1255. Maximum Score Words Formed by Letters Bit Manipulation Bitmask Array String Dynamic Programming Backtracking Hard

Problem Description

The words come from a list called words, and we are given a list of available single letters which may contain duplicates. Each letter in letters can be used only once. The score for each letter is given by an array score, where score[0] corresponds to the score of 'a', score [1] to the score of 'b', and so on unto score [25], which corresponds to the score of 'z'. The goal is to select words from the words list in such a way that we can form them from the letters in the letters list without reusing any single letter more than its available count. We cannot use any word more than once. We should return the highest possible score that can be obtained from any combination of the words formed.

The given problem is an optimization challenge where we have to find the maximum score achievable by forming valid sets of words

from a given list. Each word has an associated score based on the characters it contains and a score table provided for the alphabet.

Leetcode Link

Intuition

To solve the problem, we think of all possible subsets of the provided words array. For each subset, we calculate the score of its

constituent words if it's possible to create the subset with the given letters. We only consider a subset valid if each letter required

to form this subset of words is available the required number of times in the letters list. We use bitwise operations to generate possible subsets.

2ⁿ possible subsets. We can represent the subsets using a bitmask of length n, where the j-th bit indicates whether or not to include the j-th word in the subset. Counting letters in words: We use a data structure, Counter, to count the occurrences of each letter in both the currently considered subset of words and the available letters.

Generating subsets: We use a binary representation of numbers to iterate over all possible subsets. For a list of n words, there are

Checking validity and score calculation: For a chosen subset, we check if it can be created with the given letters by ensuring the count of each letter in the subset does not exceed the count of available letters. If valid, we calculate the subset's score by summing the individual character scores. This is done by referring to the supplied score array using the character's ASCII value adjusted with

the ASCII value of 'a' to correctly index into the score list. Maximizing the score: We compare each valid subset's score to the current known maximum score and update the maximum score if a higher one is found.

Optimization: Although the proposed solution methodically generates all potential subsets and assesses each one, it is not efficient for large lists of words due to its exponential time complexity. However, this brute-force approach provides a direct and complete search of the solution space, which is acceptable for smaller inputs.

The implementation of the solution can be explained step by step as follows: 1. Initialization: A Counter object named cnt is created to store the count of each available letter in the letters list. Next, the length of the words list is stored in variable n, and a variable ans is initialized to zero to keep track of the maximum score.

the number of words. Inside the loop, each number represents a subset where each bit in the binary representation of the number indicates the presence (1) or absence (0) of a word at that index in the subset. 3. Building a subset: For each number i in the loop, we use a list comprehension to collect words corresponding to set bits in the

binary representation of the number. This is done with [words[j] for j in range(n) if i >> j & 1]. Then, a Counter object

there is a sufficient number of letters in cnt (v <= cnt[c]). This ensures that the current subset can be formed from the available

2. Iterating over subsets: A for loop is used to iterate through numbers 0 to 2^n - 1 representing all possible subsets where n is

named cur is created to store the count of each letter in this subset of words. 4. Checking if the subset is valid: The all function is used to verify that for all characters c and their count v in the subset cur,

Solution Approach

Let's walk through a small example to illustrate the solution approach:

letters = ["a", "a", "c", "d", "d", "g", "o", "o"]

ord('a') gives the index of the score for that character in the score array.

letters without reusing any letter more than available.

obtained from any valid subset of words.

Assume we have the following inputs:

words = ["dog", "cat", "dad", "good"]

 \circ Total subset score is 4 + 3 = 7.

1 from collections import Counter

from typing import List

class Solution:

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};

will be 8, which is the result returned by the function.

