Problem Description

subsequent row contains one more number than the previous row, and these numbers are positioned such that they form a triangle. The challenge here is to compute these numbers using the given property of Pascal's triangle and to represent the triangle in the form of a list of lists, where each inner list corresponds to a row in the triangle. For example, the first 3 rows of Pascal's triangle look like this:

Given an integer numRows, the task is to return the first numRows of Pascal's triangle. In Pascal's triangle, each number is the sum of

the two numbers directly above it except for the boundaries, which are always 1. The triangle starts with a 1 at the top. Then, each

//Second row (two 1s at the boundaries) //Third row (1s at the boundaries, middle is sum of the two numbers above) 3 1 2 1

//First row (only one element)

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Intuition
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each row and add it to the final result. This can be implemented by initializing a list with the first row as its only element, then using a loop to construct each subsequent row. Inside the loop, we can use list comprehension to generate the middle values of the row by summing pairs of consecutive

The Python code encapsulates this logic in the generate function, with f holding the result list of lists and g being the new row being constructed each iteration. Finally, the function returns f after the completion of the loop. Solution Approach

In the provided code, the problem is approached by considering each row in Pascal's Triangle to be a list and the entire triangle to be

The main steps of the implementation are as follows:

a list of these lists.

f list.

1. Initialize a list, f, with a single element that is the first row of Pascal's Triangle, which is simply [1]. 2. Loop from 0 to numRows - 1 (the -1 is because we already have the first row). This loop will build one row at a time to add to our

3. For each iteration, construct a new row, g. The first element is always 1. This is done by simply specifying [1] at the start.

f[-1] to create the middle elements of the new row g.

7. This process repeats until all numRows rows are generated.

- 4. The middle elements of the row g are created by taking pairs of consecutive elements from the last row available in f and
- summing them up. This is done using list comprehension and the pairwise function, pairwise takes an iterable and returns an iterator over pairs of consecutive elements. For example, pairwise([1,2,3]) would produce (1, 2), (2, 3).

In the code, we have [a + b for a, b in pairwise(f[-1])], which sums each pair of consecutive elements from the last row

- 5. After the middle elements are calculated, [1] is appended to the end of the list to create the last element of the row, which is also 1.
- 8. Finally, the list f is returned, which contains the representation of Pascal's Triangle up to numRows. This solution uses nested lists to represent Pascal's Triangle, list comprehension to generate each row, and a loop to build the

triangle one row at a time. The pairwise function streamlines the process of summing adjacent elements from the previous row to

= [[1]] # Initial Pascal's Triangle with the first row. for i in range(numRows - 1): g = [1] + [a + b for a, b in pairwise(f[-1])] + [1] # Constructing the new rowf.append(g) # Appending the new row to the triangle

5 return f # The complete Pascal's Triangle

Here is the critical part of the Python solution:

build the interior of each new row.

exactly once.

Example Walkthrough

6. Row g is then added to the list f.

Let's walk through the solution with numRows = 5 to illustrate the generation of Pascal's Triangle:

1. We start with the initial list f which already contains the first row [1].

g = [1] + [a + b for a, b in pairwise(f[-1])] + [1]

f[-1] is [1, 1], pairwise(f[-1]) yields one pair: (1, 1).

We add [1] at the beginning and end.

accounted for, so we effectively need to generate 4 more rows. 3. For i = 0, we construct the second row:

2. We begin the loop with i ranging from 0 to numRows - 1, which is 0 to 4 in this case. Remember, the first row is already

The algorithm has a time complexity of O(n^2), where n is the number of rows, since each element of the triangle is computed

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4. Our list f now looks like [[1], [1, 1]].
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So, g = [1] + [] + [1] which is simply [1, 1]. We append [1, 1] to f.

We then add the sums of these pairs to [1] and enclose with [1] at the end.

So, g = [1] + [1 + 1] + [1] which gives us [1, 2, 1]. We append [1, 2, 1] to f.

