1840. Maximum Building Height Hard Array Math **Leetcode Link** 

## **Problem Description** In this problem, we're tasked with determining the maximum possible height of the tallest building that can be built, given some

specific constraints. We have to build n new buildings in a line, labeled from 1 to n, with the following restrictions:

 The height of each building must be a non-negative integer. • The height of the first building must be 0.

- height as the previous one, one unit taller, or one unit shorter.
- Additionally, there's an array called restrictions that provides further limits on the height of certain buildings. This array is composed of elements [id\_i, maxHeight\_i], which means the building with label id\_i must not exceed the height maxHeight\_i. It's assured that each building appears at most once in the array, and the first building (with label 1) will not be included in the

• The height difference between any two adjacent buildings cannot exceed 1. This means each building can either be the same

The goal is to find the maximum height achievable for the tallest building among those built under these constraints. Intuition

To approach this problem, we can follow these steps: • First, we add a restriction for the first building with id 1 and height 0 since it's given that the first building's height must be 0.

#### Also, if the last building n doesn't have a restriction, we add a default restriction for it as [n, n - 1], supposing we could reach the maximum height one less than its position since each building height can increase by at most 1.

restrictions.

Then, we sort the restrictions by building id so that we can iterate through the buildings in ascending order.

tallest height before descending down to meet the next restriction.

Here's a step-by-step breakdown of the implementation:

restriction minus the difference between their ids.

- The height restrictions for buildings in between the given restrictions can be effectively calculated by a forward pass, updating the maxHeight to the minimum of its own height or the height imposed by the previous building's maxHeight increased by the difference in their ids. This ensures that a building conforms not only to its explicit restrictions but also maintains the difference of 1 height unit constraint with previous buildings.
  - We repeat a similar process in a backward pass. We iterate backward through the array and update each maxHeight to be the minimum of its own or the height possible due to the height constraint from the next building decreased by the difference in ids.
- This balances the height constraints both from forward and backward directions for each building. • The tallest possible building will be at the location where we can maximize the given constraints. To find this maximum, we examine each gap between two adjacent restrictions after the above forward and backward passes. Due to the constraint that

adjacent buildings can have at most a height difference of 1, the maximum height in a gap will be at the halfway point between

- By examining each gap and calculating this potential maximum height using the adjusted restrictions, we can determine the overall maximum height of any building. The final answer is the maximum of these potential maximum heights. The intuition behind this approach is that each restriction "ripples" through its neighbors ahead and behind, effectively spreading the constraints throughout the range of buildings. We seek a balance point within each gap between restrictions where we can attain the
- Solution Approach The solution provided uses a few important programming concepts to achieve the desired result: sorting, iteration, and comparative logic.

1. Inserting Boundary Restrictions: The code begins by appending the artificial restrictions r.append([1, 0]) for the first building, which must always be height

height of the last building n is within the permissible range subject to the incremental restriction.

their ids. This maintains the constraint that no two adjacent buildings differ in height by more than 1.

0, and r.append([n, n - 1]) for the last building, if there isn't any existing restriction for it, which ensures that the possible

• The list of restrictions r is then sorted by the building id (r.sort()), so that we can consider the restrictions in the order of

Specifically, each restriction's maxHeight is updated (r[i][1] = min(r[i][1], r[i-1][1] + r[i][0] - r[i-1][0]) to

the smaller of the existing restriction or the height allowed by the previous building's restriction plus the difference between

## • A forward iteration (for i in range(1, m):) adjusts each building's height based on the constraints "rippling forward."

3. Forward Pass:

4. Backward Pass:

building positions.

5. Finding the Maximum Height:

6. Computing the Answer:

point where both constraints meet.

Let's illustrate the solution approach with a small example.

must not exceed height 2, and building 5 must not exceed height 3.

2. Sorting Restrictions:

the two restrictions.

∘ Next, the code performs a backward iteration (for i in range(m - 2, 0, -1):) to adjust the heights based on the restrictions "rippling backward." This adjustment (r[i][1] = min(r[i][1], r[i + 1][1] + r[i + 1][0] - r[i][0]))ensures that each building's height is the smaller of the existing restriction or what is allowed by the next building's

∘ The code then enters a loop that examines the gaps between two adjacent restrictions (for i in range(m - 1):). The

• Finally, within this loop, the answer (ans) is updated to the maximum height found (ans = max(ans, t)) after each iteration.

#### potential maximum height at the midpoint of the gap is calculated as t = (r[i][1] + r[i + 1][1] + r[i + 1][0] - r[i][0]) // 2. This accounts for the "climbing up" from one restriction and "climbing down" from the next, finding the highest

The algorithm smartly leverages the given constraints in a constructive manner by first ensuring that all imposed restrictions are met and then finding the maximum height that can still be achieved within those limits. It doesn't use any complex data structures, just a list to store the restrictions and simple iterations to propagate the constraints through adjacent buildings.

Suppose we need to construct 5 buildings and the array of restrictions is restrictions = [[3, 2], [5, 3]]. This implies building 3

or is already sorted by the building ids [1, 3, 5], so we do not need to perform a sort in this case.

the restrictions. The height of building 3 remains 2, as it satisfies its restriction and the incremental rule.

