801. Minimum Swaps To Make Sequences Increasing

#### Dynamic Programming Array Hard

swapping elements at the same index in both arrays. To clarify, nums1[i] can be swapped with nums2[i] for any i. What we're trying to find is the minimum number of such swaps required to achieve our goal. An array is strictly increasing if each element is larger than the one before it. The challenge assures us that there is always a way to make the arrays strictly increasing through such swaps.

In this problem, we have two integer arrays nums1 and nums2 of the same length. Our goal is to make both arrays strictly increasing by

Leetcode Link

Intuition

Problem Description

we have two choices: 1. Do not swap elements at index i: We choose this if the current elements of nums1 and nums2 are both greater than the previous elements of their respective arrays, which keeps both arrays strictly increasing without a swap.

To solve this problem, dynamic programming is employed to keep track of the minimum number of swaps needed. At each index i,

- Swap elements at index i: If the current elements are not greater than the previous ones, we must swap to maintain the strictly increasing order. In some cases, even when it's not required to maintain the strictly increasing order, swapping might still minimize the total number of swaps.
- We maintain two variables:
- a: The minimum number of swaps needed up to the current index i without swapping nums1[i] and nums2[i]. b: The minimum number of swaps needed if we swap nums1[i] and nums2[i]. After considering whether a swap is required or beneficial at each index, and updating a and b accordingly, the solution returns the

minimum of a and b after iterating through the arrays, which represents the minimum number of swaps necessary to make both

nums1 and nums2 strictly increasing.

Solution Approach

position 1, and b is the minimum number of swaps required if we do swap at the current position.

The solution uses a dynamic programming approach to minimize the number of swaps required to make both arrays strictly increasing. Let's walk through the implementation details: • We initialize two variables, a and b. Here, a represents the minimum number of swaps required if we do not swap at the current

### • a is initially set to 0, because no swaps are performed at the start, and b is set to 1 since performing a swap at the first position would count as one operation.

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from the previous swap scenario.

Let's consider two small integer arrays nums1 and nums2:

The main loop of the algorithm starts at index 1 and goes until the end of the arrays as follows: • For each index i, we first store the old values of a and b into temporary variables x and y. This is to prevent updating a and b

- simultaneously in the loop, which would give incorrect results, as the calculation of b may depend on the old value of a. There are conditions that determine if a swap is necessary or if we can move to the next index without a swap: If nums1[i-1] >= nums1[i] or nums2[i-1] >= nums2[i], then the arrays are not strictly increasing, and a swap is necessary.
- In this case, we set a to y (the old value of b) since we have to swap the previous position, and b to x + 1 because we are performing a swap at the current position, which adds to the swap count.

• Additionally, if nums1[i-1] < nums2[i] and nums2[i-1] < nums1[i], then swapping may yield a better result even if it's not

In the end, we return the minimum of a and b, as this would represent either performing no swap or swapping at the last index,

By using dynamic programming, we avoid re-computation for each index, evaluating the minimum number of swaps needed at each

If the arrays are already strictly increasing without a swap, a remains unchanged, and b becomes y + 1 since we continue

necessary. In this case, we update a to the minimum of its current value and y, and b to the minimum of its current value and x +

step. This approach ensures that the final complexity of the algorithm is O(n), where n is the length of the given arrays.

whichever has the minimum swaps overall to make the arrays strictly increasing.

According to the problem, we want to make both arrays strictly increasing by swapping elements at the same index where necessary.

Checking further, though, we see that swapping might be beneficial for future positions because nums2[1] > nums1[0] and

# At index 1:

No swaps at the start, so a = 0.

We set tempA = a and tempB = b.

nums1[1] > nums2[0].

Example Walkthrough

1 nums1: [1, 3, 5, 7]

2 nums2: [1, 2, 3, 4]

Initialization:

 Current elements are nums1[1] = 3 and nums2[1] = 2. Previous elements are nums1[0] = 1 and nums2[0] = 1.

We start our loop from index 1 and go up to the last index.

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    We update b to the minimum of b and tempA + 1, which is 1.
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Now our arrays look like this (no change because no swap was done):

We update a to the minimum of a and tempB which are both 0.

If we swap at the first position, it would count as one swap, so b = 1.

Arrays are already strictly increasing (1 < 3 and 1 < 2), so no swap needed here.</li>

- At index 2:
- We cannot move to the next index without a swap since nums2[2] is not greater than nums2[1]. Therefore, a swap is necessary for nums2.

