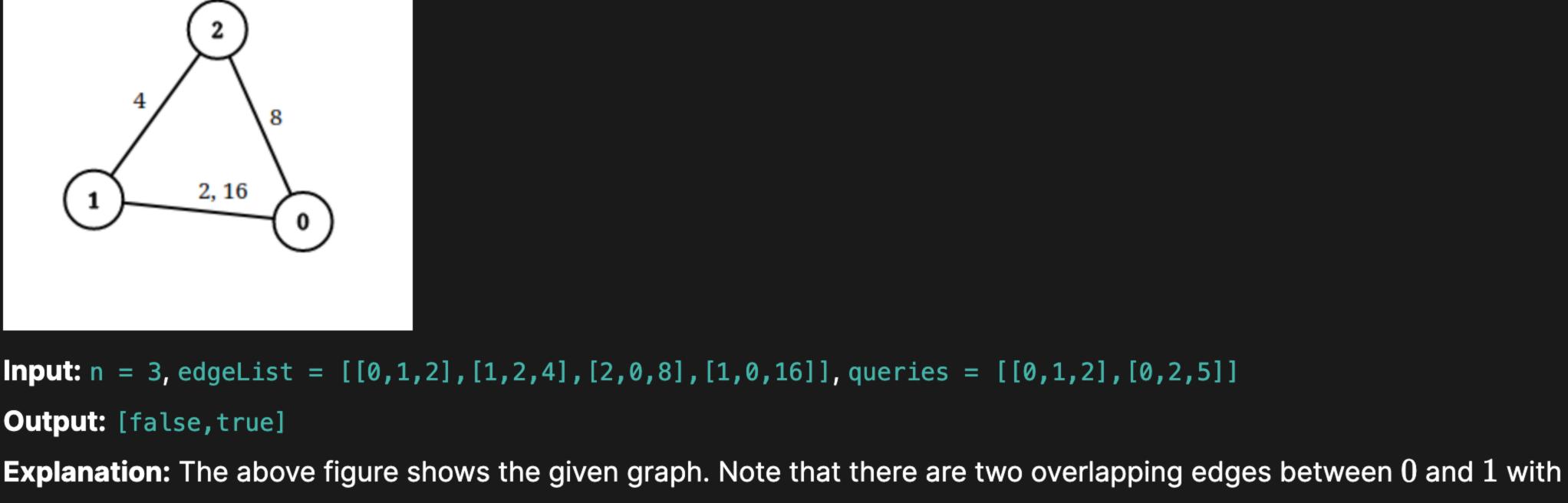
1697. Checking Existence of Edge Length Limited Paths

An undirected graph of n nodes is defined by edgeList, where edgeList[i] = $[u_i, v_i, dis_i]$ denotes an edge between nodes u_i and v_i with distance dis_i . Note that there may be **multiple** edges between two nodes.

Given an array queries, where queries $[j] = [p_j, q_j, limit_j]$, your task is to determine for each queries [j] whether there is a path between pj and qj such that each edge on the path has a distance strictly less than $\lim_{i \to j} a_i$.

Return a boolean array answer, where answer, length == queries, length and the j^{th} value of answer is true if there is a path for queries[j], and false otherwise.

