876. Middle of the Linked List

Easy Linked List Two Pointers

Problem Description

linked list is a collection of nodes where each node contains a value and a reference to the next node in the sequence. The key characteristic of this list is that you can only traverse it in one direction: from the head towards the end.

The task is to write a function that, given the head of a singly linked list, finds and returns the middle node of the list. A singly

The challenge here is determining the middle node in a single pass, since the size of the list is not given in advance. It's also specified that if the <u>linked list</u> has an even number of nodes, we should return the second of the two middle nodes.

Intuition

To solve this problem efficiently, we make use of <u>two pointers</u>: <u>slow</u> and <u>fast</u>. Both pointers start at the head of the <u>linked list</u>. The <u>fast</u> pointer moves through the list at twice the speed of the <u>slow</u> pointer. This means that for every node the <u>slow</u> pointer

travels, the fast pointer moves two nodes.

As a result of these different speeds, when the fast pointer reaches the end of the list, the slow pointer will be positioned at the

middle. This happens because the fast pointer traverses two nodes for every single step taken by the slow pointer. If the total

number of nodes is odd, the fast pointer will eventually point to None, which is the end of the list. If the number of nodes is

even, the fast pointer will point to the last node. In both cases, the slow pointer will be at the middle, where if there are two middle nodes, because fast moves two steps at a time, slow will end up at the second middle node.

This approach allows us to find the middle node in a single pass through the list, which is more efficient than first counting the nodes and then traversing again to the middle—especially in the case of very large lists.

Solution Approach

The given solution makes use of two pointers, slow and fast, both initialized to the head of the list. This approach is commonly

known as the "tortoise and hare" algorithm. Let's go through the steps of this approach:

the loop ends.

the list.

1. Both slow and fast are initialized at the head of the <u>linked list</u>, thus they start at the same position.

2. We then enter a loop that continues until fast is no longer pointing to a valid node or fast next is None. This condition

3. Inside the loop, slow is incremented to the next node (slow.next) and fast is incremented two nodes ahead

ensures that we stop when fast (which moves faster) has reached the end of the list.

o fast = fast.next.next moves the fast pointer two steps forward.

Let's walk through a small example to illustrate the solution approach:

We want to determine the middle node in a single pass.

(fast.next.next).

o slow = slow.next moves the slow pointer one step forward.

When fast reaches the end of the list or there are no more nodes to traverse (fast becomes None or fast next is None),

- 5. At this point, slow will be at the middle node of the list. If there are an odd number of nodes, it will be the exact middle. If there are an even number of nodes, it will be the second of the two middle nodes because of the way fast is moving two steps at a time.
- 6. The function then returns the slow pointer, which now points to the middle node of the <u>linked list</u>.

 No additional data structure is used, making the space complexity O(1), as we only have <u>two pointers</u> regardless of the size of the

<u>linked list</u>. Since each node is visited once by either slow or fast, the time complexity is O(n), where n is the number of nodes in

The beauty of this solution lies in its simplicity and efficiency. It effectively halves the traversal time to find the middle node,

Suppose we have a singly linked list with 7 nodes, and their values when traversed from head to tail are [1, 2, 3, 4, 5, 6, 7].

which would otherwise take longer if we first counted the entire list to find the length, and then iterated again to the middle.

Example Walkthrough

We initialize two pointers at the start, slow points to the node with the value 1, and fast also points to the node with value 1.

As we loop through the list:

In the second step, slow will move to 3; fast to 5.
In the third step, slow moves to 4, fast moves to 7.

At this point, slow is pointing to 4, which is the middle node in this list of 7 nodes. Our function would then return the node with

Now, let's consider an even-numbered list with 6 nodes, where the values are [1, 2, 3, 4, 5, 6].

the value 4 as the middle node.

• fast.next is now None. The loop ends.

On starting, both slow and fast point to 1.

'slow' will move one step at a time, and 'fast' will move two steps at a time.

Traverse the list. The loop runs until 'fast' reaches the end of the list.

// Fast pointer moves two steps at a time, slow pointer one step at a time.

fastPointer = fastPointer.next.next; // Move fast pointer two steps

while (fastPointer != null && fastPointer.next != null) {

When 'fast' reaches the end, 'slow' will be at the middle node.

• In the first step, slow will move one node and point to 2; fast will move two nodes and point to 3.

• Now, fast is pointing at the last node, and fast next is None. Thus, we reach the condition to end the loop.

In the first step, slow moves to 2; fast jumps to 3.
In the second step, slow goes to 3; fast skips to 5.

• In the third step, slow proceeds to 4 and fast jumps to the last node, 6.

in a single pass, hence delivering an efficient solution.

Class definition for a singly-linked list node.

def init (self, value=0, next_node=None):

slow_pointer = fast_pointer = head

while fast pointer and fast pointer.next_node:

slow pointer = slow pointer.next node

Move 'slow' one step forward.

