475. Heaters Medium Array **Two Pointers Binary Search** Sorting **Leetcode Link**

Problem Description

horizontal line, and each element in the heaters array represents the position of a heater on the same line. Our objective is to find the minimum radius required for all the heaters so that every house can be covered by at least one heater's warm radius. Keep in mind that all heaters are set to the same radius, and we must choose it so every house is within the radius of at least one heater. The goal is to minimize this radius while still ensuring that every house is within the warm range of at least one heater.

In this problem, we're given two arrays: houses and heaters. Each element in the houses array represents the position of a house on a

Intuition

Intuitively, we can think of this as a form of the binary search problem. We want to find the smallest radius such that every house is

warm, meaning it falls within the range of [heater position - radius, heater position + radius] for at least one heater. To do this, we start by sorting both the houses and heaters arrays to simplify the process of checking if a house is within the warm radius of a heater. The key insight behind the solution is to use binary search to find the minimum required radius. The binary search space is from 0 to the maximum possible distance between a house and a heater, which we initially assume to be a large number (like 10^9). We define

a function check that, given a radius value r, determines whether all houses can be warmed with the heaters set to the specified radius. Our binary search works as follows:

We calculate the middle value mid between left and right.

 We call the check function with this mid value to see if it's possible to cover all houses with this radius. If check returns True, it means the radius mid is sufficient, and we might be able to find a smaller radius that also works. So

1. We set left to 0 and right to a large number, defining our initial search space for the radius.

we set right to mid to look for a potentially smaller valid radius.

mid + 1 to search for a larger valid radius.

implementation steps, referencing the provided solution code:

2. We enter a loop where we continually narrow down our search space:

- If check returns False, it means the radius mid is not enough to cover all houses, so we need a larger radius. We set left to
- 3. When left is equal to right, we have found the smallest radius that can cover all the houses. The check function works by iterating through each house and determining if it's within the warm radius of at least one heater.
- Once we exit the binary search loop, left will hold the minimum radius needed so that all houses are within the range of at least one heater.
- **Solution Approach**

The solution leverages the binary search algorithm to zero in on the smallest possible radius. Here are the details of the

check function to iterate over houses and heaters in order, efficiently determining if each house is covered by the current radius. 2. Binary Search Setup: To find the correct radius, the code sets up a binary search with left as 0 and right as int(1e9) - a large

1. Sorting Input Arrays: The problem starts with sorting both houses and heaters arrays. Sorting is crucial because it allows the

enough number to ensure it's greater than any potential radius needed.

to the next heater and repeats the check. If all houses can be covered with the given radius, it returns True; otherwise, False. 4. Using Binary Search:

3. The check Function: This helper function checks whether a given radius r is sufficient to warm all houses. It initializes two

• A loop continues until left is not less than right, meaning the binary search space has been narrowed down to a single value.

pointers: i for houses and j for heaters. For each house, it checks if it falls in the range of the heater at index j. If not, it moves

- We calculate a mid value as the average of left and right. This mid represents the potential minimum radius. • We call check(mid) to verify if all houses are warmed by heaters with radius mid. ■ If True, the mid radius is large enough, and we attempt to find a smaller minimum by setting right to mid.
- 5. Convergence and Result: By continuously halving the search space, the binary search converges to the minimum radius required, which is then returned by the function when left equals right. This is because when check(mid) can no longer find a

enables it to handle a wide range of input sizes.

radius that covers all houses, left will now point to the smallest valid radius found. The main data structure used is the sorted arrays, which enable efficient traversal. The binary search algorithm is the core pattern

houses within a given warm radius. Combining sorting, binary search, and two-pointer techniques makes the solution efficient and

used to minimize the heater radius, and the check function is an implementation of a two-pointer technique to match heaters to

■ If False, the mid radius is too small, so we look for a larger radius by setting left to mid + 1.

Example Walkthrough Let's say we have the following array of houses: [1, 2, 3, 4], and heaters: [1, 4]. We want to use the solution approach to find the

1. Sorting Input Arrays: ○ The houses array is already sorted: [1, 2, 3, 4]. • The heaters array is already sorted: [1, 4]. 2. Binary Search Setup:

3. Binary Search Start

minimum heater radius.

