Sliding Window

# Problem Description

Array

Dynamic Programming

be achieved by taking two non-overlapping subarrays from nums, with one subarray having a length of firstLen and the other having a length of secondLen. A subarray is defined as a sequence of elements from the array that are contiguous (i.e., no gaps in between). It is important to note that the subarray with length firstLen can either come before or after the subarray with length secondLen, but they cannot overlap.

Given an array nums of integers and two distinct integer values firstLen and secondLen, the task is to find the maximum sum that can

### To solve this problem, an effective idea is to utilize the concept of prefix sums to quickly calculate the sum of elements in any

Intuition

Medium

recalculating it every time by adding up elements iteratively. Here's the intuition broken down into steps:

subarray of the given nums array. By using the prefix sums, you can determine the sum of elements in constant time, rather than

elements from the start up to the current index.

2. Initialize variables: We then define two variables ans to store the maximum sum found so far and t to keep track of the maximum sum of subarrays of a particular length as we traverse the array.

1. Calculate prefix sums: First, we need to create an array of prefix sums s from the input array nums, which holds the sum of the

3. Find Maximum for each configuration: Start by considering subarrays of length firstLen and then move on to subarrays of length secondLen. As we iterate through

the array, we calculate the maximum sum of a firstLen subarray ending at the current index and store it in t.

- Then we use this to calculate and update ans by adding the sum of the following secondLen subarray. We ensure that at each step, the chosen subarrays do not overlap by controlling the indices and lengths properly.
  - 4. Repeat the process in reverse: To ensure we are not missing out on any configuration (since the firstLen subarray can appear before or after the secondLen subarray), we reverse the lengths and repeat the procedure.
  - 5. Return the result: The maximum of all calculated sums is stored in ans, which we return as the final answer.
- By iterating over each possible starting point for the firstLen and secondLen subarrays and efficiently calculating sums using the prefix array, we find the maximum sum of two non-overlapping subarrays of designated lengths.
- Solution Approach

the two required subarrays. Here are the steps involved in the implementation:

The solution is built around the efficient use of a prefix sum array and two traversal patterns to evaluate all possible configurations of

## function call essentially generates a new list where each element at index i represents the sum of the nums array up to that

index. 2. Traverse and Compute for firstLen and secondLen: The algorithm starts off with two for loop constructs, each responsible for

1. Prefix Sum Array: A prefix sum array s is constructed from the input array nums using list(accumulate(nums, initial=0)). This

The first for loop starts iterating after firstLen to leave room for the first subarray. Inside this loop, t is calculated as the

non-overlapping subarray of secondLen.

sequence of index increments and subarray length considerations.

handling one of the two configurations:

maximum sum of the firstLen subarray ending at the current index i. It immediately computes the sum of the next secondLen subarray and updates the answer ans if needed, by adding the sum of the current firstLen subarray (t) and the sum of the consecutive secondLen subarray.

3. Variable t and ans: The variable t tracks the maximum sum of a subarray of length firstLen found up to the current position in

the iteration (essentially, it holds the best answer found so far for the left side). The variable ans accumulates the maximum

combined sum of two non-overlapping subarrays, comparing the sum of the current subarray of firstLen plus the sum of the

4. Repeat the Process for Reversed Lengths: After the first pass is completed, the same process is repeated, with the roles of firstLen and secondLen reversed. This ensures that all possible positions of firstLen and secondLen subarrays are evaluated.

5. Checking for Overlapping: While updating ans, care is taken to ensure that the subarrays do not overlap by controlling the

then returned. By separately handling the cases for which subarray comes first, the function ensures it examines all possible configurations while efficiently computing sums using the prefix sum array, thus arriving at the correct maximum sum of two non-overlapping subarrays

6. Return the Maximum Sum: After both traversals, the variable ans holds the maximum sum possible without overlap, which is

Example Walkthrough Let's walk through an example to illustrate the solution approach. Consider the array nums = [3, 5, 2, 1, 7, 3], with firstLen = 2 and secondLen = 3.

Step 1: Prefix Sum Array Construct a prefix sum array s from nums.

The element at index i in the prefix sum array represents the sum of all elements in nums up to index i-1.

• At index 3 (i = 3), t = max(t, s[3] - s[3 - firstLen]) which is max(0, 10 - 3) so t = 7.

