253. Meeting Rooms II **Prefix Sum** Medium Sorting Greedy Array Two Pointers

Problem Description

The problem presents a scenario where we have an array of meeting time intervals, each represented by a pair of numbers [start_i, end_i]. These pairs indicate when a meeting starts and ends. The goal is to find the minimum number of conference rooms required to accommodate all these meetings without any overlap. In other words, we want to allocate space such that no two meetings occur in the same room simultaneously.

Heap (Priority Queue)

Intuition

The core idea behind the solution is to track the changes in room occupancy over time, which is akin to tracking the number of trains at a station at any given time. We can visualize the timeline from the start of the first meeting to the end of the last meeting, and keep a counter that increments when a meeting starts and decrements when a meeting ends. This approach is similar to the sweep line algorithm, often used in computational geometry to keep track of changes over time or another dimension.

value reached by this counter at any point in time represents the peak occupancy, thus indicating the minimum number of conference rooms needed. To implement this: 1. We initialize an array delta that is large enough to span all potential meeting times. We use a fixed size in this solution, which

By iterating through all the meetings, we apply these increments/decrements at the respective start and end times. The maximum

- assumes the meeting times fall within a predefined range (0 to 1000009 in this case). 2. Iterate through the intervals list, and for each meeting interval [start, end], increment the value at index start in the delta
- array, and decrement the value at index end. This effectively marks the start of a meeting with +1 (indicating a room is now occupied) and the end of a meeting with -1 (a room has been vacated).
- The maximum number reached in this accumulated array is our answer, as it represents the highest number of simultaneous meetings, i.e., the minimum number of conference rooms required. This solution is efficient because it avoids the need to sort the meetings by their start or end times, and it provides a direct way to

3. Accumulate the changes in the delta array using the accumulate function, which applies a running sum over the array elements.

calculate the running sum of room occupancy over the entire timeline. **Solution Approach**

The solution uses a simple array and the concept of the prefix sum (running sum) to keep track of room occupancy over time—an approach that is both space-efficient and does not require complex data structures.

Here's a step-by-step breakdown of the implementation: 1. Initialization: A large array delta is created with all elements initialized to 0. The size of the array is chosen to be large enough

to handle all potential meeting times (1 more than the largest possible time to account for the last meeting's end time). In this

case, 1000010 is used.

- 2. Updating the delta Array: For each meeting interval, say [start, end], we treat the start time as the point where a new room is needed (increment counter) and the end time as the point where a room is freed (decrement counter).
- 1 for start, end in intervals: delta[start] += 1 delta[end] -= 1

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This creates a timeline indicating when rooms are occupied and vacated.
3. Calculating the Prefix Sum: We use the accumulate function from the itertools module of Python to create a running sum (also
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1 occupied_rooms_over_time = accumulate(delta)

4. Finding the Maximum Occupancy: The peak of the occupied_rooms_over_time array represents the maximum number of rooms simultaneously occupied, hence the minimum number of rooms we need. 1 min_rooms_required = max(occupied_rooms_over_time)

known as a prefix sum) over the delta array. The result is a new array indicating the number of rooms occupied at each time.

The max function is used to find this peak value, which completes our solution. The beauty of this approach is in its simplicity and efficiency. Instead of worrying about sorting meetings by starts or ends or using

increments and decrements on the timeline does not matter. As long as we correctly increment at the start times and decrement at

In conclusion, this method provides an elegant solution to the problem using basic array manipulation and the concept of prefix

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complex data structures like priority queues, we leverage the fact that when we are only interested in the max count, the order of
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1 Meeting intervals: [[1, 4], [2, 5], [7, 9]]

time 5, and the third meeting starts at time 7 and ends at time 9.

provided approach. Initially, all elements in delta are set to 0.

the end times, the accumulate function ensures we get a correct count at each time point.

sums. Example Walkthrough Let's consider a small set of meeting intervals to illustrate the solution approach:

Here we have three meetings. The first meeting starts at time 1 and ends at time 4, the second meeting starts at time 2 and ends at

1. Initialization: We create an array delta of size 1000010, which is a bit overkill for this small example, but let's go with the

Following the solution steps:

2. Updating the delta Array: We iterate through the meeting intervals and update the delta array accordingly. 1 delta[1] += 1 # Meeting 1 starts, need a room 2 delta[4] -= 1 # Meeting 1 ends, free a room

3. Calculating the Prefix Sum: Using an accumulate operation (similar to a running sum), we calculate the number of rooms

After the updates, the delta array will reflect changes in room occupancy at the start and end times of the meetings.

