853. Car Fleet Medium <u>Array</u>

## **Problem Description** The problem presents a scenario where n cars are traveling towards a destination at different speeds and starting from different

speed. Each index i in the arrays corresponds to the ith car, with position[i] representing the initial position of the car and speed[i] being its speed in miles per hour. The key condition is that cars cannot overtake each other. When a faster car catches up to a slower one, it will slow down to form a "car fleet" and they will move together at the slower car's speed. This also applies to multiple cars forming a single fleet if they

**Monotonic Stack** 

Sorting

meet at the same point. Our task is to determine the number of car fleets that will eventually arrive at the destination. A car fleet can consist of just one car, or multiple cars if they have caught up with each other along the way. Even if a car or fleet catches up with another fleet at the destination point, they are counted as one fleet.

ntuition To solve this problem, an intuitive approach is to figure out how long it would take for each car to reach the destination independently and then see which cars would form fleets along the way. By sorting the cars based on their starting positions, we

can iterate from the one closest to the destination to the one furthest from it. This allows us to determine which cars will catch up

positions on a single-lane road. The destination is target miles away. We are provided with two arrays of integers: position and

## As we iterate backwards, we calculate the time t it takes for each car to reach the destination:

to each other.

t = (target - position[i]) / speed[i] We compare this time with the time of the previously considered car (starting from the closest to the target). If t is greater than the pre (previous car's time), this means that the current car will not catch up to the car(s) ahead (or has formed a new fleet) before reaching the destination, and thus we increment our fleet count ans. The current car's time then becomes the new pre.

This process is repeated until we have considered all cars. The total number of fleets (ans) is the answer we are looking for. This

method ensures that we count all fleets correctly, regardless of how many cars they start with or how many they pick up along

the way.

Solution Approach The solution is implemented in Python and is composed of the following steps:

Sort Car Indices by Position: A list of indices is created from 0 to n-1, which is then sorted according to the starting positions of the cars. This sorting step uses the lambda function as the key for the sorted function to sort the indices based

on their associated values in the position array. The resulting idx list will help us traverse the cars in order of their starting positions from closest to furthest relative to the destination. idx = sorted(range(len(position)), key=lambda i: position[i])

Initialize Variables: Two variables are used, ans to count the number of car fleets, and pre to store the time taken by the

ans = pre = 0

for i in idx[::-1]:

speed (speed[i]).

the fleet count ans by 1.

t = (target - position[i]) / speed[i]

complexity is O(n) for storing the sorted indices.

Reverse Iterate through Sorted Indices: By iterating over the sorted indices in reverse order, the algorithm evaluates each car starting with the one closest to the destination.

previously processed car (or fleet) to reach the destination.

if t > pre: ans += 1 pre = t

The current time t is now the new pre because it will serve as the comparison time for the next car in the iteration.

Return Fleet Count: After all the iterations, the variable ans holds the total number of car fleets, and its value is returned.

The primary data structure used here is a list for indexing the cars. The sorting pattern is essential to correctly pair cars that will

become fleets, and the reverse iteration allows the algorithm to efficiently compare only the necessary cars. The time complexity

of the algorithm is dominated by the sorting step, making the overall time complexity 0(n log n) due to the sort, and the space

Calculate Time to Reach Destination: For each car, the time to reach the destination is calculated using the formula:

This formula calculates the time by taking the distance to the destination (target - position[i]) and dividing it by the car's

Evaluate Fleets: If the calculated time t is greater than the time of the last car (or fleet) pre, it implies that the current car

will not catch up to any car ahead of it before reaching the destination. Hence, we have found a new fleet, and we increment

Let's apply the solution approach to a small example to better understand how it works. Imagine we have 4 cars with positions and speeds given by the following arrays:

position: [10, 8, 0, 5] • speed: [2, 4, 1, 3] target: 12 miles away First, let's visualize the initial state of the cars and the target:

## 1. Sort Car Indices by Position: After sorting the indices by the starting positions in descending order, we have the new order of car indexes as idx = [0, 1, 3, 2]. Now the cars are sorted by proximity to the destination:

