139. Word Break

Hash Table

String

<u>Array</u>

Problem Description

Medium

Memoization

given dictionary wordDict. To put it simply, the problem is asking whether we can break the string s into chunks where each chunk matches a word in the provided list of words (which we call a dictionary). A word from the dictionary can be used multiple times if needed. For example, if s is "leetcode" and wordDict contains "leet" and "code", then the answer is true since "leetcode" can be

The LeetCode problem asks us to determine if a given string s can be split into a sequence of one or more words that exist in a

Dynamic Programming

segmented into "leet code".

Intuition

The intuition behind the solution is to use <u>Dynamic Programming</u> (DP), which is a method for solving complex problems by breaking them down into simpler subproblems. The idea here is that if we can break the string s up to a given point, then we can

independently check the remainder of the string for other words from wordDict. We can cache results to avoid redundant computations for the same substrings. One way to visualize this solution is by thinking of a chain. If breaking the chain at a given link (character of string s) gives us two parts, where the left part has been seen before and is confirmed to be composed of words in wordDict, and the right part is a

known dictionary word, then the entire chain up to that point can be composed of dictionary words. In the solution provided, the list f is used to store the results of the subproblems. Here's what it represents: f[0] is True because a string with no characters can trivially be segmented (it's an empty sequence, which is considered a

valid segmentation).

words. So f[i] is set to True if, for any j where $0 \le j \le i$, f[j] is True and the substring s[j:i] is in wordDict. The algorithm loops over the length of the string, checking at each character if there is a valid word ending at this character and,

f[i] for i>0 is True if and only if the string up to the i-th character can be segmented into one or more of the dictionary

i, we set f[i] to True. By the time we reach the end of the string if f[n] (where n is the length of the string) is True, we know the entire string can be split up according to the wordDict. Otherwise, f[n] will be False, indicating that the string s cannot be segmented into a

simultaneously, if the string before this word can be split into valid words. If both these conditions are ever fulfilled at some index

sequence of one or more dictionary words. **Solution Approach**

The solution utilizes dynamic programming, which involves solving smaller subproblems and using their solutions to effectively

solve larger problems. In this context, the subproblems are answering the question: "Can the string up to the i-th character be

An array f is created with a size of n+1 where n is the length of the string s. The array f is initialized to all False except for f[0] which is True. This represents that it's always possible to segment an empty string.

Let's delve into the algorithm and the data structures used:

segmented into a sequence of dictionary words?"

valid, two conditions must be met:

The substring s[j:i] must be in words.

We then iterate over the string s from the first character to the last, checking at each point whether the string up to that point can be segmented. This is achieved by using a nested loop, where the outer loop iterates from 1 to n and represents the end

We start by initializing a set words from wordDict for fast lookups of words in the dictionary.

of the substring. At each position i, we check all possible substrings s[j:i] where j ranges from 0 up to i-1. For a substring s[j:i] to be

of the current substring being checked (i), and the inner loop (j) iterates from 0 to i-1 and represents different start points

- The f[j] entry must be True, signifying that the string can be segmented up to the j-th character. If both conditions are satisfied for any j, we set f[i] to True because we've found that the string can be segmented up to the i-th character. Finally, f[n] indicates whether the entire string can be segmented. If it's True, then the string can be split into a valid
- sequence of dictionary words, and we return True. If it's False, then there is no way to split the entire string into valid dictionary words, and we return False. In summary, this problem is efficiently solved by breaking it down into smaller parts, solving each part individually, and then

combining those solutions to find the answer to the original problem. The any() function in Python provides a succinct way to

Example Walkthrough Let's assume s = "applepenapple" and wordDict = ["apple", "pen"]. We want to check if s can be split into words contained in

check whether any substring s[j:i] fulfills our two conditions, making the code more concise and readable.

