2556. Disconnect Path in a Binary Matrix by at Most One Flip Medium Depth-First Search Breadth-First Search Array Dynamic Programming

Matrix

Leetcode Link

Problem Description

(which the code doesn't handle explicitly).

(row, col), we can move to an adjacent cell to the right (row, col + 1) or below (row + 1, col) providing it contains a 1. The task is to determine whether we can make the matrix "disconnected" by flipping at most one cell's value, except for the cells at

The problem presents us with an m x n binary matrix, where 0 and 1 represent blocked and open cells, respectively. From any cell,

(0, 0) and (m - 1, n - 1). A disconnected matrix means there is no path from the start (0, 0) to the end (m - 1, n - 1).

Flipping a cell switches its value: if the cell was 1, it becomes 0, and if it was 0, it becomes 1. The challenge lies in deciding if it's

possible to disrupt any existing path with a single flip, assuming such a path exists. Intuition

The key intuition for this solution is to perform a Depth-First Search (DFS) from the starting cell (0, 0) two times.

then we proceed to the next step. Otherwise, if there is no such path, the grid is already disconnected, and we can return true early

After conducting the initial DFS, we mark the beginning and ending cells as open (if they aren't already), hoping to test whether forcing these cells open and disconnecting another cell can lead to a disconnected path. Therefore, another DFS is executed with these conditions.

Initially, we execute DFS to check if there exists a path from (0, 0) to (m - 1, n - 1) without flipping any cells. If such a path exists,

Here's the process: 1. Start by marking the current cell as visited (flipping from 1 to 0 to avoid revisiting). 2. If the end cell (m - 1, n - 1) is reached, we've found a path.

6. Lastly, assess the outcomes from both DFS searches. If both searches find a path, we conclude that it is not possible to

4. Perform the first DFS to check for the existing path.

5. If a path is found in step 4, flip the start and end cells to 1 (to ensure they are considered in the next DFS), then conduct the

path exists from the current cell (i, j) to the bottom-right cell (m - 1, n - 1).

DFS returns False, indicating no path can be made through this cell.

Perform a second DFS with the modified grid using b = dfs(0, 0).

paths before and after assuming at least one flip elsewhere in the grid.

We go down from (1, 1) to (2, 1) but it is blocked.

def isPossibleToCutPath(self, grid: List[List[int]]) -> bool:

return dfs(row + 1, col) or dfs(row, col + 1)

Get the number of rows and columns in the grid.

rows, cols = len(grid), len(grid[0])

has_path_first_time = dfs(0, 0)

grid[0][0] = grid[-1][-1] = 1

has_path_second_time = dfs(0, 0)

private int[][] grid; // Store the provided grid

private int cols; // Number of columns in the grid

public boolean isPossibleToCutPath(int[][] grid) {

bool isPossibleToCutPath(vector<vector<int>>& grid) {

int rows = grid.size();

int cols = grid[0].size();

return false;

return true;

grid[row][col] = 0;

private int rows; // Number of rows in the grid

if row >= rows or col >= cols or grid[row][col] == 0:

- second DFS, enforcing the use of at least one flip elsewhere.
- disconnect the grid with a single flip. If the second DFS does not find a path, it shows that flipping at most one cell (besides the start and end) can disconnect the grid. We return true if the grid can be disconnected, false otherwise.

3. If we cannot find a path to the end cell, mark it as not possible to disconnect by only flipping one cell.

found during the first traversal, the second traversal will reveal whether blocking one additional cell leads to disconnection. **Solution Approach**

This approach works because flipping the cells to 1 after the initial search guarantees that if there is another path aside from the one

structure or graph. It works by moving from the starting node and venturing as far as possible along each branch before backtracking.

In the Python code provided, a nested function dfs(i, j) is defined for the DFS traversal. This function aims to determine whether a

1. Base Case: If the current cell indices are out of bounds (greater than or equal to m or n), or if the current cell value is 0 (blocked),

The solution leverages the Depth-First Search (DFS) algorithm, which is a common technique for exploring all the paths in a grid-like

Here's a breakdown of the DFS implementation:

2. Visiting Cells: When a cell with a value 1 is visited, the function first marks it as visited by flipping it to 0. This prevents the DFS from revisiting the same cell and getting stuck in a loop.

3. Path Completion Check: If the end cell (m - 1, n - 1) is reached, DFS returns True, confirming a path has been found.

directly to the right (i, j + 1). If any of those recursive calls return True, the current function also returns True.

