54. Spiral Matrix Matrix Simulation Medium Array

Problem Description

In this problem, we are tasked with traversing a 2D array (or matrix) in a spiral pattern. Imagine starting at the top-left corner of the matrix and going right, then down, then left, and then up, turning inward in a spiral shape, until we traverse every element in the matrix exactly once. The function should return a list of the elements of the matrix in the order they were visited during this spiral traversal.

Intuition To solve this problem, we need to simulate the process of traveling around the matrix spiral. Essentially, we keep moving in the same direction (right initially) until we meet a boundary of the matrix or a previously visited cell. When we encounter such a boundary, we

1. Simulation Approach: We initiate four direction vectors (or in our case, a direction array dirs) that represent right, down, left,

There are two insightful approaches to this problem:

make a clockwise turn and continue the process.

- and up. We iterate over all elements in the matrix by taking steps in the initial direction until we can no longer move forward. At this point, we turn 90 degrees and continue. To avoid revisiting cells, we mark each visited cell by adding it to a set vis so that we know when to turn. The time complexity here is $0(m \times n)$ because we visit each element once, and the space complexity is also $0(m \times n)$ due to the extra space used to store visited cells. 2. Layer-by-layer Simulation: Instead of marking visited cells, we can visualize the matrix as a series of concentric rectangular
- layers. We traverse these layers from the outermost to the innermost, peeling them away as we go. This approach requires careful handling of the indices to ensure we stay within the bounds of the current layer. This way of traversal helps to potentially reduce extra space usage because we don't explicitly need to keep track of visited cells.

1. Initialization:

Solution Approach

The given Python solution follows the Simulation Approach described in the intuition section.

We define m and n which are the dimensions of the matrix (number of rows and number of columns respectively). ○ The dirs array dirs = (0, 1, 0, -1, 0) encodes the direction vectors. dirs[k] and dirs[k+1] together represent the

- direction we move in, with k starting at 0 and cycling through values 0 to 3 to represent right, down, left, and up in that order.
- The i and j variables represent the current row and column positions in the matrix. o and list is where we collect the elements of the matrix as we visit them. 2. Visiting Elements:
 - We loop exactly m * n times, once for each element of the matrix. • Each time through the loop, we append the current element to the ans list and mark its position (i, j) as visited by adding

3. Moving Through the Matrix:

is the if not $0 \ll x \ll m$ or not $0 \ll y \ll n$ or (x, y) in vis: check.

- We calculate the next position (x, y) based on the current direction we are moving. This is done using the current values of i, j, and k. Before we move to the next position, we check if the position is valid - it must be within bounds and not already visited. This
- ∘ If the move is invalid, we change the direction by increasing k modulo 4. This works because if k is 3 and we add 1, (k + 1) % 4 will reset k back to 0.

4. Handling Edge Cases:

5. Completing the Spiral:

it to the vis set.

• Because we update the direction whenever we hit the edge of the matrix or a visited cell, the algorithm naturally handles non-square matrices and any edge cases where the spiral must turn inward.

• The process continues, circling around the matrix and moving inward until all elements have been added to ans.

• In the reference solution, it's suggested that instead of using a vis set to keep track of visited cells (contributing to space

cause integer overflow.

6. Space Optimization:

complexity of $0(m \times n)$, we could modify the matrix itself to mark cells as visited. This could be done by adding a constant value which is outside the range of the matrix values, effectively using the input matrix as the vis state. This reduces the

• Once the direction is confirmed as valid, we update i and j to move to the next position in the matrix.

The executed code follows this approach rigorously, and through simulation, delivers the correct spiral traversal of the input matrix. The attention to directional changes and boundary conditions ensures that all cases are handled smoothly. Example Walkthrough

space complexity to 0(1), provided the matrix can be modified and that the added constant is chosen such that it doesn't

1 matrix = [[1, 2, 3], [4, 5, 6],

Now we'll walk through the solution step by step:

 \circ m = 3 (3 rows), n = 3 (3 columns)

Let's illustrate the solution approach using a small example where our input is a 2D matrix:

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○ Direction array dirs = (0, 1, 0, -1, 0) indicates the x and y offsets for right, down, left, and up movements respectively.
\circ We start at the top-left corner, so initial indices i = 0 and j = 0.
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1. Initialization:

o vis = set() to store visited positions. 2. Visiting Elements:

• ans = [] will collect the elements in spiral order.

