1031. Maximum Sum of Two Non-Overlapping Subarrays

Dynamic Programming Sliding Window

Problem Description

Array

Medium

that can be achieved by taking two non-overlapping subarrays from nums, with one subarray having a length of firstLen and the other having a length of secondLen. A subarray is defined as a sequence of elements from the array that are contiguous (i.e., no gaps in between). It is important to note that the subarray with length firstLen can either come before or after the subarray with length secondLen, but they cannot overlap.

Given an array nums of integers and two distinct integer values firstLen and secondLen, the task is to find the maximum sum

Intuition To solve this problem, an effective idea is to utilize the concept of prefix sums to quickly calculate the sum of elements in any subarray of the given nums array. By using the prefix sums, you can determine the sum of elements in constant time, rather than

recalculating it every time by adding up elements iteratively. Here's the intuition broken down into steps: Calculate prefix sums: First, we need to create an array of prefix sums s from the input array nums, which holds the sum of

the elements from the start up to the current index. Initialize variables: We then define two variables ans to store the maximum sum found so far and t to keep track of the

- maximum sum of subarrays of a particular length as we traverse the array.
- Find Maximum for each configuration: o Start by considering subarrays of length firstLen and then move on to subarrays of length secondLen. As we iterate through the array, we
- calculate the maximum sum of a firstLen subarray ending at the current index and store it in t. • Then we use this to calculate and update ans by adding the sum of the following secondLen subarray.
- We ensure that at each step, the chosen subarrays do not overlap by controlling the indices and lengths properly. Repeat the process in reverse: To ensure we are not missing out on any configuration (since the firstLen subarray can
- By iterating over each possible starting point for the firstLen and secondLen subarrays and efficiently calculating sums using the prefix array, we find the maximum sum of two non-overlapping subarrays of designated lengths.

Return the result: The maximum of all calculated sums is stored in lans, which we return as the final answer.

appear before or after the secondLen subarray), we reverse the lengths and repeat the procedure.

Solution Approach The solution is built around the efficient use of a prefix sum array and two traversal patterns to evaluate all possible

Here are the steps involved in the implementation: **Prefix Sum Array:** A prefix sum array s is constructed from the input array nums using list(accumulate(nums, initial=0)).

This function call essentially generates a new list where each element at index i represents the sum of the nums array up to

Variable t and ans: The variable t tracks the maximum sum of a subarray of length firstLen found up to the current

position in the iteration (essentially, it holds the best answer found so far for the left side). The variable ans accumulates the

maximum combined sum of two non-overlapping subarrays, comparing the sum of the current subarray of firstLen plus the

Checking for Overlapping: While updating ans, care is taken to ensure that the subarrays do not overlap by controlling the

Return the Maximum Sum: After both traversals, the variable ans holds the maximum sum possible without overlap, which is

Traverse and Compute for firstLen and secondLen: The algorithm starts off with two for loop constructs, each responsible

evaluated.

then returned.

= 2 and secondLen = 3.

Construct a prefix sum array s from nums.

Step 2: Traverse and Compute for firstLen, then secondLen

Initialize ans to -infinity (or a very small number) and t to 0.

• Start the first for loop after firstLen (index is 2 in this case).

that index.

for handling one of the two configurations: • The first for loop starts iterating after firstLen to leave room for the first subarray. Inside this loop, t is calculated as the maximum sum of the firstLen subarray ending at the current index i.

• It immediately computes the sum of the next secondLen subarray and updates the answer ans if needed, by adding the sum of the current firstLen subarray (t) and the sum of the consecutive secondLen subarray.

sequence of index increments and subarray length considerations.

configurations of the two required subarrays.

- sum of the non-overlapping subarray of secondLen. Repeat the Process for Reversed Lengths: After the first pass is completed, the same process is repeated, with the roles of firstLen and secondLen reversed. This ensures that all possible positions of firstLen and secondLen subarrays are
- subarrays of given lengths. **Example Walkthrough**

By separately handling the cases for which subarray comes first, the function ensures it examines all possible configurations

while efficiently computing sums using the prefix sum array, thus arriving at the correct maximum sum of two non-overlapping

Step 1: Prefix Sum Array

Let's walk through an example to illustrate the solution approach. Consider the array nums = [3, 5, 2, 1, 7, 3], with firstLen

 Original nums array: [3, 5, 2, 1, 7, 3] Prefix sum array s: [0, 3, 8, 10, 11, 18, 21] The element at index i in the prefix sum array represents the sum of all elements in nums up to index i-1.

