The problem provides two arrays nums1 and nums2 of the same length n. The task is to find the number of different balanced ranges

Problem Description

Array

Hard

Dynamic Programming

within these arrays. A balanced range 1, r means that for every index i within this range, you can choose either nums1[i] or nums2[i] such that the sum of the selected elements from nums1 is equal to the sum of the selected elements from nums2.

Balanced ranges [l1, r1] and [l2, r2] are considered different if either the starting points l1 and l2 differ, the ending points r1 and r2 differ, or there is at least one index i where nums1[i] is chosen in the first range, and nums2[i] is chosen in the second range, or the other way around.

The solution is based on dynamic programming. The primary intuition is to track the difference between sums of selected elements

sum difference of 0 indicates that the sums from both nums1 and nums2 are equal.

of ways to obtain j at i, ensuring that j is large enough (j >= a).

ensure the result stays within the required modulo.

Initial Setup: First, we calculate the total sums.

1. At index 0, with nums1[0] = 1 and nums2[0] = 2:

3. At index 2, with nums1[2] = 3 and nums2[2] = 2:

and it uses the modulo operator to manage large numbers efficiently.

-5 to 6. We index f from 0, so the actual index for a zero sum difference is 5, which is s2.

f[0][1 + 5] or f[0][6] represents choosing 1 from nums1 and increases by 1.

f[0][-2 + 5] or f[0][3] represents choosing 2 from nums2 and increases by 1.

1 with the differences of j - nums1[i] and j + nums2[i], if those indices are valid.

making sure we don't exceed the range of sum differences (j+b < s1 + s2 + 1).

The solution must return the count of these distinctive balanced ranges modulo $10^9 + 7$.

how many ways you can achieve a particular sum difference up to a certain point, which in turn will help you decide how many

Intuition

balanced subranges you can form.

Here's how you arrive at the solution:

1. Create a list of lists f, where f[i][j] stores the number of ways to achieve a sum difference of j - s2 using subranges that end at index i. s2 is the total sum of nums2, and this acts as a balance point to avoid negative indices in f due to potential negative

from nums1 and nums2 at each index i when considering all possible subranges ending at that index. Essentially, you want to know

2. Iterate through each index i of the arrays, and for each i, consider adding the current value a from nums1 or subtracting the

differences.

current value b from nums2 to all previously computed sum differences to update the number of ways to achieve new differences at i based on those at index i - 1. That is, f[i][j] is updated by adding f[i - 1][j - a] and f[i - 1][j + b] considering the bounds where these indices do not go beyond the size of f.

3. Each time, keep track of the number of balanced subranges, which essentially corresponds to the value of f[i][s2] because a

- 4. The final answer is the accumulated count of balanced subranges modulo 10^9 + 7 to handle the large numbers as mentioned in the problem.
 This approach efficiently uses the concept of prefix sums and dynamic programming to solve the problem in polynomial time.
- Solution Approach
- The implementation uses dynamic programming to keep track of all the possible sum differences between nums1 and nums2 as you iterate over them. Here is a detailed walkthrough:

 1. Initialization: Two sums, s1 and s2, are calculated to represent the total sums of nums1 and nums2, respectively. A 2D list f with

dimensions [n] [s1 + s2 + 1] is created. This list will store the number of ways to obtain a sum difference at various j points, for

2. Calculating Ways for Differences: As we iterate through nums1 and nums2 with index i, we increase f[i][a + s2] and f[i][-b +

s2] by 1. This reflects the fact that selecting a from nums1 or b from nums2 at the current index contributes to one way of making

∘ We update f[i][j] by adding the number of ways to achieve a difference of j-a from the previous index i-1 to the number

each i. The +1 accommodates zero difference.

the sum difference of a - b (indexed from -b + s2 to a + s2 to shift the negative range).

 $(modulo 10^9 + 7).$

3. **Updating Counts**: If i is greater than 0, we have previous states to consider. The dynamic programming aspect comes in:

Here, j is the index representing the possible sum differences, a is the element from nums1, and b is the element from nums2.

4. Counting Balanced Ranges: The f[i][s2] entry contains the number of ways to have a zero sum difference up to index i, which corresponds to a balanced range. We add f[i][s2] to ans, the accumulated total of such balanced ranges, and apply % mod to

5. Return Result: The variable ans stores the final count and is returned to represent the number of different balanced ranges

This approach uses a dynamic table f and iterates through each element of nums1 and nums2 once, updating the counts of sum

○ We also add the number of ways to achieve a difference of j+b from index i-1 to the number of ways to obtain j at i,

Example Walkthrough

Let's consider the arrays nums1 = [1,2,3] and nums2 = [2,1,2], and walk through the described solution approach.

differences as it goes. The table f stores intermediate results that are re-used, which is a classic feature of dynamic programming,

• s2 = 2 + 1 + 2 = 5

We initialize the 2D list f with dimensions [3] [6 + 5 + 1] or [3] [12], as we have 3 elements and the sum difference can range from

2. At index 1, with nums1[1] = 2 and nums2[1] = 1:

increases by 1.

