

Hash Table

Matrix

In this problem, we are provided with a binary matrix, meaning that each cell in the matrix contains either 0 or 1. Our goal is to

maximize the number of rows that are all made up of the same value, either all 0s or all 1s, by performing a certain operation. The

Problem Description

3 0 1 1

operation allowed is flipping the values in a column; flipping transforms all 0s to 1s and all 1s to 0s in that particular column.

You can flip, for instance, the second and third columns to get:

To visualize, imagine you have a matrix like this:

Thus, you would have 2 rows with all values equal.

Intuition

mapping each row to a unified pattern representation and counting the occurrences of these patterns.

The problem asks us to find the maximum number of such rows possible after performing any number of flips.

actually care about the original values but rather the pattern of the rows, because any row pattern (i.e., sequence of zeros and ones) can be flipped to its inverse. Thus, two rows that are inverses (complements) of each other will become identical after flipping the

same set of columns. Therefore, the key insight is that we can pair rows that are identical or are inverses of each other because they can be made equal with the flip operation. If we represent a row by a tuple, we can ensure that if the first element is 0, we keep it as is, and if the first element is 1, we invert the entire row. We do this because the first element determines the flip pattern we should use: if it's 0, no flip is needed for the first column, but if it's 1, we should flip the first column.

The intuition behind the solution is based on an observation about flipping columns. When we flip columns in a matrix, we don't

The approach uses a Counter to keep track of how many identical or invertible row patterns there are. It iterates through each row in the matrix, treating it directly if it starts with a 0 or treating the inverted row (flipping all bits) if it starts with a 1. The Counter will then have counts of how many times a certain pattern (or its inverse) appears in the matrix. The maximum of these counts is the number of rows that can be made equal by flipping the specified columns. In summary, we rely on patterns and their complements to determine how many rows can be made equal through column flips by

Solution Approach The implementation utilizes a Counter from the collections module in Python, which is a subclass of dict designed to count hashable objects. It implicitly counts how often each key is encountered. In the context of this problem, each key in the Counter will

Here is a breakdown of the steps involved in the implementation:

1. Initialization: Create a new Counter object named cnt. 2. Processing Rows:

For each row, check the first element:

Iterate over each row in the input matrix.

be a pattern (tuple) representing a row in the matrix after potentially inverting it.

- If it is 0, use the row as is.
- 1 and 1 to 0. 3. Counting Patterns:

use as a key in the Counter.

Counter.

its complement in the matrix. 4. Finding the Maximum Count:

After all rows are processed and counted, determine the maximum count using the max function on the values() of the

Convert the row (either used directly or inverted) to a tuple, which acts as an immutable and hashable object suitable for

o Increment the count of this tuple in cnt. This step essentially counts how many times we have seen this particular pattern or

■ If it is 1, create a new tuple by flipping each element. The bitwise XOR operator ^ is used to flip bits - x ^ 1 changes 0 to

In essence, by using a Counter to tally row patterns, we are mapping the problem onto a frequency-count problem. Instead of directly manipulating the matrix, which would be costly, we represent each row by a pattern that considers flips and then look for the most common pattern. This drastically simplify the problem and allows us to find the solution efficiently.

This maximum count represents the largest number of rows that can be made equal by flipping columns.

- Example Walkthrough
 - Matrix:
- Following the solution approach step by step:

2. Processing Rows:

Second row: 1 1 0

1. Initialization:

First row: 0 1 0

The first element is 0, so we use the row as is and move to step 3.

■ The first element is 1, so we flip the entire row using the XOR operator: 0 1 0.

We start by iterating over each row in the input matrix.

We create an empty Counter object named cnt.

Let's walk through the solution approach using a small example of a binary matrix:

- The first element is 1, so we flip the entire row using the XOR operator: 0 0 1. Third row: 1 0 1
- 3. Counting Patterns:

We convert each row into a tuple for counting.

Increment cnt[(0, 1, 0)] by 1.

First row becomes the tuple (0, 1, 0).

achieving our goal.

class Solution:

Java Solution

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 Second row (flipped) becomes the tuple (0, 0, 1). Increment cnt[(0, 0, 1)] by 1.

Third row (flipped) becomes the tuple (0, 1, 0) (same as the first row).

Increment cnt[(0, 1, 0)] by 1 again. Now cnt[(0, 1, 0)] is 2.

Our Counter now has two keys with counts: [(0, 1, 0): 2, (0, 0, 1): 1].

