

Problem Description

The problem asks for converting an integer n from base 10 to a given base k and then to find the sum of the digits of the new number in base k. It's important to note that after conversion, each digit of the base k number should be treated as an individual base 10 number. Finally, the sum of these base 10 values of the digits should be returned also in base 10.

To illustrate this with an example, if n is 34 and k is 6, the base 6 representation of 34 would be 54 ($5*6^1 + 4*6^0$). The sum needed would be the sum of the digits 5 and 4 in base 10, which equals 9.

Intuition

The solution follows a simple mathematical approach, consisting of repeatedly dividing the given number n by the base k and taking the remainder as the next base k digit. This is a common mathematical strategy to convert numbers from base 10 to another base.

The core intuition is that in each division step, n % k gives us the digit in the ones place of the base k number, and n // k reduces n to remove that digit. We keep track of the sum of these digits as we find them by adding n % k to ans at each step, which is initialized as 0. This process continues until n is reduced to 0, at which point we've looked at each digit of the number in base k, and ans holds their sum.

By treating each digit as a base 10 number immediately upon discovery, we avoid the need to first fully convert n to base k as a separate step before summing the digits. We're effectively converting and summing in one pass, which is efficient and straightforward.

Solution Approach

The implementation of the solution makes use of a simple loop and arithmetic operations to achieve the conversion and digit summation. No complex data structures or patterns are necessary, which makes the algorithm easy to understand and efficient in terms of both time and space complexity.

Here's an explanation of the steps taken in the given Python code:

- 1. We initialize ans to 0, which will be used to keep track of the cumulative sum of the base k digits.
- 2. We start a while loop that will run as long as n is not 0. Within each iteration of the loop, we are dealing with two tasks: converting to base k and summing up the digits.
- 3. The expression n % k is evaluated, which will give us the least significant digit in the base k representation of our number. For example, if n is 34 and k is 6, in the first iteration, we will get 4 because 34 % 6 equals 4.
- 4. We add this digit to ans, effectively summing the digits as we generate them in the base k representation.
- 5. Next, we need to update n for the next iteration. We do this by floor-dividing n by k using the expression n //= k. Floor division (//) gives us the quotient when n is divided by k, which effectively shifts our base k number to the right, discarding the digit we just added to ans.
- 6. The loop continues until n is reduced to 0, meaning we have processed all digits in the base k number.

After the loop exits, the final result, which is the sum of the digits in base k, is stored in ans. This value is then returned.

This approach is grounded in arithmetic and the properties of number base conversion. It is efficient, as it does not require any additional memory beyond a few integer variables, and all operations are basic arithmetic which can be performed in constant time relative to the number of digits in the base k representation.

Example Walkthrough

Let's take n = 29 and k = 7 as a small example to illustrate the solution approach. We are tasked with converting the integer n from base 10 to base k and then finding the sum of the digits of the resulting number when each digit is considered as a separate base 10 number.

2. Since n is not 0, we enter the while loop.

1. We start by initializing ans to 0. This will keep track of the cumulative sum of the base k digits.

- During the first iteration, we calculate
- 3. During the first iteration, we calculate n % k. For our example, 29 % 7 is 1. The number 1 is the least significant digit in the base 7 representation of the number 29.
- 5. We prepare for the next iteration by updating n with n // k. For our example, 29 // 7 is 4. So now n becomes 4.

4. We then add this digit to ans, so ans is now 1.

- 6. The while loop executes again because n is not 0.
- 7. During the second iteration, n % k gives 4 % 7, which is 4. This is the next digit in the base 7 representation, which is also the
- most significant digit since n is now less than k.

 8. We add the 4 to ans, resulting in ans being 1 + 4 or 5.
- 9. We update n with n // k again. This time, 4 // 7 is 0, since 4 is less than 7.

Calculate the sum of digits of a number 'n' represented in base 'k'.

// Method to calculate the sum of digits of 'n' when represented in base 'k'

// Initialize the result variable to store the sum of digits

10. The while loop terminates because n is now 0.

returned as the result.

The final result stored in ans is 5, which is the sum of the digits 4 and 1 of the number 29 when converted to base 7. This sum 5 is

1 class Solution: 2 def sumBase(self, n: int, k: int) -> int: 3

Python Solution

```
Parameters:
           n (int): The integer number to be converted.
           k (int): The base to which the number 'n' is to be converted.
           Returns:
           int: The sum of the digits of the number 'n' in base 'k'.
12
13
14
           # Initialize the variable to store the sum of digits
15
           digit_sum = 0
16
17
           # Continue looping until the number becomes 0
           while n > 0:
18
19
               # Add the last digit of 'n' in base 'k' to 'digit_sum'
               digit sum += n % k
20
21
22
               # Remove the last digit by dividing 'n' by the base 'k'
23
               n //= k
24
25
           # Return the sum of the digits
           return digit_sum
26
27
Java Solution
   class Solution {
```

int result = 0; // Continue the process until 'n' becomes 0

public int sumBase(int n, int k) {

```
while (n != 0) {
               // Add the last digit of 'n' in base 'k' to the result
9
               result += n % k; // 'n % k' gives the last digit when 'n' is represented in base 'k'
10
11
               // Divide 'n' by 'k' to remove the last digit, reducing 'n'
12
13
               n /= k; // 'n' is now equal to 'n' without its last digit in base 'k'
14
15
16
           // Return the sum of digits of 'n' in base 'k'
17
           return result;
18
19
20
C++ Solution
1 class Solution {
2 public:
       // Function to calculate the sum of digits of the number 'n' when it is represented in base 'k'.
```

11 } 12 }; 13

9

10

int sumBase(int n, int k) {

int sum = 0; // Initialize the sum of digits to 0

while (n > 0) { // Continue until the number becomes 0

sum += n % k; // Add the last digit of 'n' in base 'k' to sum

n /= k; // Divide 'n' by 'k' to remove the last digit

return sum; // Return the calculated sum of digits in base 'k'

```
Typescript Solution

1 // This function calculates the sum of the digits of a number n when represented in base k.
2 function sumBase(n: number, k: number): number {
3  let sum = 0; // Initialize sum to store the sum of the digits in base k.
4
5  // Loop continues until n is reduced to 0.
6  while (n) {
7     sum += n % k; // Add the remainder of n divided by k to sum, this is the rightmost digit in base k.
8     n = Math.floor(n / k); // Update n to be the quotient of n divided by k, removing the rightmost digit in base k.
9  }
10
```

// The function returns the sum of digits of n in base k. return sum; }

Time and Space Complexity

The time complexity of the provided code is $0(\log_k(n))$. This result is due to the fact that in each iteration, the number n is divided

digits of n in base k, which is why the logarithm comes into play.

As for the space complexity, it is 0(1) which means it is constant. The reason for this is that the variables ans and n are being reused

and updated with each iteration, and no additional space is required that scales with the input size.

by the base k, which decreases n exponentially until it reaches 0. The number of iterations required is proportional to the number of