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We begin by appending matrix[0][0] to ans, so ans = [1].
```

- 1. • This position is within bounds and not visited, so we move there and append matrix[0][1] to ans, making it [1, 2].
- We repeat this process and append [3, 6, 9] to ans. 4. Direction Change and Boundary Check:

We add (0, 0) to vis to mark it as visited.

After reaching the last column, we check the next right move and find it's out of bounds. \circ We then change direction to down (k = 1), and append [8, 7] to ans.

5. Avoiding Visited Cells:

6. Completing the Spiral:

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3. Moving Through the Matrix:

 Next, we attempt to move left but the cell (2, 0) is visited. We turn again, moving up and find the top center cell (0, 1) is also visited. • We turn right and add [4, 5] to the spiral traversal.

 \circ We calculate the next position using the current direction (right, k = 0), so x = i + dirs[k] = 0 and y = j + dirs[k+1] = 0

 We've now visited all cells, and ans is [1, 2, 3, 6, 9, 8, 7, 4, 5]. 7. Space Optimization (Optional):

This function takes a matrix and returns a list of elements in spiral order.

Define directions for spiral movement (right, down, left, up).

Initialize the answer list and a set to keep track of visited cells.

Calculate the next cell's position based on the current direction.

Change direction if out of bounds or cell is already visited.

Check if the next cell is within bounds and not visited.

direction_index = (direction_index + 1) % 4

 A potentially more space-efficient approach might entail modifying the given matrix to mark visited elements if allowed. By following the simulation approach, the function would return the traversal in spiral order as [1, 2, 3, 6, 9, 8, 7, 4, 5].

Define matrix dimensions.

result = []

visited = set()

rows, cols = len(matrix), len(matrix[0])

Mark the current cell as visited.

visited.add((row, col))

- **Python Solution** class Solution: def spiralOrder(self, matrix):
- directions = ((0, 1), (1, 0), (0, -1), (-1, 0))11 12 13 # Initialize row and column indices and the direction index. row = col = direction_index = 0 14 15

19 20 # Iterate over the cells of the matrix. for _ in range(rows * cols): 21 22 # Append the current element to the result list. 23 result.append(matrix[row][col])

next_row, next_col = row + directions[direction_index][0], col + directions[direction_index][1]

if not (0 <= next_row < rows) or not (0 <= next_col < cols) or (next_row, next_col) in visited:</pre>

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               # Update the row and column indices to the next cell's position.
36
                row += directions[direction_index][0]
37
                col += directions[direction_index][1]
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39
           # Return the result list.
40
           return result
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Java Solution
  1 import java.util.List;
  2 import java.util.ArrayList;
     class Solution {
         public List<Integer> spiralOrder(int[][] matrix) {
             // Dimensions of the 2D matrix
             int rowCount = matrix.length;
             int colCount = matrix[0].length;
             // Direction vectors for right, down, left, and up
  9
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             int[] directionRow = \{0, 1, 0, -1\};
             int[] directionCol = \{1, 0, -1, 0\};
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 12
             // Starting point
 13
             int row = 0, col = 0;
 14
             // Index for the direction vectors
 15
             int directionIndex = 0;
 16
             // List to hold the spiral order
 17
             List<Integer> result = new ArrayList<>();
 18
             // 2D array to keep track of visited cells
             boolean[][] visited = new boolean[rowCount][colCount];
 19
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 21
             for (int h = rowCount * colCount; h > 0; --h) {
 22
                 // Add the current element to the result
 23
                 result.add(matrix[row][col]);
 24
                 // Mark the current cell as visited
 25
                 visited[row][col] = true;
 26
                 // Compute the next cell position
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int nextRow = row + directionRow[directionIndex];

int nextCol = col + directionCol[directionIndex];

directionIndex = (directionIndex + 1) % 4;

// Move to the next cell

row = nextRow;

col = nextCol;

return result;

// Check if the next cell is out of bounds or visited

nextRow = row + directionRow[directionIndex];

nextCol = col + directionCol[directionIndex];

// Recompute the next cell using the new direction

// Update the direction index to turn right in the spiral order

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C++ Solution
  1 class Solution {
  2 public:
         vector<int> spiralOrder(vector<vector<int>>& matrix) {
             if (matrix.empty()) return {}; // Return an empty vector if the matrix is empty
             int rows = matrix.size(), cols = matrix[0].size(); // rows and cols store the dimensions of the matrix
  6
             vector<int> directions = {0, 1, 0, -1, 0}; // Row and column increments for right, down, left, up movements
             vector<int> result; // This vector will store the elements of matrix in spiral order
  8
             vector<vector<bool>> visited(rows, vector<bool>(cols, false)); // Keep track of visited cells
  9
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 11
             int row = 0, col = 0, dirIndex = 0; // Start from the top-left corner and use dirIndex to index into directions
 12
 13
             for (int remain = rows * cols; remain > 0; --remain) {
                 result.push_back(matrix[row][col]); // Add the current element to result
 14
 15
                 visited[row][col] = true; // Mark the current cell as visited
 16
                 // Calculate the next cell position
                 int nextRow = row + directions[dirIndex], nextCol = col + directions[dirIndex + 1];
 18
 19
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                 // Change direction if next cell is out of bounds or already visited
 21
                 if (nextRow < 0 || nextRow >= rows || nextCol < 0 || nextCol >= cols || visited[nextRow][nextCol]) {
 22
                     dirIndex = (dirIndex + 1) % 4; // Rotate to the next direction
 23
 24
 25
                 // Move to the next cell
 26
                 row += directions[dirIndex];
 27
                 col += directions[dirIndex + 1];
 28
 29
             return result; // Return the result
 30
 31 };
 32
```