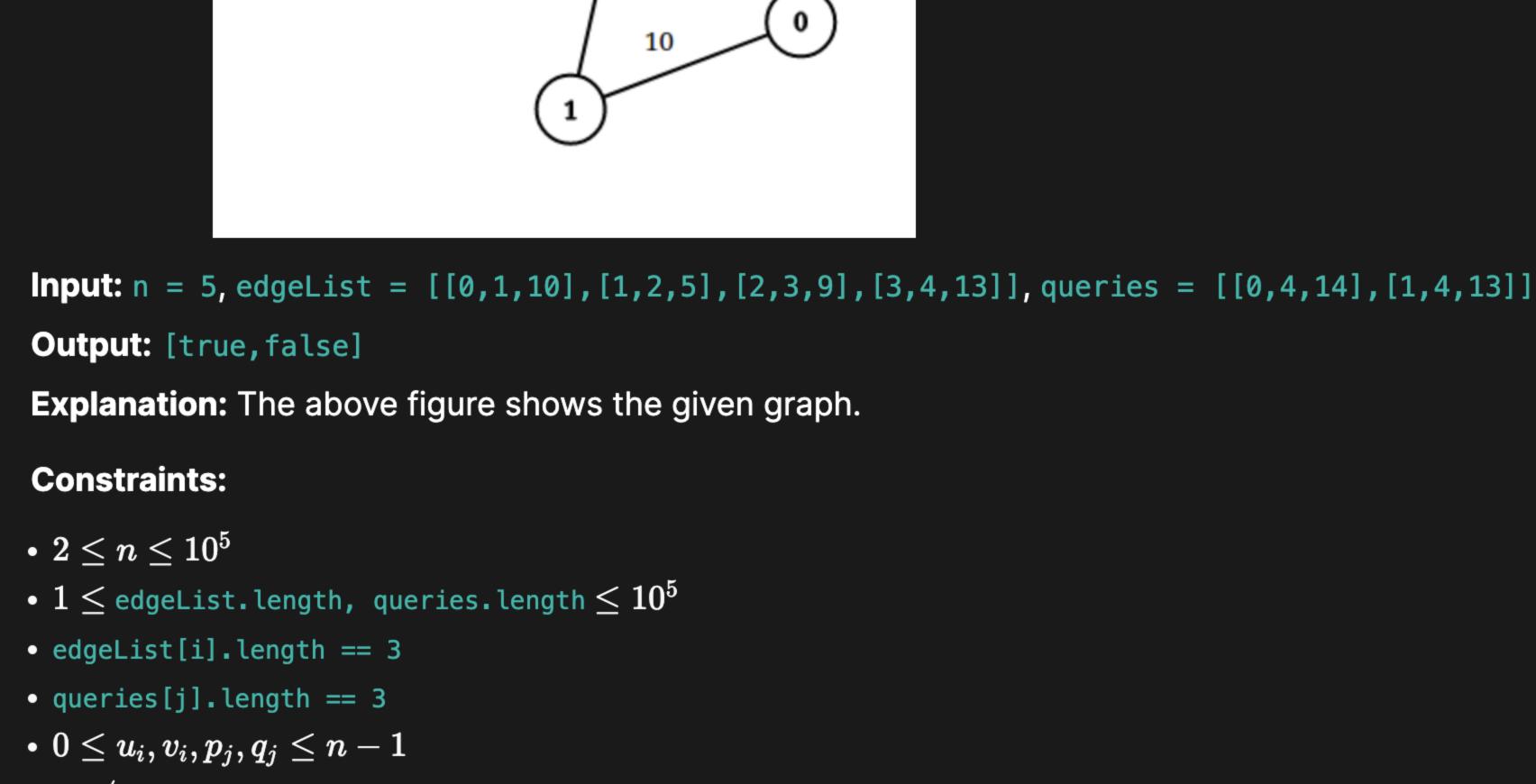
Example 1:



distances 2 and 16. For the first query, between 0 and 1 there is no path where each distance is less than 2, thus we return false for this query.

For the second query, there is a path $(0 \to 1 \to 2)$ of two edges with distances less than 5, thus we return true for this query.

Example 2:



• $u_i \neq v_i$

• $p_j \neq q_j$

- $1 \leq \operatorname{dis}_i, \operatorname{limit}_i \leq 10^9$ • There may be multiple edges between two nodes. Solution
- **Brute Force**
- connected. An alternative is to build the graph and run a BFS on it to check for connectivity from p_j to q_j . Let M denote the size of edgeList and let Q denote the size of queries.

With the DSU solution, we'll answer each query in $\mathcal{O}(M\log N)$. This leads to a total time complexity of $\mathcal{O}(QM\log N)$.

Full Solution

queries.

for the remaining queries.

Some details for implementation

Time Complexity: $\mathcal{O}((Q+M)\log N)$.

Example

build the DSU once. Why is this the case? First, we'll take a step back to our brute force solution. Let's look at what edges each <u>DSU</u> contains for each $limit_i$. Our queries are sorted by the value of $limit_i$ so $limit_{i+1}$ will always be greater or equal to $limit_i$. Since $\mathrm{limit}_{i+1} \geq \mathrm{limit}_i$, we can observe that all edges in the <u>DSU</u> for query j will always be part of the <u>DSU</u> for query j+1. We

For example, let's say we had queries with the following limits: [1,3,5,7,9]

 $\mathcal{O}(Q\log N)$. Thus, our final time complexity will be $\mathcal{O}((Q+M)\log N)$.

void Union(int x, int y) { // merges two disjoint sets into one set

static bool comp(vector<int>& a, vector<int>& b) { // sorting comparator

When we see problems about whether or not two nodes are connected, we should think about DSU as it answers queries related

to connectivity very quickly. For each query queries[j], we'll initialize a DSU and merge nodes connected by edges with a

distance **strictly less than** $limit_i$. We can then check if p_i and q_i have the same id/leader in the DSU to determine if they are

The <u>BFS</u> solution answers queries in $\mathcal{O}(N+M)$ in the worst case which leads to a total time complexity of $\mathcal{O}(Q(N+M))$.

We will focus on the brute force DSU solution and extend it to obtain the full solution. The reason why this solution is inefficient is

We can accomplish this by answering the queries by **non-decreasing** $\lim_i t_i$. If we answer queries in this order, we'll only need to

because we rebuild the <u>DSU</u> for every query. Let's find a way to answer all the queries without rebuilding the <u>DSU</u> each time.

can also observe that this means once an edge is added into the <u>DSU</u> for some query, it will stay in the <u>DSU</u> for the remaining

If edgeList had an edge with distance 4, it will be added in the DSU for queries with limits of 5, 7, and 9 as $4 \le 5, 7, 9$. We can

see that once we reach the query with the limit of 5, we will include the edge with distance 4 into our <u>DSU</u> and it will stay there

For each query, we should include another variable which is the index of that query. This is important as we have to return the answers to the queries in the order they were asked. Since we are adding edges in order from least distance to greatest distance, it would be convenient to sort the edges by the distance value and have some pointer to indicate which edges have been added so far.

