467. Unique Substrings in Wraparound String



Problem Description

The given problem is to count the number of unique non-empty substrings of a string s that can also be found in the infinite base string, which is essentially the English lowercase alphabet letters cycled indefinitely. The string s is a finite string, possibly containing repeated characters.

Leetcode Link

The task is to figure out how many unique substrings from s fit consecutively into base. The challenge here is figuring out an efficient way to calculate this without the need to generate all possible substrings of s and check them against base, which would be computationally expensive.

The intuition behind the solution leverages the properties of the base string. Since base is comprised of the English alphabet in order

Intuition

and repeated indefinitely, any substring following the pattern of contiguous letters ('abc', 'cde', etc.) will be found in base. Furthermore, if we have found a substring that fits into base, any shorter substrings starting from the same character will also fit. The solution uses dynamic programming to keep track of the maximum length for substrings starting with each letter of the alphabet

found in s. The intuition is that if you can form a substring up to a certain length starting with a particular character (like 'a'), then you can also form all smaller substrings that start with that character. Here's our approach in steps:

1. Create a list dp of 26 elements representing each letter of the alphabet to store the maximum substring length starting with that letter found in s.

- 2. Go through each character of string s and determine if it is part of a substring that follows the contiguous pattern. We do this by checking if the current and previous characters are adjacent in base.
- 3. If adjacent, increment our running length k. If not, reset k to one, because the current character does not continue from the previous character.
- 4. Determine the list index corresponding to the current character and update dp[idx] with the maximum of its current value or k.
- 5. After processing the entire string, the sum of the values in dp is the total number of unique substrings found in base. This approach prevents checking each possible substring and efficiently aggregates the counts by keeping track of the longest
- The solution uses dynamic programming, which is a method for solving complex problems by breaking them down into simpler subproblems. It utilizes additional storage to save the result of subproblems to avoid redundant calculations. Here's how the solution

approach is implemented:

length 1.

Solution Approach

contiguous substring ending at each character.

2. Iterating over p: We iterate over the string p, checking each character. 3. Checking Continuity: For each character c in p, we check if it forms a continuous substring with the previous character. This is

set to 0. This array will store the maximum length of the unique substrings ending with the respective alphabet character.

1. Initial DP Array: We create a DP (dynamic programming) array dp with 26 elements corresponding to the letters of the alphabet

- done by checking the difference in ASCII values specifically, whether (ord(c) ord(p[i 1])) % 26 == 1. This takes care of the wraparound from 'z' to 'a' by using the modulus operation.
- 4. Updating Length of Substring k: If the condition is true, it means the current character c continues the substring, and we increase our substring length counter k. If not, we reset k to 1 since the continuity is broken, and c itself is a valid substring of
- 5. Updating DP Array: We calculate the index of the current character in the alphabet idx = ord(c) ord('a') and update the dp array at this index. We set dp[idx] to be the maximum of its current value or k. This step ensures we're keeping track of the longest unique substring ending with each letter without explicitly creating all substring combinations.
- substrings ending with the respective character that can be found in base. Summing up all these maximum lengths will give us the number of unique non-empty substrings of s in base. This algorithm uses the DP array as a way to eliminate redundant checks and store only the necessary information. By keeping track

of the lengths of contiguous substrings in this manner, we avoid having to store or iterate over each of the potentially very many

6. Result by Summing DP values: After completing the iteration over p, every index of the dp array contains the maximum length of

Example Walkthrough Let's walk through an example to illustrate the solution approach.

3. Checking Continuity: As we check each character, we look for continuity from its predecessor. Since the first character 'a' has

character, 'c', and the same applies. However, when we get to the fourth character 'd', 'c' and 'd' are continuous, but for the fifth

no predecessor, we skip to the second character 'b'. The ASCII difference from 'a' to 'b' is 1, thus we continue to the third

1. Initial DP Array: We initiate a DP array dp with 26 elements set to 0. The array indices represent letters 'a' to 'z'.

Suppose our string s is "abcdbef".

Following the steps of the solution approach:

substrings explicitly.

2. **Iterating over s:** We begin iterating over string s.

4. Updating Length of Substring k: As we continue iterating:

- character 'b', 'd' and 'b' are not adjacent characters in the English alphabet.
- ∘ 'a' starts a new substring with k=1.
 - ∘ 'b' is contiguous with 'a', so k=2. ∘ 'c' is contiguous with 'b', so k=3. ∘ 'd' is contiguous with 'c', so k=4. ∘ 'b' breaks the pattern, resetting k=1.

6. Result by Summing DP Values: Summing up the values in dp, we get the total count of unique non-empty substrings of s that

∘ 'f' is contiguous with 'e', so k=2. 5. **Updating DP Array**: Throughout the iteration, we update our dp. Here's how dp changes:

After reset at 'e': dp[4] = max(dp[4], 1) => 1

can be found in base: 1 + 2 + 3 + 4 + 1 + 2 = 13

def findSubstringInWraproundString(self, p: str) -> int:

Iterate through the string, character by character.

if i > 0 and (ord(p[i]) - ord(p[i - 1])) % 26 == 1:

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o After 'a': dp[0] = max(dp[0], 1) => 1
o After 'b': dp[1] = max(dp[1], 2) => 2
o After 'c': dp[2] = max(dp[2], 3) => 3
\circ After 'd': dp[3] = max(dp[3], 4) => 4

    After reset at 'b': dp[1] = max(dp[1], 1) => 2 (no change because 'b' already had 2 from 'ab')
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o After 'f': dp[5] = max(dp[5], 2) => 2

 $max_length_end_with = [0] * 26$

return sum(max_length end with)

current_length = 0

for i in range(len(p)):

∘ 'e' is not contiguous with 'b', k=1.

So, our string s "abcdbef" has 13 unique non-empty substrings that fit consecutively into the infinite base string of the English alphabet cycled indefinitely.

Initialize a variable to keep track of the current substring length.

14 # If consecutive, increment the current length. 15 current_length += 1 else: 16 17 # Otherwise, reset the current length to 1.

The condition checks if they are in alphabetical order or if it's a 'z' followed by 'a'.

max_length_end_with[index] = max(max_length_end_with[index], current_length)

Return the sum of max lengths, which gives the total number of distinct substrings.

Check if the current character and the one before it are consecutive in the 'z-a' wraparound string.

Initialize an array to keep track of the max length of substrings that end with each letter of the alphabet.

current_length = 1 18 19 20 # Calculate the index in the alphabet for the current character. 21 index = ord(p[i]) - ord('a') 22 # Update the max length for this character if the current length is greater.

Python Solution

1 class Solution:

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35 };

Java Solution class Solution { public int findSubstringInWraproundString(String p) { // dp array to store the maximum length substring ending with each alphabet int[] maxSubstringLengths = new int[26]; int currentLength = 0; // Length of current substring // Iterate through the string for (int i = 0; i < p.length(); ++i) {</pre> char currentChar = p.charAt(i); 9 10 11 // If the current and previous characters are consecutive in the wraparound string 12 if (i > 0 && (currentChar - p.charAt(i - 1) + 26) % 26 == 1) { // Increment length of current substring 13 14 currentLength++; } else { 16 // Restart length if not consecutive 17 currentLength = 1; 18 19 20 // Find the index in the alphabet for the current character int index = currentChar - 'a'; 21 22

// Update the maximum length for the particular character if it's greater than the previous value

maxSubstringLengths[index] = Math.max(maxSubstringLengths[index], currentLength);

// Sum up all the maximum lengths as each length contributes to the distinct substrings

// dp array to keep track of the max length of unique substrings ending with each letter.

// Compute the result by summing the max lengths of unique substrings ending with each letter.

// Initialize an array to store the maximum length of unique substrings that end with each alphabet letter

int totalCount = 0; // Holds the total count of unique substrings

return totalCount; // Return total count of all unique substrings

for (int maxLength : maxSubstringLengths) {

totalCount += maxLength;

int findSubstringInWraproundString(string p) {

vector<int> maxLengthEndingWith(26, 0);

for (int i = 0; i < p.size(); ++i) {

char currentChar = p[i];

// Loop through all characters in string 'p'.

int currentLength = 0;

int result = 0;

return result;

const length = p.length;

// Current substring length

Typescript Solution

35 36 } 37

C++ Solution

1 class Solution {

public:

13 // Check if the current character forms a consecutive sequence with the previous character. 14 if $(i > 0 \& (currentChar - p[i - 1] + 26) % 26 == 1) {$ 15 // If consecutive, increment the length of the current valid substring. 16 ++currentLength; 17 } else { // If not consecutive, start a new substring of length 1. 19 currentLength = 1; 20 21 22 23 // Update the maximum length of substrings that end with the current character. int index = currentChar - 'a'; 24 25 maxLengthEndingWith[index] = max(maxLengthEndingWith[index], currentLength); 26

for (int length : maxLengthEndingWith) result += length;

// Return the total number of all unique substrings.

function findSubstringInWraproundString(p: string): number {

const maxSubstringLengthByCh = new Array(26).fill(0);

const index = p.charCodeAt(i) - 'a'.charCodeAt(0);

return maxSubstringLengthByCh.reduce((sum, value) => sum + value);

// Total length of the input string 'p'

// 'k' will be used to store the length of the current valid substring.

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let currentLength = 1;
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       // Set the maximum length for the first character
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       maxSubstringLengthByCh[p.charCodeAt(0) - 'a'.charCodeAt(0)] = 1;
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       // Iterate through the string starting from the second character
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       for (let i = 1; i < length; i++) {</pre>
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           // Check if the current and the previous characters are consecutive in the wraparound string
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// Determine the index for the current character in the alphabet array

// Update the maximum substring length for the current character if necessary

maxSubstringLengthByCh[index] = Math.max(maxSubstringLengthByCh[index], currentLength);

// Compute the sum of all maximum substring lengths to get the final count of distinct non-empty substrings

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Time and Space Complexity
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constant and does not depend on the input size.

Time Complexity

if ((p.charCodeAt(i) - p.charCodeAt(i - 1) + 26) % 26 === 1) { 15 // If they are consecutive, increment the length of the substring that includes the current character 16 17 currentLength++; } else { 18 // If not, reset the current substring length to 1 19 20 currentLength = 1;

The given code iterates through each character of the string p only once with a constant time operation for each character including

Space Complexity The space complexity is determined by the additional space used besides the input itself. Here, a constant size array dp of size 26 is used, which does not grow with the size of the input string p. Therefore, the space complexity is 0(1), since the space used is

arithmetic operations and a maximum function. This results in a time complexity of O(n), where n is the length of the string p.