552. Student Attendance Record II

# **Problem Description**

**Dynamic Programming** 

The problem asks us to determine the number of possible attendance records of length n that allows a student to be eligible for an attendance award. A record is represented by a string consisting of the characters 'A' for absent, 'L' for late, and 'P' for present.

1. They are absent for fewer than 2 days in total. 2. They are not late for 3 or more consecutive days.

A student qualifies for an award if they satisfy two conditions:

- We must return the count of such attendance records modulo 10^9 + 7, as this number could be very large.

Intuition

• They can be absent (A), which increases the count of absences unless they have already been absent once.

### To arrive at the solution, we can use <u>Dynamic Programming</u> (DP). Since we need to keep track of absent and late counts, we can use a 3-dimensional DP array, where dp[i][j][k] represents the number of permutations of attendance records ending at day 'i',

Hard

late days (0, 1, or 2). Thinking through the possible cases: • The student can be present (P) on any given day, which doesn't affect their absences or increase the count of consecutive late days. • They can be late (L), which resets the consecutive present day count but has to be carefully added so as not to surpass two consecutive late days.

with 'j' representing whether the student has been absent 0 or 1 times, and 'k' representing the count of the latest consecutive

The base case for the first day (i = 0) needs to be initialized to show that they can be present, late, or absent, but still be eligible for the award. By iterating through the days and for each day computing the possible ending in 'P', 'L', or 'A', while adhering to the rules, we can incrementally construct our DP table up to day 'n'.

Finally, the sum of all possible records up to day 'n - 1' considering both absentee scenarios, and not exceeding two consecutive 'L's gives us the total count modulo 10^9 + 7.

The solution uses a dynamic programming approach to keep track of eligible attendance records by constructing a 3D DP array dp with dimensions n, 2, and 3; where n is the number of days, 2 represents being absent for either 0 or 1 day (j index), and 3 represents the number of consecutive late days (k index).

**Initialization**: The index [i][j][k] in dp corresponds to the day i, absent status j, and consecutive late status k.

#### ○ Day i = 0: Initialize dp[0][0][0], dp[0][0][1], and dp[0][1][0] to 1. This covers the cases where the student is present, late, or absent for the first day.

**Solution Approach** 

For a Present (P) day: Update dp[i][0][0] and dp[i][1][0] to include all records from previous days where the student was present, late, or absent, ensuring that they are still eligible.

For a Late (L) day: The late status k is incremented by 1, but cannot exceed 2, which represents being late for 3 or more

For an Absent (A) day: Only include records from the previous day where the student hasn't been absent before (j=0).

want to consider all possible eligible sequences. This sum gives the total number of attendance records of length n that allow

consecutive days. Set dp[i][0][1] to dp[i - 1][0][0], dp[i][0][2] to dp[i - 1][0][1], dp[i][1][1][1] to dp[i - 1][1][0], and dp[i][1][2] to dp[i - 1][1][1].

Here are the detailed steps of the algorithm:

Filling the DP table: Iterate over days i from 1 to n - 1:

a student to be eligible for an attendance award, modulo 10^9 + 7.

must be returned modulo  $10^9 + 7$  to fit within the integer range.

and dp[0][1][0] = 1 (student was absent).

the student wasn't absent on previous days).

At each step, we take the result modulo 10^9 + 7 to avoid integer overflow due to large values. Computing the answer: Sum up all the elements dp[n - 1][j][k], where j can be 0 or 1, and k can be 0, 1, or 2, since we

Set dp[i][1][0] by summing up dp[i - 1][0][0], dp[i - 1][0][1], and <math>dp[i - 1][0][2].

Let's walk through an example using the provided solution approach to calculate the number of valid attendance records for n = 3.

Throughout the implementation, we're using the modulo operation due to the constraints that the answer may be very large and

Filling the DP table: For day i = 1, we have:

P on the first day and A on the second, L on the first and P on the second, or A on the first and P on the second).

