

Problem Description

In this problem, we are given in houses in a row and each house can be painted with one of k colors. The costs of painting each house with a certain color are provided in a two-dimensional array (matrix) called costs. The costs matrix has n rows (representing each house) and k columns (representing each color's cost for that house). For example, costs[i][j] gives the cost of painting the 1-th house with the 1-th color. The main objective is to determine the minimum total cost to paint all the houses while ensuring that no two adjacent houses are painted the same color.

Intuition

color. However, we must make this decision considering the cost of the current house as well as ensuring that it doesn't have the same color as the adjacent house. We approach the solution dynamically, by building up the answer as we go along. We initialize our answer with the cost of painting the first house, which is simply the costs of painting that house with each color

The intuition behind solving this problem lies in breaking it down into a sequence of decisions, where for each house we choose a

- (the first row of our costs matrix). Then for each subsequent house, we update the cost of painting it with each color by adding the minimum cost of painting the
- previous house with a different color. This ensures we meet the requirement that no two adjacent houses share the same color. • To efficiently perform this operation, we maintain a temporary array g which stores the new costs calculated for painting the
- excluding the j-th color. • We then add the current cost (costs[i][j]) to this minimum cost and store it in g[j]. At the end of each iteration, we assign g to f, so that f now represents the costs of painting up to the current house.

current house. For each color j, we find the minimum cost from the array f (which stores the costs for the previous house)

- After processing all houses, f will contain the total costs of painting all houses where the last house is painted with each of the k colors. Our answer is the minimum of these costs.
- Through dynamic programming, the code optimizes the painting cost by cleverly tracking and updating the costs while satisfying the problem's constraints.

Solution Approach The implementation of the solution follows a dynamic programming pattern, which is often used to break down a complex problem

1. We start with an initialization where we assign the costs of painting the first house with the k different colors directly to our first

1 for i in range(1, n):

g = costs[i][:]

into smaller, easier-to-manage subproblems.

version of the f array. This sets up our base case for the dynamic programming solution. 1 f = costs[0][:]

- 2. We then iterate over each of the remaining houses (1) from the second house (1) to the last house (n 1). For each house, we need to calculate the new costs of painting it with each possible color (j).
- 3. For each color (j), we determine the minimum cost of painting the previous house with any color other than j. This is done to ensure that the same color is not used for adjacent houses.

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the lowest cost to paint the previous house with a different color.
 1 for j in range(k):
       t = min(f[h] for h in range(k) if h != j)
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To find that minimum, we iterate through all the possible colors (h), ignoring the current color j. This inner loop effectively finds

4. The found minimum cost t is then added to the current cost of painting the house i with color j (costs[i][j]). The result is the total cost to get to house i, having it painted with color j, and is stored in g[j]. 1 g[j] += t

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5. Once all colors for the current house have been evaluated, we update the f array to be our newly calculated g.
  1 f = g
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last, with the index representing the color used for the last house.

7. The final step is to find the minimum value within the f array since this represents the lowest possible cost for painting all the houses while following the rules. This is the value that is returned as the answer. 1 return min(f)

The pattern used here leverages dynamic programming's key principle: solve the problem for a small section (the first house, in this

6. After we have finished iterating through all the houses, the f array holds the minimum cost to paint all the houses up until the

case) and then build upon that solution incrementally, tackling a new subproblem in each iteration (each subsequent house). While the problem itself has potentially a very large number of combinations, dynamic programming allows us to consider only the relevant ones and efficiently find the solution.

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Example Walkthrough
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 Imagine we have n = 3 houses and k = 3 colors. The costs matrix provided to us is: [[1,5,3], [2,9,4], [3,1,5]]. This means: To paint house 0, it costs 1 for color 0, 5 for color 1, and 3 for color 2.

Applying the approach:

g[1] += 1, resulting in g[1] = 10.

house.

g[0] = 8.

g[2] = 10.

