2499. Minimum Total Cost to Make Arrays Unequal
Hard Greedy Array Hash Table Counting

Leetcode Link

Problem Description

The problem provides two integer arrays nums1 and nums2, both of the same length n. The goal is to make sure that for every element at any index i, nums1[i] is not equal to nums2[i]. To achieve this, it's possible to perform operations that involve swapping any two elements in nums1. The cost of a single such operation is the sum of the indices of the elements that are being swapped. The task is to find the minimum total cost to ensure that nums1 and nums2 have no matching elements at the same index. If this condition cannot be fulfilled, the function should return -1.

Intuition

The following steps are used to arrive at the solution approach:

1. Identify all the indices where nums1[i] equals nums2[i], as we may need to swap these elements from nums1 to make them

The solution to this problem involves a few key observations. Firstly, since we only need to operate on nums1 to make it different from

different. Calculate the cost of these potential swaps and count how many times each number appears at the same index in both

nums2, we focus our attention on the indices where nums1 and nums2 have the same value.

arrays.

2. Find out if there is a particular value leading the count, that is, if it has more matches than half the number of same values across nums1 and nums2. If such a leading number is found, record the excess amount of times it leads (more than half).

3. Iterate through both arrays again and try to reduce the leading count by swapping non-leading values. Each swap will add to the

- total cost.

 4. If at the end of this process, the leading count is brought down to zero (meaning we managed to make all the necessary swaps),
- swapped, it's not possible to separate the arrays fully, and thus, we return -1.

 The code snippet provided uses this approach to systematically find the minimum cost required to ensure that nums1 and nums2

return the sum of costs formed by the operations. If there are still excess matches and no more non-leading values can be

Solution Approach

The given solution utilizes a Counter (a type of dictionary from the collections module in Python) to track duplicates between nums1

and nums2. Here's a step-by-step breakdown of the implementation:

1. Initialize two counters: ans for calculating the accumulated cost and same for counting the number of identical elements at

2. Loop through nums1 and nums2 using enumerate to get both the index i and the values a (from nums1) and b (from nums2):

corresponding indices in nums1 and nums2.

satisfy the required conditions.

• Whenever a is equal to b (which is a situation that we want to avoid), increment the same counter, accumulate the index to the ans as the initial cost, and update the Counter object cnt with the value of a. The cnt dictionary will hold elements as keys and the number of times they need to be swapped as their values.

same. This value would be the bottleneck in achieving our goal and needs special attention:

 If such a value is found, calculate the margin m by which this value exceeds half of the duplicates and store it along with the leading value lead.

4. Go through the arrays another time and use the m value to determine if we have enough non-leading elements to swap:

3. Search for a "leading" value in the cnt dictionary that has more than half of the number of indices where nums1 and nums2 are the

decrement m.
 This step effectively swaps non-leading values to reduce the number of problematic indices where nums1 and nums2 would be equal.

6. If m is still greater than zero, it implies that we couldn't find enough non-leading elements to swap, making it impossible to make

The algorithm applies a greedy approach to minimize costs, prioritizing swaps at the lowest indices. The Counter data structure is

For each pair (a, b) where a does not equal b and neither a nor b are the leading value, add the index i to the total cost and

elements, and nums1[i] != nums2[i] holds for all i. In this case, ans contains the minimum total cost and is returned.

pivotal for this approach, allowing for efficient tracking and updating of the frequencies of values that need to be swapped.

all elements at matching indices in nums1 and nums2 different. In that case, the function returns -1.

5. If after the end of this process the margin m became zero, it would mean that we have successfully swapped all necessary

Example Walkthrough

Let's illustrate the solution approach with a small example. Consider two arrays nums1 and nums2 of length 4 each:

We need to make sure that nums1[i] is not equal to nums2[i] for all indices i. Now let's walk through the solution approach step by step:

2. Count duplicates and calculate cost: For the pairs listed, we count how many times the same number appears at the same

1. Identify indices where values match: We find that nums1[0] equals nums2[0], and nums1[2] equals nums2[2]. So we list the pairs

index in both arrays and calculate the initial cost. The number '1' appears twice, and the cost of swapping indices 0 and 2 would be 0 + 2 = 2.

