Problem Description

by four '1's that are placed in the grid in such a way that they form the corners of an axis-aligned rectangle. Importantly, the interior of this rectangle can contain any mix of '0's and '1's; the only requirement is that the four corners are '1's. The grid, grid, is composed entirely of '0's and '1's, and its dimensions are m x n where m is the number of rows and n is the number of columns. The task is to return the total count of such distinct corner rectangles.

The given LeetCode problem asks us to count the number of distinct "corner rectangles" in a 2D grid. A "corner rectangle" is defined

To solve this problem, we leverage the fact that a rectangle is defined by its two opposite corners. Here, we iterate over all potential

Intuition

'1's in another row, forming a rectangle. To efficiently track this, we employ a counting strategy that uses a dictionary to remember how many times we've seen each pair of '1's in the same row. Whenever we encounter a pair of '1's in the same row, we check the dictionary to see if this pair has been seen before. If it has, then for each previous occurrence, there is a distinct rectangle. Therefore, the count of rectangles is incremented by the number of times the pair has been seen before. Afterwards, we increment the counter for that pair, indicating that we've found another potential set

corner pairs in the grid and try to determine if these pairs can form the upper two or lower two corners of a rectangle. We do this by

checking if we picked two '1's in the same row. For each pair of '1's in the row, we check to see if the same pair of columns also have

of top corners for future rectangles. The algorithm iterates over all rows and, within each row, all pairs of '1's. By using a counter dictionary that keeps track of pairs of indices where '1's are found, it ensures that the process of finding rectangular corners is efficient, avoiding checking every possible rectangle explicitly, which would be computationally expensive especially for large grids.

Solution Approach The solution employs a simple yet efficient approach using a hash table to keep track of the count of '1' pairs encountered so far. Here's a step-by-step walkthrough of how the code works:

Initialize a variable ans to 0, which will hold the final count of corner rectangles.

2. Iterate Over the Grid:

1. Initialize Variables:

 Create a Counter object named cnt from the Python collections module. This counter will map each pair of column indices (i, j) to the number of times that pair has been observed in grid with '1's.

- The first for loop iterates through each row of the grid.
- 3. Find Pairs of '1's in the Same Row:
 - Within each row, use a nested for loop with enumerate to get both the index i and value c1 at that index. If c1 is '1', it means we have a potential top/left corner of a rectangle.

Another nested for loop is used to check to the right of the current '1' for another '1' at index j, forming a pair of top corners

- 4. Check for Potential Top/Right Corners:
 - (i, j) of a potential rectangle.
- 5. Count and Update Rectangles:
 - count represents another row where a rectangle with these top corners can be completed. After counting the rectangles for (i, j), update cnt[(i, j)] by incrementing by 1 which signifies that we have found

This solution utilizes a smart counting approach to avoid checking each potential rectangle directly, which drastically reduces the

time complexity. The main algorithmic techniques include iterating over array elements and using hash-based counters for an

For each such pair (i, j), if they can form the top two corners of a rectangle, we increment ans by cnt [(i, j)] since each

After all rows and valid pairs are processed, return ans as the total count of corner rectangles found in the grid.

another pair of '1's that can form the top corners of potential future rectangles.

elegant and efficient solution. By checking only rows for pairs of '1's and then counting and updating the number of potential rectangles as more pairs are found, the solution effectively captures all corner rectangles without unnecessary computations.

Example Walkthrough

[1, 0, 1],

1 grid = [

6. Return the Answer:

Let's walk through a small example to illustrate how the solution approach works. Consider the following grid which is a 4×3 matrix containing both 0's and 1's.

[1, 1, 1], [1, 0, 0], [1, 0, 1] 1. Initialize Variables:

2. Iterate Over the Grid:

o ans starts at 0.

o cnt is an empty Counter object.

 Start with the first row [1, 0, 1]. 3. Find Pairs of '1's in the Same Row:

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• Identify two '1's in the row at index i = 0 and j = 2.
4. Check for Potential Top/Right Corners:
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Since cnt[(0, 2)] is not in cnt, ans remains 0, but cnt[(0, 2)] becomes 1.

row as the bottom corners).

