3068. Find the Maximum Sum of Node Values

Description

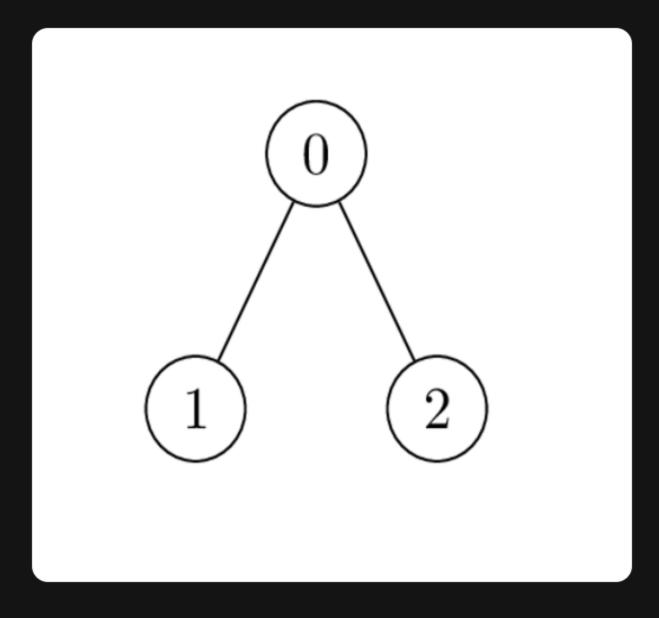
There exists an **undirected** tree with $\begin{bmatrix} n \end{bmatrix}$ nodes numbered $\begin{bmatrix} 0 \end{bmatrix}$ to $\begin{bmatrix} n-1 \end{bmatrix}$. You are given a **0-indexed** 2D integer array $\begin{bmatrix} edges \end{bmatrix}$ of length $\begin{bmatrix} n-1 \end{bmatrix}$, where $\begin{bmatrix} edges \end{bmatrix} = \begin{bmatrix} u_i, v_i \end{bmatrix}$ indicates that there is an edge between nodes $\begin{bmatrix} u_i \end{bmatrix}$ and $\begin{bmatrix} v_i \end{bmatrix}$ in the tree. You are also given a **positive** integer $\begin{bmatrix} k \end{bmatrix}$, and a **0-indexed** array of **non-negative** integers $\begin{bmatrix} nums \end{bmatrix}$ of length $\begin{bmatrix} n \end{bmatrix}$, where $\begin{bmatrix} nums \end{bmatrix}$ represents the **value** of the node numbered $\begin{bmatrix} i \end{bmatrix}$.

Alice wants the sum of values of tree nodes to be **maximum**, for which Alice can perform the following operation **any** number of times (**including zero**) on the tree:

- Choose any edge [u, v] connecting the nodes u and v, and update their values as follows:
 - \circ nums[u] = nums[u] XOR k
 - $\circ \quad \mathsf{nums[v]} = \mathsf{nums[v]} \mathsf{XOR} \mathsf{k}$

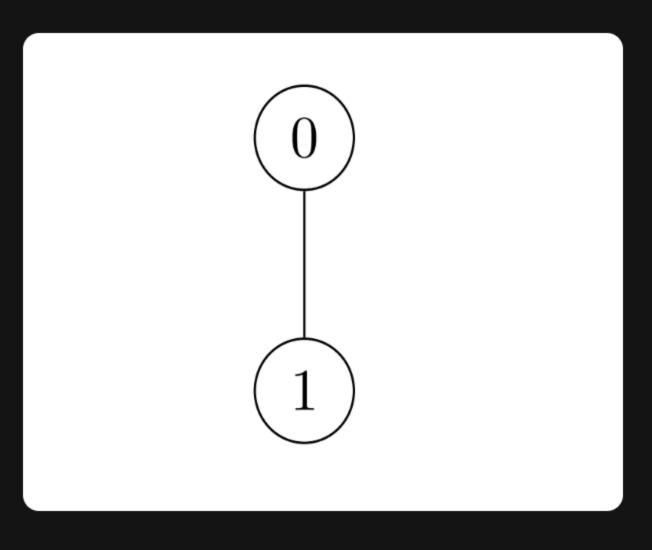
Return the maximum possible sum of the values Alice can achieve by performing the operation any number of times.

