1588. Sum of All Odd Length Subarrays

Prefix Sum Math Easy

Problem Description

subarray is a contiguous part of the original array that has an odd number of elements. For example, in the array [1, 2, 3, 4], the odd-length subarrays include [1], [2], [3], [4], [1, 2, 3], [2, 3, 4], and the entire array itself [1, 2, 3, 4]. The goal is to calculate the sum of all the elements from all such subarrays and return this sum.

The given problem entails finding the sum of all odd-length subarrays from a given array of positive integers. An odd-length

The intuition behind the solution is to consider each element of the array as a potential starting point of an odd-length subarray

Intuition

to the subarray until we reach the end of the array. We check if the length of the current subarray is odd, and if it is, we add the sum of the current subarray to our answer. As we iterate through the array arr of size n, we initialize a variable ans to store the sum of odd-length subarrays. For each element arr[i], we initialize a subarray sum s to track the sum of elements starting from arr[i]. Then for each element arr[j]

and expand the subarray one element at a time as we iterate through the array. For each starting element, we add the elements

to the right of arr[i] (including i), we add to s. After each addition, we check if the subarray from arr[i] to arr[j] has an odd length by checking if the length (j - i + 1) is odd (using bitwise & 1 to check for oddness). If it's odd, we add the current sum s to our overall answer ans. By systematically expanding and checking each potential subarray based on its starting point, we ensure that we consider all

possible odd-length subarrays. The iterative approach is straightforward and does not involve complex data structures or algorithms. Solution Approach

In the implementation of the solution, the chosen approach is a brute force method where two nested loops are utilized to

Initialize an accumulator variable ans to 0 which will hold the final sum of all odd-length subarrays.

considered.

Determine the length n of the array arr.

Start the first loop with the variable i iterating from 0 up to n-1. This loop will help us select the starting element of each

Start the second nested loop with the variable j iterating from i up to n-1. This loop will extend the subarray one element

subarray. Inside the first loop, initialize a variable s to 0. This variable will keep track of the sum of the current subarray being

calculate the sum of all possible odd-length subarrays. Here's the step-by-step process:

- at a time from the starting index i. Inside the nested loop, add the current element arr[j] to the sum s.
- Immediately after adding to s, check if the subarray from i to j is of odd length. This check is performed using the bitwise
- AND operation (j i + 1) & 1. If (j i + 1) & 1 equals 1, this means the length of the subarray (j i + 1) is odd. If the subarray length is found to be odd, increment ans by the current sum s.

The nested loop ends after reaching the final element, and all possible subarrays starting at index i have been considered.

While this solution is not the most optimized, it is easy to understand and implement. The time complexity for this approach is

- Repeat the process for every starting index i until all starting positions have been accounted for.
- O(n^2), which is acceptable when n is not excessively large. It avoids the use of any additional complex data structures maintaining the simplicity of implementation. No patterns or algorithms other than straightforward conditional statements and
- **Example Walkthrough**

Let's walk through the brute force solution approach using a small example array: [1, 2, 3]. Initialize ans to 0. This variable will store our final answer. The length n of the array [1, 2, 3] is 3. Start the first loop with i. For i = 0, we will look at subarrays starting with the element 1.

Inside the loop for i = 0, initialize s to 0. This is where we'll accumulate the sum of elements for our current subarray.

We check whether the length of the subarray (j - i + 1) is odd, which is 1 in this case. Since (1 & 1) == 1, the condition

We increment j to 1, and now consider the subarray [1, 2]. Adding arr[j] = 2 to s gives us s = 3. However, (2 - 0 + 1)

The second nested loop starts with j = i. For j = 0 which means our subarray is [1]. We add arr[j], which is 1 to s,

is true.

arithmetic operations are used.

resulting in s = 1.

yield an ans value of 12, accounting for the sums of subarrays [1], [2], [3], [1, 2, 3].

Loop over each element from the start_index to the end of the array

If it's odd, add the current subarray sum to total_sum

1) & 1 == 0, the length 3 is not odd, thus we do nothing.

def sumOddLengthSubarrays(self, arr: List[int]) -> int:

for end index in range(start index, n):

if subarray length % 2 == 1:

Add the current element to subarray_sum

Check if the length of the subarray is odd

// Calculate the sum of all odd-length subarrays in the given array.

int totalSum = 0; // Initialize the total sum of odd-length subarrays.

int subarraySum = 0; // Initialize the sum for the current subarray.

// Extend the subarray from the start index to the end of the array.

// ...then add the current subarray sum to the total sum.

return totalSum; // Return the accumulated sum of all odd-length subarrays.

// If the length of the current subarray (endIndex - startIndex + 1) is odd...

for (int endIndex = startIndex; endIndex < n; ++endIndex) {</pre>

// Add the current element to the subarray sum.

if ((endIndex - startIndex + 1) % 2 == 1) {

const arrLength = arr.length; // Store the length of the input array.

let totalSum = 0; // Initialize total sum of all odd length subarrays.

