2541. Minimum Operations to Make Array Equal II

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Medium Greedy Array Math
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Problem Description

which we can use in a specific operation that we can perform on nums1 as many times as needed. An operation consists of picking two indices, i and j, in nums1 and adding k to the value at index i while subtracting k from the value at index j. Our goal is to make the elements of nums1 match the corresponding elements in nums2 using the least number of these operations. If it is impossible to make the arrays equal, we must return -1. To understand whether it's possible to make nums1 equal to nums2, we should consider that each operation effectively transfers k units of value from one element of nums1 to another. Therefore, if the difference between any pair of corresponding elements

In this problem, we are working with two integer arrays, nums1 and nums2, both of the same length n. We're given an integer k

in nums1 and nums2 is not a multiple of k, we cannot make the elements equal through the allowed operation, and we should return -1. If all differences are multiples of k, we can then calculate the minimal number of operations required by summing the absolute values of the quotients of differences by k. ntuition

The intuition behind the solution is to first iterate over each corresponding pair of elements between nums1 and nums2. We

calculate the difference between the elements of nums1 and nums2. If k is zero, we immediately know that unless all elements are already equal, it's impossible to make them equal as no operation can modify nums1. If k is nonzero, any difference that isn't

If a difference is a multiple of k, this multiple represents how many operations of magnitude k are needed to equalize this pair of elements. We accumulate this count in an ans variable. Additionally, we keep track of the net effect of all operations in a variable x. This is because each operation has two parts: incrementing one element and decrementing another. So, if x is nonzero after considering all pairs, it means we've either

a multiple of k would make it impossible for the two corresponding elements to ever match, so we return -1.

incremented or decremented too much and can't balance this out with further operations. If x equals zero, it means that for every increment there is a corresponding decrement, and nums1 can be made equal to nums2.

However, since every operation affects two elements (increments one and decrements another), the total number of operations required is half the sum of absolute values of all quoted differences, as each operation is counted twice in ans. Hence, we return ans // 2, but only if x equals zero, which ensures that all increments and decrements are paired. **Solution Approach**

The solution follows a straightforward approach where it iterates through the two lists simultaneously using the built-in zip function. For each pair of elements (a, b) from nums1 and nums2 respectively, it performs several checks and calculations. Here's a step-by-step breakdown of the implementation:

• Initialize ans and x to 0. ans will hold the total number of operations required, while x will track the net effect of all those operations.

○ Check if k is 0. If it is and a != b, return -1 immediately because no operations can be performed to change the values. ○ Calculate the difference a - b and check if it is a multiple of k. This is done by checking if (a - b) % k equals 0. If it does not, return -1

• For each pair (a, b):

○ Otherwise, compute the quotient y = (a - b) // k, which represents how many operations of magnitude k are needed to equalize a and b. We need to consider the absolute value of y to add to ans because operations can be incrementing or decrementing, and we're counting total operations needed regardless of direction.

 Add y to the net effect tracker x. An increment in one element will be a positive y, and a decrement will be a negative y, so the net effect after all pairs are considered should balance to zero.

Let's go through a small example to illustrate the solution approach.

because it's impossible to make a equal to b through the allowed operation.

• Iterate over nums1 and nums2 in tandem using zip(nums1, nums2).

corresponding decrement. • If x is zero, return ans // 2. Each operation affects two elements of nums1, so every actual operation is counted twice in ans.

This solution approach uses simple mathematical operations and control structures to determine the minimum number of

operations. It leverages the fact that each allowed operation can be represented mathematically as an equation and that the

- After the loop, check if x is nonzero. If it is, return -1 because the net effect hasn't balanced out, implying that not all increments have a
 - collective effect of these operations must balance for equality to be possible.

