# **Problem Description**

with a grid of cells, each of which can either be alive (denoted by '1') or dead (indicated by '0'). The game progresses in steps, or generations, with each cell's fate in the next generation determined by its current state and the states of its eight neighboring cells. The challenge is to implement an algorithm that takes an m x n grid representing the current state of a board and produces the next state of the board based on the following rules: 1. Any living cell with fewer than two live neighbors dies, as if by underpopulation.

The "Game of Life" is a fascinating cellular automaton created by mathematician John Horton Conway. In this game, we're presented

2. Any living cell with two or three live neighbors lives on to the next generation.

state must remain unchanged until all cells have been considered.

- 3. Any living cell with more than three live neighbors dies, as if by overpopulation. 4. Any dead cell with exactly three live neighbors becomes a live cell, as if by reproduction.
- The game's rules are applied to every cell in the board simultaneously. This means that when calculating the next state, the original

ntuition

### The solution requires us to update the board to its next state without using additional space to store an intermediate state, which can be tricky because the update of one cell should not affect the update of another cell.

A clever approach to solving this problem within the constraints is to define intermediate states:

Let state -1 represent a cell that was dead but will become alive in the next state.

the cell is currently dead, and the exact value determines if it will remain dead or come to life.

This way, we can encode the current and next state of a cell within the same grid. A positive value indicates the cell is currently alive,

Let state 2 represent a cell that was alive but will die in the next state.

The algorithm proceeds in two passes over the grid: 1. In the first pass, we calculate the next state for each cell without updating the board to the final state. Instead, we use the intermediate states 2 and -1 if a cell's state is going to change. We use the variable live to count the number of living neighbors

and its specific integer value indicates whether it will stay alive or die in the next state. Similarly, a negative or zero value indicates

2. In the second pass, we update cells in state 2 to 0 (dead) and cells in state -1 to 1 (alive), thus applying the transitions and

around each cell considering these transitions.

- achieving the next state of the board. This approach leverages the fact that the state information is stored in-place with clear rules for interpretation, allowing us to determine a cell's original and next state without additional memory usage.
- **Solution Approach**

The solution is implemented in two major steps: firstly detecting changes that will happen in the next state, and secondly applying these changes to realize the next state. This process happens in-place within the original grid to avoid extra space usage, thanks to the in-place marking strategy explained in the intuition part.

## 1. The first part of the solution involves iterating over all cells in the grid to determine their fate according to the Game of Life rules. While doing that, we keep track of the cell's state change using temporary markers.

If a neighbor is marked with a positive value, we know it's currently alive. Since we're also interested in cells that are about to change state from living to dead, we slightly modify the neighbor count logic. We start with the count at -board[i][j], which helps us avoid counting the cell itself if it's alive.

We use an if condition with a range to ensure we stay within the bounds of the grid without wrapping around. For each live

neighbor, we increment the live counter. After counting neighbors, we apply the Game of Life rules:

To determine the fate of each cell, we need to count its living neighbors. We create a nested loop to check all neighboring cells.

marked as 2, signifying it will die. Conversely, a dead cell (indicated by board[i][j] == 0) with exactly three live neighbors (live == 3) is marked as -1, signifying it will become alive.

marked with 2 (if they are to die) or -1 (if they are to become alive). Therefore, in the second part, we make another pass over

2. Once the first pass is complete, all cells on the board will either have their original values (indicating no change) or will be

o If a cell is alive (board[i][j] > 0) but has fewer than two or more than three live neighbors (live < 2 or live > 3), it is

- the grid to finalize the state transitions. ∘ If a cell is marked 2, this means it was alive but is about to die, so we set it to 0. ∘ If a cell is marked -1, it was dead and is about to come to life, so we set it to 1.
- By treating the states 2 and -1 as temporary placeholders, the algorithm can keep track of both the current and future states of each cell without needing additional space for storing the grid's state. This efficient handling of the states demonstrates a common strategy in algorithm design called in-place computation, which is particularly useful for saving memory and often necessary when dealing with constraints such as constant space complexities.
- Let's consider a 3×3 grid to illustrate the solution approach:

We will use the rules provided and apply the first phase of the solution. Let's see how we can determine the next state for each cell. 1. First Pass (Detection Phase): • For the cell at position (0, 0), which is alive (1), it has three live neighbors. According to the rules, a living cell with two or three

at 1 and 0 respectively.

**Python Solution** 

class Solution:

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**Example Walkthrough** 

1 Current state of the grid:

• For the cell at position (0, 2), which is alive (1), it has two live neighbors. This cell continues to live, resulting in no change. • The cell at position (1, 0) is dead (0), and it has two live neighbors. It remains dead, as it doesn't meet the reproduction rule

(exactly three live neighbors required).

live neighbors lives on. Therefore, this cell does not change.