4. Exploring Adjacent Cells: The DFS continues by making recursive calls to the cell directly below (i + 1, j) and to the cell

- 5. **Determining Disconnectability**: Conduct the first DFS from the start cell (0, 0) using a = dfs(0, 0) to check for an existing path.
- 6. Result Evaluation: The piece of code not (a and b) returns True only if the first DFS found a path (a is True), and the second DFS did not find a path (b is False). Thus, the expression evaluates to True if we can disconnect the matrix, otherwise, it returns

○ After the initial DFS, enforce the start and end cells to be open by setting grid[0][0] and grid[-1][-1] to 1.

False.

The effectiveness of the solution is due to the algorithm's ability to explore all possible paths from the start to end cell, and the

logical use of DFS to determine if disrupting any cell's connectivity (by changing a single 1 to 0) will disconnect the grid without

testing every single cell explicitly. The solution cleverly checks the disconnectability of the matrix by attempting to find two distinct

Example Walkthrough Let's consider a simple 3×3 binary matrix example to illustrate the solution approach:

Following the solution steps: 1. We attempt to perform DFS from the start cell (0, 0). We check for the path existence without any flip and mark the visited cells.

Backtracking again, we move down from (0, 1) to (1, 1) and since it has a 1, we continue by going right to (1, 2) which is blocked.

Python Solution

class Solution:

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grid can be disconnected by at most one flip.

def dfs(row, col):

1 Initial Grid:

1 Grid after first DFS attempt: 2 0 0 1 3 0 1 0 4 1 0 1

Given the grid is already disconnected, this example demonstrates the scenario where the initial DFS itself concludes that no path

exists from start to end without flipping any cells, thus no need for a second DFS or flipping any additional cells to conclude that the

4. There is no need to proceed with the second DFS in this case since the grid is disconnected after the first DFS. We can directly return true.

2. Since we start at (0, 0), we mark it as 0, to not revisit and move right to (0, 1) and then to (0, 2).

Now in the top right corner, (0, 2), we go down to (1, 2) but find that it's blocked (0).

We backtrack and from (0, 2) and move down to (1, 2) and find it is also blocked.

Backtracking again, we go down from (0, 0) straight to (1, 0) which is blocked.

There is no more path to explore and we couldn't reach (2, 2), the end cell.

3. Since the first DFS didn't find any path, we know that the grid is already disconnected.

dfs is a helper function that performs a depth-first search on the grid to

Recursively check the right and down directions from the current cell.

Reset the top-left and bottom-right cells back to 1, as we made them 0 in the dfs.

Call dfs again to see if there is still a path after the first has been cut.

completely block off the grid, so we return False. Otherwise, we return True.

If there was a path both times, that means cutting the first path did not

// Determines if it's possible to cut a path from top-left to bottom-right

Call dfs to see if there is a first path from top-left to bottom-right.

return False # Mark the current cell as visited by changing it to 0 (a wall). grid[row][col] = 0 # If we have reached the bottom-right corner, return True. 11 12 if row == rows - 1 and col == cols - 1: return True 13

determine if there is a path from the top-left corner (0,0) to the bottom-right corner (m-1, n-1)

Base case: if we are out of bounds or the current cell is 0 (a wall), return False.

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            return not (has_path_first_time and has_path_second_time)
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```

Java Solution

1 class Solution {

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this.grid = grid;
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             rows = grid.length; // Initialize number of rows
  9
             cols = grid[0].length; // Initialize number of columns
 10
             // Perform a DFS from the top-left corner before the cut
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             boolean pathExistsBeforeCut = depthFirstSearch(0, 0);
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             // Simulate the cut by marking the start and end points as obstacles
 16
             grid[0][0] = 1;
 17
             grid[rows - 1][cols - 1] = 1;
 18
 19
             // Perform a DFS from the top-left corner after making the cut
 20
             boolean pathExistsAfterCut = depthFirstSearch(0, 0);
 21
             // If the path exists before and not after, then it is possible to cut the path
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             return !(pathExistsBeforeCut && pathExistsAfterCut);
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         // Helper method to perform depth-first search
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         private boolean depthFirstSearch(int row, int col) {
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             // Check boundaries and whether the current cell is an obstacle
 29
             if (row >= rows || col >= cols || grid[row][col] == 0) {
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                 return false;
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 33
             // Check if we've reached the bottom-right corner
 34
             if (row == rows - 1 && col == cols - 1) {
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                 return true;
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 38
             // Mark the current cell as an obstacle to avoid revisiting
 39
             grid[row][col] = 0;
 40
             // Recursively search in the right and down directions, returning true if a path is found
 41
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             return depthFirstSearch(row + 1, col) || depthFirstSearch(row, col + 1);
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C++ Solution
  1 #include <vector>
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// The function evaluates if it's possible to block the path from top left to bottom right by setting a cell to zero

