2964. Number of Divisible Triplet Sums

Medium Array Hash Table

Problem Description

j, k) that follow a specific criterion. This criterion requires that the indices form a strictly increasing sequence (i < j < k) and the sum of the elements at these indices is divisible by a given integer d. In other words, nums[i] + nums[j] + nums[k] should be an integer multiple of d.

To tackle this problem, we need to identify combinations of three different array elements whose indices are in ascending order

The challenge is to find out the number of unique triplets within an array nums, where each triplet consists of different indices (i,

and check for the divisibility of their sum by d. It's a computational challenge that requires efficient enumeration of the possible triplets to avoid a brute force approach that would take too long.

Intuition

To optimize the process of finding these triplets, the solution leverages a hash table strategy to avoid redundant calculations. The main idea behind the solution is to use a hash table, denoted as cnt, to keep track of how many times each remainder (when

what remainder we would need from the nums[i] (where i < j) to ensure that the sum of nums[i], nums[j], and nums[k] is divisible by d.
Here's the thinking process:
1. As we move through the array, with each nums[j], we look ahead to all future nums[k] where k > j. For each of these pairs, we calculate the remainder that would be needed by a preceding nums[i] to make the sum of nums[i] + nums[j] + nums[k]

elements of nums are divided by d) occurs up to the current index being considered. As we iterate through the array, we calculate

divisible by d. We use the aforementioned hash table to quickly check the count of such potential nums [i] elements.

before continuing to the next j.

- We then add the count from our hash table to our answer (accumulating the number of triplets that meet our criteria up to the current j).
 After considering pairs of nums[j] and nums[k], we increment the count of the remainder of nums[j] itself in the hash table
- Solution Approach
- The solution to this LeetCode problem is centered around a clever use of a hash table, specifically a defaultdict from Python's collections module, which allows us to automatically initialize missing keys with an integer (initialized to 0 in this case). This helps

The algorithm can be broken down into the following steps: 1. First, we iterate over the elements of the nums array while calculating the remainder when each element nums[j] is divided by

condition.

returned.

2. For any given index j, we look ahead to the elements nums [k] for all k such that k > j and calculate x, which is equal to (d - (nums [j] + nums [k]) % d) % d. This represents the remainder we need from some nums [i] (where i < j) so that the sum of the three elements is divisible by d.

sum up these occurrences in a variable ans, which ultimately holds the total number of triplets that satisfy the problem's

d (i.e., nums[j] % d). We use this to determine what the corresponding nums[i]'s remainder should be in order to have

3. The calculated x is then used to check in our cnt hash table how many times we've seen such a remainder before index y. We

sums if d is small relative to the values in nums.

(nums[i] + nums[j] + nums[k]) % d == 0.

us to track the frequency of remained parts of numbers modulo d.

Before we move on to the next j, we increase the count of nums[j]'s remainder in the hash table by 1, i.e., cnt[nums[j] % d] += 1, representing that we have seen another occurrence of this particular remainder.
 Once we exhaust all possibilities for j and its corresponding k, the variable ans will hold the correct answer, which is then

One of the clever patterns employed in this solution is the recognition that for triplets (i, j, k) to satisfy our condition, it is not

candidates while iterating over j and k. This avoids the need for a full, expensive three-level loop and thus significantly improves

This algorithm runs in 0(n^2) time complexity, with n being the size of the array nums, which is much more efficient than the brute

force 0(n^3). The space complexity is 0(d) due to the hash table storing at most d different remainders.

We initiate a defaultdict(int) which will serve as the cnt hash table to store the counts of seen remainders.

necessary to track each i explicitly. By using remainders and counting their occurrences, we implicitly handle all possible i

the time complexity.

The use of mathematics to track the needed remainder part instead of the raw sum also reduces the memory complexity as we only need to store counts for each possible remainder range from 0 to d-1. This is much smaller than the potential range of the

Let's illustrate the solution approach using an example:

Consider nums = [2, 3, 5, 7, 11] and d = 5.

We start by iterating through the array:

■ For a potential k with nums [k] = 7 (next element), we need a remainder x (needed from some previous nums [i]), which is (5 - (3 + 7)

■ For a future k with nums[k] = 11 (next element), we need a remainder x from some previous nums[i] which is (5 - (3 + 11) % 5) % 5

= 1. We don't have any elements that left a remainder of 1 until now (cnt[1] is 0), so no triplet can be formed.

