Problem Description

In this problem, you are given an integer array called nums and an integer k. Your task is to modify each element in the array by either adding k to it or subtracting k from it. After modifying each element in this manner, the score of the array is defined as the difference between the maximum and minimum elements in the modified array. The objective is to determine the minimum score that can be achieved by any combination of adding or subtracting k to/from the elements of nums.

Suppose nums = [1, 3, 6] and k = 3. You could transform nums as follows:

Here is an example to illustrate:

Adding k to the first element: [1 + 3, 3, 6] = [4, 3, 6]

- Subtracting k from the second element: [4, 3 3, 6] = [4, 0, 6] • Subtracting k from the third element: [4, 0, 6 - 3] = [4, 0, 3]
- The score is then max(4, 0, 3) min(4, 0, 3) = 4 0 = 4.

number in the array after each element has been increased or decreased by k.

Intuition

The problem is asking you to find the minimum score possible, that is, the smallest difference between the highest and lowest

Here's why sorting helps:

The intuition behind the solution involves recognizing that sorting the array can help in minimizing the score. By sorting, you can

• After sorting nums, the smallest and largest elements are nums [0] and nums [-1], respectively. The initial score is nums [-1] nums[0].

ensure that the operation that you perform (addition or subtraction) will not increase the range unnecessarily.

- right of i (including element at i) could be decreased by k. This creates two "blocks" within the array: one with increased values, and one with decreased values. • The new minimum possible value is the minimum of nums [0] + k (left-most element of the increased block) and nums [i] - k
- (left-most element of the decreased block). • The new maximum possible value is the maximum of nums[i - 1] + k (right-most element of the increased block) and nums[-1] k (right-most element of the decreased block).
- By iterating through all possible pivot points (from 1 to len(nums) 1), you can find the minimum score by comparing this with the previously calculated minimum ans.
- The key observation here is that by sorting and choosing an appropriate pivot, one can minimize the difference between the maximum and minimum values affected by the addition or subtraction of k, leading directly to a solution that iterates through possible pivot points to find the minimum score.

Solution Approach

The solution follows a simple yet effective approach leveraging sorting and iteration.

range unnecessarily.

where k is subtracted.

index, based on the given k.

2. Initialize the variable ans with the initial score, which is the difference between the last element and the first element of the sorted array (nums [-1] - nums [0]).

- pivot point where the array is divided into two parts: one that will get the addition of k and the other the subtraction. There is no point in considering index of for this pivot as the sorted array's first element cannot be the start of the subtraction section.
- Calculate the new maximum value mx as the maximum between nums[i 1] + k and nums[-1] k. The nums[i 1] + k is the largest value of the incremented section, and nums[-1] - k is the largest value for the decremented section.
- **Data Structures:**
- Patterns: The use of sorting to establish a predictable order of elements, hence allowing for a methodical approach to finding the solution.

By following these steps, the algorithm ensures that we calculate the minimum range after adding or subtracting k from each

element in the most efficient manner. It elegantly handles the problem by transforming it into a series of operations where we only

need to look at the edges of the two blocks created by the pivot point.

2 k = 5

Example Walkthrough

1 nums = [4, 7, 1]

score (the difference between the maximum and minimum elements of the array). Let's follow the solution approach:

1. Sort the array:

```
3. Iterate through the array starting from index 1:
  For each index i, we will calculate the potential new minimum (mi) and maximum (mx) values after either adding or subtracting k:
```

2. Initialize the score (ans):

```
\circ At index i = 1 (element 4):
```

1 mi = min(nums[0] + k, nums[i] - k) -> mi = min(1 + 5, 4 - 5) -> mi = min(6, -1) -> mi = -1

(No change in ans as the score is still 6 which is not better than the previous score)

2 mx = max(nums[i-1] + k, nums[-1] - k) -> mx = max(1 + 5, 7 - 5) -> mx = max(6, 2) -> mx = 6

