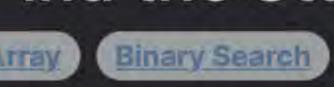
1894. Find the Student that Will Replace the Chalk

Simulation

Prefix Sum







Problem Description

In this problem, you're given an integer array chalk and an integer k, which represent the number of chalk pieces available for a group of students to use. Each element in the chalk array corresponds to the amount of chalk that each student will use to solve a problem. For example, chalk[0] is the amount of chalk the first student will use, chalk[1] the amount for the second student, and so

Leetcode Link

on, in a repeating cycle. The sequence starts with the first student (index 0) and goes to the last student (index n - 1). After the teacher has distributed problems to all students, the cycle starts again with the first student. This continues until there aren't enough chalk pieces for a

The task is to find out which student will be asked to replace the chalk. In other words, you need to return the index of the first student who cannot proceed because the chalk pieces left are fewer than what they need.

Intuition

Prefix Sum: First, we calculate the cumulative chalk usage for each student, which gives us a sequence where each element tells us

To solve this problem, it's efficient to use a prefix sum and binary search.

student to use. At that point, the student will be asked to replace the chalk.

the total amount of chalk used by all students up to that point. This can be done using the accumulate function from the itertools. module in Python, which creates a list of accumulated sums. Binary Search: Then, because the cycle starts again after reaching the last student, we can take the total amount of chalk k and find

the remainder when divided by the total accumulated chalk. This tells us how much chalk would be left after an integer number of

full cycles, and the next student to take a problem would need more chalk than what we have. Using this leftover amount of chalk, we can perform a binary search to find the first student who would need more chalk than the remnants. The built-in function bisect_right from the bisect module in Python can help us here. It searches for the place to insert the leftover chalk amount in order to maintain the sorted order. This position, effectively the index of the student, is the output of our function. Solution Approach

The solution approach for this problem is to first calculate the prefix sum of the chalk requirements for each student and then use a binary search algorithm to find the index of the student who will replace the chalk.

Here's a step-by-step breakdown of the implementation described by the provided solution code:

1. Calculate Prefix Sum: Using the accumulate function from the itertools module, we calculate the cumulative sum of the chalk

array. The result is a new list s where s[i] represents the total amount of chalk used by the first i + 1 students. This step is crucial because it allows us to understand the total chalk consumption in one complete cycle through all students.

- 2. Modulo Operation: The value of k may be very large, possibly larger than the total amount of chalk used in a full cycle by all students. To handle this, we use the modulo operation k 💝 s [-1] which gives us the remainder of k after dividing by the total chalk used in one cycle (s[-1] represents the total chalk used after all students have taken a problem once). This effectively
- 3. Binary Search: Now, we need to identify the first student who cannot proceed due to insufficient chalk. This is done by using the bisect_right function from the bisect module, which performs a binary search. The function finds the position where the leftover chalk k would be inserted to maintain the sorted order of the accumulated chalk list s. The returned index bisect_right(s, k) is the index of the first student whose chalk requirement exceeds the amount of leftover chalk k.

reduces the problem to a single incomplete cycle, making it easier to find the student who will replace the chalk.

s = list(accumulate(chalk)) # step 1 k %= s[-1] # step 2 return bisect_right(s, k) # step 3

Combining these steps, the code successfully determines the student who will replace the chalk:

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Even though this approach appears straightforward, it's highly efficient because both the prefix sum and binary search operate in
O(n) and O(log n) time complexities, respectively, making the whole solution quite performant for even large input sizes.
```

def chalkReplacer(self, chalk: List[int], k: int) -> int:

Example Walkthrough Let's walk through the solution approach with a small example to illustrate how it works in practice. Consider the chalk array [5, 1,

1. We first calculate the prefix sum, which tells us the cumulative amount of chalk used by the students in one round:

2 Prefix sum: [5, 6, 9]

1 Original chalk array: [5, 1, 3]

3] and k = 11:

1 k = 11

3 k % 9 = 2

2 Leftover: 2

class Solution:

With this, we can see that one full cycle of chalk usage by all students amounts to 9.

The modulo gives 2, so after completing one full round, we have 2 chalks left.

2. Now we apply the modulo operation to k with the total chalk used in one cycle:

2 Total chalk in one cycle = 9 (from the last element of the prefix sum)

