# 2300. Successful Pairs of Spells and Potions

Sorting

<u>Two Pointers</u> <u>Binary Search</u>

## **Problem Description**

multiply each spell with each potion:

Medium Array

strength of each spell, and similarly, the potions array contains elements representing the strength of each potion. The task is to determine for each spell, how many potions can successfully combine with it to achieve or exceed a given success threshold. A spell and potion pair is deemed successful if the product (multiplication) of their strengths is at least equal to the success value provided. You should return an array where each value corresponds to the number of successful potion combinations for each spell in the spells array. To clarify with an example, suppose spells = [10, 20], potions = [5, 8, 10], and success = 100. To find successful pairs, you

In this problem, you are provided with two arrays called spells and potions. The spells array contains elements representing the

 For the first spell (strength 10), it pairs successfully with two potions (potions of strength 10 and 8) since both products are at least 100. • For the second spell (strength 20), it pairs successfully with all three potions, as all products will be 100 or greater. The result array will be [2,

- 3] as the first spell has 2 successful combinations, and the second has 3.
- ntuition

The goal is to find an efficient way to pair spells with potions such that the product of their strengths is at least the success

Instead, by first sorting the potions array, we can take advantage of binary search to quickly find the number of successful

#### target. A brute-force approach would be to try all possible pairs, but this can be inefficient, especially with large arrays.

potions for each spell. Binary search operates by repeatedly dividing the search interval in half, which is much faster than scanning every element.

Once the potions array is sorted, for each spell, we want to find the position where the potion strength is just enough or more to meet the success target when paired with the spell. We need to find the smallest potion that, when multiplied by the spell's strength, equals or exceeds the success threshold. All potions to the right in the sorted array are guaranteed to also form successful pairs because they are equal or stronger.

The solution leverages the bisect\_left function from Python's bisect module, which uses binary search to find the insertion

point for a given element to maintain sorted order. In this context, it finds the first index in potions where the potion strength is

sufficient for the success criteria with a given spell. We then subtract this index from the total number of potions (m) to get the count of successful potions for that spell. For each spell in spells, we apply this logic and generate the final result array. **Solution Approach** 

The solution implements a binary search mechanism to optimize the process of finding successful spell-potion pairs. Here's a

**Sorting the Potions:** Begin by sorting the potions array. This is crucial for binary search to work since binary search requires

a sorted array to function correctly. Sorting is done in ascending order.

potion index that can achieve the required target when combined with the current spell.

step-wise explanation of the approach used in the solution:

with the current spell.

to the sorted property of the array.

**Calculating Successful Pairs:**  We use the bisect\_left function which finds the index at which we could insert the value success / spell\_strength into potions to maintain sorted order.

• The value we are searching for is calculated by success / spell\_strength because we want to find the potion strength that, at the minimum, when multiplied by the spell's strength, is equal to success.

Since potions is sorted, every potion at and beyond the index returned by bisect\_left would result in a successful pair when combined

Using Binary Search: For each spell's strength value, we apply a binary search to determine the number of potions that, when

multiplied by this spell's strength, will at least be equal to the success value. This is done by finding the leftmost (smallest)

**Storing Results:** ∘ For each spell, we calculate m - index to find out the number of successful potions, where m is the total number of potions and index is the position returned by bisect\_left.

o This operation gives us the count because all elements from the position index to the end of the potions array will be successful pairs due

Generating the Output: Finally, we return a list comprehension that iterates over every spell in spells, applies the above logic using bisect\_left, and calculates the number of successful pairs for that spell.

**Example Walkthrough** 

success.

- Here's the critical code snippet with explanations for clarity: potions.sort() # Step 1: [Sorting](/problems/sorting\_summary) the 'potions' array. m = len(potions) # Storing the length of the 'potions' array.
- is the number of potions. Sorting takes 0(m log m), and then each binary search operation takes 0(log m), with the linear iteration over spells representing the n in the complexity.

Consider we have spells = [15, 10], potions = [1, 5, 20, 8], and success = 120. We aim to determine for each spell, how

Using Binary Search: We then apply binary search to find the count of potions that can pair with a spell to achieve the

1. Sorting the Potions: The first step is sorting the potions array. Before: [1, 5, 20, 8] After sorting: [1, 5, 8, 20]

Through sorting and binary searching, this algorithm achieves a complexity of O(n log m), where n is the number of spells, and m

many potions achieve or exceed the success threshold when multiplied by the spell.

