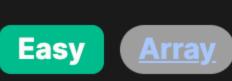
896. Monotonic Array



Problem Description

In this problem, we are given an integer array nums and our task is to determine whether the array is monotonic or not. An array is considered monotonic if it is either monotonically increasing or monotonically decreasing. This means that for each pair of indices i and j where $i \ll j$, the condition $nums[i] \ll nums[j]$ must hold true for the entire array if it's increasing, or $nums[i] \gg nums[j]$ if it's decreasing. The goal is to return true if the array meets either of these conditions for all its elements, and false otherwise.

Intuition

1. Monotone Increasing: To verify this, we need to check if every element at index i is less than or equal to the element at index i+1. This should

To understand if an array is monotonic, we need to check two conditions:

- be true for all consecutive pairs in the array.

 2. Monotone Decreasing: Similarly, we need to check if every element at index i is greater than or equal to the element at index i+1 for all
- consecutive pairs.

 The given Python solution approaches the problem by checking both conditions separately. It uses the pairwise utility which, in

this context, would generate pairs of consecutive elements from the nums array. It is important to note that pairwise is available in the itertools module from Python 3.10 onwards. For versions prior to that, we can manually create pairs using a simple loop or list comprehension.

For the increasing condition, the expression all(a <= b for a, b in pairwise(nums)) returns True if every element a is less

than or equal to the next element b, for all pairs (a, b) in the array. Similarly, the decreasing condition is checked with the expression all(a >= b for a, b in pairwise(nums)).

The solution provided in the Python code relies on a straightforward approach and the efficient use of Python's built-in functions

Solution Approach

to check if the array is monotonic. Let's break down the steps of how the algorithm is implemented:

1. The solution first attempts to determine if the array is monotonically increasing. It does this with the help of a generator expression all(a <= b for a, b in pairwise(nums)). This expression generates a sequence of boolean values for each

than or equal to b, meaning no violation of the increasing condition is found, the all function will return True.

2. Similarly, the solution tries to find out if the array is monotonically decreasing by using the expression all(a >= b for a, b in pairwise(nums)). This also generates a sequence of boolean values where each pair is compared to ensure that a is greater than or equal to b. If this is true for the whole array, the all function returns True.

pairwise comparison between items a and b in the array such that a and b are consecutive elements. If a is always less

As for the pairwise function, it is not explicitly defined within the solution, which implies it must be imported from Python's

The crucial part of the solution is the return incr or decr line of code. What it does is return True if either variable incr or

- itertools module before using the solution. pairwise creates an iterator that returns consecutive pairs of elements from the input iterable. For example, pairwise([1, 2, 3, 4]) would yield (1, 2), (2, 3), and (3, 4). If the pairwise function is unavailable, the same effect can be achieved with zip(nums, nums[1:]).
- decr is True. These two variables hold the outcomes of the monotonic increasing or decreasing checks. In essence, the array is monotonic if it is either entirely non-decreasing or non-increasing.

 By combining these checks, the problem is addressed in a concise manner that effectively determines the monotonicity of the

Example Walkthrough

array with minimal iteration, therefore optimizing the solution's time complexity to O(n), where n is the length of the input array.

。 (3, 3)

o (3, 5)

o (6, 7)

。 (5, 5) 。 (5, 6)

Let's illustrate the solution approach using a small example array nums = [3, 3, 5, 5, 6, 7, 7].

(7, 7)
 Now, we apply the check to see if the array is monotonically increasing. For this example:

First, we create pairs of consecutive elements:

We compare 3 <= 5, which is True.
We compare 5 <= 5, which is True.
We compare 5 <= 6, which is True.
We compare 6 <= 7, which is True.

We compare 3 <= 3, which is True.

We compare 7 <= 7, which is True.

Compare 3 >= 5, which is False.

that the array is monotonically increasing. However, for the sake of understanding, we would check as follows:

• Compare 3 >= 3, which is True.

Since the variable incr holds True (and decr holds False), the final result returned by the function is True.

comparison (though not needed here) would have at least one more False, confirming the array isn't monotonically decreasing.

These pairwise comparisons give us all True outcomes. Therefore, incr = True as all elements satisfy the condition a <= b.

We don't necessarily need to proceed with checking for monotonically decreasing conditions because we have already found

At this point, we already have a False, so we know decr will be False, and there's no need to continue. Every subsequent

In this example, we deduced that nums is monotonically increasing, and therefore, it is a monotonic array. The key takeaway is that the array only needs to fulfill one of the two monotonic conditions (increasing or decreasing), not both.

