2907. Maximum Profitable Triplets With Increasing Prices I Medium (Array) Dynamic Programming

Problem Description

the function should return -1.

In this problem, we're given two 0-indexed integer arrays: prices and profits. Both arrays have a length of n, and they represent items in a store where the ith item has a price of prices[i] and a potential profit of profits[i].

Leetcode Link

The task is to select three different items to maximize our profit under a specific condition: we must pick items in a manner that their indices i, j, and k follow i < j < k, and their prices also follow an increasing order, prices[i] < prices[j] < prices[k]. In simpler

terms, the second item's price and index should be higher than the first, and the third item's price and index should be higher than the second. Our profit from such a selection would be the sum of the corresponding profits of these items: profits[i] + profits[j] + profits[k].

Intuition

The intuitive approach to solve this problem is by trying to break it down and identify subproblems that make up the whole. We do

The output should be the maximum achievable profit following these rules. However, if it's impossible to find such a triplet of items,

this by picking one piece of the problem to focus on and then solving the remaining aspects around it.

price restrictions are satisfied (i < j < k with prices[i] < prices[j] < prices[k]).

one-dimensional problem focused around the chosen mid-point, which is much more efficient.

In this case, we can streamline our search by fixing one of the elements as the pivotal middle element - that's the j index or our second item's position. The aim is to select this middle element such that we can find one i and one k where both the index and

Once j is fixed, we look for the maximum profit on the left (profits[i]) and the maximum profit on the right (profits[k]) that fulfill

our conditions related to both price and index ordering. By doing this for every possible middle element, we ensure that no possible profitable combination is missed. The variables left and right in the solution help us keep track of the maximum profits found to the left and right of our fixed middle

element. If we find valid left and right profits, we calculate the total profit for the current selection and compare it with the

maximum found so far (ans). Repeating this process and updating ans when we find a greater total profit ensures that we arrive at the highest possible profit by the end of the function. This strategy reduces the problem from a three-dimensional one (where we could naively check every possible triplet of items) to a

The implementation of the solution begins by first understanding that the problem can be approached by iterating through the list of items and fixing the middle element of the triplet to simplify the process. This approach falls under the pattern of iteration combined with local optimization.

1. Initialization: The variable ans is initialized with -1, this will store the maximum profit or remain -1 if no valid trio is found.

2. Outer Loop: We start by creating an outer loop to iterate over each potential middle item j: 1 for j, x in enumerate(profits):

Solution Approach

Here's how the solution works:

3. Initialize Left and Right Profit: For each j, initialize two variables left and right both to 0. These will store the maximum profits to the left and to the right of j respectively.

(profits[i]) such that the price at i is less than the price at j: 1 for i in range(j):

1 if left and right:

left = profits[i]

5. Find Right Maximum Profit: Similarly, we iterate from the element after j to the end of the list to find the maximum profit

6. Calculate and Compare Profit: If we found valid left and right profits (meaning that left and right are not 0), we calculate the

total profit for this triplet, which is left + x + right, where x is profits[j]. We then check if this total profit is greater than the

4. Find Left Maximum Profit: We iterate from the start of the list to the element just before j to find the maximum profit

(profits[k]) such that the price at j is less than the price at k: 1 for k in range(j + 1, n): if prices[j] < prices[k] and right < profits[k]:</pre>

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ans = max(ans, left + x + right)
7. Return Result: After iterating through all possible middle elements, and contains the maximum profit. The function finally returns
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Suppose we have the following prices and profits arrays:

ans which is either the maximum profit found or -1 if no valid triplet was found.

right = profits[k]

current maximum profit stored in ans:

if prices[i] < prices[j] and left < profits[i];</pre>

improves over a naive $0(n^3)$ solution that would examine all possible triplets one by one. Example Walkthrough Let's illustrate the solution approach with a small example:

This algorithm runs in O(n^2) time, because for each of the n elements chosen as a middle element, it performs potentially O(n) work

to find left and O(n) work to find right. While not the most efficient for very large numbers of items, it's a reasonable approach that

The algorithm efficiently updates its best-known solution with each iteration, employing an iterative approach, while breaking the

problem down into smaller sub-tasks (finding left and right maximums) that can be solved independently of each other.

The process will be as follows: 1. Initialize ans = -1, as we have not found any triplet yet.

