1638. Count Substrings That Differ by One Character

ending at (i, j) and having this as their only difference should be counted.

the length of the matching substring pair starting with s[i] and t[j].

Medium Hash Table String **Dynamic Programming** 

### **Problem Description**

equivalent to finding substrings in s that differ by precisely one character from any substring in t. For example, take s = "computer" and t = "computation". If we look at the substring s[0:7] = "compute" from s, we can change the last character e to a, obtaining s[0:6] + 'a' = "computa". This new substring, computa, is also a substring of t,

The goal of this problem is to count the number of ways in which we can select a non-empty substring from a string s and

replace exactly one character in it such that the modified substring matches some substring in another string t. This is

thus constituting one valid way. The problem requires us to find the total number of such valid ways for all possible substrings in s.

To solve this problem efficiently, we can apply <u>dynamic programming</u> (DP). The intuition for using DP hinges on two key

#### observations: For every pair of indices (i, j) where s[i] is equal to t[j], the substrings ending at these indices can form a part of larger

Intuition

matching substrings, barring the one character swap. If s[i] is not equal to t[j], then we have found the place where a single character difference occurs. All substring pairs

- Given these observations, we can define two DP tables:
- f[i][j] that stores the length of the matching substring of s[0..i-1] and t[0..j-1] ending at s[i-1] and t[j-1]. Essentially, it tells us how far back we can extend the matching part to the left, before encountering a mismatch or the start of the strings.

g[i][j] serves a similar purpose but looks to the right of i and j, telling us how far we can extend the matching part of the

substrings starting at s[i] and t[j].

- The variable ans accumulates the number of valid ways. For each mismatch found (where s[i] != t[j]), we calculate how many valid substrings can be formed and add this to ans. The number of valid substrings is computed as (f[i][j] + 1) \* (g[i + 1] [j + 1] + 1). This accounts for the one-character swap by combining the lengths of matching substrings directly to the left and right of (i, j).
- We iterate through each pair of indices (i, j) comparing characters from s and t, and whenever we find a mismatch, we perform the above calculation. Finally, we return the value of ans as our answer.

The solution implements a dynamic programming approach to efficiently solve the problem by considering all possible substrings of s and t and determining if they differ by exactly one character. Here's a step-by-step breakdown of the solution code:

Initialize Variables: The solution begins by initializing an accumulator ans to keep track of the count of valid substrings, and

Create DP Tables: Two DP tables f and g are created with dimensions (m+1) x (n+1), initializing all their entries to 0. Each

cell f[i][j] will hold the length of the matching substring pair ending with s[i-1] and t[j-1]. Similarly, g[i][j] will hold

Fill the f Table: The nested loop over i and j fills the f table. For each pair (i, j), if s[i-1] is equal to t[j-1], then f[i]

Fill the g Table and Calculate ans: Another nested loop, counting downwards from m-1 to 0 for i and from n-1 to 0 for j,

fills the g table. If s[i] is equal to t[j], then g[i][j] is set to g[i+1][j+1] + 1. But when s[i] does not match t[j], a

mismatch has been found. The product (f[i][j] + 1) \* (g[i+1][j+1] + 1) calculates the number of valid ways

the lengths of the strings s and t, denoted as m and n respectively.

improving efficiency.

а

[j-1] + 1. Here's how f looks like after filling:

+ 1) \* (g[i+1][j+1] + 1) and add it to ans.

def count substrings(self, s: str, t: str) -> int:

# Populate the forward match length table

for j, char t in enumerate(t, 1):

for i in range(len t -1, -1, -1):

# Return the total count of valid substrings

int[][] commonSuffixLength = new int[m + 1][n + 1];

int[][] commonPrefixLength = new int[m + 1][n + 1];

return count; // Return the total count of valid substrings

int m = s.length(), n = t.length(); // Get the lengths of strings s and t.

// Dynamic programming arrays to keep track of matching substrings.

// Function to count the number of good substrings.

int answer = 0; // Initialize answer to zero.

memset(matchingSuffix, 0, sizeof(matchingSuffix));

memset(matchingPrefix, 0, sizeof(matchingPrefix));

int countSubstrings(string s. string t) {

int matchingSuffix[m + 1][n + 1];

int matchingPrefix[m + 1][n + 1];

// Initialize the DP tables with zeros.

