2063. Vowels of All Substrings

String

Dynamic Programming

Problem Description

The task is to calculate the total number of vowels present in all possible substrings of a given string, word. Vowels are the characters 'a', 'e', 'i', 'o', and 'u'. A substring is defined as any continuous sequence of characters within the string. It's important to note that since we are counting vowels in every possible substring, a single vowel can contribute to the count multiple times, depending on its position in the string and the number of substrings that include it. Also, the total count may be very large, so special attention should be paid to avoid integer overflow during the calculation.

Combinatorics

Intuition

Medium

to the total count. A character at position i in the string word of length n is part of i + 1 substrings starting at or before position i and part of n - i substrings ending at or after position i. Therefore, that character is found in a total of (i + 1) * (n - i)substrings. By looping through the characters of the word and checking if each character is a vowel, we can use the above formula to count

To find the solution without checking every possible substring directly, we can consider how many times each vowel contributes

how many times each vowel appears across all substrings. Then, summing these counts gives us the total number of vowels in all substrings. Python's list comprehension makes this process concise and efficient, as seen in the provided solution. This approach significantly reduces the computational complexity compared to the naive approach of generating and checking every possible substring individually.

The solution to this problem utilizes a single-pass algorithm along with the mathematical concept that each character in a string

Solution Approach

Here's a walk-through of the implementation steps with reference to the provided Python code:

- 1. We determine the length n of the string word. 2. We initialize a total sum of vowel occurrences in all substrings, which will be our final result. This sum starts at 0.

contributes to several substrings based on its position.

- 3. We then iterate through the string word using a for loop with enumerate, which gives us each character c along with its index i. 4. Within the loop, we check if the current character c is a vowel. This is accomplished by checking if c is in the string 'aeiou'.
- 5. For every vowel found, we calculate its contribution to the total count. The number of times this vowel appears in all substrings is given by (i +
- 1) * (n i), where i + 1 is the number of possible starting points for substrings that include this character, and n i is the number of possible ending points.
- 6. We add this contribution to the total sum for each vowel encountered. 7. Finally, the total sum is returned as the result.
- The provided solution uses a concise list comprehension that combines these steps into a single line. The sum function calculates

sum((i + 1) * (n - i) for i, c in enumerate(word) if c in 'aeiou')

the aggregate total by adding up the contributions from each vowel character in the string. Here's the core logic in the code:

substrings explicitly. It has a time complexity of O(n), where n is the length of the string since it iterates through the string once, and each operation within the loop is constant time. There's no complex data structure used, and the space complexity is O(1) as it only keeps track of the total sum and loop variables.

This solution is efficient because it only involves processing each character of the string once and does not require generating all

First, we determine the length of the string word, which is n = 5.

Example Walkthrough

We initialize the total sum of vowel occurrences in all substrings to 0. This will hold our result.

Let's go through an example to illustrate the solution approach using the string word = "abcde".

Let's walk through each character of the string abcde:

2. We calculate its contribution: (0 + 1) * (5 - 0) = 5.

- For character a at index i = 0:
- 1. We check if a is a vowel yes, it is.

Now, we iterate through the string word. For each iteration, we consider both the character c and its index i.

3. We add this to the total sum, so the sum is now 5.

```
For character b at index i = 1:
1. b is not a vowel, so we do not count it.
For character c at index i = 2:
```

1. d is not a vowel, so we skip it as well. For character e at index i = 4:

For character d at index i = 3:

1. c is also not a vowel, so we continue.

- 1. We check if e is a vowel it is. 2. We calculate its contribution: (4 + 1) * (5 - 4) = 5.
- substrings of "abcde" equal 10.
- This walkthrough demonstrates the core logic of the provided Python code:

3. We add this to the total sum, which becomes 5 (from a) + 5 (from e) = 10.

sum((i + 1) * (5 - i) for i, c in enumerate("abcde") if c in 'aeiou')

By following these steps, we efficiently calculate the total number of vowel occurrences in all possible substrings of a given

Since there are no more characters in the string, we have completed our iteration. The total vowel occurrences in all possible

string.

We return 10 as the final result.

Solution Implementation

```
Python
```

Initialize a variable to hold the total count of vowels in all substrings

contribution = (index + 1) * (word_length - index)

class Solution: def count_vowels(self, word: str) -> int: # Calculate the length of the word word_length = len(word)

If it's a vowel, calculate the contribution of this vowel to the total count

the number of ways to choose an end point (word_length - index choices).

// Function to count the total number of vowel appearances in all substrings of the word.

