738. Monotone Increasing Digits



Problem Description

The problem statement presents a challenge where you need to find the largest number that is less than or equal to a given integer n and also has monotone increasing digits. A number is said to have monotone increasing digits if every digit is less than or equal to the digit immediately to its right. The objective is to transform n in such a way that it satisfies this condition but still remains the largest possible number under the given constraints.

Intuition

Therefore, adjusting them will have a greater impact on the overall value of the number. As we iterate through the digits, we're looking for the point where the monotone condition is violated (a digit that is greater than the next digit). When this violation is found, we must adjust the number to restore the monotone condition.

The key insight is that once we find a pair of digits where the left digit is greater than the right digit, we can reduce the left digit by

To solve this problem, the intuition is to process the number from the left to right because the leftmost digits have a higher value.

one and change all subsequent digits to 9 to get the largest possible monotone increasing number. However, this reduction can cause a violation of the monotone condition to the left, so we must check and fix those cases too.

The solution approach involves turning the integer into a string to work with individual digits more conveniently, then walking through

the string to find the first descending point. We decrement the digit at that point and then check to the left to ensure we still have a monotone sequence, adjusting as needed. Lastly, we set all digits to the right of the adjusted digit to 9, since that will give us the largest possible number that maintains our condition.

Solution Approach

The implementation starts by converting the integer n to a string. This allows us to access each digit character easily to compare and modify them.

The algorithm proceeds in the following steps:

1. Initiate Search for Non-Monotone Point: We initialize i to 1 and start iterating over the digits from left to right, comparing each

digit with its immediate predecessor to ensure that each digit is greater than or equal to the previous one. The goal is to identify the index where the monotone increasing property fails.

number less than or equal to n with monotone increasing digits.

use of simple iterative logic to solve the problem.

- 2. **Detect Decreasing Sequence:** As we proceed, if we find a digit that is smaller than the digit before it (s[i] < s[i 1]), this is where the property of monotone increasing digits is violated. This is the point where we need to take action to correct the sequence.
- 3. **Reduce and Correct the Sequence:** To fix the violation, we move one position to the left (start decrementing i) and reduce that digit by 1(s[i-1] = str(int(s[i-1]) 1)). We continue correcting the sequence by moving leftward until we reach a point where the sequence is increasing again.
- is because '9's will maximize the resulting number while preserving the monotone property from that point forward.

 5. **Return the Result:** Finally, we convert the list of characters back into a string, and then into an integer, which is the largest

4. Maximize Remaining Digits: After correcting the sequence, we replace all digits to the right of our correction point with '9'. This

Algorithmic Concepts:

• Greedy Approach: The idea of changing only the first violating digit and replacing subsequent digits with '9's is greedy because

it makes the most significant digits as large as possible without violating the monotone condition.

• String Manipulation: By treating the number as a string, we are able to manipulate individual digits more directly compared to doing so with arithmetic operations.

• Simple Iteration: The solution performs linear scans from left to right, and in some cases from right to left, showcasing a good

- Data Structures Used:
 - List of Characters: A list is used to represent the digits of n, because string in Python is immutable, and a list allows us to make changes to individual digits conveniently.

The solution exploits the property that a number is always greater when its leftmost digits are greater, hence the left-to-right and

Example Walkthrough

1. Initiate Search for Non-Monotone Point: We will convert the number into a string for easy manipulation, s = "3214", and start looking for the point where the digits stop being monotone increasing. We initialize i to 1 and start comparing adjacent digits.

then right-to-left scans to achieve a correct and efficient approach to finding the answer.

Let's illustrate the solution approach with a small example. Consider the integer n = 3214.

condition at index i = 2.

Following the steps of the solution:

3. Reduce and Correct the Sequence: Now, we need to decrement s[i-1] from 2 to 1. But this alone makes the string "3114", which still violates the condition at i=1 (since 3>1). So, we need to also decrement s[i-2] from 3 to 2, giving us "2114".

2. Detect Decreasing Sequence: While comparing, we notice that s[1] > s[2] (which is 2 > 1), violating the monotone increasing

- 4. Maximize Remaining Digits: After the correction, we know that s[i] to s[len(s) 1] can all be set to '9' to maximize the number without violating the monotone condition. So, '2114' becomes '2999'.
- or equal to 3214 that has monotone increasing digits.

 With the original number 3214, the solution finds that at the index 2, the monotone condition is violated. It then modifies the digits in

such a way to maintain the maximum values while correcting the sequence, resulting in 2999. This effectively demonstrates the

greedy approach of the solution, which optimizes the leftmost digits first to get the largest possible number with the constraint of

5. Return the Result: We convert the string "2999" back into an integer, which gives us 2999. This is the largest number less than

Python Solution:
1 class Solution:
2 def monotoneIncreasingDigits(self, n: int) -> int:
3 # Convert the number to a list of characters for easy manipulation

10 11 # If a non-monotone digit was found, modify the number 12 if index < len(digits): 13 # Decrease the previous digit by 1 until the number becomes monotone</pre>

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monotone increasing digits.

digits = list(str(n))

index += 1

index -= 1

index = 1

Find the first digit that breaks the monotony

// If the monotone increasing property is violated,

if (i < digits.length) {</pre>

digits[i - 1]--;

digits[i] = '9';

for (; i < digits.length; i++) {</pre>

return Integer.parseInt(new String(digits));

