#### 56. Merge Intervals Sorting Medium Array

# **Problem Description**

where the first element is the start and the second is the end of the interval ([start, end]). An "overlap" occurs when one interval's start is less than or equal to the end of another interval. The goal is to simplify the list of intervals to a list where no intervals overlap, ensuring that the new list collectively spans the same range as the original intervals. Here's an example for clarification:

The given problem requires us to merge all the overlapping intervals in a list. An interval is represented as a list with two elements

Original list of intervals: [[1,3],[2,6],[8,10],[15,18]]

After merging all the overlapping intervals, we get: [[1,6],[8,10],[15,18]]

In the merged intervals, there is no pair of intervals such that one overlaps with another.

Intuition

#### 1. If we sort the intervals based on their start times, any overlapping intervals will be placed next to each other in the list.

2. To merge intervals, we only need to track the end time since the sorted order ensures that the next interval's start time is always greater than or equal to the current interval's start time.

The intuition behind the solution comes from two realizations:

- The approach is as follows:
- 1. Sort the list of intervals based on their start times.

3. Iterate through the rest of the intervals, and for each one, compare its start time with the end time of the last interval in the

intervals.

- merged list.

list to be the maximum of the end times of the last interval and the current interval.

2. Initialize a new list to hold the merged intervals and add the first interval to it.

- 4. If the start time is greater than the end time of the last interval in the merged list, then there is no overlap, and we can add the current interval as a new entry to the merged list. 5. If there is overlap (the start time is less than or equal to the end time), we update the end time of the last interval in the merged
- 6. The process continues until we have gone through all the intervals. 7. We return the merged list of intervals as the answer.
- This solution guarantees that we merge all overlapping intervals and result in a list of intervals with no overlaps.
- Solution Approach

The solution to the problem involves sorting the intervals and then iterating through the sorted list to merge any overlapping

1. First, we sort the given list of intervals. This is done in-place using the native sort function provided by Python, which sorts the

Here's a step-by-step breakdown of the implementation:

intervals based on their first element (the start times).

1 intervals.sort() By sorting the intervals, we are able to take advantage of the fact that any intervals that might need merging will appear next to

2. We then initialize a new list called ans, which will store our merged intervals, and we start by adding the first interval to it.

the currently last interval in our ans list.

we can simply add this interval to ans.

ans  $[-1][1] = \max(ans [-1][1], e)$ 

ans.append([s, e])

- This acts as a comparison base for merging subsequent intervals. 3. We then proceed to iterate over the rest of the intervals, starting from the second interval onward, to check for overlapping with
- 1 for s, e in intervals[1:]:
- 4. If the start time s of the current interval is greater than the end time of the last interval in ans, it means there is no overlap and

1 if ans[-1][1] < s:

overlapping intervals.

1 else:

readability.

each other in the list.

1 ans = [intervals[0]]

5. However, if an overlap exists, we need to merge the current interval with the last interval in ans. To do this, we update the end

time of the last interval in ans with the maximum end time between the two overlapping intervals.

Here, (s, e) represents the start and end times of the current interval we are looking at.

This ensures that the intervals are merged, covering the overlapping time spans without duplicating intervals.

6. Once we finish iterating through all intervals, the ans list contains the merged intervals. We return ans as the final set of non-

The algorithm uses the sort-merge pattern, which is common for interval problems. By sorting and then merging, we bring the overall

run-time complexity down to O(N log N) where N is the number of intervals, with the sort contributing to the log N factor and the

merge process being linear in nature. Regarding data structures, the solution leverages lists and the use of tuple unpacking for

Let's take a small example to illustrate the solution approach with the provided intervals: [[5,7], [1,3], [3,4], [2,6]].

Example Walkthrough

**Sorting the Intervals** First, we need to sort the intervals by their starting points to align any intervals that might overlap: 1 Before sort: [[5,7],[1,3],[3,4],[2,6]]
2 After sort: [[1,3],[2,6],[3,4],[5,7]]

• We look at [2,6] and compare it to the last element of ans, which is [1,3]. Since the start 2 is within [1,3] (as 3 is greater than

• Finally, we look at [5,7]. This does not overlap with [1,6] as 5 is not greater than 6. Since 7 is greater than 6, we add [5,7] as a

• [5,7] is checked again and it actually overlaps with [1,6] (since 5 is less than or equal to 6). We merge them by updating the

2), they overlap. We merge them by updating the end of the last interval in ans to the max end of both intervals, now ans

## We then initialize the ans list with the first sorted interval, treating it as the base for our merged intervals:

becomes [[1,6]].

Final Merged List

**Python Solution** 

class Solution:

Java Solution

1 import java.util.Arrays;

import java.util.ArrayList;

} else {

2 import java.util.List;

class Solution {

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C++ Solution

#include <vector>

class Solution {

public:

#include <algorithm>

// Function to merge overlapping intervals

1 ans = [[1,3]]

Next, we start iterating from the second element of the sorted intervals:

• Proceeding to [3,4], we compare it to the last element [1,6]. Again, it overlaps because 4 is not greater than 6. No need to

change the end time since 6 is already the maximum end.

new interval to ans. After the addition, ans becomes [[1,6],[5,7]].

end of the last interval in ans to 7, and ans now becomes [[1,7]].

def merge(self, intervals: List[List[int]]) -> List[List[int]]:

for start, end in intervals[1:]:

# Return the merged intervals

// Method to merge overlapping intervals.

public int[][] merge(int[][] intervals) {

mergedIntervals.add(intervals[i]);

