923. 3Sum With Multiplicity Counting Hash Table Two Pointers Medium Array Sorting Leetcode Link

Problem Description

The problem requires us to find the number of distinct triplets (i, j, k) in an integer array arr where the condition i < j < k is satisfied, and the sum of the elements at these indices is equal to a given target integer. Specifically, arr[i] + arr[j] + arr[k] == target should hold true for the counted triplets. Since the number of such triplets can be quite large, we are asked to return the answer modulo 10^9 + 7 to keep the output within integer value limits.

Intuition

checking all possible triplets due to the high time complexity that approach would imply. The algorithm usually starts by counting the occurrences of each number in the array using a Counter, which is a special kind of

dictionary in Python. This allows us to know how many times each number appears in the array without traversing it multiple times.

The key to solving this problem is to consider how we can traverse the array to find all the valid triplets efficiently. We want to avoid

Once we have these counts, we iterate through the array for the second number of the triplet. For each possible second number b at index j, we decrease its count by 1 to ensure that we do not use the same instance of b when looking for the third number.

Next, we traverse the array again up to the second number's index j to find every possible first number a. With both a and b known, we calculate the required third number c by subtracting the sum of a and b from the target.

If c is present in our Counter (which means it's somewhere in the original array), we can form a triplet (a, b, c) that sums up to target. We then add the count of c from our Counter to our answer, since there are as many possibilities to form a triplet with a and b as the count of c. It's important to use modulo with 10^9 + 7 during each addition to keep the number within bounds.

The iteration is cleverly structured to ensure that each element is used according to its occurrence and that i < j < k always holds true by managing the index and counts carefully.

The solution uses a combination of a hashmap (in Python, a Counter) and a two-pointer approach to find the valid triplets.

1. A Counter (which is a specialized hashmap/dictionary in Python) is initialized to count the occurrences of the elements in the

Solution Approach

The algorithm goes as follows:

given arr. This data structure allows for O(1) access to the count of each element, which is essential for efficient computation of the number of triplets.

2. We define a variable ans to keep the running total of the number of valid triplets.

triplet.

- 3. The mod variable is set to 10**9 + 7 to ensure that we perform all our arithmetic operations modulo this number. 4. We loop through each element b of the array using its index j. This element is considered the second element of our potential
- 5. Before starting the inner loop, we decrease the count of b in the Counter by one. This ensures that we don't count the same

the triplet. The index i is implicit in this loop.

the answer within the range of valid integers.

upheld by the two nested loops and the management of the Counter.

3:2} which reflects that each number 1, 2, and 3 occurs twice in the array.

- element b twice when looking for the third element of the triplet.
- 7. We then calculate the required third element c of the triplet by subtracting the sum of a and b from the target, i.e., c = target a - b.

6. An inner loop runs through the array up to the current index j, selecting each element a as a candidate for the first element of

9. Finally, we return ans as the result.

The algorithm ensures that no element is used more often than it appears in the array, and the i < j < k condition is naturally

The use of the Counter and looping through the array only once per element significantly reduces the computational complexity

8. The total count of valid triplets is then incremented by the count of c from the Counter if c is present. We use modulo mod to keep

- compared to checking all possible triplets directly. This pattern is a common approach in problems involving counting specific arrangements or subsets in an array, especially when the array elements are bound to certain conditions.
- Let's consider an example with arr = [1, 1, 2, 2, 3, 3] and target = 6. We want to find all unique triplets i, j, k (with i < j <

k) such that arr[i] + arr[j] + arr[k] == target.

count of c in Counter. So, ans = (ans + 2) % mod.

before. ans is updated to ans = (ans + 2) % mod.

Example Walkthrough

2. Set ans = 0 to keep track of the total number of valid triplets and mod = 10**9 + 7 for modulo operations.

3. We now look for the second number b for all triplets by iterating through arr. Consider j=2 where b = arr[j] = 2.

4. We decrement the count of b in Counter by 1. Now the Counter will look like this: {1:2, 2:1, 3:2}.

1. We begin by initializing a Counter to count the occurrences of each element in arr. The Counter will look like this: {1:2, 2:2,

5. We start the inner loop to select a as the first element of the triplet. We iterate from start to j-1, in this case, from 0 to 1. 6. For a = arr[0] = 1 at i=0, we calculate the needed c = target - a - b = 6 - 1 - 2 = 3.

7. The count of c in the Counter is 2, which means we can form two triplets (1, 2, 3) with i=0, j=2. We increment ans by the

- 8. For a = arr[1] = 1 at i=1, we calculate c = 6 1 2 = 3 again. Since i < j, it's valid and we have not used the same a as
- 10. After finishing, ans is the total number of valid triplets.
- Therefore, ans = 4.

Remember that in a real problem with a large arr, not all triples (a, b, c) will be unique because of duplicate values, and there will

(1, 2) are distinct by their positions. There's no triplet using any two '3's because that would require 1 not to be less than j.

be a variable number of contributions to ans from each triplet depending on how many times each value occurs.

