Problem Description

(rStart) and column (cStart). Your task is to simulate a walk from the starting cell in a clockwise spiral pattern until you have visited every cell in the grid. This spiral pattern means you move east, then south, then west, and finally north, increasing the distance you move in a specific direction before turning by one cell each time you complete a full cycle (east, south, west, and north). As you perform this walk, even if you move outside the grid's boundaries, you keep the pattern, and you may return to the grid's boundary later. The goal is to visit all cells on the grid and return a list of their coordinates in the order they were visited.

In this LeetCode problem, you are given the dimensions of a grid (rows x cols) and a starting cell within that grid, defined by its row

Intuition

movement direction and counter changes in direction while traversing the grid. We should keep in mind that it is necessary to handle cases where the walk takes us outside the grid boundary. We initialize the solution by adding the starting position to our result set. If the grid is of size 1×1, the problem is already solved with

The problem can be solved by simulating the walk in a spiral pattern as described. The intuition behind this solution is to track

this step. For larger grids, we have to begin walking in a spiral. We know that for a spiral walk, the number of steps we take in the east or west directions (horizontal steps) will always be one more than the number of steps we took in the previous vertical movement (north or south). Conversely, the number of steps we take in the north or south direction will be equal to the number of steps we will take in the next horizontal movement. To implement this pattern, we maintain a variable k that represents how many steps we should move in the current direction. We

start with k = 1, as the first move after the starting position is just one step to the right (east). We then increase k by 2 after a full

cycle of directions (east > south > west > north) to account for the changing step count in the spiral path. For each direction, we move k steps, updating our current position and conditionally add the new position to the result set if it lies within the grid's boundaries. We keep doing so until we have visited all rows * cols cells.

Solution Approach

The implementation of the solution follows a pattern-based approach by simulating movements on the grid. Here's how it's done

step by step:

1. We define a list ans to keep track of the cells visited, starting with the initial cell [rStart, cStart]. 2. We check if the grid size is 1x1. If so, we immediately return ans because the single starting cell is the only cell to visit. 3. We then set k = 1, which will determine the number of steps we take in a given direction before turning. This k will be increased

- as necessary to simulate the spiral pattern.
- 4. A while True loop begins, which will run until we've visited all rows * cols cells of the grid. 5. Inside the loop, we iterate over a list of direction increments and the corresponding step counts. The list has tuples in the format
- [dr, dc, dk], where dr is the row increment (0 for east or west, 1 for south, -1 for north), dc is the column increment (1 for east, -1 for west, 0 for north or south), and dk being the number of steps to move in that direction. 6. For each direction, we run another loop for dk steps:
- For each step, we update rStart and cStart with dr and dc respectively. • We then check if the new position is within the grid's boundaries by verifying 0 <= rStart < rows and 0 <= cStart < cols.
- directions. The algorithm utilizes simple iteration and directional increments to traverse the grid in a predictable, spiral pattern. No complex data

7. After completing the movement in all four directions, we increment k by 2 to maintain the spiral pattern for the next cycle of

• We check if we have visited rows * cols cells. If we have, we return ans as the complete list of visited cells.

structures are necessary beyond a list to hold the visited cell coordinates. The pattern's consistency allows us to increment k strategically, ensuring we expand our traversal in a spiraling outward fashion. This method provides full coverage of the grid while recording our path.

Example Walkthrough Let's walk through a small example to illustrate the solution approach. Consider a grid of size 3x3, where our starting cell is at rStart = 1 and cStart = 1 (the center of the grid).

2. Since the grid size is not 1×1 , we proceed with the solution.

3. We set k = 1 as our initial step length for the eastward move. 4. Since the grid has more than one cell, we enter the while True loop to start the spiral traversal.

5. The first direction from our starting cell is east. We only need to move one step east (dc = 1, dr = 0). We move to cell [1, 2],

6. Next is to move one step south (dc = 0, dr = 1). We move to [2, 2]. Again, it's within the grid, so ans becomes ans = [[1, 1],

12. Going west for three steps, we add [3, 2] and [3, 1] to ans.

1. We initialize ans with the starting cell, so ans = [[1, 1]].

If yes, we append the position to ans.

[1, 2], [2, 2]]. 7. Following is westward movement, but since k is 1, we'd move only one step west (dc = -1, dr = 0) to [2, 1]. We add this to

which is within the grid. We add this to ans, resulting in ans = [[1, 1], [1, 2]].

- ans, making it ans = [[1, 1], [1, 2], [2, 2], [2, 1]].
- already been visited, we don't add it again to ans`. 9. We've completed a full cycle (east > south > west > north), so we increment k by 2, making k = 3.

