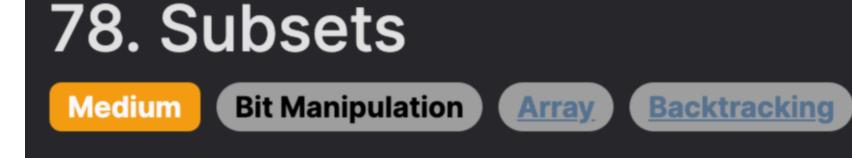
Leetcode Link



Problem Description

The LeetCode problem asks us to generate all the possible subsets from a given list of unique integers. The term 'subset' refers to any combination of numbers that can be formed from the original list, including the empty set and the set itself. For instance, if the input is [1,2,3], then the subsets would include [], [1], [2], [3], [1,2], [1,3], [2,3], and [1,2,3]. The objective is to list down all these possibilities. We should also ensure that there are no duplicate subsets in the solution and the subsets can be returned in any order.

Intuition

deciding whether to include it in the current subset (t). At each step, we have the choice to either include or not include the current element in our subset before moving to the next element. For example, if our set is [1, 2, 3], the DFS approach starts at the first element (1 then 2 then 3). For each element, we take two

To solve the problem, we are using a concept known as Depth-First Search (DFS). The process involves exploring each element and

paths: in one path we include the element into the subset, and in the other, we do not. Here's what the decision tree would look like for [1, 2, 3]:

1. Start with an empty subset []. 2. Choose whether to include 1 or not, resulting in subsets [] and [1].

- 3. For each of these subsets, choose whether to include 2, leading to [], [1], [2], and [1, 2].
- 4. Finally, for each of these, choose whether to include 3, ending with [], [1], [2], [1, 2], [3], [1, 3], [2, 3], and [1, 2, 3].

choose not to include it by simply calling dfs(i + 1) without modifying t.

systematically exploring all possible combinations without repeating them.

At the end of this process, we have explored all possible combinations, and our ans list contains all of them. Each recursive call represents a decision, and by exploring each decision, we exhaust all possibilities and build the power set.

Solution Approach The reference solution provided is a recursive approach using Depth-First Search (DFS) to build up all possible subsets. Here's a

step-by-step explanation of how the code implements this algorithm:

• We define a helper function called dfs with the parameter i, which represents the current index in the nums array we are considering.

make a copy of the current subset t and append it to our answer list ans. • If we haven't reached the end of the array, we have two choices: we can either include the current element or not. First, we

• The base case for the recursion is when i equals the length of nums. At this point, we know we've considered every element. We

- After returning from the above call, we then decide to include the current element by appending nums[i] to t. Then we call dfs(i + 1) again to continue exploring further with the element included.
- undoing the decision to include the current element. This is done by calling t.pop(). • The initial call to dfs starts with index 0, indicating that we start exploring from the first element of the array.

After the second recursive call returns, we need to backtrack, which means removing the last element added to t, essentially

- The algorithm uses a backtracking pattern, which is evident in the decision to include or not include an element and the subsequent reversal of that decision.
- The use of recursion and backtracking allows us to explore all possible combinations of elements, resulting in the power set of nums. This is because at each step we go as deep as we can into one combination (depth-first), and then we backtrack to
- explore a new one.

• The code avoids the formation of duplicate subsets by relying on the fact that nums contains unique elements and by

- The data structure used to keep track of the current subset under construction is a simple list t. The list ans collects the subsets as they are constructed. The reason we take a slice t[:] while appending to ans is to pass a copy of the current subset instead of a reference to t, which will continue to be modified as the algorithm proceeds.
- Example Walkthrough

To summarize, the solution uses a DFS approach to recursively build subsets and backtrack when necessary, adding each complete

Let's take a smaller example set [1, 2] to illustrate the solution approach. 1. Initially, our subset t is empty, and we start at index 0. The first decision is whether to include 1 in our subset or not.

