898. Bitwise ORs of Subarrays Bit Manipulation Array Medium **Dynamic Programming**

Problem Description

OR results that can be obtained from all possible non-empty contiguous subarrays of arr.

The problem presents us with a task: given an array arr of integers, we are required to find the total number of distinct bitwise

To understand the problem better, let's clarify some concepts:

Bitwise OR (|): A binary operation that takes two bit patterns of equal length and performs the logical inclusive OR operation on each pair of corresponding bits. The result in each position is 1 if at least one of the bits is 1.

- Subarray: A sequence of elements within an array that is contiguous (elements are consecutive without gaps) and nonempty.
- Distinct: Each unique value should be counted only once in the final tally.
- The problem, therefore, requires us to explore and assess every possible subarray that can be generated from the given array, perform the bitwise OR operation on its elements, and count the unique outcomes.

ntuition

The intuitive approach to solving this problem might involve a brute force strategy - calculating the bitwise OR for every subarray and then utilizing a set to count the distinct values. However, this approach would result in a high time complexity due to the multiple nested loops required (each subarray is recursively built starting from each element).

Iterative Building: It takes advantage of the fact that the bitwise OR of a subarray ending at position i depends upon the

bitwise OR result of the subarray ending at i-1. The prev variable is used to accumulate the bitwise OR result till the current

element, so that for the next element, we don't have to start from scratch.

Calculate the bitwise OR for the current subarray and add it to the set s.

• Finally, return the length of set s, which represents the number of distinct bitwise ORs.

Once the current subarray OR equals the accumulated prev OR, break early.

The solution code, however, uses a clever strategy that reduces the amount of redundant computation:

- Early Breaking: It recognizes that if a new subarray's bitwise OR equals the accumulated OR (prev), we can stop early because all subsequent subarrays will only give the same or greater OR results, which we would already have encountered due to the nature of the OR operation building on previous subarrays. Set for Uniqueness: The set s is used to store unique bitwise OR results. This way, every time we add a new OR result,
- The main algorithm goes as follows: Initialize a set s to keep track of distinct bitwise OR results.
- Loop over each element v in the array: • Start a prev accumulator that holds the bitwise OR up to the current element. Loop backwards from the current element to the beginning of the array:

By using the set and early breaking, the solution immensely reduces the number of calculations compared to the brute force approach, and therefore, is much more efficient.

Solution Approach

computation.

Example Walkthrough

Initialize a set and variables:

 \circ For element 1 (i=0), set prev = 1.

Variable prev is initialized.

duplicate values are inherently avoided.

of all subarrays. Here's how the approach works in detail: We initialize an empty set s that will hold the distinct bitwise OR results. Apart from this, we have a prev variable that is used

The implementation of the reference solution makes use of sets and two pointers to efficiently compute the distinct bitwise ORs

to keep track of the bitwise OR up to the current element in the outer loop, which goes through each element i in the array.

As we iterate over each element v in the array using an index i, we first update the prev variable to hold the bitwise OR

between itself and the current element (prev |=v|). This new prev will be the bitwise OR of all elements from the beginning of the array up to the current element i.

new variable curr to hold the result of bitwise ORs for the subarrays ending in the current element i.

3. In the inner loop, we start from the current element and go backwards through the array using another index j. We create a

During each iteration of the inner loop, we update curr to be the bitwise OR of itself and the current j th element (curr |=

The early breaking condition is checked (if curr == prev), which is based on the understanding that once the current

subarray's OR matches the overall OR up to the current element (prev), all subsequent larger subarrays will yield the same

OR value and have been considered before. When this condition is met, the inner loop breaks, avoiding unnecessary

Lastly, once both loops are done, the length of set s will represent the number of distinct bitwise ORs that can be formed

- arr[j]). After updating curr, we add it to the set s. This operation ensures that only distinct OR results are kept, as sets do not store duplicate elements.
- from all the subarrays of arr. This is the result that the function returns. The above steps form an efficient algorithm as it reduces the number of subarrays we need to check, leveraging the properties of

cases on platforms like LeetCode, where the input size can be large and brute force methods would result in a timeout error.

the bitwise OR operation and making use of sets to maintain distinct entries. Such an optimization is essential to pass all test

Let's say we have an array arr = [1, 2, 3]. We will apply the solution approach step by step:

At i=0: Only one subarray [1]:

Final Result:

Solution Implementation

unique or results = set()

prev |= value

current = 0

Python

Java

class Solution {

class Solution:

prev = 0

curr = 1

o Set s = {}

Set s becomes {1} At i=1: Subarrays [2], [1, 2]:

Since curr now equals prev, inner loop breaks early.

At i=2: Subarrays [3], [2, 3], but we stop at [2, 3] because:

Utilized at each step in the inner loop when curr matches prev.

Outer loop - Iterate over each element in the array:

 \circ For element 2 (i=1), prev becomes prev | 2 = 1 | 2 = 3.

 \circ For element 3 (i=2), prev becomes prev | 3 = 3 | 3 = 3.

Inner loop - Backward iteration from current element:

To illustrate the solution approach, let's take a small example:

curr = 3, already in set s, no need to add. ■ Loop attempts to compute curr = 3 | 2, but since prev is already 3, the inner loop breaks. Early Breaking:

• curr = 2 | 1 = 3, add to set $s \rightarrow \{1, 2, 3\}$

• curr = 2, add to set $s \rightarrow \{1, 2\}$

 The length of set s is 3, representing the distinct bitwise OR results: {1, 2, 3}. Each bitwise OR operation only computes new results, while duplicates are ignored due to the set data structure. By breaking

def subarravBitwiseORs(self. arr: List[int]) -> int:

for index, value in enumerate(arr):

for i in range(index, -1, -1):

current |= arr[i]

public int subarrayBitwiseORs(int[] arr) {

int aggregate = 0;

for (int i = 0; i < arr.length; ++i) {</pre>

for (int i = i; i >= 0; --i) {

for (int i = i; i >= 0; --i) {

if (subarrayOr == currentOr) break;

// The TypeScript standard library already includes Set, so we don't need

// Function to count the number of distinct bitwise OR values of all subsequences.

// Iterate from the current element to the beginning of the array.

Update 'prev' by taking the OR with the current value

Add 'current' to the set of unique OR results

let uniqueOrValues: Set<number> = new Set(); // To store unique OR values of subarrays.

uniqueOrValues.add(subarrayOr); // Store the calculated OR in the set.

export { subarrayBitwiseORs }; // Export the function to be available for import in other modules.

// The size of the set represents the number of distinct OR values of all subarrays.

Iterate backwards from the current index to the start of the array

Update 'current' by taking the OR with the value at j

// Break the loop if the subarray OR equals the currently calculated OR (all bits already set).

'current' will hold the cumulative OR result starting from 'index' going back to the start

If 'current' equals 'prev', no new unique values can be found by continuing; break

// a separate import for unordered_set as we would in C++.

if (subarrayOr === currentOr) break;

function subarrayBitwiseORs(arr: number[]): number {

// Iterate over each element in the array.

let subarrayOr: number = 0;

for index, value in enumerate(arr):

for i in range(index, -1, -1):

unique or results.add(current)

Return the number of unique bitwise OR results found

current |= arr[i]

if current == prev:

break

return len(unique_or_results)

Time and Space Complexity

current progression in curr.

much smaller than n^2 .

perform significantly better.

number of unique OR values across all subarrays.

Space Complexity

Time Complexity

for (let i = 0; i < arr.length; i++) {</pre>

for (let i = i; i >= 0; i--) {

subarrayOr |= arr[i];

let current0r: number = 0;

currentOr |= arr[i];

return uniqueOrValues.size;

prev |= value

current = 0

subarrayOr |= arr[i];

return uniqueOrValues.size();

aggregate |= arr[j];

Set<Integer> uniqueBitwiseORs = new HashSet<>();

// We iterate through each element in the array

Initialize a set to store unique bitwise OR results

Iterate over the input array with both value and index

'prev' will hold the cumulative OR result of the current iteration

Iterate backwards from the current index to the start of the array

Update 'current' by taking the OR with the value at j

// We use a set to store unique values of bitwise ORs for all subarrays

// We iterate from the current element down to the start of the array

due to the properties of bitwise OR, so we break out early. */

uniqueOrValues.insert(subarrayOr); // Store the calculated OR in the set.

// The size of the set represents the number of distinct OR values of all subarrays.

// Break the loop if the subarray OR equals the currently calculated OR (all bits already set).

// 'aggregate' will hold the cumulative bitwise OR value up to the current element

// We calculate the bitwise OR from the current element to the 'jth' element

Update 'prev' by taking the OR with the current value

Add 'current' to the set of unique OR results

unique or results.add(current) # If 'current' equals 'prev', no new unique values can be found by continuing; break if current == prev: break # Return the number of unique bitwise OR results found return len(unique_or_results)

early from the inner loop, we avoid unnecessary computation, optimizing the process. This compact example covers all the main

elements present in the solution approach, demonstrating its efficiency and how it leads to the final answer.

'current' will hold the cumulative OR result starting from 'index' going back to the start

```
// Add the current subarray's bitwise OR to the set
uniqueBitwiseORs.add(aggregate);
/* If the current aggregate value is the same as the previous
   aggregate value, all future aggregates will also be the same
```

```
if (aggregate == (aggregate | arr[i])) {
                 break;
       // Return the number of unique bitwise ORs found
       return uniqueBitwiseORs.size();
C++
#include <vector>
#include <unordered_set>
class Solution {
public:
   // Function to count the number of distinct bitwise OR values of all subarrays.
   int subarrayBitwiseORs(vector<int>& arr) {
       unordered set<int> uniqueOrValues; // To store unique OR values of subarrays.
       int current0r = 0;
                                      // To store the running OR value of the current subarray.
       // Iterate over each element in the array.
       for (int i = 0; i < arr.size(); ++i) {</pre>
          int subarrayOr = 0;  // Used to calculate OR for each possible subarray ending at 'i'.
          // Iterate from the current element to the beginning of the array.
```

// Update the OR for the subarray ending at 'i' starting at 'j'.

// To store the running OR value of the current subarray.

// Used to calculate OR for each possible subarray ending at 'i'.

// Update the running OR with the current element.

// Update the OR for the subarray ending at 'i' starting at 'j'.

def subarravBitwiseORs(self, arr: List[int]) -> int: # Initialize a set to store unique bitwise OR results unique or results = set() # 'prev' will hold the cumulative OR result of the current iteration prev = 0 # Iterate over the input array with both value and index

class Solution:

};

TypeScript

The time complexity of this algorithm mainly depends on the number of iterations within the double-loop structure. • The outer loop runs exactly n times where n is the number of elements in arr.

The given code aims to find the number of distinct subarray bitwise ORs. To do this, it iterates over the given array and computes

the OR of elements from the current element to all previous elements by keeping a record of the previous OR in previoud the

However, due to the properties of the bitwise OR operation, repetitions are likely to occur much earlier, resulting in earlier breaks

from the inner loop. Specifically, the sequence of ORs will eventually stablize into a set of values that does not grow with each

additional OR operation. The actual number of unique elements in these OR sequences across all iterations is bounded by a factor

While it's difficult to put a precise bound on this without specifics about the input distribution, let's denote the average unique sequence length as k (which is considerably smaller than n due to the saturation of OR operations). Therefore, the total number

• The inner loop runs up to i+1 times in the worst case (when curr never equals prev early).

of operations is approximately 0(n*k). However, it is important to note that k is not guaranteed to be a constant and its relation with n can depend heavily on the input,

time complexity argument, this won't actually occur due to the saturation of bitwise ORs.

The space complexity is due to the set s that is used to store the unique subarray OR results. • In the worst case, each subarray OR could be unique, which means the set could grow to the size of the sum of all subarray counts. As with the

implying that in the worst case the time complexity could tend towards 0(n^2), but in practical scenarios, it is expected to

Let m represent the maximum possible unique OR values which can be much less than the total subarray count of roughly n* (n+1)/2. Therefore, the space complexity can be approximated as 0(m). In conclusion, the time complexity of the code is approximately 0(n*k) (with k being influenced by the input nature and much

smaller than n) and space complexity is around O(m) for storing the unique OR results set, where m represents the maximum