Problem Description

The problem asks us to find the minimum number of intervals that need to be removed from a given list of time intervals to ensure that no two intervals overlap with each other. Intervals overlap when one interval starts before the other one ends. For example, if one interval is [1, 2] and another is [2, 3], they do not overlap, but if the second interval is [1, 3], they do overlap because the first interval has not ended before the second one starts.

Our input is an array of intervals, where each interval is represented as a list with two elements, signifying the start and the end times. The output should be an integer that represents the minimum number of intervals that must be removed to eliminate all overlaps.

The key intuition behind the solution lies in the greedy algorithm approach. A greedy algorithm makes the locally optimal choice at

Intuition

each stage with the hope of finding the global optimum. In the context of this problem, the greedy choice would be to always pick the interval that ends the earliest, because this would leave the most room for subsequent intervals. Here is the thinking process for arriving at the solution:

1. Sort the intervals based on their end times. This way, we encounter the intervals that finish earliest first and can thus make the

- greedy choice. 2. Start with the first interval, considering it as non-overlapping by default, and make a note of its end time. 3. Iterate through the subsequent intervals:
- If the start time of the current interval is not less than the end time of the last non-overlapping interval, it means this interval
- does not overlap with the previously considered intervals. We can then update our last known end time to be the end time of
 - the current interval. If the start time is less than the last known end time, an overlap occurs, and we must choose to remove an interval. Following the greedy approach, we keep the interval with the earlier end time and remove the other by incrementing our
- answer (the number of intervals to remove). By following these steps and always choosing the interval that finishes earliest, we ensure that we take up the least possible space on the timeline for each interval, and therefore maximize the number of intervals we can include without overlapping.

Solution Approach

The provided solution follows the greedy strategy mentioned in the reference solution approach. Let's discuss how the solution is

implemented in more detail: 1. Sorting Intervals: The input list of intervals is sorted based on the end times of the intervals. This is done using Python's sort

function with a lambda function as the key that retrieves the end time x[1] from each interval x. 1 intervals.sort(key=lambda x: x[1])

Sorting the intervals by their end times allows us to apply the greedy algorithm effectively.

3. Iterating Over Intervals: The code iterates through the rest of the intervals starting from the second interval (since the first

2. Initializing Variables: Two variables are initialized:

current interval's end time e.

- ans: set to 0, it keeps count of the number of intervals we need to remove. • t: set to the end time of the first interval, it represents the latest end time of the last interval that we decided to keep.
- interval's end time is stored in t).
 - 1 for s, e in intervals[1:]:
- Each interval [s, e] consists of a start time s and an end time e. 4. Checking for Overlapping: In each iteration, the code checks if the current interval's start time s is greater than or equal to the
 - by 1.

If s >= t, there is no overlap with the last chosen interval, so the current interval can be kept. We then update t to the

3 else: ans += 1 5. Returning the Result: After the loop finishes, ans holds the minimum number of intervals that need to be removed to make all

If s < t, there is an overlap with the last chosen interval, so the current interval needs to be removed, and we increment ans

remaining intervals non-overlapping, so it is returned as the final result. 1 return ans

variable t:

Example Walkthrough Let's illustrate the solution approach with a small example. Suppose we are given the following list of intervals:

We want to remove the minimum number of intervals so that no two intervals overlap. Here is how we apply the solution approach:

By following the greedy approach, the algorithm ensures that the intervals with the earliest end times are considered first, minimizing

1. Sorting Intervals: First, we sort the intervals by their end times:

Python Solution

class Solution:

10

16

17

18

19

20

21

22

23

28

30

9

10

12

19

20

21

22

24

25

26

27

28

29 }

from typing import List

1 intervals = [[1, 2], [2, 3], [3, 4], [1, 3]]

1 sorted_intervals = [[1, 2], [2, 3], [1, 3], [3, 4]]

3. Iterating Over Intervals: We iterate through the intervals starting from the second one.

2. Initializing Variables: We initialize ans = 0 and t = 2, where t is the end time of the first interval after sorting.

Comparing the 2nd interval [2, 3] with t: since 2 >= 2, we update t to 3, and no interval is removed.

potential overlap with future intervals and thus minimizing the number of intervals that need to be removed.

