713. Subarray Product Less Than K

Sliding Window Medium <u>Array</u>

Problem Description

Given an array of integers nums and an integer k, the task is to find out how many contiguous subarrays (a subarray is a sequence of adjacent elements in the array) have a product of all its elements that is less than k. The integers in the array can be any integer and the order of the array must not be changed. The output should be the count of such subarrays.

Intuition

the right and multiplying them until the product of all elements in the window is less than k. When the product becomes equal or greater than k, we'll shrink the window from the left until the product is less than k again. As we slide the window to the right across the array, we can continuously make the window as large as possible such that its

To arrive at the solution, we can think about a sliding window approach. We keep expanding our window by adding elements from

product is less than k. For each position i, if the product of the window s of elements to the left (up to j) is less than k, then adding the element at i can form i - j + 1 new subarrays with products less than k (each subarray ending at i and starting at any of the elements between i and j, inclusive).

The intuition behind while calculating i - j + 1, is that for each new element added to the window (when i is increased), we add all the possible subarrays that end with that element. For example, if our window includes elements nums[3], nums[4], nums[5], and we now include nums[6], then we can form the subarrays [nums[6]], [nums[5], nums[6]], [nums[4], nums[5], nums[6]], and

optimizing the entire process. Solution Approach

By using this approach, we can avoid recalculating the product of subarrays that have already been considered, therefore

The solution approach uses a sliding window technique to find contiguous subarrays that meet the product requirement. Here's

[nums[3], nums[4], nums[5], nums[6]].

how it breaks down: Initialization: We start with initializing three variables - ans, s, and j.

- s is used to maintain the product of the elements within the current window and is initialized to 1.
- j represents the start of the <u>sliding window</u>, and it's initialized to 0. Traversing the Array: We traverse the array using variable i, which acts as the end of the sliding window. For each element,

o ans will hold the final count of the number of subarrays whose product is less than k and is initialized to 0.

subarrays that can be formed with the current end-point i. This is done by calculating i - j + 1:

- we do the following:
- Multiply s by the current element v (the product of the window). Adjusting the Window: If the product s becomes greater than or equal to k, we need to shrink our window from the left. We
- do this in a while loop, which continues until the product s is smaller than k:

subarrays that meet the condition.

within it while keeping the product under k.

- Divide s by the value at the start of the window, nums[j], to remove it from the product. Move the start of the window to the right by incrementing j. Counting Subarrays: After adjusting the window such that the product s is less than k, we count the number of new
- the new element must be counted. These subarrays are all unique for this particular position of i. Accumulating the Answer: The number calculated from the step above is added to ans, accumulating the count of all valid

∘ The reason behind i - j + 1 is that each time the right end of the window moves (when i increases), all possible subarrays that end with

Returning the Result: Finally, after the loop has traversed the whole array, the accumulated value in ans represents the total number of contiguous subarrays where the product of all the elements is strictly less than k, and we return this value.

O(N), where N is the number of elements in the array. The sliding window efficiently keeps track of the product of elements

This approach ensures that each element is added and removed from the product at most once, leading to a time complexity of

Example Walkthrough Let's walkthrough a small example to illustrate the solution approach.

Initialization: We start with ans = 0, s = 1, and j = 0.

Traversing the Array:

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■ Counting Subarrays: i - j + 1 gives us 1 - 0 + 1 = 2, but the only valid subarray is [10]. So, ans = ans + 1 = 1.
\circ i = 1: We have the element 5 and s = s * 5 = 50 which is still less than k.
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Suppose we have nums = [10, 5, 2, 6] and k = 100.

less than 100.

product less than k = 100.

 \circ i = 2: We have the element 2 and s = s * 2 = 100 which is not less than k. Time to adjust the window. - Adjusting the Window: Since s >= k, we divide s by nums[j]. So, s = s / 10 = 10, and j = j + 1 = 1. ■ We multiply s by 2 again as our window had shrunk. Now s = 20.

product *= value # Update the product with the current value

When the product is equal or greater than k, divide it by the

// Return the total count of subarrays where the product is less than 'k'.

// Function to count the number of continuous subarrays

// Initialize the answer to 0

product *= nums[right];

int numSubarrayProductLessThanK(vector<int>& nums, int k) {

// Initialize two pointers defining the sliding window

// While the product is equal to or larger than k,

// increment the left pointer to reduce the product

// i is the right pointer, j is the left pointer,

// where the product of all elements in the subarray is less than k

// and product keeps the product of all elements within the window

// Update the product by multiplying the rightmost element

for (int right = 0, left = 0, product = 1; right < nums.size(); ++right) {</pre>

starting value and increment the start_index to reduce the window size

 \circ i = 0: We have the element 10 and s = s * 10 = 10 which is less than k. No need to adjust the window.

