String

the lexicographically largest subsequence comes first.

forms the basis of the solution's logic and its implementation in code.

This special binary substring is then added to the ans list.

substrings are arranged lexicographically largest to smallest.

List: Used to store substrings before sorting and joining.

string's structure, thus ensuring the largest possible configuration.

**Problem Description** 

Recursion

Hard

and 1's. The second rule is that every prefix (a substring starting from the first character) must not have more 0's than 1's. In other words, as we sequentially read the string from left to right, at no point should the number of 0's surpass the number of 1's. The task is to manipulate a given special binary string s through a series of permitted moves to create the lexicographically largest

Special binary strings are binary strings that strictly adhere to two rules. The first rule is that they must have an equal number of 0's

(i.e., the "biggest" or the "last" in dictionary order) string possible. Each move involves selecting two non-empty special substrings that are adjacent to each other and swapping them. To put this into perspective, consider a simplified version of alphabet ordering where we only have 0 and 1. Here, 1 is considered

Intuition

To solve this problem, we should realize that since the manipulated string must remain special, we are somewhat limited in how we

greater than 0, so for example, the string 1100 is lexicographically larger than 1001.

## can rearrange it. The key insight here is to think of the special binary string as a balanced sequence of parentheses, where 1 maps to

an open parenthesis (, and 0 maps to a close parenthesis). It's easier to recognize valid substrings if we utilize this analogy, because balanced parentheses are a common and well-understood problem. Recall that in a correctly balanced string of parentheses, the smallest unit is (). Similarly, in our binary string the smallest special

substring is 10. Building on this, we can deduce that any special binary string can be recursively divided into smaller special binary substrings. This is because a balanced parenthesis string is effectively a sequence of smaller balanced parenthesis strings. In terms of binary strings; a special binary string can be seen as a concatenation of 1, some special string 5, followed by 0 - 150. Our approach, therefore, involves recursively dividing the special binary string into these smaller substrings, solving for each smaller problem, and combining the results. After breaking the string down to manageable chunks, we sort them in reverse to ensure that

The provided solution implements this concept by counting the number of 1's and 0's. Each time the counts are equal, we've identified a valid special substring. It's sliced, solved recursively, and wrapped with 1 at the beginning and 0 at the end to maintain its special string status. These substrings are then collected and sorted reversely before being joined to form the largest possible string.

By ensuring a largest-to-smallest order in the final combination, we guarantee that the lexicographically largest string is formed. This

**Solution Approach** The Python solution's approach uses a simple but clever recursive strategy with sorting to generate the lexicographically largest

special binary string. Here's a breakdown of the algorithm and key parts of the implementation: 1. Base Case: If the input string s is empty, we return an empty string immediately, as there are no moves to make.

### ans: A list that will hold all valid special binary substrings we find. cnt: A counter that helps us track the balance of 1's and 0's.

2. Variables Initialization:

• i and j: Two pointers that mark the current position in the string and the beginning of a new special substring, respectively. 3. Finding Special Binary Substrings:

Whenever cnt becomes 0, we've identified a complete and valid special binary substring, ranging from indices j + 1 to i.

• Once a valid special binary substring is found, we recursively call makeLargestSpecial on the inner substring (excluding the

After separating and individually treating all the valid special binary substrings, we sort the ans list in reverse to ensure the

4. Recursion:

outer 1 and 0), to sort that substring's smaller units and make them as large as possible lexicographically.

As we iterate through the string s, we increase cnt when we find a 1 and decrease it when we find a 0.

After the recursion, we wrap this sorted substring with 1 at the start and 0 at the end to maintain its "special" property.

6. Data Structures and Patterns:

5. Sorting and Rebuilding:

formed.

• Recursion: Essential for breaking down the problem into smaller subproblems, in the manner of the "Divide and Conquer" paradigm.

• The sorted list is then joined into a single string, which is the lexicographically largest special binary string that can be

Through this method, we take advantage of the fact that the lexicographically largest combination of substring sequences comes from sorting them in descending order. The recursion ensures that this sorting logic is applied at every level of the special binary

Sorting: Critical to rearrange the substrings in reverse order for lexicographical precedence.

1. Base Case Check: The string s is not empty, so we proceed.

2. Variables Initialization:

**Example Walkthrough** 

o i and j: Initialize both as 0. These pointers will track the current position in the string and the start of a new special substring.

Let's illustrate the solution approach with a small example. Suppose we have the special binary string s = "11011000".

