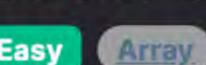
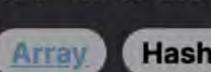
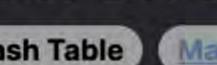
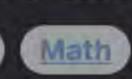
2549. Count Distinct Numbers on Board

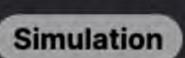












Hash Table Easy

Problem Description

In this problem, you have a board with a single positive integer n on it. You are required to follow a daily procedure for 10^9 days, which involves two steps. In the first step, for every number x currently on the board, you need to find all the numbers i in the range 1 <= i <= n, which satisfy the condition x % i == 1. In the second step, all the numbers you've found in the first step are added to the board. The task is to determine the number of distinct integers on the board after 10^9 days.

Leetcode Link

A key thing to note is that once a number is placed on the board, it stays there for the entire duration.

Intuition

The first intuition is that the process seems complex and potentially time-consuming, especially given the 10^9 days. However, we notice that the nature of the modulo operation being performed (x 🐐 🚶 == 1) simplifies things. This is because for a given x, as i increases, the set of 1's that satisfy the condition doesn't change past a certain point, since we are solely interested in 1 values that result in a remainder of 1 when x is divided by 1.

By analyzing smaller cases, we can observe that the numbers added to the board on the first day are [2, 3, 4, ..., n] — because n % i == 1 for i ranging from 1 to n-1. From the next day onwards, additional multiples do not get added to the board since these would only generate sequences similar to the first day but with bigger numbers which do not go up to n. The operation x % i == 1 only yields numbers smaller than x, so the numbers produced are already on the board.

Given this, we can deduce that after the first day, there would be no new numbers added to the board. Thus, the distinct integers present on the board would be all the numbers from 2 up to n, inclusive. This gives us a total count of n-1 distinct numbers (as we start counting from 2). If n is 1, there are no additional numbers that we can add, so the result would be 1. This knowledge lets us solve the problem in constant time with the simple solution $\max(1, n - 1)$.

Solution Approach

The reference solution provided is a direct translation of the intuition behind the problem into code. Since we have deduced that no new numbers will be added to the board after the first day, we don't need to simulate the entire 1009 days. Instead, we just need to calculate the total number of distinct numbers after the first day.

No complex algorithms or data structures are needed here, and there's no need for a pattern as the observation leads to a one-step solution.

The implementation is straightforward:

```
class Solution:
    def distinctIntegers(self, n: int) -> int:
        return max(1, n - 1)
```

The function distinctIntegers simply returns the result of $\max(1, n - 1)$. The $\max()$ function is used to handle the edge case where n is 1. In this case, there can only be one number (which is 1 itself) on the board. For all other values of n greater than 1, the function returns n - 1, which represents all the distinct numbers from 2 to n inclusive.

It's important to note that the efficiency of this solution is O(1), meaning that the time complexity does not depend on the size of the input n. Hence, it is an extremely efficient solution both in terms of time and space complexity.

Example Walkthrough

Let's illustrate the solution approach using a small example with n = 5. According to the problem statement, we start with the integer 5 on the board:

• Day 1:

- We perform the operation x % i == 1 for each i such that 1 <= i <= n. In this case, x is the initial number 5. We find the integers: 5 % 1 == 0, 5 % 2 == 1, 5 % 3 == 2, 5 % 4 == 1, and 5 % 5 == 0.
- The only i values that satisfy the condition x % i == 1 are 2 and 4.
- Therefore, we add the numbers 2 and 4 to the board.
- So, at the end of Day 1, the board contains 2, 4, and the initial 5.
- After Day 1:

We will notice that any x on the board going forward will have been generated by using the % operation with a starting

- number of 5. Now, repeating the operation x % i == 1 for each new x (which are 2 and 4) and each i in the range 1 to 5 will not provide
- any new integers satisfying the condition that are not already on the board. Since 2 and 4 are less than our starting n (5), all the resultant numbers on applying x % i == 1 are less than 2 and 4, respectively, and are thus not within the range 1 to 5. This means no new numbers will be added to the board after Day 1.
- Therefore, the board will contain the original number 5 plus every number from 2 to 5 1 (inclusive). This is exactly 5 1 = 4

No matter how many days pass, no new numbers will be added to the board since any number x will not yield a new i that satisfies x

The solution then is the function:

1 class Solution:

% i == 1 within the range 1 to n.

numbers, which are 2, 3, 4, and 5.

```
For our example with n = 5, the function call distinctIntegers(5) will return max(1, 5 - 1), which is max(1, 4), resulting in 4. This
matches our walkthrough, where the distinct numbers on the board after 10^9 days are 2, 3, 4, and 5.
```

return max(1, n - 1)

def distinctIntegers(self, n: int) -> int:

// Method to calculate the number of distinct integers

// This ensures that for n less than 2, the result is always 1

// which is not mentioned here, hence the simplified approach.

// with a difference of at least 1 between each integer

// Returns the maximum between 1 and (n - 1)

public int distinctIntegers(int n) {

return Math.max(1, n - 1);

Python Solution

def distinctIntegers(self, n: int) -> int: # This function calculates the maximum number of distinct integers. # It ensures there is at least one distinct integer by returning a minimum of 1

class Solution:

```
# and otherwise returns one less than the input number `n`.
          # Use max() to ensure the result is at least 1
           return max(1, n - 1)
Java Solution
 1 class Solution {
```

```
9
C++ Solution
1 class Solution {
   public:
       // Function to calculate the number of distinct integers
       int distinctIntegers(int num) {
           // The logic assumes that the minimum number of distinct integers
           // you can have is 1 (when num is either 0 or 1)
           // and the maximum is when you subtract 1 from num (for num > 1),
```

// since the problem may refer to counting distinct integers given a certain condition,

// For n greater than 1, return n-1 because we can have a maximum of n-1 distinct integers

// Using std::max to ensure the number returned is at least 1 11 12 13

10

```
return std::max(1, num - 1);
14 };
15
Typescript Solution
  // Returns the count of distinct integers that can be formed with 'n' elements
  // where the difference between each element must be at least one
  // except for the base case where n is 0 or 1, return 1 (only one distinct integer can be formed - zero itself)
   function distinctIntegers(n: number): number {
       // Ensure there's at least one distinct integer when n is 0 or 1
```

return Math.max(1, n - 1); 10

Time Complexity

Time and Space Complexity

The given Python function distinctIntegers executes a direct comparison and returns the result of max(1, n - 1). It does not have any loops or recursive calls. As such, the number of operations is constant, regardless of the size of n. Therefore, the time complexity of the function is 0(1).

of the function is also 0(1).

Space Complexity The function only uses a fixed amount of space for the input variable n and does not allocate any additional space that depends on the input size. It also does not use any auxiliary data structures like arrays, lists, or dictionaries. Consequently, the space complexity