Problem Description

characters. We need to determine if the pattern p matches the entire string s. The wildcard characters are defined as follows:

The problem is a classic example of pattern matching where we are given a string s and a pattern p that includes wildcard

- A question mark ('?') matches any single character. An asterisk ('*') matches any sequence of characters, including an empty sequence.
- The goal is to check if there is a complete match between the entire string and the pattern, not just a partial match.

Intuition

The key insight is to realize that we can make a decision at each character in the string based on two conditions:

1. If the current character in the pattern is a ? or matches the current character in the string, we refer to previous states where the match has been progressing without the current character and pattern.

- 2. If the current character in the pattern is a *, it can be complex because * can match an empty sequence or any sequence of characters. We need to consider multiple cases: either we use the * to match zero characters in the string (which means we look
- at the state of the match without the *), or we use the * to match at least one character in the string (which means we look at the state of the match without the current character in the string, but keep the *). This method of breaking down the problem helps us to derive a solution using a 2D matrix dp where dp[i][j] represents whether the first i characters of the string s can be matched with the first j characters of the pattern p. The final answer at dp[m][n] (where m

By filling up the matrix by iterating over the string and the pattern, we use the previously solved subproblems to inform the solution of the current subproblem. Eventually, we derive the solution to the entire problem.

and n are the lengths of the string and pattern respectively) gives us the answer to whether the entire string matches the pattern.

Solution Approach The solution uses dynamic programming, a method where complex problems are broken into simpler subproblems and solved

1. Initialize a 2D matrix dp with dimensions $(m + 1) \times (n + 1)$, where m is the length of the string s and n is the length of the pattern p. Each element dp[i][j] in this matrix will store a boolean value indicating if s[0..i-1] matches p[0..j-1]. The +1 offset allows us to easily handle the empty string and pattern cases.

3. Pre-fill the first row of the matrix by setting dp[0][j] to True if p[j-1] is * and dp[0][j-1] is also True. This loop accounts for the

previous characters.

value after initialization.

Here is a breakdown of the implementation steps:

1 for j in range(1, n + 1): 2 if p[j - 1] == '*': dp[0][j] = dp[0][j - 1]

∘ If the current character of s[i - 1] matches the current character of p[j - 1] or p[j - 1] is a ? (which can match any

single character), then set dp[i][j] to the value of dp[i - 1][j - 1] since we can carry forward the match status from

4. Iterate through the matrix starting from i = 1 and j = 1, and calculate the dp[i][j] value based on the following rules:

If the current character of the pattern is *, there are two possibilities:

■ The * matches zero characters: carry forward the status from dp[i][j - 1].

from exponential (which would be the case with a naive recursive approach) to polynomial time.

■ The * matches one or more characters: carry forward the status from dp[i - 1][j].

2. Set the first element dp[0][0] to True to represent that an empty string matches an empty pattern.

situation where the pattern starts with one or multiple * characters, which can match the empty string.

individually, with the solutions to the subproblems stored to avoid redundant calculations.

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1 if s[i - 1] == p[j - 1] or p[j - 1] == '?':
2    dp[i][j] = dp[i - 1][j - 1]
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Hence:
     ```python
 elif p[j - 1] == '*':
 dp[i][j] = dp[i - 1][j] \text{ or } dp[i][j - 1]
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For all other cases where characters don't match and there is no wildcard, dp[i][j] will remain False, which is the default

- 5. After filling the entire matrix, the value at dp[m] [n] will indicate whether the entire string s matches the pattern p.
- Let's illustrate the solution approach using a small example: Assume s = "xaabyc" and p = "\*a?b\*".

1. Initialize the 2D matrix dp: Since s has a length of 6 and p has a length of 5, our matrix dp will be a 7×6 matrix (including the

This approach ensures that each subproblem is only calculated once and then reused, dramatically reducing the time complexity

# 3. First row pre-fill: We then iterate over the first row of dp to account for a pattern that starts with \*. In this case, p[0] is \*, so

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the match between s and p efficiently.

dp[0][0] = True

Python Solution

class Solution:

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Typescript Solution

Java Solution

class Solution {

dp[0][0] = true;

4. Iterate and fill the matrix:

False.

