2237. Count Positions on Street With Required Brightness

Problem Description

Medium <u>Array</u>

Prefix Sum

You are provided with an integer n which represents the length of a street on a number line from 0 to n - 1. There are street lamps along this street, given by a 2D integer array named lights. Each element of lights is a pair [position_i, range_i], where position_i denotes the location of a street lamp and range_i is the range of its light. This range means the lamp can

The brightness at any position p on the street is defined as the count of street lamps that cover the position p. A separate 0indexed integer array named requirement specifies the minimum brightness required at each position i of the street.

illuminate the street from [max(0, position_i - range_i), min(n - 1, position_i + range_i)] (both ends included).

specified requirement at i.

The goal is to find and return the count of positions i on the street (between 0 to n - 1) where the brightness is at least the

Intuition

The intuition of the solution involves understanding that we need to calculate the brightness at each position on the street and

then check if it meets the requirement for that position. A key observation here is that by turning a lamp on, it increases the brightness of all positions within its range; similarly, turning it off would decrease the brightness. This is similar to an interval

update in a range query problem.

The challenge then is how to efficiently calculate the brightness at all positions, given that each lamp can affect a potentially broad range and there can be multiple overlaps from different lamps. Directly updating each range for each lamp would lead to a solution that is too slow, as each lamp could affect up to n positions.

To solve this efficiently, one can use a technique known as <u>prefix sum</u> or cumulative sum. We can increment the brightness at the starting position of a lamp's range and decrement it just after the ending position of the lamp's range. By doing this for all lamps,

we would have an array where the value at each position indicates how much the total brightness changes at that point on the street. Accumulating these changes from the beginning to the end will give us the actual brightness at each position. Once we have the brightness at each position, it's straightforward to compare it with the requirement at each position and count

the positions where the brightness is adequate. The given solution code performs exactly this:

3. Utilizes Python's accumulate function to calculate the prefix sum of brightness changes, giving the actual brightness at each position. 4. Counts the number of positions where the actual brightness meets or exceeds the required brightness.

The solution is elegant and efficient, taking advantage of subtle changes in brightness rather than brute-force updating the entire

2. Loops through each lamp and updates the d array to include the brightness change at the start and just after the end of each lamp's range.

1. Initializes an array d to store the differences in brightness.

range for every lamp, resulting in a more time-efficient approach.

generating the brightness levels for the entire street.

Let's consider an example to illustrate the solution approach.

the street, followed by a simple tally against the specified brightness requirements.

and compare it against requirements.

Example Walkthrough

- The solution uses a difference array to efficiently manage brightness updates across the range that each lamp covers. Here's a walkthrough of the steps involved in the solution:
- Initialize a difference array d, which is an auxiliary array that allows us to apply updates to the original array in constant time. In our case, the difference array is oversized to avoid boundary checks later.

Loop through each lamp's properties given in the lights array. For every lamp with parameters [position_i, range_i], calculate the starting index i and ending index j for its illumination. This is done by ensuring that the range does not exceed

the boundaries of the street, i.e., between 0 and n-1.

Solution Approach

Update the difference array d by incrementing the value at index i by 1 and decrementing the value at index j + 1 by 1. The increment at index i signifies that from this point onwards, the brightness level has increased due to the lamp, while the decrement at j + 1 marks that beyond this point, the influence of the current lamp does not extend, effectively lowering the

brightness level. Now that we have set up the difference array, we use the accumulate function in Python to compute the prefix sum, which essentially applies all the increments and decrements we've added in the difference array and yields the actual brightness

level at each index. The accumulate function will perform this operation in O(n) time across the difference array, thereby

Finally, we loop over the prefix sum result alongside the requirement array, comparing values at each position. For every position, we check if the brightness level at that index (obtained from the prefix sum) is greater than or equal to the required brightness level. We count all such occurrences where the condition is satisfied.

