1276. Number of Burgers with No Waste of Ingredients

Medium Math

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**Problem Description** 

slices available to make burgers. There are two types of burgers: Jumbo Burgers, which require 4 tomato slices and 1 cheese slice, and Small Burgers, which require 2 tomato slices and 1 cheese slice.

The problem provides us with two integers, tomatoSlices and cheeseSlices, representing the number of tomato and cheese

We are asked to find how many of each type of burger we can make such that after making them, there are no remaining tomato or cheese slices. If it is possible, we return a list with two elements, [total\_jumbo, total\_small], representing the count of

or cheese slices. If it is possible, we return a list with two elements, <code>[total\_jumbo, total\_small]</code>, representing the count of Jumbo and Small Burgers, respectively. If it's not possible to use all the tomato and cheese slices exactly, we return an empty list <code>[]</code>.

#### To solve this problem, we can set up a system of linear equations based on the constraints given for making Jumbo and Small

Intuition

Burgers:

Each Jumbo Burger requires 4 tomato slices and 1 cheese slice.
 Each Small Burger requires 2 tomato slices and 1 cheese slice.

- Let  $\mathbf{x}$  be the number of Jumbo Burgers and  $\mathbf{y}$  be the number of Small Burgers. We can derive two equations from the problem
- statement:

signifying that there is no possible solution.

• x + y = cheeseSlices: The total cheese used has to equal the available cheese slices.

We want to find non-negative integer solutions for x and y that satisfy both equations simultaneously. Rearranging the second

equation gives us x = cheeseSlices - y. Substituting this in the first equation allows us to solve for y:

• 4x + 2y = tomatoSlices: The total tomatoes used has to equal the available tomato slices.

4(cheeseSlices - y) + 2y = tomatoSlices 4\*cheeseSlices - 4y + 2y = tomatoSlices 4\*cheeseSlices - tomatoSlices = 2y y = (4\*cheeseSlices - tomatoSlices) / 2

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This gives us a direct way to calculate the number of Small Burgers y, and subsequently, we can find x (number of Jumbo Burgers). However, y must be a non-negative integer for the solution to be valid. Therefore, 4*cheeseSlices - tomatoSlices
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must be a non-negative even number to make y a non-negative integer. Similarly, x must also be a non-negative integer. The provided solution in Python reflects this logic. It ensures that the value for y (k // 2) is not fractional (by checking if k % 2 is not zero) and both x and y are not negative before returning [x, y]. If any of these conditions is not met, it returns [],

Solution Approach

The implementation of the solution adopts a direct approach to solving the system of linear equations derived from the problem

The primary algorithm used here is to derive two linear equations from the given constraints and simplify them to express one

### variable in terms of the other. The equations derived are as follows:

y = cheeseSlices - x

find x and y. Here are the steps in the code:

• x < 0: This checks if x is non-negative.

constraints.

The total tomatoes used for Jumbo and Small Burgers: 4x + 2y = tomatoSlices
 The total cheese used for Jumbo and Small Burgers: x + y = cheeseSlices

These two equations can be simplified to find y:

1. Multiply the second equation by 2: 2(x + y) = 2 \* cheeseSlices

2. Subtract the modified second equation from the first: (4x + 2y) - (2x + 2y) = tomatoSlices - 2 \* cheeseSlices

Now that we have x in terms of tomatoSlices and cheeseSlices, we can find y by substituting x back into one of the original

The Solution class's numOfBurgers method takes the inputs tomatoSlices and cheeseSlices and performs these operations to

equations:

3. x = cheeseSlices - y: Substitute y back into the x + y = cheeseSlices equation to solve for x.

1. k = 4 \* cheeseSlices - tomatoSlices: This is to isolate the y term by combining and rearranging the original equations. 2. y = k // 2: Integer division by 2 to solve for y.

