Problem Description

In this problem, you are given an array of integers called nums. Your task is to determine the number of ways you can remove exactly one element from the array such that, after the removal, the sum of the elements at the odd indices is equal to the sum of the elements at the even indices. The array uses 0-based indexing, which means the first element is at index 0 (even-indexed), the second element is at index 1 (odd-indexed), and so on.

Imagine you have an array like [2, 1, 3, 4]. If you remove the element at index 1 (which is the number 1), the new array would be [2, 3, 4]. In this new array, the sum of the even-indexed values (which are at indices 0 and 2) is 2 + 4 = 6, and the sum of the oddindexed value (which is at index 1) is 3. Since those sums are not equal, this would not be a "fair" array according to the problem definition.

The intuition behind the solution is to efficiently track the sums of odd and even indexed elements as we consider removing each

Intuition

We start by calculating the sum of all elements at even indices (s1) and the sum of all elements at odd indices (s2) for the original array. Once we have the total sums, as we iterate through each element to consider its removal, we can update our totals for what

element. If we just recalculated the sums each time we remove an element, it would be too slow, so we need a smarter approach.

the sums would be if we removed that element. As we remove an element, two scenarios can occur depending on whether the element is at an even or odd index:

all elements to the right will shift left by one index).

and updating all sums every time, we make adjustments based on the running tallies and the totals.

2. If the element is at an odd index, we need to subtract that element's value from the odd sum and add it to the even sum. We keep track of the running tallies of elements removed (t1 for even indices and t2 for odd indices). To avoid shifting all elements

1. If the element is at an even index, we need to subtract that element's value from the even sum and add it to the odd sum (since

We then check if removing the current element makes the sum of even-indexed elements equal to the sum of odd-indexed elements.

If so, we increment our answer count ans. The condition checks depend on the parity of the index and use the already computed sums as well as the tallies for correction. This way, we are able to efficiently process each element and determine if its removal results in a "fair" array without having to

recalculate the entire sum each time. **Solution Approach**

The implementation of the solution revolves around the use of prefix sums, which is a common technique in array manipulation problems, to pre-calculate cumulating values and use them in an efficient way. The solution makes use of several variables: s1 and

The algorithm consists of the following steps:

1. Calculate the initial sums of even and odd indexed elements and store them in s1 and s2. 1 s1, s2 = sum(nums[::2]), sum(nums[1::2])

s2 to keep track of the sum of elements at even indices and odd indices respectively, ans to count the number of ways we can make

the array fair, and t1 and t2 to keep track of the prefix sums (total of removed elements so far) at even and odd indices respectively.

3. Loop through each element in the nums array using their index i and value v.

- 4. Inside the loop, perform checks to determine if removing the element at index i will result in a fair array:
- Check if the index is even (i % 2 == 0). If true, compare t2 + s1 t1 v with t1 + s2 t2. This check is based on the

equal, there is a valid removal, so increment ans.

sum of even-indexed elements plus the prefix sum t2.

idea that, after removal, the total sum of even-indexed elements (s1) would be decreased by v, and the total sum of odd-

1 for i, v in enumerate(nums):

have been removed up to index i.

2. Initialize ans, t1, and t2 to 0.

- Check if the index is odd (i % 2 == 1). If true, compare t2 + s1 t1 with t1 + s2 t2 v. Similar to the previous case,
- ans += i % 2 == 0 and t2 + s1 t1 v == t1 + s2 t2ans += i % 2 == 1 and t2 + s1 - t1 == t1 + s2 - t2 - vt2 += v if i % 2 == 1 else 0 5. Update t1 and t2 with the value v pertaining to their respective index parities. This reflects the running sum of values that would

indexed elements (s2) would need to include what was previously part of t1 before the i-th element. If the two sums are

but in this scenario, we're removing an element from the odd indices, so we adjust \$2 instead of \$1, and compare against the

- The time complexity of this solution is O(n) since it makes a single pass through the array, and the space complexity is O(1), using only a constant amount of extra space for the variables defined. Example Walkthrough
- \circ s1 = sum of elements at even indices = 2 + 3 + 0 = 5

Let's walk through an example to illustrate the solution approach using the array [2, 1, 3, 4, 0].

6. After the loop, ans will contain the total number of indices that could be removed to make nums fair.

3. We start to loop through each element in the nums array. 4. For i = 0 (first element, value v = 2):

2. We initialize ans, t1, and t2 to 0.

This is an even index, so we check if t2 + s1 − t1 − v equals t1 + s2 − t2.

