

track of the two scenarios while traversing the array:

Problem Description

The aim of this problem is to find the length of the longest wiggle subsequence in a given integer array, nums. A wiggle sequence is defined as one where consecutive numbers alternate between increasing and decreasing. That means the difference between successive numbers should switch between positive and negative. Single-element sequences and two-element sequences with distinct values are also considered wiggle sequences.

switch signs from positive to negative and vice versa. On the other hand, [1, 4, 7, 2, 5] is not a wiggle sequence because it starts with two positive differences. Similarly, [1, 7, 4, 5, 5] isn't either because it ends with a difference of zero. A subsequence is derived by removing some elements from the original sequence while maintaining the relative order of the

For instance, [1, 7, 4, 9, 2, 5] is a wiggle sequence because the differences between consecutive numbers (6, -3, 5, -7, 3)

remaining elements. The problem asks to return the maximum length of such a longest wiggle subsequence. Intuition

The intuition behind solving this problem lies in dynamic programming. The solution leverages two counters, up and down, to keep

 up: This counter is incremented when the current element is greater than the preceding one, indicating an "up" wiggle. If this occurs, the length of the longest wiggle sequence considering the current number as an "up" number is the current value of down

- plus one. In other words, it's extending a sequence that was last going "down" with an "up" number. down: Conversely, this counter is incremented when the current element is less than the preceding one, signifying a "down" wiggle. In this situation, the length of the longest wiggle sequence considering the current number as a "down" number is derived from the current length of up plus one. That is, we're adding a "down" number to a subsequence that was previously
- "up". An important point to note is that for both up and down, we use the max() function to ensure that we are always recording the maximum length of wiggle subsequence found so far – effectively making this a dynamic programming solution where the optimal solution of the current step is built upon the previous steps. At each step, we make a decision based on the current and previous

elements to update these counters. At the end of the traversal, the length of the longest wiggle subsequence will be the maximum value between the up and down counters because we are interested in the longest possible sequence, regardless of whether it ends on an "up" wiggle or a "down" wiggle.

Solution Approach The implementation of the solution is grounded in the principles of dynamic programming, which is an optimization technique that

In this specific problem, the dynamic programming pattern used involves two one-dimensional arrays, up and down, where each entry

up[i] or down[i] would normally represent the length of the longest wiggle subsequence up to the i-th index of nums that ends with an increasing or decreasing wiggle, respectively. The reference solution compresses these arrays into two simple integer variables because it cleverly leverages the fact the current state only depends on the previous state.

1. Initialize two variables up and down to 1, since a single element is trivially a wiggle subsequence. 2. Loop through the elements of the array starting from the second element because we're comparing each element with its previous one.

∘ If nums[i] is greater than nums[i-1], it means we have a potential "up" wiggle. We then update the up counter as follows:

elements.

1 down = max(down, up + 1)

Here's how the algorithm progresses:

1 up = max(up, down + 1)

solves complex problems by breaking them down into simpler subproblems.

3. For each element at index i, compare it with the element at index i - 1.

- This is under the notion that the current "up" wiggle can extend a sequence that was previously "down", hence down + 1. ∘ If nums [i] is less than nums [i - 1], it signals a potential "down" wiggle and down is updated similarly:
- Here, the current "down" wiggle can extend a sequence that was previously "up". 4. As the for loop continues, up and down are updated dynamically with respect to the sign alternation between consecutive
- 5. After completing the traversal, the largest of up or down is returned as the maximum length of the longest wiggle subsequence found. The reason behind this simple and elegant implementation is that for every position in the array nums [i], the up and down states

captures the length of the longest wiggle subsequence that ends with a "down" or "up" wiggle up to that position, respectively. The

two possible cases of a wiggle (up or down) are covered by these two variables. There's no need to maintain an additional array

Therefore, this algorithm is efficient in terms of both time complexity, which is O(n) since it only requires a single pass through the array, and space complexity, which is 0(1) because it maintains only a constant number of variables.

because the maximum lengths of "up" and "down" wiggle subsequences at any position only depend on the immediate previous one.

wiggle subsequence. Following the solution approach:

1. Initialize two variables up and down to 1. Without loss of generality, we can think of every single number as a trivial wiggle

