1329. Sort the Matrix Diagonally

Sorting

Matrix

## **Problem Description**

<u>Array</u>

Medium

the end of the matrix. The sorting of each diagonal should be done in ascending order, and the goal is to return the matrix with all diagonals sorted. For instance, if a diagonal starts from mat[2][0] in a 6  $\times$  3 matrix, it would include the cells mat[2][0], mat[3][1], and mat[4][2]. This diagonal, like all others in the matrix, needs to be sorted so that the smallest number is at mat [2] [0] and the largest at

The task is to sort the integers in each diagonal of a given m x n matrix mat. A matrix diagonal is defined as a line of cells that

starts from a cell in either the topmost row or leftmost column and goes diagonally in the bottom-right direction until it reaches

mat[4][2].

Intuition

## To solve the problem, we understand that each diagonal can be sorted independently of the others, since the sorting of one diagonal does not affect the elements in another diagonal.

A brute force approach to sort each diagonal is to use a "bubble sort"-like method where for each diagonal, we perform a series of comparisons and swaps until each element on the diagonal is in ascending order. The solution code provided is based on this

approach. Here's how we approach it: Iterate over each possible starting cell of a diagonal. This would usually mean iterating over cells on the top row and the

leftmost column, but the code provided is only iterating through min(m, n) elements. This part of the approach seems to be limiting the number of iterations and may not cover all diagonals in a non-square matrix (where m is not equal to n).

- Perform a double loop, iterating through cells within the matrix boundaries, excluding the last row and column, to compare the current cell mat[i][j] with the next cell in the diagonal mat[i+1][j+1]. If the current cell is larger than the next cell in the diagonal, we swap them. The swap ensures that the smaller value moves
- towards the start of the diagonal. Repeat the comparison and swapping process until all cells in the matrix are checked. Note that this requires multiple passes

through the matrix to get all elements in the correct order, given the nature of the "bubble sort"-like method.

- This solution ensures each diagonal is sorted, but it's not the most efficient approach due to its high time complexity, and it's not optimized to handle non-square matrices correctly in all cases.
- The code provided uses a simplified in-place sorting algorithm similar to bubble sort to sort each diagonal of the matrix. Let's walk through the implementation step by step:

The first step is to retrieve the dimensions of the matrix using len(mat) for the number of rows (m) and len(mat[0]) for the

## It then uses a nested loop to iterate over the elements of the matrix, excluding the last row and column to prevent out-of-

number of columns (n).

Solution Approach

bounds access. The loop variables i and j represent the current cell being considered. The code compares each element mat[i][j] with the next diagonal element mat[i + 1][j + 1]. When it finds that mat[i][j] is greater than mat[i + 1][j + 1], it performs a swap. This operation is intended to move the larger numbers down and right

- along the diagonals and the smaller numbers up and left. However, the provided solution approach only iterates through the diagonals that start in the cells [0, k] for k < min(m, n).
- possible starting cells of the diagonals that could be on the leftmost column for a matrix where m > n. The code will perform the comparison and swapping process repeatedly in a brute force manner, iterating over the matrix cells m-1 times to ensure all cells are eventually sorted. Since bubble sort has a time complexity of O(N<sup>2</sup>), the time

complexity of this code will also reflect the inefficiencies of bubble sort, especially as the size of the matrix grows.

and it's not efficient due to the bubble sort approach resulting in a high time complexity.

1. The first diagonal starting from mat [0] [0] includes the elements [3] (already sorted).

the third diagonal [1, 2, 1] as an example, as it's the longest and requires actual sorting:

We retrieve the dimensions of the matrix, which are m = 3 for rows and n = 3 for columns.

Now, we compare each element on this diagonal with the subsequent diagonal element:

Compare mat [0] [2] (which is 1) with mat [1] [2] (which is 2). No swap needed since 1 is less than 2.

Compare mat[1][2] (which is 2) with mat[2][2] (which is 1). Swap needed since 2 is greater than 1.

After the necessary swap, our diagonal now looks like [1, 1, 2], and it is sorted in ascending order.

Compare mat[0][2] (which is 1) with mat[1][3] (which doesn't exist, so we skip this step).

Compare mat[1][2] (which is 2) with mat[2][3] (which doesn't exist, so we skip this step).

