1177. Can Make Palindrome from Substring

Hash Table

String

<u>Array</u>

## **Problem Description**

Bit Manipulation

Medium

replacing up to k letters to form a palindrome. This needs to be done for a series of queries, each represented by a triplet [left, right, k]. Specifically, for each query, we are allowed to: 1. Rearrange the substring s[left...right]. 2. Replace up to k letters in the substring with any other lowercase English letter.

The problem requires us to determine whether a substring of a given string s can be rearranged and possibly modified by

**Prefix Sum** 

- If the substring can be made into a palindrome using the above operations, the result for that query is true; otherwise, it is false. We are to return an array of boolean values representing the result for each query.
- Intuition

matching pair except for at most one character, which can be in the middle of the palindrome if the string length is odd.

A palindrome is a string that reads the same forward and backward. For a string to be a palindrome, each character must have a

The intuition behind the solution approach is to first understand the characteristics of a palindrome. For a string to be a

palindrome, each character except for at most one must occur an even number of times (they can be mirrored around the center

## of the string).

Given this, we can reformulate the problem as: At most how many characters in the target substring have an odd number of occurrences, and whether this number can be reduced to at most one with at most k character replacements. To efficiently compute the number of characters with odd occurrences in any given substring, the solution employs prefix sums.

Specifically, it calculates the count of each character of the alphabet up to each position in the string. This provides a quick way

Here's the step-by-step approach of the solution: 1. Create a list ss to keep track of the prefix sums – the count of each character up to each index of the string.

2. Iterate over the string s to fill up the ss list with the counts. 3. For each query, use the ss list to calculate the number of characters with an odd count in the target substring. 4. Check if the half of the number of odd-count characters is less than or equal to k, since each pair of odd-count characters can be replaced by any other character to make them even.

- This approach allows us to efficiently answer each query without having to directly manipulate the substring, reducing the
- problem to a question of counting occurrences which can be solved in constant time for each query. **Solution Approach**
- The solution uses the concept of prefix sums and bitwise operations to solve the problem efficiently. Here's how it works, with
- is 1, and so on) up to the i-th position in the string s. This list is initialized with n + 1 rows and 26 columns (since there are

 $ss = [[0] * 26 for _ in range(n + 1)]$ 

ans.append(cnt // 2 <= k)</pre>

return ans

**Example Walkthrough** 

[0, 0, 0],

[0, 0, 0],

[0, 0, 0],

[2, 2, 0], // before 'c'

[2, 2, 1], // before 'c'

k=1 characters, the result for this query is true.

# Calculate the length of the string.

# Process each query in the list of queries.

for start, end, max replacements in queries:

answers.append(can\_form\_palindrome)

[2, 2, 2]] // after 'c'

This check is appended to our result list ans.

number of queries, making it highly efficient for the problem at hand.

[0, 0, 0]] // after the last character ('c')

Let's consider the string s = "aabbcc" and queries queries = [[0,5,2], [1,4,1]].

reference to the key steps in the Python code implementation:

5. For each query, append the result (true or false) to the answer list ans.

to determine the counts of each letter in any substring.

6. Return the ans list as output once all queries are processed.

26 letters in the English alphabet) filled initially with zeros. This extra row is for handling the prefix sum from the beginning of the string.

Initialization: A two-dimensional list ss is initiated where ss[i][j] represents the count of the j-th letter (where a is 0, b

Populating Prefix Sums: As we iterate through the string s, a temporary copy of the previous row of the ss list is made, and

**Processing Queries:** For each query [1, r, k], we calculate the number of characters with an odd number of occurrences

within the substring s[l...r]. This is done by using the corresponding prefix sums to find the total count of each letter in the

The above line calculates the difference between the counts at the position after the end of the substring (r + 1) and at the

start of the substring (1). This difference gives us the count of each character in the substring. We then check if this count is

for i, c in enumerate(s, 1): ss[i] = ss[i - 1][:]ss[i][ord(c) - ord("a")] += 1

then the count of the current character is updated by incrementing the corresponding counter.

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substring and then applying a bitwise AND operation with 1 (which is equivalent to checking if the count is odd).
cnt = sum((ss[r + 1][j] - ss[l][j]) & 1 for j in range(26))
```

odd by using the bitwise AND operation with 1. Checking for Palindrome Potential: The number of odd-count characters that need to be paired off (which requires replacement) is cnt // 2. We check if this number is less than or equal to k, which signifies whether we can turn the substring into a palindrome through k or fewer character replacements.

