2457. Minimum Addition to Make Integer Beautiful

Medium Greedy Math

Problem Description

In this problem, we are given two positive integers: n, which represents the number we're starting with, and target, a threshold value for the sum of digits of a number. A number is considered beautiful if the sum of its individual digits is less than or equal to the given target. The task is to find the minimum non-negative integer x that, when added to n, results in a beautiful number. It's guaranteed that there is always a way to turn n into a beautiful by adding such an x.

The intuitive approach to solve this problem involves incrementing n gradually until we find a number that meets the condition of

Intuition

being beautiful. However, incrementing n by 1 and checking each time is inefficient. A more effective strategy should skip over likely candidates that clearly would not meet the condition. Observing that every time you reach a digit 9 in the process of incrementing n, the next increment will carry over and turn that 9 into a 🛛, increasing the next digit to the left by one, which is significant. Rather than dealing with individual increments, we want

to make more substantial jumps to avoid unnecessary checks. For instance, if n ends in a series of 9s (like 299), we know the next beautiful number will be at least 300. The solution finds the

least significant non-9 digit, increments that digit by 1, turns all the digits to its right into 0, and computes the difference from the original number n. That difference is our x, which when added to n will bypass the unnecessary candidates and get us closer to a

beautiful number. This effective jump method ensures that we do not perform redundant checks, and that we will reach the solution in far fewer steps than incrementing by 1 each time. The function f(x) in the provided solution calculates the sum of the digits of x, which is used for determining if the current number n + x is beautiful or if we need to make another jump.

Solution Approach The implementation of the solution can be broken down into the following parts:

Sum of Digits Function (f(x)): This function calculates the sum of the digits of a given integer x. It does so iteratively by

taking x % 10 to get the least significant digit, adding it to the sum y, and then using x //= 10 to remove the least significant

digit from x. This loop continues until x is reduced to zero.

Main Logic: In the makeIntegerBeautiful method of the Solution class, x is initialized to 0. This x is the additional amount we

effectively skipping all the intermediary numbers that would also not qualify as beautiful.

- will need to add to n to make it beautiful. The while loop checks whether f(n + x) > target. As long as this condition is true, the current n + x is not beautiful, and we need to increase x. a. Finding the Next Candidate: Within the loop, y = n + x is set to the current number we're evaluating. We are looking for
- is 0. Simultaneously, p is multiplied by 10, effectively keeping track of the place value of the first non-zero digit from the right. b. Jumping to the Next Significant Candidate: Once a non-zero least significant digit is found, the code calculates (y // 10 + 1) * p - n. This operation turns the least significant non-zero digit into 0 and increments the next digit to the left by 1,

the least significant non-zero digit in y. During this, the code progressively divides y by 10 if the current least significant digit

beautiful. At this point, the function returns x which is the minimum increment needed to convert n into a beautiful number. This algorithm effectively uses a greedy approach to jump through potential candidates for beautiful numbers. By identifying the digit increments that lead to the most significant change, the algorithm minimizes the number of operations needed to find the correct value of x. It is a more optimal solution than incrementing by 1 and checking each number individually.

Loop Exit and Return Value: Eventually, the while loop will exit when $f(n + x) \ll target$, which means n + x is now

Let's consider a small example to illustrate the solution approach. Suppose we have n = 28 and target = 10. We're tasked with finding the minimum non-negative integer x that can be added to n to result in a number where the sum of its digits is less than or equal to target. First, apply the Sum of Digits Function f(x) to n to see if it's already beautiful. The sum of digits of 28 is 2 + 8 = 10, which

equals the target. Since we need the sum to be less than or equal to the target, n is already beautiful, so x = 0.

In this case, we get lucky on the first try, but let's consider a slightly altered example to show the rest of the process: Let's

greater than 10.

(2 + 1) * 10 - 29. This equals 30 - 29 = 1. So x = 1.

Putting all that through the given markdown template, it will look as below:

Function to compute the sum of digits of an integer 'x'.

def sum_of_digits(x: int) -> int:

total_sum += x % 10

temp_number = n + increments

while sum_of_digits(n + increments) > target:

total_sum = 0

x //= 10

return total_sum

power_of_ten = 10

while x > 0:

Example Walkthrough

Start the while loop and set y = n + x, which is 29 currently. Then, search for the least significant non-9 digit. The least significant digit is 9, and it's also the non-9 digit we're looking for as n has only two digits. The place value p corresponding to this digit is 10.

say we have n = 29 and the same target of 10. The sum of digits of 29 is 2 + 9 = 11, which is greater than the target.

