2134. Minimum Swaps to Group All 1's Together II Sliding Window

Problem Description

Medium <u>Array</u>

elements are considered adjacent. Our task is to find the minimum number of swaps needed to group all the 1s together at any location in the array. A swap is defined as taking two distinct positions in an array and exchanging the values in them. To better understand the concept of a circular array, imagine that the last element in the array is followed by the first element,

The problem provides us with a binary circular array, which means the elements can be either 0 or 1, and the first and last

thereby creating a loop. This loop-like behavior suggests that the grouping of 1s can span from the end of the array to the beginning. The goal is to achieve this grouping using the fewest number of swaps, and we need to return that number.

Intuition

To solve this problem, we need to focus on the group of 1s and how many 0s we find within the windows that can cover all 1s.

Since the array is circular, these windows can wrap around the end to the start of the array.

that involve contiguous subarrays. Here's a step-by-step breakdown of the implementation:

which is O(n) where n is the number of elements in the array.

n], storing the cumulative count of 1s up to index i.

We begin by counting the total number of 1s in the array (cnt). Knowing this count allows us to determine the size of the

window we'll be sliding across the array. The size of the window is equal to the total number of 1s since our objective is to cluster all 1 s together.

We then double the size of the array to simplify the handling of the circular nature of the problem. By doing this, we avoid the

need for modular arithmetic and can work with a simple sliding window technique on this extended array. To efficiently check how many 1s are within any window, we construct a prefix sum array (s). This array holds the cumulative counts of 1s up to each index so that we can calculate the count of 1s within any range in constant time.

array due to its circular nature. Finally, the minimum number of swaps is determined by the size of the window (cnt) minus the maximum number of 1s found

within any window (mx). This is because if a window has x number of 1s, then it needs cnt - x swaps to move all 1s inside it

With the prefix sum array in hand, we then slide a window of size cnt over the array and track the maximum number of 1s we

can find within such a window (mx). The position of this window will vary, and it could span the end and beginning of the original

because for each 0 in the window, one swap is needed. Solution Approach

The solution approach hinges on the <u>sliding window</u> technique, which is a common pattern used to solve array-based problems

Count the Number of 1s: First, count the total number of 1s in the given array (cnt). This is done using the count method

Calculate the Extended Prefix Sum: Create an array s which will store the prefix sums of the array doubled in length. This

doubling accounts for the circular nature without dealing with wraparounds during the window sliding. If nums is [1,0,1,0,1],

then this step considers [1,0,1,0,1,1,0,1,0,1]. The prefix sum for each index i is calculated by adding s[i] to nums[i %

the end of the current window.

Slide the Window and Find Maximum 1s: Slide a window of length cnt (the number of 1s in the array) and find the maximum number of 1s in any such window in the extended array. The variable mx keeps track of this maximum count.

Iterate over each possible position the window can start from in the doubled array and compute the number of 1s in the current window using the prefix sums - by doing a constant time operation s[j + 1] - s[i], where i is the start and j is

Please note that the iteration for the sliding window is only until j < (n << 1) to ensure we do not access prefix sum array

out of bounds. Here n << 1 is a bitwise operation equivalent to multiplying n by 2, which is the length of our extended array.

Compute the Result: Once the maximum number of 1s in any window is determined (mx), the result is simply the window

size cnt minus mx. This is because the number of required swaps is equal to the number of 0s in the window that need to be

swapped with 1s outside of it. The beauty of this solution is that it reduces what could be a complex modular arithmetic problem (due to the circular nature) into a simpler linear problem by cleverly extending the size of the array and using a prefix sum array for efficient range queries.

Let's use a small example to illustrate the solution approach described above. Consider the binary circular array nums given by

[1,0,1,0,0]. We want to find the minimum number of swaps needed to group all the 1s together.

 \circ Starting at index 0: the window includes [1,0], and the count from the prefix sum is s[2] - s[0] = 1 - 0 = 1.

complexity, leveraging a sliding window mechanism on an extended array with the help of prefix sums.

