235. Lowest Common Ancestor of a Binary Search Tree

Binary Search Tree

Problem Description

Depth-First Search

Tree

In this problem, we are given a binary search tree (BST). Our task is to find the lowest common ancestor (LCA) of two given nodes, p and q, within this BST. The lowest common ancestor is the furthest node from the root that is an ancestor of both nodes. This means that the LCA is the node from which both p and q are descended, and it could be either of the nodes themselves if one is an ancestor of the other.

Binary Tree

Leetcode Link

Intuition

Medium

The intuition behind the solution stems from the properties of a BST. In a BST, for any node n, all nodes in the left subtree of n have values less than n, and all nodes in the right subtree have values greater than n. When searching for the LCA of p and q, there are three possibilities:

- 1. The values of both p and q are less than the value of the current node. This means the LCA must be in the left subtree.
- 2. The values of both p and q are greater than the value of the current node. This means the LCA must be in the right subtree. 3. One value is less than the current node's value and the other is greater (or one of them is equal to the current node's value). This
- means that the current node is the LCA because p and q are in different subtrees.

The given solution iterates over the tree without using recursion. It repeatedly compares the current node's value with p and q values

to determine the direction of the search or to conclude that the current node is the LCA.

In the provided solution, the algorithm uses iteration to navigate through the tree and find the LCA. It does so without the need for

Solution Approach

additional data structures, which keeps the space complexity at a constant O(1). There is also no recursion involved, which means the solution does not rely on the call stack and thus does not incur extra space cost due to recursion stack frames. The algorithm can be broken down into the following steps:

1. Start with the root of the BST as the current node.

- 2. Compare the values of the current node (root.val) with the values of p and q.
- 3. If both p and q have values less than root. val, the LCA must be in the left subtree. Therefore, update the current node to be
- root.left and continue the search. 4. If both p and q have values greater than root, val, the LCA must be in the right subtree. Therefore, update the current node to be
- root.right and continue the search. 5. If the value of p is less than root, val and the value of q is greater than root, val, or vice versa, this implies that p and q lie in different subtrees of the current node. Thus, the current node must be their LCA.
- 6. In a case where either p or q is equivalent to root.val, it means that either p or q is the LCA itself, as it is an ancestor of the other node (a node to be a descendant of itself).
- The algorithm continues the iteration until the condition in step 5 or 6 is met. Once either condition is met, it returns the current

Here's a breakdown of the code:

if root.val < min(p.val, q.val): # Check if both nodes are in the right subtree root = root.right

node, which is the LCA.

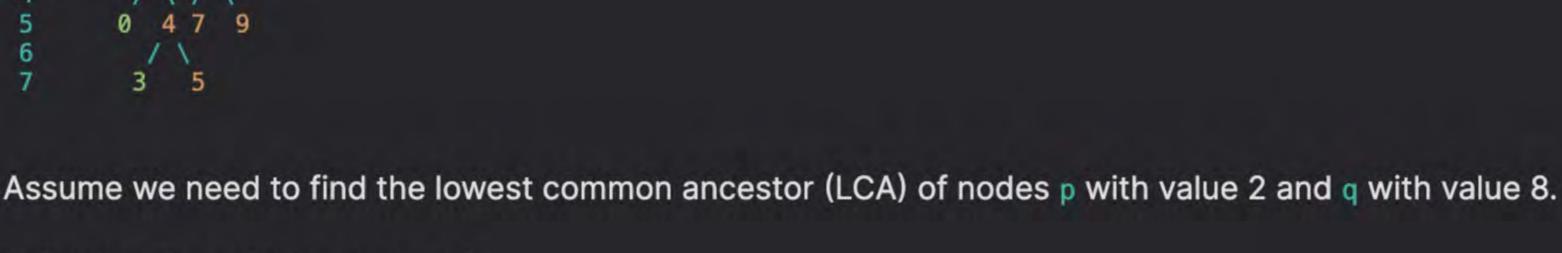
```
elif root.val > max(p.val, q.val): # Check if both nodes are in the left subtree
           root = root.left
       else:
           return root # Found the LCA or one of the nodes is the LCA itself
The loop will always terminate because of the BST property which ensures that, with each step, the current node is moving closer to
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while 1: # Start an indefinite loop that will break once LCA is found

Example Walkthrough

the LCA until it is found.

Let's consider a binary search tree (BST) for our example:



We start with the root of the BST, which has a value of 6.

o p.val is 2 and q.val is 8.

subtree of node 6.

Following the solution approach:

- 3. Since 6 is greater than 2 and less than 8, it is neither solely in the left subtree nor in the right subtree relative to both p and q.
- Therefore, we have found the condition from step 5: p and q lie in different subtrees of the current node. 4. According to the algorithm, we have found the LCA because one node is in the left subtree and the other node is in the right

2. We compare the values of p and q to the current node (root), which is 6.

So, the lowest common ancestor of nodes 2 and 8 in this BST is the node with the value 6. The search stops here and we return the

current node (root) as the LCA.

Definition for a binary tree node. class TreeNode: def __init__(self, val):

self.right = None

class Solution:

self.val = val

TreeNode(int value) {

while (root != null) {

val = value;

class Solution {

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11 }

self.left = None

Python Solution

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def lowestCommonAncestor(self, root: 'TreeNode', p: 'TreeNode', q: 'TreeNode') -> 'TreeNode':
           # Loop indefinitely until the lowest common ancestor is found
           while True:
12
               # Find the smaller and larger values of p and q
               smaller_value = min(p.val, q.val)
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               larger_value = max(p.val, q.val)
16
17
               # If both p and q are on the right of the current node, move right
               if root.val < smaller_value:</pre>
18
                   root = root.right
19
               # If both p and q are on the left of the current node, move left
20
               elif root.val > larger_value:
21
22
                   root = root.left
               # If we are in a position where p and q are on different sides
23
               # of root, or one of them is equal to root, then root is the LCA
24
               else:
25
26
                   return root
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Java Solution
  // Definition for a binary tree node.
   class TreeNode {
       int val;
       TreeNode left;
       TreeNode right;
 6
       // Constructor to create a new node with a given value
```

