# 1631. Path With Minimum Effort

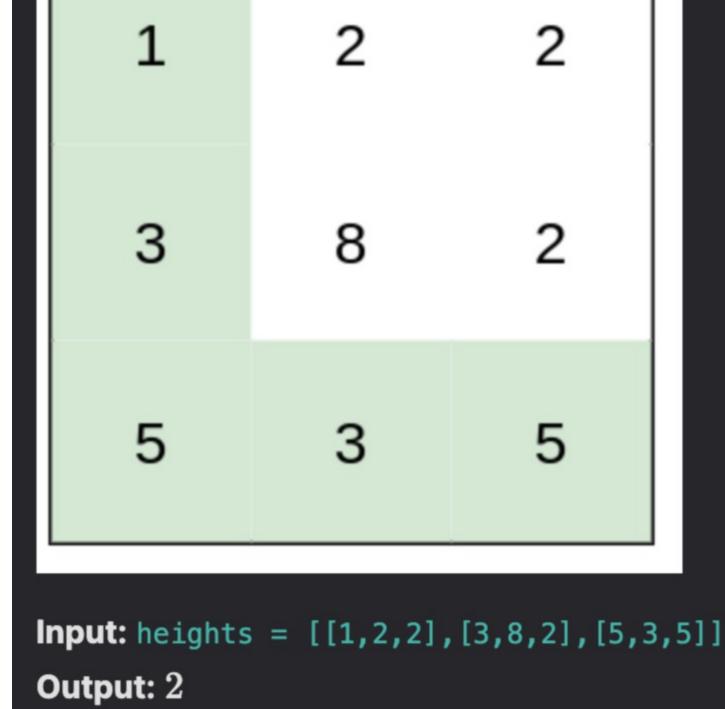
Leetcode Link

You are a hiker preparing for an upcoming hike. You are given heights, a 2D array of size rows x columns, where heights [row] [col] represents the height of cell (row, col). You are situated in the top-left cell, (0, 0), and you hope to travel to the bottom-right cell, (rows-1, columns-1) (i.e., O-indexed). You can move up, down, left, or right, and you wish to find a route that requires the minimum effort.

Return the minimum effort required to travel from the top-left cell to the bottom-right cell.

A route's **effort** is the **maximum absolute difference** in heights between two consecutive cells of the route.

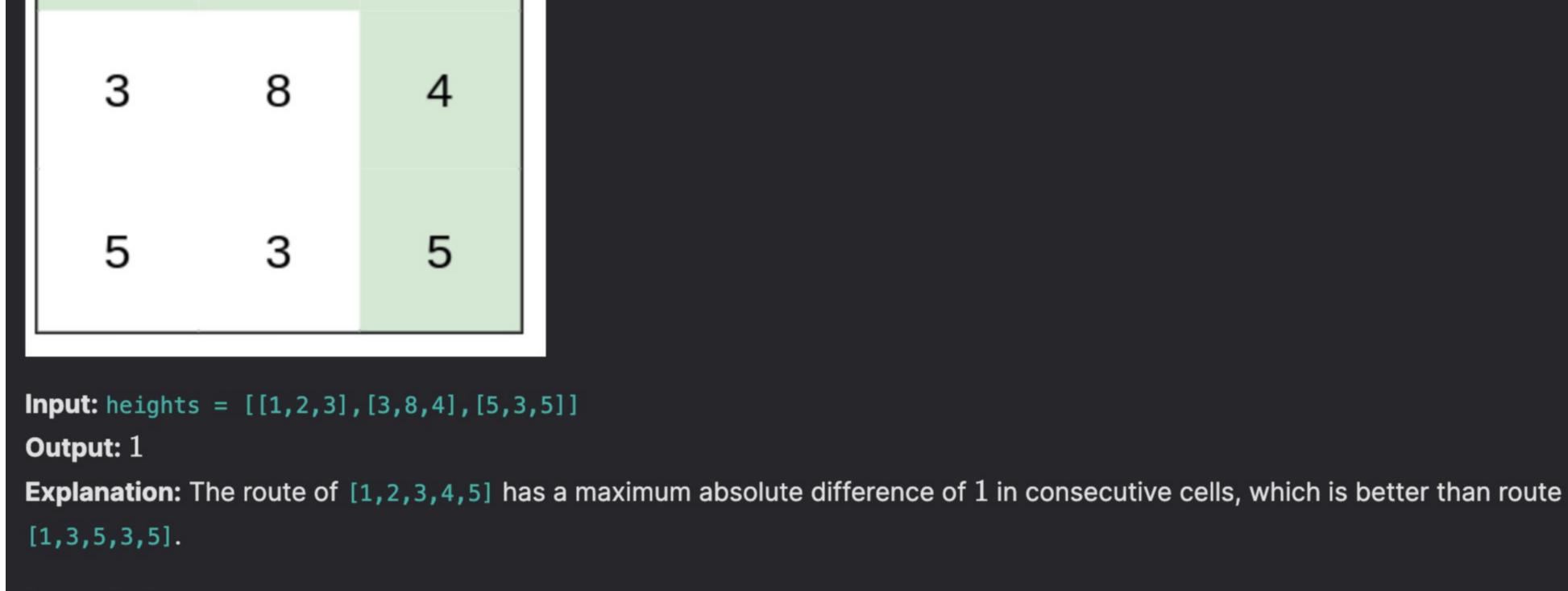
Example 1:



### [1,2,2,2,5], where the maximum absolute difference is 3.

Example 2:

**Explanation:** The route of [1,3,5,3,5] has a maximum absolute difference of 2 in consecutive cells. This is better than the route of

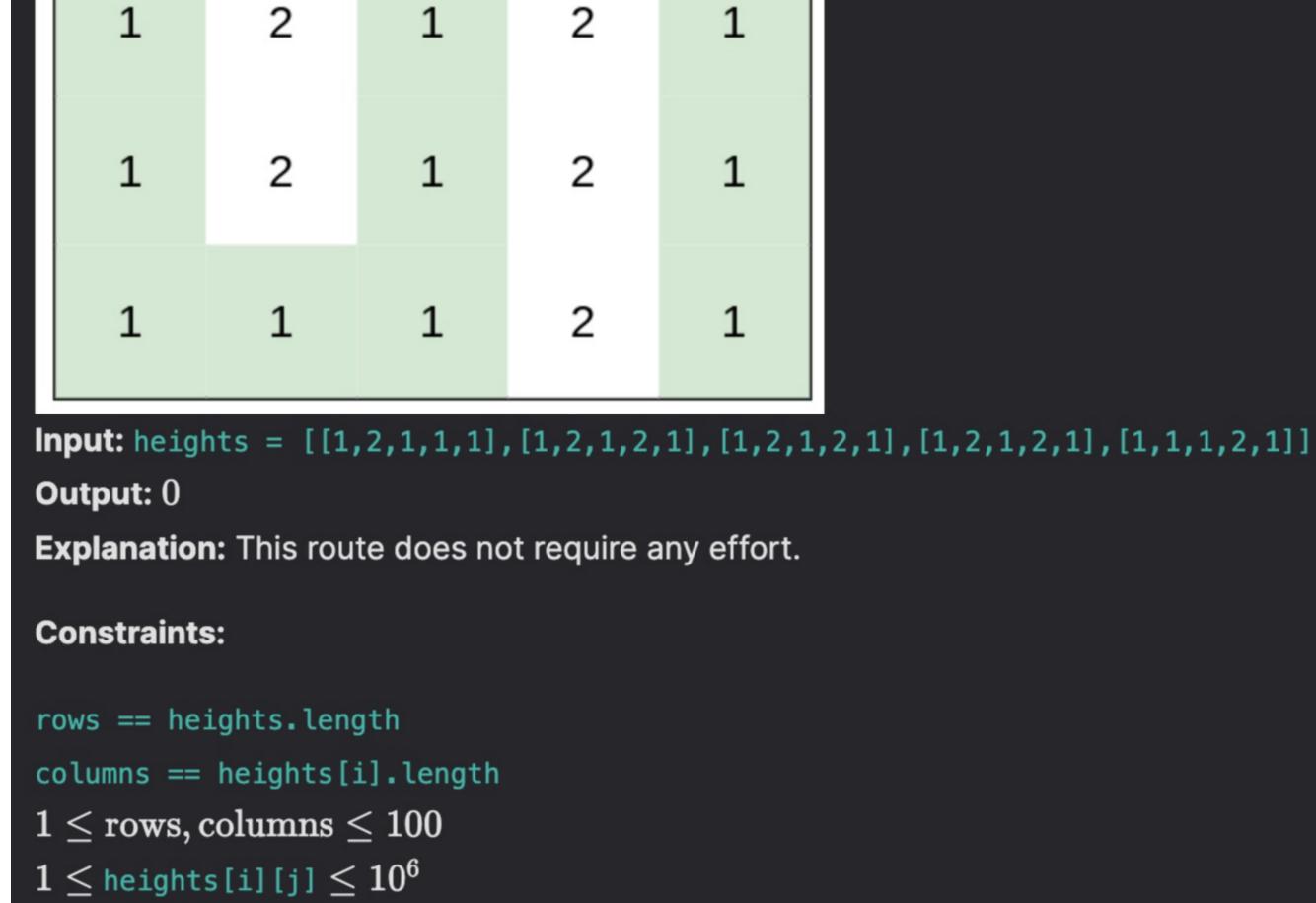


# Example 3:

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Solution

bottom-right cell. We'll then find the efforts for all these routes and return the smallest.

We'll denote an effort a as **good** if there exists a route with an effort smaller or equal to a.

**strictly** less than b are **not good** and all values greater or equal to b are **good**.

Given some effort a, how do we check if there exists a route that has an effort smaller or equal to a?

Let's first denote the distance between two adjacent cells as the absolute difference between their heights.

## **Brute Force**

# Instead of thinking of finding the efforts of all possible routes, we should think about finding routes that have some specific effort.

BFS/flood fill algorithm.

**Full Solution** 

A route will have an effort smaller or equal to a if it travels from the top-left cell to the bottom-right cell and all adjacent cells in the route have a distance that doesn't exceed a. To check if such routes exist, we can check if there exists a path from the top-left cell to the bottom-right cell such that we never travel between cells with a distance that exceeds a. We can accomplish this with a

