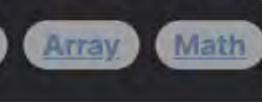




Problem Description



[xi, yi], which represent its X and Y coordinates, respectively. The task is to calculate the area of the largest triangle that can be formed by any three different points from the array. The resulting area should be approximated to within 10^-5 of the correct value to be considered acceptable. To solve this problem, we need to understand that a triangle can be formed by any three non-collinear points on a plane. Hence, we

The given problem provides an array of points representing coordinates on the X-Y plane. Each point is defined by a pair of integers,

must consider all possible combinations of three points from our array and calculate the area of the triangle they form. This is essentially a combinatorial problem where we seek the maximum value from a set of results obtained from these combinations. Intuition

The intuitive solution for this problem leverages the mathematical formula for the area of a triangle when given three points. The formula to calculate the area T of a triangle with vertices at coordinates (x1, y1), (x2, y2), and (x3, y3) is:

1 T = |(x1(y2-y3) + x2(y3-y1) + x3(y1-y2)) / 2|

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However, the provided solution code uses the cross product method to find the area of a triangle formed by three points in 2D
space. Remember, in a 2D plane, the area A of a triangle formed by points (x1, y1), (x2, y2), and (x3, y3) can also be computed
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1 A = |(x1(y2-y3) + x2(y3-y1) + x3(y1-y2)) / 2|This is equivalent to:

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1 A = |((x2-x1)*(y3-y1) - (x3-x1)*(y2-y1)) / 2|
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using the following formula derived from the cross product:

The formula is based on the fact that the absolute value of the cross product of two vectors can be interpreted as the area of the

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parallelogram they span, and the area of the triangle is half of that parallelogram.
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two sides of a potential triangle.

The code implements a brute-force approach by considering every possible triplet of points: 1. Three nested loops iterate through all combinations of three points. It computes vectors [u1, v1] and [u2, v2] that represent

twice the area of the triangle formed by the points. 3. This value is halved and the absolute value is taken to get the area of the triangle. If the calculated area is greater than a

previously recorded maximum area (ans), it updates the ans variable. 4. After exhausting all possible combinations, the largest recorded triangle area ans is returned.

2. The cross product of these vectors is calculated, which is essentially the determinant of a 2×2 matrix, and it corresponds to

- The approach is exhaustive and straightforward but can be inefficient for large input sizes because it considers all possible point
- triplets, resulting in a time complexity of O(n^3), where n is the number of points. Nevertheless, it ensures that the maximum area is found.

The solution approach utilizes a straightforward brute-force algorithm to solve the problem. Here's an in-depth breakdown of the

Solution Approach

is common in problems where all combinations of elements need to be considered.

 Data Structures: No specific data structures are needed for this solution except for the input list of points and a variable to keep track of the maximum area found.

• Patterns: The pattern here is the use of multiple nested loops to generate all possible triplets of points from the list. This pattern

• Algorithm: The algorithm loops through each possible combination of three distinct points in the input array to compute the area

of the triangle formed by those points. It uses the cross product method to determine the area, which works effectively for this

- Here's a step-by-step explanation of the solution: 1. Initial Maximum Area: A variable called ans is initialized to zero, which will store the maximum triangle area found during the
 - array. These loops pick one point in each iteration, creating triplets such as (points[i], points[j], points[k]). 3. Vector Calculation: Within the innermost loop, two vectors are determined that represent the sides of the triangle from the point

2. Nested Loops: The three nested for loops are used to iterate over all possible combinations of three points from the points

4. Cross Product: The cross product of these two vectors is computed as:

(x1, y1) to (x2, y2) and from (x1, y1) to (x3, y3).

triangle area, which is then returned as the final result.

Let's use a small set of points to illustrate the solution approach provided:

The first loop starts with i = 0, with points[i] will be (0, 0).

The third loop starts with k = 2, so points[k] will be (3, 0).

From (0,0) to (3,0) which is (3 − 0, 0 − 0) or (3,0).

3. Vector Calculation: We calculate two vectors:

The second loop starts with j = 1, so points[j] will be (0, 4).

is the determinant of the 2×2 matrix formed by vectors u1, v1 and u2, v2:

implementation steps and the rationale behind them.

2D geometric problem.

iteration.

- 1 CP = (u1 * v2 u2 * v1)
- in 2D space. 5. Area Calculation: The actual area of the triangle is found by halving and taking the absolute value of the cross product CP, which

We consider only the 'z' component, which in a 3D cross product represents the area of the parallelogram formed by two vectors

6. Updating Maximum Area: If the computed triangle area t is greater than the current maximum ans, it is updated to t. 7. Result: Once all combinations have been considered, and the maximum area has been found, the variable ans holds the largest

This elementary brute-force solution ensures that even though it might not be efficient for a large number of points (due to its O(n^3)

time complexity), it will always yield the correct maximum area of a triangle that can be formed, satisfying the problem requirements.

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Example Walkthrough
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1 t = abs(u1 * v2 - u2 * v1) / 2

- Suppose we have the following array of points: [(0,0), (0,4), (3,0)]. This array forms a right-angled triangle with the right angle at the origin (0,0). The area of this triangle can be calculated using the
- cross product approach explained in the content.
- \circ From (0,0) to (0,4) which is (0-0,4-0) or (0,4).

○ We compute the cross product CP of these vectors, which will be 0 * 0 - 3 * 4, resulting in -12.

