1340. Jump Game V

Dynamic Programming Sorting

Problem Description

under two conditions: 1. The value of x is between 1 and d, and the jump does not take you outside the bounds of the array. 2. You can only make the jump if the number at the starting index arr[i] is greater than arr[j], where j is the index you want to jump to, and arr[i] is also greater than all the numbers between indices i and j.

The problem presents an array of integers called arr alongside an integer d. You are tasked with finding the maximum number

of indices you can visit starting from any index in the array. From a given index i, you can jump to an index i + x or i - x

- You must navigate through the array by following these rules, with the goal being to maximize the number of indices visited.
- Intuition

The intuition for solving this problem hinges on dynamic programming, which keeps track of the optimal sub-structure: the maximum number of jumps that can be made from each index. The process can be visualized as follows:

Hard

1. We understand that each index is a potential starting point, and from each index, we need to consider jumps in both directions within the allowed range. 2. If we are at index i, to determine the optimal number of jumps (f[i]) from that index, we need to look at all indices j we could jump to within

- the specified d range. If a jump to j is permissible, we update f[i] to be a maximum between its current value and f[j] + 1 which accounts for the jump just made.
- 3. Since we need to ensure we are always jumping to a lower value, we sort the indices of the array based on the values at those indices. This ensures that when we are considering jumps from a particular index i, we have already computed the optimal jumps from lower valued indices. 4. In this manner, we build up an array f where f[i] represents the maximum number of indices that can be visited starting from index i. The
- end goal is to return the maximum value from this f array, representing the maximum number of indices visited from the best starting location. By building up a table of optimal solutions to sub-problems (f array) and using the sorted values to iterate in a controlled
- uncontrolled manner and encounter considerable overlap and repeated calculation of the same scenarios. Solution Approach

manner, we can use dynamic programming to compute the solution in an efficient way, without re-computing results. This makes

the program more efficient compared to brute-force approaches, which would try to make a jump from every index in an

The solution for this problem involves a dynamic programming approach. We create a table f where each index i has an initial value of 1, representing the minimum number of indices that can be visited (the index itself). We'll walk through the implementation approach step by step: The problem is framed as a <u>dynamic programming</u> one, which commonly involves filling out a table or array of values. In this

case, we're filling out the array 🕇 with the maximum number of indices that can be visited starting from each index.

Initially, all entries in f are set to 1, but as we explore jumps from each index, these entries may increase. We sort a list of pairs, where each pair consists of the value at each index arr[i] and the index itself i. This ensures we

always work from lower to higher values, respecting the jump rule that you can only jump to a smaller value. We iterate over the sorted list, and for each index i, we examine the possible indices we can jump to within the range d in both directions (to the left and to the right).

less than arr[i]. If both conditions are met, it means a jump from i to j is valid. Upon finding a valid jump, we update f[i] to be the maximum of its current value and f[j] + 1, reflecting the number of indices visited from j plus the jump just made from i to j.

For each possible jump from i to j, we check two conditions: whether the jump is within the distance d, and if arr[j] is

This updating of f[i] happens for all j within the jumpable range from i that match the criteria of lower value and within the d distance. This ensures that f[i] represents the optimal (maximum) number of indices visited starting from i.

Since f has been filled from the lowest value of arr[i] upwards, by the time we reach higher values, we've already

calculated the optimal number of indices that can be visited from all lower values; this property of the solution eliminates

unnecessary recalculations and ensures the solution is efficient. After we finish updating f[i] for all indices, the last step is to return max(f), the maximum value within f, which represents

This process structurally follows a bottom-up dynamic programming approach, going from smaller sub-problems to larger sub-

the maximum number of indices we can visit starting from the best possible index.

problems and using previous results to construct an optimal final answer.

Let's assume we have an array arr = [6, 4, 14, 6, 8] and d = 2. Following the solution approach:

We create our table f with the same length as arr and initialize all values to 1, because each index can visit at least itself.

After sorting by the first element in the pairs: [(4, 1), (6, 0), (6, 3), (8, 4), (14, 2)]. We proceed to iterate through our sorted list and consider jumps.

Starting with the pair (4, 1). There are no indices with smaller values than 4 within the range d, so we skip to the next

Considering pair (6, 3), we can jump to index 1 and index 4. We update f[3] to be the maximum of f[3] and f[1] + 1,

We create a list of pairs to sort by value in arr: [(6, 0), (4, 1), (14, 2), (6, 3), (8, 4)].