4. Checking for Overlapping:

def eraseOverlapIntervals(self, intervals: List[List[int]]) -> int:

Return the total count of removed intervals to avoid overlap

If the interval overlaps, increment the count of intervals to remove

 Comparing the 3rd interval [1, 3] with t: since 1 < 3, this interval overlaps with the previously chosen intervals. We increment ans to 1.

and by removing it, we ensured that no intervals overlap.

end_time = intervals[0][1]

end_time = end

return removed_intervals_count

removed_intervals_count += 1

else:

return overlaps;

1 #include <vector> // Required for using the vector container

2 #include <algorithm> // Required for using the sort algorithm

int eraseOverlapIntervals(vector<vector<int>>& intervals) {

sort(intervals.begin(), intervals.end(), [](const auto& a, const auto& b) {

// Sort the intervals based on their end time.

if (currentEndTime <= intervals[i][0]) {</pre>

// Return the total number of overlapping intervals to remove

++nonOverlappingCount;

return a[1] < b[1];

} else {

- Comparing the 4th interval [3, 4] with t: since 3 >= 3, we update t to 4, and no interval is removed. After checking all intervals, the number of intervals to be removed is ans = 1. This is because the interval [1, 3] was overlapping,
- The output of our algorithm for this example would be 1, indicating we need to remove a single interval to eliminate all overlaps.

Sort the intervals based on the end time of each interval intervals.sort(key=lambda interval: interval[1]) # Initialize the count of removed intervals and set the time to compare against removed_intervals_count = 0

```
# Iterate through the intervals starting from the second one
12
           for start, end in intervals[1:]:
13
               # If the current interval does not overlap, update the `end_time`
               if start >= end_time:
```

```
Java Solution
   import java.util.Arrays; // Required for Arrays.sort
   import java.util.Comparator; // Required for Comparator
    class Solution {
       public int eraseOverlapIntervals(int[][] intervals) {
           // Sort the intervals array based on the end time of each interval
           Arrays.sort(intervals, Comparator.comparingInt(a -> a[1]));
           // Set 'end' as the end time of the first interval
10
           int end = intervals[0][1];
11
           // Initialize 'overlaps' to count the number of overlapping intervals
12
            int overlaps = 0;
14
15
           // Iterate through each interval starting from the second one
            for (int i = 1; i < intervals.length; i++) {</pre>
16
17
               // If the current interval does not overlap with the previous, update 'end'
               if (intervals[i][0] >= end) {
18
                    end = intervals[i][1];
                } else {
20
21
                   // If the current interval overlaps, increment 'overlaps'
22
                    overlaps++;
23
24
25
26
           // Return the total number of overlapping intervals to be removed
27
```

13 int nonOverlappingCount = 0; // To keep track of the number of non-overlapping intervals int currentEndTime = intervals[0][1]; // Track the end time of the last added interval 14 15 16 // Iterate over all intervals starting from the second one for (int i = 1; i < intervals.size(); ++i) {</pre>

C++ Solution

class Solution {

});

public:

```
return nonOverlappingCount;
29
30 };
31
Typescript Solution
   function eraseOverlapIntervals(intervals: number[][]): number {
       // Sort the intervals based on the ending time of each interval
       intervals.sort((a, b) \Rightarrow a[1] - b[1]);
       // Initialize the end variable to the end of the first interval
       let lastIntervalEnd = intervals[0][1];
       // Initialize counter for the number of intervals to remove
 8
       let intervalsToRemove = 0;
 9
10
       // Iterate through the intervals starting from the second one
11
       for (let i = 1; i < intervals.length; i++) {
12
           // Current interval being considered
13
           let currentInterval = intervals[i];
14
           // Check if the current interval overlaps with the last non-overlapping interval
16
           if (lastIntervalEnd > currentInterval[0]) {
17
               // If it overlaps, increment the removal counter
18
               intervalsToRemove++;
           } else {
20
               // If it doesn't overlap, update the end to be the end of the current interval
                lastIntervalEnd = currentInterval[1];
23
24
25
26
       // Return the number of intervals that need to be removed to eliminate all overlaps
```

// Function to find the minimum number of intervals you need to remove to make the rest of the intervals non-overlapping.

// If the current interval starts after the end of the last added interval, it does not overlap

// If the current interval overlaps, increment the nonOverlappingCount

currentEndTime = intervals[i][1]; // Update the end time to the current interval's end time

27 return intervalsToRemove; 28 } 29

Time and Space Complexity

them overlap. Here's an analysis of its time complexity and space complexity: **Time Complexity**

The given Python code aims to find the minimum number of intervals that can be removed from a set of intervals so that none of

which has a time complexity of $O(n \log n)$, where n is the number of intervals.

n).

2. The for loop iterates through the list of intervals once. The loop runs in O(n) as each interval is visited exactly once. Combining these steps, the overall time complexity is dominated by the sorting step, leading to a total time complexity of O(n log

1. In-place sorting of the intervals doesn't require additional space proportional to the input size, so the space complexity of the

The time complexity of the code is primarily determined by the sorting operation and the single pass through the sorted interval list:

1. intervals.sort(key=lambda x: x[1]) sorts the intervals based on the end time. Sorting in Python uses the Timsort algorithm,

Space Complexity

The space complexity of the code is mainly the space required to hold the input and the variables used for the function:

sorting operation is 0(1). 2. The only extra variables that are used include ans, and t. These are constant-size variables and do not scale with the input size.

Hence, the overall space complexity of the code is 0(1), indicating it requires constant additional space.