Monotonic Queue

Sliding Window

Problem Description

Array

Queue

Hard

You are provided with an array of integers called nums, and two specific integers known as mink and maxk. The goal is to find and count the number of subarrays within nums that adhere to two criteria:

The largest number in the subarray is exactly maxk.

The smallest number in the subarray is exactly mink.

To clarify, a subarray is defined as a contiguous segment of the array. It is essential to understand that any subarray meeting these

conditions is considered a "fixed-bound subarray". The solution requires you to return the total count of such fixed-bound subarrays. Intuition

The problem is essentially asking us to isolate segments of the nums array where the range of values is strictly bounded between

subarrays.

 The most recent positions where mink and maxk were found, since these will be the bounds of our subarrays. • The last position where a value outside the acceptable range (less than mink or greater than maxk) was encountered because

mink and maxk (both inclusive). To solve this, we need to keep track of certain positions within our array:

We iterate through the array while tracking these positions. For each new element: 1. If the current element is out of bounds (< mink or > maxk), we mark the current position as the starting point for future valid

3. If the current element is equal to maxk, we update the position tracking maxk.

2. If the current element is equal to mink, we update the position tracking mink.

this will help us determine the starting point of a new possible subarray.

- The key insight here is that a new valid subarray can be formed at each step if the most recent mink and maxk are found after the last
- out-of-bounds value. The length of each new subarray added will be from the latest out-of-bound index until the minimum of the indices where mink and maxk were most recently found.

explicitly list or generate them. This makes the solution efficient as it has a linear complexity with respect to the length of the input array.

By performing these steps for each element, we are effectively counting all possible fixed-bound subarrays without having to

Solution Approach The solution approach can be broken down into a few distinct steps that relate to the iteration over the nums array:

j1 will keep track of the most recent position where mink has been found. j2 will keep track of the most recent position where maxK has been found.

discovered.

as the final result.

cannot extend beyond this point.

k signifies the most recent index before the current position where a number not within the mink and maxk range was

v the value at each index.

1. Initialization: We start by initializing three pointers j1, j2, and k to -1.

- o If v is not within the range [minK, maxK] (v < minK or v > maxK), we update k to the current index i, since valid subarrays
- If v equals mink, we update j1 to be the current index i. Similarly, if v equals maxk, we update j2.

2. Iteration and Tracking: The program iterates over the array nums using a for-loop, with the variable 1 representing the index, and

at index i, by calculating $\max(0, \min(j1, j2) - k)$. This effectively counts the number of new subarrays where $\min K$ and maxK are the minimum and maximum values respectively, and which do not include any out-of-bound elements before k.

4. Result: After the loop concludes, ans holds the total number of fixed-bound subarrays that can be found in nums. We return ans

Key Algorithm: After updating the pointers, we calculate the additional number of valid subarrays that include the element v

By employing pointers to keep track of recent occurrences of mink and maxk, and the cut-off point for valid subarrays (k), the solution efficiently leverages a sliding window technique to count subarrays without actually constructing them. The use of pointers (j1, j2,

3. Incremental Summation: We accumulate this count in ans with ans $+= \max(0, \min(j1, j2) - k)$.

efficiency since it means we only need to iterate through the array once, giving us a time complexity of O(n). Example Walkthrough

and k) to delineate bounds of subarrays is a common pattern in array processing problems and is a cornerstone of this solution's

1 nums = [1, 2, 3, 4, 5, 1, 2, 5, 3]Now let's walk through the procedure step-by-step:

Let's illustrate the solution approach using a small example. Consider the following array nums, with mink set to 2 and maxk set to 5:

j1 = −1 (most recent mink position) j2 = −1 (most recent maxK position)

1. Initialization:

 \circ k = -1 (last out-of-bound position)

j2

-1

-1

-1

-1

4

4

0

5

5

Valid Subarray length

max(0, min(-1, -1) - 0) = 0

max(0, min(1, -1) - 0) = 0

max(0, min(1, -1) - 0) = 0

max(0, min(1, 4) - 0) = 1

max(0, min(1, 4) - 5) = 0

max(0, min(6, 4) - 5) = 0

0 $\max(0, \min(1, -1) - 0) = 0$

ans

0

j1

-1

1

1

6

2. Iteration and Tracking:

nums[i]

3

1

2

0

3

5

6

6

13

14

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32

1 from typing import List

class Solution:

out of range, update k to i minK found, update j1 to i 2

Action

maxK found, update j2 to i 5

ans = 0 (accumulator for the count of valid subarrays)

within range, no pointer update

within range, no pointer update

out of range, update k to i

minK found, update j1 to i

	7	5	maxK found, update j2 to i	6	7	5	max(0, min(6, 7) - 5) = 1	2	
	8	3	within range, no pointer update	6	7	5	max(0, min(6, 7) - 5) = 1	3	
as t	heir r	naximum				d sub	arrays within nums that have	minK a	s their minimum and maxK
			subarrays accounted for in this exampostations at index 1	ole ar	e:				
	[2,	5] startin	ng at index 6						
	[2,	5, 3] sta	rting at index 6						
Eac	h tim	e we enc	ounter a valid subarray, we update ou	ır acc	umul	ator	ans, which eventually gives u	is the c	ount of all valid subarrays
by t	he tir	ne we rea	ach the end of the array.						
Ру	tho	n Solu	ıtion						

Initialize pointers for tracking the positions of min_k, max_k, and out-of-range elements

Add to the count the number of valid subarrays ending with the current element

valid_subarrays_count += max(0, min(last_min_k, last_max_k) - last_out_of_range)

which is determined by the smallest index among last_min_k and last_max_k after the

def count_subarrays(self, nums: List[int], min_k: int, max_k: int) -> int:

