

Problem Description

provided with an array of these intervals, and each interval is guaranteed not to overlap with any other. The intervals are sorted in ascending order based on their start times. Our task is to insert a new interval into this array while maintaining the order and the non-overlapping property of the intervals. If inserting the new interval causes any overlap, we must merge the overlapping intervals into a single interval that covers all the ranges.

Our goal is to return the new list of intervals after the insertion has been completed correctly.

The problem requires us to handle a collection of intervals, with each interval represented by a start and end time (inclusive). We're

Intuition

To solve this problem, we must first understand how to merge intervals. Merging involves combining overlapping intervals into one

that spans the entire range covered by any overlapping intervals. Since the existing collection of intervals is already sorted and non-overlapping, they can be left as they are. We only need to focus on the newInterval.

We start by simply appending newInterval to our intervals array. Even though this may break the sorting, we're going to merge any

intervals that need it anyway, which will handle any issues caused by the insertion.

Now, the merge process begins. We assume we have at least one interval in the array to start with. We'll compare each interval with

the last interval in our answer list. There are two cases to consider:

1. If there is no overlap (the current interval's start time is greater than the last interval's end time in the answer list), we can safely

add the current interval to the answer list.

2. If there is an overlap (the current interval's start time is less than or equal to the last interval's end time in the answer list), we

merge by updating the end time of the last interval in the answer list. The end time after the merge will be the maximum end

The merge function sorts the updated intervals array and performs the above steps to ensure that the resulting array has no overlaps. It's important to note that sorting is required only if the newInterval was inserted in such a way that it breaks the original order. Since we append newInterval directly, sorting is indeed necessary as the first step of merging. After the merge is completed, the

answer list will be returned, representing the intervals after the new interval has been inserted correctly.

interval merging. Here is a breakdown of the approach based on the provided Python code:

first can overlap with it. Hence, we can safely initialize ans with just the first interval.

Solution Approach

The solution to the problem follows a fairly straightforward algorithm, making use of simple list operations and the concept of

newInterval into the existing intervals list. This is straightforward as we can use the append() method to add newInterval to intervals. At this stage, we're not concerned with maintaining the sorted order of intervals because our next step is to

time between the overlapped intervals.

explicitly sort the list.

1 intervals.append(newInterval)

1. Append newInterval to intervals: Before we can merge the intervals to eliminate any overlaps, we need to include the

- 2. Define a merge function: The purpose of this function is to merge any overlapping intervals. We expect merge to handle all cases, even if we call it with an unsorted or overlapping list. The function first sorts the intervals list, which is necessary since we've just appended a newInterval at the end without regard to sorting.
 1 def merge(intervals: List[List[int]]) -> List[List[int]]:
- 1 def merge(intervals: List[List[int]]) -> List
 2 intervals.sort()
 3 # ... rest of the merging logic goes here

1 ans = [intervals[0]]

else:

1 return ans

the algorithm handles this:

1 [[1,2]]

1 [[1,2], [3,5]]

1 [[1,2], [3,9]]

1 [[1,2], [3,10]]

1 [[1,2], [3,10], [12,16]]

4. Iterate over the rest of the intervals and merge if necessary: This step is the core of the merging logic. For each interval (after the first), we compare it with the last interval in ans. If the intervals do not overlap, we append the current interval to ans. If they

do overlap, we update the end time of the last interval in ans to be the maximum of its own end and the current interval's end.

3. Initialize the answer list ans with the first interval: Given that merge starts with a sorted list, we know that no interval before the

```
5 ans [-1] [1] = max(ans [-1] [1], e)

5. Return the answer list ans after all intervals have been processed: After the loop concludes, ans contains the merged intervals
```

and is returned as the final result of the insert function.

ans.append([s, e])

1 for s, e in intervals[1:]:

if ans[-1][1] < s:

in the given solution, it remains an academic point here. The space complexity is 0(n) as well, since we are generating a list of intervals as output.

By calling the merge function after appending newInterval to intervals, we handle the task in a single pass through the sorted list of

intervals, making efficient use of the fact that we only need to check each interval against the last one in the ans list for potential

The overall time complexity of this approach is dominated by the sorting operation, which is 0(n log n) where n is the number of

intervals, including the new interval. However, if the intervals were already sorted (aside from the appended newInterval), this could

potentially be optimized to O(n) by carefully inserting newInterval into the correct position. Since this optimization is not presented

```
merging.

Example Walkthrough
```

1 Current intervals: [[1,2], [3,5], [6,7], [8,10], [12,16]]

After appending the new interval, it becomes:

1 [[1,2], [3,5], [6,7], [8,10], [12,16], [4,9]]

1 [[1,2], [3,5], [4,9], [6,7], [8,10], [12,16]]

with [1,2], so it is appended to ans:

[3,5] to the end time of [4,9]:

Let's walk through a simple example to illustrate the solution approach described.

