1883. Minimum Skips to Arrive at Meeting On Time

Hard Array Dynamic Programming

Leetcode Link

You are scheduled to attend a meeting and have a fixed number of hours, hoursBefore, to cover a certain distance through n roads.

Problem Description

The lengths of these roads are represented as an integer array dist, where dist[i] is the length of the ith road in kilometers. You are given a consistent speed in km/h, denoted by the variable speed.

There is a constraint imposed on your travel -- after completing each road, you're required to rest until the start of the next whole

hour before you commence the next leg of your journey. However, this mandatory rest period is waived for the final road as you've already arrived at your destination by then.

Interestingly, to help you arrive on time, you are permitted to skip some of these rest periods. Skipping a rest means you don't have

to wait for the next whole hour, which might help you align your travel more closely with the hours available.

The core challenge of the problem is determining the minimum number of rest periods you must skip to ensure you arrive at your meeting on time, if at all possible. If there's no way to make it on time, you should return -1.

To solve this problem, dynamic programming is an appropriate approach because we can break down the larger problem into smaller

subproblems. Each subproblem involves evaluating the minimal time required to reach the end of a certain road with a specific

The intuition behind this approach begins with examining every possible scenario where you choose to either wait for the rest period or skip it after each road. We aim to find the strategy that takes the least amount of time to arrive at the meeting on time while

each road.

programming.

number of skips.

skipping the fewest rest periods.

We maintain an array f, where f[i][j] represents the minimum time to reach the end of the ith road with j skips. The algorithm iterates through each road and each possible number of skips, updating the time calculation to reflect whether we wait or skip after

By initializing f[i][j] with an infinitely large number, we ensure that any actual calculated time will be considered in our comparisons. The iterative process compares the current minimum time f[i][j] with the time achieved by either waiting or skipping the rest period, updating as needed to hold the least time.

With all the subproblems solved, we look for the minimum number of skips needed that still allows us to arrive within hoursBefore. We iterate through the possible number of skips and return the smallest number for which the corresponding time does not exceed hoursBefore. If all scenarios exceed the time limit, we return -1, signaling it's impossible to attend the meeting on time.

The provided solution code represents this approach and calculates the minimum skips required accurately using dynamic

Solution Approach

The solution utilizes dynamic programming, which involves breaking down the problem into smaller, manageable subproblems and

• A 2D list f of size (n + 1) x (n + 1) is initialized with inf (representing infinity). This array will store the minimum time needed

1. Initialization: Since Python lists start at index 0 but roads start at 1, we set f [0] [0] to 0 to denote that at the beginning (before traveling any road), no time has passed.

Data Structures:

then building up to the solution.

Algorithms and Patterns:

2. Dynamic Programming Iteration:

traveling any road.

to reach each road with a given number of skips.

The inner loop iterates through every possible number of skips (j) that could be applied up to the current road i.
 State Transition:

• Inside the inner loop, the algorithm considers two scenarios to find the minimum time to complete road i with j skips:

■ Waiting: The algorithm calculates the time if we wait for the next integer hour mark after road i-1. This is done by

adding x / speed (time to travel the current road) to f[i - 1][j] (minimum time to reach the previous road with the

same number of skips) and applying ceil to round up to the next hour. An epsilon eps is subtracted before applying the

• The outer loop iterates through each road (denoted by i), starting from 1, since we consider 0 as the starting point before

ceil function to handle floating point precision issues. Skipping: The time is directly added without the ceiling for the case where we skip the rest period after road i-1. This is

4. Comparing and Updating States:

determined whether it is possible to arrive on time.

The possible states as we iterate through our array f:

Skipping is not an option since it's the first road.

3 (second road) hours, so f[2][1] = 8.

so f [3] [1] doesn't need to be considered.

the rest on the last road, f[3][2] = 14.

Without skipping, we'll spend ceil(5 / 1) = 5 hours, so f[1][0] = 5.

skipping, this attempt is infeasible, so we skip considering f[3][0].

j ranges from 0 to n (3 in this case) such that f[n][j] <= hoursBefore (6).

def minSkips(self, distances: List[int], speed: int, hours_before: int) -> int:

At the beginning, zero skips are made and the total time is also zero

A very small epsilon value to avoid floating-point precision issues

Can only skip if skips > 0, hence we check it

if dp[num_of_sections][skips] <= hours_before + epsilon:</pre>

If none fit within the hours_before limit, return -1

// Base case: no distance covered without any skips

// Small value to avoid precision issues

for (int i = 1; i <= numSegments; ++i) {</pre>

dp[i][j] = Math.min(

dp[i][j],

// If taking one less skip

dp[i][j],

for (int j = 0; j <= numSegments; ++j) {</pre>

int numDistances = distances.size();

// Iterate over each segment of the journey.

