## 1150. Check If a Number Is Majority Element in a Sorted Array

**Binary Search** Array Easy

## **Problem Description**

Given an integer array nums which is sorted in non-decreasing order, and an integer target, the task is to determine whether target is a "majority" element in nums. A majority element is one that appears more than nums, length / 2 times. The function should return true if target is indeed a majority element, and false otherwise.

#### Intuition

search to quickly find the first and last occurrences of the target element. In Python, this can be efficiently done using the bisect\_left and bisect\_right functions from the bisect module. • bisect\_left returns the index of the first occurrence of target in nums (or the index where target would be inserted to maintain the sorted

The intuition behind the solution comes from the property of the array being sorted in non-decreasing order. We can use <u>binary</u>

- order if it's not present). • bisect\_right returns the index of the first element greater than target (which would be one past the last occurrence of target if target is in nums).
- By subtracting the index returned by bisect\_left from the index returned by bisect\_right, we get the total number of times

target appears in nums. If this number is greater than nums, length / 2, then target is a majority element, and we return true. If not, we return false. Using binary search makes the solution very efficient even for large arrays, since we avoid scanning the whole array and operate

Solution Approach

The solution uses a binary search approach to find the first and last occurrences of the target element in the sorted array. The

search key is less than the item in the middle of the interval, narrow the interval to the lower half; otherwise, reduce it to the

#### binary search algorithm is a well-known method that operates by repeatedly dividing the search interval in half. If the value of the

with a time complexity of O(log n).

upper half. Repeatedly checking in this manner until the value is found or the interval is empty. Here's how the bisect\_left and bisect\_right functions contribute to the solution: bisect\_left(nums, target): This line of code uses the bisect\_left function from Python's bisect module. Given the sorted

array nums, it finds the leftmost position at which target should be inserted in order to maintain the sorted order. If target is

already in nums, bisect\_left will return the index of the first occurrence of target. This is effectively the start index of target in the array.

- bisect\_right(nums, target): Similarly, bisect\_right finds the rightmost position to insert target while keeping the array sorted. If target exists in the array, bisect\_right will return the index directly after the last occurrence of target. This is essentially the index at which target would no longer appear in the array.
- subtracting the left index from the right index (right left). This gives us the total count of target in nums. To determine if target is a majority element, the code compares the count of target with half of the array's length (len(nums) // 2). The integer division by two ensures that we have a threshold which target's count must exceed to be considered a majority

With the indices from bisect\_left and bisect\_right, the code calculates the number of times target appears in the array by

element. If the count is greater than this threshold, the function returns true; otherwise, it returns false. The data structure used here is the list nums, and the algorithm implemented is binary search through the use of bisect\_left and

bisect\_right. No additional data structures are necessary. This approach is efficient because it minimizes the number of elements inspected, and the binary search is performed in O(log n) time complexity, where n is the number of elements in nums.

Let's consider a small example to illustrate the solution approach. Suppose we have the array nums and the target given as follows:

### The array nums is sorted, and we want to determine whether 3 is a majority element. The majority element must appear more than

target = 3

nums = [1, 2, 2, 3, 3, 3, 3]

**Example Walkthrough** 

element. Let's apply the binary search approach using the bisect\_left and bisect\_right functions from the bisect module:

len(nums) / 2 = 7 / 2 = 3.5 times. Since the array length is 7, the target must appear more than 3 times to be a majority

from bisect import bisect\_left left\_index = bisect\_left(nums, target) # left\_index is 3

from bisect import bisect\_right

```
right_index = bisect_right(nums, target) # right_index is 7
  This suggests that the index directly after the last appearance of 3 in the array nums is 7.
```

is\_majority = count > len(nums) // 2 # is\_majority is True

def isMajorityElement(self, nums: List[int], target: int) -> bool:

count = right\_index - left\_index # count is 4

Find the right index for the target 3 using bisect\_right:

This indicates that the first occurrence of 3 in the array nums is at index 3.

Find the left index for the target 3 using bisect\_left:

Finally, check if count is greater than len(nums) / 2 to determine if target is a majority element:

Now we calculate the total count of target by subtracting the left index from the right index:

The variable count now holds the total number of times target appears in nums, and in this case, it is 4.

minimal computation compared to traversing the entire array. The example validates the solution's ability to efficiently solve the

So, using this binary search approach, we have determined that the target element 3 is a majority element in the array with

Since 4 is greater than 3.5, we can confirm that 3 is indeed a majority element in the array nums.

