2122. Recover the Original Array Enumeration Hash Table Sorting Array Leetcode Link Hard

Problem Description

and added k to each element in arr to form higher. Thus, lower[i] = arr[i] - k and higher[i] = arr[i] + k. Unfortunately, Alice lost all three arrays arr, lower, and higher. She now only remembers a single array nums that contains all the elements of lower and higher mingled together without any indication as to which element belongs to which array. The task is to

Alice had an initial array arr containing n positive integers. To create variability, she decided to generate two new arrays, lower and

higher, each also containing n elements. She chose a positive integer k and subtracted k from each element in arr to form lower,

help Alice by reconstructing the original array arr.

The constraints are that nums consists of 2n integers with exactly n integers from lower and n from higher. We need to return any valid construction of arr. It is important to remember that multiple valid arrays might exist, so any of them will be considered correct. Furthermore, the problem guarantees that there is at least one valid array arr.

Since the original array arr is lost, and the elements in nums cannot be directly distinguished as belonging to either lower or higher,

Intuition

potentially correspond to the original and its modification by k.

we need to analyze the properties of numbers in lower and higher. Recognizing that each element in higher is generated by adding the same fixed value k to the respective elements in lower, we can sort nums to sequentially establish pairs of elements that could

The first step in uncovering arr is sorting nums. After the sort, knowing that the smallest value must be from the lower array and the next smallest that forms a valid pair must be from higher, one can attempt to determine the value of k. This value should be twice the chosen k because it's the difference between counterpart elements from higher and lower. For each potential k (which is the difference between a pair of elements in nums), we check if it's even and not zero. Since k has to be a positive integer, this test eliminates invalid candidates.

Once a potential k is found, we proceed to form the pairs. A boolean array, vis, is used to track elements already used in pairs. If the right elements are not found for pairing, we know the current k candidate is invalid, and we move to the next candidate.

The pairing logic relies on finding elements nums [1] and nums [r] where nums [r] - nums [1] equals the difference d we're exploring as 2k. We keep appending the midpoint of these pairs (nums[l] + nums[r]) / 2 to the ans list until either we run out of elements or can no longer find valid pairs, which indicates a complete arr.

If a complete arr is found where the number of found pairs equals n, we return arr. If not, we continue testing other differences until a valid array is constructed or all possibilities have been exhausted, in which case an empty list is returned.

Alice's initial array arr. 1. Sorting nums: The very first operation in the code is sorting the nums array. This is a common preprocessing step in many problems, as it often simplifies the problem by ordering the elements. In our case, sorting is essential because it allows us to pair

2. Finding the potential k: The for-loop starts with i at index 1, iterating through the sorted nums. Each iteration examines whether

nums [i] - nums [0] is a potential 2k (the actual k multiplied by 2). Only even and non-zero differences are considered valid

elements in nums that could represent an original and its counterpart modified by k.

length of nums), then ans is returned as a valid original array.

elements from both lower and higher arrays: nums = [3, 9, 5, 7].

number that when doubled gives 2.

4. Pairing elements using two pointers:

from typing import List

nums.sort()

n = len(nums)

for i in range(1, n):

class Solution:

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C++ Solution

#include <vector>

4 class Solution {

public:

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58 }

49 };

return {};

Typescript Solution

2 #include <algorithm>

The implementation of the solution involves a few key steps that utilize algorithms and data structures effectively to reconstruct

because we need a positive integer k.

Solution Approach

3. Reconstructing arr: A boolean array vis is created to keep track of which elements have already been paired. Initially, it marks the element corresponding to the current candidate k (nums[i] at the top of the loop) as used. The code maintains two pointers,

1 and r, which start searching for pairs from the beginning of nums. These pointers skip used elements tracked by vis.

candidate 2k). For each such pair, the midpoint (nums[1] + nums[r]) / 2, representing an element in arr, is calculated and appended to ans. 5. Handling edge cases and completing the array: The pairing process continues until it's no longer possible to pair elements according to the current d value. If a complete arr is reconstructed such that the number of pairs equals n (which is half the

6. Returning the result: If, during the pairing process, an inconsistency is found, the algorithm breaks out of the inner while loop,

meaning the current d is not valid, and the for-loop continues with the next candidate. If the algorithm finds a correct sequence

of pairs for ans, it is returned as a valid candidate. Otherwise, the pairing attempt will fail for all differences d, and the function

4. Pairing elements using two pointers: The paired elements are chosen by verifying that nums [r] - nums [1] equals d (the current

The above approach takes advantage of sorted arrays, the two-pointer technique, and the boolean visitation array to implement an efficient and effective solution. Example Walkthrough

Let's walk through the solution approach with a small example. Suppose Alice remembers the following mingled array nums that has

will return an empty list, though this is guaranteed not to happen as per the problem statement.

