1171. Remove Zero Sum Consecutive Nodes from Linked List

Leetcode Link

Linked List Medium Hash Table

Problem Description In this problem, we are provided with the head node of a singly linked list, which is a data structure where each node contains a

value and a reference to the next node. Our task is to remove all consecutive sequences of nodes from this linked list that, when their values are added together, sum up to 0.

The challenge lies in the possibility of such sequences being spread across the linked list and not necessarily being adjacent immediately. Furthermore, after removing a sequence that sums to 0, new sequences can form, also leading to a sum of 0, which should be removed as well. This process must be repeated until there are no more sequences with a sum of 0 remaining.

If we remove these nodes, the linked list becomes 1 -> 1. The requirement is to keep removing such sequences until no such

sequence exists, and in this case, we would finally end up with an empty linked list as 1 -> 1 also sums up to 0. Intuition

To solve this problem, we use a two-pass approach leveraging the concept of a prefix sum and a hash table. The prefix sum for a

For example, if we have a linked list $1 \rightarrow 2 \rightarrow -3 \rightarrow 3 \rightarrow 1$, we can see that the nodes $2 \rightarrow -3 \rightarrow 3$ sum up to 2 + (-3) + 3 = 0.

node in the linked list is the sum of all node values from the head up to and including that node. If at any point, we find two nodes with the same prefix sum, the nodes between them sum to 0, and thus that sequence can be removed.

For example, suppose that for a linked list 1 -> 2 -> -3 -> 3 -> 1, the prefix sum at the first 1 is 1, then 3 at 2, back to 0 after -3, up to 3 at the second 3, and finally 4 at the last 1. The appearance of 0 as a prefix sum implies that the subsequence from the beginning up to that point sums to 0.

Here's our approach step by step: 1. We create a dummy node that we'll use as a new head, which helps us deal with edge cases where the beginning of the linked list might sum to 0 and be removed.

2. We iterate through the list, calculating the prefix sum for each node. We keep a track of the last seen node for each prefix sum in

a hash table. If the same prefix sum is encountered again, we update it in the hash map with the most recent node. This is

because any node sequences between the two nodes with the same sum can be removed, so we only care about the latest position for that prefix sum.

3. After populating the hash table, we make a second pass through the list, again calculating the prefix sum. Using our hash table,

we can now update the next pointer of the current node to skip over any nodes that are part of a zero-sum sequence by setting

- it to the next of the last node remembered for the current prefix sum. With this approach, we effectively go over the list, find all sequences summing to 0, and remove them, then return the list with all those sequences gone.
- The provided solution makes use of the prefix sum concept and a hash table to efficiently find and remove zero-sum consecutive sequences in the linked list. Here's how the implementation unfolds:

1. We initialize a dummy node that acts as a pre-head, ensuring we can handle cases where the head itself might be part of a zerosum sequence. This dummy node points to the original head of the list. 1 dummy = ListNode(next=head)

2. We declare a hash table last to record the last node for each unique prefix sum observed. The hash table is indexed by the prefix sum and contains the corresponding node as its value.

s += cur.val

last[s] = cur

cur = cur.next

Solution Approach

the previous node, since we only need the latest one. s, cur = 0, dummy

3. Starting from the dummy node (pre-head), we iterate through the linked list to calculate the prefix sum s for each node. As we

compute the prefix sum, we update the last hash table with the current node. If the same sum occurs again later, it overwrites

4. After populating the last table, we iterate the list again, starting from the dummy node, to update the next pointers. For each node, as we calculate the prefix sum s, we find the node corresponding to this sum in the last table, and we set the current node's next pointer to last[s].next. This effectively skips over and removes any nodes part of a zero-sum sequence found between the two nodes with equal prefix sums.

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5. Finally, we return dummy next — the head of the modified list, which no longer contains any sequence of nodes that sum up to 0.
The two primary components used in the solution are:
  • Prefix Sum: This technique is critical to discover sequences that total to 0. By keeping track of the cumulative sum at each node,
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1 s, cur = 0, dummy

s += cur.val

cur = cur.next

cur.next = last[s].next

2 while cur:

Example Walkthrough

Let's consider a simple linked list to illustrate the solution approach: 3 -> 4 -> -7 -> 5 -> -6 -> 6. The goal is to remove sublists

Together, these structures allow the algorithm to achieve its goal with a linear time complexity relative to the number of nodes in the

• Hash Table: By storing the last occurrence of a node for a given prefix sum, we have the ability to quickly jump over sequences

that sum to 0. This is because if a prefix sum repeats, the sum of the nodes between those repetitions is necessarily 0.

that sum to 0.