Target (12 miles)

Car 4 (idx = 3)

Car 3 (idx = 2)

 $\circ$  t = (12 - 0) / 1 = 12

 $\circ$  t = (12 - 5) / 3  $\approx$  2.33

For i = 3 (Car 4):

For i = 1 (Car 2):

For i = 0 (Car 1):

 $\circ$  t = (12 - 8) / 4 = 1

 $\circ$  t = (12 - 10) / 2 = 1

Solution Implementation

fleet count = 0

previous\_time = 0

// Number of cars

indices[i] = i;

// Count of car fleets

double previousTime = 0;

int fleetCount = 0;

int carCount = positions.length;

// Array to hold the indices of the cars

for (int i = 0; i < carCount; ++i) {</pre>

Integer[] indices = new Integer[carCount];

// Iterate through the sorted indices array

#include <algorithm> // For sort and iota functions

#include <vector> // For using vectors

for (int idx : indices) {

class Solution:

Java

C++

public:

class Solution {

});

class Solution {

Since t > pre, we have ans = 1 and pre = 12.

Since t < pre, we do not increment ans, and pre remains 12.</li>

Since t < pre, we do not increment ans, and pre remains 12.</li>

Since t < pre, we do not increment ans, and pre remains 12.</li>

way to the target. Hence, there will be 1 car fleet by the time they reach the destination.

def carFleet(self, target: int, position: List[int], speed: List[int]) -> int:

Start

Start

Target (12 miles)

Car 1 (10 miles, 2 mph)

Car 2 (8 miles, 4 mph)

Car 4 (5 miles, 3 mph)

Car 3 (0 miles, 1 mph)

Following the solution approach:

return ans

Example Walkthrough

Car 1 (idx = 0) Car 2 (idx = 1)

**Initialize Variables**: ans = 0, pre = 0 Reverse Iterate through Sorted Indices: We iterate in reverse through idx as [2, 3, 1, 0]. For i = 2 (Car 3):

**Return Fleet Count**: We have  $\frac{1}{2}$  and  $\frac{1}{2}$  indicating that all the cars will form one fleet by the time they reach the destination.

In summary, even though the cars started at different positions and had different speeds, they caught up with each other on the

**Python** from typing import List

previous\_time = time\_to\_reach\_target # Update the time of the last fleet # Return the total number of fleets return fleet\_count

# Pair each car's position with its index and sort the pairs in ascending order of positions

car\_indices\_sorted\_by\_position = sorted(range(len(position)), key=lambda idx: position[idx])

# Initialize the count of car fleets and the time of the previously counted fleet

# Iterate over the cars from the one closest to the target to the furthest

# Calculate the time needed for the current car to reach the target

# If this time is greater than the time of the previously counted fleet,

# it means this car cannot catch up with that fleet and forms a new fleet.

for i in car indices sorted by position[::-1]: # Reverse iteration

// Function to count the number of car fleets that will arrive at the target

// Sort the indices based on the positions of the cars in descending order

time to reach target = (target - position[i]) / speed[i]

if time to reach target > previous time:

fleet count += 1 # Increment fleet count

public int carFleet(int target, int[] positions, int[] speeds) {

// Populate the indices array with the array indices

Arrays.sort(indices, (a, b) -> positions[b] - positions[a]);

// The time taken by the previous car to reach the target

int carFleet(int target, vector<int>& positions, vector<int>& speeds) {

vector<int> indices(numCars); // Initialize a vector to store indices

// Sort cars by their position in descending order, so the farthest is first

double lastFleetTime = 0; // Time taken by the last fleet to reach the target

// it becomes a new fleet as it cannot catch up to the one in front

function carFleet(targetDistance: number, positions: number[], speeds: number[]): number {

const sortedIndices = Array.from({ length: numCars }, ( , index) => index)

// Calculate time required for the current car to reach the target.

