# 1198. Find Smallest Common Element in All Rows

**Binary Search** Medium <u>Array</u> Hash Table **Counting** Matrix

### **Problem Description**

In this problem, we are given a matrix mat with dimensions m  $\times$  n, where m represents the number of rows and n represents the number of columns. Each row in the matrix is sorted in strictly increasing order. We are tasked with finding the smallest element that is common to all rows in the matrix. The question specifies that if no such common element exists, we should return -1.

To visualize, imagine a matrix where each row represents sorted test scores, and we want to find the lowest score that appears in every row, indicating that it is a score that every test taker has achieved.

#### When approaching this problem, the key observation we can make is based on two factors:

Intuition

1. Each row is sorted in strictly increasing order. 2. We want to find the smallest common element across all rows.

- Given that each row is sorted, it might be tempting to look for the intersection of all rows, but with a large matrix, this can be

to track the occurrences of each element across all rows. The intuition for the solution can be broken down into the following steps:

inefficient. Instead, we leverage the fact that we want to find the smallest common element. We can employ a frequency counter

• Count the frequency of each number using a counter (a Python dictionary in the provided solution). • As soon as the count of an element equals the number of rows, meaning the element has appeared in every row, we have found our smallest

common element.

Iterate through each element x in every row in the matrix.

- Return this element.
- By checking for the condition where the count equals the number of rows, we can short-circuit as soon as we find our answer.
- Since the rows are sorted and we are iterating row-wise, the first common element we encounter will naturally be the smallest

due to the sort order.

the number of elements in a row.

This approach is both effective and efficient because: • It leverages the sorted nature of the rows to ensure the first common element we find is the smallest. • It avoids unnecessary comparisons since it will return immediately once a common element is found in all rows. • It does not require additional space for sorting or storing large portions of the matrix beyond the counter, which at most stores n keys where n is

- **Solution Approach** 
  - The solution approach for this problem utilizes a Counter from Python's collections module to track the occurrences of each
- element across all rows in the matrix. Here's an in-depth explanation of the steps involved in the given solution:

Iterate through each row of the matrix using a for loop.

Within each row, iterate through each element x.

that ensures the algorithm is efficient.

This approach works well because:

additional comparison or search algorithms.

terms of both time and space complexity.

• Import the Counter class from the collections module. The Counter is a subclass of the dictionary and is used for counting hashable objects (elements of the matrix in this case). • Create an instance of Counter which will hold elements as keys and their frequencies as values.

• Update the count for the current element x in the Counter. This is achieved by cnt[x] += 1.

- Check if the count for the current element x has reached the total number of rows len(mat). If yes, this means the current element x has appeared in each row, and by the nature of the iteration over sorted rows, x is the smallest element meeting this criterion.
- The algorithms and data structures used in this approach include:

• Hash Table/Counter: To keep track of the number of times an element appears across all rows.

• As soon as such an element x is found, return x from the function, as we have found our smallest common element.

• Nested Loops: To iterate over all elements in all rows. • Early Exit/Greedy Approach: By returning the first element that matches our condition (appears in all rows), we are using a greedy approach

• The hash table operation (checking and updating the count of each element) is on average a constant time operation (0(1)).

• If the loop completes and no common element is found, return -1.

- The solution uses a single pass through all elements with a time complexity of 0(m \* n) where m is the number of rows and n is
- each distinct element.

the number of columns. The space complexity is O(k) where k is the range of elements since we need to count occurrences of

• Since the matrix is pre-sorted, we can be confident that the first element found in all rows is the smallest possible, eliminating the need for

• The greedy component of the algorithm (returning as soon as we find the smallest common element) ensures that the solution is efficient in

Let's walk through an example to illustrate the solution approach. Imagine we have the following matrix mat with m = 3 rows and n = 4 columns: [1, 2, 3, 4], [1, 3, 5, 7],

## Each row is sorted in strictly increasing order. We want to find the smallest element that is common to all rows.

[1, 6, 8, 9],

instead.

class Solution:

Java

**Example Walkthrough** 

We start iterating through the first row, updating the counts in our Counter:

Next, we move to the second row and update the counts:

Counter after processing first row: {1: 1, 2: 1, 3: 1, 4: 1}

We notice that number 1 now has a count of 2, but since there are 3 rows, we must continue.

