817. Linked List Components

Medium Array Hash Table Linked List

Problem Description

This problem presents a scenario where you're given two inputs: the `head` of a singly linked list, which contains unique integer values, and an integer array `nums`, which contains a subset of the values found in the linked list. The task is to find out how many "connected components" are present in the array `nums`. A connected component here is defined as a sequence of numbers that appear consecutively in the linked list. Hence, if two numbers are adjacent in the linked list and both are present in `nums`, they form part of the same connected component. The question asks for the total count of such connected components.

For example, consider the linked list `1->2->3->4` and the array `nums = [2, 4]`. Here, `2` and `4` each form their own connected component because they are not consecutive in the linked list. The answer would be 2.

Intuition

The key to solving this problem lies in understanding the structure of a linked list and the definition of connected components in the context of this problem. We find connected components by traversing the linked list and checking for consecutive occurrences of the values in `nums`.

Here's a step-by-step intuition behind the solution:

1. We want to count the number of connected components, so we track that with an integer variable, which we can call `ans`.
2. We create a set `s` from `nums`. Using a set is efficient for checking if an element exists within it. This is important because we'll need to check for the existence of each linked list node's value in `nums`.
3. We begin to traverse the linked list starting from the given `head`. For each node, we first check if we are currently looking at a value that is *not in our set* `s` (thus not in `nums`). If it is not, we simply move to the next node.
4. When we find a node with a value that is in the set `s`, this indicates the potential start of a connected component. We increment our `ans` count, indicating we've found a new connected component.
5. We continue traversing the linked list from this node onward, as long as the subsequent nodes' values are in the set `s`—which means we're still within the same connected component.
6. As soon as we find a node with a value not in `s`, or we reach the end of the list, we start looking for a new connected component (repeating the process from step 3).

The result at the end, after we've traversed the entire linked list, is the count of connected components in `nums`.

Solution Approach

The solution to this problem employs a simple linear traversal algorithm, which makes use of the singly linked list and set data structures. The aim is to efficiently determine whether each node's value in the linked list is part of a connected component as defined by the array `nums`. Here is a breakdown of how the given Python solution achieves this:

1. An auxiliary data structure, a set (referred to as `s` in the reference code), is created from the list of integers `nums`. Sets provide an average time complexity of O(1) for look-up operations, which is crucial for determining whether a node's value is part of `nums`.
2. A variable `ans` is initialized to 0. This variable keeps track of the number of connected components in `nums`.
3. The solution then enters a while loop, which continues to iterate as long as there is a node (`head`) to process in the linked list.
4. Inside the top-level while loop, a nested while loop skips over any nodes whose values are not in the set `s`. This is because such nodes are not part of any connected component we're interested in.
5. The code increments `ans` by 1 if and only if it finds a node that contains a value in `s`, indicating the beginning of a potential connected component. This increment happens before entering the next nested loop, ensuring that we count each connected component once. The condition `head is not None` ensures we don't count an extra component when we reach the end of the list.
6. Another nested while loop continues to traverse the linked list as long as consecutive nodes have values in the set `s`, effectively walking through the nodes of a single connected component.
7. Once the innermost while loop ends (because it encounters a node not in `s` or reaches the end of the list), control returns to the top-level while loop to seek the next connected component.

Through this method, the solution correctly identifies each connected component in the subset `nums` by traversing the linked list once. This linear pass through the list results in a solution with O(n) time complexity, where n is the number of nodes in the linked list. The space complexity of the solution is also O(n), which is due to the creation of the set from `nums`.

Example Walkthrough

Let's consider a linked list with the following values and the array `nums = [3, 4, 1]`:

```
Linked List: 1 -> 2 -> 3 -> 4
Array `nums`: [3, 4, 1]
```

We're interested in finding how many connected components we can find in `nums` that correspond to consecutive elements in the linked list.

