2193. Minimum Number of Moves to Make Palindrome

Binary Indexed Tree Two Pointers String Greedy Hard

You are given a string s that is composed only of lowercase English letters. Your goal is to transform this string into a palindrome using the smallest number of moves possible. A palindrome is a word or phrase that reads the same backward as forward. In each move, you are allowed to select any two adjacent characters in the string and swap them.

Leetcode Link

Intuition

The challenge ensures that the given string can always be rearranged into a palindrome, so you don't need to check for the possibility of creating one, only to find the minimum number of moves to do so.

Problem Description

on, until the middle of the string is reached.

The solution approach is based on the principle that, to form a palindrome, the letters must mirror each other from the center of the

Understanding that, we can work our way inwards from both ends of the string towards the center, making swaps to position each character correctly. At each step, you look for the first occasion of the letter at the i-th position from the start of the string, starting from the j-th position from the end of the string, where j is initially length of the string - 1. When you find a matching letter, it

string outwards. That means characters at the start and end of the string must be the same, then the ones inward from them, and so

indicates that it needs to be swapped multiple times until it reaches the j-th position. Each swap is counted as one move. In some cases, there might be a character that does not have a matching pair (an unmatched character) in its immediate search. When such an unmatched situation is found, it means this character must be at the center of the palindrome. Since we know the string can always be a palindrome, there would be at most one such character. For an unmatched character, you need to bring it to

the center. This requires a specific number of moves, which is n // 2 - i, considering n is the length of the string. The process is repeated until i reaches the center of the string, accumulating the number of moves required to place each character in its rightful position for a palindrome. By following the above approach, the minimum number of moves required to make the string a palindrome can be determined.

Solution Approach

towards the center, and a greedy strategy to make the minimum number of swaps at each step. Here's a step-by-step breakdown of the algorithm, based on the provided Python implementation:

1. The string s is converted into a mutable list cs to move characters around easily since strings in Python are immutable.

The solution approach for the problem involves a two-pointer technique, iterating from the outermost characters of the string

2. Two pointers i and j are set up, where i starts at the beginning of the list (0) and j starts at the end (n - 1, where n is the length of the string).

3. We initiate a counter ans to keep track of the number of moves made. 4. The while loop begins and continues until i is less than j. Within this loop, we are progressively fixing the characters at the

5. Inside the loop, we start an inner loop that goes in reverse from j to i. This reverse loop looks for a character matching cs[i] starting from the j-th position.

should be moved to the center. The number of moves is calculated as (n // 2) - i and added to ans.

9. Pointer i is incremented, and the loop continues until all characters are in the correct position for the palindrome.

Let's illustrate the solution approach with a simple example where s = "aabb". Following the steps of the algorithm:

beginning and end of the string while moving towards the center.

1. First, we convert the string s to a list cs, so cs = ['a', 'a', 'b', 'b'].

6. We find that cs[1] equals 'a', thus setting the even flag to True.

11. Increment i to 1 and as i is now equal to j, the loop ends.

(cs[k]) towards its mirror position at cs[j]. For every swap, the counter ans is incremented. 7. Once swapping is done, j is decremented, effectively shortening the active part of the list that hasn't been fixed yet. 8. If no matching character is found (the even flag remains False), it means that the current character cs[i] is unmatched and

6. If a matching character is found (the even flag is set to True), further nested loops are used to swap the matching character

10. After the loop completes, the ans variable contains the total number of moves needed to make s a palindrome. By using greedy decision-making (choosing the nearest match to swap) and the two-pointer approach, we ensure that we are

making swaps that progress towards the desired palindrome with the least number of moves. At the end of the process, the function

- returns the calculated ans, which is the minimum number of moves needed to transform the string into a palindrome. Example Walkthrough
- 2. Initialize two pointers: i = 0 and j = 3 (since n = 4, and n 1 = 3). 3. Set a counter ans = 0 to keep track of the number of moves made. 4. The while loop begins with i < j (0 < 3) and will continue until i >= j.

5. We enter the inner loop starting from j and going towards i. We are looking for the first occurrence of the character cs[i] which

10. Since cs[2] is 'b' and not a match, and j eventually equals i with no match found, the even flag remains False. This signifies

7. Since cs [1] already matches cs [i], no swap is needed, and we do not increment ans. 8. We now decrease j to 2 and effectively shorten the list to ['a', 'a', 'b'].

without the need for further moves.