• We then update t1 with the value 2 (since it's an even index), so t1 becomes 2, and t2 remains 0. 5. For i = 1 (second element, value v = 1):

• The condition is 1 == 6, which is false, so ans stays the same.

• We update t1 to 5, adding the value 3 to the previous value of 2.

• The condition is 3 == 5, which is false, so we do not increment ans.

 \circ That is, we check if 0 + 5 - 0 - 2 equals 0 + 5 - 0.

1. We first calculate the initial sums of even and odd indexed elements:

 \circ s2 = sum of elements at odd indices = 1 + 4 = 5

 That is, we check if 0 + 5 − 2 equals 2 + 5 − 0 − 1. • The condition is 3 == 6, which is false, so we do not increment ans. We then update t2 with the value 1 (since it's an odd index), so t2 becomes 1, and t1 remains 2.

This is an odd index, so we compare t2 + s1 − t1 with t1 + s2 − t2 − v.

6. For i = 2 (third element, value v = 3): This is an even index, so the comparison is 1 + 5 − 2 − 3 on the left side and 2 + 5 − 1 on the right side.

the right side, which simplifies to 1 == 9. The condition is false, so ans is still not incremented.

If the current index is even, check if removing the element makes the array fair

A fair array has equal sum of remaining elements at even and odd positions

that the sum of the even-indexed elements is equal to the sum of the odd-indexed elements.

Calculate the initial sum of elements at even indices (odd positions) and

7. Continuing with this process for i = 3 and i = 4, we find that: \circ At i = 4, with value v = 0, given as an even index, the condition would be 1 + 5 - 5 - 0 on the left side and 5 + 5 - 1 on

def waysToMakeFair(self, nums: List[int]) -> int:

for index, value in enumerate(nums):

if index % 2 == 0:

return fair_ways_count

else:

the sum of elements at odd indices (even positions)

If fair, increment the fair ways count

fair_ways_count += is_fair_after_removal

Return the total number of ways the array can be made fair

tempEvenSum += currentValue;

tempOddSum += currentValue;

fairCount++;

// Check if the sums minus the current value are equal

return fairCount; // Return result with the number of ways to make the array fair

// Update the temporary sum for the odd indices

} else {

sum_even_index, sum_odd_index = sum(nums[::2]), sum(nums[1::2])

Enumerate over the list to consider removing each element in turn

Through this example, we can see that we process the array efficiently without recalculating the entire sum for every potential removal. This approach yields the correct answer with a linear time complexity.

8. After the loop is completed, ans contains the value 0, which indicates that there are no ways to remove a single element such

6 # Initialize counters for the number of ways to make the array fair, # the running sum of elements at even indices, and odd indices 8 fair_ways_count = running_sum_even = running_sum_odd = 0 9 10

running_sum_even + sum_odd_index - running_sum_odd)

21 # If the current index is odd, perform a similar check after removing the element 22 is_fair_after_removal = (running_sum_odd + sum_even_index - running_sum_even == running_sum_even + sum_odd_index - running_sum_odd - value) 23 24 fair_ways_count += is_fair_after_removal 25

is_fair_after_removal = (running_sum_odd + sum_even_index - running_sum_even - value ==

```
26
               # Update the running sums for even and odd indices after considering each element
27
               if index % 2 == 0:
28
                    running_sum_even += value
29
               else:
30
                    running_sum_odd += value
```

Python Solution

class Solution:

11

12

13

14

15

16

17

18

19

20

31

32

33

34

31

32

33

34

35

36 37

38

39

40

41

42

43

45

44 }

C++ Solution

```
Java Solution
   class Solution {
       public int waysToMakeFair(int[] nums) {
           int evenSum = 0; // Sum of elements at even indices
           int oddSum = 0; // Sum of elements at odd indices
           int n = nums.length;
           // Calculate the initial sum of even and odd indexed numbers
           for (int i = 0; i < n; ++i) {
               if (i % 2 == 0) {
                   evenSum += nums[i];
10
               } else {
                   oddSum += nums[i];
12
13
14
15
           int tempEvenSum = 0; // Temporary sum for even indices
16
           int tempOddSum = 0; // Temporary sum for odd indices
           int fairCount = 0;
18
19
20
           // Check each index to see if removing it would make the array fair
21
           for (int i = 0; i < n; ++i) {
               int currentValue = nums[i];
22
24
               // If the index is even, removing it would change the balance of sums
               if (i % 2 == 0) {
25
26
                   // Check if the sums minus the current value are equal
27
                   if (tempOddSum + evenSum - tempEvenSum - currentValue == tempEvenSum + oddSum - tempOddSum) {
28
                       fairCount++;
29
                   // Update the temporary sum for the even indices
30
```

