2735. Collecting Chocolates

Enumeration

Problem Description

<u>Array</u>

Medium

corresponds to the chocolate of the i^th type, and its cost is given by nums[i]. The goal is to collect one chocolate of each type at the minimum total cost. To do this, you are allowed to perform operations. Each operation incurs a fixed cost x, and as a result, it changes the type of all

In this problem, you have an array nums of size n that indicates the cost of collecting chocolates of different types. The index i

chocolates simultaneously in a cyclic manner: the chocolate of i^th type becomes the chocolate of ((i + 1) mod n)^th type. You need to calculate the minimum cost to collect all different types of chocolates assuming you can do as many operations as

needed.

To find the minimum cost to collect all chocolate types, we need to consider two types of costs: the cost of each chocolate

Intuition

collected and the cost of the operations performed to change the chocolates' types. A common strategy in such problems with cyclic operations and transformations is to simulate each possible scenario and keep track of the minimum cost. Specifically, we can simulate the cost of collecting chocolates without any operations and then after

one operation, after two operations, and so on. We continue doing this until we have simulated the scenario after n-1 operations, as doing n or more operations would just cycle back to a previous state.

At each step, while simulating for j operations, we need to consider the cheapest chocolate we can collect at each type, given that we have performed j operations. This can be precomputed in a 2D array f, where f[i][j] represents the minimum cost to collect a chocolate of the i^th type after j operations. This array is filled by finding the cheaper option for each step: purchasing the chocolate of that type without any operation, or the cost of the chocolate of the next type (considering it as the current type

due to the operation). Once we have this precomputed array, we can simply iterate over it to calculate the total cost of collecting all chocolate types for each number of operations, adding the cost of operations themselves (x * j), and choose the minimum total cost. **Solution Approach**

Precomputation for each chocolate type and operation: The solution uses a 2D list, f, of size $n \times n$, where n is the number

of chocolate types. f[i][j] represents the minimum cost to collect a chocolate of the i^th type after j operations. To fill this array, we iterate over each chocolate type i and for each type, we go through each possible number of operations j. The cost

without any operation is just the cost of the chocolate nums[i], thus f[i][0] = nums[i]. For subsequent operations, we take

The implementation of the solution involves the following concepts:

- the minimum of the cost f[i][j-1] and the cost of chocolate of the $((i+j) \mod n)^{th}$ type (nums[(i+j) % n]), because each operation shifts the chocolate types by one. Calculating the minimum cost for collecting all chocolate types: We iterate over the number of operations j from 0 to n-1, compute the cost of collecting all types of chocolates using our precomputed values in f, then add the cost of performing j operations (x * j). The variable ans is used to keep track of the minimum total cost.
- cost min(ans, cost). Here's a closer look at the nested loops: • The outer loop runs through each type index i and initializes f[i][0].

Minimizing total cost: For j operations, we sum the precomputed minimum costs of collecting each chocolate f[i][j] for all

i from 0 to n-1, add the cost of the operations, and compare it with the current ans to check if we've found a cheaper total

• The inner nested loop runs for number of operations j and computes f[i][j]. • The final loop, outside of the nested loops, runs through all possible operation counts j, sums up the minimum costs for all types and adds the operation cost, checking for a new minimum.

possibilities is feasible.

- The important data structure used here is a 2D list (list of lists in Python) to store the minimum possible costs, which is a common approach for dynamic problems where a value depends on previously computed values. Additionally, the modulus operator %
- plays a crucial role for cyclic arithmetic within the array bounds. The solution leverages complete enumeration to ensure that all options are considered, which is often a useful pattern when dealing with small enough problem spaces where considering all

Example Walkthrough

By considering all possible scenarios and picking the minimum, this approach ensures we find the optimal solution.

Firstly, we initialize our 2D list f to precompute the costs, which will look like this after initialization (assuming n = 3 for our example): f = [[5, 0, 0],[3, 0, 0], [4, 0, 0]]

Let's consider a small example to illustrate the solution approach. Suppose we have an array of chocolate costs nums given as [5,

3, 4] and the fixed cost of each operation x as 1. There are three types of chocolates, and we want to collect one of each type at

Here, f[i][0] = nums[i] because the cost of collecting the chocolate of the i^th type without any operations is just the cost itself (nums[i]).

