318. Maximum Product of Word Lengths

Bit Manipulation Array String Medium

Problem Description

do not have any letters in common. More formally, we want to find the maximum value of length(word[i]) * length(word[j]) where word[i] and word[j] are such that no letter appears in both words simultaneously. If there are no such pairs of words that satisfy this condition, the function should return 0.

Given an array of strings named words, the goal is to find the maximum product of the lengths of any two words in the array that

Intuition

The straightforward approach to solve this problem would be to compare each pair of words and check if they have any common letters. However, this would require checking every pair which leads to a time complexity of O(n^2 * m), where n is the number of words and m is the average length of a word, rendering this approach inefficient for large input sizes. To optimize this, we can preprocess each word to create a bitmask that represents the set of characters of the word. In the

bitmask, the i-th bit is set if the word contains the i-th letter of the alphabet. Since there are only 26 lowercase English letters,

this bitmask can be represented by an integer. By comparing the bitmasks of two words, we can efficiently check if two words

have common letters. If the result of a bitwise AND operation between two masks is zero, then the two words do not share any common letters. With the bitmask precomputation step, the time complexity is reduced significantly because the comparison of every pair now only takes constant time, O(1), leading to an overall time complexity of O(n^2 + n * m). Here's a step-by-step breakdown of the solution approach:

1. Iterate through each word in the input, calculate its bitmask, and store these masks in an array. 2. Iterate through all pairs of words. For each pair, use the precomputed bitmasks to check if the words share common letters by performing a bitwise AND operation. 3. If the words do not share any common letters (bitwise AND result is 0), calculate the product of their lengths and update the answer with the maximum product found so far.

Solution Approach

4. After checking all pairs, return the maximum product found.

Calculate the number n of words in the input list.

■ Initialize mask[i] to 0.

time, greatly enhancing performance.

- The solution uses a bit manipulation technique along with an array for storing the bitmasks. Here's a step-by-step breakdown of the implementation:

corresponding to each letter.

Initial Setup

Creating Bitmasks Iterate through the list of words with the index i. For each word word[i], do the following:

o Initialize an array mask of length in to store the bitmasks which will represent the unique characters of each word by setting the bit position

- For each character ch in word[i], shift 1 left by ord(ch) ord('a') bits to create a bitmask for the letter.
 - Use the bitwise OR | operation to update mask[i] by turning on the bit corresponding to each character in the word. **Finding the Maximum Product** Initialize a variable ans to 0 for storing the maximum product found.

Iterate through all unique pairs of words with indices i and j (with j > i to avoid duplication of pairs), to compare their bitmasks.

 Update ans with the maximum of itself and the calculated product. **Returning the Result**

After checking all pairs, return ans as the final result.

The code uses bitmasks stored in an integer to efficiently represent and compare the characters of the words. Rather than checking each letter individually for every pair, the solution leverages bitwise operations to check for common letters in constant

■ If the bitwise AND & of mask[i] and mask[j] is 0, it means the words have no common letters.

Example Walkthrough Let's take an example array of strings words = ["abc", "de", "fg", "hi", "aeh"].

The first step is to represent each word by a bitmask. Let's work through the words:

∘ For word "abc", the bitmask would be (set bit positions at 0, 1, 2): 0b111 which is 7 in decimal.

• For word "de", the bitmask would be (set bit positions at 3, 4): 0b11000 which is 24 in decimal.

In the next step, we will look for pairs of words with no overlapping bits in their bitmasks:

If so, calculate the product of their lengths len(words[i]) * len(words[j]).

• For word "fg", the bitmask would be (set bit positions at 5, 6): 0b1100000 which is 96 in decimal. ∘ For word "hi", the bitmask would be (set bit positions at 7, 8): 0b110000000 which is 384 in decimal. • For "aeh", the bitmask is (set bit positions at 0, 4, 7): 0b10010001 which is 145 in decimal. As a result, the mask array after processing the words array would be [7, 24, 96, 384, 145].