 \circ At index i = 2 (element 7):

Now, update the ans:

Python Solution

class Solution:

Java Solution

1 class Solution {

9

10

11

12

13

14

15

16

17

18

19

20

21

6

9

10

11

12

14

23

13

14

12

13

14

15

16

17

18

20

21

34

39

35 // Example usage:

37 // k = 3;

// nums = [1, 3, 6];

Space Complexity

from typing import List

nums.sort()

```
1 ans = min(ans, mx - mi) -> ans = min(6, 9 - 2) -> ans = min(6, 7) -> ans = 6
      Again, the score is 7, which does not improve the ans.
4. Complete the loop: The algorithm has finished checking all possible pivot points in the array.
```

In this example, the modifications to the elements are unnecessary, as the initial score is already minimal. The algorithm efficiently

identifies this by analyzing the potential effects of adding and subtracting k at each pivot point in the sorted array.

to find the minimum possible range. for i in range(1, len(nums)): # Calculate the possible minimum by adding k to the smallest value # and subtracting k from the current value. $possible_min = min(nums[0] + k, nums[i] - k)$

Calculate the possible maximum by adding k to the previous value

// First, sort the input array to deal with numbers in a sorted order.

// Calculate the initial range from the first and last element of the sorted array.

def smallestRangeII(self, nums: List[int], k: int) -> int:

and subtracting k from the maximum value.

smallest_range = nums[-1] - nums[0]

public int smallestRangeII(int[] nums, int k) {

int minRange = nums[n - 1] - nums[0];

// Get the length of the array

for (int i = 1; i < n; ++i) {

Arrays.sort(nums);

int n = nums.length;

First, sort the numbers to organize them in ascending order.

The initial range would be the max value minus the min value.

Loop through the sorted numbers, starting from the second element,

22 23 smallest_range = min(smallest_range, possible_max - possible_min) 24 25 # Finally, return the smallest range after considering all elements. 26 return smallest_range 27

// Calculate the minimum possible value after adding or subtracting k to the current or first element

// Calculate the maximum possible value after adding or subtracting k to the previous or last element

15 int currentMax = Math.max(nums[i - 1] + k, nums[n - 1] - k); // Find the smallest range by comparing the current computed range and the previously stored minimum range 16 17 minRange = Math.min(minRange, currentMax - currentMin); 18 // Return the minimum range found return minRange; 20 21 22 }

// Iterate through the array starting from the second element

int currentMin = Math.min(nums[0] + k, nums[i] - k);

// Defines the function which will find the smallest range after modification int smallestRangeII(vector<int>& nums, int k) { // Initially, sort the array in non-decreasing order sort(nums.begin(), nums.end()); int numsSize = nums.size(); // Store the size of the nums vector // Compute the initial range between the largest and smallest numbers int minRange = nums[numsSize - 1] - nums[0]; 10 11 // Iterate through the sorted numbers starting from the second element

// Determine the new minimum by comparing the increased smallest number

for (int i = 1; i < numsSize; ++i) {</pre>

2 let nums: number[]; let k: number; // Sorts the array in non-decreasing order const sortArray = (a: number, b: number) => a - b; // Finds the smallest range after modification function smallestRangeII(nums: number[], k: number): number { // Sort the array in non-decreasing order 10 nums.sort(sortArray); 11

let minRange: number = nums[numsSize - 1] - nums[0];

// Store the size of the nums array

const numsSize: number = nums.length;

for (let i = 1; i < numsSize; ++i) {</pre>

23 // Determine the new maximum by comparing the increased previous number and the decreased largest number 24 const newMax: number = Math.max(nums[i - 1] + k, nums[numsSize - 1] - k); 26 // Update the minRange with the minimum of the current and new ranges 27 minRange = Math.min(minRange, newMax - newMin); 28 29 30 // Return the smallest range found return minRange; 32 33 }

// Compute the initial range between the largest and smallest numbers

// Iterate through the sorted numbers starting from the second element

const newMin: number = Math.min(nums[0] + k, nums[i] - k);

Time Complexity The time complexity of the provided code depends on the sorting algorithm and the for loop.