 The initial value of left is 0, and right is 10^9. 4. Binary Search Iteration

■ We use check(5 * 10^8) which will definitely return True because the radius is very large and will cover all houses. We

• First Iteration:

Second Iteration: ■ Now we have left = 0, right = 5 * 10^8.

 \blacksquare mid = (left + right) / 2 = 2.5 * 10^8.

then set right to mid which now becomes $5 * 10^8$.

def findRadius(self, houses: List[int], heaters: List[int]) -> int:

The function 'can_cover' checks if a given radius 'radius'

Iterate over all houses to check coverage

if heater_idx >= num_heaters:

while house_idx < num_houses:</pre>

return False

return False

move to the next heater

heater_idx += 1

if can_cover(mid):

Arrays.sort(heaters);

for (int house : houses) {

if (index < 0) {

int minRadius = 0;

right = mid

if houses[house_idx] > max_range:

First, sort the houses and heaters to enable efficient scanning

If no more heaters are available to check, return False

We set left to 0 and right to 10^9 (a very large number).

■ mid = (left + right) / 2 which calculates to (0 + 10^9) / 2 = 5 * 10^8.

■ Again, check(2.5 * 10^8) will return True. We update right to 2.5 * 10^8. We keep iterating, and the value of right will continue to decrease until check returns False, which indicates the mid value is

insufficient for a heater radius.

to stop decreasing the right boundary.

5. Finding the Minimum Radius

6. Arriving at the Solution

needed.

class Solution:

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52 };

if (houses[i] < minHeaterRange)</pre>

if (houses[i] > maxHeaterRange)

1 function findRadius(houses: number[], heaters: number[]): number {

// Sort arrays to enable binary search later.

++j;

// All houses are covered.

else

return true;

Typescript Solution

heaters, a mid of 2 would be enough to cover all the houses (house at position 2 is at a distance of 2 from heater 1, and house at 3 is also at a distance of 1 from heater 4). ∘ So, when the check function is called with mid values lower than 2, it will start to return False, prompting the binary search

• We continue the binary search to narrow down the minimum radius that can cover all houses. Assuming our houses and

the heaters is 2.

In this way, we use the binary search algorithm to efficiently find the minimum radius for the heaters to cover all houses.

• For our example, after enough iterations, left will equal right at the value of 2. This means the minimum radius required for

• The binary search algorithm will continue to narrow down until left and right converge, giving us the minimum radius

Python Solution from typing import List

houses.sort()

heaters.sort()

- # is enough to cover all houses by heaters. Returns True if it is, False otherwise. def can_cover(radius): # Get the number of houses and heaters num_houses, num_heaters = len(houses), len(heaters) house_idx, heater_idx = 0, 0 # Start scanning from the first house and heater
- # Calculate the minimum and maximum coverage range of the current heater min_range = heaters[heater_idx] - radius max_range = heaters[heater_idx] + radius # If the current house is not covered, attempt to use the next heater if houses[house_idx] < min_range:</pre>
- 33 else: # Otherwise the house is covered, move to the next house house_idx += 1 34 35 36 return True # All houses are covered 37 38 # Start with a radius range of 0 to a large number (1e9 is given as a maximum) left, right = 0, int(1e9) 39 40 41 # Perform a binary search to find the minimum radius while left < right:</pre> 42 43 mid = (left + right) // 2 # Choose the middle value as the potential radius # If all houses can be covered with the 'mid' radius, search the lower half

If the current house is outside the current heater's max range,

else: # If not, search the upper half 48 left = mid + 149 50 # The minimum radius required to cover all houses is 'left' after the loop return left 51 52 Java Solution class Solution { public int findRadius(int[] houses, int[] heaters) {

// Sort the array of heaters to perform efficient searches later on

// Iterate through each house to find the minimum radius needed

int index = Arrays.binarySearch(heaters, house);

index = \sim index; // index = -(index + 1)

// Initialize the minimum radius required for heaters to cover all houses

// If the house is not a heater, calculate the potential insert position

// Calculate distance to the previous heater, if any, else set to max value

// Calculate distance to the next heater, if any, else set to max value

// Calculate the minimum distance to the closest heater for this house

// Perform a binary search to find the insertion point or the actual position of the house

int distanceToPreviousHeater = index > 0 ? house - heaters[index - 1] : Integer.MAX VALUE;

int minDistanceToHeater = Math.min(distanceToPreviousHeater, distanceToNextHeater);

int distanceToNextHeater = index < heaters.length ? heaters[index] - house : Integer.MAX_VALUE;</pre>

