2336. Smallest Number in Infinite Set Design Hash Table Medium Heap (Priority Queue) Leetcode Link

# **Problem Description**

all positive integers starting from 1 and extending to infinity. The class has to provide two operations: 1. popSmallest(): This operation should remove the smallest number currently in the set and return it. The initial call to this method

In this LeetCode problem, we are required to implement a class called SmallestInfiniteSet. This class simulates a set that contains

- would return 1, the second call would return 2, and so on. After a number is popped, it is no longer present in the set unless it is added back. 2. addBack(num): This operation allows one to add a number back into the set. However, a number can be added back only if it has
- The challenge is to code these operations efficiently, keeping in mind that there can be an infinite number of integers.

The solution to this problem relies on maintaining a auxiliary set to keep track of the numbers that have been popped. We can call

Intuition

been previously popped from the set and is not currently present.

## this auxiliary set "blacklist" or black in the code sample given. When popSmallest() is called, we start from 1 and check if that

check again until we find the smallest number not in the black set. When addBack() is called with a number argument, we remove it from the black set, which represents adding it back into the set of available numbers to be popped. This is because a number can only be re-added if it has been removed before, and removing from the black will allow popSmallest() to find it again as the smallest available number.

number is in the black set. If it is not, we pop it (remove and return) and add it to the black set. If it is, we increment the number and

This approach is intuitive in that it treats the infinite set of positive integers as an implicit list that we only modify by noting which elements are currently not in the set (which are in black). It uses set operations which are typically O(1) for existence check and removal, making the operations efficient.

Solution Approach Let's discuss the implementation details of the SmallestInfiniteSet class and walk through each method provided in the solution: Initializer \_\_init\_\_(self):

## the class is created.

For our SmallestInfiniteSet class:

In Python, the \_\_init\_\_ method serves as an initializer or a constructor for a class. It is automatically invoked when a new instance of

## This initializer sets up an empty set called self.black. This set will hold all numbers that have been popped and removed from the

infinite set of positive integers.

is:

self.black = set()

complexity of O(1). Method popSmallest(self) -> int:

The popSmallest method is used to pop and return the smallest integer from the infinite set. The pseudo-algorithm for this method

Data Structure: set() is used because it allows fast addition, removal, and membership check operations with an average time

1. Start with i = 1 since 1 is the smallest positive integer. 2. Increment i while i is in self.black. This is because if i is in self.black, it means that i has been previously popped. 3. Once an i is found that is not in self.black, add it to self.black and return it.

#### while i in self.black: self.black.add(i)

def popSmallest(self) -> int:

return i

 Algorithm: Linear search to find the smallest integer not in self.black. Pattern Used: Iteration starting from 1 and incrementing until an integer not in self.black is found.

• Data Structure: We use the discard method of the set, which removes num if present in self.black. This operation does not raise

The situation where addBack is called with a number that has never been popped or is already in the set doesn't change the

These methods collectively allow us to efficiently simulate the infinite set operations of popping the smallest element and adding

Let's use a small example to illustrate how the SmallestInfiniteSet class works according to the solution approach. Assume we

Method addBack(self, num: int) -> None: The addBack method is meant to add a number back into the set if it isn't currently in the set:

def addBack(self, num: int) -> None:

an error even if num is not present.

self.black.discard(num)

numbers back into the infinite set.

Call popSmallest() four times.

Call addBack(2).

Step 1

Step 2

Step 3

Step 4

Pattern Used: Conditional removal, letting the set data structure handle the existence check implicitly.

create an instance of SmallestInfiniteSet and then perform a series of operations:

We first instantiate our SmallestInfiniteSet class. The black set is initialized as empty.

self.black set, as per the problem's instructions.

This method ensures that we always return the next smallest number, as per the requirement of the problem.

Example Walkthrough

- 3. Call popSmallest() two more times. Let's go step by step:
- We call popSmallest() for the first time. Since black is empty, 1 is not in black and is returned. black is now {1}.

we return 2, and black becomes {1, 2, 3, 4}.

We call popSmallest() for the second time. Here i starts at 1 again but since 1 is in black, increment i to 2. Now 2 is not in black, so 2 is returned and black becomes {1, 2}.

black becomes {1, 2, 3}.

Now, we call addBack(2). This removes 2 from black. Therefore, black is now {1, 3, 4}.

# Initialize an empty set to keep track of popped elements

# Starting from 1, find the smallest integer not yet popped

# If the number is in the popped elements, remove it to make it available again

# Add the found integer to the popped elements set

#### We call popSmallest() for the fourth time. i starts at 1, but numbers 1, 2, and 3 are in black, so we increment i to 4. Four is returned and black becomes {1, 2, 3, 4}.

Step 6

Step 5

Step 7 We call popSmallest() again. We start at 1, which is in black. We find that 2 is now not in black (because we just added it back), so

We call popSmallest() for the third time. i starts at 1, but both 1 and 2 are in black, so we increment i to 3. Three is returned and

## Step 8 One final call to popSmallest() starts at 1 again, but we must increment until we find 5, which is not in black. We return 5 and black

becomes {1, 2, 3, 4, 5}.

