590. N-ary Tree Postorder Traversal

**Depth-First Search** 

## **Problem Description**

order in the case of n-ary trees, where N can be any number of children a node can have. N-ary trees differ from regular binary trees as they can have more than two children. In the serialization of such a tree for level order traversal, each set of children is denoted, and then a hull value is used to separate them, indicating the end of one level

The given problem requires us to conduct a postorder traversal on a given n-ary tree and return a list of the values of its nodes. In

postorder traversal, we visit the nodes in a left-right-root order for binary trees, which extends to child1-child2-...-childN-root

and the beginning of another. Intuition

3. When popping from the stack, we add the node's value to the answer list and then push all of its children onto the stack. This push operation is

#### 1. A stack data structure follows last in, first out (LIFO) principle, which can be leveraged to visit nodes in the required postorder. 2. We start by pushing the root node onto the stack.

done in the original children order, which means when we pop them, they will be in reversed order because of the LIFO property of the stack.

To solve this problem, we can utilize a stack to simulate the postorder traversal by considering the following points:

- 4. The traversal continues until the stack is empty.
- 5. After we've traversed all nodes and have our answer list, it will be in root-childN-...-child1 order. To obtain the postorder traversal, we need to reverse this list before returning it. The reversal step is essential to have the nodes in the child1-child2-...-childN-root order.
- By following the described steps, we visit each node's children before visiting the node itself (as per postorder traversal rules) by effectively leveraging the stack's characteristics to traverse the n-ary tree non-recursively. **Solution Approach**

The implementation of the postorder traversal for an n-ary tree is done using a stack to keep track of the nodes. The following steps break down the solution approach:

Initialization:

• Then, we check if the given root is None and immediately return ans if true, as there are no nodes to traverse. **Stack** Preparation:

Traversal: We enter a while loop that continues as long as stk is not empty.

fashion.

**Example Walkthrough** 

- Inside the loop, we pop the topmost node from the <u>stack</u> and append its value to list <u>ans</u>. We then iterate over the children of the popped node in their given order and push each onto the stack stk. • Since the stack follows LIFO order, children are appended to the list ans in reverse order with respect to how they were added to the stack.
- Final Step: Upon completion of the while loop (when the stack stk is empty), we have all the node values in ans but in the reverse order of the
- required postorder traversal. ∘ To fix this, we simply reverse ans using ans[::-1] and then return it.

We define a list named ans to store the postorder traversal.

We initialize a stack named stk and push the root node into it.

- By using this approach, we avoid recursion, which can be helpful in environments where the call stack size is limited. The use of a stack allows us to control the processing order of nodes, thereby enabling the simulation of post-order traversal in an iterative
- Let's illustrate the solution approach with a simple n-ary tree example:

In this tree, node 1 is the root, node 2 has one child 5, node 3 has no children, node 4 has two children 6 and 7.

#### Initialization: Define a list ans to store the postorder traversal.

Following the solution steps:

**Stack Preparation:** 

 Initialize a stack stk and push the root node 1 onto it. Traversal:

• Pop node 5 from stk, add its value to ans. No children to add here.

• Pop node 3 from stk, add its value to ans. No children to add here.

Pop node 7 from stk, add its value to ans. No children to add here.

Pop node 6 from stk, add its value to ans. No children to add here.

Pop node 4 from stk, add its value to ans, and push its children (7, 6) onto the stack.

Check if the root is None. If it is, return ans.

 Start the while loop since stk is not empty. • Pop the topmost node from stk, which is node 1. Add its value to list ans. • Push the children of node 1 (4, 3, 2) onto the stack. Note: Push in reverse order of the children as stated in the Intuition, so node 2 is on top. • Pop node 2 from stk, add its value to ans, and push its child onto the stack (5).

Final Step:

2, 6, 7, 4, 3, 1].

**Python** 

class Node:

Solution Implementation

postorder\_result = []

if root is None:

stack = [root]

• At this point, ans is in reverse order of the required post-order traversal: [1, 4, 7, 6, 3, 2, 5]. • Reverse ans to get the correct postorder traversal: [5, 2, 6, 7, 4, 3, 1]. Return the reversed list.

Now the stk is empty, exit the while loop.

def postorder(self, root: 'Node') -> list[int]:

# Stack to keep track of nodes to visit

return postorder\_result

current\_node = stack.pop()

stack.append(child)

public List<Integer> postorder(Node root) {

# List to store the postorder traversal result

# If the tree is empty, return an empty list

# Add the current node's value to the traversal result

# Push all children of the current node to the stack

postorder\_result.append(current\_node.val)

for child in current node.children:

import java.util.Deque; // Import the Deque interface

import java.util.LinkedList; // Import the LinkedList class

// If the root is null, return an empty list

stack.offerLast(root); // Start with the root node

Node current = stack.pollLast(); // Get the last node

// Iterate through children of the current node

// While there are nodes in the stack

for (Node child : current.children) {

def init (self, val=None, children=None): self.val = val self.children = children if children is not None else [] class Solution:

So using the stated steps, we successfully performed an iterative postorder traversal on the n-ary tree and the final output is [5,

