694. Number of Distinct Islands **Depth-First Search Breadth-First Search Union Find** Medium

## **Problem Description**

be "1" (representing land) or "0" (representing water). An island is defined as a group of "1"s connected horizontally or vertically. We are also told that all the edges of the grid are surrounded by water, which simplifies the problem by ensuring we don't need to handle edge scenarios where islands might be connected beyond the grid.

To consider two islands as the same, they have to be identical in shape and size, and they must be able to be translated (moved

In this problem, we are tasked to find the number of distinct islands on a given m x n binary grid. Each cell in the grid can either

Hash Table

**Hash Function** 

horizontally or vertically, but not rotated or flipped) to match one another. The objective is to return the number of distinct islands —those that are not the same as any other island in the grid.

Intuition

The solution leverages a Depth-First Search (DFS) approach. The core idea is to explore each island, marking the visited 'land'

## cells, and record the paths taken to traverse each island uniquely. These paths are captured as strings, which allows for easy comparison of island shapes.

Here's the step-by-step intuition behind the approach: 1. Iterate through each cell in the grid. 2. When land ("1") is found, commence a DFS from that cell to visit all connected 'land' cells of that island, effectively marking it to avoid revisiting.

numerical code.

6. Clear the path and continue the search for the next unvisited 'land' cell to find all islands.

whenever a '1' is encountered, and it continues until there are no more adjacent '1's to visit.

path signature for shapes that otherwise may seem similar if traversed differently.

counting distinct islands. Duplicates are automatically handled.

grid, allowing us to accurately count the number of distinct islands present.

- 4. Append reverse steps at the end of each DFS call to differentiate between paths when the DFS backtracks. This ensures that shapes are uniquely identified even if they take the same paths but in different order. 5. After one complete island is traversed and its path is recorded, add the path string to a set to ensure we only count unique islands.

3. While executing DFS, record the direction taken at each step to uniquely represent the path over the island. This is done using a representative

- 7. After the entire grid is scanned, count the number of unique path strings in the set, which corresponds to the number of distinct islands. This solution is efficient and elegant because the DFS ensures that each cell is visited only once, and the set data structure
- automatically handles the uniqueness of the islands.
- Solution Approach

patterns which are encapsulated in the DFS strategy outlined previously: **Depth-First Search (DFS):** 

This recursive algorithm is essential for traversing the grid and visiting every possible 'land' cell in an island once. The DFS is initiated

The implementation of the solution can be broken down into several key components, using algorithms, data structures, and

 As the DFS traverses the grid, it marks the cells that have been visited by flipping them from '1' to '0'. This prevents revisiting the same cell and ensures each 'land' cell is part of only one island.

Four possible directions for movement are captured in a list of deltas dirs. During DFS, the current direction taken is recorded by

appending a number to the path list, which is converted to a string for easy differentiation. **Backtracking with Signature:** 

**Directions and Path Encoding:** 

**Grid Modification to Mark Visited Cells:** 

Path Conversion and Uniqueness: After a complete island is explored, the path list is converted to a string that represents the full traversal path of the island. This string

• A set() is used to store unique island paths. This data structure's inherent property to store only unique items simplifies the task of

To handle backtracking uniquely, the algorithm appends a negative value of the move when DFS backtracks. This helps in creating a unique

allows the shape of the island to be expressed uniquely, similar to a sequence of moves in a game. **Set Data Structure:** 

**Counts Distinct Islands:** 

def dfs(i: int, j: int, k: int):

dirs = (-1, 0, 1, 0, -1)

dfs(x, y, h)

for h in range(1, 5):

path.append(str(-k))

• The final number of distinct islands is obtained by measuring the length of the set containing the unique path strings. Here is the code snippet detailing the DFS logic:

x, y = i + dirs[h - 1], j + dirs[h]if 0 <= x < m and 0 <= y < n and grid[x][y]:</pre>

grid[i][j] = 0

path.append(str(k))

Finally, the number of distinct islands is returned using len(paths) where paths is the set of unique path strings. By following these stages, the algorithm effectively captures the essence of each island's shape regardless of its location in the

1. Start scanning the grid from (0, 0).

```
Example Walkthrough
  Let's illustrate the solution approach with a small 4 \times 5 grid example:
  Assume our grid looks like this, where '1' is land and '0' is water:
1 1 0 0 0
1 1 0 1 1
0 0 0 1 1
0 0 0 0
```

5. Continue DFS to (1, 1) (down), mark as '0', and add '3' to path (assuming '3' represents moving down). 6. DFS can't move further, so backtrack appending '-3' to path to return to (0, 1), then append '-2' to backtrack to (0, 0).

13. Count the distinct islands from the paths set, which contains just one unique path string "233-3-2".

that only distinct islands are counted even when they are scattered throughout the grid.

