33. Search in Rotated Sorted Array

Medium Array Binary Search

Problem Description

nums might have been rotated at some unknown pivot index k, causing the order of elements to change. After the rotation, the part of the array after the pivot index comes before the part of the array before the pivot index. Our goal is to find the index of a given integer target in the rotated array. If the target exists in the array, we should return its index; otherwise, return -1.

Since the array is rotated, a standard <u>binary search</u> won't immediately work. We need to find a way to adapt binary search to

In this problem, we have an integer array nums that is initially sorted in ascending order and contains distinct values. However,

Since the array is rotated, a standard <u>binary search</u> won't immediately work. We need to find a way to adapt binary search to work under these new conditions. The key observation is that although the entire array isn't sorted, one half of the array around the middle is guaranteed to be sorted.

The challenge is to perform this search efficiently, achieving a time complexity of O(log n), which strongly suggests that we

should use <u>binary search</u> or a variation of it.

ntuition

The intuition behind the solution is to modify the <u>binary search</u> algorithm to handle the rotated array. We should focus on the

search, we can determine which part of the array is sorted: the part from the start to the middle or the part from the middle to the end. Once we know which part is sorted, we can see if the target lies in that range. If it does, we adjust our search to stay within the sorted part. If not, we search in the other half.

To implement this, we have two pointers left and right that define the bounds of our search space. At each step, we compare the target with the midpoint to decide on which half to continue our search. There are four cases to consider:

1. If the target and the middle element both lie on the same side of the pivot (either before or after), we perform the standard binary search

property that the rotation splits the array into two sorted subarrays. When we calculate the middle element during the binary

operation.

2. If the target is on the sorted side, but the middle element isn't, we search on the sorted side.

3. If the target is not on the sorted side, but the middle element is, we search on the side that includes the pivot.

- 4. If neither the target nor the middle element is on the sorted side, we again search on the side including the pivot.

 By repeatedly narrowing down the search space and focusing on either the sorted subarray or the subarray containing the
- By repeatedly narrowing down the search space and focusing on either the sorted subarray or the subarray containing the pivot, we can find the target or conclude it's not present in O(log n) time.
- The solution implements a modified <u>binary search</u> algorithm to account for the rotated sorted array. Below is a step-by-step

Initialize two pointers left and right to represent the search space's bounds. left starts at 0, and right starts at n - 1,

Calculate mid using (left + right) >> 1. The expression >> 1 is equivalent to dividing by 2 but is faster, as it is a bitwise

where n is the length of the input array nums.

Solution Approach

walkthrough of the algorithm as shown in the provided code snippet:

from nums [0] to nums [mid] are sorted in ascending order.

runtime complexity as required by the problem statement.

2. The <u>binary search</u> begins by entering a <u>while</u> loop that continues as long as <u>left < right</u>, meaning there is more than one element in the search space.

- right shift operation.

 4. Determine which part of the array is sorted by checking if nums [0] <= nums [mid]. This condition shows that the elements
- 5. Check if target is between nums [0] and nums [mid]. If it is, that means target must be within this sorted portion, so adjust right to mid to narrow the search space to this sorted part.
- shift the search space to the right half of the array.

 7. If the sorted portion was the right half (nums[mid] < nums[n 1]), check if target is between nums[mid] and nums[n 1].

 Adjust the search space accordingly by either moving left or right depending if the target is in the sorted portion or not.

If the target is not in the sorted portion, it must be in the other half containing the rotation point. Update left to mid + 1 to

9. After exiting the loop, check if nums [left] is the target and return left if that's the case, indicating that the target is found at that index in the array.

If the element at nums [left] is not the target, return -1 to indicate that target is not found in the array.

This binary search modification cleverly handles the rotation aspect by focusing on which part of the search space is sorted and adjusting the search bounds accordingly. No additional data structures are used, and the algorithm strictly follows an O(log n)

Let's illustrate the solution approach with a small example. Assume we have the rotated sorted array nums = [6, 7, 0, 1, 2, 4,

5] and we are looking for the target value 1. The original sorted array before rotation might look something like [0, 1, 2, 4, 5,

We initialize our search bounds, so left = 0 and right = 6 (since there are 7 elements in the array).

6, 7], and in this case, the pivot is at index 2, where the value 0 is placed in the rotated array.

Start the binary search loop. Since left < right (0 < 6), we continue.

Calculate the middle index, mid = (left + right) >> 1. This gives us mid = 3.

This loop continues until the search space is narrowed down to a single element.

4. Check if the left side is sorted by checking if nums[left] <= nums[mid] (comparing 6 with 1). It is false, so the left-half is not sorted, the right-half must be sorted.

Since 1 (our target) is less than 6 (the value at nums [left]), we know the target is not in the left side. We now look into the

Re-evaluate mid in the next iteration of the loop. Now mid = (left + right) >> 1 = (4 + 6) >> 1 = 5. The middle element

Check again where the sorted part is. Now nums [left] <= nums [mid] (1 <= 4) is true, which means we are now looking at the

right half since the rotation must have happened there. 6. Update left to mid + 1, which gives left = 4.

at index 5 is 4.

10.

Python

class Solution:

Example Walkthrough

10.

- sorted part of the array.

 9. Check if the target is within the range of nums[left] and nums[mid]. Here, 1 is within 1 to 4, so it must be within this range.
- Continue the loop. At this point, left = 4 and right = 5, mid = (4 + 5) >> 1 = 4. The value at nums [mid] is the target we are looking for (1).
 Since nums [mid] is equal to the target we return mid, which is 4.

