1716. Calculate Money in Leetcode Bank

Math Easy

Problem Description

- Hercy has a consistent saving plan to buy his first car, where he deposits money into his Leetcode bank account every day following a specific pattern. The pattern works as follows:
- On the first Monday (first day), he deposits \$1.
- From the second day (Tuesday) to the seventh day (Sunday), he increases the amount deposited by \$1 each day. On every Monday after the first, he deposits \$1 more than what he deposited on the previous Monday.
- the total amount of money Hercy will have saved in the Leetcode bank at the end of the nth day.

Given a number n, which represents the number of consecutive days Hercy has been making these deposits, the task is to find

Intuition

• Compute the total money deposited in full weeks. If n is a multiple of 7, this is straightforward; for partial weeks, we only need to account for the days that fall in the final, incomplete week.

The problem can be thought of as finding the sum of an arithmetic series with a twist. The main idea is to break down the

- Remember that each full week starts with Hercy depositing \$1 more than the previous week's Monday. This hints at a pattern similar to the sum of natural numbers, but with an offset due to the amount increasing each week.
- For each full week: ullet Hercy deposits an amount that starts at 1on the first Monday and increases by 1 each subsequent Monday.

• There is a base amount deposited every week: 1(Monday)+2 (Tuesday) + 3(Wednesday)+...+7 (Sunday) = \$28.

partial, week.

problem into smaller parts:

- Each full week has an additional amount on top of the base \$28, determined by the count of weeks that have passed.
- For the partial week (if n is not a multiple of 7), we need to calculate how many days we're into the new week (b) and the total
- amount he has deposited that week, given the extra dollar he adds at the start of each week. Thus, the problem involves finding the sum of amounts deposited in full weeks and the additional amount in the last, possibly

• It uses the divmod function to get both the quotient a (full weeks completed) and the remainder b (additional days in the incomplete week). • The term 28 + 28 + 7 * (a - 1) calculates the base amount for the first and last full week, with the middle term adapting the arithmetic series

• The term a * 2 + b + 1 calculates the amount for the partial week, considering the increase in the starting amount each Monday.

formula to account for the increasing starting amount each Monday.

the provided implementation works, step by step:

The solution code applies this logic using a mathematical formula:

- By neatly summing the contributions of full weeks and the partial week, the code computes the desired total amount.

The solution to this problem involves using simple arithmetic and understanding of how to sum an arithmetic series. Here's how

Solution Approach

First, the use of the divmod function is crucial. This function divides n by 7 to separate the problem into full weeks (a) and the

1 full week), and b would be 3 (because there are 3 days in the second week so far). With these values, the solution calculates how much money was saved in the full weeks. This is where patterns in arithmetic

remaining days of a partial week (b). For instance, if Hercy has been depositing money for 10 days, a would be 1 (representing

- series are used. The base amount without extra increments is known to be 28perfullweek. However, each subsequent week, <math>Hercystartswith1 more than he did the previous Monday. So for a full weeks, the first week has a base of 28, and the last full week would have a base of <math>28 + 7 * (a - 1). The total sum for full weeks follows the natural numbers sum formula:
- Which translates into code as: (28 + 28 + 7 * (a - 1)) * a // 2

+ 1 is the amount Hercy deposits on the last day of this partial week. The sum for these b days is again an arithmetic

For the remaining days of the partial week (b), we need to account for the initial value of the week. By the formula, a * 2 + b

```
sequence starting from a + 1 (since it's a new week, he starts with $1 more than the last Monday) to a + b. This gives us:
Sum for partial week = (initial_deposit + final_deposit) * number_of_days / 2
```

amount of time to compute the answer regardless of the input size n.

no increase for the last full week as there's only one full week in this example.

Sum for full weeks = (base_first_week + base_last_week) * number_of_full_weeks / 2

```
Finally, by adding the sum for full weeks to the sum for the partial week, we get the total amount of money saved by Hercy
after n days. The solution wisely combines these calculations in a single return statement for efficiency and brevity.
```

(a * 2 + b + 1) * b // 2

And in code this is:

Example Walkthrough Let's illustrate the solution approach using a small example: Assume Hercy has been depositing money for 10 days (n = 10).

The provided solution is effective and efficient because it reduces the problem to a series of arithmetic operations without the

need for complex data structures or algorithms. The entire solution runs in constant time (O(1)), which means it requires the same

First, we divide 10 by 7, which gives us a full week (a = 1) and a partial week of 3 days (b = 3). For the full week: The base amount of money saved without additional increments is \$28.

• Since there's only one full week (a = 1), the amount deposited on the first and last Monday of the full weeks would be the same, \$1. So, there's

For the partial week:

Now, calculating the sums:

+ 7 * (1 - 1)) * 1 / 2 = 28.

9 (from the partial week) = \$37.

def totalMoney(self, n: int) -> int:

Solution Implementation

Python

Java

class Solution:

ullet Hercy starts the new week by depositing 2onMonday, asitis1 more than what he deposited on the last Monday of the previous full week. ullet He then deposits 3onTuesdayand4 on Wednesday, following the increasing pattern of \$1 more each day.

For the full week, using the arithmetic series formula, we get: (28 + 28 + 7 * (a - 1)) * a / 2 which translates to (28 + 28

For the partial week, the amount deposited on the last day is \$4. Thus, using the arithmetic series formula again, we have: (a *2 + b + 1) * b / 2 which is (1 * 2 + 3 + 1) * 3 / 2 = (2 + 3 + 1) * 3 / 2 = 9.

The sum of an arithmetic progression for a week is 28 (1+2+...+7),

total_money = total_full_weeks_money + total_remaining_days_money

total_full_weeks_money = (week_start_sum + week_end_sum) * full_weeks // 2

week_end_sum = week_start_sum + $7 * (full_weeks - 1) # Calculate the sum for the last week_end_sum = week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_end_sum = week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_end_sum = week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_end_sum = week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_end_sum = week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_end_sum = week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the last week_start_sum + 7 * (full_weeks - 1) # Calculate the last weeks - 1 * (full_weeks - 1) # Calculate the last weeks - 1 * (full_weeks - 1) # Calculate the last weeks - 1 * (full$

total_remaining_days_money = $(remaining_start_money + remaining_end_money) * remaining_days // 2$

then it increases by 7 for each subsequent week.

week_start_sum = 28 # The sum for the first week

Sum the money from full weeks and remaining days

So, Hercy will have saved a total of \$37 in his Leetcode bank account at the end of the 10th day. This walkthrough demonstrates how the solution efficiently calculates the total amount deposited using arithmetic series properties.

Finally, we add the sums from the full and partial weeks to get the total amount saved after 10 days: 28 (from the full week) +

Calculate full weeks and remaining days full_weeks, remaining_days = divmod(n, 7) # Calculate total money after complete weeks

Calculate total money for the remaining days # The money each day starts at full_weeks + 1 and increases by 1 each day remaining_start_money = full_weeks + 1 # Starting money for the first remaining day remaining_end_money = remaining_start_money + remaining_days - 1 # Money for the last remaining day

return total_money

```
class Solution {
   /**
    * Calculates the total amount of money after n days, with the money amount increasing every day and resetting every week.
    * @param n Total number of days.
    * @return Total amount of money accumulated over n days.
   public int totalMoney(int n) {
       // Calculate the number of complete weeks.
       int completeWeeks = n / 7;
       // Calculate the remaining days after the complete weeks.
       int remainingDays = n % 7;
       // Calculate the total money saved during the complete weeks.
       // The first week, a person saves 1+2+...+7 = 28. The amount increases by 7 for every subsequent week.
       int totalCompleteWeeksMoney = (28 + (28 + 7 * (completeWeeks - 1))) * completeWeeks / 2;
       // Calculate the total money saved during the remaining days.
       // Starting day of the week determines the money saved on the first day of remaining days.
       int totalRemainingDaysMoney = ((completeWeeks * 2) + remainingDays + 1) * remainingDays / 2;
       // Return the sum of money saved during the complete weeks and the remaining days.
       return totalCompleteWeeksMoney + totalRemainingDaysMoney;
```

class Solution:

C++

public:

class Solution {

int totalMoney(int n) {

int numWeeks = n / 7;

int remainingDays = n % 7;

// Calculate the number of complete weeks

// First week total: 28 => 1+2+3+4+5+6+7

int startDayMoney = numWeeks + 1;

// Calculate the money for the remaining days

// Last day's money of the additional days

int endDayMoney = numWeeks + remainingDays;

return totalMoneyWeeks + totalMoneyRemaining;

