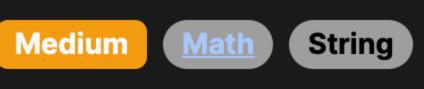
1759. Count Number of Homogenous Substrings



Problem Description

The task is to find the number of homogenous substrings in a given string s. A string is considered homogenous if all characters in the string are identical. A substring refers to a consecutive sequence of characters within a string. The answer should be returned modulo 10^9 + 7 to prevent overflow issues due to potentially large numbers.

For example, if s = "aaa", then the homogenous substrings are "a", "a", "a", "aa", "aa", and "aaa", which totals up to 6.

Intuition

1. We iterate over the string using two pointers, i and j.

To solve this problem efficiently, we can utilize a two-pointer technique.

- 2. The first pointer i marks the start of a potential homogenous substring, while j scans ahead to find where this substring ends (i.e., where a
- character different from s[i] is encountered). 3. For each character position i, we find the longest stretch of the same character by incrementally increasing j as long as s[j] is equal to s[i].
- that can be made, which is given by the formula (1 + cnt) * cnt / 2, where cnt is the length of the homogenous substring. 5. Why this formula? Consider a homogenous string of length n. We can make n single-character substrings, n-1 substrings of length 2, n-2 of

4. The length of the homogenous substring starting at i is (j - i). For each such substring, we calculate the number of homogenous substrings

- length 3, and so on, down to 1 substring of length n. This forms an arithmetic sequence that sums to n*(n+1)/2. 6. The answer is incremented by this count for each homogenous stretch we find.
- 7. We use the modulo operation to keep our calculations within the prescribed limit to avoid integer overflow.
- 8. The first pointer i is then set to j to start searching for the next homogenous substring.
- This approach optimizes the process by minimizing the number of times we traverse the string, leading to an efficient solution.
- **Solution Approach**

The implementation of the solution uses a two-pointer technique along with basic arithmetic calculations to find the number of

homogenous substrings. Here is the walkthrough of the code:

the homogenous substring.

• Two variables are declared, i being the start pointer (initialized at index 0) and n being the length of the input string s. • We also initialize a variable ans to store the cumulative number of homogenous substrings found.

2. A while loop is used to move j forward as long as s[j] is the same as s[i]. When s[j] is different from s[i], it means we have found the end of

The solution enters a loop that continues until the start pointer i has reached the end of the string (i < n):

• The function countHomogenous starts by initializing the variable mod to 10**9 + 7 for modulo operations to prevent overflow.

1. A second pointer j is set to start at the same position as i. This will be used to find the end of the current homogenous substring.

3. After the while loop, we now have a substring from index i to j-1 that is homogenous. The length of this substring is cnt = j-i. 4. To find the number of homogenous substrings within this section, we use the arithmetic series sum formula (1 + cnt) * cnt / 2, where cnt is

- the length of the homogenous substring.
- operation to make sure ans doesn't exceed 10**9 + 7. 6. Finally, we move the start pointer i to the position where j ended, as everything before j is already part of a homogenous substring we've counted.

5. The result is added to ans, which keeps the running total of homogenous substrings. Every time a new count is added, we perform a modulo

The use of the two-pointer technique efficiently reduces the time complexity since each character in the string is checked only

once. By only considering stretches of identical characters and using the arithmetic series sum formula, we avoid having to

The function ends by returning the total count ans as the resulting number of homogenous substrings. **Example Walkthrough**

• The countHomogenous function begins by initializing the variables (mod = 10^9 + 7, i = 0, n = 5, and ans = 0). The main loop starts with i < n, which is true at the start (i = 0).

We set the second pointer j = i = 0. We are now looking for a homogenous substring starting at 'a'.

Let's illustrate the solution approach with a small example. Assume the input string s = "abbba".

individually count each possible substring. This is what makes the algorithm efficient.

Starting with i = 0:

As we increment j, we realize that s[j] == s[i] only for j = 0. As soon as j becomes 1, s[j] becomes 'b', which is different

We found a homogenous substring 'a' from index 0 to 0. Thus cnt = j - i = 1 - 0 = 1.

- The number of homogenous substrings for this cnt is (1 + 1) * 1 / 2 = 1. We add this to ans, ans = 0 + 1 = 1.
- Next with i = 1: Set j to 1. The character at this index is 'b'.

We found a homogenous substring 'bbb' from index 1 to 3, so cnt = j - i = 4 - 1 = 3.

We then set i = j, so i is now 1 and we start looking for a new homogenous substring.

- We increment j while s[j] is the same as s[i]. This gives us j = 4 because indices 1, 2, and 3 are all 'b'.
- Using the formula for cnt = 3, the number of homogenous substrings is (1 + 3) * 3 / 2 = 6.

The i is moved to the index 4.

This is added to ans, which becomes ans = 1 + 6 = 7.

results in a cnt of 1, which provides a single homogenous substring 'a'.

homogenous substrings without having to count each one individually.

Define the modulus as mentioned in the problem statement.

Initialize the answer to count homogenous substrings.

substring_length = next_index - current_index

Find the end of the current homogenous substring.

Calculate the length of the current homogenous substring.

from s[i] ('a'). So the while loop stops with j = 1.

- The last character is evaluated but as there are no repeating characters beyond this point, j never increments. Therefore, this
- The answer, or total number of homogenous substrings, is summed up as ans = 7 + 1 = 8, which is the result returned by the function.