**Example Walkthrough** 

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def isMatch(self, string: str, pattern: str) -> bool:

length\_s, length\_p = len(string), len(pattern)

# Create a DP table with default values False

# The empty pattern matches the empty string

for j in range(1, length\_p + 1):

public boolean isMatch(String str, String pattern) {

// Lengths of the input string and the pattern

// match the first j characters of the pattern

// Empty string and empty pattern are a match

// as they can match the empty string

for (int j = 1; j <= patternLen; ++j) {</pre>

dp[0][j] = dp[0][j - 1];

if (pattern.charAt(j - 1) == '\*') {

// Build the dp matrix in bottom-up manner

// and continue matching

for (int j = 1; j <= patternLen; ++j) {</pre>

// we can propagate the diagonal value

else if (pattern.charAt(j - 1) == '\*') {

dp[i][j] = dp[i - 1][j] || dp[i][j - 1];

dp[i][j] = dp[i - 1][j - 1];

for (int i = 1; i <= strLen; ++i) {

int strLen = str.length(), patternLen = pattern.length();

boolean[][] dp = new boolean[strLen + 1][patternLen + 1];

// dp[i][j] will be true if the first i characters in given string

// Initialize the first row for the cases where pattern contains \*

// If the current characters match or pattern has '?',

// If pattern contains '\*', it can either match zero characters

// If the current pattern character is not a wildcard and the characters

// don't match, dp[i][j] remains false, which is the default value.

// in the string or it can match one character in the string

if  $(str.charAt(i - 1) == pattern.charAt(j - 1) || pattern.charAt(j - 1) == '?') {$ 

dp[i][j] = dp[i - 1][j - 1]

# Return the value at the bottom-right corner of the DP table

for j in range(1, length\_p + 1):

return dp[length\_s][length\_p]

# Get the lengths of the input string and the pattern

 $dp = [[False] * (length_p + 1) for _ in range(length_s + 1)]$ 

# Initialize first row of the DP table, considering the pattern starting with '\*'

if string[i - 1] == pattern[j - 1] or pattern[j - 1] == '?':

