2808. Minimum Seconds to Equalize a Circular Array

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Greedy Array
Medium
                       Hash Table
```

Problem Description

performing a specific operation repeatedly. During each second, for every element at index i, you can update nums [i] to be equal to its current value, the value of the previous element (nums[(i - 1 + n) % n]), or the value of the next element (nums[(i + 1) % n]). The modulo operation ensures that you are wrapping around the array when reaching the ends, which means it actually forms a loop or ring. The goal is to find the minimum number of seconds needed to make all the elements in the array equal. Intuition

In this problem, we are given a 0-indexed array nums of n integers. The task is to make all elements in the array equal by

values. This is because in each operation, you are allowed to choose the previous or next element's value, which can eventually spread any number's occurrence across the array. Since we want to minimize the number of seconds, the best strategy would be to choose the value that will take the least amount

of time to spread through the array. Intuitively, if we have clusters of the same number occurring together, we would prefer to

The key to solving this problem lies in understanding that we can always make the entire array equal to any one of its current

choose one such cluster's value and spread it to the rest of the array. The solution involves the following steps: • We first group indices of identical elements into lists, using a dictionary where the keys are the array's values and the values are lists of indices

• Then, for each group of identical elements:

- We calculate the distance between the first and last occurrence of the value, taking into account the wrap-around using (idx[0] + n idx[-1]). We also calculate the maximum distance between any two consecutive occurrences, as this will represent the maximum time required to

where these numbers occur.

- change the value between these two points using $\max(t, j i)$ for every pair of consecutive indices in the group. • The time needed to make the entire array equal to this value is half the maximum distance found, since the value can spread from both ends of a series.
- By applying this approach, we ensure that we pick the value that will take the least amount of time to replicate across the entire array.
- Solution Approach
- The solution provided uses Python's defaultdict to categorize indices of identical elements into lists, and the inf constant from

The minimum time across all such values is the final answer.

the math module as a representation of infinity, which is employed to find the minimum value as we compare different distances. Here is the step-by-step breakdown of the implementation:

• A defaultdict of lists is instantiated. It will map each unique value in nums to a list of indices where it occurs. This is achieved by enumerating over nums and appending the index i to the list of d[x], where x is the value at index i.

similar results.

• The function returns the value stored in ans.

• The value 1 occurs at indices [0, 4].

• The value 2 occurs at indices [1, 3].

The time needed would be 2 // 2 = 1.

• For value 3, no change as there is only one occurrence.

Step 5: Return the value in ans, which is 0.

Step 4: Find the minimum ans:

Solution Implementation

from collections import defaultdict

• The value 3 occurs at index [2].

Step 2: Initialize ans to infinity.

idx[-1]. o It then proceeds to find the maximum distance between any two consecutive occurrences of the same number within the list. This is done using Python's pairwise function (Python 3.10+). If pairwise is not available, a simple zip like zip(idx, idx[1:]) can be used to achieve

o For every pair (i, j) of consecutive indices in idx, t is updated to the maximum of its current value and the distance between the

• The algorithm updates ans with the minimum between its current value and t // 2. Since ans is initialized to infinity and we are finding the

• A variable ans is initialized to infinity (inf). This will hold the minimum number of seconds required to make all elements of the array equal.

∘ For each list of indices (idx), it calculates t, the distance considering wrap-around between the first and last occurrence: idx[0] + n -

• The algorithm then iterates over the values of the dictionary, which are the lists of indices for each distinct number in the array.

consecutive indices j - i. Finally, because the value can spread from both ends towards the middle, only half this time is needed to make all elements between i and j equal, hence t // 2.

minimum over all iterations, ans will hold the minimum time needed to make all elements equal after examining all distinct numbers.

- This approach effectively breaks down a seemingly complex problem into a series of calculations based on the distribution of values across the array, using dictionary and list structures to organize data and a simple loop to compute the minimum time.
- Let's illustrate the solution approach using a simple example:
- Given the array nums = [1, 2, 3, 2, 1], which is 0-indexed:

• There are no consecutive occurrences to calculate the maximum distance, so the maximum distance remains 1.

○ The time needed is 1 // 2 = 0 (since we can start from both ends, it needs no time to convert values in between).

Step 1: We create a dictionary of list indices for each unique value in nums. In our case:

Step 3: Evaluate each group of identical elements:

Example Walkthrough

For value 2, the indices are [1, 3]. No wrap-around is needed.

 \circ The maximum distance between consecutive occurrences is (3 - 1) = 2.

For value 3, there is only one occurrence, no distance to calculate between indices.

 \circ The distance considering wrap-around is (0 + 5 - 4) % 5 = 1.

For value 1, the list of indices is [0, 4]. Since the array forms a loop:

- For value 1, ans becomes the minimum of infinity and 0, which is 0. • For value 2, ans is the minimum of 0 and 1, which remains 0.
- the value from both ends of the occurrences.

Dictionary to store the indices of each unique number in nums

Populate index_mapping with positions for every number in nums

Time spent is the distance between first and last occurrence

Iterate over pairs of indices to find max distance in between

Update time_spent with the maximum gap found so far

Calculate the minimum seconds required (halve the max distance)

Find distance between consecutive occurrences

minimum_seconds = min(minimum_seconds, time_spent // 2)

Return the minimum seconds required to process all unique numbers

pair_time = indices[i + 1] - indices[i]

time_spent = max(time_spent, pair_time)

Python

def minimum_seconds(self, nums: list) -> int:

for index, value in enumerate(nums):

for indices in index_mapping.values():

for i in range(len(indices) - 1):

return minimum_seconds

Iterate over the indices for each unique number

time_spent = indices[0] + n - indices[-1]

and compare with minimum found so far

index_mapping = defaultdict(list)

index_mapping[value].append(index) # Initialize the minimum seconds to infinity minimum_seconds = float('inf') n = len(nums)

This would mean that no time is needed to make all the elements equal to 1 in this example, since we theoretically start spreading

Java

#include <vector>

class Solution {

public:

#include <algorithm>

using namespace std;

#include <unordered_map>

int minimumSeconds(vector<int>& nums) {

for (int i = 0; i < n; ++i) {

unordered_map<int, vector<int>> indicesMap;

// Iterate over the number—index mapping

for (int i = 1; i < m; ++i) {

return minSeconds;

int n = nums.size(); // get the size of the input vector

// Initialize the minimum number of seconds to a large value

int m = idx.size(); // Size of the index list

minSeconds = min(minSeconds, maxDistance / 2);

int maxDistance = idx[0] + n - idx[m - 1];

int minSeconds = INT_MAX; // use INT_MAX as shorthand for 1 << 30</pre>

vector<int>& idx = kv.second; // Get the vector of indices

for (auto& kv : indicesMap) { // Use 'kv' to represent key-value pairs

// Compute initial distance considering the array as circular

maxDistance = max(maxDistance, idx[i] - idx[i - 1]);

// Update the minimum number of seconds with the lower value

// Return the minimum number of seconds after completing the loop

currentTime = Math.max(currentTime, indices[i] - indices[i - 1]);

minSeconds = Math.min(minSeconds, currentTime >> 1);

Dictionary to store the indices of each unique number in nums

Populate index_mapping with positions for every number in nums

Time spent is the distance between first and last occurrence

Iterate over pairs of indices to find max distance in between

Update time_spent with the maximum gap found so far

Calculate the minimum seconds required (halve the max distance)

Find distance between consecutive occurrences

pair_time = indices[i + 1] - indices[i]

time_spent = max(time_spent, pair_time)

// Create a mapping from each unique number to its indices in the array

indicesMap[nums[i]].push_back(i); // map numbers to their indices

class Solution:

