2280. Minimum Lines to Represent a Line Chart

Medium Number Theory Geometry Math Sorting Array

Problem Description We have a 2D integer array named stockPrices, where each element consists of two integers representing a day and the

corresponding stock price on that day. The task is to determine the minimum number of straight lines required to connect all the points plotted on an XY plane, with the day as the X-axis and the price as the Y-axis, in the given order after sorting the data by the day. Essentially, we want to find the fewest lines that connect each adjacent point (each day to the next) to form a line chart.

Leetcode Link

Intuition

continue using the same line as long as consecutive segments share the same slope. When the slopes differ, we need a new line. To find the slope of the line segment between two points (x, y) and (x1, y1), we calculate (y1 - y) / (x1 - x), which gives us the rate of change in price with respect to days. Now, if we compare this slope with the next segment's slope between the points (x1, y1)

To solve this problem, the solution leverages the concept of slopes of lines. When connecting points to draw the line chart, we can

and (x2, y2), we would normally compute (y2 - y1) / (x2 - x1) and compare. To avoid division and possible precision issues with floating-point numbers, we instead compare cross-products: (y1 - y) * (x2 - x1) and (y2 - y1) * (x1 - x). If these two products are not equal, the slope has changed, and we need an additional line. The approach first sorts the stockPrices based on the day to ensure the points are in the correct order. Then, iterating through each pair of adjacent points, we calculate the aforementioned cross-product to decide whether the current segment can be connected

Remember, we increment the number of lines when a change in slope is detected between segments, and after calculating the slopes, we update the dx and dy to be the differences between the current and next points to be ready for the next iteration.

with the prior one or if a new line has to start. The variable ans keeps track of the number of lines needed.

The implementation given in the reference solution approach follows these steps:

1. Sort the Input: We start by sorting the stockPrices array. This ensures that the stock prices are ordered by day, which is

2. Initialize Variables: Two variables dx and dy are initialized to store the differences in the x (day) and y (price) coordinates of

Solution Approach

successive points. Additionally, ans is initialized to count the number of lines required.

essential as we need to connect points from one day to the next.

yields pairs of elements from the input list.

the next iteration for slope comparison.

without redundant calculations or comparisons.

Suppose we have the following 2D array stockPrices:

needed to represent the chart.

- 3. Iterate Through Points: We use a loop to go through each pair of adjacent points in the sorted array. To do this efficiently, the code leverages the pairwise utility, which is not a standard Python function but likely a user-defined or library function that
- 4. Calculate and Compare Slopes: For each pair (x, y) and (x1, y1), we calculate the change in x as dx1 = x1 x and the change in y as dy1 = y1 - y. We then compare the products of cross-multiplying these with the previous segment's dx and dy to

check if the slopes match. If dy * dx1 does not equal dx * dy1, the slope has changed, indicating a need for a new line.

5. Increment Line Count: When a slope change is detected, we increment ans by 1. 6. Update Differences: Whether a new line is added or not, we update dx and dy with the differences dx1 and dy1, to use them in

7. Return Result: After all points have been processed, the variable ans is returned. This gives us the minimum number of lines

- Here is the explanation of the algorithm, data structure, or pattern used in each step: Sorting: It's the first step and is critical for comparing the slopes of segments in the correct order.
- elements in a sequence. • Slope Comparison: This step avoids division by comparing slopes using cross-multiplication, which is a mathematical technique to avoid floating-point precision errors and ensure that comparisons are accurate when checking for collinearity between points.

By systematically comparing each pair of points, the solution efficiently calculates the number of lines needed to form the chart

Looping and Iteration: The use of a loop along with pairwise comparison is a common pattern when we need to check adjacent

Example Walkthrough

1 stockPrices = [[1, 100], [2, 200], [3, 300], [4, 200], [5, 100], [6, 200]]

Since stockPrices is already sorted by the day (the first element of each sub-array), we don't need to sort it again.

○ Imagine comparing the first point [1, 100] with the second [2, 200]. This sets our initial dx and dy to [2-1, 200-100] = [1,

We set dx and dy to 0 as there is no previous point to compare with yet.

