1593. Split a String Into the Max Number of Unique Substrings String) Backtracking Medium **Hash Table**

Problem Description

goal is to make sure that after splitting, each substring is distinct, and their concatenation would result in the original string s. It's important to note that a substring in this context is defined as a contiguous block of characters within the string s.

Given a string s, we are tasked to find the maximum number of non-empty, unique substrings into which the string can be split. The

Intuition To solve this problem, we can use a Depth First Search (DFS) approach. The intuition behind a DFS is to explore each possible

substring starting from the beginning of the string and recursively split the rest of the string in a similar manner. For each recursive

call, we track the index at which we're currently splitting the string and maintain a count of the unique substrings created so far. In addition, we keep a record of visited substrings in a set to ensure uniqueness.

Here's the step-by-step thought process:

2. At each step, choose a substring and check if it is unique (i.e., not already in the set of visited substrings). If it's unique, add it to

1. Begin at the start of the string and consider every possible substring that can be formed starting from this position.

3. Recurse with the next part of the string, starting immediately after the selected substring, while incrementing the count of

structure to ensure the uniqueness of substrings.

the count of unique substrings formed so far.

the set to track its inclusion.

different combinations.

- unique substrings.
- 4. If you reach the end of the string, compare the count of unique substrings with a global variable that maintains the maximum count seen thus far, updating it if necessary. 5. After the recursion call, backtrack by removing the last chosen substring from the visited set, allowing it to be considered in
- 6. By the end of the DFS exploration, the global variable, ans, will contain the maximum number of unique substrings we can obtain by splitting the string.
- The use of DFS ensures we explore all possible combinations of substrings, and the use of a set (vis) makes sure that all chosen substrings are unique throughout the recursion.
- Solution Approach The solution utilizes a recursive Depth First Search (DFS) algorithm to traverse through all possibilities, and uses a set as a data

Here's a detailed walkthrough of the implementation: • Define a recursive function dfs that takes two parameters: i, which represents the current starting index of the substring, and t,

represents a higher count of unique substrings.

count stored in ans.

if i >= len(s):

obtained from s is found.

vis.add(s[i:j])

vis.remove(s[i:j])

Following the steps of the depth-first search (DFS) and backtracking algorithm:

1 def dfs(i, t):

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• Otherwise, iterate over the string s starting from index i + 1 to the end of the string. This loop represents all possible ends of the substring that starts at index i. • In each iteration, we first check if the current substring s[i:j] hasn't been visited (is not in the set vis). If it is unique:

• If i reaches the length of string s, it means we have reached the end. We compare and update the global ans variable with t if it

• Add the current substring to the vis set.

- Recurse with the new index j, which is the end of the current substring, and increment the count of unique substrings t + 1. • After recursion, remove the current substring s[i:j] from the set vis to allow for other potential unique substrings that
- could use the same segment of s. Initialize the vis set that holds the unique substrings and declare a variable ans which initially holds the value 1, since the string itself can be considered as a unique substring of length one.

• Finally, start the DFS with the initial call dfs(0, 0), and after recursive exploration of all possible splits, return the maximum

Here's a snippet of the key function from the code:

The key patterns used here are recursion for exhaustive search and backtracking for exploring different paths without repeating the

visited combinations. The set data structure is essential for assuring the uniqueness constraint for substrings.

nonlocal ans ans = max(ans, t)for j in range(i + 1, len(s) + 1): if s[i:j] not in vis:

Example Walkthrough

Let's take a small example to illustrate the solution approach using the provided problem content. Consider the string s = "abab".

2. We start the DFS by calling dfs(0, 0), signifying that we start from the beginning of the string and currently have 0 unique

This method ensures that all potential substring splits are considered, and the maximum number of unique substrings that can be

```
For the recursive call dfs(1, 1):
```

it to vis, and call dfs(4, 3).

value 1.

vis and call dfs(3, 2).

explore different combinations.

be split into - these are "a", "b", and "ab".

return

return max_unique_splits

private int maxSplitCount = 1;

public int maxUniqueSplit(String s) {

private String inputString;

this.inputString = s;

if start_index >= len(s):

nonlocal max_unique_splits

For the recursive call dfs(3, 2):

For the recursive call dfs(4, 3):

We backtrack and remove "ab" from vis.

substrings.

