1038. Binary Search Tree to Greater Sum Tree **Depth-First Search Binary Search Tree** Medium **Binary Tree**

Problem Description

the BST. In a BST, the properties are as follows: The left subtree of a node has nodes with keys less than the node's key.

The given problem presents a Binary Search <u>Tree</u> (BST) and requires transforming it into a "Greater Tree." The transformation

- should be such that each node's value is updated to the sum of its original value and the values of all nodes with greater keys in
- Both left and right subtrees adhere to the BST rules themselves. The challenge lies in updating each node with the sum of values greater than itself while maintaining the inherent structure of the

The right subtree has nodes with keys greater than the node's key.

- BST.

The solution approach leverages the properties of the BST, specifically the in-order traversal property where visiting nodes in this

order will access the nodes' values in a sorted ascending sequence. However, to obtain a sum of the nodes greater than the

current node, we need to process the nodes in the reverse of in-order traversal, which means we should begin from the rightmost node (the highest value) and traverse to the leftmost node (the lowest value). We'll maintain a running sum s that accumulates the values of all nodes visited so far during our reverse in-order traversal. For each node n, we will:

• Add n's updated value (which is inclusive of its original value) to s before moving to the left subtree. This process ensures that each node's value is replaced by the sum of its original value and all greater values in the BST. Our

solution does this iteratively with the help of a Morris traversal-like algorithm that reduces the space complexity to O(1) by

temporarily modifying the tree structure during traversal and then restoring it before moving to the left subtree. **Solution Approach**

3. For each node, there are two cases to consider:

Let's illustrate the solution with a simple BST example:

Consider a BST with the following structure:

just its own value because it's the highest).

Recursively visit the right subtree to add all greater values to s.

Update n's value by adding s to n's original value.

The solution provided utilizes an iterative approach with a Morris traversal pattern, which aims to traverse the tree without

additional space for recursion or a stack. Morris traversal takes advantage of the thread, a temporary link from a node to its predecessor, to iterate through the tree. Here's the breakdown of the approach: 1. Initialize a variable s to store the running sum and a variable node to keep the reference of the original root. 2. Start iterating from the root of the BST. Continue until the root is not null, as this indicates the traversal is complete.

If there is no right child, add the node's value to s. Then, update the node's value with s and move to the left child.

• If there is a right child, find the leftmost child of this right subtree (next), which will act as the current node's predecessor.

4. If the leftmost child (next) doesn't have a left child (indicating that we haven't processed this subtree yet), make the current node its left child (creating a thread) and move to the right child of the current node, deferring its update until after the greater values have been incorporated into s. 5. If the leftmost child (next) already has a left child (meaning the current node has been threaded and it's time to update it), remove the thread, add the current node's value to s, update the current node's value with s, and move to the left child.

This Morris traversal-based algorithm effectively improves space complexity to O(1) as it doesn't use any auxiliary data structure.

Example Walkthrough

The time complexity remains O(n), where 'n' is the number of nodes in the BST since each node is visited at most twice.

6. The loop continues until all nodes have been visited in reverse in-order, which updates all nodes with the sum of all greater node values.

- We want to transform it into a "Greater Tree" using the described Morris Traversal approach. 1. We start with the root node which has the value 4. We initialize s to 0.

2. Since node 4 has a right child (6), we look for the leftmost node in node 4's right subtree. Node 6 has no left child, so this step is skipped.

3. Since node 6 has no right child, we process it by adding its value to s. Now s = 0 + 6 = 6 and update node 6 to the new value s. The BST

Node 6 has been transformed into a "Greater Node" containing the sum of values greater than itself (which in this simple case is

4. Returning to node 4, we now should add its value to s (s = 6 + 4 = 10) and update it to the new value s. The tree structure at this moment is:

and update its value:

The final "Greater Tree" is:

Solution Implementation

Definition for a binary tree node.

self.val = val

else:

else:

Return the modified tree

return root

self.left = left

self.right = right

def init (self, val=0, left=None, right=None):

and move to the left child

if current node right is None:

total sum += current node.val

current_node = current_node.left

predecessor = current node.right

predecessor = predecessor.left

predecessor.left = current node

total sum += current node.val

current node.val = total_sum

current_node = current_node.left

predecessor.left = None

current_node = current_node.right

current node.val = total sum

if predecessor.left is None:

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now looks like this:

Node 4 is now a "Greater Node" having the sum of all nodes greater than itself.

11 6 Node 1 is now a "Greater Node," which includes the sum of all nodes greater than it.

6. Since node 1 is the leftmost node and it has no left child, our traversal and the transformation are complete for this simple tree.

5. Now we consider the left child of node 4, which is node 1. Since node 1 does not have a right child, we add its value to s (s = 10 + 1 = 11)

Followed by the Morris Traversal approach discussed, each node's value has been updated with the sum of all greater node values while maintaining the BST structure.

Python

class TreeNode:

class Solution:

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def bstToGst(self, root: TreeNode) -> TreeNode: total_sum = 0 # This will store the running sum of nodes

If there is no right child, update the current node's value with total_sum

Establish a temporary link between current_node and its predecessor

revert the changed tree structure and update the current node

while predecessor.left and predecessor.left != current_node:

If the right child is present, find the leftmost child in the right subtree

When leftmost child is found and a cycle is detected (temporary link exists),

Start with the root node current_node = root # Traverse the tree while current_node:

Java

class Solution {

TreeNode *left:

class Solution {

};

public:

TreeNode *right:

TreeNode* bstToGst(TreeNode* root) {

// Traverse the tree.