1. Initialize a dummy node and a last hash table

2 s: 3 -> 3 (First node with value 3)

7 s: 5 -> 6 (The last node, summing up to 5)

3 s: 7 -> 4 (Node with value 4)

6 s: -1 -> -6

be removed.

the prefix sum s:

class ListNode:

class Solution:

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Java Solution

class Solution {

we can swiftly identify regions of the list that cancel each other out.

list, since each node is processed directly without the need for nested loops or recursion.

the dummy node points to the head of our list (3). 2. First pass: Compute prefix sums and populate the last table

4 s: $0 \rightarrow -7$ (Node with value -7, this gives us a prefix sum of 0, meaning everything from the dummy to this node sums to 0)

Notice how the prefix sum returned to 0 when we included the -7 node, implying the sublist 3 -> 4 -> -7 sums to 0 and should

We create a dummy node and initialize our last hash table to store the last node associated with each unique prefix sum. Initially,

3. Second pass: Update the next pointers using the last table We iterate through the list again, using the last table to update next pointers. We perform the following updates, recalculating

that $5 \rightarrow -6 \rightarrow 6$ also sum to 0 and should be removed.

1 s: 0, dummy.next -> last[0].next (skipping to node with value 5)

2 s: 5, 5.next -> last[5].next (skipping to node with value 6) After the second pass, the list becomes 5 -> 6, since the first part 3 -> 4 -> -7 has been skipped. We then continue and find

Starting from the dummy node, the prefix sum (s) and last table will be updated as follows:

1 s: 0 -> dummy node (There's always a dummy node associated with prefix sum 0)

5 s: 5 -> 5 (We continue the process from the node with value 5)

Python Solution 1 # Definition for singly-linked list.

def removeZeroSumSublists(self, head: Optional[ListNode]) -> Optional[ListNode]:

Reset the sum and traverse the list again to remove zero-sum sublists.

The dummy node's next now points to the head of the adjusted list.

Dictionary to keep track of the prefix sums and their corresponding nodes.

Create a dummy node which points to the head of the list. This helps with edge cases.

Set the next node to be the node that follows the last occurrence of the current sum.

def __init__(self, value=0, next_node=None):

dummy_node = ListNode(next_node=head)

current_node = current_node.next

current_sum, current_node = 0, dummy_node

current_sum += current_node.value

current_node = current_node.next

public ListNode removeZeroSumSublists(ListNode head) {

current_node.next = prefix_sums[current_sum].next

self.value = value

prefix_sums = {}

while current_node:

return dummy_node.next

self.next = next_node

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4. Final list
   After all updates, the prefix sums that led to a non-zero result have been removed, and we are left with an empty list, as the
    entire list was a combination of zero-sum sublists. The dummy next now points to None.
By using the prefix sum and a hash table to keep track of the last occurrence of each prefix sum, we have efficiently removed
consecutive sequences that sum to 0. The resulting list would be returned as the modified list without these zero-sum sequences.
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Calculate the prefix sums and store the most recent node that resulted in each sum. current_sum, current_node = 0, dummy_node while current_node: current_sum += current_node.value prefix_sums[current_sum] = current_node

