3, we can't partition it into three parts with equal sum
 16
             if (totalSum % 3 != 0) return false;
 17
 18
             // The target sum for each of the three parts
 19
             int targetSum = totalSum / 3;
 20
 21
             // Indices to iterate over the array from start (i) and end (j)
 22
             int i = 0, j = arr.size() - 1;
 23
             int sumFromStart = 0, sumFromEnd = 0;
 24
 25
             // Find the partition from the start of the array
 26
             while (i < arr.size()) {</pre>
 27
                 sumFromStart += arr[i];
                 // If we've reached the target sum, stop the loop
 28
 29
                 if (sumFromStart == targetSum) {
 30
                     break;
 31
 32
                 ++i;
 33
 34
 35
             // Find the partition from the end of the array
 36
             while (j \ge 0) {
 37
                 sumFromEnd += arr[j];
 38
                 // If we've reached the target sum, stop the loop
 39
                 if (sumFromEnd == targetSum) {
 40
                     break;
 41
 42
                 --j;
 43
 44
 45
             // After finding the two partitions, check if there is at least one element between them
 46
             return i < j - 1;
 47
 48 };
 49
 50 // Example usage:
 51 // int main() {
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// Expected output: true, because the array can be partitioned as [0, 2, 1], [-6, 6, -7, 9, 1], [2, 0, 1] with equal sum of

#### let i: number = 0, j: number = arr.length - 1; 16 17 let sumFromStart: number = 0, sumFromEnd: number = 0; 18 // Find the partition from the start of the array 19 while (i < arr.length) {

52 //

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55 //

56 // }

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Solution obj;

Typescript Solution

let totalSum: number = 0;

for (let value of arr) {

totalSum += value;

if (totalSum % 3 !== 0) return false;

let targetSum: number = totalSum / 3;

vector<int> arr =  $\{0, 2, 1, -6, 6, -7, 9, 1, 2, 0, 1\};$ 

// If the total sum is not divisible by 3, we can't partition it into three parts with equal sum

bool result = obj.canThreePartsEqualSum(arr);

1 function canThreePartsEqualSum(arr: number[]): boolean {

// The target sum for each of the three parts

// Indices to iterate over the array from start (i) and end (j)

// Calculate the sum of all elements in the array

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sumFromStart += arr[i];
           // If we've reached the target sum, stop the loop
23
           if (sumFromStart === targetSum) {
24
               break;
25
26
           ++i;
29
       // Find the partition from the end of the array
       while (j >= 0) {
30
31
           sumFromEnd += arr[j];
           // If we've reached the target sum, stop the loop
           if (sumFromEnd === targetSum) {
               break;
35
36
           --j;
37
38
       // After finding the two partitions, check if there is at least one element between them
39
       return i < j - 1;
41 }
42
   // Example usage:
   // const arr: number[] = [0, 2, 1, -6, 6, -7, 9, 1, 2, 0, 1];
  // const result: boolean = canThreePartsEqualSum(arr);
   // This would return true, because the array can be partitioned as [0, 2, 1], [-6, 6, -7, 9, 1], [2, 0, 1] with each part summing up
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Time and Space Complexity
Time Complexity
The time complexity of the provided code can be analyzed through its operations step by step.
  1. Calculation of the sum - This involves summing all the elements in the array once, which takes O(N) time, where N is the length of
    the array.
 2. Two separate while loops to find the partition points:
```

## • The first while loop iterates at most N times to find the point where the first third of the array sum can be found (a == s // 3). In the worst case, this is O(N).

• The second while loop is similar, working backwards from the end of the array. This also has a worst-case scenario of O(N). Since these loops do not overlap and are not nested, the overall time complexity is the sum of these individual components, which

would still be O(N).

**Space Complexity** 

- The space complexity of the algorithm is quite straightforward: No additional data structures that grow with the input size are introduced.
- Thus, the space complexity of the function is O(1), indicating constant space usage.

Only a fixed amount of extra variables (s, i, j, a, b) are used regardless of the input size.