2. The second diagonal starting from mat[0][1] includes the elements [3, 2].

3. The third diagonal starting from mat [0] [2] includes the elements [1, 2, 1].

To sum up, the solution attempts to use a bubble sort-like algorithm over the matrix's diagonals to sort each one in ascending

order. The problem with this implementation is that it may not sort all diagonals as desired, especially for non-square matrices,

This is a simplification and does not sort all diagonals properly in the case of non-square matrices, since it doesn't address all

Note that a more efficient solution would sort each diagonal individually by extracting the diagonal elements, sorting them using a more efficient sorting algorithm (e.g., quicksort or timsort), and then placing them back into the matrix. This approach would significantly reduce the overall time complexity to O(DlogD) for each diagonal of average length D.

Let's walk through a simple example to illustrate the solution approach described. Consider the following 3x3 matrix mat:

[2, 2, 2], [1, 1, 1] The goal is to sort the integers in each diagonal. In this matrix, there are five diagonals:

The sorting algorithm provided will iterate through these diagonals and sort them. Let's focus on how this algorithm would sort

We iterate starting from mat [0] [2], excluding the last row and column to make sure we won't access mat [3] [3] which is out

## 4. The fourth diagonal starting from mat[1][0] includes the elements [2, 1]. 5. The fifth diagonal starting from mat [2] [0] includes the elements [1, 2, 3] (already sorted).

of bounds.

mat = [

[3, 2, 1],

[2, 1, 2],

Solution Implementation

class Solution:

**Example Walkthrough** 

mat = [

[3, 3, 1],

```
Following the above approach, it seems we don't make any swaps. However, since we have to iterate m - 1 times, we will re-
iterate and compare the elements within the matrix boundaries again.
Since we are not going out of bounds, we re-iterate over the matrix:
```

[1, 1, 2]

would be to extract each diagonal, sort it, and then place it back into the matrix.

def diagonalSort(self, mat: List[List[int]]) -> List[List[int]]:

# Only need to iterate up to the smallest dimension minus one

# since we start the comparison from the second-to-last diagonal.

\* Sorts each diagonal of the given matrix independently, where a diagonal

// Compare and swap elements if current element is greater

// than the element in the next row and next column

// Swap elements using a temporary variable

if (matrix[i][j] > matrix[i + 1][j + 1]) {

matrix[i][j] = matrix[i + 1][j + 1];

\* is defined from the top-left to the bottom-right corners.

// Determine the number of rows and columns in the matrix

for (int j = 0; j < numCols - 1; ++j) {

int temp = matrix[i][j];

matrix[i + 1][j + 1] = temp;

\* @param matrix The matrix to be sorted diagonally.

for (int i = 0; i < numRows - 1; ++i) {

\* @return The diagonally sorted matrix.

int numRows = matrix.length;

// Return the sorted matrix

function diagonalSort(matrix: Matrix): Matrix {

for (let row = 0; row < rowCount; ++row) {</pre>

for (let col = 1; col < colCount; ++col) {</pre>

// Helper function that sorts a single diagonal

const diagonalElements: number[] = [];

// Collect all elements of the diagonal

// starting at (startRow, startCol)

let row = startRow;

let col = startCol;

return matrix;

const rowCount = matrix.length; // Number of rows in the matrix

// Sort each diagonal that starts from the first column

// Sort each diagonal that starts from the first row,

// except for the first diagonal which is already sorted

sortDiagonal(matrix, 0, col, rowCount, colCount);

def diagonalSort(self, mat: List[List[int]]) -> List[List[int]]:

# Only need to iterate up to the smallest dimension minus one

# since we start the comparison from the second-to-last diagonal.

if mat[row][col] > mat[row + 1][col + 1]:

# Swap the elements if they are out of order.

# Get the number of rows and columns in the matrix.

num\_rows, num\_cols = len(mat), len(mat[0])

for \_ in range(min(num\_rows, num\_cols) - 1):

for col in range(num\_cols - 1):

for row in range(num\_rows - 1):

sortDiagonal(matrix, row, ∅, rowCount, colCount);

const colCount = matrix[0].length; // Number of columns in the matrix

return matrix;

int numCols = matrix[0].length;

public int[][] diagonalSort(int[][] matrix) {

# Get the number of rows and columns in the matrix.

num\_rows, num\_cols = len(mat), len(mat[0])

for row in range(num\_rows - 1):

for \_ in range(min(num\_rows, num\_cols) - 1):

