

# 2461. Maximum Sum of Distinct Subarrays With Length K

Medium   Array   Hash Table   Sliding Window

[Leetcode Link](#)

## Problem Description

You are provided with an array `nums` consisting of integers and an integer `k`. The task is to locate the subarray (a contiguous non-empty sequence of elements within the array) with a length of exactly `k` elements such that all elements within the subarray are distinct. Once you identify such subarrays, you need to calculate their sums and determine the maximum sum that can be achieved under these constraints. If there are no subarrays that satisfy the conditions, you should return `0`.

## Intuition

The intuition behind the solution is based on a sliding window technique coupled with the use of a hash map (in Python, a Counter) to keep track of the distinct elements within the current window. The sliding window technique is a common approach for problems involving contiguous subarray (or substring) operations.

Instead of generating all possible subarrays which would be computationally expensive, we can use a sliding window to move across `nums` with a fixed length of `k`. At each step, update the sum of the current window as well as the Counter, which represents the frequency of each number within the window. The sum is updated by adding the new element that comes into the window and subtracting the one that gets removed.

If at any point, the size of the Counter is equal to `k`, it means all the elements in the window are distinct. This condition is checked after every move of the window one step forward. When this condition is met, we consider the current sum as a candidate for the maximum sum.

By maintaining a running sum of the elements in the current window and updating the Counter accordingly, we can efficiently determine the moment a subarray consisting of `k` distinct elements is formed and adjust the maximum sum if needed. The solution, therefore, arrives at finding the maximum subarray sum with the given constraints through the sliding window technique and a Counter to track the distinct elements within each window.

## Solution Approach

The solution follows a sliding window approach to maintain a subarray of length `k` and a Counter from the `collections` module to track the frequency of elements within this subarray.

Here's a step-by-step explanation of how the implementation works:

- Initialize a Counter with the first `k` elements of `nums`. This data structure will help efficiently track distinct elements by storing their frequency (number of occurrences).
- Calculate the initial sum `s` of the first `k` elements. This serves as the starting subarray sum that we will update as we traverse the `nums` array.
- Check if the initial Counter length is `k`, meaning all elements in the current window are distinct. If they are, assign that sum to `ans`. If not, `ans` is assigned a value of `0` to denote no valid subarray has been found yet.
- Iterate through the `nums` array starting at index `k` and for every new element added to the window: a. Increase the count of the new element (`nums[i]`) in the Counter and add its value to the running sum `s`. b. Decrease the count of the element that is no longer within the window (`nums[i-k]`) and subtract its value from the running sum `s`. c. Remove the element from the Counter if its frequency drops to zero, ensuring only elements actually in the current window are considered.
- After updating the Counter and the sum for the new window position, check again if the size of the Counter is `k`. If it is, check if the current sum `s` is greater than the previously recorded `ans`. If so, update `ans` with the new sum.
- Continue this process until the end of the array is reached. The maintained `ans` will be the maximum sum of a subarray that satisfies the given conditions.
- After completing the iteration, return the final value of `ans`.

The algorithm ensures that at any point, only subarrays of length `k` with all distinct elements are considered for updating the maximum sum. This is achieved using the Counter to check for distinct elements and a running sum mechanism to avoid recomputing the sum for each subarray from scratch. Thus, the implementation effectively finds the maximum subarray sum with all distinct elements within the defined length `k`.

## Example Walkthrough

Let's walk through a small example to illustrate the solution approach.

Suppose we have the following `nums` array and `k` value:

```
1 nums = [4, 2, 4, 5, 6]
2 k = 3
```

We want to find the subarray of length `k` where all elements are distinct and has the maximum sum. Let's apply our solution approach step by step:

