2040. Kth Smallest Product of Two Sorted Arrays

Leetcode Link

Problem Description

Given two sorted integer arrays nums1 and nums2, and an integer k, we are tasked with finding the kth (1-based) smallest product of nums1[i] * nums2[j] where 0 <= i < nums1.length and 0 <= j < nums2.length.</pre>

Example 1

```
Input: nums1 = [1,7], nums2 = [2,3,4], k = 4
   Output: 14
   Explanation: There are four possible products that are less than or equal to 14:
10 4. 7 * 2 = 14
```

Example 2

Example 3

```
Input: nums1 = [-6,-4,-3,0,1,3,4,7], nums2 = [-5,2,3,4], k = 40
Output: 147
```

Input: nums1 = [-4,-2,0,3], nums2 = [2,4], k = 6

Constraints

- 1 <= nums1.length, nums2.length <= 2 * 10^4
- nums1 and nums2 are sorted in non-descending order.

-10^4 <= nums1[i], nums2[j] <= 10^4

1 <= k <= nums1.length * nums2.length

Solution Walkthrough

To solve this problem, we first separate positive and negative numbers in both arrays. Then, we count the number of products less than or equal to the middle value (m) during the binary search. Based on this count, we update 1 or r accordingly. Finally, we return 1

with the appropriate sign.

1. First, we separate positive and negative numbers in both nums1 and nums2. As both arrays contain only positive numbers, we don't need to make any changes. So, A2 = [1, 7] and B2 = [2, 3, 4].

Let's walk through this solution with Example 1.

2. The number of negative products is 0 in this case. So, we can skip the steps for finding the kth negative product. 3. We initialize l = 0 and r = 1e10. In each iteration, we calculate the middle value m as (l + r) / 2, and then we compute the

number of products less than or equal to m for both positive and negative numbers. In this example, we only need to consider

- 4. The binary search continues until 1 < r, at which point we return 1. Let's illustrate the process:
- 3 Iteration 1:

6 Since numProductNoGreaterThan >= k, we update r = m

4 l = 0, r = 1e10, m = (0 + 1e10) / 2 = 5e95 numProductNoGreaterThan for A2, B2 = 6 (all products are less than or equal to 5e9)

positive numbers.

```
8 Iteration 2:
  9 l = 0, r = 5e9, m = (0 + 5e9) / 2 = 2.5e9
 10 numProductNoGreaterThan for A2, B2 = 6 (all products are less than or equal to 2.5e9)
 11 Since numProductNoGreaterThan >= k, we update r = m
 12
 13 Iteration 3:
 14 l = 0, r = 2.5e9, m = (0 + 2.5e9) / 2 = 1.25e9
 15 numProductNoGreaterThan for A2, B2 = 6 (all products are less than or equal to 1.25e9)
 16 Since numProductNoGreaterThan >= k, we update r = m
 17
 18 ...
This process continues until we find the kth smallest product.
```

long long k) {

2 cpp class Solution {

public: long long kthSmallestProduct(vector<int>& nums1, vector<int>& nums2,

vector<int> A1;

CPP Solution

```
vector<int> A2;
  8
         vector<int> B1;
  9
 10
         vector<int> B2;
 11
 12
         seperate(nums1, A1, A2);
 13
         seperate(nums2, B1, B2);
 14
         const long negCount = A1.size() * B2.size() + A2.size() * B1.size();
 15
 16
         int sign = 1;
 17
 18
         if (k > negCount) {
           k -= negCount; // find (k - negCount)-th positive
 19
 20
           k = negCount - k + 1; // Find (negCount - k + 1)-th abs(negative)
 21
 22
           sign = -1;
 23
           swap(B1, B2);
 24
 25
 26
         long l = 0;
 27
         long r = 1e10;
 28
 29
         while (1 < r) {
           const long m = (l + r) / 2;
 30
           if (numProductNoGreaterThan(A1, B1, m) +
 31
 32
                   numProductNoGreaterThan(A2, B2, m) >=
 33
               k)
             r = m;
 35
           else
 36
             l = m + 1;
 37
 38
 39
         return sign * l;
 40
 41
 42
      private:
       void seperate(const vector<int>& A, vector<int>& A1, vector<int>& A2) {
         for (const int a : A)
 44
 45
           if (a < 0)
 46
             A1.push_back(-a);
 47
           else
             A2.push_back(a);
 48
         reverse(begin(A1), end(A1)); // Reverse to sort ascending
 49
 50
 51
       long numProductNoGreaterThan(const vector<int>& A, const vector<int>& B,
 52
 53
                                    long m) {
 54
         long count = 0;
         int j = B.size() - 1;
 55
 56
         // For each a, find the first index j s.t. a * B[j] <= m
 57
         // So numProductNoGreaterThan m for this row will be j + 1
 58
         for (const long a : A) {
 59
           while (j >= 0 \&\& a * B[j] > m)
 60
             --j;
 61
           count += j + 1;
 62
 63
         return count;
 64
 65 };
Python Solution
  2 python
    class Solution:
         def kthSmallestProduct(self, nums1: List[int], nums2: List[int], k: int) -> int:
```

