1079. Letter Tile Possibilities String Backtracking Medium Hash Table Counting Leetcode Link

# In this problem, you are given n tiles, each with a letter printed on it. The problem requires you to determine the total number of

Problem Description

number of tiles available, provided that the frequency of each tile is not exceeded. Intuition To solve this problem, one efficient approach is to use depth-first search (DFS) along with backtracking. Here's the thought process:

distinct non-empty sequences of letters that you can create using these tiles. You may use each tile as many times as it appears. A

sequence of letters is a string created by concatenating the tiles in any order, and sequences can be of any length from 1 to the total

occurrences of each letter in the string tiles. 3. For each letter in the counter, if there's at least one tile of that letter left (i.e., count > 0), you can: Add it to your current sequence (and add one to the answer since adding this letter is a valid sequence by itself),

2. To keep track of the tiles you have used, you use the Count of each tile. A Counter is ideal since it allows you to count the

1. Every tile can be included or excluded in a sequence, and you count all sequences as you generate them.

- Decrease the count of that tile, Continue the search (recursive DFS call) to consider longer sequences that can be made by adding additional tiles, Increment the count back after the recursive call to backtrack and consider the next letters for the current position in the
- sequence.
- 4. This process counts all the valid letter sequences without overusing any single tile, as the counter ensures that you don't use more instances of a letter than are available.
- 5. Given the recursive nature of the approach, the base case is when there are no more tiles to be placed, at which point the recursion unwinds and accumulates the count of sequences. 6. You initiate the process by calling the dfs function with the Counter of the tiles, and return the total count of sequences minus
- one since the empty sequence is not considered a valid sequence but will be counted in the initial call. By utilizing this approach, the problem is broken down into smaller subproblems, where each subproblem deals with constructing
- sequences by either including or excluding a particular letter and then recursing on the remaining letters. Solution Approach

1. Counter Data Structure: The solution first creates a Counter from the collections module for the tiles string. The Counter is a dictionary subclass designed to keep track of the number of occurrences of each element. In this case, it keeps the count of how many times each letter appears in the tiles.

2. Depth-First Search (DFS): The dfs function is the core part of the solution. It takes a Counter (which represents the remaining

The provided Python solution makes use of a depth-first search (DFS) to explore all possible sequences of letters that can be made

from the given tiles. Let's delve deeper into the steps of the implementation:

tiles available for forming sequences) as its argument.

steps:

can be formed.

Example Walkthrough

Start Depth-First Search (DFS)

3. Recursive Exploration: Within this function, a loop iterates over each distinct letter in the Counter along with its count. For each letter:

Increment the answer (ans += 1) since using this single letter is a valid sequence.

when it is called with an empty counter or with a counter where all letters have been used up.

is one less than the count returned from dfs, effectively excluding the empty sequence.

We initialize a Counter for the tiles, resulting in Counter({'A': 2, 'B': 1}).

Now, let's go through the depth-first search process with the Counter.

We recursively call dfs with the updated Counter.

We increment the answer count for sequence "AA".

'A' is no longer available, but 'B' is. We use 'B', leaving Counter empty.

Inside Recursive Call 1 (With 'A' Used Once)

Recurse with this Counter.

Inside Recursive Call 2 (With 'AA')

If the letter's count is greater than zero (meaning the letter is available for use), the algorithm progresses with the following

■ Reduce the count of this letter in the Counter (cnt[i] -= 1) to indicate that one instance of the letter has been used.

 Perform the recursive call to dfs(cnt), which will return the count of all sequences formed by the remaining letters. Add this count to the ans. After exploring all sequences with the current letter used, backtrack by restoring the letter's count (cnt[i] += 1). 4. Backtracking: This ensures that the function explores all the sequences that can be formed when the current letter is not used

in further extensions of the current sequence. This makes sure that any one sequence is not counted more than once.

6. Final Count: The return from the initial call to dfs will be the total number of valid sequences that can be formed. This count includes the empty sequence as well, which is not desired according to the problem statement. Hence, the final result returned

5. DFS Call and Result: The initial call to the dfs function is made with the Counter of the tiles. The dfs function will implicitly return

k) and their counts. It explores all subsets of tiles, therefore in the worst case when all letters are unique, the time complexity would be O(2<sup>n</sup>), but with repeated letters, the algorithm does not re-explore identical subsets, which improves efficiency.

