2033. Minimum Operations to Make a Uni-Value Grid Matrix Medium (Array) Math Sorting

Problem Description

The problem presents us with a two-dimensional grid of integers and a single integer x. The operation that can be executed involves adding or subtracting x to any element in the grid. A uni-value grid is defined as a grid where all elements are equal. The goal is to determine the minimum number of such operations required to turn the input grid into a uni-value grid. If this objective is unattainable, the function should return -1. The critical constraint to keep in mind is that all elements in the final uni-value grid must be equal, which implies that the difference

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between any two given elements in the original grid must be a multiple of x. Otherwise, it would be impossible to reach a common value through the given operation. Intuition

To arrive at the minimum number of operations needed to achieve a uni-value grid, we need to find a target value that all elements in the grid will be equal to after the operations. Since adding or subtracting x continues to maintain the same remainder when any

element is divided by x, all elements must share the same remainder mod when divided by x; otherwise, there's no legal operation that will create a uni-value grid. Given that all elements can be modified to share the same remainder when divided by x, the next step is to decide on which value to set all elements to. A natural choice is the median of all values, as it minimizes the absolute deviation sum for a set of numbers. In other words, using the median value as a target implies the least total difference between each number and the median, hence

requiring the fewest operations. The solution approach follows these steps: 1. Flatten the grid into a list nums, to work with a single-dimensional array of all the values. 2. Check if all elements have the same remainder when divided by x. If not, return -1.

4. Sum the absolute division (//) of differences between each element in nums and the median by x. This represents the minimum

number of operations to adjust each element to make the entire grid uni-value.

3. Sort nums and find the median value.

- This solution is efficient as it minimally processes the elements by using their inherent properties (specifically, the remainder upon
- division) and statistical measures (median) to determine feasibility and achieve optimality for the problem.
- The solution approach for converting the grid to a uni-value grid with a minimum number of operations follows a simple but powerful

statistical concept. Here is the breakdown of the implementation steps, referencing the provided Python code: 1. Flatten the Grid: The first step involves transforming the two-dimensional grid into a one-dimensional array (list). This is achieved by defining an empty list nums and iterating over each row and within that, each value v, to append it to nums.

the given operation. For this purpose, we store the remainder of the first grid element (e.g., grid [0] [0] % x) in mod and then

as len(nums) // 2).

function returns.

1 Grid: [[2, 4], [6, 8]]

2 x: 2

8].

Solution Approach

check if v 🐉 x == mod for all elements in the grid. If any element doesn't satisfy this, it's impossible to reach a uni-value grid, and the function immediately returns -1.

3. Sort and Find Median: Once we have a flat list nums of all values, we sort it to arrange the numbers in ascending order. Finding

If the list's length is even, either of the two middle values will work due to the way the median minimizes the sum of absolute

the median is straightforward from this sorted list; it's the middle value, which minimizes the total number of operations needed.

deviations. The median is found using nums [len(nums) >> 1], which is an efficient way to calculate the median index (the same

2. Check Modulo Condition: Before proceeding, we need to guarantee that all elements can be adjusted to the same value using

4. Calculate Total Operations: Finally, we calculate the total number of operations needed by summing the integer division of absolute differences between each element and the median, divided by x (i.e., sum(abs(v - mid) // x for v in nums)). This represents how many times we'd need to add or subtract x to/from each element to convert it into the median value.

In terms of algorithms and patterns, the problem mainly relies on the properties of numbers (divisibility and modulo operation), and

the use of sorting and median as a means to minimize absolute differences. No complex data structures are used beyond the one-

dimensional list for sorting and iteration, and the algorithm overall exhibits a time complexity effectively determined by the sorting

5. Return Result: The result of the sum is the minimum number of operations required to make the grid uni-value, which is what the

step, which is typically O(N log N) where N is the number of elements in the grid. Example Walkthrough

Let's consider a two-dimensional grid and an integer x with the following values:

of the two middle values, 4 or 6. Here we'll choose 4 as the median (nums [4 // 2]).

