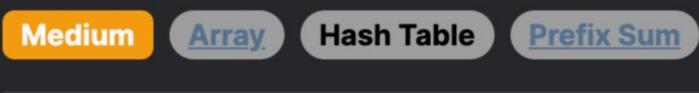
1983. Widest Pair of Indices With Equal Range Sum



In this problem, we have two binary arrays nums1 and nums2. Both arrays are of the same length and contain only 0s and 1s. Our goal

Problem Description

is to find the widest pair of indices (i, j) that satisfy two conditions: 1. i must be less than or equal to j, and

Leetcode Link

- 2. The sum of elements from i to j in nums1 must be equal to the sum of elements from i to j in nums2.
- The concept of the "widest" pair refers to the pair (i, j) with the biggest difference between i and j. This means that we are looking for the longest subarray where the sums of nums1 and nums2 are equal. The "distance" indicates the number of elements in

this subarray, which is calculated as j - i + 1. We need to return the "distance" of the widest pair of indices. If no pairs meet the condition, we should return 0.

To find the solution, we use the cumulative sums of both arrays and keep track of their differences at each index. If the difference

between the sums of subarrays from nums1 and nums2 up to the current index i has been seen before at some index j, then the subarrays from j+1 to i in both nums1 and nums2 must be equal.

Intuition

Here are the steps to solve this problem: 1. Maintain a dictionary d to store the first occurrence of each cumulative sum difference with its index. Initialize this dictionary with {0: -1}, meaning that if the difference is 0 at index 0, it can be considered as a subarray starting from index 0.

2. Iterate through the two arrays nums1 and nums2 simultaneously using enumerate(zip(nums1, nums2)) to get both the index and the elements.

with the maximum distance found so far, which is i - d[s].

add the current index i to the dictionary with the key being the sum difference s.

with {0: -1} to handle cases where the subarray starts from the first element.

During each iteration, we check if the current sum difference s is found in dictionary d.

from the previous index to the current index in both nums1 and nums2 are equal.

- 3. Calculate the cumulative difference s by subtracting the element of nums2 from the element of nums1 and adding it to the previous cumulative difference.
- 4. Check if this difference s has occurred before by looking it up in the dictionary d. If it exists, it means that there is a subarray that starts from the stored index plus 1 and ends at the current index i which has equal sums in nums1 and nums2. Update ans
- 6. After traversing through the whole arrays, the variable ans will contain the distance of the widest pair of indices. Return ans.

5. If the difference s does not exist in the dictionary, it means this is the first time we've seen this cumulative sum difference, so we

- The solution to this problem utilizes a dictionary data structure for efficient lookups and an iterative approach to find the widest pair where the subarrays have equal sums. Here's a deep dive into how the Solution class implements this:
- 1. Dictionary for Cumulative Difference Tracking:

The dictionary d is used to store cumulative sum differences as keys and their first occurring indices as values. It's initialized

As we loop through each element of both arrays, we calculate a running sum difference s by adding nums1[i] - nums2[i] to

2. Running Sum Difference Calculation:

Solution Approach

the current sum difference. This represents the difference between the cumulative sums up to the current index i. 3. Lookup and Widest Pair Tracking:

• If it exists, it indicates we have previously seen this sum difference at an earlier index, meaning the sums of subarrays

The distance of the current widest pair is calculated by subtracting the earlier index where the sum difference was the

function.

Example Walkthrough

same from the current index, i.e., i - d[s].

differences, which can be at most n in the worst case.

o If the sum difference s is not found in d, it implies this difference is encountered the first time at index i, so we add s as a key to d with the current index i as its value. This will potentially serve as the starting index for a future widest pair. 4. Returning the Result:

We update ans to the maximum of the current distance and the existing widest distance found so far.

The algorithm's complexity is primarily dictated by the single traversal of the input arrays, leading to an overall time complexity of O(n) where n is the number of elements in the input arrays. The space complexity is O(k), where k is the number of unique sum

After the loop is completed, ans holds the distance of the widest pair found. This value is returned as the output of the

The solution is efficient because it avoids nested loops by using the cumulative sum difference, which allows us to identify equal sum subarrays in linear time.

