1962. Remove Stones to Minimize the Total

Problem Description

Medium Array Heap (Priority Queue)

You are given an integer array called piles, where each element piles[i] indicates the number of stones in the i-th pile. You are

have been performed. In more detail, the operation consists of choosing any piles[i] and removing floor(piles[i] / 2) stones from it. It's important to note that the same pile can be chosen multiple times for successive operations.

remove half of the stones in it (rounded down). The goal is to minimize the total number of stones left after all the operations

also given an integer k. Your task is to perform exactly k operations on these piles, where in each operation you choose a pile and

After applying k operations, your function should return the minimum possible total number of stones remaining across all piles.

Intuition

The intuition behind the solution is to always target the pile with the largest number of stones for the reduction operation. This is because removing half from a larger number results in a bigger absolute reduction compared to removing half from a smaller pile.

Over k operations, this strategy ensures the greatest possible reduction in the total number of stones.

To effectively apply this strategy, a max-heap is used. A max-heap is a binary tree structure where the parent node is always

larger than or equal to the child nodes. This property allows for the efficient retrieval of the largest element in the collection,

which is exactly what's needed to find the pile with the most stones. In Python, the heapq library provides a min-heap, which can be turned into a max-heap by inserting negative values. Therefore, every value inserted into the heap is negated both when it's put in and when it's taken out.

Here's the step-by-step thought process: 1. Negate all the elements in piles and store them in a heap to create a max-heap out of the Python min-heap implementation. 2. For k iterations, remove the biggest element from the heap (which is the most negative), negate it to get the original value, and then remove half

3. Insert back the negated new value (after halving the biggest element) into the heap. 4. After performing k operations, the heap will contain the negated values representing the remaining stones. To get the total, negate the sum of

the heap's contents.

each operation.

of it (as per the rules of the operation).

Solution Approach The solution leverages a max-heap data structure to efficiently track and remove the largest piles first. Here's how the algorithm

By always choosing the largest pile for halving, the algorithm ensures that the decrease in the total stone count is maximized with

and data structures are utilized in the provided solution:

A heap is created to maintain the current state of the piles. Since Python's heapq library implements a min-heap, the

elements are negated before being pushed onto the heap to simulate a max-heap functionality.

by one, which in essence is dividing by two and using the floor value in integer division.

summed value as the total minimum possible number of stones remaining.

We iterate k times, each time performing the following steps: • The root of the heap (which in this case, is the maximum element, due to negation) is popped off the heap using heappop(). Since the

return -sum(h)

Example Walkthrough

• piles = [10, 4, 2, 7]

• k = 3

•

elements are negated when stored in the heap, we negate it back to get the actual number of stones in the largest pile. We then take the floor of halved value of this pile. The halving operation is conducted by adding 1 to the pile count and right-shifting (>> 1)

- This new halved number of stones is negated and pushed back onto the heap to maintain the max-heap order. This is done using heappush(). The code for this loop is as follows:
- for _ in range(k): p = -heappop(h)heappush(h, -((p + 1) >> 1))
- Finally, after k iterations, the heap contains the negated counts of stones in each pile after the operations have been applied. To find the answer, we sum up all the elements in the heap (which involves negating them back to positive) and return this
- This approach ensures that we are always working with the largest pile available after each operation, thus optimizing our strategy for minimizing the total number of stones.

original amount of stones: 10.

Now the heap is [-7, -4, -2, -5].

Now, let's walk through the solution step by step:

This final step is summarized by this line of code:

Initial State

First, we negate all the elements in piles to simulate a max-heap using Python's min-heap implementation: [-10, -4, -2,

Let's consider a small example to illustrate the solution approach. Suppose we have the following piles and value of k:

We use the heapq library to turn this into a heap: h = [-10, -4, -2, -7].

−7].

Operation 1

•

•

•

Operation 2

Operation 3

Final Summation

Next, we remove half of the stones in this pile. Half of 10 is 5. Since we need to negate and re-insert into the heap, we insert • **-5.**

Since -10 is the maximum value (or smallest when considering negation), it is popped from the heap. We negate it to find the

[-5, -4, -2, -3].

The max value in our heap is now -5. We pop, negate, halve (rounding down to 2), and re-insert -2 into the heap.

To get the total number of stones remaining, we sum the negated values of the heap: -(-4 + -3 + -2 + -2).

Removing half (rounded down) gives 7 / 2 which is 3 when rounded down. Negating and re-inserting -3, the heap is now

The current maximum (minimum in our negated heap) is -7. We pop it and negate it: 7.

So, after performing k = 3 operations on the piles, the minimum number of stones left is 11.

Initialize a max heap as Python only has a min heap implementation.

Pop the largest pile and reduce its stones by half, rounded up.

The sum of the heap is negated to return the actual sum of pile sizes.

reduced_pile = (largest_pile + 1) >> 1 # Using bit shift to divide by 2

Solution Implementation

We are inverting the values to simulate a max heap.

