2768. Number of Black Blocks

Medium Array Hash Table Enumeration

Problem Description

In the given problem, we are tasked with assessing a grid with dimensions m x n that is partially colored with black cells at specific coordinates. Initially, we assume that the entire grid is white. A matrix called coordinates is provided to us, where each element [x, y1 of this matrix represents a cell in our grid that is black.

Leetcode Link

What we are interested in is identifying the number of 'blocks' within this grid containing a certain number of black cells. A 'block' is defined as a 2 x 2 section of the grid and may therefore contain between zero and four black cells. In essence, our goal is to count the number of these blocks based on the number of black cells they have, ranging from zero to four.

We are expected to return an array of size five, arr, where arr[i] corresponds to the number of blocks containing exactly i black cells. To put this into perspective, arr [0] will represent the number of blocks with no black cells, and it progresses all the way to arr[4], which represents the number of blocks completely filled with black cells.

Intuition

each block.

Given that a block is defined by its top-left cell, we can consider each black cell's contribution to possibly four different blocks - the ones that could contain this black cell either in their top-left, top-right, bottom-left, or bottom-right position.

The intuition behind the solution involves two primary steps: identifying relevant blocks and counting the number of black cells within

To achieve this, we create a hash table (or a dictionary in Python) where the keys correspond to the top-left coordinates of all potential blocks, and the values represent the number of black cells within each block.

carefully, taking into account the edge cases: a black cell that lies on the bottom or right edge of the grid won't be the top-left cell of any block.

As we iterate through each black cell given in the coordinates, we increment the count for the blocks it is part of. We do this

The answer to our problem is partially embedded in the hash table - it tells us how many blocks have one or more black cells. However, we still need to account for the blocks that have no black cells at all. To calculate this, we subtract the total number of blocks with at least one black cell (which is just the number of keys in our hash table) from the total number of possible blocks, (m -1) * (n - 1).

the number of black cells in each block. Solution Approach

At the end, the ans array is assembled by iterating through the hash table's values and incrementing the count in the array based on

The solution employs a hash table to track the number of black cells within each potential block. A hash table is a data structure that allows us to store key-value pairs, where the key is unique. In this case, the keys are tuples representing the top-left corner of each

block (x, y), and the values are counts of how many black cells are contained within that block.

for each key. As we visit each black cell, we update the counts accordingly.

corresponding index in ans for the count of such blocks.

adhering to the problem's constraints and expectations.

Coordinates of Black Cells: [[1, 1], [1, 2], [2, 1]]

Our grid looks like this initially, where or represents white cells:

We iterate over each black cell given in the coordinates. For each cell (x, y), we consider its contribution to the surrounding blocks. The surrounding blocks that the cell contributes to are identified by shifting the cell's position one step up/to the left ((x - 1, y -

1), (x - 1, y), (x, y - 1), (x, y)). When the cell is on the edge of the grid, some of these shifts would result in invalid coordinates for a block's top-left corner, so we verify that each corner coordinate is valid by checking the grid's bounds. The Python Counter class is utilized to implement the hash table, which already provides a convenient way to increment the count

After accounting for all black cells and their contributions, we are left with a hash table where the keys are the possible upper-left

where for each key in the hash table, the value associated with it tells us how many black cells that block contains. We increment the

corners of 2 x 2 blocks, and the values are the number of black cells in those blocks. We construct the ans array from this data,

Lastly, to calculate the number of blocks that contain zero black cells, we use the formula (m - 1) * (n - 1) - sum(cnt.values()). This takes the total possible number of blocks in our grid, subtracts the number of non-zero entries from our hash table, and gives us the number of white blocks.

By iterating through the values of our hash table and assembling the ans array, we complete the solution and return it as our answer,

Let's walk through a small example using the solution approach described above. Example Grid (m x n): 3 × 3 grid where m and n are the dimensions of the grid

3 0 0 0

Example Walkthrough

Let's identify potential blocks. A 2 x 2 block is defined by its top-left corner. In a 3 x 3 grid, the potential top-left corners are (0, 0), (0, 1), (1, 0), and (1, 1).

since (1, 0) and (0, 0) do not form a complete 2×2 block within the grid.

After coloring the cells from the coordinates, our grid looks like this (1 represents black cells):

Now we iterate over each black cell and update the count for each potential block it is part of. We only increment the count if the coordinate is a valid top-left corner of a block.

