Problem Description

cells (or 0s) that are connected horizontally or vertically (4-directionally). A closed island is an island that is completely surrounded by water (1s), meaning it does not touch the edge of the grid at any point. The goal is to count how many closed islands are present in the grid. For example, a 0 that is at the edge of the grid could be part of

The problem presents a two-dimensional grid which consists of both land (0s) and water (1s). An island is defined as a group of land

Matrix

an island, but since it is touching the boundary, it cannot be considered a closed island.

Intuition To solve this problem, we can perform a depth-first search (DFS) on each cell that is land (0). When we perform a DFS, we recursively visit each connected land cell and mark them as water (1) to avoid revisiting them. While performing the DFS, we also

check if we ever touch the boundary of the grid (i.e., the row index i is 0 or m-1 or the column index j is 0 or m-1). If the DFS starts

The function dfs(i, j) is designed to perform this task, where i and j are the row and column indices, respectively. This function

from a cell that never touches the boundary, it means we are on a closed island, and thus we should count it.

marks the current cell as visited by setting grid[i][j] to 1. It then checks in all four directions and calls itself (the dfs function) on any connected land cell it finds. If any recursive call to dfs encounters the boundary, it propagates back a failure to recognize the island as closed by returning 0 (when bitwise & operator is applied). If an island is completely surrounded by water and doesn't touch the boundary at any point, dfs returns 1.

The pairwise(dirs) function combined with the surrounding for loop is a slight mistake in the code, possibly due to a misunderstanding of Python's itertools.pairwise, which doesn't apply here. Instead, it should loop over pairs of directions (like (dirs[k], dirs[k + 1]) for k in range 4) to check all four neighboring cells. The final count of closed islands is obtained by initializing a sum with a generator expression that iterates over every cell in the grid

and calls the dfs function if a land cell (0) is found. The result of dfs will only be 1 for cells that are part of a closed island, and thus the sum represents the total number of closed islands in the grid. Note: The code provided seems to have a mistake with the pairwise(dirs) portion, which does not align with standard Python functions. The intention here might be to iterate over the directions in pairs to traverse up, right, down, and left in the grid.

The solution applies the depth-first search (DFS) algorithm to explore the grid and identify islands that are closed. Here's a step-bystep breakdown of the implementation:

1. Initialization: A DFS function is defined, which will be used to explore the grid. Additionally, the size of the grid is noted in

variables m (for rows) and n (for columns). The dirs array (which should contain pairs of directions to move up, right, down, and

left) is used to facilitate the exploration of neighboring cells.

Solution Approach

2. Depth-First Search (DFS): The core of the solution is in the dfs function, which takes a cell (i, j) and: Marks it as visited by setting grid[i][j] = 1.

- Iterates in all four directions based on the dirs array, and if an adjoining cell is unvisited land (grid[x][y] == 0), it recurs with these new coordinates. If the recursive exploration touches the grid boundary, it will return 0, indicating this is not a closed island. If the exploration completes without touching the boundary, it returns 1, indicating a closed island.
- 3. Counting Closed Islands: The main function now initializes a sum with a generator expression that loops over each cell in the grid. It calls dfs on cells that are land (0) and adds up the results. Each 1 returned by dfs denotes a closed island.

○ Checks if the cell is within the boundary but not on it, meaning 0 < i < m - 1 and 0 < j < n - 1.

- Here, it is worth noting that the "Reference Solution Approach" mentioned Union find. While the given solution does not utilize this
- pattern, it's relevant to acknowledge that Union find is another approach that can solve this problem. Union find, or disjoint-set data structure, would allow us to group land cells into disjoint sets and then count sets that do not touch the boundary of the grid, which effectively would identify closed islands. However, in the provided solution, DFS is used instead, which is an equally valid method for solving this problem.

The effectiveness of the DFS approach lies in its ability to mark and visit each cell only once, ensuring that the solution is efficient,

is a natural fit for problems related to navigating and exploring grids, particularly in searching for connected components, such as

with the time complexity being O(m*n), where m is the number of rows and n is the number of columns in the grid. The DFS algorithm

Example Walkthrough Let's take a small grid as an example to illustrate how the solution approach works. Consider the following grid: 1 1 1 1 1 0 1

6 1 1 1 1 1 1 In this grid, 1 represents water and 0 represents land. We want to find how many closed islands (areas of 0s that do not touch the grid's boundary) there are.

1. We start by defining a dfs function and initializing the grid size, m and n, respectively. In this case, m = 6 (rows) and n = 6

2. We iterate over each cell in the grid. When we come across a land cell (0), we start the DFS process from it by calling our dfs function.

(columns).

5 1 0 0 1 1 1 6 1 1 1 1 1 1

islands in this context.

4. The DFS explores all connected land cells. For this example, it would change the following cells to 1:

it to 1. DFS checks the neighboring cells in four directions (up, down, left, right) based on a pair of directions.

