

Problem Description

You are tasked with finding a specific type of triplet in an integer array nums, where the array indices start at 0. This triplet needs to follow the characteristics of a mountain, which means for indices i, j, k satisfying i < j < k, the elements at these indices must adhere to the pattern nums[i] < nums[j] and nums[k] < nums[j]. The goal is to determine the smallest possible sum of such a mountain triplet. If there are no triplets that form a mountain, you should return -1.

The problem calls for an efficient way to find the smallest sum of a "mountain" within an array. To approach this, you would need to

Intuition

check each possible middle element (the peak of the mountain) to see if there's a smaller number before it (uphill) and a smaller number after it (downhill). A brute-force solution would be to try every possible triplet to find the minimum sum, but that would result in a high time complexity. Instead, we can use pre-processing to optimize this procedure. By iterating through the array once, we can store the minimum value

found to the right of each element in a new array called right. This pre-processing helps us quickly find the smallest element that can be the downhill part of the mountain for any middle element we're considering. As we traverse the array to find the middle element of potential mountain triplets, we keep track of the smallest value encountered

so far to serve as the uphill part of the mountain. This value is stored in a variable called left. At any point, if our current element is

greater than both left and the corresponding value in right, we have found a valid mountain. We then check if the sum of left, the current element, and the corresponding right is less than the best answer we have found so far, updating our answer accordingly. If after traversing the array no valid mountain is found, the answer remains at its initial infinite value and we return -1. Otherwise, we return the smallest sum found.

Solution Approach

The implementation of the solution is based on the Reference Solution Approach provided, which cleverly reduces the problem's

complexity by pre-processing the array and using two pointers to track the minimum values required to identify a potential mountain.

Here's how the solution approach is implemented step by step:

1. Pre-processing: We create an array right which holds the minimum value to the right of each index in the nums array. We

initialize every element in right to be inf (inf is a placeholder for infinity), which ensures that any number compared to it will be

smaller. Starting from the second last element in nums and moving backwards, we populate right[i] with the minimum between

right[i + 1] and nums[i].

- 2. One pass enumeration with two pointers: As we iterate through the nums array using the variable 1, we maintain two pointers/values: left: The minimum value in the subarray to the left of the current index i (including nums [i]).
- 3. Evaluating potential mountains: For each element nums [i], which we are considering to be the peak of the mountain (j), we check if we have a smaller number on its left (uphill) and on its right (downhill):

ans: The result variable which keeps track of the minimum sum of a valid mountain that has been found so far.

 If both conditions are met, nums [i] can be the peak of a mountain, and we update ans with the sum of left, nums [i], and right[i + 1] if it's smaller than the current ans.

The check right [i + 1] < nums [i] ensures that we have a valid downhill part for the mountain.

The check left < nums [i] ensures that the current peak is higher than the minimum value on the left.

5. Returning the result: Once we've iterated through the entire array, we check whether ans is still infinity. If it is, no valid mountain was found, and we return -1. Otherwise, we return the minimum sum stored in ans.

4. Updating the minimum left value: After each iteration, we update left to be the minimum value between the current left and

By following this approach, we avoid the need for a triple nested loop to check every possible triplet, which significantly optimizes the solution. The algorithm achieves a time complexity of O(n) since it only requires two passes through the nums array (one for pre-

To illustrate the solution approach, let's consider a small example of the nums array: 1 nums = [2, 1, 4, 7, 3, 2, 5]

We begin by creating a right array that will contain the minimum value to the right of each index, initializing all elements to infinity:

1 right = [inf, inf, inf, inf, inf, inf]

Step 1: Pre-processing

Example Walkthrough

processing and one for the main iteration).

nums[i].

