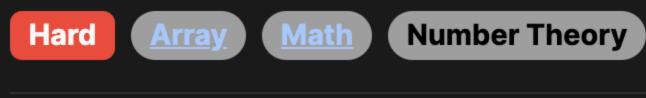
1250. Check If It Is a Good Array



Problem Description

these numbers, multiply each selected number by an integer, and then sum them up to get a total of 1. If this is possible, the array is considered "good". Otherwise, it is not good. The task is to determine if the given array is good or not, and we are to return True if it is good and False if it is not.

The problem presents us with an array of positive integers called nums. Our goal is to check if it's possible to select a subset of

Intuition

the GCD of all numbers in the array and the result is 1, this implies that we can form the number 1 as a linear combination of the array numbers, using the Bezout's identity theorem.

This means that if the GCD of the entire array is 1, there must be some subset of numbers in the array which can be multiplied by some integers to sum up to 1, since 1 is the only number that when used in linear combinations can produce any integer (and

To determine if an array is good or not, we can use a mathematical concept called the Greatest Common Divisor (GCD). The GCD

of two numbers is the largest number that divides both of them without leaving a remainder. If we can extend this concept to find

specifically the integer 1 in our case).

The Python code makes use of the reduce function and the gcd function from the [math](/problems/math-basics) module. The

reduce function is used to apply the gcd function cumulatively to the items of nums, from left to right, so that we are effectively

finding the GCD of all the numbers in the array. If the GCD turns out to be 1, the function returns True. Otherwise, it returns False. This simple approach elegantly checks if the array is good using built-in functions to perform the necessary calculations.

Solution Approach

programming construct in Python.

Here's the step-by-step breakdown of the implementation:
 Step 1: Import the gcd function from the [math](/problems/math-basics) module. gcd takes two numbers as arguments and

The solution to this problem leverages the mathematical property of the Greatest Common Divisor (GCD) and a functional

• Step 2: Use the reduce function from the functools module. The reduce function is a tool for performing a cumulative

returns their greatest common divisor.

- operation over an iterable. In this case, it applies the gcd function starting with the first two elements of the nums array, and then consecutively using the result as the first argument and the next element in the array as the second argument.
- it will calculate the gcd of the first and second elements, then take that result and calculate the gcd with the third element, and so on until it processes the entire array.

 Step 4: After reduce has processed all the elements, we evaluate whether the accumulated GCD is 1. If the result is 1, it

Step 3: The reduce function will apply the gcd function progressively across all elements of the array. Essentially, this means

signifies that there is some combination of the array elements along with respective multiplicands that could add up to 1

- **Step 5**: The <u>isGoodArray</u> method returns <u>True</u> if the GCD is 1, signaling that the array is "good", or returns <u>False</u> otherwise. The algorithm relies on the following data structures and patterns:
- Functional Programming: Using reduce is an example of functional programming, as it applies a function cumulatively to the items of an iterable in a non-mutable way.

And that's it. By efficiently applying the gcd function cumulatively across all elements in the nums array, we can ascertain

whether the array is "good" with a single line of code after the necessary functions are imported:

(thanks to Bezout's identity). If not, it implies that no such combination is possible.

class Solution:
 def isGoodArray(self, nums: List[int]) -> bool:

• Arrays: The given input is an array that the algorithm iterates through.

return reduce(gcd, nums) == 1

Example Walkthrough

Let's illustrate the solution approach with a small example. Suppose we are given the following array of positive integers:

```
nums = [6, 10, 15]

Now, let's walk through the process step by step:
```

Step 1: We first import the gcd function from the math module, which will allow us to calculate the greatest common divisor

of two given numbers.

array nums.

is indeed 1.

nums = [6, 10, 15]

class Solution:

Java

result = reduce(gcd, nums)

Solution Implementation

indicating that the array is "good".

is_good = result == 1 # This would be True in this case

def isGoodArray(self, nums: List[int]) -> bool:

Then, check if the final gcd value is 1.

int gcdValue = 0; // Initialize the gcd value to 0.

return reduce(gcd, nums) == 1

public boolean isGoodArray(int[] nums) {

• Step 2: We use the reduce function from the functools module to apply the gcd function cumulatively to the numbers in our

```
Step 3: First, reduce applies the gcd function to the first two elements, which are 6 and 10. The gcd of 6 and 10 is 2.
Step 4: The result (2) is then used with the next element in the array, which is 15. The gcd of 2 and 15 is 1.
```

Step 5: Since the reduce function has finished processing all elements, we check if the accumulated GCD is 1. In our case, it

numbers in our array nums that can add up to 1. Hence, for our input array, the function isGoodArray would evaluate to True,

According to Bezout's identity, because the final GCD is 1, there must be a combination of integer multiples of some or all

Here's a glimpse of how the code operates in this scenario:

from functools import reduce
from math import gcd

The simplicity of this algorithm lies in its use of the gcd function to examine the entire array in a single sweep. If the gcd of all elements is 1, we can confidently say that the array is "good" as it meets the criteria outlined in the problem description.

