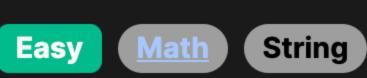
## 1071. Greatest Common Divisor of Strings



### **Problem Description**

another if it can be repeated some number of times to obtain the other string. For example, if we have str1 = "abcabc" and str2 = "abc", then str2 divides str1 because we can concatenate str2 with itself twice to get str1. In other words, str1 is the result of appending str2 to itself multiple times. The challenge is to identify the largest common string that can divide both str1 and str2 in a similar fashion.

The provided problem involves finding the largest string x that can divide two input strings str1 and str2. One string divides

To illustrate further, if str1 is "ababab" and str2 is "abab", the string "ab" is the answer since it is the largest string that divides both str1 and str2.

Intuition

(GCD), but rather than numbers, we're dealing with strings. The key insight is that if there exists such a common string x that divides both str1 and str2, then the concatenation of str1 with str2 (str1 + str2) should be the same as the concatenation of str2 with str1 (str2 + str1). If this condition doesn't hold, it implies there is no such common string and the answer is an empty string. Assuming the condition is true, we can find the length of the largest string x using the greatest common divisor of the lengths of

The underlying concept used in the provided solution is based on the mathematical idea of finding the greatest common divisor

str1 and str2. This is because the repeating pattern of string x must be a factor of both string lengths in order for it to divide both strings completely. Therefore, we find the GCD of the lengths of str1 and str2 and then return the substring of str1 up to that length. This substring is the largest common divider x. **Solution Approach** 

#### The solution provided takes advantage of Python's built-in gcd function from the [math](/problems/math-basics) library to calculate the greatest common divisor of the lengths of the two input strings str1 and str2. This is crucial for the solution, as the

gcd represents the length of the largest string that can divide both strings, if such a string exists. Here is how the solution unfolds: Check for Compatibility: The first step in the provided solution checks whether the strings are compatible to have a common

divisor by concatenating str1 with str2 and comparing it to str2 concatenated with str1. This is facilitated by the operation

- if str1 + str2 != str2 + str1, which ensures that the pattern of characters in both strings is compatible for them to have a common divisor string. If the check fails, the two strings cannot have a common divisor and the function immediately returns an empty string ''. Find Length of the Common Divisor: If the strings pass the compatibility check, the next step is to determine the length of the largest common divisor string. This is where we use the gcd function, by calling n = gcd(len(str1), len(str2)). The gcd
- Extract the Common Divisor String: With the length n obtained from the gcd function, the final step is to extract the common divisor string from str1. This is accomplished by the expression return str1[:n]. The [:n] slice operation on str1 returns the substring of str1 from the beginning up to the n-th character (exclusive), which is the required largest string that divides both str1 and str2.

function takes the lengths of str1 and str2 and returns the greatest common divisor of these two numbers.

To summarize, the algorithm consists of concatenation for compatibility checking and the greatest common divisor calculation, both of which are simple, efficient operations. The lack of any complex data structures and the use of a mathematical pattern of common division make this solution both elegant and effective. It leverages the fact that if a common divisor string exists, the repeating pattern must align with the gcd of the string lengths.

Let's use a small example to illustrate the solution approach. Suppose we have two strings str1 = "abab" and str2 = "ab". We

### Check for Compatibility: We first check if concatenating str1 with str2 is equal to str2 concatenated with str1.

divisor string.

 $\circ$  gcd(4, 2) = 2

**Example Walkthrough** 

o str2 + str1 = "ab" + "abab" = "ababab" Since str1 + str2 is equal to str2 + str1, the two strings are compatible, and therefore, it's possible they have a common

The gcd tells us that the length of the largest string that possibly divides both str1 and str2 is 2.

Find Length of the Common Divisor: Next, we find the greatest common divisor of the lengths of str1 (4) and str2 (2).

```
Extract the Common Divisor String: Since the gcd is 2, we take the first 2 characters from str1 to form our largest divisor
string x.
```

o str1 + str2 = "abab" + "ab" = "ababab"

need to find the largest string x that can divide both str1 and str2.

o str1[:2] = "ab" So, "ab" is the string we expect to divide both str1 and str2. To verify, we can see that:

```
    str2 divided by "ab" is "ab" / "ab" = "", which is the repetition of "ab" once.

The largest string that can divide both str1 and str2 is "ab", which matches our result from the solution approach. The solution is
```

# Check if the concatenation of the two strings in different order results in the same string.

# there is no common divisor string and hence return an empty string.

# Return the substring from 0 to length\_gcd from the first string,

// Base case: if b is 0, then a is the GCD (as GCD(a, 0) = a)

// Function to calculate the greatest common divisor (GCD) of two numbers

// Function to find the greatest common divisor of strings str1 and str2

// Check if concatenating the strings in both orders gives the same result

// This is required because two strings can only be multiples of each other

function gcdOfStrings(str1: string, str2: string): string {

// Recursive step: GCD(a, b) = GCD(b, a mod b)

return b == 0 ? a : gcd(b, a % b);

• str1 divided by "ab" is "abab" / "ab" = "ab", which is the repetition of "ab" twice.

elegant and efficient, leveraging simple concatenation and the mathematical concept of greatest common divisor to determine the existence and length of a common divisor string.

