

Problem Description

The problem provides us with an array nums containing integers, where our task is to find the maximum difference between two of its elements, nums[i] and nums[j], with the condition that i is less than j (that is i < j) and nums[i] is less than nums[j] (nums[i] < nums [j]). The maximum difference is defined as nums [j] - nums [i]. The constraints are such that i and j must be valid indices within the array ($0 \ll 1 < j < n$). If no such pair of indices exists, the function should return -1.

Intuition

The solution to this problem is driven by a single pass approach that keeps track of the smallest element found so far while iterating through the array. The idea is to continuously update the smallest element mi as we move through the array and simultaneously compute the difference between the current element and this smallest element whenever the current element is larger than mi.

The steps are as follows:

any elements in the array yet. • Initialize a variable ans to store the maximum difference found; set it to -1 to indicate that no valid difference has been

Initialize a variable mi to store the minimum value found so far; set it to inf (infinity) at the start because we haven't encountered

- calculated yet. Iterate over each element x in the nums array.
- If the current element x is greater than the current minimum mi, then there's potential for a larger difference. Calculate the difference x - mi and update ans to be the maximum of ans and this newly calculated difference. If the current element x is not greater than mi, then we update mi to be the current element x, since it's the new minimum.
- After iterating through the entire array, ans will contain the maximum difference found following the given criteria, or it will remain -1

the array, hence the time complexity is O(n), where n is the number of elements in nums. Solution Approach

if no such pair was found (meaning the array was non-increasing). This approach is efficient as it only requires a single pass through

The implementation of the solution utilizes a simple linear scanning algorithm that operates in a single pass through the array. No

complex data structures are needed; only a couple of variables are used to keep track of the state as we iterate. Here is a more detailed breakdown of the approach: We have an array nums of integers.

o mi: This is initially set to inf, representing an "infinity" value which ensures that any element we encounter will be less than

· Two variables are initialized:

- this value. mi serves as the minimum value encounter so far as we iterate through the array. □ ans: This is the answer variable, initialized to -1. It will store the maximum difference encountered that satisfies the problem's condition.
- We begin iterating over each element x in the nums array using a for loop.
- If the current element x is greater than mi, it means we've found a new pair that could potentially lead to a larger difference.
 - In this case, we find the difference between x and mi and update ans to be the maximum of itself and this new difference. This step uses the max function: ans = max(ans, x - mi). If x is not greater than mi, then the current element x becomes the new minimum, which updates mi to x. It's a crucial step, as this update is necessary to ensure we always have the smallest value seen so far, which allows us to find the largest
- possible difference. After the loop completes, the ans variable will hold the maximum difference possible. If ans remained -1, it implies there was no valid (i, j) pair that satisfied the condition (nums[i] < nums[j] with i < j).

not found during the computation. The algorithm's simplicity and the lack of additional data structures contribute to its time efficiency, making it a solution with O(n) time complexity, where n is the number of elements in nums.

The use of the infinity value for mi is a common pattern to simplify code as it avoids the need for special checks on the index being

valid or the array being non-empty. Similarly, using -1 for ans follows a typical convention to indicate that a satisfying condition was

Example Walkthrough

• mi is set to inf, which in practical scenarios can be represented by a very large number, assuming the array does not contain

1 nums = [7, 1, 5, 3, 6, 4]

Our task is to find the maximum difference nums[j] - nums[i] with the conditions that i < j and nums[i] < nums[j].

Let's illustrate the solution approach with a small example. Suppose we have the following array nums:

```
We'll initialize our variables mi and ans:
```

larger numbers.

- ans is set to -1 as we've not yet found a valid pair.
- 1. First element (7):

No difference is calculated because this is the first element.

o mi is inf, so we update mi to be 7.

Now we begin iterating through the array nums:

- 2. Second element (1):
 - The ans is still -1 because we didn't find a larger element yet.
- 3. Third element (5):

1 is less than mi (which is 7), so we now update mi to 1.

- Now, we update ans to the maximum of -1 and 4, which is 4. 4. Fourth element (3):
- ans remains 4 because 4 is greater than 2. 5. Fifth element (6):

 \circ 3 is greater than mi (1), so we calculate the difference (3 - 1 = 2).

◦ 5 is greater than mi (which is 1), so we calculate the difference (5 - 1 = 4).

