2971. Find Polygon With the Largest Perimeter Greedy Array Prefix Sum Sorting Medium

Problem Description

formed using the lengths provided in the nums array. If it's not possible to form a polygon from the given lengths, we must return -1. The perimeter of a polygon is simply the sum of the lengths of all its sides. The goal is to select three or more lengths from nums that meet the polygon inequality (sum of smaller sides greater than the longest side) and maximize their sum.

In this problem, we're given an array nums consisting of positive integers which represent potential side lengths of a polygon. A

polygon is a closed plane figure with at least three sides, and a crucial property of a valid polygon is that its longest side must be

shorter than the sum of its other sides. This problem asks us to determine the largest possible perimeter of a polygon that can be

To solve this problem, we start by sorting the nums array in non-decreasing order. This makes it easier to check the polygon

inequality: for any three consecutive lengths in this sorted array, if the sum of the first two is greater than the third, they can form

Intuition

Here is a step-by-step breakdown of the solution implementation.

a polygon. Once the array is sorted, we want to check every possible set of three consecutive lengths starting from the longest set and going down.

To achieve this efficiently, we accumulate the sums of nums elements by using the accumulate function from the itertools module, storing prefix sums in array s. E.g., s[k] is the sum from nums[0] to nums[k-1]. We start our check from a polygon with k sides. If the sum of the first k-1 sides (s[k - 1]) is greater than the k-th side (nums[k

- 1]), this means there can be a polygon with s[k] as its perimeter. If no such k exists, it means we cannot form a polygon, and thus, we return -1. The answer keeps track of the max perimeter found while satisfying the condition. Solution Approach

The solution provided applies a greedy approach combined with sort and prefix sum techniques to solve the problem efficiently.

Sorting: To facilitate the inequality check for forming a polygon, the first step is to sort the array of possible side lengths

nums in non-decreasing order. This helps to easily identify the potential largest side for any choice of sides and apply the

array nums. Prefix sums are helpful to quickly calculate the sum of elements that could form the sides of a potential polygon

polygon inequality, which is fundamental for the solution. nums.sort()

return ans

for k in range(3, len(nums) + 1):

combinations, thus reducing the complexity.

the initial=0 in the prefix sum array.

For k = 3 (first iteration):

if s[3 - 1] > nums[3 - 1]:

if s[5 - 1] > nums[5 - 1]:

if 8 > 4:

Solution Implementation

from itertools import accumulate

from typing import List

nums.sort()

class Solution:

12.

Python

if 3 > 2:

Data structures used include:

Example Walkthrough

perimeter found, or -1 if no polygon can be formed.

Prefix Sums: We utilize the accumulate function from Python's itertools module to compute the prefix sum of the sorted

without repeatedly adding elements in every iteration. s = list(accumulate(nums, initial=0)) Note that initial=0 is provided so that the accumulation array s starts with a 0, syncing the index of s with the

corresponding sum in nums. Iterating and Checking for a Polygon: The algorithm iterates over the sorted nums array, considering subsets starting from the third element (the smallest possible polygon has three sides) up to the end, checking if the current set can form a polygon.

if s[k - 1] > nums[k - 1]: ans = max(ans, s[k])Returning the Largest Perimeter: After the iterations, the variable ans, which is initialized with -1, will contain the largest

In this solution, the greedy choice is in selecting the largest potential side combinations starting from the end of the sorted array.

The algorithm stops at the largest perimeter found that satisfies the polygon inequality, without the need to check all possible

holds, a valid polygon can be formed, and we update the maximum perimeter ans.

For each subset, the algorithm checks if the sum of the first k-1 side lengths is greater than the k-th side. If this inequality

• A list to hold the prefix sums (s). The sorted version of the initial array (nums). These tools combined allow the solution to efficiently find the largest perimeter of a polygon with sides found in the input array or determine that such a polygon cannot exist.

nums.sort() # Becomes [1, 2, 2, 3, 4] **Prefix Sums**: Next, we use the accumulate function to get the prefix sums.

Iterating and Checking for a Polygon: We then iterate over the array, starting from the three smallest sides and move

towards the larger ones to check for the possibility of a polygon. The k-th index in nums corresponds to s[k+1] because of

Let's illustrate the solution approach using a small example. Consider the array of sides nums = [2, 1, 2, 4, 3].

Sorting: First, we sort the array to simplify the checking of potential polygons.

s = list(accumulate(nums, initial=0)) # s becomes [0, 1, 3, 5, 8, 12]

For k = 4 (second iteration):

satisfies the polygon inequality, without having to check all possible combinations.

For k = 5 (third iteration, checking for a triangle):

def largest perimeter(self, nums: List[int]) -> int:

Generate the cumulative sum of the sorted list,

cumulative_sum = list(accumulate(nums, initial=0))

with an initial value of 0 to make indices line up

Initialize the answer to be 0, where 0 will indicate

Final result, will be 0 if no triangle can be formed

Sort the numbers in non-decreasing order

that no triangle can be formed

largest_perimeter = 0

return largest_perimeter

import java.util.Arrays;

class Solution {

// Define the Solution class

int n = nums.length;

// Compute the prefix sums.

for (int i = 1; i <= n; ++i) {

// Import the Arrays class for sorting functionality

// Get the number of elements in the array.

prefixSum[i] = prefixSum[i - 1] + nums[i - 1];

// Check if a non-degenerate triangle can be formed

maxPerimeter = max(maxPerimeter, prefixSum[k]);

if $(prefixSum[k - 1] > nums[k - 1]) {$

for (int k = 3; $k \le n$; ++k) {

return maxPerimeter;

let maxPerimeter = -1;

return maxPerimeter;

from typing import List

nums.sort()

class Solution:

from itertools import accumulate

return largest_perimeter

Time and Space Complexity

the overall space complexity is O(n).

Time Complexity:

// Loop through the array to find a valid triangle

for (let index = 3; index <= numElements; ++index) {</pre>

if (sumArray[index - 1] > nums[index - 1]) {

def largest perimeter(self, nums: List[int]) -> int:

Generate the cumulative sum of the sorted list.

cumulative_sum = list(accumulate(nums, initial=0))

with an initial value of 0 to make indices line up

Initialize the answer to be 0, where 0 will indicate

Sort the numbers in non-decreasing order

// Update the maximum perimeter found so far

};

TypeScript

long long maxPerimeter = -1; // Initialize the maximum perimeter as -1

// The sum of the any two sides must be greater than the third side

// Return the maximum perimeter found, or -1 if no such triangle exists

// Initialize the answer as -1, which will indicate no triangle can be formed

// Check if the sum of the smaller two sides is greater than the current side.

// which is a necessary and sufficient condition for a non-degenerate triangle.

// Starting from the third element since a triangle needs 3 sides

maxPerimeter = Math.max(maxPerimeter, sumArray[index]);

// Return the maximum perimeter, or -1 if no valid triangle can be formed

// Iterate through the array considering each number as the longest side of the triangle

// Update the maximum perimeter with the current perimeter if it is larger

long[] prefixSums = new long[n + 1];

if s[4-1] > nums[4-1]: if 5 > 3:

Returning the Largest Perimeter: The largest perimeter found is 12, so our function would return 12.

This inequality also holds, so a polygon can be formed with sides [1, 2, 2, 3] and its perimeter is 5 + 3 = 8.

This inequality holds as well and represents a triangle with sides [2, 3, 4] which has the largest perimeter so far of 8 + 4 =

In this example, the sorted side lengths allow us to efficiently find the combination [2, 3, 4] with the largest perimeter that

This inequality holds, so a polygon can be formed with sides [1, 2, 2] and its perimeter is 3 + 2 = 5.

Iterate over the sorted numbers from the third element to the end for k in range(3, len(nums) + 1): # Check if the sum of the two smaller sides is greater than the largest side if cumulative sum[k - 1] > nums[k - 1]:

cumulative sum[k] is the perimeter of a triangle formed by nums[k-3], nums[k-2], nums[k-1]

Update the largest perimeter found so far if the above condition holds

// Method to find the largest perimeter of a triangle that can be formed with given side lengths

// Create an array to hold the sum of lengths up to the current index.

largest_perimeter = max(largest_perimeter, cumulative_sum[k])

public long largestPerimeter(int[] nums) { // Sort the array in non-decreasing order. Arrays.sort(nums);

Java

```
prefixSums[i] = prefixSums[i - 1] + nums[i - 1];
        // Initialize the variable to store the maximum perimeter found.
        long maxPerimeter = -1;
        // Loop over the array to find the maximum perimeter of any triangle that can be formed.
        for (int k = 3; k \le n; ++k) {
            // Check if the sum of the two smaller sides is greater than the largest side.
            if (prefixSums[k - 1] > nums[k - 1]) {
                // Update the maximum perimeter with the new larger perimeter.
                maxPerimeter = Math.max(maxPerimeter, prefixSums[k]);
        // Return the maximum perimeter found, or -1 if no triangle can be formed.
        return maxPerimeter;
C++
#include <vector>
#include <algorithm>
using namespace std;
class Solution {
public:
    // Function to calculate the largest perimeter of a non-degenerate triangle
    long long largestPerimeter(vector<int>& nums) {
        // First, sort the array in non-decreasing order
        sort(nums.begin(), nums.end());
        int n = nums.size(): // Size of the input array
        vector<long long> prefixSum(n + 1); // Vector to store prefix sums
        // Compute the prefix sums
        for (int i = 1; i \le n; ++i) {
```

```
function largestPerimeter(nums: number[]): number {
   // Sort the input array in non-decreasing order
   nums.sort((a, b) => a - b);
   // Get the total number of elements in the array
   const numElements = nums.length;
   // Initialize a new array to store the cumulative sums
   // The cumulative sum will be stored such that index 'i' of sumArray
   // contains the sum of the first 'i' elements of the sorted 'nums' array
   const sumArray: number[] = Array(numElements + 1).fill(0);
   // Compute the cumulative sums
   for (let i = 0; i < numElements; ++i) {</pre>
       sumArray[i + 1] = sumArray[i] + nums[i];
```

```
# that no triangle can be formed
largest_perimeter = 0
# Iterate over the sorted numbers from the third element to the end
for k in range(3, len(nums) + 1):
   # Check if the sum of the two smaller sides is greater than the largest side
    if cumulative sum[k - 1] > nums[k - 1]:
        # Update the largest perimeter found so far if the above condition holds
        # cumulative sum[k] is the perimeter of a triangle formed by nums[k-3], nums[k-2], nums[k-1]
        largest_perimeter = max(largest_perimeter, cumulative_sum[k])
# Final result, will be 0 if no triangle can be formed
```

The time complexity of the provided code is $0(n \log n)$ and the space complexity is 0(n).

elements sequentially, hence it has a time complexity of O(n).

The for loop (for k in range(3, len(nums) + 1)): This loop runs (n - 2) times (from 3 to len(nums)), which is O(n). In the loop, other than the condition check, we have an O(1) assignment for any variable (any = max(any, s[k])).

Sorting the list (nums.sort()): Sorting an array of n numbers has a time complexity of $0(n \log n)$.

- The dominant term here is from the sorting step, therefore the overall time complexity is $0(n \log n)$. **Space Complexity:**
- The sorted list does not require additional space since sorting is done in-place, hence the space complexity is 0(1) for this step.

Accumulating the sorted array (list(accumulate(nums, initial=0))): The accumulate function generates a sum of the

space complexity of O(n) for this list. The variables ans and k use constant space, contributing 0(1).

Adding these up, the main contribution to space complexity comes from the list generated by the accumulate function, therefore

When creating a list from the accumulate function, we're generating a new list of the same size as nums, hence we have a