# 2128. Remove All Ones With Row and Column Flips

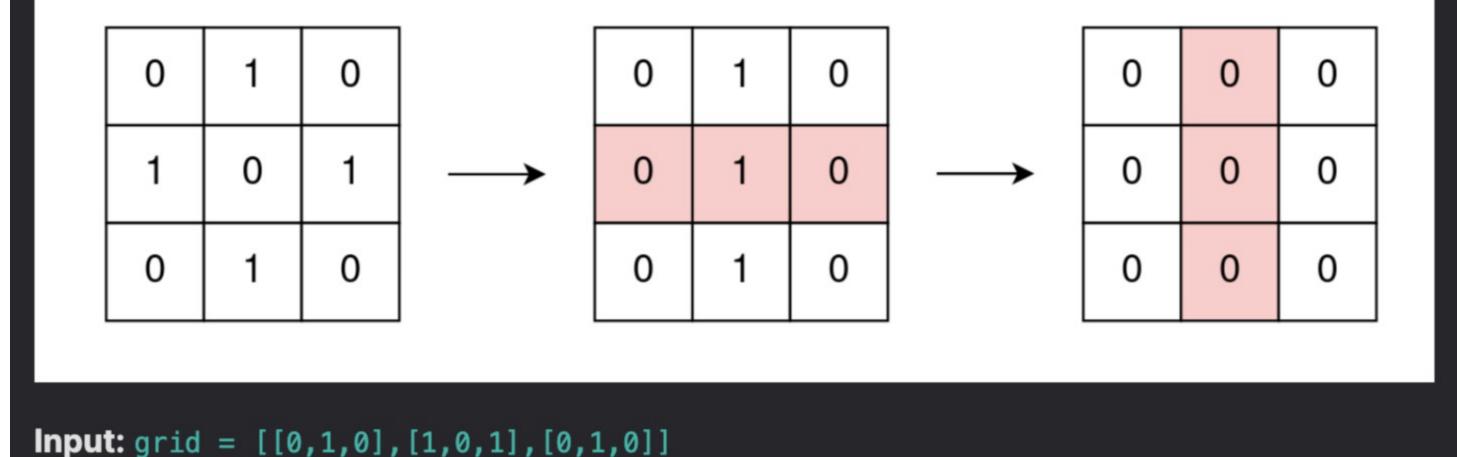
**Leetcode Link** 

You are given an  $m \times n$  binary matrix grid.

In one operation, you can choose any row or column and flip each value in that row or colum (i.e., changing all 0's to 1's, and all 1's to 0's).

Return true if it is possible to remove all 1's from grid using any number of operations or false otherwise.

Example 1:



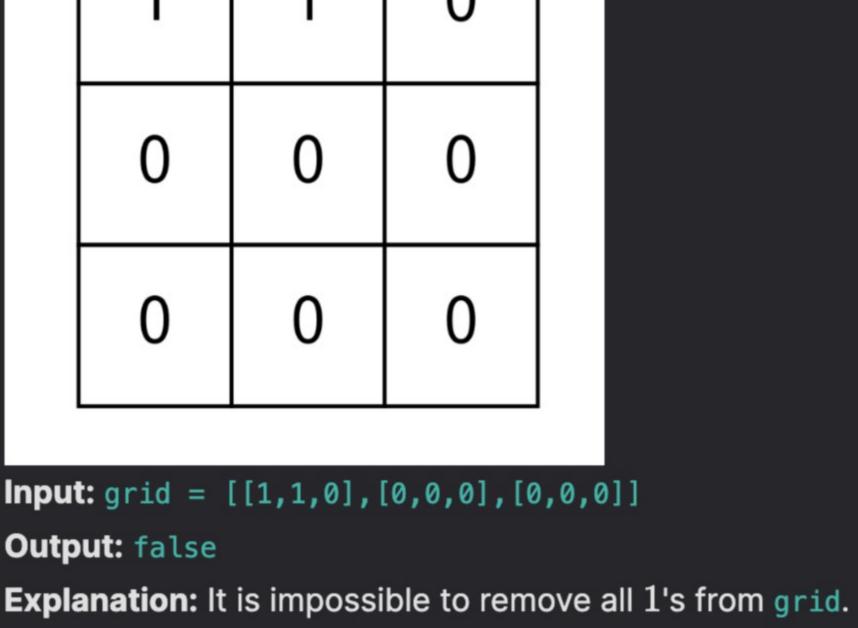
**Explanation:** One possible way to remove all 1's from grid is to:

Output: true

Flip the middle row

- Example 2:

Flip the middle column



**Input:** grid = [[0]] Output: true

**Explanation:** There are no 1's in grid.

## • n == grid[i].length

**Constraints:** 

• grid[i][j] is either 0 or 1.

