2130. Maximum Twin Sum of a Linked List Medium Stack Two Pointers

Leetcode Link

Problem Description In this LeetCode problem, we are working with a linked list of even length n. The list has a special property: each node has a "twin,"

Linked List

which is the node at the symmetric position from the other end of the list. For instance, in a list with n nodes, the 0-th node is the twin of the (n-1)-th node, and so on. The concept of twins only applies to the first half of the nodes in the list. The "twin sum" is the sum of the value of a node and its twin's value. Our goal is to calculate and return the maximum twin sum that

can be found in the given linked list. To clarify with an example, if we have a linked list 1 -> 2 -> 3 -> 4, the twins are (1, 4) and (2, 3), leading to twin sums of 5 and

5. In this case, the maximum twin sum is 5.

The challenge in this problem is to efficiently find the twin of each node so that we can calculate the twin sums. Since the list is

singly linked, we cannot directly access the corresponding twin for a node in the first half of the list without traversing it.

An intuitive approach involves reversing the second half of the linked list so that we can then pair nodes from the first half and the

Intuition

sum and determine the maximum twin sum. Here is the step-by-step thought process behind the solution:

reversed second half to calculate their sums. By iterating through the two halves simultaneously, we can easily calculate each twin

1. Find the middle of the linked list. Since we have a fast and a slow pointer, where the fast pointer moves at twice the speed of the slow pointer, when the fast pointer reaches the end of the list, the slow pointer will be at the middle. 2. Once the middle is found, reverse the second half of the list starting from the node right after the middle node.

3. Two pointers can now walk through both halves of the list at the same time. Since the second half is reversed, the

corresponding twins will be the nodes that these two pointers point to.

- 4. As we iterate, we calculate the sums of the twins and keep track of the maximum sum that we find.
- **Solution Approach**

5. Once we've traversed through both halves, the calculated maximum sum is returned as the result.

- The given solution in Python implements the approach we've discussed. The main components of the solution involve finding the midpoint of the linked list, reversing the second half of the list, and then iterating to find the maximum twin sum. Here is how each
- step is accomplished:

pa = head

6 ans = 0

2 q = slow.next

pb = reverse(q)

7 while pa and pb:

Example Walkthrough

midpoint of the list.

pa = pa.next

list, slow will be at the midpoint.

1 slow, fast = head, head.next

slow, fast = slow.next, fast.next.next

2 while fast and fast next:

curr = head

while curr:

next = curr.next

curr.next = dummy.next

2. Reversing the Second Half: Once the midpoint is found, the solution defines a helper function reverse (head) to reverse the second half of the linked list starting from the node right after the middle (slow.next). def reverse(head): dummy = ListNode()

1. Finding the Middle of the Linked List: Use the classic two-pointer technique known as the "tortoise and hare" algorithm. One

pointer (slow) moves one node at a time, while the other (fast) moves two nodes at a time. When fast reaches the end of the

dummy.next = curr curr = next return dummy.next The reverse function makes use of a dummy node to easily reverse the linked list through pointer manipulation. 3. Calculating Maximum Twin Sum: After reversing the second half, we now have two pointers, pa that points at the head of the list and pb that points at the head of the reversed second half. We then iterate through the list using both pointers, which move

in step with each other, calculating the sum of the values each points to and updating the ans variable if we find a larger sum.

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pb = pb.next
    10
 4. Returning the Result: After the iteration, and holds the maximum twin sum, which is then returned.
    1 return ans
Overall, the solution iterates over the list twice: once to find the middle and once more to calculate the twin sum. This keeps the time
complexity to O(n) where n is the number of nodes in the linked list. The space complexity is O(1) as it only uses a few extra pointers
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second half (3). Iterating through both halves simultaneously:

Move pa to the next node (4) and pb to its next node (2).

On the first calculation, pa.val is 1, and pb.val is 3. The sum is 4.

We track the maximum sum found, which is 6 after this iteration.

On the second calculation, pa.val is 4, and pb.val is 2. The sum is 6.

3 slow.next = None # Break the list into two halves

ans = max(ans, pa.val + pb.val)

with no dependency on the size of the input list.

 slow starts at 1 and fast starts at 4. After the first step, slow is at 4, and fast is at 2.

