2368. Reachable Nodes With Restrictions Graph Medium Tree Depth-First Search Breadth-First Search Array

Leetcode Link

Problem Description In this problem, we are given an undirected tree with n nodes, where each node is labeled from 0 to n - 1. A 2D integer array edges is

this, we have an integer array restricted that lists restricted nodes which should not be visited. Our goal is to find the maximum number of nodes that can be reached from node 0 without visiting any of the restricted nodes. It's important to note that node 0 is not a restricted node.

provided that contains n - 1 pairs of integers, with each pair [ai, bi] indicating an edge between the nodes ai and bi. Alongside

Hash Table

The result should be the count of accessible nodes, including node 0, keeping in mind the restricted nodes' constraint.

To solve this problem, we use depth-first search (DFS), which is a standard graph traversal algorithm, to explore the graph starting

from node 0. The graph is represented using an adjacency list, which is a common way to represent graphs in memory.

Intuition

1. Constructing an adjacency list from the edges array, allowing us to access all connected nodes from a given node easily. 2. Creating a visited array, vis, to keep track of both visited and restricted nodes, marking restricted nodes as visited preemptively

3. Implementing a recursive DFS function that will traverse the graph. For each node u that is not visited and not restricted, the function will:

so that we don't traverse them during DFS.

The key steps involve:

- Increase the count of reachable nodes, ans, by 1. Mark the node as visited.
- Recursively call DFS for all adjacent nodes of u. When the DFS function completes, ans will contain the total count of reachable nodes from node 0, ensuring that no restricted nodes
- are counted. This approach guarantees that we explore all possible paths in a depth-first manner while skipping over the restricted nodes and only counting the valid ones.
- **Solution Approach**

The solution utilizes the Depth-First Search (DFS) algorithm to traverse the tree from node 0 and count the maximum number of

1. Data Structure: We use a defaultdict to create an adjacency list g that represents the graph. Each key in this dictionary

corresponds to a node, and the value is a list of nodes that are connected to it by an edge. This allows us to efficiently access all

reachable nodes without visiting any restricted nodes. Here's how the implementation works:

2. Pre-Marking Restricted Nodes: We create a list vis of boolean values to keep track of whether a node has been visited or is

neighbor nodes of any given node.

we check if u is already visited or not. If it hasn't been visited:

We increment the reachable nodes count ans by 1.

We mark u as visited by setting vis[u] to True.

us to solve the problem with a concise and effective approach.

Based on the edges, the tree structure looks like this:

Here, node 3 is restricted and should not be visited.

1 vis = [False, False, False, True, False]

Now, let's walk through the steps of the solution approach:

1 $g = \{0: [1, 2], 1: [0, 3, 4], 2: [0], 3: [1], 4: [1]\}$

The restricted list containing the nodes that cannot be visited is restricted = [3].

restricted. Its length is n to cover all nodes. Restricted nodes are preemptively marked as visited (i.e., True) since we don't want to include them in our count.

3. Graph Construction: For each edge provided in the edges array, we add the corresponding nodes to the adjacency list of each other. Since the graph represents an undirected tree, if there is an edge between a and b, then b needs to be in the adjacency list of a and vice versa.

4. DFS (Depth-First Search) Function: We define a recursive function dfs that takes a node u as an argument. Within this function,

• We then call dfs recursively for all the unvisited neighbor nodes of u found in the adjacency list g[u]. The use of recursion

track of the number of reachable nodes. We then call dfs(0) to start the traversal from node 0. 6. Result: After the DFS completes, ans gives us the total number of nodes that can be reached from node 0 without traversing any restricted nodes, and this value is returned.

In this way, the DFS algorithm, an efficient graph traversal technique, along with an adjacency list representation of the tree, allows

5. Initialization and Invocation: Before invoking the DFS function, we initialize the ans variable to 0, which will be used to keep

inherently follows a depth-first traversal, going as deep as possible along one branch before backtracking.

Example Walkthrough Let's take a small example to illustrate the solution approach described above.

Suppose we have 5 nodes (from 0 to 4) and n - 1 edges connecting them as follows: edges = [[0, 1], [0, 2], [1, 3], [1, 4]].

2. Pre-Marking Restricted Nodes: We then create a list vis initialized with False values. Since only node 3 is restricted, vis will be:

1. Data Structure: We use a defaultdict(list) to construct the adjacency list g representing the graph:

count = 1

0, 1, 2, and 4).

Python Solution

class Solution:

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C++ Solution

1 class Solution {

2 public:

from collections import defaultdict

graph = defaultdict(list)

graph[end].append(start)

nonlocal count_visited

if visited[node]:

count_visited += 1

visited[node] = True

dfs(adjacent)

count_visited = 0

Mark the node as visited

for adjacent in graph[node]:

// Graph represented as an adjacency list

// Counter to keep track of the number of reachable nodes

// Method to return the number of reachable nodes

// Array to keep track of visited nodes

private int numberOfReachableNodes;

private List<Integer>[] graph;

private boolean[] visited;

Initialize the count of reachable nodes

Recursively visit all adjacent nodes

return

visited = [False] * n

def dfs(node):

return count

for neigh in g[u]:

count += dfs(neigh)

Node 3 is marked True to indicate it's visited/restricted.

def dfs(u): if vis[u]: return 0 vis[u] = True

3. Graph Construction: Our graph g has already been constructed from the edges array in step 1.

4. DFS (Depth-First Search) Function: We write a recursive function dfs(u) that:

This function will count reachable nodes not previously counted nor restricted.

6. Result: We visit node 0, which isn't in the restricted list nor visited. So ans is now 1. The dfs goes on to visit nodes 1 and 2.

restricted nodes. This is consistent with our tree structure, taking into account the restrictions.

def reachableNodes(self, n: int, edges: List[List[int]], restricted: List[int]) -> int:

Create a graph represented as an adjacency list

A list to keep track of visited nodes, default to False

Depth-First Search (DFS) function to traverse the graph

Increase the count of visited (reachable) nodes

If the node is already visited or restricted, return

5. Initialization and Invocation: With ans = 0, we call dfs(0) and begin the DFS traversal.

9 # Mark restricted nodes as visited so they won't be traversed 10 for node in restricted: 12 visited[node] = True 13 14 # Construct the graph by adding edges 15 for start, end in edges: graph[start].append(end)

Node 1 has two children, 3 and 4, but since 3 is restricted, it only counts 4. After the complete DFS call, the ans value is 4 (nodes

In this example, the ans value after running the DFS algorithm implies we can reach 4 nodes from node 0 without visiting any

Start DFS from the first node 37 38 dfs(0) 39 # Return the number of reachable nodes 40 return count_visited 41

Java Solution

class Solution {

```
public int reachableNodes(int n, int[][] edges, int[] restricted) {
10
           // Initialize the graph for each node
           graph = new List[n];
12
            for (int i = 0; i < n; i++) {
13
                graph[i] = new ArrayList<>();
14
15
16
           // Mark restricted nodes as visited so they won't be explored in DFS
           visited = new boolean[n];
18
           for (int restrictedNode : restricted) {
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20
                visited[restrictedNode] = true;
21
22
           // Build the graph by adding edges
24
           for (int[] edge : edges) {
25
                int from = edge[0], to = edge[1];
26
                graph[from].add(to);
27
                graph[to].add(from);
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29
           // Initialize the count of reachable nodes and start DFS from node 0
30
           numberOfReachableNodes = 0;
31
32
           dfs(0);
33
34
           // Return the total count of reachable nodes
35
           return numberOfReachableNodes;
36
37
       // DFS method to traverse nodes
       private void dfs(int node) {
39
           // If the current node is visited/restricted, do not proceed with DFS
40
           if (visited[node]) {
                return;
43
44
           // Mark the node as visited and increment the reachable nodes counter
45
           numberOfReachableNodes++;
46
           visited[node] = true;
47
48
           // Visit all the neighbors of the current node
49
           for (int neighbor : graph[node]) {
50
51
                dfs(neighbor);
52
53
54 }
```

int nodeCount; // Use a more descriptive name for this variable, which represents the count of reachable nodes.

vector<vector<int>> graph(n); // Use 'graph' to store the adjacency list representation of the graph.

vector<bool> visited(n, false); // Use 'visited' to mark the visited nodes, initialized to false.

int reachableNodes(int n, vector<vector<int>>& edges, vector<int>& restricted) {

// Mark the restricted nodes as visited so they won't be counted.

void dfs(int node, vector<vector<int>>& graph, vector<bool>& visited) {

// Initialize the reachable node count to zero before starting the DFS.

// If the node has been visited or is restricted, return early.

function reachableNodes(n: number, edges: number[][], restricted: number[]): number {

adjacencyList.set(start, [...(adjacencyList.get(start) ?? []), end]);

adjacencyList.set(end, [...(adjacencyList.get(end) ?? []), start]);

// If the node has been visited or is restricted, stop the search

if (restricted.includes(currentNode) || visited[currentNode]) {

// Increment node count and mark the node as visited

// Iterate over all adjacent nodes and explore them

const adjacencyList = new Map<number, number[]>(); // Adjacency list to represent the graph

let nodeCount = 0; // Holds the count of nodes that can be reached

// Append the end node to the adjacency list of the start node

// Append the start node to the adjacency list of the end node

const visited = new Array(n).fill(false); // Tracks visited nodes

return nodeCount; // Return the count of reachable nodes after the DFS is complete.

// Construct the graph from the given edge list.

for (int node : restricted) visited[node] = true;

int from = edge[0], to = edge[1];

// Start depth-first search from node 0.

// Mark the current node as visited.

for (int neighbor : graph[node]) {

dfs(neighbor, graph, visited);

// Construct the adjacency list from the edges

// Depth-First Search function to explore the graph

for (const [start, end] of edges) {

const dfs = (currentNode: number) => {

visited[currentNode] = true;

return;

nodeCount++;

// Increment the count of reachable nodes.

// Iterate over all the neighbors of the current node.

// Perform DFS on all non-visited neighbors.

for (const auto& edge : edges) {

graph[from].push_back(to);

graph[to].push_back(from);

nodeCount = 0;

dfs(0, graph, visited);

if (visited[node]) {

visited[node] = true;

return;

nodeCount++;

Typescript Solution

```
25
           for (const neighbor of adjacencyList.get(currentNode) ?? []) {
26
              dfs(neighbor);
       };
29
30
       // Begin the Depth-First Search from node 0
       dfs(0);
31
32
       // Return the total number of nodes that can be reached
33
       return nodeCount;
34
36
Time and Space Complexity
The given Python code defines a Solution class with a method reachableNodes to count the number of nodes in an undirected graph
that can be reached without visiting any of the restricted nodes. It uses a Depth First Search (DFS) approach.
```

The time complexity of the code is primarily determined by the DFS traversal of the graph provided by edges. • The adjacency list for the graph is constructed in linear time relative to the number of edges. for a, b in edges loop runs |E|

times, where |E| is the number of edges.

Time Complexity

True).

Space Complexity

Each edge is traversed exactly twice in an undirected graph (once for each direction), during the entire DFS process.

Therefore, the time complexity of the DFS traversal is 0(|V| + |E|), where |V| is the number of vertices and |E| is the number of edges.

• The DFS (dfs function) visits each vertex only once, because once a vertex has been visited, it is marked as visited (vis[u] =

- Combining the adjacency list construction and the DFS traversal, the total time complexity remains 0(|V| + |E|) since both are dependent on the size of the graph.
- The space complexity is determined by:

• The storage of the graph in the adjacency list g, which consumes 0(|V| + |E|) space.

• The recursive DFS call stack, which, in the worst case, could hold all vertices if the graph is a linked list shape (each vertex connected to only one other), hence O(|V|) in space.

 The vis array, which takes 0(|V|) space, to keep track of visited nodes, including restricted ones. Summing this up, the space complexity is O(|V| + |E|) when considering both the adjacency list and the DFS stack.