1573. Number of Ways to Split a String

Medium (Math) String

Problem Description

split this string into three non-empty substrings (\$1, \$2, and \$3) such that the number of '1's is the same in each substring. If this condition cannot be met, we should return 0. If there are multiple ways to split the string that satisfy the condition, we should return the total count of such possibilities. Since the number of ways can be very large, it is only required to return the result modulo 10^9 + 7. Here's a more detailed explanation:

The problem involves a binary string s, which consists only of '0's and '1's. The task is to find out how many different ways we can

Leetcode Link

 If s is split into s1, s2, and s3, then s1 + s2 + s3 = s, which means they are consecutive parts of the original string. All three parts must have the same number of '1's, which also implies that the total number of '1's in s must be divisible by 3.

- If s doesn't contain any '1's, any split that partitions s into three parts would satisfy the condition since each part will have zero '1's.
- If the total number of '1's in s isn't divisible by 3, there is no way to split s to satisfy the given condition, so the result is 0.
- ntuition

We start by counting the total number of '1's in the string. If the count is not divisible by 3, we can immediately return 0, since it's

be divisible by 3.

impossible to divide the '1's equally into three parts. If there are no '1's, then the binary string consists only of '0's. The string can then be split in any place between the '0's. The number of ways to choose two split points in a string of length n is (n-1)*(n-2)/2.

The solution is built on the understanding that to split the string into three parts with an equal number of '1's, the number of '1's must

- If there are '1's in the string, we need to find the split points that give us the correct distribution of '1's. To do this, the following steps are taken:
- We find the indices of the first and second occurrences of the cnt-th '1' (where cnt is the total number of '1's divided by 3), as well as the indices for the first and second occurrences of the 2*cnt-th '1'.
- These indices help us identify the positions at which we can make our splits.
- The number of ways to make the first split is the difference between the second and first occurrences of the cnt-th '1'. The number of ways to make the second split is similarly the difference between the second and first occurrences of the
- Multiplying these two numbers gives us the total number of ways to split the string to ensure all three parts have the same number of '1's. The modulus operation is used to ensure the result stays within numerical bounds as per the problem's instructions.
- In the given solution, the algorithm begins with some pre-processing to calculate the total number of '1's present in the input string s. This uses the sum function and a generator expression to count '1's, sum(c == '1' for c in s). The result is then divided by 3 with

If the remainder is not zero, it indicates that it's impossible to distribute '1's equally into three parts, and the function immediately

the divmod function, which returns a tuple containing the quotient and the remainder.

first third of '1's, and j1, j2, the corresponding indices for the second third of '1's.

problem's requirement to output the result modulo 10^9 + 7.

If the quotient is zero (i.e., no '1's in the string), the solution uses the combination formula to calculate the number of ways to choose two positions out of n-1 possible positions as split points. This is done using the formula ((n - 1) * (n - 2) // 2) % mod, where n is the length of the string and mod is the required modulus $10^9 + 7$.

returns 0.

2*cnt-th '1'.

Solution Approach

Next, the solution involves finding the exact points to split the string when '1's exist. For this purpose, the find function is defined, which iterates over the string and counts '1's until it reaches a target number (for example, the cnt-th '1' or 2*cnt-th '1'). It returns the index where this occurs.

• 11 is obtained by looking for the cnt-th '1', while 12 is obtained by searching for the occurrence of one more '1' after 11 (i.e., cnt + 1). Similarly, j1 is the index of the 2*cnt-th '1' and j2 for one more '1' after j1 (i.e., 2*cnt + 1). These indices mark the possible split points just before and after the identified '1's.

Once the split points are determined, the total number of ways to split s is the product of the number of ways to split at each pair of

indices i and j, effectively (i2 - i1) * (j2 - j1). The product is taken modulo mod to avoid large numbers and comply with the

• The find function is used four times to find two pairs of indices: 11, 12, which are the indices before and after the last '1' in the

linear time complexity proportionate to the length of the string s. It uses very few additional data structures outside of basic counters and indices.

The solution effectively leverages basic counting principles and a single pass through the string to accomplish the task, ensuring a

Let's consider a small example to illustrate the solution approach with a binary string s = "0011001". 1. First, we count the total number of '1's in the string s. There are 3 ones in 0011001. 2. We check if the total number of '1's is divisible by 3. Since 3 is divisible by 3, we can proceed.

4. We start scanning the string to find the 1st '1', which is the cnt-th '1' (in our case, 1 as 3/3=1), and we find it at index 2.

5. We continue scanning to find the occurrence of the next '1' after the cnt-th '1', which is at index 3. This gives us our first

To find the total number of ways to split the string to ensure all three parts have the same number of "1"s, we multiply the number of

The result we obtained is the direct application of the algorithm described in the solution. The modulus operation is not necessary in

this example because our final count is already within the bounds of 10^9 + 7. However, in a solution implementation, the count

7. These indices give us the second potential split between indices 4 and 6. Now, let's calculate how many ways we can split s at these points:

ways for each split.

