

Problem Description

Given an integer n, the objective is to calculate how many trailing zeroes are found in the factorial of n, noted as n!. The factorial of a number n is the product of all positive integers from 1 to n, inclusive. Trailing zeroes in this context refer to the number of zeroes that appear at the end of the number n! before any other digit appears.

Intuition

Trailing zeroes are created by the product of the factors 2 and 5. Since the factorial of any number n will have more factors of 2 than factors of 5, the number of trailing zeroes is determined by the number of times the factor 5 is included in the factorial.

Therefore, to count the number of trailing zeroes, we need to find out how many times the number 5 can fit into the factors of all numbers from 1 to n. This is done by dividing n by 5 and adding the quotient to the count of trailing zeroes. However, numbers that are powers of 5 (such as 25, 125, etc.) are counted multiple times because they contribute more than one factor of 5. For example, 25 is 5 * 5, so it contributes two factors of 5.

The solution approach is to iteratively divide n by 5 and add the quotient to a cumulative sum until n is zero. On each iteration, n is updated by dividing it by 5. This way, we account for additional factors of 5 contributed by powers of 5. The final sum is the number of trailing zeroes in n!.

Solution Approach

The implementation of the solution leverages a simple iterative approach without the need for any complex data structures or algorithms. It makes use of basic arithmetic division and addition operations to determine the count of trailing zeroes.

Here's the step-by-step breakdown of the solution approach:

- Initialize a variable ans to 0 to hold the accumulated count of trailing zeroes.
- 2. Enter a while loop that will continue to execute as long as n is not zero. Inside the loop:
 - Perform integer division of n by 5 and update n with the quotient. This is done using the // operator in Python which is the floor division operator. It returns the largest possible integer that is less than or equal to the division result. 1 n //= 5
 - Add the updated value of n to ans. Since n was divided by 5, it now represents the number of additional factors of 5 that can be included from the updated range of numbers to n. 1 ans += n
- 3. After the loop terminates (when n is reduced to 0), ans will contain the total count of trailing zeroes in the factorial of the original n.
- 4. Return ans as the final result.

By repeatedly dividing n by 5, the solution effectively accounts for all the factors of 5 present in the factorial of n. These factors are the ones responsible for contributing trailing zeroes since there are always sufficient factors of 2 to pair with them. This process takes into account not just the single multiples of 5 but also the multiples of higher powers of 5, which contribute more than one 5 to the factorial.

There are no additional patterns or complex algorithms used in this approach as the problem can be efficiently solved with this direct method.

Let's walk through an example to illustrate the solution approach. Suppose we want to find the number of trailing zeroes in the

Example Walkthrough

factorial of n=10. The factorial of 10 is $10! = 10 \times 9 \times 8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1$.

1. We initialize ans to 0. This will keep track of the number of trailing zeroes.

Following the steps in the solution approach:

- 2. We check how many times 10 can be divided by 5:
- \circ In the first iteration, 10 // 5 = 2. So, we set n to 2 and add 2 to ans. Now ans = 2.
- 3. We continue the while loop with the updated value of n:
- - on is now 2, which is not zero, so we continue.
 - Now, 2 // 5 = 0. We set n to 0 (since 2 is less than 5, and using floor division, we get 0).
- We add 0 to ans. This does not change ans, so it remains 2. 4. The while loop ends because n is now 0.
- 5. At the end, ans = 2, which means the factorial of 10 (10!) has 2 trailing zeroes.

def trailingZeroes(self, n: int) -> int:

public int trailingZeroes(int n) {

while (n > 0) {

while (n > 0) {

n /= 5;

This small example shows how the solution approach efficiently calculates the number of trailing zeroes of a factorial by considering the powers of 5 in n!. The process of dividing n by 5 and summing the quotients ensures we count each factor of 5 present in the

factorial, leading to the correct number of trailing zeroes. **Python Solution**

Initialize zeros count to 0 zeros_count = 0

class Solution:

```
# Keep dividing n by 5 and update zeros count
           while n:
               n //= 5
               zeros_count += n
10
           # Return the count of trailing zeros in n!
11
12
           return zeros_count
13
Java Solution
  class Solution {
```

// This method calculates the number of trailing zeros in the factorial of a given number 'n'.

// Factor out the 5's, as 10 is the product of 2 and 5,

// and there are always more 2's than 5's in factorial.

int count = 0; // Initialize a counter to store the number of trailing zeros

int count = 0; // Initialize count of trailing zeroes in factorial

// Loop to divide n by powers of 5 and add to the count

* Calculates the number of trailing zeroes in n! (n factorial).

n /= 5; // Divide 'n' by 5, reducing it to the count of factors of 5

```
count += n; // Increment the count by the number of 5's factors in the current 'n'
           return count; // Return the total count of trailing zeros
9
10
11 }
12
C++ Solution
  class Solution {
   public:
       int trailingZeroes(int n) {
```

11

```
count += n; // Accumulate the number of 5's in all factors of n
12
13
           return count; // return the number of trailing zeroes in n!
14
15 };
16
Typescript Solution
1 // Calculates the number of trailing zeroes in the factorial of a given number
2 // by counting the number of multiples of 5 in the factors of the numbers that compose the factorial.
  // This is because each pair of 2 and 5 contribute to a trailing zero, and there will always
   // be more multiples of 2 than 5, so we only count the multiples of 5.
```

* @param {number} n - The input number to calculate the factorial for. * @returns {number} The number of trailing zeroes in n!. function trailingZeroes(n: number): number {

/**

```
let zeroCount = 0; // Initialize the count of trailing zeros
13
14
       // Keep dividing n by 5 and update zeroCount to count
15
       // the factors of 5 in n! as each contributes to a trailing zero
16
       while (n > 0) {
           n = Math.floor(n / 5); // Divide n by 5
           zeroCount += n; // Increment zeroCount by the quotient
19
20
21
22
       // Return the total count of trailing zeroes in n!
23
       return zeroCount;
24 }
25
Time and Space Complexity
The given Python code function trailingZeroes calculates the number of trailing zeros in the factorial of a given number n. The main
idea behind the code is that trailing zeros are created by the pair of prime factors 2 and 5, and since there are more 2s than 5s in the
```

factorial, the number of 5s will determine the number of trailing zeros. The algorithm works by iteratively dividing n by 5 to count how many multiples of 5, 25, 125, etc., are there in n! (factorial of n), as each contributes to a trailing zero.

Time Complexity:

The time complexity is determined by the number of times n can be divided by 5. This loop runs approximately log5(n) times since we divide n by 5 in each iteration until n becomes 0. Each operation inside the loop takes constant time. Hence, the time complexity

the input n.

is O(log5(n)). **Space Complexity:**

The space complexity of this algorithm is 0(1), since we only need a fixed amount of space for the variable ans, no matter the size of