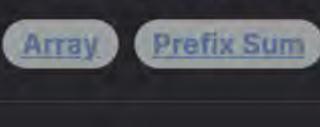


Problem Description



which is a numerical value associated with it. A garden is considered valid if:

In this problem, we are working with a garden represented by a linear arrangement of flowers, each flower having a beauty value,

It contains at least two flowers.

flowers that are left.

- The beauty value of the first flower is equal to the beauty value of the last flower in the garden.
- As the gardener, your job is to possibly remove any number of flowers from the garden to ensure that it becomes valid while maximizing the total beauty of the garden. The total beauty of the garden is defined as the sum of the beauty values of all the

To summarize, the objective is to maximize the sum of the beauty values of a valid garden by selectively removing flowers. The solution to this challenge will require an efficient algorithm to calculate the maximum possible beauty without having to try all possible combinations of flower removal, which would be inefficient.

Intuition To find the maximum beauty of a valid garden, we analyze the following key points:

1. As the valid garden must start and end with flowers having the same beauty value, and we aim to maximize beauty, we must

identify pairs of flowers with the same value that are as far from each other as possible, since all flowers between them can contribute to the total beauty.

2. Given point 1, removing any flowers with a negative beauty value from the middle of our garden will only increase the total

- beauty since they detract from it. With these points in mind, we can sketch an algorithm that: A. Keeps a running sum (s) of the beauty values (ignoring negative values as they are never beneficial to our sum), to quickly
- B. Utilizes a dictionary (d) to keep track of the last occurrence index for each beauty value we come across as we iterate through the flower array.

If we encounter a flower with a beauty value we've seen before, we have a potential garden that starts at the previous

of same-beauty flowers and calculating the maximum sum efficiently.

3. Finding Maximum Beauty Garden: As we iterate over the flowers array:

calculate the total beauty including any range of flowers.

occurrence index and ends at the current index. We calculate the potential beauty for this garden by adding the total beauty value twice (once for each flower at the ends) and subtracting the sum of values between them (as stored in s).

We update our maximum beauty (ans) if the current potential beauty is greater than what we have found so far.

The running sum (s) is updated at every step, adding the current flower's beauty value, but skipping negative values.

By iterating through the entire array just once, we are able to calculate the maximum possible garden beauty by considering all pairs

efficient data structures and patterns:

As we iterate over the flowers array:

- The given solution code implements this approach and correctly calculates the answer. Solution Approach

If we encounter a flower with a beauty value for the first time, we simply record its index in the dictionary.

The solution to this LeetCode problem involves finding subarrays with the same starting and ending beauty values and maximizing the sum of the beauty values of the elements in between. The algorithm can be broken down into the following steps, incorporating

beauty values from flowers[0] up to flowers[i-1], excluding negative values, as they reduce the total beauty. The prefix sum array allows for constant-time range sum queries, which is crucial for efficient computation.

2. Dictionary Tracking: A dictionary d is used to keep track of the last index where each beauty value appears. This is used to find

If we encounter a beauty value that has appeared before, it means there's a potential valid garden ending with the current

flower. The beauty of this potential garden is calculated as the sum of all the values between the matching pair, including

the value at the end points themselves (which are same due to the valid garden condition). We calculate this by subtracting

1. Prefix Sum Array: As an optimization for quick sum queries, a prefix sum array s is created. s [1] represents the sum of all

the most distant matching pair of the same beauty value, which potentially forms the start and end of a valid garden.

the prefix sum at the start index from the prefix sum at the end index and adding the value of the end points twice. If it's the first time we encounter a certain beauty value, we record its index in the dictionary d, marking it as the start point for potential gardens with that beauty value. 4. Maintaining Maximum Beauty Value: Throughout the iteration, we maintain a variable ans, which stores the maximum beauty

value found so far. Whenever we find a potential garden with a higher beauty value than our current maximum, we update ans.

• For each flower flowers[i], the current flower's beauty is added to the prefix sum only if it is non-negative. If flowers[i] has occurred before, compute the potential beauty by subtracting s[d[flowers[i]] + 1] from s[i] and adding flowers[i] * 2 (for the start and end flowers).

Update the dictionary d for the current beauty value to the current index so that we can use the most recent index for

O(1) look-up of indices, making the overall time complexity O(n), where n is the number of flowers. Example Walkthrough

Let's illustrate the solution approach with a small example. Suppose we have the following array of flowers with their respective

By following these steps, the provided Python code efficiently loops through the flower array once and finds the maximum possible

beauty of a valid garden. This approach leverages the usage of a prefix sum array for fast range sum calculations and a dictionary for

1 flowers = [1, -2, -1, 1, 3, 1]

beauty values:

5. Update Rules:

calculating future gardens.

