In this problem, we're given a binary tree with a depth smaller than 5, which is represented as an array of three-digit integers. The

Problem Description

666. Path Sum IV

representation of the tree using integers has specific rules: 1. The first digit (the hundreds) indicates the depth of the binary tree node (d), which can range from 1 to 4.

2. The second digit (the tens) indicates the position of the node (p) within its level, similar to its position in a full binary tree,

- ranging from 1 to 8. 3. The third digit (the units) is a value of the node (v), which can be between 0 and 9.
- The task is to find the sum of all root-to-leaf paths' values. The array is given in ascending order, and it's ensured that it represents a
- valid connected binary tree. A path is defined as a sequence of nodes from the root of the tree to any leaf node, and the path sum is the sum of values of nodes
- along that particular path.

To solve this problem, we can use Depth-First Search (DFS), a standard tree traversal algorithm that goes as deep as possible in one direction before backtracking. The goal is to traverse the tree from the root to each leaf and accumulate the values of the nodes

find a node's children.

along these paths. Here's the intuition behind the solution approach:

1. Represent the Tree Structure: Since the tree is given as a sequence of integers, we first need to map this representation to one that we can use for DFS. The mapping is based on depth and position. We can use a dictionary to store the nodes, where each key represents the depth and position (without the value digit), and the corresponding value is the node's value. This will help us

each child based on the rules.

2. Implement DFS: We'll define a recursive function that will take a node (represented as an integer with depth and position information) and a running total sum (initially set to 0). The function will perform the following actions:

Otherwise, call the function recursively for the left and right children, increasing the depth and calculating the position for

Check if the current node is a leaf (has no children) and, if so, add the running total sum to the global answer.

checking for the existence of children nodes using the mapping before trying to traverse them. 4. Compute the Result: By running DFS starting from the root, we can compute the sum of all the root-to-leaf paths. The root is

3. Handle Edge Cases: We're guaranteed that the array represents a valid tree. However, we do need to ensure that we're

- represented as 11 since the depth is 1 and position is 1. This way, we can explore all paths, sum their values, and obtain the total sum required by the problem.
- 1. Dictionary Representation: A dictionary, denoted as mp in the code, is created to efficiently store and access nodes using their hundreds and tens digits as keys (representing depth and position) and their units digit as the value. The dictionary

comprehension {num // 10: num % 10 for num in nums} achieves this by dividing each number by 10 (to remove the value

2. Depth-First Search (DFS): The DFS is implemented through a recursive function, dfs(node, t), where node is the current node

being visited and t is the running total sum of values on the path from the root to the current node.

Accumulate the node's value to the running total sum as we traverse down the tree.

3. Node Representation and Child Calculation: Each node is represented as a two-digit number where the first digit correlates to the depth and the second digit corresponds to the position. To find children of a node at depth d and position p, we calculate the

1 and increase to the right.

Here's what each number means:

1. Dictionary Representation:

3. Traversing the Tree:

5. Calculating Results:

Python Solution

class Solution:

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from typing import List

accumulates the total sum of all paths.

Solution Approach

left child as (d + 1) * 10 + (p * 2) - 1 and the right child as 1 + 1. The multiplication and addition here are based on the properties of a binary tree, where each level has twice as many nodes as the previous, and positions start on the leftmost side at

To implement the solution to this problem, a few critical components are used:

digit) and then mapping this to the remainder (the value digit).

value outside the current scope, a nonlocal declaration (nonlocal ans) is used to modify the ans variable, which holds the total path sum, within the recursive function. Finally, the DFS is kicked off from the root of the tree, which always has a depth and position of 1 (hence node 11), and an initial total

path sum of 0. The accumulated sum of all paths, stored in ans, is returned as the result after completing all recursions.

6. Global Variable: Since Python doesn't support passing primitives by reference, and updating a local variable won't affect its

4. Leaf Check and Sum Accumulation: The function checks to see if the current node is a leaf, meaning it has no children in the

5. Recursion: The DFS function is called recursively on the node's children, passing the updated total sum t combined with the

current node's value. This is done with dfs(l, t) and dfs(r, t) for the left and right child respectively.

mapping mp. If it's a leaf, the current path's sum (which includes the current node's value) is added to a global variable ans, which

the actual tree structure. **Example Walkthrough**

The efficiency of this approach lies in its use of recursion and the dictionary, which allows constant-time lookups for the existence of

child nodes, as well as the ability to directly calculate children's identifiers from a given node's identifier without needing to construct

• 122: Right child of the root with a value of 2, at depth 2 and position 2. • 131: Left child of node 121 with a value of 1, at depth 3 and position 1 (this is a leaf node). • 132: Right child of node 121 with a value of 2, at depth 3 and position 2 (this is a leaf node).

