1101. The Earliest Moment When Everyone Become Friends

There are n people in a social group labeled from 0 to n-1. You are given an array logs where logs [i] = [timestamp_i, x_i , y_i] indicates that x_i and y_i will be friends at the time $timestamp_i$.

Friendship is **symmetric**. That means if a is friends with b, then b is friends with a. Also, person a is acquainted with a person b if a is friends with b, or a is a friend of someone acquainted with b.

Return the earliest time for which every person became acquainted with every other person. If there is no such earliest time,

return -1.

```
Example 1:
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```
Input: logs = [[20190101,0,1],[20190104,3,4],[20190107,2,3],[20190211,1,5],[20190224,2,4],[20190301,0,3],
[20190312,1,2],[20190322,4,5]], n = 6
```

Output: 20190301

Explanation:

The first event occurs at timestamp = 20190101 and after 0 and 1 become friends we have the following friendship groups [0,1], [2], [3], [4], [5]. The second event occurs at timestamp = 20190104 and after 3 and 4 become friends we have the following friendship groups [0,1], [2], [3,4], [5]. The third event occurs at timestamp = 20190107 and after 2 and 3 become friends we have the following friendship groups [0,1], [2,3,4], [5]. The fourth event occurs at timestamp = 20190211 and after 1 and 5 become friends we have the following friendship groups [0,1,5], [2,3,4]. The fifth event occurs at timestamp = 20190224 and as 2 and 4 are already friends anything happens. The sixth event occurs at timestamp = 20190301 and after 0 and 3 become friends we have that all become friends.

Example 2:

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Input: logs = [[0,2,0],[1,0,1],[3,0,3],[4,1,2],[7,3,1]], n = 4
Output: 3
Constraints:
• 2 \le n \le 100
• 1 \leq logs.length \leq 10^4
• logs[i].length == 3
• 0 \le \text{timestamp}_i \le 10^9
oldsymbol{\cdot} 0 \leq \overline{x_i, y_i} \leq \overline{n-1}
```

Solution

• $x_i \neq y_i$

• All the values $timestamp_i$ are unique.

• All the pairs (x_i, y_i) occur at most one time in the input.

where the graph formed by friendships is connected. To accomplish this, we'll first sort the friendships by ${
m timestamp}_i$. Then, we'll iterate through friendships from the least to greatest ${f timestamp}_i$ and merge nodes connected by a friendship until the graph is connected. After each iteration, we'll check if the graph is connected and return the timestamp value if it is. An easy way to check if the

When we see problems related to connectivity, we should think of applying <u>DSU</u>. This problem asks us to find the first instance

graph is connected is to check if node 1 is connected to all other n-1 nodes. If the graph isn't connected after processing all the friendships, we'll return -1. Let's denote the number of friendships (edges) as M.

Since checking the connectivity of the graph is $\mathcal{O}(N\log N)$ and we do this $\mathcal{O}(M)$ times, this solution runs in $\mathcal{O}(MN\log N)$.

Since checking the connectivity of the graph is too inefficient, we'll maintain the number of components in the graph as we

include more and more friendships. We can make the observation that every time we merge two disjoint sets, the number of components decreases by 1. This is true as this operation turns f 2 disjoint sets into f 1 disjoint set without disturbing any other disjoint sets. We initially start with N components (one for each person) and once we reach one component, we'll return the respective timestamp value. -1 will be returned if we never reach one component.

Sorting takes $\mathcal{O}(M\log M)$ and the main algorithm runs in $\mathcal{O}(M\log N)$. Thus our time complexity is $\mathcal{O}(M\log M+M\log N)$.

Time Complexity

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Time Complexity: \mathcal{O}(M \log M + M \log N)
```

Bonus: We can also use union by rank mentioned <u>here</u> to improve the time complexity of <u>DSU</u> operations from $\mathcal{O}(\log N)$ to

 $\mathcal{O}(\alpha(N))$. **Space Complexity**

Our <u>DSU</u> uses $\mathcal{O}(N)$ memory.

class Solution {

public:

Space Complexity: $\mathcal{O}(N)$.

vector<int> parent;

int components = n;

for (int[] friendship : logs) {

int x = friendship[1];

int y = friendship[2];

components--;

Union(x, y)

return -1

components -= 1

return timestamp

int timestamp = friendship[0];

Union(x, y, parent);

```
int find(int x) { // finds the id/leader of a node
        if (parent[x] == x) {
            return x;
        parent[x] = find(parent[x]);
        return parent[x];
   void Union(int x, int y) { // merges two disjoint sets into one set
        x = find(x);
        y = find(y);
        parent[x] = y;
   static bool comp(vector<int>& a, vector<int>& b) { // sorting comparator
        return a[0] < b[0];
    int earliestAcq(vector<vector<int>>& logs, int n) {
        parent.resize(n);
        for (int i = 0; i < n; i++) {
            parent[i] = i;
        sort(logs.begin(), logs.end(), comp); // sorts friendships by timestamp
        int components = n;
        for (vector<int> friendship : logs) {
            int timestamp = friendship[0];
            int x = friendship[1];
            int y = friendship[2];
            if (find(x) != find(y)) { // merge two disjoint sets
                Union(x, y);
                components--;
            if (components == 1) { // reached connected graph
                return timestamp;
        return -1;
};
class Solution {
   private int find(int x, int[] parent) { // finds the id/leader of a node
        if (parent[x] == x) {
            return x;
        parent[x] = find(parent[x], parent);
        return parent[x];
   private void Union(int x, int y, int[] parent) { // merges two disjoint sets into one set
        x = find(x, parent);
        y = find(y, parent);
        parent[x] = y;
   public int earliestAcq(int[][] logs, int n) {
        int[] parent = new int[n];
        for (int i = 0; i < n; i++) {
            parent[i] = i;
```

```
if (components == 1) { // reached connected graph
                return timestamp;
        return -1;
class Solution:
   def earliestAcq(self, logs: List[List[int]], n: int) -> int:
        parent = [i for i in range(n)]
        def find(x): # finds the id/leader of a node
            if parent[x] == x:
                return x
            parent[x] = find(parent[x])
            return parent[x]
        def Union(x, y): # merges two disjoint sets into one set
           x = find(x)
           y = find(y)
            parent[x] = y
        logs.sort(key=lambda x: x[0]) # sorts friendships by timestamp
        components = n
        for friendship in logs:
            timestamp = friendship[0]
           x = friendship[1]
           y = friendship[2]
```

if find(x) != find(y): # merge two disjoint sets

if components == 1: # reached connected graph

Arrays.sort(logs, (a, b) -> a[0] - b[0]); // sorts friendships by timestamp

if (find(x, parent) != find(y, parent)) { // merge two disjoint sets