Using this approach, we successfully found the target 1 in the rotated sorted array and return the index 4. This example

demonstrates the modified binary search algorithm used within the rotated array context.

mid = (left + right) // 2 # Updated to use floor division for clarity

if nums[mid] < target <= nums[-1]: # Use -1 for last element index</pre>

Determine if the mid element is in the rotated or sorted part

If target is between mid and last element, go right

If target is between the first element and mid, go left

- Solution Implementation
- # Use binary search to find the target
 while left < right:
 # Calculate the middle index</pre>

if nums[0] <= target <= nums[mid]:</pre>

def search(self, nums: List[int], target: int) -> int:

left, right = 0, len(nums) - 1

if nums[0] <= nums[mid]:</pre>

Else, go right

Else, go left

right = mid

else:

else:

else:

right = mid

left = mid + 1

left = mid + 1

start = mid + 1;

return nums[start] == target ? start : -1;

int search(vector<int>& nums, int target) {

// Define the initial search range

if (nums[0] <= nums[mid]) {</pre>

right = mid;

// Search right side

left = mid + 1;

left = mid + 1;

right = mid;

// Search left side

int left = 0, right = size - 1;

int size = nums.size();

// Perform binary search

} else {

} else {

} else {

while (left < right) {</pre>

// Initialize the size of the input vector

end = mid;

} else {

Initialize the boundary indexes for the search

Now we update right to mid, setting right = 5.

```
# Check if the left index matches the target, otherwise return -1
        return left if nums[left] == target else -1
Java
class Solution {
    public int search(int[] nums, int target) {
       // Length of the array.
       int arrayLength = nums.length;
       // Initialize start and end pointers.
        int start = 0, end = arrayLength - 1;
       // Binary search algorithm to find target.
       while (start < end) {</pre>
            // Calculate middle index of the current segment.
            int mid = (start + end) / 2;
            // When middle element is on the non-rotated portion of the array.
            if (nums[0] <= nums[mid]) {</pre>
                // Check if the target is also on the non-rotated portion and adjust end accordingly.
                if (nums[0] <= target && target <= nums[mid]) {</pre>
                    end = mid;
                } else {
                    start = mid + 1;
            // When middle element is on the rotated portion of the array.
            } else {
```

// Check if the target is also on the rotated portion and adjust start accordingly.

int mid = left + (right - left) / 2; // Avoids potential overflow compared to (left + right) >> 1

// Target is within the left (non-rotated) range, search left side

// Target is within the right (rotated) range, search right side

if (nums[mid] < target && target <= nums[arrayLength - 1]) {</pre>

// After narrowing down to one element, check if it's the target.

// Find the middle index of the current search range

// Determine the side of the rotated sequence 'mid' is on

if (nums[0] <= target && target <= nums[mid]) {</pre>

// 'mid' is in the left (non-rotated) part of the array

// 'mid' is in the right (rotated) part of the array

if (nums[mid] < target && target <= nums[size - 1]) {</pre>

// If nums[start] is the target, return its index, otherwise return -1.

```
}
}
// The final check to see if the target is found at 'left' index
return (left == right && nums[left] == target) ? left : -1;
```

C++

public:

class Solution {

```
return (left == right && nums[left] == target) ? left : −1;
  };
  TypeScript
  function search(nums: number[], target: number): number {
      const length = nums.length;
      let leftIndex = 0;
      let rightIndex = length - 1;
      // Use binary search to find the target
      while (leftIndex < rightIndex) {</pre>
          // Calculate the middle index
          const midIndex = Math.floor((leftIndex + rightIndex) / 2); // shifted to use Math.floor for clarity
          // Check if the first element is less than or equal to the middle element
          if (nums[0] <= nums[midIndex]) {</pre>
              // If target is between the first element and middle element
              if (nums[0] <= target && target <= nums[midIndex]) {</pre>
                  // Narrow down the right bound
                  rightIndex = midIndex;
              } else {
                  // Target must be in the second half
                   leftIndex = midIndex + 1;
          } else {
              // If target is between the middle element and the last element
              if (nums[midIndex] < target && target <= nums[length - 1]) {</pre>
                  // Narrow down the left bound
                   leftIndex = midIndex + 1;
              } else {
                  // Target must be in the first half
                  rightIndex = midIndex;
      // Check if we have found the target
      return nums[leftIndex] == target ? leftIndex : -1;
class Solution:
   def search(self, nums: List[int], target: int) -> int:
        # Initialize the boundary indexes for the search
        left, right = 0, len(nums) - 1
        # Use binary search to find the target
        while left < right:</pre>
            # Calculate the middle index
            mid = (left + right) // 2 # Updated to use floor division for clarity
            # Determine if the mid element is in the rotated or sorted part
            if nums[0] <= nums[mid]:</pre>
                # If target is between the first element and mid, go left
                if nums[0] <= target <= nums[mid]:</pre>
                    right = mid
                # Else, go right
```

return left if nums[left] == target else -1 Time and Space Complexity

Time Complexity

else:

else:

else:

left = mid + 1

left = mid + 1

Else, go left

right = mid

If target is between mid and last element, go right

Check if the left index matches the target, otherwise return -1

if nums[mid] < target <= nums[-1]: # Use -1 for last element index</pre>

needed for variables left, right, mid, and n, regardless of the size of the input array nums.

The given code performs a binary search over an array. In each iteration of the while loop, the algorithm splits the array into half, investigating either the left or the right side. Since the size of the searchable section of the array is halved with each iteration of the loop, the time complexity of this operation is $O(\log n)$, where n is the number of elements in the array nums.

Space Complexity

The space complexity of the algorithm is 0(1). The search is conducted in place, with only a constant amount of additional space