Problem Description

task needs to run. The computer can run these tasks simultaneously, and we have the flexibility to turn the computer on and off as needed. Our goal is to figure out the minimum amount of time the computer needs to be active (turned on) to accomplish all the tasks within their respective time ranges. To visualize this problem, think of each task as a window of time during which it can be performed. The computer must be turned on

In this task scheduling problem, we are given a list of tasks, each with a start time, end time, and a duration indicating how long the

long enough to "cover" these windows cumulatively. Since tasks can overlap in time, we want to make sure we are efficient about when we are running the computer to minimize the total on time.

The intuition behind the solution approach is to manage the scheduling of tasks in a way that maximizes the overlap of their execution windows, hence reducing the total time the computer is on. To achieve this, we sort the tasks based on their end time.

Intuition

This allows us to prioritize the completion of tasks that need to be finished sooner. Next, we try to select time points for each task starting from the task's end time and moving backwards to fill in its required duration. This increases the likelihood that the computer's operating time for one task will also count towards the operating times of

earlier than needed for any given task. To keep track of which time points have already been scheduled, we use an array vis as a timeline, marking off time points that have been allocated. For each task, we first determine how many of its required time points are already covered by other tasks (scheduled previously), and then we fill in the remaining duration as needed. The total number of "turned on" time points, ans, gives us the

minimum time the computer needs to be active. After iterating through all tasks in this manner and updating the timeline (vis array),

subsequent tasks, essentially reusing time points. This greedy approach ensures that we do not unnecessarily turn on the computer

the final value of ans will be our desired minimum on time. By being strategic about the order in which we choose time points for tasks and by optimizing for overlap, we arrive at a solution that minimizes the computer's active time while ensuring all tasks are completed within their respective time windows. **Solution Approach**

The solution uses a greedy algorithm, a common pattern for optimization problems where we build up a solution piece by piece, selecting the most optimal choice at each step. In this case, sorting tasks by their end times and selecting time points for each task from end to start qualifies as such a choice. The underlying data structures used are a simple list for tracking tasks and an array (list)

Here's a step-by-step breakdown of the implementation:

1. Sorting tasks: We sort the tasks by their end times, which is done using Python's sort method with a lambda function defining the sorting key as x[1], where x is each task and x[1] represents the end time of each task. 1 tasks.sort(key=lambda x: x[1])

2. Initializing the timeline: An array vis is created with a sufficient size (2010 is chosen to cover the range of possible

1 vis = [0] * 2010

timestamps), initialized to 0s, indicating that no time points have been used yet.

the ans count indicating the computer was turned on for another time unit.

for recording which time points have already been selected.

and reduce the duration of the task accordingly. 1 duration -= sum(vis[start : end + 1])

4. Filling in the remaining duration: We iterate from the task's end time down to its start time, and for each unit of time, if it has

not been used (if not vis[i]), we decrease the remaining duration, mark the time point as used (vis[i] = 1), and increment

3. Greedy time point selection: For each task, we determine how many time points are already covered (sum(vis[start:end + 1]))

1 i = end

vis[i] = 1ans += 1 i -= 1

5. Returning the result: After processing all tasks, ans holds the total number of time points selected, which is the minimum time

The strategy ensures that if a time point can serve multiple tasks, it will be used for all of them, reducing the total number of distinct

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time points, and thus, the total time the computer needs to be on. By iterating from the end of the task's window towards the start,
we prioritize later usage over earlier, which aligns with our sorted task list and makes it more likely to reuse time points for
subsequent tasks.
The overall time complexity of the algorithm is O(n * k), where n is the number of tasks, and k is the average range of the tasks (end
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duration which might involve iterating over the range of the task.

represented as [start time, end time, duration].

The tasks are already sorted by their end times.

reduce duration to 0. The ans count is now 3.

We use time 6, mark it as used, and increment ans to 4.

