Problem Description

groups. The challenge is to find the minimum number of groups needed to satisfy two specific criteria:

1. Each group can only contain indices that point to the same value in 'nums'. That means if 'nums[i]' equals 'nums[j]', then 'i' and 'j'

In this problem, we're working with an array of integers called 'nums', and we've been tasked with organizing its indices into different

- can be in the same group.

 2. Every group should be as close in size as possible. The size difference between any two groups must not be more than 1.
- The goal is to achieve these conditions with the fewest number of groups possible.

Intuition

The solution strategy involves a clever use of counting and enumeration. Here's how we arrive at the solution:

distribution of values within 'nums'.

2. Understanding that the groups can have sizes that are either 'k' or 'k+1', where 'k' is the minimum occurrence count of any value,

we count partially filled groups as a whole one (this is done to minimize the number of groups).

we can enumerate possible group sizes starting from 'k' down to 1.

3. For each potential group size 'k', we look at every number's occurrence 'v' and check if it's possible to divide 'v' into groups of

1. We first count how frequently each number occurs in our 'nums' array using a hash table called 'cnt'. This helps us know the

- size 'k' or 'k+1' without violating our conditions (where the size of the groups does not differ by more than 1).

 4. If for any occurrence 'v', it is not possible to make such groups (that is, if 'v/k' is less than 'v % k'), we know that dividing into
- 4. If for any occurrence 'v', it is not possible to make such groups (that is, if 'v/k' is less than 'v % k'), we know that dividing into groups of this size would not satisfy the condition. So, we skip to the next group size.

5. If it is possible to form groups for a given 'k', we compute the number of groups by dividing 'v' by 'k+1' and rounding up to ensure

- 6. Since we are trying group sizes from largest to smallest, as soon as we find a valid grouping that satisfies our conditions, we can be assured that it's the optimal one with the minimum groups required.
- Solution Approach

By tackling it step-by-step, we ensure that we're checking all possible group sizes and finding the most economical way to distribute

The chosen approach to solve this problem can be broken down into a few strategic steps, employing common algorithms, data structures, and patterns.

First, let's detail the use of Python's Counter class for creating the frequency table, often referred to as a hash table, which is crucial

1. Hash Table Creation: Using Counter (nums), we count the occurrences of each number in nums. It allows us to easily access the

frequency v of each unique value in nums.

the indices in accordance with both conditions.

fewer groups if such groupings are possible.

for counting occurrences of each unique number from the array nums.

2. **Enumeration of Group Sizes**: We then attempt to find the minimum group sizes by starting from the minimum frequency k found in our hash table and decreasing towards 1. This takes advantage of the pattern that larger group sizes can potentially lead to

divided into groups of size k or k+1 without exceeding the size difference constraint. This is done by checking if $floor(v/k) < v \mod k$, where floor is implicit in integer division and mod is the modulo operation.

3. Divisibility Check: For each proposed group size k, we iterate through all frequencies v and check whether each value can be

next smaller size by breaking the current loop prematurely.

4. **Grouping Calculation**: If all frequencies can be grouped by the current k, it means that k is a valid group size. To ensure we use

k) // (k + 1) ensures we are creating as many full groups of size k+1 as possible before resorting to any groups of size k.

If this condition is true for any frequency v, it indicates that the size k cannot allow for a valid grouping, and we move to the

as few groups as possible, we want to create groups of k+1 first and only use groups of size k if necessary. The calculation (v +

This step is essential because we want the minimum number of groups, which means maximizing group size when possible

while still respecting the rules.

5. **Optimal Solution**: Since we enumerate k from its maximum possible value down to 1, the first k for which a valid grouping exists will give us the minimum number of groups needed to satisfy the problem conditions.

This algorithm is both efficient and effective, employing a hash table for quick value access and enumeration to systematically check

each group size. The first verified group size that holds the condition provides us with an optimal solution.

Enumeration from max to min: for k in range(min(cnt.values()), 0, -1)

1. Hash Table Creation: First, we use Counter (nums) to create a frequency table.

Divisibility check: if v // k < v % k
Group calculation: ans += (v + k) // (k + 1)
Optimal solution on first valid: if ans: return ans

Example Walkthrough

Let's walk through a small example to illustrate the solution approach with the array nums = [3,3,3,3,1,1,1].

