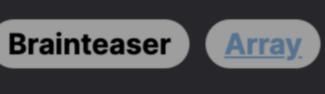
Sorting

**Prefix Sum** 







**Problem Description** 

In this problem, we are provided with an array nums which represents the initial positions of a group of robots on an infinite number line, where each element is a unique robot's starting position. Along with this, we have a string s that contains the direction each robot will head towards once they're commanded to move. The directions 'L' and 'R' stand for left (toward negative infinity) and right (toward positive infinity), respectively. Robots will move at a rate of one unit per second.

A key point in the problem is that if two robots meet at the same point at the same time, they instantaneously switch directions but continue moving without any delay. This collision means that we could consider the robots as if they pass through each other and continue in their initial directions for the purpose of calculation.

The task is to calculate the sum of all distances between pairs of robots after a given number of seconds d and to return this sum modulo 10^9 + 7 due to the potential for large numbers.

## Intuition

considering potential collisions. However, the key realization that simplifies this problem is to understand that we don't actually have to simulate the movement of robots and handle their collisions. Because robots change direction instantaneously upon collision and there is no delay, we can imagine that the robots simply pass

At first glance, calculating the distances between robots after an arbitrary number of seconds seems complicated, especially when

through each other and continue in their original direction. This means that after d seconds, regardless of any collisions that might have happened, we can calculate the new position of each robot by simply adding or subtracting d from their initial positions based on their intended direction. After determining the theoretical new positions, we can sort these positions in ascending order. We then iterate through this sorted

list to calculate the running sum of distances between each robot and all that come before it. This is effectively the cumulative distance from each of the robots to the start. Summing up the distances while iterating through the sorted list provides the total sum of distances between all pairs of robots after

This approach negates the need to handle the complexity of collisions during the movement phase, which is what makes the problem solvable within the given constraints.

**Solution Approach** 

The implementation of this problem's solution uses simple yet elegant logic and a few well-established Python techniques.

d seconds. We take care to apply the modulo operation as required to handle the potential for very large numbers.

collisions further.

Firstly, we manipulate the initial positions of the robots according to the directions specified by the s string. This is carried out by a combination of enumeration and conditional addition or subtraction. Depending on whether the direction at index i in s is 'R' (right)

or 'L' (left), we add or subtract the duration d from the corresponding starting position in nums. The updated positions array structure is then sorted. Sorting here uses the default O(n log n) sorting algorithm, which is common practice in Python. Sorting is crucial as it prepares us to compute distances without having to track individual movements or

Next, an iterative approach is used. The loop calculates the running sum of distances by traversing through the sorted array of new positions. To achieve this, two accumulator variables are used: ans, which accumulates the sum of distances, and s, which serves as the running sum of robot positions. The distance from a given robot to all robots before it in the sorted list is i \* x - s for each

robot x at index i. The product i \* x gives the sum of distances from all previous robots to the current robot if they were i units

Finally, the solution modulo 10^9 + 7 is applied to the cumulative distance sum to obtain the answer required by the problem statement. The Python code implementation follows a clear sequence and is succinct, relying on a simple enumeration pattern and basic

Example Walkthrough Let's illustrate the solution approach with a small example:

Suppose we have the array nums = [4, 1, 5] representing the starting positions of robots and a string s = "RLR" that indicates the

arithmetic to calculate the cumulative distances in the sorted array of robot positions. It does not employ complex data structures or

cumulative distance:

1. We process each position according to the direction provided. After d seconds, the new positions will be calculated as follows:

apart, while subtracting s corrects for their actual positions.

∘ For the first robot at nums [0] = 4 with direction s [0] = 'R', the new position will be 4 + 2 = 6.  $\circ$  The second robot starts at nums [1] = 1 with direction s [1] = 'L', giving us a new position of 1 - 2 = -1.

- 2. The updated array of positions then becomes [6, -1, 7].
- 3. We sort this array to get the order after d seconds: [-1, 6, 7].

○ The third robot starts at nums [2] = 5 with direction s [2] = 'R', making the new position 5 + 2 = 7.

algorithms but uses familiar constructs such as loops and sort functions effectively to derive the solution.

direction each robot will move. We are also given d = 2 seconds to simulate the movement.

- 4. To find the sum of all distances between pairs of robots after moving, we iterate through the sorted list and calculate the
- For the first robot (-1), the cumulative sum is 0. • For the second robot (6), we have (1 \* 6) - (-1) = 6 + 1 = 7.
- $\circ$  For the final robot (7), we have (2 \* 7) (6 1) = 14 5 = 9. 5. The total sum of distances is therefore 0 + 7 + 9 = 16.

 $\circ$  The distance from -1 to 6 is 6 -(-1) = 7.

 $\circ$  The distance from 6 to 7 is 7 - 6 = 1.

