2080. Range Frequency Queries Design Binary Search Medium Hash Table Segment Tree Array Leetcode Link

Problem Description

for fast frequency queries.

value within a given subarray of an integer array. A subarray is a sequence of contiguous elements from the array, and the frequency of a value is how often it appears within that sequence. To solve this, one must implement a class RangeFreqQuery with two functionalities:

This problem involves creating a data structure that can efficiently find the frequency, or the number of occurrences, of a particular

1. A constructor that takes an integer array arr and prepares it for subsequent queries. 2. A query method that, given a left and right index (left and right) and a value (value), returns how many times value appears

between arr[left] and arr[right], inclusive.

remains static after the data structure is constructed. Here's how the solution works:

- Since the array is not modified after the data structure is created, the problem statements suggest preprocessing the array to allow
- Intuition

The solution strategy is based on preprocessing the given array to make querying efficient. We make use of the fact that the array

1. Preprocessing: Instead of checking the frequency of a value each time the query is called, we build a hashmap (or dictionary in

Python) upon the class initialization. This hashmap maps each unique value in the array to a list of indices where this value occurs. Because each value is appended in the order of appearance, each list of indices is sorted.

the left and right boundaries within the preprocessed list of indices for that value. Specifically, we find: The first index in the list that is greater than or equal to left. If left is not in the list, we find the smallest index that is greater than left.

2. Answering Queries: To find the frequency of a value in a particular range, we use binary search to quickly find the position of

- The last index in the list that is less than or equal to right. If right is not in the list, we find the largest index that is less than or equal to right. The Python module bisect provides the bisect_right function, which can be used to find these indices.
- 3. Calculating Frequency: The frequency is then the difference between the positions found in the list for right and left. Since bisect_right returns a position one past the last occurrence when searching for right, subtracting these two positions directly
- So, the intuition lies in transforming the problem from repetitive frequency counting into a single preprocessing step followed by fast binary search queries.

The implementation of the RangeFreqQuery class involves two core components:

When an object of RangeFreqQuery is created, the constructor takes an input array arr and preprocesses it. The constructor uses a

hashmap (self.mp) to store the frequencies. It iterates over the array using enumerate to access both the index i and the value x at

that index. Then, it appends the index 1 to the list corresponding to the value x in the hashmap. This creates a mapping of each

unique value to a sorted list of indices where it appears in arr.

gives the correct frequency.

Solution Approach

1 self.mp = defaultdict(list) for i, x in enumerate(arr): self.mp[x].append(i)

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Querying query(self, left: int, right: int, value: int) -> int
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searches using bisect_right from the bisect module:

l, r = bisect_right(arr, left - 1), bisect_right(arr, right)

value before the left index.

1 if value not in self.mp:

Example Walkthrough

appear within specified subarrays of arr.

We initialize the RangeFreqQuery object with arr.

During the initialization, the object creates a hashmap that will look like this:

1. Call the query method with left = 2, right = 6, and value = 2.

This means there are 0 occurrences of 2 before the index '2'.

4. Next, we do a similar search for right, which is 6.

Each unique value from arr is now mapped to a sorted list of indices where it appears.

3 arr = self.mp[value]

5 return r - 1

Here's a breakdown of the initialization steps:

Initialization __init__(self, arr: List[int])

including the right index. The frequency is then the difference r - 1, which is the count of value in the subarray starting at left and ending at right. The following is the code for the query method:

The guery method is where we find out the frequency of value between the left and right index in the array. We perform two binary

1. Search for the insertion point for left - 1 in the sorted list of indices for value. This gives us 1, the number of occurrences of

2. Search for the insertion point for right in the same sorted list. This gives us r, the number of occurrences of value up to and

Notice that we return 0 when the value is not found in self.mp, as it indicates the value does not appear in the array. Otherwise, we calculate the frequency using the binary search results and return it.

In summary, the solution involves a combination of hashmap for preprocessing and binary search for efficient queries. By using these

algorithms and data structures, the RangeFreqQuery class allows us to quickly compute the frequency of a value over different subarrays following a single preprocessing pass.

