### 1276. Number of Burgers with No Waste of Ingredients



Leetcode Link

## **Problem Description**

The problem provides us with two integers, tomatoSlices and cheeseSlices, representing the number of tomato and cheese slices available to make burgers. There are two types of burgers: Jumbo Burgers, which require 4 tomato slices and 1 cheese slice, and Small Burgers, which require 2 tomato slices and 1 cheese slice.

We are asked to find how many of each type of burger we can make such that after making them, there are no remaining tomato or cheese slices. If it is possible, we return a list with two elements, [total\_jumbo, total\_small], representing the count of Jumbo and Small Burgers, respectively. If it's not possible to use all the tomato and cheese slices exactly, we return an empty list [].

### To solve this problem, we can set up a system of linear equations based on the constraints given for making Jumbo and Small

statement:

Intuition

Burgers: 1. Each Jumbo Burger requires 4 tomato slices and 1 cheese slice.

Let x be the number of Jumbo Burgers and y be the number of Small Burgers. We can derive two equations from the problem

2. Each Small Burger requires 2 tomato slices and 1 cheese slice.

• 4x + 2y = tomatoSlices: The total tomatoes used has to equal the available tomato slices.

• x + y = cheeseSlices: The total cheese used has to equal the available cheese slices.

- We want to find non-negative integer solutions for x and y that satisfy both equations simultaneously. Rearranging the second equation gives us x = cheeseSlices - y. Substituting this in the first equation allows us to solve for y:
- 4(cheeseSlices y) + 2y = tomatoSlices 4\*cheeseSlices 4y + 2y = tomatoSlices 4\*cheeseSlices tomatoSlices = 2y y = (4\*cheeseSlices - tomatoSlices) / 2

This gives us a direct way to calculate the number of Small Burgers y, and subsequently, we can find x (number of Jumbo Burgers).

However, y must be a non-negative integer for the solution to be valid. Therefore, 4\*cheeseSlices - tomatoSlices must be a nonnegative even number to make y a non-negative integer. Similarly, x must also be a non-negative integer.

zero) and both x and y are not negative before returning [x, y]. If any of these conditions is not met, it returns [], signifying that

The provided solution in Python reflects this logic. It ensures that the value for y (k // 2) is not fractional (by checking if k % 2 is not

there is no possible solution. Solution Approach

The implementation of the solution adopts a direct approach to solving the system of linear equations derived from the problem

#### The primary algorithm used here is to derive two linear equations from the given constraints and simplify them to express one

constraints.

variable in terms of the other. The equations derived are as follows: 1. The total tomatoes used for Jumbo and Small Burgers: 4x + 2y = tomatoSlices

These two equations can be simplified to find y:

Now that we have x in terms of tomatoSlices and cheeseSlices, we can find y by substituting x back into one of the original

2. Subtract the modified second equation from the first: (4x + 2y) - (2x + 2y) = tomatoSlices - 2 \* cheeseSlices

2. The total cheese used for Jumbo and Small Burgers: x + y = cheeseSlices

1. Multiply the second equation by 2: 2(x + y) = 2 \* cheeseSlices

- 3. Simplify to find x: 2x = tomatoSlices 2 \* cheeseSlices and hence x = (tomatoSlices 2 \* cheeseSlices) / 2
- equations: y = cheeseSlices - x
- and y. Here are the steps in the code:

1. k = 4 \* cheeseSlices - tomatoSlices: This is to isolate the y term by combining and rearranging the original equations.

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2. y = k // 2: Integer division by 2 to solve for y.
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3. x = cheeseSlices - y: Substitute y back into the x + y = cheeseSlices equation to solve for x. Before returning [x, y], the method checks three conditions:

The Solution class's numOfBurgers method takes the inputs tomatoSlices and cheeseSlices and performs these operations to find x

• y < 0: This checks if y is non-negative. x < 0: This checks if x is non-negative.</li>

If any of these conditions fail, it indicates that there are no non-negative integer solutions to the problem with the given

Otherwise, it means valid counts for Jumbo (x) and Small (y) Burgers have been found that use all the tomatoSlices and

tomatoSlices and cheeseSlices, and the method returns an empty list [].

burgers that exactly use up all the tomato and cheese slices.

cheeseSlices, and the solution [x, y] is returned.

• k % 2: This checks if k is an even number, as y must be a whole number.

The solution utilizes basic arithmetic operations and integer division, which are efficient operations in terms of computational complexity.

Let's consider a small example with 8 tomato slices and 5 cheese slices. We want to find out if it's possible to make some combination of Jumbo (4 tomatoes, 1 cheese) and Small (2 tomatoes, 1 cheese)

First, we use the given relationships to create our equations:

### Now, let's solve for y using these equations.

4(5 - y) + 2y = 8

20 - 4y + 2y = 8

20 - 8 = 2y

12 = 2y

solution.

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**Example Walkthrough** 

- Step 2: Substitute x in Equation 1 with 5 y:
- Step 3: Solve for y: y = 12 / 2, so y = 6.

• For tomatoes: 4x + 2y = 8 (Equation 1)

Step 1: Rearrange Equation 2 to isolate x: x = 5 - y

• For cheese: x + y = 5 (Equation 2)

As the calculated y exceeds the number of cheese slices, we would subtract y from the total cheese to find x: x = 5 - 6, which gives us x = -1. We cannot have a negative number of burgers.

more Small Burgers than the total number of cheese slices, which is not possible.

solution that exactly uses up all 8 tomato slices and 5 cheese slices with the given constraints.

def numOfBurgers(self, tomato\_slices: int, cheese\_slices: int) -> List[int]:

# Calculate the number of 'jumbo' burgers (with 4 tomato slices each)

if difference % 2 == 0 and num\_small\_burgers >= 0 and num\_jumbo\_burgers >= 0:

# If any of the conditions above are not met, return an empty list

// This method calculates the number of jumbo and small burgers one can make

// This should be even and non-negative for a valid combination.

