1497. Check If Array Pairs Are Divisible by k





Problem Description



Medium Array Counting **Leetcode Link**

The problem presents an array of integers arr with an even number of elements n and an integer k. The task is to determine whether arr can be partitioned into n/2 pairs, where the sum of the integers in each pair is divisible by k. If such a partitioning is possible, the function should return true; otherwise, it should return false.

Intuition

that (a + b) % k == 0. In other words, the remainder when a + b is divided by k is 0. For any integer x, x % k will give a remainder in the range [0, k-1]. If x % k is 0, then x is divisible by k. To make a pair with a sum

The solution is built on the property of divisibility by an integer k. If two numbers a and b have a sum that is divisible by k, it means

divisible by k, each number x in the array that has a non-zero remainder x % k requires a corresponding number y such that (x + y) % k == 0. We can think of the remainders as forming pairs themselves. For a non-zero remainder i, there must be an equal number of elements

with remainder k - i. To arrive at the solution, we use a counter to track the frequency of each remainder in the array. We then check two conditions:

1. The count of elements with a remainder of 0 must be even because they can only be paired with other elements with a remainder of 0.

- 2. For each non-zero remainder i, there should be an equal count of elements with remainder i and k i.
- If both these conditions are met, the array can be rearranged into n/2 pairs, where the sum of each pair is divisible by k.

The implementation of the solution involves using the Counter class from Python's collections module to efficiently count the

Solution Approach

occurrences of each remainder when elements of the array are divided by k. The Counter object will map each unique remainder to the number of times it appears in the array.

in arr].

Here's a step-by-step walkthrough of the solution: 1. Calculate the remainder of each element in the array when divided by k. This is done using a list comprehension: [x % k for x

3. Verify the first condition for elements with zero remainders: o cnt[0] % 2 == 0. This checks if the count of elements that are exactly divisible by k is even. These elements can only be

∘ Loop through the range from 1 to k − 1 and for each i, check if the count of elements with a remainder of i is equal to the

• The all function ensures that this condition must hold true for all remainders in the specified range for the function to return

paired with themselves, so an odd count would make it impossible to form pairs where the sum is divisible by k. 4. Verify the second condition for elements with non-zero remainders:

2. Feed this list of remainders into Counter to get the frequency count of each remainder: Counter(x % k for x in arr).

- count of elements with a remainder of k i. This check is performed by the list comprehension: all(cnt[i] == cnt[k - i] for i in range(1, k)).
- true.
- The use of the Counter and the all function makes the algorithm efficient and concise. The time complexity of this algorithm is primarily dependent on the time it takes to traverse the array and calculate the remainders, which is (O(n)), and the time to check the pair frequencies, which is (O(k)). This makes the overall time complexity (O(n + k)).

1 class Solution: def canArrange(self, arr: List[int], k: int) -> bool: cnt = Counter(x % k for x in arr) return cnt[0] % 2 == 0 and all(cnt[i] == cnt[k - i] for i in range(1, k))

By adhering to these steps, the algorithm efficiently solves the problem while respecting the constraints of even length arrays and

Here's the relevant snippet from the Python solution for reference:

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Example Walkthrough
Let's illustrate the solution approach with a small example:
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1. Calculate the remainders of each element when divided by k = 3:

Suppose we have an array arr = [2, 4, 1, 5] and an integer k = 3. We need to check if we can partition this array into pairs such

that the sum of each pair is divisible by k. Since there are 4 elements in arr, we are looking for n/2 = 2 pairs.

 \circ 5 % 3 = 2 The remainders are [2, 1, 1, 2]. 2. Count the frequency of each remainder using the Counter:

0 2 % 3 = 2

0 4 % 3 = 1

0 1 % 3 = 1

Following the solution steps:

the divisibility requirement.

 Remainder 1 appears 2 times. Remainder 2 appears 2 times.

4. Verify the second condition for elements with non-zero remainders:

3. Verify the first condition for elements with zero remainders:

 \circ Check each i from 1 to k - 1, which in this case is just 1 and 2 since k = 3.

 \circ For i = 1: Count is 2.

from collections import Counter

def canArrange(arr: List[int], k: int) -> bool:

cnt = Counter(x % k for x in arr)

13 # Call the function with the example inputs

return False

return True

Java Solution

class Solution {

All checks have passed, hence return True

public boolean canArrange(int[] arr, int k) {

count[(number % k + k) % k]++;

if (count[i] != count[k - i]) {

int[] count = new int[k];

for (int number : arr) {

for (int i = 1; i < k; ++i) {

return false;

// Create an array to store counts of modulo results

// Check pairs for each possible modulo result except for 0

// is an even number since they need to be paired among themselves

// Loop through each number in the input array

14 print(canArrange(arr, k)) # Output: True

algorithm's correctness in this scenario.

- \circ For k i = 3 1 = 2: Count is 2. \circ Since the counts are equal for **i** and **k** - **i**, the condition is met.
- Since the array only has non-zero remainders and each remainder i has an equal count to k i, we have successfully verified that it is possible to partition the array into n/2 pairs where the sum of each pair is divisible by k. Thus, the function would return true.

