Medium Tree Hash Table Depth-First Search Design Leetcode Link **Problem Description** 

# In the realm of a kingdom, we have a continuous line of succession from the king down to the various members of the royal family.

1600. Throne Inheritance

This order of inheritance begins with the king and is followed by his children, grandchildren, and so on, in order of their ages. The problem involves managing this order of inheritance, taking into account the birth of new royal members and the death of existing ones. The challenge is to maintain a dynamic list of the succession line, which can change when a new child is born or when someone dies.

# Intuition

(the values).

Let's break down the solution into the following parts: 1. Data Structure: We need to efficiently represent the family tree to allow for the addition of new children (via births) and to keep track of deaths. We use a graph represented by a dictionary (self.g) where every person is a key, and their children form a list

conducting depth-first search (DFS) traversals to generate the current order of inheritance.

This operation corresponds to adding edges to the family tree graph.

3. Deaths: We keep track of deaths in a set (self.dead). We don't remove the person from the graph because their children still need to be in the inheritance order.

4. Order of Inheritance: To find the current inheritance order, we use DFS starting from the king. In this traversal, we add a person to the current order only if they are not marked as dead. Through DFS, the children of each person are visited in the order they were added, maintaining the age-based priority.

5. Exclusion of Dead People: Since we want the order to contain only living members, we check the set of dead people during DFS

2. Births: When a child is born, we add the child to the graph by appending the child's name to the parent's list in the dictionary.

The primary approach to solving this problem involves simulating the family tree structure with appropriate data structures and then

- and only include those who are not in this set. By following this approach, we can dynamically adjust the inheritance order as births and deaths are recorded, thus maintaining an
- up-to-date succession line. **Solution Approach**

Let's dive into each of these points: 1. Data Structures: We create three main attributes within the ThroneInheritance class:

A graph self.g, represented as a dictionary, which captures the parent-child relationships.

A variable self.king to store the name of the king, which is the root of our graph.

A set self.dead to keep track of the deceased family members.

2. Class Methods: Three methods alter the state of the inheritance line:

The solution to the inheritance problem is built around several key concepts in computer science, namely data structures, depth-first

search, and class design.

 death marks a family member as deceased by adding their name to the self. dead set. getInheritanceOrder invokes a DFS traversal method to calculate the current inheritance order. 3. Depth-First Search (DFS): We perform a DFS starting from the king every time getInheritanceOrder is called. Here's the

The DFS continues recursively through the children (in the order they were added to self.g), ensuring the age-based

This implementation allows us to efficiently manage the order of inheritance dynamically as births add to the self.g graph and

deaths are recorded in self.dead. The getInheritanceOrder function can be called at any time to provide a snapshot of the living

birth receives a parent name and a child name. The child's name is appended to the parent's list of children in the graph.

 A helper function dfs is defined within getInheritanceOrder for recursive traversal. Each time the DFS visits a person, it checks if they are alive (not in self.dead). If so, the person is added to the ans list,

King George at the root.

Let's set up the ThroneInheritance at this point:

Event 1: John has a child named William.

. We execute the birth method for John and William.

breakdown of the DFS method used:

succession is preserved.

which represents the current inheritance order.

members in the line of succession, excluding those that have passed away.

John, Liam, and Claire as the children of George, listed in the order of their ages.

**Example Walkthrough** Consider a kingdom with the following initial succession line: King (George), his children: oldest (John), and middle (Liam), and youngest (Claire). In this structure, we have:

1. self.g = { "George": ["John", "Liam", "Claire"] } 2. self.dead = set() 3. self.king = "George" Now let's walk through a series of events and how the data structures would change:

## self.g becomes { "George": ["John", "Liam", "Claire"], "John": ["William"] }. Event 2: Claire gives birth to a child named Emma.

Emma.

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Event 3: Liam passes away.

