1871. Jump Game VII String ] Medium Dynamic Programming Prefix Sum Sliding Window Leetcode Link

# **Problem Description** You are given a binary string s that is 0-indexed, which means indexing starts from 0. Your task is to determine if you can move from

the start position, index 0, to the last index of the binary string, s. length - 1, using a set of movement rules defined by two integers minJump and maxJump. The conditions for moving from index i to index j are as follows: You can only jump to index j from index i if i + minJump <= j <= min(i + maxJump, s.length - 1).</li>

- The destination index j must have a value of '0' in the binary string (s[j] == '0').
- You can only start your movement from index 0 if its value is '0', and you must end at the last index s.length 1. The goal is to return true if reaching the last index is possible under the given conditions, otherwise return false.

Intuition

## The essence of this problem is to find if there's a path from the beginning to the end of s while obeying the jump constraints. One intuitive approach to solve this problem will be using dynamic programming, where we calculate the possibility of reaching a

particular index based on the possibilities of reaching previous indices. The solution hinges on the following intuitions:

 We should track reachability from the start to each index with a boolean array dp where each index i of dp signifies whether it is possible to reach s[i]. • To efficiently determine if we can reach index i, we should use a prefix sum array pre\_sum to quickly calculate the number of

- reachable indices in the range [i max]ump, i min]ump] without iterating through all of them every time. • If any index j within the range [i - maxJump, i - minJump] is reachable (dp[j] == true) and s[i] == '0', then index i is also reachable.
- Thus, starting from index 0, we iteratively compute dp and pre\_sum until we reach the end of the array or until it's clear that the end is
- not reachable. The last element of the dp array gives us the answer to whether the end is reachable. Solution Approach

To implement the solution, we use dynamic programming combined with a prefix sum strategy. Here's a step-by-step breakdown of how the solution is composed:

First, initialize two arrays dp and pre\_sum with lengths equal to n and n + 1 respectively, where n is the length of the binary string

In this case, set dp[i] to True.

The key algorithms and data structures used in this approach are:

dp = [false, false, false, false, false, false]

s. The array dp will store boolean values indicating whether each index i is reachable from the start while pre\_sum stores the prefix sums of dp. Set dp [0] to True because we start from index 0 and it's already reachable by definition. Similarly, set pre\_sum[1] to 1 as we can reach the first element.

check if the current character s[i] is '0'. If it's not, we can't possibly jump to this index anyway, so we move on.

gives us the final answer. If it's True, that means the end of the string is reachable; otherwise, it is unreachable.

 If s[i] is '0', check if there's any reachable index within the window defined by the current index i minus minJump and maxJump. To do this quickly, we calculated the prefix sum up to index i - minJump and subtract it from the prefix sum up to index i maxJump. If the resulting value is greater than 0, it means there is at least one reachable '0' we can jump from within the bounds.

· Iterate through each character in the binary string starting from index 1 as we have already initialized index 0. On each iteration,

Update the prefix sum array pre\_sum accordingly by adding the value at dp[i] to the prefix sum up to index i.

Continue this process until you've gone through all characters of the binary string. The last element of the dp array, dp [n - 1],

 Dynamic Programming (DP): Used to store the reachability state of each index as we progress through the string. • Prefix Sum Array: Allows us to efficiently calculate the sum of elements in a range, which helps in quickly determining if a jump is possible without checking every individual index within the range each time.

By using the DP and Prefix Sum Array, we efficiently solve the problem by reusing the results of the sub-problems and avoiding

redundant calculations. This way, each i is checked only once, making the solution optimal in terms of time complexity.

minJump = 2 and maxJump = 3. Step 0: Initialization

Let's consider a small example to illustrate the solution. Suppose we have a binary string s = "0010110" and the given jump rules are

# We can start from index 0 since s[0] == '0', so dp[0] = true and pre\_sum[1] = 1. Step 1: Checking each index

Step 2: Final Result

The final dp and pre\_sum look like this:

• pre\_sum = [0, 0, 0, 0, 0, 0, 0, 0]

Example Walkthrough

• Index 2 → s[2] == '0' and it's within the minJump and maxJump from 0 (0 + 2 <= 2 <= 0 + 3). We find that pre\_sum[2 - 1 + 1]  $pre_sum[2-3+1] = pre_sum[2] - pre_sum[0] = 1-0 = 1 > 0$ , indicating that a previous index is reachable. So, dp[2] =true and pre\_sum[3] = pre\_sum[2] + dp[2] = 1 + 1 = 2.

Index 1 → s[1] == '0', but index 1 cannot be reached directly from 0 as minJump > 1, so dp[1] is not changed.

Index 3 → s[3] == '1', so it can't be reached because the position does not contain '0'.

