Problem Description

The task involves an integer array nums, where each adjacent pair of integers performs a floating-point division in the given order. For instance, if nums is [2, 3, 4], it represents the expression 2/3/4. The challenge is to add parentheses to the expression in a way that maximizes the result of the expression. Parentheses can change the order of operations; hence changing the expression's value. The goal is to find where to place these parentheses to get the maximum value expression and return this expression as a string. It's important to note that the final expression must not include unnecessary parentheses.

Intuition

result. With division, the key to maximizing the outcome is to divide by the largest possible number. Based on this logic, we want to minimize the denominator as much as possible to maximize the result of the entire expression.

For three or more numbers, the maximum result is achieved when we divide the first number by the result of dividing all the

When dividing a set of numbers, placing the larger numbers in the numerator and the smaller ones in the denominator maximizes the

remaining numbers. Therefore, for nums = [a, b, c, ..., n], the optimal division is a/(b/c/.../n). This ensures that a is divided by the smallest possible value obtained from the division of the rest of the numbers. In this case, we only need parentheses around all the numbers starting from the second number in the array.

For nums with only one element, there is no division to perform, so we return the single number. When nums has exactly two elements, say [a, b], the expression is simply a/b, as there's no other way to place parentheses that can alter the result. The solution naturally emerges from these observations:

2. If nums contains two elements, the expression is "a/b". 3. For three or more elements, we use parentheses to ensure that the first element is divided by the smallest possible value

1. If nums contains only one element, that is the expression.

- obtained from the division of the rest of the numbers: "a/(b/c/.../n)". The provided Python solution implements these insights through conditional logic and string formatting.

Solution Approach

The provided Python solution implements a direct approach without the need for any complex algorithms or data structures. Here's

how the code accomplishes the task: 1. The solution first checks the length of nums:

- \circ If the array has only one element (n == 1), it returns that element as a string. \circ If the array has two elements (n == 2), it returns the division of the first element by the second as a string formatted "a/b".
- 2. For arrays with three or more elements ($n \ge 3$), the solution constructs an expression that places the first number in the
 - numerator and the rest in the denominator within a pair of parentheses. This is based on the intuition that to maximize the value of the division, you want to divide the first number by the result of the subsequence divisions, thus minimizing the denominator.
- 3. The code uses Python's string formatting and string join method to construct the final expression. The part "/".join(map(str, nums [1:])) joins all elements of nums starting from the second element with a division sign between them. It then formats the entire string by placing the first element of nums outside and the joined string inside the parentheses.

advantage of Python's string manipulation capabilities to format the output as per the problem's requirements. The simplicity of the solution comes from the mathematical insight that the highest value for the entire expression is obtained when

the first element of nums is divided by the smallest possible value from the division of the subsequent elements. This is efficiently

No additional data structures are required since the final expression is constructed directly from the input list. The solution takes

implemented in the given Python function optimalDivision. Here's the implementation logic step by step in the solution: 1 class Solution:

n = len(nums)if n == 1:

def optimalDivision(self, nums: List[int]) -> str:

```
return str(nums[0])
                                                 # Case for single element, return as string
           if n == 2:
               return f'{nums[0]}/{nums[1]}'
                                                 # Case for two elements, return "a/b"
           # Case for three or more elements, return "a/(b/c/.../n)"
           return f'{nums[0]}/({"/".join(map(str, nums[1:]))})'
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This concise implementation elegantly solves the problem by directly translating the mathematical insight of division into a formatted
string, which is exactly what the problem statement is asking for.
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Example Walkthrough Let's go through a small example using the solution approach to understand how the algorithm maximizes the expression by

Suppose we have the array nums = [8, 2, 3, 4], which represents the expression 8/2/3/4. The task is to add parentheses to

correctly placing the parentheses.

maximize this expression's value. Following the solution approach:

1. We first check the length of nums. Since n = 4, we have more than two elements.

subsequence divisions. To achieve this, we should divide the first element by the result of dividing all the subsequent numbers.

This translates to the expression: 8/(2/3/4).

 $8/(0.166...) \approx 48$, which is indeed the maximum value possible for this expression.

If there is only one number, return it as a string

For more than two numbers, the optimal division is to divide the first number

// If there are more than two numbers, we use parentheses to maximize the result

return f'{nums[0]}/{nums[1]}'

parentheses, resulting in the final expression "8/(2/3/4)".

3. To create this expression in Python, the code joins all elements of nums, starting from the second element, with a division sign, resulting in the string "2/3/4". 4. Then, the code formats the entire expression by placing the first element of nums (8) outside and the joined string inside

2. For an array with more than two elements, the goal is to maximize the first number's division by the smallest possible result from

Using this approach, we have successfully maximized the value of the original expression. In the absence of parentheses, the expression would calculate as follows: (8/2)/3/4 = 4/3/4 = 1.33. However, by placing parentheses as 8/(2/3/4), we get:

The Python code effectively and efficiently constructs this optimal expression using string formatting without the need for additional

computation or complex data structures. Python Solution

class Solution: def optimalDivision(self, nums: List[int]) -> str: # Calculate the length of the input list of numbers

