2786. Visit Array Positions to Maximize Score

• You can move from your current position i to any position j such that i < j.

• When you visit position i, you earn nums[i] points added to your score.

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Medium
               Dynamic Programming
        Array
```

You are provided with an int array nums that is 0-indexed and a positive int x. The goal is to calculate the maximum total score you can obtain starting at position 0 of the array and moving to any subsequent position. The rules are outlined as follows:

**Problem Description** 

your score. You kick off with nums [0] points, and you have to figure out the maximum score that can be achieved under these conditions.

• If you move between positions i and j and nums[i] and nums[j] have different parities (one is odd, the other is even), you lose x points from

Intuition

## The task is to maximize the score while taking into account that moving between numbers of different parity comes with a

the current number. Here's an outline of the approach: • Initialize a list f with two elements, set to negative infinity [-inf, -inf]. This list will keep track of the max scores for even and odd indices.

penalty of x points. To do this, we need to use dynamic programming to track the highest scores while considering the parity of

- Set the element of f corresponding to the parity of nums [0] (even or odd) to nums [0]. This represents the score starting at position 0. • Iterate through the nums array starting from index 1. For each value v at index i:
- ∘ Calculate the maximum score when staying on the same parity (f[v & 1] + v) and when changing parity (f[v & 1 ^ 1] + v x). Update f[v & 1] with the highest score from the above step.
- After processing all elements, the maximum score will be the maximum element from f. The key intuition in this solution comes from recognizing that at any index i in the array, you have two scenarios to consider:
- 1. The last score came from an index with the same parity as i. In this case, you just add the current value to the previous score since no penalty is incurred.
  - This process will lead us to the highest possible score, taking into account the penalty for switching parities.

2. The last score came from an index with different parity. Here, you add the current value to the previous score from the opposite parity and

Solution Approach The implementation uses a dynamic programming approach to compute the maximum score. Here's a step-by-step walkthrough:

Firstly, the algorithm initializes a list f with two elements, [-inf, -inf]. This record is to keep track of the two possible states for our score related to parity: even (0) and odd (1). In Python, -inf denotes negative infinity which is a useful placeholder for

## "not yet computed or improbably low score." The first element of nums is factored into our initial state. Since we always start at position 0, f [nums [0] & 1] is set to nums [0].

for v in nums[1:]:

subtract the penalty x.

The algorithm then iterates through elements in nums starting from index 1. For each value v, it computes the two possible scenarios: Staying on the same parity (f[v & 1] + v),

The expression nums [0] & 1 will be 0 if nums [0] is even, and 1 if it is odd, so it determines the index of f that gets updated.

The update for the score at parity v & 1 chooses whichever of these two possibilities gives a higher score. This is done by the max function.

After evaluating all elements in nums, the maximum score is the highest value in f, which can be obtained using Python's built-

∘ Switching parity (f[v & 1 ^ 1] + v - x). The ^ operator is a bitwise XOR, which flips the bit, effectively getting us the other parity.

- in max(f) function. The code snippet provided succinctly translates this approach into a Python function as part of a Solution class:
- class Solution: def maxScore(self, nums: List[int], x: int) -> int: f = [-inf] \* 2f[nums[0] & 1] = nums[0]
  - return max(f) Each iteration effectively represents a choice at every position i with a value v from nums: taking its score as part of the existing

parity sequence or starting a new sequence of the opposite parity with an x penalty. The algorithm dynamically keeps track of

the best choice by updating only the score of the relevant parity after each decision. This pattern avoids the need for recursive

We initiate the variable f with two elements [-inf, -inf] to keep track of the max scores for the even (f[0]) and odd indices

• If we stay with odd, f[1] would become 5 (since -inf + 5 is just 5), but there's a catch: we start from an even index so we must apply the

The entire process demonstrates the dynamic programming algorithm's effectiveness in computing the maximum score by

considering the penalty for switching between even and odd numbers. Each decision is based on whether to continue the

sequence of the current parity or start a new one of the opposite parity with a penalty. The algorithm avoids the need to check

