226. Invert Binary Tree

**Depth-First Search Breadth-First Search** 

## **Problem Description**

The given problem is a classic tree manipulation problem which involves inverting a binary tree. In other words, for every node in the tree, you need to swap its left and right children. This operation should be applied recursively to all nodes of the tree, thus flipping the structure of the entire tree. As a result, the leftmost child becomes the rightmost child and vice versa, effectively creating a mirror image of the original tree. The challenge lies not just in performing the swap, but also in traversing the tree correctly to ensure all nodes are covered. Your task is to implement a function that takes the root of the binary tree as input and returns the new root of the inverted tree.

**Binary Tree** 

Intuition

### To achieve the inversion of the tree, we have to traverse it and for each node visited, its left and right children are swapped. This is a typical use case for a <u>Depth-First Search</u> (DFS) traversal. The DFS algorithm starts at the root node and explores as far as

possible along each branch before backtracking. This perfectly suits our need to reach every node in order to invert the entire tree. The solution approach is recursive in nature: 1. Start with the root node.

2. Swap the left and right child nodes of the current node.

- 3. Recursively apply the same procedure to the left child node (which after swapping becomes the right child node). 4. Recursively apply the same procedure to the right child node (which after swapping becomes the left child node).
- 5. Return back to the previous stack call and continue this process until all nodes are visited. At the end of the recursion, all nodes have their children swapped, and hence the tree is fully inverted, respecting the mirror
- image condition. Since the inversion needs to happen at each node, the time complexity is O(n), where n is the number of nodes in the tree, because each node is visited once.

passed as root. left and vice-versa, hence following the inverted structure.

The solution leverages the <u>Depth-First Search</u> (DFS) algorithm to traverse the <u>tree</u> and invert it at each node. To explain this step-by-step: 1. A helper function dfs() is defined which will carry out the depth-first traversal and inversion. This function takes one argument: the current root

node being visited. 2. Inside dfs(), a base case is present where if the root is None (indicating either an empty tree or the end of a branch), the function simply returns as there's nothing to invert.

- 3. If the node is not None, the function proceeds to swap the left and right child nodes. • This swapping is done with the Python tuple unpacking syntax: root.left, root.right = root.right, root.left.
- 4. After the swap, dfs() is recursively called first with root. left and then with root. right. Note that after the swap, the original right child is now
- 5. The recursion will reach the leaf nodes and backtrack to the root, effectively inverting the subtrees as it goes up the call stack. 6. Finally, once the root node's children are swapped and the recursive calls for its children are done, the whole tree is inverted. dfs(root)
- completes its execution and the modified root node is returned by the invertTree() function.
- A binary tree data structure is utilized with nodes following the definition of TreeNode which includes the val, left, and right attributes representing the node's value and its pointers to its left and right children respectively.
- Pattern used:

• These two recursive calls ensure that every child node of the current root will also get inverted.

### inverted correctly. The time complexity of this approach is O(n) where n is the total number of nodes in the tree, as each node is visited once during the traversal.

Data structure used:

**Example Walkthrough** 

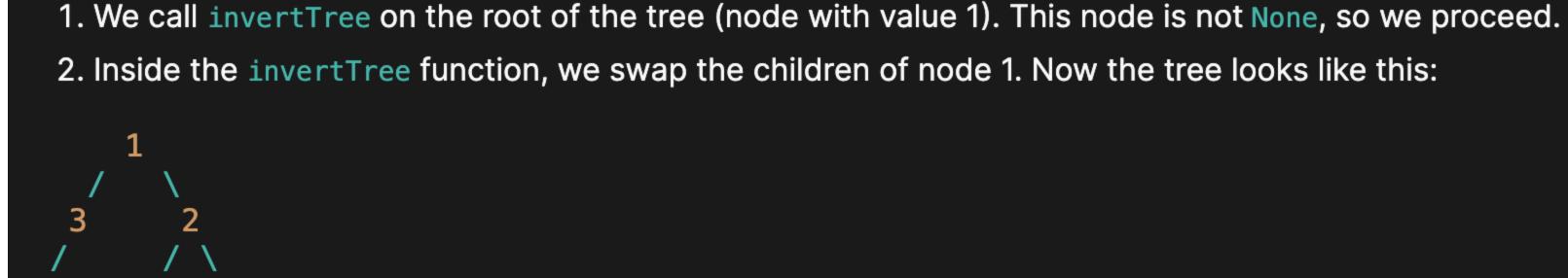
• The pattern is recursion facilitated by DFS which is appropriate for tree-based problems where operations need to be performed on all nodes.

