2909. Minimum Sum of Mountain Triplets II

Medium Array

Problem Description

You are tasked with finding a specific type of triplet in an integer array nums, where the array indices start at 0. This triplet needs to follow the characteristics of a mountain, which means for indices i, j, k satisfying i < j < k, the elements at these indices must adhere to the pattern nums[i] < nums[j] and nums[k] < nums[j]. The goal is to determine the smallest possible sum of such a mountain triplet. If there are no triplets that form a mountain, you should return -1.

Intuition

The problem calls for an efficient way to find the smallest sum of a "mountain" within an array. To approach this, you would need to check each possible middle element (the peak of the mountain) to see if there's a smaller number before it (uphill) and a smaller number after it (downhill). A brute-force solution would be to try every possible triplet to find the minimum sum, but that would result in a high time complexity.

Instead, we can use pre-processing to optimize this procedure. By iterating through the array once, we can store the minimum

element that can be the downhill part of the mountain for any middle element we're considering. As we traverse the array to find the middle element of potential mountain triplets, we keep track of the smallest value encountered so far to serve as the uphill part of the mountain. This value is stored in a variable called left. At any point, if our

value found to the right of each element in a new array called right. This pre-processing helps us quickly find the smallest

current element is greater than both left and the corresponding value in right, we have found a valid mountain. We then check if the sum of left, the current element, and the corresponding right is less than the best answer we have found so far, updating our answer accordingly. **Solution Approach**

The implementation of the solution is based on the Reference Solution Approach provided, which cleverly reduces the problem's

complexity by pre-processing the array and using two pointers to track the minimum values required to identify a potential

Here's how the solution approach is implemented step by step:

mountain.

Pre-processing: We create an array right which holds the minimum value to the right of each index in the nums array. We initialize every element in right to be inf (inf is a placeholder for infinity), which ensures that any number compared to it will be smaller. Starting from the second last element in nums and moving backwards, we populate right[i] with the minimum between right[i + 1] and nums[i].

it's smaller than the current ans.

(one for pre-processing and one for the main iteration).

check if we have a smaller number on its left (uphill) and on its right (downhill):

One pass enumeration with two pointers: As we iterate through the nums array using the variable i, we maintain two pointers/values: left: The minimum value in the subarray to the left of the current index i (including nums [i]). ans: The result variable which keeps track of the minimum sum of a valid mountain that has been found so far.

Evaluating potential mountains: For each element nums [i], which we are considering to be the peak of the mountain (j), we

∘ If both conditions are met, nums[i] can be the peak of a mountain, and we update ans with the sum of left, nums[i], and right[i + 1] if

Updating the minimum left value: After each iteration, we update left to be the minimum value between the current left

- The check left < nums[i] ensures that the current peak is higher than the minimum value on the left. The check right[i + 1] < nums[i] ensures that we have a valid downhill part for the mountain.
- and nums[i].
- mountain was found, and we return -1. Otherwise, we return the minimum sum stored in ans. By following this approach, we avoid the need for a triple nested loop to check every possible triplet, which significantly

optimizes the solution. The algorithm achieves a time complexity of O(n) since it only requires two passes through the nums array

Returning the result: Once we've iterated through the entire array, we check whether ans is still infinity. If it is, no valid

Example Walkthrough To illustrate the solution approach, let's consider a small example of the nums array:

Step 1: Pre-processing We begin by creating a right array that will contain the minimum value to the right of each index, initializing all elements to

We then update the right array by traversing from right to left:

infinity:

nums = [2, 1, 4, 7, 3, 2, 5]

right[4] is min(2, 3) = 2right = [inf, inf, inf, inf, 2, 2, inf] right[3] is min(2, 7) = 2

