### 784. Letter Case Permutation **String** Medium **Bit Manipulation Backtracking**

## **Problem Description**

In this problem, we're given a string s consisting of alphabetical characters. We have the freedom to change each of these characters individually to either lowercase or uppercase, which can lead to various permutations of the string with different cases for each letter. The task is to generate all possible strings with these different case transformations and return them as a list in any order.

This is a typical backtracking problem, as we'll consider each character and explore the possibilities of both keeping it as it is or

An example to illustrate this: for the string "a1b2", the output will be ["a1b2", "a1B2", "A1b2", "A1B2"].

changing its case, accumulating all different strings that can be formed by these choices.

## To achieve our solution, we can apply a method known as depth-first search (DFS), which is a type of backtracking algorithm. The

Intuition

DFS approach will help us traverse through all possible combinations of uppercase and lowercase transformations of the characters within the string. Here's the intuition breakdown for solving this problem: 1. Start from the first character: We begin the process with the first character of the string.

- 2. Recursive exploration: For each character, we have two choices (provided it's an alphabetical character and not a digit):
- Keep the current character as is and proceed to the next one. Change the current character's case (from lowercase to uppercase or vice versa) and move to the next one.
  - added to the list of results.
- 3. Base case: If we reach the end of the string (i.e., index i is equal to the string length), we've completed a permutation and it's
- other option (changing the case). 5. Result accumulation: As we hit the base case at different recursive call levels, we collect all permutations of the string.

4. Backtracking: After exploring one option (like keeping the character as is) for the current position, we backtrack to explore the

- This recursive approach works because it explores all possible combinations by trying each option at each step. The use of the bitwise XOR operation ^ 32 is a clever trick to toggle the case of an alphabetical character since converting between lowercase to
- uppercase (or vice versa) in ASCII entails flipping the 6th bit.

**Solution Approach** The provided solution uses a Depth-First Search (DFS) algorithm along with a recursive helper function named dfs. This function is defined within the scope of the letterCasePermutation method.

## Here's a step-by-step walk-through of the solution code:

decision to keep the current character as is.

current character's case is toggled.

DFS. 2. An empty list ans is initialized which will eventually contain all the possible permutations of the string.

1. A new list t is created from the original string s which is going to hold the characters that we are currently exploring through

are currently exploring.

4. In the body of the dfs function, the base case checks if the index i is greater than or equal to the length of s. If it is, it means we've constructed a valid permutation of string s in the list t and we append this permutation to ans. 5. If the base case condition is not met, we first call dfs(i + 1) without altering the current character. This recurses on the

3. The dfs function defined inside the letterCasePermutation takes a single argument i, which is the index of the character in t we

6. Next, if the current character is alphabetic (t[i].isalpha()), we toggle its case using t[i] = chr(ord(t[i]) ^ 32). The ord function gets the ASCII value of the character, ^ 32 toggles the 6th bit which changes the case, and chr converts the ASCII

value back to the character. After changing the case, we call dfs(i + 1) again, exploring the decision tree path where the

- 7. By recursively calling dfs with 'unchanged' and 'changed' states of each character, all combinations are eventually visited, and the resulting strings appended to ans. The DFS here is a recursive pattern that explores each possibility and undoes (backtracks) that choice before exploring the next
- possibility. The data structure used is a basic Python list which conveniently allows us to both change individual elements in place and join them into strings when we need to add a permutation to the results.

1. We start by setting up an empty list ans that will store our final permutations and a list t from the string s, which is "0a1". List t will hold the characters that we are currently exploring through the DFS algorithm. 2. Since the first character '0' is not an alphabetical character, we only have one option for it; we keep it as is. So, we move on to

add "OA1" to ans.

regarding the case of alphabetic characters.

two different string permutations: "0a1" and "0A1".

return

dfs(index + 1)

dfs(index + 1)

generatePermutations(index + 1);

charArray[index] ^= ' ';

if (Character.isLetter(charArray[index])) {

generatePermutations(index + 1);

def letterCasePermutation(self, s: str) -> List[str]:

permutations.append(''.join(current\_string))

# Recursive case: move to the next character without changing the case

# Continue the search with the flipped case character

current\_string[index] = chr(ord(current\_string[index]) ^ 32)

// Recursively call the method to handle the next character without modification

// If the current character is alphabetic, toggle its case and proceed with recursion

// IMPORTANT: revert the character back to its original case after the recursive call

# Revert the change for backtracking purposes

the next character.

