Medium

Bit Manipulation String Backtracking

Problem Description

characters individually to either lowercase or uppercase, which can lead to various permutations of the string with different cases for each letter. The task is to generate all possible strings with these different case transformations and return them as a list in any order.

In this problem, we're given a string s consisting of alphabetical characters. We have the freedom to change each of these

This is a typical backtracking problem, as we'll consider each character and explore the possibilities of both keeping it as it is or

An example to illustrate this: for the string "a1b2", the output will be ["a1b2", "a1B2", "A1b2", "A1B2"].

changing its case, accumulating all different strings that can be formed by these choices.

To achieve our solution, we can apply a method known as depth-first search (DFS), which is a type of backtracking algorithm. The

Intuition

DFS approach will help us traverse through all possible combinations of uppercase and lowercase transformations of the characters within the string. Here's the intuition breakdown for solving this problem:

1. Start from the first character: We begin the process with the first character of the string.

- 2. **Recursive exploration**: For each character, we have two choices (provided it's an alphabetical character and not a digit):
- Keep the current character as is and proceed to the next one.
 Change the current character's case (from lowercase to uppercase or vice versa) and move to the next one.
- 3. **Base case**: If we reach the end of the string (i.e., index i is equal to the string length), we've completed a permutation and it's added to the list of results.

defined within the scope of the letterCasePermutation method.

- 4. Backtracking: After exploring one option (like keeping the character as is) for the current position, we backtrack to explore the other option (changing the case).5. Result accumulation: As we hit the base case at different recursive call levels, we collect all permutations of the string.
- This recursive approach works because it explores all possible combinations by trying each option at each step. The use of the bitwise XOR operation ^ 32 is a clever trick to toggle the case of an alphabetical character since converting between lowercase to
- uppercase (or vice versa) in ASCII entails flipping the 6th bit.

Solution Approach

The provided solution uses a Depth-First Search (DFS) algorithm along with a recursive helper function named dfs. This function is

Here's a step-by-step walk-through of the solution code: 1. A new list t is created from the original string s which is going to hold the characters that we are currently exploring through

are currently exploring.

the resulting strings appended to ans.

Example Walkthrough

the next character.

DFS.

4. In the body of the dfs function, the base case checks if the index i is greater than or equal to the length of s. If it is, it means

2. An empty list ans is initialized which will eventually contain all the possible permutations of the string.

we've constructed a valid permutation of string s in the list t and we append this permutation to ans.

5. If the base case condition is not met, we first call dfs(i + 1) without altering the current character. This recurses on the decision to keep the current character as is.

3. The dfs function defined inside the letterCasePermutation takes a single argument i, which is the index of the character in t we

value back to the character. After changing the case, we call dfs(i + 1) again, exploring the decision tree path where the current character's case is toggled.

6. Next, if the current character is alphabetic (t[i].isalpha()), we toggle its case using t[i] = chr(ord(t[i]) ^ 32). The ord

function gets the ASCII value of the character, ^ 32 toggles the 6th bit which changes the case, and chr converts the ASCII

7. By recursively calling dfs with 'unchanged' and 'changed' states of each character, all combinations are eventually visited, and

possibility. The data structure used is a basic Python list which conveniently allows us to both change individual elements in place and join them into strings when we need to add a permutation to the results.

The DFS here is a recursive pattern that explores each possibility and undoes (backtracks) that choice before exploring the next

We start by setting up an empty list ans that will store our final permutations and a list t from the string s, which is "0a1". List t will hold the characters that we are currently exploring through the DFS algorithm.
 Since the first character '0' is not an alphabetical character, we only have one option for it; we keep it as is. So, we move on to

∘ Keep 'a' as it is and proceed to the next character, which will be '1'. This sequence is "0a1". Since '1' is not alphabetical, we

3. The next character is 'a'. Here, we have two choices:

regarding the case of alphabetic characters.

two different string permutations: "0a1" and "0A1".

def dfs(index):

dfs(index + 1)

dfs(index + 1)

generatePermutations(index + 1);

charArray[index] ^= ' ';

if (Character.isLetter(charArray[index])) {

std::function<void(int)> dfs = [&](int index) {

permutations.emplace_back(str);

// we toggle its case and recursively continue

if (index >= str.size()) {

if (isalpha(str[index])) {

return;

dfs(index + 1);

generatePermutations(index + 1);

def letterCasePermutation(self, s: str) -> List[str]:

Helper function for depth-first search

Let's illustrate the solution approach with a small example using the string "0a1".

keep it as is and add "0a1" to ans.