1. Create a set `s` from the array `nums`, which gives us `s = {1, 3, 4}`.
2. Initialize the counter to zero: `ans = 0`.
3. Start traversing the linked list:
   a. First node is `1`, which is in `s`. This could be the start of a connected component, so we increment `ans` to 1. b. Move to the next node, which is `2`. It's not in `s`, so the potential connected component is complete.
4. Continue traversing:
   a. The next node is `3`, which is in `s`. This is the start of another connected component. Increment `ans` to 2. b. Move to the next node, which is `4` and also in `s`. However, since `4` is directly after `3` and both are in `s`, they belong to the same connected component. No increment to `ans`. c. There are no more nodes to process.

Thus, we have traversed the linked list and counted a total of `2` connected components that are found in `nums`.

Solution Implementation

Python

```
# Definition for singly-linked list.
class ListNode:
    def __init__(self, val=0, next=None):
        self.val = val
        self.next = next

class Solution:
    def numComponents(self, head: Optional[ListNode], nums: List[int]) -> int:
        # Initialize count of connected components to 0
        count = 0
        # Convert the nums list to a set for constant-time lookups
        nums_set = set(nums)

        # Traverse through the linked list
        while head:
            # Skip nodes until a node with a value in nums_set is found
            while head and head.val not in nums_set:
                head = head.next

            # If a node with a value in nums_set is found, increment count
            if head:
                count += 1

            # Skip all subsequent nodes that are also in nums_set
            while head and head.val in nums_set:
                head = head.next

        # Return the total number of connected components
        return count

# Additional explanations about the code structure:
# 1. The first while loop progresses through nodes that are not part of any component until a start of a component is found.
# 2. Once a start of a component is detected, the connected component is counted with `count += 1`.
# 3. The second while loop continues to traverse through the linked list but only through the nodes
#    that are part of the current component, until it reaches a node that is not part of nums_set.
# 4. The process continues until all nodes in the linked list are visited.
```

Java

```
class Solution {
    // Counts the number of connected components in the list that are present in the array 'nums'.
    public int numComponents(ListNode head, int[] nums) {
        int count = 0; // Counter for the number of components
        Set<Integer> set = new HashSet<>(); // HashSet to store elements of 'nums' for constant time access

        // Add all elements of the array 'nums' to the HashSet
        for (int value : nums) {
            set.add(value);
        }

        // Traverse the linked list to find connected components
        while (head != null) {
            // Skip nodes until we find one that is contained in 'nums'
            while (head != null && !set.contains(head.val)) {
                head = head.next;
            }

            // If a node is found in set, increment the component count once
            if (head != null) {
                count++;
                // Move past the current component
                while (head != null && set.contains(head.val)) {
                    head = head.next;
                }
            }
        }

        return count; // Return the total number of components found
    }
}

// Definition for singly-linked list provided for context.
class ListNode {
    int val;
    ListNode next;
    ListNode() {}
    ListNode(int val) { this.val = val; }
    ListNode(int val, ListNode next) { this.val = val; this.next = next; }
}
```

C++

```
#include <unordered_set>
#include <vector>

// Definition for singly-linked list.
struct ListNode {
    int val;
    ListNode *next;
    ListNode() : val(0), next(nullptr) {}
    ListNode(int x) : val(x), next(nullptr) {}
    ListNode(int x, ListNode *next) : val(x), next(next) {}
};

class Solution {
public:
    // Function to count the number of connected components in the linked list
    // that appear in 'nums' array as consecutive nodes.
    int numComponents(ListNode* head, std::vector<int>& nums) {
        // Convert the vector 'nums' into an unordered_set for constant-time lookups.
        std::unordered_set<int> values_set(nums.begin(), nums.end());

        int component_count = 0; // Initialized the count of components to 0.

        while (head) {
            // Skip all nodes whose values do not appear in 'nums'.
            while (head && values_set.count(head->val) == 0) {
                head = head->next;
            }

            // If 'head' is not nullptr, we have encountered a component, so increment the count.
            if (head) {
                ++component_count;
            }

            // Move past the current component.
            while (head && values_set.count(head->val)) {
                head = head->next;
            }
        }

        return component_count; // Return the number of components found.
    }
};
```