// Overlap exists, so we extend the last interval's end time.

lastMergedInterval[1] = Math.max(lastMergedInterval[1], end);

// Convert the merged intervals list to a 2D array and return it.

return mergedIntervals.toArray(new int[mergedIntervals.size()][]);

std::vector<std::vector<int>> merge(std::vector<std::vector<int>>& intervals) {

// First, sort the intervals based on the starting times

// This will be the result vector for merged intervals

// Initialize the result vector with the first interval

// Iterate through all the intervals starting from the second one

// then simply add the current interval to the result

if (mergedIntervals.back()[1] < intervals[i][0]) {</pre>

mergedIntervals.push\_back(intervals[i]);

// If the current interval does not overlap with the last interval in the result,

// If there is an overlap, merge the current interval with the last interval

mergedIntervals.back()[1] = std::max(mergedIntervals.back()[1], intervals[i][1]);

// in the result by updating the end time to the maximum end time seen

std::sort(intervals.begin(), intervals.end());

std::vector<std::vector<int>> mergedIntervals;

for (int i = 1; i < intervals.size(); ++i) {</pre>

mergedIntervals.push\_back(intervals[0]);

return merged\_intervals

else:

if merged\_intervals[-1][1] < start:</pre>

merged\_intervals.append([start, end])

# Iterate over the intervals, starting from the second interval

We used intervals.sort() to achieve this.

Initializing and Iterating for Merging

However, our merging logic must have the current start to be greater than the last end to avoid overlap. Therefore, we should adjust the last step:

ans is: 1 [[1,7]]

This means we successfully merged all intervals to cover the same range without having any overlapping intervals. The solution

approach, by sorting and then merging, streamlined the process and ensures an efficient way to obtain the merged intervals.

Having completed the iteration over the sorted intervals, we have a list of merged intervals where no two intervals overlap. The final

# Sort the interval list based on the start times of intervals intervals.sort() # Initialize the merged\_intervals list with the first interval merged\_intervals = [intervals[0]]

# Check if the current interval does not overlap with the last interval in merged\_intervals

# updating the end time of the last interval to the maximum end time seen so far

# If it does not overlap, add the current interval to merged\_intervals

# If it does overlap, merge the current interval with the last one by

 $merged_intervals[-1][1] = max(merged_intervals[-1][1], end)$ 

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// Sort the intervals by their starting times.
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           Arrays.sort(intervals, (a, b) \rightarrow a[0] - b[0]);
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           // List that holds the merged intervals.
           List<int[]> mergedIntervals = new ArrayList<>();
           // Add the first interval to the list as starting interval for merging.
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            mergedIntervals.add(intervals[0]);
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           // Loop through all the intervals starting from the second one.
            for (int i = 1; i < intervals.length; ++i) {</pre>
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                // Get the start and end times of the current interval.
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                int start = intervals[i][0];
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                int end = intervals[i][1];
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                // Get the last interval in the merged list.
                int[] lastMergedInterval = mergedIntervals.get(mergedIntervals.size() - 1);
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                // Check if there is an overlap with the last interval in the merged list.
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                if (lastMergedInterval[1] < start) {</pre>
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                    // No overlap, so we can add the current interval as it is.
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#### 27 28 29 // Return the merged intervals 30 return mergedIntervals; 31 32 };

Typescript Solution

} else {

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1 function merge(intervals: number[][]): number[][] {
       // First, we sort the intervals array based on the start times
       intervals.sort((a, b) \Rightarrow a[0] - b[0]);
       // Initialize the merged intervals array with the first interval
       const mergedIntervals: number[][] = [intervals[0]];
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       // Iterate through the intervals starting from the second element
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       for (let i = 1; i < intervals.length; ++i) {</pre>
           // Get the last interval in the mergedIntervals array
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           const lastInterval = mergedIntervals[mergedIntervals.length - 1];
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           // If the current interval does not overlap with the last interval in mergedIntervals
           if (lastInterval[1] < intervals[i][0]) {</pre>
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               // Add the current interval to the mergedIntervals array as it cannot be merged
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               mergedIntervals.push(intervals[i]);
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           } else {
               // If there is an overlap, merge the current interval with the last interval
               // by updating the end time of the last interval to the maximum end time
               lastInterval[1] = Math.max(lastInterval[1], intervals[i][1]);
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       // Return the array containing all the merged intervals
       return mergedIntervals;
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26 }
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Time and Space Complexity
Time Complexity
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### For a list of n intervals: • The sort operation typically has a complexity of O(n log n), since Python uses TimSort (a hybrid sorting algorithm derived from

context.

merge sort and insertion sort) for sorting lists. The iteration over the list has a complexity of O(n), because we go through the intervals only once.

The given code has two main operations:

1. Sorting the intervals list.

Hence, the total time complexity is the sum of these two operations, which is  $O(n \log n) + O(n)$ . Since  $O(n \log n)$  is the higher order term, it dominates the total time complexity, which simplifies to  $O(n \log n)$ .

2. Iterating through the sorted list and merging overlapping intervals.

- **Space Complexity** The space complexity consists of the additional space used by the algorithm apart from the input:
- overlap, it will contain n intervals. Since the ans list reuses the intervals from the original input list, and the input list size itself is not included in the additional space used for computing space complexity, the space used to store ans can be considered 0(1) (constant space) in this

• The ans list which contains the merged intervals is the main additional data structure used, and in the worst case, if no intervals

Thus, the space complexity is 0(1).