Problem Description

array that meet certain conditions. Specifically, the conditions for the indices are: • Indices i, j, and k must maintain the sequence 0 < i < j < k < n-1, where n is the length of the array.

In this problem, we are given an array of integers, nums, and we need to determine if there exists a triplet of indices (i, j, k) in the

- The sum of elements in four subarrays is equal. The subarrays are: ○ Subarray 1: Elements from index 0 to i-1 (both inclusive). ○ Subarray 2: Elements from index i+1 to j-1 (both inclusive).
 - Subarray 3: Elements from index j+1 to k-1 (both inclusive).
- A subarray (1, r) represents the sequence of elements in the array nums from the 1th element to the rth element, inclusive.

The aim is to return true if at least one such triplet (i, j, k) exists, and false otherwise.

 \circ Subarray 4: Elements from index k+1 to the end of the array (index n-1).

- Intuition

The intuition behind the solution is to find a way to efficiently determine if the sum of elements in the given subarrays are equal without recalculating them each time for different values of i, j, and k. To do this, we can make use of prefix sums and a set.

Here is how we could approach the problem:

 First, we can calculate a prefix sum array s for the given nums array. The prefix sum array contains the sum of all numbers up to and including the ith index of nums. This helps us calculate the sum of any subarray in constant time.

2. Determining Equal Subarray Sums:

To find the correct index j, we need to ensure that we have enough space on either side for indices i and k to exist.

3. Checking for Match:

1. Prefix Sum Computation:

Therefore, we scan for j starting from index 3 to n - 3. If j is too close to the start or end, there can't be four subarrays with equal sums. For each j, we establish two loops:

- An inner loop over i, which ranges from 1 to j 1, looking for subarrays that could be equal in sum to the other subarrays. ■ We check if the sum of elements from 0 to i-1 is equal to the sum from i+1 to j-1. When we find such an instance, we add the sum to a set seen as a potential candidate for the subarray sum.
 - We check if the sum of elements from j+1 to k-1 is equal to the sum from k+1 to n-1.

subarrays for each possible combination of (i, j, k) triplet.

■ If it is and the sum is already in seen, there exists at least one combination of i, j, k that satisfies all conditions, thus, we return true.

■ An outer loop over k, which ranges from j + 2 to n - 1, looking for subarrays that could match the ones identified by i.

- If we exit both loops without finding such a triplet, then we conclude that no such triplet exists, and we return false.
- By implementing this approach, we avoid recalculating the sum for each subarray from scratch, which would otherwise result in a much less efficient solution.
- **Solution Approach** To implement the solution described in the intuition, we make use of a couple of important programming concepts: prefix sums and

hash sets. This enables us to have an efficient algorithm that can solve the problem without repeatedly computing the sums of the

1. Initialization and Prefix Sum Computation:

sums of nums.

subarrays.

nums up to (and including) index i-1. 2. Finding the Index j: ∘ Iterate over possible values of j starting from index 3 to n - 3. The choice of starting from 3 ensures that there is space for

at least two elements before j and ending at n - 3 ensures there's space for at least two elements after j.

o Initialize an array s with length n + 1 where n is the length of the input array nums. The s array is going to store the prefix

• Fill the s array with prefix sums, where s[i + 1] = s[i] + nums[i]. This means s[i] holds the total sum from the start of

3. Exploring Potential Values for i:

Here's a step-by-step walk-through of the implementation based on the provided solution code:

 Loop through i which starts from 1 and goes up to j - 1, perform the following: ■ Check if the sum of the subarray (0, i - 1) which is s[i], is equal to the sum of the subarray (i + 1, j - 1) which is s[j] - s[i + 1].

• For each j, initialize an empty set seen. This set is used to store sums of subarrays that could potentially match with other

n - 1) which is s[n] - s[k + 1].

5. Returning the Result:

making it a much faster algorithm.

1 nums = [1, 2, 1, 2, 1, 2, 1]

s will have 8 elements.

4. Exploring Potential Values for k:

■ If they are equal and the sum (the sum of the subarray (j + 1, k - 1)) exists in the seen set, we have found a triplet (i, j, k) that satisfies all the conditions.

This approach is efficient because we utilized the pre-computed prefix sum array to quickly access the sum of any subarray in

constant time. Additionally, by using the set to keep track of seen sums, we avoid redundant comparisons for each potential k,

■ Check if the sum of the subarray (j + 1, k - 1) which is s[k] - s[j + 1], is equal to the sum of the subarray (k + 1,

If we finish both loops and haven't returned true, we determine that no such triplet exists, and therefore, we return false.