The overall time complexity is 0(n + m), where n is the length of the street and m is the number of lamps. This is because we

process each lamp to update the difference array once and then scan through the array of length n to compute the <u>prefix sum</u>

In summary, the code efficiently uses a difference array technique and the power of prefix sum to obtain brightness levels across

Suppose we are given: • A street of length n = 5, which is from position 0 to 4. • An array lights = [[1, 2], [3, 1]], indicating there are two street lamps. The first lamp is at position 1 with a range of 2 and can illuminate

Initialize a difference array d of size n + 1 to handle brightness changes, thus d = [0, 0, 0, 0, 0, 0]. Process the first lamp [1, 2]. The starting index i is max(0, 1 - 2) = 0 and the ending index j is min(4, 1 + 2) = 3. Update

Compute the prefix sum with the accumulate function to determine the actual brightness at each position. After using

Compare these brightness levels with requirement. At positions 0, 1, 2, and 3, the brightness equals or exceeds the

requirement, which gives us 4 positions meeting the requirement. Position 4 has a brightness of 1, which does not meet the

Process the second lamp [3, 1]. The starting index i is max(0, 3 - 1) = 2 and the ending index j is min(4, 3 + 1) = 4. Update d by incrementing d[i] and decrementing d[j + 1], which after the update gives d = [1, 0, 1, 0, -1, -1].

Let's proceed with the steps:

Solution Implementation

from itertools import accumulate

delta = [0] * (n + 1)

from typing import List

class Solution:

requirement of 2. Hence, the final answer is 4 positions with adequate brightness.

def meetRequirement(self, n: int, lights: List[List[int]], requirement: List[int]) -> int:

Create a delta array to keep track of the light increments and decrements

right_effective_index = min(n - 1, position + range)

Decrease the light intensity right after the right index

// Method to calculate the number of positions that meet the required brightness

// Calculate the effective range of light for each light bulb

int currentBrightness = 0; // Holds the cumulative brightness at each position

// Calculate the current brightness by adding the net brightness change at position i

// If current brightness meets or exceeds the requirement at position i, increase count

int positionsMeetingReq = 0; // Number of positions meeting the requirement

// Make sure the range does not go below 0 or above n-1

int start = Math.max(0, light[0] - light[1]);

// Increment brightness at the start position

currentBrightness += brightnessChanges[i];

if (currentBrightness >= requirement[i]) {

// Decrement brightness just after the end position

int end = Math.min(n - 1, light[0] + light[1]);

Increase the light intensity at the left index

Use accumulate to get the prefix sum of the delta array

which represents the actual lighting at each position

from position 0 to 3. The second lamp is at position 3 with a range of 1 and can illuminate from position 2 to 4.

We want to find the count of positions where the brightness is at least the specified requirement.

d by incrementing d[i] and decrementing d[j + 1], leading to d = [1, 0, 0, 0, -1, 0].

accumulate, the brightness levels array becomes [1, 1, 2, 2, 1, 0].

• An array requirement = [1, 2, 1, 1, 2] specifying the minimum brightness required at each position on the street.

- **Python**
- # Loop through each light's position and range to update the delta array for position, range in lights: # Calculate the left and right effective indices left_effective_index = max(0, position - range)

Determine the count of positions meeting the lighting requirement by comparing # actual lighting against the requirement and summing where the condition is true return sum(actual_lighting[i] >= requirement[i] for i in range(n)) Java

for (int[] light : lights) {

++brightnessChanges[start];

--brightnessChanges[end + 1];

// Iterate over positions from 0 to n-1

for (int i = 0; i < n; ++i) {

return satisfyingPositions;

* @param {number} n - Number of positions.

for (let light of lights) {

let brightnessAccum = 0;

lightingDiff.fill(0);

from itertools import accumulate

return satisfyingPositions;

Time and Space Complexity

leading to a space complexity of O(n).

list.

let satisfyingPositions = 0;

for (let i = 0; i < n; i++) {

// Define a global constant for the maximum number of positions

let lightingDiff: number[] = new Array(MAX_POSITIONS).fill(0);

// 'lightingDiff' is an array to keep track of the differential lighting reach at positions.

* @param {number[][]} lights - Array of light sources, each with position and range.

function meetRequirement(n: number, lights: number[][], requirement: number[]): number {

* @param {number[]} requirement - Array of lighting requirements for each position.

* @returns {number} - The number of positions that meet the lighting requirements.

// Iterate through each light source to create the differential array.

// Calculate the effective range of this light source.

let rightBound = Math.min(n - 1, light[0] + light[1]);

// Decrement the position just after the end of the range.

// 'satisfyingPositions' is the count of positions meeting the requirement.

// Return the number of positions where lighting requirements are met.

let leftBound = Math.max(0, light[0] - light[1]);

// Increment the start of the range.

brightnessAccum += lightingDiff[i];

if (brightnessAccum >= requirement[i]) {

lightingDiff[leftBound]++;

lightingDiff[rightBound + 1]--;

* The function 'meetRequirement' calculates the number of positions where the lighting requirements are met.

