2483. Minimum Penalty for a Shop String] Medium **Prefix Sum**

Leetcode Link

Problem Description

hour is indicated by a character in the string. If customers[i] is 'Y', then customers visit the shop during the i-th hour. If customers [i] is 'N', no customers visit during that hour. The goal is to determine the earliest hour to close the shop so that the penalty is minimized.

In this problem, we're given a string customers which represents the customer visit log of a shop over a period of time where each

1. The number of hours the shop is open but no customers visit ('N' when the shop is open).

The penalty is defined as the sum of two components:

with a linear scan and a constant time calculation for each potential closing hour.

closing at each of those times. The calculation is as follows:

The purpose of the problem is to find the closing time that will result in the smallest penalty possible.

Intuition

2. The number of hours the shop is closed but customers do come ('Y' when the shop is closed).

The intuition behind the solution involves calculating the accumulated customer visits over time and selecting the closure time that minimizes the penalty, using a prefix sum approach.

1. We first create a prefix sum array s that records the cumulative number of customers up to each hour. This allows us to quickly calculate the number of customers who would visit whether the shop is open or closed at any given time.

2. We then iterate over each possible closing hour from 0 to n and compute the penalty at that hour. The penalty is the sum of two

Here's the reasoning:

- values: The number of hours the shop was open but had no customers (j - s[j]), and
- \circ The number of customers who would have come if the shop was closed after the j-th hour (s[-1] s[j]). 3. By comparing the penalties for all possible closing hours, we can determine the minimum penalty and the corresponding closing hour.
- The key to the solution is understanding that by using the prefix sum of customer visits, we can efficiently compute the penalty for

closing at every possible hour without recalculating from scratch each time. This approach allows us to find the optimal closing time

Solution Approach The solution uses an algorithm that leverages the prefix sum pattern to compute the optimal closing time for the shop.

1. Initialize the Prefix Sum Array: We initialize a prefix sum array s with a size of n + 1 (where n is the length of the input string

customers). We need n + 1 to also take into account the case where the shop does not open at all (closes at hour 0).

penalty.

1 class Solution:

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2. Calculate Prefix Sum: We iterate through the customers string and for each character, we add to the current prefix sum the value 1 if the character is 'Y', indicating a customer visit. This is stored in s[i + 1], effectively creating a cumulative count of

visits for each hour.

• The penalty for hours when the shop is open but no customers come is j - s[j].

Here's the step-by-step explanation of the implementation based on the reference solution approach:

 \circ The penalty for hours when the shop is closed but customers come is s[-1] - s[j]. The total penalty at hour j is the sum of these two values t = j - s[j] + s[-1] - s[j]. 4. Determine Minimum Penalty and Corresponding Hour: While iterating, we maintain two variables ans (answer) and cost

t. This ensures that by the end of the iteration, ans will hold the earliest hour at which the shop should close to minimize the

(current minimum penalty). If the penalty for closing at hour j (t) is less than the current cost, we update the ans to j and cost to

3. Iterate Over Possible Closing Times: We then iterate over every possible closing hour j from 0 to n and calculate the penalty for

The implementation makes use of linear time complexity, as it involves single passes through the data: once to build the prefix sum array and once to determine the optimal closing hour. No nested loops are required. The space complexity is linear as well, due to the additional prefix sum array.

5. Return the Optimal Closing Time: After completing the iteration over all possible closing hours, ans is returned as the final

ans, cost = 0, inf for j in range(n + 1): t = j - s[j] + s[-1] - s[j]if cost > t: 10 ans, cost = j, t 11

The use of inf in the code represents an infinitely large number to ensure that the first calculated penalty will always be smaller,

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This approach effectively balances the two types of penalties to determine the earliest closing time that minimizes overall penalty.
Example Walkthrough
Let's use a small example to illustrate the solution approach with a given customers string "YNYNNY".
First, below is the step-by-step calculation using the aforementioned solution approach:
 1. Initialize the Prefix Sum Array: We initialize a prefix sum array s of size n + 1 = 7 (since there are 6 hours in the given string). It
   will start with all zeros: [0, 0, 0, 0, 0, 0, 0].
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result, representing the optimal closing time.

n = len(customers)

s = [0] * (n + 1)

return ans

def bestClosingTime(self, customers: str) -> int:

s[i + 1] = s[i] + int(c == 'Y')

allowing the algorithm to set the initial minimum penalty properly.

