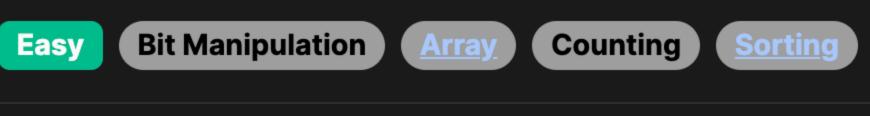
1356. Sort Integers by The Number of 1 Bits



Problem Description

rules based on the binary representation of its elements. The primary sorting criterion is the number of 1s in the binary representation of each integer. If two integers have the same number of 1s, then they should be sorted in ascending order according to their integer values. The goal is to return the array sorted first by the number of 1s in their binary representation, and then by their value when

The problem presents a task where we are given an array of integers, arr, and we need to sort this array with a specific set of

there's a tie on the first criteria.

To tackle the sorting problem, we need to decide upon a sorting strategy that complies with the rules provided:

Intuition

1. Count the number of 1 s in the binary representation of each integer. 2. Sort the integers by the number of 1s. In the event of a tie (when two numbers have the same number of 1s), sort by the integer values

- themselves, in ascending order.
- The built-in Python sorted function offers us a straightforward way to sort the elements of an array. We can customize the sorting order by providing a key argument that transforms each element before comparison during the sort. This transformation

Thus, we choose a lambda function as the key, that returns a tuple for each x in arr: $(x.bit_count(), x)$. The bit_count method returns the number of 1s in the binary representation of x, which addresses our primary criterion. By creating a tuple with $x.bit_count()$ as the first element and x as the second, we ensure that when two numbers have the same number of 1s,

the smaller number comes first, satisfying the secondary sorting criterion. The sorted list according to these criteria will thus be the result we return. **Solution Approach**

The provided Python solution makes use of Python's higher-level functionality to implement the sorting logic cleanly and efficiently. To understand the solution's implementation, let's break down the key components and the patterns leveraged in the

doesn't change the actual elements of the array, but it is used to guide the sort order.

Lambda Functions

code:

A lambda function is an anonymous function defined with the lambda keyword in Python. In the solution, the lambda function is used as a key argument to the sorted function. It defines the sorting behavior according to the specific problem constraints.

The lambda function leverages a feature of Python's sorting algorithm, which can sort tuples lexicographically. That means the

first elements of the tuples are compared first, and if those are equal, the second elements are compared, and so on.

bit_count Method The bit_count() method returns the number of 1 bits in the binary representation of an integer (an important note here is that

Tuple Sorting

bin(x).count('1') approach instead. **Sorted Function**

Finally, the sorted function is a built-in Python function that returns a new list containing all items from the iterable in ascending

order. A key feature of sorted is that it allows you to define a key function that is called on each element before making

this method is only available in Python 3.10 or later). If you're using an earlier version of Python, you would need to use the

comparisons.

element x in the array arr. The first item is the count of 1s in the binary representation of x, and the second item is x itself. Apply Sorting with Custom Key: The sorted function then uses the tuples generated by the lambda function to sort the entire array. It prioritizes the count of 1 bits first, as it's the first element of the tuple. If two tuples have the same first

Define a Key Function: The lambda function (lambda x: (x.bit_count(), x)) generates a tuple with two items for each

element (meaning the elements have the same number of 1s in their binary representations), the second element of the tuple

Return the Sorted Array: The sorted function does not modify arr in place; instead, it returns a new list, which is the

specifications. **Example Walkthrough**

By combining these Python features, the solution elegantly and efficiently sorts the array arr according to the problem's

• The binary representation of 3 is 11, which has 2 ones. The binary representation of 1 is 1, which has 1 one. The binary representation of 2 is 10, which has 1 one.

Following the primary sorting criterion (number of 1s), we'd have an intermediate sort order of [1, 2, 4] (each with one 1), and

(with two 1s). But since 1, 2, and 4 all have the same number of 1s in their binary representation, we must sort them by their value.

• For 2: (1, 2)

• For 4: (1, 4)

count and the integer value:

Solution Implementation

Python

class Solution {

C++

public:

class Solution {

The custom lambda function used as the key in the sorted algorithm will generate the following tuples based on the binary

Now, let's piece everything together. The solution approach is carried out as follows:

(the element's value) is used as a tie-breaker.

• The binary representation of 4 is 100, which has 1 one.

correctly sorted version of arr as per the problem's constraints.

Let's consider an array of integers for demonstration: arr = [3, 1, 2, 4].

• For 3: (2, 3) • For 1: (1, 1)

As a result, considering the second element of each tuple, we get the sorted array: [1, 2, 4, 3].

which satisfies both the primary and secondary sorting criteria specified in the problem.

Note: The use of 'x.bit count()' is available in Python 3.10 and later.

First, we'll determine the binary representation of each number and count the number of 1s:

1. (1, 1) comes before (1, 2) and (1, 4) because their first elements are equal and 1 is the smallest integer value among them. 2. (1, 2) comes before (1, 4) because they have the same number of 1s and 2 is smaller than 4. 3. (2, 3) comes after all (1, x) tuples because 2 is greater than 1.

