2012. Sum of Beauty in the Array

Problem Description

Medium Array

nums[i] at positions i from 1 to nums.length - 2, according to the following rules: • The beauty is 2 if nums[i] is greater than all preceding elements nums[j] where j < i, and less than all succeeding elements nums[k] where

In this problem, we are provided with a 0-indexed integer array nums. We need to determine the "beauty" for each element

- k > i. • The beauty is 1 if nums [i] is greater than the immediate preceding element nums [i - 1] and less than the immediate succeeding element
- nums [i + 1], but does not satisfy the condition for beauty 2. The beauty is 0 if none of the above conditions is satisfied.

Our goal is to calculate the sum of beauty for all such nums [i].

Intuition

the left of i and the minimum element to the right of i. This leads us to an efficient way to evaluate the beauty for each index.

1. Create two additional arrays, lmx and rmi, to record the maximum element observed from the beginning up to i - 1 and the minimum element observed from the end down to i + 1.

The solution builds on the key observation that to find the beauty of an index i, it suffices to determine the maximum element to

2. Iterate through the nums array from left to right, populating lmx by recording the maximum value seen so far. 3. Iterate through the nums array from right to left, populating rmi with the minimum value seen so far.

The approach is as follows:

4. Now, traverse the array again and for each i (from 1 to nums.length - 2), check the following:

∘ Else if nums[i - 1] < nums[i] < nums[i + 1] and the first condition is not satisfied, add 1 to the answer, marking beauty 1. 5. Sum the beauty values calculated for each i to get the final answer.

∘ If lmx[i] < nums[i] < rmi[i], add 2 to the answer since nums[i] satisfies the condition for beauty 2.

Solution Approach

To implement the solution, we follow these steps, making use of sequential iterations and auxiliary space for the arrays needed to keep track of maximum and minimum boundaries:

Initialization: Calculate the length n of the array nums.

 Initialize two arrays lmx and rmi of size n to keep track of the left maximum and right minimum values, respectively. lmx[i] will store the maximum value from the start of the array to index i - 1, and rmi[i] will store the minimum value from the end of the array to index i +

o rmi is filled with a very large number, 100001, to ensure that any real number in the array nums will be less than this placeholder value.

Populate lmx:

Populate rmi:

○ Iterate through nums from left to right starting from index 1 up to n - 1.

∘ Update lmx[i] such that it holds the maximum value seen up to nums[i - 1]. This is done using the formula lmx[i] = max(lmx[i - 1], nums[i-1]).

○ Iterate through nums from right to left starting from index n - 2 down to 0.

 \circ Iterate through the elements of nums from index 1 to n - 2 (inclusive).

Initialize lmx = [0, 0, 0, 0, 0] and rmi = [100001, 100001, 100001, 100001]

Initialize a variable ans to hold the sum of beauty scores.

• lmx is initially filled with 0 because there is no number before the start of the array.

 Update rmi[i] such that it holds the minimum value seen from nums[i + 1] to the end of the array. The formula used here is rmi[i] = min(rmi[i + 1], nums[i + 1]).Calculate the total beauty:

• Check if the beauty of nums[i] is 2 by comparing if lmx[i] < nums[i] < rmi[i]. If this condition is true, increment ans by 2. • Else if nums[i] does not qualify for a beauty of 2, check if it is greater than the element to its left and less than the element to its right (i.e., check if nums[i - 1] < nums[i] < nums[i + 1]). If true, increment ans by 1.

 If neither condition is satisfied, the beauty for that element is 0, so ans remains the same. **Return the result:** • After the loop completes, ans contains the sum of beauty for all nums[i], and we return this value.

The main data structures used in this solution are the arrays lmx and rmi for dynamic programming, which store computed

values that can be used to determine the beauty of each element efficiently. The algorithm makes use of max() and min()

functions for comparisons, and a single pass through the array (ignoring the separate passes for lmx and rmi initializations) to calculate the sum of beauty. This approach ensures that we have all the necessary information to evaluate the beauty of each element without using nested loops, which would result in a higher computational complexity.

Example Walkthrough

Step 1: Initialization

• n = 5 (length of nums)

Step 2: Populate lmx

• Starting from i = 1, iterate to i = 4: \circ lmx[1] = max(0, nums[0]) = 1

Let's walk through a small example to illustrate the solution approach. Consider the integer array nums = [1, 2, 3, 4, 2].

