162. Find Peak Element

Medium Array **Binary Search**

Problem Description

peak element is defined as an element that is strictly greater than its neighboring elements. Here the term "strictly" means that the peak element must be greater than its neighbors, not equal to them.

The problem presents an integer array called nums which is 0-indexed. We are tasked with finding an index of a peak element. A

Furthermore, the problem scenario extends the array conceptually, so that if you look at the start or end of the array, it's as if there's an invisible - to the left of the first element and to the right of the last element. This means that if the first or last element is greater than their one real neighbor, they also count as peak elements.

We're also given a constraint on the time complexity: the solution needs to run in O(log n) time, which implies that a simple linear scan of the array is not efficient enough. We need to use an algorithm that repeatedly divides the array into smaller segments—binary search is an example of such an algorithm.

Given the requirement to complete the task in O(log n) time, we must discard a linear scan approach that would take O(n) time.

Instead, we adopt a binary search method due to its logarithmic time complexity, which fits our constraint. Binary search is a technique often used for searching a sorted array by repeatedly dividing the search interval in half. Although in

this case the entire array isn't sorted, we can still use binary search because of the following key insight: if an element is not a peak (meaning it's less than either of its neighbors), then a peak must exist to the side of the greater neighbor. The reason this works is because of our — bounds at both ends of the array. We imagine a slope up from — to a non-peak

element and then down from the non-peak element towards -.... Somewhere on that rising or falling slope there must be a peak, which is a local maximum. So in our modified binary search, instead of looking for a specific value, we look for any peak as follows:

2. If the middle element is greater than its right neighbor, we've found a descending slope, and there must be a peak to the left. Hence, we restrict our search to the left half of the current interval.

3. If the middle element is less than its right neighbor, we've found an ascending slope, and a peak exists to the right. We then do our next search

1. We take the middle element of the current interval and compare it with its right neighbor.

- on the right half. 4. We continue this process of narrowing down our search interval by half until we've isolated a peak element.
- This binary search on a wave-like array ensures we find a peak in O(log n) time, satisfying the problem's constraints.
- **Solution Approach**

The solution leverages a binary search algorithm, which is ideal for situations where we need to minimize the time complexity to O(log n). The essence of binary search in this context is to reduce the search space by half after each comparison, making it

much faster than a linear approach.

and right is set to the length of the array minus one (len(nums) - 1). We enter a while loop that continues as long as left is less than right, ensuring that we are still considering a range of

We initialize two pointers, left and right, which represent the boundaries of our current search interval. left is set to 0,

Inside the loop, we calculate the midpoint of the current search interval as mid = (left + right) >> 1. The >> 1 operation

On the other hand, if nums[mid] is less than or equal to nums[mid + 1], then a peak lies to the right. Thus, we set left to

Here's a step-by-step explanation of the implementation:

mid + 1, narrowing the search interval to the right half.

def findPeakElement(self, nums: List[int]) -> int:

possible positions for a peak element.

- is a bitwise shift to the right by 1 bit, which is equivalent to dividing by two, but it's often faster. We then compare the element at the mid position with the element immediately to its right (nums[mid + 1]).
- If nums[mid] is greater than nums[mid + 1], the peak must be at mid or to the left of mid. Thus, we set right to mid, effectively narrowing the search interval to the left half.
- The loop continues, halving the search space each time, until left equals right. At this point, we have found the peak because it means that nums [left] cannot be smaller than both its neighbors (as per the nums [-1] = nums [n] = -∞ rule).
- This approach guarantees finding a peak, if not the highest peak, in logarithmic time. Here's the code snippet that follows this approach:
- mid = (left + right) >> 1 if nums[mid] > nums[mid + 1]:

We exit the loop and return left, which is the index of the peak element.

else: left = mid + 1

Suppose our input array nums is [1, 2, 3, 1]. We want to find an index of a peak element.

right = mid

left, right = 0, len(nums) - 1

while left < right:</pre>

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return left
  The simplicity of binary search in conjunction with the described logic yields an efficient and elegant solution for finding a peak
  element.
Example Walkthrough
  Let's walk through the solution with a small example.
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Initial Setup The initial value of left is 0.

Iteration 1 • Calculate the midpoint: mid = (left + right) >> 1 which is (0 + 3) >> 1 = 1.

class Solution:

 Compare nums[mid] and nums[mid + 1]: nums[1] is 2, and nums[2] is 3. • Since 2 is less than 3, we are on an ascending slope. We should move right.

• Update left to mid + 1: left becomes 2.

• left is now 2 and right is 3.

The initial value of right is len(nums) - 1, which is 3.

Iteration 2

Conclusion

 Since 3 is greater than 1, we're on a descending slope. We should move left. • Update right to mid: right becomes 2.