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occupied at each point in time. For simplicity, we will perform the cumulation manually:
 1 time
          1 2 3 4 5 6 7 8 9
 2 delta +1 +1 0 -1 -1 0 +1 0 -1
3 occupied 1 2 2 1 0 0 1 1 0 (summing up `delta` changes over time)
```

1 The minimum number of conference rooms required is 2.

3 delta[2] += 1 # Meeting 2 starts, need a room

5 delta[7] += 1 # Meeting 3 starts, need a room

4 delta[5] -= 1 # Meeting 2 ends, free a room

6 delta[9] -= 1 # Meeting 3 ends, free a room

Python Solution

The range is chosen such that it covers all possible meeting times

def minMeetingRooms(self, intervals: List[List[int]]) -> int:

at least two conference rooms are needed to accommodate all meetings without overlap.

The maximum number during this running sum is 2, which occurs at times 2 and 3.

1 from typing import List from itertools import accumulate

`max` is then used to find the maximum number of concurrent meetings, which is the minimum number of rooms required

Initialize a list to keep track of the number of meetings starting or ending at any time

The `accumulate` function is used to compute the running total of active meetings at each time

4. Finding the Maximum Occupancy: We can see that the highest value in the occupancy timeline is 2, therefore we conclude that

Go through each interval in the provided list of intervals 10 for start, end in intervals: 12 meeting_delta[start] += 1 # Increment for a meeting starting meeting_delta[end] -= 1 # Decrement for a meeting ending

int res = delta[0];

return res;

C++ Solution

1 #include <vector>

for (int i = 1; i < n; ++i) {

delta[i] += delta[i - 1];

#include <algorithm> // Include necessary headers

res = Math.max(res, delta[i]);

meeting delta = [0] * 1000010

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return max(accumulate(meeting_delta))
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19 # Example usage:
20 # sol = Solution()
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class Solution:

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31 }

```
21 # print(sol.minMeetingRooms([[0, 30], [5, 10], [15, 20]])) # Output: 2
22
Java Solution
   class Solution {
       // Function to find the minimum number of meeting rooms required
       public int minMeetingRooms(int[][] intervals) {
           // Define the size for time slots (with assumed maximum time as 10^6+10)
           int n = 1000010;
           int[] delta = new int[n]; // Array to hold the changes in ongoing meetings
 8
           // Iterate through all intervals
 9
           for (int[] interval : intervals) {
10
               // Increment the start time to indicate a new meeting starts
11
12
               ++delta[interval[0]];
13
               // Decrement the end time to indicate a meeting ends
               --delta[interval[1]];
14
15
```

// Initialize res to the first time slot to handle the case if only one meeting

// Cumulate the changes to find active meetings at time i

// Traverse over the delta array to find maximum number of ongoing meetings at any time

// Update res if the current time slot has more meetings than previously recorded

// Return the maximum value found in delta, which is the minimum number of rooms required

22 23 24 25 }; 26

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});

import { max } from "lodash";

// Iterate over each interval

intervals.forEach(interval => {

// Function to find the minimum number of meeting rooms required

const maximumTimePoint: number = 1000010; // Define the maximum possible time point

countChange[interval[0]]++; // Increment count at the start time of the meeting

// Prefix sum calculation — accumulate the count changes to find the count at each time point

countChange[interval[1]]--; // Decrement count at the end time of the meeting

function minMeetingRooms(intervals: number[][]): number {

for (let i = 0; i < maximumTimePoint - 1; ++i) {</pre>

countChange[i + 1] += countChange[i];

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class Solution {
   public:
       // Function to find the minimum number of meeting rooms required
       int minMeetingRooms(vector<vector<int>>& intervals) {
           int n = 1000010; // Define the maximum possible time point
           vector<int> countDelta(n); // Create a vector to keep track of the count changes
10
           // Iterate over each interval
11
           for (auto &interval : intervals) {
12
               ++countDelta[interval[0]]; // Increment count at the start time of the meeting
13
               --countDelta[interval[1]]; // Decrement count at the end time of the meeting
14
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16
           // Prefix sum — accumulate the count changes to find the count at each time
17
           for (int i = 0; i < n - 1; ++i) {
18
               countDelta[i + 1] += countDelta[i];
19
20
21
           // Find and return the maximum count at any time, which is the minimum number of rooms required
           return *max_element(countDelta.begin(), countDelta.end());
Typescript Solution
  // Import necessary module for max element search
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const countChange: number[] = new Array(maximumTimePoint).fill(0); // Create an array to track the count changes, initialized to

20 // Find and return the maximum count at any time point, which is the minimum number of rooms required return max(countChange); 21 22 } 23 // Example usage: 25 // const intervals: number[][] = [[0, 30], [5, 10], [15, 20]]; 26 // const numberOfRooms: number = minMeetingRooms(intervals); 27 // console.log(numberOfRooms); // Should output the minimum number of meeting rooms required 28 <u> Time and Space Complexity</u> The provided Python code is meant to determine the minimum number of meeting rooms required for a set of meetings, represented by their start and end times. The code employs a difference array to keep track of the changes in the room occupancy count caused by the start and end of meetings, then uses accumulate to find the peak occupancy which gives the required number of rooms. **Time Complexity** The time complexity of the code is determined by three steps:

n is the number of intervals (meetings).

intervals but on a constant size.

Space Complexity

3. The use of accumulate which calculates the prefix sum of the delta array. In the worst case, this operation is O(m), where m is the size of the delta array, which is a constant of 1000010.

1. Initializing the delta list, which has a fixed length of 1000010. This step is in 0(1) since it does not depend on the number of

2. The first for loop that populates the delta array with +1 and -1 for the start and end times of meetings. It runs O(n) times, where

- The final time complexity is dominated by the larger of the two variables, which in this case is the constant time for using accumulate. Hence, the time complexity is O(m), which translates to O(1) since m is a constant.
- The space complexity of the code is determined primarily by the delta array.

1. The delta list, which has a fixed length of 1000010. This is a constant space allocation and does not depend on the input size.

2. No additional data structures that grow with the size of the input are used. Therefore, the space complexity is 0(1) due to the constant size of the delta array.