1061. Lexicographically Smallest Equivalent String

Medium Union Find String

Problem Description

symmetric, and transitive; that means if a is equivalent to b, then b is equivalent to a (symmetry), and if a is equivalent to b, b is equivalent to c, then a is equivalent to c (transitivity). Using these equivalences, your goal is to transform baseStr into its lexicographically smallest equivalent string. An example provided is with s1 = "abc" and s2 = "cde", which means a == c, b == d, and c == e. For the baseStr = "eed", both "acd" and "aab" are equivalent strings, but "aab" is the lexicographically smaller one.

Leetcode Link

Intuition

'z'). 2. Iterate over \$1 and \$2 simultaneously and, using the find() function, locate the root parent of the characters at the current indices in the Union-Find. If these roots are different, we unite the sets by making the root with a smaller index the parent of the

- root with a larger index. This step builds up the equivalence classes. 3. For each character in baseStr, replace it with the smallest equivalent character in its equivalence class. We find the smallest
- equivalent character by finding the root parent of the set the character belongs to.
- Solution Approach

The solution uses the Union-Find algorithm to group equivalent characters together. Each character maps to an integer from 0 to 25, corresponding to 'a' through 'z'. The find function and an array p are used to manage the parent relationships of these integers, which is key to understanding the connected components (equivalence classes) of characters.

Initially, each character is its own parent: p[i] = i. 1 p = list(range(26))

recursively finding the parent until p[x] == x. Upon finding the root parent, path compression is performed by setting p[x] to the

2. Find Function: The find function takes an integer x and finds the root parent in the Union-Find structure. This is done by

1. Parent Array Initialization: An array p of size 26 is initialized, where each index represents a unique character from 'a' to 'z'.

1 def find(x): if p[x] != x: p[x] = find(p[x])return p[x]

if pa < pb:

else:

1 res = []

2 for a in baseStr:

5 return ''.join(res)

Example Walkthrough

p[pb] = pa

p[pa] = pb

a = ord(a) - ord('a')

res.append(chr(find(a) + ord('a')))

defined by s1 and s2, and returns the result as a new string.

pa, pb = find(a), find(b)

The implementation steps are as follows:

- 3. Union Steps: The main loop iterates over the indices of \$1 and \$2, and for each pair of characters, it calculates their corresponding integer representations. Using the find function, it locates the root parents of each character's set. To maintain lexicographical order, it unions the sets by setting the parent of the higher index to the parent of the lower index. 1 for i in range(len(s1)):
 - 4. Building the Result String: Lastly, for each character in baseStr, it is replaced by the lexicographically smallest equivalent character. This is achieved by finding the root parent of each character's set and converting it back to the character representation.

root parent to flatten the structure, making future queries faster.

a, b = ord(s1[i]) - ord('a'), ord(s2[i]) - ord('a')

• s1 = "ab" s2 = "bc" baseStr = "adb" The mapping arising from s1 and s2 means a == b and b == c. Since the equivalence relationship is transitive, we can also deduce

1. Parent Array Initialization: We initialize the array p where p[i] = i for i = 0 to 25. For simplicity, assume the array is indexed

2. Find Function: We define a find function that will be used to find the root parent of a character's set in our Union-Find structure,

Using the Union-Find algorithm, we'll follow the steps to find the lexicographically smallest equivalent string of baseStr.

Let's walk through a small example to illustrate the solution approach. Suppose we have the following input:

By following these steps, the solution re-encodes baseStr into its smallest lexicographical form according to the equivalences

ensuring that we apply path compression along the way.

 $p = [0, 1, 2, \dots 25]$

starting at 0 for 'a', 1 for 'b', etc.

For i = 0 (considering a and b):

For i = 1 (considering b and c):

b maps to 1, and c maps to 2.

Now p looks like this: [0, 0, 2, ... 25].

For a (0), find(0) returns 0, so a remains a.