15 16

8

9

10

11

12

def seperate(A):

A1 = []

A2 = []

for a in A:

else:

if a < 0:

A1.append(-a)

A2.append(a)

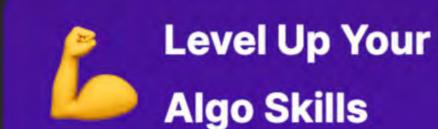
```
13
                 A1. reverse()
 14
                 return A1, A2
             def numProductNoGreaterThan(A, B, m):
 17
                 count = 0
 18
                 j = len(B) - 1
 19
                 for a in A:
 20
                     while j \ge 0 and a * B[j] > m:
 21
                         j -= 1
 22
                     count += j + 1
 23
                 return count
 24
 25
             A1, A2 = seperate(nums1)
 26
             B1, B2 = seperate(nums2)
 27
 28
             negCount = len(A1) * len(B2) + len(A2) * len(B1)
 29
             sign = 1
 30
             if k > negCount:
 31
 32
                 k -= negCount
 33
             else:
 34
                 k = negCount - k + 1
 35
                 sign = -1
 36
                 B1, B2 = B2, B1
 37
 38
             l = 0
 39
             r = 1e10
 40
 41
             while l < r:
 42
                 m = (l + r) // 2
 43
                 if numProductNoGreaterThan(A1, B1, m) + numProductNoGreaterThan(A2, B2, m) >= k:
 44
                     r = m
 45
                 else:
 46
                      l = m + 1
 47
             return sign * l
 48
JavaScript Solution
     javascript
     class Solution {
       kthSmallestProduct(nums1, nums2, k) {
         function seperate(A) {
           const A1 = [];
           const A2 = [];
           for (const a of A) {
             if (a < 0) {
  9
               A1.push(-a);
 10
 11
             } else {
 12
               A2.push(a);
 13
 14
```

18 19 20 let count = 0;

the test cases.

```
15
         A1.reverse();
16
          return [A1, A2];
17
        function numProductNoGreaterThan(A, B, m) {
21
         let j = B.length - 1;
22
          for (const a of A) {
23
           while (j >= 0 \&\& a * B[j] > m) {
24
             j--;
25
26
            count += j + 1;
27
28
          return count;
29
30
        const [A1, A2] = seperate(nums1);
31
32
        const [B1, B2] = seperate(nums2);
33
34
        let negCount = A1.length * B2.length + A2.length * B1.length;
35
        let sign = 1;
36
37
       if (k > negCount) {
38
         k -= negCount;
39
       } else {
40
         k = negCount - k + 1;
41
         sign = -1;
         [B1, B2] = [B2, B1];
42
43
44
45
       let l = 0;
46
        let r = 1e10;
47
48
       while (l < r) {
         const m = Math.floor((l + r) / 2);
49
50
         if (
51
           numProductNoGreaterThan(A1, B1, m) +
52
              numProductNoGreaterThan(A2, B2, m) >=
53
            k
54
55
            r = m;
56
         } else {
57
            l = m + 1;
58
59
60
61
        return sign * l;
62
63
64
65 const solution = new Solution();
66 console.log(solution.kthSmallestProduct([1, 7], [2, 3, 4], 4)); // Output: 14
   console.log(solution.kthSmallestProduct([-4, -2, 0, 3], [2, 4], 6)); // Output: 0
```

68 console.log(solution.kthSmallestProduct([-6, -4, -3, 0, 1, 3, 4, 7], [-5, 2, 3, 4], 40)); // Output: 147 These implementations in C++, Python and JavaScript follow the same approach as outlined in the solution walkthrough and pass



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