54. Spiral Matrix Matrix Simulation Medium <u>Array</u>

Problem Description

In this problem, we are tasked with traversing a 2D array (or matrix) in a spiral pattern. Imagine starting at the top-left corner of the matrix and going right, then down, then left, and then up, turning inward in a spiral shape, until we traverse every element in the matrix exactly once. The function should return a list of the elements of the matrix in the order they were visited during this spiral traversal.

Intuition

same direction (right initially) until we meet a boundary of the matrix or a previously visited cell. When we encounter such a boundary, we make a clockwise turn and continue the process. There are two insightful approaches to this problem:

To solve this problem, we need to simulate the process of traveling around the matrix spiral. Essentially, we keep moving in the

Simulation Approach: We initiate four direction vectors (or in our case, a direction array dirs) that represent right, down, left,

At this point, we turn 90 degrees and continue. To avoid revisiting cells, we mark each visited cell by adding it to a set vis so that we know when to turn. The time complexity here is $0(m \times n)$ because we visit each element once, and the space complexity is also $0(m \times n)$ due to the extra space used to store visited cells. Layer-by-layer Simulation: Instead of marking visited cells, we can visualize the matrix as a series of concentric rectangular layers. We traverse these layers from the outermost to the innermost, peeling them away as we go. This approach requires

and up. We iterate over all elements in the matrix by taking steps in the initial direction until we can no longer move forward.

careful handling of the indices to ensure we stay within the bounds of the current layer. This way of traversal helps to potentially reduce extra space usage because we don't explicitly need to keep track of visited cells. **Solution Approach**

Initialization:

○ The dirs array dirs = (0, 1, 0, -1, 0) encodes the direction vectors. dirs[k] and dirs[k+1] together represent the direction we move in, with k starting at 0 and cycling through values 0 to 3 to represent right, down, left, and up in that order.

• The i and j variables represent the current row and column positions in the matrix.

The given Python solution follows the Simulation Approach described in the intuition section.

o ans list is where we collect the elements of the matrix as we visit them.

• We define m and n which are the dimensions of the matrix (number of rows and number of columns respectively).

- **Visiting Elements:** \circ We loop exactly m * n times, once for each element of the matrix.
- Each time through the loop, we append the current element to the ans list and mark its position (i, j) as visited by adding it to the vis set.

<= x < m or not 0 <= y < n or (x, y) in vis: check.

- Before we move to the next position, we check if the position is valid it must be within bounds and not already visited. This is the if not 0
- **Moving Through the Matrix:** • We calculate the next position (x, y) based on the current direction we are moving. This is done using the current values of i, j, and k.
- o If the move is invalid, we change the direction by increasing k modulo 4. This works because if k is 3 and we add 1, (k + 1) % 4 will reset k back to 0.
- Because we update the direction whenever we hit the edge of the matrix or a visited cell, the algorithm naturally handles non-square matrices and any edge cases where the spiral must turn inward.

• Once the direction is confirmed as valid, we update i and j to move to the next position in the matrix.

o In the reference solution, it's suggested that instead of using a vis set to keep track of visited cells (contributing to space complexity of 0(m

Handling Edge Cases:

Completing the Spiral:

Space Optimization:

the matrix values, effectively using the input matrix as the vis state. This reduces the space complexity to 0(1), provided the matrix can be modified and that the added constant is chosen such that it doesn't cause integer overflow.

matrix. The attention to directional changes and boundary conditions ensures that all cases are handled smoothly.

• The process continues, circling around the matrix and moving inward until all elements have been added to ans.

The executed code follows this approach rigorously, and through simulation, delivers the correct spiral traversal of the input

Example Walkthrough

Let's illustrate the solution approach using a small example where our input is a 2D matrix: matrix = [

x n)), we could modify the matrix itself to mark cells as visited. This could be done by adding a constant value which is outside the range of

Now we'll walk through the solution step by step:

 \circ We calculate the next position using the current direction (right, k = 0), so x = i + dirs[k] = 0 and y = j + dirs[k+1] = 1.

\circ Direction array dirs = (0, 1, 0, -1, 0) indicates the x and y offsets for right, down, left, and up movements respectively.

Initialization:

 \circ m = 3 (3 rows), n = 3 (3 columns)

```
• ans = [] will collect the elements in spiral order.
o vis = set() to store visited positions.
```

 \circ We start at the top-left corner, so initial indices i = 0 and j = 0.

We begin by appending matrix[0][0] to ans, so ans = [1].

We add (0, 0) to vis to mark it as visited.

Direction Change and Boundary Check:

Moving Through the Matrix:

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• This position is within bounds and not visited, so we move there and append matrix[0][1] to ans, making it [1, 2].

    We repeat this process and append [3, 6, 9] to ans.
```

Avoiding Visited Cells:

Solution Implementation

def spiralOrder(self, matrix):

Define matrix dimensions.

rows, cols = len(matrix), len(matrix[0])

Iterate over the cells of the matrix.

result.append(matrix[row][col])

Mark the current cell as visited.

for _ in range(rows * cols):

visited.add((row, col))

directions = ((0, 1), (1, 0), (0, -1), (-1, 0))

Python

class Solution:

Visiting Elements:

- After reaching the last column, we check the next right move and find it's out of bounds. • We then change direction to down (k = 1), and append [8, 7] to ans.
- We turn right and add [4, 5] to the spiral traversal. **Completing the Spiral:**

We've now visited all cells, and ans is [1, 2, 3, 6, 9, 8, 7, 4, 5].

We turn again, moving up and find the top center cell (0, 1) is also visited.

Next, we attempt to move left but the cell (2, 0) is visited.

- **Space Optimization (Optional):** • A potentially more space-efficient approach might entail modifying the given matrix to mark visited elements if allowed.
- By following the simulation approach, the function would return the traversal in spiral order as [1, 2, 3, 6, 9, 8, 7, 4, 5].

Define directions for spiral movement (right, down, left, up).

Initialize row and column indices and the direction index.

Append the current element to the result list.

nextRow = row + directionRow[directionIndex];

nextCol = col + directionCol[directionIndex];

if (matrix.empty()) return {}; // Return an empty vector if the matrix is empty

vector<int> result; // This vector will store the elements of matrix in spiral order

vector<vector<bool>> visited(rows, vector<bool>(cols, false)); // Keep track of visited cells

int rows = matrix.size(), cols = matrix[0].size(); // rows and cols store the dimensions of the matrix

vector<int> directions = {0, 1, 0, -1, 0}; // Row and column increments for right, down, left, up movements

// Move to the next cell

vector<int> spiralOrder(vector<vector<int>>& matrix) {

row = nextRow;

col = nextCol;

return result;

C++

public:

class Solution {

Calculate the next cell's position based on the current direction.

This function takes a matrix and returns a list of elements in spiral order.

row = col = direction_index = 0 # Initialize the answer list and a set to keep track of visited cells. result = [] visited = set()

```
next row, next col = row + directions[direction_index][0], col + directions[direction_index][1]
           # Check if the next cell is within bounds and not visited.
            if not (0 <= next_row < rows) or not (0 <= next_col < cols) or (next_row, next_col) in visited:</pre>
               # Change direction if out of bounds or cell is already visited.
               direction_index = (direction_index + 1) % 4
            # Update the row and column indices to the next cell's position.
            row += directions[direction_index][0]
            col += directions[direction_index][1]
       # Return the result list.
       return result
Java
import java.util.List;
import java.util.ArrayList;
class Solution {
    public List<Integer> spiralOrder(int[][] matrix) {
       // Dimensions of the 2D matrix
       int rowCount = matrix.length;
       int colCount = matrix[0].length;
       // Direction vectors for right, down, left, and up
       int[] directionRow = \{0, 1, 0, -1\};
       int[] directionCol = {1, 0, -1, 0};
       // Starting point
       int row = 0, col = 0;
       // Index for the direction vectors
       int directionIndex = 0;
       // List to hold the spiral order
       List<Integer> result = new ArrayList<>();
       // 2D array to keep track of visited cells
       boolean[][] visited = new boolean[rowCount][colCount];
       for (int h = rowCount * colCount; h > 0; --h) {
           // Add the current element to the result
            result.add(matrix[row][col]);
           // Mark the current cell as visited
           visited[row][col] = true;
           // Compute the next cell position
           int nextRow = row + directionRow[directionIndex];
            int nextCol = col + directionCol[directionIndex];
           // Check if the next cell is out of bounds or visited
           if (nextRow < 0 || nextRow >= rowCount || nextCol < 0 || nextCol >= colCount || visited[nextRow][nextCol]) {
               // Update the direction index to turn right in the spiral order
               directionIndex = (directionIndex + 1) % 4;
                // Recompute the next cell using the new direction
```

