94. Binary Tree Inorder Traversal

Depth-First Search Binary Tree

Problem Description

tree traversal, there are three types of depth-first searches - inorder, preorder, and postorder. Specifically, the inorder traversal follows a defined sequence to visit the nodes: Visit the left subtree

The problem asks us to perform an inorder traversal on a binary tree and return the sequence of values from the nodes. In binary

- Visit the right subtree This pattern is recursive and is applied to each subtree within the tree. The result of performing an inorder traversal is that the

Visit the root node

nodes of the tree are visited in ascending order if the binary tree is a binary search tree. For this problem, we are required to

The proposed solution uses the Morris Traversal approach, which is an optimized way to do tree traversal without recursion and

without using extra space for a stack. The basic idea of Morris Traversal is to link the rightmost node of a node's left subtree back

to the node itself, which helps us to get back to the root node after we are done traversing the left subtree. Here's the process how we arrive at the Morris Traversal solution approach: Start with the root node.

• If the rightmost node has no right child (is not already linked back to the root), we create a temporary link from it to the root and move the

• If the rightmost node's right child is the root (already linked back), it means we have visited the left subtree already, so we add the root 's

collect the values of the nodes in the order they are visited and return them as a list.

Solution Approach

root to its left child.

value to the result list, unlink (restore the tree structure), and move to the right child of the root. This approach allows us to use the tree structure itself as a way to navigate through the tree without additional memory usage for

• If the root has no left child, it means this node can be visited now, so we add its value to the result list and move to its right child.

the call stack or an auxiliary stack, thus giving us the inorder sequence of node values in O(n) time with O(1) space complexity.

• If the root has a left child, find the rightmost node in the left subtree (the inorder predecessor of root).

The solution provided implements the Morris Traversal as the algorithm for inorder traversal of the binary tree. Here is a walkthrough of the implementation:

 The function inorderTraversal begins with an empty list ans, which will contain the sequence of node values in inorder. The main loop runs as long as there is a root to process. The steps in the loop correspond to the ideas discussed in the

If root.left is None, it implies there's no left subtree, and the root node can be visited. So, root.val is added to the ans list and root is updated to be root right, moving on to the next node in the inorder sequence.

loop.

approach.

problem.

intuition:

If root.left exists, this means we have a left subtree that needs to be processed first. We then find the inorder predecessor of the root by traversing rightwards (prev = prev.right) until we find a node that either has no right child or whose right child is the current root. This predecessor will act as a temporary bridge back to the root after we've

- finished with the left subtree.
- If the predecessor's (prev) right child is None, this means we haven't processed the left subtree yet. We, therefore, make a temporary link from the predecessor's right child to the current root (previright = root). This allows us to come back to the root after we're done with the left subtree. Then we move root to its left child and continue the
- <u>tree</u>'s structure (prev.right = None), and proceed with root.right. The loop continues until every node has been visited in the inorder sequence. Since we're altering the tree during traversal, the Morris Traversal uses no additional space for data structures like stacks or the system call stack, making it a very space-efficient

The result is a list of node values ans that have been collected in inorder. This list is then returned, providing the solution to the

This method achieves an O(n) time complexity for traversing through n nodes and O(1) space complexity, as it does not utilize

If the predecessor's right child is the current root, this indicates we've returned from traversing the left subtree, and

it's now time to visit the root. We, therefore, add root.val to the ans list, remove the temporary link to restore the

Example Walkthrough Let's consider a simple binary tree for our example:

Using the Morris Traversal approach, we would proceed as follows: We start at the root, which is 2. The root has a left child, so we find the inorder predecessor which is the rightmost node in

child, we make a temporary link from node 1 to node 2 and then move the root to its left child (1).

to visit this root node. Then we move to the right child of 2, which is node 3. Now the ans list is [1, 2].

