1245. Tree Diameter **Breadth-First Search** Medium Tree **Depth-First Search** Graph **Topological Sort Leetcode Link**

Problem Description

nodes in the tree. Given that the tree is undirected and consists of n nodes labeled from 0 to n - 1, and an array of edges indicating the connections between the nodes, the objective is to calculate and return the tree's diameter.

The task is to find the diameter of a tree. The diameter is defined as the number of edges in the longest path between any two

tree will have as its endpoints two of the tree's leaves.

Intuition Finding the diameter of a tree involves discovering the longest path between two nodes. A common technique to solve this problem

is to use a depth-first search (DFS) twice. The intuition behind this approach is based on the property that the longest path in the

The first DFS begins at an arbitrary node (usually the first node provided) and traverses the tree to find the leaf node that lies at the

greatest distance from the starting node. This leaf node will be one end of the longest path. The second DFS then begins at this leaf

node and searches for the farthest leaf node from it, thus uncovering the other end of the longest path. By keeping track of the number of edges traversed during the second DFS (which is essentially the length or the height of the tree from the perspective of the starting leaf node), we can directly calculate the diameter of the tree.

Solution Approach

The provided Python code implements a solution to the problem using a depth-first search (DFS) algorithm. Here's how it works:

1. A dfs function is defined, which takes a node u and a counter t that tracks the total number of edges traversed from the starting

node. The dfs function recursively visits nodes, incrementing the counter as it goes deeper into the tree.

2. Inside this DFS function, a base condition checks if the current node has already been visited to prevent loops. If it hasn't been

function is called again with v as the current node and the counter t incremented by 1.

- visited, it is marked as visited. 3. The recursive step involves iterating over all the adjacent nodes (v) of the current node (u). For each adjacent node, the dfs
- 4. While returning from each call of dfs, the code compares the current value of t with a variable ans, which keeps track of the maximum distance found so far. If t is greater, it means a longer path has been found, and thus ans is updated with the current
- value of t, and next is updated with the current node u. The main function treeDiameter utilizes the DFS as follows:
- A defaultdict d is created to store the tree in an adjacency list representation. This makes it easy to access all the nodes connected to a given node in the tree. The edges are used to populate this adjacency list.

An array vis is used to keep track of which nodes have been visited to prevent repeating the same nodes during the DFS.

• The first DFS is initiated from the first node in the edges list. After this DFS, we have a candidate leaf node for the longest path in

the variable next.

and then executing another DFS from that endpoint to find the actual longest path.

- The vis array is reset to prepare for the second DFS call. The second DFS is initiated from the next node found from the first DFS call.
- At the end of the second DFS, the variable ans holds the diameter of the tree, which is the number of edges in the longest path. This is returned as the function's result.
- Example Walkthrough Let's consider a small example to illustrate the solution approach. Suppose we have a tree with n=6 nodes and the following edges:

In summary, the algorithm finds the longest path (or diameter) of the tree by first locating one end of the longest path using a DFS

The tree structure would look like this:

Given this tree, we want to find its diameter. Following the solution approach:

2. We traverse the tree from node 0, and we may reach a leaf node, such as node 4. Let's assume the DFS process went along the

3. Since node 4 is a leaf, we backtrack, but in doing so, we keep track of the node that gave us the maximum depth. Let's assume

path 0->1->2->4. During this process, each time DFS calls itself, it increments the counter t.

4. With node 4 as our furthest leaf from node 0, we now reset the vis array for the second DFS.

6. If we go to 3, which is another leaf, we've found the longest path in the tree: 4->2->1->3.

if visited[node]: # If this node has already been visited, skip

dfs(neighbor, distance + 1) # DFS on connected nodes

Convert the edge-list to an adjacency list representation for the graph

Initialize a visited list to keep track of visited nodes during DFS

// Reset the visited array for the second DFS traversal

// Return the diameter

// Update the diameter and farthest node if the current distance is greater

visited = new boolean[n + 1];

private void dfs(int node, int distance) {

dfs(adjacent, distance + 1);

// Depth-First Search (DFS) function to traverse the tree

// If the current node has been visited, return

for (int adjacentNode : graph[currentNode]) {

dfs(adjacentNode, currentLength + 1);

// Importing necessary functionalities from 'collections' module in TypeScript

void dfs(int currentNode, int currentLength) {

if (visited[currentNode]) return;

visited[currentNode] = true;

// Visit all adjacent nodes

if (diameter < currentLength) {</pre>

diameter = currentLength;

import { Set, Map } from "typescript-collections";