After this process, baseStr is transformed into "aad".

each element to itself.

representative of a set.

if parent[x] != x:

return parent[x]

for i in range(len(s1)):

parent[x] = find(parent[x])

char_index = ord(char) - ord('a')

Merge the sets of characters in strings s1 and s2

def find(x):

result = []

for char in base_str:

return ''.join(result)

parent = new int[26];

parent[i] = i;

} else {

for (int i = 0; i < 26; ++i) {

// Process the mappings in s1 and s2

for (int i = 0; i < s1.length(); ++i) {

int indexS1 = s1.charAt(i) - 'a';

int indexS2 = s2.charAt(i) - 'a';

int parentS1 = find(indexS1);

int parentS2 = find(indexS2);

// Union the parents by rank

if (parentS1 < parentS2) {</pre>

// Find the parents for both indices

parent[parentS2] = parentS1;

parent[parentS1] = parentS2;

parent = list(range(26))

that a == c.

- o a maps to 0, and b maps to 1. find(0) returns 0, and find(1) returns 1. Since 0 < 1, we set p[1] to 0.
- find(1) returns 0 (after path compression), and find(2) returns 2. Since 0 < 2, we set p[2] to 0.

4. Building the Result String: We construct the lexicographically smallest equivalent string for baseStr, "adb":

```
    For d (3), find(3) returns 3, so d remains d.

o For b (1), find(1) now returns 0 due to path compression, so b is replaced by a.
```

def smallestEquivalentString(self, s1: str, s2: str, base_str: str) -> str:

 $char_s1$, $char_s2 = ord(s1[i]) - ord('a')$, ord(s2[i]) - ord('a')

Initialize the parent array for union-find structure to point

The find function uses path compression for finding the

parent_s1, parent_s2 = find(char_s1), find(char_s2)

Build the resulting equivalent string based on the base string

by replacing each character with its smallest equivalent.

Join and return the computed characters as a single string.

// Parent array representing the disjoint set (union-find structure)

* @param baseStr - the base string to be transformed

// Initialize the parent array for 26 characters

// Convert the characters to zero-based indices

- first input string with mapping rules

- second input string with mapping rules

public String smallestEquivalentString(String s1, String s2, String baseStr) {

* @return The smallest lexicographical string after applying the rules from s1 and s2

result.append(chr(find(char_index) + ord('a')))

After this step, our p array reflects the transitive closure: [0, 0, 0, ... 25].

3. Union Steps: We iterate over s1 and s2 to build the equivalency classes:

s1 and s2 is "aad". Python Solution

As a result, the smallest equivalent string we can form from the base string "adb" following the equivalence relationships defined by

Link the sets by rank (in this case, by smallest representative). if parent_s1 < parent_s2:</pre> 19 20 parent[parent_s2] = parent_s1 21 else: 22 parent[parent_s1] = parent_s2

```
private int[] parent;
/**
 * Generates the smallest equivalent string based on mapping rules.
```

*/

* @param s1

* @param s2

Java Solution

1 class Solution {

class Solution:

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40 };