} else {

while (root != nullptr) {

} else {

return node;

let current = root;

while (current != null) {

let rightNode = current.right;

totalSum += current.val;

current.val = totalSum;

if (rightNode == null) {

// Case where there is no right child

let totalSum = 0;

if (root->right == nullptr) {

sum += root->val;

root = root->left;

TreeNode(int x): val(x), left(nullptr), right(nullptr) {}

TreeNode* predecessor = root->right;

if (predecessor->left == nullptr) {

predecessor->left = nullptr;

// Function to transform a Binary Search Tree into a Greater Sum Tree

function bstToGst(root: TreeNode | null): TreeNode | null {

// Loop over the tree using Morris Traversal approach

predecessor->left = root;

sum += root->val:

predecessor = predecessor->left;

TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}

// If there is no right child, process current node and move to left child.

while (predecessor->left != nullptr && predecessor->left != root) {

// If the left child of the predecessor is null, set it to the current node.

root->val = sum; // Update the node's value to be the greater sum.

// Restore the tree structure by removing the temporary link.

// If the left child of the predecessor is the current node, process current node.

// Update the total sum with current value

// Modify the current node's value to total sum

root->val = sum: // Update the value to be the greater sum.

// Find the in-order predecessor of the current node.

root = root->right; // Move to the right child.

root = root->left; // Move to the left child.

// Return the modified tree which now represents the Greater Sum Tree.

int sum = 0: // Initialize sum to keep track of the accumulated values.

TreeNode* node = root; // Keep track of the original root node

```
public TreeNode bstToGst(TreeNode root) {
        int sum = 0; // This variable keeps track of the accumulated sum
        TreeNode currentNode = root; // Save the original root to return the modified tree later
        // Iteratively traverse the tree using the reverse in-order traversal
        // (right -> node -> left) because this order visits nodes from the largest to smallest
        while (root != null) {
            // If there is no right child, update the current node's value with the sum and go left
            if (root.right == null) {
                sum += root.val; // Accumulate the node's value into sum
                root.val = sum; // Update the node's value with the accumulated sum
                root = root.left; // Move to the left child
            } else {
                // Find the inorder successor, the smallest node in the right subtree
                TreeNode inorderSuccessor = root.right:
                // Keep going left on the successor until we reach the bottom left most node
                // that is not the current root
                while (inorderSuccessor.left != null && inorderSuccessor.left != root) {
                    inorderSuccessor = inorderSuccessor.left;
                // When we find the leftmost child of the inorder successor
                if (inorderSuccessor.left == null) {
                    // Set a temporary link back to the current root node and move to the right child
                    inorderSuccessor.left = root;
                    root = root.right;
                } else {
                    // The temporary link already exists, and we've visited the right subtree
                    sum += root.val; // Update the sum with the current value
                    root.val = sum; // Update current root's value with accumulated sum
                    inorderSuccessor.left = null; // Remove the temporary link
                    root = root.left; // Move to the left child
        // Return the modified tree starting from the original root node
        return currentNode;
C++
* Definition for a binary tree node.
*/
struct TreeNode {
    int val;
```

```
};
TypeScript
```

```
current = current.left;
                                          // Move to the left subtree
        } else {
           // Find the leftmost node in the current's right subtree
            let leftMost = rightNode;
           while (leftMost.left != null && leftMost.left != current) {
                leftMost = leftMost.left;
           // First time visiting this right subtree, make a thread back to current
           if (leftMost.left == null) {
                leftMost.left = current;
               current = rightNode;
            } else { // Second time visiting - the thread is already there
                leftMost.left = null; // Remove the thread
               totalSum += current.val; // Update the total sum with current value
               current.val = totalSum; // Modify the current node's value to the total sum
                                        // Move to the left subtree
               current = current.left;
    // Return the modified tree root
   return root;
# Definition for a binary tree node.
class TreeNode:
   def init (self, val=0, left=None, right=None):
       self.val = val
       self.left = left
       self.right = right
class Solution:
   def bstToGst(self, root: TreeNode) -> TreeNode:
       total_sum = 0 # This will store the running sum of nodes
       # Start with the root node
       current_node = root
       # Traverse the tree
       while current_node:
           # If there is no right child, update the current node's value with total_sum
           # and move to the left child
           if current node.right is None:
               total sum += current node.val
               current node.val = total sum
               current_node = current_node.left
           else:
               # If the right child is present, find the leftmost child in the right subtree
               predecessor = current node.right
```

Time Complexity

while predecessor.left and predecessor.left != current_node:

Establish a temporary link between current_node and its predecessor

revert the changed tree structure and update the current node

When leftmost child is found and a cycle is detected (temporary link exists),

predecessor = predecessor.left

predecessor.left = current node

total sum += current node.val

current_node = current_node.left

current node.val = total_sum

predecessor.left = None

Return the modified tree

Time and Space Complexity

return root

original key in BST.

current_node = current_node.right

if predecessor.left is None:

most twice—once when the right child is connected to the current node during the transformation to threaded trees and once when it is reverted. There is no recursion stack or separate data structure which keeps track of the visited nodes. The while loop and nested while loop both ensure that each node is processed. **Space Complexity**

because the recursion stack is not being used here. The operation is done by manipulating the right pointers of the original tree.

The time complexity of the code is O(n), where n is the number of nodes in the tree. This is because each node is visited at

The provided code implements a variation of the Morris traversal algorithm to convert a Binary Search Tree (BST) to a Greater

Sum Tree (GST), where every key of the original BST is changed to the original key plus the sum of all keys greater than the

The space complexity of the code is 0(1) if we do not consider the space required for the output structure - it modifies the tree nodes in place with a constant number of pointers. There is no use of recursion, nor is there any allocation of proportional size to the number of nodes. However, if the function call stack is taken into account then that will not increase our space complexity