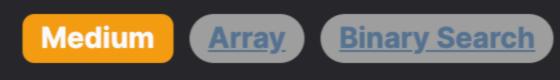
162. Find Peak Element



Problem Description

The problem presents an integer array called nums which is 0-indexed. We are tasked with finding an index of a peak element. A peak element is defined as an element that is strictly greater than its neighboring elements. Here the term "strictly" means that the peak element must be greater than its neighbors, not equal to them.

Furthermore, the problem scenario extends the array conceptually, so that if you look at the start or end of the array, it's as if there's

an invisible - to the left of the first element and to the right of the last element. This means that if the first or last element is greater than their one real neighbor, they also count as peak elements.

We're also given a constraint on the time complexity: the solution needs to run in O(log n) time, which implies that a simple linear scan of the array is not efficient enough. We need to use an algorithm that repeatedly divides the array into smaller segments binary search is an example of such an algorithm.

Intuition

Instead, we adopt a binary search method due to its logarithmic time complexity, which fits our constraint. Binary search is a technique often used for searching a sorted array by repeatedly dividing the search interval in half. Although in this

Given the requirement to complete the task in O(log n) time, we must discard a linear scan approach that would take O(n) time.

case the entire array isn't sorted, we can still use binary search because of the following key insight: if an element is not a peak (meaning it's less than either of its neighbors), then a peak must exist to the side of the greater neighbor. The reason this works is because of our -∞ bounds at both ends of the array. We imagine a slope up from -∞ to a non-peak element

and then down from the non-peak element towards -∞. Somewhere on that rising or falling slope there must be a peak, which is a local maximum. So in our modified binary search, instead of looking for a specific value, we look for any peak as follows:

1. We take the middle element of the current interval and compare it with its right neighbor. 2. If the middle element is greater than its right neighbor, we've found a descending slope, and there must be a peak to the left.

- Hence, we restrict our search to the left half of the current interval.
- 3. If the middle element is less than its right neighbor, we've found an ascending slope, and a peak exists to the right. We then do our next search on the right half.
- 4. We continue this process of narrowing down our search interval by half until we've isolated a peak element.

Solution Approach

This binary search on a wave-like array ensures we find a peak in O(log n) time, satisfying the problem's constraints.

O(log n). The essence of binary search in this context is to reduce the search space by half after each comparison, making it much

faster than a linear approach.

positions for a peak element.

Here's a step-by-step explanation of the implementation:

1. We initialize two pointers, left and right, which represent the boundaries of our current search interval. left is set to 0, and right is set to the length of the array minus one (len(nums) - 1).

The solution leverages a binary search algorithm, which is ideal for situations where we need to minimize the time complexity to

3. Inside the loop, we calculate the midpoint of the current search interval as mid = (left + right) >> 1. The >> 1 operation is a bitwise shift to the right by 1 bit, which is equivalent to dividing by two, but it's often faster.

2. We enter a while loop that continues as long as left is less than right, ensuring that we are still considering a range of possible

4. We then compare the element at the mid position with the element immediately to its right (nums [mid + 1]).

5. If nums [mid] is greater than nums [mid + 1], the peak must be at mid or to the left of mid. Thus, we set right to mid, effectively

- narrowing the search interval to the left half.
- 6. On the other hand, if nums [mid] is less than or equal to nums [mid + 1], then a peak lies to the right. Thus, we set left to mid + 1, narrowing the search interval to the right half.
- means that nums [left] cannot be smaller than both its neighbors (as per the nums $[-1] = nums[n] = -\infty$ rule). 8. We exit the loop and return left, which is the index of the peak element.

7. The loop continues, halving the search space each time, until left equals right. At this point, we have found the peak because it

- Here's the code snippet that follows this approach:
- def findPeakElement(self, nums: List[int]) -> int: left, right = 0, len(nums) - 1while left < right:</pre>

This approach guarantees finding a peak, if not the highest peak, in logarithmic time.

mid = (left + right) >> 1 if nums[mid] > nums[mid + 1]: right = mid

```
return left
10
The simplicity of binary search in conjunction with the described logic yields an efficient and elegant solution for finding a peak
element.
Example Walkthrough
```

left = mid + 1

Let's walk through the solution with a small example. Suppose our input array nums is [1, 2, 3, 1]. We want to find an index of a peak element.

The initial value of left is 0. The initial value of right is len(nums) - 1, which is 3.

Initial Setup

class Solution:

else:

Iteration 1

• Update left to mid + 1: left becomes 2.

left is now 2 and right is 3.

