1749. Maximum Absolute Sum of Any Subarray

**Dynamic Programming** 

larger than the maximum positive subarray sum.

## **Problem Description**

Array

Medium

clarify a few things first. A subarray is a contiguous part of the original array, and it can be as small as zero elements or as large as the entire array. The absolute sum is the total sum in which we consider a negative total as its positive counterpart (that is, we apply the absolute value operation to the sum). We can denote it mathematically as abs(sum) where sum is the sum of elements in the subarray. Now, the maximum absolute sum is the highest value of abs(sum) that you can get from all possible subarrays of nums.

You are given an array of integers called <a href="nums">nums</a>. The task is to find the maximum absolute sum of any subarray of this array. Let's

### The intuition behind the solution comes from dynamic programming, a method where we build up to the solution by solving

ntuition

consider both positive and negative numbers effectively because the maximum absolute sum could come from a subarray with a very negative sum due to the absolute value operation. We define two variables, f and g, that will represent the maximum and minimum subarray sum ending at the current position, respectively. As we move through the array, we keep updating these values. If f drops below zero, we reset it to zero because a subarray with a negative sum would not contribute to a maximum absolute sum; we should instead start a new subarray from the

subproblems and using those solutions to solve larger problems. Here, we aim to track two values while iterating through the

array: the maximum subarray sum so far and the minimum subarray sum so far. By keeping track of both, we can ensure that we

next element. Similarly, if g becomes positive, we reset it to zero, starting a new subarray for the minimum sum calculation. f keeps track of the maximum sum achieved so far (without taking the absolute value), and g does the same for the minimum sum. Notice that for g, we take the absolute value to compare with the max value f, because we are interested in the maximum absolute sum. Our final answer is the maximum between f and the absolute value of g throughout the entire pass. This is because for a negative subarray to contribute to the maximum absolute sum, its absolute value should be taken which might be

The brilliance of this method lies in the realization that we don't need to maintain a full array of sums, but simply update our two tracking variables as we iterate through nums. This simplifies the process and reduces our space complexity to 0(1). **Solution Approach** 

The solution uses a simple yet powerful approach based on dynamic programming, which enables us to keep track of the maximum and minimum sums of subarrays that we have encountered so far. The dynamic programming is apparent in the way we

update our running accumulations f and g, and in how they depend solely on the values at the previous index.

We also have a variable ans to store the global maximum absolute sum that we will eventually return.

#### We initialize two variables, f and g, to store the current subarray's maximum and minimum sum, respectively. •

Let's go over the logic in detail:

As we iterate over each element x in nums, we update f and g for every position: of is updated to be the maximum of freset to 0 (if it was negative) plus the current element x. This effectively means, if accumulating a sum including x leads to a sum less than zero, we are better off starting a new subarray at the next position.

f[i] = max(f[i - 1], 0) + nums[i]

The state transition for g is:

g[i] = min(g[i - 1], 0) + nums[i]

For f, the state transition can be written as:

absolute value of the current minimum subarray sum.

- ogis updated to be the minimum of greset to 0 (if it was positive) plus the current element x. This keeps track of the negative sums,
- which, when their absolute value is taken, may contribute to the absolute sum.
- After the loop completes, ans holds the maximum absolute sum possible from all the subarrays of nums. The beauty of this algorithm lies in the fact that it computes the answer in a single pass through the input array with O(n) time

complexity, where n is the length of nums, and it does so with 0(1) additional space complexity, since it doesn't require storing

Remember, the original problem allowed for the subarray to be empty, which would mean an absolute sum of 0. However, this

scenario is naturally covered in our implementation because the initialization of ans starts at 0, and f and g can only increase

After updating f and g with the current element, we update our answer ans to be the maximum of ans, f, and the absolute

value of g. This ensures that ans always holds the highest value of either the current maximum subarray sum, or the

from there. The solution could also be seen as an adaptation of the famous Kadane's algorithm, which is used to find the maximum sum

**Example Walkthrough** Let's consider an example nums array to illustrate the solution approach: nums = [2, -1, -2, 3, -4]

subarray, here cleverly tweaked to also account for negative sums by the introduction of g and maximizing the absolute values.

