800. Similar RGB Color

Easy Math String Enumeration

Problem Description

In this problem, we are dealing with hexadecimal color codes. A hexadecimal color code is a 7 character string, starting with a '#' followed by six hexadecimal digits. Each pair of digits represents a color in RGB (Red, Green, and Blue) format with values ranging from `00` to `FF`. For example, in `#AABBCC`, `AA` is for Red, `BB` for Green, and `CC` for Blue.

Sometimes, these color codes can be abbreviated if each pair of digits is the same. For example, `#AABBCC` can be abbreviated to `#ABC` because `AA = A`, `BB= B`, and `CC = C`.

The problem asks us to find the color in shorthand hexadecimal notation (`#XYZ`) that is most similar to the provided color (`#ABCDEF`) and return it as a string. The similarity between two colors `#ABCDEF` and `#UVWXYZ` is defined as `-(AB - UV)^2 - (CD - WX)^2 - (EF - YZ)^2`.

To clarify, we need to minimize the differences between the corresponding color components (AB and UV for Red, CD and WX for Green, EF and YZ for Blue) of the full hexadecimal color code and its shorthand, corresponding the given color code (`#ABCDEF`), to find the most similar shorthand color (`#XYZ`).

Intuition

The key here is to understand that for each color component (Red, Green, Blue) in the full color code, we are looking for the closest shorthand approximation which can be only one of the `00`, `11`, `22`, ..., `EE`, `FF` values in hexadecimal. Since `11` in hexadecimal is `17` in decimal, it essentially means each color component can be divided by `17` to find the nearest shorthand value.

In the given solution, the `f` function takes a two-digit hexadecimal string and returns the shorthand notation for that specific component. The first step is to convert the two-digit hexadecimal number to decimal and then to perform an integer division by 17 which gives us the multiplier for the shorthand notation. We also use the modulo operation to find the remainder, and if the remainder is greater than 8 (`x > 8`) we need to round up, otherwise we keep the quotient as it is.

Next, we use `format` to convert the decimal value back to a two-digit hexadecimal notation after multiplying by 17. This operation essentially snaps the original color component to its closest shorthand approximation.

Finally, we apply this `f` function to each of the red (`color[1:3]`), green (`color[3:5]`), and blue (`color[5:7]`) components of the given `color`, concatenate the results, and prefix with a '#' to return the most similar shorthand color.

Solution Approach

The solution follows a step-by-step approach to find the most similar shorthand RGB notation to a given 6-digit RGB color. Let's walk through the algorithm and patterns used:

1. **Define a Helper Function `f`:** This function takes a two-digit hexadecimal component of the original color and finds the nearest shorthand value. The input is a string representing a two-digit hexadecimal value (e.g. `AA`, `BC`, etc.).
2. **Conversion to Decimal:** Inside the `f` function, the two-digit hexadecimal value is converted to its decimal equivalent using `int(x, 16)`, where `x` is the hexadecimal string and `16` is the base for conversion.
3. **Find Nearest Shorthand Multiplier:** The decimal number is then divided by `17` using `divmod(int(x, 16), 17)`, which returns a quotient and a remainder. This division is based on the fact that the shorthand values in hexadecimal (`00`, `11`, `22`, ..., `EE`, `FF`) correspond to multiples of `17` in decimal.
4. **Rounding the Multiplier:** Depending on the remainder (`z`), if it is greater than `8`, the multiplier (`y`) is increased by `1` for rounding to the nearest shorthand value.
5. **Conversion Back to Hexadecimal:** The closest shorthand multiplier is then multiplied by `17` and converted back into a two-digit hexadecimal value using Python's `format` function: `'{:02x}'.format(17 * y)`.
6. **Applying the Helper Function:** The main function (`similarRGB`) extracts the individual color components from the given color code (`color`), which are `color[1:3]` for red, `color[3:5]` for green, and `color[5:7]` for blue.
7. **Construct the Result String:** The helper function `f` is applied to each extracted component to get the shorthand hexadecimal values. These are then concatenated in order to form the resulting shorthand color starting with `#`.