Python Solution

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return i;

function numWays(s: string): number {

let oneCount = countOnes(s);

let length = s.length;

return 0;

if (oneCount === 0) {

oneCount /= 3;

if (oneCount % 3 !== 0) {

return -1; // This condition should not happen due to input constraints

// If oneCount is not divisible by 3, there's no way to split the string

// If there are no '1's in the string, return the number of ways to choose

// Using modular arithmetic for calculating binomial coefficient (n - 1) choose 2

// the points to split the string in 3 parts, avoiding permutations.

// Find the indices where the first and second splits should occur

return (((length - 1) * (length - 2) / 2) % MOD);

// Adjust oneCount to be one third of the original oneCount

let firstSplitStart = findIndexOfGroupStart(s, oneCount);

let firstSplitEnd = findIndexOfGroupStart(s, oneCount + 1);

let secondSplitStart = findIndexOfGroupStart(s, oneCount * 2);

let secondSplitEnd = findIndexOfGroupStart(s, oneCount * 2 + 1);

• The first split can occur at either index 2 or 3, so 2 ways (12 - 11 where 11 = 2 and 12 = 3). The second split can occur at either index 4 or 6, so 3 ways (j2 - j1 where j1 = 4 and j2 = 6).

3. We need to find the partition points in the string such that each partition contains exactly one '1'.

- This gives us 2 * 3 = 6 ways to split the string 0011001 into three parts, each containing the same number of '1's.
- class Solution: def numWays(self, s: str) -> int: def find_nth_occurrence(x):

"""Find the index of the nth occurrence of '1' in the string."""

When the nth occurrence is reached, return the index

Enumerate over string characters and count ones

return None # If the nth occurrence doesn't exist

A modulus constant for the result as per LeetCode's requirement

When there are no '1's, we can choose 2 points to split the '0's into 3 parts

for index, char in enumerate(s):

n = len(s) # Length of the input string

Computing combination n-1 choose 2

Find the indices for splitting

return ((n-1)*(n-2) // 2) % mod

The first split is after the 'ones_count'th '1'

first_split_index_start = find_nth_occurrence(ones_count)

if total_ones == x:

return index

total_ones += int(char == '1')

13 14 # Count the total number of '1's in the string and check if it can be divided into 3 parts ones count, remainder = divmod(sum(char == '1' for char in s), 3) 15 16 # If it's not divisible by 3, there are no ways to split, return 0 17 if remainder: 18

6. We repeat the process for finding the 2*cnt-th '1' and the first occurrence after that. We find the next '1' at index 4 and the one after that at index 6.

potential split between indices 2 and 3.

would be taken modulo 10^9 + 7 as specified.

total ones = 0

return 0

mod = 10**9 + 7

if ones_count == 0:

if (remainder != 0) {

if (onesCount == 0) {

for (int i = 0;; ++i) {

return i;

oneCount += (c == '1');

// Find positions around the first third

// Find positions around the second third

private int findCutPosition(int targetOnesCount) {

if (tempCounter == targetOnesCount) {

long firstCutStart = findCutPosition(onesCount);

long firstCutEnd = findCutPosition(onesCount + 1);

long secondCutStart = findCutPosition(onesCount * 2);

long secondCutEnd = findCutPosition(onesCount * 2 + 1);

// Helper method to find the cut positions in the binary string

// Calculate the number of ways to make the cuts and take mod

tempCounter += binaryString.charAt(i) == '1' ? 1 : 0;

// If oneCount is not divisible by 3, there's no way to split.

int tempCounter = 0; // Temporary counter to track the number of '1's

// Once found, return the index of the string at that count

return 0;

Example Walkthrough

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# The second split is after the first '1' that follows the first split
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             first_split_index_end = find_nth_occurrence(ones_count + 1)
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             # Similarly for the second split
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             second_split_index_start = find_nth_occurrence(ones_count * 2)
 38
             second_split_index_end = find_nth_occurrence(ones_count * 2 + 1)
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             # Calculate the number of ways to split for the first and second split
             # Multiply them and return the result modulo 10^9 + 7
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             return (first_split_index_end - first_split_index_start) * (second_split_index_end - second_split_index_start) % mod
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 44 # Example usage:
 45 sol = Solution()
 46 result = sol.numWays("10101") # Should return 4 as there are four ways to split "10101" into three parts with equal number of '1's
    print(result) # Output: 4
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Java Solution
  1 class Solution {
         private String binaryString; // Renamed s to binaryString for clarity
         // Method to count the number of ways to split the given string in three parts with an equal number of '1's
  4
         public int numWays(String binaryString) {
  5
             this.binaryString = binaryString; // Initializing the class-level variable
  6
             int onesCount = 0; // Counter for the number of '1's in the string
             int stringLength = binaryString.length(); // Store the length of the string
             // Count the number of '1's in the string
 10
             for (int i = 0; i < stringLength; ++i) {</pre>
 11
                 if (binaryString.charAt(i) == '1') {
 12
 13
                     ++onesCount;
 14
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```

int remainder = onesCount % 3; // Calculate remainder to check if onesCount is divisible by 3

