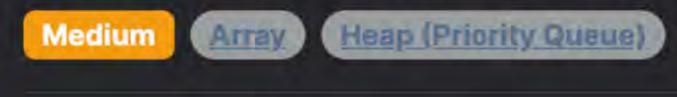
## 1962. Remove Stones to Minimize the Total



Leetcode Link

## Problem Description

also given an integer k. Your task is to perform exactly k operations on these piles, where in each operation you choose a pile and remove half of the stones in it (rounded down). The goal is to minimize the total number of stones left after all the operations have been performed. In more detail, the operation consists of choosing any piles[i] and removing floor(piles[i] / 2) stones from it. It's important to

You are given an integer array called piles, where each element piles[i] indicates the number of stones in the i-th pile. You are

note that the same pile can be chosen multiple times for successive operations. After applying k operations, your function should return the minimum possible total number of stones remaining across all piles.

Intuition

### The intuition behind the solution is to always target the pile with the largest number of stones for the reduction operation. This is

Over k operations, this strategy ensures the greatest possible reduction in the total number of stones. To effectively apply this strategy, a max-heap is used. A max-heap is a binary tree structure where the parent node is always larger than or equal to the child nodes. This property allows for the efficient retrieval of the largest element in the collection, which is

because removing half from a larger number results in a bigger absolute reduction compared to removing half from a smaller pile.

In Python, the heapq library provides a min-heap, which can be turned into a max-heap by inserting negative values. Therefore, every value inserted into the heap is negated both when it's put in and when it's taken out.

1. Negate all the elements in piles and store them in a heap to create a max-heap out of the Python min-heap implementation. 2. For k iterations, remove the biggest element from the heap (which is the most negative), negate it to get the original value, and

3. Insert back the negated new value (after halving the biggest element) into the heap.

Here's the step-by-step thought process:

exactly what's needed to find the pile with the most stones.

then remove half of it (as per the rules of the operation).

- 4. After performing k operations, the heap will contain the negated values representing the remaining stones. To get the total,
- negate the sum of the heap's contents. By always choosing the largest pile for halving, the algorithm ensures that the decrease in the total stone count is maximized with
- each operation.
- Solution Approach

The solution leverages a max-heap data structure to efficiently track and remove the largest piles first. Here's how the algorithm and data structures are utilized in the provided solution:

## are negated before being pushed onto the heap to simulate a max-heap functionality.

using heappush().

2. We iterate k times, each time performing the following steps: The root of the heap (which in this case, is the maximum element, due to negation) is popped off the heap using heappop().

1. A heap is created to maintain the current state of the piles. Since Python's heapq library implements a min-heap, the elements

pile. We then take the floor of halved value of this pile. The halving operation is conducted by adding 1 to the pile count and right-shifting (>>> 1) by one, which in essence is dividing by two and using the floor value in integer division.

This new halved number of stones is negated and pushed back onto the heap to maintain the max-heap order. This is done

Since the elements are negated when stored in the heap, we negate it back to get the actual number of stones in the largest

- The code for this loop is as follows: 1 for \_ in range(k):
- 3. Finally, after k iterations, the heap contains the negated counts of stones in each pile after the operations have been applied. To

find the answer, we sum up all the elements in the heap (which involves negating them back to positive) and return this summed

for minimizing the total number of stones.

This final step is summarized by this line of code:

value as the total minimum possible number of stones remaining.

heappush(h, -((p + 1) >> 1))

Example Walkthrough Let's consider a small example to illustrate the solution approach. Suppose we have the following piles and value of k:

• piles = [10, 4, 2, 7]

• k = 3

**Initial State** 

1 return -sum(h)

Now, let's walk through the solution step by step:

• First, we negate all the elements in piles to simulate a max-heap using Python's min-heap implementation: [-10, -4, -2, -7].

• Since -10 is the maximum value (or smallest when considering negation), it is popped from the heap. We negate it to find the

Next, we remove half of the stones in this pile. Half of 10 is 5. Since we need to negate and re-insert into the heap, we insert -5.

This approach ensures that we are always working with the largest pile available after each operation, thus optimizing our strategy

### We use the heapq library to turn this into a heap: h = [-10, -4, -2, -7].

original amount of stones: 10.

Operation 1

- Now the heap is [-7, -4, -2, -5].
- The current maximum (minimum in our negated heap) is -7. We pop it and negate it: 7. Removing half (rounded down) gives 7 / 2 which is 3 when rounded down. Negating and re-inserting -3, the heap is now [-5,

-4, -2, -3].

Operation 2

- **Operation 3**
- **Final Summation** • To get the total number of stones remaining, we sum the negated values of the heap: -( -4 + -3 + -2 + -2 ).

