2398. Maximum Number of Robots Within Budget

Prefix Sum Binary Search Sliding Window | Heap (Priority Queue) Array Hard

You are given n robots, each with a specific time it takes to charge (chargeTimes[i]) and a cost that it incurs when running (runningCosts[i]). Your goal is to determine the maximum number of consecutive robots that can be active without exceeding a given budget. The total cost to run k robots is calculated by adding the maximum charge time from the selected k robots to the product of k and the sum of their running costs. The problem is essentially asking you to find the longest subsequence of robots that can operate concurrently within the constraints

Leetcode Link

of your budget, taking into consideration both the upfront charge cost and the ongoing running costs.

Intuition

The solution utilizes the sliding window technique to find the longest subsequence of consecutive robots that can be run within the

budget. To efficiently manage the running sum of the running costs and the maximum charge time within the current window, we can use a deque (double-ended queue) and maintain the sum of the running costs.

Problem Description

We iterate through the robots using a sliding window defined by two pointers, j (the start) and i (the end). For each position i: 1. A deque is used to keep track of the indices of the robots in the current window, maintaining the indices in decreasing order of

robots are removed from the end of the deque because they are rendered irrelevant (a larger charge time has been found). 3. We add the running cost of the current robot to a running sum s. 4. We check if the current window exceeds the budget by calculating the total cost using the front of the deque (which has the

Sliding Window Technique

their chargeTimes.

2. We add the robot at position 1 to the window. If it has a charge time greater than some robots already in the window, those

robot with the maximum charge time) and the running sum s. If it does exceed the budget, we shrink the window from the left by increasing j and adjusting the sum and deque accordingly.

5. The answer (ans) is updated as we go, to be the maximum window size found that satisfies the budget constraint.

Solution Approach

The implementation uses a greedy approach combined with a sliding window technique to determine the maximum number of

By the end of the iteration, and holds the length of the longest subsequence of robots we can operate without exceeding the budget.

1. Initialization: A deque q is declared to keep track of the robots' indices in the window while ensuring access to the largest chargeTime in constant time. Variable s is used to store the running sum of runningCosts, j is the start of the current window, ans

consecutive robots that can be run within the budget. Here's a step-by-step breakdown:

is the variable that will store the final result, and n holds the length of the arrays.

from the end since they do not affect the max anymore.

The current index i is added to the end of the deque.

The running cost of the robot at j is subtracted from s.

The start index j is incremented to shrink the window.

Let's go through a small example to illustrate the solution approach.

can be run without exceeding the budget, according to the specified cost function.

2. Sliding Window: This implementation uses a single loop that iterates over all robots' indices i from 0 to n-1. For each index i:

Insert the current robot into the deque: • If there are robots in the deque with chargeTimes less than or equal to the current robot's chargeTime, they are removed

- The running cost of the robot i is added to the running sum s. 3. Maintaining the Budget Constraint: The algorithm checks if the total cost of running robots from the current window exceeds the budget: While the sum of the maximum chargeTime (from the front of the deque) and the product of s and the window size (i - j +
- 1) is greater than budget, the window needs to be shrunk from the left. This includes: If the robot at the start of the window is also at the front of the deque, it is removed.
- comparing it with the size of the current window.

5. Return the Result: After the loop finishes, the variable ans holds the length of the longest segment of consecutive robots that

4. Update the Result: After fixing the window by ensuring it's within the budget, update the maximum number of robots ans by

- The algorithm's time complexity is O(n), where n is the number of robots, since each element is inserted and removed from the deque at most once. The usage of a deque enables the algorithm to determine the maximum chargeTime in O(1) time while keeping the ability to insert and delete elements from both ends efficiently. The running sum s is also updated in constant time, making this
- Suppose we have n = 4 robots with the following chargeTimes and runningCosts: 1 chargeTimes = [3, 6, 1, 4] 2 runningCosts = [2, 1, 3, 2]

Now let's apply our sliding window technique: 1. Initialize our variable s to 0, our deque q to empty, ans to 0, and our window start j to 0. 2. Start iterating with the sliding window:

s (which is now 2). - The window size is i - j + 1 which is 1 at this point. - The total cost calculation is max(chargeTimes)

ii. Move to the next robot i = 1: - chargeTimes [i] is 6; since it's larger than the last element in the deque, we push it to the

iii. Move to robot i = 2: - chargeTimes [i] is 1, it's less than the elements in the deque, so nothing is removed and it's added to q

(now [0,1,2]). - Add runningCosts[i] to s (which is now 6). - The total cost is max(chargeTimes) (which is still 6) + s * window

(which is 3 from the deque) + s * window size = 3 + 2 * 1 = 5, which is within the budget.

max(chargeTimes) (which is 6) + s * window size = 6 + 6 * 3 = 24, still over budget.

i. Start with the first robot i = 0: - chargeTimes[i] is 3; we add it to our deque q (which is now [0]). - We add runningCosts[i] to

deque q (which is now [0,1]). - Add runningCosts[i] to s (which is now 3). - The calculation now is max(chargeTimes) (which is 6) + s * window size (2 * 2) = 6 + 4 = 10, still within the budget.

approach efficient for large inputs.