// If not divisible by three, return 0 as it's impossible to split the string properly

// Number of subarrays is a combination: Choose 2 from stringLength - 1 and take mod

// If the string contains no '1's, calculate the number of ways to split the zeros

return (int) (((stringLength - 1L) * (stringLength - 2) / 2) % mod);

onesCount /= 3; // Divide the count of '1's by 3 to find the size of each part

return (int) ((firstCutEnd - firstCutStart) * (secondCutEnd - secondCutStart) % mod);

// Look for the position in the string that corresponds to the target count of '1's

final int mod = (int) 1e9 + 7; // Modulus value for the result

1 class Solution { public: int numWays(string s) { // Count the number of '1's in the string. int oneCount = 0; for (char c : s) {

C++ Solution

```
if (oneCount % 3 != 0) {
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                 return 0;
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             // Define modulo for the result as required by the problem.
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             const int MOD = 1e9 + 7;
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             int length = s.size();
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 19
             // If there are no '1's in the string, return the number of ways to choose
             // the points to split the string in 3 parts, avoiding permutations.
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 21
             if (oneCount == 0) {
 22
                 return ((long long)(length - 1) * (long long)(length - 2) / 2) % MOD;
 23
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 25
             // Adjust oneCount to be one third of the original oneCount
 26
             oneCount /= 3;
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 28
             // Helper lambda function to find the index of the start of a particular group of '1's.
 29
             auto findIndexOfGroupStart = [&](int groupCount) -> int {
 30
                 int count = 0;
                 for (int i = 0; ; ++i) {
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 32
                     count += (s[i] == '1');
                     if (count == groupCount) {
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                         return i;
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             };
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             // Find the indices where the first and second splits should occur.
 40
             int firstSplitStart = findIndexOfGroupStart(oneCount);
 41
             int firstSplitEnd = findIndexOfGroupStart(oneCount + 1);
             int secondSplitStart = findIndexOfGroupStart(oneCount * 2);
 42
             int secondSplitEnd = findIndexOfGroupStart(oneCount * 2 + 1);
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             // Calculate the number of ways to make the splits and return the result module MOD.
 46
             return ((long long)(firstSplitEnd - firstSplitStart) * (long long)(secondSplitEnd - secondSplitStart)) % MOD;
 47
 48
    };
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Typescript Solution
  1 // Global variable to define modulo for the result as required by the problem
    const MOD: number = 1e9 + 7;
    // Function to count the number of '1's in the string
     function countOnes(s: string): number {
         let oneCount = 0;
         for (let c of s) {
             oneCount += (c === '1') ? 1 : 0;
  8
  9
         return oneCount;
 10
 11 }
 12
    // Function to find the index of the start of a particular group of '1's
     function findIndexOfGroupStart(s: string, groupCount: number): number {
 15
         let count = 0;
         for (let i = 0; i < s.length; i++) {
 16
             if (s[i] === '1') count++;
 17
             if (count === groupCount) {
 18
```

51 // Calculate the number of ways to make the first and the second split. 52 // Multiply the number of zeroes between the adjacent groups of '1', and take the result module MOD return ((firstSplitEnd - firstSplitStart) * (secondSplitEnd - secondSplitStart)) % MOD; 53 54 } 55 56 // Example usage:

57 // const s: string = "10101";

Time Complexity The given code snippet includes three significant calculations: counting the number of 1's in the string, finding the indices where certain counts of 1's occur, and calculating the total number of ways to split the string.

where n is the length of the string s.

// console.log(numWays(s)); // The output would be 4 59 Time and Space Complexity

25 // Function that calculates the number of ways the input string s can be split into three parts with equal number of '1's

2. Finding the indices with the help of the find function: This function is called four times. Each call to the find method iterates over the entire string in the worst-case scenario, which makes it O(n) for each call. Therefore, for four calls, the time complexity associated with the find function is 0(4 * n) which simplifies to 0(n).

3. Calculating combinations for zero counts of 1's: The calculation ((n - 1) * (n - 2) // 2) % mod is executed in constant time

1. Counting the number of 1's: This is done by iterating over each character in the string once. This operation takes O(n) time

Hence, the overall time complexity of the code is O(n) for scanning the string to count the number of 1's plus O(n) for the find operations, which simplifies to O(n).

space, so it is 0(1).

Space Complexity

2. Counting 1's: The sum comprehension iterates over the string and counts the number of '1's, which does not require additional 3. Variables 11, 12, 11, 12, and n: They are also constant-size integers, with no additional space dependent on the input size, so this

1. cnt and m: These are constant-size integers, which occupy 0(1) space.

0(1), as it doesn't depend on the size of the input string beyond the length calculation.

is 0(1). 4. The function find uses i and t which again are constant-size integers, hence 0(1) space.

As there are no data structures used that scale with the size of the input, the overall space complexity of the code is 0(1), which represents constant space usage.