For the pair (6, 0), we can jump to index 1 which has the value 4 (and is within d distance). We update f[0] to be the maximum of f[0] and f[1] + 1, so:

0

pair.

f[4]:

these:

max(f) = 4

Example Walkthrough

f = [1, 1, 1, 1, 1]

f = [2, 1, 1, 1, 1]

and f[3] and f[4] + 1:

f = [2, 1, 4, 2, 3]

num_elements = len(arr)

 $jumps = [1] * num_elements$

break

break

return max(jumps)

int n = heights.length;

indices[i] = i;

Integer[] indices = new Integer[n];

for (int currentIndex : indices) {

// Look left of the current index

for (int i = 0; i < n; ++i) {

Check for jumps to the left

for left in range(position - 1, -1, -1):

With pair (8, 4), we examine the indices within range d (indices 2 and 3), but we can only jump to index 3, updating

To get the answer, we just take the maximum value in f:

def maxJumps(self, arr: List[int], max distance: int) -> int:

Determine the total number of elements in the array

for height. position in sorted(zip(arr, range(num_elements))):

Update the jump count if a new max is found

Update the jump count if a new max is found

Return the maximum jump count found across all positions

// Create an array of indices from the input array

- f = [2, 1, 1, 2, 1]
- f = [2, 1, 1, 2, 3]Lastly, the pair (14, 2). This value lets us jump to any lower index within d (0, 1, 3, and 4). We update f[2] for each of
- Solution Implementation **Python**

Initial jump counts set to 1 for each position, as each position can jump at least once

Process positions in ascending order of their heights, along with their indices

Stop if out of jump distance or if an equal or higher bar is met

if position - left > max_distance or arr[left] >= height:

if right - position > max_distance or arr[right] >= height:

jumps[position] = max(jumps[position], 1 + jumps[right])

Arrays.sort(indices, (i, j) -> Integer.compare(heights[i], heights[j]));

int maxJumps = 0; // Variable to keep track of the maximum number of jumps

for (int leftIndex = currentIndex - 1; leftIndex >= 0; --leftIndex) {

// Calculate the maximum number of jumps you can do from each position

// Update the result with the maximum dp value found so far

return maxJumps; // Return the maximum number of jumps possible

// Function to find the maximum number of jumps you can make in the array

// Sort the indices based on the corresponding values in 'heights'

// Initialize a vector to store the furthest jump length from every position

// Loop through the sorted indices to fill dp in increasing order of heights

sort(indices.begin(), indices.end(), [&](int a, int b) { return heights[a] < heights[b]; });</pre>

// If the left element is out of bounds or taller, stop checking further

// If the right element is out of bounds or taller, stop checking further

if (right - index > maxDistance || heights[right] >= heights[index]) {

if (index - left > maxDistance || heights[left] >= heights[index]) {

// Update dp array for index with the optimal previous jump count

vector<int> dp(n, 1); // All elements are initialized to 1 as the minimum jump is always 1 (itself)

int maxJumps(vector<int>& heights. int maxDistance) {

int n = heights.size(); // Size of the array

// Look to the left of the current index

for (int left = index - 1; left >= 0; --left) {

dp[index] = max(dp[index], 1 + dp[left]);

for (int right = index + 1; right < n; ++right) {</pre>

iota(indices.begin(), indices.end(), 0);

vector<int> indices(n);

for (int index : indices) {

break;

break;

// Initialize an index vector with values from 0 to n-1

maxJumps = Math.max(maxJumps, dp[currentIndex]);

So the maximum number of indices we can visit starting from the best index is 4, which starts from index 2 in the example array.

Now we have our completed f table indicating the maximum number of indices that can be visited starting from each index.

jumps[position] = max(jumps[position], 1 + jumps[left]) # Check for jumps to the right for right in range(position + 1, num elements): # Stop if out of jump distance or if an equal or higher bar is met

C++

public:

#include <vector>

#include <numeric>

class Solution {

TypeScript

import { max } from 'lodash';

break;

// maxJumps([4, 2, 7, 6, 9, 14, 12], 2);

num_elements = len(arr)

 $jumps = [1] * num_elements$

break

return max(jumps)

Time Complexity

Time and Space Complexity

Check for jumps to the left

for left in range(position -1, -1, -1):

// Example usage:

class Solution:

#include <algorithm>

using namespace std;

class Solution:

