2099. Find Subsequence of Length K With the Largest Sum

Sorting Heap (Priority Queue)

size k will always include the k largest elements from the original nums array.

Problem Description

Easy

Hash Table

array nums that consists of k elements and has the largest possible sum. A subsequence is defined as a sequence that can be obtained from the original array by removing some or no elements, without changing the order of the remaining elements. The problem statement requires us to return any subsequence that satisfies the condition of having k elements and the largest sum. If there are multiple subsequences with the same largest sum, we can return any one of them.

In this problem, we are given an array of integers named nums and another integer k. Our goal is to find a subsequence of the

Intuition To approach this solution, we need to focus on finding the elements that would contribute to the largest sum. Naturally, larger

numbers will contribute more to the sum than smaller numbers. Therefore, the subsequence with the largest sum within a given

solution achieves this by first finding the indices of the k largest elements, and then reconstructing the subsequence by accessing the elements using these indices in their sorted order. 1. The solution starts by creating a list of indices idx for all elements in nums.

However, since we are interested in a subsequence, it's important to maintain the original order of elements. The provided

2. It sorts this list of indices idx based on the values in nums that they correspond to, using a lambda function as the key to the sort method. 3. By sorting idx, the last k indices now represent the largest k numbers in nums.

- 4. The subsequence is then created by selecting the elements of nums using the sorted list of the last k indices. 5. Since we need to return the subsequence in its original order, we sort the list of the last k indices, ensuring that the corresponding k elements
- will be in the same order as they appeared in nums.
- original order from nums. Solution Approach

By following this method, we can efficiently retrieve any subsequence of length k that yields the largest sum while maintaining its

In the provided reference solution, several key programming concepts and Python-specific tools are employed to extract the k largest sum subsequence:

this solution, list comprehensions are used twice, once to generate the sorted indices and then to generate the actual

List Comprehension: Python's list comprehension is used to concisely generate lists without writing out complex for-loops. In

subsequence.

Sorting with Custom Key Function: list.sort() method is used with a custom key function. The key function is provided by a lambda expression lambda i: nums[i] which sorts the list of indices idx based on the value of elements in nums at each

- index. Slicing: Python's slicing operation [-k:] is used to obtain the last k elements from the sorted list of indices, which represents the indices of the k largest numbers.
- Next, sort the list idx using the sort method with a key that references the original list's values nums [i]. After sorting, for an array nums = [1, 3, 5, 7, 9], and say k = 3, the idx array will look like [4, 3, 2, 1, 0] because we are sorting by the

Start by creating a list of indices idx with range(len(nums)) which basically gives us a list [0, 1, 2, ..., len(nums) - 1].

2].

in nums, which means the highest numbers come first:

Slicing to Get Largest Elements

Creating the Final Subsequence

values of nums in descending order.

this by sorting the slice of indices.

The steps to implement this approach are as follows:

Each index here is a direct reference to the corresponding element in nums.

Slice the last k elements from the sorted idx to get the indices of the k largest elements. For our example, we will get [4, 3,

Before creating the final subsequence, we need to ensure that its order is the same as the original array's order. We achieve

comprehension to achieve this: [nums[i] for i in sorted(idx[-k:])]. This algorithm effectively combines Python's powerful list manipulation features to provide a simple yet efficient solution. The complexity of the solution is dominated by the sorting step, which is typically O(n log n) where n is the number of elements in

Finally, the solution applies the sorted indices to nums to produce the subsequence with the largest sum. We use a list

sum. **Initial Steps**

Let's take a small sample array nums = [7, 1, 5, 3, 6, 4] and assume we want a subsequence of length k = 3 with the largest

1. First, create an array of indices, idx, which will initially be [0, 1, 2, 3, 4, 5]. **Sorting by Reference to nums Values** 2. Next, we sort the idx array while referencing the elements it points to in nums. The sorting will be done in descending order based on the values

3. Then we take the last k elements of the sorted idx. In this case k = 3, so we slice the last three indices, getting [2, 5, 3] which corresponds to nums values [5, 4, 3].

Result

get [2, 3, 5].

nums.

Example Walkthrough

Sorting Indices to Maintain Original Order 4. Before creating the final subsequence, sort the slice [2, 5, 3] to maintain the original order of elements from nums. When we sort this slice, we

sorted(idx[-k:])] becomes [nums[2], nums[3], nums[5]] which evaluates to [5, 3, 4].

5. Using these sorted indices, we construct our subsequence by taking the values from nums at these positions, hence [nums[i] for i in

○ After sorting, idx becomes [0, 4, 2, 5, 3, 1] since the corresponding nums values are [7, 6, 5, 4, 3, 1].

The subsequence [5, 3, 4] has a sum of 12, which is the largest sum possible for any 3 element subsequence in the original

efficiently solve the problem.

Solution Implementation

nums. Thus, the final answer for this example is [5, 3, 4].

def maxSubsequence(self, nums: List[int], k: int) -> List[int]:

Create a list of indices that correspond to the elements in 'nums'.

Sort the list of indices based on the values in 'nums' they point to.

Select the last 'k' elements from the sorted indices since they point to

Return the subsequence of 'nums' pointed by the sorted largest indices,

// Initialize an array 'ans' to store the result subsequence of length k

// Create a list 'indices' to keep track of the original indices of the array elements

which constitutes the k-largest elements in their original order.

max_subsequence = [nums[i] for i in sorted_largest_indices]

In summary, by identifying and extracting the indices of the k largest numbers, sorting those indices to maintain the initial array's order, and then building a subsequence from these indices, we maximally leverage Python's list manipulation abilities to

Python class Solution:

indices = list(range(len(nums)))

return max_subsequence

int[] ans = new int[k];

indices.add(i);

Java

class Solution {

indices.sort(key=lambda i: nums[i])

public int[] maxSubsequence(int[] nums, int k) {

List<Integer> indices = new ArrayList<>();

for (int i = 0; i < nums.length; ++i) {</pre>

// Loop to fill 'indices' with the array indices

vector<int> maxSubsequence(vector<int>& nums, int k) {

// Pair of index and value from the input array

indexedNums.push_back({i, nums[i]});

sort(indexedNums.begin(), indexedNums.begin() + k,

// Prepare a vector to store the answer subsequence

[](const auto& x1, const auto& x2) {

return x1.first < x2.first;</pre>

ans.push_back(indexedNums[i].second);

function maxSubsequence(nums: number[], k: number): number[] {

firstKElements.sort((a, b) => a.index - b.index);

// Return the final answer subsequence

indices = list(range(len(nums)))

largest_indices = indices[-k:]

indices.sort(key=lambda i: nums[i])

The time complexity of the code is as follows:

return answer;

class Solution:

// Prepare an array to store the answer subsequence

def maxSubsequence(self, nums: List[int], k: int) -> List[int]:

the elements with the 'k' largest values in 'nums'.

sorted_largest_indices = sorted(largest_indices)

let answer: number[] = firstKElements.map(element => element.value);

Create a list of indices that correspond to the elements in 'nums'.

Sort the list of indices based on the values in 'nums' they point to.

Sort the selected indices to maintain the original order of 'nums'.

Select the last 'k' elements from the sorted indices since they point to

// Return the final answer subsequence

// Sort the indexedNums by their values in descending order

// Populate the indexedNums with pairs of indices and their respective values

sort(indexedNums.begin(), indexedNums.end(), [](const auto& x1, const auto& x2) {

ans.reserve(k); // Reserve space for 'k' elements to avoid reallocations

// Populate the answer vector with the 'k' largest elements in their original order

// Sort only the first 'k' elements of indexedNums by their original indices to maintain the original order

// Size of the input array

int numSize = nums.size();

});

});

return ans;

// Size of the input array

let numSize: number = nums.length;

TypeScript

vector<int> ans;

for (int i = 0; i < k; ++i) {

vector<pair<int, int>> indexedNums;

for (int i = 0; i < numSize; ++i) {</pre>

return x1.second > x2.second;

the elements with the 'k' largest values in 'nums'. largest_indices = indices[-k:] # Sort the selected indices to maintain the original order of 'nums'. sorted_largest_indices = sorted(largest_indices)

```
// Sort 'indices' based on the values in 'nums' from highest to lowest
        indices.sort((i1, i2) -> Integer.compare(nums[i2], nums[i1]));
       // Initialize a temporary array 'topIndices' to store the first k sorted indices
       int[] topIndices = new int[k];
        for (int i = 0; i < k; ++i) {
            topIndices[i] = indices.get(i);
       // Sort 'topIndices' to maintain the original order of selected k elements
       Arrays.sort(topIndices);
       // Fill the 'ans' array with the elements corresponding to the sorted indices
        for (int i = 0; i < k; ++i) {
            ans[i] = nums[topIndices[i]];
       // Return the result array containing the max subsequence of length k
       return ans;
C++
#include <vector>
#include <algorithm>
class Solution {
public:
    // Method to find the subsequence of 'k' numbers with the largest sum
```

```
// Pair of index and value from the input array
let indexedNums: { index: number, value: number }[] = [];
// Populate the indexedNums with objects containing indices and their respective values
for (let i = 0; i < numSize; ++i) {</pre>
    indexedNums.push({ index: i, value: nums[i] });
// Sort the indexedNums by their values in descending order
indexedNums.sort((a, b) => b.value - a.value);
// Sort only the first 'k' elements of indexedNums by their original indices to maintain the original order
let firstKElements: { index: number, value: number }[] = indexedNums.slice(0, k);
```

```
# Return the subsequence of 'nums' pointed by the sorted largest indices,
       # which constitutes the k-largest elements in their original order.
       max subsequence = [nums[i] for i in sorted largest indices]
       return max_subsequence
Time and Space Complexity
```

Creating the idx list with list comprehension has a time complexity of O(n) where n is the number of elements in nums.

No additional space other than variables for sorting and slicing are used, which does not depend on the size of the input and

- Slicing the last k elements from the sorted idx list is O(k) because it requires iterating over the k elements to create a new list.
- Sorting the sliced list of k indices is $O(k \log k)$.

Sorting the idx list using the key, which is based on the values in nums, with the sort() function is $0(n \log n)$.

- The list comprehension in the return statement to create the final list of numbers from their indices takes 0(k). The overall time complexity is therefore dominated by the $O(n \log n)$ step, which is the sorting of the idx list.
- The space complexity of the code is:

The additional list idx that stores the indices takes O(n) space.

- hence is 0(1). The output list that is returned has k elements, so it takes 0(k) space.
 - Therefore, the total space complexity is 0(n + k), since you need to store the indices and the final output list.