265. Paint House II

Dynamic Programming

Problem Description

house with a certain color are provided in a two-dimensional array (matrix) called costs. The costs matrix has n rows (representing each house) and k columns (representing each color's cost for that house). For example, costs[i][j] gives the cost of painting the i-th house with the j-th color. The main objective is to determine the minimum total cost to paint all the houses while ensuring that no two adjacent houses are painted the same color. ntuition

In this problem, we are given n houses in a row and each house can be painted with one of k colors. The costs of painting each

The intuition behind solving this problem lies in breaking it down into a sequence of decisions, where for each house we choose a color. However, we must make this decision considering the cost of the current house as well as ensuring that it doesn't have the

Hard

We initialize our answer with the cost of painting the first house, which is simply the costs of painting that house with each color (the first row of our costs matrix). Then for each subsequent house, we update the cost of painting it with each color by adding the minimum cost of painting

same color as the adjacent house. We approach the solution dynamically, by building up the answer as we go along.

the previous house with a different color. This ensures we meet the requirement that no two adjacent houses share the same color.

To efficiently perform this operation, we maintain a temporary array g which stores the new costs calculated for painting the

current house. For each color j, we find the minimum cost from the array f (which stores the costs for the previous house) excluding the j -th color. We then add the current cost (costs[i][j]) to this minimum cost and store it in g[j]. At the end of each iteration, we assign

g to f, so that f now represents the costs of painting up to the current house.

- After processing all houses, f will contain the total costs of painting all houses where the last house is painted with each of the k colors. Our answer is the minimum of these costs. Through dynamic programming, the code optimizes the painting cost by cleverly tracking and updating the costs while satisfying
- Solution Approach The implementation of the solution follows a dynamic programming pattern, which is often used to break down a complex

problem into smaller, easier-to-manage subproblems. We start with an initialization where we assign the costs of painting the first house with the k different colors directly to our

first version of the f array. This sets up our base case for the dynamic programming solution.

finds the lowest cost to paint the previous house with a different color.

last, with the index representing the color used for the last house.

• The costs matrix provided to us is: [[1,5,3], [2,9,4], [3,1,5]]. This means:

Now g is updated to [5, 10, 5] and we update f with g. So now f = g.

Updated g for the last house is [8, 6, 10], this becomes new f, so f = [8, 6, 10].

paint all the houses while ensuring no two adjacent houses have the same color is 6.

To paint house 0, it costs 1 for color 0, 5 for color 1, and 3 for color 2.

○ To paint house 1, it costs 2 for color 0, 9 for color 1, and 4 for color 2.

the relevant ones and efficiently find the solution.

• Imagine we have n = 3 houses and k = 3 colors.

house: g = costs[1][:] or g = [2, 9, 4].

so g[2] += 1, resulting in g[2] = 5.

def minCostII(self, costs: List[List[int]]) -> int:

Iterate through the rest of the houses

for house index in range(1, num houses):

Initialize costs for the current row

curr_row_costs = costs[house_index][:]

for color index in range(num colors):

min cost except current = min(

prev_row_costs = curr_row_costs

return min(prev_row_costs)

public int minCostII(int[][] costs) {

prev_row_costs = costs[0][:]

num_houses, num_colors = len(costs), len(costs[0])

Get the number of houses (n) and the number of colors (k)

Iterate through each color for the current house

Update the previous row costs for the next iteration

Return the minimum cost for painting all houses with the last row of costs

int numHouses = costs.length; // Number of houses is the length of the costs array

int[] previousCosts = costs[0].clone(); // Clone the first house's cost as the starting point

// Add the minimum found cost to paint the previous house to the current house's color cost

int[] currentCosts = costs[houseIndex].clone(); // Clone the current house's costs

Initialize the previous row with the costs of the first house

resulting in g[0] = 8.

resulting in g[1] = 6.

class Solution:

Java

class Solution {

#include <vector>

#include <climits>

#include <algorithm>

houses while following the rules. This is the value that is returned as the answer.

t = min(f[h] for h in range(k) if h != j)

We then iterate over each of the remaining houses (i) from the second house (1) to the last house (n - 1). For each

f = costs[0][:]

for j in range(k):

g[j] += t

return min(f)

the problem's constraints.

house, we need to calculate the new costs of painting it with each possible color (j). for i in range(1, n): g = costs[i][:]

- For each color (j), we determine the minimum cost of painting the previous house with any color other than j. This is done
- to ensure that the same color is not used for adjacent houses.

To find that minimum, we iterate through all the possible colors (h), ignoring the current color j. This inner loop effectively

- The found minimum cost t is then added to the current cost of painting the house i with color j (costs[i][j]). The result is the total cost to get to house i, having it painted with color j, and is stored in g[j].
- f = gAfter we have finished iterating through all the houses, the f array holds the minimum cost to paint all the houses up until the

The final step is to find the minimum value within the f array since this represents the lowest possible cost for painting all the

Once all colors for the current house have been evaluated, we update the f array to be our newly calculated g.

- The pattern used here leverages dynamic programming's key principle: solve the problem for a small section (the first house, in
- **Example Walkthrough** Let's consider a small example to illustrate the solution approach using the dynamic programming pattern described.

this case) and then build upon that solution incrementally, tackling a new subproblem in each iteration (each subsequent house).

While the problem itself has potentially a very large number of combinations, dynamic programming allows us to consider only

 To paint house 2, it costs 3 for color 0, 1 for color 1, and 5 for color 2. Applying the approach: We initialize f with the costs to paint the first house, so f will be [1, 5, 3].

We move on to the second house and create a new temporary array g, which initially contains the costs for the second

Next, we find the minimum cost to paint the previous house with a color different from the color we want to use for the

For g[0] (house 1, color 0), we look for the minimum cost of painting house 0 with colors 1 or 2. The minimum of [5, 3] is 3,

For g[2] (house 1, color 2), we look for the minimum cost of painting house 0 with colors 0 or 1. The minimum of [1, 5] is 1,

so g[0] += 3, resulting in g[0] = 5.

current house.

For g[1] (house 1, color 1), we look for the minimum cost of painting house 0 with colors 0 or 2. The minimum of [1, 3] is 1, so g[1] += 1, resulting in g[1] = 10.

We repeat the process for the third house. We start with g = costs[2][:] or g = [3, 1, 5].

For g[0], we look for the minimum cost of f[1] or f[2], which is the minimum of [10, 5] and that is 5, so g[0] += 5

For g[1], we look for the minimum cost of f[0] or f[2], which is the minimum of [5, 5] and that is [5, 5] and that is [5, 5] and that is [5, 5] and [5, 5] an

Finally, we find the minimum cost to paint all houses by taking the minimum of f, which is 6. Therefore, the minimum cost to

- For g[2], we look for the minimum cost of f[0] or f[1], which is the minimum of [5, 10] and that is [5, 5] so g[2] += [5]resulting in g[2] = 10.
- Solution Implementation **Python**
 - prev_row_costs[color] for color in range(num_colors) if color != color_index # Add the minimum cost found to the current color cost curr_row_costs[color_index] += min_cost_except_current

int numColors = costs[0].length; // Number of colors available for painting is the length of the first item in costs array

Find the minimum cost for the previous house, excluding the current color index

// Find the minimum cost of painting the previous house with a different color for (int prevColorIndex = 0; prevColorIndex < numColors; ++prevColorIndex) {</pre> // Skip if it is the same color as the current one if (prevColorIndex != colorIndex) { minCost = Math.min(minCost, previousCosts[prevColorIndex]);

// Update previousCosts to currentCosts for the next iteration

// Find and return the minimum cost from the last house's painting cost array

for (int colorIndex = 0; colorIndex < numColors; ++colorIndex) {</pre>

for (int houseIndex = 1: houseIndex < numHouses: ++houseIndex) {</pre>

// Iterate over each house starting from the second house

// Iterate through each color for the current house

int minCost = Integer.MAX VALUE:

currentCosts[colorIndex] += minCost;

return Arrays.stream(previousCosts).min().getAsInt();

previousCosts = currentCosts;

function minCostII(costs: number[][]): number {

let dpTable: number[] = [...costs[0]];

