Problem Description

their respective levels of quietness. Each person in the group is identified by a unique number from 0 to n - 1. An array richer is provided, where each element richer[i] is a pair [a, b] that indicates person a is wealthier than person b. Then

In this LeetCode problem, we are tasked with finding the least quiet person among a group of people, given their relative wealth and

there is an array quiet where quiet[i] represents the level of quietness for person i, with a smaller value indicating a quieter person.

wealthy or wealthier than person x. Here, 'as wealthy or wealthier' means they are either directly richer than person x, or richer than someone who is richer than person x, and so on.

Our goal is to return an array answer where answer[x] is the index y of the person who is the least quiet among all those who are as

To solve this problem, we use a Depth-First Search (DFS) approach. The key observation in this problem is that the relationships

list.

Intuition

least quiet person who is as rich or richer than a person x, we are actually looking for the least quiet person in the subgraph reachable from node x. The solution involves the following steps: 1. Convert the richer array into a graph data structure to allow for efficient traversal. This graph is represented using an adjacency

between people's wealth create a directed graph without cycles because the richer relations are logically consistent. In this graph,

nodes represent people, and an edge from node a to node b indicates that a is wealthier than b. Therefore, when we look for the

2. Initialize an array answer with all elements set to -1, which will help us track the least quiet person as we traverse the graph as

- well as serve as a cache to avoid repeated calculations. 3. Perform a DFS from each person. During the search, if we have already computed the result for a node (person), we return immediately to save time.
- 4. When we visit a node, we compare its quietness with that of the already recorded least quiet person (if any). If the current node is quieter, we update the record in the answer array.
- 5. We recursively visit all richer people than the current person and apply the same logic. 6. After finishing the dfs, the answer array will contain the desired results based on the computed least quiet person reachable from each node.
- The recursive DFS and caching technique (also known as memoization) helps us avoid re-examining nodes multiple times, leading to
- efficient calculation of the answer.

The solution uses Depth-First Search (DFS) to traverse the graph built from the richer array, leveraging recursion to navigate through the nodes (people) and explore their wealth relationships. Here is a breakdown of how the implementation works:

A graph g is initialized as a default dictionary of lists, which will hold the adjacency list representation of our directed graph. For

every pair [a, b] in richer, we add a to the adjacency list of b because a is richer than b. In this analogy, b is the starting node, and a is reachable from b.

DFS operation.

Solution Approach

 We create an array ans initialized with -1s to hold the index of the quietest person richer or equally wealthy as the person at index i. This array also helps in caching the results of previous calculations for each person to avoid repeating the expensive

i, and there's no need to repeat the computation. • For the current person i, the dfs function sets ans [i] to i itself initially, assuming the person is the quietest among all people wealthier than or as wealthy as them.

A dfs function is defined, taking a person index i as its argument. The purpose of this function is to find and record the quietest

person that can be reached from the person i. If ans [i] is not -1, it means that we have already computed the result for person

each of them. After exploring each wealthier person j, it compares the quietness of the current quietest person ans [i] with the quietest person in the subgraph starting from j (ans[j]). If a quieter person is found (quiet[ans[j]] < quiet[ans[i]]), ans[i] is updated to refer to that person.

• The main loop at the end iterates through all the people, calling dfs(i) for each person i. This step ensures that even if some

people are not directly richer than others, they are still explored through the recursive DFS calls.

The function then iterates through all people that are richer than person i (all j in g[i]) and performs a recursive DFS call for

- The use of DFS in this solution is a powerful choice, as it allows us to explore the complete subset of people that are more prosperous than a given person, caching results along the way to prevent redundant calculations. The use of memoization with the ans array helps to cut down the execution time significantly, as the DFS will only compute the quietest person for each subgraph once. After the DFS for all people has been performed, the ans array contains the quietest person among all richer people for each person in the group, effectively solving the problem.
- Example Walkthrough Let's illustrate the solution approach with a small example. Assume we have the following input:

• richer = [[1, 0], [2, 1], [3, 1]]: This means person 1 is richer than person 0, person 2 is richer than person 1, and person 3

is richer than person 1. • quiet = [3, 2, 5, 4]: This indicates the level of quietness for each person. Person 0 has quietness 3, person 1 has 2, person 2 has 5 and person 3 has 4. Now, let's walk through the steps:

2. Initialize an array ans = [-1, -1, -1, -1] to indicate that no answers have been computed yet.

 Start with person 0. Since no one is richer, ans [0] will be 0 (the person itself). DFS on person 1: Recursively check for richer people and update ans [1]. Person 0 is not richer, so ans [1] will be 1.

def loudAndRich(self, richer, quiet):

if answer[index] != -1:

graph = defaultdict(list)

for (var r : richer) {

dfs(i);

private void dfs(int i) {

return;

if (answer[i] != -1) {

for (int i = 0; i < peopleCount; ++i) {</pre>

answer[i] = answer[j];

return answer; // Return the filled answer array

n = len(quiet)

answer = [-1] * n

def dfs(index):

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Here, g[i] contains the people that are less wealthy than i.

Convert richer into a graph data structure as an adjacency list:

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○ DFS on person 2: The richer people are persons 1 and 0. We check both, and since person 1 is quieter (2<5), we update</p>
  ans [2] with 1.

    DFS on person 3: The richer people are persons 1 and 0. Person 3 is quieter than person 1, so ans [3] is set to 3.
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4 q[3] = [1]

Python Solution

has been effectively found using our DFS approach and is represented in the ans array.

Depth-first search to update the answer for each person.

Otherwise, initialize this person's answer as themselves.

if quiet[answer[neighbor]] < quiet[answer[index]]:</pre>

answer[index] = answer[neighbor]

Build the graph given the richer relationship.

graph[poorer_person].append(richer_person)

Initialize the answer list with -1 for all persons.

this.quietness = quiet; // Set the quietness array

// Build the graph's adjacency list from the richer array

// Recursive Depth-First Search function that populates the answer array

// Set the default quietest person to the person themselves

if (quietness[answer[j]] < quietness[answer[i]]) {</pre>

function loudAndRich(richer: number[][], quiet: number[]): number[] {

// Construct the graph based on the richer relationships

for (const [richerPerson, lessRichPerson] of richer) {

graph[lessRichPerson].push(richerPerson);

// Graph representation, where g[x] contains all people richer than person x

const graph: number[][] = new Array(numPeople).fill(0).map(() => []);

for richer_person, poorer_person in richer:

If this person's answer is already calculated, return.

4. After performing DFS for each person, ans is updated with the least quiet richer people: ans = [0, 1, 1, 3].

To conclude, given our richer and quiet inputs, the least quiet person who is as wealthy or wealthier than person x for x in 0 to n-1

3. Perform DFS for each person to find the least quiet person that is as wealthy or wealthier than them:

from collections import defaultdict class Solution:

This method finds the quietest person in the group or among their richer acquaintances.

If the neighbor has found someone quieter, update this person's answer.

peopleCount = quiet.length; // Set the number of people based on the quiet array length

answer = new int[peopleCount]; // Initialize the answer array with peopleCount elements

Arrays.fill(answer, -1); // Initially fill the answer array with -1 indicating not found

Arrays.setAll(graph, k -> new ArrayList<>()); // Initialize each vertex's adjacency list

graph[r[1]].add(r[0]); // r[1] person is poorer so we add r[0] as an outgoing edge from r[1]

// If the quietest person for j is quieter than the current quietest person for i, update it

graph = new List[peopleCount]; // Initialize the graph with peopleCount vertices

// Perform DFS starting from every vertex to find the answer for each person

// If the quietest person for i is already found, terminate the DFS

answer[index] = index for neighbor in graph[index]: # Visit all richer neighbors. dfs(neighbor)

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           # Perform dfs for each person.
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           for i in range(n):
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               dfs(i)
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           # Return the completed answer list.
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           return answer
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Java Solution
    class Solution {
         private List<Integer>[] graph; // Graph adjacency list
         private int peopleCount; // Number of people in the problem
         private int[] quietness; // Array representing the quietness of each person
         private int[] answer; // Array representing the answer of the quietest person who is richer or as rich
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         // The main function that takes richer relations and quietness indices, and returns an array of answers
         public int[] loudAndRich(int[][] richer, int[] quiet) {
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36 answer[i] = i;37 38 // Explore all richer people coming from node i 39 for (int j : graph[i]) { dfs(j); // DFS on the richer person j 40

