436. Find Right Interval Medium Array Binary Search Sorting

Problem Description

intervals[i] represents an interval with a start_i and an end_i, we need to identify for each interval i another interval j where the interval j starts at or after the end of interval i, and among all such possible j, it starts the earliest. This means that the start of interval j (start_j) must be greater than or equal to the end of interval i (end_i), and we want the smallest such start_j. If there is no such interval j that meets these criteria, the corresponding index should be -1. The challenge is to write a function that returns an array of indices of the right intervals for each interval. If an interval has no right

The goal of this problem is to find the "right interval" for a given set of intervals. Given an array intervals, where each element

interval, as mentioned -1 will be the placeholder for that interval. Intuition

To approach this problem, we utilize a binary search strategy to efficiently find the right interval for each entry. Here's how we arrive at the solution:

1. To make it possible to return indices, we augment each interval with its original index in the intervals array. 2. We then sort the augmented intervals according to the starting points. The sort operation allows us to apply binary search later

- since binary search requires a sorted sequence. 3. Prepare an answer array filled with -1 to assume initially that there is no right interval for each interval.
- 4. For each interval, use binary search (bisect_left) to efficiently find the least starting interval j that is greater than or equal to the end of the current interval i.
- 6. After completing the search for all intervals, the answer array is returned.
- Implementing binary search reduces the complexity of finding the right interval from a brute-force search which would be O(n^2) to O(n log n) since each binary search operation takes O(log n) and we perform it for each of the n intervals.

5. If the binary search finds such an interval, update the answer array at index i with the index of the found interval j.

Solution Approach

1. Augment Intervals with Indices: First, we update each interval to include its original index. This is achieved by iterating through

the intervals array and appending the index to each interval.

1 for i, v in enumerate(intervals): v.append(i)

The solution to this problem involves the following steps, which implement a binary search algorithm:

- 2. Sort Intervals by Start Times: We then sort the augmented intervals based on their start times. This allows us to leverage binary search later on since it requires the list to be sorted.
- 1 intervals.sort()

1 for _, e, i in intervals: 2 j = bisect_left(intervals, [e])

ans[i] = intervals[j][2]

array. This array is then returned as the final answer.

to -1, which indicates that initially, we assume there is no right interval for any interval. 1 ans = [-1] * n

4. Binary Search for Right Intervals: For each interval in intervals, we perform a binary search to find the minimum start_j value

that is greater than or equal to end_i. To do this, we use the bisect_left method from the bisect module. It returns the index at

3. Initialize Answer Array: We prepare an answer array, ans, with the same length as the intervals array and initialize all its values

- which the end_i value could be inserted to maintain the sorted order.
- 5. Updating the Answer: If the binary search returns an index less than the number of intervals (n), it means we have found a right interval. We then update the ans[i] with the original index of the identified right interval, which is stored at intervals[j][2]. 1 if j < n:

6. Return the Final Array: After the loop, the ans array is populated with the indices of right intervals for each interval in the given

- 1 return ans
- search, we're able to significantly reduce the number of comparisons needed to find the right interval from linear (checking each possibility one by one) to logarithmic, thus enhancing the performance of the solution.

Let's walk through this approach with a small example. Consider the list of intervals intervals = [[1,2], [3,4], [2,3], [4,5]].

This approach efficiently uses binary search to minimize the time complexity. The key to binary search is the sorted nature of the

intervals after they are augmented with their original indices. By maintaining a sorted list of start times and employing binary

1 augmented_intervals = [[1, 2, 0], [3, 4, 1], [2, 3, 2], [4, 5, 3]]

First, we augment each interval with its index.

2. Next, we sort the augmented intervals by their start times. 1 sorted_intervals = [[1, 2, 0], [2, 3, 2], [3, 4, 1], [4, 5, 3]]

3. We initialize the answer array with all elements set to -1.

1 ans = [-1, -1, -1, -1]

For interval [1, 2, 0]:

(interval [2, 3, 2]).

Thus, the right interval index is 2.

Example Walkthrough

o The end time is 2. The binary search tries to find the minimum index where 2 could be inserted to maintain the sorted order, which is index 1

The binary search finds index 2 (interval [3, 4, 1]).

The binary search finds index 3 (interval [4, 5, 3]).

For interval [2, 3, 2]: • The end time is 3.

4. Now, using a binary search, we look for the right interval for each interval in sorted_intervals.

 The right interval index is 1. For interval [3, 4, 1]:

The right interval index is 3.

1 ans = [2, 1, 3, -1]

from bisect import bisect_left

intervals.sort()

return answer

n = len(intervals)

from typing import List

class Solution:

12

20

21

22

23

24

43

44

10

11

12

13

14

15

16

17

18

19

20

21

22

23

24

25

26

27

29

30

31

32

32

33

35

36

39

40

41

});

C++ Solution

1 class Solution {

2 public:

• The end time is 4.

5. After performing the binary search for all intervals, we update the answer array with the right intervals' indices.

1, 3, -1], indicating that the interval [1,2] is followed by [2,3], [3,4] follows [2,3], and [4,5] follows [3,4]. The last interval,

For interval [4, 5, 3]: The end time is 5, and there's no interval starting after 5.

There's no right interval, so the value remains -1.

[4,5], has no following interval that satisfies the conditions.