We then update the right array by traversing from right to left:

1 Starting with the second to last index, right[5] is min(inf, 2) = 2

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right [4] is min(2, 3) = 2
right = [inf, inf, inf, inf, 2, 2, inf]
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right[3] is min(2, 7) = 2

10 right[2] is min(2, 4) = 2

right[1] is min(2, 1) = 1

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2 right = [inf, inf, inf, inf, inf, 2, inf]

right = [inf, inf, inf, 2, 2, 2, inf]

right = [inf, inf, 2, 2, 2, 2, inf]

right = [inf, 1, 2, 2, 2, inf]

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15
16 right[0] will not be used since it must be the leftmost element of a triplet.
Final right array after pre-processing:
1 right = [inf, 1, 2, 2, 2, 2, inf]
Step 2: One pass enumeration with two pointers
We initialize two variables - left starting with infinity and ans also with infinity.
As we start iterating over the array, our pointers will update as follows:
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Step 3: Evaluating potential mountains

index 1 since left >= nums[i]. • When i is 2 (nums[i] is 4), we have left = 1 and right[3] is 2. This satisfies the mountain property (left < nums[i] > right[3]). We sum 1 + 4 + 2 to get the total sum of 7. Since ans was infinity, it is now updated to 7.

be 1 + 7 + 2 which is 10, larger than our current ans.

mountain, and 7 is the smallest sum of such a mountain triplet.

def minimumSum(self, nums: List[int]) -> int:

min_right = [float('inf')] * (num_length + 1)

for i in range(num_length - 1, -1, -1):

min_left = min(min_left, x)

public int minimumSum(int[] nums) {

return -1 if answer == float('inf') else answer

int n = nums.length; // Length of the input array

get the length of the nums list

num_length = len(nums)

After each iteration, left is updated to the minimum value it has seen so far (if smaller than nums [1]), which helps efficiently find the uphill part for the next iterations.

• When i is 0 (nums [i] is 2), i is at the leftmost edge, so left does not update because no valid mountain can start here.

• When i is 1 (nums [i] is 1), the left array so far [2] has a minimum of 2, and our right is 1. No valid mountain can have a peak at

• When i is 3 (nums[i] is 7), a sum is possible here, but it won't be minimum because right[4] = 2 and the minimum sum would

For i 4, 5, and 6, while a valley exists to the right (right[i + 1] < nums[i]), no smaller value exists to the left (left >= nums[i]),

Therefore, the smallest possible sum of a mountain triplet in the nums array is 7.

After iterating through the entire nums array, we find that ans is 7. Since it's no longer infinity, we have found at least one valid

initialize the answer and the minimum value from the left with infinity answer = min_left = float('inf') # iterate over nums to find the minimum sum

initialize a list to keep track of the minimum value to the right

populate the min_right list with the minimum values from right to left

update min_left to the smallest number found so far from the left

return -1 if answer has not been updated, otherwise return the answer

including the current position, filled with infinity to start

1 left = inf

so no valid mountain can exist at these points. Step 4: Updating the minimum left value

Step 5: Returning the result

from typing import List

class Solution:

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Python Solution

for i, x in enumerate(nums): 20 # if the current number is greater than the smallest number found 21 # to its left and to its right, consider it as a candidate for the answer 22 if min_left < x and min_right[i + 1] < x:</pre> 23 answer = min(answer, min_left + x + min_right[i + 1])

min_right[i] = min(min_right[i + 1], nums[i])

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Java Solution
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class Solution {

int[] rightMin = new int[n + 1]; // Array to hold the minimum values from the right final int INF = Integer.MAX_VALUE; // Use Java's max value to represent infinity rightMin[n] = INF; // Set the rightmost value to infinity as a sentinel value 6 // Populate rightMin with the minimum values scanned from right to left for (int i = n - 1; i >= 0; --i) { 9 rightMin[i] = Math.min(rightMin[i + 1], nums[i]); 10 11 12 13 int answer = INF; // Initialize answer with the maximum possible value (infinity) int leftMin = INF; // Variable to keep track of the minimum value scanned from left 14 15 // Iterate over the array to find the minimum sum with the specified conditions 16 for (int i = 0; i < n; ++i) { 17 18 // Check if both leftMin and rightMin[i+1] are less than nums[i] 19 if (leftMin < nums[i] && rightMin[i + 1] < nums[i]) {</pre> // Update the answer with the minimum of previous answer 20 21 // and the sum of leftMin, nums[i], and rightMin[i+1] answer = Math.min(answer, leftMin + nums[i] + rightMin[i + 1]); 23 // Update leftMin with the smallest value encountered so far 24 25 leftMin = Math.min(leftMin, nums[i]); 26 27 28 // Return the answer if it's not infinity, otherwise return -1 29 return answer != INF ? answer : -1; 30 31 } 32 C++ Solution

vector<int> right_smallest(nums_size + 1, INFINITY); // Vector to keep track of the right smallest elements.