For black cell (1, 1):

For black cell (1, 2):

3 0 1 0

1 0 0 0

For black cell (2, 1):

It contributes to blocks with top-left corners at (2, 1), (2, 0), (1, 1), and (1, 0). Only (1, 1) is a valid top-left corner for a block.

It will contribute to blocks with top-left corners at (1, 1), (1, 0), (0, 1), and (0, 0). However, only (1, 1) and (0, 1) are valid blocks

 (1, 1): 3 black cells We have only two non-empty blocks; the rest ((m - 1) * (n - 1) = 4) are empty blocks.

• (0, 1): 1 black cell

To calculate the final array, arr, we do the following: arr[0]: Number of white blocks ((m - 1) * (n - 1) - number of non-empty blocks) = 4 - 2 = 2.

arr[1]: The number of blocks with exactly 1 black cell = 1 (block with the top-left corner at (0, 1)).

arr[3]: The number of blocks with exactly 3 black cells = 1 (block with the top-left corner at (1, 1)).

It contributes to blocks with top-left corners at (1, 2), (1, 1), (0, 2), and (0, 1). Only (1, 1) and (0, 1) are valid.

black cell, 0 blocks with 2 black cells, 1 block with 3 black cells, and 0 blocks with 4 black cells.

Iterate through each coordinate

for count in block_counter.values():

result_counts[count] += 1

for x, y in coordinates:

arr[2]: The number of blocks with exactly 2 black cells = 0.

arr[4]: The number of blocks with exactly 4 black cells = 0.

At this point, the hash table (or Counter) will contain:

class Solution: def countBlackBlocks(self, m: int, n: int, coordinates: List[List[int]]) -> List[int]: # Counter to keep track of the number of occurrences for each block 6 block_counter = Counter() 8

Check if the new coordinates are inside the grid boundaries

Calculate the number of blocks with 0 count (not modified by any operation)

result_counts[0] = $(m - 1) * (n - 1) - sum(block_counter.values())$

public long[] countBlackBlocks(int rows, int cols, int[][] coordinates) {

Map<Long, Integer> sharedCornersCount = new HashMap<>(coordinates.length);

// A map to keep count of shared corners for each black block

// Array to navigate through the neighboring blocks

std::unordered_map<long long, int> block_counts;

// Loop through each coordinate in the coordinates list

// Check if the neighbor block is within bounds

// Answer vector containing counts of black blocks shaded 0 to 4 times

// Increment the count for the number of times a block is shaded

function countBlackBlocks(m: number, n: number, coordinates: number[][]): number[] {

// Ensure that the adjacent cell is within the grid bounds

// Calculate a unique key for the position in the grid

blockCount.set(key, (blockCount.get(key) || 0) + 1);

const [adjRow, adjCol] = [row + directions[k], col + directions[k + 1]];

// Decrement the answer for count type 0 since we've found a cell with >0 blocks

// Increment the block count for this key, or set to 1 if it doesn't exist

if $(adjRow >= 0 \&\& adjRow < m - 1 \&\& adjCol >= 0 \&\& adjCol < n - 1) {$

// Map to keep track of the count of blocks at each grid position

// Directions to move to adjacent cells (left, right, up, down)

const blockCount: Map<number, number> = new Map();

// Check each direction from the coordinate

// Calculate the adjacent cell's position

const key = adjRow * n + adjCol;

// Increment the answer for the corresponding count type

const directions: number[] = [0, 0, -1, -1, 0];

// Iterate over each coordinate

for (const [row, col] of coordinates) {

for (const count of blockCount.values()) {

for (let k = 0; k < 4; ++k) {

int directions $[5] = \{0, 0, -1, -1, 0\};$

for (int k = 0; k < 4; ++k) {

std::vector<long long> answer(5);

// Return the final answer vector

return answer;

Typescript Solution

for (const auto& count : block_counts) {

for (const auto& coordinate : coordinates) {

int x = coordinate[0], y = coordinate[1];

answer[0] = static_cast<long long>(m - 1) * (n - 1);

// Update the answer vector based on the counts in the map

// Check all four neighboring positions

// Directions representing the relative positions of the 4 neighboring blocks

int neighbor_x = x + directions[k], neighbor_y = y + directions[k + 1];

