1981. Minimize the Difference Between Target and Chosen Elements

Matrix

Problem Description

Dynamic Programming

Medium Array

exactly one number from each row of the matrix such that the sum of these numbers is as close as possible to the target. We need to minimize the absolute difference between this sum and the target. Absolute difference means we consider the positive distance between two numbers, regardless of their order. The output should be this minimum absolute difference.

Leetcode Link

To solve this problem efficiently, we need to keep track of all possible sums that can be generated by choosing one number from each row up to the current row being processed. Here, dynamic programming comes into play. We start with an initial set that contains only one element, 0, representing the sum before any numbers have been chosen. For each row in the matrix, we update

This way, by the time we finish the last row, our set contains all possible sums that could be generated by picking one number from each row. After this, to find the minimum absolute difference, we simply iterate over these possible sums and calculate the absolute difference between each of them and the target. The smallest absolute difference found during this process is the result we're looking for.

Although this approach seems to have a high computational complexity due to generating all possible sums, in practice, we can

optimize this by trimming the set of sums to only include relevant sums that could lead to a result close to the target. This is not

Solution Approach The solution uses a straightforward dynamic programming approach. Let's walk through the algorithms, data structures, or patterns

so far, starting with no numbers having been chosen. 1 $f = \{0\}$

1 for row in mat:

used in the provided solution code:

2. Iteration Over Rows: The outer loop goes through each row of the matrix:

1. Initialization of a Set: The variable f is initialized as a set with one element, 0. This set represents all possible sums we've seen

- 3. Generating New Sums: Inside the loop, for each row, we generate new sums by adding every element in the current row to each of the sums in f. This is done using a set comprehension:

so far.

Here, for every sum a existing in f and for each element b in the current row, we add a + b to the new set. This set

absolute difference. This is achieved by iterating over each value v in the final set f:

1 f = set(a + b for a in f for b in row)

but it provides a correct and easily understandable solution.

1. Initialization of a Set: We initialize our set f with a single element 0.

shown in the given code, but it is a useful optimization for very large matrices.

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comprehension is executed for each row, effectively updating f with all possible sums after choosing an element from each row
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1 return min(abs(v - target) for v in f) We calculate the absolute difference abs(v - target) and use the min function to find the smallest difference, which is our desired result.

The solution effectively leverages Python's set datatype to avoid duplicate sums, ensuring that only unique sums are generated and

subsequently considered when calculating the minimum absolute difference from the target. This approach, due to the nature of the

problem, may not be the most efficient in terms of time or space complexity especially if there are many large numbers in the rows,

4. Finding Minimum Absolute Difference: After processing all rows, the final set f encompasses all possible sums that could be

made by picking one number from each row. The task now is to find the sum that is closest to the target, thus minimizing the

Example Walkthrough Let's consider a small example to illustrate the solution approach. Assume we have the following matrix mat with m = 3 rows and n = 3 columns, and our target integer is target = 7.

1 $f = \{0\}$

New sums will be:

New sums will be:

So, f now becomes {1, 2, 3}.

 \circ 3 + 4 = 7, 3 + 5 = 8, 3 + 6 = 9

 \circ 5 + 7 = 12, 5 + 8 = 13, 5 + 9 = 14

 \circ 6 + 7 = 13, 6 + 8 = 14, 6 + 9 = 15

 \circ 7 + 7 = 14, 7 + 8 = 15, 7 + 9 = 16

o and so on for sums 8 and 9...

possible_sums = {0}

for row in mat:

 \circ 0 + 1 = 1

Following the steps of the solution approach:

2. Iteration Over Rows - Row 1: The first row is [1, 2, 3]. We add each number in this row to all elements in set f.

3. Iteration Over Rows - Row 2: The second row is [4, 5, 6]. Now, we add each number in this row to each sum in the current set

4. Iteration Over Rows - Row 3: The third row is [7, 8, 9]. Again, add each number in this row to each sum in the current set f.

