930. Binary Subarrays With Sum

Hash Table Sliding Window Medium Array **Prefix Sum**

Given a binary array, which consists of only 0's and 1's, and a target integer goal, the task is to find the number of subarrays whose

Problem Description

sum equals goal. A subarray is defined as any continuous sequence of the array. The binary nature of the array means any sum of its subarray will also be an integer, making the problem about finding subarray sums that match the given integer.

Intuition

are moved along the array to adjust the window size. Pointer j is used to extend the window by moving right. The variables s1 and s2 are used to track the sums of numbers within the window. • We use two sliding windows: one to find the number of subarrays with sum just over goal (s1 and i1), and another to find the

The solution employs a two-pointer approach that creates a sliding window of variable size over the array. Two pointers, i1 and i2,

- number of subarrays with sum equal to or just over goal (s2 and i2). As we move the main pointer j through the array, we increase s1 and s2 by the new element included in the window nums[j].
- Next, we need to shrink the windows if necessary. If s1 is greater than goal, we move i1 to reduce the window and the sum.
- Similarly, if s2 is greater or equal than goal, we move i2. • The difference between 12 and 11 gives us the number of new subarrays that have a sum equal to goal considering the new
- We increment ans by this difference since 12 11 represents the number of valid subarrays ending at 1 with sum exactly goal. • We repeat this process for every element of the array by incrementing j, thus exploring every potential subarray.
- Why does this work? The two sliding windows track the lower and upper bounds of sums around our goal. By taking the difference of the counts, we effectively count only those subarrays whose sum is exactly goal. Since we consider each subarray ending at

With every increment of j, we essentially say, "Given all the subarrays ending at j, count how many have a sum of goal." The sliding of i1 and i2 keeps the window's sum around goal and accurately maintains the count.

This approach is efficient since it requires only a single pass through the array, leading to a time complexity of O(n), where n is the length of the input array nums.

Solution Approach

subarrays that add up to the goal. Here's a step-by-step explanation:

goal.

element nums[j].

1. Initialize two pairs of pointers i1, i2 and their corresponding sums s1, s2 to 0. These will be used to manage two sliding windows. Also, initialize a pointer j to extend the window and ans to accumulate the number of valid subarrays found.

The solution to the subarray sum problem implements a variation of the two-pointer technique which helps to optimize the search for

- Add nums[j] to both s1 and s2, which represents attempting to add the current element to our current subarray sums. 3. If s1 exceeds the goal, shrink the first window: • Subtract nums [i1] from s1 and increment i1 to reduce the window from the left, doing this until s1 is no longer greater than
- 4. Similarly, if s2 is at least the goal, shrink the second window: • Subtract nums [12] from s2 and increment 12 to reduce the window from the left, doing this until s2 is smaller than goal.
- 5. After adjusting both windows, calculate the number of new subarrays found:

• The difference 12 - 11 tells us how many valid subarrays end at j with the desired sum goal because those will be the

Add this difference to ans which tallies our result.

subarrays contained within the window tracked by 12 but not yet by 11.

2. Iterate over the array with the main pointer j. For each element nums[j] being considered:

various j positions, we can ensure that all possible subarrays are counted.

7. Once the iteration is complete, ans holds the final count of subarrays whose sum is equal to goal.

6. Repeat steps 2 through 5 as you move the pointer j to the right until you've processed every element in the array.

The key ingredients of the solution are the two-pointer technique and a single pass, avoiding unnecessary recomputation.

algorithm iteratively adjusts these windows to find all valid subarrays in the most optimized manner.

Example Walkthrough

No complex data structures are needed because the pointers and sums effectively manage the windows of potential subarrays. The

This code efficiently finds all subarrays with the desired sum in linear time, utilizing 0(1) extra space, excluding the input and output.

Let's consider the binary array nums = [1, 0, 1, 0, 1] and the target integer goal = 2. We need to find the number of subarrays with the sum equal to goal.

