2522. Partition String Into Substrings With Values at Most K String Medium Greedy **Dynamic Programming**

Leetcode Link

Problem Description

partitioning s, there are certain constraints that define what constitutes a "good" partition: Each digit in s can only be a part of one substring, ensuring no overlap.

You are tasked with partitioning a string s which is composed of digits from 1 to 9 into a set of substrings. In the process of

The goal of this exercise is to find the minimum number of substrings that can be created while maintaining a "good" partition of s.

Each substring, when converted to an integer, should have a value less than or equal to a given threshold k.

Note:

However, if it is not possible to partition s according to the criteria, you should return -1.

A substring is a contiguous block of characters found within the larger string s.

• The conversion of a substring to its integer value must be taken into account. For instance, the substring "123" is evaluated as the integer 123.

Intuition

Depth-First Search (DFS), can be used:

substring exceeds k.

Solution Approach

In approaching the problem, the key is to break the string s into all possible substrings that comply with the value limit set by k and

• Begin at the start of the string and progressively create substrates by adding one digit at a time until the value of the current

If the value does not exceed k, you recursively call the function for the rest of the string, starting just after the current substring.

subproblems and avoid redundant calculations. This optimization is necessary to ensure that the solution is efficient, especially when

- then find the minimal count among those possible partitions. To accomplish this systematically, a recursive approach, also known as
- Keep a global record of the least number of substrates needed to partition the string successfully. Since this approach can result in the same substrings being evaluated multiple times, we use memoization to store the results of
- dealing with large strings. The pythonic way to achieve memoization is using the @cache decorator, which automatically stores the results of the expensive recursive calls.
- Lastly, if after applying this method the minimum count remains undefined (inf), that means no good partition can be made, hence the function should return -1.

efficiency. Here's the breakdown of its algorithm: 1. We define a recursive helper function dfs, which receives an index i. This function attempts to partition the string starting from i and returns the minimum number of substrings needed for a good partition from this index onward.

2. When dfs is called with an index i, it checks if i is equal or greater than the length of s. If true, this indicates the end of the

The implementation of the solution is based on a recursive depth-first search (DFS) approach, with memoization to improve

3. The function initializes two variables, res and v. The former is set to infinity to simulate a maximum possible number, which is

substring in the total.

partition is possible and -1 is returned.

Here is how we apply the solution approach:

1. Call the recursive dfs function starting at index 0.

used to find the minimum count of substrings; the latter holds the current numerical value of the substring being formed. 4. A loop is used to try forming substrings starting from the index i. In each iteration, a digit is added to the current value v, which

string has been reached and no additional substrings are needed, so it returns 0.

5. If adding another digit makes v greater than k, the loop breaks, as the substring is no longer valid.

starting index are stored and directly returned upon subsequent calls with the same index.

more manageable exploration of the problem space while avoiding redundant calculations.

Let's walk through a simple example to illustrate the solution approach:

partition s into without any of them having an integer value greater than k.

■ The current value v is 0. The digit at s [0] is 1, so v=1.

Since v is less than k, recursively call dfs with index 1.

■ The recursive call will try all possible partitions starting from s[1].

Since v is still less than or equal to k, recursively call dfs with index 2.

■ Now v=1, and the next digit is 2, so v=12 (concatenating the digits 1 and 2 to form 12).

The loop will continue to add characters until the value of v exceeds k or we reach the end of the string.

4. When the recursive calls return, they give us the minimum number of substrings needed from that index onwards.

keeps track of the integer value of the current substring.

- 6. If the current substring's value does not exceed k, dfs is called recursively with the index just after the current substring to compute the minimum substrings needed for the remainder of s.
- current digit. 8. After evaluating all possibilities starting from index i, the function returns the minimum count found plus 1 to include the current

7. The minimum value between the res and the recursive call result is taken to find the optimal number of substrings up to the

10. The dfs function is initially called with index 0 to start partitioning from the beginning of the string s. The result is checked against infinity; if it is less, that means a good partition was found, and the answer is returned. Otherwise, it means no good

This solution takes advantage of the fact that Python has built-in support for memoization through the @cache decorator as part of

the functools library, and it uses recursion to explore all possible partition strategies. This, combined with memoization, allows for a

9. The outer dfs function is wrapped with the @cache decorator. This decorator ensures that the results of dfs calls for each

Example Walkthrough

Imagine we have the string s = "1234" and the threshold k = 12. We want to find the minimum number of substrings we can

2. The function initializes res to infinity and v to 0. 3. It starts trying to form a substring by adding one character at a time, checking whether v exceeds k:

Second iteration:

First iteration:

5. We compare all these returned values to find the minimum number amongst them and add 1 to include the current substring.

