2450. Number of Distinct Binary Strings After Applying Operations

Description

You are given a **binary** string `s` and a positive integer `k`.

You can apply the following operation on the string **any** number of times:

- Choose any substring of size `k` from `s` and **flip** all its characters, that is, turn all `1`'s into `0`'s, and all `0`'s into `1`'s.

Return *the number of **distinct** strings you can obtain*. Since the answer may be too large, return it **modulo** `10^9 + 7`.

Note that:

- A binary string is a string that consists **only** of the characters `0` and `1`.
- A substring is a contiguous part of a string.

Example 1:

```
Input: s = "1001", k = 3
Output: 4
Explanation: We can obtain the following strings:
- Applying no operation on the string gives s = "1001".
- Applying one operation on the substring starting at index 0 gives s = "011 1".
- Applying one operation on the substring starting at index 1 gives s = "1 110".
- Applying one operation on both the substrings starting at indices 0 and 1 gives s = "0000".
It can be shown that we cannot obtain any other string, so the answer is 4.
```

Example 2:

```
Input: s = "10110", k = 5
Output: 2
Explanation: We can obtain the following strings:
- Applying no operation on the string gives s = "10110".
- Applying one operation on the whole string gives s = "01001".
It can be shown that we cannot obtain any other string, so the answer is 2.
```

Constraints:

- `1 <= k <= s.length <= 10^5`
- `s[i]` is either `0` or `1`.