1631. Path With Minimum Effort

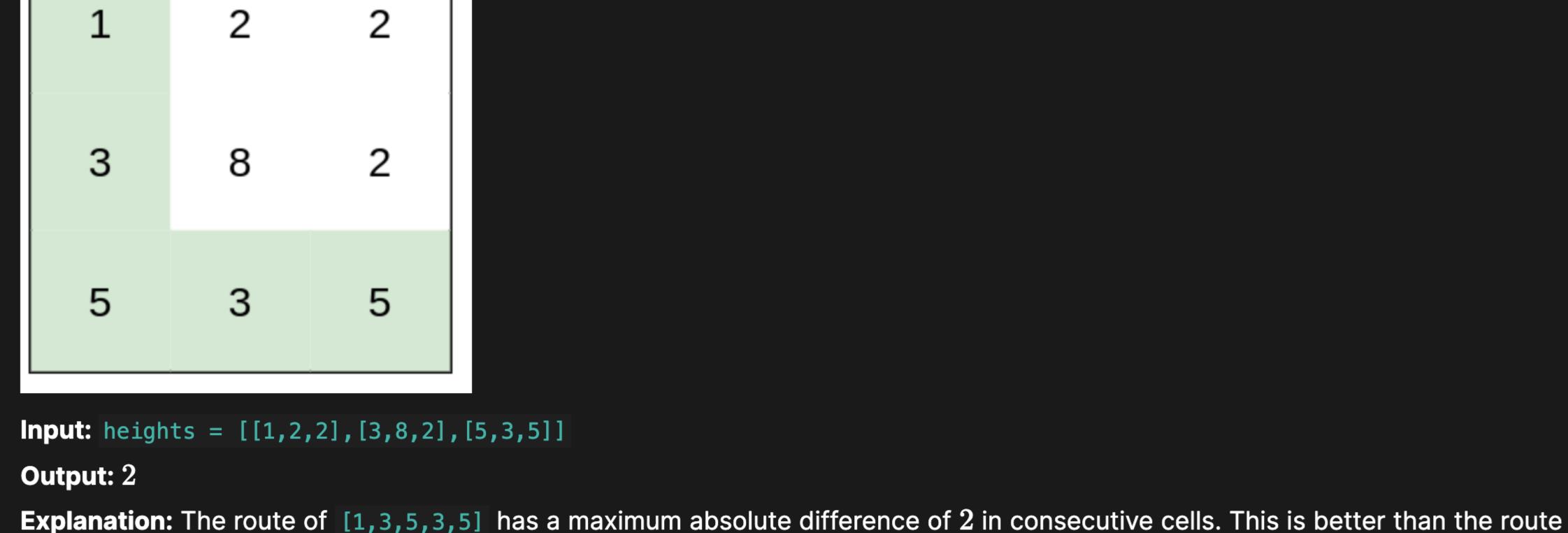
[col] represents the height of cell (row, col). You are situated in the top-left cell, (0, 0), and you hope to travel to the bottom-right cell, (rows-1, columns-1) (i.e., O-indexed). You can move up, down, left, or right, and you wish to find a route that requires the minimum effort.

You are a hiker preparing for an upcoming hike. You are given heights, a 2D array of size rows x columns, where heights[row]

A route's effort is the maximum absolute difference in heights between two consecutive cells of the route.

