1980. Find Unique Binary String

Backtracking

String

Problem Description

<u>Array</u>

The task is to find a binary string of length n that is not included in the given array nums, which contains n unique binary strings of the same length. The binary string to be found should consist only of '0's and '1's and should not match any of the binary strings in the given list. We are also given the freedom to provide any valid string that satisfies the condition in case multiple correct answers exist.

Intuition

Medium

a possibility that all binary representations from 0 to n-1 are present. However, the pigeonhole principle states that since there are n+1 possible binary numbers from 0 to n, there must be at least one number not represented by the n binary strings. The solution uses a mask variable to store which of the binary numbers represented by the count of '1's in each string are already

The intuition behind this solution involves bit manipulation. Since there are n unique binary strings, and each is n bits long, there's

present in the given nums list. A loop goes through the strings and sets a bit in the mask to 1 for each count of '1's that occurs. After that, we loop over the possible counts of '1's from 0 to n and look for a bit in the mask that is still 0 (which means this count

of '1's has not been used). When we find such a bit, we construct a binary string with this count of '1's followed by the necessary count of '0's to make the length n and return it. This string is guaranteed not to be in the list because we generated it based on a count of '1's not present in the original list. For example, if n is 3, and nums has ["000", "011", "101"], the counts of '1's are 0, 2, and 2 respectively. So, mask would have bits 0

and 2 set to 1 (00101 in binary). The number of '1's that is not represented is 1 and 3, and thus, the strings "010" or "111" would be valid outputs. **Solution Approach**

binary strings nums. The algorithm proceeds as follows:

Initialize a variable mask to 0. This mask will have its bits set to 1 at positions that correspond to the counts of '1's found in the binary strings from nums.

Obtain n, which is the length of the input list nums (also the length of every binary string in nums).

The code uses the concept of a bit mask and bit manipulation to keep track of the counts of '1's that are present in the given

- For each binary string x in nums, convert the count of '1's into a position in the mask and set that position to 1. This is done by the operation mask |= 1 << x.count("1"). In essence, for a string x, if it contains 'k' number of '1's, the k-th bit of mask is set to 1.
- Iterate from i = 0 to n (inclusive) and check if the bit at the i-th position of mask is not set (which means that no string in nums has exactly i number of '1's). This is performed by checking if mask >> i & 1 ^ 1 is True, where mask >> i shifts the mask i times to the right, creating a new mask that has the i-th bit of the original mask at the 0-th position. To check if the bit is not set, we use the XOR operation with 1 (& 1 $^{\circ}$ 1) which will yield True if and only if the bit was 0.
- with n-i number of '0's to make the string's length equal to n. This resultant string is guaranteed to be unique and not to appear in nums.

When an unset bit is found (mask >> i & 1 ^ 1 is True), construct the binary string result by concatenating i number of '1's

Return the constructed string. For example, if n is 3, and nums contains the strings ["000", "011", "101"], the mask after step 2 would be 5 (in decimal) or 101 in

Therefore, we can construct the strings "010" or "111" as our output, both of which have a length of 3 and do not appear in nums.

Let's take an example with n = 2 and nums being ["00", "01"]. We want to find a binary string of length 2 that is neither "00" nor

binary as the 0-th and 2-nd bits are set to 1. Looking for an unset bit in mask, we find that the 1-st and 3-rd positions are 0.

Example Walkthrough

0-th and 1-st bits are set.

The 0-th bit is set, so we continue.

"01".

Iterate through each string in nums: For "00", there are 0 '1's. We set the 0-th bit of mask using mask |= 1 << 0. Now mask is 01 in binary (1 in decimal).

∘ For "01", there is 1 '1'. We set the 1-st bit of mask using mask |= 1 << 1. Now mask changes from 01 to 11 in binary (3 in decimal), since both

∘ For i = 0: Check mask >> i & 1 ^ 1. We have mask >> 0 which is 11 (3) and & 1 which gives the last bit '1', then ^ 1 would give 0 (False).

o For i = 1: Check mask >> i & 1 ^ 1. We have mask >> 1 which is 1 (1) and & 1 which gives '1', then ^ 1 would give 0 (False). The 1-st bit is

We start iterating from i = 0 to n (until 2, inclusive):

Since n=2 and i=2, we get "11" as the result. This string has exactly 2 '1's, and its length matches n.

Initialize a bitmask to keep track of the count of "1"s in the binary strings

Get the length of binary strings in the nums list (assuming they all have the same length)

Find the smallest binary string with a different count of "1"s than those in nums

// This will help us to keep track of which counts are already present.

// Check if the bit representing the count of '1's at index 'i' is not set.

// If not set, we found our number. Return a binary string with 'i' ones

return std::string(i, '1') + std::string(nums.size() - i, '0');

// because there are 2^N possible binary strings of length N, and only N of them

// have unique counts of '1's, leaving at least one string that is different.

// No return is needed here as the loop is guaranteed to return a string

// Initialize a variable to act as a bitmask where each bit position represents

// Start an infinite loop to find a binary string with a different count of '1's.

// Check if the current count of '1's is not yet represented in the bitmask.

// The expression (bitmask >> i) shifts the bitmask to the right by 'i' bits,

// followed by enough zeros to match the size of the input binary strings.

for (int i = 0; i + +) { // Infinite loop, will break when found a non-existing binary string.

// Start generating different binary strings to find one not in the input.

