406. Queue Reconstruction by Height Medium <u>Greedy</u> Binary Indexed Tree Segment Tree Array

## **Problem Description**

represents the height of the person and k represents the number of people who are in front of this person in a queue and are taller or of the same height. The array people does not necessarily represent the order of people in a queue. Our task is to reconstruct the queue in such a way that the attributes of people in the reconstructed queue align with the original array people. The reconstructed queue should also be represented as an array where each element follows the same pair representation [h, k], with each pair denoting the attributes of the people in the queue.

In this problem, we are given an array of people's attributes, where each person is represented by a pair of values [h, k]. The h

To be more concrete, if  $people[i] = [h_i, k_i]$ , we need to place the ith person in such a position in the queue that  $k_i$  is the exact count of people ahead of this person with heights greater than or equal to h\_i.

## The intuition behind the solution lies in the fact that it's easier to place the tallest people first and then insert the shorter people at their appropriate positions based on the k value. Here's how we can think of the approach:

Intuition

front first.

Sort people by their height in descending order; if two people have the same height, sort them by their k value in ascending order. This way, we start with the tallest people, and for those with the same height, we place those with fewer people in

Initialize an empty list ans that will represent our queue. Iterate over the sorted list, inserting each person into the ans list at the index equal to their k value. It works because by

inserting the tallest people first, their k value corresponds exactly to the position they should be in the queue. As we insert

By following this approach, we ensure that each person is placed in accordance with the number of taller or equally tall people

the shorter people, we displace the taller ones only if needed, which maintains the integrity of the k values.

that are supposed to be in front of them according to the original array people.

Solution Approach The solution uses a greedy algorithm approach along with list operations to reconstruct the queue. Here is a step-by-step

walkthrough of the implementation based on the solution code provided:

Sort the people array in a way such that we first sort the people by height in descending order and then, if the heights are

equal, sort by the k value in ascending order. The lambda function in the sort method accomplishes this by using -x[0] for

## descending height and x[1] for ascending k values. Sorting is done with this line:

people.sort(key=lambda x: (-x[0], x[1]))

By sorting in this manner, we prioritize taller individuals and, among those of identical height, prioritize those with a smaller k value, which is the count of people in front of them. Initialize an empty list ans which will be used to construct the queue. ans = []

Iterate over the sorted people array. For each person p, we insert them into the ans list at the index specified by their k value.

This is possible because at the time of their insertion, there will be p[1] (which is k) taller or equal height people already in

the list, since those have been inserted earlier due to the sorting strategy. for p in people:

Return the ans list which now represents the reconstructed queue.

```
return ans
```

**Example Walkthrough** 

ans.insert(p[1], p)

algorithm, ensuring that the resulting ans list satisfies the requirements that are stated in the problem.

Using this greedy strategy, we are able to re-order the array so that each person is positioned in accordance with their height

and the count of people in front of them with equal or greater height. The use of sorting and list insertions are key aspects of the

1. We first sort the array people by height in descending order and k value in ascending order when the heights are equal. After sorting, our people

The insert operation places the person at the correct position in the queue, shifting elements that are already there.

Following the steps outlined in the solution approach:

people = [[7, 0], [4, 4], [7, 1], [5, 0], [6, 1], [5, 2]]

people = [[7, 0], [7, 1], [6, 1], [5, 0], [5, 2], [4, 4]]

Suppose we are given the following array people:

Let's consider a small example to illustrate the solution approach.

```
2. We initialize an empty list ans:
```

ans = []

array looks like this:

We then iterate over the sorted people array and insert each person into the ans list at the index specified by their k value: • We insert [7, 0] at index 0: ans = [[7, 0]]

The final ans list is our reconstructed queue which aligns with the original people array attributes:

```
○ We insert [5, 2] at index 2: ans = [[5, 0], [7, 0], [5, 2], [6, 1], [7, 1]]

    Finally, we insert [4, 4] at index 4: ans = [[5, 0], [7, 0], [5, 2], [6, 1], [4, 4], [7, 1]]
```

ans = [[5, 0], [7, 0], [5, 2], [6, 1], [4, 4], [7, 1]]

We insert [6, 1] at index 1: ans = [[7, 0], [6, 1], [7, 1]]

• We insert [5, 0] at index 0: ans = [[5, 0], [7, 0], [6, 1], [7, 1]]

We insert [7, 1] at index 1: ans = [[7, 0], [7, 1]]

```
Using the greedy solution approach of sorting the individuals by height and then inserting them into the queue based on their k
```

**Python** 

Java

the k value is the exact count of people ahead of them with heights greater than or equal to their own. **Solution Implementation** 

value, we have successfully reconstructed a queue that satisfies the requirements of the problem. In this queue, for every person,

```
from typing import List
class Solution:
   def reconstructQueue(self, people: List[List[int]]) -> List[List[int]]:
```

queue.insert(person[1], person)

public int[][] reconstructQueue(int[][] people) {

Arrays.sort(people, (person1, person2) ->

// Insert each person into the arrangedQueue.