• At index 4 (i = 4), t = max(t, s[4] - s[4 - secondLen]) which is max(0, 11 - 3) so t = 8.

overlapping subarrays for the lengths provided. Thus, we return 18 as the final answer for this example.

def max\_sum\_two\_no\_overlap(self, nums: List[int], first\_len: int, second\_len: int) -> int:

# Initialize the answer and a temporary variable for tracking the max sum of the first array

max\_sum = max(max\_sum, max\_sum\_first\_array + prefix\_sums[i + second\_len] - prefix\_sums[i])

# Loop through nums to consider every possible second array starting from index first\_len

# Create a prefix sum array with an initial value of 0 for easier calculation

### Initialize ans to -infinity (or a very small number) and t to 0. Start the first for loop after firstLen (index is 2 in this case).

of given lengths.

Step 3: Variable t and ans

Step 4: Repeat for Reversed Lengths

**Checking for Overlapping** 

Original nums array: [3, 5, 2, 1, 7, 3]

Prefix sum array s: [0, 3, 8, 10, 11, 18, 21]

(secondLen subarray sum) + 7 (firstLen subarray sum) = 15 is greater than ans, we update ans to 15.

We reset t to 0, and reverse the firstLen and secondLen.

# Determine the total number of elements in nums

prefix\_sums = list(accumulate(nums, initial=0))

max\_sum = max\_sum\_first\_array = 0

# Return the maximum sum found

// Initialize the length of the array

for (int i = 0; i < arrayLength; ++i) {</pre>

int[] prefixSums = new int[arrayLength + 1];

prefixSums[i + 1] = prefixSums[i] + numbers[i];

int arrayLength = numbers.length;

// Calculate prefix sums

int maxSum = 0;

int maxSum = 0;

return maxSum;

Step 2: Traverse and Compute for firstLen, then secondLen

 Start the next for loop after secondLen (index is 3 in this case). At index 3 (i = 3), we ignore because we cannot form both subarrays.

At index 2 (i = 2), we ignore because we cannot form both subarrays.

Step 6: Return the Maximum Sum

We then compute the sum of the next firstLen subarray: s[i + firstLen] - s[i] which is s[6] - s[4] so 21 - 11 = 10. We add 10

(firstLen subarray sum) to 8 (secondLen subarray sum) and get 10 + 8 = 18 which is greater than ans, so we update ans to 18.

We have finished evaluating both configurations. The variable ans now holds the value 18, which is the maximum sum of two non-

We then calculate the sum of the next secondLen subarray: s[i + secondLen] - s[i] which is s[6] - s[3] so 18 - 10 = 8. Since 8

### Python Solution 1 from itertools import accumulate

n = len(nums)

i += 1

return max\_sum

Java Solution

class Solution {

class Solution:

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38 };

i = first\_len 15 while i + second\_len - 1 < n:</pre> 16 # Find the max sum of the first array ending before the start of the second array 17 max\_sum\_first\_array = max(max\_sum\_first\_array, prefix\_sums[i] - prefix\_sums[i - first\_len]) 18 19 # Update the max\_sum with the best we've seen combining the two arrays so far

22 23 # Reset the temporary variable for the max sum of first and second arrays 24 max\_sum\_second\_array = 0 25 # Loop through nums to consider every possible first array starting from index second\_len 26 i = second\_len 27 while i + first\_len - 1 < n:</pre> 28 # Find the max sum of the second array ending before the start of the first array 29 max\_sum\_second\_array = max(max\_sum\_second\_array, prefix\_sums[i] - prefix\_sums[i - second\_len]) 30 # Update the max\_sum with the best we've seen for the swapped sizes of the two arrays 31 max\_sum = max(max\_sum, max\_sum\_second\_array + prefix\_sums[i + first\_len] - prefix\_sums[i]) 32 i += 1 33

23 24 // Second scenario: secondLength subarray is before firstLength subarray 25 // Loop from secondLength up to the point where a contiguous firstLength subarray can fit 26 for (int i = secondLength, tempMax = 0; i + firstLength - 1 < arrayLength; ++i) {</pre>

int maxL = 0; // To store max sum of subarray with length L

// where first subarray has length L and second has length M

maxSum = max(maxSum, maxL + prefixSum[i + M] - prefixSum[i]);