Count the frequency of each letter available

available_letter_count = Counter(letters)

Determine the total number of words

for i in range(1 << number_of_words):</pre>

number_of_words = len(words)

maximum_score = 0

Initialize the maximum score

- 5. Calculating the score of the subset: If the subset is valid, the score is computed using the sum function. For each character c and its count v in cur, the expression v * score[ord(c) - ord('a')] calculates the total score of the character in the subset by multiplying its count with its respective score in score. The ord function gets the ASCII value of the character, and subtracting
- 6. Updating the maximum score: The score of the current valid subset t is compared with the current ans, and if t is greater, ans is updated to t. 7. Returning the result: After the loop finishes executing, the final value of ans is returned, which contains the maximum score

The solution uses a bitmasking technique to generate all possible subsets of words and a Counter data structure to efficiently

count the occurrences of letters in both the available letters and each subset of words. The brute-force approach checks each

subset for validity and calculates its score independently. Despite its simplicity, the time complexity of this solution is 0(2^n * (m +

k)), where n is the number of words, m is the length of the longest word, and k is the number of unique characters in letters, which

- may not be performant for large datasets. Example Walkthrough
- The score array only shows the scores for the relevant characters for brevity. 1. Initialization: We calculate the count of each letter in the letters list. The counter would look like cnt = {'a': 2, 'c': 1, 'd': 2, 'g': 1, 'o': 2}. The number of words n = 4, and the starting maximum score ans = 0.

2. Iterating over subsets: We generate numbers from 0 to 2^n - 1 which is from 0 to 15 for n = 4. Each representation will be from

"cat". We determine the count of letters in the subset, cur = Counter("dogcat") = {'d': 1, 'o': 1, 'g': 1, 'c': 1, 'a': 1}.

4. Checking if the subset is valid: We compare cur against cnt and find that all letters in cur are less than or equal to those in cnt

({'d': 1, 'o': 1, 'g': 1, 'c': 1, 'a': 1} vs. {'a': 2, 'c': 1, 'd': 2, 'g': 1, 'o': 2}). Therefore, the subset is valid.

• "dog" contributes 1*score[3] + 1*score[14] + 1*score[6] = 1*1 + 1*1 + 1*2 = 4 because score[3] for 'd', score[14] for

3. Building a subset: When the loop is at i = 3 (binary 0011), it indicates including words [0] and words [1] which are "dog" and

• score = [1, 0, ..., 2, ..., 0, ..., 1, ..., 0, 2] // score for "a" is 1, "c" is 2, "d" is 1, "g" is 2, "o" is 1

'o', and score[6] for 'g'. o "cat" contributes 1*score[2] + 1*score[0] + 1*score[19] = 1*2 + 1*1 + 1*0 = 3 because score[2] for 'c', score[0] for 'a'.

6. Updating the maximum score: Since 7 is greater than 0, we update ans to 7.

0000 to 1111 in binary, corresponding to taking none or all the words, respectively.

5. Calculating the score of the subset: The score for the subset "dogcat" is calculated as follows:

7. Continuing: The loop continues, testing the validity of other subsets and updating ans as necessary. After testing all possible subsets, the highest score found is returned. For instance, if the algorithm later encounters the subset "good" with a higher score than 7, ans will be updated accordingly.

8. Returning the result: After completion, suppose the highest score was achieved by the subset "good" and it was 8. Then, ans

This walkthrough exemplifies the steps and considerations of the solution approach on a smaller scale of inputs, demonstrating how

the brute-force method selects and sums up word scores to find the maximum possible score given the constraints.

def max_score_words(self, words: List[str], letters: List[str], score: List[int]) -> int:

Iterate over all combinations of words using binary representation

Each bit in 'i' represents whether to include a word at that position or not

Check if the combination of words can be built with the given letters

Calculate the score for the current combination of words

Update the maximum score if the current score is higher

* Calculates the maximum score achievable by forming words from the given letters.

int[] currentCount = new int[26]; // To hold the count for current combination.

if $(((i >> j) \& 1) == 1) \{ // Check if the j-th word is included.$

currentCount[c - 'a']++; // Count the characters for the word.

* @param words An array of words to be considered for scoring.

* @param score An array representing the score for each alphabet letter.

public int maxScoreWords(String[] words, char[] letters, int[] score) {

* @param letters An array of letters available to form words.

int maxScore = 0; // Keep track of the maximum score.

// Loop through each combination of words possible.