By applying this approach, each and every node in the tree is visited exactly once, and it is guaranteed that the tree will be

Let's assume we have a simple binary tree:

# We want to invert this tree using the described solution approach. Here's how it happens step by step:

2. Inside the invertTree function, we swap the children of node 1. Now the tree looks like this:

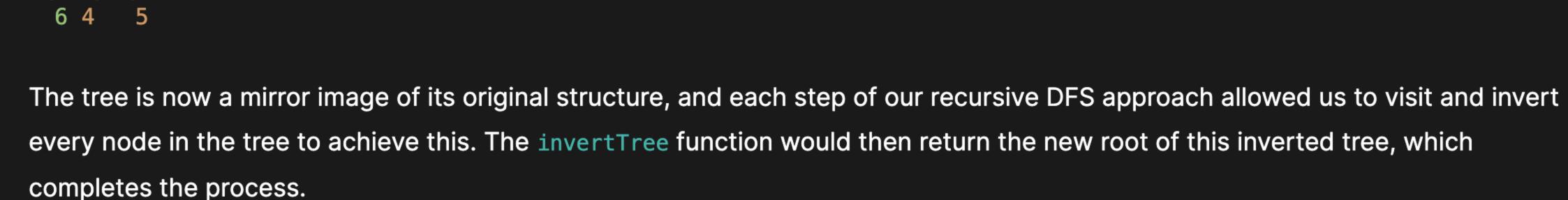


4. Next, we proceed to the right child of node 1 which is now the node with value 2. We swap the children of node 2. Now, the binary tree is:

(node with value 6) are swapped, but since it's a leaf node with no children, the tree structure remains the same at this point.

3. We call invertTree recursively on the left child (node with value 3 which was originally the right child of 1). Node 3 also isn't None, so its children

5. The node with value 2's left and right children (4 and 5) are leaf nodes and don't have children to swap. So they're left as is once reached by the recursive calls. 6. After all recursive calls have completed, we have successfully inverted every node in the tree. The final structure of the binary tree is now:



**Python** 

self.left = left self.right = right class Solution: def invertTree(self, root: Optional[TreeNode]) -> Optional[TreeNode]:

```
Returns:
Optional[TreeNode]: The root node of the inverted binary tree.
```

def invert(node):

Args:

Args:

class TreeNode:

Solution Implementation

self.val = val

"""Invert a binary tree.

if node is None:

return

"""Definition for a binary tree node."""

def \_\_init\_\_(self, val=0, left=None, right=None):

root (Optional[TreeNode]): The root node of the binary tree.

node (TreeNode): The current node to swap its children.

// Start the depth-first search inversion from the root node

// Swap the left and right children of the current node

#include <functional> // Include the functional header for std::function

TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}

std::swap(node->left, node->right);

// Invert the left subtree

// Invert the right subtree

depthFirstSearch(root);

depthFirstSearch(node->left);

depthFirstSearch(node->right);

// Return the root of the inverted tree

// Constructor to initialize the node values with given left and right children

// Swap the left and right children of the current node

// Start depth-first search from the root to invert the entire tree

\* @param {TreeNode | null} treeRoot - The root of the binary tree to invert.

\* @return {TreeNode | null} - The new root of the inverted binary tree.

def invertTree(self, root: Optional[TreeNode]) -> Optional[TreeNode]:

root (Optional[TreeNode]): The root node of the binary tree.

Optional[TreeNode]: The root node of the inverted binary tree.

node (TreeNode): The current node to swap its children.

# Swap the left child with the right child

# Recursively invert the left subtree

node.left, node.right = node.right, node.left

"""Helper function to perform depth-first search and invert the tree.

function invertTree(treeRoot: TreeNode | null): TreeNode | null {

// Recursive function to traverse the tree and swap children

TreeNode(int x, TreeNode \*left, TreeNode \*right) : val(x), left(left), right(right) {}

// A helper method that uses Depth-First Search to invert the given binary tree recursively.

