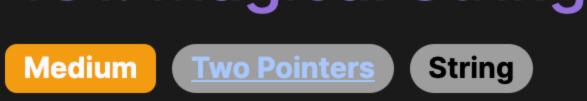
481. Magical String



Problem Description

the original sequence s.

The problem presents a unique sequence called a "magical string" that is built based on its own sequence of numbers. We start with a string s that only contains the characters '1' and '2'. The magic is that when we group the characters in s by the count of consecutive '1's and '2's, these grouped counts form the same string s.

As an example, we start with the known sequence: "1221121221221121122...". Grouping the consecutive characters yields "1 22 11 2 1 22 1 22 11 2 11 22 ...", and then the counts of '1's and '2's in these groups are "1 2 2 1 1 2 1 2 2 1 2 2 ...", which is the same as

The task is to determine the count of '1's in the first n characters of the magical string s. Specifically, given an integer n, return how many '1's appear in the initial segment of length n in the string s.

Intuition

only as far as necessary to count the number of '1's within the first n characters. The solution uses a list s to simulate the magical string and a pointer i to keep track of where in s we are currently looking to

To solve this problem, we don't need to generate the entire string, which could be very long. Instead, we can build the string s

determine how many times to repeat the next character. We begin with the known start of the magical string as [1, 2, 2]. The core idea is to iteratively extend the magical string based on its definition. For each step, we look at the value of s[i], which

tells us how many times to repeat the next character. We alternate the characters to add based on the last character in the string: if it's a '1', we add '2's; if it's a '2', we add '1's. The number of characters to add is equal to the current value of s[i].

The use of pre helps us know what the last character was (either '1' or '2'), and cur is used to determine what the next character

should be, by switching between '1' and '2'. We continue extending the string until its length is at least n. Once the length of s reaches n, we simply take the first n elements

Solution Approach

The implementation relies on a simple Python list s to simulate the construction of the magical string. An integer i serves as a

pointer that moves through the list, indicating how many times the next character should be repeated. Here's how the

implementation unfolds:

of s and count the number of '1's to get our answer.

We initialize the representation of the magical string as s = [1, 2, 2]. This is because the sequence always starts with "122". We set the pointer i = 2. This is because s[2] points to the second '2' in the initial list, which indicates that the next

determine the next sequence to append to s.

We then enter a while loop which will run as long as the length of s is smaller than n, ensuring that we build enough of the

sequence to be added should consist of two numbers. The pointer i will indicate which number in s we should look at to

- magical string to count the number of '1's in the first n characters. Inside the loop, we first store the last element of the current string in the variable pre. This is either a 1 or a 2, and it
- represents the last character in the string. Next, we calculate cur as 3 - pre. Since we only have '1' and '2' in our sequence, if the last character (pre) is '1', cur will be '2'
- (since 3 1 = 2), and if it's '2', cur will be '1'. The next step is to extend the list s by adding cur repeated s[i] times. This is akin to saying "if we have a '2' in s[i], and cur

is '1', then append '1' to s two times." We append [cur] * s[i] to s.

return the count of '1's in the first n characters of s by using s[:n].count(1).

- We then increment i by 1 to move the pointer to the next character in s. Once we exit the while loop, it means we've built a section of the magical string that is at least as long as n. The last step is to
- This approach is efficient because it constructs only as much of the magical string as is necessary to determine the number of '1's within the first n elements. It uses simple list operations and arithmetic to achieve this task.
- **Example Walkthrough** Let's walk through a small example to illustrate the solution approach. Suppose we are asked to find the number of '1's in the first

The pointer i is initially set to 2, since s[2] points to '2', which will determine what we append next to s.

[1, 2, 2, 1, 1, 2].

10 characters of the magical string s.

3, so we enter the loop.

Our while loop continues as long as the length of s is less than 10 (the n value in our example). At the start, the length of s is

The last element, pre, of the current string s is 2.

We then increment i by 1, moving the pointer to the next character in s, so i is now 3.

We start off by initializing our list s with the known beginning of the magical string: [1, 2, 2].

- We calculate cur as 3 pre. Since pre is 2, cur becomes 1.
- We extend s by adding cur repeated s[i] times. In this case, since s[i] is 2 and cur is 1, we append two '1's to s, resulting in s becoming [1, 2, 2, 1, 1].

Now, pre is 1 (the last element in s), so now cur will be 3 - pre, which is 2. s[i] is 1, so we append one '2' to s, changing s to

- We repeat steps 4 through 7, with i now at 4. s[i] is 1, the current pre is 2, so cur is 1. We add one '1' to s to get [1, 2, 2, 1, 1, 2, 1].
- Continuing this process, we increment i, calculate cur, and extend s until s is at least 10 characters long. After a few 10. iterations, s is [1, 2, 2, 1, 1, 2, 1, 2, 2, 1], and the length of s is 10.
- Thus, for n = 10, our function would return 5, as there are five '1's in the first 10 characters of the magical string s.
- Solution Implementation
- class Solution: def magicalString(self, n: int) -> int: # Initialize the magical string with the known starting sequence

Append 'current_value' to the list as many times as the value at the current 'index'

