396. Rotate Function

Problem Description



In this problem, you're given an array of integers called nums. This array has n elements. The task is to perform rotations on this array and compute a certain value, called the "rotation function F", for each rotated version of the array.

A rotation consists of shifting every element of the array to the right by one position, and the last element is moved to the first position. This is a clockwise rotation. If nums is rotated by k positions clockwise, the resulting array is named arr_k.

1 $F(k) = 0 * arr_k[0] + 1 * arr_k[1] + ... + (n - 1) * arr_k[n - 1].$

The rotation function F for a rotation k is defined as follows:

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In other words, each element of the rotated array arr_k is multiplied by its index, and the results of these multiplications are summed
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to give F(k). The objective is to find out which rotation (from F(0) to F(n-1)) yields the highest value of F(k) and to return this maximum value.

Intuition

The intuition behind the solution comes from observing that the rotation function F is closely related to the sum of the array and the previous value of F. Specifically, we can derive F(k) from F(k-1) by adding the sum of the array elements and then subtracting the

array size multiplied by the element that just got rotated to the beginning of the array (as this element's coefficient in the rotation function decreases by n). Here's the thinking process: 1. First, compute the initial value of F(0) by multiplying each index by its corresponding value in the unrotated array. This gives us

the starting point for computing subsequent values of F(k).

class Solution:

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2. Keep track of the total sum of the array, as this will be used in computing F(k) for k > 0. 3. Iterate through the array from k = 1 to k = n-1. In each iteration, calculate F(k) based on the previous F(k-1) by adding the

total sum of the array and subtracting n times the element that was at the end of the array in the previous rotation.

- 4. During each iteration, update the maximum value of F(k) found so far.
- By the end of the iteration, we have considered all possible rotations and have kept track of the maximum F(k) value, which the function returns as the answer.
 - The provided Python solution implements this thinking process: python

def maxRotateFunction(self, nums: List[int]) -> int:

f = sum(i * v for i, v in enumerate(nums))

Initial calculation of F(0)

Total sum of the array 9 n, s = len(nums), sum(nums)10 # Starting with the maximum as the initial F(0) 11 12

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# Looping through the array for subsequent Fs
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            for i in range(1, n):
                # Update F(k) based on previous value F(k-1), total sum, and subtracting the last element's contribution
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                f = f + s - n * nums[n - i]
 16
                # Update the answer with the max value found
 17
 18
                ans = max(ans, f)
 19
            return ans
Solution Approach
The solution employs a straightforward approach without any complex algorithms or data structures. It hinges on the mathematical
relationship between the values of F(k) after each rotation. Let's walk through the steps, aligning them with the provided Python
code snippet:
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which multiplies each element by its index and sums up these products. 1 f = sum(i * v for i, v in enumerate(nums))

the maximum value.

1 for i in range(1, n):

ans = max(ans, f)

proportionate to the size of the input.

Example Walkthrough

f = f + s - n * nums[n - i]

function F effectively decreases by n due to the rotation.

Let's consider a small array nums = [4, 3, 2, 6] to illustrate the solution approach.

F(0) = 0*4 + 1*3 + 2*2 + 3*6 = 0 + 3 + 4 + 18 = 25

i].

avoid recalculating these values in each iteration of the loop, which follows next. 1 n, s = len(nums), sum(nums)

The variables n and s are initialized to store the length of the array and the sum of its elements respectively. This is done to

1. Initial Value of F(0): Calculating the initial value of F(0) involves using a simple loop or in this case, a generator expression,

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1 ans = f
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3. Iterative Calculation of Subsequent F(k): We know that the subsequent value F(k) can be derived from F(k-1) by adding the

sum of the array s to it and subtracting n times the last element of the array before it got rotated to the front, which is nums [n -

The loop runs from 1 to n - 1 representing all possible k rotations (starting from 1 because we have already calculated F(0)).

2. Initializing the Maximum Value: Before beginning the loop, we record the initial value of F(0) in the variable ans as this might be

 We adjust f to find the current F(k). The s is the total sum of the array, and we subtract the value that would have been added if there had been no rotation multiplied by n, which is n * nums[n - i]. We're subtracting it because its index in the

We update ans with the maximum value found so far by comparing it with the newly computed F(k).

1. Initial Value of F(0): We calculate F(0) by multiplying each element by its index and summing them up:

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4. Returning the Result: Once all rotations have been considered, the variable ans holds the maximum value found, which is then
   returned.
In terms of complexity, the time complexity of this solution is O(n) since it iterates through the array once after calculating the initial
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F(0). The space complexity is O(1) since it uses a fixed number of variables and doesn't allocate any additional data structures

In the code, this is done using: 1 f = sum(i * v for i, v in enumerate(nums))

We also compute the total sum of the array s = 4 + 3 + 2 + 6 = 15 and store the number of elements n = 4. These are

calculated once to be used in subsequent rotation calculations: 1 n, s = len(nums), sum(nums)

1 ans = f # ans = 25 initially

1 ans = max(ans, f) # ans remains 25 as 23 < 25

Finally, calculate F(3):

Python Solution

1 class Solution:

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2. Initializing the Maximum Value: We start by considering F(0) as the potential maximum.

3. Iterative Calculation of Subsequent F(k): Now we calculate F(1) based on F(0):

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F(1) = F(0) + s - n * nums[n - 1]
F(1) = 25 + 15 - 4*6 = 25 + 15 - 24 = 16
And we check if this is greater than the current maximum ans:
1 ans = max(ans, f) # ans remains 25 as 16 < 25
Next, we calculate F(2):
F(2) = F(1) + s - n * nums[n - 2] = 16 + 15 - 4*2 = 16 + 15 - 8 = 23
Again, we update if it's greater than ans:
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1 ans = max(ans, f) # ans is now updated to 26
 4. Returning the Result: We have considered all possible rotations (F(0) through F(3)) and the maximum value of F(k) is 26,
   achieved at k = 3. This is returned as the result.
   1 return ans # returns 26
Putting all this into action with our small example array nums = [4, 3, 2, 6], we find the rotation function that yields the highest
value is F(3), and the maximum value returned is 26.
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total_function_value = sum(index * value for index, value in enumerate(nums))

Get the number of elements and the sum of all elements in nums

Iterate through the array to find the maximal F value after rotations

Rotate the array by one element towards the right and update the function value

This is achieved by adding the sum of all elements minus the last element value

int firstComputation = 0; // This will store the initial computation of the function F(0)

// Total number of elements in the array

// Calculate initial configuration values for currentFunctionValue and sumOfElements

// Compute the next value of F by adding the sumOfElements and subtracting

// Iterate over the array to find the maximal rotation function value

// the last element multiplied by the number of elements

for (int i = 0; i < numberOfElements; ++i) {</pre>

currentFunctionValue += i * nums[i];

for (int i = 1; i < numberOfElements; ++i) {</pre>

sumOfElements += nums[i];

total_function_value += sum_of_elements - num_elements * nums[num_elements - i]

that is 'rotated' to the 'front' of the array times the number of elements

Update max_function_value if the new total_function_value is greater

max_function_value = max(max_function_value, total_function_value)

F(3) = F(2) + s - n * nums[n - 3] = 23 + 15 - 4*3 = 23 + 15 - 12 = 26

Now F(3) is greater than the current maximum ans, so we update ans:

def max_rotate_function(self, nums: List[int]) -> int:

max_function_value = total_function_value

num_elements = len(nums)

sum_of_elements = sum(nums)

for i in range(1, num_elements):

public int maxRotateFunction(int[] nums) {

Calculate the initial value of the function F

Initialize ans with the initial total_function_value

23 # Return the maximum value found 24 return max_function_value 25

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int sumOfAllNumbers = 0; // This holds the sum of all the elements in the array
int n = nums.length;
// Calculate the initial value of F(0) and sum of all numbers in the array
for (int i = 0; i < n; ++i) {
    firstComputation += i * nums[i];
```

Java Solution

1 class Solution {

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sumOfAllNumbers += nums[i];
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           int maxResult = firstComputation; // Initialize maxResult with the first computation of the function
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           // Compute the maximum value of F(i) by iterating through the possible rotations
           for (int i = 1; i < n; ++i) {
14
               // Compute the next value of F based on the previous value (F = F + sum - n * nums[n - i])
15
               firstComputation = firstComputation + sumOfAllNumbers - n * nums[n - i];
16
               // Update maxResult if the new computed value is greater than the current maxResult
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               maxResult = Math.max(maxResult, firstComputation);
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           // Return the maximum result found
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           return maxResult;
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C++ Solution
1 #include <vector>
2 #include <algorithm> // For std::max
   class Solution {
   public:
       int maxRotateFunction(std::vector<int>& nums) {
           int currentFunctionValue = 0; // Initialize sum of i*nums[i]
           int sumOfElements = 0; // Initialize sum of nums[i] for all i
           int numberOfElements = nums.size(); // Number of elements in the array
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int maxFunctionValue = currentFunctionValue; // Initialize the maximal value of F with current configuration

currentFunctionValue = currentFunctionValue + sumOfElements - numberOfElements * nums[numberOfElements - i];

24 25 // Update the maxFunctionValue with the maximum of current and the newly computed value 26 maxFunctionValue = std::max(maxFunctionValue, currentFunctionValue); 27

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           // Return the maximum value found for the rotation function
           return maxFunctionValue;
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32 };
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Typescript Solution
   function maxRotateFunction(nums: number[]): number {
       const numElements = nums.length; // The number of elements in the input array
       // Calculate the sum of all numbers in the array
       const totalSum = nums.reduce((accumulator, value) => accumulator + value, 0);
 6
       // Initialize the function result using the formula F(0) = 0 * nums[0] + 1 * nums[1] + ... + (n-1) * nums[n-1]
       let maxFunctionValue = nums.reduce((accumulator, value, index) => accumulator + value * index, 0);
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       // The previous state's function value, starting with F(0)
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       let previousFunctionValue = maxFunctionValue;
13
       // Iterate through the array to find the maximum function value after each rotation
       for (let i = 1; i < numElements; i++) {</pre>
14
           // Calculate the function value F(i) for the current rotation based on F(i-1), the previous rotation
15
           previousFunctionValue = previousFunctionValue - (totalSum - nums[i - 1]) + nums[i - 1] * (numElements - 1);
           // Update the maximum function value found so far
17
           maxFunctionValue = Math.max(maxFunctionValue, previousFunctionValue);
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       // Return the maximum found function value
21
       return maxFunctionValue;
22
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Time and Space Complexity

through the numbers in nums to calculate the initial value of f, which will take 0(n) time. After that, there is a for-loop that iterates n-1 times, and in each iteration, it performs a constant amount of work which does not depend on n. Hence, the loop contributes O(n) to the time complexity as well. The space complexity of the code is 0(1). This is because only a constant amount of extra space is used for variables f, n, s, and

The time complexity of the code is O(n), where n is the length of the nums list. This is because there is one initial loop that goes

ans, and the input nums is not being copied or expanded, thus the space used does not grow with the size of the input.