Hash Table

Dynamic Programming

Problem Description In this problem, you're given an array of integers called nums, where each element represents points you can earn. The goal is to

Medium Array

accumulate the highest number of points possible by repeatedly performing a specific operation. The operation consists of the following steps:

1. Choose any element from the array (nums [i]) and earn points equal to its value (nums [i] points).

- 2. Once you've earned points from nums [i], you must then delete every element from the array that is either 1 less (nums [i] 1) or
- 1 more (nums [i] + 1) than the chosen element.

You can repeat this operation as many times as you wish in order to maximize your points. The challenge resides in selecting the

The task is to determine the maximum number of points you can earn by applying the operation optimally. Intuition

The key observation to solve this problem is recognizing that if you choose any number, you should take all instances of that number

elements in an order that prevents you from eliminating potential points that could have been earned later on.

To approach this, you can leverage dynamic programming. The first step is to create an array, sums, to accumulate the total sum of

occurrences of i in nums. Now, since you cannot pick numbers adjacent to each other (i.e., nums[i], nums[i]-1, and nums[i]+1 are mutually exclusive choices),

points that each unique number in nums can contribute. Essentially, for each value i, sums[i] holds the total points from all

 select[i]: the maximum sum you can obtain if you choose to take i. nonSelect[i]: the maximum sum you can obtain if you decide not to take i.

The state transitions work as follows: If you take the number i, you couldn't have taken i - 1, so your current maximum if you select i is the maximum of not selecting

If you don't take 1, the maximum is the larger of the previous maxima regardless of whether 1 - 1 was selected or not.

because choosing one instance will force you to delete the others anyway.

The relationship can then be defined as:

maximum value between choosing and not choosing the last element in the array.

numbers. The approach ensures that the solution is derived efficiently with optimal space usage.

We initialize the total array with the size mx + 1 (since arrays are 0-indexed).

We start iterating from 2 to mx (inclusive) to update the first and second states:

The solution iterates over the values, updating select and nonSelect based on the points from sums. The final solution will be the

Solution Approach

1 select[i] = nonSelect[i - 1] + sums[i]

2 nonSelect[i] = max(select[i - 1], nonSelect[i - 1])

of algorithms and data structures to reach an optimal solution.

2. Calculating total points for each number:

you should maintain two states:

i - 1 plus the sum of i.

The given Python solution implements this using a simplified dynamic programming approach with a single array, total, which plays the role of sums, and two variables, first and second, to keep track of the select and nonSelect states for the last two processed

1. Pre-processing step: We go through the nums array to find the maximum number (mx) among all the numbers, as it will determine the size of the total array, which is analogous to the sums array in the reference approach. This total array holds the aggregate points that each number contributes.

The solution follows a bottom-up dynamic programming approach where the operation of choosing a number encompasses a couple

We iterate through the nums array once again to sum the points for each number. For each num in nums, we add num to

4. Iterative Optimization:

total [num], which is adding the points for each occurrence of that number. 3. Dynamic Programming (DP) State Transition:

We define two states, first and second. Respectively, they correspond to nonSelect and select for two consecutive

elements being processed in a DP manner. In the reference approach, select and nonSelect arrays are used, while in the

- solution code we only use two variables for space optimization. • Initialize these variables as follows: first = total[0], as this is the point contribution for the number 0. second = max(total[0], total[1]), as this is the maximum between choosing 0 and choosing 1 but not choosing 0.
- For each number i, the current maximum points cur when choosing the number i is computed as max(first + total[i], second) which follows the transition:

whether i-1 was chosen or not.

first gets the value of second.

second gets the value of cur.

• We then update first and second for the next iteration:

- If we choose i, we add the points from choosing i (total[i]) to the maximum points without including i-1 (first). This reflects the concept that if we are taking number i, we must have not taken i-1. ■ If we don't choose i, the maximum stays at second which is the larger of the previous maxima irrespective of
- 5. Returning the Result: After the loop, second will hold the maximum number of points that can be achieved from 0 to mx, as it either includes or excludes the last number. Therefore, we return second as the solution.