// Base case: If the current node is null, there's nothing to invert; return immediately

depthFirstSearchInvert(root);

TreeNode tempNode = node.left;

// Recursively invert the left subtree

// Recursively invert the right subtree

depthFirstSearchInvert(node.left);

depthFirstSearchInvert(node.right);

// Constructor to initialize the node values

node.left = node.right;

node.right = tempNode;

// Definition for a binary tree node.

return root;

if (node == null) {

return;

// Return the new root after inversion

private void depthFirstSearchInvert(TreeNode node) {

"""Helper function to perform depth-first search and invert the tree.

```
# Swap the left child with the right child
            node.left, node.right = node.right, node.left
            # Recursively invert the left subtree
            invert(node.left)
            # Recursively invert the right subtree
            invert(node.right)
       # Start inverting the tree from the root
        invert(root)
       # Return the root of the inverted binary tree
       return root
Java
// Definition for a binary tree node.
class TreeNode {
    int val; // The value contained in the node
    TreeNode left; // Reference to the left child
    TreeNode right; // Reference to the right child
    // Constructor for creating a leaf node
    TreeNode() {}
    // Constructor for creating a node with a specific value
    TreeNode(int val) { this.val = val; }
    // Constructor for creating a node with a specific value and left/right children
    TreeNode(int val, TreeNode left, TreeNode right) {
       this.val = val;
       this.left = left;
       this.right = right;
// A solution class containing the method to invert a binary tree.
class Solution {
    // Inverts a binary tree and returns the root of the inverted tree.
    public TreeNode invertTree(TreeNode root) {
```

C++

**}**;

\*/

struct TreeNode {

int val;

TreeNode \*left;

TreeNode \*right;

```
class Solution {
public:
   // Method to invert a binary tree
   TreeNode* invertTree(TreeNode* root) {
       // Lambda function to recursively traverse the tree in a depth-first manner and invert it
       std::function<void(TreeNode*)> depthFirstSearch = [&](TreeNode* node) {
           // If the node is null, return immediately as there is nothing to invert
           if (!node) {
                return:
```

```
return root;
};
TypeScript
// TreeNode class definition
class TreeNode {
    val: number;
   left: TreeNode | null;
    right: TreeNode | null;
    constructor(val?: number, left?: TreeNode | null, right?: TreeNode | null) {
       this.val = (val === undefined ? 0 : val); // Assign the node's value or default it to 0
       this.left = (left === undefined ? null : left); // Assign the left child or default it to null
       this.right = (right === undefined ? null : right); // Assign the right child or default it to null
/**
* Inverts a binary tree by swapping all left and right children.
```

```
function invertNode(node: TreeNode | null): void {
          if (node === null) {
              return; // If the node is null, do nothing
          [node.left, node.right] = [node.right, node.left]; // Swap the left and right children
          invertNode(node.left); // Recursively invert the left subtree
          invertNode(node.right); // Recursively invert the right subtree
      invertNode(treeRoot); // Start inverting from the root node
      return treeRoot; // Return the new root after inversion
class TreeNode:
   """Definition for a binary tree node."""
   def ___init___(self, val=0, left=None, right=None):
       self.val = val
       self.left = left
       self.right = right
class Solution:
```

```
# Recursively invert the right subtree
    invert(node.right)
# Start inverting the tree from the root
invert(root)
# Return the root of the inverted binary tree
```

Time and Space Complexity

invert(node.left)

if node is None:

return

"""Invert a binary tree.

Args:

Returns:

def invert(node):

Args:

return root

dfs is called exactly once for each node in the tree.

The space complexity of the code is also 0(n) in the worst case, corresponding to the height of the tree. This happens when the tree is skewed (i.e., each node has only one child). In this case, the height of the stack due to recursive calls is equal to the number of nodes. However, in the average case (a balanced tree), the space complexity would be 0(log n), as the height of the tree would be logarithmic with respect to the number of nodes.

The time complexity of the provided code is O(n), where n is the number of nodes in the binary tree. This is because the function