Now, commence the Main Logic. Initialize x to 0, and check if f(n + x) > target. Indeed, f(29 + 0) = f(29) = 11, which is

Perform a jump as per the Jumping to the Next Significant Candidate: Calculate (y // 10 + 1) * p - n, which simplifies to

After the iteration, n + x is 29 + 1 = 30. Using function f(x), we find that f(30) = 3 + 0 = 3, which is less than target. Since

- f(n + x) <= target, the while loop exits.</pre> Return x, which is 1, as the minimum increment needed to make 29 beautiful with respect to the target 10.
- 2. **Main Logic**: Initialize `x` to `0`. - We enter the while loop since f(n + x) = f(29 + 0) = 11 is greater than the target.

4. **Jump to Next Significant Candidate**: Execute the jump calculation to get x. Now x = (y // 10 + 1) * 10 - n

5. **Verification and Loop Exit**: The new value of `n + x` is `30`. Since `f(30) = 3`, it meets the condition `(f(n

3. **Finding the Next Candidate**: With y = 29 and p = 10, we find that the least significant digit is 9.

We are given n = 29 and target = 10. The goal is to find the smallest x that can be added to n to make the su

1. **Sum of Digits Calculation**: The sum of digits for `n` is 11 (`2 + 9`), which is greater than the target. Hence,

- 6. We return the value x = 1 as the required number to add to n to make it beautiful.
- Solution Implementation

increments = 0 # Variable to keep track of how much we need to add to 'n' to make it beautiful.

class Solution: def makeIntegerBeautiful(self, n: int, target: int) -> int:

Loop until the sum of digits of 'n + increments' is greater than 'target'.

Compute increments such that 'n + increments' eliminates trailing zeros,

increments = (temp_number // 10 + 1) * power_of_ten - n

print(result) # Output depends on the function logic and provided parameters

Return the total amount required to add to 'n' to make it beautiful.

and reduces digit sum. Calculate the next temp number and adjust increments.

Find trailing zeros by reducing 'temp_number' until it's not divisible by 10. while temp_number % 10 == 0: temp_number //= 10 power_of_ten *= 10 # Increase power of 10 correspondingly.

Example usage:

sol = Solution()

return increments

int sum = 0;

sum += x % 10; // Add the last digit to 'sum'

while (sumOfDigits(n + addition) > target) {

// Skip over the trailing zeros in 'y'

function makeIntegerBeautiful(n: number, target: number): number {

const calculateDigitSum = (x: number): number => -

let addition = 0; // Initialize the addition to zero.

// Loop to add each digit to the sum.

while (x > 0) {

// Function to calculate the sum of the digits of an integer 'x'.

return digitSum; // Return the calculated sum of the digits.

digitSum += x % 10; // Add the rightmost digit to the digit sum.

x = Math.floor(x / 10); // Remove the rightmost digit from 'x'.

let digitSum = 0; // Initialize the digit sum to zero.

long long y = n + addition;

while (y % 10 == 0) {

y /= 10;

long long nextPowerOfTen = 10;

nextPowerOfTen *= 10;

 $x \neq 10$; // Remove the last digit from 'x'

long long addition = 0; // The amount to add to 'n' to make it beautiful

// Keep increasing 'n' until the sum of its digits is equal to or less than 'target'

addition = (y / 10 + 1) * nextPowerOfTen - n; // Calculate the next amount to add

return addition; // Return the amount that needs to be added to 'n' to make it beautiful

// This function computes the minimal positive integer that should be added to 'n' to make the sum of its digits less than or equ

while (x) {

return sum;

};

result = sol.makeIntegerBeautiful(123, 12)