 $\circ$  At i = 3, s[i] = 1, so cnt becomes 2.  $\circ$  At i = 4, s[i] = 1, so cnt becomes 3.

3. Finding Special Binary Substrings: We iterate through s:

 $\circ$  At  $i = \emptyset$ , s[i] = 1, so cnt becomes 1.

o At i = 1, s[i] = 1, so cnt becomes 2.

 $\circ$  At i = 2, s[i] = 0, so cnt becomes 1.

 $\circ$  At i = 5, s[i] = 0, so cnt becomes 2.

 $\circ$  At i = 6, s[i] = 0, so cnt becomes 1. ○ At i = 7, s[i] = 0, so cnt becomes 0, indicating we've found a complete special binary substring 11011000 (from j = 0 to i

6. Data Structures and Patterns:

= 7).4. Recursion:

ans: Initialize as an empty list to hold all valid special binary substrings found.

cnt: Initialize as 0. It is used for tracking the balance of 1's and 0's.

 With the found substring "11011000", we ignore the first 1 and the last 0 (substring "101100"). Recursively call makeLargestSpecial on this inner substring to sort smaller units.

further). Wrap them with 1 and 0 to maintain "special" properties, becoming "1100" and "100" respectively.

• Recursively, we would find two smaller substrings within "101100": "1010" and "100". We apply the same process to them,

Through this process, we've transformed the initial string "11011000" to its lexicographically largest form "11001000", by applying the

recursively sorting inner substrings to get "1100" for the first and just "100" for the second (since it cannot be broken down

Add these substrings into ans: ans = ["1100", "100"]. 5. Sorting and Rebuilding:

A list, ans, holds and sorts substrings.

solution's recursive strategy and sorting mechanism.

def makeLargestSpecial(self, s: str) -> str:

• We sort ans in reverse to obtain ans = ["1100", "100"].

Join the sorted substrings in ans to form the final string: "11001000".

Recursion breaks the problem down and applies logic at each level.

Sorting is used to ensure lexicographical order is largest to smallest.

**Python Solution** 

# Initialize a list to store special binary strings.

# Iterate through the characters of the input string.

balance += 1 if s[i] == '1' else -1

 $start_index = i + 1$ 

special\_strings.sort(reverse=True)

public String makeLargestSpecial(String s) {

if (s.isEmpty()) {

return "";

# Increase balance for '1' and decrease for '0'.

# Add the current special string to the list.

// Base case: If the string is empty, return an empty string.

// A list to hold special strings during the processing.

special\_strings.append(inner\_special)

# Base case: if the input string is empty, return an empty string.

18 # When the balance is zero, a special string is found. 19 if balance == 0: 20 # Recursively process the inner substring (excluding the first and last characters), # and wrap it with '1' and '0' to make it a special string. 22 23 inner\_special = '1' + self.makeLargestSpecial(s[start\_index + 1 : i]) + '0'

# Initialize counters for the current balance of 1's and 0's and the start index of a substring.

# Update the start index to the next character after the current special string.

# Sort the list of special strings in descending order to create the largest number.

// Recursive method that rearranges a special binary string to create the largest possible string.

### 33 34 # Join the sorted special strings and return the result. 35 return ''.join(special\_strings) 36

Java Solution

class Solution {

1 #include <string>

2 #include <vector>

#include <algorithm>

using namespace std;

string makeLargestSpecial(string s) {

if (s.empty()) return s;

vector<string> specials;

if (counter == 0) {

1 function makeLargestSpecial(s: string): string {

const specials: string[] = [];

**if** (s.length === 0) {

return s;

// Base case: If the string is empty, return as is.

int counter = 0; // Initialized to count the balance of 1s and 0s.

// Iterate over the string to find and process special substrings.

for (int currentIdx = 0; currentIdx < s.size(); ++currentIdx) {</pre>

// Increment counter if '1', decrement if '0'.

// When counter is 0, we found a special string.

sort(specials.begin(), specials.end(), greater<string>());

let counter = 0; // Initialize to count the balance of '1's and '0's.

// Iterate over the string to find and process special substrings.

let startIdx = 0; // Index to keep track of the start of a special substring.

// Concatenate all special strings together using accumulate.

return accumulate(specials.begin(), specials.end(), string{});

counter += s[currentIdx] == '1' ? 1 : -1;

startIdx = currentIdx + 1;

// Base case: If the string is empty, return it as is.