As there are no more unvisited nodes left, and the right child of 3 is None, the traversal is complete.

the left subtree of 2 (which happens to be the node itself since it has no right child in its subtree). Since node 1 has no right

Now the current root is 1, which has no left child. Since there's no left subtree to process, we add 1 to the ans list. There is

We arrive back at 2 because of the temporary link. We remove that temporary link and add 2 to the ans list, as we now are

At node 3, since there is no left child to process, we visit this node and add its value to the ans list. Now ans = [1, 2, 3].

In this tree, we have three nodes, where 2 is the root node, 1 is to its left, and 3 is to its right. We want to perform an inorder

traversal, which would visit the nodes in the order 1, 2, 3, as 1 comes first in the left subtree, followed by 2, the root, and finally

also no right child, so we would follow the temporary link back to 2. After visiting node 1, we have ans = [1].

3 in the right subtree.

The final ans list is [1, 2, 3], which is indeed the inorder traversal of the given binary tree.

recursion or an explicit stack to maintain the state during the traversal.

- Note that during the entire process, no extra space was used for stack or recursion, and the tree's original structure was restored after it had been temporarily altered to maintain the traversal state. Solution Implementation
- # Initialize the output list to store the inorder traversal result = [] # Continue traversing until there are no more nodes to process
- # if it does not have a right child. This node will be our "predecessor" predecessor = root.left while predecessor.right and predecessor.right != root: predecessor = predecessor.right

If the predecessor's right child is not set to the current node,

If the predecessor's right child is set to the current node,

the tree structure. Then, move to the right child.

it means we have processed the left subtree, so add the current

node's value to the result and sever the temporary link to restore

set it to the current node and move to the left child of the current node

Find the rightmost node in the left subtree or the left child itself

If there is no left child, add the current node's value to the result

Python

class TreeNode:

class Solution:

Definition for a binary tree node.

self.val = val

while root:

else:

else:

self.left = left

self.right = right

def init (self, val=0, left=None, right=None):

and move to the right child

result.append(root.val)

if predecessor right is None:

root = root.left

predecessor.right = root

result.append(root.val)

predecessor.right = None

predecessor.right = root;

// If the right child is already set to the current node,

// Thus, we should visit the current node and remove the link.

// it means we are visiting the node the second time.

TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}

// If there is no left subtree, print the root and move to the right subtree.

while (predecessor->right != nullptr && predecessor->right != root) {

predecessor->right = root; // Link predecessor to the root.

root = root->left; // Move root to its left child.

// which means we have finished processing the left subtree.

// A link from the predecessor to the current root already exists,

// Navigate to the rightmost node of the left subtree or to the current root

// Establish a link from the predecessor to the current root, if it does not exist.

// Loop through all nodes of the tree using Morris Traversal technique.

result.push back(root->val): // Add the current node value.

root = root->right; // Move to the right subtree.

// Find the inorder predecessor of the current root.

// This vector will store the inorder traversal result.

root = root.left;

result.add(root.val):

root = root.right;

predecessor.right = null;

// Return the completed list of nodes in inorder

TreeNode(): val(0), left(nullptr), right(nullptr) {}

vector<int> inorderTraversal(TreeNode* root) {

TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}

TreeNode* predecessor = root->left;

if (!predecessor->right) {

// if the link is already established.

predecessor = predecessor->right;

def inorderTraversal(self, root: Optional[TreeNode]) -> List[int]:

predecessor = predecessor.right

and move to the right child

result.append(root.val)

predecessor = root.left

if predecessor.right is None:

root = root.left

predecessor.right = root

result.append(root.val)

root = root.right

Return the result of the inorder traversal

predecessor.right = None

if root.left is None:

root = root.right

Initialize the output list to store the inorder traversal

Continue traversing until there are no more nodes to process

If there is no left child, add the current node's value to the result

while predecessor.right and predecessor.right != root:

Find the rightmost node in the left subtree or the left child itself

If the predecessor's right child is not set to the current node,

If the predecessor's right child is set to the current node.

the tree structure. Then, move to the right child.

