784. Letter Case Permutation

Medium Bit Manipulation String Backtracking

Problem Description

characters individually to either lowercase or uppercase, which can lead to various permutations of the string with different cases for each letter. The task is to generate all possible strings with these different case transformations and return them as a list in any order.

An example to illustrate this: for the string "a1b2", the output will be ["a1b2", "a1B2", "A1b2", "A1B2"].

This is a typical backtracking problem, as we'll consider each character and explore the possibilities of both keeping it as it is or

In this problem, we're given a string s consisting of alphabetical characters. We have the freedom to change each of these

changing its case, accumulating all different strings that can be formed by these choices.

Intuition

To achieve our solution, we can apply a method known as depth-first search (DFS), which is a type of backtracking algorithm.

The DFS approach will help us traverse through all possible combinations of uppercase and lowercase transformations of the characters within the string. Here's the intuition breakdown for solving this problem:

Start from the first character: We begin the process with the first character of the string.
 Recursive exploration: For each character, we have two choices (provided it's an alphabetical character and not a digit):

 Keep the current character as is and proceed to the next one.

Backtracking: After exploring one option (like keeping the character as is) for the current position, we backtrack to explore

Base case: If we reach the end of the string (i.e., index i is equal to the string length), we've completed a permutation and

• Change the current character's case (from lowercase to uppercase or vice versa) and move to the next one.

- it's added to the list of results.
 - the other option (changing the case).

is defined within the scope of the letterCasePermutation method.

decision to keep the current character as is.

and the resulting strings appended to ans.

Let's illustrate the solution approach with a small example using the string "0a1".

List t will hold the characters that we are currently exploring through the DFS algorithm.

permutations of the string are saved in ans, which now contains ["0a1", "0A1"].

permutations regarding the case of alphabetic characters.

Append the current permutation to the answer list

Recursive case: move to the next character without changing the case

If the current character is alphabetic, we can change its case

current string[index] = chr(ord(current string[index]) ^ 32)

private List<String> permutations = new ArrayList<>(); // List to hold the string permutations

private char[] charArray; // Character array to facilitate permutation generation

// Public method to generate letter case permutations for a given string

permutations.emplace_back(str);

// letters differ by exactly 32

// we toggle its case and recursively continue

return;

dfs(index + 1);

if (isalpha(str[index])) {

str[index] ^= 32;

dfs(index + 1);

// Start DFS from index 0

// Helper function to perform DFS

const dfs = (index: number) => {

dfs(index + 1);

return;

dfs(index + 1);

return permutations;

};

dfs(0);

// str[index] ^= 32;

// Return all generated permutations

// Function that generates all possible permutations of a string

const length = s.length; // The length of the input string

// Check if the current character is a letter and can change case

const results: string[] = []; // Stores the resulting permutations

const charArray = [...s]; // Converts the string to an array of characters

if (index === length) {
// If the end of the string is reached,

// It uses Depth-First Search (DFS) to explore all variations.

// with letters toggled between uppercase and lowercase.

function letterCasePermutation(s: string): string[] {

if (isLetter(charArray[index])) {

permutations.append(''.join(current_string))

Convert the input string to a list, making it mutable

Initialize a list to store all possible permutations

Start the depth-first search from the first character

if current string[index].isalpha():

- 5. **Result accumulation**: As we hit the base case at different recursive call levels, we collect all permutations of the string.
- bitwise XOR operation ^ 32 is a clever trick to toggle the case of an alphabetical character since converting between lowercase to uppercase (or vice versa) in ASCII entails flipping the 6th bit.

 Solution Approach

This recursive approach works because it explores all possible combinations by trying each option at each step. The use of the

The provided solution uses a Depth-First Search (DFS) algorithm along with a recursive helper function named dfs. This function

Here's a step-by-step walk-through of the solution code:

1. A new list t is created from the original string s which is going to hold the characters that we are currently exploring through DFS.