// Check each word in the current combination.

for (char c : words[j].toCharArray()) {

for (int i = 0; i < (1 << wordCount); ++i) {</pre>

for (int j = 0; j < wordCount; ++j) {</pre>

* @return The maximum score achievable.

int wordCount = words.length;

maximum_score = max(maximum_score, current_score)

Use a Counter to track the frequency of letters in the chosen combination of words

current_word_count = Counter(''.join(words[j] for j in range(number_of_words) if (i >> j) & 1))

- **Python Solution**
- 27 28 # Return the maximum score found 29 return maximum_score 30

current_score = sum(current_word_count[letter] * score[ord(letter) - ord('a')] for letter in current_word_count)

if all(current_word_count[letter] <= available_letter_count[letter] for letter in current_word_count):</pre>

```
// Keep track of letter counts in the given letters array.
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13
       int[] letterCounts = new int[26];
14
       for (char letter : letters) {
15
         // Increment the count for encountered letter.
16
         letterCounts[letter - 'a']++;
17
```

Java Solution

/**

*/

1 class Solution {

```
34
           // Verify if current combination can be made from available letters.
 35
           boolean isCombinationValid = true;
           int currentScore = 0;
 36
 37
           for (int j = 0; j < 26; ++j) {
             if (currentCount[j] > letterCounts[j]) { // More letters required than available.
 38
 39
               isCombinationValid = false;
              break;
 41
             currentScore += currentCount[j] * score[j]; // Accumulate score for the current combination.
 42
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           // Update maxScore if this combination is valid and its score is higher.
           if (isCombinationValid && maxScore < currentScore) {</pre>
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             maxScore = currentScore;
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         // Return the maximum score after evaluating all combinations.
 52
         return maxScore;
 53
 54 }
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C++ Solution
  1 class Solution {
  2 public:
         // Function to calculate the maximum score of a set of words given a set of letters and their corresponding scores.
         int maxScoreWords(vector<string>& words, vector<char>& letters, vector<int>& score) {
             int letterCounts[26] = {0}; // Array to hold counts of each letter in 'letters'
             // Count the occurrence of each letter in 'letters'
  6
             for (char& letter : letters) {
                 letterCounts[letter - 'a']++; // Increment the count for the corresponding letter
 10
 11
             int numWords = words.size(); // Total number of words
 12
             int maxScore = 0; // Variable to store the maximum score
 13
             // Loop through all combinations of words
 14
             for (int combination = 0; combination < (1 << numWords); ++combination) {</pre>
 15
                 int wordCounts[26] = {0}; // Current letter counts for the current combination of words
 16
 17
                 // Build the count for the current combination
                 for (int wordIndex = 0; wordIndex < numWords; ++wordIndex) {</pre>
 18
                     // Check if the word at wordIndex is included in the current combination
 20
                     if (combination >> wordIndex & 1) {
                         // If so, count each letter in the word
 21
 22
                         for (char& letter : words[wordIndex]) {
 23
                             wordCounts[letter - 'a']++; // Increment the count for the corresponding letter
 24
 25
 26
```

bool isValidCombination = true; // Flag to check if the combination is valid

break; // No need to continue if the combination is invalid

// If any letter count exceeds what is available, the combination is invalid

// If the combination is valid and the score is higher than the maximum found so far, update maxScore

int currentScore = 0; // Score for the current combination

// Calculate score for the current combination

if (isValidCombination && maxScore < currentScore) {</pre>

1 // Initializes the letter count array to track the occurrences of each letter.

3 // Variables to hold the words, letters, and score for global access.

8 // Preprocesses the 'letters' array to populate the 'letterCounts'.

letterCounts[letter.charCodeAt(0) - 'a'.charCodeAt(0)]++;

// Return the maximum score possible with the given words and letters

isValidCombination = false;

maxScore = currentScore;

2 const letterCounts: number[] = Array(26).fill(0);

5 // Maximum score initialized to zero.

for (const letter of letters) {

function preprocessLetters() {

4 let words: string[], letters: string[], score: number[];

return maxScore;

Typescript Solution

6 let maxScore: number = 0;

for (int letterIndex = 0; letterIndex < 26; ++letterIndex) {</pre>

if (wordCounts[letterIndex] > letterCounts[letterIndex]) {

currentScore += wordCounts[letterIndex] * score[letterIndex];

