



Problem Description

The problem presents a scenario where you are given a single integer num. Your task is to find two integers whose product is either num + 1 or num + 2. These two integers should be as close to each other as possible in terms of their absolute difference - meaning the difference between the two numbers without considering whether it is positive or negative should be minimal. The final solution does not require the integers to be in any specific order, thus either of the integers can come first.

Intuition

In solving this problem, the concept of factors of a number is key. For any given number, its factors are the numbers that divide it without leaving a remainder. In this case, our target numbers are num + 1 and num + 2. We look for the pair of factors, for each of these numbers, that are closest to each other. The intuition here is that the pair of factors that are closest to each other will have the smallest absolute difference.

downwards. The square root gives us a good starting point since it is the largest number that can multiply by itself to not exceed the target. Therefore, any factor larger than the square root would result in a product larger than our target number, disqualifying it from being a correct answer. Once we have the factors for both num + 1 and num + 2, we compare their absolute differences. The pair with the smaller absolute

To efficiently find such a pair for a given target number, we can start checking from the square root of the target number and move

difference is the closest pair - this represents our final answer. The reason for checking both num + 1 and num + 2 is to fulfill the task's requirement of finding the closest integers in absolute difference.

The solution uses a straightforward approach by defining a helper function f(x) which takes a number x (which will either be num + 1

Solution Approach

or num + 2) and finds the closest divisors of x.

1. Start by calculating the integer square root of x using int(sqrt(x)). This is the starting point for finding our factors.

Here's how the f(x) function works in detail:

- 2. Iterate downwards from this square root to 1 (inclusive), as any factor greater than the square root of x would result in a product
- larger than x when multiplied with another integer. 3. In each iteration, check if x % i = 0 which is the condition to confirm if i is a factor of x.
- 4. Once a factor is found, calculate the pair by dividing x by the factor i. The pair will be [i, x // i]. 5. Return the pair of factors found.
- The main function closestDivisors(num: int) -> List[int] calls this helper function twice: once with num + 1 and once with num +

2.

1. The function stores the pairs returned by f(num + 1) and f(num + 2) in variables a and b respectively. 2. It then compares the absolute differences of the two integers in each pair.

- 3. The pair with the smaller absolute difference is chosen as the result.
- 4. The result pair is returned.
- Algorithmically, this is an efficient approach because it only searches up to the square root of the target numbers rather than

To summarize, the solution algorithm involves: Finding pairs of factors (divisors) for two numbers num + 1 and num + 2.

iterating through all possible divisors, which significantly reduces the number of operations, especially for very large numbers.

- Returning the pair with the smallest absolute difference between the two factors.
- Data structures used in this solution are basic and include primarily lists to store the pairs of factors. The pattern utilized here is an

Starting the search from the square root of these numbers and iterating downwards to find these pairs.

optimization over brute force where only necessary divisors are considered, which is made possible by the mathematical property

that a number's divisors are symmetrical around the square root. Example Walkthrough

Let's assume num = 8. We want to find two integers whose product is num + 1 or num + 2, which here would be 9 and 10. These two

1. We first calculate the square root of num + 1 which is sqrt(9) = 3.

2. Then, we check if there's any number from 3 down to 1 that evenly divides 9:

- The pair is formed by 3 (the divisor) and 9 // 3 = 3. So the factor pair for num + 1 is [3, 3].
- 3. Next, we calculate the square root of num + 2, which is slightly over sqrt(10) but we use int(sqrt(10)) = 3 as our starting point.
- 4. We check divisors from 3 to 1 for the number 10:

integers should have the smallest possible absolute difference. Let's apply our solution approach:

- 3 is not a divisor of 10 since 10 % 3 != 0. 2 is a divisor since 10 % 2 == 0.
- 5. Now we have two pairs: [3, 3] for num + 1 and [2, 5] for num + 2. We compare their absolute differences:

3 is a divisor of 9 since 9 % 3 == 0.

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• The absolute difference for [3, 3] is 3 - 3 = 0.
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 \circ The absolute difference for [2, 5] is 5 - 2 = 3. 6. We choose the pair with the smallest absolute difference, which is [3, 3], with an absolute difference of 0.

quickly identify the closest pair of numbers satisfying the condition without unnecessary computation.

multiplied together, yield num + 1 (which is 9) and have the smallest absolute difference. This example walk-through demonstrates the solution approach. By checking only the divisors from the square root and below, we

Define a helper function to find the pair of divisors

Return the divisor pair [i, x // i]

if (Math.abs(divisorsNumPlusOne[0] - divisorsNumPlusOne[1]) <</pre>

// Helper function that calculates the two closest divisors of 'x'

return divisorsNumPlusOne;

return divisorsNumPlusTwo;

private int[] findClosestDivisors(int x) {

} else {

Math.abs(divisorsNumPlusTwo[0] - divisorsNumPlusTwo[1])) {

vector<int> divisorsForNumPlusTwo = findClosestDivisors(num + 2);

// Determine which pair of divisors has the smallest difference

// Return the pair with the smallest difference

// Start from the square root of 'x' and check for the closest divisors by moving downwards

of a number 'x' that are closest to each other.

def find_closest_divisors(x):

The pair for num + 2 is [2, 10 // 2], which is [2, 5].