Our most simple brute force for this problem would be to try all different routes that start from the top-left cell and end in the

Every binary search iteration, we can check whether or not some effort is good by running the BFS/flood fill algorithm mentioned

Let's denote R as number of rows, C as number of colmns, and M as maximum height in heights.

//We can also use queue<pair<int,int>> to store both the row & col in one queue

if (vis[newRow][newCol]) { // check if cell has been visited

above. **Time Complexity** 

// dimensions for heights

if (newRow < 0 || newRow >= rows || newCol < 0 || newCol >= columns) { // check if cell is in boundary

if (abs(heights[newRow][newCol] - heights[curRow][curCol]) > mid) { // check if distance exceeds limit

Since BFS/flood fill will run in  $\mathcal{O}(RC)$  and we have  $\mathcal{O}(\log M)$  binary search iterations, our final time complexity will be

The minimum effort a that's **good** is the final answer that we return. To find the minimum effort, we can implement a <u>binary search</u>.

Why can we binary search this value? Let's say our minimum **good** effort is b. Our binary search condition is satisfied since all values

### bool isValidEffort(vector<vector<int>>& heights, int mid) { int rows = heights.size(); 5 int columns = heights[0].size(); 6 vector<vector<bool>> vis(rows, vector<bool>(columns)); // keeps track of whether or not we visited a node 8 queue<int> qRow;