### • We start by appending artificial restrictions [1, 0] for the first building and [5, 4] for the last building (since there is an existing restriction, we don't change it). Now the updated restrictions list is r = [[1, 0], [3, 2], [5, 3]].

2. Sorting Restrictions:

3. Forward Pass:

4. Backward Pass:

1. Inserting Boundary Restrictions:

**Example Walkthrough** 

 $\circ$  Now applying the backward pass: For building 3, the maxHeight becomes min(2, 3 + (5 - 3)) = 2, which is no change.

• Updated r = [[1, 0], [3, 2], [5, 3]] (no changes in this phase).

• For building 1, there is still no change as the minHeight 0 is already as low as it can be.

 $\circ$  For the gap between buildings 3 and 5, we calculate t = (2 + 3 + 5 - 3) // 2 = 3.

# If the last restriction is not for the last building, add a restriction for it

# Ensuring that each next building isn't taller than the previous plus the distance between them

# Maximum possible height between two buildings, considering their restrictions and distance

# The height of the last building can't exceed n - 1 (1-indexed)

# Update the maximum height for each building in the forward direction

# Update the maximum height for each building in the backward direction

# Making sure it follows restrictions coming from the buildings in front

# Calculate the maximum height we can achieve between each adjacent pair of buildings

// Create a list to hold the restrictions and add the initial and end restrictions

restrictionList.addAll(Arrays.asList(restrictions)); // Add all other restrictions

// Sort the list of restrictions by the building index in ascending order

Collections.sort(restrictionList, (a, b) -> Integer.compare(a[0], b[0]));

if (restrictionList.get(restrictionList.size() - 1)[0] != totalBuildings) {

restrictionList.add(new int[]{totalBuildings, totalBuildings - 1});

// Find the maximum possible height between each pair of adjacent restrictions

// Ensure an end restriction is in place if not already specified

int[] previousRestriction = restrictionList.get(i - 1);

// Backward pass: adjust restrictions based on later restrictions

int[] currentRestriction = restrictionList.get(i);

int[] currentRestriction = restrictionList.get(i);

int[] currentRestriction = restrictionList.get(i);

return maximumHeight; // Return the maximum height found

int[] nextRestriction = restrictionList.get(i + 1);

maximumHeight = Math.max(maximumHeight, maxHeightBetween);

int[] nextRestriction = restrictionList.get(i + 1);

for (int i = restrictionCount - 2; i >= 0; --i) {

for (int i = 0; i < restrictionCount - 1; ++i) {</pre>

int maximumHeight = 0;

restrictionList.add(new int[]{1, 0}); // Add a restriction for the first building, height 0

rule). 5. Finding the Maximum Height: ○ Looking at the gap between buildings 1 and 3, using (r[i][1] + r[i + 1][1] + r[i + 1][0] - r[i][0]) // 2, we calculate

 $\circ$  Final updated r = [[1, 0], [3, 2], [5, 3]] (again, no changes in this phase as the restrictions match the increasing step

• We then apply the forward pass. There is no update required for building 2, since the default increasing sequence satisfies

# $\circ$ The final answer ans is the maximum value from the calculated midpoint heights, which in this case is $\max(2, 3) = 3$ .

6. Computing the Answer:

t = (0 + 2 + 3 - 1) // 2 = 2.

restrictions.append([1, 0])

if restrictions[-1][0] != n:

restrictions.append([n, n - 1])

for i in range(1, len(restrictions)):

for i in range(len(restrictions) - 1):

# Return the maximum height found

for i in range(len(restrictions) - 2, -1, -1):

max\_height = max(max\_height, peak\_height)

public int maxBuilding(int totalBuildings, int[][] restrictions) {

List<int[]> restrictionList = new ArrayList<>();

restrictions.sort()

max\_height = 0

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C++ Solution

1 #include <vector>

2 #include <algorithm>

# Sort restrictions based on the building index

**Python Solution** class Solution: def maxBuilding(self, n: int, restrictions: List[List[int]]) -> int: # Add the first building restriction (building 1 can't exceed height 0)

restrictions[i][1] = min(restrictions[i][1], restrictions[i - 1][1] + restrictions[i][0] - restrictions[i - 1][0])

restrictions[i][1] = min(restrictions[i][1], restrictions[i + 1][1] + restrictions[i + 1][0] - restrictions[i][0])

peak\_height = (restrictions[i][1] + restrictions[i + 1][1] + restrictions[i + 1][0] - restrictions[i][0]) // 2

currentRestriction[1] = Math.min(currentRestriction[1], previousRestriction[1] + currentRestriction[0] - previousRestri

currentRestriction[1] = Math.min(currentRestriction[1], nextRestriction[1] + nextRestriction[0] - currentRestriction[0]

int maxHeightBetween = (currentRestriction[1] + nextRestriction[1] + nextRestriction[0] - currentRestriction[0]) / 2;

// Calculate potential max height between restrictions, considering the allowed increase/decrease in height