[1, 2, 3, 1] after the swap.

swap of indices 0 and 2) = 4.

from collections import Counter

Initialize variables:

ans: Accumulated cost

num_same = accumulated_cost = 0

frequency_counter = Counter()

num_same += 1

if freq * 2 > num_same:

max_overlap -= 1

leader = elem

if elem1 == elem2:

Python Solution

class Solution:

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(indices) that need attention: [(0, 0), (2, 2)].

because we are swapping elements at indices 0 and 2.

def minimumTotalCost(self, nums1: List[int], nums2: List[int]) -> int:

num_same: Count of elements that are the same in both lists

Counter to store frequency of elements that are the same

for index, (elem1, elem2) in enumerate(zip(nums1, nums2)):

Calculate initial cost and count same elements

accumulated_cost += index

frequency_counter[elem1] += 1

 $max_overlap = freq * 2 - num_same$

accumulated_cost += index

Otherwise, return the accumulated cost

return -1 if max_overlap else accumulated_cost

1 nums1 = [1, 2, 3, 1] 2 nums2 = [1, 1, 2, 2]

- 1 (half of 2) = 1. Hence, m = 1.

4. Search for non-leading values to swap: We look for a pair (a, b) where a does not equal b and neither a nor b is the leading

value '1'. We find such a pair at index 1: (2, 1). We perform the swap at the lowest index (which minimizes the cost) and swap

nums1[1] with nums1[0]. This resolves one duplicate without adding to m since neither number is the leading value. Now nums1 is

3. Find the leading value: Here, the number '1' is the leading value as it appears the maximum number of times at the same index.

We calculate the margin m by which '1' exceeds half of the duplicates. Since we have 2 duplicates and both are '1', it exceeds by 2

5. **Update the counts and cost**: After the swap, we now have nums1 = [2, 1, 3, 1] and nums2 = [1, 1, 2, 2]. There's still a duplicate at index 2, but we now also have a spare '2' at index 0, which we can swap with the '3' in nums1. This swap costs 2

6. Check if all duplicates are fixed: After the swap, nums1 becomes [3, 1, 2, 1]. We see that nums1[i] != nums2[i] for all i. We

have successfully eliminated all duplicates, and our total cost is 2 (initially calculated for the problematic pair (0, 0)) + 2 (for the

Thus, the minimum total cost required to ensure that no element at index i in nums1 is equal to the element at the same index in nums2 for this example is 4.

Initialize variables to determine the leader element
max_overlap = 0
leader = 0
Find the element with more than half of the same occurrences
for elem, freq in frequency_counter.items():

if max_overlap and elem1 != elem2 and elem1 != leader and elem2 != leader:

If there is still an overlap, return -1 since it's impossible to fulfill the conditions

