Problem Description

indices you can visit starting from any index in the array. From a given index i, you can jump to an index i + x or i - x under two conditions: The value of x is between 1 and d, and the jump does not take you outside the bounds of the array.

The problem presents an array of integers called arr alongside an integer d. You are tasked with finding the maximum number of

2. You can only make the jump if the number at the starting index arr[i] is greater than arr[j], where j is the index you want to jump to, and arr[i] is also greater than all the numbers between indices i and j.

number of jumps that can be made from each index. The process can be visualized as follows:

encounter considerable overlap and repeated calculation of the same scenarios.

arr[i]. If both conditions are met, it means a jump from i to j is valid.

maximum number of indices we can visit starting from the best possible index.

You must navigate through the array by following these rules, with the goal being to maximize the number of indices visited.

Intuition

The intuition for solving this problem hinges on dynamic programming, which keeps track of the optimal sub-structure: the maximum

1. We understand that each index is a potential starting point, and from each index, we need to consider jumps in both directions within the allowed range.

- 2. If we are at index i, to determine the optimal number of jumps (f[i]) from that index, we need to look at all indices j we could jump to within the specified d range. If a jump to j is permissible, we update f[i] to be a maximum between its current value and
- f[j] + 1 which accounts for the jump just made. 3. Since we need to ensure we are always jumping to a lower value, we sort the indices of the array based on the values at those indices. This ensures that when we are considering jumps from a particular index i, we have already computed the optimal
- jumps from lower valued indices. 4. In this manner, we build up an array f where f[1] represents the maximum number of indices that can be visited starting from index i. The end goal is to return the maximum value from this f array, representing the maximum number of indices visited from
- By building up a table of optimal solutions to sub-problems (f array) and using the sorted values to iterate in a controlled manner, we can use dynamic programming to compute the solution in an efficient way, without re-computing results. This makes the program more efficient compared to brute-force approaches, which would try to make a jump from every index in an uncontrolled manner and

Solution Approach The solution for this problem involves a dynamic programming approach. We create a table f where each index 1 has an initial value of 1, representing the minimum number of indices that can be visited (the index itself). We'll walk through the implementation

The problem is framed as a dynamic programming one, which commonly involves filling out a table or array of values. In this case, we're filling out the array f with the maximum number of indices that can be visited starting from each index.

approach step by step:

the best starting location.

 Initially, all entries in f are set to 1, but as we explore jumps from each index, these entries may increase. • We sort a list of pairs, where each pair consists of the value at each index arr[1] and the index itself 1. This ensures we always work from lower to higher values, respecting the jump rule that you can only jump to a smaller value.

- We iterate over the sorted list, and for each index i, we examine the possible indices we can jump to within the range d in both directions (to the left and to the right).
- For each possible jump from i to j, we check two conditions: whether the jump is within the distance d, and if arr[j] is less than

distance. This ensures that f[i] represents the optimal (maximum) number of indices visited starting from i.

visited from j plus the jump just made from i to j. This updating of f[i] happens for all j within the jumpable range from i that match the criteria of lower value and within the d

Upon finding a valid jump, we update f[i] to be the maximum of its current value and f[j] + 1, reflecting the number of indices

the optimal number of indices that can be visited from all lower values; this property of the solution eliminates unnecessary recalculations and ensures the solution is efficient.

• After we finish updating f[i] for all indices, the last step is to return max(f), the maximum value within f, which represents the

Since f has been filled from the lowest value of arr[i] upwards, by the time we reach higher values, we've already calculated

- This process structurally follows a bottom-up dynamic programming approach, going from smaller sub-problems to larger subproblems and using previous results to construct an optimal final answer.
- Following the solution approach:

f = [1, 1, 1, 1, 1]2. We create a list of pairs to sort by value in arr: [(6, 0), (4, 1), (14, 2), (6, 3), (8, 4)].

Starting with the pair (4, 1). There are no indices with smaller values than 4 within the range d, so we skip to the next pair.

For the pair (6, 0), we can jump to index 1 which has the value 4 (and is within d distance). We update f[0] to be the

1. We create our table f with the same length as arr and initialize all values to 1, because each index can visit at least itself.

