1679. Max Number of K-Sum Pairs

Medium Array Hash Table Two Pointers Sorting

Leetcode Link

Problem Description

You're provided with an integer array called `nums` and another integer `k`. The goal is to determine how many pairs of numbers you can find and remove from the array such that the sum of each pair equals `k`. The operation of picking and removing such a pair is counted as one operation. The task is to return the maximum number of such operations that you can perform on the given array.

Intuition

To solve this problem, we use a two-pointer technique, which is a common strategy in problems involving sorted arrays or sequences. First, we sort the array in ascending order. After sorting, we position two pointers: one at the beginning (`l`) and one at the end (`r`) of the array.

- If the sum of the values at the two pointers is exactly `k`, we've found a valid pair that can be removed from the array. We increment our operation count (`ans`), and then move the left pointer to the right (`l + 1`) and the right pointer to the left (`r - 1`) to find the next potential pair.
- If the sum is greater than `k`, we need to decrease it. Since the array is sorted, the largest sum can be reduced by moving the right pointer to the left (`r - 1`).
- If the sum is less than `k`, we need to increase it. We do this by moving the left pointer to the right (`l + 1`).

We repeat this process, scanning the array from both ends towards the middle, until the two pointers meet. This approach ensures that we find all valid pairs that can be formed without repeating any number, as each operation requires removing the paired numbers from the array.

The reason this approach works efficiently is that sorting the array allows us to make decisions based on the sum comparison, ensuring that we do not need to reconsider any previous elements once a pair is found or the pointers have been moved.

Solution Approach

The solution provided uses a two-pointer approach to implement the logic that was described in the previous intuition section. Below is a step-by-step walkthrough of the algorithm, referencing the provided Python code.

1. Sort the `nums` list. This is a crucial step as it allows for the two-pointer approach to work efficiently. We need the array to be ordered so we can target sums that are too high or too low by moving the appropriate pointer.

```
nums.sort()
```

2. Initialize two pointers, `l` (left) and `r` (right), at the start and end of the array, respectively. Also, initialize an `ans` variable to count the number of operations.

```
l, r, ans = 0, len(nums) - 1, 0
```

3. Enter a while loop that will continue to execute as long as the left pointer is less than the right pointer, ensuring we do not cross pointers and recheck the same elements.

```
while l < r:
```

4. Within the loop, calculate the sum `s` of the elements at the pointers' positions.

```
s = nums[l] + nums[r]
```

5. Check if the sum `s` equals `k`. If it does:
   - Increment the `ans` variable because we found a valid operation.
   - Move the left pointer one step to the right to seek the next potential pair.
   - Move the right pointer one step to the left.

```
if s == k:
    ans += 1
    l, r = l + 1, r - 1
```

6. If the sum `s` is more significant than `k`, the right pointer must be decremented to find a smaller pair sum.

```
elif s > k:
    r -= 1
```

7. If the sum `s` is less than `k`, the left pointer must be incremented to find a greater pair sum.

```
else:
    l += 1
```

8. After the while loop concludes, return the `ans` variable, which now contains the count of all operations performed — the maximum number of pairs with the sum `k` that were removed from the array.

```
return ans
```

This approach only uses the sorted list and two pointers without additional data structures. The space complexity of the algorithm is O(log n) due to the space required for sorting, with the time complexity being O(n log n) because of the sorting step; the scanning of the array using two pointers is O(n), which does not dominate the time complexity.

Example Walkthrough

Let's take an example to see how the two-pointer solution approach works. Assume we have the following integer array called `nums` and an integer `k = 10`:

```
nums = [3, 5, 4, 6, 2]
```

Let's walk through the algorithm step-by-step:

1. First, we sort the `nums` array:

```
nums = [2, 3, 4, 5, 6] // Sorted array
```

2. We initialize our pointers and answer variable:

```
l = 0  // Left pointer index
r = 4  // Right pointer index (nums.length - 1)
ans = 0  // Number of pairs found
```

3. Start the loop with `while l < r`. Our initial pointers are at positions `nums[0]` and `nums[4]`.

4. At the first iteration, the sum of the elements at the pointers' positions is `s = nums[l] + nums[r] = nums[0] + nums[4] = 2 + 6 = 8`.

5. Since `8` is less than `k`, we increment the left pointer `l` to try and find a larger sum. The pointers are now `l = 1` and `r = 4`.

6. Now, `s = nums[1] + nums[r] = nums[1] + nums[4] = 3 + 6 = 9`.

7. Since `9` is still less than `k`, we increment `l` again. The pointers are now `l = 2` and `r = 4`.

8. Now, `s = nums[l] + nums[r] = nums[2] + nums[4] = 4 + 6 = 10`.

9. Since `10` is equal to `k`, we increment `ans` to `1` and move both pointers inward: `l` becomes `3`, and `r` becomes `3`.

