Problem Description

In this problem, you're given an array nums of integers, and an integer k which represents the size of a sliding window. This sliding window moves across the array from left to right, one element at a time. At each position of the window, you can only see k numbers within it. The objective is to return a new array that contains the maximum value from each of the windows as it slides through the entire array.

frame moves to the right by one element, the oldest number in the frame is replaced with a new number from the array. You need to find the maximum number in the frame after each move and record it.

To illustrate, imagine a section of k numbers from the array nums as a frame that only allows you to view those k numbers. As the

The intuition behind the solution arises from the need to efficiently manage the current candidates for the maximum value within the sliding window. We need a way to update the candidates as the window slides through the array, adding new elements and removing

Intuition

old ones. One efficient approach to solve this problem is to use a double-ended queue (deque) that maintains a descending order of values (indices of nums) from the largest at the front to the smallest at the back. The front of the deque will always hold the index of the

maximum number within the current window. This allows us to quickly retrieve the maximum number by looking at the element at the front of the deque. Here are the steps to arrive at the solution: Initialize a deque q to hold indices of nums and an empty list ans to hold the maximums.

3. Check if the deque is non-empty and if the element at the front of the deque is out of the sliding window's range. If so, pop it

- from the front to remove it from our candidates.
- 4. While there are elements in the deque and the value at index 1 of nums is greater than or equal to the value at the indices stored

2. Iterate through the indices and values of nums using a loop.

- in the deque's back, pop elements from the back of the deque. This is because the new value could potentially be the new maximum, and thus we remove all the values which are less than the current value since they cannot be the maximum for future windows.
- 5. Append the current index i to the deque. 6. If i is greater than or equal to k-1, it means we've filled the first window. The current maximum (the value at the front of the deque) is added to ans. Continue this process until the end of the array is reached.
- 8. Return the ans list.
- Using a deque allows us to efficiently remove indices/values from both ends and keep our window updated. This solution ensures that we have a near constant time operation for each window, making it an efficient solution.

from both the front and the back in O(1) time complexity.

Here's a step-by-step explanation of the algorithm:

Solution Approach

1 q = deque()

2 ans = []

window:

1. Initialization: We start by initializing an empty deque q and an empty list ans which will store the maximum values of the current sliding window.

The key to the efficient solution is using a double-ended queue (deque), a powerful data structure that allows insertion and deletion

2. Iterating through nums: We use a for loop to iterate over the array. Each iteration represents a potential new frame of the sliding

- 3. Maintain Window Size: Before processing the new element at each step, we ensure that the deque's front index belongs to the current window:
- 4. Maintain Deque Properties: We pop indices from the back of the deque as long as the current value is larger than the values at

1 while q and nums[q[-1]] \leftarrow v:

1 if q and i - k + 1 > q[0]:

q.popleft()

1 for i, v in enumerate(nums):

5. Add New Index: We then add the index of the current element to the deque back.

the indices at deque's rear. This ensures that the deque is decreasing so the front always has the largest element:

6. Record the Maximum: Once we reach at least the kth element (i >= k - 1), we find a maximum for the full-sized window which we record by adding the value at the front of the deque to ans list:

ans.append(nums[q[0]])

1 q.append(i)

1 if i >= k - 1:

7. Return Result: After the loop completes, ans contains the maximums for each sliding window, which we return. This algorithm hinges crucially on the deque's properties to keep the indices in a descending order of their values in nums. Keeping

Example Walkthrough Consider the array nums = [1,3,-1,-3,5,3,6,7] and a sliding window size k = 3. Let's walk through the solution step by step: 1. Initialization: An empty deque q and an empty list ans are initialized.

the deque in descending order ensures that the element at the front is the largest and should be included in ans. When the window

moves to the right, indices that are out of the window or not relevant (because there's a larger or equal value that came later) are

No indices to remove from deque, since it's empty.

one.

Python Solution

index_queue = deque()

max_values = []

nums.

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3. First Iteration (i=0, v=1):

Since 3 (nums[1]) is greater than 1 (nums[q[-1]]), we pop index 0 and then append index 1 to the deque.

Continue sliding the window, maintaining the deque by removing out-of-range indices and values smaller than the current

This walkthrough demonstrates the solution using a deque to efficiently track the maximum of the current sliding window in the array

The deque still contains only one index [0].

• Window is not yet full (i < k-1), so we don't record the maximum.

2. Iterating through nums: We start iterating over the array with indices and values.

popped out from the deque, maintaining the required properties.

1 q = deque() # deque to hold indices of nums

Append index 0 to the deque.

4. Second Iteration (i=1, v=3):

2 ans = [] # list to hold max values of each window

- Window is not yet full (i < k-1), so we don't record the maximum. 5. Third Iteration (i=2, v=-1):
- Now i >= k-1, so we record the current maximum nums [q[0]], which is 3. 6. Subsequent Iterations:

If the first element in the queue is outside the current window, remove it

If we have reached or passed the first complete window, record the maximum

○ The deque contains [1] and since -1 is not greater than 3, we only append index 2.