∘ f[-1] is [1], so pairwise(f[-1]) doesn't generate any pairs since there's only one element.

- 5. For i = 1, we construct the third row:
- f[-1] is [1, 2, 1], pairwise(f[-1]) gives (1, 2) and (2, 1).

6. Our list f now looks like [[1], [1, 1], [1, 2, 1]].

7. For i = 2, constructing the fourth row:

- The sums are [1 + 2, 2 + 1] which is [3, 3]. So, g = [1] + [3, 3] + [1] which forms [1, 3, 3, 1]. We append [1, 3, 3, 1] to f.
- 8. Our list f now looks like [[1], [1, 1], [1, 2, 1], [1, 3, 3, 1]]. 9. For i = 3, the final loop to construct the fifth row:
- g = [1] + [4, 6, 4] + [1], forming the row [1, 4, 6, 4, 1]. We append this row to f. 10. Our final list f, representing the first 5 rows of Pascal's Triangle, now looks like [[1], [1, 1], [1, 2, 1], [1, 3, 3, 1], [1, 4,

The sums are [1 + 3, 3 + 3, 3 + 1] which is [4, 6, 4].

f[-1] is [1, 3, 3, 1], pairwise(f[-1]) yields (1, 3), (3, 3), and (3, 1).

Executing these steps with a proper function such as the given generate function will yield the desired Pascal's Triangle up to the specified row. Each iteration builds upon the previous, aligning perfectly with the properties of Pascal's Triangle.

def generate(self, numRows: int) -> List[List[int]]:

Generate each row of Pascal's Triangle

pascal_triangle.append(new_row)

Return the completed Pascal's Triangle

public List<List<Integer>> generate(int numRows) {

List<List<Integer>> triangle = new ArrayList<>();

// The first row of Pascal's Triangle is always [1]

Initialize the first row of Pascal's Triangle

The first element of each row is always 1

The last element of each row is also always 1

Append the newly generated row to Pascal's Triangle

// Initialize the main list that will hold all rows of Pascal's Triangle

// Function to generate Pascal's Triangle with the given number of rows.

// Initialize a 2D vector to hold the rows of Pascal's Triangle.

// Fill in the values between the first and last '1' of the row.

// The last value in a row of Pascal's Triangle is always '1'.

// Append the newly created row to Pascal's Triangle.

// The new value is the sum of the two values directly above it.

// The first row of Pascal's Triangle is always [1].

// Generate the subsequent rows of Pascal's Triangle.

for (int rowIndex = 1; rowIndex < numRows; ++rowIndex) {</pre>

// Initialize the new row starting with a '1'.

pascalsTriangle.push_back(vector<int>(1, 1));

vector<vector<int>>> generate(int numRows) {

vector<vector<int>> pascalsTriangle;

vector<int> newRow;

newRow.push_back(1);

newRow.push_back(1);

pascalsTriangle.push_back(newRow);

Calculate the intermediate elements of the row 11 # by adding the pairs of adjacent elements from the previous row 12 for j in range(1, i): sum_of_elements = pascal_triangle[i - 1][j - 1] + pascal_triangle[i - 1][j] 14 15 new_row.append(sum_of_elements)

return pascal_triangle 25

Java Solution

class Solution {

6, 4, 1]].

Python Solution

1 class Solution:

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The function would then return this list f.

pascal_triangle = [[1]]

 $new_row = [1]$

for i in range(1, numRows):

new_row.append(1)

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triangle.add(List.of(1));
           // Loop through each row (starting from the second row)
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            for (int rowIndex = 1; rowIndex < numRows; ++rowIndex) {</pre>
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                // Initialize the list to hold the current row's values
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                List<Integer> row = new ArrayList<>();
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                // The first element in each row is always 1
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                row.add(1);
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                // Compute the values within the row (excluding the first and last element)
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                for (int j = 0; j < triangle.get(rowIndex - 1).size() - 1; ++j) {
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                    // Calculate each element as the sum of the two elements above it
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                    row.add(triangle.get(rowIndex - 1).get(j) + triangle.get(rowIndex - 1).get(j + 1));
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                // The last element in each row is always 1
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                row.add(1);
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                // Add the computed row to the triangle list
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                triangle.add(row);
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           // Return the fully constructed list of rows of Pascal's Triangle
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            return triangle;
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33 }
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30 31 32 33 };

