2874. Maximum Value of an Ordered Triplet II



Medium Array Leetcode Link

Problem Description

obtained from choosing any three different indices (i, j, k) in the array such that i < j < k. The value of a triplet (i, j, k) is calculated using the formula (nums[i] - nums[j]) * nums[k]. If we consider different combinations of three elements from the array, some might yield negative values, while others might yield

In this problem, we are given an array of integers, nums, indexed starting from 0. The task is to find the maximum value that can be

positive values or zero. We want to find the maximum positive value, or if all the possible triplets result in a negative value, we return 0. To understand the value of a triplet, let's consider that nums[i] is greater than nums[j], then (nums[i] - nums[j]) will be positive. In

this case, to maximize the value of the triplet, you would want nums [k] to be as large as possible because you are multiplying by nums[k]. If nums[i] is less than nums[j], the difference becomes negative, and a large nums[k] will only lead to a more negative value. In that case, we are not interested in those combinations as our goal is to find the maximum positive value.

The intuition behind the solution is to traverse the array while keeping track of two key values: the maximum value found so far (mx),

Intuition

maximum value of the triplet without having to explicitly check all possible triplet combinations. The maximum prefix value mx represents the largest number we have seen so far as we iterate through the array. This value could potentially be nums[i] of our triplet. As we are looking for i < j < k, any number we see can be a candidate for nums[k].

and the maximum difference between mx and the current value (mx_diff). These two variables help in efficiently computing the

The maximum difference mx_diff represents the highest value obtained from subtracting any previously encountered number from mx. It effectively keeps track of the maximum (nums[i] - nums[j]) that we have seen so far.

While we iterate through the array, for any current number num, we calculate and update ans with max(ans, mx_diff * num). This step calculates the maximum triplet value for the current number as nums [k] (since num is always the right-most element in the

potential triplet). We ensure to first update ans before updating mx_diff because mx_diff needs to be the result of the prefix, not

including the current number. By following this approach, we avoid having to compare each possible triplet explicitly, which would result in a higher computational complexity. Instead, we make use of the information that is gathered while traversing through the array to keep updating our potential maximum triplet value, all in linear time which is efficient.

Solution Approach The approach is to cleverly keep track of the necessary values as we iterate through the array, enabling us to calculate the maximum

When we start iterating through the array nums, we initialize two variables mx and mx_diff with zero. mx will keep track of the

maximum value we have encountered so far (i.e., the maximum value for nums [i]), and mx_diff will store the maximum difference computed as (nums[i] - nums[j]) during the iteration.

1. Update the Answer: For the current value num in nums, we attempt to update the answer, ans, with the maximum of either ans itself or the product of mx_diff and num. The reason behind this calculation is that num will serve as nums [k] (the potential third element in our triplet), and mx_diff represents the maximum difference from previous elements nums[i] and nums[j]. This step

ans = $max(ans, mx_diff * num)$

ensures that we always have the maximum possible product for the current state of the array.

Below are the steps that we perform as we traverse the array nums from left to right:

triplet value on the fly without the need to consider each triplet individually.

the array, we need to keep track of the largest value seen so far that could become nums [i] for future triplets. mx = max(mx, num)3. Update Maximum Difference: Finally, we update mx_diff. To maintain the invariant that mx_diff is the maximum difference for a

valid triplet, we must ensure that it is always calculated uptil the elements before num (as num is a candidate for nums [k]). Hence,

2. Update Maximum Value: Next, we update mx to be the maximum of itself or the current value num, because as we move through

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Since we always update ans before mx_diff, we can guarantee that the difference applied to the calculation of ans doesn't include
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mx_diff = max(mx_diff, mx - num)

it is updated as the maximum of itself or mx - num.

the current num as mx_diff gets updated only after ans.

linear time complexity O(n) and constant space complexity O(1).

the maximum value of (nums[i] - nums[j]) * nums[k] where i < j < k.

the array contains the maximum value for all the valid triplets (i, j, k) that we were tasked with finding. The algorithm leverages two fundamental ideas:

triplet product based on the constraints given in the problem. The final answer is stored in ans, which by the end of the iteration of

This way, as we move forward through the array, we dynamically update and maintain the necessary values to find the maximum

• Greedy Choice Property: By choosing the best options at each step (maximum value and maximum difference), we ensure the end result is optimal. This concise yet effective approach and the minimal use of extra space (just two variables) contributes to an efficient solution with

Let's walk through a small example to illustrate the solution approach. Consider the array nums = [1, 5, 6, 3, 7]. We need to find

Dynamic Updates: Instead of considering every triplet separately, it keeps track of the potential maximums dynamically.

We start by initializing mx and mx_diff as 0. The variable ans will be used to keep track of the maximum value we find.

than 5 - 1 which is 4).

nums[0] = 1: Initialize mx = 1, mx_diff = 0, ans = 0.

Import typing List to specify the type of the input nums.

Iterate through each number in the input list.

max_number = max(max_number, number)

Return the maximum possible triplet value found.

Example Walkthrough

index.

move to the next element. 2. At element 5, we update mx to 5 (since 5 is greater than mx which was 1). We cannot update mx_diff yet since we do not have a j

3. Moving to element 6, mx remains at 5. mx_diff is updated to 0 (which was 5 - 5, the only pair we've considered). We can now

5. Finally, we arrive at element 7. mx is not updated since 7 is not greater than current mx which is 5. We then calculate ans as the

maximum of 6 and $mx_diff * num$, which is 2 * 7 = 14. Thus, ans is updated to 14. mx_diff is updated to 4 (since 5 - 3 was less

consider the difference between the current mx and nums[j] which is from previous elements. However, we do not update ans

1. We begin with the first element 1. mx is updated to 1 (it's the first element). There are no previous elements to consider, so we

since we still need a k index. 4. At element 3, mx is not updated since 3 is not greater than 5. mx_diff can be updated to 2 (mx which is 5 minus current element 3).