For this example, the possible triplets are two instances of (1, 2, 3) using the first 1 and first 2, two using the first 1 and second 2, two

using the second 1 and first 2, and two using the second 1 and second 2. These are counted as four unique triplets because the pairs

from collections import Counter

Create a counter to keep track of occurrences of each number in the array

Decrement the count of the current element to avoid overcounting

third_value = target - first_value - second_value

answer = (answer + count[third_value]) % modulo

3. Replaced j and i with index and i respectively for better readability in loops.

6. Ensured that the method names and the logic of the function remained unchanged.

Calculate the third value that would make the triplet sum to the target

Add the number of occurrences of the third value to the answer

2. Replaced cnt with count for more clarity that this variable represents occurrences of numbers.

To complete this snippet, you'll need to add the following import if not already at the top of your file:

4. Renamed a and b to first_value and second_value, while c to third_value, to clearly distinguish the triplet elements.

5. Added comments explaining each portion of the code, outlining what each section does and why certain operations are

def threeSumMulti(self, arr: List[int], target: int) -> int:

Iterate over the array using index and value

Use modulo to avoid overflow

Imported List from typing to use type hints for list parameters.

performed, such as the purpose of the modulo operation.

for index, second_value in enumerate(arr):

count[second_value] -= 1

9. Continue this process for every j from 0 to len(arr), and you'll count all valid triplets.

count = Counter(arr) # Initialize answer to 0 answer = 0 # Define the modulo value for large numbers to handle overflow 12 modulo = 10**9 + 7

18 # Iterate over the elements up to the current index 19 for i in range(index): 20 first value = arr[i] # Get the current first value 21 22

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           # Return the total number of triplets that sum up to the target
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           return answer
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from typing import List

Java Solution

1 class Solution {

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Here's a breakdown of the changes made:

Python Solution

class Solution:

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public int threeSumMulti(int[] arr, int target) { int[] count = new int[101]; // Array to store count of each number, considering constraint 0 <= arr[i] <= 100</pre> // Populate the count array with the frequency of each value in arr for (int num : arr) { ++count[num];

if (third >= 0 && third <= 100) {

// Define the modulo constant for taking modulus

for (int i = 0; i < j; ++i) {

10 long ans = 0; // To store the result, using long to avoid integer overflow before taking the modulus 11 12 13 // Iterate through all elements in arr to find triplets for (int j = 0; j < arr.length; ++j) {</pre> 14

private static final int MOD = 1_000_000_007; // le9 + 7 is represented as 1000000007

15 int second = arr[j]; // The second element in the triplet --count[second]; // Decrement count since this number is being used in the current triplet 16 17 18 // Iterate from the start of the array to the current index 'j'

int first = arr[i]; // The first element in the triplet

// Function to calculate the number of triplets that sum up to the target

// Array to store the count of each number in the range [0, 100]

int threeSumMulti(vector<int>& arr, int target) {

int count[101] = {0};

for (int num : arr) {

++count[num];

long answer = 0;

// Populating the count array

// Variable to store the result

for (int j = 0; j < arr.size(); ++j) {</pre>

int secondElement = arr[j];

for (int i = 0; i < j; ++i) {

int firstElement = arr[i];

--count[secondElement];

26 27 28 29 // Cast and return the final answer as an integer 30 return (int) ans; 31

int third = target - first - second; // Calculate the third element

// Check if third element is within range and add the count to the answer

ans = (ans + count[third]) % MOD; // Use the modulo to avoid overflow and get the correct result

C++ Solution 1 class Solution { 2 public: // Modulo constant for the problem const int MOD = 1e9 + 7;

// Iterate through each element in the array to use it as the second element of the triplet

// Iterate through elements up to the current second element to find the first element

// Select the current element as the second element of the triplet

// Decrement the count as this element is considering for pairing

// Calculate the required third element to meet the target

int thirdElement = target - firstElement - secondElement;

let thirdElement: number = target - firstElement - secondElement;

// Check if the third element is within the valid range [0, 100]

// Add the count of the third element to the answer

if (thirdElement >= 0 && thirdElement <= 100) {

answer += count[thirdElement];

// If the third element is within the valid range

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if (thirdElement >= 0 && thirdElement <= 100) {
                       // Add the count of the third element to the answer
                       answer += count[thirdElement];
                       // Ensure answer is within the MOD range
                       answer %= MOD;
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           // Return the final answer
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           return answer;
45 };
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Typescript Solution
  1 // Constant for modulo operations
  2 const MOD: number = 1e9 + 7;
    // This function calculates the number of triplets in the array that sum up to the target value
     function threeSumMulti(arr: number[], target: number): number {
         // Array to store the count of occurrence for each number within the range [0, 100]
         let count: number[] = new Array(101).fill(0);
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         // Populate the count array with the number of occurrences of each element
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         for (let num of arr) {
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             count[num]++;
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         // Variable to store the result
         let answer: number = 0;
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         // Iterate through each element in the array to use it as the second element of the triplet
 18
         for (let j = 0; j < arr.length; j++) {</pre>
             // The current element is selected as the second element of the triplet
 19
 20
             let secondElement: number = arr[j];
             // Decrement the count for this element as it is being considered for pairing
 21
 22
             count[secondElement]--;
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 24
             // Iterate over all possible first elements up to the current second element
 25
             for (let i = 0; i < j; i++) {
 26
                 let firstElement: number = arr[i];
 27
                 // Calculate the required third element to meet the target sum
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Time and Space Complexity The time complexity of the provided Python code snippet is $0(n^2)$ where n is the number of elements in the input list arr. This

34 // Ensure answer remains within the range specified by MOD 35 answer %= MOD; 36 37 38 39 40 // Return the final computed answer 41 return answer; 42 } 43 // Example usage of the function // let arrExample = [1, 1, 2, 2, 3, 3, 4, 4, 5, 5]; 46 // let targetExample = 8; 47 // let result = threeSumMulti(arrExample, targetExample); // console.log(result); // Output the result 49

nested loops result in quadratic complexity. The space complexity of the code is O(m) where m is the number of unique elements in the input list arr. This complexity is due to the use of a Counter to store frequencies of all unique elements in arr. The space taken by the counter will directly depend on the number of unique values.

complexity arises because there is a nested for-loop where the outer loop runs through the elements of arr (after decrementing the

count of the current element), and the inner loop iterates up to the current index j of the outer loop. For each pair (a, b), the code

looks up the count of the third element c that is needed to sum up to the target. Even though the lookup in the counter is 0(1), the