2834. Find the Minimum Possible Sum of a Beautiful Array

Medium Greedy





Problem Description

Leetcode Link

The problem presents us with two positive integers, n and target. We are asked to find an array nums meeting specific criteria, being defined as beautiful:

All elements in nums must be distinct positive integers.

The array nums should have a length equal to n.

- There must not be any two distinct indices i and j within the range [0, n 1] for which nums[i] + nums[j] equals target.
- The goal is to determine the minimum possible sum of a beautiful array, with the added detail that the result should be given modulo

10^9 + 7. This modulus operation ensures that the numbers stay within a reasonable range, given the constraints of large number handling in most programming languages. Intuition

The solution relies on constructing the beautiful array iteratively while maintaining two key insights:

consecutive starting from 1.

2. To prevent any two numbers from being able to sum up to target, when we add a new number i to nums, we must make sure that target - i is not possible to be added in future steps. This is because if we have i in the array, and later add target - i, we would violate the condition that no two numbers can sum to target.

1. Since we want to minimize the sum of nums, we should start adding the smallest positive integers available, which are naturally

We use a set, vis, to keep track of numbers that cannot be a part of nums to satisfy the condition above. This is so we can quickly check if a number is disallowed before adding it to our array. Each iteration, we look for the smallest unvisited number starting from 1, add it to the sum, mark its complement with respect to target in vis, and move to the next smallest number.

sum remains as small as possible. Solution Approach

This iterative process is repeated n times to fill the nums array while ensuring all conditions for a beautiful array are met and that the

The implementation of the solution is straightforward and methodical. Let's break down the steps in the solution code:

1. Initialize an empty set vis which will store the integers that cannot be included in the nums array, to prevent summing up to the

target. 2. ans will hold the running sum of the nums array as we find the correct integers to include.

3. We start iterating through numbers to include in the nums array starting with i = 1, which ensures we start with the smallest positive integer.

Now we go into a loop that runs n times - once for each number that we need to add to our nums array:

5. Update the sum and set: Once we find a number that is not in vis, it means we can safely add it to ans without "violating" the

4. Check vis for the next available number: Since no two numbers should add up to target, before considering the integer i to add to ans, we check if it's already in the set vis. If it is, it means its complementary number (that would sum to target) is

target sum condition. We add i to ans, then we add target - i to vis. Adding target - i ensures that in the subsequent iterations, we don't pick a number that could combine with our current i to sum to target.

Let's use a small example to illustrate the solution approach. Suppose we have the following input:

already part of the nums array, so we increment i to the next number and check again.

6. Iterate: We increment i to consider the next integer in the following iteration. Finally, we return the total sum ans modulo 10^9 + 7. This modulus ensures that our final answer fits within the limits for integer values as prescribed by the problem and is a common practice in competitive programming to prevent integer overflow.

In this implementation, we use a greedy algorithm starting with the smallest possible integer and moving up. The set vis ensures

constant time complexity 0(1) checks and insertions, providing us with an efficient way to track and prevent selecting numbers that

potentially storing up to n integers in the vis set. Example Walkthrough

The overall time complexity of the solution is O(n) since we iterate over n elements, and the space complexity is also O(n) due to

 target = 10 Following the steps outlined in the solution approach:

1. Initialize a set and sum variable: We start with an empty set vis = {} and an integer for our running sum ans = 0.

2. Iterate through numbers starting with i = 1: Our goal is to iterate 5 times, as n = 5.

Now let's walk through each iteration:

• n = 5

could pair up to form target.

• Second Iteration (i = 2): 4. Check vis: 2 is not in vis, so it's safe to add. 5. Update ans and vis: ans = 1 + 2 = 3, vis = {9, 10

-2 = 8}. 6. Iterate to the next number: i = 3.

def minimum_possible_sum(self, n: int, target: int) -> int:

Initialize the answer (sum) to zero.

Add the current integer to the sum.

Return the computed sum after 'n' additions.

Move to the next integer.

current_int += 1

return answer

Initialize a set to keep track of visited numbers.

Initialize the current integer we are going to add to the sum.

Loop 'n' times to find 'n' unique numbers to add to the sum.

// Function to calculate the minimum possible sum of 'n' unique positive integers

// Create an array to keep track of the numbers that should not be used

// Initialize the sum to 0, the sum will be accrued over the iteration.

// Decrease the count of remaining numbers to add to our sum.

// Iterating over the potential numbers starting from 1.

// because they would add up to the target with a number already in use.

// Initialize the 'visited' array to false, indicating no numbers have been used yet.

// Skip the numbers that we can't use because they have a pair already in use.

// such that no pair of integers adds up to 'target'.

long long minimumPossibleSum(int n, int target) {

memset(visited, false, sizeof(visited));

// Add the current number to our sum.

visited[target - i] = true;

return sum; // Return the final sum.

bool visited[n + target];

for (int i = 1; n > 0; ++i) {

while (visited[i]) {

long long sum = 0;

++1;

sum += i;

--n;

= 7}. 6. Iterate to the next number: i = 4.

1 = 9}. 6. Iterate to the next number: i = 2.

