### 1124. Longest Well-Performing Interval

Medium Hash Table **Prefix Sum Monotonic Stack Array** 

#### **Problem Description**

The problem presents us with an array called hours which represents the number of hours worked by an employee each day. Our goal is to find the length of the longest interval of days where there are more "tiring days" than "non-tiring days". A "tiring day" is defined as any day where the employee works more than 8 hours. We need to understand the interval dynamics where the "wellperforming intervals" are those having a greater count of tiring days compared to non-tiring days. The challenge lies in finding the maximum length of such an interval.

Intuition

solved efficiently using a prefix sum and a hash map. The intuition here is to designate tiring days as a positive contribution (+1) and non-tiring days as a negative contribution (-1) to the sum. As we iterate over the array: • We keep a running sum (s), which is increased by 1 for tiring days and decreased by 1 for non-tiring days. • If at any point, the running sum is positive, it means there are more tiring days than non-tiring days so far, so we update the answer to the

The solution to this problem uses an interesting approach akin to finding the longest subarray with a positive sum, which can be

- current length of days (i + 1).
- If the running sum is not positive, we look to see if there is a previous running sum (s 1). If it exists, then the subarray between the day when s - 1 was the running sum and the current day is a "well-performing interval". We then update our answer if this interval is longer than our
- current longest interval. • To efficiently find these previous running sums, we use a hash map (pos) that records the earliest day that each running sum occurred. This way, we only store the first occurrence of each sum since we want the longest possible interval.
- This approach relies on the idea that if we find a running sum that is greater than a past running sum, then there must have been more tiring days than non-tiring days in between those two points. The efficiency of this solution comes from the fact that we traverse the list only once and access/update the hash map in constant time.

**Solution Approach** 

The solution uses a hash map and a running sum to efficiently track well-performing intervals. Here's the detailed breakdown of

### Initialize variables:

how the approach is implemented:

 ans tracks the length of the longest well-performing interval found so far and initializes to 0. s is our running sum, which helps determine if an interval is well-performing.

- Iterate over the hours array using enumerate to have both index i and value x for each day.
  - Update the running sum s:

pos is a hash map recording the first occurrence of each running sum.

Subtract 1 from s if x is not greater than 8 (non-tiring day).

Here's a step-by-step walkthrough using the solution approach:

update pos[1] either as it already exists.

After updating the running sum:

 $\circ$  Add 1 to s if x > 8 (tiring day).

Update the hash map pos:

current day i, which is a well-performing interval. Hence, we calculate the length of this interval (i - pos[s - 1]) and update ans if it's longer than the current ans.

 $\circ$  If s > 0, it means we've encountered more tiring days than non-tiring days up to day i, so update ans to i + 1.

corresponding earlier sum would allow for a well-performing interval to exist between it and the current day.

o If the current running sum s has not been seen before, record its first occurrence (pos[s] = i). We only update the first occurrence because we're interested in the longest interval. The code uses pos to remember the earliest day an intermediate sum occurs. By checking if s - 1 is in pos, we can infer if a

∘ If s <= 0, we look for s - 1 in pos. If it's found, it indicates there's an interval starting right after the first occurrence of s - 1 up to the

where n is the number of days. The space complexity is also O(n) due to storing the sum indices in the hash map, possibly equal to the number of days if all running sums are unique.

Using this pattern allows us to efficiently process each day in constant time, resulting in an overall time complexity of O(n),

we need to find the length of the longest well-performing interval: hours = [9, 9, 6, 0, 6, 6, 9]

Let's consider a small example using the solution approach described above. Suppose we have the following hours array where

#### We initialize our variables: ans to 0, s to 0, and pos as an empty hash map.

5.

days 0 and 1 (inclusive).

def longest wpi(self, hours) -> int:

sum\_indices = {}

 $\max$  length = cumulative sum =  $\emptyset$ 

if cumulative sum > 0:

**Example Walkthrough** 

We start iterating through hours with the values and their indices: o Day 0 (i=0, x=9): It's a tiring day because x > 8. We add 1 to s, making it 1. Since s > 0, we update ans s = 1 + 1 = 1. The hash map pos is updated with pos[1] = 0 because we haven't seen this sum before.

