# **Problem Description**

Tree

Medium

508. Most Frequent Subtree Sum

**Depth-First Search** 

adding the sum of all node values in its right subtree.

Hash Table

is the sum of the values of all nodes in a subtree which includes the root node of that subtree. A binary tree is a tree data structure where each node has at most two children, referred to as the left child and the right child. Given the root node of a binary tree, the task is to compute the sum for every possible subtree and then find out which sum(s) occur

The problem is about finding the most frequently occurring sums of all the nodes in each subtree within a binary tree. A subtree sum

**Binary Tree** 

most frequently. If there is more than one sum with the highest frequency, all such sums should be returned. The return format is a list of integers in any order. An example of a subtree sum would be taking a node, adding its value to the sum of all node values in its left subtree, and then

Intuition To solve this problem, we need to traverse the binary tree and calculate the subtree sum for each node. This is a classic case for a

For each node visited, we calculate the subtree sum by summing: 1. The value of the current node.

Counter is handy for this purpose as it allows us to maintain a running count of each subtree sum encountered during the DFS.

depth-first search (DFS) traversal, in which we go as deep as possible down one path before backing up and trying a different one.

After calculating the sum, we update a histogram (counter) that records how many times each possible sum occurs. A Python

- Once the entire tree has been traversed and all subtree sums have been computed and counted, we determine the maximum frequency among them. This tells us how many times the most frequent sum occurs.

2. The subtree sum of the left child.

3. The subtree sum of the right child.

is what will be returned as the solution. Since the counter is a dictionary with subtree sum as keys and their frequencies as values, we can easily list the keys for which the values match the maximum frequency. This gives us all the most frequent subtree sums.

Finally, we iterate over the items in our counter to find all sums that have this maximum frequency, collecting them into a list. This list

**Solution Approach** The solution involves a combination of a depth-first search (DFS) algorithm and a Counter object from Python's collections module

to keep track of subtree sum frequencies. Here's a step-by-step approach explaining the above-provided solution code: 1. Define a recursive helper function dfs which will be used to perform a depth-first search of the binary tree. This function takes a single argument, the root of the current subtree (node).

2. In the DFS function, the base case is to return a sum of 0 when a None node is encountered, meaning we've reached a leaf node's

findFrequentTreeSum method.

Consider the following binary tree:

child.

logic.

3. The function then recursively calls itself on both the left and right children of the current node to calculate their subtree sums. These results are stored in variables left and right, respectively. 4. With the left and right subtree sums, we can now calculate the current node's total subtree sum as s = root.val + left +

- right. This is the sum of the value stored in the current node plus the sum of all node values in both subtrees. 5. We use a Counter to keep track of how frequently each subtree sum occurs. This Counter (counter) object is then updated with the current subtree sum, incrementing the count of s. This is done outside the DFS function in the global scope of the
- 7. The final step involves iterating over the items in the Counter and selecting only those keys (k) whose values (v) match the maximum frequency (mx). This is done using a list comprehension that filters and collects all the keys with the highest frequency.

The solution nicely ties together the traversal of the binary tree to compute subtree sums and the use of a Counter for frequency

tracking. The combination of recursive DFS and the Counter strategy efficiently solves the problem with clear and understandable

6. After the DFS traversal is complete, we can infer which subtree sums are most frequent. The maximum frequency of occurrence

- Example Walkthrough

3. Next, we recursively call dfs on the right child of node 5 (value -5). This is also a leaf node, so the function returns -5.

4. We now calculate the subtree sum for the root node (node 5). The sum s is equal to the root's value plus the left and right

6. Now we move up and track the subtree sums of the leaf nodes. The Counter is updated with the subtree sum 2 from the left

7. After finishing the DFS traversal and recording all subtree sums, we determine the most frequent sums. The maximum frequency

8. We now filter the keys in the Counter to find those with a frequency matching the maximum frequency mx. In this case, only the

2. Since node 5 is not None, we recursively call dfs on its left child (value 2). The left child is a leaf node, so it has no children. The dfs function returns 2, as there are no further nodes to sum.

(mx) is obtained by applying the max() function to the values of the Counter object.

8. These keys represent the most frequent subtree sums, and they are returned as a list.

Let's walk through a small example to illustrate the solution approach.

Using the provided solution approach, we'll perform these steps:

1. Call the dfs function on the root node (value 5).

# subtree sums: s = 5 + 2 + (-5) = 2. 5. Update the Counter with the subtree sum of 2 for the root node. The Counter now looks like this: {2: 1}.

binary tree.

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from collections import Counter

self.val = val

def dfs(node):

if not node:

return 0

return subtree\_sum

subtree\_sum\_counter = Counter()

// Recursively find all subtree sums.

