Prefix Sum

Hash Table

# Problem Description

Stack

Array

The problem presents us with an array called hours which represents the number of hours worked by an employee each day. Our goal is to find the length of the longest interval of days where there are more "tiring days" than "non-tiring days". A "tiring day" is defined as any day where the employee works more than 8 hours. We need to understand the interval dynamics where the "wellperforming intervals" are those having a greater count of tiring days compared to non-tiring days. The challenge lies in finding the maximum length of such an interval.

Monotonic Stack

## Intuition

Medium

solved efficiently using a prefix sum and a hash map. The intuition here is to designate tiring days as a positive contribution (+1) and non-tiring days as a negative contribution (-1) to the sum. As we iterate over the array: We keep a running sum (s), which is increased by 1 for tiring days and decreased by 1 for non-tiring days.

The solution to this problem uses an interesting approach akin to finding the longest subarray with a positive sum, which can be

- If at any point, the running sum is positive, it means there are more tiring days than non-tiring days so far, so we update the answer to the current length of days (i + 1).
- If the running sum is not positive, we look to see if there is a previous running sum (s 1). If it exists, then the subarray between the day when s - 1 was the running sum and the current day is a "well-performing interval". We then update our answer if this
- interval is longer than our current longest interval. To efficiently find these previous running sums, we use a hash map (pos) that records the earliest day that each running sum occurred. This way, we only store the first occurrence of each sum since we want the longest possible interval.
- This approach relies on the idea that if we find a running sum that is greater than a past running sum, then there must have been more tiring days than non-tiring days in between those two points. The efficiency of this solution comes from the fact that we

Solution Approach

### the approach is implemented:

1. Initialize variables:

The solution uses a hash map and a running sum to efficiently track well-performing intervals. Here's the detailed breakdown of how

- pos is a hash map recording the first occurrence of each running sum.
- 2. Iterate over the hours array using enumerate to have both index i and value x for each day.

ans tracks the length of the longest well-performing interval found so far and initializes to 0.

3. Update the running sum s:

s is our running sum, which helps determine if an interval is well-performing.

traverse the list only once and access/update the hash map in constant time.

- Add 1 to s if x > 8 (tiring day).
- Subtract 1 from s if x is not greater than 8 (non-tiring day). 4. After updating the running sum:
  - If s > 0, it means we've encountered more tiring days than non-tiring days up to day i, so update ans to i + 1.
  - If s <= 0, we look for s 1 in pos. If it's found, it indicates there's an interval starting right after the first occurrence of s 1</li>

occurrence because we're interested in the longest interval.

and update ans if it's longer than the current ans.

- 5. Update the hash map pos:
- corresponding earlier sum would allow for a well-performing interval to exist between it and the current day. Using this pattern allows us to efficiently process each day in constant time, resulting in an overall time complexity of O(n), where n

If the current running sum s has not been seen before, record its first occurrence (pos[s] = i). We only update the first

up to the current day i, which is a well-performing interval. Hence, we calculate the length of this interval (i - pos[s - 1])

number of days if all running sums are unique. Example Walkthrough

is the number of days. The space complexity is also 0(n) due to storing the sum indices in the hash map, possibly equal to the

The code uses pos to remember the earliest day an intermediate sum occurs. By checking if s - 1 is in pos, we can infer if a

Let's consider a small example using the solution approach described above. Suppose we have the following hours array where we need to find the length of the longest well-performing interval: 1 hours = [9, 9, 6, 0, 6, 6, 9]

#### Here's a step-by-step walkthrough using the solution approach:

1. We initialize our variables: ans to 0, s to 0, and pos as an empty hash map. 2. We start iterating through hours with the values and their indices:

hash map pos is updated with pos[1] = 0 because we haven't seen this sum before.

