# 2140. Solving Questions With Brainpower

**Dynamic Programming** 

**Problem Description** 

<u>Array</u>

Medium

questions[i] represents a question described by two integers - points\_i and brainpower\_i. The first integer points\_i is the amount of points you'd earn by solving the ith question, and the second integer brainpower\_i is the number of subsequent questions you must skip if you decide to solve this question. The rules of the exam are such that you must make decisions on questions in order, deciding to either solve a question (earning

In this LeetCode problem, you are presented with a 0-indexed 2D integer array called questions, where each element

points and skipping the next brainpower\_i questions) or to skip it (allowing a decision on the next question). Your goal is to maximize the points you can earn by the end of the exam. To put it into a scenario, assume questions = [[3, 2], [4, 3], [4, 4], [2, 5]]:

Hence, you are looking for a strategy that allows you to accumulate the maximum number of points possible by the end of the

• However, if you skip the first question and solve the second one, you'll earn 4 points but will have to skip the last two questions.

exhaustively checking each combination, thereby arriving at an optimal solution.

Let's dissect the mostPoints function and the nested dfs function:

question, there are no more points to earn.

**Recursive Case**: At each question i, we consider two scenarios:

question and dfs(i + 1) represents the path where we skip it.

through the dynamic programming steps to find the maximum points:

Call dfs(0) to start the recursion with the first question.

■ The total score for this path is 2 + 5 = 7.

Move to dfs(3) which also returns 0 (base case).

Move to dfs(2) which, as already computed, gives 5 points.

The total score for this path remains 2 points.

■ Take the max for dfs(2) which is 7 points (solving question 2).

Skipping question 2:

Now compute dfs(1):

Solution Implementation

from typing import List

@lru\_cache(maxsize=None)

return 0

return dfs(0)

def dfs(index: int) -> int:

if index >= len(questions):

public long mostPoints(int[][] questions) {

private long dfs(int index) {

class Solution:

**Python** 

Java

Solving question 1:

maximum points starting from the first question.

the maximum score we can achieve from the exam.

If you solve the first question, you'll get 3 points but miss out on the next two questions.

- last question.
- Intuition To approach this problem, we need to think about each decision's consequences and explore different scenarios to come up with

the optimal strategy. The essence of the problem has us consider two options for each question i: solving or skipping it. When solving question i, we earn points[i] and skip the next brainpower[i] questions. If we skip it, we simply move on to making a

decision on the following question. A naive approach could involve trying all combinations of solving and skipping questions to find the optimal solution, but that would take an enormous amount of time for large arrays. Instead, we look for a <u>Dynamic Programming</u> (DP) approach that helps

us store the results of subproblems to avoid redundant calculations. The intuition behind the DP solution is to use recursion with memoization to keep track of the maximum points we can earn from

any question i onward. At each question, we consider the maximum points of two scenarios: if we solve this question or if we skip it. We use a recursive function that takes an index i and returns the maximum points starting from question i. The base case is

when we go beyond the last question, which earns us 0 points by default. By caching the results of our recursive calls, we greatly reduce the number of calculations, since we ensure that each subproblem is solved exactly once. This makes the solution time-efficient enough to handle large input sizes.

Therefore, the @cache decorator above the recursive function (called dfs in the code) plays a critical role in memoizing previously

computed results to speed up the recursive exploration. dfs(i) represents the maximum points we can earn starting from

question i. We take the max between solving the current question and proceeding with dfs(i + brainpower[i] + 1) and skipping the current question with dfs(i + 1). With this approach, we can ensure that we are considering every possible scenario and collecting the maximum points without

**Solution Approach** The solution is implemented using a recursive function with memoization, two key elements that are often utilized in dynamic programming solutions.

**<u>Dynamic Programming</u>** via Recursion: The dfs function embodies the concept of dynamic programming by breaking down the problem into smaller subproblems. At each step, we are essentially asking: "What's the maximum points I can get from

this question onwards?" This leads to a recursive relation because the answer to this question depends on the maximum

Memoization with @cache: The @cache decorator is a Python built-in decorator from the functools module that automatically

## points from subsequent questions.

saves the results of the dfs function calls into memory so that the next time the same function call is made with the same arguments, the cached result is returned immediately without recomputing. This feature helps in reducing the time complexity from exponential to polynomial.