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break

Iterate again to adjust the cost for changing elements avoiding

# the leader and until max_overlap is reduced to zero

for index, (elem1, elem2) in enumerate(zip(nums1, nums2)):
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Java Solution
    class Solution {
         public long minimumTotalCost(int[] nums1, int[] nums2) {
             long totalCost = 0; // Initialize the answer variable to store the total cost
             int sameValueCount = 0; // Counter for the number of same values at the same index
             int n = nums1.length; // Length of the input arrays
             int[] freqCount = new int[n + 1]; // Frequency array to count occurrences of each number
  6
             // Loop through the arrays to find matches and calculate part of the cost
             for (int i = 0; i < n; ++i) {
  9
                 if (nums1[i] == nums2[i]) {
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                     totalCost += i; // If the same at the same index, add the index to totalCost
 11
 12
                     ++sameValueCount; // Increment the same element counter
 13
                     ++freqCount[nums1[i]]; // Increment frequency count for this number
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             int tempCount = 0; // Temporary count for storing excess count of a number
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             int leadingNumber = 0; // The number with the maximum excess count
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 20
             // Find the number with the maximum excess appearance
 21
             for (int i = 0; i < freqCount.length; ++i) {</pre>
 22
                 int excess = freqCount[i] * 2 - sameValueCount;
 23
                 if (excess > 0) {
 24
                     tempCount = excess; // Update tempCount if a number has excess appearances
 25
                     leadingNumber = i; // Update the leadingNumber
 26
                     break; // Break because we only need the first number with an excess appearances
 27
 28
 29
 30
             // Try to reduce the cost by replacing non-leading number pairs
 31
             for (int i = 0; i < n; ++i) {
 32
                 // Check if a swap can reduce the excess count without adding leading number
```

if (tempCount > 0 && nums1[i] != nums2[i] && nums1[i] != leadingNumber && nums2[i] != leadingNumber) {

int sameElementCount = 0; // Variable to count the number of elements that are the same in nums1 and nums2.

totalCost += i; // Increment the total cost with the index value

--tempCount; // Decrement the count for the number of swaps left

// If there are still swaps left after traversing, there's no solution

long long minimumTotalCost(vector<int>& nums1, vector<int>& nums2) {

int n = nums1.size(); // Size of the input arrays.

for (int i = 0; i < n; ++i) {

long long totalCost = 0; // Variable to store the total cost.

int countArray[n + 1]; // Array to count the occurrence of each number.

totalCost += i; // Add the index to the total cost.

++sameElementCount; // Increment the same element count.

memset(countArray, 0, sizeof countArray); // Initialize the countArray with zeros.

if (nums1[i] == nums2[i]) { // If the elements at index i are the same,

// Loop through nums1 and nums2 to calculate the initial cost and count same elements.

++countArray[nums1[i]]; // Increment the count of this element in countArray.

return tempCount > 0 ? -1 : totalCost;

C++ Solution

public:

1 class Solution {

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             // Find the value with the max lead.
             for (int i = 0; i < n + 1; ++i) {
 23
                 int lead = countArray[i] * 2 - sameElementCount; // Calc. lead which is count*2 - sameElementCount.
 24
 25
                 if (lead > 0) {
 26
                                      // Update max lead.
                     maxLead = lead;
 27
                                      // Update lead value.
                     leadValue = i;
 28
                     break; // Exit the loop since we found the value.
 29
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             // Loop to potentially add more to total cost based on numbers that do not have the leading count.
 33
             for (int i = 0; i < n; ++i) {
 34
                 if (maxLead > 0 && nums1[i] != nums2[i] && nums1[i] != leadValue && nums2[i] != leadValue) {
 35
                     // Add the index to total cost if both numbers are not equal to the lead value.
 36
                     totalCost += i;
 37
                     --maxLead; // Decrease the lead as we've handled one index.
 38
 39
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 41
             // If maxLead greater than zero, we could not match all elements, return -1. Otherwise, return total cost.
 42
             return maxLead > 0 ? -1 : totalCost;
 43
 44
    };
 45
Typescript Solution
     function minimumTotalCost(nums1: number[], nums2: number[]): number {
         let totalCost: number = 0; // Variable to store the total cost.
         let sameElementCount: number = 0; // Variable to count the number of elements that are the same in nums1 and nums2.
         const n: number = nums1.length; // Size of the input arrays.
         let countArray: number[] = new Array(n + 1).fill(0); // Array to count the occurrence of each number with initial zeros.
  6
         // Loop through nums1 and nums2 to calculate the initial cost and count same elements.
         for (let i = 0; i < n; ++i) {
  8
             if (nums1[i] === nums2[i]) { // If the elements at index i are the same,
  9
 10
                 totalCost += i; // Add the index to the total cost.
                 ++sameElementCount; // Increment the same element count.
 11
 12
                 ++countArray[nums1[i]]; // Increment the count of this element in countArray.
 13
 14
 15
 16
         // Variables to store the maximum lead and the value with that lead.
 17
         let maxLead: number = 0;
 18
         let leadValue: number = 0;
 19
 20
         // Find the value with the maximum lead.
 21
         for (let i = 0; i < n + 1; ++i) {
 22
             let lead: number = countArray[i] * 2 - sameElementCount; // Calculate lead which is count*2 - sameElementCount.
 23
             if (lead > 0) {
 24
                 maxLead = lead; // Update max lead.
 25
                 leadValue = i; // Update lead value.
 26
                 break; // Exit the loop since we found the value.
```

Time and Space Complexity

for (let i = 0; i < n; ++i) {

totalCost += i;

return maxLead > 0 ? -1 : totalCost;

the Counter dictionary cnt. None of these loops are nested.

Time Complexity:

• The first for-loop runs through all elements in nums1 and nums2, contributing to a time complexity of O(N), where N is the length of

• The second for-loop iterates over the Counter dictionary cnt. The maximum size of cnt is bounded by the number of unique

The given code block consists of two separate for-loops that iterate over the provided inputs nums1 and nums2, as well as a loop over

// Loop to potentially add more to total cost based on numbers that do not have the leading count.

// Add the index to total cost if both numbers are not equal to the lead value.

--maxLead; // Decrease the lead as we've handled one index.

if (maxLead > 0 && nums1[i] !== nums2[i] && nums1[i] !== leadValue && nums2[i] !== leadValue) {

// If maxLead is greater than zero, we could not match all elements, return -1. Otherwise, return the total cost.

same, so this is also 0(N) but happens only once. Therefore, it doesn't change the overall complexity. • The third for-loop again processes each element, adding to another 0(N) time complexity.

Space Complexity:

the lists.

Combining all the loops, the time complexity remains linear, therefore the total time complexity is 0(N) where N is the size of the input arrays.

elements in nums1 since only elements that are equal in both nums1 and nums2 are counted. In the worst case, all elements are the

(since, in the worst case, all numbers in nums1 and nums2 will be the same). This gives us O(N) space complexity.

• There are constant space usages for the ans, same, m, and lead variables.

Thus, the final space complexity is O(N) accounting for the Counter object. All other variables occupy constant space, contributing O(1).

• The Counter object cnt stores the counts of the numbers that are the same in nums1 and nums2. It will at most have N entries

Therefore, the overall space complexity of the code is O(N).