Solution Implementation

Check if the sequence is monotonically increasing
is increasing = all(a <= b for a. b in pairwise(numbers))
Check if the sequence is monotonically decreasing</pre>

def pairwise(iterable):

def isMonotonic(self. numbers: List[int]) -> bool:

return is_increasing or is_decreasing

" $s \rightarrow (s0,s1), (s1,s2), (s2, s3), \dots$ "

if (!isIncreasing && !isDecreasing) {

// Initialize two boolean flags for increasing and decreasing

// Iterate over the array starting from the second element

// If the sequence has both increasing and decreasing pairs,

return false;

bool isMonotonic(vector<int>& nums) {

for (int i = 1; i < nums.size(); ++i) {</pre>

if (nums[i] < nums[i - 1]) {</pre>

isIncreasing = false;

if (nums[i] > nums[i - 1]) {

isDecreasing = false;

bool isIncreasing = true;

bool isDecreasing = true;

return true;

from itertools import pairwise # Ensure that pairwise is imported from itertools

The sequence is monotonic if it's either increasing or decreasing

Note: If the Python environment is older than 3.10, you'll need this definition of pairwise:

// If the array is neither non-decreasing nor non-increasing, return false

// If we reach this point, the array is either non-decreasing, non-increasing, or all elements are equal

// Function to determine if the array is monotonic (either entirely non-increasing or non-decreasing)

// If the current element is smaller than the previous, it's not increasing

// If the current element is larger than the previous, it's not decreasing

is decreasing = all(a >= b for a, b in pairwise(numbers))

Python

class Solution:

```
a, b = tee(iterable)
      next(b, None)
      return zip(a, b)
Java
class Solution {
    // Function to determine if the array is either entirely non-increasing or non-decreasing
    public boolean isMonotonic(int[] nums) {
        boolean isIncreasing = true; // To keep track if the array is non-decreasing
        boolean isDecreasing = true; // To keep track if the array is non-increasing
        // Iterate over the array starting from the second element
        for (int i = 1; i < nums.length; i++) {</pre>
            if (nums[i] < nums[i - 1]) {
                // If the current number is less than the previous, it's not non-decreasing
                isIncreasing = false;
            if (nums[i] > nums[i - 1]) {
                // If the current number is greater than the previous, it's not non-increasing
                isDecreasing = false;
```

C++

public:

class Solution {

```
// If it's neither increasing nor decreasing, it's not monotonic
            if (!isIncreasing && !isDecreasing) {
                return false;
        // If the array is either increasing or decreasing, then it's monotonic
        return true;
};
TypeScript
 * Determines if an array of numbers is monotonic.
 * An array is monotonic if it is either monotone increasing or monotone decreasing.
 * @param {number[]} nums The array of numbers to check.
 * @returns {boolean} True if the array is monotonic, otherwise false.
function isMonotonic(nums: number[]): boolean {
    const length = nums.length;
    let isIncreasing = false;
    let isDecreasing = false;
    // Traverse the array, starting from the second element
    for (let i = 1; i < length; i++) {
        const previous = nums[i - 1]; // Previous element
        const current = nums[i]; // Current element
        // Check if the current pair is increasing
        if (previous < current) {</pre>
            isIncreasing = true;
        // Check if the current pair is decreasing
        else if (previous > current) {
            isDecreasing = true;
```

```
// the array is monotonic.
return true;
}

from itertools import pairwise # Ensure that pairwise is imported from itertools

class Solution:
    def isMonotonic(self. numbers: List[int]) -> bool:
        # Check if the sequence is monotonically increasing
        is increasing = all(a <= b for a. b in pairwise(numbers))
        # Check if the sequence is monotonically decreasing
        is decreasing = all(a >= b for a, b in pairwise(numbers))
        # The sequence is monotonic if it's either increasing or decreasing
        return is_increasing or is_decreasing

# Note: If the Python environment is older than 3.10, you'll need this definition of pairwise:
```

return zip(a, b)

that scales with the input size.

" $s \rightarrow (s0,s1), (s1,s2), (s2, s3), ...$ "

def pairwise(iterable):

next(b, None)

a, b = tee(iterable)

// it is not monotonic.

return false;

if (isIncreasing && isDecreasing) {

// If the loop completes without returning false,

Time and Space Complexity

The time complexity of the code is O(n) where n is the length of the nums list. This is because the pairwise function is going through the list only once for each check (increasing and decreasing). Each all() call iterates over the list in a pairwise fashion,

which means there will be a total of n-1 comparisons for each call.

The space complexity of the code is 0(1) since the space used does not depend on the size of the input nums list. The pairwise function generates a sequence of tuples which is consumed by the all() function, and this does not require additional space