2709. Greatest Common Divisor Traversal

Description

You are given a **0-indexed** integer array nums, and you are allowed to **traverse** between its indices. You can traverse between index i and index j, if and only if <code>gcd(nums[i], nums[j]) > 1</code>, where <code>gcd</code> is the **greatest common divisor**.

Your task is to determine if for **every pair** of indices [i] and [j] in nums, where [i < j], there exists a **sequence of traversals** that can take us from [i] to [j].

Return true if it is possible to traverse between all such pairs of indices, or false otherwise.

Example 1:

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Input: nums = [2,3,6]
Output: true
Explanation: In this example, there are 3 possible pairs of indices: (0, 1), (0, 2), and (1, 2).
To go from index 0 to index 1, we can use the sequence of traversals 0 -> 2 -> 1, where we move from index 0 to index 2 because gcd(nums[0], nums[2]) = gcd(2, 6) = 2 > 1, and then move from index 2 to index 1 because gcd(nums[2], nums[1]) = gcd(6, 3) = 3 > 1.
To go from index 0 to index 2, we can just go directly because gcd(nums[0], nums[2]) = gcd(2, 6) = 2 > 1. Likewise, to go from index 1 to index 2, we can just go directly because gcd(nums[1], nums[2]) = gcd(3, 6) = 3 > 1.
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Example 2:

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Input: nums = [3,9,5]
Output: false
Explanation: No sequence of traversals can take us from index 0 to index 2 in this example. So, we return false.
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Example 3:

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Input: nums = [4,3,12,8]
Output: true
Explanation: There are 6 possible pairs of indices to traverse between: (0, 1), (0, 2), (0, 3), (1, 2), (1, 3), and (2, 3). A valid sequence of traversals exists for each pair, so we return true.
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Constraints:

- 1 <= nums.length <= 10 ⁵
- $1 \leftarrow nums[i] \leftarrow 10^5$