Problem Description

same length as nums. Each element result[i] in this new array should be the sum of the absolute differences between nums[i] and every other element in the array nums. Essentially, for a given element nums [i], we calculate the absolute value of the difference between nums [i] and each element nums [j] where j goes from 0 to the length of the array but is not equal to i. Then we add up all these absolute differences to get result[i].

In this problem, we have an array nums that is sorted in non-decreasing order. Our goal is to construct a new array result of the

The direct approach would be to calculate the sum of absolute differences for each element in the array by iterating over the array

the fly.

Intuition

sorted and leverage a prefix sum technique that will allow us to calculate the sum of absolute differences in a more efficient manner. Intuition behind the solution: Since the array is sorted, all numbers to the left of nums [i] are less than or equal to nums [i], and all numbers to the right are greater than or equal to it. So, for nums [i], to get the sum of absolute differences, we can sum the

for each element, which would be very inefficient with a time complexity of O(n^2). Instead, we can utilize the fact that the array is

The key insight here is to realize that we can compute the sum of absolute differences for nums [1] using Cumulative Sum (also known as Prefix Sum). A Cumulative Sum is an array cumsum where cumsum[i] represents the sum of the elements nums[0] up to

differences between nums[i] and all numbers to its left, and then sum the differences between nums[i] and all numbers to its right.

nums[i]. With this, the sum of differences to the left of nums[i] can be found by nums[i] * i - cumsum[i-1] (since nums[i] is larger than each of these numbers) and the sum of the differences to the right of nums[i] can be found by (cumsum[n-1] - cumsum[i]) nums[i] * (n-1-i) (since nums[i] is smaller than each of these numbers, subtracting it from the cumulative sum gives us the sum of the differences). By adding these two quantities together, we get the sum of absolute differences for each nums [i]. In the provided solution, instead of keeping a separate array for the cumulative sum, the sum of all elements s and running total of

sums t are used to avoid extra space. We iterate through the array, updating t and calculating the sum of absolute differences on

Solution Approach Understanding the provided Python code requires us to focus on how it implements the prefix sum technique described in the Intuition.

1. Initialize an empty list ans, which will be our result array to store the summation of absolute differences for each element.

2. Compute the total sum s of the array nums. This will be used to calculate the sum of all elements to the right of the current element. 3. Initialize a variable t to keep track of the cumulative sum (or running total) of the elements as we iterate through the list. This will

be used to calculate the sum of all elements to the left of the current element.

First, let's go through the steps involved in the algorithm:

- 4. Loop through the array nums using enumerate to get both the index i and the value x at each iteration. 5. For current element x, calculate the sum of absolute differences using the following steps:
- Calculate the sum of differences between x and all the elements on its left (the smaller elements). We can get this by multiplying x with its index i, which gives us the sum of x added i times, and subtracting the running total t which
- represents the sum of all elements up to x. Calculate the sum of differences between x and all the elements on its right (the larger elements). This is done by subtracting the running total t and x itself from the total sum s to get the sum of all elements to the right of x, and then
- Add both sums to get the total sum of absolute differences for x and append this value to ans. 6. Update the running total t by adding the current element value x to it.

subtracting x multiplied by the number of elements to the right of it (len(nums) - i).

The step where the absolute difference is calculated, the mathematical formulation is as follows:

• x * i: The sum of x added i times. • - t: Subtract the cumulative sum of elements to the left.

1 v = x * i - t + s - t - x * (len(nums) - i)

This line of the code can be broken down into parts:

7. After the loop is completed, return ans as the result array.

reducing the computational load compared to a naive O(n^2) method of calculating absolute differences for each element

• + s - t: Total sum minus the cumulative sum to get sum of all elements to the right.

• $- \times * (len(nums) - i)$: Subtract x times the count of elements to the right.

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for the running total and s as the total sum. By doing this, it's possible to compute the answer in a single pass after calculating the
sum of the array just once at the beginning.
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Example Walkthrough

individually.

Following the solution steps: 1. We initialize our result array ans as an empty list. 2. The total sum s of nums is calculated as 1 + 3 + 6 + 10 = 20.

