1030. Matrix Cells in Distance Order

Matrix

Sorting

Array Math

### Leetcode Link

## Problem Description

Geometry

Easy

four integers (row, cols, rCenter, cCenter), the problem defines a matrix of size rows x cols. Your position in the matrix is initially at the cell with coordinates (rCenter, cCenter). The goal is to return a list of coordinates of all cells in the matrix, sorted based on their Manhattan distance from the center cell

You are tasked with finding the coordinates of all cells in a given matrix, ordered by their distance from a specified center cell. Given

(rCenter, cCenter). The Manhattan distance between two points (r1, c1) and (r2, c2) is calculated as |r1 - r2| + |c1 - c2|. In other words, it's the sum of the absolute differences of their corresponding coordinates.

You have the flexibility to provide the sorted coordinates in any order as long as they are arranged from the nearest to the farthest

distance from the center cell. Intuition

as Breadth-First Search (BFS). Manhattan distance has an interesting property where cells that are an equal distance from a given point form a diamond shape

The intuition behind the solution to this problem lies in the properties of the Manhattan distance and an algorithmic technique known

when graphed on the matrix. Since the problem asks us to order the cells by their distance from a center cell, using the BFS algorithm, we can ensure that we process cells in layers - starting with the center cell and moving outwards one distance unit at a time. Therefore, the approach is to create a queue and start from the center cell, adding it to the queue. We repeatedly take a cell from the

This method ensures that we add cells to our answer list in increasing distance order without explicitly calculating the distance for every cell from the center. Once there are no more cells to add, we have processed the whole matrix, and our answer list contains all cells in the required sorted order.

front of the queue, add it to our answer list, and then add all its unvisited neighboring cells that are one unit away. To avoid adding

the same cell multiple times, we also keep track of all visited cells using a boolean matrix called vis.

Solution Approach The implementation of the solution uses Breadth-First Search (BFS) to explore the matrix starting from the given center. Here's a step-by-step walkthrough explaining how the given Python code achieves this:

1. Initialize Data Structures: A queue q is used to store cells for exploration, and it's implemented using a deque to allow efficient

popping from the front. A 2-dimensional list vis keeps track of visited cells; initially, all cells are marked as unvisited (False).

### 2. Queue Starting Cell: The starting cell, given by the coordinates (rCenter, cCenter), is added to the queue and marked as

cols.

Example Walkthrough

visited in the vis matrix. 3. Process Cells in Queue: The algorithm enters a while-loop that continues until the queue is empty. At each step, we process all

4. Explore Neighbors: Within the loop, for each cell (p) taken from the queue, its neighbors are determined by iterating over the relative positions represented by (-1, 0, 1, 0, -1) using the pairwise function which gives us pairs of relative coordinates for

cells currently in the queue, ensuring that all neighbors one unit away are considered before moving to a larger distance.

- the four directions (up, right, down, left). These are used to calculate the neighboring cells' coordinates (x, y). 5. Boundary and Visit Checks: Before a neighboring cell is added to the queue, there are two checks:
- Visit Check: The vis matrix is checked to ensure the cell has not been visited before. If it hasn't, it is marked as visited. 6. Enqueue and Store Results: If a neighbor passes these checks, it is appended to the queue for subsequent exploration and also added to the growing result set ans.

7. Return Results: After the while loop exits (when the queue is empty), it means that all cells have been explored according to

their distance from the center, and the ans list contains them in the order of increasing Manhattan distance. The list ans is

Boundary Check: The coordinates (x, y) must be inside the matrix, which is checked with 0 <= x < rows and 0 <= y <</li>

- returned as the final output. The algorithm efficiently traverses the matrix in a manner that naturally sorts the cells by their Manhattan distance, eliminating the
- need for an explicit sort operation, and is a classic example of BFS applied to grid traversal problems.
- 3×3 grid. The center cell is given by rCenter = 1 and cCenter = 1. The matrix with Manhattan distance from the center cell looks like this:

Let's illustrate the solution approach using a small example. Suppose our matrix size is defined by rows = 3 and cols = 3, creating a

Initialization: Queue q is initialized and contains the starting cell coordinates (1, 1).

### Starting cell (1, 1) is marked as visited in vis and added to q.

**Explore Neighbors:** 

Boundary and Visit Checks:

1), (1, 2), (0, 1).

Queue Starting Cell:

3 1 1 1

Process Cells in Queue: We begin processing by popping (1, 1) from the queue.

