969. Pancake Sorting

Problem Description

Two Pointers Medium Greedy Array Sorting

The problem provides us with an array of integers arr. We are tasked with sorting this array but not through conventional means. The only operation we can perform is what's termed as a "pancake flip." A pancake flip involves the following steps:

2. Reverse the sub-array arr[0...k-1], which is zero-indexed.

1. Select an integer k where 1 <= k <= arr.length.

Our goal is to sort the entire array by performing a series of these pancake flips. To illustrate, if our array is [3,2,1,4] and we perform a pancake flip with k = 3, we reverse the sub-array [3,2,1], turning the array into [1,2,3,4]. The desired output is not the sorted array itself but rather a sequence of k values for each flip performed to sort the array. Importantly, any sequence that sorts the array within 10 * arr.length flips is considered correct.

Intuition

by moving the largest number not yet in place to its final position through a sequence of at most two flips: 1. First, flip the largest number to the beginning of the array (unless it's already there).

The key to solving this problem lies in reducing it to smaller sub-problems. We can sort the array one number at a time, specifically

- 2. Then flip it again to its final destination in the sorted array.
- By repeating this process for the largest number down to the smallest, we can sort the entire array.

1. We iterate from the end of the array to the beginning (i = n-1) to (i = n-1)), as the end of the array represents where the next largest

number should go.

Now let's dive into the solution intuition:

- 2. We then find the index j where the next largest number is (i+1 indicates the number we're looking for each iteration). 3. If the largest number is not already in position i (j < i), we perform up to two flips:
- ∘ The first flip moves the largest number to the start of the array (j = 0). This is only needed if the number is not already at the start (j > 0).
- The second flip moves the number from the start to its correct position i.
- We keep a list of k values for each flip performed and return it as the result.

The solution provided uses a simple greedy algorithm to sort the array using the constraints of pancake flips.

To understand the implementation, let's walk through the algorithm and data structures used:

flips:

Solution Approach

1. A helper function named reverse is defined which takes the array and an index j. The function reverses the sub-array from the start up to the j-th element (i.e., arr[0...j]). Simple swapping within the array is used for this operation. This is done using a

while loop, where the i-th and j-th elements are swapped, incrementing i and decrementing j until they meet or cross. No additional data structures are needed here; in-place swapping is sufficient.

- 2. The main function, pancakeSort, iterates over the elements of the array in reverse order, from the last element down to the second one (as the first one will be naturally sorted if all others are). Here, n is the length of the array. 3. In each iteration, it finds the correct position j for the i-th largest value (which should be i+1 due to zero-indexing) by simply scanning the array from the start to the current position i. It uses a while loop for this, decrementing j until the value at arr[j]
- matches i+1. 4. Once the position of the unsorted largest element is found, if it's not already at its correct position, we proceed with up to two
- the front (a k value of j+1 is appended to the result list). The next flip brings the element from the start to its designated position i by reversing the sub-array from the start up to i (a k value of i+1 is appended to the result list).

o If j is greater than 0, which means that the element is not at the start, it flips the sub-array up to j to bring the element to

The reasoning behind this approach is that each iteration ensures the next largest value is placed at its final position, reducing the problem's size by one each time. Since the relative order of the previous flips is not disrupted by further flips (they only affect

5. The algorithm keeps track of all flips performed by appending the k values to the ans list, which is the final result of the function.

This approach does not require any advanced data structures. It leverages the fact that we can greedily place each largest unsorted value in its final place step by step, making it a simple yet powerful solution given the unique constraints of the problem.

Let's use a small example array [3,1,2] to illustrate the solution approach detailed above. 1. Our goal is to sort the array [3,1,2] using pancake flips.

2. We start by looking for the position of the largest number that is not yet in its correct place. Since the array is of length 3, we

3. We find that the largest number, 3, is already in the first position. This means we do not need the first flip; we can directly proceed to the second flip.

Example Walkthrough

4. We perform the second flip at the third position to move the number 3 to the end of the array. We reverse the sub-array [3,1,2], resulting in [2,1,3]. We add k=3 to our sequence of flips, as we flipped the first three elements.

9. Now, our array is fully sorted as [1,2,3], and our sequence of flips that were required is [3,2].

elements before the largest placed element), the array is sorted correctly at the end of the algorithm.

begin with the number 3, which is also the largest.

- 5. Now, the largest number is in the correct position, and we ignore it in subsequent steps. We are left with considering the subarray [2,1]. 6. Next, we move to the second largest number, which is 2. This is not in the correct position, so we find it at position 0.
- and can be skipped). 8. We then perform the second flip at the second position to move the number 2 to its correct location before the number 3. We reverse the sub-array [2,1], turning it into [1,2]. We add k=2 to our sequence of flips, as we flipped the first two elements.

7. We perform our first flip to bring the number 2 to the beginning of the array (though it's already there, so this flip is redundant

Thus, the sequence [3,2] represents the series of k values for each flip we performed to sort the array [3,1,2]. In practice, we could have avoided the redundant flip when the largest number was already at the beginning, but this walkthrough includes it for

from typing import List class Solution: def pancakeSort(self, arr: List[int]) -> List[int]: # Helper function to reverse the array from start to index 'k'. def flip(arr, k):

n = len(arr)14 15 flips = [] # To store the sequence of flips 16 # Start sorting from the end of the array 17

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illustration purposes.

