

# Problem Description

In this problem, we are given two non-negative integer numbers represented as strings, num1 and num2, and our task is to calculate the product of these two numbers and return the result as a string. The constraint is that we are not allowed to use any built-in library that can handle big integers, nor can we simply convert the strings to integers and multiply them in the standard way. This challenges us to think about how we can perform multiplication manually, mimicking the way one might do it on paper.

# Intuition

The intuition behind the solution is based on how we perform multiplication by hand between two numbers. More precisely, when we multiply, say, a three-digit number by a two-digit number, we do it digit by digit and keep track of the carries. This process results in a series of partial products, which are then added together to form the final product.

digits of the partial products. The length of this array is the sum of the lengths of num1 and num2 because that's the maximum possible length of the result (e.g., 99 \* 99 is 9801, four digits long, which is the sum of the lengths of the numbers being multiplied). Next, we iterate over each digit of num1 and num2 in nested loops, and for each pair of digits, we multiply them and add the result to

To implement this in code, we need a data structure to store intermediate results. The approach is to use an array arr to store the

the corresponding position in arr. The key formula for the index in arr where we should accumulate the product of digits at positions i and j is arr[i+j+1]. After we have all the partial products, we then iterate through the arr array to handle carries at each position, adjusting each digit so

that it represents a proper digit in a number (less than 10), and propagating the carry to the next position. Finally, we need to return the string representation of the number stored in the array, but we skip any leading zeroes, as they don't

Solution Approach

contribute to the magnitude of the number. We join the remaining digits together to form the resulting product string to be returned.

# 1. Check for Zero: If either num1 or num2 is "0", the product is "0". We catch this case early to simplify further logic.

The solution follows these steps:

- 2. Initialization: Determine the lengths m and n of num1 and num2, respectively. Initialize an array arr of length m + n to hold the digits of the product.
- 3. Digit-by-Digit Multiplication:

Iterate through the digits of num1 and num2 in descending order using two nested loops, with indices i and j.

# Add the multiplication result to an appropriate position in the array arr: arr[i + j + 1] += a \* b.

The position i + j + 1 comes from the fact that when you multiply a digit at position i of num1 with a digit at position j of

For each position, if the value is greater than 9, divide by 10 to find the carry and keep the remainder:

- num2, the result will contribute to the digits at positions i + j and i + j + 1 of the product.
- 4. Handling Carries:
- arr[i 1] += arr[i] // 10: This propagates the carry to the next higher position.
  - arr[i] = 10: This ensures that the current position has only a single digit. 5. Converting Array to String:

Iterate backwards through arr, starting from the end, to process carries.

Convert current digits to integers and multiply them: a \* b.

- If the digit at the highest position (arr[0]) is zero, it's a leading zero and should be omitted. Determine the starting index for
- the conversion (1), which is 0 if there's no leading zero, and 1 otherwise. Join the digits from the arr starting at the right index i to form a string without leading zeros: "".join(str(x) for x in
- arr[i:]).

manual multiplication on paper.

- This implementation doesn't use any special algorithms or data structures—it uses simple arrays and elementary math operations to simulate digit-by-digit multiplication, carefully considering the placement of each partial product and the handling of carries, just like
- Example Walkthrough

To illustrate the solution approach, let's walk through a small example where num1 = "13" and num2 = "24". 1. Check for Zero: Neither num1 nor num2 are "0", so we proceed.

2. Initialization: The length m of num1 is 2, and the length n of num2 is also 2. We initialize an array arr of length m + n = 4 to [0, 0,

# 0, 0].

3. Digit-by-Digit Multiplication:

○ We iterate over num1 and num2 in reverse order so we will have the indices i=1,0 for num1 and j=1,0 for num2.

o arr is [0, 6, 7, 2], so we omit the leading zero.

if num1 == "0" or num2 == "0":

# Create a result list to store the product digits

result = [0] \* (length\_num1 + length\_num2)

return "0"

- For i=1 (num1[1] = "3") and j=1 (num2[1] = "4"), we multiply the digits and add the result to arr[i + j + 1], which is arr[3] = 0 + (3 \* 4) = 12.We store 2 in arr[3] and carry over 1 to arr[2], so arr becomes [0, 0, 1, 2].
- i=1, j=0: arr[2] += 3 (num1[1]) \* 2 (num2[0]); arr becomes [0, 0, 7, 2].

