## **Leetcode Link**

# **Problem Description** The problem gives us an integer array called nums which is sorted in ascending order. Our task is to convert this sorted array into a

height-balanced binary search tree (BST). A height-balanced binary tree is defined as a binary tree in which the depth of the two subtrees of every node never differs by more than one. Intuition

The solution to the problem lies in the properties of a binary search tree and the characteristics of a sorted array. A binary search tree is a node-based binary tree where each node has the following properties:

The left and right subtrees must also be binary search trees.

The left subtree of a node contains only nodes with keys less than the node's key.

The right subtree of a node contains only nodes with keys greater than the node's key.

- The challenge is to ensure that the BST is height-balanced. To achieve this, we need to pick the middle element from the sorted
- are greater, form the right subtree.

To construct the BST, we apply a recursive strategy: 1. Find the middle element of the current segment of the array. 2. Make this element the root of the current subtree.

array and make it a root, so that the elements to the left, which are lesser, form the left subtree, and the elements to the right, which

4. Recursively perform the same action on the right half of the array to create the right subtree.

right subtrees as its children is returned.

to 2. Hence, the middle element is nums [2], which is 0.

3. We create a TreeNode with a value of 0. This is the root of our BST.

- This divide and conquer approach will ensure that the tree remains height-balanced, as each subtree is constructed from segments
- of the array that are roughly half the size of the original segment.
- By carefully selecting the middle element of the array as the root for each recursive step, the resulting tree satisfies the conditions of a binary search tree as well as being height-balanced.

3. Recursively perform the same action on the left half of the array to create the left subtree.

**Solution Approach** To implement the solution using the given Python code, the following steps are taken, which relate to the concepts of depth-first

search (DFS) and recursion: 1. A recursive helper function called dfs is defined, which takes two parameters, 1 and r, which represent the left and right bounds of the segment of the nums array that we are currently considering. This function is responsible for creating nodes in the BST.

# 2. The base case for the recursive function is checked: if 1 > r, it means we have considered all elements in this segment, and

there is nothing to create a node with. Therefore, None is returned, indicating the absence of a subtree. 3. The middle index of the current segment is found using the expression  $(1 + r) \gg 1$ , which is equivalent to finding the average

2. 4. The middle element of nums, located at index mid, is the value of the root node for the current segment of the array. A TreeNode is

of 1 and r and then taking the floor of the result. The bitwise right shift operator >> is used here to efficiently divide the sum by

created with this value. 5. To build a binary search tree, we need to recursively build the left and right subtrees. The recursive dfs call for the left subtree

6. After the left and right subtrees are created via recursion, a new TreeNode with nums [mid] as its value and the created left and

uses the bounds 1 to mid - 1, while the recursive dfs call for the right subtree uses the bounds mid + 1 to r.

strictly less than or greater than the root of any subtree, thus satisfying all the properties of the BST.

Let's use a small example to illustrate the solution approach. We are given the following sorted array:

the input array nums as the bounds for the entire tree. This approach efficiently builds the binary search tree by always dividing the array into two halves, ensuring the tree is balanced. The tree's properties as a binary search tree are maintained because we construct the left and right subtrees from elements that are

7. The outer function sortedArrayToBST initializes the construction process by calling dfs(0, len(nums) - 1) with the full range of

bounds of the current array segment at each step, simplifying the complexity of the task at each recursive call. **Example Walkthrough** 

The choice of using a recursive function encapsulates the logic for both creating TreeNode instances and ensuring that we honor the

Using the steps outlined in the solution approach, we would construct a height-balanced BST as follows: 1. We first call the dfs function with the initial bounds set to l = 0 and r = 4 (assuming zero-based array indexing).

2. We find the middle element of nums between indices 0 and 4. The midpoint calculation would be (0 + 4) >> 1, which simplifies

For this subarray, we take the middle element as the root for the left subtree. The midpoint is (0 + 1) >> 1, simplifying to 0.

### 4. Now we need to build the left subtree. We make a recursive dfs call with the new bounds, l = 0 and r = 1 (mid - 1), focusing on the subarray [-10, -3].

right subtree of 0.

binary search tree property.

self.value = value

self.right = right

def sortedArrayToBST(self, nums):

self.left = left

nums : List[int]

Args:

left\_index : int

right\_index : int

if left\_index > right\_index:

middle\_index = (left\_index + right\_index) // 2

# Recursively constructing the left subtree.

# Recursively constructing the right subtree.

return None

def \_\_init\_\_(self, value=0, left=None, right=None):

subtrees of every node never differ by more than one.

