2056. Number of Valid Move Combinations On Chessboard

Description

There is an 8×8 chessboard containing n pieces (rooks, queens, or bishops). You are given a string array pieces of length n, where pieces[i] describes the type (rook, queen, or bishop) of the i th piece. In addition, you are given a 2D integer array positions also of length n, where positions[i] = $[r_i, c_i]$ indicates that the i th piece is currently at the 1-based coordinate (r_i, c_i) on the chessboard.

When making a move for a piece, you choose a destination square that the piece will travel toward and stop on.

- A rook can only travel horizontally or vertically from (r, c) to the direction of (r+1, c), (r-1, c), (r, c+1), or (r, c-1).
- A queen can only travel **horizontally, vertically, or diagonally** from (r, c) to the direction of (r+1, c), (r-1, c), (r, c+1), (r, c-1), (r+1, c+1), (r+1, c-1), (r-1, c+1), (r-1, c-1).
- A bishop can only travel diagonally from (r, c) to the direction of (r+1, c+1), (r+1, c-1), (r-1, c+1), (r-1, c-1).

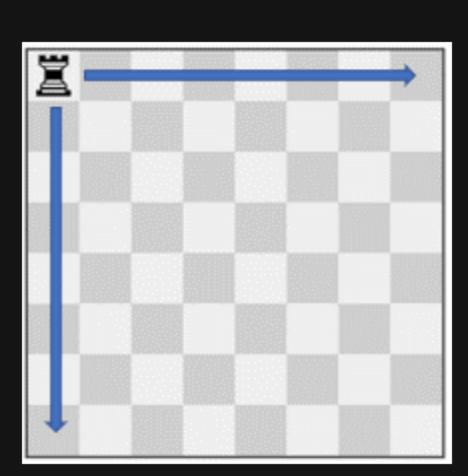
You must make a **move** for every piece on the board simultaneously. A **move combination** consists of all the **moves** performed on all the given pieces. Every second, each piece will instantaneously travel **one square** towards their destination if they are not already at it. All pieces start traveling at the second. A move combination is **invalid** if, at a given time, **two or more** pieces occupy the same square.

Return the number of valid move combinations.

Notes:

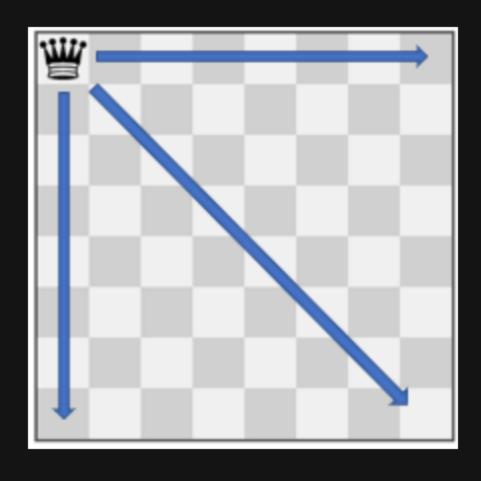
- No two pieces will start in the same square.
- You may choose the square a piece is already on as its destination.
- If two pieces are directly adjacent to each other, it is valid for them to move past each other and swap positions in one second.

Example 1:



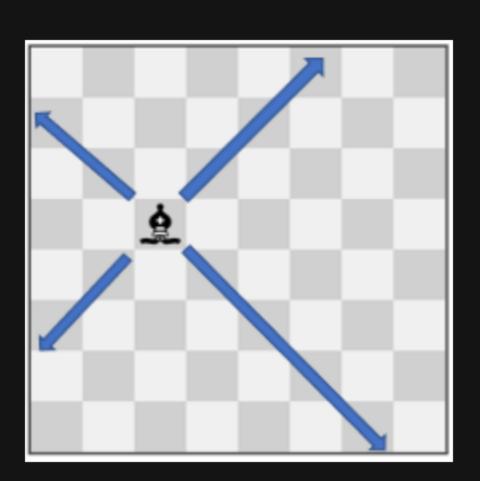
```
Input: pieces = ["rook"], positions = [[1,1]]
Output: 15
Explanation: The image above shows the possible squares the piece can move to.
```

Example 2:



```
Input: pieces = ["queen"], positions = [[1,1]]
Output: 22
Explanation: The image above shows the possible squares the piece can move to.
```

Example 3:



```
Input: pieces = ["bishop"], positions = [[4,3]]
Output: 12
Explanation: The image above shows the possible squares the piece can move to.
```

Constraints:

- n == pieces.length
- n == positions.length
- 1 <= n <= 4
- pieces only contains the strings "rook", "queen", and "bishop".
- There will be at most one queen on the chessboard.
- $1 \ll x_i, y_i \ll 8$
- Each positions[i] is distinct.