Example Walkthrough

And let's say our budget is 16.

iv. Move to robot i = 3: - chargeTimes[i] is 4, which is less than 6 but more than 3, so we pop from the end of the deque until

(which was 2), ans remains 2.

budget.

Python Solution

class Solution:

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from collections import deque

max_charge_deque = deque()

Iterate over all the robots

for i in range(len(charge_times)):

current_charge = charge_times[i]

max_charge_deque.pop()

max_charge_deque.append(i)

while (max_charge_deque and

current_running_cost = running_costs[i]

or equal to the current robot's charge time

Add the current robot's index to the deque

if max_charge_deque[0] == start_idx:

max_robots = max(max_robots, i - start_idx + 1)

Deque<Integer> queue = new ArrayDeque<>();

int numOfRobots = chargeTimes.length;

// Starting index for the current window

for (int i = 0; i < numOfRobots; ++i) {</pre>

queue.pollLast();

// Total number of robots

// Running sum of the costs

long runningSum = 0;

int windowStart = 0;

int maxRobots = 0;

// Loop over each robot

queue.offer(i);

return maxRobots;

running_cost_sum += current_running_cost

Add the current robot's running cost to the sum

for the robots in the window does not exceed the budget

size (3 * 3) = 6 + 9 = 15, within the budget.

3. To maintain the budget constraint: i. When the cost exceeds the budget (which is the case now), we need to shrink our window from the left: - Since j = 0 is at the

front of the deque, remove it from the deque q (now [1,3]). - Subtract runningCosts[j] from s to update the running sum (now

the condition is satisfied and then add index 3. Deque q is now [0,1,3]. - Add runningCosts[i] to s (which is now 8). - The total

cost now is max(chargeTimes) (which is still 6) + s * window size (4 * 4) = 6 + 16 = 22, which exceeds the budget.

6). - Increment j to 1 to shrink the window. - Now, the window size is 3 (from index 1 to 3), and the cost calculation is

size that was in budget before. iii. The current window size is now i - j + 1 which is 2, and the total cost is max(chargeTimes) (which is 4) + s * window size = 4 + 3 * 2 = 10, within the budget. - We update ans to the current window size, but since it's not bigger than the previous ans

4. After iterating through all robots, our answer ans is 2 which indicates we can run at most 2 consecutive robots within the given

By following this approach, we manage to calculate the maximum number of consecutive robots that can be active within the

allocated budget in an efficient manner, with a loop that runs linearly relative to the number of robots.

Deque to store indices of robots with charge_times in non-increasing order

Remove robots from the back of the deque if their charge time is less than

while max_charge_deque and charge_times[max_charge_deque[-1]] <= current_charge:</pre>

Ensure the sum of the max charge time in the window and the total running cost

// Method to calculate the maximum number of robots that can be activated within the budget

while (!queue.isEmpty() && chargeTimes[queue.getLast()] <= currentChargeTime) {</pre>

// If the total cost exceeds the budget, remove robots from the front of the queue

public int maximumRobots(int[] chargeTimes, int[] runningCosts, long budget) {

// Result, i.e., the maximum number of robots that can be activated

// Update the running sum with the current robot's running cost

// Current robot's charge time and running cost

if (queue.getFirst() == windowStart) {

// Update the result with the maximum number of robots

maxRobots = Math.max(maxRobots, i - windowStart + 1);

int currentChargeTime = chargeTimes[i];

// Add the current robot to the queue

runningSum += currentRunningCost;

// Return the maximum number of robots

int currentRunningCost = runningCosts[i];

If the robot at the front of the deque is the robot at start_idx, remove it

Holds the sum of the running costs of the current set of robots

def maximum_robots(self, charge_times, running_costs, budget):

ii. Repeat the process by incrementing j to 2 and adjust:q (now [3]), s to 3, and ans remains 2 which was the biggest window

running_cost_sum = 0 # Stores the maximum number of robots that can be activated max_robots = 0 # Starting index of the current window of robots start_idx = 0

max_charge_deque.popleft() # Remove the robot's running cost at start_idx from the sum and move start_idx forward 36 37 running_cost_sum -= running_costs[start_idx] 38 start_idx += 1 39 # Update the maximum number of robots that can be activated 40

// Queue to store indices of robots to ensure chargeTimes are in non-increasing order from front to back

// Remove robots from the back of the queue whose charge time is less than or equal to the current one

while (!queue.isEmpty() && chargeTimes[queue.getFirst()] + (i - windowStart + 1) * runningSum > budget) {

queue.pollFirst(); // Remove the robot at the start of the window if it is at the front of the queue

runningSum -= runningCosts[windowStart++]; // Reduce the running sum and move the window start forward

charge_times[max_charge_deque[0]] + (i - start_idx + 1) * running_cost_sum > budget):

