

Problem Description

In this problem, we are given an array of integers, nums, and an integer k. Our goal is to minimize the score of nums, defined as the difference between the maximum and minimum elements in the array.

We have the ability to perform an operation on each element of the array. The operation involves choosing an index i and then changing the value of nums[i] by adding an integer x that can range from -k to k (inclusive). We are allowed to use this operation at most once for each index.

The objective is to determine what the minimum achievable score is after applying the operation no more than once to each element of the array, if at all.

Intuition

The intuition behind the solution comes from understanding how the score is calculated—the score is simply the difference between the largest and smallest numbers in the array. If we increase the smaller numbers and/or decrease the larger numbers, we can bring them closer to each other, thus reducing the score.

Since we can only apply the operation once per index, our best strategy is to reduce the maximum possible value by k and to increase the minimum possible value by k. By doing so, we reduce or eliminate the gap between the maximum and minimum values as much as possible.

The solution checks two scenarios:

- 1. If the original maximum value minus the minimum value is less than or equal to 2 * k, then we can fully bridge the gap, making the score zero.
- 2. If the gap is larger than 2 * k, we do our best by reducing the gap by 2 * k (subtracting k from the maximum value and adding k to the minimum value) and the remaining difference is the minimal score possible.

Therefore, the formula max(0, mx - mi - k * 2) is used, where mx and mi are the maximum and minimum values in the array, respectively. We use max(0, ...) because the score cannot be negative—if the max-min difference is less than or equal to double of k, bridging the gap completely, the score would be zero.

Solution Approach

The solution to this problem is quite straightforward, without involving complex algorithms or data structures. It follows a direct mathematical approach that efficiently arrives at the result.

1. Find Maximum and Minimum Values: We start by finding the maximum (mx) and minimum (m1) values in the array nums. This can

Here's a breakdown of the solution implementation:

- be done efficiently in a linear pass over the array.

 1 mx, mi = max(nums), min(nums)
- 2. Calculate Adjusted Range: We then calculate what the new range (difference between maximum and minimum) would be if we
- 1 adjusted_range = mx mi k * 2

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3. Determine the Minimum Score: Finally, we evaluate the minimum score, which would be the adjusted range if it's positive, or 0 if the adjusted range is negative (which means the entire range has been neutralized by the operation).
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1 minimum_score = max(0, adjusted_range)

The use of max(0, ...) ensures that our final score is not negative, adhering to the definition that the score is the difference

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between two values (which is inherently non-negative).
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were to reduce the maximum value by k and increase the minimum value by k.

4. Return the Result: The calculated minimum_score is returned as the final result.

This approach uses constant extra space and has a time complexity of O(N) due to the need to iterate over the array to find the

minimum and maximum values. No additional patterns or complex operations are needed, making this an efficient and clean solution.

1 Final Management and Minimum

Example Walkthrough

1. Find Maximum and Minimum Values:

Let's take an array [1, 3, 6] as a small example to illustrate the solution approach, with k = 3.

- Maximum value mx in the array is 6.
 - Minimum value mi in the array is 1.
- We can reduce the maximum value (mx) by k (6 3 = 3) and increase the minimum value (mi) by k (1 + 3 = 4).

2. Calculate Adjusted Range:

- The new adjusted range would be the new maximum value (3) minus the new minimum value (4), which is 3 4 = -1. • However, since we cannot have a negative score, we consider the adjusted range as 0.
- 3. Determine the Minimum Score:
- The minimum score is the maximum between 0 and the adjusted range.
 Since in our example the adjusted range is -1, we use 0 because the score can't be negative.
 - Therefore, the minimum score is 0.

// This ensures that they will be replaced by actual array values.

int maxNum = nums[0]; // Initially set maxNum to the first element.

int minNum = nums[0]; // Initially set minNum to the first element.

// This function finds the smallest possible range after adding/subtracting

// The operation allows for increasing and decreasing each element by up to k.

// then we calculate the difference between the maximum and minimum of that range

// The goal is to find the smallest possible range [minValue+k, maxValue-k]

// a value k to each element in the array

int smallestRangeI(vector<int>& nums, int k) {

- 4. Return the Result:
 - \circ With the given nums array [1, 3, 6] and k = 3, the minimum achievable score after applying the operations is 0.
- overlapping, and the minimum score becomes zero, which is the best-case scenario.

Python Solution

1 # Import the typing module to use the List type hint

In this case, we can conclude that after applying +k to the minimum value and -k to the maximum value, the adjusted values end up

4 class Solution: 5 def smallestRangeI(self, nums: List[int], k: int) -> int: 6 # Find the maximum and minimum values in the list of numbers 7 max_num, min_num = max(nums), min(nums)

2 from typing import List

```
9
           # Calculate the possible smallest range after performing the operation
           # described in the problem statement, which reduces the difference
10
           # between the maximum and minimum numbers by 2*k (k from the max and
11
12
           # k from the min). If the difference is already less than 2*k,
13
           # the smallest range can be brought down to 0.
14
           smallest_range = max(0, max_num - min_num - 2 * k)
15
16
           # Return the calculated smallest range
           return smallest_range
17
18
Java Solution
1 class Solution {
       public int smallestRangeI(int[] nums, int k) {
           // Initialize maximum and minimum values to be the opposite of their extremes.
```

```
// Iterate through the array to find the maximum and minimum values.
           for (int value : nums) {
               maxNum = Math.max(maxNum, value); // Update maxNum if current value is greater.
10
               minNum = Math.min(minNum, value); // Update minNum if current value is smaller.
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12
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           // Calculate the maximum achievable difference by subtracting the range extension
15
           // from the actual range. Ensure the result is not negative.
16
           // The range extension is 'k' from both sides of the range, hence 'k * 2'.
17
           int maxDiff = Math.max(0, maxNum - minNum - k * 2);
18
19
           // Return the smallest possible range after the operations.
20
           return maxDiff;
21
23
C++ Solution
   #include <vector>
   #include <algorithm> // For std::max_element and std::min_element
```

// Find the maximum value in the array using std::max_element int maxVal = *std::max_element(nums.begin(), nums.end()); // Find the minimum value in the array using std::min_element // Find the minimum value in the array using std::min_element

class Solution {

public:

```
int minVal = *std::min_element(nums.begin(), nums.end());
13
14
           // Calculate the adjusted range after adding/subtracting k
16
           // The range cannot be negative, hence the use of std::max with 0
17
           return std::max(0, maxVal - minVal - 2 * k);
18
19 };
20
Typescript Solution
   function smallestRangeI(nums: number[], k: number): number {
       // Find the maximum value in the array using reduce method.
       const maxValue = nums.reduce((currentMax, value) => Math.max(currentMax, value), -Infinity);
       // Find the minimum value in the array using reduce method.
       const minValue = nums.reduce((currentMin, value) => Math.min(currentMin, value), Infinity);
       // Calculate the adjusted range after the operation, ensuring it can't be less than 0.
```

// if it is less than 0, we return 0 as the range cannot be negative. return Math.max(maxValue - minValue - k * 2, 0); // if it is less than 0, we return 0 as the range cannot be negative. return Math.max(maxValue - minValue - k * 2, 0); }

Time and Space Complexity

Time Complexity

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The time complexity of the code is O(N), where N is the number of elements in the given nums list. This is because the function uses the max and min functions which each need to iterate over all elements of the list once to determine the maximum and minimum values, respectively.

values, respectively.

Space Complexity

The space complexity of the code is 0(1) as the memory usage is constant and does not depend on the input size N. Only a fixed

number of variables (mx, mi, and the return value) are used, which occupy a constant amount of space.