## **Problem Description**

n. A valid pair (i, j) must satisfy two conditions: i < j (meaning the first index must be less than the second one), and nums1[i] + nums1[j] > nums2[i] + nums2[j] (meaning the sum of nums1 elements at these indices is greater than the sum of nums2 elements at the same indices). We need to count how many such pairs exist. The task is, given the two arrays nums1 and nums2, to return the total count of pairs (i, j) that meet these conditions.

The problem is to determine the number of specific pairs of indices in two arrays, nums1 and nums2. Both arrays have the same length

Intuition

### To solve this problem, we leverage the fact that if we fix one index and sort all the potential pair values, we can then use binary

1. First, compute the difference between the elements at the same indices in nums1 and nums2 and store these differences in a new array d. This transformation simplifies the problem, as we're now looking for indices where d[i] + d[j] > 0.

search to efficiently find how many values meet our condition for each fixed index. Here's a step-by-step explanation of the solution:

- 2. Sort the array d in non-decreasing order. Sorting enables us to use binary search to efficiently find indices satisfying our condition.
- 3. For each element d[i] in d, we want to find the count of elements d[j] such that j > i and d[i] + d[j] > 0. We can rewrite this
- condition to d[j] > -d[i]. Using binary search on the sorted array d, we look for the right-most position to which -d[i] could be inserted while maintaining the sorted order. This gives us the index beyond which all elements of d[j] would result in d[i] + d[j] > 0.

4. The bisect\_right function from Python's bisect module is used for this purpose. For each i, it returns the index beyond which -

- 5. The count of valid j for each i is the number of elements in d beyond the index found in step 4, which is simply n (index found by bisect\_right).
- 6. The total count of valid pairs is obtained by summing the count from step 5 for each i. Using this method, we reduce a potentially O(n^2) problem (checking each pair directly) to O(n log n) due to sorting and binary
- **Solution Approach**

1. Difference Calculation and Store in Array d: The first step is to calculate the difference array d, where each element d[i] is the difference between nums1[i] and nums2[i] for i from 0 to n-1. This subtraction is done using a list comprehension, which is a

The implemented solution follows these steps, using a mix of algorithmic techniques and Python-specific functionalities:

## 1 d = [nums1[i] - nums2[i] for i in range(n)]

ensuring that j > i.

concise way to create lists in Python.

search for each element.

d[i] would go in the sorted array.

2. Sorting the Array d: The array d is then sorted in non-decreasing order. This sorting is crucial as it prepares the array for a binary search operation. The sorted property of d allows us to apply the bisect algorithm effectively.

module to find the insertion point for -d[i] into d such that the array remains sorted.

1 sum(n - bisect\_right(d, -v, lo=i + 1) for i, v in enumerate(d))

• Transformation: to simplify the original condition to a more manageable form.

1 d.sort() 3. Using Binary Search to Find Count of Valid Pairs: For each element in d, we use the bisect\_right function from the bisect

The function bisect\_right is a binary search algorithm that returns the index in the sorted list d, where the value -d[i] should

be inserted to maintain the sorted order. The lo parameter signifies the start position for the search which in this case is i + 1,

The subtraction from n gives us the number of elements larger than -d[i], effectively counting how many j indices will satisfy the condition d[i] + d[j] > 0.

elements from nums1 at these indices is greater than the sum of the elements from nums2 at the same indices, which corresponds to the condition d[i] + d[j] > 0 post-transformation. This solution uses a combination of algorithmic concepts:

4. Summing the Counts for Each 1: The sum operation in the final line adds up the valid pairs count for each value of 1. It iterates

over the sorted array d and for each element calculates the number of valid pairs (i, j) where i < j and the sum of the original

• Binary Search: to reduce the search space for the pairs from O(n) to O(log n), greatly enhancing the overall algorithm efficiency. • Prefix Sum: implicit in the adding up of counts for each index, effectively reducing the number of direct comparisons needed. Returning the sum at the end gives us the desired count of pairs that fulfill the problem's conditions efficiently.

Let's use a small example with the arrays nums1 = [3, -1, 7] and nums2 = [4, 0, 5] to illustrate the solution approach step-by-

step. The length of both arrays, n, is 3. Our goal is to find the count of valid pairs (i, j) for which i < j and nums1[i] + nums1[j] > 1

nums2[i] + nums2[j].

First, find the difference between corresponding elements of nums1 and nums2:

Sorting: to prepare data for efficient searching.

### • d[2] = nums1[2] - nums2[2] = 7 - 5 = 2

Step 2: Sort the array d

Python Solution

class Solution:

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C++ Solution

1 class Solution {

public:

order.

Example Walkthrough

Step 1: Calculate difference array d

• d[0] = nums1[0] - nums2[0] = 3 - 4 = -1

• d[1] = nums1[1] - nums2[1] = -1 - 0 = -1

Step 4: Calculate the valid j indices and sum them up

• For i = 0: The count of valid j indices is n - 3 = 3 - 3 = 0.

• For i = 1: The count of valid j indices is n - 3 = 3 - 3 = 0.

So the difference array d is [-1, -1, 2].

We sort the array d to get [-1, -1, 2]. In this small case, sorting does not change the order, as the list is already in non-decreasing

• For i = 0 (d[0] = -1): We search for where 1 can be inserted after index 0. bisect\_right([-1, -1, 2], 1, lo=0 + 1) = 3.