2. At nums[1] = 3, the remainder is 3. • We are looking for a triplet that includes nums[i], nums[j]=3, and some future nums[k].

% 5) % 5 = 0. We look into cnt and see that cnt[0] = 0 (0 hasn't been seen yet as a remainder before index 2), so no triplets can be

Moving on to nums[2] = 5, the remainder is 0.

Now, let's look ahead for future k values:

As there are no values in cnt yet, all remainders start with a count of 0.

For nums[0] = 2, the remainder when divided by d is 2.

Update cnt[2] to 1 (since 2 % 5 = 2).

Update cnt[3] to 1 (3 % 5 = 3).

Update cnt[1] to 1 (11 % 5 = 1).

Solution Implementation

from collections import defaultdict

Length of the input list

for k in range(j + 1, n):

Loop over the list to find valid triplets

remainder_count[nums[j] % divisor] += 1

* Counts the number of divisible triplets in the given array.

The divisor for checking divisibility.

Return the total count of valid triplets

* @param nums The input array of integers.

Compute the remainder needed from the third element

for the sum of the triplet to be divisible by 'divisor'

valid_triplet_count += remainder_count[needed_remainder]

Increment the count of the remainder for the current element

* A treeplit is a sequence of three numbers (a, b, c), such that (a + b + c) % d == 0.

needed_remainder = (divisor - (nums[j] + nums[k]) % divisor) % divisor

Add the count of numbers previously encountered with the needed remainder

n = len(nums)

for j in range(n):

Python

formed here.

Let's look ahead:

There are no previous elements, so we just move to the next index.

Update cnt [0] to 1 (5 % 5 = 0).
4. At nums [3] = 7, the remainder when divided by d is 2.

No need to look ahead because 11 is the last element.

- Update cnt[2] to 2.
 Finally, at nums [4] = 11, the remainder is 1.
- using the remainders and the cnt hash table to avoid redundancy. In cases where nums contains the right combinations, the cnt table would help us tally up the valid triplet counts quickly and efficiently.

Since there are no triplets that satisfy (nums[i] + nums[j] + nums[k]) % 5 == 0, our answer thus far is 0.

class Solution:
 def divisibleTripletCount(self, nums: List[int], divisor: int) -> int:
 # Dictionary to store the frequency of remainders
 remainder_count = defaultdict(int)

Initialize the count of valid triplets
 valid_triplet_count = 0

In this example, we failed to find any valid triplets, but the process demonstrates how we would systematically check for them

return valid_triplet_count Java

class Solution {

* @param d

int answer = 0;

for (int j = 0; j < n; ++j) {

counts[nums[j] % d]++;

int n = nums.size(); // Length of the array.

for (int k = j + 1; k < n; ++k) {

// Iterate over all pairs of numbers in 'nums'.

answer += counts[complement];

int complement = (d - (nums[j] + nums[k]) % d) % d;

// For the number at position 'j', increment its frequency.

return answer; // Return the total count of divisible triplets.

function divisibleTripletCount(nums: number[], divisor: number): number {

let tripletCount = 0; // initialize triplet count to zero

// update the remainder count for the current number

const currentRemainder = nums[middleIndex] % divisor;

// Iterate over each pair of numbers in the array

const arrayLength = nums.length; // get the length of the nums array

for (let middleIndex = 0; middleIndex < arrayLength; ++middleIndex) {</pre>

// calculate the required value to complete the triplet

tripletCount += remainderCount.get(requiredValue) || 0;

return tripletCount; // return the total count of divisible triplets

for (let lastIndex = middleIndex + 1; lastIndex < arrayLength; ++lastIndex) {</pre>

// increase the count of valid triplets by the amount found in remainderCount

remainderCount.set(currentRemainder, (remainderCount.get(currentRemainder) | 0 + 1);

// Add the count of the complement to the answer.

/**

```
* @return The count of divisible triplets.
    */
    public int divisibleTripletCount(int[] nums, int d) {
       // Map to store frequency counts of numbers modulo d
        Map<Integer, Integer> frequencyCounts = new HashMap<>();
        // The answer (count of divisible triplets)
        int answer = 0;
       // Length of the nums array
        int length = nums.length;
        // Iterate through the pairs (j, k) where j < k
        for (int j = 0; j < length; ++j) {
            for (int k = j + 1; k < length; ++k) {</pre>
                // Calculate the modulo of the negative sum of nums[j] + nums[k]
                // This is the number needed to complete triplet to be divisible by d
                int neededModulo = (d - (nums[j] + nums[k]) % d) % d;
                // Add to answer the count of numbers that have the neededModulo
                answer += frequencyCounts.getOrDefault(neededModulo, 0);
            // Update the frequencyCounts map with the current number's modulo
            frequencyCounts.merge(nums[j] % d, 1, Integer::sum);
        // Return the total count of divisible triplets
        return answer;
C++
#include <vector>
#include <unordered_map>
using namespace std;
class Solution {
public:
   // Function to count the number of triplets such that sum of two elements is divisible by 'd'.
    int divisibleTripletCount(vector<int>& nums, int d) {
        // 'counts' is used to store the frequency of elements mod 'd'.
       unordered_map<int, int> counts;
```

// Calculate the complement that would make the sum of a triplet divisible by 'd'.

const remainderCount: Map<number, number> = new Map(); // map to count occurrences of each remainder

const requiredValue = (divisor - ((nums[middleIndex] + nums[lastIndex]) % divisor)) % divisor;

class Solution:

from collections import defaultdict

};

TypeScript

```
def divisibleTripletCount(self, nums: List[int], divisor: int) -> int:
       # Dictionary to store the frequency of remainders
       remainder_count = defaultdict(int)
       # Initialize the count of valid triplets
       valid_triplet_count = 0
       # Length of the input list
       n = len(nums)
       # Loop over the list to find valid triplets
       for j in range(n):
           for k in range(j + 1, n):
               # Compute the remainder needed from the third element
               # for the sum of the triplet to be divisible by 'divisor'
               needed_remainder = (divisor - (nums[j] + nums[k]) % divisor) % divisor
               # Add the count of numbers previously encountered with the needed remainder
               valid_triplet_count += remainder_count[needed_remainder]
           # Increment the count of the remainder for the current element
           remainder_count[nums[j] % divisor] += 1
       # Return the total count of valid triplets
       return valid_triplet_count
Time and Space Complexity
  The given Python code defines a method divisibleTripletCount within a Solution class that counts triplets in an array, where
  the sum of each triplet is divisible by a given integer d. The code primarily involves two nested loops: the outer loop iterates over
  each element j of the array, and the inner loop iterates over the elements following j (k). Here's a breakdown of the complexities:
```

This creates a total of around n * (n/2) comparisons, simplifying to $(n^2)/2$ which is in the order of $0(n^2)$. This is because constants are ignored in Big O notation.

amount to the space complexity.

Time Complexity:

outer loop.

Therefore, the time complexity of the code is 0(n^2).

Space Complexity:

The time complexity is determined by the number of nested iterations over the input list nums.

The outer loop runs for n iterations, with n being the length of nums.

unique value of nums[j] % d. However, since % d creates d possible remainders, the defaultdict will at most contain d entries.

• We also have a few integer variables (ans, n, x), but these do not scale with input size n, and thus contribute a constant

The space complexity refers to the amount of additional memory used by the program in relation to the input size.

The space complexity of the code is therefore dictated by the defaultdict size, along with a small constant for the variables used, so it is O(d). However, given that d is a single integer value and not related to the size of the input array nums, the d in the

A defaultdict(int) is created to store counts of nums[j] % d. In the worst case, we would have to store a number for every

• For each iteration of the outer loop, the inner loop executes n - j - 1 times, which results in an average case of n/2 times per iteration of the

space complexity could be considered a constant factor.

Thus, the space complexity of the code is 0(1) if d is considered constant with respect to n. However, since the reference answer

values modulo d, binding the space complexity to the length of the array nums. Under this assumption, the space complexity would indeed be O(n).

In conclusion, the time complexity of the code is $0(n^2)$, and the space complexity, depending on the context, is either 0(1) or

suggests that the space complexity is O(n), it seems there might be a presumption that the array might contain up to n distinct

O(n) based on the aforementioned reasoning.