Problem Description

You are given an array of integers named pref that has a length of n. Your task is to find and return another integer array called arr that also has the size n. This arr array should meet a specific requirement: Each element at index i in the pref array must be equal to the cumulative bitwise XOR of elements from 0 to 1 in the arr array. The bitwise XOR operation is represented by the ^ symbol and combines bits where the result is 1 if only one of the bits compared is 1, and 0 otherwise.

Leetcode Link

For example, if pref[i] equals 5, it means that arr[0] ^ arr[1] ^ ... ^ arr[i] must also be equal to 5.

It's important to note that there is only one unique solution to this problem. Your goal is to construct the arr array that will satisfy the given condition for each element in pref.

Intuition

crucial property of XOR is that it is self-inverse, meaning that for any number x, we have x ^ x = 0. So, if we XOR a number with itself, we get 0. Given the definition of pref[i] as arr[0] ^ arr[1] ^ ... ^ arr[i], we can deduce arr[i] using pref[i - 1] and pref[i]. Because

Now let's think about how to arrive at the solution. The key observation here is to recognize the properties of the XOR operation. One

if we have pref[i-1] as arr[0] ^ arr[1] ^ ... ^ arr[i-1], then pref[i] = (arr[0] ^ arr[1] ^ ... ^ arr[i-1]) ^ arr[i]. Now if we XOR pref[i-1] with pref[i], we can isolate arr[i] because (arr[0] ^ ... ^ arr[i-1]) ^ (arr[0] ^ ... ^ arr[i-1] ^ arr[i]) will cancel out all terms except arr[i]. Hence, we start with arr[0] which is just pref[0] since arr[0] exclusively XORed with nothing is arr[0]. Then, for subsequent

The Python code provided uses a list comprehension that takes pairs of elements from [0] + pref (we add a 0 at the beginning for convenience in calculating arr [0]) and performs the XOR operation between adjacent elements of pref. The pairwise utility

list that meets the condition defined by the pref array. Solution Approach

generates pairs of elements from the given list, which the list comprehension processes. The function returns the constructed arr

break down the implementation step-by-step to understand it better.

 First, is the initialization of the result array. The first element of arr can immediately be determined because pref[0] = arr[0]. Therefore, no calculation is needed for the first element.

The solution involves a simple but clever use of properties of the XOR operation in combination with Python's built-in functions. Let's

- Then we use a list comprehension to build the rest of the arr array. List comprehensions are a concise way to create lists in Python, and in this case, it is used to iterate through pairs of elements from the input list pref.
- These pairs are generated using the pairwise utility, which groups every two adjacent items together. Since pairwise is not a default function in Python, it is assumed to be a hypothetical utility that would perform this action. A more accurate Python code to achieve the same without pairwise would look like this:
- 1 [pref[i] ^ pref[i-1] for i in range(1, len(pref))] This code iterates over the pref array from the second element to the last, XORing each element pref[i] with its previous

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element pref[i-1]. The iteration starts from 1 because we are interested in pairs and the first element is already processed.
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we apply pairwise XOR as per the solution, we get arr as follows:

elements, we calculate arr[i] as pref[i-1] ^ pref[i].

subsequent elements, we use the XOR operation to derive them from the cumulative XOR values in pref. • To demonstrate the XOR operation's effect, consider pref to be [1, 2, 3]. After prepending a 0, it becomes [0, 1, 2, 3]. When

• Before executing the XOR operation, we prepare the list by adding a 0 to the beginning of the pref list. This is a critical step

because it allows us to obtain the first element of arr (which is equal to pref[0]) without changing the algorithm. For

- $1 \text{ arr}[0] = 0 ^ 1 = 1$ $3 \operatorname{arr}[2] = 2 ^ 3 = 1$
- Finally, by iterating through these pairs, we XOR them to reconstruct each element of arr and derive the singular unique solution as proven by the properties of XOR.

Hence, arr = [1, 3, 1].

Example Walkthrough

Let's take a small example to illustrate the solution approach. Suppose we are given the following pref array: 1 pref = [5, 1, 7]

In essence, the algorithm relies heavily on the understanding of how XOR functions as an associative and commutative operation,

and on Python's ability to elegantly iterate through elements and perform operations using list comprehensions.

We start by setting arr [0] to pref [0] because there are no previous elements to XOR with, as described in the Intuition section.

Thus: 1 arr[0] = pref[0] = 5

Our goal is to construct an arr array such that pref[i] equals the cumulative XOR from arr[0] to arr[i].

we can isolate arr[1] as follows: 1 arr[1] = pref[0] ^ pref[1] = 5 ^ 1 = 4

Next, we need to determine arr[1]. We use the fact that pref[1] is the XOR of arr[0] and arr[1]. Since pref[1] is 1 and arr[0] is 5,

```
Now we have constructed the array arr:
```

1 arr = [5, 4, 6]

We continue this process to find arr[2]:

1 arr[2] = pref[1] ^ pref[2] = 1 ^ 7 = 6

Let's verify that this arr satisfies the original problem conditions. To do this, we check the cumulative XOR for each index 1 in arr:

```
    For i = 1: arr[0] ^ arr[1] equals 5 ^ 4, which is 1, matching pref[1].

    For i = 2: arr[0] ^ arr[1] ^ arr[2] equals 5 ^ 4 ^ 6, which is 7, matching pref[2].
```

For i = 0: arr[0] is 5, which matches pref[0].

