2749. Minimum Operations to Make the Integer Zero



Problem Description

The problem presents a mathematical challenge where you have two integers, num1 and num2. You are tasked with finding the minimum number of operations required to reduce num1 to 0. In each operation, you can choose an integer i in the range [0, 60], and then subtract 2^i + num2 from num1. The operation is a two-step process: first, you choose a power of 2 (2 raised to the power i), and then you add num2 to this value before subtracting this sum from num1.

Leetcode Link

return the minimum number of these operations required to achieve the goal.

If, after a series of such operations, it is not possible to make num1 equal to 0, the function should return -1. Otherwise, it should

Intuition

The intuition behind the solution is to iteratively attempt to perform the operation described, starting with the smallest non-negative

the next multiple. This is feasible because larger values of i in the 2^i term allow for larger subtractions, potentially reaching 0 in fewer steps if carefully picked. The stopping condition for the loop is when x, which is num1 - k * num2, becomes negative, which means we've subtracted too much and it's impossible to reach exactly 0 with the current k.

multiples of num2 (expressed as k * num2) and subtracting this from num1. This is done in a loop, each time incrementing k to check

We also have a condition that x.bit_count() must be less than or equal to k. The bit_count() function returns the number of 1-bits in x. This condition ensures that we have enough operations left to eliminate all 1-bits of x (because each operation can potentially

remove one 1-bit by choosing the correct power of 2) and that k is large enough to handle its binary representation in terms of

operations. Moreover, k should be less than or equal to x, since we want to ensure we can make subtraction at least k more times; otherwise, we won't have enough operations to make num1 zero with the current multiple of num2. If we do not find such a k at the end of the loop, the function returns -1, indicating it's impossible to reduce num1 to 0 given the

conditions.

The solution approach uses a simple brute force method that takes advantage of the properties of powers of two and bit

1. Importing the necessary module: The solution begins by importing the count function from the itertools module, which provides a simple iterator that generates consecutive integers starting with the parameter supplied to it.

operations:

manipulation:

Solution Approach

2. The use of a bit count: Since every number can be represented in binary form, the bit count (x.bit_count()) is crucial for determining the number of 1-bits that we can potentially eliminate through the operations. This is because each operation has

the potential to eliminate a 1-bit if the correct power of 2 is chosen.

- 3. Looping over multiples of num2: The for loop runs indefinitely, increasing k with each iteration. k represents the multiple of num2 that is going to be subtracted along with the power of 2 from num1. The loop stops if subtracting the multiple makes num1 negative, which would indicate that it is impossible to reach 0 with the current value of k.
- 4. Calculating x: Within the loop, x is calculated by subtracting k * num2 from num1. x therefore represents the resulting number after one or more operations have been performed. 5. Checking conditions for a valid operation: Two conditions are checked to see if the current k would result in a viable number of
- ∘ k <= x: This ensures that k is not greater than x, which would mean there aren't enough remaining numbers to subtract from and thus it would be impossible to reach 0 with the current k.

6. Returning the result: If a valid k is found that satisfies both conditions, that k is returned as it represents the minimum number of

operations needed to make num1 equal to 0. If the loop finishes without finding such a k, the function returns -1 to indicate it's

This method does not require complex data structures or algorithms beyond the bitwise operations and basic control structures,

impossible to make num1 zero with the given num2.

x.bit_count() <= k: Ensure that there are enough operations to flip each 1-bit to 0 in x.
</p>

leveraging the inherent mathematical relationships within the problem's constraints.

the minimum number of operations to reduce num1 to 0 by subtracting 2^i + num2 from num1.

1. We start with k = 0. We calculate x = num1 - k * num2. At this moment, x = 42 - 0 * 3 = 42.

We don't proceed with this k since the first condition fails.

Example Walkthrough Let's walk through a small example to illustrate the solution approach. Suppose we have num1 = 42 and num2 = 3. We want to find

• Start by importing count from the itertools module if it's in Python, or if it's just a conceptual step, we set k initially to 0 and iterate over increasing values of k. • The operation we perform in each step is essentially choosing an i such that 2^i + num2 is a valid term to subtract from num1 to

Now let's run through the approach:

Conditions to check:

2. Increment k to 1. Now, x = 42 - 1 * 3 = 39.

get closer to 0.

x.bit_count() <= k? (Does 42 have less than or equal to 0 bits set to 1? No, it has more.)</p> k <= x? (Is 0 less than or equal to 42? Yes, it is.)</p>

Both conditions pass, so it is possible to reduce 36 to 0 in 2 operations by choosing the right powers of 2.

both conditions until we either find a valid k or determine that it's impossible to reach zero. If impossible, the function would return

We don't proceed with this k since the first condition fails. 3. Increment k to 2. Now x = 42 - 2 * 3 = 36.

from itertools import count

for k in count(1):

if difference < 0:</pre>

break

class Solution:

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Conditions to check:

Conditions to check: x.bit_count() <= k? (Does 36 have less than or equal to 2 bits set to 1? No, it has 2).</p>

x.bit_count() <= k? (Does 39 have less than or equal to 1 bits set to 1? No, it has more).</p>

At this point, our example concludes that the minimum number of operations required to reduce num1 to 0 is 2, considering the choice of i we make in each step can actually reduce the number down. In reality, this process repeats, incrementing k and checking

def makeTheIntegerZero(self, num1: int, num2: int) -> int:

Start an infinite loop incrementing k starting from 1

* @param num1 the initial number we're trying to make zero

public int makeTheIntegerZero(int num1, int num2) {

long result = num1 - k * num2;

for (long k = 1; ; ++k) {

if (result < 0) {

return (int) k;

if (difference < 0) {</pre>

break;

return k;

function countSetBits(num: number): number {

break;

* @param num2 the number we subtract from num1, multiplied by k

if (Long.bitCount(result) <= k && k <= result) {</pre>

// We start with k = 1 and check for every increasing k value

Calculate the difference between num1 and k times num2

If the difference becomes negative, we break out of the loop

-1. However, in our example, we succeeded with k = 2.

difference = num1 - k * num2

k <= x? (Is 2 less than or equal to 36? Yes, it is.)</p>

k <= x? (Is 1 less than or equal to 39? Yes, it is.)</p>

Python Solution

13 # Check if the number of set bits (1-bits) in 'difference' is less than or equal to 'k' 14 # and if 'k' is less than or equal to 'difference' 15 if difference.bit_count() <= k <= difference:</pre> 16 # If the condition is satisfied, we return 'k' as the result 17 return k 18 20 # If no valid 'k' is found, return -1 indicating the operation is not possible 21 return -1

* Returns the smallest positive k such that the number of 1-bits in num1 – k * num2 is less than or equal to k,

* and k is less than or equal to num1 - k * num2; otherwise, returns -1 if no such k exists.

// If the result is negative, no further positive k can satisfy the problem's condition

* @return the smallest k that satisfies the condition or -1 if no such k exists

// Calculate the new number after subtracting k times num2 from num1

// If the condition is true, return the current value of k

// Check if the number of set bits (1s) in the binary representation

if (__builtin_popcountll(difference) <= k && k <= difference) {</pre>

// If the loop ends without returning, no valid k was found; return -1.

// Method to count the number of set bits (1-bits) in the binary representation of a number.

count += num & 1; // Increment count if the least significant bit is 1.

num >>>= 1; // Right shift num by 1 bit, using zero-fill right shift.

// If the condition is met, return k as the answer.

// of the difference is \leq k, and k is less than or equal to the difference.

Java Solution class Solution {

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           // If the loop completes without returning, then no valid k was found; return -1
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           return -1;
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31 }
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C++ Solution
   #include <bitset>
   class Solution {
   public:
       // Method to find the smallest positive integer k such that:
       // 1. num1 - k * num2 is non-negative.
       // 2. The number of set bits (1-bits) in the binary representation
             of num1 - k * num2 is less than or equal to k.
       // 3. k is less than or equal to num1 - k * num2.
       int makeTheIntegerZero(int num1, int num2) {
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           // Using 'long long' for larger range, ensuring the variables can handle
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           // the case when num1 and num2 are large values.
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           // 'll' is an alias to 'long long' for convenience.
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           using ll = long long;
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           // Start with k = 1 and increase it until a valid k is found or
           // the break condition is reached when num1 - k * num2 < 0.
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           for (ll k = 1;; ++k) {
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               // Calculate the difference between num1 and k * num2.
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               ll difference = num1 - k * num2;
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               // If the difference is negative, break the loop as the
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               // desired conditions cannot be met.
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// Check if the number of 1-bits in result is less than or equal to k AND if k is less than or equal to result

Typescript Solution

let count = 0;

while (num > 0) {

return -1;

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return count;
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11 // Method to find the smallest positive integer k such that:
12 // 1. num1 - k * num2 is non-negative.
13 // 2. The number of set bits (1-bits) in the binary representation of num1 - k * num2 is less than or equal to k.
14 // 3. k is less than or equal to num1 - k * num2.
   function makeTheIntegerZero(num1: number, num2: number): number {
       // Iterate over possible values of k starting from 1 to find the valid k.
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       for (let k = 1; ; ++k) {
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           // Calculate the difference between num1 and k times num2.
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           let difference = num1 - k * num2;
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           // If the difference becomes negative, break the loop since we are not going to find a valid k this way.
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           if (difference < 0) {</pre>
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               break;
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           // Check if the number of set bits in the binary representation of the difference is <= k and k is <= difference.
           if (countSetBits(difference) <= k && k <= difference) {</pre>
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               // If the condition is met, return k as the valid result.
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       // If no valid k is found, return -1 indicating failure to meet the criteria.
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       return -1;
Time and Space Complexity
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Time Complexity

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> The function loops over k, incrementing it by one each time. • The loop runs until x = num1 - k * num2 becomes negative, which happens after approximately num1 / num2 iterations.

Here's why:

num2).

This is because:

operations. None of these operations have a complexity greater than O(1). Since these constant time operations are inside a loop that runs num1 / num2 times, the overall time complexity is 0(num1 /

The time complexity of the provided function is 0(num1 / num2).

Space Complexity

Each iteration includes calculation of x, checking if x is smaller than zero, calculation of x.bit_count(), and comparison

• There are a finite, small number of variables being used (k, x), and their size does not scale with the input size num1 or num2.

The space complexity of the function is 0(1).

 No additional data structures are being used to store values that scale with the input size. • Since the space used does not scale with the input size, the space complexity is constant.