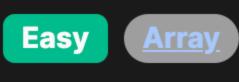
1018. Binary Prefix Divisible By 5



Problem Description

In this problem, we are given an array of binary digits, nums, which is an array of 0s and 1s. Our task is to iterate through this array to form a series of numbers x_i such that x_i is the binary number formed by the digits from nums [0] to nums [i], with nums [0] as the most significant bit. For each x_i, we need to determine whether it is divisible by 5. The result should be an array of boolean values (true or false) where each boolean value represents whether the corresponding x_i is divisible by 5.

For example, given nums = [1, 0, 1], we have:

- x_0 = 1 (1 in binary), and since 1 is not divisible by 5, the result is false. • $x_1 = 2$ (10 in binary), and since 2 is not divisible by 5, the result is false.
- x_2 = 5 (101 in binary), and since 5 is divisible by 5, the result is true.
- So the output for this input would be [false, false, true].

The key to solving this problem is to iteratively build the number x_i by appending each digit from the array nums. Since the problem only asks for the divisibility by 5, we don't actually need to store the entire number x_i, which could become very large and might cause issues with integer overflow. Instead, we can take advantage of mathematical properties of divisibility by 5 and binary numbers. The approach is to use modular arithmetic. Since we're interested in divisibility by 5, we'll use % 5 to keep track of the remainder

of x_i. In each iteration, we calculate the new x by shifting the current value of x one position to the left (equivalent to multiplying by 2) and adding the current digit v. This is equivalent to converting from binary to decimal incrementally. Then we immediately apply % 5 to get the remainder. If at any step, x is 0 after the % 5 operation, this means the current x_i is divisible by 5 and we add true to the resulting list, false

otherwise.

The solution for this problem involves the use of a loop to process each digit in the binary array. The code uses a single integer

Solution Approach

variable x to keep track of the decimal value of the current binary number being evaluated. The answer is built up in the list ans with a corresponding boolean value indicating the divisibility of each number by 5. Here is a step-by-step breakdown of the implementation:

2. Create an empty list ans to store the results (boolean values).

To process the digits and to keep the implementation efficient, the solution uses the following pattern:

1. Initialize x to 0, which will represent the current value of the decimal number as we scan through the binary digits.

For each digit v in the input array nums:

Shift the previous value of x to the left by one position. This is done by using the bitwise left shift operator "<<". In binary terms, this

- operation is equivalent to appending a zero to the binary number (or multiplying by 2 in decimal terms).
 - o Combine the shifted value of x with the current digit v using the bitwise OR operator "|". This is equivalent to appending the current binary digit to the right-most end of the existing binary number.
 - Apply a modulo operation "%" with 5 to keep only the remainder of x divided by 5. This step ensures that the value of x stays within a manageable range and directly gives us the information we need regarding divisibility by 5. • Check if x is equal to 0, if so, it means that the current number is divisible by 5; hence append True to ans. Otherwise, append False.
- Finally, the list ans is returned, which contains the boolean divisibility result for each position in the binary array nums.

The key algorithmic concepts involved include bitwise operations (to manipulate the binary representation directly), modular arithmetic (to manage the size of numbers and determine divisibility), and loop iteration (to traverse the array).

Example Walkthrough Let us illustrate the solution approach using a small example. Consider the binary array nums = [1, 1, 1, 0, 1].

We are tasked with evaluating the divisibility of the corresponding binary number at each position in the array by 5. Let's walk

through the problem step by step as per our solution approach:

1. Initialize x to 0. This will hold the decimal value represented by the binary digits considered so far. 2. Create an empty list ans to store the results as boolean values. Next, we iterate over the digits in nums and perform bitwise operations and modular arithmetic:

- Start with the first digit 1: Shift x left (x becomes 0 << 1 = 0).
- Add the current digit (x becomes 0 | 1 = 1).

Apply modulo 5 (x becomes 1 % 5 = 1).

- Since x is not 0, append False to ans.
- Next digit 1: Shift x left (x becomes 1 << 1 = 2).
- Add the current digit (x becomes 2 | 1 = 3). \circ Apply modulo 5 (x becomes 3 % 5 = 3).
- Since x is not 0, append False to ans. • Next digit 1:
- Shift x left (x becomes 3 << 1 = 6). Add the current digit (x becomes 6 | 1 = 7).
- Apply modulo 5 (x becomes 7 % 5 = 2). Since x is not 0, append False to ans.
- Next digit 0: Shift x left (x becomes 2 << 1 = 4). Add the current digit (x becomes 4 | 0 = 4).
- \circ Apply modulo 5 (x becomes 4 % 5 = 4). Since x is not 0, append False to ans.
- Last digit 1: Shift x left (x becomes 4 << 1 = 8). Add the current digit (x becomes 8 | 1 = 9).
 - \circ Apply modulo 5 (x becomes 9 % 5 = 4). Since x is not 0, append False to ans.

