# 955. Delete Columns to Make Sorted II

Medium Greedy Array String

# **Problem Description**

deleting characters at certain indices across all the strings with the aim of making the resulting array of strings sorted in lexicographic (alphabetical) order. Lexicographic order means that the strings should appear as if they were sorted in a dictionary, i.e.,  $strs[0] \ll strs[1] \ll strs[2] \ll ... \ll strs[n - 1]$ . We can select any number of indices to delete, and these deletions will occur on every string in the array. Our goal is to find the

In this problem, we are given an array strs containing n strings, where each string is of the same length. Our task involves

minimum number of indices that we need to delete to achieve the lexicographically sorted array. The problem asks us to return the smallest possible size of the set of deletion indices.

#### To solve this problem, the intuition is to iteratively check each character column (index) across all strings and decide whether that column should be deleted or kept to maintain the lexicographic order. If a column is found where a string appears before

Intuition

must be deleted. Otherwise, if the current column does not break the order, we may keep it. However, simply looking at the current column in isolation is not sufficient. We must also remember if any prior columns have already established a strict lexicographic order between any two adjacent strings. If that's the case, these strings do not impact the decision for the current column because they are already ordered properly due to previous columns. We keep track of these

another string lexicographically but has a greater character at the current index, then this column breaks the required order and

again. The solution follows these steps: 1. Iterate over each column (index) of the strings. 2. Check if the character at the current column for each string maintains the lexicographic order with the next string. 3. If the order is violated, increase the deletion count and skip to the next column.

decisions using the cut boolean array, which marks pairs of strings that are already sorted and do not need to be considered

6. Return the number of deletions that were necessary to sort the array lexicographically.

5. Continue until all the indices have been processed.

ensure the strings are in lexicographic order.

Solution Approach

order and thus we must "cut" this column by incrementing res by 1 and continue to the next column.

The implementation of the solution uses a simple but effective approach to decide which columns (indices) need to be deleted to

4. If the order is maintained, mark any string pairs that are now sorted due to this column.

Here is how the approach is implemented:

If no lexicographic violation is detected, no increment to res will happen.

strings lexicographically, is returned as the final answer.

**Initiation**: We begin by initializing the necessary variables:

## len stores the length of the array A.

 wordLen stores the length of each string within the array. res initialized to 0 will hold the count of indices required to be deleted. cut is a boolean array, initialized to false, that keeps track of which pairs of strings do not need further comparisons because they are

Column-Wise Check: We inspect each column using the outer loop which iterates over j, the index for the character position within the strings.

already in correct order according to prior columns.

after it (i and i+1). The main conditions checked in this loop are as follows: ∘ If the cut[i] is false (meaning the strings at index i and i+1 have not been marked as already sorted) and the character at the column j

for string i is greater than the character at the same column for string i+1, it implies that the current column violates the lexicographic

Mark Sorted Pairs: If a column does not lead to an increment of res, then for each string, excluding the last one, we check if

Algorithm Complexity: This approach would have a time complexity of O(N \* W) where N is the number of strings and W is

the width or length of each string. Space complexity is O(N) due to the additional array cut used to keep track of sorted

Row-Wise Comparison: For each column, a nested loop goes through each string and compares it with the string that comes

- the character at the current column is less than the character in the same column of the next string. If it is, this means these two strings are already sorted with respect to each other for the current column, hence we set cut[i] to true. Result: After inspecting all columns, the value res, which is the count of the indices that needed to be deleted to sort the
- pairs. This algorithm uses a greedy approach, attempting at each step to make a local optimal decision (deleting a column if necessary),

which leads to a globally optimal solution—the minimum number of columns deleted to achieve the lexicographically sorted array

**Example Walkthrough** 

Let's consider a small example to illustrate the solution approach. Suppose we have the following array of strings, where n = 4.

Step 1: We initialize our variables. len = 3, wordLen = 3, res = 0, and cut is an array of false values of size len = 1 which is 2 in this case, so cut = [false, false]. Step 2 & 3: We start checking each column, starting with the first column (index 0).

