1177. Can Make Palindrome from Substring

Hash Table

String

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Problem Description
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Bit Manipulation

Medium

The problem requires us to determine whether a substring of a given string s can be rearranged and possibly modified by replacing up to k letters to form a palindrome. This needs to be done for a series of queries, each represented by a triplet [left, right, k]. Specifically, for each query, we are allowed to:

Prefix Sum

Array

1. Rearrange the substring s [left...right].

If the substring can be made into a palindrome using the above operations, the result for that query is true; otherwise, it is false.

We are to return an array of boolean values representing the result for each query.

2. Replace up to k letters in the substring with any other lowercase English letter.

A palindrome is a string that reads the same forward and backward. For a string to be a palindrome, each character must have a matching pair except for at most one character, which can be in the middle of the palindrome if the string length is odd.

Intuition The intuition behind the solution approach is to first understand the characteristics of a palindrome. For a string to be a

palindrome, each character except for at most one must occur an even number of times (they can be mirrored around the center

of the string).

Given this, we can reformulate the problem as: At most how many characters in the target substring have an odd number of occurrences, and whether this number can be reduced to at most one with at most k character replacements. To efficiently compute the number of characters with odd occurrences in any given substring, the solution employs prefix sums.

Specifically, it calculates the count of each character of the alphabet up to each position in the string. This provides a quick way

to determine the counts of each letter in any substring. Here's the step-by-step approach of the solution:

1. Create a list ss to keep track of the prefix sums – the count of each character up to each index of the string. 2. Iterate over the string s to fill up the ss list with the counts. 3. For each query, use the ss list to calculate the number of characters with an odd count in the target substring.

4. Check if the half of the number of odd-count characters is less than or equal to k, since each pair of odd-count characters can be replaced by any other character to make them even. 5. For each query, append the result (true or false) to the answer list ans.

6. Return the ans list as output once all queries are processed. This approach allows us to efficiently answer each query without having to directly manipulate the substring, reducing the

problem to a question of counting occurrences which can be solved in constant time for each query.

The solution uses the concept of prefix sums and bitwise operations to solve the problem efficiently. Here's how it works, with reference to the key steps in the Python code implementation:

Initialization: A two-dimensional list ss is initiated where ss[i][j] represents the count of the j-th letter (where a is 0, b is 1, and so on) up to the i-th position in the string s. This list is initialized with n + 1 rows and 26 columns (since there are 26 letters in the English alphabet) filled initially with zeros. This extra row is for handling the prefix sum from the beginning of the

then the count of the current character is updated by incrementing the corresponding counter. for i, c in enumerate(s, 1):

ans.append(cnt // 2 <= k)</pre>

Example Walkthrough

[0, 0, 0],

[0, 0, 0],

[0, 0, 0],

[0, 0, 0],

Python

class Solution:

ss = [[0, 0, 0], // before 'a'

[1, 0, 0], // before 'a'

[2, 0, 0], // before 'b'

[2, 1, 0], // before 'b'

[2, 2, 0], // before 'c'

[2, 2, 1], // before 'c'

palindrome, so the result for this query is true.

Calculate the length of the string.

for index, char in enumerate(s, 1):

answers.append(can_form_palindrome)

int stringLength = s.length();

 $string_length = len(s)$

return answers

Java

class Solution {

class Solution {

int n = s.size();

int charCountPrefixSum[n + 1][26];

for (int j = 0; j < 26; ++j) {

for (int j = 0; j < 26; ++j) {

charCountPrefixSum[i][s[i - 1] - 'a']++;

for (int i = 1; i <= n; ++i) {

for (auto& query : queries) {

const lengthOfString = s.length;

public:

[2, 2, 2]] // after 'c'

ss[i] = ss[i - 1][:]

 $ss = [[0] * 26 for _ in range(n + 1)]$

ss[i][ord(c) - ord("a")] += 1

Solution Approach

string.

Processing Queries: For each query [1, r, k], we calculate the number of characters with an odd number of occurrences within the substring s[l...r]. This is done by using the corresponding prefix sums to find the total count of each letter in the

The above line calculates the difference between the counts at the position after the end of the substring (r + 1) and at the

substring and then applying a bitwise AND operation with 1 (which is equivalent to checking if the count is odd).

Populating Prefix Sums: As we iterate through the string s, a temporary copy of the previous row of the ss list is made, and

start of the substring (1). This difference gives us the count of each character in the substring. We then check if this count is odd by using the bitwise AND operation with 1.

number of queries, making it highly efficient for the problem at hand.

