1898. Maximum Number of Removable Characters

Problem Description

Medium Array

String

can approach this problem using binary search.

Binary Search

distinct indices from s. The goal is to find out the maximum number of characters you can remove from s (using the indices provided in removable from lowest to highest) so that p remains a subsequence of s. The steps for removing characters are as follows: mark characters in s at indices indicated by the first k elements of removable, remove them, and then check if p remains a subsequence of the modified s. A subsequence is a sequence that can be derived from another sequence by deleting some elements without changing the order of the remaining elements.

You are provided with two strings s and p, where p must be a subsequence of s. There is also an array called removable with

Intuition

The key to solving this problem lies in understanding that once you remove characters from s, you must check whether each

subsequent removal maintains p as a subsequence. Since removable contains distinct indices, and we want to maximize k, we

The intuition behind using binary search here is that if removing k characters still leaves p as a subsequence, removing fewer than k characters will also leave p as a subsequence. Conversely, if p is not a subsequence after removing k characters, removing more than k characters will certainly not leave p as a subsequence. Therefore, there is a threshold value for k which we want to find - the maximum k for which p remains a subsequence. Binary search allows us to efficiently home in on this

threshold by halving the search space with each iteration and identifying the exact point where p stops being a subsequence. In the provided solution, the function check(k) takes a number k and simulates the process of marking and removing k characters from s to verify if p remains a subsequence. The binary search then adjusts the search interval (left, right) based on the outcomes of check(k). If p is still a subsequence after removing k characters, it means we could possibly remove more, so the search space is adjusted to [mid, right]. If not, we have removed too many characters, and the search space is adjusted to [left, mid-1]. The search continues until the maximum k is found.

Solution Approach The implementation makes use of a binary search pattern, specifically what's often referred to as "Binary Search Template 2". This is due to the way the mid point is calculated and how the search space is adjusted. The pattern is conducive when we want to search for the element or condition which requires accessing the current index and its immediate right neighbour in the array.

indices in removable from s leaves p as a subsequence. We perform a binary search over the length of the array removable because the problem has a "yes" or "no" nature (is p still a subsequence after the removal?) and because the removal

condition is monotonic—that is, if removing k characters works, then removing any less than k will also work. check Function: This function simulates the removal of characters from s and checks if p is still a subsequence. It uses two pointers, i for the string s and j for the string p. As it iterates over s, it skips over the characters at the indices specified in

Binary Search Algorithm: We want to find the maximum value of k such that removing k characters specified by the first k

Set Data Structure: A set called ids is used to store the indices from removable that we're proposing to remove. This allows

constant-time checks to determine if a character at a particular index in s should be skipped during the subsequence check.

Calculating mid: The variable mid is calculated as (left + right + 1) // 2 to ensure that the search space moves towards

the first k entries of removable. If a non-removable character in s matches the current character in p, it moves the pointer j forward. If the end of p is reached (j == n), then p is still a subsequence of s after the removals.

being a subsequence, thus giving us the maximum k.

Let's consider a small example to illustrate the solution approach.

• Calculate mid = (left + right + 1) // 2 = (0 + 2 + 1) // 2 = 1.

After removal, s = "_b_acb". p = "ab" is still a subsequence of this new string s.

Since check(1) is true, we adjust the search range to [mid, right] which means [1, 2].

Since check(2) is false, we adjust the search range to [left, mid - 1] which means [1, 1].

Convert the list of removable indices up to k into a set for faster look-ups

We can form the pattern if we have gone through all characters of the pattern

if string index not in removal set and string[string_index] == pattern[pattern_index]:

while pattern index < pattern length and string index < string length:</pre>

Check if current index is not removed, and characters match

Move to the next character in the pattern

Move to the next character in the string

mid = (left + right + 1) // 2 # Pick the middle value

such that it is still possible to find the pattern `p` as a subsequence.