All neighbors are within the boundaries of the matrix and none of them are visited. They are marked as visited and added to the

The order of neighbors being added to q and result set ans may vary, but let's assume they're added in the sequence (1, 0), (2,

In the end, ans would look like [(1, 1), (1, 0), (2, 1), (1, 2), (0, 1), (0, 0), (0, 2), (2, 0), (2, 2)] or any other such

Enqueue and Store Results:

queue q.

Return Results:

The next level of neighbors would be the corners, (0, 0), (0, 2), (2, 0), (2, 2), each with Manhattan distance of 2.

The process continues until all cells have been added to ans.

sequence that preserves the non-decreasing Manhattan distance order.

# Directions for moving up, right, down, and left

directions = [(-1, 0), (0, 1), (1, 0), (0, -1)]

# Dequeue the front cell of the queue

for delta\_row, delta\_col in directions:

new\_row = current\_cell[0] + delta\_row

new\_col = current\_cell[1] + delta\_col

# Mark the new cell as visited

visited[new\_row][new\_col] = True

queue.append([new\_row, new\_col])

# Return the cells in the order they were visited

current\_cell = queue.popleft()

result.append(current\_cell)

Visited matrix vis is initialized with all values set to False.

The neighbors of (1, 1) are (1, 0), (2, 1), (1, 2), (0, 1).

This demonstrates how the BFS approach efficiently processes each layer of cells, grouped by their Manhattan distance to the center cell, until all cells have been visited and added to the result in the required sorted order.

from collections import deque

result = []

while queue:

return result

from typing import List

Python Solution

class Solution:

visited = [[False] \* cols for \_ in range(rows)] visited[r\_center][c\_center] = True 11 12 # List to store the cells in the order of increasing distance from the center

def allCellsDistOrder(self, rows: int, cols: int, r\_center: int, c\_center: int) -> List[List[int]]:

# Initialize a queue with the starting cell, which is the center cell

# Perform a Breadth-First Search (BFS) starting from the center cell

# Try moving in all four directions from the current cell

# Check if the new cell is within grid bounds and hasn't been visited

# Add the new cell to the queue to explore its neighbors later

// Check for valid boundary conditions and unvisited state

// Add new cell's coordinates to the queue

vector<vector<int>>> allCellsDistOrder(int rows, int cols, int rCenter, int cCenter) {

queue.emplace(rCenter, cCenter); // Start from the center cell

// Mark the new cell as visited

queue.offer(new int[] {x, y});

// Return the result array containing all cell coordinates

visited[x][y] = true;

if  $(x >= 0 \&\& x < rows \&\& y >= 0 \&\& y < cols \&\& !visited[x][y]) {$ 

if 0 <= new\_row < rows and 0 <= new\_col < cols and not visited[new\_row][new\_col]:</pre>

queue = deque([[r\_center, c\_center]]) # Create a 2D list to keep track of visited cells 10

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return result;

// Queue to perform BFS

queue<pair<int, int>> queue;