 $dp[6] = true and pre_sum[7] = pre_sum[6] + dp[6] = 2 + 1 = 3.$ 

given rules. Thus, the function should return true for this test case.

def canReach(self, arr: str, min\_jump: int, max\_jump: int) -> bool:

# A dynamic programming list to keep track of the possibility to reach each index

# Prefix sum array to keep track of number of reachable points in the string up to index i

# We only need to consider '0' positions since '1' positions are not reachable

# If the sum of reachable points between the bounds is greater than 0,

// within the range in the prefix sum array to jump to current position.

if (right >= left && prefixSum[right + 1] - prefixSum[left] > 0) {

// Update the prefix sum array with the sum up to the current position.

// Mark the current position as reachable.

prefixSum[i + 1] = prefixSum[i] + (isReachable[i] ? 1 : 0);

\* Function to determine if it's possible to reach the end of a string by jumping

\* Each jump can only be made if the destination is a '0' character in the string.

// Iterate through the string to fill the DP array with reachable positions

// Check if the current position is '0' and can potentially be jumped to

\* @param s The string representing safe ('0') and unsafe ('1') positions.

\* @return boolean indicating whether the end of the string can be reached.

// Return if the last position in the string is reachable.

isReachable[i] = true;

\* between the positions specified by min\_jump and max\_jump.

14 bool canReach(const std::string& s, int min\_jump, int max\_jump) {

\* @param min\_jump The minimum length of a jump.

\* @param max\_jump The maximum length of a jump.

prefix\_sum[1] = 1; // Initialize prefix sum

for (int i = 1; i < n; i++) {

return isReachable[length - 1];

left\_bound = max(0, i - max\_jump) # Lower bound for the jump

dp = [true, false, true, false, true, false, true]

# Length of the input string

can\_reach = [False] \* length

 $prefix_sum = [0] * (length + 1)$ 

for i in range(1, length):

if arr[i] == '0':

# The starting point is always reachable

# Calculate the range of jumps

can\_reach[i] = True

right\_bound = i - min\_jump

# then the current point is reachable

length = len(arr)

can\_reach[0] = True

 Index 4 → s[4] == '0'. We can jump from both indices 1 and 2 to 4. However, since dp[1] is false and dp[2] is true, we only consider the 2 index. Again, we find that  $pre_sum[4-2+1] - pre_sum[4-3+1] = pre_sum[3] - pre_sum[2] = 2-1=1$ > 0, so dp[4] = true and pre\_sum[5] = pre\_sum[4] + dp[4] = 2 + 1 = 3. Index 5 → s[5] == '1', so it's not reachable. • Index 6 → s[6] == '0'. It's reachable from index 3, 4 with minJump and maxJump rules. But since dp[3] is false, we only consider

the 4. Checking the pre\_sum, pre\_sum[6 - 2 + 1] - pre\_sum[6 - 3 + 1] = pre\_sum[5] - pre\_sum[4] = 3 - 2 = 1 > 0, so

• Checking the last element in dp array, dp[6] = true. This indicates that it's indeed possible to jump to the last index using the

• pre\_sum = [0, 1, 1, 2, 2, 3, 3, 3] We've successfully found a path that allows us to travel from index 0 to index 6, thereby adhering to the solution approach and confirming the possibility to reach the end index.

### 14 15 # Initially only the first point is reachable $prefix_sum[1] = 1$ 16 # Loop through each point in the string

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Python Solution

class Solution:

```
# Update the prefix sum array with the reachability of the current index
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               prefix_sum[i + 1] = prefix_sum[i] + int(can_reach[i])
33
34
           # Check if the last point is reachable, return the result
35
           return can_reach[length - 1]
36
Java Solution
   class Solution {
       public boolean canReach(String s, int minJump, int maxJump) {
           // Get the length of the input string.
           int length = s.length();
           // Create a dynamic programming (dp) array to hold the reachability of each position.
           boolean[] isReachable = new boolean[length];
           // Always start at position 0.
10
           isReachable[0] = true;
11
12
           // Use a prefix sum array to keep a running sum of reachable positions.
13
           int[] prefixSum = new int[length + 1];
           prefixSum[1] = 1;
14
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16
           // Iterate through the string starting at position 1 since we're always starting at position 0.
17
           for (int i = 1; i < length; ++i) {
               // Check if the current position has a '0' and therefore can be landed on.
19
               if (s.charAt(i) == '0') {
                   // Calculate the maximum left (furthest back we can jump from current position).
20
                   int left = Math.max(0, i - maxJump);
22
                   // Calculate the minimum right (closest jump we can make to current position).
23
                   int right = i - minJump;
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25
                   // Ensure that right is not less than left and that there is at least one true
```

