2873. Maximum Value of an Ordered Triplet I



Leetcode Link

Problem Description

You are provided with an array of integers, nums, which has a 0-based index. The goal is to find the maximum value of a triplet (i, j, k) in this array, following the condition that i, j, and k are distinct indices, with i being less than j, and j being less than k. In other words, you need to find the maximum value obtained from the formula (nums[i] - nums[j]) * nums[k] across all possible combinations of triplets.

In a case where the values for all possible triplets are negative, the result should be 0.

The problem asks for the efficient computation of this value without having to compare every possible triplet directly, which would be inefficient for large arrays.

Intuition

To avoid an exhaustive search which is highly inefficient, we observe that we can solve the problem by keeping track of two pieces of information as we iterate through the array from left to right.

nums [i] seen so far for any triplet. • mx_diff: This represents the maximum value of mx - nums[j], which is the first part of our target equation (nums[i] - nums[j]).

• mx: This is the maximum value found in nums up to the current point in our traversal. We can think of it as the 'best' first element

It essentially stores the best-case scenario for the difference between the first and second elements of our triplet encountered so far. As we traverse the array, at each step, we attempt to update mx_diff with the largest possible value by considering the current mx

and the current number num as if it were nums[j]. We also update mx if the current number is larger than the current mx. After updating

mx and mx_diff, we then calculate the potential best-case scenario for the triplet value with the current number as nums [k], and update the answer if it's greater than the current answer. The intuition behind this approach is that we are dynamically keeping track of the best possible scenario for the first two numbers of the triplet as we progress. When we reach any nums [k], we have already computed the best possible nums [i] and nums [j] that could

precede it, thus allowing us to directly calculate the best possible value for (nums[i] - nums[j]) * nums[k] with the elements we've passed by so far. **Solution Approach**

The solution implements a single pass approach, traversing the list once, which keeps it very efficient in terms of both time and

the maximum value found so far and the maximum difference encountered so far, respectively.

space complexity. The algorithm does not use any extra data structures, as it simply maintains two variables mx and mx_diff to track

• Initialize ans, mx, and mx_diff as zero. ans will hold the answer to be returned, mx is used to keep track of the maximum value in nums as we iterate, and mx_diff keeps track of the maximum value of mx - nums[j] found so far.

array, representing the best choice for nums[i] up to this point.

check every possible combination of i, j, and k, which is the key to its efficiency.

Loop through each element num in nums. For each num:

The approach makes use of the following steps:

• Update the ans if the current mx_diff * num is greater than ans. This step checks if the current number as nums[k] combined with the best mx_diff so far makes for a higher product than we've seen.

Update mx if num is greater than mx. This step simply keeps mx as the maximum value seen up to the current element in the

- Update mx_diff if mx num is greater than mx_diff. By doing this, you are ensuring that mx_diff holds the largest possible difference between the best nums[i] and any nums[j] seen so far.
- During each iteration, the algorithm dynamically updates the potential first two elements of the triplet, which allows it to calculate the potential best-case scenario for the triplet value in constant time.

Here is the pseudocode that captures the essence of the implementation: 1 def maximumTripletValue(nums):

By maintaining the maximum found value and the maximum difference during the iteration, the algorithm eliminates the need to

for num in nums: ans = $max(ans, mx_diff * num)$ mx = max(mx, num)mx_diff = max(mx_diff, mx - num)

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This algorithm runs in O(n) time, where n is the length of the input array, making it extremely efficient for large datasets.
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Example Walkthrough
Let's consider a small example array nums to illustrate the solution approach.
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ans = mx = mx_diff = 0

return ans

Example nums array: [3, 1, 6, 4]

We have to find the maximum value of the expression (nums[i] - nums[j]) * nums[k] with the constraints i < j < k.

We initialize ans, mx, and mx_diff to 0.

```
    mx is updated to 3 because it's the only element we've seen.

    mx_diff remains 0 because we don't have a j yet.
```

ans remains 0 for the same reason.

```
After the first iteration: ans = 0, mx = 3, mx_diff = 0.
```

1. We start with the first element 3:

- 2. Moving to the second element 1:
 - \circ We consider the element 1 as potential nums [j]. The difference mx num is 3 1 = 2.

• We calculate $mx_diff * num$ which is 2 * 4 = 8. However, ans remains 12 because 8 is not greater than 12.

 \circ mx_diff is updated, as mx - num is 6 - 4 = 2, but since mx_diff is already 2, it remains the same.

- o ans is still 0 as we have not yet encountered a valid k. After the second iteration: ans = 0, mx = 3, mx_diff = 2.
- \circ This element is considered as potential nums [k]. We compute mx_diff * num which is 2 * 6 = 12. o ans is updated to 12 because 12 is greater than the current ans which is 0.

3. Next, we process the third element 6:

○ mx_diff does not change because mx - num is -3 which is not greater than 2. After the third iteration: ans = 12, mx = 6, $mx_diff = 2$.

• mx_diff is updated to 2 because 2 is greater than the current mx_diff which is 0.

4. Finally, we look at the fourth element 4:

Now we update mx to 6 because 6 is greater than the current mx which is 3.

