



Problem Description

In this problem, we are given a "broken" calculator that can perform only two operations:

- 1. Multiply the current number displayed by 2.
- 2. Subtract 1 from the current number displayed.

The calculator initially shows a number called startValue. The task is to transform this startValue into another given number called

target using the fewest number of operations. We need to find out the minimum operations required to achieve this.

Intuition

multiplications and subtractions. However, this can be very inefficient because the number of possibilities can explode, leading to a high time complexity solution. Instead, we reverse our thinking process and start from target and try to reach startValue. We take advantage of the fact that the

The intuitive approach to solve this problem might be to start from startValue and try to reach target using a series of

reverse operations (dividing by 2 and adding 1) are more restricted since we can divide by 2 only when the current number is even. This gives us a direction in our decision-making process and reduces the number of choices at each step, making the problem much simpler. Here's the step-by-step intuition:

1. If target is greater than startValue, we can only reach it by performing the reverse operations because multiplying startValue

- may overshoot target. 2. If target is odd, the last operation performed must have been subtracting 1 (since we cannot divide an odd number by 2). So,
- we add 1 to target. 3. If target is even, the last operation could have been a division by 2, so we divide the target by 2. 4. We count each operation performed, and once target is less than or equal to startValue, we stop.
- 5. The remaining difference between startValue and target represents the number of times we'd need to subtract 1 from
- startValue to reach target.
- By following these steps, we can ensure that we use the minimum operations to transform startValue into target on the broken calculator.

Solution Approach

The Solution provided is a direct implementation of the thought process described in the Intuition section. It's a linear approach, where the algorithm goes through a series of steps to transform the target back to the startValue. The crucial insight is that

because multiplying can lead to rapidly overshooting the goal, but working backward constrains the choices. Here's a step-by-step walkthrough of the implementation: A variable ans is initialized to 0 to count the number of operations needed.

• While startValue is less than target, a loop continues to perform the reverse operations to bring target closer to startValue.

working backward from the target value is more efficient than trying to approach the target starting from the startValue. This is

o Inside the loop, first, there is a check to see if target is odd using target & 1. This is a bitwise AND operation, which is

to the ans counter to reflect these operations.

in terms of the number of operations needed.

- equivalent to checking if the last bit of target is 1. If it is odd (true), 1 is added to target to simulate the reverse of a
- subtract operation.
- If target is even (false), the target is right-shifted by 1 bit using target >>= 1, which is equivalent to dividing the target by 2. The ans counter is then incremented for each operation performed, whether it's an addition or a division. When target is less than or equal to startValue, the loop ends. The final difference between startValue and target indicates

how many subtractions would be necessary if we were working forwards from startValue. Thus, startValue - target is added

This approach is efficient because each iteration reduces target significantly (either by a factor of 2 or approaching the even

number when odd), and there are no unneeded complexities in performing the operations, leading to a time complexity that is linear

Finally, ans is returned as the minimum number of operations needed to display target on the calculator from startValue.

By continuously halving the target, we ensure that we're using the most significant reduction at each step when possible, and only when target becomes odd, we perform an addition. This way, despite simulating an inefficient calculator, the algorithm efficiently reaches the optimal solution.

Example Walkthrough Let's walk through an example to illustrate the solution approach using the broken calculator problem.

startValue = 5

target = 8

Solution Steps

Now we need to find the minimum operations to transform startValue into target.

1. Since target > startValue, we know we have to work backwards from target to startValue.

Example

- First iteration: target is 8, which is even.
- Increment ans to 1.

2. Initial ans is 0 because no operations have been performed yet.

Second iteration: target is 4, which is even.

Now we enter the loop:

- Again, we divide by 2. So, target = target / 2 = 4 / 2 = 2. Increment ans to 2.
- Third iteration: target is 2, which is even.

We perform the reverse of multiplication by dividing by 2. So, target = target / 2 = 8 / 2 = 4.

 Continue with division. So, target = target / 2 = 2 / 2 = 1. Increment ans to 3.