• nums2 = [5, 1, 3]• k = 2We want to make each element in nums1 match the corresponding element in nums2 using the smallest number of operations. Following the solution approach:

Starting with the first pair (1, 5):

Next, the pair (3, 1):

Finally, the pair (5, 3):

Solution Implementation

num_operations = total_difference = 0

for num1, num2 in zip(nums1, nums2):

difference = (num1 - num2) // k

Update the total difference

total_difference += difference

num operations += abs(difference)

public long minOperations(int[] nums1, int[] nums2, int k) {

// Initialize the answer and the total adjustments needed

// If k is 0, we cannot perform any operation, and if num1 is not equal to num2

// Check if (num1 - num2) is not a multiple of k, return -1 as it's impossible

// Calculate the number of operations needed to make the two numbers equal

// Update the total adjustments which might be positive, negative or zero

continue; // Otherwise, no operation needed for this pair, continue to next pair

// it means it's impossible to make them equal, thus return -1

// to equalize the pair with increments/decrements of k

// Accumulate the absolute value of the operations needed

// If total adjustments sum to zero, the result is totalOperations / 2

// since each operation can be counted twice (once for each array element)

long long totalOperations = 0, totalAdjustments = 0;

// Iterate over both arravs

 $if (k == 0) {$

for (int i = 0; i < nums1.size(); ++i) {</pre>

if (num1 != num2) {

if ((num1 - num2) % k != 0) {

int operationsNeeded = (num1 - num2) / k;

totalOperations += abs(operationsNeeded);

return totalAdjustments == 0 ? totalOperations / 2 : −1;

totalAdjustments += operationsNeeded;

return -1;

return -1;

int num1 = nums1[i], num2 = nums2[i];

if (num1 - num2) % k:

return -1

long totalOperations = 0;

long netChanges = 0;

from typing import List

Python

class Solution:

Example Walkthrough

• nums1 = [1, 3, 5]

Suppose we have the following input:

 The difference 3 − 1 is 2, which is a multiple of k. \circ The quotient y is 2 // 2 = 1. We add the absolute value |y| = 1 to ans, so now ans = 3.

Since x is 0, all increments have matching decrements. We can therefore equalize nums1 to nums2.

to nums2. The steps as outlined in the solution approach guide us through a process of calculating the necessary number of

Our answer is $\frac{1}{2} = \frac{4}{2} = \frac{2}{2}$. Hence, the minimum number of operations required is 2.

 \circ The quotient y is -4 // 2 = -2. We take the absolute value |y| = 2 and add it to ans, so now ans = 2.

Initialize ans and x to 0. These will track the number of operations and the net effect, respectively.

 \circ The quotient y is 2 // 2 = 1. We add the absolute value |y| = 1 to ans, now ans = 4. \circ We add y to x, and as x was previously -1 and y is 1, the net effect balances out, x = 0.

Iterate over the pairs (1, 5), (3, 1), and (5, 3) from nums1 and nums2.

 \circ The difference 1 - 5 is -4, which is a multiple of k (2).

 \circ We add y (which is -2) to x to track the net effect, now x = -2.

 \circ We add y (which is 1) to x, making the net effect now x = -1.

The difference 5 − 3 is 2, which is also a multiple of k.

This example clearly demonstrated that we need to perform two operations of magnitude k (2 in this case) to make nums1 equal

def minOperations(self, nums1: List[int], nums2: List[int], k: int) -> int:

Calculate how many times we need to add or subtract k

Iterate over pairs of elements from nums1 and nums2

Initialize the number of operations required and the difference accumulator

If the difference between num1 and num2 is not divisible by k, return -1

Increment the number of operations by the absolute value of difference

Using the // 2 because each pair's operations partially cancel each other out

// 'totalOperations' will store the total number of operations performed

// 'netChanges' will accumulate the net changes made to the nums1 array elements

If the total difference is not zero, return -1 since it is not possible to equalize

// This method calculates the minimum number of operations needed to make elements in two arrays equal

// where each operation consists of adding or subtracting a number 'k' from an element in nums1 array.

operations or determining the impossibility of equalizing the two arrays.

If k is 0, no operations can make a difference, we need to check if arrays are same if k == 0: **if** num1 != num2: return -1 # Arrays differ and we cannot perform operations continue # Arrays are same up to now, continue checking

