1016. Binary String With Substrings Representing 1 To N

String Medium

Problem Description

given positive integer n as substrings. A substring is a sequence of characters that occur in order without any interruptions within a string. For example, if s = "0110" and n = 3, we need to check if the binary representations of 1 ("1"), 2 ("10"), and 3 ("11") are all present as substrings in s. To solve the problem, we need to generate the binary representation of each number from 1 to n and verify if each representation

The problem requires us to determine if a given binary string s contains all the binary representations of numbers from 1 to a

is a substring of s.

The solution involves a few key observations and steps:

Intuition

Binary Length: The binary representation of a number grows in length when the number doubles. Therefore, as we approach

representation as a string is a substring of s (bin(i)[2:] in s).

numbers, but as mentioned earlier, this condition may be arbitrary.

n, more significant numbers would have longer binary strings, and if they are not found in s, we can determine the answer is false without checking smaller numbers. **Efficient Checking:** We start checking from n and go down to n//2. The reasoning is that every binary string that would

represent a number from 1 to n//2 will also be a substring of a string representing a number from n//2 to n. For example, "10"

- for 2 is contained within "110" for 6. **Performance Boundaries:** Since the binary length grows with the number size, the code includes a quick exit condition when n is greater than 1000, possibly to avoid performance issues with extremely large strings. However, this condition seems
- arbitrary and depends on constraints not mentioned in the problem description. It may not be necessary if the input string s is always large enough to potentially contain all representations. All-encompassing Check: To verify if all binary representations are in s, a Python built-in function all() is used, which checks for the truthiness of all elements in an iterable. In this case, a generator expression checks if each binary
- **Solution Approach** The solution approach utilizes a simple and direct method for checking the presence of binary substrings within the given string

s. Below are the components and steps of the implementation using the provided Python code:

the '0b' prefix with [2:]. Then we check whether this binary representation is a substring of s.

Function Signature:

we need to check the binary representations. The function returns a Boolean value. **Early Return Condition:**

o if n > 1000: return False: The code immediately returns False if n is more than 1000, implying a performance optimization for large

o def queryString(self, s: str, n: int) -> bool: This is the function signature where s is the input string and n is the integer until which

Main Checking Loop:

- ∘ return all(bin(i)[2:] in s for i in range(n, n // 2, -1)): Here the algorithm employs Python's built-in function all() which tests if all elements in an iterable are true. The iterable, in this case, is a generator expression that goes through the range of integers from n to n // 2 (integer division by 2) in descending order.
- **Binary Conversion and Substring Check:**
 - **Data Structures:** • No additional data structures are used in this solution. The input string s and integer n are directly utilized within the algorithm. **Algorithmic Patterns:**

The algorithm does not use complex patterns or advanced data structures. It relies on Python's expressive syntax and built-in functions to

o bin(i)[2:] in s: For each i in the specified range, the built-in bin() function generates its binary representation as a string and strips off

- perform substring checking efficiently.
- The loop iterates through only half of the specified range (from n to n // 2) in reverse order because if i can be represented within s as a binary string, all smaller numbers can also be substrings of those representations or will have occurred earlier within
- the binary sequence. This approach takes advantage of the fact that binary representations of numbers are nested within those

given range within the string s succinctly and efficiently.

of larger numbers, providing a significant performance improvement over checking every single number individually from 1 to n. In summary, the code leverages Python's capabilities to check for the presence of each binary representation of numbers in the

Example Walkthrough To illustrate the solution, let's consider an example where s = "01101101" and n = 4. We would like to determine if the binary representations of numbers from 1 to 4, which are "1" (1), "10" (2), "11" (3), and "100" (4), appear as substrings in s.

Check for Early Return: The first check in our solution is to see if n is greater than 1000. In this case, n = 4, so we do not

Initialize the Main Loop: Starting with i = 4 and iterating down to i = 2 (half of n), we check each binary representation to

return early and proceed.

see if it's a substring in s.

illustration purposes.

"100" was not found, all() will return False.

necessary binary representations and utilizing Python's built-in tools.

def query_string(self, string: str, upper_bound: int) -> bool:

Steps:

Binary Conversion: ∘ For i = 4, we convert 4 to binary, getting "100". Check if "100" is in s. It is not, so we could already return False. However, continue for

∘ For i = 3, convert 3 to binary, yielding "11". Check if "11" is a substring of s, which it is, as s is "01101101".

∘ For i = 2, convert 2 to binary to get "10". We then check if "10" is part of s, and indeed, it is present.

If the upper bound (n) is greater than 1000, return false as per the given logic.

return all(bin(i)[2:] in string for i in range(upper_bound, upper_bound // 2, -1))

* Checks if all binary representations of numbers from 1 to n are substrings of the string s.

* @param s The string in which binary representations are to be searched.

// from 1 to n are substrings of the input string s.

// value representable with 10 binary digits.

// Early exit condition if n is greater than the maximum

// Loop through numbers starting from n to half of n

// since the bit representation of numbers less than n/2

// will always be contained in the bit representation of

// Remove leading zeroes from the binary string.

if (s.find(binaryString) == std::string::npos) {

* Checks if a binary string represents all numbers from 1 to n.

* @param {string} binaryString - The string consisting of binary digits.