Python Solution

7. The final result is [3, 3], indicating that these are the two integers (which in this case happen to be identical) that, when

from math import sqrt class Solution: def closestDivisors(self, num: int) -> List[int]:

Start by finding the square root of 'x' and iterate backwards for i in range(int(sqrt(x)), 0, -1): 10 # If 'i' is a divisor of 'x' 11 12 if x % i == 0:

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1 from typing import List

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return [i, x // i]
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           # Find the closest divisors for 'num + 1'
           closest_divisors_num_plus_one = find_closest_divisors(num + 1)
17
18
           # Find the closest divisors for 'num + 2'
           closest_divisors_num_plus_two = find_closest_divisors(num + 2)
19
20
21
           # Compare which pair of divisors has the smallest difference
22
           # and return that pair.
23
           if abs(closest_divisors_num_plus_one[0] - closest_divisors_num_plus_one[1]) < abs(closest_divisors_num_plus_two[0] - closest_
24
               return closest_divisors_num_plus_one
           else:
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               return closest_divisors_num_plus_two
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Java Solution
   class Solution {
       // This function finds two closest divisors of the input number 'num'
       public int[] closestDivisors(int num) {
           // Find the closest divisors for the number 'num + 1'
           int[] divisorsNumPlusOne = findClosestDivisors(num + 1);
           // Find the closest divisors for the number 'num + 2'
           int[] divisorsNumPlusTwo = findClosestDivisors(num + 2);
           // Compare abs difference of divisors pairs and return the pair with the smallest difference
```

```
// If 'i' divides 'x' with no remainder, 'i' and 'x / i' are divisors of 'x'
               if (x \% i == 0) {
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                   // Found the closest divisors, return them in an array
26
                   return new int[] {i, x / i};
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30 }
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C++ Solution
 1 #include <vector>
 2 #include <cmath> // Include cmath for sqrt function
   class Solution {
   public:
       // Function to find the closest divisors of an integer 'num'
       vector<int> closestDivisors(int num) {
           // Lambda function to find the divisors closest to the square root of 'x'
           auto findClosestDivisors = [](int x) -> vector<int> {
               // Start from the largest possible factor that could be closest to sqrt of x
10
               for (int i = sqrt(x); i > 0; —i) { // Ensure i is always positive
11
                   if (x \% i == 0) {
12
                       // If i is a divisor, return the pair (i, x/i)
13
                       return vector<int>{i, x / i};
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17
               // This code should never reach here since every number has at least one pair of divisors
           };
18
19
           // Find the closest divisors for both num+1 and num+2
20
21
           vector<int> divisorsForNumPlusOne = findClosestDivisors(num + 1);
```

for (int i = (int) Math.sqrt(x); true; --i) { // the condition is always true, it breaks inside if a divisor pair is found

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// Remember to include necessary headers before using this code.
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Typescript Solution
   // Import sqrt function from Math module
   import { sqrt, abs } from 'math';
   // Function to find closest divisors of an integer 'num'
   function closestDivisors(num: number): number[] {
       // Lambda function to find the divisors closest to the square root of 'x'
       const findClosestDivisors = (x: number): number[] => {
           // Start from the largest possible factor that could be closest to sqrt of x
           for (let i = Math.floor(sqrt(x)); i > 0; --i) { // Ensure i is always positive
               if (x \% i === 0) {
                   // If i is a divisor, return the pair [i, x/i]
                   return [i, x / i];
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           // Since every number has at least one pair of divisors, this line should not be reached.
           throw new Error("No divisors found"); // To handle edge cases theoretically unreachable
16
       };
18
       // Find the closest divisors for both num+1 and num+2
19
       const divisorsForNumPlusOne: number[] = findClosestDivisors(num + 1);
20
       const divisorsForNumPlusTwo: number[] = findClosestDivisors(num + 2);
21
       // Determine which pair of divisors has the smallest difference, and return the pair with the smallest difference
       return abs(divisorsForNumPlusOne[0] - divisorsForNumPlusOne[1]) < abs(divisorsForNumPlusTwo[0] - divisorsForNumPlusTwo[1])
           ? divisorsForNumPlusOne
           : divisorsForNumPlusTwo;
```

return abs(divisorsForNumPlusOne[0] - divisorsForNumPlusOne[1]) < abs(divisorsForNumPlusTwo[0] - divisorsForNumPlusTwo[1]) ?

Time and Space Complexity

Time Complexity The time complexity of the function primarily depends on the for loop within the nested function f(x), which iterates over numbers

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22 23 24 25 26 27 }

starting from int(sqrt(x)) to 1. Since the square root function essentially reduces the number of iterations to the square root of x, the time complexity for finding

Given that the function f(x) is called twice—once for num + 1 and once for num + 2—the overall time complexity is then 0(sqrt(num + 1) + sqrt(num + 2)), which simplifies to O(sqrt(num)), as the higher order term dominates and adding 1 or 2 to num has a

The space complexity of this algorithm is 0(1), as the space used does not grow with the input size num. The only extra space used

Space Complexity

is for a handful of variables that store the divisor pairs and their differences.

the divisors would be 0(sqrt(x)).

negligible effect for large numbers.