2917. Find the K-or of an Array

Problem Description

In this problem, we're given an array of integers called nums and an integer k. We need to compute the K-or of nums. The K-or is a special value that is determined by looking at each bit position across all numbers in nums. For each bit position i, if at least k numbers in nums have a 1 in the ith bit position, then the ith bit of the K-or will also be 1. Otherwise, it will be 0. The K-or of nums is the combined result of checking this condition for each bit position from 0 to 31 (since we are dealing with 32-bit integers). This problem is essentially about understanding and manipulating binary representations of integers.

Intuition

Easy

and bitwise OR (|). A bitwise AND between two bits results in 1 if both bits are 1, otherwise it's 0. A bitwise OR between two bits results in 1 if at least one of the bits is 1. To find the K-or of nums, we follow these steps:

To understand the solution, we need to grasp the concept of bitwise operations. Specifically, we will be using bitwise AND (&)

• We initialize our answer variable ans to 0. This will hold the final K-or value.

- We iterate over each bit position i from 0 to 31 (since the problem states that nums is an array of non-negative integers, and non-negative
- integers are represented by 32-bit binary numbers). • For each bit position i, we count how many numbers in nums have the ith bit set to 1. We do this by right-shifting (>>) each number in nums
- by i positions, thus bringing the ith bit to the rightmost position. We then perform a bitwise AND with 1 (which has only the rightmost bit set to 1). This gives us the value of the ith bit. Summing up these values across all numbers in nums gives us the total count of numbers with ith bit set, cnt. • If cnt is greater than or equal to k, then we should have the ith bit of ans set to 1. To achieve this, we use the bitwise OR operation to set the ith bit of ans. We create a value with only the ith bit set (1 << i) and OR it with ans.
- After checking all bit positions, ans will be the K-or of nums, which we return.
- **Solution Approach**

element x in nums and applying $x \gg i \& 1$.

The algorithm employs a for loop to iterate through 32 possible bit positions (from 0 to 31) since we are working with non-

negative integers, which in this case are 32-bit.

 \blacksquare x >> i shifts the bits of x right by i positions, moving the ith bit to the least significant position.

■ If ans does not have the ith bit set and cnt is greater than or equal to k, |= will set that bit to 1.

The implementation of the solution follows a straightforward approach hinging on the concept of bitwise operations.

For each bit position i, the algorithm performs a key operation:

It counts the number of elements in nums (cnt) that have the ith bit set to 1. This is achieved by iterating through each

If the count cnt is greater than or equal to k, this indicates that at least k elements of nums have the ith bit set to 1,

■ The & 1 operation is a bitwise AND which masks all bits other than x's least significant bit; effectively it extracts the value of the ith bit post-shift.

and thus we should set the ith bit in our solution ans.

If ans already has the ith bit set, |= will leave that bit set.

- To set the ith bit in ans, we use the operation ans |=1 << i. 1 << i creates a number with only the ith bit set (2ⁱ), and |= (bitwise OR assignment) combines this with the current ans.
- bits that met the condition (a count of at least k). The algorithm then returns the accumulated result stored in ans as the K-or of nums.

There is no need for any additional data structures for this approach, which keeps the space complexity to O(1) - only counters

and the answer variable. The time complexity is O(N * M), with N being the length of the input list and M being the number of bits

we are checking (in this case, 32). The simplicity comes with the direct counting and bitwise manipulation for each of the bit

By the end of the loop, we have considered all bits from the least significant to the most significant and ans contains all the

positions. The reference to 2^i in the solution approach, wrapping it in "`", makes clear the relationship between shifting bits and

powers of two which is central to understanding bitwise operations in this context. **Example Walkthrough** Let's consider an example where the nums array is [3, 5, 12] and k is set to 2. The problem asks us to find the K-or of nums. First, we examine the binary representations of each number in the array:

• 5 in binary is 0101

• 12 in binary is 1100

3 >> 0 & 1 = 1

o 5 >> 0 & 1 = 1

• 3 in binary is 0011

least k (2 in our example). Let's step through a few iterations of the process for each bit position i from 0 to 31.

○ 12 >> 0 & 1 = 0 The count cnt of numbers with the least significant bit set to 1 is 2, which is equal to k. Thus, we set the least

We need to look through each bit position and count how many numbers have that bit set to 1. Then we'll check if this count is at

For i = 0 (the least significant bit or LSB), we have:

For i = 1 (the second least significant bit), we have:

significant bit of ans to 1. Now, ans = 0001.

from typing import List # Necessary for type hinting

def findKOr(self, nums: List[int], k: int) -> int:

since an integer in Python has 32 bits

count = sum(1 for x in nums if x >> i & 1)

* when compared across all numbers in the given array.