For the first hour 'Y', s becomes [0, 1, 0, 0, 0, 0].

• The second hour 'N', no change as no customers came.

The third hour 'Y', s becomes [0, 1, 1, 2, 0, 0, 0].

The last hour 'Y', s becomes [0, 1, 1, 2, 2, 2, 3].

 \circ Closing at hour 0, penalty t = 0 - 0 + 3 - 0 = 3.

 \circ Closing at hour 1, penalty t = 1 - 1 + 3 - 1 = 2.

 \circ Closing at hour 2, penalty t = 2 - 1 + 3 - 1 = 3.

 \circ Closing at hour 3, penalty t = 3 - 2 + 3 - 2 = 2.

 \circ Closing at hour 4, penalty t = 4 - 2 + 3 - 2 = 3.

 \circ Closing at hour 5, penalty t = 5 - 2 + 3 - 2 = 4.

 \circ Closing at hour 6, penalty t = 6 - 3 + 3 - 3 = 3.

By the end, the prefix sum array s looks like this: [0, 1, 1, 2, 2, 2, 3].

The fourth hour 'N', no change.

The fifth hour 'N', no change.

for i, c in enumerate(customers):

sum array:

2. Calculate Prefix Sum: Now, we process the customer string "YNYNNY". For each 'Y' we add 1 to the running total of the prefix

3. Iterate Over Possible Closing Times: Next, we compute the penalty for each possible closing time:

4. Determine Minimum Penalty and Corresponding Hour: As we iterate, we find the minimum penalty:

Initialize an array to keep track of the cumulative number of customers up to each point

Increment cumulative count based on presence of a customer ('Y' or 'N')

Initialize variables for the optimal answer and its associated cost

Evaluate each potential closing time to find the one with the lowest cost

missed_customers = current_time - cumulative_customers[current_time]

// Create an array to store the cumulative sum of customers up to each point

// Initialize variables to store the best closing time and its associated cost

// Evaluate each potential closing time from 0 to n to find the minimum cost

// Cost for each time is calculated by the number of customers before j and

int cost = j - cumulativeSum[j] + (cumulativeSum[length] - cumulativeSum[j]);

cumulativeSum[i + 1] = cumulativeSum[i] + (customers.charAt(i) == 'Y' ? 1 : 0);

Cost is calculated as the sum of the customers missed before closing

cumulative_customers[i + 1] = cumulative_customers[i] + int(customer == 'Y')

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• After checking all hours, the minimum penalties are 2, which occur when closing at hour 1 and 3.
 5. Return the Optimal Closing Time: Since we want the earliest closing time with the minimum penalty, the answer would be 1, the
   first instance where the penalty reaches its minimum value.
By following this implementation, the bestClosingTime method would return 1, which is the hour the shop should close to minimize
penalties, given that we have two instances with the same minimum penalty and we choose the earliest.
Python Solution
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def bestClosingTime(self, customers: str) -> int:

for i, customer in enumerate(customers):

best_time, lowest_cost = 0, float('inf')

and the customers that came after closing

Return the best time to close that minimizes the total cost

// Method to determine the best closing time for the customers

public int bestClosingTime(String customers) {

int[] cumulativeSum = new int[length + 1];

// Calculate the cumulative sum of customers

// the number of vacant time slots after j

int length = customers.length();

for (int i = 0; i < length; ++i) {</pre>

int lowestCost = Integer.MAX_VALUE;

for (int j = 0; j <= length; ++j) {</pre>

if (lowestCost > cost) {

bestTime = j;

for current_time in range(n + 1):

 $cumulative_customers = [0] * (n + 1)$

- customers_after_closing = cumulative_customers[-1] cumulative_customers[current_time] 18 total_cost = missed_customers + customers_after_closing 19 20 21 # If the current cost is lower than the lowest known cost, update best_time and lowest_cost 22 if lowest_cost > total_cost: 23 best_time, lowest_cost = current_time, total_cost
- Java Solution

