710. Random Pick with Blacklist

Math

Hash Table

Binary Search Sorting

itself. If it is blacklisted, it maps to a non-blacklisted number outside the range.

Problem Description

Array

Hard

The problem states that an integer n and an array blacklist are given. The task is to design an algorithm that can randomly choose an integer from 0 to n - 1 that is not included in the blacklist. Every valid integer within the range should have an equal chance of being picked. The algorithm should also minimize the number of calls to the random function provided by the programming language you are using.

Randomized

This means that we need to find an efficient way to track which numbers have been blacklisted and ensure that only nonblacklisted numbers are considered when we want to pick a random number. All non-blacklisted numbers should be equally likely to be chosen.

Intuition

The primary challenge lies in designing an algorithm that maintains the equal probability of picking a non-blacklisted number while keeping the process efficient.

One intuitive way is to map all the blacklisted numbers within the range [0, k) to some non-blacklisted numbers in the range

[k, n], where k is the count of non-blacklisted numbers. This is done because the random number selection will only happen

within the [0, k) range, thereby avoiding the blacklisted numbers. If a number within this range is not blacklisted, it maps to

The intuition for the solution comes from the observation that picking a random number in the [0, n - len(blacklist)) range will ensure that each pick is equally likely. Then we can 'remap' these picks if they are supposed to be a blacklisted value to some non-blacklisted value. This remapping is done using a dictionary that keeps track of the blacklisted numbers and their corresponding non-blacklisted 'replacement'. When picking a number, we first check if it needs to be remapped and get the corresponding value if needed.

The Solution class is initialized by creating the mapping of blacklisted numbers if they are within the [0, k) range to the first non-blacklisted numbers outside of this range. As for the pick method, it randomly selects a number within [0, k) and returns the corresponding value in the mapping if it exists, or itself if it is not blacklisted. **Solution Approach**

The solution to this problem employs a smart mapping strategy and a clever use of data structures to efficiently enable the

random selection of non-blacklisted numbers. By understanding that only those blacklisted numbers that fall within the range of

[0, k) truly interfere with our random pick, the solution avoids the need to deal with ones that are naturally excluded from the

Initialization (__init__ method): Compute k as n minus the size of the blacklist, which effectively represents the count of valid integers after excluding the blacklisted

random range.

ones. o Initialize a dictionary selfed that will hold the mapping from the blacklisted within [0, k) to the unblacklisted numbers in [k, n). Loop through each number in the blacklist: ■ For each blacklisted number b that is less than k (and hence within the range of numbers we can randomly pick from), find a number i (starting from k) which is not in the blacklist. This determines the non-blacklisted number that b will map to. Update self.d[b] to i to keep the track of the mapping.

 Randomly select an integer x within the range [0, k). If x is a key in our mapping dictionary (which signifies that x is blacklisted), retrieve the mapped value (the substitute non-blacklisted)

Move to the next integer for mapping (increment i).

number). Otherwise, if x is not blacklisted, it can be returned as is.

To illustrate the solution approach, consider the following example:

because we want to avoid picking a blacklisted number directly.

Blacklisted 3 maps to 7, as 7 is the first non-blacklisted number available.

• Blacklisted 5 maps to 9, as 8 is blacklisted and 9 is the next available non-blacklisted number.

Here's a walk-through of the implementation details:

The use of the dictionary data structure allows the algorithm to quickly access the remapped value, thereby minimizing the

this potentially expensive operation.

Example Walkthrough

Random Pick (pick method):

runtime complexity for each pick operation to constant time (0(1)). Together with only initializing the mappings once in the constructor, this makes the random pick operation very efficient. By limiting the calls to the random function to the interval [0, k), the algorithm ensures that it minimizes the number of calls to

within [0, k), and the time complexity for the pick method is constant, irrespective of the size of the blacklist.

Overall, this solution is both time and space-efficient, where space complexity is dictated by the number of blacklisted numbers

• Let n be 10, so the valid range of numbers is [0, 9]. • Let the blacklist be [3, 5, 8]. In the initialization step of our solution, we perform the following actions:

Compute k as n - len(blacklist), which is 10 - 3 = 7. Therefore, k is 7, and our random pick range becomes [0, 6],

Initialize an empty dictionary self.d to hold the mappings. Since 3 and 5 are the only blacklisted numbers within [0, k),

they will need mapping to non-blacklisted numbers in [k, n). We map blacklisted numbers within [0, k] to the first available non-blacklisted numbers starting from k. Starting at k = 7,

The dictionary now looks like this: $self.d = \{3: 7, 5: 9\}$.