def carFleet(self, target: int, position: List[int], speed: List[int]) -> int:

const currentTimeToTarget = (targetDistance - positions[index]) / speeds[index];

// If the current car takes longer to reach the target than the previous car (or fleet),

# Pair each car's position with its index and sort the pairs in ascending order of positions

car\_indices\_sorted\_by\_position = sorted(range(len(position)), key=lambda idx: position[idx])

# Initialize the count of car fleets and the time of the previously counted fleet

# Iterate over the cars from the one closest to the target to the furthest

# Calculate the time needed for the current car to reach the target

# If this time is greater than the time of the previously counted fleet,

# it means this car cannot catch up with that fleet and forms a new fleet.

previous\_time = time\_to\_reach\_target # Update the time of the last fleet

caught up by another. The time complexity and space complexity of the code are analyzed below.

for i in car indices sorted by position[::-1]: # Reverse iteration

time to reach target = (target - position[i]) / speed[i]

fleet count += 1 # Increment fleet count

// If the current car's time to target is greater than the last fleet's time,

iota(indices.begin(), indices.end(), 0); // Filling the indices vector with 0, 1, ..., numCars - 1

double timeToTarget = 1.0 \* (target - positions[idx]) / speeds[idx]; // Calculate the time to target

lastFleetTime = timeToTarget; // And update the last fleet's time to this car's time

// Create an array of indices corresponding to cars, sorted in descending order of their starting positions.

previousTimeToTarget = currentTimeToTarget; // Update the time to match the new fleet's time.

.sort((indexA, indexB) => positions[indexB] - positions[indexA]);

int numCars = positions.size(); // Number of cars

return positions[i] > positions[j];

if (timeToTarget > lastFleetTime) {

const numCars = positions.length; // Number of cars.

// it cannot catch up and forms a new fleet.

if (currentTimeToTarget > previousTimeToTarget) {

fleetCount++; // Increment the fleet counter.

return fleetCount; // Return the total number of car fleets.

for (const index of sortedIndices) {

from typing import List

fleet count = 0

previous\_time = 0

return fleet\_count

**Time Complexity** 

**Space Complexity** 

length of the positions list.

• Time Complexity: O(N log N)

Space Complexity: 0(N)

class Solution:

return fleetCount; // Return total number of fleets

sort(indices.begin(), indices.end(), [&](int i, int j) {

int fleetCount = 0; // Initializing count of car fleets

// Iterate over the sorted cars by their initial position

fleetCount++; // Increment the number of fleets

for (int index : indices) { // Calculate the time taken for the current car to reach the target double timeToReach = 1.0 \* (target - positions[index]) / speeds[index]; // If the time taken is greater than the previous time, it forms a new fleet if (timeToReach > previousTime) { fleetCount++; previousTime = timeToReach; // Update the previous time // If the time is less or equal, it joins the fleet of the previous car // Return the total number of fleets return fleetCount;

let fleetCount = 0: // Counter for the number of car fleets. let previousTimeToTarget = 0; // Time taken for the previous car (or fleet) to reach the target. // Loop through the sorted car indices.

**}**;

**TypeScript** 

Time and Space Complexity The given Python code is to calculate the number of car fleets that will reach the target destination without any fleet getting

# Return the total number of fleets

if time to reach target > previous time:

• The for loop iterates over the list of positions in reverse: This has a time complexity of O(N) as it goes through each car once. • Therefore, the overall time complexity of the function is dominated by the sorting operation and is O(N log N).

The space complexity of the code can be analyzed as follows:

The time complexity of the code can be analyzed as follows:

 Variables ans and pre use constant space: 0(1). • Space taken by sorting depends on the implementation, but for most sorting algorithms such as Timsort (used in Python's sort method), it

• Sorting the list of positions: This is done by using the sort() method, which typically has a time complexity of O(N log N), where N is the

- requires O(N) space in the worst case. Therefore, the overall space complexity of the function is O(N).

• Additional space is required for the sorted indices array idx, which will be of size O(N).

Combining the time and space complexities, we get the following results: