### 795. Number of Subarrays with Bounded Maximum



**Problem Description** 

**Leetcode Link** 

Given an array of integers called nums, and two other integers known as left and right, the problem asks us to calculate how many non-empty subarrays (continuous parts of the array) have a maximum element that falls within the range [left, right]. To clarify, for a subarray to be counted, its largest number must be greater than or equal to left and less than or equal to right. Essentially, we're tasked with identifying portions of the array where if you pick out the biggest number, it wouldn't be smaller than left or larger than right.

### Intuition

provided solution uses a helper function f(x) which counts subarrays where all elements are less than or equal to x. The idea is that we can count all subarrays that have elements under or equal to right, which captures all subarrays that could potentially meet our condition. Then, we subtract the count of subarrays with elements under or equal to left - 1, which represents subarrays that don't meet our condition (since their maximum would be too small).

To solve this problem, we can use the concept of counting subarrays with elements less than or equal to a given maximum. The

The reasoning here is that when we have the count of subarrays with maximums not surpassing right, we include both valid

subarrays (those we are looking for) and subarrays that have maximums that are too small. We don't want the latter, so we find out how many of them there are (using the same count technique but with a maximum of left - 1) and remove them from our total. The difference gives us exactly the number of valid subarrays we're seeking. The f(x) function works by scanning through the array and using a temporary count t to keep track of valid subarrays ending at the

current position. If a value is encountered that is not greater than x, it can be added to existing valid subarrays to form new ones; hence, t is incremented by 1. If a value is too large, t is reset to 0, as no new valid subarrays can end at this position. The variable cnt accumulates the count of all valid subarrays as we iterate through nums. **Solution Approach** 

### The approach taken in the given solution involves a clever use of prefix sums, a common technique in which we construct an array of sums that represent the sum of elements up to a certain index. However, in this specific implementation, rather than directly

computing a sum, we are counting the possible subarrays up to a certain index that respect the maximum value condition. Let's break down the f(x) function, which is at the heart of the approach: 1. Initialize cnt and t to 0. cnt will hold the total count of subarrays that do not exceed the maximum allowed element x, and t will

2. Iterate over each value v in the nums array.

count such subarrays ending at the current index in nums.

- 3. If v is greater than x, then any subarray including v cannot be part of our solution, so we reset t to 0. This essentially says "you can't start or continue a valid subarray from this point."
- 4. If v is less than or equal to x, then we can extend every subarray counted by t with this new value v plus one extra: the subarray that only includes v itself. Thus, we increment t by 1.
- 5. For every iteration, we add t to cnt which accumulates our count. The outer function numSubarrayBoundedMax makes use of f(x) to apply our subarray counting method twice:
  - First, we count all valid subarrays with maximums not more than right, which gives us f(right).

that have their maximum element between left and right, inclusive.

The subarrays we want to exclude from our count are the ones where the maximum element value is strictly less than 'left'. By

counting these with f(left - 1), we get the count of subarrays with maximum values in the range [0, left-1]. Thus, when we subtract f(left - 1) from f(right), we remove these invalid subarrays from our total, leaving us with the number of valid subarrays

• Then, we count the subarrays that are strictly smaller than left, which is f(left - 1).

This elegant subtraction of prefix counts helps to efficiently compute the final desired count without having to evaluate each subarray independently, thereby reducing the time complexity. **Example Walkthrough** 

Let's walk through a small example to illustrate the solution approach: Suppose we have the array nums = [2, 1, 4, 3] and the integers left = 2 and right = 3. We want to count the number of

First, let's consider the f(x) function that counts the subarrays with maximum elements less than or equal to x:

2. For v = 2 (first value), t is incremented to 1 (t += 1), so cnt = 1.

3. For v = 1 (second value), t is incremented to 2 (t += 1), so cnt = 3.

subarrays where the maximum is at least left and at most right.

• Using f(right), which is f(3): 1. Initialize cnt = 0 and t = 0.

4. For v = 4 (third value), t is reset to 0, as 4 is greater than 3. 5. For v = 3 (fourth value), t is incremented to 1 (t += 1), so cnt = 4.

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f(3) gives us a count of 4 subarrays.

    Using f(left - 1), which is f(1):

      1. Initialize cnt = 0 and t = 0.
     2. For v = 2 (first value), t is reset to 0, since 2 is greater than 1.
     3. For v = 1 (second value), t is incremented to 1 (t += 1), so cnt = 1.
     4. For v = 4 (third value), t is reset to 0, as it's greater than 1.
     5. For v = 3 (fourth value), t is reset again to 0, since 3 is also greater than 1.
    f(1) gives us a count of 1 subarray.
Now, we calculate the number of subarrays we are looking for by subtracting f(left - 1) from f(right):

    Count of subarrays we are seeking = f(right) - f(left - 1) = 4 - 1 = 3.

