2656. Maximum Sum With Exactly K Elements

Greedy Array Easy

Problem Description

You are provided with an array nums, which contains integer elements and is indexed starting from 0. Along with this, you are given an integer k. The goal is to maximize your score through a specific operation that you can perform exactly k times.

The operation consists of the following steps:

1. Pick an element m from the array nums.

- 2. Remove this element from the array.
- 3. Insert a new element into the array that has a value of m + 1.
- 4. Increase your score by m.

ntuition

After performing this operation exactly k times, you need to determine the maximum score you can achieve.

To maximize the score from each operation, it's logical to always select the largest element available in the array. If you always

each time.

Here's the thinking process step by step: • In the first operation, choose the maximum element in the array, x. Your score increases by x and now the array has a new element x + 1. • For the second operation, since you now have x + 1 in the array (which is greater than the original x), you select and remove x + 1, and then

choose the largest element, which we will denote as x, you ensure that your score increments by the maximum possible value

- add x + 2. Your score increases by x + 1 this time.
- You continue this process, each time selecting the current maximum, which continues to increase by 1 with each operation. After k operations, your total score will be an accumulated sum of all selected elements: x from the first operation, x + 1 from
- the second, and so on, up to x + k 1 for the kth operation.

common difference of 1. Thus, the formula to calculate the final score is:

So, you can calculate the total score by taking the sum of the arithmetic sequence that starts with x, has k terms, and a

Score = k * x + (1 + 2 + ... + (k - 1))We can simplify the summation using the formula for the sum of the first n natural numbers:

Sum = n * (n + 1) / 2

done by using the built-in max() function.

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Therefore, you can express the score as:
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Score = k * x + (k - 1) * k / 2

Applying this formula grants us the maximum score after k operations without the need to simulate the operations step by step.

The solution outlined above hinges on understanding and applying a mathematical concept rather than running complex

First, we need to determine the maximum element from the array nums, which is denoted as x. In Python, this can be easily

algorithms or relying on particular data structures. Here's how we translate the mathematical solution into a concrete implementation:

Solution Approach

x = max(nums)Now that we have the maximum number (x), we must calculate the score based on the formula derived earlier:

Score = k * x + (k - 1) * k / 2In the formula, k * x accounts for selecting the maximum element x * k times, while the second part of the formula (k - 1)

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* k / 2 is the sum of the arithmetic series contributing to the incrementality of the score with each operation.
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line of code in Python:

The implementation of this calculation is straightforward and directly derived from the formula. It can be written in a single

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Here, the // operator is used to perform integer division to avoid any floating-point result, which is suitable since we are
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dealing with integers only.

return k * x + k * (k - 1) // 2

By abstracting the problem into a formula, the time complexity of the solution is O(n), where n is the length of the array, coming from the time complexity of finding the maximum element. The space complexity is 0(1), as we only store the maximum element and use no additional data structures to hold intermediate values.

Let's illustrate the solution approach with a small example: Suppose our input array nums is [3, 5, 2] and we are allowed to perform the operation k = 2 times. We first find the maximum element in the array, which is x = 5.

Score = k * x + (k - 1) * k / 2

operation) = 11.

nums = [3, 5, 2]

x = max(nums)

k = 2

Python

Implementing this step-by-step:

score = k * x + k * (k - 1) // 2

 $max_num = max(nums)$

return maximized_sum

print(score) # Output should be 11

Example Walkthrough

Plugging in the values: Score = 2 * 5 + (2 - 1) * 2 / 2 Score = 10 + 1 Score = 11

after performing the operation twice is 11.

So, without physically removing elements and adding them back to the array, we can directly compute that the maximum score

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increased our score by 5. After the second operation, we would select the new maximum element, which is 6, remove it, add 7
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by avoiding multiple iterations for selecting and replacing elements with their increments.

Then, we calculate the maximum score by using the earlier derived formula:

1. From array nums = [3, 5, 2], find the maximum element x, which is 5. 2. Calculate the maximum score using the given values k = 2 and x = 5. 3. Substitute into the formula to get the result: Score = 2 * 5 + 1 * (2 - 1) = 11.