Invalidate the subarray if the value is out of the specified range

last_min_k = last_max_k = last_out_of_range = -1

Update the last seen index for min_k, if found

Update the last seen index for max_k, if found

long long countSubarrays(vector<int>& nums, int minK, int maxK)

int lastMinIndex = -1; // Index of the last occurrence of minK

long long answer = 0; // Variable to store the final count of subarrays

if value < min_k or value > max_k:

last_out_of_range = index

if value == min_k:

if value == max_k:

return valid_subarrays_count

last_min_k = index

 $last_max_k = index$

last out-of-range element

Return the total count of valid subarrays

Initialize the counter for the valid subarrays valid_subarrays_count = 0 9 10 11 # Iterate through the list, checking each number against min_k and max_k 12 for index, value in enumerate(nums):

```
Java Solution
   class Solution {
       public long countSubarrays(int[] nums, int minK, int maxK) {
            long totalCount = 0; // Variable to store the total count of subarrays
           int lastMinIndex = -1; // Index of the last occurrence of minK
            int lastMaxIndex = -1; // Index of the last occurrence of maxK
           int lastInvalidIndex = -1; // Index of the last element not in [minK, maxK]
           // Iterate over each element in the array
           for (int currentIndex = 0; currentIndex < nums.length; ++currentIndex) {</pre>
 9
               // If the current element is outside of the [minK, maxK] range, update lastInvalidIndex
10
               if (nums[currentIndex] < minK || nums[currentIndex] > maxK) {
11
                    lastInvalidIndex = currentIndex;
12
13
14
               // If the current element is equal to minK, update lastMinIndex
15
               if (nums[currentIndex] == minK) {
16
                    lastMinIndex = currentIndex;
17
18
19
               // If the current element is equal to maxK, update lastMaxIndex
20
               if (nums[currentIndex] == maxK) {
21
22
                    lastMaxIndex = currentIndex;
23
24
25
               // Calculate the number of valid subarrays ending at the current index
26
               // It is the distance between the last invalid index and the minimum of the last occurrences of minK and maxK
27
               totalCount += Math.max(0, Math.min(lastMinIndex, lastMaxIndex) - lastInvalidIndex);
28
29
            return totalCount; // Return the total count of valid subarrays
30
31
32 }
33
```

// Counts and returns the number of subarrays where the minimum value is at least minK and the maximum value is at most maxK.

int lastMaxIndex = -1; // Index of the last occurrence of maxK int lastIndexOutsideRange = -1; // Index of the last number that is outside the [minK, maxK] range 9 // Iterate through the array to count valid subarrays 10 for (int i = 0; i < nums.size(); ++i) {</pre> 11

C++ Solution

1 class Solution {

2 public:

```
// If current element is outside the [minK, maxK] range, update the index
12
13
               if (nums[i] < minK || nums[i] > maxK) lastIndexOutsideRange = i;
14
               // If current element equals minK, update the index of the last occurrence of minK
15
               if (nums[i] == minK) lastMinIndex = i;
               // If current element equals maxK, update the index of the last occurrence of maxK
16
               if (nums[i] == maxK) lastMaxIndex = i;
17
18
               // Count subarrays ending at index i which have minK and maxK within them
19
               answer += max(0, min(lastMinIndex, lastMaxIndex) - lastIndexOutsideRange);
20
21
22
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           return answer; // Return the total count of valid subarrays
24
25 };
26
Typescript Solution
   function countSubarrays(nums: number[], minK: number, maxK: number): number {
       let result = 0; // This will hold the final count of subarrays
       let minIndex = -1; // Stores the latest index of the element equal to minK
       let maxIndex = -1; // Stores the latest index of the element equal to maxK
       let invalidIndex = -1; // Stores the latest index of the element outside of the [minK, maxK] range
6
       nums.forEach((number, index) => {
           if (number === minK) {
               minIndex = index; // Update minIndex when we find an element equal to minK
10
           if (number === maxK) {
11
12
               maxIndex = index; // Update maxIndex when we find an element equal to maxK
13
           if (number < minK || number > maxK) {
               invalidIndex = index; // Update invalidIndex for numbers outside the range
```

Time Complexity: The time complexity of the code can be determined by analyzing the for loop since it is the only part of the code that iterates

});

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23

24 Time and Space Complexity

// Calculate the number of valid subarrays that end at the current index

result += Math.max(Math.min(minIndex, maxIndex) - invalidIndex, 0);

return result; // Return the total count of valid subarrays

The provided code snippet is designed to count the number of subarrays within an array nums where the minimum element is mink

and the maximum element is maxk. To analyze the computational complexity, we will examine the time taken by each component of the code and then aggregate these components to get the final complexity.

- Because there are no nested loops or recursive calls, the time complexity is directly proportional to the number of elements in the nums list.
- Inside the for loop, the code performs constant-time checks and assignments (such as comparison, assignment, and max operations), and these do not depend on the size of the input.

through the list of elements. • The for loop iterates through each element of nums exactly once, meaning the loop runs for n iterations, where n is the number of

Therefore, the **time complexity** of the code is O(n).

elements in nums.

Space Complexity:

- For space complexity, we look at the extra space required by the algorithm, not including the input and output: • The code uses a fixed number of variables (j1, j2, k, ans, and i), and no additional data structures that grow with the input size
- The space required for these variables is constant and does not scale with the size of the input list nums. As a result, the space complexity of the code is 0(1), meaning it requires a constant amount of extra space.

are used.