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// Dummy node to serve as a new starting point for the linked list
           ListNode dummyHead = new ListNode(0, head);
           // HashMap to store the cumulative sum and corresponding node
           Map<Integer, ListNode> cumulativeSumMap = new HashMap<>();
            int sum = 0; // Variable to hold the cumulative sum of node values
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            ListNode current = dummyHead; // Current node, starting from the dummy head
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           // First pass: Calculate cumulative sums and save the last occurrence
           // of each sum in the HashMap
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           while (current != null) {
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                sum += current.val;
                cumulativeSumMap.put(sum, current);
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               current = current.next;
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            sum = 0; // Reset the sum for the second pass
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            current = dummyHead; // Reset current node to the dummy head
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           // Second pass: Remove zero-sum sublists
           while (current != null) {
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                sum += current.val; // Update the cumulative sum
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                // If we have seen this sum before, it means the sublist between the
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               // previous occurrence and this one sums to zero
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                current.next = cumulativeSumMap.get(sum).next;
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                current = current.next; // Move to the next node
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            return dummyHead.next; // Return the updated list without the dummy head
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35 }
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               prefixSum += current->val;
               // Link the current node to the node following the last occurrence of the same prefix sum
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               // This effectively removes the zero-sum sublists
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               current->next = lastSeenPrefixSum[prefixSum]->next;
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               current = current->next;
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C++ Solution

struct ListNode {

int val;

class Solution {

public:

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#include <unordered_map>

ListNode *next;

// Definition for singly-linked list.

ListNode(): val(0), next(nullptr) {}

ListNode* current = dummyHead;

prefixSum += current->val;

current = current->next;

int prefixSum = 0;

while (current) {

prefixSum = 0;

current = dummyHead;

Time and Space Complexity

while (current) {

ListNode(int x) : val(x), next(nullptr) {}

ListNode(int x, ListNode *next) : val(x), next(next) {}

// Create a dummy head node to handle edge cases seamlessly

// First pass to record the last occurrence of each prefix sum

// Reset the prefix sum and re-iterate from the dummy head

// Second pass to connect nodes bypassing the zero-sum sublists

std::unordered_map<int, ListNode*> lastSeenPrefixSum;

ListNode* removeZeroSumSublists(ListNode* head) {

ListNode* dummyHead = new ListNode(0, head);

lastSeenPrefixSum[prefixSum] = current;

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// Return the next element of the dummy head which would be the new list head
           return dummyHead->next;
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44 };
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Typescript Solution
   // Type definition for a ListNode.
  type ListNode = {
     val: number;
     next: ListNode | null;
   };
    * Removes all contiguous sublists with sum zero from a linked list.
    * @param head The head of the singly linked list.
    * @return The head of the modified linked list, with zero-sum sublists removed.
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   function removeZeroSumSublists(head: ListNode | null): ListNode | null {
     // Dummy node at the start of the list to simplify edge cases.
     const dummy: ListNode = { val: 0, next: head };
     // A map to store the cumulative sum of nodes and their last occurrences.
15
     const lastOccurrenceOfSum: Map<number, ListNode> = new Map();
     let sum = 0;
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     // First pass: Compute the cumulative sum and track the last occurrence of each sum.
20
     for (let currentNode: ListNode | null = dummy; currentNode; currentNode = currentNode.next) {
       sum += currentNode.val;
       lastOccurrenceOfSum.set(sum, currentNode);
     sum = 0; // Reset sum for the second pass.
     // Second pass: Use the last occurrence map to skip over zero-sum sublists.
     for (let currentNode: ListNode | null = dummy; currentNode; currentNode = currentNode.next) {
       sum += currentNode.val;
       // The next node will be the one after the last occurrence of the current sum.
       // As we have removed zero-sum sublists, the sums will not repeat in the new list.
       currentNode.next = lastOccurrenceOfSum.get(sum)!.next;
     // Return the modified list, sans the dummy node.
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21 22 23 24 25 26 27 28 29 32 33 34 35 36 return dummy.next; 37 } 38

nodes that are part of a zero-sum sublist by setting the next pointer of previous non-zero-sum nodes to the next node in the last occurrence of that sum. The space complexity of the code is O(n) as well. The primary factor contributing to the space complexity is the dictionary (last) which stores a value for each unique cumulative sum encountered while iterating through the list. In the worst-case scenario, there could be as many unique sums as there are nodes in the list (when no sublists sum to zero), which would require storing each node in the dictionary, hence O(n) space is needed.

The provided code has a time complexity of O(n) where n is the length of the linked list. This is because the code consists of two

cumulative sums of the nodes up to that point to the corresponding node. The second while loop uses the dictionary to skip over

separate while loops that each iterate through the list once. The first while loop constructs a dictionary (last) mapping the