325. Maximum Size Subarray Sum Equals k

Prefix Sum Medium <u>Array</u> Hash Table

Problem Description

exactly equal to the given integer k. A subarray is a contiguous part of an array. If such a subarray doesn't exist, we should return 0.

The problem asks us to find the maximum length of a subarray from the given array nums, such that the sum of its elements is

To clarify with an example, let's say our array is [1, -1, 5, -2, 3] and k is 3. The subarray [1, -1, 5, -2] sums to 3, and its length is 4, which would be the answer because there's no longer subarray that sums to 3.

a certain point, and determine if there is a previous point where the sum was exactly k less than the current sum. If we can find such a place, then the elements between these two points form a subarray that sums to k.

The intuition behind the solution lies in the use of a running sum and a hash table (or dictionary in Python). As we iterate through

To approach this problem, we need to find a way to efficiently look up the sum of elements from the beginning of the array up to

the array, we keep track of the cumulative sum of elements. The hash table stores the earliest index at which each cumulative

Intuition

sum appears. Here's the reasoning: • Start with a hash table d that maps a cumulative sum to the first index where it appears. Initialize it with the pair (0: -1), which says the sum

o is achieved before the first element.

• Initialize variables for the current sum (s) and the maximum length found (ans) to 0. • Iterate through nums, updating the running total s by adding each element x to it.

• Check if s - k has been seen before. If it has, we've found a subarray ending at the current index with a sum of k.

- Update ans with the length of this subarray if it is longer than the maximum found so far.
- Add the current sum to the hash table with its corresponding index, but only if this sum hasn't been seen before to maintain the earliest index.

of the same sum would yield a shorter subarray.

Here's a detailed walkthrough of the implementation:

The reason we only store the earliest occurrence of a sum is because we're looking for the longest subarray; any later occurrence

Solution Approach The solution leverages a hashing strategy to efficiently track the sum of elements in the subarrays and their starting indices.

Hash Table Initialization: We initiate a hash table (dictionary in Python) named d with a key-value pair {0: -1}. This

represents that the sum ∅ is achieved before starting the iterations, essentially before the first element at index -1. This base case ensures that if the sum of elements from the beginning reaches k, the length can be calculated correctly.

Preparing Variables: Two variables are prepared: ans to store the maximum length of the subarray with sum k found so far

Checking for a Matching Subarray: During each iteration, after updating the running sum, we check if s - k is present in the

before. We do this because we are interested in the first occurrence of this running sum to ensure the longest possible

- and s to keep track of the running sum. **Iteration & Running Sum:** We use a loop to iterate over the array using enumerate(nums) which gives us both the index i and the value x. We increment the running sum s by the value of x.
- hash table d. If it is, it means that from the earliest index d[s k] to the current index i, the elements sum up exactly to k. We then compare (i - d[s - k]) with ans and store the larger one in ans. Updating the Hash Table: The hash table is updated with the running sum only if this running sum has not been recorded
- subarray. Returning the Result: After the loop ends, ans will be holding the length of the longest subarray that sums to k. This value is returned as the final result.
- since it processes each element of nums just once. The space complexity is also 0(n) in the worst case, as it might store each sum occurring in the array.

This algorithm effectively uses the hashing technique to reduce the time complexity otherwise inevitable with brute force

solutions. By using a hash table to record the first occurrence of each sum, the solution approaches an O(n) time complexity,

Let's use the solution approach to walk through a small example. Consider the array nums = [3, 4, -3, 2, 1] and the target sum k = 3. Hash Table Initialization: Initialize a hash table d with {0: −1}. This signifies that before we start, the cumulative sum of 0 is

Iteration & Running Sum:

reached at an index before the array starts.

occurrences with the indices 0, 1, 2, and 3.

def maxSubArravLen(self, nums: List[int], target: int) -> int:

Initialize a dictionary to store the cumulative sum up to all indices

Check if there is a subarray whose sum equals 'target'

Return the maximum length of subarray found that adds up to 'target'

Initialize variables to store the maximum length of subarray and the cumulative sum

If this cumulative sum has not been seen before, add it to the dictionary

k = 3. This is our final result.