Base Case: If i >= len(questions), the recursion stops (base case) and returns 0 because once we move past the last

• Solving the question: We earn points[i] and skip the next brainpower[i] questions. This is done by recursing with dfs(i + brainpower[i] + 1). • Skipping the question: We move to the next question by calling dfs(i + 1) without earning any points.

We take the max between these two scenarios. The call to dfs(i + b + 1) represents the path where we solve the current

**Recursion Stack**: Recursion uses a stack implicitly where each recursive call adds a frame to the stack. Once a call finishes, it

is removed from the stack and the function returns to the previous call. This means we explore each branch (solve or skip) one at a time while maintaining only the current path in the stack, which is a depth-first search pattern.

Starting the Recursion: After defining the dfs function, we initiate the recursion by calling dfs(0), which evaluates the

By combining these elements we arrive at an efficient solution that systematically explores each decision's consequences and

appropriately tabulates them to avoid unnecessary re-computation. The result is that the first call to dfs(0) will eventually give us

**Example Walkthrough** 

Let's illustrate the solution approach with a small example. Given the array questions = [[2, 1], [3, 1], [5, 2]], let's walk

Solving question 0: ■ Earn 2 points and move to dfs(0 + brainpower[0] + 1) which is dfs(2). ■ Now compute dfs(2): Solving question 2:

■ Earn 5 points. There's no question 3, so dfs(2 + brainpower[2] + 1) is dfs(5) which returns 0 (base case).

Skipping question 0: ■ Move to dfs(0 + 1) which is dfs(1).

Compute dfs(0):

The total score for this path is 3 points. Skipping question 1:

The total score for this path is 5 points.

of questions by optimally choosing whether to solve or skip each of them.

from functools import lru\_cache # Importing `lru\_cache` for memoization

# Use lru\_cache to memoize the recursive function results for efficiency

# Base case: If the index is beyond the questions list, no points can be earned

def mostPoints(self, questions: List[List[int]]) -> int:

The total score for solving question 0 is 7 points.

■ Take the max for dfs(1) which is 5 points (skipping question 1). ■ The total score for skipping question 0 is 5 points. Take the max between solving (dfs(0) = 7) and skipping (dfs(0) = 5) the first question, which is 7 points.

The recursive calls, leveraging memoization, ensure that dfs(2) is not recomputed when accessed through different paths.

At the end of this process, dfs(0) returns the answer, which is 7 points - the maximum number of points we can earn for this set

■ Earn 3 points and move to dfs(1 + brainpower[1] + 1) which is dfs(3) and returns 0.

- # Unpack points (p) and bonus (b) from the current question points, bonus = questions[index] # Recursive case: Choose the maximum between two options: # 1. Earning points for the current question and jumping over the bonus questions
- class Solution { private int numQuestions; // Total number of questions private Long[] memoization; // Cache to store solutions to sub-problems private int[][] questionsData; // 2D array representing questions and their points/bonus

numQuestions = questions.length; // Initialize number of questions

memoization = new Long[numQuestions]; // Initialize the cache array

questionsData = questions; // Reference to the original questions array

return dfs(0); // Start the depth-first search from the first question

// Recursive method using Depth-First Search to calculate the maximum points

int points = questionsData[index][0]; // Points for the current question

return 0; // No more points can be earned, return 0

// Start the calculation from the first question

return calculatePoints(0);

function mostPoints(questions: number[][]): number {

const numQuestions = questions.length;

if (index >= numQuestions) {

return 0;

return findMaxPoints(0);

if (memo[index] > 0) {

return memo[index];

if index >= len(questions):

points, bonus = questions[index]

return 0

return dfs(0)

one.

Time and Space Complexity

const memo = Array(numQuestions).fill(0);

// n represents the total number of questions.

const findMaxPoints = (index: number): number => {

const [points, bonus] = questions[index];

// Calculate the maximum points by choosing either:

// Start finding maximum points from the first question.

from functools import lru\_cache # Importing `lru\_cache` for memoization

# Unpack points (p) and bonus (b) from the current question

# Recursive case: Choose the maximum between two options:

return max(points + dfs(index + bonus + 1), dfs(index + 1))

# 2. Skipping the current question to try the next one

# Start the depth-first search from the first question (index 0)

The time complexity of the code primarily depends on two factors:

// 2. Skipping the current question and checking the next question.

