552. Student Attendance Record II **Dynamic Programming**

Problem Description

The problem asks us to determine the number of possible attendance records of length n that allows a student to be eligible for an attendance award. A record is represented by a string consisting of the characters 'A' for absent, 'L' for late, and 'P' for present. A student qualifies for an award if they satisfy two conditions:

Leetcode Link

- 1. They are absent for fewer than 2 days in total. 2. They are not late for 3 or more consecutive days.
- We must return the count of such attendance records modulo $10^9 + 7$, as this number could be very large.

Intuition

To arrive at the solution, we can use Dynamic Programming (DP). Since we need to keep track of absent and late counts, we can use

days.

Hard

representing whether the student has been absent 0 or 1 times, and 'k' representing the count of the latest consecutive late days (0, 1, or 2). Thinking through the possible cases:

• The student can be present (P) on any given day, which doesn't affect their absences or increase the count of consecutive late

a 3-dimensional DP array, where dp[i][j][k] represents the number of permutations of attendance records ending at day 'i', with 'j'

consecutive late days.

• They can be absent (A), which increases the count of absences unless they have already been absent once.

• They can be late (L), which resets the consecutive present day count but has to be carefully added so as not to surpass two

- The base case for the first day (i = 0) needs to be initialized to show that they can be present, late, or absent, but still be eligible for the award.
- By iterating through the days and for each day computing the possible ending in 'P', 'L', or 'A', while adhering to the rules, we can incrementally construct our DP table up to day 'n'.

Finally, the sum of all possible records up to day 'n - 1' considering both absentee scenarios, and not exceeding two consecutive 'L's gives us the total count modulo 10^9 + 7.

Solution Approach The solution uses a dynamic programming approach to keep track of eligible attendance records by constructing a 3D DP array dp

with dimensions n, 2, and 3; where n is the number of days, 2 represents being absent for either 0 or 1 day (j index), and 3 represents

the number of consecutive late days (k index).

Here are the detailed steps of the algorithm:

1. Initialization: The index [i][j][k] in dp corresponds to the day i, absent status j, and consecutive late status k. ∘ Day i = 0: Initialize dp[0][0][0][0], dp[0][0][1], and dp[0][1][0] to 1. This covers the cases where the student is present, late, or absent for the first day.

• For a Present (P) day: Update dp[i][0][0] and dp[i][1][0] to include all records from previous days where the student

• For a Late (L) day: The late status k is incremented by 1, but cannot exceed 2, which represents being late for 3 or more consecutive days. Set dp[i][0][1] to dp[i - 1][0][0], dp[i][0][2] to dp[i - 1][0][1], dp[i][1][1][1] to dp[i - 1][1][0],

2. Filling the DP table: Iterate over days i from 1 to n - 1:

was present, late, or absent, ensuring that they are still eligible.

student to be eligible for an attendance award, modulo 10^9 + 7.

(student was late), and dp[0][1][0] = 1 (student was absent).

Present case, no update needed for this case.

[1] + dp[2][1][2] = 3 + 3 + 1 + 3 + 3 + 1 = 14.

 $dp = [[[0, 0, 0], [0, 0, 0]] for _ in range(n)]$

Iterate over each day starting from the second one.

We can have 0, 1, or 2 'L's (Late) before this 'A'.

dp[i][1][0] = sum(dp[i - 1][0][l] for l in range(3)) % MOD

dp[i][0][1] = dp[i-1][0][0] # One possible 'L' before current day

dp[i][0][2] = dp[i - 1][0][1] # Two possible 'L's before current day

def checkRecord(self, n: int) -> int:

dp[0][0][0] = 1 # Present

dp[0][1][0] = 1 # Absent

private static final int MOD = 1000000007;

long[][][] dp = new long[n][2][3];

// Building the DP table for subsequences of length i

// Adding 'A' to the sequence ending without 'A's and less than 2 'L's

// Adding 'L' to the sequence, considering previous 'L's and 'A's

// Adding 'P' to the sequence, considering previous 'A's and 'L's

ans = (ans + dp[n - 1][j][k]) % MOD; // Aggregate counts

dp[i][1][0] = (dp[i-1][0][0] + dp[i-1][0][1] + dp[i-1][0][2]) % MOD;

dp[i][0][0] = (dp[i-1][0][0] + dp[i-1][0][1] + dp[i-1][0][2]) % MOD;

dp[i][1][0] = (dp[i][1][0] + dp[i - 1][1][0] + dp[i - 1][1][1] + dp[i - 1][1][2]) % MOD;

public int checkRecord(int n) {

dp[0][0][0] = 1; // P

dp[0][0][1] = 1; // L

dp[0][1][0] = 1; // A

for (int i = 1; i < n; i++) {

// Sum up all valid sequences

long ans = 0;

dp[i][0][1] = dp[i - 1][0][0];

dp[i][1][1] = dp[i - 1][1][0];

dp[i][1][2] = dp[i - 1][1][1];

dp[i][0][2] = dp[i - 1][0][1];

for (int j = 0; j < 2; j++) { // 0 or 1 'A's

for (int k = 0; k < 3; k++) { // 0 to 2 trailing 'L's

// Base cases

dp[0][0][1] = 1 # Late

for i in range(1, n):

and adding A scenarios where the student wasn't absent on previous days).

