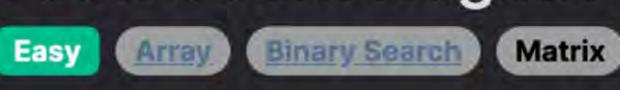
1351. Count Negative Numbers in a Sorted Matrix



Given a matrix grid which has dimensions m x n, our task is to count all the negative numbers within this grid. The matrix is sorted in a non-increasing (also known as non-decreasing) order across both rows and columns—this means the numbers go from larger on the top-left to smaller on the bottom-right.

Leetcode Link

To visualize, we might have a matrix like this:

The goal is to count how many negative numbers are present.

In the above example, you can see that rows and columns are sorted in non-increasing order and there are 8 negative numbers.

Intuition

Since the grid is sorted in non-increasing order row-wise and column-wise, we can use a more efficient approach than checking

each cell individually.

Here's the intuition step by step: 1. We start at the bottom-left corner of the matrix (grid[m - 1][0]). The reason for doing this is that if this number is negative,

if this number is not negative, we can move one column to the right.

the current row.

2. We keep track of our current position with indices i for rows and j for columns. We set ans to 0 to keep track of our count of negative numbers. 3. We use a while loop that runs as long as i is within the rows and j is within the columns of the grid.

then all numbers to its right are guaranteed to be negative because the row is sorted in non-increasing order. On the other hand,

- 4. If the current element where we are (grid[i][j]) is negative, we add the count of remaining columns in that row to our answer (i.e., ans += n - j) because all of these will be negative. After doing that, we move one row up (1 -= 1) since we're done with
- 5. If the element is not negative, we move one column to the right (j += 1) to check the next number in the same row. 6. The process is repeated until we've gone through all rows or columns. 7. We return the count ans which contains the number of negative numbers in the grid at the end of our loop.

The solution leverages the sorted property of the matrix to skip over non-negative elements and only count consecutive negatives,

- which makes it efficient.
- Solution Approach

The solution uses a simple algorithm that takes advantage of the properties of the matrix, namely that it is sorted in non-increasing order in both rows and columns. No additional data structures are needed; we can operate directly on the given grid.

1. Initiate two pointers, i for rows, starting from the last row (m - 1), and j for columns, starting from the first column (0).

case scenario, we'll make m+n moves.

2. Initiate a variable ans to store the count of negative numbers, initially set to 0. 3. Enter a while loop with the condition that i is greater than or equal to 0 (to make sure we are within the bounds of the rows) and

4. In the loop, check if the current element grid[i][j] is negative. If it is, increment ans by the number of columns remaining in the

current row (n - j). This is because, since the rows are non-increasing, all elements to the right of grid[i][j] will also be

negative. Then, decrease the row pointer i by 1, to move up to the previous row.

j is less than n (to make sure we are within the bounds of the columns).

5. If grid[i][j] is not negative, just move to the next column by incrementing j by 1.

Here is a step-by-step walkthrough of the implementation:

6. The loop continues until one of the exit conditions of the while loop is met (either all rows have been checked or the end of a row has been reached).

The time complexity of this algorithm is O(m + n), where m is the number of rows and n is the number of columns. This is because at

each step of the algorithm, we're either moving one row up or one column to the right until we exit the matrix bounds. In the worst-

The space complexity is O(1) as we are not using any additional space proportional to the size of the input grid; instead, we're just

No complex patterns are used here; the implementation is straightforward once the insight about the grid's sorted property is

using a few extra variables for counting and indexing.

7. Finally, return the ans variable, which now contains the count of negative numbers in the grid.

Example Walkthrough Let's consider a smaller example to clearly illustrate the use of the solution approach in a concrete situation. Suppose we have the following grid matrix with dimensions 3 x 4:

1. We initialize our pointers i with the index of the last row which is 2 for this grid (since we are using 0-based indexing), and j with

3. We begin our while loop. Our initial element to check is grid[2][0], which is 1. Since it's not negative, we move one column to

4. Now, grid[2][1] is -1, which is negative. We find that there are 4 - 1 = 3 columns remaining in the row, including the current

the index of the first column which is 0. 2. We set ans to 0 as our count of negative numbers.

the right by incrementing j to 1.

understood.

column. So, we add 3 to ans, making it 3, and move up a row by decrementing i to 1. 5. Our new position is grid[1][1], which is 1. It's not negative, so we move one column to the right again by incrementing j to 2.

We want to count the number of negative numbers in this grid. Here's how we can apply the solution approach:

6. We check grid[1][2], it's -1. There are 4 - 2 = 2 columns remaining, so we add 2 to ans, which becomes 5. We then move up a row by decrementing i to 0.

8. At grid[0][3], we have -1. With only 1 column at this last index, we add 1 to ans, resulting in a final count of 6. Since there are no

- Thus, the grid contains 6 negative numbers. With this example, it is clear how the algorithm smartly traverses the matrix, leveraging the sorted property to count negative
- def countNegatives(self, grid: List[List[int]]) -> int:

All elements in the current row to the right are also negative

7. The element grid[0][2] is 1, not negative. We increment j to 3.

numbers efficiently, without needing to check each element.

