Problem Description

Medium Array

The problem is to create an algorithm that can efficiently search for a specific value, called target, within a 2-dimensional matrix. The dimensions of the matrix are $m \times n$, which means it has m rows and n columns. The matrix is not just any random assortment of integers—it has two key properties that can be leveraged to make searching efficient:

Matrix

1. Each row of the matrix is sorted in ascending order from left to right.

- 2. Each column of the matrix is sorted in ascending order from top to bottom.
- Given these sorted properties of the matrix, the search should be done in a way that is more optimized than a brute-force

Binary Search Divide and Conquer

approach which would check every element. Intuition

To intuitively understand the solution, we should recognize that because of the row and column properties, the matrix resembles

search, we can make an observation: • If we start in the bottom-left corner of the matrix (or the top-right), we find ourselves at an interesting position: moving up decreases the value (since columns are sorted in ascending order from top to bottom), and moving right increases the value (since rows are sorted in ascending

a 2D binary search problem. However, instead of splitting our search space in half each time as we would in a conventional binary

order from left to right). This starting point gives us a "staircase" pattern to follow based on comparisons: 1. If the target is greater than the value at our current position, we know it can't be in the current row (to the left), so we move to the right

2. If the target is less than the value at our current position, we know it can't be in the current column (below), so we move up (decrease the row index).

- By doing this, we are eliminating either a row or a column at each step, leveraging the matrix's properties to find the target or
- conclude it's not there. We keep this up until we find the target or exhaust all our moves (when we move out of the bounds of the matrix), in which case the target is not present. This is why the while loop condition in the code checks if i >= 0 and j < n. The process is very much like tracing a path through the matrix that "zig-zags" closer and closer to the value if it's present. The

solution here effectively combines aspects of both binary search and linear search but applied in a 2-dimensional space. **Solution Approach**

The solution provided is a direct implementation of the intuitive strategy discussed previously. Here's how the solution is

We declare a Solution class with a method searchMatrix that accepts a 2D matrix and the target value as parameters.

Inside the searchMatrix method, we start by getting the dimensions of the matrix: m for the number of rows and n for the

implemented:

(increase the column index).

number of columns, which will be used for boundary checking during the search. We initiate two pointers, i and j, which will traverse the matrix. i is initialized to m - 1, which means it starts from the last

- row (bottom row), and j is initialized to 0, which is the first column (leftmost column). This represents the bottom-left corner of the matrix.
- sure that i is never less than 0 (which would mean we've moved above the first row) and j is less than n (to ensure we don't move beyond the last column to the right).

The search begins and continues as long as our pointers are within the bounds of the matrix. The while loop condition makes

- 1. If the element at the current position matrix[i][j] equals the target, then our search is successful, and we return True. 2. If the element at matrix[i][j] is greater than the target, we must move up (decrease the value of i) to find a smaller element. 3. Conversely, if matrix[i][j] is less than the target, we must move right (increase the value of j) in hopes of finding a larger element. If we exit the loop without returning True, it means we have exhausted all possible positions in the matrix without finding the
- This approach effectively traverses the matrix in a manner such that with each comparison, a decision can be made to eliminate either an entire row or an entire column, significantly reducing the search space and making the algorithm efficient. The worst

And let's say we are searching for the target value 5.

Start from the bottom left corner of the matrix

Check if the current element is the target

Return False if we haven't returned True by this point

if matrix[row index][col_index] == target:

while row index >= 0 and col index < num cols:</pre>

Loop until we have a valid position within the matrix bounds

row_index, col_index = num_rows - 1, 0

return True

col_index += 1

// Target was not found in the matrix

// @param matrix The matrix of integers.

// Get the number of rows.

// Get the number of columns.

int rows = matrix.size();

// @param target The target integer to find.

// Searches for a target value within a 2D matrix. This matrix has the following properties:

// Integers in each row are sorted in ascending from left to right.

// Integers in each column are sorted in ascending from top to bottom.

// row will be too large given the matrix's sorted properties

// move right to the next column since all values in previous

// If we've exited the while loop, the target is not present in the matrix

Loop until we have a valid position within the matrix bounds

If current element is larger than target, move up to reduce value

// columns will be too small given the matrix's sorted properties

// If the current element is less than the target,

if (currentElement > target) {

def searchMatrix(self. matrix. target):

Rows and columns in the matrix

row_index, col_index = num_rows - 1, 0

num_rows, num_cols = len(matrix), len(matrix[0])

while row index >= 0 and col index < num cols:</pre>

Start from the bottom left corner of the matrix

Check if the current element is the target

if matrix[row index][col_index] == target:

if matrix[row index][col_index] > target:

Return False if we haven't returned True by this point

--currentRow;

++currentColumn;

} else {

return false;

class Solution:

return false;

#include <vector>

class Solution {

public:

using namespace std;

n), where m is the number of rows and n is the number of columns.

target, and thus we return False.

