## 2845. Count of Interesting Subarrays

Medium Hash Table **Prefix Sum** <u>Array</u>

## **Problem Description**

to count the number of subarrays considered "interesting." A subarray is defined as a contiguous non-empty sequence of elements within the array. For a subarray nums [l.r] to be interesting, it must satisfy the condition that among its elements, the number of indices i (where  $1 \le i \le r$ ) such that nums [i] % modulo == k must itself be congruent to k when taken modulo modulo,

The problem provides an integer array called nums, indexed from 0. Additionally, two integers modulo and k are given. The task is

i.e., cnt % modulo == k. To understand better, consider these points:

For each subarray, you count the elements that, when divided by modulo, leave a remainder of k.

Here's the intuitive step-by-step breakdown:

calculate the total number of '1's in any subarray.

• If the count of such elements in the subarray also, when divided by modulo, leaves a remainder of k, that subarray is called interesting, and you

You go through the array and find all possible contiguous subarrays.

- need to increase the interesting subarray count by one. • The output is the total number of interesting subarrays found this way.
- Intuition

To approach this problem efficiently, without checking every possible subarray individually (which would be too time-consuming),

## we can use a technique from combinatorics that involves keeping track of the cumulative sums of certain conditions.

1. Transform the original array nums such that each element becomes 1 if it satisfies nums[i] % modulo == k or 0 otherwise. Let's call this array arr. 2. Create a prefix sum array s such that s[i] represents the total count of '1's from the start of arr to the current index i. This helps us to quickly

3. Use a hash-based data structure, like Counter in Python, to keep track of how many times each possible prefix sum modulo modulo has occurred. The key idea is that if the difference between the prefix sums of two indices is congruent to k modulo modulo, it implies the subarray between those two indices is interesting.

4. As we iterate through the arr, we add to a running sum (s) the value of the current element. We then look up in our Counter how many times

- we've seen prefix sums that are k less than the current sum mod modulo. These contribute to our answer. 5. We update our Counter with the new running sum mod modulo at each index, incrementing the count since we've now encountered another subarray with that sum.
- Applying these ideas, we achieve a solution that is linear with respect to the size of nums, hence much more efficient than examining all possible subarrays individually.
- **Solution Approach** The provided solution utilizes an array transformation, prefix sums, modular arithmetic, and a hash map for efficient lookups to

tackle the subarray counting challenge. Array Transformation: First, the code transforms the original nums array into a binary array array arr with the same length. Each element in arr is set to 1 if nums[i] % modulo equals k, otherwise, it is set to 0. This transformation simplifies the problem by

converting it into a problem of counting the number of subarrays whose sum is congruent to k modulo modulo.

## arr = [int(x % modulo == k) for x in nums]

0 (no elements).

cnt = Counter()

s += x

Using a HashMap (Counter) for Prefix Sum Lookup: The Counter is used to store the frequency of the occurrence of prefix sums modulo modulo. Initially, Counter is set to {0: 1} because we start with a sum of 0 and there is one way to have a sum of

cnt[0] = 1Calculating Prefix Sums and Counting Interesting Subarrays: As we iterate through each element in the transformed array arr, we maintain a running sum s. For each new element x, the running sum s is incremented by x, representing the sum of a

seen prefix sums that would make the sum of the current subarray equal to k modulo modulo. This is done by checking cnt [(s

After checking for interesting subarrays, we update the Counter with the new running sum modulo modulo to account for the

```
We then determine the number of interesting subarrays that end at the current index by looking up how many times we've
```

- k) % modulo].

prefix ending at this index.

ans += cnt[(s - k) % modulo]

new subarray ending at this index. cnt[s % modulo] += 1 Returning the Result: The variable ans is used to accumulate the count of interesting subarrays. After iterating over the array arr, ans holds the final count of all interesting subarrays, which is returned as the result.

The overall time complexity of the solution is O(n), as it requires a single pass through the array, and space complexity is also

O(n) due to the additional array arr and the Counter which might store up to modulo distinct prefix sums.

```
Example Walkthrough
```

 $cnt = Counter(\{0: 1\})$ 

process dynamically:

returned.

**Python** 

class Solution:

subarrays based on the given criteria.

Let's work through an example to illustrate the solution approach.

return ans

becomes [1, 0, 1, 0, 1], since 1, 3, and 5 are odd numbers and give a remainder of 1 when divided by 2. Using a HashMap (Counter) for Prefix Sum Lookup: Initialize a Counter with {0: 1}, representing that the sum of zero occurs once at the beginning (no subarray).