```
return str(nums[0])
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           # If there are two numbers, return them as a division
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           if size == 2:
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from typing import List

size = len(nums)

if size == 1:

```
# by the result of the division of all remaining numbers to achieve the largest result.
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           # This is done by grouping all but the first number inside parentheses.
18
           return f'{nums[0]}/(' + "/".join(map(str, nums[1:])) + ')'
19
20
Java Solution
1 class Solution {
       // Method to find the optimal division of integers as a string
       public String optimalDivision(int[] nums) {
           // Get the number of elements in the array
           int arrayLength = nums.length;
           // If there is only one number, return it as there's nothing to divide
           if (arrayLength == 1) {
               return String.valueOf(nums[0]);
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           // If there are two numbers, return their division
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19 20 // Start the string with the first number and an opening parenthesis 21 result.append(nums[0]).append("/("); 22 23 // Loop through the rest of the array, except for the last element

if (arrayLength == 2) {

return nums[0] + "/" + nums[1];

StringBuilder result = new StringBuilder();

for (int i = 1; i < arrayLength - 1; ++i) {</pre>

25 // Add each number followed by a division sign 26 result.append(nums[i]).append("/"); 27 28 // Add the last element of the array and the closing parenthesis 29 30 result.append(nums[arrayLength - 1]).append(")"); 31 32 // Return the constructed string 33 return result.toString(); 34 35 } 36 C++ Solution 1 class Solution { public: // This function finds the optimal division of array numbers as a string expression string optimalDivision(vector<int>& nums) { int n = nums.size(); // If there is only one number, return it as a string if (n == 1) { return to_string(nums[0]); 9 10 11 12 // If there are two numbers, return their division if (n == 2) { 13

return to_string(nums[0]) + "/" + to_string(nums[1]);

string answer = to_string(nums[0]) + "/(";

for (int i = 1; i < n - 1; i++) {

// For more than two numbers, enclose all but the first number in parentheses

// This is to ensure the division is performed correctly for optimal result

// Append all the remaining numbers separated by a division operator

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                answer.append(to_string(nums[i]) + "/");
24
25
26
```

```
// Add the last number and close the parentheses
           answer.append(to_string(nums[n - 1]) + ")");
28
29
           return answer;
30
31 };
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Typescript Solution
 1 /**
    * Returns a string representation of the division of numbers that maximizes the result.
    * If there are more than two numbers, brackets are added to divide the first number by
    * the result of the division of all subsequent numbers.
    * @param {number[]} numbers - An array of numbers to divide.
    * @returns {string} - The string representation of the optimal division.
   function optimalDivision(numbers: number[]): string {
       // Get the number of elements in the array
       const count = numbers.length;
10
12
       // Combine the numbers into a string separated by slashes
       const divisionString = numbers.join('/');
13
14
       // If there are more than two numbers, add brackets after the first division
15
       if (count > 2) {
16
           // Find the index of the first slash to insert the opening bracket
           const firstSlashIndex = divisionString.indexOf('/') + 1;
           // Return the string with brackets inserted
19
           return `${divisionString.slice(0, firstSlashIndex)}(${divisionString.slice(firstSlashIndex)})`;
20
21
22
       // If there are two or fewer numbers no brackets are needed
```

return divisionString; 24 25 } 26

Time and Space Complexity

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The time complexity of the code primarily depends on the length of the nums array. The map function iterates over nums [1:], which has a complexity of 0(n-1) where n is the length of the array. The join operation on a list of strings has a complexity of 0(m), where m is the total length of the strings being concatenated. Since in this case we're dealing with string representations of the numbers, the length of each integer after conversion to string can vary, but in the worst case, it will be proportional to the logarithm of the number. However, for the purpose of time complexity analysis, we can consider m to be linearly dependent on n because the number of divisions does not change the overall complexity class. Hence, the join operation is also 0(n). The overall time complexity is 0(n).

The space complexity includes the space required for the output and the temporary lists created by map and join. The size of the

output string is O(n) since it includes all the elements of nums plus additional characters. The temporary list created by map is also

O(n). However, these are not additional spaces in terms of space complexity analysis since they are required for the output. Thus,

Space Complexity

the space complexity is O(n).

Time Complexity