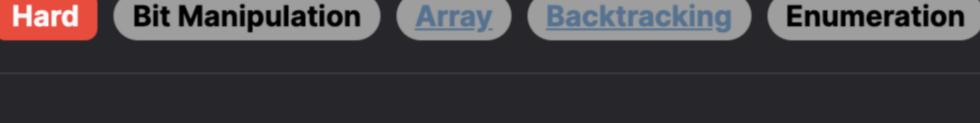
1601. Maximum Number of Achievable Transfer Requests



We are given n buildings, and an array of employee transfer requests between these buildings. Each request is represented by a pair [from, to], meaning an employee wants to transfer from one building to another. A request array is deemed achievable if the transfers can happen without altering the total number of employees in each building; that is to say, the incoming employees must balance the outgoing ones for every building. The objective is to return the maximum number of such achievable transfer requests.

Leetcode Link

building ends up with the same number of employees it started with.

Intuition

To put it simply, we have to find the largest subset of the given requests that can be satisfied simultaneously, ensuring that every

Problem Description

The solution approach is based on the idea of checking every possible combination of requests, from no requests being satisfied to all of them being considered. To do this efficiently, a bitmask representation is utilized.

whether to include or exclude a particular request. The total number of bitmasks to check will be 2^len(requests), because that's how many subsets are possible.

A bitmask approach involves creating a mask for each possible subset of requests. Each bit in the mask corresponds to a decision

The intuition behind using a bitmask is that it allows us to efficiently iterate over all subsets of requests, including the empty set and the set containing all requests. By incrementally checking each bitmask, we determine whether that particular combination of requests leads to a balanced transfer where each building's employee count remains unchanged.

Checking a mask involves updating a list of net change in employees for each building (cnt). If a request is included in the mask (indicated by the corresponding bit being 1), we decrement the employees count from the from building and increment it in the to building. At the end of this process, we check if all buildings' counts are zero. If they are, it means that particular combination is achievable.

achievable.

The final step keeps track of the maximum number of requests that form a valid set (ans). This is done by comparing the number of requests in the current mask (cnt) with the highest number found so far. If the current mask is both a larger set and a valid transfer

Solution Approach

The implementation of the solution employs a brute force approach with a bit manipulation technique to iterate through all possible subsets of the transfer requests.

1. Define a helper function check(mask: int) -> bool:

This brute force method ensures that all possible request combinations are checked, and the largest valid subset is found.

It creates an array cnt of size n, initialized with zeros. The array represents the net change in the number of employees in each building.

set, it updates the maximum found.

Here's the step-by-step breakdown of the code:

that the subset is achievable.

number of set bits (or 1s) in the bitmask.

Overall, the key data structures used in this approach are:

The function iterates over all requests and for each request, checks if the corresponding bit in the mask is set to 1. If it is, it means the request is included in the current subset and the function updates the cnt array by decrementing the count for

• The range of the loop is 1 << len(requests), which gives us all possible combinations of including or excluding each

After iterating through all requests, it checks if all buildings have a net change of zero, and returns True if they do, indicating

2. Initialize a variable ans with 0 to keep track of the maximum number of achievable requests found.

3. Iterate through all possible masks/subsets using a for-loop:

the from building and incrementing it for the to building.

request.

• The variable mask represents the current subset of requests being considered.

can be accommodated without changing the number of employees in each building.

An array cnt for tracking the net change in employees for each building within a subset.

the number of buildings, since for each of the 2ⁿ subsets, we perform n operations to validate it.

An integer mask to represent a subset of requests and facilitate bit manipulation.

Here's a step-by-step walkthrough using a bitmask approach for the given requests:

This function takes a bitmask as an argument, representing a subset of requests.

subset is achievable, update ans with the count of the current subset.

6. After considering all possible subsets, return ans as the final result. This value represents the maximum number of requests that

5. If the current mask has more requests than ans (the previous maximum), and the check(mask) function confirms that the current

4. Inside the loop, calculate the number of requests included in the current subset using mask.bit_count(), which returns the

- This algorithm makes use of combinatorial logic (to generate all possible subsets of requests) and bitwise operations (to manage and evaluate these subsets efficiently). The time complexity of this approach is $O(2^m * n)$ where m is the number of requests and n is
- Let's take a small example to illustrate the solution approach.

 Suppose we have n = 3 buildings and a list of 4 employee transfer requests, as follows:

With 4 requests, there are 2⁴ = 16 possible combinations of these requests, from no requests (bitmask 0000) to all requests

o Bitmask 0001: The subset includes just the last request [2, 0]. This is achievable as we can transfer one employee from

o Bitmask 0010: The subset includes the request [0, 2]. This is also achievable in isolation, but ans remains at 1 because we

these transfers would be 0, so the subset is achievable. Since this subset has 3 transfers, ans is updated to 3.