• Toggle the case of 'a' to 'A' and then proceed to the next character, '1'. This sequence is "0A1". Again, we keep '1' as it is and add "0A1" to ans.

4. At this point, the dfs function has recursively explored and returned from both branches for character 'a', and the two

permutations of the string are saved in ans, which now contains ["0a1", "0A1"].

5. Since there are no more characters to explore, the recursion terminates, and the ans list now holds all the possible permutations

And that's the end of the example. The original list "0a1" only had one alphabetical character that could be toggled, which resulted in

Python Solution

1 class Solution:

Base case: if the current index is equal to the length of the string

Recursive case: move to the next character without changing the case

If the current character is alphabetic, we can change its case

current_string[index] = chr(ord(current_string[index]) ^ 32)

// If the current character is alphabetic, toggle its case and proceed with recursion

// IMPORTANT: revert the character back to its original case after the recursive call

Revert the change for backtracking purposes

if index == len(s):
 # Append the current permutation to the answer list
 permutations.append(''.join(current_string))
return

```
if current_string[index].isalpha():
    # Flip the case: if the current character is uppercase, make it lowercase and vice versa
    current_string[index] = chr(ord(current_string[index]) ^ 32)
# Continue the search with the flipped case character
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           # Convert the input string to a list, making it mutable
24
           current_string = list(s)
           # Initialize a list to store all possible permutations
25
26
           permutations = []
27
           # Start the depth-first search from the first character
28
           dfs(0)
29
           # Return the computed permutations
30
           return permutations
31
32 # Example of usage:
33 # sol = Solution()
34 # result = sol.letterCasePermutation("a1b2")
35 # print(result) # Output: ["a1b2", "a1B2", "A1b2", "A1B2"]
Java Solution
 1 class Solution {
       private List<String> permutations = new ArrayList<>(); // List to hold the string permutations
       private char[] charArray; // Character array to facilitate permutation generation
       // Public method to generate letter case permutations for a given string
       public List<String> letterCasePermutation(String s) {
           charArray = s.toCharArray(); // Convert string to character array for modification
           generatePermutations(0); // Start recursion from the first character
           return permutations; // Return all generated permutations
10
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12
       // Helper method to recursively generate permutations
       private void generatePermutations(int index) {
13
           // Base case: If the end of the array is reached, add the current permutation to the list
14
15
           if (index >= charArray.length) {
               permutations.add(new String(charArray));
16
17
               return;
18
           // Recursively call the method to handle the next character without modification
19
```

// Toggle the case: lowercase to uppercase or vice versa using XOR operation with the space character

charArray[index] ^= ' '; // This step ensures the original structure is intact for future permutations

// If the character is not alphabet, it is left as—is and the recursion takes care of other characters

// Utility lambda function to perform a Depth-First Search (DFS) for all possible letter case combinations

// Base case: if we reach the end of the string, add the current permutation to the results

// Recursive case: continue with the next character without changing the current one

// Toggle the case of the current character: lowercase to uppercase or vice versa

// Only if the current character is alphabetical (either uppercase or lowercase)

6 public: 7 // Function to generate all permutations of a string where each letter can be lowercase or uppercase 8 std::vector<std::string> letterCasePermutation(std::string str) { 9 // Resultant vector to store all permutations 10 std::vector<std::string> permutations;