- We initialize a Counter with the first `k` elements of `nums`, which are `[4, 2, 4]`. The Counter will look like: `{4: 2, 2: 1}`.
- Calculate the initial sum `s` of these `k` elements: `4 + 2 + 4 = 10`.
- The initial Counter length is not `k` (because we have only two distinct elements, and `k` is 3), so we do not have all distinct elements. We set `ans` to `0`.
- Now we start iterating from the index `k` in the `nums` array, which is `nums[k] = nums[3] = 5`.
  - We increase the count of the new element (`nums[3] = 5`) in the Counter. So the Counter becomes `{4: 1, 2: 1, 5: 1}`.
  - We add the new element's value to the sum: `s = 10 - 4 + 5 = 11` (we subtract the first element of the current window `4` and add the new element `5`).
  - We decrease the count of the element that slid out of the window (`4`) in the Counter. Since its frequency drops to zero, it is removed from the Counter.
- The Counter now looks like: `{2: 1, 5: 1, 6: 1}` with distinct counts and we have a new sum `s = 11`. As the size of the Counter is equal to `k`, we compare `s` to `ans`. Since `11 > 0`, we update `ans = 11`.
- Next, we slide the window by one more element and repeat steps 4 and 5:
  - Add `nums[4] = 6` to the Counter, updating it to `{2: 1, 5: 1, 6: 1}` and sum `s = 11 - 2 + 6 = 15`.
  - Now, each element's count is 1 and the Counter size is equal to `k`, which means all elements are distinct. We compare the sum `s` to `ans`. Since `15 > 11`, we update `ans` to `15`.
- After finishing the iteration, we end up with the final value of `ans = 15`, which is the maximum sum of a subarray where all elements are distinct for the given `k`.

Thus, the subarray `[4, 5, 6]` of length `k = 3` gives us the maximum sum of `15` under the constraint that all elements within it are distinct.

## Python Solution

```
1 from collections import Counter
2
3 class Solution:
4     def maximumSubarraySum(self, nums: List[int], k: int) -> int:
5         # Initialize a counter for the first 'k' elements
6         num_counter = Counter(nums[:k])
7
8         # Calculate the sum of the first 'k' elements
9         current_sum = sum(nums[:k])
10
11        # If the number of unique elements equals 'k', assign sum to 'max_sum', else 0
12        max_sum = current_sum if len(num_counter) == k else 0
13
14        # Iterate over the rest of the elements, starting from the 'k'th element
15        for i in range(k, len(nums)):
16            # Add the new element to the counter and sum
17            num_counter[nums[i]] += 1
18            current_sum += nums[i]
19
20            # Remove the (i-k)'th element from the counter and sum
21            num_counter[nums[i - k]] -= 1
22            current_sum -= nums[i - k]
23
24            # If there's no more instances of the (i-k)'th element, remove it from the counter
25            if num_counter[nums[i - k]] == 0:
26                del num_counter[nums[i - k]]
27
28            # Update 'max_sum' if the number of unique elements in the window equals 'k'
29            if len(num_counter) == k:
30                max_sum = max(max_sum, current_sum)
31
32        # Return the maximum sum found that matches the unique count condition
33        return max_sum
34
```

## Java Solution

```
1 class Solution {
2     public long maximumSubarraySum(int[] nums, int k) {
3         int n = nums.length; // Store the length of input array nums
4         // Create a HashMap to count the occurrences of each number in a subarray of size k
5         Map<Integer, Integer> countMap = new HashMap<>(k);
6         long sum = 0; // Initialize sum of elements in the current subarray
7
8         // Traverse the first subarray of size k and initialize the countMap and sum
9         for (int i = 0; i < k; ++i) {
10             countMap.merge(nums[i], 1, Integer::sum);
11             sum += nums[i];
12         }
13
14         // Initialize the answer with the sum of the first subarray if all elements are unique
15         long maxSum = countMap.size() == k ? sum : 0;
16
17         // Loop over the rest of the array, updating subarrays and checking for maximum sum
18         for (int i = k; i < n; ++i) {
19             // Add current element to the countMap and update the sum
20             countMap.merge(nums[i], 1, Integer::sum);
21             sum += nums[i];
22
23             // Remove the element that's k positions behind the current one from countMap and update the sum
24             int count = countMap.merge(nums[i - k], -1, Integer::sum);
25             if (count == 0) {
26                 countMap.remove(nums[i - k]);
27             }
28             sum -= nums[i - k];
29
30             // Update maxSum if the countMap indicates that we have a subarray with k unique elements
31             if (countMap.size() == k) {
32                 maxSum = Math.max(maxSum, sum);
33             }
34         }
35
36         // Return the maximum sum found
37         return maxSum;
38     }
39 }
40
```