[0, 0, 0], // before the second character ('a') and so on

ss = [[0, 0, 0], // before the first character ('a')

substring into a palindrome through k or fewer character replacements.

cnt = sum((ss[r + 1][j] - ss[l][j]) & 1 for j in range(26))

This check is appended to our result list ans. Returning Results: Once all queries are processed, the list ans containing the result of each query is returned. return ans

The use of prefix sums allows for a quick calculation of character occurrences within any given substring in 0(1) time, after an

0(n) preprocessing phase. The overall complexity of the solution is 0(n + q), where n is the length of the string and q is the

Checking for Palindrome Potential: The number of odd-count characters that need to be paired off (which requires

replacement) is cnt // 2. We check if this number is less than or equal to k, which signifies whether we can turn the

Let's consider the string s = "aabbcc" and queries queries = [[0,5,2], [1,4,1]]. Initialization with Prefix Sums: We first initialize our ss list with extra space to handle cases when the substring starts at index 0.

The initialized ss list looks like this initially (considering a simplified alphabet of three letters for this illustration):

[0, 0, 0]] // after the last character ('c') Populating Prefix Sums: After populating the ss list with the prefix sums of each character, the list reflects the following (the -th index in the inner lists corresponds to the alphabetically j-th character):

Query 1: [0, 5, 2] We need to check the substring s[0...5] which is "aabbcc". For this substring, the counts of each character

are 2 a's, 2 b's, and 2 c's. The count of odd-occurring characters cnt is therefore 0. We don't need any replacements to make a

Query 2: [1, 4, 1] This time, we're looking at the substring s[1...4] which is "abbc". Here, the count of each character is 1 a, 2

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bs, and 1 c. Therefore, we have cnt=2 characters occurring an odd number of times ("a" and "c"). We need 1 replacement to make
  either "a" or "c" match the other character (e.g., change "c" to "a" to form "abba"). Since we are allowed to replace up to k=1
  characters, the result for this query is true.
  Answer: Thus, the array of boolean values representing the result for each query is [true, true].
Solution Implementation
```

def canMakePaliQueries(self, s: str, queries: List[List[int]]) -> List[bool]:

Populate the prefix sum matrix with the counts of each character.

can_form_palindrome = odd_count // 2 <= max_replacements</pre>

Return the answers list containing results for all queries.

public List<Boolean> canMakePaliQueries(String s, int[][] queries) {

int[][] charCountPrefixSum = new int[stringLength + 1][26];

// Prefix sum array to keep count of characters up to the ith position

vector<bool> canMakePaliQueries(string s, vector<vector<int>>& queries) {

// Populate the prefix sum array with character frequency counts

charCountPrefixSum[i][j] = charCountPrefixSum[i - 1][j];

int left = query[0], right = query[1], maxReplacements = query[2];

vector<bool> answers; // This will store the answers for each query

// Go through each query to check for palindrome possibility

answers.emplace_back(oddCount / 2 <= maxReplacements);</pre>

return answers; // Return the final answers for all queries

function canMakePaliQueries(s: string, queries: number[][]): boolean[] {

// Create a 2D array to keep track of character frequency up to each position in the string

int oddCount = 0; // Variable to track the count of characters appearing odd number of times

oddCount += (charCountPrefixSum[right + 1][j] - charCountPrefixSum[left][j]) & 1;

// A palindrome can be formed if the half of the odd count is less than or equal to allowed replacements

// Count how many characters appear an odd number of times within the query's range

memset(charCountPrefixSum, 0, sizeof(charCountPrefixSum)); // Initialize the array with 0

Add the result for the current query to the answers list.

prefix_sum = [[0] * 26 for _ in range(string_length + 1)]

prefix_sum[index] = prefix_sum[index - 1][:] prefix_sum[index][ord(char) - ord("a")] += 1 # Initialize a list to store the answers for the queries. answers = []# Process each query in the list of queries. for start, end, max_replacements in queries:

A palindrome can be formed if the half of odd_count is less than or equal to the allowed max_replacements.

Calculate the count of odd occurrences of each letter in the range [start, end].

odd_count = sum((prefix_sum[end + 1][j] - prefix_sum[start][j]) & 1 for j in range(26))

Initialize a prefix sum array where each element is a list representing the count of letters up to that index.