4. Enter the while loop with i < j (0 < 4).

2. Pointers are i = 0, j = 4.

3. Counter is ans = 0.

Python Solution

char list = list(s)

while left < right:</pre>

found = False

moves = 0

n = len(s)

right = n - 1

left = 0

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is 'a'.

cs[i] is the unmatched character. However, since a does have a match already at cs[1], we know this process completes here

9. Pointers are now i = 0 and j = 2. The inner loop will then try to find a match for cs[i] which is 'a' again.

Let's take a slightly more complex example: s = "abbaa". 1. Convert the string s to a list cs, so cs = ['a', 'b', 'b', 'a', 'a'].

For this simple example, there were 0 moves needed because the string was already in a palindromic order.

5. Looking for a match for cs[i] (which is 'a') starting from cs[j]. 6. No swap needed immediately as cs[j] is 'a'. 7. Decrease j to 3. Move i to 1 since i and j match.

Please note that while these examples are simple, the approach works even with more complex strings and ensures the minimum

12. The unanswered character 'a' in cs[i] now has to be moved to the center. For this example, one swap is needed to move 'a' from the end to the center, making the string ababa which is a palindrome.

9. We find the match immediately at cs [2] which is 'b'.

11. Increment i to 2. Now i is greater than j, the loop ends.

class Solution: def min_moves_to_make_palindrome(self, s: str) -> int:

Initialize the number of moves and the indexes.

Iterate until we have checked all characters.

found = True

while k < right:</pre>

k += 1

right -= 1

moves += 1

moves += (n // 2) - left

Move to the next character from the left.

Return the total number of moves required to form a palindrome.

// Function to find the minimum number of moves to make a string palindrome.

// Use two pointers approach to move characters to form palindrome

--j; // Move the right pointer inwards

// Loop to find a character from the right that matches with str[i]

std::swap(str[k], str[k + 1]); // Swap characters

++moves; // Increment moves count for each swap

// Initialize the number of moves to 0

// Move the matching character to the correct position on the right

bool foundPair = false; // Flag to check if a character matching the left pointer is found on the right

int minMovesToMakePalindrome(string str) {

for (int k = j; k > i; --k) {

break;

if (str[i] == str[k]) {

foundPair = true;

for (; k < j; ++k) {

int strSize = str.size(); // Length of the string

for (int i = 0, j = strSize - 1; i < j; ++i) {

Convert the string into a list for easy manipulation.

Flag to check if we found a matching character.

by swapping adjacent characters.

we decrement the right index.

When we find a match, we set found to True.

Increment the moves count for each swap.

We then move the matched character to its correct position

Once we have moved the character to the correct position,

char_list[k], char_list[k + 1] = char_list[k + 1], char_list[k]

number of moves because of the greedy two-pointer strategy used.

8. Now look for a match for cs[i] (which is 'b') starting from cs[j].

10. Decrease j to 2. Since j is now equal to i, no swap is needed.

Iterate from right to left starting from the current right index, 16 # looking for a matching character. for k in range(right, left, -1): if char_list[left] == char_list[k]: 19

32 break 33 34 # If we did not find a matching character, it means 35 # the character needs to be moved to the center for odd length palindrome.

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               if not found:
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                   # For this unmatched character, how many moves will it take to reach the center?
                   # It will be half the length of the string minus the current index.
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left += 1