100].

5. Increment Line Count:

6. Update Differences:

4. Calculate and Compare Slopes:

2. Initialize Variables:

1. Sort the Input:

 ans is initialized to 1 because we need at least one line to connect the first point to the next one. 3. Iterate Through Points:

Let's walk through a small example to illustrate the solution approach.

○ On the next iteration, we compare the point [2, 200] with [3, 300]. We calculate the changes dx1 = 3 - 2 and dy1 = 300 -200, resulting in [1, 100].

We don't increment ans as the line didn't change.

- Now we compare the slopes. Since dy * dx1 = dx * dy1 (100 * 1 = 1 * 100), the slope hasn't changed, and we stay on the same line.
- We set dx and dy to dx1 and dy1 respectively, for the next comparison. Continue this process for the remaining points:
- 8. Comparing [4, 200] with [5, 100], dx1 = 5 4 and dy1 = 100 200, resulting in [1, -100].

10. Return Result:

Python Solution

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from itertools import pairwise

num_lines = 0

prev_diff_x, prev_diff_y = 0, 1

num_lines += 1

Initialize the count of lines needed to 0

Iterate over each pair of adjacent stock prices

prev_diff_x, prev_diff_y = diff_x, diff_y

Return the total number of lines needed

public int minimumLines(int[][] stockPrices) {

from typing import List

After all points have been processed, we conclude that we need ans = 3 lines to connect all the points.

7. Comparing [3, 300] with [4, 200], we calculate dx1 = 4 - 3 and dy1 = 200 - 300, resulting in [1, -100].

Slopes match (as they're both [1, -100]), so we don't increment ans and just update dx and dy.

9. Finally, comparing [5, 100] with [6, 200], dx1 = 6 - 5 and dy1 = 200 - 100, resulting in [1, 100].

 \circ Slopes differ again (dy * dx1 = -100 * 1!= 1 * 100 = dx * dy1), so we increment ans to 3.

 \circ Slopes differ (dy * dx1 = 100 * 1!= -1 * 100 = dx * dy1), so we increment ans to 2 and update dx and dy.

- With this hands-on example, we've illustrated how the solution approach can be applied to determine the minimum number of lines required to connect a series of points in a line chart.
- class Solution: def minimumLines(self, stock_prices: List[List[int]]) -> int: # Sort the stock prices based on the days stock_prices.sort()

// Sort the stock prices array based on the day (the 0th element of each sub-array);

// if the days are equal, sort based on the price (the 1st element of each sub-array)

for (current_x, current_y), (next_x, next_y) in pairwise(stock_prices):

Compute the differences in x and y for the current pair

Update the previous differences for the next iteration

Arrays.sort(stockPrices, (a, b) -> Integer.compare(a[0], b[0]));

int minimumLines(std::vector<std::vector<int>>& stockPrices) {

// Initialize previous difference in x and y to compare slopes.

// Iterate through stockPrices starting from the second point

int nextX = stockPrices[i][0], nextY = stockPrices[i][1];

// If the cross product of the two segments is not zero,

// Calculate differences in x and y for the current segment

// Get x and y of the current and previous points

int deltaX = nextX - currX, deltaY = nextY - currY;

// Starting with an impossible value for the very first comparison.

int currX = stockPrices[i - 1][0], currY = stockPrices[i - 1][1];

// Update the previous slope to the current slope for the next iteration

previousSlope = [differenceX, differenceY];

// Return the total number of lines required

// they are not collinear, so the slope has changed and a new line is needed.

// Update previous differences to current one for next iteration comparison.

if (static_cast<long long>(prevDeltaY) * deltaX != static_cast<long long>(prevDeltaX) * deltaY) {

std::sort(stockPrices.begin(), stockPrices.end());

for (int i = 1; i < stockPrices.size(); ++i) {</pre>

// Sort stockPrices by their x-value (date)

int prevDeltaX = 0, prevDeltaY = 1;

// Begin with no lines drawn

++numLines;

prevDeltaX = deltaX;

prevDeltaY = deltaY;

int numLines = 0;

Initialize the previous differences in x and y to 0 and 1 respectively as placeholders.

