

# 2319. Check if Matrix Is X-Matrix

Easy

Array

Matrix

[Leetcode Link](#)

## Problem Description

The problem requires us to determine if a given square matrix can be classified as an X-Matrix. A square matrix can be considered an X-Matrix if it meets two conditions:

1. All elements on both its main diagonal (from top-left to bottom-right) and its anti-diagonal (from top-right to bottom-left) must be non-zero.
2. All other elements, which are not part of the diagonals, must be zero.

Given an input matrix named `grid`, which is represented as a 2D integer array of size `n x n`, our task is to return `true` if `grid` is an X-Matrix, and `false` otherwise.

## Intuition

To solve this problem, we can iterate over each element of the matrix and verify it against the two conditions provided for an X-Matrix. We can follow these steps:

1. Loop through each element in the matrix using a nested loop, where `i` is the index for rows, and `j` is the index for columns.
2. Check if the current element (`grid[i][j]`) belongs to either the main diagonal or the anti-diagonal. This is true when `i == j` (main diagonal) or `i + j == len(grid) - 1` (anti-diagonal).
3. If the current element belongs to one of the two diagonals, check if it is non-zero. If it is zero, we can immediately return `false`, as it violates the first condition for an X-Matrix.
4. If the current element does not belong to a diagonal, check if it is zero. If it isn't, return `false` since this violates the second condition.
5. If none of these violations occur during the traversal, return `true`, as the matrix satisfies both conditions for an X-Matrix.

The solution approach directly translates this intuition into a pair of nested loops that inspect each element based on its position in the matrix. By ensuring that diagonal elements are non-zero and others are zero, the solution effectively determines the X-Matrix validity.

## Solution Approach

The solution leverages a straightforward approach without using any additional data structures or complex patterns. It is purely based on element-wise inspection of the matrix. Here is how the code implements the strategy to check if the given matrix is an X-Matrix:

1. We use two nested loops to traverse each element of `grid`, where the outer loop uses the variable `i` to iterate over rows, and the inner loop uses `j` to iterate over columns. This allows us to check each element (denoted as `v`).
2. The main diagonal is where the row index is equal to the column index (`i == j`). The anti-diagonal can be identified in a square matrix of size `n` by the condition where the sum of the row index and column index equals `n - 1` (`i + j == len(grid) - 1`).
3. Inside the loop, we check if the element belongs to either the main or anti-diagonal by evaluating the above two conditions. If the current element is part of a diagonal, we verify if it's non-zero. If a zero is found on any diagonal, the function immediately returns `false`, as it contradicts the first rule of an X-Matrix.
4. If the current element does not lie on a diagonal, it must be zero to fulfill the second condition of an X-Matrix. Thus, any non-zero value encountered in this case leads to a return value of `false`.
5. If the loop concludes without finding any violations of the X-Matrix rules, it means all diagonals contain non-zero values and all other elements are zero. Thus the function returns `true`, confirming that the `grid` is an X-Matrix.

The implementation is efficient, with a time complexity of  $O(n^2)$ , which is required to check every element, and space complexity of  $O(1)$ , as no additional space is required beyond input and variables for iteration.

## Example Walkthrough

Let's illustrate the solution approach with a small example.

Consider a small `3x3` matrix (`grid`):

```
1 [
2   [2, 0, 3],
3   [0, 4, 0],
4   [1, 0, 5]
5 ]
```

We need to determine if this matrix is an X-Matrix according to the rules provided.

1. To check if each diagonal element is non-zero, we start with the first element on the main diagonal, `grid[0][0]`, which is `2`. It's non-zero, so we proceed.
2. Checking the next main diagonal element, `grid[1][1]`, we find a `4`. It's also non-zero, so we continue.
3. Checking the last element on the main diagonal, `grid[2][2]`, we see a `5`. It's non-zero as well, hence the main diagonal condition is satisfied.
4. Next, we move to the anti-diagonal. We start with `grid[0][2]`, which is `3`, and then `grid[1][1]` (which we've already checked), and finally `grid[2][0]`, which is `1`. All these elements are also non-zero, satisfying the anti-diagonal condition.
5. None of the diagonal elements are zero, so the first condition for an X-Matrix is met.
6. Now we check all other elements, which should all be zero. We review `grid[0][1]`, `grid[1][0]`, `grid[1][2]`, and `grid[2][1]`. They are all zero, as required.
7. Since we have verified that all diagonal elements are non-zero and all other elements are zero, we confirm that the matrix is an X-Matrix. Therefore, the function would return `true`.

