712. Minimum ASCII Delete Sum for Two Strings String] Medium **Dynamic Programming**

are the lengths of s1 and s2 respectively, we build up to the solution.

respectively. This table will hold the solutions to subproblems, initialized with zeros.

Problem Description

we need to find out how many and which characters we should delete (from either or both strings) so that the remaining characters of s1 and s2 will be the same, and the sum of the ASCII values of these deleted characters is as small as possible. We only need the sum, not the specific characters to delete.

This problem asks for the lowest ASCII sum of deleted characters to make two given strings, s1 and s2, equal. In other words,

Intuition The solution to this problem involves dynamic programming, a method for solving complex problems by breaking them down into simpler subproblems. We can visualize the problem as a grid where one string (s1) forms the rows and the other string (s2) forms the columns. Each cell in the grid represents the cost (lowest ASCII sum of deleted characters) to make the substrings

equal up to that point.

Here's the intuition broken down into steps: **Subproblem Definition**: Define f[i][j] as the minimum cost to make the first i characters of s1 and the first j characters of s2 equal. Initial Conditions: Start by filling in the base cases. If one string is empty (i or j is 0), then f[i][j] is the sum of the ASCII

- values of all the characters in the other string up to that point.
- Iterative Solution: For each character pair (from s1[i] and s2[j]), we check if the characters are equal. If they are, the cost does not increase and it's the same as the cost for f[i-1][j-1]. If they aren't, we choose the cheaper option between
- deleting a character from s1 or s2. This means we add the ASCII value of the character we consider deleting to the corresponding cost, and we take the minimum of both options as our new cost for f[i][j].

Build Up Solution: By filling out the grid following these rules, starting from f[0][0] and going to f[m][n] where m and n

Final Answer: After the grid is entirely filled, the answer to the problem will be the value at f[m] [n], as it represents the cost

- of making both entire strings s1 and s2 equal. By constructing this table, we systematically consider the cost of each possible operation, ensuring that we arrive at the minimum total cost for the entire strings.
- The implementation of this solution utilizes dynamic programming, which involves storing and reusing solutions to subproblems in order to build up to the solution for the whole problem. The specific data structure used here to implement dynamic programming is a 2-dimensional list (a list of lists), which acts as a table to store the minimum cost for each subproblem.

The algorithm proceeds as follows: Initialize the Table: Create a 2D list f with dimensions $(m+1) \times (n+1)$, where m and n are the lengths of s1 and s2,

Set Up Base Cases: Populate the first row and the first column of the table f. Each cell in the first row represents the

minimum ASCII sum for making the first i characters of s1 equal to an empty s2 by deleting characters. Each cell in the first

column represents the same but for s2 to an empty s1.

for i in range(1, m + 1):

f[i][0] = f[i - 1][0] + ord(s1[i - 1])

the following rules to calculate f[i][j]:

for j in range(1, n + 1):

else:

Example Walkthrough

[0, 0, 0, 0]

[0, 0, 0, 0],

[0, 0, 0, 0],

if s1[i - 1] == s2[i - 1]:

f[i][j] = min(

grid will look like this with m=3 and n=3:

After converting characters to their ASCII sums:

f[i][j] = f[i - 1][j - 1]

f[i - 1][i] + ord(s1[i - 1]),

Solution Approach

for j in range(1, n + 1): f[0][j] = f[0][j-1] + ord(s2[j-1])

Fill in the Table: Loop through each cell of the table (excluding the first row and column which are already filled) and apply

- \circ If s1[i-1] == s2[j-1], set f[i][j] to f[i-1][j-1], since there is no need to delete any character when they are the same. ∘ If s1[i - 1] != s2[j - 1], set f[i][j] to the minimum between f[i - 1][j] + ord(s1[i - 1]) and f[i][j - 1] + ord(s2[j - 1]). This represents the cost of making strings equal either by deleting the current character from s1 or s2. for i in range(1, m + 1):
- f[i][j-1] + ord(s2[j-1])Extract the Final Answer: After populating the entire table, read the value f[m] [n]. This cell holds the minimum ASCII sum of deleted characters to make the two strings equal. By following this approach, the algorithm ensures that all possible deletions are considered, and the best choice is made at each step, leading to the optimal solution.

Let's walk through a small example to illustrate the solution approach described above. Suppose we have two strings s1 = "sea"

Initialization: We start by initializing a 2D list f with the dimensions $(m+1) \times (n+1)$. For s1 = "sea" and s2 = "eat", the

and s2 = "eat". We want to find the lowest ASCII sum of characters that need to be deleted to make s1 and s2 equal.