Create an extended sum list which is twice the length of the nums list plus one

Fill the sum list with prefix sums, allowing wrap around to simulate a circular array

Iterate through the prefix sum array to find the maximum number of ones in any subarray

The minimum number of swaps needed is the total one count minus the maximum ones found

of the size count of ones, which is the number of swaps needed on a circular array

This is for the purpose of creating a sliding window later on

prefix_sum[i + 1] = prefix_sum[i] + nums[i % length_of_nums]

... and so on, until we cover all possible start positions of the window in the extended array.

together. **Calculate the Extended Prefix Sum:** We double the length of nums so that it becomes [1,0,1,0,0,1,0,1,0,0]. The prefix sum array s will be calculated from this

In nums, there are two 1s. So, cnt = 2. This means our sliding window will need to be of size 2 because we want all 1s to be

extended array: s = [0,1,1,2,2,2,3,3,4,4,4]. Notice how for each index i, s[i+1] accounts for the total number of 1s up

Slide the Window and Find Maximum 1s: We slide a window of length 2 across the array and use the prefix sum to calculate

From these calculations, we find that the maximum number of 1s in any window of size cnt is 1 (in this case, since all

• Starting at index 1: the window includes [0,1], and the count from the prefix sum is s[3] - s[1] = 2 - 1 = 1. • Starting at index 2: the window includes [1,0], and the count from the prefix sum is s[4] - s[2] = 2 - 1 = 1.

just one swap.

from typing import List

class Solution:

Example usage:

Java

C++

public:

class Solution {

sol = Solution()

class Solution {

Solution Implementation

def minSwaps(self, nums: List[int]) -> int:

count_of_ones = nums.count(1)

Get the length of the list

 $length_of_nums = len(nums)$

max_ones_found = 0

Count the number of ones in the list

for i in range(length of nums << 1):</pre>

for i in range(length of nums << 1):</pre>

return count_of_ones - max_ones_found

int[] sumArray = new int[(n << 1) + 1];</pre>

for (int i = 0; i < (n << 1); ++i) {

for (int i = 0; i < (n << 1); ++i) {

int j = i + onesCount - 1;

if (i < (n << 1)) {

return onesCount - maxOnes;

int n = nums.size();

print(result) # Output would be the minimum number of swaps required

// Create an extended array of sums to handle circular array

// Determine the end index for the range of size onesCount

maxOnes = Math.max(maxOnes, sumArray[j + 1] - sumArray[i]);

// Compute the number of 1's in the current range and update maxOnes if necessary

// The minimum number of swaps is the difference between total ones and the maximum ones found in any range of size onesCount

sumArray[i + 1] = sumArray[i] + nums[i % n];

result = sol.minSwaps([0,1,0,1,1,0,0])

public int minSwaps(int[] nums) {

Initialize max ones_found variable as 0

prefix_sum = [0] * ((length_of_nums << 1) + 1)</pre>

Example Walkthrough

Count the Number of 1s:

to that index in the extended array.

windows contain only one 1).

the number of 1 s in each window. For instance:

Compute the Result: Given that cnt = 2 and the maximum number of 1s we found in any window (mx) is 1, the minimum number of swaps required is cnt - mx = 2 - 1 = 1. Thus, only a single swap is necessary to group all 1s together. In the given example, we can swap the first 0 right after the last 1 to get [1,1,0,0,0], and all 1s are now grouped together using

This example clearly demonstrates each step of the solution approach and how it can effectively minimize the problem

- **Python** # Import the List type from types module for type hinting
 - end index = i + count of ones 1if end index < (length of nums << 1):</pre> # Update max ones found with the maximum ones found in the current sliding window max_ones_found = max(max_ones_found, prefix_sum[end_index + 1] - prefix_sum[i])
- // Count how many 1's are there in the array int onesCount = 0: for (int value : nums) { onesCount += value;

int n = nums.length;

int max0nes = 0;

int minSwaps(vector<int>& nums) { // Count the total number of ones in the input vector int oneCount = 0; for (int value : nums) { oneCount += value;

// This is used to simulate a circular array

let maxOnesInAnyWindow: number = onesCountInWindow;

for (let i = totalOnes; i < arrayLength + totalOnes; i++) {</pre>

let elementEntering: number = nums[i % arrayLength];

onesCountInWindow += elementEntering - elementExiting;

// Identify the element going out of the window.

// Identify the new element entering the window.

