1828. Queries on Number of Points Inside a Circle Medium Geometry

Leetcode Link

Problem Description

This problem presents a geometric challenge involving both points on a plane and circles described by a center and a radius. You are

Array

Math

provided with two arrays; the first, points, contains coordinates of various points on a 2D plane, and the second, queries, contains the specifications for several circles. Each entry in queries provides the central coordinates of a circle and its radius. The task is to determine how many points from the points array fall within or on the boundary of each circle described in queries. To

fall within or on the boundary, a point's distance from the center of the circle must be less than or equal to the circle's radius. For each circle in queries, the output should be the count of such points, and these counts are to be returned as an array.

The key aspect to consider here is the definition of a point being inside a circle. Geometrically, a point (x, y) is inside or on the

boundary of a circle with center (xc, yc) and radius r if the distance from (x, y) to (xc, yc) is less than or equal to r. The distance between the two points is calculated using the Pythagorean theorem, which in this case does not require the square root calculation because we can compare the squares of the distances directly to the square of the radius. Intuition

To find the intuitive solution to this problem, think about the standard way of measuring distance between two points on a plane -

#### through the Pythagorean theorem. Usually, the formula $\sqrt{(x^2 - x^1)^2 + (y^2 - y^1)^2}$ is used, where (x1, y1) and (x2, y2) are coordinates of two points. In the context of a circle, a point lies inside or on the circle if this distance is less than or equal to the

radius of the circle.

However, since comparing distances can be done without extracting the square root, the formula simplifies to (x2 - x1)^2 + (y2 y1)^2 <= r^2. This squared comparison avoids unnecessary computation of square roots, makes the program run faster, and is helpful for counting points within the radius.

points array. For each point, we calculate this squared distance from the point to the circle's center and compare it to the square of the radius. If the squared distance is less than or equal to the squared radius, we increment a count. After checking all points for a particular circle, we append the total count to our answer array, and then proceed to the next circle.

We arrive at our solution by iterating over each circle described in queries, and for each circle, we go through every point in the

The solution, therefore, follows a straight-forward brute-force approach. Its efficiency could, however, be improved by eliminating the need to calculate the distance for all points with respect to all circles, possibly by pre-sorting or partitioning the points. Solution Approach

utilizes basic data structures from Python's standard library, namely lists, to store the sequence of points and queries and to accumulate the answer. The algorithm follows two nested loops to compare each point with every circle.

The solution provided in Python makes use of a direct implementation of the brute-force approach discussed in the intuition. It

### Initialize an empty list named ans which will store the number of points inside each circle. 1 ans = []

Here's a step by step explanation of the algorithm:

boundary. This counter will be reset for each circle.

y) and the radius r. 1 for x, y, r in queries: 3. Inside the outer loop, we initialize a counter cnt to zero for counting how many points are within the current circle including on its

2. The outer loop iterates over every circle query in the queries list. For each circle, the loop retrieves the center coordinates (x,

4. A nested inner loop runs through every point in points, where i and j are the x and y coordinates of the current point being checked.

1 for i, j in points:

1 cnt = 0

coordinates dx = i - x, the difference in y coordinates dy = j - y, and then summing their squares dx \* dx + dy \* dy. 1 dx, dy = i - x, j - y

6. It then checks if this squared distance is less than or equal to the square of the radius r \* r. If this condition is true, it means

the point is inside or on the boundary of the circle, so it increments the counter cnt.

5. For each point, the solution calculates the squared distance from the point to the circle's center using the difference in x

7. After the inner loop has finished checking all points, the inner loop ends, and the code appends the count for the current circle to the ans array.

boundary of each circle.

Example Walkthrough

• points = [(1, 3), (3, 3), (5, 3)]

queries = [((2, 3), 2), ((4, 3), 1)]

1. Point (1, 3): dx = 1 - 2 = -1, dy = 3 - 3 = 0

2. Point (3, 3): dx = 3 - 2 = 1, dy = 3 - 3 = 0

Squared distance = 1^2 + 0^2 = 1

Squared distance = (-1)^2 + 0^2 = 1

1 <= 4 (True), so this point is inside the circle.</p>

1 <= 4 (True), so this point is also inside the circle.</li>

9 <= 4 (False), so this point is outside the circle.</p>

There are 2 points inside or on the boundary of the first circle.

9 <= 1 (False), so this point is outside the circle.</li>

1 <= 1 (True), so this point is on the boundary of the circle.</li>

public int[] countPoints(int[][] points, int[][] queries) {

// Prepare an array to store the results for each query

// Extract the coordinates of the point

int distanceX = pointX - centerX;

int distanceY = pointY - centerY;

// Retrieve the center and radius of the current query circle

// Return the array containing the count of points within each circle

// Loop through each point to check if it is inside the query circle

// Calculate the distance from the point to the center of the circle

if (distanceX \* distanceX + distanceY \* distanceY <= radius \* radius) {</pre>

// Check if the point is within the circle by comparing the squares of the distances

// Increment the counter for this query if the point is inside the circle

// Determine the number of queries to process

int queryCount = queries.length;

// Loop through each query

int[] answer = new int[queryCount];

for (int k = 0; k < queryCount; ++k) {</pre>

int centerX = queries[k][0];

int centerY = queries[k][1];

int radius = queries[k][2];

for (int[] point : points) {

int pointX = point[0];

int pointY = point[1];

++answer[k];

1 <= 1 (True), so this point is also on the boundary of the circle.</li>

1 ans.append(cnt)

1 cnt += dx \* dx + dy \* dy <= r \* r

checking using squares avoids the need for math library calls, which improves computation time, but still, the solution has a time complexity of O(n \* m), where n is the number of points and m is the number of queries, which is not efficient for larger datasets.

