## 461. Hamming Distance



### **Problem Description**

The task is to calculate the Hamming distance between two integers. The Hamming distance is simply the number of positions at which the corresponding bits of the two numbers differ. For example, if we have two numbers, say 1 (01 in binary) and 4 (100 in binary), their Hamming distance is 2 because they differ at two positions: the first and third bits (when looking at the binary representation from right to left with leading zeros taken into account for aligning the bit patterns).

This is a problem that deals with bit manipulation, a common topic in computer science that focuses on operations directly on binary digits or bits of the number.

#### Intuition

The solution uses a bitwise XOR operation to determine the different bits between the two provided integers (x and y). The XOR operation, represented by the caret symbol ^, compares two bits and results in 1 if they are different and 0 if they are the same. For example:

```
• 0 ^ 0 = 0
1 ^ 0 = 1
```

0 ^ 1 = 1

1 ^ 1 = 0

Therefore, by performing x ^ y, we get a number whose binary representation has 1s in all the positions where the binary representation of x and y differ. To count the number of 1s in the binary representation of the result (which represents the Hamming distance), we use the

bit\_count() method which efficiently counts the number of set bits in the integer.

**Solution Approach** 

## The solution to finding the Hamming distance between two integers involves a single line of code in Python, primarily making use

of a bitwise operation and a built-in method. As a first step, we calculate the XOR (^) of the two numbers x and y. In Python, the XOR operation is applied using the ^ symbol

between the two numbers: xor\_result = x ^ y

same. This binary representation is the keystone for finding the Hamming distance. Next, we count the number of 1s within this bit pattern to determine the Hamming distance. This can be done through iterating

The xor\_result carries a bit pattern where each bit is 1 if the corresponding bits of x and y are different, and 0 if they are the

over each bit and adding to a count if the bit is 1, a process that would take O(n) time, where n is the number of bits in the numbers. However, Python provides the .bit\_count() method to do this in a more performant manner, taking advantage of the underlying hardware's ability to count set bits more efficiently. The method is directly applied to the XOR result: hamming\_distance = xor\_result.bit\_count()

This hamming\_distance is the number of positions where x and y have different bits, i.e., the Hamming distance. The .bit\_count()

method returns the number of set bits (bits with value 1) in the integer, which is what our XOR result highlights - differing bits. In summary, the algorithm makes use of the bitwise XOR to highlight differences and then applies a bit count to quantify these

differences. This approach is efficient as it utilizes a single bitwise operation followed by a specialized count operation, both of which are very fast on modern hardware.

## Let's walk through a small example to illustrate the solution approach, considering the calculation of the Hamming distance

**Example Walkthrough** 

between two integers, say 10 and 15. Firstly, we must understand the binary representations of these integers.

• The binary representation of 10 is 1010. • The binary representation of 15 is 1111.

- Following the outlined solution approach, we start by calculating the XOR of 10 and 15.
- x = 10 # 1010 in binary y = 15 # `1111` in binary

xor\_result = x ^ y

```
Performing the XOR operation, we get:
```

• 1111 (binary for 15)

bits), thus finding the Hamming distance.

• 0101 (result of XOR operation)

• 1010 (binary for 10)

Next, we use the .bit\_count() method on the XOR result to count the number of 1s in the binary representation (the differing

hamming\_distance = xor\_result.bit\_count()

Therefore, the Hamming distance between the integers 10 (1010) and 15 (1111) is 2.

// Integer.bitCount method counts the number of one-bits in the XOR result.

// Return the count of differing bits as the Hamming Distance

// Function to calculate the Hamming distance between two integers.

// This count represents the number of differing bits, which is the Hamming Distance.

Now, xor\_result will hold the value 0101 in binary, which is 5 in decimal.

The bit\_count() method will count the number of 1s in the binary number 0101 which is 2.

In summary, through a simple XOR operation followed by using \_bit\_count() on the result, we efficiently arrived at the Hamming distance between two integers, showcasing the power of bit manipulation and built-in methods.

# **Python**

return count;

def hammingDistance(self, x: int, y: int) -> int:

int count = Integer.bitCount(xorResult);

\* @param  $\{number\} x - The first integer to compare.$ 

\* @param {number} y - The second integer to compare.

\* @return {number} The Hamming distance between x and y.

function hammingDistance(x: number, y: number): number {

Solution Implementation

```
# XOR the two numbers to find the bits that are different
xor = x ^ y
# Convert the result to a binary string and count the number of '1's
```

class Solution:

```
# The count of '1's is equal to the Hamming distance
       return bin(xor).count('1')
Java
class Solution {
   // Method to calculate the Hamming Distance between two integers.
   public int hammingDistance(int x, int y) {
       // Use XOR to find differing bits between x and y
       int xorResult = x ^ y;
```

C++

public:

class Solution {

```
int hammingDistance(int x, int y) {
       // Xor operation between x and y will set the bits that are different to 1.
       int xorValue = x ^ y;
       // __builtin_popcount function counts the number of set bits(1s) in the integer.
       // This gives us the number of different bits, which is the Hamming distance.
       int count = __builtin_popcount(xorValue);
       // Return the Hamming distance.
       return count;
};
TypeScript
/**
* Calculates the Hamming distance between two numbers.
* The Hamming distance is the number of positions at which
 * the corresponding bits are different.
```

```
// Perform bitwise XOR operation on x and y.
// This will set the bits in x to 1 wherever x and y differ.
x ^= y;
```

```
// Initialize answer to store the total count of differing bits.
      let distanceCount = 0;
      // Count the number of bits set to 1.
      while (x) {
         // Remove the rightmost bit set to 1 from x. The expression (x \& -x)
         // isolates the rightmost bit set to 1, and subtracting it from x
         // removes that bit.
         x = x \& -x;
         // Increment the count of differing bits.
         distanceCount++;
      // Return the total count of differing bits, which is the Hamming distance.
      return distanceCount;
class Solution:
   def hammingDistance(self, x: int, y: int) -> int:
       # XOR the two numbers to find the bits that are different
       xor = x ^ y
       # Convert the result to a binary string and count the number of '1's
       # The count of '1's is equal to the Hamming distance
       return bin(xor).count('1')
Time and Space Complexity
  The time complexity of the hammingDistance function is primarily dependent on the number of bits in the binary representation of
```

time on most modern computers. However, counting the number of bits set to 1 — which is essentially what bit\_count() does varies depending on the number of bits set to 1 after the XOR operation. In the worst case, where all bits are different, this would be O(n), where n is the number of bits required to represent the numbers in the system. Nevertheless, since the size of integers is fixed in Python (usually 32 or 64 bits), the overall time complexity can be considered 0(1) as well.

the numbers x and y. The XOR operation x ^ y itself takes 0(1) time since integer operations are typically performed in constant

The space complexity of the code is 0(1) because the space required for the computation does not increase with the size of the inputs. The only space needed is for the temporary storage of the XOR result and its bit count, which is a constant number of memory cells regardless of the input size.