2167. Minimum Time to Remove All Cars Containing Illegal Goods

Dynamic Programming

String

Hard

Problem Description

amount of time possible. We have three operations that we can use: 1. Removing a car from the left end of the train takes 1 unit of time. 2. Removing a car from the right end of the train also takes 1 unit of time. 3. Removing a car from any other position takes 2 units of time.

In this problem, we are dealing with a 0-indexed binary string s, where each character represents a train car. A car can either

contain illegal goods (denoted by '1') or not (denoted by '0'). The goal is to remove all cars with illegal goods in the least

A car removal operation is directed towards a car containing illegal goods, and we want to know the minimum time required to remove all such cars.

To solve this problem, we use a dynamic programming approach. The intuition lies in breaking down the problem into simpler sub-

problems:

Intuition

2. The minimum time to remove all 'bad' cars from the end (right side) of the train from any given position to the end. The goal is to find out the optimal point (or points) where we switch from removing cars from the left to removing cars from the

right, or vice versa, to minimize the total time. We solve for two arrays, pre and suf, where pre[i] is the minimum time to

remove all cars with illegal goods from the first i cars, and suf[i] is the minimum time to remove all cars with illegal goods from

position i to the end. For pre:

1. The minimum time to remove all 'bad' cars from the beginning (left side) of the train up to any given position.

 If a car at position i does not contain illegal goods ('0'), then pre[i + 1] = pre[i] since no action is needed. • If it does contain illegal goods ('1'), we check if it's cheaper to remove it individually, taking 2 units of time, or remove all the i+1 cars from the left which take i+1 units of time. For suf:

• If it does contain illegal goods ('1'), we check if it's cheaper to remove it individually, taking 2 units of time, or remove all cars from position i to the end which will take n-i units of time (where n is the total number of cars).

Finally, we iterate through the arrays pre and suf to find the minimum combined time taking into account both the left and right removals at each position. The minimum value from this combination gives us the least amount of time needed to remove all the

optimal removal times from the left and from the right, respectively.

Here's the detailed implementation of the solution step by step:

• If a car at position i does not contain illegal goods ('0'), then suf[i] = suf[i + 1] as no action is needed here too.

cars containing illegal goods. Solution Approach

The solution implementation uses a dynamic programming approach with two additional arrays pre and suf to keep track of the

Initialize the pre and suf arrays with zeros, and set their sizes to one more than the length of the string s. This is done to handle the prefix up to i and suffix from i inclusively, easily without running into array index issues. Iterate through the string s from left to right. If you encounter a '0' (no illegal goods), simply copy the value from the

previous index of pre. This means no additional time is needed to handle this car. If there is a '1' (illegal goods exist),

calculate the minimum time between the time stored in pre at the previous index plus 2 (removing this particular car) and i +

for i, c in enumerate(s): pre[i + 1] = pre[i] if c == '0' else min(pre[i] + 2, i + 1)

Example Walkthrough

the current position to the end).

for i in range(n - 1, -1, -1):

Similarly, iterate through the string s from right to left to fill in the suf array. You do the mirror operation of what was done with pre: if a '0' is encountered, carry over the value from the right index of suf. If a '1' is found, calculate the minimum

time between the time stored in suf at the next index plus 2 (removing this particular car) and n - i (removing all cars from

1 (removing all cars from the left up to the current position) and store that minimum value in pre[i + 1].

suf[i] = suf[i + 1] if s[i] == '0' else min(suf[i + 1] + 2, n - i)

position) and find the minimum sum of corresponding pairs.

return min(a + b for a, b in zip(pre[1:], suf[1:]))

involves evaluating the sum of pairs of prefix and suffix solutions.

For s having a length of 6, pre and suf will be of length 7.

For s[0] = '0': pre[1] = pre[0] = 0 (no illegal goods, so no removal time needed).

Fill the suf Array: We mirror the above process, but from right to left:

 \circ For s[4] = '1': suf[4] = min(suf[5] + 2, 2) = min(1 + 2, 2) = 2.

Fill the pre Array: Next, we iterate from left to right:

 \circ For s[1] = '0': pre[2] = pre[1] = 0.

 \circ For s[3] = '0': pre[4] = pre[3] = 2.

Now, pre = [0, 0, 0, 2, 2, 4, 6].

 \circ For s[0] = '0': suf[0] = suf[1] = 4.

Now, suf = [4, 4, 4, 2, 2, 1, 0].

 \circ For i = 3:sum is pre[3] + suf[3] = 2 + 2 = 4.

 \circ For i = 4: sum is pre[4] + suf[4] = 2 + 2 = 4.

 \circ For i = 5: sum is pre[5] + suf[5] = 4 + 1 = 5.

 \circ For i = 6: sum is pre[6] + suf[6] = 6 + 0 = 6.

right end of the train.

