2070. Most Beautiful Item for Each Query

Binary Search Sorting

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Problem Description
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Medium Array

In this problem, we have a list of items, each represented by a pair [price, beauty]. Our goal is to answer a series of queries, each asking for the maximum beauty value among all items whose price is less than or equal to the query value.

If no items fit the criteria for a given query (all items are more expensive than the query value), the answer for that query is 0. We are asked to return a list of the maximum beauty values corresponding to each query.

Intuition

the maximum beauty for any given price limit. We approach this by sorting the items by price. Sorting the items allows us to employ a binary search technique to efficiently find

To solve the problem efficiently, we first notice that we can handle the queries independently. So, we want a quick way to find

the item with the highest beauty below a certain price threshold.

After sorting items, we create two lists: prices, which holds the sorted prices, and mx, which holds the running maximum beauty

observed as we iterate through the sorted items. This ensures that for each price prices[i], mx[i] is the maximum beauty of all items with a price less than or equal to prices[i].

The binary search is carried out by using the bisect\_right function from Python's bisect module. For each query, bisect\_right finds the index j in the sorted prices list such that all prices to the left of j are less than or equal to the query value.

If such an index j is found and is greater than 0, it means there exists at least one item with a price lower than or equal to the query value. We use j - 1 as the index to get the maximum beauty value from the mx list.

Otherwise, if no index j is returned because all items are too expensive, we default the answer for that query to 0. This algorithm allows us to answer each query in logarithmic time with respect to the number of items, which is desirable when

dealing with a large number of items or queries.

**Solution Approach** The solution uses a mix of sorting, dynamic programming, and binary search to efficiently answer the maximum beauty queries

Here's the step-by-step implementation strategy: **Sorting Items:** Start by sorting the items based on their price. This is vital because it allows us to leverage binary search later

for given price limits.

on. Sorting is done using Python's default sorting algorithm, Timsort, which has a time complexity of O(n log n). Extracting Prices and Initializing Maximum Beauty List (mx):

simply the beauty of the first item in the sorted list.

Extract the sorted prices into a list called prices.

**Building a Running Maximum Beauty:** • Iterate through each item, starting from the second one (since the first element's max beauty is already recorded).

Initialize a list mx, which keeps track of the maximum beauty encountered so far as we iterate through the items. The first element of mx is

For each item, update the mx list with the greater value between the current item's beauty and the last recorded max beauty in mx. This is a

form of dynamic programming, where the result of each step is based on the previous step's result. **Answering Queries with Binary Search:** 

 Initialize an answer list ans of the same size as queries, defaulting all elements to 0. For each query, use the bisect\_right function from the bisect module to perform a binary search on prices to find the point where the query value would be inserted while maintaining the list's order.

∘ If j is not 0, it means an item with a suitable price exists, and the answer for this query is mx[j - 1] - the corresponding max beauty by that

• bisect\_right returns an index j that is one position past where the query value would be inserted, so a price less than or equal to the query must be at an index before j.

price. If j is 0, it means no items are cheaper than the query, and the answer remains 0.

**Return the Answer List:** After all queries have been processed, return the answer list ans filled with the maximum beauties for each respective query.

This approach effectively decouples the item price-beauty relationship from the queries, by pre-computing a list of maximum beauties (mx) that can later be quickly referenced using binary search. This transforms what could be an O(n\*m) problem (naively checking n items for each of m queries) into an O(n log n + m log n) problem, where n is the number of items and m the number

of queries.

Suppose we have the following items and queries: • items = [[3, 2], [5, 4], [3, 1], [10, 7]] • queries = [2, 4, 6] Following the steps:

## Extract prices: prices = [3, 3, 5, 10] Initialize mx with the maximum beauty of the first item: mx = [2]

**Sorting Items:** 

**Example Walkthrough** 

```
Building a Running Maximum Beauty:
```

Initialize an answer list ans with all zeros: ans = [0, 0, 0]

Query 1: 2 is less than all prices, therefore ans [0] remains 0.