We start by setting ans to 0, as we have not processed any requests yet.

(bitmask 1111).

building 2 to 0.

final answer.

from typing import List

class Solution:

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C++ Solution

public:

1 #include <vector>

class Solution {

2 #include <cstring> // for memset

int requestCount = requests.size();

for (int value : balance) {

return false;

// Iterate over all combinations of requests.

auto checkBalance = [&](int mask) -> bool {

25 # Example usage:

26 # sol = Solution()

Java Solution

class Solution {

1 requests = [[0, 1], [1, 2], [0, 2], [2, 0]]

2. Iterate Through All Possible Subsets:

1. Initialize Maximum Achievable Requests (ans):

For each bitmask, we perform the following steps:

already found a subset of 1 request.

4. Check Each Subset For Balance (Using check Function):

subset of requests is balanced and thus achievable.

maintaining the balance of employees in all buildings.

Example Walkthrough

3. Evaluate Each Subset (Bitmask):

Bitmask 0000: No requests are included, thus ans remains 0.

...and so on for each combination...
 Bitmask 1011: This subset includes requests [0, 1], [1, 2], and [0, 2]. Upon checking, the count for each building after

def maximumRequests(self, n: int, requests: List[List[int]]) -> int:

Internal function to check if the current combination of requests

for idx, (from_building, to_building) in enumerate(requests):

maximum_val = count # Update the maximum value

satisfies the balance of incoming and outgoing requests for each building.

balance = [0] * n # Initialize a list to keep track of balance for each building

if combination >> idx & 1: # If the current request is included in the combination

balance[to_building] += 1 # Increment the balance for the 'to' building

return all(value == 0 for value in balance) # Return True if all balances are zero

return maximum_val # Return the maximum number of requests that can be satisfied

28 # where 'n' is the number of buildings and 'requests' is the list of request pairs [from, to].

balance[from_building] -= 1 # Decrement the balance for the 'from' building

count = bin(combination).count('1') # Count how many requests are included in this combination

if maximum_val < count and is_valid(combination): # If this combination has more requests than the max found so far, and

5. Find Maximum Number of Achievable Requests:

As we evaluate all possible subsets, we use the ans variable to keep track of the greatest number of requests in a balanced

subset encountered so far. In our example, upon checking all subsets, the maximum achievable number is 3, which would be the

When we evaluate each set, the check function will update an array cnt that tracks the net change in number of employees at

each building, considering which requests are included in the current subset. If all entries in cnt are 0, it means that the current

Python Solution

For this example, the final ans represents that there is a subset of 3 transfer requests which can be satisfied simultaneously,

private int numRequests; // Total number of requests

private int numBuildings; // Total number of buildings

private int[][] requestsArray; // Array containing requests

return true; // If all buildings are balanced, return true

int maximumRequests(int n, std::vector<std::vector<int>>& requests) {

27 # result = sol.maximumRequests(n, requests)

def is_valid(combination: int) -> bool:

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public int maximumRequests(int numBuildings, int[][] requestsArray) {
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            this.numRequests = requestsArray.length;
            this.numBuildings = numBuildings;
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            this.requestsArray = requestsArray;
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            int maxRequests = 0; // Maximum number of requests that can be fulfilled without imbalance
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            // Iterate over all possible combinations of requests
            for (int mask = 0; mask < (1 << numRequests); ++mask) {</pre>
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                int requestCount = Integer.bitCount(mask); // Count of requests in the current combination
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                // If the current combination has more requests and is balanced, update maxRequests
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                if (maxRequests < requestCount && isBalanced(mask)) {</pre>
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                    maxRequests = requestCount;
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            return maxRequests; // Return the maximum number of requests that can be fulfilled
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        // Helper method to check if a combination of requests is balanced
        private boolean isBalanced(int mask) {
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            int[] balance = new int[numBuildings]; // Array to keep track of the balance of each building
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            // Apply requests in the current combination to the balance array
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            for (int i = 0; i < numRequests; ++i) {</pre>
                if ((mask >> i \& 1) == 1) { // If the i-th request is in the combination}
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                    int from = requestsArray[i][0], to = requestsArray[i][1];
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                    --balance[from]; // Decrement the count of the 'from' building
                    ++balance[to]; // Increment the count of the 'to' building
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            // Check if all buildings are balanced, i.e., have a zero balance
            for (int v : balance) {
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                if (v != 0) {
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                    return false; // If any building is unbalanced, return false
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// Function to find the maximum number of requests that can be fulfilled without leaving any building imbalanced.

if $(mask \gg i \& 1) \{ // Check if the i-th request is chosen in the current combination <math>(mask)$.

int from = requests[i][0], to = requests[i][1]; // Get the 'from' and 'to' buildings for the request.

int maxFulfilledRequests = 0; // Variable to store the maximum number of requests fulfilled.

