# 915. Partition Array into Disjoint Intervals

Medium <u>Array</u>

# The problem gives us an integer array called <a href="nums">nums</a>. We are required to split this array into two contiguous subarrays named <a href="left">left</a>

**Problem Description** 

and right. The conditions for the split are: 1. Every element in left should be less than or equal to every element in right.

2. Both subarrays left and right should be non-empty.

- 3. The subarray left should be as small as possible.

the lowest value at each index that right can have.

For clarity: If nums is [5,0,3,8,6], one correct partition could be left = [5,0,3] and right = [8,6], and we would return 3

The goal is to return the length of the left subarray after partitioning it according to the rules mentioned above.

because left has a length of 3. Intuition

### To solve this problem, we need to find the point where we can divide the array into <code>left</code> and <code>right</code> such that every element in left is smaller or equal to the elements in right.

Intuitively, as we traverse nums from left to right, we can keep track of the running maximum value. This value will indicate the highest number that must be included in the left subarray to satisfy the condition that all elements in left are smaller or equal

to the elements in right. Conversely, if we traverse the array from right to left, we can compute the running minimum. This minimum will provide us with

The partition point should be at a place where the running maximum from the left side is less than or equal to the running minimum on the right side. This means that all values to the left of the partition point can form the left subarray, as they are guaranteed to be less than or equal to all values to the right of the partition point, which would form the right subarray.

**Solution Approach** The implementation follows a two-step process: **Step 1: Calculate Minimums From Right to Left** 

• An array mi is initialized to store the running minimums from the right-hand side of the given nums array. This new array will have n+1 elements,

where n is the length of nums, and is initialized with inf which represents infinity, guaranteeing that all actual numbers in nums are smaller

### than inf. • We iterate over nums starting from the last element to the first (right to left), updating mi such that every mi[i] contains the smallest element

from nums[i] to nums[n-1].

## **Step 2: Find Partition Index**

def partitionDisjoint(self, nums: List[int]) -> int:

mi = [float('inf')] \* (n + 1)

for i in range(n - 1, -1, -1):

subarray that satisfies the given partitioning conditions.

Starting from the last element of nums, we fill mi as follows:

(Note: The example is following 1-based indexes for this explanation)

• Index i = 1, nums[i] = 1, mx = 1, mi[i] = 12. Condition mx <= mi[i] is True.

• Index i = 2, nums[i] = 1, mx = 1, mi[i] = 6. Condition mx <= mi[i] is True.

• Index i = 5, nums[i] = 6, mx = 6, mi[i] = 0. Condition mx <= mi[i] is False.

• Index i = 6, nums[i] = 12, mx = 12, mi[i] = inf. Condition mx <= mi[i] is True.

As we can see, the last true condition for  $mx \ll mi[i]$  occurred at index i = 3.

- A variable mx is initialized to zero to keep track of the running maximum as we iterate through the array from left to right (important for determining the left subarray). • We iterate over the <a href="mailto:nums">nums</a>, using <a href="mailto:enumerate">enumerate</a>() to get both the index and the value at each step.
- For each element in nums, we update mx to be the maximum of mx and the current element v. This running maximum represents the largest element that would have to be included in the left subarray for all elements in left to be smaller or equal to any element in right.

• We then check if mx is less than or equal to mi[i] at this index. If this condition holds, it signifies that all elements up to this index in nums can

## form the left subarray, and they are all less than or equal to any element to their right. The index i is then returned as the size of left.

- The algorithm described above uses a greedy approach to find the earliest point where the left could end, ensuring the conditions for the partition are met. By leveraging the pre-computed minimums and maintaining a running maximum, we can make this determination in a single pass over the input array after the initial setup, resulting in an efficient solution.

n = len(nums)

Here's a snippet of the implementation described: class Solution:

mi[i] = min(nums[i], mi[i + 1])mx = 0for i, v in enumerate(nums, 1): mx = max(mx, v)**if** mx <= mi[i]: return i

The above python code snippet represents the full implementation of the solution approach for finding the length of the left

Let's walk through a small example to illustrate the solution approach described above.

```
Example Walkthrough
  Consider the array nums = [1, 1, 1, 0, 6, 12].
  Step 1: Calculate Minimums From Right to Left
  We need to initialize an array mi to store the running minimums from the right-hand side of the nums array.
```

mi = [inf, 12, 6, 6, 0, 0, inf]

### **Step 2: Find Partition Index** We traverse nums from left to right, keeping track of the running maximum (mx).

• Index i = 3, nums[i] = 1, mx = 1, mi[i] = 6. Condition mx <= mi[i] is True. • Index i = 4, nums[i] = 0, mx = 1, mi[i] = 0. Condition mx <= mi[i] is False.

1], which has a length of 3, and that is the answer returned by our function.

def partitionDisjoint(self, nums: List[int]) -> int:

right\_min = [float('inf')] \* (length + 1)

# Iterate through the array to find the partition point.

# Return the position as the partition index.

# Get the length of the input array

for i in range(length -1, -1, -1):

for i, value in enumerate(nums):

left\_max = max(left\_max, value)

if left max <= right min[i + 1]:</pre>

public int partitionDisjoint(int[] nums) {

for (int  $i = length - 1; i >= 0; --i) {$ 

int length = nums.length;

At each index, our mx and mi arrays will look like this:

solution = Solution() assert solution.partitionDisjoint([1, 1, 1, 0, 6, 12]) == 3

# Create a list to store the minimum values encountered from right to left.

# Initialize each position with positive infinity for later comparison.

# Populate the right min list with the minimum values from right to left.

# Update the running maximum value found in the left partition.

minRightArray[length] = nums[length - 1]; // Initialize the last element.

// Fill minRightArray with the minimum values starting from the end.

minRightArray[i] = Math.min(nums[i], minRightArray[i + 1]);

// Track the maximum element found so far from the left.

// to every element on the right of the partition.

leftMax = std::max(leftMax, currentVal);

for (int i = 1; i <= size; ++i) {</pre>

return i;

return 0;

int currentVal = nums[i - 1];

// we found our partition point.

function partitionDisjoint(nums: number[]): number {

// Get the size of the input array.

if (leftMax <= rightMinimums[i]) {</pre>

// Return the partition index.

// Iterate to find the partition point where every element on the left is less than or equal

// If the current maximum of the left is less than or equal to the minimum of the right,

// Return 0 as a default (though the problem guarantees a solution will be found before this).

int leftMax = 0;

**Python** class Solution:

Therefore, the smallest index i we found that satisfies the conditions is 3. This suggests our left subarray should be [1, 1,

right\_min[i] = min(nums[i], right\_min[i + 1]) # Initialize a variable to keep track of the maximum value seen so far from left to right. left max = 0

# Check if the left max value is less than or equal to the right min at the current position.

# i + 1 is used because the left partition includes the current element at index i.

int[] minRightArray = new int[length + 1]; // This will store the minimum from right to left.

# This means all values to the left are less than or equal to values to the right, satisfying the condition.

The implementation for this example would execute the partitionDisjoint method on the array and return 3.

```
return i + 1
# The function will always return within the loop above, as the partition is guaranteed to exist.
```

Java

class Solution {

Solution Implementation

length = len(nums)

```
int maxLeft = 0; // This will hold the maximum value in the left partition.
       // Iterate through the array to find the partition.
        for (int i = 1; i <= length; ++i) {
            int currentValue = nums[i - 1];
                                              // Current value from nums array.
           maxLeft = Math.max(maxLeft, currentValue); // Update maxLeft with the current value if it's greater.
           // If maxLeft is less than or equal to the minimum in the right partition,
           // we have found the partition point.
           if (maxLeft <= minRightArray[i]) {</pre>
               return i; // The partition index is i.
        return 0; // Default return value if no partition is found (won't occur given problem constraints).
#include <vector>
#include <limits>
class Solution {
public:
   int partitionDisjoint(std::vector<int>& nums) {
       // Get the size of the input array.
       int size = nums.size();
       // Create a vector to keep minimums encountered from the right side of the array.
       // Initialize every element to INT MAX.
       std::vector<int> rightMinimums(size + 1, std::numeric_limits<int>::max());
       // Fill the rightMinimums array with the actual minimums encountered from the right.
        for (int i = size - 1; i >= 0; ---i) {
            rightMinimums[i] = std::min(nums[i], rightMinimums[i + 1]);
```

```
let size = nums.length;
```

**}**;

**TypeScript** 

```
// Create an array to keep track of the minimums encountered from the right side of the array.
   // Initialize every element to Infinity.
   let rightMinimums: number[] = new Array(size + 1).fill(Infinity);
   // Populate the rightMinimums array with the actual minimum values encountered from the right.
   for (let i = size - 1; i >= 0; --i) {
        rightMinimums[i] = Math.min(nums[i], rightMinimums[i + 1]);
   // Variable to track the maximum element found so far from the left side.
   let leftMax = 0;
   // Iterate through the array to find the partition point.
   // All elements to the left of this point are less than or equal to every element on the right.
   for (let i = 1; i <= size; ++i) {
        let currentValue = nums[i - 1]:
        leftMax = Math.max(leftMax, currentValue);
       // Check if the current maximum of the left is less than or equal to the minimum on the right.
       if (leftMax <= rightMinimums[i]) {</pre>
           // If so, the current index is the correct partition index, so return it.
           return i;
   // The problem statement quarantees a solution before reaching this point.
   // Return 0 as a default (non-achievable in this problem context).
   return 0;
class Solution:
   def partitionDisjoint(self. nums: List[int]) -> int:
       # Get the length of the input array
       length = len(nums)
       # Create a list to store the minimum values encountered from right to left.
       # Initialize each position with positive infinity for later comparison.
       right_min = [float('inf')] * (length + 1)
       # Populate the right min list with the minimum values from right to left.
       for i in range(length -1, -1, -1):
            right_min[i] = min(nums[i], right_min[i + 1])
       # Initialize a variable to keep track of the maximum value seen so far from left to right.
       left_max = 0
       # Iterate through the array to find the partition point.
       for i, value in enumerate(nums):
           # Update the running maximum value found in the left partition.
            left_max = max(left_max, value)
```

## # The function will always return within the loop above, as the partition is guaranteed to exist. Time and Space Complexity

return i + 1

if left max <= right min[i + 1]:</pre>

# Return the position as the partition index.

The time complexity of the provided code is O(n), where n is the length of the array nums. This is because there are two separate for-loops that each iterate over the array once. The first for-loop goes in reverse to fill the mi array with the minimum value encountered so far from the right side of the array. The second for-loop finds the maximum so far and compares it with values in the mi array to find the partition point. Each loop runs independently of the other and both iterate over the array once, hence maintaining a linear time complexity. The space complexity of the code is also O(n). This is due to the additional array mi that stores the minimum values up to the

# This means all values to the left are less than or equal to values to the right, satisfying the condition.

# Check if the left max value is less than or equal to the right min at the current position.

# i + 1 is used because the left partition includes the current element at index i.

current index from the right side of the array. This mi array is the same length as the input array nums, so the space complexity is directly proportional to the input size.