661. Image Smoother

Matrix

Problem Description

image is represented as a 2D integer matrix, where each cell contains a grayscale value. The smoother considers the value of a cell and the values of the eight surrounding cells to calculate an average. This average is then rounded down and placed into the corresponding cell in the resulting image. When cells on the edges or corners of the image do not have eight surrounding cells, the smoother only averages over the existing neighbouring cells. The challenge is to apply this filter correctly, ensuring that boundary conditions are handled and only valid neighbours are included in the average calculation. Intuition

The task is to write an algorithm for an "image smoother," which is a filter operation applied to each cell of a grayscale image. The

The solution approach involves a nested loop to traverse each cell in the image. For each cell, a sub-loop considers the

surrounding cells within a distance of 1 cell in all directions. To manage cells at the edges and corners that have fewer neighbours, the algorithm checks if each potential neighbouring cell is within the image boundaries before including it in the average calculation. The steps are:

4. Check if the neighbouring cell is within the image boundaries (its indexes are neither less than 0 nor exceeding the image dimensions).

updated based on its neighbours.

1. Loop over each cell in the input image.

- 2. Initialize sum (s) and count (cnt) variables for each cell. The sum will hold the total grayscale value sum of the neighbours, and count will keep track of the number of valid neighbours considered. 3. Use a nested loop to go through each of the surrounding cells, including the cell itself.

8. Return the resulting image matrix after the smoother has been applied to all cells.

5. If the cell is within bounds, add its value to the sum and increment the count.

- 6. After considering all valid neighbours, calculate the average by dividing the sum by the count. 7. Assign the rounded down average to the corresponding cell in the output image matrix.
- Solution Approach

j-1 to j+1, attempting to cover all nine cells in the block including the center cell.

used (// in Python), which gives us a rounded down result as required.

The calculated average is then assigned to the corresponding cell in the ans matrix.

Here's a detailed breakdown of the solution approach:

The algorithm starts by determining the dimensions of the image matrix, which are stored in variables m and n, representing the number of rows and columns, respectively.

An output matrix ans of the same dimensions as the input (img) is created to store the smoothed values. This is initialized to

The implementation of the image smoother involves tackling the problem with a brute-force approach, where each cell's value is

zero for all cells. A nested for loop is used to traverse through each cell of the image matrix img using row index i and column index j.

- For each cell (i,j), we initialize s and cnt to zero. Here s will accumulate the sum of the grayscale values of the current cell and its valid neighbours, while cnt will count the number of valid neighbouring cells considered in the smoothing operation
- (including the cell itself).

Another nested for loop iterates over the cells in the 3×3 block centered at (i, j). The ranges of these loops are i-1 to i+1 and

For every neighbouring cell, the algorithm checks if its coordinates (x, y) are within the image's boundaries using $0 \ll x \ll y$

and 0 <= y < n. This ensures we do not attempt to access cells outside the array, which would result in an 'index out of

Once all valid neighbours are considered, the algorithm computes the average value by dividing s by cnt. Integer division is

- range' error. Only valid neighbours are included in the average calculation by adding their values to the s and incrementing the cnt.
- After the completion of both nested loops, the matrix ans is fully populated with the smoothed values and is returned as the final result.
- The simplicity of the brute-force approach makes it an uncomplicated solution that is easy to understand and implement.
- the smoothing filter is fixed and small. **Example Walkthrough**

Let's illustrate the solution approach using a small example. Imagine we have the following 3×3 grayscale image matrix:

because we are visiting each cell surrounding every cell in the matrix. Using brute force is acceptable here because the size of

However, it does have a time complexity of O(m x n x k), where k is the number of neighbouring cells to consider (in this case, 9),

[100, 200, 100], [200, 300, 200], [100, 200, 100]] This matrix represents the grayscale values for a 3×3 image. Now, let's walk through the steps to apply the image smoother for

We create an output matrix ans with the same dimensions, all initialized to zero:

[0, 0, 0]]

the central cell (1,1) with the value 300.

covers all nine cells in the block.

s = 100+200+100+200+300+200+100+200+100 = 1500

cnt = 9 (including the central cell itself)

Using a nested for loop, we traverse each cell. We'll focus on the central cell (i=1, j=1). Initially, let s = 0 and cnt = 0.

The nested for loop runs over the neighbours of the central cell. The loop ranges from i-1 to i+1 and j-1 to j+1, meaning it

As all cells are within the boundary for the central cell, we add each cell's value to s and increment cnt for each cell. So we end up with:

We check each cell in this range to see if they are within the boundaries.

We determine the dimensions of the image, which here are m = 3 and n = 3.

We calculate the average grayscale value by integer division of s by cnt, which is 1500 // 9 = 166.

The average is then 600 // 4 = 150.

returned as the result of the smoothed image.

• cnt = 4.

class Solution:

[0, 0, 0], [0, 166, 0], 0, 0]]

The same approach is repeated for other edge cells, considering the valid neighbors. Once all cells are processed, ans matrix is

10. After repeating steps 3-9 for all other cells and adjusting the boundary cases accordingly, the final smoothed image matrix becomes:

[[150, 183, 150], [183, 166, 183], [150, 183, 150]

Here's how the boundary cases are averaged for top-left corner cell (i=0, j=0):

We place the average value in the central cell of the output:

The value 150 is placed in the top-left cell of the output matrix.

• s = 100+200+200+300, as only 4 cells (including itself) are valid neighbors.

Solution Implementation **Python**

Initialize an output image with the same dimensions, filled with zeros

Initialize the sum and count of neighboring pixels

Calculate the smoothed value for the current pixel

smoothed_image[row][col] = pixel_sum // pixel_count

def imageSmoother(self, img: List[List[int]]) -> List[List[int]]:

smoothed_image = [[0] * num_cols for _ in range(num_rows)]

pixel_count += 1

Get the number of rows and columns in the image

num_rows, num_cols = len(img), len(img[0])

Iterate through each pixel in the image

pixel_sum = pixel_count = 0

for col in range(num_cols):

for row in range(num_rows):

Return the smoothed image

public int[][] imageSmoother(int[][] img) {

// Get the dimensions of the image

Check all 9 positions in the neighborhood (including the pixel itself) for neighbor_row in range(row - 1, row + 2): for neighbor_col in range(col - 1, col + 2): # Ensure the neighbor is within image boundaries before including it

if 0 <= neighbor_row < num_rows and 0 <= neighbor_col < num_cols:</pre>

pixel_sum += img[neighbor_row][neighbor_col]

by taking the average of the sum of the neighborhood pixels

```
return smoothed_image
Java
```

class Solution {

```
int rows = img.length;
        int cols = img[0].length;
       // Initialize the smoothed image array
        int[][] smoothedImg = new int[rows][cols];
       // Iterate through each pixel in the image
        for (int i = 0; i < rows; ++i) {
            for (int j = 0; j < cols; ++j) {
                int sum = 0; // Sum of pixel values in the smoothing window
                int count = 0; // Number of pixels in the smoothing window
                // Iterate through the neighboring pixels including the current pixel
                for (int x = i - 1; x \le i + 1; ++x) {
                    for (int y = j - 1; y \le j + 1; ++y) {
                        // Check if the neighbor is within the image boundaries
                        if (x >= 0 \&\& x < rows \&\& y >= 0 \&\& y < cols) {
                            count++; // Increment the pixel count
                            sum += img[x][y]; // Add the pixel value to the sum
                // Compute the average pixel value and assign it to the smoothed image
                smoothedImg[i][j] = sum / count;
       // Return the smoothed image
       return smoothedImg;
C++
class Solution {
public:
    vector<vector<int>> imageSmoother(vector<vector<int>>& image) {
                                       // Number of rows in the image
        int rows = image.size();
       int cols = image[0].size();  // Number of columns in the image
```

// Create a 2D vector with the same dimensions as the input image to store the result

int sum = 0; // Sum of the surrounding cell values including itself

int count = 0; // Counter for the number of cells included in the sum

// Check if the neighboring cell (x, y) is within the bounds of the image

// Iterate through the neighboring cells centered at (i, j)