// Method to find the maximum number of characters that can be removed from

int maximumRemovals(std::string s, std::string p, std::vector<int>& removable) {

// Binary search to find the maximum number of characters that can be removed

// Check if the subsequence 'p' is still in 's' after removing 'mid' characters

right = mid - 1; // If not, decrease the upper bound of the search range

left = mid; // If it is, increase the lower bound of the search range

// Helper function to check if 'p' is a subsequence of 's' after removing 'mid' characters

bool checkSubsequence(std::string& s, std::string& p, std::vector<int>& removable, int mid) {

int left = 0, right = removable.size();

int mid = (left + right + 1) / 2;

std::unordered set<int> removedIndices;

removedIndices.insert(removable[k]);

for (int k = 0; k < mid; ++k) {

// Choose the midpoint of the current range

if (checkSubsequence(s, p, removable, mid)) {

return left; // The maximum number of characters we can remove

int i = 0, j = 0; // Pointers for string 's' and the subsequence 'p'

// Using a set to keep track of the indices that have been removed

while (left < right) {</pre>

} else {

int sLength = s.size();

int pLength = p.size();

Check if the pattern can be formed after removing mid characters

left = mid # If it is possible, try removing more characters

The above code checks the maximum number of indices that can be removed from the string `s`

Here's the breakdown of the solution approach:

Adjusting Search Space: Based on the results of check(mid), the binary search narrows the search space. If removing mid characters works, it means we should look for a possibly higher k, so the new search interval is [mid, right]. If not, we search the space [left, mid - 1]. The search ends when left and right meet, which will be the point just before p stops

the higher numbers when the check(mid) is successful, ultimately helping to identify the upper bound of k.

subsequence in s, despite the removals. **Example Walkthrough**

The combination of these components results in a solution that efficiently pinpoints the largest k for which p remains a

Suppose: s = "abcacb" • p = "ab" • removable = [3, 1, 0]

Initial Setup: We set up our binary search with bounds left = 0 and right = len(removable) - 1 = 2. The goal is to find the maximum k such that p is still a subsequence of the modified s after the removal.

• Use check(1) to simulate the removal of characters at indices removable[0] and removable[1], which are 0 and 1.

• Use check(2) to simulate the removal of characters at indices removable[0], removable[1], and removable[2], which are 0, 1, and 3. After removal, s = "_b__cb". p = "ab" is no longer a subsequence of s.

Applying Binary Search

First Iteration:

Second Iteration:

 \circ Calculate mid = (1 + 2 + 1) // 2 = 2.

(removing the characters at indices [0, 1] from s).

removal set = set(removable[:k])

Iterate through string and pattern

pattern index += 1

return pattern_index == pattern_length

if can form pattern after removals(mid):

It uses binary search to efficiently find this maximum number.

// string s so that string p is still a subsequence of s

string index += 1

Since left and right are the same, we conclude the binary search. We determined that the maximum k for which p = "ab"remains a subsequence of s after removal is 1.

Therefore, the maximum number of characters that can be removed from s while ensuring p remains a subsequence is 1

```
Solution Implementation
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Python

from typing import List class Solution: def maximum removals(self, string: str, pattern: str, removable: List[int]) -> int: def can form pattern after removals(k: int) -> bool: # Initialize pointers for pattern and string pattern index = 0 string index = 0

Get string and pattern lengths string length, pattern length = len(string), len(pattern) # Set the search space for the binary search left, right = 0, len(removable) # Perform binary search to find the maximum number of removable characters

else: right = mid - 1 # Otherwise, try with fewer removable characters return left # The maximum number of removable characters is left # Explanation:

Java

class Solution {

class Solution {

public:

while left < right:</pre>

```
public int maximumRemovals(String s, String p, int[] removable) {
        int left = 0, right = removable.length; // Define binary search boundaries
        // Perform binary search to find the maximum index 'mid'
        while (left < right) {</pre>
            int mid = (left + right + 1) / 2; // Choose a middle point (avoid overflow)
            // Check if string p is still a subsequence of s after removing mid characters
            if (checkSubsequence(s, p, removable, mid)) {
                left = mid; // Move left pointer to mid if p is still a subsequence
            } else {
                right = mid - 1; // Move right pointer if p is not a subsequence
        return left; // Returns maximum removables that still keep p as a subsequence of s
    // Helper method to check if p is a subsequence of s after removing certain characters
    private boolean checkSubsequence(String s, String p, int[] removable, int mid) {
        int sLen = s.length(); // Length of string s
        int pLen = p.length(); // Length of string p
        int i = 0; // Index for iterating over s
        int j = 0; // Index for iterating over p
        // Create a hash set to store the indices of characters to be removed
        Set<Integer> removalSet = new HashSet<>();
        for (int k = 0; k < mid; k++) {
            removalSet.add(removable[k]); // Add removable characters' indices up to mid
        // Iterate over string s and p to check if p is a subsequence
       while (i < sLen && j < pLen) {</pre>
            // If current index is not in the removal set and characters match, move j
            if (!removalSet.contains(i) && s.charAt(i) == p.charAt(j)) {
                j++;
            i++; // Always move i to the next character
        // If we've found the whole string p, return true; otherwise, return false
        return j == pLen;
C++
#include <vector>
#include <string>
#include <unordered_set>
```

