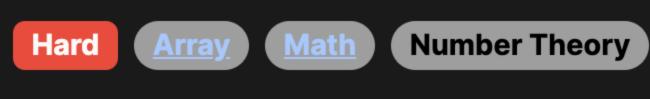
## 1250. Check If It Is a Good Array



### Problem Description

these numbers, multiply each selected number by an integer, and then sum them up to get a total of 1. If this is possible, the array is considered "good". Otherwise, it is not good. The task is to determine if the given array is good or not, and we are to return True if it is good and False if it is not.

The problem presents us with an array of positive integers called nums. Our goal is to check if it's possible to select a subset of

## Intuition

of two numbers is the largest number that divides both of them without leaving a remainder. If we can extend this concept to find the GCD of all numbers in the array and the result is 1, this implies that we can form the number 1 as a linear combination of the array numbers, using the Bezout's identity theorem.

This means that if the GCD of the entire array is 1, there must be some subset of numbers in the array which can be multiplied by

To determine if an array is good or not, we can use a mathematical concept called the Greatest Common Divisor (GCD). The GCD

some integers to sum up to 1, since 1 is the only number that when used in linear combinations can produce any integer (and specifically the integer 1 in our case).

The Python code makes use of the reduce function and the gcd function from the [math] (/problems/math-basics) module. The

reduce function is used to apply the gcd function cumulatively to the items of nums, from left to right, so that we are effectively finding the GCD of all the numbers in the array. If the GCD turns out to be 1, the function returns True. Otherwise, it returns False. This simple approach elegantly checks if the array is good using built-in functions to perform the necessary calculations.

#### The solution to this problem leverages the mathematical property of the Greatest Common Divisor (GCD) and a functional

programming construct in Python.

Solution Approach

Here's the step-by-step breakdown of the implementation:

returns their greatest common divisor.

• **Step 2**: Use the <u>reduce</u> function from the <u>functools</u> module. The <u>reduce</u> function is a tool for performing a cumulative operation over an iterable. In this case, it applies the <u>gcd</u> function starting with the first two elements of the <u>nums</u> array, and

then consecutively using the result as the first argument and the next element in the array as the second argument.

Step 1: Import the gcd function from the [math] (/problems/math-basics) module. gcd takes two numbers as arguments and

will calculate the gcd of the first and second elements, then take that result and calculate the gcd with the third element, and so on until it processes the entire array.

Step 4: After reduce has processed all the elements, we evaluate whether the accumulated GCD is 1. If the result is 1, it

Step 3: The reduce function will apply the gcd function progressively across all elements of the array. Essentially, this means it

- signifies that there is some combination of the array elements along with respective multiplicands that could add up to 1 (thanks to Bezout's identity). If not, it implies that no such combination is possible.

   Step 5: The isGoodArray method returns True if the GCD is 1, signaling that the array is "good", or returns False otherwise.
- Arrays: The given input is an array that the algorithm iterates through.
   Functional Programming: Using reduce is an example of functional programming, as it applies a function cumulatively to the items of an iterable

And that's it. By efficiently applying the gcd function cumulatively across all elements in the nums array, we can ascertain whether

The algorithm relies on the following data structures and patterns:

def isGoodArray(self, nums: List[int]) -> bool:

return reduce(gcd, nums) == 1

the array is "good" with a single line of code after the necessary functions are imported:

class Solution:

Example Walkthrough

```
nums = [6, 10, 15]
```

Now, let's walk through the process step by step:

#### • Step 1: We first import the gcd function from the math module, which will allow us to calculate the greatest common divisor of

array nums.

indeed 1.

from functools import reduce

Solution Implementation

from math import gcd

in a non-mutable way.

two given numbers.
 Step 2: We use the reduce function from the functools module to apply the gcd function cumulatively to the numbers in our

Step 3: First, reduce applies the gcd function to the first two elements, which are 6 and 10. The gcd of 6 and 10 is 2.

Let's illustrate the solution approach with a small example. Suppose we are given the following array of positive integers:

- Step 4: The result (2) is then used with the next element in the array, which is 15. The gcd of 2 and 15 is 1.
   Step 5: Since the reduce function has finished processing all elements, we check if the accumulated GCD is 1. In our case, it is
- According to Bezout's identity, because the final GCD is 1, there must be a combination of integer multiples of some or all numbers in our array nums that can add up to 1. Hence, for our input array, the function isGoodArray would evaluate to True,
- indicating that the array is "good".

  Here's a glimpse of how the code operates in this scenario:

nums = [6, 10, 15]
result = reduce(gcd, nums)
is\_good = result == 1 # This would be True in this case

The simplicity of this algorithm lies in its use of the gcd function to examine the entire array in a single sweep. If the gcd of all

# The function uses the greatest common divisor (gcd) to check if the array is 'good'.

# Use the reduce function to apply the gcd function cumulatively to the items of 'nums',

// An array is considered good if the Greatest Common Divisor (GCD) of all its elements is 1.

