

Problem Description

The task requires us to find the number of unique pairs (i, j) from a given integer array nums, where the first element of the pair is at an index less than the second element of the pair (1 < 1). The condition for these pairs to count is two-fold:

- The values at these indices must be the same (nums[i] == nums[j]).
- 2. The product of the indices i * j must be evenly divisible by a given integer k (which means (i * j) % k == 0 should be true).

In other words, for array nums with n integers and the given integer k, we need to count how many distinct pairs of indices have the same value in nums and their index product is a multiple of k.

This is a combinatorial problem that involves both array traversal and elementary number theory.

Intuition

two conditions mentioned. This means we: 1. Iterate through the array using two loops:

The intuition behind the solution is based on a brute-force approach where we evaluate all possible pairs to see if they satisfy the

- An outer loop, where we pick every element i starting from index 0 to n-2
 - An inner loop, where we pick every element j starting from index i+1 to n-1
- 2. For each pair (i, j) found through this iteration, check if nums [i] and nums [j] are equal. 3. If the numbers at i and j are equal, further check if the product (i * j) is divisible by k.
- 4. If both conditions hold true, count this pair towards our total count.
- The solution uses a single return statement with a sum of a generator expression. This generator expression iterates over all pairs as
- described and uses a conditional expression to count only those pairs that satisfy the two conditions. Since it loops through half of

but can be inefficient for large arrays since it performs checks for every index pair. Solution Approach

The implementation of the solution uses a brute-force algorithm with nested loops to iterate over all possible pairs of indices in the

the possible combinations (since i < j), it ensures that each unique pair is only considered once. This approach is simple and direct

given array. There is no use of additional data structures; the solution operates directly on the input array nums. Here is how the solution is implemented:

1. We define a function countPairs that takes in an array nums and an integer k as input. 2. Inside the function, we calculate the length of the array n. This is necessary to know the range for our iterations.

- The outer loop runs from ∅ to n-1. The variable i in this loop represents the first index of the pair.
 - The inner loop runs from i+1 to n. The variable j represents the second index of the pair.
- 4. For each pair (i, j), the algorithm performs two checks encapsulated in a conditional statement: First, it checks if nums[i] is equal to nums[j]. This is done by nums[i] == nums[j], ensuring that the values at these indices

3. We use a nested loop construct to generate all possible pairs:

- are the same.
- Second, it checks if the product of i and j (i * j) is divisible by k. This is achieved through (i * j) % k == 0, confirming
- that the product is divisible by k without a remainder. 5. The conditional statement is part of a generator expression that evaluates to True for each pair that meets the above conditions
- and False otherwise. 6. The sum function is then applied directly to this generator expression. In Python, True equates to 1 and False to 0, so summing the generator expression effectively counts the number of True (valid pairs) instances, which is the answer we need to return.
- One key reason why this is a brute-force algorithm is because it does not attempt to optimize by using any patterns or early exit conditions. The solution evaluates every index pair before reaching the count. This solution is straightforward and easy to understand, but it has a time complexity of O(n^2), which means that the algorithm's running time increases quadratically with the

size of the input array. Such time complexity is not ideal for large datasets. The algorithm does not use additional space beyond the input and intermediate variables, thus has a space complexity of O(1). To summarize, the implementation uses simple iteration and basic conditional checks to find and count the pairs that satisfy both

conditions. This brute-force approach is naturally chosen for its simplicity when dealing with small to moderately sized arrays.

Example Walkthrough Let's illustrate the solution approach with a small example.

Suppose we have an array nums = [1, 2, 1, 3, 2] and our given integer k = 2. We are interested in finding pairs (i, j) where

nums[i] == nums[j] and (i * j) % k == 0.

We define our function: countPairs(nums, k).

Following the steps outlined in the solution approach:

2. We determine the length of nums which is 5. We will need this for our loop ranges.

 \circ For i = 0, our pairs would be (0, 1), (0, 2), (0, 3), and <math>(0, 4).

3. We start our loops:

We see that nums [0] == nums [2] which is 1 == 1, and (0 * 2) % 2 == 0. So (0, 2) is a valid pair.

○ The outer loop will have i iterate from 0 to 4 (the range is 0 to n-1).

• No other pairs with i = 0 satisfy both conditions, so we move to i = 1.

The inner loop will begin from i+1 and go up to 5. So for i = 0, the inner loop will start at 1.

 None of these satisfy both conditions. Either nums[i] != nums[j] or (i * j) % 2 != 0. \circ Continue to the next index i = 2.

same and their product is divisible by the given k.

:return: The count of such pairs

pair_count += 1

#include <vector> // Include the vector header for vector usage

int countPairs(std::vector<int>& nums, int k) {

int count = 0; // Initialize count of pairs

// Iterate over all unique pairs of indices (i, j) where i < j.