The answer ans is now the maximum of 0 and $mx_diff * num$, which is 2 * 3 = 6.

• nums[1] = 5: Update mx = 5. ans and mx_diff cannot be updated as we need a k.

• nums[2] = 6: mx_diff can now be calculated, but remains 0, mx remains 5.

nums[3] = 3: Update mx_diff = 2. Update ans = max(0, 2 * 3) = 6.

- After the iteration, ans holds the value 14, which is the maximum value for the expression (nums[i] nums[j]) * nums[k]. To summarize, the steps were as follows:
- The procedure efficiently finds the maximum value by dynamically updating the mx, mx_diff, and ans variables while traversing the array a single time. The solution did not require examining all possible triplets, thus maintaining a linear time complexity.

• nums[4] = 7: Do not update mx but update ans = max(6, 2 * 7) = 14. Update $mx_diff = max(2, 5 - 3) = 4$.

Python Solution

Calculate the maximum triplet value by taking the maximum between the current max_triplet_value

Update max_difference which is the maximum difference found between max_number and any number.

Update max_number if the current number is greater than the max_number seen so far.

and the maximum difference between the maximum number and the current number.

and the product of max_difference and the current number.

max_difference = max(max_difference, max_number - number)

2 #include <algorithm> // Include necessary headers for vector and max function

max_triplet_value = max(max_triplet_value, max_difference * number)

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class Solution:
   def maximumTripletValue(self, nums: List[int]) -> int:
       # Initialize variables to store the maximum triplet value, the maximum number encountered so far,
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from typing import List

max_triplet_value = 0

max_difference = 0

for number in nums:

return max_triplet_value

max_number = 0

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Java Solution
   class Solution {
       // Method to calculate the maximum triplet value.
       public long maximumTripletValue(int[] nums) {
           // Initialize three variables to store the current maximum value,
           // the maximum difference found so far, and the answer we will return.
            long currentMax = 0;
            long maximumDiff = 0;
            long answer = 0;
           // Iterate through each number in the array.
           for (int num : nums) {
               // Calculate the tentative answer as the current number times the maximum difference,
               // update the answer if the result is greater than the current answer.
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               answer = Math.max(answer, num * maximumDiff);
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               // Update currentMax if the current number is greater than currentMax.
               currentMax = Math.max(currentMax, num);
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               // Update maximumDiff if the difference between currentMax and current number
               // is greater than maximumDiff.
21
               maximumDiff = Math.max(maximumDiff, currentMax - num);
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           // Return the final answer.
26
           return answer;
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```

class Solution { 5 public:

C++ Solution

1 #include <vector>

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long long maximumTripletValue(std::vector<int>& nums) {
            long long maxTripletValue = 0; // This will hold the maximum value of the triplet found so far
           int maxNum = 0; // This will keep track of the maximum number encountered in the array
           int maxDifference = 0; // This will keep the maximum difference we've found between maxNum and a smaller number
           // Iterate over the elements of nums
            for (int num : nums) {
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               // Update the maximum value of any triplet found so far.
               // The maximum triplet value is defined by maxDifference multiplied by the current number.
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               maxTripletValue = std::max(maxTripletValue, 1LL * maxDifference * num);
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               // Update maxNum if the current number is greater than the previous maxNum.
               maxNum = std::max(maxNum, num);
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               // Update maxDifference if the difference between the current maxNum and num is greater
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               // than the previous maxDifference.
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               maxDifference = std::max(maxDifference, maxNum - num);
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           return maxTripletValue; // Return the maximum triplet value found.
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27 };
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Typescript Solution
   function maximumTripletValue(nums: number[]): number {
       // Initialize variables:
       // ans - to store the maximum product of the triplet.
       // maxNum - to store the maximum number encountered so far.
       // maxDifference - to store the maximum difference encountered so far.
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let [maxProduct, maxNum, maxDifference] = [0, 0, 0]; // Loop through each number in the array to calculate the maximum triplet value. for (const num of nums) { // Update the maxProduct with the maximum of current maxProduct and 10 // the product of maxDifference and the current num. maxProduct = Math.max(maxProduct, maxDifference * num); 13 // Update maxNum with the maximum of current maxNum and the current num. 14 15 maxNum = Math.max(maxNum, num); 16 // Update maxDifference with the maximum of current maxDifference and // the difference between current maxNum and the current num. maxDifference = Math.max(maxDifference, maxNum - num); 20 21 // Return the calculated maximum product of a triplet. 22

Time and Space Complexity

stays constant regardless of the input size.

return maxProduct;

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As the loop runs n times, where n is the length of the array, the overall time complexity is linear. The space complexity of the code is 0(1). The reason for this constant space complexity is that only a fixed number of variables (ans, mx, and mx_diff) are used. These variables do not depend on the size of the input, hence, the amount of allocated memory

The time complexity of the provided code is O(n) because there is a single for loop that iterates through the array nums once. Each

operation inside the loop, such as updating ans, mx, and mx_diff, is done in constant time, independent of the size of the input array.