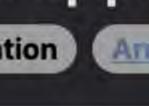


Medium Greedy

Bit Manipulation







Matrix

Problem Description

perform as many "moves" as you want. A move consists of picking any row or column and flipping all the bits in it; that is, all 0s are changed to 1s and vice versa. For example, if you have a row [1, 0, 1] and you perform a move, this row will become [0, 1, 0].

You are presented with a binary matrix grid, which is a 2D array containing os and 1s. Your task is to maximize the "score" of this

matrix. The score is calculated by summing up all the rows considered as binary numbers. In order to raise the score, you can

The primary goal is to find the highest score possible after performing an optimal sequence of moves.

Intuition

The key observation to solve this problem is to realize that the most significant bit in a binary number has the highest value, so it

we flip the entire row. The next step is to consider each column, starting from the second one since the first column should already have all 1s after the initial step. At each column, we can maximize the score by making sure that the number of 1s is greater than or equal to the number of 0s. If there are more 0s than 1s, we flip the entire column. This is because flipping a column doesn't change the leftmost 1s that

should always be set to 1 to maximize the number. Therefore, the first step is to ensure all rows start with a 1. If a row starts with a 0,

we have set in the first step but increases the number of 1s in the current column, therefore increasing the overall score. By applying these two steps, first row-wise, then column-wise, we ensure that each bit contributes the maximum possible value to the score of the matrix.

Here's the reasoning for the solution: 1. Flip the rows if the first bit is 0 (outer loop over rows). 2. For each column, count the number of 1s. If the number is less than half of the total rows, flip the column (inner loop over

columns). 3. Calculate the score by adding the value of each column's bits to the total score.

Here's the breakdown of how the code implements the solution:

- In the provided code, grid[i][j] = 1 is used to flip the bits (using the XOR operator). max(cnt, m cnt) * (1 << (n j 1)) is the calculation of the contribution of each column to the score, choosing to flip the column or not depending on which option gives more 1s, and then multiplying by the value of the bit position, which decreases as we move right.
- Solution Approach

contribution to the score mathematically, without modifying the matrix.

The solution takes a greedy approach to maximizing the score of the binary matrix by making sure that the most significant bit of every row is set to 1 and then ensuring that each column contains as many 1s as possible.

1. The first loop iterates through each row in the binary matrix grid. The size of the matrix is determined by m rows and n columns.

Example Walkthrough

3 0 1

toggles each element grid[i][j] ^= 1. This is done using the XOR operator ^, which will flip a 0 to 1 and vice versa.

3. The outer loop with the variable j goes through each column. The inner loop counts the number of 1s in the current column.

Instead of flipping each bit when necessary, we're just counting the number of 1s because we can compute the column

2. Inside this loop, we check if the first element of the row (grid[i][0]) is 0. If so, we flip the entire row using a nested loop which

4. For each column, we calculate the maximum possible value it can contribute to the score based on the current state of bits in that column. This is computed by max(cnt, m - cnt). We take the larger value between the number of 1s (cnt) and the number

of 0s (m - cnt), considering that if the 0s were in the majority, a column flip would change them to 1s.

the position. In a binary number, the leftmost bit is the most significant; hence, the value is computed by $1 \ll (n - j - 1)$, which is equivalent to raising 2 to the power of the column's index from the right (0-based). For example, if the column is the second from the right in a 4-column grid, its value is $2^{(4-2-1)} = 2^{(1)} = 2$.

5. The column's contribution to the overall score is then computed by multiplying this maximum number with the binary value of

- 7. Once all columns have been processed, the variable ans holds the highest possible score, which is returned. The algorithm efficiently calculates the maximum score possible without needing to actually perform the flips visually or record the state of the matrix after each flip, thanks to mathematical binary operations and the properties of binary numbers.
- Let's take a simple example and walk through the solution approach to understand it better.

Consider the binary matrix, grid, represented by the following 2D array:

Row 1 starts with 0, so we flip it: 0 1 becomes 1 0.

6. This contribution is added to ans for each column to build up the total score.

The matrix has 3 rows (m = 3) and 2 columns (n = 2). We want to maximize the "score" of this matrix through flips.

 Row 3 also starts with 0, we flip it: 0 1 becomes 1 0. After this step, our grid looks like this:

2. Now, we need to maximize 1s in each column. We note that the first column already has all 1s because of the initial row flips. So

Step by Step Solution:

There is only 1 1 in the second column.

Total score = 6 + 2

result = 0

return result

Iterate over columns

for j in range(num_cols):

// Loop through each column.

int matrixScore(vector<vector<int>>& A) {

// Number of columns in the matrix

for (int row = 0; row < num_rows; ++row) {</pre>

// Iterate through columns to maximize the score

for (int col = 0; col < num_cols; ++col) {</pre>

col_count += A[row][col];

for (int col = 0; col < num_cols; ++col) {</pre>

int col_count = 0; // Count of 1s in the current column

// Determine the value to add to the score for this column

// We take the larger number between 'col_count' and 'num_rows - col_count'

// Count the number of 1s in the current column

for (int row = 0; row < num_rows; ++row) {</pre>

// Number of rows in the matrix

int num_rows = A.size();

int total_score = 0;

int num_cols = A[0].size();

if $(A[row][0] == 0) {$

return ans;

C++ Solution

1 class Solution {

2 public:

for (int col = 0; col < numCols; ++col) {</pre>

colCount += grid[row][col];

for (int row = 0; row < numRows; ++row) {

// Add to the column count if the bit is 1.

Python Solution

class Solution:

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3. Count the number of 1s in the second column:

this column flipped for maximization purposes.

