

**Problem Description** 

The given problem involves calculating and summing the power of all non-empty groups of heroes based on their strength values provided in an integer array nums. The power of a group is determined by the following:

The power of this group is the square of the maximum strength value among these heroes multiplied by the minimum strength

minimums for subgroups based on their position in the sorted array.

smallest, which aligns with how we consider maximums for subgroups.

minimum value in a subgroup with any of the previous elements as the maximum.

Identify the heroes in the group by their indices in the array, say i₀, i₁, ..., iҡ.

value of the same heroes, i.e., max(nums[i<sub>0</sub>], nums[i<sub>1</sub>], ..., nums[i<sub>k</sub>])<sup>2</sup> \* min(nums[i<sub>0</sub>], nums[i<sub>1</sub>], ..., nums[i<sub>k</sub>]).

The goal is to add up the power of all possible non-empty groups of heroes. Since the result could be quite large, it should be returned modulo 10° + 7.

# Intuition

of all groups would be too time-consuming due to the potentially large number of hero combinations. Instead, we can analyze the pattern of how the power of groups contributes to the total sum. The solution revolves around observing that sorting the array nums will make it easier to identify the maximums and minimums for

To solve the problem, we need to figure out how to efficiently calculate the sum of the powers of all groups. Brute force enumeration

subsequent smaller subgroups ending with this element. Reverse iterate over the sorted nums. We count the contributions to the power from each element when it acts as both a maximum and minimum within different subgroups.

different groups. Once sorted, any group with the last element as its maximum will have this last element as the maximum for all

- A running prefix sum p is kept. When a new element x is considered, it has an additional contribution when acting as the maximum—due to all possible subgroups ending with x. Its contribution is  $x^3$  added to all contributions from previous elements. • When x is a minimum, it adds x \* p to the result, where p includes the contributions from elements to the right of x in the sorted
- array when they act as maximums. • The prefix sum p is updated for the contribution of x being the maximum so far. It's the sum of all previous p values doubled
- (since every subgroup comes in two variants—with and without the new element x) plus the square of the new element x (which is the new maximum for subgroups ending with x). The answer is computed by summing contributions while iterating through the array and using modulo arithmetic to handle large
- numbers. Solution Approach

The solution uses a simple array and basic arithmetic operations to calculate the required sum. The steps in the provided solution approach can be broken down as follows:

### 1. Sort the array – Before iterating over nums, it is sorted in ascending order. This sorting enables us to find the maximums and

formed with x as the maximum.

2. Initialize variables – The solution sets an initial value for ans, which will hold the sum of powers, and p, which is our running prefix sum representing the contributions of maximum values so far.

- 3. Iterate in reverse The solution then iterates the sorted array in reverse (nums [::-1]), considering each number from largest to
- After entering the loop, it performs the following operations for every element x:
- Add to ans the value of x cubed (x \* x % mod) \* x modulo 10\*\*9 + 7. This covers the new subgroups where x is the maximum.

Add to ans the value of x multiplied by the current prefix sum p, effectively capturing the contribution of x when it is the

- Update the prefix sum p by doubling it and adding the square of the current element x. Doubling accounts for the fact that each existing subgroup can now be extended by either including or excluding x. Adding x\*x accounts for the new subgroups
- 4. Modulo operations To handle potentially large numbers and overflow issues, modulo arithmetic is consistently applied (% mod) to ensure that all intermediate values and the resulting sum remain within integer limits. By considering each element as the potential minimum and maximum of various subgroups, the solution efficiently accumulates the
- Example Walkthrough

array, while the time complexity is driven by the sorting operation and the subsequent linear traversal of the array.

power of all possible combinations. The space complexity is optimal as it only uses a fixed number of variables and the original input

Let's use a small example to illustrate the solution approach with the given problem: Suppose we have an integer array of hero strengths nums = [2, 1, 3].

2. Initialize variables: We initialize ans to 0, which will store the final answer, and p to 0, which is the prefix sum of contributions

At the start, ans = 0 and p = 0. We go through each element x in nums [::-1] (which gives us [3, 2, 1]) and perform the next

## when numbers act as maximums.

operation in this example.

Python Solution

from typing import List

nums.sort()

answer = 0

power\_sum = 0

return answer

return (int) answer;

Java Solution

for num in reversed(nums):

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respectively to keep the values within the limit.

3. Iterate in reverse: Now, we iterate from the end of the sorted array.

1. Sort the array: The first step is to sort nums to [1, 2, 3].

- steps.  $\circ$  For x = 3:
- p gets updated to  $2 * p + x^2 = 0 + 3^2 = 9$ .  $\circ$  For x = 2:

■ Update p to  $2 * p + x^2 = 2 * 22 + 1^2 = 44 + 1 = 45$ .

example, the answers are still small, so we don't need to apply modulo.

# Initialize the answer variable to accumulate the sum of powers

answer = (answer + (num \* num % modulo) \* num) % modulo

powers = (powers \* 2 + currentNum \* currentNum % MOD) % MOD;

// Cast the long result back to int before returning, as per the method signature expectation

# Iterate over the numbers in reverse (largest to smallest)

# Initialize a variable 'power\_sum' to store the accumulated powers of elements

■ Update ans by adding 3^3 % (10^9 + 7) = 27.

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■ Update ans by adding both 2^3 \% (10^9 + 7) = 8 and 2 * p = 2 * 9 = 18. Now, ans = ans + 8 + 18 = 27 + 26 = 53.
    ■ Update p to 2 * p + x^2 = 2 * 9 + 2^2 = 18 + 4 = 22.
\circ For x = 1:
   ■ Update ans by adding both 1^3 % (10^9 + 7) = 1 and 1 * p = 1 * 22 = 22. Now, ans = 53 + 1 + 22 = 76.
```

4. **Modulo operations**: Always use modulo 10^9 + 7 during the addition to keep the numbers within bounds. However, in our small

After iterating through all elements, we have the final ans = 76. This is the sum of the power of all possible non-empty groups of heroes calculated with the given formula, and since the value is already less than 10^9 + 7, we don't need to apply the modulo

In a larger example, if at any step the value of ans or p exceeds 10^9 + 7, we would take ans % (10^9 + 7) or p % (10^9 + 7)

class Solution: def sumOfPower(self, nums: List[int]) -> int: # Define the modulo to perform operations under modulo = 10\*\*9 + 7# Sort the list of numbers in non-descending order

```
# Add the current number times the accumulated power_sum to the answer
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               answer = (answer + num * power_sum) % modulo
18
19
               # Update the power_sum with the current num squared plus twice the previous power_sum
20
               power_sum = (power_sum * 2 + num * num) % modulo
           # Return the computed answer
21
```

# For each number, add the cubed value (mod modulo) multiplied by the number to the answer

```
class Solution {
       public int sumOfPower(int[] nums) {
           // Define the modulus value for large numbers to stay within the integer bounds
           final int MOD = (int) 1e9 + 7;
           // Sort the input array in ascending order
           Arrays.sort(nums);
9
           // Initialize the answer as 0 and a helper variable p to compute powers
            long answer = 0;
10
            long powers = 0;
11
12
13
           // Iterate over the array in reverse to compute the sum of powers
           for (int i = nums.length - 1; i \ge 0; --i) {
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                long currentNum = nums[i];
15
16
               // Compute the contribution of the current number raised to the power of 3
17
18
               // Make sure to take the modulo to prevent integer overflow
19
               answer = (answer + (currentNum * currentNum % MOD) * currentNum) % MOD;
20
21
               // Add the contribution of the current number times the partial sum of powers (p)
22
               // Again, use modulo to avoid overflow
23
               answer = (answer + currentNum * powers % MOD) % MOD;
24
               // Update p to be 2 times itself plus the current number squared (mod MOD)
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C++ Solution
1 class Solution {
2 public:
       int sumOfPower(vector<int>& nums) {
           const int MOD = 1e9 + 7; // define modulo value to prevent integer overflow
           sort(nums.rbegin(), nums.rend()); // sort the numbers in descending order
           long long totalSum = 0; // holds the total sum result
           long long powerSum = 0; // holds the sum of squares, multiplied by 2 each iteration
9
           // Iterate through all the numbers in the vector
           for (long long num : nums) {
11
               // Add to totalSum the current number cubed, modulo MOD
12
               totalSum = (totalSum + (num * num % MOD) * num) % MOD;
13
14
               // Add to totalSum the current number multiplied by powerSum, modulo MOD
15
               totalSum = (totalSum + num * powerSum % MOD) % MOD;
16
17
               // Update powerSum by multiplying by 2 and adding the current number squared, modulo MOD
18
               powerSum = (powerSum * 2 + num * num % MOD) % MOD;
19
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22
           return static_cast<int>(totalSum); // cast totalSum to int and return the final answer
23
25
Typescript Solution
   function sumOfCubedPowers(nums: number[]): number {
       // The modulo to use for preventing overflow
       const MODULO = 10 ** 9 + 7;
```

#### 30 return answer; 31 } 32

// Return the final answer

Time and Space Complexity

which do not depend on the size of nums.

// Sort the numbers array in ascending order

for (let  $i = nums.length - 1; i >= 0; --i) {$ 

const currentNum = BigInt(nums[i]);

// Initialize the prefix sum, representing sum of powers

// Get the current number as a BigInt for precision in calculations

// Add the cube of the current number modulo MODULO to the answer

// Update the prefixSum: multiply by 2 and add the square of currentNum

answer = (answer + Number((currentNum \* currentNum \* currentNum) % BigInt(MODULO))) % MODULO;

// Add the product of the currentNum and the prefixSum modulo MODULO to the answer

answer = (answer + Number((currentNum \* BigInt(prefixSum)) % BigInt(MODULO))) % MODULO;

prefixSum = Number((BigInt(prefixSum) \* 2n + currentNum \* currentNum) % BigInt(MODULO));

nums.sort((a, b) => a - b);

let answer = 0;

let prefixSum = 0;

// Initialize the answer to 0

// Iterate over the array in reverse

#### Time Complexity The time complexity of the provided function is determined by a few key operations:

**Space Complexity** 

2. The for-loop that iterates over the sorted list in reverse: The loop runs n times, where n is the length of nums. Inside the loop, all operations are constant time (0(1)), as they involve basic arithmetic operations and modulo % operation,

Combining these constants with the iteration gives us O(n) for the loop.

Combining both operations, the total time complexity of the code is  $O(n \log n)$  for sorting the list plus O(n) for the loop, which simplifies to 0(n log n) overall, as 0(n log n) is the dominating term.

1. Sorting the nums list: The sort() function has a time complexity of O(n log n) where n is the number of elements in the list.

- 1. The additional space used by the sorting algorithm. Most Python implementations use an in-place sorting algorithm, like Timsort,

The space complexity of the provided function is determined by:

- which would make the space complexity of sorting O(n) in the worst case. However, the sorted list uses the same space that was allocated for nums, so this may not count as additional space.
- with the input).

Overall, if the sort is considered in-place, the space complexity is 0(1); otherwise, it may be 0(n) in the worst case.

Considering the above points, the space complexity of the function is 0(1) for the variables defined outside the loop since they do not use additional space dependent on the input list size. However, taking into account the potential additional space required for sorting (if interpreted as additional space rather than in-place), it could be argued to be O(n) in a pessimistic assessment.

2. Variables ans, p, and mod occupy 0(1) space as they store integers that don't depend on the size of the input list.

3. The loop itself does not use any additional space that depends on n (no new list or data structure is being created that grows