// Calculate the smoothed value and assign it to the result image

Initialize an output image with the same dimensions, filled with zeros

Initialize the sum and count of neighboring pixels

for neighbor_col in range(col - 1, col + 2):

Calculate the smoothed value for the current pixel

Check all 9 positions in the neighborhood (including the pixel itself)

pixel_sum += img[neighbor_row][neighbor_col]

Ensure the neighbor is within image boundaries before including it

if 0 <= neighbor_row < num_rows and 0 <= neighbor_col < num_cols:</pre>

resultImage[row][col] = Math.floor(sum / count);

def imageSmoother(self, img: List[List[int]]) -> List[List[int]]:

smoothed_image = [[0] * num_cols for _ in range(num_rows)]

for neighbor_row in range(row - 1, row + 2):

pixel count += 1

Get the number of rows and columns in the image

num_rows, num_cols = len(img), len(img[0])

Iterate through each pixel in the image

pixel_sum = pixel_count = 0

for col in range(num_cols):

// Return the smoothed image

for row in range(num_rows):

Time and Space Complexity

return resultImage;

class Solution:

vector<vector<int>> smoothedImage(rows, vector<int>(cols));

for (int x = i - 1; $x \le i + 1$; ++x) {

for (int y = j - 1; $y \le j + 1$; ++y) {

// Iterate through each cell in the image

for (int j = 0; j < cols; ++j) {

for (int i = 0; i < rows; ++i) {

```
if (x >= 0 \&\& x < rows \&\& y >= 0 \&\& y < cols) {
                                           // Increment the counter for each valid cell
                            count++;
                            sum += image[x][y]; // Add the cell value to the sum
                // Compute the average value of the surrounding cells and assign to the corresponding cell in the result
                smoothedImage[i][j] = sum / count;
        // Return the resulting smooth image
        return smoothedImage;
};
TypeScript
function imageSmoother(img: number[][]): number[][] {
    // Get the dimensions of the image
    const rows = img.length;
    const cols = img[0].length;
   // Define the relative positions of the neighbors around a pixel
    const neighborOffsets = [
        [-1, -1], [-1, 0], [-1, 1],
        [0, -1], [0, 0], [0, 1],
        [1, -1], [1, 0], [1, 1]
    ];
    // Initialize the result image with the same dimensions
    const resultImage = new Array(rows).fill(0).map(() => new Array(cols).fill(0));
    for (let row = 0; row < rows; row++) {</pre>
        for (let col = 0; col < cols; col++) {</pre>
            let sum = 0; // Sum of the pixel values in the smooth box
            let count = 0; // Number of pixels in the smooth box
            // Iterate through all neighbors including the current pixel
            for (const [offsetRow, offsetCol] of neighborOffsets) {
                const neighborRow = row + offsetRow;
                const neighborCol = col + offsetCol;
                // Check if the neighbor is within the image boundaries
                if (neighborRow >= 0 && neighborRow < rows && neighborCol >= 0 && neighborCol < cols) {</pre>
                    sum += img[neighborRow][neighborCol]; // Add the neighbor's value to the sum
                    count++; // Increase the pixel count
```

by taking the average of the sum of the neighborhood pixels smoothed_image[row][col] = pixel_sum // pixel_count # Return the smoothed image return smoothed_image

n is the number of columns. For each cell (i, j), it considers up to 9 neighboring cells (including the cell itself) in a 3×3 grid. This nested iteration contributes a constant factor of 9 for each cell, because the innermost two loops (over x and y) run at most 3

Time Complexity

times each. Thus, the total time complexity is 0(m * n * 9), which simplifies to 0(m * n) since 9 is a constant factor and does not affect the asymptotic complexity.

The given code iterates through every cell of the img matrix, represented by dimensions mxn, where m is the number of rows and

Space Complexity

The space complexity comes from the additional matrix ans that is created to store the smoothed values. It's the same size as the

input matrix img, so the space complexity is 0(m * n). No additional space is used that grows with the size of the input, as the variables s (sum of the neighbor values) and cnt (the count of neighbors considered) use constant space. Therefore, the total space complexity remains 0(m * n).