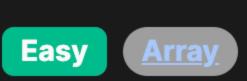
2873. Maximum Value of an Ordered Triplet I



Problem Description

You are provided with an array of integers, nums, which has a 0-based index. The goal is to find the maximum value of a triplet (i, j, k) in this array, following the condition that i, j, and k are distinct indices, with i being less than j, and j being less than k. In other words, you need to find the maximum value obtained from the formula (nums[i] - nums[j]) * nums[k] across all possible combinations of triplets.

In a case where the values for all possible triplets are negative, the result should be 0.

The problem asks for the efficient computation of this value without having to compare every possible triplet directly, which would be inefficient for large arrays.

Intuition

pieces of information as we iterate through the array from left to right. mx: This is the maximum value found in nums up to the current point in our traversal. We can think of it as the 'best' first

To avoid an exhaustive search which is highly inefficient, we observe that we can solve the problem by keeping track of two

- mx_diff: This represents the maximum value of mx nums[j], which is the first part of our target equation (nums[i] -
- nums [j]). It essentially stores the best-case scenario for the difference between the first and second elements of our triplet encountered so far.
- As we traverse the array, at each step, we attempt to update mx_diff with the largest possible value by considering the current mx and the current number num as if it were nums[j]. We also update mx if the current number is larger than the current mx. After updating mx and mx_diff, we then calculate the potential best-case scenario for the triplet value with the current number as

nums [k], and update the answer if it's greater than the current answer. **Solution Approach**

The solution implements a single pass approach, traversing the list once, which keeps it very efficient in terms of both time and

space complexity. The algorithm does not use any extra data structures, as it simply maintains two variables mx and mx_diff to track the maximum value found so far and the maximum difference encountered so far, respectively.

•

Initialize ans, mx, and mx_diff as zero. ans will hold the answer to be returned, mx is used to keep track of the maximum value in nums as we iterate, and mx_diff keeps track of the maximum value of mx - nums[j] found so far.

• Update the ans if the current mx_diff * num is greater than ans. This step checks if the current number as nums[k] combined with the best mx_diff so far makes for a higher product than we've seen.

Loop through each element num in nums. For each num:

The approach makes use of the following steps:

element nums [i] seen so far for any triplet.

 Update mx if num is greater than mx. This step simply keeps mx as the maximum value seen up to the current element in the array, representing the best choice for nums [i] up to this point.

During each iteration, the algorithm dynamically updates the potential first two elements of the triplet, which allows it to calculate

- Update mx_diff if mx num is greater than mx_diff. By doing this, you are ensuring that mx_diff holds the largest possible difference between the best nums [i] and any nums [j] seen so far.
- check every possible combination of i, j, and k, which is the key to its efficiency. Here is the pseudocode that captures the essence of the implementation:

By maintaining the maximum found value and the maximum difference during the iteration, the algorithm eliminates the need to

def maximumTripletValue(nums): ans = mx = mx_diff = 0 for num in nums:

the potential best-case scenario for the triplet value in constant time.

```
This algorithm runs in O(n) time, where n is the length of the input array, making it extremely efficient for large datasets.
Example Walkthrough
  Let's consider a small example array nums to illustrate the solution approach.
  Example nums array: [3, 1, 6, 4]
```

We initialize ans, mx, and mx_diff to 0.

We start with the first element 3:

Moving to the second element 1:

ans = $max(ans, mx_diff * num)$

mx_diff = max(mx_diff, mx - num)

mx = max(mx, num)

return ans

We have to find the maximum value of the expression (nums[i] - nums[j]) * nums[k] with the constraints i < j < k.

```
o ans remains of for the same reason.
```

```
    mx_diff remains 0 because we don't have a j yet.
```

 \circ We consider the element 1 as potential nums[j]. The difference mx - num is 3 - 1 = 2. • mx_diff is updated to 2 because 2 is greater than the current mx_diff which is 0. o ans is still 0 as we have not yet encountered a valid k.

o ans is updated to 12 because 12 is greater than the current ans which is 0.

Now we update mx to 6 because 6 is greater than the current mx which is 3.

∘ mx_diff does not change because mx - num is -3 which is not greater than 2.

```
Next, we process the third element 6:
```

After the second iteration: ans = 0, mx = 3, $mx_diff = 2$.

mx is updated to 3 because it's the only element we've seen.

After the first iteration: ans = 0, mx = 3, mx_diff = 0.

```
After the third iteration: ans = 12, mx = 6, mx_diff = 2.
```

Finally, we look at the fourth element 4:

```
    mx does not change because 4 is not greater than 6.

   \circ mx_diff is updated, as mx - num is 6 - 4 = 2, but since mx_diff is already 2, it remains the same.
    After the fourth and final iteration: ans = 12, mx = 6, mx_diff = 2.
At the end of the iterations, the maximum value found for the expression (nums[i] - nums[j]) * nums[k] is 12, which is the final
answer. The triplet that gives us this value is (3, 1, 6) where i = 0, j = 1, and k = 2. Therefore, the function
maximumTripletValue with the array [3, 1, 6, 4] as input will return 12.
```

 \circ We calculate mx_diff * num which is 2 * 4 = 8. However, ans remains 12 because 8 is not greater than 12.