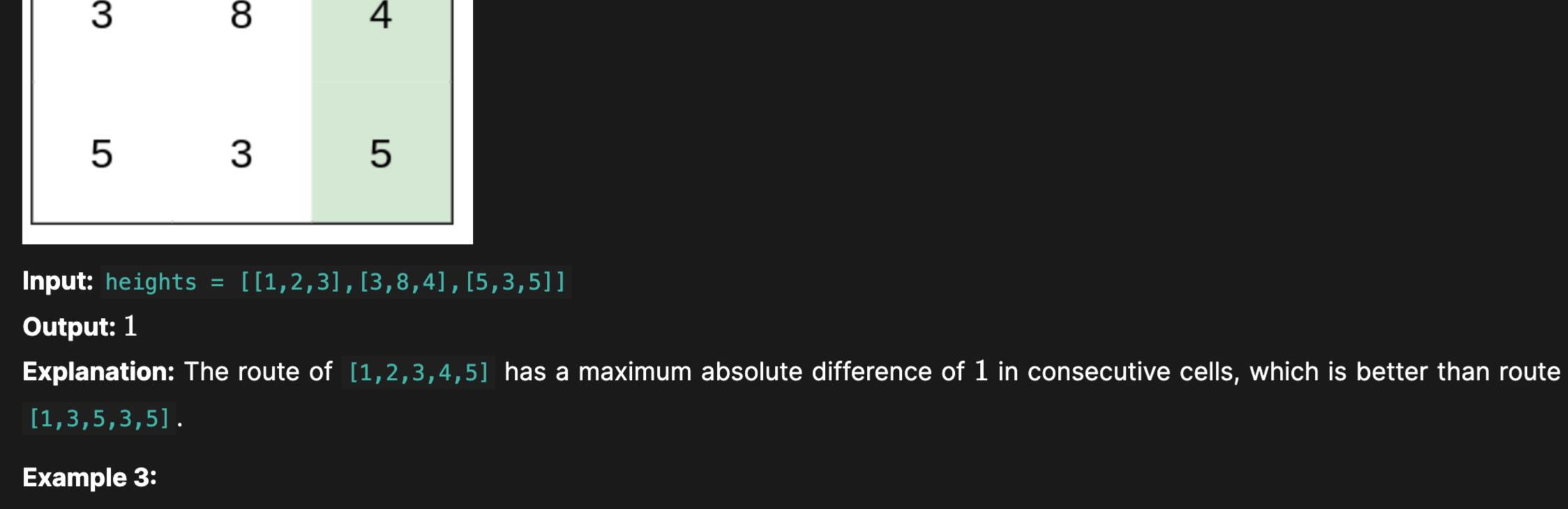
Return the minimum effort required to travel from the top-left cell to the bottom-right cell.

Example 1:



of [1,2,2,2,5], where the maximum absolute difference is 3.

Example 2:



Output: 0 **Explanation:** This route does not require any effort.

Constraints:

rows == heights.length

 $1 \leq \text{rows}, \text{columns} \leq 100$

with a BFS/flood fill algorithm.

columns == heights[i].length

 $1 \leq \text{heights[i][j]} \leq 10^6$ Solution

Input: heights = [[1,2,1,1,1],[1,2,1,2,1],[1,2,1,2,1],[1,2,1,2,1],[1,1,1,2,1]]

bottom-right cell. We'll then find the efforts for all these routes and return the smallest.

Brute Force

Full Solution

effort. Given some effort a, how do we check if there exists a route that has an effort smaller or equal to a?

above.

Let's first denote the distance between two adjacent cells as the absolute difference between their heights. A route will have an effort smaller or equal to a if it travels from the top-left cell to the bottom-right cell and all adjacent cells in

the route have a distance that doesn't exceed a. To check if such routes exist, we can check if there exists a path from the top-

left cell to the bottom-right cell such that we never travel between cells with a distance that exceeds a. We can accomplish this

The minimum effort a that's **good** is the final answer that we return. To find the minimum effort, we can implement a binary

Every binary search iteration, we can check whether or not some effort is good by running the BFS/flood fill algorithm mentioned

Instead of thinking of finding the efforts of all possible routes, we should think about finding routes that have some specific

Our most simple brute force for this problem would be to try all different routes that start from the top-left cell and end in the

<u>search</u>. Why can we binary search this value? Let's say our minimum **good** effort is b. Our binary search condition is satisfied since all values **strictly** less than b are **not good** and all values greater or equal to b are **good**.

We'll denote an effort a as **good** if there exists a route with an effort smaller or equal to a.

Time Complexity Let's denote R as number of rows, C as number of colmns, and M as maximum height in <code>heights</code> . Since BFS/flood fill will run in $\mathcal{O}(RC)$ and we have $\mathcal{O}(\log M)$ binary search iterations, our final time complexity will be

// dimensions for heights

queue<int> qCol; gRow.push(0); qCol.push(0); // BFS starts in top-left cell //We can also use queue<pair<int,int>> to store both the row & col in one queue

vis[0][0] = true;

qRow.pop();

qCol.pop();

while (!qRow.empty()) {

Time Complexity: $\mathcal{O}(RC \log M)$

const vector<int> deltaRow = $\{-1, 0, 1, 0\}$;

const vector<int> deltaCol = {0, 1, 0, -1};

int curRow = qRow.front();

int curCol = qCol.front();

bool isValidEffort(vector<vector<int>>& heights, int mid) {

int rows = heights.size(); int columns = heights[0].size(); vector<vector<bool>> vis(rows, vector<bool>(columns)); // keeps track of whether or not we visited a node queue<int> qRow;

 $\mathcal{O}(RC\log M)$.

C++ Solution

class Solution {

```
for (int dir = 0; dir < 4; dir++) {
                int newRow = curRow + deltaRow[dir];
                int newCol = curCol + deltaCol[dir];
                if (newRow < 0 || newRow >= rows || newCol < 0 || newCol >= columns) { // check if cell is in bounce
                    continue;
                if (vis[newRow][newCol]) { // check if cell has been visited
                    continue;
                if (abs(heights[newRow][newCol] - heights[curRow][curCol]) > mid) { // check if distance exceeds li
                    continue;
                vis[newRow][newCol] = true;
                gRow.push(newRow);
                qCol.push(newCol);
                // process next node
        return vis[rows - 1][columns - 1];
   public:
    int minimumEffortPath(vector<vector<int>>& heights) {
                             // every effort less or equal to low will never be good
        int low = -1;
        int high = (int)1e6; // every effort greater or equal to high will always be good
        int mid = (low + high) / 2;
        while (low + 1 < high) {</pre>
            if (isValidEffort(heights, mid)) {
                high = mid;
            } else {
                low = mid;
            mid = (low + high) / 2;
        return high;
Java Solution
class Solution {
    final int[] deltaRow = \{-1, 0, 1, 0\};
    final int[] deltaCol = \{0, 1, 0, -1\};
    private boolean isValidEffort(int[][] heights, int mid){
        int rows = heights.length;
        int columns = heights[0].length; // dimensions for heights
        boolean[][] vis = new boolean[rows][columns]; // keeps track of whether or not we visited a node
        Oueue<Integer> aRow = new LinkedList():
        Queue<Integer> qCol = new LinkedList();
        qRow.add(0);
        qCol.add(0); // BFS starts in top-left cell
        vis[0][0] = true;
        while (!qRow.isEmpty()) {
            int curRow = qRow.poll();
            int curCol = qCol.poll();
            for (int dir = 0; dir < 4; dir++) {
                int newRow = curRow + deltaRow[dir];
                int newCol = curCol + deltaCol[dir];
                if (newRow < 0 || newRow >= rows || newCol < 0</pre>
                     || newCol >= columns) { // check if cell is in boundary
                    continue;
                if (vis[newRow][newCol]) { // check if cell has been visited
                    continue;
```

return vis[rows-1][columns-1]; public int minimumEffortPath(int[][] heights) { int rows = heights.length;

```
return high;
Python Solution
import collections
class Solution:
```

if (Math.abs(heights[newRow][newCol] - heights[curRow][curCol]) > mid){

// check if distance exceeds limit

int columns = heights[0].length; // dimensions for heights

int low = -1; // every effort less or equal to low will never be good

int high = (int) 1e6; // every effort greater or equal to high will always be good

continue;

gRow.add(newRow):

gCol.add(newCol);

int mid = (low + high) / 2;

high = mid;

low = mid;

mid = (low + high) / 2;

while (low + 1 < high) {</pre>

} else {

return high

// process next node

vis[newRow][newCol] = true;

if (isValidEffort(heights,mid)) {

```
def minimumEffortPath(self, heights: List[List[int]]) -> int:
    rows = len(heights)
   columns = len(heights[0]) # dimensions for heights
    low = -1 # every effort less or equal to low will never be good
   high = 10 ** 6 # every effort greater or equal to high will always be good
   mid = (low + high) // 2
   def isValidEffort(heights, mid):
        vis = [[False] * columns for a in range(rows)]
       # keeps track of whether or not we visited a node
        gRow = collections.deque([0])
        qCol = collections.deque([0]) # BFS starts in top-left cell
        vis[0][0] = True
       while qRow:
            curRow = gRow.popleft()
           curCol = qCol.popleft()
            for [deltaRow, deltaCol] in [(-1, 0), (0, 1), (1, 0), (0, -1)]:
                newRow = curRow + deltaRow
                newCol = curCol + deltaCol
                if (newRow < 0 or newRow >= rows or newCol < 0 or newCol >= columns):
                    # check if cell is in boundary
                    continue
                if vis[newRow][newCol] == True: # check if cell has been visited
                    continue
                if (abs(heights[newRow][newCol] - heights[curRow][curCol]) > mid):
                    # check if distance exceeds limit
                    continue
                vis[newRow][newCol] = True
                gRow_append(newRow)
                gCol.append(newCol)
                # process next node
        return vis[rows-1][columns-1]
   while low + 1 < high:
        if isValidEffort(heights,mid):
           high = mid
        else:
            low = mid
        mid = (low + high) // 2
```