Now we calculate the sum of all distances:

Applying the solution modulo  $10^9 + 7$ , the final answer remains 16, since 16 is much smaller than  $10^9 + 7$ . Using this walkthrough, we gain a clear understanding of how to approach and solve the problem as outlined in the solution

 $modulo_value = 10**9 + 7$ 

total\_sum\_distance = 0

numbers[index] -= distance

else:

Python Solution class Solution:

def sumDistance(self, numbers: List[int], directions: str, distance: int) -> int:

// Initialize variables for storing the result and the cumulative sum

result = (result + i \* adjustedDistances[i] - cumulativeSum) % modulo;

long result = 0, cumulativeSum = 0;

final int modulo = (int) 1e9 + 7;

for (int i = 0; i < n; ++i) {

// Define modulo constant for large number handling

cumulativeSum += adjustedDistances[i];

// Calculate the weighted sum of distances and update result

// Update cumulative sum with the current element's value

# Define the modulo value for large numbers to prevent overflow

# Update each number in the list according to the corresponding direction character for index, direction\_char in enumerate(directions): if direction\_char == "R": # If character is "R", add the distance value numbers[index] += distance

# If character is not "R", subtract the distance value (implying "L" is encountered)

approach without directly considering robot collisions. This simplifies the calculations and allows for an efficient solution to the

## # Sort the numbers to calculate total sum distance 15 numbers.sort() 16 # Initialize variables for the answer and the cumulative sum 18

problem.

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20
            cumulative_sum = 0
21
           # Calculate the sum-distance (sum of all |Pj - Pi|)
           for index, number in enumerate(numbers):
               # The current element's contribution is its value times its index
24
25
               # minus the cumulative sum of all previous elements
26
                total_sum_distance += index * number - cumulative_sum
27
28
               # Update the cumulative sum with the current number
                cumulative_sum += number
30
31
           # Return the total sum distance modulo the defined modulo_value
32
            return total_sum_distance % modulo_value
33
Java Solution
   class Solution {
       public int sumDistance(int[] numbers, String direction, int distance) {
           // Get the length of the input array
           int n = numbers.length;
           // Create an array to store adjusted distances
           long[] adjustedDistances = new long[n];
 8
           // Calculate adjusted distances based on direction and store them
 9
           for (int i = 0; i < n; ++i) {
10
               // Subtract or add the distance based on if the direction is 'L' or 'R'
11
                adjustedDistances[i] = (long) numbers[i] + (direction.charAt(i) == 'L' ? -distance : distance);
12
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15
           // Sort the adjusted distances
           Arrays.sort(adjustedDistances);
16
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           // Return the result cast back to integer
           return (int) result;
35 }
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C++ Solution
1 #include <algorithm> // Required for std::sort
2 #include <vector>
                         // Required for std::vector
   #include <string>
                         // Required for std::string
   class Solution {
6 public:
       // Function to calculate the sum of distances based on conditions.
       int sumDistance(vector<int>& nums, string s, int d) {
           int n = nums.size(); // Get the size of the input vector 'nums'.
9
           vector<long long> adjustedPositions(n); // Create a vector to store adjusted positions.
10
11
12
           // Calculate adjusted positions based on 'L' or 'R' in string 's'.
13
           for (int i = 0; i < n; ++i) {
               adjustedPositions[i] = 1LL * nums[i] + (s[i] == 'L' ? -d : d);
14
15
16
17
           // Sort the adjusted positions to access them in non-decreasing order.
           sort(adjustedPositions.begin(), adjustedPositions.end());
18
19
20
            long long answer = 0; // Initialize the sum of distances as 0.
21
           long long prefixSum = 0; // Keep track of the sum of previous adjusted positions.
22
           const int MOD = 1e9 + 7; // Define the modulus value for avoiding integer overflow.
23
24
           // Calculate the sum of distances using prefix sums.
25
           for (int i = 0; i < n; ++i) {
26
               answer = (answer + i * adjustedPositions[i] - prefixSum) % MOD;
27
               prefixSum = (prefixSum + adjustedPositions[i]) % MOD; // Update prefix sum.
28
29
           return answer; // Return final answer.
```

// Update the result with the current index times the element minus the cumulative sum so far

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31 };

```
Typescript Solution
   function sumDistance(nums: number[], directions: string, distance: number): number {
       // Define the length of the nums array
       const length = nums.length;
       // Update the nums array by adding or subtracting the distance based on the direction
       for (let i = 0; i < length; ++i)</pre>
           nums[i] += directions[i] === 'L' ? -distance : distance;
8
9
       // Sort the nums array in ascending order
10
       nums.sort((a, b) => a - b);
11
12
13
       // Initialize the answer and a variable to keep track of the cumulative sum
       let answer = 0;
14
15
       let cumulativeSum = 0;
16
17
       // Define the modulus value to handle large numbers
       const modulus = 1e9 + 7;
18
20
       // Iterate over nums to calculate the final answer
       for (let i = 0; i < length; ++i) {</pre>
21
           // Update the answer according to the formula
           answer = (answer + i * nums[i] - cumulativeSum) % modulus;
23
24
           // Update the cumulative sum with the current number
26
           cumulativeSum += nums[i];
27
28
29
       // Return the answer
30
       return answer;
32
```

# The given code's time complexity primarily comes from the sorting operation.

Time and Space Complexity

 Sorting a list of n elements typically takes 0(n log n) time. This is the dominating factor in the time complexity of this function. The remaining part of the code iterates over the list once, which is an O(n) operation. However, since O(n log n) + O(n)

simplifies to  $O(n \log n)$ , the overall time complexity remains  $O(n \log n)$ .

For space complexity:

The given code modifies the input list nums in-place and uses a fixed number of integer variables (mod, ans, s). Thus, apart from

 However, since the input list nums itself takes O(n) space, and we consider the space taken by inputs for space complexity analysis, the overall space complexity is O(n).

Therefore, we can conclude that:

The space complexity of the code is O(n).

the input list, only constant extra space is used.

The time complexity of the code is 0(n log n).