Let's say we have the following array arr = [1, 1, 2, 3, 2, 2, 4, 1, 2], and we want to find out how often particular values

2 1: [0, 1, 7], 2: [2, 4, 5, 8], 3: [3], 4: [6]

Now, let's suppose we want to find out how often the value 2 appears between indices 2 and 6 (left = 2, right = 6). We perform

2. Look for the sorted list of indices for the value 2 in our hashmap, which is [2, 4, 5, 8]. 3. Using the bisect_right function from the bisect module, we find the insertion point for left - 1, which is 1 in this case. bisect_right([2, 4, 5, 8], 1) will return 0 because 1 would fit at the start of the list.

following Python code:

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20 # Example query

Python Solution

from typing import List

class RangeFreqQuery:

Java Solution

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1 import java.util.HashMap;

import java.util.ArrayList;

2 import java.util.List;

import java.util.Map;

class RangeFreqQuery {

1 from collections import defaultdict

from bisect import bisect_left, bisect_right

def __init__(self, arr: List[int]):

self.index_map = defaultdict(list)

from collections import defaultdict

for i, x in enumerate(arr):

self.mp[x].append(i)

def query(self, left, right, value):

21 print(rangeFreqQuery.query(2, 6, 2)) # Output: 3

if value not in self.mp:

return 0

from bisect import bisect_right

the following steps:

 There are 3 occurrences of 2 up to and including index 6. 5. The frequency of value 2 between indices 2 and 6 is therefore 3 - 0 = 3.

Putting it all together, if we wanted to illustrate this using the RangeFreqQuery class and the querying process, we would write the

class RangeFreqQuery: def __init__(self, arr): self.mp = defaultdict(list)

(inclusive). This walk-through demonstrates the efficiency and effectiveness of the solution approach.

bisect_right([2, 4, 5, 8], 6) will return 3 since 6 would fit between 5 and 8.

arr = self.mp[value] l, r = bisect_right(arr, left - 1), bisect_right(arr, right) 15 return r - l 16 17 # Initialize with the given array rangeFreqQuery = RangeFreqQuery([1, 1, 2, 3, 2, 2, 4, 1, 2])

In this example, the print statement would output 3, as the value 2 occurs three times in the subarray of arr from indices 2 to 6

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for index, value in enumerate(arr):
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                self.index_map[value].append(index)
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       def query(self, left: int, right: int, value: int) -> int:
           # Check if the value is not in the index map, returning 0 frequency.
            if value not in self.index_map:
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                return 0
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           # Find the closest index at the left and right boundary using binary search.
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            indices = self.index_map[value]
           # bisect_left to find start position inclusively, while bisect_right for the end position exclusively.
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            start_position_inclusive = bisect_left(indices, left)
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            end_position_exclusive = bisect_right(indices, right)
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           # Calculate the frequency by subtracting end and start position.
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            frequency = end_position_exclusive - start_position_inclusive
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            return frequency
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  # Example of how to instantiate and use the RangeFreqQuery class:
29 # obj = RangeFreqQuery(arr)
30 # freq = obj.query(left, right, value)
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private Map<Integer, List<Integer>> indexMap = new HashMap<>();

// Queries the frequency of a value in the specified range.

// It uses binary search to find the frequency of the value.

// It maps each number to its indices in the array.

public int query(int left, int right, int value) {

List<Integer> indices = indexMap.get(value);

int endIndex = binarySearch(indices, right);

int startIndex = binarySearch(indices, left - 1);

// Helper method to perform a binary search on a list of indices.

// Finds the first index where 'targetValue' could be inserted.

private int binarySearch(List<Integer> list, int targetValue) {

if (!indexMap.containsKey(value)) {

return endIndex - startIndex;

int right = list.size();

for (int i = 0; i < arr.length; i++) {</pre>

public RangeFreqQuery(int[] arr) {

return 0;

int left = 0;

return left;

// The class could be used as follows:

// Constructor to initialize the data structure with the given array.

// If the value is not present in the array, return 0 frequency

indexMap.computeIfAbsent(arr[i], k -> new ArrayList<>()).add(i);

// Find the starting index where the value could be inserted to maintain sorted order.

// Find the ending index where the value could be inserted to maintain sorted order.

// The frequency is the difference between the start and end insertion points.

Dictionary to store the indices of each value in the array.