C++ Solution

1 #include <vector>

2 #include <string>

class Solution {

#include <functional>

```
// XOR with 32 takes advantage of the fact that the ASCII values of upper and lower case
28
                    // letters differ by exactly 32
29
                     str[index] ^= 32;
30
                     // Recursive call with the case of the current character toggled
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                     dfs(index + 1);
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                    // Optional: Toggle the case back if you want to use the original string elsewhere
                    // after this function call. If str is not used after this, you can omit this step.
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36
                    // str[index] ^= 32;
37
38
            };
39
            // Start DFS from index 0
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            dfs(0);
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43
            // Return all generated permutations
44
            return permutations;
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46 };
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Typescript Solution
 1 // Function that generates all possible permutations of a string
 2 // with letters toggled between uppercase and lowercase.
 3 // It uses Depth-First Search (DFS) to explore all variations.
    function letterCasePermutation(s: string): string[] {
       const length = s.length;
const charArray = [...s];
const results: string[] = [];
// The length of the input string
// Converts the string to an array of characters
// Stores the resulting permutations
        // Helper function to perform DFS
 9
        const dfs = (index: number) => {
10
            if (index === length) {
                                                  // If the end of the string is reached,
11
12
                results.push(charArray.join('')); // join the characters to form a permutation and add to results.
13
                return;
14
                                                    // Recursive call with the next character (no change)
15
            dfs(index + 1);
16
17
            // Check if the current character is a letter and can change case
            if (isLetter(charArray[index])) {
18
                toggleCase(charArray, index); // Toggle the case of the character at the current index
19
20
                dfs(index + 1);
                                                    // Recursive call with the toggled character
21
22
        };
23
        // Function to check if a character is a letter (could be replaced with regex or other methods)
24
        function isLetter(c: string): boolean {
25
            return (c >= 'A' && c <= 'Z') || (c >= 'a' && c <= 'z');
26
27
28
```

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Time and Space Complexity

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To analyze the time complexity, let us consider the number of permutations possible for a string with n characters. Each character can either remain unchanged or change its case if it's an alphabetic character. For each alphabetic character, there are 2 possibilities

The given Python code generates all possible permutations of a string s where the permutation can include lowercase and

// Function that toggles the case of a letter by using bitwise XOR with the space character (32)

uppercase characters. A depth-first search (DFS) algorithm is employed to explore all possibilities.

function toggleCase(arr: string[], index: number): void {

dfs(0); // Start the DFS from the first character

return results; // Return the array of permutations

arr[index] = String.fromCharCode(arr[index].charCodeAt(0) ^ 32);

alphabetic characters in the string, there would be 2ⁿ different permutations.

 $0(2^m * n)$ as we store 2^m permutations, each of length n.

the output), then the space complexity would be O(n).

changed), and it's called once for each non-alphabetic character. Thus, the time complexity of this process can be represented as: $0(2^m * n)$, where n is the length of the string and m is the number of alphabetic characters in the string as each permutation includes building a string of length n.

Space Complexity:

(uppercase or lowercase), while non-alphabetic characters have only 1 possibility (as they don't have case). If we assume there are m

However, one might consider the space used for each layer of the recursion separately from the space used to store the results since the latter is part of the problem's output. If we only consider the space complexity for the recursion (excluding the space for

The space complexity includes the space needed for the recursion call stack as well as the space for storing all the permutations.

The maximum depth of the recursive call stack would be n, as that's the deepest the DFS would go. The space needed for ans will be

Combining both the space for the recursion and the output, the space complexity can be represented as: $0(2^m * n + n), \text{ which simplifies to } 0(2^m * n) \text{ when considering } 2^m \text{ to be significantly larger than } n.$

In conclusion, the time complexity is $0(2^m * n)$ and the space complexity is $0(2^m * n)$ when accounting for both the recursion stack and the output list.

The DFS function is recursively called twice for each alphabetic character (once without changing the case, once with the case changed), and it's called once for each non-alphabetic character. Thus, the time complexity of this process can be represented

Time Complexity: