2302. Count Subarrays With Score Less Than K

Prefix Sum

Sliding Window

Leetcode Link

Problem Description

Binary Search

Array

Hard

The problem provides us with an array of positive integers, nums, and a number k. Our task is to find the number of contiguous nonempty subarrays within nums where the score of the subarray is less than k. The score of a subarray is calculated by multiplying the sum of the elements in the subarray by the length of the subarray. A subarray is just a sequence of elements from the array that are adjacent to each other.

Intuition

To solve this problem, we need to find a way to efficiently calculate the score for all possible subarrays in nums and count how many of them have a score less than k. Doing this directly would require examining every subarray separately, which can be very inefficient for large arrays.

as we expand and contract the window. By keeping track of the sum of elements currently in the window, we can determine the score quickly for the current window size. Here's the general idea:

The intuition behind the solution is to use a sliding window approach that allows us to calculate the score of subarrays dynamically

We start with a window at the beginning of the array.

- We expand the window to the right by adding elements until the score exceeds or equals k.
- When the score is equal to or greater than k, we shrink the window from the left by removing elements until the score is less than k again.
- For each window size, we count the number of valid subarrays that can be formed, which is equivalent to the number of elements we can add to the right of the current window while maintaining a score less than k.
- This approach ensures we only calculate the score for relevant subarrays and prevents unnecessary recalculations, leading us to the solution in an efficient manner.

Solution Approach

The implementation of the solution uses a two-pointer (or sliding window) approach that keeps track of the current subarray being considered. These two pointers are denoted as i (the right pointer) and j (the left pointer), which represent the current bounds of

the subarray. Here is a step-by-step explanation of the algorithm:

1. Initialize ans to 0; this will count the number of valid subarrays. Also, initialize s to 0; this will hold the sum of the elements of the current subarray. Initialize the left pointer j to 0, which represents the start of the current subarray.

of the subarray to reduce the score.

Increment j to effectively shrink the window from the left.

- 2. Iterate over each element v in nums using its index i, which acts as the end of the subarray. This loop will expand the window to
- the right. Add the value of the current element, v, to s, which maintains the sum of the subarray from index j to i.

3. While the score of the current subarray is greater than or equal to k (i.e., s * (i - j + 1) >= k), remove elements from the start

- Subtract nums [j] from s to reduce the sum. This corresponds to "removing" the element at the start of the subarray.
- 4. At this point, the sum multiplied by the window length is less than k. Therefore, for the current end of the window (1), we can count the number of valid subarrays that end at i as i - j + 1, since we can form a valid subarray by starting from any element between j and i.
 - Add i j + 1 to ans, which accumulates the number of valid subarrays.

5. After the iteration is complete, ans will hold the total number of valid subarrays, and we return this value as the final answer.

By using this algorithm, we avoid explicitly calculating the score for every possible subarray, and we efficiently count the valid subarrays by maintaining an ongoing sum and adjusting the window size. The algorithm has an overall time complexity of O(n)

because each element is added to s and removed from s at most once, keeping the number of operations linear with the size of the input array. Example Walkthrough

We will follow the steps described in the solution approach:

the left pointer j to 0.

1. We initialize ans to 0, which will store the total count of valid subarrays, s to 0 for the sum of the current subarray elements, and

Let's walk through the provided solution with an example. Suppose our array nums is [2, 1, 4, 1] and the number k is 8.

10, which is still greater than 8.

answer = current sum = start index = 0

for end_index, value in enumerate(nums):

start_index += 1

Iterate through the array with index and value

current_sum -= nums[start_index]

start++; // Increment the start index

return count; // Return the total count of valid subarrays

count += end - start + 1;

shrink the window from the left (increase start_index)

while current_sum * (end_index - start_index + 1) >= k:

+ 1 = 0 - 0 + 1 = 1 to ans.

- 2. We begin iterating over nums with the right pointer i. For each element v in nums, we perform the following steps: \circ i = 0, v = 2: Add 2 to s. s becomes 2. (s * (i - j + 1)), which is (2 * (0 - 0 + 1)) = 2, is less than 8, so we add i - j
- \circ i = 1, v = 1: Add 1 to s. s becomes 3. (s * (i j + 1)), which is (3 * (1 0 + 1)) = 6, is less than 8, so we add i j

which is less than 8. Now we add i - j + 1 = 2 - 2 + 1 = 1 to ans.

```
+1=1-0+1=2 to ans.
\circ i = 2, v = 4: Add 4 to s. s becomes 7. (s * (i - j + 1)), which is (7 * (2 - 0 + 1)) = 21, is greater than 8, so we start
 shrinking the window from the left:
```

 \circ i = 3, v = 1: Add 1 to s. s becomes 5. (s * (i - j + 1)), which is (5 * (3 - 2 + 1)) = 10, is again greater than 8. We need to shrink the window:

■ We do not need to remove any elements from the window since j is already at 2 and score 10 is from subarray [4, 1].

