232. Implement Queue using Stacks

Queue

Leetcode Link

The task is to implement a queue with the FIFO (first in, first out) principle using two stacks. In a typical queue, elements are added,

Problem Description

Stack

Easy

Design

or 'pushed', to the back and removed, or 'popped', from the front. Additionally, you should be able to 'peek' at the element at the front without removing it and test if the queue is 'empty'. This should be done using only the standard operations of a stack: 'push to top', 'peek/pop from top', 'size', and 'is empty'.

Intuition The key to solving this problem is to use two stacks, stk1 and stk2, to invert the order of elements twice so that they come out in the same order that they went in. Initially, all new elements are pushed onto stk1. However, we can't directly pop from stk1 for the queue's pop operation because stacks follow LIFO order. So, to get the FIFO order of a queue, we reverse stk1 by popping all its

elements and pushing them onto stk2. The first element pushed into stk1 (and therefore the first in queue order) is now at the top of

stk2, allowing us to perform the FIFO pop correctly.

The move method is our helper that handles this transfer if stk2 is empty. It is lazily called only when necessary (when popping or peeking). This efficiency is important as it minimizes the number of operations. Once all elements are transferred to stk2, they can be popped or peeked in the correct FIFO order.

The empty method simply checks both stacks. If both are empty, the queue is empty. The elegance of this solution arises from the delayed transfer of elements until necessary (amortized analysis), which minimizes the number of total operations needed.

Solution Approach

The implementation consists of the following steps, utilizing two stacks, stk1 and stk2, which are simply represented as Python lists:

1. Constructor (__init__): Two empty stacks are initialized. stk1 is for adding new elements (push operation), and stk2 is used for

1 self.stk1 = []

2 self.stk2 = []

FIFO retrieval (pop and peek operations).

2. Push Operation (push): Elements are added to stk1. Each new element is simply appended to the end of stk1, which is the top

of the stack. 1 def push(self, x: int) -> None:

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3. Pop Operation (pop): To remove an element from the front of the queue, we need to get it from the bottom of stk1. The move
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method is called to transfer elements from stk1 to stk2, if stk2 is empty, effectively reversing the stack order. The element at the top of stk2 (the front of the queue) is then popped.

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4. Peek Operation (peek): Similar to pop, but instead of removing the element at the front of the queue, we only retrieve it. move
  ensures the element is moved to stk2 so that it can be peeked at.
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1 def empty(self) -> bool:

if not self.stk2:

while self.stk1:

return self.stk2[-1]

1 def peek(self) -> int:

self.move()

are empty.

1 def move(self):

Example Walkthrough

return self.stk2.pop()

1 def pop(self) -> int:

self.move()

self.stk1.append(x)

6. Move Helper Method (move): This is an essential method that transfers elements from stk1 to stk2 when stk2 is empty. It's called only before a pop or peek operation and only when necessary (i.e., when stk2 is empty and the next front of the queue needs to be accessed).

At its core, this approach leverages the fact that the stack data structure (using append and pop in Python lists) can be reversed by

5. Empty Operation (empty): This operation checks if both stk1 and stk2 are empty. The queue is empty if and only if both stacks

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transferring elements from one stack to another. By having two stacks, we can ensure elements are in the correct FIFO order for
queue operations by handling elements in the 'lazy' manner - that is, by only moving elements when absolutely necessary.
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Consider the following sequence of operations:

1. push(1) - Add the element '1' to the queue.

5. empty() - Check if the queue is empty.

Now let's examine how each operation is handled:

2. push(2): stk1 grows to [1, 2]. stk2 is still [].

1. push(1): stk1 receives the element as [1]. stk2 remains [].

return not self.stk1 and not self.stk2

self.stk2.append(self.stk1.pop())

2. push(2) - Add the element '2' to the queue after '1'. 3. peek() - Get the element at the front of the queue without removing it. 4. pop() - Remove the element from the front of the queue.

Let's walk through a small example to illustrate how the queue implementation using two stacks—stk1 and stk2—works.

