

# 1865. Finding Pairs With a Certain Sum

Medium   Design   Array   Hash Table

[Leetcode Link](#)

## Problem Description

You are provided with two integer arrays, `nums1` and `nums2`, and the goal is to create a data structure that supports two types of queries. Firstly, you should be able to add a positive integer to an element at a given index in `nums2`. Secondly, you need to count the number of pairs  $(i, j)$  where the sum of `nums1[i]` and `nums2[j]` is equal to a specified value (`tot`). The pairs should only be considered if `i` and `j` are valid indexes within `nums1` and `nums2`, respectively.

To accomplish the task, you should implement a class `FindSumPairs` with the following methods:

- `FindSumPairs(int[] nums1, int[] nums2)`: a constructor that initializes the object with the two integer arrays, `nums1` and `nums2`.
- `add(int index, int val)`: a method that adds the integer `val` to the element at `index` in `nums2`.
- `count(int tot)`: a method that returns the number of pairs  $(i, j)$  where `nums1[i] + nums2[j]` equals the integer `tot`.

## Intuition

The intuitive approach to solving this problem involves efficient data retrieval and update methods. If we were to perform a brute force approach for the count operation, we would iterate through all possible  $(i, j)$  pairs to find their sum and compare with `tot`, which would result in a time-consuming process, especially with large arrays.

A better way is to use a hash table to keep track of the frequency of each number in `nums2`. This allows us to quickly calculate how many times a certain number that can be added to elements of `nums1` appears in `nums2` to reach the required sum (`tot`).

Here's the intuition for the methods:

- The constructor initializes the object and also creates a counter (`Counter` from `collections` in Python) that maps each number in `nums2` to its frequency.
- The `add` method updates the specific element in `nums2` and adjusts the counter correspondingly. If a number's frequency changes (because it's being increased by `val`), we decrease the count of the old number and increase the count for the new, updated number.
- The `count` method calculates the required pairs by traversing through `nums1` and checking if the complement to reach `tot` (calculated as `tot - nums1[i]`) exists in the hash table (counter for `nums2`). The sum of all the frequencies of these complements gives us the total number of valid pairs that meet the condition.

## Solution Approach

The implementation of the `FindSumPairs` class makes use of hash tables to store elements and their frequencies from `nums2`. This is essentially a mapping from each unique integer in `nums2` to the number of times it appears. The Python `Counter` class from the `collections` module is used here for this purpose as it automatically counts the frequency of items in a list.

Here's the breakdown of the implementation:

The `__init__` function of the `FindSumPairs` class initializes two properties, `nums1` and `nums2`, with the corresponding input arrays. Additionally, a `Counter` object named `cnt` is created to store the frequency count of elements in `nums2`.

```
1 def __init__(self, nums1: List[int], nums2: List[int]):
2     self.nums1 = nums1
3     self.nums2 = nums2
4     self.cnt = Counter(nums2)
```

The `add` function takes in an `index` and a value `val` to add to `nums2` at the specified index. Before updating `nums2[index]` with the new value, it decreases the count of the old value in `cnt`. Then, it increases the count of `nums2[index]` plus `val`. After updating the `cnt`, `nums2` is updated with the new value.

```
1 def add(self, index: int, val: int) -> None:
2     old = self.nums2[index]
3     self.cnt[old] -= 1
4     if self.cnt[old] == 0:
5         del self.cnt[old] # Remove the entry from the counter if the frequency is zero
6     self.cnt[old + val] += 1
7     self.nums2[index] += val
```

The `count` function takes in a value `tot` and returns the number of pairs  $(i, j)$  where `nums1[i] + nums2[j] == tot`. To do this, it sums up the counts of `tot - nums1[i]` in `cnt` for each element `i` in `nums1`. In other words, for every number in `nums1`, it calculates the complement (the number that needs to be added to it in order to reach `tot`) and uses this to get the frequency of such complements from the `Counter`.

```
1 def count(self, tot: int) -> int:
2     return sum(self.cnt[tot - v] for v in self.nums1)
```

By utilizing the `Counter`, the class is able to execute the `count` function in  $O(n)$  time relative to the size of `nums1`, as it only has to iterate over `nums1` and can retrieve the complement counts in constant time from the hash table. This is significantly more efficient than attempting to calculate the pairs through nested loops, which would be  $O(n * m)$  where `n` and `m` are the sizes of `nums1` and `nums2`.