23 for (int i = 0; i < nums_size; ++i) {</pre> 24 // Check if the current element is greater than both the left and right smallest elements. if (left_smallest < nums[i] && right_smallest[i + 1] < nums[i]) {</pre> 25 26 // Update the result with the minimum sum found so far. 27 result = min(result, left_smallest + nums[i] + right_smallest[i + 1]);

1 #include <vector>

3 using std::vector;

using std::min;

6 class Solution {

public:

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2 #include <algorithm> // Including algorithm for std::min

for (int $i = nums_size - 1; i >= 0; --i) {$

int nums_size = nums.size(); // Size of the nums vector.

// Iterate through the vector to find the minimum sum.

left_smallest = min(left_smallest, nums[i]);

right_smallest[i] = min(right_smallest[i + 1], nums[i]);

const int INFINITY = 1 << 30; // Representing infinity as a very large number.</pre>

// Populate the right_smallest vector with the smallest value found from the right.

int result = INFINITY; // This will hold the final result, initialized to infinity.

int left_smallest = INFINITY; // Keeping track of the smallest value from the left.

right_smallest[nums_size] = INFINITY; // Initialization to infinity at the end of the vector.

// Update left_smallest to be the smallest value from the left up to the current position.

int minimumSum(vector<int>& nums) {

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           // If the result is still infinity, then a sum cannot be formed as per the problem's requirement.
34
           // Return -1 in that case. Otherwise, return the result.
35
           return result == INFINITY ? -1 : result;
36
37 };
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Typescript Solution
   function minimumSum(nums: number[]): number {
       // Initialize the length of the given array
       const numsLength = nums.length;
       // Create an array 'right' to keep track of the smallest number to the right
       // for each position, initialized to Infinity.
 6
       const rightMinValues: number[] = Array(numsLength + 1).fill(Infinity);
 8
       // Populate the 'rightMinValues' array from right to left
 9
       for (let i = numsLength - 1; i >= 0; --i) {
10
            rightMinValues[i] = Math.min(rightMinValues[i + 1], nums[i]);
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       // Declare variables to keep track of the minimum answer and left minimum value
14
       let minAnswer = Infinity;
15
       let leftMinValue = Infinity;
16
17
       // Iterate over the array to compute the minimum sum of a valid triplet
18
       for (let i = 0; i < numsLength; ++i) {
19
           // Check if the current number is larger than the minimum on both sides
20
           if (leftMinValue < nums[i] && rightMinValues[i + 1] < nums[i]) {
               // Update the minimum answer with the sum of the triplet
23
               // if it is smaller than the current minimum
24
               minAnswer = Math.min(minAnswer, leftMinValue + nums[i] + rightMinValues[i + 1]);
25
26
           // Store the minimum on the left up to the current element
27
            leftMinValue = Math.min(leftMinValue, nums[i]);
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return minAnswer === Infinity ? -1 : minAnswer;

their combined time complexity remains linear with the size of the input list.

33 Time and Space Complexity The time complexity of the provided code is indeed 0(n). This is because the code consists of two loops over the nums list, each running for n iterations, where n is the length of the input list nums. The first loop is a reverse iteration used to build the right list, and

the second loop goes through the nums list to compute the ans variable. Since both loops are independent and execute sequentially,

// Return the minimum answer or -1 if the answer remains Infinity (no valid triplet found)

The space complexity of the code is O(n) as well due to the allocation of the right list, which stores the minimum value encountered from the right side of the nums list. This right list has a length equal to n + 1, where n is the length of the nums list. The other variables used (ans, left, and a few others) do not depend on n and thus contribute a constant factor, which is ignorable when assessing space complexity.