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right = [inf, 1, 2, 2, 2, inf]
right[0] will not be used since it must be the leftmost element of a triplet.
```

Final right array after pre-processing:

Step 2: One pass enumeration with two pointers

right = [inf, 1, 2, 2, 2, inf]

right = [inf, inf, inf, inf, inf, inf, inf]

right = [inf, inf, inf, inf, inf, 2, inf]

right = [inf, inf, inf, 2, 2, 2, inf]

right = [inf, inf, 2, 2, 2, inf]

right[2] is min(2, 4) = 2

right[1] is min(2, 1) = 1

left = inf

left >= nums[i].

ans = inf

Starting with the second to last index, right [5] is min(inf, 2) = 2

Step 3: Evaluating potential mountains

• When i is 0 (nums[i] is 2), i is at the leftmost edge, so left does not update because no valid mountain can start here.

• When i is 1 (nums [i] is 1), the left array so far [2] has a minimum of 2, and our right is 1. No valid mountain can have a peak at index 1 since

• When i is 2 (nums[i] is 4), we have left = 1 and right[3] is 2. This satisfies the mountain property (left < nums[i] > right[3]). We sum 1 +

• For i 4, 5, and 6, while a valley exists to the right (right[i + 1] < nums[i]), no smaller value exists to the left (left >= nums[i]), so no valid

After each iteration, left is updated to the minimum value it has seen so far (if smaller than nums[i]), which helps efficiently find

We initialize two variables - left starting with infinity and ans also with infinity.

As we start iterating over the array, our pointers will update as follows:

• When i is 3 (nums[i] is 7), a sum is possible here, but it won't be minimum because right[4] = 2 and the minimum sum would be 1 + 7 + 2 which is 10, larger than our current ans.

mountain, and 7 is the smallest sum of such a mountain triplet.

Therefore, the smallest possible sum of a mountain triplet in the nums array is 7.

initialize a list to keep track of the minimum value to the right

populate the min_right list with the minimum values from right to left

initialize the answer and the minimum value from the left with infinity

if the current number is greater than the smallest number found

update min_left to the smallest number found so far from the left

answer = Math.min(answer, leftMin + nums[i] + rightMin[i + 1]);

// Update leftMin with the smallest value encountered so far

// Return the answer if it's not infinity, otherwise return -1

leftMin = Math.min(leftMin, nums[i]);

return answer != INF ? answer : −1;

#include <algorithm> // Including algorithm for std::min

C++

#include <vector>

using std::vector;

using std::min;

TypeScript |

class Solution:

function minimumSum(nums: number[]): number {

const numsLength = nums.length;

// Initialize the length of the given array

// for each position, initialized to Infinity.

for (let $i = numsLength - 1; i >= 0; --i) {$

def minimumSum(self, nums: List[int]) -> int:

min_right = [float('inf')] * (num_length + 1)

min_right[i] = min(min_right[i + 1], nums[i])

for i in range(num_length - 1, -1, -1):

iterate over nums to find the minimum sum

if min_left < x and min_right[i + 1] < x:</pre>

return -1 if answer == float('inf') else answer

get the length of the nums list

answer = min_left = float('inf')

min_left = min(min_left, x)

for i, x in enumerate(nums):

num_length = len(nums)

// Populate the 'rightMinValues' array from right to left

// Create an array 'right' to keep track of the smallest number to the right

const rightMinValues: number[] = Array(numsLength + 1).fill(Infinity);

initialize a list to keep track of the minimum value to the right

populate the min_right list with the minimum values from right to left

initialize the answer and the minimum value from the left with infinity

if the current number is greater than the smallest number found

update min_left to the smallest number found so far from the left

answer = min(answer, min_left + x + min_right[i + 1])

return -1 if answer has not been updated, otherwise return the answer

to its left and to its right, consider it as a candidate for the answer

including the current position, filled with infinity to start

answer = min(answer, min_left + x + min_right[i + 1])

return -1 if answer has not been updated, otherwise return the answer

to its left and to its right, consider it as a candidate for the answer

including the current position, filled with infinity to start

min_right = [float('inf')] * (num_length + 1)

min_right[i] = min(min_right[i + 1], nums[i])

for i in range(num_length - 1, -1, -1):

iterate over nums to find the minimum sum

if min_left < x and min_right[i + 1] < x:</pre>

answer = min_left = float('inf')

min_left = min(min_left, x)

for i, x in enumerate(nums):

4 + 2 to get the total sum of 7. Since ans was infinity, it is now updated to 7.

Step 5: Returning the result After iterating through the entire nums array, we find that ans is 7. Since it's no longer infinity, we have found at least one valid

Solution Implementation

num_length = len(nums)

Python

mountain can exist at these points.

Step 4: Updating the minimum left value

the uphill part for the next iterations.

