## 802. Find Eventual Safe States

**Depth-First Search Breadth-First Search Graph** 

#### **Problem Description**

In this problem, we are given a directed graph with n nodes labeled from 0 to n-1. The graph is defined by a 2-dimensional array graph where graph[i] contains a list of nodes that have directed edges from node i. If a node doesn't have any outgoing edges, we label it as a terminal node. Our task is to find all the safe nodes in this graph. A safe node is one from which every possible path leads to a terminal node or to another safe node (which will eventually lead to a terminal node).

**Topological Sort** 

Our goal is to return an array of all the safe nodes in sorted ascending order.

### The concept of safe nodes can be thought of in terms of a topological sort—the nodes that can eventually reach terminal nodes

Intuition

Medium

without falling into a cycle are considered safe. We can represent each node with different states to help us in our search for safe nodes: unvisited (color 0), visiting (color 1), and safe (color 2). The depth-first search (DFS) algorithm can help us perform this search. If we are visiting a node and encounter a node that is

already being visited, this means we have a cycle, and hence, the starting node cannot be a safe node. On the contrary, if all paths from a node lead to nodes that are already known to be safe or terminal, the node in question is also safe. We make use of a coloring system to mark the nodes:

• Color 1: The node is currently being visited (we're in the process of exploring its edges). • Color 2: The node and all its children can safely lead to a terminal node.

• Color 0: The node has not been visited yet.

- We start our DFS with the unvisited nodes and explore their children. If during the exploration, we encounter a node that is
- currently being visited (color 1), this means there is a cycle, and we return False, marking the node as unsafe. We continue this process for all nodes, and those that end up marked as color 2 (safe), are added to our list of safe nodes.

topological sort, which is suitable for such dependency-based problems. Solution Approach

This approach ensures that we are only considering nodes that lead to terminal nodes as safe, effectively implementing a

The solution approach is centered on using the concepts of <a href="Depth-First Search">Depth-First Search</a> (DFS) and coloring to determine which nodes are safe in the graph.

## The key part of the implementation is the dfs function, which is recursive and performs the following steps:

final list of safe nodes.

1. Check if the current node i has already been visited: If so, return whether it's a safe node (color[i] == 2). 2. Mark the node as currently being visited (color it with 1).

3. Iterate through all the adjacent nodes (those found in [graph](/problems/graph\_intro)[i]): • For each adjacent node, call the dfs function on it. If the dfs on any child returns False, marking it as part of a cycle or path to an unsafe

Let's consider a simple directed graph with four nodes (0 to 3) defined by the 2-dimensional array graph:

- node, the current node i cannot be a safe node, so return False. 4. If all adjacent nodes are safe or lead to safe nodes, mark the current node i as safe (color it with 2) and return True.
- The driver code does the following:

• Initializes an array color with n elements as 0, to store the state (unvisited, visiting, or safe) of each node.

node. This approach is efficient as it marks nodes that are part of cycles as unsafe early on through the depth-first search and avoids

reprocessing nodes that have already been determined to be safe or unsafe. This minimizes the exploration we need to do when

• It then iterates over each node and applies the dfs function. If the dfs function returns True, it indicates the node is safe, and it's added to the

• The list of safe nodes is then returned, which are the nodes from which every path leads to a terminal node or eventually reaches another safe

determining the safety of subsequent nodes. **Example Walkthrough** 

graph[0] = [1, 2]graph[1] = [2]graph[2] = [3]graph[3] = []

Here, we have edges from node 0 to nodes 1 and 2, from node 1 to node 2, and from node 2 to node 3. Node 3 doesn't have any

#### outgoing edges, so it's a terminal node.

as safe.

2. We see that node 0 has two adjacent nodes: node 1 and node 2. We explore node 1 first: Node 1 is unvisited; mark it as visiting (color 1).

```
■ Node 2 is unvisited; mark it as visiting (color 1).
Node 2 has one adjacent node, node 3. We explore node 3:
    ■ Node 3 is unvisited and has no outgoing edges, so it's a terminal node. Mark it as safe (color 2).
```

Node 1 has one adjacent node, node 2. We explore node 2:

We apply our DFS-based solution approach to identify safe nodes.