Java class Solution { public int maxJumps(int[] heights, int maxDistance) {

```
break;
   // Update the dp value if we find a better path
   dp[currentIndex] = Math.max(dp[currentIndex], 1 + dp[leftIndex]);
// Look right of the current index
for (int rightIndex = currentIndex + 1; rightIndex < n; ++rightIndex) {</pre>
   // If it's too far or the height at rightIndex is higher or equal, we can't jump from there
   if (rightIndex - currentIndex > maxDistance || heights[rightIndex] >= heights[currentIndex]) {
        break;
   // Update the dp value if we find a better path
   dp[currentIndex] = Math.max(dp[currentIndex], 1 + dp[rightIndex]);
```

// Sort the indices based on the heights, if the same height maintain the order of indices

Arrays.fill(dp, 1); // Initialize with 1 since the min jumps for each position is 1 (stand still)

// If it's too far or the height at leftIndex is higher or equal, we can't jump from there

if (currentIndex - leftIndex > maxDistance || heights[leftIndex] >= heights[currentIndex]) {

int[] dp = new int[n]; // Dynamic programming array to store the max number of jumps

// Update dp array for index with the optimal previous jump count dp[index] = max(dp[index], 1 + dp[right]); // Return the maximum jumps that can be made, found in the dp array return *max_element(dp.begin(), dp.end()); **}**;

// Importing necessary functionalities from arrays and algorithms

function maxJumps(heights: number[], maxDistance: number): number {

const n: number = heights.length; // Size of the array

// Initialize an index array with values from 0 to n-1

indices.sort((a, b) => heights[a] - heights[b]);

// Look to the right of the current index

// Function to find the maximum number of jumps you can make in the array

const indices: number[] = Array.from({ length: n }, (_, i) => i);

// Sort the indices based on the corresponding values in 'heights'

// Initialize an array to store the furthest jump length from every position

// If the left element is out of maxDistance or taller, stop checking further

// If the right element is out of maxDistance or taller, stop checking further

if (right - index > maxDistance || heights[right] >= heights[index]) {

// If you want to call the function, you would pass in the heights array and maxDistance like so:

Process positions in ascending order of their heights, along with their indices

Stop if out of jump distance or if an equal or higher bar is met

if position - left > max_distance or arr[left] >= height:

jumps[position] = max(jumps[position], 1 + jumps[left])

jumps[position] = max(jumps[position], 1 + jumps[right])

Initial jump counts set to 1 for each position, as each position can jump at least once

if (index - left > maxDistance || heights[left] >= heights[index]) {

// Update dp array for index with the optimal previous jump count

// Look to the right of the current index

const dp: number[] = new Array(n).fill(1); // All elements are initialized to 1 as the minimum jump is always 1 (itself) // Loop through the sorted indices to fill dp in increasing order of heights indices.forEach((index) => { // Look to the left of the current index for (let left = index - 1; left >= 0; --left) {

dp[index] = Math.max(dp[index], 1 + dp[left]);

for (let right = index + 1: right < n: ++right) {</pre>

break; // Update dp array for index with the optimal previous jump count dp[index] = Math.max(dp[index], 1 + dp[right]); }); // Return the maximum jumps that can be made, found in the dp array return Math.max(...dp);

def maxJumps(self, arr: List[int], max distance: int) -> int:

Determine the total number of elements in the array

Check for jumps to the right for right in range(position + 1, num elements): # Stop if out of jump distance or if an equal or higher bar is met if right - position > max_distance or arr[right] >= height: break

for height, position in sorted(zip(arr, range(num_elements))):

Update the jump count if a new max is found

Update the jump count if a new max is found

Return the maximum jump count found across all positions

The time complexity of the given code can be analyzed based on the following: 1. Sorting the array arr alongside the indices has a complexity of O(n log n) where n is the length of the array arr.

2. The double nested loops contribute to the time complexity in the following way:

- Each inner loop performs a linear scan in both directions, but due to the constraint limiting the jumps to distance d, the inner loops each run at most d times. \circ Therefore, the inner loops collectively contribute at most 0(n * 2d) = 0(nd) time complexity.
- Combining these, the total time complexity of the code is $0(n \log n + nd)$.
- **Space Complexity**

The outer loop runs n times since it iterates over the sorted arrays of heights and indices.

- The space complexity of the given code can be analyzed based on the following: 1. An auxiliary array f of size n is used to store the maximum number of jumps from each position, contributing an O(n) space complexity. 2. Since there are no recursive calls or additional data structures that grow with the input size, and the sorting operation can be assumed to use
 - 0(1) space given that most sorting algorithms can be done in-place (like Timsort in Python), the additional space complexity imposed by the stack frames during the for loops and sorting is constant. Therefore, the total space complexity of the code is O(n).