Python

Java

class Solution {

class Solution:

Solution Implementation

length = len(s)

else:

else:

def minimumTime(self. s: str) -> int:

Calculate the length of the string s

prefix[i + 1] = prefix[i]

for i in range(length -1, -1, -1):

suffix[i] = suffix[i + 1]

// Get the length of the input string s

int[] prefixCost = new int[length + 1];

int[] suffixCost = new int[length + 1];

for (int i = 0; i < length; ++i) {

if (s.charAt(i) == '0') {

if s[i] == '0':

return minimum_cost

public int minimumTime(String s) {

int length = s.length();

flipping all to this position

prefix[i + 1] = min(prefix[i] + 2, i + 1)

suffix[i] = min(suffix[i + 1] + 2, length - i)

Calculate the suffix time cost similarly but in reverse from the end of the string

/* This method finds the minimum time required to clear a string `s` of obstacles ('1's) */

// Create prefix and suffix arrays to store the minimum cost to clear up to that index

// If there is no obstacle, then the cost is the same as the previous

// Calculate the minimum cost to clear obstacles from the start to each index

// Minimum between the cost of flipping this car

suffix[i] = min(suffix[i + 1] + 2, size - i);

// Iterate through boundaries where prefix and suffix meet.

// Define the minimumTime function which calculates the minimum time required

const size: number = s.length; // Store the size of the input string.

// Calculate prefix minimum cost by iterating over each character in the string.

minCost = min(minCost, prefix[i] + suffix[i]);

return minCost; // Return the minimum cost calculated.

// to remove or flip cars represented by a string of '0's and '1's.

return minCost; // Return the minimum cost calculated.

// console.log(result); // Outputs the minimum time required to remove or flip cars.

Calculate the prefix time cost for each position in the string

Initialize prefix and suffix lists of length + 1 to accommodate edge cases

If current character is '0', no additional cost is added

Calculate the suffix time cost similarly but in reverse from the end of the string

where cost is minimum of removing '1's by flipping twice each or turning all to '0's up to that point

Find the minimum cost to make the entire string '0's by considering both prefix and suffix costs

minimum_cost = min(prefix_cost + suffix_cost for prefix_cost, suffix_cost in zip(prefix[1:], suffix[:-1]))

If current character is '1', choose the lesser cost between adding 2 to the previous cost or

// const result: number = minimumTime("0010");

def minimumTime(self, s: str) -> int:

prefix = [0] * (length + 1)

suffix = [0] * (length + 1)

for i, char in enumerate(s):

if char == '0':

length = len(s)

else:

Calculate the length of the string s

prefix[i + 1] = prefix[i]

for i in range(length -1, -1, -1):

flipping all to this position

prefix[i + 1] = min(prefix[i] + 2, i + 1)

for (int i = 0; i <= size; ++i) {

function minimumTime(s: string): number {

for (let i = 0; i < size; ++i) {

};

TypeScript

// Example usage:

class Solution:

// and the chain of cars till now, or just removing all cars including this one.

int minCost = INT_MAX; // Initialize minimum cost to maximum possible integer value.

const prefix: number[] = new Array(size + 1).fill(0); // Array to store the prefix minimum cost.

const suffix: number[] = new Array(size + 1).fill(0); // Array to store the suffix minimum cost.

// Loop to find the minimum total cost by combining prefix and suffix costs.

Find the minimum cost to make the entire string '0's by considering both prefix and suffix costs

minimum_cost = min(prefix_cost + suffix_cost for prefix_cost, suffix_cost in zip(prefix[1:], suffix[:-1]))

Once you have the pre and suf arrays constructed, find the point where the sum of removal times from the left and from the right is minimal. Iterate through the combined view of pre (excluding the zeroth position) and suf (excluding the last

In this approach, the <u>dynamic programming</u> pattern helps avoid redundant calculations by building up the solution using

previously computed values, and the two-pointer technique is not explicitly used but is conceptually present as the solution

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presence of illegal goods in a train car.
1. Initialize pre and suf Arrays: First, we initialize pre and suf arrays to store the minimum removal times from the left and
    from the right, respectively.
```

Let's illustrate the solution approach with a small example. Assume we have a binary string s = "001011" where 1 indicates the

 \circ For s[3] = '0': suf[3] = suf[4] = 2. \circ For s[2] = '1': suf[2] = min(suf[3] + 2, 4) = min(2 + 2, 4) = 4 (either way is the same, so minimal is 4). \circ For s[1] = '0': suf[1] = suf[2] = 4.

 \circ For s[5] = '1': suf[5] = min(suf[6] + 2, 1) = min(0 + 2, 1) = 1 (cheaper to remove cars from the right).

• For s[2] = '1': pre[3] = min(pre[2] + 2, 3) = min(0 + 2, 3) = 2 (cheaper to remove this car only).

 \circ For s[4] = '1': pre[5] = min(pre[4] + 2, 5) = min(2 + 2, 5) = 4 (cheaper to remove both bad cars separately).

 \circ For s[5] = '1': pre[6] = min(pre[5] + 2, 6) = min(4 + 2, 6) = 6 (cheaper to remove all cars from the left).

Find Minimal Combined Time: Lastly, we iterate through the combined view of pre (excluding the zeroth index) and suf (excluding the last index) and find the minimum sum. \circ For i = 1: sum is pre[1] + suf[1] = 0 + 4 = 4. \circ For i = 2:sum is pre[2] + suf[2] = 0 + 4 = 4.

The minimum time from these sums is 4 units of time, so that is the least amount of time required to remove all the cars

containing illegal goods. This can be interpreted as removing the first bad car individually and the other two bad cars from the

Initialize prefix and suffix lists of length + 1 to accommodate edge cases prefix = [0] * (length + 1)suffix = [0] * (length + 1)# Calculate the prefix time cost for each position in the string # where cost is minimum of removing '1's by flipping twice each or turning all to '0's up to that point for i, char in enumerate(s): **if** char == '0': # If current character is '0', no additional cost is added

If current character is '1', choose the lesser cost between adding 2 to the previous cost or

prefixCost[i + 1] = prefixCost[i]; } else { // The cost is either removing this obstacle and all before it (i + 1) or // turning off the previously considered obstacles and turning this one on (prefixCost[i] + 2) prefixCost[i + 1] = Math.min(prefixCost[i] + 2, i + 1);