Now, ans is incremented by 1.

row.

5. Count and Update Rectangles:

Repeat steps 2-5 for remaining rows:

• cnt[(0, 1)] becomes 1, cnt[(0, 2)] is incremented to 2 (since we already have one from the first row), and cnt[(1, 2)] becomes 1.

Second row [1, 1, 1] has '1's at indices 0, 1, and 2.

Finally, after iterating through all rows, we conclude with:

Continuing on to the third and fourth rows, you'll do the same pair checks and counts, but no updates to ans occur until the fourth

pair (which is two times so far), a rectangle can be completed, so ans gets incremented by 2.

directly. The Counter efficiently handles this incrementation and checking for previously seen pairs.

Pairs (0, 1), (0, 2), and (1, 2) each have the potential to form corner rectangles.

These are the potential top corners of multiple rectangles.

 ans = 3 (total count of corner rectangles found in the grid). This example illuminated how only pairs of '1's in the same rows are used to determine the possibility of forming rectangles, and with

If both columns have a 1 at the current row, this forms a potential rectangle corner

Increase the count for this column pair as we found another rectangle corner

rectangle_count += pair_counter[(col_index_first, col_index_second)]

pair_counter[(col_index_first, col_index_second)] += 1

Update the counter for the current pair, adding one more occurrence

2. pair_counter: Renamed cnt to pair_counter which is a Counter object to keep track of pairs of columns that make the corners

each row's pairs, we effectively keep a running count of potential rectangles without the need for checking all possible rectangles

• In the fourth row [1, 0, 1], the same pair (0, 2) is found as in the first row, meaning that for every previous occurrence of this

As we process this row, and gets updated because cnt [(0, 2)] was already 1 (one rectangle can now be formed with the previous

def countCornerRectangles(self, grid: List[List[int]]) -> int: rectangle_count = 0 # This will hold the final count of corner rectangles pair_counter = Counter() # Counter to track pairs of columns that have a 1 at the same row num_cols = len(grid[0]) # The number of columns in the grid

return rectangle_count

Changes and comments explanation:

for row in grid:

Iterate through each row in the grid

Return the total count of rectangles found

public int countCornerRectangles(int[][] grid) {

// Loop through each row in the grid.

if (row[leftCol] == 1) {

// This will store the final count of corner rectangles.

Map<List<Integer>, Integer> pairsCount = new HashMap<>();

for (int leftCol = 0; leftCol < numCols; ++leftCol) {</pre>

if (row[rightCol] == 1) {

// The result is the total count of rectangles found.

int countCornerRectangles(vector<vector<int>>& grid) {

int num_columns = grid[0].size();

// Initialize the answer to 0

int answer = 0;

// n represents the number of columns in the grid

// Iterate over every possible pair of columns within this row

// If the current cell is a 1, explore further for a rectangle.

for (int rightCol = leftCol + 1; rightCol < numCols; ++rightCol) {</pre>

// Only if the paired cell is also a 1, do we consider it.

// Create a pair to check in our current map.

List<Integer> pair = List.of(leftCol, rightCol);

cornerRectanglesCount += pairsCount.getOrDefault(pair, 0);

// Increment the count of found rectangles with these 1's as the top corners.

// A map to store the counts of 1's pairs across rows.

// Number of columns in the grid.

int numCols = grid[0].length;

int cornerRectanglesCount = 0;

for (int[] row : grid) {

1 from collections import Counter

Python Solution

class Solution:

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13 # Only process if the cell at the current column has a 1 if cell_first: 14 # Consider pairs of columns, starting from the current one 15 for col_index_second in range(col_index_first + 1, num_cols): 16 17 # Check if the second column also has a 1 at the current row

1. rectangle_count: Renamed ans to rectangle_count to better describe what the variable is used for.