# Initialize the maximum length of well-performing interval and sum so far

# Initialize a dictionary to store the earliest index of a particular cumulative sum

# If the cumulative sum is positive, we found a well-performing interval

max\_length = max(max\_length, index - sum\_indices[cumulative\_sum - 1])

Day 1 (i=1, x=9): Another tiring day. We increment s to 2. ans is updated to i + 1 = 2 and pos[2] = 1.

o Day 0 (i=0, x=9): It's a tiring day because x>8. We add 1 to s, making it 1. Since s>0, we update ans =i+1=1. The

 Day 2 (i=2, x=6): A non-tiring day, so we subtract 1 from s, making it 1 again. Since s is still positive, we don't update ans, but we don't update pos [1] either as it already exists.

update to ans and we set pos[-1] = 4.

- Day 3 (i=3, x=0): Non-tiring, subtract 1 from s to 0. ans remains unchanged, and we add pos [0] = 3 to the hash map. ○ Day 4 (i=4, x=6): Non-tiring, subtract 1 from s to -1. Since s <= 0, we check for s - 1 which is -2 in pos, but it's not there. No
- pos[-2] = 5.

3. The iteration is now complete. The longest well-performing interval we found has a length of 2, which occurred between days 0

 □ Day 6 (i=6, x=9): Tiring, we add 1 to s, bringing it up to -1. We check for s - 1 which is -2 in pos and find it at position 5. We calculate the interval length i - pos[-2] = 6 - 5 = 1. Since this does not exceed our current maximum of ans = 2, we do not update ans.

○ Day 5 (i=5, x=6): Non-tiring, s goes to -2. We check for s - 1 which is -3 in pos, but it's not found. ans stays the same and

Therefore, the answer for this given hours array is 2. **Python Solution** 

8 # Iterate through each hour in the list for index, hour in enumerate(hours): 9 # Increment or decrement the cumulative sum based on the hour's value 10 cumulative\_sum += 1 if hour > 8 else -1 11

# from the beginning up to the current index

if cumulative\_sum - 1 in sum\_indices:

if (scoreToIndexMap.containsKey(score - 1)) {

scoreToIndexMap.putIfAbsent(score, i);

def longest\_wpi(self, hours) -> int:

sum\_indices = {}

max\_length = cumulative\_sum = 0

```
15
               if cumulative_sum > 0:
                   max_length = index + 1
16
               else:
17
                   # If cumulative_sum - 1 is in the sum_indices, it means we previously had a smaller sum
18
19
                   # By finding the length from that index to the current index, we ensure a positive hour count
```

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28 }

and 1 (inclusive).

class Solution:

```
22
23
                   # If this sum has not been seen before, map it to the current index
                   # We only want to record the first occurrence of a cumulative sum to achieve the longest interval
24
                   if cumulative_sum not in sum_indices:
25
26
                       sum_indices[cumulative_sum] = index
27
28
           # The resulting max_length is the length of the longest well-performing interval
29
           return max_length
30
Java Solution
   class Solution {
       public int longestWPI(int[] hours) {
            int longestSequence = 0; // This will hold the final result, length of the longest well-performing interval.
           int score = 0; // This tracks the current score indicating the balance of hours (tiring vs. non-tiring).
           Map<Integer, Integer> scoreToIndexMap = new HashMap<>(); // Mapping from scores to their first occurrence index.
 6
           // Iterate over the input array.
           for (int i = 0; i < hours.length; ++i) {</pre>
               // If the number of hours worked is more than 8 in a day, increment score, otherwise decrement.
 9
               score += hours[i] > 8 ? 1 : -1;
10
11
12
               // If the current score is positive, it means there is a well-performing interval from 0 to i-th day.
               if (score > 0) {
13
                   longestSequence = i + 1; // Update the length of the longest sequence.
14
15
               } else {
                   // If there's a previous score that is one less than the current score...
16
```

longestSequence = Math.max(longestSequence, i - scoreToIndexMap.get(score - 1));

// Store the current score's first occurrence index if it's not already stored.

return longestSequence; // Return the length of the longest well-performing sequence found.