○ Compare "abc" (7) and "de" (24): (7 & 24) equals Ø which means no common letters. Product of lengths equals 3 * 2 = 6.

Compare "abc" (7) and "fg" (96): (7 & 96) equals 0; product is 3 * 2 = 6. • Compare "abc" (7) and "hi" (384): (7 & 384) equals 0; product is 3 * 2 = 6.

"fg" with "aeh", and "hi" with "aeh".

def max product(self, words: List[str]) -> int:

Create a list to store the bitmask representation of each word

Compare every pair of words to find the maximum product of lengths

if masks[i] & masks[i] == 0: # No common characters

// Create an array to store the bitmask representation of each word

// Set the bit corresponding to the character 'c'

of two words which have no characters in common (no common bits in the bitmask).

max_product = max(max_product, len(words[i]) * len(words[j]))

// Convert each word into a bitmask representation and store it in the bitMasks array

// Compare each pair of words to find the pair with the maximum product of lengths

// Update max product if this pair gives us a bigger product

// Function to calculate the maximum product of lengths of two words that don't share common characters

// Create bitmasks. Each bit in a mask represents if a character ('a' to 'z') is in the word

// If two words have no common letters, their masks will not share any common bits

maxProduct = Math.max(maxProduct, words[i].length * words[j].length);

// Update max product if this pair gives us a bigger product

const wordsCount: number = words.length; // Count of the words in the array

const masks: number[] = new Array(wordsCount); // Bitmasks for each word

maxProduct = max(maxProduct, (int)(words[i].size() * words[j].size()));

Update max product if this pair has a larger product

Generate a bitmask for each word where bit i is set if the

Get the number of words in the list

Solution Implementation

num words = len(words)

masks = [0] * num_words

for i in range(num words - 1):

Return the maximum product found

// Get the length of the words array

int[] bitMasks = new int[length];

for (int i = 0; i < length; ++i) {</pre>

// Initialize the maximum product to 0

// Return the maximum product found

function maxProduct(words: string[]): number {

for (let i = 0; i < wordsCount; ++i) {</pre>

for (const char of words[i]) {

for (let i = 0; i < wordsCount - 1; ++i) {</pre>

let maxProduct = 0; // Initialize max product to be 0

for (let j = i + 1; j < wordsCount; ++j) {</pre>

if ((masks[i] & masks[i]) === 0) {

// The bitwise AND of their masks will be 0

Create a list to store the bitmask representation of each word

Compare every pair of words to find the maximum product of lengths

common characters. The analysis of time and space complexity is as follows:

since each word's bitmask is compared with every other word's bitmask.

of two words which have no characters in common (no common bits in the bitmask).

Generate a bitmask for each word where bit i is set if the

word contains the i-th letter of the alphabet

masks[i] |= 1 << (ord(ch) - ord('a'))

// Initialize all masks to 0

// Compare each pair of words

// Return the maximum product found

num words = len(words)

masks = [0] * num_words

for ch in word:

max_product = 0

for i, word in enumerate(words):

Initialize max_product to 0

for i in range(num words - 1):

for j in range(i + 1, num words):

return maxProduct;

masks.fill(0);

return maxProduct;

};

TypeScript

for (char c : words[i].toCharArray()) {

bitMasks[i] |= (1 << (c - 'a'));

int length = words.length;

for j in range(i + 1, num words):

from typing import List

class Solution:

Python

•

○ Compare "abc" (7) and "aeh" (145): (7 & 145) is not 0 as they share letters, so do not calculate product. Compare "de" (24) and "fg" (96): (24 & 96) equals 0; product is 2 * 2 = 4.

Compare "de" (24) and "hi" (384): (24 & 384) equals 0; product is 2 * 2 = 4.

○ Compare "de" (24) and "aeh" (145): (24 & 145) is not 0, so do not calculate product.

Compare "hi" (384) and "aeh" (145): (384 & 145) equals 0; product is 2 * 3 = 6.

