2349. Design a Number Container System Medium Design Hash Table Ordered Set Heap (Priority Queue)

smallest index of any given number. We use two main data structures to achieve this:

### **Leetcode Link**

## The LeetCode problem entails designing a system that can manage a set of numbers each located at a unique index. The system

container, the system should return -1.

**Problem Description** 

needs to support two primary operations:

1. change: This operation must insert or replace a number at a specified index. If an index already contains a number, it should be

- replaced with the new number. 2. find: This operation should return the smallest index at which a specific number is located. If the number is not present in any
- The challenge is to implement these operations efficiently, meaning we need to optimize for both insert/replace and search operations, ensuring that find queries are performed in an optimized manner, especially in a dataset where searches are frequent

compared to updates. Intuition

To arrive at the solution, we need a data structure that can efficiently keep track of each number's indices and quickly retrieve the

### 1. A hash map (self.mp), where the key is the index and the value is the number at that index. This allows us to quickly check if an

index already has a number and to update the number at any index. 2. A default dictionary of SortedSet (self.t), indexed by numbers. SortedSet is a data structure that maintains the elements in

sorted order. This allows us to quickly retrieve the smallest index for a given number as it will always be the first element.

- When we perform the change operation, we update the index's number in the hash map. If the index already had a number, we remove the index from the SortedSet of that old number. Then we add the index to the SortedSet of the new number.
- During the find operation, we look up the SortedSet for the given number. If the SortedSet is not empty, we return the first element (since it's the smallest index due to the properties of the SortedSet). If the SortedSet is empty, it means the number is not present at any index, so we return -1.

This approach allows us to efficiently update the indices and retrieve the smallest index for any number, making the NumberContainers class a fast and reliable system for the operations required.

The implementation of the NumberContainers class uses a hash map and a default dictionary of SortedSet structures. The SortedSet is chosen for its properties of maintaining the elements in sorted order, which is essential for efficient retrieval of indices.

1. Initialization (\_\_init\_\_ method): • A hash map self.mp is initialized to keep track of which number is at which index.

**Solution Approach** 

SortedSet if it does not already exist in the dictionary. 2. Change operation (change method):

A default dictionary selfit of SortedSet is initialized to store sets of indices for each number. The defaultdict from the

Python collections module ensures that each number key in the dictionary will automatically be associated with an empty

■ If the index already exists in the hash map (indicating a number is already present at that index), remove the index from

Add the index to the SortedSet of the new number. This operation automatically keeps the SortedSet in sorted order.

the SortedSet of the current number associated with that index. Update the hash map with the new number at the index.

Python code snippet for the change operation:

1 def change(self, index: int, number: int) -> None:

To find the smallest index for a given number:

Let's illustrate the solution approach with a small example:

1. change(2, 1): We want to insert number 1 at index 2.

2. change(1, 1): Now, we insert number 1 at index 1.

Given an index and a number:

Here's a step-by-step breakdown of the implementation:

self.t[number].add(index)

3. Find operation (find method):

if index in self.mp:

v = self.mp[index]

1 def find(self, number: int) -> int:

return s[0] if s else -1

Example Walkthrough

self.mp[index] = number

self.t[v].remove(index)

■ If the SortedSet is empty, return -1 indicating the number is not present at any index. Python code snippet for the find operation:

• If the SortedSet is not empty, return the first element (smallest index) since the indices are maintained in sorted order.

balances the need for dynamic updates with frequent and fast queries, delivering the functionalities required by the NumberContainers system.

The choice of SortedSet is crucial for the solution's efficiency. SortedSet allows for fast addition and removal of index elements while

maintaining a sort order, making the find operation a simple and quick retrieval of the smallest element. This solution thus capably

Suppose we initialize our NumberContainers class and the following operations are performed sequentially:

Since index 2 is not yet mapped, we simply insert it into self.mp: self.mp becomes {2: 1}.

We add the index to the SortedSet of number 1 in self.t: self.t[1] now contains {2}.

Retrieve the SortedSet associated with the number from self.t.

• We add the new key-value pair to self.mp: self.mp becomes {2: 1, 1: 1}. • Index 1 is added into the SortedSet of number 1 in self.t: self.t[1] now contains {1, 2}, automatically sorted. 3. change(2, 2): Number 2 is now inserted at index 2, which already has a number 1. • We remove index 2 from the SortedSet of the old number, self.t[1], which then becomes {1}.

