1329. Sort the Matrix Diagonally

Sorting

Problem Description

<u>Array</u>

Matrix

Medium

starts from a cell in either the topmost row or leftmost column and goes diagonally in the bottom-right direction until it reaches the end of the matrix. The <u>sorting</u> of each diagonal should be done in ascending order, and the goal is to return the matrix with all diagonals sorted.

For instance, if a diagonal starts from mat[2][0] in a 6 x 3 matrix, it would include the cells mat[2][0], mat[3][1], and mat[4]

The task is to sort the integers in each diagonal of a given m x n matrix mat. A matrix diagonal is defined as a line of cells that

For instance, if a diagonal starts from mat[2][0] in a 6 x 3 matrix, it would include the cells mat[2][0], mat[3][1], and mat[4][2]. This diagonal, like all others in the matrix, needs to be sorted so that the smallest number is at mat[2][0] and the largest at mat[4][2].

diagonal does not affect the elements in another diagonal.

Intuition

of comparisons and swaps until each element on the diagonal is in ascending order. The solution code provided is based on this approach.

To solve the problem, we understand that each diagonal can be sorted independently of the others, since the sorting of one

A brute force approach to sort each diagonal is to use a "bubble sort"-like method where for each diagonal, we perform a series

Here's how we approach it:

1. Iterate over each possible starting cell of a diagonal. This would usually mean iterating over cells on the top row and the leftmost column, but the code provided is only iterating through min(m, n) elements. This part of the approach seems to be

limiting the number of iterations and may not cover all diagonals in a non-square matrix (where m is not equal to n).

2. Perform a double loop, iterating through cells within the matrix boundaries, excluding the last row and column, to compare the current cell mat[i][j] with the next cell in the diagonal mat[i+1][j+1].

- If the current cell is larger than the next cell in the diagonal, we swap them. The swap ensures that the smaller value moves towards the start of the diagonal.
 Repeat the comparison and swapping process until all cells in the matrix are checked. Note that this requires multiple passes
- through the matrix to get all elements in the correct order, given the nature of the "bubble sort"-like method.

 This solution ensures each diagonal is sorted, but it's not the most efficient approach due to its high time complexity, and it's not
- optimized to handle non-square matrices correctly in all cases.

 Solution Approach

Let's walk through the implementation step by step:1. The first step is to retrieve the dimensions of the matrix using len(mat) for the number of rows (m) and len(mat[0]) for the number of columns (n).

It then uses a nested loop to iterate over the elements of the matrix, excluding the last row and column to prevent out-of-

The code compares each element mat[i][j] with the next diagonal element mat[i + 1][j + 1]. When it finds that mat[i]

This is a simplification and does not sort all diagonals properly in the case of non-square matrices, since it doesn't address all

cells m - 1 times to ensure all cells are eventually sorted. Since bubble sort has a time complexity of O(N^2), the time

The code provided uses a simplified in-place sorting algorithm similar to bubble sort to sort each diagonal of the matrix.

bounds access. The loop variables i and j represent the current cell being considered.

[j] is greater than mat[i + 1][j + 1], it performs a swap. This operation is intended to move the larger numbers down and right along the diagonals and the smaller numbers up and left.

4. However, the provided solution approach only iterates through the diagonals that start in the cells [0, k] for k < min(m, n).

possible starting cells of the diagonals that could be on the leftmost column for a matrix where m > n.

5. The code will perform the comparison and swapping process repeatedly in a brute force manner, iterating over the matrix

complexity of this code will also reflect the inefficiencies of bubble sort, especially as the size of the matrix grows.

To sum up, the solution attempts to use a bubble sort-like algorithm over the matrix's diagonals to sort each one in ascending order. The problem with this implementation is that it may not sort all diagonals as desired, especially for non-square matrices, and it's not efficient due to the bubble sort approach resulting in a high time complexity.

Note that a more efficient solution would sort each diagonal individually by extracting the diagonal elements, sorting them using

a more efficient sorting algorithm (e.g., quicksort or timsort), and then placing them back into the matrix. This approach would

significantly reduce the overall time complexity to O(DlogD) for each diagonal of average length D.

The goal is to sort the integers in each diagonal. In this matrix, there are five diagonals:

5. The fifth diagonal starting from mat [2] [0] includes the elements [1, 2, 3] (already sorted).

the third diagonal [1, 2, 1] as an example, as it's the longest and requires actual sorting:

We retrieve the dimensions of the matrix, which are m = 3 for rows and n = 3 for columns.

