2661. First Completely Painted Row or Column

Matrix

Problem Description

<u>Array</u>

Hash Table

Medium

respective row and column.

on the sequence provided in arr. Both arr and mat contain all integers in the range [1, m * n]. The process involves iterating over arr and painting the cell in mat that corresponds to each integer arr[i]. The goal is to determine the smallest index i at which either a whole row or a whole column in the matrix mat is completely painted. In other words, find the earliest point at which there's either a full row or a full column with all cells painted in the matrix. ntuition

Given a 0-indexed integer array arr and an m x n integer matrix mat, the task is to process arr and paint the cells in mat based

The solution revolves around tracking the painting progress in mat as we process each element in arr. The core thought is that

auxiliary data structures. This leads us to the idea of using two arrays row and col to maintain the count of painted cells for each

we don't need to modify the matrix mat itself but can instead track the number of painted cells in each row and column with

Since we need to find the positions in the matrix mat that correspond to the integers in arr, we can set up a hash table idx to map each number in the matrix to its coordinate (i, j). This allows us to quickly access the correct row and column to increment our counts.

Solution Approach

Firstly, we create a hash table named idx to store the position of each element in the matrix mat. For each element in mat, we

The implementation consists of several key steps that use algorithms and data structures to efficiently solve the problem.

make an entry in idx where the key is the element mat[i][j] and the value is a tuple (i, j) representing its row and column indices.

 $idx = \{\}$

row[i] += 1

return k

mat = [

[1, 2],

[3, 4]

row = [0, 0]

col = [0, 0]

Python

class Solution:

arr = [3, 1, 4, 2]

for i in range(m): for j in range(n):

idx[mat[i][j]] = (i, j)This hash table allows us to have constant-time lookups for the position of any element later when we traverse arr.

```
Next, we define two arrays, row and col, with lengths corresponding to the number of rows m and the number of columns n in
 the matrix mat. These arrays are used to count how many cells have been painted in each row and column, respectively.
row = [0] * m
col = [0] * n
```

The main part of the solution involves iterating through the array arr. For each element arr[k], we get its corresponding

position (i, j) in the matrix mat using the hash table idx.

the first index where a row or column is completely painted.

if row[i] == n or col[j] == m:

for k in range(len(arr)): i, j = idx[arr[k]] We increment the counts in row[i] and col[j] since arr[k] marks the cell at (i, j) as painted.

```
col[j] += 1
 Then, we check if we have completed painting a row or a column. In other words, if either row[i] equals the number of columns
 n or col[j] equals the number of rows m, we have found our solution. At that point, we can return the current index k as this is
```

This approach efficiently determines the solution by using a hash table for fast lookups and simple arrays for counting, thus avoiding the need to make any modifications to the matrix mat itself.

```
Example Walkthrough
  Let's illustrate the solution with a small example. Assume we are given the following matrix mat and array arr:
```

 $idx = \{1: (0, 0), 2: (0, 1), 3: (1, 0), 4: (1, 1)\}$

The matrix mat is of size 2×2 , so m = 2 and n = 2. Our goal is to paint the cells in mat in the order specified by arr and find

```
• For arr[0] = 3, the position in mat is idx[3] = (1, 0). Increment row[1] and col[0]. Now row = [0, 1], col = [1, 0].
• For arr[1] = 1, the position in mat is idx[1] = (0, 0). Increment row[0] and col[0]. Now row = [1, 1], col = [2, 0].
```

def first complete index(self. sequence: List[int], matrix: List[List[int]]) -> int:

Create a dictionary to map each number to its position in the matrix.

Iterate through the sequence and update row and column counters.

row index. col index = number_position_index[number]

// Returns the first index at which all numbers in a row or column are filled

// Populate a hash map with the number as the key and its position (i, j)

// Create a vector to keep track of the count of filled numbers in each row and column.

// Increment the filled numbers count for the respective row and column.

// If a row or a column is completely filled, return the current index.

// The code prior quarantees a result, so this return statement might never be reached.

int firstCompleteIndex(vector<int>& order, vector<vector<int>>& matrix) {

// Iterate through the order vector to simulate filling the matrix.

// Get the position of the current number in the order array

int rows = matrix.size(), cols = matrix[0].size();

vector<int> rowCount(rows, 0), colCount(cols, 0);

auto [i, j] = numberToPosition[order[k]];

if (rowCount[i] == cols || colCount[j] == rows) {

unordered_map<int, pair<int, int>> numberToPosition;

numberToPosition[matrix[i][j]] = {i, j};

Step 1: Create a hash table idx mapping matrix values to coordinates:

Step 2: Initialize counts for rows and columns:

Get the dimensions of the matrix.

for row index in range(rows count):

row counters = [0] * rows count

col_counters = [0] * cols_count

for index, number in enumerate(sequence):

if number in number position index:

row counters[row index] += 1

col_counters[col_index] += 1

The List type needs to be imported from the typing module.

This would then allow you to use the Solution class and its method.