**Python** from math import gcd

#### # This is required as the strings should be made of the same substrings for them to have a common divisor. **if** str1 + str2 != str2 + str1: # If they don't form the same string when concatenated in different orders,

return ''

return str1[:length\_gcd]

def gcd0fStrings(self, str1: str, str2: str) -> str:

# which is the greatest common divisor string.

class Solution:

Solution Implementation

```
# Find the gcd of the lengths of the two strings.
# The gcd of the lengths will give us the maximum length the common divisor string can have.
length gcd = gcd(len(str1), len(str2))
```

```
Java
class Solution {
   // Function to find the greatest common divisor of lengths of two strings.
   // This GCD can be used to find the longest substring that can construct
   // the given strings by repeated concatenation.
   public String gcdOfStrings(String str1, String str2) {
       // Check if the two strings can be constructed from a common substring
       // Only if str1+str2 equals str2+str1, they have a common divisor string
       if (!(str1 + str2).equals(str2 + str1)) {
           return ""; // If not, return an empty string as there is no common divisor
       // Calculate the GCD of lengths of the two strings
       int len = gcd(str1.length(), str2.length());
       // The substring from the beginning of str1 with length 'len' is the gcd string
       return str1.substring(0, len);
   // Helper function to calculate the greatest common divisor (GCD) of two integers
   // It uses the Euclidean algorithm to find the GCD
   private int gcd(int a, int b) {
```

```
C++
#include <algorithm> // include algorithm header for std::gcd
class Solution {
public:
   // Function to find the greatest common divisor of strings str1 and str2
   string gcdOfStrings(string str1, string str2) {
       // check if concatenating the strings in both orders gives the same result
       // this is required because two strings can only be multiples of each other
       // if this condition is true
       if (str1 + str2 != str2 + str1) {
            return ""; // if they are not equivalent, return an empty string
       // calculate the greatest common divisor (GCD) of the sizes of the two strings
       // std::gcd is available in C++17 and later. For C++14 and earlier, use a custom gcd function
        int gcdValue = std::gcd(str1.size(), str2.size());
       // return the common divisor string which is the substring from start of str1 to its GCD length
        return str1.substr(0, gcdValue);
};
```

# return ""; // If they are not equivalent, return an empty string

**TypeScript** 

// Uses Euclidean algorithm

while (b !== 0) {

let t = b;

b = a % b;

// if this condition is true

if (str1 + str2 !== str2 + str1) {

a = t;

return a;

function gcd(a: number, b: number): number {

```
// Calculate the greatest common divisor (GCD) of the lengths of the two strings
      const gcdValue = gcd(str1.length, str2.length);
      // Return the common divisor string which is the substring from start of str1 to its GCD length
      return str1.substring(0, gcdValue);
from math import gcd
class Solution:
   def gcdOfStrings(self, str1: str, str2: str) -> str:
       # Check if the concatenation of the two strings in different order results in the same string.
       # This is required as the strings should be made of the same substrings for them to have a common divisor.
       if str1 + str2 != str2 + str1:
           # If they don't form the same string when concatenated in different orders,
           # there is no common divisor string and hence return an empty string.
           return ''
       # Find the gcd of the lengths of the two strings.
       # The gcd of the lengths will give us the maximum length the common divisor string can have.
        length gcd = gcd(len(str1), len(str2))
       # Return the substring from 0 to length_gcd from the first string,
       # which is the greatest common divisor string.
       return str1[:length_gcd]
Time and Space Complexity
  The code contains the gcd0fStrings method that finds the greatest common divisor (GCD) of lengths of two strings str1 and
  str2 to determine the largest string that can be repeatedly used to construct str1 and str2.
Time Complexity:
```

#### The time complexity of this function mainly depends on two operations: the string concatenation operation (str1 + str2 and str2 + str1) and the greatest common divisor computation (gcd(len(str1), len(str2))).

from both strings need to be combined once. Checking String Equality: Comparing the concatenated strings takes 0(n + m) time. If the strings differ, the method returns

String Concatenation: If str1 is of length n and str2 of length m, the concatenation will take 0(n + m) time as each character

- Greatest Common Divisor: The gcd function typically employs Euclid's algorithm, which has a time complexity of O(log(min(n, m))) where n and m are the lengths of the strings.
- dominating factor for large values of n and m will tend to be the concatenation and comparison, so we can approximate the time complexity as 0(n + m).

Therefore, the overall time complexity combines these operations resulting in  $O(n + m + \log(\min(n, m)))$ . However, the

# **Space Complexity:**

early.

The space complexity of the gcd0fStrings function can be analyzed as follows:

- Temporary Strings: The creation of concatenated strings str1 + str2 and str2 + str1 requires additional space of 0(n + m). GCD Computation: The gcd function itself may use constant space, 0(1), if the Euclidean algorithm is implemented in an
- iterative manner.

As such, no additional space that grows with the input size is required except for the string concatenation. Hence, the space complexity is 0(n + m).