- 6 is greater than mi (1), so we calculate the difference (6 1 = 5). Update ans to 5, since that's greater than the current ans of 4.
- 4 is greater than mi (1), so we calculate the difference (4 1 = 3).

6. Sixth element (4):

Python Solution

class Solution:

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25 }

- o ans remains 5, as it is still the maximum difference found. At the end of the iteration, and contains the value 5, which is the maximum difference obtained by subtracting an earlier, smaller
- Therefore, the maximum difference in the given array nums is 5.

Initialize the minimum value seen so far to infinity

there is a potential for a new maximum difference

update the minimum value to the current number

Return the maximum difference found; if no valid difference was found,

If the current number is greater than the minimum value seen,

Initialize the maximum difference as -1 (default if not found) $max_diff = -1$ # Iterate over each number in the list for num in nums:

number from a later, larger number in the array, satisfying nums[j] - nums[i] where i < j and nums[i] < nums[j].

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                   # Update the maximum difference if the current difference
                   # is greater than the previous maximum difference
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                   max_diff = max(max_diff, num - min_val)
               else:
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                   # If the current number is not greater than the minimum value seen,
```

def maximumDifference(self, nums: List[int]) -> int:

min_val = float('inf')

if num > min_val:

min_val = num

this will return -1

```
23
           return max_diff
24
Java Solution
   class Solution {
       public int maximumDifference(int[] nums) {
           // Initialize the minimum value to a very large value
           int minVal = Integer.MAX_VALUE;
           // Initialize the answer to -1, assuming there is no positive difference found
           int maxDiff = -1;
           // Loop through each number in the input array
           for (int num : nums) {
               // If the current number is greater than the minimum value found so far
               if (num > minVal) {
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                   // Update the maximum difference with the greater value between the current maximum difference
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                   // and the difference between the current number and the minimum value found so far
                   maxDiff = Math.max(maxDiff, num - minVal);
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               } else {
                   // If the current number is not greater than the minimum value found so far,
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                   // then update the minimum value to the current number
                   minVal = num;
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// Return the maximum difference found, or -1 if no positive difference exists

C++ Solution

return maxDiff;

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1 class Solution {
   public:
        int maximumDifference(vector<int>& nums) {
           // Initialize min_value with a large number well above any expected input.
            int min_value = INT_MAX; // INT_MAX is more idiomatic than 1 << 30.</pre>
           // Initialize the answer with -1, indicating no positive difference found yet.
            int max_difference = -1;
           // Iterate over each number in the input vector 'nums'.
10
            for (int num : nums) {
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               // If the current number is larger than the min_value seen so far,
               // update max_difference with the greater of current max_difference and
13
               // the difference between current number and min_value.
14
               if (num > min_value) {
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                    max_difference = max(max_difference, num - min_value);
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                } else {
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                    // If the current number is smaller than min_value, update min_value
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                    // with the current number.
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                    min_value = num;
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           // Return the maximum positive difference found, or -1 if no such difference exists.
25
            return max_difference;
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27 };
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```

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Typescript Solution

function maximumDifference(nums: number[]): number {

// detn is the length of the nums array

const numElements = nums.length;

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// Initialize the minimum value to the first element of the nums array
       let minimumValue = nums[0];
       // Initialize the maximum difference as -1; this will change if a greater difference is found
       let maxDifference = -1;
       // Loop through the array starting from the second element
       for (let index = 1; index < numElements; index++) {</pre>
10
           // Calculate the current difference and update the maxDifference if the current difference is greater
           maxDifference = Math.max(maxDifference, nums[index] - minimumValue);
           // Update the minimumValue with the smallest number encountered so far
           minimumValue = Math.min(minimumValue, nums[index]);
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15
16
       // If no positive maximum difference was found, return -1; otherwise, return the maxDifference
17
       return maxDifference > 0 ? maxDifference : -1;
18
19 }
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Time and Space Complexity
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The time complexity of the provided code can be analyzed by looking at the operations within the main loop. The code iterates

the input list, this does not change, which means the space complexity is constant, or 0(1).

through the list of numbers once, performing constant-time operations within each iteration, such as comparison, subtraction, and

assignment. Thus, the time complexity is O(n) where n is the length of the input list nums. For space complexity, the code uses a fixed amount of additional memory to store the variables mi and ans. Regardless of the size of