Example 1:



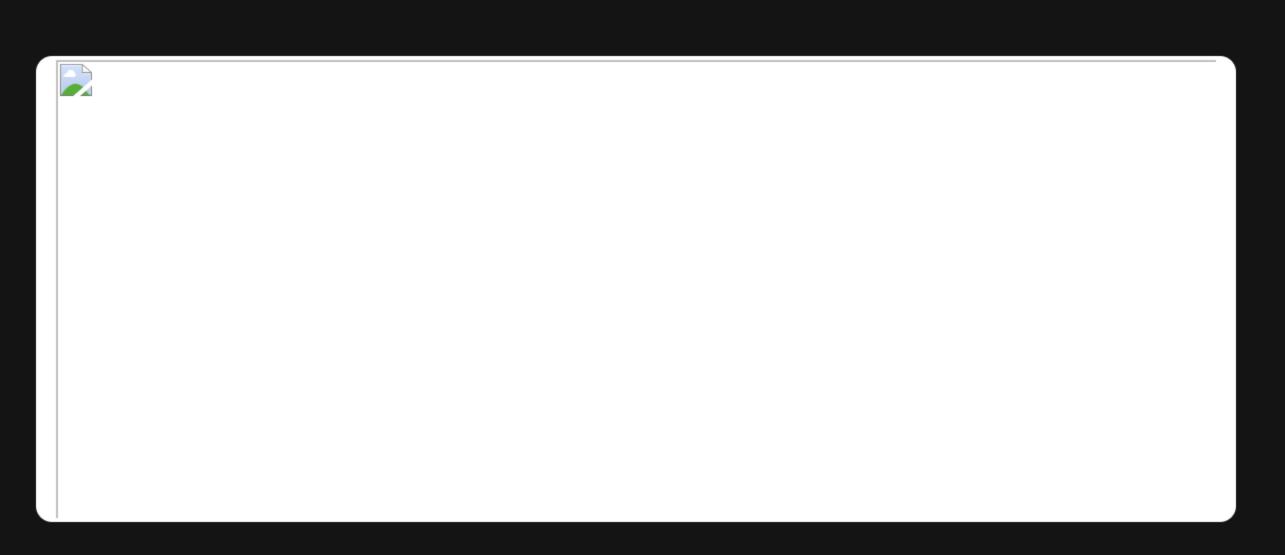
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Input: nums = [1,2,1], k = 3, edges = [[0,1],[0,2]]
Output: 6
Explanation: Alice can achieve the maximum sum of 6 using a single operation:
- Choose the edge [0,2]. nums[0] and nums[2] become: 1 XOR 3 = 2, and the array nums becomes: [1,2,1] -> [2,2,2].
The total sum of values is 2 + 2 + 2 = 6.
It can be shown that 6 is the maximum achievable sum of values.
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Example 2:



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Input: nums = [2,3], k = 7, edges = [[0,1]]
Output: 9
Explanation: Alice can achieve the maximum sum of 9 using a single operation:
- Choose the edge [0,1]. nums[0] becomes: 2 XOR 7 = 5 and nums[1] become: 3 XOR 7 = 4, and the array nums becomes: [2,3] -> [5,4].
The total sum of values is 5 + 4 = 9.
It can be shown that 9 is the maximum achievable sum of values.
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Example 3:



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Input: nums = [7,7,7,7,7,7], k = 3, edges = [[0,1],[0,2],[0,3],[0,4],[0,5]]
Output: 42
Explanation: The maximum achievable sum is 42 which can be achieved by Alice performing no operations.
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Constraints:

- 2 <= n == nums.length <= 2 * 10 4
- 1 <= k <= 10 ⁹
- 0 <= nums[i] <= 10 9
- edges.length == n 1
- edges[i].length == 2
- 0 <= edges[i][0], edges[i][1] <= n 1
- The input is generated such that edges represent a valid tree.