Problem Description

String

very small range of numbers around n.

Math

Hard

number that reads the same backward as forward. We're not allowed to consider the integer n itself, and if there are two palindromes equally close to n, we must return the smaller one. The closeness between two integers is defined by the absolute difference between them, so we are looking for the integer with the minimum absolute difference from n that is also a palindrome. Intuition

The problem asks for the closest integer to a given integer n, where the closest integer must be a palindrome. A palindrome is a

1. The nearest palindrome could be smaller or larger than n: We must check in both directions. 2. Palindromes of different lengths can be candidates: For example, if n is a 3-digit number, then 99 and 1001 (palindromes just

To find the closest palindrome, we can consider different cases. The following intuition helps us arrive at a solution:

- below and above the nearest 3-digit ones) might be closer than any other 3-digit palindrome. 3. We can focus on changing the first half of n: Any palindrome can be reflected by its first half. For example, to form palindromes
- near 12345, we could reflect 123 to form 12321, or change it slightly to 12221 (by reflecting 122) or 12421 (by reflecting 124). 4. There's no need to examine too many candidates: Because we're looking for the nearest palindrome, we only need to look at a
- 5. We pick the closest palindrome and resolve ties by choosing the smaller: This is done by comparing absolute differences and values directly. The solution creates potential candidates by examining numbers formed by reflecting the digits around the center of n and by
- compares the remaining candidates to find the one with the minimum absolute difference to n.

considering edge cases like 999→1001 (where all digits are 9). It then discards the original number n if it's already a palindrome and

Solution Approach The provided solution uses algorithmic techniques and a logical approach to determine the nearest palindrome. Here's how the implementation tackles the problem:

closest palindrome to 999).

statement asks for a different number.

would be much less efficient.

Example Walkthrough

Mirroring 11 gives us 111.

• abs(99 - 123) gives us 24.

• abs(1001 - 123) gives us 878.

abs(111 - 123) gives us 12.

• abs(121 - 123) gives us 2.

follows:

• 10 ** (1 - 1) - 1 which handles the case where the closest palindrome has one less digit and consists of all 9's (for example, 999 is the closest palindrome to 1000). • 10**1 + 1 which handles the case of a palindrome that has one more digit and starts and ends with a 1 (for example, 1001 is the

The int(n[: (1 + 1) >> 1]) gets the first half of the digits (more precisely, the first half rounded-up if the length is odd, due to the >> 1 which is equivalent to dividing by 2 using bit shifting).

consider the middle digit (for odd lengths) when creating the mirrored palindromes.

to 123 that is a palindrome, considering both smaller and larger potential palindromes.

• 10 ** (1 - 1) - 1, which for 123 gives us 99 (the largest 2-digit palindrome).

The solution then considers the numbers just below, equal to, and just above 12: these are 11, 12, and 13.

For each of these numbers, we generate a palindrome by mirroring the first half. For instance:

We add these palindromes to our set res. Now, res contains 99, 1001, 111, 121, and 131.

• 10 ** 1 + 1, which for 123 gives us 1001 (the smallest 4-digit palindrome).

First, the solution creates a set res to store potential palindromic numbers, including two edge cases:

- The loop for i in range(left 1, left + 2): generates palindromes by considering the reflected versions of numbers just below, equal to, and just above the first half of n. The if l % 2 == 0 condition checks the length of n to decide on whether or not to
- Within the loop, while j: is used to append the reversed digits of the first half to generate the full palindrome (i). Once complete, it adds these potential palindromes to the res set.

The line residiscard(x) ensures that the original number n is not considered if it is already a palindrome because the problem

Finally, the solution iterates through the set res to find the candidate with the smallest absolute difference to x. It does this by

considering both the difference and the value of t, using the abs() function to find the smallest absolute difference and resolve ties by choosing the smaller number.

In conclusion, the algorithm very efficiently narrows down the potential palindromes to consider and then picks the closest one by

numerical comparison. By doing so, it avoids the brute force approach of checking each number in the range individually, which

Now, we add our two edge cases to the set res:

First, we determine the length 1 of n. For 123, 1 is 3. We create a set res that we will use to store our potential palindrome candidates.

Let's work through a small example using the number 123. According to the solution approach, our goal is to find the closest integer

Next, we extract the first half of n. For 123, the first half (rounded up in the case of odd lengths) is 12. We will use this to generate palindromes that have the same first half as 123.

• Mirroring 13 gives us 131.

Mirroring 12 (which is n's exact first half) gives us 121.

Since 123 is not a palindrome, we don't need to discard it from our set res. If 123 were a palindrome, we would remove it from the set since we are looking for a different integer.

Finally, we iterate through our set res to determine which number has the smallest absolute difference to 123. We calculate as

• abs(131 - 123) gives us 8. The smallest difference is 2 for the palindrome 121. Since we are asked to return the closest palindrome and in case of a tie return

Convert the string to an integer for numerical operations

the smaller number, 121 is our answer as it is the closest palindrome to 123.