• m == grid.length

• 1 <= m, n <= 300

- Solution
- **Brute Force**

because if we flip a row/column twice, it will have no effect on the grid.

Let's call grid reachable if it's possible to apply some row/column flips to remove all 0's.

MN). Let's look for a faster solution as this is way too slow.

flips if all rows have the same integer (i.e. all 0's or all 1's).

# The first observation we can make is that for every row/column, we will either flip that row/column once or zero times. This is

### With this in mind, for each row and column, we can either choose to flip it or not flip it. If we brute force every combination, we will take O(MN) to simulate each combination. Since there are $O(2^{M+N})$ combinations, this gives us a time complexity of $O(2^{M+N} imes 1)$

**Full Solution** 

We can observe that if each row/column is flipped at most once, there is only one set of rows and columns that can be flipped to set all cells to 0 (assuming a solution exists). Let's call these necessary rows and columns. To check whether or not grid is reachable, we'll first flip all necessary columns, and then the necessary rows.

Example

Let's first assume that we already flipped all necessary columns on grid. We can observe that grid is now reachable by only row

Here, we have a grid reachable by only row flips as all rows have the same integer. We can remove all 1's from grid by flipping rows with all 1's. Here, we will flip rows 1 and 5. Our goal is to figure out a way to flip some set of columns such that grid will only contain rows with all 0's or all 1's. With that in mind, our algorithm will go as follows. First, find all cells in the first row of grid with a 1. For every cell (0, j) in the first row that's a 1, let's flip the  $j^{th}$  column so that the cell (0, j) becomes a 0. This is important as it causes the first row to have all 0's. At this point there are two cases to consider. • The first case is that the rest of the rows have all 0's or all 1's. In this case, we can conclude that grid is reachable and we'll return true. • The second case is that there exists a row that has a mix of 0's and 1's, which we don't want. In this case, we'll return false

flips take O(M) to simulate, our total time complexity is O(NM).

bool removeOnes(vector<vector<int>>& grid) {

for (int j = 0; j < n; j++) {

sum += grid[i][j];

if (sum == 0 || sum == n) {

int n = grid[0].size();

bool ans = true;

int sum = 0;

ans = false;

continue;

continue;

ans = false;

return ans;

if (grid[0][i] == 1) {

int m = grid.size(); // get dimensions of grid

grid[j][i] = 1 - grid[j][i];

for (int i = 0; i < n; i++) { // flip columns so that first row only has 0's

for (int i = 0; i < m; i++) { // checks if each row has all 0's or all 1's

**Time Complexity** In the worst scenario, we will perform O(M) row flips and O(N) column flips. Since row flips take O(N) to simulate and column

since we can observe that it's impossible to get all rows to have all 0's or all 1's. This is because if we try to change the other

rows to have all 0's or 1's with more column flips, the content of the first row will change and it will no longer have all 0's.

Since we don't actually use additional arrays or lists, our space complexity is O(1). Space Complexity: O(1).

### for (int j = 0; j < m; j++) { // flips a column 10 11 12

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C++ Solution

class Solution {

public:

Time Complexity: O(NM).

**Space Complexity** 

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           return ans;
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26 };
Java Solution
   class Solution {
       public boolean removeOnes(int[][] grid) {
           int m = grid.length; // get dimensions of grid
           int n = grid[0].length;
           for (int i = 0; i < n; i++) { // flip columns so that first row only has 0's
               if (grid[0][i] == 1) {
                   for (int j = 0; j < m; j++) { // flips a column
                       grid[j][i] = 1 - grid[j][i];
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 9
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           boolean ans = true;
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            for (int i = 0; i < m; i++) { // checks if each row has all 0's or all 1's
                int sum = 0;
                for (int j = 0; j < n; j++) {
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                   sum += grid[i][j];
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               if (sum == 0 || sum == n) {
```

# class Solution:

```
Python Solution
         def removeOnes(self, grid: List[List[int]]) -> bool:
             m = len(grid) # get dimensions of grid
             n = len(grid[0])
             for i in range(n): # flip columns so that first row only has 0's
  6
                 if grid[0][i] == 1:
                    for j in range(m): # flips a column
                        grid[j][i] = 1 - grid[j][i]
             ans = True
             for i in range(m): # checks if each row has all 0's or all 1's
 10
 11
                 sum = 0
                 for j in range(n):
 12
 13
                    sum += grid[i][j]
 14
                 if sum == 0 or sum == n:
 15
                    continue
 16
                 ans = False
 17
             return ans
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```

Got a question? Ask the Teaching Assistant anything you don't understand.