[0, 0, 0, 0]] Set Up Base Cases: Next, we populate the first row and the first column based on the ASCII sum of the prefixes of s1 and

[[0, 'e', 'a', 't'], ['s', 0, 0, 0], ['e', 0, 0, 0], ['a', 0, 0, 0]]

[[0, 101, 197, 314],

[[0, 101, 197, 314],

[115, 216, 313, 330],

[216, 115, 216, 313],

[313, 216, 209, 216]]

"eat" to make them equal is 216.

Solution Implementation

Python

Java

C++

using namespace std;

class Solution {

TypeScript

const s1Length = s1.length;

const s2Length = s2.length;

for (let i = 1; i <= s1Length; ++i) {</pre>

for (let j = 1; j <= s2Length; ++j) {</pre>

for (let i = 1; i <= s1Length; ++i) {</pre>

} else {

return dp[s1Length][s2Length];

class Solution:

for (let i = 1; i <= s2Length; ++i) {</pre>

dp[i][i] = Math.min(

if (s1[i - 1] === s2[i - 1]) {

dp[i][j] = dp[i - 1][j - 1];

// The last cell of the dp table will have the answer

def minimumDeleteSum(self, s1: str, s2: str) -> int:

 $dp = [[0] * (len_s2 + 1) for _ in range(len_s1 + 1)]$

dp[i][0] = dp[i - 1][0] + ord(s1[i - 1])

dp[0][j] = dp[0][j - 1] + ord(s2[j - 1])

Pre-fill the first column with the delete sum of s1[i:]

Pre-fill the first row with the delete sum of s2[j:]

Start filling the DP table from (1,1) to (len_s1, len_s2)

Calculate the length of both strings

 len_s1 , $len_s2 = len(s1)$, len(s2)

for i in range(1, len s1 + 1):

for j in range(1, len s2 + 1):

for i in range(1, len s1 + 1):

dp[i][i] = min(

// value of the deleted character

class Solution:

s2:

[115, 0, 0, 0], [115 + 101, 0, 0, 0],[115 + 101 + 97, 0, 0, 0]

The fully populated base cases are: [[0, 101, 197, 314], [115, 0, 0, 0], [216, 0, 0, 0], [313, 0, 0, 0]

For f[1][1]: 's' vs 'e', they are different, so we take the min between f[0][1] + ASCII('s') = 101 + 115 and f[1][0] +

For f[1][2]: 's' vs 'a', they are different, so we take the min between f[0][2] + ASCII('s') = 197 + 115 and f[1][1] +

The logic behind each calculation is to minimize the ASCII sum required to make the two substrings equal, considering

Extract the Final Answer: The value of f[3][3] represents the minimum ASCII sum of deleted characters to make s1 and s2 equal. From the table, this value is 216. Therefore, the lowest ASCII sum of characters that need to be deleted from "sea" and

def minimumDeleteSum(self, s1: str, s2: str) -> int:

 $dp = [[0] * (len_s2 + 1) for _ in range(len_s1 + 1)]$

Pre-fill the first column with the delete sum of s1[i:]

Calculate the length of both strings

for j in range(1, len s2 + 1):

dp[i][i] = min(

for (int i = 1; i <= length1; ++i) {</pre>

for (int i = 1; i <= length2; ++i) {</pre>

for (int i = 1; i <= length1; ++i) {</pre>

} else {

return dp[length1][length2];

#include <cstring> // for using memset

#include <algorithm> // for using min function

function minimumDeleteSum(s1: string, s2: string): number {

dp[i][0] = dp[i - 1][0] + s1.charCodeAt(i - 1);

dp[0][j] = dp[0][j - 1] + s2.charCodeAt(j - 1);

// Dynamic programming to fill out the rest of the dp table

// If characters match, take the diagonal value

dp[i - 1][i] + s1.charCodeAt(i - 1),

dp[i][j-1] + s2.charCodeAt(j-1),

Initialize a 2D array to store the minimum delete sum for sub-problems

Find the minimum between deleting a character from s1 or s2

dp[i-1][j] + ord(s1[i-1]), # Delete from s1

dp[i][j-1] + ord(s2[j-1]) # Delete from s2

The value at dp[len s1][len_s2] will be the minimum delete sum for s1 and s2

// Initialize a 2D array to store the minimum delete sum dp values

const dp = Array.from({ length: s1Length + 1 }, () => Array(s2Length + 1).fill(0));

// Fill out the base cases for the first row, cumulative ASCII sum of s1's prefixes

// Fill out the base cases for the first column, cumulative ASCII sum of s2's prefixes

// Otherwise, take the minimum of deleting from s1 or s2, and add the ASCII

for (int j = 1; j <= length2; ++j) {</pre>

dp[i][0] = dp[i - 1][0] + s1.charAt(i - 1);

dp[0][j] = dp[0][j - 1] + s2.charAt(j - 1);

dp[i][j] = dp[i - 1][j - 1];

else:

return dp[len s1][len s2]

if s1[i - 1] == s2[i - 1]:

dp[i][j] = dp[i - 1][j - 1]

 len_s1 , $len_s2 = len(s1)$, len(s2)

whether we should delete a character from s1 or s2 at each step.