TypeScript

```
// Class definition for singly-linked list node.
class ListNode {
  val: number;
  next: ListNode | null;
}

/**
 * Counts the number of connected components in the linked list
 * that are present in the given 'nums' array.
 *
 * @param head The head node of the linked list.
 * @param nums An array of numbers representing the target values.
 * @return The number of connected components that are subsets of 'nums'.
 */
function numComponents(head: ListNode | null, nums: number[]): number {
    // Initialize a Set with the elements from 'nums' to facilitate constant-time checks.
    const numsSet = new Set<number>(nums);
    // Variable to hold the count of connected components found.
    let componentCount = 0;
    // Iterator for traversing the linked list nodes.
    let currentNode = head;
    // Flag to keep track of whether we're inside a component.
    let isInComponent = false;

    // Traverse the linked list.
    while (currentNode !== null) {
        // If the current node's value is in 'numSet', we might be in a component.
        if (numsSet.has(currentNode.val)) {
            // If 'isInComponent' is false, we've found the start of a new component.
            if (!isInComponent) {
                isInComponent = true; // We're now inside a component.
                componentCount++;     // Increment our component count.
            }
        } else {
            // If the current node's value is not in 'numSet', we're not in a component.
            isInComponent = false;
        }
        // Move to the next node in the list.
        currentNode = currentNode.next;
    }

    // Return the total components count.
    return componentCount;
}
```

```
# Definition for singly-linked list.
class ListNode:
    def __init__(self, val=0, next=None):
        self.val = val
        self.next = next

class Solution:
    def numComponents(self, head: Optional[ListNode], nums: List[int]) -> int:
        # Initialize count of connected components to 0
        count = 0
        # Convert the nums list to a set for constant-time lookups
        nums_set = set(nums)

        # Traverse through the linked list
        while head:
            # Skip nodes until a node with a value in nums_set is found
            while head and head.val not in nums_set:
                head = head.next

            # If a node with a value in nums_set is found, increment count
            if head:
                count += 1

            # Skip all subsequent nodes that are also in nums_set
            while head and head.val in nums_set:
                head = head.next

        # Return the total number of connected components
        return count

# Additional explanations about the code structure:
# 1. The first while loop progresses through nodes that are not part of any component until a start of a component is found.
# 2. Once a start of a component is detected, the connected component is counted with `count += 1`.
# 3. The second while loop continues to traverse through the linked list but only through the nodes
#    that are part of the current component, until it reaches a node that is not part of nums_set.
# 4. The process continues until all nodes in the linked list are visited.
```

Time and Space Complexity

The provided Python code aims to determine the number of connected components in a linked list where every node's value exists in the given `nums` list. To analyze the time complexity and space complexity of the code, let's break it down:

Time Complexity:

The time complexity of the code is analyzed by examining the operations performed at each step:

1. There is a while loop that continues as long as there are nodes in the linked list.
2. Inside this loop, there are two nested while loops:
   - The first inner while loop iterates until a node's value that exists in `s` (set containing all values from `nums`) is found, or until the end of the list is reached.
   - The second inner while loop continues as long as the nodes' values belong to `s`.

Each node of the linked list is visited at most twice: once to check for traversal to a component that is part of `s`, and once to move through that component. Therefore, if there are `n` nodes in the linked list, the algorithm will take `O(n)` time.

Space Complexity:

The space complexity is determined by the additional space used by the algorithm:

1. A set `s` is created to store the values from `nums`. If there are `m` numbers in `nums`, the space complexity for the set will be `O(m)`.
2. No other data structures are used that grow with the size of the input. Thus, the overall space complexity is `O(m)`.

Hence, the time complexity is `O(n)` and the space complexity is `O(m)`.