**Python Solution** 

from typing import List

class ThroneInheritance:

from collections import defaultdict

def \_\_init\_\_(self, king\_name: str):

# Store the king's name

def death(self, name: str) -> None:

self.deceased.add(name)

def dfs(current\_member):

# Start DFS from the king

# Return the inheritance order

40 # Example of using the ThroneInheritance class

42 # throne\_inheritance.birth("King", "Andy")

41 # throne\_inheritance = ThroneInheritance("King")

# Mark a family member as deceased

def get\_inheritance\_order(self) -> List[str]:

def birth(self, parent\_name: str, child\_name: str) -> None:

# Helper function to perform depth-first search (DFS)

if current\_member not in self.deceased:

# List to store the current order of inheritance

private Map<String, List<String>> familyTree = new HashMap<>();

// The name of the reigning king or the root of the family tree

// Constructor initializes the ThroneInheritance with the name of the king

// Method to record the birth of a child, assigning the child to a parent in the family tree

// Method to record the death of a family member by adding them to the set of deceased members

// Helper method to perform a Depth-First Search on the family tree starting from a given family member

familyTree.computeIfAbsent(parentName, k -> new ArrayList<>()).add(childName);

// Method to return the current order of inheritance, skipping deceased members

// Set to hold all the deceased family members

// List to hold the order of inheritance

public ThroneInheritance(String kingName) {

public List<String> getInheritanceOrder() {

private void dfs(String currentMember) {

inheritanceOrder = new ArrayList<>();

// Start the Depth-First-Search with the king

return inheritanceOrder; // Return the computed order

void depthFirstSearch(const string& name) {

depthFirstSearch(child);

\* Example of using the ThroneInheritance class:

\* vector<string> order = obj->getInheritanceOrder();

const familyTree: Record<string, string[]> = {};

// Array to store the computed inheritance order

// Initializes the family tree with the reigning monarch

function initializeThroneInheritance(kingName: string) {

function birth(parentName: string, childName: string) {

deceased.add(name); // Add the member to the deceased set

inheritanceOrder = []; // Clear the previous order

51 // Examples of using the above global functions and variables:

31 // Gets the current order of inheritance, representing the line of succession to the throne

depthFirstSearch(child); // Recursively search for each child

depthFirstSearch(monarch); // Recursively compute the order starting from the monarch

const children = familyTree[name] || []; // Get the children or an empty array if there are none

// Store the set of deceased family members

const deceased: Set<string> = new Set();

// The name of the current monarch

let inheritanceOrder: string[] = [];

monarch = kingName;

// Records the birth of a child

if (!familyTree[parentName]) {

26 // Records the death of a family member

function getInheritanceOrder(): string[] {

for (const child of children) {

52 // initializeThroneInheritance('King');

59 // console.log(getInheritanceOrder());

Time and Space Complexity

function death(name: string)

32 // Filters out deceased members

return inheritanceOrder;

familyTree[parentName] = [];

familyTree[parentName].push(childName);

\* delete obj; // Don't forget to free allocated memory.

\* obj->birth(parentName, childName);

\* obj->death(name);

Typescript Solution

let monarch: string;

inheritanceOrder.push\_back(name);

for (const auto& child : familyTree[name]) {

\* ThroneInheritance\* obj = new ThroneInheritance(kingName);

if (!deceased.count(name)) {

// Helper function that performs a depth-first search on the family tree

// starting from the given family member to determine the line of succession.

// Define an adjacency list to hold the family tree where each parent maps to a list of children

private List<String> inheritanceOrder;

private String king;

dfs(king);

king = kingName;

public void death(String name) {

return inheritanceOrder;

deceasedMembers.add(name);

private Set<String> deceasedMembers = new HashSet<>();

public void birth(String parentName, String childName) {

# Append the current member to the order if they are not deceased

# Add a child under the parent in the family tree

self.family\_tree[parent\_name].append(child\_name)

self.king = king\_name

 We call the birth method for Claire and Emma. self.g is updated to { "George": ["John", "Liam", "Claire"], "John": ["William"], "Claire": ["Emma"] }.

Current Inheritance Order: At this time, if we call getInheritanceOrder, the DFS would start from George, move to John (as he is the

oldest child), and then to William (child of John), skip Liam because he is in the self.dead set, and continue with Claire, and then

This way, we can see how the dynamic list of succession maintains the correct order throughout the births and deaths within the

 death method is called for Liam; so Liam is added to self.dead. self.dead becomes { "Liam" }.

 DFS order: George → John → William → Liam (skipped, he's deceased) → Claire → Emma The ans list would be ["George", "John", "William", "Claire", "Emma"].

royal family, representing the living members in the correct order of precedence at all times.

Note that Liam is not removed from self.g because it will affect the children's structure (if he had any).