1. Sort nums: After sorting, the array nums becomes [3, 5, 7, 9]. Sorting ensures that the smallest element, which must be from the lower array, is at the beginning. 2. Finding potential k: Starting from the second smallest number in nums, which is 5, we take the difference with the smallest

number 3, resulting in 2. Since the difference must be 2k (and k is a positive integer), valid potential k values are 1, the only

According to the problem description and solution approach, we want to reconstruct the original array arr. Follow these steps:

3. Reconstructing arr: Initialize vis = [false, false, false, false] since no elements have been paired yet. We will look for pairs that have a difference of 2 (our potential 2k).

We start with the first element 3 and look for an element that has a difference of 2. The next element is 5, and 5 - 3 = 2

 \circ Now, we calculate the midpoint, (3 + 5) / 2 = 4, which is a candidate for arr. Hence, arr = [4]. We continue to the next unvisited element which is 7, and look for its pair. We find 9 (9 - 7 = 2). Now vis = [true, true, true, true].

5. Completing the array: At this point, all elements in nums have been visited and paired correctly. There are two pairs, and this

matches n (since nums is of length 2n and arr of length n). The process is complete, and we have successfully reconstructed arr.

which is our 2k. We mark elements 3 and 5 as visited: vis = [true, true, false, false].

• The midpoint of 7 and 9 is (7 + 9) / 2 = 8, which is added to arr. Now arr = [4, 8].

to effectively reconstruct the array arr that Alice had before the arrays were lost.

Create an array to keep track of visited numbers.

def recoverArray(self, nums: List[int]) -> List[int]:

Initialize the array to be returned.

While there are more elements to process:

Move the r pointer to the next element

// Use i to scan through the array, starting from index 1

for (int i = 1, length = nums.length; i < length; ++i) {</pre>

// Create a boolean array to keep track of visited elements

// Initialize a list to store the elements of the original array

// Advance the right pointer until the condition is met

while (r < length && nums[r] - nums[l] < difference) {</pre>

if (r == length || nums[r] - nums[l] > difference) {

// Iterate through the array, trying to find the correct difference 'd'.

// Keep a visited array to mark the elements that have been used.

for (int left = 1, right = i + 1; right < n; ++left, ++right) {</pre>

while (left < n && visited[left]) ++left;</pre>

// Find the next unvisited element for the left pointer.

while (right < n && nums[right] - nums[left] < diff) ++right;</pre>

if (right == n || nums[right] - nums[left] > diff) break;

visited[right] = true; // Mark the right element as visited.

// Recover and add the original element to 'originalArray'.

originalArray.push_back((nums[left] + nums[right]) / 2);

// If we have successfully recovered the whole array, return it.

if (originalArray.size() == (n / 2)) return originalArray;

// Find the next unvisited element for the left pointer.

while (right < nums.length && nums[right] - nums[left] < diff) {</pre>

if (right >= nums.length || nums[right] - nums[left] > diff) {

// Recover and add the next element to the 'originalArray'.

originalArray.push((nums[left] + nums[right]) / 2);

// If the original array was successfully recovered, return it.

// Move to the next possible unvisited elements.

while (left < nums.length && visited[left]) {</pre>

// Mark the right element as visited.

if (originalArray.length === nums.length / 2) {

// Return an empty array if no valid solution is found.

The time complexity of the algorithm can be analyzed as follows:

left++;

right++;

break;

left++;

right++;

Time and Space Complexity

return [];

Time Complexity

case.

Space Complexity

In conclusion, the space complexity is O(n).

visited[right] = true;

return originalArray;

// Return an empty array if no valid solution is found.

originalArray.push_back((nums[0] + nums[i]) / 2); // Add the first element.

// Skip if the difference is zero or odd, since the problem assumes an even difference.

// Use two pointers to recover the original array using the current difference 'diff'.

// Break if there is no pair found or the difference is larger than 'diff'.

// Find the corresponding pair for the left element such that the difference is 'diff'.

// Advance the left pointer past any already visited elements

// Break if the pointer has reached the end or condition is not met

// Mark the right element as visited and add the reconstructed element

visited[i] = true; // Mark the current element as visited

int difference = nums[i] - nums[0];

continue;

++1;

++r;

break;

int idx = 0;

return ans;

return null;

visited[r] = true;

// Skip if the difference is zero or odd

boolean[] visited = new boolean[length];

tempArray.add((nums[0] + nums[i]) >> 1);

while (l < length && visited[l]) {</pre>

List<Integer> tempArray = new ArrayList<>();

// Add the reconstructed element to the temp list

for (int l = 1, r = i + 1; r < length; ++l, ++r) {

tempArray.add((nums[l] + nums[r]) >> 1);

int[] ans = new int[tempArray.size()];

// Convert the list to an array and return it

if (tempArray.size() == (length >> 1)) {

for (int elem : tempArray) {

ans[idx++] = elem;

// If no array was recovered, return null.

vector<int> recoverArray(vector<int>& nums) {

int diff = nums[i] - nums[0];

vector<bool> visited(n, false);

vector<int> originalArray;

for (int i = 1, n = nums.size(); i < n; ++i) {</pre>

if (diff == 0 || diff % 2 == 1) continue;

// This will store the original array.

