1644. Lowest Common Ancestor of a Binary Tree II Binary Tree Medium Tree Depth-First Search

Leetcode Link

Problem Description

The task is to find the lowest common ancestor (LCA) of two given nodes, p and q, in a binary tree. The LCA is defined as the lowest node (furthest from the root) that has both nodes p and q as descendants. It's important to note that a node can be a descendant of itself according to the problem statement. If either p or q doesn't exist in the tree, the result should be null. Every node in the tree

has a unique value. Intuition

the root and moving towards the leaves, to find the nodes p and q. We should check three conditions during traversal: 1. Whether the current node is p or q.

To solve this problem, we can use a depth-first search (DFS) traversal. The main idea is to recursively explore the tree, starting from

The lowest common ancestor will be the node where both the left and right subtree searches report finding either p or q. In other

True if p or q is found,

Solution Approach

words, it's the point in the tree where paths from the root to p and q diverge.

2. Whether one of the node's left descendants is p or q.

3. Whether one of the node's right descendants is p or q.

If p and q are on the same branch, the LCA will be the one higher up on the path. If p is an ancestor of q, then p is the LCA and vice versa. To implement this, we can do a post-order traversal and return three possible values:

 False if neither is found, A node if it is the ancestor of both p and q.

nodes p and q. To do this, we define a helper function dfs within the lowestCommonAncestor method.

A global variable or a nonlocal in Python, which Python allows to be modified inside a nested function, is used to keep track of the answer. Once we find p and q, we assign the LCA to this variable.

The solution uses a Depth-First Search (DFS) traversal to go through each node in the binary tree and check for the presence of

It begins with a base case that checks if the root is None, meaning we have reached the end of a path without finding a node. If

this is the case, it returns False. Left Recursion: Recursively call dfs for the left child of the current node (root.left). Right Recursion: Recursively call dfs for the right child of the current node (root.right).

The function takes three arguments: root, p, and q, where root is the current node of the tree that we are exploring.

• 1: Whether node p or q has been found in the left subtree. r: Whether node p or q has been found in the right subtree.

Using this information, we can detect the LCA:

Here is a breakdown of how the dfs function works:

The value of the current node.

These recursive calls will do a post-order traversal of the tree. After these calls, we have three pieces of information:

• If 1 and r are both True, it implies that p is found in one subtree and q in the other, making the current node their LCA, so we set ans to root.

Finally, lowestCommonAncestor initializes a variable ans to None, which is used to store the LCA. We declare ans as nonlocal inside dfs

so that it can be modified within the nested function. The dfs function is then called with the original root, p, and q. The ans is

returned as the final result of the lowestCommonAncestor method. If p and q are both present in the tree, ans will be their lowest

This approach efficiently utilizes the single pass post-order DFS traversal to not just search for p and q but also to identify the LCA

- If one of 1 or r is True and the current node's value matches p or q, the current node is the LCA this happens when one is a descendant of the other.
- After the visit to each node, we return a boolean to indicate if either p or q has been found in the current subtree or if the current node is p or q. This boolean is the OR of:
- a check whether the current root matches either p or q.

1 (result from the left subtree),

r (result from the right subtree), and

- Example Walkthrough
- Let's consider a binary tree and walk through the solution to find the lowest common ancestor (LCA) for two given nodes, p and q.

common ancestor; if either is not present, ans will remain None.

without any additional storage or multiple passes through the tree.

3. Since root is not None, it's not the base case, so we proceed.

4. Left Recursion: We call dfs(root.left, p, q) which is dfs(5, 5, 4).

Entering the dfs function again for node 5, we check the left and right children.

Left Recursion: Calling dfs(5.left, p, q) which is dfs(6, 5, 4) returns False.

For our example, let's assume we want to find the LCA of nodes 5 and 4. 1. We initiate the lowestCommonAncestor method with the root node (3) and nodes p (5) and q (4). 2. We enter the dfs function with the current root (node 3) and check for p and q.