To break it down further, after the first operation, we would have selected element 5, removed it, added 6 to the array, and

to the array, and increase our score by another 6. Therefore, the total score would be 5 (initial score) + 6 (second

This hypothetical set of operations confirms the correctness of our direct calculation using the formula. The formula saves time

This program would output 11, which represents the maximum score achieved after performing the operation k times. Solution Implementation

The strategy to maximize the sum is to repeatedly increment the maximum number.

of the first k natural numbers, which is k * (k - 1) // 2 using the formula for the sum

We will do this k times, each time adding the maximum number to the sum.

This is equivalent to max num * k (adding max num k times), plus the sum

And for each iteration, we also add the i-th increment (0 to k-1).

// And then adding the sum of first k natural numbers (k*(k-1)/2)

* @param $\{number\}$ k - The number of top elements to consider for maximizing the sum.

int totalIncrement = k * maxElement + k * (k - 1) / 2;

// Return the sum after all increments are done

* Maximizes the sum by adding the top k numbers where the

function maximizeSum(nums: number[], k: number): number {

// Find the maximum value in the nums array.

const sum = k * maxValue + (k * (k - 1)) / 2;

* first number is the maximum in the array and every subsequent

* @param {number[]} nums - The array of numbers to search through.

* @returns {number} The maximized sum according to the described formula.

return totalIncrement;

* number is one less than the previous.

// Return the calculated sum.

from typing import List class Solution: def maximizeSum(self, nums: List[int], k: int) -> int: # Find the maximum number in the given list of numbers

of the first 'n' natural numbers.

Return the calculated maximized sum

public int maximizeSum(int[] nums, int k) {

 $maximized_sum = k * max_num + k * (k - 1) // 2$

A Python implementation of this example would be:

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// Initialize a variable to store the maximum value found in the array
int maxVal = 0;
// Iterate through all elements in the array to find the maximum value
for (int value : nums) {
```

class Solution {

Java

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maxVal = Math.max(maxVal, value);
       // Calculate and return the sum of the largest k numbers in an arithmetic progression
        // starting from maxVal and with a common difference of 1.
        return k * maxVal + k * (k - 1) / 2;
C++
#include <vector>
#include <algorithm> // Include algorithm for std::max_element
class Solution {
public:
    // Function to maximize sum by performing k increments on the maximum element
    int maximizeSum(std::vector<int>& nums, int k) {
        // Find the maximum element in the vector
        int maxElement = *std::max_element(nums.begin(), nums.end());
       // Calculate the total increment on the max element after k operations
       // This is done by multiplying the maximum element with k
```

```
const maxValue = Math.max(...nums);
// Calculate the sum of the top k numbers starting from the maxValue.
// The formula used is the sum of the first k elements of an arithmetic series
// starting with maxValue and decrementing by 1 each time.
```

*/

};

/**

TypeScript

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return sum;
from typing import List
class Solution:
    def maximizeSum(self, nums: List[int], k: int) -> int:
       # Find the maximum number in the given list of numbers
       max_num = max(nums)
       # The strategy to maximize the sum is to repeatedly increment the maximum number.
       # We will do this k times, each time adding the maximum number to the sum.
       # And for each iteration, we also add the i-th increment (0 to k-1).
        # This is equivalent to max num * k (adding max num k times). plus the sum
        # of the first k natural numbers, which is k * (k - 1) // 2 using the formula for the sum
        # of the first 'n' natural numbers.
       maximized_sum = k * max_num + k * (k - 1) // 2
       # Return the calculated maximized sum
        return maximized_sum
Time and Space Complexity
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The given Python code consists of two main operations: finding the maximum value in the list nums, and performing arithmetic

calculations to obtain the result.

The time complexity of finding the maximum element in a list of n elements using max(nums) is O(n), as it requires checking each element exactly once. The arithmetic operations k * x + k * (k - 1) // 2 involve constant time calculations, hence their

complexity is 0(1).

Space Complexity

Time Complexity

Overall, the time complexity of the function is O(n) + O(1), which simplifies to O(n).

In terms of space complexity, there are no additional data structures used that grow with the input size. Only a constant amount of additional space is used for variables like x. Therefore, the space complexity of the function is 0(1).

In conclusion, the time complexity of the provided code is 0(n) and the space complexity is 0(1).