2344. Minimum Deletions to Make Array Divisible Math Sorting Heap (Priority Queue) Hard Array Number Theory

Problem Description

This problem presents us with two arrays of positive integers, nums and numsDivide. The goal is to perform the minimum number of deletions in nums to ensure that the smallest number in nums divides all numbers in numsDivide. If no element in nums can be the divisor for every element in numsDivide, the function should return -1.

Leetcode Link

The division rule here is that an integer x divides another integer y if the remainder when y is divided by x is zero, denoted as y % x == 0. To solve this problem, you need to consider two main steps:

1. Identify the smallest number in nums that can be a divisor for all elements in numsDivide. 2. Find the minimum number of deletions in nums required to make this number the smallest in nums.

Intuition

(GCD) of numsDivide. All elements of numsDivide must be divisible by this GCD, so our potential divisor in nums must also divide the GCD of numsDivide. Therefore, the smallest number in nums that also divides the GCD of numsDivide will serve as the required divisor.

Next, we search for the smallest number in nums that can divide this GCD, which can be done using a generator expression within the min function. If no such number exists in nums (when min returns the default=0), we cannot perform the desired operation, therefore we return -1.

To begin, since we want a number from nums that divides all elements in numsDivide, we need to find the Greatest Common Divisor

If a divisor is found, we count the number of elements in nums that are smaller than this divisor since any such elements must be

With that in mind, the first step is to calculate the GCD of all elements in numsDivide using a built-in function.

deleted for the divisor to be the smallest element in nums. The count of these elements gives us the minimum number of deletions needed. The summing using a generator expression in the return statement calculates this count and returns it. Solution Approach

The implementation of the solution for this problem follows a straightforward approach, with the primary focus being the calculation of the Greatest Common Divisor (GCD) and the minimization of deletions. Here's the step-by-step breakdown of the solution:

we can pass all elements of numsDivide to this function to find their collective GCD. 1 x = gcd(*numsDivide)

The gcd function from the Python standard library can compute GCD of two numbers. Leveraging the unpacking operator *,

 The condition x % v == 0 ensures we only consider those elements that properly divide the GCD x. The min function is used to find the smallest of such elements.

Calculate the GCD of elements in numsDivide array:

2. Identify the smallest number in nums that divides the GCD:

We use a generator expression to iterate over all the values v in nums.

 The default=0 is used to handle the scenario where no such divisibility is possible, which will lead to the min function returning 0. 1 y = min((v for v in nums if x % v == 0), default=0)

If we found a divisor y, then we count the number of elements in nums that are less than y. These elements would prevent y

from being the smallest element if not deleted. This count is computed with the sum of a generator expression.

3. Count and return the minimum deletions:

 \circ For every element v in nums, if v < y, it adds 1 to the sum. 1 return sum(v < y for v in nums) 4. Handle the case where no suitable divisor is found:

∘ If no element in nums can divide the GCD, which means y is 0, we cannot perform the operation, so we return -1.

generator expressions for memory-efficient iteration, and conditional logic to directly return the minimum number of deletions or -1 if the problem conditions cannot be met.

Let's consider an example to illustrate the solution approach. Suppose we have the following arrays:

In summary, the solution leverages mathematical properties (divisibility and GCD), along with Python's built-in gcd function,

Calculating the GCD of Elements in numsDivide First, we find the GCD of all elements in the numsDivide array: The GCD of 24 and 48 can be found as:

Identifying the Smallest Number in nums Dividing the GCD

have led us to return -1.

Python Solution

from math import gcd

class Solution:

Java Solution

1 class Solution {

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C++ Solution

using namespace std;

int gcdValue = 0;

class Solution {

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from typing import List

GCD(24, 48) = 24

1 if y else -1

Example Walkthrough

nums = [4, 3, 6]

numsDivide = [24, 48]

All numbers [4, 3, 6] in nums can divide 24, but we need the smallest one; hence we find the min which is 3.

