654. Maximum Binary Tree Medium **Divide and Conquer** Stack Array

Problem Description

build what's called a maximum binary tree. This tree is constructed using a specific set of rules: The maximum value in the array becomes the root node of the tree.

You are given an array named nums, which contains a set of integers and has no duplicate elements. Your task is to use this array to

Binary Tree

Monotonic Stack

- The subarray to the left of the maximum value is used to construct the left subtree of the tree by applying the same rule. Similarly, the subarray to the right of the maximum value is used to build the right subtree by applying the same rule.
- This process is recursive, meaning that you apply the same set of rules to each subarray (left and right of the maximum value found)
- to build the entire tree. The goal is to construct and return the maximum binary tree.
- Intuition

tree.

the array into two subarrays: one to the left and one to the right of where the maximum value was found. These subarrays will be used to construct the left and right subtrees, respectively. We follow the same strategy recursively for the subtrees.

This approach leads us to divide-and-conquer strategy, where we divide the problem into smaller instances of the same problem

(finding the maximum element and building left and right subtrees) and then combine the solutions (subtrees) to construct the final

To build the maximum binary tree, we need to find the maximum element in the array and make it the root of the tree. We then split

The provided solution uses a helper function dfs that implements this recursive strategy. The base case for the recursion is when there are no elements in the current subarray (nums), in which case the function returns None because there's nothing left to construct. When elements are present, the function:

2. Determines the index of this maximum value. 3. Creates a new tree node with the maximum value. 4. Recursively calls itself to build the left subtree with the elements to the left of the maximum value. 5. Recursively calls itself to build the right subtree with the elements to the right of the maximum value.

7. Returns the current tree node (which forms a part of the larger tree).

Solution Approach

1. Finds the maximum value in the current subarray.

- The recursion unwinds, building up the entire tree, which is finally returned by the outermost call to dfs.
- The solution implementation makes use of the divide-and-conquer strategy, recursion, and the binary tree data structure. Here's
- how these concepts are applied to construct the maximum binary tree: 1. Divide and Conquer: The array nums is repeatedly divided into two subarrays around the maximum value found. This approach

at which point the function returns None since there are no more nodes to create.

When employing recursion to build the tree, the approach is as follows:

6. Links the constructed left and right subtrees to the created node (now the parent node).

2. Recursion: To manage the repetitive task of building subtrees from subarrays, the solution implements a recursive helper

b. Create a new TreeNode with val as its value, which will serve as the root node for the current (sub)tree.

splits the problem into smaller problems, specifically building the left and right subtrees.

3. Binary Tree Construction: The nature of the problem requires constructing a binary tree, so the TreeNode class is used to create tree nodes. Each node has a value as well as potential left and right children, which correspond to the left and right subtrees.

val.

construction.

Example Walkthrough

approach solves this:

1. Find the maximum value in nums. In this case, it is 6.

The final maximum binary tree constructed from nums looks like this:

def __init__(self, val=0, left=None, right=None):

2. Since 6 is the maximum value, it will be the root of the maximum binary tree.

c. For the left child of the current node, recursively call dfs(nums[:i]), which constructs the subtree from the elements to the left of val.

d. For the right child, a similar recursive call is made with dfs(nums[i + 1:]) to build the subtree from the elements to the right of

e. After the recursive calls, the left and right children are connected to the root node of the subtree, thereby completing the subtree

Each recursive call builds a part of the tree and returns it to the calling function, which then attaches it to the appropriate left or right

a. Identify the maximum value val in the current subarray nums using the max() function and find its index i with nums.index(val).

function dfs(). Recursion continues until the base case is met, which occurs when the passed-in subarray is empty (not nums),

child of the current node. This step-by-step process continues until the original call returns the entire maximum binary tree, which is the final output of the constructMaximumBinaryTree function.

Let's walk through a small example to illustrate the solution approach. Let's say we have the following array nums:

1 nums = [3, 2, 1, 6, 0, 5]According to the problem description, we need to construct a maximum binary tree following the given rules. Here's how the

3. Divide the array into two subarrays around the maximum value found. Here we have left_sub = [3, 2, 1] and right_sub = [0, 5]. 4. To construct the left subtree, repeat the same process for left_sub. Find the maximum value, which is 3, and make it the left child of 6.

Now, 2 will have a right child which is 1, as 2 is the maximum and only element in the subarray to its left, and no elements are

6. For the right subtree of the root 6, we examine right_sub. The maximum value in [0, 5] is 5, so 5 becomes the right child of 6.

5. The subarray to the left of 3 is empty, so the left child of 3 would be None. The subarray to the right of 3 is [2, 1].

• Find the maximum value in [2, 1], which is 2, and make it the right child of 3.

to its right.