The solution capitalizes on recursion and backtracking to explore all unique permutations of the tiles. It counts each sequence as it

builds them up and backtracks to explore new sequences, ensuring that the final count includes all possible non-empty strings that

7. Time Complexity: The time complexity of this approach depends on the number of different letters in tiles (let's denote this as

and 1 'B' tile. We want to count all distinct non-empty sequences of letters that can be made with these tiles. Initialization

Let's use a small example to illustrate the solution approach. Suppose the given tiles string is "AAB". This means we have 2 'A' tiles

Iteration 1: Choosing 'A' We take one 'A' from the Counter, leaving us with Counter({'A': 1, 'B': 1}). Increase the answer count by 1, as "A" is a valid sequence.

After the recursion returns, we backtrack, returning the 'B' to the Counter, making it Counter({'A': 0, 'B': 1}) again.

# We increment the answer for "AAB". Recurse with an empty Counter, which is the base case and returns.

**Backtrack to Recursive Call 1** 

Iteration 1: Backtracking

We finish exploring with "AA", so we exit and return to the first level of recursion.

We can still use 'A', so we take another 'A'. Now the Counter is Counter ({'A': 0, 'B': 1}).

 We return the 'A' to the Counter from the first 'A' use, so it's Counter({'A': 1, 'B': 1}) again. Now we consider using 'B' instead of 'A' at this level.

We take the 'B', leaving us with Counter({'A': 2}).

Two 'A's are available. Use one 'A' and increase the count for "BA".

Recurse with an empty Counter, which is the base case and returns.

We restore the 'A' to the Counter, and it's Counter({'A': 2}) again.

Place the 'B' back, having now counted "B", "BA", and "BAA" as valid sequences.

End of recursion since all possibilities have been considered.

Increase the answer count for "B".

Inside Recursive Call 3 (With 'B' Used)

Recursively call dfs with this Counter.

. One 'A' left. Increase the answer for "BAA".

# Recurse with Counter({'A': 1}).

Iteration 2: Backtracking

**Final Answer** 

our final answer.

Conclusion

Python Solution

class Solution:

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35 }

29 };

};

Typescript Solution

31 # Example usage:

32 # sol = Solution()

Java Solution

class Solution {

from collections import Counter

Inside Recursive Call 4 (With 'BA')

Iteration 2: Choosing 'B'

**Backtrack to Recursive Call 3** 

We have counted "A", "AA", "AAB", "B", "BA", and "BAA". Thus, we have 6 distinct non-empty sequences that can be created, which is

By going through the above steps, we explore all possible sequences that can be formed with the given tiles, by including or

# Recursively count further possibilities by using the recently used tile.

# Undo the choice to backtrack and allow for different combinations.

# Start DFS with the count of available tiles to find all possible combinations.

excluding each tile, while ensuring we never exceed the available count of each letter. This depth-first search with backtracking is an

**Finalization** The initial dfs call returned the number of valid sequences, including the empty sequence. So, we subtract one from the answer to exclude the empty sequence, which results in a final answer count of 6 - 1 = 5 different non-empty sequences.

efficient method to solve this combinatorial problem.

def numTilePossibilities(self, tiles: str) -> int:

# Iterate through each tile in the counter.

tile\_counter[tile] += 1

return combinations\_count

tile\_counter = Counter(tiles)

return dfs(tile\_counter)

33 # result = sol.numTilePossibilities("AAB")

# Count the occurrences of each tile.

public int numTilePossibilities(String tiles) {

for (char tile : tiles.toCharArray()) {

int[] count = new int[26];

count[tile - 'A']++;

if (count[i] > 0) {

for (char tile : tiles) {

int result = 0;

return dfs(count);

for (const tile of tiles) {

let sum = 0;

return sum;

return dfs(count);

Time and Space Complexity

return dfs(count);

# Return the total number of combinations.

def dfs(tile\_counter: Counter) -> int:

for tile, count in tile\_counter.items(): # If there is at least one tile available, use one to form a new sequence. 11 if count > 0: 13 combinations\_count += 1 # Include this tile as a new possibility. tile counter[tile] -= 1 # Use one tile. 14 15

combinations\_count += dfs(tile\_counter)

34 # print(result) # Output will be the number of possible sequences that can be formed.