We again set tempA = a and tempB = b (here tempA = 0 and tempB = 1).

We set a to tempB since we are continuing from the previous decision to swap.

Current elements are nums1[2] = 5 and nums2[2] = 3.

Previous elements are nums1[1] = 3 and nums2[1] = 2.

We set b to tempA + 1 which equals 1.

After swapping, our arrays looks like this:

But now we have a problem as nums1 is no longer strictly increasing. We must also swap at index 1 to correct this.

Result after also swapping at index 1: 1 nums1: [1, 2, 3, 7]

At index 3:

2 nums2: [1, 3, 5, 4]

1 nums1: [1, 3, 3, 7]

2 nums2: [1, 2, 5, 4]

Arrays are nums1: [1, 2, 3, 7] and nums2: [1, 3, 5, 4].

Current elements are fine as 3 < 7 and 5 < 4 requires a swap.</li>

Finally, our arrays look like this, which are both strictly increasing:

increasing while minimizing the total number of swaps necessary.

def minSwap(self, nums1: List[int], nums2: List[int]) -> int:

no\_swap\_cost, swap\_cost = no\_swap, swap

# Iterate over arrays starting from the second element (index 1)

# If swapping makes both arrays increasing,

To minimize total swaps, we choose not to swap here, so b = tempB + 1.

1 nums1: [1, 2, 3, 7] 2 nums2: [1, 3, 5, 4]

We set tempA = a and tempB = b.

The minimum number of swaps required is min(a, b). Given the values of a = 0 and b = 2, the minimum number of swaps is 0. This small example illustrated the solution approach using dynamic programming, where we made both nums1 and nums2 strictly

**Python Solution** 

class Solution:

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from typing import List

 $no_swap$ , swap = 0, 1

for i in range(1, len(nums1)):

return min(no\_swap, swap)

int notSwap = 0, swap = 1;

public int minSwap(int[] nums1, int[] nums2) {

for (int i = 1; i < nums1.length; ++i) {</pre>

notSwap = swap = nums1.length;

notSwap = prevNotSwap;

// Return the minimum of the two final states.

swap = prevSwap + 1;

return Math.min(notSwap, swap);

// Initialize the two states: 'swap' and 'notSwap'.

int prevNotSwap = notSwap, prevSwap = swap;

// Reset the values for the current state.

// swap: min swaps needed when the last element is swapped.

// notSwap: min swaps needed when the last element is not swapped.

if  $(nums1[i-1] < nums1[i] && nums2[i-1] < nums2[i]) {$ 

// Iterate through each pair of elements starting from the second pair.

// 'prevNotSwap' and 'prevSwap' hold the previous state's values.

if nums1[i - 1] >= nums1[i] or nums2[i - 1] >= nums2[i]: 11 12 # If the current pair or the previous pair is not strictly increasing, 13 # we must swap this pair to make the sequence increasing no\_swap, swap = swap\_cost, no\_swap\_cost + 1 else:

# consider minimum swaps by either swapping or not swapping previous pairs

no\_swap, swap = min(no\_swap, swap\_cost), min(swap, no\_swap\_cost + 1)

// Check if the current and previous elements of both arrays are strictly increasing.

// If we choose to swap the current elements, add 1 to the previous swap value.

// Check if swapping the previous elements makes the current pair strictly increasing.

// If no swap is needed, carry forward the previous notSwap value.

# Initialize the number of swaps when not swapping or swapping the i-th element

# If it is strictly increasing, no need to swap the previous pair

swap = swap\_cost + 1 # We can choose to swap the current pair

# Return the minimum number of swaps to make both arrays strictly increasings

if nums1[i - 1] < nums2[i] and nums2[i - 1] < nums1[i]:</pre>

• Since the arrays without the current elements being swapped are increasing, we do not update a.

Java Solution class Solution {

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if (nums1[i-1] < nums2[i] && nums2[i-1] < nums1[i]) {
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                   // If so, notSwap can also be the minimum of itself and the previous swap value.
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                   notSwap = Math.min(notSwap, prevSwap);
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                   // Similarly, swap can also be the minimum of itself and prevNotSwap+1.
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                   swap = Math.min(swap, prevNotSwap + 1);
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```