In this example, we've walked through the matrix and checked both conditions specified for an X-Matrix. The matrix given fulfills both conditions, so it is indeed an X-Matrix.

## Python Solution

```
1 class Solution:
2     def checkXMatrix(self, grid: List[List[int]]) -> bool:
3         n = len(grid) # The dimension of the square grid
4         # Iterate through each element of the grid
5         for i in range(n):
6             for j in range(n):
7                 # Check if we are on the main or secondary diagonal
8                 if i == j or i + j == n - 1:
9                     # If the value on the diagonal is 0, the condition fails
10                    if grid[i][j] == 0:
11                        return False
12                else:
13                    # If the value is not on the diagonal and is not 0, the condition fails
14                    if grid[i][j] != 0:
15                        return False
16            # If all conditions are satisfied, return True
17        return True
18
```

## Java Solution

```
1 class Solution {
2
3     // Function to check if the given grid forms an X-Matrix
4     public boolean checkXMatrix(int[][] grid) {
5         // Get the length of the grid (since it's an N x N matrix)
6         int n = grid.length;
7
8         // Loop through each element of the grid
9         for (int i = 0; i < n; ++i) {
10            for (int j = 0; j < n; ++j) {
11                // Check the diagonal and anti-diagonal
12                if (i == j || i + j == n - 1) {
13                    // On the diagonals, all elements should be non-zero
14                    // If a zero is found, the grid is not an X-Matrix
15                    if (grid[i][j] == 0) {
16                        return false;
17                    }
18                } else {
19                    // For all other positions (off the diagonals), elements should be zero
20                    // If a non-zero number is found, the grid is not an X-Matrix
21                    if (grid[i][j] != 0) {
22                        return false;
23                    }
24                }
25            }
26        }
27
28        // If all conditions are met, then it's an X-Matrix
29        return true;
30    }
31 }
32
```

## C++ Solution

```
1 class Solution {
2 public:
3     // Function to check if a given grid forms an X-Matrix
4     bool checkXMatrix(vector<vector<int>>& grid) {
5         // Get the size of the grid
6         int n = grid.size();
7
8         // Iterate over each element in the grid
9         for (int i = 0; i < n; ++i) {
10            for (int j = 0; j < n; ++j) {
11                // Check the diagonals: primary (i == j) and secondary (i + j == n - 1)
12                if (i == j || i + j == n - 1) {
13                    // If an element on the diagonal is zero, the grid does not form an X-Matrix
14                    if (grid[i][j] == 0) {
15                        return false;
16                    }
17                }
18                // Check the elements that are not on the diagonals
19                else {
20                    // If an off-diagonal element is not zero, the grid does not form an X-Matrix
21                    if (grid[i][j] != 0) {
22                        return false;
23                    }
24                }
25            }
26        }
27
28        // Return true if all diagonal elements are non-zero and all off-diagonal elements are zero
29        return true;
30    };
31 }
```

## Typescript Solution

```
1 // Function to check if a given 2D grid forms an X-Matrix.
2 // An X-Matrix has non-zero integers on both its diagonals,
3 // and zeros on all other positions.
4 function checkXMatrix(grid: number[][]): boolean {
5     // Get the size of the grid.
6     const size = grid.length;
7
8     // Loop over each element in the grid.
9     for (let row = 0; row < size; ++row) {
10        for (let col = 0; col < size; ++col) {
11            // Check the main diagonal and anti-diagonal elements
12            if (row === col || row + col === size - 1) {
13                // If any diagonal element is 0, return false.
14                if (grid[row][col] === 0) {
15                    return false;
16                }
17            } else {
18                // If any off-diagonal element is non-zero, return false.
19                if (grid[row][col] !== 0) {
20                    return false;
21                }
22            }
23        }
24    }
25
26    // If no rule is violated, return true.
27    return true;
28 }
29
```

## Time and Space Complexity

The given code snippet is designed to check whether a given square 2D grid is an 'X-Matrix'. An 'X-Matrix' has non-zero elements on its diagonals and zero elements elsewhere.

### Time Complexity

To determine the time complexity, we look at the number of operations relative to the input size. The code iterates over every element in the `N x N` grid exactly once, performing a constant amount of work for each element by checking if it's on the diagonal or anti-diagonal and then validating the value. Therefore, the time complexity is  $O(N^2)$ , where `N` is the length of the grid's side.

### Space Complexity

The solution only uses a fixed number of variables (`i`, `j`, `v`) and does not allocate any additional space that grows with the input size. Hence, the space complexity is  $O(1)$  as it does not depend on the size of the input grid.