1365. How Many Numbers Are Smaller Than the Current Number

Leetcode Link



Hash Table

The problem is to find for each element in the array nums, how many elements are smaller than the current element. In other words, you walk through each item in the input list, and for each of these items, you need to count all other numbers in the list that are less than it. It's important to remember that you should not include the current element in the count. The goal is to create an output array of the same length as nums where each index contains this count of smaller numbers.

1, one number is smaller than the first occurrence of 2, and so on.

Example: If nums = [8,1,2,2,3], the output would be [4,0,1,1,3]. Here, four numbers are smaller than 8, no number is smaller than

To find a solution to this problem, we could consider the following:

Intuition

Easy

1. Brute Force: We could use a nested loop to compare each pair of elements and count how many elements are smaller, but this

the elements, which we need to preserve.

algorithm. Here is a detailed walkthrough of the solution:

Counting

Sorting

- would be O(n^2) in time complexity, which is not efficient for large arrays. 2. Sorting: We could sort the array and then map each element to its corresponding index, but this would lose the original order of
- 3. Counting Sort Principle: Since we know the elements in nums are integers and the problem typically has constraints that limit their range (not stated in the problem description here but usually up to 100), we can use a counting sort approach. This means
- we tally how many times each number occurs (the frequency), and then we can deduce how many numbers are smaller by looking at numbers (frequencies) to the left of the current number. The intuition behind the provided solution is to build a frequency array cnt with an extra element so we can easily accumulate the counts. We use the accumulate function from Python's itertools to get a prefix sum of counts, effectively giving us a running total of

how many numbers are smaller than each value up to 101 (assuming nums contains numbers up to 100 for this argument). By doing

this, s[x] corresponds to the count of numbers less than x in the original array, as desired. Thus, s is used to create the output result conveniently and efficiently. Solution Approach

The implementation of the solution makes use of a frequency array approach, which is a technique commonly used in counting sort

1. Initialize a frequency array cnt with a size of 102 to include all possible values from 0 to 100 along with an extra slot for ease of

calculation. If nums contains numbers up to maxValue, the size of cnt should be maxValue + 2. 1 cnt = [0] * 102

allow us to later easily calculate the number of elements smaller than a given number using prefix sums. 1 for x in nums: cnt[x + 1] += 1

2. Iterate over each element x in the input nums and increment the count of x + 1 in the frequency array cnt. This shift by one is to

- 3. Calculate the prefix sum using Python's accumulate function from the itertools module. This operation will give us a new list s
- 4. Iterate through the elements in nums again to create the results array. For each element x in nums, we look up s[x] which gives us the number of elements that are less than x and add this count to our result array.

representing the cumulative frequency. Now s[x] will represent the total count of numbers that are less than x.

```
1 return [s[x] for x in nums]
```

1 s = list(accumulate(cnt))

This approach leverages the itertools.accumulate function to avoid manually calculating prefix sums, which provides a clean and efficient way to obtain the cumulative frequency. The beauty of this solution lies in its simplicity and efficiency, allowing us to conclude the counts of smaller numbers in a single pass

The solution thus effectively uses the counting sort algorithm, which is often preferred for small integer ranges due to its 0(n + k)

complexity, where n is the number of elements in the array and k is the range of input numbers. This is more efficient than

comparison-based sorting methods when k is relatively small compared to n.

while utilizing a non-comparison-based sorting concept.

elements are smaller than each element in nums.

Example Walkthrough Let's illustrate the solution approach using a smaller example array, nums = [4, 0, 2, 1]. Here we want to find out how many

1. We initialize the frequency array cnt with a size of 102 to cover all possible values in the range 0 to 100 inclusively, with an extra slot:

1 nums = [4, 0, 2, 1]

3 After processing each element:

1 result = [s[x] for x in nums]

2 # result = [s[4], s[0], s[2], s[1]]

0 numbers are smaller than 0

1 number is smaller than 2 (0)

1 number is smaller than 1 (0)

count = [0] * 102

for number in nums:

count[number + 1] += 1

sum_count = list(accumulate(count))

12

13

14

15

16

17

18

19

20

21

22

23

3 # result now should be: [3, 0, 1, 1]

4 - cnt[4 + 1] = cnt[5] += 1 # increment at index 5

5 - cnt[0 + 1] = cnt[1] += 1 # increment at index 1

6 - cnt[2 + 1] = cnt[3] += 1 # increment at index 3

7 - cnt[1 + 1] = cnt[2] += 1 # increment at index 2

1 cnt = [0] * 102

9 The frequency array ('cnt') looks like this after iteration: 10 cnt = $[0, 1, 1, 1, 0, 1, 0, \dots, 0]$

2. We then iterate over each element in nums and increment the corresponding index in cnt (shifted by one):

```
3. We use Python's accumulate function to calculate the prefix sum, which gives us the cumulative count of smaller numbers:
   1 from itertools import accumulate
   3 s = list(accumulate(cnt))
   4 # s now looks like this: [0, 1, 2, 3, 3, 4, 4, ..., 4]
   5 # This array represents the cumulative count of numbers less than the index.
4. Lastly, we iterate through the elements in nums again and create our result array using the s array we just computed:
```

The final result array indicates that: 3 numbers are smaller than 4 (0, 1, and 2)

This example walkthrough demonstrates each step of the method described in the content above, yielding an efficient outcome that

```
correctly matches each element in nums with the count of elements that are smaller than it.
Python Solution
   from itertools import accumulate
   class Solution:
       def smallerNumbersThanCurrent(self, nums: List[int]) -> List[int]:
           # Initialize a count array with additional space to accumulate counts.
           # We use 102 instead of 101 because we're using cnt[x+1] in the loop.
```

Count how many times each number (0-100) appears in nums.