43 return max_robots 44

Java Solution

class Solution {

C++ Solution

#include <vector>

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2 #include <deque>
    using std::vector;
    using std::deque;
    using std::max;
    class Solution {
    public:
         // Finds the maximum number of robots that can be activated within a given budget
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         int maximumRobots(vector<int>& chargeTimes, vector<int>& runningCosts, long long budget) {
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             // Deque to store indices of robots with chargeTimes in non-increasing order
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             deque<int> maxChargeDeque;
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             // Holds the sum of the running costs of the current set of robots
             long long runningCostSum = 0;
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             // Stores the maximum number of robots that can be activated
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             int maxRobots = 0;
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             // Starting index of the current window of robots
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             int startIdx = 0;
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             int numRobots = chargeTimes.size();
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             // Iterate over all the robots
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             for (int i = 0; i < numRobots; ++i) {</pre>
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                 int currentCharge = chargeTimes[i];
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                 int currentRunningCost = runningCosts[i];
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                 // Remove robots from the back of the deque if their charge time is less than
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                 // or equal to the current robot's charge time
                 while (!maxChargeDeque.empty() && chargeTimes[maxChargeDeque.back()] <= currentCharge) {</pre>
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                     maxChargeDeque.pop_back();
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                 // Add the current robot's index to the deque
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                 maxChargeDeque.push_back(i);
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                 // Add the current robot's running cost to the sum
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                 runningCostSum += currentRunningCost;
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                 // Ensure the sum of the max charge time in the window and the total running cost
                 // for the robots in the window does not exceed the budget
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                 while (!maxChargeDeque.empty() && chargeTimes[maxChargeDeque.front()] + (i - startIdx + 1) * runningCostSum > budget) {
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                     // If the robot at the front of the deque is the robot at the startIdx, remove it
                     if (maxChargeDeque.front() == startIdx) {
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                         maxChargeDeque.pop_front();
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                     // Remove the robot's running cost at startIdx from the sum and move the startIdx forward
                     runningCostSum -= runningCosts[startIdx++];
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                 // Update the maximum number of robots that can be activated
                 maxRobots = max(maxRobots, i - startIdx + 1);
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             return maxRobots;
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 54 };
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Typescript Solution
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function maximumRobots(chargeTimes: number[], runningCosts: number[], budget: number): number {

// Remove robots from the back of the deque if their charge time is less than

// Ensure the sum of the max charge time in the window and the total running cost

// If the robot at the front of the deque is the robot at startIdx, remove it

while (maxChargeDeque.length > 0 && chargeTimes[maxChargeDeque[maxChargeDeque.length - 1]] <= currentCharge) {</pre>

while (maxChargeDeque.length > 0 && chargeTimes[maxChargeDeque[0]] + (i - startIdx + 1) * runningCostSum > budget) {

// Deque to store indices of robots with chargeTimes in non-increasing order

// Holds the sum of the running costs of the current set of robots

// Stores the maximum number of robots that can be activated

// Starting index of the current window of robots

const currentCharge = chargeTimes[i];

runningCostSum += currentRunningCost;

const currentRunningCost = runningCosts[i];

// or equal to the current robot's charge time

// Add the current robot's index to the deque

if (maxChargeDeque[0] === startIdx) {

maxRobots = Math.max(maxRobots, i - startIdx + 1);

maxChargeDeque.shift();

// Add the current robot's running cost to the sum

// for the robots in the window does not exceed the budget

const maxChargeDeque: number[] = [];

const numRobots = chargeTimes.length;

for (let i = 0; i < numRobots; ++i) {</pre>

maxChargeDeque.pop();

maxChargeDeque.push(i);

// Iterate over all the robots

let runningCostSum = 0;

let maxRobots = 0;

let startIdx = 0;

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34 // Remove the robot's running cost at startIdx from the sum and move the startIdx forward 35 36 runningCostSum -= runningCosts[startIdx++]; 37 38 39 // Update the maximum number of robots that can be activated

Time Complexity

Space Complexity

return maxRobots;

Adding elements to the deque which takes 0(1) time per operation, but elements are only added when they are larger than the last element. Since elements are removed from the deque if they are not greater, each element is added and removed at most once.

Time and Space Complexity

• Removing elements from the dequeue from both ends also takes 0(1) time per operation, ensuring that no element is processed more than once. The while loop inside the for loop is executed to ensure that the current maximum charge time and total cost do not exceed the

The given code maintains a deque (q) and iterates over the chargeTimes array once. The primary operations within the loop are:

- budget. Although it seems nested, it does not make the overall algorithm exceed 0(n) because each element is added to the deque only once, and hence can be removed only once.
- Given these observations, each operation is in constant time regarding the current index, and since we only iterate over the array once, the time complexity is O(n) where n is the length of the chargeTimes array.

in non-decreasing order. Thus, in the worst-case scenario, the space complexity is O(n) where n is the length of the chargeTimes array. Other variables used (such as s, j, a, b, and ans) only require constant space (0(1)), so do not affect the overall space complexity.

The space complexity is primarily determined by the deque q, which in the worst case might hold all elements if the chargeTimes are