Initial State: • Let nums1 = [1, 0, 0, 1] and nums2 = [0, 1, 1, 0]. Initialize the dictionary d with {0: −1} to handle the case where the sum difference starts from index 0.

1. Start iterating over both arrays. Initialize a variable s to keep track of the cumulative sum difference, and ans to store the

2. Iteration 0: The elements at index 0 are nums1[0] = 1 and nums2[0] = 0.

maximum width found so far.

○ The sum difference s becomes 1 - 0 = 1.

nums1 is equal to the sum of elements in nums2.

 $index_map = \{0: -1\}$

max_width = 0

sum_diff = 0

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Step-by-Step Solution:

 This difference is not in d, so we add it: d[1] = 0. 3. Iteration 1: The elements at index 1 are nums1[1] = 0 and nums2[1] = 1.

Let's walk through a small example to illustrate the solution approach using two binary arrays nums1 and nums2.

 We have already seen 0 in d. \circ The width is 2 - (-1) + 1 = 4.

 \circ The sum difference s becomes 1 + (0 - 1) = 0, which is already in d.

 \circ The width between d[0] + 1 = 0 and index 1 is 1 - 0 + 1 = 2.

4. **Iteration 2:** The elements at index 2 are nums1[2] = 0 and nums2[2] = 1.

5. Iteration 3: The elements at index 3 are nums1[3] = 1 and nums2[3] = 0.

 \circ The sum difference s becomes 0 + (1 - 0) = 1, which is already in d.

The solution finds the widest subarray efficiently, utilizing a dictionary to track the first occurrence of each cumulative sum difference and iterating over the arrays only once.

 \circ We do not update ans because the current distance 3 - d[1] = 3 is not greater than the current ans (which is 4).

6. After traversing all items, ans is 4, which represents the distance of the widest pair of indices where the sum of elements in

○ The sum difference s remains 0 (since 0 - 0 + 0 - 1 = -1 and we add this to the previous s which was 1, making the new s

25 26 else: 27 # Otherwise, record the first occurrence of this sum difference index_map[sum_diff] = index 28 29

Update ans to 4, since this is larger than the previous value of ans.

• Update ans to 2.

back to 0).

Python Solution class Solution: def widestPairOfIndices(self, nums1: List[int], nums2: List[int]) -> int:

Initialize a dictionary to store the first occurrence of a

with a base case: 0 sum difference occurs at index -1.

Initialize variable to track the maximum width

Loop through each pair of values from the two lists

for index, (value1, value2) in enumerate(zip(nums1, nums2)):

Map<Integer, Integer> firstOccurrenceMap = new HashMap<>();

// Iterate over the elements of the input arrays.

if (firstOccurrenceMap.containsKey(sumDiff)) {

firstOccurrenceMap.put(sumDiff, i);

for (int i = 0; i < arrayLength; ++i) {</pre>

sumDiff += nums1[i] - nums2[i];

int arrayLength = nums1.length; // Length of the input arrays.

// Calculate the cumulative sum difference at current index.

// Return the maximum distance found (the widest pair of indices).

int widestPairOfIndices(vector<int>& nums1, vector<int>& nums2) {

int length = nums1.size(); // Length of the input arrays

prefixSumDifference += nums1[i] - nums2[i];

int maxWidth = 0; // To store the maximum width

// Iterate over the array elements

for (int i = 0; i < length; ++i) {</pre>

prefixSums[0] = -1; // Initialize with 0 difference at index -1

// Function to calculate the widest pair of indices where the sum of subarrays are equal

int prefixSumDifference = 0; // To store the running difference of prefix sums

// Update the running difference between nums1 and nums2 at index i

unordered_map<int, int> prefixSums; // Maps prefix sum difference to the earliest index

// Check if the cumulative sum difference has been seen before.