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live neighbors to become alive.
• The cell at position (1, 2) is dead (0), with three live neighbors. According to the rules, a dead cell with three live neighbors
  becomes alive. Therefore, this cell is marked as -1 (an intermediate state showing it will be alive in the next state).
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For the corner cells at positions (2, 0) and (2, 2), both being alive with only one living neighbor, they will die due to underpopulation.

• The cell at position (1, 1) is dead (0) and has four live neighbors. It continues to be dead because it doesn't have exactly three

Thus, these cells are marked as 2. 1 Intermediate state of the grid after the first pass:

• For the cell at position (0, 1), which is alive (1), it has three live neighbors. This cell also lives on, so no change.

2. Second Pass (Update Phase): Now we go through the grid again and apply the second part of the algorithm to update the cells.

• Cells at positions (0, 0), (0, 1), (0, 2), and (1, 0) retain the same state since they weren't assigned any intermediate state, staying

 The cell at position (1, 2) was marked as -1 and is set to 1 to finalize its transition to a live cell. • Cells at positions (2, 0) and (2, 2) were marked as 2 (meaning they should die) and are now set to 0.

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1 Next state of the grid after the second pass:
2 1 1 1
3 0 1 0
4 0 0 0
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• The cell at position (1, 1) remains dead, so no change.

The final state of the grid, representing the next state, is now:

def gameOfLife(self, board: List[List[int]]) -> None:

for x in range(row - 1, row + 2):

for y in range(col - 1, col + 2):

live\_neighbors += 1

Do not return anything, modify 'board' in-place instead.

This example demonstrates how each cell's next state is determined using intermediate states to facilitate in-place updates, maintaining the integrity of the game's rules without additional space.

# Examine all the neighbor cells in the surrounding 3x3 area

# Check if the neighbor is within bounds and is alive

# Apply the rules of the Game of Life for the next state of the cell

if board[row][col] and (live\_neighbors < 2 or live\_neighbors > 3):

board[row][col] = 2 # Mark this cell for death

board[row][col] = -1 # Mark this cell for life

if board[row][col] == 0 and live\_neighbors == 3:

if  $0 \ll x \ll x \ll and 0 \ll y \ll cols and board[x][y] > 0:$ 

14 # Get the dimensions of the board rows, cols = len(board), len(board[0]) 15 16 # Iterate over each cell of the board to compute the next state 17 for row in range(rows): 18

live neighbors = -board[row][col] # Start with the negated cell state to offset the current cell count later

# If the cell is alive and has too few or too many neighbors, it becomes 'dead' for the next state

# If the cell is dead and has exactly 3 live neighbors, it becomes 'alive' for the next state

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This function computes the next state of the Game of Life board.
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           Rules for the Game of Life:
           1. Any live cell with fewer than two live neighbors dies, as if caused by underpopulation.
           2. Any live cell with two or three live neighbors lives on to the next generation.
           3. Any live cell with more than three live neighbors dies, as if by overpopulation.
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           4. Any dead cell with exactly three live neighbors becomes a live cell, as if by reproduction.
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for col in range(cols):

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             # Finalize the next state of the board
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             for row in range(rows):
 37
                 for col in range(cols):
                     # Set the cell state to 'dead' if it was marked for death
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 39
                     if board[row][col] == 2:
 40
                         board[row][col] = 0
                     # Set the cell state to 'alive' if it was marked for life
 41
 42
                     elif board[row][col] == -1:
 43
                         board[row][col] = 1
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Java Solution
     class Solution {
         public void gameOfLife(int[][] board) {
             // numRows and numCols hold the dimensions of the board
             int numRows = board.length;
             int numCols = board[0].length;
             // Traverse through every cell of the board
             for (int row = 0; row < numRows; ++row) {</pre>
  8
                 for (int col = 0; col < numCols; ++col) {</pre>
  9
 10
                     // Count live neighbors, initializing at -board[row][col] to offset self-counting if alive
                     int liveNeighbors = -board[row][col];
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 12
                     for (int i = row - 1; i \le row + 1; ++i) {
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                          for (int j = col - 1; j \le col + 1; ++j) {
 14
                             // Check if neighbor is within bounds and alive
 15
                              if (i \ge 0 && i < numRows && <math>j \ge 0 && j < numCols && board[i][j] > 0) {
 16
                                  liveNeighbors++;
 17
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                     // Apply the Game of Life rules to determine next state:
 22
 23
                     // Rule 1 or Rule 3: Any live cell with fewer than two live neighbors
 24
                     // or with more than three live neighbors dies (set to 2 for temporary state)
 25
                     if (board[row][col] == 1 && (liveNeighbors < 2 || liveNeighbors > 3)) {
 26
                          board[row][col] = 2;
 27
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// Rule 4: Any dead cell with exactly three live neighbors becomes a live cell

