1608. Special Array With X Elements Greater Than or Equal X

Problem Description

Array

Easy

Binary Search Sorting

number x which meets a particular condition. The condition is that the count of numbers within the array nums that are greater than or equal to x must be exactly equal to x. It is important to note that x doesn't need to be a part of the nums array. Your task is to find and return the number x if the array meets the criteria of being special. In the case where the array is not

You are provided with an array called **nums** that contains non-negative integers. The array is classified as **special** if you can find a

special, you should return -1. It is also mentioned that if an array is special, the value of x that satisfies the condition is always unique.

elements after it in the array.

Intuition

The core idea to solve this problem efficiently is based on the realization that a sorted array makes it easier to find the count of

elements greater than or equal to a given value. To elaborate, once nums is sorted, you can determine how many numbers are greater than or equal to x by finding the position of the first number in nums that is at least x and then calculating the number of

Here's how the thinking progresses towards a solution: 1. Sort the array. In Python, this can be achieved using nums.sort(). 2. Iterate through potential x values, starting from 1 to the size of the array n. For each potential x, use a binary search to find the leftmost position where x could be inserted into the array without violating the sorted order. This operation tells us the count of elements greater than or equal to x by subtracting the insertion index from the length of the array n. In Python, this can be achieved using bisect_left(nums, x)

3. For each x, if the count of elements greater than or equal to x is equal to x itself, we have found the special value and return it.

By using the sorted array and binary search, we can determine the count of elements >= x quickly for each x, allowing us to find

Let's break down the solution step-by-step:

4. If none of the \times values meet the condition, then the array is not special, and we return -1.

the special value or determine that it does not exist with a good time efficiency.

array sorting and binary search - a common pattern when dealing with ordered datasets.

which is imported from the **bisect** module.

Solution Approach The implementation of the solution uses several straightforward steps following an algorithmic pattern that takes advantage of

subsequent steps which is essential for binary search. In Python, we achieve this using the nums.sort() method which sorts the list in place.

Binary Search: To find out how many numbers are greater than or equal to a number x, we can perform a binary search to find the index of the first number in nums that is equal to or greater than x. The bisect_left function from the bisect

Sorting: The input array nums is sorted in non-decreasing order. This is done to leverage the ordered nature of the array in

module is used here which takes a sorted list and a target value x, then finds the leftmost insertion point for x in the list. The use of bisect_left ensures we have an efficient O(log n) lookup for the index.

index.

to n inclusive, checking if any of these values satisfy the special condition. Counting Greater or Equal Elements: For each x, the solution calculates the number of elements greater than or equal to x. This is done using $n - bisect_left(nums, x)$. The bisect_left function gives us the index at which x could be inserted to

Loop Over Potential x Values: We know x can be at most the length of the array n. The solution iterates x from 1 through

maintain the list's sorted order. Therefore, the count of numbers greater than or equal to x is the length of nums minus this

Verification and Return: The loop checks whether each x value equals the count of elements greater than or equal to x.

When it finds a match (cnt == x), it returns x because we've found the unique number that makes the array special. If no

The pattern followed here is a classic example of combining sorting with binary search to optimize the lookup steps, common in many algorithmic problems for reducing time complexity. **Example Walkthrough**

such x is found by the time the loop ends, the solution returns -1, indicating that the array is not special.

Let's go through an example to illustrate the solution approach. Suppose our given nums array is [3, 6, 7, 7, 0].

Sorting: First, we need to sort the array nums. After sorting, it becomes [0, 3, 6, 7, 7].

 \circ For x = 1, binary search (bisect_left) insertion index in sorted nums is 0. The count is 5 - 0 = 5.

which is $\frac{5}{5}$ in this case. So, our potential x values are $\frac{1}{5}$, $\frac{2}{5}$, $\frac{3}{5}$, $\frac{4}{5}$. Counting Greater or Equal Elements: We calculate the count of elements greater than or equal to x for each x. For instance:

Binary Search: We will use binary search to find the position for potential x values. For example, if we're checking for x = 3,

Loop Over Potential x Values: We start checking for all potential x values starting from 1 up to the length of the array,

\circ For x = 5, binary search insertion index is 5. The count is 5 - 5 = 0.

Python

class Solution:

 \circ For x = 2, 4 != 2. No match.

 \circ For x = 3, 4 != 3. No match.

from bisect import bisect_left

nums.sort()

Sort the input array.

return x

public int specialArray(int[] nums) {

for (int x = 1; x <= n; ++x) {

while (left < right) {</pre>

} else {

if $(nums[mid] >= x) {$

right = mid;

left = mid + 1;

// Calculate the count of numbers >= x

int countGreaterOrEqualX = n - left;

Verification and Return: We check each x against the count of elements greater or equal to it: \circ For x = 1, 5 != 1. No match.

Since none of the potential x values resulted in the count being equal to x itself, we return -1. Therefore, the example array [3,

Solution Implementation

Use binary search (bisect left) to find the leftmost position in nums

Check if count is equal to x (which is our definition of a special array).

where x could be inserted, then subtract it from n to get the count

 \circ For x = 2, binary search insertion index is 1. The count is 5 - 1 = 4.

 \circ For x = 3, binary search insertion index is 1. The count is 5 - 1 = 4.

 \circ For x = 4, binary search insertion index is 2. The count is 5 - 2 = 3.

