1627. Graph Connectivity With Threshold

Description

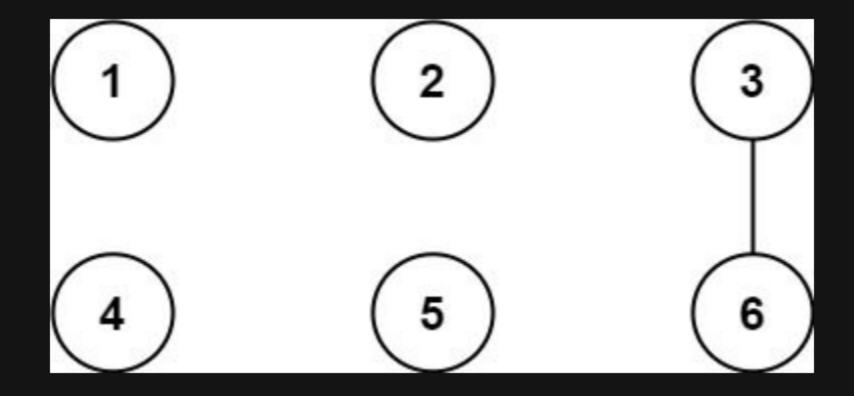
We have n cities labeled from 1 to n. Two different cities with labels x and y are directly connected by a bidirectional road if and only if x and y share a common divisor **strictly greater** than some threshold. More formally, cities with labels x and y have a road between them if there exists an integer z such that all of the following are true:

- x % z == 0,
- y % z == 0 , and
- z > threshold.

Given the two integers, [n] and [threshold], and an array of [queries], you must determine for each $[queries[i] = [a_i, b_i]]$ if cities $[a_i]$ and $[b_i]$ are connected directly or indirectly. (i.e. there is some path between them).

Return an array answer, where answer.length == queries.length and answer[i] is true if for the [i th query, there is a path between a i and [b i , or answer[i] is false if there is no path.

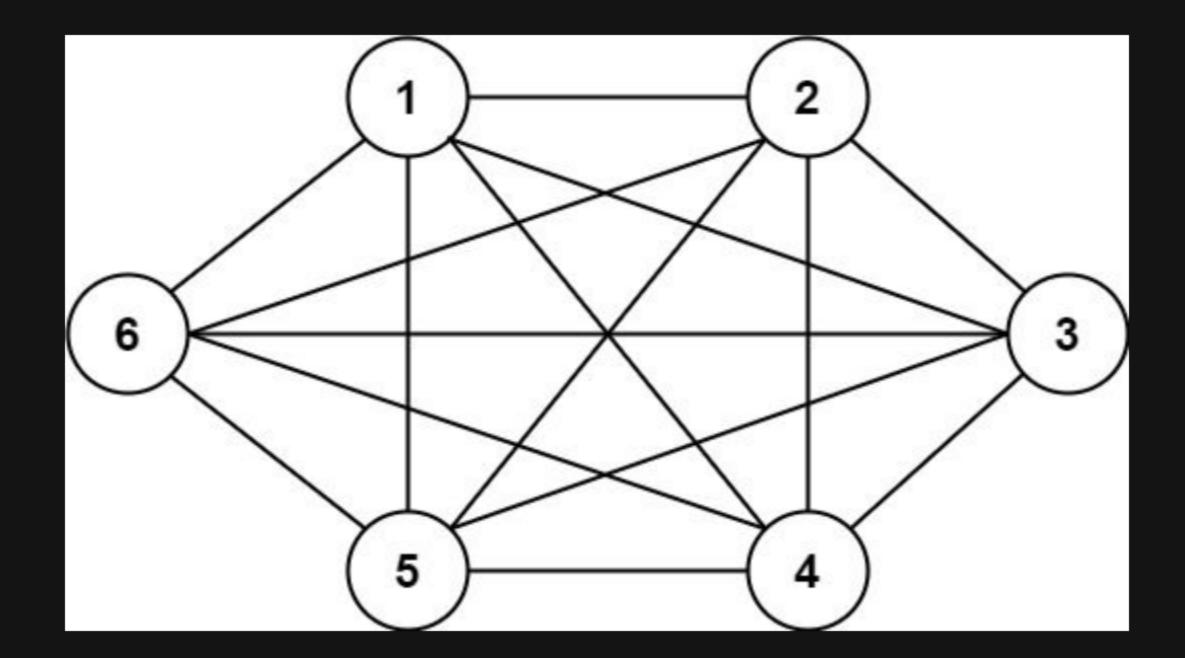
Example 1:



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Input: n = 6, threshold = 2, queries = [[1,4],[2,5],[3,6]]
Output: [false,false,true]
Explanation: The divisors for each number:

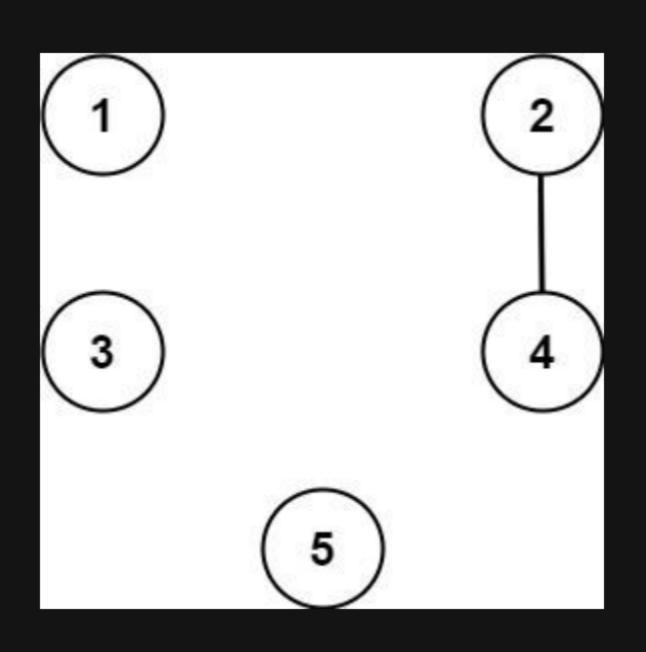
1:    1
2:    1,    2
3:    1,    3
4:    1,    2,    4
5:    1,    5
6:    1,    2,    3,    6
Using the underlined divisors above the threshold, only cities 3 and 6 share a common divisor, so they are the only ones directly connected. The result of each query:
[1,4]    1 is not connected to 4
[2,5]    2 is not connected to 5
[3,6]    3 is connected to 6 through path 3—6
```

Example 2:



```
Input: n = 6, threshold = 0, queries = [[4,5],[3,4],[3,2],[2,6],[1,3]]
Output: [true,true,true,true,true]
Explanation: The divisors for each number are the same as the previous example. However, since the threshold is 0,
all divisors can be used. Since all numbers share 1 as a divisor, all cities are connected.
```

Example 3:



```
Input: n = 5, threshold = 1, queries = [[4,5],[4,5],[3,2],[2,3],[3,4]]
Output: [false,false,false,false,false]
Explanation: Only cities 2 and 4 share a common divisor 2 which is strictly greater than the threshold 1, so they are the only ones directly connected.
Please notice that there can be multiple queries for the same pair of nodes [x, y], and that the query [x, y] is equivalent to the query [y, x].
```

Constraints:

- 2 <= n <= 10 ⁴
- 0 <= threshold <= n
- 1 <= queries.length <= 10 ⁵
- queries[i].length == 2
- $1 \ll a_i$, $b_i \ll cities$
- a _i != b _i