1887. Reduction Operations to Make the Array Elements Equal

## **Problem Description**

Sorting

Medium Array

The goal of the given problem is to perform a series of operations on an integer array nums until all the elements in the array are equal. An operation consists of three steps:

1. Find the **largest** value in the array, denoted as largest. If there are multiple elements with the largest value, we select the one with the smallest index i.

- 3. Replace the element at index i with nextLargest.
- The problem asks us to return the number of operations required to make all elements in the array equal.

Intuition

2. Find the **next largest** value that is **strictly smaller** than **largest**, denoted as **nextLargest**.

## To solve this problem, a key insight is that <u>sorting</u> the array will make it easier to track the reductions needed to equalize all elements. After sorting:

The largest element will be at the end of the sorted array, and the next largest will be right before it.
 Subsequent steps involve moving down the sorted array and reducing the largest remaining element to the next largest.
 By maintaining a sorted array, we can avoid repeatedly searching for the largest and next largest elements, thus optimizing the

process.

Here's the process of the solution approach:
First, sort the array in non-decreasing order. This will ensure that each subsequent value from left to right will be greater than or equal to the previous one.

Then, iterate through the sorted array from the second element onwards, comparing the current element with the previous one:
 If they are the same, no operation is needed for this step, but we keep a count of how many times we would have had to reduce other

elements to the current value.

o If the current value is larger, it means an ope

current value.

- If the current value is larger, it means an operation was needed to get from the previous value to this one. We increment the operation count
  (cnt) and add it to the total answer (ans) because we will need that number of operations for each element that needs to be reduced to this
- Each increment of cnt represents a step in which all larger elements need one more operation to reach equality, and by adding cnt to the answer every time, you account for the operations needed to reduce all larger elements to the current one. The final
- answer is the total count of operations needed.

  Solution Approach

arrive at the answer. Here's a breakdown of how the solution is implemented:
 Algorithm: The primary algorithm used here is <u>sorting</u>, which is an integral part of the solution. Python's built-in sorting is typically implemented as Timsort, which is efficient for the given task.

Pattern Used: The approach follows a pattern similar to counting, where for each unique value in the sorted array, we track

A for loop with enumerate is set to iterate through the array (excluding the first element, as there's nothing to compare it to).

Data Structures: The solution primarily works with the list data structure in Python, which is essentially an array.

The given Python solution follows a straightforward approach, leveraging simple algorithms and data structure manipulation to

## how many operations are needed if we want to reduce the larger numbers to this number.

Two variables are maintained:

predecessor (nums[i]):

as the result.

**Example Walkthrough** 

Sort the array:

Initial setup:

Iteration:

Final count:

Solution Implementation

nums.sort()

operations\_count = 0

different\_elements\_count = 0

for i in range(1, len(nums)):

if nums[i] != nums[i - 1]:

# result = solution.reductionOperations([5,1,3])

int operationsCount = 0;

int distinctElementsCount = 0;

for (int i = 1; i < nums.length; ++i) {</pre>

++distinctElementsCount;

function reductionOperations(nums: number[]): number {

for (let i = 1; i < nums.length; ++i) {</pre>

if (nums[i] !== nums[i - 1]) {

countDistinct++;

result += countDistinct;

operations\_count = 0

different\_elements\_count = 0

for i in range(1, len(nums)):

return operations\_count

# Usage example:

**Time Complexity** 

if nums[i] != nums[i - 1]:

different\_elements\_count += 1

# to the next lower number in the list.

operations\_count += different\_elements\_count

# Return the total count of reduction operations required.

nums.sort( $(a, b) \Rightarrow a - b);$ 

let countDistinct = 0;

let result = 0;

// Sort the given array in non-decreasing order.

if (nums[i] != nums[i - 1]) {

different\_elements\_count += 1

# to the next lower number in the list.

# print(result) # Output would be the number of operations required.

// Initialize a variable to count the number of operations needed

// Initialize a variable to count the distinct elements processed

// Iterate over the sorted array, starting from the second element

// Check if the current element is different from the previous one

// Increment the distinct elements count since a new value has been encountered

**Python** 

class Solution:

reduced to the previous smaller value.

current and all previous larger values) is added to ans.

def reductionOperations(self, nums: List[int]) -> int:

ans = cnt = 0 # Initialize counters to zero

ans += cnt # Add to total answer

return ans # Return the total

Let's examine the implementation step by step:

1. The nums list is sorted in non-decreasing order using nums.sort().

cnt: This keeps count of how many different operations are performed. It starts at 0 because no operations are performed at the first element.
 ans: This accumulates the total number of operations.

Inside the loop, each element v at index i (where i starts from 1 since we skipped the first element) is compared to its

If v equals the previous element (nums[i]), it means that no new operation is needed for v to become equal to the

Therefore, we increment cnt by 1 since all occurrences of this new value would require an additional operation to be

After assessing each pair of elements, the value of cnt (which indicates the cumulative operations required to reduce the

Finally, after the loop completes, ans holds the total number of operations required to make all elements equal and is returned

- previous element (as it's already equal).

  o If v is different (meaning it is larger since the array is sorted), then we found a new value that wasn't seen before.
- Here is the critical part of the code with added comments for clarity:

  class Solution:

nums.sort() # [Sorting](/problems/sorting\_summary) the array in non-decreasing order

cnt += 1 # Increment the number of operations needed

enumerated items by one, meaning nums [i] actually refers to the element immediately preceding v.

mechanism properly aggregates the steps needed to reach the desired equal state of the nums array.

for i, v in enumerate(nums[1:]): # Iterate through the array, skipping the first element

if v != nums[i]: # If current element is greater than the previous one (not equal)

Notice that the enumerate function in the loop is used with the sublist nums [1:] which effectively shifts the indices of the

To summarize, the use of sorting simplifies the identification of unique values that require operations, and the counting

Let's walk through a small example using the solution approach described above. Consider the following array of integers:

Sort the `nums` array: nums = [1, 3, 3, 5, 5]

Initialize our counters: cnt = 0 and ans = 0.

```
Nums = [5, 1, 3, 3, 5]

We want to perform operations until all the elements in this array are equal, following the given steps: sort the array, identify the largest and next largest elements, and replace occurrences of the largest element with the next largest until the array is homogenized.

Here is the breakdown of how we apply our algorithm to the example:
```

Start iterating from the second element of nums (since we need to compare each element with its previous one).