Python Solution

start = 0

while start < k:</pre>

k -= 1

Swap values

for target_index in range(n - 1, 0, -1):

// Perform the necessary flips

return ans; // Return the list of flip positions

arr[i] = arr[j]; // Swap the elements

if (maxIndex > 0) {

private void reverse(int[] arr, int j) {

arr[j] = temp;

for (int i = 0; i < j; i++, j--) {

// Flip the sub-array if the max index is not at the beginning

ans.add(i + 1); // Flip the sub-array from 0 to i

// Method to reverse the elements in the sub-array from index 0 to index j

int temp = arr[i]; // Temporary variable to hold the current element

ans.add(maxIndex + 1); // Add the flip position to the answer list

reverse(arr, i); // Performed to move the max element to the correct position

reverse(arr, maxIndex); // Flip the sub-array from 0 to maxIndex

if (maxIndex < i) {</pre>

max_index = arr.index(target_index + 1)

start += 1

arr[start], arr[k] = arr[k], arr[start]

Find the index of the next largest element to sort

```
# If the largest element is not already in place
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               if max_index != target_index:
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                    # Bring the largest element to the start if it's not already there
                   if max index > 0:
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                       flips.append(max_index + 1)
                       flip(arr, max_index)
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                   # Now flip the largest element to its correct target index
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                    flips.append(target_index + 1)
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                    flip(arr, target_index)
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           return flips
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Java Solution
   import java.util.List;
   import java.util.ArrayList;
   class Solution {
       // Method to sort the array using pancake sort
       public List<Integer> pancakeSort(int[] arr) {
           int length = arr.length; // The length of the array
           List<Integer> ans = new ArrayList<>(); // The list to store the flips performed
 9
           // Start from the end of the array and move towards the start
           for (int i = length - 1; i > 0; --i) {
               // Find the index of the next largest value expected at 'i'
13
               int maxIndex = i;
               while (maxIndex > 0 && arr[maxIndex] != i + 1) {
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                   --maxIndex;
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C++ Solution
 1 #include <vector>
 2 #include <algorithm>
   class Solution {
   public:
       std::vector<int> pancakeSort(std::vector<int>& arr) {
           int n = arr.size();
           std::vector<int> sorted_operations;
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           // We iterate over each element in the array starting from the end
           for (int target_position = n - 1; target_position > 0; --target_position) {
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                int current_index = target_position;
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               // Find the index of the next largest element which should be at target_position
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               for (; current_index > 0 && arr[current_index] != target_position + 1; --current_index);
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               // If the element is already in the right place, skip it
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               if (current_index == target_position) continue;
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               // If the element is not at the beginning, flip the subarray so that the element
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               // is at the beginning
               if (current_index > 0) {
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                   sorted_operations.push_back(current_index + 1); // We add +1 because indices are 1-based in pancake sort
                   std::reverse(arr.begin(), arr.begin() + current_index + 1); // Perform the flip operation
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               // Next, flip the subarray to move the element from the beginning to its target position
28
               sorted_operations.push_back(target_position + 1);
                std::reverse(arr.begin(), arr.begin() + target_position + 1);
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32
           // Return the sequence of flips performed to sort the array
33
           return sorted_operations;
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35 };
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```

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Typescript Solution

1 // Function to sort an array using pancake sort algorithm.

2 // The main idea is to do a series of pancake flips (reversing sub-arrays) to sort the array.

```
function pancakeSort(arr: number[]): number[] {
        let output = []; // This will store our sequence of flips.
       // Iterate over the array from the last element down to the second one.
       for (let currentSize = arr.length; currentSize > 1; currentSize--) {
            let maxIndex = 0;
           // Find the index of the largest element in the unsorted part of the array.
10
           for (let i = 1; i < currentSize; i++) {</pre>
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                if (arr[i] >= arr[maxIndex]) {
13
                    maxIndex = i;
14
           // If the largest element is already at its correct position, continue.
           if (maxIndex == currentSize - 1) continue;
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           // Otherwise, flip the array at maxIndex and at currentSize - 1 to move
           // the largest element to its correct position.
            // Add the flip operations (+1 because operations are 1-based in pancakesort problem).
22
           if (maxIndex > 0) {
                reverse(arr, maxIndex);
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25
                output.push(maxIndex + 1);
26
           reverse(arr, currentSize - 1);
28
           output.push(currentSize);
29
30
        return output; // Return the sequence of flips.
31
32 }
33
   // Function to reverse the elements in the array from index 0 to end.
   function reverse(nums: number[], end: number): void {
       let start = 0; // Start of the sub-array to reverse.
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       // Swap positions starting from the ends towards the center.
       while (start < end) {</pre>
            [nums[start], nums[end]] = [nums[end], nums[start]]; // Perform the swap.
           start++;
           end--;
42
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44 }
45
```

of each reversal on time and space.

Time and Space Complexity

Time Complexity: 1. The outer loop runs from n - 1 down to 1, which gives us a total of n iterations.

2. Inside the outer loop, there is a while loop that searches for the position j of the i+1-th largest element. The while loop can

3. Two reversals can occur in each iteration of the outer loop; one if the largest element is not already in the right place, and

iterate at most i times in the worst case, which is when the largest element is at the beginning of the array.

The provided code achieves the goal of sorting a list through a series of pancake flips, which are represented as reversals of prefixes

of the array. To analyze the time and space complexity, we need to consider both the number of reversals performed and the impact

another reversal puts the largest element at the end of the array. This yields a total of at most 2n reversals (each involving at most n elements to be swapped) across all iterations of the outer loop. Consequently, the worst-case time complexity is $O(n^2)$ because each of the 2n reversals takes up to O(n) time.

the last one.

total space complexity of O(n).

- **Space Complexity:**
- The space complexity of the code consists of the space used by the input array and the additional space used to store the answer
- 1. No additional data structures that depend on the size of the input are allocated; the reversals are performed in place. 2. The ans list will contain at most 2n - 2 elements because, in the worst case, two flips are performed for each element except for

Therefore, the space complexity is O(n) for the ans list, in addition to O(1) auxiliary space for the variables used, which results in

list that keeps track of the flips.