1288. Remove Covered Intervals

#### **Medium** Array Sorting

**Problem Description** 

The problem presents a scenario in which you're given a list of intervals, with each interval represented as a pair of integers [start, end). The notation [start, end) signifies that the interval includes start and goes up to but does not include end. The goal is to remove intervals that are "covered" by other intervals. An interval [a, b) is considered covered by another interval [c, d) if both c <= a and b <= d. In simple terms, if one interval lies completely within the boundary of another, the inner interval is said to be covered by the outer interval. Your task is to find out how many intervals remain after removing all the covered

intervals.

## The intuitive approach to solving this problem involves checking each interval against all others to see if it is covered by any.

Intuition

intervals in a way that makes it easier to identify and remove the covered intervals. By sorting the intervals first by their start times and then by their end times in descending order, we line up intervals in such a way that once we find an interval not covered by the previous one, none of the following intervals will cover it either. This sorting

However, this would be inefficient, particularly for large lists of intervals. Thus, the key to an efficient solution is to sort the

strategy allows us to only compare each interval with the last one that wasn't removed. With the sorted list, we iterate through the intervals, where the main idea is to compare the current interval's end with the previous interval's end. If the current end is greater, this interval isn't covered by the previous interval. We count this interval, and

it becomes the new previous interval for subsequent comparisons. If the current end is not greater, it means this interval is covered by the previous interval, and we do not count it and proceed to the next interval. After checking all intervals, the count cnt gives the number of intervals that remain.

**Solution Approach** 

The solution makes use of a greedy algorithm approach, where we aim to remove the minimal number of intervals by keeping the

#### ones that aren't covered by any other. Let's walk through the solution approach along with the algorithms, data structures, or patterns used:

class Solution:

for e in intervals[1:]:

**Sorting:** We begin by sorting the intervals list using a custom sort key. This key sorts the intervals primarily by their start times in ascending order. If two intervals have the same start time, we sort them by their end times in descending order. This ensures that we have the longer intervals earlier if the start times are the same, making it easier to identify covered intervals.

- Initializing Counters: After sorting, we initialize our count cnt to 1. This is because we consider the first interval as not being covered by any previous one, as there are no previous intervals yet. We also initialize pre to keep track of the last interval that was not covered by the one before it.
- Iterating Through Intervals: We loop through the sorted intervals starting from the second one. At each iteration, we compare the current interval's end time (e[1]) with the end time of pre (pre[1]): If pre[1] (previous interval's end time) is less than e[1] (current interval's end time), it indicates that the current interval is

not completely covered by pre. Hence, we increment our count cnt and update pre to the current interval.

If pre[1] is greater than or equal to e[1], the current interval is covered by pre, and we don't increment cnt.

covered by another interval. It's important to understand that by sorting the intervals first by starting time and then by the ending time (in opposite order), we

Return the Result: After iterating through all intervals, cnt holds the count of intervals that remain after removing all that are

limit the comparison to only the previous interval and the current one in the loop. This greatly reduces the number of comparisons needed, resulting in a more efficient algorithm.

def removeCoveredIntervals(self, intervals: List[List[int]]) -> int: # Sort intervals by start time, and then by end time in descending order intervals.sort(key=lambda x: (x[0], -x[1])) cnt, pre = 1, intervals[0] # Initialize the counter and the previous interval tracker # Iterate through each interval in the sorted list

# If the current interval's end time is greater than the previous', it's not covered

Below is the reference code implementation based on this approach:

```
if pre[1] < e[1]:
                cnt += 1  # Increment the counter, as this interval isn't covered
                             # Update the 'pre' interval tracker to the current interval
        return cnt # Return the final count of non-covered intervals
  With the combination of a clever sorting strategy and a single loop, this code neatly solves the problem in an efficient manner.
Example Walkthrough
  Let's go through a small example to illustrate the solution approach described.
  Suppose we have a list of intervals: [[1,4), [2,3), [3,6)].
```

1. Sorting: Applying our custom sort, the list is sorted by start times in ascending order, and for those with the same start time, by end times in descending order. But since all our example intervals have different start times, we only need to sort by the first element:

Initializing Counters: We initialize our count cnt to 1, assuming the first interval [1,4) is not covered. We also initialize pre

# **Iterating Through Intervals:**

Following our solution approach:

Sorted list: [[1,4), [2,3), [3,6)]

with this interval.

covered by [1,4). So, we increment cnt to 2 and update pre to [3,6).