MOD = 10**9 + 7 # Define the modulus for the problem, to prevent overflow.

Base cases: there is one way to have a sequence end in either 'P', 'L', or 'A' on the first day

If the day ends in 'L' (Late), the previous day can have 0 or 1 'L' or be 'P' (Present).

If the day ends in 'A' (Absent), the sequence must not have any 'A's before.

must be returned modulo 10^9 + 7 to fit within the integer range.

dp[i][1][0] by summing up dp[i-1][0][0], dp[i-1][0][1], and dp[i-1][0][2].

- and dp[i][1][2] to dp[i 1][1][1]. • For an Absent (A) day: Only include records from the previous day where the student hasn't been absent before (j=0). Set
- At each step, we take the result modulo $10^9 + 7$ to avoid integer overflow due to large values. 3. Computing the answer: Sum up all the elements dp[n - 1][j][k], where j can be 0 or 1, and k can be 0, 1, or 2, since we want to consider all possible eligible sequences. This sum gives the total number of attendance records of length n that allow a
- 1. Initialization: ○ We start with day i = 0 and initialize our dp array such that dp[0][0][0] = 1 (student was present), dp[0][0][1] = 1

Let's walk through an example using the provided solution approach to calculate the number of valid attendance records for n = 3.

Throughout the implementation, we're using the modulo operation due to the constraints that the answer may be very large and

\circ For day i = 1, we have:

first and P on the second).

2. Filling the DP table:

Example Walkthrough

 Present (P) case: Since the student can be present after any attendance status of the previous day without restrictions, we set dp[1][0][0] = sum(dp[0][0]) = 2 (from being P or L on the first day), and dp[1][1][0] = sum(dp[0][1]) +

sum(dp[0][0]) = 3 (from being P on the first day and A on the second, L on the first and P on the second, or A on the

■ Late (L) case: The student can only be late for a maximum of two consecutive days, so we update dp[1][0][1] (was P

now L) and dp[1][1][1] (was A now L), dp[1][0][1] = dp[0][0][0] = 1 and dp[1][1][1] = dp[0][1][0] = 1.

- Absent (A) case: The student can be absent for at most once, so dp[1][1][0] (was P now A) is already covered in
 - \circ For day i = 2, we repeat the process: ■ Present (P) case: dp[2][0][0] = sum(dp[1][0]) = 3 (from all P and L scenarios of the previous day where the student wasn't absent), and dp[2][1][0] = sum(dp[1][1]) + sum(dp[1][0]) = 4 (from all P and L scenarios of the previous day
- Absent (A) case: dp[2][1][0] = sum(dp[1][0]) = 3 (from all non-absent previous day records). 3. Computing the answer:

(consecutive late count), resulting in the final count: dp[2][0][0] + dp[2][0][1] + dp[2][0][2] + dp[2][1][0] + dp[2][1]

 \circ After filling in the dp table, we sum up all the possibilities on the last day i = 2 considering both j (absent count) and k

■ Late (L) case: Update the dp array considering the consecutive L scenarios, dp[2][0][1] = dp[1][0][0] = 3 and dp[2]

[0][2] = dp[1][0][1] = 1; similarly for j=1, dp[2][1][1] = dp[1][1][0] = 3 and dp[2][1][2] = dp[1][1][1] = 1.

- So, for n = 3, there are 14 valid attendance records that meet the criteria for an awards eligibility, and the final answer modulo 10^9 + 7 would be 14 (since 14 is already less than 10^9 + 7).
- # Initialize a 3D DP array where: # 1st dimention is the day, # 2nd dimention is the absence count (0 or 1, because more than 1 is not allowed), # 3rd dimention is the late count (0, 1, or 2, because more than 2 in a row is not allowed).

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Python Solution

class Solution:

24 dp[i][1][1] = dp[i - 1][1][0] # One 'L', with an 'A' at some point before25 dp[i][1][2] = dp[i - 1][1][1] # Two 'L's, with an 'A' before26 27 # If the day ends in 'P' (Present), there are no constraints for this particular day. 28 for j in range(2): # j=0: no 'A' yet, j=1: there has been an 'A' dp[i][j][0] = sum(dp[i - 1][j][l] for l in range(3)) % MOD29 30 31 # Calculate the total number of valid attendance record combinations 32 # by summing over all possibilities on the last day. 33 total = 0 34 for j in range(2): 35 for k in range(3): 36 total = (total + dp[n - 1][j][k]) % MODreturn total # Return the total number of valid combinations. 37 38 Java Solution

// dp[i][j][k]: number of valid sequences of length i, with j 'A's and a trailing 'L's of length k.