Following this process for the string s = "1234" with k = 12:

pre-computed value due to memoization.

def minimumPartition(self, s: str, k: int) -> int:

@lru_cache(maxsize=None)

return 0

return result + 1

string_length = len(s)

answer = dfs(0)

Length of the input string.

if index >= string_length:

result, value = math.inf, 0

for j in range(index, string_length):

result = min(result, dfs(j + 1))

private int strLength; // length of the input string

private String str; // the original input string

public int minimumPartition(String s, int k) {

int minimumPartition(std::string s, int k) {

memset(dp.data(), 0, sizeof(dp[0]) * n);

// Start the depth-first search from index 0

// A recursive function for depth-first search with memoization

for (let endIndex = startIndex; endIndex < n; endIndex++) {</pre>

result = Math.min(result, dfs(endIndex + 1));

return answer < INF ? answer : -1;

const dfs = (startIndex: number): number => {

std::vector<int> dp(n, 0); // Create a vector for dynamic programming storage

// Define a recursive lambda function for depth-first search (memoization approach)

if (startIndex >= n) return 0; // Base case: if we reach the end of string

if (dp[startIndex] > 0) return dp[startIndex]; // Memoization to save results

currentValue = currentValue * 10 + (s[endIndex] - '0'); // Calculate number value

result = std::min(result, dfs(endIndex + 1)); // Recursively solve the subproblem

if (currentValue > k) break; // If current number is bigger than k, break

return dp[startIndex] = result + 1; // Store the minimum number of partitions

const int INF = 1 << 30; // Define an 'infinity' value for initialization</pre>

// Try all possible partitions starting from the current index

// If the answer is not updated, meaning it's not possible, return -1

if (startIndex >= n) return 0; // Base case: if we reach the end of the string

// Try all possible partitions by considering the current index as the starting point

if (currentValue > k) break; // Break if the current number exceeds 'k'

if (dp[startIndex] !== 0) return dp[startIndex]; // Use memoized results to save computation time

// Recursively solve the subproblem and update the result with the minimum partitions needed

currentValue = currentValue * 10 + (s.charCodeAt(endIndex) - '0'.charCodeAt(0)); // Calculate the numeric value of the

for (int endIndex = startIndex; endIndex < n; ++endIndex) {</pre>

std::function<int(int)> dfs = [&](int startIndex) -> int {

int n = s.size();

int result = INF;

int answer = dfs(0);

let result = INF;

let currentValue = 0;

long currentValue = 0;

strLength = s.length();

str = s;

maxValue = k;

memo = new Integer[strLength];

Start the partitioning process from the first character.

def dfs(index):

Utility function to perform the Depth-First Search (DFS).

Caches the results to avoid recalculating for the same inputs.

If the index is beyond the string length, no more partitions are needed.

Iterate through the string characters starting from the current index.

private Integer[] memo; // memoization table for storing solutions to subproblems

private int maxValue; // the maximum allowed value for partitioning the number

// Main method to calculate minimum number of splits to partition

private final int INF = 1 << 30; // representing infinity, used for comparisons</pre>

int result = performDFS(0); // starts the depth-first search from the beginning of the string

return result < INF ? result : -1; // if the result is infinity, return -1, indicating it's not possible

'value' will store the numeric value generated from the string as we traverse.

Initialize the result as infinity to find the minimum partitions.

than or equal to k.

Python Solution

approach.

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};

Typescript Solution

6. Once the final recursive call finishes, we check if the result is infinity. If not, we return that result, which will represent the minimum number of substrings.

paths to explore. It cannot go further to dfs(3) because 123 is greater than k.

In the end, the minimum substrings that s can be partitioned into using this approach are two: "12" and "34", both of which are less

valid. dfs(3) calls will continue until it reaches the end of the string, incrementing the substring count as needed.

