## 2064. Minimized Maximum of Products Distributed to Any Store



**Problem Description** 

**Leetcode Link** 

number of product types, denoted by an array quantities where each entry quantities[i] represents the amount available for the i-th product type. The objective is to distribute these products to the stores following certain rules: Each store can receive at most one product type.

The problem presents a scenario where there is a given number of specialty retail stores, denoted by an integer n, and a certain

have after the distribution is completed.

The goal is to minimize the maximum number of products given to any single store.

A store can receive any amount of the one product type it is given.

product as possible, in order to minimize potential waste or overstock.

In simple terms, you are asked to find the smallest number x which represents the maximum number of products that any store will

This situation is akin to finding the most balanced way of distributing products such that the store with the largest stock has as little

The solution involves using a binary search algorithm. The key insight here is that if we can determine a minimum possible x such

## Here's the reasoning process:

• We know that the value of x must be between 1 (if there's at least one store for each product) and the maximum quantity in quantities (if there's only one store).

• To test if a given x is valid, we check if all products can be distributed to stores without any store getting more than x products.

- exceed n. The check function in the provided code snippet helps with this validation by returning True if a given x allows for all the products to
- be distributed within the n stores.

that all products can be distributed without exceeding x products in any store, we have our answer.

• Using binary search, we can quickly narrow down the range to find the smallest possible x.

The Python bisect\_left function is used to perform the binary search efficiently. It returns the index of the first element in the given range that matches True when passed to the check function. This means it effectively finds the lowest number x such that check(x) is true, which is our desired minimum possible maximum number of products per store (x).

Solution Approach

Binary search is an optimal choice here because it allows for a significant reduction in the number of guesses needed compared to linear search, especially when there's a large range of possible values for x.

• The binary search is used to find the minimum x such that all products can be distributed according to the rules. It is

The solution adopts a binary search algorithm to efficiently find the minimum value of x that satisfies the distribution conditions.

#### products within the available stores. • For each product type in quantities, the function calculates the number of stores required by dividing the quantity of that

- The Python function bisect\_left from the bisect module is employed to perform the binary search. The function takes in a range, a target value (True in this case, as check returns a boolean), and a key function (check). The key function is called with each mid-value during the search to determine if x is too high or too low.
- the key function effectively turns the range into a sorted boolean array (False for values below our target and True for values at or above it), the position i represents the smallest x for which check(x) is True. 4. Outcome: • The value of x found by the bisect\_left search is incremented by 1 because the range is 0-indexed, whereas the quantities

bisect\_left will find the position i to insert the target value (True) in the range in order to maintain the sorted order. Since

• The possible values for x start with a lower bound of 1, and an upper bound of 10\*\*6. 2. First Mid-point Check:

 $\circ$  We run the check function with x = 5. We need one store for the first product type (3/5 rounded up is still 1 store), two

point to start could be 500,000. However, for the sake of example, we'll use 5 as it's a more illustrative number.

Let's pick a mid-point for x during the binary search. Since our bounds are 1 and 10\*\*6, a computationally reasonable mid-

• Since 5 is too small, we adjust our search range. The next mid-point we check is halfway between 5 and 10\*\*6, but again as

Let's consider an example where we have n = 2 specialty retail stores and quantities = [3, 6, 14] for the product types.

### stores for the second product type (6/5 rounded up is 2 stores), and three stores for the third product type (14/5 rounded up is 3 stores).

1. Binary Search Initialization:

 Since we can't distribute the products without exceeding 5 products in any store with only 2 stores, check(5) returns False. 3. Adjusting the Search Range:

exactly 2 stores), totaling 1 + 1 + 2 = 4 stores. This is still more than 2 stores, so check(7) returns False.

#### $\circ$ We run the check function with x = 7. This time we would need 1 store for the first product type (3/7 rounded up is still 1 store), 1 store for the second product type (6/7 rounded up is still 1 store), and 2 stores for the third product type (14/7 is

this is an example, we choose 7.

Continuing the binary search, let's try x = 10.

- requires 1 store (6/10 rounded up is still 1 store), and the third product type requires 2 stores (14/10 rounded up is 2 stores). The total is 1 + 1 + 2 = 4 stores, which is still too many. However, if we check x = 15, we see that each product type would only require 1 store: (3/15, 6/15, 14/15 all round up to 1
- stores, which matches n = 2. • Since check(20) returns True and we cannot go lower than 20 without needing more stores than we have, 20 is our smallest possible x.

In practice, the binary search would proceed by narrowing down the range between the values where check returns False and where

check returns True. In our manually stepped-through example, x = 20 is the solution. This means that we can distribute the products

to the 2 stores in such a way that no store has more than 20 products, thereby minimizing the maximum number of products per

Now running check(20), each product type will require only 1 store: (3/20, 6/20, 14/20 all round up to 1). The sum is exactly 2

# Calculate the total number of stores required if each store can hold up to 'x' # items. The expression (quantity + x - 1) // x is used to ceiling divide the quantity # by x to find out how many stores are required for each quantity. total\_stores\_needed = sum((quantity + x - 1) // x for quantity in quantities)# Check if the total number of stores needed does not exceed the available 'n' stores.

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• Running check(10), the first product type requires 1 store (3/10 rounded up is still 1 store), the second product type also
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 $\circ$  Finally, we try  $\times = 20$ .

4. Finding the Valid x:

- 1 from bisect import bisect\_left 2 from typing import List
  - def minimizedMaximum(self, n: int, quantities: List[int]) -> int: # Define a check function that will be used to determine if a specific value of 'x' # allows distributing all the quantities within 'n' stores such that the maximum # quantity in any store does not exceed 'x'. def is\_distribution\_possible(x):
  - return total\_stores\_needed <= n</pre>
    - # the items does not exceed the number of stores. We search in the range from 1 to 10\*\*6 # as an upper limit, assuming that the maximum quantity per store will not exceed 10\*\*6. # The second argument to bisect\_left is 'True' because we are interested in finding the point # where the 'is\_distribution\_possible' function returns 'True'. min\_max\_quantity = 1 + bisect\_left(range(1, 10\*\*6), True, key=is\_distribution\_possible)
  - # Return the smallest possible maximum quantity that can be put in a store. return min\_max\_quantity
  - class Solution { public int minimizedMaximum(int stores, int[] products) { // Initial search space: the lowest possible maximum is 1 (each store can have at least one of any product),
- // Each store can take 'mid' amount, calculate how many stores are required 18 19 // for this particular product, rounding up count += (quantity + mid - 1) / mid;

// If we can distribute all products to 'stores' or less with 'mid' maximum product per store,

// we are possibly too high in the product capacity (or just right) so we try a lower capacity

// and the highest possible maximum is assumed to be 100000

// Using binary search to find the minimized maximum value

// Midpoint of the current search space

// Distribute products among stores

for (int quantity : products) {

if (count <= stores) {</pre>

// Counter for the number of stores needed

int mid = (left + right) / 2;

int left = 1, right = 100000;

while (left < right) {</pre>

int count = 0;

// (based on the problem constraints if given in the problem description).

# Use binary search (bisect\_left) to find the smallest 'x' such that distributing

- right = mid; } else { // If we are too low and need more than 'stores' to distribute all products, // we need to increase the product capacity per store left = mid + 1; 31 32 33 // 'left' will be our minimized maximum product per store that fits all products into 'stores' stores. 34 35 return left; 36 37 } 38
- int left = 1; // Start with the minimum possible value per shelf int right = 1e5; // Assume an upper bound for the maximum value per shelf 10 // Use binary search 11 while (left < right) {</pre>

let searchEnd = 1e5; // Assuming 1e5 is the maximum possible quantity.

// Calculate the middle value of the current search interval.

// Counter to keep track of the total number of stores needed.

const middle = Math.floor((searchStart + searchEnd) / 2);

storeCount += Math.ceil(quantity / middle);

// Binary search to find the minimized maximum number of products per store.

// Iterating over each product quantity to distribute among stores.

// We take the ceiling to account for incomplete partitions.

// Increment the store count by the number of stores needed for this product.

// Else we need to increase the number of products per store and keep looking.

// Method to find the minimized maximum number of products per shelf

int minimizedMaximum(int n, vector<int>& quantities) {

12 int mid = (left + right) >> 1; // Calculate mid value 13 int count = 0; // Initialize count of shelves needed 14 15 // Iterate through the quantities array 16 for (int& quantity : quantities) { 17 // Calculate and add number of shelves needed for each quantity count += (quantity + mid - 1) / mid; 19 20 21 22 // If the count of shelves needed is less than or equal to the available shelves 23 // there might be a solution with a smaller max quantity, search left side **if** (count <= n) { right = mid; 27 // Otherwise, search the right side with larger quantities 28 else { 29 left = mid + 1; 30 31 32 // When left meets right, it's the minimized max quantity per shelf 33 return left; 34 35 }; 36 Typescript Solution function minimizedMaximum(stores: number, products: number[]): number { // Define the search interval with a sensible start and end.

#### 19 20 // If the store count fits within the number of available stores, 21 // we proceed to check if there's an even smaller maximum. if (storeCount <= stores) {</pre>

let searchStart = 1;

while (searchStart < searchEnd) {</pre>

for (const quantity of products) {

searchEnd = middle;

searchStart = middle + 1;

let storeCount = 0;

Time and Space Complexity The given Python code aims to find a value of x that, when used to distribute the quantities of items amongst n stores, results in a minimized maximum number within a store while ensuring all quantities are distributed. This is achieved by using a binary search via

# limit of the search range. Inside the check function, there is a loop which computes the sum with complexity 0(0) for each check,

**Time Complexity:** 

using the values in quantities without additional data storage that depends on the size of quantities or the range of values. Hence,

The binary search is performed on a range from 1 to a constant value (10\*\*6), resulting in O(log(C)) complexity, where C is the upper

The code uses a constant amount of additional memory outside of the quantities list input. The check function computes the sum the space complexity is 0(1), as no significant additional space is consumed in relation to the input size.

This is done by calculating the number of stores needed for each product type (rounded up) and ensuring the sum does not

By starting the binary search at 1 and going up to 10\*\*6 (an arbitrary high number to ensure the maximum quantity is covered), we guarantee finding the minimum x within the valid range.

Here is the step-by-step implementation of the solution: 1. Binary Search Algorithm:

efficient because it repeatedly divides the search interval in half. ∘ In this case, the lower and upper bounds for the search are 1 and 10\*\*\*6 respectively. The upper bound is a sufficiently large number to cover the maximum possible quantity. 2. Helper Function (check): • A helper function, check, is used during the binary search to validate whether a given x can be used to distribute all the

product type by x and rounding up (since we can't have a fraction of a store). This is done using (v + x - 1) // x for each v in quantities. The rounding up is achieved by adding x - 1 before performing integer division. 3. **Using bisect\_left**:

need to be 1-indexed (since x can't be zero). This approach of binary search combined with a check for the validity of the distribution ensures that the solution is both efficient and correct, taking  $0(\log M * N)$  time complexity, where M is the range of possible values for x and N is the length of quantities. **Example Walkthrough** 

∘ In total, we would need 1 + 2 + 3 = 6 stores to distribute the products with each store receiving no more than 5 products. However, we only have 2 stores.

since we can't have a fraction of a store). The total is 3 stores, which is still more than 2, so check(15) returns False. 5. Binary Search Conclusion:

**Python Solution** class Solution:

store.

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C++ Solution

1 #include <vector>

class Solution {

public:

using namespace std;

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bisect\_left on a range of possible values for x.

where Q is the length of the quantities list. Therefore, the time complexity of the entire algorithm is O(Q \* log(C)). **Space Complexity:** 

23 25 26 29 30 31 // The minimized maximum number of products per store that will fit. return searchStart; 32 33 } 34