```
import java.util.ArrayList;
import java.util.HashMap;
import java.util.List;
import java.util.Map;
class Solution {
    public int minimumSeconds(List<Integer> nums) {
       // Create a map to hold lists of indices for each unique number in 'nums'
       Map<Integer, List<Integer>> indicesMap = new HashMap<>();
       int n = nums.size(); // Total number of elements in the list
       // Populate the map with lists of indices for each number
       for (int i = 0; i < n; ++i) {
            indicesMap.computeIfAbsent(nums.get(i), k -> new ArrayList<>()).add(i);
       int minSeconds = Integer.MAX_VALUE; // Initialize the minimum seconds to the highest possible value
       // Iterate over the map values, which are lists of indices
        for (List<Integer> indices : indicesMap.values()) {
            int m = indices.size(); // Total number of indices in the current list
            int timeDiff = indices.get(0) + n - indices.get(m - 1);
           // Calculate the initial time difference
           // as the distance from the first to the last occurrence
           // Update the time difference to be the maximum gap between any two consecutive occurrences
            for (int i = 1; i < m; ++i) {
                timeDiff = Math.max(timeDiff, indices.get(i) - indices.get(i - 1));
            // Update the minimum time by comparing with the current calculated time
           minSeconds = Math.min(minSeconds, timeDiff / 2);
       return minSeconds; // Return the minimum number of seconds
```

