75. Sort Colors

Two Pointers Medium Array Sorting

In this problem, you are given an array nums which contains n elements. Each element represents a color coded as an integer: 0 for red, 1 for white, and 2 for blue. Your task is to sort this array in a way that the colors are grouped together and in the order of red, white, and blue. The sorting has to be done in-place, without using any extra space for another array, and you cannot use the

different types.

Problem Description

library's sort function. Intuition

To solve this problem, the solution approach uses a variant of the famous Dutch National Flag algorithm proposed by Edsger Dijkstra.

The crux of this algorithm is a three-way partitioning technique that segments an array into three parts to sort the elements of three

In this case, we will maintain three pointers:

2. j - All elements from index j onwards are 2s (blues).

1. i - All elements before index i are 0s (reds).

- 3. k Current element that is being inspected.
- Initially, i is set to -1, indicating there are no 0s in the beginning, and j is set to the length of nums, indicating there are no 2s at the

end. The k pointer will start from 0 and move towards j. We iterate through the array with k, and when we find a 0, we increment i and swap the values at i and k. If we find a 2, we

might be 0, so it needs to be rechecked. If the element is 1, it's already in its correct place since we are ensuring all 0s and 2s are moved to their correct places. So, for 1, we just move k forward. We continue this process until k meets j, at which point all elements to the left of i are 0s, elements between i and j are 1s, and all

decrement j and swap the values at k and j but we don't move the pointer k because the new element we swapped from position j

elements from j onwards are 2s, resulting in a sorted array. **Solution Approach**

The solution implements the Dutch National Flag algorithm, which is a partitioning strategy.

Here's a step-by-step explanation using the Reference Solution Approach:

∘ i starts just before the array at -1. This will eventually track the position up to which 0s have been sorted.

o j starts after the end of the array at len(nums). This will eventually track the position from which 2s have been sorted.

1. Initialize three pointers (i, j, and k):

- k starts at 0 and is used to iterate through the array. 2. Perform iterations while k < j:
 - Increment i to move it to the next unsorted position.
- Swap the elements at i and k (nums[i], nums[k] = nums[k], nums[i]), effectively moving the 0 to its correct place.
 - Increment k to move on to the next element.

o If nums [k] == 0, this element needs to be moved to the front.

- Else, if nums[k] == 2, this element needs to be moved to the end.
 - Decrement j to move it towards the first unsorted position from the end. Swap the elements at k and j (nums[j], nums[k] = nums[k], nums[j]), moving the 2 closer to its correct place. Here we
 - Simply increment k to continue to the next element.

don't increment k because the newly swapped element could be 0 or 1 and it has not been evaluated yet.

• If nums [k] == 1, no action is needed as 1s are automatically sorted when 0s and 2s are moved to their correct places.

By following this approach, we continue to partition the array into three parts: 0s before i, 1s between i and j, and 2s after j. The loop continues until k becomes equal to j, meaning all elements have been examined and placed in their correct position. Therefore,

the array is now sorted in-place with red (0), white (1), and blue (2) colors in the correct order without using any additional space or

the library sort function. Example Walkthrough

Here's a step-by-step process of how the algorithm would sort this array:

∘ i is set to -1

1. Initialize the pointers i, j, and k:

Let's say we have an array nums as [2, 0, 1, 2, 1, 0]. We need to sort this array using the Dutch National Flag algorithm so that all

o k is set to 0

0s (reds) come first, followed by 1s (whites), and then 2s (blues).

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2. Start iterating with k while k < j (while k is less than 6):
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Iteration 1: • nums [k] is 2. Since k==0, we need to move this 2 to the end.

j is set to 6 (since the array length is 6)

- We decrement j to 5.
- We don't increment k as we need to evaluate the swapped element. Iteration 2:
- Now nums [k] is 0. This needs to go at the beginning.
 - We increment i to 0.

■ We swap nums [k] with nums [j]. So the array becomes [0, 0, 1, 2, 1, 2].

- We swap nums[i] with nums[k]. The array is still [0, 0, 1, 2, 1, 2] since both nums[i] and nums[k] are 0. ■ We increment k to 1.
- Iteration 3: nums[k] is another 0.
- We increment i to 1. ■ We swap nums[i] with nums[k], but the array remains unchanged [0, 0, 1, 2, 1, 2] as they are the same value.

Iteration 4:

Iteration 6:

or sorting functions.

• nums [k] is 1. This is already in the correct position.

Increment k to 2.

We simply increment k to 3. • Iteration 5:

nums [k] is 2, needs to move to the end.

