1513. Number of Substrings With Only 1s





Problem Description

String

The problem requires us to find and count the number of substrings within a given binary string s that consist entirely of the character '1'. For example, in the string "0110111", there are several such substrings: "1", "11", "111", "11", "11", and each of them should be counted. The challenge here is to do this efficiently and to deal with potentially very large numbers, the counts need to be returned modulo 10^9 + 7, which is a large prime number commonly used to prevent integer overflow issues in competitive programming.

Intuition

The intuition behind the solution is based on the observation that for a sequence of '1's of length n, there are exactly n * (n + 2 substrings that can be formed, all of which consist solely of '1's. This is because each additional '1' potentially adds as many new substrings as its position in the sequence (first '1' adds 1 substring, second '1' adds 2 substrings, and so on). So, we are essentially counting the lengths of continuous sequences of '1's and calculating the number of substrings for each sequence. The solution involves iterating through the string and using a counter variable cnt to keep track of the length of a consecutive

sequence of '1's. When we encounter a '1', we increment cnt. If we encounter a '0', we reset cnt to zero, because it breaks the sequence of '1's. After each step, regardless of whether we're continuing a sequence or ending one, we add the current value of cnt to ans, which accumulates the total number of substrings of '1's we've seen so far. Finally, since the answer could be a very large number, we return the total count modulo 10^9 + 7 as instructed by the problem

description.

The implementation of the solution is relatively straightforward with no need for complex data structures; the only variable that

Solution Approach

holds state during iteration is cnt, which counts the length of consecutive '1's. With every step forward in the string, the algorithm performs the following actions: 1. Check the current character (c) of the string. 2. If c is '1', increment the cnt variable: this increases the length of the current sequence of '1's by one.

'1's and resets the count for the next sequence.

- 3. If c is not '1' (in this case, it could only be '0' since it's a binary string), reset cnt to zero. This indicates the end of the current sequence of
- encountered so far. This process works because each time a '1' is encountered and cnt is incremented, it effectively counts all the new substrings

4. After updating cnt, add its current value to ans. This step accumulates the total number of valid substrings formed by the sequences of '1's

all the previous substrings plus a new substring that includes the entire sequence. The use of the modulo operation % (10***9 + 7) ensures that we handle the possibility of very large outputs, preventing integer overflow and keeping the result within the limits of the problem's constraints.

that could end with this '1'. If you have a sequence of length n, then adding one more '1' to the sequence adds n + 1 substrings:

scan, as it requires only one iteration through the input string to compute the result. **Example Walkthrough**

No additional data structures are required, and the pattern used in this algorithm is commonly known as a single pass or linear

Initialize cnt = 0 (to count the consecutive '1's) and ans = 0 (to accumulate the total number of substrings).

Character s [0] is '1':

Character s [1] is '1':

Start iterating over the string s from left to right.

Let's consider a small example binary string s = "11011". Here's how we would apply the solution approach to this input:

- Increment cnt to 1. Current substrings are: "1". ■ Add cnt to ans: ans += 1, hence ans = 0 + 1 = 1.
- Increment cnt to 2. Current substrings are: "1", "11".

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■ Add cnt to ans: ans += 2, hence ans = 1 + 2 = 3.
The next character s[2] is '0', which interrupts the sequence of '1's:
• Reset cnt to 0.

    ans remains unchanged.

Continue iteration.
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Increment cnt to 1. Current substrings are: "1". ■ Add cnt to ans: ans += 1, hence ans = 3 + 1 = 4.

Character s [3] is '1':

- Character s [4] is '1': Increment cnt to 2. Current substrings are: "1", "11". ■ Add cnt to ans: ans += 2, hence ans = 4 + 2 = 6.
- At this point, we have finished iterating over the entire string. The total count of substrings consisting only of '1's is stored in ans, which equals 6. Return ans % (10^9 + 7) to adhere to the problem constraints. Since 6 is well below the modulo, the final result is simply 6.

total_substrings = consecutive_ones_count = 0

consecutive ones count += 1

total substrings += consecutive ones count

Initialize the answer and a temporary counter for consecutive "1"s

// Add the current count of consecutive '1's to countSubstrings

countSubstrings = (countSubstrings + consecutiveOnes) % MODULO;

// Return the total number of substrings found, modulo the defined constant

// ending at this character that has not been counted vet

// Function to count the number of substrings containing only '1's

int count = 0; // Initialize a counter for consecutive '1's

long long answer = 0; // Initialize the answer to 0

// Iterate over each character in the input string

count = character == '1' ? count + 1 : 0;

// Otherwise, reset the count to 0

// This works because for each new '1' character, it forms a new substring

const int MODULUS = 1e9 + 7; // Define the modulus value for preventing integer overflow

// If the current character is '1', increase the count of consecutive '1's

// Add the current count to the answer. This works because for each '1' found.