Example Walkthrough

4. We proceed to iterate through our sorted list and consider jumps.

maximum of f[0] and f[1] + 1, so:

Let's assume we have an array arr = [6, 4, 14, 6, 8] and d = 2.

f = [2, 1, 1, 1, 1]Considering pair (6, 3), we can jump to index 1 and index 4. We update f[3] to be the maximum of f[3] and f[1] + 1, and

3. After sorting by the first element in the pairs: [(4, 1), (6, 0), (6, 3), (8, 4), (14, 2)].

- f = [2, 1, 1, 2, 1] With pair (8, 4), we examine the indices within range d (indices 2 and 3), but we can only jump to index 3, updating f[4]:
 - Lastly, the pair (14, 2). This value lets us jump to any lower index within d (0, 1, 3, and 4). We update f[2] for each of these: f = [2, 1, 4, 2, 3]

get the answer, we just take the maximum value in f:

def maxJumps(self, arr: List[int], max_distance: int) -> int:

Determine the total number of elements in the array

f = [2, 1, 1, 2, 3]

f[3] and f[4] + 1:

5. Now we have our completed f table indicating the maximum number of indices that can be visited starting from each index. To

So the maximum number of indices we can visit starting from the best index is 4, which starts from index 2 in the example array.

Python Solution

num_elements = len(arr)

Check for jumps to the left

Check for jumps to the right

break

break

break;

// Update the dp value if we find a better path

return maxJumps; // Return the maximum number of jumps possible

maxJumps = Math.max(maxJumps, dp[currentIndex]);

// Update the result with the maximum dp value found so far

dp[currentIndex] = Math.max(dp[currentIndex], 1 + dp[rightIndex]);

return max(jumps)

for left in range(position - 1, -1, -1):

Stop if out of jump distance or if an equal or higher bar is met

if position - left > max_distance or arr[left] >= height:

jumps[position] = max(jumps[position], 1 + jumps[left])

Update the jump count if a new max is found

for right in range(position + 1, num_elements):

Return the maximum jump count found across all positions

max(f) = 4

1 class Solution:

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Initial jump counts set to 1 for each position, as each position can jump at least once 6 jumps = [1] * num elements8 # Process positions in ascending order of their heights, along with their indices 9 for height, position in sorted(zip(arr, range(num_elements))): 10

Stop if out of jump distance or if an equal or higher bar is met 21 if right - position > max_distance or arr[right] >= height: 23 24 # Update the jump count if a new max is found 25 jumps[position] = max(jumps[position], 1 + jumps[right])

