Problem Description

Medium Tree

where for every node, the left children are less than the current node, and the right children are greater. The problem can be broken into two main parts:

This problem involves modifying a Binary Search Tree (BST) by deleting a specific node with a given key. The BST has a property

- 1. Locating the node that should be removed.
- The complication in deletion comes from ensuring that the BST property is maintained after the node is removed. This means correctly rearranging the remaining nodes so that the tree remains a valid BST.

2. Once the node is found, executing the removal process.

Binary Search Tree

Intuition

The solution follows the property of BST. If the key to be deleted is less than the root node's key, then it lies in the left subtree. If the

the node to be deleted. For the deletion, there are three scenarios: 1. Node with only one child or no child: If the node to be deleted has one or no children, we can simply replace the node with its

key to be deleted is greater than the root's key, then it lies in the right subtree. If the key is equal to the root's key, then the root is

2. Node with two children: Find the inorder successor (smallest in the right subtree or largest in the left subtree) of the node. Copy the inorder successor's content to the node and delete the inorder successor. This is because inorder successors are always a

child (if any) or set it to None.

- leaf or have a single child, making them easier to remove. 3. Leaf node: If the node is a leaf and needs to be deleted, we can simply remove the node from the tree.
- The given solution first finds the node to delete, then based on its children, replaces the node accordingly. When a node with two children is deleted, instead of searching for the inorder predecessor, the algorithm finds the inorder successor, which is the smallest
- node in the right subtree, and swaps the values. Then the algorithm recursively deletes the successor node. **Solution Approach**

The solution to the delete operation in a BST uses recursion to simplify the deletion process. Let's walk through the implementation approach: 1. Base Case: If the root is None, there is nothing to delete, so we return None.

values to the right).

self.deleteNode(root.right, key) Here, the algorithm is using recursion to traverse the tree in a BST property-aware manner (lesser values to the left, greater

self.deleteNode(root.left, key) If the key is greater than the root's value, we need to go to the right subtree: root.right =

2. Searching Phase: If the key is less than the root's value, we need to go to the left subtree: root.left =

- 3. Node Found: Once we find the node with the value equal to the key (i.e., root.val == key), we need to delete this node while keeping the tree structure.
- a. Node with One or No Child: If the node to be deleted has either no children (root.left is None and root.right is None) or one child, it can be deleted by replacing it with its non-null child or with None.
- b. Node with Two Children: If the node to be deleted has two children, we need to find the inorder successor of the node, which is the smallest node in the right subtree. We do this by traversing to the leftmost child in the right subtree.

Once the inorder successor is found, we replace the node's value with the successor's value. In the code, this is accomplished

- the structure of the recursion). This intuitive approach of handling different cases separately and utilizing the BST property ensures that the updated tree maintains

Let's use a small example to illustrate the solution approach. Consider the following BST where we want to delete the node with key

1. Base Case: The root is not None, so we proceed with the operation. 2. Searching Phase: The key 7 is greater than the root's value 5, so we examine the right subtree:

3. Node Found: As the node's key matches, we proceed with deletion.

The BST properties are maintained, and 7 has been successfully removed.

Since 7 is lesser than 8, we now go to the left subtree of node 8, where we find our node with the value 7.

def __init__(self, val=0, left=None, right=None): self.val = val self.left = left self.right = right

If the key to be deleted is smaller than the root's key,

If the key to be deleted is greater than the root's key,

// Function to delete a node with a given key from a binary search tree

// If the key is smaller than root's value, delete in the left subtree

// If the key is greater than root's value, delete in the right subtree

// If the root has no left child, return the right child directly

// If the root has no right child, return the left child directly

public TreeNode deleteNode(TreeNode root, int key) {

if (root == null) {

return null;

if (root.val > key) {

return root;

if (root.val < key) {</pre>

return root;

if (root.left == null) {

return root.right;

if (root.right == null) {

return root.left;

root = root.right;

return root;

// Return the modified tree

TreeNode successor = root.right;

while (successor.left != null) {

// Base case: if the root is null, return null

root.left = deleteNode(root.left, key);

root.right = deleteNode(root.right, key);

// If the root itself is the node to be deleted

// If the root has both left and right children

// Find the successor (smallest in the right subtree)

root.left = self.deleteNode(root.left, key)

root.right = self.deleteNode(root.right, key)

def deleteNode(self, root: Optional[TreeNode], key: int) -> Optional[TreeNode]:

If the root is None, then there is nothing to delete, return None

removed from the tree. This means the left child of the node 8 will be set to None.

b. **Node with Two Children**: This does not apply here since our node 7 is a leaf.