- Counting Subarrays: i j + 1 gives us 3 1 + 1 = 3. The new valid subarrays are [2], [5, 2]. So ans = ans + 2 = 5.
 - \circ i = 3: We have the element 6 and s = s * 6 = 120 which is not less than k. ■ Adjusting the Window: We continue to shrink the window. s = s / 5 = 24, and j = j + 1 = 2.

■ Counting Subarrays: i - j + 1 gives us 2 - 0 + 1 = 3. The new valid subarrays are [5], [10, 5]. So, ans = ans + 2 = 3.

- Counting Subarrays: i j + 1 gives us 4 2 + 1 = 3. The new valid subarrays are [6], [2, 6]. So, ans = ans + 2 = 7. **Returning the Result**: After traversing the whole array, ans = 7, which is the count of contiguous subarrays with a product
- So, by following the algorithm's steps, we can determine that there are seven contiguous subarrays within nums that have a
- Solution Implementation

Python

def numSubarrayProductLessThanK(self, nums: List[int], k: int) -> int: # Initialize count of subarrays, product of elements, and the start index count_subarrays = 0 product = 1

start index = 0

from typing import List

class Solution:

```
# Iterate over the list using index and value
for end_index, value in enumerate(nums):
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while start_index <= end_index and product >= k:
                product //= nums[start index]
               start_index += 1
           # Calculate the new subarrays with the current element
            # Here, (end_index - start_index + 1) gives the count of subarrays ending with nums[end_index]
            count_subarrays += end_index - start_index + 1
       # The final result is the count of subarrays satisfying the condition
       return count_subarrays
Java
class Solution {
    public int numSubarrayProductLessThanK(int[] nums, int k) {
       int count = 0; // Initialize the count of subarrays
       // Initialize 'start' and 'end' as the current window's start and end indices,
       // and 'product' as the product of the elements within the window.
        for (int start = 0, end = 0, product = 1; end < nums.length; end++) {</pre>
           // Multiply the product by the current element.
           product *= nums[end];
           // While the product is not less than 'k' and 'start' is not beyond 'end'...
           while (start <= end && product >= k)
                // ...divide the product by the 'start' element and move the start forward.
                product /= nums[start++];
           // Add to count the number of subarray combinations with the current 'end'.
           // This is found by subtracting 'start' from 'end' and adding 1.
            count += end - start + 1;
```

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C++
class Solution {
```

public:

return count;

int count = 0;

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// and contract the window size from the left
           while (left <= right && product >= k) {
                product /= nums[left++];
            // The number of subarrays with a product less than k
           // that end with nums[right] is equal to the size of the current window
            count += right - left + 1;
       // Return the total count
        return count;
};
TypeScript
function numSubarrayProductLessThanK(nums: number[], k: number): number {
    let count = 0; // Initialize the count of subarrays
    let product = 1; // Initialize the product of the current subarray
    let left = 0; // Left index of the sliding window
    // Process all numbers in the input array
    for (let right = 0; right < nums.length; ++right) {</pre>
       // Accumulate the product of the elements within the sliding window
       product *= nums[right];
       // If the product is greater than or equal to k,
       // shrink the window from the left
       while (left <= right && product >= k) {
            product /= nums[left++];
       // Add the number of subarrays ending at 'right' that have a product less than k
       // This step utilizes the idea that if 'right' is the end of a valid subarray,
       // then there are 'right - left + 1' possible starting positions for subarrays
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count += right - left + 1;

```
// Return the total count of subarrays
      return count;
from typing import List
class Solution:
   def numSubarrayProductLessThanK(self, nums: List[int], k: int) -> int:
       # Initialize count of subarrays, product of elements, and the start index
        count_subarrays = 0
       product = 1
        start_index = 0
       # Iterate over the list using index and value
        for end index, value in enumerate(nums):
           product *= value # Update the product with the current value
           # When the product is equal or greater than k, divide it by the
           # starting value and increment the start_index to reduce the window size
           while start_index <= end_index and product >= k:
               product //= nums[start_index]
               start_index += 1
           # Calculate the new subarrays with the current element
           # Here, (end_index - start_index + 1) gives the count of subarrays ending with nums[end_index]
           count subarrays += end index - start index + 1
       # The final result is the count of subarrays satisfying the condition
        return count_subarrays
Time and Space Complexity
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The provided code implements a two-pointer approach to find the number of contiguous subarrays where the product of all elements in the subarray is less than k.

Time Complexity

The time complexity of the code is O(n), where n is the number of elements in the input list nums. This is because there is a single

loop over the elements, and within this loop, there is a while loop. However, the inner while loop does not result in a time complexity greater than O(n) since each element is visited at most twice by the pointers — once by the outer loop and at most once by the j pointer moving forward. Every element is processed by the inner loop only once when the product exceeds k, and after it's processed, the j pointer does not go back. **Space Complexity**

The space complexity of the code is 0(1). This is because the space used does not grow with the size of the input nums. Instead,

only a fixed number of integers (ans, s, j, i, v) are used to keep the state of the algorithm, which occupies constant space.