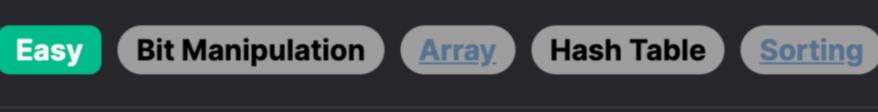
645. Set Mismatch



In this problem, we're dealing with a particular set of integers ranging from 1 to n where due to an error, one of the numbers was duplicated, causing another number to be missing. Our task is to figure out which number was duplicated (appears twice) and which one is missing from the array nums given to us.

The key to solving this problem lies in taking advantage of the properties of exclusive or (XOR) operations and the specifics of the data corruption that occurred.

Problem Description

Intuition

doing x XOR x gives us 0, and x XOR 0 gives us x. Thus, XOR-ing a number with itself cancels it out. With this property in mind, we can XOR all elements in the nums array with each integer from 1 to n. Ideally, if no number was

The intuition behind the solution can be developed by considering the properties of XOR operation. We know that for any number x,

duplicate and one missing number, we'll be left with the XOR of these two numbers. From there, we can distinguish between the duplicate and missing numbers by noticing that they must differ in at least one bit. We

duplicated and none missing, the result should be 0 because every number would cancel itself out. However, since we have one

find this differing bit (the rightmost bit is usually a good choice), and use it as a mask to separate the numbers into two groups - one with this bit set and one without it. Now, we apply XOR operation within each group, including the numbers from 1 to n. This separate XORing would give us the

duplicate number and the missing number, but we don't know which is which yet. We verify by checking each number in nums again. The number that we come across in the array is the duplicate, and the other one is the missing number. By applying XOR in such strategic ways, we leverage its ability to cancel equal pairs and isolate the odd ones out: in this case, our

Solution Approach

There are multiple approaches to solving this problem, each using different algorithms, data structures, or patterns. Here, we'll

discuss three distinct approaches.

duplicate and missing numbers.

Solution 1: Mathematics Using the principle of arithmetical sums, we can find the difference between the sum of a complete set from 1 to n (s_1) and the sum

of our corrupted array (s_2 after duplicates removal). The sum difference s - s_2 gives us the repeated element, while s_1 - s_2

identifies the missing element. This approach is direct and relies on simple arithmetic operations. However, it requires handling

Solution 2: Hash Table

This approach is more straightforward: construct a hash table to count the number of times each element appears in nums. Then, simply iterate through the range 1 to n and check the count for each number. If the count is 2, the number is duplicated; if 0, it's the missing number. The hash table provides a direct mapping from elements to their counts, making lookups efficient (0(1) on average).

The bit manipulation solution is more complex but efficient, especially regarding space complexity. The idea revolves around XOR

the XOR of the duplicate number a and the missing number b (xs = a XOR b). To separate these two values, we find the rightmost bit that is set in xs (lb = xs & -xs). We use this bit to divide the numbers into two groups and perform XOR operations on those groups. After separating elements into two piles, we XOR all elements that have

this bit set and all elements that don't. This will result in two numbers, one being a and the other b. To identify which is which, we

Finally, we return the duplicate and missing numbers as a list [a, b], ensuring the order is correct based on the final check with the

operations. We iterate through the array nums and range from 1 to n, XOR-ing each element and index. This process will give us xs,

original array. The brilliance of this approach lies in using the distinct patterns of XOR to segregate and identify unique elements while maintaining a very low space complexity.

Let's illustrate the third solution approach with XOR operation using a small example.

$xs = 1^2^2^4^1^2^3^4$

cancel out.

Example Walkthrough

After canceling out duplicate pairs (1^1, 2^2, and 4^4) we are left with:

iterate through the nums array again. The one we find in the array is our duplicate number.

potentially large sums, which could lead to integer overflow issues if not careful.

