42. Trapping Rain Water

Two Pointers

## **Problem Description**

Hard

Imagine you have a side-view silhouette of a series of blocks with various heights. These blocks represent the elevation map in the problem. When it rains, water will fill in the gaps between these blocks. The water can be trapped between the elevations where the adjacent blocks are higher. The width of each block is 1 unit. The task is to calculate the total amount of water that these blocks can hold without spilling over, after a rainfall.

**Monotonic Stack** 

**Dynamic Programming** 

To tackle this, picture placing water on top of the blocks. Some water will be trapped between taller blocks, while some will flow off the sides if there are no sufficient barriers. The amount of trapped water at any point depends on the tallest blocks to its left and to its right because these will act as barriers. At any given point, the amount of water that can be held above it is the difference between the height of the shorter of the two barriers (either left or right) and the height of the block itself.

## The solution to this problem is based on the observation that the amount of water above a bar is determined by the highest bar

Intuition

to the left and the highest bar to the right. No matter what the arrangements of other bars are, the water above a given bar can never exceed the height difference between the bar and the shortest of the two highest bars flanking it.

To approach this problem efficiently, we use <u>dynamic programming</u>. We create two arrays, <u>left</u> and <u>right</u>, which represent the highest bars up to that point from the left and right, respectively. These arrays are populated by traversing the height array twice

— once from left to right, updating the left array with the maximum height seen so far, and once from right to left, updating the right array similarly.

Once we have these two arrays, the amount of water above each bar is simply the difference between it and the minimum of the highest bars to its left and right. The solution is then to accumulate this difference for each bar to get the total amount of trapped

water.

To put it more concretely, the left[i] array gets updated as we go, ensuring that at each step i, we have the height of the tallest bar up to that point. The right[i] array does the same but in the opposite direction. When calculating the trapped water at index

i, we look at min(left[i], right[i]) which gives us the maximum water level possible at that point. Then, we subtract the

height of the current bar height[i] to know how much water can actually be trapped there. Summing these values together for all indices gives us the total amount of trapped water.

Solution Approach

The solution uses a combination of arrays and iteration to calculate the volume of trapped rainwater.

## left[i] contains the height of the tallest pillar to the left of the position with index i, including the pillar at i itself. right[i] contains the height of the tallest pillar to the right of the position with index i, also including the pillar at i.

We initialize left[0] with the height of the first pillar height[0], since there's nothing to its left. Similarly, we initialize right[n-1]

(where n is the number of pillars) with the height of the last pillar height [n-1].

• Initialize left array with the same length as height with left[0] = height[0], which is 0.

and determine that our example silhouette can trap a total of 6 units of water.

# Fill the max\_left array with the maximum height to the left of each element.

# Fill the max\_right array with the maximum height to the right of each element.

• Initialize right array with the same length as height with right [-1] = height [-1], which is 1.

Next two senarate loops are used to popula

Firstly, we define two arrays, left and right:

- Next, two separate loops are used to populate these arrays:
- using max(left[i 1], height[i]) and store it in left[i]. This ensures that left[i] contains the height of the tallest bar to the left including the current bar.

For left[i], starting from i=1 and moving towards the end of the array, we calculate the maximum height encountered so far

For right[i], we move in the opposite direction, starting from i=n-2 down to 0. We update right[i] with max(right[i + 1],

With these arrays filled, we can then iterate through each index i and calculate the trapped water above the bar at i. The amount

of trapped water here is min(left[i], right[i]) - height[i] because it is bounded by the shortest of the two tallest pillars on

height[i]). This accomplishes the same as the left array but for bars to the right.

either side. Finally, we sum up the calculated trapped water values for all i to find the total amount of trapped rainwater. The result is computed using sum(min(l, r) - h for l, r, h in zip(left, right, height)), taking advantage of Python's built-in functions

and list comprehensions for concise code. By zipping the left, right, and height arrays together, we can iterate over them

Throughout this process, we use simple arrays and loops, a technique that falls under the category of <u>dynamic programming</u>, where we break down the problem into simpler subproblems and iteratively build up solutions to larger problems leveraging the solutions to smaller problems.

simultaneously, allowing us to easily calculate the minimum of left[i] and right[i], subtract the height[i], and sum all these

0, 2, 1, 0, 1, 3, 2, 1, 2, 1].

