Problem Description

In this problem, you are given an integer array called nums and an integer k. Your task is to modify each element in the array by either adding k to it or subtracting k from it. After modifying each element in this manner, the score of the array is defined as the difference between the maximum and minimum elements in the modified array. The objective is to determine the minimum score that can be achieved by any combination of adding or subtracting k to/from the elements of nums.

Suppose nums = [1, 3, 6] and k = 3. You could transform nums as follows:

Here is an example to illustrate:

Adding k to the first element: [1 + 3, 3, 6] = [4, 3, 6]

- Subtracting k from the second element: [4, 3 3, 6] = [4, 0, 6] Subtracting k from the third element: [4, 0, 6 - 3] = [4, 0, 3]
- The score is then $\max(4, 0, 3) \min(4, 0, 3) = 4 0 = 4$.
- The problem is asking you to find the minimum score possible, that is, the smallest difference between the highest and lowest

number in the array after each element has been increased or decreased by k.

The intuition behind the solution involves recognizing that sorting the array can help in minimizing the score. By sorting, you can

Here's why sorting helps:

Intuition

nums [0]. Consider a pivot point at index i in the sorted array. Everything to the left of i could be increased by k, and everything to the right of i (including element at i) could be decreased by k. This creates two "blocks" within the array: one with increased values,

After sorting nums, the smallest and largest elements are nums [0] and nums [-1], respectively. The initial score is nums [-1] -

ensure that the operation that you perform (addition or subtraction) will not increase the range unnecessarily.

- and one with decreased values. • The new minimum possible value is the minimum of nums [0] + k (left-most element of the increased block) and nums [1] - k (left-most element of the decreased block). • The new maximum possible value is the maximum of nums [i - 1] + k (right-most element of the increased block) and nums [-1]
- k (right-most element of the decreased block). • By iterating through all possible pivot points (from 1 to len(nums) - 1), you can find the minimum score by comparing this with the previously calculated minimum ans.
- The key observation here is that by sorting and choosing an appropriate pivot, one can minimize the difference between the maximum and minimum values affected by the addition or subtraction of k, leading directly to a solution that iterates through
- possible pivot points to find the minimum score. Solution Approach

The solution follows a simple yet effective approach leveraging sorting and iteration. Algorithm:

1. Sort the nums array. This will help us easily identify the smallest and largest elements and ensures that we do not increase the

range unnecessarily.

where k is subtracted.

index, based on the given k.

2. Initialize the variable ans with the initial score, which is the difference between the last element and the first element of the sorted array (nums [-1] - nums [0]).

- 3. Iterate through the array starting from index 1 up to len(nums) 1. The reason we start at 1 is because we are considering the
 - 4. For each index i, calculate the minimum and maximum values as follows: • Calculate the new minimum value mi as the minimum between nums [0] + k and nums [i] - k. The nums [0] + k represents

point in considering index of for this pivot as the sorted array's first element cannot be the start of the subtraction section.

pivot point where the array is divided into two parts: one that will get the addition of k and the other the subtraction. There is no

the smallest possible value after the increment and nums [i] - k represents the smallest value for the section of the array

○ Calculate the new maximum value mx as the maximum between nums[i - 1] + k and nums[-1] - k. The nums[i - 1] + k is

the largest value of the incremented section, and nums[-1] - k is the largest value for the decremented section. 5. Update the score (ans) to be the minimum value between the current ans and the difference mx - mi. This ensures that with

each iteration, we are considering the lowest possible range after applying our operation at each pivot.

The sorted array itself is the primary data structure used. No additional data structures are required.

Iteration to explore possible optimal solutions by checking pivot points in the array.

need to look at the edges of the two blocks created by the pivot point.

Suppose we have the following nums array and integer k:

Data Structures:

6. Once the loop completes, ans contains the minimum score achievable after performing the add or subtract operation at each

Patterns: The use of sorting to establish a predictable order of elements, hence allowing for a methodical approach to finding the solution.

element in the most efficient manner. It elegantly handles the problem by transforming it into a series of operations where we only

By following these steps, the algorithm ensures that we calculate the minimum range after adding or subtracting k from each

1 nums = [4, 7, 1]

2 k = 5

Example Walkthrough

Let's go through the solution approach with a small example to better illustrate the algorithm.

Decision-making to update the candidate solution (ans) based on comparisons calculated within the loop.

According to the problem, we have to either add k to or subtract k from each element in the array to achieve the smallest possible score (the difference between the maximum and minimum elements of the array). Let's follow the solution approach:

