1558. Minimum Numbers of Function Calls to Make Target Array

Medium <u>Greedy</u> Bit Manipulation Array

Problem Description

arr, which is the same length as nums but initially filled with 0s. Your goal is to make arr look exactly like nums. To achieve your goal, you are allowed to use a special modify function, which can perform one of two operations:

You are provided with two integer arrays. The first one is called nums, and it contains some integers. The second one is called

1. Increment by 1: Choose any index i and increase the value of arr[i] by 1.

2. Double all: Double the value of each element in the array arr.

and the highest number of doubling operations for the whole array.

Here is what the code does, broken down step by step:

complexity of O(n) where n is the length of the nums array.

We want to convert the arr array: [0, 0, 0] to look exactly like nums.

• For the number 8, it has a binary representation of 1000, which has 1 set bit.

For the number 1, it has a binary representation of 1, which has 1 set bit.

Now, let's walk through the solution approach for this example:

Now, combining both the increment and doubling operations:

operations required by summing up the number of set bits in each of the numbers.

Your task is to figure out the minimum number of calls to the modify function required to transform arr into nums. The end goal is to achieve this transformation with the smallest possible number of operations.

Intuition

The solution strategy revolves around working backwards from <a href="https://nums.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.nc/lines.n

than incrementing or doubling. The insight is that any number in nums is formed by starting with 0, potentially doubling several

times, and then incrementing.

To minimize calls to modify, we should maximize the use of the doubling operation, because each doubling operation is equivalent to many increment operations. Thus, the strategy is to: 1. Find the total number of increment operations needed for each number in nums by counting the number of set bits (since each set bit represents an increment operation that has occurred).

2. Find the maximum number of doubling operations needed. This is achieved by determining the highest power of 2 required to reach the maximum number in nums, which is equivalent to the bit length of the maximum number minus 1 (since starting from 0 and doubling does not

- count as an operation). By combining the count of set bits across all numbers with the maximum bit length, we arrive at the minimum number of
- operations needed to transform arr into nums. **Solution Approach**

logical steps: Iterate through each number in the given nums array to calculate the total number of increment operations for each number

The solution uses simple bitwise operations to find the answer. Here's how the implementation goes by breaking it down into

For each number, we use the bitwise operation bit_count(), which returns the count of set bits (1-bits) in the number. The

count of set bits actually represents how many times the increment operation has been performed to reach this number from 0 because each increment operation can only set a bit from 0 to 1.

To get the maximum number of doubling operations across all numbers in the array, we look for the maximum value in nums.

We call bit_length() on this number, which gives us the position of the highest set bit, i.e., the number of times we can

potentially divide the number by 2 until it reaches 0. This represents the doubling operations needed to reach this number

the maximum number of doubling operations $(\max(0, \max(nums), bit_length() - 1))$. We also ensure that the number of

sum(v.bit_count() for v in nums) - This part goes through every number in nums and accumulates the total increment

max(nums).bit_length() - This part finds the maximum number in nums and then calculates the length of the bits needed to

- from 1. Since we start with 0, not 1, we subtract 1 from the bit length as the initial state does not count as a doubling operation. The total minimum number of function calls is the sum of all increment operations (sum(v.bit_count() for v in nums)) and
- doubling operations is not negative (which can happen if nums contains all zeros), by taking max(0, ...). The Python implementation provided uses a list comprehension to calculate the total count of bits for all numbers in nums and finds the maximum bit length among all numbers. Then it adds these two values to get the final answer.
- represent that number, which corresponds to the number of doubling operations needed plus one (since index starts at zero). Subtracting 1 from the bit length - We subtract 1 because the sequence starts from 0 and doubling from 0 does not change the number, so the first doubling operation effectively starts when going from 1 to 2.

Therefore, by combining these steps, the implementation efficiently computes the minimum number of operations with a time

Example Walkthrough Let's assume we have the following input:

Increment Operations: • For the number 3, it has a binary representation of 11, which has 2 set bits.

So the total number of increment operations needed is 2 (for 3) + 1 (for 8) + 1 (for 1) = 4.

• The maximum number in nums is 8, which has a binary representation of 1000. The bit length is 4. Therefore, we would need 3 doubling operations to get from 1 to 8. Since we start from 0, we subtract one, leaving us with 4 - 1 = 3 doubling operations.

Doubling Operations:

Total increment operations = 4 (from step 1)

Total doubling operations = 3 (from step 2)

incrementing and doubling appropriately.

Solution Implementation

Python

Java

class Solution {

/**

nums array: [3, 8, 1]

class Solution: def minOperations(self, nums: List[int]) -> int:

This walk through shows that we need 7 modify operations to make arr look exactly like nums, which are [3, 8, 1], by

Calculate the total number of set bits (1s) in all the numbers. # This corresponds to the number of increment operations needed. num_of_increment_ops = sum(bin(num).count('1') for num in nums) # Find the maximum number in the list to determine the number of # double operations needed.

We need to find the position of the highest set bit (most significant bit),

that value. This is equivalent to the bit length of the maximum number minus 1

The total number of operations is the sum of the increment and double operations.

