Enumeration

Problem Description

Array

Easy

fulfill two conditions: 1. The sum of three elements at indices a, b, and c is equal to the element at index d: nums[a] + nums[b] + nums[c] == nums[d].

In this LeetCode problem, we are given an integer array nums. Our task is to find the count of unique quadruplets (a, b, c, d) that

- 2. The indices a, b, c, and d must follow a strict increasing order, such that a < b < c < d.
- The objective is to determine how many such quadruplets exist in the provided array.

Intuition

To solve this problem, the intuition is to iterate over the array in a structured way so that we can check possible combinations that

a counting approach to aid in this process. The solution employs a hashmap, which in Python is provided by the Counter class from the collections module, to keep track of the differences between nums [d] and nums [c]. This is valuable because if we fix b and c, and find a d > c, we can update our counter

fulfill the given conditions without redundancy. Instead of checking every possible quadruplet, which could be inefficient, we can use

for the difference nums[d] - nums[c]. Then, for all a < b, we can directly check if the sum nums[a] + nums[b] is present as a key in our counter. This represents the fact that nums[d] exists such that nums[a] + nums[b] + nums[c] == nums[d]. The approach involves reverse iterating over the potential b indices starting from the third-to-last index down to the first index (since a must be less than b). After fixing b, we iterate over c and d to the end of the array and update the counter for each such pair. Then,

in another loop moving from 0 to b, we use the counter to check how many times nums[a] + nums[b] appears as a sum nums[d] -

nums [c], as that indicates valid quadruplets. The count of these occurrences is added to the total answer (ans). By using this method, we avoid the need to individually check each quadruplet and improve the efficiency of the algorithm significantly, leading to a solution that can handle arrays with larger numbers of elements.

The implemented solution follows a three-pointer approach that uses the Counter data structure to optimize the searching process for the sum condition specified in the problem statement.

1. Initialize a variable ans to keep track of the total count of valid quadruplets and obtain the length n of the given nums array.

Here is how the algorithm unfolds:

Solution Approach

2. Prepare a Counter object named counter that is going to keep track of the frequency of the differences nums [d] - nums [c] observed thus far in the remaining part of the array to the right of b.

there is enough space for c and d to the right, as the condition a < b < c < d must be respected.

represents the number of valid quadruplets with the current a and b.

4. For each fixed b, iterate forwards through the indices c and d, where c starts immediately after b and d moves past c towards the end of the array. For each c and d pair, update the counter to record the frequency of nums[d] - nums[c]. This setup aids in the

3. Perform a reverse iteration over the potential b positions, starting from n-3 and decrementing down to 1. This step ensures that

future checking of the sum condition without extra iteration through the array. 5. After populating the counter for a specific b, start another loop from 0 up to b - 1 to find valid a indices. With a and b fixed, and the counter holding information for all c and d pairs beyond b, we can find out how many times nums [a] + nums [b] appears as a

sum nums[d] - nums[c]. For each a, increment the total count and by the value of counter[nums[a] + nums[b]], which

6. Return the total count ans as the final result. The Counter is crucial as it serves as a hash map (dictionary in Python) to efficiently record and access frequency counts of specific sum differences. This allows for constant-time lookups which are much faster than iterating over the array to find matching sums for each potential quadruplet.

By optimizing the lookup process and managing how we iterate through the array, this solution avoids the naive approach that would

otherwise have a much higher time complexity. The use of a Counter combines with strategic pointer movement to solve this

Let's consider an example to illustrate the solution approach. Suppose we have the following integer array nums: 1 nums = [1, 1, 2, 2, 3, 3, 4]

○ We start by setting c = 5 and d = 6. Since nums[d] - nums[c] = 4 - 3 = 1, update counter to have counter[1] = 1.

• For a = 0: The sum nums[a] + nums[b] = 1 + 3 = 4. The counter has 1 for key 1, which does not match, so no valid

3. Begin reverse iteration for b starting from n-3, which is index 4. This leaves room for c and d.

Reset counter.

since we've observed another 1.

problem in a more efficient manner.

Example Walkthrough

Let's walk through the algorithm:

For b = 4 (nums[b] is 3):

4. Now, for this b (index 4), we loop over all a less than b. We can only consider a at indices 0, 1, 2, and 3.

2. Prepare an empty Counter object named counter to keep track of the frequency of the differences observed.

Checking each a:

There's no more room to increment c and d, so we proceed to the next step.

We initialize counter to an empty state again since we shift b leftward.