// 'brightnessAccum' will keep track of accumulated brightness as we move along the positions.

// If current accumulated brightness meets or exceeds the requirement, increment the count.

// Iterate through each position and sum up the differential to get the actual brightness.

};

/**

TypeScript

const MAX POSITIONS = 100010;

delta[left_effective_index] += 1

delta[right_effective_index + 1] -= 1

actual_lighting = list(accumulate(delta))[:-1]

```
public int meetRequirement(int n, int[][] lights, int[] requirement) {
   // Array 'brightnessChanges' holds the net change in brightness at each position
    int[] brightnessChanges = new int[100010];
   // Loop through the array of lights to populate the 'brightnessChanges' array
```

class Solution {

```
++positionsMeetingReq;
       // Return the total number of positions meeting the brightness requirement
       return positionsMeetingReq;
C++
class Solution {
public:
    int meetRequirement(int n, vector<vector<int>>& lights, vector<int>& requirement) {
       // Define a vector to keep track of the differential lighting reach at positions.
       vector<int> lightingDiff(100010, 0);
       // Iterate through each light source to create the differential array.
        for (auto& light : lights) {
            // Calculate the effective range of this light source.
            int leftBound = max(0, light[0] - light[1]);
            int rightBound = min(n - 1, light[0] + light[1]);
            // Increment the start of the range.
            ++lightingDiff[leftBound];
            // Decrement the position just after the end of the range.
            --lightingDiff[rightBound + 1];
       // 'brightnessAccum' will keep track of accumulated brightness as we move along the positions.
       int brightnessAccum = 0;
       // 'satisfyingPositions' is the count of positions meeting the requirement.
        int satisfyingPositions = 0;
       // Iterate through each position and sum up the differential to get the actual brightness.
        for (int i = 0; i < n; ++i) {
            brightnessAccum += lightingDiff[i];
            // If current accumulated brightness meets or exceeds the requirement, increment the count.
            if (brightnessAccum >= requirement[i]) {
                ++satisfyingPositions;
       // Return the number of positions where lighting requirements are met.
```

satisfyingPositions++; // Reset 'lightingDiff' for potential subsequent calls to 'meetRequirement' to ensure correctness

```
from typing import List
class Solution:
   def meetRequirement(self, n: int, lights: List[List[int]], requirement: List[int]) -> int:
       # Create a delta array to keep track of the light increments and decrements
       delta = [0] * (n + 1)
       # Loop through each light's position and range to update the delta array
        for position, range in lights:
            # Calculate the left and right effective indices
            left_effective_index = max(0, position - range)
            right_effective_index = min(n - 1, position + range)
```

Time Complexity The main operations within the meetRequirement function are as follows:

return sum(actual_lighting[i] >= requirement[i] for i in range(n))

Increase the light intensity at the left index

Use accumulate to get the prefix sum of the delta array

which represents the actual lighting at each position

Decrease the light intensity right after the right index

Determine the count of positions meeting the lighting requirement by comparing

actual lighting against the requirement and summing where the condition is true

delta[left_effective_index] += 1

delta[right_effective_index + 1] -= 1

actual_lighting = list(accumulate(delta))[:-1]

- 2. Using the itertools.accumulate function to compute the prefix sums of the array d. This has a time complexity of O(n) since accumulate will sum across the n elements of the d array. 3. Zipping the accumulated sums with the requirement array and iterating over it to count the number of positions meeting the requirement. The zipping has a time complexity of O(n) since it operates on two arrays of n elements each. The sum operation also takes O(n).
- Therefore, the time complexity of the complete function is 0(m + n) because 0(m) for the iterations over the lights list and 0(n)for the operations involving the d array are independent and do not nest.

1. Iterating over the lights list to populate the differences in the d array. This has a time complexity of O(m), where m is the length of the lights

- **Space Complexity** For space complexity, the main data structures that are used in the function include:
- 1. The difference array d, which has a fixed maximum size due to its initialization. This maximum size (100010) gives us a space complexity of 0(1) since it does not scale with the input size n. 2. The use of itertools.accumulate which generates an iterator. The space taken by this iterator is proportional to the number of elements in d,

3. The intermediate tuples created during the zipping process are not stored; they're generated on-the-fly during iteration, making their additional

space impact negligible. In conclusion, the space complexity of the function is O(n) due to the storage requirements of the difference array d as it scales linearly with the input size n.