In above f matrix:

And so forth for other elements...

Solution Implementation

class Solution:

Hence, the answer for this example is 11.

the minimum cost.

f = [[5, 3, 3],[3, 4, 3], [4, 5, 3]]

Comparing the total costs, we see that the minimum cost to collect all chocolate types is 11 after performing 2 operations.

• f[0][1] = min(f[0][0], nums[(0 + 1) % 3]) = min(5, 3) = 3• f[1][1] = min(f[1][0], nums[(1 + 1) % 3]) = min(3, 4) = 3

Now, we start filling out f for each chocolate after each operation:

• For 1 operation, f[i][1] would be the minimum of f[i][0] and nums[(i + 1) % n].

• For 2 operations, f[i][2] would be the minimum of f[i][1] and nums[(i + 2) % n].

• For 0 operations, no change is made; we leave the initial values.

After precomputation, the f matrix will be filled out:

Now we calculate the minimum total cost of collecting all types of chocolates for each number of operations:

def min_cost(self, nums: List[int], x: int) -> int:

Initialize an NxN matrix to hold the minimum values

min_values = [[0] * num_count for _ in range(num_count)]

for subarrays starting from each index with varying lengths.

Start by populating the matrix with the individual numbers

And then fill in the rest by comparing with previous minimum values.

Analyze each subarray's minimum value and calculate the total cost

cost = sum(min_values[i][j] for i in range(num_count)) + x * j

considering the cost multiplier 'x' and find the minimum cost.

Get the length of the input array.

for i, value in enumerate(nums):

min_values[i][0] = value

num_count = len(nums)

min_cost = float('inf')

for j in range(num_count):

min_cost = min(min_cost, cost)

Return the computed minimum cost.

• With 0 operations, the cost is 5 + 3 + 4 = 12. • With 1 operation, the cost is 3 + 4 + 5 (cost from f) + 1 (cost of operation) = 13.

• With 2 operations, the cost is 3 + 3 + 3 (cost from f) + 2 * 1 (cost of operations) = 11.

Python

for j in range(1, num_count): min_values[i][j] = min(min_values[i][j - 1], nums[(i + j) % num_count]) # The initial minimum cost is set to be infinity for comparison purposes.

return min_cost

Java

#include <vector>

class Solution {

public:

};

#include <algorithm>

using namespace std;

long long minCost(vector<int>& nums, int x) {

for (int j = 1; j < n; ++j) {

for (int i = 0; i < n; ++i) {

cost += minValues[i][j];

return ans; // Return the minimum possible cost

for (int i = 0; i < n; ++i) {

for (int j = 0; j < n; ++j) {

ans = min(ans, cost);

ans = Math.min(ans, cost);

class Solution:

return ans; // Return the minimum possible cost

def min_cost(self, nums: List[int], x: int) -> int:

Initialize an NxN matrix to hold the minimum values

min_values = [[0] * num_count for _ in range(num_count)]

for subarrays starting from each index with varying lengths.

Start by populating the matrix with the individual numbers

And then fill in the rest by comparing with previous minimum values.

The initial minimum cost is set to be infinity for comparison purposes.

Analyze each subarray's minimum value and calculate the total cost

 $min_values[i][j] = min(min_values[i][j - 1], nums[(i + j) % num_count])$

Get the length of the input array.

for i, value in enumerate(nums):

min_values[i][0] = value

for j in range(1, num_count):

num_count = len(nums)

min_cost = float('inf')

Time and Space Complexity

int n = nums.size(); // Get the size of nums vector

vector<vector<int>> minValues(n, vector<int>(n, 0));

// Initialize a 2D vector with 'n' rows and 'n' values in each row to store minimum values

minValues[i][0] = nums[i]; // Base case: minimum of one element is the element itself

// Add the minimum value found starting from i, with j elements considered

// If the cost for this number of rotations is less than the current answer, update the answer

// Calculate min value in nums starting from i, considering j elements, wrapping around using modulus

