3047. Find the Largest Area of Square Inside Two Rectangles

Problem Description

Geometry

Array

Math

x and y coordinates of their bottom left and the top right corners to do so.

Medium

two separate 2D arrays: bottomLeft and topRight. Our task is to identify the largest area of a square that can fit within an intersection of any two of these rectangles.

If no rectangles intersect, then the area of the largest square that can be fitted is zero by definition. Otherwise, we are to find and

In this problem, we are given n rectangles on a 2D plane. Each rectangle's bottom-left and top-right coordinates are provided via

return the largest possible square area that can be inscribed within such an intersection.

Intuition

To find the solution, we apply an enumeration method. What this means is we will be checking all possible pairs of rectangles to

find intersections. For each pair of rectangles, we determine the coordinates of their overlapping area. Specifically, we look at the

Rectangles intersect if and only if one rectangle's bottom left is less than the other's top right for both the x and y axes. If they do intersect, the dimensions of the intersection can be calculated using max and min functions. The intersection's bottom-left x

coordinate is the larger of the two rectangles' bottom-left x coordinates, and similarly, the bottom-left y coordinate is the larger of the two rectangles' bottom-left y coordinates. The top-right x coordinate is the smaller of the top-right x coordinates, and the top-right y coordinate is the smaller of the y coordinates.

Once we have the dimensions of the intersecting area, we need to sheek if they can form a square. A square is constrained by its

Once we have the dimensions of the intersecting area, we need to check if they can form a square. A square is constrained by its smallest dimension, so we take the smaller of the intersection's width or height as the potential size of the square. Then we calculate the area of the square (side length squared) and keep track of the largest area found during our enumeration. If a square can be placed within the intersection region, we update our answer with the area of that square if it's larger than the previously recorded answer.

Solution Approach

The solution approach involves iterating through all possible pairs of rectangles and calculating their possible intersection. This is a brute-force approach powered by the combinatorial power of the combinations function from the Python standard library's itertools module. This function generates all unique pairs of rectangles so that we can consider their potential intersection.

For width w:

For height h:

e = min(w, h)

Example Walkthrough

`ans = max(ans, e * e)`

bottomLeft = [[1, 2], [3, 5], [6, 7]]

Pair 1: Rectangle 1 and Rectangle 2

Pair 2: Rectangle 1 and Rectangle 3

Pair 3: Rectangle 2 and Rectangle 3

We skip over this pair.

update ans to max(0, 1) which is 1.

Solution Implementation

from typing import List

class Solution:

from itertools import combinations

max_square_area = 0

intersections and possible inscribed squares:

min(4, 6) - max(1, 3), resulting in w = 1.

topRight = [[4, 8], [6, 10], [9, 9]]

h = min(y2, y4) - max(y1, y3)

formulas:

•

 $\hat{w} = \min(x^2, x^4) - \max(x^1, x^3) \hat{w}$ The min function is used to find the least top-right x-coordinate between the two rectangles, and the max function finds the

greatest bottom-left x-coordinate. The difference gives the horizontal span of the intersection.

square's sides must be equal, and the intersection's smallest dimension limits the side's length.

bottom-left y-coordinate. The difference gives the vertical span of the intersection.

After finding the intersection dimensions, the following steps are carried out:

Once we have a pair of rectangles, the implementation computes the width w and height h of their intersection using the following

If either w or h is negative, it means that there is no positive area of intersection between the two rectangles, and we skip over that pair.

We then find the side length of the largest possible inscribed square by taking the minimum of w and h. This is because a

Similarly, the min function is used to determine the least top-right y-coordinate, and the max function locates the greatest

We ensure that the side length is positive (e > 0). If it is, we have a valid square, and we compute its area (e * e).
 The solution keeps updating the variable ans with the maximum area found so far. This is done using another max function:

- At the end of the iteration through all rectangle pairs, the value of ans represents the largest square area that can be inscribed in any intersection of two input rectangles, which is what the function returns.
- Using the solution approach outlined above, let's walk through the steps to find the largest square that can fit in an intersection of any two of these rectangles.