1. Start with node 0, which is unvisited. We mark it as visiting (color it with 1).

3. Then we resume exploring the adjacent nodes of node 0 and move on to node 2.

Since node 2 is safe, we mark node 1 as safe (color 2) and return True.

 Node 2 is already marked safe (color 2), so we return True. 4. All paths from node 0 lead to safe nodes, so we mark node 0 as safe (color 2).

■ Since node 3 is safe, we mark node 2 as safe (color 2) and return True.

In the end, the driver code collects all nodes colored as 2, sorts them (which is not necessary in this case, as the array is already sorted), and returns the list of safe nodes: [0, 1, 2, 3].

def eventualSafeNodes(self, graph: List[List[int]]) -> List[int]:

# If all connected nodes are safe, mark this node as safe (color 2)

// A node is considered safe if all its possible paths lead to a terminal node.

nodeColors[node] = 1; // Mark the node as visited (color coded as 1)

if (nodeColors[node] > 0) { // If the node is already visited, return its state

return node colors[node index] == 2

# Mark this node as visited (color 1)

if node colors[node index]:

node\_colors[node\_index] = 1

return False

node\_colors[node\_index] = 2

private boolean isNodeSafe(int node) {

// Explore all connected nodes recursively

return true; // Return true indicating the node is safe

for (int neighbor : graph[node]) {

return colors[nodeIndex] == 2;

for (int neighbor : graph[nodeIndex]) {

if (!dfs(neighbor, graph)) {

return false;

colors[nodeIndex] = 1; // Mark the node as visiting

colors[nodeIndex] = 2; // Mark the node as safe

return true; // Return true as the node is safe

// Function to determine the eventual safe nodes in a graph

const eventualSafeNodes = (graph: number[][]): number[] => {

const dfs = (nodeIndex: number): boolean => {

return color[nodeIndex] === 2;

return true; // The node is safe

if node\_colors[node\_index]:

node\_colors[node\_index] = 1

return False

node\_colors[node\_index] = 2

# Get the number of nodes in the graph

return True

return safe\_nodes

total nodes = len(graph)

node\_colors = [0] \* total\_nodes

return node\_colors[node\_index] == 2

for next\_node\_index in graph[node\_index]:

# Initialize a list to store the status of the nodes

# Color 0 means unvisited, 1 means visiting, 2 means safe

# Mark this node as visited (color 1)

if not dfs(next\_node\_index):

// Iterate over each node in the graph

// @returns An array of indices representing eventual safe nodes

// @param nodeIndex - The current node index being visited

// @param graph - The adjacency list representation of a directed graph

const n: number = graph.length; // Number of nodes in the graph

// Depth-first search function to determine if a node leads to a cycle or not

// @returns A boolean indicating if the node is safe (does not lead to a cycle)

// If the node has been visited, return true if it's marked as safe, false otherwise

color[nodeIndex] = 2; // Mark the node as safe since no cycles were found from it

// Explore all the neighbors of the current node

return false;

return True

**Python** from typing import List

Since we've visited all nodes and no cycles were detected, and all nodes lead to a terminal node, all nodes (0, 1, 2, 3) are marked

# Helper function to perform a depth-first-search (dfs) # to determine if a node leads to a cycle (not safe) or not. def dfs(node\_index): # If the node is already visited, return True if it is safe (color 2)

#### # Traverse all connected nodes to see if they lead to a cycle for next\_node\_index in graph[node\_index]: # If a connected node is not safe, then this node is also not safe if not dfs(next\_node\_index):

class Solution:

Solution Implementation

```
# Get the number of nodes in the graph
       total nodes = len(graph)
       # Initialize a list to store the status of the nodes
       # Color 0 means unvisited, 1 means visiting, 2 means safe
       node_colors = [0] * total_nodes
       # Use list comprehension to gather all nodes that are safe after DFS
       # These are the eventual safe nodes that do not lead to any cycles
       safe_nodes = [node_index for node_index in range(total_nodes) if dfs(node_index)]
       return safe nodes
Java
class Solution {
   private int[] nodeColors;
   private int[][] graph;
   // Method to determine all the eventual safe nodes in a graph
    public List<Integer> eventualSafeNodes(int[][] graph) {
       int n = graph.length;
       nodeColors = new int[n]; // Initialize array to store the state of each node
       this.graph = graph; // Assign graph to class variable for easy access
       List<Integer> safeNodes = new ArrayList<>(); // List to store eventual safe nodes
       // Iterate over each node to determine if it's a safe node
        for (int i = 0; i < n; ++i) {
            if (isNodeSafe(i)) { // If the current node is safe, add it to the list
               safeNodes.add(i);
       return safeNodes; // Return the final list of safe nodes
   // Helper method - Conducts a depth-first search to determine if a node is safe.
```

