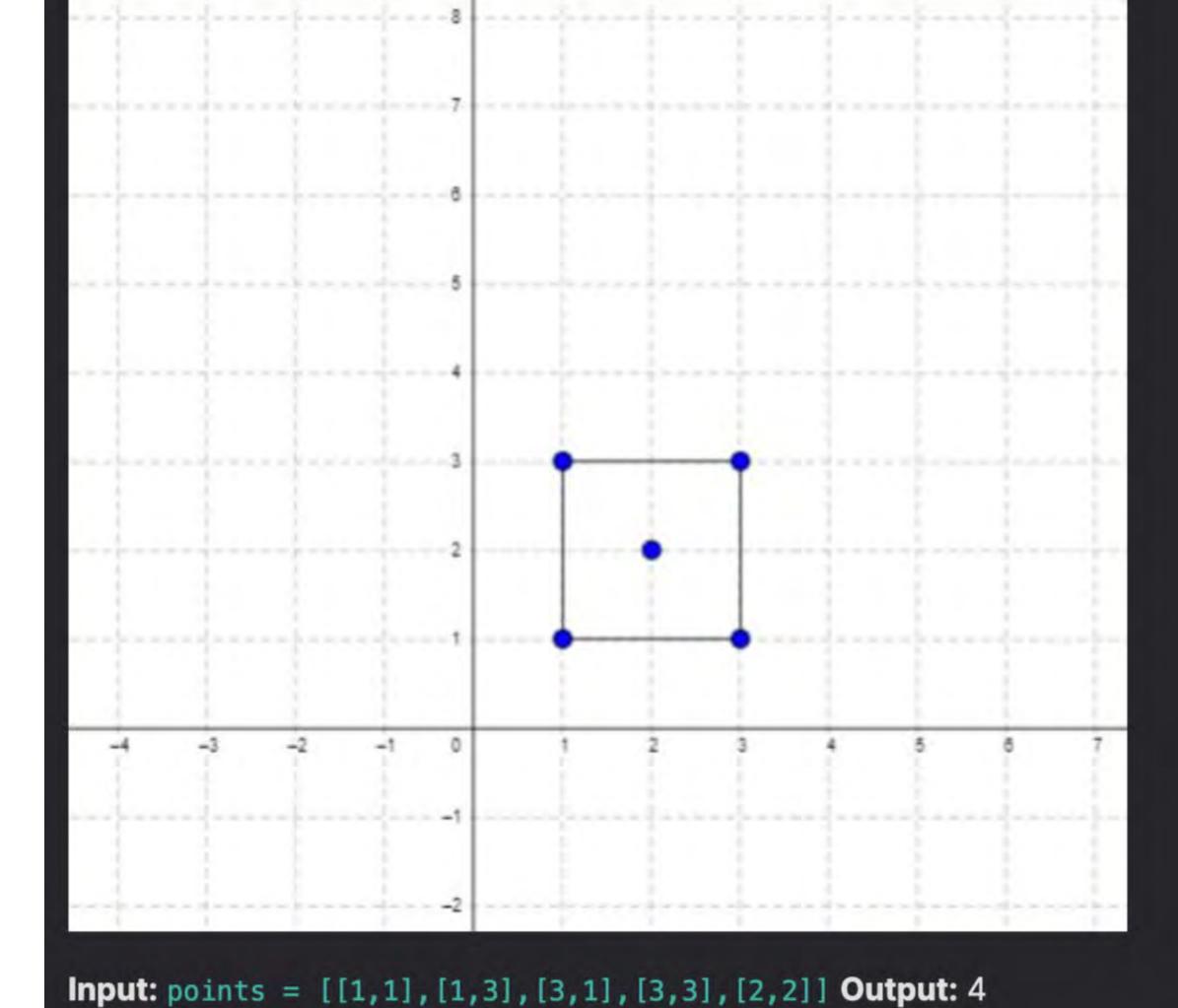
# 939. Minimum Area Rectangle

Leetcode Link

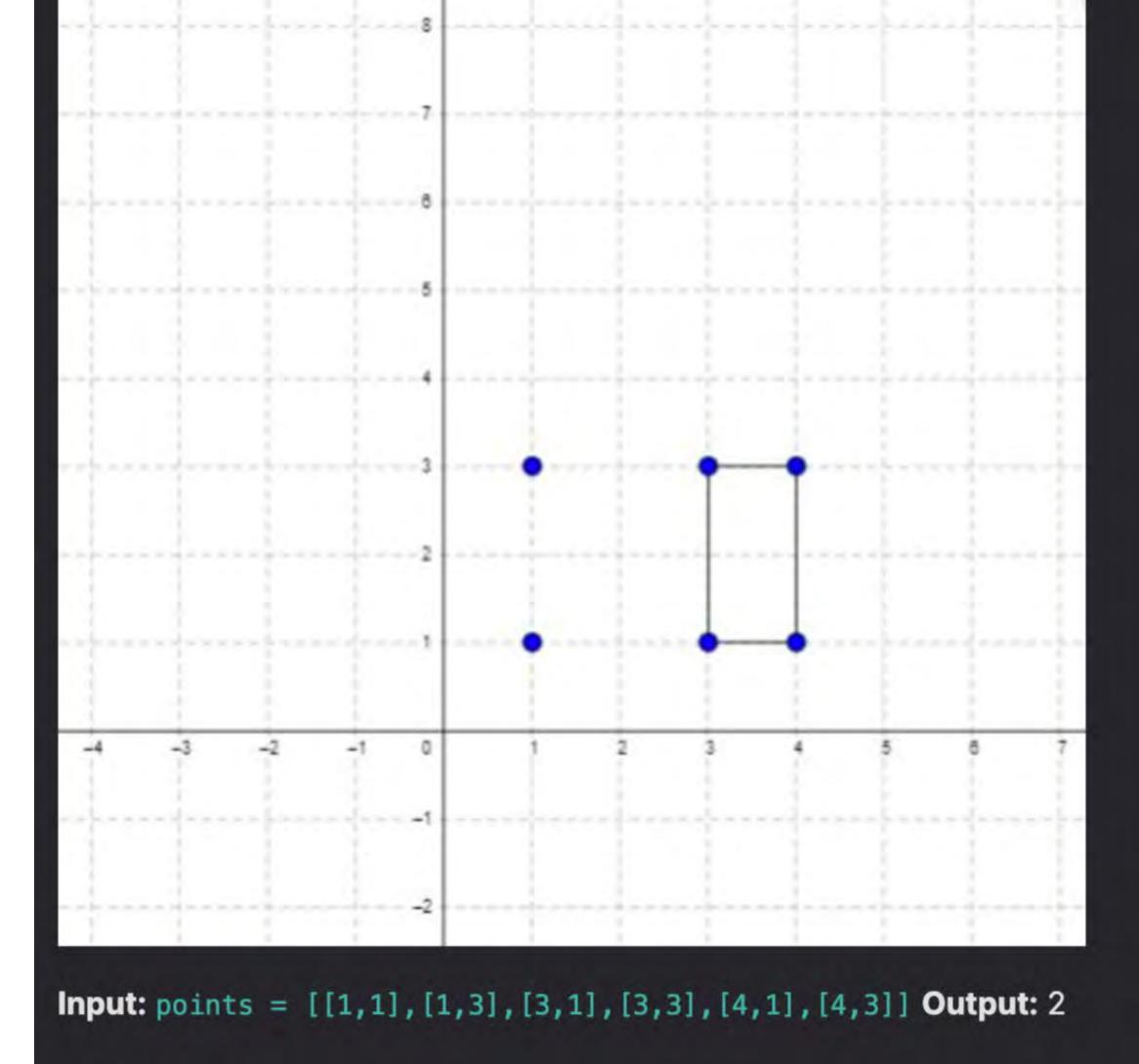
You are given an array of points in the X-Y plane points where points [i] =  $[x_i, y_i]$ .