Putting the pieces together, this approach efficiently calculates the desired values with a time complexity of O(n), significantly

The algorithm cleverly handles the calculation without using additional space for a cumulative sum array by updating and utilizing t

First iteration (i=0, x=1):

Now ans is [16].

■ Calculate the left sum: x*i - t which is 1*0 - 0 = 0 because there are no elements to the left of the first element. ■ Calculate the right sum: (s - t) - x*(len(nums)-i) which is (20 - 0) - 1*(4-0) = 20 - 1*4 = 16.

■ The total sum of absolute differences for x is 0 + 16 = 16. So we append 16 to ans.

Let's take a small example to illustrate the solution approach. Suppose our array nums is [1, 3, 6, 10].

■ We update t by adding x to it: t = 0 + 1 = 1. Second iteration (i=1, x=3):

3. We set t to 0 which will hold the cumulative sum as we iterate.

4. Now we iterate through nums. Here are the detailed steps:

Now our ans is [16, 12].

■ The total sum of differences is 2 + 10 = 12. Append 12 to ans.

■ Left sum: x*i - t which is 6*2 - 4 = 8 since the sum of 1 + 3 is 4. ■ Right sum: (s - t) - x*(len(nums)-i) which is (20 - 4) - 6*(4-2) = 16 - 6*2 = 4.

■ Left sum: x*i - t which is 3*1 - 1 = 2 since the sum of all elements to the left of 3 is 1.

■ Right sum: (s - t) - x*(len(nums)-i) which is (20 - 1) - 3*(4-1) = 19 - 3*3 = 10.

■ Left sum: x*i - t which is 10*3 - 10 = 20 since the sum of 1 + 3 + 6 is 10. Right sum: There are no elements to the right of the last element, hence the value is 0. ■ The total is 20 + 0 = 20. Append 20 to ans.

■ The total is 8 + 4 = 12. Append 12 to ans.

• Update t: t = 1 + 3 = 4.

Our ans is now [16, 12, 12].

Fourth iteration (i=3, x=10):

Now ans is [16, 12, 12, 20].

■ Update t: t = 4 + 6 = 10.

Third iteration (i=2, x=6):

Thus, the array [1, 3, 6, 10] transforms into [16, 12, 12, 20] following our solution approach. Each element in the result array represents the sum of the absolute differences between that element in nums and all other elements. This process provides a much more efficient calculation with a linear time complexity.

def getSumAbsoluteDifferences(self, nums: List[int]) -> List[int]:

Calculate the sum of the entire array to use later in calculations.

'value * index' is the sum of 'value' being subtracted from all

'total_sum - prefix_sum' is the sum of all the elements to the

Iterate through the list, with both the index and the value.

elements to the left of 'value' (including itself).

Update the prefix sum with the current value.

Compute the value for the current index.

Initialize a list to store the answers.

There's no need to update t as we're at the end of the array.

5. We've completed the loop and now ans holds our final result, which is [16, 12, 12, 20].

20 # right of 'value'. # Subtract 'value * (len(nums) - index)', which is 'value' being # added to all elements to the right of 'value'. current_value = value * index - prefix_sum + total_sum - prefix_sum - value * (len(nums) - index) 24 25 # Append the computed value to the answer list.

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             return answers
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Java Solution

class Solution {

Python Solution

class Solution:

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from typing import List

answers = []

prefix_sum = 0

total_sum = sum(nums)

Initialize a prefix sum to 0.

for index, value in enumerate(nums):

answers.append(current_value)

Return the list of computed answers.

public int[] getSumAbsoluteDifferences(int[] nums) {

// Initialize the total sum of the array elements to 0

prefix_sum += value

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int totalSum = 0;
           // Calculate the total sum of the array elements
           for (int num : nums) {
               totalSum += num;
10
           int n = nums.length; // Store the length of the array
11
           int[] result = new int[n]; // Initialize the result array to store answers
13
           int prefixSum = 0; // Initialize the prefix sum to keep track of the sum of elements till the current index
14
15
           // Loop through each element to calculate the sum of absolute differences
           for (int i = 0; i < n; ++i) {
16
               // Calculate the sum of absolute difference for the current element
17
               // The sum of differences of all elements to the left of the current
19
               // element can be found by nums[i] * i (since there are 'i' elements to the left)
20
               // minus the sum of all elements to the left which is given by prefixSum (t in your code).
               // Similarly, the sum of differences of all elements to the right of the current
               // element is the total sum of all elements minus the sum of all elements till the
23
               // current index (including itself), minus the sum total of the elements to the left
24
               // times the number of elements to the right: (totalSum - prefixSum - nums[i]) * (n - i).
25
               int sumAbsoluteDifferences = nums[i] * i - prefixSum + totalSum - prefixSum - nums[i] * (n - i);
               result[i] = sumAbsoluteDifferences; // Assign the computed value to the result array
26
27
               prefixSum += nums[i]; // Update the prefix sum with the current element's value
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           // Return the final result array
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           return result;
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33 }
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C++ Solution
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26 27 28 29