By employing this dynamic programming technique, the problem avoids brute-force repetitions and overcomes the potential

exponential time complexity we would face if we tried every possible combination of elements to delete from the nums array. This

implementation ensures that the solution is reached in O(n + k) time, where 'n' is the length of nums and 'k' is the range of numbers in

Let's consider a small input array nums containing the following elements: [3, 4, 2, 2, 3, 4]. 1. Pre-processing step: We find the maximum number in nums, which is 4.

For i=2, we calculate cur = max(first + total[2], second) which is max(0+4, 0) resulting in cur = 4. Update first to 0

The loop ends with second being 12, which signifies that by following the described selection process, we have maximally

Initialize second = max(total[0], total[1]) which is max(0, 0) because the number 1 does not appear in nums. Thus, second is 0.

nums.

Example Walkthrough

2. Calculating total points for each number:

4. Iterative Optimization:

Initialize first = total[0] which is 0 (no contribution from the number 0).

We initialize the total array with a length of 5 (0-indexed, so we go from 0 to 4).

By iterating through nums, we calculate the total as follows:

total[3] would be 6 (two 3's, so 3*2=6).

total[4] would be 8 (two 4's, so 4*2=8).

3. Dynamic Programming (DP) State Transition:

total[2] would be 4 (because there are two 2's and 2*2=4).

(previous second) and second to 4. • For i=3, we calculate cur = max(first + total[3], second) which is max(0+6, 4) resulting in cur = 6. Update first to 4

5. Returning the Result:

Python Solution

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15 }

};

from typing import List

for num in nums:

and second to 6. • For i=4, we calculate cur = max(first + total[4], second) which is max(4+8, 6) resulting in cur = 12. Update first to 6 and second to 12.

 $total_points = [0] * (max_value + 1)$

total_points[num] += num

earn_prev_prev = total_points[0]

for i in range(2, max_value + 1):

earn_prev_prev = earn_prev

earn_prev = current_max

// Return 0 if the array is empty

int[] valueSums = new int[10010];

int[] dpSelect = new int[10010];

int[] dpNonSelect = new int[10010];

// Variable to store the maximum value in nums

maxValue = Math.max(maxValue, num);

for (int i = 1; i <= maxValue; i++) {

for (int i = 1; i < values.size(); ++i) {</pre>

prevMax = currentMax;

currentMax = tempMax;

function deleteAndEarn(numbers: number[]): number {

cumulativeValues[num] += num;

// following the delete and earn rule.

return currentMax;

for (let num of numbers) {

return rob(cumulativeValues);

function rob(values: number[]): number {

Typescript Solution

// Calculate the new max amount that can be earned

// including the current number or by excluding it.

int tempMax = max(values[i] + prevMax, currentMax);

// update currentMax to the newly calculated tempMax.

// At the end, currentMax will contain the maximum amount that

// can be earned by either taking or skipping each number.

// Populate cumulativeValues so that each index's value is the sum

// of all occurrences of that number in the input numbers array.

// Use the rob function to find the maximum amount we can earn

// Initialize variables to keep track of the two states:

// prevMax stores the maximum amount we can get from [0...i-2]

// currentMax stores the maximum amount we can get from [0...i-1]

// The rob function uses dynamic programming to calculate the maximum earnable amount.

// c decides whether to take the current number or not.

// Move currentMax to prevMax for the next iteration, and

if (nums.length == 0) {

return 0;

int maxValue = 0;

for (int num : nums) {

valueSums[num] += num;

Fill the total_points list where the index represents the number

total points earned up to the previous and current positions

// Create an array to store the sum of points for each number

// Populate the valueSums array and find the maximum value

dpSelect[i] = dpNonSelect[i - 1] + valueSums[i];

dpNonSelect[i] = Math.max(dpSelect[i - 1], dpNonSelect[i - 1]);

// Create an array to store the maximum points if we select the current number

// Create an array to store the maximum points if we do not select the current number

// Dynamic programming to decide whether to select or not select a particular number

// If we select i, we can't use i-1, so we add the points of i to dpNonSelect[i-1]