Python Solution

class Solution:

self.val = val

self.left = left

self.right = right

def build_max_tree(sub_nums):

return None

max_value = max(sub_nums)

root = TreeNode(max_value)

return build_max_tree(nums)

1 // Definition for a binary tree node.

this.val = val;

this.left = left;

private int[] nodeValues;

this.nodeValues = nums;

if (left > right) {

return null;

this.right = right;

TreeNode(int val) { this.val = val; }

TreeNode(int val, TreeNode left, TreeNode right) {

// Declare an array to hold the input values

if not sub_nums:

7. Repeat the process for the subarray to the left of 5, which is [0]. Since 0 is the only element, it becomes the left child of 5. No elements are to the right of 5, so its right child is None.

becomes the root of a subtree, with recursive calls constructing its children until the entire tree is built.

Helper function to construct the tree using a divide and conquer approach

Base case: if there are no numbers, return None

Find the maximum value in the list of numbers

Call the helper function with the initial list of numbers

This constructs a maximum binary tree as defined by the problem statement,

36 # where the root is the maximum number in the array, and the left and right subtrees

* This method constructs a maximum binary tree from the given array.

* @param left The left boundary (inclusive) of the current subarray.

* @param right The right boundary (inclusive) of the current subarray.

// Create the root node of the subtree with the maximum element

// Recursively construct the left subtree with the elements before the maximum element

// Recursively construct the right subtree with the elements after the maximum element

// Constructor to create a tree node with given values, default to 0 for val and null for left and right.

constructor(val: number = 0, left: TreeNode | null = null, right: TreeNode | null = null) {

// A maximum binary tree is a binary tree where every node has a value greater than its children.

TreeNode* root = new TreeNode(nums[maxIndex]);

// Return the root of the subtree

return root;

1 // Definition for a binary tree node.

left: TreeNode | null;

right: TreeNode | null;

this.val = val;

this.left = left;

this.right = right;

Typescript Solution

class TreeNode {

val: number;

root->left = constructTree(nums, left, maxIndex - 1);

root->right = constructTree(nums, maxIndex + 1, right);

// Function to construct a maximum binary tree from an array of numbers.

// If the array is empty, return null as no tree can be constructed.

return (currentMax[0] < value) ? [value, index] : currentMax;</pre>

function constructMaximumBinaryTree(nums: number[]): TreeNode | null {

// Base case: when the left index is greater than the right, we've gone past the leaf node

* @return The constructed maximum binary tree's root node.

public TreeNode constructMaximumBinaryTree(int[] nums) {

* @return The root node of the constructed subtree.

private TreeNode constructTreeInRange(int left, int right) {

* @param nums The input array containing elements to be used in the tree.

are constructed from the elements before and after the maximum number, respectively.

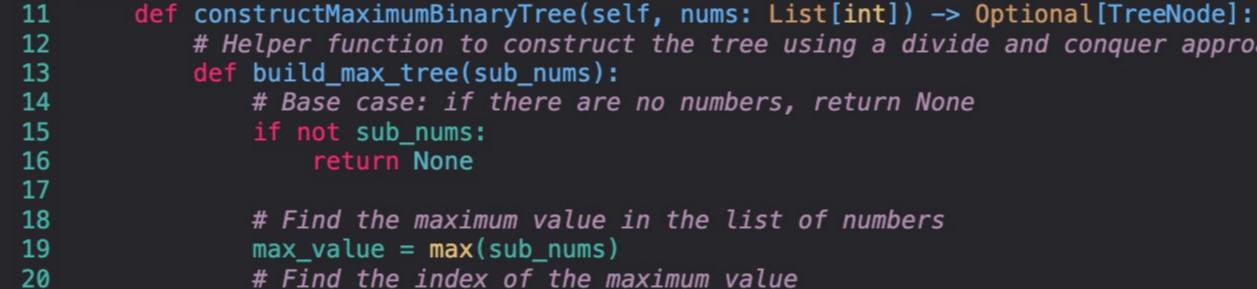
Find the index of the maximum value

max_index = sub_nums.index(max_value)

Create a tree node with the maximum value

- from typing import List, Optional # Definition for a binary tree node.

This example demonstrates the divide-and-conquer and recursive nature of the solution, where the maximum value in each subarray



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Java Solution

class TreeNode {

int val;

class Solution {

/**

TreeNode left;

TreeNode() {}

TreeNode right;

26 root.left = build_max_tree(sub_nums[:max_index]) 27 # Recursively build the right subtree using the elements to the right of the max value 28 root.right = build_max_tree(sub_nums[max_index + 1:]) 29 30 return root 31

Recursively build the left subtree using the elements to the left of the max value

27 // Start the recursive tree construction process from the full range (0 to length-1) return constructTreeInRange(0, nums.length - 1); 28 29 30 31 /** 32 * This private helper method creates the maximum binary tree recursively.