**Example Walkthrough** 

3. The next character is 'a'. Here, we have two choices:

Let's illustrate the solution approach with a small example using the string "0a1".

- Keep 'a' as it is and proceed to the next character, which will be '1'. This sequence is "0a1". Since '1' is not alphabetical, we keep it as is and add "0a1" to ans. ∘ Toggle the case of 'a' to 'A' and then proceed to the next character, '1'. This sequence is "0A1". Again, we keep '1' as it is and
- 4. At this point, the dfs function has recursively explored and returned from both branches for character 'a', and the two permutations of the string are saved in ans, which now contains ["0a1", "0A1"].

5. Since there are no more characters to explore, the recursion terminates, and the ans list now holds all the possible permutations

And that's the end of the example. The original list "0a1" only had one alphabetical character that could be toggled, which resulted in

Python Solution

# Helper function for depth-first search def dfs(index): # Base case: if the current index is equal to the length of the string if index == len(s): # Append the current permutation to the answer list

### # If the current character is alphabetic, we can change its case 14 if current\_string[index].isalpha(): 15 # Flip the case: if the current character is uppercase, make it lowercase and vice versa 16 current\_string[index] = chr(ord(current\_string[index]) ^ 32) 17

9

10

11

12

13

18

19

20

21

19

20

21

22

23

24

25

26

27

28

29

30

31

32

34

class Solution:

```
22
23
           # Convert the input string to a list, making it mutable
24
           current_string = list(s)
           # Initialize a list to store all possible permutations
25
26
           permutations = []
27
           # Start the depth-first search from the first character
28
           dfs(0)
29
           # Return the computed permutations
30
           return permutations
31
32 # Example of usage:
33 # sol = Solution()
34 # result = sol.letterCasePermutation("a1b2")
35 # print(result) # Output: ["a1b2", "a1B2", "A1b2", "A1B2"]
Java Solution
   class Solution {
       private List<String> permutations = new ArrayList<>(); // List to hold the string permutations
       private char[] charArray; // Character array to facilitate permutation generation
       // Public method to generate letter case permutations for a given string
       public List<String> letterCasePermutation(String s) {
           charArray = s.toCharArray(); // Convert string to character array for modification
           generatePermutations(0); // Start recursion from the first character
           return permutations; // Return all generated permutations
10
11
       // Helper method to recursively generate permutations
12
13
       private void generatePermutations(int index) {
           // Base case: If the end of the array is reached, add the current permutation to the list
14
15
           if (index >= charArray.length) {
16
               permutations.add(new String(charArray));
17
               return;
18
```

// Toggle the case: lowercase to uppercase or vice versa using XOR operation with the space character

charArray[index] ^= ' '; // This step ensures the original structure is intact for future permutations

// If the character is not alphabet, it is left as—is and the recursion takes care of other characters