```
// Fill the prefix sum array with character counts
        for (int i = 1; i <= stringLength; ++i) {</pre>
            // Copy the counts from previous index
            for (int j = 0; j < 26; ++j) {
                charCountPrefixSum[i][j] = charCountPrefixSum[i - 1][j];
            // Increment the count of the current character
            charCountPrefixSum[i][s.charAt(i - 1) - 'a']++;
       // List to store results of queries
       List<Boolean> results = new ArrayList<>();
       // Process each query
        for (int[] query : queries) {
            int left = query[0], right = query[1], maxReplacements = query[2];
            int oddCount = 0;
           // Compute the count of characters with odd occurrences in the
           // substring [left, right]
            for (int j = 0; j < 26; ++j) {
                oddCount += (charCountPrefixSum[right + 1][j] - charCountPrefixSum[left][j]) & 1;
            // Add true if half of the oddCount is less than or equal to allowed replacements (maxReplacements)
            results.add(oddCount / 2 <= maxReplacements);
        // Return the list containing results of queries
        return results;
C++
#include <vector>
#include <cstring>
using namespace std;
```

```
const charCountPrefixSum: number[][] = Array(lengthOfString + 1)
    .fill(0)
    .map(() => Array(26).fill(0)); // Array to store the prefix sum of character counts
```

};

TypeScript

```
// Calculate the prefix sum of character counts
      for (let i = 1; i <= lengthOfString; ++i) {</pre>
          charCountPrefixSum[i] = charCountPrefixSum[i - 1].slice(); // Copy previous count
          ++charCountPrefixSum[i][s.charCodeAt(i - 1) - 'a'.charCodeAt(0)]; // Increment count of current character
      const result: boolean[] = [];
      // Process each query
      for (const [left, right, maxReplacements] of queries) {
          let oddCount = 0; // Count of characters that appear an odd number of times
          // Calculate the number of characters with an odd count in the substring
          for (let j = 0; j < 26; ++j) {
              oddCount += (charCountPrefixSum[right + 1][j] - charCountPrefixSum[left][j]) & 1;
          // Push true if half of the odd count is less than or equal to k, otherwise false.
          result.push((oddCount >> 1) <= maxReplacements);</pre>
      return result; // Return the array of boolean results for each query
class Solution:
   def canMakePaliQueries(self, s: str, queries: List[List[int]]) -> List[bool]:
       # Calculate the length of the string.
        string_length = len(s)
       # Initialize a prefix sum array where each element is a list representing the count of letters up to that index.
        prefix_sum = [[0] * 26 for _ in range(string_length + 1)]
       # Populate the prefix sum matrix with the counts of each character.
        for index, char in enumerate(s, 1):
            prefix_sum[index] = prefix_sum[index - 1][:]
            prefix_sum[index][ord(char) - ord("a")] += 1
       # Initialize a list to store the answers for the queries.
        answers = []
       # Process each query in the list of queries.
        for start, end, max_replacements in queries:
           # Calculate the count of odd occurrences of each letter in the range [start, end].
            odd_count = sum((prefix_sum[end + 1][j] - prefix_sum[start][j]) & 1 for j in range(26))
            # A palindrome can be formed if the half of odd_count is less than or equal to the allowed max_replacements.
            can_form_palindrome = odd_count // 2 <= max_replacements</pre>
            # Add the result for the current query to the answers list.
            answers.append(can_form_palindrome)
       # Return the answers list containing results for all queries.
        return answers
Time and Space Complexity
```

palindrome with at most k replacements. The computation of this solution involves pre-computing the frequency of each character in the alphabet at each index of the string s, and then using that information to answer each query.

Time Complexity:

Space Complexity:

1. Building the prefix sum array ss takes 0(n * 26) time, where n is the length of the string s, since we iterate over the string and for each character, we copy the previous counts and update the count of one character. 2. Answering each query involves calculating the difference in character counts between the right and left indices for each of the 26 letters, which

is 0(26). This is done for each query. If there are q queries, this part of the algorithm takes 0(q * 26) time.

The given Python code provides a solution for determining if a substring of the input string s can be rearranged to form a

3. The total time complexity is therefore 0(n * 26 + q * 26) which simplifies to 0(n + q) when multiplied by the constant 26 factor for the alphabet size.

```
1. The prefix sum array ss uses 0(n * 26) space to store the count of characters up to each index in the string s.
2. The space for the answer list is O(q), where q is the number of queries.
3. As such, the total space complexity is the sum of the space for the prefix sum array and the space for the answer list, which is 0(n * 26 + q).
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Hence, the time complexity is 0(n + q).

Thus, the space complexity is 0(n * 26 + q) which can be approximated to 0(n) since the size of the alphabet is constant.