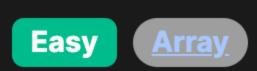
2016. Maximum Difference Between Increasing Elements



Problem Description

The problem provides us with an array nums containing integers, where our task is to find the maximum difference between two of its elements, nums[i] and nums[j], with the condition that i is less than j (that is i < j) and nums[i] is less than nums[j] (nums[i] < nums[j]). The maximum difference is defined as nums[j] - nums[i]. The constraints are such that i and j must be valid indices within the array ($0 \ll i < j < n$). If no such pair of indices exists, the function should return -1.

ntuition

iterating through the array. The idea is to continuously update the smallest element mi as we move through the array and simultaneously compute the difference between the current element and this smallest element whenever the current element is larger than mi. The steps are as follows:

The solution to this problem is driven by a single pass approach that keeps track of the smallest element found so far while

• Initialize a variable mi to store the minimum value found so far; set it to inf (infinity) at the start because we haven't encountered any elements

- in the array yet. • Initialize a variable ans to store the maximum difference found; set it to -1 to indicate that no valid difference has been calculated yet.
- Iterate over each element x in the nums array. ∘ If the current element x is greater than the current minimum mi, then there's potential for a larger difference. Calculate the difference x - mi
- and update ans to be the maximum of ans and this newly calculated difference. ∘ If the current element x is not greater than mi, then we update mi to be the current element x, since it's the new minimum.
- Solution Approach

The implementation of the solution utilizes a simple linear scanning algorithm that operates in a single pass through the array. No complex data structures are needed; only a couple of variables are used to keep track of the state as we iterate. Here is a more

detailed breakdown of the approach: We have an array nums of integers.

o mi: This is initially set to inf, representing an "infinity" value which ensures that any element we encounter will be less than this value. mi

Two variables are initialized:

- serves as the minimum value encounter so far as we iterate through the array.
 - ∘ ans: This is the answer variable, initialized to -1. It will store the maximum difference encountered that satisfies the problem's condition. We begin iterating over each element x in the nums array using a for loop. ∘ If the current element x is greater than mi, it means we've found a new pair that could potentially lead to a larger difference. In this case, we
- find the difference between x and mi and update ans to be the maximum of itself and this new difference. This step uses the max function: ans = max(ans, x - mi).
 - necessary to ensure we always have the smallest value seen so far, which allows us to find the largest possible difference. After the loop completes, the ans variable will hold the maximum difference possible. If ans remained -1, it implies there was no valid (i, j) pair that satisfied the condition (nums[i] < nums[j] with i < j).

o If x is not greater than mi, then the current element x becomes the new minimum, which updates mi to x. It's a crucial step, as this update is

condition was not found during the computation. The algorithm's simplicity and the lack of additional data structures contribute to its time efficiency, making it a solution with O(n) time complexity, where n is the number of elements in nums.

The use of the infinity value for mi is a common pattern to simplify code as it avoids the need for special checks on the index

being valid or the array being non-empty. Similarly, using -1 for ans follows a typical convention to indicate that a satisfying

Example Walkthrough Let's illustrate the solution approach with a small example. Suppose we have the following array nums:

Our task is to find the maximum difference nums[j] - nums[i] with the conditions that i < j and nums[i] < nums[j].

nums = [7, 1, 5, 3, 6, 4]

• mi is set to inf, which in practical scenarios can be represented by a very large number, assuming the array does not contain larger numbers.

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Now we begin iterating through the array nums:
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Second element (1):

Fourth element (3):

Solution Implementation

min_val = float('inf')

if num > min_val:

min_val = num

for num in nums:

else:

return maxDiff;

int maximumDifference(vector<int>& nums) {

// with the current number.

min_value = num;

int $max_difference = -1$;

C++

public:

class Solution {

class Solution:

First element (7):

 mi is inf, so we update mi to be 7. No difference is calculated because this is the first element.

ans is set to −1 as we've not yet found a valid pair.

We'll initialize our variables mi and ans:

1 is less than mi (which is 7), so we now update mi to 1.

o ans remains 4 because 4 is greater than 2.

- Third element (5): ◦ 5 is greater than mi (which is 1), so we calculate the difference (5 - 1 = 4).
- \circ 3 is greater than mi (1), so we calculate the difference (3 1 = 2).

○ The ans is still -1 because we didn't find a larger element yet.

Now, we update ans to the maximum of −1 and 4, which is 4.

