112. Path Sum **Binary Tree** Depth-First Search **Breadth-First Search Leetcode Link** Tree Easy

Problem Description

node down to any leaf node such that the sum of the values of all the nodes along the path is equal to the given integer targetSum. A leaf node is defined as a node that does not have any children. If such a path exists, the function should return true; otherwise, it

The problem presents a binary tree where each node contains an integer value. The goal is to find out if there is a path from the root

should return false.

Intuition The solution to this problem is based on the Depth-First Search (DFS) algorithm. DFS is a common tree traversal method that can be

alternative path. We traverse down one branch of the tree, adding the values of each node we pass through, until we reach a leaf. Once at a leaf, we check if the accumulated sum is equal to targetSum. If we hit a leaf and the sum does not equal targetSum, we backtrack and try a different path. This backtracking is naturally handled

The intuition behind using DFS in this particular problem is the need to explore each possible path fully before moving to an

Thus, the solution approach is to start from the root and explore each branch recursively, carrying forwards the cumulative sum. If at any point we reach a leaf and the sum matches targetSum, we return true. Otherwise, if we exhaust all paths and none meet the

criteria, we return false. As part of the recursion, we ensure two things:

1. If the current node is None (i.e., we've reached beyond a leaf), this path is not valid, and we return false. 2. When we reach a leaf node (both its children are None), we check if the cumulative sum equals targetSum and return the result of

this comparison.

by the call stack in a recursive DFS approach.

The provided code defines a nested dfs function inside the main function hasPathSum that handles the recursive traversal and the

used efficiently to search all possible paths in a tree from the root node down to the leaves.

accumulation of the sum.

Solution Approach The solution utilizes a straightforward recursive DFS strategy. By defining a helper function dfs(root, s), we can keep track of the

current sum s as we traverse down the tree. The base case checks if the current node root is None, meaning that the path has

reached beyond a leaf node, and hence, it returns False since there cannot be a valid path through a non-existing node.

When the recursive function dfs is called, it performs the following steps:

1 def dfs(root, s):

1 return dfs(root, 0)

22.

return True

path, the function will return True.

1. It first checks if the current node is None. If true, the recursion stops and returns False. 2. If the current node is not None, it adds the node's value to the ongoing sum s.

3. Next, it checks if the current node is a leaf (both root.left and root.right are None). If it is a leaf, and s equals targetSum, it

indicates that a valid path has been found and returns True. 4. If the current node is not a leaf, the function proceeds to call itself recursively for both the left and right children of the current

- node, if they exist (dfs(root.left, s) and dfs(root.right, s)).
- 5. The result of these recursive calls is combined using logical OR (or), which means if either the left or the right subtree has a valid
- The dfs function encapsulates the logic for searching the tree and determining if a valid path exists that sums up to targetSum. It is initiated by passing the root of the tree and an initial sum of 0 to the dfs function.
- Here is how the dfs function is implemented within the context of the provided solution code snippet:
- if root is None: # Base case: empty node, return False return False s += root.val # Increment the sum by the current node's value # If it's a leaf and the sum matches targetSum, return True if root.left is None and root.right is None and s == targetSum:

And the hasPathSum function then calls this dfs function with the initial parameters:

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In summary, the recursive function explores all possible paths from the root to each leaf, checking for a match against targetSum. It
returns True as soon as a valid path is found, or False if no such path exists, effectively implementing a depth-first search for the
problem at hand.
Example Walkthrough
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Recursively search the left and right subtrees

return dfs(root.left, s) or dfs(root.right, s)

Let's walk through a small example to illustrate the solution approach. Assume we have the following binary tree and targetSum of

Call dfs(root=4, s=5) to continue on the left child.

Call dfs(root=11, s=9).

Now, let's follow the dfs function to see how it works:

First, call dfs(root=7, s=20). Then we will call dfs(root=2, s=20), but let's follow the first call for now.

5. At node 7, s becomes 27 (20 + 7). This is a leaf, but s is not equal to the targetSum of 22. Returns False.

Once True is encountered, the function does not need to explore any further branches. The propagation of True through the

recursive calls will eventually lead to the hasPathSum function returning True, indicating that there is a path that adds up to the

The binary tree has successfully been searched with a depth-first approach to find a path sum that matches the target. In this case,

4. At node 11, s becomes 20 (9 + 11). Not a leaf, we have two children, so we make two recursive calls.

2. At root (5), s becomes 5 (0 + 5). This node is not a leaf, so we make recursive calls for left and right children.

1. Begin at the root (node with value 5), with a starting sum s of 0. Call dfs(root=5, s=0).

3. At node 4, s becomes 9 (s + 4). This is also not a leaf. Recursive call on left child.

- Backtrack to node 11 and proceed with the second call, dfs(root=2, s=20). 6. At node 2, s becomes 22 (20 + 2). This is a leaf and s matches targetSum. Returns True.
- the path with values [5, 4, 11, 2] yields the desired sum, and so our problem is solved with the function returning True.

self.right = right class Solution: def hasPathSum(self, root: Optional[TreeNode], target_sum: int) -> bool: 10 Determines if the tree has a root-to-leaf path such that 11 12 adding up all the values along the path equals the given sum.

22 to find a root-to-leaf path that sums to the target_sum. 23 24 :param node: TreeNode, the current node being traversed 25 :param current_sum: int, the sum of the values from the root node up to the current node 26 :return: bool, True if a path is found, False otherwise

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targetSum of 22.

