750. Number Of Corner Rectangles

Dynamic Programming

Matrix

Problem Description

Array

Math

Medium

defined by four '1's that are placed in the grid in such a way that they form the corners of an axis-aligned rectangle. Importantly, the interior of this rectangle can contain any mix of '0's and '1's; the only requirement is that the four corners are '1's. The grid, grid, is composed entirely of '0's and '1's, and its dimensions are $m \times n$ where m is the number of rows and n is the number of columns. The task is to return the total count of such distinct corner rectangles.

The given LeetCode problem asks us to count the number of distinct "corner rectangles" in a 2D grid. A "corner rectangle" is

Intuition

To solve this problem, we leverage the fact that a rectangle is defined by its two opposite corners. Here, we iterate over all

potential corner pairs in the grid and try to determine if these pairs can form the upper two or lower two corners of a rectangle.

We do this by checking if we picked two '1's in the same row. For each pair of '1's in the row, we check to see if the same pair of

columns also have '1's in another row, forming a rectangle. To efficiently track this, we employ a counting strategy that uses a dictionary to remember how many times we've seen each pair of '1's in the same row. Whenever we encounter a pair of '1's in the same row, we check the dictionary to see if this pair has been seen before. If it has, then for each previous occurrence, there is a distinct rectangle. Therefore, the count of rectangles is incremented by the number of times the pair has been seen before. Afterwards, we increment the counter for that pair, indicating that we've found another potential set of top corners for future rectangles.

indices where '1's are found, it ensures that the process of finding rectangular corners is efficient, avoiding checking every possible rectangle explicitly, which would be computationally expensive especially for large grids. Solution Approach

The algorithm iterates over all rows and, within each row, all pairs of '1's. By using a counter dictionary that keeps track of pairs of

The solution employs a simple yet efficient approach using a hash table to keep track of the count of '1' pairs encountered so far. Here's a step-by-step walkthrough of how the code works: **Initialize Variables:**

Find Pairs of '1's in the Same Row:

Iterate Over the Grid: • The first for loop iterates through each row of the grid.

• Create a Counter object named cnt from the Python collections module. This counter will map each pair of column indices (i, j) to the

∘ If c1 is '1', it means we have a potential top/left corner of a rectangle.

Check for Potential Top/Right Corners: o Another nested for loop is used to check to the right of the current '1' for another '1' at index j, forming a pair of top corners (i, j) of a

• Within each row, use a nested for loop with enumerate to get both the index i and value c1 at that index.

potential rectangle. **Count and Update Rectangles:**

Example Walkthrough

• For each such pair (i, j), if they can form the top two corners of a rectangle, we increment ans by cnt[(i, j)] since each count represents another row where a rectangle with these top corners can be completed. After counting the rectangles for (i, j), update cnt[(i, j)] by incrementing by 1 which signifies that we have found another pair of '1's

After all rows and valid pairs are processed, return ans as the total count of corner rectangles found in the grid.

Initialize a variable ans to 0, which will hold the final count of corner rectangles.

number of times that pair has been observed in grid with '1's.

that can form the top corners of potential future rectangles. **Return the Answer:**

elegant and efficient solution. By checking only rows for pairs of '1's and then counting and updating the number of potential rectangles as more pairs are found, the solution effectively captures all corner rectangles without unnecessary computations.

This solution utilizes a smart counting approach to avoid checking each potential rectangle directly, which drastically reduces the

time complexity. The main algorithmic techniques include iterating over array elements and using hash-based counters for an

matrix containing both 0's and 1's. grid = [[1, 0, 1], [1, 1, 1], [1, 0, 0], [1, 0, 1]

Let's walk through a small example to illustrate how the solution approach works. Consider the following grid which is a 4×3

Start with the first row [1, 0, 1].

fourth row.

Initialize Variables:

Iterate Over the Grid:

• cnt is an empty Counter object.

Find Pairs of '1's in the Same Row:

Repeat steps 2-5 for remaining rows:

Check for Potential Top/Right Corners:

• Second row [1, 1, 1] has '1's at indices 0, 1, and 2.

• Identify two '1's in the row at index i = 0 and j = 2.

Since cnt[(0, 2)] is not in cnt, ans remains 0, but cnt[(0, 2)] becomes 1.

• Pairs (0, 1), (0, 2), and (1, 2) each have the potential to form corner rectangles.

two times so far), a rectangle can be completed, so ans gets incremented by 2.