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Java Solution
   class Solution {
       public int maxJumps(int[] heights, int maxDistance) {
           int n = heights.length;
           // Create an array of indices from the input array
           Integer[] indices = new Integer[n];
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           for (int i = 0; i < n; ++i) {
                indices[i] = i;
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           // Sort the indices based on the heights, if the same height maintain the order of indices
12
           Arrays.sort(indices, (i, j) -> Integer.compare(heights[i], heights[j]));
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           int[] dp = new int[n]; // Dynamic programming array to store the max number of jumps
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           Arrays.fill(dp, 1); // Initialize with 1 since the min jumps for each position is 1 (stand still)
16
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           int maxJumps = 0; // Variable to keep track of the maximum number of jumps
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           // Calculate the maximum number of jumps you can do from each position
           for (int currentIndex : indices) {
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21
               // Look left of the current index
22
                for (int leftIndex = currentIndex - 1; leftIndex >= 0; --leftIndex) {
23
                   // If it's too far or the height at leftIndex is higher or equal, we can't jump from there
24
                   if (currentIndex - leftIndex > maxDistance || heights[leftIndex] >= heights[currentIndex]) {
25
                       break;
26
27
                   // Update the dp value if we find a better path
28
                   dp[currentIndex] = Math.max(dp[currentIndex], 1 + dp[leftIndex]);
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31
               // Look right of the current index
32
               for (int rightIndex = currentIndex + 1; rightIndex < n; ++rightIndex) {</pre>
```

// If it's too far or the height at rightIndex is higher or equal, we can't jump from there

if (rightIndex - currentIndex > maxDistance || heights[rightIndex] >= heights[currentIndex]) {

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C++ Solution
  1 #include <vector>
  2 #include <algorithm>
    #include <numeric>
    using namespace std;
    class Solution {
    public:
         // Function to find the maximum number of jumps you can make in the array
         int maxJumps(vector<int>& heights, int maxDistance) {
  9
             int n = heights.size(); // Size of the array
 10
 11
             // Initialize an index vector with values from 0 to n-1
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             vector<int> indices(n);
             iota(indices.begin(), indices.end(), 0);
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             // Sort the indices based on the corresponding values in 'heights'
             sort(indices.begin(), indices.end(), [&](int a, int b) { return heights[a] < heights[b]; });</pre>
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             // Initialize a vector to store the furthest jump length from every position
 20
             vector<int> dp(n, 1); // All elements are initialized to 1 as the minimum jump is always 1 (itself)
 21
 22
             // Loop through the sorted indices to fill dp in increasing order of heights
 23
             for (int index : indices) {
                 // Look to the left of the current index
 24
 25
                 for (int left = index - 1; left >= 0; --left) {
 26
                     // If the left element is out of bounds or taller, stop checking further
 27
                     if (index - left > maxDistance || heights[left] >= heights[index]) {
 28
                         break;
 29
 30
                     // Update dp array for index with the optimal previous jump count
                     dp[index] = max(dp[index], 1 + dp[left]);
 31
 32
 33
                 // Look to the right of the current index
 34
                 for (int right = index + 1; right < n; ++right) {</pre>
 35
                     // If the right element is out of bounds or taller, stop checking further
 36
                     if (right - index > maxDistance || heights[right] >= heights[index]) {
 37
                     // Update dp array for index with the optimal previous jump count
 39
 40
                     dp[index] = max(dp[index], 1 + dp[right]);
 41
 42
             // Return the maximum jumps that can be made, found in the dp array
 43
             return *max_element(dp.begin(), dp.end());
 44
 45
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    };
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Typescript Solution
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2 import { max } from 'lodash';

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         // Initialize an array to store the furthest jump length from every position
 15
         const dp: number[] = new Array(n).fill(1); // All elements are initialized to 1 as the minimum jump is always 1 (itself)
 16
 17
         // Loop through the sorted indices to fill dp in increasing order of heights
         indices.forEach((index) => {
 18
 19
             // Look to the left of the current index
 20
             for (let left = index - 1; left >= 0; --left) {
                 // If the left element is out of maxDistance or taller, stop checking further
 21
 22
                 if (index - left > maxDistance || heights[left] >= heights[index]) {
 23
                    break;
                // Update dp array for index with the optimal previous jump count
                 dp[index] = Math.max(dp[index], 1 + dp[left]);
 27
 28
            // Look to the right of the current index
             for (let right = index + 1; right < n; ++right) {
 29
                 // If the right element is out of maxDistance or taller, stop checking further
 30
                 if (right - index > maxDistance || heights[right] >= heights[index]) {
 31
 32
                    break;
 33
 34
                // Update dp array for index with the optimal previous jump count
 35
                dp[index] = Math.max(dp[index], 1 + dp[right]);
 36
 37
         });
 38
 39
         // Return the maximum jumps that can be made, found in the dp array
 40
         return Math.max(...dp);
 41 }
 42
    // Example usage:
    // If you want to call the function, you would pass in the heights array and maxDistance like so:
    // maxJumps([4, 2, 7, 6, 9, 14, 12], 2);
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Time and Space Complexity
Time Complexity
The time complexity of the given code can be analyzed based on the following:
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1 // Importing necessary functionalities from arrays and algorithms

const n: number = heights.length; // Size of the array

// Initialize an index array with values from 0 to n-1

indices.sort((a, b) => heights[a] - heights[b]);

// Function to find the maximum number of jumps you can make in the array

const indices: number[] = Array.from({ length: n }, (_, i) => i);

// Sort the indices based on the corresponding values in 'heights'

function maxJumps(heights: number[], maxDistance: number): number {

- 1. Sorting the array arr alongside the indices has a complexity of O(n log n) where n is the length of the array arr. 2. The double nested loops contribute to the time complexity in the following way: The outer loop runs n times since it iterates over the sorted arrays of heights and indices.
- Each inner loop performs a linear scan in both directions, but due to the constraint limiting the jumps to distance d, the inner loops each run at most d times.
- Therefore, the inner loops collectively contribute at most 0(n * 2d) = 0(nd) time complexity. Combining these, the total time complexity of the code is $0(n \log n + nd)$.

Space Complexity

The space complexity of the given code can be analyzed based on the following: 1. An auxiliary array f of size n is used to store the maximum number of jumps from each position, contributing an O(n) space

complexity. 2. Since there are no recursive calls or additional data structures that grow with the input size, and the sorting operation can be

- assumed to use 0(1) space given that most sorting algorithms can be done in-place (like Timsort in Python), the additional space complexity imposed by the stack frames during the for loops and sorting is constant.

Therefore, the total space complexity of the code is O(n).