* @param {number} maxNumber - The maximum number to check up to (inclusive).

* @returns {boolean} - Returns true if all numbers from 1 to maxNumber are

// If not found, return false immediately.

// Convert the number to binary (bitset) and then to string.

std::string binaryString = std::bitset<32>(i).to_string();

binaryString.erase(0, binaryString.find_first_not_of('0'));

// Check if the resulting binary string is a substring of s.

// All required binary representations are substrings of s. Return true.

bool queryString(std::string s, int n) {

// numbers between n/2 and n.

return false;

for (int i = n; i > n / 2; --i) {

if (n > 1023) {

return true;

return false;

checking.

Python

class Solution:

Example usage:

class Solution {

/**

sol = Solution()

Conclusion: Since not all binary representations from 1 to 4 were found as substrings in s ("100" was missing), the all()

function will evaluate to False. Therefore, the given string s does not contain all binary representations as substrings.

This step-by-step walkthrough demonstrates the simplicity and efficiency of the approach by focusing on checking only the

No Additional Data Structures: We have not used additional data structures outside the string s and the numbers we're

Evaluate with all() Function: Use the all() function to verify whether all these checks (i = 4 to i = 2) are True. Since

- Solution Implementation
 - return False # 'all' checks whether all elements in the iterable are True. # The loop starts from 'upper_bound' and goes till 'upper_bound // 2' (integer division by 2), moving backwards. # 'bin(i)[2:]' converts the integer 'i' to its binary representation in string format, stripping off the '0b' prefix.

'in string' checks if each binary representation is a substring of the input string 'string'.

result = sol.query_string("0110", 3) # print(result) # This would print 'True' if all binary numbers from n to n//2 are substrings of "0110" Java

if upper_bound > 1000:

```
* @param n The maximum value up to which binary representations should be checked.
  * @return True if all binary representations from 1 to n are found in s, otherwise False.
  */
  public boolean queryString(String s, int n) {
   // If n is greater than the maximum allowed value (as binary representation within the string),
    // which is 2^10 - 1 = 1023 for a 10-bit binary number, return false as the condition can't be met.
    if (n > 1023) {
      return false;
    // Iterate from n down to n / 2 since every number smaller than n/2 is a binary substring of a number
    // that is larger than n/2 (because the binary representation of a number is also a suffix of the
    // binary representation of its double).
    // If a substring representing the binary of i is not found within string s, return false.
    for (int i = n; i > n / 2; i--) {
      if (!s.contains(Integer.toBinaryString(i))) {
        return false;
    // Return true if all required binary substrings have been found.
    return true;
C++
#include <bitset>
#include <string>
class Solution {
public:
    // Function to check if all binary representations of numbers
```

```
};
TypeScript
```

/**

```
* represented in the binaryString, otherwise false.
   */
  function queryString(binaryString: string, maxNumber: number): boolean {
      // Check if the maxNumber is larger than the largest number that can be represented
      // with a 10-bit binary number, which is 1023.
      if (maxNumber > 1023) {
          return false;
      // Iterate from the maxNumber down to half of it, since every number from 1 to n / 2
      // will be a substring of the binary representation of numbers from n / 2 + 1 to n.
      for (let currentNum = maxNumber; currentNum > maxNumber / 2; --currentNum) {
          // Convert the current number to its binary string representation.
          const binaryRepresentation = currentNum.toString(2);
          // Check if the current binary representation is a substring of binaryString.
          // If it is not found, the method returns -1, therefore, return false.
          if (binaryString.indexOf(binaryRepresentation) === -1) {
              return false;
      // If all necessary binary representations are found in the string, return true.
      return true;
class Solution:
   def query_string(self, string: str, upper_bound: int) -> bool:
       # If the upper bound (n) is greater than 1000, return false as per the given logic.
        if upper_bound > 1000:
            return False
       # 'all' checks whether all elements in the iterable are True.
       # The loop starts from 'upper_bound' and goes till 'upper_bound // 2' (integer division by 2), moving backwards.
       # 'bin(i)[2:]' converts the integer 'i' to its binary representation in string format, stripping off the '0b' prefix.
       # 'in string' checks if each binary representation is a substring of the input string 'string'.
        return all(bin(i)[2:] in string for i in range(upper bound, upper bound // 2, -1))
# Example usage:
# sol = Solution()
# result = sol.query_string("0110", 3)
# print(result) # This would print 'True' if all binary numbers from n to n//2 are substrings of "0110"
```

The time complexity of the provided code can be determined by analyzing the two main operations: the all function and the string containment check in.

Time and Space Complexity

Time Complexity: • The all function iterates over the range from n to n // 2, decreasing by 1 each time. This results in approximately n/2 iterations. • For each iteration, the string containment check in is performed, which, in the worst case, has a complexity of O(m), where m is the length of the

string s.

- Therefore, the overall worst-case time complexity is 0(m * n/2), as the containment check is performed n/2 times.
- **Space Complexity:** No extra space is used for data storage that scales with the input size; only a fixed number of variables are used. • The binary representation string created for each number i is temporary and its length is at most 0(log(n)).

Hence, the space complexity is 0(1), which means it is constant since the space required does not grow with the input size n or the string length m.