498. Diagonal Traverse Matrix **Simulation** Medium

Problem Description

Array

arranged in a specific order. This order follows the diagonal patterns of the matrix. We start from the top-left corner, move diagonally up and to the right, and upon reaching the top or right boundary, we move to the next diagonal, which starts from the leftmost or bottommost element of the current boundary. The process continues until all elements are traversed. It is important to note that when moving along the diagonals, the order of traversal alternates. Diagonals that have a bottom-left to top-right orientation are traversed from top to bottom, while diagonals with a top-right to bottom-left orientation are traversed from bottom to top. Intuition

The problem provides us with an $m \times n$ matrix, named mat, and asks us to return an array of all the elements in the matrix

The solution uses a single-pass algorithm that iterates over the potential starting points for each diagonal in the matrix. A crucial observation is that if you list the starting points, they follow the border of the matrix, first going downward along the left side and

simply sum m and n. **Solution Approach** The solution approach involves iterating through all the possible diagonals in the matrix. These diagonals are indexed by a variable called k which runs from 0 to m + n - 2 inclusive.

then going rightward along the bottom side. The total number of such diagonals would correspond to m + n - 1, considering

every element of the first and last row and column except the bottom-right corner element, which is accounted for twice if we

Here are the steps taken by the algorithm:

Example Walkthrough

Given matrix mat:

9 10 11 12

A loop begins with k starting from 0 and running up to m + n - 1. Each iteration of this loop corresponds to a diagonal in the matrix.

For each k, we determine the starting position (i, j) of the current diagonal. If k is less than n (number of columns), then

i starts at 0 and j starts at k. Otherwise, when k is at least n, i starts at k - n + 1 and j starts at n - 1.

- A temporary list t is created to store the elements of the current diagonal. We use while loop to navigate through the diagonal and collect elements from mat[i][j] as long as i < m and j >= 0, incrementing i and decrementing j.
- The direction of iteration along the diagonal is important. After collecting elements in the temporary list, if k is even, the order of the elements is reversed (using t[::-1]), to adhere to the proper diagonal traversal sequence as specified by the problem.

The elements in t (in the correct order) are then added to ans, which is the list that will ultimately be returned.

- After all iterations, ans contains all matrix elements in the desired diagonal order, and the list is returned. This approach uses straightforward indexing to access the matrix elements and employs a list to collect the output. The
- conditional reversal of the temporary list accounts for the zigzag pattern of the traversal, alternating between diagonals. Such an approach is space-efficient since it does not require additional space proportional to the size of the matrix, besides the output
- Let's walk through an example to illustrate the solution approach with a 3×4 matrix.

from top to bottom. Our answer list ans begins with [1]. Move to k = 1, representing the second diagonal [2, 5]. k is odd, so we reverse the order when appending to ans. The answer list becomes [1, 5, 2].

For k = 2, the diagonal is [3, 6, 9]. k is even, so append in original order: ans = [1, 5, 2, 3, 6, 9].

k = 3 gives diagonal [4, 7, 10]. k is odd, so reverse it: ans = [1, 5, 2, 3, 6, 9, 10, 7, 4].

Start with k = 0, which corresponds to the first diagonal, which is just the element 1. Since k is even, we collect elements

For k = 4, the diagonal is [8, 11]. k is even: ans = [1, 5, 2, 3, 6, 9, 10, 7, 4, 8, 11]. Finally, k = 5 corresponds to the last diagonal which is simply [12]. Since k is odd, it remains as is: ans = [1, 5, 2, 3, 6,

matrix traversal into a 1-dimensional list that preserves the diagonal ordering constraint.

Calculate the starting row index. It is 0 for the first 'num cols' diagonals,

Calculate the starting column index. It is 'k' for the first 'num_cols' diagonals,

Continue while 'row' is within the matrix row range and 'col' is non-negative.

