967. Numbers With Same Consecutive Differences

Medium Breadth-First Search Backtracking

## **Problem Description**

pair of consecutive digits is 'k'. The key points to consider are: 1. The length of each integer should be exactly 'n' digits long.

The given problem requires us to generate all possible integers of a specified length 'n' where the absolute difference between every

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- 2. Consecutive digits in an integer should have a difference of 'k'.
- 3. The integers should not contain any leading zeros.
- 4. The result can be returned in any order.
- For example, if n = 3 and k = 7, one possible integer could be 181, where the difference between 8 and 1 is 7.

guide for the DFS approach:

Intuition

1. Start with a digit between 1 and 9 (since we cannot have leading zeros), and treat this as the current integer. 2. Perform DFS to add the next digit to the current integer. This digit must be within the range 0-9 and should differ by 'k' from the last digit of the current integer.

To solve this problem, a depth-first search (DFS) algorithm can be leveradged. The intuition behind using DFS is to build each valid

integer digit by digit and to backtrack when a digit that does not satisfy the constraints is reached. Here is a step-by-step intuition

- 3. If 'k' is zero, ensure that you only add the same digit as previously added to prevent duplicates.
- 4. Repeat the process until the length of the current integer is 'n'. 5. Once an integer of length 'n' is built, add it to the result list.
- 6. Continue exploring other possibilities by backtracking and trying other digits for each position.
- The DFS continues until all possible combinations that meet the conditions have been explored and added to the result list. By using DFS, we both build the integers and validate them at each step of the process.

The implementation uses a Depth-First Search (DFS) method defined as dfs, a recursive approach, which is suitable for building combinations and is used to explore each possible number according to the constraints. The dfs function receives three parameters:

### Here's a step-by-step explanation of the solution approach based on the provided code:

n, k, and the current temporary integer t.

added to the answer list, ans.

Exploring Next Digits:

**Solution Approach** 

1. Initializing the Answer List: A list named ans is initialized to store the resulting valid integers. 2. Depth-First Search (DFS): The dfs function is defined with the following logic:

• Base Case: If the remaining length for the integer (n) is zero, the current integer (t) satisfies the length requirement and is

Calculating the Next Digit: The last digit is obtained by performing t % 10.

possibility of adding last + k as the next digit.

of length 2 where the absolute difference between every pair of adjacent digits is 1.

Base Case: For dfs(1, 1, 1), n is not zero, so we do not add t to ans yet.

Calculating the Next Digit: The last digit obtained is 1 (since t % 10 = 1).

- If last + k is less than or equal to 9, a recursive call dfs(n 1, k, t \* 10 + last + k) is made to explore the
- This recursive pattern allows the exploration of all valid combinations of digits where the difference between each consecutive pair is k.

3. Initiating DFS for Each Starting Digit: A loop from 1 to 9 is used to start the process since the numbers cannot have leading

zeros. For each starting digit i, the dfs function is called with n - 1 since one digit is already used, k, and i as the current

■ Similarly, if last - k is greater or equal to zero and k is not zero (to avoid duplicate digits when k is zero), another

recursive call dfs(n-1, k, t\*10 + last - k) is made to explore the possibility of adding last - k as the next digit.

- 4. Returning the Result: After all the DFS calls are completed, return the list ans which contains all the valid integers meeting the specified conditions. Pattern used: **DFS** (Depth-First Search)
- The recursive nature of DFS helps in building numbers digit by digit while maintaining the difference k between consecutive digits, thus satisfying all the constraints of the problem effectively.

To illustrate the solution approach, let's consider a small example where n = 2 and k = 1. We want to generate all possible integers

2. Initiating DFS for Each Starting Digit: We iterate through digits 1 to 9 as the first digit of our potential integer because we cannot

○ Let's choose the starting digit 1. We now call dfs(n - 1, k, t), which translates to dfs(1, 1, 1) since we have used one

1. Initializing the Answer List: We start by initializing an empty list ans which will store our results.

have leading zeros.

Exploring Next Digits:

list ans.

Call dfs(1, 1, 2).

Pattern used: **DFS** (Depth-First Search)

class Solution:

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C++ Solution

class Solution {

public:

results = []

if num\_length == 0:

return

which is dfs(0, 1, 12).

Example Walkthrough

temporary integer t.