• Fourth Iteration (i = 4): 4. Check vis: 4 is not in vis, so we can use it. 5. Update ans and vis: ans = 6 + 4 = 10, vis = {9, 8, 7, 10 - 4 = 6}. 6. Iterate to the next number: i = 5.

• Fifth Iteration (i = 5): 4. Check vis: 5 is not in vis, but adding it we need to consider that its target complement would be 5

• Third Iteration (i = 3): 4. Check vis: 3 is not in vis, so we take it. 5. Update ans and vis: ans = 3 + 3 = 6, vis = {9, 8, 10 - 3

• First Iteration (i = 1): 4. Check vis: 1 is not in vis, so we can consider it. 5. Update ans and vis: ans = 0 + 1 = 1, vis = {10 -

same, no new entry is added to vis. 6. There are no more iterations, as we've reached n additions. Finally, we return ans $% (10^9 + 7)$, which in this case is $15 % (10^9 + 7) = 15$, since 15 is already less than $10^9 + 7$.

The final beautiful array that satisfies all conditions could be [1, 2, 3, 4, 5] with the minimum possible sum being 15. The set vis

helped us to avoid including the numbers which would sum up to the target with any other number already in the array.

(since 10 - 5 = 5), and we're trying to add 5 now, so it's okay to choose it as 5 will not be added again. 5. Update ans and vis:

Since 5 can be added to ans, it's updated to ans = 10 + 5 = 15, and vis would include its target complement, but since it's the

Remember, in scenarios where n and target are much larger, the modulo operation would assure that the output fits within the 32-bit or 64-bit signed integer range commonly used in programming languages. Python Solution

14 # Find the next unvisited integer to add to the sum. 15 while current int in visited: 16 current_int += 1 17

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                answer += current_int
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               # Mark the counterpart (target - current_int) as visited.
23
                visited.add(target - current_int)
```

class Solution:

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visited = set()

current_int = 1

for _ in range(n):

answer = 0

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Java Solution
   class Solution {
       public long minimumPossibleSum(int n, int target) {
           // Create an array to keep track of visited numbers
           boolean[] visited = new boolean[n + target];
           // Initialize the answer (sum) to 0
            long sum = 0;
           // Loop over the numbers starting from 1 up to n
           for (int i = 1; n > 0; --n, ++i) {
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10
               // If the current number has been visited, skip to the next one
               while (visited[i]) {
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                   ++i;
13
               // Add the smallest unvisited number to the sum
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               sum += i;
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               // If the target is greater than or equal to the current number, mark the corresponding number as visited
               if (target >= i && (target - i) < visited.length) {</pre>
18
                   visited[target - i] = true;
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22
           // Return the final sum which is the minimum possible sum
23
           return sum;
24
25 }
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25 // Check if the counterpart of the current number (target - i) can potentially 26 // be used in the future, and mark it as visited to avoid using it. if (target >= i) { 27 28

C++ Solution

#include <cstring>

class Solution {

public:

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36 };
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Typescript Solution
    * Calculates the minimum possible sum of 'n' distinct integers where
    * each integer 'i' in the array does not equal 'target - i'.
    * @param {number} n - The count of distinct integers to sum
    * @param {number} target - The target value that must not be met by the expression 'i' + 'array[i]'
    * @returns {number} - The minimum possible sum of 'n' distinct integers.
    */
    function minimumPossibleSum(n: number, target: number): number {
       // Initialize a boolean array with false values to track visited numbers
10
       const visited: boolean[] = Array(n + target).fill(false);
11
       let sum = 0; // Initialize the sum of integers.
12
13
       // Iterate over the range of possible values until 'n' distinct integers are found
14
       for (let i = 1; n > 0; ++i, --n) {
15
16
           // Skip over the numbers that have already been visited
17
           while (visited[i]) {
18
               ++i;
19
           // Add the current integer to the sum
21
           sum += i;
22
23
           // Mark the corresponding pair value as visited if it falls within the array bounds
24
           if (target >= i && (target - i) < visited.length) {
               visited[target - i] = true;
25
26
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29
       // Return the minimum sum of 'n' distinct integers
30
       return sum;
31 }
```

The provided Python code snippet finds the minimum possible sum of a sequence of n integers such that each value and its complement with respect to target are unique in the sequence.

Time and Space Complexity

The time complexity of the code is O(n).

Here is the breakdown:

Inside the loop, there is a while loop that continues until i is not in vis. Since the while loop increments i each time a collision

with vis is detected and the number of possible collisions is limited by n, the amortized time complexity due to the while loop is 0(1).

Time Complexity

 Inserting and checking the presence of an item in a set in Python is 0(1) on average, as set is implemented as a hash table. Therefore, the time complexity for the complete for loop is essentially O(n).

Thus, the set vis dictates the space complexity, which is O(n).

There is a for loop that goes n times, which is O(n).

The space complexity of the code is O(n). Here is the breakdown:

Space Complexity

- A set named vis is used to keep track of visited numbers, which would at most store n elements because for every element we
- add, we loop n times. Other than vis, only a few variables are used (ans, i) with constant space requirement.