// If we don't select i, take the maximum points from the previous selection or non-selection

Iterate over the total_points list starting from the second index

current_max = max(earn_prev_prev + total_points[i], earn_prev)

Update the points from two steps before and the previous step

Initialize first and second variables to store the

earn_prev = max(total_points[0], total_points[1])

- earned 12 points. Therefore, for the array [3, 4, 2, 2, 3, 4], the maximum number of points that can be earned is 12.
- class Solution: def deleteAndEarn(self, nums: List[int]) -> int: # Find the maximum value in nums array max_value = max(nums) # Create a list to store the total points for each number

30 # The last 'earn_prev' contains the maximum points that can be earned 31 32 return earn_prev 33

Calculate the current max points by either taking the current number

and the points from two steps before, or the points from the previous step

and the value at that index is the total points that can be earned from that number

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public class Solution {
    // Method to calculate the maximum points you can earn by deleting elements
    public int deleteAndEarn(int[] nums) {
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Java Solution

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           // The result is the max points of selecting or not selecting the highest value
           return Math.max(dpSelect[maxValue], dpNonSelect[maxValue]);
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35 }
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C++ Solution
 1 class Solution {
2 public:
       // The deleteAndEarn function.
       int deleteAndEarn(vector<int>& numbers) {
           // We create vals with size enough to cover all potential
           // input numbers, initializing with 0s. This will store the cumulative values.
           vector<int> cumulativeValues(10001, 0);
           // Populate cumulativeValues so that each index's value is the sum
           // of all the occurrences of that number in the numbers vector.
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           for (int num : numbers) {
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               cumulativeValues[num] += num;
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           // Now we use our rob function to find the maximum amount we can earn
           // following the delete and earn rule.
           return rob(cumulativeValues);
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       // The rob function uses dynamic programming to find the maximum earnable amount.
       int rob(vector<int>& values) -
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           // Initialize the two variables to keep track of two states:
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           // prevMax: the maximum amount we can get from [0...i-2]
           // currentMax: the maximum amount we can get from [0...i-1]
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           int prevMax = 0, currentMax = values[0];
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1 // Define an array to represent the cumulative values of numbers. let cumulativeValues: number[] = new Array(10001).fill(0); // The deleteAndEarn function, which takes an array of numbers and returns the maximum points that can be earned.

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       let prevMax = 0;
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       let currentMax = values[0];
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       for (let i = 1; i < values.length; i++) {
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           // Calculate the tempMax which is the new maximum amount that can
           // be earned by including or excluding the current number.
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           let tempMax = Math.max(values[i] + prevMax, currentMax);
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           // Update prevMax to the previous currentMax for the next iteration,
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           // and set currentMax to the newly calculated max (tempMax).
           prevMax = currentMax;
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           currentMax = tempMax;
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       // currentMax will hold the maximum amount that can be earned
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       // after considering all the numbers.
       return currentMax;
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39 }
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Time and Space Complexity
The provided code is designed to solve the problem by first calculating the maximum value in the list of numbers, creating an array
that sums the same elements' values, and then using a dynamic programming approach similar to the house robber problem. The
complexities are as follows:
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The time complexity of the algorithm is O(N + M), where N is the length of the nums array and M is the maximum number in the nums. This is because:

Time Complexity

1. The first for loop which calculates the maximum number, mx, iterates over all elements in nums, which takes O(N). 2. The second for loop creates the total array by summing the value of each number where the num appears. This also takes O(N) time as it iterates over all elements in nums.

3. The third for loop iterates over the range from 2 to mx, to calculate the maximum points that can be earned without adjacent

- Therefore, adding these up we get O(N) + O(N) + O(M) which simplifies to O(N + M) as the dominant terms.
- **Space Complexity** The space complexity of the algorithm is O(M), where M is the maximum number in nums. This is due to:

Therefore, the additional space used by the algorithm is predominated by the size of the total array.

numbers. This runs in O(M) time, where M is the maximum number in nums.

1. The total array, which has a length of mx + 1, accounting for all numbers from 0 to mx inclusive. 2. Constant space for variables first, second, cur, and mx.