2808. Minimum Seconds to Equalize a Circular Array Medium Greedy Array

Hash Table

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Problem Description
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In this problem, we are given a 0-indexed array nums of n integers. The task is to make all elements in the array equal by performing a specific operation repeatedly. During each second, for every element at index i, you can update nums[i] to be equal to its current value, the value of the previous element (nums[(i - 1 + n) % n]), or the value of the next element (nums[(i + 1) % n]). The modulo operation ensures that you are wrapping around the array when reaching the ends, which means it actually forms a loop or ring. The goal is to find the minimum number of seconds needed to make all the elements in the array equal.

Intuition

The key to solving this problem lies in understanding that we can always make the entire array equal to any one of its current

values. This is because in each operation, you are allowed to choose the previous or next element's value, which can eventually

spread any number's occurrence across the array.

Since we want to minimize the number of seconds, the best strategy would be to choose the value that will take the least amount of time to spread through the array. Intuitively, if we have clusters of the same number occurring together, we would prefer to choose one such cluster's value and spread it to the rest of the array. The solution involves the following steps:

• We first group indices of identical elements into lists, using a dictionary where the keys are the array's values and the values are lists of indices where these numbers occur. • Then, for each group of identical elements:

○ We calculate the distance between the first and last occurrence of the value, taking into account the wrap-around using (idx[0] + n -

idx[-1]).

ends of a series.

- change the value between these two points using $\max(t, j i)$ for every pair of consecutive indices in the group.
- We also calculate the maximum distance between any two consecutive occurrences, as this will represent the maximum time required to • The time needed to make the entire array equal to this value is half the maximum distance found, since the value can spread from both
- array. Solution Approach

By applying this approach, we ensure that we pick the value that will take the least amount of time to replicate across the entire

The solution provided uses Python's defaultdict to categorize indices of identical elements into lists, and the inf constant from

the math module as a representation of infinity, which is employed to find the minimum value as we compare different distances. Here is the step-by-step breakdown of the implementation:

The minimum time across all such values is the final answer.

• A defaultdict of lists is instantiated. It will map each unique value in nums to a list of indices where it occurs. This is achieved by enumerating over nums and appending the index i to the list of d[x], where x is the value at index i.

• A variable ans is initialized to infinity (inf). This will hold the minimum number of seconds required to make all elements of the array equal.

∘ For each list of indices (idx), it calculates t, the distance considering wrap-around between the first and last occurrence: idx[0] + n -

• The algorithm then iterates over the values of the dictionary, which are the lists of indices for each distinct number in the array.

• It then proceeds to find the maximum distance between any two consecutive occurrences of the same number within the list. This is done using Python's pairwise function (Python 3.10+). If pairwise is not available, a simple zip like zip(idx, idx[1:]) can be used to achieve

idx[-1].

similar results.

Example Walkthrough

consecutive indices j - i. • Finally, because the value can spread from both ends towards the middle, only half this time is needed to make all elements between i and

• For every pair (i, j) of consecutive indices in idx, t is updated to the maximum of its current value and the distance between the

j equal, hence t // 2. • The algorithm updates ans with the minimum between its current value and t // 2. Since ans is initialized to infinity and we are finding the

minimum over all iterations, ans will hold the minimum time needed to make all elements equal after examining all distinct numbers.

• The function returns the value stored in ans. This approach effectively breaks down a seemingly complex problem into a series of calculations based on the distribution of

values across the array, using dictionary and list structures to organize data and a simple loop to compute the minimum time.

Let's illustrate the solution approach using a simple example: Given the array nums = [1, 2, 3, 2, 1], which is 0-indexed:

Step 1: We create a dictionary of list indices for each unique value in nums. In our case:

For value 1, the list of indices is [0, 4]. Since the array forms a loop:

For value 3, there is only one occurrence, no distance to calculate between indices.

• The distance considering wrap-around is (0 + 5 - 4) % 5 = 1.

• The value 1 occurs at indices [0, 4]. • The value 2 occurs at indices [1, 3]. • The value 3 occurs at index [2].

This would mean that no time is needed to make all the elements equal to 1 in this example, since we theoretically start

• There are no consecutive occurrences to calculate the maximum distance, so the maximum distance remains 1. ○ The time needed is 1 // 2 = 0 (since we can start from both ends, it needs no time to convert values in between).

Python

Step 2: Initialize ans to infinity.

For value 2, the indices are [1, 3]. No wrap-around is needed. \circ The maximum distance between consecutive occurrences is (3 - 1) = 2.

The time needed would be 2 // 2 = 1.

Step 4: Find the minimum ans:

from collections import defaultdict

Step 3: Evaluate each group of identical elements:

Step 5: Return the value in ans, which is 0.

• For value 1, and becomes the minimum of infinity and 0, which is 0.

For value 2, ans is the minimum of 0 and 1, which remains 0.

spreading the value from both ends of the occurrences.

for index. value in enumerate(nums):

for indices in index mapping.values():

for i in range(len(indices) - 1):

public int minimumSeconds(List<Integer> nums) {

minimum seconds = float('inf')

index_mapping[value].append(index)

Initialize the minimum seconds to infinity

Iterate over the indices for each unique number

time_spent = indices[0] + n - indices[-1]

• For value 3, no change as there is only one occurrence.

Solution Implementation

Populate index mapping with positions for every number in nums

Time spent is the distance between first and last occurrence

Iterate over pairs of indices to find max distance in between

Update time spent with the maximum gap found so far

Return the minimum seconds required to process all unique numbers

// Create a map to hold lists of indices for each unique number in 'nums'

Map<Integer, List<Integer>> indicesMap = new HashMap<>();

int n = nums.size(); // Total number of elements in the list

// Initialize the minimum number of seconds to a large value

int m = idx.size(); // Size of the index list

minSeconds = min(minSeconds, maxDistance / 2);

int maxDistance = idx[0] + n - idx[m - 1];

// Iterate over the number—index mapping

for (int i = 1; i < m; ++i) {

* @returns the minimum number of seconds required.

const indexMap: Map<number, number[]> = new Map();

// Variable to keep track of the minimum seconds needed

function minimumSeconds(nums: number[]): number {

return minSeconds;

const length = nums.length;

for (let i = 0; i < length; ++i) {

if (!indexMap.has(nums[i])) {

indexMap.get(nums[i])!.push(i);

indexMap.set(nums[i], []);

int minSeconds = INT_MAX; // use INT_MAX as shorthand for 1 << 30</pre>

vector<int>& idx = kv.second; // Get the vector of indices

for (auto& kv : indicesMap) { // Use 'kv' to represent key-value pairs

// Compute initial distance considering the array as circular

maxDistance = max(maxDistance, idx[i] - idx[i - 1]);

// Update the minimum number of seconds with the lower value

// Return the minimum number of seconds after completing the loop

// Initializes a map to hold arrays of indices for each unique number

// Populates the indexMap with the indices of occurrences of each number

// Loop over the indices to find the largest distance between any two consecutive indices

* Computes the minimum seconds needed to cover all numbers by a segment of continuous numbers in the list nums.

* @param nums array of numbers representing different values where we search for the minimum segment.

Find distance between consecutive occurrences

pair time = indices[i + 1] - indices[i]

time_spent = max(time_spent, pair_time)

class Solution: def minimum seconds(self, nums: list) -> int: # Dictionary to store the indices of each unique number in nums index_mapping = defaultdict(list)

Calculate the minimum seconds required (halve the max distance) # and compare with minimum found so far minimum_seconds = min(minimum_seconds, time_spent // 2)

import iava.util.ArrayList;

import java.util.HashMap;

import java.util.List;

import java.util.Map;

class Solution {

Java

return minimum_seconds

n = len(nums)

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// Populate the map with lists of indices for each number
        for (int i = 0; i < n; ++i) {
            indicesMap.computeIfAbsent(nums.get(i), k -> new ArrayList<>()).add(i);
        int minSeconds = Integer.MAX_VALUE; // Initialize the minimum seconds to the highest possible value
        // Iterate over the map values, which are lists of indices
        for (List<Integer> indices : indicesMap.values()) {
            int m = indices.size(): // Total number of indices in the current list
            int timeDiff = indices.get(0) + n - indices.get(m - 1);
            // Calculate the initial time difference
            // as the distance from the first to the last occurrence
            // Update the time difference to be the maximum gap between any two consecutive occurrences
            for (int i = 1; i < m; ++i) {
                timeDiff = Math.max(timeDiff, indices.get(i) - indices.get(i - 1));
            // Update the minimum time by comparing with the current calculated time
            minSeconds = Math.min(minSeconds, timeDiff / 2);
        return minSeconds; // Return the minimum number of seconds
C++
#include <vector>
#include <unordered map>
#include <algorithm>
using namespace std;
class Solution {
public:
    int minimumSeconds(vector<int>& nums) {
        // Create a mapping from each unique number to its indices in the array
        unordered map<int, vector<int>> indicesMap;
        int n = nums.size(); // get the size of the input vector
        for (int i = 0; i < n; ++i) {
            indicesMap[nums[i]].push_back(i); // map numbers to their indices
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let minSeconds = 1 << 30; // Large initial value</pre> // Iterates through each set of indices in the map for (const [number, indices] of indexMap) {

};

/**

TypeScript

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const indicesLength = indices.length;
        // Calculates the initial time as the time to cover from the first to the last occurrences
        let currentTime = indices[0] + length - indices[indicesLength - 1];
        // Updates the currentTime based on the maximum gap between consecutive indices
        for (let i = 1; i < indicesLength; ++i) {</pre>
            currentTime = Math.max(currentTime, indices[i] - indices[i - 1]);
        // Updates the minimum time
       minSeconds = Math.min(minSeconds, currentTime >> 1);
   // Returns the minimum seconds calculated
   return minSeconds;
from collections import defaultdict
class Solution:
   def minimum seconds(self, nums: list) -> int:
       # Dictionary to store the indices of each unique number in nums
        index_mapping = defaultdict(list)
       # Populate index mapping with positions for every number in nums
        for index. value in enumerate(nums):
            index_mapping[value].append(index)
       # Initialize the minimum seconds to infinity
       minimum seconds = float('inf')
       n = len(nums)
       # Iterate over the indices for each unique number
        for indices in index mapping.values():
           # Time spent is the distance between first and last occurrence
            time_spent = indices[0] + n - indices[-1]
           # Iterate over pairs of indices to find max distance in between
            for i in range(len(indices) - 1):
                # Find distance between consecutive occurrences
                pair time = indices[i + 1] - indices[i]
                # Update time spent with the maximum gap found so far
                time_spent = max(time_spent, pair_time)
            # Calculate the minimum seconds required (halve the max distance)
```

• The loop that goes through d.values() which can potentially iterate through all elements again in the worst case. If all the elements in nums are unique, this would again take O(n) time. • Inside the second loop, there's a nested call to pairwise(idx). The pairwise function itself has 0(k) complexity, where k is the length of the

to a worst-case time complexity of $O(n^2)$.

return minimum_seconds

Time and Space Complexity

Time Complexity

list idx passed to it. In the worst case, where nums has many repeated elements, this nested loop could have 0(n) complexity if all elements are the same. Given that pairwise is called inside the loop for every key in the dictionary d, the overall complexity of these nested loops

Therefore, the overall worst-case time complexity of the code is O(n^2).

The time complexity of the given code is determined by several factors:

and compare with minimum found so far

minimum_seconds = min(minimum_seconds, time_spent // 2)

Return the minimum seconds required to process all unique numbers

depends on the distribution of the numbers in the nums list. The worst-case scenario happens when all elements are the same, leading to a complexity of O(n) for the iterations throughout d.values(), compounded with the complexity of pairwise, leading

• The loop that creates the dictionary d, which has a time complexity of O(n) since it goes through all the elements of nums once.

Space Complexity The space complexity can be analyzed as follows:

numbers are the same, the list of indices would also contain n values. Therefore, the worst-case space complexity for d is O(n).

• The dictionary d that stores the indices of each element can potentially store n keys with a list of indices as values. In the worst case where all

• The space used by variables ans, t, idx, i, and j is constant, hence 0(1). Taking the above points into consideration, the total space complexity is 0(n) for the dictionary storage.

In conclusion, the code has a time complexity of $O(n^2)$ and a space complexity of O(n).