370. Range Addition

**Prefix Sum** 

### **Problem Description**

**Medium** Array

In this problem, we are given an integer length which refers to the length of an array initially filled with zeros. We are also given an array of update operations called updates. Each update operation is described as a tuple or list with three integers: [startIdx, endIdx, inc]. For each update operation, we are supposed to add the value inc to each element of the array starting at index startIdx up to and including the index endIdx.

The goal is to apply all the update operations to the array and then return the modified array. For instance, if length = 5 and an update action specifies [1, 3, 2], then after this update, the array will have 2 added to its

1st, 2nd, and 3rd positions (keeping zero-based indexing in mind), resulting in the array [0, 2, 2, 2, 0] after this single operation. After applying all updates, we need to return the final state of the array.

the increments and decrements outlined in the updates.

#### The intuitive brute force approach would be to go through each update and add inc to all elements ranging from startIdx to endIdx for every update in updates. However, this would be time-consuming, especially for a large number of updates or a large

range within the updates. This is where the <u>prefix sum</u> technique comes into play. It is a very efficient way for handling operations that involve adding some value to a range of elements in an array. The main intuition behind prefix sums is that we can record changes at the borders – at

the start index, we begin to add the increment, and just after the end index, we cancel it out. In more detail, for each update [startIdx, endIdx, inc], we add inc to the position startIdx and subtract inc from endIdx + 1. This marks the range where the increment is valid. When we compute the prefix sum of this array, it will apply the inc

increment to all elements since startIdx, and the subtraction at endIdx + 1 will counterbalance it, returning the array to its original state beyond endIdx.

The accumulation step goes through the array and adds each element to the sum of all previous elements, effectively applying

In the presented solution, the Python accumulate function from the itertools module takes care of the accumulation step for

us, summing up the differences and giving us the array after all updates have been applied. Solution Approach

The implementation of this solution is straightforward once we understand the intuition behind using prefix sums. Here's a stepby-step rundown of the algorithm:

We initialize an array d with a length of length filled with zeros. This array will serve as our difference array which records

#### the difference of each position compared to the previous one. We then iterate over each update in the updates array. Each update is in the format [startIdx, endIdx, inc].

complexity.

class Solution:

this is returned as the final result.

d = [0] \* length

d[l] += c

for l, r, c in updates:

Let's illustrate the solution approach with a small example.

4, 3]] which includes two update operations.

Apply the first update [1, 3, 2]:

For each update, we add inc to d[startIdx]. This signifies that from startIdx onwards, we have an increment of inc to be applied.

We then check if endIdx + 1 < length, which is to ensure we do not go out of bounds of the array. If we are still within bounds, we subtract inc from d[endIdx + 1]. This effectively cancels out the previous increment beyond the endIdx.

After processing all updates, d now contains all the changes that are needed to be applied in the form of a difference array.

The returned value from the accumulate function gives us the modified array arr after all updates have been applied, and

Finally, we use the accumulate function of Python to calculate the prefix sum array from the difference array d. This step goes through the array adding each element to the sum of all the previous elements and thus applies the increments tracked

in d at their respective starting indices and cancels them after their respective ending indices.

def getModifiedArray(self, length: int, updates: List[List[int]]) -> List[int]:

the elements. This effectively does the last step of our prefix sum implementation for us.

Add the increment 2 to d[startIdx] which is d[1], so now d = [0, 2, 0, 0].

With all updates applied, the difference array d is: d = [0, 2, 3, 0, 0]

from itertools import accumulate # Import the accumulate function from itertools

def getModifiedArrav(self, length: int, updates: List[List[int]]) -> List[int]:

# Iterate through each update operation described by [start, end, increment]

# Use accumulate to compute the running total, which applies the updates

int startIndex = update[0]; // Start index for the update

int increment = update[2]; // Value to add to the subarray

// apply the negation of increment to the element after the end index

int endIndex = update[1]; // End index for the update

// Convert the 'difference' array into the actual array 'result'

// where each element is the cumulative sum from start to that index

// Return the result — the final array after all updates have been applied

// Define TypeScript Function with specified input types and return type.

\* @param {number} arrayLength - The length of the array to be modified.

// Create an array filled with zeros of the specified length.

const differenceArray = new Array<number>(arrayLength).fill(0);

\* @param {number[1[1] updates - Array containing the updates to be applied.

function getModifiedArray(arrayLength: number, updates: number[][]): number[] {

// Apply the increment to the start index of the difference array.

from itertools import accumulate # Import the accumulate function from itertools

# Initialize the result array with zeros of given length

array. The analysis of the time and space complexity is as follows:

def getModifiedArrav(self, length: int, updates: List[List[int]]) -> List[int]:

# Iterate through each update operation described by [start, end, increment]

# If the end index + 1 is within bounds, apply the negative increment

# This is done to cancel the previous addition beyond the end index

// If the end index + 1 is within the bounds of the array, decrement the value.

// Iterate over the array, adding the previous element's value to each current element,

\* Get the modified array after applying a series of updates.

\* @returns {number[]} - The modified array after all updates.

for (const [startIdx, endIdx, increment] of updates) {

differenceArray[endIdx + 1] -= increment;

differenceArray[i] += differenceArray[i - 1];

// Iterate over each update operation provided.

differenceArray[startIdx] += increment;

if (endIdx + 1 < arrayLength) {</pre>

// effectively applying the range updates.

for start, end, increment in updates:

result[start] += increment

if end + 1 < length:</pre>

# Apply the increment to the start index

result[end + 1] -= increment

for (let i = 1; i < arrayLength; ++i) {</pre>

result = [0] \* length

The final array after applying all updates will be [0, 2, 5, 5, 5].

