

Problem Description

In this problem, we are tasked with traversing a 2D array (or matrix) in a spiral pattern. Imagine starting at the top-left corner of the matrix and going right, then down, then left, and then up, turning inward in a spiral shape, until we traverse every element in the matrix exactly once. The function should return a list of the elements of the matrix in the order they were visited during this spiral traversal.

Intuition

To solve this problem, we need to simulate the process of traveling around the matrix spiral. Essentially, we keep moving in the same direction (right initially) until we meet a boundary of the matrix or a previously visited cell. When we encounter such a boundary, we make a clockwise turn and continue the process. There are two insightful approaches to this problem:

1. Simulation Approach: We initiate four direction vectors (or in our case, a direction array dirs) that represent right, down, left,

and up. We iterate over all elements in the matrix by taking steps in the initial direction until we can no longer move forward. At

- this point, we turn 90 degrees and continue. To avoid revisiting cells, we mark each visited cell by adding it to a set vis so that we know when to turn. The time complexity here is $0 (m \times n)$ because we visit each element once, and the space complexity is also $O(m \times n)$ due to the extra space used to store visited cells. 2. Layer-by-layer Simulation: Instead of marking visited cells, we can visualize the matrix as a series of concentric rectangular layers. We traverse these layers from the outermost to the innermost, peeling them away as we go. This approach requires
- careful handling of the indices to ensure we stay within the bounds of the current layer. This way of traversal helps to potentially reduce extra space usage because we don't explicitly need to keep track of visited cells. In the provided solution code, we follow the simulation approach. We appropriately update our direction of movement based on the bounds of the matrix and whether we've visited a cell. The direction change is done by iterating over the dirs array and updating our

Solution Approach The given Python solution follows the Simulation Approach described in the intuition section.

row and column pointers i and j respectively. The result list ans stores the elements as we traverse the matrix.

1. Initialization:

 We define m and n which are the dimensions of the matrix (number of rows and number of columns respectively). The dirs array dirs = (0, 1, 0, -1, 0) encodes the direction vectors. dirs[k] and dirs[k+1] together represent the

ans list is where we collect the elements of the matrix as we visit them.

direction we move in, with k starting at 0 and cycling through values 0 to 3 to represent right, down, left, and up in that

order.

2. Visiting Elements:

- The i and j variables represent the current row and column positions in the matrix.
- We loop exactly m * n times, once for each element of the matrix. Each time through the loop, we append the current element to the ans list and mark its position (i, j) as visited by adding
- it to the vis set.
- 3. Moving Through the Matrix:

We calculate the next position (x, y) based on the current direction we are moving. This is done using the current values of

i, j, and k.

is the if not $0 \le x \le m$ or not $0 \le y \le n$ or (x, y) in vis: check. If the move is invalid, we change the direction by increasing k modulo 4. This works because if k is 3 and we add 1, (k + 1) % 4 will reset k back to 0.

Before we move to the next position, we check if the position is valid - it must be within bounds and not already visited. This

 Once the direction is confirmed as valid, we update i and j to move to the next position in the matrix. 4. Handling Edge Cases:

Because we update the direction whenever we hit the edge of the matrix or a visited cell, the algorithm naturally handles

non-square matrices and any edge cases where the spiral must turn inward. 5. Completing the Spiral:

o In the reference solution, it's suggested that instead of using a vis set to keep track of visited cells (contributing to space

complexity of $O(m \times n)$, we could modify the matrix itself to mark cells as visited. This could be done by adding a constant

- The process continues, circling around the matrix and moving inward until all elements have been added to ans. 6. Space Optimization:
- value which is outside the range of the matrix values, effectively using the input matrix as the vis state. This reduces the space complexity to 0(1), provided the matrix can be modified and that the added constant is chosen such that it doesn't
- The attention to directional changes and boundary conditions ensures that all cases are handled smoothly. Example Walkthrough Let's illustrate the solution approach using a small example where our input is a 2D matrix: 1 matrix = [

The executed code follows this approach rigorously, and through simulation, delivers the correct spiral traversal of the input matrix.

