





Problem Description



In this problem, we are given two complex numbers in the form of strings, where the format of each string is "real+imaginaryi". The task is to multiply these two complex numbers and output the result as a string in the same format. Complex numbers are numbers that include a real part and an imaginary part. The imaginary part is represented by 'i', and by definition,  $1^2 = -1$ . Multiplication of two complex numbers follows the distributive property from algebra and the special rule of 1^2.

The inputs:

- num1: a string representation of the first complex number. num2: a string representation of the second complex number.
- Each part of the complex numbers (real and imaginary) are within the range of [-100, 100].

The output:

A string that represents the multiplication of num1 and num2 following the structure "real+imaginaryi".

# Intuition

1. Parsing the input strings to extract the real and imaginary parts as integers.

To solve this problem, we can break it down by:

2. Performing the multiplication of two complex numbers using the following formula from complex number arithmetic: (a+b1)

c) and the imaginary part (b or d) separately for each number.

- $(c+di) = ac + adi + bci + bdi^2$ 3. Simplifying the equation by considering that  $i^2 = -1$ . This will give us: (a+bi)(c+di) = (ac - bd) + (ad + bc)i
- 4. The terms ac bd and ad + bc give us the real and imaginary parts of the result, respectively.
- 5. Convert these parts back into the string format, following the required output format.
- The implementation of this intuition is straightforward algebra. Given this structure, we split the real and imaginary parts of each input number, perform the arithmetic, and combine the results into a string formatted as a complex number.

Solution Approach

## The implementation of the solution follows the mathematical approach detailed in the previous section. Here, we discuss how the

string except the last one.

imaginary parts (since  $\frac{1}{2} = -1$ ).

provided Python code adheres to the formula (a+bi)(c+di) = ac - bd + (ad + bc)i for multiplication of complex numbers. 1. Parsing the Input: The first step in the solution is to parse the input strings num1 and num2. We want to extract the real part (a or

- We use the split('+') function to separate the real and imaginary parts from the num1 and num2 strings since they follow the format "real+imaginaryi". It splits the string into two parts wherever the '+' sign appears.
- To ignore the imaginary unit 'i' at the end of the string, we use the slicing operation [:-1] which gives us all the characters in the
- The map function is then applied to convert both parts into integers. The real and imaginary parts are stored in variables a, b for num1 and c, d for num2.

2. Multiplying the Complex Numbers: Next, we calculate the multiplication of the complex numbers using the distributive property

- and by considering  $\frac{1^2}{1^2} = -1$ . The actual multiplication is performed using the following components: • a \* c - b \* d is the real part of the result. This comes from multiplying the real parts and subtracting the product of the
- the imaginary part of the other.

• a \* d + b \* c is the imaginary part of the result. This represents the sum of the products of the real part of one number with

- 3. Formatting the Result: Finally, we need to format the result into the required string format "real+imaginaryi". Using an f-string (formatted string literal) in Python, we can directly embed expressions inside a string literal:
- format. The placeholders {} are replaced with the evaluated result of the expressions inside them. In conclusion, the algorithm doesn't use complex data structures or patterns as the solution is a direct application of the formula for

• The expression f'{a \* c - b \* d}+{a \* d + c \* b}i' converts the real and imaginary parts back into the required string

multiplying complex numbers. The parsing of strings and arithmetic operations are the main aspects of the solution.

## and num2 = "2+41". We want to multiply these two complex numbers as per the formula and return the result in the standard complex number format.

Example Walkthrough

1. Parsing the Input:

Let's illustrate the solution approach with an example. Consider the two complex numbers represented by the strings num1 = "1+3i"

- num1: "1+3i" -> real part 1 and imaginary part "3i". num2: "2+4i" -> real part 2 and imaginary part "4i".
  - We remove the trailing 'i' from the imaginary parts.

We use the distributive property: (a+bi)(c+di) = ac - bd + (ad + bc)i.

We split num1 and num2 by '+' to get the real and imaginary parts separately.

- Imaginary part of num1: "3i" -> "3". Imaginary part of num2: "4i" -> "4".
- Convert these strings into integers.
  - num1: real part a = 1, imaginary part b = 3. num2: real part c = 2, imaginary part d = 4.
- 2. Multiplying the Complex Numbers:
  - Multiply the real parts and subtract the product of the imaginary parts, since i^2 = -1: 1 \* 2 − 3 \* 4 = 2 − 12 = -10. Add the product of the real part of one number with the imaginary part of the other: 1 \* 4 + 3 \* 2 = 4 + 6 = 10.
- The resulting real part is -10 and the imaginary part is +10i. 3. Formatting the Result:

Therefore, multiplying num1 = "1+3i" and num2 = "2+4i" using the given approach yields the result "-10+10i". This demonstrates the

- We combine the real and imaginary parts into one string: "-10+10i". This string follows the format "real+imaginaryi", which is our final output.
- implementation of the mathematical multiplication of complex numbers in the provided Python code, and how the parsed parts are used in the distributive property to get the desired output.