// Calculate the remaining days after complete weeks

// Calculate the total money for the complete weeks

// The total for each full week forms an arithmetic progression starting from 28

// Sum for weeks: (first_week_total + last_week_total) / 2 * numWeeks

int totalMoneyWeeks = (28 + 28 + 7 * (numWeeks - 1)) * numWeeks / 2;

// Starting with the next day's money after the last complete week

// Sum for remaining days: (startDayMoney + endDayMoney) * remainingDays / 2

int totalMoneyRemaining = (startDayMoney + endDayMoney) * remainingDays / 2;

// Total money is the sum of money saved in complete weeks and remaining days

// Second week total: $28 + 7 \Rightarrow (1+1)+(2+1)+(3+1)+(4+1)+(5+1)+(6+1)+(7+1)$, and so on.

// General formula for the sum of an arithmetic series: $n/2 * (first_term + last_term)$

```
};
TypeScript
// Calculates the total amount of money saved over 'n' days
function totalMoney(n: number): number {
   // Calculate the number of complete weeks
   const numWeeks: number = Math.floor(n / 7);
   // Calculate the remaining days after complete weeks
   const remainingDays: number = n % 7;
   // Calculate the total money saved during the complete weeks
   // The total for each complete week forms an arithmetic progression starting from 28
   // Sum for weeks is calculated using the formula for the sum of the first n terms of an arithmetic series
   const firstWeekTotal: number = 28;
   const lastWeekTotal: number = 28 + 7 * (numWeeks - 1);
   const totalMoneyWeeks: number = (firstWeekTotal + lastWeekTotal) * numWeeks / 2;
   // Calculate the money saved during the remaining days, which is part of an arithmetic progression
   // Starting from the money that would be saved on the next day if there was another complete week
   const startDayMoney: number = numWeeks + 1;
   // Ending on the last remaining day's money
   const endDayMoney: number = numWeeks + remainingDays;
   // Sum for the remaining days is again calculated using the formula for the sum of arithmetic series
   const totalMoneyRemaining: number = (startDayMoney + endDayMoney) * remainingDays / 2;
   // The total money saved is the sum of the money saved during complete weeks and the remaining days
   return totalMoneyWeeks + totalMoneyRemaining;
```

// This also forms an arithmetic sequence starting from some number depending on the number of passed weeks

```
return total_money
Time and Space Complexity
```

def totalMoney(self, n: int) -> int:

Calculate full weeks and remaining days

full_weeks, remaining_days = divmod(n, 7)

Calculate total money after complete weeks

then it increases by 7 for each subsequent week.

week start sum = 28 # The sum for the first week

Sum the money from full weeks and remaining days

Calculate total money for the remaining days

The sum of an arithmetic progression for a week is 28 (1+2+...+7),

total_full_weeks_money = (week_start_sum + week_end_sum) * full_weeks // 2

The money each day starts at full_weeks + 1 and increases by 1 each day

total_money = total_full_weeks_money + total_remaining_days_money

does not scale with the input size n, it is constant space complexity.

week_end_sum = week_start_sum + $7 * (full_weeks - 1) # Calculate the sum for the last week_end_sum = week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_end_sum = week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_end_sum = week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_end_sum = week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_end_sum = week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_end_sum = week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the sum for the last week_start_sum + 7 * (full_weeks - 1) # Calculate the last week_start_sum + 7 * (full_weeks - 1) # Calculate the last week_start_sum + 7 * (full_weeks - 1) # Calculate the last week_start_sum + 7 * (full_weeks - 1) # Calculate the last$

remaining_end_money = remaining_start_money + remaining_days - 1 # Money for the last remaining day

total_remaining_days_money = (remaining_start_money + remaining_end_money) * remaining_days // 2

remaining_start_money = full_weeks + 1 # Starting money for the first remaining day

The given Python function totalMoney calculates the total amount of money based on a weekly saving pattern. Here is the analysis of its time complexity and space complexity:

or recursion that would otherwise affect the time complexity based on the size of n. Hence, the calculation time is constant.

Time Complexity

Space Complexity The space complexity of the function is also 0(1). It uses a fixed amount of additional space: two variables a and b to store the quotient and remainder from the division of n by 7, and a few auxiliary variables for intermediate calculations. As the space used

The time complexity of the function is 0(1). This is because the calculation involves a constant number of arithmetic operations

(addition, multiplication, modulus, and integer division), regardless of the value of n. These operations do not depend on iteration