





Problem Description

The provided problem involves finding the largest string x that can divide two input strings str1 and str2. One string divides another if it can be repeated some number of times to obtain the other string. For example, if we have str1 = "abcabc" and str2 = "abc", then str2 divides str1 because we can concatenate str2 with itself twice to get str1. In other words, str1 is the result of appending str2 to itself multiple times. The challenge is to identify the largest common string that can divide both str1 and str2 in a similar

fashion. To illustrate further, if str1 is "ababab" and str2 is "abab", the string "ab" is the answer since it is the largest string that divides both

str1 and str2.

Intuition

(GCD), but rather than numbers, we're dealing with strings. The key insight is that if there exists such a common string x that divides both str1 and str2, then the concatenation of str1 with str2 (str1 + str2) should be the same as the concatenation of str2 with str1 (str2 + str1). If this condition doesn't hold, it implies there is no such common string and the answer is an empty string. Assuming the condition is true, we can find the length of the largest string x using the greatest common divisor of the lengths of

The underlying concept used in the provided solution is based on the mathematical idea of finding the greatest common divisor

str1 and str2. This is because the repeating pattern of string x must be a factor of both string lengths in order for it to divide both strings completely. Therefore, we find the GCD of the lengths of str1 and str2 and then return the substring of str1 up to that length. This substring is the largest common divider x.

The solution provided takes advantage of Python's built-in gcd function from the math library to calculate the greatest common

Solution Approach

divisor of the lengths of the two input strings strl and str2. This is crucial for the solution, as the gcd represents the length of the largest string that can divide both strings, if such a string exists. Here is how the solution unfolds:

1. Check for Compatibility: The first step in the provided solution checks whether the strings are compatible to have a common

- divisor by concatenating str1 with str2 and comparing it to str2 concatenated with str1. This is facilitated by the operation if str1 + str2 != str2 + str1, which ensures that the pattern of characters in both strings is compatible for them to have a common divisor string. If the check fails, the two strings cannot have a common divisor and the function immediately returns an empty string ". 2. Find Length of the Common Divisor: If the strings pass the compatibility check, the next step is to determine the length of the
- largest common divisor string. This is where we use the gcd function, by calling n = gcd(len(str1), len(str2)). The gcd function takes the lengths of str1 and str2 and returns the greatest common divisor of these two numbers. 3. Extract the Common Divisor String: With the length n obtained from the gcd function, the final step is to extract the common divisor string from str1. This is accomplished by the expression return str1[:n]. The [:n] slice operation on str1 returns the
- substring of str1 from the beginning up to the n-th character (exclusive), which is the required largest string that divides both str1 and str2. To summarize, the algorithm consists of concatenation for compatibility checking and the greatest common divisor calculation, both of which are simple, efficient operations. The lack of any complex data structures and the use of a mathematical pattern of common

division make this solution both elegant and effective. It leverages the fact that if a common divisor string exists, the repeating pattern must align with the gcd of the string lengths. Example Walkthrough

Let's use a small example to illustrate the solution approach. Suppose we have two strings str1 = "abab" and str2 = "ab". We need

Since str1 + str2 is equal to str2 + str1, the two strings are compatible, and therefore, it's possible they have a common

to find the largest string x that can divide both str1 and str2.

divisor string.

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1. Check for Compatibility: We first check if concatenating str1 with str2 is equal to str2 concatenated with str1. o str1 + str2 = "abab" + "ab" = "ababab"

2. Find Length of the Common Divisor: Next, we find the greatest common divisor of the lengths of str1 (4) and str2 (2).

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\circ gcd(4, 2) = 2
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o str2 + str1 = "ab" + "abab" = "ababab"

str1 divided by "ab" is "abab" / "ab" = "ab", which is the repetition of "ab" twice.

• str2 divided by "ab" is "ab" / "ab" = "", which is the repetition of "ab" once.

def gcdOfStrings(self, str1: str, str2: str) -> str:

Find the gcd of the lengths of the two strings.

// Calculate the GCD of lengths of the two strings

int len = gcd(str1.length(), str2.length());

// It uses the Euclidean algorithm to find the GCD

// Recursive step: GCD(a, b) = GCD(b, a mod b)

#include <algorithm> // include algorithm header for std::gcd

string gcdOfStrings(string str1, string str2) {

// if this condition is true

if (str1 + str2 != str2 + str1) {

return str1.substr(0, gcdValue);

return str1.substring(0, len);

private int gcd(int a, int b) {

if str1 + str2 != str2 + str1:

The gcd tells us that the length of the largest string that possibly divides both str1 and str2 is 2.

o str1[:2] = "ab" So, "ab" is the string we expect to divide both str1 and str2. To verify, we can see that:

3. Extract the Common Divisor String: Since the gcd is 2, we take the first 2 characters from str1 to form our largest divisor string

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The largest string that can divide both str1 and str2 is "ab", which matches our result from the solution approach. The solution is
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elegant and efficient, leveraging simple concatenation and the mathematical concept of greatest common divisor to determine the existence and length of a common divisor string.