Calculate the length of the current subarray

subarray_length = end_index - start_index + 1

Check if the length of the subarray is odd

If it's odd, add the current subarray sum to total_sum

if subarray length % 2 == 1:

result = solution.sumOddLengthSubarrays([1,4,2,5,3])

total_sum += subarray_sum

Return the total sum of all odd length subarrays

int n = arr.size(); // Get the size of the array.

for (int startIndex = 0; startIndex < n; ++startIndex) {</pre>

// Traverse the array starting from each element.

subarraySum += arr[endIndex];

totalSum += subarraySum;

function sumOddLengthSubarrays(arr: number[]): number {

int sumOddLengthSubarravs(std::vector<int>& arr) {

- Because our subarray length is odd, we increment ans by s, so ans = ans + 1 = 1.
- Increment j to 2 and our subarray becomes [1, 2, 3]. We add arr[j] = 3 to s to get s = 6. The subarray length is 3 which is odd: (3 - 0 + 1) & 1 == 1. We add 6 to ans, making ans = 1 + 6 = 7.
- We've considered all elements for the starting index i = 0. Now we increment i to 1 and repeat the process for the new starting element, 2.

Through this repeated process, we would continue iterating over all starting indices, finding all possible odd-length subarrays,

and summing their elements to ans. The final value of ans after considering all starting points would be the answer to our

problem: the sum of all elements in all odd-length subarrays of the array [1, 2, 3]. Using this method with our example would

Solution Implementation **Python**

Initialize the total_sum to accumulate the sum of all odd length subarrays total_sum = 0 # Get the length of the array n = len(arr)# Loop over each element in the array as the starting point of the subarrays for start index in range(n): # Initialize subarray_sum to hold the sum of the current subarray

subarray_sum += arr[end_index] # Calculate the length of the current subarray subarray_length = end_index - start_index + 1

subarray_sum = 0

from typing import List

class Solution:

```
total_sum += subarray_sum
        # Return the total sum of all odd length subarrays
        return total_sum
# Example usage:
# solution = Solution()
# result = solution.sumOddLengthSubarrays([1,4,2,5,3])
# print(result) # Output would be 58
Java
class Solution {
    public int sumOddLengthSubarrays(int[] arr) {
        int n = arr.length; // The length of the input array
        int totalSum = 0; // This will hold the sum of all odd-length subarrays
        // We iterate over each element of the array as the start point for our subarrays
        for (int startIndex = 0; startIndex < n; ++startIndex) {</pre>
            int subarraySum = 0; // Holds the sum of the current subarray
            // We increase the end point of our subarray one element at a time
            for (int endIndex = startIndex; endIndex < n; ++endIndex) {</pre>
                // Add the current element to our subarray sum
                subarraySum += arr[endIndex];
                // Check if the length of the current subarray is odd
                if ((endIndex - startIndex + 1) % 2 == 1) {
                    // If it's odd, add the current subarray sum to the total sum
                    totalSum += subarraySum;
        // Return the total sum of all odd-length subarrays
        return totalSum;
```

};

C++

public:

#include <vector>

class Solution {

TypeScript

```
// Iterate through each element of the array.
    for (let startIndex = 0; startIndex < arrLength; ++startIndex) {</pre>
        let subarraySum = 0; // Initialize sum for the current subarray.
        // Form subarrays starting with the element at startIndex.
        for (let endIndex = startIndex; endIndex < arrLength; ++endIndex) {</pre>
            subarraySum += arr[endIndex]; // Add the current element to the subarray sum.
            // Check if the length of the current subarray is odd.
            if ((endIndex - startIndex + 1) % 2 === 1) {
                totalSum += subarraySum; // If it's odd, add the subarray's sum to the total sum.
   return totalSum; // Return the total sum of all odd length subarrays.
from typing import List
class Solution:
   def sumOddLengthSubarrays(self, arr: List[int]) -> int:
       # Initialize the total_sum to accumulate the sum of all odd length subarrays
        total_sum = 0
       # Get the length of the array
       n = len(arr)
       # Loop over each element in the array as the starting point of the subarrays
        for start index in range(n):
            # Initialize subarray_sum to hold the sum of the current subarray
            subarray_sum = 0
           # Loop over each element from the start_index to the end of the array
            for end index in range(start index, n):
                # Add the current element to subarray_sum
                subarray_sum += arr[end_index]
```

The provided Python function sum0ddLengthSubarrays computes the sum of elements of all odd length subarrays of the given array arr. Let's analyze both time complexity and space complexity:

the sum precisely (n*(n+1))/2 times.

Thus, the time complexity is $0(n^2)$.

print(result) # Output would be 58

Time and Space Complexity

return total sum

Example usage:

solution = Solution()

The time complexity of the code is determined by the two nested loops. The outer loop runs from ∅ to n-1, where n is the length of the array. The inner loop starts from the current index of the outer loop \mathbf{i} and goes to $\mathbf{n-1}$.

Since for every element in the array, we are iterating over all subsequent elements (progressively fewer as i increases), the number of operations can be approximated by the sum of an arithmetic series.

Time Complexity

The total number of operations is close to 1 + 2 + ... + n, which is given by the formula (n*(n+1))/2. But since we are only adding to the sum for odd indices, we can estimate roughly half of these operations are meaningful, giving us an estimate of (n*

(n+1))/4. However, the presence of odd or even length subarrays does not change the fact that each element is considered in

Space Complexity

The space complexity is determined by the amount of additional memory used by the algorithm, which is independent of the size of the input array arr. Only a fixed number of individual integer variables ans, n, s, i, and j are used.

No additional data structures are dependent on the input size, hence the space complexity is 0(1), that is, constant.