Now, follow the steps below:

Firstly, we initialize our left and right arrays:

Let's take a small example to illustrate the solution approach: Suppose our height map for the blocks is given by height = [0, 1,

## Secondly, we populate the left and right arrays: • Start filling the left array from left[1] to left[-1]. For each left[i], we consider max(left[i - 1], height[i]). This updates left to [0, 1,

rainfall.

**Python** 

1, 2, 2, 2, 2, 3, 3, 3, 3, 3].

1, 0, 1, 2, 1, 0, 0, 1, 0, 0].

**Example Walkthrough** 

values.

• Fill the right array in reverse (starting from the second to last element and moving to the first). For each right[i], we consider max(right[i + 1], height[i]). This updates right to [3, 3, 3, 3, 3, 3, 3, 2, 2, 2, 1].

• For each position i, calculate the trapped water as min(left[i], right[i]) - height[i], which gives us the volume at each position as [0, 0,

Lastly, sum the trapped water calculated for every position:

• Calculate the sum which is 0 + 0 + 1 + 0 + 1 + 2 + 1 + 0 + 0 + 1 + 0 + 0, giving us a total of 6 units of water that the blocks can hold after

With both arrays filled, we now calculate the trapped water above each index i in the height array:

Solution Implementation

By following the described solution approach step by step, we easily solve the problem using dynamic programming concepts

# Find the number of elements in height.
num\_elements = len(height)

# Initialize arrays to store the maximum to the left and right of each element.
max\_left = [height[0]] \* num\_elements

```
# Calculate the total amount of trapped water using the height difference
# between the minimum of max_left and max_right for each element and the height at that element.
trapped_water = sum(min(max_left[i], max_right[i]) - height[i] for i in range(num_elements))
```

Java

return trapped\_water

from typing import List

def trap(self, height: List[int]) -> int:

for i in range(1, num\_elements):

max\_right = [height[-1]] \* num\_elements

for i in range(num\_elements -2, -1, -1):

# Return the total amount of trapped water.

for (int i = 0; i < length; ++i) {</pre>

// Return the total trapped water.

return totalWater;

left\_max[0] = height[0];

max\_left[i] = max(max\_left[i - 1], height[i])

max\_right[i] = max(max\_right[i + 1], height[i])

class Solution:

```
class Solution {
    public int trap(int[] height) {
       // The length of the given height array.
       int length = height.length;
       // Arrays to store the maximum height to the left and right of every bar.
       int[] maxLeft = new int[length];
        int[] maxRight = new int[length];
       // Initialize the first element of maxLeft with the first height
       // as there's nothing to the left of it.
       maxLeft[0] = height[0];
       // Initialize the last element of maxRight with the last height
       // as there's nothing to the right of it.
       maxRight[length - 1] = height[length - 1];
       // Populate the maxLeft array by finding the maximum height to the left
       // of the current position, including itself.
        for (int i = 1; i < length; ++i) {</pre>
           maxLeft[i] = Math.max(maxLeft[i - 1], height[i]);
       // Populate the maxRight array by finding the maximum height to the right
       // of the current position, including itself. This loop runs backwards.
       for (int i = length - 2; i >= 0; --i) {
           maxRight[i] = Math.max(maxRight[i + 1], height[i]);
       // Variable to store the total amount of trapped water.
       int totalWater = 0;
       // Calculate the trapped water at each position by finding the
       // minimum of maxLeft and maxRight at that position (which is the maximum
       // water level the position can hold) and subtracting the height of the bar.
```

right\_max[num\_elements - 1] = height[num\_elements - 1];

left\_max[i] = max(left\_max[i - 1], height[i]);

right\_max[i] = max(right\_max[i + 1], height[i]);

maxLeftHeights[i] = Math.max(maxLeftHeights[i - 1], heights[i]);

maxRightHeights[i] = Math.max(maxRightHeights[i + 1], heights[i]);

