548. Split Array with Equal Sum

Subarray 2: Elements from index i+1 to j−1 (both inclusive).

Prefix Sum

Problem Description

In this problem, we are given an array of integers, nums, and we need to determine if there exists a triplet of indices (i, j, k) in

Hard

• Indices i, j, and k must maintain the sequence 0 < i < j < k < n-1, where n is the length of the array. The sum of elements in four subarrays is equal. The subarrays are: ○ Subarray 1: Elements from index 0 to i-1 (both inclusive).

the array that meet certain conditions. Specifically, the conditions for the indices are:

 Subarray 3: Elements from index j+1 to k−1 (both inclusive). \circ Subarray 4: Elements from index k+1 to the end of the array (index n-1). A subarray (1, r) represents the sequence of elements in the array nums from the 1th element to the rth element, inclusive.

The aim is to return true if at least one such triplet (i, j, k) exists, and false otherwise.

Intuition

The intuition behind the solution is to find a way to efficiently determine if the sum of elements in the given subarrays are equal without recalculating them each time for different values of i, j, and k. To do this, we can make use of prefix sums and a set.

Here is how we could approach the problem:

• First, we can calculate a prefix sum array s for the given nums array. The prefix sum array contains the sum of all numbers up to and

Prefix Sum Computation:

including the ith index of nums. This helps us calculate the sum of any subarray in constant time. **Determining Equal Subarray Sums:** ∘ To find the correct index j, we need to ensure that we have enough space on either side for indices i and k to exist. Therefore, we scan

For each j , we establish two loops:

for j starting from index 3 to n - 3. If j is too close to the start or end, there can't be four subarrays with equal sums. ■ An inner loop over i, which ranges from 1 to j - 1, looking for subarrays that could be equal in sum to the other subarrays.

■ We check if the sum of elements from 0 to i-1 is equal to the sum from i+1 to j-1. ■ When we find such an instance, we add the sum to a set seen as a potential candidate for the subarray sum.

Initialization and <u>Prefix Sum</u> Computation:

Exploring Potential Values for 1:

which is s[n] - s[k + 1].

satisfies all the conditions.

Returning the Result:

making it a much faster algorithm.

Consider the array nums with the following elements:

representing the sum of nums from index 0 to 2.

Exploring Potential Values for k for j = 3:

Example Walkthrough

8 elements.

Finding the Index j:

If they are equal, add the sum to the set seen.

At this point, return true since the required triplet exists.

■ An outer loop over k, which ranges from j + 2 to n - 1, looking for subarrays that could match the ones identified by i. • We check if the sum of elements from j+1 to k-1 is equal to the sum from k+1 to n-1. ■ If it is and the sum is already in seen, there exists at least one combination of i, j, k that satisfies all conditions, thus, we return true.

Checking for Match:

 If we exit both loops without finding such a triplet, then we conclude that no such triplet exists, and we return false. By implementing this approach, we avoid recalculating the sum for each subarray from scratch, which would otherwise result in a

much less efficient solution.

of the subarrays for each possible combination of (i, j, k) triplet. Here's a step-by-step walk-through of the implementation based on the provided solution code:

To implement the solution described in the intuition, we make use of a couple of important programming concepts: prefix sums

and hash sets. This enables us to have an efficient algorithm that can solve the problem without repeatedly computing the sums

o Initialize an array s with length n + 1 where n is the length of the input array nums. The s array is going to store the prefix sums of nums.

• Fill the s array with prefix sums, where s[i + 1] = s[i] + nums[i]. This means s[i] holds the total sum from the start of nums up to

(and including) index i-1.

Solution Approach

Finding the Index j: ∘ Iterate over possible values of j starting from index 3 to n - 3. The choice of starting from 3 ensures that there is space for at least two elements before j and ending at n-3 ensures there's space for at least two elements after j.

For each j, initialize an empty set seen. This set is used to store sums of subarrays that could potentially match with other subarrays.

■ Check if the sum of the subarray (0, i - 1) which is s[i], is equal to the sum of the subarray (i + 1, j - 1) which is s[j] - s[i + 1].

Loop through i which starts from 1 and goes up to j - 1, perform the following:

Exploring Potential Values for k: ○ Next, loop through k which starts from j + 2 and ends at n - 1, perform the following:

• If we finish both loops and haven't returned true, we determine that no such triplet exists, and therefore, we return false. This approach is efficient because we utilized the pre-computed prefix sum array to quickly access the sum of any subarray in

constant time. Additionally, by using the set to keep track of seen sums, we avoid redundant comparisons for each potential k,

■ Check if the sum of the subarray (j + 1, k - 1) which is s[k] - s[j + 1], is equal to the sum of the subarray (k + 1, n - 1)

■ If they are equal and the sum (the sum of the subarray (j + 1, k - 1)) exists in the seen set, we have found a triplet (i, j, k) that

nums = [1, 2, 1, 2, 1, 2, 1]Let's walk through the solution approach with this example: **Initialization and Prefix Sum Computation:**

• First, we initialize an array s for storing prefix sums with n + 1 elements, where n is the length of nums. In this case, n is 7, so s will have

• Then we compute the prefix sums. So the s array after prefix sum computation will be [0, 1, 3, 4, 6, 7, 9, 10]. For instance, s[4] = 6

• For k = 5, we check the sums: s[5] - s[4] = 7 - 6 = 1 and s[7] - s[6] = 10 - 9 = 1. They are equal, and 1 is in the seen set.

