40. Combination Sum II Backtracking Medium Array

Problem Description In this problem, we are given a set of candidate numbers (an array candidates) and a target number (target). Our goal is to find all

unique combinations where the sum of the numbers in each combination equals the target. Importantly, we can only use each number in candidates once in any given combination. Another important requirement is that the solution set must not include any duplicate combinations. Even though the same number

Leetcode Link

Essentially, we need to explore all possible combinations of the numbers that add up to the target and return a list of all combinations that meet the criteria without any repetitions.

Intuition

Since we need to find all combinations that add up to the target and any number in the candidates can be used only once, we sort

the candidates first. Sorting the array helps us to easily skip over duplicate elements and avoid generating duplicate combinations.

The intuition behind the solution involves a backtracking technique, which is similar to depth-first search (DFS).

Then, we perform DFS with backtracking, starting from the beginning of the candidates array and exploring each possibility by either including or excluding a candidate. After including a candidate in the combination, we call the function recursively, reducing the

can occur multiple times in the candidates, it can only appear once in each combination.

target by the value of that candidate and moving to the next index. While exploring, we keep track of the current sum of the combination, and when the sum equals the target, we add the current

combination to the answer. If at any point, the sum exceeds target or we reach the end of the candidates array, we backtrack.

To prevent duplicates, we skip subsequent candidates that are the same as the previous one at each stage in the loop. This way, we ensure that if a number has been used in a combination, the same number is not used immediately again to form another similar combination.

The result of the function will be a list of lists, where each inner list is a unique combination of numbers that sum to the target value.

Solution Approach

The solution uses depth-first search (DFS), backtracking, and sorting to effectively find all unique combinations. Let's break down

1. Sorting the Candidates: The candidates array is first sorted to ensure that we can easily skip duplicates. 1 candidates.sort()

2. Depth-First Search (DFS) Function: The dfs function is defined to handle the recursion, taking two parameters: i (the current

1 def dfs(i: int, s: int):

they are all larger.

combination:

continue

1 t.append(candidates[j])

3 t.pop()

constructed.

3 dfs(0, target)

Example Walkthrough

2 dfs(j + 1, s - candidates[j])

3. Condition to Add to the Answer: Inside the dfs function, we check if the remaining sum s is zero, meaning we found a valid

combination that sums to the target. In that case, we add a copy of the current combination to the answer list.

1 if s == 0: ans.append(t[:])

index in the candidates list) and s (the remaining sum needed to reach the target).

- 4. Base Cases for Termination: We return if the index i moves beyond the length of the candidates or if the remaining sum s is less than the current candidate, which means we can't reach the desired total with the current and subsequent candidates since

duplicates in our answer list (since we've already considered this value in the previous steps).

return 5. Loop Over the Candidates: Starting from the current index to the end of candidates, we try to include the candidate in the

1 for j in range(i, len(candidates)):

1 if i >= len(candidates) or s < candidates[i]:</pre>

if j > i and candidates[j] == candidates[j - 1]:

how each part of the code contributes to the solution:

7. Backtracking: After including a candidate, the dfs function is called recursively with the updated index (j+1) and the updated remaining sum (s - candidates[j]). After this recursive call, we backtrack by removing the last candidate from the combination and moving on to the next candidate.

The solution utilizes a list ans to store all the unique combinations and a temporary list to store the current combination being

The DFS and backtracking continue until all possible combinations that meet the criteria have been explored, after which ans is

This approach efficiently explores all possible combinations and prunes the search space to avoid duplicates and unnecessary

6. Skipping Duplicates: Before including a candidate in the combination, we skip over it if it's the same as its predecessor to avoid

After defining dfs, the solution begins the search with: 1 ans = []

returned, containing all the valid combinations.

searches, thereby finding the solution set in an optimal manner.

4. On the first iteration, j is 0, and the candidate is 1.

to get [1, 2, 2] and call dfs(3, 0).

by the included candidate's value (5 - 1 = 4).

Let's assume our candidates array is [2, 5, 2, 1, 2], and our target is 5.

2. The dfs function starts with i as 0 (the first index) and the target sum s as 5.

3. We enter a loop that will iterate through the candidates starting from index 0.

Following the solution approach: 1. First, we **sort** the candidates to [1, 2, 2, 2, 5].

 We include 2 to make our combination [1, 2] and call dfs(2, 2). 6. The function dfs(2, 2) again finds the candidate 2 at index 2.

7. Since the remaning sum s is 0 (dfs(3, 0)), we've found a valid combination which sums to the target. So we add [1, 2, 2] to

5. The function dfs(1, 4) starts and enters a loop starting at index 1; the first candidate it considers is 2.

• We include 1 in our temporary combination t and call dfs(1, 4), which moves to the next index and decrements the target

However, this time j is not greater than i, which means it's the first occurrence of this candidate in the loop, so we include 2

o The loop in dfs(2, 2) continues with the next j as 3, but the candidate 2 at index 3 is a duplicate. Thus, we skip it and continue to j as 4. Since candidates [4] is 5, which is greater than our remaining sum 2, this does not lead to a valid

our answer list ans.

from typing import List

class Solution:

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};

return answer;

Typescript Solution

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38 # Example usage:

39 # sol = Solution()

5 public class Solution {

combination. So, we finish dfs(2, 2) without further action.

