169. Majority Element

Divide and Conquer

Hash Table

Leetcode Link

Problem Description

You are given an array called nums that has a certain number of elements, denoted as n. You have to find the majority element in this array. The majority element is defined as the one that appears more than n / 2 times. It's guaranteed that there is always a majority element in the array you're given.

Sorting

Counting

Intuition

Easy

The intuition behind the solution comes from the understanding that if an element occurs more than n / 2 times, it means that element is present more often than all other elements combined. For every instance of a non-majority element, there must be more instances of the majority element. We can use this intuition with a clever algorithm known as the Moore Voting Algorithm.

The Moore Voting Algorithm works by keeping a current candidate for majority element and a counter. As it goes through the array, the algorithm either increases the count if the current number matches the candidate or decreases the count otherwise. When the count reaches zero, it means that up to that point, there is no majority element, and the algorithm selects the current number as the new candidate. The key insight is that the majority element's surplus count will withstand the count decrements due to non-majority elements.

Therefore, we initialize a counter cnt to zero and a majority element candidate m to none. Then, for each element x in nums, we make the following check:

If cnt is not zero, we increase the count by 1 if x is equal to m (our current candidate), otherwise, we decrease the count.

If cnt is zero, we assume the current element x can be a new majority candidate m, and we set cnt to 1.

element exists, we don't need to verify m on a second pass.

After processing all elements of the array, our current candidate m is the majority element. Since we are guaranteed that a majority

The solution uses the Moore Voting Algorithm, which is efficient in finding the majority element of an array when such an element

Solution Approach

definitely exists.

the presumed majority element, and the counter cost indicating the strength of our presumption that m is indeed the majority element. To implement the algorithm, we iterate through each element x of the array nums. During this iteration, the following logic is applied:

The algorithm works in a single pass and uses constant extra space. It consists of two main variables: the candidate m representing

1. When cot equals zero, there's no current candidate for majority element, or the previous candidate has been completely offset

- by other elements. So we assign the current element x to be the new candidate m, and set cnt to 1, because we start counting the occurrences of m again. 2. If cnt is not zero, it means there's a candidate set and we need to compare the current element x with m.
- If x is equal to m, this means we've found another instance of our candidate, and we increment the counter cnt by 1,
 - strengthening the candidacy of m. o If x is not equal to m, this means we have encountered an element that opposes our candidate. To denote this opposition, we decrement the counter cnt by 1.
- By the end of the loop, despite all the increments and decrements, the surplus repetitions of the majority element ensure that m will remain as the candidate and cnt will be greater than zero.

Given the guarantee that a majority element always exists, in is the majority element at the end of this single pass, and we can return m as the answer.

It's important to note that if the problem statement didn't guarantee the existence of a majority element, a second pass would be necessary to confirm that our candidate m is indeed the majority by counting its total occurrences in nums and comparing it to n / 2.

Assume we have an array nums = [3, 3, 1, 3, 2, 3]. We want to use the Moore Voting Algorithm to find the majority element. The

Example Walkthrough

majority element is the element that appears more than n / 2 times in the array (n is the size of the array which in this case is 6, so n / 2 is 3). The steps are as follows: 1. We initialize cnt to 0 and m to any value (let's choose m = None for the start).

- Start with the first element (nums [0] = 3).
- \circ Since cnt is 0, we set m = 3 and cnt = 1.

2. Traverse the elements of nums:

- Move to the second element (nums [1] = 3).
- Since cnt is not 0 and m is equal to nums [1], we increment cnt to 2. Proceed to the third element (nums [2] = 1).
- The current element is not equal to m, so we decrement cnt to 1. Next, the fourth element (nums [3] = 3).
- The current element is equal to m, therefore cnt is incremented to 2.
- Then, the fifth element (nums [4] = 2). This is not equal to m, and so cnt is decremented to 1.
- Finally, the sixth element (nums [5] = 3).
- It is equal to m, meaning cnt gets incremented again, now cnt = 2.
- 3. Despite the increment and decrement of cnt, at the end of the traversal, m remains 3. Since cnt is greater than 0, we are left with