**Python** 

# Find the leftmost index where `target` should be inserted to keep the list sorted.

# Find the rightmost index where `target` should be inserted to keep the list sorted.

// Function to check if the target is the majority element in the sorted array

# Check if the count of `target` in the list is greater than half the length of the list.

# This is done by comparing the difference between `right\_index` and `left\_index`, which

#### # gives the number of occurrences of `target`, to half the length of the list. return right\_index - left\_index > len(nums) // 2 Java

given problem.

class Solution:

class Solution {

Solution Implementation

from bisect import bisect\_left, bisect\_right

left\_index = bisect\_left(nums, target)

right\_index = bisect\_right(nums, target)

public boolean isMajorityElement(int[] nums, int target) {

int startIndex = findFirstOccurrence(nums, target);

#include <algorithm> // Required for std::lower\_bound and std::upper\_bound

// Use lower\_bound to find the first occurrence of 'target'

// Calculate the number of times 'target' appears in the vector

auto firstOccurrence = std::lower\_bound(nums.begin(), nums.end(), target);

auto lastOccurrence = std::upper\_bound(nums.begin(), nums.end(), target);

// Check if the count of 'target' is more than half the size of the vector

// Use upper\_bound to find the position immediately after the last occurrence of 'target'

bool isMajorityElement(vector<int>& nums, int target) {

int count = lastOccurrence - firstOccurrence;

bool isMajority = count > nums.size() / 2;

return isMajority;

from bisect import bisect\_left, bisect\_right

Time and Space Complexity

left index = bisect left(nums, target)

class Solution:

// Find the start index of the target value

```
// Find the start index of the value immediately after the target
   int endIndex = findFirstOccurrence(nums, target + 1);
   // Check if the count of the target value is more than half of the array's length
   return (endIndex - startIndex) > nums.length / 2;
// Helper function to find the first occurrence of a value using binary search
private int findFirstOccurrence(int[] nums, int value) {
    int left = 0;
    int right = nums.length;
   while (left < right) {</pre>
       // Compute the middle index
        int mid = left + (right - left) / 2;
       // Narrow down to the left half if the middle element is greater than or equal to the value
        if (nums[mid] >= value) {
            right = mid;
        } else {
            // Otherwise, narrow down to the right half
            left = mid + 1;
   // Return the starting index where the target value would be or is located
   return left;
```

```
};
```

C++

public:

#include <vector>

class Solution {

```
TypeScript
// This function determines if a given target is the majority element in a sorted array.
function isMajorityElement(nums: number[], target: number): boolean {
   // Helper function that performs a binary search to find the start
   // index of a given number (x) in the sorted array.
   const binarySearch = (x: number): number => {
        let leftIndex = 0;
        let rightIndex = nums.length;
       // Perform a binary search.
       while (leftIndex < rightIndex) {</pre>
            let midIndex = (leftIndex + rightIndex) >> 1; // Equivalent to Math.floor((leftIndex + rightIndex) / 2)
            if (nums[midIndex] >= x) {
                rightIndex = midIndex;
            } else {
                leftIndex = midIndex + 1;
       return leftIndex;
   };
   // Using the helper function to find the first occurrence of the target.
   const firstTargetIndex = binarySearch(target);
   // Finding the first index past the last occurrence of the target
   // using the next number (target + 1).
   const firstIndexPastTarget = binarySearch(target + 1);
   // Determine if the target is the majority element by comparing the
```

return firstIndexPastTarget - firstTargetIndex > nums.length >> 1; // Equivalent to Math.floor(nums.length / 2)

```
# Find the rightmost index where `target` should be inserted to keep the list sorted.
right index = bisect right(nums, target)
# Check if the count of `target` in the list is greater than half the length of the list.
# This is done by comparing the difference between `right_index` and `left_index`, which
# gives the number of occurrences of `target`, to half the length of the list.
return right index - left index > len(nums) // 2
```

# Find the leftmost index where `target` should be inserted to keep the list sorted.

// number of occurrences to more than half the size of the array.

def isMajorityElement(self, nums: List[int], target: int) -> bool:

**Time Complexity** The time complexity of the provided code is determined by the functions bisect\_left and bisect\_right from Python's bisect module. Both functions perform binary search to find the leftmost and rightmost positions of target in the sorted array nums,

performs two binary searches, one for bisect\_left and one for bisect\_right, the total time complexity is:

 $2 * 0(\log n) = 0(\log n)$ This simplifies to  $O(\log n)$  because the constants are dropped in Big O notation.

array nums. Therefore, the space requirements of the algorithm do not scale with the input size.

# **Space Complexity**

respectively.

The space complexity of the code is 0(1) since it uses only a fixed amount of extra space. The variables left and right are used to store the indices found by the binary search, and no additional data structures are created that depend on the size of the input

The binary search algorithm has a time complexity of  $O(\log n)$ , where n is the number of elements in the array. Since the code