Now, we compare each element on this diagonal with the subsequent diagonal element:

Compare mat[0][2] (which is 1) with mat[1][2] (which is 2). No swap needed since 1 is less than 2.

Compare mat[1][2] (which is 2) with mat[2][2] (which is 1). Swap needed since 2 is greater than 1.

After the necessary swap, our diagonal now looks like [1, 1, 2], and it is sorted in ascending order.

Compare mat[0][2] (which is 1) with mat[1][3] (which doesn't exist, so we skip this step).

Compare mat[1][2] (which is 2) with mat[2][3] (which doesn't exist, so we skip this step).

iterate and compare the elements within the matrix boundaries again.

If we repeat this process for all diagonals, the final sorted matrix will be:

Let's walk through a simple example to illustrate the solution approach described. Consider the following 3x3 matrix mat:

mat = [
[3, 3, 1],
[2, 2, 2],

The first diagonal starting from mat[0][0] includes the elements [3] (already sorted).
 The second diagonal starting from mat[0][1] includes the elements [3, 2].
 The third diagonal starting from mat[0][2] includes the elements [1, 2, 1].
 The fourth diagonal starting from mat[1][0] includes the elements [2, 1].

The sorting algorithm provided will iterate through these diagonals and sort them. Let's focus on how this algorithm would sort

2. We iterate starting from mat[0][2], excluding the last row and column to make sure we won't access mat[3][3] which is out

of bounds.

mat = [

[3, 2, 1],

[2, 1, 2],

[1, 1, 2]

Example Walkthrough

[1, 1, 1]

4. Since we are not going out of bounds, we re-iterate over the matrix:

Following the above approach, it seems we don't make any swaps. However, since we have to iterate m - 1 times, we will re-

However, the described algorithm is not efficient as it might require many iterations for larger matrices due to its similarity to bubble sort, which has a high time complexity. Also, this example is for a square matrix – the algorithm may not perform correctly

Iterate through each element in the matrix except for the last row and column.

Compare the current element with the element in the next diagonal position.

mat[row][col], mat[row + 1][col + 1] = mat[row + 1][col + 1], mat[row][col]

Note that each diagonal is individually sorted, even if the matrix as a whole isn't.

would be to extract each diagonal, sort it, and then place it back into the matrix.

Solution Implementation

Python

class Solution:

for non-square matrices because it does not iterate through all possible starting cells of the diagonals. A more efficient approach

class Solution {
 /**

* is defined from the top-left to the bottom-right corners.

// Determine the number of rows and columns in the matrix

for (int k = 0; $k < Math.min(numRows.numCols) - 1; ++k) {$

for (int j = 0; j < numCols - 1; ++j) {

int temp = matrix[i][j];

matrix[i + 1][j + 1] = temp;

* @param matrix The matrix to be sorted diagonally.

for (int i = 0; i < numRows - 1; ++i) {

* @return The diagonally sorted matrix.

int numRows = matrix.length;

return matrix;

int row = startRow;

int col = startCol;

++row:

++col;

row = startRow:

col = startCol;

let row = startRow;

let col = startCol;

++row;

++col;

row = startRow:

col = startCol;

++row;

++col;

class Solution:

const diagonalElements: number[] = [];

// Collect all elements of the diagonal

// Sort the collected diagonal elements

diagonalElements.sort((a, b) => a - b);

for (const element of diagonalElements) {

matrix[row][col] = element;

while (row < rowCount && col < colCount) {</pre>

diagonalElements.push(matrix[row][col]);

// Put the sorted elements back into their places on the diagonal

def diagonalSort(self, mat: List[List[int]]) -> List[List[int]]:

Only need to iterate up to the smallest dimension minus one

since we start the comparison from the second-to-last diagonal.

if mat[row][col] > mat[row + 1][col + 1]:

Swap the elements if they are out of order.

Iterate through each element in the matrix except for the last row and column.