3. The dfs function

3. The dfs function defined inside the letterCasePermutation takes a single argument i, which is the index of the character in t we are currently exploring.
4. In the body of the dfs function, the base case checks if the index i is greater than or equal to the length of s. If it is, it

If the base case condition is not met, we first call dfs(i + 1) without altering the current character. This recurses on the

function gets the ASCII value of the character, ^ 32 toggles the 6th bit which changes the case, and chr converts the ASCII

value back to the character. After changing the case, we call dfs(i + 1) again, exploring the decision tree path where the

means we've constructed a valid permutation of string s in the list t and we append this permutation to ans.

6. Next, if the current character is alphabetic (t[i].isalpha()), we toggle its case using $t[i] = chr(ord(t[i]) ^ 32)$. The ord

An empty list ans is initialized which will eventually contain all the possible permutations of the string.

- current character's case is toggled.

 7. By recursively calling dfs with 'unchanged' and 'changed' states of each character, all combinations are eventually visited,
- possibility. The data structure used is a basic Python list which conveniently allows us to both change individual elements in place and join them into strings when we need to add a permutation to the results.

 Example Walkthrough

We start by setting up an empty list ans that will store our final permutations and a list t from the string s, which is "0a1".

Since the first character '0' is not an alphabetical character, we only have one option for it; we keep it as is. So, we move on to

The DFS here is a recursive pattern that explores each possibility and undoes (backtracks) that choice before exploring the next

The next character is 'a'. Here, we have two choices:
Keep 'a' as it is and proceed to the next character, which will be '1'. This sequence is "0a1". Since '1' is not alphabetical, we keep it as is and add "0a1" to ans.

o Toggle the case of 'a' to 'A' and then proceed to the next character, '1'. This sequence is "0A1". Again, we keep '1' as it is and add "0A1" to

And that's the end of the example. The original list "0a1" only had one alphabetical character that could be toggled, which

At this point, the dfs function has recursively explored and returned from both branches for character 'a', and the two

5. Since there are no more characters to explore, the recursion terminates, and the ans list now holds all the possible

Python

class Solution:

Solution Implementation

return

dfs(index + 1)

current string = list(s)

Return the computed permutations

permutations = []

return permutations

dfs(0)

Example of usage:

sol = Solution()

class Solution {

ans.

the next character.

- resulted in two different string permutations: "0a1" and "0A1".
- def letterCasePermutation(self, s: str) -> List[str]:
 # Helper function for depth-first search
 def dfs(index):
 # Base case: if the current index is equal to the length of the string
 if index == len(s):
- # Continue the search with the flipped case character
 dfs(index + 1)
 # Revert the change for backtracking purposes
 current_string[index] = chr(ord(current_string[index]) ^ 32)

Flip the case: if the current character is uppercase, make it lowercase and vice versa