// Count the number of occurrences of 1 in the first 'n' elements of the magical string

// Return the count of 1's in the first 'n' elements of the magical string

Use index to track the position in the string for generating the next elements

Generate the magical string until its length is at least 'n'

magical_str.extend([current_value] * magical_str[index])

The loop stops since s now has a length of 10. We count the number of '1's in s[:10], which is 5.

```
while len(magical_str) < n:</pre>
    # Get the last value in the magical string
    last value = magical str[-1]
```

index = 2

 $magical_str = [1, 2, 2]$

int countOnes = 0;

for (int idx = 0; idx < n; ++idx) {

countOnes++;

if (magicalStr.get(idx) == 1) {

current_value = 3 - last value

Python

```
# Move to the next index
            index += 1
       # Slice the magical string until 'n' and count the occurrences of `1`
        return magical_str[:n].count(1)
Java
class Solution {
    public int magicalString(int n) {
       // Initialize the magical string as a list with the first three numbers
       List<Integer> magicalStr = new ArrayList<>(Arrays.asList(1, 2, 2));
       // Use a pointer to iterate through the magical string to generate the next numbers
        int i = 2; // Starting from index 2 because the first three numbers are already in the list
       while (magicalStr.size() < n) {</pre>
            int lastNum = magicalStr.get(magicalStr.size() - 1); // Get the last number in the current magical string
            int nextNum = 3 - lastNum; // Calculate the next number (if lastNum is 1, then nextNum is 2; if lastNum is 2, then nextNum is 2.
            // Add 'nextNum' to the magical string 's.get(i)' times as per the current number's frequency
            for (int j = 0; j < magicalStr.get(i); ++j) {</pre>
                magicalStr.add(nextNum);
            i++; // Move to the next number
```

The current value to be appended is the "opposite" of the last value (1 switches to 2, and 2 switches to 1)

```
return countOnes;
C++
#include <vector>
#include <algorithm>
class Solution {
public:
    int magicalString(int n) {
        std::vector<int> magical_seq = {1, 2, 2}; // Initialize the magical sequence with its first three elements
        // Use 'index' to iterate through the magical sequence
        // The loop continues until the size of magical_seq is at least n
        for (int index = 2; magical_seq.size() < n; ++index) {</pre>
            int last_number = magical_seq.back(); // Get the last number in the current sequence
            int next_number = 3 - last_number; // Determine the next number to add, which will be 1 if the last is 2, and 2 if the
            // Append the next_number to the sequence s[i] times where s[i] is the current element at position i
            // This loop controls the count of the next number to be appended
            for (int count = 0; count < magical_seq[index]; ++count) {</pre>
                magical_seq.emplace_back(next_number); // Append the number to the end of the sequence
        // Count the number of 1's up to the nth element and return that count
        return std::count(magical_seq.begin(), magical_seq.begin() + n, 1);
};
```

TypeScript

function magicalString(n: number): number {

let magicalStr = [...'1221121'];

while (magicalStr.length < n) {</pre>

let readIndex = 5;

// Initialize the magical string with the known beginning sequence

// Initialize the index for counting group occurrences

// Generate the magical string up to the required length 'n'

const lastChar = magicalStr[magicalStr.length - 1];

magicalStr.push(lastChar === '1' ? '2' : '1');

if (magicalStr[readIndex] !== '1') {

// Get the last character of the current magical string

magicalStr.push(lastChar === '1' ? '2' : '1');

// Append the opposite character to the string ('1' becomes '2', and '2' becomes '1')

// If the current read index character is '2', repeat the action once more

```
// Move to the next index
          readIndex++;
      // Calculate the number of '1's in the first 'n' characters of the magical string
      return magicalStr.slice(0, n).reduce((count, char) => count + (char === '1' ? 1 : 0), 0);
class Solution:
   def magicalString(self, n: int) -> int:
       # Initialize the magical string with the known starting sequence
        magical_str = [1, 2, 2]
       # Use index to track the position in the string for generating the next elements
        index = 2
       # Generate the magical string until its length is at least 'n'
       while len(magical_str) < n:</pre>
           # Get the last value in the magical string
            last_value = magical_str[-1]
            # The current value to be appended is the "opposite" of the last value (1 switches to 2, and 2 switches to 1)
            current value = 3 - last value
            # Append 'current_value' to the list as many times as the value at the current 'index'
            magical_str.extend([current_value] * magical_str[index])
           # Move to the next index
            index += 1
       # Slice the magical string until 'n' and count the occurrences of `1`
        return magical_str[:n].count(1)
```

Time and Space Complexity

Time Complexity

The time complexity of the function primarily comes from the while loop that generates the magical string until its length is at least n. In each iteration, the loop appends up to s[i] elements to the list s where s[i] could be either 1 or 2. This results in a maximum of 2 additions per iteration. However, since each iteration of the loop adds at least one element, and we iterate until we have n elements, the overall time complexity can be approximated as O(n).

Space Complexity

The space complexity of this function is also defined by the size of the list s, which grows to match the input n in the worst-case scenario. Since we need to store each element of the magical string up to the nth position, the space complexity is 0(n).