875. Koko Eating Bananas

Medium Array Binary Search

Problem Description

In the given LeetCode problem, Koko loves bananas and has n piles of them, with the i-th pile containing $piles[i]$ bananas. Koko has h hours to eat all the bananas before the guards return, and she can set a constant eating speed of k bananas per hour. At each hour, she eats k bananas from a pile; if the pile has fewer than k bananas, she'll finish that pile and then stop eating for that hour. The goal is to determine the minimum eating speed k that allows Koko to consume all the bananas within the h hours available.

The problem is essentially about finding the lowest possible rate of eating bananas per hour, which allows Koko to eat all bananas in the given time without running out of time. The speed k must be an integer, and the challenge is to find the smallest such k that still meets the time constraint.

Intuition

The solution is based on a binary search approach. Since we're looking for the minimum integer value of k that enables Koko to finish all bananas within h hours, and k can range from 1 (eating very slowly) to the maximum number of bananas in any pile in the worst-case scenario (eating very fast), we can use binary search to narrow down the possible values of k.

We start with the lower bound `left` of 1 (the slowest possible eating speed) and an upper bound `right` which is set to a high enough value (like 10^9) that it's guaranteed to be higher than the maximum necessary speed.

At each step of the binary search, we calculate the midpoint `mid` between `left` and `right`. We then calculate the total hours s it would take for Koko to eat all the bananas at this speed. If s is less than or equal to h, this means `mid` is a viable eating speed and could possibly be the answer, so we move the right bound to `mid`, potentially reducing the range. If s is greater than h, then eating at speed `mid` is too slow and we need to increase the eating speed, so we move the left bound up to `mid + 1`.

The binary search continues until `left` and `right` converge to the minimum possible value of k that allows Koko to eat all bananas in h hours.

Solution Approach

The reference solution approach suggests employing a binary search algorithm to efficiently find the minimum eating speed k. This approach is chosen due to the nature of the problem, which quite clearly forms a sorted space where the speed can be increased or decreased based on whether Koko can finish the bananas within the given time h or not.

Here is a detailed walk-through of the algorithm:

1. Initialize two pointers: one for the lower bound `left` set to 1 (since Koko has to eat at least one banana per hour), and another for the upper bound `right` set to a large number, such as 10^9, to ensure that it is larger than any real-world scenario would require.
2. While `left` is less than `right`, we continue the binary search:
   - We find the midpoint `mid` by averaging the `left` and `right` pointers (`(left + right) >> 1`). Here, the `>> 1` operation is a bitwise shift that effectively divides the sum by two.
   - We then compute the total number of hours s it would take to eat all the piles at the eating speed `mid`. This is done by iterating over each pile in `piles` and calculating the hours needed for each pile using `(x + mid - 1) // mid`, which is a way to perform ceiling division without using floats to ensure we get an integer result. This formula accounts for the fact that if there are less than `mid` bananas in a pile, Koko will spend an entire hour eating it (represented by the `x + mid - 1` part).
3. After calculating s, we make a decision based on whether this proposed eating speed `mid` is fast enough:
   - If s is less than or equal to h, we know that `mid` is at least as fast as the eating speed needs to be, so we adjust the upper bound `right` to `mid`. This narrows the search and potentially lowers the eating speed.
   - If s is greater than h, the proposed eating speed `mid` is too slow, and we need to look for a faster eating speed; thus, we move the lower bound `left` up to `mid + 1`.
4. The binary search ends when `left` equals `right`, at which point `left` represents the minimum integer eating speed k that allows Koko to eat all bananas within h hours.

The binary search efficiently zeros in on the optimal value without having to try every possible eating speed, which significantly reduces the number of calculations and, thus, the running time of the algorithm.

Example Walkthrough

Let's consider a small example to illustrate the solution approach described above. Assume Koko has 4 piles of bananas where `piles = [3, 6, 7, 11]`, and she has $h = 8$ hours to eat all of them. We need to determine the minimum integer value of k such that Koko can finish the bananas within 8 hours.

