

2021. Brightest Position on Street

Medium

Array

Ordered Set

Prefix Sum

[Leetcode Link](#)

Problem Description

In this problem, we are provided with a representation of a street and its street lamps. The street is visualized as a number line, and street lamps are given as a 2D integer array `lights`. Each entry in this array, `lights[i]`, contains two integers: `position_i` and `range_i`. The first integer `position_i` indicates the location of the street lamp on the number line, while the second integer `range_i` tells us how far to the left and right the lamp illuminates from its position. Consequently, the area that each street lamp lights up is from `position_i - range_i` to `position_i + range_i` inclusive.

The problem defines the **brightness** of a position on the street as the number of street lamps that illuminate that particular position. Our task is to determine the **brightest position** on the street, which is the position that is lit by the highest number of street lamps. If there happens to be more than one position with the same maximum brightness, the problem asks us to return the smallest of these brightest positions.

Intuition

The intuition behind solving this problem involves treating the street as a range of positions and each lamp as contributing a unit of brightness to a specific range. We can use sweep line algorithm concepts to efficiently determine the brightness of each position. Here's how we can approach the problem:

- Consider each lamp as triggering an 'event' at the start and end of its range.
- When a lamp starts at `position_i - range_i`, it adds to the brightness (+1), and when its influence ends at `position_i + range_i + 1`, it subtracts from the brightness (-1). This is because the range is inclusive, so the end of the influence is technically one position beyond the range.
- We can sweep over all the positions influenced by any lamp, and at each point, we can add or subtract the brightness accordingly.
- We use a dictionary to keep track of all these 'events' of starting and ending of a lamp's influence, then sort this dictionary by the key (which represents positions on the street).
- We sweep the sorted positions and maintain a running sum (s) of the brightness, updating the maximum brightness (mx) seen so far and the position (ans) where this maximum brightness occurs.
- At the end of the sweep, `ans` will hold the smallest position with the maximum brightness because we sorted the positions and the calculation respects the order.

The implementation translates this intuition into a working solution, utilizing Python's `defaultdict` to facilitate the management of the brightness changes and keeping track of the running sum and maximum brightness dynamically as we sweep through the positions.

Solution Approach

The implementation of the solution uses a variety of data structures and an intelligent algorithm to achieve an efficient approach.

- Data Structures Used:**
 - defaultdict(int):** A Python `defaultdict` with `int` type is used to track the starting and ending influence points of each lamp's light on the street. If an index is not already in the dictionary, it defaults to `0` which is convenient because it represents the initial state of brightness for any position on the street.
- Algorithms and Patterns:**
 - Sweep Line Algorithm:** This algorithm is used to simulate the process of 'sweeping' through the street from left to right. As we 'sweep' through the street, we encounter events that start or end a lamp's range.
 - Event Processing:** Each lamp generates two events: one where its light begins (`position_i - range_i`) and one where it ends (`position_i + range_i + 1`). In the `defaultdict`, we increase the brightness by 1 at the start and decrease it by 1 at the end of the range.
 - Sorting the Events:** Sorting the keys of the `defaultdict` ensures that we process these events in the order of their occurrence along the street.
 - Running Sum and Maximization:** In the sweep process, a running sum `s` is maintained which updates at each event, increasing or decreasing according to the lamp's influence. We then compare this running sum to the maximum brightness `mx` encountered so far. If the current sum is greater, we update the `mx` and record the position `ans` at which this new maximum occurs.

The code reflects these concepts as follows:

- We iterate through each lamp in `lights` and calculate the starting (`l`) and ending (`r`) points of its range, updating the `defaultdict` accordingly.
- We then sort the keys of the `defaultdict` (the positions where brightness changes occur) and perform the 'sweep' by iteratively adding or subtracting from the running sum `s`.
- Whenever the running sum `s` exceeds the previously tracked maximum brightness `mx`, we update `mx` with `s` and set `ans` to the current position `k`.

As a result, the code does not require us to calculate the brightness for every single position on the street. Instead, it efficiently tracks changes in brightness at specific points, which allows us to find the brightest position without redundant calculations.

Example Walkthrough

Let's go through the solution approach with a small example. Suppose we are given the following `lights` array representing the street lamps:

```
1 lights = [[1, 1], [4, 1]]
```

Each of the subarrays represents a street lamp with [`position_i`, `range_i`]. Now, we will walk through the algorithm step by step.