Python

from random import randrange

from typing import List

class Solution:

Let's proceed with the random pick method:

def init (self, n: int, blacklist: List[int]):

Iterate through each blacklisted number

mapping_start_index += 1

for black number in blacklist:

self.mapping dict = {} # Dictionary to hold the mapping

find a non-blacklisted number to map it to

if black number < self.mapping range limit:</pre>

random pick = randrange(self.mapping range limit)

Instantiate the Solution object with a length n and a blacklist

private Map<Integer, Integer> mapping = new HashMap<>();

// Convert the blacklist into a set for faster lookup.

// Instance of Random to generate random numbers.

Set<Integer> blacklistSet = new HashSet<>();

private Random random = new Random();

threshold = n - blacklist.length;

for (int b : blacklist) {

blacklistSet.add(b);

int upperIndex = whitelistSize;

for (int& blackNumber : blacklist) {

++upperIndex;

int randomIndex = rand() % whitelistSize;

function initialize(n: number, blacklist: number[]): void {

let blacklistSet: Set<number> = new Set(blacklist);

// Iterate over each item in the blacklist array.

while (blacklistSet.has(upperIndex)) {

whitelistMapping.set(blackNumber, upperIndex++);

// Generate a random index within the initial whitelist range.

self.mapping dict = {} # Dictionary to hold the mapping

return whitelistMapping.get(randomIndex) ?? randomIndex;

def init (self, n: int, blacklist: List[int]):

mapping_start_index = self.mapping_range_limit

find a non-blacklisted number to map it to

while mapping start index in blacklist_set:

if black number < self.mapping range limit:</pre>

mapping start index += 1

Iterate through each blacklisted number

mapping_start_index += 1

for black number in blacklist:

let randomIndex: number = Math.floor(Math.random() * whitelistSize);

// Convert the blacklist array into a Set for O(1) lookups.

// Focus on blacklisted numbers within the initial whitelist range.

// Locate a non-blacklisted number beyond the initial whitelist range.

// Create a mapping for the blacklisted number to the identified whitelisted number.

whitelistMapping = new Map<number, number>();

let whitelistMapping: Map<number, number>;

whitelistSize = n - blacklist.length;

let upperIndex: number = whitelistSize;

if (blackNumber < whitelistSize) {</pre>

// Function to select a random whitelisted index.

blacklist.forEach(blackNumber => {

upperIndex++;

let whitelistSize: number;

// Iterate over each number in the blacklist.

while (blacklistSet.count(upperIndex)) {

whitelistMapping[blackNumber] = upperIndex++;

// Otherwise, return it as is because it's not blacklisted.

// Function to randomly pick an index from the available whitelisted indices

// Choose a random index from the initial range of whitelisted indices.

// TypeScript lacks `unordered_map` and `unordered_set` but has the `Map` and `Set` classes.

// Initialize necessary structures and perform calculations as would be performed in the constructor.

// If the index has been remapped due to being blacklisted, fetch the remapped index.

return whitelistMapping.count(randomIndex) ? whitelistMapping[randomIndex] : randomIndex;

if (blackNumber < whitelistSize) {</pre>

return self.mapping_dict.get(random_pick, random_pick)

we map:

Solution Implementation

We invoke the pick method to randomly select a number. Let's say the random function returns 5.

We check if 5 is in our mapping dictionary self.d. Since 5 is a key in self.d, we return self.d[5], which is 9.

If the random function returned 4, since 4 is not in self.d, 4 is not blacklisted, and we would return 4 directly.

operation remains efficient as it involves a constant-time dictionary lookup and a random choice within the reduced range.

This process ensures that numbers are only picked from the valid set [0, 6], and if a blacklisted number is picked, it is properly

mapped to a non-blacklisted number hence maintaining equal probability of picking any non-blacklisted number. The pick

blacklist_set = set(blacklist) # Convert the blacklist to a set for efficient lookup # Initialize an index to start mapping from blacklist numbers less than the mapping range limit mapping_start_index = self.mapping_range_limit

self.mapping range limit = n - len(blacklist) # The upper limit for the mapping

If the blacklisted number is within the range of mappable values,

Pick a random number from 0 to the upper exclusive limit (mapping_range_limit)

Return the mapped value if it exists, otherwise return the random_pick itself

self.mapping dict[black number] = mapping start index

Move on to the next possible number for mapping

// A map to keep the mapping of blacklisted numbers to the safe numbers.