if (tempOddSum + evenSum - tempEvenSum == tempEvenSum + oddSum - tempOddSum - currentValue) {

```
#include <vector>
   class Solution {
   public:
       int waysToMakeFair(std::vector<int>& nums) {
           int sumEven = 0, sumOdd = 0; // Initialize sums of even and odd indices
           int n = nums.size();
           // Calculate the total sum of elements at even and odd indices
           for (int i = 0; i < n; ++i) {
10
               if (i % 2 == 0) {
11
                   sumEven += nums[i];
12
13
               } else {
                   sumOdd += nums[i];
14
15
16
17
           int prefixSumEven = 0, prefixSumOdd = 0; // Prefix sums for even and odd indices
18
           int countFairIndices = 0; // This will hold the result - number of fair indices
20
21
           // Loop to find all indices where removing the element would make the array fair
           for (int i = 0; i < n; ++i) {
22
23
               int currentValue = nums[i];
24
               if (i % 2 == 0) {
                   // Check if removing an element from even index makes sums equal
25
26
                   if (prefixSumOdd + (sumEven - prefixSumEven - currentValue) == (prefixSumEven + sumOdd - prefixSumOdd)) {
27
                       countFairIndices++;
28
29
                   prefixSumEven += currentValue; // Update prefix sum for even index
30
               } else {
                   // Check if removing an element from odd index makes sums equal
31
32
                   if ((prefixSumOdd + sumEven - prefixSumEven) == (prefixSumEven + sumOdd - prefixSumOdd - currentValue)) {
33
                        countFairIndices++;
34
35
                   prefixSumOdd += currentValue; // Update prefix sum for odd index
36
37
38
           return countFairIndices; // Return the result
39
40 };
41
Typescript Solution
  1 /**
     * Calculates the number of ways to delete exactly one element from the
     * array so that the sum of the elements at the odd indices of the new array
```

24 25 26

```
* is equal to the sum of the elements at the even indices of the new array.
     * @param {number[]} nums - The input array.
     * @return {number} - The number of ways to make the array fair.
    var waysToMakeFair = function(nums: number[]): number {
         // Variables to keep track of even and odd sums.
 10
         let evenSumOriginal: number = 0;
         let oddSumOriginal: number = 0;
 11
 12
         let tempEvenSum: number = 0;
 13
         let tempOddSum: number = 0;
 14
 15
         const length = nums.length;
 16
 17
         // Calculate initial sums for even and odd indices.
         for (let i = 0; i < length; ++i) {</pre>
 18
 19
             if (i % 2 === 0) {
                 evenSumOriginal += nums[i];
 20
 21
             } else {
 22
                 oddSumOriginal += nums[i];
 23
         let fairWaysCount = 0;
 27
 28
         // Iterate through the array and count the ways to make the array fair
 29
        // by testing the condition after removing each element.
         for (let i = 0; i < length; ++i) {</pre>
 30
             const value = nums[i];
 31
 32
 33
             // When removing an element at an even index, check if the sum without that
 34
             // element makes the array fair.
 35
             if (i % 2 === 0 && tempOddSum + evenSumOriginal - tempEvenSum - value === tempEvenSum + oddSumOriginal - tempOddSum) {
 36
                 fairWaysCount += 1;
 37
 38
 39
             // When removing an element at an odd index, check if the sum without that
 40
             // element makes the array fair.
 41
             if (i % 2 === 1 && tempOddSum + evenSumOriginal - tempEvenSum === tempEvenSum + oddSumOriginal - tempOddSum - value) {
 42
                 fairWaysCount += 1;
 43
 44
 45
             // Update temporary even and odd sums with the current element value.
 46
             tempEvenSum += i % 2 === 0 ? value : 0;
 47
             tempOddSum += i % 2 === 1 ? value : 0;
 48
 49
 50
         return fairWaysCount;
 51 };
 52
Time and Space Complexity
```

checks) are all constant time operations. The space complexity of the code is 0(1). Only a fixed number of variables (s1, s2, ans, t1, t2) are used, and their space requirement

list just once with a single loop, and within that loop, the operations performed (including arithmetic operations and conditional

The time complexity of the provided code is O(n), where n is the length of the nums list. This is because the code iterates through the

does not scale with the size of the input list nums. No additional data structures that grow with the input size are used.