• Index 2 is added to the SortedSet of number 2 (which was an empty SortedSet before): self.t[2] now contains {2}.

This example demonstrates how each change and find operation works as expected, providing efficient updates and lookups as per

#### Lookup self.t[1], which contains {1}. • The smallest index in the sorted set is the first element, which is 1, thus we return 1.

the problem requirements.

class NumberContainers:

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def \_\_init\_\_(self):

from collections import defaultdict

from sortedcontainers import SortedSet

self.index\_to\_number = {}

Since number 3 has never been inserted, self.t[3] is an empty SortedSet.

The sequence of these operations would result in the following internal states for our NumberContainers class:

Default dictionary of number to SortedSets of indices: self.t = {1: SortedSet([1]), 2: SortedSet([2])}

self.mp is updated to reflect the change: self.mp becomes {2: 2, 1: 1}.

4. find(1): We want to find the smallest index where number 1 is located.

5. find(3): We want to find the smallest index where number 3 is located.

Hash map of index to numbers: self.mp = {1: 1, 2: 2}

○ We return -1, indicating that number 3 is not present at any index.

Python Solution

# Defaultdict to hold SortedSets which will contain indices for each number

"""Returns the smallest index for the given number; if not found, returns -1."""

# SortedSets are used for maintaining the indices in sorted order

self.number\_to\_indices[current\_number].remove(index)

# Update the number at the index in our index\_to\_number mapping

# If there are any indices, return the smallest one (first element)

33 # The NumberContainers class can now be instantiated and methods called as described.

private final Map<Integer, Integer> indexToNumberMap = new HashMap<>();

// Intentionally left blank, no initialization needed here

private final Map<Integer, TreeSet<Integer>> numberToIndicesMap = new HashMap<>();

# If not, return -1 indicating the number is not assigned to any index

1 # Import the defaultdict from collections and SortedSet from sortedcontainers

# Dictionary to hold the current number at each index

self.number\_to\_indices = defaultdict(SortedSet)

self.index\_to\_number[index] = number

def find(self, number: int) -> int:

# Add the index to the new number's SortedSet

# Get the SortedSet of indices for the given number

self.number\_to\_indices[number].add(index)

indices = self.number\_to\_indices[number]

return indices [0] if indices else -1

def change(self, index: int, number: int) -> None: """Update the number at the given index and maintain the indices sorted.""" # If the index is already in our mapping, remove it from the current number's SortedSet if index in self.index\_to\_number: current\_number = self.index\_to\_number[index]

#### Java Solution 1 import java.util.HashMap; import java.util.Map; import java.util.TreeSet;

34 # obj = NumberContainers()

35 # obj.change(index, number)

36 # param\_2 = obj.find(number)

class NumberContainers {

// Constructor

public NumberContainers() {

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       /**
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        * Updates the number at a given index and maintains the mapping of numbers to a sorted set of indices.
16
        * @param index The index to change.
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        * @param number The new number to associate with the index.
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       public void change(int index, int number) {
           // If index already contains a number, update the mapping
21
           if (indexToNumberMap.containsKey(index)) {
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               int currentNumber = indexToNumberMap.get(index);
24
               // Remove the index from the current number's set
25
               TreeSet<Integer> indicesSet = numberToIndicesMap.get(currentNumber);
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               indicesSet.remove(index);
27
               // If the set is empty after removal, remove it from the map
               if (indicesSet.isEmpty()) {
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                   numberToIndicesMap.remove(currentNumber);
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           // Add or update the index-to-number mapping
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           indexToNumberMap.put(index, number);
           // Add index to the new number's set, creating the set if it doesn't exist
34
           numberToIndicesMap.computeIfAbsent(number, k -> new TreeSet<>()).add(index);
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       /**
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        * Finds the lowest index for a number.
        * If the number is not associated with any index, returns -1.
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        * @param number The number to find the lowest index for.
        * @return The lowest index of the given number or -1 if not found.
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       public int find(int number) {
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           // Check if number exists in the map and return the first (lowest) index
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           return numberToIndicesMap.containsKey(number) ? numberToIndicesMap.get(number).first() : -1;
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  // The NumberContainers object usage remains the same; example of instantiation and method calls:
  // NumberContainers obj = new NumberContainers();
  // obj.change(index,number);
  // int lowestIndex = obj.find(number);
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C++ Solution
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# 49

1 #include <map>

public:

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#include <set>

class NumberContainers {

// Default constructor.