Our example does not have any element with a remainder of 0, so we can skip this.

The corresponding Python function would process the information as follows:

Since there is no remainder of 0, we skip checking cnt[0] % 2

return all(cnt[i] == cnt[k - i] for i in range(1, k))

Validate the second condition using a list comprehension and all()

9 # Example array and k 10 arr = [2, 4, 1, 5]11 k = 312

By adhering to the solution steps, we are given a working example of the algorithm applied to this simple array, confirming the

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Python Solution
   from collections import Counter
   class Solution:
       def canArrange(self, arr: List[int], k: int) -> bool:
           # Count the frequency of each remainder when each element in arr is divided by k
           remainder_count = Counter(x % k for x in arr)
           # Check if the number of elements that are divisible by k is even
           if remainder_count[0] % 2 != 0:
               return False
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           # Check if each non-zero remainder has a complementary count of elements
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           # Such that remainder + complementary = k
           # The counts of remainder and its complementary need to be the same
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           for remainder in range(1, k):
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if remainder_count[remainder] != remainder_count[k - remainder]:

// Increment the count at the index equal to the number's modulo k,

// taking into account negative numbers by adding k before modding

return count[0] % 2 == 0; 25 26 27 } 28

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// This function checks if it's possible to rearrange 'arr' such that the sum of every pair of elements is divisible by 'k'.
       bool canArrange(vector<int>& arr, int k) {
           // Create a count array to store frequencies of mod values
           vector<int> count(k, 0);
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           // Increment the count for each element's mod value with 'k', properly handling negative numbers
           for (int number : arr) {
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               int modValue = ((number % k) + k) % k;
               ++count[modValue];
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           // Check pairs from 1 to k-1. For every 'i', there must be equal number of elements with 'k-i' as mod.
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           for (int i = 1; i < k; ++i) {
               if (count[i] != count[k - i]) {
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                   // If counts are not equal, pairs cannot be formed to satisfy the condition.
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                   return false;
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           // The count of elements evenly divisible by 'k' must be even for them to be paired.
           return count[0] % 2 == 0;
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25 };
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Typescript Solution
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1 // Function checks if it's possible to rearrange 'arr' so that the sum of every pair of elements is divisible by 'k'.

// If counts are not equal, pairs cannot be formed to satisfy the condition.

// The count of elements evenly divisible by 'k' must be even for them to be paired successfully.

// Check pairs from 1 to k-1. For every 'i', there must be an equal number of elements with 'k-i' as their mod value.

24 25 // Example usage: 26 // let result: boolean = canArrange([1, 2, 3, 4, 5, 10, -10], 5);27 // console.log(result); // This should output true or false based on the array and k value.

Time Complexity

length of arr.

Space Complexity

The time complexity of the given code can be analyzed by looking at the operations performed:

function canArrange(arr: number[], k: number): boolean {

let modCount: number[] = new Array(k).fill(0);

if (modCount[i] !== modCount[k - i]) {

// properly handling negative numbers

arr.forEach(number => {

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});

modCount[modValue]++;

for (let i = 1; i < k; i++) {

return false;

return modCount[0] % 2 === 0;

Time and Space Complexity

// Create an array to store frequencies of mod values

let modValue: number = ((number % k) + k) % k;

// Increment the count for each element's mod value with 'k',

- The return statement consists of two parts: Checking if cnt[0] % 2 == 0 is a constant time 0(1) operation because we access a dictionary key and then check for
- \circ The list comprehension all(cnt[i] == cnt[k i] for i in range(1, k)) could iterate up to k times. In the worst case, this is 0(k). However, since there are only 'n' unique modulo results possible (all elements x in arr are used to compute x %
- Based on these observations, the total time complexity is O(n) + O(1) + O(min(n, k)) which simplifies to O(n + min(n, k)). Since n and k are independent variables, we cannot simplify this further without knowing the relationship between n and k.

• The list comprehension x % k for x in arr iterates over each element in arr, resulting in O(n) time complexity, where n is the

• The Counter from the standard collections module constructs the frequency dictionary in once again O(n) time complexity.

evenness.

k), we are effectively iterating up to min(n, k), hence O(min(n, k)).

- The space complexity is determined by the auxiliary space used by the program. In this case:
- The frequency dictionary cnt may contain up to min(n, k) different keys (since these are the unique modulo results) and therefore has a space complexity of O(min(n, k)). • The space complexity for the list comprehension is 0(1) since it's not stored but used directly in the all function.
- Consequently, the space complexity of the whole code is dominated by the space requirement of the frequency dictionary, which is $0(\min(n, k)).$

C++ Solution 1 class Solution { 2 public:

// For a valid pair, count of modulo i should be equal to count of modulo (k - i)

// If they are not equal, the condition is not met, so return false

// Check that count of numbers that are exactly divisible by k (modulo result is 0)