8. The last direction in this cycle is north (dc = 0, dr = -1). We move one step north to [1, 1], but since this cell has

would be [1, 3], within the grid, so it's added to ans - ans = [[1, 1], [1, 2], [2, 2], [2, 1], [1, 3]]. 11. Continuing the cycle, we go south three steps, adding positions [2, 3] and [3, 3] to ans.

10. For the next eastward movement, we will move three steps, but after one step, we're already at the edge. The next position

The final ans, with the cells visited in the order of the spiral from the center, would be:

13. Finally, moving north, we add [2, 1] and the last remaining cell [1, 1] is ignored as it's already visited.

- 1 [[1, 1], [1, 2], [2, 2], [2, 1], [1, 3], [2, 3], [3, 3], [3, 2], [3, 1], [2, 1]]
- Python Solution

Initialize the answer list with the starting cell

If there's only one cell, return it immediately

result = [[r_start, c_start]]

14. All cells of the 3x3 grid have been added to ans, and the traversal is complete.

if rows * cols == 1: return result 8 9

def spiralMatrixIII(self, rows: int, cols: int, r_start: int, c_start: int) -> List[List[int]]:

'k' represents the number of steps we take in a given direction before turning

It starts at 1 and gets incremented after finishing an east and north pass

Each iteration goes in the pattern: East, South, West, North

public int[][] spiralMatrixIII(int rows, int cols, int rStart, int cStart) {

// Initialize the answer array with a size equal to the number of elements

// Determine the total number of elements in the matrix

// Starting position is the first element in the result array

// If there's only one element, return the result immediately

// Directions and step increment: right, down, left, and up

int rowStep = dir[0], colStep = dir[1], steps = dir[2];

int totalElements = rows * cols;

if (totalElements == 1) {

for (int k = 1; k += 2) {

};

int[][] result = new int[totalElements][2];

int[][] directions = new int[][] {

// Iterate through each direction

for (int[] dir : directions) {

{0, 1, k}, // Move right k steps

 $\{0, -1, k + 1\}, // Move left (k+1) steps$

 $\{-1, 0, k + 1\}$ // Move up (k+1) steps

{1, 0, k}, // Move down k steps

for (int stepIncrease = 1; ; stepIncrease += 2) {

// Go through each of the four directions

// Update the starting position

return result;

startRow += rowIncrement;

startCol += colIncrement;

// Move the number of steps in the current direction

if (result.size() == totalCells) {

// Check if the new position is within the matrix bounds

// If we've added all cells, return the result

result.push_back({startRow, startCol}); // Add to result

if (startRow >= 0 && startRow < rows && startCol >= 0 && startCol < cols) {</pre>

for (auto& dir : directions) {

int steps = dir[2];

while (steps-- > 0) {

int rowIncrement = dir[0];

int colIncrement = dir[1];

// Directions are East, South, West, North.

result[0] = new int[] {rStart, cStart};

This example demonstrated the simulated spiral movement through a grid following the solution approach outlined.

12 k = 113 14 # Continue generating the spiral pattern until we've filled the result with all cells 15 while True:

10

11

16

6

9

10

11

17

18

19

20

21

22

23

24

25

26

27

28

29

30

15

16

17

18

19

20

21

22

23

24

25

26

27

28

29

30

31

32

33

34

35

36

37

38

39

class Solution:

```
# 'dr' and 'dc' represent the change to rows and cols respectively
17
               # 'dk' represents how many steps we take in each direction before turning
18
19
               for dr, dc, dk in [[0, 1, k], [1, 0, k], [0, -1, k + 1], [-1, 0, k + 1]]:
                   # Repeat the movement 'dk' times for the current orientation
20
                   for _ in range(dk):
21
22
                       # Update the current position
23
                       r start += dr
24
                       c_start += dc
25
                       # If we're still within the bounds of the matrix, add to result
26
                       if 0 <= r_start < rows and 0 <= c_start < cols:</pre>
27
                           result.append([r_start, c_start])
                           # If the result is now filled with all matrix cells, return it
28
29
                           if len(result) == rows * cols:
30
                               return result
31
               # Increment 'k' for the next spiral arm to have the correct step count
32
               k += 2
33
34 # The return type should be List[List[int]], but this cannot be used directly in a code snippet
35 # without importing List from typing. Be sure to include that in your actual implementation.
Make sure to include the import statement for List from the typing module at the beginning of your code if you're running this
outside of LeetCode's environment where the import might be implicit:
1 from typing import List
Java Solution
    class Solution {
```

12 return result; 13 14 15 int index = 1; // Start from the second element in the result array 16

