

Problem Description

String

Medium (Math)

The problem requires us to find and count the number of substrings within a given binary string s that consist entirely of the character '1'. For example, in the string "0110111", there are several such substrings: "1", "11", "11", "11", "11", and each of them should be counted. The challenge here is to do this efficiently and to deal with potentially very large numbers, the counts need to be returned modulo 10^9 + 7, which is a large prime number commonly used to prevent integer overflow issues in competitive programming.

Intuition

2 substrings that can be formed, all of which consist solely of '1's. This is because each additional '1' potentially adds as many new substrings as its position in the sequence (first '1' adds 1 substring, second '1' adds 2 substrings, and so on). So, we are essentially counting the lengths of continuous sequences of '1's and calculating the number of substrings for each sequence.

The intuition behind the solution is based on the observation that for a sequence of '1's of length n, there are exactly n * (n + 1) /

The solution involves iterating through the string and using a counter variable cont to keep track of the length of a consecutive sequence of '1's. When we encounter a '1', we increment cnt. If we encounter a '0', we reset cnt to zero, because it breaks the sequence of '1's. After each step, regardless of whether we're continuing a sequence or ending one, we add the current value of cnt to ans, which accumulates the total number of substrings of '1's we've seen so far.

Finally, since the answer could be a very large number, we return the total count modulo 10^9 + 7 as instructed by the problem description.

Solution Approach

state during iteration is cnt, which counts the length of consecutive '1's. With every step forward in the string, the algorithm performs the following actions:

The implementation of the solution is relatively straightforward with no need for complex data structures; the only variable that holds

2. If c is '1', increment the cnt variable: this increases the length of the current sequence of '1's by one.

Check the current character (c) of the string.

- 3. If c is not '1' (in this case, it could only be '0' since it's a binary string), reset cnt to zero. This indicates the end of the current
- sequence of '1's and resets the count for the next sequence. 4. After updating cnt, add its current value to ans. This step accumulates the total number of valid substrings formed by the
- sequences of '1's encountered so far. This process works because each time a '1' is encountered and cot is incremented, it effectively counts all the new substrings that

could end with this '1'. If you have a sequence of length n, then adding one more '1' to the sequence adds n + 1 substrings: all the previous substrings plus a new substring that includes the entire sequence. The use of the modulo operation % (10***9 + 7) ensures that we handle the possibility of very large outputs, preventing integer

No additional data structures are required, and the pattern used in this algorithm is commonly known as a single pass or linear scan, as it requires only one iteration through the input string to compute the result.

Example Walkthrough Let's consider a small example binary string s = "11011". Here's how we would apply the solution approach to this input:

1. Initialize cnt = 0 (to count the consecutive '1's) and ans = 0 (to accumulate the total number of substrings).

- 2. Start iterating over the string s from left to right.
- Character s [0] is '1':

```
Increment cnt to 1. Current substrings are: "1".
        Add cnt to ans: ans += 1, hence ans = 0 + 1 = 1.
    Character s [1] is '1':
        Increment cnt to 2. Current substrings are: "1", "11".
         Add cnt to ans: ans += 2, hence ans = 1 + 2 = 3.
3. The next character s [2] is '0', which interrupts the sequence of '1's:
```

overflow and keeping the result within the limits of the problem's constraints.

- Reset cnt to 0. ans remains unchanged.
- Continue iteration.
- Character s [3] is '1':
- Increment cnt to 1. Current substrings are: "1".
 - Character s [4] is '1':
 - Increment cnt to 2. Current substrings are: "1", "11". Add cnt to ans: ans += 2, hence ans = 4 + 2 = 6.

Initialize the answer and a temporary counter for consecutive "1"s

int countSubstrings = 0; // Store the count of valid substrings

int consecutiveOnes = 0; // Counter for consecutive '1's

// Iterate through the string character by character

// Otherwise, reset the count to 0

count = (char === '1') ? count + 1 : 0;

answer = (answer + count) % modulus;

• Add cnt to ans: ans += 1, hence ans = 3 + 1 = 4.

