**Two Pointers** 

Array

### **Problem Description**

Medium Greedy

You are presented with an integer array called height which represents the heights of vertical lines placed at positions indexed from 1 to n (0-indexed in the array). Imagine that each height[i] is linked to a line on a chart that extends upward from the x-axis to a point (i, height[i]). Your task is to find two lines that, along with the x-axis, enclose the greatest possible area, which represents the maximum water that can be trapped between them without allowing any spillage over the sides of the lines (the container cannot be slanted). The goal is to calculate and return this maximum trapped water area.

# Intuition

the end, and these pointers represent the potential container boundaries. At each step, the trapped water is determined by the distance between the pointers (which is the container's width) and the height of the smaller line (since the water level can't be higher than the smaller of the two boundaries). This is the area that could potentially be the maximum. To maximize the area, after calculating the trapped water at each step and comparing it to the maximum we've seen so far, we move

To solve this problem efficiently, we use a two-pointer technique. We place one pointer at the beginning of the array and the other at

the pointer at the shorter line towards the other pointer. This is because keeping the pointer at the taller line stationary and moving the shorter one might lead us to find a taller line and thus a larger area. There's no advantage in moving the taller pointer first, as it would only reduce the potential width without guaranteeing a taller line to increase height. We repeat this process of calculating, updating the maximum water area, and moving the shorter line pointer towards the other pointer until the two pointers meet, at which point we've considered every possible container and the maximum stored water has been found. By approaching this problem with each step optimized to either maintain or improve the potential maximum area, we are able to

**Solution Approach** 

## The implementation of the solution follows the two-pointer approach. Here's a step-by-step guide to how the solution works:

1. Initialize two pointers: i is set to the start of the array (0), and j is set to the end of the array (len(height) - 1).

2. Initialize a variable ans to keep track of the maximum area discovered so far. Initially, ans is set to 0.

arrive at the solution efficiently, resulting in an algorithm that runs in linear time relative to the number of lines.

- 3. Enter a loop that continues as long as i is less than j. This loop allows us to explore all possible combinations of lines from i to j to maximize the area.
- 4. Inside the loop, calculate the area trapped between the lines at pointers i and j using the formula: area = (j i) \*min(height[i], height[j]). This calculates the width of the container (j - i) and multiplies it by the height, which is the smaller of the two heights at height[i] and height[j].
- 5. Update ans with the maximum of its current value and the calculated area. ans = max(ans, area) ensures that ans holds the highest value of trapped water area at each step.
- 6. Determine which pointer to move. We need to move the pointer corresponding to the shorter line since this is the limiting factor for the height of the trapped water. We do this using a conditional statement:
- 7. Continue looping until the pointers meet. At this point, ans would have the maximum area that can be trapped between any two lines.
- This solution uses a greedy approach, and its efficiency stems from the fact that at each stage, the move made is the best possible

If height[i] < height[j], then we increment i (i += 1) to potentially find a taller line.</li>

○ Else, decrement j (j -= 1) for the same reason from the other end.

move to increase or at least maintain the potential of the maximum area. By incrementally adjusting the width and height of the considered container, it efficiently narrows down to the optimal solution.

done within the loop. **Example Walkthrough** 

The algorithm has a linear-time complexity, O(n), as each element is visited at most once, and there's a constant amount of work

Let's illustrate the solution approach using a small example.

### 1. We start with two pointers: i at the start (0), representing the first line, and j at the end (8), representing the last line. Thus, i

2. We set ans = 0, as we have not calculated any area yet.

Consider the integer array height = [1, 8, 6, 2, 5, 4, 8, 3, 7].

points to height[0] which is 1, and j points to height[8] which is 7.

- 3. Now we start our loop where i < j. Since 0 < 8, we enter the loop. 4. We calculate the area between lines at pointers i and j. The width is j - i which is 8 - 0 = 8, and the height is the smaller of
- 6. Since height[i] is less than height[j], we move the i pointer to the right to potentially find a taller line. Now i becomes 1.

7. Our two pointers now are at i = 1 and j = 8. We will continue this process until i and j meet.

5. We update ans to be the maximum of its current value and the calculated area. So, ans = max(0, 8) = 8.

two heights at height[i] and height[j], so min(1, 7) = 1. Thus, the area is 8 \* 1 = 8.

- 8. Repeat steps 4-6:
- $\circ$  Update ans to be max(8, 49) = 49. Since height[1] is greater than height[8], we move j to the left (now j is 7).

• New area at pointers i = 1 and j = 8: area = (8 - 1) \* min(8, 7) = 7 \* 7 = 49.

9. Continue iterations:

- New area at pointers i = 1 and j = 7: area = (7 1) \* min(8, 3) = 6 \* 3 = 18. • ans remains 49 since 49 > 18.
- 10. The process continues in this manner, always moving the pointer at the shorter height until i and j are equal.

amount of water that can be trapped between two lines without spilling.

