444. Sequence Reconstruction

Description

You are given an integer array nums of length n where nums is a permutation of the integers in the range [1, n]. You are also given a 2D integer array sequences where sequences[i] is a subsequence of nums.

Check if nums is the shortest possible and the only **supersequence**. The shortest **supersequence** is a sequence **with the shortest length** and has all sequences[i] as subsequences. There could be multiple valid **supersequences** for the given array sequences.

- For example, for sequences = [[1,2],[1,3]], there are two shortest supersequences, [1,2,3] and [1,3,2].
- While for sequences = [[1,2],[1,3],[1,2,3]], the only shortest **supersequence** possible is [1,2,3]. [1,2,3,4] is a possible supersequence but not the shortest.

Return true if nums is the only shortest supersequence for sequences, or false otherwise.

A **subsequence** is a sequence that can be derived from another sequence by deleting some or no elements without changing the order of the remaining elements.

Example 1:

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Input: nums = [1,2,3], sequences = [[1,2],[1,3]]
Output: false
Explanation: There are two possible supersequences: [1,2,3] and [1,3,2].
The sequence [1,2] is a subsequence of both: [ 1 , 2 ,3] and [ 1 ,3, 2 ].
The sequence [1,3] is a subsequence of both: [ 1 ,2, 3 ] and [ 1 ,3 ,2 ].
Since nums is not the only shortest supersequence, we return false.
```

Example 2:

```
Input: nums = [1,2,3], sequences = [[1,2]]
Output: false
Explanation: The shortest possible supersequence is [1,2].
The sequence [1,2] is a subsequence of it: [ 1 , 2 ].
Since nums is not the shortest supersequence, we return false.
```

Example 3:

```
Input: nums = [1,2,3], sequences = [[1,2],[1,3],[2,3]]
Output: true
Explanation: The shortest possible supersequence is [1,2,3].
The sequence [1,2] is a subsequence of it: [ 1 , 2 ,3].
The sequence [1,3] is a subsequence of it: [ 1 ,2, 3 ].
The sequence [2,3] is a subsequence of it: [1, 2 , 3 ].
Since nums is the only shortest supersequence, we return true.
```

Constraints:

- n == nums.length
- 1 <= n <= 10 ⁴
- nums is a permutation of all the integers in the range [1, n].
- 1 <= sequences.length <= 10 4
- 1 <= sequences[i].length <= 10 4
- 1 <= sum(sequences[i].length) <= 10 ⁵
- 1 <= sequences[i][j] <= n
- All the arrays of sequences are unique.
- sequences[i] is a subsequence of nums.