2. We first choose not to include 1, so our subset t remains []. We call dfs(1) to handle the next element (index 1 now refers to 2 in

our set).

3. At index 1, again we decide whether to include 2 or not. First, we choose not to include it, so subset t remains as []. We've now

the end, we add this to ans, resulting in [[], [2], [1]].

has been considered, so we add [2] to ans, which becomes [[], [2]].

A helper function using depth-first search to find all subsets

all_subsets.append(current_subset[:])

Exclude the current element and move to the next

Once we've considered all elements, take a snapshot of the current subset

Backtrack: remove the current element before going up the recursion tree

* This method uses Depth-First Search (DFS) to explore all potential subsets.

* @param index The current index in the numbers array being explored.

// If the current index has reached the length of the array,

def depth_first_search(index: int):

depth_first_search(index + 1)

This list will hold all the subsets

if index == len(nums):

current_subset.pop()

all subsets = []

depthFirstSearch(0);

private void depthFirstSearch(int index) {

currentSubset.pop_back();

function subsets(nums: number[]): number[][] {

generateSubsets(0);

return answer;

Typescript Solution

// Start the recursion with the first index

1 // This function generates all possible subsets of the given array.

return subsetsList;

return

subset to the solution once all elements have been considered.

- considered every element, so we append this subset to our answer list ans, which now has [[]].
- 5. Now we have finished exploring the possibilities for index 1 (with element 2), so we backtrack to the situation before including 2. This means we remove 2 from our subset t by calling t.pop().

4. Backtracking to the previous choice for 2, this time we include it in the subset t, which now becomes [2]. Again, each element

move to index 1 by calling dfs(1) to make decisions for 2. 7. At index 1, we start with decision not to include 2 first, which means our subset t does not change, and is [1]. Since we are at

6. We then backtrack to the first decision at index 0 and choose the path where we include 1 in our subset. Now, t contains [1]. We

- 8. Finally, we include 2 in our subset to have [1, 2] and since all elements are now considered, we include this subset in ans, resulting in [[], [2], [1], [1, 2]].
- our example).

cover different subsets as we make different decisions (to include/not include an element). The incremental nature of adding to the

The solution methodically explores all combinations through recursive DFS calls and includes backtracking to make sure that we

subset t, along with the corresponding backtracking step, ensures the completeness and correctness of the algorithm.

to the length of nums. This ensures we include every possible combination in our ans, the list of all subsets ([], [1], [2], [1, 2] for

Throughout this process, we've been adding our subset t only when we have considered all elements, which means when i is equal

Python Solution class Solution: def subsets(self, nums: List[int]) -> List[List[int]]:

12 # Include the current element and move to the next 13 current_subset.append(nums[index]) 14 depth_first_search(index + 1) 15

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33 };

