Problem Description

The problem asks us to perform an inorder traversal on a binary tree and return the sequence of values from the nodes. In binary tree traversal, there are three types of depth-first searches - inorder, preorder, and postorder. Specifically, the inorder traversal follows a defined sequence to visit the nodes:

Visit the right subtree

Visit the root node

Visit the left subtree

This pattern is recursive and is applied to each subtree within the tree. The result of performing an inorder traversal is that the nodes

of the tree are visited in ascending order if the binary tree is a binary search tree. For this problem, we are required to collect the values of the nodes in the order they are visited and return them as a list. Intuition

The proposed solution uses the Morris Traversal approach, which is an optimized way to do tree traversal without recursion and

the node itself, which helps us to get back to the root node after we are done traversing the left subtree. Here's the process how we arrive at the Morris Traversal solution approach:

without using extra space for a stack. The basic idea of Morris Traversal is to link the rightmost node of a node's left subtree back to

 If the root has no left child, it means this node can be visited now, so we add its value to the result list and move to its right child.

Start with the root node.

- If the root has a left child, find the rightmost node in the left subtree (the inorder predecessor of root). If the rightmost node has no right child (is not already linked back to the root), we create a temporary link from it to the root and move the root to its left child.
- If the rightmost node's right child is the root (already linked back), it means we have visited the left subtree already, so we add the root's value to the result list, unlink (restore the tree structure), and move to the right child of the root.
- This approach allows us to use the tree structure itself as a way to navigate through the tree without additional memory usage for the call stack or an auxiliary stack, thus giving us the inorder sequence of node values in O(n) time with O(1) space complexity.
- Solution Approach

The solution provided implements the Morris Traversal as the algorithm for inorder traversal of the binary tree. Here is a walkthrough of the implementation:

The function inorderTraversal begins with an empty list ans, which will contain the sequence of node values in inorder. The main loop runs as long as there is a root to process. The steps in the loop correspond to the ideas discussed in the intuition:

 If root.left is None, it implies there's no left subtree, and the root node can be visited. So, root.val is added to the ans list and root is updated to be root.right, moving on to the next node in the inorder sequence.

- If root, left exists, this means we have a left subtree that needs to be processed first. We then find the inorder predecessor of the root by traversing rightwards (prev = prev.right) until we find a node that either has no right child or whose right
- child is the current root. This predecessor will act as a temporary bridge back to the root after we've finished with the left subtree.
 - If the predecessor's (prev) right child is None, this means we haven't processed the left subtree yet. We, therefore, make a temporary link from the predecessor's right child to the current root (prev.right = root). This allows us to come back to the root after we're done with the left subtree. Then we move root to its left child and continue the loop. • If the predecessor's right child is the current root, this indicates we've returned from traversing the left subtree, and it's now time to visit the root. We, therefore, add root.val to the ans list, remove the temporary link to restore the tree's

structure (prev.right = None), and proceed with root.right.

Morris Traversal uses no additional space for data structures like stacks or the system call stack, making it a very space-efficient approach. The result is a list of node values ans that have been collected in inorder. This list is then returned, providing the solution to the

recursion or an explicit stack to maintain the state during the traversal. Example Walkthrough

This method achieves an O(n) time complexity for traversing through n nodes and O(1) space complexity, as it does not utilize

The loop continues until every node has been visited in the inorder sequence. Since we're altering the tree during traversal, the

traversal, which would visit the nodes in the order 1, 2, 3, as 1 comes first in the left subtree, followed by 2, the root, and finally 3 in

In this tree, we have three nodes, where 2 is the root node, 1 is to its left, and 3 is to its right. We want to perform an inorder

make a temporary link from node 1 to node 2 and then move the root to its left child (1).

The final ans list is [1, 2, 3], which is indeed the inorder traversal of the given binary tree.

no right child, so we would follow the temporary link back to 2. After visiting node 1, we have ans = [1].

Using the Morris Traversal approach, we would proceed as follows:

the right subtree.

problem.

1. We start at the root, which is 2. The root has a left child, so we find the inorder predecessor which is the rightmost node in the left subtree of 2 (which happens to be the node itself since it has no right child in its subtree). Since node 1 has no right child, we

Let's consider a simple binary tree for our example:

this root node. Then we move to the right child of 2, which is node 3. Now the ans list is [1, 2]. 4. At node 3, since there is no left child to process, we visit this node and add its value to the ans list. Now ans = [1, 2, 3]. 5. As there are no more unvisited nodes left, and the right child of 3 is None, the traversal is complete.

3. We arrive back at 2 because of the temporary link. We remove that temporary link and add 2 to the ans list, as we now are to visit

2. Now the current root is 1, which has no left child. Since there's no left subtree to process, we add 1 to the ans list. There is also

after it had been temporarily altered to maintain the traversal state.

Note that during the entire process, no extra space was used for stack or recursion, and the tree's original structure was restored

def __init__(self, val=0, left=None, right=None): self.val = val self.left = left self.right = right

If there is no left child, add the current node's value to the result

Find the rightmost node in the left subtree or the left child itself

If the predecessor's right child is not set to the current node,

set it to the current node and move to the left child of the current node

def inorderTraversal(self, root: Optional[TreeNode]) -> List[int]: # Initialize the output list to store the inorder traversal result = [] 11 12 # Continue traversing until there are no more nodes to process 13

if it does not have a right child. This node will be our "predecessor" predecessor = root.left 24 while predecessor.right and predecessor.right != root: 25

Python Solution

class TreeNode:

class Solution:

while root:

else:

} else {

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and move to the right child

result.append(root.val)

predecessor = predecessor.right

if predecessor.right is None:

if root.left is None:

root = root.right

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1 # Definition for a binary tree node.