Suppose we have the following set of intervals already sorted and non-overlapping:

1. Append newInterval to intervals: Initially, our list of intervals is:

1 [[1,2], [3,5], [6,7], [8,10], [12,16]]

2. Sort the intervals: After appending the newInterval, the list of intervals has to be sorted again since the newInterval was added

The task is to insert a new interval [4,9] into this set while maintaining the sorted order and non-overlapping intervals. Here's how

3. Initialize the answer list ans with the first interval: The ans list starts as:

at the end without considering the order. The intervals list after sorting:

```
4. Iterate over the rest of the intervals and merge if necessary: The second interval in the sorted list is [3,5]. There is no overlap
```

The next interval [6,7] is already covered by [3,9], so no new interval is added, but the same interval remains. The interval [8,10] also gets merged into [3,9], resulting in:

Next, we encounter the newInterval which is [4,9]. Since it overlaps with [3,5], we merge them by updating the end time of

```
Finally, the interval [12,16] does not overlap with [3,10], and is appended to ans:

1 [[1,2], [3,10], [12,16]]
```

This function merges overlapping intervals.

intervals.sort(key=lambda x: x[0])

for start, end in intervals[1:]:

else:

return merged_intervals

intervals.append(new_interval)

return merge(intervals)

def merge(intervals: List[List[int]]) -> List[List[int]]:

if merged_intervals[-1][1] < start:</pre>

Return the merged list of intervals.

Add the new interval to the existing list of intervals.

// Function to insert a new interval into an existing list of intervals

int[][] expandedIntervals = new int[intervals.length + 1][2];

public int[][] insert(int[][] intervals, int[] newInterval) {

mergedIntervals.add(intervals[i]);

// Convert the list back into an array and return

// Add the new interval to the end of the intervals vector

// Sort the intervals in ascending order based on the start times

// Add the first interval to the merged list as a starting point

// Iterate through the intervals starting with the second interval

// it means we can add it as a new entry to the merged list

intervals.emplace_back(newInterval);

return merge(intervals);

// Merge the updated list of intervals

// Method to merge overlapping intervals in a list

sort(intervals.begin(), intervals.end());

mergedIntervals.emplace_back(intervals[0]);

for (int i = 1; i < intervals.size(); ++i) {</pre>

// This will hold the merged intervals

vector<vector<int>> mergedIntervals;

vector<vector<int>> merge(vector<vector<int>>& intervals) {

return mergedIntervals.toArray(new int[mergedIntervals.size()][]);

// Method to insert a new interval into the list of existing intervals and then merge them

// If the current interval does not overlap with the last interval in the merged list,

mergedIntervals.back()[1] = max(mergedIntervals.back()[1], intervals[i][1]);

vector<vector<int>> insert(vector<vector<int>>& intervals, vector<int>& newInterval) {

} else {

First we sort the intervals based on the starting times.

Python Solution

1 from typing import List

This illustrates how the intervals are correctly merged and the final list of intervals is obtained by following the solution approach.

5. Return the answer list ans after all intervals have been processed: The final ans returned by the algorithm is:

def insert(self, intervals: List[List[int]], new_interval: List[int]) -> List[List[int]]:

merged_intervals = [intervals[0]] # Initialize with the first interval.

merged_intervals.append([start, end]) # Keep it separate.

They overlap, so we merge them by updating the end time of

merged_intervals[-1][1] = max(merged_intervals[-1][1], end)

Call the merge function to merge any overlapping intervals including the new one.

// Initialize an expanded array to hold the existing intervals and the new interval

If the current interval does not overlap with the last merged interval.