1. Prefix Sum Array (s): We will construct this array on the fly as we iterate through the flowers array. Let's initialize the prefix sum array with 0.

• flowers [2] has a beauty of -1, again negative, so we continue. Prefix sum is still s[0] = 1.

We wish to identify a valid garden with the maximum total beauty. We will use the given solution approach to solve it.

 Iterating over the given flowers array: o For flowers [0] which has a beauty value of 1, d[1] does not exist yet, so we add it to d with a value of 0 and set the prefix

o flowers [1] with a beauty value of -2 is negative, so we do not add it to our prefix sum. Prefix sum remains s [0] = 1.

When we reach flowers [3] with the beauty value of 1, d[1] exists and suggests a potential valid garden from index 0 to 3.

garden is s[3] - s[d[1] + 1] + flowers[3] * 2 = 1 - 1 + 2 = 2. This is our first potential garden, so we set ans to 2.

Next, flowers [4] has a beauty value of 3. We add its index to d as d[3] = 4 and update our prefix sum to include this

4. Maintaining Maximum Beauty Value (ans): Throughout the iteration, we have updated ans whenever we found a potential

We compute the beauty by checking the prefix sum at the start index of and end index 3. The total beauty of this potential

Lastly, flowers [5] has a beauty value of 1. Again, d[1] exists, so we check this potential garden which spans from index 0 to

5. The total beauty is s[5] - s[d[1] + 1] + flowers[5] * 2 = 4 - 1 + 2 = 5. This potential garden has a higher beauty than our current ans, so we update ans to 5.

Update the dictionary d with the most recent index for the current beauty value.

Enumerate through the flowers list with index and value

Update the 'last_seen' index for the current flower

Dictionary 'last_seen' keeps track of the last seen index for each flower value

// Initialize a prefix sum array that includes an extra initial element set to 0

// Create a map to keep track of the first index of each flower value encountered

// Calculate the beauty using the current and first occurrence of currentValue

Initialize 'ans' to negative infinity to handle the case when no valid scenario is found

Update the maximum beauty. It is the maximum of the current maximum beauty and

flower's positive beauty value, making s[4] = 4.

2. Dictionary Tracking (d): We'll start with an empty dictionary.

garden with a higher beauty value. First, ans was 2, but after considering the full array, we updated ans to 5.

a valid garden with [1, -2, -1, 1, 3, 1].

last_seen = {}

return max_beauty

max_beauty = float('-inf')

if value in last_seen:

last_seen[value] = index

public int maximumBeauty(int[] flowers) {

int maxBeauty = Integer.MIN_VALUE;

// Iterate through the flowers array

int currentValue = flowers[i];

unordered_map<int, int> lastAppearance;

for (int i = 0; i < numFlowers; ++i) {

} else {

int maxBeauty = INT_MIN; // The maximum beauty to be calculated

int beautyValue = flowers[i]; // Current flower's beauty value

// Keep track of the first appearance of this beauty value

cumulativeSum[i + 1] = cumulativeSum[i] + max(beautyValue, 0);

// Function to calculate maximum beauty of a garden based on flowers' beauty values

// Update the cumulative sum with the current beauty value if it's positive

// and this appearance, plus double the beautyValue

// Update the maxBeauty with the sum between first appearance of this value

maxBeauty = max(maxBeauty, cumulativeSum[i] - cumulativeSum[lastAppearance[beautyValue] + 1] + beautyValue * 2);

// Iterate over all flowers to find the maximum beauty

if (lastAppearance.count(beautyValue)) {

lastAppearance[beautyValue] = i;

// Check if this beauty value has appeared before

return maxBeauty; // Return the highest calculated beauty

for (int i = 0; i < flowers.length; ++i) {

int[] prefixSums = new int[flowers.length + 1];

Map<Integer, Integer> firstIndexMap = new HashMap<>();

if (firstIndexMap.containsKey(currentValue)) {

// Initialize the answer to the minimum possible integer value

// Check if the current flower value has been seen before

for index, value in enumerate(flowers):

If we have seen the value before

Python Solution

3. Finding Maximum Beauty Garden:

sum s [0] to 1.

5. Update Rules:

When a flower's beauty value has been encountered before, calculate the potential beauty as described above.