Slow is at the value 4, which is the second of the two middle nodes in this list of 6 nodes, meeting our requirement to return the second middle node in the case of an even-numbered list.

With this explanation, it should be clear how the "tortoise and hare" algorithm functions, allowing us to find the middle of the list

Solution Implementation

class Solution:
 def middleNode(self, head: ListNode) -> ListNode:
 # Initialize two pointers, both starting at the head of the list.

Move 'fast' two steps forward. fast_pointer = fast_pointer.next_node.next_node

return slow_pointer

// Iterate through the list.

slowPointer = slowPointer.next;

self.value = value

self.next_node = next_node

Python

Java

class ListNode:

```
// Definition for singly-linked list.
class ListNode {
   int value;
   ListNode next;
   // Constructor with no parameters
   ListNode() {}
   // Constructor with value parameter
   ListNode(int value) {
       this.value = value;
   // Constructor with value and next node parameters
   ListNode(int value, ListNode next) {
        this.value = value;
       this.next = next;
public class Solution {
   /**
    * Finds the middle node of a singly linked list.
    * @param head The head of the linked list.
    * @return The middle node of the linked list.
    */
   public ListNode middleNode(ListNode head) {
       // Initialize two pointers, slow and fast.
       ListNode slowPointer = head;
       ListNode fastPointer = head;
```

// Move slow pointer one step

```
// When fast pointer reaches the end of the list,
       // slow pointer will be at the middle element.
        return slowPointer;
C++
/**
* Definition for a singly-linked list node.
struct ListNode {
   int val;
                     // The value the node stores
    ListNode *next;
                     // Pointer to the next list node in the linked list
    // Constructor to initialize a node with no next node
    ListNode(): val(0), next(nullptr) {}
    // Constructor to initialize a node with a specific value and no next node
    ListNode(int x) : val(x), next(nullptr) {}
    // Constructor to initialize a node with a specific value and a next node
    ListNode(int x, ListNode *next) : val(x), next(next) {}
};
class Solution {
public:
    /**
    * Finds the middle node of a singly linked list.
    * If there are two middle nodes, the second middle node is returned.
     * @param head The head of the linked list.
    * @return The middle node of the linked list
    ListNode* middleNode(ListNode* head) {
       ListNode *slow = head; // 'slow' pointer moves one node at a time
       ListNode *fast = head; // 'fast' pointer moves two nodes at a time
       // Continue until 'fast' reaches the end of the list
       while (fast != nullptr && fast->next != nullptr) {
            slow = slow->next;  // Move 'slow' by one node
            fast = fast->next->next; // Move 'fast' by two nodes
       // When 'fast' reaches the end, 'slow' will be at the middle node
```

```
let slowPointer: ListNode | null = head; // Pointer that will move one step at a time
// Loop until the fast pointer reaches the end of the list
while (fastPointer !== null && fastPointer.next !== null) {
```

};

/**

TypeScript

interface ListNode {

val: number;

return slow;

next: ListNode | null;

// Definition for singly-linked list node.

* @return The middle node of the list.

* Finds the middle node of a singly linked list.

* @param head The head of the singly linked list.

function middleNode(head: ListNode | null): ListNode | null {

let fastPointer: ListNode | null = head; // Pointer that will move two steps at a time

fastPointer = fastPointer.next.next; // Move fast pointer two steps

```
// Move slow pointer one step
        slowPointer = slowPointer.next;
   // When the fast pointer reaches the end of the list,
   // the slow pointer will be at the middle
   return slowPointer;
# Class definition for a singly-linked list node.
class ListNode:
   def init (self, value=0, next_node=None):
       self.value = value
       self.next_node = next_node
class Solution:
   def middleNode(self, head: ListNode) -> ListNode:
       # Initialize two pointers, both starting at the head of the list.
       # 'slow' will move one step at a time, and 'fast' will move two steps at a time.
       slow_pointer = fast_pointer = head
       # Traverse the list. The loop runs until 'fast' reaches the end of the list.
       while fast pointer and fast pointer next node:
           # Move 'slow' one step forward.
           slow pointer = slow pointer.next_node
           # Move 'fast' two steps forward.
            fast_pointer = fast_pointer.next_node.next_node
       # When 'fast' reaches the end, 'slow' will be at the middle node.
       return slow_pointer
```

Time and Space Complexity

(where n is even) or n-1 nodes (where n is odd), and it takes two iterations of the loop to move the fast pointer two nodes ahead, the loop executes approximately n/2 iterations, which is linear with respect to the number of nodes.

The space complexity is 0(1) irrespective of the number of nodes in the linked list because only two additional pointers (variables along and foot) are used which execute constant appears

The time complexity of the given code is O(n), where n is the number of nodes in the linked list. This is because the fast pointer

advances two steps at a time and the slow pointer advances one step at a time. They start at the same point, so when the fast

pointer reaches the end of the list, the slow pointer must be at the middle. Since the fast pointer traverses at most n nodes

(variables slow and fast) are used, which occupy constant space.