// Iterate over the possible number of skips.

// If we are not skipping the current segment.

for (int i = 1; i <= numDistances; ++i) {</pre>

for (int j = 0; $j \le i$; ++j) {

if (j < i) {

double eps = 1e-8;

if (dp[numSegments][j] <= hoursBefore + eps) {</pre>

return j; // Found the minimum skips required

int minSkips(vector<int>& distances, int speed, int hoursBefore) {

// Number of different distances that we need to travel.

return -1; // It's not possible to reach on time with given constraints

dp[i][j] = Math.min(

for (int j = 0; $j \le i$; ++j) {

Initialize a DP table with infinity to store number of skips for reaching certain points

Option 2: Skip this section and therefore no rest needed (no ceil)

// If not taking the maximum number of skips (which would be the segment index)

Math.ceil(dp[i - 1][j] - eps) + (double) distances[i - 1] / speed

// 'dp' will store the minimum time required to reach a certain point with a given number of skips.

 $dp[i][j] = min(dp[i][j], ceil(dp[i - 1][j] + static_cast<double>(distances[i - 1]) / speed - eps));$

// A small epsilon is used to perform accurate floating-point comparisons later on.

dp[i-1][j-1] + (double) distances[i-1] / speed

// Determine the minimum number of skips needed to reach the target within hoursBefore

Check each possible number of skips to see if it fits within the hours_before limit

dp[i][skips] = min(dp[i][skips], dp[i - 1][skips - 1] + distance / speed)

dp = [[float('inf')] * (num_of_sections + 1) for _ in range(num_of_sections + 1)]

and we conclude that it is impossible to arrive on time. We return -1.

Iterate through each section of the distances

for i, distance in enumerate(distances, 1):

for skips in range(num_of_sections + 1):

Length of the distances array

num_of_sections = len(distances)

Mathematical Formulas:

Example Walkthrough

mark.

1 f[0][0] = 0

1 f[0][0] = 0

The algorithm compares the outcomes of waiting and skipping, updating f[i][j] with the minimum value.
 Finding the Result:

only applicable if j is non-zero, i.e., we have skipped at least once.

the smallest number of skips that would still allow us to arrive within hoursBefore.
 This is done by iterating over the possible number of skips for the final road (f[n][j] where j ranges from 0 to n) and checking if that time is less than or equal to hoursBefore. A small epsilon eps is added to the time limit to handle floating point precision issues.
 If such a j is found, it's returned as the minimum number of skips required. If all possible skips result in times greater than hoursBefore, the function returns -1.

By the end of the iteration, the solution will have considered every possible way to allocate the skips to minimize the travel time and

• The ceil function is used to account for the need to round up to the next integer hour when waiting after each road, and

The algorithm's complexity is bounded by the number of roads n and the number of possible skips, which can also be at most n.

subtraction of an epsilon is used to correct for any floating point errors that could incorrectly round down when right on the hour

After we've filled in the f array with the minimum traveling times for all possible skips for each road, the algorithm looks for

Hence, we have a time complexity of O(n^2), which is generally acceptable for the road lengths and number of hours before the meeting typically encountered in this type of problem.

To illustrate the solution approach, let's take a small example. Assume we need to cover a distance through 3 roads with lengths

given by the array dist = [5, 3, 6], where hoursBefore = 6 hours and our consistent speed is speed = 1 km/h.

skips. The f array would be a 4×4 array in this case, considering n=3.

We first initialize f[0][0]=0. This denotes that we're at the starting point and haven't spent any time or skips yet.

Let's create an array f of size (n + 1) x (n + 1) filled with inf to represent the minimum time taken with a corresponding number of

2 f[1][0] = 5 Next, the second road of 3 km:

Finally, the third road of 6 km:

f[0][0] = 0

Python Solution

class Solution:

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from math import ceil

dp[0][0] = 0

epsilon = 1e-8

if skips:

return skips

return -1

dp[0][0] = 0;

double eps = 1e-8;

// Populate the dp array

 $if (j < i) {$

);

if (j > 0) {

);

Moving on to the first road of 5 km:

1 f[0][0] = 0 2 f[1][0] = 5 3 f[2][0] = 8 4 f[2][1] = 8

Without skipping, we're now at ceil((8 + 6) / 1) = 14 hours, but since we can't reach our destination on time without

With one skip carried over and skipping after the second road, we would spend 5 + 3 + 6 = 14 hours, which is again infeasible,

With two skips, assuming we skipped after the first and second roads, we would spend 5 + 3 + 6 = 14 hours. Since we can skip

Without skipping, we'll spend ceil((5 + 3) / 1) = 8 hours in total (5 from the first road, and 3 for this road), so f[2][0] = 8.