// Check if the elements at indices i and j are equal.

// Check if the product of indices i and j is divisible by k.

for (let i = 0; i < length - 1; i++) {

for (let j = i + 1; j < length; j++) {

if (numbers[i] === numbers[j]) {

6. With i = 2, we consider pairs (2, 3) and (2, 4).

4. Now, we need to check every pair (i, j):

- Again, none of these are valid because the numbers at the indices don't match or their product isn't divisible by 2. \circ Move on to i = 3.
- 7. At i = 3, the only pair to consider is (3, 4). Since nums [3] != nums [4], this is not a valid pair.

def count_pairs(self, numbers: List[int], k: int) -> int:

:param numbers: List of integers to find pairs in

and the product of their indices is divisible by 'k'.

Counts the number of pairs in 'numbers' where the elements are equal

:param k: The divisor used to check if the product of indices is divisible

and the product of indices i and j is divisible by k

If the condition satisfies, increment the count of pairs

// Count pairs in an array where the elements are equal and their product is divisible by k

int size = nums.size(); // Get the size of the vector to avoid multiple size() calls within loop

if numbers[i] == numbers[j] and (i * j) % k == 0:

5. With i = 1, we consider pairs (1, 2), (1, 3), and (1, 4).

- Putting it all together, the only valid pair we have found is (0, 2). Therefore, the function countPairs (nums, k) will return 1. This example helps to illustrate how the solution iteratively checks each possible pair according to the algorithm's conditions,
- Python Solution

incrementing the count when both conditions are met. The result is a count of unique index pairs where the array values are the

10 11 # Get the length of the numbers list 12 num_length = len(numbers) 14 15 # Initialize the pairs count to zero

```
# Generate all unique pairs using two-pointer approach
            for i in range(num_length):
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                for j in range(i + 1, num_length):
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                   # Check the condition: numbers at index i and j are the same
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pair_count = 0

class Solution:

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           # Return the total pairs count that satisfies the condition
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           return pair_count
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31 # Note: The function name 'countPairs' has been modified to 'count_pairs'
32 # to follow the snake_case naming convention typical of Python function names.
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Java Solution
   class Solution {
       // Method to count the number of pairs (i, j) such that nums[i] == nums[j] and the product of i and j is divisible by k.
       public int countPairs(int[] nums, int k) {
           int length = nums.length; // Store the length of the input array nums.
                                    // Initialize the counter for the number of valid pairs to 0.
           int pairCount = 0;
 6
           // Iterate over the elements using two nested loops to consider all possible pairs (i, j) where i < j.
           for (int i = 0; i < length; ++i) {
 8
               for (int j = i + 1; j < length; ++j) {
                   // Check if the values at index i and j are equal and if the product of i and j is divisible by k.
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                   if (nums[i] == nums[j] && (i * j) % k == 0) {
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                       pairCount++; // If condition met, increment the count of valid pairs.
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           return pairCount; // Return the total number of valid pairs found.
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18 }
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C++ Solution
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// Iterate over all possible pairs for (int i = 0; i < size; ++i) { for (int j = i + 1; j < size; ++j) {

class Solution {

public:

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// Check if the elements are equal and if their product is divisible by k
                   if (nums[i] == nums[j] && (i * j) % k == 0) {
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                       ++count; // Increment count if the conditions are met
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           return count; // Return the total pair count
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22 };
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   // Note that this code uses <std::vector> which requires the vector header file.
  // The naming has been standardized to use camelCase for variable names.
   // Comments are added to explain the code in English.
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Typescript Solution
1 function countPairs(numbers: number[], k: number): number {
       // Get the length of the numbers array.
       const length = numbers.length;
       // Initialize a variable to count the number of valid pairs.
       let count = 0;
```

if ((i * j) % k === 0) { 14 // If both conditions are met, increment the count of valid pairs. 15 16 count++; 17 18

Time Complexity The provided code has a nested loop, where the outer loop runs from 0 to n-1 and the inner loop runs from 1+1 to n-1. Here, n is the

Time and Space Complexity

20 21 22 // Return the total count of valid pairs that satisfy the conditions. 23 return count; 24 } 25

length of the nums list. In the worst case, the number of iterations will be the sum of the series from 1 to n-1, which is (n-1)*(n)/2 or $0(n^2/2)$. Since

Space Complexity

constants are dropped in Big O notation, the time complexity is O(n^2).

The code doesn't use any additional data structures that grow with the input size. The only variables used are for loop counters and

temporary variables for calculations, which occupy constant space. Therefore, the space complexity is 0(1).