# The first interval is the current reference for comparison

previous\_interval = current\_interval

# Return the final count of non-covered intervals

# Iterate over the sorted intervals starting from the second interval

We first compare [1,4) with [2,3). Here, pre[1] is 4 and e[1] is 3. Since pre[1] >= e[1], we find that [2,3) is covered by

[1,4) and thus, we do not increment cnt.

Return the Result: Having finished iterating through the intervals, we find that the count cnt is 2, which means there are two intervals that remain after removing all that are covered: [[1,4), [3,6)].

Next, we compare [1,4) with [3,6). Here, pre [1] is 4 and e [1] is 6. Since pre [1] < e [1], we find that [3,6) is not

Solution Implementation

This example walk-through demonstrates the efficiency of the algorithm by effectively reducing the number of necessary

comparisons and clearly exhibiting how the sorting step greatly simplifies the process of identifying covered intervals.

class Solution: def removeCoveredIntervals(self, intervals: List[List[int]]) -> int: # Sort intervals based on the start time; in case of a tie, sort by end time in descending order intervals.sort(key=lambda interval: (interval[0], -interval[1]))

# Initialize count of non-covered intervals to 1, as the first one can never be covered by others

```
for current_interval in intervals[1:]:
   # If the end of the current interval is greater than the end of the previous interval,
   # it's not covered, and we should update the count and reference interval
    if previous_interval[1] < current_interval[1]:</pre>
       non_covered_count += 1
```

non\_covered\_count = 1

return non\_covered\_count

previous\_interval = intervals[0]

from typing import List

**Python** 

Java

```
class Solution {
    public int removeCoveredIntervals(int[][] intervals) {
       // Sort the intervals. First by the start in ascending order.
       // If the starts are equal, sort by the end in descending order.
       Arrays.sort(intervals, (a, b) -> {
            if (a[0] == b[0]) {
                return b[1] - a[1];
            } else {
                return a[0] - b[0];
        });
       // Initialize the previous interval as the first interval
       int[] previousInterval = intervals[0];
       // Count the first interval
       int count = 1;
       // Iterate through all intervals starting from the second one
        for (int i = 1; i < intervals.length; ++i) {</pre>
           // If the current interval's end is greater than the previous interval's end,
           // it means the current interval is not covered by the previous interval.
            if (previousInterval[1] < intervals[i][1]) {</pre>
                // Increment the count of non-covered intervals.
                ++count;
                // Update the previous interval to the current interval.
                previousInterval = intervals[i];
```

// If the current interval's end is not greater than the previous interval's end,

// it's covered by the previous interval and we do nothing.

// Return the number of non-covered intervals

// Importing necessary functionalities from standard libraries

// A function that sorts the intervals based on certain criteria

function removeCoveredIntervals(intervals: Interval[]): number {

// Sort the intervals using the defined sorting function

const sortedIntervals = sortIntervals(intervals);

if (intervalA[0] === intervalB[0]) // If start times are the same

return intervalA[0] - intervalB[0]; // Otherwise sort by start time

let countNotCovered = 1; // Initialize count of intervals not covered by others

return intervalB[1] - intervalA[1]; // Sort by end time in descending order

function sortIntervals(intervals: Interval[]): Interval[] {

return intervals.sort((intervalA, intervalB) => {

// Interval type definition for better type clarity

import { sort } from 'algorithm';

type Interval = [number, number];