 \circ For x = 4, count = 3, and x = 4 do not match. No match.

 \circ For x = 5, count = 0, and x = 5 do not match. No match.

6, 7, 7, 0] is not special according to the problem statement.

def specialArray(self, nums: List[int]) -> int:

of elements greater than or equal to x.

If it is a special array, return x.

if count greater or equal to x == x:

If no special value is found, return -1.

// Iterate through possible values of x

count_greater_or_equal_to_x = n - bisect_left(nums, x)

int left = 0; // Initialize left pointer of binary search

int right = n; // Initialize right pointer of binary search

// Perform binary search to find the first position where the value is >= x

// If mid value is >= x, shrink the right end of the search range

// If mid value is < x, shrink the left end of the search range

int mid = (left + right) >> 1; // Calculate the middle index

// Function to find if there exists any integer x such that x is the number of elements

// Right bound of the binary search, cannot be more than the length of the array

// Calculate the count of numbers that are greater than or equal to mid

// Calculate the middle index of the current search range

// If we exit the loop without finding a special number, return -1

// If count equals mid, we found a special number, so return it

const mid = Math.floor((lowerBound + upperBound) / 2);

// in nums that are greater than or equal to x. If such an x is found, return x, otherwise return -1.

const count = nums.reduce((accumulator, value) => accumulator + (value >= mid ? 1 : 0), 0);

// If count is greater than mid, we need to search in the upper half of the range

// If count is less than mid, we need to search in the lower half of the range

we want to find the index where 3 could be inserted.

Find the length of the nums array and store it in a variable n. n = len(nums)# Iterate through potential special values (x). for x in range(1, n + 1):

// Sort the array to enable binary search Arrays.sort(nums); int n = nums.length; // Get the length of the sorted array

return -1

class Solution {

Java

```
// If the count of numbers >= x equals x, we found the special value
            if (countGreaterOrEqualX == x) {
                return x; // Return the special value of x
        // If no special value is found, return -1
        return -1;
C++
class Solution {
public:
    int specialArray(vector<int>& nums) {
        // Calculate the size of the array
        int size = nums.size();
        // Sort the array in non-decreasing order
        sort(nums.begin(), nums.end());
        // Iterate for each potential special value 'x' starting from 1 to size of array
        for (int x = 1; x \le size; ++x) {
            // Calculate the count of numbers greater than or equal to 'x' using lower bound
            // which returns an iterator to the first element that is not less than 'x'.
            // Subtracting this from the beginning of the array gives the number of elements
            // less than 'x', and subtracting from 'size' gives the elements greater than or equal to 'x'.
            int count = size - (lower_bound(nums.begin(), nums.end(), x) - nums.begin());
            // If the number of elements greater than or equal to 'x' is exactly 'x',
            // Then we found the special value 'x' and return it
            if (count == x) {
                return x;
        // If no such 'x' exists, return -1
        return -1;
```

from bisect import bisect_left

};

TypeScript

function specialArray(nums: number[]): number {

// Left bound of the binary search

while (lowerBound < upperBound) {</pre>

const length = nums.length;

let upperBound = length;

// Perform binary search

if (count === mid) {

return mid;

if (count > mid) {

} else {

return -1;

lowerBound = mid + 1;

upperBound = mid;

let lowerBound = 0;

// Total number of elements in the array

```
class Solution:
   def specialArray(self, nums: List[int]) -> int:
       # Sort the input array.
       nums.sort()
       # Find the length of the nums array and store it in a variable n.
       n = len(nums)
       # Iterate through potential special values (x).
       for x in range(1, n + 1):
           # Use binary search (bisect left) to find the leftmost position in nums
           # where x could be inserted, then subtract it from n to get the count
           # of elements greater than or equal to x.
           count_greater_or_equal_to_x = n - bisect_left(nums, x)
           # Check if count is equal to x (which is our definition of a special array).
           if count greater or equal to x == x:
               # If it is a special array, return x.
               return x
       # If no special value is found, return -1.
       return -1
Time and Space Complexity
 The provided Python code attempts to find a special array with a non-negative integer x. An array is special if the number of
 numbers greater than or equal to x is equal to x.
```

The sorting operation on an array of n elements has a time complexity of $O(n \log n)$. The loop runs from 1 to n+1 times; in each iteration, a binary search is performed using the bisect_left function. The binary

The time complexity of the given code consists of two parts:

search has a time complexity of O(log n) for each search. Considering that the binary search is performed n times, the total time complexity for all binary searches in the worst case is 0(n

2. Performing a binary search for each value of x in the sorted nums array using the bisect_left function.

complexity of $0(n \log n + n \log n)$. This simplifies to $0(n \log n)$ since the sorting term is the dominant term and the additional n log n term does not change the asymptotic growth rate. **Space Complexity**

Hence, the overall time complexity is dominated by the sorting and the n binary searches, which in combination yields a time

The space complexity of the algorithm is determined by the space used besides the input array nums. 1. Sorting is in-place, so it does not use additional space proportional to the input array.

In summary:

log n).

Time Complexity

1. Sorting the nums array.

2. The binary search uses only a few variables such as x and cnt, which take up constant space.

There is no additional space that is dependent on the size of the input, thus the space complexity is 0(1), which means it uses constant additional space.

• Time Complexity: O(n log n) • Space Complexity: 0(1)