// Function to count the number of good substrings.

let answer = 0; // Initialize answer to zero.

function countSubstrings(s: string, t: string): number {

const m = s.length; // Get the length of string s.

const n = t.length; // Get the length of string t.

// Build the table for suffix matching substrings.

for (let i = 0; i < m; i++) {

for (let j = 0; j < n; j++) {

**if** (s[i] === t[i]) {

// Initialize arrays to keep track of matching substrings.

// If characters match, extend the suffix by 1.

matchingSuffix[i + 1][j + 1] = matchingSuffix[i][j] + 1;

const matchingSuffix: number[][] = Array.from({ length: m + 1 }, () => Array(n + 1).fill(0));

const matchingPrefix: number[][] = Array.from({ length: m + 1 }, () => Array(n + 1).fill(0));

for i, char s in enumerate(s, 1):

if char s == char t:

for i in range(len s - 1, -1, -1):

**if** s[i] == t[i]:

for (int i = 0; i < m; i++) {

for (int j = 0; j < n; j++) {

else:

return count

C++

public:

#include <cstring>

#include <string>

class Solution {

# Lengths of the input strings

len s, len t = len(s), len(t)

# Initializes the count of valid substrings

# Initialize the forward and backward match length tables

forward match = [[0] \* (len t + 1) for in range(len s + 1)]

backward\_match =  $[[0] * (len_t + 1) for _ in range(len_s + 1)]$ 

# Populate the backward match length table, and calculate the count

 $forward_match[i][j] = forward_match[i - 1][j - 1] + 1$ 

backward\_match[i][j] = backward\_match[i + 1][j + 1] + 1

int count = 0; // Initialize count to track the number of valid substrings

int m = s.length(), n = t.length(); // Lengths of the input strings

# When characters do not match, we multiply the forward match

# and backward match lengths and add these matched substrings to the count.

count += (forward\_match[i][j] + 1) \* (backward\_match[i + 1][j + 1] + 1)

// f[i][i] will store the length of the common substring of s and t ending with s[i-1] and t[j-1]

// q[i][i] will store the length of the common substring of s and t starting with s[i] and t[j]

// Compute the length of the common suffixes for all pairs of characters from s and t

the valid ways for these mismatches, adding the results to ans.

**Solution Approach** 

- [j] is set to the value of f[i-1][j-1] + 1, which extends the length of the matching substring by one. Otherwise, f[i][j] is already 0, indicating no match.
- Return the Result: After iterating through all possible substrings, the ans variable will have accumulated the total number of valid substrings where a single character replacement in s can result in a substring in t. This accumulated result is returned as the final answer.

In this solution, dynamic programming tables f and g efficiently store useful computed values which are used to keep track of

matches and calculate the number of possible valid substrings dynamically for each pair of indices (i,j). By avoiding redundant

comparisons and reusing previously computed values, the algorithm avoids the naive approach's extensive computation, thus

considering the mismatch as the single difference point, and this number is added to the accumulator ans.

**Example Walkthrough** Let's walk through a small example to illustrate the solution approach using strings s = "acdb" and t = "abc".

**Initialize Variables:** We set ans to 0. The lengths of the strings m and n are 4 and 3 respectively.

Create DP Tables: We initialize the DP tables f and g as 5×4 matrices, as s has length 4, and t has length 3.

0 0 а 0 0 0 d

Fill the g Table and Calculate ans: Next, we fill in the g table by iterating backwards. On mismatches, we calculate (f[i][j]

○ Continue for other elements. Discrepancies are found at s[2] = 'd' and t[0] = 'a', as well as s[0] = 'a' and t[1] = 'b'. We calculate

Fill the f Table: We iterate through strings s and t with indices i and j. When characters match, we set f[i][j] = f[i-1]

### Steps while filling g:

0

0

Here's the g matrix:

0

0

0

0

С

d

**Python** 

class Solution:

count = 0

0 | 1

0

b

 Start at s[3] = 'b' and t[2] = 'c', no match, set g[3][2] = 0. Move to s[3] = 'b' and t[1] = 'b', they match, so set g[3][1] = g[4][2] + 1 which is 1.