5 const graph: Map<number, Set<number>> = new Map();

// Function to calculate the diameter of the tree

function treeDiameter(edges: number[][]): number {

if (!graph.containsKey(edge[0])) {

7 const visited: Map<number, boolean> = new Map();

// Global graph representation using an adjacency list

6 // Global visited Map to keep track of visited nodes during DFS

10 // Variable to store the node that will be the next candidate for DFS

8 // Variable to store the length of the diameter of the tree

furthestNode = currentNode;

// Mark the current node as visited

dfs(farthestNode, 0);

if (visited[node]) {

visited[node] = true;

if (diameter < distance) {</pre>

return diameter;

return;

5. The second DFS starts at node 4 and proceeds to find the furthest node from it. Node 4 will branch only to 2, so we go to 2, then to 1, and we have a choice to go to node 0 or node 3.

Function to find the diameter of a tree given its edges

1. We first use DFS starting from an arbitrary node, say node 0.

this maximum depth was first encountered at node 4.

During the second DFS, we keep a variable ans that tracks the max length. Since the path 4->2->1->3 is the longest path in the tree, ans would be 3 in the end, which means there are three edges in the path. Thus, the diameter of this tree is 3.

That concludes the example walkthrough using the solution approach. We've illustrated how the algorithm recursively searches for

the furthest possible nodes step by step and eventually finds the longest path, which defines the diameter of the tree.

def treeDiameter(self, edges: List[List[int]]) -> int: # Helper function to perform a depth-first search (DFS) def dfs(node, distance): nonlocal max_diameter, visited, graph, next_node

14 15 # Update the diameter and the next node if we found a longer path if max_diameter < distance:</pre> 16 max diameter = distance 17 18 next_node = node

```
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Python Solution

class Solution:

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from collections import defaultdict

return

graph = defaultdict(set)

for u, v in edges:

visited[node] = True

for neighbor in graph[node]:

visited = [False] * (len(edges) + 1)

Establish the adjacency list from the edges

```
graph[u].add(v)
               graph[v].add(u)
29
           max_diameter = 0 # Initialize the diameter of the tree
30
           next_node = 0 # This variable will hold one end of the maximum diameter
31
32
           # Perform the first DFS to find one end of the maximum diameter path
33
           dfs(edges[0][0], 0)
34
           # Reset the visited list for the next DFS
35
36
           visited = [False] * (len(edges) + 1)
37
38
           # Perform the second DFS from the farthest node found in the first DFS
39
           dfs(next_node, 0)
40
           # The maximum distance found during the second DFS is the tree diameter
41
42
           return max_diameter
43
Java Solution
   class Solution {
         private Map<Integer, Set<Integer>> graph; // Represents the adjacency list for the graph
         private boolean[] visited;
                                         // Array to keep track of visited nodes
  3
                                                  // Tracks the farthest node found during DFS
         private int farthestNode;
  4
                                                   // Stores the current diameter of the tree
  5
         private int diameter;
  6
         public int treeDiameter(int[][] edges) {
             int n = edges.length;  // Number of nodes will be #edges + 1 in a tree
  8
                                       // Initialize diameter as zero
            diameter = 0;
  9
 10
            graph = new HashMap<>(); // Initialize the graph
 11
 12
            // Building an undirected graph using the provided edges
 13
            for (int[] edge : edges) {
 14
                 graph.computeIfAbsent(edge[0], k -> new HashSet<>()).add(edge[1]);
 15
                 graph.computeIfAbsent(edge[1], k -> new HashSet<>()).add(edge[0]);
 16
 17
 18
             // Initialize the visited array for the first DFS traversal
 19
             visited = new boolean[n + 1]; // Index 0 is ignored since node numbering starts from 1
 20
             farthestNode = edges[0][0]; // Start from the first node
 21
             dfs(farthestNode, 0);
                                         // Perform DFS to find the farthest node
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// Perform DFS from the farthest node to find the diameter

36 diameter = distance; 37 farthestNode = node; 38 39 // Visit all the connected nodes of the current node using DFS 40 for (int adjacent : graph.get(node)) {

C++ Solution

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Typescript Solution

let diameter: number = 0;