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1 class Solution {

 $\mathcal{O}(RC\log M)$ .

```
C++ Solution
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queue<int> qCol;

vis[0][0] = true;

qRow.pop();

qCol.pop();

while (!qRow.empty()) {

qRow.push(0);

const vector<int> deltaRow =  $\{-1, 0, 1, 0\}$ ;

const vector<int> deltaCol =  $\{0, 1, 0, -1\}$ ;

int curRow = qRow.front();

int curCol = qCol.front();

continue;

continue;

continue;

qCol.push(0); // BFS starts in top-left cell

for (int dir = 0; dir < 4; dir++) {

int newRow = curRow + deltaRow[dir];

int newCol = curCol + deltaCol[dir];

Time Complexity:  $\mathcal{O}(RC\log M)$ 

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vis[newRow][newCol] = true;
 31
                     qRow.push(newRow);
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 33
                     qCol.push(newCol);
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                     // process next node
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             return vis[rows - 1][columns - 1];
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        public:
 41
         int minimumEffortPath(vector<vector<int>>& heights) {
 42
                                   // every effort less or equal to low will never be good
             int low = -1;
 43
             int high = (int)1e6; // every effort greater or equal to high will always be good
 44
             int mid = (low + high) / 2;
             while (low + 1 < \text{high}) {
 45
 46
                 if (isValidEffort(heights, mid)) {
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                     high = mid;
 48
                 } else {
 49
                     low = mid;
 50
 51
                 mid = (low + high) / 2;
 52
 53
             return high;
 54
 55 };
Java Solution
    class Solution {
         final int[] deltaRow = \{-1, 0, 1, 0\};
         final int[] deltaCol = {0, 1, 0, -1};
         private boolean isValidEffort(int[][] heights, int mid){
             int rows = heights.length;
             int columns = heights[0].length; // dimensions for heights
  6
             boolean[][] vis = new boolean[rows][columns]; // keeps track of whether or not we visited a node
  8
             Queue<Integer> qRow = new LinkedList();
  9
             Queue<Integer> qCol = new LinkedList();
 10
             qRow.add(0);
 11
             qCol.add(0); // BFS starts in top-left cell
 12
             vis[0][0] = true;
 13
             while (!qRow.isEmpty()) {
 14
                 int curRow = qRow.poll();
 15
                 int curCol = qCol.poll();
 16
                 for (int dir = 0; dir < 4; dir++) {</pre>
                     int newRow = curRow + deltaRow[dir];
 17
                     int newCol = curCol + deltaCol[dir];
                     if (newRow < 0 || newRow >= rows || newCol < 0</pre>
 19
 20
                          || newCol >= columns) { // check if cell is in boundary
 21
                         continue;
 22
 23
                     if (vis[newRow][newCol]) { // check if cell has been visited
 24
                         continue;
 25
 26
                     if (Math.abs(heights[newRow][newCol] - heights[curRow][curCol]) > mid){
 27
                         // check if distance exceeds limit
 28
                         continue;
 29
                     vis[newRow][newCol] = true;
 30
 31
                     qRow.add(newRow);
 32
                     qCol.add(newCol);
 33
                     // process next node
 34
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return vis[rows-1][columns-1];

int rows = heights.length;

int mid = (low + high) / 2;

public int minimumEffortPath(int[][] heights) {

int columns = heights[0].length; // dimensions for heights

int low = -1; // every effort less or equal to low will never be good

int high = (int) 1e6; // every effort greater or equal to high will always be good

```
44
             while (low + 1 < high) {
 45
                 if (isValidEffort(heights,mid)) {
 46
                     high = mid;
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                 } else {
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                     low = mid;
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                 mid = (low + high) / 2;
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 52
             return high;
 53
 54 }
Python Solution
    import collections
     class Solution:
         def minimumEffortPath(self, heights: List[List[int]]) -> int:
             rows = len(heights)
             columns = len(heights[0]) # dimensions for heights
             low = -1 # every effort less or equal to low will never be good
  6
             high = 10 ** 6 # every effort greater or equal to high will always be good
             mid = (low + high) // 2
  8
             def isValidEffort(heights, mid):
  9
                 vis = [[False] * columns for a in range(rows)]
 10
                 # keeps track of whether or not we visited a node
 11
                 qRow = collections.deque([0])
 12
 13
                 qCol = collections.deque([0]) # BFS starts in top-left cell
 14
                 vis[0][0] = True
 15
                 while qRow:
 16
                     curRow = qRow.popleft()
                     curCol = qCol.popleft()
 17
 18
                     for [deltaRow, deltaCol] in [(-1, 0), (0, 1), (1, 0), (0, -1)]:
 19
                         newRow = curRow + deltaRow
 20
                         newCol = curCol + deltaCol
 21
                         if (newRow < 0 or newRow >= rows or newCol < 0 or newCol >= columns):
 22
                             # check if cell is in boundary
 23
                             continue
 24
                         if vis[newRow][newCol] == True: # check if cell has been visited
 25
                             continue
 26
                         if (abs(heights[newRow][newCol] - heights[curRow][curCol]) > mid):
 27
                             # check if distance exceeds limit
 28
                             continue
 29
                         vis[newRow][newCol] = True
 30
                         qRow.append(newRow)
 31
                         qCol.append(newCol)
 32
                         # process next node
 33
                 return vis[rows-1][columns-1]
 34
             while low + 1 < high:
 35
                 if isValidEffort(heights,mid):
 36
                     high = mid
 37
                 else:
                     low = mid
```

Got a question? Ask the Teaching Assistant anything you don't understand.

mid = (low + high) // 2

return high