// If at any point the gcd becomes 1, we can return true immediately.

# An array is 'good' if the gcd of all numbers in the array is 1.

# from left to right, which reduces the array to a single value.

// Method to check if the array is a good array based on the condition.

// Iterate over each element in the array to find the overall gcd.

greatestCommonDivisor = std::gcd(number, greatestCommonDivisor);

// The array is "good" if the GCD is 1 after processing all elements.

// Note: TypeScript does not have a gcd function built-in, so you'll need to

// either implement it yourself or include a library that provides it.

return greatestCommonDivisor == 1;

// Importing gcd function from a math utilities module

function gcd(a: number, b: number): number {

// Recursively calling gcd with the remainder

function isGoodArray(nums: number[]): boolean {

let greatestCommonDivisor: number = 0; // Initialize to 0

// Iterating through each element in the given array 'nums'.

// Base case for the recursion

if (b === 0) return a;

return gcd(b, a % b);

int gcdValue = 0; // Initialize the gcd value to 0.

elements is 1, we can confidently say that the array is "good" as it meets the criteria outlined in the problem description.

```
Python

from functools import reduce
from math import gcd
```

def isGoodArray(self, nums: List[int]) -> bool:

# Then, check if the final gcd value is 1.

return reduce(gcd, nums) == 1

public boolean isGoodArray(int[] nums) {

for (int num : nums) {

if (gcdValue == 1) {

return true;

```
class Solution {
```

Java

class Solution:

```
// The array is good if the final gcd value is 1.
       return gcdValue == 1;
   // Helper method to calculate the gcd of two numbers using Euclid's algorithm.
    private int gcd(int a, int b) {
       if (b == 0) {
           // If the second number b is 0, then gcd is the first number a.
            return a;
        } else {
           // Recursively call gcd with the second number and the remainder of a divided by b.
            return gcd(b, a % b);
C++
#include <vector>
#include <numeric> // Required for std::gcd
class Solution {
public:
   // Function to determine if the array is a "good" array.
    // A "good" array is defined as an array where the greatest
    // common divisor of all its elements is 1.
    bool isGoodArray(std::vector<int>& nums) {
        int greatestCommonDivisor = 0; // Initialize to 0
       // Iterating through each element in the given array 'nums'.
        for (int number : nums) {
           // Update the greatest common divisor using std::gcd,
           // which is in the numeric header.
```

gcdValue = gcd(num, gcdValue); // Update gcdValue using the current element and the accumulated gcd.

```
// Function to determine if the array is a "good" array.
// A "good" array is defined as an array where the greatest
// common divisor of all its elements is 1.
```

**}**;

**TypeScript** 

```
for (let number of nums) {
      // Update the greatest common divisor using the gcd function.
      greatestCommonDivisor = gcd(greatestCommonDivisor, number);
    // The array is "good" if the GCD is 1 after processing all elements.
    return greatestCommonDivisor === 1;
from functools import reduce
from math import gcd
class Solution:
   def isGoodArray(self, nums: List[int]) -> bool:
       # The function uses the greatest common divisor (gcd) to check if the array is 'good'.
       # An array is 'good' if the gcd of all numbers in the array is 1.
       # Use the reduce function to apply the gcd function cumulatively to the items of 'nums',
       # from left to right, which reduces the array to a single value.
       # Then, check if the final gcd value is 1.
        return reduce(gcd, nums) == 1
Time and Space Complexity
Time Complexity
  The time complexity of the function is determined by the reduce function and the gcd (greatest common divisor) operations it
  performs on the list elements.
 • The reduce function applies the gcd function cumulatively to the items of the list, from start to end, to reduce the list to a single value.
 • The gcd function runs in O(log(min(a, b))) time, where a and b are the numbers whose GCD is being calculated.
```

# Assuming there are n elements in the nums list, the reduce function will perform n-1 gcd operations. Due to the nature of GCD calculation, where after the first operation, the resulting GCD will often be lesser than or equal to the smallest number among the

0(n\*log(k))

operands, each subsequent gcd operation is typically faster than the last. However, for worst-case analysis, we'll consider each operation to have the complexity of O(log(k)), where k is the smallest element after each operation.

## Where $\bf n$ is the number of elements in the list and $\bf k$ is the smallest number in the list at each step of the reduction.

Therefore, the time complexity is:

Space Complexity

The space complexity of the code is 0(1).

This space complexity comes from the fact that the gcd operations do not require additional space that scales with the input size, as they are computed in constant space.
The reduce function does not create any new data structures that depend on the input size; it just iterates over the existing list and updates the

accumulator in-place.

Thus, the space complexity is:

0(1)