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2. Initialize the score (ans):
  1 ans = nums[-1] - nums[0] -> ans = 7 - 1 -> ans = 6
```

1 nums.sort() -> nums = [1, 4, 7]

At index i = 1 (element 4):

1. Sort the array:

3. Iterate through the array starting from index 1:

1 ans = min(ans, mx - mi) -> ans = min(6, 6 - (-1)) -> ans = min(6, 7) -> ans = 6

1 ans = min(ans, mx - mi) -> ans = min(6, 9 - 2) -> ans = min(6, 7) -> ans = 6

4. Complete the loop: The algorithm has finished checking all possible pivot points in the array.

1 The minimum score achievable after adding or subtracting `k` from each element in nums is 6.

Calculate the possible minimum by adding k to the smallest value

Calculate the possible maximum by adding k to the previous value

smallest_range = min(smallest_range, possible_max - possible_min)

// Calculate the initial range from the first and last element of the sorted array.

Finally, return the smallest range after considering all elements.

Again, the score is 7, which does not improve the ans.

Now, we update the ans if mx - mi is smaller than the current ans:

1 mi = min(nums[0] + k, nums[i] - k) -> mi = min(1 + 5, 4 - 5) -> mi = min(6, -1) -> mi = -1

2 mx = max(nums[i-1] + k, nums[-1] - k) -> mx = max(1 + 5, 7 - 5) -> mx = max(6, 2) -> mx = 6

(No change in ans as the score is still 6 which is not better than the previous score) \circ At index i = 2 (element 7):

Now, update the ans:

 $1 \text{ mi} = \min(\text{nums}[0] + k, \text{ nums}[i] - k) -> \min = \min(1 + 5, 7 - 5) -> \min = \min(6, 2) -> \min = 2$ 2 mx = max(nums[i-1] + k, nums[-1] - k) -> mx = max(4 + 5, 7 - 5) -> mx = max(9, 2) -> mx = 9

For each index i, we will calculate the potential new minimum (mi) and maximum (mx) values after either adding or subtracting k:

Python Solution from typing import List

for i in range(1, len(nums)):

return smallest_range

// Get the length of the array

int minRange = nums[numsSize - 1] - nums[0];

// and the decreased current number

// and the decreased largest number

int newMin = min(nums[0] + k, nums[i] - k);

minRange = min(minRange, newMax - newMin);

1 // Array `nums` holds the numbers and `k` is the allowed modification range

for (int i = 1; i < numsSize; ++i) {</pre>

// Return the smallest range found

return minRange;

Typescript Solution

// Iterate through the sorted numbers starting from the second element

int newMax = max(nums[i - 1] + k, nums[numsSize - 1] - k);

// Determine the new minimum by comparing the increased smallest number

// Determine the new maximum by comparing the increased previous number

// Update the minRange with the minimum of the current and new ranges

int n = nums.length;

and subtracting k from the current value.

and subtracting k from the maximum value.

 $possible_max = max(nums[i - 1] + k, nums[-1] - k)$

Update the smallest range if a smaller one is found.

possible_min = min(nums[0] + k, nums[i] - k)

5. **Result**: The ans calculated is 6, which means:

class Solution: def smallestRangeII(self, nums: List[int], k: int) -> int: # First, sort the numbers to organize them in ascending order. nums.sort() # The initial range would be the max value minus the min value. smallest_range = nums[-1] - nums[0] # Loop through the sorted numbers, starting from the second element, # to find the minimum possible range.

In this example, the modifications to the elements are unnecessary, as the initial score is already minimal. The algorithm efficiently

identifies this by analyzing the potential effects of adding and subtracting k at each pivot point in the sorted array.

1 class Solution { public int smallestRangeII(int[] nums, int k) { // First, sort the input array to deal with numbers in a sorted order. Arrays.sort(nums);

Java Solution

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```
int minRange = nums[n - 1] - nums[0];
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           // Iterate through the array starting from the second element
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           for (int i = 1; i < n; ++i) {
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               // Calculate the minimum possible value after adding or subtracting k to the current or first element
               int currentMin = Math.min(nums[0] + k, nums[i] - k);
13
               // Calculate the maximum possible value after adding or subtracting k to the previous or last element
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               int currentMax = Math.max(nums[i - 1] + k, nums[n - 1] - k);
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               // Find the smallest range by comparing the current computed range and the previously stored minimum range
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               minRange = Math.min(minRange, currentMax - currentMin);
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           // Return the minimum range found
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           return minRange;
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22 }
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C++ Solution
 1 class Solution {
2 public:
       // Defines the function which will find the smallest range after modification
       int smallestRangeII(vector<int>& nums, int k) {
           // Initially, sort the array in non-decreasing order
           sort(nums.begin(), nums.end());
           int numsSize = nums.size(); // Store the size of the nums vector
           // Compute the initial range between the largest and smallest numbers
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// Sorts the array in non-decreasing order const sortArray = (a: number, b: number) => a - b;

2 let nums: number[];

let k: number;

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// Finds the smallest range after modification
   function smallestRangeII(nums: number[], k: number): number {
       // Sort the array in non-decreasing order
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       nums.sort(sortArray);
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       // Store the size of the nums array
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       const numsSize: number = nums.length;
15
       // Compute the initial range between the largest and smallest numbers
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       let minRange: number = nums[numsSize - 1] - nums[0];
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18
       // Iterate through the sorted numbers starting from the second element
       for (let i = 1; i < numsSize; ++i) {</pre>
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           // Determine the new minimum by comparing the increased smallest number and the decreased current number
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           const newMin: number = Math.min(nums[0] + k, nums[i] - k);
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24
           // Determine the new maximum by comparing the increased previous number and the decreased largest number
           const newMax: number = Math.max(nums[i - 1] + k, nums[numsSize - 1] - k);
26
27
           // Update the minRange with the minimum of the current and new ranges
           minRange = Math.min(minRange, newMax - newMin);
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30
       // Return the smallest range found
32
       return minRange;
33 }
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  // Example usage:
   // nums = [1, 3, 6];
37 // k = 3;
   // console.log(smallestRangeII(nums, k)); // Output would be the result of the smallestRangeII function
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Time and Space Complexity
```

The time complexity of the provided code depends on the sorting algorithm and the for loop.

nums.

Time Complexity

2. The for loop \rightarrow Iterates through the sorted list once, accounting for a time complexity of O(n).

Combining both, the time complexity remains dominated by the sorting step, and therefore, the overall time complexity is 0(n log

1. $nums.sort() \rightarrow The sort operation typically has a time complexity of <math>O(n \log n)$ where n is the number of elements in the list

- n). Space Complexity
 - The space complexity of the provided code is mainly due to the sorted list. 1. $nums.sort() \rightarrow The sort operation in Python is usually done in-place, which means the space complexity is <math>0(1)$.
- 2. No additional data structures are used that are dependent on the number of elements in the list, and therefore, no extra space is
- utilized that is proportional to the input size. Thus, the space complexity of the code is 0(1).