Problem Description

operator. The result should be the integer part of the quotient, with the division result truncated towards zero, meaning that any fractional part is disregarded. This operation should be handled with care as the problem also specifies dealing with overflows by capping the return value at 32-bit signed integer limits. In essence, we are to implement a form of division that replicates how integer division works in programming languages where the

The problem at hand requires us to divide two integers, dividend and divisor, without using multiplication, division, and mod

result is truncated towards zero, ensuring we work within the 32-bit integer range. We have to be cautious, as the direct operations that normally achieve this (/, *, %) are not permitted.

The solution relies on the concept of subtraction and bit manipulation to accomplish the division. Since we can't use the division

Intuition

divided by 2, it means how many times we can subtract 2 from 10 until we reach a number less than 2. The intuition behind the solution is to use a subtraction-based approach where we keep subtracting the divisor from the dividend and count how many times we can do this until the dividend is less than the divisor. This is a valid first step but not efficient enough

operator, we think about what division actually means. Division is essentially repeated subtraction. For instance, when we say 10

for large numbers, which is where bit manipulation comes in handy. To improve efficiency, instead of subtracting the divisor once at a time, we exponentially increase the subtracted amount by left shifting the divisor (which is equivalent to multiplying by powers of 2) and subtract this from the dividend if possible. This approach

is much faster, as left shifting effectively doubles the subtracted amount each time, allowing us to subtract large chunks in logarithmic time compared to a linear approach. The whole process loops, increasing the amount being subtracted each time (as long as the double of the current subtraction

amount is still less than or equal to the remaining dividend) and adding the corresponding power of 2 to our total. This loop

ensuring the result stays within the specified integer range. Time and space complexity is considered, especially since we are working within a constrained environment that doesn't allow typical operations. The time complexity here is O(log(a) * log(b)), with 'a' being the dividend and 'b' the divisor. This complexity arises because the algorithm processes parts of the dividend in a time proportional to the logarithm of its size, and likewise for the

represents a divide and conquer strategy that works through the problem using bit-level operations to mimic standard division while

number of variables regardless of the size of the inputs. **Solution Approach** The approach to solving the division problem without multiplication, division, or mod operator involves a few key steps and utilizes

divisor since the subtraction step is proportional to its logarithm as well. The space complexity is constant, O(1), since we use a fixed

1. Handle Signs:

or 1 for a positive one.

 First, we need to handle the sign of the quotient. If the dividend and divisor have the same sign, the result is positive; otherwise, it's negative. We define the variable sign and use a simple comparison to set its value to -1 for a negative result

2. Initialize Variables:

would exceed the current dividend.

Reduce the dividend by divisor << cnt.

Here's a step-by-step walkthrough of the implementation:

simple yet powerful concepts of bit manipulation to efficiently find the quotient.

- Set INT_MAX as (1 << 31) − 1, which represents the maximum positive value for a 32-bit integer. \circ Set INT_MIN as -(1 << 31), representing the minimum negative value for a 32-bit integer. Initialize the quotient tot to 0. 3. Bitwise Shift for Division:

• We start a loop where we continue to subtract the divisor from the dividend until dividend is smaller than divisor. For

■ Inside an inner loop, left shift the divisor by cnt + 1 positions, effectively multiplying the divisor by 2 each time, until it

each subtraction: Initialize a counter cnt with 0.

4. Finalizing Result:

Example Walkthrough

 After finding the maximum amount by which we can multiply the divisor without exceeding the dividend, we add 1 < cnt to our running total tot. This is equivalent to adding 2^cnt.

The actual division operation will be conducted on the absolute values of the dividend and divisor.

If the result exceeds the range, return INT_MAX.

If the result is within the range [INT_MIN, INT_MAX], return the result.

Handle potential integer overflow by comparing the result against INT_MAX and INT_MIN:

Multiply the tot by the sign to apply the correct sign to the result.

complexity is 0(1) since the number of variables used does not scale with input size. The pattern used here can be thought of as a "divide and conquer" as well as "bit manipulation". By using these principles, we can

efficiently and accurately divide two integers in a constrained environment.

INT_MAX is set as (1 << 31) - 1 and INT_MIN is set as -(1 << 31).

