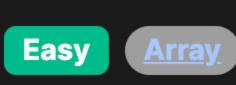
## 1636. Sort Array by Increasing Frequency

**Sorting** 

the rearranged array that satisfies these sorting rules.





**Problem Description** 

The problem provides us with an array of integers nums. The task is to sort the array, but not by the usual ascending or descending orders based purely on the number values. Instead, we need to first sort the array based on how frequent each number appears, which we'll call its frequency. So, numbers with a lower frequency should come first. In the event that two numbers have the same frequency, we need to sort these numbers in decreasing order amongst themselves. Finally, we'll return

Intuition

to sort by two criteria: frequency, and then by the value itself if frequencies are equal. In Python, we can achieve this by using a sorting function that allows a custom key, to which we can pass a lambda function. The lambda function will return a tuple with two elements: the frequency of the number and the negation of the number itself.

The reason for negating the number is because Python sorts tuples in lexicographical order, starting with the first element. For

To solve this problem, one strategy is to lean on Python's sorting capabilities but with a custom sorting rule. We need to be able

the first element, we want a normal increasing order based on frequency, but for the second element, we want decreasing order. Since Python will normally sort in increasing order, negating the numbers allows us to "invert" this to get the desired decreasing order. The standard sorted function in Python will then take care of the rest, applying our custom key to sort the array as required by the problem. We use the Counter class from the collections module to quickly tally up the frequencies of each element in the nums array. This

construct, when used in the sorted function's key, performs the sort based on the aforementioned tuple, (frequency, -value). Solution Approach

## The solution uses a combination of a custom sorting function and a hash table, provided by Python's Counter from the collections module, to count the frequency of each element in the nums array.

Here's a step-by-step walkthrough: The Counter (nums) function creates a hash table that maps each unique number in the nums array to its frequency. Let's call

this map cnt.

- The built-in sorted function in Python is used to sort the numbers, but instead of sorting by the numbers themselves, it sorts by a key that we define. This key is a lambda function, which Python allows for customization of the sort order.
- The lambda function takes an element x from nums and returns a tuple: (cnt[x], -x). Here, cnt[x] is the frequency of x, so the first element of the tuple dictates that the sorter first arranges elements based on increasing frequency (lower frequency comes first).

The second element of the tuple is -x, the negation of the number itself. This part ensures that if two elements have the same

frequency (cnt[x] is equal), the sorter will arrange these particular items based on their value in descending order (since -x

converts the sort order). To clarify via an example, let's say nums contains [1, 1, 2, 2, 3, 3]. The Counter would yield cnt as {1: 2, 2: 2, 3: 3}. The sorted key would transform these into sort keys [2, -1], [2, -1], [2, -2], [2, -2], [3, -3], [3, -3], [3, -3]. The sorted

**Example Walkthrough** 

In the end, the lambda function in conjunction with sorted() applies a sorting algorithm that respects the two key sorting rules

## This gives us a frequency map cnt like so: {4: 3, 1: 1, 6: 3}.

We then call the built-in sorted function with a custom key. The key is defined by a lambda function such that each element x

Let's consider a small example with the array nums = [4, 1, 6, 6, 4, 4, 6] to illustrate the solution approach.

function would use these keys to sort nums into [3, 3, 3, 2, 2, 1, 1].

outlined in the problem description, effectively yielding the desired sorted array.

from nums is transformed into a sort key (cnt[x], -x).

Applying this lambda function to each element of nums gives us the following sort keys: (3, -4) for each 4, (1, -1) for the 1,

First, we apply the Counter(nums) function from the collections module to count the frequency of each unique number in nums.

and (3, -6) for each 6. The sort keys are derived from the cnt map and negation of the value as per our lambda function. These sort keys are then used by the sorted function to sort nums. The first element of the tuple determines that we sort by

increasing frequency, with lower frequencies coming first. The array element with the lowest frequency (1 in this case) will

thus come first in the sorted array. For elements with the same frequency (4 and 6 in this case), the second element of the tuple comes into play, sorting these

in decreasing order due to the negation (-x). This means that between 4 and 6, which have the same frequency, 6 will come

In practice, the sorted function sorts the keys as follows: [(1, -1), (3, -6), (3, -6), (3, -6), (3, -6), (3, -4), (3,]. Once translated back into the actual nums values, we get the final sorted array: [1, 6, 6, 6, 4, 4, 4]. We have successfully walked through the steps of the approach using a small example, which shows how the array is transformed according to the given two-step sorting process: first by increasing frequency of the elements, then by their values

Solution Implementation **Python** 

## def frequencySort(self, nums: List[int]) -> List[int]: # Count the frequency of each number in the list using Counter num\_frequency = Counter(nums)

class Solution:

from collections import Counter

before 4 in the sorted array.

in decreasing order where frequencies are equal.

transformedList.sort((a, b) ->

// Return the sorted vector

function frequencySort(nums: number[]): number[] {

// Iterate through the array of numbers.

const frequencyMap = new Map<number, number>();

const freqA = frequencyMap.get(a) ?? 0;

return nums;

for (const num of nums) {

// Sort the numbers array.

return nums.sort((a, b) => {

// Create an array to store the sorted values.