```
The use of prefix sums allows for a quick calculation of character occurrences within any given substring in 0(1) time, after an
O(n) preprocessing phase. The overall complexity of the solution is O(n + q), where n is the length of the string and q is the
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**Returning Results**: Once all queries are processed, the list ans containing the result of each query is returned.

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0. The initialized ss list looks like this initially (considering a simplified alphabet of three letters for this illustration):
ss = [[0, 0, 0], // before the first character ('a')
      [0, 0, 0], // before the second character ('a') and so on
      [0, 0, 0],
```

Initialization with Prefix Sums: We first initialize our ss list with extra space to handle cases when the substring starts at index

Populating Prefix Sums: After populating the ss list with the prefix sums of each character, the list reflects the following (the th index in the inner lists corresponds to the alphabetically j-th character): ss = [[0, 0, 0], // before 'a'][1, 0, 0], // before 'a' [2, 0, 0], // before 'b' [2, 1, 0], // before 'b'

Query 1: [0, 5, 2] We need to check the substring s[0...5] which is "aabbcc". For this substring, the counts of each character

are 2 a's, 2 b's, and 2 c's. The count of odd-occurring characters cnt is therefore 0. We don't need any replacements to make

Query 2: [1, 4, 1] This time, we're looking at the substring s[1...4] which is "abbc". Here, the count of each character is 1 a,

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a palindrome, so the result for this query is true.
```

Solution Implementation

string\_length = len(s)

answers = []

return answers

// Process each query

return results;

int n = s.size();

// Process each query

class Solution:

for (const [left, right, maxReplacements] of queries) {

result.push((oddCount >> 1) <= maxReplacements);

return result; // Return the array of boolean results for each query

def canMakePaliQueries(self, s: str, queries: List[List[int]]) -> List[bool]:

for (let j = 0; j < 26; ++j) {

# Calculate the length of the string.

let oddCount = 0; // Count of characters that appear an odd number of times

oddCount += (charCountPrefixSum[right + 1][j] - charCountPrefixSum[left][j]) & 1;

// Push true if half of the odd count is less than or equal to k, otherwise false.

// Calculate the number of characters with an odd count in the substring

C++

public:

#include <vector>

#include <cstring>

class Solution {

using namespace std;

for (int[] query : queries) {

// substring [left, right]

for (int j = 0; j < 26; ++j) {

results.add(oddCount / 2 <= maxReplacements);

// Return the list containing results of queries

int oddCount = 0;

Java

class Solution {

**Python** 

class Solution:

2 bs, and 1 c. Therefore, we have cnt=2 characters occurring an odd number of times ("a" and "c"). We need 1 replacement to make either "a" or "c" match the other character (e.g., change "c" to "a" to form "abba"). Since we are allowed to replace up to

Answer: Thus, the array of boolean values representing the result for each query is [true, true].

# Calculate the count of odd occurrences of each letter in the range [start, end].

odd\_count = sum((prefix\_sum[end + 1][j] - prefix\_sum[start][j]) & 1 for j in range(26))

def canMakePaliQueries(self, s: str, queries: List[List[int]]) -> List[bool]:

can\_form\_palindrome = odd\_count // 2 <= max\_replacements</pre>

# Return the answers list containing results for all queries.

# Add the result for the current query to the answers list.

int left = query[0], right = query[1], maxReplacements = query[2];

oddCount += (charCountPrefixSum[right + 1][j] - charCountPrefixSum[left][j]) & 1;

// Add true if half of the oddCount is less than or equal to allowed replacements (maxReplacements)

// Compute the count of characters with odd occurrences in the

vector<bool> canMakePaliQueries(string s, vector<vector<int>>& queries) {

# Initialize a prefix sum array where each element is a list representing the count of letters up to that index. prefix\_sum = [[0] \* 26 for \_ in range(string\_length + 1)] # Populate the prefix sum matrix with the counts of each character. for index. char in enumerate(s. 1): prefix sum[index] = prefix sum[index - 1][:] prefix\_sum[index][ord(char) - ord("a")] += 1 # Initialize a list to store the answers for the queries.

