# 523. Continuous Subarray Sum

**Math Prefix Sum** Medium <u>Array</u> Hash Table

### **Problem Description**

The problem provides an integer array nums and an integer k. The task is to determine whether there exists at least one subarray within nums that is both of length two or more and whose sum of elements is a multiple of k. A subarray is defined as a contiguous sequence of elements within the parent array. It's important to note that any integer is considered a multiple of k if it can be expressed as n \* k for some integer n. Zero is also considered a multiple of k by this definition (since 0 = k \* 0).

## Intuition

To solve this problem, we can utilize the properties of modular arithmetic. The key observation here is that if the sum of a subarray nums[i:j] (where i < j) is a multiple of k, then the cumulative sums sum[0:i-1] and sum[0:j] will have the same remainder when divided by k. This stems from the fact that if (sum[0:j] - sum[0:i-1]) is a multiple of k, then (sum[0:j] % k) =

The algorithm proceeds as follows:

(sum[0:i-1] % k).

- 1. Iterate through the array, computing the cumulative sum s as we go.
- 2. At each step, calculate the remainder of the sum s divided by k (denoted as r = s % k). 3. Maintain a dictionary (mp) that maps each remainder to the earliest index where that remainder was seen.

beginning of the array (i.e., the subarray starts at index 0).

subarray" has been found. In this case, the function returns False.

- 4. For each calculated remainder r, check if we have seen this remainder before. If we have and the distance between the current index and the index stored in the dictionary mp[r] is at least two, this means we've found a good subarray, and we return True.
- 5. If the remainder has not been seen before, store the current index in the dictionary against the remainder r. 6. If no good subarray is found throughout the iteration, return False after the loop completes.
- By using this approach, we are effectively tracking the cumulative sums in such a way that we can efficiently check for subarrays whose sum is a multiple of k. The storage of the earliest index where each remainder occurs is crucial for determining the length

of the subarray without having to store all possible subarrays. **Solution Approach** 

The solution approach leverages the concept of prefix sums and modular arithmetic to identify a subarray sum that is a multiple

## of k. Here is the step-by-step explanation of how the solution is implemented:

Initialize a Variable to Store Cumulative Sum (s): We define a variable s that will hold the cumulative sum of the elements as we iterate through the array.

Create a Dictionary (mp) to Store Remainders and Their Earliest Index: A Python dictionary mp is used to map each

- encountered remainder when dividing the cumulative sum by k to the lowest index where this remainder occurs. The dictionary is initialized with {0: -1} which handles the edge case wherein the cumulative sum itself is a multiple of k from the
- Iterate Through the Array: Using a for-loop, we iterate through the array while keeping track of the current index i and the element value v. Update Cumulative Sum: With each iteration, we update the cumulative sum s by adding the current element value v to it: s
- += v. Calculate Remainder: We calculate the remainder r of the current cumulative sum s when divided by k: r = s % k.

Check for a Previously Encountered Remainder: If the remainder r has been seen before, and the index difference i - mp[r]

is greater than or equal to 2, we have found a "good subarray." This is because the equal remainders signify that the sum of

Store the Remainder and Index If Not Already Present: If the remainder r has not been previously encountered, we store this remainder with its corresponding index i into the dictionary: mp[r] = i.

Return False If No Good Subarray Is Found: If the for-loop completes without returning True, it implies that no "good

elements in between these two indices is a multiple of k. If such a condition is met, the function returns True.

- By using a hashmap to keep track of the remainders, the algorithm ensures a single-pass solution with O(n) time complexity and 0(min(n, k)) space complexity, since the number of possible remainders is bounded by k.
- Let's go through an example to illustrate the solution approach. Suppose we have an array nums = [23, 2, 4, 6, 7] and an integer k = 6. We want to find out if there exists at least one subarray with a sum that is a multiple of k.

### **Iteration 1:**

**Example Walkthrough** 

 $\circ$  Index i = 0, Element v = 23.  $\circ$  Update s: s = 0 + 23 = 23.  $\circ$  Calculate remainder r: r = 23 % 6 = 5.

**Iteration 2:**  $\circ$  Index i = 1, Element v = 2.

 $\circ$  Remainder 5 is not in mp, so we add it: mp =  $\{0: -1, 5: 0\}$ .

def checkSubarraySum(self, nums: List[int], k: int) -> bool:

# Get the modulus of the prefix sum with 'k'

 $mod_index_map = \{0: -1\}$  # The modulus 0 is at the "imaginary" index -1

# If the modulus has been seen before and the distance between

// Put the remainder and index in the map if not already present

// Function to check if the array has a contiguous subarray of size at least 2

modIndexMap[0] = -1; // Initialize with a special case to handle edge case

// If the distance between two same modulus is at least 2,

// it indicates a subarray sum that is a multiple of k

// Create a map to store the modulus occurrence with their index

remainderIndexMap.putIfAbsent(remainder, i);

// If we reach here, no valid subarray was found

return false;

# Initialize the prefix sum as zero

modulus = prefix\_sum % k

Initialize Cumulative Sum and Dictionary: s = 0. Dictionary mp is initialized as  $\{0: -1\}$ .

 $\circ$  Update s: s = 23 + 2 = 25.