// Calculate excess tomato slices after subtracting 4 times the cheese slices.

// Subtracting the number of small burgers from total cheese slices gives

// with the given number of tomato and cheese slices.

// us the number of jumbo burgers.

// Jumbo burgers require 4 tomato slices and 1 cheese slice.

// Small burgers require 2 tomato slices and 1 cheese slice.

int excessTomato = 4 \* cheeseSlices - tomatoSlices;

int jumboBurgers = cheeseSlices - smallBurgers;

vector<int> numOfBurgers(int tomatoSlices, int cheeseSlices) {

num\_jumbo\_burgers = cheese\_slices - num\_small\_burgers

return [num\_jumbo\_burgers, num\_small\_burgers]

**Python Solution** from typing import List

However, since y (the number of Small Burgers) is 6 and x + y must be 5, we already know something is wrong because we have

Since we have found impossible values (negative or more than available cheese slices) for x and y, we conclude that there is no

In correspondence with the Solution class in Python, the method numOfBurgers (8, 5) would return an empty list [], indicating no

# Find the difference between quadruple the cheese slices and the tomato slices difference = 4 \* cheese\_slices - tomato\_slices # Calculate the number of 'small' burgers (with 2 tomato slices each) num\_small\_burgers = difference // 2

# The result should be valid only if the difference is even, and neither of burgers is negative

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22 # solution = Solution()
  # print(solution.numOfBurgers(16, 7)) # Should output [1, 6] since it is possible to make 1 jumbo and 6 small burgers
24
```

Java Solution

21 # Example usage:

else:

return []

class Solution:

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class Solution {
       // Method to calculate the number of Jumbo and Small burgers that can be made given
       // the number of tomato and cheese slices.
       public List<Integer> numOfBurgers(int tomatoSlices, int cheeseSlices) {
           // Calculate the difference between four times the number of cheese slices and tomato slices
           int difference = 4 * cheeseSlices - tomatoSlices;
           // Calculate the number of Small burgers by dividing the difference by 2
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           int numSmallBurgers = difference / 2;
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           // Calculate the number of Jumbo burgers by subtracting the number of Small burgers
           // from the total cheese slices
           int numJumboBurgers = cheeseSlices - numSmallBurgers;
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           // Check if difference is even and both calculated burger amounts are non-negative
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           boolean isSolutionValid = difference % 2 == 0 && numSmallBurgers >= 0 && numJumboBurgers >= 0;
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           // Return the number of Jumbo and Small burgers, if possible; otherwise, return an empty list
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           return isSolutionValid ? Arrays.asList(numJumboBurgers, numSmallBurgers) : Collections.emptyList();
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22 }
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C++ Solution
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#### 11 12 // If excessTomato is even, half of it represents the difference in number of 13 // tomato slices used by small burgers compared to jumbo burgers. 14 int smallBurgers = excessTomato / 2;

1 class Solution {

2 public:

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           // If excessTomato is odd or if we end up with negative counts for either burger,
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           // return an empty vector (no solution).
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           return (excessTomato % 2 == 0 && jumboBurgers >= 0 && smallBurgers >= 0) ?
23
                  vector<int>{jumboBurgers, smallBurgers} : vector<int>{};
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25 };
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Typescript Solution
 1 // This function calculates the number of jumbo and small burgers one can make
2 // with the given number of tomatoSlices and cheeseSlices.
3 // Jumbo burgers require 4 tomato slices and 1 cheese slice.
 4 // Small burgers require 2 tomato slices and 1 cheese slice.
5 // It returns an array with the number of jumbo and small burgers one can make,
 6 // or an empty array if there's no valid combination.
 7 function numOfBurgers(tomatoSlices: number, cheeseSlices: number): number[] {
       // Calculate excess tomato slices after subtracting 2 times the number of cheese slices.
       // This excess must be even and non-negative for a valid combination.
       const excessTomato: number = tomatoSlices - 2 * cheeseSlices;
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       // If the excess is divisible by 2, it represents the additional tomatoes
       // needed to upgrade small burgers to jumbo burgers.
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       const conversionToJumbo: number = excessTomato / 2;
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       // The number of jumbo burgers is equal to the excess divided by 2,
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```

#### // Otherwise, return the counts in an array where the first element is jumbo burgers // and the second is small burgers. if (excessTomato % 2 === 0 && jumboBurgers >= 0 && conversionToJumbo >= 0) { return [jumboBurgers, conversionToJumbo]; 25

Time and Space Complexity

} else {

#### // since each conversion to a jumbo requires 2 additional tomatoes. const jumboBurgers: number = cheeseSlices - conversionToJumbo; 18 19 20 // If the excess is odd or we have a negative count of either type of burger, // return an empty array to indicate no solution is possible.

return []; 28 29 } 30

# are executed a constant number of times. Therefore, the time complexity is 0(1).

**Time Complexity** 

**Space Complexity** The space complexity of the code is also 0(1) since it uses a fixed amount of space for the variables k, y, x, and the return list regardless of the input size. The solution does not utilize any additional data structures that grow with the size of the input.

The given code consists of simple arithmetic calculations and conditional checks, which do not depend on the size of the input but