// Define an array to hold special substrings.

int startIdx = 0; // Index to keep track of the start of a special substring.

// We concatenate '1' at the beginning and '0' at the end.

// Sort the special substrings in descending order to make the string largest.

// Set the start index for the next special substring.

// Make a special string by recursively calling makeLargestSpecial on the inner part.

specials.push\_back("1" + makeLargestSpecial(s.substr(startIdx + 1, currentIdx - startIdx - 1)) + "0");

// Define a vector to hold special substrings.

#include <numeric>

class Solution {

public:

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class Solution:

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if s == '':

balance = 0

start\_index = 0

return ''

special\_strings = []

for i in range(len(s)):

### 10 List<String> specialStrings = new ArrayList<>(); int count = 0; // Counter to check the number of '1's and '0's. 11 12 13 // Loop through the string to identify special substrings. for (int start = 0, end = 0; end < s.length(); ++end) {</pre> 14 15 // Increment counter for '1', decrement for '0'. 16 count += s.charAt(end) == '1' ? 1 : -1; 17 // When the count is zero, we found a balanced part of the special string. 18 **if** (count == 0) { 20 // Recursively process the inside of this special substring 21 // and add "1" at the beginning and "0" at the end. 22 String inner = makeLargestSpecial(s.substring(start + 1, end)); 23 specialStrings.add("1" + inner + "0"); 24 // Set the start to the next character after the current special substring. 26 start = end + 1;27 28 29 30 // Sort the processed special strings in reverse order to make the largest string. specialStrings.sort(Comparator.reverseOrder()); 31 32 33 // Join all sorted special substrings into one string and return it. 34 return String.join("", specialStrings); 35 36 } 37 C++ Solution

# Typescript Solution

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for (let currentIdx = 0; currentIdx < s.length; currentIdx++) {</pre>
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           // Increment counter if '1', decrement if '0'.
           counter += (s[currentIdx] === '1') ? 1 : -1;
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           // When counter is 0, we have found a special string.
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19
           if (counter === 0) {
               // Construct a special string by recursively calling makeLargestSpecial on the inner part,
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               // then concatenate '1' at the beginning and '0' at the end.
               specials.push('1' + makeLargestSpecial(s.substring(startIdx + 1, currentIdx)) + '0');
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               // Set the start index for the next potential special substring.
               startIdx = currentIdx + 1;
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       // Sort the special substrings in descending order to make the string largest.
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       specials.sort((a, b) => b.localeCompare(a));
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       // Concatenate all special strings together by joining the array elements.
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       return specials.join('');
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34 }
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   // The method can be exported if needed, to be used in other modules.
   export { makeLargestSpecial };
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Time and Space Complexity
Time Complexity
The time complexity of the function mainly stems from the recursive calls and the sorting operation. Let's break it down:
 1. Recursion: The function makeLargestSpecial is called recursively every time a special binary string is detected (when cnt
   returns to 0). The maximum depth of recursion is bounded by n (the length of the string), since in the worst case scenario, the
```

2. Sorting: After each inner special string is made largest through the recursive call, the resulting substrings are sorted in reverse order. This sorting step takes 0(k log k) where k is the number of special substrings at the same level of recursion. Since all special substrings from the entire input string are eventually sorted at the top level, in the worst-case scenario, this sorting can

- Considering both recursion and sorting, and the fact that sorting can happen at each level of recursion, the overall worst-case time complexity is  $0(n^2 \log n)$  because the sorting time  $(0(n \log n))$  could potentially be performed n times (at each character position
- **Space Complexity** The space complexity is primarily due to the recursive call stack and the space needed for storing intermediate substrings in the ans array:
  - call stack of depth n. This contributes O(n) in space complexity.

1. Call Stack: Since the recursion can go as deep as the length of the string in the worst-case scenario, we could potentially have a

- In summary, considering the call stack and the storage for intermediate strings, the space complexity of the algorithm is O(n). Note that the sorting operation is in-place and doesn't significantly add to space complexity.

take up to  $O(n \log n)$  time where n is the length of the input string.

whole string is a special binary string, which needs to be decomposed entirely.

# in the string in the worst case).

2. Intermediate Strings: The ans list stores intermediate substrings, which, together, will not exceed the length of the input string. Thus, this contributes 0(n) in space complexity. Additionally, substring slicing creates new strings, which may also contribute to

- the space complexity.