NumberContainers() {

} else {

int find(int number) {

// Maps each index to the number it contains.

std::map<int, std::set<int>> numberToIndicesMap;

// Check if the index is already in the map.

numberToIndicesMap[it->second].erase(index);

// If the index is new, just add it to the map.

// Update the index to the new number.

indexToNumberMap[index] = number;

numberToIndicesMap[number].insert(index);

auto it = numberToIndicesMap.find(number);

auto it = indexToNumberMap.find(index);

// Changes the number at the given index.

if (it != indexToNumberMap.end()) {

void change(int index, int number) {

it->second = number;

// Maps each number to a set of indices that contain this number.

// to its current number, as it's about to be reassigned.

// Insert the index to the set corresponding to the new number.

// Attempt to find the set of indices for the given number.

// If the number is not found or the set is empty, return -1.

// If the index is already there, remove the index from the set corresponding

// Finds the smallest index that contains the given number. Returns -1 if such an index cannot be found.

return (it == numberToIndicesMap.end() || it->second.empty()) ? -1 : \*it->second.begin();

std::map<int, int> indexToNumberMap;

```
* The NumberContainers object will be instantiated and called like this:
    * NumberContainers* obj = new NumberContainers();
    * obj->change(index, number);
    * int param_2 = obj->find(number);
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    */
Typescript Solution
   // Mapping from index to number.
   const indexToNumberMap: Map<number, number> = new Map();
   // Mapping from number to a set of indices containing that number.
   const numberToIndicesMap: Map<number, Set<number>> = new Map();
   /**
    * Changes the number at the given index.
    * @param index The index of the number to change.
    * @param number The new number to set at the index.
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    */
   function change(index: number, number: number): void {
       // Check if the index already maps to a number.
13
       if (indexToNumberMap.has(index)) {
14
           // Retrieve the current number at the index.
           const currentNumber = indexToNumberMap.get(index);
16
           // Remove index from the set of the current number.
17
           numberToIndicesMap.get(currentNumber)?.delete(index);
18
19
20
       // Update the index to the new number.
       indexToNumberMap.set(index, number);
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23
       // If there's no existing set for this number, create one.
       if (!numberToIndicesMap.has(number)) {
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25
           numberToIndicesMap.set(number, new Set());
26
       // Add the index to the set corresponding to the new number.
27
28
       numberToIndicesMap.get(number)?.add(index);
29 }
30
    * Finds the smallest index that contains the given number.
    * @param number The number to find the smallest index for.
    * @returns The smallest index containing the given number, or -1 if not found.
35
   function find(number: number): number {
36
37
       // Attempt to find the set of indices for the given number.
       const indicesSet = numberToIndicesMap.get(number);
38
       // If there's no set for the number or the set is empty, return -1.
       if (!indicesSet || indicesSet.size === 0) {
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           return -1;
       // Return the smallest index (first value) in the sorted set.
43
       return Math.min(...indicesSet);
45 }
```

# Time complexity:

Time and Space Complexity

// let smallestIndex = find(10);

// Example usage:

// change(1, 10);

already exists in self.mp, since SortedSet removes the element in O(log n) and adds the element in O(log n) time complexity. If an element is not present, adding to a SortedSet is O(log n) as well. Updating the dictionary self.mp has a time complexity of 0(1).

The given Python code defines a class NumberContainers that manages a mapping between indices and numbers and provides two

• \_\_init\_\_ function: The initialization function has a constant time complexity of 0(1), as it only involves the initialization of two

change function: The change method has a time complexity of O(log n) for updating the SortedSet in the case where the index

• find function: The find method has a time complexity of 0(1) for accessing the first element of the SortedSet since SortedSet

Space complexity: • \_\_init\_\_ function: The space complexity for the initialization function is 0(1) as it initializes empty data structures.

unique index and self.t holds unique numbers each associated with a SortedSet which in turn contains indices.

maintains the elements in sorted order, and accessing the elements by index is done in constant time.

// console.log(smallestIndex); // Outputs the smallest index where the number 10 is located, if present.

methods: change to change the number at a given index, and find to find the smallest index with a given number.

data structures: a dictionary self.mp and a defaultdict of SortedSet self.t.

• change and find functions: The space complexity is 0(m + k) where m is the number of unique indices and k is the total number of unique numbers present in the NumberContainers object. This is because self.mp can potentially hold a mapping for each

Overall, this data structure is optimized for quick updates and lookups, with the SortedSet providing efficient ordering for the indices.