828. Count Unique Characters of All Substrings of a Given String String] **Hash Table Dynamic Programming Leetcode Link** Hard

The problem is about counting unique characters within all possible substrings of a given string s. The goal is to compute the sum of

Problem Description

appears exactly once in it. To clarify the requirement, let's consider if s = "ABC", we then look at each substring:

the number of unique characters (countUniqueChars) for each substring in s. A unique character in a substring is a character that

 "A" has 1 unique character, "B" has 1 unique character,

- "AB" has 2 unique characters,
- "BC" has 2 unique characters,

"C" has 1 unique character,

- "ABC" has 3 unique characters.
- Adding these counts together, the sum would be 1 + 1 + 1 + 2 + 2 + 3 = 10. The challenge of the problem is that a straightforward approach to finding and counting unique characters for each substring could
- be very inefficient, especially when s is long, because the number of substrings grows quadratically with the length of s.

To efficiently solve this problem, we need an approach that avoids redundantly counting unique characters in overlapping substrings.

This is where the intuition for the provided solution comes into play.

index (8 - 5).

efficiently.

evaluating each substring individually.

Here's a step-by-step explanation:

3. Iterate Over Each Character's Occurrences:

occurrence and end before its next occurrence.

with the number of possible endpoints (right).

Iterate over characters of the string: A, B, A.

3. Iterate Over Each Character's Occurrences:

contribution is 1 * 2 = 2.

characters for all substrings of s.

Example Walkthrough

2. Initializing the Answer:

Initialize ans to 0.

occurrence of the character (not the -1 or len(s)), calculate:

Intuition

understand where each character contributes to the uniqueness in the substrings. By iterating through the dictionary, we can consider each character independently and determine its contribution to the overall

count. A key insight is that the contribution of a character at position i to the sum is determined by the distance to the previous

occurrence of the same character and the distance to the next occurrence of the same character. This is because a character

contributes to the uniqueness of all substrings that start after its previous occurrence and end before its next occurrence.

We create a dictionary, d, that maps each character in the string s to the list of indices where it appears. This allows us to quickly

For example, if character 'A' appears at indices 3, 5, and 8 in s, then for the substring s[4:6] (which includes character at index 5), 'A' is unique. The number of such substrings is the product of the distance from the previous index (5 - 3) and the distance to the next

The solution efficiently calculates the contribution of each character by iterating through the list of indices in v (enhanced with start and end markers at -1 and len(s), respectively) for each character, multiplying the distances from the current index to its previous and next, and summing up these products to get the total count.

Solution Approach

The solution uses a combination of dictionary and list data structures alongside some clever indexing to solve the problem

Overall, the intuition is to transform the original problem into calculating character contributions based on their positions, rather than

where that character appears. This is achieved through enumeration of string s. 2. Initializing the Answer: Start with a variable ans initialized to 0. This variable will hold the sum of unique characters counts for all substrings.

1. Dictionary Creation: Create a dictionary d where each key-value pair consists of a character from the string and a list of indices

end -1 and len(s). These sentinels represent fictive occurrences before the start and after the end of the string to handle

edge cases for the first and last characters. Recursive Sub-problem Identification: Each unique occurrence of a character can be viewed as the center of a range

extending to its previous and next occurrences. This character is unique in all substrings that start after its previous

For each character, we get its list of indices where it appears in the string and add two sentinel indices at the beginning and

4. Accumulate Contribution: Iterate over the list of indices (now with added sentinels) for the given character. For index i that corresponds to a true

■ The distance to the previous index: left = v[i] - v[i - 1]. ■ The distance to the next index: right = v[i + 1] - v[i]. The contribution of the character at this particular index to the overall unique character count is given by left * right. It

represents the count of substrings where this character is unique, by combining the number of possible start points (left)

5. Sum Up Contributions: Add each character's contributions to the ans variable. 6. Return the Result: After processing all characters, return the final accumulated value in ans, which represents the sum of unique

This solution approach leverages the indexing pattern to avoid redundant calculations by using the distances between character

occurrences to infer the number of substrings where those characters are unique. It's a great example of how considering the

Create a dictionary d where we record the indices of each character: d = {'A': [0, 2], 'B': [1]}.

1. Dictionary Creation:

Let's go through an example to illustrate the solution approach using the string s = "ABA".

problem from a different angle can lead to an efficient approach that avoids brute-force inefficiency.

 ○ We add sentinel values to the list of indices for each character in d. The updated lists will be {'A': [-1, 0, 2, 3], 'B': [-1, 1, 3]4. Accumulate Contribution: For character A:

■ For the first true occurrence at index 0: The left distance is 0 - (-1) = 1 and the right distance is 2 - 0 = 2. The

■ For the second true occurrence at index 2: The left distance is 2 - 0 = 2 and the right distance is 3 - 2 = 1. The

• For the true occurrence at index 1: The left distance is 1 - (-1) = 2 and the right distance is 3 - 1 = 2. The

contribution is 2 * 1 = 2. \circ The total contribution for A is 2 + 2 = 4.

For character B:

5. Sum Up Contributions:

Update ans to 8.

6. Return the Result:

Python Solution

class Solution:

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from collections import defaultdict

unique_count = 0

return unique_count

index_map = defaultdict(list)

Initialize the answer to 0.

for indices in index_map.values():

contribution is 2 * 2 = 4. The total contribution for B is 4.

Sum up the contributions: 4 (from A) + 4 (from B) = 8.

def unique_letter_string(self, input_string: str) -> int:

for index, character in enumerate(input_string):

Iterate through the values in the index map dictionary.

Iterate through the indices of the current character.

