2167. Minimum Time to Remove All Cars Containing Illegal Goods String **Dynamic Programming Leetcode Link** Hard

# **Problem Description**

illegal goods (denoted by '1') or not (denoted by '0'). The goal is to remove all cars with illegal goods in the least amount of time possible. We have three operations that we can use: Removing a car from the left end of the train takes 1 unit of time.

In this problem, we are dealing with a 0-indexed binary string s, where each character represents a train car. A car can either contain

- 2. Removing a car from the right end of the train also takes 1 unit of time.
- 3. Removing a car from any other position takes 2 units of time.
- A car removal operation is directed towards a car containing illegal goods, and we want to know the minimum time required to remove all such cars.

Intuition

# To solve this problem, we use a dynamic programming approach. The intuition lies in breaking down the problem into simpler subproblems:

1. The minimum time to remove all 'bad' cars from the beginning (left side) of the train up to any given position. 2. The minimum time to remove all 'bad' cars from the end (right side) of the train from any given position to the end.

- The goal is to find out the optimal point (or points) where we switch from removing cars from the left to removing cars from the right, or vice versa, to minimize the total time. We solve for two arrays, pre and suf, where pre[i] is the minimum time to remove all cars
- with illegal goods from the first i cars, and suf[i] is the minimum time to remove all cars with illegal goods from position i to the

For pre: • If a car at position i does not contain illegal goods ('0'), then pre[i + 1] = pre[i] since no action is needed. If it does contain illegal goods ('1'), we check if it's cheaper to remove it individually, taking 2 units of time, or remove all the i+1 cars from the left which take i+1 units of time.

For suf:

end.

- If a car at position i does not contain illegal goods ('0'), then suf[i] = suf[i + 1] as no action is needed here too. • If it does contain illegal goods ('1'), we check if it's cheaper to remove it individually, taking 2 units of time, or remove all cars from position i to the end which will take n-i units of time (where n is the total number of cars).

removals at each position. The minimum value from this combination gives us the least amount of time needed to remove all the cars

Finally, we iterate through the arrays pre and suf to find the minimum combined time taking into account both the left and right

containing illegal goods.

**Solution Approach** 

1 for i, c in enumerate(s):

current position to the end).

Example Walkthrough

right, respectively.

presence of illegal goods in a train car.

1 for i in range(n - 1, -1, -1):

- Here's the detailed implementation of the solution step by step:
- The solution implementation uses a dynamic programming approach with two additional arrays pre and suf to keep track of the optimal removal times from the left and from the right, respectively.

1. Initialize the pre and suf arrays with zeros, and set their sizes to one more than the length of the string s. This is done to handle the prefix up to i and suffix from i inclusively, easily without running into array index issues. 2. Iterate through the string s from left to right. If you encounter a '0' (no illegal goods), simply copy the value from the previous

index of pre. This means no additional time is needed to handle this car. If there is a '1' (illegal goods exist), calculate the

cars from the left up to the current position) and store that minimum value in pre[i + 1].

pre[i + 1] = pre[i] if c == '0' else min(pre[i] + 2, i + 1)

suf[i] = suf[i + 1] if s[i] == '0' else min(suf[i + 1] + 2, n - i)

minimum time between the time stored in pre at the previous index plus 2 (removing this particular car) and i + 1 (removing all

3. Similarly, iterate through the string s from right to left to fill in the suf array. You do the mirror operation of what was done with

pre: if a '0' is encountered, carry over the value from the right index of suf. If a '1' is found, calculate the minimum time between the time stored in suf at the next index plus 2 (removing this particular car) and n - i (removing all cars from the

and find the minimum sum of corresponding pairs.

1 return min(a + b for a, b in zip(pre[1:], suf[1:])) In this approach, the dynamic programming pattern helps avoid redundant calculations by building up the solution using previously computed values, and the two-pointer technique is not explicitly used but is conceptually present as the solution involves evaluating the sum of pairs of prefix and suffix solutions.

Let's illustrate the solution approach with a small example. Assume we have a binary string s = "001011" where 1 indicates the

4. Once you have the pre and suf arrays constructed, find the point where the sum of removal times from the left and from the

right is minimal. Iterate through the combined view of pre (excluding the zeroth position) and suf (excluding the last position)

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1. Initialize pre and suf Arrays: First, we initialize pre and suf arrays to store the minimum removal times from the left and from the
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For s having a length of 6, pre and suf will be of length 7.

3. Fill the suf Array: We mirror the above process, but from right to left:

2. Fill the pre Array: Next, we iterate from left to right:

Now, pre = [0, 0, 0, 2, 2, 4, 6].

 $\circ$  For s[1] = '0': suf[1] = suf[2] = 4.

 $\circ$  For s[0] = '0': suf[0] = suf[1] = 4.

(excluding the last index) and find the minimum sum.