**Python** 

class Solution:

```
\circ Calculate remainder r: r = 25 % 6 = 1.
      \circ Remainder 1 is not in mp, so we add it: mp = {0: -1, 5: 0, 1: 1}.
      Iteration 3:
      \circ Index i = 2, Element v = 4.
      \circ Update s: s = 25 + 4 = 29.
      ○ Calculate remainder r: r = 29 % 6 = 5.
      ∘ Remainder 5 is already in mp, and i - mp[5] = 2 - 0 = 2 which is equal to or greater than 2, hence we have found a "good subarray" [23, 2,
        4] with sum 29 which is a multiple of k (since 29 - 23 = 6 which is 6*1).
      • Return True.
  In this example walkthrough, we found a "good subarray" in the third iteration and therefore returned True. This means at least
  one subarray meets the criteria, thus the function would terminate early with a positive result.
Solution Implementation
```

prefix sum = 0 # A dictionary to keep track of the earliest index where # a particular modulus (prefix\_sum % k) is found.

#### # Iterate over the list of numbers for index, value in enumerate(nums): # Update the prefix sum with the current value prefix\_sum += value

```
# the current index and the earlier index of the same modulus
           # is at least 2, we found a subarray sum that's multiple of k
            if modulus in mod_index_map and index - mod_index_map[modulus] >= 2:
                return True
           # Store the index of this modulus if it's not seen before
            if modulus not in mod_index_map:
               mod_index_map[modulus] = index
       # No subarray found that sums up to a multiple of k
       return False
Java
class Solution {
    public boolean checkSubarraySum(int[] nums, int k) {
       // HashMap to store the remainder of the sum encountered so far and its index
       Map<Integer, Integer> remainderIndexMap = new HashMap<>();
       // To handle the case when subarray starts from index 0
       remainderIndexMap.put(0, -1);
       // Initialize the sum to 0
       int sum = 0;
       // Iterate through the array
       for (int i = 0; i < nums.length; ++i) {</pre>
           // Add current number to the sum
           sum += nums[i];
           // Calculate the remainder of the sum w.r.t k
            int remainder = sum % k;
            // If the remainder is already in the map and the subarray is of size at least 2
            if (remainderIndexMap.containsKey(remainder) && i - remainderIndexMap.get(remainder) >= 2) {
               // We found a subarray with a sum that is a multiple of k
               return true;
```

C++

public:

#include <vector>

class Solution {

using namespace std;

#include <unordered\_map>

// that sums up to a multiple of k

} else {

bool checkSubarraySum(vector<int>& nums, int k) {

// Iterate through the numbers in the vector

sum += nums[i]; // Add current number to sum

// Check if the modulus has been seen before

def checkSubarraySum(self, nums: List[int], k: int) -> bool:

# a particular modulus (prefix\_sum % k) is found.

# A dictionary to keep track of the earliest index where

# Update the prefix sum with the current value

# Get the modulus of the prefix sum with 'k'

 $mod_index_map = \{0: -1\}$  # The modulus 0 is at the "imaginary" index -1

# If the modulus has been seen before and the distance between

# the current index and the earlier index of the same modulus

# is at least 2, we found a subarray sum that's multiple of k

# Store the index of this modulus if it's not seen before

if modulus in mod\_index\_map and index - mod\_index\_map[modulus] >= 2:

# Initialize the prefix sum as zero

# Iterate over the list of numbers

modulus = prefix\_sum % k

prefix\_sum += value

return True

for index, value in enumerate(nums):

if modulus not in mod\_index\_map:

int mod = sum % k; // Current modulus of sum by k

if (i - modIndexMap[mod] >= 2) return true;

for (int i = 0; i < nums.size(); ++i) {</pre>

if (modIndexMap.count(mod)) {

unordered\_map<int, int> modIndexMap;

int sum = 0; // Accumulated sum

```
// If this modulus hasn't been seen before, record its index
                modIndexMap[mod] = i;
       // If no qualifying subarray is found, return false
        return false;
};
TypeScript
// Importing necessary utilities
import { HashMap } from 'hashmap';
// Function to check if the array has a contiguous subarray of size at least 2
// that sums up to a multiple of k
function checkSubarraySum(nums: number[], k: number): boolean {
    // Create a map to store the modulus occurrence with their index
    let modIndexMap: Map<number, number> = new Map();
    modIndexMap.set(0, -1); // Initialize with a special case to handle edge case
    let accumulatedSum = 0; // Accumulated sum
    // Iterate through the numbers in the array
    for (let i = 0; i < nums.length; ++i) {</pre>
        accumulatedSum += nums[i]; // Add current number to the accumulated sum
        let mod = accumulatedSum % k; // Current modulus of the accumulated sum by k
        // Check if the modulus has been seen before
        if (modIndexMap.has(mod)) {
           // If the distance between two same modulus is at least 2,
            // it indicates a subarray sum that is a multiple of k
            if (i - modIndexMap.get(mod)! >= 2) return true;
        } else {
            // If this modulus hasn't been seen before, record its index
            modIndexMap.set(mod, i);
    // If no qualifying subarray is found, return false
    return false;
```

#### mod\_index\_map[modulus] = index # No subarray found that sums up to a multiple of k return False

Time and Space Complexity

**Time Complexity** 

class Solution:

prefix\_sum = 0

The provided code consists of a single loop that iterates over the list nums once. For each element of nums, it performs constanttime operations involving addition, modulus, and dictionary access (both lookup and insert). Therefore, the time complexity is determined by the loop and is O(n), where n is the number of elements in nums.

**Space Complexity** 

The space complexity of the code is primarily dependent on the dictionary mp that is used to store the remainders and their respective indices. In the worst case, each element could result in a unique remainder when taken modulo k. Therefore, the maximum size of mp could be n (where n is the number of elements in nums). Thus, the space complexity is also O(n).