Counting Balanced Ranges:

Plugging in the numbers:

Return Result:

• s1 = 1 + 2 + 3 = 6

Calculating Ways for Differences:

f[1][2 + 5] or f[1][7] represents choosing 2 from nums1. Since i > 0, we add the values from f[0][7-2] (or f[0][5], which is currently 0) and f[0][7+1] (or f[0][8], which does not exist and is considered 0). Hence, f[1][7] increases by 1.

∘ f[1][-1 + 5] or f[1][4] represents choosing 1 from nums2 and we perform the same additions as above, so f[1][4]

• For every j from 0 to 11 (which corresponds to the range of -5 to 6), update f[i][j] by adding the values from the last index i -

○ We update f[2][3 + 5] or f[2][8] and f[2][-2 + 5] or f[2][3] similarly.Updating Counts:

1. After index 0, f[0][6] = 1 and f[0][3] = 1. No balanced range yet.

2. After index 1, f[1][7] = 1 and f[1][4] = 1. No balanced range yet.

counts = $[[0] * (sum1 + sum2 + 1) for _ in range(length)]$

for i, (num1, num2) in enumerate(zip(nums1, nums2)):

if j + num2 < sum1 + sum2 + 1:

total_count = (total_count + counts[i][sum2]) % modulo

For each index i, we add f[i][5] to ans, because f[i][5] represents the count of balanced ranges up to index i. For instance, f[2][5] will tell us the number of ways we can have a balanced subrange ending at index 2.

• After these steps, ans, now containing the total count of balanced ranges, is returned as the answer modulo 10^9 + 7.

Our ans would be 1 modulo 10^9 + 7, which is just 1, since we found one balanced range. This would be the final returned value.

3. After index 2, f[2][8] and f[2][3] are updated. We find f[2][5] = 1 indicating one balanced range [0,2].

length = len(nums1) # store the length of nums1 and nums2, which should be the same

create a 2D list to keep track of counts while avoiding index-out-of-range errors

modulo = 10**9 + 7 # the value for modulo operation to avoid large integers

update the total count for subranges that sum up to zero difference

sum1, sum2 = sum(nums1), sum(nums2) # calculate the sum of the elements in nums1 and nums2

total_count = 0 # initialize the result to accumulate the total count of valid subranges

iterate through both lists in parallel using enumerate to get both index and elements

1 from typing import List 2 3 class Solution: 4 def countSubranges(self, nums1: List[int], nums2: List[int]) -> int:

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Python Solution

counts[i][num1 + sum2] += 1 # increment the count where the first element is picked from nums1

counts[i][j] = (counts[i][j] + counts[i - 1][j + num2]) % modulo

counts[i][-num2 + sum2] += 1 # increment the count where the first element is picked from nums2

return total_count # return the total count of valid subranges

return total_count # return the total count of valid subranges

The function countSubranges calculates the number of subranges where the sum of selected elements from nums1 # equals the sum of selected elements from nums2. It modifies the subproblem's state space to make it solvable using dynamic programming, ensuring that each choice at every step is either to include

Java Solution

class Solution {

33 # an element from nums1 or an element from nums2.

public int countSubranges(int[] nums1, int[] nums2) {

int n = nums1.length; // Get the length of the input arrays.

int countSubranges(vector<int>& nums1, vector<int>& nums2) {

memset(dp, 0, sizeof(dp)); // initialize dp array to 0

const int mod = 1e9 + 7; // modulo value for the answer

for (int j = 0; $j \le sum1 + sum2$; ++j) {

if (j + b <= sum1 + sum2) {</pre>

dp[i][a + sum2]++; // If we take nums1[i], add to count

dp[i][-b + sum2]++; // If we take nums2[i], add to count

// Update the 'dp' array for the rest of the possible sums

// Calculate the number of subranges for each element

int ans = 0; // this will hold the final answer

int sum1 = accumulate(nums1.begin(), nums1.end(), 0); // sum of nums1

int sum2 = accumulate(nums2.begin(), nums2.end(), 0); // sum of nums2

// We'll use a dynamic programming array 'dp' to store the number of ways

// to get a sum taking first (i+1) elements where the sum is offset by sum2

int a = nums1[i], b = nums2[i]; // Current elements from both arrays

dp[i][j] = (dp[i][j] + dp[i - 1][j - a]) % mod;

dp[i][j] = (dp[i][j] + dp[i - 1][j + b]) % mod;

if (i > 0) { // we skip the first element because there's nothing to accumulate from

// from the previous subrange sum without current nums1[i]

// from the previous subrange sum without current nums2[i]

// Include the current nums1[i] in the subrange and add the count

// Include the current nums2[i] in the subrange and add the count

int n = nums1.size(); // size of the input arrays

// to handle negative sums.

int dp[n][sum1 + sum2 + 1];

for (int i = 0; i < n; ++i) {

if $(j >= a) {$

int sumNums1 = Arrays.stream(nums1).sum(); // Sum of all elements in nums1.

int sumNums2 = Arrays.stream(nums2).sum(); // Sum of all elements in nums2.