 $\circ$  For i = 1: sum is pre[1] + suf[1] = 0 + 4 = 4.

 $\circ$  For i = 2: sum is pre[2] + suf[2] = 0 + 4 = 4.

 $\circ$  For i = 3: sum is pre[3] + suf[3] = 2 + 2 = 4.

 $\circ$  For i = 4: sum is pre[4] + suf[4] = 2 + 2 = 4.

 $\circ$  For i = 5: sum is pre[5] + suf[5] = 4 + 1 = 5.

 $\circ$  For i = 6: sum is pre[6] + suf[6] = 6 + 0 = 6.

for i in range(length -1, -1, -1):

suffix[i] = suffix[i + 1]

suffix[i] = min(suffix[i + 1] + 2, length - i)

if s[i] == '0':

return minimum\_cost

public int minimumTime(String s) {

int length = s.length();

} else {

// Get the length of the input string s

int[] prefixCost = new int[length + 1];

int[] suffixCost = new int[length + 1];

for (int i = length - 1; i >= 0; --i) {

int minimumTotalCost = Integer.MAX\_VALUE;

// Return the minimum total cost calculated

for (int i = 1; i <= length; ++i) {</pre>

return minimumTotalCost;

**if** (s.charAt(i) == '0') {

prefixCost[i + 1] = prefixCost[i];

// Initialize the answer to the maximum possible value

for (int i = 0; i < length; ++i) {</pre>

if (s.charAt(i) == '0') {

else:

Now, suf = [4, 4, 4, 2, 2, 1, 0].

**Python Solution** 

class Solution:

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o For s[1] = '0': pre[2] = pre[1] = 0. • For s[2] = '1': pre[3] = min(pre[2] + 2, 3) = min(0 + 2, 3) = 2 (cheaper to remove this car only). $\circ$  For s[3] = '0': pre[4] = pre[3] = 2.

 $\circ$  For s[4] = '1': pre[5] = min(pre[4] + 2, 5) = min(2 + 2, 5) = 4 (cheaper to remove both bad cars separately).

 $\circ$  For s[5] = '1': pre[6] = min(pre[5] + 2, 6) = min(4 + 2, 6) = 6 (cheaper to remove all cars from the left).

 $\circ$  For s[2] = '1': suf[2] = min(suf[3] + 2, 4) = min(2 + 2, 4) = 4 (either way is the same, so minimal is 4).

4. Find Minimal Combined Time: Lastly, we iterate through the combined view of pre (excluding the zeroth index) and suf

For s[0] = '0': pre[1] = pre[0] = 0 (no illegal goods, so no removal time needed).

- $\circ$  For s[5] = '1': suf[5] = min(suf[6] + 2, 1) = min(0 + 2, 1) = 1 (cheaper to remove cars from the right).  $\circ$  For s[4] = '1': suf[4] = min(suf[5] + 2, 2) = min(1 + 2, 2) = 2.  $\circ$  For s[3] = '0': suf[3] = suf[4] = 2.
- The minimum time from these sums is 4 units of time, so that is the least amount of time required to remove all the cars containing illegal goods. This can be interpreted as removing the first bad car individually and the other two bad cars from the right end of the train.
  - def minimumTime(self, s: str) -> int: # Calculate the length of the string s length = len(s)# Initialize prefix and suffix lists of length + 1 to accommodate edge cases prefix = [0] \* (length + 1)suffix = [0] \* (length + 1)# Calculate the prefix time cost for each position in the string # where cost is minimum of removing '1's by flipping twice each or turning all to '0's up to that point for i, char in enumerate(s): **if** char == '0': # If current character is '0', no additional cost is added prefix[i + 1] = prefix[i] else: # If current character is '1', choose the lesser cost between adding 2 to the previous cost or # flipping all to this position prefix[i + 1] = min(prefix[i] + 2, i + 1)

# Calculate the suffix time cost similarly but in reverse from the end of the string

/\* This method finds the minimum time required to clear a string `s` of obstacles ('1's) \*/

// Create prefix and suffix arrays to store the minimum cost to clear up to that index

// If there is no obstacle, then the cost is the same as the previous

// The cost is either removing this obstacle and all before it (i + 1) or

// Calculate the minimum cost to clear obstacles from the start to each index

prefixCost[i + 1] = Math.min(prefixCost[i] + 2, i + 1);

// Calculate the minimum cost to clear obstacles from the end to each index

// If there is no obstacle, then the cost is the same as the next

// Find the minimum among the sum of prefix and suffix costs at every split point

minimumTotalCost = Math.min(minimumTotalCost, prefixCost[i] + suffixCost[i]);

Java Solution 1 class Solution {

// turning off the previously considered obstacles and turning this one on (prefixCost[i] + 2)