Initialize starting index for iterating the string and the length of the string.

while next_index < string_length and s[next_index] == s[current_index]:</pre>

Count the number of homogenous substrings which can be formed from

Python

This walkthrough simplifies how the solution makes efficient use of the two-pointer technique to calculate the number of

homogenous_count = 0 # Iterate over the string to find homogenous substrings. while current_index < string_length:</pre>

class Solution:

Solution Implementation

def countHomogenous(self, s: str) -> int:

next_index = current_index

next index += 1

current_index, string_length = 0, len(s)

 $modulo_factor = 10**9 + 7$

```
# the current homogenous substring using the formula for the sum of
            # the first n natural numbers: n * (n + 1) / 2.
            homogenous_count += (1 + substring_length) * substring_length // 2
            # Use modulo operation to avoid large numbers as per problem constraints.
            homogenous_count %= modulo_factor
            # Move to the beginning of the next potential homogenous substring.
            current_index = next_index
       # Return the final count of homogenous substrings.
       return homogenous_count
Java
class Solution {
    private static final int MOD = (int) 1e9 + 7;
    public int countHomogenous(String s) {
       // Length of the input string
       int length = s.length();
       // Variable to hold the total count of homogenous substrings
        long totalHomogenousSubstrings = 0;
       // Loop through the string characters
        for (int startIndex = 0, endIndex = 0; startIndex < length; startIndex = endIndex) {</pre>
           // Set the end index to the current start index
            endIndex = startIndex;
           // Extend the end index while the end character is the same as the start character
           while (endIndex < length && s.charAt(endIndex) == s.charAt(startIndex)) {</pre>
                endIndex++;
           // Calculate the length of the homogeneous substring
            int homogeneousLength = endIndex - startIndex;
           // Use the formula for sum of first n natural numbers to calculate the number of substrings
            totalHomogenousSubstrings += (long) (1 + homogeneousLength) * homogeneousLength / 2;
            // Apply modulo operation to prevent overflow
            totalHomogenousSubstrings %= MOD;
       // Cast the result to int before returning, since the final output must be an integer
       return (int) totalHomogenousSubstrings;
```

C++

public:

class Solution {

int countHomogenous(string s) {

end = start;

++end;

int count = end - start;

current_index, string_length = 0, len(s)

next_index = current_index

next_index += 1

Initialize the answer to count homogenous substrings.

inner loop throughout the entire run of the algorithm sum up to O(n).

```
return static_cast<int>(answer); // Return the answer as an integer.
  };
  TypeScript
  // Function to count the number of homogenous substrings in a given string.
  // A homogenous substring is one that consists of a single unique character.
  // For example, in the string "aa", there would be three homogenous substrings: "a", "a", and "aa".
  function countHomogenous(s: string): number {
      const MODULO: number = 1e9 + 7; // Define a constant for modulo to avoid large numbers
      const n: number = s.length; // Length of the input string
      let count: number = 0; // Initialize the count of homogenous substrings
      // Use two pointers to iterate through the string
      for (let startIndex = 0, currentIndex = 0; currentIndex < n; currentIndex++) {</pre>
          // If the current character is different from the starting character,
          // update the starting index to the current index
          if (s[startIndex] !== s[currentIndex]) {
              startIndex = currentIndex;
          // Calculate the number of homogenous substrings found so far based on the current sequence
          // Add the number of new homogenous substrings from startIndex to currentIndex
          count = (count + (currentIndex - startIndex + 1)) % MODULO;
      // Return the total count of homogenous substrings modulo the defined constant
      return count;
class Solution:
   def countHomogenous(self, s: str) -> int:
       # Define the modulus as mentioned in the problem statement.
       modulo_factor = 10**9 + 7
```

static constexpr int MOD = 1e9 + 7; // Define the modulus constant for preventing integer overflow.

// Method to count the number of homogenous substrings in the given string s.

long long answer = 0; // To store the final answer, initialized to 0.

// Compute the count of characters in the current homogenous substring.

// We use long long to avoid integer overflow during the calculation.

Initialize starting index for iterating the string and the length of the string.

while next_index < string_length and s[next_index] == s[current_index]:</pre>

// which is the sum of the first count natural numbers: count * (count + 1) / 2.

answer %= MOD; // Apply the modulus to keep the answer within the integer limits.

int length = s.size(); // The length of the input string.

// Loop through the string to count all homogenous substrings.

// Calculate the number of possible homogenous substrings,

answer += static_cast<long long>(count + 1) * count / 2;

for (int start = 0, end = 0; start < length; start = end) {</pre>

// Find the end of the current homogenous substring.

while (end < length && s[end] == s[start]) {</pre>

homogenous_count = 0 # Iterate over the string to find homogenous substrings. while current_index < string_length:</pre> # Find the end of the current homogenous substring.

```
# Calculate the length of the current homogenous substring.
           substring_length = next_index - current_index
           # Count the number of homogenous substrings which can be formed from
           # the current homogenous substring using the formula for the sum of
           # the first n natural numbers: n * (n + 1) / 2.
           homogenous_count += (1 + substring_length) * substring_length // 2
           # Use modulo operation to avoid large numbers as per problem constraints.
           homogenous count %= modulo factor
           # Move to the beginning of the next potential homogenous substring.
           current index = next index
       # Return the final count of homogenous substrings.
       return homogenous_count
Time and Space Complexity
  The time complexity of the given code is O(n), where n is the length of the string s. This is because each character in the string is
  checked exactly once to form homogenous substrings (characters that are the same and contiguous). The inner while loop runs
```

The space complexity of the code is 0(1). This is because the algorithm uses a constant number of additional variables (mod, i, n, ans, j, cnt) which do not scale with the input size - they use a constant amount of space regardless of the length of the string s.

only once for each homogenous substring, and since it only moves j to the end of a homogenous substring, the iterations of the