■ We again subtract num[j], now 1, from s and increment j. Now s is 4 and j is 2. The score is (4 * (2 - 2 + 1)) = 4,

■ We subtract num[j] which is 2 from s and increment j. Now s is 5 and j is 1. The updated score is (5 * (2 - 1 + 1)) =

Now since we cannot shrink the window and the score is greater than k, we simply move on. At the end of the iteration, we have the total number of valid subarrays which is the value of ans. By adding the counts at each step,

ans = 1 + 2 + 1 = 4. Thus, [2], [2, 1], [1] and [1, 4] are valid subarrays whose scores are less than 8, and the final answer is 4.

from typing import List class Solution: def countSubarrays(self, nums: List[int], k: int) -> int: # Initialize answer, current sum, and start index of the window

```
# Add the current number to the current sum
10
               current_sum += value
11
12
13
               # While the product of the sum of the current subarray
               # and the length of the subarray is at least k,
14
```

9

15

16

17

18

15

16

17

18

19

20

21

22

23

25

24 }

Python Solution

```
19
20
               # The number of subarrays ending with the current number
21
               # is the length of the current window (end_index - start_index + 1)
22
               answer += end_index - start_index + 1
23
24
           # Return the total number of subarrays found
25
           return answer
26
Java Solution
   class Solution {
       public long countSubarrays(int[] nums, long k) {
            long count = 0; // To store the number of subarrays
           long sum = 0; // Sum of the elements in the current subarray
           int start = 0; // Start index for the current subarray
           // Traverse through the array starting from the 0th element
           for (int end = 0; end < nums.length; ++end) {</pre>
               sum += nums[end]; // Add the current element to sum
9
10
11
               // Shrink the subarray from the left if the condition is violated
12
               // sum * length should be less than k
13
               while (sum * (end - start + 1) >= k) {
14
                   sum -= nums[start]; // Removing the element from the start of subarray
```

// At this point, for each element nums[end], we find how many subarrays ending at 'end' are valid

// The number of valid subarrays is given by the difference btw current end and the new start position

```
C++ Solution
 1 class Solution {
 2 public:
        long long countSubarrays(vector<int>& nums, long long k) {
            long long count = 0; // Initialize the count of subarrays
           long long sum = 0; // Initialize the sum of elements in the current subarray
           int start = 0;
                                // Start index for our sliding window
           // Iterate through each element in the array
           for (int end = 0; end < nums.size(); ++end) {</pre>
 9
               sum += nums[end]; // Add the current element to the sum
11
12
               // If the constraint is violated (average * number of elements >= k)
13
               // increment start index to reduce the number of elements and sum
               while (sum * (end - start + 1) >= k) {
14
                   sum -= nums[start++]; // Remove the element pointed by start from sum and increment start
15
16
17
               // Count the number of subarrays ending with nums[end]. If no elements were removed in the while loop,
18
               // this will include all subarrays starting from nums[0..end]. If some elements were removed,
19
               // it will include all subarrays starting from nums[start..end].
20
21
               count += end - start + 1;
23
24
           return count; // Return the total count of valid subarrays
25
26 };
27
```

function countSubarrays(nums: number[], k: number): number {

Typescript Solution

```
let count = 0; // Initialize the count of subarrays
       let sum = 0; // Initialize the sum of the elements in the current subarray
       let start = 0; // Start index for our sliding window
       // Iterate through each element in the array
       for (let end = 0; end < nums.length; end++) {</pre>
           sum += nums[end]; // Add the current element to the sum
 8
 9
           // While the average of the subarray multiplied by the number of elements
10
           // is greater than or equal to k, adjust the start index to shrink the subarray
           while (sum * (end - start + 1) >= k) {
12
               sum -= nums[start]; // Remove the element pointed to by start from the sum
13
14
               start++; // Increment start index to reduce the subarray size
15
16
           // Count the number of subarrays ending with nums[end]. This includes all
           // subarrays starting from nums[start..end]. If the while loop above didn't
           // run, it would also include all subarrays from nums[0..end].
           count += end - start + 1;
       return count; // Return the total count of valid subarrays
Time and Space Complexity
```

20 21 22

23 24 25

element being considered only once by each pointer, resulting in a linear traversal. Thus, the time complexity of this algorithm is O(n), where n is the number of elements in the array nums. This is because both

pointers 1 and 1 can only move from the start to the end of the array once, and the operations inside the for-loop and while-loop are

Space Complexity

all constant time operations.

Time Complexity The given code uses a sliding window technique to count the number of subarrays whose elements product is less than k. In this code, two pointers (i and j) are used, which move forward through the array without stepping backwards. This results in each

The space complexity is determined by the extra space used aside from the input. In this case, only a fixed number of variables (ans, s, j, i, v) are used. These do not depend on the size of the input array. Therefore, the space complexity of the code is 0(1), which is

constant space complexity since no additional space that grows with the input size is used.