Solution 3: Bit Operation (implemented in the provided code)

 $xs = 2^3$

Assume our array nums is [1, 2, 2, 4] for n = 4. The ideal array without any errors would be [1, 2, 3, 4].

1. We start by initializing xs to 0 and we XOR all elements in nums and all numbers from 1 to n. Doing so gives us:

```
xs = 2^3 = 0010^011 = 0001
The rightmost set bit is 1 (we can find it by performing xs & −xs).
```

xs is now the XOR of the duplicate number and the missing number.

We perform XOR operations separately on these two groups alongside the numbers from 1 to n:

3. We now use this bit as a mask to split the elements into two groups. The first group will have this bit set (3 for our case) and the

2. Next, we find the rightmost set bit in xs, which we'll use as a bitmask to differentiate between the two numbers that didn't

4. Now, we have two results from each group: 3 and 2. We don't yet know which is the duplicate number and which is the missing one.

can identify the duplicate and the missing numbers in an array with a corrupted sequence of integers.

First pass: calculate the XOR of all indices and the elements in nums

Check if `number_a` is the duplicated number or the missing number

If `number_a` is found in nums, it is the duplicated one

Without bit set: 2 (since 1¹ and 4⁴ cancel themselves out leaving 2² which, after XORing, gives 2)

```
6. Since 3 did not appear in nums, it is the missing number.
7. We conclude that the duplicate number (a) is 2, and the missing number (b) is 3. Our ordered result would be [2, 3].
```

second will not (2 for our case).

Without bit set: 1^2^2^4^1^4

∘ With bit set: 3

After cancellation:

In this example walkthrough, we have effectively demonstrated how the third solution approach, which focuses on bit manipulation,

def findErrorNums(self, nums: List[int]) -> List[int]:

Obtain the rightmost set bit (least significant bit)

This will serve as a mask for segregating numbers

rightmost_set_bit = xor_result & -xor_result

for index, value in enumerate(nums, 1):

for index, value in enumerate(nums, 1):

if index & rightmost_set_bit:

if value & rightmost_set_bit:

return [number_a, number_b]

// XORing with xorResult to find the other number

return new int[] {number1, number2};

// Iterate over the array to check which one is the duplicate number

// If number1 is the duplicate, return number1 and number2 in order

// If number1 is not the duplicate then number2 is, so return number2 and number1 in order

int number2 = xorResult ^ number1;

for (int i = 0; i < length; ++i) {</pre>

if (nums[i] == number1) {

number_a ^= index

for value in nums:

if value == number_a:

xor_result ^= index ^ value

With bit set: 3 (already isolated, no duplicates to cancel it out)

Python Solution

5. To find out, we have to compare it against the nums array. In our example, we find 2 in nums, meaning 2 is the duplicate number.

11 12 # We will use `number_a` to find one of the numbers by segregating into two buckets 13 # The rightmost set bit will allow us to xor numbers into two groups # One group where the bit is set and another where it's not 14 15 number_a = 0

```
20
                    number_a ^= value
21
22
           # `number_b` is the other number we need to find
23
           number_b = xor_result ^ number_a
24
```

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class Solution:

xor_result = 0

```
31
           # If `number_a` is not in nums, it's the missing number and `number_b` is the duplicate
32
           return [number_b, number_a]
33
Java Solution
   class Solution {
       public int[] findErrorNums(int[] nums) {
           // The length of the array
           int length = nums.length;
           // Variable to store the XOR of all indices and values
           int xorResult = 0;
           // XOR all the indices with their corresponding values
8
9
           for (int i = 1; i <= length; ++i) {</pre>
               xorResult ^= i ^ nums[i - 1];
13
           // Find the rightmost set bit of xorResult
14
           int rightmostSetBit = xorResult & -xorResult;
15
           // Initialize variables to 0 that will store the two unique numbers
16
           int number1 = 0;
17
18
19
           // Separate the numbers into two groups and XOR them individually
20
           for (int i = 1; i <= length; ++i) {</pre>
21
               // Check for the rightmost set bit and XOR
22
               if ((i & rightmostSetBit) > 0) {
23
                    number1 ^= i;
24
25
               if ((nums[i - 1] & rightmostSetBit) > 0) {
26
                    number1 ^= nums[i - 1];
27
28
29
```