We repeat this for all pairs of digits:

- i=0, j=1: arr[1] += 1 (num1[0]) \* 4 (num2[1]); arr becomes [0, 4, 7, 2]. i=0, j=0: arr[1] += 1 (num1[0]) \* 2 (num2[0]); arr becomes [0, 6, 7, 2]. 4. Handling Carries:
  - Starting from the end of arr, we process the carries: At arr[2] (7): We add 7 // 10 to arr[1] and set arr[2] to 7 % 10. arr stays [0, 6, 7, 2] as 7 is less than 10.

The final result of multiplying "13" by "24" using our manual algorithm results in "672", which matches what we expect from standard

• The final product string is "672" as we join the digits from arr starting from index 1.

At arr[1] (6): We do the same. There's no carry since 6 is also less than 10.

Python Solution

multiplication.

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5. Converting Array to String:

class Solution: def multiply(self, num1: str, num2: str) -> str: # If either number is "0", return "0" because the product will also be "0"

// Initialize an array to store the product of each digit multiplication.

// Add the product of the two digits to the corresponding position.

int[] productArray = new int[length1 + length2];

for (int  $j = length2 - 1; j >= 0; --j) {$ 

int digit2 = num2.charAt(j) - '0';

for (int  $i = length1 - 1; i >= 0; --i) {$ 

int digit1 = num1.charAt(i) - '0';

// Loop over each digit in num1 and num2 and multiply them.

productArray[i + j + 1] += digit1 \* digit2;

// Multiply each digit of num1 with each digit of num2

result[i + j + 1] += digit1 \* digit2;

// Handle carrying over the value for digits greater than 9

for (int  $j = length2 - 1; j >= 0; --j) {$ 

for (int i = result.size() - 1; i > 0; --i) {

int startIndex = result[0] == 0 ? 1 : 0;

// Convert the result vector to a string

// Return the final product as a string

// Iterate over each digit in the first number.

for (let i = 0; i < length1; i++) {</pre>

let partialSum = '';

for (int i = startIndex; i < result.size(); ++i) {</pre>

string resultStr;

return resultStr;

Typescript Solution

int digit1 = num1[i] - '0'; // Convert char to integer

int digit2 = num2[j] - '0'; // Convert char to integer

// Add to the corresponding position in the result vector

resultStr += '0' + result[i]; // Convert integer to char and append to resultStr

1 // Multiplies two non-negative integers represented as number strings and returns the product as a string.

for (int  $i = length1 - 1; i >= 0; --i) {$ 

6 # Determine the lengths of the input strings 7 length\_num1, length\_num2 = len(num1), len(num2) 8 9

# Add product of current digits to the previously stored value in result list

#### 13 # Reverse process of multiplication, processing digits from the end 14 for i in range(length\_num1 - 1, -1, -1): 15 digit\_num1 = int(num1[i]) for j in range(length\_num2 - 1, -1, -1): 16 17 digit\_num2 = int(num2[j])

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                     result[i + j + 1] += digit_num1 * digit_num2
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             # Handle carrying over digits > 9 to the next place
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             for i in range(length_num1 + length_num2 - 1, 0, -1):
 23
                 result[i - 1] += result[i] // 10 # carry over
                 result[i] %= 10
                                                     # keep only the last digit
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             # Skip leading zeros in the result list
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             start_index = 0 if result[0] != 0 else 1
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             # Convert the result list to string
             return "".join(str(digit) for digit in result[start_index:])
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Java Solution
    class Solution {
         public String multiply(String num1, String num2) {
             // If either number is 0, the product will be 0.
             if ("0".equals(num1) || "0".equals(num2)) {
  4
                 return "0";
             }
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  8
             // Get lengths of both numbers.
  9
             int length1 = num1.length(), length2 = num2.length();
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### 22 23 24 25 // Normalize the productArray so that each position is a single digit. 26 for (int i = productArray.length - 1; i > 0; --i) {