* Method to calculate minimum operations to make all elements of nums equal to zero.

totalOperations += Integer.bitCount(number); // add number of 1's in binary representation

which determines the number of times we need to double from 1 to reach

num_of_double_ops = highest_num.bit_length() - 1 if highest_num > 0 else 0

since starting from 1 (2^0) requires no doubling operations.

highest num = max(nums) if nums else 0

return num_of_increment_ops + num_of_double_ops

1) Subtract 1 from an element if it's not 0 or,

// and find the maximum number simultaneously

maxNumber = Math.max(maxNumber, number);

// which accounts for the division by 2 operations

// Return the total count of operations needed

let operationsCount: number = 0; // Initialize counter for minimum operations

* Calculate the minimum number of operations to make all element of nums equal to zero.

// Add the number of set bits (1s) in the current value to operationsCount

let maxNum: number = 0; // Variable to store the maximum value in nums

operationsCount = 0; // Reset the counter for each function call

// Update maxNum to the maximum value encountered so far

* @param {number[]} nums - The array of numbers to be processed.

* @return {number} The minimum number of operations required.

function minOperations(nums: number[]): number {

// Loop through all numbers in the array

maxNum = max([maxNum, value]) || 0;

operationsCount += countSetBits(value);

return operationsCount;

TypeScript

/**

*/

// Importing Array object

maxNum = 0;

import { max } from 'lodash';

for (let value of nums) {

2) Divide all elements by 2 if all elements are even

int maxNumber = 0; // to track the maximum number in the array

// Calculate the sum of bit counts (number of 1's) for all numbers

// Add the length of the binary string of the maximum number minus 1

totalOperations += Integer.toBinaryString(maxNumber).length() - 1;

Therefore, the minimum number of function calls required to transform arr into nums is 4 + 3 = 7.

* @return the minimum number of operations required public int minOperations(int[] nums) { int totalOperations = 0; // to track the total minimum operations

* An operation is defined as either:

* @param nums array of integers

for (int number : nums) {

```
return totalOperations;
C++
#include <vector>
#include <algorithm> // For std::max
class Solution {
public:
    int minOperations(std::vector<int>& nums) {
        int operationsCount = 0; // Initialize counter for minimum operations
        int maxNum = 0; // Variable to store the maximum value in nums
        // Loop through all numbers in the vector
        for (int value : nums) {
            // Update maxNum to the maximum value encountered so far
            maxNum = std::max(maxNum, value);
            // Add the number of set bits (1s) in the current value to operationsCount
            operationsCount += __builtin_popcount(value);
        // If maxNum is greater than 0, add the number of bits to reach the most significant bit
        // of the largest number in nums (the number of left shifts needed for the largest number)
        if (maxNum) {
            operationsCount += 31 - __builtin_clz(maxNum);
```

```
// If maxNum is greater than 0, add the number of bits to reach the most significant bit
   // (the number of left shifts needed for the largest number)
   if (maxNum) {
       operationsCount += 31 - clz(maxNum);
   // Return the total count of operations needed
   return operationsCount;
* Count the number of set bits in an integer (Naive method).
* @param {number} n - The number in which set bits are to be counted.
* @return {number} The count of set bits in n.
*/
function countSetBits(n: number): number {
   let count: number = 0;
   while (n) {
        count += n & 1; // Increment count if the least significant bit is set
       n = n >>> 1; // Right shift n by 1 bit to process the next bit
   return count;
/**
* Compute the number of leading zero bits in the integer's binary representation.
* @param {number} num - The number whose leading zeros are to be counted.
* @return {number} The count of leading zero bits in num.
function clz(num: number): number {
   if (num === 0) return 32;
   let leadingZeros = 0;
   for (let i = 31; i >= 0; i--) {
       if ((num & (1 << i)) === 0) {</pre>
            leadingZeros++;
       } else {
           break;
   return leadingZeros;
class Solution:
```

The total number of operations is the sum of the increment and double operations. return num of increment ops + num of double ops

Time and Space Complexity

double operations needed.

def minOperations(self, nums: List[int]) -> int:

highest num = max(nums) if nums else 0

Calculate the total number of set bits (1s) in all the numbers.

This corresponds to the number of increment operations needed.

Find the maximum number in the list to determine the number of

since starting from 1 (2^0) requires no doubling operations.

We need to find the position of the highest set bit (most significant bit),

that value. This is equivalent to the bit length of the maximum number minus 1

which determines the number of times we need to double from 1 to reach

num_of_double_ops = highest_num.bit_length() - 1 if highest_num > 0 else 0

num_of_increment_ops = sum(bin(num).count('1') for num in nums)

finding the maximum number to calculate its bit length. Calculating the bit count for a single number is 0(1), and we do this for every number in the list, resulting in O(n) complexity where n is the length of the list. Finding the maximum value in the list also takes O(n) time. The bit_length function is also O(1) as it typically involves calculating the position of the highest bit set in the integer representation, which does not depend on the size of the number itself but on the number of bits.

The time complexity of the code can be calculated based on two operations: the calculation of bit counts for all numbers and

As for the space complexity, since no additional significant space is used apart from a few variables to store intermediate results, the space complexity is 0(1).

Thus, the time complexity of the function is O(n) where n is the size of the nums list.

In summary: • Time Complexity: 0(n)

- Space Complexity: 0(1)