return moves

Java Solution

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class Solution {
       public int minMovesToMakePalindrome(String s) {
           // Length of the given string
           int length = s.length();
           // Initialize the count of minimum moves to 0
           int minimumMoves = 0;
           // Convert the string to character array for easy manipulation
           char[] characters = s.toCharArray();
9
           // We'll use two pointers, starting from the outside of the array moving inwards
           for (int leftIndex = 0, rightIndex = length - 1; leftIndex < rightIndex; ++leftIndex) {</pre>
               // A variable to check if we have found a matching pair or not
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               boolean pairFound = false;
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                for (int searchIndex = rightIndex; searchIndex != leftIndex; --searchIndex) {
                   // Check if the characters match.
16
                   if (characters[leftIndex] == characters[searchIndex]) {
                        // If match is found, we set the pairFound status to true
                        pairFound = true;
19
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21
                        // Now we need to move the matching character to the right place
22
                        for (; searchIndex < rightIndex; ++searchIndex) {</pre>
23
                            // Swap characters
                            char temp = characters[searchIndex];
24
25
                            characters[searchIndex] = characters[searchIndex + 1];
26
                            characters[searchIndex + 1] = temp;
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                            // Incrementing the move counter for each swap
29
                            ++minimumMoves;
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                        // Since we found a pair and moved the character, we can move the right pointer inwards
                        --rightIndex;
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                        break; // Done with moving the pair, break to outer loop for next character
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               // If no pair was found for the current character
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               if (!pairFound) {
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                   // This means it's the middle character in a palindrome with odd length
                   // We need to move it to the center
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                   minimumMoves += length / 2 - leftIndex;
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           // Return the minimum number of moves needed to make the string a palindrome
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           return minimumMoves;
C++ Solution
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1 class Solution {

int moves = 0;

2 public:

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// If no matching character is found, it must be moved to the center of palindrome
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               if (!foundPair) {
                   moves += strSize / 2 - i; // Increment moves by the required positions to reach center
28
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           return moves; // Return total number of moves
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33 };
Typescript Solution
  // Function to find the minimum number of moves to make a string palindrome.
   function minMovesToMakePalindrome(str: string): number {
       const strSize: number = str.length; // Length of the string
       let moves: number = 0;
                                             // Initialize the number of moves to 0
       // Use two pointers approach to move characters to form palindrome
       for (let i = 0, j = strSize - 1; i < j; i++) {
            let foundPair: boolean = false; // Flag to check if a character matching the left pointer is found on the right
           // Loop to find a character from the right that matches with str.charAt(i)
           for (let k = j; k > i; k--) {
               if (str.charAt(i) === str.charAt(k)) {
12
                   foundPair = true;
13
                   // Move the matching character to the correct position on the right
14
                   for (; k < j; k++) {
15
                       str = swapCharacters(str, k, k + 1); // Swap characters
16
                       moves++; // Increment moves count for each swap
17
18
                   j--; // Move the right pointer inwards
19
20
                   break;
21
23
24
           // If no matching character is found, it must be moved to the center of the palindrome
25
           if (!foundPair) {
26
               moves += Math.floor(strSize / 2) - i; // Increment moves by the required positions to reach center
27
28
29
       return moves; // Return total number of moves
```

Time and Space Complexity

required to make the input string a palindrome.

charArray[i] = charArray[j];

return charArray.join(''); // Convert array back to string and return

series summation formula. The time complexity approximates to 0(n^2).

charArray[j] = temp;

30 } 31 32 // Helper function to swap characters in a string and return the new string function swapCharacters(s: string, i: number, j: number): string { const charArray: string[] = [...s]; // Convert string to array for swapping const temp: string = charArray[i]; 35

The given Python code defines a method minMovesToMakePalindrome that calculates the minimum number of adjacent swaps

The time complexity of the code is governed by the two nested loops (the while and the inner for loop) that traverse the characters of the string. The outer while loop runs for approximately n/2 iterations, where n is the length of the string (since i starts from 0 and starts from n - 1 and they move towards the center).

Time Complexity:

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39 }

Inside the outer loop, the for loop searches for a matching character from the end of the substring to the current position of i. In the worst-case scenario, this can lead to about n comparisons for the first iteration of the outer loop, then n-2 for the next, and so on. This pattern of comparisons forms a series that can be approximated to n/2 computations on average per outer loop iteration.

Furthermore, the swapping operations within the while loop (inside the inner for if a match is found) have a potential to run up to n times in worst-case scenarios. This adds up to another series of operations contributing to the time complexity.

Thus, the total time complexity is the summation of these two series of operations, which can be estimated with the arithmetic

Space Complexity:

The space complexity is determined by the additional space required by the algorithm aside from the input string. Here, the input string is converted to a list cs, which utilizes O(n) space. The rest of the variables (ans, n, i, j, even, and k) use constant space.

Therefore, the total space complexity of the algorithm is O(n), as the space used by the list cs is the only space that grows proportionally with the input size.