# Upper bound for the jump

if right\_bound >= left\_bound and prefix\_sum[right\_bound + 1] - prefix\_sum[left\_bound] > 0:

#### int n = s.length(); // Length of the string std::vector<int> dp(n, 0); // DP array to store whether a position is reachable 16 std::vector<int> prefix\_sum(n + 1, 0); // Array to store the prefix sum of the DP 17 18 dp[0] = 1; // Starting position is always reachable 19

C++ Solution

1 #include <vector>

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#include <string>

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if (s[i] == '0') {
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               int left_bound = std::max(0, i - max_jump); // Left boundary for the window from which we can jump
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27
               int right_bound = i - min_jump; // Right boundary for the window from which we can jump
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               // If there is at least one reachable position within the window, mark the current position as reachable
30
               if (left_bound <= right_bound && prefix_sum[right_bound + 1] - prefix_sum[left_bound] > 0) {
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                   dp[i] = 1;
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           // Update the prefix sum array with the current reachability status
35
           prefix_sum[i + 1] = prefix_sum[i] + dp[i];
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       // Return if the last position is reachable
39
       return dp[n-1] == 1;
40 }
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   // Example usage:
43 /*
44 int main() {
       bool result = canReach("011010", 2, 3);
45
       std::cout << (result ? "true" : "false") << std::endl; // Expected output: true or false
46
       return 0;
47
48 }
49 */
50
Typescript Solution
  1 // Function to determine if it's possible to reach the end of a string by jumping
  2 // between the positions specified by minJump and maxJump.
  3 // Each jump can only be made if the destination is a '0' character in the string.
  4 /**
     * @param s The string representing safe(0) and unsafe(1) positions.
     * @param minJump The minimum length of a jump.
      * @param maxJump The maximum length of a jump.
     * @returns boolean indicating whether the end of the string can be reached.
     */
  9
 10 const canReach = (s: string, minJump: number, maxJump: number): boolean => {
         const n: number = s.length; // Length of the string
 11
         let dp: number[] = new Array(n).fill(0); // DP array to store whether a position is reachable
 12
 13
         let prefixSum: number[] = new Array(n + 1).fill(0); // Array to store the prefix sum of the DP
 14
 15
         dp[0] = 1; // Starting position is always reachable
 16
         prefixSum[1] = 1; // Initialize prefix sum
 17
 18
         // Iterate through the string to fill the DP array with reachable positions
 19
         for (let i = 1; i < n; i++) {
 20
             // Check if the current position is '0' and can potentially be jumped to
 21
             if (s.charAt(i) === '0') {
 22
                 let leftBound = Math.max(0, i - maxJump); // Left boundary for the window from which we can jump
 23
                 let rightBound = i - minJump; // Right boundary for the window from which we can jump
 24
 25
                 // If there is at least one reachable position within the window, mark current position as reachable
 26
                 if (leftBound <= rightBound && prefixSum[rightBound + 1] - prefixSum[leftBound] > 0) {
 27
                     dp[i] = 1;
 28
 29
 30
             // Update the prefix sum array with current reachability status
```

### 37 38 // Example usage: // const result: boolean = canReach("011010", 2, 3); // console.log(result); // Expected output: true or false

return dp[n - 1] === 1;

Time and Space Complexity

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prefixSum[i + 1] = prefixSum[i] + dp[i];

// Return if the last position is reachable

The given Python code implements a dynamic programming solution to determine if it is possible to reach the end of a string given certain jumping rules.

# 1. Initialization of the dp and pre\_sum arrays with False and 0 respectively, which takes O(n) time each, where n is the length of the input string. 2. A single for-loop on the index i ranges from 1 to n-1, resulting in 0(n) iterations.

Space Complexity

space complexity.

time.

**Time Complexity** 

3. Inside the for-loop, the check  $pre_sum[r + 1] - pre_sum[l] > 0$  is a constant time operation, O(1), as it involves accessing elements of the prefix sum array and subtraction. 4. The update of the pre\_sum array with pre\_sum[i + 1] = pre\_sum[i] + dp[i] is also a constant time operation, executed once

The time complexity of the algorithm can be analyzed based on loop operations and array manipulations:

- each loop iteration. Combining these observations, the overall time complexity can be considered as O(n) because the for-loop dominates the execution
- The space complexity is determined by the space required to store the dynamic programming states and additional constructs: 1. The dp array that stores Boolean values representing if a position i can be reached, has a size of n, contributing 0(n) to the

2. The pre\_sum array helps keep track of the prefix sums of dp, also requiring O(n) space. Hence, the overall space complexity of this solution is O(n), which is a sum of space used by dp and pre\_sum.

In conclusion, the given code has a time complexity of O(n) and a space complexity of O(n).