2. Start iterating with pointer j from left to right. The main goal is to add nums[j] to both s1 and s2 and then adjust the windows

• For j = 0 (the first element is 1):

with pointers i1 and i2. Using the array provided, here's how the solution progresses:

∘ s1 = s2 = 1. No window adjustment needed since neither s1 nor s2 is over the goal yet.

∘ s1 = s2 = 1. Still no adjustment as we are not over the goal.

1. We initialize pointers and sums: i1 = i2 = 0, s1 = s2 = 0, and ans = 0.

• For j = 1 (the second element is 0):

• For j = 2 (the third element is 1): o s1 = s2 = 2. Since s2 >= goal, we increment i2. Now, i2 = 1 and s2 = 1 (s1 remains 2 because we have to exceed goal to

- adjust i1). \circ i2 - i1 = 1. We found one valid subarray [1, 0, 1] and increment ans by 1.
- For j = 3 (the fourth element is 0): ∘ s1 = 2 and s2 = 1. No adjustment required.
- For j = 4 (the fifth element is 1): \circ s1 = s2 = 2. Both sums are equal to the goal.
- Since s1 == goal, we increment i1. Now, i1 = 1 and s1 = 1. Similarly, i2 also increments because s2 >= goal. Now, i2 = 3 and s2 = 0.
- \circ i2 i1 = 2. The two new valid subarrays are [1, 0, 1] and [0, 1] ending at j=4. So we increment ans by 2. After iterating through the array, we've found ans = 3 valid subarrays ([1, 0, 1], [1, 0, 1], and [0, 1]) where the sum matches the goal.
- It's important to understand that the same subarray may be counted at different stages depending on the j position. This method ensures that every unique subarray is considered without double counting, and the result is achieved with a single traversal.

def numSubarraysWithSum(self, nums: List[int], goal: int) -> int:

Iterate over the array to find subarrays with sum equal to goal

Decrease sum1 until it's no more than goal by moving left1 pointer right

left1 = left2 = sum1 = sum2 = idx = total subarrays = 0

while left2 <= idx and sum2 >= goal:

while (left2 <= right && sum2 >= goal) {

// with sums that are exactly equal to the goal.

sum2 -= nums[left2++];

result += left2 - left1;

++right;

// Move to the next element.

sum2 -= nums[left2]

left2 += 1

Python Solution

Increase running sums with the current number sum1 += nums[idx] 9 sum2 += nums[idx] 11

```
while left1 <= idx and sum1 > goal:
                   sum1 -= nums[left1]
14
15
                   left1 += 1
16
               # Decrease sum2 until it's just less than goal by moving left2 pointer right
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```

class Solution:

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array_length = len(nums)

while idx < array_length:</pre>