Compare the second 3 with the first 3. They are equal, no new operation is needed, cnt stays 1 and ans becomes 2.

• After the loop concludes, ans = 6, which represents the total number of operations needed to make all elements equal.

o Compare 5 with 3.5 is greater, so cnt becomes 2 (indicating each 5 needs two operations to become a 3) and ans becomes 4.

Compare 3 with 1. Since 3 is greater, we found a new value. So, cnt becomes 1 and ans becomes 1.

Compare the second 5 with the first 5. They are equal, so cnt stays 2 and ans becomes 6.

mechanism effectively calculates the necessary steps to achieve uniformity across the array.

# This variable keeps track of the number of different elements encountered.

# Check if the current number is different from the previous one,

# as only unique numbers will contribute to new operations.

# Iterate through the sorted list of numbers, starting from the second element.

# If it's different, increment the count of different elements.

# Add the count of different elements to the total operations count.

# This accounts for the operations required to reduce this number

After sorting the array in non-decreasing order, we can easily identify which elements need to be replaced in each operation.

Through this walkthrough, we find that a total of 6 operations are required to make all elements of the array [5, 1, 3, 3, 5] equal. The sorted form, [1, 3, 3, 5, 5], simplifies the identification of which elements need to be replaced, and our counting

def reductionOperations(self, nums: List[int]) -> int:

# Sort the list of numbers in non-decreasing order.

# Initialize the number of operations required to 0.

operations\_count += different\_elements\_count

# Return the total count of reduction operations required.
return operations\_count

# Usage example:

```
class Solution {
    public int reductionOperations(int[] nums) {
        // Sort the array in non-decreasing order
        Arrays.sort(nums);
```

# solution = Solution()

Java

**}**;

**TypeScript** 

```
// Add the current distinct elements count to the total operations
           // This represents making the current element equal to the previous one
            operationsCount += distinctElementsCount;
       // Return the total count of reduction operations required
       return operationsCount;
C++
// This solution utilizes sorting and then counts the steps required to reduce elements to make all equal.
class Solution {
public:
    int reductionOperations(vector<int>& nums) {
       // Sort the nums vector in non-decreasing order
        sort(nums.begin(), nums.end());
       // Initialize the answer and count variables
       int operations = 0; // Number of operations needed to make all elements equal
        int stepCounter = 0; // Number of steps needed to decrement to the next lower number
       // Iterate through the sorted vector starting from index 1
        for (int i = 1; i < nums.size(); ++i) {</pre>
           // If the current number is different from the one before it,
           // it means a new decrement step is needed.
            if (nums[i] != nums[i - 1]) {
                stepCounter++;
            // Add the number of steps to the total operations
            operations += stepCounter;
       // Return the total number of operations required
       return operations;
```

```
// Return the total number of operations needed to make all elements equal.
return result;
}

class Solution:
    def reductionOperations(self, nums: List[int]) -> int:
        # Sort the list of numbers in non-decreasing order.
        nums.sort()
```

# This variable keeps track of the number of different elements encountered.

# Check if the current number is different from the previous one,

# as only unique numbers will contribute to new operations.

# Iterate through the sorted list of numbers, starting from the second element.

# If it's different, increment the count of different elements.

# Add the count of different elements to the total operations count.

# This accounts for the operations required to reduce this number

# Initialize the number of operations required to 0.

// Initialize a variable `result` to keep the count of operations.

// Iterate through the sorted array, starting from the second element.

// Add the current count of distinct elements to the result.

// Initialize a variable `countDistinct` to track the number of distinct elements encountered.

// If the current element is different from the previous one, increment the distinct count.

// This represents the number of operations needed for each element to reach the previous smaller element.

```
# solution = Solution()
# result = solution.reductionOperations([5,1,3])
# print(result) # Output would be the number of operations required.

Time and Space Complexity
```

## Sorting the array has a time complexity of O(n log n), where n is the length of the nums list. This is because the Timsort algorithm, which is the sorting algorithm used by Python's sort() function, typically has this complexity. The for loop iterates through the array once, which gives a time complexity of O(n) for this part of the code.

Since the sorting operation is likely to dominate the overall time complexity, the final time complexity of the code is  $0(n \log n)$ .

The given code has two main operations: sorting the nums array and iterating through the sorted array to calculate the ans.

- Space Complexity

  The space complexity concerns the amount of extra space or temporary space that an algorithm uses.
- The variables ans and cnt use a constant amount of space, thus contributing 0(1) to the space complexity.
   The enumeration in the for loop does not create a new list but rather an iterator over the sliced list (nums[1:]). The slice operation in Python creates a new list object, so this operation takes 0(n-1) space, which simplifies to 0(n).

The nums.sort() operation sorts the list in-place, which means it does not require additional space proportional to the size of

Therefore, the space complexity of the code is 0(n) due to the list slicing operation.

the input (nums). Thus, this part of the operation has a space complexity of 0(1).