○ We start with day i = 0 and initialize our dp array such that dp[0][0][0] = 1 (student was present), dp[0][0][1] = 1 (student was late),

• Present (P) case: Since the student can be present after any attendance status of the previous day without restrictions, we set dp[1]

[0][0] = sum(dp[0][0]) = 2 (from being P or L on the first day), and dp[1][1][0] = sum(dp[0][1]) + sum(dp[0][0]) = 3 (from being

■ Late (L) case: The student can only be late for a maximum of two consecutive days, so we update dp[1][0][1] (was P now L) and dp[1]

■ Present (P) case: dp[2][0][0] = sum(dp[1][0]) = 3 (from all P and L scenarios of the previous day where the student wasn't absent),

and dp[2][1][0] = sum(dp[1][1]) + sum(dp[1][0]) = 4 (from all P and L scenarios of the previous day and adding A scenarios where

# [1] [1] (was A now L), dp[1][0][1] = dp[0][0][0] = 1 and dp[1][1][1] = dp[0][1][0] = 1. ■ Absent (A) case: The student can be absent for at most once, so dp[1][1][0] (was P now A) is already covered in Present case, no

**Example Walkthrough** 

**Initialization:** 

update needed for this case. For day i = 2, we repeat the process:

■ Late (L) case: Update the dp array considering the consecutive L scenarios, dp[2][0][1] = dp[1][0][0] = 3 and dp[2][0][2] = dp[1]

+ 3 + 3 + 1 = 14.

Solution Implementation

def checkRecord(self, n: int) -> int:

# 1st dimention is the day,

dp[0][0][1] = 1 # Late

for i in range(1, n):

dp[0][1][0] = 1 # Absent

# Initialize a 3D DP array where:

# Iterate over each day starting from the second one.

# by summing over all possibilities on the last day.

total = (total + dp[n - 1][j][k]) % MOD

return total # Return the total number of valid combinations.

// where j tracks the absence count (0 for no A, 1 for one A)

vector<vector<vector<ll>>>> dp(n, vector<vector<ll>>>(2, vector<ll>(3)));

// For A: append A after sequences that do not contain A ('j' == 0)

// For L: append L after sequences ending in no L or 1 L

dp[i][0][2] = dp[i - 1][0][1]; // 1 L followed by another L

result = (result + dp[n - 1][absence][late]) % MOD;

// A function to check the number of valid sequences of attendance records of length n

// dp[i][j][k] represents the number of valid sequences of length i

// For A: append A after sequences that do not contain A ('j' == 0)

// For L: append L after sequences ending in no L or 1 L

dp[i][0][2] = dp[i - 1][0][1]; // 1 L followed by another L

result = (result + dp[n - 1][absence][late]) % MOD;

dp[i][0][1] = dp[i - 1][0][0]; // No L followed by L

// For sequences that already contain A, append P

dp[i][1][0] = (dp[i-1][0][0] + dp[i-1][0][1] + dp[i-1][0][2]) % MOD;

dp[i][1][1] = dp[i - 1][1][0]; // No L followed by L, already contains A

dp[i][0][0] = (dp[i-1][0][0] + dp[i-1][0][1] + dp[i-1][0][2]) % MOD;

MOD = 10\*\*9 + 7 # Define the modulus for the problem, to prevent overflow.

# 2nd dimention is the absence count (0 or 1, because more than 1 is not allowed),

# If the day ends in 'A' (Absent), the sequence must not have any 'A's before.

# 3rd dimention is the late count (0, 1, or 2, because more than 2 in a row is not allowed).

# Base cases: there is one way to have a sequence end in either 'P', 'L', or 'A' on the first day

dp[i][1][2] = dp[i - 1][1][1]; // 1 L followed by another L, already contains A

// where j tracks the absence count (0 for no A, 1 for one A)

// and k tracks the late count (0, 1, or 2 consecutive L's)

Array.from({ length: 2 }, () => Array(3).fill(0))

// Define 'll' as alias for 'number' type since TypeScript doesn't have 'long long' type

dp[i][0][1] = dp[i - 1][0][0]; // no L followed by L

// for sequences that already contain A, append P

// For P: append P after any sequence

for (int absence = 0; absence < 2; ++absence) {</pre>

for (int late = 0; late < 3; ++late) {</pre>

// MOD constant for modulo operation to prevent overflow

// Create a 3D array to hold the state information

let dp: ll[][][] = Array.from({ length: n }, () =>

dp[i][1][0] = (dp[i-1][0][0] + dp[i-1][0][1] + dp[i-1][0][2]) % MOD;

dp[i][1][1] = dp[i - 1][1][0]; // no L followed by L, already contains A

dp[i][0][0] = (dp[i-1][0][0] + dp[i-1][0][1] + dp[i-1][0][2]) % MOD;

