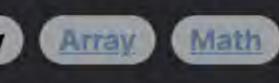




Problem Description



The problem presents us with an array called coordinates. Each element within this array is itself an array that represents a point in the form [x, y]—where x is the x-coordinate and y is the y-coordinate of a point on the XY plane. The task is to determine if all

these points lie on a single straight line or not. Intuition

To check if points lie on the same straight line, we need to ensure that the slope between any two points is the same across all points. The slope is a measure of how steep a line is. If pairs of points have different slopes, the points do not lie on a single straight

line. To calculate the slope between two points (x1, y1) and (x2, y2), we use the formula slope = (y2 - y1) / (x2 - x1). If the slope is consistent between consecutive points, then all the points are on the same line.

avoid the potential division by zero error, we check the equality of slopes using a cross-multiplication method. Specifically, instead of directly computing (y2 - y1) / (x2 - x1) == (y - y1) / (x - x1), we check if (x - x1) * (y2 - y1) == (y - y1) * (x2 - x1)

In our solution, we take the first two points from coordinates to calculate a reference slope. For computational efficiency and to

for subsequent points (x, y). If the equality holds for all pairs of points in the coordinates array, the function returns True, which means all points lie on a single straight line. If any pair of points fails the equality test, the function returns False, and we know that not all points are on the same

The intuition behind this approach is that we're using the properties of slopes in a way that's computationally efficient and avoids possible arithmetic errors when dealing with real numbers.

The algorithm follows a straightforward approach by checking if the slope between any two points is the same across all points. No additional data structures or complex patterns are necessary. The algorithm involves simple arithmetic operations and a for loop.

Solution Approach

line.

Here's a step-by-step implementation break down: 1. The algorithm starts by storing the x and y coordinates of the first two points from the coordinates array in x1, y1 and x2, y2. These two points are used to find the reference slope for the line.

- 2. The algorithm then iterates over the remaining points in coordinates, starting from the third point, using a for x, y in coordinates[2:]: loop.
- 3. Inside the loop, for each point (x, y), the algorithm checks if the cross-product of the differences in coordinates between point (x, y) and the first point (x1, y1) equals the cross-product of the differences between the second point (x2, y2) and the first
- point. The check is made using the following condition: 1 if (x - x1) * (y2 - y1) != (y - y1) * (x2 - x1):

This expression is derived from the slope equality slope1 = slope2. Instead of dividing the differences, which can cause a

return False

straight line.

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division by zero, it multiplies the opposite sides and compares them for equality.
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5. If the loop completes without encountering any point that fails the slope check, the function returns True, signaling that all points do indeed lie on a straight line.

4. If the check fails for any point, the function immediately returns False, indicating that the points do not all lie on the same

The time complexity of this algorithm is O(n), where n is the number of points, since we have to check the condition for each point

once. The space complexity is O(1) since we are using a fixed amount of additional space regardless of the number of points.

Example Walkthrough Let's walk through a small example to illustrate the solution approach:

Suppose coordinates = [[1, 2], [2, 3], [3, 4]]. We are looking to confirm whether these points fall on a single straight line.

1. Based on our algorithm, we first take the coordinates of the first two points to calculate the reference slope. So from our

coordinates, we have x1, y1 = 1, 2 and x2, y2 = 2, 3.

iterate over just one point: [3, 4].

2. Next, the algorithm will iterate over the remaining points in coordinates. Since we only have three points in this example, it will

- 3. Now, the algorithm will check if the cross-product of differences with the new point [3, 4], denoted as (x, y), and the first point (x1, y1) equals the cross-product of the differences between the second point (x2, y2) and the first point. This equation looks like:
- Simplifying the expressions on each side of the inequality gives: if 2 * 1 != 2 * 1:

In this case, both sides are equal, meaning that the slope between point [1, 2] and point [3, 4] is the same as the slope

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between point [1, 2] and point [2, 3].
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if (3-1)*(3-2)!=(4-2)*(2-1):

4. Since there are no more points to check, and the equality held true for the third point, the algorithm would return True.

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5. This confirms that all the given points in the example line [1, 2], [2, 3], [3, 4] are on the same straight line.
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def checkStraightLine(self, coordinates: List[List[int]]) -> bool:

Check if the subsequent points are in a straight line

(x - x1)/(x2 - x1) should be equal to (y - y1)/(y2 - y1)

(x - x1) * (y2 - y1) should be equal to (y - y1) * (x2 - x1)

Use the cross product to determine if three points are on the same line:

If they are not equal for any point, the points do not form a straight line

// Check if the current point lies on the line formed by the first two points

// This is done by using the cross product which should be zero for collinear points

Cross-multiplying to avoid division (to handle the case when $x^2 - x^2$ is 0) we get:

if (4-1)*(3-2)!=(6-2)*(2-1):which simplifies to:

If we had a point that did not satisfy the slope equality, for example [4, 5] replaced by [4, 6], the algorithm would compare:

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This inequality is true, indicating that the point [4, 6] does not lie on the same straight line as the others, so the algorithm would
return False.
```

Extract the first 2 points

Coordinates of the second point

int deltaX1 = currentX - x1;

int deltaY2 = currentY - y1;

int deltaY1 = y2 - y1;

int deltaX2 = x2 - x1;

for point in coordinates[2:]:

x2, y2 = second_point

x, y = point

from typing import List class Solution:

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30 };

return true;

Typescript Solution

import { Vector } from 'prelude-ts';

const x1 = coordinates[0][0];

// Extract the first point (x1, y1)

// Necessary import statement when working with arrays in TypeScript

// Function to check if all points lie on a straight line.

function checkStraightLine(coordinates: number[][]): boolean {

Python Solution

if 3 != 4:

first_point = coordinates[0] second_point = coordinates[1] # Coordinates of the first point x1, y1 = first_point 10

```
24
               if (x - x1) * (y2 - y1) != (y - y1) * (x2 - x1):
25
                    return False
26
           # If the loop completes without returning False, all points are in a straight line
28
            return True
29
Java Solution
   class Solution {
        * Checks if all the given points lie on a straight line.
        * @param coordinates Array of point coordinates on a 2D plane.
 6
        * @return true if all points lie on a single straight line, false otherwise.
 8
       public boolean checkStraightLine(int[][] coordinates) {
 9
           // Coordinates of the first point
10
           int x1 = coordinates[0][0];
11
            int y1 = coordinates[0][1];
12
13
14
           // Coordinates of the second point
15
           int x2 = coordinates[1][0];
            int y2 = coordinates[1][1];
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17
18
           // Loop over the rest of the points starting from the third one
           for (int i = 2; i < coordinates.length; i++) {</pre>
19
20
               // Coordinates of the current point
                int currentX = coordinates[i][0];
21
                int currentY = coordinates[i][1];
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31
               // If current point does not satisfy the line equation then return false
               if (deltaX1 * deltaY1 != deltaY2 * deltaX2) {
33
                    return false;
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35
36
37
           // If all the points satisfy the line equation then return true
38
           return true;
39
40 }
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C++ Solution
 1 #include<vector> // Needed to use std::vector
 2 using std::vector;
   class Solution {
   public:
       // Function to check if all points lie on a straight line.
       bool checkStraightLine(vector<vector<int>>& coordinates) {
           // Extract the first point (x1,y1)
           int x1 = coordinates[0][0], y1 = coordinates[0][1];
           // Extract the second point (x2,y2)
11
           int x2 = coordinates[1][0], y2 = coordinates[1][1];
12
           // Loop through all the remaining points
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           for (int i = 2; i < coordinates.size(); ++i) {</pre>
14
               // Extract the current point (x,y)
15
               int x = coordinates[i][0], y = coordinates[i][1];
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               // Check if the cross product of the vectors is zero
               // This is a vector algebra way of checking colinearity:
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20
               //(x-x1)/(x2-x1) should be equal to (y-y1)/(y2-y1) for all points on the line
               // By cross-multiplying to avoid division (and potential division by zero),
21
               // we get (x-x1)*(y2-y1) == (y-y1)*(x2-x1)
               if ((x - x1) * (y2 - y1) != (y - y1) * (x2 - x1)) {
24
                    return false; // The current point doesn't lie on the straight line defined by the first two points
25
26
27
           // All points lie on the same straight line
```

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const y1 = coordinates[0][1];
 9
10
       // Extract the second point (x2, y2)
       const x2 = coordinates[1][0];
11
       const y2 = coordinates[1][1];
12
13
14
       // Loop through all the remaining points
15
       for (let i = 2; i < coordinates.length; i++) {</pre>
16
           // Extract the current point (x, y)
17
           const x = coordinates[i][0];
           const y = coordinates[i][1];
18
19
20
           // Check if the cross product of the vectors is zero
21
           // This is a vector algebra way of checking collinearity:
22
           // (x-x1)/(x2-x1) should be equal to (y-y1)/(y2-y1) for all points on the line
23
           // By cross-multiplying to avoid division (and potential division by zero),
24
           // we get (x-x1) * (y2-y1) == (y-y1) * (x2-x1)
           if((x-x1)*(y2-y1)!==(y-y1)*(x2-x1)) {
25
26
               return false; // The current point doesn't lie on the straight line defined by the first two points
27
29
       // All points lie on the same straight line
30
       return true;
31
32 }
33
Time and Space Complexity
Time Complexity
```

The time complexity of the function checkStraightLine is O(n), where n is the number of coordinate points in the input list

Space Complexity The space complexity of the function is 0(1). The function uses a fixed amount of extra space to store the variables x1, y1, x2, y2, x,

coordinates. This is because the function uses a single loop that iterates through the coordinates starting from the third element,

and for each iteration, it performs a constant number of mathematical operations to check if the points lie on the same line. These

operations do not depend on the size of the input other than the fact that they iterate once for each element beyond the first two.

and y. The amount of space used does not scale with the size of the input list, meaning that the space usage is constant.