

Problem Description

The problem gives us an array of numbers named arr and asks us to determine whether we can rearrange the array's elements to form an arithmetic progression. An arithmetic progression is a sequence of numbers where the difference between any two consecutive numbers is always the same. For example, in the sequence [1, 3, 5, 7], the difference between consecutive elements is 2, which is consistent throughout the sequence, so it is an arithmetic progression. The goal is to return true if the given array can be rearranged to form such a sequence, or false otherwise.

Intuition

The intuition behind the solution is to first sort the array. Sorting the array is a key step because if an arithmetic progression exists, it must be the case that when sorted, the difference between each pair of consecutive elements is consistent. Once the array is sorted, we calculate the common difference, which should be the difference between the first two elements (since the sorted array should now represent an arithmetic progression if one is possible).

After calculating this common difference, we iterate through the array to check if every consecutive pair of elements has this same difference. If at any point we find a pair of elements that do not have the common difference, we can conclude that it is not possible to form an arithmetic progression and should return false. If we successfully iterate through the entire array without finding discrepancies, then the array can indeed form an arithmetic progression and we return true.

The pairwise function utilized in the solution is a Python utility that allows us to iterate through the array in element pairs which simplifies the process of checking the difference between consecutive elements. With all, we check if all pairs have the same difference d, and hence it satisfies the condition of an arithmetic progression.

The solution approach leverages a sorting algorithm and a simple iteration pattern to verify the arithmetic progression. Here's a step-

Solution Approach

by-step breakdown of the implementation applied in the provided Python code:

1. Sorting the Array: The first line in the function sorts the array in-place using arr.sort(), which is a built-in Python method that

- sorts the list ascendingly by default. The sorted array is necessary to easily compare the difference between consecutive elements. 2. Finding the Common Difference: The variable d is computed as arr[1] - arr[0] i.e., the difference between the first two
- elements of the sorted array. This difference d is what we expect between every pair of consecutive elements in an arithmetic progression. 3. Verifying the Arithmetic Progression: The last step is to verify if each consecutive pair of elements in the sorted array has the
- 4. The pairwise function is from Python's itertools module (potentially, the grouper pattern could also be used), which is used here to iterate over the array elements in pairs. Each pair of elements (a, b) consists of consecutive elements from the sorted array.

same difference d. This is done using the expression all(b - a == d for a, b in pairwise(arr)).

- 5. The all function ensures that every element of the provided iterator evaluates to True. It processes the generator expression,
- which for each pair of elements checks if the difference b a is equal to d. 6. If any pair does not satisfy this, all will immediately return False, indicating that the progression cannot be formed. Otherwise, it
- will return True, confirming that the array is indeed an arithmetic progression. The elegance of this approach lies in its simplicity and the efficient use of Python's standard libraries to achieve the desired outcome

with very few lines of code. Since sorting is the most computationally expensive part of the algorithm, the overall time complexity is O(n log n) where n is the number of elements in the array due to the sorting operation. The verification process has a time complexity of O(n) since it iterates through the sorted elements once. Therefore, the total time complexity remains O(n log n).

Let's take an example to illustrate the solution approach. Consider the array arr = [9, 5, 1, 3, 7]. Our goal is to check whether we can rearrange this array into an arithmetic progression.

Example Walkthrough

Following the solution approach:

2. Finding the Common Difference: We calculate the common difference d as the difference between the first two elements, which

form an arithmetic progression [1, 3, 5, 7, 9].

common_difference = arr[1] - arr[0]

int difference = arr[1] - arr[0];

return false;

for (int i = 2; i < arr.length; ++i) {</pre>

int commonDifference = arr[1] - arr[0];

for (size_t i = 2; i < arr.size(); i++) {

return false;

// Iterate through the array starting from the third element

if (arr[i] - arr[i - 1] != commonDifference) {

// If the difference between the current and the previous element

// is not equal to the common difference 'd', return false

// If all consecutive elements have the same difference, return true

if (arr[i] - arr[i - 1] != difference) {

is d = arr[1] - arr[0] = 3 - 1 = 2.