Python Solution

class Solution:

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1. We initialize f with the costs to paint the first house, so f will be [1, 5, 3].

Let's consider a small example to illustrate the solution approach using the dynamic programming pattern described.

= costs[1][:] or g = [2, 9, 4].3. Next, we find the minimum cost to paint the previous house with a color different from the color we want to use for the current

To paint house 1, it costs 2 for color 0, 9 for color 1, and 4 for color 2.

To paint house 2, it costs 3 for color 0, 1 for color 1, and 5 for color 2.

g[0] += 3, resulting in g[0] = 5. For g[1] (house 1, color 1), we look for the minimum cost of painting house 0 with colors 0 or 2. The minimum of [1, 3] is 1, so

For g[0] (house 1, color 0), we look for the minimum cost of painting house 0 with colors 1 or 2. The minimum of [5, 3] is 3, so

2. We move on to the second house and create a new temporary array g, which initially contains the costs for the second house: g

g[2] += 1, resulting in g[2] = 5. 4. Now g is updated to [5, 10, 5] and we update f with g. So now f = g.

For g[2] (house 1, color 2), we look for the minimum cost of painting house 0 with colors 0 or 1. The minimum of [1, 5] is 1, so

5. We repeat the process for the third house. We start with g = costs[2][:] or g = [3, 1, 5].

For g[0], we look for the minimum cost of f[1] or f[2], which is the minimum of [10, 5] and that is 5, so g[0] += 5 resulting in

For g[1], we look for the minimum cost of f[0] or f[2], which is the minimum of [5, 5] and that is 5, so g[1] += 5 resulting in

g[1] = 6.For g[2], we look for the minimum cost of f[0] or f[1], which is the minimum of [5, 10] and that is 5, so g[2] += 5 resulting in

all the houses while ensuring no two adjacent houses have the same color is 6.

Get the number of houses (n) and the number of colors (k)

Iterate through each color for the current house

Add the minimum cost found to the current color cost

curr_row_costs[color_index] += min_cost_except_current

Update the previous row costs for the next iteration

6. Updated g for the last house is [8, 6, 10], this becomes new f, so f = [8, 6, 10]. 7. Finally, we find the minimum cost to paint all houses by taking the minimum of f, which is 6. Therefore, the minimum cost to paint

def minCostII(self, costs: List[List[int]]) -> int:

num_houses, num_colors = len(costs), len(costs[0])

curr_row_costs = costs[house_index][:]

for color_index in range(num_colors):

min_cost_except_current = min(

prev_row_costs = curr_row_costs

Initialize the previous row with the costs of the first house prev_row_costs = costs[0][:] # Iterate through the rest of the houses for house_index in range(1, num_houses): # Initialize costs for the current row

Find the minimum cost for the previous house, excluding the current color index

prev_row_costs[color] for color in range(num_colors) if color != color_index

26 27 # Return the minimum cost for painting all houses with the last row of costs return min(prev_row_costs) 28 29

Java Solution

class Solution {

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public int minCostII(int[][] costs) {
            int numHouses = costs.length; // Number of houses is the length of the costs array
            int numColors = costs[0].length; // Number of colors available for painting is the length of the first item in costs array
            int[] previousCosts = costs[0].clone(); // Clone the first house's cost as the starting point
           // Iterate over each house starting from the second house
           for (int houseIndex = 1; houseIndex < numHouses; ++houseIndex) {</pre>
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                int[] currentCosts = costs[houseIndex].clone(); // Clone the current house's costs
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               // Iterate through each color for the current house
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                for (int colorIndex = 0; colorIndex < numColors; ++colorIndex) {</pre>
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                    int minCost = Integer.MAX_VALUE;
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                    // Find the minimum cost of painting the previous house with a different color
                    for (int prevColorIndex = 0; prevColorIndex < numColors; ++prevColorIndex) {</pre>
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                        // Skip if it is the same color as the current one
                        if (prevColorIndex != colorIndex) {
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                            minCost = Math.min(minCost, previousCosts[prevColorIndex]);
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                    // Add the minimum found cost to paint the previous house to the current house's color cost
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                    currentCosts[colorIndex] += minCost;
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               // Update previousCosts to currentCosts for the next iteration
                previousCosts = currentCosts;
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           // Find and return the minimum cost from the last house's painting cost array
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           return Arrays.stream(previousCosts).min().getAsInt();
29
30 }
31
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C++ Solution