Now we'll walk through the solution step by step:

We calculate the next position using the current direction (right, k = 0), so x = i + dirs[k] = 0 and y = j + dirs[k+1] =

\circ m = 3 (3 rows), n = 3 (3 columns)

2. Visiting Elements:

3. Moving Through the Matrix:

5. Avoiding Visited Cells:

7. Space Optimization (Optional):

def spiralOrder(self, matrix):

Define matrix dimensions.

rows, cols = len(matrix), len(matrix[0])

Iterate over the cells of the matrix.

result.append(matrix[row][col])

Mark the current cell as visited.

for _ in range(rows * cols):

visited.add((row, col))

Python Solution

class Solution:

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1. Initialization:

cause integer overflow.

 Direction array dirs = (0, 1, 0, -1, 0) indicates the x and y offsets for right, down, left, and up movements respectively. We start at the top-left corner, so initial indices i = 0 and j = 0.

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    We begin by appending matrix[0][0] to ans, so ans = [1].
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1.

 This position is within bounds and not visited, so we move there and append matrix[0][1] to ans, making it [1, 2]. We repeat this process and append [3, 6, 9] to ans.

Next, we attempt to move left but the cell (2, 0) is visited.

We turn right and add [4, 5] to the spiral traversal.

• ans = [] will collect the elements in spiral order.

vis = set() to store visited positions.

We add (0, 0) to vis to mark it as visited.

 After reaching the last column, we check the next right move and find it's out of bounds. • We then change direction to down (k = 1), and append [8, 7] to ans.

4. Direction Change and Boundary Check:

- 6. Completing the Spiral: We've now visited all cells, and ans is [1, 2, 3, 6, 9, 8, 7, 4, 5].
- A potentially more space-efficient approach might entail modifying the given matrix to mark visited elements if allowed. By following the simulation approach, the function would return the traversal in spiral order as [1, 2, 3, 6, 9, 8, 7, 4, 5].

This function takes a matrix and returns a list of elements in spiral order.

Initialize the answer list and a set to keep track of visited cells.

Calculate the next cell's position based on the current direction.

Append the current element to the result list.

We turn again, moving up and find the top center cell (0, 1) is also visited.

Define directions for spiral movement (right, down, left, up). directions = ((0, 1), (1, 0), (0, -1), (-1, 0))# Initialize row and column indices and the direction index. row = col = direction_index = 0

next_row, next_col = row + directions[direction_index][0], col + directions[direction_index][1]

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                # Check if the next cell is within bounds and not visited.
                if not (0 <= next_row < rows) or not (0 <= next_col < cols) or (next_row, next_col) in visited:</pre>
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                    # Change direction if out of bounds or cell is already visited.
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result = []

visited = set()

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direction_index = (direction_index + 1) % 4
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               # Update the row and column indices to the next cell's position.
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               row += directions[direction_index][0]
37
               col += directions[direction_index][1]
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           # Return the result list.
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           return result
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Java Solution
  1 import java.util.List;
  2 import java.util.ArrayList;
     class Solution {
         public List<Integer> spiralOrder(int[][] matrix) {
             // Dimensions of the 2D matrix
  6
             int rowCount = matrix.length;
             int colCount = matrix[0].length;
  8
             // Direction vectors for right, down, left, and up
 10
             int[] directionRow = \{0, 1, 0, -1\};
 11
             int[] directionCol = {1, 0, -1, 0};
 12
             // Starting point
 13
             int row = 0, col = 0;
             // Index for the direction vectors
 14
             int directionIndex = 0;
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             // List to hold the spiral order
 17
             List<Integer> result = new ArrayList<>();
 18
             // 2D array to keep track of visited cells
 19
             boolean[][] visited = new boolean[rowCount][colCount];
 20
             for (int h = rowCount * colCount; h > 0; --h) {
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 22
                 // Add the current element to the result
 23
                 result.add(matrix[row][col]);
 24
                 // Mark the current cell as visited
 25
                 visited[row][col] = true;
 26
                 // Compute the next cell position
 27
                 int nextRow = row + directionRow[directionIndex];
 28
                 int nextCol = col + directionCol[directionIndex];
 29
                 // Check if the next cell is out of bounds or visited
 30
                 if (nextRow < 0 || nextRow >= rowCount || nextCol < 0 || nextCol >= colCount || visited[nextRow][nextCol]) {
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// Update the direction index to turn right in the spiral order

directionIndex = (directionIndex + 1) % 4;