// Initialize the variable to store the answer

* @param k Number representing the minimum count of 1-bits.

for i in range(32):

if count >= k:

* @param nums Array of integers.

public int findKOr(int[] nums, int k) {

for (int i = 0; i < 32; ++i) {

return answer

int answer = 0;

answer |= 1 << i

Initialize the answer to 0. The function will build up

Count number of integers in nums where the ith bit is set

* Finds an integer which has at least k 1-bits in the respective bit positions,

* @return The integer with at least k 1-bits in the corresponding bit positions.

// Iterate through each bit position (0 to 31, assuming 32-bit integers)

// Initialize a counter for the number of 1-bits in the current bit position

If the count is greater than or equal to k, it means at least k numbers

have a bit set at the ith position. Hence, set the ith bit in the answer.

- 3 >> 1 & 1 = 1 o 5 >> 1 & 1 = 0
- 3 >> 2 & 1 = 0 5 >> 2 & 1 = 1

○ 12 >> 1 & 1 = 0 The count cnt is 1, which is less than k. We do not change ans. ans remains 0001.

If we continue this process up to i = 31, we would see that no more bits would meet the condition of having at least k counts. This is because our numbers are quite small and do not have 1s in higher bit positions.

For i = 2, we have:

This is the K-or of nums [3, 5, 12] with k = 2.

class Solution:

Solution Implementation **Python**

○ 12 >> 2 & 1 = 1 The count cnt is 2, equal to k. We set the third least significant bit (2^2 position) of ans. Now, ans = 0101.

After completing this process for all bit positions, we conclude that the final ans equals 0101 in binary, which is 5 in decimal.

the answer by setting bits where appropriate. answer = 0 # Loop through each bit position from 0 to 31 (inclusive)

```
# Return the computed answer where bits are set based on the count of set bits
# at every bit position in the input numbers compared to k.
```

Java

class Solution {

/**

```
int count = 0;
            // Iterate through all numbers in the array
            for (int number : nums) {
                // Shift the number i bits to the right and bitwise AND with 1
                // This extracts the i-th bit and increases the count if it's 1
                count += (number >> i) & 1;
            // If the count is at least k, set the i-th bit of the answer to 1
            if (count >= k) {
                answer |= 1 << i;
        // Return the computed answer with the required bits set to 1
        return answer;
C++
class Solution {
public:
    // Method to find the number where each bit position has appeared at least k times across all numbers in the vector.
    int findKOr(vector<int>& nums, int k) {
        int result = 0; // Initializes the result which will be returned.
        // Iterate through each bit position (0 to 31 for a 32-bit integer).
        for (int i = 0; i < 32; ++i) {
            int count = 0; // Count the number of times the i-th bit is set across all numbers in nums.
            // Iterate through all numbers in the vector.
            for (int num : nums) {
                // If the i-th bit is set in num, increment the count.
                count += (num >> i) & 1;
            // If the i-th bit is set at least k times across all numbers, set this bit in the result.
            if (count >= k)
                result |= (1 << i);
```

// Return the result, where each bit represents it appeared at least k times across all numbers in nums.

// If the count of set bits is greater than or equal to k, set the bit at this position in the answer

};

TypeScript

return result;

function findKOr(nums: number[], k: number): number {

count += (num >> bitPosition) & 1;

answer |= 1 << bitPosition;</pre>

for (const num of nums) {

if (count >= k) {

let answer = 0; // Initialize the answer which will hold the result

for (let bitPosition = 0; bitPosition < 32; ++bitPosition) {</pre>

// Iterate over 32 bits because we're assuming numbers are within 32-bit integer range

// Iterate over the array and count the bits set at the current bit position

let count = 0; // Count the number of times a bit is set at the current position

```
// Return the final calculated answer
    return answer;
from typing import List # Necessary for type hinting
class Solution:
    def findKOr(self, nums: List[int], k: int) -> int:
        # Initialize the answer to 0. The function will build up
        # the answer by setting bits where appropriate.
        answer = 0
        # Loop through each bit position from 0 to 31 (inclusive)
        # since an integer in Python has 32 bits
        for i in range(32):
            # Count number of integers in nums where the ith bit is set
            count = sum(1 \text{ for } x \text{ in nums if } x >> i \& 1)
           # If the count is greater than or equal to k, it means at least k numbers
            # have a bit set at the ith position. Hence, set the ith bit in the answer.
            if count >= k:
                answer |= 1 << i
        # Return the computed answer where bits are set based on the count of set bits
        # at every bit position in the input numbers compared to k.
        return answer
Time and Space Complexity
```

Time Complexity

The time complexity of the given code is 0(n * 32), which simplifies to 0(n) since 32 is a constant. Here, n is the length of the array nums. The time complexity assessment comes from the single loop running 32 times (once for each bit in a 32-bit integer) and the inner computation that performs a bitwise operation and a sum for all n elements in the array nums. This inner computation runs in O(n) time, and since it's nested inside a loop that runs a constant number of times, the overall time complexity remains linear with respect to the number of elements in nums.