1 vis = [..., 0, 1, 1, 1, 0, 1, 0, ...] # Now index 6 is also marked as 1.

def findMinimumTime(self, tasks: List[List[int]]) -> int:

while i >= start_time and duration > 0:

if not visited[i]:

duration -= 1

visited[i] = 1

If the time slot is not yet visited

Mark this time slot as visited

minimum_time_required += 1

Initialize a pointer at the end time of the current task

Check if we can place the task in the current window and still need more duration

Decrease the remaining duration since we are using this time slot

Increment the minimum time required since we've occupied another time slot

Move to the previous time slot and repeat till the start time or the task duration is met

2 while i >= start and duration > 0:

duration -= 1

if not vis[i]:

the computer needs to be on.

Example Walkthrough Let's use a simplified example to illustrate the solution approach. Assume we have 3 tasks that need to be scheduled, with each task

- start). It is dominated by the time taken to find the sum of visited time points for each task and attempting to fill its remaining

3 Task 3: [5, 8, 1] **Step 1:** Sort the tasks by their end times. After sorting: 1 Task 1: [1, 4, 3]

Step 2: Initialize the timeline (vis) as an array with sufficient size.

2 Task 2: [2, 6, 2]

3 Task 3: [5, 8, 1]

Task List:

1 Task 1: [1, 4, 3] 2 Task 2: [2, 6, 2]

1 vis = [0] * 2010 # 2010 is just for example purposes and assumes no times will exceed this value. Step 3: Move through the tasks one by one and try to cover each task's duration, starting from its end time.

• For Task 1 [1, 4, 3], we start from time 4. Since no other task is scheduled yet, we mark times 4, 3, and 2 as used in vis and

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• For Task 2 [2, 6, 2], we see that time 2 is already used by Task 1. We only need to schedule Task 2 for one more unit of time.
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2 ans = 3

2 ans = 4

1 vis = [..., 0, 1, 1, 1, 0, 1, 0, 1, ...] # Index 8 is marked as 1. 2 ans = 5

• For Task 3 [5, 8, 1], we start from time 8. It's free, so we mark it as used, and ans increments to 5.

