

Problem Description

and from South to North (direction 2), while on Road B, they can travel from West to East (direction 3) and from East to West (direction 4). There is a traffic light for each road. The key aspects are:

The problem describes an intersection of two roads, Road A and Road B. Cars can travel on Road A from North to South (direction 1)

- A red light means cars cannot cross and must wait for a green light.
- The lights for the two roads cannot be green simultaneously. When one is green, the other must be red.

A green light allows cars to cross the intersection along that road.

- Initially, Road A has a green light and Road B has a red light.
- The traffic lights should avoid causing a deadlock, where cars are perpetually waiting to cross.
- Cars arriving at the intersection are represented with a carld and roadId. The roadId signifies which road the car intends to use. The direction of the car is indicated by direction. Two functions are provided - turnGreen, which turns the traffic light green on the

current road, and crossCar, allowing the car to cross the intersection. The core challenge is to design a system using these components to ensure cars can cross the intersection without deadlocks.

Intuition

To ensure a deadlock-free traffic system, we need to manage the traffic lights in a way that each car will eventually be able to cross the intersection. The logic should meet two main criteria:

 No two cars from different roads should cross at the same time. Changing the traffic light to green on a road when it is already green is unnecessary and should be avoided.

- The solution uses a lock mechanism via the Lock class from the threading module to prevent the intersection state from being changed by multiple cars at the same time, ensuring consistency in traffic light changes and crossings. The idea is to synchronize
- the access to the traffic light state, so at any moment, only one car can influence it.

Then, we check if the car's road ID is the same as the road currently allowed to cross. If not, we call turnGreen() to change the traffic light to green for this car's road and update the self. road attribute. Then, we let the car cross by calling crossCar() and release the lock so the next car can proceed. This mechanism ensures that the cars will cross one at a time, changing the traffic light

A TrafficLight object maintains the state of the traffic light for both roads with a variable, starting with road A as green (road = 1).

When a car arrives at the intersection (carArrived method), we acquire the lock to prevent other cars from entering the intersection.

only when necessary and thus preventing deadlocks. **Solution Approach** The solution utilizes a simple concurrency control mechanism with a Lock from the threading module in Python, ensuring that the state of the traffic light is manipulated by only one car at a time.

Here's the step-by-step implementation:

1. An instance of TrafficLight is initialized with: A Lock object to control concurrent access to the traffic light state.

2. When a car arrives, it invokes the carArrived method with its carId, roadId, the direction it wants to travel, and two callback functions: turnGreen and crossCar.

- 3. The first action within carArrived is to acquire the lock by calling self.lock.acquire(). This step ensures that only one car can execute the following code at any given time, effectively serializing cross-intersection operations.

Updating self. road to roadId of the current car, indicating which road is now green.

o Calling the turnGreen() function to simulate the traffic light changing to green for that road.

An integer field road, initialized to 1, indicating that road A is green at the start.

comparing the roadId of the car with the road attribute of the TrafficLight instance. If they are not equal, it means the car is on the road that currently has a red light and the light needs to be changed to green. This is performed by:

5. After ensuring the road is green for the car, the crossCar() function is called, allowing the car to cross the intersection.

The Lock effectively serves as a gatekeeper to ensure the intersection's state integrity is maintained, eliminating the chances of

4. Once inside the critical section, the method proceeds to check if the traffic light needs to be changed. This is determined by

6. Finally, before exiting, the carArrived method releases the acquired lock by calling self.lock.release(), allowing the next car to proceed with its attempt to cross the intersection.

Deadlock by serializing the changes to the traffic lights and the crossing of cars. This design is simplistic but sufficient for the stated

problem requirements, showcasing a classic use of concurrency primitives such as mutexes (locks) to ensure thread-safe operations.

Example Walkthrough Let's illustrate the solution approach with a hypothetical situation involving four cars arriving at the intersection. Assume that initially, Road A has a green light and Road B has a red light as per the rules.

The lock is acquired, and it's checked against the traffic light's state.

 Since Car 1 is on Road A, which is already green, no traffic light change is necessary. crossCar is called for Car 1, allowing it to cross. The lock is released.

o carArrived is called for Car 2. Car 2 successfully acquires the lock as Car 1 has released it.

3. Car 3 arrives next, with carId = 3, roadId = 2 (Road B), and direction = 3 (West to East).

2. Car 2 arrives shortly after, with carId = 2, roadId = 1 (Road A), and direction = 2 (South to North).

Car 1 arrives, with carId = 1, roadId = 1 (Road A), and direction = 1 (North to South).

 The traffic light is still green for Road A. crossCar is called for Car 2, allowing it to cross.

The lock is released.

carArrived is called for Car 1.

- carArrived is called for Car 3.
- The lock is acquired. • The traffic light check reveals a change is needed since Car 3 is on Road B, and the current green light is for Road A.
- The road attribute is updated to 2. turnGreen() is called, setting the traffic light green for Road B.

Since the light is already green for Road B, no light change is needed.

crossCar is called for Car 3, and it crosses the intersection.

Road B thanks to Car 3. The lock is acquired by the carArrived method for Car 4.

The lock is finally released.

Python Solution

10

11

12

13

14

15

16

18

19

20

21

23

24

19

20

21

23

24

26

13

14

25 }

from threading import Lock

from typing import Callable

def carArrived(

self,

) -> None:

with self.lock:

crossCar is called for Car 4 to cross.

The lock is released.