o Day 2 (i=2, x=6): A non-tiring day, so we subtract 1 from s, making it 1 again. Since s is still positive, we don't update ans, but we don't

○ Day 5 (i=5, x=6): Non-tiring, s goes to -2. We check for s - 1 which is -3 in pos, but it's not found. ans stays the same and pos[-2] =

```
○ Day 3 (i=3, x=0): Non-tiring, subtract 1 from s to 0. ans remains unchanged, and we add pos[0] = 3 to the hash map.
○ Day 4 (i=4, x=6): Non-tiring, subtract 1 from s to -1. Since s <= 0, we check for s - 1 which is -2 in pos, but it's not there. No update to
  ans and we set pos[-1] = 4.
```

○ Day 6 (i=6, x=9): Tiring, we add 1 to s, bringing it up to -1. We check for s - 1 which is -2 in pos and find it at position 5. We calculate the interval length i - pos[-2] = 6 - 5 = 1. Since this does not exceed our current maximum of ans = 2, we do not update ans.

o Day 1 (i=1, x=9): Another tiring day. We increment s to 2. ans is updated to i + 1 = 2 and pos[2] = 1.

Therefore, the answer for this given hours array is 2. Solution Implementation

The iteration is now complete. The longest well-performing interval we found has a length of 2, which occurred between

# Iterate through each hour in the list for index, hour in enumerate(hours): # Increment or decrement the cumulative sum based on the hour's value cumulative\_sum += 1 if hour > 8 else -1

 $max_length = index + 1$ 

# from the beginning up to the current index

if cumulative sum - 1 in sum indices:

# Initialize the maximum length of well-performing interval and sum so far

# Initialize a dictionary to store the earliest index of a particular cumulative sum

# If the cumulative sum is positive, we found a well-performing interval

# If this sum has not been seen before, map it to the current index

# If cumulative sum - 1 is in the sum indices, it means we previously had a smaller sum

max\_length = max(max\_length, index - sum\_indices[cumulative\_sum - 1])

return longestSequence; // Return the length of the longest well-performing sequence found.

int longestInterval = 0: // Variable to store the length of the longest interval found

unordered\_map<int, int> firstOccurrence; // Map to store the first occurrence of a score

// If the score is positive, we've found a well-performing interval from the start

// Check if there's a previous score that is one less than the current score

longestInterval = max(longestInterval, i - firstOccurrence[score - 1]);

longestInterval = i + 1; // Update the longest interval length

// Record the first occurrence of a score if it hasn't already been recorded

// Update the longest interval found if necessary

# Initialize the maximum length of well-performing interval and sum so far

# Increment or decrement the cumulative sum based on the hour's value

# If the cumulative sum is positive, we found a well-performing interval

# If this sum has not been seen before, map it to the current index

# If cumulative sum - 1 is in the sum indices, it means we previously had a smaller sum

max\_length = max(max\_length, index - sum\_indices[cumulative\_sum - 1])

# By finding the length from that index to the current index, we ensure a positive hour count

# We only want to record the first occurrence of a cumulative sum to achieve the longest interval

# Initialize a dictionary to store the earliest index of a particular cumulative sum

// Increase the score for well-performing days (hours > 8), decrease for non-well-performing days

// If the score becomes non-positive, try to find a well-performing interval in the middle

