2875. Minimum Size Subarray in Infinite Array

Medium Array Hash Table Prefix Sum Sliding Window

Problem Description

You are given an array called nums, which starts from the index 0. There is also an integer called target. There's a hypothetical array called infinite_nums, which is made by continuously repeating the nums array infinitely. Your task is to find the shortest contiguous subarray within infinite_nums that adds up to the target value. The length of this subarray (the number of elements it includes) is what you need to return. If such a subarray can't be found, you must return -1. For example, if nums is [1,2,3] and the target is 5, you can use the subarray [2,3] from nums or [3,1,1] from infinite_nums, both

Leetcode Link

sum up to 5 but the shortest length is 2 from the [2,3] subarray in nums.

Intuition

The intuition behind the solution is to use mathematical properties and an efficient data structure to avoid direct iteration through the infinite array, which would be impractical.

First, calculate the sum of all elements in nums, which is referred to as s. Compare s with the target. If the target is larger than s, then you can construct part of the required subarray using whole chunks of nums, each of which contributes s to the overall sum. This means you can repeatedly subtract s from target until target is less than s, and count how many times you've done this as part

of the subarray length. Then, the problem is reduced to two cases within the original nums array: 1. Find the shortest subarray that sums up exactly to target. 2. If it's not possible (because target is now less than s after subtraction), find two subarrays where one is at the start and one is

at the end of nums such that their total sum equals s - target. This effectively simulates wrapping around due to the infinite

nature of infinite_nums.

- To achieve this efficiently, we use a prefix sum array and a hash table. The prefix sum array allows us to calculate the sum of any subarray quickly, and the hash table lets us lookup whether a needed sum to reach the target has been seen before as we iterate through nums. When we find such sums, we can calculate the length of the subarray that reaches the target.

With the above strategy, we ensure that we can get our answer without explicitly dealing with the infinite array, all while maintaining

Solution Approach The given solution approach leverages a combination of prefix sums and hash tables to solve the problem with efficiency.

Here's a step-by-step breakdown of the implementation:

2. Initialize a hash table pos to keep track of the last position of every prefix sum encountered. Set the prefix sum for an empty

3. Initialize a variable pre to hold the ongoing prefix sum as we iterate through the array and a variable b as inf (infinity) which will

1. Compute the sum s of the entire nums array. Then check if target is greater than s. If yes, you can cover a significant portion of

the target by using whole arrays of nums. Calculate a = n * (target // s), which denotes the array length contributed by the

complete nums blocks. After this, subtract (target // s * s) from target, reducing the problem to finding a shorter subarray

good time complexity.

that sums up to the new target. If the new target matches s, return n since it is the shortest subarray that can be formed by the whole array.

4. Iterate through the nums array, updating the pre (prefix sum) by adding each element x from nums to it.

array to -1 to handle cases where the subarray starts at the beginning of nums.

later hold the length of the shortest qualifying subarray found.

algorithm avoids the need for nested loops, resulting in an efficient solution.

Also, initialize b as inf which indicates the shortest found subarray (to be minimized).

solution approach. If no such subarray exists, -1 would be returned.

num_count = len(nums) # Get the length of the array

If target equals total_sum, return the array length

min_length = inf # Set initial min length to infinity

min_length = min(min_length, i - pos[t])

if (t := prefix_sum - (total_sum - target)) in pos:

prefix_sum = 0 # Initialize the prefix sum

if (t := prefix_sum - target) in pos:

num_full_rotations = (target // total_sum) * num_count

pos = {0: -1} # Create a dictionary to store the prefix sum indices

Check if there is a circular subarray that sums to target

min_length = min(min_length, num_count - (i - pos[t]))

Check if there's a subarray that ends at index i with sum equals target

Initialize an 'a' which is the number of complete array rotations required

5. Two main checks are performed for each iteration: ∘ If the difference t = pre - target exists in pos, it means a subarray sums up to target. Update b to be the minimum of its current value or the distance from the current index to the index stored in pos[t].

∘ If the difference t = pre - (s - target) exists in pos, it implies that there's a contiguous subarray from the start and end of

Otherwise, return -1 indicating that a subarray satisfying the conditions does not exist. This approach uses a hash table to store prefix sums and their corresponding last index. This data structure combined with the

prefix sum concept allows us to find contiguous subarrays that add up to a target effectively. By doing this in a single pass, the

nums which together add up to target. Again, update b to be the minimum of its current value or n - (i - pos[t]).

6. After the loop, check if b has changed from inf. If it has, this means a valid subarray was found, and the solution returns a + b.

Let's illustrate the solution approach using a small example. Suppose the given nums array is [3, 1, 2], and the target is 6. We want to find the shortest contiguous subarray within infinite_nums that sums up to 6.

directly return the length of nums, which is 3, as the shortest subarray because using the whole nums array once sums to the target. However, for sake of walkthrough, let's proceed as if we were to look for a subarray since often the target might not exactly match s.

