2271. Maximum White Tiles Covered by a Carpet Medium **Binary Search** Greedy Prefix Sum Sorting Array

Leetcode Link

Problem Description

In this problem, we are provided with a list of intervals, where each interval represents a set of consecutive white tiles on the floor. Each interval is given as a pair, with the first number representing the starting position of the sequence of white tiles, and the second number representing the ending position of this sequence. Additionally, we have been given the length of a carpet (carpetLen) that we can use to cover a continuous stretch of white tiles. Our

goal is to strategically place this carpet such that it covers the maximum number of white tiles possible. To summarize, we must find the optimal position for our carpet to maximize the number of covered white tiles and return this

The intuition behind the solution is to use a sliding window algorithm. A sliding window is a subset of data that moves through a set

Intuition

of elements, which is useful when you have an array or list and you want to consider a subarray/sublist of a specific length (in our case, the length is defined by carpetLen).

maximum number.

1. First, we sort the intervals based on their starting positions. This allows us to process the tiles sequentially and determine the carpets' positions more efficiently. 2. We initialize two pointers, i and j, to traverse the intervals. The pointer i denotes the beginning of the window while j is used to

- find the extent to which the carpet can cover tiles (tiles fully covered by the carpet without exceeding its length). 3. We iterate over the tiles with pointer i. For every new position of i, we proceed with pointer j to extend the window's reach this includes adding on the number of tiles that are within the range that the carpet could potentially cover.
- 4. Since the carpet can partially cover an interval, the check if j < n and li + carpetLen > tiles[j][0] is used to add the remaining portion of white tiles not completely covered by the interval at j, up to the length of the carpet.
- 5. We store the maximum number of covered tiles in a variable ans, updating it with the maximum between its current value and the number of covered tiles (including partial coverage on the last interval if necessary).

coverage from our current sum s and continue to find the optimal number of covered tiles until all intervals have been

sorted tile intervals and accounting for both fully and partially covered intervals.

considered. This process allows us to effectively find the maximum white tiles that the carpet can cover by shifting our sliding window across the

6. As we move our window (incrementing the pointer i), we subtract the number of tiles that are no longer included in the carpet's

Solution Approach The solution provided employs a sliding window technique, coupled with sorting and careful addition and subtraction of the tiles within each range. Let's break down the implementation step-by-step:

1. Sorting Intervals: The code first sorts the tiles list by the starting position of each interval. This sequential order is crucial for

the sliding window technique to work efficiently because it ensures that we're always looking at contiguous sections of floor

2. Initializing Variables: The function initializes n as the length of the tiles list, s as the current count of white tiles covered by the

1 tiles.sort()

1 n = len(tiles)

tiles.

carpet (initially set to 0), and as the answer to be returned (also starting at 0), and j as the second pointer that will stretch the window to its limits.

2 s = ans = j = 03. Sliding Window: The primary loop iterates over the sorted intervals using the index and the interval itself ((i, (li, ri))): It uses a while loop to extend pointer j as far as possible without the carpet length (carpetLen) being exceeded,

accumulating the count of white tiles that any position of the carpet could cover in s.

carpet would partially cover the next set of tiles and updates the answer accordingly.

1 while j < n and tiles[j][1] - li + 1 <= carpetLen:</pre>

s += tiles[j][1] - tiles[j][0] + 1

1 if j < n and li + carpetLen > tiles[j][0]:

be covered once i moves to i + 1.

1 s -= ri - li + 1

memory usage.

2 CarpetLen: 4

white tiles as we can.

Example Walkthrough

1 Intervals: [(1, 2), (3, 5), (7, 10)]

- ans = max(ans, s + li + carpetLen tiles[j][0]) 3 else: ans = max(ans, s)

For partially covered ranges (where the carpet covers only a part of the j-th range), an if condition checks whether the

4. Returning the Result: After the loop terminates, the highest number of covered white tiles recorded in ans during the traversal is returned as the solution. 1 return ans

This approach aggregates the number of tiles that can be covered by the carpet while tracking partially covered ranges correctly.

coverage. The sorting step ensures that the sliding window does not move back and forth, which would be inefficient, and instead

incrementally adjusts by moving both i and j forward through the tiles. This yields an optimal solution in terms of execution time and

The sliding window advances across the floor, effectively examining each possible placement of the carpet to find the maximum

After considering the current position of i, the code needs to subtract from s the number of tiles in the range of i that won't

Let's illustrate the solution approach with a small example: Suppose we have a list of intervals given by white tiles on the floor and a carpet length of 4 tiles:

Following the steps outlined in the solution: 1. Sorting Intervals: We sort the intervals by their starting positions, although our example list is already sorted. 2. Initializing Variables: We set:

The intervals represent sequences of consecutive white tiles. Our carpet can cover 4 consecutive tiles, and we aim to cover as many

 Carpet cannot entirely cover the next interval (7, 10) without exceeding its length, so ans = max(ans, s) = 4. • Before moving to the next element, subtract the number of tiles in range (1, 2) as it won't be covered in the next iteration.