• The max value in our heap is now -5. We pop, negate, halve (rounding down to 2), and re-insert -2 into the heap.

from heapq import heappop, heappush class Solution: def minStoneSum(self, piles, k):

# We are inverting the values to simulate a max heap.

largest\_pile = -heappop(max\_heap)

heappush(max\_heap, -reduced\_pile)

totalStones += maxHeap.poll();

return totalStones;

// Return the total number of stones remaining after k operations

So, after performing k = 3 operations on the piles, the minimum number of stones left is 11.

# Initialize a max heap as Python only has a min heap implementation.

# Pop the largest pile and reduce its stones by half, rounded up.

# The sum of the heap is negated to return the actual sum of pile sizes.

# Push the reduced pile size back into the max heap.

reduced\_pile = (largest\_pile + 1) >> 1 # Using bit shift to divide by 2

The final state of the heap after 3 operations is [-4, -3, -2, -2].

This gives us 4 + 3 + 2 + 2 = 11 as the final answer.

### for pile in piles: # The minus sign ensures we create a max heap. 9 heappush(max\_heap, -pile) 10 11 12 # Perform 'k' operations to reduce the stones in the piles

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Python Solution

 $max_heap = []$ 

for \_ in range(k):

return -sum(max\_heap)

```
Java Solution
   class Solution {
       public int minStoneSum(int[] piles, int k) {
           // Create a max-heap to store the piles in descending order
           PriorityQueue<Integer> maxHeap = new PriorityQueue<>((a, b) -> b - a);
           // Add each pile to the max-heap
           for (int pile : piles) {
               maxHeap.offer(pile);
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           // Perform the reduction operation k times
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           while (k-->0) {
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               // Retrieve and remove the largest pile from the heap
               int largestPile = maxHeap.poll();
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               // Calculate the reduced number of stones and add back to the heap
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               maxHeap.offer((largestPile + 1) >> 1);
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           // Calculate the total number of stones after k reductions
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           int totalStones = 0;
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           while (!maxHeap.isEmpty()) {
               // Remove the stones from the heap and add them to the total count
```

### int minStoneSum(vector<int>& piles, int k) { // Create a max-heap to keep track of the stones in the piles priority\_queue<int> maxHeap;

public:

C++ Solution

#include <vector>

#include <queue>

class Solution {

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           // Populate the max-heap with the number of stones in each pile
           for (int pile : piles) {
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               maxHeap.push(pile);
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           // Perform the operation k times
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           while (k-- > 0) {
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               // Retrieve the pile with the most stones
               int largestPile = maxHeap.top();
               maxHeap.pop();
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               // Remove half of the stones from the largest pile, round up if necessary
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               maxHeap.push((largestPile + 1) / 2);
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           // Calculate the remaining number of stones after k operations
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           int remainingStones = 0;
           while (!maxHeap.empty()) {
               remainingStones += maxHeap.top();
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               maxHeap.pop();
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           // Return the total number of remaining stones
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           return remainingStones;
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35 };
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Typescript Solution
 1 // Import the necessary components for Heap
   import { Heap } from 'collections/heap.js'; // This library or similar would need to be imported for heap functionality.
   // Function signature in TypeScript with types defined
   function minStoneSum(piles: number[], k: number): number {
       // Create a max-heap to keep track of the stones in the piles
       let maxHeap = new Heap<number>(piles, null, (a: number, b: number) => b - a);
```

### while (maxHeap.length > 0) { remainingStones += maxHeap.pop(); 21 22 23 24 // Return the total number of remaining stones return remainingStones;

**Time Complexity** 

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# Time and Space Complexity

// Perform the operation 'k' times

// Retrieve the pile with the most stones

maxHeap.push(Math.ceil(largestPile / 2));

// Calculate the remaining number of stones after 'k' operations

for (let i = 0; i < k; i++) {

let remainingStones = 0;

# 1. Converting the list piles into a heap: This operation is O(n) where n is the length of piles.

31 // heap structure to use this function as intended.

2. The main loop which is executed k times: The heap operation heappop: Each pop operation has a complexity of O(log n).

The time complexity of the given code is determined by the following major operations:

// Note that the `Heap` class I'm using above does not exist in default JavaScript/TypeScript and must be imported

// You'll need to find a suitable library with heap implementation, or you would have to implement your own

// from a library that provides heap data structure implementation. The example uses a fictional 'collections/heap.js'.

let largestPile = maxHeap.pop(); // Assumes that Heap.pop retrieves the max element

// Remove half of the stones from the largest pile, round up if necessary

Therefore, the overall time complexity of the loop is 0(k \* log n). Combining this with the heap conversion, the total time complexity is 0(n + k \* log n).

• The update and heappush back into the heap: These have a complexity of O(log n) for each push operation.

**Space Complexity** 

The space complexity is determined by the space needed to store the heap. Since we are not using any additional data structures that grow with input size other than the heap, the space complexity is O(n), where n is the length of the list piles.