1 vis = [..., 0, 1, 1, 1, 0, 0, ...] # '...' represents unchanged values; index 2 to 4 are marked as 1.

```
Step 4: After all tasks have been scheduled, ans is 5, which means the minimum time the computer needs to be active is 5 units.
Summary: The tasks overlap between time 2 and 4, so the computer only needs to be active for a total of 5 time units to cover all
tasks, even though the sum of individual task durations is 6. The greedy approach successfully minimized the computer's on time by
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Initialize a list to keep track of visited time slots, assuming the maximum end time is less than 2010 visited = [0] * 2010 9 10 # Initialize answer to count the minimum time required to finish all tasks 11 12 minimum_time_required = 0

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           # Iterate over each task
15
           for start_time, end_time, duration in tasks:
               # Decrease duration by the number of already visited time slots within the task's window
16
               duration -= sum(visited[start_time:end_time + 1])
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i = end_time

Python Solution

class Solution:

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41 }

return ans;

2 #include <algorithm> // For sort

bitset<2010> visited;

int minimumTimeRequired = 0;

for (const auto& task : tasks) {

C++ Solution

1 #include <vector>

#include <bitset>

class Solution {

6 public:

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from typing import List

scheduling overlapping tasks simultaneously.

Sort tasks by the end time

tasks.sort(key=lambda x: x[1])

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                    i -= 1
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38
           # Return the computed minimum time required to finish all tasks
39
            return minimum_time_required
40
Java Solution
   import java.util.Arrays;
   class Solution {
       public int findMinimumTime(int[][] tasks) {
           // Sort the tasks based on their end times
           Arrays.sort(tasks, (a, b) \rightarrow a[1] - b[1]);
           // Initialize an array to track the usage of each time slot
           int[] visits = new int[2010];
10
           // Initialize an answer variable to keep the count of visited time slots
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13
           int ans = 0;
14
           // Iterate through each task
           for (int[] task : tasks) {
16
                int startTime = task[0]; // Start time of the current task
17
                int endTime = task[1]; // End time of the current task
18
                int duration = task[2]; // Duration of the current task needs in terms of unvisited time slots
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20
21
               // Decrease duration for each visited time slot within the task's time range
                for (int i = startTime; i <= endTime; i++) {</pre>
                  duration -= visits[i];
23
24
                    if (duration < 0) {</pre>
                        duration = 0; // Duration shouldn't be less than 0
25
26
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29
               // Allocate unvisited time slots starting from the end time of the task
                for (int i = endTime; i >= startTime && duration > 0; i--) {
30
                    if (visits[i] == 0) { // If time slot is unvisited
31
                        --duration; // Decrement the remaining duration
                        ans += visits[i] = 1; // Visit this time slot and increment the answer
33
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// Return the total number of visited time slots used to execute all tasks

sort(tasks.begin(), tasks.end(), [&](const auto& a, const auto& b) { return a[1] < b[1]; });</pre>

// Initialize a bitset to keep track of visited time slots, assuming maximum 2010 slots

// Calculate the amount of duration that can be allocated within the time window

// Reduce duration for already visited time slots within the window

// Initialize the answer to store the minimum number of time slots required

// Function to find the minimum time to complete all tasks

// Sort the tasks by their end time in ascending order

for (int i = startTime; i <= endTime; ++i) {</pre>

int findMinimumTime(vector<vector<int>>& tasks) {

// Iterate over each task to schedule them

duration -= visited[i];

20 // Extracting the start time, end time and duration for each task 21 int startTime = task[0]; int endTime = task[1]; 23 int duration = task[2]; 24

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31
               // Assign time slots for remaining duration in reverse order to meet end time
               for (int i = endTime; i >= startTime && duration > 0; --i) {
                   // If the time slot is not yet visited
33
                   if (!visited[i]) {
34
35
                       // Decrease remaining duration and mark this time slot as visited
36
                       --duration;
                       minimumTimeRequired += visited[i] = 1;
37
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41
           // Return the computed minimum time required to complete all tasks
           return minimumTimeRequired;
45 };
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Typescript Solution
   function findMinimumTime(tasks: number[][]): number {
     // Sort the tasks array by end time in ascending order
     tasks.sort((taskA, taskB) => taskA[1] - taskB[1]);
     // Create an array to keep track of visited times, initialized with zeros
     const visited = new Array(2010).fill(0);
     // Initialize the answer variable to count the minimum time needed to complete tasks
     let minimumTime = 0;
9
10
11
     // Iterate through each task to find the minimum time necessary
     for (let task of tasks) {
12
       const [startTime, endTime, taskDuration] = task; // Destructure task details
14
15
       let remainingDuration = taskDuration; // Initialize remaining task duration
16
17
       // Calculate the remaining duration after considering previously visited time slots
       for (let time = startTime; time <= endTime; ++time) {</pre>
18
         remainingDuration -= visited[time];
20
21
22
       // Fill the time slots from end to start respecting the task duration
23
       for (let time = endTime; time >= startTime && remainingDuration > 0; --time) {
         if (visited[time] === 0) {
24
           --remainingDuration; // Decrease remaining duration as we fill the time slot
           minimumTime += visited[time] = 1; // Mark the time slot as visited and increment minimum time
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30 // Return the computed minimum time necessary to complete the tasks 31 32 return minimumTime; 33 } 34

Time and Space Complexity

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The given code sorts the tasks list, which takes O(NlogN) time, where N is the number of tasks. After sorting, the code iterates through each task with a nested while loop. In the worst case, for each task, the while loop could

Time Complexity

iterate from end to start, which could be O(M), where M is the range of possible start and end times. As a rough upper bound, this nested iteration could result in the inner operation being executed N * M times, since for each of 'N'

tasks, the while loop could potentially iterate 'M' times (where 'M' is the largest possible end time — in this case, 2010). However, because each time unit can only be visited once due to the vis condition, the total number of operations of the inner loop is bounded by 'M' across all tasks. This makes the nested while loop take O(M) in total.

we consider M to be a constant, then the time complexity simplifies to O(NlogN). **Space Complexity**

Summing these two parts, the overall time complexity is O(NlogN + M). Note that in practice, M is bounded by a constant (2010), so if

The space consumed by the solution includes the storage for the visited time units vis, which has a fixed size based on the problem constraints (2010), and the internal space used for the sorted array of tasks. Therefore, the space complexity is 0(M + N). If M is considered to be a constant due to its fixed upper bound, then the space complexity simplifies to O(N).