Get the dimensions of the grid

num_rows, num_cols = len(grid), len(grid[0])

Initialize pointers for the row and column

row_index, col_index = num_rows - 1, 0

If current element is negative

row_index -= 1

col_index += 1

public int countNegatives(int[][] grid) {

return negative_count

else:

if grid[row_index][col_index] < 0:</pre>

Move up to the previous row

Move right to the next column

Return the total count of negative numbers

negative_count += num_cols - col_index

// Function to count the number of negative numbers in a 2D grid

int rowCount = grid.size(); // Number of rows in the grid

int colCount = grid[0].size(); // Number of columns in the grid

int negativeCount = 0; // Initialize the counter for negative numbers

// If the current element is negative, then all elements to its right are also negative

// If the current element is not negative, move right to the next column

negativeCount += colCount - currentColumn; // Add all negative numbers in the current row

--currentRow; // Move up to the previous row to continue with the negative number sweep

int countNegatives(std::vector<std::vector<int>>& grid) {

// Start from the bottom-left corner of the grid

while (currentRow >= 0 && currentColumn < colCount) {</pre>

if (grid[currentRow][currentColumn] < 0) {</pre>

int currentRow = rowCount - 1;

// Loop through the grid diagonally

++currentColumn;

int currentColumn = 0;

} else {

more rows above, the loop ends here as i is decremented and falls below 0.

Initialize counter for negative numbers 9 negative_count = 0 10 11 12 # Iterate over the grid, starting from the bottom left corner while row_index >= 0 and col_index < num_cols:</pre> 13

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Java Solution
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1 class Solution {

Python Solution

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int rowCount = grid.length; // The number of rows in the grid.
           int colCount = grid[0].length; // The number of columns in the grid.
           int negativeCount = 0; // Initialize a count for negative numbers.
           // Start from the bottom-left corner of the grid and move upwards in rows and rightwards in columns.
           for (int rowNum = rowCount - 1, colNum = 0; rowNum >= 0 && colNum < colCount;) {
               // If the current element is negative, all the elements to its right are also negative.
               if (grid[rowNum][colNum] < 0) {</pre>
                   negativeCount += colCount - colNum; // Add the remaining elements in the row to the count.
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                   rowNum--; // Move up to the previous row to continue checking for negatives.
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               } else {
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                   colNum++; // Move right to the next column to check for non-negative elements.
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           return negativeCount; // Return the total count of negative numbers in the grid.
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C++ Solution
   #include <vector> // Necessary for using vectors
   class Solution {
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// Return the total count of negative numbers found in the grid return negativeCount; 29 30 }; 31

public:

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Typescript Solution
1 // Counts the number of negative numbers in a row-wise and column-wise sorted grid.
  // @param grid - A 2D array of numbers where each row and column is sorted in non-increasing order.
   // @returns The total count of negative numbers in the grid.
   function countNegatives(grid: number[][]): number {
       // Number of rows in the grid
       const rowCount = grid.length;
       // Number of columns in the grid - assumes at least 1 row exists
       const columnCount = grid[0].length;
       // Counter for negative numbers
       let negativeCount = 0;
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       // Start from the bottom-left corner of the grid
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       let row = rowCount - 1;
       let column = 0;
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       // Loop until we reach the top of the grid or the end of a row
       while (row >= 0 && column < columnCount) {
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           // If the current number is negative,
           // add all remaining negatives in the row to the counter
           // (as the row is sorted in non-increasing order)
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           if (grid[row][column] < 0) {</pre>
               // All numbers to the right of the current position are negative
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               negativeCount += columnCount - column;
               // Move up to the previous row since we've counted all negatives in the current row
               row--;
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               // If the current number is non-negative, move right to the next column
               column++;
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       // Return total count of negative numbers
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       return negativeCount;
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The provided code implements an algorithm to count the number of negative numbers in an m x n grid, which is assumed to be nonincreasing both row-wise and column-wise. The algorithm starts from the bottom-left corner of the grid and moves upwards or to

Time and Space Complexity

the right depending on the sign of the current cell value. **Time Complexity:**

• The outer loop runs a maximum of m times if we're moving upwards from the bottom row to the topmost row in the worst case.

 The inner condition can lead to moving rightwards across up to n columns. However, you will never revisit a row or a column once you've moved on from it (since you move up if you find a negative and move

The time complexity of the code can be analyzed as follows:

- right if you find a non-negative number), meaning each cell is visited at most once. Therefore, the maximum number of steps is m + n.
- **Space Complexity:** The space complexity of the code is:

Constant extra space is used for the variables m, n, i, j, and ans.

Thus, the time complexity of the algorithm is 0(m + n).

No additional data structures are being used that grow with the size of the input.

Considering the above points, the overall space complexity of the algorithm is 0(1), as it uses a constant amount of extra space regardless of the input size.

Problem Description