4. Finding the Maximum Count: We find the maximum count in cnt, which in this case is 2 corresponding to the pattern (0, 1, 0).

def maxEqualRowsAfterFlips(self, matrix: List[List[int]]) -> int:

Iterating through each row in the matrix

Python Solution from collections import Counter

Standardizing the row:

return max(row_counter.values())

// The number of columns in the matrix

// Iterate over each row in the matrix

// Create a character array to represent the pattern

// Build the pattern based on the first element in the row

// Update the pattern frequency map with the new pattern,

maxEqualRows = Math.max(maxEqualRows, patternCount);

int patternCount = patternFrequency.merge(pattern, 1, Integer::sum);

// Return the maximum number of equal rows that can be obtained after flips

// Update maxEqualRows if the current pattern count is greater

char[] patternChars = new char[columnCount];

String pattern = String.valueOf(patternChars);

// incrementing the count of the pattern by 1

for (int i = 0; i < columnCount; ++i) {</pre>

int columnCount = matrix[0].length;

for (int[] row : matrix) {

return maxEqualRows;

row_counter = Counter()

for row in matrix:

If the first element is 0, keep the row unchanged; otherwise flip all bits standardized_row = tuple(row) if row[0] == 0 else tuple(1 - x for x in row) # Updating the counter for the standardized row row_counter[standardized_row] += 1

Returning the maximum frequency found in the counter as the result

Initializing a counter to keep track of the frequency of each standardized row

1 class Solution { public int maxEqualRowsAfterFlips(int[][] matrix) { // HashMap to keep track of the frequency of each unique pattern Map<String, Integer> patternFrequency = new HashMap<>(); // Variable to keep track of the max number of equal rows after flips int maxEqualRows = 0;

Following these steps, we determine that the maximum number of rows with all values equal after flipping any number of columns is

2. In this case, if we flip the first and the last columns of the original matrix, we can make the first and third rows identical (all zeros),

// XOR the first element with each element in the row 16 17 // If row[0] == row[i], the result will be 0; otherwise, it will be 1 patternChars[i] = (char) ('0' + (row[0] ^ row[i])); 18 19 20 // Convert the character array to a string representing the pattern

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C++ Solution
 1 #include <vector>
 2 #include <string>
 3 #include <unordered_map>
   #include <algorithm>
   using namespace std;
   class Solution {
   public:
       int maxEqualRowsAfterFlips(vector<vector<int>>& matrix) {
           unordered_map<string, int> patternCount; // This will map row patterns to their counts
            int maxEqualRows = 0; // This will keep track of the maximum number of equal rows
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           // Iterate through rows of the matrix
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           for (auto& row : matrix) {
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               string pattern; // Initialize an empty string to store the row pattern
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               // Build the pattern for the given row considering flips
               for (int cell: row) {
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                   // If the first cell is 0, keep the number as is; otherwise flip the number
                    char representation = '0' + (row[0] == 0 ? cell : cell ^ 1);
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                    pattern.push_back(representation);
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               // Increase the count for the current pattern
               int currentCount = ++patternCount[pattern];
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               // Update maxEqualRows if the current pattern count exceeds it
               maxEqualRows = max(maxEqualRows, currentCount);
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            return maxEqualRows; // Return the maximum number of equal rows after flips
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32 };
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// If the first element of the row is a 1, we flip the entire row to make sorting consistent. 12 13 if (row[0] === 1) { // Perform the flip by XOR'ing each element in the row with 1. 14 for (let i = 0; i < row.length; i++) { 15 16

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Typescript Solution

for (const row of matrix) {

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row[i] ^= 1;
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           // Convert the row to a string to use as a key in the map.
           const rowString = row.join('');
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           // Update the count in the map for the given row pattern.
21
           // If it doesn't exist yet, initialize to 0 then add 1, else increment the current count.
           countMap.set(rowString, (countMap.get(rowString) | | 0) + 1);
24
           // Update maxEqualRows with the maximum of the current value and the new count for this pattern.
25
           maxEqualRows = Math.max(maxEqualRows, countMap.get(rowString)!);
26
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       // Return the highest frequency of equal row patterns after flips.
       return maxEqualRows;
30 }
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Time and Space Complexity
Time Complexity
The time complexity of the given code is primarily determined by the number of iterations through each row of the matrix and
operations performed for each row. Since we iterate once over each row, and for each row, we either take the tuple as-is if the
starting element is 0 or iterate once more through the row to flip each bit and create a tuple, the time per row is O(N) where N is the
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* Determines the maximum number of rows that can be made equal after a series of flips.

const countMap = new Map<string, number>(); // Map to store the frequency of each row pattern.

* Flips can be performed on an entire row which flips all 0s to 1s, and vice versa.

* @returns {number} - The maximum number of rows that can be made equal by flipping.

let maxEqualRows = 0; // Variable for tracking the maximum number of equal rows.

* @param {number[][]} matrix - The 2D array on which flips are performed.

function maxEqualRowsAfterFlips(matrix: number[][]): number {

number of columns. With M being the number of rows, iterating over all rows results in a time complexity of O(M * N).

and remains 0(M * N).

In all, the space complexity of the algorithm is O(M * N).

Space Complexity The space complexity depends on the space required to store the counter dictionary and the tuples created for each row. Each tuple

Furthermore, the max function that is called on the Counter object takes O(U) time, where U is the number of unique rows after

normalizing which in the worst case could be M. Thus, the overall time complexity combines the row iterations and the max function,

can have at most N elements, and in the worst case, we could have M unique tuples if no two rows are the same or opposites. Therefore, the space complexity is 0 (M * N), since M tuples of N elements each may need to be stored in the counter dictionary.