2. Initialize a hash table pos with -1 as the prefix sum for an empty array, and a variable pre for ongoing prefix sums starting at 0.

1. First, we compute the sum s of the entire nums array, which in this case is 3 + 1 + 2 = 6. Since target is equal to s, we can

3. As we iterate, we build our prefix sum array on the fly, and update pos with the last position we encountered a specific prefix

equals 3.

Python Solution

from math import inf

num_full_rotations = 0

if target > total sum:

if target == total_sum:

return num_count

sum.

Example Walkthrough

Following the solution approach:

4. We start iterating nums: \circ At index 0, pre becomes 3. pos does not have pre - target = 3 - 6 = -3, so we continue. \circ At index 1, pre becomes 4. pos does not have pre - target = 4 - 6 = -2, so we continue.

• At index 2, pre becomes 6, pos does have pre - target = 6 - 6 = 0, which is the prefix sum for an empty array, so we find

that subarray [3, 1, 2] sums to target. We update b to current index (2) plus one minus -1 (position of 0 in pos), which

subarray that sums up to the target. In this case, iteration reveals that using the entire array nums itself is the shortest subarray to reach the target of 6. In scenarios

5. After the iteration, b is no longer inf; it's 3. So, we can directly return the length 3, indicating that [3, 1, 2] is the shortest

where target is not equal to s, the method would identify the shortest contiguous subarray as per the steps described in the

class Solution: def minSizeSubarray(self, nums: List[int], target: int) -> int: total_sum = sum(nums) # Calculate the total sum of all numbers in the array

target -= (target // total sum) * total sum # Update the target after the full rotations

Traverse through the array 23 for i, num in enumerate(nums): 24 prefix_sum += num # Update prefix sum 25

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               # Store the latest index of this prefix sum
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                pos[prefix_sum] = i
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37
           # If min_length is still infinity, no subarray was found. Return -1.
           # Otherwise, return the answer which includes the rotations 'a' + the found subarray length 'b'
38
39
            return -1 if min_length == inf else num_full_rotations + min_length
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Java Solution
  import java.util.Arrays;
2 import java.util.HashMap;
   import java.util.Map;
   class Solution {
6
       // Function to find the smallest subarray sum greater than or equal to the target
       public int minSizeSubarray(int[] nums, int target) {
           // Compute the sum of all elements in the array
            long totalSum = Arrays.stream(nums).sum();
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            int length = nums.length;
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           int additionalElements = 0;
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14
           // If target is greater than the total sum, scale the number of times the whole array is needed
15
           if (target > totalSum) {
                additionalElements = length * (target / (int) totalSum);
               target -= target / totalSum * totalSum;
18
19
20
           // If the target is now equal to the total sum, simply return the length of the array
21
           if (target == totalSum) {
22
                return length;
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24
25
           // Create a map to store the prefix sum and its corresponding index
           Map<Long, Integer> prefixSumToIndex = new HashMap<>();
26
27
           prefixSumToIndex.put(0L, -1); // Initialize with 0 sum at index -1
28
            long currentPrefixSum = 0;
            int minSize = Integer.MAX_VALUE; // Start with the maximum possible value
29
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31
           // Iterate through the array to find the minimum size subarray
32
           for (int i = 0; i < length; i++) {</pre>
33
               currentPrefixSum += nums[i];
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// If the prefix sum indicating the end of subarray achieving the target is seen before

if (prefixSumToIndex.containsKey(currentPrefixSum - (totalSum - target))) {

// Otherwise, return the minimum size added by the number of additional elements needed

minSize = Math.min(minSize, i - prefixSumToIndex.get(currentPrefixSum - target));

// Check if there's a complement subarray sum that together with the currentPrefixSum gives totalSum

minSize = Math.min(minSize, length - (i - prefixSumToIndex.get(currentPrefixSum - (totalSum - target))));

if (prefixSumToIndex.containsKey(currentPrefixSum - target)) {

// Update the map with the current prefix sum and index

// If minSize is unchanged, no such subarray exists; return -1.

return minSize == Integer.MAX_VALUE ? -1 : additionalElements + minSize;

prefixSumToIndex.put(currentPrefixSum, i);