2. Reverse the second half: We reverse the list starting from the node right after the middle (slow.next), so we reverse the list

3. Calculating Maximum Twin Sum: We initialize two pointers, pa at the head of the list (1) and pb at the head of the reversed

from 3 onwards. The list is small, so after reversing, the second half would just be [3 -> 2]. We would have:

After the second step, slow is at 2, and fast has reached the end None. At this point, we stop the iteration and slow is at the

1. Find the middle of the linked list: We start with two pointers, slow and fast. slow moves one step at a time, while fast moves

To illustrate the solution approach, let's walk through a small example with the following linked list [1 -> 4 -> 2 -> 3].

two steps. We initialize them as slow = head and fast = head.next. In our example:

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Original list: 1 -> 4 -> 2 -> 3
After reversing: 1 -> 4 -> 3 -> 2
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Python Solution

def __init__(self, val=0, next=None):

def pairSum(self, head: Optional[ListNode]) -> int:

prev = current_node

Reverse the second half of the list

while first_half_head and second_half_head:

first_half_head = first_half_head.next

second_half_head = second_half_head.next

Initialize the answer to zero

Return the maximum pair sum found

max_pair_sum = 0

return max_pair_sum

1 // Definition for singly-linked list.

ListNode(int val) { this.val = val; }

current_node = next_node

slow_pointer, fast_pointer = head, head.next

second_half_head = reverse_list(second_half_start)

Traverse both halves simultaneously and find the max pair sum

ListNode(int val, ListNode next) { this.val = val; this.next = next; }

// Use fast and slow pointers to find the middle of the list

fast = fast.next.next; // move fast pointer two steps

// The next step is to reverse the second half of the linked list

ListNode secondHalfStart = slow.next; // Start of the second half

ListNode reversedSecondHalf = reverse(secondHalfStart); // Reverse the second half

maxSum = Math.max(maxSum, firstHalf.val + reversedSecondHalf.val);

firstHalf = firstHalf.next; // Move to the next node in the first half

// Update the maximum sum using sums of pairs (firstHalf value and reversedSecondHalf value)

reversedSecondHalf = reversedSecondHalf.next; // Move to the next node in the reversed second half

slow = slow.next; // move slow pointer one step

// After the loop, slow will be at the middle of the list

ListNode firstHalf = head; // Start of the first half

slow.next = null; // Split the list into two halves

while (fast != null && fast.next != null) {

// Initialize the maximum sum variable

// Traverse the two halves together

while (firstHalf != null) {

// Return the maximum sum found

int maxSum = 0;

max_pair_sum = max(max_pair_sum, current_pair_sum)

current_pair_sum = first_half_head.val + second_half_head.val

Define a function to reverse a linked list

self.val = val

self.next = next

def reverse_list(node):

return prev

class ListNode:

class Solution:

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60 };

ListNode* reverse(ListNode* head) {

current->next = prev;

function pairSum(head: ListNode | null): number {

let slow: ListNode | null = head;

let fast: ListNode | null = head;

while (fast && fast.next) {

slow = slow.next;

slow.next = prev;

prev = slow;

slow = next;

while (left && right) {

left = left.next;

right = right.next;

Time and Space Complexity

fast = fast.next.next;

let prev: ListNode | null = null;

const next: ListNode | null = slow.next;

// Iterate through both halves of the list.

maxSum = Math.max(maxSum, left.val + right.val);

// Return the maximum twin sum after traversing the entire list.

sum of values from nodes that are equidistant from the start and end of the list.

the reversed second half of the list, yielding a time complexity of O(n/2).

let left: ListNode | null = head;

let right: ListNode | null = prev;

ListNode* next = current->next;

// Iterate over the linked list and reverse the pointers.

// The 'prev' pointer now points to the new head of the reversed linked list.

// Reverse the second half of the linked list, starting from the slow pointer.

1 // Function to find the maximum twin sum of a linked list. The twin sum is defined as the sum of nodes that are equidistant from the

// Calculate the twin sum by adding values of 'left' and 'right' pointers and update 'maxSum' if a larger sum is found.

The given Python code defines a function to find the maximum twin sum in a singly-linked list, where the twin sum is defined as the

// Move the fast pointer two nodes at a time and the slow pointer one node at a time. The loop ends when fast reaches the end of

// Initialize two pointers, slow and fast. The fast pointer will move at twice the speed of the slow pointer.

ListNode* prev = nullptr;

ListNode* current = head;

prev = current;

current = next;

while (current) {

return prev;

Typescript Solution

example linked list [1 -> 4 -> 2 -> 3] is 6. We return this value as the final result.