44 } 45

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```
return new int[] {number2, number1};
43
C++ Solution
 1 class Solution {
   public:
       vector<int> findErrorNums(vector<int>& nums) {
            int size = nums.size(); // Get the size of the input vector
           int xorSum = 0; // Initialize variable for XOR sum
           // Calculate XOR for all numbers from 1 to n and all elements in nums
           for (int i = 1; i <= size; ++i) {
               xorSum ^= i ^nums[i - 1];
 9
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12
           // Determine the rightmost set bit (which differs between the missing and duplicate)
13
           int rightMostBit = xorSum & -xorSum;
            int oneBitSetNum = 0; // This will hold one of the two numbers (missing or duplicate)
14
15
16
           // Divide the numbers into two groups based on the rightMostBit and XOR within groups
17
           for (int i = 1; i <= size; ++i) {
               if (i & rightMostBit) { // If the bit is set
18
                    oneBitSetNum ^= i; // XOR for the range 1 to N
19
20
               if (nums[i - 1] & rightMostBit) { // If the bit is set in the current element
21
                   oneBitSetNum ^= nums[i - 1]; // XOR with the nums elements
22
23
24
25
26
           int otherNum = xorSum ^ oneBitSetNum; // Find the second number using the xorSum
27
28
           // Determine which number is the missing number and which one is the duplicate
           for (int i = 0; i < size; ++i) {
29
               if (nums[i] == oneBitSetNum) {
30
                   // If we find oneBitSetNum in nums array, it is the duplicate
31
                    return {oneBitSetNum, otherNum}; // Return the duplicate and missing numbers
32
33
34
35
36
           // If not found, then oneBitSetNum is the missing number and otherNum is the duplicate
37
           return {otherNum, oneBitSetNum};
38
39 };
40
```

```
function findErrorNums(nums: number[]): number[] {
       // Calculate the total number of elements in the array.
       const length = nums.length;
       // Initialize xorSum to 0, which will be used to find the XOR sum of all elements and their indices.
       let xorSum = 0;
       // Loop through the array and XOR both the index and value of each element.
       for (let index = 1; index <= length; ++index) {</pre>
           xorSum ^= index ^ nums[index - 1];
10
11
12
       // Determine the rightmost set bit in xorSum using two's complement.
13
       const rightmostSetBit = xorSum & -xorSum;
14
15
       // Initialize a variable to hold one of the two numbers we're looking for.
16
       let oneNumber = 0;
17
18
       // Loop through the array and indices to partition them based on the rightmostSetBit.
19
       for (let index = 1; index <= length; ++index) {</pre>
20
           if (index & rightmostSetBit) {
22
               oneNumber ^= index;
23
24
           if (nums[index - 1] & rightmostSetBit) {
25
               oneNumber ^= nums[index - 1];
26
27
28
       // Determine the other number by XORing oneNumber with xorSum.
29
       const otherNumber = xorSum ^ oneNumber;
30
31
32
       // Check which number is missing from the array and which number is duplicated.
       // The number that appears in the nums array is the duplicated one,
33
       // and the one that's missing is the number that should have been there.
34
       return nums.includes(oneNumber) ? [oneNumber, otherNumber] : [otherNumber, oneNumber];
35
36 }
37
Time and Space Complexity
```

the loops are constant time operations.

Typescript Solution

The time complexity of the given code is O(n) where n is the length of the array nums. This is because each of the loops in the

function (for i, x in enumerate(nums, 1): and for x in nums:) iterates over the list nums exactly once, and all operations within

The space complexity of the function is 0(1), which means it uses a constant amount of extra space. Despite the input list size, the space consumed by the variables xs, lb, a, and b does not scale with n, thus having no additional space depending on the input size.