3. peek(): We want to see the front element of the queue, which is '1'. However, since stk1 is LIFO, we need to move elements to

class MyQueue:

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32 + obj = MyQueue()

def __init__(self):

Initialize two stacks

def push(self, x: int) -> None:

self.in_stack = []

self.out_stack = []

self._shift_stacks()

Get the front element

return self.out_stack[-1]

self._shift_stacks()

def peek(self) -> int:

def empty(self) -> bool:

def _shift_stacks(self):

return self.out_stack.pop()

stk2 to access '1'. move() is called, transferring all elements from stk1 to stk2, resulting in stk1 as [] and stk2 as [2, 1]. Now we can peek the top of stk2 which is '1', the first element.

4. pop(): We need to pop the front element, which is '1'. Since stk2 already has the correct order, we simply pop from stk2. stk2

5. empty(): To determine if the queue is empty, we check if both stk1 and stk2 are empty. Since stk2 has an element '2', the

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The sequence of stk1 and stk2 after each operation is shown below:
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1. After push(1): stk1: [1], stk2: []

2. After push(2): stk1: [1, 2], stk2: []

method returns False, indicating the queue is not empty.

becomes [2] after popping '1', and stk1 is still [].

- 3. After peek(): stk1: [], stk2: [2, 1] 4. After pop(): stk1: [], stk2: [2]
- 5. After empty(): No change in stacks, stk1: [], stk2: [2]
- **Python Solution**

The queue is operational, demonstrating that two stacks used in this manner can effectively implement a FIFO queue.

Push an element onto the end of the queue self.in_stack.append(x) 9 10 def pop(self) -> int: 11

Return True if the queue is empty, False otherwise

Move elements from in_stack to out_stack if out_stack is empty

// Return true if the queue is empty, which is when both stacks are empty.

// Helper method to move elements from stkInput to stkOutput. It ensures that

// stkOutput contains elements in correct queue order for peeking or popping.

* The following operations demonstrate how to instantiate and operate on the MyQueue object:

* int param_3 = obj.peek(); // Retrieves but does not remove the front element of the queue

// Remove element from stack

// Return the saved element

* int param_2 = obj.pop(); // Retrieves and removes the front element of the queue

// Pushes element x to the back of the queue

return stkInput.isEmpty() && stkOutput.isEmpty();

stkOutput.push(stkInput.pop());

* MyQueue obj = new MyQueue(); // Creates an instance of MyQueue

* boolean param_4 = obj.empty(); // Checks whether the queue is empty

// Constructor for MyQueue doesn't need to do anything since

// Removes the element from the front of the queue and returns it

int element = outputStack.top(); // Save the top element

// The queue is empty only if both stacks are empty

return inputStack.empty() && outputStack.empty();

stack<int> inputStack; // Stack for enqueuing elements

stack<int> outputStack; // Stack for dequeuing elements

// Only move elements if outputStack is empty

while (!inputStack.empty()) {

// Helper function to move elements from inputStack to outputStack

// the standard library stack initializes itself

// Adds an element to the back of the queue

return not self.in_stack and not self.out_stack

Pop an element from the start of the queue

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               while self.in_stack:
29
                    self.out_stack.append(self.in_stack.pop())
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31 # The MyQueue object will be instantiated and called as following:
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if not self.out_stack:

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# obj.push(x)
  # param_2 = obj.pop()
35  # param_3 = obj.peek()
36 # param_4 = obj.empty()
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Java Solution
   class MyQueue {
       // Use two stacks to simulate a queue:
       // stkInput is used for input operations (push)
       // stkOutput is used for output operations (pop and peek)
       private Deque<Integer> stkInput = new ArrayDeque<>();
       private Deque<Integer> stkOutput = new ArrayDeque<>();
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       // Constructor for MyQueue. No initialization needed as
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       // member variables are already initialized.
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       public MyQueue() {
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       // Push element x to the back of the queue. Since a stack is LIFO (last-in, first-out),
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       // pushing to stkInput will reverse the order when transferred to stkOutput.
       public void push(int x) {
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           stkInput.push(x);
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       // Pop the element from the front of the queue.
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       // If stkOutput is empty, refill it by popping all elements
       // from stkInput and pushing them into stkOutput.
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       public int pop() {
           move();
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           return stkOutput.pop();
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       // Get the front element.
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       // Similar to pop, ensure stkOutput contains elements by moving
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       // them from stkInput if necessary and then return the top element.
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       public int peek() {
31
           move();
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private void move() { 42 43 // Only move elements if stkOutput is empty. if (stkOutput.isEmpty()) { 44 45 // Move all elements from stkInput to stkOutput. while (!stkInput.isEmpty()) { 46