3. Simplify to find x: 2x = tomatoSlices - 2 \* cheeseSlices and hence x = (tomatoSlices - 2 \* cheeseSlices) / 2

k % 2: This checks if k is an even number, as y must be a whole number.
y < 0: This checks if y is non-negative.</li>

- If any of these conditions fail, it indicates that there are no non-negative integer solutions to the problem with the given
- Otherwise, it means valid counts for Jumbo (x) and Small (y) Burgers have been found that use all the tomatoSlices and

burgers that exactly use up all the tomato and cheese slices.

cheeseSlices, and the solution [x, y] is returned.

Before returning [x, y], the method checks three conditions:

The solution utilizes basic arithmetic operations and integer division, which are efficient operations in terms of computational complexity.

tomatoSlices and cheeseSlices, and the method returns an empty list [].

Let's consider a small example with 8 tomato slices and 5 cheese slices.

We want to find out if it's possible to make some combination of Jumbo (4 tomatoes, 1 cheese) and Small (2 tomatoes, 1 cheese)

First, we use the given relationships to create our equations:

• For tomatoes: 4x + 2y = 8 (Equation 1)

### Step 1: Rearrange Equation 2 to isolate x: x = 5 - y

20 - 8 = 2y

no solution.

class Solution:

Java

class Solution {

Solution Implementation

12 = 2y

• For cheese: x + y = 5 (Equation 2)

Now, let's solve for y using these equations.

**Example Walkthrough** 

Step 2: Substitute x in Equation 1 with 5 - y:

have more Small Burgers than the total number of cheese slices, which is not possible.

def numOfBurgers(self, tomato slices: int, cheese slices: int) -> List[int]:

# Calculate the number of 'small' burgers (with 2 tomato slices each)

difference = 4 \* cheese\_slices - tomato\_slices

return [num\_jumbo\_burgers, num\_small\_burgers]

# Find the difference between quadruple the cheese slices and the tomato slices

if difference % 2 == 0 and num small burgers >= 0 and num\_jumbo\_burgers >= 0:

# If any of the conditions above are not met, return an empty list

// This method calculates the number of jumbo and small burgers one can make

// This should be even and non-negative for a valid combination.

// tomato slices used by small burgers compared to jumbo burgers.

// Calculate excess tomato slices after subtracting 4 times the cheese slices.

// If excessTomato is even, half of it represents the difference in number of

// If excessTomato is odd or if we end up with negative counts for either burger,

// Subtracting the number of small burgers from total cheese slices gives

return (excessTomato % 2 == 0 && jumboBurgers >= 0 && smallBurgers >= 0) ?

vector<int>{jumboBurgers, smallBurgers} : vector<int>{};

// This function calculates the number of jumbo and small burgers one can make

// It returns an array with the number of jumbo and small burgers one can make,

# Calculate the number of 'jumbo' burgers (with 4 tomato slices each)

if difference % 2 == 0 and num small burgers >= 0 and num\_jumbo\_burgers >= 0:

# If any of the conditions above are not met, return an empty list

# The result should be valid only if the difference is even, and neither of burgers is negative

num\_jumbo\_burgers = cheese\_slices - num\_small\_burgers

return [num\_jumbo\_burgers, num\_small\_burgers]

// with the given number of tomato and cheese slices.

int smallBurgers = excessTomato / 2;

// us the number of jumbo burgers.

// return an empty vector (no solution).

// with the given number of tomatoSlices and cheeseSlices.

// Jumbo burgers require 4 tomato slices and 1 cheese slice.

// Small burgers require 2 tomato slices and 1 cheese slice.

const excessTomato: number = tomatoSlices - 2 \* cheeseSlices;

// Jumbo burgers require 4 tomato slices and 1 cheese slice.

// Small burgers require 2 tomato slices and 1 cheese slice.

int excessTomato = 4 \* cheeseSlices - tomatoSlices;

int jumboBurgers = cheeseSlices - smallBurgers;

vector<int> numOfBurgers(int tomatoSlices, int cheeseSlices) {

# The result should be valid only if the difference is even, and neither of burgers is negative

solution that exactly uses up all 8 tomato slices and 5 cheese slices with the given constraints.