Check if a row or a column is complete.

number position index = {}

rows_count, cols_count = len(matrix), len(matrix[0])

Step 3: Start iterating through arr:

Solution Implementation

the smallest index i at which either a whole row or a whole column is completely painted.

```
Since col[0] is now equal to the number of rows m, we've painted an entire column. The smallest index at this point is i = 1.
So, the earliest index in arr at which a whole row or column is painted is 1.
```

for col index in range(cols count): number = matrix[row index][col index] number_position_index[number] = (row_index, col_index) # Initialize counters for each row and column.

```
if row counters[row_index] == cols_count or col_counters[col_index] == rows_count:
            return index
# If no row or column has been completed, return -1 as a default case.
```

solution instance = Solution()

return -1

from typing import List

Example usage:

```
# result = solution_instance.first_complete_index(sequence, matrix)
Java
class Solution {
     * Finds the first index in the input array where a complete row or column is found in the input matrix.
     * @param arr Single-dimensional array of integers.
     * @param mat Two-dimensional matrix of integers.
     * @return The earliest index at which the input array causes a row or a column in the matrix to be filled.
     */
    public int firstCompleteIndex(int[] arr, int[][] mat) {
        // Dimensions of the matrix
        int rowCount = mat.length;
        int colCount = mat[0].length;
        // Mapping from the value to its coordinates in the matrix
        Map<Integer. int[]> valueToIndexMap = new HashMap<>();
        for (int row = 0; row < rowCount; ++row) {</pre>
            for (int col = 0; col < colCount; ++col) {</pre>
                valueToIndexMap.put(mat[row][col], new int[]{row, col});
        // Arrays to keep track of the number of values found per row and column
        int[] rowCompletion = new int[rowCount];
        int[] colCompletion = new int[colCount];
        // Iterate through the array `arr`
        for (int k = 0; ; ++k) {
            // Get the coordinates of the current array value in the matrix
            int[] coordinates = valueToIndexMap.get(arr[k]);
            int rowIndex = coordinates[0];
            int colIndex = coordinates[1];
            // Increment the counters for the row and column
            rowCompletion[rowIndex]++;
            colCompletion[colIndex]++;
            // Check if the current row or column is completed
            if (rowCompletion[rowIndex] == colCount || colCompletion[colIndex] == rowCount) {
                // Return the current index if a row or column is complete
                return k;
```

```
};
```

C++

public:

#include <vector>

class Solution {

#include <unordered_map>

// according to the order given in 'arr'.

// in the matrix as the value.

// from the hash map.

++rowCount[i];

++colCount[j];

return k;

return -1;

return -1

from typing import List

solution instance = Solution()

Time and Space Complexity

Example usage:

for (int i = 0; i < rows; ++i) {

for (int i = 0: i < cols: ++i) {

for (int k = 0; k < order.size(); ++k) {</pre>

// However, it is here as a fail-safe.

```
TypeScript
// Function to find the first index at which all numbers in either the
// same row or the same column of the matrix have appeared in the array.
function firstCompleteIndex(arr: number[], mat: number[][]): number {
    // Get the dimensions of the matrix
    const rowCount = mat.length;
    const colCount = mat[0].length;
    // Map to store the position for each value in the matrix
    const positionMap: Map<number. number[]> = new Map();
    // Fill the map with positions of each value
    for (let row = 0; row < rowCount; ++row) {</pre>
        for (let col = 0; col < colCount; ++col) {</pre>
            positionMap.set(mat[row][col], [row, col]);
    // Arrays to keep track of the count of numbers found in each row and column
    const rowCompletionCount: number[] = new Array(rowCount).fill(0);
    const colCompletionCount: number[] = new Array(colCount).fill(0);
    // Iterate through the array elements to find the complete row/col index
    for (let index = 0; index < arr.length; ++index) {</pre>
        // Get the position of the current element from the map
        const [row, col] = positionMap.get(arr[index])!;
        // Increment completion count for the row and column
        ++rowCompletionCount[row]:
        ++colCompletionCount[col];
        // Check if the current row or column is completed
        if (rowCompletionCount[row] === colCount || colCompletionCount[col] === rowCount) {
            // Return the current index if a complete row or column is found
            return index;
    // In case no complete row or column is found.
    // the function will keep running indefinitely due to the lack of a stopping condition in the for loop.
class Solution:
    def first complete index(self, sequence: List[int], matrix: List[List[int]]) -> int:
        # Get the dimensions of the matrix.
        rows_count, cols_count = len(matrix), len(matrix[0])
        # Create a dictionary to map each number to its position in the matrix.
        number position index = \{\}
        for row index in range(rows count):
            for col index in range(cols count):
                number = matrix[row index][col index]
                number_position_index[number] = (row_index, col_index)
        # Initialize counters for each row and column.
        row counters = [0] * rows count
        col_counters = [0] * cols_count
        # Iterate through the sequence and update row and column counters.
        for index, number in enumerate(sequence):
            if number in number position index:
                row index. col index = number_position_index[number]
                row counters[row index] += 1
                col_counters[col_index] += 1
                # Check if a row or a column is complete.
                if row counters[row_index] == cols_count or col_counters[col_index] == rows_count:
                    return index
```

The time complexity of the given code can be broken down into two main parts. Firstly, populating the idx dictionary requires iterating through each element of the $m \times n$ matrix, which takes $0(m \times n)$ time. Secondly, iterating over the arr array with k elements and updating the row and col counts takes O(k) time. However, each element's index is accessed in constant time due to the dictionary. Therefore, the overall time complexity is the sum of both parts, 0(m * n + k).

If no row or column has been completed, return -1 as a default case.

The List type needs to be imported from the typing module.

This would then allow you to use the Solution class and its method.

result = solution_instance.first_complete_index(sequence, matrix)

```
The space complexity involves the storage used by the idx dictionary, which holds one entry for each element in the m x n
matrix, hence 0(m * n) space. Additionally, the row and col arrays utilize 0(m) and 0(n) space, respectively. Consequently, the
total space complexity is 0(m * n) since 0(m + n) is subsumed under 0(m * n) when m and n are of the same order.
```