it means we have processed the left subtree, so add the current

node's value to the result and sever the temporary link to restore

if it does not have a right child. This node will be our "predecessor"

set it to the current node and move to the left child of the current node

} else {

return result;

* Definition for a binary tree node.

vector<int> result;

} else {

while (root != nullptr) {

if (!root->left) {

} else {

if root.left is None:

root = root.right

def inorderTraversal(self, root: Optional[TreeNode]) -> List[int]:

```
root = root.right
        # Return the result of the inorder traversal
        return result
Java
/**
 * Definition for a binary tree node.
 * public class TreeNode {
       int val;
       TreeNode left;
       TreeNode right;
       TreeNode() {}
       TreeNode(int val) { this.val = val; }
       TreeNode(int val, TreeNode left, TreeNode right) {
           this.val = val;
           this.left = left:
           this.right = right;
 *
 */
class Solution {
    public List<Integer> inorderTraversal(TreeNode root) {
        // Initialize an empty list to store the inorder traversal result
        List<Integer> result = new ArrayList<>();
        // Continue the process until all nodes are visited
        while (root != null) {
            // If there is no left child, visit the current node and go to the right child
            if (root.left == null) {
                result.add(root.val);
                root = root.right;
            // Find the inorder predecessor of the current node
                TreeNode predecessor = root.left:
                // Move to the rightmost node of the left subtree or
                // the right child of the predecessor if it's already set
                while (predecessor.right != null && predecessor.right != root) {
                    predecessor = predecessor.right;
                // If the right child of the predecessor is not set.
                // this means this is our first time visit this node, thus,
                // set the right child to the current node and move to the left child
                if (predecessor.right == null) {
```

C++

/**

};

public:

struct TreeNode {

TreeNode *left;

TreeNode *right;

int val;

class Solution {

```
result.push back(root->val); // Add the value of the current node.
                    predecessor->right = nullptr: // Remove the link to restore tree structure.
                    root = root->right;
                                                 // Move to the right subtree.
        return result; // Return the result vector containing the inorder traversal.
};
TypeScript
// Definition for a binary tree node.
interface TreeNode {
  val: number;
  left: TreeNode | null;
  right: TreeNode | null;
/**
* Performs an inorder traversal of a binary tree.
 * @param {TreeNode | null} root - The root node of the binary tree.
 * @returns {number[]} - An array of node values in the inorder sequence.
function inorderTraversal(root: TreeNode | null): number[] {
    // Base case: if the current root is null, return an empty array.
    if (root === null) {
        return [];
    // Recursive case:
    // 1. Traverse the left subtree and collect the values.
    // 2. Include the value of the current node.
    // 3. Traverse the right subtree and collect the values.
    // Then concatenate them in inorder sequence.
    return
        ...inorderTraversal(root.left). // Left subtree values
                                       // Current node value
        root.val,
        ...inorderTraversal(root.right) // Right subtree values
    ];
# Definition for a binary tree node.
class TreeNode:
    def init (self, val=0, left=None, right=None):
        self.val = val
        self.left = left
        self.right = right
```

The code implements the Morris In-order Traversal algorithm for a binary tree. Let's analyze both the time and space complexity:

The time complexity of the algorithm is O(n), where n is the number of nodes in the binary tree. Each node gets visited exactly twice in the worst case, once to establish the temporary link to its in-order predecessor and once to remove it and visit the node

itself. The otherwise O(n) traversal is not affected by this temporary linking as it only adds a constant amount of work for each

Space Complexity

Time Complexity

node.

class Solution:

result = []

while root:

else:

else:

return result

Time and Space Complexity

The space complexity of the algorithm is 0(1). Unlike traditional in-order traversal using recursion (which could lead to 0(h) space complexity where h is the height of the tree due to the call stack), the Morris Traversal does not use any additional space for auxiliary data structures such as stacks or recursion. It uses the given tree's null right pointers to temporarily store the successors of nodes, thereby using the tree itself to guide the traversal.