```
int row = 0, col = 0, dirIndex = 0; // Start from the top-left corner and use dirIndex to index into directions
        for (int remain = rows * cols; remain > 0; --remain) {
            result.push_back(matrix[row][col]); // Add the current element to result
            visited[row][col] = true; // Mark the current cell as visited
           // Calculate the next cell position
            int nextRow = row + directions[dirIndex], nextCol = col + directions[dirIndex + 1];
           // Change direction if next cell is out of bounds or already visited
           if (nextRow < 0 || nextRow >= rows || nextCol < 0 || nextCol >= cols || visited[nextRow][nextCol]) {
               dirIndex = (dirIndex + 1) % 4; // Rotate to the next direction
           // Move to the next cell
            row += directions[dirIndex];
            col += directions[dirIndex + 1];
        return result; // Return the result
};
TypeScript
function spiralOrder(matrix: number[][]): number[] {
   const rowCount = matrix.length; // Number of rows in the matrix
   const colCount = matrix[0].length; // Number of columns in the matrix
   const result: number[] = []; // The array that will be populated and returned
   const visited = new Array(rowCount).fill(0).map(() => new Array(colCount).fill(false)); // A 2D array to keep track of visite
    const directions = [0, 1, 0, -1, 0]; // Direction array to facilitate spiral traversal: right, down, left, up
    let remainingCells = rowCount * colCount; // Total number of cells to visit
   // Starting point coordinates and direction index
    let row = 0;
    let col = 0;
    let dirIndex = 0;
   // Iterate over each cell, decrementing the count of remaining cells
   for (; remainingCells > 0; --remainingCells) {
        result.push(matrix[row][col]); // Add the current cell's value to the result
       visited[row][col] = true; // Mark the current cell as visited
       // Calculate the indices for the next cell in the current direction
```

if (nextRow < 0 || nextRow >= rowCount || nextCol < 0 || nextCol >= colCount || visited[nextRow][nextCol]) {

dirIndex = (dirIndex + 1) % 4; // Change direction (right -> down -> left -> up)

```
col += directions[dirIndex + 1];
      return result; // Return the array containing the spiral order traversal of the matrix
class Solution:
   def spiralOrder(self, matrix):
```

This function takes a matrix and returns a list of elements in spiral order.

const nextRow = row + directions[dirIndex];

row += directions[dirIndex];

Define matrix dimensions.

row = col = direction_index = 0

rows, cols = len(matrix), len(matrix[0])

directions = ((0, 1), (1, 0), (0, -1), (-1, 0))

row += directions[direction_index][0]

col += directions[direction_index][1]

Return the result list.

return result

const nextCol = col + directions[dirIndex + 1];

// Check if the next cell is out of bounds or already visited

// Move to the next cell in the updated/current direction

Define directions for spiral movement (right, down, left, up).

Initialize row and column indices and the direction index.

```
result = []
visited = set()
# Iterate over the cells of the matrix.
for _ in range(rows * cols):
    # Append the current element to the result list.
    result.append(matrix[row][col])
    # Mark the current cell as visited.
    visited.add((row, col))
```

Calculate the next cell's position based on the current direction.

Initialize the answer list and a set to keep track of visited cells.

Check if the next cell is within bounds and not visited. if not (0 <= next_row < rows) or not (0 <= next_col < cols) or (next_row, next_col) in visited:</pre> # Change direction if out of bounds or cell is already visited. direction_index = (direction_index + 1) % 4 # Update the row and column indices to the next cell's position.

next_row, next_col = row + directions[direction_index][0], col + directions[direction_index][1]

Time and Space Complexity

input matrix. This is because the function iterates over every element in the matrix exactly once. The space complexity of the function, however, is not O(1) as stated in the reference answer. Instead, it is O(m * n) because the function uses a set vis to track visited elements, which in the worst-case scenario, can grow to contain every element in the matrix.

The time complexity of the function spiralOrder is O(m * n) where m is the number of rows and n is the number of columns in the