Append the original index to each interval

for index, interval in enumerate(intervals):

Sort intervals based on their start times

public int[] findRightInterval(int[][] intervals) {

List<int[]> startIndexPairs = new ArrayList<>();

vector<int> findRightInterval(vector<vector<int>>& intervals) {

vector<pair<int, int>> startWithIndexPairs;

for (const auto& interval : intervals) {

for (int i = 0; i < n; ++i) {

while (left < right) {

vector<int> result;

else

int n = intervals.size(); // The total number of intervals

// Emplace back will construct the pair in-place

// Iterate over each interval to find the right interval

int left = 0, right = n - 1; // Binary search bounds

if (startWithIndexPairs[mid].first >= end)

int end = interval[1]; // The end of the current interval

// Perform a binary search to find the least start >= end

startWithIndexPairs.emplace_back(intervals[i][0], i);

sort(startWithIndexPairs.begin(), startWithIndexPairs.end());

// Vector of pairs to hold the start of each interval and its index

// Sort the startWithIndexPairs array based on the interval starts

// This will hold the result; for each interval the index of the right interval

int mid = (left + right) / 2; // This avoids the overflow that (l+r)>>1 might cause

right = mid; // We have found a candidate, try to find an earlier one

left = mid + 1; // Not a valid candidate, look further to the right

// Check if the found interval starts at or after the end of the current interval

int numIntervals = intervals.length;

interval.append(index)

if right_index < n:</pre>

6. The ans array, which keeps track of the right interval for each interval, is returned as the final answer. In our example, this is [2,

The binary search returns an index of 4, which is outside the array bounds.

Python Solution

def findRightInterval(self, intervals: List[List[int]]) -> List[int]:

answer = [-1] * n # Initialize the answer list with -1

answer[original_index] = intervals[right_index][2]

// This list will hold the start points and their corresponding indices

This approach efficiently finds the right intervals for each given interval with reduced time complexity.

Iterate through the sorted intervals for _, end, original_index in intervals: # Find the leftmost interval starting after the current interval's end 17 right_index = bisect_left(intervals, [end]) 18 # If such an interval exists, update the corresponding position in answer 19

Java Solution

1 class Solution {

```
// Populate the list with the start points and their indices
            for (int i = 0; i < numIntervals; ++i) {</pre>
                startIndexPairs.add(new int[] {intervals[i][0], i});
9
10
11
12
           // Sort the startIndexPairs based on the start points in ascending order
13
            startIndexPairs.sort(Comparator.comparingInt(a -> a[0]));
14
15
           // Prepare an array to store the result
            int[] result = new int[numIntervals];
16
17
           // Initialize an index for placing interval results
18
19
            int resultIndex = 0;
20
21
           // Loop through each interval to find the right interval
22
            for (int[] interval : intervals) {
23
                int left = 0, right = numIntervals - 1;
24
                int intervalEnd = interval[1];
25
26
               // Binary search to find the minimum start point >= interval's end point
27
               while (left < right) {</pre>
28
                    int mid = (left + right) / 2;
29
                    if (startIndexPairs.get(mid)[0] >= intervalEnd) {
30
                        right = mid;
                    } else {
31
32
                        left = mid + 1;
33
34
35
36
               // Check if the found start point is valid and set the result accordingly
37
                result[resultIndex++] = startIndexPairs.get(left)[0] < intervalEnd ? -1 : startIndexPairs.get(left)[1];
38
39
40
           // Return the populated result array
            return result;
41
42
```

// If not, append -1 to indicate there is no right interval 33 34 35 36

```
int index = (startWithIndexPairs[left].first >= end) ? startWithIndexPairs[left].second : -1;
                result.push_back(index);
37
38
            return result; // Return the populated result vector
39
40 };
41
Typescript Solution
   function findRightInterval(intervals: number[][]): number[] {
       // Get the total number of intervals
       const intervalCount = intervals.length;
       // Create an array to store the start points and their original indices
       const startPoints = Array.from({ length: intervalCount }, () => new Array<number>(2));
       // Fill the startPoints array with start points and their original indices
8
       for (let i = 0; i < intervalCount; i++) {</pre>
            startPoints[i][0] = intervals[i][0]; // Start point of interval
                                                 // Original index
            startPoints[i][1] = i;
11
12
13
       // Sort the array of start points in ascending order
14
       startPoints.sort((a, b) \Rightarrow a[0] - b[0]);
15
16
       // Map each interval to the index of the interval with the closest start point that is greater than or equal to the end point of
17
       return intervals.map(([_, end]) => {
18
            let left = 0;
19
            let right = intervalCount;
20
           // Binary search to find the right interval
           while (left < right) {</pre>
23
24
                const mid = (left + right) >>> 1; // Equivalent to Math.floor((left + right) / 2)
25
                if (startPoints[mid][0] < end) {</pre>
                    left = mid + 1;
26
                } else {
                    right = mid;
29
30
31
```

Time and Space Complexity

if (left >= intervalCount) {

return startPoints[left][1];

// Return the original index of the found interval

return -1;

The time complexity of the provided code consists of two major operations: sorting the intervals list and performing binary search using bisect_left for each interval.

1. Sorting the intervals list using the sort method has a time complexity of O(n log n), where n is the number of intervals.

2. Iterating over each interval and performing a binary search using bisect_left has a time complexity of O(n log n) since the

- Thus, the combined time complexity of these operations would be $0(n \log n + n \log n)$. However, since both terms have the same order of growth, the time complexity simplifies to $O(n \log n)$.
- The space complexity of the code is O(n) for the following reasons: 1. The intervals list is expanded to include the original index position of each interval, but the overall space required is still linearly
- proportional to the number of intervals n. 2. The ans list is created to store the result for each interval, which requires O(n) space.

// If left is out of bounds, return -1 to indicate no such interval was found

binary search operation is $O(\log n)$ and it is executed n times, once for each interval.

3. Apart from the two lists mentioned above, no additional space that scales with the size of the input is used. Therefore, the total space complexity is O(n).