3. We call the dfs function on the land cell in the second row, second column (grid[1][1]). The cell is marked as visited by setting

5. The DFS does not reach the boundary for this group of land cells, so it counts as one closed island.

6. The next unvisited land cell initiates another DFS call which is on the fourth row, fourth column (grid[3][3]). The process is

similar; it explores connected land cells:

The DFS algorithm efficiently identified areas that constitute closed islands, ensuring no cell is visited more than once, resulting in a

time complexity of O(m*n). While the pairwise(dirs) part in the example content is confusing, the logic of the DFS here applies the

At the end of this process, we see that only the first group of land cells (grid[1][1]) constitutes a closed island. Thus, the final count is 1.

Python Solution

class Solution:

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def dfs(row: int, col: int) -> int: 4 # Check if the cell is within the inner part of the grid 5 # Considering the edges can't form a closed island. result = 1 if 0 < row < rows - 1 and 0 < col < cols - 1 else 0

Perform depth-first search to find and mark all cells connected to (i, j).

Define the directions for the DFS. The pairs are (up, right, down, left).

7. However, this time, the DFS touches the boundary at cell (grid[4][1]), so this island is not closed.

8. The final unvisited land cell group starts at grid[4][1] and is similarly adjacent to the boundary.

correct four-directional checks by iterating over each direction pair to look at neighboring cells.

def closedIsland(self, grid: List[List[int]]) -> int:

Mark the current cell as visited

result &= dfs(new_row, new_col)

Get the number of rows and columns in the grid

rows, cols = len(grid), len(grid[0])

if grid[i][j] == 0:

// Explore all 4 adjacent cells

int nextRow = row + directions[k];

int nextCol = col + directions[k + 1];

&& grid[nextRow][nextCol] == 0) {

// Verify if the adjacent cell is within the grid and if it is land (0)

if (nextRow >= 0 && nextRow < height && nextCol >= 0 && nextCol < width</pre>

return isClosed; // Return 1 if the island is closed, otherwise 0

// Perform DFS on the adjacent cell and use logical AND to update the isClosed status

isClosed &= dfs(nextRow, nextCol); // If any part touches the border, it's not closed

for (int k = 0; k < 4; ++k) {

Initialize the count of closed islands

directions = (-1, 0, 1, 0, -1)

grid[row][col] = 1

return result

closed_islands = 0

Explore all four directions (up, right, down, left) 13 for direction in range(4): 14 new_row = row + directions[direction] 15 new_col = col + directions[direction + 1] 16 17 # If the new cell is within the grid and not visited 18 if 0 <= new_row < rows and 0 <= new_col < cols and grid[new_row][new_col] == 0:</pre>

Continue the DFS and use logical AND to ensure all connected cells are closed

Perform DFS from the current cell and check if it forms a closed island

31 32 # Iterate over each cell of the grid 33 for i in range(rows): 34 for j in range(cols): 35 # If the cell is land (0) and has not been visited

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38
                         closed_islands += dfs(i, j)
 39
 40
             # Return the total count of closed islands
 41
             return closed_islands
 42
Java Solution
    class Solution {
         private int height; // Variable to store the height of the grid
         private int width; // Variable to store the width of the grid
  3
         private int[][] grid; // 2D array to represent the grid itself
  6
         // Function to count the number of closed islands in the grid
         public int closedIsland(int[][] grid) {
             height = grid.length; // Set the height of the grid
  8
             width = grid[0].length; // Set the width of the grid
  9
             this.grid = grid; // Assign the grid argument to the instance variable
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             int count = 0;
                                     // Initialize count of closed islands
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             // Iterate over each cell in the grid
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             for (int i = 0; i < height; ++i) {</pre>
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                 for (int j = 0; j < width; ++j) {
                     // If the current cell is 0 (land), perform a DFS to mark the connected components
 16
                     if (grid[i][j] == 0) {
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                         count += dfs(i, j); // Increment count if the land is part of a closed island
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             return count; // Return the total number of closed islands
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         // Helper method to perform DFS and determine if a connected component is a closed island
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         private int dfs(int row, int col) {
 27
             // If not on the border, assume it's a closed island; otherwise, it's not
             int isClosed = (row > 0 && row < height - 1 && col > 0 && col < width - 1) ? 1 : 0;</pre>
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             grid[row][col] = 1; // Mark the current cell as visited by setting it to 1
 30
             int[] directions = \{-1, 0, 1, 0, -1\}; // Array to help traverse in 4 cardinal directions
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// Calculate the next row index