Finally, the updated BST looks like this after deleting node 7:

24 return root 25 26 # If the key is the same as root's key, then this is the node to be deleted 27 28 # If the node has only one child or no child if root.left is None:

```
# If the node has two children, get the inorder successor
           # (smallest in the right subtree)
37
           min_right_subtree = root.right
           while min_right_subtree.left:
               min_right_subtree = min_right_subtree.left
           # Copy the inorder successor's content to this node
           root.val = min_right_subtree.val
           # Delete the inorder successor
           root.right = self.deleteNode(root.right, min_right_subtree.val)
           return root
Java Solution
1 // Definition for a binary tree node.
2 class TreeNode {
       int val;
       TreeNode left;
       TreeNode right;
       // Constructor with no arguments
       TreeNode() {}
9
       // Constructor with value only
       TreeNode(int val) { this.val = val; }
       // Constructor with value, left, and right child nodes
       TreeNode(int val, TreeNode left, TreeNode right) {
           this.val = val;
           this.left = left;
           this.right = right;
   class Solution {
```

successor = successor.left; 60 61 62 // Move the left subtree of the root to the left of the successor 63 successor.left = root.left; 64 // The new root should be the right child of the deleted node

```
C++ Solution
  1 /**
     * Definition for a binary tree node.
      */
    struct TreeNode {
         int val;
        TreeNode *left;
         TreeNode *right;
         TreeNode() : val(0), left(nullptr), right(nullptr) {}
         TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
         TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}
 10
 11 };
 12
    class Solution {
    public:
 14
         TreeNode* deleteNode(TreeNode* root, int key) {
 15
             // If root is null, return immediately
 16
 17
             if (!root) {
 18
                 return root;
 19
 20
             // If the key to be deleted is smaller than the root's value,
 21
 22
             // then it lies in left subtree
 23
             if (root->val > key) {
 24
                 root->left = deleteNode(root->left, key);
 25
                 return root;
 26
 27
             // If the key to be deleted is greater than the root's value,
 28
 29
             // then it lies in right subtree
             if (root->val < key) {</pre>
 30
 31
                 root->right = deleteNode(root->right, key);
 32
                 return root;
 33
 34
 35
             // If key is the same as root's value, then this is the node
 36
             // to be deleted
 37
             // Node with only one child or no child
 38
             if (!root->left) {
 39
                 return root->right;
 40
 41
 42
             if (!root->right) {
 43
                 return root->left;
 44
 45
 46
             // Node with two children: Get the inorder successor (smallest
             // in the right subtree)
 47
             TreeNode* successorNode = root->right;
             while (successorNode->left) {
                 successorNode = successorNode->left;
 50
 51
 52
 53
             // Copy the inorder successor's content to this node
 54
             root->val = successorNode->val;
 55
 56
             // Delete the inorder successor since its value is now copied
 57
             root->right = deleteNode(root->right, successorNode->val);
 58
 59
             return root;
 60
 61 };
 62
```

if (root.val > key) { 24 25 26 27

if (root === null) {

return root;

Typescript Solution

interface TreeNode {

left: TreeNode | null;

right: TreeNode | null;

val: number;

* Definition for a binary tree node.

* Deletes a node with the specified key from the binary search tree.

* @param {number} key - The value of the node to be deleted.

// If the root is null, return null (base case).

