Problem Description

consists only of '0's and '1's. We also have two integer constraints, m and n, which are the maximum number of '0's and '1's allowed in our subset, respectively.

In this problem from LeetCode, we are tasked with finding the largest subset of binary strings from a given array strs. A binary string

A subset means every element in our selected group of strings must also exist in the original group (strs), but not necessarily all

The key part to understand here is:

- elements in strs have to be in our subset. When creating the largest subset, the total count of '0's in all the strings of our subset cannot exceed m, and the total count of
- '1's cannot exceed n. Our goal is to identify the size of this largest subset. Size means the number of strings within it, not the length of each string.

Intuition

To solve this problem, we use a dynamic programming approach.

1. We start by understanding that the choice of including each string can affect our ability to include other strings. If we include a string with many '0's and '1's, it may prevent us from adding additional strings later. Thus, we have to make careful choices.

- 2. Generally, in dynamic programming, we try to solve smaller subproblems and use their results to construct solutions for larger subproblems. This concept is called optimal substructure.
- 3. Here, we define a two-dimensional array f where f[i][j] represents the size of the largest subset we can form with at most i
- '0's and j '1's. The values of i range from 0 to m, and the values of j range from 0 to n, representing all possible constraints we might encounter.
- manner, starting from m to the count of '0's in the current string (a) and from n to the count of '1's (b). 6. While updating, we consider two cases for each cell f[i][j]:

5. We iterate through each string in strs and count its '0's and '1's. Then, for each string, we update our array f in a decreasing

Not including the current string, which means the f[i][j] would remain unchanged.

4. We initialize our array with zeros, as the largest subset with zero '0's and '1's is an empty subset, hence zero size.

 Including the current string, where we have to look at the value in the cell that represents the leftover capacity (f[i - a][j b]) after including this string and add 1 to that value to represent the current string being counted.

7. We choose the maximum of these two choices at every step, which ensures that we always have the largest possible subset for

conforming to our constraints. This dynamic programming solution is efficient as it avoids recalculating the largest subset sizes for every combination of '0's and

8. After iterating through all strings and updating the array, the value of f[m] [n] will give us the size of the largest subset

Solution Approach

The implementation of the solution follows the dynamic programming approach to methodically work towards the final answer. Here's an in-depth walk-through of the pattern and the algorithm used:

used to include the case where 0 '0's or '1's are used. 2. Initialization: The two-dimensional list f is initialized with zeroes, since the largest subset without considering any strings (and

our subset.

a given i and j.

'1's by building upon previously computed values.

thus having 0 '0's and 1's) has a size of 0`. 3. Counting '0's and '1's: For each string s in strs, s.count("0") and s.count("1") are called to count the number of '0's (a) and

1. Data Structure: A two-dimensional list f is created with dimensions (m + 1) x (n + 1). In Python, this is realized as a list of

lists. Each cell f[i][j] in this array represents the size of the largest subset with i '0's and j '1's. The + 1 in both dimensions is

- '1's (b) respectively. 4. Updating the DP Table: We iterate over the list in reverse for i from m to a - 1 and j from n to b - 1. We do this because we want to make sure that when we account for a new string, we are not overwriting cells that could affect the calculation of cells
- 5. Choice: At each cell f[i][j], we attempt to include the current string. To do this, we compare the existing value f[i][j] (not including the current string) with f[i - a][j - b] + 1 (including the string). f[i - a][j - b] represents the largest subset

possible with the remaining capacity after including the current string. We add 1 because we are including the current string in

later in the iteration. This is a common technique in dynamic programming known as avoiding "state contamination."

6. Taking the Maximum: We use Python's max function to always store the maximum of the two values. Thus, f[i][j] will always hold the size of the largest subset for the specific capacity represented by i and j. 7. Result: After completely filling the two-dimensional list, f[m] [n] will give us the maximum size of our desired subset since it

represents the size of the largest subset under the full capacity of m '0's and n '1's.

problems by relying on the solutions to smaller problems) and overlapping subproblems (saving computation by storing intermediate results). The use of a two-dimensional DP table is crucial, as it allows tracking the state of the problem (how many '0's and '1's can

This implementation successfully leverages the central ideas of dynamic programming, namely optimal substructure (solving bigger

1. Initialization: We create a two-dimensional list f with dimensions $(m + 1) \times (n + 1)$, so f would be a 6×4 matrix, as we include zero counts. It's filled with zeros, like so:

Assume we have the following array of binary strings strs: ["10", "0001", "111001", "1", "0"], and our integer constraints are m =

[0, 0, 0, 0], [0, 0, 0, 0], [0, 0, 0, 0],

[0, 1, 1, 1],

[0, 1, 1, 1],

[0, 1, 1, 1],

[0, 1, 1, 1]

[0, 0, 0, 0],

[0, 1, 1, 1],

[1, 1, 2, 2],

[1, 2, 2, 2],

[1, 2, 3, 3],

[1, 2, 3, 4]

Python Solution

class Solution:

from typing import List

for s in strings:

return dp[max_zeros][max_ones]

the max value for each cell.