Calculating Prefix Sums and Counting Interesting Subarrays: Now, we start iterating through arr and sketch out the

Consider the integer array nums = [1, 2, 3, 4, 5], with modulo = 2, and k = 1. The task is to count the number of interesting

Array Transformation: We transform nums into arr by setting each arr[i] to 1 if nums[i] % 2 == 1, otherwise 0. Thus, arr

2] = cnt[0], which is 1, as we have seen a prefix sum (that sums to 0) exactly once before adding arr[0]. We add 1 to our answer and update the Counter to cnt[1] += 1. For arr[1] with a value of 0, our running sum does not change (s = 1). We look up cnt[(1 - 1) % 2] = cnt[0], again

finding a 1. We add it to our answer (now ans = 2) and leave the Counter unchanged since arr[1] is 0.

For arr [0], which equals 1, we increment our running sum s = 0 + 1 = 1. We then look in the Counter for cnt [(1 - 1) %

increments to 3. We then increment cnt[2 % 2] = cnt[0] by 1. By iterating over the entire array arr, we keep a running sum s, check the Counter, and update the counts of encountered modulated prefix sums, accumulating the number of interesting subarrays into ans.

the variable ans. Assuming we were incrementing ans along with the iterations as described, the final result would be

For arr[2] = 1, s is updated to 2. We check cnt[(2 - 1) % 2] = cnt[1] in the Counter, which is 1, so our answer

This approach simplifies the process, ensuring we only need to traverse the array once, giving an O(n) time complexity, which is efficient for large arrays. Solution Implementation

Returning the Result: After iterating over the entire array arr, we will have the final count of all interesting subarrays stored in

# Initialize answer and cumulative sum count\_interesting\_subarrays = 0 cumulative\_sum = 0

def countInterestingSubarrays(self, nums: List[int], modulo: int, k: int) -> int:

# Initialize with 0 sum having 1 frequency as this represents empty subarray

# The current sum minus the target sum (k) mod modulo will tell us

public long countInterestingSubarrays(List<Integer> nums, int modulo, int k) {

int[] remainders = new int[totalCount]; // Array to store the remainders

// Populate the remainders array with 1 if nums[i] % modulo == k or with 0 otherwise

int totalCount = nums.size(); // Total number of elements in nums

# if there is a subarray ending at the current index which is interesting

count\_interesting\_subarrays += cumulative\_sum\_frequency[(cumulative\_sum - k) % modulo]

// Method that counts the number of subarrays where the number of elements equal to k modulo is also k.

# in the original nums array satisfies the condition (x % modulo == k).

# This array will contain 1s at the positions where the element

interesting\_elements = [int(num % modulo == k) for num in nums]

# Counter to store the frequency of cumulative sums mod modulo

# Iterate through the boolean array to count interesting subarrays

cumulative\_sum\_frequency[cumulative\_sum % modulo] += 1

cumulative\_sum\_frequency = Counter()

for element in interesting\_elements:

for (int i = 0; i < totalCount; i++) {</pre>

// Function that counts the number of "interesting" subarrays

for (int i = 0; i < n; ++i) {

for (int element : modArray) {

const binaryRemainderArray: number[] = [];

for (const num of nums) {

std::unordered\_map<int, int> prefixCount;

int n = nums.size(); // Get the size of the 'nums' vector

modArray[i] = (nums[i] % modulo == k) ? 1 : 0;

# Update cumulative frequency counter

cumulative\_sum += element

cumulative\_sum\_frequency[0] = 1

# Return the total count of interesting subarrays return count\_interesting\_subarrays

import java.util.List;

import java.util.HashMap;

import java.util.Map;

class Solution {

from collections import Counter

C++

public:

#include <vector>

class Solution {

**TypeScript** 

#include <unordered map>

Java

```
remainders[i] = nums.get(i) % modulo;
    if (remainders[i] == k) {
        remainders[i] = 1;
    } else {
        remainders[i] = 0;
Map<Integer, Integer> remainderCounts = new HashMap<>(); // Map to store the remainder frequencies
remainderCounts.put(0, 1); // Initialize with 0 remainder seen once
long interestingSubarraysCount = 0; // Variable to hold the final count of interesting subarrays
int sum = 0; // Variable to accumulate the sum of remainders
// Iterate over the remainders array
for (int remainder: remainders) {
    sum += remainder; // Increase the sum with the current remainder
    // Increase the count by the number of occurrences where the adjusted sum matches the expected remainder
    interestingSubarraysCount += remainderCounts.getOrDefault((sum - k + modulo) % modulo, 0);
    // Update the map with the current modulus of the sum and increase the count by 1 or set it to 1 if not present
    remainderCounts.merge(sum % modulo, 1, Integer::sum);
return interestingSubarraysCount; // Return the count of interesting subarrays
```

```
prefixCount[currentSumModulo % modulo]++;
// Return the final count of "interesting" subarrays
return interestingSubarraysCount;
```

binaryRemainderArray.push(num % modulo === targetRemainder ? 1 : 0);

def countInterestingSubarrays(self, nums: List[int], modulo: int, k: int) -> int:

# Initialize with 0 sum having 1 frequency as this represents empty subarray

# The current sum minus the target sum (k) mod modulo will tell us

# if there is a subarray ending at the current index which is interesting

count\_interesting\_subarrays += cumulative\_sum\_frequency[(cumulative\_sum - k) % modulo]

# in the original nums array satisfies the condition (x % modulo == k).

# This array will contain 1s at the positions where the element

interesting\_elements = [int(num % modulo == k) for num in nums]

# Counter to store the frequency of cumulative sums mod modulo

# Iterate through the boolean array to count interesting subarrays

cumulative\_sum\_frequency[cumulative\_sum % modulo] += 1

// An "interesting" subarray is one where the sum of its elements, modulo 'modulo', equals 'k'

// Preprocessing: Populate 'modArray' with 1 if nums[i] % modulo == k, otherwise 0

prefixCount[0] = 1; // Initialize for the case where subarray begins at index 0

int currentSumModulo = 0; // Variable to store current prefix sum modulo 'modulo'

// Calculate adjusted sum for negative cases and find count in 'prefixCount'

function countInterestingSubarrays(nums: number[], modulo: number, targetRemainder: number): number {

interestingSubarraysCount += prefixCount[(currentSumModulo - k + modulo) % modulo];

long long interesting Subarrays Count = 0; // Variable to store the count of interesting subarrays

long long countInterestingSubarrays(std::vector<int>& nums, int modulo, int k) {

std::vector<int> modArray(n); // Array to store modulo transformations

// Hash map to keep track of the count of prefix sums modulo 'modulo'

// Iterate over the modified array to count "interesting" subarrays

currentSumModulo += element; // Update current prefix sum

// Increase the count for this sum modulo 'modulo'

```
// Create a map to count the occurrences of cumulative sums modulo 'modulo'.
const cumulativeSumCounts: Map<number, number> = new Map();
cumulativeSumCounts.set(0, 1); // Initialize with a zero sum to account for subarrays that start from index 0.
let interestingSubarraysCount = 0; // Initialize the count of interesting subarrays.
let cumulativeSum = 0; // Initialize the cumulative sum of binary values.
for (const binaryValue of binaryRemainderArray) {
   // Accumulate the binary values to keep track of the number of elements equal to targetRemainder modulo 'modulo'
    cumulativeSum += binaryValue;
   // Calculate the adjusted cumulative sum for the interesting subarray.
   const adjustedSum = (cumulativeSum - targetRemainder + modulo) % modulo;
   // Add the number of occurrences where the adjusted cumulative sum has been seen before.
    interestingSubarraysCount += cumulativeSumCounts.get(adjustedSum) || 0;
   // Increment the count for the current cumulative sum.
   cumulativeSumCounts.set(cumulativeSum % modulo, (cumulativeSumCounts.get(cumulativeSum % modulo) || 0) + 1);
return interestingSubarraysCount; // Return the total count of interesting subarrays found.
```

// Initialize an array to store binary values, 1 for integers that have a remainder equal to targetRemainder when divided by

```
cumulative sum frequency[0] = 1
# Initialize answer and cumulative sum
count_interesting_subarrays = 0
```

cumulative\_sum = 0

cumulative\_sum\_frequency = Counter()

for element in interesting\_elements:

# Update cumulative frequency counter

cumulative\_sum += element

from collections import Counter

class Solution:

```
# Return the total count of interesting subarrays
       return count_interesting_subarrays
Time and Space Complexity
  The time complexity of the code is O(n), where n is the length of the input list nums. This is because the code iterates through the
  nums list once, performing a constant amount of work for each element by computing the modulo, updating the sum s, looking up
  and updating the count in the cnt dictionary, and incrementing the answer ans.
```

The space complexity of the code is also 0(n) due to the use of the cnt dictionary, which stores up to n unique sums modulo the value of modulo, and the list arr which stores n elements.