// Calculate the final result by summing up all possible sequences of length 'n'

dp[i][1][2] = dp[i - 1][1][1]; // 1 L followed by another L, already contains A

dp[i][1][0] = (dp[i][1][0] + dp[i - 1][1][0] + dp[i - 1][1][1] + dp[i - 1][1][2]) % MOD;

// and k tracks the late count (0, 1, or 2 consecutive L's)

// base cases for first day

for (int i = 1; i < n; ++i) {

dp[0][0][0] = 1; // P

dp[0][0][1] = 1; // L

dp[0][1][0] = 1; // A

ll result = 0;

return result;

const MOD: number = 1e9 + 7;

type ll = number;

function checkRecord(n: number): number {

// Base cases for the first day

dp[0][0][0] = 1; // P present

dp[0][1][0] = 1; // A absent

for (let i = 1; i < n; ++i) {

dp[0][0][1] = 1; // L late

return result;

class Solution:

**}**;

**TypeScript** 

);

# We can have 0, 1, or 2 'L's (Late) before this 'A'.

dp[i][1][0] = sum(dp[i - 1][0][l] for l in range(3)) % MOD

dp[i][1][2] = dp[i - 1][1][1] # Two 'L's, with an 'A' before

dp[i][0][1] = dp[i-1][0][0] # One possible 'L' before current day

dp[i][0][2] = dp[i - 1][0][1] # Two possible 'L's before current day

dp[i][1][1] = dp[i - 1][1][0] # One 'L', with an 'A' at some point before

**Python** 

class Solution:

- [0][1] = 1; similarly for j=1, dp[2][1][1] = dp[1][1][0] = 3 and dp[2][1][2] = dp[1][1][1] = 1. ■ Absent (A) case: dp[2][1][0] = sum(dp[1][0]) = 3 (from all non-absent previous day records). Computing the answer:
- So, for n = 3, there are 14 valid attendance records that meet the criteria for an awards eligibility, and the final answer modulo  $10^9 + 7$  would be 14 (since 14 is already less than  $10^9 + 7$ ).

After filling in the dp table, we sum up all the possibilities on the last day i = 2 considering both j (absent count) and k (consecutive late

count), resulting in the final count: dp[2][0][0] + dp[2][0][1] + dp[2][0][2] + dp[2][1][0] + dp[2][1][1] + dp[2][1][2] = 3 + 3 + 1

 $dp = [[[0, 0, 0], [0, 0, 0]] for _ in range(n)]$ # Base cases: there is one way to have a sequence end in either 'P', 'L', or 'A' on the first day dp[0][0][0] = 1 # Present

MOD = 10\*\*9 + 7 # Define the modulus for the problem, to prevent overflow.

# 2nd dimention is the absence count (0 or 1, because more than 1 is not allowed),

# If the day ends in 'A' (Absent), the sequence must not have any 'A's before.

# If the day ends in 'L' (Late), the previous day can have 0 or 1 'L' or be 'P' (Present).

# 3rd dimention is the late count (0, 1, or 2, because more than 2 in a row is not allowed).

#### # If the day ends in 'P' (Present), there are no constraints for this particular day. for j in range(2): # j=0: no 'A' yet, j=1: there has been an 'A' dp[i][j][0] = sum(dp[i - 1][j][l] for l in range(3)) % MOD# Calculate the total number of valid attendance record combinations

total = 0

Java

for j in range(2):

