Problem Description

the goal is to determine the root node of the given N-ary tree.

In this problem, we are given all the nodes of an N-ary tree in the form of an array of Node objects. Each Node has a unique value, and

Leetcode Link

An N-ary tree is a tree in which a node can have any number of children (0 or more). The array provided does not directly show the structure of the tree or the parent-child relationships. Instead, we need to infer which one of these nodes is the root based on the details given.

To aid in this, we have a way to serialize the tree through its level order traversal: each group of children is followed by a null value to indicate the end of that particular level of children. The given example uses serialization to show the structure of an N-ary tree.

ary tree. A key aspect of the problem is that the underlying tree structure is not provided explicitly, and we have to determine the root node without reconstructing the tree.

Our task is to implement a function, findRoot, which will receive an unsorted array of Node objects and must return the root of the N-

twice—once as a node value and once as a child value.

The intuition behind the provided solution involves using a property of XOR (exclusive or) operation, which is that $x \land x = \emptyset$ for any integer x, and x ^ 0 = x. In essence, if you XOR an even number of the same number, you get 0, but if you have an odd number of a number (which would be the case with the root value because it is not someone's child), you'd be left with that number. To find the root of the tree, the solution exploits the fact that the root is the only node that does not appear as a child of any other

node. By XOR'ing all the values of the nodes and their children, every node except the root will cancel out because they will appear

The algorithm iterates through all nodes, XOR'ing the node's value and XOR'ing the values of its children. Since all nodes except the

root will appear twice and XOR'ing a number with itself yields 0, the final result of the XOR operations will be the value of the root node, because it's the only one that doesn't get canceled out. At the end of the XOR operation, we are left with a value that corresponds to the root node's value. We can then easily find the root

matches. **Solution Approach**

node by comparing the value obtained from our XOR operation with the values of each node in the array and returning the node that

The solution implements an efficient approach to find the root of an N-ary tree without rebuilding the tree structure. The primary algorithmic idea uses bitwise XOR (exclusive or) to identify the root node. The XOR operation has a unique property where XORing a number with itself results in 0, and XORing a number with 0 gives the number back. Furthermore, XOR is commutative and associative, which means the order of operations does not matter.

1. Initialize an accumulator variable x to 0. This variable will be used to collect the result of consecutive XOR operations. 2. Iterate over each node in the tree array. a. XOR the node's value with the accumulator x. b. Iterate over each child of the current

node and XOR the child's value with x.

The implementation uses two for loops:

The first is to apply the above-described XOR operations.

def findRoot(self, tree: List['Node']) -> 'Node':

XOR the values of children

for child in node.children:

nodes without explicit parent-child linkage information.

Let's illustrate the solution approach with a small example.

x ^= child.val

Algorithm:

3. After the completion of the iterations, x will hold the value of the root node. This occurs because the root is the only node not XOR'd twice (once as a node and once as a child). 4. Iterate through the tree array again and find the node with the value equal to x. This is the root node.

The second is to find and return the node whose value matches the result of the XOR operations.

Patterns:

- **Data Structures:**
- The primary data structure used for storing nodes is the given array tree, which holds Node objects. A single integer x is used to accumulate the XOR results.

The provided solution utilizes minimal additional space and performs the task in linear time relative to the number of nodes, making it

Bit manipulation via XOR is the main pattern that allows us to avoid reconstructing the entire tree.

an efficient approach for this problem.

x ^= node.val

Reference Solution Code:

1 class Solution:

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for node in tree: # XOR the node's value

Identify the node with the accumulated XOR value (the root)

return next(node for node in tree if node.val == x)

The next function in the last line is a Python built-in that returns the next item from the iterator, in this case, the node for which node.val == x.

As we can see from the code, the solution is concise, leveraging the XOR operation to cleverly discern the root node from a pool of

3 (Here, "1 -> [3, 5, 6]" means that the node with value 1 has children with values 3, 5, and 6, and similarly for the others.)

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Suppose we are given an array of Node objects representing an N-ary tree:
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1 tree = [

Initial x: 0

4)

Python Solution

class Node:

class Solution:

Java Solution

class Node {

import java.util.List;

2 import java.util.ArrayList;

// Definition for a Node.

public List<Node> children;

public Node(int value) {

val = value;

val = value;

int xorSum = 0;

class Solution {

children = new ArrayList<>();

children = new ArrayList<>();

public Node findRoot(List<Node> tree) {

children = childrenList;

for (Node node : tree) {

xorSum ^= node.val;

public Node(int value, ArrayList<Node> childrenList) {

// Function to find the root of the given N-ary tree.

// Iterate through each node of the tree

for (Node child : node.children) {

// Xor the value of each child

return node; // Return the root node.

* Find the root of a tree based on the property that the root's value

let xorSum = 0; // This will hold the XOR sum of all node values.

// XOR the values of the current node's children.

// Iterate over all nodes in the tree.

xorSum ^= child.val;

// XOR the current node's value.

for (const child of node.children) {

for (const node of tree) {

xorSum ^= node.val;

grow with the size of the input.

// Note: The infinite loop in the original code is removed as the return within the loop

// will always exit the method once the root node is found or the loop ends.

// In case no root is found (which shouldn't happen), return nullptr.

