1382. Balance a Binary Search Tree Medium Binary Search Tree Greedy Tree Depth-First Search

Problem Description

BST is considered balanced if, for every node in the tree, the depth difference between its left and right subtrees is no more than 1. The solution must maintain the original BST's node values and is not required to be unique—any correctly balanced BST with the original values is considered a valid answer.

Divide and Conquer

Binary Tree

Leetcode Link

Intuition

The problem presents us with a binary search tree (BST) and asks us to transform it into a balanced binary search tree (BBST). A

BBST.

To balance a BST, we want to ensure that we minimize the depth differences between the left and right subtrees of all the nodes. A well-known approach to creating a balanced BST is to first convert the BST into a sorted array and then to rebuild the BST from this array. The intuition behind this is that a sorted array will have the smaller values towards the beginning and larger values towards the end.

By consistently selecting the middle element of the array (or subarray) to be the root node of the (sub)tree, we can ensure that the number of nodes on the left and right of any node is as equal as possible, thus creating a balanced tree. The entire process consists of two main phases:

1. In-Order Traversal (dfs function): Perform an in-order traversal of the BST and store each node's value in an array. An in-order

traversal of a BST will process all nodes in ascending order, which aligns with the order we'd want in the array to reconstruct a

2. Building the Balanced BST (build function): Using the sorted array, recursively select the middle element as the root node, then

for constructing the balanced BST from the sorted values array.

build the left subtree from the elements before it and the right subtree from the elements after it. This step is akin to a binary search where we use the middle of the current array (or subarray) as the root and apply the logic recursively to the left and right halves.

The provided solution implements these two key phases with the help of two helper functions: dfs for in-order traversal and build

Solution Approach The implementation of the solution is done in two parts as per the problem requirement: first, the BST is converted to a sorted list, and then the list is used to construct a balanced BST.

Conversion of BST to Sorted List The conversion of the BST to a sorted list is done using an in-order traversal, which is a depth-first search (DFS). Before the

traversal, an empty list vals is initialized. The dfs function is defined to perform the traversal:

1. If the current node (root) is None, the function returns, as it means we've reached a leaf node's child.

2. It recursively calls itself on the left child (dfs(root.left)), processing all left descendants first (which are smaller in a BST). 3. The value of the current node is appended to the list vals (vals.append(root.val)). 4. It recursively calls itself on the right child (dfs(root.right)), processing all right descendants afterward (which are larger in a

build the subtrees.

faster to compute.

entirety of the sorted list.

Example Walkthrough

subarray.

len(vals) - 1).

BST).

After defining the dfs function, it is called initially with the root of the BST. This will result in vals containing all the node values in sorted order since BSTs inherently maintain an in-order sequence of ascending values.

- **Building the Balanced BST**
- The balanced BST is constructed using the build function which follows a divide and conquer strategy: 1. The function takes two indices, 1 and 1, which represent the start and end of the current subarray within vals we're using to
- in this subarray. 3. The middle index mid is calculated using (i + j) >> 1, which is a bitwise operation equivalent to dividing the sum by 2 but is

2. The base case checks if i is greater than j. If so, it returns None, as this means there are no more elements to create nodes from

4. A new TreeNode is created using vals [mid] as the root value. 5. The left subtree of the root is built by recursively calling build(i, mid - 1), effectively using the left half of the current

6. The right subtree of the root is built by recursively calling build(mid + 1, j), using the right half of the current subarray.

The build function initializes the process by being called with the start 0 and end len(vals) - 1 indices, essentially representing the

Finally, the balanceBST function returns the root node of the newly constructed balanced BST, which results from calling build(0,

Throughout the solution, we make use of recursion and divide-and-conquer techniques to arrive at a balanced BST that meets the

depth difference requirement for all nodes.

1. Begin at the root (1). Left child is None, so move to step 3.

3. Move to the right child, repeat steps for node 2, and so on.

Now, we use the sorted list vals to construct a balanced BST.

Calculate mid = (0 + 0) >> 1, resulting in mid = 0.

Create a new TreeNode with vals[0] (which is 1).

Calculate mid = (2 + 3) >> 1, resulting in mid = 2.

Create a new TreeNode with vals [2] (which is 3).

2. Calculate mid = (0 + 3) >> 1, resulting in mid = 1.

1. Call build(0, 3) since vals has four elements, indices ranging from 0 to 3.

No more elements to the left or right, so the left subtree is just the node with 1.