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                        predecessor.right = root
31
                        root = root.left
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                    else:
33
                        # If the predecessor's right child is set to the current node,
34
                        # it means we have processed the left subtree, so add the current
                        # node's value to the result and sever the temporary link to restore
35
36
                        # the tree structure. Then, move to the right child.
37
                        result.append(root.val)
                        predecessor.right = None
38
39
                        root = root.right
40
           # Return the result of the inorder traversal
42
            return result
43
Java Solution
 1 /**
    * Definition for a binary tree node.
    * public class TreeNode {
          int val;
          TreeNode left;
          TreeNode right;
          TreeNode() {}
          TreeNode(int val) { this.val = val; }
          TreeNode(int val, TreeNode left, TreeNode right) {
              this.val = val;
              this.left = left;
              this.right = right;
14
    */
16
   class Solution {
18
       public List<Integer> inorderTraversal(TreeNode root) {
           // Initialize an empty list to store the inorder traversal result
19
           List<Integer> result = new ArrayList<>();
20
21
22
           // Continue the process until all nodes are visited
23
           while (root != null) {
24
               // If there is no left child, visit the current node and go to the right child
25
               if (root.left == null) {
26
                    result.add(root.val);
27
                    root = root.right;
```

// Find the inorder predecessor of the current node

// Move to the rightmost node of the left subtree or

// If the right child of the predecessor is not set,

// the right child of the predecessor if it's already set

// this means this is our first time visit this node, thus,

while (predecessor.right != null && predecessor.right != root) {

// set the right child to the current node and move to the left child

// Thus, we should visit the current node and remove the link.

// If the right child is already set to the current node,

// it means we are visiting the node the second time.

result.push_back(root->val); // Add the current node value.

// Find the inorder predecessor of the current root.

// Move to the right subtree.

// Navigate to the rightmost node of the left subtree or to the current root

// Establish a link from the predecessor to the current root, if it does not exist.

// Move root to its left child.

while (predecessor->right != nullptr && predecessor->right != root) {

predecessor->right = root; // Link predecessor to the root.

TreeNode predecessor = root.left;

if (predecessor.right == null) {

root = root.left;

result.add(root.val);

root = root.right;

predecessor.right = null;

// Return the completed list of nodes in inorder

} else {

return result;

predecessor.right = root;

predecessor = predecessor.right;

C++ Solution 1 /** * Definition for a binary tree node. */ struct TreeNode { int val; TreeNode *left; TreeNode *right; TreeNode(): val(0), left(nullptr), right(nullptr) {} 8 TreeNode(int x) : val(x), left(nullptr), right(nullptr) {} 9 TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {} 10 11 }; 12 class Solution { 14 public: vector<int> inorderTraversal(TreeNode* root) { 15 vector<int> result; // This vector will store the inorder traversal result. 16 17 // Loop through all nodes of the tree using Morris Traversal technique. 18 19 while (root != nullptr) { 20 // If there is no left subtree, print the root and move to the right subtree. if (!root->left) { 21

TreeNode* predecessor = root->left;

// if the link is already established.

predecessor = predecessor->right;

39 // A link from the predecessor to the current root already exists, // which means we have finished processing the left subtree. 40 result.push_back(root->val); // Add the value of the current node. 41 42 predecessor->right = nullptr; // Remove the link to restore tree structure. 43 root = root->right; // Move to the right subtree. 44 45 46 47 return result; // Return the result vector containing the inorder traversal. 48 49 };

} else {

if (!predecessor->right) {

root = root->left;

root = root->right;

} else {

/** * Performs an inorder traversal of a binary tree. * @param {TreeNode | null} root - The root node of the binary tree. * @returns {number[]} - An array of node values in the inorder sequence. 12 */

if (root === null) {

return [];

// Recursive case:

Typescript Solution

left: TreeNode | null;

right: TreeNode | null;

interface TreeNode {

val: number;

// Definition for a binary tree node.

```
// 1. Traverse the left subtree and collect the values.
       // 2. Include the value of the current node.
       // 3. Traverse the right subtree and collect the values.
22
       // Then concatenate them in inorder sequence.
       return [
24
           ...inorderTraversal(root.left), // Left subtree values
25
          root.val,
                                        // Current node value
           ...inorderTraversal(root.right) // Right subtree values
28
       1;
29 }
30
Time and Space Complexity
The code implements the Morris In-order Traversal algorithm for a binary tree. Let's analyze both the time and space complexity:
Time Complexity
```

function inorderTraversal(root: TreeNode | null): number[] {

// Base case: if the current root is null, return an empty array.

thereby using the tree itself to guide the traversal.

otherwise O(n) traversal is not affected by this temporary linking as it only adds a constant amount of work for each node.

The space complexity of the algorithm is 0(1). Unlike traditional in-order traversal using recursion (which could lead to 0(h) space complexity where h is the height of the tree due to the call stack), the Morris Traversal does not use any additional space for auxiliary data structures such as stacks or recursion. It uses the given tree's null right pointers to temporarily store the successors of nodes,

The time complexity of the algorithm is O(n), where n is the number of nodes in the binary tree. Each node gets visited exactly twice

in the worst case, once to establish the temporary link to its in-order predecessor and once to remove it and visit the node itself. The **Space Complexity**