# Problem Description

subsequence is one that satisfies two conditions. First, it must be a subsequence of s, which means it can be formed by removing some or no characters from s without changing the order of the remaining characters. Second, for every pair of adjacent letters in this subsequence, the absolute difference in their alphabetical order must be less than or equal to a given integer k. To explain further, a subsequence is different from a substring since a substring is contiguous and appears in the same order within

The LeetCode problem presented asks us to find the length of the longest ideal subsequence from a given string s. An ideal

the original string, whereas a subsequence is not required to be contiguous but must appear in the same relative order.

Leetcode Link

The problem statement also clarifies that the alphabetical order difference isn't cyclic, meaning that the difference between a and z is considered to be 25, not 1.

Intuition

#### To solve this problem, we can use dynamic programming, which involves breaking the problem into smaller subproblems and solving each subproblem just once, storing the solution in a table for easy access when solving subsequent subproblems.

The intuition behind the approach is to consider each character in the string s one by one and determine the length of the longest ideal subsequence ending with that character. For each character, we need to find the previous character in the subsequence that

can be connected to it (based on the condition about the alphabetical difference) for which the subsequence length is the longest

possible. We create a dictionary d that keeps track of the last occurrence index for each character that can be a candidate for forming a subsequence. We also maintain an array dp where dp[i] represents the length of the longest ideal subsequence ending at s[i]. For each character s[i] in the string, we iterate over every lowercase letter and check if it can form a sequence with s[i], satisfying

the absolute difference condition. If it's a valid character, we update dp[i] to the maximum of its current value or 1 plus the length of the subsequence ending with the valid character found in our dictionary d. By doing this iteratively, we build upon the solutions of the subproblems until we reach the end of the string. Finally, the answer is the maximum value in the dp array, which represents the

Solution Approach The implementation of the solution provided follows the dynamic programming approach to tackle the problem of finding the longest ideal subsequence.

Firstly, we initialize an array dp with all elements as 1, because the minimum length of an ideal subsequence that can end at any

### character is at least 1 - the character itself. We also create a dictionary d to keep track of the last index where each character occurred while checking the sequence.

ideal subsequence.

s[i]).

length of the longest ideal subsequence we can obtain from s.

Inside the outer loop is an inner loop: for b in ascii\_lowercase:

To illustrate the solution approach, we'll walk through the example step-by-step:

The core of the solution code is a nested loop. The outer loop iterates through the string s, and the inner loop iterates through all lowercase ASCII letters to check whether they can form an ideal subsequence with the current character s[1]. Here's a breakdown of each element of the code:

• n = len(s): We determine the length of the given string s. dp = [1] \* n: Creates a list dp with n elements, all initialized to 1. • d = {s[0]: 0}: Initializes the dictionary d with the first character of the string s as the key and 0 as its index.

• for i in range(1, n): Outer loop to traverse the string s starting from index 1 since index 0 is used for initialization.

means they cannot form an ideal sequence. o if b in d: If character b is within the difference k, and it's in dictionary d, then it's a candidate for creating or extending an

abs(a - ord(b)) > k: Checks if the absolute difference between the ASCII values of the characters is greater than k, which

a = ord(s[i]): Converts the current character s[i] to its ASCII value to facilitate comparison based on alphabetical order.

- dp[i] = max(dp[i], dp[d[b]] + 1): Here, the dynamic programming comes into play. We update the dp[i] with the maximum of its current value or the length of the ideal subsequence ending with b plus one (to include the current character
- d[s[i]] = i: We update or add the current character and its index to dictionary d to keep track of the last position it was seen. • return max(dp): After filling the dp table, the length of the longest ideal subsequence will be the maximum value in the dp list.
- finds the longest one possible. Example Walkthrough

Let's consider a string s = "abcd" and k = 2, which signifies the maximum allowed absolute difference in the alphabetical order.

2. Starting Point: With s[0] = 'a', we initialize d with {'a': 0}. Since 'a' is the first character, dp[0] = 1.

By keeping track of the ideal subsequences ending with different characters and building upon each other, this algorithm efficiently

1. Initialization: We have n = 4 since the length of s is 4. We create a dp list of length n initialized with all 1s because the minimum subsequence length ending at each character is 1 (the character itself). We also have a dictionary, d, which will keep track of the

# 3. Iteration with i = 1 for s[i] = 'b':

last seen index for each character.

