1838. Frequency of the Most Frequent Element

Greedy Array Binary Search Prefix Sum Sorting Sliding Window

### **Problem Description**

Medium

Intuition

You are given an integer array nums and an integer k. The task is to find the maximum frequency of any element in nums after you're allowed to increment any element by 1 up to k times. The frequency of an element is how many times that element appears in the array. The objective is to find the highest possible frequency of any number in the array after making at most k increments in total.

The intuition behind the solution is to first sort the array. By doing this, we can then use a sliding window to check each subarray and calculate how many operations we would need to make all elements in the subarray equal to the rightmost element.

Starting with the smallest elements on the left, we work towards the right. For each position r (right end of the window), we

position r. This is done by multiplying the difference between nums[r] and nums[r - 1] by r - 1 (size of the current window minus one). If the total operations required exceed k, we shrink the window from the left by increasing 1, subtracting the necessary operations as we go to keep the window valid (total operations less than or equal to k). Meanwhile, we're always keeping track of

calculate the number of operations needed to raise all elements from 1 (left end of the window) to r to the value of the element at

the maximum window size we're able to achieve without exceeding k operations, as this directly corresponds to the maximum frequency. The solution uses a two-pointer technique to maintain the window, expanding and shrinking it as needed while traversing the sorted array only once, which gives an efficient time complexity.

The algorithm implemented in the given solution follows a <u>sliding window</u> approach using two pointers, 1 and r, which represent the left and right ends of the window, respectively. The fundamental data structure used here is the list (nums), which is sorted to

### Sort the Array: The array nums is sorted to allow comparing adjacent elements and to use the sliding window technique effectively.

facilitate the sliding window logic. Here is a step-by-step breakdown:

ans = 1 # A single element has at least a frequency of 1.

Solution Approach

nums.sort() Initialize Pointers and Variables: Three variables are initialized: l (left pointer) which starts at 0.

- r (right pointer) which starts at 1 since the window should at least contain one element to make comparisons. ans which keeps track of the maximum frequency found. window which holds the total number of operations performed in the current window. l, r, window = 0, 1, 0
- **Expand the Window**: The algorithm enters a loop that continues until the right pointer r reaches the end of the array.
  - while r < len(nums):</pre>

frequency ans if the current window size (r - 1) is greater than the previous maximum.

Shrink the Window: If window exceeds k, meaning we cannot increment the elements of the current window to match nums [r] with the allowed number of operations, move 1 to the right to reduce the size of the window until window is within the limit

again.

r += 1

while window > k:

the value of nums[r].

window += (nums[r] - nums[r - 1]) \* (r - 1)

window -= nums[r] - nums[l] l += 1 Update Maximum Frequency: After adjusting the window to ensure we do not exceed k operations, update the maximum

**Return the Result**: Once we have finished iterating through the array with the right pointer r, the ans variable holds the

The sliding window technique coupled with the sorted nature of the array allows for an efficient solution. This technique avoids

recalculating the increment operations for each window from scratch; instead, it updates the number of operations incrementally

Calculate Operations: In each iteration, calculate the operations needed to increment all numbers in the current window to

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maximum frequency that can be achieved, and we return it.
return ans
```

as the window expands or shrinks.

Suppose we have an array nums = [1, 2, 3] and k = 3.

First, we sort nums, which in this case is already sorted: [1, 2, 3].

Initialize the pointers and variables: l = 0, r = 1, window = 0, and ans = 1.

ans = max(ans, r - l)

Example Walkthrough Let's consider a small example to illustrate the solution approach in action:

Since window  $\leq$  k, we do not need to shrink the window. We then update ans with the new window size, which is r - 1. ans

Putting it all together, we found that after incrementing the elements optimally, we can have at least two elements with the same

value in the array [1, 2, 3] by using at most 3 increments (for example: incrementing 1 and 2 to make the array [3, 3, 3]).

Enter the loop. nums[r] is 2, and nums[l] is 1. window becomes (2 - 1) \* (1 - 0) = 1. •

 $= \max(1, 1 - 0) = 1.$ 

Increment r and it becomes 2.

Thus, the maximum frequency is 2.

Solution Implementation

from typing import List

nums.sort()

while right < n:</pre>

left, right, n = 0, 1, len(nums)

max\_freq, cumulative\_diff = 1, 0

while cumulative\_diff > k:

max\_freq = max(max\_freq, right - left)

# print(sol.maxFrequency([1,2,4], 5)) # Expected output: 3

int maxFrequency(std::vector<int>& nums, int k) {

// Initialize variables: n is the size of the vector,

// 'window' represents the total increments needed to make

// Using two pointers technique: l -> left, r -> right.

// element nums[right] to the value of nums[right - 1].

maxFrequency = std::max(maxFrequency, right - left + 1);

for (int left = 0, right = 1; right < n; ++right) {</pre>

window -= (nums[right] - nums[left]);

cumulative\_diff -= nums[right] - nums[left]

The class and method could be tested with a simple test case as follows:

elements that can be made equal by applying up to k operations.

Therefore, the overall time complexity of the code is  $O(n \log n)$ .

one direction and can move at most n times, so it also contributes to O(n) operations.

max\_freq = max(max\_freq, right - left)

# print(sol.maxFrequency([1,2,4], 5)) # Expected output: 3

# Move the right pointer to the next element in the list.

# Update the maximum frequency using the current window size.

# Return the maximum frequency achievable with total operations  $\leq k$ .

left += 1

right += 1

return max\_freq

Time and Space Complexity

// all elements in the current window equal to the current maximum element.

// Update the 'window' with the cost of bringing the newly included

// If the total increments exceed k, shrink the window from the left.

// Calculate max frequency by finding the maximum window size till now.

window += 1LL \* (nums[right] - nums[right - 1]) \* (right - left);

// Beginning with the second element as there's nothing to the left of the first.

std::sort(nums.begin(), nums.end());

// ans will hold the maximum frequency.

// Sort the given vector.

int n = nums.size();

int maxFrequency = 1;

long long window = 0;

while (window > k) {

// Return the maximum frequency found.

left++;

return maxFrequency;

#### Next iteration, nums [2] is 3. We calculate operations needed: window += (3 - 2) \* (2 - 0) = 1 + 2 = 3. •

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Return ans. So the maximum frequency after k increments is 2. •

Increment r and it becomes 3. Since r is now equal to len(nums), the loop ends.

Again, window  $\leq$  k, so we do not shrink the window. Update ans = max(1, 2 - 0) = 2.

**Python** 

# Increase the total difference by the difference between the current right element

# and its predecessor multiplied by the number of elements in the current window.

class Solution: def maxFrequency(self, nums: List[int], k: int) -> int: # Sort the input list in non-decreasing order.

# Initialize two pointers for sliding window and the variables needed.

cumulative\_diff += (nums[right] - nums[right - 1]) \* (right - left)

# Update the maximum frequency using the current window size.

# Return the maximum frequency achievable with total operations  $\leq k$ .

# The class and method could be tested with a simple test case as follows:

# If the cumulative differences exceed k, shrink the window from the left.

# Iterate with right pointer over the list to expand the window.

cumulative\_diff -= nums[right] - nums[left] left += 1 # Move the right pointer to the next element in the list.

right += 1

return max\_freq

# sol = Solution()

#include <vector>

class Solution {

public:

#include <algorithm>

Java