## Example Walkthrough

Let's step through the problem using a small example to illustrate the solution approach.

Suppose `nums1` is `[1, 2, 3]` and `nums2` is `[1, 4, 5, 2]`, and we are interested in finding pairs whose sum equals `tot = 5`.

Upon class initialization:

- `nums1` remains `[1, 2, 3]`.
- `nums2` remains `[1, 4, 5, 2]`.
- A `Counter` is created from `nums2`, resulting in `{1: 1, 4: 1, 5: 1, 2: 1}`.

Now, let's say we perform an `add` operation – `add(2, 2)` – which adds `2` to the element at index `2` in `nums2`.

- The old value at `nums2[2]` is `5`, so the counter for `5` is decreased from `1` to `0` and consequently removed since its count is now zero.
- The value at `nums2[2]` is updated to `7` (`5 + 2`), so the counter for `7` is increased from `0` to `1`.
- Now `nums2` becomes `[1, 4, 7, 2]`, and the `Counter` reflects `{1: 1, 4: 1, 7: 1, 2: 1}`.

Next, we perform a `count` operation – `count(5)` to find pairs summing up to `5`.

- We iterate through `nums1`, looking for values that, when added to values from `nums2`, yield `5`.
- For `nums1[0] = 1`, we find `tot - nums1[0] = 5 - 1 = 4`; `cnt[4]` equals `1` indicating a pair  $(1, 4)$ .
- For `nums1[1] = 2`, `tot - nums1[1] = 5 - 2 = 3`; `cnt[3]` equals `0` indicating no valid pair exists with the second element `2`.
- For `nums1[2] = 3`, `tot - nums1[2] = 5 - 3 = 2`; `cnt[2]` equals `1` indicating a pair  $(3, 2)$ .
- Sum up the counts of valid pairs for all elements in `nums1`, giving us `cnt[4] + cnt[3] + cnt[2] = 1 + 0 + 1 = 2`.

Therefore, the `count(5)` operation tells us there are `2` valid pairs  $(1, 4)$  and  $(3, 2)$  whose sum equals `5`.

This example demonstrates the efficiency of the approach using a `Counter` to avoid iterating over `nums2` each time we call `count`. Instead, we make use of the precomputed frequencies to quickly tally the number of pairs that sum up to `tot`.

## Python Solution

```
1 from collections import Counter
2 from typing import List
3
4 class FindSumPairs:
5     def __init__(self, nums1: List[int], nums2: List[int]):
6         # Store the two lists and create a counter for nums2 to keep track of occurrences
7         self.nums1 = nums1
8         self.nums2 = nums2
9         self.cnts = Counter(nums2) # using 'counts' in place of 'cnt' for readability
10
11     def add(self, index: int, val: int) -> None:
12         # Function to update the value at a given index in nums2 and adjust the counter
13         old_val = self.nums2[index]
14         # Decrease the count for the old value
15         self.cnts[old_val] -= 1
16         # If the old value count drops to 0, remove it from the counter to keep it clean
17         if self.cnts[old_val] == 0:
18             del self.cnts[old_val]
19         # Update the value in nums2
20         self.nums2[index] += val
21         # Increase the count for the new value
22         self.cnts[self.nums2[index]] += 1
23
24     def count(self, total: int) -> int:
25         # Function to find the number of pairs from nums1 and nums2 that sum up to 'total'
26         result = 0
27         # Iterate over values in nums1 and check if (total - value) exists in nums2's counter
28         for value in self.nums1:
29             result += self.cnts[total - value]
30         return result
31
32 # The class FindSumPairs can be used as follows:
33 # obj = FindSumPairs(nums1, nums2)
34 # obj.add(index, val)
35 # pair_count = obj.count(total)
```