// Return the final arrangement of the queue.

arrangedQueue.splice(person[1], 0, person);

// Return the final arrangement of the queue.

// let queue = reconstructQueue(peopleInput);

queue.insert(person[1], person)

# Return the reconstructed queue

Time and Space Complexity

Sorting the people array:

return arrangedQueue;

for (let person of people) {

return arrangedQueue;

// Example of usage:

from typing import List

return queue

**Time Complexity** 

**}**;

**TypeScript** 

for (const std::vector<int>& person : people) {

// The index to insert the person is determined by the person's "k-value",

arrangedQueue.insert(arrangedQueue.begin() + person[1], person);

// The index at which to insert is determined by the person's k-value,

// let peopleInput: number[][] = [[7, 0], [4, 4], [7, 1], [5, 0], [6, 1], [5, 2]];

// console.log(queue); // Outputs arranged queue based on the given conditions.

// Sort the array. First, sort by height in descending order.

// Initialize a list to hold the final queue reconstruction,

List<int[]> reconstructedQueue = new ArrayList<>(people.length);

// which allows us to insert people at specific indices.

# Return the reconstructed queue

# Sort the 'people' array in descending order of height (h),

people.sort(key=lambda person: (-person[0], person[1]))

# and in the case of a tie, in ascending order of the number of people in front (k).

# which represents the number of people in front of them with equal or greater height.

// If heights are equal, sort by the number of people in front (k-value) in ascending order.

person1[0] == person2[0] ? person1[1] - person2[1] : person2[0] - person1[0]);

# Initialize an empty list to hold the final queue reconstruction queue = [] # Iterate over the sorted 'people' list for person in people: # Insert each person into the queue. The index for insertion is the k-value,

```
import java.util.ArrayList;
import java.util.List;
class Solution {
```

import java.util.Arrays;

return queue

```
// Iterate over the sorted array, and insert each person into the list
       // at the index specified by their k-value.
        for (int[] person : people) {
            // The second value of each person array (person[1])
            // specifies the index at which this person should be added in the queue
            reconstructedQueue.add(person[1], person);
       // Convert the list back to an array before returning it.
        return reconstructedQueue.toArray(new int[reconstructedQueue.size()][]);
C++
#include <vector>
#include <algorithm>
class Solution {
public:
    std::vector<std::vector<int>> reconstructQueue(std::vector<std::vector<int>>& people) {
       // Sort the people to arrange them according to their height in descending order.
       // If two people are of the same height, order them by their "k-value" in ascending order.
       std::sort(people.begin(), people.end(), [](const std::vector<int>& personA, const std::vector<int>& personB) {
            return personA[0] > personB[0] || (personA[0] == personB[0] && personA[1] < personB[1]);</pre>
       });
       // Initialize an empty vector for the final arrangement.
        std::vector<std::vector<int>> arrangedQueue;
```

// which indicates the number of people in front of this person who have a height greater than or equal to this person's

```
function reconstructQueue(people: number[][]): number[][] {
   // Sort the `people` array to arrange them by their height in descending order.
   // If two people have the same height, order them by their k-value in ascending order.
    people.sort((a, b) => {
       return b[0] - a[0] || a[1] - b[1];
   });
   // Initialize an empty array for the final arrangement.
   let arrangedQueue: number[][] = [];
   // Insert each person into the `arrangedQueue`.
```

// which indicates the number of people in front of them with a height greater than or equal.

```
class Solution:
   def reconstructQueue(self, people: List[List[int]]) -> List[List[int]]:
       # Sort the 'people' array in descending order of height (h),
       # and in the case of a tie, in ascending order of the number of people in front (k).
        people.sort(key=lambda person: (-person[0], person[1]))
       # Initialize an empty list to hold the final queue reconstruction
       queue = []
       # Iterate over the sorted 'people' list
        for person in people:
           # Insert each person into the queue. The index for insertion is the k-value,
            # which represents the number of people in front of them with equal or greater height.
```

This operation uses a sorting algorithm, typically Timsort in Python, which has a time complexity of O(n log n) for an array of n elements.

Reconstructing the queue by inserting elements:

The time complexity of the code can be broken down into two major operations:

of the list. Since insert is called for each person in the sorted array and the list can grow up to n elements, this operation will have a worst-case complexity of  $0(n^2)$  as it performs n insertions into a structure that can be up to n in size.

By combining these, the overall time complexity of the code is  $0(n \log n) + 0(n^2)$ , which simplifies to  $0(n^2)$  since  $0(n^2)$  is the dominating term when n is large.

The insert operation within a list has a time complexity of O(n) in the worst case because it may require shifting the elements

**Space Complexity** The space complexity of the code is the amount of extra space used by the algorithm, not counting the space occupied by the

## input itself. In this case:

Sorted people array: Since the sorting operation is done in-place, it does not contribute to additional space complexity beyond what is taken by the input people array.

This list is created to store the output and grows to contain n elements, which are the same elements from the input people array. Thus, the space required is O(n).

The ans list:

Therefore, the overall space complexity of the code is O(n).