// Convert the result to an array.

return result;

if (node == null) {

return 0;

return sum;

// Store the sums that have the highest frequency.

for (Map.Entry<Integer, Integer> entry : sumFrequency.entrySet()) {

// Helper method to perform a depth-first search and calculate subtree sums.

// Return the sum of the subtree rooted at the current node.

// Calculate the sum including the current node and its left and right subtrees.

int sum = node.val + calculateSubtreeSum(node.left) + calculateSubtreeSum(node.right);

List<Integer> frequentSums = new ArrayList<>();

if (entry.getValue() == maxFrequency) {

int[] result = new int[frequentSums.size()];

result[i] = frequentSums.get(i);

private int calculateSubtreeSum(TreeNode node) {

// If the node is null, return sum as 0.

for (int i = 0; i < frequentSums.size(); i++) {</pre>

frequentSums.add(entry.getKey());

calculateSubtreeSum(root);

left\_sum = dfs(node.left)

self.left = left

self.right = right

# Definition for a binary tree node.

def \_\_init\_\_(self, val=0, left=None, right=None):

:return: List[int], a list of most frequent subtree sums

:return: int, the sum of the current subtree

Perform a depth-first search to calculate the sum of each subtree.

# Initialize a Counter to keep track of the frequency of each subtree sum

# Start the DFS traversal from the root to fill the subtree\_sum\_counter

:param node: TreeNode, the current node in the binary tree

# Recursively find the sum of left and right subtrees

from typing import List

class TreeNode:

mx from the Counter is 2 (since the subtree sum 2 occurred twice).

subtree sum 2 matches, so it will be collected in the resulting list.

child and -5 from the right child, leading to: {2: 2, -5: 1}.

Python Solution

The final list of most frequent subtree sums to be returned is [2], as this is the sum that occurred most frequently in our example

class Solution: def findFrequentTreeSum(self, root: TreeNode) -> List[int]: Find all subtree sums that occur the most frequently in the binary tree. :param root: TreeNode, the root of the binary tree 16

#### right\_sum = dfs(node.right) 32 # Calculate the sum of the current subtree 33 subtree\_sum = node.val + left\_sum + right\_sum # Increment the counter for the subtree sum 34 35 subtree\_sum\_counter[subtree\_sum] += 1

dfs(root)

```
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           # Find the maximum frequency among the subtree sums
           max_frequency = max(subtree_sum_counter.values())
43
           # Collect all subtree sums with the maximum frequency
44
           return [subtree_sum for subtree_sum, frequency in subtree_sum_counter.items() if frequency == max_frequency]
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Java Solution
   import java.util.ArrayList;
  2 import java.util.HashMap;
    import java.util.List;
     import java.util.Map;
    // Definition for a binary tree node.
    class TreeNode {
         int val;
         TreeNode left;
        TreeNode right;
         TreeNode() {}
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 12
         TreeNode(int val) {
 13
             this.val = val;
 14
 15
         TreeNode(int val, TreeNode left, TreeNode right) {
 16
             this.val = val;
 17
             this.left = left;
 18
             this.right = right;
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 21
    class Solution {
 23
         // A map to keep track of the sum occurrences.
 24
         private Map<Integer, Integer> sumFrequency;
 25
 26
         // A variable to keep track of the maximum frequency of the sum.
 27
         private int maxFrequency;
 28
 29
         // Method to find the tree sums that appear most frequently.
 30
         public int[] findFrequentTreeSum(TreeNode root) {
 31
             sumFrequency = new HashMap<>();
 32
             maxFrequency = Integer.MIN_VALUE;
```

### 63 64 // Update the frequency of the sum in the map. sumFrequency.put(sum, sumFrequency.getOrDefault(sum, 0) + 1); 65 66 67 // Update the maximum frequency if necessary. 68 maxFrequency = Math.max(maxFrequency, sumFrequency.get(sum));

