1609. Even Odd Tree Medium Tree **Breadth-First Search Binary Tree Leetcode Link**

Problem Description The problem provides a binary tree and introduces a special condition called Even-Odd. A binary tree meets the Even-Odd condition

if: • The root node is at level 0, its children are at level 1, their children at level 2, and so on.

- Nodes at levels with an even index (like 0, 2, 4, ...) must have odd integer values, and these values must be in strictly increasing
- order from left to right. • Nodes at levels with an odd index (like 1, 3, 5, ...) must have even integer values, and these values must be in strictly decreasing
- order from left to right. The goal is to write a function that takes the root node of a binary tree as an input and returns true if the tree satisfies the Even-Odd
- condition; otherwise, it should return false. Intuition

Solution Approach

Here's how we approach the solution:

To solve this problem, we use the Breadth-First Search (BFS) algorithm. BFS allows us to traverse the tree level by level. This fits our needs perfectly since the Even-Odd condition applies to individual levels of the tree.

1. Initialize a queue and add the root node to it. The queue is used to keep track of nodes to visit in the current level.

 For each node, check if the value meets the required criteria based on whether the current level is even or odd. Maintain a prev value to compare with the current node's value ensuring the strictly increasing or decreasing order. After processing all nodes in the current level, toggle the even/odd level flag using XOR with 1.

3. If at any point a node does not meet the requirements, return false. 4. If the loop completes without finding any violations, return true since the tree meets the Even-Odd condition.

2. Traverse each level of the tree using a while loop that runs as long as there are nodes left in the queue:

By using BFS, we are able to check the values level by level, and by maintaining a variable to track the previous node's value, we can easily check the strictly increasing or decreasing order requirement.

traversed (odd or even). A queue q is used to keep track of nodes in the current level.

The solution approach is based on a Breadth-First Search (BFS) pattern. Here's a walkthrough of the implementation details: 1. Initialize Variables: A flag variable even, which is initially set to 1, is used to represent the current parity of the level being

2. BFS Loop: The solution iterates through the tree by using a while loop that continues as long as there are nodes in the queue. 1 while q:

= deque([root])

1 for _ in range(len(q)):

the current size of the queue (len(q)).

4. Initialization Per Level: At the beginning of each level, initialize prev to 0 if the current level is supposed to contain even values, and to inf for odd values.

3. Level Traversal: Within the loop, a for loop iterates over each node in the current level. The number of nodes is determined by

1 prev = 0 if even else inf 5. Node Validation: For each node, the algorithm checks if the current node's value meets the appropriate conditions:

For even levels, node values must be odd and increasing, checked by root.val % 2 == 0 or prev >= root.val.

7. Queue Update: The left and right children of the current node are added to the queue if they exist.

- For odd levels, node values must be even and decreasing, checked by root.val % 2 == 1 or prev <= root.val. If a node does not meet its corresponding condition, the function returns False. 1 if even and (root.val % 2 == 0 or prev >= root.val):
- 6. Track Previous Value: The prev value is updated to the current node's value for the next iteration.

q.append(root.left)

q.append(root.right)

satisfies the Even-Odd condition.

Suppose we have the following binary tree:

done by using the XOR operator (even $^{-}$ 1).

the tree against the provided conditions level by level.

2. **BFS Loop**: Start the while loop since the queue is not empty.

5. Node Validation: We check the value of the root node:

12. Node Validation: Evaluate the nodes in this odd level:

but 7 is odd, so it fails the condition.

5, which is odd, so it passes. The function continues.

8. Toggle Even/Odd Level: At the end of the level, toggle even to 0.

9. BFS Loop: Now we have 10 and 7 in the queue; the while loop continues.

return False

1 prev = root.val

1 if root.left:

3 if root.right:

3 if not even and (root.val % 2 == 1 or prev <= root.val):</pre>

1 even ^= 1 9. Completion: After the entire tree has been traversed without returning False, the function returns True, confirming that the tree

By using a queue to manage nodes, this approach maintains a clear delineation between levels and employs BFS efficiently to verify

8. Toggle Even/Odd Level: After each level is processed, the even flag is toggled to 1 if it was 0, or to 0 if it was 1. The toggle is

- Example Walkthrough Let's take a small binary tree to illustrate the solution approach.
- Let's walk through the steps: 1. Initialize Variables: Set even to 1 and put the root node with value 5 in the queue.

3. Level Traversal: Process nodes in the current level. We have one node, which is 5. 4. Initialization Per Level: At level 0 (even level), we initialize prev to inf.

Since it's an even level, we expect an odd value and as it's the first value, it doesn't need to be increasing. The root's value is

We move on to the next node in the same level, which is 7. We expect an even value and a value less than prev (which is 10),

7. Queue Update: Nodes 10 and 7 are children of 5, so add them to the queue.

BFS traversal.

Python Solution

class Solution:

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54 };

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Java Solution

class TreeNode {

class Solution {

int value;

TreeNode left;

TreeNode() {}

TreeNode right;

TreeNode(int value) {

this.value = value;

this.value = value;

this.right = right;

queue.offer(root);

this.left = left;

from collections import deque

self.right = right

queue = deque([root])

Traverse the tree by levels

return False

return False

if node.left:

return True

// Definition of the binary tree node.

previous_value = node.val

If all conditions are met, return True

TreeNode(int value, TreeNode left, TreeNode right) {

// Queue for performing level order traversal

Deque<TreeNode> queue = new ArrayDeque<>();

// Loop while there are nodes in the queue

root = queue.poll();

// Number of nodes at the current level

int previousValue = isLevelEven ? 0 : 1000001;

for (int levelSize = queue.size(); levelSize > 0; --levelSize) {

// 'isEvenLevel' indicates whether the current level is even or odd.

// 'previousValue' holds the previously encountered value in the current level.

// Check whether the current node's value is appropriately odd or even.

previousValue = root->val; // Update the 'previousValue'.

// Add child nodes to the queue for the next level.

// Toggle the level indicator after finishing each level.

if (root->left) nodeQueue.push(root->left);

if (root->right) nodeQueue.push(root->right);

return true; // The tree meets the even-odd tree conditions.

// 'isEvenLevel' indicates whether the current level is even or odd.

previousValue = node.val; // Update the 'previousValue'.

// Add child nodes to the queue for the next level.

if (node.left) nodeQueue.push(node.left);

let node = nodeQueue.shift()!; // '!' asserts that 'node' won't be null.

if (isEvenLevel && (node.val % 2 === 0 || previousValue >= node.val)) return false;

if (!isEvenLevel && (node.val % 2 === 1 || previousValue <= node.val)) return false;</pre>

// Check whether the current node's value is appropriately odd or even.

some point during execution, which determines the maximum amount of space needed at any time.

if (isEvenLevel && (root->val % 2 == 0 || previousValue >= root->val)) return false;

if (!isEvenLevel && (root->val % 2 == 1 || previousValue <= root->val)) return false;

int previousValue = isEvenLevel ? 0 : INT_MAX; // Initialize based on the level.

bool isEvenLevel = true;

while (!nodeQueue.empty()) {

nodeQueue.pop();

isEvenLevel = !isEvenLevel;

function isEvenOddTree(root: TreeNode | null): boolean {

let nodeQueue: (TreeNode | null)[] = [root];

let levelSize = nodeQueue.length;

for (let i = 0; i < levelSize; i++) {</pre>

// Queue for level order traversal.

queue<TreeNode*> nodeQueue{{root}};

// Process all nodes at the current level.

root = nodeQueue.front();

for (int i = nodeQueue.size(); i > 0; --i) {

public boolean isEvenOddTree(TreeNode root) {

boolean isLevelEven = true;

while (!queue.isEmpty()) {

level = 0

while queue:

10. Level Traversal: There are two nodes in this level 11. Initialization Per Level: Set prev to 0 because we are at an odd level now.

6. Track Previous Value: The prev value becomes the current node's value, which is 5.

We start with the node 10. We expect an even value and decreasing order (however, as it's the first node of this level, we

only check for an even value). Node 10 has an even value, so it passes for now.

Depending on the current level, set the previous value accordingly

At odd levels, values must be even and strictly decreasing

// Tracks whether the current level is even (starting with the root level as even).