Suppose we're given the following representation of a binary tree using an array of three-digit integers: [111, 121, 122, 131, 132].

6 14: 2 // Right child of node 12

We define a recursive function dfs(node, t).

dfs(14, 2) respectively since 12 + 1 = 2.

 \circ Our ans turns out to be 3 + 4 = 7.

def pathSum(self, nums: List[int]) -> int:

if node not in tree_map:

total += tree_map[node]

dfs(right_child, total)

answer = 0

dfs(11, 0)

return answer

right_child = left_child + 1

def dfs(node, total):

return

13: 1, // Left child of node 12

12: 1, // Left child of root

13: 2, // Right child of root

• We create a dictionary mp like so:

2 11: 1, // Root node

2. Implementing DFS:

This maps the depth-position identifier to the node's value.

Let's walk through a simple example to illustrate the solution approach.

• 121: Left child of the root with a value of 1, at depth 2 and position 1.

Now let's map this representation to one suitable for depth-first search:

• 111: Root node with a value of 1, at depth 1 and position 1.

• For the right child 122, we also calculate its identifier as 13 and since it's in mp, we call dfs(13, 1). 4. Summing Path Values:

call dfs(12, 1) (1 being the current total sum plus root's value).

Initially, we call dfs(11, 0) because our root is 111, and our initial total path sum is 0.

Starting with node 11, we check for its children, which are, in theory, 121 (left child) and 122 (right child).

• For the left child 121, we calculate its identifier as 12 (by stripping away the value digit), which is present in mp. Therefore, we

∘ We then traverse to node 121 (12 in mp). We check for children 131 and 132 similarly, ending up calling dfs(13, 2) and

 By recursing through both left and right children for all nodes, we add all the root-to-leaf paths to ans. The paths we have taken are: 111 -> 121 -> 131 and 111 -> 121 -> 132. \circ This results in sums of 1 + 1 + 1 = 3 and 1 + 1 + 2 = 4 respectively.

Both are leaves, so we add their sums (2 + 1) and (2 + 2) to a global variable ans.

Finally, ans contains the sum of the values of all root-to-leaf paths which in our case is 7. This is returned as the result of our problem.

If the current node is not in the tree, stop the recursion

Calculate the node code for the left and right children

Initialize the answer variable to accumulate the total path sums

if left_child not in tree_map and right_child not in tree_map:

Add the current node's value to the running total

left_child = (depth + 1) * 10 + (pos * 2) - 1

tree_map = {num // 10: num % 10 for num in nums}

Return the accumulated total path sums

// Computes the sum of all paths in the tree.

valueMap.put(num / 10, num % 10);

private void dfs(int node, int currentSum) {

if (!valueMap.containsKey(node)) {

currentSum += valueMap.get(node);

// If the node does not exist, return

// Start DFS from the root node, which is always 11

// Performs a depth-first search to calculate all path sums.

// Add the value of the current node to the running sum

// Calculate the node values for the left and right children

sum += nodesMap[nodeId]; // Add the node's value to the running sum.

// Check if the node is a leaf node (i.e., it doesn't have any children)

* Function to calculate the sum of the path values for a binary tree represented by an array.

* @param nums An array representing a binary tree where each element is composed of 3 digits.

// Clear the map before starting the computation.

// Populate the map with node values where key is node id and value is node value.

// Initialize the total path sum.

// Check if the node id exists in the map. If not, return immediately.

// Calculate the ids for the left and right children of the current node.

// Check if the current node is a leaf node (does not have any children).

// Recursively call dfs for the left and right children if they exist.

Each element in the array is visited exactly once to populate the mp dictionary.

const leftChildId: number = (depth + 1) * 10 + (position * 2) - 1;

if (!nodesMap.has(leftChildId) && !nodesMap.has(rightChildId)) {

// Since it's a leaf, add the path sum to the total.

if (!nodesMap.count(leftChildId) && !nodesMap.count(rightChildId)) {

totalPathSum += sum; // Add the sum to the total path sum.

// Compute the current node's depth and position.

int leftChildId = (depth + 1) * 10 + (position * 2) - 1;

// Calculate left and right children's ids.

// Recursive calls for left and right children.

int rightChildId = leftChildId + 1;

1 // Global variable to hold the total sum of path values.

nodesMap.set(Math.floor(num / 10), num % 10);

* Recursive depth-first search function to compute path sums.

// Return the total sum of path values computed.

* @param sum The sum of values along the current path.

// Add the current node's value to the running sum.

const depth: number = Math.floor(nodeId / 10);

const rightChildId: number = leftChildId + 1;

// Calculate the depth and position for the current node.