Initialize the set words from wordDict for quick lookups: words = {"apple", "pen"} Initialize the array f with False and set f[0] = True (an empty string can always be segmented):

Then we iterate over the length of the string s from 1 through n, which is 15 in this case for "applepenapple".

f[0] = True

= [False] * (len(s) + 1)

∘ Is "apple" (s[0:5]) in words? Yes, it is.

∘ Is "pen" in words? Yes, it is.

apple", all words from wordDict.

Solution Implementation

words = set(word_set)

 $length_of_s = len(s)$

return can_break[length_of_s]

// Get the length of the string 's'

// Empty string is a valid decomposition

for (int i = 1; i <= strLength; ++i) {</pre>

// Try different break points

for (int j = 0; j < i; ++j) {

int strLength = s.length();

wordBreakTracker[0] = true;

Python

Java

class Solution:

Move to i = 8, the substring is "pen" (s[5:8]):

At i = 15, our substring is "apple" again (s[8:15]):

wordDict.

o Is f [0] True? Yes, because we initialized it as such, indicating that up to the previous characters (none in this case), the string can be segmented. • Therefore, f[5] becomes True.

 \circ Is f[5] True? Yes, because we know "apple" can be segmented till i = 5. • We set f[8] to True.

For each i from 1 to 15, we will check all substrings s[j:i] for j from 0 up to i-1.

Consider the case when i = 5, we are looking at the substring "apple":

- ∘ Is "apple" in words? Yes. Is f[8] True? Yes, due to previous segments.
- ∘ f[15] is set to True. Finally, we check f[n], which is f[15] in this case. It is True, which means "applepenapple" can be segmented as "apple pen

def wordBreak(self, s: str, word_set: List[str]) -> bool:

Get the length of the string to process

Initialize a set with dictionary words for quicker look-up

By following these steps, we have broken down the problem to show how s can be segmented using wordDict, illustrating the dynamic programming approach described in the solution.

can_break = [True] + [False] * length_of_s # Iterate over all the positions of the string for i in range(1, length_of_s + 1):

Initialize a list where f[i] represents whether s[:i] can be segmented into words in the dictionary

Determine if there is a j where s[:j] can be segmented and s[j:i] is in the dictionary

// f[i] is true if first i characters of the string can be segmented into dictionary words

can_break[i] = any(can_break[j] and s[j:i] in words for j in range(i))

Return the value for the whole string, whether it can be segmented or not

// Initialize a boolean array to keep track of possible word breaks

// Then, mark the position i as true in wordBreakTracker

if (wordBreakTracker[j] && wordSet.contains(s.substring(j, i))) {

boolean[] wordBreakTracker = new boolean[strLength + 1];

// Check each substring starting from length 1 to strLength

wordBreakTracker[i] = true;

```
class Solution {
    public boolean wordBreak(String s, List<String> wordDict) {
       // Convert the list of words into a hash set for efficient look-up
       Set<String> wordSet = new HashSet<>(wordDict);
```

```
// Break out of the loop since we have found a valid break point
                    break;
       // The last entry in wordBreakTracker tells if the entire string can be segmented or not
       return wordBreakTracker[strLength];
C++
#include <string>
#include <vector>
#include <unordered_set>
#include <cstring>
class Solution {
public:
    // Function to determine if the string s can be segmented into space-separated
    // sequence of one or more dictionary words.
    bool wordBreak(string s, vector<string>& wordDict) {
       // Create a set containing all the words in the dictionary for constant time look-up.
       unordered_set<string> word_set(wordDict.begin(), wordDict.end());
       // Get the length of the string.
       int strLength = s.size();
       // Array to hold the status of substrings, f[i] is true if s[0...i-1] can be segmented.
       bool canSegment[strLength + 1];
       // Initialize the canSegment array with false values.
       memset(canSegment, false, sizeof(canSegment));
       // Empty string is always a valid segmentation.
       canSegment[0] = true;
       // Start checking for all substrings starting from the first character.
        for (int i = 1; i <= strLength; ++i) {</pre>
           // Check all possible sub-strings ending at position i.
            for (int j = 0; j < i; ++j) {
                // If s[0..j-1] can be segmented and s[j..i-1] is in the word set,
                // then set canSegment[i] to true.
                if (canSegment[j] && word_set.count(s.substr(j, i - j))) {
                    canSegment[i] = true;
                    // Break because we found a valid segmentation until i.
                    break;
```