// work backwards to find the digit which can be decremented.

for (; i > 0 && digits[i - 1] > digits[i]; i--) {

while index < len(digits) and digits[index - 1] <= digits[index]:</pre>

while index > 0 and digits[index - 1] > digits[index]:

digits[index - 1] = str(int(digits[index - 1]) - 1)

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# Setting the rest of the digits to '9' to guarantee the largest monotone number
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19
               index += 1
               while index < len(digits):</pre>
20
                    digits[index] = '9'
                    index += 1
23
24
           # Convert the list of characters back to an integer and return
25
           return int(''.join(digits))
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Java Solution
 1 class Solution {
       public int monotoneIncreasingDigits(int n) {
           // Convert the input integer n to a character array to process each digit individually.
           char[] digits = String.valueOf(n).toCharArray();
           // Initialize index i for iterating through the digits.
           int i = 1;
 8
           // Find the point where digits are no longer increasing (i.e., digits[i-1] > digits[i]).
9
           for (; i < digits.length && digits[i - 1] <= digits[i]; i++) {</pre>
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               // This loop will keep iterating until it finds a decreasing point or reaches the end.
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// Decrement the violating digit and find the position from which to replace with 9s.

// Convert the updated character array back to an integer and return the result.

1 // This function finds the largest monotone increasing number that is less than or equal to n.

// Traverse the digits of the number to find where the monotone increasing sequence is broken

// Convert the integer n to a string representation for digit manipulation

while (marker < numStr.length && numStr[marker - 1] <= numStr[marker]) {</pre>

// Reduce the previous digit by 1 to maintain the monotone increasing property.

// Reset remaining digits to '9' beginning from the current index to the end of the array.

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32 }
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C++ Solution
 1 class Solution {
  public:
       // This function finds the largest monotone increasing number that is less than or equal to n.
        int monotoneIncreasingDigits(int n) {
           // Convert the integer n to a string representation for digit manipulation
           string numStr = to_string(n);
            int marker = 1;
           // Traverse the digits of the number until we find a digit that is less than the previous digit,
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           // indicating that the sequence is no longer monotone increasing
           while (marker < numStr.size() && numStr[marker - 1] <= numStr[marker]) {</pre>
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                ++marker;
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           // If we found a position where the monotone property is violated
           if (marker < numStr.size()) {</pre>
16
               // Go back and find the position where we need to decrement to restore the monotone property
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               while (marker > 0 && numStr[marker - 1] > numStr[marker]) {
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                    numStr[marker - 1]--;
                    --marker;
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               // Fill the rest of the digits after marker with '9' to maximize the resultant number
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                for (int i = marker + 1; i < numStr.size(); ++i) {</pre>
                    numStr[i] = '9';
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           // Convert the modified string back to an integer and return it
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           return stoi(numStr);
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31 };
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```

12 } 13 14 // Check if we found a position where the sequence is no longer monotone increasing 15 if (marker < numStr.length) {</pre>

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Typescript Solution

function monotoneIncreasingDigits(n: number): number {

// Initialize marker as a pointer to traverse the digits

let numStr: string = n.toString();

let marker: number = 1;

marker++;

```
if (marker < numStr.length) {</pre>
           // Step back to find the correct digit to decrement in order to keep the number monotone increasing
16
           while (marker > 0 && numStr[marker - 1] > numStr[marker]) {
17
               // Decrement the digit at marker - 1
18
               let prevDigit = parseInt(numStr[marker - 1], 10) - 1;
19
               numStr = numStr.substring(∅, marker - 1) + prevDigit.toString() + numStr.substring(marker);
20
21
               // Move the marker back to the left as needed
23
               marker--;
24
25
           // Fill the rest of the string with '9' after the marker to maximize the resulting number
26
           for (let i = marker + 1; i < numStr.length; i++) {</pre>
               numStr = numStr.substring(0, i) + '9' + numStr.substring(i + 1);
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32
       // Convert the modified string back to an integer and return it
       return parseInt(numStr, 10);
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34 }
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Time and Space Complexity
The provided code aims to find the largest monotone increasing number that is less than or equal to a given number n. The time
complexity and space complexity are analyzed as follows:
Time Complexity
  • Best-case scenario: When the digits are already in a monotone increasing order, the algorithm would traverse the number's
    digits once. Thus, in the best case, the time complexity is O(d), where d is the number of digits in n.
```

Once to identify the first position where s[i - 1] is greater than s[i]. And a second pass to correct the number by decrementing the digit at position i - 1 and setting all subsequent digits to

depends on the number of digits d in n.

'9'.
Since each of these operations is linear with respect to the number of digits in n, the worst-case time complexity will also be 0(d).

• Worst-case scenario: The algorithm will need to traverse the digits twice if a decrease is found:

- In conclusion, the overall time complexity is O(d), with d being the number of digits in n.
- Space Complexity

 The input number n is converted to a list s of its digits in string format. This is the only significant additional memory used, which
- No other additional data structures are used that grow with the input size. The variables used for iteration and comparison are constant in size.

Therefore, the space complexity is O(d), where d is the number of digits in n.