Data Structures: List for storing the results (ans).

digit (1) already. 3. Depth-First Search (DFS): Inside the DFS function:

■ Now we also check if we can subtract k from last, but since last - k would be 0 and it's already been considered, we don't proceed with this subtraction. 4. We proceed to the next starting digit 2 and repeat the DFS steps:

■ Since last + k is 2 (which is less than or equal to 9), we make a recursive call: dfs(n - 1, k, t \* 10 + last + k)

■ For dfs(0, 1, 12), n is zero, meaning we've built a valid integer of the correct length, hence we add 12 to our answer

21, 23, 32, 34, 43, ..., 89, 98]. For this example, we have iteratively built each possible 2-digit number that follows the absolute difference constraint of 1 by

6. Returning the Result: After all DFS calls with starting digits 1 to 9 are completed, we return the list ans which now contains [12,

**Python Solution** 1 from typing import List

def numsSameConsecDiff(self, n: int, k: int) -> List[int]:

# Define a depth-first search function for constructing numbers

def depth\_first\_search(num\_length: int, k: int, current\_number: int):

# Base case: when the number length becomes 0, we have a complete number

# Initialize a list to hold the final results

results.append(current\_number)

# Get the last digit of the current number

exploring each digit starting from 1 to 9 and using the DFS method to build out the integers.

22 23 # Start the DFS process from digits 1 to 9 (since the number cannot start with 0) 24 for i in range(1, 10): 25 depth\_first\_search(n - 1, k, i)

- Possible next digits are 1 (2-1) and 3 (2+1). ■ For 1, call dfs(0, 1, 21) and add 21 to ans. For 3, call dfs(0, 1, 23) and add 23 to ans. 5. Continue this process with all starting digits from 1 to 9.
- Data Structures: List (ans) for storing the results.

last\_digit = current\_number % 10 16 # If adding k to the last digit fills the condition (digit stays between 0 to 9) if last\_digit + k <= 9:</pre> 17 depth\_first\_search(num\_length - 1, k, current\_number \* 10 + last\_digit + k) 18 # If subtracting k from the last digit fills the condition and k is not 0 (to prevent duplicates) 19 if last\_digit - k >= 0 and k != 0: 20

31 # print(solution.numsSameConsecDiff(3, 7)) # This will print all the numbers of length 3 with consecutive differences of 7.

depth\_first\_search(num\_length - 1, k, current\_number \* 10 + last\_digit - k)

26 # Return the list of results after DFS completion 27 return results 28

return;

// Get the last digit of the current number

if (lastDigit - diff >= 0 && diff != 0) {

function dfs(n: number, k: number, current: number): void {

return; // Exit the current recursive call.

if (n === 0) { // Base case: if the number has reached its required length,

const lastDigit = current % 10; // Extract the last digit of the current number.

result.push(current); // it is added to the result array.

// If the new digit after adding 'k' is still in the range [0, 9],

// Also, avoid repeating the same number if diff is 0

// Check if we can add 'diff' to the last digit without exceeding 9

// Check if we can subtract 'diff' from the last digit without going below 0

vector<int> result; // Use a more descriptive name for the global answer storage.

int lastDigit = currentNum % 10;

if (lastDigit + diff <= 9) {</pre>

29 # Example usage:

30 # solution = Solution()

Java Solution class Solution { // Main method to find and return all numbers of length n where the difference between // every two consecutive digits is k public int[] numsSameConsecDiff(int n, int k) { List<Integer> results = new ArrayList<>(); 6 // Starting from 1 because numbers cannot have leading zeros for (int i = 1; i < 10; ++i) { depthFirstSearch(n - 1, k, i, results); 9 10 11 // Convert the list to an array 12 int[] answer = new int[results.size()]; 13 for (int i = 0; i < results.size(); ++i) {</pre> answer[i] = results.get(i); 14 15 16 return answer; 17 18 // Helper function for depth-first search 19 20 private void depthFirstSearch(int remainingDigits, int diff, int currentNum, List<Integer> results) { // Base case: if no more digits are needed, add the current number to the result 21 22 if (remainingDigits == 0) { 23 results.add(currentNum);

depthFirstSearch(remainingDigits -1, diff, currentNum \*10 + lastDigit + diff, results);

depthFirstSearch(remainingDigits -1, diff, currentNum \*10 + lastDigit - diff, results);

// Function to find all numbers with unique digits and a difference of 'k' between consecutive digits.