# Initialize a graph to represent the family tree self.family\_tree = defaultdict(list) # Set to keep track of the deceased individuals 10 self.deceased = set()

order.append(current\_member) 28 29 # Continue DFS for each child of the current member 30 for child in self.family\_tree[current\_member]: 31 dfs(child) 32

order = []

dfs(self.king)

return order

43 # throne\_inheritance.death("King")

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44 # inheritance_order = throne_inheritance.get_inheritance_order()
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Java Solution
1 import java.util.ArrayList;
2 import java.util.Collections;
  import java.util.HashMap;
   import java.util.HashSet;
  import java.util.List;
6 import java.util.Map;
   import java.util.Set;
   class ThroneInheritance {
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       // Graph to hold the family tree, where each key is a parent and the value is a list of children
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## 52 53 54 55 56

// If the current member is not deceased, add them to the inheritance order 48 if (!deceasedMembers.contains(currentMember)) { 49 inheritanceOrder.add(currentMember); 50 51 // Recurse on all children of the current member for (String child : familyTree.getOrDefault(currentMember, Collections.emptyList())) { dfs(child); 57 } 58 // Usage example: // ThroneInheritance inheritance = new ThroneInheritance("king"); 61 // inheritance.birth("king", "andy"); 62 // inheritance.birth("king", "bob"); 63 // inheritance.birth("andy", "matthew"); 64 // inheritance.death("bob"); // List<String> order = inheritance.getInheritanceOrder(); // Gets the inheritance order 66 C++ Solution 1 #include <string> 2 #include <vector> #include <unordered map> #include <unordered set> using namespace std; class ThroneInheritance { private: unordered\_map<string, vector<string>> familyTree; // Holds the family tree as an adjacency list unordered\_set<string> deceased; // Keeps track of deceased family members 10 string monarch; // The name of the current king or queen 11 12 vector<string> inheritanceOrder; // Used to store the computed inheritance order 13 public: 14 // Constructor initializes the family tree with the reigning monarch. 15 ThroneInheritance(string kingName) : monarch(kingName) {} 16 17 // Function to record the birth of a child 18 // parentName: The parent's name in the family tree 20 // childName: The child's name to be added under the parent 21 void birth(string parentName, string childName) { 22 familyTree[parentName].push\_back(childName); 23 24 25 // Function to record the death of a family member // name: The name of the deceased member 26 27 void death(string name) { 28 deceased.insert(name); // Add the member to the deceased set 29 30 // Function to get the current order of inheritance which represents the 31 32 // line of succession to the throne; filters out deceased members. 33 vector<string> getInheritanceOrder() { 34 inheritanceOrder.clear(); // Clear the previous order 35 depthFirstSearch(monarch); // Recursively compute the order starting from the monarch

### 38 // Performs a depth-first search on the family tree from the given family member // to determine the line of succession function depthFirstSearch(name: string) { if (!deceased.has(name)) { // If the person is not deceased, add to the inheritance order 42 inheritanceOrder.push(name); 43 44

53 // birth('King', 'Andy');

55 // birth('Andy', 'Matthew');

54 // birth('King', 'Bob');

56 // birth('Bob', 'Alex');

57 // birth('Bob', 'Asha');

58 // death('Bob');

<u>init</u> method

death method

insertion into the set.

complexity is 0(1) as well because it just adds one more element to the existing data structure.

lists), a set (self.dead), and assigns the self.king variable. The space complexity of the \_\_init\_\_ method is also 0(1) assuming the input kingName size does not contribute to the space complexity as it's a single value. birth method The birth method has a time complexity of 0(1) as it just appends the child to the parent's children list in the graph. The space

The <u>init</u> method has a time complexity of 0(1) as it simply initializes the data structures: a graph (self.g as a defaultdict of

getInheritanceOrder method

The getInheritanceOrder method has a time complexity of O(N) where N is the total number of people in the inheritance order (both alive and dead). This is because it performs a depth-first search (DFS) over the entire family tree, visiting each person once. The space complexity of the getInheritanceOrder method can be considered to be O(N) for the DFS recursion stack in the worst case (assuming the family tree is heavily unbalanced and resembles a linked list), plus O(N) for the ans list where N is the number of alive

The death method has a time complexity of 0(1) as it adds a name to the self. dead set. The space complexity is 0(1) due to a single

people. So, the total space complexity is O(N). Overall, the main performance concern in the code is related to how the DFS might behave on a very unbalanced family tree — in that case, the recursion could be a problem, and iterative approaches might need to be considered to keep the stack depth under control.