1. Initialize the arr array by setting arr[0] to pref[0].

As we can see, each pref[i] is equal to the cumulative XOR of elements from 0 to i in the constructed arr, validating our solution.

By following this approach, we have successfully solved the problem by understanding the behavior of the XOR operation and

applying it systematically.

class Solution:

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def find_array(self, pref):

return orig_array

orig_array_with_zero = [0] + pref

To summarize the steps:

Python Solution

Initialize an array with a leading zero that will be used

for computing the original array based on the prefix XOR array.

orig_array = [a ^ b for a, b in pairwise(orig_array_with_zero)]

1 # The following import is necessary to use the pairwise utility. # It creates an iterator that returns consecutive pairs of elements from the input. 3 from itertools import pairwise

2. Iterate through the pref array from index 1 to n-1, where n is the number of elements in pref.

4. The resultant arr array will have the same size as pref and will meet the required condition.

3. Calculate arr[i] using the formula arr[i] = pref[i-1] ^ pref[i] for each i.

Compute the original array by XORing each consecutive pair of elements. # This reverses the prefix XOR operation since a^a=0 and a^0=a. 12 # The resulting array is the original array that was used to compute 13 # the prefix XOR array. 14

```
20 # If pref = [1, 3, 5]
21 # The Solution().find_array(pref) will return the original array [1, 2, 7].
22
```

Java Solution

19 # An example usage:

```
class Solution {
       // Method to find the original array from its prefix XOR array
       public int[] findArray(int[] prefixXorArray) {
           // Number of elements in the prefix XOR array
           int length = prefixXorArray.length;
           // Initialize the array to store the original array elements
8
           int[] originalArray = new int[length];
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10
           // The first element of the original array is the same as the first element of the prefix XOR array
           originalArray[0] = prefixXorArray[0];
12
13
14
           // Iterate through the prefix XOR array starting from the second element
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           for (int i = 1; i < length; ++i) {
               // Each element of the original array is obtained by XORing the current and previous elements of the prefix XOR array
16
               originalArray[i] = prefixXorArray[i - 1] ^ prefixXorArray[i];
17
18
19
20
           // Return the original array
21
           return originalArray;
22
23 }
24
```

// Function to find the original array from its prefix XOR array. std::vector<int> findArray(std::vector<int>& prefixXor) { // The size of the prefix XOR array. int size = prefixXor.size();

public:

class Solution {

C++ Solution

#include <vector> // Required for using the std::vector

// doesn't change (ans[0] = pref[0] since XOR with 0 is a no-op).

answerArray[i] = prefixArray[i - 1] ^ prefixArray[i];

// XOR the current element with the previous element of prefixArray

// and store the result in the answerArray, effectively computing the

for (let i = 1; i < prefixArray.length; i++) {</pre>

// original array before the prefix sums.

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           // Initialize the resultant array with the first element from prefixXor,
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           // since the first element of both the original and prefix XOR arrays would be the same.
11
12
           std::vector<int> originalArray = {prefixXor[0]};
13
14
           // Iterating over the prefixXor array starting from the second element.
           for (int i = 1; i < size; ++i) {
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               // The current original array element is the XOR of the previous and current elements
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17
               // in the prefixXor array because the prefixXor[i] represents the XOR of all elements
               // in originalArray from 0 to i, so "undoing" the previous XOR (prefixXor[i-1]) will
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19
               // give us the original value.
20
               originalArray.push_back(prefixXor[i - 1] ^ prefixXor[i]);
21
23
           // Return the fully populated originalArray.
24
           return originalArray;
25
26 };
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Typescript Solution
   function findArray(prefixArray: number[]): number[] {
       // Create a copy of the prefixArray to hold the answer.
       let answerArray = prefixArray.slice();
       // Iterate over the prefixArray starting from index 1, as the first element
```

12 13 // Return the resultant array after reversing the prefix sum operation. 14 return answerArray; 15

16 } 17 // Example usage: // const result = findArray([1,3,2,3]); // Should return [1,2,0,1] 20 Time and Space Complexity The given code snippet implements a function to find an array from its prefix XOR array. The time and space complexities of the code can be analyzed as follows:

the pref array plus an extra element (0 appended to the front), performing a constant-time XOR operation for each pair of elements.

complexity of O(n) due to the reasons mentioned above.

Time Complexity

Space Complexity

The space complexity of the function is O(n) as well, because it creates a new list with the same number of elements as the input

The time complexity is O(n), where n is the length of the input pref array. This is because the function executes a single loop through

list. This new list is populated with the results of the XOR operations between adjacent elements of the extended list [0] + pref. In the case of the pairwise function, which is usually imported from the itertools module (not explicitly shown in the code), if it is implemented in such a way that it yields pairs of elements on-the-fly without creating a separate list or collection for them, the additional space overhead is 0(1) (constant space). However, the resulting list still retains the time complexity of 0(n) and space