∘ For spell 10: We need a potion of at least 120 / 10 = 12.

It finds the position of 8 because 8 \* 15 is exactly 120.

Spell is 10: bisect\_left([1, 5, 8, 20], 120/10)

index = 3, successful combinations: 4 - 3 = 1.

index = 2, total potions m = 4, successful combinations: 4 - 2 = 2.

It passes over 8 (since  $8 \times 10$  is less than 120) and settles before 20.

Find the number of potions for each spell that when combined

spells: List of integers representing the strength of spells.

potions: List of integers representing the volume of potions.

# Sort the potions list in ascending order for binary searching

import java.util.Arrays; // Ensure to import the necessary Arrays class for sorting.

// Sort the potions array for binary search

// ans will hold the answer to the problem

// Find the first potion that, when multiplied with the spell,

// We use 1.0 to cast success to double for correct division.

// Push the number of successful pairs into the answer vector.

// Initialize an array to store the number of successful pairs for each spell

// spell \* potionValue is greater than or equal to success threshold

// If not, move the left pointer to narrow the search

// The number of potions that meet the success criteria with the current spell

// is the length of the potions array minus the left bound found by binary search

// is greater than or equal to the success threshold.

sort(potions.begin(), potions.end());

// m is the size of the potions array

ans.push\_back(m - index);

// Sort the potions array in ascending order

const successfulPairsCount: number[] = [];

// Set the initial bounds for binary search

// Calculate the middle index

// Perform binary search to find the index where

successfulPairsCount.push(potionCount - left);

vector<int> ans;

int m = potions.size();

// Iterate over each spell

for (int spell : spells) {

// Return the final answer

potions.sort((a, b) => a - b);

// Iterate over each spell

let left = 0;

for (const spell of spells) {

let right = potionCount;

while (left < right) {</pre>

right = mid;

left = mid + 1;

// The number of potions available

const potionCount = potions.length;

return ans;

**}**;

**TypeScript** 

result in a product equal to or greater than the success threshold.

List containing the count of successful potion combinations for each spell.

**Calculating Successful Pairs:** 

# Step 2, 3, and 4: List comprehension iterating over 'spells'.

return [m - bisect\_left(potions, success / v) for v in spells]

Let's walk through a small example based on the solution approach given above.

```
• For spell 15: Using bisect_left, we find the index where 8 could fit in the sorted potions array [1, 5, 8, 20], which is index 2.
• For spell 10: Using bisect_left, we find the index where 12 could fit, which is after 8 and before 20. Hence, the index would be 3.
Storing Results:
```

 $\circ$  For spell 15: m - index is 4 - 2 = 2. So, there are 2 successful potion combinations for the spell 15.

successful combinations for each spell. The result for our example will be [2, 1].

 $\circ$  For spell 10: m - index is 4 - 3 = 1. Therefore, there is 1 successful potion combination for the spell 10.

def successful\_pairs(self, spells: List[int], potions: List[int], success: int) -> List[int]:

success: An integer representing the minimum success threshold for a spell-potion combination.

# For each spell strength 'spell\_strength' in 'spells', we find the index of the first potion

# minus this index, giving the number of potions that meet or exceed the product threshold.

return [num\_potions - bisect\_left(potions, success / spell\_strength) for spell\_strength in spells]

# The count of successful pairings for each spell is then the total number of potions

• For spell 15: We search for the smallest potion that when multiplied is at least 120. That potion should be 120 / 15 = 8.

