



Problem Description

The problem presents a situation where we need to calculate the sum of two integers a and b. However, the challenge here is that we are restricted from using the usual addition and subtraction operators, which are + and -. This requires a different approach to perform the addition operation by means other than direct arithmetic operators.

Intuition

addition process. A common way to achieve this is by using bitwise XOR and AND operations. The XOR operation can be used to simulate the addition without carrying, and the AND operation followed by a left shift can be used to determine the carry from the addition. Here's a step-by-step process of the thinking:

The intuition behind the solution is based on bitwise operations. Since we cannot use the + and - operators, we need to simulate the

1. XOR for Addition: The XOR operation gives a binary number that represents the summation of two bits where carrying is not accounted for. For example, 1 XOR 1 is 0, 1 XOR 0 is 1, which aligns with addition of bits without carrying.

- 2. AND for Carry: The AND operation gives a binary number that represents the bits that would need to be carried in a standard addition operation. For example, 1 AND 1 is 1, which means there is a carry.
- 3. Shift for Carry Position: The carried value from the AND operation is then left-shifted one bit because the carry from any particular bit would go to the next higher bit in a binary addition.
- 4. Iteration Until No Carry: We need to repeat this process until there is no carry left, i.e., the result of the AND operation is 0.
- bitwise operations are performed with a mask of 0xFFFFFFFF.

5. Masking with OxFFFFFFFF: To ensure compatibility with negative numbers and to simulate 32-bit integer overflow behavior,

- 6. Check for Negative Result: If the result has its leftmost bit (bit 31) set, it is negative (in 32-bit two's complement form). To convert it to a negative number that Python recognizes, the inverse operation is applied (via ~(a ^ 0xFFFFFFFF)).

Considering the above intuition, the solution approach simulates the addition of two integers using bitwise operations that reflect the

Solution Approach The implementation of the solution uses bitwise operations to mimic the addition process. Below is a detailed walk-through of how

the provided code implements the algorithm:

1 a, b = a & 0xfffffffff, b & 0xfffffffff

This ensures that we're only considering the lower 32 bits of the integers, which simulates the overflow behavior of a 32-bit

machine. In a 32-bit environment, integers wrap around when they exceed their maximum or minimum limits, and bitwise operations in Python can produce similar results by using this mask.

