2106. Maximum Fruits Harvested After at Most K Steps

Sliding Window

Problem Description

Array

Binary Search

Prefix Sum

In this problem, we are given a sorted 2D integer array fruits where each entry fruits[i] consists of two integers, position_i and amount_i. position_i represents a unique position on an infinite x-axis where fruits are located, and amount_i is the number of fruits available at that position. Additionally, we have a starting position on the axis, startPos, and an integer k which represents the maximum number of steps we can take in total. The goal is to find the maximum total number of fruits one can harvest.

One can walk either left or right on the x-axis, and upon visiting a position, all fruits there are harvested and thus removed from

that position. Walking one unit on the x-axis counts as one step, and the total number of steps cannot exceed k. The task is to devise a strategy for harvesting the most fruits under these constraints.

To arrive at the solution, we first need to understand that walking too far in one direction might prevent collecting fruits in the

Intuition

Hard

and then potentially changing direction to collect more if the steps allow.

The intuition behind the solution is to use a <u>sliding window</u> technique to keep track of the total amount of fruits that can be collected within k steps from <u>startPos</u>. We slide the window across the sorted positions while ensuring the total number of steps

other direction because of the step limit k. To maximize the harvest, we should consider walking in one direction to collect fruits

the starting point of our sliding window to the right to shrink the harvesting range back within the allowed steps.

We calculate the maximum number of fruits that can be collected within this range and update our answer accordingly. At each step, we consider reaching the farthest point in our window from startPos and then returning to the nearest point. The heart of

including the return to startPos does not exceed k. If at any point the total distance of our sliding window exceeds k, we move

this approach relies on the optimal substructure of the problem—maximizing fruits within a range naturally contributes to maximizing the overall harvest.

Solution Approach

The solution implements a sliding window approach to maintain a range of positions we can visit to collect fruits within k steps.

The fruits array gives us the positions and the number of fruits at each position, sorted by the positions. The implementation

iterates over this array, expanding and shrinking the window to find the optimal total amount of fruits that can be harvested. The maxTotalFruits function starts by initializing important variables: ans to store the maximum number of fruits we can harvest,

from the sum s.

positions once.

s -= fruits[i][1]

• fruits array: [[0,3], [2,1], [5,2]]

i to denote the start of the <u>sliding window</u>, s to keep the sum of fruits within the window, and j to iterate over the fruit positions.

Here is a step-by-step explanation of the algorithm:

1. Iterate through the fruit array using the index j and for each position pj with fruit count fj, add fj to the sum s.

2. Check if the current window [i, j] exceeds k steps. This is done by calculating the distance pj - fruits[i] [0] (the width of the window) and adding the smaller distance from startPos to either end of the window.
3. If the window is too wide (exceeds k steps), we shrink the window from the left by incrementing i, effectively removing fruits at fruits[i] [1]

4. At each iteration, after adjusting the window, update ans with the maximum of itself or the current sum s. 5. Continue this process until all positions have been checked.

Here is a portion of the code explaining the critical part of the algorithm:

The core concept here leverages the fact that, since the fruit positions are sorted and unique, we can efficiently determine the range of positions to harvest by only considering the endpoints of the current window.

The algorithm uses constant space for variables and O(n) time where n is the number of positions since it scans through the

for j, (pj, fj) in enumerate(fruits):
 s += fj
 while i <= j and pj - fruits[i][0] + min(abs(startPos - fruits[i][0]), abs(startPos - pj)) > k:

ans = max(ans, s)

The loop adds fruits to s and potentially contracts the window by advancing i if the condition (pj - fruits[i][0] +

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is updated to the maximum sum s found within the constraints.

This elegant approach effectively balances expanding and contracting the harvesting range on the fly to maximize fruit collection within the step limit.

Example Walkthrough
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min(abs(startPos - fruits[i][0]), abs(startPos - pj))) > k is met, ensuring the total steps do not exceed k. The answer ans

• k: 4

Here, we can move a maximum of 4 steps from the starting position, and positions [0, 2, 5] have [3, 1, 2] fruits respectively.

1. Initialize ans as 0 (maximum number of fruits harvested), i as 0 (start of the sliding window), and s as 0 (sum of fruits within the window).

required are abs(startPos - fruits[i][0]) + (fruits[j][0] - fruits[i][0]) = abs(1 - 0) + (2 - 0) = 3 steps to go from startPos to pj,

5. Move to the next item in the array, j = 2. Add fruit count at that position to s, so now s = 4 + 2 = 6. The window [i, j] is now [0, 5], and we

2. Start iterating through fruits array with index j. As we add fj to sum s, the sum of fruits becomes 3 when j = 0. 3. There is no need to shrink the window yet since we are within k steps range (the max steps we can move is 4).

which still does not exceed k.

k so we keep the window.