# C++ Solution

1 #include <vector>

2 #include <string>

#include <functional>

```
class Solution {
 6 public:
       // Function to generate all permutations of a string where each letter can be lowercase or uppercase
       std::vector<std::string> letterCasePermutation(std::string str) {
           // Resultant vector to store all permutations
10
           std::vector<std::string> permutations;
11
           // Utility lambda function to perform a Depth-First Search (DFS) for all possible letter case combinations
12
           std::function<void(int)> dfs = [&](int index) {
13
               // Base case: if we reach the end of the string, add the current permutation to the results
14
               if (index >= str.size()) {
                    permutations.emplace_back(str);
16
17
                   return;
18
19
20
               // Recursive case: continue with the next character without changing the current one
               dfs(index + 1);
21
22
23
               // Only if the current character is alphabetical (either uppercase or lowercase)
24
               // we toggle its case and recursively continue
               if (isalpha(str[index])) {
25
26
                   // Toggle the case of the current character: lowercase to uppercase or vice versa
                   // XOR with 32 takes advantage of the fact that the ASCII values of upper and lower case
28
                   // letters differ by exactly 32
29
                   str[index] ^= 32;
30
31
                   // Recursive call with the case of the current character toggled
                   dfs(index + 1);
32
33
34
                   // Optional: Toggle the case back if you want to use the original string elsewhere
35
                   // after this function call. If str is not used after this, you can omit this step.
36
                   // str[index] ^= 32;
37
38
           };
39
40
           // Start DFS from index 0
           dfs(0);
41
42
43
           // Return all generated permutations
44
           return permutations;
45
46 };
47
Typescript Solution
```

### 15 16 17 18

9

1 // Function that generates all possible permutations of a string

const results: string[] = []; // Stores the resulting permutations

3 // It uses Depth-First Search (DFS) to explore all variations.

2 // with letters toggled between uppercase and lowercase.

function letterCasePermutation(s: string): string[] {

// Helper function to perform DFS

```
const dfs = (index: number) => {
10
           if (index === length) {
11
                                              // If the end of the string is reached,
12
               results.push(charArray.join('')); // join the characters to form a permutation and add to results.
13
               return;
14
           dfs(index + 1);
                                                // Recursive call with the next character (no change)
           // Check if the current character is a letter and can change case
           if (isLetter(charArray[index])) {
               toggleCase(charArray, index); // Toggle the case of the character at the current index
19
20
               dfs(index + 1);
                                                // Recursive call with the toggled character
21
22
       };
23
       // Function to check if a character is a letter (could be replaced with regex or other methods)
24
25
       function isLetter(c: string): boolean {
           return (c >= 'A' && c <= 'Z') || (c >= 'a' && c <= 'z');
26
27
28
29
       // Function that toggles the case of a letter by using bitwise XOR with the space character (32)
30
       function toggleCase(arr: string[], index: number): void {
           arr[index] = String.fromCharCode(arr[index].charCodeAt(0) ^ 32);
31
32
33
34
       dfs(0); // Start the DFS from the first character
35
       return results; // Return the array of permutations
36 }
37
Time and Space Complexity
The given Python code generates all possible permutations of a string s where the permutation can include lowercase and
uppercase characters. A depth-first search (DFS) algorithm is employed to explore all possibilities.
Time Complexity:
To analyze the time complexity, let us consider the number of permutations possible for a string with n characters. Each character
can either remain unchanged or change its case if it's an alphabetic character. For each alphabetic character, there are 2 possibilities
```

# alphabetic characters in the string, there would be 2<sup>n</sup> different permutations.

**Space Complexity:** 

stack and the output list.

The DFS function is recursively called twice for each alphabetic character (once without changing the case, once with the case changed), and it's called once for each non-alphabetic character. Thus, the time complexity of this process can be represented as: 0(2<sup>m</sup> \* n), where n is the length of the string and m is the number of alphabetic characters in the string as each permutation includes building a string of length n.

(uppercase or lowercase), while non-alphabetic characters have only 1 possibility (as they don't have case). If we assume there are m

The space complexity includes the space needed for the recursion call stack as well as the space for storing all the permutations. The maximum depth of the recursive call stack would be n, as that's the deepest the DFS would go. The space needed for ans will be

 $0(2^m * n)$  as we store  $2^m$  permutations, each of length n. However, one might consider the space used for each layer of the recursion separately from the space used to store the results

since the latter is part of the problem's output. If we only consider the space complexity for the recursion (excluding the space for

Combining both the space for the recursion and the output, the space complexity can be represented as:

the output), then the space complexity would be O(n).

 $0(2^m * n + n)$ , which simplifies to  $0(2^m * n)$  when considering  $2^m$  to be significantly larger than n. In conclusion, the time complexity is  $0(2^m * n)$  and the space complexity is  $0(2^m * n)$  when accounting for both the recursion