- Compare "fg" (96) and "hi" (384): (96 & 384) equals 0; product is 2 * 2 = 4. Compare "fg" (96) and "aeh" (145): (96 & 145) equals 0; product of lengths is 2 * 3 = 6.
- The final step is to find the maximum product from these comparisons: The calculated products are 6, 6, 6, 4, 4, 4, 6, 6.
- The maximum product is 6. Return the maximum product, which is 6. The words yielding this product are "abc" with "de", "abc" with "fg", "abc" with "hi",
- individually. The final solution would implement the process outlined in the "Solution Approach" section efficiently by leveraging bitwise operations and precomputation of the bitmasks for each word.

This illustrates how the bitmask approach greatly simplifies the computation and avoids the overhead of checking each letter

word contains the i-th letter of the alphabet for i, word in enumerate(words): for ch in word: masks[i] |= 1 << (ord(ch) - ord('a')) # Initialize max_product to 0

Java class Solution { public int maxProduct(String[] words) {

return max_product

int maxProduct = 0;

max_product = 0

```
// where the words do not share any common characters
        for (int i = 0; i < length - 1; ++i) {
            for (int i = i + 1; i < length; ++i) {
                // Check if the two words share any common characters using the '&' bitwise operator
                if ((bitMasks[i] & bitMasks[j]) == 0) {
                    // Calculate the product of the lengths of the two words
                    int product = words[i].length() * words[j].length();
                    // Update maxProduct with the maximum value between the existing maxProduct and the current product
                    maxProduct = Math.max(maxProduct, product);
        // Return the maximum product found
        return maxProduct;
C++
#include <vector>
#include <string>
#include <algorithm>
using namespace std;
class Solution {
public:
    int maxProduct(vector<string>& words) {
        int wordsCount = words.size(); // Count of the words in the vector
        vector<int> masks(wordsCount); // Bitmasks for each word
        // Create bitmasks. Each bit in mask represents if a character ('a' to 'z') is in the word
        for (int i = 0; i < wordsCount; ++i) {
            for (char ch : words[i]) {
                masks[i] |= 1 << (ch - 'a'); // Set the bit corresponding to the current character
        int maxProduct = 0; // Initialize max product to be 0
        // Compare each pair of words
        for (int i = 0; i < wordsCount - 1; ++i) {
            for (int j = i + 1; j < wordsCount; ++j) {</pre>
                // If two words have no common letters, their masks will not share any common bits
                // The bitwise AND of their masks will be 0
                if (!(masks[i] & masks[i])) {
```

// Import statements are not necessary in plain TypeScript, and there are no direct equivalents for `vector` and `using namespace sto

masks[i] |= 1 << (char.charCodeAt(0) - 'a'.charCodeAt(0)); // Set the bit corresponding to the current character

from typing import List class Solution: def max product(self, words: List[str]) -> int: # Get the number of words in the list

if masks[i] & masks[i] == 0: # No common characters # Update max product if this pair has a larger product max_product = max(max_product, len(words[i]) * len(words[j])) # Return the maximum product found return max_product Time and Space Complexity The provided code calculates the maximum product of the lengths of two words such that the two words do not share any

Time Complexity

words.

Checking for common characters and updating the maximum product happens in constant time, 0(1), for each pair of words compared.

Calculating the bitmask for each word: The first loop goes through each word and each character within those words to

create a bitmask. This process occurs in O(N * L) time, where N is the number of words, and L is the average length of the

Comparing the bitmasks: The nested loop compares each pair of generated bitmasks. This results in O(N^2) comparisons,

Since typically L <= 1000 and the main contributing factor for large inputs is N, and because N^2 grows faster than N * L, the N^2 term dominates for large N, so the overall time complexity can be considered $O(N^2)$.

Combining these steps, the overall time complexity is $0(N * L + N^2)$.

- **Space Complexity** The space used to store the bitmasks: For N words, we store a bitmask for each, which uses O(N) space.
 - No additional significant space is used, since other variables use constant space.
- Hence, the space complexity of the code is O(N).