Finally, after iterating through all rows, we conclude with:

def countCornerRectangles(self, grid: List[List[int]]) -> int:

rectangle count = 0 # This will hold the final count of corner rectangles

Enumerate over the row to get both column index and value

Only process if the cell at the current column has a 1

Consider pairs of columns, starting from the current one

for col index second in range(col index first + 1, num cols):

Check if the second column also has a 1 at the current row

pair_counter[(col_index_first, col_index_second)] += 1

1. `rectangle count`: Renamed `ans` to `rectangle count` to better describe what the variable is used for.

5. Comments: Added explanatory comments throughout the code to provide clarity on each step of the process.

for col index first, cell first in enumerate(row):

if row[col index second]:

Return the total count of rectangles found

public int countCornerRectangles(int[][] grid) {

// This will store the final count of corner rectangles.

Map<List<Integer>, Integer> pairsCount = new HashMap<>();

if (row[rightCol] == 1) {

// The result is the total count of rectangles found.

for (int leftCol = 0; leftCol < numCols; ++leftCol) {</pre>

// Iterate over every possible pair of columns within this row

// If the current cell is a 1, explore further for a rectangle.

// A map to store the counts of 1's pairs across rows.

// Number of columns in the grid.

// Loop through each row in the grid.

if (row[leftCol] == 1) {

int numCols = grid[0].length;

int cornerRectanglesCount = 0;

for (int[] row : grid) {

return cornerRectanglesCount;

return answer;

function countCornerRectangles(grid: number[][]): number {

const pairCounts: Map<number, number> = new Map();

// Looping through each cell in the row

for (let i = 0; i < columnsCount; ++i) {</pre>

if (row[i] === 1) {

// Check if the current cell has value 1

const columnsCount = grid[0].length;

// Looping through each row in the grid

if (row[i] === 1) {

return cornerRectanglesCount;

from collections import Counter

for row in grid:

let cornerRectanglesCount = 0;

for (const row of grid) {

// Initialization of n to represent the number of columns

// Initialization of the answer variable to count corner rectangles

for (let j = i + 1; j < columnsCount; ++j) {</pre>

const pairKey = i * 200 + j;

// Returning the total count of corner rectangles found in the grid

def countCornerRectangles(self, grid: List[List[int]]) -> int:

Iterate through each row in the grid

if cell first:

return rectangle_count

Changes and comments explanation:

num_cols = len(grid[0]) # The number of columns in the grid

if row[col index second]:

Return the total count of rectangles found

// Using a Map to keep track of the count of pairs of cells with value 1

// Nested loop to find another cell with value 1 in the same row

// Creating a unique kev for the pair of cells

// Increment count for the current pair of cells

// Update the pair count map with the new count

rectangle count = 0 # This will hold the final count of corner rectangles

Only process if the cell at the current column has a 1

Consider pairs of columns, starting from the current one

for col index second in range(col index first + 1, num cols):

Check if the second column also has a 1 at the current row

pair_counter[(col_index_first, col_index_second)] += 1

1. `rectangle count`: Renamed `ans` to `rectangle count` to better describe what the variable is used for.

5. Comments: Added explanatory comments throughout the code to provide clarity on each step of the process.

Make sure to replace `List` by the correct import statement from 'typing' at the beginning of the file:

cornerRectanglesCount += pairCounts.get(pairKey) ?? 0;

pairCounts.set(pairKey, (pairCounts.get(pairKey) ?? 0) + 1);

pair counter = Counter() # Counter to track pairs of columns that have a 1 at the same row

};

TypeScript

• ans = 3 (total count of corner rectangles found in the grid).

ans starts at 0.

 These are the potential top corners of multiple rectangles. Count and Update Rectangles:

```
As we process this row, and gets updated because cnt[(0, 2)] was already 1 (one rectangle can now be formed with the
previous row as the bottom corners).
Now, ans is incremented by 1.
Continuing on to the third and fourth rows, you'll do the same pair checks and counts, but no updates to ans occur until the
```

• In the fourth row [1, 0, 1], the same pair (0, 2) is found as in the first row, meaning that for every previous occurrence of this pair (which is

This example illuminated how only pairs of '1's in the same rows are used to determine the possibility of forming rectangles, and

with each row's pairs, we effectively keep a running count of potential rectangles without the need for checking all possible

rectangles directly. The Counter efficiently handles this incrementation and checking for previously seen pairs.

• cnt[(0, 1)] becomes 1, cnt[(0, 2)] is incremented to 2 (since we already have one from the first row), and cnt[(1, 2)] becomes 1.