# Calculate the area formed between the two pointers

// Method to find the maximum area formed between the vertical lines

// Initialize two pointers at the beginning and end of the array

// Update the maximum area if the current area is larger

} else { // Otherwise, move the right pointer to the left

return maxArea; // Return the maximum area found

int currentArea = Math.min(height[left], height[right]) \* (right - left);

current\_area = (right - left) \* min(height[left], height[right])

def maxArea(self, height: List[int]) -> int:

if height[left] < height[right]:</pre>

left, right = 0, len(height) - 1

while left < right:</pre>

height[1] is greater than height[7], so we move j to the left (now j is 6).

Python Solution

# Initialize two pointers, one at the beginning and one at the end of the height array

# Initialize maximum area to 0 max\_area = 0 8 # Use a while loop to iterate until the two pointers meet

At the end of these iterations, and holds the maximum area that can be trapped, which in this example, is 49. This is the largest

```
# Update the maximum area if current_area is larger
12
               max_area = max(max_area, current_area)
13
14
15
               # Move the pointer that points to the shorter line inward,
               # since this might lead to a greater area
16
```

9

10

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17

class Solution:

```
left += 1
18
19
               else:
20
                   right -= 1
21
22
           # Return the maximum area found
23
           return max_area
Please note that the type hint List[int] requires importing List from the typing module in Python 3.5+. If you're using Python 3.9+
it's also possible to use built-in list type hints directly like list[int]. If you want to include the necessary import, here's how you
would do that:
   from typing import List # This line is needed for the type hint (Python 3.5 - 3.8)
   class Solution:
       # ... rest of the code remains the same
Java Solution
```

// Calculate the area with the shorter line as the height and the distance between the lines as the width

### 17 // Move the pointer that points to the shorter line towards the center 18 if (height[left] < height[right]) {</pre> 19 left++; 20 21 } else {

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29 };

class Solution {

public int maxArea(int[] height) {

int right = height.length - 1;

// Variable to keep track of the maximum area

maxArea = Math.max(maxArea, currentArea);

// Iterate until the two pointers meet

int left = 0;

int maxArea = 0;

while (left < right) {</pre>

right--;

++left;

--right;

```
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24
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26
           // Return the maximum area found
27
            return maxArea;
29 }
30
C++ Solution
 1 #include <vector>
   #include <algorithm> // Include algorithm for std::min and std::max
   class Solution {
   public:
        int maxArea(vector<int>& heights) {
            int left = 0; // Starting from the leftmost index
            int right = heights.size() - 1; // Starting from the rightmost index
            int maxArea = 0; // Initialize the maximum area to 0
 9
10
           // Continue looping until the left and right pointers meet
           while (left < right) {</pre>
               // Calculate the current area with the minimum of the two heights
13
               int currentArea = std::min(heights[left], heights[right]) * (right - left);
14
               // Update the maximum area if the current area is larger
15
               maxArea = std::max(maxArea, currentArea);
16
17
               // Move the pointers inward. If left height is less than right height
18
               // then we move the left pointer to right hoping to find a greater height
19
               if (heights[left] < heights[right]) {</pre>
20
```

```
Typescript Solution
   function maxArea(height: number[]): number {
       // Initialize two pointers, one at the start and one at the end of the array
       let leftIndex = 0;
       let rightIndex = height.length - 1;
       // Initialize the variable to store the maximum area
       let maxArea = 0;
       // Iterate until the two pointers meet
       while (leftIndex < rightIndex) {</pre>
9
           // Calculate the area with the current pair of lines
           const currentArea = Math.min(height[leftIndex], height[rightIndex]) * (rightIndex - leftIndex);
           // Update maxArea if the current area is larger
12
           maxArea = Math.max(maxArea, currentArea);
14
           // Move the pointer that's at the shorter line inwards
15
           // If the left line is shorter than the right line
16
           if (height[leftIndex] < height[rightIndex]) {</pre>
               ++leftIndex; // Move the left pointer to the right
18
           } else {
19
               --rightIndex; // Move the right pointer to the left
20
21
22
       // Return the maximum area found
       return maxArea;
```

### The given Python code implements a two-pointer technique to find the maximum area of water that can be contained between two lines, given an array of line heights.

Time and Space Complexity

23 24 25 26 } 27

# **Time Complexity**

relative to the number of elements n in the height array. Hence, the time complexity is O(n).

The function initializes two pointers at the start and end of the array respectively and iterates inwards until they meet, performing a

constant number of operations for each pair of indices. Since the pointers cover each element at most once, the iteration is linear

The code uses a fixed number of integer variables (i, j, ans, and t) and does not allocate any additional memory that scales with the size of the input array.

Thus, the space complexity is 0(1).

**Space Complexity**