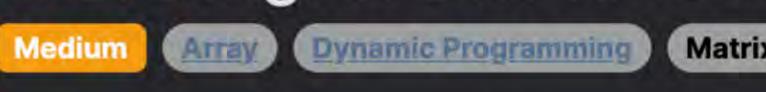
562. Longest Line of Consecutive One in Matrix



Matrix Leetcode Link

Problem Description

The problem presents a binary matrix (mat), which is simply a grid made up of 0s and 1s. Our goal is to find the maximal length of a continuous line of 1s that could be arranged in any of four possible directions: horizontal, vertical, diagonal from top left to bottom right (referred to as 'diagonal'), and diagonal from top right to bottom left (referred to as 'anti-diagonal'). The task is to return the length of this longest line.

Intuition

the matrix that is a 1 and updating counts of consecutive 1s in each direction. The intuition for the solution can be broken down as follows:

To solve this problem, we can execute a comprehensive scan of the matrix. This involves checking each direction for each element in

1. For each cell that contains a 1 in the matrix, we have the potential to extend a line horizontally, vertically, diagonally, or antidiagonally.

- 2. We can maintain four separate 2D arrays (of the same dimensions as the original matrix, with an extra buffer row and column to handle edge cases) to keep track of the maximum line length in each of the four directions at each cell.
- a[] [] for the vertical direction b[] [] for the horizontal direction
 - od[][] for the anti-diagonal direction

o c[][] for the diagonal direction

- 3. By iterating over each cell in the matrix, we update the arrays for directions only if the current cell is a 1. For example, the length of the vertical line at a[i][j] is 1 plus the length at a[i-1][j] if the cell at mat[i-1][j-1] is a 1.

5. At every step, we update a variable ans to store the maximum line length found so far, resulting in having the maximum length by

the time we end our scan.

4. Because we are only interested in consecutive 1s, whenever we hit a 0, the count resets to 0.

- 6. The use of padding (an extra row and column) in arrays a, b, c, and d allows easy indexing without the need to check the matrix boundaries, which simplifies the logic and makes the code cleaner.
- matrix (O(m * n)) and with extra space for the four tracking matrices.

Following this approach allows us to resolve the problem with time complexity that is linear with respect to the number of cells in the

Solution Approach The solution approach for this problem involves dynamic programming to keep track of the longest line of 1s for each of the four

directions (horizontal, vertical, diagonal, and anti-diagonal) at every cell. Here is a breakdown of how the implementation works,

tying back to the Python code provided: 1. Initialization: The solution first initializes four 2D arrays, a, b, c, and d, each with m + 2 rows and n + 2 columns. These arrays are

columns serve as a buffer that simplifies boundary condition handling. 2. Iterative Processing: The algorithm iterates through each cell in the matrix using two nested loops. The outer loop goes down each row, and the inner loop goes across each column. Only cells with a value of 1 are processed to extend the lines.

used to store the maximum length of consecutive ones up to that point in the matrix for each direction. The extra rows and

- 3. Updating Directional Counts: For each cell with a 1, the four arrays are updated as follows: a[i][j] is updated to a[i - 1][j] + 1, incrementing the count of vertical consecutive ones from the top.
- ∘ c[i][j] is updated to c[i 1][j 1] + 1, incrementing the count of diagonal consecutive ones from the top left. od[i][j] is updated tod[i - 1][j + 1] + 1, incrementing the count of anti-diagonal consecutive ones from the top right.

4. Updating the Answer: The maximum value of the four array cells at the current position (a[i][j], b[i][j], c[i][j], d[i][j]) is

compared with the current answer (ans). If any of them is greater, ans is updated. This ensures ans always holds the maximum

b[i][j] is updated to b[i][j - 1] + 1, incrementing the count of horizontal consecutive ones from the left.

- line length found up to that point. 5. Return the Result: After completely scanning the matrix, the maximum length (ans) is returned as the answer. The data structures used, in this case, are additional 2D arrays that help us track the solution state as we go, characteristic of

dynamic programming. The implementation is relatively straightforward and relies on previous states to compute the current state.

This ensures that at any given point in the matrix, we know the longest line of 1s that could be formed in any of the four directions

without having to re-scan any part of the matrix, which is efficient and reduces the overall time complexity of the algorithm.

Example Walkthrough

Let's illustrate the solution approach with a small binary matrix example: 1 mat = [[0, 1, 1, 0], [0, 1, 1, 1], [1, 0, 0, 1]

1. Initialization: We create four extra 2D arrays a, b, c, and d, each with dimensions 4 x 5 to accommodate the buffer rows and

columns.