 1. Generate all unique pairs of rectangles from our n = 3 rectangles. We will have the following three pairs to check for

For each of these pairs, we calculate the width and height of their potential intersection. Let's enumerate through them:

■ The width w of the overlapping area is calculated as min(x2[0], x4[0]) - max(x1[0], x3[0]), which for their given coordinates is

Let's say we are given the following pairs of bottom-left (bottomLeft) and top-right (topRight) coordinates for n = 3 rectangles:

```
    For Pair 1 (Rectangles 1 & 2):
```

1.

Python

The possible square side length e = min(w, h) = 1, so the area of the square is e * e = 1.
 For Pair 2 (Rectangles 1 & 3 - no intersection as they are far apart):

■ Similarly, for width w, we get w = min(4, 9) - max(1, 6) which results in a negative value, indicating no positive area of intersection.

For Pair 3 (Rectangles 2 & 3):
 ■ The width w is min(x2[0], x4[0]) - max(x1[0], x3[0]) giving us w = min(6, 9) - max(3, 6), which results in w = 0 (edges touching, but no area of intersection).

• Calculating height h similarly would not matter as we already have w = 0. We skip over this pair.

def largestSquareArea(self, bottom_left: List[List[int]], top_right: List[List[int]]) -> int:

for ((x1, y1), (x2, y2)), ((x3, y3), (x4, y4)) in combinations(zip(bottom_left, top_right), 2):

Calculate the largest square area from overlapping rectangles.

Initialize the variable to store the maximum square area found.

The edge of the largest square inside the overlapping area

If there is an overlapping area, calculate its square area.

Generate all pairs of rectangles to check for overlapping.

Calculate the width of the overlapping area.

Calculate the height of the overlapping area.

width = min(x2, x4) - max(x1, x3)

height = min(y2, y4) - max(y1, y3)

edge = min(width, height)

is the minimum of width and height.

■ The height h is min(y2[1], y4[1]) - max(y1[1], y3[1]), which gives us h = min(8, 10) - max(2, 5), so h = 3.

5. At the end of the iteration, we return the largest square area found which is 1. This is the largest square that can fit within an intersection of any of the given rectangles.

As we iterate over these pairs, we keep track of the maximum square area ans. Initially, ans = 0. After checking Pair 1, we

Since Pair 2 and Pair 3 do not contribute any area (no valid intersections for a square), the ans does not change and remains

param bottom_left: List of [x, y] coordinates for the bottom left corner of rectangles. param top_right: List of [x, y] coordinates for the top right corner of rectangles. return: Area of the largest square that can be formed within the overlapping area of rectangles.

```
max_square_area = max(max_square_area, edge * edge)

# Return the largest square area found.
return max_square_area
```

class Solution {

// Loop through each rectangle

for (int i = 0; i < bottomLeft.size(); ++i) {</pre>

int x1 = bottomLeft[i][0], y1 = bottomLeft[i][1];

for (int j = i + 1; j < bottomLeft.size(); ++j) {</pre>

int x2 = topRight[i][0], y2 = topRight[i][1];

let maximumArea = 0; // Initialize the maximum area to 0

// Continue iterating to find the overlapping areas

// Calculate the overlap width and height

for (let j = i + 1; j < bottomLeftCorners.length; ++j) {</pre>

const width = Math.min(x2, x4) - Math.max(x1, x3);

const height = Math.min(y2, y4) - Math.max(y1, y3);

Initialize the variable to store the maximum square area found.

The edge of the largest square inside the overlapping area

If there is an overlapping area, calculate its square area.

max_square_area = max(max_square_area, edge * edge)

Generate all pairs of rectangles to check for overlapping.

Calculate the width of the overlapping area.