# Extract a list of prices for binary search

prices = [price for price, \_ in items]

for index in range(1, len(items)):

answers = [0] \* len(queries)

**Answering Queries with Binary Search:** 

**Return the Answer List:** 

from bisect import bisect\_right

items.sort()

**Python** 

class Solution:

We sort items by price: sorted\_items = [[3, 2], [3, 1], [5, 4], [10, 7]]

Extracting Prices and Initializing Maximum Beauty List (mx):

Let's illustrate the solution approach with a small example:

 Query 2: 4 is equal to the second price, bisect\_right would place it after index 1, so we use mx[0]: ans = [0, 2, 0] Query 3: 6 would fit between indexes 2 and 3, bisect\_right returns 3 so we use mx[2]: ans = [0, 2, 4]

• The final answer list reflecting maximum beauties for each query is: ans = [0, 2, 4] Thus, for the queries [2, 4, 6], the maximum beauty values for items within these price limits are [0, 2, 4], respectively.

Process the third item: new price with higher beauty, update mx: mx = [2, 4]

Process the fourth item: new price with higher beauty, update mx: mx = [2, 4, 7]

 $\circ$  Process the second item: it has the same price but lower beauty, so mx remains the same: mx = [2]

Solution Implementation

max\_beauty.append(max(max\_beauty[-1], items[index][1]))

# Process each query to find the maximum beauty for that price

# Initialize the answer list for the queries with zeroes

answers[i] = max\_beauty[index - 1]

# Return the list of answers to the queries

def maximumBeauty(self, items: List[List[int]], queries: List[int]) -> List[int]:

# Sort the items by price first (since the first item of each sub-list is price)

# Update the max\_beauty list with the maximum beauty seen up to current index

# Create a list to store the maximum beauty encountered so far max\_beauty = [items[0][1]] # initialize with the first item's beauty

## for i, query in enumerate(queries): # Find the rightmost item that is not greater than the query price index = bisect\_right(prices, query) # If we found an item, store the corresponding max beauty (if not, zero stays by default)

if index:

} else {

**if** (left > 0) {

return answers;

left = mid + 1;

answers[i] = items[left - 1][1];

// Return the array of answers for all the queries

if (items[mid][0] > queries[i])

if (left > 0) answers[i] = items[left - 1][1];

let mid = Math.floor((left + right) / 2);

if (items[mid][0] > queries[i])

answers[i] = items[left - 1][1];

right = mid;

for index in range(1, len(items)):

for i, query in enumerate(queries):

index = bisect\_right(prices, query)

answers = [0] \* len(queries)

else

**if** (left > 0) {

return answers;

right = mid;

left = mid + 1;

else

return answers;

**}**;

**TypeScript** 

```
return answers
Java
class Solution {
    public int[] maximumBeauty(int[][] items, int[] queries) {
       // Sort the items array based on the price in increasing order
       Arrays.sort(items, (item1, item2) -> item1[0] - item2[0]);
       // Update the beauty value in the sorted items array to ensure that each
       // item has the maximum beauty value at or below its price.
        for (int i = 1; i < items.length; ++i) {</pre>
           // The current maximum beauty is either the beauty of the current item
           // or the maximum beauty of all previous items.
            items[i][1] = Math.max(items[i - 1][1], items[i][1]);
       // The number of queries to process
       int queryCount = queries.length;
       // Array to store the answer for each query
       int[] answers = new int[queryCount];
       // Process each query to find the maximum beauty for the specified price
        for (int i = 0; i < queryCount; ++i) {
           // Use binary search to find the rightmost item with a price not
           // exceeding the query (price we can spend).
            int left = 0, right = items.length;
            while (left < right) {</pre>
                int mid = (left + right) >> 1; // equivalent to (left + right) / 2
                if (items[mid][0] > queries[i]) {
                    // If the mid item's price exceeds the query price, move the right pointer
                    right = mid;
```