return nodeColors[node] == 2; // Return true if the node leads to a terminal node, i.e., is safe (color coded as 2)

if (!isNodeSafe(neighbor)) { // If any connected node is not safe, then this node is not safe either

```
nodeColors[node] = 2; // Since all connected nodes are safe, mark this node as safe (color coded as 2)
```

C++

public:

#include <vector>

class Solution {

using namespace std;

**}**;

**TypeScript** 

**}**;

```
vector<int> eventualSafeNodes(vector<vector<int>>& graph) {
    int n = graph.size();
   colors.assign(n, 0); // Initialize all nodes as unvisited
   vector<int> safeNodes; // List to hold the eventual safe nodes
   // Check each node to see if it's eventually safe
    for (int i = 0; i < n; ++i) {
        if (dfs(i, graph)) {
            safeNodes.push_back(i); // If it is safe, add it to the list
    return safeNodes; // Return the list of safe nodes
// Depth-first search to determine if a node is safe
bool dfs(int nodeIndex, vector<vector<int>>& graph) {
   if (colors[nodeIndex]) {
```

const color: number[] = new Array(n).fill(0); // Array to mark the state of each node: 0 = unvisited, 1 = visiting, 2 = safe

vector<int> colors; // Color array to mark the states of nodes: 0 = unvisited, 1 = visiting, 2 = safe

// If the node has been visited already, return true only if it's marked as safe

// If any neighbor is not safe, the current node is not safe either

#### color[nodeIndex] = 1; // Mark the node as visiting for (const neighbor of graph[nodeIndex]) { // Visit all neighbors to see if any lead to a cycle if (!dfs(neighbor)) { // If any neighbor is not safe, the current node is not safe either return false;

for (let i = 0; i < n; ++i) {

**if** (dfs(i)) {

if (color[nodeIndex]) {

```
// If the node is safe, add it to the result
              ans.push(i);
      return ans; // Return the list of safe nodes
from typing import List
class Solution:
   def eventualSafeNodes(self, graph: List[List[int]]) -> List[int]:
       # Helper function to perform a depth-first-search (dfs)
       # to determine if a node leads to a cycle (not safe) or not.
       def dfs(node_index):
```

# If the node is already visited, return True if it is safe (color 2)

# If a connected node is not safe, then this node is also not safe

safe\_nodes = [node\_index for node\_index in range(total\_nodes) if dfs(node\_index)]

# If all connected nodes are safe, mark this node as safe (color 2)

# Traverse all connected nodes to see if they lead to a cycle

# Use list comprehension to gather all nodes that are safe after DFS

# These are the eventual safe nodes that do not lead to any cycles

let ans: number[] = []; // Initialize an array to keep track of safe nodes

```
Time Complexity
```

**Time and Space Complexity** 

The time complexity is 0(N + E), where N is the number of nodes and E is the number of edges in the graph. This is because each node is processed exactly once, and we perform a Depth-First Search (DFS) that in total will explore each edge once. When a node is painted grey (color[i] = 1), it represents that the node is being processed. If it is painted black (color[i] = 2), the node and all nodes leading from it are safe. The DFS will terminate early if a loop is found (thus encountering a grey node during DFS), ensuring each edge is only fully explored once in the case of a safe node.

# The space complexity is O(N). This is due to the color array, which keeps track of the state of each node, using space

**Space Complexity** 

proportional to the number of nodes N. Additionally, the system stack space used by the recursive DFS calls must also be considered; in the worst case, where the graph is a single long path, the recursion depth could potentially be N, adding to the space complexity. However, since space used by the call stack during recursion and the color array are both linear with respect to the number of nodes, the overall space complexity remains O(N).