2233. Maximum Product After K Increments

Greedy Array Heap (Priority Queue)

Medium

nums by 1 during each operation, and you can perform this operation at most k times. The goal is to maximize the product of all the elements in the array nums. After finding the maximum product, we need to return the result modulo 10^9 + 7 because the maximum product could be a very large number. The core of the problem lies in strategically choosing which numbers to increment to maximize the final product. Intuition

In order to maximize the product of the numbers, we want to even out the values as much as possible. This is because the

12. With this in mind, we arrive at the solution approach: Use a min-heap (a data structure that allows us to always extract the smallest number efficiently) to manage the numbers.

This ensures that we can always increment the smallest number available, which helps in balancing them as evenly as

product of numbers that are closer together is generally higher than the product of the same numbers that are not evenly spread.

For example, the product of [4, 4, 4] is 64, while the product of [2, 4, 6] is only 48, even though both sets have the same sum of

possible.

- Perform k operations of incrementing the smallest value in the min-heap. After each increment, the updated number is pushed back into the heap, maintaining the heap order. Once all the operations are done, calculate the product of all the elements in the heap. We have to keep in mind the modulo
- By following this approach, we effectively distribute the increments in a way that pushes the product to its maximum possible value before taking the modulo.

10^9 + 7 during this step by taking the modulo after each multiplication to prevent integer overflow.

The solution to this problem is implemented in Python and makes use of the heap data structure, which allows us to easily and efficiently access and increment the smallest element in the nums list. Here is the step-by-step explanation of the implementation:

Heapify the List: The first step is to convert the list nums into a min-heap using the heapify function from Python's heapq module. In a min-heap, the smallest element is always at the root, which allows us to apply our increments as effectively as

heapify(nums)

the next operation.

heappush(nums, heappop(nums) + 1)

for _ in range(k):

possible.

Solution Approach

Perform Increment Operations: Next, we perform k increments. For each operation, we extract the smallest element from the heap using heappop(nums), increment it by 1, and then push it back into the heap using heappush(nums, heappop(nums) + 1).

This ensures that our heap remains in a consistent state, with the smallest element always on top, ready to be incremented in

overflow. We initialize the ans variable to 1 and iterate through each value v in nums, applying the modulo operation as we multiply: ans = 1mod = 10**9 + 7for v in nums: ans = (ans * v) % mod

The key algorithm used here is the heap (priority queue), which allows us to prioritize incrementing the smallest numbers. The

pattern is simple yet effective: by giving priority to the smallest elements for incrementation, we use the operations to balance

the numbers, aiming for a more uniform distribution which leads to a maximized product. The implementation is careful to take

the product modulo 10^9 + 7 at each step, ensuring that the final result is within the correct range and doesn't overflow.

After heapify: [1, 2, 3] (Note: Since the array is already a valid min-heap, there's no visible change)

2nd increment: Now we have two 2s at the top. We pop one out, increment to 3, and push back.

Calculate the Product: Now we calculate the product of the heap's elements modulo 10^9 + 7.

Calculate the Product: Once all increments are done, we iterate through all elements in the heap to calculate the product.

Because we're looking for the product modulo 10^9 + 7, we take the modulo after each multiplication to prevent integer

Example Walkthrough

Starting array: [1, 2, 3]

Starting with ans = 1,

Solution Implementation

heapify(nums)

product = 1

for _ in range(k):

modulo = 10**9 + 7

for num in nums:

return product

class Solution {

Python

class Solution:

Imagine we have nums = [1, 2, 3] and k = 3.

Heapify the List: We convert nums into a min-heap.

1st increment: Smallest is 1. We pop 1 out, increment to 2, and push back to heap. Heap after 1st increment: [2, 2, 3]

Return the Result: Finally, we return the calculated ans as the result.

Let's walk through a small example to illustrate the solution approach.

Perform Increment Operations: We are allowed 3 increments.

Heap after 3rd increment: [3, 3, 3] We've used our 3 increments to even out the numbers, as predicted by our intuition.

For next 3: ans = (3 * 3) % 1000000007 = 9

For last 3: ans = (9 * 3) % 1000000007 = 27

So the final product modulo 10^9 + 7 is 27.

from heapq import heapify, heappop, heappush

def maximumProduct(self, nums, k):

3rd increment: One more increment to the remaining 2.

Heap after 2nd increment: [2, 3, 3]

For 3: ans = (1 * 3) % 1000000007 = 3

Return the Result: The result, 27, is returned as the final output.

Java

// increment it and add it back to the heap.