Begin the loop to subtract divisor from dividend.

Add 1 << cnt which is 1 << 1 or 2 to tot.

Add 1 << cnt which is 1 to tot. Now, tot = 2 + 1 = 3.

def divide(self, dividend: int, divisor: int) -> int:

sign = -1 if (dividend * divisor) < 0 else 1

Define the boundaries for an integer (32-bit signed integer)

Work with positive values for both dividend and divisor

while dividend >= (divisor << (count + 1)):</pre>

Increment total_quotient by the number of times we doubled the divisor

Decrease dividend by the matched part which we just calculated

// If the result is still outside the range, return the max integer value

// Determine sign of the result based on the signs of dividend and divisor

Let's walk through a small example to illustrate the solution approach as described. Suppose our dividend is 10 and our divisor is 3. We need to find out how many times we can subtract 3 from 10, with the operations restricted as per the problem statement. 1. Handle Signs:

This algorithm effectively simulates division by breaking it down into a combination of subtraction and left bitwise shift operations,

with each recursive subtraction, hence the $0(\log a * \log b)$ time complexity, where a is the dividend and b is the divisor. Space

replicating multiplication by powers of 2. It's a logarithmic solution in the sense that it reduces the problem size by approximately half

• Both the dividend (10) and divisor (3) are positive, so our result will also be positive. Thus, sign = 1.

3. Bitwise Shift for Division:

2. Initialize Variables:

Initialize total quotient tot = 0.

■ 3 << 0 is 3, and 3 << 1 (which is 6) is still <= 10 (dividend). ■ 3 << 2 would be 12, which exceeds 10. So, we can stop at cnt = 1.

∘ Subtract divisor << cnt which is 3 << 1 or 6 from dividend. Now, dividend = 10 - 6 = 4.

On the first iteration, cnt = 0. We check if (divisor << cnt + 1) <= dividend:</p>

∘ Subtract divisor << cnt (which is 3) from dividend. Now, dividend = 4 - 3 = 1.

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    With the new dividend of 4, repeat the process:

    On the second iteration, cnt = 0.3 << cnt + 1 is 6, which is greater than 4. So we can't shift cnt to 1 this time.</li>
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Python Solution

 $INT_MAX = 2**31 - 1$

dividend = abs(dividend)

Initialize the total quotient

count += 1

elif result > INT_MAX:

return INT_MAX

return result

return Integer.MAX_VALUE;

int divide(int dividend, int divisor) {

total_quotient += 1 << count

dividend -= divisor << count

Multiply the result by the sign

divisor = abs(divisor)

 $INT_MIN = -2**31$

1 class Solution:

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4. Finalizing Result: Because dividend is now less than divisor, we can conclude our calculation. Since we began with tot = 0 and added 2 first and then 1 to it, we have tot = 3. Multiply tot by sign. Since sign = 1, the result remains tot = 3. Check for overflow, which isn't the case here, so the final result is 3. Thus, dividing 10 by 3 yields a quotient of 3 using this approach. Since we are only concerned with the integer part of the division, the remainder is disregarded, aligning with the truncation towards zero rule. The bit manipulation significantly speeds up the process by allowing us to subtract larger powers of 2 wherever possible.

Determine the sign of the output. If dividend and divisor have different signs, result will be negative

total_quotient = 0 15 16 17 # Loop to find how many times the divisor can fit into the dividend while dividend >= divisor: 18 # Count will keep track of the number of times we can double the divisor while still being less than or equal to dividenc 19 20 count = 0 # Double the divisor as much as possible without exceeding the dividend 21

30 result = sign * total_quotient 31 32 # Check and correct for overflow: if result is out of the 32-bit signed integer range, clamp it to INT_MAX 33 if result < INT_MIN:</pre> 34 return INT_MIN

