1642. Furthest Building You Can Reach
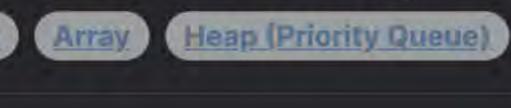
     Leetcode Link

Problem Description

In this problem, you are given an array `heights` that represents the heights of a series of buildings in a line. You are also given a certain number of `bricks` and `ladders`. As you move from one building to the next, you can either use bricks or ladders based on the following rules:

- If the building you are currently on is of equal or greater height than the next one, you can move ahead without using any bricks or ladders.
- If the building you are currently on is shorter than the next one, you need to bridge the height difference by either using a ladder or using as many bricks as the height difference.

Your goal is to figure out the farthest building index (0-indexed) you can reach by using the ladders and bricks in the best way possible.

Intuition

The intuition behind the solution revolves around optimizing the use of ladders, which are more versatile and valuable than bricks. Since ladders can cover any height difference and you have a limited number of them, you want to use ladders for the largest height differences. For smaller height differences, it's more economical to use bricks.

One effective approach to solve this problem is using a min-heap to keep track of the `ladders` largest height differences encountered so far as you iterate through the array. Here's the thought process:

1. As you traverse each building, calculate the height difference with the next building if it's greater than the current one.
2. Add these differences to a min-heap. Since the size of the heap is limited to the number of available ladders, whenever you add an item and the heap size exceeds the number of ladders, you pop the smallest item. This represents using bricks for the smallest climb that you initially thought of using a ladder for.
3. When popping from the heap (which means using bricks instead of a ladder), subtract the height difference (number of bricks needed) from the available bricks.
4. If at any point you run out of bricks, this means you can't make the climb using bricks anymore, and you've used all your ladders for higher climbs. The current index is the furthest you can reach.

This strategy ensures that ladders are reserved for the biggest climbs, and bricks are used for the smaller ones, which is an optimal way to go as far as possible.

Solution Approach

The solution approach uses a greedy algorithm to decide when to use bricks and when to save the ladders for taller buildings. To implement this strategy, we use a min-heap, which is a data structure that allows us to efficiently track and update the smallest height differences for which we've decided to use ladders.

Here are the steps taken in the Python code implementation:

1. We initialize a min-heap `h` as an empty list, which will store the heights differences when a ladder is used.
2. We then iterate through the `heights` array with the variable `i` indicating our current position, comparing each building `a` with the next building `b`.
3. For each pair of buildings where building `b` is taller (i.e., the height difference `d` is greater than 0), we push the difference to the heap using `heappush(h, d)`.
4. We then check if the length of the heap exceeds the number of available ladders. If it does, this means we must use bricks instead of a ladder for the smallest height difference encountered so far. To do this, we pop from the heap using `heappop(h)`, which removes and returns the smallest item from the heap. We then subtract this value from our available `bricks`.
5. If at any point our count of bricks falls below 0, we can no longer proceed to the next building using bricks. We return the current index `i` because that's the furthest we can go.
6. If we finish iterating through the array without running out of bricks, it means we were able to reach the last building. We return `len(heights) - 1` as we have successfully reached the end.

The use of a min-heap here is crucial for keeping our algorithm efficient. Without the heap, we would have to search through all height differences we've encountered whenever we need to use bricks, which would make our solution much slower. With the min-heap, we ensure that we are always removing the smallest height difference in logarithmic time complexity, which keeps the overall time complexity of the algorithm controlled and efficient.

Example Walkthrough

Let's walk through a small example to illustrate the solution approach:

Imagine you have an array `heights = [4, 2, 7, 6, 9, 14, 12]`, `bricks = 5`, and `ladders = 1`.