'a' can form an ideal subsequence with 'b'.

max(dp[2], dp['b' index] + 1), which is 3.

- Thus, we update dp[1] with the maximum of dp[1] and dp['a' index] + 1. Since dp[0] = 1, this means dp[1] becomes 2. Update d to include 'b': 1.
  - We check 'a' and 'b' to form an ideal subsequence with 'c'. Both are within k distance. Since both 'a' and 'b' can precede 'c', we choose the one that provides the longest subsequence. dp [2] is updated to

We check if 'a' can form an ideal subsequence with 'b'. Since abs(ord('a') - ord('b')) = 1 which is less than or equal to k,

• We again choose the best predecessor, which is 'c' in this case. We update dp[3] to max(dp[3], dp['c' index] + 1), which

from string import ascii\_lowercase

dp = [1] \* string\_length

last\_index\_dict = {s[0]: 0}

for i in range(1, string\_length):

for b in ascii lowercase:

continue

last\_index\_dict[s[i]] = i

current\_char\_ascii = ord(s[i])

Update d to include 'c': 2.

5. Iteration with i = 3 for s[i] = 'd':

4. Iteration with i = 2 for s[i] = 'c':

6. Finish: We have processed all characters in s. The dp array is [1, 2, 3, 4], and thus the length of the longest ideal

preceding characters provide the longer ideal subsequence according to the k condition.

# Iterate through the string starting from the first character

# Get the ascii value of the current character

if abs(current\_char\_ascii - ord(b)) > k:

# Update the last index for the current character

Repeat the above step for 'd', checking 'a', 'b', and 'c'. Again, all are within k distance.

class Solution: def longestIdealString(self, s: str, k: int) -> int: # The length of the input string string\_length = len(s) # Initialize the dp array where dp[i] represents the length of the longest ideal substring ending at index i

# Loop through all lowercase letters to find characters within the ideal distance from the current character

# Dictionary to keep track of the last index of each character we have encountered so far.

# If the ascii difference is greater than k, skip this character

// Update the last seen index of the current character to be the current index.

// Return the length of the longest ideal string that can be formed from the input string.

longestLength = Math.max(longestLength, dynamicProgramming[i]);

lastSeenCharacterMap.put(currentChar, i);

# If the character is within the ideal distance and we've seen this character before

# Return the maximum value in the dp array which represents the length of the longest ideal substring

strings with repeating characters or larger alphabetic differences, we would see more variation in the dp updates based on which

#### 25 if b in last\_index\_dict: 26 # Update the dp value by considering the length of the ideal substring ending at the last index of character b pl 27 dp[i] = max(dp[i], dp[last\_index\_dict[b]] + 1) 28

Python Solution

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return max(dp)
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Java Solution
   class Solution {
       public int longestIdealString(String s, int k) {
            int lengthOfString = s.length(); // The length of the string s.
            int longestLength = 1; // Initialize the answer to 1 character as the minimum length of ideal string.
           int[] dynamicProgramming = new int[lengthOfString]; // Array to store the length of the longest ideal substring ending at eac
           Arrays.fill(dynamicProgramming, 1); // At minimum, each character itself is an ideal string.
           // HashMap to keep track of the last index of each character that is part of the longest ideal string so far.
           Map<Character, Integer> lastSeenCharacterMap = new HashMap<>(26);
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           // Place the first character in the map to start the process.
            lastSeenCharacterMap.put(s.charAt(0), 0);
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           // Iterate through each character in the string starting from the second character.
            for (int i = 1; i < lengthOfString; ++i) {</pre>
               char currentChar = s.charAt(i); // The current character for which we are finding the ideal string.
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               // Check closeness of every character in the alphabet to the current character within the limit k.
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               for (char prevChar = 'a'; prevChar <= 'z'; ++prevChar) {</pre>
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                    // If the absolute difference in ASCII value is within the limit k, we proceed.
21
                   if (Math.abs(currentChar - prevChar) > k) {
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                        continue;
                   // If the previous character has been seen and is part of an ideal string,
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                   // we update the DP table by taking the max of the current dp value or
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                   // the dp value of the previous character's last index plus one.
27
                   if (lastSeenCharacterMap.containsKey(prevChar)) {
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dynamicProgramming[i] = Math.max(dynamicProgramming[i], dynamicProgramming[lastSeenCharacterMap.get(prevChar)] +

// Update longestLength to be the maximum of itself and the current length of the longest ideal string ending at i.