```
TypeScript
/**
* Computes the minimum seconds needed to cover all numbers by a segment of continuous numbers in the list nums.
* @param nums array of numbers representing different values where we search for the minimum segment.
* @returns the minimum number of seconds required.
*/
function minimumSeconds(nums: number[]): number {
   // Initializes a map to hold arrays of indices for each unique number
   const indexMap: Map<number, number[]> = new Map();
   const length = nums.length;
   // Populates the indexMap with the indices of occurrences of each number
   for (let i = 0; i < length; ++i) {</pre>
        if (!indexMap.has(nums[i])) {
            indexMap.set(nums[i], []);
        indexMap.get(nums[i])!.push(i);
   // Variable to keep track of the minimum seconds needed
    let minSeconds = 1 << 30; // Large initial value</pre>
   // Iterates through each set of indices in the map
    for (const [number, indices] of indexMap) {
        const indicesLength = indices.length;
       // Calculates the initial time as the time to cover from the first to the last occurrences
        let currentTime = indices[0] + length - indices[indicesLength - 1];
       // Updates the currentTime based on the maximum gap between consecutive indices
        for (let i = 1; i < indicesLength; ++i) {</pre>
```

// Loop over the indices to find the largest distance between any two consecutive indices

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# and compare with minimum found so far
    minimum_seconds = min(minimum_seconds, time_spent // 2)
# Return the minimum seconds required to process all unique numbers
return minimum_seconds
```

Time and Space Complexity

unique, this would again take O(n) time.

Time Complexity

// Updates the minimum time

return minSeconds;

n = len(nums)

class Solution:

from collections import defaultdict

// Returns the minimum seconds calculated

def minimum seconds(self, nums: list) -> int:

for index, value in enumerate(nums):

for indices in index_mapping.values():

for i in range(len(indices) - 1):

index_mapping[value].append(index)

Initialize the minimum seconds to infinity

Iterate over the indices for each unique number

time_spent = indices[0] + n - indices[-1]

index_mapping = defaultdict(list)

minimum_seconds = float('inf')

The time complexity of the given code is determined by several factors: • The loop that creates the dictionary d, which has a time complexity of O(n) since it goes through all the elements of nums once. • The loop that goes through d.values() which can potentially iterate through all elements again in the worst case. If all the elements in nums are

• Inside the second loop, there's a nested call to pairwise(idx). The pairwise function itself has 0(k) complexity, where k is the length of the list idx passed to it. In the worst case, where nums has many repeated elements, this nested loop could have O(n) complexity if all elements are the same.

- depends on the distribution of the numbers in the nums list. The worst-case scenario happens when all elements are the same, leading to a complexity of O(n) for the iterations throughout d.values(), compounded with the complexity of pairwise, leading to
- a worst-case time complexity of $0(n^2)$. Therefore, the overall worst-case time complexity of the code is 0(n^2).

Given that pairwise is called inside the loop for every key in the dictionary d, the overall complexity of these nested loops

- **Space Complexity** The space complexity can be analyzed as follows:
- The dictionary d that stores the indices of each element can potentially store n keys with a list of indices as values. In the worst case where all numbers are the same, the list of indices would also contain n values. Therefore, the worst-case space complexity for d is 0(n). • The space used by variables ans, t, idx, i, and j is constant, hence 0(1).
- Taking the above points into consideration, the total space complexity is 0(n) for the dictionary storage. In conclusion, the code has a time complexity of $O(n^2)$ and a space complexity of O(n).