We then calculate the sum of the next secondLen subarray: s[i + secondLen] - s[i] which is s[6] - s[3] so 18 - 10 = 8.

We then compute the sum of the next firstLen subarray: s[i + firstLen] - s[i] which is s[6] - s[4] so 21 - 11 = 10. We

add 10 (firstLen subarray sum) to 8 (secondLen subarray sum) and get 10 + 8 = 18 which is greater than ans, so we

We have finished evaluating both configurations. The variable ans now holds the value 18, which is the maximum sum of two

Since 8 (secondLen subarray sum) + 7 (firstLen subarray sum) = 15 is greater than ans, we update ans to 15.

At index 2 (i = 2), we ignore because we cannot form both subarrays. • At index 3 (i = 3), t = max(t, s[3] - s[3 - firstLen]) which is max(0, 10 - 3) so t = 7.

Step 4: Repeat for Reversed Lengths

Solution Implementation

from itertools import accumulate

i = first len

i += 1

i = second len

Python

Step 3: Variable t and ans

Checking for Overlapping • At index 4 (i = 4), t = max(t, s[4] - s[4 - secondLen]) which is max(0, 11 - 3) so t = 8.

We reset t to 0, and reverse the firstLen and secondLen.

• Start the next for loop after secondLen (index is 3 in this case).

• At index 3 (i = 3), we ignore because we cannot form both subarrays.

update ans to 18. **Step 6: Return the Maximum Sum**

Create a prefix sum array with an initial value of 0 for easier calculation

Initialize the answer and a temporary variable for tracking the max sum of the first array

Loop through nums to consider every possible second array starting from index first_len

Find the max sum of the first array ending before the start of the second array

Loop through nums to consider every possible first array starting from index second_len

Find the max sum of the second array ending before the start of the first array

Update the max sum with the best we've seen for the swapped sizes of the two arrays

Update the max sum with the best we've seen combining the two arrays so far

Reset the temporary variable for the max sum of first and second arrays

public int maxSumTwoNoOverlap(int[] numbers, int firstLength, int secondLength) {

// Create a prefix sum array with an additional 0 at the beginning

// Initialize the answer to be the maximum sum we are looking for

// Same as above, but first subarray has length M and second has length L

maxSum = max(maxSum, maxM + prefixSum[i + L] - prefixSum[i]);

// The `nums` array stores the integers, `L` and `M` are the lengths of the subarrays

// Return the max possible sum of two non-overlapping subarrays

function maxSumTwoNoOverlap(nums: number[], L: number, M: number): number {

let maxSum: number = 0; // Max sum of two non-overlapping subarrays

// First loop: fixing the first subarray with length L and finding optimal M

maxSum = Math.max(maxSum, maxL + prefixSum[i + M] - prefixSum[i]);

let maxL: number = 0; // Max sum of subarray with length L

let maxM: number = 0; // Max sum of subarray with length M

maxL = Math.max(maxL, prefixSum[i] - prefixSum[i - L]);

const prefixSum: number[] = new Array(n + 1).fill(0);

prefixSum[i + 1] = prefixSum[i] + nums[i];

maxM = max(maxM, prefixSum[i] - prefixSum[i - M]);

for (int i = M; i + L - 1 < n; ++i) {

return maxSum;

const n: number = nums.length;

for (let i = 0; i < n; ++i) {

for (let i = L; i + M <= n; ++i) {

// Calculate prefix sums

max sum first array = max(max sum first array, prefix sums[i] - prefix sums[i - first_len])

max sum = max(max_sum, max_sum_first_array + prefix_sums[i + second_len] - prefix_sums[i])

max sum second array = max(max sum second array, prefix sums[i] - prefix sums[i - second_len])

prefix_sums = list(accumulate(nums, initial=0))

max_sum = max_sum_first_array = 0

while i + second len - 1 < n:

max sum second array = 0

while i + first len - 1 < n:

// Initialize the length of the array

for (int i = 0; i < arrayLength; ++i) {

int[] prefixSums = new int[arrayLength + 1];

prefixSums[i + 1] = prefixSums[i] + numbers[i];

int arrayLength = numbers.length;

// Calculate prefix sums

int maxSum = 0;

class Solution: def max sum two no overlap(self, nums: List[int], first_len: int, second_len: int) -> int: # Determine the total number of elements in nums n = len(nums)

non-overlapping subarrays for the lengths provided. Thus, we return 18 as the final answer for this example.