2 0 0 0 0 0

3 0 0 1 2 0

After the second row:

1 a (vertical)

2. Iterative Processing: We step through each cell in the matrix one by one.

Following the steps outlined in the solution approach:

cell in mat is 1. Assume ans = 0 at the start.

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a (vertical) b (horizontal)

To better understand, let's look at the updates after processing the first two rows: After the first row:

c (diagonal) d (anti-diagonal)

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3. Updating Directional Counts and Answer: We update the counts in our four arrays only at positions where the corresponding

00000 00000 4 0 0 0 0 0 00000 5 ans = 2

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Here, ans is 2, as that is the largest count in any of the arrays.

d (anti-diagonal)

4. Return the Result: After completely iterating over the matrix, we find that the ans is 3, which indicates the length of the longest

00000 00000 2 0 0 0 0 0 00000 3 0 0 1 2 0 0 0 0 1 2 0 0 0 0 1 00120 4 0 0 2 3 0 000123 00012 00031 5 ans = 3

c (diagonal)

After processing the cell mat [1] [3], ans updates to 3, as that is now the highest value found.

b (horizontal)

continuous line of 1s. We would return 3 in this case.

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And so, by iterating over the matrix and updating our directional counts, we can determine that the longest continuous line of 1s in
mat spans 3 cells and is found horizontally in the second row.
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max_length = 0

return max_length

public int longestLine(int[][] mat) {

// Get the number of rows and columns in the matrix

int[][] horizontal = new int[rows + 2][cols + 2];

int rows = mat.length, cols = mat[0].length;

Iterate through the matrix

for i in range(1, rows + 1):

for j in range(1, cols + 1):

value = matrix[i - 1][j - 1]

```
Python Solution
     from typing import List # Import typing to use List type hint
    class Solution:
        def longestLine(self, matrix: List[List[int]]) -> int:
            # Get the dimensions of the matrix
            rows, cols = len(matrix), len(matrix[0])
```

 $horizontal = [[0] * (cols + 2) for _ in range(rows + 2)]$

 $anti_diagonal = [[0] * (cols + 2) for _ in range(rows + 2)]$

Value of the current cell in the input matrix

 $vertical = [[0] * (cols + 2) for _ in range(rows + 2)]$

diagonal = $[[0] * (cols + 2) for _ in range(rows + 2)]$

Variable to store the maximum length of continuous 1s

horizontal, vertical, diagonal, anti-diagonal

Initialize four matrices to keep track of continuous 1s in all four directions:

```
23
                   if value == 1:
24
                       # Update counts for all four directions by adding 1 to the counts from previous
25
                       # relevant cells (up, left, top-left diagonal, top-right diagonal).
26
                       horizontal[i][j] = horizontal[i][j - 1] + 1
                       vertical[i][j] = vertical[i - 1][j] + 1
27
28
                       diagonal[i][j] = diagonal[i - 1][j - 1] + 1
                       anti_diagonal[i][j] = anti_diagonal[i - 1][j + 1] + 1
29
30
31
                       # Update the max_length for the current cell's longest line of continuous 1s.
32
                       max_length = max(max_length, horizontal[i][j], vertical[i][j],
33
                                         diagonal[i][j], anti_diagonal[i][j])
34
35
           # Return the maximum length of continuous 1s found.
```

Java Solution

1 class Solution {

```
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             int[][] vertical = new int[rows + 2][cols + 2];
             int[][] diagonal = new int[rows + 2][cols + 2];
             int[][] antiDiagonal = new int[rows + 2][cols + 2];
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             // Initialize a variable to keep track of the maximum length
 11
             int maxLength = 0;
 12
 13
             // Iterate over each cell in the matrix
 14
             for (int i = 1; i <= rows; ++i) {
 15
                 for (int j = 1; j <= cols; ++j) {
 16
                     // If the current cell has a value of 1
 17
                     if (mat[i - 1][j - 1] == 1) {
 18
                         // Update the counts for each direction (horizontal, vertical, diagonal, antiDiagonal)
 19
                         horizontal[i][j] = horizontal[i][j - 1] + 1;
                                                                          // Left
                         vertical[i][j] = vertical[i - 1][j] + 1;
 20
                                                                          // Up
 21
                         diagonal[i][j] = diagonal[i - 1][j - 1] + 1; 	// Top-left
 22
                         antiDiagonal[i][j] = antiDiagonal[i - 1][j + 1] + 1; // Top-right
 23
 24
                         // Update the maximum length if a higher count is found
 25
                         maxLength = getMax(maxLength, horizontal[i][j], vertical[i][j], diagonal[i][j], antiDiagonal[i][j]);
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             // Return the maximum length of a line of consecutive ones
 30
             return maxLength;
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         // Helper function to calculate the maximum value
 34
         private int getMax(int... values) {
 35
             int max = 0;
 36
             for (int value : values) {
 37
                 max = Math.max(max, value);
 38
 39
             return max;
 40
 41 }
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C++ Solution
  1 #include <vector>
  2 #include <algorithm> // For max()
    using namespace std;
```

