1011. Capacity To Ship Packages Within D Days

Medium Array Binary Search

Problem Description

belt within a specified number of days. Each package has a certain weight, and the ship cannot carry more than its maximum weight capacity. Therefore, the goal is to determine the smallest maximum weight that the ship can handle such that all the packages can still be shipped on time.

To accomplish this task, the packages must be loaded onto the ship in the same order as they are placed on the conveyor belt. This

In this problem, we are tasked with finding the minimum weight capacity of a ship that is required to ship all packages on a conveyor

restriction adds complexity since we cannot reorder the packages to better fit the ship's weight capacity on a given day. Additionally, there is a limit to the number of days available to ship all packages.

Put simply, we need to discover the lightest possible maximum weight of the ship that allows all packages to be shipped within the

given time frame. This weight determines how many packages can be loaded each day without exceeding the ship's weight limit, thus ensuring timely delivery.

Intuition

The solution to this problem relies on binary search, an efficient algorithm for finding an item in a sorted array. However, the direct

application is not obvious because the weights are not sorted, and we are also dealing with an optimization problem, not just a simple search.

We use <u>binary search</u> to narrow down the possible range of the ship's weight capacity. The intuition here is that there is a lower bound, which is at least as large as the heaviest package (since the ship must be able to carry the heaviest package), and an upper bound, which is the sum of all package weights (since the ship can carry all packages at once).

The <u>binary search</u> will repeatedly split the range in half. At each step, it will guess a middle value and use a helper function check to determine if it is possible to ship all packages within 'days' days, without exceeding the guess weight capacity. The helper function will simulate the process of loading packages onto the ship:

When the maximum is reached, it simulates the start of a new day, incrementing a day counter.
 If the day counter exceeds the allowed number of days, the guess is too low and we must try a larger capacity.
 The <u>binary search</u> is constrained within the range between the heaviest package and the total weight using the <u>bisect_left</u>

function. bisect_left will find the position to insert the lower bound of the ship's capacity in such a way that all packages are

shipped within the time frame. At the end of the binary search, the minimum weight capacity of the ship is found, which is the goal of

It sums the weights of the packages until adding another package would exceed the assumed maximum capacity.

the problem.

packages within days days, given a maximum shipping weight of mx.

the ship must have to ensure even the heaviest package can be shipped.

Here, it's used to find the minimum valid capacity.

position gives us the exact weight capacity.

We first determine the search range for the ship's capacity:

Day 3: The last package 1 is loaded.

right becoming the current guess 8.

4. Repeat the binary search process:

The solution approach revolves around <u>binary search</u>, and here's a step-by-step breakdown of how the provided solution in Python implements it:

1. **Define the check Function**:

• The helper function check(mx) simulates the loading of packages onto the ship to determine if it is possible to ship all

It iterates through each weight in weights and aggregates them until the current load exceeds mx. Once the aggregated weight exceeds mx, it simulates starting a new day by resetting the load to the

Solution Approach

Once the aggregated weight exceeds mx, it simulates starting a new day by resetting the load to the current weight and incrementing the day count.
 After iterating through all weights, if the number of days needed is less than or equal to days, it means the mx is a viable

2. Determine the Search Range:

capacity; otherwise, it is not.

upper bound for the binary search:

o bisect_left function is used to perform the binary search. This is a function provided by Python's standard library, which

uses binary search to find the insertion point for a given element x in a sorted array to maintain the array's sorted order.

The range from left to right is provided along with a key function check which bisect_left uses to determine the validity

position is the insertion point returned by bisect_left. Since left is the starting point of the search range, adding the

• The upper bound right is set to the sum of all weights plus one (sum(weights) + 1), the plus one being a non-inclusive

• The lower bound left is set to the maximum single package weight (max(weights)). This is the absolute minimum capacity

of the capacity. True represents the element to be inserted, corresponding to the condition of finding a workable capacity.

4. Return the Calculated Capacity:

• The minimum weight capacity is found when bisect_left concludes the search. It's computed as left + position where

By leveraging binary search, the solution minimizes the number of times it needs to check for a viable shipping plan, which

drastically reduces the time complexity compared to linearly searching through all possible capacities. The use of bisect_left

provides a concise and efficient way to perform the search. The check function acts as a simulation/verification step that guarantees that the found capacity is indeed the lowest that can still ship all packages within the provided number of days.

The heaviest package is 4, so our lower bound left is 4.
The sum of all package weights is 3+2+2+4+1 = 12, so our upper bound right is 13 (one more than the sum for binary search).
Now, we apply the binary search approach:
1. We start with the middle of our range. The initial guess for the ship's capacity will be (left + right) / 2 which is (4 + 13) / 2

= 8.5. We round this down to 8 (since ship capacity must be an integer and binary search takes the lower mid).