// Calculate the product of all elements now in the heap.

int incrementedValue = minHeap.poll() + 1;

answer = (answer * minHeap.poll()) % MOD;

int maximumProduct(std::vector<int>& nums, int k) {

// Create a min-heap from the given vector nums

// Compute the product of all elements modulo mod

import { MinPriorityQueue } from '@datastructures-js/priority-queue';

const int mod = 1e9 + 7; // Modulo value for the final result

std::make_heap(nums.begin(), nums.end(), std::greater<int>());

++nums.back(); // Increment the smallest element

// Iteratively increment the smallest element and then reheapify

long long product = 1; // Use long long to avoid integer overflow

return static_cast<int>(product); // Cast to int to match return type

* Calculates the maximum product of an array after incrementing any element "k" times.

std::pop_heap(nums.begin(), nums.end(), std::greater<int>());

std::push_heap(nums.begin(), nums.end(), std::greater<int>()); // Reheapify

product = (product * v) % mod; // Update the product with each element

// Return the final product modulo MOD as an integer.

minHeap.offer(incrementedValue);

// Define the MOD constant to use for avoiding integer overflow issues.

// Function to calculate the maximum product of array elements after

Convert the list nums into a min-heap in-place

Increment the smallest element in the heap k times

Calculate the product of all elements mod 10^9 + 7

product = (product * num) % modulo

private static final int MOD = (int) 1e9 + 7;

smallest = heappop(nums) # Pop the smallest element

```
// incrementing any element 'k' times.
public int maximumProduct(int[] nums, int k) {
   // Initialize a min-heap (PriorityQueue) to store the elements.
   PriorityQueue<Integer> minHeap = new PriorityQueue<>();
   // Add all the elements to the min-heap.
    for (int num : nums) {
       minHeap.offer(num);
   // Increment the smallest element in the heap 'k' times.
   while (k-- > 0) {
       // Retrieve and remove the smallest element from the heap,
```

// Initialize the answer as a long to prevent overflow during the computation.

// Take each element from the heap, multiply it with the current answer

heappush(nums, smallest + 1) # Increment the smallest element and push back onto heap

```
#include <algorithm>
#include <functional> // for std::greater
class Solution {
public:
```

while (k-- > 0) {

#include <vector>

C++

/**

long answer = 1;

return (int) answer;

while (!minHeap.isEmpty()) {

// and compute the modulus.

```
};
TypeScript
```

* @param {number[]} nums An array of numbers.

* @param {number} k The number of increments to perform.

* @returns {number} The maximum product modulo 10^9 + 7.

function maximumProduct(nums: number[], k: number): number {

for (int v : nums) {

```
const n: number = nums.length;
      let priorityQueue: MinPriorityQueue<number> = new MinPriorityQueue<number>();
      // Initialize the priority queue with all elements from the nums array
      for (let i = 0; i < n; i++) {
          priorityQueue.enqueue(nums[i]);
      // Increment the smallest element in the queue k times
      for (let i = 0; i < k; i++) {
          let minElement: number = priorityQueue.dequeue().element;
          priorityQueue.enqueue(minElement + 1);
      let product: number = 1;
      const MODULO: number = 10 ** 9 + 7;
      // Calculate the product of all elements in the queue
      for (let i = 0; i < n; i++) {
          product = (product * priorityQueue.dequeue().element) % MODULO;
      return product;
  // Note: This code assumes that MinPriorityQueue<number> is imported correctly and available.
from heapq import heapify, heappop, heappush
class Solution:
```

heappush(nums, smallest + 1) # Increment the smallest element and push back onto heap

Time Complexity The time complexity of this code is determined by the following parts:

Time and Space Complexity

def maximumProduct(self, nums, k):

heapify(nums)

product = 1

for _ in range(k):

modulo = 10**9 + 7

for num in nums:

return product

Convert the list nums into a min-heap in-place

Increment the smallest element in the heap k times

Calculate the product of all elements mod 10^9 + 7

product = (product * num) % modulo

smallest = heappop(nums) # Pop the smallest element

elements in nums. K Pop and Push Operations: We pop the smallest element and then push an incremented value back onto the heap, k times.

which is a tree of height log n. Therefore, the time complexity for this part is 0(k log n). Final Iteration to Calculate Product: We iterate over the heap of size n once and do a multiplication each time. Since the heap

Heapify Operation: Converting the nums array into a min-heap has a time complexity of O(n) where n is the number of

is already a valid heap structure, and we are simply iterating over it, the iteration takes O(n) time. Thus, the overall time complexity is $0(n + k \log n + n) = 0(n + k \log n)$, assuming k pop and push operations dominate for

Each such operation might take O(log n) time since in the worst case, the element might need to sift down/up the heap

The space complexity is determined by:

larger values of k.

Space Complexity

Heap In-Place: Since the heap is constructed in-place, it does not require additional space proportional to the input size

- beyond the initial list. Therefore, we consider this 0(1) additional space. Intermediate Variables: Only a constant amount of extra space is used for variables like ans and mod, which is also 0(1).
- Therefore, the space complexity of the algorithm is 0(1).

- **Problem Description** The problem provides us with a list of non-negative integers named nums and an integer k. The task is to increase any element of