return -1 if total_difference else num_operations // 2 Java

class Solution {

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// Iterate over elements of both arrays
        for (int i = 0; i < nums1.length; ++i) {
            int num1 = nums1[i]; // Element from the nums1 array
            int num2 = nums2[i]; // Corresponding element from the nums2 array
            // If 'k' is zero, it's impossible to perform operations, so we check if elements are already equal
            if (k == 0) {
                if (num1 != num2) {
                    return -1; // If any pair of elements is not equal, return -1 to indicate no solution
                continue; // Skip to the next pair of elements since no operation is needed
            // Check if the difference between num1 and num2 is divisible by 'k'
            if ((num1 - num2) % k != 0) {
                return -1; // If it's not, the operation cannot be performed so return -1
            // Calculate the number of operations needed for the current pair of elements
            int operationsNeeded = (num1 - num2) / k;
            // Increment 'totalOperations' by the absolute number of operations needed
            totalOperations += Math.abs(operationsNeeded);
            // Update 'netChanges' by adding operations needed (this could be negative or positive)
            netChanges += operationsNeeded;
        // If the net effect of all operations is zero, we can pair operations to cancel each other out
        // Therefore, we return half of 'totalOperations', since each operation can be paired with its inverse
        return netChanges == 0? totalOperations / 2 : -1; // If 'netChanges' is not zero, a solution is not possible
C++
#include <vector>
#include <cstdlib> // For abs()
using std::vector;
class Solution {
public:
    // Function to calculate the minimum operations to make each corresponding
    // pair of elements in nums1 and nums2 equal using increments or decrements by k
    long long minOperations(vector<int>& nums1, vector<int>& nums2, int k) {
```

};

```
TypeScript
// Function to find the minimum number of operations required to make both arrays equal
// by only incrementing or decrementing elements by a value of 'k'.
// Returns the minimum number of operations needed, or -1 if it's not possible.
function minOperations(nums1: number[], nums2: number[], incrementStep: number): number {
    // Number of elements in the first array
    const arrayLength = nums1.length;
    // If incrementStep is zero, check if arrays are already equal
    if (incrementStep === 0) {
        return nums1.every((value, index) => value === nums2[index]) ? 0 : -1;
    // Initial sum of differences and the total adjustments needed
    let sumDifferences = 0:
    let totalAdjustments = 0;
    // Loop through each element to sum the differences and total adjustments needed
    for (let i = 0; i < arrayLength; i++) {
        // Calculate the difference between the corresponding elements
        const difference = nums1[i] - nums2[i];
        // Accumulate the sum of differences
        sumDifferences += difference;
        // If the difference is not divisible by incrementStep, it's not possible to make arrays equal
        if (difference % incrementStep !== 0) {
            return -1;
        // Sum the absolute value of the difference to calculate total adjustment steps needed
        totalAdjustments += Math.abs(difference);
    // If the sum of differences is not zero, arrays cannot be made equal
    if (sumDifferences !== 0) {
        return -1;
    // Return the number of operations calculated by the total adjustments
    // divided by the step size multiplied by two (since each operation changes
    // the difference by incrementStep * 2)
    return totalAdjustments / (incrementStep * 2);
from typing import List
class Solution:
    def minOperations(self, nums1: List[int], nums2: List[int], k: int) -> int:
        # Initialize the number of operations required and the difference accumulator
        num_operations = total_difference = 0
        # Iterate over pairs of elements from nums1 and nums2
        for num1, num2 in zip(nums1, nums2):
            # If k is 0, no operations can make a difference, we need to check if arrays are same
            if k == 0:
               if num1 != num2:
                    return -1 # Arrays differ and we cannot perform operations
                continue # Arrays are same up to now, continue checking
```

Time and Space Complexity

if (num1 - num2) % k:

difference = (num1 - num2) // k

num operations += abs(difference)

Update the total difference

total_difference += difference

return -1

The time complexity of the given code is O(N) where N is the length of the shorter of the two input lists, nums1 and nums2. This is because the code iterates over each pair of elements from nums1 and nums2 once by using zip, and the operations within the loop (such as modulo, division, comparison, and addition) are all 0(1) operations. No nested loops or recursive calls that would increase the complexity are present.

If the difference between num1 and num2 is not divisible by k, return -1

Increment the number of operations by the absolute value of difference

Using the // 2 because each pair's operations partially cancel each other out

If the total difference is not zero, return -1 since it is not possible to equalize

Calculate how many times we need to add or subtract k

return -1 if total_difference else num_operations // 2

The space complexity of the code is 0(1) since the space used does not increase with the size of the input; it only uses a fixed number of variables (ans, x, a, b, y) to process the input and produce the output.