17 18 // Iterate through each cell of the matrix to fill DP tables for (int i = 1; i <= rows; ++i) { 19 20 for (int j = 1; $j \ll cols; ++j$) { 21

class Solution {

int longestLine(vector<vector<int>>& matrix) {

int rows = matrix.size(), cols = matrix[0].size();

if (matrix[i - 1][j - 1] == 1) {

// Create 2D vectors with extra padding to handle indices during DP calculations

vector<vector<int>> vertical(rows + 2, vector<int>(cols + 2, 0));

vector<vector<int>> diagonal(rows + 2, vector<int>(cols + 2, 0));

// Only process the cell if it contains a '1'

// Update the dynamic programming tables

vector<vector<int>> horizontal(rows + 2, vector<int>(cols + 2, 0));

vector<vector<int>> antiDiagonal(rows + 2, vector<int>(cols + 2, 0));

int maxLength = 0; // To keep track of the longest line of consecutive ones

// Compute number of consecutive ones in all directions

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                        vertical[i][j] = vertical[i - 1][j] + 1; // Count consecutive ones vertically
 26
                        horizontal[i][j] = horizontal[i][j - 1] + 1; // Count consecutive ones horizontally
 27
                        diagonal[i][j] = diagonal[i - 1][j - 1] + 1; // Count consecutive ones diagonally
 28
                         antiDiagonal[i][j] = antiDiagonal[i - 1][j + 1] + 1; // Count consecutive ones anti-diagonally
 29
 30
                        // Check if the current count is larger than the current maximum length
                         int currentMax = max(vertical[i][j], max(horizontal[i][j],
 31
 32
                                            max(diagonal[i][j], antiDiagonal[i][j])));
 33
                         maxLength = max(maxLength, currentMax);
 34
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 38
            // Return the length of the longest consecutive line of ones found
             return maxLength;
 39
 40
 41 };
 42
Typescript Solution
    function longestLine(matrix: number[][]): number {
         let rows = matrix.length;
         let cols = matrix[0].length;
  4
        // Initialize 2D arrays with extra padding to handle indices during dynamic programming calculations
  5
         let vertical = Array.from({ length: rows + 2 }, () => Array(cols + 2).fill(0));
  6
         let horizontal = Array.from({ length: rows + 2 }, () => Array(cols + 2).fill(0));
         let diagonal = Array.from({ length: rows + 2 }, () => Array(cols + 2).fill(0));
  8
         let antiDiagonal = Array.from({ length: rows + 2 }, () => Array(cols + 2).fill(0));
  9
 10
 11
         let maxLength = 0; // To keep track of the longest line of consecutive ones
 12
        // Iterate through each cell of the matrix to fill the DP arrays
 13
 14
         for (let i = 1; i <= rows; i++) {
 15
             for (let j = 1; j <= cols; j++) {
 16
                 // Only process the cell if it contains a '1'
                 if (matrix[i - 1][j - 1] === 1) {
 17
                     // Update the dynamic programming arrays
 18
 19
                     // Compute the number of consecutive ones in all directions
 20
                     vertical[i][j] = vertical[i - 1][j] + 1; // Count consecutive ones vertically
 21
                     horizontal[i][j] = horizontal[i][j - 1] + 1; // Count consecutive ones horizontally
```

32 33 34 return maxLength; 35

of operations for each cell.

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23 antiDiagonal[i][j] = antiDiagonal[i - 1][j + 1] + 1; // Count consecutive ones anti-diagonally 24 // Check if the current count is larger than the maximum length found so far 25 26 let currentMax = Math.max(vertical[i][j], Math.max(horizontal[i][j], 27 Math.max(diagonal[i][j], antiDiagonal[i][j]))); 28 maxLength = Math.max(maxLength, currentMax); 29 30 31 // Return the length of the longest consecutive line of ones found

diagonal[i][j] = diagonal[i - 1][j - 1] + 1; // Count consecutive ones diagonally

36 Time and Space Complexity The time complexity of the provided code is 0(m * n), where m is the number of rows and n is the number of columns in the input

The space complexity of the code is also 0(m * n) because it creates four auxiliary matrices (a, b, c, d), each of the same size as the input matrix mat. These matrices are used to keep track of the length of consecutive ones in four directions - horizontal, vertical, diagonal, and anti-diagonal.

matrix mat. This complexity arises because the code iterates over each cell of the matrix exactly once, performing a constant number