### 1371. Find the Longest Substring Containing Vowels in Even Counts



Hash Table String Prefix Sum

Leetcode Link

## In this problem, you're given a string s. Your task is to find the length of the longest substring of s where each of the vowels - 'a', 'e',

Problem Description

'i', 'o', 'u' - appears an even number of times. Substrings are continuous parts of the original string, and in this case, any substring that satisfies the vowel condition could potentially be the longest. The goal is to figure out the maximum length possible while adhering to the even occurrence condition for vowels.

### The intuition behind the solution is to use a bitwise representation to track the count of vowels in the substring efficiently. Because

Intuition

appeared an even or odd number of times. Thus, each vowel can be represented with 1 bit, resulting in a 5-bit integer for all five vowels (where 0 means even and 1 means odd number of occurrences). The key insight is that if at two different points in the string, the 5-bit integer (or state) is the same, it means that we have a substring (between these two points) where all vowels have appeared an even number of times.

we only care about even or odd occurrences, we don't need to keep a count of each vowel; we only need to know if a vowel has

The solution iterates through the string and toggles the respective bit in the state when a vowel is found. If the state has been seen before, we calculate the length of the new substring ending at the current character and update the answer if it's longer than the previous maximum. The pos array keeps track of the first occurrence of each state to calculate lengths of valid substrings. We start

by initializing the pos array with inf to denote that those states have not been seen yet, except for the state 0, which is initialized to -1 to handle the edge case where a valid substring starts at the beginning of the input string. By using this bitwise state and the pos array, we can efficiently find the longest substring where all vowels appear an even number of times.

Solution Approach The solution utilizes a bitwise approach combined with a hash map (implemented as a list called pos in the code) to keep track of the

## **Key Components of the Solution:**

• Vowels Bitmasking: Each vowel has a corresponding bit in a 5-bit integer, where the order is 'a', 'e', 'i', 'o', 'u'. For example, if only 'a' and 'i' have been seen an odd number of times, the state would be 10100 in binary, which is 20 in decimal.

• Tracking States: The state variable is a 5-bit integer representing the current state of vowels' counts (even/odd). The initial

## state is o since we start with an even count (zero occurrences) for all vowels.

indices at which each state occurs for the first time.

 Index Memory (pos): An array called pos of size 32 (since there are 2^5 possible states due to 5 vowels) is used to remember the earliest occurrence of every state. This array is initialized with inf, except for pos [0] which is set to -1.

• Iterating Through the String: As we iterate through the string, we check each character. If it's a vowel, we flip the corresponding

- bit in the state using the exclusive OR (XOR) operation: state ^= 1 << j, where j is the index of the vowel in the string 'aeiou'. Updating the Answer: With each new character processed, we check if the current state has been encountered before:
- First Occurrence: We also check if the current state's first occurrence needs to be updated in the pos array. If the current index is less than the stored value in pos[state], we update pos[state] with the current index.

By the end of the string traversal, ans will hold the length of the longest substring where all vowels appear an even number of times,

If it's been seen, we calculate the length of the substring from the first occurrence of this state to the current position.

If the calculated length is greater than the ans (which keeps track of the maximum length seen so far), we update ans.

- and that's what we return as the solution.
- Let's walk through a quick example:

 We start at state = 0 and pos[0] = -1 because we have an even count (zero) for all vowels at the start. • Iterating over s, whenever we encounter a vowel, we update state. Suppose state becomes 3 after some operations; this means

We continue this process until the end of the string, constantly updating ans with longer valid substrings as we find them.

### • If state is 3 again at a later point, we know that between these two indices, 'a' and 'e' must have appeared an even number of times. Therefore, we calculate the length of this substring and check if it's the maximum.

'a' and 'e' have been seen an odd number of times so far.

3. As we iteratively check each character in s, we use the following steps:

At index 4, s[4] = 'b': 'b' is not a vowel; state remains 01111.

At index 5, s[5] = 'c': 'c' is not a vowel; state remains 01111.

At index 3, s[3] = 'o': Toggling 'o': state = 01111.