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0 + 2 = 2
0 + 3 = 3
```

f.

1 mat = [

[1, 2, 3],

[4, 5, 6],

[7, 8, 9]

○ 1 + 4 = 5, 1 + 5 = 6, 1 + 6 = 7 \circ 2 + 4 = 6, 2 + 5 = 7, 2 + 6 = 8

Calculating the new sums, we get a multitude of values, but we're only interested in the unique ones:

can be seen to be 0, which occurs for sum 7 (which is directly in our set after adding the first two rows).

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The resulting set f now consists of {12, 13, 14, 15, 16, ...} along with other sums from the additions involving 8 and 9 from
  the third row.
5. Finding Minimum Absolute Difference: Now we have a set of all possible sums. We must find the one which is closest to our
  target of 7.
  The absolute differences between each sum v in set f and the target are calculated as abs (v - 7). The minimum difference here
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Initialize a set containing just the element 0

public int minimizeTheDifference(int[][] mat, int target) {

boolean[] possibleSums = {true};

if (possibleSums[sumIndex]) {

// Return the minimum difference found.

return minimumDifference;

vector<int> possibleSums = {1};

for (int element : row) {

for (auto& row : mat) {

// Iterate over each row in the matrix.

Iterate over each row in the matrix

This set will hold all possible sums up till the current row

Use a set comprehension to generate all possible sums

After adding these amounts, f now becomes {5, 6, 7, 8, 9}.

Python Solution class Solution: def minimizeTheDifference(self, mat: List[List[int]], target: int) -> int:

This is done by iterating over all possible sums and computing the absolute difference with the target min_difference = min(abs(sum_val - target) for sum_val in possible_sums) # Return the minimum difference found return min_difference

by adding each element in the current row to all possible sums calculated in the previous step

This ensures we only consider sums that include exactly one element from each row

possible_sums = {elem + row_elem for elem in possible_sums for row_elem in row}

Find the minimum absolute difference between any possible sum and the target

// Initialize an array to keep track of possible sums using the first row.

// Find the smallest difference between any possible sum and the target.

minimumDifference = Math.min(minimumDifference, Math.abs(sumIndex - target));

// Function to find the minimum absolute difference between the sum of elements from each row and the target value.

// Find the maximum element in the current row to determine the new size of 'nextPossibleSums'.

// Compute the next state of possible sums by adding each element of the current row to the 'possibleSums'.

// Initialize a vector 'possibleSums' representing possible sums with just one element set to 1 (meaning sum 0 is possible).

for (int sumIndex = 0; sumIndex < possibleSums.length; ++sumIndex) {</pre>

int minimizeTheDifference(vector<vector<int>>& mat, int target) {

int maxElementInRow = *max_element(row.begin(), row.end());

vector<int> nextPossibleSums(possibleSums.size() + maxElementInRow);

nextPossibleSums[j] |= possibleSums[j - element];

for (int j = element; j < possibleSums.size() + element; ++j) {</pre>

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The closest sum to the target is the sum itself when it is present in the set. So, the solution returns 0, as this is the smallest
absolute difference we can achieve.
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Java Solution

class Solution {

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// Loop over each row in the matrix.
           for (int[] row : mat) {
               // Variable to keep track of the maximum element in the current row.
               int maxElement = 0;
                for (int element : row) {
                   maxElement = Math.max(maxElement, element);
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               // Extend the possible sums array to accommodate the new maximum element.
14
                boolean[] newPossibleSums = new boolean[possibleSums.length + maxElement];
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               // Update new possible sums by adding each element in the current row
               // to the sums calculated so far.
18
                for (int element : row) {
19
                    for (int sumIndex = element; sumIndex < possibleSums.length + element; ++sumIndex) {</pre>
20
                        newPossibleSums[sumIndex] |= possibleSums[sumIndex - element];
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               // Move to the next set of possible sums.
26
                possibleSums = newPossibleSums;
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           // Initialize the answer to a large number (infinity equivalent).
30
           int minimumDifference = Integer.MAX_VALUE;
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18 19 // Move 'nextPossibleSums' to 'possibleSums' to use in the next iteration. 20 21 possibleSums = move(nextPossibleSums); 22 23

C++ Solution

1 class Solution {

2 public:

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           // Initialize 'minDifference' to a large number to find the minimum difference.
            int minDifference = 1 << 30; // Equivalent to a large number using bit left shift.</pre>
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26
27
           // Iterate over all possible sums to calculate the smallest difference to 'target'.
28
            for (int sum = 0; sum < possibleSums.size(); ++sum) {</pre>
29
                if (possibleSums[sum]) {
                    minDifference = min(minDifference, abs(sum - target));
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           // Return the minimum absolute difference found.
35
           return minDifference;
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37 };
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Typescript Solution
 1 // Function to find the minimum element in an array using the reduce method.
   function maxElement(array: number[]): number {
        return array.reduce((max, currentValue) => Math.max(max, currentValue));
 4
   // Function to find the minimum absolute difference between the sum of elements from each row and the target value.
    function minimizeTheDifference(mat: number[][], target: number): number {
       // Initialize an array 'possibleSums' representing possible sums with just zero sum possible initially.
 8
       let possibleSums: number[] = [1];
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       // Iterate over each row in the matrix.
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       mat.forEach(row => {
           // Find the maximum element in the current row to determine the new size of 'nextPossibleSums'.
13
            const maxElementInRow = maxElement(row);
14
            const nextPossibleSums: number[] = new Array(possibleSums.length + maxElementInRow).fill(0);
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           // Compute the next state of possible sums by adding each element of the current row to the 'possibleSums'.
17
            row.forEach(element => {
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                for (let j = element; j < possibleSums.length + element; ++j) {</pre>
19
                    if (possibleSums[j - element]) {
20
                        nextPossibleSums[j] = 1;
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           });
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26 // Update 'possibleSums' with newly computed 'nextPossibleSums'. possibleSums = nextPossibleSums; 27 }); 28 29 30 // Initialize 'minDifference' with a large number to ensure it is higher than any possible sum. 31 let minDifference = Infinity; 32 // Iterate over all possible sums to calculate the smallest difference to the 'target'. 33 possibleSums.forEach((value, sum) => { 34 if (value) { 35 36 minDifference = Math.min(minDifference, Math.abs(sum - target)); 37 38 }); 39 40 // Return the minimum absolute difference found. return minDifference; 41 42 } 43

a factor of up to m with each iteration (each new row of mat). Therefore, in the worst case, the time complexity is 0(m^n). However, since each element of f represents a unique sum and m can be large, this is still a considerable amount of computation. The space complexity is influenced by the size of the set f. At any given point, f holds all unique sums that can be formed with the current rows of mat being processed. In the worst case, f can grow to O(m^n) unique sums. Therefore, the space complexity is also

The time complexity of the given code can be understood by analyzing the nested loops and the set comprehension. In the worst-

case scenario, the set f contains all possible sums that can be formed by adding the elements from each previous row of mat to the

existing sums in f. If the maximum number of elements a row can contribute to the set is m, and there are n rows, the set can grow by

Time Complexity: 0(m^n)

 $O(m^n)$.

To sum up:

Space Complexity: 0(m^n)

Time and Space Complexity

- this set by adding each element of the current row to each of the sums we have accumulated so far.
- In this problem, we are given a matrix mat which has m rows and n columns, and a target integer called target. Our goal is to choose Intuition