Python

```
Java
class Solution {
    // Method to adjust a number n to make its digit sum equal to a specified target
    public long makeIntegerBeautiful(long n, int target) {
        long adjustment = 0; // Initialize an adjustment value as 0
       // Loop until the sum of digits of n + adjustment is greater than the target
        while (sumOfDigits(n + adjustment) > target) {
            long temp = n + adjustment; // Create a temporary variable to hold n + adjustment
            long multiplier = 10;  // Initialize a multiplier for finding the next number divisible by 10
            // Find the number of trailing zeros in the current number
            while (temp % 10 == 0) {
                                       // Remove the trailing zero
                temp /= 10;
                temp /= 10; // Remove the trailing zero
multiplier *= 10; // Increase the multiplier by a factor of 10
           // Calculate the next adjustment value
            // It's like increment the number until it has no trailing zeros and then subtract n
            adjustment = (temp / 10 + 1) * multiplier - n;
        return adjustment; // Return the final adjustment value
    // Helper method to calculate the sum of digits of a given number x
    private int sumOfDigits(long x) {
        int sum = 0; // Initialize sum as 0
       while (x > 0) {
            sum += x % 10; // Add the last digit to sum
                           // Remove the last digit
            \times /= 10;
        return sum; // Return the final sum of digits
C++
class Solution {
public:
    // Function to add a certain amount to a number 'n' to make the sum of its digits equal to 'target'
    long long makeIntegerBeautiful(long long n, int target) {
        // Define a lambda function to calculate the sum of digits of a given number.
        auto sumOfDigits = [](long long x) {
```

};

};

TypeScript

```
// Loop until the sum of the digits of (n + addition) is not greater than 'target'.
      while (calculateDigitSum(n + addition) > target) {
          let modifiedN = n + addition; // The modified value of 'n' after the addition.
          let multiplier = 10; // A multiplier used to find the next significant digit to increment.
          // Loop to disregard trailing zeros in the modified 'n' value.
          while (modifiedN % 10 === 0) {
              modifiedN = Math.floor(modifiedN / 10); // Divide by 10 to remove the trailing zero.
              multiplier *= 10; // Update the multiplier for the next significant digit.
          // Calculate the value to be added so that the next addition results in a digit sum less than or equal to 'target'.
          addition = (Math.floor(modifiedN / 10) + 1) * multiplier - n;
      return addition; // Return the least number to add to 'n' to make it beautiful.
  // Example usage:
  // let result = makeIntegerBeautiful(1234, 10);
  // console.log(result); // Shows the minimal positive integer addition to make '1234' have a digit sum not greater than '10'.
class Solution:
   def makeIntegerBeautiful(self, n: int, target: int) -> int:
       # Function to compute the sum of digits of an integer 'x'.
        def sum_of_digits(x: int) -> int:
            total_sum = 0
           while x > 0:
               total_sum += x % 10
               x //= 10
            return total sum
        increments = 0 # Variable to keep track of how much we need to add to 'n' to make it beautiful.
       # Loop until the sum of digits of 'n + increments' is greater than 'target'.
       while sum_of_digits(n + increments) > target:
            temp_number = n + increments
            power_of_ten = 10
           # Find trailing zeros by reducing 'temp_number' until it's not divisible by 10.
           while temp_number % 10 == 0:
               temp_number //= 10
               power_of_ten *= 10 # Increase power of 10 correspondingly.
            # Compute increments such that 'n + increments' eliminates trailing zeros,
            # and reduces digit sum. Calculate the next temp number and adjust increments.
            increments = (temp_number // 10 + 1) * power_of_ten - n
       # Return the total amount required to add to 'n' to make it beautiful.
        return increments
# Example usage:
# sol = Solution()
# result = sol.makeIntegerBeautiful(123, 12)
# print(result) # Output depends on the function logic and provided parameters
Time and Space Complexity
Time Complexity
  The time complexity of the given code is determined by two nested loops: the while loop that iterates until f(n + x) is no longer
  greater than target, and the inner while loop that determines the next value of x.
```

worst-case scenario, the digits of n are large, and it takes several increments of n to reduce the sum of its digits to target. For each increment, the inner loop runs until a non-zero digit is found (dividing by 10 each time). The cost of an iteration of the inner

The outer while loop can be executed potentially many times depending on the initial value of n and the target value. In the

while loop is O(log(n)) as it is iterating over the digits of y, which is at most O(log(n)) digits long. However, the inner loop execution time is offset by the fact that on each iteration, the value of x is increased significantly due to the multiplication by p (which is increased by a factor of 10 for each trailing zero of y). This effectively reduces the number of times the outer loop executes because the next n + x will have fewer trailing zeroes and thus will return a smaller digit sum f(n + x) more quickly. It could lead to the outer loop having less than linear time complexity in n on average. This complexity is hard to

Given this, we can cautiously estimate the worst-case time complexity to be O(log(n)^2) but the actual time complexity may vary greatly and could be much lower on average, depending on the input values.

define precisely without specifics about the distribution of n and target.

Space Complexity

The space complexity is O(1), which means it requires constant additional space regardless of the input size. This is because the space used does not increase with the size of n or the target. Only a fixed number of variables (x, y, p) are used to store intermediate results and they do not depend on the size of the input.