First, consider i = 0:

• Now i = 1; we take s[1:2] which is "b", add it to vis, and call dfs(2, 2). For the recursive call dfs(2, 2):

■ i = 2; we can't choose "a" again (as s[2:3]) because it is already in vis. Hence, we move to s[2:4], which is "ab", add

• i = 4; we have reached the end of the string. We compare and update ans with 3 which is greater than the initial

1. We begin with an empty set vis for maintaining unique substrings and a variable ans initialized to 1.

• We take the substring s [0:1] which is "a" and since it's not in vis, we add it to vis and call dfs(1, 1).

■ The calls dfs(3, 3) and previous layers would not produce any further unique substrings, so we backtrack completely to the first call after "b" and s[1:2] is removed from vis. • Back in dfs(1, 1), we continue looking for substrings and try s[1:3] which is "ab". It's unique at this point, so we add it to

• i = 3; we choose s[3:4] which is "b", add it to vis, and call dfs(4, 3).

For the recursive call dfs(4, 3): • i = 4; we are at the end of the string. ans is again compared and updated if necessary, but it remains 3.

In each recursive call, after we reach the end, we backtrack by removing the last inserted substring from vis. This allows us to

Python Solution class Solution: def maxUniqueSplit(self, s: str) -> int: def backtrack(start_index, unique_count):

Base Case: If the starting index reaches or exceeds the length of the string

Try to split the string from the current index to all possible subsequent indexes

Backtrack: remove the substring from the set to try other possibilities

Update the maximum number of unique splits

for end_index in range(start_index + 1, len(s) + 1):

If this substring has not been seen before

backtrack(end_index, unique_count + 1)

Initialize a set to keep track of seen substrings

Return the maximum number of unique splits found

// Variable to store the maximum number of unique splittings

// Main method that is called to get the max unique split count

// Start recursive depth-first search from index 0 with count 0

unordered_set<string> visited; // Set to store visited substrings

// The DFS function to explore all possible unique splits

maxCount = max(maxCount, uniqueCount);

if (!visited.count(currentSubstring)) {

// Mark the substring as visited

dfs(endIndex, uniqueCount + 1);

visited.erase(currentSubstring);

visited.insert(currentSubstring);

void dfs(int startIndex, int uniqueCount) {

if (startIndex >= inputString.size()) {

// The main function to be called to find the maximum number of unique splits

dfs(0, 0); // Begin the depth-first search (DFS) from the first character

// Base case: if the index has reached or exceeded the size of the string

// Check if the substring has not been visited (i.e., is unique)

for (int endIndex = startIndex + 1; endIndex <= inputString.size(); ++endIndex) {</pre>

string currentSubstring = inputString.substr(startIndex, endIndex - startIndex);

// Recursively call dfs with the updated parameters to proceed with the next part of the string

// Backtrack: erase the current substring from visited set as we return from the recursion

// Update the maximum count of unique splits found so far

// Iterate through the string, attempting to split at each index

// Generate the current substring using substr

// Initialize inputString with the input parameter

// The input string on which splitting is performed

if s[start_index:end_index] not in seen_substrings:

seen_substrings.add(s[start_index:end_index])

max_unique_splits = max(max_unique_splits, unique_count)

Add the substring to the set of seen substrings

seen_substrings.remove(s[start_index:end_index])

At the end of the DFS, ans will contain the value 3, which is the maximum number of non-empty, unique substrings that "abab" can

22 seen_substrings = set() 23 # Initialize the maximum number of unique splits variable 24 max_unique_splits = 1 # Start the recursive backtracking process from the beginning of the string 26 backtrack(0, 0)

Continue splitting the rest of the string with one additional unique substring found

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1 class Solution {
      // HashSet to keep track of visited substrings
      private Set<String> visited = new HashSet<>();
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Java Solution