Initialize mask to 0. This will be used to track the count of '1's present in the binary strings from nums.

also set, so we continue. ∘ For i = 2: Check mask >> i & 1 ^ 1. We have mask >> 2 which is 0 (0) and & 1 which gives '0', then ^ 1 would give 1 (True). The 2-nd bit is

Now that n is 2, we check for bits in mask which are not set.

def findDifferentBinaryString(self, nums: List[str]) -> str:

The bit position is the count of "1"s

bitmask |= 1 << binary_string.count("1")

- not set; this means no string in nums has 2 '1's. As soon as we find an i-th bit not set, we construct the binary string with i number of '1's followed by n-i number of '0's.
- Thus, the string "11" is returned. This string is of length n, not present in nums, and follows the correct format.
- **Python**

Iterate over each binary string in the nums list for binary_string in nums: # Count the number of "1"s and set the corresponding bit in the bitmask

n = len(nums)

mask |= 1 << countOnes;</pre>

if ((mask >> i & 1) == 0) {

if $(((bitmask >> i) \& 1) == 0) {$

function findDifferentBinaryString(nums: string[]): string {

// Set the corresponding bit in the bitmask.

// the count of '1's in the binary strings seen so far.

// Count the number of '1's in the current string.

let countOnes: number = [...str].filter(c => c === '1').length;

// and then checks if the least significant bit is not set.

bitmask = 0

class Solution:

Solution Implementation

```
for i in range(n + 1):
           # Check if there is no binary string in nums with i "1"s
           if bitmask >> i & 1 ^ 1:
               # Return the binary string with i "1"s followed by (n - i) "0"s
                # Ensuring it has the same length as other strings in nums
                return "1" * i + "0" * (n - i)
Java
class Solution {
    public String findDifferentBinaryString(String[] nums) {
       // Initialize a mask to keep track of the counts of 1s found in the binary strings.
        int mask = 0;
       // Iterate over each binary string in the input array.
        for (String binaryString : nums) {
           // Initialize a count for the number of '1's in the current string.
           int countOnes = 0;
           // Iterate through each character in the binary string.
            for (int i = 0; i < binaryString.length(); i++) {</pre>
                // If the character is '1', increment the counter.
                if (binaryString.charAt(i) == '1') {
                    countOnes++;
           // Set the corresponding bit in the mask for the count of '1's found.
```

};

TypeScript

let bitmask: number = 0;

for (let str of nums) {

for (let i = 0; ; ++i) {

// Loop through the binary strings.

bitmask |= 1 << countOnes;

```
// Create a binary string with 'i' number of '1's followed by enough '0's to make it the same length as input str
                // Then return the newly created binary string.
                String ones = "1".repeat(i);
                String zeros = "0".repeat(nums.length - i);
                return ones + zeros;
#include <string>
#include <vector>
#include <algorithm>
class Solution {
public:
    std::string findDifferentBinaryString(std::vector<std::string>& nums) {
       // Initialize a variable to serve as a bitmask where each bit represents
       // the count of '1's in the binary strings seen so far.
        int bitmask = 0;
       // Loop through the binary strings.
        for (auto& str : nums) {
           // Count the number of '1's in the current string.
            int countOnes = std::count(str.begin(), str.end(), '1');
           // Set the corresponding bit in the bitmask.
            bitmask |= 1 << countOnes;</pre>
       // Loop indefinitely to find a binary string with a different count of '1's.
        for (int i = 0;; ++i) {
           // Check if the current count of '1's is not represented in the bitmask.
           // The expression (bitmask >> i) shifts the bitmask to the right by 'i' bits,
           // and then checks if the least significant bit is not set.
```

```
if (((bitmask >> i) & 1) === 0) {
              // If not set, we have found our number. Return a binary string with 'i' '1's
              // followed by enough '0's to match the size of the input binary strings.
              return '1'.repeat(i) + '0'.repeat(nums[0].length - i);
      // No explicit return is necessary here as the loop condition assures a return,
      // because there are 2^N possible binary strings of length N, and only N of them
      // can have unique counts of '1's, ensuring at least one string that is different.
  // The method names are not modified and the above function can be used directly.
  // Usage example:
  // let result = findDifferentBinaryString(["01", "10"]);
  // console.log(result); // Outputs a binary string that is different from the input strings
class Solution:
   def findDifferentBinaryString(self, nums: List[str]) -> str:
       # Initialize a bitmask to keep track of the count of "1"s in the binary strings
       bitmask = 0
       # Iterate over each binary string in the nums list
       for binary_string in nums:
           # Count the number of "1"s and set the corresponding bit in the bitmask
           # The bit position is the count of "1"s
           bitmask |= 1 << binary_string.count("1")
       # Get the length of binary strings in the nums list (assuming they all have the same length)
       n = len(nums)
       # Find the smallest binary string with a different count of "1"s than those in nums
       for i in range(n + 1):
           # Check if there is no binary string in nums with i "1"s
           if bitmask >> i & 1 ^ 1:
               # Return the binary string with i "1"s followed by (n - i) "0"s
               # Ensuring it has the same length as other strings in nums
               return "1" * i + "0" * (n - i)
Time and Space Complexity
Time Complexity
```

The time complexity of the given code is determined by iterating over the input list nums once, and then iterating through a range that is at most n + 1, where n is the length of nums.

The first for loop iterates over each string in nums and involves a bitwise OR operation as well as counting the number of '1's in each string. Both of these operations occur in constant time (since the strings are of length n and binary string length is fixed in this scenario). Hence, this part of the loop runs in O(n) time.

- The second for loop runs from 0 to n, and each iteration involves a constant-time operation: a bitwise right shift followed by a bitwise AND, and a bitwise XOR. Therefore, the loop runs in O(n) time.
- Combining both parts, the overall time complexity is 0(n + n) which simplifies to 0(n). **Space Complexity**

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The space complexity is determined by the additional space used by the algorithm beyond the input itself. The variable mask is an integer that requires 0(1) space.

No other additional data structures that grow with the size of the input are used in the algorithm.

Hence, the overall space complexity of the code is 0(1).