5. Returning to dfs(5, 5, 4), the left call returned False, but the right returned True, and since the current root is p (5), we find

 Right Recursion: Calling dfs(5.right, p, q) which is dfs(2, 5, 4). For node 2, we again explore its children. Left Recursion: Calling dfs(2.left, p, q) which is dfs(7, 5, 4) returns False. Right Recursion: Calling dfs(2.right, p, q) which is dfs(4, 5, 4) returns True because root matches q. Since dfs(2, 5, 4) found q, it returns True to dfs(5, 5, 4) call.

structure.

class TreeNode:

class Solution:

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*/

C++ Solution

struct TreeNode {

int val;

11 class Solution {

/**

private:

/**

TreeNode *left;

TreeNode *right;

* Definition for a binary tree node.

TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}

* @param p The first node for which LCA is to be found.

* @param g The second node for which LCA is to be found.

* @param root The root node of the binary tree.

findLowestCommonAncestor(root, p, q);

* Helper method to perform DFS to find LCA.

* @param current The current node being looked at.

// Recursively search in the left subtree.

// Recursively search in the right subtree.

if (leftSearch && rightSearch) {

answer = currentNode;

// the current node is the LCA.

answer = currentNode;

(leftSearch | | rightSearch) &&

// Return the identified LCA or null if none found.

const leftSearch = depthFirstSearch(currentNode.left);

const rightSearch = depthFirstSearch(currentNode.right);

// If both left and right subtrees return true, the current node is the LCA.

(currentNode.val === node1.val || currentNode.val === node2.val)

* @param nodeP The first node for which LCA is to be found.

* @param nodeQ The second node for which LCA is to be found.

* @return True if the current subtree contains either nodeP or nodeQ.

* @return The LCA of nodes p and q.

return ancestor;

* Finds the lowest common ancestor (LCA) of two given nodes in a binary tree.

TreeNode* lowestCommonAncestor(TreeNode* root, TreeNode* p, TreeNode* q) {

TreeNode* ancestor = nullptr; // Holds the lowest common ancestor once found

Definition for a binary tree node.

def __init__(self, x):

Args:

Returns:

if current_node is None:

Search left subtree for p or q

Search right subtree for p or q

Check if current node is either p or q

Call dfs to initiate the depth-first search

mid = current_node == p or current_node == q

right = dfs(current_node.right)

if mid + left + right >= 2:

left = dfs(current_node.left)

return False

self.left = None

self.right = None

This path will not find either p or q, and will therefore return False.

6. The result of True is then carried up and we exit the left side of the root.

7. Right Recursion: We now call dfs(root.right, p, q) which is dfs(1, 5, 4).

that 5 is indeed the LCA because it is an ancestor to q (4).

8. With dfs(3, 5, 4), since the 1 (Left Recursion) returned True and r (Right Recursion) returned False, and no match for p or q is found at the current node (3), we simply propagate the True back up.

recursive traversal and updates an ancestor variable when both nodes are found within the subtrees.

def lowestCommonAncestor(self, root: 'TreeNode', p: 'TreeNode', q: 'TreeNode') -> 'TreeNode':

bool: True if the current node is ancestor or is a subtree containing p or q.

If any two of the three flags left, right, mid are True, current_node is an ancestor

The provided solution can be used to find the lowest common ancestor (LCA) of two nodes in a binary tree.

// Return true if the current node is either p or q or if p or q is found in either subtree.

return foundInLeftSubtree || foundInRightSubtree || currentNode.val == p.val || currentNode.val == q.val;

current_node (TreeNode): The current node being visited.

Python Solution

9. Since the LCA has been set to node 5 within dfs(5, 5, 4), the global ans variable will now hold the reference to the LCA.

10. Finally, lowestCommonAncestor returns ans which is node 5, and this node is indeed the LCA of nodes 5 and 4 as per our tree

In conclusion, the example walks through the DFS approach to efficiently find the LCA by using a helper dfs function that handles

This variable will hold the lowest common ancestor once it is found. 11 self.ancestor = None 12 def dfs(current_node): 14 15 16 Perform a depth-first search to find the lowest common ancestor. 17

self.ancestor = current_node 38 39 # Return True if the current node is p, q, or if p or q is in the subtree rooted at current_node 40 return mid or left or right 41 42

dfs(root)