8. Now, we backtrack and the temporary combination t becomes [1, 2] again.

- 9. We continue backtracking to dfs(1, 4); t is now [1]. • The loop resumes with the next j, which is 2. But since candidates [2] is a duplicate of the previous candidate, we skip it and do the same for j as 3.
- However, this 2 is not considered as it is a duplicate of the previous candidate. 11. The next non-duplicate candidate is the 5 at j as 4.
- We include this 5 and call dfs(5, 0). Since the remaining sum s is 0, we've found another valid combination that sums to the target, so [5] is added to our answer list ans.

Finally, our dfs is done exploring all possibilities, and we have ans as [[1, 2, 2], [5]], which are the unique combinations that sum

• For j as 4, the candidate is 5, but adding 5 to [1] will exceed the remaining sum (4). So no further action is taken.

10. Finally, we backtrack to the very first dfs(0, 5), t is now [], and we continue to the next candidate, which is 2 at j as 1.

- to the target 5. Python Solution
- if current_sum == 0: combinations.append(combination[:]) 10 # If the index is out of bounds or the current element is larger than the current_sum, stop recursion 11

Iterate over the candidates starting from the current index

Add the current candidate to the current combination

Skip duplicates to avoid repeating the same combination

if i > start_index and candidates[i] == candidates[i - 1]:

If the current sum is 0, we found a valid combination

Helper function to perform depth-first search

for i in range(start_index, len(candidates)):

Sort the candidates to handle duplicates easily

This temp list will store the current combination

Return all unique combinations that add up to the target

41 # print(result) # Output would be a list of lists with all the unique combinations

This list will hold all unique combinations

def dfs(start_index: int, current_sum: int):

def combinationSum2(self, candidates: List[int], target: int) -> List[List[int]]:

if start_index >= len(candidates) or current_sum < candidates[start_index]:</pre>

combination.append(candidates[i]) 21 22 # Recursively call dfs with the next index and the remaining sum 23 dfs(i + 1, current_sum - candidates[i]) 24 # Backtrack by removing the last added candidate 25 combination.pop() 26

Start the depth-first search

40 # result = sol.combinationSum2([10,1,2,7,6,1,5], 8)

continue

return

candidates.sort()

combinations = []

combination = []

return combinations

dfs(0, target)

```
Java Solution
 1 import java.util.ArrayList;
2 import java.util.Arrays;
   import java.util.List;
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private List<List<Integer>> combinations = new ArrayList<>(); // List to hold the final combinations.

if (startIndex >= sortedCandidates.length || remainingSum < sortedCandidates[startIndex]) {</pre>

private int[] sortedCandidates; // Array to hold the input candidates after sorting.

// If the remaining sum is 0, the current combination is a valid combination.

if (i > startIndex && sortedCandidates[i] == sortedCandidates[i - 1]) {

// Method to find all possible unique combinations that add up to the target.

public List<List<Integer>> combinationSum2(int[] candidates, int target) {

return combinations; // Return the final list of combinations.

backtrack(0, target); // Begin the backtrack algorithm.

combinations.add(new ArrayList<>(combination));

// Iterate through the candidates starting from startIndex.

// Skip duplicates to avoid redundant combinations.

// Add the candidate to the current combination.

combination.add(sortedCandidates[i]);

for (int i = startIndex; i < sortedCandidates.length; ++i) {</pre>

// Backtrack method to find all valid combinations.

if (remainingSum == 0) {

continue;

return;

return;

private void backtrack(int startIndex, int remainingSum) {

private List<Integer> combination = new ArrayList<>(); // Temporary list to hold a single combination.

Arrays.sort(candidates); // Sort the array to handle duplicates and to make it easier to prune branches.

// If the startIndex is out of bounds or the smallest candidate is greater than the remainingSum, there are no valid combinat

sortedCandidates = candidates; // Storing the sorted array in an instance variable for easy access.

// Recursively call the method with the next index and the updated remaining sum. 38 39 backtrack(i + 1, remainingSum - sortedCandidates[i]); // Backtrack: remove the last added candidate to try other candidates. 40 combination.remove(combination.size() - 1); 41 42 43