5. Move b to the next index, 3 (nums [b] is 2), and repeat steps 3 and 4.

by strategically checking for the sums that align with our conditions.

def countQuadruplets(self, nums: List[int]) -> int:

for b_index in range(length - 3, 0, -1):

int[] differenceCounter = new int[310];

for (int b = length - 3; b > 0; b--) {

for (int a = 0; a < b; ++a) {

1 // Define a global array to store input numbers.

5 let frequency: number[] = new Array(310).fill(0);

count += frequency[nums[a] + nums[b]];

fill(frequency.begin(), frequency.end(), 0);

// Reset the frequency array for the next iteration.

return count; // Return the final count of special quadruplets.

4 // Global array to store the frequencies of values for the differences of c and d.

// If a sum of nums[a] and nums[b] happened to be the difference

// This ensures that we only count the differences relevant to the current 'b'.

// previously recorded, it contributes to the total count.

for (int d = c + 1; d < length; d++) {

int difference = nums[d] - nums[c];

++differenceCounter[difference];

int c = b + 1;

frequency_counter = Counter()

c_index = b_index + 1

count = 0 # Initialize the count of quadruplets to 0

length = len(nums) # Store the length of the input list

Iterate from the third last element down to the second element

// Counter array to hold the frequency of differences between nums[d] and nums[c]

// We are calculating the frequency of the difference between nums[d] and nums[c]

// and storing it in our counter. This will help us to check for quadruplets quickly later.

if (difference >= 0) { // Ensure we don't have a negative index for the counter array

// We are iterating from the third last element down to the second element

// Initialized to 310 based on the constraints that nums[i] <= 100

// because we need at least two more elements for 'c' and 'd'

Start c_index from the element right after b_index

Update the frequency counter for each pair (c, d)

for d_index in range(c_index + 1, length):

return count # Return the final count of quadruplets

Counter to track the frequency of (nums[d] - nums[c])

1. Initialize ans to 0 as the counter and obtain the length of nums, which is n = 7 in this case.

- quadruplet is found here. \circ For a = 1: The sum nums[a] + nums[b] = 1 + 3 = 4. Again, no valid quadruplet.
- For a = 2: The sum nums[a] + nums[b] = 2 + 3 = 5. Again, no valid quadruplet. For a = 3: The sum nums[a] + nums[b] = 2 + 3 = 5. Again, no valid quadruplet.
- For b = 3:
 - Start c at 4 and d > c. Suppose c = 4 and d = 5, nums[d] nums[c] = 3 2 = 1, we update the counter to counter[1] = 1.

• Move d to 6, nums[d] - nums[c] = 4 - 2 = 2, the counter is updated to counter[2] = 1.

For a = 1: The sum nums[a] + nums[b] = 1 + 2 = 3. Again, no match and no valid quadruplet.

- Loop over a indices less than 3: For a = 0: The sum nums[a] + nums[b] = 1 + 2 = 3. This does not match any key in the counter.
- quadruplet, (nums[a], nums[b], nums[c], nums[d]) = (2, 2, 2, 4). So, ans = ans + counter[4 nums[b]] = 0 + 1 = 1. 6. We would continue to reverse iterate b down to the index 1 and repeat the above steps. However, for the sake of brevity, let's stop the walkthrough here.

The total ans at the end of the full iteration (not shown for the entire array to keep this brief) would give us the count of all unique

This walkthrough demonstrates how the combination of reverse iteration and the use of a Counter can efficiently solve the problem

quadruplets where the sum of elements at a, b, and c equals the element at d, while maintaining the order a < b < c < d.

• For a = 2: The sum nums[a] + nums[b] = 2 + 2 = 4. The counter has 2 for key 2, which matches. We found one valid

There's no more room for d, move c to 5, and d to 6, nums[d] - nums[c] = 4 - 3 = 1, the counter is now counter[1] = 2

Python Solution from collections import Counter # Importing Counter from collections module class Solution:

frequency_counter[nums[d_index] - nums[c_index]] += 1 19 # Count quadruplets for each pair (a, b_index) 20 21 for a_index in range(b_index): 22 count += frequency_counter[nums[a_index] + nums[b_index]]

```
class Solution {
    public int countQuadruplets(int[] nums) {
        int count = 0; // Holds the number of valid quadruplets found
        int length = nums.length; // The length of the input array
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Java Solution

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               // Now we check for all 'a' values that come before 'b'
               // For each 'a', if the sum of nums[a] and nums[b] exists as an index in the counter array,
25
26
               // it means there exists a 'c' and 'd' such that nums[a] + nums[b] = nums[c] + nums[d].
27
               // Hence, we add the frequency (number of occurrences) of that sum (difference) to the count of quadruplets.
28
               for (int a = 0; a < b; ++a) {
29
                    int sum = nums[a] + nums[b];
                    count += differenceCounter[sum];
30
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34
            return count; // Return the total count of quadruplets found
35
36 }
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C++ Solution
 1 class Solution {
 2 public:
       // Function to count the number of special quadruplets [a, b, c, d] in the given array.
       // A quadruplet is considered special if a + b + c = d.
       int countQuadruplets(vector<int>& nums) {
           int count = 0; // This will hold the final count of special quadruplets.
           int size = nums.size(); // Get the size of the input array.
           vector<int> frequency(310, 0); // Array to store the frequencies of values for the differences of c and d.
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           // Start from the second-to-last element and go backwards, as this is the 'b' in the quadruplet.
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           for (int b = size -3; b > 0; --b) {
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               // 'c' is always to the right of 'b', so start from 'b + 1'.
               for (int c = b + 1; c < size - 1; ++c) {
13
                    // 'd' is always to the right of 'c', so start from 'c + 1'.
14
                    for (int d = c + 1; d < size; ++d) {
15
                       if (nums[d] - nums[c] >= 0) {
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17
                           // Increment the frequency of this particular difference.
                           frequency[nums[d] - nums[c]]++;
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               // Now looking for 'a' which is to the left of 'b'.
```

// Function to count the number of special quadruplets [a, b, c, d] in 'nums' array.

Typescript Solution

2 let nums: number[] = [];

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// A quadruplet is considered special if a + b + c = d.
    function countQuadruplets(): number {
         let count = 0; // This will hold the final count of special quadruplets.
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 11
         let size = nums.length; // Get the size of the input array.
 12
 13
        // Start from the second-to-last element and go backwards, as this is the 'b' in the quadruplet.
 14
         for (let b = size - 3; b > 0; --b) {
 15
            // 'c' is always to the right of 'b', so start from 'b + 1'.
 16
             for (let c = b + 1; c < size - 1; ++c) {
                // 'd' is always to the right of 'c', so start from 'c + 1'.
 17
                for (let d = c + 1; d < size; ++d) {
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 19
                    if (nums[d] - nums[c] >= 0) {
 20
                        // Increment the frequency of this particular difference.
 21
                        frequency[nums[d] - nums[c]]++;
 22
 23
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 25
            // Now looking for 'a' which is to the left of 'b'.
 26
             for (let a = 0; a < b; ++a) {
 27
                // If a sum of nums[a] and nums[b] happened to be the difference
                // previously recorded, it contributes to the total count.
 28
 29
                count += frequency[nums[a] + nums[b]];
 30
 31
            // Reset the frequency array for the next iteration.
 32
            // This ensures that we only count the differences relevant to the current 'b'.
 33
             frequency.fill(0);
 34
 35
         return count; // Return the final count of special quadruplets.
 36 }
 37
 38 // Example usage:
 39 // nums = [1, 2, 3, 4];
 40 // let result = countQuadruplets();
 41 // console.log(result); // Should log the count of special quadruplets
 42
Time and Space Complexity
The given Python code defines a method countQuadruplets which counts the number of quadruples (a, b, c, d) in an array nums
where a < b < c < d and nums[a] + nums[b] + nums[c] == nums[d].
```

Time Complexity: The outermost loop runs from the third-to-last element to the beginning (n - 3 to 1), which gives us at most n iterations. Inside this

loop, we have two nested loops: 1. The first nested loop iterates over the range from c + 1 to n - 1, where c starts from b + 1. In the worst case, this loop runs for n - b - 2 iterations.

- factor of n/2 iterations.
- The nested loops are not entirely independent: as b decreases, the number of iterations in the first nested loop increases, but the iterations in the second nested loop decrease proportionally.

2. The second nested loop runs from 0 to b - 1. In the worst-case scenario, where b is close to n / 2, this loop also contributes a

- The time complexity of these nested loops is hence proportional to the sum of the two sequences, which forms an arithmetic progression from 1 to approximately n/2. The sum of the first n/2 positive integers is given by (n/2) * ((n/2) + 1) / 2, simplifying to 0(n^2).
- Therefore, the overall time complexity of the function is $O(n^2)$.
- The space complexity is governed by the Counter object, which stores a mapping of the differences between nums [d] and nums [c]. In

Space Complexity:

- Thus, the space complexity of the function is O(n).
- the worst case, the Counter could store up to n different values if all the differences are unique. This gives us a space complexity of O(n) for the counter variable.