* obj.push(x);

C++ Solution

#include <stack>

using std::stack;

MyQueue() {}

int pop() {

bool empty() {

void push(int x) {

inputStack.push(x);

prepareOutputStack();

outputStack.pop();

// Checks if the queue is empty

void prepareOutputStack() {

if (outputStack.empty()) {

return element;

class MyQueue {

public:

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return stkOutput.peek();

public boolean empty() {

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/**

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       // Returns the element at the front of the queue without removing it
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       int peek() {
           prepareOutputStack();
25
26
           return outputStack.top(); // Return the top element
27
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private:

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outputStack.push(inputStack.top()); // Move element to outputStack
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 45
                     inputStack.pop();
                                                         // Remove it from inputStack
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     };
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    /**
      * Example usage:
      * MyQueue* queue = new MyQueue();
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      * queue->push(1);
     * queue->push(2);
 55
     * int elem1 = queue->pop(); // returns 1
      * int elem2 = queue->peek(); // returns 2, the new front after popping 1
      * bool empty = queue->empty(); // returns false since there's still 2 in the queue
      * delete queue; // Don't forget to free memory
 60
      */
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Typescript Solution
 1 // These arrays will act as the stack containers for the queue.
   let stack1: number[] = [];
   let stack2: number[] = [];
   // This function simulates the push operation of a queue, where 'x' is the element to be added to the queue.
   function push(x: number): void {
       stack1.push(x);
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   // This function simulates the pop operation of a queue, by moving elements from the first stack to the second if necessary.
   function pop(): number {
       moveStacks();
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       return stack2.pop();
14 }
15
   // This function simulates the peek operation of a queue, returning the element at the front without removing it.
   function peek(): number {
       moveStacks();
       return stack2[stack2.length - 1];
20 }
21
   // This function checks whether the queue is empty.
   function empty(): boolean {
        return stack1.length === 0 && stack2.length === 0;
24
25 }
26
   // This helper function moves elements from stack1 to stack2 if stack2 is empty, effectively reversing the order to simulate queue be
   function moveStacks(): void {
       if (stack2.length === 0) {
29
           while (stack1.length !== 0) {
30
               stack2.push(stack1.pop());
```

Time and Space Complexity

let isEmpty = empty();

let val1 = pop();

Time Complexity:

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34 }

36 // Usage

38 push(1);

• pop(): Amortized O(1) - In the worst case, this operation can be O(n), where n is the number of elements in stk1, because it has to move all elements from stk1 to stk2 if stk2 is empty. However, each element is only moved once due to the two-stack arrangement, and, across a series of moperations, this gives an average (or amortized) time complexity of O(1).

__init__(): O(1) - Initializing two empty stacks takes constant time.

37 // Instead of creating an instance of MyQueue, you would directly call the functions:

• peek(): Amortized O(1) - Similar to pop(), it may involve moving all elements from stk1 to stk2 in the worst case, but due to the amortized analysis, it averages to constant time.

• push(x): O(1) - Append operation on a list (stack) is an amortized constant time operation.

- empty(): O(1) Checking if two lists are empty is a constant time operation. • move(): Amortized O(1) - Although it can be O(n) in the worst case when moving all elements from stk1 to stk2, it is part of the pop() and peek() operations and contributes to their amortized time complexity.
- **Space Complexity:** Overall space complexity for the MyQueue class is O(n), where n is the number of elements in the queue at a given time. This is because all elements are stored in two stacks (stk1 and stk2). No additional space is used that is proportional to the number of
 - elements in the queue except for these two stacks.