**}**;

**TypeScript** 

return memoization[index]; // Return the cached result

# 2. Skipping the current question to try the next one

# Start the depth-first search from the first question (index 0)

return max(points + dfs(index + bonus + 1), dfs(index + 1))

// Public method to start the process and return the maximum points that can be obtained

if (index >= numQuestions) { // Base case: if the index exceeds the number of questions

if (memoization[index] != null) { // If the result for this index is already computed

```
int bonus = questionsData[index][1]; // Bonus (number of questions to skip) for the current question
       // Recur in two scenarios: either answer the current question and jump over the bonus questions,
       // or move to the next question. Take the maximum of these two choices.
       return memoization[index] = Math.max(points + dfs(index + bonus + 1), dfs(index + 1));
C++
#include <vector> // Include for using vectors
#include <cstring> // Include for using memset
class Solution {
public:
    long long mostPoints(std::vector<std::vector<int>>& questions) {
        int numQuestions = questions.size(); // Get the total number of questions
        std::vector<long long> dp(numQuestions, 0); // Dynamic programming array to store the max points upto each question
       // Function to recursively calculate the max points starting from question i
        std::function<long long(int)> calculatePoints = [&](int index) -> long long {
           // If the question index is beyond the number of questions, return 0 as there are no more points to collect
            if (index >= numQuestions) {
               return OLL;
           // If we have already calculated the result for this index, use it and avoid recomputation
           if (dp[index] != 0) {
               return dp[index];
           // Points for current question and break before next question can be taken
           int points = questions[index][0], breakTime = questions[index][1];
           // Recursively calculate the max points by taking this question or skipping to the next
            dp[index] = std::max(points + calculatePoints(index + breakTime + 1), calculatePoints(index + 1));
            return dp[index];
       };
```

// Create an array 'memo' to store the maximum points that can be obtained starting from each question.

// If we have gone past the last question, no points can be scored, return 0.

// If we have already computed the answer for this question, return the stored result.

// 1. Solving the current question and adding the result of the next available question.

# Base case: If the index is beyond the questions list, no points can be earned

# 1. Earning points for the current question and jumping over the bonus questions

// Define a recursive function 'findMaxPoints' to find the maximum points from a given question index 'index'.

// Extract the points 'points' and the bonus 'bonus' for skipping questions from the current question.

return (memo[index] = Math.max(points + findMaxPoints(index + bonus + 1), findMaxPoints(index + 1)));

### class Solution: def mostPoints(self, questions: List[List[int]]) -> int: # Use lru\_cache to memoize the recursive function results for efficiency @lru\_cache(maxsize=None) def dfs(index: int) -> int:

from typing import List

**}**;

solve a dynamic programming problem. It involves making a decision at each question whether to solve it or to skip to the next **Time Complexity** 

The given Python function mostPoints uses memoization (@cache) to optimize the recursive depth-first search (dfs) function to

### current question and jumping to the one after the bonus, or moving to the next question directly. Each state of the dfs function is uniquely defined by the index i of the current question, and since each question gives us two

choices, in the worst case, the function could be called for every index from 0 to n-1. However, due to memoization, each state is only computed once, and subsequent calls for the same state i return the cached result. Therefore, the time complexity is O(n).

1. The number of subproblems to solve, which is O(n), where n is the number of questions.

**Space Complexity** The space complexity is determined by:

1. The space used by the recursion stack, which, in the worst case, could be O(n) if we go question by question without jumping through bonuses.

2. The computation done for each subproblem, which is in this case 0(1) since we are only making a choice between two options: solving the

Since these two factors are additive, the total space complexity is O(n) as well. Each question index i is visited only once due to caching, which stores a constant amount of information (the maximum points from that question to the end).

2. The space used by the memoization cache, which stores a result for each subproblem, resulting in O(n) space.

In conclusion, both the time complexity and the space complexity of the mostPoints function are O(n).