2320. Count Number of Ways to Place Houses

Medium **Dynamic Programming**

Problem Description

ways to build houses on these plots with the constraint that no two houses can be adjacent to each other on the same side of the street. Interestingly, if a house is built on one side of a plot, it's still allowed to build another directly across from it on the other side of the street. The final answer to the number of ways to arrange houses should be provided modulo 10^9 + 7 to keep the numbers manageable, due to potentially large results for big values of n.

Imagine a street that has n plots on each side, making a total of n * 2 plots. The task is to determine the number of different

The solution uses dynamic programming to solve the problem efficiently. To understand the intuition behind this approach, let's

Intuition

choices: either to place a house on it or not. If you choose to place a house, the next plot cannot have a house because of the no-adjacent-houses rule. Conversely, if you choose not to place a house, you are free to place a house on the next plot. We can define two states expressed as arrays f and g, where f[i] represents the number of ways to place houses up to plot i with a house on the ith plot, and g[i] represents the number of ways to place houses up to plot i without a house on the ith

consider the subproblem of deciding whether to place a house on a plot. When you're considering a new plot, you have two

plot. These states are dependent on the previous states: • f[i] relies on g[i-1] since a house on plot i means the i-1th plot cannot have a house. • g[i] combines f[i-1] and g[i-1] because plot i being empty allows for either a house or no house on the i-1 th plot.

placements on one side of the street is the sum of f[-1] and g[-1].

The solution iterates through each plot, updating these states according to the rules established, and takes the modulo 10**9 + 7 to ensure the answer remains in the required bounds. With the values for the final plot calculated, the total number of house

again modulo 10***9 + 7, to account for all combinations on both sides of the street. **Solution Approach**

Since the problem allows for independent house placement on either side of the street, the final answer is the square of this sum,

The solution implements a form of <u>dynamic programming</u>, which is an optimization over plain recursion where subproblems are solved once and stored for future use, thus avoiding the recomputation of the same subproblems. The dynamic programming

approach used here is tabulation, where we iteratively calculate and store the solution to each subproblem in a bottom-up

fashion. In this case, the subproblems are the number of ways to place houses up to a certain plot without violating the "no

adjacent houses" rule.

The code uses two lists, f and g, as mentioned before: • f is initialized with n elements, all set to 1, representing that there is initially one way to arrange a house on the ith plot. f[0] is always 1 because placing a house on the first plot obviously has no restrictions from previous plots. • g is also initialized with n elements, all set to 1, because at the beginning there is also one way to have a plot without a house on it. The core logic of the problem is encapsulated in the for-loop:

f[i] is updated to g[i - 1]. This captures the idea that if there is a house on the ith plot, then there could not have been

one on the i-1th plot, and the number of ways to reach this state is exactly the number of ways to reach plot i-1 without a

g[i] is updated to (f[i-1] + g[i-1]) % mod. Here, if the ith plot does not have a house, we are free to choose

house.

programming to find the count of all possible ways to build houses according to the given rules:

Next, we iterate through the plots one by one and use the given relations to update f[i] and g[i].

whether we had a house on the i-1th plot or not, and the total number of ways to arrange houses up to the ith plot is the sum of both possibilities.

After the loop ends, you have the total count of placements for a side street stored in f[n - 1] and g[n - 1]. Since we can

combine any arrangement on one side of the street with any arrangement on the other side, the total number of arrangements is

the square of the sum of f[n-1] and g[n-1]. This value is calculated as v * v % mod, where v is f[-1] + g[-1], and mod

This approach efficiently calculates the solution in O(n) time, as it only involves a single pass through the plots, and in O(n) space, due to the storage required for the f and g arrays. **Example Walkthrough**

We start by initializing the arrays f and g with 3 elements each, set to 1, since there's initially one way to have a house or not have a house on every plot. Hence, f = [1, 1, 1] and g = [1, 1, 1].

