1046. Last Stone Weight Heap (Priority Queue)

Problem Description

In this problem, we have a collection of stones with different weights, given in an array stones, where each stone's weight is

represented by stones[i]. We are simulating a game where we repeatedly smash the two heaviest stones together and determine the outcome according to the following rules: • If both stones have the same weight (x == y), both stones get completely destroyed.

• If the weights are different (x != y), the lighter stone gets destroyed, and the weight of the heavier stone gets reduced by that of the lighter stone (y - x).

The game continues until there is either one stone left or no stones remaining. The goal is to return the weight of the last remaining stone. If there are no stones left as a result of the smashes, we should return 0.

Intuition

min heaps.

The solution requires us to repeatedly find and remove the two heaviest stones. Since we need to do this repeatedly, a heap is an ideal data structure as it allows for efficient retrieval and updating of the largest elements. A max heap keeps the maximum element at the top. However, Python's heapq module provides a min heap, so we insert the

negative of stone weights to simulate the behavior of a max heap. Here is the step-by-step approach to the solution:

1. Convert all stone weights to their negative and create a min heap. This negation is necessary because the Python heapq module only supports

2. While there are at least two stones in the heap:

1. Pop the heaviest stone (which is the smallest in the min heap due to negation) and store its negated value in y. 2. Pop the second heaviest stone (again the smallest in our min heap) and store its negated value in \times .

3. If x and y are not equal, we push the weight difference negated (x - y) back onto the heap since stone x got destroyed and the weight

of stone y reduced by x. 3. After the loop, if the heap is empty, it means no stones are left and we return 0. Else, we return the negation of the weight of the last stone left in the heap (as we stored negative values, we need to negate it back to return the actual weight).

Using this approach, we efficiently simulate the stone smashing game and find the weight of the last stone or determine that no stones are left.

as long as the length of the heap (h) is greater than one.

Solution Approach The method lastStoneWeight is implemented using a min heap to efficiently manage the stones according to their weights.

• A min heap is created from the list of stones. Each stone's weight is negated prior to insertion because Python's heapq module works as a min

heap. A min heap allows quick access to the smallest element, so by negating the weights, we get quick access to the largest element.

h = [-x for x in stones]heapify(h)

return 0 if not h else -h[0]

Example Walkthrough

Here's a breakdown of the solution:

The solution iteratively processes the heap until there's one or zero stones left. This is handled by a while loop that continues

Inside the loop, the two heaviest stones (which are actually the two smallest values in the heap due to negation) are popped from the heap. This is done using heappop(h), and the negated value of the pops represents y and x.

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y, x = -heappop(h), -heappop(h)
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destroyed, while the other (y) is reduced in weight. The difference (y - x) is computed, negated, and pushed back into the heap. if x != y: heappush(h, x - y)

After the loop exits, which happens when only one stone is left or none at all, the function checks if the heap is empty. If it is empty (not h), the

Using heapq for maintaining a heap and negating values is an efficient approach to simulate a max heap in Python. This problem

showcases an excellent use of the heap data structure to solve a problem related to constant removal and insertion of elements

function returns 0. Otherwise, it returns the weight of the last stone left, negating it to convert it back to the original weight value.

• If the weight of the two stones is not equal (x != y), it means that after smashing the stones, one of them (the lighter stone x) is completely

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to achieve a sorted characteristic (largest or smallest).
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4, 1, 8, 1]. We need to perform the following steps: Convert the weights to their negative and create a min heap: \circ We negate the weights: $\begin{bmatrix} -2, -7, -4, -1, -8, -1 \end{bmatrix}$ \circ Create a min heap from these negated weights: h = [-8, -7, -4, -1, -2, -1]

Let's consider a small example to illustrate the solution approach: Suppose we have an array of stone weights stones = [2, 7,

2. Pop the second heaviest stone: $\mathbf{x} = -\text{heappop}(h)$ gives us $\mathbf{x} = 7$, and now $\mathbf{h} = [-4, -2, -1, -1]$ 3. Push the weight difference negated back onto the heap since $x \neq y$:

Repeat the process: • Next, y = -heappop(h) gives us y = 4, h = [-2, -1, -1, -1]

 \circ Then, x = -heappop(h) gives us x = 2, h = [-1, -1, -1]

 \circ Next, y = -heappop(h) gives us y = 2, h = [-1, -1]

 \circ Then, x = -heappop(h) gives us x = 1, h = [-1]

 \circ Next, y = -heappop(h) gives us y = 1, h = [-1]

def lastStoneWeight(self, stones: List[int]) -> int:

max heap = [-stone for stone in stones]

stone1 = -heappop(max heap)

stone2 = -heappop(max_heap)

public int lastStoneWeight(int[] stones) {

for (int stone : stones) {

maxHeap.offer(stone);

while (maxHeap.size() > 1) {

// Add all stone weights to the max-heap

// Get the two heaviest stones

int stoneOne = maxHeap.poll();

int stoneTwo = maxHeap.poll();

maxHeap.offer(stoneOne - stoneTwo);

if (stoneOne != stoneTwo) {

return 0 if not max_heap else -max_heap[0]

* Simulate the process of smashing stones together and return

Since x == y, we don't push anything back onto the heap.

o Then, x = -heappop(h) gives us x = 1, h = []

Solution Implementation

heapify(max_heap)

while len(max heap) > 1:

class Solution:

• y = -heappop(h) gives us y = 8, and now h = [-7, -2, -4, -1, -1]

■ The difference is 8 - 7 = 1. After negating, we push -1 back onto the heap.