real1, imaginary1 = map(int, num1[:-1].split('+'))

imaginary\_part = real1 \* imaginary2 + real2 \* imaginary1

String[] complexTwoComponents = num2.split("\\+|i");

sscanf(num2.c\_str(), "%d+%di", &real2, &imag2);

int realProduct = real1 \* real2 - imag1 \* imag2;

int imagProduct = real1 \* imag2 + real2 \* imag1;

// Construct the result string in the format "real+imagi"

// Calculate the real part of the product of the two complex numbers

// Return the resulting string of the complex number multiplication

// Calculate the imaginary part of the product of the two complex numbers

string result = to\_string(realProduct) + "+" + to\_string(imagProduct) + "i";

// Parse the real and imaginary parts of the first complex number

int imaginaryPartOne = Integer.parseInt(complexOneComponents[1]);

// Parse the real and imaginary parts of the second complex number

int imaginaryPartTwo = Integer.parseInt(complexTwoComponents[1]);

int realPartOne = Integer.parseInt(complexOneComponents[0]);

int realPartTwo = Integer.parseInt(complexTwoComponents[0]);

result = f'{real\_part}+{imaginary\_part}i'

Python Solution class Solution: def complexNumberMultiply(self, num1: str, num2: str) -> str:

# Calculate the imaginary part as (real1 \* imaginary2 + real2 \* imaginary1)

# Return the result as a string in the format 'real\_part+imaginary\_parti'

# Split the real and imaginary parts of the first complex number 'num1'

# Split the real and imaginary parts of the second complex number 'num2' real2, imaginary2 = map(int, num2[:-1].split('+')) # Perform multiplication of two complex numbers using the formula: # (a + bi) \* (c + di) = (ac - bd) + (ad + bc)i9 # Calculate the real part as (real1 \* real2 - imaginary1 \* imaginary2) 10 real\_part = real1 \* real2 - imaginary1 \* imaginary2

#### // Function to multiply two complex numbers given as strings public String complexNumberMultiply(String num1, String num2) { // Split each input string into real and imaginary parts String[] complexOneComponents = num1.split("\\+|i");

Java Solution

1 class Solution {

return result

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           // Apply the formula for multiplication of two complex numbers:
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           // (a + bi) * (c + di) = ac + adi + bci - bd = (ac - bd) + (ad + bc)i
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           int realResult = realPartOne * realPartTwo - imaginaryPartOne * imaginaryPartTwo;
20
           int imaginaryResult = realPartOne * imaginaryPartTwo + imaginaryPartOne * realPartTwo;
21
           // Construct the resulting complex number as a string and return it
22
23
           return String.format("%d+%di", realResult, imaginaryResult);
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25 }
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C++ Solution
1 #include <string>
2 using namespace std;
   class Solution {
5 public:
       // Function to multiply two complex numbers given as strings
       string complexNumberMultiply(string num1, string num2) {
           // Initializing integer variables to contain real and imaginary parts
           int real1, imag1, real2, imag2;
           // Parse the first complex number string and extract real and imaginary parts
11
           sscanf(num1.c_str(), "%d+%di", &real1, &imag1);
13
           // Parse the second complex number string and extract real and imaginary parts
```

### 26 27 }; 28

return result;

```
Typescript Solution
   function complexNumberMultiply(num1: string, num2: string): string {
       // Split the complex numbers into real and imaginary parts.
       let partsOfNum1 = num1.split('+'),
           partsOfNum2 = num2.split('+');
       // Parse the real parts of the complex numbers from the strings.
       let realPart1 = Number(parts0fNum1[0]),
           realPart2 = Number(parts0fNum2[0]);
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       // Parse the imaginary parts of the complex numbers from the strings.
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       // The 'i' character is stripped from the end of the string.
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       let imaginaryPart1 = Number(partsOfNum1[1].slice(0, -1)),
           imaginaryPart2 = Number(partsOfNum2[1].slice(0, -1));
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       // Calculate the real part of the product by using the formula:
       // (a + bi) * (c + di) = (ac - bd) + (ad + bc)i
       // where a and b are the real and imaginary parts of the first complex number,
       // and c and d are the same for the second number.
       let productReal = realPart1 * realPart2 - imaginaryPart1 * imaginaryPart2;
       // Calculate the imaginary part of the product.
       let productImaginary = realPart1 * imaginaryPart2 + realPart2 * imaginaryPart1;
       // Construct the string representation of the complex product.
       return `${productReal}+${productImaginary}i`;
```

20 21 22 23 24 25 26 }

# Time and Space Complexity

Space complexity

complexity is constant.

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Time complexity The time complexity of the code is 0(1). This is because the code involves a constant number of operations regardless of the input size. Splitting the strings and performing arithmetic operations does not depend on the length of the input, as the format of the input is fixed (it represents a complex number).

The space complexity of the code is also 0(1). Only a fixed number of additional variables are used for storing the parsed integers

(a, b, c, d) and for constructing the final result. The storage required does not scale with input size, confirming that the space