1638. Count Substrings That Differ by One Character

String Medium Dynamic Programming Hash Table

The goal of this problem is to count the number of ways in which we can select a non-empty substring from a string s and replace exactly one character in it such that the modified substring matches some substring in another string t. This is equivalent to finding substrings in s that differ by precisely one character from any substring in t.

Leetcode Link

last character e to a, obtaining s[0:6] + 'a' = "computa". This new substring, computa, is also a substring of t, thus constituting one valid way. The problem requires us to find the total number of such valid ways for all possible substrings in s.

For example, take s = "computer" and t = "computation". If we look at the substring s[0:7] = "compute" from s, we can change the

Intuition

To solve this problem efficiently, we can apply dynamic programming (DP). The intuition for using DP hinges on two key observations:

Problem Description

1. For every pair of indices (i, j) where s[i] is equal to t[j], the substrings ending at these indices can form a part of larger matching substrings, barring the one character swap.

at (i, j) and having this as their only difference should be counted. Given these observations, we can define two DP tables:

2. If s[i] is not equal to t[j], then we have found the place where a single character difference occurs. All substring pairs ending

 f[i][j] that stores the length of the matching substring of s[0..i-1] and t[0..j-1] ending at s[i-1] and t[j-1]. Essentially, it tells us how far back we can extend the matching part to the left, before encountering a mismatch or the start of the strings.

• g[i][j] serves a similar purpose but looks to the right of i and j, telling us how far we can extend the matching part of the

substrings starting at s[i] and t[j].

the above calculation. Finally, we return the value of ans as our answer.

single difference point, and this number is added to the accumulator ans.

- The variable ans accumulates the number of valid ways. For each mismatch found (where s[i] != t[j]), we calculate how many valid substrings can be formed and add this to ans. The number of valid substrings is computed as (f[i][j] + 1) * (g[i + 1][j +
- 1] + 1). This accounts for the one-character swap by combining the lengths of matching substrings directly to the left and right of (i, j).

We iterate through each pair of indices (i, j) comparing characters from s and t, and whenever we find a mismatch, we perform

Solution Approach The solution implements a dynamic programming approach to efficiently solve the problem by considering all possible substrings of

s and t and determining if they differ by exactly one character. Here's a step-by-step breakdown of the solution code:

1. Initialize Variables: The solution begins by initializing an accumulator ans to keep track of the count of valid substrings, and the

lengths of the strings s and t, denoted as m and n respectively.

indicating no match.

final answer.

Example Walkthrough

f[i][j] will hold the length of the matching substring pair ending with s[i-1] and t[j-1]. Similarly, g[i][j] will hold the length of the matching substring pair starting with s[i] and t[j].

3. Fill the f Table: The nested loop over i and j fills the f table. For each pair (i, j), if s[i-1] is equal to t[j-1], then f[i][j] is

set to the value of f[i-1][j-1] + 1, which extends the length of the matching substring by one. Otherwise, f[i][j] is already 0,

2. Create DP Tables: Two DP tables f and g are created with dimensions (m+1) x (n+1), initializing all their entries to 0. Each cell

4. Fill the g Table and Calculate ans: Another nested loop, counting downwards from m-1 to 0 for i and from n-1 to 0 for j, fills the g table. If s[i] is equal to t[j], then g[i][j] is set to g[i+1][j+1] + 1. But when s[i] does not match t[j], a mismatch has been found. The product (f[i][j] + 1) * (g[i+1][j+1] + 1) calculates the number of valid ways considering the mismatch as the

5. Return the Result: After iterating through all possible substrings, the ans variable will have accumulated the total number of valid

substrings where a single character replacement in s can result in a substring in t. This accumulated result is returned as the

- In this solution, dynamic programming tables f and g efficiently store useful computed values which are used to keep track of matches and calculate the number of possible valid substrings dynamically for each pair of indices (i, j). By avoiding redundant comparisons and reusing previously computed values, the algorithm avoids the naive approach's extensive computation, thus improving efficiency.
- Let's walk through a small example to illustrate the solution approach using strings s = "acdb" and t = "abc". 1. Initialize Variables: We set ans to 0. The lengths of the strings m and n are 4 and 3 respectively.