// Calculates the maximum score for a combination of words. 16 function calculateMaxScore() { const numWords = words.length; 17 18 19

```
// Iterates through all possible combinations of words using bitwise operations.
       for (let combination = 0; combination < (1 << numWords); ++combination) {</pre>
         const wordCounts = Array(26).fill(0); // Letter counts for the current combination.
 20
 21
         // Builds the count for the current combination by iterating through each word.
 22
         for (let wordIndex = 0; wordIndex < numWords; ++wordIndex) {</pre>
 23
           // Checks if the word at 'wordIndex' is included in the current combination.
           if (combination & (1 << wordIndex)) {
 24
 25
             // Increments the count for each letter in the word.
 26
             for (const letter of words[wordIndex]) {
 27
               wordCounts[letter.charCodeAt(0) - 'a'.charCodeAt(0)]++;
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 31
 32
         let isValidCombination: boolean = true; // Flag to check the combination's validity.
 33
         let currentScore: number = 0; // Score accumulator for the current combination.
 34
         // Calculating score and checking the validity of the combination.
 35
         for (let letterIndex = 0; letterIndex < 26; ++letterIndex) {</pre>
 36
           // If the letter count exceeds the available count, mark the combination as invalid.
 37
           if (wordCounts[letterIndex] > letterCounts[letterIndex]) {
 38
             isValidCombination = false;
 39
             break;
 40
 41
           // Summing up the score for the current combination.
           currentScore += wordCounts[letterIndex] * score[letterIndex];
 42
 43
 44
         // Update maxScore if the current score is greater and the combination is valid.
 45
 46
         if (isValidCombination && maxScore < currentScore) {</pre>
 47
           maxScore = currentScore;
 48
 49
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 51
     // Function to initiate the calculation of max score by processing the input data.
     function maxScoreWords(wordsInput: string[], lettersInput: string[], scoreInput: number[]): number {
       words = wordsInput;
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       letters = lettersInput;
 55
 56
       score = scoreInput;
 57
       preprocessLetters(); // Fills the letterCounts based on the letters available
       calculateMaxScore(); // Calculates the score for each possible combination
 58
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       return maxScore; // Returns the highest score found
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Time and Space Complexity
The given code snippet is a solution to the problem of finding the maximum score from forming words using given letters with each
letter having a score.
Time Complexity:
To analyze the time complexity, let's consider n to be the number of words and 1 to be the total number of letters across all words.
 1. The code uses a bit mask to generate all possible combinations of words, which results in 2<sup>n</sup> combinations as it iterates over a
```

dominates the constant 26 and 1.

Space Complexity:

range of size 2ⁿ.

Now, let's look at the space complexity: 1. The counter cnt stores the frequency of each letter available. This is at most 0(26), which is a constant 0(1) because we only

- 2. The cur counter inside the loop could store at most 0(26) entries due to the lowercase letters, so this is also 0(1).
- 3. The list [words[j] for j in range(n) if i >> j & 1] is ephemeral and its space complexity in terms of the number of characters it can hold is up to 0(1), when all words are selected.

Considering all the above, the space complexity of the code is dominated by the space needed for the ephemeral list of selected

2. For each combination, it attempts to create a Counter object for the selected words. This operation is linear with respect to the

3. The all function inside the loop checks if all letters in the current combination are less than or equal to the count of available

length of the concatenated string of chosen words. In the worst case, this could be 0(1) when all words are chosen.

letters. This runs in 0(26) since there are 26 lowercase English letters, in the worst case where every letter is used.

4. The sum function, which calculates the total score of current combination of words, will iterate over each character in the

To summarize, the time complexity is $0(2^n * 1)$, and the space complexity is 0(1 + n).

4. The combination bitmask takes up to O(n) space to store the indices of words.

words and the bitmask, and hence it is 0(1 + n).

have 26 letters.

concatenated string. This is O(1) in the worst case for the same reason as step 2. 5. Updating the maximum answer ans is 0(1) for each of the 2ⁿ combinations. Combining these steps, the worst-case time complexity is $0(2^n * (1 + 26 + 1 + 1))$, which simplifies to $0(2^n * 1)$ as 1