

**Problem Description** 

The problem presents us with a task to calculate the bitwise AND for all numbers in the range from 'left' to 'right' inclusive. The 'bitwise AND' operation takes two bit operands and performs the logical AND operation on each pair of corresponding bits. The result is 1 if both bits are 1, and 0 otherwise. This problem thus requires us to perform this operation on a sequence of integers, starting from 'left' up to 'right'.

1. We take two integers, 'left' and 'right'.

Here is a step-by-step understanding of the problem:

- 2. We apply the bitwise AND to every pair of numbers in that range.
- 3. We want to find the cumulative result of the AND operation applied in sequence from 'left' to 'right'.
- To illustrate, if our range is [5, 7], we need to calculate the bitwise AND of 5, 6, and 7.

The binary representation of 6 is 110.

- The binary representation of 7 is 111.

The binary representation of 5 is 101.

The bitwise AND of 5 AND 6 is 100 (in binary), and the bitwise AND of 100 AND 111 is 100, so the result for our example would be 4.

Intuition

## The intuition behind the provided solution leverages the idea that the result of the bitwise AND operation of a range of numbers is

0 within the range, due to the nature of the AND operation (which requires all operands for a particular bit position to be 1 in order to yield a 1), that bit will be 0 in the final outcome. The crucial observation is that if we progressively strip off the lowest bit of the 'right' number until it is less than or equal to 'left', the bits that remain align with the bits of the final AND operation result.

determined by the common bits i.e., the bits that don't change across all numbers in the range. The moment a bit changes from 1 to

Here's why: • If 'left' and 'right' are the same, the bits remain unchanged as there's nothing to compare or operate against, so the bitwise AND

is equal to the 'left' or 'right' value.

- If 'left' is less than 'right', at some point, the least significant bit that differs between 'left' and 'right' will become 0 in 'right' after a certain number of operations because 'right' will be decremented for every bit that is 1 starting from the least significant bit. • Since 'right' is getting smaller with right & (right - 1) and 'left' is constant, eventually 'right' will be less than or equal to 'left' or the
- differing bits at the end of 'right' have been turned off. The remaining bits before the changed bit in 'right' are common with 'left', therefore they remain unchanged and represent the
- By employing this method, we avoid the necessity of iterating through all numbers in the range and directly arrive at the result by focusing only on the bits that won't be altered by the AND operation in the range.

**Solution Approach** 

The provided solution uses a simple while loop and a bitwise operation to iteratively narrow down the range to finally arrive at the

bitwise AND of all numbers within the range [left, right]. Here's a step-by-step explanation of how the solution works:

## 1. The solution approach starts with a condition while left < right: which means that we will keep iterating as long as our right

bitwise AND of all numbers in the range.

any bits to the right of this bit, it sets them to 1.

the range [left, right] become 0.

[left, right].

turns off one set bit.

value is greater than our left value. 2. Inside the loop, the key operation is right &= right - 1. This operation takes the current value of right and performs a bitwise

- AND with the number one less than right (right 1). 3. The expression right - 1 has the effect of flipping the least significant bit (LSB) of right that is set to 1 to 0, and if there are
- while the corresponding bit in right 1 is 0. 5. As a result of this operation, the right value becomes smaller with each iteration, which means we are effectively stripping off

4. The bitwise AND operation &= then turns off the least significant bit that was just flipped in right because the LSB in right is 1,

- the lowest set bit one by one until right is no longer greater than left. 6. This iterative process continues to turn off the variable bits starting from least significant until all the bits that would change in
- off, and the remaining common unchanged bits represent the result of the bitwise AND for the range. 8. The return statement return right gives us the final answer, which by now holds the bitwise AND of all numbers in the range

7. The loop exits when left is the same as or greater than right. At this point, all the differentiating bits of right have been turned

This implementation does not require any additional data structures and thus operates in-place with O(1) space complexity. The time complexity is based on the number of set bits in right, specifically, it is O(log n), where n is the value of right, since each iteration

No extra patterns or algorithms are used here, just bit manipulation to iteratively approach the solution. This approach is very efficient because it avoids the explicit bitwise AND of every two numbers in the range, which can be computationally expensive especially for large ranges.

Let's illustrate the solution approach with a small example where left = 10 and right = 15. In binary, these numbers are represented as: left = 10 = 1010 (in binary)

## 1. We check the condition while left < right: Since 10 < 15, we enter the loop.

1110 (right - 1)

right = 15 = 1111 (in binary)

Following the steps of the provided solution approach:

3. The expression right - 1 affects right by:

Example Walkthrough

2. The key operation of the loop is right &= right - 1. Initially, right is 15, which is 1111 in binary. Then, right - 1 is 14, which is 1110 in binary.