```
3. Using binary search, we find where 2 (the remaining chalk pieces) would be inserted in our prefix sum array to maintain the
  sorted order:
  1 Prefix sum array: [5, 6, 9]
```

2 remaining. Hence, the answer is 0, the index of the first student in our chalk array.

def chalkReplacer(self, chalk: List[int], k: int) -> int:

to find out the total chalk needed for one round.

Find the index of the smallest number in the accumulated

chalk list that is greater than k using binary search.

Accumulate the chalk requirements in a list

return bisect_right(total_chalk_per_round, k)

k %= total_chalk_per_round[-1]

k %= prefixSum[numberOfStudents];

if (prefixSum[mid] > k) {

while (left < right) {</pre>

int left = 0, right = numberOfStudents;

// Initialize search boundaries for binary search

// such that prefixSum[left] is greater than 'k'

// Performing binary search to find the minimum index 'left'

// If the sum up to mid is greater than k, search the left half

1 # First, we need to import the required functions from the itertools and bisect modules.

This is the index of the student who will be the next to receive chalk.

inserted at index 0. Thus, the student at index 0 (the first student) would be the one who can't proceed because they require 5 chalks, and we only have

A binary search for 2 in the array [5, 6, 9] would place it before the first element since 2 is less than 5. Therefore, it would be

from itertools import accumulate from bisect import bisect_right class Solution:

```
total_chalk_per_round = list(accumulate(chalk))
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           # The remaining chalk after multiple complete rounds
11
           # is the remainder of k divided by the total chalk per round.
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Python Solution

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20 # We need to import the typing module to use List[int] as a type hint in the function signature
   from typing import List
22
Java Solution
1 class Solution {
       public int chalkReplacer(int[] chalk, int k) {
           int numberOfStudents = chalk.length;
           // Define a prefix sum array with an extra space for easier calculations
           long[] prefixSum = new long[numberOfStudents + 1];
           // Calculate the prefix sum of chalk requirements
           // Here, starting index of prefixSum should be 1 to match the chalk indices.
           prefixSum[1] = chalk[0];
           for (int i = 1; i < numberOfStudents; ++i) {</pre>
               prefixSum[i + 1] = prefixSum[i] + chalk[i];
12
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           // Find the remaining chalk after it has been distributed once
```

right = mid; } else { // Otherwise, search the right half 29 left = mid + 1;30 31 32 33 34 // The index 'left' points to the first student that cannot finish // their chalk round, that's the student to start the next round 35 return left - 1; // Adjusting the index because prefixSum started from 1 instead of 0 36 37 38 } 39 C++ Solution 1 #include <vector> #include <algorithm> // Needed for std::upper_bound class Solution { public: // Function to find the index of the student who will receive the last chalk piece before the chalk runs out int chalkReplacer(vector<int>& chalk, int k) { int numStudents = chalk.size(); vector<long long> prefixSum(numStudents, chalk[0]); // Calculate prefix sums of chalk requirements 10 for (int i = 1; i < numStudents; ++i) {</pre> 11 prefixSum[i] = prefixSum[i - 1] + chalk[i]; 12 13 // The amount of chalk K is now how much chalk will be needed in the last round 14 // because we are interested in a full cycle where every student has received chalk exactly once 15 k %= prefixSum[numStudents - 1]; 16 17 // Use upper bound to return the first element in the prefix sum which is greater than k 18 // this will be the first student who will not be able to finish writing as the chalk will run out before this student 19 20 return std::upper_bound(prefixSum.begin(), prefixSum.end(), k) - prefixSum.begin();

int mid = (left + right) >> 1; // Equivalent to (left + right) / 2 but more efficient

```
const sum = acc + current;
       prefixSums.push(sum);
10
       return sum;
     }, 0);
11
```

Typescript Solution

import _ from 'lodash';

// Function to calculate prefix sums of an array.

const prefixSums: number[] = [];

chalk.reduce((acc, current) => {

const calculatePrefixSums = (chalk: number[]): number[] => {

22 };

23

```
return prefixSums;
12
13 };
14
  // Main function to find the index of the student who will receive the last chalk piece before the chalk runs out.
  const chalkReplacer = (chalk: number[], k: number): number => {
     const numStudents = chalk.length;
     const prefixSums: number[] = calculatePrefixSums(chalk);
     // Adjust the number of chalk (k) by taking modulus with the total sum to find remainder chalk after full cycles.
     k %= prefixSums[prefixSums.length - 1];
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     // Use lodash's sortedIndex to find the smallest index at which k should be inserted
     // into `prefixSums` in order to maintain the array's sorted order.
23
24
     const studentIndex: number = _.sortedIndex(prefixSums, k);
25
26
     // This index represents the student who cannot finish writing as the chalk runs out before their turn.
     return studentIndex;
27
28 };
29
   export { chalkReplacer };
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Time and Space Complexity
The time complexity of the given code is determined by two main operations: accumulating the chalk array and performing the
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// Import the necessary functions from `lodash` for calculating the prefix sums and finding the upper bound.

Time Complexity

• The accumulate function computes the prefix sums of the chalk list, which takes O(n) time, where n is the length of chalk.

binary search.

Combining these complexities, we get $O(n + \log n)$ which simplifies to O(n) since O(n) dominates $O(\log n)$.

bisect_right is a binary search function, which takes O(log n) time to find the insert position for k in the sorted list s.

Space Complexity

chalk, the space complexity is O(n).

The modulus operation k %= s[-1] is constant time, 0(1).

The space complexity of the code comes from storing the prefix sums in the list s. Since this list has the same length as the input list