1208. Get Equal Substrings Within Budget

String] Binary Search Prefix Sum Sliding Window Medium

Problem Description

In this problem, we are given two strings s and t of equal length, and an integer maxCost. The objective is to convert string s into string t by changing characters at corresponding positions. Each change comes with a cost, which is the absolute difference in the ASCII values of the characters in the same position in both strings. We aim to find the maximum length of a substring of s that can be transformed into the corresponding substring of t without exceeding a given maxCost. If no substring from s can be changed within the cost constraints, the function should return 0.

Intuition

problems where a running condition—like a fixed sum or cost—needs to be maintained.

The solution to this problem involves using the two-pointer technique, which is commonly applied to array or string manipulation

Here, the idea is to iterate over the strings with two pointers, i and j, marking the beginning and end of the current substring being considered. We start with both pointers at the beginning of the strings and calculate the cost of changing the current

characters of s to match t. This cost is added to a running total sum. If at any point the sum exceeds maxCost, we need to move the j pointer (the start of the substring) to the right, effectively shortening the substring and reducing our total cost by removing the cost of changing the character at the j th position.

We continue to move the i pointer to the right, expanding the substring, and checking if the conversion cost still stays within maxCost. After each step, we update our result ans with the maximum length of a valid substring found so far, which is the

considered every possible substring starting at every possible point in s. The intuition behind the sliding window is that we are looking for the longest possible contiguous sequence (the window) within s and t where the total conversion cost does not exceed maxCost. By sliding the window along the strings, we can explore all options in linear time without the need for nested loops, which would significantly increase the computational complexity.

difference between our two pointers plus one (to account for zero-based indexing). This process continues until we've

Here's a step-by-step breakdown of the algorithm used in the solution:

the given maxCost.

Solution Approach

Initialize: on to store the length of the strings s and t, ensuring that the length is the same for both.

The provided solution code implements the sliding window technique to track the longest substring that can be changed within

Two pointers, j to mark the start and i as the current position in the string, which together define the bounds of the current substring.

- A variable ans to store the maximum length of a substring that meets the cost condition.
 - Iterate over each character in both strings using the i pointer. For every iteration:

A variable sum to keep track of the cumulative cost of changing characters from s to t.

If at any point the sum is greater than maxCost, enter a while loop that will:

zero-indexing), and update ans with the maximum length found so far.

fly, exemplifies the efficiency of the sliding window algorithm in such problems.

 Subtract the cost associated with the j th character (start of the current substring) from sum. Increment j to effectively shrink the window and reduce the cost, as we are now removing the starting character of our substring. After adjusting j to ensure sum doesn't exceed maxCost, calculate the current substring length by i - j + 1 (accounting for

Calculate the cost (absolute character difference) between the ith character of s and t, and add it to the sum.

possible substring that can be transformed from s into t without exceeding the maxCost. Notice that there are no nested loops; the two pointers move independently, which ensures that the complexity of the solution is

0(n), where n is the length of the strings. This single pass through the data, while adjusting the window's starting point on the

Continue iterating until all potential substrings have been considered. As a result, ans will hold the length of the longest

The code finishes execution once the end of string s is reached, and returns the length of the longest substring with the transformation cost within the given budget, maxCost.

substring we can change from s to t without exceeding the maxCost. Initial Setup:

Let's consider an example with strings s = "abcde", t = "axcyz", and maxCost = 6. We need to find the length of the longest

First Character:

Example Walkthrough

 i = ∅, comparing 'a' from s with 'a' from t, the cost is ∅ (since they are the same). o sum = 0, and sum <= maxCost.</pre>

Pointers i = 0 and j = 0, marking the current character and the start of the substring, respectively.

 Since sum now exceeds maxCost, we cannot include this character in our substring, and ans remains 1. **Third Character:**

Second Character:

 With j now at 1 and i incrementing to 2, we compare 'c' with 'c' and the cost is 0. sum = 0 (we discarded the previous sum since we moved j), and sum <= maxCost.
</p>

Move j to the right (j = 1) to remove the cost of the first character.

○ i = 1, comparing 'b' from s with 'x' from t, the cost is | 'b' - 'x' | = 22.

 \circ Length n = 5 (since both strings are of length 5).

 \circ Therefore, ans becomes i - j + 1 = 1.

sum = 22, which is greater than maxCost.

Sum sum = 0, to keep track of the cumulative cost.

Answer ans = 0, to store the maximum length of a valid substring.

Fourth Character:

s to t without exceeding maxCost. Therefore, the answer to this example is 3.

max length - the maximum length of a substring that satisfies the cost condition

Calculate the cost for the current index by taking the absolute difference of

If the total cost exceeds the max cost, shrink the window from the left till

Return the maximum length of a substring that can be obtained under the given cost

total cost -= abs(ord(s[start_index]) - ord(t[start_index]))

 \circ i = 3, comparing 'd' from s with 'y' from t, the cost is |'d' - 'y'| = 21.

Fifth Character: ○ i = 4, comparing 'e' with 'z' gives a cost of | 'e' - 'z' | = 21.

 \circ ans is updated to i - j + 1 = 3.

• sum = 21, which is still within maxCost.

 \circ ans is updated to i - j + 1 = 2.

This brings sum to 21 again (as the cost for 'e' and 'z' is 21), and ans remains 3.