// Move to the next cell

row = nextRow;

col = nextCol;

return result;

nextRow = row + directionRow[directionIndex];

nextCol = col + directionCol[directionIndex];

// Recompute the next cell using the new direction

public:

C++ Solution

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1 class Solution {
         vector<int> spiralOrder(vector<vector<int>>& matrix) {
             if (matrix.empty()) return {}; // Return an empty vector if the matrix is empty
             int rows = matrix.size(), cols = matrix[0].size(); // rows and cols store the dimensions of the matrix
             vector<int> directions = {0, 1, 0, -1, 0}; // Row and column increments for right, down, left, up movements
             vector<int> result; // This vector will store the elements of matrix in spiral order
  8
             vector<vector<bool>> visited(rows, vector<bool>(cols, false)); // Keep track of visited cells
  9
 10
             int row = 0, col = 0, dirIndex = 0; // Start from the top-left corner and use dirIndex to index into directions
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             for (int remain = rows * cols; remain > 0; --remain) {
                 result.push_back(matrix[row][col]); // Add the current element to result
 14
 15
                 visited[row][col] = true; // Mark the current cell as visited
 16
 17
                 // Calculate the next cell position
                 int nextRow = row + directions[dirIndex], nextCol = col + directions[dirIndex + 1];
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 20
                 // Change direction if next cell is out of bounds or already visited
 21
                 if (nextRow < 0 || nextRow >= rows || nextCol < 0 || nextCol >= cols || visited[nextRow][nextCol]) {
 22
                     dirIndex = (dirIndex + 1) % 4; // Rotate to the next direction
 23
 24
 25
                 // Move to the next cell
 26
                 row += directions[dirIndex];
 27
                 col += directions[dirIndex + 1];
 28
 29
             return result; // Return the result
 30
 31 };
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Typescript Solution
    function spiralOrder(matrix: number[][]): number[] {
         const rowCount = matrix.length; // Number of rows in the matrix
         const colCount = matrix[0].length; // Number of columns in the matrix
         const result: number[] = []; // The array that will be populated and returned
```

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const visited = new Array(rowCount).fill(0).map(() => new Array(colCount).fill(false)); // A 2D array to keep track of visited
  5
         const directions = [0, 1, 0, -1, 0]; // Direction array to facilitate spiral traversal: right, down, left, up
  6
         let remainingCells = rowCount * colCount; // Total number of cells to visit
  8
  9
        // Starting point coordinates and direction index
 10
        let row = 0;
 11
         let col = 0;
 12
         let dirIndex = 0;
 13
 14
        // Iterate over each cell, decrementing the count of remaining cells
        for (; remainingCells > 0; --remainingCells) {
             result.push(matrix[row][col]); // Add the current cell's value to the result
             visited[row][col] = true; // Mark the current cell as visited
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 19
             // Calculate the indices for the next cell in the current direction
 20
             const nextRow = row + directions[dirIndex];
             const nextCol = col + directions[dirIndex + 1];
 21
 22
 23
            // Check if the next cell is out of bounds or already visited
            if (nextRow < 0 || nextRow >= rowCount || nextCol < 0 || nextCol >= colCount || visited[nextRow][nextCol]) {
 24
                dirIndex = (dirIndex + 1) % 4; // Change direction (right -> down -> left -> up)
 25
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 27
            // Move to the next cell in the updated/current direction
 28
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             row += directions[dirIndex];
 30
             col += directions[dirIndex + 1];
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 33
         return result; // Return the array containing the spiral order traversal of the matrix
 34 }
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Time and Space Complexity
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The time complexity of the function spiralOrder is 0(m * n) where m is the number of rows and n is the number of columns in the input matrix. This is because the function iterates over every element in the matrix exactly once.

The space complexity of the function, however, is not 0(1) as stated in the reference answer. Instead, it is 0(m * n) because the function uses a set vis to track visited elements, which in the worst-case scenario, can grow to contain every element in the matrix.