Medium Stack Array Monotonic Stack

Problem Description

You are given an array maxHeights which consists of n integers. Imagine the responsibility of constructing n towers along a straight line where the i-th tower is positioned at coordinate i and may vary in height, up to a maximum height specified by maxHeights[i]. The goal is to build these towers in such a way that they form a beautiful configuration. A beautiful configuration is defined by two criteria:

2. The height sequence of the towers (heights) must form a mountain array, meaning there exists an index i in heights such that:

1. The height of each tower (heights[i]) must be at least 1 and at most maxHeights[i].

- For any index j less than i, heights[j] is less than or equal to heights[j+1] (ascending order).
 - For any index k greater than i, heights[k] is greater than or equal to heights[k+1] (descending order).
- The challenge is to find the configuration of towers that is beautiful and yields the maximal possible sum of heights across all towers.

Intuition

towers will transition from ascending to descending heights). For each potential peak position i, we determine the maximum sum of

The approach to solve this problem involves iterating through each possible peak of the mountain (the highest point where the

heights for a mountain configuration where the peak is at 1. To achieve this, we initialize the peak tower's height with 'x' - the value given by maxHeights[i]. We then expand this peak to the left and right to construct the ascending and descending parts of the mountain. While expanding to the left, we ensure that the heights of the towers are both less than or equal to maxHeights[j] and the height of the previous tower to maintain a non-decreasing slope. Similarly, when expanding to the right, we maintain heights that are less than

or equal to maxHeights[j] and the previous tower to ensure a non-increasing slope. The total sum for this configuration is computed by accumulating the heights as we expand from the peak to both the left and right ends. After exploring all potential peak positions, we keep track of the maximum sum of heights that we have encountered. This value represents the highest sum of tower heights for any beautiful configuration possible, and thus, is the answer we return.

Solution Approach

1. The function maximumSumOfHeights begins with initializing variable ans to store the maximum sum found for any beautiful

The provided solution uses a straightforward brute force approach to simulate the construction of the mountain from each potential

peak position. The approach does not use complex data structures or advanced algorithms; it relies on basic iteration and condition checking. Here's a step-by-step breakdown of how the solution is implemented:

configuration, and variable n to store the number of towers (the length of the maxHeights array). 2. It then enters a loop to consider each element x in maxHeights as the peak of the mountain (tallest tower). The variable i refers to the index where the peak is located.

- 3. Inside the loop, two additional loops are used:
- The first inner loop decreases from the peak's index 1-1 to the start of the array. We initialize y as the height of the peak tower and t as the total sum starting with the peak. For every element left of the peak (j index), we update y to the
- minimum of the current y and maxHeights[j] to ensure that the tower heights are non-decreasing as we move towards the

with the current maximum ans, updating ans if t is greater.

- peak. We then add the height y to the total sum t. The second inner loop increases from the peak's index i+1 to the end of the array, similarly initializing y to the height of the peak. As we iterate to the right, we update y with the minimum of the current y and maxHeights[j] to ensure the mountain array condition is maintained with non-increasing tower heights. Each y value is added to the total sum t. 4. After both loops, we have constructed the tallest possible mountain whose peak is at index i and we compare its total sum t
- 5. Finally, after all iterations, ans contains the maximum sum that can be achieved by a beautiful configuration of towers and is returned.

Throughout the implementation, variables ans, y, and t are used to keep track of the current best answer, the height of the previous

tower (to maintain a valid mountain shape), and the cumulative sum of the current configuration, respectively. No extra data structures are used; the solution operates directly on the input array, and no sorting or other modifications are

Example Walkthrough

needed. The simplicity of the problem allows for a direct brute force method, exploring every possibility and comparing sums directly

Let's walk through a small example to illustrate the solution approach using the following maxHeights array: 1 maxHeights = [2, 1, 4, 3]

In this scenario, we have four positions to place towers, and we can set their heights with the constraints provided in the maxHeights

array. We need to build the towers such that they form a mountain array. Let's examine the construction step-by-step by trying each position for the peak.

to find the optimal configuration.

1. Trying the first position as the peak (i = 0). The peak height x = 2.

To the left of the peak, there are no taller towers, so we can't extend in that direction.