// Construct the graph

edges.forEach(edge => {

11 let furthestNode: number;

```
#include <vector>
   #include <unordered_map>
   #include <unordered_set>
   class Solution {
   public:
       // Graph representation using an adjacency list
       unordered_map<int, unordered_set<int>> graph;
 8
       // Visited vector to keep track of visited nodes during DFS
 9
10
       vector<bool> visited;
       // Variable to store the length of the diameter of the tree
11
12
       int diameter;
13
       // Variable to store the node that will be the next candidate for DFS
14
        int furthestNode;
15
16
       // Function to calculate the diameter of the tree
17
        int treeDiameter(vector<vector<int>>& edges) {
18
           // Construct the graph
19
            for (auto& edge : edges) {
20
                graph[edge[0]].insert(edge[1]);
21
                graph[edge[1]].insert(edge[0]);
22
23
            int numNodes = edges.size();
24
            diameter = 0;
25
           // Initialize visited vector of size numNodes+1 (since it's a tree, it has numNodes+1 vertices)
26
            visited.resize(numNodes + 1, false);
           // Initialize the furthestNode with any node (e.g., the first node of the first edge)
27
28
            furthestNode = edges[0][0];
29
30
           // Perform the first DFS to find the furthest node from the starting node
31
           dfs(furthestNode, 0);
32
           // Reset the visited vector for the next DFS
33
            visited.assign(visited.size(), false);
34
           // Perform the DFS starting from the furthest node to determine the diameter
35
            dfs(furthestNode, 0);
36
37
            // Diameter is the maximum number of edges between any two nodes in the tree
38
            return diameter;
39
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```

// If the current length is greater than the diameter, update the diameter and furthestNode

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18 graph.setValue(edge[0], new Set()); 19 20 if (!graph.containsKey(edge[1])) { 21 graph.setValue(edge[1], new Set()); 22 23 graph.getValue(edge[0]).add(edge[1]); 24 graph.getValue(edge[1]).add(edge[0]); 25 }); 26 27 const numNodes: number = edges.length; diameter = 0; // Initialize visited Map for all nodes as false for (let i = 0; i < numNodes + 1; i++) {</pre> visited.setValue(i, false); // Initialize the furthestNode with any node (e.g., the first node of the first edge) 34 furthestNode = edges[0][0]; 35 36 // Perform the first DFS to find the furthest node from the starting node 37 dfs(furthestNode, 0); 38 // Reset the visited Map for the next DFS 39 visited.forEach((value, key) => { 40 visited.setValue(key, false); 41 42 // Perform the DFS starting from the furthest node to determine the diameter 43 dfs(furthestNode, 0); 44 45 // Diameter is the maximum number of edges between any two nodes in the tree 46 return diameter; 47 } 48 // Depth-First Search (DFS) function to traverse the tree function dfs(currentNode: number, currentLength: number): void { 51 // If the current node has been visited, return if (visited.getValue(currentNode)) { 52 53 return; 54 55 // Mark the current node as visited 56 visited.setValue(currentNode, true); 57 // If the current length is greater than the diameter, update the diameter and furthestNode if (currentLength > diameter) { 58 59 diameter = currentLength; furthestNode = currentNode; 60 61 62 // Visit all adjacent nodes 63 graph.getValue(currentNode).forEach(adjacentNode => { 64 dfs(adjacentNode, currentLength + 1); 65 }); 66 } 67 Time and Space Complexity

Time Complexity The given Python code snippet defines a Solution class with a method treeDiameter to find the diameter of an undirected tree

Let n be the number of nodes in the tree, which is one more than the number of edges (len(edges)), as it is a connected, undirected tree with n-1 edges. The time complexity for constructing the adjacency list d is O(n), since each edge (u, v) is processed exactly twice, once for each

direction. Each dfs call traverses all edges in the tree exactly once. Since there are n-1 edges and each edge contributes to two entries in the

adjacency list (one for each end of the edge), the total number of adjacency entries to traverse is 2(n-1), which is 0(n). There are

represented by a list of edges. The algorithm uses a depth-first search (dfs) starting from an arbitrary node to find the farthest node

from it, and then performs a second depth-first search from this newly discovered node to find the diameter of the tree.

two dfs calls, meaning that the total time for traversing the tree is 2*0(n), which simplifies to 0(n). Therefore, the overall time complexity of the code is O(n).

Space Complexity The space complexity consists of the storage for the adjacency list d, the visited flags array vis, and the auxiliary space used by the dfs recursion call stack.

The adjacency list d has 2(n-1) entries as explained earlier; thus, its space complexity is 0(n). The vis array is of length n, so it also occupies O(n) space.

The depth of the recursive dfs call stack will be at most n in the worst case (a path graph), contributing an additional O(n) to the space complexity.

Combining these factors, the overall space complexity of the algorithm is O(n).