■ Having found a k such that the sum from j+1 to k-1 matches the sum from k+1 to n-1 and is also in seen, we have found a valid

This example illustrates how the intuition and approach to the problem can be used to efficiently find a triplet in the array that

 \circ We iterate over possible values of j from 3 to 4 (as n - 3 is 4 for this example). Exploring Potential Values for i for j = 3: • We initialize an empty set seen for j = 3. Loop through i which starts from 1 and goes up to 2 (j - 1):

• For i = 1, we check the sums: s[1] = 1 and s[3] - s[2] = 4 - 3 = 1. They are equal, so we add 1 to seen.

 \circ We loop through k which can only be 5 since it starts from j + 2 and ends at n - 1 for this j.

triplet (i, j, k) which is (1, 3, 5). We return true since we have found the required triplet.

Returning the Result:

meets the requirements.

from typing import List

n = len(nums)

Python

class Solution:

Solution Implementation

 In this case, we found at least one valid triplet that satisfies all the conditions. Hence, if we were to implement this example in code, the result would be true.

def splitArray(self, nums: List[int]) -> bool:

Initialize a prefix sum array with an extra position for simplicity

The main loop to check for split positions starting at index 3

Check for all possible splits in the first half

seen_sums.add(prefix_sum[left])

If we reach this point, no valid split was found

prefixSums[i + 1] = prefixSums[i] + nums[i];

// 'i' is the potential middle split point

for (int i = 1; i < j - 1; ++i) {

Set<Integer> seenSums = new HashSet<>();

seenSums.add(prefixSums[i]);

// Traverse through the array, starting from index 3 to n-4

// First pass to check possible sums from the left subarray

if (prefixSums[i] == prefixSums[j] - prefixSums[i + 1]) {

and ending at n-4 to ensure there are enough elements on both sides

If a valid split is found, add the sum to the set

Check for all possible splits in the second half of the array

Store sums that can be created from the first half of the array

if prefix sum[left] == prefix sum[mid] - prefix_sum[left + 1]:

// Array to store the prefix sums, one extra element for ease of calculations

Check if there is a valid split that matches any sum in 'seen sums'

and prefix_sum[n] - prefix_sum[right + 1] in seen_sums):

if (prefix sum[n] - prefix sum[right + 1] == prefix sum[right] - prefix_sum[mid + 1]

Get the length of the input array

 $prefix_sum = [0] * (n + 1)$

for mid in range(3, n - 3):

for left in range(1, mid - 1):

return True

int[] prefixSums = new int[n + 1];

// Calculate the prefix sums

for (int i = 0; i < n; ++i) {

for (int i = 3; i < n - 3; ++i) {

for (int i = 0; i < n; ++i) {

return true;

// with one element between these parts.

let n: number = nums.length;

for (let i = 0; i < n; ++i) {

function splitArray(nums: number[]): boolean {

// Calculate prefix sums for all elements.

prefixSum[i + 1] = prefixSum[i] + nums[i];

// Use a three-pointer approach to find the split points.

// Find all possible sums for the left section

seenSums.add(prefixSum[left]);

for (let left = 1; left < middle - 1; ++left) {</pre>

};

TypeScript

// Example usage:

class Solution:

from typing import List

n = len(nums)

return False

Time Complexity

Space Complexity

let nums: number[] = [1, 2, 1, 2, 1, 2, 1];

 $prefix_sum = [0] * (n + 1)$

for i, num in enumerate(nums):

for mid in range(3, n - 3):

seen_sums = set()

def splitArray(self, nums: List[int]) -> bool:

Get the length of the input array

prefixSum[i + 1] = prefixSum[i] + nums[i];

// Use a three-pointer approach to find the split points.

// Find all possible sums for the left section.

for (int left = 1; left < middle - 1; ++left) {</pre>

seenSums.insert(prefixSum[left]);

return false; // Return false if no such split is found.