Counter after processing third row: {1: 3, 2: 1, 3: 2, 4: 1, 5: 1, 7: 1, 6: 1, 8: 1, 9: 1}

Counter after processing second row: {1: 2, 2: 1, 3: 2, 4: 1, 5: 1, 7: 1}

First, we create a Counter to keep track of the counts of each element across the rows.

common to all of them. Since we are looking for the smallest common element and the rows are sorted, the first element to reach the count of 3 - in

# Initialize a counter to keep track of the occurrences of each element.

# If the count of this element is equal to the number of rows,

# Since we are iterating in order, the first element

# that satisfies this condition is the smallest common element.

# it means this element is present in each row.

if element\_counter[element] == len(mat):

// Function to find the smallest common element in all rows of 'mat'

// Increment the count of the current element.

// common element found so far. Return it.

// If no common element is found in all rows, return -1.

if (count[element] == mat.size()) {

// If the current element's count equals the number of rows in 'mat',

// it means the element is present in all rows and is the smallest

// Array to keep track of the count of each number across all rows.

int smallestCommonElement(vector<vector<int>>& mat) {

// Iterate over each row of the matrix 'mat'.

// Iterate over each element in the row.

this case, number '1' - is the smallest element. Once we hit this condition, we return '1'.

Finally, we iterate through the third row and again update the counts:

Solution Implementation **Python** 

In the given example, the smallest element common to all rows is 1, and the algorithm will return this result without having to

iterate through all elements in the matrix, showcasing its efficiency. If no common element was found, we would return -1

At this point, we see that the number 1 has been encountered in each row (count == number of rows == 3), which means it is

for row in mat: # Go through each element in the row. for element in row: # Increase the count for this element. element\_counter[element] += 1

#### return element # If no common element is found, return -1. return -1

from collections import Counter

def smallestCommonElement(self, mat):

# Go through each row in the matrix.

element\_counter = Counter()

```
class Solution {
    public int smallestCommonElement(int[][] matrix) {
       // Initialize an array to hold the count of each element
        int[] elementCount = new int[10001];
       // Iterate through each row of the matrix
        for (int[] row : matrix) {
           // Iterate through each element in the row
            for (int element : row) {
                // Increment the count for this element
                elementCount[element]++;
                // If the count for the current element equals the number of rows
                // it means we have found a common element present in all rows
                if (elementCount[element] == matrix.length) {
                   // Return the first smallest common element found
                    return element;
       // If no common element is found in all rows, return -1
       return -1;
C++
```

class Solution:

def smallestCommonElement(self, mat):

Time and Space Complexity

#include <vector>

class Solution {

public:

using namespace std;

int count[10001] = {};

for (auto& row : mat) {

for (int element : row) {

++count[element];

return element;

```
return -1;
  TypeScript
  function smallestCommonElement(matrix: number[][]): number {
      // Create an array to count occurrences of each element
      const elementCount: number[] = new Array(10001).fill(0);
      // Iterate through each row in the matrix
      for (const row of matrix) {
          // Iterate through each element in the current row
          for (const element of row) {
              // Increment the count for this element
              elementCount[element]++;
              // If the current element's count matches the number of rows,
              // it means the element is common to all rows, thus return it
              if (elementCount[element] === matrix.length) {
                  return element;
      // If no common element was found in all rows, return -1
      return -1;
from collections import Counter
```

```
element counter = Counter()
# Go through each row in the matrix.
for row in mat:
    # Go through each element in the row.
    for element in row:
        # Increase the count for this element.
        element_counter[element] += 1
        # If the count of this element is equal to the number of rows,
        # it means this element is present in each row.
        if element_counter[element] == len(mat):
            # Since we are iterating in order, the first element
            # that satisfies this condition is the smallest common element.
            return element
# If no common element is found, return -1.
return -1
```

# Initialize a counter to keep track of the occurrences of each element.

check for the count cnt[x] to equal len(mat) is O(1) since it's a simple dictionary access.

## Hence, the overall time complexity is 0(m \* n). **Space Complexity**

**Time Complexity** 

The space complexity is dominated by the Counter dictionary used to store the counts of each element. In the worst case, if all elements in the matrix are distinct, the counter would need to store n elements from each of m rows, which could lead to storing up to m \* n key-value pairs.

The given Python code iterates through all elements in the matrix mat, which has a size of m \* n, with m being the number of rows

and n being the number of columns. The time complexity is therefore 0(m \* n) because each element is visited exactly once. The

Thus, the space complexity is 0(m \* n) in the worst case. However, if there are common elements among the rows, the number of keys in the dictionary will be less than m \* n. Still, the worst-case space complexity remains 0(m \* n).