// Previous has no trailing 'L'

// Previous has an 'A' and no trailing 'L'

// Previous has an 'A' and 1 trailing 'L'

// Previous has 1 trailing 'L'

34 35 36 return (int) ans; // Final answer 37 38

1 class Solution {

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C++ Solution
 1 constexpr int MOD = 1e9 + 7;
 3 class Solution {
 4 public:
        int checkRecord(int n) {
            // Define 'll' as shorthand for 'long long' type
 6
            using ll = long long;
            // Create a 3D vector to hold the state information
 8
           // dp[i][j][k] represents the number of valid sequences of length i
 9
            // where j tracks the absence count (0 for no A, 1 for one A)
10
            // and k tracks the late count (0, 1, or 2 consecutive L's)
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            vector<vector<vector<ll>>> dp(n, vector<vector<ll>>>(2, vector<ll>(3)));
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            // base cases for first day
15
            dp[0][0][0] = 1; // P
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            dp[0][0][1] = 1; // L
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            dp[0][1][0] = 1; // A
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            for (int i = 1; i < n; ++i) {
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                // For A: append A after sequences that do not contain A ('j' == 0)
                dp[i][1][0] = (dp[i-1][0][0] + dp[i-1][0][1] + dp[i-1][0][2]) % MOD;
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                // For L: append L after sequences ending in no L or 1 L
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                dp[i][0][1] = dp[i - 1][0][0]; // no L followed by L
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                dp[i][0][2] = dp[i - 1][0][1]; // 1 L followed by another L
                dp[i][1][1] = dp[i-1][1][0]; // no L followed by L, already contains A
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                dp[i][1][2] = dp[i-1][1][1]; // 1 L followed by another L, already contains A
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                // For P: append P after any sequence
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                dp[i][0][0] = (dp[i-1][0][0] + dp[i-1][0][1] + dp[i-1][0][2]) % MOD;
31
                // for sequences that already contain A, append P
32
                dp[i][1][0] = (dp[i][1][0] + dp[i - 1][1][0] + dp[i - 1][1][1] + dp[i - 1][1][2]) % MOD;
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            // Calculate the final result by summing up all possible sequences of length 'n'
36
            ll result = 0;
37
            for (int absence = 0; absence < 2; ++absence) {</pre>
38
                for (int late = 0; late < 3; ++late) {</pre>
39
                    result = (result + dp[n - 1][absence][late]) % MOD;
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            return result;
43
44 };
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dp[i][1][2] = dp[i-1][1][1]; // 1 L followed by another L, already contains A30 31 32 // For P: append P after any sequence 33 dp[i][0][0] = (dp[i-1][0][0] + dp[i-1][0][1] + dp[i-1][0][2]) % MOD;// For sequences that already contain A, append P 34

let result: ll = 0;

return result;

Typescript Solution

2 const MOD: number = 1e9 + 7;

type ll = number;

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);

1 // MOD constant for modulo operation to prevent overflow

// Create a 3D array to hold the state information

let dp: ll[][][] = Array.from({ length: n }, () =>

function checkRecord(n: number): number {

// Base cases for the first day

dp[0][0][0] = 1; // P present

dp[0][0][1] = 1; // L late

dp[0][1][0] = 1; // A absent

for (let i = 1; i < n; ++i) {

// A function to check the number of valid sequences of attendance records of length n

// For A: append A after sequences that do not contain A ('j' == 0)

// For L: append L after sequences ending in no L or 1 L

dp[i][0][2] = dp[i - 1][0][1]; // 1 L followed by another L

result = (result + dp[n - 1][absence][late]) % MOD;

dp[i][0][1] = dp[i - 1][0][0]; // No L followed by L

for (let absence = 0; absence < 2; ++absence) {</pre>

for (let late = 0; late < 3; ++late) {</pre>

dp[i][1][0] = (dp[i-1][0][0] + dp[i-1][0][1] + dp[i-1][0][2]) % MOD;

dp[i][1][1] = dp[i - 1][1][0]; // No L followed by L, already contains A

// Calculate the final result by summing up all possible sequences of length 'n'

dp[i][1][0] = (dp[i][1][0] + dp[i - 1][1][0] + dp[i - 1][1][1] + dp[i - 1][1][2]) % MOD;

// dp[i][j][k] represents the number of valid sequences of length i

// where j tracks the absence count (0 for no A, 1 for one A)

// and k tracks the late count (0, 1, or 2 consecutive L's)

Array.from({ length: 2 }, () => Array(3).fill(0))

// Define 'll' as alias for 'number' type since TypeScript doesn't have 'long long' type

Time and Space Complexity **Time Complexity**

The algorithm uses a dynamic programming approach to calculate the number of ways a student can attend classes over n days without being absent for consecutive 3 days and without being absent for 2 days in total. The time complexity is determined by the triple-nested loops:

 For each day, there are 2 states of absence (either the student has been absent once or not at all), and 3 states for tardiness (the student has not been late, has been late once, or has been late twice).

• The outer loop runs n times, which represents each day.

Hence, the time complexity of the algorithm is 0(2 * 3 * n), which simplifies to 0(n) because the constants can be removed in Big O notation.

The space complexity is determined by the space required to store the dynamic programming states. The dp array is a two-

and lates.

Space Complexity

dimensional array where the first dimension is n, and the second dimension is a 2×3 matrix to store all different states for absences

Therefore, the space complexity is 0(2 * 3 * n), which simplifies to 0(n) as the constants can be disregarded.