Converts a sorted array into a height-balanced binary search tree (BST).

An integer array which is sorted in non-decreasing order.

The starting index of the subarray to be processed.

left\_subtree = convert\_to\_bst(left\_index, middle\_index - 1)

# Choosing the middle element of the subarray to be the root of the BST.

A height-balanced binary tree is a binary tree in which the depth of the two

1 nums = [-10, -3, 0, 5, 9]

The element at that index in nums is -10, so we create a TreeNode with value -10.  $\circ$  For the left child of -10, the dfs call with l = 0 and r = -1 returns None since l > r.

subarray is 1 and the element at that index is -3, so -3 becomes the right child node of -10.

 $\circ$  The left child of 5 would be None since a recursive call with bounds 1 = 3 and r = 2 returns None.

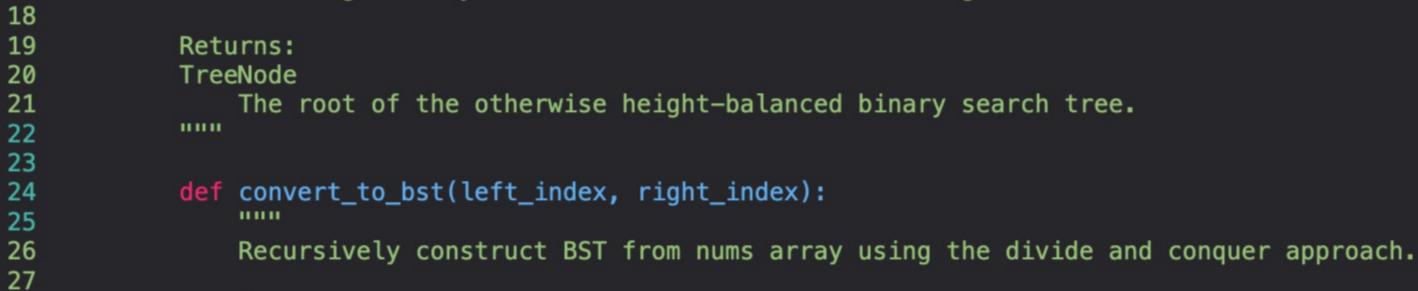
5. Returning to our root 0, we build the right subtree with a new dfs call using the bounds l = 3 (mid + 1) and r = 4, focusing on the subarray [5, 9].

 $\circ$  For the right child, we have nums [mid + 1] where mid is 0. We make a recursive call with l = 1 and r = 1. mid for this

 For the right child, the new midpoint is 4 (mid + 1 where mid = 3), leading to the element 9 being selected. Hence, 9 is the right child node of 5. 6. At this point, we have successfully constructed all parts of the BST, which would look like this:

• The midpoint here is (3 + 4) >> 1, which is 3. The element at index 3 in nums is 5. So, 5 becomes the left child node of the

- By following these steps, we have successfully transformed the sorted array nums into a height-balanced BST. The recursive process ensures that each subtree is constructed from the middle of the subarray it refers to, making the tree balanced and maintaining the
- **Python Solution** class TreeNode: # Definition for a binary tree node.



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class Solution:

Args:

32 The ending index of the subarray to be processed. 33 34 Returns: 35 TreeNode 36 The constructed BST node (root for the subarray). 37 1111111 # Base case: If the left index is greater than the right index, 38 # the subarray is empty, and there is no tree to construct. 39