- Initialization of Events:**
 - For the first lamp `[1, 1]`, it influences the street in the range `[0, 2]` (from `position_i - range_i` to `position_i + range_i`).
 - For the second lamp `[4, 1]`, it influences the street in the range `[3, 5]`.
- Creating and Populating Event Points:**
 - We treat the start and end of each range as events. We use a `defaultdict` to store the brightness increase and decrease at specific points:

```
1 events = defaultdict(int)
2 events[0] += 1
3 events[3] += 1
4 events[2+1] -= 1 # We add 1 because the range end is inclusive
5 events[5+1] -= 1 # Same as above
```
- Sorting Events:**
 - We now have the events `{0: 1, 3: 1, 3: -1, 6: -1}`.
 - Sorting them by key gives us the order `[0, 3, 3, 6]`.
- Sweeping Through Sorted Event Points:**
 - We begin with a running sum `s = 0`, maximum brightness `mx = 0`, and the answer `ans = 0`.
 - At position `0`, we encounter the start of the first lamp's influence, so `s += events[0]` (now `s = 1`).
 - At position `3`, we have two events. The start of the second lamp's influence (`s += events[3]`, now `s = 2`) and the end of the first lamp's influence (`s += events[3]`, now `s = 1`).
 - At position `6`, we encounter the end of the second lamp's influence, so `s -= events[6]` (now `s = 0`).
 - After processing each event, we update `mx` and `ans` whenever we find a new maximum brightness.
- Finding the Brightest Position:**
 - During the process, we found the maximum brightness to be `mx = 2` at positions `3`, but since there are two events at `3`, this number decreases back to `1` by the end of processing all events at `3`.
 - `ans` during the occurrence of `mx` is set to the position at which this happened, which in this case, initially, is `3`.

Hence, by the end of the sweep, we determined that the brightest position on the street is `3` with a brightness of `2`, and that is our final answer.

By following this approach, we only calculate the brightness at specific event points instead of for every position on the street, which makes the algorithm efficient and effective for solving this kind of problem.

Python Solution

```
1 from collections import defaultdict
2
3 class Solution:
4     def brightestPosition(self, lights: List[List[int]]) -> int:
5         # Initialize a dictionary to store the changes in brightness
6         brightness_changes = defaultdict(int)
7
8         # Iterate over each light
9         for position, radius in lights:
10             # Determine the range of positions affected by the light's brightness
11             left_border = position - radius
12             right_border = position + radius
13
14             # Increment the brightness at the start of the range
15             brightness_changes[left_border] += 1
16             # Decrement the brightness just after the end of the range
17             brightness_changes[right_border + 1] -= 1
18
19         # Initialize variables to keep track of the current brightness,
20         # the maximum brightness observed, and the position of the maximum brightness
21         current_brightness = max_brightness = 0
22         brightest_position = 0
23
24         # Iterate over the positions in the sorted order of the keys
25         for position in sorted(brightness_changes):
26             # Update the current brightness
27             current_brightness += brightness_changes[position]
28             # If the current brightness is greater than the maximum recorded brightness
29             if max_brightness < current_brightness:
30                 # Update the maximum brightness and brightest position
31                 max_brightness = current_brightness
32                 brightest_position = position
33
34         # Return the position with the maximum brightness
35         return brightest_position
36
```

Java Solution

```
1 class Solution {
2     public int brightestPosition(int[][] lights) {
3         // Use a TreeMap to easily manage the range of light contributions on the positions
4         TreeMap<Integer, Integer> deltaBrightness = new TreeMap<>();
5
6         // Iterate over each light array to calculate the influence ranges and store them
7         for (int[] light : lights) {
8             int leftBoundary = light[0] - light[1]; // Calculate left boundary of the light
9             int rightBoundary = light[0] + light[1]; // Calculate right boundary of the light
10
11             // Increase brightness at the start of the range
12             deltaBrightness.merge(leftBoundary, 1, Integer::sum);
13             // Decrease brightness right after the end of the range
14             deltaBrightness.merge(rightBoundary + 1, -1, Integer::sum);
15         }
16
17         int brightestPosition = 0; // To hold the result position with the brightest light
18         int currentBrightness = 0; // Current accumulated brightness
19         int maxBrightness = 0; // Max brightness observed at any point
20
21         // Iterate over the entries in the TreeMap
22         for (var entry : deltaBrightness.entrySet()) {
23             int changeInBrightness = entry.getValue();
24             currentBrightness += changeInBrightness; // Apply the change on the current brightness
25
26             // Check if the current brightness is the maximum observed so far
27             if (maxBrightness < currentBrightness) {
28                 maxBrightness = currentBrightness; // Update the maximum brightness
29                 brightestPosition = entry.getKey(); // Update the position of the brightest light
30             }
31         }
32
33         return brightestPosition; // Return the position with the maximum brightness
34     }
35 }
36
```