:return: int, the minimum number of operations or -1 if it's not possible

Flatten the grid into a single sorted list to make it easier to handle

we return -1 because the whole grid cannot be equalized

Start by storing the remainder of the first element (for modulo comparison)

If the current value cannot be achieved by any number of operations,

Calculate the sum of operations required to make all values equal to the median

operations = sum(abs(value - median) // x for value in flattened_grid)

We want to convert the given grid into a uni-value grid using the minimum number of operations where we can add or subtract x to any element. Following the solution approach:

1. Flatten the Grid: We transform our two-dimensional grid into a one-dimensional list nums. After flattening, nums will be [2, 4, 6,

2. Check Modulo Condition: We check if all elements have the same remainder when divided by x. For our grid, all elements (2 %

3. Sort and Find Median: We sort the list nums to get [2, 4, 6, 8]. The length of the list is 4 (even), so the median could be either

2, 4 % 2, 6 % 2, 8 % 2) have a remainder of 0 when divided by 2. Since they all have the same remainder, we can proceed.

4. Calculate Total Operations: We calculate the number of operations needed to transform each element into the median. For

every element v in nums, we calculate abs(v - median) // x and sum these values up: For 2: abs(2 - 4) // 2 equals 1 operation.

Python Solution

class Solution:

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For 8: abs (8 - 4) // 2 equals 2 operations.

def minOperations(self, grid, x):

flattened_grid = []

for row in grid:

required_modulo = grid[0][0] % x

return -1

if value % x != required_modulo:

Find the median, which will be our target value

median = flattened_grid[len(flattened_grid) // 2]

operationCount += Math.abs(value - median) / x;

// Return the total operation count

int minOperations(vector<vector<int>>& grid, int x) {

// Calculate the dimensions of the grid

return operationCount;

int rows = grid.size();

int cols = grid[0].size();

Iterate through the grid

for value in row:

Summing these up gives us 1 + 0 + 1 + 2 = 4 operations.

 For 4: abs(4 - 4) // 2 equals 0 operations. For 6: abs (6 - 4) // 2 equals 1 operation.

5. Return Result: The minimum number of operations required to make the grid uni-value is 4. This is the final result we return.

- Through these steps, we've used a statistical approach (median) alongside modulo operations to efficiently determine the required operations to reach a uni-value grid, ensuring that the chosen operations are valid and minimal.
 - Determine the minimum number of operations required to make all elements in the grid equal, where in one operation you can add or subtract `x` to any element in the grid. :param grid: List[List[int]] :param x: int

27 # Otherwise, store the value in our flattened grid 28 flattened_grid.append(value) 29 30 # Sort all values in our list to easily find the median flattened_grid.sort() 31

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           # Return the total number of operations
           return operations
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42 # Example usage:
  # solution = Solution()
44 # grid = [[1, 5], [2, 3]]
45 \# x = 1
  \# print(solution.minOperations(grid, x)) \# Outputs the minimum number of operations required
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Java Solution
   class Solution {
       public int minOperations(int[][] grid, int x) {
           // Get the number of rows
           int rows = grid.length;
           // Get the number of columns
           int cols = grid[0].length;
           // Initialize an array to store all elements in the grid
           int[] flattenedGrid = new int[rows * cols];
           // Modulo of the first element in the grid. All other elements should have the same modulo if a solution is possible
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           int initialMod = grid[0][0] % x;
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           // Flatten the 2D grid into a 1D array while checking if operation is not possible
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           for (int i = 0; i < rows; ++i) {
               for (int j = 0; j < cols; ++j) {
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                   // If any element has a different modulo than the first element, return -1 as it's not possible to make them all equa
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                   if (grid[i][j] % x != initialMod) {
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                       return -1;
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                   // Store elements of the grid in the flattened 1D array
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                   flattenedGrid[i * cols + j] = grid[i][j];
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           // Sort the flattened 1D array
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           Arrays.sort(flattenedGrid);
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           // Find the median element
27
           int median = flattenedGrid[flattenedGrid.length / 2];
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           // Initialize operation count to 0
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           int operationCount = 0;
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           // Calculate the total number of operations required to make all elements equal to the median
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           for (int value : flattenedGrid) {
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               // Increment the operation count by the number of operations needed for each element.
               // The distance between the element and the median is divided by x
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               // as that's the number of operations required to make them equal
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C++ Solution

