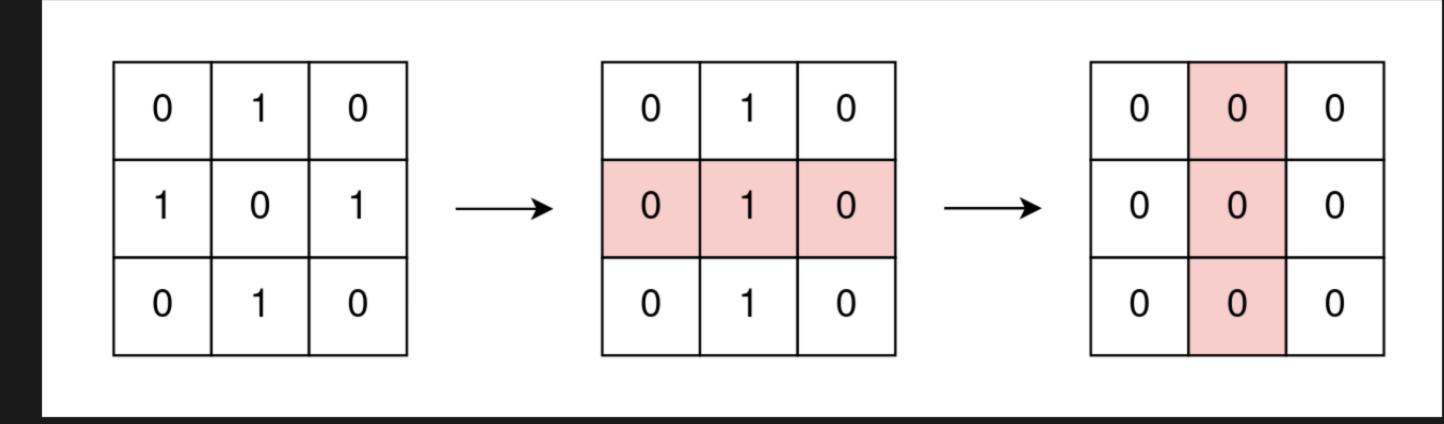
# 2128. Remove All Ones With Row and Column Flips

You are given an  $m \times n$  binary matrix grid.

In one operation, you can choose **any** row or column and flip each value in that row or colum (i.e., changing all 0's to 1's, and all 1's to 0's).

Return true if it is possible to remove all 1's from grid using any number of operations or false otherwise.

## Example 1:



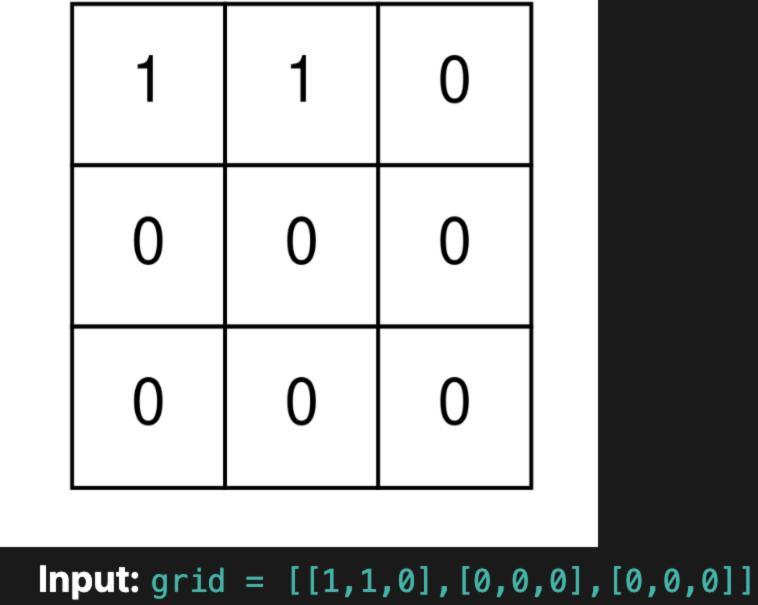
Input: grid = [[0,1,0],[1,0,1],[0,1,0]]