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if (root.val < Math.min(firstNode.val, secondNode.val)) {</pre>
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                    root = root.right; // Move to the right child
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23
               // If both nodes are less than current node, search in left subtree
24
               else if (root.val > Math.max(firstNode.val, secondNode.val)) {
                    root = root.left; // Move to the left child
25
26
               // We've found the lowest common ancestor node
               else {
29
                    return root;
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32
           // In case the while loop exits without returning (it shouldn't in proper usage), return null
33
           return null;
34
35 }
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C++ Solution
    * Definition for a binary tree node.
    * struct TreeNode {
          int value;
          TreeNode *left;
          TreeNode *right;
          TreeNode(int x) : value(x), left(nullptr), right(nullptr) {}
    * };
    */
11 class Solution {
12 public:
       // Function to find the lowest common ancestor in a binary search tree.
13
       TreeNode* lowestCommonAncestor(TreeNode* root, TreeNode* p, TreeNode* q) {
14
           // Loop until the lowest common ancestor is found.
```

// If both p and q are greater than root, then LCA must be in the right subtree.

// If both p and q are less than root, then LCA must be on the left subtree.

// If we are in a state where p and q are on different sides of the root,

if (root->value < min(p->value, q->value)) {

else if (root->value > max(p->value, q->value)) {

// or one of them is the root itself, we've found the LCA.

root = root->right;

root = root->left;

// Function to find the lowest common ancestor of two nodes in a binary search tree

// If both nodes are greater than current node, search in right subtree

// Traverse the tree starting with the root

public TreeNode lowestCommonAncestor(TreeNode root, TreeNode firstNode, TreeNode secondNode) {

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while (true) {

else {

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                   return root;
32 };
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Typescript Solution
   // Definition of the binary tree node class interface to illustrate the structure of nodes in the binary tree.
   interface ITreeNode {
       val: number;
       left: ITreeNode | null;
       right: ITreeNode | null;
 6 }
    * Finds the lowest common ancestor (LCA) of two nodes in a binary search tree.
    * @param root The root node of the binary search tree.
    * @param nodeP The first node to find the LCA for.
    * @param nodeQ The second node to find the LCA for.
    * @returns The lowest common ancestor of nodeP and nodeQ.
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    */
   function lowestCommonAncestor(root: ITreeNode | null, nodeP: ITreeNode | null, nodeQ: ITreeNode | null): ITreeNode | null {
       // Continue searching for the LCA as long as the current root is not null.
       while (root) {
18
           // If both nodes are smaller than the current root, LCA must be in the left subtree.
           if (root.val > nodeP.val && root.val > nodeQ.val) {
               root = root.left:
           // If both nodes are larger than the current root, LCA must be in the right subtree.
           } else if (root.val < nodeP.val && root.val < nodeQ.val) {
               root = root.right;
           // If we are in a situation where one node is on the left and the other is on the right,
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23 24 25 // or one of the nodes is equal to the root, the current root is the LCA. 26 } else { 28 return root; 29 30 31 32 // If the root is null, it means we haven't found the LCA (which should not happen in a valid BST with both nodes present). 33 return null; 34 } 35

Time and Space Complexity The time complexity of the given code is O(H), where H is the height of the binary tree. This is because the code traverses the tree

nodes. The space complexity of the code is 0(1) regardless of the tree's structure, because it uses a fixed amount of space for pointers and

from the root to the lowest common ancestor (LCA) without visiting any nodes more than once. In the worst case scenario, when the

binary tree is unbalanced, the height H could be linear in respect to the number of nodes, N, resulting in a time complexity of O(N).

However, in a balanced tree, time complexity is O(log N) since the height of the tree is logarithmic in respect to the number of

without any recursive calls or additional data structures that depend on the size of the tree.