While there are at least two stones in the heap:

1. Pop the heaviest stone (smallest in negated form):

■ Now, h = [-4, -2, -1, -1, -1]

- \circ The difference is 4 2 = 2. After negating, we push -2 back onto the heap. \circ Now, h = [-2, -1, -1] Continue:
- \circ Now, h = [-1, -1] Final iterations will destroy both of the stones because they have the same weight:

Now the heap is empty (h = []), that is, no stones are left. We return \emptyset .

 \circ The difference is 2 - 1 = 1. After negating, we push -1 back onto the heap.

Python from heapq import heapify, heappush, heappop

Create a max heap by inverting the values of the stones

Continue processing until there is one or no stones left

Stones are negated again to get their original values

If the heap is empty, return 0: else return the weight of the last stone

// Create a max-heap to store and compare the stone weights in descending order

// If they are not the same weight, put the difference back into the max-heap

// If they are equal, both stones are completely smashed, and nothing is added back

PriorityQueue<Integer> maxHeap = new PriorityQueue<>((a, b) -> b - a);

// Continue until there is only one stone left or none at all

// Return the last stone's weight or 0 if no stones are left

Pop the two largest stones from the heap

If the largest stones are not of the same weight if stone1 != stone2: # The result of the collision is added back to the heap heappush(max_heap, -(stone1 - stone2))

The final result for the example input stones = [2, 7, 4, 1, 8, 1] is [0, as all stones are eventually destroyed.]

```
* the weight of the last remaining stone (if any).
* @param stones An array of stone weights.
* @return The weight of the last stone, or 0 if no stones are left.
```

*/

/**

class Solution {

Java

```
return maxHeap.isEmpty() ? 0 : maxHeap.poll();
#include <vector>
#include <queue>
class Solution {
public:
   // Function to return the last stone's weight after smashing the largest two until one or none are left
    int lastStoneWeight(vector<int>& stones) {
       // Priority queue to store the stones with max heap property to easily retrieve the heaviest stones
       priority_queue<int> maxHeap;
       // Insert all stones into the priority queue
        for (int stone : stones) {
            maxHeap.push(stone);
       // Loop until there is only one stone left or none
       while (maxHeap.size() > 1) {
            // Take out the heaviest stone
            int heaviestStone = maxHeap.top();
            maxHeap.pop();
            // Take out the second heaviest stone
            int secondHeaviestStone = maxHeap.top();
            maxHeap.pop();
            // If the two stones have different weights, push the difference back into the queue
            if (heaviestStone != secondHeaviestStone) -
                maxHeap.push(heaviestStone - secondHeaviestStone);
           // If the stones have the same weight, both get destroyed and nothing goes back into the queue
       // If there are no stones left, return 0, otherwise return the weight of the remaining stone
       return maxHeap.empty() ? 0 : maxHeap.top();
```

// If there is a weight difference, enqueue the difference as a new stone if (heavierStone !== lighterStone) { priorityQueue.enqueue(heavierStone - lighterStone);

class Solution:

TypeScript

/**

*/

// Import the necessary module for Priority Queue

* @param {number[]} stones - An array of stone weights.

function getLastStoneWeight(stones: number[]): number {

// Enqueue all the stones to the priority queue

// Initialize a max priority queue for the stones

const priorityQueue = new MaxPriorityQueue<number>();

// Loop until there is either one stone left or none

def lastStoneWeight(self, stones: List[int]) -> int:

max heap = [-stone for stone in stones]

const heavierStone = priorityQueue.dequeue().element;

const lighterStone = priorityQueue.dequeue().element;

return priorityQueue.isEmpty() ? 0 : priorityQueue.dequeue().element;

Create a max heap by inverting the values of the stones

Continue processing until there is one or no stones left

Stones are negated again to get their original values

Pop the two largest stones from the heap

* stone, or 0 if none are left.

for (const stone of stones) {

priorityQueue.enqueue(stone);

// Dequeue the two heaviest stones

while (priorityOueue.size() > 1) {

from heapq import heapify, heappush, heappop

heapify(max_heap)

while len(max heap) > 1:

import { MaxPriorityQueue } from '@datastructures-js/priority-queue';

* Simulates a process where stones smash each other. If two stones have

* @return {number} The weight of the last remaining stone, or 0 if none.

* The smaller stone is then considered destroyed. The process repeats until

* different weights, the weight of the smaller one is subtracted from the other.

* there is one stone left or none. The function returns the weight of the remaining

stone1 = -heappop(max heap) $stone2 = -heappop(max_heap)$ # If the largest stones are not of the same weight if stone1 != stone2: # The result of the collision is added back to the heap heappush(max_heap, -(stone1 - stone2)) # If the heap is empty, return 0; else return the weight of the last stone return 0 if not max_heap else -max_heap[0] Time and Space Complexity

// If the priority queue is empty, return 0; otherwise, return the weight of the last stone

The main operations in the algorithm are: 1. Converting the stones list into a heap which takes O(n) time, where n is the number of stones. 2. The while loop. In the worst case, the heap contains n - 1 elements, and heappop() is called twice per iteration. Since each heappop()

complexity of the given code.

Time Complexity

3. The loop runs at most n - 1 times because in each iteration at least one stone is removed.

Putting it all together, the worst-case scenario would involve (2 * log n + log n) operations per iteration due to two heappop()

operation takes 0(log n) time, and in each iteration, we might do a heappush() which also takes 0(log n) time.

calls and one potential heappush() call, across n-1 iterations. Hence, the total time complexity is $0(n \log n)$. **Space Complexity**

The given code implements a heap to solve the last stone weight problem. Let's analyze both the time complexity and the space

The space complexity consists of: 1. The heap h which stores at most n integers, thus requiring O(n) space. 2. Constant extra space for variables x and y.

So, the overall space complexity of the algorithm is O(n) since the heap size is proportional to the input size, and other space usage is constant.