## Java Solution

```
1 import java.util.HashMap;
2 import java.util.Map;
3
4 // Class to find count of pairs from two arrays that sum up to a given value
5 class FindSumPairs {
6     // Arrays to store the two input integer arrays
7     private int[] nums1;
8     private int[] nums2;
9     // Map to keep the frequency count of elements in the second array
10    private Map<Integer, Integer> frequencyMap = new HashMap<>();
11
12    // Constructor initializes the class with two integer arrays
13    public FindSumPairs(int[] nums1, int[] nums2) {
14        this.nums1 = nums1;
15        this.nums2 = nums2;
16
17        // Populating the frequency map with the count of each number in nums2
18        for (int value : nums2) {
19            frequencyMap.put(value, frequencyMap.getOrDefault(value, 0) + 1);
20        }
21    }
22
23    // Method that increments an element of nums2 at a given index by a given value
24    public void add(int index, int value) {
25        // Obtain the original value at the given index in nums2
26        int originalValue = nums2[index];
27        // Decrement the frequency of the original value in the frequency map
28        frequencyMap.put(originalValue, frequencyMap.get(originalValue) - 1);
29        // Increment the original value by the given value and update in nums2
30        nums2[index] = value;
31        // Increment the frequency of the new value in the frequency map
32        frequencyMap.put(nums2[index], frequencyMap.getOrDefault(nums2[index], 0) + 1);
33    }
34
35    // Method that counts the pairs across nums1 and nums2 that sum up to a given total
36    public int count(int total) {
37        int count = 0;
38        // Iterate through each value in nums1
39        for (int value : nums1) {
40            // For the current value in nums1, check if there's a complement in nums2 that sums up to total
41            count += frequencyMap.getOrDefault(total - value, 0);
42        }
43        // Return the count of such pairs
44        return count;
45    }
46 }
47
48 /*
49 * The usage of the FindSumPairs class:
50 *
51 * FindSumPairs obj = new FindSumPairs(nums1, nums2);
52 * obj.add(index, value);
53 * int result = obj.count(total);
54 */
```

## C++ Solution

```
1 #include <vector>
2 #include <unordered_map>
3 using namespace std;
4
5 class FindSumPairs {
6 public:
7     // Constructor initializes the object with two integer vectors
8     FindSumPairs(vector<int>& nums1, vector<int>& nums2) {
9         this->nums1 = nums1; // Assign the first vector to the class member
10        this->nums2 = nums2; // Assign the second vector to the class member
11
12        // Populate the count map with the frequency of each number in nums2
13        for (int value : nums2) {
14            ++countMap[value];
15        }
16    }
17
18    // Function to add a value to an element in nums2 and update the count map
19    void add(int index, int value) {
20        int oldValue = nums2[index]; // Retrieve the old value from nums2 at the given index
21        --countMap[oldValue]; // Decrease the count of the old value in the map
22        ++countMap[oldValue + value]; // Increase the count of the new value in the map
23        nums2[index] += value; // Update the value in nums2 by adding the given value
24    }
25
26    // Function to count the pairs with the given sum 'total'
27    int count(int total) {
28        int pairsCount = 0; // Initialize the count of valid pairs
29
30        // Iterate through elements in nums1 and calculate the complement
31        for (int value : nums1) {
32            pairsCount += countMap[total - value]; // Add the count of the complement from the map to the pairs count
33        }
34
35        return pairsCount; // Return the total count of valid pairs
36    }
37
38 private:
39    vector<int> nums1; // First input vector
40    vector<int> nums2; // Second input vector
41    unordered_map<int, int> countMap; // Map to store the frequency of each number in nums2
42 };
43
44 /**
45 * The FindSumPairs class is instantiated and used as follows:
46 * FindSumPairs* obj = new FindSumPairs(nums1, nums2); // Create a new FindSumPairs object
47 * obj->add(index, value); // Add a value to the element at the given index in nums2
48 * int result = obj->count(total); // Count the pairs that add up to a total
49 * delete obj; // Clean up the object when done (important for memory management)
50 */
```