Python Solution

2 class TreeNode:

Definition for a binary tree node.

self.current_sum = left

def dfs(node, current_sum):

self.val = val

def __init__(self, val=0, left=None, right=None):

:param root: TreeNode, the root of the binary tree

* @return True if such a path exists, otherwise false.

public boolean hasPathSum(TreeNode root, int targetSum) {

* Helper method to perform depth-first search to find the path sum.

* @return True if a path with the given sum is found, otherwise false.

// If the node is null, we've hit a dead end and should return false.

// Check if the current node is a leaf and the current sum equals zero,

private boolean hasPathSumDFS(TreeNode node, int currentSum) {

// Subtract the value of current node from current sum.

return hasPathSumDFS(root, targetSum);

* @param node The current node being visited.

if (node == null) {

return false;

currentSum -= node.val;

* @param currentSum The sum accumulated so far.

:param target_sum: int, the target sum to be achieved

:return: bool, True if such a path exists, False otherwise

Depth-first search helper function that traverses the tree

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               if node is None:
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                   # Base case: if the current node is None, no path exists
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                    return False
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32
               # Update the current_sum by adding the current node's value
                current_sum += node.val
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               # Check if the current node is a leaf and matches the target_sum
               if node.left is None and node.right is None and current_sum == target_sum:
36
37
                    return True
38
               # Recursively search in the left and right subtrees for the path
39
               # If either subtree returns True, a valid path has been found
40
                return dfs(node.left, current_sum) or dfs(node.right, current_sum)
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42
           # Start DFS traversal from the root with an initial sum of 0
43
           return dfs(root, 0)
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Java Solution
1 /**
   * Definition for a binary tree node.
   class TreeNode {
       int val;
       TreeNode left;
       TreeNode right;
       TreeNode() {}
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10
       TreeNode(int val) {
11
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           this.val = val;
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       TreeNode(int val, TreeNode left, TreeNode right) {
           this.val = val;
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17
           this.left = left;
           this.right = right;
18
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20 }
21
   class Solution {
23
       /**
        * Returns true if the tree has a root-to-leaf path such that adding up all the values along the path equals the given target sun
24
25
        * @param root The root of the binary tree.
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        * @param targetSum The target sum to find.
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51 // which means we've found a path with the required sum. 52 54

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/**

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if (node.left == null && node.right == null && currentSum == 0) {
               return true;
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           // Recursively check the left and right subtrees for the remaining sum.
57
           // If either subtree returns true, a path has been found.
           return hasPathSumDFS(node.left, currentSum) || hasPathSumDFS(node.right, currentSum);
58
59
60 }
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C++ Solution
   // Definition for a binary tree node
 2 struct TreeNode {
       int val;
       TreeNode *left;
       TreeNode *right;
       // Constructor to initialize a tree node with a value and optional left and right children
       TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
       // Constructor to initialize a tree node with a value and both children
       TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}
10 };
11
12 class Solution {
13 public:
       // Checks if the binary tree has a root-to-leaf path that sums up to the targetSum
14
       bool hasPathSum(TreeNode* root, int targetSum) {
           // Lambda function that performs depth-first search on the tree to find path sum
           // [&] captures local variables by reference
           std::function<bool(TreeNode*, int)> dfs = [&](TreeNode* node, int sumSoFar) -> bool {
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               // If the node is null, return false as we've reached beyond a leaf node
19
               if (!node) return false;
20
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               // Add the current node's value to the running sum
23
               sumSoFar += node->val;
24
25
               // Check if the current node is a leaf and the sum equals the targetSum
26
               if (!node->left && !node->right && sumSoFar == targetSum) {
                   return true;
28
29
               // Continue searching in the left and right subtrees
30
31
               // If any of the recursive calls return true, the whole expression will be true
32
               // Utilize the short-circuit evaluation of the '||' operator
33
               return dfs(node->left, sumSoFar) || dfs(node->right, sumSoFar);
           };
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           // Start the depth-first search from the root node with an initial sum of 0
           return dfs(root, 0);
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  };
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Typescript Solution
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if (root === null) { 17 return false; 18 19 20 // Destructure the current node to get its value and its children.

const { val, left, right } = root;

return targetSum - val === 0;

Time and Space Complexity

if (left === null && right === null) {

2 type TreeNode = {

6 };

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val: number;

left: TreeNode | null;

right: TreeNode | null;

// Typescript type definition for a binary tree node.

* @param {TreeNode | null} root - The root node of the binary tree.

* @param {number} targetSum - The target sum to find the path for.

* @returns {boolean} - True if such a path exists, otherwise False.

// If the root is null, there is no path, return false.

// If the node is a leaf (no left or right children),

function hasPathSum(root: TreeNode | null, targetSum: number): boolean {

// Check if subtracting the node's value from the target sum equals 0.

* Determines if the binary tree has a root-to-leaf path that sums up to the given target sum.

// Recursively check the left and right subtrees reducing the target sum by the current node's value.

// Return true if either subtree has a path that sums up to the adjusted target sum.

return hasPathSum(left, targetSum - val) || hasPathSum(right, targetSum - val);

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Time Complexity
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The time complexity of the given code is O(n), where n is the number of nodes in the binary tree. The reason for this is that the code implements a depth-first search (DFS) algorithm, which visits each node exactly once in the worst-case scenario.

Space Complexity

The space complexity of the code is O(h), where h is the height of the binary tree. This space is used by the execution stack for recursive calls. In the worst-case scenario where the tree is completely unbalanced, the space complexity will be O(n). But on a balanced tree, the height h can be considered as $O(\log n)$, making the average space complexity $O(\log n)$.