Within the loop, there are three cases to consider:

Example Walkthrough Let's walk through a small example to illustrate the solution approach. Consider the following 3×4 matrix and a target value to

case scenario would be traversing from the bottom-left corner to the top-right corner, which gives us a time complexity of O(m +

search for: [[1, 4, 7, 11],

Using the solution approach, we start at the bottom-left corner of the matrix. This means our starting position is at the last row, first column: matrix[2][0], which is 3.

[2, 5, 8, 12],

[3, 6, 9, 16]]

Now, we compare the target value 5 with the value at our current position: target (5) > matrix[2][0] (3) so the target can't be in the current row because all values to the left are smaller. We move

```
right to increase the value (increment j): now we are at matrix[2][1], which is 6.
target (5) < matrix[2][1] (6) so the target can't be in the current column because all values below are larger. We move up
```

This approach avoided checking every single element in the matrix, instead, by leveraging the sorted nature of the rows and

columns, it quickly hones in on the target with a clear strategy. Even if the target number was not present, the process would

eventually move out of the matrix bounds, at which point we would return False, signifying that the target is not found.

Solution Implementation

to decrease the value (decrement i): now we are at matrix[1][1], which is 5.

At this point, matrix[1][1] equals the target value 5, so our search is successful, and we return True.

Python class Solution: def searchMatrix(self, matrix, target): # Rows and columns in the matrix num_rows, num_cols = len(matrix), len(matrix[0])

If current element is larger than target, move up to reduce value if matrix[row index][col_index] > target: row index -= 1 # If current element is smaller than target, move right to increase value

else:

return False

Java

class Solution {

```
/**
* Searches for a target value in a 2D matrix.
* The matrix has the following properties:
 * - Integers in each row are sorted in ascending from left to right.
* - The first integer of each row is greater than the last integer of the previous row.
* @param matrix 2D matrix of integers
* @param target The integer value to search for
* @return boolean indicating whether the target is found
*/
public boolean searchMatrix(int[][] matrix, int target) {
    // Get the number of rows and columns in the matrix
    int rowCount = matrix.length;
    int colCount = matrix[0].length;
    // Start from the bottom—left corner of the matrix
    int row = rowCount - 1;
    int col = 0;
    // Perform a staircase search
    while (row >= 0 && col < colCount) {</pre>
        if (matrix[row][col] == target) {
            // Target is found at the current position
            return true;
        if (matrix[row][col] > target) {
            // Target is less than the current element, move up
            row--;
        } else {
            // Target is greater than the current element, move right
            col++;
```

// @return True if target is found, false otherwise. bool searchMatrix(vector<vector<int>>& matrix, int target) {

```
int columns = matrix[0].size();
        // Start from the bottom-left corner of the matrix.
        int currentRow = rows - 1;
        int currentColumn = 0;
        // While the position is within the bounds of the matrix...
        while (currentRow >= 0 && currentColumn < columns) {</pre>
            // If the current element is the target, return true.
            if (matrix[currentRow][currentColumn] == target) return true;
            // If the current element is larger than the target, move up one row.
            if (matrix[currentRow][currentColumn] > target) {
                --currentRow;
            // If the current element is smaller than the target, move right one column.
            else {
                ++currentColumn;
        // If the target is not found, return false.
        return false;
};
TypeScript
/**
* Searches for a target value in a matrix.
 * This matrix has the following properties:
 * 1. Integers in each row are sorted from left to right.
 * 2. The first integer of each row is greater than the last integer of the previous row.
 * @param matrix A 2D array of numbers representing the matrix.
 * @param target The number to search for in the matrix.
 * @return A boolean indicating whether the target exists in the matrix.
function searchMatrix(matrix: number[][], target: number): boolean {
    // Get the number of rows (m) and columns (n) in the matrix
    let rowCount = matrix.length.
        columnCount = matrix[0].length;
    // Start our search from the bottom-left corner of the matrix
    let currentRow = rowCount - 1,
        currentColumn = 0;
    // Continue the search while we're within the bounds of the matrix
    while (currentRow >= 0 && currentColumn < columnCount) {</pre>
        // Retrieve the current element to compare with the target
        let currentElement = matrix[currentRow][currentColumn];
        // Check if the current element matches the target
        if (currentElement === target) return true;
        // If the current element is greater than the target,
        // move up to the previous row since all values in the current
```

row index -= 1 # If current element is smaller than target, move right to increase value else: col_index += 1

Time and Space Complexity

return True

Time Complexity

return False

The time complexity of the search algorithm is 0(m + n), where m is the number of rows and n is the number of columns in the matrix. This is because the algorithm starts from the bottom-left corner of the matrix and moves either up (i decreases) or right increases) at each step. At most, it will move m steps upwards and n steps to the right before it either finds the target or reaches the top-right corner, thus completing the search.

Space Complexity

The space complexity of the algorithm is 0(1). This is because the algorithm uses a fixed amount of extra space (variables i and j) regardless of the size of the input matrix. It doesn't require any additional data structures that grow with the input size.