7. Since all adjacent '1's are visited, the DFS for this island ends, and the path is ['2', '3', '-3', '-2'].

3. Visit (0, 0), mark as '0', and add direction code to path. Since there's no previous cell, we skip encoding here.

4. From (0, 0), move to (0, 1) (right), mark as '0', and add '2' to path (assuming '2' represents moving right).

10. Repeat the steps to traverse the second island. Assume the resulting path for the second island is "233-3-2".

12. Finish scanning the grid, with no more '1's left.

11. Conversion and insertion into paths set have no effect as it's a duplicate.

9. Continue scanning the grid and start a new DFS at (1, 3), where the next '1' is found.

```
We conclude that there is only 1 distinct island in this example grid.
This walkthrough demonstrates how the DFS exploration with unique path encoding can be used to solve this problem, ensuring
```

directions = (-1, 0, 1, 0, -1)

for h in range(4):

# Dimensions of the grid

return len(paths)

paths = set()

path = []

8. Convert path to a string "233-3-2" and insert into the paths set.

Now, let's walk through the DFS approach outlined above:

2. At (0, 0), find '1' and start DFS, initializing an empty path list.

- Solution Implementation
- class Solution: def numDistinctIslands(self, grid: List[List[int]]) -> int: # Depth-first search function to explore the island def depth first search(i: int, j: int, move: int):

grid[i][i] = 0 # Marking the visited cell as '0' to avoid revisiting

# Check if the new cell is within bounds and is part of an island

# Possible movements in the four directions: up, right, down, left

depth first search(x, v, h+1) path.append(str(-move)) # Add the reverse move to path to differentiate shapes # Set to store unique paths that represent unique island shapes

if value: # Check if the cell is part of an island

# Number of distinct islands is the number of unique path shapes

if (grid[i][j] == 1) { // if it's part of an island

return uniqueIslands.size(); // the number of unique islands

private void exploreIsland(int i, int j, char direction) {

// directions represented as delta x and delta y

path.append(direction); // append the direction to path

path = new StringBuilder(); // initialize the path

char[] dirCodes = {'U', 'R', 'D', 'L'}; // corresponding directional codes

for (int dir = 0; dir < 4; ++dir) { // iterate over possible directions</pre>

private int cols: // number of columns in the grid

rows = grid.length; // set the number of rows

cols = grid[0].length; // set the number of columns

private int[][] grid; // grid representation

public int numDistinctIslands(int[][] grid) {

this grid = grid; // reference the grid

for (int i = 0; i < cols; ++i) {

for (int i = 0; i < rows; ++i) {

grid[i][i] = 0; // mark as visited

int[]  $dX = \{-1, 0, 1, 0\};$ 

int[]  $dY = \{0, 1, 0, -1\}$ ;

int x = i + dX[dir];

int v = i + dY[dir];

path.clear() # Clear the path for next island

depth first search(i, j, 0) # Start DFS from this cell

private StringBuilder path; // used to store the path during DFS to identify unique islands

Set<String> uniqueIslands = new HashSet<>(); // store unique island paths as strings

uniqueIslands.add(path.toString()); // add the path to the set

exploreIsland(i, i, 'S'); // start DFS with dummy direction 'S' (Start)

if  $(x \ge 0)$  && x < rows &&  $y \ge 0$  && y < rols &&  $qrid[x][y] == 1) { // check for valid next cell$ 

paths.add("".join(path)) # Add the path shape to the set of paths

path.append(str(move)) # Add the move direction to path

x, y = i + directions[h], i + directions[h+1]

if 0 <= x < m and 0 <= y < n and grid[x][y]:</pre>

# Temporary list to store the current island's path shape

# Iterating over the four possible directions

# Calculate new cell's coordinates

m, n = len(grid), len(grid[0]) # Iterate over every cell in the grid for i, row in enumerate(grid): for i, value in enumerate(row):

```
Java
class Solution {
    private int rows; // number of rows in the grid
```

**}**;

**TypeScript** 

**}**;

class Solution:

function numDistinctIslands(grid: number[][]): number {

// Helper function to perform DFS.

for (let i = 1; i < 5; ++i) {

currentPath.push(directionIndex);

// Iterate through all cells of the grid.

if (grid[row][col]) {

for (let row = 0; row < rowCount; ++row) {</pre>

for (let col = 0; col < colCount; ++col) {</pre>

const rowCount = grid.length: // The number of rows in the grid.

const colCount = grid[0].length; // The number of columns in the grid.

const dfs = (row: number, col: number, directionIndex: number) => {

// Explore all four directions: up, right, down, left.

const nextRow = row + directions[i - 1];

const nextCol = col + directions[i];

const currentPath: number[] = []; // Array to keep the current DFS path.

grid[row][col] = 0; // Mark the cell as visited by setting it to 0.

// Check if the next cell is within bounds and not visited.