Calculate the prefix sum to determine how many numbers are

The 'accumulate' function is like a cumulative sum.

For each number in the original array, we now look up

return [sum_count[number] for number in nums]

We increment the count at index x+1 to later use this space for accumulate.

less than the current number. This would help in getting counts directly.

The result for each number is simply sum_count at the index of that number.

how many numbers are smaller than it by referring to our sum_count.

```
Java Solution
   class Solution {
       public int[] smallerNumbersThanCurrent(int[] nums) {
           // Container to store the count of the number of smaller elements for each element in 'nums'.
           int[] count = new int[102]; // We use 102 instead of 101 to simplify the algorithm,
                                       // so we don't need to handle the case of 0 separately.
           // Populate the count array where index represents the number+1 and
           // the value at that index represents the count of that number in 'nums'.
           for (int num : nums) {
               ++count[num + 1];
10
11
12
13
           // Convert the count array to a prefix sum array
           // where count[i] contains the number of elements less than i.
14
15
           for (int i = 1; i < count.length; ++i) {</pre>
16
               count[i] += count[i - 1];
17
18
           // Length of the original 'nums' array.
19
20
           int n = nums.length;
           // Result array where each element will be replaced by the count of numbers less than it.
22
           int[] result = new int[n];
23
24
           // Fill the result array using the count array.
25
           for (int i = 0; i < n; ++i) {
```

// the count of elements less than that number.

```
26
                result[i] = count[nums[i]]; // nums[i] gives the number and count[nums[i]] gives
27
28
29
30
           // Return the result array.
```

return result;

31

32

34

33 }

33 };

34

8

9

10

```
C++ Solution
   #include <vector>
   class Solution {
   public:
       // Function to find the number of elements smaller than each element in the array
       vector<int> smallerNumbersThanCurrent(vector<int>& nums) {
           // Array to store the count of each number plus one value ahead (prefix sum)
           int count[102] = {0}; // Initialize all elements to 0
           // Count how many times each number appears in the input vector
10
           for (int number : nums) {
11
12
               ++count[number + 1];
13
14
           // Calculate the prefix sum to get the number of elements less than current
15
           for (int i = 1; i < 102; ++i) {
16
                count[i] += count[i - 1];
17
18
19
           // Initialize the answer vector to store the results
20
           vector<int> answer;
22
23
           // Determine the number of smaller elements for each element in nums
24
            for (int number : nums)
25
               // The count at the index 'number' of the prefix sum will be the
               // number of elements smaller than 'number'
26
               answer.push_back(count[number]);
28
29
30
           // Return the complete answer
31
           return answer;
32
```

16 17 18

Typescript Solution

for (const num of nums) {

++frequencyArray[num + 1];

```
// Each element at index i now holds the total count of numbers less than i-1.
11
12
       for (let i = 1; i < frequencyArray.length; ++i) {</pre>
13
           frequencyArray[i] += frequencyArray[i - 1];
14
15
       // The length of the input array.
       const lengthOfNums = nums.length;
       // Initialize an array to hold the answer.
19
       const result: number[] = new Array(lengthOfNums);
20
       // For each number in the input array, find the count of numbers smaller than itself using the prefix sum array.
22
       for (let i = 0; i < lengthOfNums; ++i) {
23
           result[i] = frequencyArray[nums[i]];
24
25
26
       // Return the resulting array with counts for each number.
       return result;
28
29 }
30
Time and Space Complexity
The time complexity of the code is 0(n + m), where n is the number of elements in the input nums list and m is the range of numbers in
nums. Here, the range m is fixed at 101 since we are using a count array cnt of size 102 (the extra one is to accommodate the 0
```

// Initialize a frequency array with 102 elements (to cover numbers 0-100 inclusive and an extra one for indexing purposes).

// Populate the frequency array with the count of each number in the input array (shifted by one index).

function smallerNumbersThanCurrent(nums: number[]): number[] {

const frequencyArray: number[] = new Array(102).fill(0);

// Transform the frequency array into a prefix sum array.

indexing and the fact that we started from x + 1). The time complexity breaks down as follows:

• O(m) for the accumulate function which iterates over the cnt array of fixed size 102. O(n) for the list comprehension that constructs the result list by iterating over the nums list again.

• O(n) for the first for-loop where we iterate over the nums list and update the cnt array.

Thus, the overall time complexity is dominated by the terms O(n) and O(m), resulting in O(n + m).

The space complexity of the code is O(m), which comes from the cnt array of fixed size 102, and the s array, which will have the same size due to the use of the accumulate function on cnt. The space required for the output list is not counted towards the space complexity as it is required for the output of the function. Since m is a fixed constant (102), the space complexity can also be considered 0(1), constant space complexity.