Step 3: Populate rmi

• Initialize ans = 0

• For i = 1 to n - 2:

 \circ For i = 1:

 Starting from i = 3, iterate to i = 0: \circ rmi[3] = min(100001, nums[4]) = 2

o rmi[0] = min(2, nums[1]) = 2 • Now rmi = [2, 2, 2, 2, 100001]

Step 4: Calculate the total beauty

 \circ lmx[2] = max(1, nums[1]) = 2

 \circ lmx[3] = max(2, nums[2]) = 3

 \circ lmx[4] = max(3, nums[3]) = 4

o rmi[2] = min(2, nums[3]) = 2

o rmi[1] = min(2, nums[2]) = 2

• Now lmx = [0, 1, 2, 3, 4]

lmx[1] is 1, nums[1] is 2, rmi[1] is 2. nums[1] is greater than lmx[1] but not less than rmi[1], so check next condition. nums[0] is 1, nums[1] is 2, nums[2] is 3. It satisfies nums[0] < nums[1] < nums[2], so add 1 to ans.</p> • For i = 2: lmx[2] is 2, nums[2] is 3, rmi[2] is 2. nums [2] does not satisfy any beauty conditions, so ans stays the same. \circ For i = 3: lmx[3] is 3, nums[3] is 4, rmi[3] is 2.

The final value of ans after the loop is 1.

def sumOfBeauties(self, nums: List[int]) -> int:

for i in range(1, num elements):

for i in range(1, num elements - 1):

public int sumOfBeauties(int[] nums) {

int sumOfBeauties(vector<int>& nums) {

for (int i = 1; i < size; ++i) {

for (int $i = size - 2; i >= 0; --i) {$

for (int i = 1; i < size - 1; ++i) {

totalBeauty += 2;

totalBeauty += 1;

return totalBeauty;

// Return the total beauty of the array.

leftMax[i] = max(leftMax[i - 1], nums[i - 1]);

rightMin[i] = min(rightMin[i + 1], nums[i + 1]);

if (leftMax[i] < nums[i] && nums[i] < rightMin[i]) {</pre>

// to its immediate neighbors, add 1 to total beauty.

else if $(nums[i - 1] < nums[i] && nums[i] < nums[i + 1]) {$

int size = nums.size();

Step 5: Return the result

Solution Implementation

from typing import List

Python

Java

C++

public:

class Solution {

class Solution {

class Solution:

 $max_left[i] = max(max_left[i - 1], nums[i - 1])$ # Populate min right by finding the minimum on the right for each position in nums for i in range(num elements -2, -1, -1): min_right[i] = min(min_right[i + 1], nums[i + 1])

beauty_sum = 0 # This variable will hold the cumulative beauty of the array

vector<int> leftMax(size); // Stores the maximum to the left of each element.

int totalBeauty = 0; // This will store the total beauty of the array.

// If the current element is greater than the maximum on its left

// and less than the minimum on its right, add 2 to total beauty.

// Populate leftMax by keeping track of the maximum number seen so far from the left.

// Populate rightMin by keeping track of the minimum number seen so far from the right.

// Calculate the beauty for each number in the array excluding the first and last element.

// If it doesn't meet the first condition but is still increasing with respect

// Function to calculate the sum of beauties for all elements in the array except the first and last.

Populate max left by finding the maximum on the left for each position in nums

num elements = len(nums) # Get the number of elements in the list

Loop through each element of the array except the first and last

return beauty_sum # Return the total accumulated beauty

int n = nums.length; // Get the length of the input array

nums[3] is greater than both lmx[3] and rmi[3], so it adds nothing to ans.

The result, which is the sum of beauty for all nums [i], is 1. This is the final answer to the problem.

In this particular example, the only element to contribute to the beauty sum was nums [1] with a beauty of 1.

 \max left = [0] * num elements # Initialize a list to store the maximum to the left of each position

Check if the element is greater than the max to the left and less than the min to the right

int[] leftMax = new int[n]; // Initialize an array to keep track of maximum values from the left

min_right = [100001] * num_elements # Initialize a list to store the minimum to the right of each position

if max left[i] < nums[i] < min right[i]:</pre> beauty sum += 2 # If it is, the beauty score for this number is 2 # Otherwise, check if the element is greater than its previous and less than its next element elif nums[i - 1] < nums[i] < nums[i + 1]: beauty_sum += 1 # If so, the beauty score for this number is 1

```
int[] rightMin = new int[n]; // Initialize an array to keep track of minimum values from the right
rightMin[n - 1] = 100001; // Set the last element to a high value as a sentinel
// Fill the leftMax array with the maximum value encountered from the left up to that index
for (int i = 1; i < n; ++i) {
    leftMax[i] = Math.max(leftMax[i - 1], nums[i - 1]);
// Fill the rightMin array with the minimum value encountered from the right up to that index
for (int i = n - 2; i >= 0; --i) {
    rightMin[i] = Math.min(rightMin[i + 1], nums[i + 1]);
int totalBeauty = 0; // Variable to hold the total sum of beauty
// Loop through the array, omitting the first and last element
for (int i = 1; i < n - 1; ++i) {
    // Check if the current element is larger than the maximum to its left and smaller than the minimum to its right
    if (leftMax[i] < nums[i] && nums[i] < rightMin[i]) {</pre>
        totalBeauty += 2; // Add 2 to beauty as it satisfies the special condition
    } else if (nums[i - 1] < nums[i] && nums[i] < nums[i + 1]) {
        totalBeauty += 1; // Add 1 to beauty if it's simply larger than its adjacent elements
// Return the sum of beauty of all elements
return totalBeauty;
```