// If the current cell is part of an island (value is 1).

return uniquePaths.size; // Return the number of distinct islands.

path.append(str(move)) # Add the move direction to path

x, y = i + directions[h], i + directions[h+1]

if 0 <= x < m and 0 <= y < n and grid[x][y]:</pre>

if value: # Check if the cell is part of an island

# Number of distinct islands is the number of unique path shapes

path.clear() # Clear the path for next island

depth first search(i, j, 0) # Start DFS from this cell

paths.add("".join(path)) # Add the path shape to the set of paths

def numDistinctIslands(self, grid: List[List[int]]) -> int:

# Depth-first search function to explore the island

# Iterating over the four possible directions

depth first search(x, v, h+1)

# Calculate new cell's coordinates

def depth first search(i: int, j: int, move: int):

directions = (-1, 0, 1, 0, -1)

for h in range(4):

dfs(row, col, 0); // Start DFS from the current cell.

// Upon return, push the backtracking direction index to the current path.

const uniquePaths: Set<string> = new Set(); // Set to store unique island shapes.

const directions: number[] = [-1, 0, 1, 0, -1]; // Array for row and column movements.

currentPath.push(directionIndex); // Append the direction index to the current path.

dfs(nextRow, nextCol, i); // Recursively perform DFS on the next cell.

currentPath.length = 0; // Reset the currentPath for the next island.

grid[i][i] = 0 # Marking the visited cell as '0' to avoid revisiting

# Check if the new cell is within bounds and is part of an island

# Possible movements in the four directions: up, right, down, left

if (nextRow >= 0 && nextRow < rowCount && nextCol >= 0 && nextCol < colCount && grid[nextRow][nextCol]) {</pre>

uniquePaths.add(currentPath.join('.')): // Add the current path to the set of unique paths.

**Python** 

```
exploreIsland(x, y, dirCodes[dir]); // recursive DFS call
        path.append('B'); // append backtrack code to ensure paths are unique after recursion return
C++
#include <vector>
#include <string>
#include <unordered set>
#include <functional> // Include necessary headers
class Solution {
public:
    int numDistinctIslands(vector<vector<int>>& grid) {
        unordered set<string> uniqueIslandPaths; // Store unique representations of islands
        string currentPath: // Store the current traversal path
        int rowCount = grid.size(), colCount = grid[0].size(); // Dimensions of the grid
        int directions [5] = \{-1, 0, 1, 0, -1\}; // Used for moving in the grid
        // Depth-first search (DFS) to traverse islands and record paths
        function<void(int, int, int)> dfs = [&](int row, int col, int moveDirection) {
            grid[row][col] = 0; // Mark the current cell as visited
            currentPath += to_string(moveDirection); // Record move direction
            // Explore all possible directions: up, right, down, left
            for (int d = 1; d < 5; ++d) {
                int newRow = row + directions[d - 1], newCol = col + directions[d];
                if (newRow >= 0 && newRow < rowCount && newCol >= 0 && newCol < colCount && grid[newRow][newCol]) {
                    // Continue DFS if the next cell is part of the island (i.e., grid value is 1)
                    dfs(newRow, newCol, d);
            // Record move direction again to differentiate between paths with same shape but different sizes
            currentPath += to_string(moveDirection);
        };
        // Iterate over all grid cells to find all islands
        for (int i = 0; i < rowCount; ++i) {</pre>
            for (int i = 0; i < colCount; ++i) {</pre>
                // If the cell is part of an island
                if (grid[i][j]) {
                    dfs(i, i, 0); // Start DFS
                    uniqueIslandPaths.insert(currentPath); // Add the path to the set
                    currentPath.clear(); // Reset path for the next island
        // The number of unique islands is the size of the set containing unique paths
        return uniqueIslandPaths.size();
```

```
path.append(str(-move)) # Add the reverse move to path to differentiate shapes
# Set to store unique paths that represent unique island shapes
paths = set()
# Temporary list to store the current island's path shape
```

return len(paths)

Time and Space Complexity

# Dimensions of the grid

m, n = len(grid), len(grid[0])

for i, row in enumerate(grid):

# Iterate over every cell in the grid

for i, value in enumerate(row):

path = []

```
The time complexity of the provided code is 0(M * N), where M is the number of rows and N is the number of columns in the
grid. This is due to the fact that we must visit each cell at least once to determine the islands. The dfs function is called for each
land cell (1) and it ensures every connected cell is visited only once by marking visited cells as water (0) immediately, thus
avoiding revisiting.
```

The space complexity is 0(M \* N) in the worst case. This could happen if the grid is filled with land, and a deep recursive call stack is needed to explore the island. Additionally, the path variable which records the shape of each distinct island can in the worst case take up as much space as all the cells in the grid (if there was one very large island), therefore the space complexity would depend on the input size.