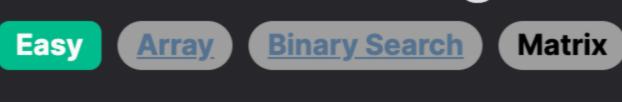
1351. Count Negative Numbers in a Sorted Matrix



Problem Description

a non-increasing (also known as non-decreasing) order across both rows and columns—this means the numbers go from larger on the top-left to smaller on the bottom-right.

Given a matrix grid which has dimensions m x n, our task is to count all the negative numbers within this grid. The matrix is sorted in

To visualize, we might have a matrix like this:

The goal is to count how many negative numbers are present.

In the above example, you can see that rows and columns are sorted in non-increasing order and there are 8 negative numbers.

Intuition

Since the grid is sorted in non-increasing order row-wise and column-wise, we can use a more efficient approach than checking

each cell individually.

Here's the intuition step by step:

then all numbers to its right are guaranteed to be negative because the row is sorted in non-increasing order. On the other hand, if this number is not negative, we can move one column to the right.

2. We keep track of our current position with indices i for rows and j for columns. We set ans to 0 to keep track of our count of negative numbers.

1. We start at the bottom-left corner of the matrix (grid[m - 1][0]). The reason for doing this is that if this number is negative,

- 4. If the current element where we are (grid[i][j]) is negative, we add the count of remaining columns in that row to our answer (i.e., ans += n - j) because all of these will be negative. After doing that, we move one row up (i -= 1) since we're done with
- the current row.

3. We use a while loop that runs as long as i is within the rows and j is within the columns of the grid.

5. If the element is not negative, we move one column to the right (j += 1) to check the next number in the same row. 6. The process is repeated until we've gone through all rows or columns.

The solution uses a simple algorithm that takes advantage of the properties of the matrix, namely that it is sorted in non-increasing

The solution leverages the sorted property of the matrix to skip over non-negative elements and only count consecutive negatives, which makes it efficient.

7. We return the count ans which contains the number of negative numbers in the grid at the end of our loop.

- **Solution Approach**
- Here is a step-by-step walkthrough of the implementation:

order in both rows and columns. No additional data structures are needed; we can operate directly on the given grid.

3. Enter a while loop with the condition that i is greater than or equal to 0 (to make sure we are within the bounds of the rows) and

1. Initiate two pointers, i for rows, starting from the last row (m - 1), and j for columns, starting from the first column (0).

current row (n - j). This is because, since the rows are non-increasing, all elements to the right of grid[i][j] will also be negative. Then, decrease the row pointer i by 1, to move up to the previous row.

2. Initiate a variable ans to store the count of negative numbers, initially set to 0.

j is less than n (to make sure we are within the bounds of the columns).

5. If grid[i][j] is not negative, just move to the next column by incrementing j by 1. 6. The loop continues until one of the exit conditions of the while loop is met (either all rows have been checked or the end of a row

The time complexity of this algorithm is O(m + n), where m is the number of rows and n is the number of columns. This is because at

each step of the algorithm, we're either moving one row up or one column to the right until we exit the matrix bounds. In the worst-

The space complexity is O(1) as we are not using any additional space proportional to the size of the input grid; instead, we're just

No complex patterns are used here; the implementation is straightforward once the insight about the grid's sorted property is

4. In the loop, check if the current element grid[i][j] is negative. If it is, increment ans by the number of columns remaining in the

using a few extra variables for counting and indexing.

7. Finally, return the ans variable, which now contains the count of negative numbers in the grid.

Example Walkthrough Let's consider a smaller example to clearly illustrate the use of the solution approach in a concrete situation. Suppose we have the

1. We initialize our pointers i with the index of the last row which is 2 for this grid (since we are using 0-based indexing), and j with

3. We begin our while loop. Our initial element to check is grid[2][0], which is 1. Since it's not negative, we move one column to

2. We set ans to 0 as our count of negative numbers.

has been reached).

understood.

case scenario, we'll make m+n moves.

following grid matrix with dimensions 3×4 :

the index of the first column which is 0.

the right by incrementing j to 1.

row by decrementing i to 0.

Python Solution

class Solution:

Java Solution

1 class Solution {

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20 }

4. Now, grid[2][1] is -1, which is negative. We find that there are 4 - 1 = 3 columns remaining in the row, including the current column. So, we add 3 to ans, making it 3, and move up a row by decrementing i to 1.

We want to count the number of negative numbers in this grid. Here's how we can apply the solution approach:

- 5. Our new position is grid[1][1], which is 1. It's not negative, so we move one column to the right again by incrementing j to 2. 6. We check grid[1][2], it's -1. There are 4 - 2 = 2 columns remaining, so we add 2 to ans, which becomes 5. We then move up a
- 7. The element grid[0][2] is 1, not negative. We increment j to 3. 8. At grid[0][3], we have -1. With only 1 column at this last index, we add 1 to ans, resulting in a final count of 6. Since there are no

def countNegatives(self, grid: List[List[int]]) -> int:

num_rows, num_cols = len(grid), len(grid[0])

Initialize pointers for the row and column

while row_index >= 0 and col_index < num_cols:</pre>

If current element is negative

public int countNegatives(int[][] grid) {

if (grid[rowNum][colNum] < 0) {</pre>

} else {

if grid[row_index][col_index] < 0:</pre>

Iterate over the grid, starting from the bottom left corner

int rowCount = grid.length; // The number of rows in the grid.