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# result = sol.letterCasePermutation("a1b2")
# print(result) # Output: ["a1b2", "a1B2", "A1b2", "A1B2"]
Java
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```
public List<String> letterCasePermutation(String s) {
        charArray = s.toCharArray(); // Convert string to character array for modification
        generatePermutations(0); // Start recursion from the first character
        return permutations; // Return all generated permutations
    // Helper method to recursively generate permutations
    private void generatePermutations(int index) {
        // Base case: If the end of the array is reached, add the current permutation to the list
        if (index >= charArray.length) {
            permutations.add(new String(charArray));
            return;
        // Recursively call the method to handle the next character without modification
        generatePermutations(index + 1);
        // If the current character is alphabetic, toggle its case and proceed with recursion
        if (Character.isLetter(charArray[index])) {
            // Toggle the case: lowercase to uppercase or vice versa using XOR operation with the space character
            charArray[index] ^= ' ';
            generatePermutations(index + 1);
            // IMPORTANT: revert the character back to its original case after the recursive call
            charArray[index] ^= ' '; // This step ensures the original structure is intact for future permutations
       // If the character is not alphabet, it is left as—is and the recursion takes care of other characters
C++
#include <vector>
#include <string>
#include <functional>
class Solution {
public:
    // Function to generate all permutations of a string where each letter can be lowercase or uppercase
    std::vector<std::string> letterCasePermutation(std::string str) {
        // Resultant vector to store all permutations
        std::vector<std::string> permutations;
        // Utility lambda function to perform a Depth-First Search (DFS) for all possible letter case combinations
        std::function<void(int)> dfs = [&](int index) {
            // Base case: if we reach the end of the string, add the current permutation to the results
            if (index >= str.size()) {
```

// Recursive case: continue with the next character without changing the current one

// Toggle the case of the current character: lowercase to uppercase or vice versa

// Optional: Toggle the case back if you want to use the original string elsewhere

// after this function call. If str is not used after this, you can omit this step.

results.push(charArray.join('')); // join the characters to form a permutation and add to results.

toggleCase(charArray, index); // Toggle the case of the character at the current index

// Recursive call with the next character (no change)

// Recursive call with the toggled character

// XOR with 32 takes advantage of the fact that the ASCII values of upper and lower case

// Only if the current character is alphabetical (either uppercase or lowercase)

// Recursive call with the case of the current character toggled

};

TypeScript

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};
    // Function to check if a character is a letter (could be replaced with regex or other methods)
    function isLetter(c: string): boolean {
        return (c >= 'A' && c <= 'Z') || (c >= 'a' && c <= 'z');
    // Function that toggles the case of a letter by using bitwise XOR with the space character (32)
    function toggleCase(arr: string[], index: number): void {
        arr[index] = String.fromCharCode(arr[index].charCodeAt(0) ^ 32);
    dfs(0); // Start the DFS from the first character
    return results; // Return the array of permutations
class Solution:
    def letterCasePermutation(self, s: str) -> List[str]:
        # Helper function for depth-first search
        def dfs(index):
            # Base case: if the current index is equal to the length of the string
            if index == len(s):
                # Append the current permutation to the answer list
                permutations.append(''.join(current_string))
                return
           # Recursive case: move to the next character without changing the case
            dfs(index + 1)
            # If the current character is alphabetic, we can change its case
            if current string[index].isalpha():
                # Flip the case: if the current character is uppercase, make it lowercase and vice versa
                current string[index] = chr(ord(current string[index]) ^ 32)
                # Continue the search with the flipped case character
                dfs(index + 1)
                # Revert the change for backtracking purposes
                current_string[index] = chr(ord(current_string[index]) ^ 32)
        # Convert the input string to a list, making it mutable
        current string = list(s)
        # Initialize a list to store all possible permutations
        permutations = []
        # Start the depth-first search from the first character
        dfs(0)
        # Return the computed permutations
        return permutations
# Example of usage:
# sol = Solution()
# result = sol.letterCasePermutation("a1b2")
# print(result) # Output: ["a1b2", "a1B2", "A1b2", "A1B2"]
Time and Space Complexity
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Time Complexity: To analyze the time complexity, let us consider the number of permutations possible for a string with n characters. Each

includes building a string of length n.

character can either remain unchanged or change its case if it's an alphabetic character. For each alphabetic character, there are 2 possibilities (uppercase or lowercase), while non-alphabetic characters have only 1 possibility (as they don't have case). If we assume there are m alphabetic characters in the string, there would be 2^m different permutations.

The given Python code generates all possible permutations of a string s where the permutation can include lowercase and

uppercase characters. A depth-first search (DFS) algorithm is employed to explore all possibilities.

The DFS function is recursively called twice for each alphabetic character (once without changing the case, once with the case changed), and it's called once for each non-alphabetic character. Thus, the time complexity of this process can be represented

as:

Space Complexity:

The space complexity includes the space needed for the recursion call stack as well as the space for storing all the permutations. The maximum depth of the recursive call stack would be n, as that's the deepest the DFS would go. The space needed for ans will be $0(2^m * n)$ as we store 2^m permutations, each of length n.

0(2^m * n), where n is the length of the string and m is the number of alphabetic characters in the string as each permutation

However, one might consider the space used for each layer of the recursion separately from the space used to store the results since the latter is part of the problem's output. If we only consider the space complexity for the recursion (excluding the space for the output), then the space complexity would be O(n).

Combining both the space for the recursion and the output, the space complexity can be represented as: $0(2^m * n + n)$, which simplifies to $0(2^m * n)$ when considering 2^m to be significantly larger than n.

In conclusion, the time complexity is $0(2^m * n)$ and the space complexity is $0(2^m * n)$ when accounting for both the recursion stack and the output list.