Solution Implementation

 $sum_to_index = \{0: -1\}$

max_length = cumulative_sum = 0

cumulative_sum += num

Iterate through the list of numbers

if cumulative sum not in sum to index:

sumToIndexMap.putIfAbsent(sum, i);

return maxLength;

#include <algorithm> // For using max function

long long cumulativeSum = 0;

int maxSubArrayLen(vector<int>& nums, int k) {

for (int i = 0; i < nums.size(); ++i) {</pre>

cumulativeSum += nums[i];

// Return the maximum length found.

// Return the maximum length of the subarray found

// Create a hashmap to store the cumulative sum and its index.

// Initialize variables to store the cumulative sum 's' and max length 'maxLen'.

maxLen = max(maxLen, i - indexByCumulativeSum[cumulativeSum - k]);

// This ensures we keep the smallest index to get the longest subarray.

Initialize variables to store the maximum length of subarray and the cumulative sum

max_length = max(max_length, index - sum_to_index[cumulative_sum - target])

operations: arithmetic operations, dictionary lookup and dictionary insertion (when s is not already in d).

If this cumulative sum has not been seen before, add it to the dictionary

Check if there is a subarrav whose sum equals 'target'

Return the maximum length of subarray found that adds up to 'target'

if (cumulative sum - target) in sum to index:

sum_to_index[cumulative_sum] = index

if cumulative sum not in sum to index:

// If the current cumulative sum minus 'k' is found in the map, we found a subarray.

// Only add the current cumulative sum and its index to the map if it's not already there.

unordered map<long long, int> indexBvCumulativeSum{{0, -1}};

// Loop through the array to compute the cumulative sum.

if (indexByCumulativeSum.count(cumulativeSum - k)) {

if (!indexByCumulativeSum.count(cumulativeSum)) {

indexByCumulativeSum[cumulativeSum] = i;

sum_to_index[cumulative_sum] = index

for index. num in enumerate(nums):

Update the cumulative sum

Example Walkthrough

ans to 1 - (-1) = 2. \circ For the second element 4, s becomes 7. We look for s - k = 4 in the hash table, but it's not there, so no change to ans. \circ For the third element -3, s is now 4. We look for s - k = 1 which is not in the hash table, non update to ans.

 \circ For the fourth element 2, s becomes 6. We look for s - k = 3, and since it's not present, no update to ans. \circ For the last element 1, s increases to 7. We look for s - k = 4. It has appeared before when s was 7 for the second element. The index then was 1. Now, the index is 4, so the length of the subarray is 4 - 1 = 3 which is greater than the current ans, so we update ans to 3.

Checking for a Matching Subarray: Every iteration includes this check. We successfully find a matching sum during the first

Updating the Hash Table: As we proceed, we update the hash table with the sums 3, 7, 4, and 6 at their respective first

Returning the Result: At the end of the iteration, ans holds the value 3, which is the length of the longest subarray with sum

 \circ For the first element 3, the running sum s becomes 3. Since $s - k = 3 - 3 = \emptyset$ and the hash table contains \emptyset with index -1, we update

and last elements.

Preparing Variables: The variables ans (maximum subarray length) and s (running sum) are both set to 0.