This means any divisor in nums needs to divide 24 to be a valid divisor for all numbers in numsDivide.

This means no numbers from nums need to be deleted for the smallest number within it to divide all numbers in numsDivide.

Now, we look for the smallest number in nums that can divide the GCD 24:

For 3, we check 24 % 3 and find it's also True as 24 is divisible by 3.

For 6, we check 24 % 6 and see that this is True as well.

For 4, we check if 24 % 4 == 0, which is True.

Counting and Returning Minimum Deletions

Therefore, the minimum number of deletions is 0.

Handling the Case of No Appropriate Divisor Found

Using the aforementioned steps, the solution successfully calculates that no deletions are needed from nums so that the smallest number in nums can divide all elements in numsDivide.

Since we did find the number 3 as a suitable divisor, we did not encounter the scenario of the min function returning 0, which would

To make 3 the smallest number in nums, we must delete all numbers that are smaller than 3. In nums, there are no such numbers.

common_divisor = gcd(*numsDivide) # Find the smallest element in nums that is a divisor of the GCD 9 # If there is no such element, the default value will be 0 10

if min_divisible == 0:

return -1

int operations = 0;

return operations;

private int gcd(int a, int b) {

for (int value : nums) {

operations++;

if (value < minDivisibleValue) {</pre>

// Return the number of operations required.

// If b is zero, a is the gcd by definition.

return b == 0 ? a : gcd(b, a % b);

1 #include <vector> // Required to include vector

for (int& value : numsDivide) {

for (int& value : nums) {

return -1;

int operationsCount = 0;

for (int& value : nums) {

2 #include <algorithm> // Required for std::min function

int minOperations(vector<int>& nums, vector<int>& numsDivide) {

operationsCount += value < minValueGreaterThanAll;

return operationsCount; // Returning the minimum number of operations.

// Calculating GCD of all elements in numsDivide

gcdValue = gcd(gcdValue, value);

if (gcdValue % value == 0) {

if (minValueGreaterThanAll == 1 << 30) {</pre>

// Function to calculate the gcd of two numbers

1 // Importing necessary functionalities from external libraries

// Helper method to compute the gcd of two numbers using the Euclidean algorithm.

// Initializing gcdValue with 0 to calculate GCD of all values in numsDivide

// Setting the minimum possible value greater than all elements in nums

// Finding the smallest number in nums that divides the gcdValue without remainder

// If minValueGreaterThanAll is not changed, it means no such number is found. Return -1.

// Counting the number of operations to remove numbers smaller than minValueGreaterThanAll

minValueGreaterThanAll = min(minValueGreaterThanAll, value);

int minValueGreaterThanAll = 1 << 30; // Large value as upper limit.</pre>

def minOperations(self, nums: List[int], numsDivide: List[int]) -> int:

Calculate the greatest common divisor (GCD) of all elements in numsDivide

If the smallest element is not found, return -1 as it's not possible

Calculate the number of operations needed by counting elements in nums

to make all numsDivide elements divisible by any number in nums

that are smaller than the smallest valid divisor (min_divisible)

operations = sum(value < min_divisible for value in nums)

// This method finds the minimum number of operations required

// to make every number in numsDivide divisible by some number

// in nums by removing the smallest numbers in nums.

public int minOperations(int[] nums, int[] numsDivide) {

min_divisible = min((value for value in nums if common_divisor % value == 0), default=0)

21 22 # Return the count of operations needed 23 return operations 24

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// Initialize the greatest common divisor (gcd) of all numbers in numsDivide.
           int gcdValue = 0;
            for (int value : numsDivide) {
               gcdValue = gcd(gcdValue, value);
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           // Set an initial high value to find the minimum value in nums that divides the gcd without remainder.
           int minDivisibleValue = Integer.MAX_VALUE;
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            for (int value : nums) {
               if (gcdValue % value == 0) {
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                   minDivisibleValue = Math.min(minDivisibleValue, value);
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           // If no number was found, return -1 as it's not possible to satisfy the condition with any deletions.
           if (minDivisibleValue == Integer.MAX_VALUE) {
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                return -1;
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// Count the numbers of operations (number of elements smaller than the minDivisibleValue to be deleted).