It is important to note that this is more of a mathematical problem than an algorithmic one since we're performing direct calculations to find the nearest values and don't need to iterate over a set of possibilities or maintain any data structures. The solution optimizes the calculation by utilizing the unique property of hexadecimal color codes and the way they are presented in shorthand notations.

Example Walkthrough

Let's go through an example to illustrate the solution approach. Assume we are given the color `#09ABCD`. Our task is to find the closest shorthand hexadecimal color notation.

Here are the steps we'd follow according to the solution approach:

1. **Define a Helper Function `f`:** This function finds the nearest shorthand value for any two-digit hexadecimal string input it receives.
2. **Conversion to Decimal:** For the first component (red) `09`, we convert it to decimal which gives us `int('09', 16) = 9`.
3. **Find Nearest Shorthand Multiplier:** Next, we divide `9` by `17` which gives us `y = 0` and a remainder `z = 9` (since `9 < 17`).
4. **Rounding the Multiplier:** Since `z > 8`, we increase `y` by `1`, leading to `y = 1`.
5. **Conversion Back to Hexadecimal:** We now convert the shorthand multiplier `y = 1` into hexadecimal. `1` multiplied by `17` is `17`, which is `11` in hexadecimal (`'{:02x}'.format(17 * y) = '11'`).
6. **Applying the Helper Function:** Repeat steps 2 to 5 for the green and blue components:
   - Green: `AB` in decimal is `171`. `171 / 17` is `10` with a remainder of `1`, hence `y = 10`. In hexadecimal, `10` is `A` and no rounding is needed (`z < 8`).
   - Blue: `CD` in decimal is `205`. `205 / 17` gives a quotient of `12` and a remainder of `1` (`205 = 12 * 17 + 1`), so `y = 12`. `12` in hexadecimal is `C` and no rounding is needed.
7. **Construct the Result String:** The concatenation of the shorthand hex values we have computed with `#` reads `#1AC`. So `#1AC` is the shorthand hexadecimal color notation that is the most similar to `#09ABCD`.

Solution Implementation

Python

```python
class Solution:
    def similarRGB(self, color: str) -> str:
        # Helper function to find the closest similar value in terms of RGB
        def get_similar_value(comp_hex):
            # Convert the two hexadecimal digits to an integer
            comp_int = int(comp_hex, 16)
            # Divide the integer by 17 to find the closest factor of 17 (0x11), since we are working with values in the form of 0x11
            major, remainder = divmod(comp_int, 17)
            if remainder > 8:
                # If the remainder is greater than half of 17, increase the major by 1 to find the closer factor of 17
                major += 1
            # Return the string reorepresentation of the new similar component, formatted as two hexadecimal digits
            return '{:02x}'.format(17 * major)

        # Extract the red, green, and blue components from the hexadecimal color string
        red_component = color[1:3]
        green_component = color[3:5]
        blue_component = color[5:7]

        # Get the closest similar color by aaplying the helper function to each RGB component
        # Then, concatenate the '#' symbol with the new similar components to form the hexadecimal color string
        return f'#{get_similar_value(red_component)}{get_similar_value(green_component)}{get_similar_value(blue_component)}'
```

Java

```java
class Solution {
    // Method to find the most similar color in hexadecimal RGB format
    public String similarRGB(String color) {
        // Extracting the red, green, and blue components from the input color string
        String redComponent = color.substring(1, 3);
        String greenComponent = color.substring(3, 5);
        String blueComponent = color.substring(5, 7);

        // Constructing the similar color by finding the closest component values
        return "#" + getClosestColorComponent(redComponent) +
                     getClosestColorComponent(greenComponent) +
                     getClosestColorComponent(blueComponent);
    }

    // Helper method to find the closest component value
    private String getClosestColorComponent(String component) {
        // Converting the hexadecimal string to an integer
        int value = Integer.parseInt(component, 16);

        // Finding the nearest multiple of 17 (0x11), since all similar colors
        // have components that are multiples of 17
        value = value / 17 + (value % 17 > 8 ? 1 : 0);

        // Returning the component as a 2-digit hexadecimal string
        return String.format("%02x", 17 * value);
    }
}
```