Compare nums[mid] and nums[mid + 1]: nums[2] is 3, and nums[3] is 1.

• Calculate the new midpoint: mid = (left + right) >> 1 which is (2 + 3) >> 1 = 2.

• The loop ends when left equals right, which is now the case (left and right are both 2). • Therefore, we have found our peak at index 2 where the element is 3, and it is greater than both its neighbors (where the neighbor on the right is 1, and the neighbor on the left is 2, and conceptually — on both ends).

the peak element, satisfying the $O(\log n)$ time complexity constraint.

If the middle element is greater than its next element,

When start and end pointers meet, we've found a peak element.

int left = 0; // Initialize the left boundary of the search space

// Continue the loop until the search space is reduced to one element

int right = nums.length - 1; // Initialize the right boundary of the search space

// Using (left + (right - left) / 2) avoids potential overflow of integer addition

it means a peak element is on the left side(inclusive of mid).

Solution Implementation **Python**

def findPeakElement(self. nums: List[int]) -> int:

Initialize the start and end pointers.

Binary search to find the peak element.

start, end = 0, len(nums) - 1

Find the middle index.

mid = (start + end) // 2

public int findPeakElement(int[] nums) {

// Perform binary search

// Find the middle index

right = mid;

left = mid + 1;

function findPeakElement(nums: number[]): number {

// Find the middle index using bitwise operator

while (leftBoundary < rightBoundary) {</pre>

end = mid

else:

} else {

return left;

int mid = left + (right - left) / 2;

if (nums[mid] > nums[mid + 1]) {

// If the middle element is areater than the next element,

// If the middle element is smaller than the next element,

// At the end of the loop, left == right, which points to the peak element

const middleIndex: number = leftBoundary + ((rightBoundary - leftBoundary) >> 1);

// the peak must be in the right half (excluding mid)

// the peak must be in the left half (including mid)

// Initialize the search boundaries to the start and end of the array

Otherwise, the peak is in the right half of the array.

while (left < right) {</pre>

while start < end:</pre>

return start

from typing import List

class Solution:

Thus, the index 2 is returned.

if nums[mid] > nums[mid + 1]: end = mid# Otherwise, the peak is in the right half of the array. else: start = mid + 1

Using this approach with the given example, we can see how the binary search algorithm rapidly narrows down the search to find

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Java
class Solution {
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while (left < right) {</pre>
            // Calculate the middle index of the current search space
            int mid = left + (right - left) / 2;
            // If the middle element is greater than its next element, then a peak must be to the left (including mid)
            if (nums[mid] > nums[mid + 1]) {
                // Narrow the search space to the left half
                right = mid;
            } else {
                // Otherwise, the peak exists in the right half (excluding mid)
                // Narrow the search space to the right half
                left = mid + 1;
        // When left == right, we have found the peak element's index, return it
        return left;
C++
#include <vector> // Include vector header for using the vector container
class Solution {
public:
    int findPeakElement(vector<int>& nums) {
        // Initialize the left and right pointers
        int left = 0;
        int right = nums.size() - 1;
```

let leftBoundary: number = 0; let rightBoundary: number = nums.length - 1; // Continue searching as long as the search space contains more than one element

};

TypeScript

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// Compare the middle element to its next element
        if (nums[middleIndex] > nums[middleIndex + 1]) {
            // If the middle element is greater than the next element,
            // then a peak element is in the left half (including middle)
            rightBoundary = middleIndex;
        } else {
            // Otherwise, the peak element is in the right half (excluding middle)
            leftBoundary = middleIndex + 1;
   // When leftBoundary equals rightBoundary, we found the peak element.
   // Return its index.
   return leftBoundary;
from typing import List
class Solution:
   def findPeakElement(self, nums: List[int]) -> int:
       # Initialize the start and end pointers.
       start, end = 0, len(nums) - 1
       # Binary search to find the peak element.
       while start < end:</pre>
           # Find the middle index.
           mid = (start + end) // 2
           # If the middle element is greater than its next element,
           # it means a peak element is on the left side(inclusive of mid).
            if nums[mid] > nums[mid + 1]:
```

start = mid + 1# When start and end pointers meet, we've found a peak element. return start

Time and Space Complexity The time complexity of the provided algorithm is $O(\log n)$, where n is the length of the input array nums. The algorithm uses a binary search approach, whereby at each step, it halves the search space. This halving continues until the peak element is found,

requiring at most log2(n) iterations to converge on a single element. The space complexity of the algorithm is 0(1) as it only uses a constant amount of extra space. The variables left, right, and mid, along with a few others for storing intermediate results, do not vary with the size of the input array nums, ensuring that the space used remains fixed.