# 1814. Count Nice Pairs in an Array

Medium Array Hash Table Math Counting

## Problem Description

You are given an array called `nums` which is filled with non-negative integers. The challenge is to find all pairs of indices `(i, j)` that meet a certain "nice" criterion. This criterion is defined by two conditions:

- The first condition is that the indices `i` and `j` must be different and `i` must be less than `j`.
- The second condition is that when you take the number at position `i` and add it to the reversal of the number at position `j`, this sum must be equal to the number at position `j` plus the reversal of the number at position `i`.

Now, because simply reversing a number isn't mathematically challenging, the real complexity of the problem lies in finding all such pairs efficiently. Since the number of nice pairs can be very large, you need to return the count modulo `10**9 + 7`, which is a common technique in programming contests to avoid dealing with extraordinarily large numbers.

## Intuition

Let's look at the condition provided in the problem - `nums[i] + rev(nums[j]) == nums[j] + rev(nums[i])`. If we play around with this equation a bit, we can rephrase it into `nums[i] - rev(nums[i]) == nums[j] - rev(nums[j])`. This observation is crucial because it allows us to switch from searching pairs to counting the frequency of unique values of `nums[i] - rev(nums[i])`.

The intuition behind the problem is to count how many numbers have the same value after performing the operation `number - reversed_number`. If a certain value occurs `k` times, any two unique indices with this value will form a nice pair. The number of unique pairs that can be formed from `k` numbers is given by the formula `k * (k - 1) / 2`.

We use a hash table (python's `Counter` class) to store the count of each `nums[i] - rev(nums[i])` value. Then, we calculate the sum of the combination counts for each unique `nums[i] - rev(nums[i])` value. The `Combination Formula` is used here to find the number of ways you can select pairs from a group of items.

Finally, remember to apply modulo `10**9 + 7` to our result to get the final answer.

## Solution Approach

The solution uses a clever transformation of the check for a nice pair of indices. Instead of directly checking whether `nums[i] + rev(nums[j]) == nums[j] + rev(nums[i])` for each pair, which would be time-consuming, it capitalizes on the insight that if two `nums[i]` have the same value after subtracting their reverse, `rev(nums[i])`, they can form a nice pair with any `nums[j]` that shows the same characteristic.

The following steps outline the implementation:

1. Define a `rev` function which, given an integer `x`, reverses its digits. This is accomplished by initializing `y` to zero, and then repeatedly taking the last digit of `x` by `x % 10`, adding it to `y`, and then removing the last digit from `x` using integer division by 10.
2. Iterate over all elements in `nums` and compute the transformed value `nums[i] - rev(nums[i])` for each element. We use a hash table to map each unique transformed value to the number of times it occurs in `nums`. In Python, this is efficiently done using the `Counter` class from the `collections` module.
3. Once the hash table is filled, iterate over the values in the hash table. For each value `v`, which represents the number of occurrences of a particular transformed value, calculate the number of nice pairs that can be formed with it using the combination formula `v * (v - 1) / 2`. This formula comes from combinatorics and gives the number of ways to choose 2 items from a set of `v` items without considering the order.
4. Sum these counts for each unique transformed value to get the total number of nice pairs. Because the count might be very large, the problem requires us to modulo the result by `10**9 + 7` to keep the result within the range of a 32-bit signed integer and to prevent overflow issues.

By transforming the problem and using a hash table to track frequencies of the transformed values, we turn an `O(n^2)` brute force solution into an `O(n)` solution, which is much more efficient and suitable for larger input sizes.

The code that accomplishes this:

```
class Solution:
    def countNicePairs(self, nums: List[int]) -> int:
        def rev(x):
            y = 0
            while x:
                y = y * 10 + x % 10
                x //= 10
            return y

        cnt = Counter(x - rev(x) for x in nums)
        mod = 10**9 + 7
        return sum(v * (v - 1) // 2 for v in cnt.values()) % mod
```

In the provided Python code, `rev` is the function that reverses an integer, and `Counter(x - rev(x) for x in nums)` creates the hash table mapping each `nums[i] - rev(nums[i])` to its frequency. The final summation and modulo operation provide the count of nice pairs as required.