Following the steps of the solution:

1. **Initialize a Min-Heap:** Start with an empty min-heap.
2. **Iterate Over Buildings:** Begin traversing the buildings. The comparison starts at the first building (`i = 0`) and goes to the second last one.
3. **Building Heights Comparison:**
   - From 4 to 2: No bricks or ladders needed because the next building is shorter.
   - From 2 to 7: The height difference is 5, so we push 5 into the heap (`h = [5]`).
   - From 7 to 6: No action needed, as the next building is shorter.
4. **Heap Size Check and Bricks Use:**
   - No check necessary since we have used only one ladder till now, and the heap size is within the limit of available ladders (heap size = 1, ladders = 1).
5. **Building Heights Comparison Continued:**
   - From 6 to 9: The height difference is 3, add this to the heap (`h = [3, 5]`).
6. **Heap Size Exceeds Available Ladders:**
   - Because we have more items in the heap than available ladders, we must pop the smallest item. We pop 3 and subtract it from the bricks (`bricks = 5 - 3 = 2`).
7. **Building Heights Comparison Continued:**
   - From 9 to 14: The height difference is 5. Add this to the heap (`h = [5, 5]`).
8. **Heap Size Exceeds Again:**
   - Again, we have more items in the heap than ladders. Pop the smallest item (which is 5) and subtract from the bricks (`bricks = 2 - 5 = -3`).
9. **Bricks Are Depleted:**
   - Our brick count goes below 0, which means we cannot proceed further using bricks.
10. **Conclusion:**
    - We are currently at index 4 (`heights[4] = 9`) and can't move to index 5 because we have a negative brick count. The furthest index we could reach is 4.

In the given example, the algorithm allows us to move as far as possible, using ladders for the most significant height differences when necessary and bricks for the smallest one until the bricks run out. The index 4 is the farthest building we can reach given the constraints of our `bricks` and `ladders`.

Python Solution

```python
1  from heapq import heappush, heappop
2
3  class Solution:
4      def furthestBuilding(self, heights, bricks, ladders):
5          """
6          This method determines how far you can reach by climbing buildings of various heights using a given number of bricks and lad
7
8          :param heights: A list of integers representing the heights of the buildings
9          :param bricks: The total number of bricks available to climb up the buildings
10         :param ladders: The total number of ladders available to climb up the buildings
11         :return: The index of the furthest building that can be reached
12         """
13         # A priority queue (min heap) to store the heights that we have used ladders for.
14         height_diffs_heap = []
15
16         for i in range(len(heights) - 1):
17             current_height = heights[i]
18             next_height = heights[i + 1]
19             # Calculate the height difference between the current building and the next one.
20             height_diff = next_height - current_height
21
22             # We use a ladder and add the height difference to the heap.
23             heappush(height_diffs_heap, height_diff)
24             # If we have used more ladders than available, we must replace one ladder with bricks.
25             if len(height_diffs_heap) > ladders:
26                 bricks -= heappop(height_diffs_heap)  # Replace the ladder for the smallest height diff.
27                 # If at any point we do not have enough bricks, we cannot move to the next building.
28                 if bricks < 0:
29                     return i
30
31         # If we can climb all the buildings with the given bricks and ladders, return the last building index.
32         return len(heights) - 1
```

Java Solution

```java
1  class Solution {
2      public int furthestBuilding(int[] heights, int bricks, int ladders) {
3          // Create a priority queue to store the heights that we can climb using ladders.
4          PriorityQueue<Integer> heightDifferences = new PriorityQueue<>();
5
6          // Get the number of buildings from the heights array.
7          int numberOfBuildings = heights.length;
8
9          // Iterate through the array of building heights.
10         for (int i = 0; i < numberOfBuildings - 1; i++) {
11             // Current building height and the next building height.
12             int currentHeight = heights[i];
13             int nextHeight = heights[i + 1];
14
15             // Calculate the height difference between the current and next building.
16             int diff = nextHeight - currentHeight;
17
18             // If the next building is taller, a climb is needed.
19             if (diff > 0) {
20                 // Add the height difference to the priority queue.
21                 heightDifferences.offer(diff);
22
23                 // If we have used more ladders than available, we use bricks.
24                 if (heightDifferences.size() > ladders) {
25                     // Remove the smallest height difference and use bricks to climb up.
26                     bricks -= heightDifferences.poll();
27
28                     // If we do not have enough bricks to climb, return the current index.
29                     if (bricks < 0) {
30                         return i;
31                     }
32                 }
33             }
34         }
35
36         // If we can climb all buildings, return the last building index.
37         return numberOfBuildings - 1;
38     }
39 }
```