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// Create a 2D array to store the number of ways to form subranges.
           int[][] dp = new int[n][sumNums1 + sumNums2 + 1];
           int answer = 0; // Initialize the answer variable to store the total count of subranges.
            final int MOD = (int) 1e9 + 7; // Define the modulo value.
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           // Iterate through each element in both arrays.
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           for (int i = 0; i < n; ++i) {
               int num1 = nums1[i], num2 = nums2[i]; // Get the current elements from both arrays.
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               dp[i][num1 + sumNums2]++; // Increment the number of ways to achieve this sum with only the current element from nums1.
               dp[i][-num2 + sumNums2]++; // Increment the number of ways to achieve this sum with only the current element from nums2.
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               // If not in the first iteration, update the dp array based on previous subranges.
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               if (i > 0) {
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                    for (int j = 0; j \le sumNums1 + sumNums2; ++j) {
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                        if (j \ge num1) {
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                            dp[i][j] = (dp[i][j] + dp[i - 1][j - num1]) % MOD; // Add ways to achieve this sum including the current number
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                       if (j + num2 \le sumNums1 + sumNums2) {
                            dp[i][j] = (dp[i][j] + dp[i - 1][j + num2]) % MOD; // Add ways to achieve this sum including the current number
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               answer = (answer + dp[i][sumNums2]) % MOD; // Update the answer with the number of ways to achieve zero sum difference.
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           return answer; // Return the total count of subranges with zero sum difference.
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C++ Solution
  1 #include <vector>
  2 #include <numeric>
     #include <cstring>
```

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class Solution {

public:

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possible sums.

Time Complexity

43 // Sum up the ways to achieve sum2 (offset sum is 0) for the current element ans = (ans + dp[i][sum2]) % mod;44 45 46 47 return ans; // Return the total number of valid subranges 48 49 }; 50 Typescript Solution function countSubranges(nums1: number[], nums2: number[]): number { const lengthOfNums = nums1.length; const sumOfNums1 = nums1.reduce((total, current) => total + current, 0); const sumOfNums2 = nums2.reduce((total, current) => total + current, 0); // Initialize dynamic programming table to store intermediate results const dpTable: number[][] = Array(lengthOfNums) .fill(0) .map(() => Array(sumOfNums1 + sumOfNums2 + 1).fill(0)); 8 const modulo = 1e9 + 7; // The modulo value to ensure results within integer limits 9 10 let countOfSubranges = 0; // Variable to keep the final count of subranges 11 12 // Iterate over each pair of elements from nums1 and nums2 13 for (let i = 0; i < lengthOfNums; ++i) {</pre> 14 const valueFromNums1 = nums1[i]; 15 const valueFromNums2 = nums2[i]; // Increase the count for the subrange that only includes current element dpTable[i][valueFromNums1 + sumOfNums2]++; dpTable[i][-valueFromNums2 + sumOfNums2]++; 19 20 // If current index is not the first, calculate the count of subranges that end at the current index if (i > 0) { for (let j = 0; j <= sumOfNums1 + sumOfNums2; ++j) {</pre> // If subrange can be extended by adding value from nums1 if (j >= valueFromNums1) { 24 dpTable[i][j] = (dpTable[i][j] + dpTable[i - 1][j - valueFromNums1]) % modulo; 25 26 // If subrange can be extended by subtracting value from nums2 27 if (j + valueFromNums2 <= sumOfNums1 + sumOfNums2) {</pre> 28 dpTable[i][j] = (dpTable[i][j] + dpTable[i - 1][j + valueFromNums2]) % modulo; 29 30 31

// Add the count of balanced subranges (where sum of nums1 elements equals sum of nums2 elements) to the answer

The given Python code aims to count the number of subranges in two arrays, nums1 and nums2, where for each subrange (i, j), the

sum from i to j in nums1 is equal to the sum from i to j in nums2. The algorithm uses dynamic programming to keep track of the

Time and Space Complexity

return countOfSubranges;

// Return the total count of subranges found

• Inside the outer loop that iterates over n, where n is the length of nums1 (or nums2), there is an inner loop that runs from 0 to s1 + s2, where s1 is the sum of all elements in nums1 and s2 is the sum of all elements in nums2. This means that the inner loop runs for

To analyze the time complexity, we consider the number of operations performed:

countOfSubranges = (countOfSubranges + dpTable[i][sumOfNums2]) % modulo;

0(s1 + s2) iterations for each i.
 The inner loop operations consist of a constant number of arithmetic

• The algorithm iterates over each pair (a, b) from nums1 and nums2.

• The inner loop operations consist of a constant number of arithmetic operations, each having a time complexity of 0(1).

Combining this information, the total time complexity is 0(n * (s1 + s2)), as there are n iterations in the outer loop and 0(s1 + s2) operations for each iteration in the inner loop.

• The algorithm allocates a 2D list f with n rows and s1 + s2 + 1 columns, where n is the length of the arrays and s1 + s2 is the

Space Complexity

For space complexity, we consider the storage used:

sum of the elements in nums1 and nums2. Therefore, the space required for this list is 0(n * (s1 + s2)).

This results in a total space complexity of 0(n * (s1 + s2)), dominated by the space required for the 2D list f.

Other variables used (n, s1, s2, ans, mod, a, b, i, j) require constant space, hence 0(1).