Initialize a 2D array to store the minimum delete sum for sub-problems

If the current characters are equal, then no deletion is needed

dp[i-1][i] + ord(s1[i-1]). # Delete from s1

dp[i][j-1] + ord(s2[j-1]) # Delete from s2

The value at dp[len s1][len_s2] will be the minimum delete sum for s1 and s2

// Fill in the first column with the ASCII values of characters of sl

// Fill in the first row with the ASCII values of characters of s2

// Calculate the minimum delete sum for each substring of s1 and s2

// If characters are different, calculate the minimum delete sum

// by comparing the cost of deleting from s1 to the cost of deleting from s2

// The answer is in dp[length1][length2] which contains the minimum delete sum to make the strings equal

dp[i][j] = Math.min(dp[i - 1][j] + s1.charAt(i - 1), dp[i][j - 1] + s2.charAt(j - 1));

if $(s1.charAt(i - 1) == s2.charAt(j - 1)) {$

Find the minimum between deleting a character from s1 or s2

Fill in the Table: Now, we loop through the rest of the cells:

And so on, until we fill the entire table:

ASCII('e') = 115 + 101. We choose the minimum which is 216, so f[1][1] = 216.

ASCII('a') = 216 + 97. We choose the minimum which is 216 + 97, so f[1][2] = 313.

- for i in range(1, len s1 + 1): dp[i][0] = dp[i - 1][0] + ord(s1[i - 1])# Pre-fill the first row with the delete sum of s2[j:] for j in range(1, len s2 + 1): dp[0][j] = dp[0][j-1] + ord(s2[j-1])# Start filling the DP table from (1,1) to (len_s1, len_s2) for i in range(1, len s1 + 1):
- class Solution { public int minimumDeleteSum(String s1, String s2) { // Lengths of strings s1 and s2 int length1 = s1.length(), length2 = s2.length(); // Initialize a 2D array to store the minimum delete sum int[][] dp = new int[length1 + 1][length2 + 1];

// If the current characters are the same, no need to delete, so copy the value from dp[i-1][j-1]

```
public:
   int minimumDeleteSum(string s1, string s2) {
       int m = s1.size();
       int n = s2.size();
       // dp array to store the minimum ASCII delete sum for two substrings ending up to (i-1) in s1 and (j-1) in s2
       int dp[m + 1][n + 1];
       // Initializing the dp array with 0's
       memset(dp, 0, sizeof(dp));
       // Calculate the delete sum for s1 when s2 is empty
        for (int i = 1; i <= m; ++i) {
           dp[i][0] = dp[i - 1][0] + s1[i - 1];
       // Calculate the delete sum for s2 when s1 is empty
        for (int i = 1; i <= n; ++i) {
           dp[0][j] = dp[0][j - 1] + s2[j - 1];
       // Compute dp values in a bottom-up manner
        for (int i = 1; i <= m; ++i) {
            for (int j = 1; j <= n; ++j) {
               // If characters are the same, no need to delete, carry over the sum from previous subproblem
               if (s1[i - 1] == s2[i - 1]) {
                    dp[i][j] = dp[i - 1][j - 1];
                } else {
                   // Otherwise, choose the minimum sum achieved by deleting character from either s1 or s2
                    dp[i][j] = min(dp[i - 1][j] + s1[i - 1], dp[i][j - 1] + s2[j - 1]);
       // The final result is stored in dp[m][n], which involves the whole of s1 and s2
       return dp[m][n];
};
```

for j in range(1, len s2 + 1): # If the current characters are equal, then no deletion is needed if s1[i - 1] == s2[i - 1]: dp[i][j] = dp[i - 1][j - 1]else:

The time complexity of the code is determined by the nested loops that iterate over the lengths of both strings s1 and s2. Since we iterate over all i from 1 to m and all j from 1 to n, where m is the length of s1 and n is the length of s2, the time complexity is 0(m * n).

return dp[len_s1][len_s2]

Time and Space Complexity

Time Complexity

Space Complexity

The space complexity of the code is primarily due to the 2D list f, which has dimensions (m + 1) x (n + 1), requiring a total of (m + 1) * (n + 1) space. So, the space complexity is also 0(m * n).