• Initialize f and g to 0. f is the maximum subarray sum so far, and g is the minimum subarray sum so far. Also, initialize ans to 0, which will hold the final answer. Start iterating over the nums array.

#### $\circ$ Update g: g = min(0, 0) + 2 = 2 $\circ$ Update ans: ans = max(0, 2, abs(2)) = 2

First element is 2:

Second element is -1:

Third element is -2:

Fourth element is 3:

• Update f: f = max(0, 0) + 2 = 2

• Update f: f = max(2, 0) - 1 = 1

 $\circ$  Update g: g = min(2, 0) - 1 = -1

• Update f: f = max(0, 0) + 3 = 3

• Update g: g = min(0, 0) - 4 = -4

 $\circ$  Update ans: ans = max(3, 0, abs(-4)) = 4

def maxAbsoluteSum(self, nums: List[int]) -> int:

# ans stores the maximum absolute sum found so far.

The maximum absolute subarray sum.

# Iterate through each number in nums.

 $f_{max} = max(f_{max}, 0) + num$ 

an array of sums.

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\circ Update ans: ans = max(2, 1, abs(-1)) = 2
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We want to find the maximum absolute sum of any subarray of this array.

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• Update f: f = max(1, 0) - 2 = -1 (But since f is now less than 0, we reset it to 0)
\circ Update g: g = min(-1, 0) - 2 = -3
\circ Update ans: ans = max(2, 0, abs(-3)) = 3
```

 $\circ$  Update g: g = min(-3, 0) + 3 = 0 (But since g would become positive, we reset it to 0)  $\circ$  Update ans: ans = max(3, 3, abs(0)) = 3 Fifth element is -4:

Solution Implementation

from typing import List

Returns:

ans = 0

public:

**Python** 

class Solution:

 After iterating through the entire array, the final answer (ans) is 4, which is the maximum absolute sum of any subarray in nums. Thus, in this example, the maximum absolute sum is 4, obtained from the subarray [-4] whose absolute sum is abs(-4) = 4.

• Update f: f = max(3, 0) - 4 = -1 (Again, reset f to 0 since it's less than 0)

Args: nums: List[int] - the list of integers over which we want to find the maximum absolute sum.

This function finds the maximum absolute sum of any non-empty subarray of the given array.

# f max keeps track of the maximum subarray sum ending at the current position.

# q min keeps track of the minimum subarray sum ending at the current position.

# Update the maximum subarray sum ending at the current position.

# Reset to current number if the max sum becomes negative.

// Function to calculate the maximum absolute sum of any subarray of nums

// Variable to store the final maximum absolute sum

currentMaxSum = max(0, currentMaxSum) + num;

currentMinSum = min(0, currentMinSum) + num;

// Update maxAbsoluteSum if necessary

// Return the final maximum absolute sum

// Iterate over the numbers in the vector

// Initialize the variables to keep track of the current max and min subarray sum

// Update currentMaxSum: reset to zero if it becomes negative, then add the current element

// Update currentMinSum: reset to zero if it is positive, then add the current element

// Find the maximum between currentMaxSum and the absolute value of currentMinSum

nums: List[int] - the list of integers over which we want to find the maximum absolute sum.

# f max keeps track of the maximum subarray sum ending at the current position.

# q min keeps track of the minimum subarray sum ending at the current position.

# Update the maximum subarray sum ending at the current position.

# Update the minimum subarray sum ending at the current position.

# Update the ans with the larger value between the current ans,

# the current maximum subarray sum, and the absolute value of

# Reset to current number if the max sum becomes negative.

# Reset to current number if the min sum becomes positive.

maxAbsoluteSum = max({maxAbsoluteSum, currentMaxSum, abs(currentMinSum)});

int maxAbsoluteSum(vector<int>& nums) {

int currentMaxSum = 0:

int currentMinSum = 0;

int maxAbsoluteSum = 0;

for (int& num : nums) {

return maxAbsoluteSum;

#### # Update the minimum subarray sum ending at the current position. # Reset to current number if the min sum becomes positive. $g_{min} = min(g_{min}, 0) + num$

for num in nums:

 $f_{max} = g_{min} = 0$ 