Update the previous value for the next comparison

previous_value = 0 if level % 2 == 0 else float('inf')

For even levels, we start comparing from the smallest possible value (0)

For odd levels, we start comparing from the largest possible value (infinity)

if level % 2 == 0 and (node.val % 2 == 0 or previous_value >= node.val):

if level % 2 == 1 and (node.val % 2 == 1 or previous_value <= node.val):</pre>

- Since we detected a violation at node 7, the function should return False. This small example contradicts the Even-Odd condition in the second level and illustrates the checking mechanism per level using
- # Definition for a binary tree node. class TreeNode: def __init__(self, val=0, left=None, right=None): self.val = val self.left = left

def isEvenOddTree(self, root: TreeNode) -> bool:

Initialize the queue with the root node

Initialize the level to 0 (0-indexed, so even)

25 # Process all nodes in the current level for _ in range(len(queue)): 26 27 node = queue.popleft() 28 29 # Check the Even-Odd Tree condition for the current node 30 # At even levels, values must be odd and strictly increasing

42 queue.append(node.left) 43 if node.right: 44 queue.append(node.right) 45 46 # Move to the next level 47 level += 1

Add child nodes to the queue

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                   // For even levels, values must be odd and strictly increasing
                   if (isLevelEven && (root.value % 2 == 0 || previousValue >= root.value)) {
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                        return false;
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                   // For odd levels, values must be even and strictly decreasing
                   if (!isLevelEven && (root.value % 2 == 1 || previousValue <= root.value)) {</pre>
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                        return false;
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                   // Update the 'previousValue' with the current node's value
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                    previousValue = root.value;
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                   // Add the left and right children, if they exist, to the queue for the next level
                   if (root.left != null) {
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                        queue.offer(root.left);
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                   if (root.right != null) {
                        queue.offer(root.right);
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               // Toggle the level indication for the next level traversal
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               isLevelEven = !isLevelEven;
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           // If all levels meet the condition, return true
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           return true;
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67 }
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C++ Solution
  1 /**
     * Definition for a binary tree node.
  3 */
  4 struct TreeNode {
         int val;
         TreeNode *left;
  6
         TreeNode *right;
         TreeNode() : val(0), left(nullptr), right(nullptr) {}
  8
         TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
  9
         TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}
 10
 11 };
 12
 13 class Solution {
 14 public:
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         /**
 16
          * Checks whether a binary tree is an even-odd tree.
          * A binary tree is an even-odd tree if it meets the following conditions:
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          * - At even-indexed levels, all nodes' values are odd, and they are
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              increasing from left to right.
          * - At odd-indexed levels, all nodes' values are even, and they are
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              decreasing from left to right.
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          * @param root The root of the binary tree.
 24
          * @return True if the binary tree is an even-odd tree, otherwise false.
 25
          */
 26
         bool isEvenOddTree(TreeNode* root) {
```

// 'previousValue' will store the last value seen at the current level to check the strictly increasing or decreasing orc

12 13 while (nodeQueue.length > 0) { // 'previousValue' holds the previously encountered value in the current level. 14 let previousValue: number = isEvenLevel ? 0 : Number.MAX_SAFE_INTEGER; // Initialize based on the level. 15 16 // Process all nodes at the current level.

Typescript Solution

left: TreeNode | null;

right: TreeNode | null;

let isEvenLevel = true;

// Queue for level order traversal.

1 interface TreeNode {

val: number;

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               if (node.right) nodeQueue.push(node.right);
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          // Toggle the level indicator after finishing each level.
           isEvenLevel = !isEvenLevel;
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       return true; // The tree meets the even-odd tree conditions.
34 }
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Time and Space Complexity
// The time complexity of the provided code is O(n) where n is the number of nodes in the binary tree. This is because the code
traverses each node exactly once. Each node is popped from the queue once, and its value is checked against the conditions for an
even-odd tree, which takes constant time. The enqueue operations for the children of the nodes also happen once per node,
maintaining the overall linear complexity with respect to the number of nodes.
// The space complexity of the code is O(m) where m is the maximum number of nodes at any level of the binary tree, or the maximum
breadth of the tree. This is because the queue q can at most contain all the nodes at the level with the maximum number of nodes at
```