After completing these steps, we have successfully constructed the following balanced BST:

After traversing all the nodes, the vals list becomes:

- Let's consider a binary search tree (BST) that is skewed to the right as our example:
- This BST is not balanced because the right subtree of each node has a height that is more than 1 greater than the left subtree (which is non-existent). Our objective is to balance this BST according to the solution approach described above.

Following the in-order traversal, we obtain the values from the tree in sorted order. We start with an empty list vals.

This list represents the in-order traversal of the given BST and is sorted.

Building the Balanced BST

Python Solution

class TreeNode:

class Solution:

Java Solution

1 class Solution {

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Definition for a binary tree node.

self.val = val

self.left = left

self.right = right

def inorder_traversal(node):

return None

private List<Integer> treeValues;

inOrderTraversal(root);

1 // Definition for a binary tree node.

TreeNode(): val(0), left(nullptr), right(nullptr) {}

return rebuildTree(0, nodeValues.size() - 1);

// Helper function to perform an in-order traversal of a BST.

TreeNode* balanceBST(TreeNode* root) {

void inOrderTraversal(TreeNode* node) {

TreeNode* rebuildTree(int start, int end) {

newNode->left = rebuildTree(start, mid - 1);

return newNode; // Return the new subtree root.

newNode->right = rebuildTree(mid + 1, end);

int mid = (start + end) / 2;

1 // Definition for a binary tree node.

left: TreeNode | null;

right: TreeNode | null;

this.val = val;

this.left = left;

this.right = right;

inOrderTraversal(root);

TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}

TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}

vector<int> nodeValues; // Vector to store the values of nodes in sorted order.

// Main function to create a balanced BST from the unbalanced BST `root`.

// Rebuild the tree using the sorted values from `nodeValues`.

if (!node) return; // Base case: if the node is null, do nothing.

nodeValues.push_back(node->val); // Visit the node and add its value to `nodeValues`.

TreeNode* newNode = new TreeNode(nodeValues[mid]); // Create a new node with the mid value.

if (start > end) return nullptr; // Base case: no nodes to construct the tree.

// Recursively construct the left and right subtrees and link them to the new node.

constructor(val: number = 0, left: TreeNode | null = null, right: TreeNode | null = null) {

// Calculate the middle index and use it as the root to balance the tree.

inOrderTraversal(node->left); // Traverse the left subtree.

// Helper function to build a balanced BST from the sorted values.

inOrderTraversal(node->right); // Traverse the right subtree.

// Perform in-order traversal to get the values in the sorted order.

2 struct TreeNode {

11 class Solution {

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12 }

};

};

12 public:

int val;

TreeNode *left;

TreeNode *right;

public TreeNode balanceBST(TreeNode root) {

treeValues = new ArrayList<>();

def build_balanced_bst(start, end):

return

def __init__(self, val=0, left=None, right=None):

def balanceBST(self, root: TreeNode) -> TreeNode:

1 vals = [1, 2, 3, 4]

Conversion of BST to Sorted List

2. Append 1 to vals (thus vals = [1]).

3. Create a new TreeNode with vals[1] (which is 2), making it the root. 4. For the left subtree, we call build(0, 0):

This resulting tree is balanced as the depth difference between the left and right subtrees for all nodes is no more than 1. It maintains

 For the right subtree of 3, call build(3, 3): Only one element left, so create a new TreeNode with vals [3] (which is 4). No more elements to the left or right.

5. For the right subtree, we call build(2, 3):

For the left subtree of 3, there's no element, so return None.

all the original values from the input BST and is a valid solution according to the problem description.

node values = [] # Initialize an empty list to store the tree node values. 31 32 inorder_traversal(root) # Fill the node_values list with values from the BST. 33 # Build and return a balanced BST using the list of values. return build_balanced_bst(0, len(node_values) - 1) 34 35

// Method to turn a binary search tree into a balanced binary search tree.

// Populate the treeValues list with the values in sorted order.

// Helper method to perform an in-order traversal of the tree and store the values.

Recursively build left and right subtrees using the split lists.

Helper function to perform inorder traversal and collect values in a list.

node_values.append(node.val) # Append the value of the current node.

if start > end: # If starting index is greater than ending, subtree is empty.

node = TreeNode(node_values[mid]) # Create a node with the middle value.

if node is None: # Base case: If node is None, return.

inorder_traversal(node.left) # Recurse on left subtree.

mid = (start + end) // 2 # Compute the middle index.

node.left = build_balanced_bst(start, mid - 1)

node.right = build_balanced_bst(mid + 1, end)

return node # Return the newly created node.