- The correct subarray that has the sum of 3 and the maximum length is [4, -3, 2]. The running sum at the start of this subarray was $\frac{4}{1}$, and by adding the subarray elements, it became $\frac{7}{1}$. The subarray has $\frac{3}{1}$ elements, hence $\frac{1}{1}$ is returned.
- **Python** class Solution:

if (cumulative sum - target) in sum to index: # Update max length with the larger of the previous max length and the current subarray length max_length = max(max_length, index - sum_to_index[cumulative_sum - target])

return max_length

```
Java
import java.util.HashMap;
import java.util.Map;
class Solution {
    public int maxSubArrayLen(int[] nums, int k) {
        // Create a hashmap to store the sum up to the current index as the key
        // and the index as the value.
        Map<Long. Integer> sumToIndexMap = new HashMap<>();
        // Initialize the map with base case: a sum of 0 before index -1
        sumToIndexMap.put(0L, -1);
        // This will hold the maximum length of the subarray found so far
        int maxLength = 0;
        // This will keep track of the running sum
        long sum = 0;
        // Loop through every element in the array
        for (int i = 0; i < nums.length; ++i) {
            // Update the running sum with the current element
            sum += nums[i];
            // If a subarray ending at index i has a sum of (sum - k),
            // then a subarray with sum k exists.
            if (sumToIndexMap.containsKev(sum - k)) {
                // Compare and store the maximum length found so far
                maxLength = Math.max(maxLength, i - sumToIndexMap.get(sum - k));
            // If the current sum has not been seen before,
            // add it to the map with the corresponding index.
```

};

C++

public:

#include <vector>

class Solution {

#include <unordered map>

int maxLen = 0;

return maxLen;

```
TypeScript
/**
* Finds the maximum length of a subarray with a sum equal to k.
 * @param nums - The input array of numbers.
 * @param k - The target sum to look for.
 * @returns The length of the longest subarray which sums to k.
function maxSubArrayLen(nums: number[], k: number): number {
    // Initialize a map to store the cumulative sum as the key and its index as the value.
    const cumSumIndexMap: Map<number, number> = new Map();
    cumSumIndexMap.set(0, -1); // Base case: set the sum of an empty subarray before the first element to -1.
    let maxLength = 0; // Initialize the maximum subarray length to zero.
    let cumulativeSum = 0; // Variable to store the cumulative sum of elements.
    // Iterate over the elements of the array.
    for (let i = 0; i < nums.length; ++i) {
        cumulativeSum += nums[i]; // Increment the cumulative sum with the current element.
        // If cumulativeSum - k exists in the map, there's a subarray with sum k ending at the current index.
        if (cumSumIndexMap.has(cumulativeSum - k)) {
            // Update maxLength with the higher value between the previous maxLength and the new subarray length.
            maxLength = Math.max(maxLength, i - cumSumIndexMap.get(cumulativeSum - k)!);
       // If the current cumulativeSum isn't in the map, set it with the current index.
        if (!cumSumIndexMap.has(cumulativeSum)) {
            cumSumIndexMap.set(cumulativeSum, i);
    // Return the maxLength found.
    return maxLength;
class Solution:
    def maxSubArravLen(self, nums: List[int], target: int) -> int:
       # Initialize a dictionary to store the cumulative sum up to all indices
        sum_to_index = \{0: -1\}
```

Time and Space Complexity

return max length

max_length = cumulative_sum = 0

cumulative_sum += num

Iterate through the list of numbers

for index. num in enumerate(nums):

Update the cumulative sum

The provided Python code finds the length of the longest subarray which sums up to k. It makes use of a hashmap (dictionary in Python terms) to store the cumulative sum at each index, which helps in finding subarrays that sum up to k in constant time. **Time Complexity**

The time complexity of the code is O(n), where n is the number of elements in the input list nums. This is because the algorithm

iterates through the list once, and for each element it performs a constant time operation of adding the element to the running

sum, checking if (s - k) is in the dictionary d and updating the maximum length ans. All these operations are constant time

Update max length with the larger of the previous max length and the current subarray length

Space Complexity

The space complexity of the code is 0(n). In the worst case, every running sum is unique, and hence, each sum (represented by s in the code) would be stored in the dictionary d along with its corresponding index. Since there are n such running sums in the worst case, the dictionary could contain up to n key-value pairs.