### 452. Minimum Number of Arrows to Burst Balloons

Medium Greedy Array Sorting

### Problem Description

represented by the XY-plane. Each balloon is specified by a pair of integers [x\_start, x\_end], which represent the horizontal diameter of the balloon on the X-axis. However, the balloons' vertical positions, or Y-coordinates, are unknown.

We are tasked with finding the minimum number of arrows that need to be shot vertically upwards along the Y-axis from different

In this LeetCode problem, we are presented with a scenario involving a number of spherical balloons that are taped to a wall,

points on the X-axis to pop all of the balloons. An arrow can pop a balloon if it is shot from a point x such that x\_start <= x <= x\_end for that balloon. Once an arrow is shot, it travels upwards infinitely, bursting any balloon that comes in its path.

The goal is to determine the smallest number of arrows necessary to ensure that all balloons are popped.

#### To solve this problem, we need to look for overlapping intervals among the balloons' diameters. If multiple balloons' diameters

Intuition

We can approach this problem by:

balloon that ends first. By doing this, we ensure that we can shoot as many balloons as possible with a single arrow.

overlap with each other, a single arrow can burst all of them.

2. Scanning through the sorted balloons and initializing last, the position of the last shot arrow, to negative infinity (since we haven't shot any arrow yet).

1. Sorting the balloons based on their x\_end value. This allows us to organize the balloons in a way that we always deal with the

- 3. For each balloon in the sorted list, we check if the balloon's x\_start is greater than last, which would mean this balloon doesn't overlap with the previously shot arrow's range and requires a new arrow. If so, we increment the arrow count ans and update last with the balloon's x\_end, marking the end of the current arrow's reach.
- 4. If a balloon's start is within the range of the last shot arrow (x\_start <= last), it is already burst by the previous arrow, so we don't need to shoot another arrow.
- required to burst all balloons.

  By the end of this process, we have efficiently found the minimum number of arrows needed, which is the solution to the problem.

5. We keep following step 3 and 4 until all balloons are checked. The arrow count ans then gives us the minimum number of arrows

Solution Approach

The implementation of the solution involves a <u>greedy</u> algorithm, which is one of the standard strategies to solve optimization

problems. Here, the algorithm tests solutions in sequence and selects the local optimum at each step with the hope of finding the

#### global optimum.

1 last = b

1 sorted(points, key=lambda x: x[1])

set last to this balloon's end coordinate:

and will be burst by it, so ans is not incremented.

1. First, we sort the balloons by their ending points (x\_end):

1. First, a sort operation is applied on the points list. The key for sorting is set to lambda x: x[1], which sorts the balloons in ascending order based on their ending x-coordinates (x\_end).

before moving on to the next arrow. The steps of the algorithm are implemented as follows in the given Python code:

In this specific case, the greedy choice is to sort balloons by their right bound and burst as many balloons as possible with one arrow

A variable ans is initialized to 0 to keep track of the total number of arrows used.
 Another variable last is initialized to negative infinity (-inf). This variable is used to store the x-coordinate of the last shot arrow

- that will help us check if the next balloon can be burst by the same arrow or if we need a new arrow.

  4. A for loop iterates through each balloon in the sorted list points. The loop checks if the current balloon's start coordinate is
- This ensures that any subsequent balloon that starts before **b** (the current last) can be burst by the current arrow.

5. If the start coordinate of the balloon is not greater than last, it means the balloon overlaps with the range of the current arrow

6. After the loop finishes, the variable ans has the minimum number of arrows required, which is then returned as the final answer.

complexity of O(n log n) due to the sort operation (where n is the number of balloons) and a space complexity of O(1), assuming the

greater than last. If the condition is true, it implies that the current arrow cannot burst this balloon, hence we increment ans and

The use of the <u>greedy</u> algorithm along with <u>sorting</u> simplifies the problem and allows the solution to be efficient with a time

- Example Walkthrough

  Let's illustrate the solution approach with a small example. Suppose we have the following set of balloons with their x\_start and
- 1 Balloons: [[1,6], [2,8], [7,12], [10,16]]

  According to the approach:

#### 1 Sorted Balloons: [[1,6], [2,8], [7,12], [10,16]]

update last to 6.

all balloons.

class Solution:

solution.

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arrows.

sort is done in place on the input list.

x\_end values represented as intervals:

3. We begin iterating over the balloons list:

We increment ans to 2 and update last to 12.

def findMinArrowShots(self, points: List[List[int]]) -> int:

num\_arrows, last\_arrow\_pos = 0, float('-inf')

# Loop through the sorted balloon points

for start, end in sorted\_points:

last\_arrow\_pos = end

public int findMinArrowShots(int[][] points) {

# Sort the balloon points by their end positions

sorted\_points = sorted(points, key=lambda x: x[1])

# Initialize counter for arrows and set the last arrow position to negative infinity

# If the start of the current balloon is greater than the position

// Sort the "points" array based on the end point of each interval.