# Find the minimum cost to make the entire string '0's by considering both prefix and suffix costs

minimum\_cost = min(prefix\_cost + suffix\_cost for prefix\_cost, suffix\_cost in zip(prefix[1:], suffix[:-1]))

## suffixCost[i] = suffixCost[i + 1]; 28 } else { 29 30 // The cost is either removing this obstacle and all after it (n - i) or // turning off the subsequently considered obstacles and turning this one on (suffixCost[i + 1] + 2)31 32 suffixCost[i] = Math.min(suffixCost[i + 1] + 2, length - i);

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C++ Solution
  1 class Solution {
    public:
         int minimumTime(string s) {
             int size = s.size(); // Variable to store the size of the input string.
             vector<int> prefix(size + 1); // Vector to store the prefix minimum cost.
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             vector<int> suffix(size + 1); // Vector to store the suffix minimum cost.
  8
             // Calculate prefix minimum cost.
             // Loop through the string and fill the 'prefix' vector with the calculated costs.
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             for (int i = 0; i < size; ++i) {
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                 if (s[i] == '0') {
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                     // If the character is '0', the cost is same as the previous one.
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                     prefix[i + 1] = prefix[i];
                 } else {
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                     // If the character is '1', take the minimum between the cost of flipping this car
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                     // and the chain of cars till now, or just removing all cars including this one.
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                     prefix[i + 1] = min(prefix[i] + 2, i + 1);
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             // Calculate suffix minimum cost similarly, from the end of the string.
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             for (int i = size - 1; i >= 0; --i) {
 24
                 if (s[i] == '0') {
 25
                     // Cost is same as the next one for '0' character.
 26
                     suffix[i] = suffix[i + 1];
 27
                 } else {
                     // Minimum between the cost of flipping this car
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                     // and the chain of cars till now, or just removing all cars including this one.
 30
                     suffix[i] = min(suffix[i + 1] + 2, size - i);
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             int minCost = INT_MAX; // Initialize minimum cost to maximum possible integer value.
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             // Loop to find the minimum total cost by combining prefix and suffix costs.
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             // Iterate through boundaries where prefix and suffix meet.
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             for (int i = 0; i <= size; ++i) {
                 minCost = min(minCost, prefix[i] + suffix[i]);
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             return minCost; // Return the minimum cost calculated.
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    };
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# 19 20 21 // Calculate suffix minimum cost similarly, starting from the end of the string. 22 for (let i = size - 1; i >= 0; --i) { 23 if (s.charAt(i) === '0') {

} else {

} else {

Typescript Solution

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the string.

3 function minimumTime(s: string): number {

for (let i = 0; i < size; ++i) {

if (s.charAt(i) === '0') {

prefix[i + 1] = prefix[i];

suffix[i] = suffix[i + 1];

1 // Define the minimumTime function which calculates the minimum time required

prefix[i + 1] = Math.min(prefix[i] + 2, i + 1);

// Cost is the same as the next one for '0' character.

// the cost of removing all cars including this one.

// Find the minimum total cost by combining prefix and suffix costs.

constant time, hence the first loop takes O(n) time and the second also takes O(n) time.

suffix[i] = Math.min(suffix[i + 1] + 2, size - i);

const size: number = s.length; // Store the size of the input string.

// Calculate prefix minimum cost by iterating over each character in the string.

// If the character is '1', choose the minimum between the cost

// Choose the minimum between the cost of flipping this car and

// If the character is '0', the cost is the same as the previous one.

const prefix: number[] = new Array(size + 1).fill(0); // Array to store the prefix minimum cost.

const suffix: number[] = new Array(size + 1).fill(0); // Array to store the suffix minimum cost.

// of flipping this car and the cost of removing all cars including this one.

2 // to remove or flip cars represented by a string of '0's and '1's.

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// Iterate through the possible boundaries where prefix and suffix meet.
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 37
         for (let i = 0; i <= size; ++i) {
 38
             minCost = Math.min(minCost, prefix[i] + suffix[i]);
 39
 40
         return minCost; // Return the minimum cost calculated.
 41
 42 }
 43
    // Example usage:
 45 // const result: number = minimumTime("0010");
    // console.log(result); // Outputs the minimum time required to remove or flip cars.
Time and Space Complexity
The time complexity of the provided code is O(n), where n is the length of the input string s. This is because the code iterates over
the string twice: once to fill the pre array with the minimum operations required to remove '1's from the start of the string and once to
fill the suf array with the minimum operations required to remove '1's from the end of the string. Each element is computed in
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The space complexity of the code is also 0(n). Two extra arrays, pre and suf, each of size n + 1, are used to store the intermediate

results for the prefix and suffix operations, respectively. The space required by these auxiliary arrays is proportional to the length of

let minCost: number = Number.MAX\_SAFE\_INTEGER; // Initialize minimum cost to the maximum safe integer value.