The return value of the sorted function with the custom lambda function as the provided key will give us this final sorted array

When we pass these tuples to the sorted function, it will sort the numbers first by the number of 1s in their binary

class Solution: def sort by bits(self. arr: List[int]) -> List[int]: # Sort the array based on the number of 1's in the binary representation # of each number ('x.bit count()'). In the event of a tie, the numbers

return sorted(arr, key=lambda x: (bin(x).count('1'), x))

int n = arr.length; // Store the length of the array

// Add to each element in the array a value that represents

Arrays.sort(arr); // Sort the array with modified values

// Function to sort the numbers based on the number of 1-bits they have.

return arr; // Return the sorted array by bits

// In case of a tie, sort by the values themselves.

vector<int> sortByBits(vector<int>& arr) {

num &= num - 1:

count++;

return arr.sort((a, b) => {

return count;

return a - b;

// Increment the count of 1-bits

// First, compare by the number of 1-bits

if (bitCountComparison !== 0) {

return bitCountComparison;

result = solution.sort_by_bits([0,1,2,3,4,5,6,7,8])

these, the overall space complexity remains O(n).

// In the case of a tie, sort by numerical value (asc order).

const bitCountComparison = countBits(a) - countBits(b);

return sorted(arr, key=lambda x: (bin(x).count('1'), x))

// Sorting the array based on the number of 1-bits each number has (asc order).

// If the number of 1-bits is the same, compare by the numbers themselves

Note: The use of 'x.bit count()' is available in Python 3.10 and later.

For versions before Python 3.10, we can use bin(x) count('1')' instead.

// the bit count of the number multiplied by 100000 to ensure

int bitCount = Integer.bitCount(arr[i]); // Count number of 1-bits in arr[i]

arr[i] += bitCount * 100000; // Add 100000 for each 1-bit to prioritize in sorting

are sorted based on their value ('x').

public int[] sortByBits(int[] arr) {

for (int i = 0; i < n; ++i) {

// it is prioritized in the sorting

representation, and then by their integer value in case of a tie.

Here is what the sorting stage looks like with these tuples:

```
# For versions before Python 3.10, we can use 'bin(x).count('1')' instead.
# Example usage:
# solution = Solution()
# result = solution.sort_by_bits([0,1,2,3,4,5,6,7,8])
Java
import java.util.Arrays; // Importing Arrays class for sort function
```

// After sorting retrieve the original values by taking modulo 100000 for (int i = 0; i < n; ++i) { arr[i] %= 100000; // Reduce each element back to original value

```
// Apply a transformation to each number in the array.
        // The transformation adds the number of 1-bits in the number times 100000
        // to the number itself. This is done to couple the number of 1-bits with the number.
        for (int& num : arr) {
            num += __builtin_popcount(num) * 100000;
        // Sort the transformed array.
        // The numbers are now ordered first by the number of 1-bits, then by the number's value.
        sort(arr.begin(), arr.end());
        // Iterate through the array to revert the transformation and obtain
        // the original numbers, preserving the new order.
        for (int& num : arr) {
            num %= 100000; // Remove the added portion to get back the original number.
        // Return the sorted array.
        return arr;
};
TypeScript
// Function to sort an array of numbers based on the number of 1-bits each number has.
// In the case of a tie, numbers are sorted by their value.
function sortByBits(arr: number[]): number[] {
    // Helper function to count the number of 1-bits in a binary representation of a number.
    const countBits = (num: number): number => {
        let count = 0;
        while (num) {
            // Remove the rightmost 1-bit from the number
```

```
class Solution:
   def sort by bits(self. arr: List[int]) -> List[int]:
       # Sort the array based on the number of 1's in the binary representation
       # of each number ('x.bit count()'). In the event of a tie, the numbers
       # are sorted based on their value ('x').
```

Example usage:

solution = Solution()

});

};

Time and Space Complexity Time Complexity The time complexity of the provided code primarily depends on the complexity of the sorting algorithm used by Python's sorted function. Python uses the TimSort algorithm, which has a time complexity of O(n log n) for the average and worst case, where n is the number of elements in the array to be sorted.

process. Thus, assuming k is the number of comparisons performed by the sorting algorithm, the total time complexity considering the bit count operations for comparison purposes becomes O(k). Since k can be as large as n log n comparisons, the total time

In this case, for each comparison, the sorting algorithm also calculates the bit count (number of 1s in the binary representation of

the number), which is 0(1) as Python's integer bit count implementation is efficient and not based on the value of the number

but the number of set bits. However, this bit count operation will be performed multiple times per element during the sorting

Space Complexity

complexity remains O(n log n).

The space complexity of this function is O(n), as the sorted function returns a new list containing the sorted elements and does not sort the list in place. Hence, a new array of the same size as the input array is created. Additionally, there is no significant extra space used during the sorting process, except for the temporary variables used in the

lambda function during comparison, so the space complexity due to the lambda function remains constant, 0(1). Combining