1. **Initialize Lower and Upper Bounds:**
   - We set `left = 1` since Koko needs to eat at least one banana per hour.
   - We set `right = max(piles) + 1` since the minimum speed k cannot be more than the largest pile (Koko could eat any pile in an hour at this speed).
2. **Binary Search:**
   - While `left < right`, we continue to search:
     - Initially, `left = 1`, `right = 11`.
     - Midpoint `mid = (left + right) >> 1 = (1 + 11) / 2 = 6`.
3. **Calculate Total Hours s at Speed `mid`:**
   - For `mid = 6`, we calculate the total hours to eat each pile:
     - Pile 1: `(3 + 6 - 1) // 6 = 1` hour.
     - Pile 2: `(6 + 6 - 1) // 6 = 1` hour.
     - Pile 3: `(7 + 6 - 1) // 6 = 2` hours.
     - Pile 4: `(11 + 6 - 1) // 6 = 2` hours.
   - Total hours $s = 1 + 1 + 2 + 2 = 6$ hours.
4. **Adjust Pointers:**
   - Since $s <= h$, we can try a smaller k. So we adjust `right = mid`, now `right = 6`.
   - The new `left` and `right` bounds are `left = 1` and `right = 6`.
5. **Repeat Binary Search:**
   - With `left = 1` and `right = 6`, `mid = (left + right) >> 1 = (1 + 6) / 2 = 3.5`, which rounds down to `3`.
   - Repeat the total hours s calculation for `mid = 3`.
6. **Continue Until `left` equals `right`:**
   - The binary search is repeated, updating `left` and `right` based on the calculated hours s until they equal.
   - Each time, if $s <= h$, decrease `right`; if $s > h$, increase `left`.
   - Eventually, `left` will equal `right`, giving the minimum speed k.

In this example, when `mid = 6`, the total hours s will be equal to 8 hours, which is exactly the time Koko has. Thus, the minimum speed k is bananas per hour. At this rate, Koko will finish exactly on time:

- Pile 1 in 1 hour,
- Pile 2 in 2 hours,
- Pile 3 in 2 hours, and
- Pile 4 in 3 hours.

For simplicity, not all steps are shown here, but following this approach, the algorithm investigates fewer possibilities than checking each speed sequentially, thus finding the correct k more efficiently.

Solution Implementation

Python

```python
from typing import List

class Solution:
    def minEatingSpeed(self, piles: List[int], hours: int) -> int:
        # Initialize the search space for Koko's possible eating speed
        # left represents the minimum possible eating speed
        # right represents the maximum possible eating speed which we initialize to 1e9
        left, right = 1, int(1e9)

        # Use binary search to find the minimum eating speed
        while left < right:
            # Calculate the middle point of the current search space
            # Equivalent to (left + right) // 2 but avoids possible overflow in other languages
            mid = (left + right) >> 1

            # Calculate total hours needed to eat all piles at this eating speed
            total_hours = sum(pile + mid - 1) // mid for pile in piles)

            # If Koko can eat all bananas within the given hours at this speed,
            # update the upper bound of the search space
            if total_hours <= hours:
                right = mid
            else:
                # Otherwise, this speed is too slow, update the lower bound
                left = mid + 1

        # The left pointer will be at the minimum eating speed at which Koko can
        # eat all the bananas within the given hours
        return left
```

Java

```java
class Solution {

    /**
     * Finds the minimum eating speed to eat all bananas in 'h' hours.
     *
     * @param piles Array of banana piles.
     * @param h Total hours within which all bananas must be eaten.
     * @return The minimum integer eating speed.
     */
    public int minEatingSpeed(int[] piles, int h) {
        // Initialize the lower bound of the eating speed, cannot be less than 1.
        int minSpeed = 1;
        // Initialize the upper bound of the eating speed to a high number, (int) 1e9 is used as an approximation.
        int maxSpeed = (int) 1e9;

        // Binary search to find the minimum eating speed.
        while (minSpeed < maxSpeed) {
            // Find the mid point which is the candidate for our potential eating speed.
            int midSpeed = minSpeed + (maxSpeed - minSpeed) / 2;

            // Initialize the total hours needed with the chosen speed.
            int totalHours = 0;

            // Calculate the total hours needed to eat the piles at midSpeed.
            for (int bananas : piles) {
                // The time to eat a pile is the pile size divided by eating speed, rounded up.
                totalHours += (bananas + midSpeed - 1) / midSpeed;
            }

            // If the total hours with midSpeed is less or equal to h, we might be able to do better,
            // so we brina down the maximum speed to midSpeed.
            if (totalHours <= h) {
                maxSpeed = midSpeed;
            } else {
                // Otherwise, if we need more than 'h' hours, the speed is too slow.
                // We need to increase our eating speed, so we update minSpeed to midSpeed + 1.
                minSpeed = midSpeed + 1;
            }
        }

        // Loop finishes when minSpeed == maxSpeed, which is the minimum speed to eat all bananas in 'h' hours.
        return minSpeed;
    }
}
```