At this point, return true since the required triplet exists.

○ Next, loop through k which starts from j + 2 and ends at n - 1, perform the following:

Example Walkthrough

instance, s[4] = 6 representing the sum of nums from index 0 to 2.

○ Loop through i which starts from 1 and goes up to 2 (j - 1):

Consider the array nums with the following elements:

Let's walk through the solution approach with this example:

If they are equal, add the sum to the set seen.

1. Initialization and Prefix Sum Computation: • First, we initialize an array s for storing prefix sums with n + 1 elements, where n is the length of nums. In this case, n is 7, so

• Then we compute the prefix sums. So the s array after prefix sum computation will be [0, 1, 3, 4, 6, 7, 9, 10]. For

■ For k = 5, we check the sums: s[5] - s[4] = 7 - 6 = 1 and s[7] - s[6] = 10 - 9 = 1. They are equal, and 1 is in the

In this case, we found at least one valid triplet that satisfies all the conditions. Hence, if we were to implement this example

2. Finding the Index j: \circ We iterate over possible values of j from 3 to 4 (as n - 3 is 4 for this example). 3. Exploring Potential Values for i for j = 3:

• For i = 1, we check the sums: s[1] = 1 and s[3] - s[2] = 4 - 3 = 1. They are equal, so we add 1 to seen. 4. Exploring Potential Values for k for j = 3:

seen set.

5. Returning the Result:

Python Solution

class Solution:

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from typing import List

n = len(nums)

return False

■ Having found a k such that the sum from j+1 to k-1 matches the sum from k+1 to n-1 and is also in seen, we have found a valid triplet (i, j, k) which is (1, 3, 5). We return true since we have found the required triplet.

def splitArray(self, nums: List[int]) -> bool:

for left in range(1, mid - 1):

return True

int[] prefixSums = new int[n + 1];

// Calculate the prefix sums

for (int i = 0; i < n; ++i) {

for (int j = 3; j < n - 3; ++j) {

for right in range(mid + 2, n - 1):

Get the length of the input array

 $prefix_sum = [0] * (n + 1)$

for i, num in enumerate(nums):

in code, the result would be true.

We initialize an empty set seen for j = 3.

This example illustrates how the intuition and approach to the problem can be used to efficiently find a triplet in the array that meets the requirements.

Initialize a prefix sum array with an extra position for simplicity

Compute the prefix sum array where prefix_sum[i] represents

Check for all possible splits in the first half

seen_sums.add(prefix_sum[left])

If we reach this point, no valid split was found

prefixSums[i + 1] = prefixSums[i] + nums[i];

// 'j' is the potential middle split point

// Traverse through the array, starting from index 3 to n-4

If a valid split is found, add the sum to the set

Check for all possible splits in the second half of the array

// Array to store the prefix sums, one extra element for ease of calculations

if prefix_sum[left] == prefix_sum[mid] - prefix_sum[left + 1]:

Check if there is a valid split that matches any sum in 'seen_sums'

and prefix_sum[n] - prefix_sum[right + 1] in seen_sums):

if (prefix_sum[n] - prefix_sum[right + 1] == prefix_sum[right] - prefix_sum[mid + 1]

the sum of elements from nums[0] to nums[i-1]

prefix_sum[i + 1] = prefix_sum[i] + num

 \circ We loop through k which can only be 5 since it starts from j + 2 and ends at n - 1 for this j.

The main loop to check for split positions starting at index 3 17 # and ending at n-4 to ensure there are enough elements on both sides 18 for mid in range(3, n - 3): 19 # Store sums that can be created from the first half of the array 20 seen_sums = set() 21

class Solution { public boolean splitArray(int[] nums) { int n = nums.length;

