1898. Maximum Number of Removable Characters

Medium Array Binary Search String

Problem Description

indices from s. The goal is to find out the maximum number of characters you can remove from s (using the indices provided in removable from lowest to highest) so that p remains a subsequence of s. The steps for removing characters are as follows: mark characters in s at indices indicated by the first k elements of removable, remove them, and then check if p remains a subsequence of the modified s. A subsequence is a sequence that can be derived from another sequence by deleting some elements without changing the order of the remaining elements.

You are provided with two strings s and p, where p must be a subsequence of s. There is also an array called removable with distinct

Leetcode Link

The key to solving this problem lies in understanding that once you remove characters from s, you must check whether each

Intuition

approach this problem using binary search. The intuition behind using binary search here is that if removing k characters still leaves p as a subsequence, removing fewer than k

subsequent removal maintains p as a subsequence. Since removable contains distinct indices, and we want to maximize k, we can

characters will also leave p as a subsequence. Conversely, if p is not a subsequence after removing k characters, removing more than k characters will certainly not leave p as a subsequence. Therefore, there is a threshold value for k which we want to find - the maximum k for which p remains a subsequence. Binary search allows us to efficiently home in on this threshold by halving the search

space with each iteration and identifying the exact point where p stops being a subsequence. In the provided solution, the function check(k) takes a number k and simulates the process of marking and removing k characters from s to verify if p remains a subsequence. The binary search then adjusts the search interval (left, right) based on the outcomes of check(k). If p is still a subsequence after removing k characters, it means we could possibly remove more, so the search space is

adjusted to [mid, right]. If not, we have removed too many characters, and the search space is adjusted to [left, mid-1]. The search continues until the maximum k is found. Solution Approach The implementation makes use of a binary search pattern, specifically what's often referred to as "Binary Search Template 2". This is

due to the way the mid point is calculated and how the search space is adjusted. The pattern is conducive when we want to search

for the element or condition which requires accessing the current index and its immediate right neighbour in the array.

is monotonic—that is, if removing k characters works, then removing any less than k will also work.

higher numbers when the check(mid) is successful, ultimately helping to identify the upper bound of k.

If the end of p is reached (j = n), then p is still a subsequence of s after the removals.

Here's the breakdown of the solution approach:

1. Binary Search Algorithm: We want to find the maximum value of k such that removing k characters specified by the first k indices in removable from s leaves p as a subsequence. We perform a binary search over the length of the array removable because the problem has a "yes" or "no" nature (is p still a subsequence after the removal?) and because the removal condition

2. check Function: This function simulates the removal of characters from s and checks if p is still a subsequence. It uses two

pointers, i for the string s and j for the string p. As it iterates over s, it skips over the characters at the indices specified in the first k entries of removable. If a non-removable character in s matches the current character in p, it moves the pointer j forward.

subsequence, thus giving us the maximum k.

Let's consider a small example to illustrate the solution approach.

- 3. Set Data Structure: A set called ids is used to store the indices from removable that we're proposing to remove. This allows constant-time checks to determine if a character at a particular index in s should be skipped during the subsequence check. 4. Calculating mid: The variable mid is calculated as (left + right + 1) // 2 to ensure that the search space moves towards the
- 5. Adjusting Search Space: Based on the results of check(mid), the binary search narrows the search space. If removing mid characters works, it means we should look for a possibly higher k, so the new search interval is [mid, right]. If not, we search the space [left, mid - 1]. The search ends when left and right meet, which will be the point just before p stops being a
- in s, despite the removals. Example Walkthrough

The combination of these components results in a solution that efficiently pinpoints the largest k for which p remains a subsequence

s = "abcacb" p = "ab"

1. Initial Setup: We set up our binary search with bounds left = 0 and right = len(removable) - 1 = 2. The goal is to find the

2. First Iteration:

3. Second Iteration:

subsequence of s after removal is 1.

from typing import List

class Solution:

the characters at indices [0, 1] from s).

pattern_index = 0

 \circ Calculate mid = (1 + 2 + 1) // 2 = 2.