```
C++ Solution
  1 class Solution {
    public:
         vector<vector<int>> combinationSum2(vector<int>& candidates, int target) {
             // Sort the candidate numbers to handle duplicates and ease the combination process.
             sort(candidates.begin(), candidates.end());
             // Initialize the answer vector that will hold all unique combinations.
  8
             vector<vector<int>> answer;
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             // Temporary vector to store individual combinations.
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             vector<int> temp;
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             // Define a recursive lambda function to perform deep-first search (DFS) for combinations.
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             // 'currentIndex' is the start index for exploring candidates,
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             // and 'currentSum' is the remaining sum we need to hit the target.
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             function<void(int, int)> dfs = [&](int currentIndex, int currentSum) {
                 // Base case: if remaining sum is zero, we found a valid combination.
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                 if (currentSum == 0) {
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                     answer.emplace_back(temp);
 19
 20
                     return;
 21
 22
                 // If out of bounds or the current number exceeds the remaining sum, backtrack.
 23
                 if (currentIndex >= candidates.size() || currentSum < candidates[currentIndex]) {</pre>
 24
                     return;
 25
 26
 27
                 // Iterate through the candidates starting from 'currentIndex'.
 28
                 for (int j = currentIndex; j < candidates.size(); ++j) {</pre>
 29
                     // Skip duplicates to guarantee uniqueness of combinations.
                     if (j > currentIndex && candidates[j] == candidates[j - 1]) {
 30
                         continue;
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                     // Choose candidate 'j' and go deeper into the recursion tree.
 34
                     temp.emplace_back(candidates[j]);
 35
 36
                     // Recurse with the next index and the new remaining sum.
 37
                     dfs(j + 1, currentSum - candidates[j]);
 38
 39
                     // Backtrack and remove the previously chosen candidate.
 40
                     temp.pop_back();
 41
             };
 42
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 44
             // Start the DFS process with index 0 and the target sum.
 45
             dfs(0, target);
 46
             // Return all unique combinations that add up to the target.
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```

1 // This function finds all unique combinations of candidates where the candidate numbers sum to target.

// If the startIndex is out of bounds or the smallest candidate exceeds the remainingSum

if (startIndex >= candidates.length || remainingSum < candidates[startIndex]) {</pre>

// Initialize the depth-first search with starting index 0 and the initial target sum

// First, sort the input candidates to simplify the process of skipping duplicates

// Add a copy of the current combination to the final results

// Skip duplicate elements to prevent duplicate combinations

if (i > startIndex && candidates[i] === candidates[i - 1]) {

2 // Each number in candidates may only be used once in the combination.

// Depth-first search function to explore all possibilities

const dfs = (startIndex: number, remainingSum: number) => {

combinations.push(tempCombination.slice());

// there's no need to continue exploring this path

// If remaining sum is zero, we found a valid combination

// Iterate over the candidates starting from the startIndex

// Return all unique combinations found that sum up to the target

for (let i = startIndex; i < candidates.length; i++) {</pre>

// Temporary array to store one potential combination

function combinationSum2(candidates: number[], target: number): number[][] {

// This will hold all the unique combinations that meet the target sum

// It returns a list of all unique combinations.

candidates.sort((a, b) => a - b);

if (remainingSum === 0) {

continue;

tempCombination.pop();

return;

return;

const combinations: number[][] = [];

const tempCombination: number[] = [];

30 31 // Include the current candidate in the temporary combination 32 tempCombination.push(candidates[i]); 33 // Continue exploring further with the next candidates and a reduced remaining sum 34 dfs(i + 1, remainingSum - candidates[i]); 35 // Backtrack and remove the last candidate from the combination

dfs(0, target);

return combinations;

Time and Space Complexity

to find all unique combinations that sum up to a given target.

exponential part is more dominant, we can approximate it as 0(2^n).

};

Time Complexity The time complexity of this code primarily depends on the depth of the recursion and the number of recursive calls made at each level.

1. The recursion depth is at most the target value if we choose candidates with a value of 1 every time. However, since the same

2. At every level of recursion, we iterate over the remaining candidates, so, in the worst case, the number of recursive calls can be

exponential in nature, implied by 0(2ⁿ), where n is the number of candidates. However, since we skip duplicates after sorting,

candidate cannot be used repeatedly, the recursion depth is constrained by the number of candidates in the worst case.

The provided Python code solves the combination sum problem where each number in the array candidates can only be used once

the number of branches in the recursion tree can be less than that. A more accurate bound is not straightforward because it depends on the candidates and the target value. The worst-case time

complexity, without considering duplicates, is $0(2^n)$, where n is the number of candidates. 3. The sorting operation at the start of the code takes 0(n*log(n)) time.

Space Complexity The space complexity of the code consists of:

Combining the sorting with the recursion leads to a worst-case time complexity of O(n*log(n) + 2^n). Considering that the

- 1. Space used by the recursion stack, which in the worst case is equivalent to the depth of recursion, at most 0(n) if all candidates are used.
 - 2. Space for the temporary list t, which stores the current combination, will at most contain n values, adding another 0(n). 3. Finally, the output list ans that could potentially hold all unique combinations of candidates. In the worst case, this could be all
- possible combinations which can be exponential, represented as O(2^n). Hence, the overall space complexity, considering the output space and the recursion stack depth, is 0(n + 2^n). Typically, the output space can be a separate consideration, and if we exclude it, the space complexity for computation is O(n). However, if we

include the space needed for the output, it would be 0(2^n) due to the possibility of storing all combinations.