So, there are 3 subarrays where the maximum element is between 2 and 3, inclusive. These subarrays are [2], [2, 1], and [3]. This
method allows us to efficiently calculate the desired count without having to examine each subarray individually.
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from typing import List class Solution: def numSubarrayBoundedMax(self, nums: List[int], left: int, right: int) -> int:

# Define a helper function that counts the number of subarrays

# Reset temporary count if value is greater than the bound,

# or increase it if value is within the subarray criteria.

temp\_count = 0 if value > bound else temp\_count + 1

# Calculate the number of subarrays where the maximum element is

int count = 0; // Count of subarrays meeting the condition

// Iterate through each element of the array

currentSubarrayCount = 0;

for (int num : nums) {

} else {

if (num <= bound) {</pre>

# by 'right' and subtracting those strictly bounded by 'left - 1'.

# between 'left' and 'right' by taking the count of subarrays bounded

# with element values less than or equal to 'bound'.

def count\_subarrays(bound: int) -> int:

count = temp\_count = 0

for value in nums:

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                    # Add the current temporary count to the total count.
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                    count += temp_count
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                return count
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Python Solution

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# This ensures that we only include subarrays where the maximum
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           # value is at least 'left'.
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           return count_subarrays(right) - count_subarrays(left - 1)
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Java Solution
1 class Solution {
       // Method to count the number of subarrays with elements bounded by left and right
       public int numSubarrayBoundedMax(int[] nums, int left, int right) {
           // Calculate the number of subarrays where the maximum element is at most right
           // and subtract the count of subarrays where the maximum element is less than left
           return countSubarraysAtMost(nums, right) - countSubarraysAtMost(nums, left - 1);
       // Helper method to count the number of subarrays with elements at most x
9
       private int countSubarraysAtMost(int[] nums, int bound) {
10
```

// If the current element is not greater than bound, extend the current subarray sequence

currentSubarrayCount += 1; // Include this number in the current subarray

// If current element is greater than bound, reset the temporary count

// Number of subarrays where the max element is less than or equal to right

int currentSubarrayCount = 0; // Temporary count for current valid subarray sequence

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               // Add the count of valid subarrays up to the current index
25
               count += currentSubarrayCount;
26
27
28
           // Return the total count of valid subarrays
29
           return count;
30
31 }
32
C++ Solution
 1 class Solution {
2 public:
       // Function finds the number of subarrays with elements bounded by left and right.
       int numSubarrayBoundedMax(vector<int>& nums, int left, int right) {
           // Lambda function to count subarrays where the max element is less than or equal to a given bound.
           auto countSubarrays = [&](int bound) {
               int count = 0; // Number of valid subarrays
                int currentLength = 0; // Current length of the subarray satisfying the condition
 9
               // Iterate through the elements of the nums vector
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               for (int value : nums) {
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                   // If the current value is greater than the bound, reset currentLength to 0
                   // If not, increase currentLength by 1 (extend the valid subarray by the current element)
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14
                    currentLength = value > bound ? 0 : currentLength + 1;
15
                   // Add the length of the current valid subarray to count
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                   // This adds all subarray ends with this element and bounded by the value
                    count += currentLength;
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               return count;
           };
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```

### 24 // and subtracting those where the max element is less than left (to exclude them) 25 return countSubarrays(right) - countSubarrays(left - 1); 26 27 }; 28

```
Typescript Solution
  // The type definition for a list of numbers
2 type NumberList = number[];
   // Function finds the number of subarrays with elements bounded by 'left' and 'right'.
5 // Params:
6 // nums: The input array of numbers.
7 // left: The lower bound for the maximum of the subarrays.
8 // right: The upper bound for the maximum of the subarrays.
9 // Returns: The count of subarrays meeting the criteria.
   function numSubarrayBoundedMax(nums: NumberList, left: number, right: number): number {
       // Lambda function to count subarrays where the max element is less than or equal to a given bound.
12
       // Params:
       // bound: The bound to check for in subarrays.
       // Returns: The count of subarrays where the maximum element is less than or equal to the bound.
14
       const countSubarrays = (bound: number): number => {
15
           let count: number = 0; // Number of valid subarrays
16
           let currentLength: number = 0; // Current length of the subarray satisfying the condition
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18
           // Iterate through the elements of the nums array
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           for (let value of nums) {
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21
               // If the current value is greater than the bound, reset currentLength to 0
               // If not, increase currentLength by 1 (extend the valid subarray by the current element)
23
               currentLength = value > bound ? 0 : currentLength + 1;
24
25
               // Add the length of the current valid subarray to count
26
               // This adds all subarray ends with this element and bounded by the value
27
               count += currentLength;
28
           return count;
       };
```

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Time and Space Complexity

## Time Complexity

to 0(n).

30 31 32 // Number of subarrays where the max element is less than or equal to right 33 // and subtracting those where the max element is less than left (to exclude them) return countSubarrays(right) - countSubarrays(left - 1); 34 35 } 36 // Example usage: // const result = numSubarrayBoundedMax([2, 1, 4, 3], 2, 3);// console.log(result); // Outputs the count of subarrays meeting the criteria

represented as n. Given that there are no nested loops and each operation inside the loop takes constant time, the time taken by f(x) is proportional

to the number of elements in the array, which is O(n). Since f(x) is called twice, the total time complexity is O(2n), which simplifies

The time complexity of the provided code is determined by the function f(x) which is called twice within the numSubarrayBoundedMax

method. This function iterates through each element of the nums array exactly once. The number of elements in the nums array is

## **Space Complexity**

The space complexity of the code can be analyzed by looking at the space taken by variables that could scale with the input. The

function f(x) uses two variables cnt and t that do not scale with the size of the input array and are thus constant extra space (0(1)).

Since there are no additional data structures utilized that grow proportionally with the input size, the space complexity remains constant, irrespective of the size of the input array nums. Therefore, the space complexity of the code is 0(1).