2. Loop for Iterative Addition: Next, a while loop is started, which continues as long as b is non-zero:

mechanics of binary addition while respecting the constraints of 32-bit signed integer overflow.

```
1 While b:
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the result by 1 bit:

negative number:

1 carry = ((a & b) << 1) & 0xFFFFFFFF

The value of b holds the carry bits that need to be added to a. The loop iterates until there are no carry bits left to add.

3. Calculating Carry: Inside the loop, the carry is calculated by performing a bitwise AND between a and b, and then left shifting

The result is again masked to ensure it stays within 32 bits. 4. Adding Without Carry: The XOR operation is then used to add a and b without considering the carry:

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1 a, b = a ^ b, carry
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Python can interpret correctly.

Here, a now contains the intermediate sum without the carry bits, while b takes on the value of the carry bits that need to be added in the next iteration.

1 return a if a < 0x80000000 else ~(a ^ 0xFFFFFFFF)

If the most significant bit of a (bit 31) is not set, a is returned directly. If it is set, it indicates a negative number in 32-bit two's

complement form, so the bitwise complement operator ~ is used in conjunction with ^(XOR) to get the negative integer that

5. Handling Negative Numbers: Once the loop completes (when there is no carry left), the function checks if the result is a

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The code leverages the concept of two's complement for negative numbers. In two's complement, a negative number is represented
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through the XOR and AND operations). No additional data structures are used in this implementation; the solution is carried out with simple integer variables and bitwise operations.

In conclusion, this implementation carefully applies fundamental binary arithmetic operations in a loop to achieve the same result as

by inverting all the bits of its positive counterpart and then adding 1 to the least significant bit (which happens here indirectly

the addition operator while conforming to the specified constraints relating to arithmetic operators and integer overflow behavior. Example Walkthrough

Let's take smaller, more manageable integers to explain the logic clearly. We will add two integers, a = 13 and b = 8, without using

the + and - operators. In binary form, a is 1101 and b is 1000. 1. Mask both a and b with 0xFFFFFFFF. For the value ranges in our example, this has no effect because both a and b are positive

2. Enter the while loop where b is not zero. Initially, b is 1000 (or 8), so the loop commences.

1 a, b = a ^ b, carry

6. Inside the loop again:

and within the 32-bit limit.

1 a, b = 13 & 0xfffffffff, 8 & 0xfffffffff

4 # carry = 10000 & 0xFFFFFFFF

5 # carry = 16, in binary: 10000

1 carry = ((a & b) << 1) & 0xFFFFFFFF</pre>

3 # carry = (00000 << 1) & 0xFFFFFFF

4 # b = carry = 00000, which is 0 in decimal

def getSum(self, a: int, b: int) -> int:

a, b = a & MASK, b & MASK

 $a, b = a ^ b, carry$

if a < 0x80000000:

return a

MASK = 0xFFFFFFFF

Mask to get 32-bit representation

Convert a and b to 32-bit integers

carry = ((a & b) << 1) & MASK

4 # carry = 00000 & 0xFFFFFFF

5 # carry = 0, in binary: 00000

And for the XOR operation:

2 # carry = ((0101 & 10000) << 1) & 0xFFFFFFFF

- 1 carry = ((a & b) << 1) & 0xFFFFFFFF 2 # carry = ((1101 & 1000) << 1) & 0xFFFFFFFF 3 # carry = (1000 << 1) & 0xFFFFFFF
- 2 # a = 1101 ^ 1000 3 # a = 0101, which is 5 in decimal 4 # b = carry = 10000, which is 16 in decimal

5. Since b is still not zero, the loop continues with the new values of a and b.

4. Perform the addition without carry using XOR, and update the carry from step 3:

3. Calculate the carry by ANDing a and b, then left shifting by one (<<1):

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1 a, b = a ^ b, carry
2 # a = 0101 ^ 10000
3 + a = 10101, which is 21 in decimal
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- 1 return a # which is 21 in our example Thus, we have successfully added a and b using bitwise operations, simulating their binary addition process without using the + and
 - # Iterate while there is a carry while b: # Calculate the carry from a and b, # and ensure it's within the 32-bit boundary

The operation 'a < 0x80000000' checks if the result is within the positive range

XOR a and b to find the sum without considering carries,

If a is outside the 32-bit integer range, which means it is negative,

// Perform XOR operation to add 'a' and 'b' without the carry

analyze the time and space complexity, we'll consider each operation within the loop:

// Once 'b' is zero, there is no carry and 'a' has the sum result; return it.

// Assign the carry to 'b' for the next iteration

then consider the carry for the next iteration

of a 32-bit integer (from 0x00000000 to 0x7FFFFFFF)

If a is within the 32-bit integer range, return it directly

7. Since b is now zero, we exit the loop. We check if a is negative by looking at bit 31 (it is not in our case).

8. Return a because the most significant bit of a is not set, implying that the result is a positive number:

operators. This example demonstrates how we obtain the sum 21, which we expect from adding 13 and 8.

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           # return the two's complement negative value, which is the bitwise negation of a
           # (by XORing with MASK, which is 'all 1's for a 32-bit number') and adding 1
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            return ~(a ^ MASK)
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Python Solution

class Solution:

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Java Solution
   class Solution {
       public int getSum(int a, int b) {
           // If there is no carry (b == 0), then we have found the sum and can return 'a'
           if (b == 0) {
               return a;
           } else {
           // If there is a carry, recursively call getSum with the following parameters:
           // 1. a XOR b - This calculates the sum without carry
           // 2. (a AND b) << 1 - This calculates the carry and shifts it one bit to the left, as carry affects the next higher bit
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               return getSum(a ^ b, (a & b) << 1);</pre>
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12
13 }
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C++ Solution
 1 class Solution {
 2 public:
       int getSum(int a, int b) {
           // Loop until there is no carry
           while (b != 0) {
               // Calculate the carry and cast to unsigned int to handle overflow
               unsigned int carry = (unsigned int)(a & b) << 1;
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function getSum(a: number, b: number): number { // Loop until there is no carry.

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19 };

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while (b !== 0) {
          // Calculate the carry, and use >>> 0 to ensure it is treated as an unsigned 32-bit integer.
           let carry: number = (a & b) << 1 >>> 0;
          // Perform XOR operation (add without carry).
           a = a ^ b;
           // Assign the carry to 'b' for the next iteration.
          b = carry;
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       // Once 'b' is zero, there is no carry and 'a' has the sum; return 'a'.
Time and Space Complexity
The given Python code is an implementation of bit manipulation to calculate the sum of two integers without using the + operator. To
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14 16 }

 $a = a ^ b;$

b = carry;

return a;

Typescript Solution

Time Complexity:

XOR. These operations themselves have a time complexity of O(1). However, the number of iterations of the loop depends on the values of a and b and when the carry will become 0. In the worst case, it will iterate approximately log C times where C is the maximum possible value for carry. Considering 32-bit integers, the loop runs at most 32 times (the number of bits), thus the time complexity can be considered 0(1) for 32-bit integers, since it does not depend on the size of the input, but rather on the fixed number of bits used to represent the integers in memory.

The while loop in the code runs as long as b is not zero. Each iteration involves constant-time bit operations: AND, SHIFT LEFT, and

Space Complexity:

The space complexity of the algorithm is 0(1) as well, as it uses a fixed number of integer variables (a, b, carry) regardless of the input size. There is no use of dynamic memory allocation or data structures that grow with input size.