3. Fill the f Table: We iterate through strings s and t with indices i and j. When characters match, we set f[i][j] = f[i-1][j-1]

0 0

0

0

+ 1. Here's how f looks like after filling:

0

0

Start at s[3] = 'b' and t[2] = 'c', no match, set g[3][2] = 0.

b c

0 0

0 0

0

Here's the g matrix:

0

0

0

a

0 0

0 1

0 0

1 0

0 0 0

2. Create DP Tables: We initialize the DP tables f and g as 5×4 matrices, as s has length 4, and t has length 3.

4. Fill the g Table and Calculate ans: Next, we fill in the g table by iterating backwards. On mismatches, we calculate (f[i][j] + 1)

Move to s[3] = 'b' and t[1] = 'b', they match, so set g[3][1] = g[4][2] + 1 which is 1.

We calculate the valid ways for these mismatches, adding the results to ans.

 \circ For s[2] != t[0], (f[2][0] + 1) * (g[3][1] + 1) = (0 + 1) * (0 + 1) = 1.

• For s[0] != t[1], (f[0][1] + 1) * (g[1][2] + 1) = (0 + 1) * (0 + 1) = 1.

* (g[i+1][j+1] + 1) and add it to ans. Steps while filling g:

○ Continue for other elements. Discrepancies are found at s[2] = 'd' and t[0] = 'a', as well as s[0] = 'a' and t[1] = 'b'.

5. Return the Result: The variable ans now has the value 2, which is the number of valid substrings in s that can match substrings

0 1 0 a

In this case, ans will be calculated as follows:

We add these to ans, getting us an ans = 2.

for j, char_t in enumerate(t, 1):

for j in range(len_t - 1, -1, -1):

public int countSubstrings(String s, String t) {

for (int i = 0; i < m; i++) {

for (int j = 0; j < n; j++) {

for (int i = m - 1; i >= 0; i--) {

int[][] commonSuffixLength = new int[m + 1][n + 1];

int[][] commonPrefixLength = new int[m + 1][n + 1];

if (s.charAt(i) == t.charAt(j)) {

if char_s == char_t:

for i in range(len_s - 1, -1, -1):

if s[i] == t[j]:

C

b

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in t by changing exactly one character. We return this value as the answer.
Python Solution
    class Solution:
         def count_substrings(self, s: str, t: str) -> int:
             # Initializes the count of valid substrings
  3
             count = 0
  4
             # Lengths of the input strings
             len_s, len_t = len(s), len(t)
  6
             # Initialize the forward and backward match length tables
             forward_match = [[0] * (len_t + 1) for _ in range(len_s + 1)]
  8
             backward_match = [[0] * (len_t + 1) for _ in range(len_s + 1)]
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 11
             # Populate the forward match length table
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             for i, char_s in enumerate(s, 1):
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};

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Java Solution

class Solution {

else: # When characters do not match, we multiply the forward match # and backward match lengths and add these matched substrings to the count. count += (forward_match[i][j] + 1) * (backward_match[i + 1][j + 1] + 1) # Return the total count of valid substrings return count

// f[i][j] will store the length of the common substring of s and t ending with s[i-1] and t[j-1]

// g[i][j] will store the length of the common substring of s and t starting with s[i] and t[j]

// Compute the length of the common suffixes for all pairs of characters from s and t

commonSuffixLength[i + 1][j + 1] = commonSuffixLength[i][j] + 1;

commonPrefixLength[i][j] = commonPrefixLength[i + 1][j + 1] + 1;

// When there is a mismatch, count the valid substrings using the common prefix and suffix

count += (commonSuffixLength[i][j] + 1) * (commonPrefixLength[i + 1][j + 1] + 1);

// Compute the length of the common prefixes and the number of valid substrings

// If characters match, extend the common prefix by 1

return count; // Return the total count of valid substrings

 $forward_match[i][j] = forward_match[i - 1][j - 1] + 1$

 $backward_match[i][j] = backward_match[i + 1][j + 1] + 1$

int count = 0; // Initialize count to track the number of valid substrings

int m = s.length(), n = t.length(); // Lengths of the input strings

Populate the backward match length table, and calculate the count

for (int j = n - 1; j >= 0; j--) { 23 if (s.charAt(i) == t.charAt(j)) { 24 25 26 27 } else {