int gcd(int a, int b) { 37 38 return b == 0 ? a : gcd(b, a % b); 39 40 }; 41

import { min } from 'lodash'; // Function to calculate the greatest common divisor (GCD) of two numbers

Typescript Solution

function calculateGCD(a: number, b: number): number { return b === 0 ? a : calculateGCD(b, a % b); // Function to find the minimum number of operations required function minOperations(nums: number[], numsDivide: number[]): number { // Initialize gcdValue with 0 to calculate GCD of all values in numsDivide let gcdValue: number = 0; 12 13 // Calculate GCD of all elements in numsDivide 14 for (const value of numsDivide) { 15 gcdValue = calculateGCD(gcdValue, value); 16 17 18 19 // Initialize minValueGreaterThanAll with a large number as an upper limit. let minValueGreaterThanAll: number = 1 << 30;</pre> 20 21 22 // Find the smallest number in nums that divides the gcdValue without a remainder for (const value of nums) { 23 24 if (gcdValue % value === 0) { 25 minValueGreaterThanAll = Math.min(minValueGreaterThanAll, value); 26 27 28 29 // If minValueGreaterThanAll is not changed, no such number is found; return -1. if (minValueGreaterThanAll === 1 << 30) {</pre> 30 return -1; 31 32 33 // Count the number of operations to remove numbers smaller than minValueGreaterThanAll 34 35 let operationsCount: number = 0; for (const value of nums) { 36 37 operationsCount += value < minValueGreaterThanAll ? 1 : 0; 38 39 // Return the minimum number of operations. 40 return operationsCount; 43

The given Python code aims to find the minimum number of operations to delete elements from nums so that the greatest common

divisor (GCD) of numsDivide can divide all elements in the modified nums list. It finds the GCD of the elements of numsDivide, then

1. gcd(*numsDivide): The function computes the GCD of all elements in numsDivide. The time complexity of the gcd function for two

2. min((v for v in nums if x % v == 0), default=0): This generator expression iterates over all elements v in nums and checks if

v divides x without remainder. In the worst case, it will iterate through the entire nums list, resulting in a time complexity of O(n).

numbers is O(log(min(a, b))), where a and b are the two numbers. The GCD function will be called for every element in

finds the minimum element y in nums that is a divisor of the GCD, and counts elements in nums less than y.

Time Complexity Let n be the length of the nums list and m be the length of the numsDivide list.

Time and Space Complexity

numsDivide beyond the first two. Therefore, the time complexity for this portion can be considered 0(m * log (A)), where A is the average of the numsDivide list.

3. sum(v < y for v in nums): This expression iterates over the list nums, and for each element, it increments the sum if the element is less than y. This operation also has a time complexity of O(n) because it goes through all n elements.

constant factor, we can't simplify it further. However, typically m and log(A) are much smaller than n in practical scenarios, such that we can consider it as O(n) for practical purposes. Space Complexity

1. gcd(*numsDivide): The gcd function itself uses 0(1) additional space as it only requires a constant space for the computation.

Combining these, the overall worst-case time complexity is: 0(m * log (A) + 2n). Since m * log (A) and n are not related by a

2. min((v for v in nums if x % v == 0), default=0): The generator expression used here does not store intermediate results

Let's analyze the space complexity of the algorithm:

and computes the minimum on the fly. Therefore, it also uses 0(1) space. 3. sum(v < y for v in nums): Similar to the min function call, this sum leverages a generator expression and does not store

intermediate results, so it uses 0(1) additional space. The space complexity of the entire algorithm is 0(1) since all additional space used is constant and does not scale with the size of

the input nums or numsDivide.