75. Sort Colors

Medium

## **Problem Description**

<u>Array</u>

Two Pointers

Sorting

In this problem, you are given an array nums which contains n elements. Each element represents a color coded as an integer: 0 for red, 1 for white, and 2 for blue. Your task is to sort this array in a way that the colors are grouped together and in the order of the library's sort function.

red, white, and blue. The sorting has to be done in-place, without using any extra space for another array, and you cannot use Intuition

# To solve this problem, the solution approach uses a variant of the famous Dutch National Flag algorithm proposed by Edsger

Dijkstra. The crux of this algorithm is a three-way partitioning technique that segments an array into three parts to sort the elements of three different types. In this case, we will maintain three pointers:

1. i - All elements before index i are 0 s (reds).

- 2. j All elements from index j onwards are 2 s (blues).
- 3. k Current element that is being inspected.
- at the end. The k pointer will start from 0 and move towards j. We iterate through the array with k, and when we find a 0, we increment i and swap the values at i and k. If we find a 2, we

Initially, i is set to -1, indicating there are no ∅s in the beginning, and j is set to the length of nums, indicating there are no 2s

decrement j and swap the values at k and j but we don't move the pointer k because the new element we swapped from

position j might be 0, so it needs to be rechecked. If the element is 1, it's already in its correct place since we are ensuring all os and 2s are moved to their correct places. So, for 1, we just move k forward. We continue this process until k meets j, at which point all elements to the left of i are 0s, elements between i and j are 1s,

**Solution Approach** 

## Here's a step-by-step explanation using the Reference Solution Approach:

Initialize three pointers (i, j, and k):

The solution implements the Dutch National Flag algorithm, which is a partitioning strategy.

∘ i starts just before the array at -1. This will eventually track the position up to which 0 s have been sorted. o j starts after the end of the array at len(nums). This will eventually track the position from which 2 s have been sorted.

and all elements from j onwards are 2 s, resulting in a sorted array.

k starts at 0 and is used to iterate through the array.

If nums [k] == 0, this element needs to be moved to the front.

Increment i to move it to the next unsorted position.

- Perform iterations while k < j:
- Increment k to move on to the next element. Else, if nums [k] == 2, this element needs to be moved to the end.

any additional space or the library sort function.

Swap the elements at k and j (nums[j], nums[k] = nums[k], nums[j]), moving the 2 closer to its correct place. Here we don't

Decrement j to move it towards the first unsorted position from the end.

∘ If nums [k] == 1, no action is needed as 1s are automatically sorted when 0s and 2s are moved to their correct places. Simply increment k to continue to the next element.

By following this approach, we continue to partition the array into three parts: 0 s before i, 1 s between i and j, and 2 s after

Swap the elements at i and k (nums[i], nums[k] = nums[k], nums[i]), effectively moving the 0 to its correct place.

j. The loop continues until k becomes equal to j, meaning all elements have been examined and placed in their correct position. Therefore, the array is now sorted in-place with red (0), white (1), and blue (2) colors in the correct order without using

increment k because the newly swapped element could be 0 or 1 and it has not been evaluated yet.

**Example Walkthrough** Let's say we have an array nums as [2, 0, 1, 2, 1, 0]. We need to sort this array using the Dutch National Flag algorithm so that all 0s (reds) come first, followed by 1s (whites), and then 2s (blues).

## Initialize the pointers i, j, and k:

∘ i is set to -1 j is set to 6 (since the array length is 6) ∘ k is set to 0

Iteration 1: 0

We don't increment k as we need to evaluate the swapped element.

Start iterating with k while k < j (while k is less than 6):

Here's a step-by-step process of how the algorithm would sort this array:

- nums [k] is 2. Since k==0, we need to move this 2 to the end.
- We decrement j to 5. ■ We swap nums[k] with nums[j]. So the array becomes [0, 0, 1, 2, 1, 2].
- Iteration 2: 0 ■ Now nums[k] is 0. This needs to go at the beginning.

■ We increment k to 1.

- We increment i to 0. ■ We swap nums[i] with nums[k]. The array is still [0, 0, 1, 2, 1, 2] since both nums[i] and nums[k] are 0.
- Iteration 3: nums[k] is another 0.
  - We increment i to 1. ■ We swap nums[i] with nums[k], but the array remains unchanged [0, 0, 1, 2, 1, 2] as they are the same value. ■ Increment k to 2.

■ We swap nums[k] with nums[j]. Now the array looks like [0, 0, 1, 1, 2, 2].

Iteration 4:

Iteration 5:

space or sorting functions.

**Solution Implementation** 

**Python** 

Java

class Solution {

class Solution:

nums [k] is 2, needs to move to the end. ■ We decrement j to 4.

nums [k] is now 1. It should stay in place.

def sortColors(self, nums: List[int]) -> None:

while current index < next two index:</pre>

if nums[current index] == 0:

next zero index += 1

current index += 1

next two index -= 1

elif nums[current index] == 2:

# Move to the next element

// Method to sort the array containing 0s, 1s, and 2s

// This function is used to sort the colors, represented by numbers 0, 1, and 2.

// 'right' is the position one more than where the next 2 should go,

// then move both 'left' and 'current' one step right.