// Update the minimum radius to be the maximum of previous radii or the minimum distance for this house

30 31 32 // Return the minimum radius required 33 return minRadius; 34 35 }

minRadius = Math.max(minRadius, minDistanceToHeater);

#include <vector> #include <algorithm> public:

C++ Solution

class Solution { // Function to find the minimum radius of heaters required to cover all houses. int findRadius(std::vector<int>& houses, std::vector<int>& heaters) { // Sort the house and heater positions to perform binary search later. std::sort(houses.begin(), houses.end()); std::sort(heaters.begin(), heaters.end()); 10 11 12 // Setting initial binary search range. 13 int left = 0, right = 1e9; 14 15 // Binary search to find the minimum radius. while (left < right) {</pre> 16 int mid = (left + right) / 2; 17 // Check if with this radius all houses can be covered. 18 if (canCoverAllHouses(houses, heaters, mid)) 19 right = mid; // Radius can be smaller or is optimal, reduce the search to left half. 20 21 else 22 left = mid + 1; // Radius too small, need to increase, search in right half. 23 24 // Once left meets right, we've found the smallest radius needed. 25 return left; 26 27 28 // Function to check if all houses can be covered with a given radius 'radius'. 29 bool canCoverAllHouses(const std::vector<int>& houses, const std::vector<int>& heaters, int radius) { 30 int numHouses = houses.size(), numHeaters = heaters.size(); 31 int i = 0, j = 0; // Initialize pointers for houses and heaters 32 33 // Iterate over houses to check coverage. 34 while (i < numHouses) {</pre> 35 if (j >= numHeaters) return false; // Run out of heaters, can't cover all houses. int minHeaterRange = heaters[j] - radius; 36 37 int maxHeaterRange = heaters[j] + radius; 38 39 // Current house is not covered by heater j's range.

return false; // House i can't be covered by any heater, so return false.

// Current house is outside the range of heater j, move to next heater.

++i; // Current house is covered, move to the next house.

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houses.sort((a, b) \Rightarrow a - b);
       heaters.sort((a, b) \Rightarrow a - b);
       // Initialize variables for the lengths of the houses and heaters arrays
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       const totalHouses = houses.length;
       const totalHeaters = heaters.length;
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       // Initialize answer variable to store the final result, the minimum radius needed
       let minRadius = 0;
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       // Initialize houseIndex and heaterIndex for traversing through the houses and heaters.
       for (let houseIndex = 0, heaterIndex = 0; houseIndex < totalHouses; houseIndex++) {</pre>
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           // Calculate current radius for this house to the current heater
            let currentRadius = Math.abs(houses[houseIndex] - heaters[heaterIndex]);
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           // Continue moving to the next heater to find the closest heater for this house
18
           while (heaterIndex + 1 < totalHeaters &&</pre>
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               Math.abs(houses[houseIndex] - heaters[heaterIndex]) >= Math.abs(houses[houseIndex] - heaters[heaterIndex + 1])) {
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               // Keep track of the minimum radius required for the current house
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                currentRadius = Math.min(Math.abs(houses[houseIndex] - heaters[++heaterIndex]), currentRadius);
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           // Update the minimum radius required for all houses
           minRadius = Math.max(currentRadius, minRadius);
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       // Return the minimum radius required for all houses
       return minRadius;
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32 }
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Time and Space Complexity
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The time complexity of the solution is determined by the following factors: • Sorting the houses and heaters arrays, which takes O(mlogm + nlogn) time, where m is the number of houses and n is the number

Time Complexity

of heaters. • The binary search to find the minimum radius, which takes O(log(max(houses) - min(houses))) iterations. Each iteration

performs a check which has a linear pass over the houses and heaters arrays, taking 0(m + n) time in the worst case. • Combining these, the overall time complexity is O(mlogm + nlogn + (m + n)log(max(houses) - min(houses))).

• The space used to sort the houses and heaters arrays, which is 0(m + n) if we consider the space used by the sorting algorithm.

- **Space Complexity** The space complexity of the solution is determined by the following factors:
- The space for the variables and pointers used within the findRadius method and the check function, which is 0(1) since it's a constant amount of space that doesn't depend on the input size. Combining the sorting space and the constant space, the overall space complexity is 0(m + n).