C++ Solution 1 #include <cstring> #include <string> class Solution { public: // Function to count the number of good substrings. int countSubstrings(string s, string t) { int answer = 0; // Initialize answer to zero. 8 int m = s.length(), n = t.length(); // Get the lengths of strings s and t. 9 10 11 // Dynamic programming arrays to keep track of matching substrings. int matchingSuffix[m + 1][n + 1]; 12 int matchingPrefix[m + 1][n + 1]; 13 14 15 // Initialize the DP tables with zeros. memset(matchingSuffix, 0, sizeof(matchingSuffix)); 16 memset(matchingPrefix, 0, sizeof(matchingPrefix)); 17 18 19 // Build the DP table for suffix matching substrings. for (int i = 0; i < m; ++i) { 20 for (int j = 0; j < n; ++j) { 21 22 if (s[i] == t[j]) { 23 // If characters match, extend the suffix by 1. 24 matchingSuffix[i + 1][j + 1] = matchingSuffix[i][j] + 1; 25 26 27 28 29 // Build the DP table for prefix matching substrings. for (int i = m - 1; i >= 0; --i) { 30 31 for (int j = n - 1; j >= 0; --j) { 32 if (s[i] == t[j]) { // If characters match, extend the prefix by 1. 33 34 matchingPrefix[i][j] = matchingPrefix[i + 1][j + 1] + 1;

// If characters don't match, calculate the count of

answer += (matchingSuffix[i][j] + 1) * (matchingPrefix[i + 1][j + 1] + 1);

// good substrings ending here.

// Return the total number of good substrings.

1 // Function to count the number of good substrings.

function countSubstrings(s: string, t: string): number {

const m = s.length; // Get the length of string s.

const n = t.length; // Get the length of string t.

let answer = 0; // Initialize answer to zero.

// Initialize arrays to keep track of matching substrings. 8 9 10 11

Typescript Solution

} else {

return answer;

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const matchingSuffix: number[][] = Array.from({ length: m + 1 }, () => Array(n + 1).fill(0));
         const matchingPrefix: number[][] = Array.from({ length: m + 1 }, () => Array(n + 1).fill(0));
         // Build the table for suffix matching substrings.
 12
         for (let i = 0; i < m; i++) {
 13
             for (let j = 0; j < n; j++) {
 14
                 if (s[i] === t[j]) {
 15
                    // If characters match, extend the suffix by 1.
 16
                    matchingSuffix[i + 1][j + 1] = matchingSuffix[i][j] + 1;
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 19
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 21
        // Build the table for prefix matching substrings.
 22
        for (let i = m - 1; i >= 0; i--) {
 23
             for (let j = n - 1; j >= 0; j--) {
 24
                 if (s[i] === t[j]) {
 25
                    // If characters match, extend the prefix by 1.
                    matchingPrefix[i][j] = matchingPrefix[i + 1][j + 1] + 1;
 26
 27
                } else {
                    // If characters don't match, calculate the count of
 28
                    // good substrings ending at this position.
 29
                    answer += (matchingSuffix[i][j] + 1) * (matchingPrefix[i + 1][j + 1] + 1);
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        // Return the total number of good substrings.
 36
         return answer;
 37 }
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Time and Space Complexity
Time Complexity
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loops and 0(m * n) for the inner nested loops, resulting in 0(m * n) overall.

The given code consists of a nested loop structure, where two independent loops iterate over the length of s and t. The outer loop runs for m + n times and the inner nested loops run m * n times separately for the loops that build the f and g 2D arrays. The computation within the inner loops operates in O(1) time. Therefore, the total time complexity combines the O(m + n) for the outer

Space Complexity

The space complexity is determined by the size of the two-dimensional arrays f and g, each of which has a size of (m + 1) * (n + 1). Hence, the space used by these data structures is 0 (m * n). No other data structures are used that grow with the input size, so the total space complexity is 0(m * n).