## C++ Solution

```
1 #include <vector>
2 #include <unordered_map>
3 #include <algorithm>
4
5 class Solution {
6 public:
7     // Function to compute the maximum subarray sum with exactly k unique elements
8     long maximumSubarraySum(std::vector<int>& nums, int k) {
9         using ll = long long; // Alias for long long to simplify the code
10         int n = nums.size(); // Size of the input array
11         std::unordered_map<int, int> count; // Map to store the frequency of elements
12         ll sum = 0; // Initialize sum of the current subarray
13         // Initialize the window of size k
14         for (int i = 0; i < k; ++i) {
15             count[nums[i]]++; // Increment the frequency of the current element
16             sum += nums[i]; // Add the current element to the sum
17         }
18         // Initialize answer with the sum of the first window if it contains k unique elements
19         ll maxSum = count.size() == k ? sum : 0;
20         // Slide the window across the array
21         for (int i = k; i < n; ++i) {
22             count[nums[i]]++; // Increment frequency of the new element in the window
23             sum += nums[i]; // Add new element to current sum
24
25             count[nums[i - k]]--; // Decrement frequency of the oldest element going out of the window
26             sum -= nums[i - k]; // Subtract this element from current sum
27             // If the oldest element frequency reaches 0, remove it from the count map
28             if (count[nums[i - k]] == 0) {
29                 count.erase(nums[i - k]);
30             }
31             // Update maxSum if current window contains k unique elements
32             if (count.size() == k) {
33                 maxSum = std::max(maxSum, sum);
34             }
35         }
36         // Return the maximum subarray sum with exactly k unique elements
37         return maxSum;
38     }
39 };
40
```

## Typescript Solution

```
1 function maximumSubarraySum(nums: number[], k: number): number {
2     const n: number = nums.length;
3     const countMap: Map<number, number> = new Map();
4     let currentSum: number = 0;
5
6     // Initialize the count map and current sum with the first 'k' elements
7     for (let i: number = 0; i < k; ++i) {
8         countMap.set(nums[i], (countMap.get(nums[i]) ?? 0) + 1);
9         currentSum += nums[i];
10    }
11
12    // Check if the first subarray of length 'k' has 'k' distinct numbers
13    let maxSum: number = countMap.size === k ? currentSum : 0;
14
15    // Traverse the array starting from the 'k'th element
16    for (let i: number = k; i < n; ++i) {
17        // Add the next number to the count map and current sum
18        countMap.set(nums[i], (countMap.get(nums[i]) ?? 0) + 1);
19        currentSum += nums[i];
20
21        // Update the count map and current sum by removing the (i-k)'th number
22        const prevCount: number = countMap.get(nums[i - k])! - 1;
23        countMap.set(nums[i - k], prevCount);
24        currentSum -= nums[i - k];
25
26        // If after decrementing, the count is zero, remove it from the map
27        if (prevCount === 0) {
28            countMap.delete(nums[i - k]);
29        }
30
31        // If the current subarray has 'k' distinct elements, update maxSum
32        if (countMap.size === k) {
33            maxSum = Math.max(maxSum, currentSum);
34        }
35    }
36
37    // Return the maximum sum of a subarray with 'k' distinct numbers
38    return maxSum;
39 }
40
```

## Time and Space Complexity

The given Python code defines a method `maximumSubarraySum` within a class `Solution` to calculate the maximum sum of a subarray of size `k` with unique elements. The code uses a sliding window approach by keeping a counter for the number of occurrences of each element within the current window of size `k` and computes the sum of elements in the window.

### Time Complexity:

The time complexity of the algorithm is  $O(n)$ , where `n` is the total number of elements in the input list `nums`. This is because the code iterates through all the elements of `nums` once. For each element in the iteration, the time to update the `cnt` counter (Counter from the `collections` module) for the current window is constant on average due to the hash map data structure used internally. The operations inside the loop including incrementing, decrementing, deleting from the counter, and computing the sum are done in constant time. Since these operations are repeated for every element just once, it amounts to  $O(n)$ .

### Space Complexity:

The space complexity of the algorithm is  $O(k)$ . The `cnt` counter maintains the count of elements within a sliding window of size `k`. In the worst-case scenario, if all elements within the window are unique, the counter will hold `k` key-value pairs. Hence, the amount of extra space used is proportional to the size of the window `k`.