 After each slide, if the window is full, add the maximum to ans. 7. After Sliding Through Entire Array:

def maxSlidingWindow(self, nums: List[int], k: int) -> List[int]:

if index_queue and current_index - k + 1 > index_queue[0]:

Initialize a deque for storing indices of elements

List to store the maximums for each sliding window

from collections import deque class Solution:

Iterate over each element, with its index

index_queue.popleft()

for current_index, value in enumerate(nums):

Add the current index to the queue

max_values.append(nums[index_queue[0]])

index_queue.append(current_index)

public int[] maxSlidingWindow(int[] nums, int k) {

if current_index >= k - 1:

The final ans list will be [3, 3, 5, 5, 6, 7].

15 # Remove elements from the back of the queue if they are smaller than 16 17 # or equal to the current element since they will not be needed anymore while index_queue and nums[index_queue[-1]] <= value:</pre> 18 19 index_queue.pop()

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           # Return the list of maximums
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            return max_values
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Java Solution

class Solution {

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int numsLength = nums.length;
           int[] result = new int[numsLength - k + 1]; // Array to store the max values for each window
           Deque<Integer> deque = new ArrayDeque<>(); // Double-ended queue to maintain the max element indices
           for (int i = 0, j = 0; i < numsLength; ++i) {
               // Remove the indices of elements from the deque that are out of the current window
               if (!deque.isEmpty() && i - k + 1 > deque.peekFirst()) {
                   deque.pollFirst();
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               // Remove indices of elements from the deque that are less than
               // the current element nums[i] since they are not useful
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               while (!deque.isEmpty() && nums[deque.peekLast()] <= nums[i]) {</pre>
                    deque.pollLast();
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               // Add current element's index to the deque
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               deque.offer(i);
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               // When we've hit size k, add the current max to the result
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               // This corresponds to the index at the front of the deque
               if (i >= k - 1) {
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                    result[j++] = nums[deque.peekFirst()];
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           // Return the populated result array containing max of each sliding window
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           return result;
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32 }
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C++ Solution
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// This function computes the maximum value in each sliding window of size k in the array nums

deque<int> windowIndices; // Deque to store indices of elements in the current window

// Pop elements from the back that are less than or equal to the current element

while (!windowIndices.empty() && nums[windowIndices.back()] <= nums[i]) {</pre>

// Vector to store the maximum value for each window

vector<int> maxSlidingWindow(vector<int>& nums, int k) {

// Remove indices of elements not in the current window

// Maintain the elements in decreasing order in the deque

if (!windowIndices.empty() && i - k >= windowIndices.front()) {

for (int i = 0; i < nums.size(); ++i) {</pre>

windowIndices.pop_front();

windowIndices.pop_back();

windowIndices.push_back(i);

// Push current element's index onto the deque

vector<int> maxValues;

27 // If we've reached the end of the first window, record the max for the current window 28 if (i >= k - 1) { 29

#include <vector>

using namespace std;

2 #include <deque>

class Solution {

6 public:

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maxValues.emplace_back(nums[windowIndices.front()]);
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           return maxValues; // Return the list of maximum values
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35 };
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Typescript Solution
   /**
    * Calculates the max sliding window for an array of numbers.
    * @param {number[]} nums - The input array of numbers.
    * @param {number} k - The size of the sliding window.
    * @return {number[]} - Array of the maximum numbers for each sliding window.
    */
 6
    function maxSlidingWindow(nums: number[], k: number): number[] {
       // Initialize an array to hold the maximum values for each sliding window.
       let maxValues: number[] = [];
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       // Initialize a deque to store indices of elements in nums.
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       // Elements in the deque are in decreasing order from the start (front) to the end (back).
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       let deque: number[] = [];
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       // Iterate through nums using 'i' as the right boundary of the sliding window.
       for (let i = 0; i < nums.length; ++i) {</pre>
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           // If the left boundary of the window has exceeded the left-most index in the deque,
           // remove the left-most index as it's no longer in the window.
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           if (deque.length && i - k + 1 > deque[0]) {
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               deque.shift();
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           // While the deque is not empty and the current element is greater than the
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           // last element indexed in deque, remove the last element from the deque.
           // This ensures elements in the deque are always in decreasing order.
26
           while (deque.length && nums[deque[deque.length - 1]] <= nums[i]) {</pre>
27
               deque.pop();
           // Add the current index to the deque.
           deque.push(i);
```

43 Time and Space Complexity

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Time Complexity

29 30 33 // If we have hit the size of the window, append the maximum value (front of the deque) 34 // to the maxValues array. if (i >= k - 1) { maxValues.push(nums[deque[0]]); 39 // Return the array containing the maximum for each sliding window. 40 return maxValues; 41 42 }

The time complexity of the code is O(n), where n is the number of elements in the array nums. This is because the code iterates

through each element in nums once. Each element is added to the deque q once, and it's potential removal is also done at most once due to the while loop condition. Despite the nested while loop, the overall number of operations for each element remains constant, ensuring a linear time complexity.

Space Complexity The space complexity is O(k), where k is the size of the sliding window. The deque q is used to store indices of elements and its size is restricted by the bounds of the sliding window, which at most can have k indices stored at a time. Additionally, the output list ans grows linearly with n - k + 1 (the number of windows), but it does not depend on the input size in a nested or exponential manner,

so it does not affect the asymptotic space complexity with respect to k.