++block_counts[static_cast<long long>(neighbor_x) * n + neighbor_y];

// Increment the count for the neighbor block key in the map

// Initially set the count of blocks not shaded to the total number of possible blocks

if $(\text{neighbor}_x >= 0 \& \text{\& neighbor}_x < m - 1 \& \text{\& neighbor}_y >= 0 \& \text{\& neighbor}_y < n - 1) {$

int[] directions = $\{0, 0, -1, -1, 0\}$;

Generate 4 adjacent positions using pairwise

if $0 \le i \le m - 1$ and $0 \le j \le n - 1$:

i, j = x + delta_x, y + delta_y

for delta_x, delta_y in pairwise([0, 0, -1, -1, 0]):

Increment the count for this block

Update the result list with the counts from the counter

New coordinates for the adjacent position

Therefore, the final returned array will be: arr = [2, 1, 0, 1, 0]. This means there are 2 blocks with 0 black cells, 1 block with 1

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Python Solution

1 from collections import Counter

from itertools import pairwise

19 block_counter[(i, j)] += 1 20 21 # List to store the result; there can be 0 to 4, total 5 different counts 22 $result_counts = [0] * 5$ 23

31 return result_counts 32

Java Solution

class Solution {

```
// Iterate through the coordinates of the black blocks
             for (int[] coordinate : coordinates) {
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                 int x = coordinate[0], y = coordinate[1];
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                 // Consider the neighboring cells, as they share corners with the current cell
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                 for (int k = 0; k < 4; k++) {
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                     int i = x + directions[k], j = y + directions[k + 1];
 14
                     // Check if the neighboring cell is within the boundaries of the grid
 15
                     if (i >= 0 \&\& i < rows - 1 \&\& j >= 0 \&\& j < cols - 1) {
 16
                         // Using long to avoid integer overflow for indexing
 17
                         long index = 1L * i * cols + j;
 18
                         // Count the shared corners for each cell
 19
                         sharedCornersCount.merge(index, 1, Integer::sum);
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             // Array to hold the count of cells with a specific number of shared corners
 25
             long[] result = new long[5];
 26
             // By default, all the cells are initialized with no shared corners
 27
             result[0] = (long)(rows - 1) * (cols - 1);
 28
             // Iterate through the counts and update the result array accordingly
             for (int count : sharedCornersCount.values()) {
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                 result[count]++;
                                      // Increment the count for the specific shared corners
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                                       // Decrement the count of cells with no shared corners
                 result[0]--;
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             return result;
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 36 }
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C++ Solution
   #include <vector>
    #include <unordered_map>
    class Solution {
    public:
         std::vector<long long> countBlackBlocks(int m, int n, std::vector<std::vector<int>>& coordinates) {
             // A map to keep count of the black blocks shaded by each coordinate
```

++answer[count.second]; 34 35 // Decrement the count of blocks not shaded 36 --answer[0]; 37 38

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21 22 23 // Array to store the final count of black blocks for each count type (0 to 4) 24 const answer: number[] = Array(5).fill(0); // Initialize the answer for count type 0 to the total possible number of grid cells 25 answer[0] = (m - 1) * (n - 1);27 28 // Iterate over the block count map to populate the answer array

++answer[count];

Time and Space Complexity

--answer[0];

return answer;

Time Complexity The time complexity of the code is primarily dominated by the for loop that iterates through each of the coordinates. Within this

Space Complexity

coordinate.

loop, there's a call to pairwise, which will have a constant number of iterations (specifically, 2 in this case) since it is paired with a fixed size tuple. Therefore, the complexity due to pairwise does not depend on the size of the input.

Given that each iteration of the main for loop is constant time and we have 1 coordinates, the overall time complexity is 0(1).

Next, we have a nested for loop, but since it also iterates over a fixed-size tuple (four elements), it runs in constant time per

The space complexity is influenced by the Counter object cnt that collects the frequency of each black block. In the worst-case scenario, each coordinate touches a unique block, thus the space required to store counts can grow linearly with the number of coordinates. Therefore, the space complexity is also 0(1), where 1 is the length of coordinates.

Note that the output array ans has a fixed size of 5, and the fixed tuples used for iteration do not scale with input size, so they do not affect the space complexity.