Conclusion

The loop ends here because target = 1 is less than startValue = 5. We now add startValue - target to ans.

divisions (halving the number three times) and four subtractions. Python Solution

The minimum number of operations required for the broken calculator starting from 5 to reach 8 is 7. These operations are three

• startValue - target = 5 - 1 = 4. This means we need to perform 4 subtractions if we were moving forwards from startValue.

class Solution: def broken_calc(self, start_value: int, target: int) -> int: # Initialize the number of operations to 0 operations = 0

Increment the operations counter

while start_value < target:

target += 1

target >>= 1

operations += start_value - target

if ((target & 1) == 1) {

target++;

return numOfOperations;

} else {

if target % 2:

operations += 1

else:

15

16

17

18

19

20

16

19

20

21

22

23

24

25 26

27

28

29

30

31

32

34

33 }

Loop until the start value is greater than or equal to target

If target is even, divide it by 2 using right shift

Add the difference between start value and the target to the operations

This handles the case where we need to perform 'multiply by 2' operations

If target is odd, increment it to make it even

Add 4 to ans, which is 3 from earlier. Now ans = 3 + 4 = 7.

```
21
           # Return the total number of operations performed
22
           return operations
23
Java Solution
   class Solution {
       /**
        * Calculates the minimum number of operations to transform
        * startValue to target by either multiplying by 2 or decrementing by 1.
        * @param startValue The starting value.
        * @param target
                           The target value.
        * @return
                            The minimum number of operations required.
9
10
       public int brokenCalc(int startValue, int target) {
11
           int numOfOperations = 0; // Initialize operation count
12
13
           // Work backwards from the target value until we reach or go below startValue
14
           while (startValue < target) {</pre>
15
```

// If target is odd, increment it (reverse of decrementing in forward direction)

// If target is even, halve it (reverse of doubling in forward direction)

target >>= 1; // Equivalent to target /= 2;

// Once we reach or go below startValue, add the difference

// Since at this point only decrements are allowed

numOfOperations += startValue - target;

// Return the total number of operations

1 // Global variable to store the minimum number of operations.

// Function to calculate the minimum number of operations required

function brokenCalc(startValue: number, target: number): number {

// of subtracting 1 in the problem context).

// If the 'target' is even, divide it by 2.

the loop runs in O(log(target)) time with respect to the target value.

// Reset operation count at the start of the function call.

// Continue the process until 'startValue' is at least as large as the 'target'.

// If the 'target' is an odd number, increment it to make it even.

// in an even number), so we add 1 (which is the reverse operation

// An odd number cannot be reached by doubling (which always results

5 // to reach from 'startValue' to 'target' by either multiplying by 2 or

numOfOperations++; // Increment the count of operations

10 11 12 13 14

2 let operationCount = 0;

9

10

11

12

13

14

15

16

17

18

19

20

21

37

6 // subtracting 1 in each operation.

while (startValue < target) {

if (target % 2 === 1) {

target++;

operationCount = 0;

C++ Solution

```
1 class Solution {
 2 public:
       // Function to calculate the minimum number of operations required
       // to reach from 'startValue' to 'target' by either multiplying by 2 or
       // subtracting 1 in each operation.
       int brokenCalc(int startValue, int target) {
            int operationCount = 0; // Variable to store the minimum number of operations.
 8
           // Continue the process until startValue is at least as large as the target.
 9
           while (startValue < target) {</pre>
               // If the target is an odd number, increment it to make it even.
               // An odd number cannot be reached by doubling (which always results in an even number),
               // so we add 1 (which is the reverse operation of subtracting 1).
               if (target & 1) {
15
16
                   target++;
17
               // If the target is even, perform a right bit shift operation equivalent to dividing by 2.
19
               // This is the reverse operation of multiplying by 2.
20
               else {
21
                   target >>= 1;
22
23
24
               // Increase the operation count after each modification to the target.
25
               ++operationCount;
26
27
           // Once we have a startValue greater than or equal to the target,
28
29
           // we need to perform (startValue - target) subtractions to reach the target.
30
           operationCount += startValue - target;
31
32
           // Return the total number of operations required.
33
           return operationCount;
34
35 };
36
Typescript Solution
```

32 33 34

Time and Space Complexity

// This is the reverse operation of multiplying by 2. 22 else { target /= 2; 24 25 26 // Increase the operation count after each modification to the 'target'. operationCount++; 28 29 // Once we have a 'startValue' greater than or equal to the 'target', 30 // we need to perform ('startValue' - 'target') subtractions to reach the 'target'. 31 operationCount += startValue - target; // Return the total number of operations required. return operationCount; 35 36 }

The time complexity of the given code is O(log(target)). The while loop runs until startValue is greater than or equal to target. At each iteration of the loop, if target is even, it is halved (which significantly decreases the target in logarithmic steps), or if it's odd, it is incremented by 1, which eventually makes it even for the next step. Since target is divided by 2 in potentially every other iteration,

Time Complexity

Space Complexity The space complexity of the code is 0(1). The solution does not use any additional storage that grows with the size of the input. It uses a fixed amount of space for the variables ans, startValue, and target irrespective of the input size.