Solution Implementation **Python**

from collections import Counter

if cell first:

class Solution:

pair counter = Counter() # Counter to track pairs of columns that have a 1 at the same row num_cols = len(grid[0]) # The number of columns in the grid # Iterate through each row in the grid for row in grid:

If both columns have a 1 at the current row, this forms a potential rectangle corner

Increase the count for this column pair as we found another rectangle corner

rectangle count += pair counter[(col index first, col index second)]

3. `num cols`: Introduced this variable as a clearer name for the number of columns in the grid (`n` in the original code).

Update the counter for the current pair, adding one more occurrence

Make sure to replace `List` by the correct import statement from 'typing' at the beginning of the file: ```python from typing import List

import java.util.HashMap;

import iava.util.List;

import java.util.Map;

class Solution {

C++

return rectangle_count

Changes and comments explanation:

Java

2. `pair counter`: Renamed `cnt` to `pair counter` which is a Counter object to keep track of pairs of columns that make the corners

4. `col index first` and `cell first`: Renamed `i` and `c1` for clarity in the enumeration of the first column index and cell value.

6. Standard imports: Included the import statement for the 'Counter' class from the 'collections' module explicitly, which allows for

```
List<Integer> pair = List.of(leftCol, rightCol);
// Increment the count of found rectangles with these 1's as the top corners.
cornerRectanglesCount += pairsCount.getOrDefault(pair, 0);
// Increment the count of this pair in our map.
pairsCount.merge(pair, 1, Integer::sum);
```

for (int rightCol = leftCol + 1; rightCol < numCols; ++rightCol) {</pre>

// Only if the paired cell is also a 1, do we consider it.

// Create a pair to check in our current map.

```
#include <vector>
#include <map>
using namespace std;
class Solution {
public:
   int countCornerRectangles(vector<vector<int>>& grid) {
        // n represents the number of columns in the grid
        int num columns = grid[0].size();
        // Initialize the answer to 0
        int answer = 0;
        // Define a map to store the count of pairs of columns that form the vertical sides of potential rectangles
        map<pair<int, int>, int> column_pairs_count;
        // Iterate through each row of the grid
        for (const auto& row : grid) {
            // Check each pair of columns within the row
            for (int i = 0; i < num columns; ++i) {
                // If the current cell contains a 1, search for a potential second column to form a rectangle
                if (row[i]) {
                    for (int j = i + 1; j < num columns; ++j) {</pre>
                        // If we find a pair of 1s, this could form the corner of a rectangle
                        if (row[i]) {
                            // Increase the answer by the count of rectangles that can be formed using this column pair
                            answer += column pairs count[{i, j}];
                            // Increment the count for this column pair
                            ++column_pairs_count[{i, j}];
        // Return the total count of corner rectangles
```

```
# Enumerate over the row to get both column index and value
for col index first, cell first in enumerate(row):
```

row.

class Solution:

```python from typing import List Time and Space Complexity **Time Complexity** 

The given code's time complexity primarily comes from the nested loops that it uses to iterate over each pair of columns for each

• Inside this loop, the second loop (for i, c1 in enumerate(row)) iterates over each element in the row, which occurs n times where n is the

Considering the iterations of the third nested loop, the number of column pairs (i, j) that will be considered for each row

The space complexity is determined by the storage used by the cnt Counter, which keeps track of the frequency of each pair of

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3. `num cols`: Introduced this variable as a clearer name for the number of columns in the grid (`n` in the original code).

# If both columns have a 1 at the current row, this forms a potential rectangle corner

# Increase the count for this column pair as we found another rectangle corner

rectangle count += pair counter[(col index first, col index second)]

# Update the counter for the current pair, adding one more occurrence

### number of columns. • The innermost loop (for j in range(i + 1, n)) iterates from the current column i to the last column, with the average number of iterations being roughly n/2 since it's a triangular iteration overall.

Therefore, the time complexity is 0(m \* nC2) or 0(m \* n \* (n - 1) / 2), which simplifies to  $0(m * n^2)$ . **Space Complexity** 

follows the pattern of a combination of selecting two out of n columns or nC2.

column pairs would be the same nC2 we calculated before, or n \* (n - 1) / 2 pairs.

• The first loop (for row in grid) goes through each row in the grid, which occurs m times where m is the number of rows.

- columns that have been seen with '1' at both the ith and jth positions. • In the worst case scenario, the cnt Counter would have an entry for every possible pair of columns. As there are n columns, the number of
- Therefore, the space complexity for the cnt Counter is 0(n^2). Thus, the overall space complexity is  $0(n^2)$  since the Counter's size is the dominant term, and this space is additional to the input (grid) since the grid itself is not being modified.