Step 3: Use binary search for each i We use bisect\_right to find where -d[i] can be inserted:

• For i = 1 (d[1] = -1): We search for where 1 can be inserted after index 1. bisect\_right([-1, -1, 2], 1, lo=1 + 1) = 3. We do not search for i = 2 because it's the last element, and no j can satisfy i < j.</li>

The total count of valid pairs (i, j) is the sum of the counts above: 0 + 0 = 0.

def countPairs(self, nums1: List[int], nums2: List[int]) -> int:

# Calculate the difference between the two lists element-wise

differences = [nums1[i] - nums2[i] for i in range(length)]

# Sort the differences to prepare for binary search

- Therefore, for the given arrays nums1 and nums2, there are no valid pairs (i, j) that meet the condition nums1[i] + nums1[j] > nums2[i] + nums2[j].
- 1 from typing import List 2 from bisect import bisect\_right

# Subtract this position from the total number of elements that

count += length - bisect\_right(differences, -value, lo=i + 1)

// Add the count of valid pairs for this position to the answer

// Create a difference vector to store differences of nums1[i] - nums2[i]

int j = upper\_bound(diff.begin() + i + 1, diff.end(), -diff[i]) - diff.begin();

// Increment the result by the number of valid pairs with the current element at index i

# can be paired with the current element, which is (length -i - 1).

# We use `lo=i+1` because we shouldn't pair an element with itself.

### for i, value in enumerate(differences): 16 # For each element, find the number of elements in the sorted 17 18 # list that would create a negative sum with the current element. 19 # The `bisect\_right` function is used to find the position to 20 # insert `-value` which gives the number of such elements.

answer += n - left;

return answer;

// Return the total number of valid pairs

// Get the size of the input vectors

// Populate the difference vector

for (int i = 0; i < size; ++i) {

sort(diff.begin(), diff.end());

diff[i] = nums1[i] - nums2[i];

int size = nums1.size();

vector<int> diff(size);

long long result = 0;

result += size - j;

return result;

// Return the computed number of valid pairs

long long countPairs(vector<int>& nums1, vector<int>& nums2) {

// Sort the difference vector in non-decreasing order

// Initialize result variable to store the final count of pairs

# Initialize count of pairs to 0

# Loop through the sorted differences list

# Return the total count of valid pairs

# Length of the input lists

length = len(nums1)

differences.sort()

count = 0

return count

Java Solution

```
class Solution {
       public long countPairs(int[] nums1, int[] nums2) {
           // Get the length of the arrays
           int n = nums1.length;
           // Create a new array to store the differences between nums1 and nums2
            int[] differences = new int[n];
            for (int i = 0; i < n; ++i) {
               differences[i] = nums1[i] - nums2[i];
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           // Sort the array of differences
13
           Arrays.sort(differences);
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           // Initialize answer to count the valid pairs
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            long answer = 0;
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           // Iterate over each element in the differences array
           for (int i = 0; i < n; ++i) {
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               // Use binary search to find the number of valid pairs
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               int left = i + 1, right = n;
               while (left < right) {</pre>
                    int mid = (left + right) / 2;
                   // Check if this position contributes to a valid pair
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                    if (differences[mid] > -differences[i]) {
26
                        right = mid;
                    } else {
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                        left = mid + 1;
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```

### 20 21 // Iterate through each element in the difference vector 22 for (int i = 0; i < size; ++i) { 23 // Find the index of the first element that is greater than -diff[i] 24 // This is done to ensure that for any pair (i, j), diff[i] + diff[j] > 0

```
Typescript Solution
1 function countPairs(nums1: number[], nums2: number[]): bigint {
       // Get the size of the input arrays
       const size: number = nums1.length;
       // Create a difference array to store differences of nums1[i] - nums2[i]
       let diff: number[] = new Array<number>(size);
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       // Populate the difference array
       for (let i = 0; i < size; i++) {
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           diff[i] = nums1[i] - nums2[i];
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       // Sort the difference array in non-decreasing order (ascending)
       diff.sort((a, b) => a - b);
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       // Initialize result variable to store the final count of pairs
16
       let result: bigint = BigInt(0);
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       // Iterate through each element in the difference array
20
       for (let i = 0; i < size; i++) {
21
           // Find the index of the first element that is strictly greater than -diff[i]
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           // This is done to ensure that for any pair (i, j), diff[i] + diff[j] > 0
23
           let j: number = findUpperBound(diff, i + 1, size, -diff[i]);
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           // Increment the result by the number of valid pairs with the current element at index i
26
           result += BigInt(size - j);
27
28
29
       // Return the computed number of valid pairs
       return result;
30
31 }
32
   function findUpperBound(arr: number[], start: number, end: number, value: number): number {
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       // Binary search for the first element in the sorted array that is strictly greater than the given value
       let low: number = start;
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       let high: number = end;
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37
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       while (low < high) {</pre>
39
           const mid: number = low + Math.floor((high - low) / 2);
           if (arr[mid] <= value) {</pre>
40
               low = mid + 1;
```

# Time and Space Complexity

high = mid;

return low;

**Time Complexity** 

**Space Complexity** 

## 1. Create a difference list d by subtracting nums2 from nums1. This step is 0(n) where n is the length of the input lists.

The space complexity is evaluated as follows:

2. Sort the difference list d. Sorting algorithms generally have a time complexity of O(n log n). 3. For each element in d, perform a binary search using bisect\_right. Since we perform a binary search (0(log n)) for each element in the list, this step has a time complexity of  $O(n \log n)$ .

algorithms, like Timsort (used by Python's sort method), use O(log n) space.

The time complexity of the code can be broken down into several steps:

Adding these up, the overall time complexity is dominated by the sorting and binary search steps, which leads to 0(n log n).

// Return the index where the value would be inserted (first index greater than the value)

- 1. We are creating a difference list d of size n, therefore requiring O(n) additional space. 2. Sorting the list in-place (as Python's sort does) has a space complexity of O(log n), as typical implementations of sorting
- 3. The binary search itself does not use additional space (aside from a few pointers), so the space used remains 0(log n). As the additional space required for the difference list is the largest contributor, the overall space complexity is O(n).