## 51 53 54

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                right_subtree = convert_to_bst(middle_index + 1, right_index)
               # Creating the root node with the middle element, passing the
               # left and right subtrees as its children.
                return TreeNode(nums[middle_index], left_subtree, right_subtree)
55
56
           # Initiating the recursive function with the whole array range.
            return convert_to_bst(0, len(nums) - 1)
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Java Solution
 1 /**
    * Definition for a binary tree node.
    */
   class TreeNode {
       int val; // Node value
       TreeNode left; // Left child
       TreeNode right; // Right child
 8
       // Constructor
 9
       TreeNode() {}
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12
       // Constructor with value
13
       TreeNode(int val) { this.val = val; }
14
       // Constructor with value, left child, and right child
15
       TreeNode(int val, TreeNode left, TreeNode right) {
16
17
           this.val = val;
           this.left = left;
18
           this.right = right;
19
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21 }
22
23
   class Solution {
24
       private int[] nums;
25
26
        * Convert a sorted array into a height-balanced binary search tree.
27
28
29
        * @param nums Sorted array of integers
        * @return Root of the height-balanced binary search tree
30
31
        */
32
       public TreeNode sortedArrayToBST(int[] nums) {
33
            this.nums = nums;
34
            return constructBSTRecursive(0, nums.length - 1);
35
36
37
       /**
38
        * Recursive helper method to construct BST from the sorted array.
39
        * @param left The starting index of the subarray
40
        * @param right The ending index of the subarray
41
        * @return The root of the BST subtree constructed from subarray
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43
        */
       private TreeNode constructBSTRecursive(int left, int right) {
44
           // Base case: If left > right, the subarray is empty and should return null
45
           if (left > right) {
46
```

// Find the middle element to maintain BST properties. Use `left + (right - left) / 2`

// Create a new TreeNode with the mid element and the previously constructed left and right subtrees

#### 15 public: /\*\* 16 17 18

C++ Solution

struct TreeNode {

int val;

return null;

return node;

\* Definition for a binary tree node.

// to avoid integer overflow

int mid = left + (right - left) / 2;

// Recursively construct the left subtree

// Recursively construct the right subtree

TreeNode leftSubtree = constructBSTRecursive(left, mid - 1);

TreeNode rightSubtree = constructBSTRecursive(mid + 1, right);

TreeNode node = new TreeNode(nums[mid], leftSubtree, rightSubtree);

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TreeNode *left;
       TreeNode *right;
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       // Constructor for a tree node with a given value and optional left and right children.
 9
       TreeNode(int x, TreeNode *left = nullptr, TreeNode *right = nullptr)
10
            : val(x), left(left), right(right) {}
11
12 };
13
   class Solution {
        * Converts a sorted array into a binary search tree with minimal height.
        * @param nums The vector of integers sorted in non-decreasing order.
19
        * @return A pointer to the root of the constructed binary search tree.
20
       TreeNode* sortedArrayToBST(vector<int>& nums) {
21
22
           // Recursive function that converts a subarray into a BST.
23
            function<TreeNode*(int, int)> convertToBST = [&](int leftIndex, int rightIndex) -> TreeNode* {
               // Base case: if left index is greater than right, the subarray is empty and returns nullptr.
24
25
               if (leftIndex > rightIndex) {
                    return nullptr;
26
27
28
               // Choose the middle element as the root to maintain minimal height.
29
30
               int mid = leftIndex + (rightIndex - leftIndex) / 2;
31
32
               // Recursively construct the left subtree.
33
               auto leftChild = convertToBST(leftIndex, mid - 1);
34
35
               // Recursively construct the right subtree.
               auto rightChild = convertToBST(mid + 1, rightIndex);
37
38
               // Create and return the current tree node with its left and right children.
               return new TreeNode(nums[mid], leftChild, rightChild);
           };
40
41
           // Start the recursive process with the full array range.
           return convertToBST(0, nums.size() - 1);
43
45 };
46
Typescript Solution
   interface TreeNode {
       val: number;
       left: TreeNode | null;
       right: TreeNode | null;
 6
    * Converts a sorted array into a height-balanced binary search tree.
```

#### **if** (length === 0) { 17 return null; 18 19

```
* @param {number[]} nums - A sorted array of numbers.
    * @return {TreeNode | null} - The root node of the constructed BST, or null if the array is empty.
   function sortedArrayToBST(nums: number[]): TreeNode | null {
       // Determine the length of the array.
       const length = nums.length;
14
       // Base Case: If array is empty, return null.
20
       // Find the middle index of the array.
       const middleIndex = Math.floor(length / 2);
23
       // Recursively construct the BST by choosing the middle element of the
       // current subsection as the root, and the left and right subsections as the left and right subtrees.
25
26
       const rootNode = {
           val: nums[middleIndex],
           left: sortedArrayToBST(nums.slice(0, middleIndex)),
           right: sortedArrayToBST(nums.slice(middleIndex + 1))
29
       };
30
31
32
       // Return the root node of the BST.
33
       return rootNode;
34 }
35
   // Note: No class has been defined as per the instructions.
   // TreeNode and sortedArrayToBST are both defined in the global scope.
38
```

Time and Space Complexity

The space complexity of the code is also 0(n) if we consider the space required for the output BST. However, if we only consider the auxiliary space (excluding the space taken by the output), it is O(log n) in the best case (which is the height of a balanced BST). The worst-case space complexity would be O(n) if the binary tree is degenerated (i.e., every node only has one child) which would be the case if the input list is sorted in strictly increasing or decreasing order.

The time complexity of the given code is O(n), where n is the number of elements in the input list nums. This is because each element

of the array is visited exactly once to construct each node of the resulting binary search tree (BST).