// Loop indefinitely; the exit condition is when all matrix elements have been added to result

```
31
                     // Move within the current direction for 'steps' times
 32
                     while (steps-- > 0) {
 33
                         // Move to the next cell in the current direction
 34
                         rStart += rowStep;
 35
                         cStart += colStep;
 36
 37
                         // Check if the current cell is within the boundaries of the matrix
                         if (rStart >= 0 && rStart < rows && cStart >= 0 && cStart < cols) {</pre>
 38
 39
                             // Add the current cell to the result
 40
                             result[index++] = new int[] {rStart, cStart};
                             // If we've added all matrix elements to the result, return the result
 41
 42
                             if (index == totalElements) {
 43
                                 return result;
 44
 45
 46
 47
 48
 49
 50
 51
C++ Solution
  1 class Solution {
  2 public:
         vector<vector<int>> spiralMatrixIII(int rows, int cols, int startRow, int startCol) {
             int totalCells = rows * cols; // Total number of cells in the matrix
             vector<vector<int>> result; // This will store the path of the spiral
             result.push_back({startRow, startCol}); // Starting position
  8
             // If there is only one cell in the matrix, return the result now
             if (totalCells == 1) {
  9
 10
                 return result;
 11
 12
 13
             // Spiral can be formed by increasing the steps in the east and north directions,
 14
             // and then increasing by an additional step when moving west and south.
```

// The third value in each vector holds the number of steps to take in that direction.

{1, 0, stepIncrease}, // Move down (South)

// 'dir' is vector<int> that contains the row increment, column increment, and number of steps.

{0, −1, stepIncrease + 1}, // Move left (West)

{-1, 0, stepIncrease + 1}}; // Move up (North)

vector<vector<int>> directions = {{0, 1, stepIncrease}, // Move right (East)

40 41 42 43 44

```
45
 46
 47
 48
    };
 49
Typescript Solution
    function spiralMatrixIII(rows: number, cols: number, startRow: number, startCol: number): number[][] {
        // Total number of cells in the matrix
        const totalCells: number = rows * cols;
        // This will store the path of the spiral
  4
         const path: number[][] = [[startRow, startCol]];
  5
  6
        // If there is only one cell in the matrix, return the path now
        if (totalCells === 1) {
  8
             return path;
  9
 10
 11
 12
        // Loop wherein each iteration potentially adds two sides of the spiral.
 13
         for (let stepIncrease = 1; ; stepIncrease += 2) {
 14
            // Directions are East, South, West, North.
            // Each tuple contains the row and column increments, and the number of steps to take.
 15
 16
             const directions: [number, number, number][] = [
 17
                 [0, 1, stepIncrease], // Move right (East)
 18
                 [1, 0, stepIncrease], // Move down (South)
 19
                 [0, -1, stepIncrease + 1], // Move left (West)
                 [-1, 0, stepIncrease + 1] // Move up (North)
 20
 21
            1;
 22
 23
             for (const [rowIncrement, colIncrement, steps] of directions) {
 24
                 // Initialize a variable for the number of steps to be taken in the current direction
 25
                 let stepsRemaining = steps;
 26
 27
                 // Move the number of steps in the current direction
 28
                 while (stepsRemaining-- > 0) {
 29
                     // Update the starting position
 30
                     startRow += rowIncrement;
 31
                     startCol += colIncrement;
 32
                     // Check if the new position is within the matrix bounds
 33
 34
                     if (startRow >= 0 && startRow < rows && startCol >= 0 && startCol < cols) {</pre>
 35
                         // Add the new position to the path
                         path.push([startRow, startCol]);
 36
 37
                         // If we've added all cells, return the path
 38
                         if (path.length === totalCells) {
                             return path;
 41
 42
 43
 44
 45
 46
    // Example use:
```

Time and Space Complexity The given Python code generates all the coordinates in a matrix in a spiral order starting from a given cell (rStart, cStart).

space complexity of the code.

// const result = spiralMatrixIII(5, 6, 1, 4);

// console.log(result); // This would log the spiral matrix to the console.

Time Complexity: The time complexity of this function can be analyzed by understanding the number of steps taken to complete the spiral. The

number of steps increases as the spiral grows. The spiral growth is implemented by incrementing the step size k after every two

Considering each coordinate in a rows x cols grid needs to be visited exactly once, let's analyze both the time complexity and

directions (right-up and left-down). Initially, k starts at 1, and after each full cycle (right \rightarrow down \rightarrow left \rightarrow up), k is incremented by 2. This means that for a matrix that requires n cycles to fill, the total number of steps 5 would be the sum of an arithmetic series:

50

1 S = 1 + 2 + 3 + 4 + ... + (2n - 1) + 2nThis sum is equal to n(2n + 1), which is $0(n^2)$.

Since n is proportional to the larger dimension of the matrix (rows or cols), and the number of iterations required to cover all cells of

the matrix will be bound by the total number of cells, we can conclude that the time complexity is 0(max(rows, cols)^2).

Space Complexity:

The space complexity of the algorithm is determined by the amount of space needed to store the output. Since the output ans is a list of all coordinates in the matrix, it needs to store exactly rows * cols elements.

Thus, the space complexity is 0(rows * cols).