C++ Solution

```
1 #include <unordered_map>
  2 #include <vector>
    #include <climits> // For INT_MIN
    // Definition for a binary tree node.
  6 struct TreeNode {
         int val;
        TreeNode* left;
        TreeNode* right;
        TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
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        TreeNode(int x, TreeNode* left, TreeNode* right) : val(x), left(left), right(right) {}
 12 };
 13
 14 class Solution {
 15 public:
 16
        // Using an unordered map to keep track of the sum frequencies
         std::unordered_map<int, int> sumFrequency;
 17
        // Variable to keep track of the highest frequency encountered
 18
         int maxFrequency;
 19
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 21
        // Constructor initializes the maximum frequency to the minimum integer value
 22
         Solution() : maxFrequency(INT_MIN) {}
 23
 24
         // Function to find the most frequent subtree sums
 25
         vector<int> findFrequentTreeSum(TreeNode* root) {
 26
             // Reset the max frequency for each call
             maxFrequency = INT_MIN;
 27
 28
             // Calculate the subtree sums starting from the root
 29
             depthFirstSearch(root);
             vector<int> result;
 30
             // Iterate over the counter map and select the sums with frequency equal to maxFrequency
 31
 32
             for (auto& entry : sumFrequency) {
 33
                 if (entry.second == maxFrequency) {
 34
                     result.push_back(entry.first);
 35
 36
 37
             return result;
 38
 39
 40
         // Helper function to perform a depth-first search and calculate subtree sums
 41
         int depthFirstSearch(TreeNode* node) {
 42
             // If the node is null, return 0 as it contributes nothing to the sum
 43
             if (!node) {
 44
                 return 0;
 45
 46
             // Calculate the sum of the current subtree
 47
             int sum = node->val + depthFirstSearch(node->left) + depthFirstSearch(node->right);
 48
             // Increment the frequency count for the current sum
 49
             ++sumFrequency[sum];
             // Update the max frequency if the current sum's frequency is higher
 50
 51
             maxFrequency = std::max(maxFrequency, sumFrequency[sum]);
             // Return the sum of this subtree to be used by its parent
 52
 53
             return sum;
 54
 55 };
 56
Typescript Solution
    // TypeScript function to find all subtree sums occurring with the highest frequency in a binary tree.
    // TreeNode class definition
    class TreeNode {
         val: number;
```

### 49 for (const [sum, frequency] of sumFrequencyMap) { if (frequency === maxFrequency) { 50 51 mostFrequentSums.push(sum); 52 53 54

left: TreeNode | null;

let maxFrequency = 0;

if (node === null) {

// Update the frequency map

return 0;

return subtreeSum;

calculateSubtreeSum(root);

const mostFrequentSums = [];

return mostFrequentSums;

Time and Space Complexity

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};

13 }

right: TreeNode | null;

this.val = (val === undefined ? 0 : val);

this.left = (left === undefined ? null : left);

function findFrequentTreeSum(root: TreeNode | null): number[] {

const leftSum = calculateSubtreeSum(node.left);

const rightSum = calculateSubtreeSum(node.right);

const subtreeSum = node.val + leftSum + rightSum;

sumFrequencyMap.set(subtreeSum, currentFrequency);

// Start the subtree sum calculation from the root

// Array to store the most frequent subtree sums

// Find all sums that have the max frequency

// Return the most frequent subtree sums

// Update the max frequency if the current one is greater

maxFrequency = Math.max(maxFrequency, currentFrequency);

const sumFrequencyMap = new Map<number, number>();

// Map to store subtree sum frequencies

this.right = (right === undefined ? null : right);

// Function to calculate the subtree sums with the highest frequency.

// Variable to keep track of the highest frequency of subtree sum

const calculateSubtreeSum = (node: TreeNode | null): number => {

// Depth-first search function to explore the tree and calculate the sums

const currentFrequency = (sumFrequencyMap.get(subtreeSum) ?? 0) + 1;

constructor(val?: number, left?: TreeNode | null, right?: TreeNode | null) {

# 1. DFS Traversal: Every node in the given binary tree is visited exactly once. If the tree has N nodes, the DFS traversal takes O(N) time. 2. Counter Operations:

object that is used as a hash map.

**Time Complexity** 

be considered 0(1) for each update since Counter uses a hash table for storage. Max Operation: The operation max(counter.values()) is performed once and takes 0(N) time in the worst case because it scans through all values in the counter.

Update: The update of the Counter counter for each subtree sum happens N times (once for each node). This operation can

The time complexity of the code is mainly determined by the DFS traversal of the tree and the operations performed on the Counter

**Space Complexity** 

The space complexity of the code is a combination of the space used by the recursion stack during the DFS traversal and the space

used by the Counter. 1. DFS Recursion Stack: In the worst case, i.e., when the tree is completely unbalanced, the height of the tree could be N, leading to a recursion stack depth of O(N). In the best case, i.e., when the tree is perfectly balanced, the height of the tree would be

In total, we have O(N) for DFS and O(N) for the max operation, which is linear. Thus, the overall time complexity is O(N).

this could be O(N) distinct sums if every subtree has a unique sum. Therefore, the overall space complexity of the algorithm is O(N) in the worst case, which includes the space for the Counter and the

Counter: The Counter object counter can potentially store a distinct sum for each subtree of the binary tree. In the worst case,

- log(N), leading to a recursion stack depth of O(log(N)). Thus, the space used by the recursion stack can vary between
  - recursion stack.

O(log(N)) and O(N).