4. Returning the Result: With the iterations complete and no more nodes to traverse, we found that the maximum twin sum in our

prev = None current_node = node # Iterate through the list and reverse the links while current_node: next_node = current_node.next current_node.next = prev

Initialize slow and fast pointers to find the middle of the linked list

22 while fast_pointer and fast_pointer.next: 23 slow_pointer, fast_pointer = slow_pointer.next, fast_pointer.next.next 24 25 # Split the list into two halves first_half_head = head 26 27 second_half_start = slow_pointer.next 28 slow_pointer.next = None # Break the list to create two separate lists 29

```
// Function to find the maximum Twin Sum in a singly-linked list
11
       public int pairSum(ListNode head) {
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13
           // Initialize two pointers, slow and fast
           ListNode slow = head;
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           ListNode fast = head.next;
15
16
```

class Solution {

Java Solution

class ListNode {

int val;

ListNode next;

ListNode() {}

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           return maxSum;
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       // Helper function to reverse a singly-linked list
       private ListNode reverse(ListNode head) {
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           // Initialize a dummy node to help with the reversal
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           ListNode dummy = new ListNode();
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           // Traverse the list and reverse pointers
           ListNode current = head;
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           while (current != null) {
53
                ListNode next = current.next; // Keep the reference to the next node
54
                current.next = dummy.next; // Reverse the pointer
55
                dummy.next = current; // Move dummy next to the current node
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                current = next; // Move to the next node
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           // Return the reversed list, which starts at dummy.next
            return dummy.next;
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62 }
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C++ Solution
 1 /**
    * Definition for singly-linked list.
    * struct ListNode {
          int val;
          ListNode *next;
          ListNode() : val(0), next(nullptr) {}
          ListNode(int x) : val(x), next(nullptr) {}
          ListNode(int x, ListNode *next) : val(x), next(next) {}
    * };
    */
11 class Solution {
12 public:
       // Main function to find the twin sum of the linked list.
14
        int pairSum(ListNode* head) {
15
           // Use two pointers 'slow' and 'fast' to find the midpoint of the linked list.
           ListNode* slow = head;
16
           ListNode* fast = head->next;
           while (fast && fast->next) {
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                slow = slow->next;
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                fast = fast->next->next;
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           // Split the linked list into two halves.
24
           ListNode* firstHalf = head;
25
           ListNode* secondHalfStart = slow->next;
26
            slow->next = nullptr; // This null assignment splits the linked list into two.
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           // Reverse the second half of the linked list.
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           ListNode* reversedSecondHalf = reverse(secondHalfStart);
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           // Initialize the maximum pair sum as zero.
32
            int maxPairSum = 0;
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34
           // Traverse the two halves in tandem to calculate the max pair sum.
           while (firstHalf && reversedSecondHalf) {
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36
                maxPairSum = max(maxPairSum, firstHalf->val + reversedSecondHalf->val);
37
                firstHalf = firstHalf->next;
38
                reversedSecondHalf = reversedSecondHalf->next;
39
40
            return maxPairSum;
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43
       // Helper function to reverse the linked list.
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```

21 // The 'prev' pointer now points to the head of the reversed second half of the list. 'head' points to the beginning of the first 22 23 24 // Initialize 'maxSum' to keep track of the maximum twin sum. 25 let maxSum: number = 0;

return maxSum;

Time Complexity

while (slow) {

```
linked list once, with a time complexity of O(n/2), where n is the total number of nodes in the list, because it stops at the
  midpoint of the list due to the previous pointer manipulation.
2. Finding the midpoint of the linked list: This is achieved by the "tortoise and hare" technique, where we move a slow pointer by
  one step and a fast pointer by two steps. When the fast pointer reaches the end, the slow pointer will be at the midpoint, and
  this has a time complexity of O(n/2) since the fast pointer traverses the list twice as fast as the slow pointer.
```

1. Reversing the second half of the linked list: The reverse function iterates over the nodes of the second half of the original

Space Complexity 1. Additional space for reversing: The reverse function uses a constant amount of extra space, as it just rearranges the pointers without allocating any new list nodes.

3. Calculating the maximum twin sum: This involves a single pass through the first half of the list while simultaneously traversing

Adding these together gives 2 * 0(n/2) + 0(n/2), simplifying to 0(n) as constants are dropped and n/2 is ultimately proportional to

- 2. Space for pointers: A few extra pointers are used for traversal and reversing the linked list (dummy, curr, slow, fast, pa, pb), which use a constant amount of space.
- Therefore, the space complexity of the provided code is 0(1) since it does not grow with the size of the input list and only a fixed amount of extra memory is utilized.