This walkthrough demonstrates how the lock mechanism ensures that each car's arrival is dealt with one by one, allowing for proper management of the traffic lights and safe crossing of the intersection without deadlocks. The lights change only when necessary,

and multiple cars on the same road can take advantage of the light being green without requiring the light to be repeatedly changed.

4. Finally, Car 4 approaches, with carId = 4, roadId = 2 (Road B), and direction = 4 (East to West), while the light is still green on

class TrafficLight: def __init__(self): self.lock = Lock() # lock to control concurrency and avoid race condition # state to keep track of which road is green

direction: int, # direction the car is traveling in

acquire lock to ensure exclusive access to the light

change the traffic light to this car's road

roadId: int, # identifier of the road the car is on; can be 1 or 2

turnGreen: Callable[[], None], # function to call to turn the light green

crossCar: Callable[[], None], # function to call to let the car cross

If the car's road ID is different from the current green road,

self.green_road_id = roadId # update the green road ID

initially, road 1 is set to green

carId: int, # identifier of the car

if self.green_road_id != roadId:

// Allow the car to cross the intersection

crossCar.run();

self.green_road_id = 1

```
25
                turnGreen() # call the method to turn the traffic light green
26
27
             crossCar() # allow the car to cross the intersection
28
             # lock is released automatically when the 'with' block ends
29
Java Solution
1 class TrafficLight {
      private int currentRoadId = 1; // Variable to store which road has the green light
      public TrafficLight() {
         // Constructor - no initialization needed as we start with road 1 by default
6
      // Synchronized method to allow cars to arrive at the intersection without race conditions
      public synchronized void carArrived(
9
          10
          12
          int direction, // Direction of the car, not used in the current context
13
         Runnable turnGreen, // Runnable to turn light to green on the car's current road
         Runnable crossCar // Runnable to allow the car to cross the intersection
14
15
         // Check if the road that the car wants to use does not have green light
16
17
         if (roadId != currentRoadId) {
             turnGreen.run();
                                // Turn the light green for the current road
18
```

currentRoadId = roadId; // Update the current road ID to the car's road ID

public: // Constructor - no initialization needed as we start with road 1 by default 10 TrafficLight() {} 11 12

C++ Solution

1 #include <mutex>

5 private:

12): void {

synchronized(() => {

if (roadId !== currentRoadId) {

// Exit synchronization lock

Time and Space Complexity

lock is also a constant time operation.

13

16

19

20

33

34

36

35 }

action();

2 #include <functional>

class TrafficLight {

void carArrived(

```
15
           int carId,
                               // ID of the car arriving at the intersection
16
                                 // ID of the road the car is on. Can be 1 (road A) or 2 (road B)
           int roadId,
           int direction,
                                 // Direction of the car, not used in the current context
17
           std::function<void()> turnGreen,
                                            // Function to turn light to green on the car's road
           std::function<void()> crossCar
                                             // Function to allow the car to cross the intersection
20
21
22
               // Locking the mutex to ensure exclusive access to the shared variable currentRoadId
23
               std::lock_guard<std::mutex> lock(mtx);
24
25
               // Check if the road that the car wants to use does not have green light
26
               if (roadId != currentRoadId) {
27
                                           // Turn the light green for the current road
                   turnGreen();
28
                   currentRoadId = roadId; // Update the current road ID to the car's road ID
29
30
           } // Mutex is released automatically when lock goes out of scope
31
32
           // Allow the car to cross the intersection
33
           crossCar();
34
35 };
36
Typescript Solution
   // Variable to store the ID of the current road with a green light
   let currentRoadId = 1;
   // Function to simulate the car arriving at the intersection
  // Ensures synchronization to prevent race conditions
   function carArrived(
     carId: number,
                            // ID of the car arriving at the intersection
     roadId: number,
                           // ID of the road the car is on. Can be 1 (for road A) or 2 (for road B)
     direction: number, // Direction of the car, not currently used
     turnGreen: () => void, // Function to invoke to turn the traffic light green for the current road
     crossCar: () => void // Function to invoke to allow the car to cross the intersection
```

// The synchronization mechanism provided by the `synchronized` keyword in Java is

// Simulate synchronization lock to ensure one car processes at a time

// (This is conceptual, actual implementation would require additional code.)

// not directly available in TypeScript/JavaScript. We would typically need to manage

// concurrency with Promise chains, Async/Await, or other synchronization primitives.

int currentRoadId = 1; // Variable to store which road has the green light

std::mutex mtx; // Mutex to protect shared resources and prevent race conditions

// Synchronized method to allow cars to arrive at the intersection without race conditions

21 turnGreen(); // If the car's road ID differs from the current, turn the light to green currentRoadId = roadId; // Update the current road ID 24 crossCar(); // Once the traffic light is green, the car can cross the intersection 25 26 27 } 28 // Synchronization helper function (Note: This is a placeholder as JavaScript/TypeScript // does not directly support the synchronized concept out-of-the-box) function synchronized(action: () => void): void { // Enter synchronization lock

Time Complexity The time complexity of the carArrived method is 0(1). This is because there are no loops or recursive calls that depend on the size of the input. Each function call to turnGreen() and crossCar() is considered a constant time operation. Acquiring and releasing a

Space Complexity The space complexity of the TrafficLight class is 0(1). It uses a fixed amount of space: one lock and one integer variable, regardless of the number of times the carArrived method is called or the number of car objects interacting with the system.