Java Solution

else:

```
class Solution {
       public int divide(int dividend, int divisor) {
           // Determine the sign of the result
            int sign = 1;
            if ((dividend < 0) != (divisor < 0)) {</pre>
                sign = -1;
            // Use long to avoid integer overflow issues
            long longDividend = Math.abs((long) dividend);
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            long longDivisor = Math.abs((long) divisor);
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            // This will accumulate the result of the division
            long total = 0;
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            // Loop to find how many times the divisor can be subtracted from the dividend
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           while (longDividend >= longDivisor) {
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                // This counter will keep track of the number of left shifts
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                int count = 0;
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                // Double the divisor until it is less than or equal to the dividend
21
               while (longDividend >= (longDivisor << (count + 1))) {</pre>
                    count++;
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                // Add the number of times we could double the divisor to the total
27
                total += 1L << count;
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                // Subtract the final doubled divisor value from the dividend
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                longDividend -= longDivisor << count;</pre>
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            // Multiply the sign back into the total
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            long result = sign * total;
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           // Handle overflow cases by clamping to the Integer range
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            if (result >= Integer.MIN_VALUE && result <= Integer.MAX_VALUE) {</pre>
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                return (int) result;
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C++ Solution

1 class Solution {

2 public:

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int resultSign = (dividend < 0) ^ (divisor < 0) ? -1 : 1;
           // Use long long to avoid overflow issues for abs(INT32_MIN)
            long long absDividend = abs(static_cast<long long>(dividend));
            long long absDivisor = abs(static_cast<long long>(divisor));
            long long result = 0; // Initialize result
           // Loop until the dividend is smaller than divisor
           while (absDividend >= absDivisor) {
                int shiftCount = 0; // Count how many times the divisor has been left-shifted
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               // Find the largest shift where the shifted divisor is smaller than or equal to dividend
               while (absDividend >= (absDivisor << (shiftCount + 1))) {</pre>
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                    ++shiftCount;
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               // Add to the result the number represented by the bit at the found position
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                result += 1ll << shiftCount;
23
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                // Reduce dividend by the found multiple of divisor
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                absDividend -= absDivisor << shiftCount;</pre>
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           // Apply sign of result
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            result *= resultSign;
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           // Handle overflow by returning INT32_MAX if the result is not within int range
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           if (result >= INT32_MIN && result <= INT32_MAX) {</pre>
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                return static_cast<int>(result);
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           return INT32_MAX;
36
37 };
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Typescript Solution
  1 // Global function for division without using division operator
     function divide(dividend: number, divisor: number): number {
         // Determine sign of the result based on the signs of dividend and divisor
         let resultSign: number = (dividend < 0) ^ (divisor < 0) ? -1 : 1;</pre>
         // Use number to accommodate for JavaScript's safe integer range
         // and to avoid precision issues with bitwise operations
         let absDividend: number = Math.abs(dividend);
         let absDivisor: number = Math.abs(divisor);
  9
         let result: number = 0; // Initialize result
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if (result >= -(2 ** 31) && result <= (2 ** 31) - 1) {

return Math.trunc(result);

return (2 ** 31) - 1;

Time and Space Complexity

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The time complexity of the given code is $O(\log(a) * \log(b))$. This is because in the first while loop, we're checking if a is greater than or equal to b, which requires O(log(a)) time since in each iteration a is reduced roughly by a factor of two or more. The inner

Time Complexity

11 12 // Loop until the dividend is smaller than divisor 13 while (absDividend >= absDivisor) { 14 let shiftCount: number = 0; // Count how many times the divisor has been multiplied by 2 15 // Find the largest multiple of 2 for divisor that is still less than or equal to dividend 16 while (absDividend >= (absDivisor * Math.pow(2, shiftCount + 1))) { 17 18 shiftCount++; 19 20 21 // Accumulate the quotient by the power of 2 corresponding to the shift count 22 result += Math.pow(2, shiftCount); 23 24 // Decrease dividend by the found multiple of the divisor 25 absDividend -= absDivisor * Math.pow(2, shiftCount); 26 27 // Apply the sign of the result result *= resultSign; // Handle overflow by returning the maximum safe integer value if the result is not within 32-bit signed integer range

while loop is responsible for finding the largest shift of b that a can handle, which will execute at most 0(log(b)) times, as shifting b left by one doubles its value, and cnt increases until a is no longer greater than b shifted by cnt + 1. Therefore, these two loops combined yield the time complexity mentioned.

Space Complexity

The space complexity of the given code is 0(1). Only a fixed number of integer variables sign, tot, and cnt are used, which do not depend on the size of the input. Hence, the space used is constant.