



Problem Description

The problem requires us to determine whether a given string s can be divided into three non-empty substrings that each form a palindrome. A palindrome is a string that reads the same forward and backward—for example, racecar or madam. If it is possible to split the input string into such three palindromic segments, we return true; otherwise, we return false.

Intuition

characters are the same, and if the substring between them (if any) is also a palindrome. The intuition behind the solution involves checking all possible ways of splitting the string into three substrings and testing for each split if all three resulting substrings are palindromes.

The solution approach involves first understanding the characteristics of a palindrome. A string is a palindrome if the first and last

To decide whether a substring is a palindrome, we can precompute the palindromic status of all possible substrings. We create a 2D array g where g[i][j] is True if the substring from index i to index j is a palindrome. This precomputation uses dynamic programming. Once we have this 2D array, we can iterate through all possible splits with two nested loops, using the g array to check if each potential three-segment split consists of palindromes. If such a three-palindrome partitioning exists, we return True; if we finish our iterations without finding one, we return False.

ensuring that the substring between them is a palindrome (by checking the entry g[i+1][j-1]). By precomputing the palindrome statuses, we save time in the later stage where we're iterating over potential partition indices,

The dynamic programming part to fill the g array checks palindromes by comparing the characters at the indices i and j, and by

Solution Approach

The solution employs dynamic programming and precomputation to determine the palindromic nature of all substrings in the string s. The data structure used for this is a 2-dimensional array g where g[i][j] holds a boolean value indicating whether the substring

starting at index i and ending at index j is a palindrome. Here's a step-by-step breakdown of the implementation:

1. Initialize a 2D array g of size n * n filled with True, where n is the length of the string s. Since a substring of length 1 is trivially a

palindrome, the diagonal of the array g (where i==j) represents these substrings and is thus initialized to True.

allowing this solution to be efficient and effective for the problem.

2. Populate the g array using a nested loop. Starting from the end of the string, we move towards the beginning (decreasing i). For each i, we iterate j from i+1 to the end of the string. We update g[i][j] to True only if the characters at i and j are equal and

the substring g[i+1][j-1] is a palindrome. This check ensures that we confirm the palindromic property for a substring by

comparing its outer characters and using the previously computed statuses of its inner substrings. 3. Once the g array is computed, we use two nested loops to try all possible partitions. The first loop iterates over the first potential cut in the string (denoted by i; it marks the end of the first substring), which goes from index 0 to n-3. The second loop goes over the second potential cut (denoted by j; it marks the end of the second substring), which starts one position after i and

goes until n-2. These loops make sure that each of the three resulting substrings is non-empty.

4. For each pair of positions (i, j), we check if the substrings s[0...i], s[i+1...j], and s[j+1...end] (end being n-1, inclusive) are palindromes. This is done using the g array: if g[0][i], g[i+1][j], and g[j+1][n-1] are all True, this means that the current partition forms three palindromic substrings. 5. If a valid partition is found, we immediately return True.

6. If no valid partition is found after going through all possible pairs of (i, j), then it's not possible to split the string into three

The use of dynamic programming makes this process efficient since we avoid recomputing the palindrome status of substrings when

palindromic substrings, and we return False.

checking possible partition positions.

character is a palindrome by itself.

Example Walkthrough

Let's use the string "abacaba" to illustrate the solution approach. 1. We first initialize the 2D array g of size 7 x 7 (since "abacaba" has 7 characters) with True on the diagonal, as any single

2. We then fill the g array with the palindromic status for all substrings. For example, g[0][1] will be False because s[0] is 'a' and

s[1] is 'b', and "ab" is not a palindrome. We continue this for all possible substrings, ending up with g[0][6] being True because

- "abacaba" is a palindrome, and similarly g[2][4] being True for the substring "aca".
- (since we need at least two characters after the first partition for the remaining two palindromic substrings to be non-empty), and our nested loop with variable j will run from i+1 to 5. 4. For each pair (i, j), we check the 2D array g to see if g[0][i], g[i+1][j], and g[j+1][6] are all True.

3. Next, we iterate over all possible pairs of indices (i, j) to find valid partitions. Our first loop with variable i will run from 0 to 4

- 5. When i is 2 (end of the first substring) and j is 4 (end of the second substring), we find that: g[0][2] which represents "aba" is True,
- 7. We eventually find that when i is 0 and j is 3, we get:

6. So the substring partitions "aba ca ba" are not palindromes collectively. We continue searching.

- g[1][3] which represents "bac" is False, and o g[4][6] which represents "aba" is True.
 - g[0][2] is True for "aba", ∘ g[3] [5] is True for "cac", and

def checkPartitioning(self, s: str) -> bool:

Fill the palindrome matrix with correct values

the substring s[i+1:j] is also a palindrome

for start in range(length − 1, −1, −1):

for first_cut in range(length - 2):

for (int i = 0; i < length - 2; ++i) {

return true;

return true;

// If no partitioning satisfies the condition, return false

return false;

for (int j = i + 1; j < length - 1; ++j) {

// If no partitioning was found, return false.

A substring s[i:j+1] is a palindrome if s[i] == s[j] and

for second_cut in range(first_cut + 1, length - 1):

Get the length of the string

length = len(s)

∘ g[6][6] is True for "a".

No palindromic partition here, so we keep searching.

o g[3][4] which represents "ca" is False, and

• g[5][6] which represents "ba" is False.

g[0] [0] which represents "a" is True,

No further searching is needed; we have successfully found a split of the example string "abacaba" into three palindromic substrings using the outlined solution approach.