If we repeat this process for all diagonals, the final sorted matrix will be:

Note that each diagonal is individually sorted, even if the matrix as a whole isn't. However, the described algorithm is not efficient as it might require many iterations for larger matrices due to its similarity to

bubble sort, which has a high time complexity. Also, this example is for a square matrix – the algorithm may not perform correctly

for non-square matrices because it does not iterate through all possible starting cells of the diagonals. A more efficient approach

**Python** 

# Iterate through each element in the matrix except for the last row and column.

for col in range(num\_cols - 1): # Compare the current element with the element in the next diagonal position. if mat[row][col] > mat[row + 1][col + 1]: # Swap the elements if they are out of order. mat[row][col], mat[row + 1][col + 1] = mat[row + 1][col + 1], mat[row][col]# Return the sorted matrix. return mat

```
// Iterate over each element of the matrix except the last row and column
for (int k = 0; k < Math.min(numRows, numCols) - 1; ++k) {</pre>
```

C++

Java

class Solution {

/\*\*

\*/

```
#include <vector>
#include <algorithm> // For std::sort function
class Solution {
public:
    std::vector<std::vector<int>> diagonalSort(std::vector<std::vector<int>>& matrix) {
        int rowCount = matrix.size(); // Number of rows in the matrix
        int colCount = matrix[0].size(); // Number of columns in the matrix
       // Sort each diagonal that starts from the first column
        for (int row = 0; row < rowCount; ++row) {</pre>
            sortDiagonal(matrix, row, 0, rowCount, colCount);
        // Sort each diagonal that starts from the first row, except the first diagonal which is already sorted
        for (int col = 1; col < colCount; ++col) {</pre>
            sortDiagonal(matrix, 0, col, rowCount, colCount);
        return matrix;
private:
    // Helper function to sort a single diagonal starting at (startRow, startCol)
    void sortDiagonal(std::vector<std::vector<int>>& matrix, int startRow, int startCol, int rowCount, int colCount) {
        int row = startRow;
        int col = startCol;
        std::vector<int> diagonalElements;
       // Collect all elements of the diagonal
       while (row < rowCount && col < colCount) {</pre>
            diagonalElements.push_back(matrix[row][col]);
            ++row;
            ++col;
       // Sort the collected diagonal elements
        std::sort(diagonalElements.begin(), diagonalElements.end());
       // Put the sorted elements back into their places on the diagonal
        row = startRow;
        col = startCol;
        for (int element : diagonalElements) {
            matrix[row][col] = element;
            ++row;
            ++col;
TypeScript
type Matrix = number[][];
// This function sorts the matrix diagonally
```

```
while (row < rowCount && col < colCount) {</pre>
    diagonalElements.push(matrix[row][col]);
    ++row;
    ++col;
// Sort the collected diagonal elements
diagonalElements.sort((a, b) => a - b);
// Put the sorted elements back into their places on the diagonal
row = startRow;
col = startCol;
for (const element of diagonalElements) {
   matrix[row][col] = element;
   ++row;
    ++col;
```

# Iterate through each element in the matrix except for the last row and column.

# Compare the current element with the element in the next diagonal position.

mat[row][col], mat[row + 1][col + 1] = mat[row + 1][col + 1], mat[row][col]

function sortDiagonal(matrix: Matrix, startRow: number, startCol: number, rowCount: number, colCount: number): void {

```
diagonals. Let's analyze both the time and space complexity:
```

# Return the sorted matrix.

**Time and Space Complexity** 

return mat

**Time Complexity** The outermost loop is controlled by min(m, n) - 1, where m is the number of rows and n is the number of columns in the matrix.

The provided code has a nested loop structure that iterates over the elements in the matrix in a specific pattern to sort the

This loop will run for the minimum dimension - 1. Inside the outer loop, there are two nested loops that each run m-1 and m-1 times respectively, iterating over the elements of

n) \* m \* n).

class Solution:

the matrix. The combined time complexity is the product of these factors, resulting in O((min(m, n) - 1) \* (m - 1) \* (n - 1)).

Simplifying, we drop constants and lower-order terms to focus on the growth rates, which gives us a time complexity of O(min(m,

**Space Complexity** The space complexity of the code is 0(1) because there are no data structures being used that grow with the size of the input.

The only extra space used here is for the loop variables and a couple of temporary variables for the swapping process.