Add pseudo-indices at the beginning and end.

indices = [-1] + indices + $[len(input_string)]$

index_map[character].append(index)

for i in range(1, len(indices) - 1):

Return the total count of unique substrings.

List<Integer>[] indexList = new List[26];

for (int i = 0; i < 26; ++i) {

// Initialize lists for each character 'A' to 'Z'

Arrays.setAll(indexList, x -> new ArrayList<>());

// representing the position before the start of the string

// Add a starting index -1 for each character,

Create a default dictionary to store the indices of each character.

Iterate through the characters in the string, along with their indices.

Calculate the contribution of each index to the unique count.

from the previous occurrence to the current (v[i] - v[i-1]),

and from the current to the next occurrence (v[i+1] - v[i]).

unique_count += (indices[i] - indices[i - 1]) * (indices[i + 1] - indices[i])

The idea is that for each index, we count contributions

// Create a list of lists to keep track of the occurrences of each letter

 After processing all characters, return the accumulated value in ans, which is 8. This example demonstrates the efficiency of the solution approach, which counts the unique characters in all substrings without directly examining each substring.

Java Solution 1 class Solution { public int uniqueLetterString(String s) {

1 class Solution {

int uniqueLetterString(string s) {

for (auto& indices : index) {

2 function uniqueLetterString(s: string): number {

// Initialize the counter for the answer.

charIndices.push(s.length);

occurrence towards the unique substrings.

indices.forEach((charIndices: number[]) => {

int count = 0;

return count;

Typescript Solution

let count: number = 0;

vector<vector<int>> index(26, {-1});

for (int i = 0; i < s.size(); ++i) {

indices.push_back(s.size());

index[s[i] - 'A'].push_back(i);

// Initialize the counter for the answer.

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indexList[i].add(-1);
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           // Iterate over the string and add the index of each character to the corresponding list
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           for (int i = 0; i < s.length(); ++i) {</pre>
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                indexList[s.charAt(i) - 'A'].add(i);
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           // Initialize a variable to hold the sum of unique letter strings
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           int ans = 0;
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           // Iterate through each list in indexList
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           for (var occurences : indexList) {
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               // Add the length of the string as the last index for each character
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               occurences.add(s.length());
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               // Calculate contributions for each index
               for (int i = 1; i < occurences.size() - 1; ++i) {
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                    // The count for a unique letter string is determined by the product of the distance to
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                    // the previous and next occurrence of the same character
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                    ans += (occurrences.get(i) - occurrences.get(i - 1)) * (occurrences.get(i + 1) - occurrences.get(i));
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35
           // Return the total sum of unique letter strings
36
           return ans;
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38 }
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C++ Solution
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// Function to calculate the sum of counts of unique characters in all substrings of the given string.

// Create a 2D vector with 26 rows to store the indices of each character's occurrence.

// Push the dummy index equal to the length of the string for the calculation.

// Calculate the contribution of the character at position 'i' and add to the answer.

// The multiplier is the number of substrings where this character is unique.

count += (indices[i] - indices[i - 1]) * (indices[i + 1] - indices[i]);

// Return the total count of unique characters in all substrings of the string.

1 // Function to calculate the sum of counts of unique characters in all substrings of the given string.

// Create a 2D array with 26 elements to store the indices of each character's occurrence.

// Push the dummy index equal to the length of the string for the calculation.

// Return the total count of unique characters in all substrings of the string.

times the i-th character appears in s). This results in a time complexity of $0(m * k_i)$.

// Calculate the contribution of the character at position 'i' and add to the answer.

count += (charIndices[i] - charIndices[i - 1]) * (charIndices[i + 1] - charIndices[i]);

// The contribution is the number of substrings where this character is unique.

// Initialize the first index as -1, which is used as a dummy index for calculation.

// Loop through the given string to fill in the actual indices of each character.

// Loop through the 2D vector to calculate the count for each character.

// Loop through each group of indices for the character.

for (int i = 1; i < indices.size() - 1; ++i) {</pre>

indices[s.charCodeAt(i) - 'A'.charCodeAt(0)].push(i);

// Loop through the 2D array to calculate the count for each character.

// Loop through each group of indices for the character.

for (let i = 1; i < charIndices.length - 1; i++) {</pre>

// Initialize the first index as -1, which is used as a dummy index for calculation. let indices: number[][] = Array.from({ length: 26 }, () => [-1]); // Loop through the given string to fill in the actual indices of each character. for (let i = 0; i < s.length; i++) {</pre>

});

return count;

```
Time and Space Complexity
Time Complexity
The given Python code computes the number of substrings where each character occurs exactly once. To understand the time
complexity, let's analyze the steps in the code:
 1. A dictionary d is created using a defaultdict to store positions of each character in string s.
 2. The string s is enumerated over once, so this is O(n) where n is the length of the string s.
 3. For each character, the positions stored are iterated over in a nested loop to calculate the contribution of each character
```

and there are at most "26" English letters, the m and k_i can be bound by n, leading to a simplified bound of $0(n^2)$. **Space Complexity**

1. A dictionary d is used to store the index positions for each character in s. If s contains all unique characters, the space

Hence, the overall time complexity is $0(n + m * k_i)$. However, since a character cannot appear more times than the string length n,

4. There are m characters in string s, and the nested loop iterates over k_i positions for the i-th character (k_i is the number of

complexity of this operation would be O(n). 2. Temporary lists are created for the positions of individual characters with two extra elements for boundary positions; however, their impact on space complexity is negligible as they don't grow with n.

For space complexity,

The predominant factor is the space taken by d which is O(n). So, the space complexity of the code is O(n).

Note that the auxiliary storage created within the loop is small and does not exceed the length of the string s. Since there are a fixed number of english characters, this does not affect the overall space complexity significantly.