1 class Solution {

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// Determine the modulo of the first element as a reference
           int referenceModulo = grid[0][0] % x;
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           // Flatten the grid into a single vector for ease of manipulation
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           vector<int> flattenedGrid(rows * cols);
           // Process the grid while checking if it's possible to make all elements equal
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           for (int i = 0; i < rows; ++i) {
                for (int j = 0; j < cols; ++j) {
16
                   // If an element's modulo isn't equal to the reference, it's not possible to make all elements equal
17
                   if (grid[i][j] % x != referenceModulo) {
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                       return -1;
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                   // Populate the flattened grid
22
                   flattenedGrid[i * cols + j] = grid[i][j];
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           // Sort the flattened grid to find the median
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           sort(flattenedGrid.begin(), flattenedGrid.end());
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           // The median value is the target value for all elements to make them equal
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           int targetValue = flattenedGrid[(rows * cols) / 2];
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           // Calculate the total number of operations needed
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           int totalOps = 0;
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            for (int value : flattenedGrid) {
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               // Add the required number of operations per element
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                totalOps += abs(value - targetValue) / x;
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           // Return the total number of operations
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           return totalOps;
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42 };
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Typescript Solution
   // Function to find the minimum number of operations needed to make all elements of a grid equal.
   function minOperations(grid: number[][], x: number): number {
       // Calculate the dimensions of the grid
       let rows = grid.length;
       let cols = grid[0].length;
       // Determine the modulo of the first element as a reference
       let referenceModulo = grid[0][0] % x;
 9
       // Flatten the grid into a single array for ease of manipulation
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       let flattenedGrid: number[] = [];
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```

27 // The median value is the target value for all elements to make them equal 28 let targetValue = flattenedGrid[Math.floor((rows * cols) / 2)]; 30 31 // Calculate the total number of operations needed

let totalOps = 0;

return totalOps;

for (let i = 0; i < rows; i++) {

return -1;

flattenedGrid.sort((a, b) => a - b);

for (let value of flattenedGrid) {

// Return the total number of operations

add or subtract a value x from elements in the grid.

for (let j = 0; j < cols; j++) {

// Populate the flattened grid

// Sort the flattened grid to find the median

flattenedGrid.push(grid[i][j]);

if (grid[i][j] % x !== referenceModulo) {

// Add the required number of operations per element

totalOps += Math.abs(value - targetValue) / x;

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Time and Space Complexity The given Python code is used to determine the minimum number of operations to make all elements in a grid equal if one can only

// If an element's modulo isn't equal to the reference, it's not possible to make all elements equal

The time complexity of the code is analyzed as follows:

Space Complexity:

Time Complexity:

1. Creating the nums list with a nested loop through the grid: This takes O(m*n), where m and n are the dimensions of the grid. 2. Sorting the nums list: The sort operation has a time complexity of O(k*log(k)), where k is the total number of elements in the grid

- (k = m*n).3. Calculating the median and the number of operations: This involves a single pass through the sorted nums list, which takes O(k).
- Combining these, the dominant term is the sorting step, therefore the overall time complexity is O(k*log(k)) which simplifies to O(m*n*log(m*n)) since k = m*n.

1. Storing the nums list: Space complexity is O(k), which is O(m*n) where k is the total number of elements in the grid.

// Process the grid while checking if it's possible to make all elements equal

2. Variables mod and mid: These are constant space and do not scale with the input, so they contribute 0(1). Thus, the overall space complexity is 0(m*n) since the storage for the nums list dominates the space usage.