C++

```cpp
class Solution {
public:
    // Method to find the closest similar color in hexadecimal RGB format
    string similarRGB(string color) {
        // Extracting the red, green, and blue components from the input color string
        string redComponent = color.substr(1, 2);
        string greenComponent = color.substr(3, 2);
        string blueComponent = color.substr(5, 2);

        // Constructing the similar color by finding the closest component values
        return "#" + getClosestColorComponent(redComponent) +
                     getClosestColorComponent(greenComponent) +
                     getClosestColorComponent(blueComponent);
    }

private:
    // Helper method to find the closest component value
    string getClosestColorComponent(string component) {
        // Converting the hexadecimal component to an integer
        int value = stoi(component, nullptr, 16);

        // Nearest multiple of 17 (0x11), since all similar colors
        // have components that are multiples of 17 (0x11 is hex for 17)
        value = value / 17 + (value % 17 > 8 ? 1 : 0);

        // Preparing the nearest value by multiplying it by 17
        int roundedValue = 17 * value;

        // Formatting the component as a two-digit hexadecimal string
        char formattedComponent[3];
        sprintf(formattedComponent, "%02x", roundedValue);

        // Return the formatted string
        return formattedComponent;
    }
};
```

TypeScript

```typescript
// Function to find the most similar color in hexadecimal RGB format
function similarRGB(color: string): string {
  // Extracting the red, green, and blue components from the input color string
  const redComponent = color.substring(1, 3);
  const greenComponent = color.substring(3, 5);
  const blueComponent = color.substring(5, 7);

  // Constructing the similar color by finding the closest component values
  return "#" + getClosestColorComponent(redComponent) +
               getClosestColorComponent(greenComponent) +
               getClosestColorComponent(blueComponent);
}

// Helper function to find the closest component value
function getClosestColorComponent(component: string): string {
  // Converting the hexadecimal string to an integer
  let value = parseInt(component, 16);

  // Finding the nearest multiple of 17 (0x11), since all similar colors
  // have components that are multiples of 17
  value = Math.floor(value / 17) + (value % 17 > 8 ? 1 : 0);

  // Returning the component as a 2-digit hexadecimal string
  return toTwoDigitHex(17 * value);
}

// Helper function to convert a number to a 2-digit hexadecimal string
function toTwoDigitHex(num: number): string {
  // Creating a hexadecimal string with padding to ensure 2 digits are returned
  const hex = num.toString(16);
  return hex.length === 1 ? '0' + hex : hex;
}
```

```python
class Solution:
    def similarRGB(self, color: str) -> str:
        # Helper function to find the closest similar value in terms of RGB
        def get_similar_value(comp_hex):
            # Convert the two hexadecimal digits to an integer
            comp_int = int(comp_hex, 16)
            # Divide the integer by 17 to find the closest factor of 17 (0x11), since we are working with values in the form of 0x11
            major, remainder = divmod(comp_int, 17)
            if remainder > 8:
                # If the remainder is greater than half of 17, increase the major by 1 to find the closer factor of 17
                major += 1
            # Return the string reorepresentation of the new similar component, formatted as two hexadecimal digits
            return '{:02x}'.format(17 * major)

        # Extract the red, green, and blue components from the hexadecimal color string
        red_component = color[1:3]
        green_component = color[3:5]
        blue_component = color[5:7]

        # Get the closest similar color by aaplying the helper function to each RGB component
        # Then, concatenate the '#' symbol with the new similar components to form the hexadecimal color string
        return f'#{get_similar_value(red_component)}{get_similar_value(green_component)}{get_similar_value(blue_component)}'
```

Time and Space Complexity

Time Complexity

The time complexity of the function `similarRGB` primarily depends on the operations involving string slicing and calculations for each of the three components of the color code (red, green, and blue). Each call to `f(x)` involves parsing the component as hexadecimal, performing a division and conditional operation, and then formatting the result back into a string. Since these operations are constant in time for a given two-character string, and there are only three such strings in the input, the overall time complexity is `O(1)`.

Space Complexity

As for the space complexity, the function uses a fixed amount of extra space for the variables `a`, `b`, `c`, and the result of the formatting operation inside `f(x)`. The space required does not change with the size of the input, as the input is always a fixed-sized string representing the color code. Therefore, the space complexity is also `O(1)`.