// Function to remove covered intervals

});

return count;

```
C++
#include <vector>
#include <algorithm> // Include algorithm header for std::sort
// Definition for the Solution class with removeCoveredIntervals method
class Solution {
public:
    int removeCoveredIntervals(vector<vector<int>>& intervals) {
        // Sort the intervals. First by the start time, and if those are equal, by the
        // end time in descending order (to have the longer intervals come first).
        sort(intervals.begin(), intervals.end(), [](const vector<int>& intervalA, const vector<int>& intervalB) {
            if (intervalA[0] == intervalB[0]) // If the start times are the same
                return intervalB[1] < intervalA[1]; // Sort by end time in descending order</pre>
            return intervalA[0] < intervalB[0]; // Otherwise sort by start time</pre>
        });
        int countNotCovered = 1; // Initialize count of intervals not covered by others.
        vector<int> previousInterval = intervals[0]; // Store the first interval as the initial previous interval
        // Iterate through the intervals starting from the second
        for (int i = 1; i < intervals.size(); ++i) {</pre>
            // If the current interval is not covered by the previous interval
            if (previousInterval[1] < intervals[i][1]) {</pre>
                ++countNotCovered; // Increment count as this interval is not covered
                previousInterval = intervals[i]; // Update the previous interval to current interval
        // Return the count of intervals that are not covered by other intervals
        return countNotCovered;
};
TypeScript
// You might need to install the required type definitions for running this code in a TypeScript environment.
```

```
let previousInterval = sortedIntervals[0]; // Store the first interval as the initial previous interval
      // Iterate through the sorted intervals starting from the second one
      for (let i = 1; i < sortedIntervals.length; i++) {</pre>
          // If the current interval is not covered by the previous interval
          if (previousInterval[1] < sortedIntervals[i][1]) {</pre>
              countNotCovered++; // Increment count as this interval is not covered
              previousInterval = sortedIntervals[i]; // Update the previous interval to current interval
      // Return the number of intervals that are not covered by other intervals
      return countNotCovered;
from typing import List
class Solution:
   def removeCoveredIntervals(self, intervals: List[List[int]]) -> int:
       # Sort intervals based on the start time; in case of a tie, sort by end time in descending order
        intervals.sort(key=lambda interval: (interval[0], -interval[1]))
       # Initialize count of non-covered intervals to 1, as the first one can never be covered by others
       non_covered_count = 1
       # The first interval is the current reference for comparison
        previous interval = intervals[0]
       # Iterate over the sorted intervals starting from the second interval
        for current_interval in intervals[1:]:
           # If the end of the current interval is greater than the end of the previous interval,
           # it's not covered, and we should update the count and reference interval
            if previous_interval[1] < current_interval[1]:</pre>
               non covered count += 1
               previous_interval = current_interval
       # Return the final count of non-covered intervals
       return non_covered_count
Time and Space Complexity
Time Complexity
```

### The time complexity of the code is dominated by two operations: the sorting of the intervals and the single pass through the sorted list.

**Space Complexity** 

1. The sort() function in Python uses the Timsort algorithm, which has a time complexity of O(n log n) where n is the number of intervals. 2. After sorting, the code performs a single pass through the list to count the number of non-covered intervals, which has a time complexity of

- 0(n). Combining these two steps, the overall time complexity is  $0(n \log n + n)$ . Simplified, it remains  $0(n \log n)$  because the n log n
- term is dominant.
- 1. Sorting the list is done in-place, which means it doesn't require additional space proportional to the input size. Therefore, the space complexity due to sorting is constant, 0(1).

2. Aside from the sorted list, the algorithm only uses a fixed number of variables (cnt, pre, and e) which also take up constant space.

Hence, the overall space complexity is 0(1), because no additional space that scales with the size of the input is used.

The space complexity refers to the amount of extra space or temporary storage that an algorithm requires.