Solution Implementation

is_divisible = []

prefix_number = 0

demonstrates how each step of the solution approach is executed to solve the problem efficiently.

Initialize a variable to represent the current prefix number

prefix_number = ((prefix_number << 1) | digit) % 5</pre>

is_divisible.append(prefix_number == 0)

results.add(currentValue == 0);

return results;

// bits is divisible by 5

for (int bit : nums) {

// Return the list of Booleans representing divisibility by 5.

// Function to return a vector of boolean values indicating

vector<bool> results; // Vector to store the results

// whether the binary number formed by the given prefix of

vector<bool> prefixesDivBy5(vector<int>& nums) {

// Iterate over every bit in the given vector

// Use modulo 5 to avoid large integer issues

results.push(currentPrefix === 0);

currentPrefix = ((currentPrefix << 1) | num) % 5;</pre>

the binary numbers formed at each index is divisible by 5.

class Solution: def prefixesDivBy5(self, nums: List[int]) -> List[bool]: # Initialize an empty list to store the results

After processing all digits, our ans list stands as [False, False, False, False, False] which correctly represents that none of

Hence, the final output for input nums = [1, 1, 1, 0, 1] is [False, False, False, False, False]. This walkthrough clearly

```
# Iterate over the binary digits in the input list
for digit in nums:
    # Shift the current prefix number left by 1 bit and add the new digit
    # Then take the modulo by 5 to keep the number manageable and check divisibility
```

Python

```
# Return the list containing divisibility status of prefixes
        return is_divisible
Java
class Solution {
   // This method takes an array of binary digits (0s and 1s) and checks if the
   // binary number formed by the prefix of the array is divisible by 5.
    public List<Boolean> prefixesDivBy5(int[] binaryArray) {
       // This list will store the results as Booleans corresponding to each prefix.
       List<Boolean> results = new ArrayList<>();
       // This variable will hold the current value of the binary number.
       int currentValue = 0;
       // Iterate over the binary digits in the array.
        for (int digit : binaryArray) {
           // Left shift the current value to make room for the new digit,
            // and then OR it with the new digit. After that,
           // we take modulo 5 to keep the currentValue within range and
           // also to check divisibility by 5.
            currentValue = ((currentValue << 1) | digit) % 5;</pre>
           // If currentValue is 0, that means the binary number
           // formed by the current prefix is divisible by 5.
```

Append True to the result list if the current prefix number is divisible by 5, otherwise append False

C++

public:

class Solution {

```
currentValue = ((currentValue << 1) | bit) % 5;</pre>
            // Check if currentValue is divisible by 5 and add the result to the results vector
            results.push_back(currentValue == 0);
        // Return the filled results vector
        return results;
};
TypeScript
function prefixesDivBy5(nums: number[]): boolean[] {
    // Initialize the result array to hold boolean values
    const results: boolean[] = [];
    // Initialize a variable to hold the binary number being formed
    let currentPrefix = 0;
    // Loop through each number in the input array
    for (const num of nums) {
       // Left shift the current prefix by 1 and add the current number
```

int currentValue = 0; // Variable to keep track of the binary value converted to int

// the remainder of the current value when divided by 5, which is sufficient

// Shift currentValue one bit to the left and add the current bit.

// to determine divisibility by 5 for any subsequent steps.

// The `% 5` operation is used to avoid an overflow by keeping only

```
// Return the array of boolean values indicating divisibility by 5
      return results;
class Solution:
   def prefixesDivBy5(self, nums: List[int]) -> List[bool]:
       # Initialize an empty list to store the results
        is divisible = []
       # Initialize a variable to represent the current prefix number
        prefix_number = 0
       # Iterate over the binary digits in the input list
        for digit in nums:
           # Shift the current prefix number left by 1 bit and add the new digit
            # Then take the modulo by 5 to keep the number manageable and check divisibility
            prefix_number = ((prefix_number << 1) | digit) % 5</pre>
            # Append True to the result list if the current prefix number is divisible by 5, otherwise append False
            is_divisible.append(prefix_number == 0)
```

// If the current prefix is divisible by 5, add true to the results, otherwise false

Time and Space Complexity

return is_divisible

Return the list containing divisibility status of prefixes

The time complexity of the given code is O(N), where N is the length of the input list nums. This is because the code iterates through each element of the list exactly once, performing a constant amount of work for each element by shifting the number x, performing a bitwise OR operation with the current value v, and then taking the modulo with 5.

The space complexity of the given code is O(N), since it maintains a list ans that contains one boolean for each element in the input list. Thus, the size of the auxiliary space used by the program scales linearly with the input size.