// This means for any score, we save the earliest index at which the score occurred.

// ... then there's a well-performing interval from that previous score's index to the current index i.

# C++ Solution

```
1 #include <vector>
 2 #include <unordered_map>
   using namespace std;
   class Solution {
   public:
       // Function to find the length of the longest well-performing interval
       int longestWPI(vector<int>& hours) {
            int longestInterval = 0; // Variable to store the length of the longest interval found
           int score = 0;
                                       // A score to determine well-performing days vs. non-well-performing days
10
           unordered_map<int, int> firstOccurrence; // Map to store the first occurrence of a score
11
12
13
           // Iterate over the hours array
           for (int i = 0; i < hours.size(); ++i) {</pre>
14
               // Increase the score for well-performing days (hours > 8), decrease for non-well-performing days
15
               score += hours[i] > 8 ? 1 : -1;
16
17
18
               // If the score is positive, we've found a well-performing interval from the start
               if (score > 0) {
19
20
                    longestInterval = i + 1; // Update the longest interval length
               } else {
21
                   // If the score becomes non-positive, try to find a well-performing interval in the middle
23
                   // Check if there's a previous score that is one less than the current score
24
                   if (firstOccurrence.count(score - 1)) {
25
                        // Update the longest interval found if necessary
26
                        longestInterval = max(longestInterval, i - firstOccurrence[score - 1]);
27
28
               // Record the first occurrence of a score if it hasn't already been recorded
29
30
               if (!firstOccurrence.count(score)) {
31
                    firstOccurrence[score] = i;
32
33
34
           return longestInterval; // Return the length of the longest well-performing interval found
35
36 };
37
```

```
let score: number = 0; // A score to determine well-performing days vs non-well-performing days
       let firstOccurrence: Map<number, number> = new Map(); // Map to store the first occurrence of a score
 9
10
       // Iterate over the hours array
       for (let i = 0; i < hours.length; ++i) {</pre>
11
12
           // Increase score for well-performing days (hours > 8), decrease for non-well-performing days
           score += hours[i] > 8 ? 1 : -1;
13
14
15
           // If the score is positive, a well-performing interval from the start has been found
           if (score > 0) {
16
17
               longestInterval = i + 1; // Update the longest interval length
           } else {
18
               // If the score is non-positive, try to find a well-performing interval in the middle
19
               // Check if there's a previous score that is one less than the current score
20
               if (firstOccurrence.has(score - 1)) {
21
22
                   // Update the longest interval found if necessary
23
                   longestInterval = Math.max(longestInterval, i - (firstOccurrence.get(score - 1) as number));
24
25
26
27
           // Record the first occurrence of a score if it hasn't already been recorded
28
           if (!firstOccurrence.has(score)) {
29
               firstOccurrence.set(score, i);
30
31
32
33
       return longestInterval; // Return the length of the longest well-performing interval found
34 }
35
Time and Space Complexity
Time Complexity
```

// Import necessary libraries from JavaScript/TypeScript (no include statement needed in TypeScript)

let longestInterval: number = 0; // Variable to store the length of the longest interval found

// The typing for unordered\_map in TypeScript would use a Map or Record

// Define the function to find the longest well-performing interval

function longestWPI(hours: number[]): number {

hours.

**Typescript Solution** 

The given Python function longestWPI exhibits a time complexity of O(N), where N represents the length of the input list hours. This is due to the fact that the function iterates through the list exactly once. During each iteration, it performs a constant amount of work:

updating the sum s, checking conditions, and updating the pos dictionary or ans as needed. Space Complexity The space complexity of the function is also O(N). The post dictionary is the primary consumer of space in this case, which in the worst-case scenario might need to store an entry for every distinct sum s encountered during the iteration through hours. In a worst-

case scenario where every value of s is unique, the dictionary's size could grow linearly with respect to N, the number of elements in