Reverse every other diagonal's elements before appending it to the result list

Extend the main result list with the elements of the current diagonal.

std::vector<int> findDiagonalOrder(std::vector<std::vector<int>>& matrix) {

// Initialize row index (i) and column index (i) for the start of the diagonal

// If the diagonal index is even, we need to reverse the diagonal elements

std::reverse(diagonalElements.begin(), diagonalElements.end());

// Append the current diagonal's elements to the result vector

// Clear the diagonal elements vector for the next diagonal

// Return the final vector with all elements in diagonal order

This is the list which will hold the elements in diagonal order.

Temp list to store the elements of the current diagonal.

row = 0 if k < num_cols else k - num_cols + 1

col = k if k < num_cols else num_cols - 1</pre>

while row < num rows and col >= 0:

to get the right order.

temp = temp[::-1]

diagonal_order.extend(temp)

temp.append(matrix[row][col])

otherwise we start at 'num cols - 1' and go down.

Fetch the elements along the current diagonal.

row += 1 # Move down to the next row.

col -= 1 # Move left to the next column.

There will be (num rows + num cols -1) diagonals to cover in the matrix.

otherwise we start at an index which goes down from 'num_rows - 1'.

Calculate the starting row index. It is 0 for the first 'num cols' diagonals,

Calculate the starting column index. It is 'k' for the first 'num_cols' diagonals,

Continue while 'row' is within the matrix row range and 'col' is non-negative.

Reverse every other diagonal's elements before appending it to the result list

Extend the main result list with the elements of the current diagonal.

the elements of each diagonal and appending them to the final result in a specified order.

int rows = matrix.size(), columns = matrix[0].size();

// Iterate over all possible diagonals in the matrix

int j = diag < columns ? diag : columns - 1;</pre>

// to maintain the "zigzag" diagonal order

for (int value : diagonalElements) {

result.push_back(value);

diagonalElements.clear();

return result;

for (int diag = 0; diag < rows + columns - 1; ++diag) {</pre>

int i = diag < columns ? 0 : diag - columns + 1;</pre>

// Collect all elements in the current diagonal

diagonalElements.push_back(matrix[i++][j--]);

std::vector<int> result;

std::vector<int> diagonalElements;

while (i < rows && i >= 0) {

if (diag % 2 == 0) {

otherwise we start at an index which goes down from 'num_rows - 1'.

def findDiagonalOrder(self, matrix: List[List[int]]) -> List[int]:

Determine the number of rows and columns in the matrix.

row = 0 if k < num_cols else k - num_cols + 1

Fetch the elements along the current diagonal.

row += 1 # Move down to the next row.

col -= 1 # Move left to the next column.

while row < num rows and col >= 0:

to get the right order.

temp = temp[::-1]

diagonal_order.extend(temp)

if k % 2 == 0:

temp.append(matrix[row][col])

num_rows, num_cols = len(matrix), len(matrix[0])

We need to collect the elements in the matrix following a specific diagonal pattern:

list. It also traverses each element exactly once, making it time-efficient.

9, 10, 7, 4, 8, 11, 12].

Through these steps, the solution iterates over each possible starting point for the diagonals, collects the elements in either

forward or reverse order depending on the index of the diagonal, and constructs the output list efficiently. The k loop guarantees that we cover all possible diagonals in the matrix. The given solution is a simple yet effective means to convert 2-dimensional

The final output is [1, 5, 2, 3, 6, 9, 10, 7, 4, 8, 11, 12], the matrix elements arranged in the desired diagonal order.

Python from typing import List

This is the list which will hold the elements in diagonal order. diagonal_order = [] # There will be (num rows + num cols -1) diagonals to cover in the matrix. for k in range(num_rows + num_cols - 1): # Temp list to store the elements of the current diagonal. temp = []

otherwise we start at 'num cols - 1' and go down. col = k if k < num_cols else num_cols - 1

