Medium Hash Table <u>Array</u>

Problem Description

food item. We are tasked with finding combinations of exactly two different food items such that their total deliciousness equals a power of two. These combinations are called "good meals". To clarify, two food items are considered different if they are at different indices in the array, even if their deliciousness values are identical. The output should be the number of good meals that we can create from the given list, and because this number could be very

In this problem, we are given an array called deliciousness where each element represents the deliciousness level of a specific

large, we are instructed to return it modulo 10^9 + 7. A modular result is a standard requirement in programming challenges to avoid overflow issues with high numbers.

Intuition

To solve this problem, we can use a hash map (in Python, this is a dictionary) to store the frequency of each deliciousness value.

We iterate over all possible powers of two (up to the 21st power since the input constraint is 2^20), and within this iteration, we check each unique deliciousness value. For each of these values, say a, we look for another value b such that a + b equals the

Here's the step-by-step breakdown of our approach: 1. Initialize a Counter for the array deliciousness to keep track of the number of occurrences of each value of deliciousness. 2. Initialize a variable ans to keep track of the total number of good meals. 3. Loop through all the powers of two up to 2^21. This covers the range of possible sums of the two deliciousness values.

4. For each deliciousness value a found in the hash map we created, calculate $b = 2^i - a$.

- 5. If b is also in the hash map and a != b, then we have found a pair of different food items whose deliciousness sums to a power of two.
- o In this case, we add to ans the product of the number of times a appears and the number of times b appears. 6. If a == b, we have found a pair of the same food items, and we add to ans the product of the number of times a appears with m - 1 because you

current power of two we're checking against. This value b must be 2ⁱ - a.

- cannot count the same pair twice. 7. Since each pair will be counted twice during this process (once for each element as a and once as b), we must divide the total answer by 2 to get the correct count.
- 8. Finally, take the modulo of the count by $10^9 + 7$ to get our answer within the required range. Solution Approach
- The implementation uses a Counter from the Python collections module, which is essentially a hash map or dictionary designed
- to count the occurrences of each element in an iterable. This data structure is ideal for keeping track of the frequency of deliciousness in the given deliciousness array.

Here's a step-by-step guide to how the algorithm and data structures are used in the solution:

First, a Counter object named cnt is created to store the frequency of each value of deliciousness from the array. We set ans to 0 as an accumulator for the total number of good meals.

regarding deliciousness. Inside this loop, we calculate $s = 1 \ll i$, which is a bit manipulation operation that left-shifts the number 1 by i places, effectively calculating 2^i.

We loop through all possible powers of two up to 2^21 (specified as 22 in the range(22) because range goes up to but does

not include the end value in Python). We need to cover 2^20 since it's the maximum sum according to the problem constraints

With each power of two, we iterate over the items in the Counter object, where a is a deliciousness value from the array, and m

is its frequency (the number of times it appears).

combinations without repetition.

and b.

problem's requirement.

- We then calculate b = s a, to find the complementary deliciousness value that would make a sum of s with a. We check if b is present in our Counter. If it is, we have a potential good meal. However, we must be mindful of counting pairs
- correctly: If a equals b, then we increment ans by m * (m - 1) because we can't use the same item twice, hence we consider the
- After the loop, since every pair is counted twice (once for each of its two items, as both a and b), we divide ans by 2 to obtain the actual number of good meals.

Lastly, we apply modulo 10^9 + 7 to our result to handle the large numbers and prevent integer overflow issues as per the

By utilizing a hash map (Counter) and iterating over the powers of two, the solution effectively pairs up food items while avoiding

If a does not equal b, then we increment ans by m * cnt[b], considering all combinations between the occurrences of a

Example Walkthrough Let's walk through a small example to illustrate the solution approach using the array deliciousness = [1, 3, 5, 7, 9].

We first create a Counter object from the deliciousness array, which will count the frequency of each value. In this case, all

nested loops that would significantly increase the time complexity. This allows for an efficient solution to the problem.

values are unique and appear once, so our counter (cnt) would look like this: {1:1, 3:1, 5:1, 7:1, 9:1}.

We initialize ans to 0 to begin counting the number of good meals.

in our counter. We have a as the key and m as the frequency (always 1 in this case).

For each a, we calculate b = s - a to find the complementary deliciousness value.

product of their frequencies (since m is always 1, it would just be incremented by 1).