And we wish to maximize our profit by selecting three items such that their prices and indices are in strictly increasing order.

2. The outer loop iterates with j starting from 0 to n-1. In this case, n is 4. So j will take on values 0, 1, 2, and 3 one by one.

5. For j = 1, we have:

6. Move to j = 2:

• prices = [3, 1, 4, 2]

profits = [4, 1, 5, 3]

 Start i loop from 0 to (j-1), i.e., i = 0. Check if prices [0] < prices [1], which is 3 < 1. This is false, so we skip.

3. For each j, initialize left = 0 and right = 0.

left = 0: No profit picked yet.

left = 0: No profit picked yet.

Start i loop:

• i = 0: prices[0] < prices[2] is 3 < 4, true, and profits[0] is 4, which is greater than left.</p>

• i = 1: prices[1] < prices[2] is 1 < 4, true, but profits[1] is 1, which is not greater than the current left.

• Start k loop from (j+1) to n, i.e., k = 3.

Update left = 4.

Keep left = 4.

7. Continue to j = 3:

Final step:

update ans.

Python Solution

class Solution:

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o prices[2] < prices[3] is 4 < 2. This is false, so no right profit is updated.

• i = 0: prices[0] < prices[3] is 3 < 2. This is false, so continue.</pre>

4. For j = 0, there is no element to the left of profits[j], so we can skip and continue with j = 1.

- left = 0 again. Start i loop:
 - i = 1: prices[1] < prices[3] is 1 < 2. This is true and profits[1] is 1. Update left = 1. i = 2: prices[2] < prices[3]. This is false, so keep left = 1.</pre>

Since we are at the last element, there are no elements to the right for comparison; hence, no update to right.

• The maximum profit calculated with j=2 was left + profits[j] + right, but because we did not find a valid right, we do not

• Therefore, the output of the algorithm would be -1 since we never updated our initial ans value from -1 given that no valid triplet

could satisfy the conditions of the problem with the provided example arrays.

num_prices = len(prices)

return max_profit_value

int n = prices.length;

int maxLeftProfit = 0;

int maxRightProfit = 0;

 $max_profit_value = -1$ 9 # Iterate through each price and associated profit 10 for current_index, current_profit in enumerate(profits): # Initialize the max left and right profits to zero 11

Initialize the maximum profit to -1 to signify that initially, there is no profit

Search to the left of the current index for a price that is lower than the current price

if prices[left_index] < prices[current_index] and max_profit_left < profits[left_index]:</pre>

if prices[current_index] < prices[right_index] and max_profit_right < profits[right_index]:</pre>

Search to the right of the current index for a price that is higher than the current price

and also search for the maximum left profit that is associated with such a price

and also search for the maximum right profit associated with such a price

calculate the sum of the current profit and the left and right profits

total_profit = max_profit_left + current_profit + max_profit_right

and update the maximum profit if greater than the current maximum

max_profit_value = max(max_profit_value, total_profit)

Return the maximum profit after examining all possible transactions

def max_profit(self, prices: List[int], profits: List[int]) -> int:

max_profit_left = profits[left_index]

for right_index in range(current_index + 1, num_prices):

max_profit_right = profits[right_index]

Get the number of available prices/profits

max_profit_left = max_profit_right = 0

for left_index in range(current_index):

If both left and right profits are found,

if max_profit_left and max_profit_right:

public int maxProfit(int[] prices, int[] profits) {

35 Java Solution

// 'n' holds the total number of elements in the prices and profits arrays, as they are of the same length.

// 'maxLeftProfit' will keep track of the maximum profit to the left of the 'current' index.

// 'maxRightProfit' will keep track of the maximum profit to the right of the 'current' index.

