1556. Thousand Separator

Easy String

Problem Description

The given problem requires us to take an integer `n` and format it as a string that represents the number with a dot `.` inserted every three digits from the right. This is commonly known as adding a "thousand separator." For example, if `n` is `123456789`, the output should be `"123.456.789"`. If `n` is less than 1000, it should be returned without change, since there are no thousands to separate.

Intuition

To solve this problem, one intuitive approach is to process the integer digit by digit from right to left (least significant digit to most significant digit). We can achieve that by continuously dividing the number by 10 and getting the remainder, which represents the current rightmost digit.

Each time we extract a digit, we append it to a result list. We also need to keep a count of how many digits we've added so that we know when to insert a dot. For this problem, we insert a dot every three digits. When there are no more digits left (i.e., the remaining number is 0), we stop the process. Finally, we reverse the result list since we built the number from right to left, join the elements to form a string, and return the formatted number.

Here are the specific steps of the process:

1. Initialize a count `cnt` to 0. This will keep track of the number of digits processed.
2. Initialize an empty list `ans` to build the answer from individual digits and dots.
3. Enter a loop that will run until there are no more digits to process in the number `n`. Within the loop:
    - Divide `n` by 10, separate the quotient and the remainder. The remainder is the current digit to add to the answer, while the quotient is the reduced number for the next iteration.
    - Convert the remainder to a string and append it to `ans`.
    - Increment the count `cnt`.
    - If `cnt` is equal to 3 and there are still digits in `n` (i.e., `n` is not 0), append a `.` to `ans` and reset `cnt` to 0.
4. Break the loop when `n` is reduced to 0.
5. Reverse the list `ans` since we built it backwards.
6. Join the elements in `ans` to form the final string.
7. Return the resulting string.

Solution Approach

The solution to this problem involves a straightforward implementation of the intuition described. The solution uses simple arithmetic operations and a list as the primary data structure to build the answer. No particular algorithmic pattern is necessary other than following this numeric processing method:

1. The solution class `Solution` contains the method `thousandSeparator`, which takes an integer `n` as an argument and returns a string with the formatted number.
2. A counter `cnt` is initialized to 0. This counter is used to track the number of digits added to the answer list `ans` since the last dot was added (or since the beginning if no dot has been added yet).
3. An empty list `ans` is created to accumulate the digits and dots in reverse order, as we will be processing the digits from least significant to most significant.
4. The while loop `while 1:` ensures that the loop continues until explicitly broken.
5. Inside the loop, `n, v = divmod(n, 10)` divides `n` by 10, storing the quotient back in `n` for the next iteration and the remainder in `v`. The remainder represents the current least significant digit to be added to the `ans` list.
6. `ans.append(str(v))` adds the current digit to the answer list as a string, since we want the final output to be a string.
7. The counter `cnt` is incremented by 1 each time a digit is added to `ans`.
8. A conditional `if n == 0:` checks whether the number `n` has been fully processed. If `n` is 0, the loop is terminated by executing a `break`.
9. Another conditional `if cnt == 3:` checks if three digits have been added to `ans` since the last dot or since the start. If true, a dot `'.'` is appended to `ans`, and `cnt` is reset to 0 to count the next three digits.
10. Once the loop is broken, `return ''.join(ans[::-1])` is executed. This joins the elements of `ans` together into a string, and `ans[::-1]` reverses the list since we built the number from the least significant digit to the most significant.

By maintaining a counter and using the divmod function to split the integer into digits, the approach avoids string-to-integer conversions except when appending digits to the answer list. The use of a list to construct the answer in reverse order helps efficiently build the result since lists in Python have a time complexity of O(1) for typical append operations. Once the number is fully converted into a list of characters, the reversal and join operations form the final string to be returned.

Example Walkthrough

Let's walk through the solution with a small example. Supposing the input integer `n` is `12345`. We need to format it as a string with a dot inserted every three digits from the right. So, our expected output is `"12.345"`.

Here are the steps demonstrating how the algorithm would process this input:

1. Initialize the counter `cnt` to 0 and the list `ans` to an empty list.
2. Enter the loop since `n` is non-zero.
3. In the first iteration, `divmod(n, 10)` gives us `n = 1234` and `v = 5`. We append `'5'` to `ans` and increment `cnt` by 1.
4. In the second iteration, now `n = 123` and `v = 4`. We append `'4'` to `ans` and increment `cnt` by 1.
5. In the third iteration, `n = 12` and `v = 3`. We append `'3'` to `ans`. `cnt` is now 3, so we append a `'.'` to `ans` and reset `cnt` to 0.
6. In the fourth iteration, `n = 1` and `v = 2`. We append `'2'` to `ans` and increment `cnt` by 1.
7. In the fifth iteration, `n = 0` and `v = 1`. We append `'1'` to `ans`. Since `n` is now 0, we break out of the loop.
8. Now `ans` is `['5', '4', '3', '.', '2', '1']`. We need to reverse the list to get the digits in the correct order.
9. After reversing, `ans` is `['1', '2', '.', '3', '4', '5']`.
10. Joining the elements in `ans` with `''`, we get the final result `"12.345"`.
11. We return the resulting string `"12.345"`.

Note: If `n` had been smaller than 1000, say `n = 12`, the process would be the same without the insertion of a dot, resulting in `"12"`.