// console.log(smallestRangeII(nums, k)); // Output would be the result of the smallestRangeII function

- nums.
- 2. The for loop \rightarrow Iterates through the sorted list once, accounting for a time complexity of O(n). Combining both, the time complexity remains dominated by the sorting step, and therefore, the overall time complexity is 0(n log

1. $nums.sort() \rightarrow The sort operation typically has a time complexity of <math>0(n \log n)$ where n is the number of elements in the list

- The space complexity of the provided code is mainly due to the sorted list.
- 2. No additional data structures are used that are dependent on the number of elements in the list, and therefore, no extra space is utilized that is proportional to the input size.
- Thus, the space complexity of the code is 0(1).

• Consider a pivot point at index i in the sorted array. Everything to the left of i could be increased by k, and everything to the

Algorithm: 1. Sort the nums array. This will help us easily identify the smallest and largest elements and ensures that we do not increase the

- 3. Iterate through the array starting from index 1 up to len(nums) 1. The reason we start at 1 is because we are considering the
 - 4. For each index i, calculate the minimum and maximum values as follows: • Calculate the new minimum value mi as the minimum between nums[0] + k and nums[i] - k. The nums[0] + k represents the smallest possible value after the increment and nums[i] - k represents the smallest value for the section of the array
 - each iteration, we are considering the lowest possible range after applying our operation at each pivot. 6. Once the loop completes, ans contains the minimum score achievable after performing the add or subtract operation at each

5. Update the score (ans) to be the minimum value between the current ans and the difference mx - mi. This ensures that with

- Suppose we have the following nums array and integer k:

The sorted array itself is the primary data structure used. No additional data structures are required.

Decision-making to update the candidate solution (ans) based on comparisons calculated within the loop.

Iteration to explore possible optimal solutions by checking pivot points in the array.

Let's go through the solution approach with a small example to better illustrate the algorithm.

1 nums.sort() \rightarrow nums = [1, 4, 7]

According to the problem, we have to either add k to or subtract k from each element in the array to achieve the smallest possible

Now, we update the ans if mx - mi is smaller than the current ans: 1 ans = min(ans, mx - mi) -> ans = min(6, 6 - (-1)) -> ans = min(6, 7) -> ans = 6

1 ans = nums[-1] - nums[0] -> ans = 7 - 1 -> ans = 6

- 1 mi = min(nums[0] + k, nums[i] k) -> mi = min(1 + 5, 7 5) -> mi = min(6, 2) -> mi = 22 mx = max(nums[i-1] + k, nums[-1] - k) -> mx = max(4 + 5, 7 - 5) -> mx = max(9, 2) -> mx = 9
- 5. **Result**: The ans calculated is 6, which means: 1 The minimum score achievable after adding or subtracting `k` from each element in nums is 6.

possible_max = max(nums[i - 1] + k, nums[-1] - k)# Update the smallest range if a smaller one is found.

```
C++ Solution
1 class Solution {
2 public:
```

```
15
               // and the decreased current number
               int newMin = min(nums[0] + k, nums[i] - k);
16
               // Determine the new maximum by comparing the increased previous number
17
               // and the decreased largest number
               int newMax = max(nums[i - 1] + k, nums[numsSize - 1] - k);
               // Update the minRange with the minimum of the current and new ranges
20
21
               minRange = min(minRange, newMax - newMin);
22
23
24
           // Return the smallest range found
           return minRange;
26
27 };
28
Typescript Solution
1 // Array `nums` holds the numbers and `k` is the allowed modification range
```

// Determine the new minimum by comparing the increased smallest number and the decreased current number

Time and Space Complexity

n).

- 1. $nums.sort() \rightarrow The sort operation in Python is usually done in-place, which means the space complexity is <math>0(1)$.