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38
           // Build the result string based on baseStr and union-find structure
           StringBuilder result = new StringBuilder();
39
            for (char ch : baseStr.toCharArray()) {
40
               // Translate the base characters according to the smallest parent character
               char smallestEquivalentChar = (char) (find(ch - 'a') + 'a');
                result.append(smallestEquivalentChar);
43
           return result.toString();
45
46
47
48
       /**
49
        * Finds the representative of the set that element x is part of.
50
        * @param x - an element for which to find the set representative
51
        * @return The parent or the representative of the set
52
53
       private int find(int x) {
54
55
           // Path compression: Update the parent along the search path
           if (parent[x] != x) {
56
               parent[x] = find(parent[x]);
57
58
59
           return parent[x];
60
61 }
62
C++ Solution
 1 class Solution {
2 public:
       vector<int> parent; // 'parent' vector represents the parent of each character set
       // Constructor initializes the 'parent' vector to self indicating each character is its own parent
       Solution() {
           parent.resize(26);
           iota(parent.begin(), parent.end(), 0);
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       // Function to find the smallest lexicographical equivalent string
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12
       string smallestEquivalentString(string s1, string s2, string baseStr) {
13
           // Union-Find algorithm to merge the equivalence of characters in s1 and s2
           for (int i = 0; i < s1.size(); ++i) {
14
                int charIndex1 = s1[i] - 'a'; // convert character from 'a' to 'z' into index 0 to 25
15
               int charIndex2 = s2[i] - 'a';
16
               int parent1 = find(charIndex1), parent2 = find(charIndex2);
17
               if (parent1 < parent2) // Union by rank: attach the larger parent to the smaller one
18
                    parent[parent2] = parent1;
19
               else
20
                    parent[parent1] = parent2;
21
22
23
24
           // Build the result by replacing each character in baseStr with its smallest equivalent
           string result = "";
25
26
            for (char c : baseStr) {
27
                result += (find(c - 'a') + 'a');
28
29
           return result;
30
31
32
       // Function to find the representative of the set that 'x' belongs to
33
       int find(int x) {
           if (parent[x] != x) {
34
```

// Path compression: make every node on the path point directly to the root

parent[x] = find(parent[x]);

// Global parent array to represent the parent of each character set

// Function to find the representative of the set that 'x' belongs to

// Path compression: make every node on the path point directly to the root

const parent: number[] = Array.from({ length: 26 }, (_, i) => i);

// Function to merge the equivalence of characters in s1 and s2

// Union by rank: attach the larger parent to the smaller one

const charIndex2 = s2.charCodeAt(i) - 'a'.charCodeAt(0);

// Build the result by replacing each character in baseStr with its smallest equivalent

A loop that iterates through s1 and s2 strings (both are of equal length): for i in range(len(s1)).

function union(charIndex1: number, charIndex2: number): void {

return parent[x];

function find(x: number): number {

parent[x] = find(parent[x]);

const parent1 = find(charIndex1);

const parent2 = find(charIndex2);

parent[parent2] = parent1;

parent[parent1] = parent2;

union(charIndex1, charIndex2);

Time and Space Complexity

result += smallestEquivalentCharacter;

if (parent1 < parent2) {</pre>

Typescript Solution

if (parent[x] !== x) {

return parent[x];

24 // Function to find the smallest lexicographical equivalent string function smallestEquivalentString(s1: string, s2: string, baseStr: string): string { // Loop through the provided strings to perform the Union-Find algorithm 27 for (let i = 0; i < s1.length; ++i) {</pre> 28 const charIndex1 = s1.charCodeAt(i) - 'a'.charCodeAt(0); // convert character from 'a' to 'z' into index 0 to 25 29

let result = "";

return result;

Time Complexity:

for (const c of baseStr) {

} else {

The given code represents a solution to find the smallest equivalent string based on the character mappings described by \$1 and \$2, and then applies this mapping to baseStr.

const smallestEquivalentCharacter = String.fromCharCode(find(c.charCodeAt(0) - 'a'.charCodeAt(0)) + 'a'.charCodeAt(0));

 The find function, which is a path compression technique in the Union-Find algorithm. The amortized time complexity for each call to find is $O(\alpha(n))$, where $\alpha(n)$ is the Inverse Ackermann function. It is nearly constant and very slow-growing, basically considered a constant for practical purposes.

The time complexity of the code is derived from the following operations:

Since we run the find operation for each character in \$1/\$2 and then again for each character in baseStr, the total time complexity is $0(n + m * \alpha(n))$, where n is the length of s1/s2 and m is the length of baseStr. The term $\alpha(n)$ can usually be omitted when discussing practical time complexity, leading to O(n + m).

Iterating through each character in baseStr and performing the find operation.

Space Complexity: The space complexity is determined by:

• The parent array p of fixed size 26, which corresponds to the 26 possible characters: 0(26) or 0(1) since it's a constant size.

Therefore, the space complexity is 0(m + 1) or simply 0(m) since the term 0(1) is negated when compared to non-constant space usage.

The res list that will eventually contain every character in baseStr: 0(m), where m is the length of baseStr.

In conclusion, the time complexity of the provided code is 0(n + m) and the space complexity is 0(m).

4. After processing all characters of baseStr, the resulting string is the lexicographically smallest equivalent string.

The provided solution code follows the above approach using Union-Find to efficiently transform baseStr into its lexicographically smallest form respecting the equivalency relations defined by \$1 and \$2.

To find the lexicographically smallest string equivalent to baseStr, we can leverage a classic data structure known as the Union-Find or Disjoint Set Union (DSU). This structure helps efficiently handle equivalence relationships by finding and uniting equivalent components. 1. Initialize a disjoint set where each character initially belongs to its own set, which is indexed from 0 to 25 (mapping to 'a' through

In this problem, you're given three strings s1, s2, and baseStr, all of which are of the same length. Characters at corresponding positions in s1 and s2 are considered equivalent, which means s1[i] is equivalent to s2[i]. This equivalence relationship is reflexive,