// Calculate the minimum values starting from each index i going up to j elements

minValues[i][j] = min(minValues[i][j - 1], nums[(i + j) % n]);

long long ans = 1LL << 60; // Initialize answer to a very large value

// Check each possibility of j rotations and the corresponding cost

long long cost = 1LL * j * x; // Cost for rotating j times

```
class Solution {
    public long minCost(int[] nums, int x) {
        int arrayLength = nums.length;
       // Dynamic programming table where f[i][j] will hold the minimum value of nums[i]
       // when considered up to i+j shifted circularly by the array length
       int[][] dpTable = new int[arrayLength][arrayLength];
       // Initialize the dynamic programming table
        for (int i = 0; i < arrayLength; ++i) {</pre>
            dpTable[i][0] = nums[i];
            for (int j = 1; j < arrayLength; ++j) {</pre>
                // Calculate the minimum value within the shifting window
                dpTable[i][j] = Math.min(dpTable[i][j - 1], nums[(i + j) % arrayLength]);
       // Initialize answer to a very large value
        long minCost = Long.MAX_VALUE;
       // Calculate the minimum cost by iterating over possible shift steps
        for (int shiftSteps = 0; shiftSteps < arrayLength; ++shiftSteps) {</pre>
            // Cost of making the shifts
            long cost = 1L * shiftSteps * x;
            // Calculate the total cost including the minimum values at each shift step
            for (int i = 0; i < arrayLength; ++i) {
                cost += dpTable[i][shiftSteps];
            // Update the minimum cost if a lower one is found
           minCost = Math.min(minCost, cost);
       // Return the minimum cost found
        return minCost;
C++
```

```
TypeScript
function minCost(nums: number[], x: number): number {
   const n = nums.length; // Get the size of nums array
   // Initialize a 2D array with 'n' rows and 'n' values in each row to store minimum values
   const minValues: number[][] = Array.from({ length: n }, () => Array(n).fill(0));
   // Calculate the minimum values starting from each index i up to j elements
   for (let i = 0; i < n; ++i) {
       minValues[i][0] = nums[i]; // Base case: minimum of one element is the element itself
        for (let j = 1; j < n; ++j) {
           // Calculate min value in nums starting from i, considering j elements, wrapping around using modulus
           minValues[i][j] = Math.min(minValues[i][j - 1], nums[(i + j) % n]);
   let ans = Number.MAX SAFE INTEGER; // Initialize answer to a very large value
   // Check each possibility of j rotations and the corresponding cost
   for (let j = 0; j < n; ++j) {
        let cost = 1 * j * x; // Cost for rotating j times
        for (let i = 0; i < n; ++i) {
           // Add the minimum value found starting from i, with j elements considered
           cost += minValues[i][j];
       // If the cost for this number of rotations is less than the current answer, update the answer
```

```
# considering the cost multiplier 'x' and find the minimum cost.
for j in range(num_count):
    cost = sum(min_values[i][j] for i in range(num_count)) + x * j
    min_cost = min(min_cost, cost)
# Return the computed minimum cost.
return min_cost
```

2. Inside this loop, another for loop with variable j is running from 0 to n. This loop is executed n*(n-1)/2 times in total because it starts at 1 and iterates to n - 1 for each value of i. 3. Inside the inner loop, there's the expression nums[(i + j) % n], which has a constant time operation.

Time Complexity

4. The computation of min(f[i][j-1], nums[(i+j) % n]) is also a constant time operation. Combining these, we have the i loop running n times and the j loop running at most n times for each i. Therefore, the time

The given Python code consists of multiple nested loops. Here is the breakdown of its time complexity:

1. The first for loop with variable i is iterating through the list nums. It executes n times, where n is the length of the list.

complexity for these loops is $0(n^2)$. The second part of the code includes another for loop with variable j iterating n times.

1. Inside this loop, the sum() function iterates over all n elements of f for each j, which takes O(n) time.

Hence, the additional time complexity contributed by the second part is $0(n^2)$. Adding both parts, the **overall time complexity** of the code is $0(n^2) + 0(n^2) = 0(n^2)$.

Space Complexity The space complexity of the code primarily involves the storage used by the two-dimensional list f which has n lists of n integers

each. Apart from this, there are constant space usages for variables such as n, i, v, cost, and ans.

The two-dimensional list f requires 0(n^2) space. Thus, the **overall space complexity** of the code is $0(n^2)$.

2. The calculation x * j is a constant time operation executed n times.