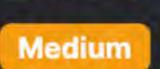
## 2155. All Divisions With the Highest Score of a Binary Array



Medium Array

# Problem Description

two subarrays, nums\_left and nums\_right, such that the division score is maximized. The division score is defined as the count of 0s in nums\_left plus the count of 1s in nums\_right. The array can be divided at any index i, which creates nums\_left with elements from the start of the array up to index i-1, and

You are given a binary array, nums, that contains only 0s and 1s. The task is to find all indices at which you can divide this array into

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nums\_right with elements from index i to the end. Note that if i is 0, then nums\_left is empty and nums\_right contains all the elements, while if i is the length of the array (n), then nums\_left contains all the elements and nums\_right is empty.

Intuition

The goal is to return indices that yield the highest division score. The indices can be returned in any order.

### To solve this problem, we need to understand that at each potential division index, the score is affected by the number of zeros to

can easily calculate the division score for each index without having to count the number of ones to the right every time. Here's the approach to solve the problem:

1. Initialize two counters, left and right. left will hold the number of 0s that we've encountered so far as we iterate from the

the left and the number of ones to the right of that index. Therefore, if we know the total number of ones in the array beforehand, we

beginning of the array towards the end, and right starts off as the total count of 1s in the entire array.

- 2. Initialize a variable mx that will hold the maximum division score that we've found so far. Initially, this will be equal to right because before any division, all 1s would be in nums\_right and this is the highest possible score at the start.
- 3. Start iterating through the array. With each element, update left and right accordingly. If you encounter a 0, increment left. If you encounter a 1, decrement right. This is because a zero would now be contributing to the division score on the left, and a one would no longer contribute to the score on the right after passing the division point.
- 4. At each index, calculate the current division score, t, as the sum of left and right. If it's equal to mx, append the current index + 1 to the list of indices with maximum score, ans. If the current score is greater than the max score found so far (mx), update mx with t and reset and to a new list containing just the current index + 1. This keeps track of all indices where we have encountered the maximum score.
- 5. After we have finished iterating through the array, we will have a list of all indices at which the maximum division score can be achieved. We return this list. By keeping track of the running count of zeros and ones, we optimize the solution by only iterating through the array once (O(n) time complexity), rather than recalculating the division score from scratch at each possible division point.
- Solution Approach

The implementation follows a simple but efficient algorithm that ensures we only need a single pass through the input array, which is a key characteristic of an O(n) time complexity solution. The approach heavily relies on the usage of two variables to represent the current number of zeros and ones relevant to the potential division at any index in the array. Here's the detailed implementation

### 1. Initialize a counter left to 0. This will track the number of 0s to the left of the current index as we iterate through the array. 2. Initialize a counter right to the sum of the elements in the nums array (since the array contains only 0s and 1s, this sum equals

approach:

index 0.

the number of 1s in the array). 3. Set the maximum score mx initially equal to right because, at the start (when the division point is at index 0 and nums\_left is empty), all 1s are in nums\_right. 4. Create an array ans with a single element 0 because initially, the highest score can be achieved when the division point is at

o If the current element num is 0, increment left because we've found another 0 that contributes to the score when it's in nums\_left.

5. Iterate over the elements in the nums array using a loop. For each element at index i, do the following:

Compare the temporary score t with the maximum score mx:

score and the previous indices are no longer valid.

- If the current element is 1, decrement right as this 1 no longer contributes to the score in nums\_right after moving past index i.
  - If t is equal to mx, append i + 1 to ans. The +1 is necessary because the division occurs after the current index, so the next index is the potential division point. ■ If t is greater than mx, update mx to t and set ans to a new list containing only i + 1, since we have found a new highest

6. Continue this process until the end of the array. After the loop ends, the ans array contains all indices where the maximum

for handling large arrays efficiently. The space complexity is also kept low since we are only using a handful of variables and an

Calculate the temporary score t as the sum of left and right, which represents the current division score at index i.

division score is achieved. 7. Finally, return the ans array.

The use of a single loop and constant-time update operations ensures that the overall time complexity remains linear, which is crucial

- output array, avoiding any additional data structures that could increase the space usage. Example Walkthrough
- Let's walk through an example to illustrate the solution approach with a binary array nums.

Suppose nums = [0, 1, 0, 1, 1]. We want to find all indices where we can divide this array to maximize the division score.

2. Set mx to 3 because at the index 0, nums\_right would contain all the 1s, giving the maximum possible score initially.

1. Initialize left to 0 and right to 3 since there are three 1s in the array.

Following the solution approach:

3. Create an array ans with a single element 0.

Let's iterate through each element and apply the steps:

we update mx to 4 and set ans to [1] (next index after division).

4. Start iterating over the array nums.

At index 0, nums [0] is 0. Increment left to 1 (now left = 1, right = 3), the score here is 1 + 3 = 4. Since 4 is greater than mx,

the array at indices 1 or 3 gives us both subarrays that maximize the division score.

# Initialize the score for the left partition (initially 0) and the right partition

# If the number is 0, it contributes to the left partition's score

# If the number is 1, it contributes to the right partition's score

# Current total score is the sum of the scores from both partitions

# Found a new max score, update max score and reset best indices

def maxScoreIndices(self, nums: List[int]) -> List[int]:

current\_score = score\_left + score\_right

elif max\_score < current\_score:</pre>

resultIndices.clear();

return resultIndices;

private int sum(int[] nums) {

for (int num : nums) {

sum += num;

// Sum all elements in the array

int sum = 0;

return sum;

resultIndices.add(i + 1);

// Return the list of all indices that provide maximum score

// Helper method to calculate the sum of ones in the array

max\_score = current\_score

best\_indices = [index + 1]

# Iterate through the list of numbers

for index, num in enumerate(nums):

score left += 1

score\_right -= 1

than mx (4), so we continue without updating mx or ans. • At index 2, nums [2] is 0. Increment left to 2 (now left = 2, right = 2), the new score is 2 + 2 = 4. This equals the mx, thus we append 3 to ans (becoming [1, 3]).

• At index 1, nums [1] is 1. Decrement right to 2 (now left = 1, right = 2), the score now is 1 + 2 = 3. The score 3 is not greater

- At index 3, nums [3] is 1. Decrement right to 1 (now left = 2, right = 1), and the score here is 2 + 1 = 3. No change to mx or ans since the score is less.
- **Python Solution** 1 from typing import List

At index 4, nums [4] is 1. Decrement right to 0 (now left = 2, right = 0), and the score is 2 + 0 = 2, which is again less than mx.

The iteration is complete, and the ans array [1, 3] contains all the indices that give the maximum division score of 4. Thus, dividing

# Set the maximum score as the initial score of right partition 9 max\_score = score\_right 10 11 # The initial best index is 0 12

27 # Check if the current score equals the max score found so far 28 if max\_score == current\_score: # This index yields a score equal to the current max score 29 best\_indices.append(index + 1) 30

class Solution:

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score\_left = 0

score\_right = sum(nums)

best\_indices = [0]

if num == 0:

elif num == 1:

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           # Return the list of indices that yield the maximum score
37
           return best_indices
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Java Solution
   class Solution {
       // Method to find all indices where we can split the input array nums such that the sum of zeros to the left and ones to the righ
       public List<Integer> maxScoreIndices(int[] nums) {
           // Initialize count of zeros to the left and ones to the right of the index
           int zerosCount = 0, onesCount = sum(nums);
           // Initialize max score with the score if we split before the first index (all ones to the right)
           int maxScore = onesCount;
           // List to store all indices that provide maximum score
           List<Integer> resultIndices = new ArrayList<>();
           // Add index 0 as a valid split (no elements to the left)
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            resultIndices.add(0);
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           // Iterate over the array to find all valid split indices
           for (int i = 0; i < nums.length; ++i) {</pre>
15
               // If current element is 0, increase zeros count
16
               if (nums[i] == 0) {
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18
                   ++zerosCount;
19
               } else {
20
                   // If current element is 1, decrease ones count
21
                   --onesCount;
22
23
               // Current score is the sum of zeros to the left and ones to the right
24
               int currentScore = zerosCount + onesCount;
25
               // If current score equals the max score, add index to result
26
               if (maxScore == currentScore) {
                    resultIndices.add(i + 1);
27
28
               } else if (maxScore < currentScore) {</pre>
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                   // If current score exceeds max score, update max score and clear previous indices
30
                   maxScore = currentScore;
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C++ Solution
 1 class Solution {
 2 public:
       vector<int> maxScoreIndices(vector<int>& nums) {
           int leftZeroes = 0; // Counter for the number of zeroes on the left
           int rightOnes = accumulate(nums.begin(), nums.end(), 0); // Counter for the number of ones on the right
           int maxScore = rightOnes; // Maximum score initialized with the sum of ones
           vector<int> resultIndices; // Vector to store the indices where max score occurs
           resultIndices.push_back(0); // 0 is a potential max score index
 9
           // Iterate through the nums array to find where the maximum score occurs
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           for (int i = 0; i < nums.size(); ++i) {</pre>
11
               if (nums[i] == 0) {
12
                   ++leftZeroes; // Increment leftZeroes for each zero encountered
14
               } else {
15
                   --rightOnes; // Decrement rightOnes for each one encountered
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               int currentScore = leftZeroes + rightOnes; // Calculate current score
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19
               // Check if the current score matches the maximum score found so far
20
               if (maxScore == currentScore) {
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22
                   // If it matches, add the current index + 1 to the result
23
                   resultIndices.push_back(i + 1);
               } else if (maxScore < currentScore) {
24
25
                   // If the current score is greater, update the maxScore
                   maxScore = currentScore;
26
                   // Clear the resultIndices vector and start again with the current index + 1
27
28
                   resultIndices.clear();
29
                   resultIndices.push_back(i + 1);
30
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32
           return resultIndices; // Return the vector with all indices where the max score occurs
33
34 };
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Typescript Solution
 1 // Calculates the indices where the score is maximized when splitting the array 'nums' into two parts
   function maxScoreIndices(nums: number[]): number[] {
       // Calculate the length of the numbers array
       const length = nums.length;
```

#### 16 17 } else { 18

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// Compute the total count of '1's in the array

const totalOnes = nums.reduce((accumulator, current) => accumulator + current, 0);

let scoreAtEachIndex: Array<number> = [totalOnes]; // Include the score when split index is 0

let onesToRight = totalOnes; // Number of `1`s to the right of the current index

let zerosToLeft = 0; // Number of `0`s to the left of the current index

// Initialize an array to store the combined score at each index

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       // Compute the score for each index in the input array
       for (const num of nums) {
13
           // Update corresponding scores based on the current number
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15
           if (num === 0) {
               zerosToLeft++; // Increment as we found a '0'
               onesToRight--; // Decrement as we found a `1`
20
           // Record the current score
21
           scoreAtEachIndex.push(zerosToLeft + onesToRight);
22
23
       // Determine the maximum score out of all scores
24
       const maxScore = Math.max(...scoreAtEachIndex);
       let maxIndices: Array<number> = []; // Array to store indices with max score
27
28
       // Collect all indices where the score equals the maximum score
       for (let i = 0; i <= length; i++) {
29
           if (scoreAtEachIndex[i] === maxScore) {
30
               maxIndices.push(i);
32
33
34
       // Return the array of indices with maximum score
36
       return maxIndices;
37 }
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Time and Space Complexity
The time complexity of the code is O(n), where n is the length of the input list nums. This is because the code iterates once over all
the elements of the list, performing a constant amount of work for each element (incrementing left if it's a 0, decrementing right if it's
a 1, and comparing and possibly updating the maximum score).
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The space complexity of the code is O(k), where k is the number of indices at which the maximum score is achieved. In the worstcase scenario, every index could be a part of the answer, in which case the space complexity would be 0(n). However, under normal circumstances where not every index is a solution, k is typically much less than n. Fundamental to the space complexity is the list

ans, which stores the indices. Besides that, the algorithm uses only a constant amount of additional space for variables like left, right, mx, and t.