2465. Number of Distinct Averages

Two Pointers

Sorting

Problem Description

Hash Table

series of operations until the array becomes empty. In each operation, we must remove the smallest and the largest numbers from the array then calculate their average. This process is repeated until no numbers are left in the array. Our goal is to determine how many *distinct averages* we can get from these operations. It is important to note that in case of multiple instances of the minimum or maximum values, any occurrence of them can be removed.

Intuition

The given problem involves an array of integers nums, which has an even number of elements. We are instructed to perform a

Considering that we need to find the minimum and maximum values of the array to calculate averages, a straightforward

Easy

approach would be to sort the array first. With the array sorted, the minimum value will always be at the beginning of the array, and the maximum value will be at the end.

By <u>sorting</u> the array, we simplify the problem as follows:

• The maximum number will be nums [-1], the second-largest nums [-2], and similar for the other elements.

complexity of O(n log n) due to the sorting step.

Here's a step-by-step explanation of the solution:

After each operation of removing the smallest and largest elements, the subsequent smallest and largest elements become the

• The minimum number of the array will be nums [0], the second smallest nums [1], and so on.

adjacent values (the next elements in the sorted array). Therefore, we avoid the need for repeated searching for min and max in an unsorted array.

To find the distinct averages:
 We iterate over half of the list (len(nums) >> 1), since every operation removes two elements.
 For each iteration, we calculate the average of nums[i] and nums[-i - 1], which is effectively the average of the ith smallest and ith largest

• We use a set to collect these averages, which automatically ensures that only distinct values are kept.

value in the array.

- The length of this set is the number of distinct averages we have calculated, which is what we want to return.

 This algorithm is efficient because it sorts the array once, and then simply iterates through half of the array, resulting in a
- Solution Approach

The solution uses Python's built-in <u>sorting</u> mechanism to organize the elements in <u>nums</u> from the smallest to the largest. By sorting the array, the algorithm simplifies the process of finding the smallest and largest elements in each step.

First, nums.sort() is called to sort the array in place. After the sort, nums[0] will contain the smallest value, and nums[-1] will contain the largest value, and so on for the ith smallest and ith largest elements.

bit-shift to the right.

- The generator expression (nums[i] + nums[-i 1] for i in range(len(nums) >> 1)) then iterates through the first half of the elements in the sorted list. The expression len(nums) >> 1 is an efficient way to divide the length of nums by 2, using a
- to finding the sum of the elements at the symmetric positions from the start and the end of the sorted array.

 This sum is divided by 2 to calculate the average, but since the division by 2 is redundant when only interested in uniqueness (it does not affect whether the values are unique), it is not performed explicitly.

In each iteration, nums[i] + nums[-i - 1] calculates the sum of the ith smallest and ith largest element, which is equivalent

All of these sums (representing the averages) are then collected into a set. As sets only store distinct values, any duplicate

- Finally, len(set(...)) returns the number of distinct elements in the set, which corresponds to the number of distinct averages that were calculated.
 In terms of data structures and patterns used:
- This solution is particularly elegant because it leverages the sorted order of the array and the property of set collections to avoid unnecessary computations and simplify logic.

The problem requires us to continually remove the smallest and largest numbers, calculate their average, and determine the

number of distinct averages we can get from these operations. Let's walk through this step by step:

Suppose we have the following array:

Example Walkthrough

nums = [1, 3, 2, 6, 4, 5]

averages = set()

Iteration example:

averages = $\{7\}$

Python

set, it's not added again.

Solution Implementation

nums.sort()

Sort the input list of numbers

unique_averages = set()

Initialize an empty set to store unique averages

average = nums[i] + nums[-i - 1]

unique_averages.add(average)

public int distinctAverages(int[] nums) {

// Sort the array to facilitate pairing of elements

// Create an array to count distinct averages.

return len(unique_averages)

int[] count = new int[201];

#include <algorithm> // For std::sort

int distinctAverages(vector<int>& nums) {

// the frequency of the sum of pairs.

// Obtain the size of the input vector.

for (int i = 0; $i < numElements / 2; ++i) {$

if (++countArray[pairSum] == 1) {

// Return the count of distinct averages.

++distinctCount;

sort(nums.begin(), nums.end());

int numElements = nums.size();

int countArray[201] = {};

int distinctCount = 0;

// Sort the input vector in non-decreasing order.

// Initialize a count array of size 201 to store

// Initialize a variable to store the count of distinct averages.

int pairSum = nums[i] + nums[numElements - i - 1];

// Loop through the first half of the vector as we are creating pairs

// that consist of one element from the first half and one from the second.

// If this sum appears for the first time, increase the distinct count.

// Calculate the sum of the current pair: the i-th element and its corresponding

// element in the second half of the array (mirror position regarding the center).

#include <vector>

class Solution {

public:

using namespace std;

Return the number of unique averages

Calculate the average of each pair of numbers, one from the start

for i in range(len(nums) // 2): # Integer division to get half-way index

Add the calculated sum (which represents an average) to the set

We don't actually divide by 2 since it's the average of two nums and

we are interested in distinct averages. The div by 2 won't affect uniqueness.

and one from the end of the list, moving towards the middle

Calculate the sum of the pair and add it to the set.

Step 1: Sort the array. Sorting the array in increasing order will give us:

Step 3: Remove the smallest and largest numbers and calculate their averages.

Since there are six elements, we iterate over half of that, which is three elements.

Let's use a small example to illustrate the solution approach described above.

averages calculated during the iteration will only appear once.