// Find if there's a corresponding sum for the right section.

for (int right = middle + 2; right < n - 1; ++right) {

if (prefixSum[left] == prefixSum[middle] - prefixSum[left + 1]) {

&& seenSums.count(prefixSum[n] - prefixSum[right + 1])) {

// Function that determines if the array can be splitted into four parts with the same sum,

if (prefixSum[left] === prefixSum[middle] - prefixSum[left + 1]) {

// If a sum that can be the left section is found, add it to 'seenSums'.

if (prefixSum[n] - prefixSum[right + 1] == prefixSum[right] - prefixSum[middle + 1]

for right in range(mid + 2, n - 1):

seen_sums = set()

Compute the prefix sum array where prefix sum[i] represents # the sum of elements from nums[0] to nums[i-1] for i, num in enumerate(nums): prefix_sum[i + 1] = prefix_sum[i] + num

Java class Solution { public boolean splitArray(int[] nums) { int n = nums.length:

return False

```
// Second pass to check matching sums from the right subarray
            for (int k = i + 2; k < n - 1; ++k) {
                if (prefixSums[n] - prefixSums[k + 1] == prefixSums[k] - prefixSums[j + 1] && seenSums.contains(prefixSums[n] - prefi
                    return true; // Found a valid split
        // If no valid split is found
        return false;
C++
class Solution {
public:
    // Function that determines if the array can be split into four parts
    // with the same sum, with one element between these parts.
    bool splitArray(vector<int>& nums) {
        int n = nums.size();
        vector<int> prefixSum(n + 1, 0); // Initialize prefix sums array with an additional 0 at the start.
        // Calculate prefix sums for all elements.
```

for (int middle = 3; middle < n - 3; ++middle) { // middle is the middle cut, avoiding the first 2 and last 2 elements.

// If the sum for the right section equals one of the left section sums, return true for a successful split.

unordered_set<int> seenSums; // Store sums that we've seen which are candidates for the first section.

let prefixSum: number[] = new Array(n + 1).fill(0); // Initialize prefix sums array with an additional 0 at the start.

for (let middle = 3; middle < n - 3; ++middle) { // 'middle' is the middle cut, avoiding the first 2 and last 2 elements.

let seenSums: Set<number> = new Set<number>(); // Store sums that we've seen which are candidates for the first section.

```
// Find if there's a corresponding sum for the right section.
    for (let right = middle + 2; right < n - 1; ++right) {</pre>
        if (prefixSum[n] - prefixSum[right + 1] === prefixSum[right] - prefixSum[middle + 1]
            && seenSums.has(prefixSum[n] - prefixSum[right + 1])) {
            // If the sum for the right section equals one of the left section sums, return true for a successful split.
            return true;
return false; // Return false if no such split is found.
```

console.log(splitArray(nums)); // Output should be true or false depending on the array content.

Initialize a prefix sum array with an extra position for simplicity

Compute the prefix sum array where prefix sum[i] represents

The main loop to check for split positions starting at index 3

Check for all possible splits in the first half

seen_sums.add(prefix_sum[left])

and ending at n-4 to ensure there are enough elements on both sides

If a valid split is found, add the sum to the set

Check for all possible splits in the second half of the array

Store sums that can be created from the first half of the array

if prefix sum[left] == prefix sum[mid] - prefix_sum[left + 1]:

Check if there is a valid split that matches any sum in 'seen sums'

and prefix_sum[n] - prefix_sum[right + 1] in seen_sums):

if (prefix sum[n] - prefix sum[right + 1] == prefix sum[right] - prefix_sum[mid + 1]

The given Python function splitArray is designed to determine if an array can be split into four parts with equal sums. The

The third loop can be considered separately and again runs at most (n-j-2) iterations for each j. But this time, the check

2. The hash set seen, which in the worst-case scenario could store up to ((n/2)-2) sums (since only sums before j are considered and j starts

the sum of elements from nums[0] to nums[i-1]

prefix_sum[i + 1] = prefix_sum[i] + num

// If a sum that can be the left section is found, add it to 'seenSums'.

Time and Space Complexity

return True

for left in range(1, mid - 1):

for right in range(mid + 2, n - 1):

If we reach this point, no valid split was found

Looking at the nested loops, the first loop runs (n-6) times, where j ranges from 3 to (n-4). The second nested loop runs at most (j-2) times for each j. The worst-case scenario for the second loop would be when j is around n/2, which would yield roughly (n/2) iterations. Thus, the innermost condition is checked $0(n^2)$ times.

involves a hash set lookup, which is an 0(1) operation on average. In the worst case, this loop will also contribute to 0(n^2) iterations. Overall, the time complexity of the code is $O(n^2)$ due to the nested loops.

function uses a prefix sum array s to efficiently calculate the sums of subarrays.

The space complexity for this function is determined by the space required for: 1. The prefix sum array s, which contains (n+1) integers. This contributes 0(n) space complexity.

at 3). This also contributes 0(n) space complexity. Therefore, the overall space complexity of the function is O(n).