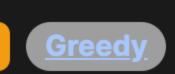
2938. Separate Black and White Balls

String)





Problem Description



In this problem, we're given n balls on a table, colored black or white, and represented by a binary string s of length n. The character 1 represents a black ball, while 0 represents a white ball. The objective is to group all the black balls to the right side of the string and all the white balls to the left side, using a series of adjacent swaps. Each step allows a swap of two neighboring balls. The final goal is to determine the minimum number of such swaps needed to achieve the segregation of the balls into their respective groups by color.

Intuition

position on the right side. Due to the nature of the swaps, every time we move a black ball one position to the right, one swap is required. However, as we progress in grouping the black balls to the right, each successive black ball we encounter will have to be moved a few positions less than the previous one because of the black balls that we have already moved.

To calculate the number of moves efficiently, we simulate this process in reverse order by iterating from the right to the left. We

The key insight behind the solution is to count the number of steps it takes to bring each black ball (represented by 1) to its final

use a variable cnt to keep track of the black balls that have been encountered, and we use ans to sum up the moves needed. With every black ball encountered, we increase cnt by one since one more black ball is now in its right-most position. We add n i - cnt to ans each time we find a black ball because the ball needs to pass over n - i - cnt black balls that have already been placed to the right. By moving from right to left, we can calculate the minimum steps with a single pass through the string, making the process

efficient and avoiding the need for simulating actual swaps. **Solution Approach**

The implementation of the solution starts by initializing two variables, cnt and ans, both set to 0. The variable cnt will keep track

of the number of black balls (1s) we have encountered starting from the rightmost side, while ans will accumulate the total number of steps (swaps) required to move all black balls to the right. We begin with a reverse iteration of the string, from the last character to the first (index n−1 to ∅). We traverse in reverse because

we're interested in calculating the number of steps a black ball needs to move from its current position to its final destination, which we can easily compute once we know how many black balls are already positioned to the right of it. During the iteration, for each black ball we encounter, which is marked by a 1 in string s:

current one.

Here's the reference approach, expressed as pseudocode to describe the process:

• We increment cnt by 1, representing another black ball that is in its appropriate position on the right.

- We add this calculated number of swaps to ans, which is our total.
- The algorithm does not use auxiliary data structures, thereby maintaining a space complexity of 0(1). The time complexity is

• We calculate n - i - cnt, which gives us the number of swaps needed to move this particular black ball past the cnt black balls already in

place. Note that i is the current index in the iteration. We do this because each black ball already placed means one less swap needed for the

O(n), as we only need to traverse the string once to count the necessary swaps.

function minimumSteps(s: string) -> integer: n = length(s)cnt = 0ans = 0

```
if s[i] == '1':
          cnt = cnt + 1
          ans = ans + (n - i - cnt)
  return ans
The beauty of this solution lies in its simplicity. By intelligently choosing to iterate in reverse and keep track of the number of
encountered black balls, we can calculate the solution in a single pass without simulating the swaps, which could have been
significantly costlier in terms of performance.
```

for i from n-1 to 0:

Example Walkthrough Let's walk through an example to better understand the solution approach using the problem content above.

Imagine we have the binary string 10101, representing 5 balls where the 1s are black balls, and the 0s are white balls. Using the

solution approach, we want to calculate the minimum number of swaps needed to group all black balls to the right.

Following the steps of the algorithm:

1. We start with cnt and ans initialized to 0. 2. The string 10101 has length n = 5.

∘ i = 4, s[4] = 1 (black ball): We increment cnt to 1. ans becomes ans + (5 - 4 - 1) which is ans + 0 (no swap needed because it is already

- in the last position). • i = 3, s[3] = 0 (white ball): No action taken because we only count swaps for black balls. cnt and ans are unchanged.
- ∘ i = 2, s[2] = 1 (black ball): We increment cnt to 2. ans becomes ans + (5 2 2) which is ans + 1 (one swap needed to move to the end).