An array/list data structure is the primary structure utilized.

• A set is used to deduplicate values and count distinct elements.

• Sorting is the main algorithmic pattern applied.

length_half = len(nums) >> 1 # Equivalent to dividing the length of nums by 2
for i in range(length_half):

nums.sort() # After sorting: [1, 2, 3, 4, 5, 6]

Step 2: Initialize an empty set to store unique averages.

minimum = nums[i] # ith smallest after sorting

maximum = nums[-i - 1] # ith largest after sorting
We calculate the sum since the division by 2 won't affect uniqueness
avg = minimum + maximum
averages.add(avg) # Add the sum (representing the average) to the set of unique averages

```
First iteration for i=0: minimum is nums [0] which is 1; maximum is nums [-1] which is 6. Their sum is 1 + 6 = 7. Add 7 to the set of averages.
Second iteration for i=1: minimum is nums [1] which is 2; maximum is nums [-2] which is 5. Their sum is 2 + 5 = 7. As 7 is already present in the
```

Step 5: Get the number of unique averages. Finally, we get the unique count by measuring the length of the set averages:

unique_averages_count = len(averages) # This will be 1

Based on this example, even though we calculated the average (its sum representation) three times, our set contains only one

element. Therefore, the number of distinct averages in the nums array we started with is 1.

Step 4: The set of averages now has distinct sums. After the iterations, our set of averages will be:

• Third iteration for i=2: minimum is nums [2] which is 3; maximum is nums [-3] which is 4. Their sum is 3 + 4 = 7. Again, already present.

This example illustrates that the solution approach is efficient and avoids unnecessary complexity by using sorting, taking

advantage of the properties of the set, and simplifying the problem into one that can be solved in linear time after sorting.

from typing import List

class Solution:
 def distinct_averages(self, nums: List[int]) -> int:

Java

Arrays.sort(nums);

class Solution {

```
// Get the length of the nums array
       int n = nums.length;
       // Initialize the variable to store the number of distinct averages
       int distinctCount = 0;
       // Loop through the first half of the sorted array
        for (int i = 0; i < n / 2; ++i) {
           // Calculate the average of the ith and its complement element (nums[i] + nums[n - i - 1])
           // and increase the count for this average.
           // We do not actually compute the average to avoid floating point arithmetic
           // since the problem seems to be working with integer addition only.
           int sum = nums[i] + nums[n - i - 1];
           if (++count[sum] == 1) {
               // If the count of a particular sum is 1, it means it is distinct, increase the distinctCount
               ++distinctCount;
       // Return the total count of distinct averages found
       return distinctCount;
C++
```

// Since the problem constraints are not given, assuming 201 is the maximum value based on the given code.

```
return distinctCount;
  };
  TypeScript
  // This function calculates the number of distinct averages that can be formed
  // by the sum of pairs taken from the start and end of a sorted array.
  function distinctAverages(nums: number[]): number {
      // Sort the array in non-decreasing order
      nums.sort((a, b) \Rightarrow a - b);
      // Initialize a frequency array to keep track of the distinct sums
      const frequency: number[] = Array(201).fill(0);
      // Variable to hold the number of distinct averages
      let distinctCount = 0;
      // Determine the length of 'nums' array
      const length = nums.length;
      // Iterate over the first half of the sorted array
      for (let i = 0; i < length >> 1; ++i) {
          // Calculate the sum of the current element and its corresponding element from the end
          const sum = nums[i] + nums[length - i - 1];
          // Increase the frequency count for the calculated sum
          frequency[sum]++;
          // If this is the first time the sum appears, increment the distinctCount
          if (frequency[sum] === 1) {
              distinctCount++;
      // Return the total number of distinct averages
      return distinctCount;
from typing import List
class Solution:
   def distinct_averages(self, nums: List[int]) -> int:
       # Sort the input list of numbers
        nums.sort()
       # Initialize an empty set to store unique averages
```

The time complexity of the code above is $O(n \log n)$ and the space complexity is O(n).

Time Complexity

unique_averages = set()

average = nums[i] + nums[-i - 1]

unique_averages.add(average)

return len(unique_averages)

Time and Space Complexity

Return the number of unique averages

2. The list comprehension set(nums[i] + nums[-i - 1] for i in range(len(nums) >> 1)) iterates over the sorted list but only up to the halfway point, which is n // 2 iterations. Although the iteration is linear in time with respect to the number of

nums.sort(): Sorting the list of n numbers has a time complexity of O(n log n).

Calculate the average of each pair of numbers, one from the start

for i in range(len(nums) // 2): # Integer division to get half-way index

Add the calculated sum (which represents an average) to the set

We don't actually divide by 2 since it's the average of two nums and

we are interested in distinct averages. The div by 2 won't affect uniqueness.

and one from the end of the list, moving towards the middle

Calculate the sum of the pair and add it to the set.

elements it processes, the dominant term for time complexity comes from the sorting step. Therefore, combining both steps we get $O(n \log n)$, which is the overall time complexity.

itself (0(1) space).

- Space Complexity1. The sorted in-place method nums.sort() does not use additional space other than a few variables for the sorting algorithm
- 2. The list comprehension inside the set function creates a new list with potentially n / 2 elements (in the worst-case scenario, where all elements are distinct before combining them), and then a set is created from this list. The space required for this

set is proportional to the number of distinct sums, which is also up to n / 2. Hence, this gives us a space complexity of O(n).

Combining both considerations, the overall space complexity is O(n). This accounts for the space needed to store the unique sums in the worst-case scenario where all sums are distinct.