• For each flower flowers[i], if the flower's beauty value is positive, it is added to the prefix sum. If not, it is ignored.

class Solution: def maximumBeauty(self, flowers: List[int]) -> int: # The 'running_sum' list holds the cumulative sum of the flowers' beauty values # It has an extra initial element 0 for easier calculations of sums in slices $running_sum = [0] * (len(flowers) + 1)$

the sum of beauty values since the flower was last seen (not inclusive) plus the beauty value doubled

max_beauty = max(max_beauty, running_sum[index] - running_sum[last_seen[value] + 1] + value * 2)

By the end of this process, we determine that taking the entire array from index 0 to 5 gives us the maximum beauty of 5, resulting in

23 # Update the cumulative sum 24 25 running_sum[index + 1] = running_sum[index] + max(value, 0) 26 27 # Return the calculated maximum beauty

Java Solution

class Solution {

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                   // and update maxBeauty accordingly
                   int firstIndex = firstIndexMap.get(currentValue);
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18
                   maxBeauty = Math.max(maxBeauty, prefixSums[i] - prefixSums[firstIndex + 1] + currentValue * 2);
19
               } else {
20
                   // If the value has not been seen, map the current value to its first index
21
                   firstIndexMap.put(currentValue, i);
22
23
               // Calculate the running total of positive values to form the prefix sums array
24
               prefixSums[i + 1] = prefixSums[i] + Math.max(currentValue, 0);
25
26
27
           // Return the maximum beauty encountered
28
           return maxBeauty;
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30 }
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C++ Solution
 1 #include <vector>
 2 #include <unordered_map>
  #include <algorithm>
   #include <climits>
   class Solution {
   public:
       // Calculates the maximum beauty of a garden based on the flowers' 'beauty' values
       int maximumBeauty(vector<int>& flowers) {
           int numFlowers = flowers.size(); // Number of flowers in the garden
10
           // Create a sum vector, where s[i] will hold the accumulated sum of all
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           // flowers' beauty that can contribute positively up to index i-1
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           vector<int> cumulativeSum(numFlowers + 1, 0);
           // Dictionary to store the last index of a particular 'beauty' value flower
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```

// Structure representing a Flower, holds the beauty value 2 interface Flower { beauty: number; 4

Typescript Solution

```
function maximumBeauty(flowers: Flower[]): number {
       const numFlowers: number = flowers.length; // Number of flowers in the garden
       // Array to track cumulative sum of positive beauty values up to each flower
       const cumulativeSum: number[] = new Array(numFlowers + 1).fill(0);
10
       // Map to track the last index at which a particular beauty value appeared
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       const lastAppearance: Map<number, number> = new Map<number, number>();
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       let maxBeauty: number = Number.MIN_SAFE_INTEGER; // Variable to track the maximum beauty
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       // Loop through all flowers to find the maximum possible beauty
       for (let i = 0; i < numFlowers; ++i) {</pre>
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17
           const beautyValue = flowers[i].beauty; // Current flower's beauty value
18
           if (lastAppearance.has(beautyValue)) {
19
               // Update maxBeauty using the sum of beauty values between two appearances, plus double the beautyValue
20
               maxBeauty = Math.max(
                   maxBeauty,
                   cumulativeSum[i] - cumulativeSum[lastAppearance.get(beautyValue)! + 1] + beautyValue * 2
               );
           } else {
               // Record the first appearance of this beauty value
               lastAppearance.set(beautyValue, i);
           // Update the cumulative sum, ignoring negative beauty values
           cumulativeSum[i + 1] = cumulativeSum[i] + Math.max(beautyValue, 0);
       return maxBeauty; // Return the calculated maximum beauty
34
35 }
36
Time and Space Complexity
The given Python code snippet defines a Solution class with a method maximumBeauty that calculates a specific value related to the
beauty of a sequence of flowers represented by an integer array. The method employs a dynamic programming approach and uses
additional storage to keep track of sum results and indices.
```

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operations performed within this loop.

The time complexity of the method maximumBeauty can be analyzed based on the single loop through the flowers array and the

Therefore, the dominating factor of time complexity is the loop itself, which gives us a total time complexity of O(n).

There is a loop that iterates through each element of the input list flowers, which gives us an O(n) where n is the length of flowers.

Space Complexity:

Time Complexity:

 Within this loop, operations such as checking if a value is in a dictionary, updating the dictionary, computing a maximum, and updating the prefix sum array are all 0(1) operations.

- The space complexity of the method maximumBeauty is determined by the additional space used by the data structures s and d. • The prefix sum array s is of length len(flowers) + 1, which introduces an O(n) space complexity where n is the length of
- flowers. • The dictionary d stores indices of distinct elements encountered in flowers. In the worst case, all elements of flowers are

distinct, resulting in an O(n) space complexity, where n is the length of flowers.

The final space complexity is the sum of the complexities of the prefix sum array and the dictionary, both of which are O(n). Thus, the overall space complexity of the method maximumBeauty is O(n) as well.