• Comparing the first characters c, d, and g of each string, we see that they are already in the lexicographic order, so we don't increment res.

cut [0] is false and 'a' < 'b', we need to delete this column to maintain the order. We increment res by 1 and we do not need to check further

Step 6: Having inspected all columns, we get res = 1 (since we had to delete the second column). This is the minimum number

Additionally, we don't mark any pairs as sorted because c < d and d < g, indicating that the order cannot be affected by subsequent

Here our goal is to ensure this array is sorted lexicographically with the minimum number of column deletions.

### Step 4: Move to the second column (index 1). • Comparing the second characters b, a, h of each string, we notice the lexicographic order is violated (a should not come after b). Since

characters.

**Python** 

class Solution:

of strings.

strs = ["cba", "daf", "ghi"]

Step 5: Inspect the third column (index 2). • Comparing the third characters a, f, i of each string, they are in correct lexicographic order, and no further action is needed.

Thus, our function would return 1 for this example. **Solution Implementation** 

# Check if the input list is None or has only one string; if so, no deletion is needed.

break # Skip to the next column without updating the sorted status.

else: # This else belongs to the for, it is executed if the loop is not 'break'-ed.

# Update sorted status if this column does not need to be deleted.

# If the characters are in ascending order, mark as sorted.

// Check if input array is null or has only one string, if so no deletion needed.

# Initialize the number of strings and the length of the first string.

# Initialize a list to keep track of which strings are already sorted.

# Attempt to update sorted status for this column.

for i in range(num of strings - 1):

if strings[i][i] < strings[i + 1][j]:</pre>

sorted\_status[i] = True

# If the current string is not sorted with the next, and the current character # is greater than the next string's character, we need to delete this column. if not sorted status[i] and strings[i][j] > strings[i + 1][j]: # Increment the deletion counter.

deletions += 1

public int minDeletionSize(String[] strings) {

int minDeletionSize(std::vector<std::string>& strings) {

// Initialize the length variables and the result counter.

// Inner loop to compare characters in the current column.

if (!sorted[i] && strings[i][j] > strings[i + 1][j]) {

deletions++; // Increment the deletion count

if (strings.empty() || strings.size() <= 1) {</pre>

int numOfStrings = strings.size():

// Iterate through each column.

int stringLength = strings[0].size();

// Vector to keep track of sorted strings.

for (int j = 0; j < stringLength; ++j) {</pre>

// Return the total number of deletions.

std::vector<bool> sorted(num0fStrings, false);

for (int i = 0;  $i < numOfStrings - 1; ++i) {$ 

for (int i = 0; i < numOfStrings - 1; ++i) {

if (strings[i][j] < strings[i + 1][j]) {</pre>

sorted[i] = true; // Mark as sorted

// Check if input vector is empty or has only one string, if so no deletion is needed.

// than the character in the next string, we need to delete this column.

// Update the sorted vector for strings that are already sorted in this column.

break; // Skip to the next column without updating the sorted vector.

// If the current and the next string are not sorted and the current character is greater

# Iterate over each column by index.

def min deletion size(self, strings):

num of strings = len(strings)

string length = len(strings[0])

for i in range(string length):

return 0

deletions = 0

if strings is None or len(strings) <= 1:</pre>

sorted\_status = [False] \* num\_of\_strings

for i in range(num of strings - 1):

values in this column, so we continue to the next column.

of deletions required to sort the strings lexicographically.

#### # Return the total number of columns that need to be deleted. return deletions Java

class Solution {

class Solution {

return 0;

int deletions = 0;