// it contributes to that many substrings ending at that point (e.g., "111" has

Add the current count of consecutive "1"s to the total substrings.

substrings consisting of '1's.

As we can see from the example, the algorithm correctly counts the individual substrings of '1's and sums them up. It counts "11"

at the beginning as 2 substrings, resets the count after the '0', and then counts "1" and "11" again, adding up to a total of 6

Solution Implementation **Python**

Each time we encounter a "1", it forms a substring with all the consecutive "1"s before it.

Iterate through each character in the string for char in s: # If the character is "1", increment the consecutive "1"s counter if char == "1":

def numSub(self, s: str) -> int:

return countSubstrings;

for (char& character : s) {

class Solution:

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# If the character is not "1", reset the consecutive "1"s counter to 0
            else:
                consecutive_ones_count = 0
        # Return the total number of substrings, modulo 10^9 + 7
        return total_substrings % (10**9 + 7)
Java
class Solution {
    // This method counts the number of substrings that contains only the character '1'
    public int numSub(String s) {
        final int MODULO = (int) 1e9 + 7; // Define a constant for modulo operation
        int countSubstrings = 0; // Store the count of valid substrings
        int consecutiveOnes = 0; // Counter for consecutive '1's
        // Iterate through the string character by character
        for (int i = 0; i < s.length(); ++i) {</pre>
            // If the current character is '1', increment the consecutive ones counter
            // Otherwise, reset it to zero since we're only interested in consecutive '1's
            consecutiveOnes = s.charAt(i) == '1' ? consecutiveOnes + 1 : 0;
```

C++

public:

class Solution {

int numSub(string s) {

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// substrings "1", "11", and "111" ending at the last character).
            // Apply modulus operation to keep the number within bounds and handle overflow
            answer = (answer + count) % MODULUS;
        // Return the final count of substrings
        return static_cast<int>(answer); // Cast the long long answer to int before returning
};
TypeScript
function numSub(sequence: string): number {
    // Define the modulus value to keep the result within integer limits
    const modulus = 10 ** 9 + 7;
    // Initialize the answer to be returned
    let answer = 0;
    // Counter for the consecutive '1's
    let count = 0;
    // Iterate through each character in the string
    for (const char of sequence) {
        // If the character is '1', increase count, otherwise reset count to 0
        count = (char === '1') ? count + 1 : 0;
        // Add the current count to the answer and apply modulus to prevent overflow
        answer = (answer + count) % modulus;
```

```
return answer;
class Solution:
    def numSub(self, s: str) -> int:
        # Initialize the answer and a temporary counter for consecutive "1"s
        total_substrings = consecutive_ones_count = 0
       # Iterate through each character in the string
        for char in s:
           # If the character is "1", increment the consecutive "1"s counter
           if char == "1":
               consecutive ones count += 1
               # Add the current count of consecutive "1"s to the total substrings.
               # Each time we encounter a "1", it forms a substring with all the consecutive "1"s before it.
               total substrings += consecutive ones count
           # If the character is not "1", reset the consecutive "1"s counter to 0
           else:
               consecutive_ones_count = 0
       # Return the total number of substrings, modulo 10^9 + 7
        return total_substrings % (10**9 + 7)
Time and Space Complexity
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The code provided counts the number of substrings of contiguous '1's in a given string s. The time complexity and space

// Return the computed answer

complexity of the algorithm are analyzed below. **Time Complexity**

operations such as checking if a character is '1' or '0', incrementing the cnt variable, and adding the value of cnt to ans. Because these operations do not depend on the size of the string and are repeated for each character, the time complexity is directly proportional to the length of the string. Therefore, the time complexity is O(n), where n is the length of the input string S. **Space Complexity**

The algorithm goes through each character of the input string s exactly once. During this process, it performs constant time

The space used by the algorithm includes a fixed number of integer variables ans and cnt, which do not scale with the size of the input string. As a result, the algorithm uses a constant amount of additional space, resulting in a space complexity of 0(1), indicating that it is independent of the input size.