

Intuition



Problem Description



The given problem presents us with an integer array nums. Our task is to find the sum of all divisors of each integer in nums that exactly have four divisors. To clarify, for an integer to qualify, it must have exactly four distinct divisors - including '1' and itself. If an integer in the array doesn't meet this criteria, it's not included in the sum. If there's no such integer in the array meeting the criteria, then the function should return 0.

To approach this problem, consider that an integer with exactly four divisors can only qualify if it's either a product of two distinct prime numbers or a cube of a prime number (since the cube will have divisors 1, the prime, the square of the prime, and the cube of the prime). Given this premise, our strategy is as follows:

For each element, try to find all its divisors.

if it has exactly four divisors, otherwise returns 0.

Iterate through every element of the input array nums.

- Keep a count of how many divisors we've found and simultaneously calculate their sum. If by the end, the count of divisors is exactly 4, add the sum of these divisors to our overall total.
- If it's not 4 divisors, disregard this integer and move to the next one.
- Repeat this process until we've checked all the integers in the array, and return the total sum.
- The provided solution code defines a nested function f(x) that calculates the sum of divisors of an integer x if it has exactly four

updated accordingly. Once all potential divisors are checked, the function returns either the sum of divisors, if there are exactly four, or 0 otherwise. This nested function is then applied to each element in nums with a generator expression that's passed to the sum function, rolling up the total sum of qualifying divisors. The concept of generators is efficient here since it avoids the need for an intermediate list to

divisors. This function uses a while loop to find divisors of x. For each divisor i found, the count is incremented and the sum is

hold values for divisors' sums, thus saving memory. **Solution Approach**

The solution implements a brute-force algorithm to find integers with exactly four divisors. Here's the step-by-step approach broken down:

1. A helper function f(x) is declared inside the Solution class, which takes an integer x as input and returns the sum of its divisors

- 2. Inside the function f(x), we initialize two variables: cnt to count the number of divisors (starting with 2, to account for '1' and x itself), and s to keep the sum of divisors (initialized to x + 1 for the same reason).
- 3. A while loop is used to iterate over possible divisors i, starting from 2 up to the square root of x. We use the square root as an optimization because if x is divisible by a number greater than its square root, the corresponding divisor (x // i) will already
- 4. For each i within the loop: \circ We check if i divides x entirely (x % i == 0). If it does, it means i is a divisor.

o If i is not a perfect square of x (to avoid counting the same divisor twice), we increment cnt again and add the

• The count of divisors cnt is incremented, and i is added to the sum s.

have been counted.

corresponding divisor (x // i) to the sum s.

sum() function. This expression calls function f(x) for every element x of the array nums.

- 5. After the loop, we check if the count of divisors cnt is exactly 4. If this condition holds true, the function returns the sum s, otherwise, it returns 0.
- 6. In the main function sumFourDivisors, we aggregate the results by using a generator expression f(x) for x in nums inside the
- 7. The sum() function calculates the cumulative sum of returned values by f(x) (sum of divisors for qualified integers) and returns it.
- A helper function to encapsulate the logic for evaluating individual numbers.

 A generator expression to handle the accumulation of sums in a memory-efficient manner. Optimization by checking divisibility only up to the square root of the number to reduce redundant calculations.

To reiterate, data structures and patterns used in this approach include:

- Example Walkthrough

• Standard mathematical operations (modulo %, integer division //, and square root) for divisor evaluation.

Let's consider an example array nums = [8, 10, 20] to illustrate the solution approach:

2. For x = 8, the function f(8) tries to find divisors. We know that 8 is a cube of the prime number 2, so its divisors are 1, 2, 4, and 8. Here the count of divisors is indeed 4. The sum of the divisors is 1 + 2 + 4 + 8 = 15. Since it has exactly four divisors, the

have exactly four divisors.

function f(8) will return 15.

3. For x = 10, the divisors are 1, 2, 5, and 10. Again, we have exactly four divisors. The sum is 1 + 2 + 5 + 10 = 18, and the

while divisor <= num // divisor:</pre>

count += 1

sum_of_divisors += divisor

if divisor * divisor != num:

sum_of_divisors += num // divisor

int divisorCount = 2; // Start with 2 divisors: 1 and the number itself

int divisorSum = 1 + number; // Sum of divisors starts with 1 and the number

count += 1

private int sumOfFourDivisors(int number) {

// Iterate to find other divisors

if (number % i == 0) {

++divisorCount;

// Otherwise, return 0

sumOfDivisors += i;

if (i * i != number) {

++divisorCount;

return divisorCount == 4 ? sumOfDivisors : 0;

sumOfDivisors += number / i;

// If the number has exactly four divisors, return the sum

for (int i = 2; i <= number / i; ++i) {</pre>

if (i * i != number) {

// Check if 'i' is a divisor of 'number'

divisorCount++; // Increase count of divisors

divisorSum += i; // Add 'i' to the sum of divisors

// Check if 'i' and 'number/i' are not the same divisor

divisorCount++; // If not, we have another divisor

// Check if the divisor is not the square root of the number

// This means the quotient is also a divisor

1. We start by applying the function f(x) to each element in nums.

- function f(10) returns 18. 4. For x = 20, the divisors are 1, 2, 4, 5, 10, and 20. There are more than four divisors, so the function f(20) does not meet the criteria and returns 0.
- 6. Therefore, the sumFourDivisors function will return 33, as it is the sum of all the divisors of integers within the array nums that

5. Finally, the sum of all sums returned by f(x) for each element in the array is calculated. This is 15 + 18 + 0 = 33.

- By using this step-by-step approach for each number in any given array nums, we can efficiently find the sum of the divisors for numbers with exactly four divisors.
- def sumFourDivisors(self, nums: List[int]) -> int: # Define a helper function to find if a number has exactly four divisors def sum_if_four_divisors(num: int) -> int: divisor = 2

count, sum_of_divisors = 2, num + 1 # start with 1 and 'num' as divisors

Check if the divisor and its counterpart are different

Iterate through potential divisors starting from 2 up to the square root of 'num'

if num % divisor == 0: 11 12

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Python Solution

1 class Solution:

```
divisor += 1
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               # If exactly 4 divisors have been found, return their sum, otherwise return 0
17
               return sum_of_divisors if count == 4 else 0
18
19
20
           # Sum the results of the helper function for each number in the input list 'nums'
           return sum(sum_if_four_divisors(num) for num in nums)
21
22
Java Solution
   class Solution {
       // Method to calculate the sum of all four divisors of the elements in the array.
       public int sumFourDivisors(int[] nums) {
           int sumTotal = 0; // Initialize the sum of the four divisors
           for (int number : nums) {
               sumTotal += sumOfFourDivisors(number); // Add the sum of the four divisors of the current number
           return sumTotal; // Return the total sum
11
12
       // Helper method to calculate the sum of four divisors of a single number.
```

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```
26
                       divisorSum += number / i; // Add 'number/i' to the sum of divisors
27
28
           // Return the sum of divisors only if exactly four divisors are found
32
           return divisorCount == 4 ? divisorSum : 0;
33
34 }
35
C++ Solution
 1 class Solution {
2 public:
       // Function to sum the divisors of each number in the given vector
       // that have exactly four distinct divisors.
       int sumFourDivisors(vector<int>& nums) {
           int totalSum = 0; // This will hold the sum of the divisors
           // Iterate through all numbers in the given vector
           for (int number : nums) {
                totalSum += sumDivisorsIfFour(number);
10
           return totalSum;
12
13
       // Helper function to calculate the sum of divisors of a number
14
       // if and only if it has exactly four distinct divisors.
       int sumDivisorsIfFour(int number) {
            int divisorCount = 2; // Start with 2 (1 and the number itself)
17
           int sumOfDivisors = number + 1; // Include 1 and the number in the sum
18
19
           // Iterate over possible divisors starting from 2 up to the square root of number
20
           for (int i = 2; i <= number / i; ++i) {</pre>
               if (number % i == 0) { // Check if i is a divisor
23
                   // Increment the divisor count and add it to the sum
```

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Typescript Solution
  * Function that returns the sum of four divisors for a single number
    * @param x The number to find the sum of its four divisors
    * @return The sum of the four divisors if there are exactly four, or 0 otherwise
    function sumOfDivisors(x: number): number {
       // Start with 2 divisors (1 and the number itself) and their sum
       let divisorCount = 2;
       let sumOfDivisors = x + 1;
       // Start from 2 to check for factors other than 1 and the number itself
11
       for (let i = 2; i * i <= x; ++i) {
12
           if (x % i === 0) {
13
14
               // If i is a divisor, increment count and add it to the sum
               ++divisorCount;
               sumOfDivisors += i;
16
17
               // If i is not a square root of x, account for the quotient as well
18
               if (i * i !== x) {
19
                   ++divisorCount;
20
                   sumOfDivisors += Math.floor(x / i);
23
24
25
       // If there are exactly 4 divisors, return the sum, otherwise, return 0
26
       return divisorCount === 4 ? sumOfDivisors : 0;
27
28 }
29
    * Function that finds the sum of all numbers in the input array that have exactly four divisors
    * @param nums Array of numbers
    * @return The sum of numbers with only four divisors from the input array
34
    */
   function sumFourDivisors(nums: number[]): number {
       let totalSum = 0;
36
       for (const num of nums) {
           // For each number, calculate the sum of its four divisors if any
           totalSum += sumOfDivisors(num);
       // Return the total sum for the array
```

Time and Space Complexity

of the sum of four divisors for each number within the list.

return totalSum;

input size is allocated.

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45 }

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The outer part of the code is a simple iteration through each number x in nums, which has a complexity of O(n), where n is the size of nums.

The time complexity of the solution is determined by two parts: the iteration through the list of numbers nums, and the computation

function iterates over potential divisors from 2 to sqrt(x). In the worst-case scenario, this runs in O(sqrt(x)) time, because the number of divisors up to the square root of x determines how many times the loop executes.

The total time complexity of this algorithm is a combination of the iteration through nums and the divisor function applied to each

The more complex part is the function f(x), which calculates the sum of the divisors for each number. The while loop within this

element. Therefore, the time complexity is 0(n * sqrt(x)), where x is the value of the largest number in nums. The space complexity of the provided code is 0(1). Other than a few variables for intermediate calculations, the space used does not depend on the input size. The cnt, s, i, and x variables are reused for each function call, and no extra space that scales with the