## 1 class Solution { 2 public:

C++ Solution

return longestLength;

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int longestIdealString(string s, int k) {
            int stringLength = s.size(); // The length of the input string
            int longestLength = 1; // Initialize the longest length with 1, as the minimum ideal string length is 1
           vector<int> dp(stringLength, 1); // Dynamic programming table with a base case of 1 for each character
           unordered_map<char, int> lastOccurrence; // Stores the last occurrence index of each character encountered
           // Initialize the last occurrence for the first character in the string
            lastOccurrence[s[0]] = 0;
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           // Iterate over the string starting from the second character
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            for (int i = 1; i < stringLength; ++i) {
                char currentChar = s[i]; // Current character being processed
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               // Try extending the ideal string including all characters within 'k' distance of current character
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               for (char otherChar = 'a'; otherChar <= 'z'; ++otherChar) {
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                   // If the other character is more than 'k' distance away, skip it
18
                   if (abs(currentChar - otherChar) > k) continue;
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                   // Check if we have seen the other character before and extend the ideal string length if possible
22
                   if (lastOccurrence.count(otherChar))
                       dp[i] = max(dp[i], dp[lastOccurrence[otherChar]] + 1);
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               // Update the last occurrence index for the current character
                lastOccurrence[currentChar] = i;
27
               // Update the longest length found so far
29
                longestLength = max(longestLength, dp[i]);
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           // Return the length of the longest ideal string found
34
           return longestLength;
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36 };
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Typescript Solution
   function longestIdealString(s: string, k: number): number {
       // Create a dynamic programming array initialized to 0.
       // This array represents the length of the longest ideal subsequence ending with each letter.
       const longestSubseqLengths = new Array(26).fill(0);
```

// Iterate over each character in the input string. for (const char of s) { // Get the index (0-25) corresponding to the current character. const index = char.charCodeAt(0) - 'a'.charCodeAt(0); 9 // Temporary variable to hold the maximum subsequence length found so far. 10 let maxLength = 0; 11 12 13 // Iterate over all possible characters to update the current character's maximum length. 14 for (let i = 0; i < 26; i++) { 15 // If the current character is within 'k' distance of character at index 'i' // in the alphabet, update the max length if a longer subsequence is found. 16 17 if (Math.abs(index - i) <= k) {</pre> maxLength = Math.max(maxLength, longestSubseqLengths[i] + 1); 18 19 20 21 22 // Update the longest subsequence length ending with the current character. 23 longestSubseqLengths[index] = Math.max(longestSubseqLengths[index], maxLength); 24 25 26 // Return the maximum value in the dynamic programming array,

of k because it checks all possibilities within the range) to find characters within the allowed difference k. Therefore, we look at all possible 26 characters for each of the n positions in the worst case. Additionally, for each character b in ascii\_lowercase, we look up in dictionary d which has an average-case lookup time of 0(1). Hence, we multiply 26 by this constant lookup time, which doesn't change the O-notation. The space complexity of the code is O(n) because the dp array is of size n, where n is the size of the input string s. The dictionary d

also stores up to n index values for all unique characters that have been seen. In this case, the number of unique keys in the

complexity which is dominated by the dp array.

dictionary is bounded by the size of the ascii\_lowercase set, which is a constant (26), so it does not change the overall space

allowed for the ideal string. For each character in the string s, the code iterates over all 26 letters in the ascii\_lowercase (regardless

// which is the length of the longest ideal subsequence found. 27 28 return longestSubseqLengths.reduce((maxValue, currentLength) => Math.max(maxValue, currentLength), 0); 29 } 30 Time and Space Complexity The time complexity of the given code is 0(n \* 26 \* k) where n is the length of the input string s and k is the maximum difference

is 4. Update d to include 'd': 3. subsequence is max(dp) which is 4. In this example, the longest ideal subsequence we can form from "abcd" with k = 2 is "abcd" itself, with the length of 4. However, for