10. Since `l` is no longer less than `r`, the loop ends.

11. We return the `ans` variable, which stands at `1`, indicating we have found one pair `(4, 6)` that sums up to `k`.

Hence, using this approach, the maximum number of operations (pairs summing up to `k`) we can perform on `nums` is `1`.

Python Solution

```
from typing import List

class Solution:
    def max_operations(self, nums: List[int], k: int) -> int:
        # Sort the array first to apply the two-pointer technique
        nums.sort()

        # Initialize two pointers, one at the start and one at the end
        left, right = 0, len(nums) - 1

        # Initialize a counter to keep track of valid operations
        operations_count = 0

        # Iterate through the list with two pointers
        while left < right:
            # Calculate the sum of elements pointed by left and right
            sum_of_pair = nums[left] + nums[right]

            # If the sum equals k, we found a valid pair
            if sum_of_pair == k:
                # Increment the count of valid operations
                operations_count += 1
                # Move both pointers towards the center
                left += 1
                right -= 1
            # If the sum is too large, move the right pointer to the left
            elif sum_of_pair > k:
                right -= 1
            # If the sum is too small, move the left pointer to the right
            else:
                left += 1

        # Return the total count of valid operations
        return operations_count
```

Java Solution

```
class Solution {
    public int maxOperations(int[] nums, int k) {
        // Sort the array to use two pointers approach
        Arrays.sort(nums);

        // Initialize two pointers, one at the start (left) and one at the end (right) of the array
        int left = 0, right = nums.length - 1;

        // Initialize the answer variable to count the number of operations
        int answer = 0;

        // Use a while loop to move the two pointers towards each other
        while (left < right) {
            // Calculate the sum of the two-pointer elements
            int sum = nums[left] + nums[right];

            // Check if the sum is equal to k
            if (sum == k) {
                // If it is, increment the number of operations
                ++answer;
                // Move the left pointer to the right and the right pointer to the left
                ++left;
                --right;
            } else if (sum > k) {
                // If the sum is greater than k, we need to decrease the sum
                // We do this by moving the right pointer to the left
                --right;
            } else {
                // If the sum is less than k, we need to increase the sum
                // We do this by moving the left pointer to the right
                ++left;
            }
        }
        // Return the total number of operations
        return answer;
    }
}
```

C++ Solution

```
#include <vector> // Include necessary header for vector
#include <algorithm> // Include algorithm header for sort function

class Solution {
public:
    int maxOperations(std::vector<int>& nums, int k) {
        // Sort the vector to make two-pointer technique applicable
        std::sort(nums.begin(), nums.end());

        int count = 0; // Initialize count of operations
        int left = 0; // Initialize left pointer
        int right = nums.size() - 1; // Initialize right pointer

        // Use two-pointer technique to find pairs that add up to k
        while (left < right) {
            // When the sum of the current pair equals k
            if (nums[left] + nums[right] == k) {
                left++; // Move left pointer to the right
                right--; // Move right pointer to the left
                count++; // Increment the count of valid operations
            } else if (nums[left] + nums[right] > k) {
                // If the sum is greater than k, move right pointer to the left
                right--;
            } else {
                // If the sum is less than k, move left pointer to the right
                left++;
            }
        }

        return count; // Return the total count of operations
    }
};

// Example usage of the class:
// Solution sol;
// std::vector<int> nums = {3, 1, 3, 4, 3};
// int k = 6;
// int result = sol.maxOperations(nums, k);
// std::cout << "Maximum operations to reach sum k: " << result << std::endl;
```

Typescript Solution

```
function maxOperations(nums: number[], targetSum: number): number {
    const countMap = new Map<number, number>();
    let operationsCount = 0;

    // Iterate over each number in the array
    for (const num of nums) {
        const complement = targetSum - num; // Calculate the complement of the current number

        // If the complement is already in the map,
        // we can form a pair whose sum is equal to targetSum
        if (countMap.get(complement) > 0) {
            countMap.set(complement, countMap.get(complement) - 1); // Decrement the count of complement in map
            operationsCount++; // Increment the count of valid operations
        } else {
            // If the complement is not there, store/update the count of the current number
            const currentCount = (countMap.get(num) || 0) + 1;
            countMap.set(num, currentCount);
        }
    }

    return operationsCount; // Return the total number of operations
}
```

Time and Space Complexity

Time Complexity

The given code has a time complexity of $O(n \log n)$.

Here's the breakdown:

- Sorting the `nums` list takes $O(n \log n)$ time.
- The while loop runs in $O(n)$ time because it iterates through the list at most once by moving two pointers from both ends towards the center. In each iteration, one of the pointers moves, ensuring that the loop cannot run for more than n iterations.
- The operations inside the while loop are all constant time checks and increments, each taking $O(1)$.

Therefore, the combined time complexity is dominated by the sorting step, giving us $O(n \log n)$.

Space Complexity

The space complexity of the code is $O(1)$ provided that the sorting algorithm used in place.

- No additional data structures are used that depend on the input size of `nums`.
- Extra variables `l`, `r`, and `ans` are used, but they occupy constant space.