2366. Minimum Replacements to Sort the Array

Greedy Array Hard

Problem Description

perform involves replacing a single element in the array with any two elements that sum up to the original element. For instance, if you have an element 6 in the array, you can replace it with two elements 2 and 4 since 2 + 4 = 6. The challenge lies in figuring out the minimum number of such operations required to sort the entire array.

You are provided with an array of integers called nums. The goal is to sort this array into non-decreasing order (where each

number is less than or equal to the next) by performing a specific operation as many times as needed. The operation you can

Intuition

The solution to this problem hinges on a key observation: replacing any number with two smaller numbers can potentially make sorting the array harder, as it introduces more elements that need to be in non-decreasing order. Therefore, we should aim to

To minimize operations, we work our way from the end of the array (the largest elements in a sorted array) to the beginning, adjusting each element so that it's not larger than the one already considered and positioned at the end. As we move backwards:

perform each replacement in a way that either maintains the current order or requires the least amount of subsequent operations.

1. We want the current element to be less than or equal to the element after it (since the array must be in non-decreasing order). 2. If the current element is already less than or equal to the next element, no operation is needed, and we move to the previous element.

3. If the current element is larger, we need to split it into smaller numbers in a way that requires the minimum number of splits while ensuring that

each new number is not larger than the next element.

- The algorithm keeps track of the maximum allowed value (mx) for each replacement, which initially is the value of the last
- element. It computes the minimum number of splits (k) needed for the current element to satisfy the non-decreasing order constraint, and updates the answer (ans) with the number of operations needed (which is k - 1, since replacing one number

with two requires one operation). After this, it updates the maximum allowed value for the next element accordingly.

The process continues until we've considered all elements of the array, and the minimum number of operations required to achieve a non-decreasing array is returned. **Solution Approach**

the array since we aim to ensure that all preceding numbers are less than or equal to this value. The main logic resides in a for-loop that starts from the second-to-last element and moves towards the first element (index 0).

To implement the solution, we follow a reverse iteration. We initiate by setting the variable mx to the value of the last element in

For-loop iteration: The loop starts at index n - 2 because we're comparing each element with the one after it. We

decrement our index with every iteration, essentially moving from the end of the array to the start. Conditional Operation: For each number, we check if it's less than or equal to mx. If it is, we're already maintaining the non-

if nums[i] <= mx:</pre>

mx = nums[i]

as large as possible without exceeding mx.

reverse) number in the array.

iteration through the array.

Example Walkthrough

procedure step by step.

maximum allowed value for the preceding element) and continue.

decreasing order. So the answer (ans) is 1.

def minimumReplacement(self, nums: List[int]) -> int:

Get the number of elements in the nums list.

for i in range(num elements -2, -1, -1):

public long minimumReplacement(int[] nums) {

// Get the number of elements in the array.

long replacements = 0;

int maxValue = nums[n - 1];

int n = nums.length;

Set the current maximum to the last element in the nums list.

Initialize the count of replacements to 0.

once, making the complexity O(n).

replacement_count = 0

 $num_elements = len(nums)$

current_max = nums[-1]

Here's a breakdown:

decreasing order, so we set mx to the current number (since this can be the new maximum for the upcoming previous elements) and continue to the next iteration without any further action.

continue Calculation of Splits (k): When the current number is greater than mx, we calculate k, the minimum number of parts we

need to split the current number into. This must be done such that each part does not exceed the value of mx. The

calculation of k is given by (nums[i] + mx - 1) // mx. We add mx - 1 before integer division to ensure that all parts will be

Updating Answer: The number of new elements added (which is equal to the number of operations performed) will be k - 1.

nums[i] // k. This new value of mx will now act as the upper limit for the next (actually the previous since we're iterating in

ans += k - 1Updating mx for the next iteration: We update mx to the largest possible value that a part can take after the split, which is

This value is added to ans, the variable tallying the minimum number of operations.