C++ Solution

```
1 class Solution {
2 public:
3     int brightestPosition(vector<vector<int>>& lights) {
4         // Create a map to store the changes in brightness at different positions
5         map<int, int> brightnessDeltas;
6
7         // Loop through each light and update the map with the range it illuminates
8         for (auto& light : lights) {
9             // Calculate the left and right bounds of the light's effect
10            int left = light[0] - light[1];
11            int right = light[0] + light[1];
12
13            // Increase brightness at the starting position of the light's effect
14            ++brightnessDeltas[left];
15            // Decrease brightness just after the end of the light's effect
16            --brightnessDeltas[right + 1];
17        }
18
19        // Variable to store the brightest position found so far
20        int brightestPosition = 0;
21        // Variable to keep track of the current sum of brightness as we iterate
22        int currentBrightness = 0;
23        // Variable to store the maximum brightness encountered
24        int maxBrightness = 0;
25
26        // Iterate through brightnessDeltas to find the brightest position
27        for (auto& [position, delta] : brightnessDeltas) {
28            // Update the current brightness based on the delta
29            currentBrightness += delta;
30
31            // If we find a brighter position, update maxBrightness and brightestPosition
32            if (maxBrightness < currentBrightness) {
33                maxBrightness = currentBrightness;
34                brightestPosition = position;
35            }
36        }
37
38        // Return the position with the maximum brightness
39        return brightestPosition;
40    }
41 };
42
```

Typescript Solution

```
1 // Define the type structure for the light positions array
2 type LightPosition = [number, number];
3
4 /**
5  * Returns the brightest position on a street given the array of lights.
6  * @param lights - An array of tuples representing lights, where each tuple consists of the position and range.
7  * @return The position of the brightest point.
8  */
9 const brightestPosition = (lights: LightPosition[]): number => {
10     // Create a map where the key is the position on the street and the value is the change in brightness at that point.
11     const deltaBrightness = new Map<number, number>();
12
13     // Populate the map with brightness changes, accounting for the lights turning on at their start position
14     // and off immediately after their end position.
15     for (const [position, range] of lights) {
16         const start = position - range;
17         const end = position + range;
18         deltaBrightness.set(start, (deltaBrightness.get(start) ?? 0) + 1);
19         deltaBrightness.set(end + 1, (deltaBrightness.get(end + 1) ?? 0) - 1);
20     }
21
22     // Extract and sort the keys from the map to iterate over positions in ascending order.
23     const sortedPositions = Array.from(deltaBrightness.keys()).sort((a, b) => a - b);
24
25     let currentBrightness = 0; // Accumulated brightness at the current position.
26     let maxBrightness = 0; // Maximum brightness encountered so far.
27     let brightestPos = 0; // Position with the maximum brightness.
28
29     // Iterate over all positions to find the maximum accumulated brightness.
30     for (const position of sortedPositions) {
31         currentBrightness += deltaBrightness.get(position) || 0;
32
33         // Update maximum brightness and position if the current brightness is greater.
34         if (maxBrightness < currentBrightness) {
35             maxBrightness = currentBrightness;
36             brightestPos = position;
37         }
38     }
39
40     // Return the position with the maximum brightness.
41     return brightestPos;
42 };
43
44 // Example usage (Optional):
45 // const lights: LightPosition[] = [[1, 2], [3, 6], [5, 5]];
46 // console.log(brightestPosition(lights)); // Should output the position of the brightest point
47
```

Time and Space Complexity

The time complexity of the code is $O(N \log N)$ where N is the number of light ranges in the `lights` list. This complexity arises because we sort the keys of our dictionary `d`, which contains at most $2N$ keys (each light contributes two keys: the start and end of its illumination range). Sorting these keys dominates the runtime complexity.

The space complexity of the code is $O(N)$ since we use a dictionary to store the changes to brightness at each key point. In the worst case, if every light has a unique range, the dictionary could have as many as $2N$ keys, where N is the number of light ranges in the `lights` list.