• We get cnt = Counter({3: 4, 1: 3}). This shows us that the number 3 occurs 4 times, and the number 1 occurs 3 times.

2. Enumeration of Group Sizes: Next, we look for the minimum group size starting from min(cnt.values()), which is 3 in this case,

This approach elegantly combines these elements to guarantee the most efficient grouping under the given constraints.

3. Divisibility Check: For k = 3, we check each value in cnt to see if it can be divided into groups of size 3 or 4 (k+1) while

and decrement towards 1.

We iterate k from 3 down to 1.

visualized as: [3, 3, 3], [3], and [1, 1, 1].

from collections import Counter

Python Solution

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int k = 1e9;

int minGroups = k;

while (k > 0) {

for (auto& element : frequency) {

int tempGroupCount = 0;

break;

if (tempGroupCount > 0) {

return tempGroupCount;

// Decrement k and try again

for (auto& element : frequency) {

int freq = element.second;

if (freq / k < freq % k) {

tempGroupCount = 0;

30 # Example usage:

Java Solution

class Solution {

31 # solution = Solution()

respecting the size difference condition.

The formulae and concepts used:

Hash table frequency count: Counter(nums)

Since both checks passed, we move to the Grouping Calculation step.
 4. Grouping Calculation: Both numbers can create groups with size 3 or 4. We calculate the number of groups for each:

 \circ For the number 3 in nums (v = 4): ans += (4 + 3) // (4) results in ans += 2.

This gives 1 < 1, which is false, so a group size of 3 is valid for this occurrence.

This gives 1 < 0, which is false, so a group size of 3 is valid for this occurrence as well.

For the number 1 in nums (v = 3): ans += (3 + 3) // (4) results in ans += 1.
 Total ans now is 2 + 1 = 3.

 \circ For value v = 4 (number 3 in nums), we check if 4 // 3 < 4 % 3.

 \circ For value v = 3 (number 1 in nums), we check if 3 // 3 < 3 % 3.

5. **Optimal Solution**: The first valid group size was 3, which required 3 groups. Since this is the first valid solution we've encountered as we decremented from $k = \min(\text{cnt.values}())$, it is the optimal solution. Thus, we need a minimum of 3 groups to satisfy the problem conditions.

Putting it all together, we've found that the array nums = [3,3,3,3,1,1,1] can be organized into a minimum of 3 groups such that

each group contains indices that point to the same value, and the sizes of the groups differ by at most 1. The groups can be

class Solution:
 def minGroupsForValidAssignment(self, nums: List[int]) -> int:
 # Count the frequency of each number in the given list
 frequency_count = Counter(nums)

groups_needed = 0 # Initialize the number of groups needed for this group size

Calculate the number of groups needed for each number with its frequency

32 # print(solution.minGroupsForValidAssignment([1,2,3,3,3,4,4])) # Replace with the actual numbers list

* Calculates the minimum number of groups for a valid assignment based on the input array.

* The method counts the frequency of each number in the array and determines the smallest

* number of groups such that the frequency of the numbers is proportionally distributed.

// Initialize k as the number of elements in nums, the maximum possible frequency

If the distribution of frequency across groups is invalid, reset groups and break

for group_size in range(max(frequency_count.values()), 0, -1):

if frequency // group_size < frequency % group_size:</pre>

Iterate from the maximum frequency down to 1

Iterate through each frequency value

groups_needed = 0

* @param nums The input array containing numbers.

// Initialize k with an arbitrarily large number

// Variable to store the minimum number of groups

minGroups = min(minGroups, element.second);

// Decrease k until a valid configuration is found

// Check if the configuration is valid for current k

// If we found a valid group configuration, return it

// Find the smallest frequency to initialize the minimum number of groups

// Temporary variable to store count of groups for the current k

// If at any point we cannot satisfy the condition, break out

// Otherwise, add the number of groups needed for this frequency

tempGroupCount += (freq + k - 1) / k; // Use integer ceiling division

* @return The minimum number of groups required.

break

for frequency in frequency_count.values():

groups_needed += -(-frequency // (group_size + 1)) # Same as ceil division

If groups are successfully calculated, return the result

if groups_needed:

return groups_needed

If unable to calculate number of groups, return 0

return 0 # As per the original code (although this line is unnecessary since the function implicitly returns None if no return.