// Get the length of the customers string which depicts whether a customer is present (Y) or not (N)

// If the cost for this time is lower than the current lowest cost, update bestTime and lowestCost

28 lowestCost = cost; 29 30 31 32 // Return the best closing time that minimizes the cost

C++ Solution

class Solution:

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'N' for no).

n = len(customers)

return best_time

int bestTime = 0;

return bestTime;

class Solution {

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1 class Solution {
 2 public:
       // Calculates the best time to close the shop based on the customer presence data.
       int bestClosingTime(string customers) {
           int totalCustomers = customers.size();
           // The prefix sum array where s[i] represents the number of 'Y' up to index i.
           vector<int> prefixSum(totalCustomers + 1, 0);
            for (int i = 0; i < totalCustomers; ++i) {</pre>
 9
               prefixSum[i + 1] = prefixSum[i] + (customers[i] == 'Y' ? 1 : 0);
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           int bestTime = 0; // To store the best time to close.
           int minCost = INT_MAX; // Initialize it with the maximum possible value.
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           // Consider closing at each possible time and calculate the cost.
           for (int currentTime = 0; currentTime <= totalCustomers; ++currentTime) {</pre>
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               // Cost is the number of customers who have not arrived yet plus
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               // the number of customers who arrived after currentTime.
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               int cost = currentTime - prefixSum[currentTime] + prefixSum[totalCustomers] - prefixSum[currentTime];
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               // If the new cost is smaller, update the best closing time and minimum cost.
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               if (minCost > cost) {
                   bestTime = currentTime;
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                   minCost = cost;
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           // Return the best closing time after iterating through all possibilities.
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           return bestTime;
32 };
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Typescript Solution
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25 26 27 // Return the best closing time after iterating through all possibilities. 28 return bestTime; 29 }

if (minCost > cost) {

Time and Space Complexity

minCost = cost;

bestTime = currentTime;

Time Complexity:

We analyze the time complexity by considering the operations performed within the function:

// Calculates the best time to close the shop based on the customer presence data.

prefixSum[i + 1] = prefixSum[i] + (customers[i] === 'Y' ? 1 : 0);

for (let currentTime = 0; currentTime <= totalCustomers; ++currentTime) {</pre>

// Cost is the number of customers who have not arrived yet plus

const prefixSum: number[] = Array(totalCustomers + 1).fill(0);

// Consider closing at each possible time and calculate the cost.

// the number of customers who arrived after currentTime.

let bestTime = 0; // To store the best time to close.

// The prefix sum array where prefixSum[i] represents the number of 'Y' up to index i.

// If the new cost is smaller, update the best closing time and minimum cost.

let minCost = Number.MAX_SAFE_INTEGER; // Initialize it with the maximum safe integer value in JavaScript.

const cost = currentTime - prefixSum[currentTime] + prefixSum[totalCustomers] - prefixSum[currentTime];

The given Python code is designed to determine the best time to close a store based on when customers are inside the store. The

input is a string where each character represents a time unit and indicates whether a customer is present at that time ('Y' for yes,

• Creating a prefix sum array s of length n+1: This takes O(n) time as it involves iterating over the entire customers string once.

function bestClosingTime(customers: string): number {

const totalCustomers = customers.length;

for (let i = 0; i < totalCustomers; ++i) {</pre>

 We have a loop that iterates n+1 times. Inside the loop, all operations (calculating t, comparison, and assignment) are constant time 0(1).

The predominant factor in the time complexity is the loop that runs n+1 times with constant-time operations within it. Consequently, the time complexity of the code is:

Initializing n with the length of the customers string: 0(1).

The loop to calculate the best closing time:

• 0(n + 1) * 0(1) = 0(n)

Space Complexity:

For space complexity, we consider the additional space used by the algorithm apart from the input:

- The array s that holds the prefix sums is of length n+1, so it requires 0(n) space. Variables ans, cost, and t use constant space 0(1). Thus, the space complexity of the code is:
- 0(n) + 0(1) = 0(n)