1930. Unique Length-3 Palindromic Subsequences

Problem Description

Hash Table

String

Prefix Sum

Medium

The problem requires us to determine the number of unique palindromic subsequences of length three that can be extracted from a given string s. Recall the definitions for a palindrome and a subsequence: • A palindrome is a sequence of characters that reads the same forward and backward, like "abcba" or "mom".

- A subsequence is derived from the original string by deleting some characters without changing the order of the remaining characters. For instance, "ace" is a subsequence of "abcde".
- With this in mind, we are to focus on palindromes that have a length of exactly three characters. The key term here is unique—if a palindromic subsequence can be formed in multiple ways, it still counts as one unique instance.

Intuition To devise a solution, let's consider the characteristics of a three-character palindrome: it begins and ends with the same

character, with a different third character sandwiched in between. A three-character palindrome will always have the form "XYX".

To find such palindromes, we need to:

1. Find the first and last occurrence of a character "X" in the string. 2. Look between those occurrences for any characters "Y" that can form a palindrome "XYX". Our algorithm iterates through each letter of the alphabet. For each letter, it finds the leftmost (1) and the rightmost (r)

occurrence in the string s. If the indices 1 and r are the same, it means there is only one instance of that letter, and thus a

characters. The size of this set gives the number of unique characters that can form a palindrome with the current character as

The solution optimizes searching using the find() and rfind() functions. find() returns the lowest index of the substring if

- three-character palindrome cannot be formed with that letter as the start and end. If the indices are different, and particularly if r -1 > 1, it ensures that there is at least one character between them to potentially create a palindrome.
- Inside the slice s[1 + 1 : r] (which excludes the outer characters), we convert the substring into a set to get unique

the first and last letter. We sum up these counts for all characters of the alphabet to get our answer.

ascii_lowercase from the string module contains all lowercase letters of the alphabet.

found, else returns -1. rfind() functions similarly but returns the highest index. Solution Approach

The implementation of the solution provided above leverages a couple of Python's string methods and a simple loop to find a

Iterate over the alphabet: Using a for loop, we iterate through each character c in the ascii_lowercase. The

Finding character positions: For each character c, we use sifind(c) to get the index 1 of the first occurrence and

solution efficiently. Here's the breakdown of the approach: Initialization: We start by setting up a counter ans. This variable will hold the cumulative count of unique palindromes.

s.rfind(c) to get the index r of the last occurrence of that character in the string s.

return ans

Example Walkthrough

Check for valid palindrome positions: We then check if r - 1 > 1. This condition is crucial, as it ensures there are at least two characters between the first and last occurrence to potentially form a 3-character palindrome. o If 1 and r are the same, it would mean that only one instance of the character c exists in s and thus a palindrome cannot be formed.

character to form a palindrome. Counting unique middle characters: If the condition r - 1 > 1 is satisfied, we take a slice of the string from 1 + 1 to r to

∘ If 1 and r are different but r - 1 <= 1, it would mean the character c occurs in consecutive positions, leaving no room for a middle

duplicate characters. **Update the count**: The length of the set gives the number of unique characters that can form a palindrome with the character

isolate the characters between the first and last occurrence of c. We then convert this substring into a set to remove

Return the result: Once the loop has gone through each letter in the alphabet, ans will contain the total count of unique

- Here is the critical algorithm part in the code enclosed in backticks for markdown display: for c in ascii lowercase: l, r = s.find(c), s.rfind(c) if r - l > 1:
- utilizing the built-in functions provided by Python for string manipulation.

This code snippet clearly highlights the search for the leftmost and rightmost occurrences of each character and the calculation

of the number of distinct middle characters that can form a palindrome with the current character. It does so effectively by

Let's take the string s = "abcbabb" as an example to illustrate the solution approach. The strategy is to identify unique

Initialization: We initiate ans = 0 to accumulate the count of unique palindromes. Iterate over the alphabet: We start checking for each character in ascii_lowercase. We'll illustrate this with a few selected

c sandwiched between them. We add this number to our counter ans.

ans += len(set(s[l + 1 : r]))

palindromic subsequences of the format "XYX" within s.

r = s.rfind('a') results in 0. (last occurrence of 'a')

l = s.find('b') results in 1. (first occurrence of 'b')

r = s.rfind('b') results in 6. (last occurrence of 'b')

■ Since r - 1 is greater than 1, we have a valid situation.

palindromic subsequences within the given string s.

def countPalindromicSubsequence(self, s: str) -> int:

for char in ascii lowercase:

left index = s.find(char)

right_index = s.rfind(char)

if right index - left index > 1:

Initialize the count of unique palindromic subsequences

Iterate through each character in the lowercase English alphabet

count += len(set(s[left_index + 1 : right_index]))

// Method to count the unique palindromic subsequences in the given string

for (char currentChar = 'a'; currentChar <= 'z'; ++currentChar) {</pre>

int leftIndex = s.index0f(currentChar);

// last occurrence of 'currentChar'

// last occurrence of 'currentChar'

count += uniqueChars.size();

int countPalindromicSubsequence(string s) {

let uniqueChars = new Set<string>();

countPaliSubseq += uniqueChars.size();

uniqueChars.add(s[i]);

return countPaliSubseq;

count = 0

return count

Time Complexity

Space Complexity

Time and Space Complexity

from string import ascii_lowercase

for char in ascii lowercase:

left index = s.find(char)

right_index = s.rfind(char)

for (let i = firstIndex + 1; i < lastIndex; i++) {</pre>

// Insert unique characters into the Set

// Return the total count of palindromic subsequences

def countPalindromicSubsequence(self, s: str) -> int:

Initialize the count of unique palindromic subsequences

Iterate through each character in the lowercase English alphabet

count += len(set(s[left_index + 1 : right_index]))

