

Problem Description

Cells with isWater[i][j] == 0 are land, and cells with isWater[i][j] == 1 are water. Water cells must have a height of 0, while land cells must be assigned a non-negative height. The key requirement is that any pair of adjacent cells must differ in height by at most 1. The goal is to maximize the highest height in the matrix while following the aforementioned conditions. The solution should return a new matrix, height, where height[i][j] represents the height of cell(i, j).

Given a matrix iswater representing a map with land and water cells, the task is to assign each cell a height based on certain rules.

Intuition

First Search (BFS), which starts from all the water cells simultaneously since we know their height is 0. We consider each water cell as a source and begin to explore outward to adjacent land cells, increasing the height step by step. As multiple water sources spread out, the "wavefront" of land cells being assigned heights grows. Each step from a water cell is assigning a height of 1 to adjacent land cells, and as we continue BFS, we move from these land cells to their adjacent cells,

The problem is similar to filling a terrain with water and watching the water rise, respecting the rule that water doesn't spill over to

neighboring cells if the height difference is greater than 1. A good way to approach this problem is by using Multi-Source Breadth-

incrementing height by 1 each time. This process naturally ensures that land cells near water are lower, and as we move away, the height increases up to the point where the maximum height that follows the rules is achieved. The key to BFS is to visit each cell only once and assign the correct height the first time it is visited, which avoids the need for recalculation. The BFS process continues until there are no more cells to update, meaning every cell has been assigned a height as

per the rule. **Solution Approach**

The solution utilizes the Multi-Source Breadth-First Search (BFS) algorithm to iterate through the matrix. Let's walk through the key

1. Initialization: We create a new matrix ans with the same dimensions as isWater, initializing all cells with -1. This will eventually

store the final heights of all cells. Then, we declare a queue q to manage the BFS process.

through the matrix.

components and the algorithm's implementation:

2. Discovering Water Sources: We iterate through iswater, and for each cell that contains water, we set the corresponding cell in ans to 0 (since the height of water cells is always 0) and add the cell coordinates to q.

3. BFS Process: We start the BFS by popping elements from the queue q. For each cell (i, j), we consider its adjacent cells in the four cardinal directions (north, south, east, west) - these are the potential "next steps" in the BFS. To check for valid adjacent

cells, we ensure they are within the matrix bounds and that their height has not been set yet (indicated by -1).

height. When the queue is empty, every cell has been reached, and their heights satisfy the rules provided.

matrix. It solely relies on simple iterations and checks, ensuring it meets the problem constraints effectively.

- 4. Updating Heights: If an adjacent cell is a valid next step, we set its height to be one more than the current cell's (i, j) height. This step ensures that the height difference condition is satisfied. Doing this for all water source cells gradually propagates
- 5. Queueing Next Cells: After updating the height of an adjacent cell, we add the cell coordinates to the queue q. Placing the cell in the queue ensures that its adjacent cells will be visited in subsequent iterations of BFS.

6. Repeating Process: The BFS continues until current passes through the entire matrix, visiting each cell and assigning the correct

contains the heights of all cells. By converging from multiple sources and using a queue for BFS, the solution efficiently spreads out to maximize the heights in the

7. Returning Results: When there are no more cells to update, the BFS is completed, and we return the ans matrix, which now

Here is the code snippet that embodies the approach: class Solution: def highestPeak(self, isWater: List[List[int]]) -> List[List[int]]:

for j, v in enumerate(row): q.append((i, j)) 9 10 ans[i][j] = 0

this cell to our BFS queue q.

'ans' matrix after discovering water sources:

heights to 1. Then we enqueue these cells.

3 [-1, -1]

[-1, 0]

[-1, -1]

6 [(0, 1)]

5 Queue 'q' contains:

6 [(0, 0), (1, 1)]

(1, 0).

[1, 0]

[2, -1]

5 Queue 'q' contains:

5 Queue 'q' is empty.

The final ans matrix is:

6 [(1, 1), (1, 0)]

q = deque()

while q:

return ans

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Example Walkthrough
Let's consider a small example of the isWater matrix to see how the solution works step by step:
1 Given 'isWater' matrix:
2 [0, 1]
3 [0, 0]
We have a 2×2 matrix where the top right cell represents water (1) and the rest are land (0).
 1. Initialization: We initialize the ans matrix with all -1 to represent unset heights.
1 'ans' matrix after initialization:
2[-1, -1]
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for a, b in pairwise((-1, 0, 1, 0, -1)):

ans[x][y] = ans[i][j] + 1

if $0 \le x \le m$ and $0 \le y \le n$ and ans[x][y] == -1:

m, n = len(isWater), len(isWater[0])

ans = $[[-1] * n for _ in range(m)]$

for i, row in enumerate(isWater):

x, y = i + a, j + b

q.append((x, y))

i, j = q.popleft()

3. **BFS Process**: Dequeue (0, 1) from q and look for adjacent land cells.