• dfs(0) starts, and attempts to build substrings. It sees that both dfs(1) (after using "1") and dfs(2) (after using "12") are valid

• dfs(1) will further break down the string "234", and once again, it finds that both dfs(2) (using "2") and dfs(3) (using "23") are

• dfs(2) will also try to explore, but as dfs(3) has already computed the minimum substrings from that point, it will provide the

1 from functools import lru_cache import math class Solution:

This example simplifies the process but effectively demonstrates the recursive and memoization techniques used in the solution

21 value = value * 10 + int(s[j])22 23 # If the generated value exceeds 'k', no valid partition can be made, so break out of the loop. if value > k: 24 break

Accumulate the numeric value by considering the current character as part of a number.

Recursively find the minimum number of partitions needed for the remaining substring.

Return the result of 1 (for the current partition) plus the recursively calculated partitions.

Add 1 for the current partition and take the minimum with the current result.

```
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           # If the answer is infinity, no partitioning scheme is valid, so return -1.
           # Otherwise, return the calculated minimum number of partitions.
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           return answer if answer < math.inf else -1
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```

Java Solution

1 class Solution {

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// Helper method that uses DFS to find the minimum splits recursively
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         private int performDFS(int index) {
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             // if the current index has reached the end of the string
 21
             if (index >= strLength) {
 22
                 return 0;
 23
 24
             // if the current index's result is already computed, return it
             if (memo[index] != null) {
 25
 26
                 return memo[index];
 27
 28
             int result = INF;
 29
             long currentValue = 0; // to store the numeric value of the current partition
 30
 31
             // iterate over the string starting from the current index
 32
             for (int j = index; j < strLength; ++j) {</pre>
                 currentValue = currentValue * 10 + (str.charAt(j) - '0'); // build the next number by appending the current digit
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                 // if the currentValue exceeds the maxValue allowed for a partition, abort this loop
 35
 36
                 if (currentValue > maxValue) {
 37
                     break;
 38
 39
                 // Recursively perform DFS for the next part and take the minimum result so far
                 result = Math.min(result, performDFS(j + 1));
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 42
             // Add 1 for the current split and store the result in memoization table before returning
             memo[index] = result + 1;
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             return memo[index];
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C++ Solution
    #include <vector>
  2 #include <cstring>
    #include <functional>
  5 class Solution {
    public:
```

1 function minimumPartition(s: string, k: number): number { const n: number = s.length; const dp: number[] = new Array(n).fill(0); // Dynamic programming storage const INF: number = 1 << 30; // Initialize 'infinity' value for impossible cases</pre> 4 5

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            // Store the minimum number of partitions in dp and return
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            dp[startIndex] = result + 1;
 27
            return dp[startIndex];
         };
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        // Start the DFS from the first index
 31
         const answer = dfs(0);
 32
 33
        // Return the answer if it's valid, otherwise return -1 to indicate impossibility
 34
         return answer < INF ? answer : -1;
 35 }
 36
 37 // The types are specified based on TypeScript best practices
 38 // and function definition requirements. This version does not utilize classes
 39 // but defines methods at the global scope as requested.
Time and Space Complexity
Time Complexity
The function uses a depth-first search (DFS) approach with memoization, implemented through the @cache decorator. This
exploration can visit each index i at most once for each unique state, resulting in a finite number of states limited by the length n of
the string s.
When we call dfs(i), in the worst case, it iterates through the rest of the string to calculate the potential partitions that do not
```

once v exceeds k, the loop breaks, constraining the number of iterations. The time complexity can be seen as 0(n * t), where n is the length of the string s and t is the average number of iterations

Space Complexity

depending on the nature of input s and the value of k.

performed in the loop before v exceeds k. The average number of iterations t is difficult to precisely quantify without specific knowledge about k and the digit makeup of s, but it can be bounded by n. Thus, the worst-case time complexity is 0(n^2) as a rough estimate, although in practical scenarios it could be significantly less,

exceed the value k. Each recursive dfs(j + 1) call attempts to partition the string at a different index j. Since v can grow up to k,

maximum recursion depth can be n, and the @cache decorator will store a result for each unique call to dfs(i). Since we can have at most n unique calls to the dfs function, the space complexity is O(n) because of memoization. However, we must also consider the implicit call stack due to recursion, which adds to the space complexity. In the worst case, the call stack's maximum depth would also be n since we could be making a recursive call for every character in the string. Thus, the

The space complexity of the code is driven by the recursion depth and the space needed to store the memoization states. The

overall space complexity remains O(n).