Iterate through the rest of the intervals to merge overlapping ones.

the last interval in the merged list if needed.

```
Java Solution
```

class Solution {

class Solution:

10

11

12

13

14

15

16

17

18

19

20

21

22

23

24

25

26

27

28

2

42

43

44

45

46

47

48

49

50

51

53

52 }

C++ Solution

1 class Solution {

2 public:

8

9

10

11

12

13

14

15

16

17

18

19

20

21

22

23

24

25

31

32

```
// Copy existing intervals into the expanded array
 8
            for (int i = 0; i < intervals.length; ++i) {</pre>
 9
                expandedIntervals[i] = intervals[i];
10
11
12
            // Add the new interval to the end of the expanded intervals array
13
14
            expandedIntervals[intervals.length] = newInterval;
15
16
            // Merge overlapping intervals and return the result
17
            return merge(expandedIntervals);
18
19
20
        // Helper function to merge overlapping intervals
21
        private int[][] merge(int[][] intervals) {
            // Sort the intervals based on the starting times
22
23
            Arrays.sort(intervals, (a, b) -> Integer.compare(a[0], b[0]));
24
            // List to hold the merged intervals
25
26
            List<int[]> mergedIntervals = new ArrayList<>();
27
28
            // Add the first interval to the list as initialization
29
            mergedIntervals.add(intervals[0]);
30
31
            // Iterate through each interval and merge if necessary
32
            for (int i = 1; i < intervals.length; ++i) {</pre>
33
                // Get the start and end times of the current interval
34
                int start = intervals[i][0];
35
                int end = intervals[i][1];
36
37
                // Get end time of the last interval in the list.
38
                int lastEnd = mergedIntervals.get(mergedIntervals.size() - 1)[1];
39
40
                // If the current interval does not overlap with the previous, simply add it
                if (lastEnd < start) {</pre>
41
```

// Otherwise, merge the current interval with the previous one by updating the end time

mergedIntervals.get(mergedIntervals.size() - 1)[1] = Math.max(lastEnd, end);

if (mergedIntervals.back()[1] < intervals[i][0]) { mergedIntervals.emplace_back(intervals[i]); } else { // If they overlap, merge the current interval with the last interval of the merged list // by updating the ending time of the last interval in mergedList</pre>

```
33
34
35
           // Return the list of merged intervals
36
           return mergedIntervals;
37
38 };
39
Typescript Solution
   function insert(intervals: number[][], newInterval: number[]): number[][] {
       let [start, end] = newInterval; // Destructure the start and end of the new interval
       const result: number[][] = []; // Initialize an array to hold the merged intervals
       let inserted = false;
                                       // Flag to check if new interval has been added
       // Loop through each interval in the sorted list
       for (const [intervalStart, intervalEnd] of intervals) {
           if (end < intervalStart) { // If the end of newInterval is before the current interval</pre>
               if (!inserted) {
                                  // And if newInterval hasn't been inserted yet
 9
                   result.push([start, end]); // Insert the newInterval
10
11
                   inserted = true;
                                              // Set the flag as inserted
12
13
               result.push([intervalStart, intervalEnd]); // Add the current interval
           } else if (intervalEnd < start) { // If the current interval ends before newInterval starts</pre>
14
15
               result.push([intervalStart, intervalEnd]); // Add the current interval
           } else {
16
                                              // If intervals overlap
               start = Math.min(start, intervalStart); // Merge intervals by taking the min start
17
               end = Math.max(end, intervalEnd);  // And max end
18
19
20
21
       // If newInterval was not inserted, add it to the end
22
       if (!inserted) {
23
           result.push([start, end]);
24
25
26
       return result; // Return the merged list of intervals
27 }
28
```

1. **Sorting**: The sort() function in Python uses the Timsort algorithm, which has a time complexity of $0(n \log n)$ where n is the number of intervals. Since we are appending a new interval before sorting, the sorting step will operate on n + 1 intervals, but

additional space.

Time Complexity

Time and Space Complexity

operation contributes to the total time complexity:

2. **Merging**: The merge function iterates through the sorted list of intervals once to combine overlapping intervals. This is a linear pass, which means it runs in O(n) time, considering n as the number of intervals including the new one we added.

The given code consists of two main operations: sorting the list of intervals, and then merging these intervals. Here's how each

log n).

Space Complexity

Combining both steps, the time complexity of the algorithm is dominated by the sorting step, so the overall time complexity is 0(n

- The space complexity is determined by the extra space used by the algorithm. In this case, we have:

 1. The additional list ans that is initially a copy of the first interval, and worst-case, could be extended to include all intervals if none
- overlap. This results in a worst-case space complexity of 0(n).

 2. The in-place sort() generally has a space complexity of 0(1) for the actual sorting since Timsort is a hybrid stable sorting algorithm that takes advantage of the existing order in the list. Yet, it might require a temporary space of up to 0(n) in the worst case when merging runs. But since we are considering the space for the output as separate, we do not count this towards

Thus, the overall space complexity of the algorithm is 0(n).

this does not change the overall complexity class, so it remains $O(n \log n)$.