Let's assume we have the following input where weights = [3, 2, 2, 4, 1] represent the weights of the packages, and we need to

Day 1: We load 3 + 2 + 2 because adding the next package would exceed the capacity. Day 2: We start with the next package and load 4.

Example Walkthrough

ship all packages within days = 3.

We managed to load all the packages in 3 days which is within our allowed days. This indicates capacity 8 is possible.

3. Since 8 worked, we now try to find if there is a smaller possible capacity. We adjust our search range to left remaining 4 and

Day 3: We load the last package 1.
 Again, we have managed to load all the packages in 3 days, so capacity 6 seems to work as well.

Day 2: We continue with 2 + 4, we reach the capacity exactly.

 \circ New middle is (4 + 8) / 2 = 6. So we check capacity 6.

6. New middle is (4 + 6) / 2 = 5. So we check capacity 5.

the total weight, we eliminate half of the possibilities with each step.

to ship all the packages within 'days' days

Loop through the weights of the packages

if current_weight > max_capacity:

current_weight = weight

32 # min_capacity = solution.shipWithinDays([1,2,3,4,5,6,7,8,9,10], 5)

leftBoundary = midCapacity + 1;

private boolean canShip(int[] weights, int capacity, int days) {

int currentLoad = 0; // Current weight load of the ship

// Iterating over each weight to simulate the shipping process

// Start with the first day

currentLoad = weight; // Reset load with the current weight

// Move to the next day

// If the number of shipping days needed is within the allowed range, return true

// Return the minimum valid ship capacity

return leftBoundary;

int dayCount = 1;

for (int weight : weights) {

dayCount++;

return dayCount <= days;</pre>

currentLoad += weight;

if (currentLoad > capacity)

def can_ship_with_capacity(max_capacity):

day_count += 1

for weight in weights:

return min_capacity_needed

2. With a capacity of 8, we simulate the loading using the check function:

5. We continue the binary search with the new range left is 4 and right is now 6.

Day 1: We load 3 and cannot add 2 because it would exceed capacity, so we load just 3.

Day 1: We load 3 + 2 because adding another package would exceed the capacity.

Day 2: We load 2 + 2 and stop there, as adding 4 would exceed the capacity.
 Day 3: We load 4, but now we cannot load the last package as it would require an additional day.
 In this case, we failed to load all packages within 3 days using capacity 5. This tells us the capacity of 5 is too low.

Given that left and right are now the same, the search ends, and we have found that the minimum capacity needed is 6.

By using binary search and simulating the loading of packages, we determined that the minimum capacity of the ship to load all the

packages within 3 days is 6. This approach is efficient because instead of trying every capacity between the heaviest package and

Python Solution

1 from typing import List
2 from bicoct import higher left

Helper function to check if the given capacity 'max_capacity' is enough

current_weight += weight # Add package weight to current load

and reset the current load to the current package's weight

If the current load exceeds the max capacity, start a new day

Use binary search to find the minimum capacity needed to ship within 'days' days

The search will find the first value where 'can_ship_with_capacity' returns True

// Helper method to determine if the given capacity can ship all weights within the given days

// If adding weight exceeds capacity, ship current load and increment day counter

min_capacity_needed = left + bisect_left(range(left, right), True, key=can_ship_with_capacity)

current_weight, day_count = 0, 1 # Initialize current total weight and day count

7. Now adjust the range with left becoming 6, since 5 didn't work, and right staying 6.

The capacity is enough if we can ship within required days
return day_count <= days

Define the search space between largest single package and total weight
left, right = max(weights), sum(weights)</pre>

1 from typing import List
2 from bisect import bisect_left
3
4 class Solution:
5 def shipWithinDays(self, weights: List[int], days: int) -> int:

9

10

11

12

13

14

15

16

17

18

19

20

21

22

23

24

25

26

27

28

29

20

21

22

24

25

26

27

28

29

30

31

32

33

34

35

36

37

38

39

40

41

42

43

44

46

45 }

C++ Solution

1 #include <vector>

30 # Example usage:

31 # solution = Solution()

33 # print(min_capacity) # Output: 15

- 34 Java Solution class Solution { public int shipWithinDays(int[] weights, int days) { // Setting initial left boundary to the largest weight // and right boundary to the sum of all weights int leftBoundary = 0, rightBoundary = 0; for (int weight : weights) { leftBoundary = Math.max(leftBoundary, weight); rightBoundary += weight; 9 10 11 // Binary search to find the minimum capacity of the ship that will work within given days 12 while (leftBoundary < rightBoundary) {</pre> 13 // Midpoint to test if it's a valid ship capacity int midCapacity = (leftBoundary + rightBoundary) >> 1; 14 // Check if midCapacity is enough, if so, look for a smaller potential capacity 15 if (canShip(weights, midCapacity, days)) { 16 rightBoundary = midCapacity; } else { 19 // Otherwise, discard midCapacity and look for a larger one
- 2 #include <algorithm> // For max()
 3 using std::vector;
 4 using std::max;
 5
 6 class Solution {
 7 public:
 8 // Function to find the minimum capacity of a ship that can ship all the packages within 'days' days
 9 int shipWithinDays(vector<int>& weights, int days) {
 10 int minCapacity = 0; // Lower boundary of binary search max weight in the shipment
- int maxCapacity = 0; // Upper boundary of binary search sum of all weights 11 12 13 // Calculate the minimum and maximum capacity for (int weight : weights) { 14 15 minCapacity = max(minCapacity, weight); 16 maxCapacity += weight; 17 18 19 // Lambda function to check if mid value can work as the capacity 20 auto canShipWithCapacity = [&](int capacity) -> bool { int currentWeightSum = 0; // Current weight sum of the ongoing shipment 21 22 int dayCount = 1; // Counter for the number of days needed 23 24 for (int weight : weights) { currentWeightSum += weight; 25 26 27 // Check if adding the current weight exceeds capacity, if so, reset for the next day 28 if (currentWeightSum > capacity) { 29 currentWeightSum = weight; 30 dayCount++; 31 32 33 34 // Check if we can ship within the given number of days with the current capacity 35 return dayCount <= days;</pre> 36 **}**; 37 38 // Binary search to find the minimum capacity required while (minCapacity < maxCapacity) {</pre> 39 int midCapacity = (minCapacity + maxCapacity) / 2; 40 41 // Check if the midCapacity can be a possible solution, adjust search boundaries based on it 43 if (canShipWithCapacity(midCapacity)) { maxCapacity = midCapacity; 44 45 } else { 46 minCapacity = midCapacity + 1; 49 50 // Return the minimum capacity needed to ship within 'days' days 51 return minCapacity; 52 53 };

let currentWeightSum = 0; // Current total weight in the current shipment let requiredDays = 1; // Start with 1 day, the minimum possible for (const weight of weights) { currentWeightSum += weight; }

Typescript Solution

let lowerBound = 0;

let upperBound = 0;

for (const weight of weights) {

function shipWithinDays(weights: number[], days: number): number {

// Initialize the lower and upper bounds for the binary search

// Calculate the initial bounds for the capacity of the ship

const canShipInDays = (maxCapacity: number): boolean => {

if (currentWeightSum > maxCapacity) {

++requiredDays;

return requiredDays <= days;</pre>

54

6

9

10

11

12

13

20

21

22

23

24

25

26

27

28

29

};

```
30
       // Perform a binary search to find the minimum capacity needed to ship within 'days'
31
       while (lowerBound < upperBound)</pre>
32
           const midCapacity = Math.floor((lowerBound + upperBound) / 2); // Mid-point of the current bounds
33
34
           // If it's possible to ship with this capacity, reduce the upper bound to midCapacity
35
36
           if (canShipInDays(midCapacity)) {
37
               upperBound = midCapacity;
38
           } else {
39
               // Otherwise, increase the lower bound just above midCapacity
               lowerBound = midCapacity + 1;
40
41
42
43
       // The lower bound at the end of the binary search will be the minimum capacity needed to meet the requirement
44
       return lowerBound;
45
46 }
47
Time and Space Complexity
The time complexity of the code is 0(n * log(S)), where n is the number of elements in weights, and S is the sum of weights minus
the maximum weight in weights. This is because the binary search is performed over a range with left and right as lower and upper
```

current weight sum and the count of days, both of which do not depend on the input size.

lowerBound = Math.max(lowerBound, weight); // The ship's capacity must be at least as much as the heaviest package

currentWeightSum = weight; // Reset the currentWeightSum with the current weight as the start for the next day

// Increment the day counter as we move to the next day

upperBound += weight; // The maximum capacity is the sum of all weights, i.e., shipping all at once

// If adding the current weight exceeds max capacity, need a new shipment (next day)

// Return true if the number of required days is less than or equal to the given days, false otherwise

bounds, respectively. The check function, called at each step of the binary search, runs in O(n) time since it iterates through all the

elements of weights. Since the binary search narrows the range by half each time, it will run log(S - max(weights)) times.

The space complexity of the code is 0(1) as it uses a constant amount of space. The check function uses variables to store the

// Function to determine if it's possible to ship all packages within 'days' given a maximum capacity 'maxCapacity'