Return the final count of unique palindromic subsequences

Find the first (leftmost) and last (rightmost) indices of the character in the string

where 'c' is the current character and 'X' represents any unique set of characters

If so, add the number of unique characters between them to the count

This creates a palindromic subsequence of the form "cXc"

int rightIndex = s.lastIndexOf(currentChar);

Set<Character> uniqueChars = new HashSet<>();

// Return the total count of unique palindromic subsequences

// Initialize the count of palindromic subsequences to 0

// Find the first and last occurrence of 'currentChar' in the string

// Create a HashSet to store unique characters between the first and

// The number of unique characters added to the HashSet is the number

// of palindromic subsequences starting and ending with 'currentChar'

// Use a Set to store unique characters between the first and last occurrence

// Iterate over the characters between the first and last occurrence

// Increment the count by the number of unique characters found

// Iterate over the substring that lies between the first and

Return the final count of unique palindromic subsequences

palindromic subsequences of length three in our input string s. This value is then returned.

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characters from s: 'a', 'b', and 'c'.
Finding character positions:
    For character 'a':
   • l = s.find('a') results in 0. (first occurrence of 'a')
```

■ Since r - 1 is not greater than 1, we do not have enough space to form a 3-character palindrome with 'a', so we move on.

Check for valid palindrome positions: For character 'b', the condition r - 1 > 1 is true (6 - 1 > 1), indicating potential for 3-

Counting unique middle characters: We extract the substring s[l + 1 : r] which is "cbab". Converting this to a set gives

Return the result: After iterating through all alphabet characters, assume we found no additional characters that can form a

This walkthrough provides a clear example of the steps outlined in the solution approach, demonstrating the counting of unique

Update the count: The set length for character 'b' as the outer character is 3, meaning we have 'bcb', 'bab', and 'bab' as unique palindromic subsequences. Since 'bab' can be formed by different indices, it still counts as one. We add 3 to ans,

Solution Implementation

class Solution:

count = 0

return count

Java

class Solution {

making ans = 3.

{'c', 'b', 'a'}.

character palindromes.

For character 'b':

For character 'c': ■ Similarly, we would find l = 2, r = 2, so no palindrome can be formed, and we move on.

Find the first (leftmost) and last (rightmost) indices of the character in the string

Check if there is more than one character between the leftmost and rightmost occurrence

where 'c' is the current character and 'X' represents any unique set of characters

If so, add the number of unique characters between them to the count

This creates a palindromic subsequence of the form "cXc"

unique palindromic subsequence. Therefore, our final answer for string s is ans = 3.

- **Python** from string import ascii_lowercase
 - public int countPalindromicSubsequence(String s) { // Initialize the count of unique palindromic subsequences to 0 int count = 0; // Iterate through all lowercase alphabets

for (int i = leftIndex + 1; i < rightIndex; ++i) {</pre> // Add each character in the substring to the HashSet uniqueChars.add(s.charAt(i));

return count;

#include <string>

class Solution {

public:

using namespace std;

#include <unordered set>

```
int countPaliSubseq = 0;
        // Iterate over all lowercase alphabets
        for (char c = 'a'; c <= 'z'; ++c) {
            // Find the first and last occurrence of the current character
            int firstIndex = s.find first of(c);
            int lastIndex = s.find_last_of(c);
            // Use an unordered set to store unique characters between the first and last occurrence
            unordered_set<char> uniqueChars;
            // Iterate over the characters between the first and last occurrence
            for (int i = firstIndex + 1; i < lastIndex; ++i) {</pre>
                // Insert unique characters into the set
                uniqueChars.insert(s[i]);
            // Increment the count by the number of unique characters found
            countPaliSubseq += uniqueChars.size();
        // Return the total count of palindromic subsequences
        return countPaliSubseq;
TypeScript
// Import necessary features from the standard utility library
import { Set } from "typescript-collections";
// Function that counts the number of unique palindromic subsequences in a string
function countPalindromicSubsequence(s: string): number {
    // Initialize the count of palindromic subsequences to 0
    let countPaliSubseq = 0;
    // Iterate over all lowercase alphabets
    for (let c = 'a'.charCodeAt(0); c <= 'z'.charCodeAt(0); c++) {</pre>
        let currentChar = String.fromCharCode(c);
        // Find the first and last occurrence of the current character
        let firstIndex = s.indexOf(currentChar);
        let lastIndex = s.lastIndexOf(currentChar);
```

Check if there is more than one character between the leftmost and rightmost occurrence if right index - left index > 1:

class Solution:

The code iterates over all lowercase ASCII characters, which are constant in number (26 characters). This loop runs in O(1) with respect to the input size.

The time complexity of the given code can be analyzed as follows:

- is the length of the string s. If a character c is found in the string, the code computes the set of unique characters in the substring s[1 + 1 : r], where 1 is the index of the first occurrence of c, and r is the index of the last occurrence of c. Since the substring extraction s[1
- have all unique characters), this operation is O(n). Therefore, for each character iteration, the total time complexity is O(n) + O(n) + O(n), which simplifies to O(n).

Inside the loop for each character c, the code performs s.find(c) and s.rfind(c), each of which operates in O(n), where n

+ 1 : r] is O(n) and computing the set of unique characters could also be O(n) (since in the worst case, the substring could

However, because the set is re-used for each character (i.e., it doesn't grow for each character found in s) and does not

The space complexity of the algorithm can be analyzed as follows: A set is created for each character in the loop to hold the unique characters in the substring. The largest this set can be is the

Given that the outer loop runs 26 times, the time complexity in total will be O(26*n), which simplifies to O(n).

depend on the size of the input s, the space complexity is O(1). In conclusion, the time complexity is O(n) and the space complexity is O(1).

total alphabet set size, so at most 26 characters.