// Method to calculate the number of possible permutations of the tiles

// Array to hold the count of each uppercase letter from A to Z

// Increment the respective array position for each character in tiles string

// Start the recursive Depth-First Search (DFS) to calculate permutations

// If count of a particular character is positive, process it

// Increase the sum as we have found a valid character

// Decrease the count for that character as it is being used

int count[26] = {}; // Initialize array to store the count of each letter

if (count[i] > 0) { // If the tile character is available

++count[i]; // Backtrack and add the tile back

// Start the recursion with the initial count and return the result

// Function to calculate the number of possible sequences from a given set of tiles

// Increment the sum for the current combination

// Add the number of combinations from the sub-problem

// Choose the tile and explore further

// Return the total number of combinations found

// Start the depth-first search with the initial count array

// Backtrack and return the tile to the pool

// Iterate through each tile and increment the corresponding count

count[tile.charCodeAt(0) - 'A'.charCodeAt(0)]++;

// Depth-first search function to explore all combinations

// Create a counter array initialized with zeros for each letter of the alphabet

++count[tile - 'A']; // Increase the count for the corresponding letter

// Define the recursive depth-first search function that calculates the possibilities

++result; // This is a valid possibility by adding one tile

result += dfs(count); // Explore further and add the result

return result; // Return the total possibilities at this recursion level

--count[i]; // Use one tile of the current character to explore further

// Count the occurrences of each letter in the tiles string

function<int(int\* count)> dfs = [&](int\* count) -> int {

// Iterate over all possible tile characters

for (int i = 0; i < 26; ++i) {

function numTilePossibilities(tiles: string): number {

const count: number[] = new Array(26).fill(0);

const dfs = (count: number[]): number => {

// Loop through the alphabet

count[i]--;

count[i]++;

sum += dfs(count);

sum++;

# Helper function to perform depth-first search on tile counts.

combinations\_count = 0 # Initialize the count of combinations.

## 13 14 // Recursive Depth-First Search method to calculate possible permutations private int dfs(int[] count) { 15 int sum = 0; // Initialize sum to hold number of permutations 16 // Iterate over the count array 17 for (int i = 0; i < count.length; i++) { 18

24 count[i]--; // Further deep dive into DFS with reduced count 25 sum += dfs(count); 26 27 // Once DFS is back from recursion, revert the count used for the character 28 count[i]++; 29 30 // Return the sum of permutations 31 32 return sum; 33 34 } 35 C++ Solution 1 class Solution { 2 public: int numTilePossibilities(string tiles) {

## for (let i = 0; i < 26; ++i) { // If a tile of the current letter is available, explore further combinations 16 19

};

grows factorially with the number of unique characters in the input string. In the worst case, all characters are unique, which would mean for a string of length n, there would be n! permutations. At each level of the recursion, we iterate through all the unique characters left in the counter, decreasing the count for that character and then proceeding with the DFS. The recursion goes as deep as the number of characters in the string, and in each level, it branches based on the number of characters left. Therefore, the upper bound for the time complexity can be represented as O(n!), where n is the length of the tiles string. However,

because the actual running time depends on the number of unique characters, if we let k be the number of unique characters, a

The space complexity is mainly determined by the call stack used for the recursive DFS calls, and the Counter object that maps characters to their counts. The maximum depth of the recursive call stack is n, which is the number of characters in the tiles string. Therefore, the space complexity for the recursion stack is O(n). The Counter object will have a space complexity of O(k), where k is the number of unique characters in the tiles string, which is less

by the Counter object.

string. Let's analyze both the time complexity and space complexity of the code. **Time Complexity** The time complexity of this function is determined by the number of recursive calls made to generate all possible sequences, which

The given code uses a depth-first search (DFS) strategy with backtracking to generate all unique permutations of the given tiles

more precise representation would be O(k^n), because at each step, we can choose to add any of the remaining k characters to the sequence.

Space Complexity

Thus, the total space complexity of the algorithm can be considered as O(n) because the recursion depth dominates the space used

than or equal to n.

In conclusion, the time complexity of this code is  $O(k^n)$  and the space complexity is O(n), where n is the total length of the input

string and k is the number of unique characters.