[0, 0, 0, 0],

[0, 0, 0, 0],

1 f = [

still be included) at each step.

Example Walkthrough

[0, 0, 0, 0]

Let's take a small example to illustrate the solution approach.

5 and n = 3. This means we cannot have more than 5 '0's and 3 '1's in our subset.

2. Counting and updating: We go through each string in strs and update our DP table.

and j = 3 to 1, comparing the existing value f[i][j] with f[i - 1][j - 1] + 1 (since a=1 and b=1).

∘ For the string "10", we have a=1 (the number of '0's) and b=1 (the number of '1's). We update cells in the range of i = 5 to 1

After this string, our DP table update looks like this: 1 f = [[0, 0, 0, 0], // No strings considered yet

Applying a similar process for other strings: "0001", "111001", "1", and "0", updating f for the '0's and '1's in each and choosing

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3. Final DP Table: Once we process all strings, our DP table will display the maximum number of strings that can be included for a
   given i number of '0's and j number of '1's. For our case, we getf[m] [n] as the result. Let's assume our final table after all
   updates looks like this:
1 f = [
```

[0, 1, 1, 1], // '10' considered for i=1 (up to 1 '0's used)

4. Result: From the last entry f[5][3], we see that the maximum size of the subset we can get under the given constraints is 4.

Thus, with m = 5 and n = 3, we are able to include four strings from the array strs in our subset without exceeding the number of

'0's and '1's allowed. The subset, in this case, could be ["10", "0001", "1", "0"], which includes 4 strings, adheres to the

constraints (`5 '0's and 3 '1's), and is the largest possible subset for these constraints.

def findMaxForm(self, strings: List[str], max_zeros: int, max_ones: int) -> int:

Count the number of zeros and ones in the current string

The answer is the value corresponding to using maximum zeros and ones

// The main function to find maximum number of strings that can be formed with m zeros and n ones

// Increment the respective count (0 or 1) based on the current character

 $dp = [[0] * (max_ones + 1) for _ in range(max_zeros + 1)]$

zero_count, one_count = s.count("0"), s.count("1")

Iterate through each string in the input list

// Iterate through the characters of the string

for (int i = 0; i < s.length(); ++i) {</pre>

++count[s.charAt(i) - '0'];

// Return the count array

return count;

Initialize the DP table with dimensions (max_zeros + 1) by (max_ones + 1)

Iterate over the DP table in reverse to avoid using a result before it's updated for zeros in range(max_zeros, zero_count - 1, -1): for ones in range(max_ones, one_count - 1, -1): # Update the DP table value for the current subproblem dp[zeros][ones] = max(dp[zeros][ones], dp[zeros - zero_count][ones - one_count] + 1)

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Java Solution

public class Solution {

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```
public int findMaxForm(String[] strs, int m, int n) {
           // Initialize a DP table where f[i][j] will represent the max number of strings that can be formed with i zeros and j ones
           int[][] dp = new int[m + 1][n + 1];
           // Iterate through each string in the input list
           for (String s : strs) {
               // Count the number of zeros and ones in the current string
10
               int[] count = countZerosAndOnes(s);
               // Loop over the dp array from bottom up considering the current string's zeros and ones
13
               for (int i = m; i >= count[0]; --i) {
14
                    for (int j = n; j >= count[1]; --j) {
15
                        // Update the dp value with the higher value between the current and the new computed one
16
                        dp[i][j] = Math.max(dp[i][j], dp[i - count[0]][j - count[1]] + 1);
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           // Return the result from the DP table which is the maximum number of strings that can be formed
23
           return dp[m][n];
24
25
26
       // Helper function to count the number of zeros and ones in a string
27
       private int[] countZerosAndOnes(String s) {
28
           // Initialize a count array where the first element is the number of zeros and the second is the number of ones
29
           int[] count = new int[2];
```