4(5 - y) + 2y = 820 - 4y + 2y = 8

However, since y (the number of Small Burgers) is 6 and x + y must be 5, we already know something is wrong because we

Since we have found impossible values (negative or more than available cheese slices) for x and y, we conclude that there is no

In correspondence with the Solution class in Python, the method <a href="mailto:num0fBurgers">num0fBurgers</a>(8, 5) would return an empty list [], indicating

Step 3: Solve for y: y = 12 / 2, so y = 6.

As the calculated y exceeds the number of cheese slices, we would subtract y from the total cheese to find x: x = 5 - 6 which gives us x = -1. We cannot have a negative number of burgers.

Python

from typing import List

num\_small\_burgers = difference // 2
# Calculate the number of 'jumbo' burgers (with 4 tomato slices each)
num\_jumbo\_burgers = cheese\_slices - num\_small\_burgers

# Example usage: # solution = Solution() # print(solution.numOfBurgers(16, 7)) # Should output [1, 6] since it is possible to make 1 jumbo and 6 small burgers

return []

// Method to calculate the number of Jumbo and Small burgers that can be made given // the number of tomato and cheese slices. public List<Integer> numOfBurgers(int tomatoSlices, int cheeseSlices) { // Calculate the difference between four times the number of cheese slices and tomato slices int difference = 4 \* cheeseSlices - tomatoSlices; // Calculate the number of Small burgers by dividing the difference by 2 int numSmallBurgers = difference / 2; // Calculate the number of Jumbo burgers by subtracting the number of Small burgers // from the total cheese slices int numJumboBurgers = cheeseSlices - numSmallBurgers; // Check if difference is even and both calculated burger amounts are non-negative boolean isSolutionValid = difference % 2 == 0 && numSmallBurgers >= 0 && numJumboBurgers >= 0; // Return the number of Jumbo and Small burgers, if possible; otherwise, return an empty list return isSolutionValid ? Arrays.asList(numJumboBurgers, numSmallBurgers) : Collections.emptyList(); class Solution { public:

```
// or an empty array if there's no valid combination.
function numOfBurgers(tomatoSlices: number, cheeseSlices: number): number[] {
    // Calculate excess tomato slices after subtracting 2 times the number of cheese slices.
    // This excess must be even and non-negative for a valid combination.
```

**}**;

**TypeScript** 

```
// If the excess is divisible by 2, it represents the additional tomatoes
   // needed to upgrade small burgers to jumbo burgers.
   const conversionToJumbo: number = excessTomato / 2;
   // The number of jumbo burgers is equal to the excess divided by 2,
   // since each conversion to a jumbo requires 2 additional tomatoes.
   const jumboBurgers: number = cheeseSlices - conversionToJumbo;
   // If the excess is odd or we have a negative count of either type of burger,
   // return an empty array to indicate no solution is possible.
   // Otherwise, return the counts in an array where the first element is jumbo burgers
   // and the second is small burgers.
   if (excessTomato % 2 === 0 && iumboBurgers >= 0 && conversionToJumbo >= 0) {
        return [jumboBurgers, conversionToJumbo];
   } else {
       return [];
from typing import List
class Solution:
   def numOfBurgers(self. tomato slices: int. cheese slices: int) -> List[int]:
       # Find the difference between quadruple the cheese slices and the tomato slices
       difference = 4 * cheese_slices - tomato_slices
       # Calculate the number of 'small' burgers (with 2 tomato slices each)
       num_small_burgers = difference // 2
```

# return [] # Example usage: # solution = Solution() # print(solution.numOfBurgers(16, 7)) # Should output [1, 6] since it is possible to make 1 jumbo and 6 small burgers

else:

## Time Complexity

Time and Space Complexity

The given code consists of simple arithmetic calculations and conditional checks, which do not depend on the size of the input but are executed a constant number of times. Therefore, the time complexity is 0(1).

## Space Complexity

The space complexity of the code is also 0(1) since it uses a fixed amount of space for the variables k, y, x, and the return list regardless of the input size. The solution does not utilize any additional data structures that grow with the size of the input.