Let's illustrate the solution approach with a street that has n = 3 plots on each side. Here's how we would use dynamic

• We update f[1] to g[0], which is 1, because if we put a house on the second plot, we can't have had a house on the first plot.

When i = 1 (second plot):

to take modulo $10^9 + 7$.

the last plot is empty.

the last plot is occupied.

f = [1] * n

g = [1] * n

v = f[-1] + g[-1]

return (v * v) % MOD

// Base cases

public int countHousePlacements(int n) {

for (int i = 1; i < n; ++i) {

Python

is 10**9 + 7.

When i = 2 (third plot): o f[2] becomes g[1], which is 2, signifying that if we build on the third plot, we must not have built on the second.

• We update g[1] to (f[0] + g[0]) % mod, which is (1 + 1) % mod, resulting in 2, because if we don't put a house on the second plot, we

o g[2] becomes (f[1] + g[1]) % mod, which is (1 + 2) % mod, resulting in 3. This accounts for the scenarios where the second plot was either empty or had a house, affecting the possibilities for the third plot. Now f = [1, 1, 2] and g = [1, 2, 3].

For the final count on one side of the street, we add the last elements of f and g, resulting in 2 + 3 = 5, meaning there are

For both sides of the street, we take this result and square it, giving us the final answer: 5 * 5 = 25. But we must remember

The calculations above simply illustrate the process. For different values of n, we would run the exact same process and

could have either had a house or not had a house on the first plot.

5 unique ways to place houses along one side of a 3-plot street.

f represents the count of ways to place houses such that

q represents the count of ways to place houses such that

v is the total number of ways to place houses on the last plot.

we square the number of ways to find the total combinations.

We return the result modulo MOD to handle large numbers.

// Fill in the arrays using dynamic programming approach

// Calculate the total number of ways for all positions

return (int) (totalWays * totalWays % MODULO);

long totalWays = (place[n - 1] + noPlace[n - 1]) % MODULO;

// Base case for the DP, 1 way to place on 0th index for both situations

// Define the modulo constant for the final result to prevent overflow

const totalCount = emptyPlotCounts[n - 1] + housePlotCounts[n - 1];

// We must cast BigInt result back to a number before returning

q represents the count of ways to place houses such that

If the last plot is occupied, it can come after either

Iterate over the plots starting from the second one.

an empty plot or another occupied plot.

g[i] = (f[i - 1] + g[i - 1]) % MOD

// The square comes from calculating the same for both sides of the street

// Count for the current plot being empty depends on the previous plot having a house

housePlotCounts[i] = (emptyPlotCounts[i - 1] + housePlotCounts[i - 1]) % mod;

If the last plot is empty, then it must come after an occupied plot.

// Count for the current plot having a house depends on the previous plot being either empty or having a house

// Calculate final value from both arrays, representing both placing or not placing a house on the last plot

// Populate both arrays using dynamic programming approach

emptyPlotCounts[i] = housePlotCounts[i - 1];

// Return the total number of ways squared modulo mod

return Number(totalCount ** 2n % mod);

the last plot is occupied.

for i in range(1, n):

f[i] = g[i - 1]

def countHousePlacements(self, n: int) -> int:

// 'n' is a BigInt literal (ES2020+ feature)

const mod = BigInt(10 ** 9 + 7);

for (let i = 1; i < n; ++i) {

emptyPlotCounts[0] = housePlotCounts[0] = 1n;

Since we can independently choose how to place houses on each side of the street,

final int MODULO = 1 000 000 007; // Define a constant for the modulo value

place[0] = 1; // Only one way to not place a house at the first position

noPlace[0] = 1; // Only one way to place a house at the first position

Solution Implementation

compute the final count accordingly. Every step carefully abides by the rule of not allowing adjacent houses on the same side,

while assuming both sides are independent, thus squaring the final sum before taking the modulo. This example demonstrates

the solution approach for a small example where n is 3. The same principles apply for any value of n.