// Function to count the number of negative numbers in a 2D grid

int rowCount = grid.size(); // Number of rows in the grid

int colCount = grid[0].size(); // Number of columns in the grid

1 // Counts the number of negative numbers in a row-wise and column-wise sorted grid.

// Number of columns in the grid — assumes at least 1 row exists

// Loop until we reach the top of the grid or the end of a row

negativeCount += columnCount - column;

// All numbers to the right of the current position are negative

// If the current number is non-negative, move right to the next column

// @returns The total count of negative numbers in the grid.

// Start from the bottom—left corner of the grid

function countNegatives(grid: number[][]): number {

// Number of rows in the grid

const rowCount = grid.length;

const columnCount = grid[0].length;

// Counter for negative numbers

let negativeCount = 0;

let row = rowCount - 1;

row--;

} else {

let column = 0;

2 // @param grid — A 2D array of numbers where each row and column is sorted in non-increasing order.

int negativeCount = 0; // Initialize the counter for negative numbers

int countNegatives(std::vector<std::vector<int>>& grid) {

int colCount = grid[0].length; // The number of columns in the grid.

for (int rowNum = rowCount - 1, colNum = 0; rowNum >= 0 && colNum < colCount;) {

return negativeCount; // Return the total count of negative numbers in the grid.

int negativeCount = 0; // Initialize a count for negative numbers.

Thus, the grid contains 6 negative numbers.

more rows above, the loop ends here as i is decremented and falls below 0.

With this example, it is clear how the algorithm smartly traverses the matrix, leveraging the sorted property to count negative numbers efficiently, without needing to check each element.

row_index, col_index = num_rows - 1, 0 8 9 # Initialize counter for negative numbers negative_count = 0 10 11

Get the dimensions of the grid

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# All elements in the current row to the right are also negative
16
                    negative_count += num_cols - col_index
17
18
19
                    # Move up to the previous row
20
                    row_index -= 1
21
               else:
22
                    # Move right to the next column
23
                    col_index += 1
24
25
           # Return the total count of negative numbers
26
            return negative_count
27
```

// Start from the bottom-left corner of the grid and move upwards in rows and rightwards in columns.

negativeCount += colCount - colNum; // Add the remaining elements in the row to the count.

// If the current element is negative, all the elements to its right are also negative.

rowNum--; // Move up to the previous row to continue checking for negatives.

colNum++; // Move right to the next column to check for non-negative elements.

#include <vector> // Necessary for using vectors class Solution {

public:

C++ Solution

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           // Start from the bottom-left corner of the grid
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           int currentRow = rowCount - 1;
            int currentColumn = 0;
13
14
           // Loop through the grid diagonally
           while (currentRow >= 0 && currentColumn < colCount) {</pre>
16
               // If the current element is negative, then all elements to its right are also negative
17
                if (grid[currentRow][currentColumn] < 0) {</pre>
18
19
                    negativeCount += colCount - currentColumn; // Add all negative numbers in the current row
20
                    --currentRow; // Move up to the previous row to continue with the negative number sweep
                } else {
22
                    // If the current element is not negative, move right to the next column
23
                    ++currentColumn;
24
25
26
27
           // Return the total count of negative numbers found in the grid
28
            return negativeCount;
29
30 };
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Typescript Solution
```

while (row >= 0 && column < columnCount) {</pre> 17 // If the current number is negative, // add all remaining negatives in the row to the counter 20 // (as the row is sorted in non-increasing order) if (grid[row][column] < 0) {</pre> 21

Time Complexity:

regardless of the input size.

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```
column++;
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       // Return total count of negative numbers
       return negativeCount;
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34 }
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Time and Space Complexity
The provided code implements an algorithm to count the number of negative numbers in an m x n grid, which is assumed to be non-
increasing both row-wise and column-wise. The algorithm starts from the bottom-left corner of the grid and moves upwards or to
the right depending on the sign of the current cell value.
```

// Move up to the previous row since we've counted all negatives in the current row

• The inner condition can lead to moving rightwards across up to n columns. However, you will never revisit a row or a column once you've moved on from it (since you move up if you find a negative and move

Thus, the time complexity of the algorithm is O(m + n).

right if you find a non-negative number), meaning each cell is visited at most once. Therefore, the maximum number of steps is m + n.

The time complexity of the code can be analyzed as follows:

- **Space Complexity:** The space complexity of the code is:
- Constant extra space is used for the variables m, n, i, j, and ans. No additional data structures are being used that grow with the size of the input. Considering the above points, the overall space complexity of the algorithm is 0(1), as it uses a constant amount of extra space

• The outer loop runs a maximum of m times if we're moving upwards from the bottom row to the topmost row in the worst case.