for k in range(3):

```
class Solution {
   private static final int MOD = 1000000007;
   public int checkRecord(int n) {
       // dp[i][j][k]: number of valid sequences of length i, with j 'A's and a trailing 'L's of length k.
       long[][][] dp = new long[n][2][3];
       // Base cases
       dp[0][0][0] = 1; // P
       dp[0][0][1] = 1; // L
       dp[0][1][0] = 1; // A
       // Building the DP table for subsequences of length i
       for (int i = 1; i < n; i++) {
           // Adding 'A' to the sequence ending without 'A's and less than 2 'L's
           dp[i][1][0] = (dp[i-1][0][0] + dp[i-1][0][1] + dp[i-1][0][2]) % MOD;
           // Adding 'L' to the sequence, considering previous 'L's and 'A's
           dp[i][0][1] = dp[i - 1][0][0]; // Previous has no trailing 'L'
           dp[i][0][2] = dp[i - 1][0][1]; // Previous has 1 trailing 'L'
           dp[i][1][1] = dp[i - 1][1][0];
                                                       // Previous has an 'A' and no trailing 'L'
           dp[i][1][2] = dp[i - 1][1][1];
                                                        // Previous has an 'A' and 1 trailing 'L'
           // Adding 'P' to the sequence, considering previous 'A's and 'L's
           dp[i][0][0] = (dp[i-1][0][0] + dp[i-1][0][1] + dp[i-1][0][2]) % MOD;
           dp[i][1][0] = (dp[i][1][0] + dp[i - 1][1][0] + dp[i - 1][1][1] + dp[i - 1][1][2]) % MOD;
       // Sum up all valid sequences
        long ans = 0;
       for (int j = 0; j < 2; j++) { // 0 or 1 'A's
           for (int k = 0; k < 3; k++) { // 0 to 2 trailing 'L's
               ans = (ans + dp[n - 1][j][k]) % MOD; // Aggregate counts
       return (int) ans; // Final answer
C++
constexpr int MOD = 1e9 + 7;
class Solution {
public:
   int checkRecord(int n) {
       // Define 'll' as shorthand for 'long long' type
       using ll = long long;
       // Create a 3D vector to hold the state information
       // dp[i][j][k] represents the number of valid sequences of length i
```

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dp[i][1][0] = (dp[i][1][0] + dp[i - 1][1][0] + dp[i - 1][1][1] + dp[i - 1][1][2]) % MOD;
// Calculate the final result by summing up all possible sequences of length 'n'
let result: ll = 0;
for (let absence = 0; absence < 2; ++absence) {</pre>
```

 $dp = [[[0, 0, 0], [0, 0, 0]] for _ in range(n)]$ 

# Iterate over each day starting from the second one.

total = (total + dp[n - 1][j][k]) % MOD

return total # Return the total number of valid combinations.

# We can have 0, 1, or 2 'L's (Late) before this 'A'.

for (let late = 0; late < 3; ++late) {</pre>

def checkRecord(self, n: int) -> int:

# 1st dimention is the day,

dp[0][0][0] = 1 # Present

dp[0][1][0] = 1 # Absent

dp[0][0][1] = 1 # Late

for i in range(1, n):

# Initialize a 3D DP array where:

// For P: append P after any sequence

```
dp[i][1][0] = sum(dp[i - 1][0][l] for l in range(3)) % MOD
   # If the day ends in 'L' (Late), the previous day can have 0 or 1 'L' or be 'P' (Present).
    dp[i][0][1] = dp[i-1][0][0] # One possible 'L' before current day
    dp[i][0][2] = dp[i-1][0][1] # Two possible 'L's before current day
    dp[i][1][1] = dp[i - 1][1][0] # One 'L', with an 'A' at some point before
    dp[i][1][2] = dp[i - 1][1][1] # Two 'L's, with an 'A' before
    # If the day ends in 'P' (Present), there are no constraints for this particular day.
    for j in range(2): \# j=0: no 'A' yet, j=1: there has been an 'A'
        dp[i][j][0] = sum(dp[i - 1][j][l] for l in range(3)) % MOD
# Calculate the total number of valid attendance record combinations
# by summing over all possibilities on the last day.
```

# The algorithm uses a dynamic programming approach to calculate the number of ways a student can attend classes over n days without being absent for consecutive 3 days and without being absent for 2 days in total. The time complexity is determined by the triple-nested loops:

total = 0

**Time Complexity** 

Big O notation.

for j in range(2):

for k in range(3):

Time and Space Complexity

 The outer loop runs n times, which represents each day. • For each day, there are 2 states of absence (either the student has been absent once or not at all), and 3 states for tardiness (the student has not been late, has been late once, or has been late twice).

Hence, the time complexity of the algorithm is 0(2 \* 3 \* n), which simplifies to 0(n) because the constants can be removed in

**Space Complexity** The space complexity is determined by the space required to store the dynamic programming states. The dp array is a two-

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dimensional array where the first dimension is n, and the second dimension is a 2×3 matrix to store all different states for
absences and lates.
```

Therefore, the space complexity is 0(2 \* 3 \* n), which simplifies to 0(n) as the constants can be disregarded.