Now, we loop through all possible powers of two up to 2^21. For simplicity, consider that we just check up to 2^3 (or 8) for this example. Our powers of two are therefore [1, 2, 4, 8].

For the power of 2 (say $s = 2^i$), we loop through the Counter object items. Let's first choose s = 4 and consider the entries

We check if b exists in our counter. If it does, and a is not equal to b, then we found a good meal pair and increment ans by the

Solution Implementation

mod = 10**9 + 7

answer = 0

count = Counter(deliciousness)

Initialize the answer to zero

def countPairs(self, deliciousness: List[int]) -> int:

for value, frequency in count.items():

if value == complement:

if complement in count:

Return the final answer modulo 10^9 + 7

else:

Define the modulus for the final answer due to large numbers

Create a counter to count occurrence of each value in deliciousness

complement = power_two_sum - value # Find the complement

answer += frequency * (frequency - 1) // 2

If the complement is also in deliciousness

Python

class Solution:

However, if a equals b, then we increment ans by m * (m - 1) / 2 which is zero in this case, as there's only one of each item.

At the end of the loop, assuming we found no other pairs for other powers of two, ans would be 2 (since we found the (1, 3) pair twice). We then divide it by 2 to correct for the double counting, leaving us with a final ans of 1.

Lastly, we apply modulo 10^9 + 7 to our result. Since our ans is much less than 10^9 + 7, it remains unchanged.

good meals because 1+3=4, which is a power of two. Both pairs are counted separately, so ans is incremented twice.

We continue this process for all powers of two. Given our example and s = 4, we notice that pairs (1, 3) and (3, 1) form

- Our final answer is that there is 1 good meal combination in the deliciousness array [1, 3, 5, 7, 9] when considering powers of two up to 2³. If we extended it to 2²1, there may be more combinations available.
- from collections import Counter

If value and complement are the same, choose pairs from the same number (frequency choose 2)

Iterate through powers of two from 2^0 to 2^21 for i in range(22): power_two_sum = 1 << i # Calculate the power of two for current i</pre> # Iterate through each unique value in deliciousness

If they are different, we count all unique pairs (frequency_a * frequency_b) answer += frequency * count[complement] # Divide by 2 because each pair has been counted twice answer //= 2

Java

return answer % mod

```
class Solution {
   // Define the modulus value for large numbers to avoid overflow
   private static final int MOD = (int) 1e9 + 7;
   // Method to count the total number of pairs with power of two sums
   public int countPairs(int[] deliciousness) {
       // Create a hashmap to store the frequency of each value in the deliciousness array
       Map<Integer, Integer> frequencyMap = new HashMap<>();
        for (int value : deliciousness) {
           frequencyMap.put(value, frequencyMap.getOrDefault(value, 0) + 1);
        long pairCount = 0; // Initialize the pair counter to 0
       // Loop through each power of 2 up to 2^21 (because 2^21 is the closest power of 2 to 10^9)
        for (int i = 0; i < 22; ++i) {
           int sum = 1 << i; // Calculate the sum which is a power of two</pre>
           for (var entry : frequencyMap.entrySet()) {
               int firstElement = entry.getKey(); // Key in the map is a part of the deliciousness pair
               int firstCount = entry.getValue(); // Value in the map is the count of that element
               int secondElement = sum - firstElement; // Find the second element of the pair
               // Check if the second element exists in the map
               if (!frequencyMap.containsKey(secondElement)) {
                   continue; // If it doesn't, continue to the next iteration
               // If the second element exists, increment the pair count
               // If both elements are the same, we must avoid counting the pair twice
               pairCount += (long) firstCount * (firstElement == secondElement ? firstCount - 1 : frequencyMap.get(secondElement
       // Divide the result by 2 because each pair has been counted twice
       pairCount >>= 1;
       // Return the result modulo MOD to get the answer within the range
       return (int) (pairCount % MOD);
C++
```

```
// Populate the frequency map with deliciousness counts
for (const value of deliciousness) {
    const count = countMap.get(value) || 0;
    countMap.set(value, count + 1);
```

TypeScript

const MOD = 1e9 + 7;

};

class Solution {

const int MOD = 1e9 + 7;

int countPairs(vector<int>& deliciousness) {

unordered_map<int, int> countMap;

for (int& value : deliciousness) {

// Populate the frequency map

for (int i = 0; i < 22; ++i) {

++countMap[value];

// Create map to store the frequency of each deliciousness value

long long totalPairs = 0; // Using long long to prevent overflow

int sum = 1 << i; // Current sum target (power of two)</pre>

// Else multiply frequencies of the two numbers

totalPairs >>= 1; // Each pair is counted twice, so divide by 2

return totalPairs % MOD; // Modulo operation to avoid overflow

// Define MOD constant for modulus operation to avoid overflow

let totalPairs = 0; // Using long to prevent overflow

// Iterate over all possible powers of two up to 2^21

// Create map to store the frequency of each deliciousness value

const sum = 1 << i; // Current sum target (power of two)</pre>

// Function to count pairs with sum that are power of two

function countPairs(deliciousness: number[]): number {

const countMap = new Map<number, number>();

for (let i = 0; i < 22; ++i) {

totalPairs += deliciousValue == complement ?

int complement = sum - deliciousValue; // Complement to make a power of two

static_cast<long long>(frequency) * (frequency - 1) :

static_cast<long long>(frequency) * countMap[complement];

// If it's the same number, pair it with each other (except with itself)

// Iterate over the frequency map to check for pairs

for (auto& [deliciousValue, frequency] : countMap) {

// Check if complement exists in the map

if (!countMap.count(complement)) continue;

// Iterate over all possible powers of two up to 2^21

public:

```
// Iterate over the frequency map to check for pairs
          for (const [deliciousValue, frequency] of countMap.entries()) {
              const complement = sum - deliciousValue; // Complement to make a power of two
              if (!countMap.has(complement)) continue; // Continue if complement does not exist
              // Calculate the total pairs
              // If it's the same number, combine it with each other (except with itself)
              // Else multiply frequencies of the two numbers
              totalPairs += deliciousValue === complement
                  ? frequency * (frequency - 1)
                  : frequency * (countMap.get(complement) as number);
      totalPairs /= 2; // Each pair is counted twice, so divide by 2
      // Return the number of pairs mod MOD to prevent overflow
      return totalPairs % MOD;
from collections import Counter
class Solution:
   def countPairs(self, deliciousness: List[int]) -> int:
       # Define the modulus for the final answer due to large numbers
       mod = 10**9 + 7
       # Create a counter to count occurrence of each value in deliciousness
        count = Counter(deliciousness)
       # Initialize the answer to zero
        answer = 0
       # Iterate through powers of two from 2^0 to 2^21
        for i in range(22):
            power_two_sum = 1 << i # Calculate the power of two for current i</pre>
            # Iterate through each unique value in deliciousness
            for value, frequency in count.items():
                complement = power_two_sum - value # Find the complement
               # If the complement is also in deliciousness
                if complement in count:
                   # If value and complement are the same, choose pairs from the same number (frequency choose 2)
                    if value == complement:
                        answer += frequency * (frequency - 1) // 2
                   else:
                        # If they are different, we count all unique pairs (frequency_a * frequency_b)
                        answer += frequency * count[complement]
       # Divide by 2 because each pair has been counted twice
        answer //= 2
       # Return the final answer modulo 10^9 + 7
```

The provided code has two nested loops. The outer loop is constant, iterating 22 times corresponding to powers of two up to 2^21 , as any pair of meals should have a sum that is a power of two for a maximum possible pair value of $2^(20+20) = 2^40$, and the closest power of two is 2^41.

Time Complexity

return answer % mod

Time and Space Complexity

loop has a time complexity of O(n). The if condition inside the inner loop checks if b exists in cnt, which is a Counter (essentially a dictionary), and this check is 0(1) on average. The increment of ans is also 0(1). So, multiplying the constant 22 by the O(n) complexity of the inner loop gives the total time complexity:

The inner loop iterates through every element a in the deliciousness list once. So, if n is the length of deliciousness, the inner

T(n) = 22 * 0(n) = 0(n)

Space Complexity

The cnt variable is a Counter that stores the occurrences of each item in deliciousness. At worst, if all elements are unique, cnt

would be the same size as deliciousness, so the space used by cnt is O(n) where n is the length of deliciousness. S(n) = O(n)

size of deliciousness and thus does not affect the overall space complexity.

There is a negligible additional space used for the loop indices, calculations, and single-item b, which does not depend on the