4. Calculate the contribution of each column to the total score:

5. The total score is then the sum of the contributions from step 4:

Total score = Score from column 1 + Score from column 2

we consider the second column.

1. Make sure that all rows start with 1:

• The first column, having all 1s, contributes $2^{(n-1-0)} = 2^{(2-1-0)} = 2^1 = 2$ for each row, totaling 2 * 3 = 6. The second column, we consider flipped (for scoring purposes), so it effectively has 2 1s, and each contributes 2^(n-2-0) = $2^{(2-2-0)} = 2^{0} = 1$ to the score. The total from this column will be 1 * 2 = 2.

We want the majority of the bits in each column to be 1. Since there is only 1 '1' and 2 '0's in the second column, we'll consider

Total score = 8

def matrixScore(self, grid: List[List[int]]) -> int:

for j in range(num_cols):

Initialize the variable to store the result

Count the number of 1s in the current column

max_value = max(num_ones, num_rows - num_ones)

result $+= \max_{value} * (1 << (num_{cols} - j - 1))$

Return the maximized score after considering all rows and columns

Add the value of the column to the result

num_ones = sum(grid[i][j] for i in range(num_rows))

grid[i][j] ^= 1

- The highest possible score for the given matrix after the optimal sequence of moves is 8.
 - num_rows, num_cols = len(grid), len(grid[0]) # Flip the rows where the first element is 0 for i in range(num_rows): if grid[i][0] == 0:

XOR operation to flip the bits (0 becomes 1, and 1 becomes 0)

Maximize the column value by flipping if necessary (the majority should be 1s)

Use the maximum of the number of 1s or the number of 0s in the column

The value is determined by the number of 1s times the value of the bit

position (1 << $(num_cols - j - 1)$) is the bit value of the current column

Get the number of rows (m) and columns (n) in the grid

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Java Solution
   class Solution {
       public int matrixScore(int[][] grid) {
           // Get the number of rows (m) and columns (n) in the grid.
           int numRows = grid.length, numCols = grid[0].length;
           // Step 1: Flip the rows where the first element is 0.
            for (int row = 0; row < numRows; ++row) {</pre>
               // Check if the first column of the current row is 0.
               if (grid[row][0] == 0) {
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                   // Flip the entire row.
                   for (int col = 0; col < numCols; ++col) {</pre>
                        grid[row][col] ^= 1; // Bitwise XOR operation flips the bit.
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           // Step 2: Calculate the final score after maximizing the columns.
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           int ans = 0; // This variable stores the final score.
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// Maximize the column by choosing the maximum between colCount and (numRows - colCount).

// Use bit shifting (1 << (numCols - col - 1)) to represent the value of the column.

ans += Math.max(colCount, numRows - colCount) * (1 << (numCols - col - 1));

// Return the final score of the binary matrix after row and column manipulations.

// Flip the rows where the first element is 0 to maximize the leading digit

A[row][col] ^= 1; // Xor with 1 will flip 0s to 1s and vice versa

int colCount = 0; // Count the number of 1s in the current column.

30 // to maximize the column value (since either all 1s or all 0s since we can flip) 31 int max_col_value = std::max(col_count, num_rows - col_count); 32 // The value of a set bit in the answer is equal to 2^(num_cols - col - 1) 33

total_score += max_col_value * (1 << (num_cols - col - 1)); 34 35 36 return total_score; // Return the maximized score after performing the operations 37 38 }; 39 Typescript Solution function matrixScore(grid: number[][]): number { const rows = grid.length; // number of rows in the grid const cols = grid[0].length; // number of columns in the grid // Step 1: Toggle rows to ensure the first column has all 1s for (let row = 0; row < rows; ++row) { if (grid[row][0] === 0) { // If the first cell is 0, toggle the entire row for (let col = 0; col < cols; ++col) { grid[row][col] ^= 1; // XOR with 1 will toggle the bit 10 11 12 13 14 15 let score = 0; // Initialize the total score 16 // Step 2: Maximize each column by toggling if necessary 17 for (let col = 0; col < cols; ++col) { 18 let countOnes = 0; // Count of ones in the current column 20 for (let row = 0; row < rows; ++row) {</pre> // Count how many 1s are there in the current column 21 countOnes += grid[row][col]; 23 // Choose the max between countOnes and the number of 0s (which is rows - countOnes) 25 score += Math.max(countOnes, rows - countOnes) * (1 << (cols - col - 1));</pre> 26 27

Time and Space Complexity **Time Complexity**

return score; // Return the total score

counting the number of 1's in each column to maximize the row score.

The first loop, which toggles the cells if the leftmost bit is 0, traverses all cells in the grid and performs a constant-time XOR operation. This double loop runs in O(m * n) time, where m is the number of rows and n is the number of columns.

Space Complexity

space complexity.

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 The second loop calculates the count of 1's in each column and determines the maximum score by considering the current and the inverse value count. This also runs in 0(m * n) time since it involves iterating over each column for all rows.

The time complexity of the given solution involves iterating over each cell of the grid to potentially toggle its value, followed by

- The two operations above are consecutive, resulting in a total time complexity of 0(m * n) + 0(m * n), which simplifies to 0(m * n)because constant factors are dropped.
- No extra space is used for processing besides a few variables for iteration (i, j) and storing intermediate results (such as cnt and ans). These use a constant amount of space irrespective of the input size.

• Since the grid is modified in place, and no additional data structures are used to store intermediate results, the space complexity

The space complexity of the algorithm is determined by any additional space that we use relative to the input size:

remains constant. Given the fixed number of variables with space independent of the input size, the space complexity is 0(1), which signifies constant