Iterate through the list and map each value to its indices.

while (left < right) {</pre> 41 42 int mid = (left + right) >> 1; // Equivalent to (left + right) / 2 if (list.get(mid) > targetValue) { 43 right = mid; 44 45 } else { left = mid + 1;46

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// RangeFreqQuery obj = new RangeFreqQuery(arr);
   // int frequency = obj.query(left, right, value);
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C++ Solution
   #include <vector>
 2 #include <unordered_map>
   #include <algorithm> // includes std::upper_bound
  class RangeFreqQuery {
 6 public:
       // HashMap that stores each distinct number and its indices in the input array
       std::unordered_map<int, std::vector<int>> numToIndicesMap;
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       // Constructor that fills the HashMap for the given array
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       RangeFreqQuery(std::vector<int>& arr) {
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           for (int i = 0; i < arr.size(); ++i)
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               numToIndicesMap[arr[i]].push_back(i); // Appends the current index to the corresponding number's vector
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       // Method to return the frequency of 'value' within the range [left, right]
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       int query(int left, int right, int value) {
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           // If 'value' is not found in the map, return 0 as its frequency is 0
18
           if (numToIndicesMap.find(value) == numToIndicesMap.end()) return 0;
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           // References the vector of indices for 'value'
22
           auto& indices = numToIndicesMap[value];
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           // Find the position in the vector for the first index greater than 'left - 1' (upper_bound is exclusive)
           auto leftIt = std::upper_bound(indices.begin(), indices.end(), left - 1);
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           // Find the position in the vector for the first index greater than 'right'
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           auto rightIt = std::upper_bound(indices.begin(), indices.end(), right);
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           // The frequency is the number of elements in the range [leftIt, rightIt)
           return rightIt - leftIt;
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33 };
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35 // The RangeFreqQuery class can be used as follows:
36 // RangeFreqQuery* obj = new RangeFreqQuery(arr);
37 // int frequency = obj->query(left, right, value);
Typescript Solution
  // Import necessary features from array and algorithm modules (hypothetical imports)
   // In TypeScript/JavaScript, there's no standard library providing an upper_bound function like C++'s <algorithm>,
   // so we'll need to create it or use a third-party library that implements algorithmic functions.
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let numToIndicesMap: { [key: number]: number[] } = {}; // equivalent to unordered_map in C++

numToIndicesMap[value].push(index); // Append the current index to the corresponding number's array

return start; // end and start both will be pointing to the first element greater than target

// Find the position for the first index greater than 'left - 1' (simulating upper_bound exclusive nature)

// Function to 'construct' the numToIndicesMap with indices

function upperBound(arr: number[], target: number): number {

31 // Function to return the frequency of 'value' within the range [left, right]

function query(left: number, right: number, value: number): number {

// Find the position for the first index greater than 'right'

// The frequency is the count of elements in the range [leftIndex, rightIndex)

let mid = Math.floor((start + end) / 2);

let leftIndex = upperBound(indices, left - 1);

let rightIndex = upperBound(indices, right);

function rangeFreqQueryConstructor(arr: number[]): void {

arr.forEach((value, index) => {

let start = 0, end = arr.length;

if (arr[mid] <= target) {</pre>

start = mid + 1;

if (!(value in numToIndicesMap)) {

return rightIndex - leftIndex;

Time and Space Complexity

end = mid;

while (start < end) {

} else {

if (!numToIndicesMap[value]) {

numToIndicesMap[value] = [];

// Helper function to mimic the 'std::upper_bound'

return 0; // If 'value' is not found, its frequency is 0 34 35 36 let indices = numToIndicesMap[value]; // Get the array of indices for 'value' 37 38

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});

_init__ constructor: • The time complexity for initializing the RangeFreqQuery class is O(n), where n is the length of the input array. This is because the

Time Complexity

indices in the array. query method:

constructor iterates through all n elements to populate the self.mp dictionary, which maps each unique value to a list of its

The query method utilizes binary search twice through the bisect_right function to find the range of positions of a particular

value between indices left and right. Therefore, the time complexity for each query is 0(log k), where k is the number of

occurrences of the value being queried (k can be at most n).

Space Complexity • The self.mp dictionary stores lists of indices for each unique value in the array. In the worst case, the space complexity is O(n),

if all values are unique and each value appears only once. This would mean that the self.mp dictionary would have n keys with a single index in each list. In summary, the time complexity is O(n) for the constructor and $O(\log k)$ for each query, and the space complexity is up to O(n).