For even lengths, use the entire prefix.

j = i if num_length % 2 == 0 else i // 10

Remove the original number itself if it's in the set

Check for the smallest absolute difference

Convert the closest palindrome back to a string and return

// Get the first half of n (if odd, include the middle digit)

StringBuilder candidateBuilder = new StringBuilder();

candidateBuilder.append(i); // Append the first half

for (long i = firstHalf - 1; i <= firstHalf + 1; ++i) {</pre>

// Add the generated number to candidates

return candidates; // Return the set of candidates

candidates.remove(Long.parseLong(n));

// Main function to find the nearest palindrome

long firstHalf = Long.parseLong(n.substring(0, (length + 1) / 2));

candidates.add(Long.parseLong(candidateBuilder.toString()));

// Generate candidates by varying the first half from -1 to 1 and mirroring to get palindromes

// Remove the number itself if it's a palindrome, as we want the nearest different palindrome

// Mirror and append the reverse of the first half (excluding the middle digit if odd length)

candidateBuilder.append(new StringBuilder(Long.toString(i)).reverse().substring(length % 2));

if (closest_palindrome == -1 or

return str(closest_palindrome)

closest_palindrome = candidate

For odd lengths, exclude the last digit of the prefix.

Append the reverse of 'j' to 'i' to construct the palindrome

If the absolute difference is the same, choose the smaller number

abs(candidate - num) < abs(closest_palindrome - num) or</pre>

Python Solution 1 class Solution: def nearestPalindromic(self, n: str) -> str:

6 # Initialize a set with the smallest and largest possible palindromes # with different digit lengths compared to the input number 8 candidates = { 9 10**(num_length - 1) - 1, # Smallest palindrome with one less digit 10 11 10**num_length + 1 # Smallest palindrome with one more digit 12 13 # Find the higher and lower palindromes around the input number 14 # 'prefix' is the first half of the input number 15 $prefix = int(n[:(num_length + 1) // 2])$ 16 17 18 # Generate palindromes by varying the prefix by -1, 0, +1 for i in range(prefix - 1, prefix + 2): 19

num = int(n)

 $num_length = len(n)$

palindrome = i

candidates.discard(num)

while j > 0:

palindrome = palindrome * 10 + j % 10 27 28 i //= 10 29 30 # Add the constructed palindrome to the candidate set 31 candidates.add(palindrome) 32

(abs(candidate - num) == abs(closest_palindrome - num) and candidate < closest_palindrome)):</pre>

35 36 # Find the closest palindrome to the original number 37 $closest_palindrome = -1$ 38 for candidate in candidates:

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C++ Solution

2 public:

1 class Solution {

```
Java Solution
    class Solution {
         // Function to find the nearest palindromic number in string form
         public String nearestPalindromic(String n) {
             // Convert the input string to a long integer for comparison
             long number = Long.parseLong(n);
  6
             // Variable to store the closest palindrome number
             long closestPalindrome = -1;
  9
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 11
             // Get all potential palindrome candidates
 12
             for (long candidate : getPalindromeCandidates(n)) {
 13
                 // If this is the first candidate or it's closer to the input number than the current closest
                 // or equally close but smaller, then update the closest palindrome
 14
 15
                 if (closestPalindrome == -1 ||
 16
                     Math.abs(candidate - number) < Math.abs(closestPalindrome - number) ||
 17
                     (Math.abs(candidate - number) == Math.abs(closestPalindrome - number) && candidate < closestPalindrome)) {
 18
 19
                     closestPalindrome = candidate;
 20
 21
 22
             // Convert the closest palindrome back to a string and return it
 23
             return Long.toString(closestPalindrome);
 24
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         // Helper function to generate palindrome candidates based on the input string
 27
         private Set<Long> getPalindromeCandidates(String n) {
 28
             int length = n.length(); // Length of the input number
 29
             Set<Long> candidates = new HashSet<>(); // Set to store palindrome candidates
 30
 31
             // Add 9's (One less digit than n and all 9's) e.g. 999 for n=1000
 32
             candidates.add((long)Math.pow(10, length - 1) - 1);
             // Add 1 followed by all zeros and then a 1 (One more digit than n) e.g. 10001 for n=999
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 34
             candidates.add((long)Math.pow(10, length) + 1);
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```

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string nearestPalindromic(string n) {
             long originalNumber = stol(n); // Convert the original string to a long
             long closestPalindrome = -1; // Initialize the closest palindrome
  6
             // Loop through all possible palindromes and choose the nearest one
  8
             for (long candidate : getCandidates(n)) {
  9
 10
                 if (closestPalindrome == -1 ||
                     abs(candidate - originalNumber) < abs(closestPalindrome - originalNumber) ||</pre>
 11
                     (abs(candidate - originalNumber) == abs(closestPalindrome - originalNumber) && candidate < closestPalindrome)) {
 12
                     closestPalindrome = candidate;
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             return to_string(closestPalindrome); // Return the string representation of the nearest palindrome
 17
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 19
         // Helper function to generate possible palindromes
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         unordered_set<long> getCandidates(string& n) {
 21
             int length = n.size();
 22
             unordered_set<long> candidates;
 23
             // Add the edge cases: the largest number with one less digit and the smallest number with one more digit
 24
 25
             candidates.insert((long) pow(10, length -1) -1);
             candidates.insert((long) pow(10, length) + 1);
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 28
             // Get the first half of the original number and consider the number one less, one greater, and itself
             long firstHalf = stol(n.substr(0, (length + 1) / 2));
 29
             for (long i = firstHalf - 1; i <= firstHalf + 1; ++i) {</pre>
 30
                 string prefix = to_string(i); // First half as a string
 31
 32
 33
                 // Create a palindrome by appending the reverse of the prefix, considering odd/even length
 34
                 string candidate = prefix + string(prefix.rbegin() + (length & 1), prefix.rend());
 35
 36
                 // Add the generated palindrome to the set of candidates
                 candidates.insert(stol(candidate));
 37
 38
 39
 40
             // Remove the original number from the candidate set to ensure it's not considered as its own nearest palindrome
 41
             candidates.erase(originalNumber);
 42
 43
             return candidates; // Return the set of candidate palindromes
 44
 45
    };
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Typescript Solution
  1 // Main function to find the nearest palindrome
    function nearestPalindromic(n: string): string {
         const originalNumber: number = parseInt(n, 10); // Convert the original string to a number
         let closestPalindrome: number = −1; // Initialize the closest palindrome
         // Loop through all possible palindromes and choose the nearest one
  6
         for (const candidate of getCandidates(n)) {
             if (closestPalindrome === -1 ||
  8
                 Math.abs(candidate - originalNumber) < Math.abs(closestPalindrome - originalNumber) ||
  9
                 (Math.abs(candidate - originalNumber) === Math.abs(closestPalindrome - originalNumber) && candidate < closestPalindrome
 10
                 closestPalindrome = candidate;
 11
 12
```

return closestPalindrome.toString(); // Return the string representation of the nearest palindrome

// Add the edge cases: the largest number with one less digit and the smallest number with one more digit

// Get the first half of the original number and consider the number one less, one greater, and itself

// Create a palindrome by appending the reverse of the prefix, considering odd/even length

const firstHalf: number = parseInt(n.substr(0, Math.ceil(length / 2)), 10);

const reversedPrefix: string = prefix.split('').reverse().join('');

const candidateStr: string = prefix + reversedPrefix.substr(length % 2);

// Remove the original number from the candidate set to ensure it's not considered

const prefix: string = i.toString(); // First half as a string

for (let i: number = firstHalf - 1; i <= firstHalf + 1; i++) {</pre>

// Add the generated palindrome to the set of candidates

candidates.add(parseInt(candidateStr, 10));

40 // as its own nearest palindrome 41 candidates.delete(originalNumber); 42 43 return candidates; // Return the set of candidate palindromes 44 }

Time and Space Complexity

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The time complexity of the given code can be broken down as follows: 1. Calculating res by adding the smallest and largest possible palindrome numbers around the length of n, which is 0(1) since size

Time Complexity

2. Generation of near-by candidate palindromes involves constant time operations by iterating over a small range left - 1 to left + 2, which is 0(1).

of the res set remains constant regardless of the size of n.

elements (fixed size), the loop runs in 0(1) time.

17 // Helper function to generate possible palindrome candidates

const candidates: Set<number> = new Set<number>();

candidates.add(Math.pow(10, length -1) -1);

candidates.add(Math.pow(10, length) + 1);

function getCandidates(n: string): Set<number> {

const length: number = n.length;

- 3. Constructing palindromes involves a while loop that iterates approximately 1/2 times, where 1 is the length of n, resulting in
- O(len(n)) for each palindrome creation. Since we create at most three palindromes, the overall contribution is O(len(n)). 4. Discarding the original number x from the set res is also 0(1) as it's a single operation.

5. The final for loop to choose the best palindrome candidate iterates over the elements in res. Since res has a maximum of 5

- Overall, summing these contributions, the time complexity of the code is primarily dependent on the length of n, leading to 0(len(n)).
- The space complexity analysis is as follows: 1. A set res is created which holds at most 5 integers, thus contributing 0(1) space.
- 2. Temporary variables such as x, l, left, i, j, ans, and t are all constant space overhead, adding up to 0(1). Therefore, the total space complexity of the code is 0(1).

Space Complexity