- Fifth element (6): \circ 6 is greater than mi (1), so we calculate the difference (6 - 1 = 5).
- Sixth element (4): 4 is greater than mi (1), so we calculate the difference (4 - 1 = 3).

• ans remains 5, as it is still the maximum difference found.

Update ans to 5, since that's greater than the current ans of 4.

At the end of the iteration, ans contains the value 5, which is the maximum difference obtained by subtracting an earlier, smaller number from a later, larger number in the array, satisfying nums[j] - nums[i] where i < j and nums[i] < nums[j].

Therefore, the maximum difference in the given array nums is 5.

Python

```
# Initialize the maximum difference as -1 (default if not found)
\max diff = -1
# Iterate over each number in the list
```

Initialize the minimum value seen so far to infinity

there is a potential for a new maximum difference

max_diff = max(max_diff, num - min_val)

is greater than the previous maximum difference

update the minimum value to the current number

If the current number is greater than the minimum value seen,

Update the maximum difference if the current difference

If the current number is not greater than the minimum value seen,

// Return the maximum difference found, or -1 if no positive difference exists

// Initialize min_value with a large number well above any expected input.

// Initialize the answer with -1, indicating no positive difference found yet.

// If the current number is smaller than min_value, update min_value

int min_value = INT_MAX; // INT_MAX is more idiomatic than 1 << 30.</pre>

def maximumDifference(self, nums: List[int]) -> int:

```
# Return the maximum difference found; if no valid difference was found,
       # this will return -1
       return max_diff
Java
class Solution {
    public int maximumDifference(int[] nums) {
       // Initialize the minimum value to a very large value
       int minVal = Integer.MAX_VALUE;
       // Initialize the answer to -1, assuming there is no positive difference found
       int maxDiff = -1;
       // Loop through each number in the input array
        for (int num : nums) {
           // If the current number is greater than the minimum value found so far
           if (num > minVal) {
               // Update the maximum difference with the greater value between the current maximum difference
               // and the difference between the current number and the minimum value found so far
               maxDiff = Math.max(maxDiff, num - minVal);
            } else {
               // If the current number is not greater than the minimum value found so far,
                // then update the minimum value to the current number
               minVal = num;
```

```
// Iterate over each number in the input vector 'nums'.
for (int num : nums) {
   // If the current number is larger than the min_value seen so far,
   // update max_difference with the greater of current max_difference and
   // the difference between current number and min_value.
    if (num > min_value) {
        max_difference = max(max_difference, num - min_value);
    } else {
```

```
// Return the maximum positive difference found, or -1 if no such difference exists.
       return max_difference;
};
TypeScript
function maximumDifference(nums: number[]): number {
    // detn is the length of the nums array
    const numElements = nums.length;
    // Initialize the minimum value to the first element of the nums array
    let minimumValue = nums[0];
    // Initialize the maximum difference as -1; this will change if a greater difference is found
    let maxDifference = -1;
    // Loop through the array starting from the second element
    for (let index = 1; index < numElements; index++) {</pre>
       // Calculate the current difference and update the maxDifference if the current difference is greater
       maxDifference = Math.max(maxDifference, nums[index] - minimumValue);
```

// Update the minimumValue with the smallest number encountered so far

minimumValue = Math.min(minimumValue, nums[index]);

is greater than the previous maximum difference

update the minimum value to the current number

Return the maximum difference found; if no valid difference was found,

If the current number is not greater than the minimum value seen,

max_diff = max(max_diff, num - min_val)

return maxDifference > 0 ? maxDifference : −1;

```
class Solution:
   def maximumDifference(self, nums: List[int]) -> int:
       # Initialize the minimum value seen so far to infinity
       min_val = float('inf')
       # Initialize the maximum difference as -1 (default if not found)
        \max diff = -1
       # Iterate over each number in the list
        for num in nums:
           # If the current number is greater than the minimum value seen,
           # there is a potential for a new maximum difference
           if num > min_val:
               # Update the maximum difference if the current difference
```

// If no positive maximum difference was found, return -1; otherwise, return the maxDifference

this will return -1 return max_diff

Time and Space Complexity

min_val = num

else:

The time complexity of the provided code can be analyzed by looking at the operations within the main loop. The code iterates through the list of numbers once, performing constant-time operations within each iteration, such as comparison, subtraction, and assignment. Thus, the time complexity is O(n) where n is the length of the input list nums.

For space complexity, the code uses a fixed amount of additional memory to store the variables mi and ans. Regardless of the size of the input list, this does not change, which means the space complexity is constant, or 0(1).