 \circ n = 3 (length of the intervals list)

s = 0 (current sum of covered tiles)

j = 0 (second pointer to extend the window)

Carpet can cover (1, 2) entirely, s = 2 now.

Carpet can cover (3, 5) entirely, s = 3 now.

■ ans = max(ans, s) = 5 for this iteration.

1 return ans # returns 5 as the maximum number of covered tiles

carpet can cover a maximum of 5 white tiles when placed starting from tile 3 to tile 6.

Sort the tile intervals by the starting point of each tile.

Extending the carpet to cover as many tiles as possible.

covered += tiles[pointer][1] - tiles[pointer][0] + 1

max_covered = max(max_covered, covered)

public int maximumWhiteTiles(int[][] tiles, int carpetLen) {

Arrays.sort(tiles, (a, b) -> a[0] - b[0]);

int totalCovered = 0, maxTilesCovered = 0;

int numberOfTiles = tiles.length;

++rightIndex;

++right;

} else {

return maxCovered;

// Sort the tiles array based on the left edge of each tile.

// Use two pointers to navigate through the tiles array.

while pointer < num_tiles and tiles[pointer][1] - start + 1 <= carpet_length:</pre>

Add the number of tiles covered by the current part of the carpet.

Else the carpet lies within a contiguous stretch of white tiles.

Subtract the number of tiles covered by the current start tile

as we move the start to the next tile in the subsequent iteration.

Return the maximum number of white tiles that can be covered by the carpet.

// Initialize the total number of tiles and the answer (maximum tiles covered).

for (int leftIndex = 0, rightIndex = 0; leftIndex < numberOfTiles; ++leftIndex) {</pre>

totalCovered += tiles[rightIndex][1] - tiles[rightIndex][0] + 1;

// Slide the right pointer to the right while the carpet can cover the new tile entirely.

while (rightIndex < numberOfTiles && tiles[rightIndex][1] - tiles[leftIndex][0] + 1 <= carpetLen) {</pre>

3. Sliding Window: We iterate through each interval.

so s += 2, resulting in s = 4.

ans = 0 (answer to return, the maximum number of tiles that can be covered)

So, s -= 2. \circ For i = 1: interval (3, 5). We see if the carpet can cover interval (3, 5) entirely and reach into the next one.

∘ For i = 0: interval (1, 2). We see if the carpet can cover interval (1, 2) entirely and reach into the next one.

■ Then we check if it can cover (3, 5) without exceeding the length. It can cover until 4 (since the carpet is 4 tiles long),

4. Returning the Result: The loop has terminated, and the highest number of covered white tiles recorded is ans = 5, which is the solution. We return ans.

■ It can partially cover (7, 10), up to 7, so we add 2 to s for the partial coverage, resulting in s = 5.

We don't perform a subtraction step here, as there are no more intervals for the carpet to slide over.

Python Solution class Solution: def maximumWhiteTiles(self, tiles: List[List[int]], carpet_length: int) -> int:

This example demonstrates that by sorting the intervals and using a sliding window approach, we can efficiently determine that the

Move the pointer to see if more tiles can be covered with the remaining carpet length. 16 17 pointer += 1 18 # Checking whether extending the carpet partially covers a tile. 19 if pointer < num_tiles and start + carpet_length > tiles[pointer][0]: 20 # Update the max_covered by adding partial coverage of the next tile.

max_covered = max(max_covered, covered + start + carpet_length - tiles[pointer][0])

```
import java.util.Arrays;
class Solution {
    // Method to calculate the maximum number of white tiles that can be covered by the carpet.
```

Java Solution

tiles.sort()

else:

return max_covered

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35 };

Initialize useful variables.

covered = max_covered = pointer = 0

Iterate through the sorted tiles.