// Update the count of 1's in the current window.

return totalOnes - maxOnesInAnyWindow;

Import the List type from types module for type hinting

def minSwaps(self, nums: List[int]) -> int:

count_of_ones = nums.count(1)

Get the length of the list

length_of_nums = len(nums)

max_ones_found = 0

Count the number of ones in the list

Initialize max ones_found variable as 0

end index = i + count of ones - 1

if end index < (length of nums << 1):</pre>

print(result) # Output would be the minimum number of swaps required

used to find the maximum number of 1's within a window of size cnt.

for i in range(length of nums << 1):</pre>

return count_of_ones - max_ones_found

result = sol.minSwaps([0.1.0.1.1.0.0])

Time and Space Complexity

// Iterate over each window of size 'totalOnes' in the circular array.

let elementExiting: number = nums[(i - totalOnes) % arrayLength];

maxOnesInAnyWindow = Math.max(onesCountInAnyWindow, maxOnesInAnyWindow);

vector<int> prefixSum((n << 1) + 1, 0);</pre>

for (int i = 0; i < (n << 1); ++i) {

// Initialize an extended sum vector that is twice as long as the input

// Populate the prefix sum array by adding the current element

// Initialize the count of 1's in the first window of size equal to total number of 1's.

let onesCountInWindow: number = nums.slice(0, totalOnes).reduce((acc, current) => acc + current, 0);

// Update the maximum count of 1's found so far in any window if current window has more.

// Calculate minimum swaps as total number of 1's minus the maximum number of 1's in a window.

Create an extended sum list which is twice the length of the nums list plus one

Iterate through the prefix sum array to find the maximum number of ones in any subarray

The minimum number of swaps needed is the total one count minus the maximum ones found

Update max ones found with the maximum ones found in the current sliding window

max_ones_found = max(max_ones_found, prefix_sum[end_index + 1] - prefix_sum[i])

of the size count of ones, which is the number of swaps needed on a circular array

// Initialize the maximum count of 1's found in any window - this will be used to calculate minimum swaps.

// Note: Use modulus to simulate the circular array

prefixSum[i + 1] = prefixSum[i] + nums[i % n];

int max0nes = 0; // Slide a window of length equal to the number of ones (oneCount) // over the prefix sum array to find the maximum number of ones in any // subarray of the same length for (int i = 0; i < (n << 1); ++i) { // Calculate the end of the window int windowEnd = i + oneCount - 1; // Ensure that we do not go past the end of the sum array if (windowEnd < (n << 1)) {</pre> int windowSum = prefixSum[windowEnd + 1] - prefixSum[i]; maxOnes = max(maxOnes, windowSum); // The minimum number of swaps needed is the difference between // the number of ones in the array and the maximum number of ones // found in any window of size equal to the number of ones. // This tells us how many zeros we need to swap out of the window. return oneCount - maxOnes; **}**; **TypeScript** function minSwaps(nums: number[]): number { // Get the length of the input array. const arrayLength: number = nums.length; // Calculate the total number of 1's in the array. const totalOnes: number = nums.reduce((acc, current) => acc + current, 0);

This is for the purpose of creating a sliding window later on prefix_sum = [0] * ((length_of_nums << 1) + 1)</pre> # Fill the sum list with prefix sums, allowing wrap around to simulate a circular array for i in range(length of nums << 1):</pre> prefix_sum[i + 1] = prefix_sum[i] + nums[i % length_of_nums]

Example usage:

sol = Solution()

from typing import List

class Solution:

Time Complexity The time complexity of the given code is mainly determined by two loops: the loop used to populate the s array and the loop

Populating the s array requires iterating over each element once, and since it's done over 2 * n elements (to handle the

The s array is the primary additional data structure, which has a length of (2 * n) + 1. Therefore, the space complexity due

The calculation of mx within the second loop involves iterating up to 2 * n times, and within each iteration, we perform a constant time operation of computing the sum and finding the maximum. This results in a time complexity of 0(2n), again

Overall, since both operations are sequential and not nested, the total time complexity of the code is O(n). **Space Complexity**

simplifying to O(n).

The space complexity is determined by the additional space required besides the input. In this algorithm:

circular nature of the problem), this operation has a time complexity of 0(2n), which simplifies to 0(n).

- Other variables used (i, j, mx, cnt) are all constant-sized, adding a negligible 0(1) to the space complexity. •

Hence, the total space complexity of the algorithm is O(n).

to s alone is O(2n), which simplifies to O(n).