Output: true

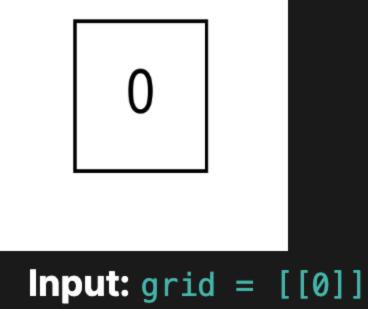
Explanation: One possible way to remove all 1's from grid is to:

- Flip the middle row
- Flip the middle column

Example 2:



**Output:** false **Explanation:** It is impossible to remove all 1's from grid.



Output: true

**Explanation:** There are no 1's in grid.

**Constraints:** • m == grid.length

- n == grid[i].length • 1 <= m, n <= 300 • grid[i][j] is either 0 or 1.
- Solution

## The first observation we can make is that for every row/column, we will either flip that row/column once or zero times. This is

With this in mind, for each row and column, we can either choose to flip it or not flip it. If we brute force every combination, we will take O(MN) to simulate each combination. Since there are  $O(2^{M+N})$  combinations, this gives us a time complexity of

 $O(2^{M+N} imes MN)$ . Let's look for a faster solution as this is way too slow. Let's call grid reachable if it's possible to apply some row/column flips to remove all 0's. We can observe that if each row/column is flipped at most once, there is only one set of rows and columns that can be flipped to

To check whether or not grid is reachable, we'll first flip all necessary columns, and then the necessary rows.

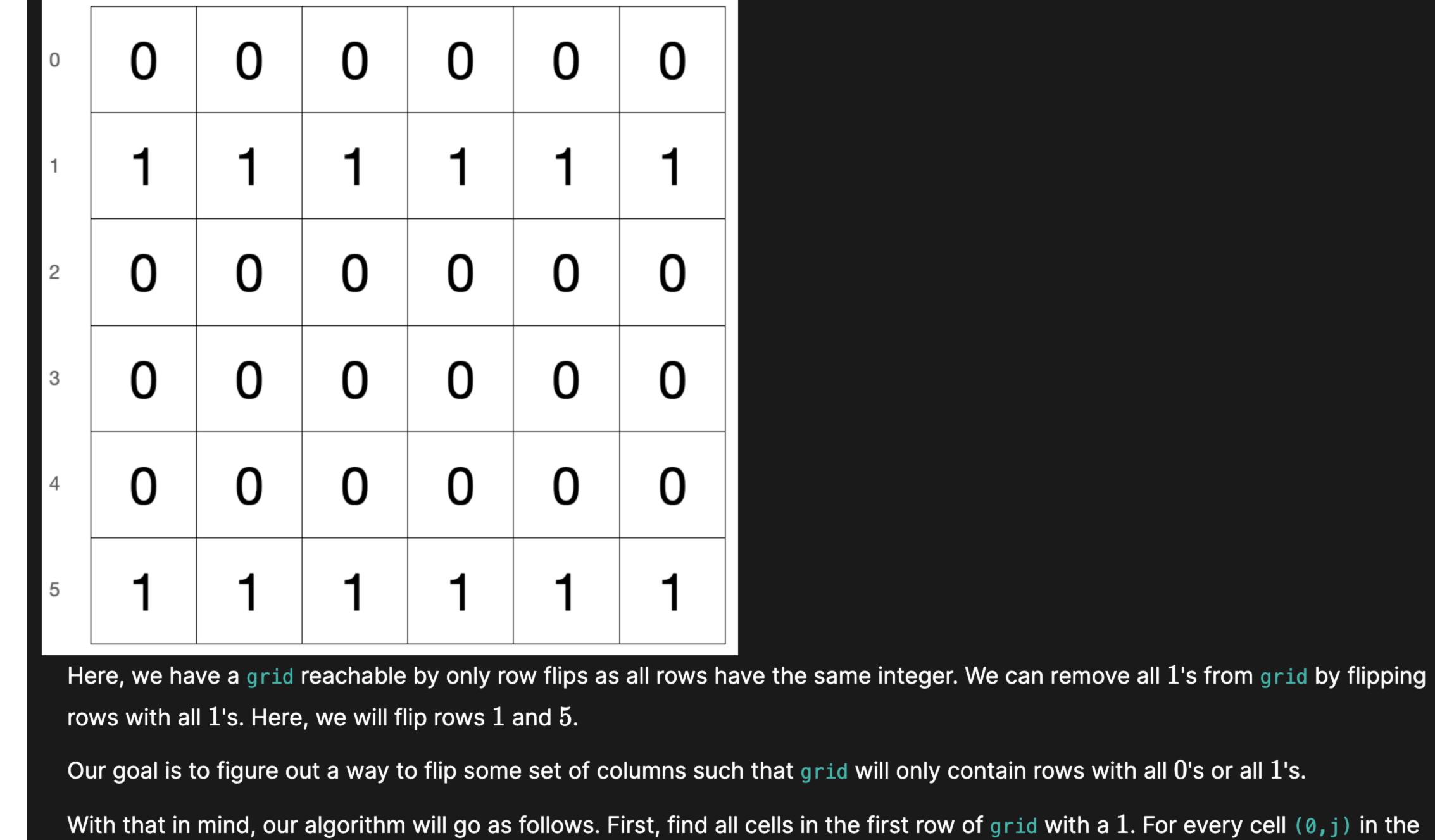
set all cells to 0 (assuming a solution exists). Let's call these necessary rows and columns.