Solution Implementation

class Solution:

```
# Return the final result list.
        return diagonal_order
Java
class Solution {
    public int[] findDiagonalOrder(int[][] matrix) {
        // matrix dimensions
        int m = matrix.length;
        int n = matrix[0].length;
        // result arrav
        int[] result = new int[m * n];
        // index for the result array
        int index = 0;
        // temporary list to store diagonal elements
        List<Integer> diagonal = new ArrayList<>();
        // loop through each diagonal starting from the top—left corner moving towards the right—bottom corner
        for (int diag = 0; diag < m + n - 1; ++diag) \{
            // determine the starting row index for the current diagonal
            int row = diag < n ? 0 : diag - n + 1;
            // determine the starting column index for the current diagonal
            int col = diag < n ? diag : n - 1;</pre>
            // collect all the elements from the current diagonal
            while (row < m && col >= 0) {
                diagonal.add(matrix[row][col]);
                ++row;
                --col;
            // reverse the diagonal elements if we are in an even diagonal (starting counting from 0)
            if (diag % 2 == 0) {
                Collections.reverse(diagonal);
            // add the diagonal elements to the result array
            for (int element : diagonal) {
                result[index++] = element;
            // clear the temporary diagonal list for the next iteration
            diagonal.clear();
        return result;
#include <vector>
#include <algorithm>
class Solution {
```

```
};
```

TypeScript

public:

```
function findDiagonalOrder(matrix: number[][]): number[] {
    // Initialize the result array where diagonal elements will be stored.
    const result: number[] = [];
    // Determine the number of rows (m) and columns (n) in the matrix.
    const numRows = matrix.length;
    const numCols = matrix[0].length;
    // Define the starting indices for matrix traversal.
    let row = 0:
    let col = 0:
    // A boolean flag to determine the direction of traversal.
    let isUpward = true;
    // Continue traversing until the result array is filled with all elements.
    while (result.length < numRows * numCols) {</pre>
        if (isUpward) {
            // Move diagonally up-right until the boundary is reached.
            while (row >= 0 && col < numCols) {</pre>
                result.push(matrix[row][col]);
                row--;
                col++;
            // If we've exceeded the top row, reset to start from the next column.
            if (row < 0 && col < numCols) {</pre>
                row = 0;
           // If we've exceeded the right-most column, move down to the next row.
            if (col === numCols) {
                row += 2;
                col--;
        } else {
            // Move diagonally down-left until the boundary is reached.
            while (row < numRows && col >= 0) {
                result.push(matrix[row][col]);
                row++;
                col--;
           // If we've exceeded the bottom row, reset to start from the next column.
            if (row === numRows) {
                row--:
                col += 2;
            // If we've exceeded the left-most column, move up to the next row.
            if (col < 0) {
                col = 0;
        // Flip the direction for the next iteration.
        isUpward = !isUpward;
    // Return the array containing elements in diagonal order.
    return result;
from typing import List
class Solution:
    def findDiagonalOrder(self. matrix: List[List[int]]) -> List[int]:
       # Determine the number of rows and columns in the matrix.
       num_rows, num_cols = len(matrix), len(matrix[0])
```

Return the final result list. return diagonal_order

Time and Space Complexity

if k % 2 == 0:

diagonal order = []

temp = []

for k in range(num_rows + num_cols - 1):

Time Complexity: O(m * n)

The time complexity of the code is determined by the number of iterations needed to traverse all the elements of the matrix.

Since the matrix has m rows and n columns, there are m * n elements in total. The outer loop runs for m + n - 1 iterations,

The given code snippet traverses through all the elements of a two-dimensional matrix mat of size m x n diagonally, collecting

where each diagonal is processed. In each iteration of this loop, a while-loop runs, collecting elements along the current diagonal.

output space.

Each element in the matrix is processed exactly once inside the nested while-loops. Thus, the total number of operations is proportional to the number of elements in the matrix, leading to a time complexity of 0(m * n). Space Complexity: O(min(m, n)) The space complexity of the code is primarily due to the auxiliary data structure t used for storing each diagonal before appending it to the result list ans. The length of a diagonal is at most min(m, n), because the diagonals are limited either by the

number of rows or the number of columns. The reversing operation, t[::-1], creates a new list of the same size as t, and thus,

the temporary space required is also in the order of min(m, n). Since the additional space needed is not dependent on the total number of elements but rather on the longer dimension of the input matrix, the space complexity is 0(min(m, n)). The result list ans grows to hold all m * n elements, but this does not contribute to space complexity in the analysis, as it is required to hold the output of the function. Hence, we only consider the additional space used by the algorithm beyond the