- In the binary form 1110, we see that it's the last digit that changes when subtracting 1 from 1111. 4. Applying the bitwise AND operation: **1111** (right)
- 5. After the first iteration, right is now 14 (1110 in binary). 6. We run the loop again since left (1010 in binary) is still less than right (1110 in binary).

**1110** (result of right & (right - 1))

1100 (result of right & (right - 1))

1011 (right - 1)

**Python Solution** 

while left < right:</pre>

right &= right - 1

right &= (right - 1);

n = n & (n - 1);

return right;

class Solution:

**Java Solution** 

10

11

8

10

11

12

13

14

15

16

17

19

10

11

12

13

14

13

14

15

16

19

18 }

18 }

8. Apply the bitwise AND operation again: 1110 (right) 1101 (right - 1)

Flipping the least significant bit set to 1 to 0 (the rightmost bit in this case).

 $\circ$  right - 1 = 11 = 1011 in binary. • The AND operation: 1100 (right)

**1000** (result of right & (right - 1))

9. right is now 12 (1100 in binary), and we proceed with the loop.

def rangeBitwiseAnd(self, left: int, right: int) -> int:

# Loop until 'left' is not less than 'right'

7. Subtract 1 from right: right -1 = 13 = 1101 in binary.

integers will eventually result in the bits that change within the range being set to 0, leaving the common unchanged bits as the result. In this case, 1000 in binary or 8 in decimal.

# This effectively reduces 'right' each time, moving towards 'left'

# their binary representations which is the answer to the problem.

# This function finds the bitwise AND of all numbers within the inclusive range [left, right]

# At the point where the while loop stops, 'left' and 'right' have the same prefix for

# We use the trick "right &= right - 1" to clear the least significant bit of 'right'

10. Once more, as left (1010 in binary) is still less than right (1100 in binary), we continue.

12 return right 13

// Goal is to remove the least significant bit of 'right' by doing 'right' & (right - 1)

// bits will eventually become zero due to the range of AND operations before we reach 'left'.

// to reduce right. This is because we know if left < right, the least significant

// By the end, 'right' is modified such that it represents the common bits of

// The idea is to remove the rightmost bit of 'n' to make it smaller.

// For example, n = 1010 (10 in decimal), n - 1 = 1001 (9 in decimal),

// Once m and n become equal, all bits to the right of the current bit position

// Return the value of 'right' which at this point equals the bitwise AND of the range

// then n & (n-1) = 1000 (8 in decimal), effectively removing the least significant bit.

// have had differing values within the range [m, n], and therefore result in zero when ANDed.

// The current value of 'n' is the bitwise AND of all numbers between the original 'm' and 'n'.

// This helps move 'n' closer to 'm' without affecting the result of bitwise AND of the range.

// all numbers in the range [left, right], thus the bitwise AND result.

11. right is now 8 (1000 in binary), and left is 10 (1010 in binary). Now, since left is not less than right, the loop ends.

We return right which is 8. This value is indeed the bitwise AND of the range [10, 15] because any sequence of consecutive

12. The last value left in right which stands now at 8 (1000 in binary) is the bitwise AND of all numbers from 10 to 15.

class Solution { // Function to find the bitwise AND of all numbers in the range [left, right] public int rangeBitwiseAnd(int left, int right) { // Keep iterating until the right value is greater than or equal to the left value while (left < right) {</pre>

```
1 class Solution {
2 public:
      int rangeBitwiseAnd(int m, int n) {
          // Loop until m is no longer less than n.
          while (m < n) {
```

C++ Solution

```
15
           return n;
16
17 };
18
Typescript Solution
1 /**
    * Applies a bitwise AND operation to all numbers within a given range.
    * @param {number} left - The starting point of the range (inclusive).
    * @param {number} right - The end point of the range (inclusive).
    * @return {number} - The result of the bitwise AND operation applied sequentially from left to right.
   function rangeBitwiseAnd(left: number, right: number): number {
       // Loop until the 'left' value is greater than or equal to 'right'
       while (left < right) {</pre>
10
11
```

## Time and Space Complexity

right &= right - 1;

return right;

// Apply bitwise AND between 'right' and 'right-1' then store it back in 'right' // This operation removes the least significant bit of 'right'

- The provided code snippet is designed to find the bitwise AND of all numbers between two integers, left and right inclusive. The while loop continues to strip the least significant bit from right until right is no longer greater than left.
  - Python has at most  $log2(max_int)$  bits, the loop runs at most log2(right left + 1) times which simplifies to 0(log(n)).

• Time Complexity: The time complexity of the algorithm is  $O(\log(n))$ , where n is the distance between left and right. In the

worst-case scenario, we will need to iterate through all bits of right until right becomes equal to left. Since an integer in

• Space Complexity: The space complexity of the algorithm is 0(1). This is because the algorithm only uses a constant amount of space, as it only modifies right without allocating any other data structures proportional to the size of the input range.