### Example Walkthrough

Let's explain the solution using a small example. Suppose we have the following array:

```
nums = [42, 13, 20, 13]
```

We want to find the count of all "nice" pairs, which means for any two different indices `(i, j)` with `i < j`, the condition `nums[i] + rev(nums[j]) == nums[j] + rev(nums[i])` holds true. Following the steps defined in the solution:

1. **Define the reverse function**: This function reverses the digits of a given number. For example, `rev(42)` returns `24` and `rev(13)` returns `31`.
2. **Compute transformed values and frequency**:
   - For `nums[0] = 42`: `42 - rev(42) = 42 - 24 = 18`
   - For `nums[1] = 13`: `13 - rev(13) = 13 - 31 = -18`
   - For `nums[2] = 20`: `20 - rev(20) = 20 - 02 = 18`
   - For `nums[3] = 13` (again): `13 - rev(13) = 13 - 31 = -18`

   At this point, we notice that the transformed value `18` occurs twice and also `-18` occurs twice.
3. **Use a hash table to map transformed values to frequencies**:

   ```
   { 18: 2, -18: 2 }
   ```

4. **Calculate the number of nice pairs using combination formula**:
   - For `18`, the number of nice pairs is calculated as `2 * (2 - 1) / 2 = 1`
   - For `-18`, similarly, we calculate `2 * (2 - 1) / 2 = 1`
5. **Sum the counts and apply modulo**: We add up the counts from the previous step to get the total count of nice pairs. So, `1 + 1 = 2`. There's no need for the modulo operation in this small example as the result is already small enough.

Hence, the count of nice pairs in this example is `2`.

## Solution Implementation

### Python

```
from collections import Counter

class Solution:
    def countNicePairs(self, nums: List[int]) -> int:
        # Helper function to reverse the digits of a number
        def reverse_number(x: int) -> int:
            rev = 0
            while x > 0:
                rev = rev * 10 + x % 10  # Append the last digit of x to rev
                x //= 10  # Remove the last digit from x
            return rev

        # Create a counter to count the occurrences of differences between
        # each number and its reversed version
        difference_counter = Counter(x - reverse_number(x) for x in nums)

        # Define the modulus for the answer to prevent overflow
        mod = 10**9 + 7

        # Calculate the number of nice pairs using the formula:
        # k * (k - 1) // 2 for each count 'k' in the counter
        # The formula is derived from the combination formula C(n, 2) = n! / (2! * (n - 2)!)
        # which simplifies to n * (n - 1) / 2
        nice_pairs_count = sum(k * (k - 1) // 2 for k in difference_counter.values()) % mod

        # Return the total count of nice pairs modulo 10^9 + 7
        return nice_pairs_count
```

### Java

```
class Solution {
    public int countNicePairs(int[] nums) {
        // Create a HashMap to store the counts of each difference value
        Map<Integer, Integer> countMap = new HashMap<>();

        // Iterate through the array of numbers
        for (int number : nums) {
            // Calculate the difference between the number and its reverse
            int difference = number - reverse(number);
            // Update the count of the difference in the HashMap
            countMap.merge(difference, 1, Integer::sum);
        }

        // Define the modulo value to ensure the result fits within integer range
        final int mod = (int) 1e9 + 7;

        // Initialize the answer as a long to handle potential overflows
        long answer = 0;

        // Iterate through the values in the countMap
        for (int count : countMap.values()) {
            // Calculate the number of nice pairs and update the answer
            answer = (answer + (long) count * (count - 1) / 2) % mod;
        }

        // Cast the answer back to an integer before returning
        return (int) answer;
    }

    // Helper function to reverse a given integer
    private int reverse(int number) {
        // Set initial reversed number to 0
        int reversed = 0;

        // Loop to reverse the digits of the number
        while (number > 0) {
            // Append the last digit of number to reversed
            reversed = reversed * 10 + number % 10;
            // Remove the last digit from number
            number /= 10;
        }

        // Return the reversed integer
        return reversed;
    }
}
```

### C++

```
#include <vector>
#include <unordered_map>
using namespace std;

class Solution {
public:
    // Function to calculate the reverse of a given number
    int reverseNumber(int num) {
        int reversedNum = 0;
        // Iterate over the digits of the number
        while (num > 0) {
            reversedNum = reversedNum * 10 + num % 10; // Append the last digit to the reversedNum
            num /= 10; // Remove the last digit from num
        }
        return reversedNum;
    }

    // Function to count nice pairs in an array
    int countNicePairs(vector<int>& nums) {
        // Create a map to count occurrences of differences
        unordered_map<int, int> differenceCount;

        // Iterate over the given numbers
        for (int& num : nums) {
            // Calculate the difference between the number and its reverse
            int difference = num - reverseNumber(num);
            // Increase the count of the current difference
            differenceCount[difference]++;
        }

        long long answer = 0;
        const int mod = 1e9 + 7; // Use modulo to avoid integer overflow

        // Iterate through the map to calculate the pairs
        for (auto& kv : differenceCount) {
            int count = kv.second; // Extract the number of occurrences
            // Update the answer using the combination formula C(n, 2) = n! / (2! * (n - 2)!)
            // Simplifies to n * (n - 1) / 2
            answer = (answer + 1LL * (count - 1) / 2 % mod);
        }

        return answer; // Return the final count of nice pairs
    }
};
```

### TypeScript

```
function countNicePairs(nums: number[]): number {
    // Helper function to reverse the digits of a number
    const reverseNumber = (num: number): number => {
        let rev = 0;
        while (num) {
            rev = rev * 10 + (num % 10);
            num = Math.floor(num / 10);
        }
        return rev;
    };

    // Define the modulo constant to prevent overflow
    const mod = 1e9 + 7;
    // Map to store the count of each difference occurrence
    const countMap = new Map<number, number>();
    // Initialize the answer to be returned
    let answer = 0;

    // Loop through the array of numbers
    for (let i = 0; i < nums.length; ++i) {
        // Calculate the difference of the original and reversed number
        const difference = nums[i] - reverseNumber(nums[i]);
        // Update the answer with the current count of the difference
        // If the difference is not yet encountered, it treats the count as 0
        answer = (answer + (countMap.get(difference) ?? 0)) % mod;
        // Update the count of the current difference in the map
        countMap.set(difference, (countMap.get(difference) ?? 0) + 1);
    }

    // Return the final answer
    return answer;
}
```

```
from collections import Counter

class Solution:
    def countNicePairs(self, nums: List[int]) -> int:
        # Define a helper function to reverse the digits of a number
        def reverse_number(x: int) -> int:
            rev = 0
            while x > 0:
                rev = rev * 10 + x % 10  # Append the last digit of x to rev
                x //= 10  # Remove the last digit from x
            return rev

        # Create a counter to count the occurrences of differences between
        # each number and its reversed version
        difference_counter = Counter(x - reverse_number(x) for x in nums)

        # Define the modulus for the answer to prevent overflow
        mod = 10**9 + 7

        # Calculate the number of nice pairs using the formula:
        # k * (k - 1) // 2 for each count 'k' in the counter
        # The formula is derived from the combination formula C(n, 2) = n! / (2! * (n - 2)!)
        # which simplifies to n * (n - 1) / 2
        nice_pairs_count = sum(k * (k - 1) // 2 for k in difference_counter.values()) % mod

        # Return the total count of nice pairs modulo 10^9 + 7
        return nice_pairs_count
```

## Time and Space Complexity

### Time Complexity

The time complexity of the given code consists of two main operations:

1. Calculating the reverse of each number and constructing the counter object.
2. Summing up all pairs for each unique difference (value in the counter object).

The first operation depends on the number of digits for each integer in the `nums` list. Reversing an integer `x` is proportional to the number of digits in `x`, which is $O(\log M)$ where `M` is the value of the integer. Since we perform this operation for each element in the list, the time complexity of this part is $O(n * \log M)$.

The second operation involves iterating over each value in the counter object and calculating the number of nice pairs using the formula `v * (v - 1) // 2`. As there are at most `n` unique differences (in the case that no two numbers have the same difference), iterating over each value in the counter will be $O(n)$ in the worst case.

Hence, the overall time complexity is dominated by the first part, which is $O(n * \log M)$.

### Space Complexity

The space complexity is determined by the additional space used by the algorithm beyond the input size. In this case, it is the space used to store the counter object. The counter object could have as many as `n` entries (in the worst case where each number's difference after reversals is unique).

Therefore, the space complexity of the code is $O(n)$.