C++ Solution

```cpp
1  #include <vector>
2  #include <queue>
3  using namespace std;
4
5  class Solution {
6  public:
7      int furthestBuilding(vector<int>& heights, int bricks, int ladders) {
8          // Min-heap to keep track of the minimum heights we have had to jump using ladders
9          priority_queue<int, vector<int>, greater<int>> min_heap;
10         int buildingCount = heights.size(); // Total number of buildings
11
12         // Go through each building except the last one
13         for (int i = 0; i < buildingCount - 1; ++i) {
14             int current_height = heights[i];     // Height of the current building
15             int next_height = heights[i + 1];    // Height of the next building
16             int height_difference = next_height - current_height; // Calculate the height difference
17
18             if (height_difference > 0) { // If the next building is taller
19                 min_heap.push(height_difference); // Use a ladder for now to climb up
20                 if (min_heap.size() > ladders) { // If we've simulated using more ladders than we have
21                     bricks -= min_heap.top();    // Replace one ladder use with bricks
22                     min_heap.pop();              // Remove the smallest height difference we overcame with a ladder
23                     if (bricks < 0) { // If we don't have enough bricks to go to the next building
24                         return i; // Return the index of the current building
25                     }
26                 }
27             }
28         }
29         // If we manage to consider all the buildings, return the index of the last building
30         return buildingCount - 1;
31     }
32 };
```

Typescript Solution

```typescript
1  function furthestBuilding(heights: number[], bricks: number, ladders: number): number {
2      // Since TypeScript does not have a built-in priority queue, we'll use an array to simulate it.
3      let minHeap: number[] = []; // This will function as our min-heap.
4
5      const buildingCount = heights.length; // Total number of buildings.
6
7      // Helper function to simulate the operation of the priority queue.
8      function pushHeap(value: number) {
9          minHeap.push(value);
10         minHeap.sort((a, b) => a - b); // Sort to keep the smallest elements at the start.
11     }
12
13     // Helper function to simulate the pop operation of the priority queue.
14     function popHeap() {
15         minHeap.shift(); // Remove the smallest element, akin to popping from a min-heap.
16     }
17
18     // Go through each building except the last one.
19     for (let i = 0; i < buildingCount - 1; ++i) {
20         const current_height = heights[i];     // Height of the current building.
21         const next_height = heights[i + 1];    // Height of the next building.
22         const heightDifference = next_height - current_height; // Calculate the height difference.
23
24         if (heightDifference > 0) { // If the next building is taller.
25             pushHeap(heightDifference); // Use a ladder, represented by storing heightDifference.
26             if (minHeap.length > ladders) { // If we've simulated using more ladders than we have.
27                 bricks -= minHeap[0]; // Replace one ladder use with bricks.
28                 popHeap(); // Remove the smallest height difference we overcame with a ladder.
29                 if (bricks < 0) { // If we don't have enough bricks to reach the next building.
30                     return i; // Return the index of the current building.
31                 }
32             }
33         }
34     }
35     // If able to consider all the buildings, return the index of the last building.
36     return buildingCount - 1;
37 }
38
39 // Example usage:
40 // const result = furthestBuilding([4, 2, 7, 6, 9, 14, 12], 5, 1);
41 // console.log(result); // Outputs the index of the furthest building that can be reached.
```

Time and Space Complexity

Time Complexity:

The function `furthestBuilding` iterates through the `heights` array once, which has n elements (n being the number of buildings). For each building, it may add a height difference to a min-heap:

- The for-loop iterates $n - 1$ times as it skips the last building. We know that inserting into a heap is $O(\log k)$, where k is the number of elements in the heap. In the worst case, the heap size could be equal to the number of ladders (l). Thus, the worst-case time for insertion over $n - 1$ iterations is $O((n - 1) * \log l)$.
- The number of removals from the heap is at most equal to the number of ladders l, so the total time for all removals is $O(l * \log l)$ assuming each removal is followed by a heapify operation, which is $O(\log l)$.

Combining these, since l is less than or equal to $n - 1$, we get the total time complexity to be $O(n \log l)$.

Space Complexity:

The space complexity is mostly determined by the min-heap that stores the height differences. In the worst case, the heap could store as many elements as there are ladders, so the space complexity is $O(l)$.