The minus sign ensures we create a max heap.

Perform 'k' operations to reduce the stones in the piles

Push the reduced pile size back into the max heap.

This gives us 4 + 3 + 2 + 2 = 11 as the final answer.

The final state of the heap after 3 operations is [-4, -3, -2, -2].

$max_heap = []$ for pile in piles:

Java

C++

public:

#include <vector>

#include <queue>

class Solution {

Python

class Solution:

from heapq import heappop, heappush

for _ in range(k):

return -sum(max_heap)

return totalStones;

int minStoneSum(vector<int>& piles, int k) {

priority_queue<int> maxHeap;

maxHeap.push(pile);

// Perform the operation k times

// Retrieve the pile with the most stones

int largestPile = maxHeap.top();

maxHeap.push((largestPile + 1) / 2);

remainingStones += maxHeap.top();

// Return the total number of remaining stones

for (int pile : piles) {

while (k-- > 0) {

maxHeap.pop();

int remainingStones = 0;

maxHeap.pop();

return remainingStones;

// Import the necessary components for Heap

// Perform the operation 'k' times

for (let i = 0; i < k; i++) {

let remainingStones = 0;

return remainingStones;

from heapq import heappop, heappush

 $max_heap = []$

for pile in piles:

for _ in range(k):

def minStoneSum(self, piles, k):

heappush(max_heap, -pile)

largest_pile = -heappop(max_heap)

while (maxHeap.length > 0) {

remainingStones += maxHeap.pop();

// Return the total number of remaining stones

// heap structure to use this function as intended.

// Function signature in TypeScript with types defined

function minStoneSum(piles: number[], k: number): number {

// Create a max-heap to keep track of the stones in the piles

// Calculate the remaining number of stones after 'k' operations

Initialize a max heap as Python only has a min heap implementation.

Pop the largest pile and reduce its stones by half, rounded up.

reduced_pile = (largest_pile + 1) >> 1 # Using bit shift to divide by 2

We are inverting the values to simulate a max heap.

The minus sign ensures we create a max heap.

Perform 'k' operations to reduce the stones in the piles

let maxHeap = new Heap<number>(piles, null, (a: number, b: number) => b - a);

while (!maxHeap.empty()) {

// Create a max-heap to keep track of the stones in the piles

// Populate the max-heap with the number of stones in each pile

// Calculate the remaining number of stones after k operations

// Remove half of the stones from the largest pile, round up if necessary

import { Heap } from 'collections/heap.js'; // This library or similar would need to be imported for heap functionality.

def minStoneSum(self, piles, k):

heappush(max_heap, -pile)

largest_pile = -heappop(max_heap)

heappush(max_heap, -reduced_pile)

```
class Solution {
    public int minStoneSum(int[] piles, int k) {
       // Create a max-heap to store the piles in descending order
       PriorityQueue<Integer> maxHeap = new PriorityQueue<>((a, b) -> b - a);
       // Add each pile to the max-heap
       for (int pile : piles) {
           maxHeap.offer(pile);
       // Perform the reduction operation k times
       while (k-- > 0) {
           // Retrieve and remove the largest pile from the heap
           int largestPile = maxHeap.poll();
           // Calculate the reduced number of stones and add back to the heap
           maxHeap.offer((largestPile + 1) >> 1);
       // Calculate the total number of stones after k reductions
       int totalStones = 0;
       while (!maxHeap.isEmpty()) {
           // Remove the stones from the heap and add them to the total count
            totalStones += maxHeap.poll();
       // Return the total number of stones remaining after k operations
```

// Retrieve the pile with the most stones let largestPile = maxHeap.pop(); // Assumes that Heap.pop retrieves the max element // Remove half of the stones from the largest pile, round up if necessary maxHeap.push(Math.ceil(largestPile / 2));

class Solution:

Time Complexity

};

TypeScript

```
# Push the reduced pile size back into the max heap.
           heappush(max_heap, -reduced_pile)
       # The sum of the heap is negated to return the actual sum of pile sizes.
       return -sum(max_heap)
Time and Space Complexity
```

// Note that the `Heap` class I'm using above does not exist in default JavaScript/TypeScript and must be imported

// You'll need to find a suitable library with heap implementation, or you would have to implement your own

// from a library that provides heap data structure implementation. The example uses a fictional 'collections/heap.js'.

2. The main loop which is executed k times: The heap operation heappop: Each pop operation has a complexity of O(log n). The update and heappush back into the heap: These have a complexity of O(log n) for each push operation.

1. Converting the list piles into a heap: This operation is O(n) where n is the length of piles.

The time complexity of the given code is determined by the following major operations:

Therefore, the overall time complexity of the loop is 0(k * log n). Combining this with the heap conversion, the total time complexity is 0(n + k * log n).

Space Complexity

The space complexity is determined by the space needed to store the heap. Since we are not using any additional data structures that grow with input size other than the heap, the space complexity is O(n), where n is the length of the list piles.