Each edge is added at most once so this contributes $\mathcal{O}(M\log N)$ to our time complexity. Answering all Q queries will contribute

Bonus: We can use union by rank mentioned <u>here</u> to improve the time complexity of <code>DSU</code> operations from $\mathcal{O}(\log N)$ to $\mathcal{O}(lpha(N))$

Our <code>DSU</code> takes $\mathcal{O}(N)$ space and storing the answers to all Q queries takes $\mathcal{O}(Q)$ space so our final space complexity is $\mathcal{O}(N+1)$ Q).

C++ Solution

class Solution {

public:

Space Complexity

Space Complexity: $\mathcal{O}(N+Q)$

return parent[x];

x = find(x);

y = find(y);

parent[x] = y;

return a[2] < b[2];

parent[x] = find(parent[x]);

for (int j = 0; j < queries.length;</pre>

int[] query = queries[j];

while (i < edgeList.length &&</pre>

int u = edgeList[i][0];

int v = edgeList[i][1];

ans[queryIndex] = true;

Union(u, v, parent);

int queryIndex = query[3];

int limit = query[2];

i++;

return ans;

Python Solution

class Solution:

int p = query[0];

int q = query[1];

def distanceLimitedPathsExist(

boolean[] ans = new boolean[queries.length];

for (int j = 0; j < queries.length; j++) {</pre>

int i = 0;

j++) { // keeps track of original index for each query

self, n: int, edgeList: List[List[int]], queries: List[List[int]]

queries[j] = new int[]{queries[j][0], queries[j][1], queries[j][2], j};

Arrays.sort(queries, (a, b)->a[2] - b[2]); // sort queries by value for limit

edgeList[i][2] < limit) { // keeps adding edges with distance < limit</pre>

if (find(p, parent) == find(q, parent)) { // checks if p and q are connected

Time Complexity

vector<int> parent; int find(int x) { // finds the id/leader of a node if $(parent[x] == x) {$ return x;

vector<vector<int>>& queries) {

vector<bool> distanceLimitedPathsExist(int n, vector<vector<int>>& edgeList, parent.resize(n); for (int i = 0; i < n; i++) { parent[i] = i;

```
sort(edgeList.begin(), edgeList.end(), comp); // sort edges by value for distance
        for (int j = 0; j < queries.size();</pre>
             j++) { // keeps track of original index for each query
            queries[j].push_back(j);
        sort(queries.begin(), queries.end(), comp); // sort queries by value for limit
        int i = 0;
        vector<bool> ans(queries.size());
        for (vector<int> query : queries) {
            int limit = query[2];
            while (i < edgeList.size() &&</pre>
                   edgeList[i][2] < limit) { // keeps adding edges with distance < limit</pre>
                int u = edgeList[i][0];
                int v = edgeList[i][1];
                Union(u, v);
                i++;
            int p = query[0];
            int q = query[1];
            int queryIndex = query[3];
            if (find(p) == find(q)) { // checks if p and q are connected
                ans[queryIndex] = true;
        return ans;
};
Java Solution
class Solution {
   private
   int find(int x, int[] parent) { // finds the id/leader of a node
        if (parent[x] == x) {
            return x;
        parent[x] = find(parent[x], parent);
        return parent[x];
   private
   void Union(int x, int y, int[] parent) { // merges two disjoint sets into one set
        x = find(x, parent);
        y = find(y, parent);
        parent[x] = y;
   public
   boolean[] distanceLimitedPathsExist(int n, int[][] edgeList, int[][] queries) {
        int[] parent = new int[n];
        for (int i = 0; i < n; i++) {
            parent[i] = i;
        Arrays.sort(edgeList, (a, b)->a[2] - b[2]); // sort edges by value for distance
```

Java

C++

TypeScript

```
-> List[bool]:
        parent = [i for i in range(n)]
        def find(x): # finds the id/leader of a node
            if parent[x] == x:
                return x
            parent[x] = find(parent[x])
            return parent[x]
        def Union(x, y): # merges two disjoint sets into one set
            x = find(x)
            y = find(y)
            parent[x] = y
        edgeList.sort(key=lambda x: x[2]) # sort edges by value for distance
        for i in range(len(queries)): # keeps track of original index for each query
            queries[i].append(i)
        queries.sort(key=lambda x: x[2]) # sort queries by value for limit
        i = 0
        ans = [False for j in range(len(queries))]
        for query in queries:
            limit = query[2]
            while (
                i < len(edgeList) and edgeList[i][2] < limit</pre>
            ): # keeps adding edges with distance < limit</pre>
                u = edgeList[i][0]
                v = edgeList[i][1]
                Union(u, v)
                i += 1
            p = query[0]
            q = query[1]
            queryIndex = query[3]
            if find(p) == find(q): # checks if p and q are connected
                ans[queryIndex] = True
        return ans
Solution Implementation
 Python
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