191. Number of 1 Bits

Bit Manipulation **Divide and Conquer Easy**

Problem Description

The task is to write a function that receives an unsigned integer's binary representation and calculates the number of '1' bits (also called the Hamming weight) in it. A binary representation means the number is expressed in base 2, consisting only of '0's and '1's. For example, the binary representation of the decimal number 5 is '101', which has two '1' bits.

It's important to note that in some programming languages, such as Java, there isn't an unsigned integer type, which means that you might have to deal with negative numbers as well. However, for the purpose of counting '1' bits, you can consider the binary representation regardless of whether the integer is signed or unsigned. In 2's complement notation, which Java uses to represent signed integers, negative numbers also have a binary representation that can be used to count the number of '1' bits.

Intuition

The solution approach uses a bit manipulation technique that exploits a nice property of binary numbers: subtracting 1 from a number flips all the bits after the rightmost '1' bit (including the '1' bit). So, if we perform a bitwise AND between the number n and n-1, we effectively remove the rightmost '1' bit from n.

For instance, if n is 101100, n-1 is 101011. The bitwise AND of n and n-1 would be 101000, which removes the rightmost '1' bit from the original number. We repeatedly do this operation and count how many times we perform it until n becomes 0. The count gives us the number of '1' bits in the original number since each operation removes exactly one '1' bit.

By following this approach, we can calculate the Hamming weight efficiently. Let's break down the steps involved in the provided solution:

2. Use a while loop to iterate as long as n is not zero.

1. Initialize a variable ans to zero. This will be used to track the number of '1' bits.

- 3. Inside the loop, perform the operation $n \le n 1$, which removes the rightmost '1' bit from n. 4. Increment ans by one after each bit-removal operation.
- 5. Once n becomes zero, which means all '1' bits have been removed, return ans, the count of '1' bits.
- This technique is efficient because it directly targets the '1' bits and minimizes the number of operations relative to the number of

'1' bits in the binary representation.

The provided Python solution implements a commonly known algorithm for counting the number of '1' bits in the binary

Solution Approach

representation of an unsigned integer using bit manipulation. Here are the key components of the implementation:

Bitwise AND Operator (&): The bitwise AND operator is used to perform the AND operation on each bit of the binary

- representations of two numbers. It is a fundamental operation used in the given solution to remove the rightmost '1' bit. While Loop: The solution utilizes a while loop to iterate until the given number n is reduced to zero. The condition of the while
- Thus, the loop continues as long as n has at least one '1' bit remaining. Bit Manipulation Trick (n &= n - 1): This specific operation is used to clear the least significant '1' bit of the number n. In each iteration of the while loop, n is updated to n & (n - 1), which removes the rightmost '1' bit from n. This is the core step

loop while n: takes advantage of the fact that in Python, zero is considered False and all other integers are considered True.

- that reduces the value of n while also counting the number of '1' bits. Counter Variable (ans): A counter variable ans is used to track the number of '1' bits. It is incremented by 1 for each iteration of the while loop, which corresponds to the removal of each '1' bit.
- require any additional data structures, since the count is maintained in a single integer variable, and the input number n is manipulated in place to count the number of '1' bits. The pattern used here is quite effective for dealing with common bit manipulation problems and is a good example of using

The combination of these elements leads to an elegant and efficient approach to solving the problem. The solution does not

bitwise operators to simplify complex operations. Since each operation potentially reduces n by eliminating a '1' bit, the number of iterations is equal to the number of '1' bits, making the algorithm run in O(k) time complexity, where k is the number of '1' bits in the binary representation of n. **Example Walkthrough**

representation 1011. Let's apply the algorithm step-by-step to calculate the Hamming weight.

1. We initialize the counter ans to zero. This will keep track of the number of '1' bits. 2. The binary representation of the integer 11 is 1011, and it's not zero, so we enter the while loop. 3. We calculate n-1. For n = 1011 (11 in decimal), n-1 would be 1010 (10 in decimal).