1 #include <vector>

class Solution {

5 public:

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2 #include <numeric> // For std::accumulate

int partial_sum = 0;

int n = nums.size();

vector<int> result(n);

for (int i = 0; i < n; ++i) {

// Function to calculate the sum of absolute differences of each element

// Initialize variable to keep track of the sum of elements seen so far

// Calculate the sum of absolute differences for the current element

// Update the partial sum with the value of the current element

+ total_sum - partial_sum

 $- \text{nums}[\overline{i}] * (n - i);$

int total_sum = std::accumulate(nums.begin(), nums.end(), 0);

int absolute_difference_sum = nums[i] * i - partial_sum

// Store the result in the corresponding position

// Initialize result vector with the same size as input

vector<int> getSumAbsoluteDifferences(vector<int>& nums) {

// Calculate the sum of the entire array

// Get number of elements in the array

// Iterate over each element in the array

result[i] = absolute_difference_sum;

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partial_sum += nums[i];
           // Return the final result vector
           return result;
30
31 };
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Typescript Solution
   function getSumAbsoluteDifferences(nums: number[]): number[] {
       // Calculate the sum of all elements in the array.
       const totalSum = nums.reduce((previousValue, currentValue) => previousValue + currentValue, 0);
       let cumulativeSum = 0;
       const length = nums.length;
       const result = new Array(length); // Initialize the result array.
       // Iterate through the elements of the array to calculate the
 8
       // sum of absolute differences for each element.
       for (let i = 0; i < length; ++i) {</pre>
10
           // Calculate the sum of absolute differences for nums[i]:
11
           // This includes the difference between nums[i] and each element to the left of it,
13
           // and each element to the right of it.
           const absoluteDifferenceSum = nums[i] * i - cumulativeSum
14
                                          + totalSum - cumulativeSum - nums[i] * (length - i);
15
16
            result[i] = absoluteDifferenceSum; // Store the computed value in the result array.
17
           // Update the cumulative sum with the value of the current element.
18
           cumulativeSum += nums[i];
19
20
21
       return result; // Return the final array containing the sum of absolute differences for each element.
22 }
23
```

The given code snippet implements an algorithm to get the sum of absolute differences for each number in the input list nums with every other number in the list.

where n is the number of elements in nums.

Time and Space Complexity

To analyze the time complexity, let's consider the number of operations performed by the code: • We first calculate the sum of all numbers in nums (s = sum(nums)). This iteration over the array has a time complexity of O(n),

- precomputed total sum s and the temporary sum t. The formula v = x * i t + s t x * (len(nums) i) does so using a constant number of operations for each element.
- The total number of operations inside the loop is independent of the size of the list, meaning it's 0(1) per element. As we do a constant amount of work for each of the n elements during this iteration, the time complexity for this loop is O(n).

• Then, we iterate over the list nums once. For each element x at index i, we calculate the sum of absolute differences using the

- Combining both steps, the overall time complexity of the algorithm is O(n) + O(n), which simplifies to O(n).
- **Space Complexity:**

When analyzing the space complexity of the code, consider the following:

Time Complexity:

 A new list ans is created to store the result. In the worst case, it will contain the same number of elements as the input list nums, hence it takes O(n) space.

space used by the algorithm is essentially the space taken by the ans list.

- The variables s, t, and v use constant space, i.e., 0(1). Since all other variables (i and x) are also using constant space and there are no other data structures used, the total additional
- Therefore, the overall space complexity of the function is O(n). In summary, the function has a time complexity of O(n) and a space complexity of O(n).