class Solution: def countHousePlacements(self, n: int) -> int: # Define the modulo constant to handle large numbers. MOD = 10**9 + 7

Iterate over the plots starting from the second one. for i in range(1, n): # If the last plot is empty, then it must come after an occupied plot. f[i] = g[i - 1]# If the last plot is occupied, it can come after either # an empty plot or another occupied plot. g[i] = (f[i - 1] + g[i - 1]) % MOD

int[] place = new int[n]; // place[i] represents the number of ways to place houses up to position i without a house at posit

int[] noPlace = new int[n]; // noPlace[i] represents the number of ways to place houses up to position i with a house at posi

noPlace[i] = (place[i - 1] + noPlace[i - 1]) % MODULO; // We can place a house if the previous position is either empty c

// After calculating for n-1 positions, we have to consider options for placement at the nth place hence (place[n - 1] + noPl

// Since we are considering placements on two sides of the street, we need to square the value for one side to get the total

place[i] = noPlace[i - 1]; // We can only place a house if the previous position has no house

// Return the total number of ways with modulo, ensuring we don't exceed integer limits

C++

Java

class Solution {

```
class Solution {
public:
    int countHousePlacements(int n) {
        // Initialize a constant MOD to use for modulo operation to avoid overflow
        const int MOD = 1e9 + 7;
        // Create two arrays to hold the number of ways to place houses
        // f represents number of ways when the last plot is empty
        // g represents number of ways when the last plot has a house
        // Initialize the first element as 1 since there's 1 way to place 0 houses
        int f[n + 1], q[n + 1];
        f[0] = g[0] = 1;
        // Calculate the number of ways to place houses dynamically
        for (int i = 1; i < n; ++i) {
            f[i] = q[i - 1]; // If the current plot is empty, previous plot can either be empty or have a house
            g[i] = (f[i-1] + g[i-1]) % MOD; // If the current plot has a house, previous plot must be empty
        // Calculate the final number of ways, considering both plots can be either empty or have a house
        // Long is used here to avoid integer overflow due to squaring the value
        long result = (f[n - 1] + g[n - 1]) % MOD;
        result = (result * result) % MOD; // We square it because we calculate for both sides of the street
        // Return the final result modulus MOD
        return static_cast<int>(result);
};
TypeScript
// Function to count the number of ways to place houses in plots
function countHousePlacements(n: number): number {
    // Initialize two arravs to store intermediate values
    const emptyPlotCounts = new Array(n);
    const housePlotCounts = new Array(n);
```

Define the modulo constant to handle large numbers. MOD = 10**9 + 7# f represents the count of ways to place houses such that # the last plot is empty.

class Solution:

f = [1] * n

g = [1] * n

```
# v is the total number of ways to place houses on the last plot.
       v = f[-1] + g[-1]
       # Since we can independently choose how to place houses on each side of the street,
       # we square the number of ways to find the total combinations.
       # We return the result modulo MOD to handle large numbers.
       return (v * v) % MOD
Time and Space Complexity
 The given code snippet is designed to count the number of ways to place houses on a street with n plots, where houses cannot
 be placed on adjacent plots. This is solved using dynamic programming with two arrays f and g representing the number of
 ways to arrange houses with certain conditions.
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• Inside the loop, the operations are constant-time; f[i] = g[i - 1] and g[i] = (f[i - 1] + g[i - 1]) % mod each take 0(1). • Calculation of v and final return statement also takes 0(1) time.

• The loop runs from 1 to n-1, which indicates O(n) iterations.

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Space Complexity:
For space complexity:
```

Time Complexity:

 We are using two arrays f and g, each of size n, resulting in O(n) space. The variables mod and v use constant space, 0(1).

To analyze the time complexity, we look at the operations inside the main loop:

Hence, the space complexity of the code is O(n) due to the two arrays.

Therefore, the overall time complexity of the code is O(n).