* @param nodeId The id of the current node.

if (!nodesMap.has(nodeId)) {

totalPathSum += sum;

dfs(leftChildId, sum);

dfs(rightChildId, sum);

return;

sum += nodesMap.get(nodeId) || 0;

const position: number = nodeId % 10;

function dfs(nodeId: number, sum: number): void {

// Start depth-first search at the root node which has id 11.

int depth = nodeId / 10;

return;

Typescript Solution

dfs(leftChildId, sum);

dfs(rightChildId, sum);

11 function pathSum(nums: number[]): number {

totalPathSum = 0;

nodesMap.clear();

nums.forEach(num => {

return totalPathSum;

return;

int position = nodeId % 10;

// Calculate level and position for the current node

Helper function for depth-first search from a given node with cumulative total `total`

If both children are absent, add the current total to the global 'answer'

Create a mapping from node codes (depth and position) to values using list comprehension

Start the DFS traversal from the root node (code 11) with an initial total of 0

private int totalPathSum; // Use a more descriptive name for the variable 'ans'.

private Map<Integer, Integer> valueMap; // Rename 'mp' to 'valueMap' for clarity.

depth, pos = divmod(node, 10) # Split the node code into depth and positional information

nonlocal answer 18 19 answer += total 20 return 21 # Recurse on the left and right children 22 dfs(left_child, total)

// Dividing by 10 gives us the {node level}{node position}, modulo 10 gives us the value at that node

public int pathSum(int[] nums) { totalPathSum = 0; valueMap = new HashMap<>(nums.length); // Store each value in a map with its key as {node level}{node position} 10 for (int num : nums) { 11

dfs(11, 0);

return totalPathSum;

return;

int level = node / 10;

int position = node % 10;

Java Solution

class Solution {

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int leftChild = (level + 1) * 10 + (position * 2) - 1;
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           int rightChild = leftChild + 1;
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           // If the node is a leaf node, add the running sum to the total path sum
           if (!valueMap.containsKey(leftChild) && !valueMap.containsKey(rightChild)) {
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               totalPathSum += currentSum;
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               return;
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           // Continue DFS on the left and right children
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           dfs(leftChild, currentSum);
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           dfs(rightChild, currentSum);
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49 }
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C++ Solution
  1 class Solution {
    public:
         int totalPathSum; // Holds the total sum of path values
         unordered_map<int, int> nodesMap; // Maps the node id to its value
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  6
         // Main function to calculate the sum of the path values.
         int pathSum(vector<int>& nums) {
             totalPathSum = 0; // Initialize total path sum
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             nodesMap.clear(); // Clear the map before computation
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             // Populate the map with node values. Node id as key and node value as value.
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             for (int num : nums) {
                 nodesMap[num / 10] = num % 10;
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             // Start depth-first search at the root node, which is id 11.
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             dfs(11, 0);
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             // Return the computed total path sum.
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             return totalPathSum;
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         // Recursive depth-first search function to compute path sums.
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         void dfs(int nodeId, int sum) {
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             // Check if node id is not present, and return if it's not.
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             if (!nodesMap.count(nodeId)) {
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                 return;
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```

let totalPathSum: number = 0; 4 // Global map to associate node ids with their values. let nodesMap = new Map<number, number>(); 6 /**

*/

});

dfs(11, 0);

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Time and Space Complexity The provided code defines a method pathSum which computes the sum of all paths in a binary tree represented in a compact array form where an integer xyz represents a node at depth x (1-indexed), position y (1-indexed) within its level, with value z. To calculate the sum of all root-to-leaf paths, the code uses a Depth-First Search (DFS) algorithm. **Time Complexity** The time complexity of the function is O(N), where N is the number of elements in the nums array. This is because:

beyond O(N). **Space Complexity**

The space complexity of the function is O(H), where H is the height of the binary tree represented by the nums array. This accounts for:

Since N can represent a full binary tree, in the worst case, H could be O(logN) because N = 2^H - 1 in a full binary tree.

Considering the most constraining factor, the overall space complexity is O(H). In the context of this problem, since the depth of the

• The space used by the mp dictionary, which is equal to the number of elements in nums, i.e., O(N).

• The maximum depth of the recursion stack, which is equal to the height of the tree H, i.e., O(H).

- tree is limited (in practical scenarios by the binary tree representation), the space complexity due to the call stack may also be considered 0(1) as a constant factor, depending on the constraints of the problem. However, without specific constraints given, we stick with O(H).

• The dfs function is called recursively to explore all possible paths from the root to the leaves. In the worst case, the tree is a full

represent a binary tree with a height where 2^h - 1 is equal to the length of nums, the dfs call does not increase the complexity

binary tree, and dfs will be called exactly 2^h - 1 times, where h is the height of the tree. Since the nums array can at most