2779. Maximum Beauty of an Array After Applying Operation Medium Array Binary Search Sorting Sliding Window Leetcode Link

Problem Description

You are provided with an array nums which is 0-indexed. This means the first element of the array is at position 0, the next element is at position 1, and so on. A non-negative integer k is also given to you.

There is a set of operations you can perform on nums to potentially increase its beauty. An array's beauty is defined as the length of

the longest subsequence where all elements are equal. A subsequence is any subset of the array that is not necessarily contiguous but maintains the original order of elements.

Each operation follows two steps:

Choose an index i from the array which has not been chosen before.
 Replace the element at nums[i] with any number within the range [nums[i] - k, nums[i] + k].

array after applying all possible operations.

- Vour goal is to execute these energtions as many times as you ase fit to
- Your goal is to execute these operations as many times as you see fit to maximize the beauty of the array, but you can only choose each index once. The question asks for the maximum beauty that can be achieved through such operations.

nums[i] - k to nums[i] + k), where all numbers in this reach can be made equal to nums[i].

Intuition

The problem is, in essence, about finding the largest group of numbers in the nums array that can be made equal through the allowed operations. If we can increase or decrease each number by up to k, we can think of each number as having a "reach" of 2k + 1 (from

its count.

One approach to solving this problem is to use a difference array, which is an efficient method for applying updates over a range of indices in an array. The general idea is to build an augmented array, d, where each element represents the difference between successive elements in the nums array. This array d is then used to accumulate the total possible count of each value in the original

The array d is initialized with zeros and should have enough capacity to accommodate the largest number after an operation (which is max(nums) + 2 * k + 1) plus an additional element. For each element in nums, we can perform the following in the array d:

1. Increment the value at index x (the original number) because you can always choose not to change the number, contributing to

2. Decrement the value at index x + 2 * k + 1, which is beyond the reach of the operations from nums [i], thus ending the impact of this specific number.

found, which corresponds to the maximum beauty of the array.

In each step, s is incremented by the current value in d, and ans is updated if s is greater than the current ans.

Here's a step-by-step breakdown of the maximumBeauty function's implementation:

 \circ Decrement the count at d[x + k * 2 + 1] to indicate the end point of the range.

Here, the variable ans is used to track the maximum beauty, and s is the running sum while iterating through the augmented array d.

Once the difference array d is fully populated, we iterate over it, accumulating the counts and keeping track of the maximum value

Overall, this approach effectively allows assessing the impact of all operations in a cumulative fashion, facilitating the computation of the maximum beauty in a time-efficient manner.

The provided solution uses a difference array as a key data structure. A difference array is an array that allows updates over intervals in the original array in O(1) time and querying in O(n) time, where n is the number of elements. This turns out to be very

efficient for certain types of problems — such as this one, where we repeatedly perform a fixed change to a range of elements.

1. Calculate the size m for the difference array by taking the maximum element in nums, adding twice k, and then adding 2. This guarantees the difference array can cover all the values after all the operations. The actual value is m = max(nums) + k * 2 + 2.

Solution Approach

Initialize a difference array d with size m filled with zeros. This array will track the potential increases and decreases over the ranges from all nums [i].
 Loop through each number x in nums and:

• Increment the count at d[x] to indicate the potential start point of numbers in the range [x-k, x+k] to be adjusted to x.

4. Initialize ans, which will store the maximum beauty of the array, and s, which will be used as the running sum to apply the effect of the difference array when traversing it.

5. Traverse the difference array d, accumulating the total effect in s at each step, and update ans if the new sum s is greater than

the current ans. This traversal allows us to collect the effective total count for each number as though all operations have been

applied.

the maximum beauty of the array nums.

- 6. Finally, return ans, which is now the longest length of a subsequence that can be created through the allowed modifications —
- directly compute the result instead of performing each operation individually.

To sum up, this solution is based on the insight that we can use a difference array to efficiently simulate all the operations and

Suppose we have an array nums = [1, 3, 4] and k = 1.

First, we follow these steps to maximize the beauty of the array:

Calculate the size for the difference array. With a max(nums) of 4, k * 2 is 2, so m is 4 + 2 + 2 which gives us 8.
 Initialize the difference array d to be size 8, filled with zeros: d = [0, 0, 0, 0, 0, 0, 0, 0].

• For x = 1, increment d[1] and decrement d[1 + 1 * 2 + 1], so d becomes [0, 1, 0, -1, 0, 0, 0]. • For x = 3, increment d[3] and decrement d[3 + 1 * 2 + 1], so d becomes [0, 1, 0, 0, 0, -1, 0, 0].

4. Initialize ans to 0 and s to 0.

Example Walkthrough

 \circ For x = 4, increment d[4] and decrement d[4 + 1 * 2 + 1], so d becomes [0, 1, 0, 0, 1, -1, 0, -1].

 \circ s = 1 + 0 \rightarrow d[3] = 0, ans remains 1.

 \circ s = 1 + 1 \rightarrow d[4] = 1, update ans to 2.

 \circ s = 2 - 1 → d[5] = -1, ans remains 2.

3. Loop through each number in nums and update the difference array:

5. Traverse the difference array d, updating ans as we accumulate s:

Let's consider a small example to illustrate the solution approach.

- s = 0 → d[0] = 0, ans remains 0.
- s = 0 + 1 → d[1] = 1, update ans to 1.
 s = 1 + 0 → d[2] = 0, ans remains 1.
- s = 1 + 0 → d[6] = 0, ans remains 2.
 s = 1 1 → d[7] = -1, ans remains 2.

def maximumBeauty(self, flowers: List[int], steps: int) -> int:

Initialize a difference array with the same range

 $max_flower = max(flowers) + steps * 2 + 2$

diff_array[flower_count] += 1

diff_array = [0] * max_flower

for flower_count in flowers:

max_beauty = running_sum = 0

for count_diff in diff_array:

running_sum += count_diff

Return the maximum beauty value found

int maximumBeauty(vector<int>& flowers, int k) {

diffArray[flower + k * 2 + 1] --;

vector<int> diffArray(maxValue, 0);

for (int flower : flowers) {

diffArray[flower]++;

for (int count : diffArray) {

currentSum += count;

// Calculate the maximum value in the vector and set the range accordingly,

// Iterate over the original array and update the differential array accordingly.