vector<int> rightMin(size, 100001); // Stores the minimum to the right of each element, initially set high

};

TypeScript

```
function sumOfBeauties(nums: number[]): number {
   // Determine the length of input array.
    let n: number = nums.length;
   // Initialize prefix and postfix arrays to keep track of max and min values seen so far from either end.
    let prefixMax: number[] = new Array(n).fill(0);
    let postfixMin: number[] = new Array(n).fill(0);
   // Set the first element of prefix and the last element of postfix to be the corresponding values from 'nums'.
   prefixMax[0] = nums[0];
   postfixMin[n - 1] = nums[n - 1];
   // Fill the prefixMax and postfixMin arrays.
   for (let i: number = 1, j: number = n - 2; i < n; ++i, --j) {
        prefixMax[i] = Math.max(nums[i], prefixMax[i - 1]);
        postfixMin[j] = Math.min(nums[j], postfixMin[j + 1]);
   // Initialize the sum of beauties.
    let sumOfBeautyPoints: number = 0;
   // Check the beauty for each element, based on the conditions and update the sum accordingly.
    for (let i: number = 1; i < n - 1; ++i) {
       // Check for beauty level 2 condition.
        if (prefixMax[i - 1] < nums[i] && nums[i] < postfixMin[i + 1]) {</pre>
            sumOfBeautvPoints += 2:
       // Check for beauty level 1 condition.
        } else if (nums[i - 1] < nums[i] && nums[i] < nums[i + 1]) {</pre>
            sumOfBeautyPoints += 1;
   // Return the total sum of beauty points.
   return sumOfBeautyPoints;
from typing import List
class Solution:
   def sumOfBeauties(self, nums: List[int]) -> int:
        num elements = len(nums) # Get the number of elements in the list
        \max left = [0] * num elements # Initialize a list to store the maximum to the left of each position
```

 $min_right = [100001] * num_elements # Initialize a list to store the minimum to the right of each position$

Check if the element is greater than the max to the left and less than the min to the right

Otherwise, check if the element is greater than its previous and less than its next element

Populate max left by finding the maximum on the left for each position in nums

Populate min right by finding the minimum on the right for each position in nums

beauty sum += 2 # If it is, the beauty score for this number is 2

beauty_sum += 1 # If so, the beauty score for this number is 1

beauty_sum = 0 # This variable will hold the cumulative beauty of the array

Loop through each element of the array except the first and last

Time Complexity

Time and Space Complexity

for i in range(1, num elements):

for i in range(num elements -2, -1, -1):

if max left[i] < nums[i] < min right[i]:</pre>

elif nums[i - 1] < nums[i] < nums[i + 1]:

return beauty_sum # Return the total accumulated beauty

for i in range(1. num elements - 1):

 $max_left[i] = max(max_left[i - 1], nums[i - 1])$

min_right[i] = min(min_right[i + 1], nums[i + 1])

length of the input array nums, which is denoted as n. 1. The first loop initializes the lmx array, which takes 0(n) time as it iterates from 1 to n-1. 2. The second loop initializes the rmi array, which also takes O(n) time as it iterates from n-2 to O(n)

When we add these up, since they are executed in sequence and not nested, the overall time complexity of the code is O(n) +

The space complexity of the code is due to the additional arrays lmx and rmi that are both of length n, and the space used for

3. The third loop calculates the ans (answer) by iterating once again in linear time over the range from 1 to n-1, resulting in O(n) time.

The given code consists of three separate for loops that are not nested. Each of these loops runs linearly with respect to the

Space Complexity

2. The rmi array also uses O(n) space. Besides these arrays, only a constant amount of extra space is used for the loop indices and the ans variable. Thus, the total

variables like n, i, and ans.

1. The lmx array uses O(n) space.

O(n) + O(n), which simplifies to O(n).

auxiliary space used by the algorithm is O(n) + O(n) which simplifies to O(n). In conclusion, the time complexity of the algorithm is O(n) and the space complexity is O(n).