For better understanding, here's how the binary search part of the code would operate in a step-by-step manner: Spell is 15: bisect\_left([1, 5, 8, 20], 120/15)

Generating the Output: According to the steps described in the solution approach, we create a list with the counts of

- Thus, the final returned value for this particular example with the spells and potions given would be [2, 1]. Each spell has a corresponding count of potions that, when multiplied, meet or exceed the success threshold.
- from bisect import bisect\_left from typing import List

Solution Implementation

**Python** 

Java

class Solution {

class Solution:

Args:

Returns:

potions.sort() # Length of the potions list num\_potions = len(potions) # Using list comprehension to generate the list of counts for successful combinations

# in the sorted 'potions' list that meets or exceeds the 'success' threshold when combined with the spell.

```
// This function determines the number of successful pairs of spells and potions.
    public int[] successfulPairs(int[] spells, int[] potions, long successThreshold) {
        Arrays.sort(potions); // Sort the potions array for binary search.
        int nSpells = spells.length; // Number of spells.
        int nPotions = potions.length; // Number of potions.
        int[] successfulPairs = new int[nSpells]; // Array to store the answer.
       // Iterate over each spell.
        for (int i = 0; i < nSpells; ++i) {</pre>
            int left = 0, right = nPotions; // Set search boundaries for binary search.
            // Binary search to find the first potion that results in a successful pair.
            while (left < right) {</pre>
                int mid = (left + right) / 2; // Calculate the mid index.
                // Check if the current spell and potion at mid index is a successful pair.
                if ((long) spells[i] * potions[mid] >= successThreshold) {
                    right = mid; // If successful, narrow the search to the left half.
                } else {
                    left = mid + 1; // If not successful, narrow the search to the right half.
            // The number of successful pairs for the current spell is the total number
            // of potions minus the number of potions that did not meet the success threshold.
            successfulPairs[i] = nPotions - left;
        return successfulPairs; // Return the array of successful pair counts.
C++
class Solution {
public:
    // Function to find the number of successful pairs
    vector<int> successfulPairs(vector<int>& spells, vector<int>& potions, long long success) {
```

int index = lower\_bound(potions.begin(), potions.end(), (success + spell - 1) / spell) - potions.begin();

// Subtract the found index from the size to determine the number of successful potions.

function successfulPairs(spells: number[], potions: number[], successThreshold: number): number[] {

```
const mid = Math.floor((left + right) / 2);
// Check if the current combination meets the success requirement
if (spell * potions[mid] >= successThreshold) {
    // If it does, we need to find if there's a smaller index that also satisfies the condition
```

} else {

```
// Return the array containing the counts of successful spell-potion pairs
      return successfulPairsCount;
from bisect import bisect_left
from typing import List
class Solution:
   def successful_pairs(self, spells: List[int], potions: List[int], success: int) -> List[int]:
       Find the number of potions for each spell that when combined
        result in a product equal to or greater than the success threshold.
       Args:
        spells: List of integers representing the strength of spells.
        potions: List of integers representing the volume of potions.
        success: An integer representing the minimum success threshold for a spell-potion combination.
       Returns:
       List containing the count of successful potion combinations for each spell.
       # Sort the potions list in ascending order for binary searching
        potions.sort()
       # Length of the potions list
       num_potions = len(potions)
```

# Using list comprehension to generate the list of counts for successful combinations

# The count of successful pairings for each spell is then the total number of potions

# For each spell strength 'spell\_strength' in 'spells', we find the index of the first potion

# minus this index, giving the number of potions that meet or exceed the product threshold.

return [num\_potions - bisect\_left(potions, success / spell\_strength) for spell\_strength in spells]

# in the sorted 'potions' list that meets or exceeds the 'success' threshold when combined with the spell.

### The time complexity of the given code snippet consists of two parts: sorting the potions list and performing binary searches using the bisect\_left function.

of O(s) where s is the number of spells.

Time and Space Complexity

**Time Complexity** 

Therefore, combining both operations, the total time complexity is  $0(n \log n + s \log n)$ . **Space Complexity** 

1. **Sorting:** The potions.sort() operation has a time complexity of O(n log n) where n is the number of potions.

The space complexity is determined by the additional space required beyond the input data. 1. Sorting Space: The sorting is done in place, which does not require additional space, so it's 0(1). 2. Output List: There is a list comprehension that generates a list of the same length as the number of spells. Therefore, it has a space complexity

2. Binary Search: The binary search inside the list comprehension using bisect\_left is performed for each spell. If there are s spells, and the

binary search has a time complexity of O(log n) for each spell, the entire list comprehension has a time complexity of O(s log n).

Given that O(s) is the larger term between O(1) and O(s), the overall space complexity is O(s).