covered -= end - start + 1

for index, (start, end) in enumerate(tiles):

num_tiles = len(tiles)

```
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21
               // Check if the carpet partially covers the next tile.
               if (rightIndex < numberOfTiles && tiles[leftIndex][0] + carpetLen > tiles[rightIndex][0]) {
22
23
                    maxTilesCovered = Math.max(maxTilesCovered, totalCovered + tiles[leftIndex][0] + carpetLen - tiles[rightIndex][0]);
                } else {
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25
                   // Carpet does not reach the next tile, just consider current total coverage.
26
                    maxTilesCovered = Math.max(maxTilesCovered, totalCovered);
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28
               // Move the left pointer to the right and decrease the total coverage accordingly.
29
                totalCovered -= (tiles[leftIndex][1] - tiles[leftIndex][0] + 1);
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           // Return the maximum number of tiles that the carpet can cover.
34
           return maxTilesCovered;
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36 }
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C++ Solution
   #include <vector>
   #include <algorithm>
   class Solution {
   public:
       int maximumWhiteTiles(vector<vector<int>>& tiles, int carpetLength) {
           // Sort the tiles based on their starting position.
            sort(tiles.begin(), tiles.end());
10
            int covered = 0, maxCovered = 0, numTiles = tiles.size();
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           // Two pointers approach: `left` tracks the start of the carpet, `right` the end.
            for (int left = 0, right = 0; left < numTiles; ++left) {</pre>
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               // Extend the right boundary of the carpet as far as possible within carpet length.
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               while (right < numTiles && tiles[right][1] - tiles[left][0] + 1 <= carpetLength) {</pre>
15
                    covered += tiles[right][1] - tiles[right][0] + 1;
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```

// If the carpet can't extend to cover the whole next tile, include partial coverage.

// Otherwise, compare the current covered area to the max covered so far.

// Move the left boundary of the carpet, reducing the covered area accordingly.

// Return the maximum white tiles space that can be covered by the carpet.

maxCovered = std::max(maxCovered, covered + tiles[left][0] + carpetLength - tiles[right][0]);

if (right < numTiles && tiles[left][0] + carpetLength > tiles[right][0]) {

maxCovered = std::max(maxCovered, covered);

covered -= (tiles[left][1] - tiles[left][0] + 1);

1. Sorting the tiles requires $O(n \log n)$ time, where n is the number of tiles.

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Typescript Solution
1 function maximumWhiteTiles(tiles: number[][], carpetLength: number): number {
       // Sort the tiles based on their starting position.
       tiles.sort((a, b) => a[0] - b[0]);
       let covered = 0;
       let maxCovered = 0;
       let numTiles = tiles.length;
8
       // Two pointers approach: `left` tracks the start of the carpet, `right` the end.
9
       for (let left = 0, right = 0; left < numTiles; ++left) {</pre>
10
           // Extend the right boundary of the carpet as far as possible within carpet length.
11
           while (right < numTiles && tiles[right][1] - tiles[left][0] + 1 <= carpetLength) {</pre>
12
13
               covered += tiles[right][1] - tiles[right][0] + 1;
14
               ++right;
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16
17
           // If the carpet can't extend to cover the whole next tile, include partial coverage.
           if (right < numTiles && tiles[left][0] + carpetLength > tiles[right][0]) {
18
19
               maxCovered = Math.max(maxCovered, covered + tiles[left][0] + carpetLength - tiles[right][0]);
           } else {
20
21
               // Otherwise, compare the current covered area to the max covered so far.
22
               maxCovered = Math.max(maxCovered, covered);
23
24
           // Move the left boundary of the carpet, reducing the covered area accordingly.
           covered -= (tiles[left][1] - tiles[left][0] + 1);
26
27
28
29
       // Return the maximum white tiles space that can be covered by the carpet.
       return maxCovered;
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31 }
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Time and Space Complexity
```

Time Complexity The time complexity of the code is primarily determined by the sorting of the tiles array and the two-pointer technique used to iterate through the tiles.

because the sorting term is dominant.

The space complexity is 0(1) or constant space, as the sorting is done in-place (assuming the sort function does in-place sorting) and only a fixed number of integer variables are used to keep track of the pointers, the sum of the tiles within the carpet, and the current maximum.

2. The two-pointer technique involves a while-loop that iterates through the tiles. In the worst case, both i and j pointers can touch each tile once, resulting in O(n) time complexity. Since these processes are sequential, the overall time complexity of the algorithm is 0(n log n + n), which simplifies to 0(n log n) **Space Complexity**

The auxiliary space for variables like s, ans, i, and j is negligible and does not grow with the input size. Thus, the space complexity does not rely on the number of tiles and remains constant.