• This element is considered as potential nums [k]. We compute $mx_diff * num which is 2 * 6 = 12$.

class Solution: def maximumTripletValue(self, nums: List[int]) -> int: # Initialize variables: # max_product - to keep track of the maximum product of max_difference and the current number, # max_number - to store the maximum value encountered so far, # max_difference - to store the maximum difference between max_number and any other number. max_product = 0

```
# Update max_number if the current num is greater than the previously stored max_number.
max_number = max(max_number, num)
# Update max_difference if the difference between the current max_number and num
# is greater than the previously stored max_difference.
```

return answer;

max_number = 0

max_difference = 0

for num in nums:

Iterate through all numbers in the list.

Update max_product with the maximum product obtained

by multiplying max_difference with the current num.

// Return the maximum product of a triplet found in the array

// Function to calculate the maximum product of a triplet in the array such that

long long maximumTripletValue(vector<int>& nums) {

// Loop through each number in the array 'nums'

int maxDifference = 0;

for (int num : nums) {

// the indices of the triplet (i, j, k) satisfy i < j < k and nums[i] < nums[j] < nums[k].

long long maxProduct = 0; // To store the maximum product of a triplet

maxProduct = max(maxProduct, static_cast<long long>(maxDifference) * num);

// Update maxProduct with the maximum between current maxProduct and the product

int maxElement = 0;
// To store the maximum element seen so far

max_product = max(max_product, max_difference * num)

Solution Implementation

from typing import List

Python

```
# with num potentially being the third element.
           max_difference = max(max_difference, max_number - num)
       # After iterating through all numbers, max_product will hold
       # the maximum product of a triplet's first and third elements.
       return max_product
Java
class Solution {
   public long maximumTripletProduct(int[] nums) {
       long maxVal = 0;  // Initialize maximum value found in the array to 0
       long maxDiff = 0;  // Initialize maximum difference between maxVal and any other value to 0
       long answer = 0;
                                  // Initialize the result for the maximum product of the triplet
       // Iterate through all elements in the nums array
       for (int num : nums) {
           // Update the answer with the maximum between the current max product
           // or the product of the current number and maxDiff
           answer = Math.max(answer, num * maxDiff);
           // Update maxVal with the maximum between the current maxVal or the current number
           maxVal = Math.max(maxVal, num);
           // Update maxDiff with the maximum difference found so far
           maxDiff = Math.max(maxDiff, maxVal - num);
```

This difference represents a potential first and second element of a triplet,

C++

public:

#include <vector>

class Solution {

#include <algorithm>

using namespace std;

```
maxElement = max(maxElement, num);
            // Update maxDifference with the maximum difference between maxElement and the current number 'num'
           maxDifference = max(maxDifference, maxElement - num);
        // Return the maximum product of a triplet found in the array
        return maxProduct;
};
TypeScript
// Calculates the maximum product of any triplet in the given array
// that can be formed by multiplying any three numbers which indices
// are strictly in increasing order.
function maximumTripletValue(nums: number[]): number {
   let maxProduct = 0; // Variable to store the maximum product found
    let maxNum = 0; // Variable to store the maximum number found so far
    let maxDifference = 0; // Variable to store the maximum difference found so far
    // Iterate through the array of numbers
    for (const num of nums) {
       // Update the maxProduct with the maximum between the current maxProduct and
       // the product of num and maxDifference which represents a potential triplet product
       maxProduct = Math.max(maxProduct, maxDifference * num);
        // Update the maxNum with the greatest number encountered so far
       maxNum = Math.max(maxNum, num);
        // Update the maxDifference with the greatest difference between maxNum and the current num
        maxDifference = Math.max(maxDifference, maxNum - num);
    // Return the maximum product found for the triplet
    return maxProduct;
```

// To store the maximum difference seen so far

// of maxDifference and the current number 'num'. This accounts for the third element of the triplet.

// Update maxElement with the maximum between current maxElement and the current number 'num'

```
# max_difference - to store the maximum difference between max_number and any other number.
max_product = 0
max_number = 0
max_difference = 0
```

class Solution:

from typing import List

Initialize variables:

for num in nums:

```
# Update max_product with the maximum product obtained
# by multiplying max_difference with the current num.
max_product = max(max_product, max_difference * num)
# Update max_number if the current num is greater than the previously stored max_number.
max_number = max(max_number, num)
```

Update max_difference if the difference between the current max_number and num

This difference represents a potential first and second element of a triplet,

max_product - to keep track of the maximum product of max_difference and the current number,

return max_product Time and Space Complexity

is greater than the previously stored max_difference.

max_difference = max(max_difference, max_number - num)

the maximum product of a triplet's first and third elements.

After iterating through all numbers, max_product will hold

with num potentially being the third element.

```
The time complexity of the given code segment is O(n), where n is the length of the array nums. This is because there is a single
for-loop that iterates over all the elements in the array once.
```

The space complexity is 0(1) since the extra space used does not grow with the input size; only a fixed number of variables ans, mx, and mx_diff are used regardless of the size of the input array.

def maximumTripletValue(self, nums: List[int]) -> int:

Iterate through all numbers in the list.

max_number - to store the maximum value encountered so far,