At the end of the iterations, the maximum value found for the expression (nums[i] - nums[j]) * nums[k] is 12, which is the final answer. The triplet that gives us this value is (3, 1, 6) where i = 0, j = 1, and k = 2. Therefore, the function maximumTripletValue

mx does not change because 4 is not greater than 6.

def maximumTripletValue(self, nums: List[int]) -> int:

Iterate through all numbers in the list.

max_number = max(max_number, num)

with the array [3, 1, 6, 4] as input will return 12.

Initialize variables:

After the fourth and final iteration: ans = 12, mx = 6, $mx_diff = 2$.

max_product - to keep track of the maximum product of max_difference and the current number, # max_number - to store the maximum value encountered so far, # max_difference - to store the maximum difference between max_number and any other number. max_product = 0 9 max_number = 0 10 max_difference = 0 11 12

Update max_number if the current num is greater than the previously stored max_number.

for num in nums: 14 # Update max_product with the maximum product obtained 16 # by multiplying max_difference with the current num. 17 max_product = max(max_product, max_difference * num) 18

13

19

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Python Solution

class Solution:

from typing import List

```
22
               # Update max_difference if the difference between the current max_number and num
23
               # is greater than the previously stored max_difference.
24
               # This difference represents a potential first and second element of a triplet,
25
               # with num potentially being the third element.
26
               max_difference = max(max_difference, max_number - num)
27
28
           # After iterating through all numbers, max_product will hold
29
           # the maximum product of a triplet's first and third elements.
30
           return max_product
31
Java Solution
   class Solution {
       public long maximumTripletProduct(int[] nums) {
            long maxVal = 0;  // Initialize maximum value found in the array to 0
            long maxDiff = 0;
                                      // Initialize maximum difference between maxVal and any other value to 0
           long answer = 0;
                                       // Initialize the result for the maximum product of the triplet
 6
           // Iterate through all elements in the nums array
           for (int num : nums) {
               // Update the answer with the maximum between the current max product
 9
               // or the product of the current number and maxDiff
               answer = Math.max(answer, num * maxDiff);
11
12
13
               // Update maxVal with the maximum between the current maxVal or the current number
               maxVal = Math.max(maxVal, num);
14
15
               // Update maxDiff with the maximum difference found so far
16
               maxDiff = Math.max(maxDiff, maxVal - num);
17
18
19
           // Return the maximum product of a triplet found in the array
20
21
           return answer;
22
```

2 #include <algorithm> using namespace std; class Solution {

C++ Solution

1 #include <vector>

23 }

24

```
public:
       // Function to calculate the maximum product of a triplet in the array such that
       // the indices of the triplet (i, j, k) satisfy i < j < k and nums[i] < nums[j] < nums[k].
       long long maximumTripletValue(vector<int>& nums) {
           long long maxProduct = 0;  // To store the maximum product of a triplet
           int maxElement = 0;
                                            // To store the maximum element seen so far
           int maxDifference = 0;
                                             // To store the maximum difference seen so far
12
13
           // Loop through each number in the array 'nums'
14
15
           for (int num : nums) {
               // Update maxProduct with the maximum between current maxProduct and the product
16
               // of maxDifference and the current number 'num'. This accounts for the third element of the triplet.
               maxProduct = max(maxProduct, static_cast<long long>(maxDifference) * num);
18
19
               // Update maxElement with the maximum between current maxElement and the current number 'num'
20
21
               maxElement = max(maxElement, num);
23
               // Update maxDifference with the maximum difference between maxElement and the current number 'num'
24
               maxDifference = max(maxDifference, maxElement - num);
25
26
27
           // Return the maximum product of a triplet found in the array
28
           return maxProduct;
29
30 };
31
Typescript Solution
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2 // that can be formed by multiplying any three numbers which indices
3 // are strictly in increasing order.
   function maximumTripletValue(nums: number[]): number {
       let maxProduct = 0; // Variable to store the maximum product found
       let maxNum = 0; // Variable to store the maximum number found so far
       let maxDifference = 0; // Variable to store the maximum difference found so far
       // Iterate through the array of numbers
9
       for (const num of nums) {
10
           // Update the maxProduct with the maximum between the current maxProduct and
11
           // the product of num and maxDifference which represents a potential triplet product
           maxProduct = Math.max(maxProduct, maxDifference * num);
           // Update the maxNum with the greatest number encountered so far
           maxNum = Math.max(maxNum, num);
15
           // Update the maxDifference with the greatest difference between maxNum and the current num
16
17
           maxDifference = Math.max(maxDifference, maxNum - num);
18
19
20
       // Return the maximum product found for the triplet
21
       return maxProduct;
22 }
23
Time and Space Complexity
```

1 // Calculates the maximum product of any triplet in the given array

loop that iterates over all the elements in the array once.

The time complexity of the given code segment is O(n), where n is the length of the array nums. This is because there is a single for-

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The space complexity is 0(1) since the extra space used does not grow with the input size; only a fixed number of variables ans, mx,
and mx_diff are used regardless of the size of the input array.
```