In this example, the tallest building that can be built will have a maximum height of 3. This approach illustrates how the algorithm

efficiently adheres to the constraints by working within the boundaries defined by the restrictions and incrementally adjusting the

highest feasible point that satisfies both the '1 unit height difference' rule and the height limits given in any additional restrictions.

heights of the buildings through forward and backward passes. The smart traversal of gaps between restrictions helps find the

31 return max\_height 32 Java Solution import java.util.\*;

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            int restrictionCount = restrictionList.size();
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            // Forward pass: ensure that each restriction respects the previous one
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            for (int i = 1; i < restrictionCount; ++i) {</pre>
```

class Solution {

```
using namespace std;
  6 class Solution {
    public:
         int maxBuilding(int n, vector<vector<int>>& restrictions) {
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             // Append the first restriction explicitly - starting at building 1, height is 0.
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             restrictions.push_back({1, 0});
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             sort(restrictions.begin(), restrictions.end());
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             // If there is no restriction for the last building, add it with maximum possible height.
             if (restrictions.back()[0] != n) restrictions.push back({n, n - 1});
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             // Update restrictions from left to right.
             for (int i = 1; i < restrictions.size(); ++i) {</pre>
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                 // The restriction height should be the minimum of its current value and the maximum height allowed by the previous res
                 restrictions[i][1] = min(restrictions[i][1], restrictions[i - 1][1] + restrictions[i][0] - restrictions[i - 1][0]);
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             // Update restrictions from right to left.
             for (int i = restrictions.size() - 2; i > 0; --i) {
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                 // The restriction height should be the minimum of its current value and the maximum height allowed by the next restric
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                 restrictions[i][1] = min(restrictions[i][1], restrictions[i + 1][1] + restrictions[i + 1][0] - restrictions[i][0]);
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             // Calculate the maximum height we can build for the entire range.
             int maxPossibleHeight = 0; // Initialize the answer to be the maximum possible height.
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             for (int i = 0; i < restrictions.size() - 1; ++i) {
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                 // This is the theoretical maximum height that can be achieved at the mid-point between two restrictions, taking both i
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                 int peakHeight = (restrictions[i][1] + restrictions[i + 1][1] + restrictions[i + 1][0] - restrictions[i][0]) / 2;
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                 // Update the maximum possible height if the current peak is higher.
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                 maxPossibleHeight = max(maxPossibleHeight, peakHeight);
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             // Return the maximum possible height that can be achieved.
 39
             return maxPossibleHeight;
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 41 };
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Typescript Solution
  1 function maxBuilding(n: number, restrictions: number[][]): number {
       // Append the first restriction explicitly - starting at building 1, height is 0.
       restrictions.push([1, 0]);
       restrictions.sort((a, b) => a[0] - b[0]);
```

// If there is no restriction for the last building, add it with maximum possible height.

restrictions[i - 1][1] + restrictions[i][0] - restrictions[i - 1][0]

restrictions[i + 1][1] + restrictions[i + 1][0] - restrictions[i][0]

// Update the maximum possible height if the current peak height is higher.

// Return the maximum possible height that can be achieved given the restrictions.

let maxPossibleHeight = 0; // Initialize the variable to keep track of the maximum possible building height.

// Calculate the maximum height we can build for the entire range.

maxPossibleHeight = Math.max(maxPossibleHeight, peakHeight);

if (restrictions[restrictions.length - 1][0] !== n) {

// Update the restrictions from left to right.

// Update the restrictions from right to left.

for (let i = restrictions.length - 2; i >= 0; --i) {

for (let i = 1; i < restrictions.length; ++i) {</pre>

restrictions.push([n, n - 1]);

restrictions[i][1] = Math.min(

restrictions[i][1] = Math.min(

restrictions[i][1],

restrictions[i][1],

return maxPossibleHeight;

Time and Space Complexity

#### for (let i = 0; i < restrictions.length - 1; ++i) {</pre> 29 // Calculate the maximum height at the midpoint between two restrictions. 30 let peakHeight = 31 (restrictions[i][1] + restrictions[i + 1][1] + 33 restrictions[i + 1][0] - restrictions[i][0]) /

2;

**Time Complexity** 

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The time complexity consists of the following parts: 1. Appending initial and end restrictions: 0(1) - Constant time operations to append two additional restrictions. 2. Sorting the restrictions: 0(m log m) - Sorting m restrictions where m is the number of restrictions including the two appended

- between consecutive buildings doesn't exceed the difference in their indices. 4. Backward pass to adjust the heights: 0(m) - Another single pass through the sorted restrictions in the reverse direction for the
- same purpose as in step 3. 5. Finding the maximum height: 0(m) - A final pass to find the maximum height between consecutive buildings.

3. Forward pass to adjust the heights: 0(m) - A single pass through the sorted restrictions to enforce that the height difference

- Since sorting dominates the complexity, the total time complexity is 0(m log m) where m is the number of restrictions including the added ones.
  - appended ones.

The space complexity is comprised of:

**Space Complexity** 

- 1. Storing the restrictions list with the two additional restrictions: 0(m) Where m is the number of restrictions including the two
- 2. No additional significant space is used. Thus, the total space complexity is O(m) where m is the number of restrictions including the added ones.