// Calculate the next column index

public: int closedIsland(vector<vector<int>>& grid) {

C++ Solution

1 class Solution {

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// Get the number of rows and columns in the grid.
             int rowCount = grid.size(), colCount = grid[0].size();
             // Initialize the count of closed islands to zero.
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             int closedIslandCount = 0;
  9
             // Define directions for traversing the grid (up, right, down, left).
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             int directions [5] = \{-1, 0, 1, 0, -1\};
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             // Define a recursive Depth-First Search (DFS) lambda function to find closed islands.
             function<int(int, int)> depthFirstSearch = [&](int row, int col) -> int {
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 15
                 // If the current cell is surrounded by non-border cells, mark as potential closed island.
                 int isClosedIsland = (row > 0 && row < rowCount - 1 && col > 0 && col < colCount - 1) ? 1 : 0;</pre>
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                 // Mark the current cell as visited.
                 grid[row][col] = 1;
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 21
                 // Explore all 4 directions.
 22
                 for (int k = 0; k < 4; ++k) {
                     int nextRow = row + directions[k], nextCol = col + directions[k + 1];
 23
                     // If the next cell is on the grid and unvisited, continue the DFS.
 24
 25
                     if (nextRow >= 0 && nextRow < rowCount && nextCol >= 0 && nextCol < colCount && grid[nextRow][nextCol] == 0) {</pre>
 26
                         // If any recursive DFS call returns 0, then it's not a closed island.
 27
                         isClosedIsland &= depthFirstSearch(nextRow, nextCol);
 28
 29
                 // Return whether the current cell is part of a closed island.
 31
                 return isClosedIsland;
 32
             };
 33
 34
             // Loop over all cells in the grid.
             for (int i = 0; i < rowCount; ++i) {</pre>
 35
                 for (int j = 0; j < colCount; ++j) {</pre>
 36
 37
                     // If the cell is land (0) and the DFS returns true for a closed island, increment the count.
 38
                     closedIslandCount += (grid[i][j] == 0 && depthFirstSearch(i, j));
 39
 40
 41
             // Return the total count of closed islands found.
 42
 43
             return closedIslandCount;
 44
 45
    };
 46
Typescript Solution
  1 // Function to calculate the number of closed islands in a grid.
  2 // A closed island is a group of connected 0s that is completely surrounded by 1s (representing water),
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36 for (let row = 0; row < rowCount; ++row) {</pre> 37 for (let col = 0; col < colCount; col++) {</pre> 38 // If a cell is land and unvisited, perform DFS. if (grid[row][col] === 0) { 39 40 closedIslandsCount += depthFirstSearch(row, col); 41

};

3 // and does not touch the edge of the grid.

6 function closedIsland(grid: number[][]): number {

// Store the dimensions of the grid.

const directions = [-1, 0, 1, 0, -1];

for (let k = 0; k < 4; ++k) {

5 // @returns The count of closed islands.

const rowCount = grid.length;

grid[row][col] = 1;

return isClosed;

let closedIslandsCount = 0;

return closedIslandsCount;

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const colCount = grid[0].length;

4 // @param grid - The 2D grid of 0s (land) and 1s (water).

// DFS function to explore the cells in the grid.

// Directions for traversing up, down, left, and right in the grid.

const depthFirstSearch = (row: number, col: number): number => {

// It's closed only if it doesn't touch the grid's edge.

// Explore all 4 adjacent directions (up, down, left, right).

isClosed &= depthFirstSearch(newRow, newCol);

// Check if the new cell is within bounds and is land (0).

// If any recursive call returns 0, the island isn't closed.

let isClosed = row > 0 && col > 0 && row < rowCount - 1 && col < colCount - 1 ? 1 : 0;

// A flag to indicate if the current island is closed.

// Mark the cell as visited by setting it to 1.

const newCol = col + directions[k + 1];

const newRow = row + directions[k];

// Return whether the island is closed.

// Initialize the count of closed islands.

// Iterate through all cells in the grid.

// Return the final count of closed islands.

Time and Space Complexity The given Python code is a solution for finding the number of "closed islands" in a 2D grid, where 0 represents land and 1 represents water. A "closed island" is one that is surrounded by water and doesn't touch the edge of the grid. The algorithm uses Depth-First

if (newRow >= 0 && newCol >= 0 && newRow < rowCount && newCol < colCount && grid[newRow][newCol] === 0) {</pre>

because the algorithm potentially visits each cell in the grid once. The DFS is started only if the current cell is a 0 (land), and then it marks every visited land cell as 1 (water) to prevent revisiting. In the worst case, all cells in the grid will be traversed once.

not affecting the overall space complexity.

Time Complexity

Search (DFS) to explore the grid.

Space Complexity

The time complexity of the code is 0(m * n), where m is the number of rows and n is the number of columns in the grid. This is

space is used by the recursion call stack during the depth-first search. However, if we consider that modern Python implementations use a technique called "tail-recursion elimination" in some cases, the

The space complexity of the DFS is 0(m * n) in the worst case. This might happen when the depth of the recursion stack grows

proportionally to the number of cells in the worst-case scenario, such as when the grid forms a large area of contiguous land. The

space complexity can be effectively less than 0(m * n) for some grids because not all calls will result in an additional stack frame. But in the analysis of DFS, it is conventional to consider the worst-case scenario regarding recursion. The additional space used by the dirs variable and a few integer variables is negligible compared to the recursive stack space, thus