1 #include <vector>

6 class Solution {

public:

2 #include <algorithm>

#include <climits>

using namespace std;

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int minCostII(vector<vector<int>>& costs) {
           int numHouses = costs.size(); // Number of houses
           int numColors = costs[0].size(); // Number of colors
           // Initialize the first row of the DP table with costs of painting the first house
           vector<int> dpTable = costs[0];
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           // Loop over each house starting from the second
           for (int houseIndex = 1; houseIndex < numHouses; ++houseIndex) {</pre>
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               // Temporary vector to hold the new costs for the current house
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               vector<int> newCosts = costs[houseIndex];
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               // Loop over each color for the current house
               for (int currentColor = 0; currentColor < numColors; ++currentColor) {</pre>
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                    int minCost = INT_MAX; // Initialize minCost to the largest possible value
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                   // Find the minimum cost to paint the previous house with a color different from currentColor
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                    for (int previousColor = 0; previousColor < numColors; ++previousColor) {</pre>
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                        if (previousColor != currentColor) {
                            minCost = min(minCost, dpTable[previousColor]);
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                   // Add the minimum cost found to paint the previous house with the cost to paint the current house
                   newCosts[currentColor] += minCost;
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               // Move the values in newCosts to dpTable for the next iteration
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               dpTable = move(newCosts);
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           // Return the minimum element in dpTable (which now contains the minimum cost to paint all houses)
           return *min_element(dpTable.begin(), dpTable.end());
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42 };
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Typescript Solution
   function minCostII(costs: number[][]): number {
       const numHouses: number = costs.length; // Number of houses
       const numColors: number = costs[0].length; // Number of colors
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// Initialize the first row of the DP table with costs of painting the first house

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let dpTable: number[] = [...costs[0]];

// Loop over each house starting from the second

for (let houseIndex = 1; houseIndex < numHouses; houseIndex++) {</pre>

const newCosts: number[] = [...costs[houseIndex]];

// Temporary array to hold the new costs for the current house

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// Loop over each color for the current house
           for (let currentColor = 0; currentColor < numColors; currentColor++) {</pre>
               let minCost: number = Number.MAX_SAFE_INTEGER; // Initialize minCost to the largest possible safe integer value
               // Find the minimum cost to paint the previous house with a color different from currentColor
               for (let previousColor = 0; previousColor < numColors; previousColor++) {</pre>
18
                   if (previousColor !== currentColor) 
                       minCost = Math.min(minCost, dpTable[previousColor]);
20
21
22
23
               // Add the minimum cost found to paint the previous house with the cost to paint the current house
24
25
               newCosts[currentColor] += minCost;
26
27
28
           // Move the values in newCosts to dpTable for the next iteration
           dpTable = newCosts;
29
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31
       // Return the minimum element in dpTable (which now contains the minimum cost to paint all houses)
32
33
       return Math.min(...dpTable);
34 }
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Time and Space Complexity
Time Complexity:
The given code iterates over n rows, and for each row, it iterates over k colors to calculate the minimum cost. Inside the inner loop,
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there is another loop that again iterates over k colors to find the minimum cost of painting the previous house with a different color, avoiding the current one. Therefore, for each of the n rows, the code performs O(k) operations for each color, and within that, it performs another O(k) to find the minimum. This results in a time complexity of O(n * k * k).

Space Complexity: The space complexity of the code is determined by the additional space used for the f and g arrays, both of size k. No other significant space is being used that scales with the input size. Thus the space complexity is O(k).