// Number of rows in the grid

// Helper function to perform depth-first search from (row, col) position in the grid

// Base case checks: If out of bounds or encountered a zero, return false

// Returns true if there is a path to bottom right, false otherwise.

if (row >= rows || col >= cols || grid[row][col] == 0) {

// Reached the bottom-right cell, return true

// Explore the path downwards and rightwards;

bool existsPathInitially = performDFS(0, 0);

bool existsPathAfterReset = performDFS(0, 0);

return !(existsPathInitially && existsPathAfterReset);

// Set the current cell to 0 to prevent revisiting

// the path exists if either of them returns true

return performDFS(row + 1, col) || performDFS(row, col + 1);

// Check if there is a path from top left to bottom right in the current grid

// Return the negation of the logical AND to indicate if it's possible to cut the path

if (row == rows - 1 && col == cols - 1) {

function<bool(int, int)> performDFS = [&](int row, int col) -> bool {

// Number of columns in the grid

32 33 // Reset the top-left and bottom-right values of the grid to 1 34 grid[0][0] = grid[rows - 1][cols - 1] = 1;35 36 // Check if there is a path after the first DFS and setting cells back to 1

};

2 #include <functional>

4 class Solution {

public:

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 43 };
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Typescript Solution
   function isPossibleToCutPath(grid: number[][]): boolean {
       // Store the number of rows (m) and columns (n) from the input grid
       const numRows = grid.length;
       const numCols = grid[0].length;
 6
       // Define the depth-first search function to traverse the grid
       const depthFirstSearch = (rowIndex: number, colIndex: number): boolean => {
           // Base case: return false if the current position is out of bounds or not a path (non-1 value)
           if (rowIndex >= numRows || colIndex >= numCols || grid[rowIndex][colIndex] !== 1) {
               return false;
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           // Mark the current cell as visited by setting it to 0
13
           grid[rowIndex][colIndex] = 0;
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15
           // Base case: return true if reached the bottom-right cell of the grid
           if (rowIndex === numRows - 1 && colIndex === numCols - 1) {
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               return true;
18
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20
           // Recursively explore the right and down neighbors of the current cell
           // Return true if any recursion call returns true
           return depthFirstSearch(rowIndex + 1, colIndex) || depthFirstSearch(rowIndex, colIndex + 1);
23
       };
24
25
       // Perform DFS traversal from the top-left corner (0,0)
26
       const firstTraversalResult = depthFirstSearch(0, 0);
27
28
       // Reset the top-left and bottom-right cells for the second traversal
29
       grid[0][0] = 1;
30
       grid[numRows - 1][numCols - 1] = 1;
31
       // Perform DFS traversal again to see if path can still be found after first pass
32
       const secondTraversalResult = depthFirstSearch(0, 0);
33
       // The path can be cut if both first and second traversals did not find a path (i.e., false status)
35
       return !(firstTraversalResult && secondTraversalResult);
36
37 }
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```

// If a path was found in both checks, then it's impossible to cut the path by setting a single cell to zero

Time and Space Complexity **Time Complexity**

The time complexity of the given algorithm is primarily dependent on the depth-first search (DFS) implementation that explores all

possible paths from the top-left to the bottom-right corner of the grid, if such a path exists. In the worst case, every cell in the grid might be visited during the DFS. For a grid with m rows and n columns, the worst-case time complexity is O(m*n) since each cell is visited at most once during the search.

The space complexity is primarily driven by the call stack used by the recursive DFS function. In the worst case, the function may recurse to a depth equal to the sum of the number of rows and columns of the grid, because at most, the path can be as long as moving to the rightmost column and then downwards to the bottommost row (or vice versa).

Space Complexity

Therefore, the space complexity, in the worst case, is O(m+n). Additionally, it should be noted that the input grid is modified during the search process, which means the algorithm uses 0(1) extra

space aside from the stack space used by the recursion.