 To the right, we need to construct descending towers. However, given the height 1 at the next position, we cannot make a descending sequence from 2. The sequence fails to form a mountain, and the sum here would simply be 2. 2. Trying the second position as the peak (i = 1). The peak height x = 1.

The sum for this peak would be 1.

3. Trying the third position as the peak (i = 2). The peak height x = 4.

No towers to the right since this is the end of the array.

 Descending from the peak to the right, the next and final tower can be up to 3. The mountain array [2, 1, 4, 3] forms a valid, beautiful configuration with a sum of 2 + 1 + 4 + 3 = 10.

Since the peak is the smallest possible tower, we cannot create a proper mountain.

- 4. Trying the fourth position as the peak (i = 3). The peak height x = 3.
 - The sequence [2, 1, 3] is not a valid mountain as it lacks a descending part, making this an invalid peak position.

Calculate the length of the maxHeights list once as it is used multiple times

Move to the left of the current position and add the minimum of all

Move to the right of the current position and add the minimum of all

10 as the maximum sum for creating a beautiful tower configuration. The simple brute force approach worked effectively for this example by checking each possible peak and ensuring that all criteria of

Ascending from the left, we start with 2, can increase to 1, but then we cannot go higher because the peak is at 3.

Out of all the trials, the third position peak yields the highest sum of tower heights, which is 10. Therefore, the solution would return

a mountain array are met. By calculating the sums for each valid configuration and keeping track of the maximum, we identified the

Ascending from the left, we can have the first tower at height 2, next cannot exceed 1, so it stays 1.

class Solution: def maximumSumOfHeights(self, maxHeights: List[int]) -> int: # Initialize the variable to hold the maximum sum of heights

Initialize temporary variables for moving left and right from the current index 11 12 left_min_height = current_height right_min_height = current_height # Temporary sum for current position including the current height itself temp_sum = current_height 16

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# encountered heights so far to the temporary sum
                for left_index in range(i - 1, -1, -1):
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                    left_min_height = min(left_min_height, maxHeights[left_index])
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                    temp_sum += left_min_height
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optimal construction.

Python Solution

max_sum = 0

num_heights = len(maxHeights)

Iterate through each height in the maxHeights list

encountered heights so far to the temporary sum

maxSum = Math.max(maxSum, tempSum);

// Return the maximum sum of heights found

function maximumSumOfHeights(maxHeights: number[]): number {

const arrayLength = maxHeights.length;

// Get the total number of elements in the maxHeights array.

for i, current_height in enumerate(maxHeights):