* @param {TreeNode | null} root - The root of the binary search tree.

function deleteNode(root: TreeNode | null, key: number): TreeNode | null {

* @returns {TreeNode | null} - The root of the binary search tree after deletion.

```
21
22
     // Check if the key to delete is smaller or greater than the root's value to traverse the tree.
23
         // The key to be deleted is in the left subtree.
         root.left = deleteNode(root.left, key);
     } else if (root.val < key) {</pre>
         // The key to be deleted is in the right subtree.
28
         root.right = deleteNode(root.right, key);
29
     } else {
         // When the node to be deleted is found
30
         if (root.left === null && root.right === null) {
31
32
             // Case 1: Node has no children (it is a leaf), simply remove it.
33
             root = null;
         } else if (root.left === null || root.right === null) {
34
35
             // Case 2: Node has one child, replace the node with its child.
36
             root = root.left || root.right;
37
         } else {
38
             // Case 3: Node has two children.
39
             if (root.right.left === null) {
                 // If the immediate right child has no left child, promote the right child.
40
                 root.right.left = root.left;
41
                 root = root.right;
42
             } else {
43
44
                 // If the right child has a left child, find the in-order predecessor.
                 let minPredecessorNode = root.right;
45
                 while (minPredecessorNode.left && minPredecessorNode.left.left !== null) {
46
                     minPredecessorNode = minPredecessorNode.left;
47
48
                 // Replace the root's value with the in-order predecessor's value.
49
                 const minValue = minPredecessorNode.left.val;
50
51
                 root.val = minValue;
52
                 // Delete the in-order predecessor.
53
                 minPredecessorNode.left = deleteNode(minPredecessorNode.left, minValue);
54
55
56
57
58
     // Return the updated root.
59
     return root;
60 }
61
Time and Space Complexity
Time Complexity
The time complexity of the given code for deleting a node from a BST (Binary Search Tree) depends on the height of the tree h.
  1. Finding the node to delete takes 0(h) time since in the worst case, we might have to traverse from the root to the leaf.
 2. The deletion process itself is 0(1) for nodes with either no child or a single child.
 3. For nodes with two children, we find the minimum element in the right subtree, which also takes 0(h) time in the worst case
```

Therefore, the overall time complexity is O(h), which would be O(log n) for a balanced BST and O(n) for a skewed BST (where n is the number of nodes).

(when the tree is skewed).

Space Complexity The space complexity of the code is determined by the maximum amount of space used at any one time during the recursive calls

- 2. There are no additional data structures used that grow with the input size. The space complexity is therefore O(h), which corresponds to O(log n) for a balanced BST and O(n) for a skewed BST due to the
- recursive function calls.

If the left child is None, it means the node either has a right child or no child at all. Hence, we return root.right. If the right child is None, it means the node has a left child only, so we return root.left.

its BST properties after the deletion is performed.

Example Walkthrough

Following the solution approach:

- by swapping the root node with its right child first and then attaching the original left subtree to the new root. Finally, we delete the inorder successor node which has been moved to the root position by calling delete on the right subtree: root.right = self.deleteNode(root.right, successor.val) (not explicitly shown in the given reference code but implied by
- a. Node with One or No Child: Node 7 is a leaf node in this scenario (no children). According to the third case, it can be simply
- **Python Solution**

class TreeNode:

class Solution:

if root is None:

return None

if key < root.val:</pre>

return root

if key > root.val:

return root.right

return root.left

if root.right is None:

then it lies in the left subtree

then it lies in the right subtree

10

13

- 29 30 31 32 33 34 35 36
- 38 39 40 41 42 43 44 45 46 47 48
- 10 11 12
- 13 14 15 16 18 19 }
- 20 22 23
- 24 25 26 27 28 29 30
- 31 32 33 34 35
- 36 37 38 39 40 41 42 43
- 44
- 48 49
- 52
- 54
- 55 56
- 57 58

- 65

67

68

69

70

72

71 }

- 59

- 8 9 10 15

18

20

1 /**

*/

/**

*/

- (the call stack size). 1. The maximum depth of recursive calls is equal to the height h of the tree.