Python Solution from math import gcd class Solution:

This is required as the strings should be made of the same substrings for them to have a common divisor.

Check if the concatenation of the two strings in different order results in the same string.

The gcd of the lengths will give us the maximum length the common divisor string can have.

return ""; // If not, return an empty string as there is no common divisor

// The substring from the beginning of strl with length 'len' is the gcd string

// Helper function to calculate the greatest common divisor (GCD) of two integers

// Base case: if b is 0, then a is the GCD (as GCD(a, 0) = a)

// Function to find the greatest common divisor of strings strl and str2

// check if concatenating the strings in both orders gives the same result

return ""; // if they are not equivalent, return an empty string

// this is required because two strings can only be multiples of each other

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# If they don't form the same string when concatenated in different orders,
# there is no common divisor string and hence return an empty string.
return ''
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length_gcd = gcd(len(str1), len(str2))
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           # Return the substring from 0 to length_gcd from the first string,
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           # which is the greatest common divisor string.
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           return str1[:length_gcd]
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Java Solution
   class Solution {
       // Function to find the greatest common divisor of lengths of two strings.
       // This GCD can be used to find the longest substring that can construct
       // the given strings by repeated concatenation.
       public String gcdOfStrings(String str1, String str2) {
           // Check if the two strings can be constructed from a common substring
           // Only if str1+str2 equals str2+str1, they have a common divisor string
           if (!(str1 + str2).equals(str2 + str1)) {
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22 return b == 0 ? a : gcd(b, a % b); 23 24 } 25

C++ Solution

class Solution {

public:

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13 // calculate the greatest common divisor (GCD) of the sizes of the two strings 14 // std::gcd is available in C++17 and later. For C++14 and earlier, use a custom gcd function 15 int gcdValue = std::gcd(str1.size(), str2.size()); 16 17

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21 };
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Typescript Solution
 1 // Function to calculate the greatest common divisor (GCD) of two numbers
 2 // Uses Euclidean algorithm
   function gcd(a: number, b: number): number {
       while (b !== 0) {
           let t = b;
           b = a % b;
           a = t;
       return a;
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   // Function to find the greatest common divisor of strings strl and str2
    function gcdOfStrings(str1: string, str2: string): string {
       // Check if concatenating the strings in both orders gives the same result
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       // This is required because two strings can only be multiples of each other
       // if this condition is true
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// return the common divisor string which is the substring from start of str1 to its GCD length

const gcdValue = gcd(str1.length, str2.length); 23 24 // Return the common divisor string which is the substring from start of strl to its GCD length return str1.substring(0, gcdValue); 25

if (str1 + str2 !== str2 + str1) {

Time and Space Complexity The code contains the gcd0fStrings method that finds the greatest common divisor (GCD) of lengths of two strings str1 and str2 to determine the largest string that can be repeatedly used to construct str1 and str2.

return ""; // If they are not equivalent, return an empty string

// Calculate the greatest common divisor (GCD) of the lengths of the two strings

str1) and the greatest common divisor computation (gcd(len(str1), len(str2))).

Time Complexity:

1. String Concatenation: If str1 is of length n and str2 of length m, the concatenation will take 0(n + m) time as each character from both strings need to be combined once.

The time complexity of this function mainly depends on two operations: the string concatenation operation (str1 + str2 and str2 +

3. Greatest Common Divisor: The gcd function typically employs Euclid's algorithm, which has a time complexity of O(log(min(n, m))) where n and m are the lengths of the strings.

2. Checking String Equality: Comparing the concatenated strings takes 0(n + m) time. If the strings differ, the method returns early.

Therefore, the overall time complexity combines these operations resulting in $O(n + m + \log(\min(n, m)))$. However, the dominating factor for large values of n and m will tend to be the concatenation and comparison, so we can approximate the time complexity as 0(n + m).

complexity is O(n + m).

Space Complexity:

The space complexity of the gcd0fStrings function can be analyzed as follows:

1. Temporary Strings: The creation of concatenated strings str1 + str2 and str2 + str1 requires additional space of 0(n + m). 2. GCD Computation: The gcd function itself may use constant space, 0(1), if the Euclidean algorithm is implemented in an iterative

manner. As such, no additional space that grows with the input size is required except for the string concatenation. Hence, the space