18 diff_x, diff_y = next_x - current_x, next_y - current_y 19 20 # If the cross product of the differences does not equal to zero, 21 # then the points are not on the same line. Increment the number of lines. 22 if prev_diff_y * diff_x != prev_diff_x * diff_y:

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29
            return num_lines
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Java Solution

1 class Solution {

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// Initialize variables to keep track of previous slope components
           int prevDeltaX = 0, prevDeltaY = 1; // Initiated to 0 and 1 to handle the starting calculation
           int lineCount = 0; // Counter for the minimum lines needed
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           // Iterate over the stock prices starting from the second price
           for (int i = 1; i < stockPrices.length; ++i) {</pre>
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               // Get the previous day's stock price
               int previousX = stockPrices[i - 1][0], previousY = stockPrices[i - 1][1];
14
               // Get the current day's stock price
               int currentX = stockPrices[i][0], currentY = stockPrices[i][1];
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               // Calculate the change in x and y (i.e., the slope components) for the current line
18
               int deltaX = currentX - previousX, deltaY = currentY - previousY;
19
20
               // Check if the current line has a different slope than the previous one
21
22
               // by comparing cross products of the slope components (to avoid floating-point division)
23
               if (prevDeltaY * deltaX != prevDeltaX * deltaY) {
24
                   ++lineCount; // A different slope means a new line is needed
25
26
27
               // Update previous slope components for the next iteration
28
               prevDeltaX = deltaX;
29
               prevDeltaY = deltaY;
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32
           // Return the total number of lines needed to connect all points with straight lines
33
           return lineCount;
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35 }
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C++ Solution
1 #include <vector>
```

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#include <algorithm>

class Solution {

5 public:

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// Return the total number of lines needed
           return numLines;
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  };
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Typescript Solution
   function minimumLines(stockPrices: number[][]): number {
       // Get the number of stock price entries
       const stockPricesCount = stockPrices.length;
4
       // Sort the stock prices based on the first value of each pair (the dates are sorted)
       stockPrices.sort((a, b) => a[0] - b[0]);
6
8
       // Initialize the number of lines needed to connect all points
       let linesRequired = 0;
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       // Initialize a variable to store the previous slope as a pair of BigInts for accurate calculation
       let previousSlope: [BigInt, BigInt] = [BigInt(0), BigInt(0)];
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13
       // Start from the second point and compare slopes of consecutive points
14
       for (let i = 1; i < stockPricesCount; i++) {</pre>
15
16
           // Get the coordinates of the current point and the previous point
           const [previousX, previousY] = stockPrices[i - 1];
17
           const [currentX, currentY] = stockPrices[i];
18
19
20
           // Calculate the difference in x and y using BigInt for accuracy (to handle very large numbers)
21
           const differenceX = BigInt(currentX - previousX);
22
           const differenceY = BigInt(currentY - previousY);
23
24
           // If it's the first line or the slope differs from the previous slope, increment the line count
25
           if (i == 1 || differenceX * previousSlope[1] !== differenceY * previousSlope[0]) {
26
               linesRequired++;
```

Time Complexity The given Python code first sorts the stockPrices. Sorting takes O(n log n) time where n is the number of stockPrices.

stockPrices list, which takes O(n) time.

Time and Space Complexity

return linesRequired;

Inside the loop, it performs constant-time arithmetic operations to determine if a new line segment is required. Therefore, these operations do not increase the overall complexity beyond O(n).

Since sorting is the most time-consuming operation and is followed by a linear pass, the total time complexity of this algorithm is 0(n log n) + O(n), which simplifies to O(n log n).

Then, it iterates through the sorted prices to determine the number of lines required. This iteration involves a single pass through the

Space Complexity

The space complexity is determined by the additional space required by the algorithm besides the input. Here, the algorithm uses a fixed amount of space to store temporary values like dx, dy, dx1, and dy1, so it uses 0(1) additional space.

Sorting is typically done in-place (especially if the Python sort() method is used), therefore, the space complexity remains 0(1).

In summary, the space complexity of the algorithm is 0(1).