9. Thus, "abacaba" can be split into three palindromic substrings: "aba", "cac", and "a". At this point, we return True.

8. Continuing this, we finally hit a combination when i is 2 and j is 5, resulting in the partitions "aba cac aba":

Initialize a matrix to keep track of palindrome substrings palindrome = [[True] * length for _ in range(length)] 8

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for end in range(start + 1, length):
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                    palindrome[start][end] = s[start] == s[end] and (start + 1 == end or palindrome[start + 1][end - 1])
15
           # Attempt to partition the string into three palindromes
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           # The external two loops iterate over every possible first and second partition
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Python Solution

class Solution:

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if palindrome[0][first_cut] and palindrome[first_cut + 1][second_cut] and palindrome[second_cut + 1][-1]:
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 23
                         return True
             # If no partitioning into three palindromes is found, return False
 24
             return False
 25
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Java Solution
   class Solution {
       public boolean checkPartitioning(String s) {
           int length = s.length();
           // dp[i][j] will be 'true' if the string from index i to j is a palindrome.
           boolean[][] dp = new boolean[length][length];
           // Initial fill of dp array with 'true' for all single letter palindromes.
           for (boolean[] row : dp) {
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               Arrays.fill(row, true);
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           // Fill the dp array for substrings of length 2 to n.
           for (int start = length - 1; start >= 0; --start) {
14
15
               for (int end = start + 1; end < length; ++end) {</pre>
16
                   // Check for palindrome by comparing characters and checking if the substring
17
                   // between them is a palindrome as well.
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dp[start][end] = s.charAt(start) == s.charAt(end) && dp[start + 1][end - 1];

// If the three parts [0, i], [i+1, j], [j+1, length-1] are all palindromes,

// return true indicating the string can be partitioned into 3 palindromes.

// Try to partition the string into 3 palindrome parts by checking all possible splits.

if (dp[0][i] && dp[i + 1][j] && dp[j + 1][length - 1]) {

If the three substrings created by first_cut and second_cut are all palindromes,

return True, as it is possible to partition the string into three palindromes

C++ Solution 1 class Solution { public: bool checkPartitioning(string str) { int strSize = str.size(); // A 2D dynamic programming matrix to store palindrome status vector<vector<bool>> isPalindrome(strSize, vector<bool>(strSize, true)); // Fill the dp matrix for all substrings for (int start = strSize - 1; start >= 0; --start) { 9 for (int end = start + 1; end < strSize; ++end) {</pre> 10 // Check and set palindrome status 11 12 isPalindrome[start][end] = (str[start] == str[end]) && (start + 1 == end || isPalindrome[start + 1][end - 1]); 13 14 15 16 17 // Check all possible partitions // The outer loop is for the first cut 18 19 for (int firstCut = 0; firstCut < strSize - 2; ++firstCut) {</pre> 20 // The inner loop is for the second cut for (int secondCut = firstCut + 1; secondCut < strSize - 1; ++secondCut) {</pre> 21 22 // If the three partitions are palindromes, return true if (isPalindrome[0][firstCut] && 23 24 isPalindrome[firstCut + 1][secondCut] && 25 isPalindrome[secondCut + 1][strSize - 1]) {

Typescript Solution

return false;

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// Method to check if a string can be partitioned into three palindromic substrings
   function checkPartitioning(str: string): boolean {
       const strSize = str.length;
       // A 2D array to store palindrome status
       const isPalindrome: boolean[][] = Array.from({length: strSize}, () => Array(strSize).fill(true));
       // Fill the array for checking palindrome substrings
       for (let start = strSize - 1; start >= 0; --start) {
           for (let end = start + 1; end < strSize; ++end) {</pre>
               // Check and set palindrome status
10
               isPalindrome[start][end] = (str[start] === str[end]) &&
                                           (start + 1 === end || isPalindrome[start + 1][end - 1]);
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       // Try all possible partitions with two cuts
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       // The outer loop is for the position of the first cut
       for (let firstCut = 0; firstCut < strSize - 2; ++firstCut) {</pre>
18
19
           // The inner loop is for the position of the second cut
20
           for (let secondCut = firstCut + 1; secondCut < strSize - 1; ++secondCut) {</pre>
               // Check if the partitions created by these cuts are palindromic
21
               if (isPalindrome[0][firstCut] &&
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23
                   isPalindrome[firstCut + 1][secondCut] &&
24
                   isPalindrome[secondCut + 1][strSize - 1]) {
25
                   // If all three partitions are palindromes, return true
26
                   return true;
27
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31
       // If no partition satisfies the condition, return false
       return false;
33 }
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Time and Space Complexity
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Time Complexity

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The time complexity of the provided code is $0(n^3)$. Here's a breakdown: • Building the g matrix involves a nested loop that compares each character to every other character, resulting in a 0(n^2) time

- complexity. • The nested loops where i ranges from 0 to n-3 and j ranges from i+1 to n-2 have a combined time complexity of 0(n^2). • Within the innermost loop, the code checks if three substrings (g[0][i], g[i+1][j], and g[j+1][-1]) are palindromes, which is
- an 0(1) operation since the g matrix already contains this information.

These two processes are sequential, so we consider the larger of the two which is 0(n^3) as the time complexity. This comes from the fact that for each potential partition point j, we consider each i and for each i and j, we check a constant-time condition.

Space Complexity

The space complexity of the code is $0(n^2)$. This stems from the space required to store a 2D list (g) that maintains whether each substring from i to j is a palindrome. Since g is an n by n matrix, the space required is proportional to the square of the length of string s.