// Xor the current node value

xorSum ^= child.val;

// Initialize a variable that will be used for xor operation

// Iterate through the children of the current node

public int val;

public Node() {

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Definition for a Node in a tree.

xor_sum = 0

for node in all_nodes:

xor_sum ^= node.value

for child in node.children:

xor_sum ^= child.value

Node(5),

Node(6),

Example Walkthrough

1 Nodes: [1, 2, 3, 4, 5, 6]

2 Edges: 1 -> [3, 5, 6], 2 -> [4], 3 -> [2]

Node(3, [Node(2, [Node(4)])]),

Node(2, [Node(4)]), Node(4) 8]

Let's walk through the XOR operation as described:

Processing Node(5): x = x ^ 5 (x becomes 1)

Processing Node(6): x = x ^ 6 (x becomes 7)

So our Node objects array (unsorted) could look something like this:

Node(1, [Node(3, [Node(2, [Node(4)])]), Node(5), Node(6)]),

Though the problem doesn't provide the tree structure, this is added here for illustrative purposes.

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• Processing Node(1): x = x ^1 (x becomes 1) Child Node(3): x = x ^3 (x becomes 2) Child Node(5): x = x ^5 (x becomes
 7) Child Node(6): x = x ^ 6 (x becomes 1)
• Processing Node(3): x = x ^ 3 (x becomes 2) Child Node(2): x = x ^ 2 (x becomes 0) Child Node(4): x = x ^ 4 (x becomes
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 Processing Node(2): x = x ^ 2 (x becomes 5) Child Node(4): x = x ^ 4 (x becomes 1) Processing Node(4): x = x ^ 4 (x becomes 5)

itself out and leaving us with x = 1 at the end, which is the value of the root.

The given code is already written in Python 3 syntax, but I will revise it to

Loop over each node and its children in the list of all nodes.

Loop over the children of the current node.

self.children = children if children is not None else [] # Child nodes

2 # include clearer variable names and add comments to enhance readability.

self.value = value # The value contained in the node

def __init__(self, value=None, children=None):

Class to encapsulate the solution methods.

Using this approach, the algorithm identifies the root node without reconstructing the tree's structure. It is efficient because each node and its children are processed exactly once, with the XOR operation ensuring that only the root node's value remains at the end.

Notice how every node that is not the root appeared twice in the XOR operation due to being a child of some other node, canceling

Method to find the root of a tree where all nodes are present in an array. # The tree has no cycles and each child has exactly one parent, so the root 14 # has no parent. def findRoot(self, all_nodes: List['Node']) -> 'Node': 16 # Initialize an integer to use it for XOR operation.

XOR is used because it cancels out when applied to a pair of the same numbers.

it will appear only once and stay in the xor_sum as all other non-root

XOR each child's value as well, cancelling out their values.

XOR the node's value with the xor_sum. If it's the root's value,

nodes will be cancelled out with their children counterpart.

Now, we can go through the array of nodes again to find the node with value 1, which is our root node.

31 32 # After the above operation, the xor_sum will contain the value of the root node only. 33 # Loop over the nodes once more to find the node with the same value as the xor_sum. 34 return next(node for node in all_nodes if node.value == xor_sum) 35

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           // After the above loops, xorSum will have the value of the root node (as it's only counted once)
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           // Now, search for the node with the value equal to xorSum (which is the root)
            for (Node potentialRoot : tree) {
                if (potentialRoot.val == xorSum) {
                    // If the value matches, we have found the root
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                    return potentialRoot;
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           // The code should never reach this point, as the root must be in the tree,
           // we do not need to handle the case where the root isn't found
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            return null; // This return added just to satisfy the function's return type contract
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C++ Solution
   #include <vector>
   // Forward declaration for Node.
   class Node{
   public:
       int val; // Node's value
       std::vector<Node*> children; // Children of the node
       // Constructor for a node without children.
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       Node() {}
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       // Constructor for a node with a given value.
       Node(int _val) {
           val = _val;
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       // Constructor for a node with a given value and a list of children.
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       Node(int _val, std::vector<Node*> _children) {
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           val = _val;
           children = _children;
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22 };
23
   class Solution {
25 public:
       Node* findRoot(std::vector<Node*> tree) {
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            int xorSum = 0; // Initialize the XOR accumulator.
           // Calculate the XOR of all the node values and their children's values.
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           for (Node* node : tree) {
               // XOR with the current node's value.
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               xorSum ^= node->val;
               // XOR with each of the node's children values.
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                for (Node* child : node->children) {
35
                    xorSum ^= child->val;
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           // Find the node whose value is equal to the xorSum result,
39
           // this is the root node because its value will only be counted once (all other nodes will be counted twice).
            for (Node* node : tree) {
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                if (node->val == xorSum) {
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* will appear an odd number of times when XOR'ing all values together. * @param {INode[]} tree - An array of nodes representing a tree. * @return {INode | null} - The root node or null if not found. 11 */ function findRoot(tree: INode[]): INode | null {

interface INode {

val: number;

return nullptr;

Typescript Solution

children: INode[];

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       // Find and return the node whose value matches the xorSum.
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       // This is the root node, as its value will only be XOR'd once.
27
       return tree.find(node => node.val === xorSum) || null;
28
29 }
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Time and Space Complexity
The provided code calculates the root of an N-ary tree. It uses bitwise XOR to identify the root node, under the assumption that each
value in the tree is unique.
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code iterates through all nodes exactly once and iterates once more through all the children of each node.

• Time Complexity: The time complexity of the code is O(N), where N is the total number of nodes in the tree. This is because the

because the code only uses a variable x to keep track of the XOR operation and does not use any additional data structures that

• Space Complexity: The space complexity of the function is 0(1), not considering the space taken by the input itself. This is