Initialize a prefix sum difference variable

sum_diff += value1 - value2

Return the maximum width found

return max_width

Java Solution

particular prefix sum difference. The sum difference is initialized

Update the running sum difference with the difference of the current pair

If the sum difference has been seen before, calculate the width

- if sum_diff in index_map: 20 # The width is the current index minus the index where the same 21 22 # sum difference was first recorded 23 width = index - index_map[sum_diff] 24
 - # Update the maximum width if this width is greater max_width = max(max_width, width)
 - class Solution { public int widestPairOfIndices(int[] nums1, int[] nums2) { // HashMap to store the first occurrence of the sum difference 'sumDiff' as a key and its index as the value.

int maxDistance = 0; // Variable to store the maximum distance (widest pair) found.

maxDistance = Math.max(maxDistance, i - firstOccurrenceMap.get(sumDiff));

firstOccurrenceMap.put(0, -1); // Initialize with sumDiff 0 occurring before the array starts.

int sumDiff = 0; // Variable to keep track of the cumulative sum difference between nums1 and nums2.

// If seen before, calculate the distance and update the maximum distance if current is greater.

// If not seen before, record the first occurrence of this sum difference with its index.

27 return maxDistance; 28 29 } 30

C++ Solution

1 class Solution {

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} else {

// If this difference has been seen before, calculate width 16 if (prefixSums.count(prefixSumDifference)) { 17 // Update maxWidth if we found a wider pair 18 19

maxWidth = max(maxWidth, i - prefixSums[prefixSumDifference]); 20 } else { // Else, store the current index for this difference 22 prefixSums[prefixSumDifference] = i; 23 24 25 // Return the maximum width found 26 return maxWidth; 27 28 }; 29 Typescript Solution // Importing necessary utility 2 import { max } from "lodash"; // Function to calculate the widest pair of indices where the sum of subarrays are equal function widestPairOfIndices(nums1: number[], nums2: number[]): number { let prefixSums: { [key: number]: number } = {}; // Maps prefix sum difference to the earliest index prefixSums[0] = -1; // Initialize with 0 difference at index -1let maxWidth = 0; // To store the maximum width let prefixSumDifference = 0; // To store the running difference of prefix sums let length = nums1.length; // Length of the input arrays 10 11 12 // Iterate over the array elements for (let i = 0; i < length; i++) {</pre> 13 // Update the running difference between nums1 and nums2 at index i prefixSumDifference += nums1[i] - nums2[i]; 16 // If this difference has been seen before, calculate width

Time and Space Complexity

Space Complexity:

} else {

return maxWidth;

the differences between the prefixes of the two lists and when each difference was first seen. **Time Complexity:**

• Within each iteration, the function performs constant-time operations: a calculation involving a and b, an if condition check, a

The given Python function widestPairOfIndices seeks to find the widest pair of indices (i, j) such that sum(nums1[k]) for k in

range(0, i + 1) is equal to sum(nums2[k]) for k in range(0, i + 1). It accomplishes this by using a dictionary d to keep track of

The time complexity of the function can be analyzed as follows:

if (prefixSumDifference in prefixSums) {

// Return the maximum width found

prefixSums[prefixSumDifference] = i;

// Update maxWidth if we found a wider pair

// Else, store the current index for this difference

maxWidth = max([maxWidth, i - prefixSums[prefixSumDifference]])!;

dictionary lookup, and an update to the dictionary (which on average is constant time for a hash table) and variable for the answer ans.

• There is a single loop that iterates over the elements of nums1 and nums2, which both have the same length, say n.

- These operations within the loop are conducted in constant time, regardless of the size of the input. As the loop runs n times where n is the length of the input lists, and each iteration is done in constant time, the time complexity of
- the function is O(n).

The space complexity of the function depends on the auxiliary space used, which is mainly for storing the dictionary d: • In the worst-case scenario, the dictionary could store a distinct entry for each element in the input lists if all prefix sums were

- unique. Thus, in the worst case, it could have up to n entries. Aside from this, the space used by variables s and ans is constant, as well as a few other intermediate variables.
- Therefore, the worst-case space complexity is O(n) where n is the length of the input lists.