```
// Iterate over both strings and check if 'p' is a subsequence of 's'
        while (i < sLength && j < pLength) {</pre>
            // If the current character is not removed and matches with `p[j]`,
            // move the pointer `j` of subsequence `p`
            if (removedIndices.count(i) == 0 && s[i] == p[j]) {
                ++j;
            ++i; // Always move the pointer `i` of string `s`
        // If we have iterated through the entire subsequence `p`, it's a subsequence of `s`
        return j == pLength;
};
TypeScript
// Function to determine the maximum number of characters that can be removed
// from string 's' such that string 'p' is still a subsequence of 's'.
function maximumRemovals(s: string, p: string, removable: number[]): number {
    let leftIndex = 0:
    let rightIndex = removable.length;
    while (leftIndex < rightIndex) {</pre>
        // Midpoint calculation to use as the possible number of characters to be removed
        let midPoint = Math.floor((leftIndex + rightIndex + 1) / 2);
        // Check if 'p' is still a subsequence after removing 'midPoint' characters
        if (isSubsequence(s, p, new Set(removable.slice(0, midPoint)))) {
            leftIndex = midPoint;
        } else {
            rightIndex = midPoint - 1;
    // The maximum number of characters that can be removed
    return leftIndex;
// Function to check if 'sub' is a subsequence of 'str' when indices in 'removedIndices' are removed.
function isSubsequence(str: string, sub: string, removedIndices: Set<number>): boolean {
    let strLength = str.length:
    let subLength = sub.length;
    let indexStr = 0;
    let indexSub = 0;
    // Iterate over each character of 'str' and 'sub' to check for subsequence
    while (indexStr < strLength && indexSub < subLength) {</pre>
        // If the current index is not removed, and characters match, increment 'sub' index
        if (!removedIndices.has(indexStr) && str.charAt(indexStr) === sub.charAt(indexSub)) {
            indexSub++;
        indexStr++;
    // Check if the end of 'sub' was reached, indicating it is a subsequence
    return indexSub === subLength;
from typing import List
class Solution:
    def maximum removals(self, string: str, pattern: str, removable: List[int]) -> int:
        def can form pattern after removals(k: int) -> bool:
            # Initialize pointers for pattern and string
            pattern index = 0
            string index = 0
            # Convert the list of removable indices up to k into a set for faster look-ups
            removal set = set(removable[:k])
            # Iterate through string and pattern
```

Time Complexity:

Time and Space Complexity

The time complexity of the function mainly comes from two parts: the binary search and repeatedly checking whether p is a subsequence of s after certain characters have been removed. The binary search is done over the length of removable, which has a complexity of O(log k) where k is the length of removable.

For each iteration of binary search, the check function is called, which iterates over the characters of s and p. The check function can take 0(m + k) time in the worst case, where m is the length of s and k is the length of the prefix of removable considered in the check function. Although k changes with each binary search iteration, we need to consider the

Combining these two parts, the overall time complexity is O((m + k) * log k). **Space Complexity:**

worst-case scenario where the function checks the entire prefix, hence k.

while pattern index < pattern length and string index < string length:</pre>

Check if current index is not removed, and characters match

Perform binary search to find the maximum number of removable characters

Check if the pattern can be formed after removing mid characters

left = mid # If it is possible, try removing more characters

The above code checks the maximum number of indices that can be removed from the string `s`

right = mid - 1 # Otherwise, try with fewer removable characters

We can form the pattern if we have gone through all characters of the pattern

Move to the next character in the pattern

Move to the next character in the string

string length, pattern length = len(string), len(pattern)

mid = (left + right + 1) // 2 # Pick the middle value

return left # The maximum number of removable characters is left

such that it is still possible to find the pattern `p` as a subsequence.

pattern index += 1

return pattern_index == pattern_length

Set the search space for the binary search

if can form pattern after removals(mid):

It uses binary search to efficiently find this maximum number.

string index += 1

Get string and pattern lengths

left, right = 0, len(removable)

while left < right:</pre>

else:

Explanation:

if string index not in removal set and string[string_index] == pattern[pattern_index]:

The space complexity is primarily due to the set ids used in the check function, which stores the indices that are removable up to k. This set can grow up to size k. Thus, the space complexity is O(k).