max sum = max(max_sum, max_sum_second_array + prefix_sums[i + first_len] - prefix_sums[i]) i += 1 # Return the maximum sum found return max_sum

class Solution {

Java

```
// First scenario: firstLength subarray is before secondLength subarray
        // Loop from firstLength up to the point where a contiguous secondLength subarray can fit
        for (int i = firstLength, tempMax = 0; i + secondLength - 1 < arrayLength; ++i) {
            // Get the maximum sum of any firstLength subarray up to the current index
            tempMax = Math.max(tempMax, prefixSums[i] - prefixSums[i - firstLength]);
            // Update the maxSum with the sum of the maximum firstLength subarray and the contiguous secondLength subarray
           maxSum = Math.max(maxSum, tempMax + prefixSums[i + secondLength] - prefixSums[i]);
        // Second scenario: secondLength subarray is before firstLength subarray
        // Loop from secondLength up to the point where a contiguous firstLength subarray can fit
        for (int i = secondLength, tempMax = 0; i + firstLength - 1 < arrayLength; ++i) {
            // Get the maximum sum of any secondLength subarray up to the current index
            tempMax = Math.max(tempMax, prefixSums[i] - prefixSums[i - secondLength]);
            // Update the maxSum with the sum of the maximum secondLength subarray and the contiguous firstLength subarray
           maxSum = Math.max(maxSum, tempMax + prefixSums[i + firstLength] - prefixSums[i]);
        // Return the maximum sum found for both scenarios
        return maxSum;
C++
#include <vector>
#include <algorithm> // For std::max
using std::vector;
using std::max;
class Solution {
public:
    int maxSumTwoNoOverlap(vector<int>& nums, int L, int M) {
        int n = nums.size();
        vector<int> prefixSum(n + 1, 0);
        // Calculate prefix sums
        for (int i = 0; i < n; ++i) {
            prefixSum[i + 1] = prefixSum[i] + nums[i];
        int maxSum = 0;
        int maxL = 0; // To store max sum of subarray with length L
        // Find max sum for two non-overlapping subarrays
        // where first subarray has length L and second has length M
        for (int i = L; i + M - 1 < n; ++i) {
            maxL = max(maxL, prefixSum[i] - prefixSum[i - L]);
            maxSum = max(maxSum, maxL + prefixSum[i + M] - prefixSum[i]);
        int maxM = 0; // To store max sum of subarray with length M
```

// Second loop: fixing the first subarray with length M and finding optimal L for (let i = M; i + L <= n; ++i) {

};

TypeScript

```
maxM = Math.max(maxM, prefixSum[i] - prefixSum[i - M]);
        maxSum = Math.max(maxSum, maxM + prefixSum[i + L] - prefixSum[i]);
    // Return the max possible sum of two non-overlapping subarrays
    return maxSum;
from itertools import accumulate
class Solution:
    def max sum two no overlap(self, nums: List[int], first_len: int, second_len: int) -> int:
        # Determine the total number of elements in nums
        n = len(nums)
        # Create a prefix sum array with an initial value of 0 for easier calculation
        prefix_sums = list(accumulate(nums, initial=0))
        # Initialize the answer and a temporary variable for tracking the max sum of the first array
        max_sum = max_sum_first_array = 0
        # Loop through nums to consider every possible second array starting from index first_len
        i = first len
        while i + second len - 1 < n:
           # Find the max sum of the first array ending before the start of the second array
            max sum first array = max(max sum first array, prefix sums[i] - prefix sums[i - first_len])
           # Update the max sum with the best we've seen combining the two arrays so far
           max sum = max(max_sum, max_sum_first_array + prefix_sums[i + second_len] - prefix_sums[i])
            i += 1
        # Reset the temporary variable for the max sum of first and second arrays
        max sum second array = 0
        # Loop through nums to consider every possible first array starting from index second_len
        i = second len
       while i + first len - 1 < n:
            # Find the max sum of the second array ending before the start of the first array
           max sum second array = max(max sum second array, prefix sums[i] - prefix sums[i - second_len])
           # Update the max sum with the best we've seen for the swapped sizes of the two arrays
           max sum = max(max_sum, max_sum_second_array + prefix_sums[i + first_len] - prefix_sums[i])
            i += 1
        # Return the maximum sum found
        return max_sum
Time and Space Complexity
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list twice with while-loops. In each iteration, it performs a constant number of operations (addition, subtraction, and comparison). The space complexity of the code is O(n), due to the additional list s that is created with the accumulate function to store the prefix sums of the nums list. The size of the s list is directly proportional to the size of the nums list.

The time complexity of the given code is O(n), where n is the length of the nums list. This is because the code iterates over the