// Check if the character is a vowel - 'a', 'e', 'i', 'o', or 'u'.

currentChar == 'o' || currentChar == 'u') {

// Return the total count of vowel appearances in all substrings.

if (currentChar == 'a' || currentChar == 'e' || currentChar == 'i' ||

totalVowels += (static_cast<long long>(i) + 1) * (wordLength - i);

long long totalVowels = 0; // Initialize a variable to keep track of the total vowels count.

char currentChar = word[i]; // Store the current character to compare it against vowels.

// The number of times this vowel character will appear in all possible substrings

// is the product of its position (1-indexed) and its "rightward reach" (n-i).

int wordLength = word.size(); // Find the length of the word once to avoid multiple calls to `size()`.

The vowel contributes to all substrings that start before (or at) this character

by multiplying the number of ways to choose a start point (index + 1 choices) by

and end after (or at) this character. The number of such substrings can be calculated

```
# Iterate through each character in the word along with its index
for index, char in enumerate(word):
    # Check if the current character is a vowel
```

vowel_count = 0

if char in 'aeiou':

```
# Add the contribution of this vowel to the total count
               vowel_count += contribution
       # Return the total count of vowels in all substrings
       return vowel_count
Java
class Solution {
   public long countVowels(String word) {
        long totalCount = 0; // Initialize total count of vowels in substrings
        int wordLength = word.length(); // Cache the length of the word for efficiency
       // Iterate over each character in the word
       for (int i = 0; i < wordLength; ++i) {
           char currentChar = word.charAt(i); // Get the character at the current index
           // Check if the current character is a vowel
           if (currentChar == 'a' || currentChar == 'e' || currentChar == 'i' || currentChar == 'o' || currentChar == 'u') {
               // If it's a vowel, add to the total count based on its position and remaining length
               // The count is the product of the number of times this vowel can appear in
               // the start of a substring (i+1 times) and in the end of a substring (wordLength - i times)
               totalCount += (long) (i + 1) * (wordLength - i);
       // Return the total count of vowels found in all the substrings
       return totalCount;
C++
```

```
return totalVowels;
};
TypeScript
```

class Solution {

long long countVowels(string word) {

// Loop through each character of the word.

for (int i = 0; i < wordLength; ++i) {</pre>

public:

```
// Function to count the total number of vowels in a given string, where each vowel
  // is counted as many times as it contributes to each possible substring.
  // @param {string} word — The word to count vowels in
  // @returns {number} - The total count of vowels contributing to substrings
  function countVowels(word: string): number {
      const wordLength = word.length;
      let vowelCount = 0;
      // Loop over all characters in the word
      for (let index = 0; index < wordLength; ++index) {</pre>
          // Check if the current character is a vowel
          if (['a', 'e', 'i', 'o', 'u'].includes(word[index])) {
              // If it is a vowel, add the count to the running total, factoring in
              // the number of possible substrings it can be part of:
              // Multiply the position of the vowel in the string (index + 1)
              // by the number of ways to choose the ending of the substring (wordLength - index)
              vowelCount += (index + 1) * (wordLength - index);
      // Return the total count of vowels
      return vowelCount;
class Solution:
   def count_vowels(self, word: str) -> int:
       # Calculate the length of the word
       word_length = len(word)
       # Initialize a variable to hold the total count of vowels in all substrings
        vowel_count = 0
       # Iterate through each character in the word along with its index
        for index, char in enumerate(word):
           # Check if the current character is a vowel
           if char in 'aeiou':
               # If it's a vowel, calculate the contribution of this vowel to the total count
               # The vowel contributes to all substrings that start before (or at) this character
```

Time and Space Complexity

return vowel_count

The given Python code snippet defines a function that counts the number of times a vowel appears in a string, such that each occurrence of a vowel is counted as many times as the number of substrings that include it.

and end after (or at) this character. The number of such substrings can be calculated

by multiplying the number of ways to choose a start point (index + 1 choices) by

the number of ways to choose an end point (word_length - index choices).

contribution = $(index + 1) * (word_length - index)$

vowel_count += contribution

Return the total count of vowels in all substrings

Add the contribution of this vowel to the total count

The time complexity of the function is O(n) where n is the length of the input string word. This is because the function contains a single loop (created by the sum function and list comprehension) that iterates over each character in the string exactly once.

Time Complexity: O(n)

Inside the loop, each step involves simple arithmetic operations that are constant time, namely (i + 1) * (n - i), and a membership test c in 'aeiou', which is also constant time since the set of vowels is of fixed size. The calculation of the arithmetic progression is done for each vowel character in the string, thus the total operations scale linearly with the size of the input n.

Space Complexity: O(1)

The space complexity of the function is O(1). There are no data structures used that grow with the input size. Temporary variables like i and c are reused for each character in the string. The string 'aeiou' is a constant space that does not change with the input. Thus, the algorithm uses a fixed amount of space regardless of the size of the input.