// Lambda function to check if the selected requests sequence balances the building.

std::memset(balance, 0, sizeof(balance)); // Initialize all balances to zero.

--balance[from]; // Decrement balance for the 'from' building.

++balance[to]; // Increment balance for the 'to' building.

// Check if all buildings are balanced, i.e., have a net balance of zero.

if (value) { // If any building is not balanced, return false.

return true; // All buildings are balanced, return true.

int balance[n]; // Array to hold the net balance of each building.

for (int i = 0; i < requestCount; ++i) { // Traverse each request.</pre>

for (int mask = 0; mask < (1 << requestCount); ++mask) { int currentCount = __builtin_popcount(mask); // Count the number of bits set in mask, which equals the number of reques // If the current combination has more requests than maxFulfilledRequests and is balanced. if (maxFulfilledRequests < currentCount && checkBalance(mask)) { maxFulfilledRequests = currentCount; // Update the maximum number of requests fulfilled.

};

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if (maxFulfilledRequests < currentCount && checkBalance(mask)) {</pre>
                     maxFulfilledRequests = currentCount; // Update the maximum number of requests fulfilled.
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             // Return the final answer, which is the maximum number of requests that can be fulfilled.
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             return maxFulfilledRequests;
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    };
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Typescript Solution
   // Function to calculate the maximum number of requests that can be fulfilled without any building ending up in a deficit.
   function maximumRequests(n: number, requests: number[][]): number {
       const numberOfRequests = requests.length;
       let maximumFulfilledRequests = 0;
       // Function to check if the given combination of requests keeps all buildings balanced.
       const checkBalancedRequests = (mask: number): boolean => {
           const balanceCounter = new Array(n).fill(0);
            for (let i = 0; i < numberOfRequests; ++i) {</pre>
               if ((mask >> i) & 1) {
                    const [fromBuilding, toBuilding] = requests[i];
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                    // Decrement for the 'from' building, and increment for the 'to' building.
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                    --balanceCounter[fromBuilding];
                   ++balanceCounter[toBuilding];
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           // Check if all the buildings are balanced (end up with 0 transfers).
           return balanceCounter.every(value => value === 0);
       };
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       // Iterate over all possible combinations of requests.
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       for (let mask = 0; mask < (1 << numberOfRequests); ++mask) {</pre>
            const numberOfSetBits = bitCount(mask); // Count the number of bits set in mask.
           if (maximumFulfilledRequests < numberOfSetBits && checkBalancedRequests(mask)) {</pre>
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               maximumFulfilledRequests = numberOfSetBits; // Update max if a better combination is found.
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       return maximumFulfilledRequests; // Return the maximum number of requests that can be fulfilled.
29 }
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   // Function to count the number of bits set to 1 in the binary representation of a number.
   function bitCount(i: number): number {
       i = i - ((i >>> 1) \& 0x55555555);
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```

The time complexity of the code is primarily determined by two nested operations: 1. The outer loop, which iterates over all possible subsets of requests. There are len(requests) requests, and for each request,

factors influencing space complexity here are:

i = (i & 0x33333333) + ((i >>> 2) & 0x333333333);

return i & 0x3f; // Return the number of bits set.

i = (i + (i >>> 4)) & 0x0f0f0f0f;

Time and Space Complexity

i = i + (i >>> 8);

i = i + (i >>> 16);

2. The inner function check(mask), which is called for each subset to verify whether choosing a particular subset of requests satisfies the balance criterion (every building ends up with the same number of people). This function iterates through all requests and then all buildings to ensure balance, contributing a complexity of 0(m + n), where n is the number of building

Time Complexity

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requests and then all buildings to ensure balance, contributing a complexity of 0(m + n), where n is the number of buildings. The combined effect of these operations leads to a total time complexity of $0(2^m * (m + n))$.

resulting in a time complexity of $O(2^m)$ for this loop, where m is the length of requests.

Space Complexity

The space complexity of the provided code can be analyzed by looking at the additional memory used by the algorithm. The key

there are two possibilities (either the request is fulfilled or it is not). Therefore, there are 2^(len(requests)) possible subsets,

2. The bit mask, which does not add significant space complexity, as it is just an integer value storing the current subset being checked.

1. The counter array cnt for building balances, which uses O(n) space, where n is the number of buildings.

Thus, the overall space complexity of the algorithm is 0(n), as it's primarily dependent on the number of buildings to store the balance counter for each building.