There are no additional data structures or sophisticated patterns employed in this solution. It relies on the fact that distance

Let's consider a simple example to illustrate the solution approach. Suppose we have the following points and queries:

We're supposed to find out how many points fall within or on the boundary of each circle described by the queries.

8. Finally, once all queries have been checked, the function returns the list ans which contains the count of points inside or on the

Query 1 Center (x, y) = (2, 3), Radius (r) = 2 For each point, calculate the squared distance to the center and compare it to the squared radius (r^2 = 4):

#### 3. Point (5, 3): dx = 5 - 2 = 3, dy = 3 - 3 = 0Squared distance = 3^2 + 0^2 = 9

Query 2 Center (x, y) = (4, 3), Radius (r) = 1

2. Point (3, 3): dx = 3 - 4 = -1, dy = 3 - 3 = 0

3. Point (5, 3): dx = 5 - 4 = 1, dy = 3 - 3 = 0

Squared distance = 1^2 + 0^2 = 1

Squared distance = (-1)^2 + 0^2 = 1

Perform the same steps with  $r^2 = 1$ :

1. Point (1, 3): dx = 1 - 4 = -3, dy = 3 - 3 = 0 Squared distance = (-3)^2 + 0^2 = 9

There is 1 point inside or on the boundary of the second circle. In summary, the counts for each query are [2, 1]. Thus, the final returned list of counts would be [2, 1], indicating that two points

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Python Solution
   from typing import List
   class Solution:
       def countPoints(self, points: List[List[int]], queries: List[List[int]]) -> List[int]]:
           # Initialize an empty list for storing the answer
           answer = []
           # Iterate over each query which consists of a circle defined by (x, y, r)
           for center_x, center_y, radius in queries:
               # Initialize the count of points inside the current circle
                count = 0
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               # Check each point to see if it lies within the circle
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                for point_x, point_y in points:
14
15
                   # Calculate the horizontal (dx) and vertical (dy) distance of the point from the circle's center
16
                   dx, dy = point_x - center_x, point_y - center_y
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18
                   # Check if the point is inside the circle using the equation of a circle
                   if dx * dx + dy * dy <= radius * radius:</pre>
19
20
                       # If the point is inside the circle, increment the count
21
                       count += 1
22
23
               # After checking all points, append the count of the current circle to the answer list
24
               answer.append(count)
25
26
           # Return the list containing the count of points within each circle
27
           return answer
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Java Solution
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are within or on the boundary of the first described circle, and one point is within or on the boundary of the second described circle.

# C++ Solution

return answer;

class Solution {

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#include <vector>
   using std::vector;
   class Solution {
   public:
       // Function to count points that are within each circular query region
       vector<int> countPoints(vector<vector<int>>& points, vector<vector<int>>& queries) {
           vector<int> results; // This will hold the final count of points for each query
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           // Loop over each query, which defines a circle
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           for (auto& query : queries) {
11
               int centerX = query[0]; // X coordinate of the circle's center
13
               int centerY = query[1]; // Y coordinate of the circle's center
14
               int radius = query[2]; // Radius of the circle
15
               int count = 0;
                                      // Count of points inside the circle
16
               // Compare each point with the current query circle
               for (auto& point : points) {
                   int pointX = point[0]; // X coordinate of the point
20
                   int pointY = point[1]; // Y coordinate of the point
21
22
                   // Calculate squared distance from the point to the center of the circle
23
                   int dx = pointX - centerX;
24
                   int dy = pointY - centerY;
                   // If the distance is less than or equal to the radius squared, increment count
26
                   if (dx * dx + dy * dy <= radius * radius) {
27
                       count++;
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               // Store the count of points in the result vector
31
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               results.push_back(count);
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           // Return the vector with counts for each query
           return results;
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38 };
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Typescript Solution
 1 // Function to count points within each circular query region.
 2 // points: an array of arrays where each sub-array contains 2 integers representing the x and y coordinates of a point
```

## **Time Complexity** The time complexity of the provided code is O(n \* m), where n is the number of points and m is the number of queries. This is

Time and Space Complexity

// Initialize counter for the number of points within the current circle let count = 0; // Iterate through each point 15 for (const [pointX, pointY] of points) { // Calculate the distance from the point to the center of the circle 16 const distance = Math.sqrt((centerX - pointX) \*\* 2 + (centerY - pointY) \*\* 2); 18 // If the distance is less than or equal to the radius, the point is inside the circle 19 if (distance <= radius) {</pre> 20 21 count++; 22 23 24 25 // Return the count of points within the circle for the current query 26 return count; 27 });

// queries: an array of arrays where each sub-array represents a circle with a center at (x, y) and radius r

// Map through each query and calculate the number of points within the circle defined by the query

function countPoints(points: number[][], queries: number[][]): number[] {

const [centerX, centerY, radius] = query;

// Destructure the query into center x, center y, and radius

return queries.map(query => {

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28 }

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// Returns an array of integers where each integer represents the number of points inside a corresponding query circle.

The space complexity of the code is O(m), where m is the number of queries. This is due to the fact that we are only using an additional list ans to store the results for each query. The size of this list grows linearly with the number of queries, therefore the space complexity is directly proportional to the number of queries.

of the query circle. **Space Complexity** 

because there are two nested loops: the outer loop iterates over each query (which is m in number), and the inner loop iterates over

each point (which is n in number). In the inner loop, we are doing a constant-time computation to check if a point is within the radius