public int minGroupsForValidAssignment(int[] nums) { // Create a map to store the frequency count of each unique number in nums Map<Integer, Integer> frequencyCount = new HashMap<>(); for (int number : nums) { // Increment the frequency count for each number frequencyCount.merge(number, 1, Integer::sum); }

int k = nums.length;

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           // Find the smallest value among the frequencies to identify the initial group size
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           for (int frequency : frequencyCount.values()) {
                k = Math.min(k, frequency);
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           // Continuously try smaller values of k to optimize the number of groups
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           while (k > 0) {
               int groupsNeeded = 0;
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                for (int frequency : frequencyCount.values()) {
                   // If the frequency divided by k leaves a remainder larger than the quotient,
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                   // the current value of k isn't a valid group size, break and try a smaller k
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                   if (frequency % k > frequency / k) {
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                        groupsNeeded = 0;
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                        break;
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                   // Calculate the number of groups needed for the current value of k
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                    groupsNeeded += (frequency + k - 1) / k;
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               // If the number of needed groups is greater than zero, we've found a valid grouping
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               if (groupsNeeded > 0) {
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                    return groupsNeeded;
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               // Decrement k and try again for a smaller group size
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               k--;
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           // The code should never reach this point
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           return -1; // This line is just for the sake of completeness; logically, it'll always return from the loop
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50 }
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C++ Solution
 1 #include <vector>
 2 #include <unordered_map>
   #include <algorithm>
   using namespace std;
   class Solution {
   public:
       int minGroupsForValidAssignment(vector<int>& nums) {
           // Create a map to store the frequency of each number in nums
           unordered_map<int, int> frequency;
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           for (int num : nums) {
                frequency[num]++;
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--k;

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Typescript Solution
   function minGroupsForValidAssignment(nums: number[]): number {
       // A map to count the frequency of each number in the input array
       const frequencyMap: Map<number, number> = new Map();
       // Populating the frequency map
       for (const num of nums) {
           frequencyMap.set(num, (frequencyMap.get(num) || 0) + 1);
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       // Trying to find the minimum group size starting from the smallest frequency
       for (let groupSize = Math.min(...frequencyMap.values()); ; --groupSize) {
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            let groupsNeeded = 0; // Variable to hold the number of groups needed
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           // Calculate the number of groups needed for each unique number
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           for (const [_, frequency] of frequencyMap) {
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               // Calculate how many full groups can be formed with the current frequency
               const fullGroups = (frequency / groupSize) | 0;
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               // If the number of full groups is less than the remainder, we cannot form a valid group
20
               if (fullGroups < frequency % groupSize) {
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                   groupsNeeded = 0; // Reset groups needed, as the current group size is invalid
23
                   break;
24
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26
               // Increase the count of total groups needed
27
               groupsNeeded += Math.ceil(frequency / (groupSize + 1));
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           // If we found a valid number of groups, return it
           if (groupsNeeded) {
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               return groupsNeeded;
33
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           // Note: there is no explicit break in this loop for when group size reaches 0
36
           // The loop relies on eventually finding a valid group size before that happens
37
38 }
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```

Time and Space Complexity

well as their frequencies. The time complexity can be analyzed as follows: • Counter(nums) has a complexity of O(n) since it goes through each ele

counter.

Time Complexity

Counter(nums) has a complexity of O(n) since it goes through each element of nums.
 The outer loop runs at most min(cnt.values()) times which depends on the minimum frequency of a number in nums.
 The inner loop runs O(u) times where u is the number of unique elements in nums because it iterates through all values in the

The time complexity is actually not O(n) in general, it depends on both n, the length of nums, and also the range of unique values as

- So, the complexity is 0(n + min(min(cnt.values()), n/u) * u) which is $0(n + min_count * u)$ if we let min_count be min(cnt.values()).
- Giving a final verdict on time complexity without constraints of input can lead to a misleading statement since it can vary. If

 min_count is small, it could be close to linear but could also go up to 0(n^2) in the worst scenario when all elements are unique.

Space Complexity

The space complexity is O(n) for the counter dictionary that stores up to n unique values from nums where n is the length of nums. No other significant space is used.