Return the minimum area of a rectangle formed from these points, with sides parallel to the X and Y axes. If there is not any such rectangle, return 0.

## Example 1:



Example 2:



 $1 \leq exttt{points.length} \leq 500 exttt{ points[i].length} == 2 \ 0 \leq x_i, y_i \leq 4*10^4 ext{ All the given points are unique.}$ 

Solution

**Constraints:** 

# **Brute Force Solution**

## Then, we return the minimum area from a rectangle formed with these points. One key point is that we need to make sure the

rectangle has positive area.

Let N denote the size of points. This algorithm runs in  $\mathcal{O}(N^4)$ .

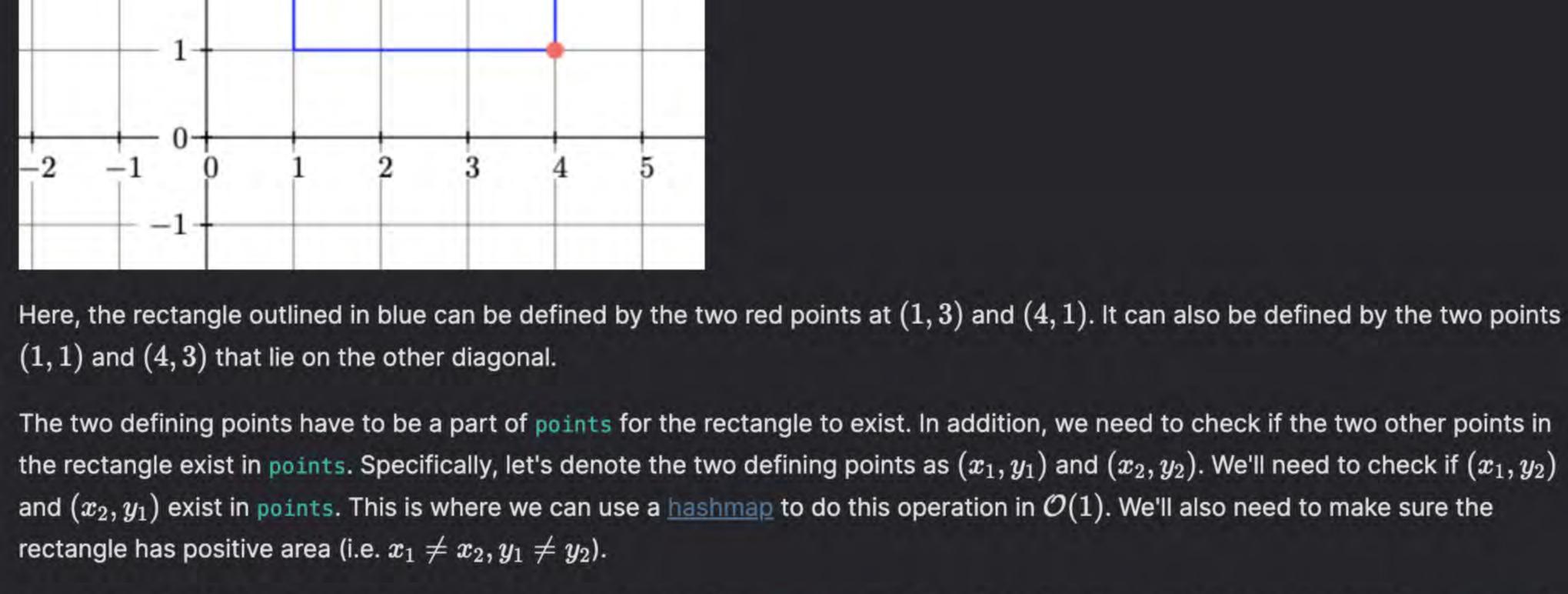
Since we need to form a rectangle from 4 different points, we can check all combinations of 4 points to see if it forms a rectangle.

**Full Solution** 

Let's try to optimize our algorithm to find all possible rectangles faster. One observation we can make is that a rectangle can be

# Example





defined by two points that lie on one of the two diagonals.