```
class Solution {
   // Function to find the maximum frequency of an element after performing operations
   public int maxFrequency(int[] nums, int k) {
       // Sort the array to group similar elements together
       Arrays.sort(nums);
       int n = nums.length; // Store the length of the array for iteration
       int maxFreq = 1;  // Initialize max frequency as 1 (at least one number is always there)
        int operationsSum = 0; // This will hold the sum of operations used at any point
       // Start with two pointers:
       // 'left' at 0 for the start of the window,
       // 'right' at 1, since we'll start calculating from the second element
       for (int left = 0, right = 1; right < n; ++right) {</pre>
           // Calculate the total operations done to make all elements from 'left' to 'right' equal to nums[right]
           operationsSum += (nums[right] - nums[right - 1]) * (right - left);
           // If the total operations exceed k, shrink the window from the left
           while (operationsSum > k) {
               operationsSum -= (nums[right] - nums[left++]);
           // Calculate the max frequency based on the window size and update it if necessary
           maxFreq = Math.max(maxFreq, right - left + 1);
       // Return the maximum frequency
       return maxFreq;
C++
```

```
};
```

**TypeScript** 

```
function maxFrequency(nums: number[], k: number): number {
      // Sort the array
      nums.sort((a, b) => a - b);
      // Initialize the answer with a single element frequency
      let maxFrequency = 1;
      // Initialize a variable to keep track of the total sum that needs to be added to make all elements equal during a window sli
      let windowSum = 0;
      // Get the count of elements in the array
      let n = nums.length;
      // Initialize two pointers for our sliding window technique
      for (let left = 0, right = 1; right < n; right++) {</pre>
          // Update the window sum by adding the cost of making the right-most element equal to the current right-most element
          windowSum += (nums[right] - nums[right - 1]) * (right - left);
          // Shrink the window from the left if the cost exceeds the value of k
          while (windowSum > k) {
              windowSum -= nums[right] - nums[left];
              left++;
          // Update the maximum frequency with the current window size if it's greater
          maxFrequency = Math.max(maxFrequency, right - left + 1);
      // Return the maximum frequency achieved
      return maxFrequency;
from typing import List
class Solution:
   def maxFrequency(self, nums: List[int], k: int) -> int:
       # Sort the input list in non-decreasing order.
       nums.sort()
       # Initialize two pointers for sliding window and the variables needed.
        left, right, n = 0, 1, len(nums)
        max_freq, cumulative_diff = 1, 0
       # Iterate with right pointer over the list to expand the window.
       while right < n:</pre>
           # Increase the total difference by the difference between the current right element
            # and its predecessor multiplied by the number of elements in the current window.
            cumulative_diff += (nums[right] - nums[right - 1]) * (right - left)
           # If the cumulative differences exceed k, shrink the window from the left.
            while cumulative_diff > k:
```

# **Time Complexity**

sol = Solution()

• Sorting the list: Sorting takes O(n log n) time, where n is the number of elements in nums. • Two-pointer window iteration: The while loop iterates over the sorted list, adjusting the window of elements by incrementing the right pointer and potentially the left pointer. The right pointer makes only one pass over the list, resulting in O(n) operations. The left pointer moves only in

The provided code first sorts the nums list, and then uses a two-pointer approach to iterate over the list, adjusting the window of

Combining the sort and the two-pointer iteration results in a time complexity of 0(n log n + n), which simplifies to 0(n log n) since n log n dominates n for large n.

## The space complexity of the code depends on the space used to sort the list and the additional variables used for the algorithm.

**Space Complexity** 

• Sorting the list: The sort operation on the list is in-place; however, depending on the sorting algorithm implemented in Python (Timsort), the sorting can take up to O(n) space in the worst case. • Additional variables: The code uses a few additional variables (l, r, n, ans, window). These require constant space (0(1)).

Therefore, considering both the sorting and the additional variables, the space complexity of the code is O(n) in the worst case due to the sorting operation's space requirement.