C++ Solution

1 class Solution {

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2 public:
       int minSwap(vector<int>& nums1, vector<int>& nums2) {
                               // Initialize noSwap, representing the minimum swaps needed without swapping the current element.
           int noSwap = 0;
           int swap = 1;
                               // Initialize swap, representing the minimum swaps needed with swapping the current element.
            int numElements = nums1.size(); // Get the number of elements in the arrays.
           // Loop through the arrays starting from the second element
           for (int i = 1; i < numElements; ++i) {</pre>
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                int prevNoSwap = noSwap; // Store the previous noSwap value
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                int prevSwap = swap; // Store the previous swap value
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               // Reset noSwap and swap for the current iteration
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                noSwap = numElements;
               swap = numElements;
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               // Check if it is not possible to proceed without swapping (i.e. strictly increasing not maintained)
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               if (nums1[i - 1] >= nums1[i] || nums2[i - 1] >= nums2[i]) {
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                   // If an element at index i or index i-1 must be swapped to remain strictly increasing:
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                   // Current noSwap takes the value of previous swap
                   // Current swap takes the value of one plus the previous noSwap
                    noSwap = prevSwap;
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                   swap = prevNoSwap + 1;
               } else {
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                   // If current configuration already strictly increasing without swapping
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                   // swap value should consider at least one more swap (previous swap + 1)
27
                    swap = prevSwap + 1;
                   // Check if arrays are both strictly increasing if we swapped the previous pair
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                   if (nums1[i - 1] < nums2[i] && nums2[i - 1] < nums1[i]) {</pre>
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                       // Minimal swaps can be either previous noSwap or swap, take the minimum.
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                        noSwap = min(noSwap, prevSwap);
                       // Similarly, current swap can also be minimum of it or noSwap plus one (accounting for a swap at the previous st
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                        swap = min(swap, prevNoSwap + 1);
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```

// it gives the minimum number of swaps to make both sequences strictly increasing.

// Return the minimum of noSwap and swap for the last element,

let noSwap = 0; // Minimum swaps needed without swapping the current element

const numElements = nums1.length; // Get the number of elements in the arrays

// Reset noSwap and swap for the current iteration to a large value

// No change required if both arrays are already strictly increasing

// If either pair can be swapped to maintain a strictly increasing order

// The new swap can potentially be the previous noSwap plus one

// Current configuration is already strictly increasing without swapping

// this will yield the minimum number of swaps to make both sequences strictly increasing.

// The new noSwap can potentially be the previous swap (if the previous was swapped)

let swap = 1; // Minimum swaps needed with swapping the current element

const prevNoSwap = noSwap; // Store the previous noSwap value

// Loop through both arrays, starting from the second element

const prevSwap = swap; // Store the previous swap value

if (nums1[i - 1] < nums1[i] && nums2[i - 1] < nums2[i]) {</pre>

// Increment swap because we consider it's possible

if  $(nums1[i-1] < nums2[i] && nums2[i-1] < nums1[i]) {$ 

console.log(minSwap(nums1, nums2)); // Output will be minimum swaps required

noSwap = Math.min(noSwap, prevSwap);

// that we may have swapped the previous pair

1 // Function to calculate the minimum number of swaps required

function minSwap(nums1: number[], nums2: number[]): number {

return min(noSwap, swap);

2 // to make two arrays strictly increasing

noSwap = numElements;

noSwap = prevNoSwap;

swap = prevSwap + 1;

return Math.min(noSwap, swap);

Time and Space Complexity

swap = numElements;

for (let i = 1; i < numElements; ++i) {</pre>

Typescript Solution

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swap = Math.min(swap, prevNoSwap + 1);
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       // Return the smaller of noSwap and swap for the final element,
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// Example usage:

41 const nums1 = [1, 3, 5];

 $42 \quad const \quad nums2 = [1, 2, 3];$ 

The code provided is a dynamic programming solution designed to determine the minimum number of swaps needed to make two lists strictly increasing.

To analyze the time complexity of this approach, we need to consider the operations performed with each iteration of the loop that

Within each iteration, the algorithm performs constant-time comparisons and assignments, regardless of the size of the lists.

## The loop runs for every element of the two lists starting from index 1, which means it runs n-1 times, where n is the number of elements in each list. As the time taken per iteration does not depend on the size of the dataset, the overall time complexity of the algorithm is 0(n),

For the space complexity:

Time Complexity

runs len(nums1) times.

where n is the length of the lists. Space Complexity

- Two variables, a and b, are used to keep track of the minimum number of swaps when the ith element is not swapped and when it is swapped, respectively. Additionally, temporary variables x and y are used within the loop.
- Since the space used does not increase with the size of the input lists, this algorithm has a constant space complexity, thus the space complexity is 0(1).