Returning the result: Once the loop has been completed, the variable ans will hold the minimum number of operations needed to sort the array, which is returned as the result.

The algorithm does not require any additional data structures; it operates in-place, using only a few additional variables for

keeping track of the state (ans, mx, k). It's a simple, yet efficient solution with a time complexity of O(n) as it requires a single

Let's consider an example to illustrate the solution approach. Suppose we are given the following array nums: nums = [10, 5, 13]

We need to sort this array into non-decreasing order by replacing elements into sums as needed. Let's walk through the

We start by setting mx to the value of the last element in nums, which is 13. This is the maximum allowed value for its preceding elements. We then begin iterating from the second-to-last element, which is 5 at index 1.

∘ For nums [1] which is 5, since 5 ≤ mx (13), we do not need to perform any operations. We set mx to 5 (since 5 now becomes the

Next, we check nums[0], which is 10. Since 10 > mx (5 now), we need to perform operations. Calculating k gives us:

The number of new elements added is k - 1 which is 1. Thus, we have 1 operation performed.

We update ans with the number of operations performed, so ans becomes 1.

k = (nums[0] + mx - 1) // mx = (10 + 5 - 1) // 5 = 2

class Solution:

We update mx to the largest value possible after the splits, which is nums[0] // k = 10 // 2 = 5. Having iterated over all elements, we conclude that we needed a minimum of 1 operation to sort the array into non-

This is the result of using the approach described in the solution. The process is time-efficient as it iterates through the array just

Since k is 2, it means we need to split 10 into two parts, each not exceeding 5 (the current mx). We can split it into [5, 5].

- **Solution Implementation Python**
 - # no replacements are needed. Update the current maximum to this element. if nums[i] <= current max:</pre> current_max = nums[i] else:

This maximum represents the highest number we can decrease to without making any replacements.

Iterate through the list in reverse order, starting from the second to last element.

This is done by dividing the current element by the current maximum.

Then compute how many replacements are needed to reach this value.

Update the current maximum to the value obtained by evenly dividing

replacements needed = (nums[i] + current max - 1) // current max

and rounding up to ensure we get a value no larger than the current max.

replacement_count += replacements_needed - 1 # Increase the count of replacements

This will be the new threshold for further calculations on previous elements.

// Initialize the max value to the last element in the array (it's already in correct position).

If the current element is less than or equal to the current maximum,

If the current element is greater than the current maximum,

we calculate the minimum number of replacements required.

the current element by the number of replacements needed.

// Method to find the minimum number of replacements to make the array non-increasing.

// such that each replaced number is less than or equal to maxElement

// Update maxElement to the value of the largest possible replaced number

int replacements = (nums[i] + maxElement - 1) / maxElement;

// Return the total number of operations required to make the array

// non-decreasing by replacing some numbers with multiple numbers.

* Calculates the minimum number of replacements needed such that for every i,

// Initialize variable to store the current lowest number from the back

operations += replacements - 1;

* nums[i] is greater than or equal to nums[i + 1].

function minimumReplacement(nums: number[]): number {

* @param {number[]} nums - Array of numbers to be modified.

* @return {number} - The minimum number of replacements needed.

return operations;

// Get the length of the array

let currentMin = nums[length - 1];

const length = nums.length;

};

/**

TypeScript

maxElement = nums[i] / replacements;

// The actual replacements will be one less than the calculated

// replacements since we are also including the current element

// Initialize the answer to accumulate the number of replacements.