Solution Implementation

class Solution:

startPos: 1

3. There is no need to shrink the window yet since we are within k steps range (the max steps we can move is 4).

4. Move to the next item in the array, j = 1. The sum of fruits s becomes 3 + 1 = 4. The window [i, j] is now [0, 2], and the total steps

Let's consider a small example to illustrate the solution approach. Suppose we have the following input:

check the steps: abs(startPos - fruits[i][0]) + (fruits[j][0] - fruits[i][0]) = abs(1 - 0) + (5 - 0) = 6. This exceeds k, so we need to shrink the window from the left by incrementing i.

7. As i moves up, s decreases to 2, having removed the fruits at position 0. Since this is still less than k, we continue.

6. The new window [i, j] is now [2, 5]. We update s by subtracting the fruits at fruits[i][1] and calculate steps again: s = 6 - fruits[i][1] = 6 - 3 = 3. The steps are abs(startPos - fruits[i][0]) + (fruits[j][0] - fruits[i][0]) = abs(1 - 2) + (5 - 2) = 4, which is equal to

def maxTotalFruits(self, fruits: List[List[int]], startPos: int, k: int) -> int:

for window_end, (position_j, fruits_at_j) in enumerate(fruits):

> k # Check if the total distance is within 'k'

total_fruits -= fruits[window_start][1]

max_fruits = window_start = total_fruits = 0

window_start <= window_end</pre>

and position_j

We want to maximize the number of fruits we can pick within those 4 steps.

Here's how the solution approach would work on this example:

- 8. Now, ans is updated to a maximum of itself or current sum s, so ans = max(0, 3) = 3.
 9. No more positions left, we end with ans = 3, which is the amount of fruit we harvested.
 Therefore, following this approach with our example, the maximum number of fruits that can be harvested is 3.
- Python

Initialize variables for the answer, starting index of the window, and the sum of fruits within the window

- fruits[window_start][0] # Distance between the current end of the window and its start

+ min(abs(startPos - fruits[window_start][0]), abs(startPos - position_j)) # Minimum distance to startPos from &

If the window exceeds 'k' distance, subtract the fruits at 'window_start' and move window start to the right

Iterate over the fruits list with index 'j' and unpack positions and fruits as 'position_j' and 'fruits_at_j'

Add the fruits at position 'j' to the running total within the window
total_fruits += fruits_at_j
Shrink the window from the left as long as the condition is met

Return the maximum number of fruits that can be collected within 'k' units of movement

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window_start += 1
# Update the 'max_fruits' if the current window's total fruits is greater than the previously recorded maximum
max_fruits = max(max_fruits, total_fruits)
```

Java

class Solution {

public:

};

let maxFruits = 0;

return max_fruits

while (

```
class Solution {
    public int maxTotalFruits(int[][] fruits, int startPos, int k) {
        int maxFruits = 0; // Stores the maximum number of fruits we can collect
        int currentSum = 0; // Stores the current sum of fruits between two points
       // Two pointers approach: i is for the start point and j is for the end point
        for (int i = 0, j = 0; j < fruits.length; ++j) {</pre>
            int positionJ = fruits[j][0]; // The position of the j-th tree
            int fruitsAtJ = fruits[j][1]; // The number of fruits at the j-th tree
            currentSum += fruitsAtJ; // Add fruits at the j-th tree to the current sum
           // Adjust the starting point i to not exceed the maximum distance k
           while (i <= j &&
                   positionJ - fruits[i][0] +
                  Math.min(Math.abs(startPos - fruits[i][0]), Math.abs(startPos - positionJ))
                  > k) {
                // Subtract the number of fruits at the i-th tree as we move the start point forward
                currentSum -= fruits[i][1];
                i++; // Increment the start point
           // Update maxFruits with the maximum of current sum and previously calculated maxFruits
           maxFruits = Math.max(maxFruits, currentSum);
       return maxFruits; // Return the maximum number of fruits that can be collected
C++
#include <vector>
#include <algorithm>
```