- This approach effectively reduces the time complexity of the problem, as we only need to make a constant-time update for each range increment, rather than incrementing all elements within the range for each update which could lead to a much higher time
- Here's the mentioned code for the described solution approach that uses these steps: from itertools import accumulate

if r + 1 < length: d[r + 1] -= creturn list(accumulate(d))

In this code example, accumulate is an in-built Python function from the itertools module that computes the cumulative sum of

Consider an array of length = 5 which is initially [0, 0, 0, 0]. Suppose we have the following updates = [[1, 3, 2], [2,

Initialize the difference array d which is the same size as our initial array: d = [0, 0, 0, 0, 0]

## Apply the second update [2, 4, 3]:

operations.

class Solution:

result = [0] \* length

for start, end, increment in updates:

result[start] += increment

return list(accumulate(result))

unchanged here.

**Example Walkthrough** 

 Add the increment 3 to d[startIdx] which is d[2], now d = [0, 2, 3, 0, 0]. • Subtract the increment 3 from d[endIdx + 1] which is not applicable here as endIdx + 1 equals 5 which is out of bounds, hence no subtraction is done.

Now use the accumulate function to calculate the prefix sum array from the difference array d: Final array =

This example confirms that the prefix sum technique updates the initial zero-filled array efficiently with the given range update

• Subtract the increment 2 from d[endIdx + 1] which is d[4], but d[4] is out of bounds for the first update's end index, so d remains

- list(accumulate(d)) = [0, 2, 5, 5, 5]
- **Solution Implementation Python**

# If the end index + 1 is within bounds, apply the negative increment # This is done to cancel the previous addition beyond the end index if end + 1 < length:</pre> result[end + 1] -= increment

# Apply the increment to the start index

# print(sol.getModifiedArray(5, [[1,3,2],[2,4,3],[0,2,-2]]))

// Apply each update in the updates array

// Apply increment to the start index

// If the end index is not the last element,

difference[endIndex + 1] -= increment;

difference[startIndex] += increment;

if (endIndex + 1 < length) {</pre>

for (int i = 1; i < length; i++) {</pre>

difference[i] += difference[i - 1];

for (int[] update : updates) {

# Initialize the result array with zeros of given length

```
class Solution {
   // Method to compute the modified array after a sequence of updates
   public int[] getModifiedArray(int length, int[][] updates) {
       // Create an array 'difference' initialized to zero, with the given length
       int[] difference = new int[length];
```

Java

# Example usage:

# sol = Solution()

```
// Return the resultant modified array
        return difference;
C++
#include <vector>
class Solution {
public:
    // Function to calculate the modified array based on intervals of updates
    std::vector<int> getModifiedArray(int length, std::vector<std::vector<int>>& updates) {
        // Initialize the difference array with zeros
        std::vector<int> diff_array(length, 0);
        // Iterate through each update operation represented by a triplet [startIdx, endIdx, inc]
        for (auto& update : updates) 
            int start idx = update[0]; // Starting index for the update
            int end idx = update[1]; // Ending index for the update
            int increment = update[2]; // Increment value to be added
            // Apply the increment to the start index in the difference array
            diff_array[start_idx] += increment;
            // Apply the negative increment to the position after the end index if in bounds
            // This marks the end of the increment segment
            if (end idx + 1 < length) {
                diff_array[end_idx + 1] -= increment;
        // Iterate through the difference array to compute the final values
        // by adding the current value to the cumulative sum
        for (int i = 1; i < length; ++i) {</pre>
            diff_array[i] += diff_array[i - 1];
```

```
// Return the modified array with all updates applied.
return differenceArray;
```

class Solution:

return diff\_array;

**}**;

**TypeScript** 

```
# Use accumulate to compute the running total, which applies the updates
       return list(accumulate(result))
# Example usage:
# sol = Solution()
# print(sol.getModifiedArray(5, [[1,3,2],[2,4,3],[0,2,-2]]))
Time and Space Complexity
```

# end index (or one past the end index).

• The algorithm iterates over the updates list once. If there are k updates given, this part of the algorithm has a time complexity of O(k). • Each update operation itself is constant time (i.e., 0(1)), since it only involves updating two elements in the d array: the start index and the

The given Python code utilizes the prefix sum (accumulation) strategy to compute the results of multiple range updates on an

• After applying all updates, the algorithm uses accumulate from the itertools module to compute the prefix sums over the entire d array. Computing the prefix sum of an array of length n is an O(n) operation.

**Time Complexity:** 

**Space Complexity:** • The space complexity of the algorithm is primarily determined by the d array, which holds the prefix sum and has a length equal to the input length. Therefore, it is O(n), where n is the length of the result array. • The updates list does not count towards the extra space since it is part of the input.

All other operations use constant space, meaning they do not depend on the size of the input, hence do not significantly contribute to the

space complexity. Therefore, the space complexity is O(n).

Combining the two parts, the overall time complexity of the algorithm is 0(k + n).

In conclusion, the given algorithm has a time complexity of 0(k + n) and a space complexity of 0(n).