// Loop over each house starting from the second

const numHouses: number = costs.length; // Number of houses

const numColors: number = costs[0].length; // Number of colors

for (let houseIndex = 1; houseIndex < numHouses; houseIndex++) {</pre>

const newCosts: number[] = [...costs[houseIndex]];

if (previousColor !== currentColor) {

// Loop over each color for the current house

// Temporary array to hold the new costs for the current house

for (let currentColor = 0; currentColor < numColors; currentColor++) {</pre>

for (let previousColor = 0; previousColor < numColors; previousColor++) {</pre>

minCost = Math.min(minCost, dpTable[previousColor]);

// Initialize the first row of the DP table with costs of painting the first house

using namespace std; class Solution { public: int minCostII(vector<vector<int>>& costs) { int numHouses = costs.size(); // Number of houses int numColors = costs[0].size(); // Number of colors // Initialize the first row of the DP table with costs of painting the first house vector<int> dpTable = costs[0]; // Loop over each house starting from the second for (int houseIndex = 1; houseIndex < numHouses; ++houseIndex) {</pre> // Temporary vector to hold the new costs for the current house vector<int> newCosts = costs[houseIndex]; // Loop over each color for the current house for (int currentColor = 0; currentColor < numColors; ++currentColor) {</pre> int minCost = INT_MAX; // Initialize minCost to the largest possible value // Find the minimum cost to paint the previous house with a color different from currentColor for (int previousColor = 0; previousColor < numColors; ++previousColor) {</pre> if (previousColor != currentColor) { minCost = min(minCost, dpTable[previousColor]); // Add the minimum cost found to paint the previous house with the cost to paint the current house newCosts[currentColor] += minCost; // Move the values in newCosts to dpTable for the next iteration dpTable = move(newCosts); // Return the minimum element in dpTable (which now contains the minimum cost to paint all houses) return *min_element(dpTable.begin(), dpTable.end()); **}**; **TypeScript**

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// Add the minimum cost found to paint the previous house with the cost to paint the current house
            newCosts[currentColor] += minCost;
        // Move the values in newCosts to dpTable for the next iteration
        dpTable = newCosts;
    // Return the minimum element in dpTable (which now contains the minimum cost to paint all houses)
    return Math.min(...dpTable);
class Solution:
    def minCostII(self, costs: List[List[int]]) -> int:
        # Get the number of houses (n) and the number of colors (k)
        num_houses, num_colors = len(costs), len(costs[0])
        # Initialize the previous row with the costs of the first house
        prev_row_costs = costs[0][:]
        # Iterate through the rest of the houses
        for house index in range(1, num houses):
            # Initialize costs for the current row
            curr_row_costs = costs[house_index][:]
            # Iterate through each color for the current house
            for color index in range(num colors):
                # Find the minimum cost for the previous house, excluding the current color index
                min cost except current = min(
                    prev_row_costs[color] for color in range(num_colors) if color != color_index
                # Add the minimum cost found to the current color cost
                curr_row_costs[color_index] += min_cost_except_current
            # Update the previous row costs for the next iteration
            prev_row_costs = curr_row_costs
        # Return the minimum cost for painting all houses with the last row of costs
        return min(prev_row_costs)
Time and Space Complexity
Time Complexity:
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let minCost: number = Number.MAX_SAFE_INTEGER; // Initialize minCost to the largest possible safe integer value

// Find the minimum cost to paint the previous house with a color different from currentColor

The given code iterates over n rows, and for each row, it iterates over k colors to calculate the minimum cost. Inside the inner

different color, avoiding the current one. Therefore, for each of the n rows, the code performs 0(k) operations for each color, and within that, it performs another O(k) to find the minimum. This results in a time complexity of O(n * k * k). **Space Complexity:**

loop, there is another loop that again iterates over k colors to find the minimum cost of painting the previous house with a

The space complexity of the code is determined by the additional space used for the f and g arrays, both of size k. No other significant space is being used that scales with the input size. Thus the space complexity is O(k).