# Continue processing nodes until stack is empty while stack: # Pop a node from the stack

# Note: We push children in the order as they are in the list so that they are processed

# in reverse order when popped (because stack is LIFO), which is needed for postorder.

LinkedList<Integer> result = new LinkedList<>(); // Use 'result' instead of 'ans' for clarity

result.addFirst(current.val); // Add the node value to the front of the result list (for postorder)

Deque<Node> stack = new ArrayDeque<>(); // Use 'stack' to represent the deque of nodes

stack.offerLast(child); // Add each child to the stack for processing

# Return the result reversed, as we need to process children before their parent

# This reverse operation gives us the correct order of postorder traversal

// Import the List interface

### return postorder\_result[::-1] Java

import java.util.List;

if (root == null) {

return result;

while (!stack.isEmptv()) {

std::vector<int> postorder(Node\* root) {

std::stack<Node\*> stack;

while (!stack.empty()) {

stack.pop();

root = stack.top();

stack.push(root);

std::vector<int> postorderTraversal;

if (!root) return postorderTraversal;

// Loop until the stack is empty.

// Return empty vector if the root is null.

// Get the top node from the stack.

postorderTraversal.push\_back(root->val);

for (Node\* child : root->children) {

\* Post-order traversal function which returns an array of values.

// An array to store the result of the post-order traversal

\* Post-order traversal means visiting the child nodes before the parent node.

\* @param root - The root node of the tree or null if the tree is empty.

stack.push(child);

// Return the postorder traversal.

\* @returns An array of node values in post-order.

function postorder(root: INode | null): number[] {

const result: number[] = [];

return postorderTraversal;

children: INode[];

// Use a stack to hold the nodes during traversal.

// Initialize an empty vector to store the postorder traversal.

// Append the node's value to the traversal vector.

// Push all children of the current node to the stack.

// the postorder by reversing the relation at the end.

// Reverse the order of the nodes to get the correct postorder.

std::reverse(postorderTraversal.begin(), postorderTraversal.end());

// We traverse from left to right, the stack is LIFO, so we need to reverse

class Solution {

```
return result; // Return the populated list as the result
// Definition for a Node.
class Node {
   public int val;
    public List<Node> children;
   // Constructors
    public Node() {}
   public Node(int _val) {
       val = _val;
   public Node(int _val, List<Node> _children) {
       val = val;
       children = _children;
#include <vector>
#include <stack>
#include <algorithm>
// Definition for a Node.
class Node {
public:
   int val:
   std::vector<Node*> children;
   Node() {}
   Node(int value) {
       val = value;
   Node(int value, std::vector<Node*> childNodes) {
       val = value;
       children = childNodes;
};
class Solution {
public:
```

#### **TypeScript** // Definition for the Node class. (Do not create a Node class since the instruction is to define everything globally) interface INode { val: number;

**}**;

```
/**
     * Helper function for depth-first search post-order traversal of the node tree.
     * It recursively visits children first before the parent node then pushes the value to the result array.
     * @param node - The current node being visited.
     */
    const depthFirstSearchPostOrder = (node: INode | null) => {
        if (node == null) {
            // If the node is null, i.e., either the tree is empty or we've reached the end of a branch, return
            return;
        // Loop through each child of the current node and recursively perform a post-order traversal
        for (const childNode of node.children) {
            depthFirstSearchPostOrder(childNode);
        // After visiting the children, push the current node's value to the result array
        result.push(node.val);
   };
    // Initiate the post-order traversal from the root of the tree
    depthFirstSearchPostOrder(root);
    // Return the result of the traversal
    return result;
class Node:
   def init (self, val=None, children=None):
        self.val = val
        self.children = children if children is not None else []
class Solution:
    def postorder(self, root: 'Node') -> list[int]:
       # List to store the postorder traversal result
        postorder_result = []
       # If the tree is empty, return an empty list
       if root is None:
            return postorder_result
```

# **Time and Space Complexity**

stack = [root]

while stack:

# Stack to keep track of nodes to visit

# Pop a node from the stack

current\_node = stack.pop()

stack.append(child)

total space complexity remains O(N).

return postorder\_result[::-1]

# Continue processing nodes until stack is empty

postorder\_result.append(current\_node.val)

for child in current node.children:

# Add the current node's value to the traversal result

# Push all children of the current node to the stack

nodes, and let C be the maximum number of children a node can have. In the worst case, every node will be pushed and popped from the stack once, and all of its children (up to C children) will be processed. Therefore, the time complexity is O(N \* C). However, since every node is visited once, and C is a constant factor, the time complexity simplifies to O(N).

Time Complexity: Each node is visited exactly once, and all its children are added to the stack. Assuming the tree has N

The given code implements a post-order traversal of an n-ary tree iteratively using a stack. Analyzing the complexity:

# Note: We push children in the order as they are in the list so that they are processed

# in reverse order when popped (because stack is LIFO), which is needed for postorder.

# Return the result reversed, as we need to process children before their parent

# This reverse operation gives us the correct order of postorder traversal

- Space Complexity: The space complexity is determined by the size of the stack and the output list. In the worst case, if the tree is imbalanced, the stack could hold all nodes in one of its branches. Therefore, the space complexity is O(N) for storing the N nodes in the worst-case scenario. The list ans also stores N node values. Hence, when considering the output list, the

Therefore, the overall time complexity of the code is O(N) and the space complexity is O(N).