



**Problem Description** 

characters of the string. Note that a subsequence maintains the original order of characters but does not necessarily include all characters. Importantly, if the solution is a very large number, it should be returned modulo 10^9 + 7 to keep the number within manageable bounds. This modular operation ensures that we deal with smaller numbers that are more practical for computation and comparison.

Given a string s, the task is to calculate the total number of distinct non-empty subsequences that can be formed from the

### Intuition

down into simpler subproblems. The key insight is to build up the number of distinct subsequences as we iterate through each character of the given string.

We maintain an array dp of size 26 (to account for each letter of the alphabet) which keeps track of the contribution of each

The intuition for solving this problem lies in dynamic programming - a method used for solving complex problems by breaking them

character towards the number of distinct subsequences so far. The variable ans stores the total count of distinct subsequences at any given point.

As we traverse the string:

• We calculate the index i corresponding to the character c (by finding the difference between the ASCII value of c and that of a).

- The variable add is set to the difference between the current total number of subsequences ans and the old count of subsequences ending with the character c (dp[i]). We add 1 to this because a new subsequence consisting of just the character
- c can also be formed.
  The ans is updated to include the new subsequences introduced by including the character c. The new ans is also taken modulo
  10^9 + 7 to handle the large numbers.
- The count of subsequences ending with the character c (dp[i]) is incremented by add to reflect the updated state.

  This approach ensures that each character's contribution is accounted for exactly once, and by the end of the iteration, ans contains
- the count of all possible distinct subsequences modulo 10^9 + 7.

Solution Approach

The implementation of the solution is fairly straightforward once we've understood the intuition behind it. This problem employs

#### 1. Initialize the Modulus and DP Array:

○ We use a modulus mod set to 10\*\*\*9 + 7 to ensure we manage the large numbers effectively by returning the number of

dynamic programming and a single array to keep track of the contributing counts. Here's the breakdown of the approach:

the count of subsequences that end with a particular character.

subsequences modulo this value.

- 2. Iterate Over the String:
- For each character c in the string s, we do the following steps:
   Determine the Index for c:

The data structure dp is an array initialized to size 26 (representing the English alphabet) with all zeroes. This array will store

- We calculate an index i by taking the ASCII value of the character c, subtracting the ASCII value of 'a' from it (ord(c) -
- ord('a')). This gives us a unique index from 0 to 25 for each lowercase letter of the alphabet.

  4. Calculate the Additive Contribution:
- We add one to add to account for the subsequence consisting solely of the new character c.

  5. Update the Total Count of Subsequences:

   Update ans by adding the new contribution from the character c. Applying modulo mod here ensures we handle overflow and

Compute add, which will determine how much the current character c will contribute to the new subsequences count. It is

determined by the current total of distinct subsequences ans minus the previous count stored in dp[i] for that character c.

o Increase the count in dp[i] by the value of add. This means that any subsequences that now end with the current character

large numbers.

6. Update the DP Array:

Using this method, we build up the solution incrementally, considering the influence of each character on the subsequences. The reason we have to subtract the old count of subsequences for the character c before adding it again (after increasing with add) is to

performing O(1) operations for each.

Example Walkthrough

The complexity of this solution is O(n), where n is the length of the string since we go through every character of the string once,

1. Initialize the Modulus and DP Array:

We set mod to 10^9 + 7. Our dp array, which has 26 elements for each letter of the English alphabet, is initialized to zeroes.

#### We begin iterating through the string "aba" character by character.

2. Iterate Over the String:

3. First Character - 'a':

Determine the Index for 'a': We calculate the index for 'a' as 0 (since 'a' - 'a' = 0).

To illustrate the solution approach, let's go through a small example using the string "aba".

c include the old subsequences plus any new subsequences formed due to adding c.

ensure that we do not double-count subsequences already accounted for by previous appearances of c.

add = ans (initially 0) - dp[0] + 1 = 0 - 0 + 1 = 1.

4. Second Character - 'b':

- Update the Total Count of Subsequences: We set ans = ans + add = 0 + 1 = 1 (the subsequences are now "" and "a").
   Update the DP Array: We update dp[0] to dp[0] + add = 0 + 1 = 1.
- Determine the Index for 'b': The index for 'b' is 1 ('b' 'a' = 1).
   Calculate the Additive Contribution: The current total count of distinct subsequences, ans, is 1. add = ans dp[1] + 1 = 1

Calculate the Additive Contribution: Since this is the first character, and there are no previous subsequences, we calculate

Update the Total Count of Subsequences: Now ans = ans + add = 1 + 2 = 3 (the subsequences are "", "a", "b", and "ab").

Calculate the Additive Contribution: We know ans is 3, and since we've encountered 'a' before, we subtract its previous

Determine the Index for 'a': The index is still 0.

Update the DP Array: We update dp[1] to dp[1] + add = 0 + 2 = 2.

- 0 + 1 = 2 (which corresponds to new subsequences "b" and "ab").

contribution from ans and add 1: add = ans - dp[0] + 1 = 3 - 1 + 1 = 3 (these are new subsequences: "a", "ba", and "aba").

5. Third Character - 'a' (again):

• Update the Total Count of Subsequences: The new ans will be ans + add = 3 + 3 = 6 (the subsequences now are "", "a", "b", "ab", "ba", "aa", and "aba"; note that we don't count subsequences like "aa" as distinct since the order must be maintained).

Update the DP Array: We set dp[0] to dp[0] + add = 1 + 3 = 4.

we would apply the modulo operation to ensure we obtain a result within the bounded range.