```
22
               # Add the number of new subarrays found to the total
                total_subarrays += left2 - left1
23
24
25
               # Move to the next element
26
               idx += 1
27
28
           return total_subarrays
29
Java Solution
 1 class Solution {
       // Method to count the number of subarrays with a sum equal to the given goal.
       public int numSubarraysWithSum(int[] nums, int goal) {
           int left1 = 0, left2 = 0, sum1 = 0, sum2 = 0, right = 0, result = 0;
           int n = nums.length;
 6
           // Iterate over the elements of the array using 'right' as the right end of the subarray.
           while (right < n) {</pre>
               // Increase sums by the current element.
 9
               sum1 += nums[right];
10
               sum2 += nums[right];
11
12
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               // Shrink the window from the left (left1) until the sum (sum1) is not greater than the goal.
               while (left1 <= right && sum1 > goal) {
14
                    sum1 -= nums[left1++];
15
16
17
               // Shrink the window from the left (left2) until the sum (sum2) is not greater than or equal to the goal.
18
```

// The window between left2 and left1 contains all the starting points for subarrays ending at 'right'

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31
           // Return total count of subarrays with a sum equal to the goal.
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           return result;
33
34 }
35
C++ Solution
1 class Solution {
2 public:
       int numSubarraysWithSum(vector<int>& nums, int goal) {
           int startIndexForStrictlyGreater = 0; // Start index for subarrays with sum strictly greater than goal
           int startIndexForAtLeastGoal = 0; // Start index for subarrays with sum at least as much as goal
           int sumForStrictlyGreater = 0; // Current sum for the subarrays which is strictly greater than goal
           int sumForAtLeastGoal = 0; // Current sum for the subarrays which is at least as much as goal
           int endIndex = 0; // Current end index of the subarray
8
           int countSubarrays = 0; // Count of subarrays with sum exactly equals to goal
9
10
           int numSize = nums.size(); // Size of the input array
11
12
           // Iterate over each element in nums to find subarrays with sum equal to goal
13
           while (endIndex < numSize) {</pre>
               sumForStrictlyGreater += nums[endIndex]; // Increment sum by current element for strictly greater sum
14
               sumForAtLeastGoal += nums[endIndex]; // Increment sum by current element for at least goal sum
15
16
               // Move startIndexForStrictlyGreater till the sum is strictly greater than the goal
17
               while (startIndexForStrictlyGreater <= endIndex && sumForStrictlyGreater > goal) {
18
19
                   sumForStrictlyGreater -= nums[startIndexForStrictlyGreater++];
20
21
22
               // Move startIndexForAtLeastGoal till the sum is at least as much as the goal
23
               while (startIndexForAtLeastGoal <= endIndex && sumForAtLeastGoal >= goal) {
24
                   sumForAtLeastGoal -= nums[startIndexForAtLeastGoal++];
25
26
27
               // The number of subarrays which sum up to the goal equals to the difference of indices
               // This gives us the count of all the subarrays between the two starts
28
29
               countSubarrays += startIndexForAtLeastGoal - startIndexForStrictlyGreater;
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31
               // Move to the next element
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return countSubarrays; // Return the total count of subarrays with sum equal to goal

*/

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36 };

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Typescript Solution
1 /**
    * Counts the number of subarrays with a sum equal to the given goal.
3
    * @param {number[]} nums - The array of numbers to search within.
    * @param {number} goal - The target sum for the subarrays.
    * @return {number} The number of subarrays whose sum equals the goal.
   const numSubarraysWithSum = (nums: number[], goal: number): number => {
       let leftIndexForStrict = 0, // Left index for the subarray where the sum is strictly more than the goal.
           leftIndexForLoose = 0, // Left index for the subarray where the sum is at least the goal.
10
           strictSum = 0, // Sum of the current subarray for the strict condition.
11
12
           looseSum = 0, // Sum of the current subarray for the loose condition.
           rightIndex = 0, // Right index of the subarray currently being considered.
           count = 0; // The count of valid subarrays.
14
15
       const length = nums.length;
16
17
       // Traverse through the array using the right index.
       while (rightIndex < length) {</pre>
18
           // Add the current element to both the strict and loose sum.
20
           strictSum += nums[rightIndex];
           looseSum += nums[rightIndex];
21
22
23
           // If the strict sum is greater than the goal, move the left index to reduce the sum.
24
           while (leftIndexForStrict <= rightIndex && strictSum > goal) {
25
               strictSum -= nums[leftIndexForStrict++];
26
27
28
           // If the loose sum is at least the goal, move the left index to find the next valid subarray start.
29
           while (leftIndexForLoose <= rightIndex && looseSum >= goal) {
               looseSum -= nums[leftIndexForLoose++];
30
31
32
33
           // The difference between leftIndexForLoose and leftIndexForStrict gives the count of subarrays where the sum equals the goal
34
           count += leftIndexForLoose - leftIndexForStrict;
35
36
           // Move to the next element in the array.
37
           ++rightIndex;
38
39
       // Return the total count of valid subarrays.
40
       return count;
42 };
43
```

Time and Space Complexity

++endIndex;

// This function can now be called with TypeScript's type checking. 45

The code provided uses two pointers technique to keep track of subarrays with sums equal to or just above the goal. The time

complexity of the code is O(n) because the while loop runs for each element in the array (n elements), and inside the loop, each

pointer (i1 and i2) moves forward (never backwards), meaning each element is processed once.

The space complexity of the code is 0(1) as the space used does not grow with the input size n. The variables i1, i2, s1, s2, j, ans, and n use a constant amount of space.