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26
               for right_index in range(i + 1, num_heights):
27
                   right_min_height = min(right_min_height, maxHeights[right_index])
28
                   temp_sum += right_min_height
29
               # Update the maximum sum if the temporary sum is greater than the current maximum
30
31
               max_sum = max(max_sum, temp_sum)
32
33
           # Return the maximum sum after considering all positions
34
           return max_sum
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Java Solution
1 class Solution {
       // Method to calculate the maximum sum of heights, considering that each position
       // can act as a pivot, and the sum includes the minimum height from the pivot to each side.
       public long maximumSumOfHeights(List<Integer> maxHeightList) {
            long maxSum = 0; // This will store the maximum sum of heights we find
           int listSize = maxHeightList.size(); // The size of the provided list
           // Iterate through each element in the list to consider it as a potential pivot
           for (int i = 0; i < listSize; ++i) {</pre>
9
               int currentHeight = maxHeightList.get(i); // Height at the current pivot
10
11
               long tempSum = currentHeight; // Initialize temp sum with current pivot's height
12
               // Calculate the sum of heights to the left of the pivot
               for (int j = i - 1; j >= 0; ---j) {
                   currentHeight = Math.min(currentHeight, maxHeightList.get(j)); // Update to the smaller height
                   tempSum += currentHeight; // Add this height to the running total for the pivot
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               currentHeight = maxHeightList.get(i); // Reset height for current pivot
20
               // Calculate the sum of heights to the right of the pivot
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22
               for (int j = i + 1; j < listSize; ++j) {
23
                   currentHeight = Math.min(currentHeight, maxHeightList.get(j)); // Update to the smaller height
```

tempSum += currentHeight; // Add this height to the running total for the pivot

// Update maxSum if the sum for the current pivot is greater than the previous maximum

C++ Solution 1 class Solution { 2 public:

return maxSum;

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// Function to calculate the maximum sum of heights.
       long long maximumSumOfHeights(vector<int>& maxHeightSequence) {
            long long maxSum = 0; // Initialize variable to hold the maximum sum
           int sequenceLength = maxHeightSequence.size(); // Get the length of the sequence
           // Loop through the entire sequence to find the maximum sum of heights
           for (int i = 0; i < sequenceLength; ++i) {</pre>
9
                long long tempSum = maxHeightSequence[i]; // Start with the current height
10
                int minHeight = maxHeightSequence[i]; // Initialize the minimum height seen so far
               // Extend to the left of position 'i' and accumulate heights
                for (int leftIndex = i - 1; leftIndex >= 0; --leftIndex) {
                    minHeight = min(minHeight, maxHeightSequence[leftIndex]); // Update the min height
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                    tempSum += minHeight; // Add the minimum height to the temporary sum
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18
               // Reset minHeight for checking to the right of 'i'
19
               minHeight = maxHeightSequence[i];
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22
               // Extend to the right of position 'i' and accumulate heights
23
                for (int rightIndex = i + 1; rightIndex < sequenceLength; ++rightIndex) {</pre>
24
                   minHeight = min(minHeight, maxHeightSequence[rightIndex]); // Update the min height
                    tempSum += minHeight; // Add the minimum height to the temporary sum
25
26
27
               // Update maxSum if the current temporary sum is greater
28
               maxSum = max(maxSum, tempSum);
29
30
31
           // Return the maximum sum found
33
           return maxSum;
34
35 };
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Typescript Solution
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// This function calculates the maximum sum of heights based on the rules provided in the maxHeights array.

// Initialize the answer variable that holds the maximum sum of heights encountered.

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let maximumSum = 0;

```
// Iterate over the maxHeights array.
       for (let currentIndex = 0; currentIndex < arrayLength; ++currentIndex) {</pre>
           // Get the height at the current index.
           const currentHeight = maxHeights[currentIndex];
11
           // Initialize the minimum height variables for left and right directions.
           let minHeightToLeft = currentHeight;
13
           let totalSum = currentHeight;
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16
           // Iterate over the previous elements from the current index to calculate the sum.
           for (let leftIndex = currentIndex - 1; leftIndex >= 0; --leftIndex) {
17
               // Identify the new minimum height to the left.
               minHeightToLeft = Math.min(minHeightToLeft, maxHeights[leftIndex]);
               // Add the minimum height to the left to the total sum.
20
               totalSum += minHeightToLeft;
24
           // Reinitialize the minimum height to the current height for the right direction.
25
           let minHeightToRight = currentHeight;
26
27
           // Iterate over the next elements from the current index to calculate the sum.
28
           for (let rightIndex = currentIndex + 1; rightIndex < arrayLength; ++rightIndex) {</pre>
29
               // Identify the new minimum height to the right.
               minHeightToRight = Math.min(minHeightToRight, maxHeights[rightIndex]);
30
               // Add the minimum height to the right to the total sum.
32
               totalSum += minHeightToRight;
33
34
35
           // Compare the current total sum with the previous maximum sum and update maximumSum if necessary.
36
           maximumSum = Math.max(maximumSum, totalSum);
37
38
       // Return the maximum sum of heights after considering all possible positions.
       return maximumSum;
39
40 }
41
Time and Space Complexity
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Time Complexity

in maxHeights, the code iterates over the elements to its left and then to its right in separate for-loops. Each of these nested loops runs at most n - 1 times in the worst case, leading to roughly 2 * (n - 1) operations for each of the n elements, thus the quadratic time complexity.

Space Complexity

The space complexity of the provided code is 0(1) as it only uses a constant amount of extra space. Variables ans, n, i, x, y, t, and j are used for computations, but no additional space that scales with the input size is used. Therefore, the space used does not depend on the input size and remains constant.

The time complexity of the provided code is $O(n^2)$, where n is the length of the maxHeights list. This is because for each element x