This walkthrough demonstrates how the algorithm incrementally computes the count of distinct subsequences using dynamic programming and efficient arithmetic operations, handling each character's contribution exactly once.

At the end of this process, the final answer for the total count of distinct non-empty subsequences is 6. However, if ans were larger,

# Define the modulo value to handle large numbers
MOD = 10\*\*9 + 7

# Initialize an array to keep track of the last count of subsequences
# ending with each letter of the alphabet

# # (which we have already counted with the current character) plus 1 for the character itself added\_subseq = total\_count - last\_count[index] + 1 # Update the total count of distinct subsequences total\_count = (total\_count + added\_subseq) % MOD

Python Solution

def distinctSubseqII(self, s: str) -> int:

# Initialize the total count of distinct subsequences

# Get the index of the current character in the alphabet (0-25)

# Calculate how many new subsequences are added by this character:

# Update the last count of subsequences for the current character

last\_count[index] = (last\_count[index] + added\_subseq) % MOD

# It is total\_count (all previous subsequences) minus last\_count[index]

# Iterate over each character in the string

index = ord(char) - ord('a')

 $last_count = [0] * 26$ 

total\_count = 0

for char in s:

class Solution:

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           # Return the total count of distinct subsequences
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           return total_count
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Java Solution
1 class Solution {
       private static final int MOD = (int) 1e9 + 7; // Modulus value for handling large numbers
       public int distinctSubseqII(String s) {
           int[] lastOccurrenceCount = new int[26]; // Array to store the last occurrence count of each character
           int totalDistinctSubsequences = 0; // Variable to store the total count of distinct subsequences
           // Iterate through each character in the string
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           for (int i = 0; i < s.length(); ++i) {</pre>
9
10
               // Determine the alphabet index of current character
               int alphabetIndex = s.charAt(i) - 'a';
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               // Calculate the number to add. This number represents the new subsequences that will be formed by adding the new charact
               // Subtract the last occurrence count of this character to avoid counting subsequences formed by prior occurrences of thi
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               // And add 1 for the subsequence consisting of the character itself.
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               int newSubsequences = (totalDistinctSubsequences - lastOccurrenceCount[alphabetIndex] + 1 + MOD) % MOD;
17
               // Update the totalDistinctSubsequences by adding newSubsequences
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               totalDistinctSubsequences = (totalDistinctSubsequences + newSubsequences) % MOD;
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               // Update the last occurrence count for this character in the lastOccurrenceCount array
22
               lastOccurrenceCount[alphabetIndex] = (lastOccurrenceCount[alphabetIndex] + newSubsequences) % MOD;
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           // Since the result can be negative due to the subtraction during the loop,
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           // we add MOD and then take the modulus to ensure a non-negative result
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           return (totalDistinctSubsequences + MOD) % MOD;
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```

## const int MODULO = 1e9 + 7; // Method to calculate the number of distinct subsequences in the string `s`. int distinctSubseqII(string s) { vector<long> lastOccurrence(26, 0): // Array to store the last occurrence

C++ Solution

1 class Solution {

2 public:

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vector<long> lastOccurrence(26, 0); // Array to store the last occurrence contribution for each character
           long totalCount = 0; // Total count of distinct subsequences
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           // Loop through each character in the string
           for (char& c : s) {
               int index = c - 'a'; // Map character 'a' to 'z' to index 0 to 25
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               long additionalCount = (totalCount - lastOccurrence[index] + 1 + MODULO) % MODULO; // Calculate the additional count for
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               totalCount = (totalCount + additionalCount) % MODULO; // Update the total count
               lastOccurrence[index] = (lastOccurrence[index] + additionalCount) % MODULO; // Update the last occurrence contribution fo
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           return (int)totalCount; // Return the total count of distinct subsequences as an integer
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21 };
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Typescript Solution
   function distinctSubseqII(s: string): number {
       const MODULO: number = 1e9 + 7; // A constant for the modulo operation to prevent overflow
       const lastOccurrence = new Array<number>(26).fill(0); // Store the count of distinct subsequences ending with each letter
       // Iterate over each character in the string
       for (const char of s) {
           const charIndex: number = char.charCodeAt(0) - 'a'.charCodeAt(0); // Map 'a' to 0, 'b' to 1, etc.
```

### // Return the sum of all distinct subsequences modulo the defined constant to avoid overflow return lastOccurrence.reduce((runningTotal, currentValue) => (runningTotal + currentValue) % MODULO, 0);

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// Calculate the number of new distinct subsequences ending with the current character
// It is the sum of all distinct subsequences seen so far plus 1 (for the char itself)
lastOccurrence[charIndex] = lastOccurrence.reduce((runningTotal, currentValue) =>
(runningTotal + currentValue) % MODULO, 0) + 1;

## Time Complexity

Time and Space Complexity

The provided code computes the count of distinct subsequences in a string using dynamic programming.

alphabet). The time complexity is therefore O(N), where N is the length of the string s.

space does not scale with the input size but is a constant size due to the fixed alphabet size.

## The key operation is iterating over each character in the input string s. For each character, the algorithm performs a constant amount of work; it updates ans and modifies an element in the dp array, which is of fixed size 26 (corresponding to the lowercase English

Space Complexity

The space complexity of the algorithm is defined by the space needed to store the dp array and the variables used. The dp array requires space for 26 integers, regardless of the length of the input string. Hence, the space complexity is O(1) since the required