C++

```cpp
#include <vector> // Include the vector library

class Solution {
public:
    // The function minEatingSpeed calculates the minimum speed at which
    // all bananas in the piles can be eaten within 'h' hours.
    // Parameters:
    // piles: A vector of integers representing the number of bananas in each pile.
    // h: The total number of hours within which all bananas must be eaten.
    // Returns:
    // The minimum integer representing the minimum eating speed (bananas per hour).
    int minEatingSpeed(vector<int>& piles, int h) {
        int left = 1; // Minimum possible eating speed (cannot be less than 1)
        int right = 1e9; // A large upper bound for the maximum eating speed.

        // Perform a binary search between the range [left, right)
        while (left < right) {
            int mid = left + (right - left) / 2; // Prevents overflow
            int hoursSpent = 0; // Initialize the hours spent to 0

            // Calculate the total number of hours it would take at the current speed 'mid'
            for (int pile : piles) {
                // The number of hours spent on each pile is the ceil of pile/mid
                // (pile + mid - 1) / mid is an efficient way to calculate ceil(pile/mid)
                hoursSpent += (pile + mid - 1) / mid;
            }

            // If the current speed 'mid' requires less than or equal to 'h' hours,
            // it is a potential solution and we try to find a smaller one.
            if (hoursSpent <= h) {
                right = mid;
            } else {
                // If the current speed 'mid' requires more than 'h' hours,
                // it is not a valid solution and we must try a larger speed.
                left = mid + 1;
            }
        }
        // 'left' is now the minimum speed at which Koko can eat all the bananas within 'h' hours.
        return left;
    }
};
```

TypeScript

```typescript
/**
 * Determines the minimum eating speed required to eat all banana piles within `h` hours.
 * @param piles Array of integers representing the number of bananas in each pile.
 * @param h Number of hours available to eat all the piles.
 * @return The minimum integer speed at which all bananas can be eaten within `h` hours.
 */
function minEatingSpeed(piles: number[], h: number): number {
    let minSpeed = 1; // The minimum possible eating speed.
    let maxSpeed = Math.max(...piles); // The maximum possible eating speed, which cannot exceed the largest pile.

    // We use binary search to find the minimum speed.
    while (minSpeed < maxSpeed) {
        const midSpeed = Math.floor((minSpeed + maxSpeed) / 2); // Calculate the middle speed in the current range.
        let hoursSpent = 0; // Initialize hours spent to 0 for each iteration.

        // Calculate total hours spent eating with the current speed.
        for (const pile of piles) {
            hoursSpent += Math.ceil(pile / midSpeed);
        }

        // If the hours spent is within the allowed hours `h`, we can try to see if there is a smaller speed.
        if (hoursSpent <= h) {
            maxSpeed = midSpeed;
        } else {
            // If hours spent is more than `h`, we need to increase the speed.
            minSpeed = midSpeed + 1;
        }
    }
    // Return the minimum speed found that enables finishing within `h` hours.
    return minSpeed;
}
```

```python
from typing import List

class Solution:
    def minEatingSpeed(self, piles: List[int], hours: int) -> int:
        # Initialize the search space for Koko's possible eating speed
        # left represents the minimum possible eating speed
        # right represents the maximum possible eating speed which we initialize to 1e9
        left, right = 1, int(1e9)

        # Use binary search to find the minimum eating speed
        while left < right:
            # Calculate the middle point of the current search space
            # Equivalent to (left + right) // 2 but avoids possible overflow in other languages
            mid = (left + right) >> 1

            # Calculate total hours needed to eat all piles at this eating speed
            total_hours = sum(pile + mid - 1) // mid for pile in piles)

            # If Koko can eat all bananas within the given hours at this speed,
            # update the upper bound of the search space
            if total_hours <= hours:
                right = mid
            else:
                # Otherwise, this speed is too slow, update the lower bound
                left = mid + 1

        # The left pointer will be at the minimum eating speed at which Koko can
        # eat all the bananas within the given hours
        return left
```

Time and Space Complexity

Time Complexity

The time complexity of the code is determined by the binary search and the computation required to sum up the hours needed to eat all the piles at a particular speed. The binary search runs in $O(\log(\max(piles)))$ because it searches between 1 and `max(piles)` upper-bounded by 10^9. During each step of the search, we calculate the sum of hours which takes $O(n)$ where n is the number of piles. Therefore, the overall time complexity of the algorithm is $O(n*\log(\max(piles)))$.

Space Complexity

The space complexity of the code is $O(1)$ as only a constant amount of extra space is used besides the input piles. Variables like `left`, `right`, `mid`, and `s` occupy constant space and no additional data structures dependent on input size are introduced.