// Otherwise, move the left pointer to continue searching to the right

// If there's at least one item that costs less than or equal to the query price

// The answer is the maximum beauty found among all the affordable items

// If no such item is found, the default answer of 0 (for beauty) will remain

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C++
#include <vector>
#include <algorithm>
using namespace std;
class Solution {
public:
    // Function that returns the maximum beauty item that does not exceed the query price
    vector<int> maximumBeauty(vector<vector<int>>& items, vector<int>& queries) {
        // Sort items based on their price in ascending order
        sort(items.begin(), items.end());
       // Preprocess items to keep track of the maximum beauty so far at each price point
        for (int i = 1; i < items.size(); ++i) {</pre>
            items[i][1] = max(items[i - 1][1], items[i][1]);
        int numOfQueries = queries.size();
        vector<int> answers(num0fQueries);
        // Iterate over each query to find the maximum beauty that can be obtained
        for (int i = 0; i < numOfQueries; ++i) {</pre>
            int left = 0, right = items.size();
            // Perform a binary search to find the rightmost item with price less than or equal to the query price
            while (left < right) {</pre>
                int mid = (left + right) / 2;
```

// Item is too expensive, reduce the search range

// If search ended with left pointing to an item, take the beauty value of the item to the left of it

// If left is 0, then all items are too expensive, thus the answer for this query is 0 by default

// because the binary search gives us the first item with a price higher than the query

// Item is affordable, potentially look for more expensive items

```
// Import necessary functions from 'lodash' for sorting and binary search
import _ from 'lodash';
// Function that returns the maximum beauty item that does not exceed the query price
function maximumBeauty(items: number[][], queries: number[]): number[] {
    // Sort items based on their price in ascending order
    items.sort((a, b) => a[0] - b[0]);
    // Preprocess items to keep track of the maximum beauty so far at each price point
    for (let i = 1; i < items.length; ++i) {</pre>
        items[i][1] = Math.max(items[i - 1][1], items[i][1]);
    let numOfQueries = queries.length;
    let answers = new Array(numOfQueries).fill(0);
    // Iterate over each query to find the maximum beauty that can be obtained
    for (let i = 0; i < numOfQueries; ++i) {</pre>
        let left = 0, right = items.length;
       // Perform a binary search to find the rightmost item with price less than or equal to the query price
       while (left < right) {</pre>
```

// Item is too expensive, reduce the search range

left = mid + 1; // Item is affordable, potentially look for more expensive items

// If search ended with left pointing to an item, take the beauty value of the item to the left of it

// If left is 0, then all items are too expensive, thus the answer for this query is 0 by default

// because the binary search gives us the first item with a price higher than the query

```
from bisect import bisect_right
class Solution:
   def maximumBeauty(self, items: List[List[int]], queries: List[int]) -> List[int]:
       # Sort the items by price first (since the first item of each sub-list is price)
        items.sort()
       # Extract a list of prices for binary search
       prices = [price for price, _ in items]
```

# Update the max\_beauty list with the maximum beauty seen up to current index

# Create a list to store the maximum beauty encountered so far

max\_beauty.append(max(max\_beauty[-1], items[index][1]))

# Process each query to find the maximum beauty for that price

# Initialize the answer list for the queries with zeroes

max\_beauty = [items[0][1]] # initialize with the first item's beauty

# Find the rightmost item that is not greater than the query price

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if index:
              answers[i] = max_beauty[index - 1]
       # Return the list of answers to the queries
       return answers
Time and Space Complexity
Time Complexity
```

# If we found an item, store the corresponding max beauty (if not, zero stays by default)

## Creating the prices list: This involves iterating over the sorted items list to build a new list of prices, which will take O(n).

log(n)), where n is the number of items.

Creating the mx list: A single for-loop is used to construct the mx list. This also runs in O(n) time as it iterates over n items once.

The time complexity of the provided code can be broken down into the following parts:

Answering the queries by binary search: Each query performs a binary search to find the right index in the prices list, which

takes O(log(n)). Since this is done for q queries, the total time complexity for this step is O(q \* log(n)).

Combining these steps, the overall time complexity is 0(n \* log(n) + n + n + q \* log(n)), which simplifies to 0(n \* log(n) + n + n + q \* log(n))q \* log(n)) because the linear terms are overshadowed by the n \* log(n) term when n is large.

Sorting the items list: The items.sort() method is called on the list of items, which typically has a time complexity of O(n \*

**Space Complexity** 

The space complexity of the code can be analyzed by considering the additional data structures used:

- The prices list: This consumes O(n) space.
- The mx list: This also consumes O(n) space. **The ans list**: Space needed is O(q) for storing the answers for q queries.
- Therefore, the overall space complexity is 0(n + n + q) which simplifies to 0(n + q) as we add the space required for the two lists related to items and the space for the answers to the queries.