Python Solution

1 class SmallestInfiniteSet:

self.popped\_elements = set()

while smallest in self.popped\_elements:

self.popped\_elements.remove(num)

// A HashSet to store numbers that have been popped.

private Set<Integer> poppedNumbers = new HashSet<>();

self.popped\_elements.add(smallest)

# Return the smallest integer

def addBack(self, num: int) -> None:

if num in self.popped\_elements:

def popSmallest(self) -> int:

smallest += 1

smallest = 1

return smallest

elements have been 'popped' and are not currently available unless added back. By incrementing the minimal candidate and checking against black, we ensure that popSmallest() always returns the smallest available integer, and by using discard in addBack, we maintain an efficient model of this infinite integer set.

This walkthrough exemplifies how an implied infinite set of positive integers can be manipulated using a black set to track which

20 # Note that if the number is not in the popped elements, no action is taken 22 # Example of how to use the SmallestInfiniteSet class 23 # obj = SmallestInfiniteSet() # Instantiate the class 24 # param\_1 = obj.popSmallest() # Pop the smallest element available 25 # obj.addBack(num) # Add back a specific number into the set of available numbers 26

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**Java Solution** 

import java.util.Set;

import java.util.HashSet;

// Constructor

class SmallestInfiniteSet {

```
public SmallestInfiniteSet() {
           // Nothing to initialize since HashSet is already initialized.
TO
11
12
13
       // Method to pop the smallest number that has not been popped yet.
       public int popSmallest() {
14
15
           // Starting from 1, as it's the smallest positive integer.
           int smallest = 1;
16
           // Loop over the set to find the smallest non-popped number (the ones not in poppedNumbers).
           while (poppedNumbers.contains(smallest)) {
               // If current number is in the set, increase it to check the next one.
19
20
               smallest++;
21
22
           // Once the smallest number is found, add it to the set to indicate it has been popped.
           poppedNumbers.add(smallest);
           // Return the smallest number that hasn't been popped before.
24
25
           return smallest;
26
27
28
       // Method to add back a number to the set of available numbers.
       public void addBack(int num) {
29
           // Remove the specified number from the set of popped numbers.
           poppedNumbers.remove(num);
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33 }
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35
    * The SmallestInfiniteSet object will be instantiated and called as follows:
    * SmallestInfiniteSet obj = new SmallestInfiniteSet();
    * int param_1 = obj.popSmallest();
                                          // Pops the smallest available number
    * obj.addBack(num);
                                          // Adds back a number to the available set
40
    */
41
```

// Class representing an infinite set with functionality to get the smallest element and add elements back

// 'removedNumbers' holds all numbers that have been popped from the set

#### // Constructor does not need to initialize anything for this implementation. // An alternative could be initializing an internal data structure if needed. 13 14 15 16

private:

10 public:

C++ Solution

1 #include <unordered\_set>

5 class SmallestInfiniteSet {

SmallestInfiniteSet() {

unordered\_set<int> removedNumbers;

2 using namespace std;

```
// Function to pop the smallest number from the set that hasn't been popped yet
17
       int popSmallest() {
           int current = 1; // We start from 1 as it is the smallest possible positive integer for the infinite set
           // Loop to find the first number that hasn't been removed yet
19
           while (removedNumbers.count(current)) {
20
               current++; // If current number is in 'removedNumbers', increment and check the next
21
22
           // Once we find the smallest number not in 'removedNumbers', add it to the set to mark it as removed
           removedNumbers.insert(current);
24
25
           return current; // Return the smallest number
26
27
28
       // Function to add back a number to the set, making it available to be popped again
       void addBack(int num) {
29
           // Erase the number from 'removedNumbers' to mark it as not removed
31
           removedNumbers.erase(num);
32
33 };
34
  // Example usage:
36 // SmallestInfiniteSet* obj = new SmallestInfiniteSet();
37 // int param_1 = obj->popSmallest();
   // obj->addBack(num);
39
Typescript Solution
 1 // Initialize a variable to store the smallest available numbers,
  // using an array to represent a set of initialized values to true.
    let smallestAvailable: boolean[] = new Array(1001).fill(true);
   /**
    * Retrieves and removes the smallest number available from the set.
    * @returns {number} The smallest number that was available.
    */
    function popSmallest(): number {
       for (let i = 1; i <= 1001; i++) {
           if (smallestAvailable[i]) {
11
               smallestAvailable[i] = false; // Mark the number as unavailable.
               return i; // Return the number that's now popped out of the set.
13
```

14 15 return -1; 16 17 } 18 19 /\*\* \* Adds a number back into the set if it's not already marked as available.

#### 26 27 } 28

Time and Space Complexity

\* @param {number} num - The number to add back to the set. 22 \*/ function addBack(num: number): void { if (num >= 1 && num <= 1000 && !smallestAvailable[num]) {</pre> 24

smallestAvailable[num] = true; // Mark the number as available again.

The given Python code defines a class SmallestInfiniteSet that maintains a set of integers from which the smallest number can be

"popped" (i.e., returned and removed from the set) and to which specific numbers can be "added back" to the set if they have been

## that have been added to the black set. In the worst-case scenario, the method iterates through all elements that have been added to the set to find the smallest one that is not in the set.

previously removed.

**Time Complexity** 

2. addBack Method: The time complexity for addBack is 0(1). This is because the discard method of a set in Python, which is used to remove an element if it exists in the set, operates in constant time.

1. popSmallest Method: The time complexity for popSmallest is O(n), where n is the number of consecutive integers starting from 1

Space Complexity The space complexity of the entire class is  $0 \, (m)$ , where m is the number of unique elements that have been popped and not added

back. The black set will grow as more unique elements are popped and retained in the set. It will not grow larger than the number of elements that have been popped and not added back, hence the space complexity of O(m).