0 | 1 | In this case, ans will be calculated as follows:  $\circ$  For s[2] != t[0], (f[2][0] + 1) \* (g[3][1] + 1) = (0 + 1) \* (0 + 1) = 1.  $\circ$  For s[0] != t[1], (f[0][1] + 1) \* (g[1][2] + 1) = (0 + 1) \* (0 + 1) = 1. We add these to ans, getting us an ans = 2. Return the Result: The variable ans now has the value 2, which is the number of valid substrings in s that can match substrings in t by changing exactly one character. We return this value as the answer. Solution Implementation

Java class Solution { public int countSubstrings(String s, String t) {

```
if (s.charAt(i) == t.charAt(j)) {
            commonSuffixLength[i + 1][j + 1] = commonSuffixLength[i][j] + 1;
// Compute the length of the common prefixes and the number of valid substrings
for (int i = m - 1; i >= 0; i--) {
    for (int i = n - 1; i \ge 0; i--) {
        if (s.charAt(i) == t.charAt(j)) {
            // If characters match, extend the common prefix by 1
            commonPrefixLength[i][j] = commonPrefixLength[i + 1][j + 1] + 1;
        } else {
            // When there is a mismatch, count the valid substrings using the common prefix and suffix
            count += (commonSuffixLength[i][j] + 1) * (commonPrefixLength[i + 1][j + 1] + 1);
```

```
// Build the DP table for suffix matching substrings.
for (int i = 0; i < m; ++i) {
    for (int i = 0: i < n: ++j) {
        if (s[i] == t[i]) {
            // If characters match, extend the suffix by 1.
            matchingSuffix[i + 1][j + 1] = matchingSuffix[i][j] + 1;
// Build the DP table for prefix matching substrings.
for (int i = m - 1; i >= 0; ---i) {
    for (int i = n - 1: i >= 0; ---j) {
        if (s[i] == t[i]) {
            // If characters match, extend the prefix by 1.
            matchingPrefix[i][j] = matchingPrefix[i + 1][j + 1] + 1;
        } else {
            // If characters don't match, calculate the count of
            // good substrings ending here.
            answer += (matchingSuffix[i][j] + 1) * (matchingPrefix[i + 1][j + 1] + 1);
// Return the total number of good substrings.
return answer;
```

**}**;

**TypeScript** 

```
// Build the table for prefix matching substrings.
   for (let i = m - 1; i >= 0; i--) {
        for (let j = n - 1; j >= 0; j--) {
           if (s[i] === t[i]) {
               // If characters match, extend the prefix by 1.
               matchingPrefix[i][j] = matchingPrefix[i + 1][j + 1] + 1;
           } else {
               // If characters don't match, calculate the count of
               // good substrings ending at this position.
               answer += (matchingSuffix[i][j] + 1) * (matchingPrefix[i + 1][j + 1] + 1);
   // Return the total number of good substrings.
   return answer;
class Solution:
   def count substrings(self, s: str, t: str) -> int:
       # Initializes the count of valid substrings
       count = 0
       # Lengths of the input strings
       len s, len t = len(s), len(t)
       # Initialize the forward and backward match length tables
       forward match = [[0] * (len t + 1) for in range(len s + 1)]
       backward_match = [[0] * (len_t + 1) for _ in range(len_s + 1)]
       # Populate the forward match length table
       for i, char s in enumerate(s, 1):
            for i, char t in enumerate(t, 1):
               if char s == char t:
                    forward_match[i][j] = forward_match[i - 1][j - 1] + 1
       # Populate the backward match length table, and calculate the count
       for i in range(len s -1, -1, -1):
            for j in range(len t -1, -1, -1):
               if s[i] == t[i]:
                   backward_match[i][j] = backward_match[i + 1][j + 1] + 1
               else:
                   # When characters do not match, we multiply the forward match
                   # and backward match lengths and add these matched substrings to the count.
                   count += (forward_match[i][j] + 1) * (backward_match[i + 1][j + 1] + 1)
       # Return the total count of valid substrings
        return count
```

## **Time Complexity**

Time and Space Complexity

The given code consists of a nested loop structure, where two independent loops iterate over the length of s and t. The outer loop runs for m + n times and the inner nested loops run m \* n times separately for the loops that build the f and g 2D arrays. The computation within the inner loops operates in 0(1) time. Therefore, the total time complexity combines the 0(m + n) for the outer loops and 0(m \* n) for the inner nested loops, resulting in 0(m \* n) overall.

# **Space Complexity**

The space complexity is determined by the size of the two-dimensional arrays f and g, each of which has a size of (m + 1) \* (n + 1). Hence, the space used by these data structures is 0(m \* n). No other data structures are used that grow with the input size, so the total space complexity is 0(m \* n).