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traversal through all potential positions and parities, significantly reducing the complexity of the problem.
Example Walkthrough
  Let's illustrate the solution approach with a small example:
  Suppose we have the array nums = [4, 5, 2, 7, 3] and the penalty x = 3.
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 $f[v \& 1] = max(f[v \& 1] + v, f[v \& 1 ^ 1] + v - x)$ 

We move to nums[1] = 5, which is odd:

penalty x. The new score would be 5 - 3 = 2.

• Staying with even parity, f[0] + 2 = 4 + 2 = 6.

• f = [4, -inf]

• f = [4, 9]

• f = [8, 9]

• f = [8, 16]

• f = [-inf, -inf]

(f[1]).

Next, nums [2] = 2, which is even:

• Switching to odd, f[1] + 2 - x = 9 + 2 - 3 = 8. The higher score is 8, so f[0] becomes 8.

• Switching to even, f[0] + 3 - x = 8 + 3 - 3 = 8. The max is 19, so f[1] remains 19.

Starting at position 0, nums[0] = 4, which is even, so we update f[0] with the value of nums[0].

With nums[3] = 7, which is odd: • Staying odd, f[1] + 7 = 9 + 7 = 16. • Switching to even, f[0] + 7 - x = 8 + 7 - 3 = 12. We take the max which is 16 and update f[1].

• If we switch to even, f[0] + nums[1] would be 4 + 5 = 9. We take the max of both, which is 9, so we update f[1].

• f = [8, 19]The maximum score we can get is max(f), which is 19.

Solution Implementation

from typing import List

def maxScore(self, nums: List[int], x: int) -> int:

# and assigned as the initial score for that parity

# Return the maximum score between the even and odd parities

// Iterate over the array, starting from the second element.

max\_scores = [-math.inf, -math.inf]

max\_scores[nums[0] % 2] = nums[0]

// Method to calculate the maximum score.

public long maxScore(int[] nums, int x) {

long[] maxScoreForOddEven = new long[2];

Arrays.fill(maxScoreForOddEven, -(1L << 60));

// numParity is 0 for even and 1 for odd.

maxScoreForOddEven[numParity] = Math.max(

// Return the maximum score among the two parities.

maxScoreForOddEven[numParity] + nums[i],

maxScoreForOddEven[numParity ^ 1] + nums[i] - x

return Math.max(maxScoreForOddEven[0], maxScoreForOddEven[1]);

maxScoreForOddEven[nums[0] & 1] = nums[0];

for (int i = 1; i < nums.length; ++i) {</pre>

int numParity = nums[i] & 1;

return max(max\_scores)

**Python** 

import math

Java

class Solution {

class Solution:

Lastly, nums [4] = 3, which is odd:

• Staying odd, f[1] + 3 = 16 + 3 = 19.

each path separately, instead of using a running tally that gets updated in each step, which is considerably more efficient.

# Initialize a list with two elements representing negative infinity

# The first number's score is determined based on its parity (even/odd)

# The list is used to track the maximum scores for even and odd numbers separately

// Array f to store the current maximum score for odd and even indexed numbers.

// Initialize both entries with a very small number to simulate negative infinity.

// The first number decides the initial maximum score for its parity (odd or even).

// Update the maximum score for the current parity (odd or even).

# Iterate over the remaining numbers starting from the second element for value in nums[1:]: # Determine the parity of the current number, 0 if even, 1 if odd parity = value % 2 # Update the score for the current parity # max() is choosing the greater value between continuing the same parity # or switching parity and applying the penalty/subtraction of x max\_scores[parity] = max(max\_scores[parity] + value, max\_scores[parity ^ 1] + value - x)

**TypeScript** 

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C++
#include <vector>
#include <algorithm> // For max() function
using namespace std;
class Solution {
public:
    long long maxScore(vector<int>& nums, int x) {
       // Define an infinite value for long long type
       const long long INF = 1LL << 60;</pre>
       // Create a vector to track the maximum scores for even and odd indices
       vector<long long> maxScores(2, -INF); // Initialized with -INF
       // Initialize the first element of the score according to whether it's even or odd
       maxScores[nums[0] & 1] = nums[0];
       // Calculate the number of elements
        int n = nums.size();
       // Loop over the elements starting from the second element
        for (int i = 1; i < n; ++i) {
           // Update the max score for the current parity (even/odd index) of the number
           // This is the maximum of either adding the current number to the existing
            // score of the same parity, or switching parity and subtracting the penalty x
           maxScores[nums[i] \& 1] = max(
               maxScores[nums[i] & 1] + nums[i],  // Same parity: add current number
               maxScores[(nums[i] & 1) ^1] + nums[i] - x // Opposite parity: switch parity and subtract x
       // Return the maximum value of the two max scores
       return max(maxScores[0], maxScores[1]);
};
```