if (nextRow < 0 || nextRow >= rowCount || nextCol < 0 || nextCol >= colCount || visited[nextRow][nextCol]) {

8 9 10 let row = 0;

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Typescript Solution

1 function spiralOrder(matrix: number[][]): number[] {

const rowCount = matrix.length; // Number of rows in the matrix

const colCount = matrix[0].length; // Number of columns in the matrix

const result: number[] = []; // The array that will be populated and returned

```
const directions = [0, 1, 0, -1, 0]; // Direction array to facilitate spiral traversal: right, down, left, up
  6
         let remainingCells = rowCount * colCount; // Total number of cells to visit
        // Starting point coordinates and direction index
        let col = 0;
 11
 12
         let dirIndex = 0;
 13
 14
        // Iterate over each cell, decrementing the count of remaining cells
 15
         for (; remainingCells > 0; --remainingCells) {
 16
             result.push(matrix[row][col]); // Add the current cell's value to the result
 17
             visited[row][col] = true; // Mark the current cell as visited
 18
             // Calculate the indices for the next cell in the current direction
 19
 20
             const nextRow = row + directions[dirIndex];
             const nextCol = col + directions[dirIndex + 1];
 21
 22
 23
            // Check if the next cell is out of bounds or already visited
            if (nextRow < 0 || nextRow >= rowCount || nextCol < 0 || nextCol >= colCount || visited[nextRow][nextCol]) {
 24
                dirIndex = (dirIndex + 1) % 4; // Change direction (right -> down -> left -> up)
 25
 26
 27
 28
            // Move to the next cell in the updated/current direction
 29
             row += directions[dirIndex];
             col += directions[dirIndex + 1];
 30
 31
 32
 33
         return result; // Return the array containing the spiral order traversal of the matrix
 34 }
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Time and Space Complexity
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const visited = new Array(rowCount).fill(0).map(() => new Array(colCount).fill(false)); // A 2D array to keep track of visited

The time complexity of the function spiralOrder is O(m * n) where m is the number of rows and n is the number of columns in the input matrix. This is because the function iterates over every element in the matrix exactly once.

The space complexity of the function, however, is not 0(1) as stated in the reference answer. Instead, it is 0(m * n) because the function uses a set vis to track visited elements, which in the worst-case scenario, can grow to contain every element in the matrix.