Solution Implementation

Initialize variables:

for end index in range(n):

while total cost > max cost:

start_index += 1

n - length of the input strings

class Solution:

Python

Iterate over the characters in both strings

def equalSubstring(self, s: str, t: str, max_cost: int) -> int:

total cost - accumulated cost of transforming s into t

the character codes of the current characters of s and t

total_cost += abs(ord(s[end_index]) - ord(t[end_index]))

the total cost is less than or equal to max_cost

public int equalSubstring(String s, String t, int maxCost) {

// Two pointers for the sliding window approach

int end; // End index of the current window

currentCost += abs(s[end] - t[end]);

for (end = 0; end < length; ++end) -</pre>

while (currentCost > maxCost) {

// Two pointers for the sliding window approach

for (end = 0; end < length; ++end) {</pre>

let end: number; // End index of the current window

int start = 0; // Start index of the current window

maxLength = max(maxLength, end - start + 1);

function equalSubstring(s: string, t: string, maxCost: number): number {

let start: number = 0: // Start index of the current window

maxLength = Math.max(maxLength, end - start + 1);

const length: number = s.length; // Stores the length of the input strings

let currentCost: number = 0; // Current cost of making substrings equal

// Iterate through the string with the end pointer of the sliding window

currentCost += Math.abs(s.charCodeAt(end) - t.charCodeAt(end));

// Iterate through the string with the end pointer of the sliding window

// If the currentCost exceeds maxCost, shrink the window from the start

++start; // Move the start pointer forward to shrink the window

return maxLength; // Return the maximum length of equal substring within maxCost

let maxLength: number = 0; // Stores the maximum length of equal substring within maxCost

// Calculate the cost of making s[end] and t[end] equal and add it to currentCost

// Calculate the length of the current window and update maxLength if necessary

// Calculate the cost of making s[end] and t[end] equal and add it to currentCost

// Calculate the length of the current window and update maxLength if necessary

currentCost -= abs(s[start] - t[start]); // Reduce the cost of the start character

start index - start index for the current substring

Adding this cost makes sum = 42, which exceeds maxCost.

n = len(s)total cost = 0 start index = 0 max_length = 0

At the end of our iteration, ans holds the value 3, which is the length of the longest valid substring that could be changed from

We must move j right again; now j should be at position 3, where 'd' is located in s, and subtract the cost of 'd' and 'y'.

Update max length if the length of the current substring (end_index - start_index + 1) # is greater than the previously found max length max_length = max(max_length, end_index - start_index + 1)

return max_length

Java

class Solution {

```
// Length of the input strings
        int length = s.length();
        // This will hold the cumulative cost of transformations
        int cumulativeCost = 0;
        // This will keep track of the maximum length substring that meets the condition
        int maxLength = 0;
        // Two-pointer technique:
        // Start and end pointers for the sliding window
        for (int start = 0, end = 0; end < length; ++end) {
            // Calculate and add the cost of changing s[end] to t[end]
            cumulativeCost += Math.abs(s.charAt(end) - t.charAt(end));
            // If the cumulative cost exceeds maxCost, shrink the window from the start
            while (cumulativeCost > maxCost) {
                // Remove the cost of the starting character as we're about to exclude it
                cumulativeCost -= Math.abs(s.charAt(start) - t.charAt(start));
                // Move the start pointer forward
                ++start;
            // Update the maximum length found so far (end - start + 1 is the current window size)
            maxLength = Math.max(maxLength, end - start + 1);
        // Return the final maximum length found
        return maxLength;
C++
class Solution {
public:
    int equalSubstring(string s, string t, int maxCost) {
        int length = s.size(); // Stores the length of the input strings
        int maxLength = 0; // Stores the maximum length of equal substring within maxCost
        int currentCost = 0; // Current cost of making substrings equal
```

// If the currentCost exceeds maxCost, shrink the window from the start while (currentCost > maxCost) { currentCost -= Math.abs(s.charCodeAt(start) - t.charCodeAt(start)); // Reduce the cost of the start character ++start; // Move the start pointer forward to shrink the window

};

TypeScript

```
return maxLength; // Return the maximum length of equal substring within maxCost
class Solution:
   def equalSubstring(self, s: str, t: str, max_cost: int) -> int:
       # Initialize variables:
       # n - length of the input strings
       # total cost - accumulated cost of transforming s into t
       # start index - start index for the current substring
       # max length - the maximum length of a substring that satisfies the cost condition
       n = len(s)
       total cost = 0
       start index = 0
       max_length = 0
       # Iterate over the characters in both strings
       for end index in range(n):
           # Calculate the cost for the current index by taking the absolute difference of
           # the character codes of the current characters of s and t
           total cost += abs(ord(s[end index]) - ord(t[end index]))
           # If the total cost exceeds the max cost, shrink the window from the left till
           # the total cost is less than or equal to max cost
           while total cost > max cost:
               total cost -= abs(ord(s[start_index]) - ord(t[start_index]))
               start_index += 1
           # Update max length if the length of the current substring (end_index - start_index + 1)
           # is greater than the previously found max length
           max_length = max(max_length, end_index - start_index + 1)
       # Return the maximum length of a substring that can be obtained under the given cost
       return max_length
```

Time Complexity The time complexity of the given code is O(n), where n is the length of the strings s and t. This linear time complexity arises

Time and Space Complexity

loop does not add to the overall time complexity since it only moves the j pointer forward and does not result in reprocessing of any character — the total number of operations in the while loop across the entire for loop is proportional to n. **Space Complexity**

from the single for loop that iterates over each character of the two strings exactly once. Inside the loop, there are constant-time

operations such as calculating the absolute difference of character codes and updating the sum. The while loop inside the for

The space complexity of the given code is 0(1) because the extra space used by the algorithm does not grow with the input size

n. The variables sum, j, and ans use a constant amount of space, as do the indices i and n which store fixed-size integer

values. There are no data structures used that scale with the size of the input.