// Initialize answer vector

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Java Solution
   import java.util.ArrayDeque;
  2 import java.util.Deque;
    class Solution {
         // Method to return the coordinates of all cells in the matrix, sorted by their distance from (rCenter, cCenter)
         public int[][] allCellsDistOrder(int rows, int cols, int rCenter, int cCenter) {
  6
             // Initialize a queue to perform the breadth-first search
             Deque<int[]> queue = new ArrayDeque<>();
  8
             // Start from the center cell
  9
             queue.offer(new int[] {rCenter, cCenter});
 10
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 12
             // Create a visited matrix to keep track of visited cells
 13
             boolean[][] visited = new boolean[rows][cols];
 14
             // Mark the center cell as visited
 15
             visited[rCenter][cCenter] = true;
 16
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             // Create a result array to hold all cells in the required order
 18
             int[][] result = new int[rows * cols][2];
 19
             // Use the `dirs` array to explore in all four directions
             int[] dirs = \{-1, 0, 1, 0, -1\};
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             // Index to insert the next point in `result`
 22
             int index = 0;
 23
 24
             // Perform breadth-first search
 25
             while (!queue.isEmpty()) {
 26
                 for (int size = queue.size(); size > 0; size--) {
 27
                     // Get the current cell from the queue
 28
                     int[] point = queue.poll();
 29
                     // Assign the current cell's coordinates to the result array
                     result[index++] = point;
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                     // Explore the neighbors of the current cell
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                     for (int k = 0; k < 4; ++k) {
 34
                         int x = point[0] + dirs[k], y = point[1] + dirs[k + 1];
```

### 13 vector<vector<int>> answer; 14 15 // Visited matrix to keep track of visited cells 16

public:

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// Perform BFS

while (queue.length > 0) {

// Add the current cell to the answer

// Explore the neighboring cells

for (let k = 0; k < 4; k++) {

answer.push([currentRow, currentCol]);

const newRow: number = currentRow + directions[k];

// Return the cells sorted by their distance from the center

const newCol: number = currentCol + directions[k + 1];

// Check if the new cell is within bounds and not visited

visited[newRow][newCol] = true; // Mark cell as visited

C++ Solution

#include <vector>

#include <cstring>

2 #include <queue>

class Solution {

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bool visited[rows][cols];
             memset(visited, false, sizeof(visited)); // Set all cells to unvisited
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             visited[rCenter][cCenter] = true; // Mark the center cell as visited
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             // Array to easily access all 4 surrounding cells (up, right, down, left)
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             int directions [5] = \{-1, 0, 1, 0, -1\};
 22
 23
             // Perform BFS
 24
             while (!queue.empty()) {
 25
                 int queueSize = queue.size(); // Number of elements at current level
 26
                 while (queueSize--) {
                     auto [currentRow, currentCol] = queue.front();
 28
                     queue.pop();
 29
 30
                     // Add the current cell to the answer
                     answer.push_back({currentRow, currentCol});
 31
 32
 33
                     // Explore the neighboring cells
 34
                     for (int k = 0; k < 4; ++k) {
 35
                         int newRow = currentRow + directions[k];
                         int newCol = currentCol + directions[k + 1];
 36
 37
                         // Check if the new cell is within bounds and not visited
 38
                         if (newRow >= 0 && newRow < rows && newCol >= 0 && newCol < cols && !visited[newRow][newCol]) {
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                             visited[newRow][newCol] = true; // Mark cell as visited
 41
                             queue.emplace(newRow, newCol); // Add the cell to the queue for further BFS
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             return answer; // Return the cells sorted by their distance from the center
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    };
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Typescript Solution
    type Cell = [number, number]; // Defines a type for cells
    // Define a function to calculate all cells in distance order
    function allCellsDistOrder(rows: number, cols: number, rCenter: number, cCenter: number): Cell[] {
         // Queue to perform BFS
         const queue: Cell[] = [[rCenter, cCenter]];
         // Initialize answer array
  8
         const answer: Cell[] = [];
  9
 10
 11
         // Visited matrix to keep track of visited cells. Initialize with false values.
 12
         const visited: boolean[][] = Array.from({ length: rows }, () => Array(cols).fill(false));
 13
 14
         // Mark the center cell as visited
         visited[rCenter][cCenter] = true;
 15
 16
 17
         // Array to easily access all 4 adjacent cells (up, right, down, left)
 18
         const directions: number[] = [-1, 0, 1, 0, -1];
 19
```

const [currentRow, currentCol] = queue.shift()!; // Get the first cell in the queue ! non-null assertion operator since Arr

# Time and Space Complexity

return answer;

Time Complexity

the number of cells.

For each cell, it checks all four adjacent cells (up, down, left, right), which are represented by the pairwise combinations (-1, 0, 1, 0, -1).The time complexity of this approach is O(R \* C), where R is the number of rows and C is the number of columns in the matrix. This is because each cell is visited exactly once. The check 0 <= x < rows and 0 <= y < cols happens for 4 neighbors for each of the R \*

cells, but since each neighbor is only enqueued once (guarded by vis[x][y]), the total number of operations is still proportional to

The given code uses a BFS (Breadth-First Search) approach to traverse the matrix starting from the center cell (rcenter, ccenter).

if (newRow >= 0 && newRow < rows && newCol >= 0 && newCol < cols && !visited[newRow][newCol]) {</pre>

queue.push([newRow, newCol]); // Add the cell to the queue for further BFS

Space Complexity

2. The queue q, which in the worst case may contain all cells before being dequeued, thus also requiring up to R \* C space. 3. The ans array, which will eventually hold all R \* C cells in the order they were visited. Therefore, the space required is proportional to the number of cells in the matrix.

1. The vis array, which is a 2D array used to keep track of visited cells, consuming R \* C space.

The space complexity of the code is also O(R \* C). The main factors contributing to the space complexity are: