1658. Minimum Operations to Reduce X to Zero

#### Binary Search Sliding Window Medium Array Hash Table Prefix Sum

You are given an array of integers called nums and another integer x. Your goal is to remove either the first or last element from the array in each operation. By doing so, you decrease the value of x by the value of the element you removed. This process changes the array for the next operation since the element is no longer part of it.

Leetcode Link

The challenge is to find the minimum number of operations needed to reduce x to exactly 0. It's a puzzle where you must choose which side to take numbers from at each step. However, the array has a fixed order, so you cannot rearrange it. If it's possible to reduce x to 0, you should return the minimum number of operations you need. If it's not possible to do so, then the answer is -1.

## The initial intuition might be to always choose the larger number between the first and last element of the array to subtract from x.

Intuition

Problem Description

method: instead of thinking in terms of our original target x, think about the rest of the numbers that will remain in the array nums after all the operations. The key insight is to transform the problem into finding the longest subarray in nums that sums up to a new target, which is sum(nums) - x. This approach flips the original problem on its head—you're now looking for the subarray that remains rather than the numbers

However, this greedy approach might not lead to the optimal solution. Instead, a different perspective can provide a more systematic

to reduce x to zero. In the code, an inf (infinity) is initially set to represent an impossible situation. A two-pointer approach is then used to find the longest subarray whose sum equals sum(nums) - x. As we iterate through the array with a variable i, indicating the right end of our

subarray, a variable s (the running sum) is continuously updated. A second pointer j represents the potential left end of our subarray.

We make sure to adjust j and s whenever our current running sum surpasses our new target, by subtracting values while moving j to

the right. When we find a subarray that sums to the new target, we calculate the number of operations it would take to remove the other elements by subtracting the length of this subarray from the total number of elements n. This operation count is kept if it is smaller than our current best answer in variable ans.

Solution Approach

Once the loop is finished, if ans remains as infinity, it means no suitable subarray was found, and we return -1. Otherwise, we return

the value of ans, which represents the minimum number of operations required to reduce x to exactly 0.

and slide it to explore different subsets, according to conditions given in the problem.

The solution follows a sliding window approach, which is a pattern used when we need to find a range or a subarray in an array that satisfies certain conditions. The idea behind a sliding window approach is to maintain a subset of items from the array as the window

this is that the sum of elements removed (to reduce x to 0) and the sum of elements that remain (the subarray) should equal the sum

## In this specific problem, the target condition for the subarray is that its elements' sum should equal sum(nums) - x. The reason for

Here is a step-by-step explanation of the code:

the array, which gives us a time complexity of O(n).

2. Start iterating over the array, beginning with i = 0:

provides us with an O(n) complexity for the problem.

def minOperations(self, nums: List[int], x: int) -> int:

for right\_index, value in enumerate(nums):

current\_sum -= nums[left\_index]

Second iteration (i=1): window is [3, 2], s = 5.

Third iteration (i=2): window is [3, 2, 20], s = 25.

as we find valid subarrays.

nums[j] from s).

of the original array.

1. Calculate the new target x as the sum of all elements in nums minus the original x. This represents the sum of the subarray we want to find. 2. Initialize ans with the value inf to represent a very high number of operations (assumed to be impossible) that will be minimized

- 4. Start iterating through the array with index i representing the end boundary of the sliding window. Add nums [i] to the sum s. 5. While the current sum s exceeds the target x, adjust the window by moving the start j to the right (increasing j and subtracting
- gives us the number of operations because i j + 1 is the length of our subarray, and subtracting this from the total length n gives the number of operations needed to achieve the original x.

3. Set n to the length of nums, s to 0 as the current sum, and j to 0 as the starting index of our sliding window.

7. Continue the steps 4-6 until all elements have been visited.

8. At the end, if no valid subarray is found (meaning ans is still inf), return -1. Otherwise, return the value of ans as the final result.

The use of a sliding window ensures that we check every possible subarray in an efficient manner, only making a single pass through

6. When a subarray sum equals the target, update ans with the minimum of its current value and n - (i - j + 1). This calculation

Example Walkthrough Let's take a small example to illustrate the solution approach. Consider the following array nums and integer x:

1. Initialize ans with a value representing infinity, s (current sum) to 0, j (window start index) to 0, and n (the length of nums) to 6.

### Now we apply the sliding window approach:

1 nums = [3, 2, 20, 1, 1, 3]

First iteration (i=0): window is [3], s = 3.

The sum of nums is 3 + 2 + 20 + 1 + 1 + 3 = 30, so our new target is sum(nums) - x which is 30 - 10 = 20.

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At this point, our sum s exceeds our target 20. We need to adjust the window:
  \circ j is incremented to 1 (removing nums [0] from sum), so the window is [2, 20], and s = 22.
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 $\circ$  j is incremented to 2 (removing nums [1]), so the window is [20], and s = 20.

found. The window would shrink and grow as the sum oscillates relative to our target.

- 3. We have found a subarray that sums up to our target (20), which is [20]. We update ans with the number of operations needed to remove the other elements: n - (i - j + 1) which is 6 - (2 - 2 + 1) = 5.
- 2) and the last three elements (1, 1, and 3) while keeping the subarray [20], which adds up exactly to our target of 20. Hence, the minimum number of operations required to reduce x to 0 in this example is 5.

The sliding window approach makes this process efficient by ensuring that we only need to scan through the array once, which

4. Continue the algorithm with the rest of nums, checking for a longer subarray that sums to 20, but no such longer subarray will be

5. At the end of the process, we will find that the smallest ans was 5, which corresponds to removing the first two elements (3 and

- Python Solution
- # Calculate new target which is the sum of elements that remain after removing the elements summing to x. target = sum(nums) - x# Initialize variables: set answer to infinity to represent initially impossible scenario

# `n` holds the length of the nums list; `current\_sum` and `left\_index` for the sliding window

# Use a sliding window approach to find if there's a continuous subarray summing to `target`

# Expand the window by adding the current value to the `current\_sum`

answer = min(answer, n - (right\_index - left\_index + 1))

while left\_index <= right\_index and current\_sum > target:

# Shrink the window from the left as long as `current\_sum` exceeds `target`

# If answer has not been updated, return -1, otherwise return the minimum operations

minimumOperations = Math.min(minimumOperations, n - (left - right + 1));

left\_index += 1 23 # If `current\_sum` matches `target`, we found a valid subarray 24 25 # Update the answer with the minimum number of operations

answer = inf

n = len(nums)

current\_sum = left\_index = 0

current sum += value

if current\_sum == target:

// If no such subarray is found, return -1

// Otherwise, return the minimum number of operations

return minimumOperations == Integer.MAX\_VALUE ? -1 : minimumOperations;

from math import inf

class Solution:

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           return -1 if answer == inf else answer
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Java Solution
   class Solution {
       public int minOperations(int[] nums, int x) {
           int target = -x;
           // Calculate the negative target by adding all the numbers in 'nums' array
           // Since we are looking for a subarray with the sum that equals the modified 'target'
           for (int num : nums) {
                target += num;
10
           int n = nums.length;
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           int minimumOperations = Integer.MAX_VALUE;
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           int sum = 0;
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15
           // Two pointers approach to find the subarray with the sum equals 'target'
           for (int left = 0, right = 0; left < n; ++left) {</pre>
16
               // Add the current element to 'sum'
               sum += nums[left];
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               // If 'sum' exceeds 'target', shrink the window from the right
21
               while (right <= left && sum > target) {
                    sum -= nums[right];
23
                    right++;
24
25
26
               // If a subarray with sum equals 'target' is found, calculate the operations required
27
               if (sum == target) {
```

# Since we're looking for the minimum operations, we subtract the length of current subarray from total length

#### public: 9

C++ Solution

1 #include <vector>

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2 #include <unordered_map>
   #include <numeric>
   #include <algorithm>
   class Solution {
       // Calculate the minimum number of operations to reduce the sum of the array
       // by 'x' by either removing elements from the start or end.
       int minOperations(std::vector<int>& nums, int x) {
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           // Compute the new target which is the desired sum of the subarray we want to find
11
            int target = std::accumulate(nums.begin(), nums.end(), 0) - x;
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            // If target is negative, no solution is possible as we cannot create a negative sum.
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            if (target < 0) {</pre>
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                return -1;
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            // Special case: if target is 0, it means we want to remove the whole array
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           if (target == 0) {
               return nums.size();
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            // Use a hashmap to store the cumulative sum at each index
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            std::unordered_map<int, int> prefixSumIndex;
26
            prefixSumIndex[0] = -1; // Initialize hashmap with base case
27
            int n = nums.size(); // Size of the input array
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            // Initialize the answer with a large number, signifying that we haven't found a solution yet
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            int minOperations = std::numeric_limits<int>::max();
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            for (int i = 0, sum = 0; i < n; ++i) {
                sum += nums[i]; // Cumulative sum up to the current index
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                // Record the first occurrence of this sum. This prevents overwriting previous indices.
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                if (!prefixSumIndex.count(sum)) {
                    prefixSumIndex[sum] = i;
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41
                // Check if (sum - target) has been observed before
42
                if (prefixSumIndex.count(sum - target)) {
                    int startIdx = prefixSumIndex[sum - target];
43
                    // Calculate operations as the difference between the current ending index and
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                    // the starting index of the subarray, adjusting for whole array length.
                    minOperations = std::min(minOperations, n - (i - startIdx));
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            // If minOperations hasn't changed, return -1 to indicate no solution found
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            return minOperations == std::numeric_limits<int>::max() ? -1 : minOperations;
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   };
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```

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Typescript Solution

const length = nums.length;

function minOperations(nums: number[], x: number): number {

// Calculate the target sum by subtracting x from the total sum of nums

let minimumOps = Infinity; // Initialize with a large number representing infinity

let target = nums.reduce((acc, current) => acc + current, 0) - x;

```
// Initialize two pointers for the sliding window and a sum to hold the window's sum
       let windowStart = 0;
 8
       let currentSum = 0;
 9
10
       // Loop over the array to find the maximum-sized subarray that adds up to target
11
       for (let windowEnd = 0; windowEnd < length; ++windowEnd) {</pre>
           // Add the current element to windowSum
           currentSum += nums[windowEnd];
15
16
           // Shrink the window from the start if the currentSum exceeds the target
17
           while (windowStart <= windowEnd && currentSum > target) {
               currentSum -= nums[windowStart++];
18
19
20
           // If the currentSum equals the target, update minimumOps if the found window is better
21
22
           if (currentSum == target) {
               minimumOps = Math.min(minimumOps, length - (windowEnd - windowStart + 1));
23
24
25
26
       // Return minimum operations required, or -1 if the target sum isn't achievable
27
       return minimumOps == Infinity ? -1 : minimumOps;
28
29 }
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Time and Space Complexity
```

# **Time Complexity**

#### (denoted by j), but it does not iterate more than n times across the entire for loop due to the nature of the two-pointer strategy each element is visited by each pointer at most once.

Space Complexity

The space complexity of the code is 0(1). Outside of the input data, the algorithm uses only a constant number of additional variables (x, ans, n, s, j, i, and v). The space required for these variables does not scale with the size of the input list; hence, the space complexity is constant.

The provided code has a time complexity of O(n), where n is the length of the input list nums. This is because the code uses a two-

pointer approach (variables i and j) that iterates through the list only once. The inner while loop adjusts the second pointer