- Calculate the midpoint: mid = (left + right) >> 1 which is (0 + 3) >> 1 = 1. • Compare nums [mid] and nums [mid + 1]: nums [1] is 2, and nums [2] is 3.
- Iteration 2

• Calculate the new midpoint: mid = (left + right) >> 1 which is (2 + 3) >> 1 = 2.

Since 2 is less than 3, we are on an ascending slope. We should move right.

- Compare nums [mid] and nums [mid + 1]: nums [2] is 3, and nums [3] is 1. Since 3 is greater than 1, we're on a descending slope. We should move left. • Update right to mid: right becomes 2.
- The loop ends when left equals right, which is now the case (left and right are both 2). • Therefore, we have found our peak at index 2 where the element is 3, and it is greater than both its neighbors (where the neighbor on the right is 1, and the neighbor on the left is 2, and conceptually -∞ on both ends).

the peak element, satisfying the O(log n) time complexity constraint.

Initialize the start and end pointers.

Binary search to find the peak element.

start, end = 0, len(nums) - 1

Find the middle index.

mid = (start + end) // 2

start = mid + 1

end = mid

if nums[mid] > nums[mid + 1]:

while start < end:</pre>

else:

Thus, the index 2 is returned.

10

13

14

16

17

18

19

20

21

23

24

26

25 }

Conclusion

Python Solution

Using this approach with the given example, we can see how the binary search algorithm rapidly narrows down the search to find

from typing import List class Solution: def findPeakElement(self, nums: List[int]) -> int:

If the middle element is greater than its next element,

Otherwise, the peak is in the right half of the array.

When start and end pointers meet, we've found a peak element.

#include <vector> // Include vector header for using the vector container

// Continue searching as long as the search space contains more than one element

const middleIndex: number = leftBoundary + ((rightBoundary - leftBoundary) >> 1);

it means a peak element is on the left side(inclusive of mid).

22 return start 23

Java Solution 1 class Solution { public int findPeakElement(int[] nums) { int left = 0; // Initialize the left boundary of the search space int right = nums.length - 1; // Initialize the right boundary of the search space // Continue the loop until the search space is reduced to one element while (left < right) {</pre> // Calculate the middle index of the current search space int mid = left + (right - left) / 2; 9 10 // If the middle element is greater than its next element, then a peak must be to the left (including mid) 11 if (nums[mid] > nums[mid + 1]) { 12 // Narrow the search space to the left half right = mid; 14 } else { 15 // Otherwise, the peak exists in the right half (excluding mid) 16 // Narrow the search space to the right half 17 left = mid + 1; 18 19 20 21 22 // When left == right, we have found the peak element's index, return it

int findPeakElement(vector<int>& nums) { // Initialize the left and right pointers int left = 0;

public:

class Solution {

C++ Solution

return left;

```
int right = nums.size() - 1;
           // Perform binary search
11
           while (left < right) {</pre>
               // Find the middle index
12
               // Using (left + (right - left) / 2) avoids potential overflow of integer addition
13
               int mid = left + (right - left) / 2;
14
15
               // If the middle element is greater than the next element,
16
               // the peak must be in the left half (including mid)
17
               if (nums[mid] > nums[mid + 1]) {
18
                   right = mid;
19
20
               } else {
                   // If the middle element is smaller than the next element,
21
                   // the peak must be in the right half (excluding mid)
23
                   left = mid + 1;
24
25
26
           // At the end of the loop, left == right, which points to the peak element
27
           return left;
28
29 };
30
Typescript Solution
   function findPeakElement(nums: number[]): number {
       // Initialize the search boundaries to the start and end of the array
       let leftBoundary: number = 0;
       let rightBoundary: number = nums.length - 1;
```

// Compare the middle element to its next element 11 if (nums[middleIndex] > nums[middleIndex + 1]) { 12 // If the middle element is greater than the next element, // then a peak element is in the left half (including middle)

used remains fixed.

10

while (leftBoundary < rightBoundary) {</pre>

rightBoundary = middleIndex;

at most log2(n) iterations to converge on a single element.

// Find the middle index using bitwise operator

```
16
           } else {
               // Otherwise, the peak element is in the right half (excluding middle)
               leftBoundary = middleIndex + 1;
19
20
21
22
       // When leftBoundary equals rightBoundary, we found the peak element.
23
       // Return its index.
       return leftBoundary;
24
25 }
26
Time and Space Complexity
The time complexity of the provided algorithm is O(\log n), where n is the length of the input array nums. The algorithm uses a binary
```

search approach, whereby at each step, it halves the search space. This halving continues until the peak element is found, requiring

The space complexity of the algorithm is 0(1) as it only uses a constant amount of extra space. The variables left, right, and mid,

along with a few others for storing intermediate results, do not vary with the size of the input array nums, ensuring that the space