because if we flip a row/column twice, it will have no effect on the grid.

flips if all rows have the same integer (i.e. all 0's or all 1's).

Let's first assume that we already flipped all necessary columns on grid. We can observe that grid is now reachable by only row

**Example** 



flips take O(M) to simulate, our total time complexity is O(NM).

Since we don't actually use additional arrays or lists, our space complexity is O(1).

for (int j = 0; j < m; j++) { // flips a column

grid[j][i] = 1 - grid[j][i];

for (int i = 0; i < n; i++) { // flip columns so that first row only has 0's

first row that's a 1, let's flip the  $j^{th}$  column so that the cell (0, j) becomes a 0. This is important as it causes the first row to have all 0's. At this point there are two cases to consider.

The first case is that the rest of the rows have all 0's or all 1's. In this case, we can conclude that grid is reachable and we'll

The second case is that there exists a row that has a mix of 0's and 1's, which we don't want. In this case, we'll return false since we can observe that it's impossible to get all rows to have all 0's or all 1's. This is because if we try to change the other rows to have all 0's or 1's with more column flips, the content of the first row will change and it will no longer have all 0's.

**Time Complexity** 

return true.

**Space Complexity** 

In the worst scenario, we will perform O(M) row flips and O(N) column flips. Since row flips take O(N) to simulate and column

class Solution { public: bool removeOnes(vector<vector<int>>& grid) { int m = grid.size(); // get dimensions of grid

int n = grid[0].size();

if (grid[0][i] == 1) {

Space Complexity: O(1).

Time Complexity: O(NM).

```
bool ans = true;
        for (int i = 0; i < m; i++) { // checks if each row has all 0's or all 1's
            int sum = 0;
            for (int j = 0; j < n; j++) {
                sum += grid[i][j];
            if (sum == 0 || sum == n) {
                continue;
            ans = false;
        return ans;
};
class Solution {
    public boolean removeOnes(int[][] grid) {
        int m = grid.length; // get dimensions of grid
        int n = grid[0].length;
        for (int i = 0; i < n; i++) { // flip columns so that first row only has 0's
            if (grid[0][i] == 1) {
                for (int j = 0; j < m; j++) { // flips a column</pre>
                    grid[j][i] = 1 - grid[j][i];
        boolean ans = true;
        for (int i = 0; i < m; i++) { // checks if each row has all 0's or all 1's
            int sum = 0;
            for (int j = 0; j < n; j++) {
                sum += grid[i][j];
```

```
if (sum == 0 || sum == n) {
               continue;
           ans = false;
        return ans;
class Solution:
   def removeOnes(self, grid: List[List[int]]) -> bool:
        m = len(grid) # get dimensions of grid
        n = len(grid[0])
        for i in range(n): # flip columns so that first row only has 0's
            if grid[0][i] == 1:
                for j in range(m): # flips a column
                   grid[j][i] = 1 - grid[j][i]
        ans = True
        for i in range(m): # checks if each row has all 0's or all 1's
            sum = 0
            for j in range(n):
                sum += grid[i][j]
           if sum == 0 or sum == n:
                continue
```

ans = False

return ans