4. Adding these up, ans = 0 + 1 + 2 which equals 3.

3. We iterate in reverse, starting from the last character (index 4) to the first (index 0).

Initialize 'answer' for holding the minimum steps and

for i in range(length -1, -1, -1):

if s[i] == '1':

int length = s.length();

// Iterate over the string from right to left

// Increase the count of '1's

// Check if the current character is '1'

answer += length - i - oneCount;

// Add the number of steps to move this '1' to the right end

for (int i = length - 1; i >= 0; --i) {

if (s.charAt(i) == '1') {

++oneCount;

Check if the current character is '1'

Traverse the string in reverse from last to first character

- ∘ i = 1, s[1] = 0 (white ball): Again, no action is needed for white balls. No changes to cnt or ans. ∘ i = 0, s[0] = 1 (black ball): Increment cnt to 3. ans becomes ans + (5 - 0 - 3) which is ans + 2 (two swaps needed to move to the end).
- Therefore, for the given string 10101, it will take a minimum of 3 swaps to move all the black balls to the right side of the string.
- This matches the logic of our solution approach. The black balls initially at indices 0 and 2 need to each move past two white balls to reach the far right, with the last black ball at index 4 already in the correct position.

Python class Solution:

def minimumSteps(self, s: str) -> int: # Length of the given string length = len(s)

answer = 0

Solution Implementation

```
# 'one_count' for keeping track of the number of '1's encountered
one_count = 0
```

```
# If it's '1', increment the 'one_count'
               one count += 1
               # Update answer by how many steps needed to move this '1' to the end
               # considering the number of ones already counted.
               answer += (length - i - 1) - one_count + 1
       # Return the total minimum steps calculated
       return answer
Java
class Solution {
    /**
    * Calculates the minimum number of steps to move all '1's to the right end of the string
    * @param s the input string representing a binary number
    * @return the minimum number of steps required
    */
    public long minimumSteps(String s) {
       // Initialize the answer to 0
       long answer = 0;
       // Counter for the number of '1's found
       int oneCount = 0;
       // Length of the string
```

```
// Return the total number of steps calculated
       return answer;
C++
#include <string>
class Solution {
public:
    // Function to calculate the minimum number of steps required.
    long long minimumSteps(std::string s) {
        long long steps = 0; // Variable to store the minimum steps.
        int onesCount = 0; // Counter for the occurrences of '1'.
        int length = s.size(); // Get the size of the string.
       // Traverse the string from the end to the beginning.
        for (int i = length - 1; i >= 0; --i) {
            if (s[i] == '1') { // If the current character is '1'.
```

++onesCount; // Increment the count of '1's.

// the number of '1's encountered so far.

steps += length - i - onesCount;

// Return the computed minimum steps.

// Iterate over the string in reverse order.

for (let $i = stringLength - 1; i >= 0; --i) {$

// Accumulate the distance from right-most end minus

```
function minimumSteps(s: string): number {
   const stringLength = s.length; // Get the length of the input string.
   let steps = 0;
```

TypeScript

};

return steps;

let countOfOnes = 0;

if (s[i] === '1') {

++countOfOnes;

```
// the count of '1's encountered so far, which do not need to be moved.
              steps += stringLength - i - countOfOnes;
      // Return the total number of steps required to move all '1's to the end of the string.
      return steps;
class Solution:
   def minimumSteps(self, s: str) -> int:
       # Length of the given string
        length = len(s)
       # Initialize 'answer' for holding the minimum steps and
       # 'one_count' for keeping track of the number of '1's encountered
       answer = 0
       one_count = 0
       # Traverse the string in reverse from last to first character
       for i in range(length -1, -1, -1):
           # Check if the current character is '1'
           if s[i] == '1':
               # If it's '1', increment the 'one_count'
               one count += 1
               # Update answer by how many steps needed to move this '1' to the end
               # considering the number of ones already counted.
               answer += (length -i-1) - one_count +1
       # Return the total minimum steps calculated
        return answer
Time and Space Complexity
```

// Initialize the steps counter to zero.

// Accumulate the necessary steps to bring the '1' to the end of the string, taking into account

// The '~' before 'i' is a bitwise NOT operator, used here as a shorthand for (i !==-1).

// If the current character is '1', increment the count of '1's.

// Initialize a counter to keep track of the number of '1's encountered.

Time Complexity

increase with the size of the input string s.

first. Since each element of the string s is processed exactly once during this iteration, the time complexity of this operation is 0(n), where n is the length of the string s. Inside the loop, only constant time operations are performed (i.e., basic arithmetic operations and conditional checks), which do not depend on the size of the input, therefore they don't affect the overall linear time complexity. **Space Complexity**

The algorithm uses a fixed number of variables (n, ans, cnt, and i) that do not scale with the size of the input. This implies that

the space complexity is constant. Therefore, the space complexity of the code is 0(1), as the amount of memory used does not

The given code involves a single for-loop that iterates over the string s in reverse order, starting from the last character to the