from typing import List class Solution: def minimumSum(self, nums: List[int]) -> int: # get the length of the nums list

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return -1 if answer == float('inf') else answer
Java
class Solution {
    public int minimumSum(int[] nums) {
        int n = nums.length; // Length of the input array
        int[] rightMin = new int[n + 1]; // Array to hold the minimum values from the right
        final int INF = Integer.MAX_VALUE; // Use Java's max value to represent infinity
        rightMin[n] = INF; // Set the rightmost value to infinity as a sentinel value
       // Populate rightMin with the minimum values scanned from right to left
        for (int i = n - 1; i >= 0; --i) {
            rightMin[i] = Math.min(rightMin[i + 1], nums[i]);
        int answer = INF; // Initialize answer with the maximum possible value (infinity)
        int leftMin = INF; // Variable to keep track of the minimum value scanned from left
       // Iterate over the array to find the minimum sum with the specified conditions
        for (int i = 0; i < n; ++i) {
           // Check if both leftMin and rightMin[i+1] are less than nums[i]
           if (leftMin < nums[i] && rightMin[i + 1] < nums[i]) {</pre>
               // Update the answer with the minimum of previous answer
               // and the sum of leftMin, nums[i], and rightMin[i+1]
```

```
class Solution {
public:
    int minimumSum(vector<int>& nums) {
        int nums_size = nums.size(); // Size of the nums vector.
        const int INFINITY = 1 << 30; // Representing infinity as a very large number.</pre>
        vector<int> right smallest(nums size + 1, INFINITY); // Vector to keep track of the right smallest elements.
       // Populate the right_smallest vector with the smallest value found from the right.
        right_smallest[nums_size] = INFINITY; // Initialization to infinity at the end of the vector.
        for (int i = nums_size - 1; i >= 0; --i) {
            right_smallest[i] = min(right_smallest[i + 1], nums[i]);
        int result = INFINITY; // This will hold the final result, initialized to infinity.
        int left_smallest = INFINITY; // Keeping track of the smallest value from the left.
        // Iterate through the vector to find the minimum sum.
        for (int i = 0; i < nums_size; ++i) {</pre>
            // Check if the current element is greater than both the left and right smallest elements.
            if (left_smallest < nums[i] && right_smallest[i + 1] < nums[i]) {</pre>
                // Update the result with the minimum sum found so far.
                result = min(result, left_smallest + nums[i] + right_smallest[i + 1]);
            // Update left_smallest to be the smallest value from the left up to the current position.
            left_smallest = min(left_smallest, nums[i]);
       // If the result is still infinity, then a sum cannot be formed as per the problem's requirement.
        // Return -1 in that case. Otherwise, return the result.
        return result == INFINITY ? -1 : result;
};
```

```
rightMinValues[i] = Math.min(rightMinValues[i + 1], nums[i]);
      // Declare variables to keep track of the minimum answer and left minimum value
      let minAnswer = Infinity;
      let leftMinValue = Infinity;
      // Iterate over the array to compute the minimum sum of a valid triplet
      for (let i = 0; i < numsLength; ++i) {</pre>
          // Check if the current number is larger than the minimum on both sides
          if (leftMinValue < nums[i] && rightMinValues[i + 1] < nums[i]) {</pre>
              // Update the minimum answer with the sum of the triplet
              // if it is smaller than the current minimum
              minAnswer = Math.min(minAnswer, leftMinValue + nums[i] + rightMinValues[i + 1]);
          // Store the minimum on the left up to the current element
          leftMinValue = Math.min(leftMinValue, nums[i]);
      // Return the minimum answer or -1 if the answer remains Infinity (no valid triplet found)
      return minAnswer === Infinity ? -1 : minAnswer;
from typing import List
```

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Time and Space Complexity
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running for n iterations, where n is the length of the input list nums. The first loop is a reverse iteration used to build the right list, and the second loop goes through the nums list to compute the ans variable. Since both loops are independent and execute sequentially, their combined time complexity remains linear with the size of the input list. The space complexity of the code is O(n) as well due to the allocation of the right list, which stores the minimum value

The time complexity of the provided code is indeed O(n). This is because the code consists of two loops over the nums list, each

encountered from the right side of the nums list. This right list has a length equal to n + 1, where n is the length of the nums list. The other variables used (ans, left, and a few others) do not depend on n and thus contribute a constant factor, which is ignorable when assessing space complexity.