// then decrement 'right' to move it leftward.

next\_zero\_index, next\_two\_index, current\_index = -1, len(nums), ∅

# Move the 0 to the next position for 0

# Move the 2 to the next position for 2

# Process elements until the current index reaches the next\_two\_index

# The function modifies the list in place, so there is no return value

// 'left' is the position where the next 0 should go,

// 'current' is the current index being considered.

swap(nums[++left], nums[current++]);

swap(nums[--right], nums[current]);

int left = -1, right = nums.size(), current = 0;

// It uses the Dutch National Flag algorithm to sort in place with O(n) complexity.

while (current < right) { // Process elements until 'current' reaches 'right'</pre>

// When a 0 is found, swap it with the element at 'left' position,

// If the element is 1, just move 'current' one step to the right.

// When a 2 is found, swap it with the element just before 'right' position,

// Note 'current' is not incremented because the swapped element needs to be checked.

public void sortColors(int[] nums) {

void sortColors(vector<int>& nums) {

if (nums[current] == 0) {

} else if (nums[current] == 2) {

// Initialize pointers:

} else {

++current;

# Move the 0 to the next position for 0

# Move the 2 to the next position for 2

• nums [k] is 1. This is already in the correct position.

■ Do not increment k as we need to evaluate the swapped element. Iteration 6:

We simply increment k to 3.

- Increment k to 4. Now k == j, so we stop. The final sorted array is [0, 0, 1, 1, 2, 2], with all the colors grouped together in the correct order without using any extra
- # Initialize pointers for the next position of 0, the next position of 2, and the current element next\_zero\_index, next\_two\_index, current\_index = -1, len(nums), 0 # Process elements until the current index reaches the next\_two\_index

nums[next zero index]. nums[current\_index] = nums[current\_index], nums[next\_zero\_index]

nums[next two index], nums[current index] = nums[current index], nums[next two index]

```
# Do not increment current_index because we need to check the newly swapped element
    else:
        # If the current element is a 1, just move to the next element
        current index += 1
# The function modifies the list in place, so there is no return value
```

```
// Initialize pointers for the current element (currIndex),
        // the last position of 0 (lastZeroIndex) and the first position of 2 (firstTwoIndex)
        int lastZeroIndex = -1;
        int firstTwoIndex = nums.length;
        int currIndex = 0;
        // Process elements until currIndex reaches firstTwoIndex
        while (currIndex < firstTwoIndex) {</pre>
            if (nums[currIndex] == 0) {
                // If the current element is 0, swap it to the position after the last 0 we found
                swap(nums, ++lastZeroIndex, currIndex++);
            } else if (nums[currIndex] == 2) {
                // If the current element is 2, swap it with the element at the position
                // just before the first 2 we found
                swap(nums, --firstTwoIndex, currIndex);
            } else {
                // If the current element is 1, just move to the next element
                ++currIndex;
    // Helper method to swap two elements in an array
    private void swap(int[] nums, int i, int j) {
        int temp = nums[i];
        nums[i] = nums[j];
        nums[j] = temp;
C++
#include <vector>
using namespace std;
class Solution {
```

public:

```
TypeScript
 * Sorts an array of numbers in-place, so that all 0s come first,
 * followed by all 1s, and then all 2s. This pattern is known as the Dutch national flag problem.
 * @param {number[]} nums - The input array containing 0s, 1s, and 2s.
 */
function sortColors(nums: number[]): void {
    let zeroIndex = -1; // Initialize the index where 0s will be placed.
    let twoIndex = nums.length; // Initialize the index where 2s will be placed.
    let currentIndex = 0; // The current index we're scanning from the array.
    while (currentIndex < twoIndex) {</pre>
        if (nums[currentIndex] === 0) {
            // When the current element is 0, swap it with the element at zeroIndex,
            // then increment zeroIndex and currentIndex.
            zeroIndex++;
            [nums[zeroIndex], nums[currentIndex]] = [nums[currentIndex], nums[zeroIndex]];
            currentIndex++;
        } else if (nums[currentIndex] === 2) {
            // When the current element is 2, decrement twoIndex and swap the current element
            // with the element at twoIndex.
            twoIndex--;
            [nums[twoIndex], nums[currentIndex]] = [nums[currentIndex], nums[twoIndex]];
            // Do not increment currentIndex here because the element swapped from twoIndex
            // may be 0, which will need to be moved to zeroIndex in the next iteration.
        } else {
            // If the element is 1, just move on to the next element.
            currentIndex++;
class Solution:
    def sortColors(self, nums: List[int]) -> None:
        # Initialize pointers for the next position of 0, the next position of 2, and the current element
```

### # Do not increment current\_index because we need to check the newly swapped element else: # If the current element is a 1, just move to the next element current index += 1

Time and Space Complexity

while current index < next two index:</pre>

if nums[current index] == 0:

next zero index += 1

current index += 1

next two index -= 1

elif nums[current index] == 2:

# Move to the next element

The time complexity of the code is O(n), where n is the length of the input list nums. This is because the while loop iterates through each element of the list at most once. The variables i, j, and k are used to traverse the array without the need to revisit elements. The increment and decrement operations on i, j, and k, as well as the swaps, all occur in constant time, and the loop runs until k is no longer less than j.

nums[next zero index], nums[current\_index] = nums[current\_index], nums[next\_zero\_index]

nums[next two index], nums[current index] = nums[current index], nums[next two index]

The space complexity of the code is 0(1) because the sorting is done in place. No additional storage is needed that scales with the input size n. The only extra space used is for the three pointers i, j, and k, which use a constant amount of space regardless of the size of the input list.