Python

from functools import reduce
from math import gcd

The function uses the greatest common divisor (gcd) to check if the array is 'good'.

Use the reduce function to apply the acd function cumulatively to the items of 'nums',

An array is 'good' if the gcd of all numbers in the array is 1.

from left to right, which reduces the array to a single value.

class Solution { // Method to check if the array is a good array based on the condition. // An array is considered good if the Greatest Common Divisor (GCD) of all its elements is 1.

```
// Iterate over each element in the array to find the overall gcd.
    for (int num : nums) {
        qcdValue = qcd(num, gcdValue); // Update gcdValue using the current element and the accumulated gcd.
        if (gcdValue == 1) {
            // If at any point the gcd becomes 1, we can return true immediately.
            return true;
    // The array is good if the final gcd value is 1.
    return gcdValue == 1;
// Helper method to calculate the gcd of two numbers using Euclid's algorithm.
private int qcd(int a, int b) {
    if (b == 0) {
       // If the second number b is 0, then gcd is the first number a.
        return a;
    } else {
        // Recursively call gcd with the second number and the remainder of a divided by b.
        return gcd(b, a % b);
```

// Note: TypeScript does not have a gcd function built—in, so you'll need to // either implement it yourself or include a library that provides it.

};

TypeScript

#include <vector>

class Solution {

public:

#include <numeric> // Required for std::gcd

for (int number : nums) {

// common divisor of all its elements is 1.

bool isGoodArray(std::vector<int>& nums) {

return greatestCommonDivisor == 1;

// Importing acd function from a math utilities module

def isGoodArray(self, nums: List[int]) -> bool:

Then, check if the final gcd value is 1.

return reduce(gcd, nums) == 1

// Function to determine if the array is a "good" array.

// A "good" array is defined as an array where the greatest

int greatestCommonDivisor = 0; // Initialize to 0

// which is in the numeric header.

// Iterating through each element in the given array 'nums'.

// Update the greatest common divisor using std::gcd,

greatestCommonDivisor = std::gcd(number, greatestCommonDivisor);

// The array is "good" if the GCD is 1 after processing all elements.

```
function gcd(a: number, b: number): number {
  // Base case for the recursion
  if (b === 0) return a:
  // Recursively calling gcd with the remainder
  return gcd(b, a % b);
// Function to determine if the array is a "good" array.
// A "good" array is defined as an array where the greatest
// common divisor of all its elements is 1.
function isGoodArray(nums: number[]): boolean {
  let greatestCommonDivisor: number = 0; // Initialize to 0
  // Iterating through each element in the given array 'nums'.
  for (let number of nums) {
    // Update the greatest common divisor using the gcd function.
    greatestCommonDivisor = gcd(greatestCommonDivisor, number);
  // The array is "good" if the GCD is 1 after processing all elements.
  return greatestCommonDivisor === 1;
from functools import reduce
```

The time complexity of the function is determined by the reduce function and the gcd (greatest common divisor) operations it performs on the list elements.

Therefore, the time complexity is:

Time and Space Complexity

The reduce function applies the gcd function cumulatively to the items of the list, from start to end, to reduce the list to a single value. The gcd function runs in O(log(min(a, b))) time, where a and b are the numbers whose GCD is being calculated.

from math import gcd

Time Complexity

class Solution:

operands, each subsequent gcd operation is typically faster than the last. However, for worst-case analysis, we'll consider each operation to have the complexity of O(log(k)), where k is the smallest element after each operation.

Assuming there are n elements in the nums list, the reduce function will perform n-1 gcd operations. Due to the nature of GCD

calculation, where after the first operation, the resulting GCD will often be lesser than or equal to the smallest number among the

0(n*log(k))

The function uses the greatest common divisor (gcd) to check if the array is 'good'.

Use the reduce function to apply the gcd function cumulatively to the items of 'nums',

An array is 'good' if the gcd of all numbers in the array is 1.

from left to right, which reduces the array to a single value.

Space Complexity The space complex

The space complexity of the code is 0(1).

• This space complexity comes from the fact that the gcd operations do not require additional space that scales with the input size, as they are

Where n is the number of elements in the list and k is the smallest number in the list at each step of the reduction.

This space complexity comes from the fact that the gcd operations do not require additional space that scales with the input size, as they are computed in constant space.
 The reduce function does not create any new data structures that depend on the input size; it just iterates over the existing list and updates the

Thus, the appear complexity is:

```
Thus, the space complexity is:

0(1)
```