# A palindrome can be formed if the half of odd count is less than or equal to the allowed max\_replacements.

```
public List<Boolean> canMakePaliQueries(String s, int[][] queries) {
    int stringLength = s.length();
    // Prefix sum array to keep count of characters up to the ith position
    int[][] charCountPrefixSum = new int[stringLength + 1][26];
    // Fill the prefix sum array with character counts
    for (int i = 1; i <= stringLength; ++i) {</pre>
        // Copy the counts from previous index
        for (int i = 0; i < 26; ++i) {
            charCountPrefixSum[i][j] = charCountPrefixSum[i - 1][j];
        // Increment the count of the current character
        charCountPrefixSum[i][s.charAt(i - 1) - 'a']++;
    // List to store results of queries
    List<Boolean> results = new ArrayList<>();
```

```
// Create a 2D array to keep track of character frequency up to each position in the string
        int charCountPrefixSum[n + 1][26];
        memset(charCountPrefixSum, 0, sizeof(charCountPrefixSum)); // Initialize the array with 0
        // Populate the prefix sum array with character frequency counts
        for (int i = 1; i \le n; ++i) {
            for (int i = 0; i < 26; ++i) {
                charCountPrefixSum[i][j] = charCountPrefixSum[i - 1][j];
            charCountPrefixSum[i][s[i - 1] - 'a']++;
        vector<bool> answers; // This will store the answers for each query
        // Go through each query to check for palindrome possibility
        for (auto& query : queries) {
            int left = query[0], right = query[1], maxReplacements = query[2];
            int oddCount = 0; // Variable to track the count of characters appearing odd number of times
            // Count how many characters appear an odd number of times within the query's range
            for (int i = 0; i < 26; ++i) {
                oddCount += (charCountPrefixSum[right + 1][j] - charCountPrefixSum[left][j]) & 1;
            // A palindrome can be formed if the half of the odd count is less than or equal to allowed replacements
            answers.emplace_back(oddCount / 2 <= maxReplacements);</pre>
        return answers; // Return the final answers for all queries
TypeScript
function canMakePaliQueries(s: string, queries: number[][]): boolean[] {
    const lengthOfString = s.length;
    const charCountPrefixSum: number[][] = Array(lengthOfString + 1)
        .fill(0)
        .map(() => Array(26).fill(0)); // Array to store the prefix sum of character counts
    // Calculate the prefix sum of character counts
    for (let i = 1; i <= length0fString; ++i) {</pre>
        charCountPrefixSum[i] = charCountPrefixSum[i - 1].slice(); // Copy previous count
        ++charCountPrefixSum[i][s.charCodeAt(i - 1) - 'a'.charCodeAt(0)]; // Increment count of current character
    const result: boolean[] = [];
```

```
string length = len(s)
       # Initialize a prefix sum array where each element is a list representing the count of letters up to that index.
        prefix_sum = [[0] * 26 for _ in range(string_length + 1)]
       # Populate the prefix sum matrix with the counts of each character.
        for index, char in enumerate(s, 1):
           prefix sum[index] = prefix sum[index - 1][:]
           prefix_sum[index][ord(char) - ord("a")] += 1
       # Initialize a list to store the answers for the queries.
       answers = []
       # Process each query in the list of queries.
        for start, end, max replacements in queries:
           # Calculate the count of odd occurrences of each letter in the range [start, end].
           odd_count = sum((prefix_sum[end + 1][j] - prefix_sum[start][j]) & 1 for j in range(26))
           # A palindrome can be formed if the half of odd count is less than or equal to the allowed max_replacements.
           can_form_palindrome = odd_count // 2 <= max_replacements</pre>
           # Add the result for the current query to the answers list.
           answers.append(can_form_palindrome)
       # Return the answers list containing results for all queries.
        return answers
Time and Space Complexity
  The given Python code provides a solution for determining if a substring of the input string s can be rearranged to form a
  palindrome with at most k replacements. The computation of this solution involves pre-computing the frequency of each
```

## character in the alphabet at each index of the string s, and then using that information to answer each query. **Time Complexity:**

1. Building the prefix sum array ss takes 0(n \* 26) time, where n is the length of the string s, since we iterate over the string and for each character, we copy the previous counts and update the count of one character. 2. Answering each query involves calculating the difference in character counts between the right and left indices for each of the 26 letters, which

3. The total time complexity is therefore 0(n \* 26 + q \* 26) which simplifies to 0(n + q) when multiplied by the constant 26 factor for the

is 0(26). This is done for each query. If there are q queries, this part of the algorithm takes 0(q \* 26) time.

1. The prefix sum array ss uses 0(n \* 26) space to store the count of characters up to each index in the string s.

- alphabet size. Hence, the time complexity is 0(n + q).
- **Space Complexity:**
- 2. The space for the answer list is O(q), where q is the number of queries. 3. As such, the total space complexity is the sum of the space for the prefix sum array and the space for the answer list, which is 0(n \* 26 + q). Thus, the space complexity is 0(n \* 26 + q) which can be approximated to 0(n) since the size of the alphabet is constant.