```
/**
 * Calculates the maximum total number of fruits that can be collected from fruit trees lined up in a row.
 * The farmer starts at a given position and can move a maximum total distance k.
 *
```

// Function to calculate the maximum total number of fruits that can be collected

int maxFruits = 0; // Store the maximum total fruits that can be collected.

int currentSum = 0; // Store the current sum of fruits being considered.

int positionJ = fruits[j][0]; // Position of the j-th fruit tree

// If the distance from start to the current fruit is more than k

i++; // Move the start of the window to the right

int fruitCountJ = fruits[j][1]; // Number of fruits at the j-th fruit tree

// after adjusting for the closest path, shrink the window from the left.

// Update maxFruits with the maximum of the current value and currentSum.

return maxFruits; // Return the maximum number of fruits that can be collected

* @param {number[][]} fruitPositions - An array where each element is a pair [position, fruitCount];

// The current maximum number of fruits that can be collected

fruits at that tree.

let currentFruits = 0; // The running total of fruits collected within the current window

for (let leftIndex = 0, rightIndex = 0; rightIndex < fruitPositions.length; rightIndex++) {</pre>

function maxTotalFruits(fruitPositions: number[][], startPos: number, k: number): number {

// Two-pointer approach to find the optimal range of trees to collect fruits from

int maxTotalFruits(vector<vector<int>>& fruits, int startPos, int k) {

// "k" is the maximum number of steps that can be taken.

for (int i = 0, j = 0; j < fruits.size(); ++j) {</pre>

while (i <= j && positionJ - fruits[i][0] +</pre>

maxFruits = max(maxFruits, currentSum);

* @param {number} startPos - The starting position of the farmer.

* @param {number} k - The maximum total distance the farmer can move.

> k # Check if the total distance is within 'k'

Return the maximum number of fruits that can be collected within 'k' units of movement

total_fruits -= fruits[window_start][1]

max_fruits = max(max_fruits, total_fruits)

* @returns {number} The maximum total fruits that can be collected.

// Use a sliding window defined by the indices [i, j].

// "fruits" vector holds pairs of positions and fruit counts, "startPos" is the starting position,

currentSum += fruitCountJ; // Add the fruits from the j-th tree to the current sum

min(abs(startPos - fruits[i][0]), abs(startPos - positionJ)) > k) {

currentSum -= fruits[i][1]; // Remove the fruits from the i-th tree from the current sum

position is the position of a tree, fruitCount is the number of

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// Current fruit position and count
          const [currentPosition, fruitCount] = fruitPositions[rightIndex];
          currentFruits += fruitCount; // Add the fruits from the right pointer's current tree
          // Adjust the left pointer while the total distance required to collect fruits
          // from the range exceeds the maximum distance k
          while (
              leftIndex <= rightIndex &&</pre>
              currentPosition - fruitPositions[leftIndex][0] +
              Math.min(Math.abs(startPos - fruitPositions[leftIndex][0]), Math.abs(startPos - currentPosition)) > k
              // Subtract the fruits from the left pointer's current tree and move the left pointer to the right
              currentFruits -= fruitPositions[leftIndex++][1];
          // Update the maximum fruits collected if the current total is greater
          maxFruits = Math.max(maxFruits, currentFruits);
      return maxFruits; // Return the maximum fruits collected after checking all ranges
class Solution:
   def maxTotalFruits(self, fruits: List[List[int]], startPos: int, k: int) -> int:
       # Initialize variables for the answer, starting index of the window, and the sum of fruits within the window
       max_fruits = window_start = total_fruits = 0
       # Iterate over the fruits list with index 'j' and unpack positions and fruits as 'position_j' and 'fruits_at_j'
        for window_end, (position_j, fruits_at_j) in enumerate(fruits):
            # Add the fruits at position 'j' to the running total within the window
            total_fruits += fruits_at_j
           # Shrink the window from the left as long as the condition is met
           while (
               window_start <= window_end</pre>
               and position_j
                - fruits[window_start][0] # Distance between the current end of the window and its start
               + min(abs(startPos - fruits[window_start][0]), abs(startPos - position_j)) # Minimum distance to startPos from eithe
```

Time and Space Complexity

return max fruits

Time Complexity

Space Complexity

window_start += 1

The time complexity of the given code is O(N), where N represents the number of pairs in the fruits list. Although the code features a nested loop, each fruit in the fruits list is processed only once due to the use of two-pointer technique. The inner while loop only advances the i pointer and does not perform excessive iterations for each j index in the outer loop. Therefore, every element is visited at most twice, keeping the overall time complexity linear with respect to the number of fruit positions.

If the window exceeds 'k' distance, subtract the fruits at 'window_start' and move window start to the right

Update the 'max_fruits' if the current window's total fruits is greater than the previously recorded maximum

The space complexity of the given code is 0(1). The only extra space used is for variables to keep track of the current maximum fruit total (ans), the current sum of fruits (s), and the pointers (i, j) used for traversing the fruits list. This use of space does not scale with the size of the input, and as such, remains constant.