current_max = nums[i] // replacements_needed

```
# Return the total count of replacements required to make the array non-increasing.
        return replacement_count
Java
```

class Solution {

```
// Loop through the array from second-to-last to the first element.
        for (int i = n - 2; i >= 0; --i) {
            // If the current element is less than or equal to the max value,
            // it is already in right position, thus move to the previous element.
            if (nums[i] <= maxValue) {</pre>
                maxValue = nums[i]; // Update the max value to the current element.
                continue;
            // If the current element is larger than the max value, calculate the number of parts
            // this element needs to be split into to maintain non-increasing order.
            int parts = (nums[i] + maxValue - 1) / maxValue;
            // Update the replacements count by adding the number of new elements added
            // (parts - 1 means how many splits we do, which equals to additional numbers introduced).
            replacements += parts - 1:
            // The new max value should be the average of the current element
            // after replacing it with 'parts' equal or almost equal numbers.
            maxValue = nums[i] / parts;
        // Return the total number of replacements done to make the array non-increasing.
        return replacements;
C++
#include <vector>
class Solution {
public:
    long long minimumReplacement(std::vector<int>& nums) {
        long long operations = 0; // Stores the total number of operations required
        int size = nums.size(); // Size of the input vector
        int maxElement = nums[size - 1]; // Initialize maxElement with the last item in the vector
        // Iterate from the second to last element to the beginning
        for (int i = size - 2; i >= 0; --i) {
            // If the current element is less than or equal to maxElement.
            // it's already in the correct order, update maxElement if necessary
            if (nums[i] <= maxElement) {</pre>
                maxElement = nums[i];
                continue;
            // Calculate the minimum number of replacements needed for nums[i]
```

```
// Initialize variable to store the answer
   let replacements = 0;
   // Iterate from the second-to-last element down to the first element
   for (let i = length - 2; i >= 0; --i) {
       // If the current element is less than or equal to the current lowest number, no need to replace
       if (nums[i] <= currentMin) {</pre>
            currentMin = nums[i];
            continue;
       // Calculate how many times the current number needs to be divided
       // to be less than or equal to the current lowest number.
        const factor = Math.ceil(nums[i] / currentMin);
       // Accumulate the total number of replacements needed
        replacements += factor - 1;
       // Update the current lowest number to be the divided number
       currentMin = Math.floor(nums[i] / factor);
   // Return the total number of replacements
   return replacements;
class Solution:
   def minimumReplacement(self, nums: List[int]) -> int:
       # Initialize the count of replacements to 0.
        replacement_count = 0
       # Get the number of elements in the nums list.
       num_elements = len(nums)
       # Set the current maximum to the last element in the nums list.
       # This maximum represents the highest number we can decrease to without making any replacements.
       current_max = nums[-1]
       # Iterate through the list in reverse order, starting from the second to last element.
       for i in range(num elements -2, -1, -1):
           # If the current element is less than or equal to the current maximum,
           # no replacements are needed. Update the current maximum to this element.
           if nums[i] <= current max:</pre>
               current_max = nums[i]
           else:
               # If the current element is greater than the current maximum,
               # we calculate the minimum number of replacements required.
               # This is done by dividing the current element by the current maximum,
               # and rounding up to ensure we get a value no larger than the current max.
               # Then compute how many replacements are needed to reach this value.
                replacements needed = (nums[i] + current max - 1) // current max
                replacement_count += replacements_needed - 1 # Increase the count of replacements
               # Update the current maximum to the value obtained by evenly dividing
               # the current element by the number of replacements needed.
               # This will be the new threshold for further calculations on previous elements.
```

return replacement_count Time and Space Complexity

current_max = nums[i] // replacements_needed

Return the total count of replacements required to make the array non-increasing.

The time complexity of the code provided is O(n) where n is the length of the input list nums. This is because the algorithm

Time Complexity

iterates through the list once in reverse, beginning from the penultimate element to the first element. The operations within each iteration of the loop take constant time, such as comparison, arithmetic operations, and variable assignments. There are no nested loops or additional function calls that would change the linearity of the time complexity. **Space Complexity**

The space complexity of the code provided is 0(1). The algorithm uses a fixed amount of extra space regardless of the input size. Only a few single-value variables (ans, n, mx) are used for storage, and their space does not scale with the size of the input nums. No additional data structures that would grow with the size of the input are used, so the space usage remains constant.