• With one skip (assuming we skipped after finishing the first road), we would spend 5 (from the first road without waiting) +

2 f[1][0] = 5
3 f[2][0] = 8 (infeasible as exceeds `hoursBefore`)
4 f[2][1] = 8 (infeasible as exceeds `hoursBefore`)
5 f[3][0] = x
6 f[3][1] = x
7 f[3][2] = 14

Now, we must consider all options for the number of skips (up to the number of roads n=3). Ideally, we would look for f[n][j] where

When evaluating f[3][2], we can see the value is 14 which exceeds hoursBefore. Thus, none of our options meet the requirement,

For each section, calculate the minimum number of skips required to reach it
for skips in range(i + 1):
 if skips < i:
 # Option 1: Do not skip this section but might need to skip a future section
Ceil is used to round up to the nearest integer to enforce a rest period
dp[i][skips] = min(dp[i][skips], ceil(dp[i - 1][skips] + distance / speed - epsilon))</pre>

// Initialize all values to a very high number, interpreted as 'infinity'. vector<vector<double>> dp(numDistances + 1, vector<double>(numDistances + 1, 1e20)); // Base case: the time to reach the starting point with 0 skips is 0. dp[0][0] = 0;

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return -1;

C++ Solution

public:

class Solution {

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                     // If we decide to skip a resting time period.
                     if (j > 0) {
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                         dp[i][j] = min(dp[i][j], dp[i - 1][j - 1] + static_cast<double>(distances[i - 1]) / speed);
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             // Look for the smallest number of skips needed to arrive before or exactly at the prescribed time.
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             for (int j = 0; j <= numDistances; ++j) {</pre>
                 if (dp[numDistances][j] <= hoursBefore + eps) {</pre>
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                     return j; // The minimum number of skips required.
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             // If it is not possible to arrive on time, return -1.
 41
             return -1;
 42
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    };
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Typescript Solution
     function minSkips(distances: number[], speed: number, hoursBefore: number): number {
         // Number of road segments
         const numSegments = distances.length;
  5
         // Create a 2D array to record the minimum time needed to skip certain number of rests
         const minTime = Array.from({ length: numSegments + 1 },
  6
                                    () => Array.from({ length: numSegments + 1 },
                                    () => Infinity));
  8
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 10
         // Base case: starting with no distance and no skips, so time is 0
 11
         minTime[0][0] = 0;
 12
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         // Small epsilon value to avoid precision issues with floating point numbers
 14
         const eps = 1e-8;
 15
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         // Iterate through each segment
 17
         for (let i = 1; i <= numSegments; ++i) {</pre>
             // Calculate the minimum time required with available number of skips
 18
             for (let j = 0; j <= i; ++j) {
 19
                 // If we do not skip the current rest, use ceil to round to the next integer if necessary
 20
                 if (j < i) {
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 22
                     minTime[i][j] = Math.min(minTime[i][j],
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                                              Math.ceil(minTime[i - 1][j] + distances[i - 1] / speed - eps));
 24
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                 // If we can skip, use the exact value (no need to round)
 27
                 if (j) {
 28
                     minTime[i][j] = Math.min(minTime[i][j],
 29
                                              minTime[i - 1][j - 1] + distances[i - 1] / speed);
```

Time and Space Complexity The time complexity of the provided code is $0(n^3)$, where n is the length of the dist array. This is because there are three nested

for (let j = 0; j <= numSegments; ++j) {</pre>

// Check the minimum number of skips needed to reach within hoursBefore

return j; // Returns the minimum number of skips needed

if (minTime[numSegments][j] <= hoursBefore + eps) {</pre>

// If impossible to reach within hoursBefore, return -1

i+1, and the other considers two possible scenarios for each j (either skipping or not skipping). Each operation inside the innermost loop is 0(1), but since the loops are nested, the total time complexity scales cubically.

loops: the outermost loop iterating through each element in dist, and two inner loops, where one loop iterates through j from 0 to

The space complexity of the code is $0(n^2)$ because of the 2D list f that has dimensions n+1 by n+1. This list stores the minimum time required to reach each point with a given number of skips. Since it needs to hold a value for every combination of distances and skips, the space required grows quadratically with the number of distances.