// Populate the maxRightHeights array with the maximum heights to the right of each index

// Subtract the height of the current bar to get the water trapped at this index

# Initialize arrays to store the maximum to the left and right of each element.

# Fill the max\_left array with the maximum height to the left of each element.

# Fill the max\_right array with the maximum height to the right of each element.

# Calculate the total amount of trapped water using the height difference

totalWaterTrapped += Math.min(maxLeftHeights[i], maxRightHeights[i]) - heights[i];

// The water level at the current index is the minimum of the max heights to the left and right

for (int i = 1; i < num\_elements; ++i) {</pre>

for (int  $i = num_elements - 2; i >= 0; --i) {$ 

totalWater += Math.min(maxLeft[i], maxRight[i]) - height[i];

```
int total_water = 0; // Initialize total water to be trapped
        // Calculate trapped water at each index 'i' by finding the
       // smaller of the left and right max bars and subtracting the current height.
       // The result is added to total_water to find the cumulative water trapped across the entire array.
        for (int i = 0; i < num_elements; ++i) {</pre>
            total_water += min(left_max[i], right_max[i]) - height[i];
        // Return the total amount of trapped water
        return total_water;
};
TypeScript
function trap(heights: number[]): number {
    const numElements = heights.length;
    // Initialize arrays to store the maximum height to the left/right of each index
    const maxLeftHeights: number[] = new Array(numElements).fill(heights[0]);
    const maxRightHeights: number[] = new Array(numElements).fill(heights[numElements - 1]);
    // Populate the maxLeftHeights array with the maximum heights to the left of each index
    for (let i = 1; i < numElements; ++i) {</pre>
```

// Fill left\_max array such that left\_max[i] contains highest bar height to the left of index 'i' including itself

// Fill right\_max array such that right\_max[i] contains highest bar height to the right of index 'i' including itself

```
from typing import List

class Solution:
    def trap(self, height: List[int]) -> int:
        # Find the number of elements in height.
        num_elements = len(height)
```

max\_left = [height[0]] \* num\_elements

for i in range(1, num\_elements):

heights represented by the height list.

behind this time complexity is as follows:

max\_right = [height[-1]] \* num\_elements

for i in range(num\_elements - 2, -1, -1):

max\_left[i] = max(max\_left[i - 1], height[i])

max\_right[i] = max(max\_right[i + 1], height[i])

let totalWaterTrapped = 0;

return totalWaterTrapped;

for (let  $i = numElements - 2; i >= 0; --i) {$ 

// Calculate the total amount of trapped water

for (let i = 0; i < numElements; ++i) {</pre>

```
trapped_water = sum(min(max_left[i], max_right[i]) - height[i] for i in range(num_elements))

# Return the total amount of trapped water.
return trapped_water

Time and Space Complexity
```

The provided code implements a solution to calculate the amount of water that can be trapped between the bars of different

**Time complexity**: The time complexity of the solution is O(n) where n is the number of elements in the height list. The reasoning

Creating the left and right lists takes 0(n) each as they are initialized based on the first and last element respectively.
Populating the left and right lists with the maximum height encountered so far from the left and right involves a single pass through the height list from left to right and right to left, which again takes 0(n) time each.

# between the minimum of max\_left and max\_right for each element and the height at that element.

- list from left to right and right to left, which again takes 0(n) time each.
   Finally, the sum(min(l, r) h for l, r, h in zip(left, right, height)) computation is also linear, as it involves a single pass through the zipped lists, for a total of 0(n) time.
- Overall, as all these steps are sequential and each of them takes O(n) time, the total time complexity is O(n).

  Space complexity: The space complexity of the solution is also O(n). This is because additional space is used to store the left

and right lists which both have the same length as the input list height. No other significant storage is used that depends on n (the length of the height list), therefore, the space complexity is O(n).

To summarize, the code provided efficiently computes the water trapping problem with a linear time complexity and uses linear space to store interim results.