Sorting

**Monotonic Stack** 

**Greedy** Array

### **Problem Description**

You are given an integer array called arr, which contains n elements. Each element in the array is unique and ranges from 0 to n – 1, essentially representing a permutation of these numbers. The goal is to divide this array into several non-overlapping "chunks" (subarrays), sort each of these chunks individually, and then concatenate them back together to form a single sorted array. The task is to find the maximum number of chunks that can be made such that when they are sorted individually and then concatenated, the result is a sorted version of the original array.

#### Intuition

Medium

The intuition behind the solution is based on the property of permutations and how the original array can be split into the maximum number of chunks. Since the array is a permutation of numbers from 0 to n - 1, if all the chunks are individually sorted, then regardless of where the chunks are split, the concatenated chunks will produce a sorted array. To maximize the number of chunks, we need to exploit the fact that if the maximum value in a chunk is equal to its last index, then this chunk can be independently sorted without affecting the <u>sorting</u> of the entire array.

For example, consider we are at index i in the array, and the maximum value encountered so far is mx. If i and mx are equal, it

means all numbers from 0 to i are included in this chunk, so this chunk can be independently sorted. We increment our chunk count (ans) everytime such a condition occurs. The process is repeated as we iterate through the array, resulting in ans incrementing each time a self-contained chunk (where its maximum value matches its last index) is found. This logic ensures we are splitting the array into the largest possible number of valid chunks that, when sorted individually, will form the overall sorted array.

This approach's correctness lies in the fact that for every chunk ending at index i, if the maximum value in that chunk is also i, sorting that chunk will simply place all elements from 0 to i (which are already within the chunk) in their correct sorted position. No other elements outside this chunk are affected, guaranteeing that each such chunk contributes to the overall sorted array.

### The impementation of the solution is straightforward. The steps can be broken down as follows:

**Solution Approach** 

1. We initialize two variables, mx and ans. mx will keep track of the maximum value encountered so far as we iterate through the

- array, and ans will count the number of chunks.

  2. We use a for loop to iterate through each element represented by i and its value v in the arr.
- 3. For every element v in the array, we update mx to be the maximum of mx and v, using the expression max(mx, v). This ensures that mx reflects the highest number among all the elements we've encountered up to the current position.
- 4. We check if the current index i is equal to the maximum value mx we've found so far. If it is, it means we've found a valid chunk all integers from 0 up to the current index i must be contained within this chunk, as the permutation contains every
- integer from 0 to n 1 exactly once. Therefore, we can independently sort this chunk without affecting the overall sorting of the array. When such a condition is met, we increment the ans by 1, indicating we can form one more chunk.

  5. We continue this process for all elements in the arr.

After the loop completes, ans contains the largest number of chunks we can form such that individually sorting these chunks

- and then concatenating them results in a sorted array.
- No additional data structures are needed, and the pattern used is simple iteration with a check for the current index against the current maximum value. This is an efficient solution as it achieves the task with a time complexity of O(n) where n is the length of

arr, as it requires only a single pass through the array. The space complexity is also O(1) since we're not using any additional storage that scales with the input size.

Here is the implemented function:

class Solution:

def maxChunksToSorted(self, arr: List[int]) -> int:

mx = ans = 0
for i, v in enumerate(arr):
 mx = max(mx, v)

```
if i == mx:
    ans += 1
return ans

This function takes the arr as input and returns the maximum number of chunks ans.

Example Walkthrough
```

Let's illustrate the solution approach using a small example array arr: [1, 0, 2, 4, 3]

### 1. Initially, we set mx and ans to 0. mx will track the maximum number we encounter, and ans will count the chunks.

• At i = 0, v = arr[0] = 1; we update mx = max(0, 1) so mx becomes 1. Since i is not equal to mx, we do not increment ans.

- At i = 1, v = arr[1] = 0; we update mx = max(1, 0) so mx stays 1. Now, i is equal to mx, which means all numbers from 0 to 1 are within this chunk. We increment ans to 1.
- At i = 2, v = arr[2] = 2; we update mx = max(1, 2) so mx becomes 2. Again, i equals mx, indicating another chunk. We increment ans to 2.
   At i = 3, v = arr[3] = 4; we update mx = max(2, 4) so mx becomes 4. i is not equal to mx, we do not increment ans.

We begin iterating through arr with a for loop:

- At i = 4, v = arr[4] = 3; we update mx = max(4, 3) so mx stays 4. Now, i equals mx, indicating another valid chunk. We increment ans to 3. Having completed the loop, we find that the array can be split into a maximum of 3 chunks: [1, 0], [2], and [4, 3]. When we sort these subarrays independently and then concatenate them, we get the sorted array: [0, 1, 2, 3, 4].
- confirmed by our walkthrough with the example array.