C++ Solution

```
1 #include <vector>
 2 #include <string>
 3 #include <algorithm>
   #include <cstring> // For memset
   using namespace std;
   class Solution {
   public:
        int findMaxForm(vector<string>& strs, int m, int n) {
10
           // Create a 2D array (dp) with dimensions m+1 and n+1
11
12
           // Initialize all elements to zero
           int dp[m + 1][n + 1];
13
14
           memset(dp, 0, sizeof(dp));
15
16
           // Iterate over each string in the given vector 'strs'
            for (auto& str : strs) {
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18
                // Count the number of zeroes and ones in the current string
                pair<int, int> zeroOneCount = countZeroesAndOnes(str);
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                int zeroes = zeroOneCount.first;
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                int ones = zeroOneCount.second;
22
23
                // Iterate over the matrix in reverse, to avoid over-counting
24
                // when using previously computed sub-solutions
25
                for (int i = m; i >= zeroes; --i) {
26
                    for (int j = n; j >= ones; --j) {
27
                        // Update the dp matrix by taking the maximum between:
28
                        // 1. Current cell value (previous computed max)
                        // 2. Value computed by including the current string
29
                        // Add 1 to the subproblem solution because
30
31
                        // we are including one more string
                        dp[i][j] = max(dp[i][j], dp[i - zeroes][j - ones] + 1);
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36
           // Return the maximum number of strings that can be formed
            // with given 'm' zeroes and 'n' ones
37
38
            return dp[m][n];
39
40
41
   private:
42
       // Helper function to count the number of zeroes and ones in a string
43
        pair<int, int> countZeroesAndOnes(string& str) {
44
            int countZeroes = count_if(str.begin(), str.end(), [](char c) { return c == '0'; });
45
           // First of the pair is number of zeroes, second is the number of ones
46
            // Since the total length minus zeroes gives the number of ones
47
            return {countZeroes, static_cast<int>(str.size()) - countZeroes};
48
49
   };
50
```

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Typescript Solution

```
function findMaxForm(strings: string[], zeroLimit: number, oneLimit: number): number {
       // Initialize a memoization table with dimensions (zeroLimit + 1) \times (oneLimit + 1).
       // This table will help us keep track of the maximum number of strings we can include
       // given a specific limit of zeroes and ones.
       const dpTable = Array.from({ length: zeroLimit + 1 }, () =>
5
           Array.from({ length: oneLimit + 1 }, () => 0)
6
       );
8
9
       // A helper function to count the number of zeroes and ones in a string.
       // It returns a tuple [zeroCount, oneCount].
10
       const countZeroesAndOnes = (str: string): [number, number] => {
11
12
           let zeroCount = 0;
           for (const char of str) {
               if (char === '0') {
                   zeroCount++;
16
17
18
           return [zeroCount, str.length - zeroCount];
       };
19
20
21
       // Iterate through each string in the input array.
22
       for (const str of strings) {
23
           // Count the number of zeroes and ones in the current string.
           const [zeroes, ones] = countZeroesAndOnes(str);
           // Update the dpTable in reverse to avoid overwriting data we still need to use.
           for (let i = zeroLimit; i >= zeroes; --i) {
28
               for (let j = oneLimit; j >= ones; --j) {
                   // The maximum number of strings that can be included is either the current count
                   // or the count obtained by including the current string plus the count of strings
                   // that can be included with the remaining zeroes and ones.
                   dpTable[i][j] = Math.max(dpTable[i][j], dpTable[i - zeroes][j - ones] + 1);
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36
37
       // The final result is stored in dpTable[zeroLimit][oneLimit], reflecting the maximum number
38
       // of strings we can include given the original zeroLimit and oneLimit.
       return dpTable[zeroLimit][oneLimit];
39
40 }
41
Time and Space Complexity
```

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Time Complexity: The time complexity of the given solution is 0(k * m * n), where k is the length of the input list strs, m is the maximum number of zeroes, and n is the maximum number of ones that our subsets from strs can contain. This complexity arises because we iterate

over all strings in strs, and for each string, we iterate through a 2D array of size m * n in a nested loop fashion.

Space Complexity:

The space complexity of the solution is 0(m * n), as we are constructing a 2D array f with m + 1 rows and n + 1 columns to store the intermediate results for dynamic programming. No other data structures are used that grow with the size of the input, so the space complexity is directly proportional to the size of the 2D array.