// Populate the sortedArr with sorted values from the list,

// converting them back by removing the offset of 100.

int[] sortedArr = new int[nums.length];

# Sort the numbers based on the frequency (ascending order)

// Sort the list first by frequency, then by value if frequencies are equal.

frequency[a] == frequency[b] ? b - a : frequency[a] - frequency[b]

// Otherwise, sort by ascending order of frequencies (cnt[a] - cnt[b]).

// If frequencies are the same, sort in descending order of the values (b - a).

```
# When frequencies are the same, sort by the number itself (descending order)
sorted_nums = sorted(nums, key=lambda x: (num_frequency[x], -x))
return sorted_nums
```

Java

```
class Solution {
    public int[] frequencySort(int[] nums) {
       // Array to keep track of the frequency of each number.
       // Since the range of numbers is from -100 to 100, an offset of 100 is used
       // to map them to indices 0 to 200.
       int[] frequency = new int[201];
       // Transform the input array into a list to facilitate custom sorting.
       List<Integer> transformedList = new ArrayList<>();
       // Count frequencies and populate the list.
        for (int num : nums) {
           num += 100; // Apply offset to handle negative values.
            ++frequency[num]; // Increment frequency count for this number.
            transformedList.add(num); // Add to transformed list.
```

int i = 0;

**}**;

**TypeScript** 

```
for (int val : transformedList) {
            sortedArr[i++] = val - 100;
       return sortedArr; // Return the sorted array.
C++
#include <vector> // Include the necessary header for using the vector container
#include <algorithm> // Include the algorithm header for the sort function
class Solution {
public:
    vector<int> frequencySort(vector<int>& nums) {
       // Vector to store the frequency of numbers
       // 201 in size to account for numbers from -100 to 100 (inclusive)
       vector<int> frequency(201, 0);
       // Counting each number's frequency
       // Shift the index to fit in the range of [0, 200]
        for (int num : nums) {
            ++frequency[num + 100];
       // Custom sort the numbers
       sort(nums.begin(), nums.end(), [&](const int num1, const int num2) {
           // When frequencies are equal, sort by number value in descending order
            if (frequency[num1 + 100] == frequency[num2 + 100]) return num1 > num2;
            // Otherwise, sort by frequency in ascending order
            return frequency[num1 + 100] < frequency[num2 + 100];</pre>
       });
```

```
const freqB = frequencyMap.get(b) ?? 0;
// If frequencies are different, sort by frequency in ascending order.
if (freqA !== freqB) {
    return freqA - freqB;
```

```
// If frequencies are the same, sort by number in descending order.
         return b - a;
      });
from collections import Counter
class Solution:
   def frequencySort(self, nums: List[int]) -> List[int]:
       # Count the frequency of each number in the list using Counter
       num frequency = Counter(nums)
       # Sort the numbers based on the frequency (ascending order)
       # When frequencies are the same, sort by the number itself (descending order)
       sorted_nums = sorted(nums, key=lambda x: (num_frequency[x], -x))
       return sorted_nums
Time and Space Complexity
  The given Python code sorts an array of integers based on the frequency of each number and uses the Counter from the
  collections module to count occurrences. Then, it employs a custom sorting function.
Time Complexity:
```

// Defines a function to sort an array of numbers based on frequency of each number,

// and for numbers with the same frequency, sort them in descending order.

// Update the Map with the new frequency of the current number.

// Create a Map to keep track of the frequency of each number.

frequencyMap.set(num, (frequencyMap.get(num) ?? 0) + 1);

// Retrieve the frequency of both numbers being compared.

2. Sorting with the sorted function: Python's sorting function uses the Timsort algorithm, which has a time complexity of O(n log n) in the average and worst case.

The time complexity of the code is determined by several operations:

3. Custom sorting function: Sorting based on two criteria (count and then number itself in the reverse order) does not change the overall time complexity of O(n log n).

1. Counting the occurrences with Counter: This has a time complexity of O(n) where n is the number of elements in nums.

Therefore, considering these together, the total time complexity is 0(n + n log n), which simplifies to 0(n log n) since n log n

The space complexity is determined by: 1. Counter dictionary: The Counter creates a dictionary with as many entries as the unique elements in nums, which in the worst case is O(n).

**Space Complexity:** 

is the dominating term.

2. Sorted function: Timsort requires O(n) space in the worst case. Thus, the overall space complexity of the function is O(n) where n is the number of elements in nums.