Java Solution

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Set<Integer> seenSums = new HashSet<>();
15
               // First pass to check possible sums from the left subarray
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               for (int i = 1; i < j - 1; ++i) {
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                   if (prefixSums[i] == prefixSums[j] - prefixSums[i + 1]) {
                       seenSums.add(prefixSums[i]);
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               // Second pass to check matching sums from the right subarray
               for (int k = j + 2; k < n - 1; ++k) {
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                   if (prefixSums[n] - prefixSums[k + 1] == prefixSums[k] - prefixSums[j + 1] && seenSums.contains(prefixSums[n] - prefi
                       return true; // Found a valid split
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           // If no valid split is found
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           return false;
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33 }
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C++ Solution
1 class Solution {
2 public:
       // Function that determines if the array can be split into four parts
       // with the same sum, with one element between these parts.
       bool splitArray(vector<int>& nums) {
           int n = nums.size();
           vector<int> prefixSum(n + 1, 0); // Initialize prefix sums array with an additional 0 at the start.
           // Calculate prefix sums for all elements.
           for (int i = 0; i < n; ++i) {
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               prefixSum[i + 1] = prefixSum[i] + nums[i];
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           // Use a three-pointer approach to find the split points.
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           for (int middle = 3; middle < n - 3; ++middle) { // middle is the middle cut, avoiding the first 2 and last 2 elements.
               unordered_set<int> seenSums; // Store sums that we've seen which are candidates for the first section.
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               // Find all possible sums for the left section.
               for (int left = 1; left < middle - 1; ++left) {</pre>
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                   if (prefixSum[left] == prefixSum[middle] - prefixSum[left + 1]) {
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// If a sum that can be the left section is found, add it to 'seenSums'.

if (prefixSum[n] - prefixSum[right + 1] == prefixSum[right] - prefixSum[middle + 1]

// If the sum for the right section equals one of the left section sums, return true for a successful split.

seenSums.insert(prefixSum[left]);

return false; // Return false if no such split is found.

return true;

// Find if there's a corresponding sum for the right section.

&& seenSums.count(prefixSum[n] - prefixSum[right + 1])) {

1 // Function that determines if the array can be splitted into four parts with the same sum,

for (int right = middle + 2; right < n - 1; ++right) {</pre>

15 16 17

Typescript Solution

2 // with one element between these parts.

let n: number = nums.length;

for (let i = 0; i < n; ++i) {

function splitArray(nums: number[]): boolean {

// Calculate prefix sums for all elements.

prefixSum[i + 1] = prefixSum[i] + nums[i];

```
12
         // Use a three-pointer approach to find the split points.
 13
         for (let middle = 3; middle < n - 3; ++middle) { // 'middle' is the middle cut, avoiding the first 2 and last 2 elements.
             let seenSums: Set<number> = new Set<number>(); // Store sums that we've seen which are candidates for the first section.
 14
             // Find all possible sums for the left section
             for (let left = 1; left < middle - 1; ++left) {</pre>
 18
                 if (prefixSum[left] === prefixSum[middle] - prefixSum[left + 1]) {
 19
                     // If a sum that can be the left section is found, add it to 'seenSums'.
                     seenSums.add(prefixSum[left]);
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 24
             // Find if there's a corresponding sum for the right section.
 25
             for (let right = middle + 2; right < n - 1; ++right) {</pre>
                 if (prefixSum[n] - prefixSum[right + 1] === prefixSum[right] - prefixSum[middle + 1]
 26
                     && seenSums.has(prefixSum[n] - prefixSum[right + 1])) {
 27
 28
                     // If the sum for the right section equals one of the left section sums, return true for a successful split.
 29
                     return true;
 30
 31
 32
 33
         return false; // Return false if no such split is found.
 34 }
 35
 36 // Example usage:
    let nums: number[] = [1, 2, 1, 2, 1, 2, 1];
    console.log(splitArray(nums)); // Output should be true or false depending on the array content.
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Time and Space Complexity
Time Complexity
The given Python function splitArray is designed to determine if an array can be split into four parts with equal sums. The function
uses a prefix sum array s to efficiently calculate the sums of subarrays.
```

let prefixSum: number[] = new Array(n + 1).fill(0); // Initialize prefix sums array with an additional 0 at the start.

(j-2) times for each j. The worst-case scenario for the second loop would be when j is around n/2, which would yield roughly (n/2) iterations. Thus, the innermost condition is checked 0(n^2) times. The third loop can be considered separately and again runs at most (n-j-2) iterations for each j. But this time, the check involves a

Overall, the time complexity of the code is $O(n^2)$ due to the nested loops. **Space Complexity**

hash set lookup, which is an 0(1) operation on average. In the worst case, this loop will also contribute to 0(n^2) iterations.

Looking at the nested loops, the first loop runs (n-6) times, where j ranges from 3 to (n-4). The second nested loop runs at most

The space complexity for this function is determined by the space required for: 1. The prefix sum array s, which contains (n+1) integers. This contributes O(n) space complexity.

2. The hash set seen, which in the worst-case scenario could store up to ((n/2)-2) sums (since only sums before j are considered

and j starts at 3). This also contributes O(n) space complexity. Therefore, the overall space complexity of the function is O(n).