Now, instead of trying all combinations of 4 different points from points, we'll try all combinations of 2 different points from points to be the two defining points of the rectangle.

In our algorithm, we check all combinations of 2 different points in points. Since each check runs in  $\mathcal{O}(1)$  and there are  $\mathcal{O}(N^2)$ 

combinations, this algorithm runs in  $\mathcal{O}(N^2)$ . Time Complexity:  $\mathcal{O}(N^2)$ .

# Since we store $\mathcal{O}(N)$ integers in our hashmap, our space complexity is $\mathcal{O}(N)$ . Space Complexity: $\mathcal{O}(N)$ .

C++ Solution

class Solution {

**Space Complexity** 

**Time Complexity** 

unordered\_map<int, unordered\_map<int, bool>> hashMap; for (vector<int> point : points) { // add all points into hashmap hashMap[point[0]][point[1]] = true;

index1++) { // iterate through first defining point

for (int index2 = index1 + 1; index2 < points.size();</pre>

y1 == y2) { // rectangle doesn't have positive area

ans = min(ans, abs(x1 - x2) \* abs(y1 - y2));

y1)) { // check if other points in rectangle exist

public: int minAreaRect(vector<vector<int>>& points) {

int x1 = points[index1][0];

int y1 = points[index1][1];

continue;

int x1 = points[index1][0];

int y1 = points[index1][1];

for (int index1 = 0; index1 < points.size();</pre>

if (hashMap[x1].count(y2) &&

hashMap[x2].count(

int ans = INT\_MAX;

14 index2++) { // iterate through second defining point 15 int x2 = points[index2][0]; 16 int y2 = points[index2][1]; if (x1 == x2 || 17 18

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## 27 28 if (ans == INT\_MAX) { // no solution 29 return 0; 30 31 return ans; 32 33 }; Java Solution 1 class Solution { public int minAreaRect(int[][] points) { HashMap<Integer, HashMap<Integer, Boolean>> hashMap = new HashMap<>(); for (int[] point : points) { // add all points into hashmap if (!hashMap.containsKey(point[0])) { hashMap.put(point[0], new HashMap<>()); hashMap.get(point[0]).put(point[1], true); 9 int ans = Integer.MAX\_VALUE; for (int index1 = 0; index1 < points.length;</pre> 11 12 index1++) { // iterate through first defining point

for (int index2 = index1 + 1; index2 < points.length;</pre>

index2++) { // iterate through second defining point

### 17 int x2 = points[index2][0]; 18 int y2 = points[index2][1]; 19 if (x1 == x2 || y1 == y2) { // rectangle doesn't have positive area 20 continue; 21 if (hashMap.get(x1).containsKey(y2) && hashMap.get(x2).containsKey(y1)) { // check if other points in rectangle exist 24 ans = Math.min(ans, Math.abs(x1 - x2) \* Math.abs(y1 - y2)); 25 26 27 28 if (ans == Integer.MAX\_VALUE) { // no solution 29 return 0; 30 31 return ans; 32 33 } Python Solution Small note: You can use a set in python which acts as a hashset and essentially serves the same purpose as a hashmap for this

solution.

```
1 class Solution:
       def minAreaRect(self, points: List[List[int]]) -> int:
           min_area = 10 ** 9
           points_table = {}
           for x, y in points: # add all points into hashset
6
               points_table[(x, y)] = True
8
           for x1, y1 in points: # iterate through first defining point
9
               for x2, y2 in points: # iterate through second defining point
10
                   if x1 > x2 and y1 > y2: # Skip looking at same point
11
                       if (x1, y2) in points_table and (x2, y1) in points_table: # check if other points in rectangle exist
12
13
                           area = abs(x1 - x2) * abs(y1 - y2)
                           if area:
14
15
                                min_area = min(area, min_area)
16
17
           return 0 if min_area == 10 ** 9 else min_area
```

Got a question? Ask the Teaching Assistant anything you don't understand.