Let's walk through an example to illustrate the solution approach. Consider the unsigned integer 11, which has the binary

- 4. Then, we perform $n \le n 1$, which is 1011 & 1010 resulting in 1010 (10 in decimal), thereby removing the last '1' bit.
- 5. We increment ans by one. ans is now 1.
- 6. n is now 1010 (10 in decimal), which is still not zero, so the while loop continues.
- 7. Again, n-1 is calculated to be 1001 (9 in decimal).
- 8. Performing $n \le n 1$ now, which is 1010 & 1001, results in 1000 (8 in decimal), removing another '1'.
- 9. Increment ans by one again. ans is now 2.
- 10. n is now 1000 (8 in decimal), which is still not zero.
- 11. n-1 is 0111 (7 in decimal). 12. Performing $n \le n - 1$ again results in 1000 & 0111, which results in 0000 (0 in decimal).
- 13. We increment ans by one last time. ans is now 3.
- 14. Now, n is zero, so we exit the while loop.

complexity that is linear with respect to the number of '1' bits in the binary representation.

- After exiting the loop, ans is 3, which is the number of '1' bits in the binary representation of the unsigned integer 11 (1011). Thus, the Hamming weight of 11 is 3.
- This technique minimizes the number of operations by ensuring that each iteration removes one '1' bit, leading to a time

Solution Implementation

Python

class Solution: def hammingWeight(self, n: int) -> int: # Initialize count of set bits to 0 count_of_set_bits = 0

while n:

Iterate until all bits are traversed

Perform bitwise AND operation between n and (n-1)

int onesCount = 0; // Store the count of 1-bits encountered

// Use '!=0' in the condition to ensure we process all bits of n.

* Function to count the number of 1 bits in the binary representation of a positive integer.

// Apply bitwise AND between n and n-1, which flips the least significant 1 bit of n to 0

* @returns The number of 1's in the binary representation of n.

This operation removes the rightmost set bit from n

```
n &= n - 1
           # Increment count of set bits
            count_of_set_bits += 1
       # Return the total count of set bits in the integer
       return count_of_set_bits
Java
public class Solution {
   /**
    * This method calculates the number of 1-bits in the binary representation of a number.
    * Treats the input number as an unsigned value.
    * @param n - The input integer (considered as unsigned) to count the 1-bits in.
    * @return The number of 1s in the binary representation of n.
    public int hammingWeight(int n) {
```

while (n != 0) {

n &= n - 1;

```
// Increment the count of 1-bits for every 1-bit cleared by the operation above.
           ++onesCount;
       return onesCount; // Return the total count of 1-bits found
C++
class Solution {
public:
   // This function returns the number of '1' bits in the binary representation of the given unsigned integer.
    int hammingWeight(uint32_t n) {
        int count = 0; // Initialize a counter for the '1' bits
       while (n) { // Continue until all bits are traversed
           n \&= n - 1; // Clear the least significant '1' bit
           ++count; // Increment the counter by one
       return count; // Return the total count of '1' bits
};
```

// Since Java does not support unsigned int natively, we interpret n as unsigned by comparing directly to 0.

// Apply the bit manipulation trick n & (n - 1) which clears the least significant 1-bit in n.

let count: number = 0; // Continue looping as long as n is not 0 while (n !== 0) {

TypeScript

* @param n - a positive integer

n &= n - 1;

function hammingWeight(n: number): number {

// Initialize a count for the number of 1 bits

/**

```
// Increment the count of 1 bits
          count++;
      // Return the final count of 1 bits in n
      return count;
class Solution:
   def hammingWeight(self, n: int) -> int:
       # Initialize count of set bits to 0
       count_of_set_bits = 0
       # Iterate until all bits are traversed
       while n:
           # Perform bitwise AND operation between n and (n-1)
           # This operation removes the rightmost set bit from n
           n &= n - 1
           # Increment count of set bits
           count_of_set_bits += 1
       # Return the total count of set bits in the integer
       return count_of_set_bits
Time and Space Complexity
  The given Python code defines a function hammingWeight that calculates the number of 1s in the binary representation of a given
  integer n. The algorithm works by turning off the rightmost 1-bit of n at each step until n becomes 0.
```

Time Complexity The time complexity of the algorithm is O(k), where k is the number of 1-bits in n. In the worst case, when n is a power of 2, k will

be logarithmic in the value of n because there will be only one 1-bit. In the average case, it will be less than logarithmic since

numbers typically have fewer than the maximum possible number of 1-bits. Therefore, in terms of n, the time complexity can be considered O(log n) because k will not exceed the number of bits in n, which is the logarithm of n.

depend on the input size.

Space Complexity The space complexity of the algorithm is 0(1) because it uses a fixed number of variables (ans and n) whose size does not