// Sort the input array.

visited[i] = true;

sort(nums.begin(), nums.end());

if (difference == 0 || difference % 2 == 1) {

// Calculate the difference between the current element and the first one

// Use two pointers to traverse the array and try to reconstruct the original array

while l < n and visited[l]:</pre>

Move the l pointer to the next unvisited element.

that makes the difference exactly 'difference'.

while r < n and nums[r] - nums[l] < difference:</pre>

Sort the input array in ascending order.

difference = nums[i] - nums[0]

visited = [False] * n

l += 1

r += 1

visited[i] = True

while r < n:

6. Returning the result: The array arr = [4, 8] is returned as a valid construction of Alice's original array.

Python Solution

By following these steps, we have used the sorted array, the two-pointer technique, and a boolean array that tracks paired elements

13 # Ignore differences of zero or that are odd, since 14 # the original problem constraint requires that the difference is even. if difference == 0 or difference % 2 == 1: 15 16 continue

Try to find the difference between a pair of original and added numbers.

23 original_numbers = [(nums[0] + nums[i]) // 2] 24 25 # Initialize pointers for the smaller value (1) 26 # and the larger value (r) in a candidate pair. 27 l, r = 1, i + 128

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# If r reaches the end or the difference is incorrect, break the loop.
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                     if r == n or nums[r] - nums[l] > difference:
                         break
                     # If a valid pair is found, add to visited and original_numbers array.
                     visited[r] = True
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                     original_numbers.append((nums[l] + nums[r]) // 2)
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                     # Move both pointers to the next potential pair.
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                     l, r = l + 1, r + 1
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                 # If the size of the original_numbers is half the size of the input array,
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                 # then we have found all pairs and can return the result.
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                 if len(original_numbers) == n // 2:
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                     return original_numbers
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             # If no valid configuration is found, return an empty array.
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             return []
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 59 # Example use:
 60 # solution = Solution()
 61 # result = solution.recoverArray([1, 3, 4, 2])
 62 # print(result) # Output: The recovered array of original integers.
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Java Solution
  1 import java.util.Arrays;
  2 import java.util.ArrayList;
    import java.util.List;
    class Solution {
         public int[] recoverArray(int[] nums) {
             // Sort the input array to ensure the order
             Arrays.sort(nums);
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38 39 40 41 42 // If we've added the correct number of elements, the array is recovered

31 32 33 34 35 36

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function recoverArray(nums: number[]): number[] {
       // Sort the input array.
        nums.sort((a, b) \Rightarrow a - b);
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       // Iterate through the array, attempting to find the correct difference 'd'.
        for (let i = 1; i < nums.length; i++) {
            let diff = nums[i] - nums[0];
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            // Skip if the difference is zero or odd, since the difference should be even.
            if (diff === 0 || diff % 2 === 1) {
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                continue;
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            // Initialize an array to keep track of visited elements.
            let visited: boolean[] = new Array(nums.length).fill(false);
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            visited[i] = true;
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            // Initialize the array that will store the recovered original array.
            let originalArray: number[] = [];
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            // Add the first element of the original array.
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            originalArray.push((nums[0] + nums[i]) / 2);
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            // Use two pointers to attempt to recover the original array using the current difference 'diff'.
24
            for (let left = 1, right = i + 1; right < nums.length;) {</pre>
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// Find the corresponding pair for the left element that meets the difference 'diff'.

// If the pointers exceed bounds or the difference exceeds 'diff', break out.

2. The outer loop runs at most n times because it iterates through the sorted nums array starting from the second element. 3. For each element in the outer loop, there are two inner loops (while loops) that could potentially run in times each in the worst

However, each element from the nums array gets paired at most once due to the vis array tracking the visited status. This means that in total, each inner loop contributes at maximum n iterations across all iterations of the outer loop, not n per outer loop iteration.

The first inner loop increments 1 until it finds an unvisited element.

Thus, the time complexity is primarily dictated by the outer loop and the pairing process, leading to a complexity of O(n log n) for

1. Sorting the nums array: Sorting an array of size n typically takes 0(n log n) time.

- sorting plus O(n) for pairing, which simplifies to $O(n \log n)$ for the entire algorithm. Therefore, the overall time complexity of the code is $O(n \log n)$.
- The space complexity can be considered by analyzing the storage used by the algorithm: 1. The vis array: An array of size n used to keep track of the visited elements, which occupies O(n) space.

 \circ The second inner loop increments r until it finds the pair element that satisfies nums [r] - nums [1] == d.

- 2. The ans array: Potentially, this array could store n/2 elements when all the correct pairings are made (since pairs are formed), so it uses O(n) space as well.
- As such, the space complexity of the algorithm is determined by the additional arrays used for keeping track of visited elements and storing the answer, leading to 0(n) space complexity.