// Class member to hold the tree values in sorted order.

// Reconstruct the tree in a balanced manner.

return buildBalancedTree(0, treeValues.size() - 1);

inorder_traversal(node.right) # Recurse on right subtree.

Helper function to build a balanced BST given a sorted value list.

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private void inOrderTraversal(TreeNode node) {
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           if (node == null) {
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               // Base case: if the node is null, do nothing.
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               return;
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           // Traverse the left subtree first.
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           inOrderTraversal(node.left);
22
           // Store the value of the current node.
23
           treeValues.add(node.val);
24
           // Traverse the right subtree next.
25
           inOrderTraversal(node.right);
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       // Helper method to build a balanced binary search tree using the stored values.
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29
       private TreeNode buildBalancedTree(int start, int end) {
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           // Base case: if start index is greater than end index, subtree is null.
           if (start > end) {
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               return null;
33
           // Find the mid point to make the current root.
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           int mid = start + (end - start) / 2;
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           // Create a new TreeNode with the mid value.
37
           TreeNode root = new TreeNode(treeValues.get(mid));
38
           // Recursively build the left subtree.
39
           root.left = buildBalancedTree(start, mid - 1);
           // Recursively build the right subtree.
40
            root.right = buildBalancedTree(mid + 1, end);
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           // Return the node.
43
           return root;
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45 }
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C++ Solution
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46 Typescript Solution

2 class TreeNode {

val: number;

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    // Array to store the values of nodes in sorted order
    const nodeValues: number[] = [];
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    // Main function to create a balanced BST from the unbalanced BST 'root'
    function balanceBST(root: TreeNode | null): TreeNode | null {
         if (root === null) return null; // Guard clause for null input
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         // Perform in-order traversal to get the values in sorted order
         inOrderTraversal(root);
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         // Rebuild the tree using the sorted values from 'nodeValues'
         return rebuildTree(0, nodeValues.length - 1);
 24
 25 }
 26
    // Helper function to perform an in-order traversal of a BST
 28 function inOrderTraversal(node: TreeNode | null): void {
         if (node === null) return; // Base case: if the node is null, do nothing
 29
         inOrderTraversal(node.left); // Traverse the left subtree
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 31
         nodeValues.push(node.val); // Visit the node and add its value to 'nodeValues'
 32
         inOrderTraversal(node.right); // Traverse the right subtree
 33 }
 34
     // Helper function to build a balanced BST from the sorted values
     function rebuildTree(start: number, end: number): TreeNode | null {
 37
         if (start > end) return null; // Base case: no nodes to construct the tree
 38
 39
         // Calculate the middle index and use it as the root to balance the tree
         const mid = start + Math.floor((end - start) / 2);
 40
         const newNode = new TreeNode(nodeValues[mid]); // Create a new node with the mid value
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         // Recursively construct the left and right subtrees and link them to the new node
 44
         newNode.left = rebuildTree(start, mid - 1);
 45
         newNode.right = rebuildTree(mid + 1, end);
 46
 47
         return newNode; // Return the new subtree root
 48 }
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Time and Space Complexity
The given code consists of a depth-first search (DFS) traversal (dfs function) to collect the values of the nodes in an inorder fashion
```

Time Complexity 1. DFS Traversal (dfs function): The DFS traversal visits each node exactly once. With n being the number of nodes in the tree, the time complexity for the DFS traversal is O(n).

2. Constructing Balanced BST (build function): The build function is called once for each element in the sorted list of values. Similar to binary search, at each recursive call, it splits the list into two halves until the base case is reached (when i > j). Therefore, constructing the balanced BST would also take O(n) time since each node is visited once during the construction.

and a recursive function (build function) to construct a balanced binary search tree (BST) from the sorted list of values.

Adding both complexities together, the overall time complexity of the algorithm is O(n).

1. DFS Traversal: The auxiliary space is used to store the inorder traversal of the BST in the vals list, which will contain n elements, thus requiring O(n) space.

Space Complexity

- 2. Constructing Balanced BST: The recursive build function will use additional space on the call stack. In the worst case, there will
- be O(log n) recursive calls on the stack at the same time, given that the newly constructed BST is balanced (hence the maximum height of the call stack corresponds to the height of a balanced BST).

Overall, considering both the space used by the list vals and the recursion call stack, the space complexity of the algorithm is O(n) for the list and O(log n) for the call stack, leading to O(n) space complexity when combined.