## Typescript Solution

```
1 // The original C++ includes and namespace declaration are not needed in TypeScript.
2
3 // Global variables for the two number arrays and the count map
4 let nums1: number[];
5 let nums2: number[];
6 let countMap: { [key: number]: number } = {};
7
8 // Function to initialize the object with two integer arrays
9 function initialize(nums1Input: number[], nums2Input: number[]): void {
10    nums1 = nums1Input; // Assign the first array to the global variable
11    nums2 = nums2Input; // Assign the second array to the global variable
12
13    // Populate the count map with the frequency of each number in nums2
14    countMap = {}; // Reset count map
15    nums2.forEach((value) => {
16        if (countMap[value] === undefined) {
17            countMap[value] = 0;
18        }
19        countMap[value]++;
20    });
21 }
22
23 // Function to add a value to an element in nums2 and update the count map
24 function add(index: number, value: number): void {
25    const oldValue = nums2[index]; // Retrieve the old value from nums2 at the given index
26    countMap[oldValue]--; // Decrease the count of the old value in the map
27    const newValue = oldValue + value;
28    if (countMap[newValue] === undefined) {
29        countMap[newValue] = 0;
30    }
31    countMap[newValue]++; // Increase the count of the new value in the map
32    nums2[index] = newValue; // Update the value in nums2 by adding the given value
33 }
34
35 // Function to count the pairs with the given sum 'total'
36 function count(total: number): number {
37    let pairsCount = 0; // Initialize the count of valid pairs
38
39    // Iterate through elements in nums1 and calculate the complement
40    nums1.forEach((value) => {
41        const complement = total - value;
42        pairsCount += countMap[complement] ?? 0; // Add the count of the complement from the map to the pairs count
43    });
44
45    return pairsCount; // Return the total count of valid pairs
46 }
47
48 // Example usage:
49 /*
50 initialize([1, 2, 3, 4], [2, 3, 4, 5]);
51 add(3, 2); // Now nums2 is [2, 3, 4, 7]
52 const result = count(8); // There are 2 pairs that add up to 8: (1,7) and (4,4)
53 console.log(result); // Outputs: 2
54 */
```

## Time and Space Complexity

### Time Complexity

- `__init__(self, nums1: List[int], nums2: List[int])`: The constructor initializes two lists `nums1` and `nums2`. It also counts the elements of `nums2` using `Counter` which takes  $O(n)$  time where `n` is the length of `nums2`.
- `add(self, index: int, val: int) -> None`: This method updates an element in `nums2` and modifies the count of the old and the new value in `cnt`. The update operation and the changes in the counter have a constant time complexity  $O(1)$  since dictionary (counter) operations in Python have an average-case complexity of  $O(1)$ .

- `count(self, tot: int) -> int`: The count method iterates over `nums1` and for each element `v` in `nums1`, it accesses the counter `cnt` to find the count of  $(tot - v)$ . If `nums1` has `m` elements, the time complexity is  $O(m)$  since each lookup in the counter is  $O(1)$  on average.

### Space Complexity

- `__init__(self, nums1: List[int], nums2: List[int])`: Apart from the input lists `nums1` and `nums2`, a counter `cnt` is created to store the frequency of each element in `nums2`. The space complexity is  $O(n)$  where `n` is the number of unique elements in `nums2`.
- `add(self, index: int, val: int) -> None`: This method uses no extra space and thus has a space complexity of  $O(1)$ .
- `count(self, tot: int) -> int`: This method does not use extra space apart from a few variables for its operation, hence the space complexity is  $O(1)$ .

Overall, the space complexity of the `FindSumPairs` class is determined by the space required for storing the input lists and the counter, which is  $O(n)$  where `n` is the size of `nums2` and the number of unique elements it contains.