```
# Update the ans with the larger value between the current ans,
            # the current maximum subarray sum, and the absolute value of
            # the current minimum subarray sum.
            ans = max(ans, f_max, abs(g_min))
        # Return the maximum absolute subarray sum found.
        return ans
Java
class Solution {
    public int maxAbsoluteSum(int[] nums) {
        int maxEndingHere = 0; // Represents the maximum subarray sum ending at the current position
        int minEndingHere = 0; // Represents the minimum subarray sum ending at the current position
        int maxAbsoluteSum = 0; // Keeps track of the maximum absolute subarray sum
        // Traverse the array
        for (int num : nums) {
            // Calculate the maximum subarray sum ending here by taking the maximum of
            // the current maximum subarray sum (extended by the current number) and 0
            maxEndingHere = Math.max(maxEndingHere + num, 0);
            // Calculate the minimum subarray sum ending here by taking the minimum of
            // the current minimum subarray sum (extended by the current number) and 0
            minEndingHere = Math.min(minEndingHere + num, 0);
            // Calculate the current maximum absolute subarray sum by taking the maximum of
            // the current maximum absolute sum, the current maximum subarray sum ending here,
            // and the absolute value of the current minimum subarray sum ending here
            maxAbsoluteSum = Math.max(maxAbsoluteSum, Math.max(maxEndingHere, Math.abs(minEndingHere)));
        // Return the overall maximum absolute subarray sum found
        return maxAbsoluteSum;
class Solution {
```

```
};
TypeScript
function maxAbsoluteSum(nums: number[]): number {
    // Initialize local variables to track the maximum subarray sum and the minimum subarray sum
    let maxSubarraySum = 0; // f represents the maximum potential subarray sum at the current index
    let minSubarraySum = 0; // g represents the minimum potential subarray sum at the current index
    let maxAbsoluteSumResult = 0; // ans is the final answer tracking the maximum absolute sum found
    // Iterate through the array of numbers
    for (const num of nums) {
        // Update the maximum subarray sum: reset to 0 if negative, or add current number
        maxSubarraySum = Math.max(maxSubarraySum, 0) + num;
        // Update the minimum subarray sum: reset to 0 if positive, or add current number
        minSubarraySum = Math.min(minSubarraySum, 0) + num;
        // Update the maximum absolute sum found so far by comparing it with the
        // current maximum subarray sum and the absolute value of the current minimum subarray sum
        maxAbsoluteSumResult = Math.max(maxAbsoluteSumResult, maxSubarraySum, -minSubarraySum);
    // Return the maximum absolute sum of any subarray
    return maxAbsoluteSumResult;
from typing import List
class Solution:
    def maxAbsoluteSum(self, nums: List[int]) -> int:
        This function finds the maximum absolute sum of any non-empty subarray of the given array.
        Aras:
```

```
# Return the maximum absolute subarray sum found.
return ans
```

Returns:

ans = 0

 $f_{max} = g_{min} = 0$ 

for num in nums:

Time and Space Complexity

The maximum absolute subarray sum.

# Iterate through each number in nums.

 $f_{max} = max(f_{max}, 0) + num$ 

 $g_{min} = min(g_{min}, 0) + num$ 

# the current minimum subarray sum.

ans = max(ans, f\_max, abs(g\_min))

# ans stores the maximum absolute sum found so far.

Time complexity The time complexity of the provided code is O(n) since it passes through the array nums once, performing a constant amount of work for each element in the array. No nested loops or recursive calls are present that would increase the complexity. Here n is the length of the array nums.

# **Space complexity**

The space complexity of the code is 0(1) because the space used does not grow with the size of the input array. Only a fixed number of variables f, g, and ans are used, irrespective of the input size.