C++ Solution

1 class Solution {

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// Return the fully generated Pascal's Triangle.
           return pascalsTriangle;
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Typescript Solution
   // Generates Pascal's Triangle with a given number of rows
   function generate(numRows: number): number[][] {
       // Initialize the triangle with the first row
       const triangle: number[][] = [[1]];
       // Populate the triangle row by row
       for (let rowIndex = 1; rowIndex < numRows; ++rowIndex) {</pre>
           // Initialize the new row starting with '1'
           const row: number[] = [1];
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           // Calculate each value for the current row based on the previous row
           for (let j = 0; j < triangle[rowIndex - 1].length - 1; ++j) {
                row.push(triangle[rowIndex - 1][j] + triangle[rowIndex - 1][j + 1]);
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           // End the current row with '1'
16
           row.push(1);
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19
           // Add the completed row to the triangle
           triangle.push(row);
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       // Return the fully generated Pascal's Triangle
       return triangle;
24
```

for (int elementIndex = 0; elementIndex < pascalsTriangle[rowIndex - 1].size() - 1; ++elementIndex) {</pre>

newRow.push_back(pascalsTriangle[rowIndex - 1][elementIndex] + pascalsTriangle[rowIndex - 1][elementIndex + 1]);

The provided code generates Pascal's Triangle with numRows levels. Here is the analysis of its time and space complexity:

Time and Space Complexity

 Inside the loop, pairwise(f[-1]) generates tuples of adjacent elements from the last row which takes 0(j) time, where j is the number of elements in the previous row (since every step inside the enumeration would be constant time).

• There are numRows - 1 iterations since the first row is initialized before the loop.

The time complexity of the code can be understood by analyzing the operations inside the for-loop that generates each row of

• The list comprehension [a + b for a, b in pairwise(f[-1])] performs j - 1 additions, so this is also O(j) where j is the size of the previous row. Appending the first and last 1 is 0(1) each for a total of 0(2) which simplifies to 0(1).

complexity of 0(numRows^2).

Space Complexity

to the nature of Pascal's Triangle.

Time Complexity

Pascal's Triangle.

As the rows of Pascal's Triangle increase by one element each time, summing up the operations over all rows gives us a total time of approximately 0(1) for the first row, plus $0(2) + 0(3) + \dots + 0(numRows)$ for the numRows - 1 remaining rows. This results in a time

 f is initialized with a single row containing one 1 which we can consider 0(1). In each iteration of the loop, a new list with i + 2 elements is created (since each new row has one more element than the

The space complexity is determined by the space required to store the generated rows of Pascal's Triangle.

previous one) and appended to f. Summing this up, the space required will be 0(1) for the first row, plus 0(2) + 0(3) + ... + 0(numRows) for the rest of the rows.

This results in a space complexity of O(numRows^2) since the space required is proportional to the square of the number of rows due

Therefore, the overall space complexity is O(numRows^2).

Therefore, the overall time complexity is 0(numRows^2).

The solution to generating Pascal's triangle is a direct application of its properties. The key idea is to start with the first row [1], and then generate each following row based on the previous row. For any new row, aside from the first and last elements which are 1,

elements from the last row. We use the pairwise function (assuming Python 3.10+) to obtain the pairs, and then enclose the generated middle values with [1] on both ends to complete the row. After constructing each row, we append it to our result list. We

repeat this process numRows - 1 times since the first row is already initialized.

each element is obtained by adding the two numbers directly above it in the triangle. With this approach, we can iteratively construct