2219. Maximum Sum Score of Array

Prefix Sum

Problem Description

Medium <u>Array</u>

You need to calculate what is called the sum score for each index of the array. The sum score at a particular index i is defined as the maximum between two sums:

In this problem, you're provided with an array of integers named nums indexed from 0 to n-1, where n is the length of the array.

 The sum of elements from index i through the end of the array. Your task is to determine the maximum **sum score** that can be obtained at any index **i** in the provided array.

the last element of the prefix sum array.

• The sum score at index i is the maximum of these two sums.

The sum of elements from the start of the array up through index i.

- ntuition

The key to solving this problem lies in understanding prefix and suffix sums, which are cumulative sums of the elements of the array from the beginning up to a certain element, and from a certain element to the end, respectively.

This is stored in an array s where s[i] would represent the sum of elements from nums[0] to nums[i-1].

Calculate the prefix sum for the array, which gives you the sum of elements from the start of the array up to each index i.

- Iterate through the array to calculate the sum score at each index. This can be done in a single pass after the prefix sum array has been built:
- For each index i, determine the sum from the start of the array to index i. This is given by the prefix sum at index i + 1 (since we initialized prefix sum with 0 at the beginning).

• To determine the sum from index i to the end of the array, subtract the prefix sum up to index i from the total sum of the array, which is

- After calculating the sum scores for each index, the maximum sum score is the answer, which represents the maximum value obtained from any index i.
- By using a prefix sum array and iterating through the array only once, we can solve this problem efficiently with a time complexity of O(n), where n is the length of the input array.
- The given solution implements the intuition behind the problem in Python. It utilizes the accumulate function from the itertools module to generate prefix sums efficiently and a simple loop to compare sums at each index.

The line s = [0] + list(accumulate(nums)) is crucial. It creates a new list s that stores the prefix sums of the nums array. The

1].

Step 1: Calculate Prefix Sums

Solution Approach

accumulate function takes each element and adds it to the sum of all the previous elements. The [0] at the start of this list is to simplify calculations for the prefix sum at index 0. After this line, s[i] will contain the sum of nums from nums[0] up to nums[i-

The expression (max(s[i + 1], s[-1] - s[i]) for i in range(len(nums))) uses a generator to calculate sum scores without

Step 2: Iterate to Find Maximum Sum Score

array, which is the last element in the prefix sums list).

a single time to find the desired maximum value.

overall time complexity of the function is O(n).

calculations as outlined in the problem description.

Let's walk through an example to illustrate the solution approach.

s = [0] + list(accumulate([3, 1, -2, 5, 2])) = [0, 3, 4, 2, 7, 9]

Next, we iterate through the array to calculate the sum score at each index i.

storing them. For each index i in nums, it calculates two sums:

• s[i + 1] gives us the sum of elements from the beginning of the array to index i (prefix sum).

Here is a step-by-step explanation of the provided code:

• s[-1] - s[i] gives us the sum of elements from index i to the end of the array (this works because s[-1] represents the total sum of the

Step 3: Find the Maximum Value

The max function is used again to find the maximum sum score from the generator. This is the maximum value that can be obtained from any of the sum scores calculated in the previous step. The result of the max function call is returned as the final answer, representing the overall maximum sum score at any index i in

data structure (in this case, a <u>prefix sum</u> array), enabling efficient calculations of subarray sums. It then iterates through the array

the input nums array.

Algorithm Pattern

Data Structure

An array (or list in Python) is the primary data structure used here for storing the prefix sums. **Time Complexity**

Since each of the steps above runs in O(n) time, where n is the length of the nums array, and there are no nested loops, the

The algorithm follows a pattern often used for solving cumulative sum problems: it first preprocesses the input array to build a

Consider the array nums = [3, 1, -2, 5, 2]. Our goal is to find the maximum sum score at any index i after performing the

Example Walkthrough

Step 1: Calculate Prefix Sums

First, we calculate the prefix sums for the array nums. 1. Initialize an array s with an extra 0 at the beginning to simplify the prefix sum calculations. 2. Using the accumulate function from the itertools module, we generate the prefix sums of nums. This results in the following array:

In this array, s[i] represents the sum of elements from nums[0] to nums[i-1]. For example, s[3] = 2 corresponds to the sum of elements 3 +

For index i = 1, the sum from the start to index 1 is s[2] = 4, and from index 1 to the end is s[-1] - s[1] = 9 - 3 = 6.

1 - 2.

Step 2: Iterate to Find Maximum Sum Score

Index 1: max(4, 6) = 6

Index 2: max(4, 7) = 7

Index 3: max(2, 7) = 7

Index 4: max(7, 2) = 7

Step 3: Find the Maximum Value

Solution Implementation

from itertools import accumulate

max score = max(

return max_score

from typing import List

Python

class Solution:

For index i = 0, the sum from the start to index 0 is s[1] = 3, and from index 0 to the end is s[-1] - s[0] = 9 - 0 = 9. The sum score for index 0 is the maximum of these two, which is 9.

The sum score for index 1 is the maximum, which is 6.