Example Walkthrough:

1 s = "eleetminicoworoep"

The implementation is efficient with a time complexity of O(n), where n is the length of the string, because we only need a single

1 s = "aeiobcdf"

- pass through the string to compute the result, and each operation within that pass is of constant time complexity.
- Example Walkthrough Let's illustrate the solution approach using the string:
- 1. Initialize the pos array with length 32 to represent all possible states of vowel occurrences (2^5 for 5 vowels). Set all values to

2. We start with state = 0 (since no vowels have been seen yet) and ans = 0 (since no substrings have been found yet).

When at index 0, s[0] = 'a': We see our first vowel 'a'. The bit for 'a' in the state is toggled from 0 to 1. Now, state = 00001.

### At index 1, s[1] = 'e': We toggle the bit for 'e'. Now, state = 00011. At index 2, s[2] = 'i': Toggling the 'i' bit: state = 00111.

state is 01111.

**Python Solution** 

from math import inf

state = max\_length = 0

for index, char in enumerate(s):

if char == vowel:

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inf, except pos[0] to -1.

 At index 6, s[6] = 'd': 'd' is not a vowel; state remains 01111. At index 7, s[7] = 'f': 'f' is not a vowel; state remains 01111.

4. We've reached the end of the string, and throughout, each vowel has appeared exactly once, so their counts are odd. Our final

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5. Throughout our iteration, the state has changed from 00000 to 01111. After toggling the bits whenever we encountered a vowel,
   we checked pos to see if the current state had been recorded before. In this instance, since no state repeated other than the
   initial state 0, the length of the longest valid substring is zero because we have not encountered a state twice where the state
   would be 00000 again (meaning that all vowels have an even count).
So, the ans remains on this example; there are no substrings where each vowel occurs an even number of times.
The key takeaway is the tracking of vowel occurrences through bit manipulation, using XOR to toggle between even and odd counts,
and using the pos array to store the first occurrence of a state. This approach allows for quick lookups and updates while maintaining
an efficient assessment of the longest valid substring. However, in our example, there were no repeated states to determine a valid
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10 11 12 # List of vowels for reference vowels = 'aeiou'

# `max\_length` to keep track of the length of the longest valid substring so far

// Function to find the length of the longest substring containing vowels in even counts

int[] earliestPos = new int[32]; // 32 possible states for 5 vowels (2^5)

// State 0 (no vowels seen or all seen even times) starts at index -1

// This will keep track of the current state of vowels encountered.

// The result variable to store the length of the longest substring.

// Calculate the length if the current state has occurred before

// The length of the valid string would be difference of indices.

// Update the occurrence of current state if it's the first time.

firstOccurrence[currentState] = min(firstOccurrence[currentState], i);

for (int j = 0; j < 5; ++j) { // There are 5 vowels.

// Check if the current character is a vowel and update the state accordingly.

// Toggle the j-th bit of the state to represent the occurrence of vowel.

longestSubstringLength = max(longestSubstringLength, i - firstOccurrence[currentState]);

// pos array to keep track of the earliest index of each state

// Initialize all positions to max value except for state 0

# Toggle the corresponding bit if we encounter a vowel

# Iterate over the string characters with their index

# Check if the current character is a vowel

for j, vowel in enumerate(vowels):

state ^= 1 << j

public int findTheLongestSubstring(String s) {

// String of vowels to check against

earliestPos[0] = -1;

String vowels = "aeiou";

Arrays.fill(earliestPos, Integer.MAX\_VALUE);

substring. In a longer string with repeated vowel occurrences, the ans would likely be greater than zero.