Process each number in the list

count = 1

for (int num : nums) {

} else {

if (count == 0) {

count = 1;

} else {

candidate = num;

count++;

if (num == candidate) {

// If different, decrement count

// If count is not 0, increment or decrement the count

// (due to the problem's guarantee that a majority element always exists)

// Decrement if it is different

count += (candidate == num) ? 1 : -1;

// After the loop, the candidate is the majority element

// Increment if the current element is the same as the candidate

- m = 3 as the candidate for the majority element.
- majority element is 3. By the end of the process, we successfully used the Moore Voting Algorithm to find the majority element which is 3 in the given

4. As the problem guarantees the presence of a majority element, we don't need to check m in a second pass. We declare that the

example array.

class Solution: def majorityElement(self, nums: List[int]) -> int: # Initialize the count and the candidate for majority element count = 0 majority_candidate = None

If the current number is the same as the majority candidate, increase the count

// If count is zero, we choose the current element as the new candidate

// If the current element is the same as the candidate, increment count

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for num in nums:
               # If the current count is 0, we choose a new number as the potential majority candidate
               if count == 0:
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                   majority_candidate = num
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Python Solution

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elif majority_candidate == num:
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                   count += 1
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               # Otherwise, decrease the count
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               else:
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                   count -= 1
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           # The majority candidate is the number that remains after pairing off different elements
           return majority_candidate
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Java Solution
   class Solution {
       // This method finds the majority element in an array, which is defined as the element that appears more than n/2 times
       public int majorityElement(int[] nums) {
           // Initialize count and candidate for majority element
           int count = 0;
           int candidate = 0;
           // Iterate over all elements in the array
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count--;
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           // The candidate is the majority element, which is guaranteed to exist
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           return candidate;
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C++ Solution
   #include <vector> // Include the vector header for using the vector container
   class Solution {
   public:
       // Function to find the majority element in the array
       // A majority element is an element that appears more than n/2 times in the array
       int majorityElement(vector<int>& nums) {
           int count = 0; // Counter for the number of times the current candidate is found
           int candidate = 0; // Variable to store the current potential majority element
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           // Iterate through all the elements in the given array
           for (int num : nums) {
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               if (count == 0) {
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                   // If the count is 0, we select the current element as our new candidate for majority element
                   candidate = num;
16
                   count = 1; // Set the count for this new candidate to 1
17
               } else {
```

28 29 }; 30

return candidate;

```
Typescript Solution
   function majorityElement(numbers: number[]): number {
       // Initialize a count variable to keep track of the frequency of the majority element.
       let count: number = 0;
       // Initialize a variable to hold the current majority element.
       let majorityElement: number = 0;
       // Iterate through each number in the numbers array.
       for (const number of numbers) {
           // If count is zero, we found a new possible majority element.
           if (count === 0) {
               majorityElement = number;
               count = 1;
13
           // If the current number is the same as the majority element, increment the count.
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           // Otherwise, decrement the count.
15
           else {
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               count += (majorityElement === number) ? 1 : -1;
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       // At the end of the loop, the majorityElement variable will contain the majority element.
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       return majorityElement;
23 }
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```

Time and Space Complexity

The given Python code snippet is an implementation of the Boyer-Moore Voting Algorithm, designed to find a majority element (an element that appears more than n/2 times) from a list. The time complexity and space complexity of this algorithm are analyzed as

The function iterates through the list nums exactly once. For each element x in nums, the code executes a constant number of operations, either incrementing, decrementing, or setting the count cnt and possibly updating the candidate majority element m. Thus, the number of operations is proportional to the length of nums, which is n. Therefore, the time complexity is O(n).

The algorithm uses a fixed amount of extra space: two variables cnt and m to keep track of the current count and the potential

majority element respectively. The amount of space used does not depend on the size of the input list, therefore, the space

Space Complexity:

complexity is constant, 0(1).

follows: **Time Complexity:**