public:

```
if (strings == null || strings.length <= 1) {</pre>
            return 0;
        // Initialize the length variables and the result counter.
        int numOfStrings = strings.length;
        int stringLength = strings[0].length();
        int deletions = 0;
        // Boolean array to keep track of sorted strings.
        boolean[] sorted = new boolean[numOfStrings];
        // Iterate through each column.
        for (int j = 0; j < stringLength; j++) {</pre>
            // Inner loop to compare characters in the current column.
            for (int i = 0; i < num0fStrings - 1; i++) {
                // If the current and the next string are not sorted and the current character is greater
                // than the next, we need to delete this column.
                if (!sorted[i] && strings[i].charAt(j) > strings[i + 1].charAt(j)) {
                    deletions += 1:
                    continue; // Skip to the next column without updating the sorted array.
            // Update the sorted array for characters that are already sorted.
            for (int i = 0; i < numOfStrings - 1; i++) {
                if (strings[i].charAt(j) < strings[i + 1].charAt(j)) {</pre>
                    sorted[i] = true;
        // Return the total number of deletions.
        return deletions;
C++
#include <vector>
#include <string>
```

```
return deletions;
};
TypeScript
// Initialize a variable to hold the minimum number of deletions.
let minDeletions: number = 0;
// Function to calculate the minimum number of deletions required to make each column non-decreasing.
function minDeletionSize(strings: string[]): number {
    // Check if input array is null or has only one string; if so, no deletion needed.
    if (!strings || strings.length <= 1) {</pre>
        return 0;
    // Initialize the length variables.
    const numOfStrings: number = strings.length;
    const stringLength: number = strings[0].length;
    // Boolean array to keep track of which strings are sorted.
    const sorted: boolean[] = new Array(numOfStrings).fill(false);
    // Iterate through each column.
    for (let j = 0; j < stringLength; j++) {</pre>
        // Reset the deletion flag for the current column.
        let needToDeleteColumn: boolean = false;
        // Compare characters in the current column.
        for (let i = 0; i < num0fStrings - 1; i++) {
            // If current and next strings are not sorted, and current char is greater than next,
            // mark the column for deletion.
            if (!sorted[i] && strings[i].charAt(j) > strings[i + 1].charAt(j)) {
                needToDeleteColumn = true;
                break; // Break out of the loop since we've decided to delete this column.
        // If we need to delete the column, increment the deletion count and continue to the next column.
        if (needToDeleteColumn) {
            minDeletions++;
            continue;
        // Update the sorted array for rows that are sorted with the current column considered.
        for (let i = 0: i < numOfStrings - 1: i++) {
            if (strings[i].charAt(j) < strings[i + 1].charAt(j)) {</pre>
                // Mark this string as sorted up to the current column.
                sorted[i] = true;
    // Return the total number of deletions required.
    return minDeletions;
class Solution:
    def min deletion size(self, strings):
        # Check if the input list is None or has only one string; if so, no deletion is needed.
        if strings is None or len(strings) <= 1:</pre>
            return 0
        # Initialize the number of strings and the length of the first string.
        num of strings = len(strings)
        string length = len(strings[0])
        deletions = 0
        # Initialize a list to keep track of which strings are already sorted.
        sorted_status = [False] * num_of_strings
        # Iterate over each column by index.
        for j in range(string length):
            # Attempt to update sorted status for this column.
            for i in range(num of strings - 1):
                # If the current string is not sorted with the next, and the current character
                # is greater than the next string's character, we need to delete this column.
                if not sorted status[i] and strings[i][j] > strings[i + 1][j]:
                    # Increment the deletion counter.
```

## return deletions Time and Space Complexity

deletions += 1

for i in range(num of strings - 1):

if strings[i][j] < strings[i + 1][j]:</pre>

# Return the total number of columns that need to be deleted.

sorted\_status[i] = True

range for updating the cut array. Therefore, each character is visited once in the check and once in the update step for each inner loop, which leads to a total of O(wordLen \* len) operations where wordLen is the length of the strings and len is the total number of strings. The space complexity of the code is mostly dependent on the additional boolean array cut used to store the information on which strings do not need to be compared further. The cut array has a size equivalent to the number of strings len, so the space complexity is O(len).

The time complexity of the given code can be analyzed based on the nested for-loops. The outer loop runs for j from 0 to

wordLen, and for each iteration of j, the inner loop runs for i from 0 to len - 1. There's also another nested loop with the same

Overall, the time complexity of the algorithm is 0(wordLen \* len), and the space complexity is 0(len).

break # Skip to the next column without updating the sorted status.

else: # This else belongs to the for, it is executed if the loop is not 'break'-ed.

# Update sorted status if this column does not need to be deleted.

# If the characters are in ascending order, mark as sorted.