// Calculate the maximum beauty seen so far by taking the maximum of the

// Increase the count at the start of the window (flower's position).

int maxValue = *max_element(flowers.begin(), flowers.end()) + k * 2 + 2;

// Create a differential array with the size based on calculated range.

// Decrease the count at the end of the window.

// Update the running sum with the current count.

// current running sum and the previous maxBeauty.

maxBeauty = max(maxBeauty, currentSum);

// considering the range needs to be large enough to account for adding k to both sides.

Calculate the maximum constant for adjusting the range

Construct the difference array to perform range updates

Initialize the variables for tracking the maximum beauty and the running sum

Apply the difference array technique to find the total at each point

diff_array[flower_count + steps * 2 + 1] -= 1

max_beauty = max(max_beauty, running_sum)

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From the walkthrough, we can see with nums = [1, 3, 4] and k = 1, the maximum beauty that can be achieved is 2, since we can transform the array to [3, 3, 3] by incrementing the first element 1 by 2 (which is within the range [1 - 1, 1 + 1]) and decrementing the last element 4 by 1 (which is within the range [4 - 1, 4 + 1]), resulting in two 3s which creates the longest subsequence of equal numbers.

Python Solution
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6. Finally, return ans which is 2. This means the largest length of a subsequence where all elements are equal after the operations

return max_beauty 26

Java Solution

import java.util.Arrays;

1 from typing import List

class Solution:

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public class Solution {
       public int maximumBeauty(int[] flowers, int additions) {
           // Calculate the maximum value after all possible additions.
           // We add extra space for fluctuations in the count within the k range.
           int maxValue = Arrays.stream(flowers).max().getAsInt() + additions * 2 + 2;
            int[] delta = new int[maxValue];
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           // Build the difference array using the number of additions possible adding and subtracting at the range ends.
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           for (int flower: flowers) {
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               delta[flower]++;
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               delta[flower + additions * 2 + 1]--;
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           int maxBeauty = 0; // This will hold the maximum beauty calculated so far.
            int runningSum = 0; // This will be used to compute the running sum from the difference array.
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           // Compute the running sum and find the maximum value.
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            for (int value : delta) {
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                runningSum += value;
               maxBeauty = Math.max(maxBeauty, runningSum);
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           // Return the computed maximum beauty of the bouquet.
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           return maxBeauty;
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29 }
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// Initialize variables to track the sum and the maximum beauty so far. int currentSum = 0, maxBeauty = 0; // Iterate over the differential array and calculate the prefix sum, // which gives us the running count of flowers.

C++ Solution

1 class Solution {

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           // Return the maximum beauty that can be achieved.
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           return maxBeauty;
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35 };
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Typescript Solution
   function maximumBeauty(nums: number[], operationsAllowed: number): number {
       // Calculate a maximum boundary to create an array that is big enough to hold all possible values after operations.
       const maxBoundary = Math.max(...nums) + operationsAllowed * 2 + 2;
       // Initialize difference array to hold the frequency of numbers up to the maximum boundary.
       const differenceArray: number[] = new Array(maxBoundary).fill(0);
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       // Iterate over the input array and update the difference array based on the allowed operations.
       for (const num of nums) {
           // For each number, increment the count at the number's index in the difference array.
           differenceArray[num]++;
           // Decrement the count at the index that is 'operationsAllowed' doubled and one past the current number.
           differenceArray[num + operationsAllowed * 2 + 1]--;
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       let maxBeauty = 0; // Store the maximum beauty value found.
       let sum = 0:
                          // Accumulator to store the running sum while iterating over the difference array.
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       // Iterate over the difference array to find the maximum accumulated frequency (beauty).
18
       for (const frequency of differenceArray) {
           // Update the running sum by adding the current frequency.
           sum += frequency;
           // Update the maximum beauty value if the current running sum is greater than the previous maximum.
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           maxBeauty = Math.max(maxBeauty, sum);
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25
       // Return the maximum beauty value found.
26
       return maxBeauty;
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The provided code implements a function to determine the maximum beauty of an array after performing certain operations. The key operations to analyze are the loops and the creation of the list d.

Time and Space Complexity

Time Complexity:
 The first part of the analysis involves the line m = max(nums) + k * 2 + 2. This operation is O(n) where n is the number of elements in nums, as it requires a pass through the entire list to determine the maximum value.

The loop that populates the list d iterates over each element in nums, so this part is 0(n). Inside this loop, there are constant-time operations 0(1) (incrementing and decrementing the values).

max(nums) + 2 * k.

maximum value in nums.

The variables ans and s are of constant space 0(1).

• The final loop iterates through the list d which has a length of m. This loop has a time complexity of O(m) as it needs to visit each element in d to accumulate the sum and compute the maximum.

• The creation of the list d with a length of m is O(m). This accounts for the space required to store the frequency differences.

- Combining these complexities, we get O(n) + O(m) + O(n) + O(m) which simplifies to O(n + m), with m being proportional to
- Space Complexity:

 The list d with length m is the most significant factor in space complexity, making it O(m), as it depends on the value of k and the
- Hence, the final time complexity is 0(n + m) and the space complexity is 0(m), taking into account the size of the input nums and the range of values derived from it combined with k.

range of values derived from it combined with k.