Calculate the height of the overlapping area.

width = min(x2, x4) - max(x1, x3)

height = min(y2, y4) - max(y1, y3)

Return the largest square area found.

edge = min(width, height)

is the minimum of width and height.

max_square_area = 0

if edge > 0:

return max_square_area

// Edge of the largest possible square within the overlap

for (let i = 0; i < bottomLeftCorners.length; ++i) {</pre>

public:

};

TypeScript

if edge > 0:

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Java
class Solution {
    public long largestSquareArea(int[][] bottomLeftCorners, int[][] topRightCorners) {
        long maxSquareArea = 0; // Initialize the maximum square area to 0
       // Iterate through each rectangle
        for (int i = 0; i < bottomLeftCorners.length; ++i) {</pre>
           // Get the bottom left and top right coordinates of the first rectangle
            int x1 = bottomLeftCorners[i][0], y1 = bottomLeftCorners[i][1];
            int x2 = topRightCorners[i][0], y2 = topRightCorners[i][1];
           // Compare the first rectangle with every other rectangle
            for (int j = i + 1; j < bottomLeftCorners.length; ++j) {</pre>
                // Get the bottom left and top right coordinates of the second rectangle
                int x3 = bottomLeftCorners[j][0], y3 = bottomLeftCorners[j][1];
                int x4 = topRightCorners[j][0], y4 = topRightCorners[j][1];
                // Calculate the width and height of the overlapping rectangle
                int overlapWidth = Math.min(x2, x4) - Math.max(x1, x3);
                int overlapHeight = Math.min(y2, y4) - Math.max(y1, y3);
                // Find the maximum square edge for the overlapping area
                int maxSquareEdge = Math.min(overlapWidth, overlapHeight);
                // If an overlap exists (positive edge length), calculate the possible square area
                if (maxSquareEdge > 0) {
                   // Update the maximum square area if the current square area is greater
                    maxSquareArea = Math.max(maxSquareArea, 1L * maxSquareEdge * maxSquareEdge);
       // Return the maximum square area found
        return maxSquareArea;
C++
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// Get the coordinates of the bottom left and top right corners of the second rectangle
int x3 = bottomLeft[j][0], y3 = bottomLeft[j][1];
int x4 = topRight[j][0], y4 = topRight[j][1];

// Calculate width and height of the overlapping area between two rectangles
int overlapWidth = min(x2, x4) - max(x1, x3);
int overlapHeight = min(y2, y4) - max(y1, y3);

// The edge length of the largest square is limited by the smaller of the two dimensions
int squareEdge = min(overlapWidth, overlapHeight);

// If there's a valid overlapping area, calculate its square area
if (squareEdge > 0) {
    maxSquareArea = max(maxSquareArea, static_cast<long long>(squareEdge) * squareEdge);
}

// Return the largest square area found
return maxSquareArea;
}
```

function largestSquareArea(bottomLeftCorners: number[][], topRightCorners: number[][]): number {

// Iterate through each rectangle by using bottom—left and top—right corners

const [x1, y1] = bottomLeftCorners[i]; // Bottom left corner (x1, y1)

const [x2, y2] = topRightCorners[i]; // Top right corner (x2, y2)

// Function to calculate the largest square area formed by overlapping rectangles

long long maxSquareArea = 0; // Initialize the maximum square area to 0

// Now compare the first rectangle with every other rectangle

long long largestSquareArea(vector<vector<int>>& bottomLeft, vector<vector<int>>& topRight) {

// Get the coordinates of the bottom left and top right corners of the first rectangle

for ((x1, y1), (x2, y2)), ((x3, y3), (x4, y4)) in combinations(zip(bottom_left, top_right), 2):

const [x3, y3] = bottomLeftCorners[j]; // Compare with next bottom left corner (x3, y3)

const [x4, y4] = topRightCorners[j]; // Compare with next top right corner (x4, y4)

```
Time and Space Complexity

The time complexity of the given code is 0(n^2), where n is the number of rectangles. This is due to the use of the combinations function with 2 as the second argument, which generates all pairs of rectangles to determine the area of the potential square.
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Since for n elements there are n*(n-1)/2 combinations, this operation is bound by a quadratic function of n.

The space complexity of the code is 0(1). This refers to the constant extra space used by the variables within the function. The algorithm's space requirements do not grow with the input size; ans, w, h, and e variables use a fixed amount of space regardless of the number of rectangles.