Solution Implementation

Python

```python
class Solution:
    def thousandSeparator(self, value: int) -> str:
        # Initialize a counter to track the number of digits processed
        digit_counter = 0

        # Initialize a list to build the answer incrementally
        result_parts = []

        # Loop until the entire number has been processed
        while True:
            # Divide the number by 10 to get the next digit and the remainder
            value, remainder = divmod(value, 10)

            # Convert the remainder (a digit) to a string and append to the list
            result_parts.append(str(remainder))

            # Increment the digit counter
            digit_counter += 1

            # Check if the number has been completely divided
            if value == 0:
                break

            # If three digits have been processed, insert a period and reset counter
            if digit_counter == 3:
                result_parts.append('.')
                digit_counter = 0

        # Since digits are processed in reverse order, reverse the list and join the parts into a string
        formatted_number = ''.join(result_parts[::-1])

        return formatted_number
```

Java

```java
class Solution {
    // This method converts an integer to a string with dot separators for every three digits
    public String thousandSeparator(int number) {
        int count = 0; // Initialize a counter to keep track of every three digits
        StringBuilder formattedNumber = new StringBuilder(); // Use StringBuilder to efficiently manipulate strings

        // Loop until the entire number has been processed
        while (true) {
            int digit = number % 10; // Extract the last digit of the number
            number /= 10; // Remove the last digit from the number
            formattedNumber.append(digit); // Append the digit to the StringBuilder
            count++; // Increment the counter

            // If the number is reduced to zero, break out of the loop
            if (number == 0) {
                break;
            }

            // After every third digit, append a dot to the StringBuilder
            if (count == 3) {
                formattedNumber.append('.');
                count = 0; // Reset the counter after appending the dot
            }
        }

        // Reverse the StringBuilder content to maintain the correct order
        // and convert it to a String before returning
        return formattedNumber.reverse().toString();
    }
}
```

C++

```cpp
class Solution {
public:
    // Function to add a thousand separator in the given integer.
    // It inserts a period '.' every three digits from right to left
    string thousandSeparator(int n) {
        int count = 0;          // Initialize a counter to keep track of the number of digits
        string formattedNumber;  // Initialize an empty string to build the result

        // Proceed to iterate until the entire number has been processed
        do {
            int digit = n % 10;   // Extract the rightmost digit
            n /= 10;              // Remove the rightmost digit from the number
            formattedNumber += to_string(digit); // Append the digit to the result string
            count++;              // Increment the digit counter

            // Insert a period after every third digit from the right, but only if more digits are left to process
            if (count == 3 && n != 0) {
                formattedNumber += '.';
                count = 0;        // Reset the digit counter after inserting a period
            }
        } while (n != 0);         // Continue as long as there are digits left

        // Since the digits were added in reverse order, reverse the string to get the correct format
        reverse(formattedNumber.begin(), formattedNumber.end());

        return formattedNumber;   // Return the properly formatted number
    }
};
```

TypeScript

```typescript
/**
 * Function to add a thousand separator in the given integer.
 * It inserts a period '.' every three digits from right to left.
 * @param {number} n - The number in which the thousand separator must be added.
 * @returns {string} - The number as a string with thousand separators added.
 */
function thousandSeparator(n: number): string {
    let count = 0;          // Initialize a counter to keep track of the number of digits.
    let formattedNumber = '';  // Initialize an empty string to build the result.

    // Proceed to iterate until the entire number has been processed.
    do {
        const digit = n % 10;    // Extract the rightmost digit.
        n = Math.floor(n / 10);  // Remove the rightmost digit from the number.
        formattedNumber += digit.toString(); // Append the digit to the result string.
        count++;                 // Increment the digit counter.

        // Insert a period after every third digit from the right, but only if more digits are left to process.
        if (count === 3 && n !== 0) {
            formattedNumber += '.';
            count = 0;           // Reset the digit counter after inserting a period.
        }
    } while (n !== 0);           // Continue as long as there are digits left.

    // Since the digits were added in reverse order, reverse the string to get the correct format.
    formattedNumber = reverseString(formattedNumber);

    return formattedNumber; // Return the properly formatted number.
}

/**
 * Helper function to reverse a string.
 * @param {string} str - The string to be reversed.
 * @returns {string} - The reversed string.
 */
function reverseString(str: string): string {
    return str.split('').reverse().join('');
}
```

```python
class Solution:
    def thousandSeparator(self, value: int) -> str:
        # Initialize a counter to track the number of digits processed
        digit_counter = 0

        # Initialize a list to build the answer incrementally
        result_parts = []

        # Loop until the entire number has been processed
        while True:
            # Divide the number by 10 to get the next digit and the remainder
            value, remainder = divmod(value, 10)

            # Convert the remainder (a digit) to a string and append to the list
            result_parts.append(str(remainder))

            # Increment the digit counter
            digit_counter += 1

            # Check if the number has been completely divided
            if value == 0:
                break

            # If three digits have been processed, insert a period and reset counter
            if digit_counter == 3:
                result_parts.append('.')
                digit_counter = 0

        # Since digits are processed in reverse order, reverse the list and join the parts into a string
        formatted_number = ''.join(result_parts[::-1])

        return formatted_number
```

Time and Space Complexity

The time complexity of the provided code is $O(d)$, where d is the number of digits in the integer `n`. This is because the while loop runs once for each digit of `n` until `n` becomes `0`, performing a constant amount of work inside the loop for each digit (division, modulo, and counter operations).

The space complexity is also $O(d)$, as the main additional space used is the list `ans` which stores each digit as a character. In the worst case, for every three digits, there is an additional period character, resulting in $d/3$ period characters. Thus, the total space used is proportional to the number of digits d.