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a. For i = 1 and j = 1, the pattern has * which matches zero characters from s. So, dp[1][1] is True because dp[0][0] was
true.
```

extra row and column for the empty string and pattern case). Initially, all values in dp are set to False.

dp [0] [1] should be set to True. Following that logic, here's how the first row will look after pre-filling:

2. First element dp[0][0]: We set dp[0][0] to True to denote that an empty pattern matches an empty string.

c. Eventually, by following the iteration rules while filling out the matrix, we will have:

b. When j = 2 and i = 1, the pattern is a but our string is x. Since they don't match and the pattern is not a ?, dp[1][2] stays

- 5. Final Check: Our final cell dp [6] [5] contains True. Therefore, we can deduce that with the given example, the string s matches the pattern p.
- 14 if pattern[j - 1] == '\*': 15 dp[0][j] = dp[0][j - 1]16 17 # Fill the DP table for i in range(1, length\_s + 1): 18

# If characters match or pattern has '?', we can move back diagonally in the table (match found)

By processing the dp matrix according to the dynamic programming approach, we've avoided redundant calculations and determined

## # If pattern has '\*', we check two cases: 24 # 1. '\*' matches no character: move left in the table 25 # 2. '\*' matches at least one character: move up in the table 26 elif pattern[j - 1] == '\*': 27 dp[i][j] = dp[i - 1][j] or dp[i][j - 1]28

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 // The value in the bottom right corner will be our answer
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 return dp[strLen][patternLen];
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C++ Solution
 #include <vector>
 #include <string>
 class Solution {
 public:
 bool isMatch(const std::string& s, const std::string& p) {
 int strSize = s.size(), patternSize = p.size();
 // Create a DP table with dimensions (m+1) \times (n+1) initialized to false.
 // dp[i][j] will be true if the first i characters of s match the first j
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 // characters of p.
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 std::vector<std::vector<bool>> dp(strSize + 1, std::vector<bool>(patternSize + 1, false));
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 // The empty pattern matches the empty string.
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 dp[0][0] = true;
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 // Initialize the first row of the DP table. If we find '*', it can match
 17
 // an empty string, which is the state of dp[0][j-1].
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 for (int j = 1; j <= patternSize; ++j) {</pre>
 19
 if (p[j-1] == '*') {
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 dp[0][j] = dp[0][j - 1];
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 // Fill the DP table.
 25
 for (int i = 1; i <= strSize; ++i) {</pre>
 26
 for (int j = 1; j <= patternSize; ++j) {</pre>
 27
 // If the characters match or the pattern character is '?',
 // we can transition from the state dp[i-1][j-1].
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 if (s[i-1] == p[j-1] \mid\mid p[j-1] == '?')
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 dp[i][j] = dp[i - 1][j - 1];
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 // If the pattern character is '*', it can either match zero characters,
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 // meaning we transition from dp[i][j-1], or it can match one character,
 34
 // meaning we transition from dp[i-1][j].
 35
 else if (p[j - 1] == '*') {
 dp[i][j] = dp[i][j - 1] || dp[i - 1][j];
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 // The empty pattern matches the empty string.
 dp[0][0] = true;
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 // Initialize the first row of the DP table. If we find '*', it can match
 // an empty string, thereby adopting the value from dp[0][j-1].
 14
 15
 for (let j = 1; j <= patternLen; j++) {</pre>
 if (p[j - 1] === '*') {
 16
 17
 dp[0][j] = dp[0][j - 1];
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 21
 // Fill the DP table.
 22
 for (let i = 1; i <= strLen; i++) {
 23
 for (let j = 1; j <= patternLen; j++) {</pre>
 24
 // If the characters match or the pattern character is '?',
 25
 // we can transition from the state dp[i-1][j-1].
 if (s[i-1] === p[j-1] || p[j-1] === '?') {
 26
 27
 dp[i][j] = dp[i - 1][j - 1];
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 29
 // If the pattern character is '*', it can either match zero characters,
 // meaning we transition from dp[i][j-1], or it can match one or more characters,
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 31
 // meaning we transition from dp[i-1][j].
 32
 else if (p[j - 1] === '*') {
 33
 dp[i][j] = dp[i][j - 1] || dp[i - 1][j];
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 // The final state dp[strLen][patternLen] gives us the answer to whether the entire
 38
 // strings s and p match with each other.
 return dp[strLen][patternLen];
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Time and Space Complexity
The time complexity of the provided code is 0(m * n), where m is the length of the string s and n is the length of the pattern p. This is
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// The final state dp[m][n] gives us the answer to whether the entire

// Create a DP table with dimensions (strLen+1) x (patternLen+1) initialized to false.

// dp[i][j] will be true if the first i characters of s match the first j characters of p.

() => Array<boolean>(patternLen + 1).fill(false));

// strings s and p match with each other.

return dp[strSize][patternSize];

function isMatch(s: string, p: string): boolean {

let dp: boolean[][] = Array.from({ length: strLen + 1 },

let strLen: number = s.length;

let patternLen: number = p.length;

computes whether the first i characters of s match the first j characters of p, and the computation of each cell is constant time. The space complexity of the code is also 0(m \* n). This is due to the use of a two-dimensional list dp, which has (m + 1) \* (n + 1)

because the code involves a nested loop structure that iterates through the lengths of s and p. Each cell in the DP table dp[i][j]

elements, to store the states of substring matches. Each element of this list represents a subproblem, with extra rows and columns to handle empty strings.

For solving this problem, dynamic programming is a common approach because it allows us to break down the complex problem into smaller subproblems and then build up the solution from these.