*/

*/

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           int maxIndex = left; // Start with the leftmost index
45
46
           // Find the index of the maximum element in the current subarray
47
           for (int j = left; j <= right; ++j) {</pre>
               if (nodeValues[maxIndex] < nodeValues[j]) {</pre>
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49
                   maxIndex = j;
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           // Create a new tree node with the maximum element as its value
           TreeNode root = new TreeNode(nodeValues[maxIndex]);
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           // Recursively construct the left subtree using elements left to the maximum element
56
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            root.left = constructTreeInRange(left, maxIndex - 1);
58
59
           // Recursively construct the right subtree using elements right to the maximum element
            root.right = constructTreeInRange(maxIndex + 1, right);
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61
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           return root; // Return the root node of the constructed subtree
63
64 }
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C++ Solution
     * Definition for a binary tree node.
      */
  4 struct TreeNode {
         int val; // The value of the node
         TreeNode *left; // Pointer to the left child
  6
         TreeNode *right; // Pointer to the right child
  8
  9
         // Constructor for a tree node with a given value, initially with no children
         TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
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         // Constructor for a tree node with given value, left and right children
 12
         TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}
 13
 14 };
 15
 16 class Solution {
 17 public:
 18
         /**
          * Constructs a maximum binary tree from the given integer array.
 19
          * @param nums The vector of integers.
          * @return The root TreeNode of the constructed maximum binary tree.
 21
 22
          */
 23
         TreeNode* constructMaximumBinaryTree(vector<int>& nums) {
             return constructTree(nums, 0, nums.size() - 1);
 24
 25
 26
    private:
 28
         /**
 29
          * Helper function to construct the maximum binary tree using Depth First Search.
          * @param nums The vector of integers.
 30
          * @param left The left boundary of the current segment.
 31
 32
          * @param right The right boundary of the current segment.
 33
          * @return The root TreeNode of the constructed maximum binary tree for the segment.
 34
 35
         TreeNode* constructTree(vector<int>& nums, int left, int right) {
             // If the current segment is invalid, return nullptr to indicate no subtree
 36
             if (left > right) return nullptr;
 37
 38
 39
             // Find the index of the maximum element in the current segment
 40
             int maxIndex = left;
             for (int currentIndex = left; currentIndex <= right; ++currentIndex) {</pre>
 41
                 if (nums[maxIndex] < nums[currentIndex]) {</pre>
 42
 43
                     maxIndex = currentIndex;
 44
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if (nums.length === 0) { 20 return null; 21 22 23 // Find the maximum value and its index in the array. // The reduce method processes each number, keeping track of the largest number and its index. 24 let maxValueIndex = nums.reduce<[number, number]>((currentMax, value, index) => {

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13 }

59 };

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       }, [-Infinity, -1]);
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       // Destructure the result to get max value and index.
       const [maxValue, maxIndex] = maxValueIndex;
32
       // Recursively build the tree:
33
       // - The maximum value becomes the root.
       // - The left child is constructed from the subarray left of the maximum value.
34
       // - The right child is constructed from the subarray right of the maximum value.
       let rootNode = new TreeNode(
           maxValue,
           constructMaximumBinaryTree(nums.slice(0, maxIndex)),
39
           constructMaximumBinaryTree(nums.slice(maxIndex + 1))
       );
40
41
       // Return the constructed tree node.
43
       return rootNode;
44 }
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Time and Space Complexity
Time Complexity
The time complexity of the function constructMaximumBinaryTree is determined by multiple factors: the number of elements in the
nums list, finding the maximum value in the current portion of the list, splitting the list into two parts, and recursively building the left
and right subtrees.
  1. For each node of the binary tree, finding the maximum element takes O(n) time where n is the number of elements in the current
    portion of the list.
 2. The nums.index(val) operation also takes O(n) time for each node to find the index of the maximum element.
 3. The dfs function is called recursively for each element in the list to create a node, meaning there will be n calls in total (where n
```

reduce the problem size by 1 each time. **Space Complexity**

is the size of the original list).

1. In the best case (when the input list is already balanced), the depth of the recursive stack is 0(log n) since the tree would be roughly balanced. This would happen when the maximum element always ends up being in the middle of the current subarray. 2. In the worst case (input list is sorted), the depth of the recursive stack is 0(n) because the constructed tree would be skewed (like a linked list), and hence we would have a chain of recursive calls equal to the size of the input list.

Considering the recursive nature and that finding the max and index takes linear time at each level of recursion, the total time

The space complexity is determined by the recursive stack depth and the space needed to store the constructed binary tree.

complexity is 0(n^2) in the worst case, when the input list is sorted in ascending or descending order, causing the divide step to only

Because the space needed to store the binary tree is O(n) and the recursive stack space in the worst case is also O(n), the overall space complexity is O(n).