- 5. At this point, we have finished iterating over the entire string. The total count of substrings consisting only of '1's is stored in ans,
 - which equals 6.

total_substrings = consecutive_ones_count = 0

- 6. Return ans % (10^9 + 7) to adhere to the problem constraints. Since 6 is well below the modulo, the final result is simply 6. As we can see from the example, the algorithm correctly counts the individual substrings of '1's and sums them up. It counts "11" at
- consisting of '1's.

the beginning as 2 substrings, resets the count after the '0', and then counts "1" and "11" again, adding up to a total of 6 substrings

Python Solution class Solution: def numSub(self, s: str) -> int:

Iterate through each character in the string for char in s: # If the character is "1", increment the consecutive "1"s counter

```
if char == "1":
10
                   consecutive_ones_count += 1
                   # Add the current count of consecutive "1"s to the total substrings.
11
                   # Each time we encounter a "1", it forms a substring with all the consecutive "1"s before it.
12
13
                   total_substrings += consecutive_ones_count
               # If the character is not "1", reset the consecutive "1"s counter to 0
14
15
               else:
16
                   consecutive_ones_count = 0
17
           # Return the total number of substrings, modulo 10^9 + 7
18
19
           return total_substrings % (10**9 + 7)
20
Java Solution
1 class Solution {
       // This method counts the number of substrings that contains only the character '1'
       public int numSub(String s) {
           final int MODULO = (int) 1e9 + 7; // Define a constant for modulo operation
```

for (int i = 0; i < s.length(); ++i) {</pre> 9 // If the current character is '1', increment the consecutive ones counter 10 // Otherwise, reset it to zero since we're only interested in consecutive '1's 11 12

```
consecutiveOnes = s.charAt(i) == '1' ? consecutiveOnes + 1 : 0;
13
               // Add the current count of consecutive '1's to countSubstrings
14
               // This works because for each new '1' character, it forms a new substring
15
               // ending at this character that has not been counted yet
16
               countSubstrings = (countSubstrings + consecutiveOnes) % MODULO;
17
18
19
20
           // Return the total number of substrings found, modulo the defined constant
21
           return countSubstrings;
23 }
24
C++ Solution
 1 class Solution {
   public:
       // Function to count the number of substrings containing only '1's
       int numSub(string s) {
            long long answer = 0; // Initialize the answer to 0
           int count = 0; // Initialize a counter for consecutive '1's
           const int MODULUS = 1e9 + 7; // Define the modulus value for preventing integer overflow
           // Iterate over each character in the input string
           for (char& character : s) {
```

13 count = character == '1' ? count + 1 : 0; 14 // Add the current count to the answer. This works because for each '1' found, 16

11

12

13

18

23

```
// it contributes to that many substrings ending at that point (e.g., "111" has
               // substrings "1", "11", and "111" ending at the last character).
17
               // Apply modulus operation to keep the number within bounds and handle overflow
18
               answer = (answer + count) % MODULUS;
19
20
21
           // Return the final count of substrings
23
           return static_cast<int>(answer); // Cast the long long answer to int before returning
24
25 };
26
Typescript Solution
   function numSub(sequence: string): number {
       // Define the modulus value to keep the result within integer limits
       const modulus = 10 ** 9 + 7;
       // Initialize the answer to be returned
       let answer = 0;
       // Counter for the consecutive '1's
       let count = 0;
10
       // Iterate through each character in the string
       for (const char of sequence) {
```

// If the current character is '1', increase the count of consecutive '1's

// If the character is '1', increase count, otherwise reset count to 0

// Add the current count to the answer and apply modulus to prevent overflow

19 20 // Return the computed answer return answer; 21 22 }

Time and Space Complexity The code provided counts the number of substrings of contiguous '1's in a given string s. The time complexity and space complexity of the algorithm are analyzed below.

Time Complexity

that it is independent of the input size.

The algorithm goes through each character of the input string s exactly once. During this process, it performs constant time operations such as checking if a character is '1' or '0', incrementing the cnt variable, and adding the value of cnt to ans. Because these operations do not depend on the size of the string and are repeated for each character, the time complexity is directly

proportional to the length of the string. Therefore, the time complexity is O(n), where n is the length of the input string s.

Space Complexity The space used by the algorithm includes a fixed number of integer variables ans and cnt, which do not scale with the size of the input string. As a result, the algorithm uses a constant amount of additional space, resulting in a space complexity of 0(1), indicating