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 47 }
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C++ Solution
1 #include <vector>
2 #include <functional>
  using std::vector;
   class Solution {
   public:
       vector<int> loudAndRich(vector<vector<int>>& richer, vector<int>& quiet) {
           int numPeople = quiet.size(); // The number of people
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           vector<vector<int>> graph(numPeople); // Graph to hold richer relationships
           // Build the graph with directed edges from richer to poorer
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           for (const auto& pair: richer) {
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               graph[pair[1]].push_back(pair[0]);
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           // Answer vector with an initial value of -1 for each element
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           vector<int> answer(numPeople, -1);
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           // Define a lambda function for Depth First Search
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           std::function<void(int)> dfs = [&](int node) {
               // If we have already computed the answer for this node, return
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               if (answer[node] != -1) {
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                   return;
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               // Initially, assume the person is the quietest
               answer[node] = node;
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               // Explore all the richer people
25
               for (int neighbor : graph[node]) {
                   dfs(neighbor); // depth-first search the neighbor
26
                   // If the neighbor has a quieter answer, update this node's answer
                   if (quiet[answer[neighbor]] < quiet[answer[node]]) {</pre>
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                       answer[node] = answer[neighbor];
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           };
33
           // Perform a DFS from each person to find the quietest person they are richer than
34
           for (int i = 0; i < numPeople; ++i) {</pre>
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               dfs(i);
36
           // Return the final answer array
38
           return answer;
40 };
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Typescript Solution
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// Total number of people

const numPeople = quiet.length;

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// Filled initially with -1 to indicate that we haven't computed the answer for that person yet
       const answer: number[] = new Array(numPeople).fill(-1);
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       // Depth-First Search (DFS) function to determine the quietest person in the subgraph
       const dfs = (person: number) => {
18
           // If we've already computed the answer for this person, return the answer array
19
           if (answer[person] !== -1) {
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               return answer;
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24
           // The quietest person initially being themselves
25
           answer[person] = person;
26
27
           // Explore all the richer people
28
           for (const richerPerson of graph[person]) {
               dfs(richerPerson);
               // If we find a quieter richer person, update the answer for the current person
31
               if (quiet[answer[richerPerson]] < quiet[answer[person]]) {</pre>
                   answer[person] = answer[richerPerson];
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       };
37
       // Perform DFS for each person to find the quietest person they know directly or indirectly
38
       for (let i = 0; i < numPeople; ++i) {
           dfs(i);
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       // Return the array containing the quietest person for each index
43
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       return answer;
45 }
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Time and Space Complexity
Time Complexity
The time complexity of this code is primarily determined by the depth-first search recursion implemented through the dfs() function.
Since each node in the graph g represents a person and each edge in the graph represents the "richer" relation, the depth-first
search will visit each node and each edge at most once. Given that there are n nodes (individuals) and m edges (relations), the
traversal has a complexity of O(n+m).
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However, notice that the DFS process is performed for each node in the for i in range(n): loop, and during each DFS execution, it processes only the nodes that have not been previously processed (if ans[i] != -1: return). Once a node has been processed, it will not be processed again in any subsequent DFS calls. Thus, each node triggers the DFS call at most once, and each edge is considered once across all DFS calls. Therefore, despite the outer loop suggesting 0(n^2) behavior at first glance, the function still achieves O(n+m) because each node and edge is effectively processed only a single time.

The space complexity of the code is O(n) due to multiple factors: ans array of size n.

Space Complexity

- g dictionary, which in the worst case could have up to n keys with a single value in the list (if the graph is a star shape where one person is richer than all n-1 others), so it uses O(n) space.
- The recursion stack for the DFS could, in the worst case, go as deep as n if the graph is a long chain, contributing another O(n) to the space complexity.

The space complexity, in this case, is determined primarily by the system's recursion stack depth and the additional data structures

(ans and g), which together yield O(n).