return self.ancestor

49 Java Solution class Solution { // The variable 'answer' will hold the solution. private TreeNode answer; // This method returns the lowest common ancestor of two nodes in the binary tree. public TreeNode lowestCommonAncestor(TreeNode root, TreeNode p, TreeNode q) { // Initiate the depth-first search. findLowestCommonAncestor(root, p, q); 10 return answer; 11 12 13 // Helper method for a DFS to identify if the current node is part of the path to p or q. private boolean findLowestCommonAncestor(TreeNode currentNode, TreeNode p, TreeNode q) { 14 15 // Base case: if the current node is null, return false. if (currentNode == null) { 16 return false; 18 19 20 // Traverse the left side of the tree and store if p or q was found in the left subtree. 21 boolean foundInLeftSubtree = findLowestCommonAncestor(currentNode.left, p, q); 22 // Traverse the right side of the tree and store if p or q was found in the right subtree. 23 boolean foundInRightSubtree = findLowestCommonAncestor(currentNode.right, p, q); 24 25 // If both left and right subtrees contain p or q, then the current node is the LCA. 26 if (foundInLeftSubtree && foundInRightSubtree) { 27 answer = currentNode; 28 29 30 // If either left or right subtree contains p or q, and the current node is either p or q, // then the current node is the LCA. 31 32 if ((foundInLeftSubtree || foundInRightSubtree) && (currentNode.val == p.val || currentNode.val == q.val)) { 33 answer = currentNode; 34 35

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bool findLowestCommonAncestor(TreeNode* current, TreeNode* nodeP, TreeNode* nodeQ) {
           if (!current) {
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               return false; // Base case: reached the end of a branch
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           bool left = findLowestCommonAncestor(current->left, nodeP, nodeQ); // Search LCA in the left subtree
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           bool right = findLowestCommonAncestor(current->right, nodeP, nodeQ); // Search LCA in the right subtree
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           // If both left and right are true, current is the LCA
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           if (left && right) {
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               ancestor = current;
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           // If either left or right is true and current is either nodeP or nodeQ, current is the LCA
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           if ((left || right) && (current->val == nodeP->val || current->val == nodeQ->val)) {
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                ancestor = current;
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           // Return true if current is nodeP or nodeQ or if left or right are true
           return left || right || current->val == nodeP->val || current->val == nodeQ->val;
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56 };
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Typescript Solution
   // Definition for a binary tree node.
   class TreeNode {
       val: number;
        left: TreeNode | null;
       right: TreeNode | null;
       constructor(val: number) {
           this.val = val;
           this.left = this.right = null;
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11 }
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   /**
    * Finds the lowest common ancestor (LCA) of two nodes in a binary tree.
    * @param {TreeNode} root - The root of the binary tree.
    * @param {TreeNode} node1 - The first node to find the LCA for.
   * @param {TreeNode} node2 - The second node to find the LCA for.
   * @return {TreeNode | null} - The LCA of node1 and node2, or null if none found.
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    */
   const lowestCommonAncestor = (
       root: TreeNode,
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       node1: TreeNode,
       node2: TreeNode
   ): TreeNode | null => {
       // Declaration of the LCA variable.
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       let answer: TreeNode | null = null;
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       // Depth-first search (DFS) function to traverse the tree and find the LCA.
29
       const depthFirstSearch = (currentNode: TreeNode | null): boolean => {
           if (!currentNode) {
30
               // If the current node is null, return false indicating the node is not part of the ancestry of nodel or node2.
31
               return false;
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```

// If either the left or right subtree returns true and the current node equals one of the nodes we're looking for,

// Return true if the current node is equal to nodel or node2 or if either the left or right subtree returns true.

leftSearch || rightSearch || currentNode.val === node1.val || currentNode.val === node2.val

The provided code implements a Depth First Search (DFS) algorithm to find the lowest common ancestor (LCA) of two nodes in a binary tree.

Time Complexity:

nodes p and q.

return (

return answer;

// Initialize the search.

Time and Space Complexity

depthFirstSearch(root);

};

 It visits each node exactly once. The work done at each node is constant (comparisons and boolean checks).

To determine the time complexity, we consider that the function dfs is called recursively for every node in the tree until it finds the

Space Complexity: The space complexity is determined by the depth of the recursion stack which is the height of the binary tree.

Therefore, the time complexity is O(N), where N is the number of nodes in the binary tree.

- In the worst case for a skewed tree (like a linked list), the recursion stack could be as deep as the number of nodes, which would be 0(N). • In the best case for a balanced tree, the height of the tree would be log(N), and thus the space complexity would be O(log(N)).
- The space complexity of the algorithm is O(H), where H is the height of the tree, which is O(N) in the worst case and O(log(N)) in the best case.