2 #include <algorithm> // Include the algorithm header for using the sort function

// Method to find the minimum number of arrows needed to burst all balloons

// Sort the input vector based on the ending coordinate of the balloons

// Definition for the class Solution where our method will reside

return point1[1] < point2[1];</pre>

int findMinArrowShots(std::vector<std::vector<int>>& points) {

Arrays.sort(points, Comparator.comparingInt(interval -> interval[1]));

Since our balloons are already sorted by their x\_end, we don't need to change the order.

2. We initialize ans to 0 since we haven't used any arrows yet, and last to negative infinity to signify that we have not shot any

not increment ans, and last remains 6.

c. Moving on to the third balloon [7,12], x\_start is greater than last (7 > 6), indicating no overlap with the last arrow's range.

a. For the first balloon [1,6], x\_start is greater than last (-inf in this case), so we need a new arrow. We increment ans to 1 and

b. The next balloon [2,8] has x\_start <= last (since 2 <= 6), so it overlaps with the range of the last arrow. Therefore, we do

d. Finally, for the last balloon [10,16], since x\_start <= last (as 10 <= 12), it can be popped by the previous arrow, so we keep ans as it is.

4. After checking all balloons, we have used 2 arrows as indicated by ans, which is the minimum number of arrows required to pop

By following this greedy strategy, we never miss the opportunity to pop overlapping balloons with a single arrow, ensuring an optimal

Python Solution

# of the last arrow, we need a new arrow
if start > last\_arrow\_pos:
# Increment the number of arrows needed
num\_arrows += 1
# Update the position for the last arrow

## # Return the minimum number of arrows required return num\_arrows 21

Java Solution

class Solution {

```
// Initialize the counter for the minimum number of arrows.
           int arrowCount = 0;
           // Use a "lastArrowPosition" variable to track the position of the last arrow.
           // Initialize to a very small value to ensure it is less than the start of any interval.
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           long lastArrowPosition = Long.MIN_VALUE;
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           // Iterate through each interval in the sorted array.
           for (int[] interval : points) {
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               int start = interval[0]; // Start of the current interval
               int end = interval[1]; // End of the current interval
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               // If the start of the current interval is greater than the "lastArrowPosition",
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               // it means a new arrow is needed for this interval.
               if (start > lastArrowPosition) {
                   arrowCount++; // Increment the number of arrows needed.
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22
                   lastArrowPosition = end; // Update the position of the last arrow.
23
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26
           // Return the minimum number of arrows required to burst all balloons.
27
           return arrowCount;
28
29 }
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C++ Solution
                        // Include the vector header for using the vector container
1 #include <vector>
```

std::sort(points.begin(), points.end(), [](const std::vector<int>& point1, const std::vector<int>& point2) {

// Initialize the count of arrows to zero

// Increment the arrow count

int start = point[0], end = point[1]; // Extract start and end points of the balloon

// If the start point of the current balloon is greater than the last burst position

long long lastBurstPosition =  $-(1LL \ll 60)$ ; // Use a very small value to initialize the position of the last burst

// Update the last burst position with the end of the current balloon

# 27 } 28 29 return arrowCount; // Return the total number of arrows needed 30 } 31 };

class Solution {

});

int arrowCount = 0;

// Iterate over all balloons

++arrowCount;

for (const auto& point : points) {

// it means a new arrow is needed

if (start > lastBurstPosition) {

lastBurstPosition = end;

6 public:

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Typescript Solution
   // Function to determine the minimum number of arrows
 2 // required to burst all balloons
   function findMinArrowShots(points: number[][]): number {
       // Sort the points by the end coordinates
       points.sort((a, b) => a[1] - b[1]);
       // Initialize the counter for the minimum number of arrows
       let arrowsNeeded = 0;
 8
 9
       // Initialize the position where the last arrow was shot
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       // It starts at the smallest possible value so the first balloon gets shot
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12
       let lastArrowPosition = -Infinity;
13
       // Iterate over all points (balloons)
14
       for (const [start, end] of points) {
           // If the current balloon's start position is
           // greater than the position where the last arrow was shot,
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           // it means a new arrow is needed for this balloon
18
           if (lastArrowPosition < start) {</pre>
20
               // Increment the arrow counter
               arrowsNeeded++;
               // Update the last arrow's position to the current balloon's end position
23
               // as we can shoot it at the end and still burst it
24
               lastArrowPosition = end;
25
26
27
       // Return the total number of arrows needed
28
29
       return arrowsNeeded;
30 }
31
```

## The time complexity of the given code can be broken down into two major parts: the sorting of the input list and the iteration over the sorted list.

1. Sorting:

Time and Space Complexity

The sorted() function has a time complexity of O(n log n), where n is the number of intervals in points.
This is the dominant factor in the overall time complexity as it grows faster than linear with the size of the input.
Iteration:

- After sorting, the code iterates over the sorted list only once.
   The iteration has a linear time complexity of O(n), where n is the number of intervals.
- Combining these two operations, the overall time complexity of the algorithm is  $0(n \log n)$  due to the sorting step which dominates the iteration step.
- The space complexity is determined by the additional space used by the algorithm apart from the input.

  1. Additional Space:

• The sorted() function returns a new list that is a sorted version of points, which consumes O(n) space.

• The variables ans and last use a constant amount of space 0(1).

The overall space complexity of the algorithm is 0(n) to account for the space required by the sorted list.