Let's consider the following input array: nums = [1, 17, 5, 10, 13, 15, 10, 5, 16, 8]. We want to find the length of the longest

\circ At i = 1 (nums[1] = 17, nums[0] = 1):

 \circ At i = 8:

 \circ At i = 9:

Python Solution

if not nums:

return 0

up_sequence_length = 1

if nums[i] > nums[i - 1]:

elif nums[i] < nums[i - 1]:</pre>

public int wiggleMaxLength(int[] nums) {

#include <algorithm> // Include algorithm for max

int wiggleMaxLength(std::vector<int>& nums) {

for (int i = 1; i < nums.size(); ++i) {</pre>

// Check for an 'up' wiggle

if (nums[i] > nums[i - 1]) {

// Check for a 'down' wiggle

else if (nums[i] < nums[i - 1]) {

// Iterate through the array starting from the second element

class Solution:

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subsequence.

Example Walkthrough

1 up = max(up, down + 1) = max(1, 1 + 1) = 2 \circ At i = 2 (nums[2] = 5, nums[1] = 17):

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\circ At i = 3 (nums[3] = 10, nums[2] = 5):
    As nums [3] > nums [2], we have an "up" wiggle. Update up:
       1 up = max(up, down + 1) = max(2, 3 + 1) = 4
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2. Start loop from index 1, since we can only start determining a wiggle by comparing at least two numbers:

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3. Continue this process for each element in the array. The updates will proceed as follows:
    \circ At i = 4:
         ■ nums[4] = 13, nums[3] = 10, so up remains 4 (13 continues the "up" sequence from 10).
    \circ At i = 5:
         • nums [5] = 15, nums [4] = 13, so up remains 4 (15 continues the "up" sequence from 13).
    \circ At i = 6:
         • nums[6] = 10, nums[5] = 15, we update down to 5 (as 10 is down from 15).
    \circ At i = 7:
         • nums[7] = 5, nums[6] = 10, down remains 5 (5 continues the "down" sequence from 10).
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As nums[1] > nums[0], we have an "up" wiggle. Update up:

■ As nums [2] < nums [1], we have a "down" wiggle. Update down:

1 down = max(down, up + 1) = max(1, 2 + 1) = 3

• nums[9] = 8, nums[8] = 16, we update down to 7 (as 8 is down from 16). 4. By the end of the loop, the up and down variables have been updated accordingly. The maximum length of the longest wiggle subsequence is the larger one of up and down, which in this case is down = 7.

this method, we can effectively solve the problem in linear time with constant extra space.

ending with a rising edge (up) and with a falling edge (down),

If the current element is smaller than the previous one,

update the falling edge length (down_sequence_length)

Return the maximum length between the two wiggle subsequences

return max(up_sequence_length, down_sequence_length)

Initialize the two counters that represent the lengths of the longest wiggle sequences

up_sequence_length = max(up_sequence_length, down_sequence_length + 1)

down_sequence_length = max(down_sequence_length, up_sequence_length + 1)

int increasingLength = 1, decreasingLength = 1; // Initialize lengths of the wiggle subsequence

def wiggleMaxLength(self, nums: List[int]) -> int:

starting with the first element both being 1.

• nums[8] = 16, nums[7] = 5, we update up to 6 (as 16 is up from 5).

down_sequence_length = 1 11 12 # Iterate through the array starting from the second element 13 for i in range(1, len(nums)): 14 # If the current element is greater than the previous one, # update the rising edge length (up_sequence_length) 15

This example illustrates how the approach keeps updating the two counters that represent the length of the longest possible wiggle

subsequences based on whether the current element goes "up" or "down" relative to the previous element in the subsequence. With