- We decrement j to 4. ■ We swap nums[k] with nums[j]. Now the array looks like [0, 0, 1, 1, 2, 2].
- nums [k] is now 1. It should stay in place. Increment k to 4. Now k == j, so we stop.

while current_index < next_two_index:</pre>

current_index += 1

next_two_index -= 1

elif nums[current_index] == 2:

// Helper method to swap two elements in an array

private void swap(int[] nums, int i, int j) {

int temp = nums[i];

nums[i] = nums[j];

nums[j] = temp;

Move the 2 to the next position for 2

Python Solution class Solution: def sortColors(self, nums: List[int]) -> None:

 $next_zero_index$, $next_two_index$, $current_index = -1$, len(nums), 0

Process elements until the current_index reaches the next_two_index

Do not increment k as we need to evaluate the swapped element.

if nums[current_index] == 0: # Move the 0 to the next position for 0 10 next_zero_index += 1 nums[next_zero_index], nums[current_index] = nums[current_index], nums[next_zero_index] 11 12 # Move to the next element

Initialize pointers for the next position of 0, the next position of 2, and the current element

nums[next_two_index], nums[current_index] = nums[current_index], nums[next_two_index]

Do not increment current_index because we need to check the newly swapped element

The final sorted array is [0, 0, 1, 1, 2, 2], with all the colors grouped together in the correct order without using any extra space

else: 19 # If the current element is a 1, just move to the next element 20 current_index += 1 21 22 # The function modifies the list in place, so there is no return value

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*/

33 }

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Java Solution
   class Solution {
       // Method to sort the array containing 0s, 1s, and 2s
       public void sortColors(int[] nums) {
           // Initialize pointers for the current element (currIndex),
           // the last position of 0 (lastZeroIndex) and the first position of 2 (firstTwoIndex)
           int lastZeroIndex = -1;
           int firstTwoIndex = nums.length;
           int currIndex = 0;
10
           // Process elements until currIndex reaches firstTwoIndex
11
12
           while (currIndex < firstTwoIndex) {</pre>
               if (nums[currIndex] == 0) {
                   // If the current element is 0, swap it to the position after the last 0 we found
15
                    swap(nums, ++lastZeroIndex, currIndex++);
                } else if (nums[currIndex] == 2) {
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                   // If the current element is 2, swap it with the element at the position
                   // just before the first 2 we found
                    swap(nums, --firstTwoIndex, currIndex);
19
20
               } else {
21
                   // If the current element is 1, just move to the next element
22
                   ++currIndex;
23
24
25
```

public: // This function is used to sort the colors, represented by numbers 0, 1, and 2.

C++ Solution

1 #include <vector>

2 using namespace std;

class Solution {

```
// It uses the Dutch National Flag algorithm to sort in place with O(n) complexity.
       void sortColors(vector<int>& nums) {
           // Initialize pointers:
           // 'left' is the position where the next 0 should go,
10
           // 'right' is the position one more than where the next 2 should go,
11
           // 'current' is the current index being considered.
12
13
           int left = -1, right = nums.size(), current = 0;
           while (current < right) { // Process elements until 'current' reaches 'right'</pre>
               if (nums[current] == 0) {
16
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                   // When a 0 is found, swap it with the element at 'left' position,
                   // then move both 'left' and 'current' one step right.
                    swap(nums[++left], nums[current++]);
19
                } else if (nums[current] == 2) {
20
                   // When a 2 is found, swap it with the element just before 'right' position,
21
                   // then decrement 'right' to move it leftward.
22
23
                   // Note 'current' is not incremented because the swapped element needs to be checked.
                   swap(nums[--right], nums[current]);
24
               } else {
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26
                   // If the element is 1, just move 'current' one step to the right.
27
                   ++current;
28
29
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31 };
32
Typescript Solution
 1 /**
    * Sorts an array of numbers in-place, so that all 0s come first,
    * followed by all 1s, and then all 2s. This pattern is known as the Dutch national flag problem.
```

```
function sortColors(nums: number[]): void {
       let zeroIndex = -1; // Initialize the index where 0s will be placed.
       let twoIndex = nums.length; // Initialize the index where 2s will be placed.
       let currentIndex = 0; // The current index we're scanning from the array.
10
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       while (currentIndex < twoIndex) {</pre>
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           if (nums[currentIndex] === 0) {
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               // When the current element is 0, swap it with the element at zeroIndex,
               // then increment zeroIndex and currentIndex.
15
               zeroIndex++;
16
               [nums[zeroIndex], nums[currentIndex]] = [nums[currentIndex], nums[zeroIndex]];
18
               currentIndex++;
           } else if (nums[currentIndex] === 2) {
19
               // When the current element is 2, decrement twoIndex and swap the current element
20
21
               // with the element at twoIndex.
22
               twoIndex--;
               [nums[twoIndex], nums[currentIndex]] = [nums[currentIndex], nums[twoIndex]];
23
               // Do not increment currentIndex here because the element swapped from twoIndex
24
25
               // may be 0, which will need to be moved to zeroIndex in the next iteration.
26
           } else {
27
               // If the element is 1, just move on to the next element.
               currentIndex++;
28
29
30
31 }
32
Time and Space Complexity
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* @param {number[]} nums - The input array containing 0s, 1s, and 2s.

size of the input list.

The increment and decrement operations on i, j, and k, as well as the swaps, all occur in constant time, and the loop runs until k is no longer less than j. The space complexity of the code is 0(1) because the sorting is done in place. No additional storage is needed that scales with the input size n. The only extra space used is for the three pointers i, j, and k, which use a constant amount of space regardless of the

The time complexity of the code is O(n), where n is the length of the input list nums. This is because the while loop iterates through

each element of the list at most once. The variables i, j, and k are used to traverse the array without the need to revisit elements.