  Solution Implementation

The final answer ans is 3, which signifies there are 3 chunks that can be individually sorted to result in a fully sorted array. This is

Python \_\_\_\_\_\_

## class Solution: def maxChunksToSorted(self, arr: List[int]) -> int: # Initialize the maximum value found so far and the answer counter

max\_value = 0

chunks count = 0

from typing import List

```
# it means we can form a chunk that, when sorted independently,
            # would still maintain the overall order when merged with adjacent chunks.
            if index == max_value:
                # Thus, we increase the chunks count by 1
                chunks_count += 1
       # Return the total number of chunks we can split the array into
        return chunks_count
Java
class Solution {
    public int maxChunksToSorted(int[] arr) {
        int chunkCount = 0; // Initialize the count of chunks
        int maxSoFar = 0; // Initialize the maximum value found so far in the array
       // Iterate through the array
        for (int index = 0; index < arr.length; ++index) {</pre>
           // Update the maximum value seen so far
           maxSoFar = Math.max(maxSoFar, arr[index]);
```

// If the current index is equal to the maximum value encountered,

// and this position is a valid chunk boundary

return chunkCount; // Return the total number of chunks

// Increment the count of chunks

if (index == maxSoFar) {

if (index == maxElement) {

// Update the current maximum value found.

currentMax = Math.max(arr[i], currentMax);

**}**;

++chunkCount;

// it means all values before this index are smaller or equal to 'index'

# Enumerate over the array to get both index and value

# Update the maximum value found in the array thus far

# If the current index equals the maximum value encountered,

for index, value in enumerate(arr):

max\_value = max(max\_value, value)

```
#include <vector>
#include <algorithm> // For use of the max function

class Solution {
public:
    int maxChunksToSorted(vector<int>& arr) {
        int chunkCount = 0; // Variable to count chunks
        int maxElement = 0; // Variable to store the maximum element found so far

        // Iterate through the vector elements
        for (int index = 0; index < arr.size(); ++index) {
            maxElement = std::max(maxElement, arr[index]); // Update maxElement with the highest between maxElement and the curre</pre>
```

// If the maximum element we've found so far is equal to the index,

// it means all previous elements are ≤ index and can form a chunk

++chunkCount; // Increment the chunk count as we can make a new chunk

```
TypeScript

// Function to determine the maximum number of chunks that the array can be
// split into so that after sorting each chunk individually and then concatenating
// them back in order, the resultant array is sorted.
function maxChunksToSorted(arr: number[]): number {
    const n: number = arr.length; // The length of the input array.
    let answer: number = 0; // The number of chunks that the input array can be split into.
    let currentMax: number = 0; // The maximum value found so far in the array up to the current index.

// Iterate through the array to find chunks.
for (let i: number = 0; i < n; i++) {</pre>
```

// If the current maximum is equal to the index, a sorted chunk is found.

# it means we can form a chunk that, when sorted independently,

# Thus, we increase the chunks count by 1

# Return the total number of chunks we can split the array into

# would still maintain the overall order when merged with adjacent chunks.

return chunkCount; // Return the total number of chunks

```
// the number at index i should be i itself, if the chunks before are correctly placed.
          if (currentMax === i) {
              answer++; // Increment the answer as we can split here.
      // Return the number of sorted chunks possible.
      return answer;
from typing import List
class Solution:
   def maxChunksToSorted(self, arr: List[int]) -> int:
       # Initialize the maximum value found so far and the answer counter
       max_value = 0
        chunks_count = 0
       # Enumerate over the array to get both index and value
        for index, value in enumerate(arr):
            # Update the maximum value found in the array thus far
            max_value = max(max_value, value)
           # If the current index equals the maximum value encountered,
```

// This is based on the property that in a sorted array of distinct numbers ranging from 0 to n-1,

### Time and Space Complexity

return chunks\_count

if index == max\_value:

chunks count += 1

The given code snippet is designed to find the maximum number of chunks a given array can be divided into so that, when each

# chunk is sorted individually, the entire array is sorted. Time Complexity:

The time complexity of the function is determined by the for loop iterating over each element of the array. Since there is only one loop in the function that goes through the array of n elements once, the time complexity is O(n), where n is the size of the array.

### Space Complexity:

The space complexity is determined by the amount of additional memory used by the algorithm. Here, only a fixed number of

variables mx and ans are used regardless of the input size, which means the space complexity is O(1) as they use constant space.