// Same as above, but first subarray has length M and second has length L

maxSum = max(maxSum, maxM + prefixSum[i + L] - prefixSum[i]);

maxL = max(maxL, prefixSum[i] - prefixSum[i - L]);

int maxM = 0; // To store max sum of subarray with length M

maxM = max(maxM, prefixSum[i] - prefixSum[i - M]);

// Return the max possible sum of two non-overlapping subarrays

// Find max sum for two non-overlapping subarrays

for (int i = L; i + M - 1 < n; ++i) {

for (int i = M; i + L - 1 < n; ++i) {

public int maxSumTwoNoOverlap(int[] numbers, int firstLength, int secondLength) {

// Create a prefix sum array with an additional 0 at the beginning

// Initialize the answer to be the maximum sum we are looking for

// First scenario: firstLength subarray is before secondLength subarray

// Loop from firstLength up to the point where a contiguous secondLength subarray can fit

maxSum = Math.max(maxSum, tempMax + prefixSums[i + secondLength] - prefixSums[i]);

for (int i = firstLength, tempMax = 0; i + secondLength - 1 < arrayLength; ++i) {</pre>

tempMax = Math.max(tempMax, prefixSums[i] - prefixSums[i - firstLength]);

// Get the maximum sum of any firstLength subarray up to the current index

```
27
               // Get the maximum sum of any secondLength subarray up to the current index
28
               tempMax = Math.max(tempMax, prefixSums[i] - prefixSums[i - secondLength]);
29
               // Update the maxSum with the sum of the maximum secondLength subarray and the contiguous firstLength subarray
               maxSum = Math.max(maxSum, tempMax + prefixSums[i + firstLength] - prefixSums[i]);
30
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32
           // Return the maximum sum found for both scenarios
33
34
           return maxSum:
35
36 }
37
C++ Solution
 1 #include <vector>
 2 #include <algorithm> // For std::max
   using std::vector;
   using std::max;
   class Solution {
   public:
       int maxSumTwoNoOverlap(vector<int>& nums, int L, int M) {
 9
           int n = nums.size();
10
           vector<int> prefixSum(n + 1, 0);
           // Calculate prefix sums
12
           for (int i = 0; i < n; ++i) {
13
               prefixSum[i + 1] = prefixSum[i] + nums[i];
14
15
16
```

// Update the maxSum with the sum of the maximum firstLength subarray and the contiguous secondLength subarray

### Typescript Solution 1 // The `nums` array stores the integers, `L` and `M` are the lengths of the subarrays

```
function maxSumTwoNoOverlap(nums: number[], L: number, M: number): number {
       const n: number = nums.length;
       const prefixSum: number[] = new Array(n + 1).fill(0);
       // Calculate prefix sums
6
       for (let i = 0; i < n; ++i) {
           prefixSum[i + 1] = prefixSum[i] + nums[i];
9
10
11
       let maxSum: number = 0; // Max sum of two non-overlapping subarrays
       let maxL: number = 0; // Max sum of subarray with length L
12
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14
       // First loop: fixing the first subarray with length L and finding optimal M
       for (let i = L; i + M <= n; ++i) {
15
           maxL = Math.max(maxL, prefixSum[i] - prefixSum[i - L]);
16
           maxSum = Math.max(maxSum, maxL + prefixSum[i + M] - prefixSum[i]);
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20
       let maxM: number = 0; // Max sum of subarray with length M
21
22
       // Second loop: fixing the first subarray with length M and finding optimal L
23
       for (let i = M; i + L <= n; ++i) {
           maxM = Math.max(maxM, prefixSum[i] - prefixSum[i - M]);
24
           maxSum = Math.max(maxSum, maxM + prefixSum[i + L] - prefixSum[i]);
25
26
27
       // Return the max possible sum of two non-overlapping subarrays
28
29
       return maxSum;
30 }
31
Time and Space Complexity
```

The time complexity of the given code is O(n), where n is the length of the nums list. This is because the code iterates over the list twice with while-loops. In each iteration, it performs a constant number of operations (addition, subtraction, and comparison).

The space complexity of the code is O(n), due to the additional list s that is created with the accumulate function to store the prefix sums of the nums list. The size of the s list is directly proportional to the size of the nums list.