```
// Calculate the minimum cost to clear obstacles from the end to each index
        for (int i = length - 1; i >= 0; --i) {
            if (s.charAt(i) == '0') {
                // If there is no obstacle, then the cost is the same as the next
                suffixCost[i] = suffixCost[i + 1];
            } else {
                // The cost is either removing this obstacle and all after it (n - i) or
                // turning off the subsequently considered obstacles and turning this one on (suffixCost[i + 1] + 2)
                suffixCost[i] = Math.min(suffixCost[i + 1] + 2, length - i);
        // Initialize the answer to the maximum possible value
        int minimumTotalCost = Integer.MAX VALUE;
        // Find the minimum among the sum of prefix and suffix costs at every split point
        for (int i = 1; i <= length; ++i) {
            minimumTotalCost = Math.min(minimumTotalCost, prefixCost[i] + suffixCost[i]);
        // Return the minimum total cost calculated
        return minimumTotalCost;
C++
class Solution {
public:
    int minimumTime(string s) {
        int size = s.size(); // Variable to store the size of the input string.
        vector<int> prefix(size + 1); // Vector to store the prefix minimum cost.
        vector<int> suffix(size + 1); // Vector to store the suffix minimum cost.
        // Calculate prefix minimum cost.
        // Loop through the string and fill the 'prefix' vector with the calculated costs.
        for (int i = 0; i < size; ++i) {
            if (s[i] == '0') {
                // If the character is '0', the cost is same as the previous one.
                prefix[i + 1] = prefix[i];
            } else {
                // If the character is '1', take the minimum between the cost of flipping this car
                // and the chain of cars till now. or just removing all cars including this one.
                prefix[i + 1] = min(prefix[i] + 2, i + 1);
        // Calculate suffix minimum cost similarly, from the end of the string.
        for (int i = size - 1; i >= 0; ---i) {
            if (s[i] == '0') {
                // Cost is same as the next one for '0' character.
                suffix[i] = suffix[i + 1];
            } else {
```

```
if (s.charAt(i) === '0') {
       // If the character is '0', the cost is the same as the previous one.
       prefix[i + 1] = prefix[i];
    } else {
       // If the character is '1', choose the minimum between the cost
       // of flipping this car and the cost of removing all cars including this one.
        prefix[i + 1] = Math.min(prefix[i] + 2, i + 1);
// Calculate suffix minimum cost similarly, starting from the end of the string.
for (let i = size - 1; i >= 0; --i) {
    if (s.charAt(i) === '0') {
       // Cost is the same as the next one for '0' character.
        suffix[i] = suffix[i + 1];
    } else {
       // Choose the minimum between the cost of flipping this car and
       // the cost of removing all cars including this one.
        suffix[i] = Math.min(suffix[i + 1] + 2, size - i);
let minCost: number = Number.MAX_SAFE_INTEGER; // Initialize minimum cost to the maximum safe integer value.
// Find the minimum total cost by combining prefix and suffix costs.
// Iterate through the possible boundaries where prefix and suffix meet.
for (let i = 0; i <= size; ++i) {
   minCost = Math.min(minCost, prefix[i] + suffix[i]);
```

```
if s[i] == '0':
    suffix[i] = suffix[i + 1]
else:
    suffix[i] = min(suffix[i + 1] + 2, length - i)
```

return minimum_cost

Time and Space Complexity

over the string twice: once to fill the pre array with the minimum operations required to remove '1's from the start of the string and once to fill the suf array with the minimum operations required to remove '1's from the end of the string. Each element is computed in constant time, hence the first loop takes O(n) time and the second also takes O(n) time.

The time complexity of the provided code is O(n), where n is the length of the input string s. This is because the code iterates

The space complexity of the code is also O(n). Two extra arrays, pre and suf, each of size n + 1, are used to store the intermediate results for the prefix and suffix operations, respectively. The space required by these auxiliary arrays is proportional to the length of the string.