With only one combination of points, the final ans we get is the maximum area, which is 6 in this case. Hence, the largest triangle

the underlying mechanics of the solution approach, where the algorithm evaluates all combinations of three points to find the

1. Initial Maximum Area: We initialize a variable ans to zero. This will store the maximum triangle area we find.

5. Area Calculation: • The absolute value of the cross product is |CP| = |-12| = 12.

triangle with the maximum area.

for x1, y1 in points:

return max_area

for x2, y2 in points:

for x3, y3 in points:

u1, v1 = x2 - x1, y2 - y1

 u^2 , $v^2 = x^3 - x^1$, $y^3 - y^1$

Return the largest found area of a triangle

public double largestTriangleArea(int[][] points) {

int x1 = point1[0], y1 = point1[1];

for (int[] point2 : points) {

for (int[] point1 : points) {

for (auto& point1 : points) {

nested loops each iterating over all the points.

int x1 = point1[0], y1 = point1[1];

for (auto& point3 : points) {

int x2 = point2[0], y2 = point2[1];

int x3 = point3[0], y3 = point3[1];

int vector1X = x2 - x1, vector1Y = y2 - y1;

int vector2X = x3 - x1, vector2Y = y3 - y1;

largestArea = std::max(largestArea, area);

// Update largestArea if a larger area is found

for (auto& point2 : points) {

area = abs(u1 * v2 - u2 * v1) / 2

max_area = max(max_area, area)

Python Solution

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4. Cross Product:

2. Nested Loops:

6. Updating Maximum Area: Since t is 6 and ans is 0, we update ans to 6.

that can be formed by any three points from the given array has an area equal to 6.

The area of the triangle would be half of this, t = CP / 2 = 6.

- By using the above steps on our small set of points, the brute-force algorithm effectively determines that the right-angled triangle formed by these points produces the largest area among all possible triangles formed from these points. This example demonstrates
 - class Solution: def largest_triangle_area(self, points: List[List[int]]) -> float: # Initialize the max area to 0 max_area = 0

Iterate over all possible combinations of three points to form triangles

Calculate vector (u1, v1) from point 1 to point 2

Calculate vector (u2, v2) from point 1 to point 3

Update the max_area if the current area is larger

double maxArea = 0; // Initialize maxArea as the largest triangle area found so far.

// Iterate through all the points to get the second point (p2) of the triangle.

double largestArea = 0; // Initialize the variable to hold the largest triangle area

// Calculate the vector from point1 to point2 and point1 to point3

// Use the cross product of vectors to find the area of the triangle

double area = std::abs(vector1X * vector2Y - vector2X * vector1Y) / 2.0;

// Iterate over all possible combinations of three points to find the largest area

// Calculate the vectors from point1 to point2 and from point1 to point3

// Iterate through all the points to get the first point (p1) of the triangle.

int vector1X = x2 - x1, vector1Y = y2 - y1;

int vector2X = x3 - x1, vector2Y = y3 - y1;

(cross product of two vectors) divided by 2

20 Java Solution class Solution {

Calculate the triangle's area using the absolute value of the determinant

int x2 = point2[0], y2 = point2[1]; 11 12 13 // Iterate through all the points to get the third point (p3) of the triangle. for (int[] point3 : points) { 14 15 int x3 = point3[0], y3 = point3[1];16

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                        // Calculate the area of the triangle using the determinant |u1 v1|
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                                                                               |u2 v2|
23
                        // which is |x^2 - x^1| y^2 - y^1|
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                                     |x3 - x1 \quad y3 - y1| divided by 2. Note: this represents
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                        // the absolute value of the cross product of vectors (point1 to point2)
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                        // and (point1 to point3) divided by 2.
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                        double area = Math.abs(vector1X * vector2Y - vector2X * vector1Y) / 2.0;
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                        // Update maxArea if the calculated area is larger than the current maxArea.
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                        maxArea = Math.max(maxArea, area);
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           // Return the largest area found.
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            return maxArea;
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37 }
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C++ Solution
   #include <vector>
 2 #include <cmath>
   #include <algorithm>
   class Solution {
   public:
       double largestTriangleArea(vector<vector<int>>& points) {
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26 return largestArea; // Return the result 27 28 }; 29

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Typescript Solution
   function largestTriangleArea(points: number[][]): number {
        let largestArea: number = 0; // Initialize the variable to hold the largest triangle area
       // Triple nested loop to iterate over all possible combinations of three points
       points.forEach(point1 => {
           const x1 = point1[0], y1 = point1[1];
           points.forEach(point2 => {
               const x2 = point2[0], y2 = point2[1];
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               points.forEach(point3 => {
11
                   const x3 = point3[0], y3 = point3[1];
12
13
                   // Calculate the vectors from point1 to point2, and from point1 to point3
14
15
                   const vector1X = x2 - x1, vector1Y = y2 - y1;
                   const vector2X = x3 - x1, vector2Y = y3 - y1;
16
                   // Calculate the cross product of the vectors to get twice the area of the triangle
                   const area = Math.abs(vector1X * vector2Y - vector2X * vector1Y) / 2.0;
                   // Update largestArea if a larger area is found
                   largestArea = Math.max(largestArea, area);
               });
           });
       });
       // Return the largest area found
       return largestArea;
28
29 }
30
   // Example usage:
  const examplePoints: number[][] = [[0, 0], [0, 1], [1, 0], [0, 2], [2, 0]];
   console.log(largestTriangleArea(examplePoints)); // Possible output: 2 (for the triangle formed by the last three points)
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Time and Space Complexity The time complexity of the code is $O(n^3)$ where n is the number of points provided in the points list. This is because there are three

The space complexity of the code is 0(1) because the only extra space used is for variables to store the current point coordinates, the components of two vectors (u1, v1, u2, v2), and the area of the current triangle (t). These variables require a constant amount of space regardless of the input size.