Applying Binary Search

removable = [3, 1, 0]

Suppose:

Calculate mid = (left + right + 1) // 2 = (0 + 2 + 1) // 2 = 1. • Use check(1) to simulate the removal of characters at indices removable[0] and removable[1], which are 0 and 1.

Since check(1) is true, we adjust the search range to [mid, right] which means [1, 2].

After removal, s = "_b_acb". p = "ab" is still a subsequence of this new string s.

maximum k such that p is still a subsequence of the modified s after the removal.

 Use check(2) to simulate the removal of characters at indices removable[0], removable[1], and removable[2], which are 0, 1, and 3. After removal, s = "_b__cb". p = "ab" is no longer a subsequence of s. Since check(2) is false, we adjust the search range to [left, mid - 1] which means [1, 1].

Since left and right are the same, we conclude the binary search. We determined that the maximum k for which p = "ab" remains a

Therefore, the maximum number of characters that can be removed from s while ensuring p remains a subsequence is 1 (removing

Python Solution

def maximum_removals(self, string: str, pattern: str, removable: List[int]) -> int:

Check if current index is not removed, and characters match

We can form the pattern if we have gone through all characters of the pattern

Move to the next character in the pattern

Move to the next character in the string

mid = (left + right + 1) // 2 # Pick the middle value

Check if the pattern can be formed after removing mid characters

// Create a hash set to store the indices of characters to be removed

if (!removalSet.contains(i) && s.charAt(i) == p.charAt(j)) {

// If we've found the whole string p, return true; otherwise, return false

int maximumRemovals(std::string s, std::string p, std::vector<int>& removable) {

// Binary search to find the maximum number of characters that can be removed

// Iterate over string s and p to check if p is a subsequence

i++; // Always move i to the next character

int left = 0, right = removable.size();

int mid = (left + right + 1) / 2;

// Choose the midpoint of the current range

while (left < right) {

removalSet.add(removable[k]); // Add removable characters' indices up to mid

// If current index is not in the removal set and characters match, move j

Set<Integer> removalSet = new HashSet<>();

for (int k = 0; k < mid; k++) {

while (i < sLen && j < pLen) {

j++;

return j == pLen;

def can_form_pattern_after_removals(k: int) -> bool:

Initialize pointers for pattern and string

pattern index += 1

return pattern_index == pattern_length

string_index += 1

while left < right:

string_index = 0 # Convert the list of removable indices up to k into a set for faster look-ups removal_set = set(removable[:k]) 10 # Iterate through string and pattern 11 12 while pattern_index < pattern_length and string_index < string_length:</pre>

if string_index not in removal_set and string[string_index] == pattern[pattern_index]:

22 # Get string and pattern lengths string_length, pattern_length = len(string), len(pattern) 23 24 # Set the search space for the binary search 25 left, right = 0, len(removable) 26 # Perform binary search to find the maximum number of removable characters

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C++ Solution

#include <vector>

#include <unordered_set>

2 #include <string>

class Solution {

public:

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```
if can_form_pattern_after_removals(mid):
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                   left = mid # If it is possible, try removing more characters
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               elser
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                   right = mid - 1 # Otherwise, try with fewer removable characters
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            return left # The maximum number of removable characters is left
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36 # Explanation:
37 # The above code checks the maximum number of indices that can be removed from the string `s`
38 # such that it is still possible to find the pattern `p` as a subsequence.
39 # It uses binary search to efficiently find this maximum number.
Java Solution
 1 class Solution {
       // Method to find the maximum number of characters that can be removed from
       // string s so that string p is still a subsequence of s
       public int maximumRemovals(String s, String p, int[] removable) {
           int left = 0, right = removable.length; // Define binary search boundaries
 6
           // Perform binary search to find the maximum index 'mid'
           while (left < right) {</pre>
               int mid = (left + right + 1) / 2; // Choose a middle point (avoid overflow)
 9
               // Check if string p is still a subsequence of s after removing mid characters
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               if (checkSubsequence(s, p, removable, mid)) {
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                   left = mid; // Move left pointer to mid if p is still a subsequence
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               } else {
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                   right = mid - 1; // Move right pointer if p is not a subsequence
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           return left; // Returns maximum removables that still keep p as a subsequence of s
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       // Helper method to check if p is a subsequence of s after removing certain characters
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       private boolean checkSubsequence(String s, String p, int[] removable, int mid) {
            int sLen = s.length(); // Length of string s
           int pLen = p.length(); // Length of string p
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            int i = 0; // Index for iterating over s
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            int j = 0; // Index for iterating over p
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                 // Check if the subsequence 'p' is still in 's' after removing 'mid' characters
                 if (checkSubsequence(s, p, removable, mid)) {
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                     left = mid; // If it is, increase the lower bound of the search range
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                 } else {
 19
                     right = mid - 1; // If not, decrease the upper bound of the search range
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             return left; // The maximum number of characters we can remove
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         // Helper function to check if 'p' is a subsequence of 's' after removing 'mid' characters
 26
         bool checkSubsequence(std::string& s, std::string& p, std::vector<int>& removable, int mid) {
 27
             int sLength = s.size();
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             int pLength = p.size();
 29
             int i = 0, j = 0; // Pointers for string 's' and the subsequence 'p'
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 31
             // Using a set to keep track of the indices that have been removed
             std::unordered_set<int> removedIndices;
             for (int k = 0; k < mid; ++k) {
                 removedIndices.insert(removable[k]);
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             // Iterate over both strings and check if 'p' is a subsequence of 's'
 38
             while (i < sLength && j < pLength) {</pre>
 39
                 // If the current character is not removed and matches with `p[j]`,
                 // move the pointer 'j' of subsequence 'p'
 40
                 if (removedIndices.count(i) == 0 && s[i] == p[j]) {
 41
 42
                     ++j;
 43
 44
                 ++i; // Always move the pointer `i` of string `s`
 45
 46
 47
             // If we have iterated through the entire subsequence `p`, it's a subsequence of `s`
 48
             return j == pLength;
 49
 50 };
 51
Typescript Solution
1 // Function to determine the maximum number of characters that can be removed
2 // from string 's' such that string 'p' is still a subsequence of 's'.
   function maximumRemovals(s: string, p: string, removable: number[]): number {
       let leftIndex = 0;
       let rightIndex = removable.length;
       while (leftIndex < rightIndex) {</pre>
           // Midpoint calculation to use as the possible number of characters to be removed
           let midPoint = Math.floor((leftIndex + rightIndex + 1) / 2);
9
10
           // Check if 'p' is still a subsequence after removing 'midPoint' characters
11
           if (isSubsequence(s, p, new Set(removable.slice(0, midPoint)))) {
               leftIndex = midPoint;
13
14
           } else {
```

40 Time and Space Complexity

indexStr++;

return leftIndex;

let indexStr = 0;

let indexSub = 0;

let strLength = str.length;

let subLength = sub.length;

indexSub++;

return indexSub === subLength;

rightIndex = midPoint - 1;

// The maximum number of characters that can be removed

while (indexStr < strLength && indexSub < subLength) {</pre>

// Function to check if 'sub' is a subsequence of 'str' when indices in 'removedIndices' are removed.

// If the current index is not removed, and characters match, increment 'sub' index

if (!removedIndices.has(indexStr) && str.charAt(indexStr) === sub.charAt(indexSub)) {

function isSubsequence(str: string, sub: string, removedIndices: Set<number>): boolean {

// Iterate over each character of 'str' and 'sub' to check for subsequence

// Check if the end of 'sub' was reached, indicating it is a subsequence

The time complexity of the function mainly comes from two parts: the binary search and repeatedly checking whether p is a

Time Complexity:

subsequence of s after certain characters have been removed. The binary search is done over the length of removable, which has a complexity of O(log k) where k is the length of removable. For

considered in the check function. Although k changes with each binary search iteration, we need to consider the worst-case

each iteration of binary search, the check function is called, which iterates over the characters of s and p. The check function can take 0(m + k) time in the worst case, where m is the length of s and k is the length of the prefix of removable

scenario where the function checks the entire prefix, hence k. Combining these two parts, the overall time complexity is O((m + k) * log k).

Space Complexity: The space complexity is primarily due to the set ids used in the check function, which stores the indices that are removable up to k.

This set can grow up to size k. Thus, the space complexity is O(k).