

**Problem Description** 

A company is conducting interviews and needs to fly interviewees to two different cities, city a and city b. They have a total of 2n people to interview and need to send exactly n people to each city. The cost of flying each person to each city is different and is provided in a list known as costs. The costs list is structured such that costs[i] = [aCost\_i, bCost\_i], with aCost\_i representing the cost to fly the ith person to city a and bCost\_i representing the cost to fly the ith person to city b. The goal is to determine the minimum possible total cost to fly exactly n people to city a and n people to city b.

# Intuition

The intuition behind the solution is to use a greedy strategy. A greedy algorithm makes the locally optimal choice at each step with the hope of finding the global optimum. In the context of this problem, we want to minimize the total cost of flying people to the two cities. To do this, we need to find the n people for whom the difference between flying to city a and city b is the largest in favor of city a, and fly them there. This will ensure that we are saving as much money as possible on the first n flights.

By sorting the costs array based on the difference aCost\_i - bCost\_i in ascending order, we can easily find the n people to fly to

city a (those at the start of the sorted list) and the n people to fly to city b (those at the end of the list). This sorting allows us to consider the relative costs of flying each person to each city and ensure that, overall, we are making the most cost-effective decisions. The solution handles the sorting and then computes the total cost by summing up the costs for flying the first n people to city a and

**Solution Approach** 

# The solution approach for the given problem uses a greedy algorithm, which is a common pattern for optimization problems. The

the last n people to city b.

idea here is to make a sequence of choices that are locally optimal in order to reach a solution that is close to or equal to the optimal global solution. Here's a breakdown of how the approach is implemented: Steps Involved:

### 1. Sorting Costs: First, we sort the costs array by the difference in cost between flying to city a and city b (aCost\_i - bCost\_i). By doing this, we cluster people who are cheaper to fly to city a at the beginning of the array and those cheaper to city b towards

the end. costs.sort(key=lambda x: x[0] - x[1])

2. Calculating Half Length: Since we need to send n people to each city and we have 2n people in total, we find n by dividing the

length of the costs array by 2. Note that we're using a bit shift operation to divide by 2, which is equivalent but slightly faster in

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most programming languages.
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city b, which gives us the minimum cost. sum(costs[i][0] + costs[i + n][1] for i in range(n))

3. Determining Minimum Cost: Finally, we take the sum of the costs for flying the first n people to city a and the last n people to

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    A list of lists is used to store the flying costs to both cities for each person.
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### Algorithms & Patterns Used:

**Data Structures Used:** 

n = len(costs) >> 1

• Greedy Algorithm: The algorithm sorts the array and then selects the first n elements for one city and the last n elements for the other city, based on the local optimality of the cost difference.

### List Comprehension: Python list comprehension is used to sum the costs which result in a concise and readable implementation.

individual costs to minimize the total expenditure.

1 costs = [[400, 200], [300, 600], [100, 500], [200, 300]]

**Complexity Analysis:** • The time complexity of the solution is dominated by the sorting step, which is 0(n log n) where n is the number of people.

Sorting: A key step in the greedy approach where the array is sorted based on a specific condition (cost difference here).

with the size of the input. The algorithm implemented here effectively balances the costs for both cities by understanding and utilizing the differences in

The space complexity is 0(1) or constant space, aside from the input, since no additional data structures are used that grow

Let's consider an example where a company has 2n = 4 people (n = 2) to send to cities a and b. The costs for flying each person to cities a and b are provided as follows:

# Now, let's walk through the solution approach step by step using this example:

len(costs) >> 1.

1 Person 1: 400 - 200 = 200

2 Person 2: 300 - 600 = -300

3 Person 3: 100 - 500 = -400

4 Person 4: 200 - 300 = -100

Example Walkthrough

1. Sorting Costs First, we sort the costs array based on the difference between flying to city a and city b, so we calculate aCost\_i - bCost\_i for each person:

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After sorting these based on the difference in ascending order, our costs array looks like this:
 1 costs = [[100, 500], [300, 600], [200, 300], [400, 200]]
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1 For city a: costs[0][0] + costs[1][0] = 100 + 300 = 4002 For city b: costs[2][1] + costs[3][1] = 300 + 200 = 500

# Sort the costs list based on the cost difference between the two cities (A and B).

sum(costs[i + num\_people][1] for i in range(num\_people))

num people = len(costs) // 2 # Using // for floor division which is standard in Python 3.

def two\_city\_sched\_cost(self, costs: List[List[int]]) -> int:

# Compute the number of people that should go to each city.

total\_cost = sum(costs[i][0] for i in range(num\_people)) + \

return totalCost; // Return the accumulated total cost

// Function to calculate the minimum cost to send n people to two cities.

// Calculate half the length of the costs array since we're splitting the group in two

// Iterate over the first half of the sorted array for city A costs and the second

// Add the cost of sending the i-th person to city A from the first half

// Add the cost of sending the i-th person to city B from the second half

# Since it's a two-city schedule, half the people will go to each city.

costs.sort(key=lambda cost: cost[0] - cost[1])

Now, the first two people on the list are the ones we will fly to city a, and the last two to city b.

The total minimum cost to fly all these people is the sum of the costs for city a and city b: 400 + 500 = 900. Through this example, we can see how the company efficiently reduces the total cost for flying out interviewees to two different

2. Calculating Half Length Here, n is already given as 2 (since 2n = 4). In a more general sense, we would compute n as

3. Determining Minimum Cost Lastly, we will add the cost for flying the first n people to city a and the last n people to city b:

**Python Solution** 

# This helps in figuring out the cheaper city for each person in a way that can minimize the total cost.

cities by implementing a greedy algorithm that focuses on sending each person to the city that results in the lowest additional cost.

#### 13 # Calculate the total minimum cost by adding the cost of sending the first half # of the people to city A and the remaining half to city B. 14 15 # This works because the costs array is now sorted in a way that the first half # are the people who have a cheaper cost going to city A compared 16 17 # to city B, and vice versa for the second half.

return total\_cost

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from typing import List

class Solution:

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23 # Example usage:
24 # costs = [[10,20],[30,200],[400,50],[30,20]]
25 # solution = Solution()
26 # print(solution.two_city_sched_cost(costs)) # Should print the result of the cost calculation based on the provided costs array.
Java Solution
   import java.util.Arrays; // Import the Arrays class to use the sort method
   class Solution {
       public int twoCitySchedCost(int[][] costs) {
           // Sort the array based on the cost difference between the two cities (a and b)
           // for each person. The comparator subtracts the cost of going to city B from the
           // cost of going to city A for each person, and sorts based on these differences.
           Arrays.sort(costs, (a, b) \rightarrow (a[0] - a[1]) - (b[0] - b[1]));
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           int totalCost = 0; // Initialize total cost to 0
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           int n = costs.length / 2; // Calculate n, where n is half the number of people (half will go to city A, half to city B)
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           // Accumulate the minimum cost by sending the first n people to city A
           // and the remaining n people to city B based on the sorted order
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           for (int i = 0; i < n; ++i) {
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               totalCost += costs[i][0]; // Add cost for city A
16
               totalCost += costs[i + n][1]; // Add cost for city B
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C++ Solution

1 #include <vector>

class Solution {

public:

2 #include <algorithm> // Include necessary headers

int twoCitySchedCost(vector<vector<int>>& costs) {

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// Sort the input vector based on the cost difference for attending city A and city B
           sort(costs.begin(), costs.end(), [](const vector<int>& a, const vector<int>& b) {
                return a[0] - a[1] < b[0] - b[1];
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           });
           // The total number of people is twice the number of people we need to send to one city
           int totalPeople = costs.size();
           // Calculate the number of people to send to each city
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           int halfPeople = totalPeople / 2;
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           // Initialize answer to store the total minimized cost
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           int totalCost = 0;
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           // Calculate the minimum total cost
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           for (int i = 0; i < halfPeople; ++i) {</pre>
22
               // Add up the cost of sending the first half of people to city A
23
               totalCost += costs[i][0];
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               // Add up the cost of sending the second half of people to city B
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               totalCost += costs[i + halfPeople][1];
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           // Return the computed total cost
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           return totalCost;
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31 };
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Typescript Solution
   function twoCitySchedCost(costs: number[][]): number {
       // Sort the array of costs based on the difference in cost between sending
       // a person to city A and city B.
       costs.sort((firstPair, secondPair) => (firstPair[0] - firstPair[1]) - (secondPair[0] - secondPair[1]));
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#### 22 // Return the computed total cost return totalCost; 23 24 } 25

let totalCost = 0;

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const halfLength = costs.length / 2;

for (let i = 0; i < halfLength; ++i) {</pre>

totalCost += costs[i][0];

Time and Space Complexity

// Initialize an accumulator for the total cost

totalCost += costs[i + halfLength][1];

// half for city B costs to compute the minimum total cost

## **Time Complexity** The time complexity of the provided code consists of the following parts:

**Space Complexity** 

n), where n is the total number of elements in the list. Here n is 2N since we're supposed to send 2N people to two cities (N to each city).

2. Summing up the costs: The list comprehension iterates over the first half and the second half of the sorted list, resulting in N iterations (since n = len(costs) >> 1 computes to N). The summing operation inside the list comprehension is O(1) for each element, so the overall time for this part is O(N). Combining these two parts, the total time complexity is  $O(n \log n) + O(N)$ , which simplifies to  $O(n \log n)$  since logarithmic factors

1. Sorting the costs list: Since the sort() function in Python uses the Timsort algorithm, which has a time complexity of O(n log

are dominant for large n. Hence, the time complexity of the code is  $0(n \log n)$ .

The space complexity of the code analysis involves:

- 1. The sorted list costs: Sorting is done in-place, so it does not consume additional space proportional to the input size.
- 2. The list comprehension for summing the costs and the range used within: both utilize only a small constant amount of additional space.

Therefore, the space complexity of the entire operation is 0(1), as no significant additional space is used that would increase with the size of the input.

Overall, the space complexity of the code is 0(1).