// 'maxProfit' will keep track of the maximum profit found. Initialized to -1 as a default value. int maxProfit = -1; // Iterate through all the possible purchase indexes. for (int current = 0; current < n; ++current) {</pre> 10

class Solution {

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// Checking for the maximum profit that can be obtained before the current index.
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                for (int i = 0; i < current; ++i) {
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                    // Only consider the profit if the price previously was less than the current price.
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                    if (prices[i] < prices[current]) {</pre>
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                        maxLeftProfit = Math.max(maxLeftProfit, profits[i]);
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               // Checking for the maximum profit that can be obtained after the current index.
                for (int k = current + 1; k < n; ++k) {
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                    // Only consider the profit if the current price is less than the future price.
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                    if (prices[current] < prices[k]) {</pre>
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                        maxRightProfit = Math.max(maxRightProfit, profits[k]);
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               // If there's a possible profit both to the left and right of the current index, check if this transaction sequence is the
               if (maxLeftProfit > 0 && maxRightProfit > 0) {
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                    maxProfit = Math.max(maxProfit, maxLeftProfit + profits[current] + maxRightProfit);
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           // Return the maximum profit found. If no profitable sequence is found, return -1.
            return maxProfit;
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42 }
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C++ Solution
   #include <vector>
 2 #include <algorithm> // For max function
   using namespace std;
   class Solution {
   public:
        int maxProfit(vector<int>& prices, vector<int>& profits) {
            int numDays = prices.size(); // Number of days is the size of the prices vector
            int maxProfit = -1; // Initialize maxProfit to -1 (will signify no profit if it stays the same)
           // Iterate through each day to find the maximum profit
           for (int today = 0; today < numDays; ++today) {</pre>
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                int bestProfitBeforeToday = 0; // Maximum profit from previous transactions before today
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int bestProfitAfterToday = 0; // Maximum profit from transactions after today

bestProfitBeforeToday = max(bestProfitBeforeToday, profits[prevDay]);

bestProfitAfterToday = max(bestProfitAfterToday, profits[nextDay]);

int totalProfit = bestProfitBeforeToday + profits[today] + bestProfitAfterToday;

// If there is a profit possible before and after today, update maxProfit

// Calculate the best profit from transactions before today

// Calculate the best profit from transactions after today

for (int nextDay = today + 1; nextDay < numDays; ++nextDay) {</pre>

if (bestProfitBeforeToday > 0 && bestProfitAfterToday > 0) {

for (int prevDay = 0; prevDay < today; ++prevDay) {</pre>

if (prices[prevDay] < prices[today]) {</pre>

if (prices[today] < prices[nextDay]) {</pre>

maxProfit = max(maxProfit, totalProfit);

// Return the maximum profit that can be achieved

return maxProfit;

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40 };
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Typescript Solution
   function maxProfit(prices: number[], profits: number[]): number {
       // Get the length of the arrays.
       const numPrices = prices.length;
       // Initialize the answer to -1 to indicate no profit if not updated.
       let maximumProfit = -1;
       // Iterate over all prices.
       for (let current = 0; current < numPrices; ++current) {</pre>
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           // Initialize the maximum profit before and after the current index.
           let maxProfitBefore = 0;
           let maxProfitAfter = 0;
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           // Compute the maximum profit before the current index.
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           for (let before = 0; before < current; ++before) {</pre>
               if (prices[before] < prices[current]) {</pre>
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                   maxProfitBefore = Math.max(maxProfitBefore, profits[before]);
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           // Compute the maximum profit after the current index.
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           for (let after = current + 1; after < numPrices; ++after) {
               if (prices[current] < prices[after]) {
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                   maxProfitAfter = Math.max(maxProfitAfter, profits[after]);
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           // If there is a profit before and after the current index,
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           // update the maximum profit if the sum of profits is greater than the current maximum.
           if (maxProfitBefore > 0 && maxProfitAfter > 0) {
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               maximumProfit = Math.max(maximumProfit, maxProfitBefore + profits[current] + maxProfitAfter);
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       // Return the maximum possible profit, or -1 if not found.
       return maximumProfit;
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37 }
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Time and Space Complexity
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The space complexity of this function is 0(1). This is because the extra space used by the function does not depend on the input size n. Only a fixed number of variables (ans, left, right, n, j, x, i, and k) are used to keep track of the maximum profit as well as

The time complexity of this function maxProfit is $O(n^2)$. This is because there are two nested loops. The outer loop runs n times,

where n is the length of the input lists prices and profits. For each iteration of the outer loop, the inner loops (one for calculating

these inner loops are nested within the outer loop, the total number of operations can be up to n * n, which simplifies to $O(n^2)$.

left and another for calculating right) in total can iterate up to n times in the worst case (when j is at the center of the array). Since

loop counters and values. Therefore, the space used remains constant regardless of the input size.