// (set to -1 for temporary state)

for (int col = 0; col < numCols; ++col) {</pre>

else if (board[row][col] == -1) {

board[row][col] = -1;

for (int row = 0; row < numRows; ++row) {</pre>

**if** (board[row][col] == 2) {

board[row][col] = 0;

board[row][col] = 1;

if (board[row][col] == 0 && liveNeighbors == 3) {

// Re-traverse the board to rewrite the temporary states to final states

// A value of 2 means the cell was previously alive and now is dead

// A value of -1 means the cell was previously dead and now is alive

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C++ Solution
  1 class Solution {
  2 public:
        // Function that simulates the Game of Life on the given board.
         void gameOfLife(vector<vector<int>>& board) {
             int rows = board.size(); // Number of rows in the board
             int cols = board[0].size(); // Number of columns in the board
             // Iterate over each cell in the board
  8
             for (int i = 0; i < rows; ++i) {
  9
                 for (int j = 0; j < cols; ++j) {
 10
                     int liveNeighbors = -board[i][j]; // Initialize live neighbors count
 11
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                     // Iterate over all the neighbors of the current cell
 14
                     for (int x = i - 1; x \le i + 1; ++x) {
 15
                         for (int y = j - 1; y \le j + 1; ++y) {
 16
                             // Check if the neighbor is within the board boundaries and is alive
 17
                             if (x >= 0 \&\& x < rows \&\& y >= 0 \&\& y < cols \&\& board[x][y] > 0) {
 18
                                 ++liveNeighbors;
 19
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 23
                     // Apply the Game of Life rules for living cells
 24
                     if (board[i][j] == 1 && (liveNeighbors < 2 || liveNeighbors > 3)) {
                         board[i][j] = 2; // Mark for death
 25
 26
 27
                     // Apply the Game of Life rules for dead cells
                     if (board[i][j] == 0 && liveNeighbors == 3) {
 28
 29
                         board[i][j] = -1; // Mark for life
 30
 31
 32
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 34
             // Update the board with the new state
 35
             for (int i = 0; i < rows; ++i) {
                 for (int j = 0; j < cols; ++j) {</pre>
 36
                     // If the cell was marked for death, make it dead
 38
                     if (board[i][j] == 2) {
 39
                         board[i][j] = 0;
                     } else if (board[i][j] == -1) { // If the cell was marked for life, make it alive
 40
 41
                         board[i][j] = 1;
 42
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 44
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 46 };
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Typescript Solution
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\* @param board - The 2D array representing the Game of Life board, where 1 is a live cell and 0 is a dead cell.

// Increment live neighbor count if neighbor is alive

// 1. Any live cell with fewer than two or more than three live neighbors dies

if (board[row][col] === 1 && (liveNeighbors < 2 || liveNeighbors > 3)) {

// 2. Any dead cell with exactly three live neighbors becomes a live cell

board[row][col] = 2; // Mark the cell to become dead

// Initialize live neighbor count; the cell itself is counted and will be subtracted later if alive

### 17 for (let y = col - 1; $y \le col + 1$ ; ++y) { 18 // Check if neighbor coordinates are within the board bounds if $(x >= 0 \&\& x < rows \&\& y >= 0 \&\& y < cols \&\& board[x][y] > 0) {$ 19 20 21 22

\* Apply the Game of Life rules to the board in place.

for (let col = 0; col < cols; ++col) {</pre>

// Iterate over each cell to apply the Game of Life rules

// Check all 8 neighbors of the current cell

for (let x = row - 1;  $x \le row + 1$ ; ++x) {

++liveNeighbors;

// Apply the Game of Life rules:

let liveNeighbors = -board[row][col];

function gameOfLife(board: number[][]): void {

for (let row = 0; row < rows; ++row) {</pre>

const rows = board.length;

const cols = board[0].length;

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                if (board[row][col] === 0 && liveNeighbors === 3) {
 33
                     board[row][col] = -1; // Mark the cell to become alive
 34
 35
 36
 37
 38
        // Finalize the board state by changing marked cells to their new states
 39
         for (let row = 0; row < rows; ++row) {</pre>
 40
             for (let col = 0; col < cols; ++col) {</pre>
                 if (board[row][col] === 2) {
 41
                     board[row][col] = 0; // Dead cells become 0
 42
 43
                if (board[row][col] === -1) {
 44
 45
                     board[row][col] = 1; // New live cells become 1
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Time and Space Complexity
// The time complexity of the code is 0(m * n), where m is the number of rows and n is the number of columns in the board. This is
because there are two nested loops that iterate through each cell of the board once.
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// The space complexity of the code is 0(1) since it modifies the board in place without using any additional space proportional to

the size of the input. All changes are made directly on the input board, and only a fixed number of extra variables are used.