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class Solution:
       def findTheLongestSubstring(self, s: str) -> int:
           # Initialize a list to store the first position we encounter a given state
           # State is represented as a bitmask integer of size 32 (for 5 vowels, each can be on/off)
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           positions = [inf] * 32
           # The starting state (all vowels have even counts) is at index 0
           positions[0] = -1
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           # `state` to keep track of the count of vowels encountered (even/odd as a bitmask)
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#### 26 27 # Calculate max length using current index and first index where current state was seen 28 max\_length = max(max\_length, index - positions[state]) 29 # Update the position for this state if it's the first time we're seeing this state 30 positions[state] = min(positions[state], index) 31 32 return max\_length 33

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Java Solution

class Solution {

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           // 'state' will represent the binary value of the vowels seen odd number of times
           int state = 0;
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           // 'maxLength' stores the length of the longest substring found so far
            int maxLength = 0;
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           // Loop through characters of input string
           for (int i = 0; i < s.length(); i++) {</pre>
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               char currentChar = s.charAt(i);
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               // Check and flip the corresponding bit for the vowel
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               for (int j = 0; j < 5; j++) {
                   if (currentChar == vowels.charAt(j)) {
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                        state ^= (1 << j);
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               // If state has been seen before, update the maxLength
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               maxLength = Math.max(maxLength, i - earliestPos[state]);
               // If state has not been seen before, set it to the current index
               if (earliestPos[state] == Integer.MAX_VALUE) {
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                    earliestPos[state] = i;
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           // Return the length of the longest substring
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           return maxLength;
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41 }
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C++ Solution
1 class Solution {
   public:
       int findTheLongestSubstring(string s) {
           // Initialize a vector to keep track of the first occurrence of all states.
           vector<int> first0ccurrence(32, INT_MAX);
           // Setting the base condition that for state '0', the first occurrence is at -1
           first0ccurrence[0] = -1;
           // Define a string of vowels for easy indexing.
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           string vowels = "aeiou";
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#### 32 33 34 // Return the length of the longest valid substring found. 35 return longestSubstringLength; 36

int currentState = 0;

int longestSubstringLength = 0;

for (int i = 0; i < s.size(); ++i) {

**if** (s[i] == vowels[j]) {

// Iterate over the characters of the string.

currentState ^= (1 << j);

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Typescript Solution
1 // Define a string of vowels for easy indexing.
2 const vowels: string = "aeiou";
   // This function calculates and returns the length of the longest substring
  // where the count of each vowel is even.
   function findTheLongestSubstring(s: string): number {
       // Initialize an array to keep track of the first occurrence of all states.
       let firstOccurrence: number[] = new Array(32).fill(Number.MAX_SAFE_INTEGER);
       // Setting the base condition that for state '0', the first occurrence is at -1
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       first0ccurrence[0] = -1;
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       // This will keep track of the current state of vowels encountered.
       let currentState: number = 0;
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       // The variable to store the length of the longest substring.
       let longestSubstringLength: number = 0;
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       // Iterate over the characters of the string.
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       for (let i = 0; i < s.length; i++) {</pre>
20
           // Check if the current character is a vowel and update the state accordingly.
           for (let j = 0; j < vowels.length; j++) {</pre>
21
               if (s[i] === vowels[j]) {
                   // Toggle the j-th bit of the state to represent the occurrence of the vowel.
24
                   currentState ^= (1 << j);
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           // If the current state hasn't occurred before, update the occurrence of the current state.
28
           if (firstOccurrence[currentState] === Number.MAX_SAFE_INTEGER) {
29
               firstOccurrence[currentState] = i;
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           // Calculate the length if the current state has occurred before
           // The length of the valid substring would be the difference of indices.
           longestSubstringLength = Math.max(longestSubstringLength, i - firstOccurrence[currentState]);
       // Return the length of the longest valid substring found.
       return longestSubstringLength;
```

# Time and Space Complexity

32 33 34 35 36 37 38 39 } 40

# Because these operations all have a constant time complexity, the overall time complexity of the function is O(n).

**Space Complexity** 

Time Complexity

The space complexity is determined by the fixed-size array pos, which has 32 elements (one for each possible state of the 5 vowel bits), and a few additional integer variables (state, ans, and the loop variables). Therefore, the space complexity of the algorithm is since the space required does not grow with the size of the input string s.

The given code iterates over each character of the string s, which has a length n. It performs a constant amount of work for each

character: checking if the character is a vowel, possibly flipping a bit in the state variable, and updating ans and pos[state].