Compare the current element with the element in the next diagonal position.

mat[row][col], mat[row + 1][col + 1] = mat[row + 1][col + 1], mat[row][col]

Get the number of rows and columns in the matrix.

num_rows, num_cols = len(mat), len(mat[0])

for in range(min(num rows, num cols) - 1):

for col in range(num cols - 1):

for row in range(num rows - 1):

std::vector<int> diagonalElements;

// Collect all elements of the diagonal

// Sort the collected diagonal elements

for (int element : diagonalElements) {

matrix[row][col] = element;

while (row < rowCount && col < colCount)</pre>

diagonalElements.push_back(matrix[row][col]);

std::sort(diagonalElements.begin(), diagonalElements.end());

// Put the sorted elements back into their places on the diagonal

private:

int numCols = matrix[0].length;

public int[][] diagonalSort(int[][] matrix) {

* Sorts each diagonal of the given matrix independently, where a diagonal

// Iterate over each element of the matrix except the last row and column

// than the element in the next row and next column

// Swap elements using a temporary variable

if (matrix[i][j] > matrix[i + 1][j + 1]) {

matrix[i][j] = matrix[i + 1][j + 1];

// Helper function to sort a single diagonal starting at (startRow, startCol)

// Compare and swap elements if current element is greater

def diagonalSort(self, mat: List[List[int]]) -> List[List[int]]:

Only need to iterate up to the smallest dimension minus one

since we start the comparison from the second-to-last diagonal.

if mat[row][col] > mat[row + 1][col + 1]:

Swap the elements if they are out of order.

Get the number of rows and columns in the matrix.

num_rows, num_cols = len(mat), len(mat[0])

for in range(min(num rows, num cols) - 1):

for col in range(num cols - 1):

for row in range(num rows - 1):

Return the sorted matrix.

return mat

Java

*/

```
// Return the sorted matrix
        return matrix;
C++
#include <vector>
#include <algorithm> // For std::sort function
class Solution {
public:
    std::vector<std::vector<int>> diagonalSort(std::vector<std::vector<int>>& matrix) {
        int rowCount = matrix.size(); // Number of rows in the matrix
        int colCount = matrix[0].size(); // Number of columns in the matrix
        // Sort each diagonal that starts from the first column
        for (int row = 0; row < rowCount; ++row) {</pre>
            sortDiagonal(matrix, row, 0, rowCount, colCount);
        // Sort each diagonal that starts from the first row, except the first diagonal which is already sorted
        for (int col = 1; col < colCount; ++col) {</pre>
            sortDiagonal(matrix, 0, col, rowCount, colCount);
```

void sortDiagonal(std::vector<std::vector<int>>& matrix, int startRow, int startCol, int rowCount, int colCount) {

```
++row;
            ++col;
TypeScript
type Matrix = number[][];
// This function sorts the matrix diagonally
function diagonalSort(matrix: Matrix): Matrix {
    const rowCount = matrix.length:
                                     // Number of rows in the matrix
    const colCount = matrix[0].length; // Number of columns in the matrix
    // Sort each diagonal that starts from the first column
    for (let row = 0; row < rowCount; ++row) {</pre>
        sortDiagonal(matrix, row, 0, rowCount, colCount);
    // Sort each diagonal that starts from the first row.
    // except for the first diagonal which is already sorted
    for (let col = 1; col < colCount; ++col) {</pre>
        sortDiagonal(matrix, 0, col, rowCount, colCount);
    return matrix;
// Helper function that sorts a single diagonal
// starting at (startRow, startCol)
```

function sortDiagonal(matrix: Matrix, startRow: number, startCol: number, rowCount: number, colCount: number): void {

```
# Return the sorted matrix.
return mat
```

Time and Space Complexity

Time Complexity

The provided code has a nested loop structure that iterates over the elements in the matrix in a specific pattern to sort the diagonals. Let's analyze both the time and space complexity:

The outermost loop is controlled by min(m, n) - 1, where m is the number of rows and n is the number of columns in the matrix.

Inside the outer loop, there are two nested loops that each run m-1 and n-1 times respectively, iterating over the elements of the matrix.

This loop will run for the minimum dimension - 1.

of the matrix.

The combined time complexity is the product of these factors, resulting in $0((\min(m, n) - 1) * (m - 1) * (n - 1))$.

Simplifying, we drop constants and lower-order terms to focus on the growth rates, which gives us a time complexity of 0(min(m, n) * m * n).

Space Complexity

The space complexity of the code is 0(1) because there are no data structures being used that grow with the size of the input.

The only extra space used here is for the loop variables and a couple of temporary variables for the swapping process.