C++ Solution

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let repeatedFullArrayCount = 0;

if (target > totalSum) {

if (target === totalSum) {

let runningSum = 0;

return nums.length;

let minSubarraySize = Infinity;

runningSum += nums[i];

for (let i = 0; i < nums.length; ++i) {</pre>

```
#include <vector>
  2 #include <numeric>
    #include <unordered map>
    #include <algorithm>
  6 class Solution {
    public:
         int minSizeSubarray(vector<int>& nums, int target) {
             // Calculate the total sum of the array
             long long totalSum = accumulate(nums.begin(), nums.end(), 0LL);
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 11
             int n = nums.size();
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             // Calculate how many complete arrays are needed to reach close to the target
             int completeArraysCount = 0;
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 15
             if (target > totalSum) {
 16
                 completeArraysCount = n * (target / totalSum);
 17
                 target -= (target / totalSum) * totalSum;
 18
 19
 20
             // If target equals totalSum, a complete array is needed
 21
             if (target == totalSum) {
 22
                 return n;
 23
 24
 25
             // Hash map to keep track of the prefix sum and its corresponding index
 26
             unordered_map<int, int> prefixSumIndex{{0, -1}};
 27
 28
             long long prefixSum = 0; // Initialize prefix sum
             int minLength = 1 << 30; // Initialize the minimum length to a very large number</pre>
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 31
             // Iterate over the array to find the minimum subarray
 32
             for (int i = 0; i < n; ++i) {
 33
                 prefixSum += nums[i]; // Update the prefix sum
 34
 35
                 // Check if there is a subarray with sum equal to (prefixSum - target)
 36
                 if (prefixSumIndex.count(prefixSum - target)) {
 37
                     minLength = min(minLength, i - prefixSumIndex[prefixSum - target]);
 38
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 40
                 // Check if there is a subarray that, when added to the current subarray, gives the complement to the target
                 if (prefixSumIndex.count(prefixSum - (totalSum - target))) {
 41
                     minLength = min(minLength, n - (i - prefixSumIndex[prefixSum - (totalSum - target)]));
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 45
                 // Update the index for the current prefix sum
 46
                 prefixSumIndex[prefixSum] = i;
 47
 48
 49
             // If minLength has not been updated, return -1, as no valid subarray exists.
             // Otherwise, return the minimum length found plus the count of complete arrays needed.
 50
             return minLength == 1 << 30 ? -1 : completeArraysCount + minLength;
 51
 52
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    };
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Typescript Solution
  1 // This function finds the minimal length of a contiguous subarray of which the sum is at least the target value.
  2 // If there is no such subarray, the function returns -1.
    function minSizeSubarray(nums: number[], target: number): number {
        // Calculate the sum of the entire array.
         const totalSum = nums.reduce((acc, num) => acc + num);
```

Time Complexity

Time and Space Complexity

minSubarraySize = Math.min(minSubarraySize, i - prevIndex); 36 37 38 39 // Similar check as above, accounting for the case where sum of nums minus target exists as a prefix sum. 40 // This helps in covering scenarios where the sum cycles through the array. 41 if (prefixSums.has(runningSum - (totalSum - target))) { const prevIndex = prefixSums.get(runningSum - (totalSum - target))!; 42 43 minSubarraySize = Math.min(minSubarraySize, nums.length - (i - prevIndex)); 44 45 46 // Update the prefix sum map with the current running sum and index. 47 prefixSums.set(runningSum, i); 48 49 50 // If no subarray was found that adds up to the target, return -1. 51 // Otherwise, return the count of full array repetitions plus the found subarray size. 52 return minSubarraySize === Infinity ? -1 : repeatedFullArrayCount + minSubarraySize;

// Initial preparations: calculation of repetitions of the full array sum to reach the target.

// Decrease the target by the amount already covered by the full array repetitions.

// If after the subtraction the target equals the total sum, we can return the array length.

// Calculate how many times we can fit the total sum into the target sum.

repeatedFullArrayCount = Math.floor(target / totalSum);

// Map to store the prefix sum and its corresponding index.

// Iterate over the array to find the minimum length subarray.

// If it does, we possibly found a smaller subarray.

if (prefixSums.has(runningSum - target)) {

prefixSums.set(0, -1); // Initialize with prefix sum of 0 and index -1.

// Variables for running prefix sum and the minimum size of the subarray found.

// Check if the current prefix sum, minus the target, already exists.

const prevIndex = prefixSums.get(runningSum - target)!;

target -= repeatedFullArrayCount * totalSum;

const prefixSums = new Map<number, number>();

through each element of nums exactly once. The operations within the loop have constant time complexity, such as the calculation of the running sum (pre), checking for the existence of a value in the hash table (pos), and updating the hash table. As a result, these constant-time operations do not change the overall linear time complexity.

Space Complexity The space complexity of the function is also O(n), which comes from the use of a hash table post hat keeps track of the indices of the prefix sums. In the worst case, if all prefix sums are unique, the hash table will have as many entries as there are elements in nums. Therefore, the space used by the hash table is directly proportional to the size of the input array, leading to linear space complexity.

The time complexity of the function is O(n) where n is the length of the array nums. This is because there is a single loop that goes