Enumerate over the row to get both column index and value

for col_index_first, cell_first in enumerate(row):

if row[col_index_second]:

of rectangles. 3. num_cols: Introduced this variable as a clearer name for the number of columns in the grid (n in the original code). 4. col_index_first and cell_first: Renamed i and c1 for clarity in the enumeration of the first column index and cell value. 5. Comments: Added explanatory comments throughout the code to provide clarity on each step of the process. 6. Standard imports: Included the import statement for the 'Counter' class from the 'collections' module explicitly, which allows for counting occurrences of elements in a hashable object. Make sure to replace List by the correct import statement from 'typing' at the beginning of the file: from typing import List Java Solution import java.util.HashMap; import java.util.List;

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                                 // Increment the count of this pair in our map.
                                 pairsCount.merge(pair, 1, Integer::sum);
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return cornerRectanglesCount;

import java.util.Map;

class Solution {

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C++ Solution

1 #include <vector>

using namespace std;

2 #include <map>

5 class Solution {

6 public:

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// Define a map to store the count of pairs of columns that form the vertical sides of potential rectangles
           map<pair<int, int>, int> column_pairs_count;
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           // Iterate through each row of the grid
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           for (const auto& row : grid) {
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                // Check each pair of columns within the row
                for (int i = 0; i < num_columns; ++i) {</pre>
                   // If the current cell contains a 1, search for a potential second column to form a rectangle
                    if (row[i]) {
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                        for (int j = i + 1; j < num_columns; ++j) {</pre>
22
                            // If we find a pair of 1s, this could form the corner of a rectangle
23
                            if (row[j]) {
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                                // Increase the answer by the count of rectangles that can be formed using this column pair
                                answer += column_pairs_count[{i, j}];
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                                // Increment the count for this column pair
26
                                ++column_pairs_count[{i, j}];
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           // Return the total count of corner rectangles
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           return answer;
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36 };
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Typescript Solution
   function countCornerRectangles(grid: number[][]): number {
       // Initialization of n to represent the number of columns
       const columnsCount = grid[0].length;
       // Initialization of the answer variable to count corner rectangles
       let cornerRectanglesCount = 0;
       // Using a Map to keep track of the count of pairs of cells with value 1
       const pairCounts: Map<number, number> = new Map();
       // Looping through each row in the grid
       for (const row of grid) {
           // Looping through each cell in the row
           for (let i = 0; i < columnsCount; ++i) {</pre>
               // Check if the current cell has value 1
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                if (row[i] === 1) {
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// Nested loop to find another cell with value 1 in the same row

// Creating a unique key for the pair of cells

// Increment count for the current pair of cells

// Update the pair count map with the new count

cornerRectanglesCount += pairCounts.get(pairKey) ?? 0;

pairCounts.set(pairKey, (pairCounts.get(pairKey) ?? 0) + 1);

for (let j = i + 1; $j < columnsCount; ++j) {$

const pairKey = i * 200 + j;

if (row[j] === 1) +

Time and Space Complexity

where n is the number of columns.

Time Complexity

28 29 // Returning the total count of corner rectangles found in the grid 30 return cornerRectanglesCount; 31 32 } 33

The given code's time complexity primarily comes from the nested loops that it uses to iterate over each pair of columns for each row. The first loop (for row in grid) goes through each row in the grid, which occurs m times where m is the number of rows.

• Inside this loop, the second loop (for i, c1 in enumerate(row)) iterates over each element in the row, which occurs n times

• The innermost loop (for j in range(i + 1, n)) iterates from the current column i to the last column, with the average number

of iterations being roughly n/2 since it's a triangular iteration overall. Considering the iterations of the third nested loop, the number of column pairs (i, j) that will be considered for each row follows the pattern of a combination of selecting two out of n columns or nC2.

Space Complexity

Therefore, the time complexity is 0(m * nC2) or 0(m * n * (n - 1) / 2), which simplifies to $0(m * n^2)$.

The space complexity is determined by the storage used by the cnt Counter, which keeps track of the frequency of each pair of columns that have been seen with '1' at both the ith and jth positions.

- In the worst case scenario, the cnt Counter would have an entry for every possible pair of columns. As there are n columns, the number of column pairs would be the same nC2 we calculated before, or n * (n - 1) / 2 pairs. Therefore, the space complexity for the cnt Counter is 0(n^2).
- Thus, the overall space complexity is 0(n^2) since the Counter's size is the dominant term, and this space is additional to the input (grid) since the grid itself is not being modified.