Skip all numbers that are in the blacklist until a valid one is found while mapping start index in blacklist_set: mapping start index += 1 # Map the blacklisted number within range to a non-blacklisted number

Get a random number that's not on the blacklist # param_1 = obj.pick() Java

import java.util.HashMap;

import iava.util.HashSet;

import iava.util.Random;

import java.util.Map;

import java.util.Set;

class Solution {

obj = Solution(n, blacklist)

Example usage:

def pick(self) -> int:

```
// The threshold for picking a safe number.
private int threshold;
// Constructor that takes the total number of elements (n) and the list of blacklisted elements (blacklist).
public Solution(int n, int[] blacklist) {
```

```
int nextSafeNumber = threshold;
        for (int b : blacklist) {
            // Only remap blacklisted numbers below the threshold.
            if (b < threshold) {</pre>
                // Find the next non-blacklisted number to map to.
                while (blacklistSet.contains(nextSafeNumber)) {
                    ++nextSafeNumber;
                // Add the mapping from the blacklisted number to the safe number.
                mapping.put(b, nextSafeNumber++);
    // Function to pick a random non-blacklisted number.
    public int pick() {
        // Generate a random number within the range [0, threshold).
        int randomNumber = random.nextInt(threshold);
        // If the number is remapped, return the remapped number, otherwise return it as is.
        return mapping.getOrDefault(randomNumber, randomNumber);
/**
 * Your Solution object will be instantiated and called as such:
* Solution obj = new Solution(n, blacklist);
 * int param_1 = obj.pick();
 */
C++
#include <unordered map>
#include <unordered_set>
#include <vector>
class Solution {
private:
    std::unordered map<int, int> whitelistMapping;
    int whitelistSize;
public:
    // Constructor takes the size of the array (n) and a list of blacklisted indices (blacklist).
    Solution(int n, std::vector<int>& blacklist) {
        // Calculate the effective size of the whitelist (array size minus the size of the blacklist).
        whitelistSize = n - blacklist.size();
```

// Set an index pointing to the start of the upper range which is outside of the whitelist.

// Find the next number not in the blacklist past the initial whitelist range.

// Establish a mapping from the blacklisted number to a whitelisted number from the upper range.

std::unordered_set<int> blacklistSet(blacklist.begin(), blacklist.end());

// Only process blacklisted numbers that would have been chosen otherwise.

// Initialize a variable to the start of the possible non-blacklisted numbers above the threshold.

* Your Solution object will be instantiated and called as such: * Solution* obj = new Solution(n, blacklist); * int result = obj->pick(); */

TypeScript

});

class Solution:

function pick(): number {

};

/**

int pick() {

// Usage example: // initialize(100, [1, 2, 3]); // let randomPick: number = pick(); from random import randrange from typing import List

self.mapping range limit = n - len(blacklist) # The upper limit for the mapping

If the blacklisted number is within the range of mappable values,

self.mapping dict[black number] = mapping start index

Move on to the next possible number for mapping

blacklist_set = set(blacklist) # Convert the blacklist to a set for efficient lookup

Skip all numbers that are in the blacklist until a valid one is found

Map the blacklisted number within range to a non-blacklisted number

Initialize an index to start mapping from blacklist numbers less than the mapping range limit

// Check and return the mapped index if originally blacklisted, else return the original.

```
def pick(self) -> int:
        # Pick a random number from 0 to the upper exclusive limit (mapping_range_limit)
        random pick = randrange(self.mapping range limit)
        # Return the mapped value if it exists, otherwise return the random_pick itself
        return self.mapping_dict.get(random_pick, random_pick)
# Example usage:
# Instantiate the Solution object with a length n and a blacklist
# obj = Solution(n, blacklist)
```

Time and Space Complexity

Get a random number that's not on the blacklist

Time Complexity <u>_init</u>_ method: The initialization method initializes the mapping of a blacklist to new values. For each value in the blacklist, there is a possibility of a while loop running if the value is less than self.k. Considering that i is incremented each time to

param_1 = obj.pick()

find a non-blacklisted value, and assuming the worst-case scenario where all the blacklisted values are less than k, the while loop has to iterate over all values from self.k to n - 1 in the worst case. However, since each value from the blacklist requires only one mapping operation, and we do not revisit already mapped values, the time complexity would be O(B), where

(not likely in average scenarios) due to hash collisions, it could be O(k) but we generally do not consider this for average-case analysis, particularly because Python dictionaries are well optimized. Hence, the time complexity of pick is O(1). **Space Complexity** • The space complexity of the __init__ method is O(B). The dictionary self.d used to store the remapped values will at most have B entries,

• The pick method does not use any additional space that scales with the input size, so its space complexity is O(1).

where B is the length of the blacklist. The set black also takes O(B) space.

B is the length of the blacklist, assuming set membership test operations are O(1) which is the average case for Python sets.

pick method: This method generates a random number and looks up the value in the dictionary (if it is a blacklisted value

that has been remapped). Generating a random number is O(1), and dictionary lookup is on average O(1). In the worst case