// If the string up to j can be broken into valid words, and the substring from j to i is in the dictionary

```
// Check for every possible partition position 'startIndex'.
    for (let startIndex = 0; startIndex < endIndex; ++startIndex) {</pre>
       // If the string can be segmented up to 'startIndex' and the substring from 'startIndex' to 'endIndex'
       // is in the word dictionary, update 'canBreak' for 'endIndex' and break out of the loop.
        if (canBreak[startIndex] && wordSet.has(s.substring(startIndex, endIndex))) {
            canBreak[endIndex] = true;
            break;
// Return whether the string can be segmented up to its entire length.
return canBreak[stringLength];
```

const wordSet = new Set(wordDict); // Create a Set from the wordDict for efficient look-up.

canBreak[0] = true; // The string can always be segmented at index 0 (empty string).

// Initialize an array 'canBreak' to keep track of whether the string can be segmented up to each index.

// Return true if the whole string can be segmented, otherwise false.

const stringLength = s.length; // Store the length of the input string.

const canBreak: boolean[] = new Array(stringLength + 1).fill(false);

for (let endIndex = 1; endIndex <= stringLength; ++endIndex) {</pre>

return canSegment[strLength];

// Iterate over the string.

words = set(word_set)

 $length_of_s = len(s)$

function wordBreak(s: string, wordDict: string[]): boolean {

def wordBreak(self, s: str, word_set: List[str]) -> bool:

Get the length of the string to process

can break = [True] + [False] * length of s

for i in range(1, length_of_s + 1):

one or more dictionary words from wordDict.

return can_break[length_of_s]

Time and Space Complexity

Space Complexity

Iterate over all the positions of the string

Initialize a set with dictionary words for quicker look-up

};

TypeScript

class Solution:

```
Time Complexity
 To calculate the time complexity, we need to consider the operations performed within the loop:
```

The given code defines a method wordBreak that checks whether you can segment a string s into a space-separated sequence of

Initialize a list where f[i] represents whether s[:i] can be segmented into words in the dictionary

Determine if there is a j where s[:j] can be segmented and s[j:i] is in the dictionary

can_break[i] = any(can_break[j] and s[j:i] in words for j in range(i))

Return the value for the whole string, whether it can be segmented or not

3. For each of these elements, we check if f[j] is True (constant time) and s[j:i] in words which is O(i-j) in the worst case since looking up in a set is O(1) but slicing the string is O(i-j). The worst-case time complexity is when s[j:i] is a word for all j and i, so we have to check every possible substring. Thus, the

1. We iterate over the length of the string s which gives us an O(n) where n is the length of the input string.

2. Inside each iteration, the any() function is called which in worst-case will iterate over i elements.

- time complexity becomes $0(n^2 * k)$ where k is the maximum length of the word because for each i, we perform i checks and each check could take up to k time due to string slicing.
- The space complexity can be analyzed by looking at the storage used: 1. The set words is O(m) where m is the total number of characters across all words in wordDict. 2. The list f is 0(n+1) which simplifies to 0(n) where n is the length of the input string s.

Therefore, the overall space complexity is 0(n + m).

Note: Due to Python's internal implementation of string slicing, it can be argued that string slicing is done in 0(1) under normal circumstances due to string interning and slicing just pointing to a subpart of the existing string without actually creating a new one. However, to be safe, especially considering the worst-case scenarios where slicing may not benefit from such optimizations, we generally consider the string slicing time complexity as O(k).