// Function to find the length of the longest well-performing interval

if (first0ccurrence.count(score - 1)) {

if (!first0ccurrence.count(score)) {

# By finding the length from that index to the current index, we ensure a positive hour count

## else:

**Python** 

class Solution:

```
# We only want to record the first occurrence of a cumulative sum to achieve the longest interval
                if cumulative sum not in sum indices:
                    sum_indices[cumulative_sum] = index
        # The resulting max_length is the length of the longest well-performing interval
        return max_length
Java
class Solution {
    public int longestWPI(int[] hours) {
        int longestSequence = 0; // This will hold the final result, length of the longest well-performing interval.
        int score = 0; // This tracks the current score indicating the balance of hours (tiring vs. non-tiring).
        Map<Integer, Integer> scoreToIndexMap = new HashMap<>(); // Mapping from scores to their first occurrence index.
        // Iterate over the input array.
        for (int i = 0; i < hours.length; ++i) {</pre>
            // If the number of hours worked is more than 8 in a day, increment score, otherwise decrement.
            score += hours[i] > 8 ? 1 : -1;
            // If the current score is positive, it means there is a well-performing interval from 0 to i-th day.
            if (score > 0) {
                longestSequence = i + 1; // Update the length of the longest sequence.
            } else {
                // If there's a previous score that is one less than the current score...
                if (scoreToIndexMap.containsKey(score - 1)) {
                    // ... then there's a well-performing interval from that previous score's index to the current index i.
                    longestSequence = Math.max(longestSequence, i - scoreToIndexMap.get(score - 1));
                // Store the current score's first occurrence index if it's not already stored.
                // This means for any score, we save the earliest index at which the score occurred.
                scoreToIndexMap.putIfAbsent(score, i);
```

// A score to determine well-performing days vs. non-well-performing days

C++

public:

#include <vector>

class Solution {

using namespace std;

#include <unordered map>

int longestWPI(vector<int>& hours) {

int score = 0;

**if** (score > 0) {

} else {

// Iterate over the hours array

for (int i = 0; i < hours.size(); ++i) {</pre>

score += hours[i] > 8 ? 1 : -1;

```
first0ccurrence[score] = i;
        return longestInterval; // Return the length of the longest well-performing interval found
};
TypeScript
// Import necessary libraries from JavaScript/TypeScript (no include statement needed in TypeScript)
// The typing for unordered_map in TypeScript would use a Map or Record
// Define the function to find the longest well-performing interval
function longestWPI(hours: number[]): number {
    let longestInterval: number = 0; // Variable to store the length of the longest interval found
    let score: number = 0; // A score to determine well-performing days vs non-well-performing days
    let firstOccurrence: Map<number, number> = new Map(); // Map to store the first occurrence of a score
    // Iterate over the hours array
    for (let i = 0; i < hours.length; ++i) {</pre>
        // Increase score for well-performing days (hours > 8), decrease for non-well-performing days
        score += hours[i] > 8 ? 1 : -1;
        // If the score is positive, a well-performing interval from the start has been found
        if (score > 0) {
            longestInterval = i + 1; // Update the longest interval length
        } else {
            // If the score is non-positive, try to find a well-performing interval in the middle
            // Check if there's a previous score that is one less than the current score
            if (firstOccurrence.has(score - 1)) {
                // Update the longest interval found if necessary
                longestInterval = Math.max(longestInterval, i - (firstOccurrence.get(score - 1) as number));
        // Record the first occurrence of a score if it hasn't already been recorded
        if (!firstOccurrence.has(score)) {
            firstOccurrence.set(score, i);
    return longestInterval; // Return the length of the longest well-performing interval found
```

#### # The resulting max\_length is the length of the longest well-performing interval return max length Time and Space Complexity

# **Time Complexity**

class Solution:

def longest wpi(self, hours) -> int:

sum\_indices = {}

else:

max length = cumulative sum = 0

if cumulative sum > 0:

# Iterate through each hour in the list

 $max_length = index + 1$ 

cumulative\_sum += 1 if hour > 8 else -1

# from the beginning up to the current index

if cumulative sum - 1 in sum indices:

if cumulative sum not in sum indices:

sum\_indices[cumulative\_sum] = index

for index, hour in enumerate(hours):

The given Python function longestWPI exhibits a time complexity of O(N), where N represents the length of the input list hours. This is due to the fact that the function iterates through the list exactly once. During each iteration, it performs a constant amount of work: updating the sum s, checking conditions, and updating the pos dictionary or ans as needed.

# **Space Complexity**

The space complexity of the function is also O(N). The post dictionary is the primary consumer of space in this case, which in the worst-case scenario might need to store an entry for every distinct sum s encountered during the iteration through hours. In a worst-case scenario where every value of s is unique, the dictionary's size could grow linearly with respect to N, the number of elements in hours.