Java Solution

class Solution {

```
// Loop through the array starting from the second element
           for (int i = 1; i < nums.length; ++i) {</pre>
                if (nums[i] > nums[i - 1]) {
                   // If the current element is greater than the previous one,
                   // then a 'wiggle' peak has been found.
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                    // Update the increasingLength to be the larger of itself or
                    // one more than decreasingLength (indicating a new peak).
11
                    increasingLength = Math.max(increasingLength, decreasingLength + 1);
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13
               } else if (nums[i] < nums[i - 1]) {</pre>
                   // If the current element is less than the previous one,
14
                   // then a 'wiggle' trough has been found.
15
                    // Update the decreasingLength to be the larger of itself or
16
                    // one more than increasingLength (indicating a new trough).
17
                    decreasingLength = Math.max(decreasingLength, increasingLength + 1);
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               // If nums[i] == nums[i - 1], do nothing, as equal values do not contribute to wiggle length
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           // The maximum length of wiggle subsequence would be the max of both
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           // increasing and decreasing lengths
25
            return Math.max(increasingLength, decreasingLength);
26
27 }
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C++ Solution
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int lengthUp = 1; // Initialize 'lengthUp' to represent the length of a wiggle sequence ending with an 'up' difference

int lengthDown = 1; // Initialize 'lengthDown' to represent the length of a wiggle sequence ending with a 'down' difference

14 // If the current number is greater than the previous, update 'lengthUp' // It's the max of itself and 'lengthDown + 1' (to include the current 'up' wiggle) 15 lengthUp = std::max(lengthUp, lengthDown + 1); 16 17

1 #include <vector>

class Solution {

public:

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                   // If the current number is less than the previous, update 'lengthDown'
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                   // It's the max of itself and 'lengthUp + 1' (to include the current 'down' wiggle)
22
                    lengthDown = std::max(lengthDown, lengthUp + 1);
23
               // If nums[i] == nums[i - 1], do nothing as equal elements do not contribute to wiggle sequence
24
25
26
           // Return the maximum length of the two possible wiggle sequences
27
           return std::max(lengthUp, lengthDown);
28
29 };
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Typescript Solution
 1 /**
    * Calculates the length of the longest wiggle sequence from the given array.
    * A wiggle sequence is made up of elements where the differences between
    * successive numbers strictly alternate between positive and negative.
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    * @param {number[]} nums - The input array of numbers
    * @return {number} - The length of the longest wiggle sequence
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    */
    function wiggleMaxLength(nums: number[]): number {
       // Initialize 'up' and 'down' to count the length of the last wiggle subsequences
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       // that are respectively increasing and decreasing.
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       let upSequenceLength = 1;
       let downSequenceLength = 1;
13
14
       // Iterate through the array starting from the second element
15
16
       for (let i = 1; i < nums.length; i++) {</pre>
           const previousNum = nums[i - 1];
17
            const currentNum = nums[i];
18
19
```

32 // If the numbers are equal, neither sequence length is updated, as it doesn't contribute 33 // to a wiggle pattern (since there's no change). 34 35 36 // Return the maximum length between the two subsequences since they track the last wiggle

if (currentNum > previousNum)

else if (currentNum < previousNum) {</pre>

Time and Space Complexity

The given Python code snippet implements the solution for finding the length of the longest wiggle subsequence in an array.

// If the current number is greater than the previous, the sequence is going up.

upSequenceLength = Math.max(upSequenceLength, downSequenceLength + 1);

// If the current number is less than the previous, the sequence is going down.

// which represents adding the current number to the sequence after an up.

downSequenceLength = Math.max(downSequenceLength, upSequenceLength + 1);

// which represents adding the current number to the sequence after a down.

// Update upSequenceLength to be the downSequenceLength plus 1

// Update downSequenceLength to be the upSequenceLength plus 1

// and the longest sequence can end on either an 'up' or a 'down'.

return Math.max(upSequenceLength, downSequenceLength);

To analyze the time complexity, let's look at the operations performed by the code. The code iterates through the nums list once using a single loop that starts from 1 up to len(nums) (non-inclusive). Inside this loop, there are only constant-time operations:

Time Complexity

comparisons, arithmetic operations, and max function calls on integers. As the loop runs for n-1 iterations (where n is the length of nums) and each operation within the loop takes constant time, the overall

time complexity of the code is O(n).

Space Complexity Regarding space complexity, the code uses a fixed number of integer variables (up and down). No matter the size of the input, the

space used by these variables does not increase. There are no additional data structures like lists or sets that grow with the size of the input.

Therefore, the space complexity of the code is 0(1), which means it's constant space complexity.