'ans' matrix after the first BFS iteration: [-1, -1]5 Queue 'q' contains:

5. Queueing Next Cells: We remove (0, 0) from the queue. The adjacent land cells [1] [0] can be updated to 2. Now we enqueue

4. Updating Heights: We find two adjacent cells to (0, 1) that are [0] [0] and [1] [1]. They are both valid moves, so we set their

2. Discovering Water Sources: We find that isWater[0][1] is a water source, so we set the corresponding cell in ans to 0 and add

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Then we dequeue (1, 0) and check its adjacents but there are no -1 values in ans meaning all land cells have been reached and
heights assigned.
1 'ans' matrix after BFS is completed:
   [2, 1]
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satisfying the rule that adjacent cells differ by at most 1.

adhering to the provided constraints and maximizing the heights of land cells.

def highestPeak(self, is_water: List[List[int]]) -> List[List[int]]:

queue.append((row_index, col_index))

answer_grid[row_index][col_index] = 0

Directons for exploring neighboring cells (up, right, down, left)

Populate the queue with water cells and set their height to 0 in answer_grid

Retrive the number of rows (m) and columns (n)

for row_index, row in enumerate(is_water):

if value:

while queue:

for col_index, value in enumerate(row):

directions = [(-1, 0), (0, 1), (1, 0), (0, -1)]

current_row, current_col = queue.popleft()

queue.offer(new int[] {i, j});

int[] directions = $\{-1, 0, 1, 0, -1\}$;

// Poll a cell from the queue.

int[] position = queue.poll();

// Explore all adjacent cells.

int x = row + directions[k];

int y = col + directions[k + 1];

for (int k = 0; k < 4; ++k) {

while (!queue.isEmpty()) {

int row = position[0];

int col = position[1];

// Perform BFS to find the highest peak values.

// Directions for exploring adjacent cells (up, right, down, left).

// Calculate coordinates of the adjacent cell.

// Check if the adjacent cell is within bounds and if it is land.

highestPeaks[x][y] = highestPeaks[row][col] + 1;

// Enqueue the position of the land cell.

queue.offer(new int[] {x, y});

if $(x >= 0 \&\& x < rows \&\& y >= 0 \&\& y < cols \&\& highestPeaks[x][y] == -1) {$

// Set the height of the land cell to be one more than the current cell.

Perform BFS to populate the answer grid

Explore all neighboring cells

Dequeue the first cell

1 'ans' matrix after updating (0, 0):

1 [1, 0] 2 [2, 1]

This walkthrough demonstrates how the process of Multi-Source Breadth-First Search works to assign heights to cells while

7. Returning Results: Since the BFS queue is empty, we completed the BFS of all cells, and the ans matrix is returned with heights

6. Repeating Process: We dequeue (1, 1). Since it is already at the boundary, there are no new cells to consider.

num_rows, num_cols = len(is_water), len(is_water[0]) # Initialize answer grid with -1s indicating unvisited cells 8 answer_grid = $[[-1] * num_cols for _ in range(num_rows)]$ 9 # Queue to hold the cells to visit in Breadth-First Search (BFS) 10 queue = deque()

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Python Solution

class Solution:

1 from collections import deque

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                 for delta_row, delta_col in directions:
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                     # Calculate neighbor coordinates
                     neighbor_row, neighbor_col = current_row + delta_row, current_col + delta_col
 31
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                     # Check if neighbor is within the grid and is unvisited
 33
                     if (0 <= neighbor_row < num_rows and</pre>
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                             0 <= neighbor_col < num_cols and</pre>
 35
                             answer_grid[neighbor_row][neighbor_col] == -1):
 36
                         # Update the height of the neighbor cell
 37
                         answer_grid[neighbor_row][neighbor_col] = answer_grid[current_row][current_col] + 1
 38
                         # Enqueue the neighbor cell for visiting
 39
                         queue.append((neighbor_row, neighbor_col))
 40
 41
             # Return the populated answer grid
 42
             return answer_grid
 43
Java Solution
  1 class Solution {
         public int[][] highestPeak(int[][] isWater) {
             // Obtain dimensions of the input matrix.
             int rows = isWater.length;
  5
             int cols = isWater[0].length;
  6
             // Initialize the answer matrix with the same dimensions.
             int[][] highestPeaks = new int[rows][cols];
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  9
 10
             // Queue for BFS (Breadth-first search).
 11
             Deque<int[]> queue = new ArrayDeque<>();
 12
 13
             // Initialize answer matrix and enqueue all water cells.
             for (int i = 0; i < rows; ++i) {
 14
 15
                 for (int j = 0; j < cols; ++j) {
 16
                     // Mark water cells with 0 and land cells with -1
                     highestPeaks[i][j] = isWater[i][j] - 1;
 17
 18
 19
                     // Add water cell coordinates to the queue.
 20
                     if (highestPeaks[i][j] == 0) {
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// Return the filled highestPeaks matrix.
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             return highestPeaks;
 55
 56 }
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C++ Solution
  1 #include <vector>
  2 #include <queue>
    using namespace std;
    class Solution {
    public:
         // Define directions for exploring adjacent cells: up, right, down, left.
         const vector<int> dirs{-1, 0, 1, 0, -1};
  9
 10
         // Function to calculate the highest peak elevation for each cell.
         vector<vector<int>> highestPeak(vector<vector<int>>& isWater) {
 11
             int m = isWater.size();
                                         // Number of rows.
 12
 13
             int n = isWater[0].size(); // Number of columns.
 14
             vector<vector<int>> ans(m, vector<int>(n));
 15
             queue<pair<int, int>> q; // Queue to perform a breadth-first search.
 16
 17
             // Initialize the answer matrix and enqueue all water cells.
             for (int i = 0; i < m; ++i) {
 18
 19
                 for (int j = 0; j < n; ++j) {
 20
                     ans[i][j] = isWater[i][j] - 1; // Water cells become 0, land cells -1.
                     if (ans[i][j] == 0) {
 21
 22
                         // If the cell is water, add it to the queue for BFS.
 23
                         q.emplace(i, j);
 24
 25
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 28
             // Perform breadth-first search to determine elevation of each cell.
 29
             while (!q.empty()) {
 30
                 auto [i, j] = q.front(); // Get the front cell from the queue.
 31
                 q.pop();
 32
                 for (int k = 0; k < 4; ++k) { // Explore all 4 adjacent cells.
 33
                     int x = i + dirs[k]; // Calculate the new x-coordinate.
 34
                     int y = j + dirs[k + 1]; // Calculate the new y-coordinate.
                     // Check if the new coordinates are in bounds and the cell is not yet visited.
 35
 36
                     if (x \ge 0 \& x < m \& y \ge 0 \& y < n \& ans[x][y] == -1) {
 37
                         // Set the elevation of the cell to be one more than current cell's elevation.
 38
                         ans[x][y] = ans[i][j] + 1;
 39
                         // Add this cell to the queue to continue BFS from here.
 40
                         q.emplace(x, y);
 41
 42
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             return ans; // Return the elevation matrix.
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Typescript Solution

function highestPeak(isWater: number[][]): number[][] {

const rows = isWater.length; // Number of rows

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const cols = isWater[0].length; // Number of columns
        let answer: number[][] = []; // Matrix to store the final height map
        let queue: number[][] = [];  // Queue to perform Breadth-First Search (BFS)
        // Initialize the answer matrix with -1 and queue with the water cells (0 elevation)
        for (let i = 0; i < rows; i++) {
            answer.push(new Array(cols).fill(-1));
            for (let j = 0; j < cols; j++) {</pre>
10
                if (isWater[i][j] === 1) {
                    queue.push([i, j]);
                     answer[i][j] = 0;
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        // Directions for exploring the neighbors of a cell (up, right, down, left)
19
        const directions = [-1, 0, 1, 0, -1];
20
21
        // Perform BFS to populate the answer matrix with height/elevation levels
22
        while (queue.length) {
            let tempQueue: number[][] = [];
23
24
            for (const [currentRow, currentCol] of queue) {
25
                for (let k = 0; k < 4; k++) { // Explore the 4 neighbors of the current cell
26
                     const newRow = currentRow + directions[k];
                    const newCol = currentCol + directions[k + 1];
27
28
                    // If the new cell is within bounds and not yet visited (elevation -1)
                    if (\text{newRow} >= 0 \& \& \text{newRow} < \text{rows} \& \& \text{newCol} >= 0 \& \& \text{newCol} < \text{cols} \& \& \text{answer[newRow]}[\text{newCol}] === -1) {
29
30
                         tempQueue.push([newRow, newCol]);
                         answer[newRow][newCol] = answer[currentRow][currentCol] + 1;
31
32
33
34
35
            queue = tempQueue; // Update the queue with the next level of cells to be visited
36
37
38
        return answer; // Return the populated height map
39 }
40
```

Time and Space Complexity

The time complexity of the code is 0(m * n), where m is the number of rows and n is the number of columns in the matrix isWater. This is because the algorithm must visit every cell at least once to determine its height in the final output matrix, and in the worst case, each cell is enqueued and dequeued exactly once in the BFS process.

The space complexity of the code is also 0(m * n) because it requires a queue to store at least one entire level of the grid's cells, and each cell is stored once. Also, the ans matrix of size m * n is maintained to store the heights of each cell in the final output.