### 27 productArray[i - 1] += productArray[i] / 10; // Carry over the tens to the next left cell. 28 productArray[i] %= 10; // Keep the units in the current cell. 29 30 31 // Skip the leading 0 in the product array if it exists. 32 int startIndex = productArray[0] == 0 ? 1 : 0; 33 // Convert the product array into a string. 34 35 StringBuilder product = new StringBuilder(); 36 for (int i = startIndex; i < productArray.length; ++i) {</pre> 37 product.append(productArray[i]); 38 39 return product.toString(); 40 41 } 42 C++ Solution 1 class Solution { public: string multiply(string num1, string num2) { // Check if either input is "0", if yes, then result is "0" if (num1 == "0" || num2 == "0") { return "0"; 8 9 // Initialize the sizes of the input numbers 10 int length1 = num1.size(), length2 = num2.size(); 11 12 // Create a vector to store the multiplication result 13 vector<int> result(length1 + length2, 0); 14

#### 27 result[i - 1] += result[i] / 10; // Carry over 28 result[i] %= 10; // Remainder stays at current position 29 30 31 // Skip any leading zeros in the result vector

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**}**;

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function multiply(num1: string, num2: string): string {
       // If either number is '0', the product will be '0'.
       if ([num1, num2].includes('0')) return '0';
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 6
       // Get the lengths of the two number strings.
       const length1 = num1.length;
       const length2 = num2.length;
 8
       let answer = '';
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let currentDigit1 = parseInt(num1.charAt(length1 - i - 1), 10);

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            // Iterate over each digit in the second number.
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            for (let j = 0; j < length2; j++) {</pre>
                let currentDigit2 = parseInt(num2.charAt(length2 - j - 1), 10);
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19
                // Multiply current digits and add them to the partial sum with proper offset.
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                partialSum = addString(partialSum, (currentDigit1 * currentDigit2) + '0'.repeat(j));
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24
           // Construct the answer with the accumulated partial sum with proper offset.
25
            answer = addString(answer, partialSum + '0'.repeat(i));
26
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28
       // Return the final product as a string.
29
        return answer;
30 }
31
32 // Adds two number strings and returns the sum as a string.
   function addString(numString1: string, numString2: string): string {
        const length1 = numString1.length;
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35
        const length2 = numString2.length;
36
       let answerArray = [];
37
       let carry = 0;
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39
       // Add the two strings together, digit by digit, from the end to the beginning.
40
       for (let i = 0; i < Math.max(length1, length2) || carry > 0; i++) {
41
            let digit1 = i < length1 ? parseInt(numString1.charAt(length1 - i - 1), 10) : 0;</pre>
```

### 51 return answerArray.join(''); 52 } 53

Time and Space Complexity

let sum = digit1 + digit2 + carry;

// Join the computed digits to form the final sum string.

answerArray.unshift(sum % 10);

carry = Math.floor(sum / 10);

Time Complexity: The time complexity of the given code is 0(m \* n), where m and n are the lengths of the input strings num1 and num2 respectively. The code involves a double loop where the outer loop runs m times and the inner loop runs n times, leading to m \* n multiplication operations. Additionally, there is a loop for carrying over the values, which runs in 0(m + n) time. However, since 0(m

Space Complexity: The space complexity is 0(m + n), as an additional array arr of size m + n is used to store the intermediate results of the multiplication before they are converted to the final string result.

\* n) dominates 0(m + n), the overall time complexity stays 0(m \* n).

let digit2 = i < length2 ? parseInt(numString2.charAt(length2 - i - 1), 10) : 0;</pre>

// Calculate the sum for current place and maintain the carry for the next iteration.