Calculate the common difference 'd' between the first two elements

// Iterate through the sorted array starting from the third element

// If not, return false since it can't form an arithmetic progression

1. Sorting the Array: We first sort the array, which results in arr = [1, 3, 5, 7, 9].

- 3. Verifying the Arithmetic Progression: We then check if the difference between every consecutive pair of elements is equal to d.
- \circ The difference between the second and the third elements (3 and 5) is $\frac{5}{3} = \frac{3}{3} = \frac{2}{3}$, which is equal to d.
 - \circ The difference between the fourth and the fifth elements (7 and 9) is 9 7 = 2, which is also equal to d.
- Since all pairs have the same difference, which is equal to d, the function all(b a == d for a, b in pairwise(arr)) would return

 \circ The difference between the third and the fourth elements (5 and 7) is 7 - 5 = 2, which is again equal to d.

True.

The consistent common difference and the successful run of the all function on pairwise compared elements support the conclusion that arr can be rearranged to form an arithmetic progression, and thus, the final answer is true.

Therefore, based on the solution approach, we can conclude that it is indeed possible to rearrange the array [9, 5, 1, 3, 7] to

Python Solution

```
def canMakeArithmeticProgression(self, arr: List[int]) -> bool:
    # Sort the array in non-decreasing order
    arr.sort()
```

class Solution:

from typing import List

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# Iterate over the sorted array to check if each pair of successive
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           # elements has the same difference 'd'
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           for i in range(1, len(arr) - 1):
               # If the difference between the current and next element does not equal
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               # the common difference 'd', the sequence is not an arithmetic progression
               if arr[i + 1] - arr[i] != common_difference:
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                   return False
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           # If all differences are equal, return True (it is an arithmetic progression)
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           return True
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Java Solution
   class Solution {
       // Function to check if it is possible to form an arithmetic progression
       public boolean canMakeArithmeticProgression(int[] arr) {
           // Sort the array in non-decreasing order
           Arrays.sort(arr);
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           // If the loop completes without returning false, it means the array can form an arithmetic progression
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           return true;
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23 }
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C++ Solution
 1 #include <vector> // Include the vector header
2 #include <algorithm> // Include the algorithm header for sort
   using namespace std; // Using the standard namespace
   class Solution {
   public:
       bool canMakeArithmeticProgression(vector<int>& arr) {
           // Sort the array in non-decreasing order
           sort(arr.begin(), arr.end());
           // Calculate the common difference 'd' of the first two elements
```

// Find the common difference 'difference' by subtracting the second element by the first element

// Check if the current difference is equal to the common difference 'difference'

24 return true; 25 26 };

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Typescript Solution
  // Function to check if the provided array can form an arithmetic progression
   function canMakeArithmeticProgression(arr: number[]): boolean {
       // Sort the input array in ascending order
       arr.sort((a, b) => a - b);
       const lengthOfArray = arr.length; // Store the length of the array
       // Loop through the array starting from the third element
       for (let i = 2; i < lengthOfArray; i++) {
           // Calculate the differences between the consecutive elements
           const firstDifference = arr[i - 1] - arr[i - 2];
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           const secondDifference = arr[i] - arr[i - 1];
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           // If the consecutive differences are not equal, return false
           if (firstDifference !== secondDifference) {
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               return false;
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       // If all consecutive differences are equal, return true
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       return true;
21 }
```

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Time and Space Complexity

The time complexity of the canMakeArithmeticProgression function is determined primarily by the sorting operation. In Python, the

Time Complexity

default sort function uses an algorithm called Timsort, which has a time complexity of O(n log n), where n is the length of the array. The subsequent operation consists of iterating through the sorted array to check if every pair of successive elements has the same

difference, d. This check uses a generator expression with the all() function combined with pairwise iteration, which is 0(n-1) or

simply 0(n) since it's walking through the array only once. Thus, the dominating factor here is the sorting, and the overall time complexity of the function is $0(n \log n)$.

Space Complexity

For space complexity, the sort operation can be done in-place, but certain implementations may require additional space. Python's

Timsort requires O(n) space in the worst case. The pairwise iteration does create pairs for every two adjacent elements in the array, but since this is done by the generator

expression, it doesn't create an additional list in memory, it simply iterates through the existing sorted array yielding one element at a

time.

Hence, the space complexity of the function, which is mostly governed by the sorting operation's space requirement, is O(n).