};

```
# This is a temporary list to hold the current subset
23
           current_subset = []
24
           # Start the depth-first search from index 0
25
           depth_first_search(0)
           # Return the final list of all subsets
26
27
           return all_subsets
28
Java Solution
1 class Solution {
       // A list to store all subsets
       private List<List<Integer>> subsetsList = new ArrayList<>();
       // A temporary list to store one subset
       private List<Integer> tempSubset = new ArrayList<>();
       // An array to store the given numbers
       private int[] numbers;
10
11
       /**
12
        * This is the main method that returns all possible subsets of the given array.
13
        * @param nums Array of integers for which subsets are to be found.
        * @return A list of all possible subsets of the given array.
14
15
        */
       public List<List<Integer>> subsets(int[] nums) {
16
17
           this.numbers = nums;
18
           // Start the Depth-First Search (DFS) with the first index
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// it means we've formed a subset which can now be added to the list of subsets. if (index == numbers.length) { 30 31 32 33

/**

*/

subsetsList.add(new ArrayList<>(tempSubset)); return; 34 35 // Case 1: The current number is excluded from the subset, 36 // so we simply call dfs on the next index. 37 depthFirstSearch(index + 1); 38 39 // Case 2: The current number is included in the subset. // Add the current number to the tempSubset. 40 tempSubset.add(numbers[index]); 41 42 43 // Move on to the next index to explore further with the current number included. depthFirstSearch(index + 1); 44 45 // Backtrack: remove the last number added to the tempSubset, 46 // this effectively removes the current number from the subset. tempSubset.remove(tempSubset.size() - 1); 48 49 50 } 51 C++ Solution 1 class Solution { 2 public: vector<vector<int>> subsets(vector<int>& nums) { // Initialize the answer vector to hold all subsets vector<vector<int>> answer; // Temporary vector to hold the current subset vector<int> currentSubset; // Define a recursive function to generate all possible subsets function<void(int)> generateSubsets = [&](int index) -> void { // Base case: If we have considered all numbers if (index == nums.size()) { // Add the current subset to the answer 13 14 answer.push_back(currentSubset); 15 return; 16 // Recursive case 1: Exclude the current number and move to the next generateSubsets(index + 1); 20 // Include the current number in the subset currentSubset.push_back(nums[index]); // Recursive case 2: Include the current number and move to the next 22 generateSubsets(index + 1); 24 25 // Backtrack: Remove the current number before going back up the recursion tree

```
// 'allSubsets' will store all the subsets.
       const allSubsets: number[][] = [];
       // 'currentSubset' is a temporary storage to build each subset.
       let currentSubset: number[] = [];
       // Helper function to perform depth-first search to build subsets.
       const buildSubsets = (index: number): void => {
           // If the current index is equal to the length of 'nums'
           // a subset is complete and we can add a copy to 'allSubsets'.
           if (index === nums.length) {
               allSubsets.push(currentSubset.slice());
14
15
               return;
16
           // Recursive case 1: Exclude the current element and move to the next.
           buildSubsets(index + 1);
20
           // Include the current element in the 'currentSubset'.
           currentSubset.push(nums[index]);
21
23
           // Recursive case 2: Include the current element and move to the next.
           buildSubsets(index + 1);
26
           // Backtrack: Remove the last element before going up the recursive tree.
27
           currentSubset.pop();
       };
28
29
       // Start building subsets from the first index.
       buildSubsets(0);
31
       return allSubsets;
32
33 }
34
Time and Space Complexity
The provided code is a solution for finding all subsets of a given set of numbers. This is implemented using a depth-first search
```

(DFS) approach with backtracking.

Each number has two possibilities: either it is part of a subset or it is not. Thus, for each element in the input list nums, we are making two recursive calls. This results in a binary decision tree with a total of 2ⁿ leaf nodes (where n is the number of elements in nums).

This leads to a total of 2ⁿ function calls. In each call, we deal with 0(1) complexity operations (excluding the recursive calls), such

Therefore, the time complexity of the code is 0(2ⁿ).

Space Complexity:

Time Complexity:

For space complexity, we consider two factors: the space used by the recursive call stack and the space used to store the output.

as appending an element to the temporary list t or appending the list to ans.

- 1. Recursive Call Stack: In the worst case, the maximum depth of the recursive call stack is n (the number of elements in nums), as we make a decision for each element. Hence, the space used by the call stack is O(n).
- 2. Output Space: The space used to store all subsets is the dominating factor. Since there are 2ⁿ subsets and each subset can be at most n elements, the output space complexity is $0(n * 2^n)$.

However, it is important to note that in the context of subsets or combinations problems, the space used to store the output is often considered as auxiliary space and not part of the space complexity used for algorithmic analysis. If we only consider the auxiliary space (ignoring the space for the output), the space complexity would be O(n).

Taking both aspects into account, the total space complexity of the code is $0(n * 2^n)$ considering the space for the output, or 0(n)if we are only considering auxiliary space.