// Initialize an array 'scores' with two elements representing the max scores for even and odd indices.

// The updated score is the max of the current score for the same parity plus the current number,

// Case when adding the current number to the same parity.

// with the penalty x.

// Case when adding the current number leads to change in p

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// Return the maximum score between the even and odd indices.
      return Math.max(scores[0], scores[1]);
from typing import List
import math
class Solution:
```

max\_scores = [-math.inf, -math.inf]

max\_scores[nums[0] % 2] = nums[0]

for value in nums[1:]:

return max(max\_scores)

parity = value % 2

def maxScore(self, nums: List[int], x: int) -> int:

# and assigned as the initial score for that parity

# Update the score for the current parity

for (let i = 1; i < nums.length; ++i) {</pre>

const isOdd = nums[i] & 1;

function maxScore(nums: number[], x: number): number {

const INFINITY = 1 << 30;</pre>

scores[nums[0] &  $\mathbf{1}$ ] = nums[0];

// Define a very large number to represent "infinity".

// Loop through the numbers starting from the second element.

// Update the score for the current parity (even or odd).

// For the first number, update the score based on it being even or odd.

// or the score for the other parity plus the current number minus x.

# Initialize a list with two elements representing negative infinity

# The first number's score is determined based on its parity (even/odd)

# Iterate over the remaining numbers starting from the second element

# Determine the parity of the current number, 0 if even, 1 if odd

# or switching parity and applying the penalty/subtraction of x

# Return the maximum score between the even and odd parities

# max() is choosing the greater value between continuing the same parity

max\_scores[parity] = max(max\_scores[parity] + value, max\_scores[parity ^ 1] + value - x)

# The list is used to track the maximum scores for even and odd numbers separately

scores[is0dd] = Math.max(scores[is0dd] + nums[i], scores[is0dd ^ 1] + nums[i] - x);

const scores: number[] = Array(2).fill(-INFINITY);

```
Time and Space Complexity
  The given Python code snippet aims to calculate a certain "maximum score" by iterating through the input list nums and applying
  some operations based on the elements' parity (odd or even) and a given integer x. To analyze the time and space complexity of
  this code, let's consider n to be the length of the input list nums.
```

## • The for-loop runs (n - 1) times, as it starts from the second element in nums. • Within the loop, a constant number of operations are executed: two bitwise AND operations, four direct accesses by index to the list f, up to two max operations, and a few arithmetic operations.

nums list:

**Time Complexity** 

- Since these operations inside the loop are all of constant time complexity, the overall time complexity of the loop is 0(n 1). Simplifying this, we get:
- 0(n 1) = 0(n).

The time complexity of this code is determined by the number of operations performed in the for-loop that iterates through the

- Thus, the time complexity of the code is O(n). **Space Complexity**
- As for the space complexity: • A new list f of fixed size 2 is created. This does not depend on the size of the input and is thus 0(1). Variable v is a single integer that is used to iterate through nums, which is also 0(1) space.
- Therefore, the space complexity of the code is 0(1). Without a reference answer provided alongside the code, the analysis is based solely on the provided snippet.

There are no other data structures or recursive calls that use additional space that scales with the input size.