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vector<int> numsSameConsecDiff(int n, int k) {
           // Start from digit 1 to 9, and use these as the starting digits for our numbers.
           for (int start = 1; start <= 9; ++start) {</pre>
               dfs(n - 1, k, start); // Start a DFS for each number of length n with the given 'k'.
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           return result; // Return the global result vector containing all valid numbers.
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       // Helper Depth-First Search function to build numbers according to the given constraints.
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       void dfs(int n, int k, int current) {
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           if (n == 0) { // If the number has reached its target length
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                result.push_back(current); // Add the number to the result list
                return; // Exit the recursion
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           int lastDigit = current % 10; // Get the last digit of the current number
           // Check if adding 'k' to the last digit remains a digit
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           if (lastDigit + k < 10) {
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               dfs(n-1, k, current * 10 + lastDigit + k); // Form the next number in the sequence
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           // Check if subtracting 'k' from the last digit remains a digit and 'k' is non-zero to avoid repeats
26
           if (lastDigit - k >= 0 && k != 0) {
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               dfs(n - 1, k, current * 10 + lastDigit - k); // Form the next number in the sequence
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30 };
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Typescript Solution
 1 let result: number[] = []; // This now uses camelCase naming and TypeScript syntax for type declaration
  // Function to find all numbers with unique digits and a fixed difference 'k' between consecutive digits.
   function numsSameConsecDiff(n: number, k: number): number[] {
       // Start from digit 1 to 9, treating these as the initial digits for potential numbers.
       for (let start = 1; start <= 9; ++start) {</pre>
           dfs(n - 1, k, start); // Initiate a Depth-First Search for each number of length 'n' matching difference 'k'.
       return result; // Return the populated result array containing all valid numbers.
10 }
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   // Helper function for Depth-First Search to construct numbers adhering to the constraints.
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# Time and Space Complexity

if (lastDigit + k < 10) {</pre>

if (lastDigit - k >= 0 && k !== 0) {

#### The given Python code defines a function numsSameConsecDiff that generates numbers of length n having a difference of k between every two consecutive digits. The function uses Depth-First Search (DFS) with pruning. For each starting digit from 1 to 9 (i in the loop), the DFS function is called. Inside dfs, the recursive call reduces the n by 1 until it

**Time Complexity** 

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28 29 } 30 31 // Example of calling the method: // const uniqueNumbers = numsSameConsecDiff(3, 7); 33

dfs(n - 1, k, current \* 10 + lastDigit + k); // Construct and explore this next number in the sequence.

dfs(n-1, k, current \* 10 + lastDigit - k); // Construct and explore this next number in the sequence.

// If the new digit after subtracting 'k' is in the range [0, 9] and 'k' is not zero (to avoid duplicates),

last + k and another for last - k, however, when k is 0, they result in the same digit being added, so only one recursive call is need in that case, effectively pruning the search space. The worst-case time complexity is when k is not 0 and we have to explore both increasing and decreasing options at each step, which gives us 0(2<sup>n</sup>) - this is because, at each step, you have a possibility of two different digits to be appended, effectively

reaches 0, at which point a number is formed and added to the answer list (ans). There are two recursive calls in the function, one for

1. Pruning occurs when last + k > 9 or last - k < 0, in which case the respective recursive call is not made. 2. There's no branching when k = 0, since last + k and last - k result in the same digit.

doubling the possibilities with each additional digit until reaching the desired length n.

However, the actual time complexity might be less than 0(2^n) due to two factors:

- **Space Complexity**
- The space complexity of the code is O(n). This is because of the call stack that is used when the dfs function is recursively called.

space, but it doesn't contribute more than 0(10^n) in space complexity, since we're only generating number sequences of length n starting with a non-zero digit, which in the worst-case gives us all permutations of n-length numbers starting with non-zero digits. However, this is a constant factor when considering space complexity with respect to n.

The depth of the recursive call stack will at most be n, where n is the length of the number we want to create. The list ans also uses

Thus, the overall space complexity is O(n) from the recursive call stack. Meanwhile, the space to hold the generated numbers is dependent on the number of valid combinations found, which is not directly dependent on n, but rather a combination of both n and k.