Continuing in this way for each index, we compute the sum score: Index 0: max(3, 9) = 9

Finally, we find the maximum sum score from all the calculated sum scores, which is 9 (obtained at index 0).

- Using this approach, we can efficiently determine that the maximum sum score for the array [3, 1, -2, 5, 2] is 9. The solution only iterates through the array once (after computing the prefix sums), thus ensuring a time complexity of O(n).
- prefix_sums = [0] + list(accumulate(nums)) # Calculate the maximum sum score by iterating through each element # in the nums array while taking into account both the sum of elements

Prefix sum array initialization with an extra zero at the beginning

to handle the case where we accumulate from the start of the array.

before the current element (prefix sum) and the sum of elements

max(prefix sums[i + 1], prefix_sums[-1] - prefix_sums[i])

def maximum sum score(self, nums: List[int]) -> int:

after the current element (suffix sum).

for i in range(len(nums))

public long maximumSumScore(int[] nums) {

for (int i = 0; i < length; ++i) {</pre>

// Create an array to store the prefix sums

prefixSums[i + 1] = prefixSums[i] + nums[i];

// the sum from the start to the current element or

// Create and initialize a prefix sum array with an additional

// where prefixSums[i] will hold the sum of nums[0] to nums[i - 1]

// Initialize the answer variable to the minimum possible value

// 1. The sum of elements from the start to the current index (inclusive)

// Compare the sum score at each index with the maxSumScore found so far

Prefix sum array initialization with an extra zero at the beginning

before the current element (prefix sum) and the sum of elements

max(prefix sums[i + 1], prefix_sums[-1] - prefix_sums[i])

1. We first precompute the prefix sums with accumulate(nums), which takes O(n) time.

Math.max(prefixSums[i + 1], prefixSums[numElements] - prefixSums[i])

// 2. The sum of elements from the current index (excluding) to the end

// Iterate through each element and calculate the sum score

// first element set to 0 for ease of calculation

for (let i = 0; i < numElements; ++i) {</pre>

// since we are looking for the maximum

// by taking the higher value between:

for (let i = 0; i < numElements: ++i) {</pre>

// Return the maximum sum score found

def maximum sum score(self, nums: List[int]) -> int:

after the current element (suffix sum).

for i in range(len(nums))

Return the maximum sum score found.

let maxSumScore = -Infinity;

maxSumScore = Math.max(

maxSumScore,

);

let prefixSums = new Array(numElements + 1).fill(0);

prefixSums[i + 1] = prefixSums[i] + nums[i];

// Populate the prefix sum array with cumulative sums.

// the sum from the current element to the end

long sumFromStart = prefixSums[i + 1];

// Initialize the maximum sum as the smallest possible value

// Find the maximum sum score by choosing the larger between

long sumFromEnd = prefixSums[length] - prefixSums[i];

maxSum = Math.max(maxSum, Math.max(sumFromStart, sumFromEnd));

long[] prefixSums = new long[length + 1];

int length = nums.length;

// Calculate the prefix sums

long maxSum = Long.MIN_VALUE;

for (int i = 0; i < length; ++i) {</pre>

// Return the maximum score found

return maxSum;

Return the maximum sum score found.

C++

Java

class Solution {

```
#include <vector>
#include <algorithm> // for std::max
#include <climits> // For INT MIN constant
class Solution {
public:
    long long maximumSumScore(vector<int>& nums) {
        int n = nums.size(): // Get the size of the input vector
        vector<long long> prefixSums(n + 1, 0); // Initialize prefix sums vector with an extra element
        // Calculate prefix sums for the entire array
        for (int i = 0; i < n; ++i) {
            prefixSums[i + 1] = prefixSums[i] + nums[i];
        long long maxScore = LLONG_MIN; // Initialize the maxScore with the smallest possible value for long long
        // Iterate through the array to find the maximum sum score
        for (int i = 0; i < n; ++i) {
            // For each element, we consider two cases:
            // 1. The sum of elements from start up to i (prefixSums[i + 1])
            // 2. The sum of elements from i to the end of the array (prefixSums[n] - prefixSums[i])
            // The maximum of these two values is compared with the maxScore to update it
            maxScore = max(maxScore, max(prefixSums[i + 1], prefixSums[n] - prefixSums[i]));
        // Return the maximum sum score
        return maxScore;
};
TypeScript
function maximumSumScore(nums: number[]): number {
    const numElements = nums.length; // Total number of elements in the array
```

to handle the case where we accumulate from the start of the array. prefix_sums = [0] + list(accumulate(nums)) # Calculate the maximum sum score by iterating through each element # in the nums array while taking into account both the sum of elements

max score = max(

return max_score

following reasons:

return maxSumScore;

from itertools import accumulate

from typing import List

class Solution:

Time and Space Complexity The time complexity of the given code is O(n), where n is the number of elements in the input list nums. This is due to the

2. Then, we perform a single pass over the nums list to calculate the maximum sum score. During each iteration, we calculate the maximum between s[i + 1] and s[-1] - s[i]. There are n such calculations, each taking constant time.

The space complexity of the code is O(n). This is because we are creating a new list called s that contains the prefix sums of

the nums array, which is of size n + 1.