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           dfs(0, 0);
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           // Return the maximum number of unique splittings found
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           return maxSplitCount;
21
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23
       // Recursive Depth-First Search method to split the string and track maximum unique splitting
       private void dfs(int startIndex, int splitCount) {
24
           // Base case: if we have reached the end of the string
25
26
           if (startIndex >= inputString.length()) {
27
               // Update the maxSplitCount with the maximum value between current max and current split count
28
               maxSplitCount = Math.max(maxSplitCount, splitCount);
29
               return; // End the current branch of recursion
30
           // Recursive case: try to split the string for all possible next positions
31
32
            for (int endIndex = startIndex + 1; endIndex <= inputString.length(); ++endIndex) {</pre>
33
               // Get the current substring to be considered
34
               String currentSubstring = inputString.substring(startIndex, endIndex);
35
36
               // Check and add the current substring to the visited set if it's not already present
               if (visited.add(currentSubstring)) {
37
                   // Continue search with the next part of the string, increasing the split count
38
39
                   dfs(endIndex, splitCount + 1);
40
                   // Backtrack and remove the current substring from the visited set
41
                   visited.remove(currentSubstring);
44
45
46 }
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C++ Solution
 1 #include <unordered_set>
 2 #include <algorithm>
 3 #include <string>
   using namespace std;
   class Solution {
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// Store the maximum count of unique splits

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public:

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string inputString;

int maxCount = 1;

int maxUniqueSplit(string s) {

inputString = s;

return maxCount;

return;

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Typescript Solution
1 // Importing a set equivalent in TypeScript
   import { Set } from "typescript-collections";
   // Global variable to store visited substrings
5 const visited = new Set<string>();
6 // Global variable for the input string
7 let inputString: string;
  // Global variable to store the maximum count of unique splits, initially 1
   let maxCount: number = 1;
10
   // Function to find the maximum number of unique splits in a string
   function maxUniqueSplit(s: string): number {
       inputString = s;
13
       dfs(0, 0); // Begin the depth-first search (DFS) from the first character
14
       return maxCount;
17
  // Recursive DFS function to explore all possible unique splits of the string
   function dfs(startIndex: number, uniqueCount: number): void {
       // If the startIndex reaches or exceeds the length of the inputString, we update maxCount if necessary
20
       if (startIndex >= inputString.length) {
21
22
           maxCount = Math.max(maxCount, uniqueCount);
23
           return;
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26
       // Iterate through the string, attempting to split at each possible position
27
       for (let endIndex = startIndex + 1; endIndex <= inputString.length; ++endIndex) {</pre>
28
           // Generate a substring based on the current start and end indices
29
           let currentSubstring: string = inputString.substring(startIndex, endIndex);
30
31
           // Check if this substring hasn't been seen before
32
           if (!visited.contains(currentSubstring)) {
33
               // Mark this substring as visited
34
               visited.add(currentSubstring);
35
36
               // Recursively call dfs on the next segment of the string
37
               dfs(endIndex, uniqueCount + 1);
38
39
               // Backtrack by removing the current substring from the visited set
40
               visited.remove(currentSubstring);
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   // Note: The Set collection may not have exactly the same API as the JavaScript Set.
  // If using 'typescript-collections' doesn't match the expected behavior, you would have to
47 // implement the Set functionality to appropriately reflect the expected behavior or find an
   // appropriate library that mimics the JavaScript Set API closely.
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```

substrings that can be split from a given string. To determine the time complexity, consider each step in the code:

Time and Space Complexity

Time Complexity

string is reached.

substring.

A substring is added to the vis set only if it's not already seen. This operation takes O(k) where k is the length of the substring,

- as strings are immutable in Python and need to be hashed for insertion in a set. Since we consider every possible split for a string of length n, and in each step we could potentially generate all possible substrings,
- the worst-case is exponential in nature with respect to the input size. The worst-case time complexity is therefore $0(n * 2^n)$, because at each of the n positions, we could make a decision to split or not

to split the string, and we are doing this for all n positions except the last one which is determined by the choices made for the

The provided code implements a depth-first search (DFS) approach to solve the problem of finding the maximum number of unique

• The dfs function is called recursively, considering all possible splits starting at different positions in the string until the end of the

In each function call, it performs a loop from i + 1 to len(s) + 1, exploring all the possibilities for the next starting point of a

previous substrings. Space Complexity

• The set vis stores the unique substrings we have encountered. In the worst case, it can store all possible substrings of s, which

Looking at the space complexity:

- amounts to 0(2^n) substrings if we consider all possible splits. • The recursion depth can go up to n in the case of splitting each character as a separate substring. Hence, the space complexity due to recursive calls is O(n).
- Therefore, combining the storage for the set and the recursive call stack space, the overall space complexity is 0(2ⁿ + n), where 0(2ⁿ) is the dominant term, simplifying the space complexity to 0(2ⁿ).