**Dynamic Programming** 

## **Problem Description**

Array

Math

You are given an array nums with positive integers. The task is to find out how many subarrays within this array are in strictly increasing order. A subarray is defined as a consecutive sequence of elements from the given array.

### Intuition

Medium

The intuition behind the solution is to use a two-pointer approach to iterate through the array and identify all the consecutive, strictly increasing subarrays. An incrementing counter is maintained to track the length of each found increasing subarray.

greater than the previous one, indicating an increasing sequence. When the inner loop finds that the sequence is no longer increasing, it stops, and the number of subarrays that can be formed with the identified sequence is calculated.

As the outer loop moves through the array, the inner loop expands the current subarray window as long as the next element is

To calculate the number of strictly increasing subarrays that fit within the length of the contiguous sequence, we use the formula for the sum of the first n natural numbers, which is n(n + 1) / 2. This formula is applied because every element in the increasing subarray can be the start of a new subarray, and the number of subarrays ending at each element increases by one for each additional element.

Once counted, the outer loop moves to the end of the previously identified increasing subarray to begin the search for the next sequence. This process continues until the end of the array is reached. The solution has linear time complexity since each element is visited only once by the inner loop.

## **Solution Approach** The given solution uses a simple algorithm with the help of two pointers, i and j. The Python code uses a while loop to iterate over

the array with its index i. Inside this loop, another while loop is initiated with index j set to i + 1. Here's a breakdown of the approach:

2. Start the outer loop with i at zero, and it will run until it reaches the length of nums.

1. Initialize an answer variable ans to zero. This will keep the count of strictly increasing subarrays.

- 3. Inside the outer loop, immediately start the inner loop with j = i + 1.
- 4. Continue the inner loop as long as j is less than the length of nums and the current element nums [j] is greater than the previous
- element nums [j 1] (the condition for a strictly increasing subarray). 5. If the condition satisfies inside the inner loop, increment j to expand the current window of the increasing subarray.
- 6. Calculate the count cnt of consecutive increasing numbers as j i.
- 7. Use the formula (1 + cnt) \* cnt // 2 to add the number of subarrays that can be formed within the window i to j 1 to ans.
- This formula derives from the sum of the first n natural numbers formula n \* (n + 1) / 2, as each element of the subarray can be the starting element for a new subarray, adding to the total count. 8. Assign i to j to move to the end of the current strictly increasing sequence and then look for the next one in the outer loop.
- 9. After the outer loop concludes, return the cumulative count ans as the result.
- This approach does not require any additional data structures and relies on a simple calculation and pointer manipulation to arrive at

the solution.

## Let's walk through the solution approach with a small example array nums = [1, 2, 3, 1, 2].

Example Walkthrough

1. Initialize ans to 0. This is our counter for strictly increasing subarrays. 2. Begin with i = 0. The value at nums [i] is 1.

- 3. Start the inner loop by setting j = i + 1, which is 1 (the second element, which has a value of 2). 4. Now, nums[j] > nums[j - 1] because 2 (at j) is greater than 1 (at i). Hence, there is a strictly increasing subarray from index 0
- to index 1.
- 5. Continue incrementing j. It becomes 2, and nums[j] is 3 which still satisfies nums[j] > nums[j 1].
- 6. Incrementing j again to 3, we get nums[j] = 1. This is not greater than 3 (the previous value), so the inner loop stops here. 7. Calculate the count cnt as j - i, which gives 3 - 0 = 3. We've found a strictly increasing subarray of length 3.
- 8. We can form (1 + cnt) \* cnt // 2, which is (1 + 3) \* 3 // 2 = 6 strictly increasing subarrays from index 0 to index 2.
- 9. Add 6 to ans. Now, ans is 6.
- 10. Move i to j, so i = 3. The value at nums[i] is 1. 11. Repeat the process with the new value of i. Start the inner loop with j = i + 1, which is 4. We have nums [j] = 2.
- 12. Continue as nums[j] > nums[j 1] (2 > 1), but since j is now pointing to the last element, the inner loop will stop after this.

while start\_index < len(nums):</pre>

public long countSubarrays(int[] nums) {

long totalSubarrays = 0;

int arraySize = nums.length;

int startIdx = 0;

// Initialize count of subarrays as 0

// Start index of the current subarray

// Total number of elements in the array

- 13. Calculate the count cnt as 1 because only one pair 1, 2 satisfies the condition of a strictly increasing subarray.
- 14. We can form (1 + cnt) \* cnt // 2, which is (1 + 1) \* 1 // 2 = 1 additional strictly increasing subarray from index 3 to index
- 4.
- 15. Add 1 to ans. Now, ans is 6 + 1 = 7. 16. There's no more elements beyond j = 4 to check, so we finish iteration.
- At the end of this process, we have determined that there are 7 strictly increasing subarrays within nums.

# Loop over the array to find all increasing subarrays

// Method to count strictly increasing contiguous subarrays within an array.

Python Solution

#### def countSubarrays(self, nums: List[int]) -> int: # Initialize the answer and the starting index subarray\_count = start\_index = 0

class Solution:

```
# Move to the next index to compare with the current element
               end_index = start_index + 1
10
               # Check if the next element is greater than the current
11
12
               # Continue moving end_index as long as we have an increasing subarray
               while end_index < len(nums) and nums[end_index] > nums[end_index - 1]:
13
                   end_index += 1
14
15
               # Calculate the length of the current increasing subarray
16
               length = end index - start index
17
18
               # Compute the number of possible contiguous subarrays in the increasing subarray
19
               # and add to the total count
20
               subarray_count += (1 + length) * length // 2
21
22
23
               # Move start_index to the next point to start checking for a new subarray
24
               start_index = end_index
26
           # Return the total count of increasing subarrays
27
           return subarray_count
28
Java Solution
   class Solution {
```

#### 10 // Iterate over the array 11

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```
12
           while (startIdx < arraySize) {</pre>
13
               // Initialize end index of the current subarray to be just after startIdx
14
               int endIdx = startIdx + 1;
               // Extend the end index until it no longer forms a strictly increasing subarray
               while (endIdx < arraySize && nums[endIdx] > nums[endIdx - 1]) {
16
                    endIdx++;
17
18
               // Calculate the count of increasing subarrays that can be formed between startIdx and endIdx
19
               long currentSubarrayCount = endIdx - startIdx;
20
               // Use the formula for the sum of first n numbers to calculate combinations
                totalSubarrays += (currentSubarrayCount + 1) * currentSubarrayCount / 2;
22
23
               // Move the start index to the end index for the next iteration
24
               startIdx = endIdx;
25
26
27
           // Return the total count of strictly increasing subarrays
28
           return totalSubarrays;
29
C++ Solution
 1 class Solution {
   public:
        long long countSubarrays(vector<int>& nums) {
            long long count = 0; // This will hold the total count of valid subarrays
            int start = 0, n = nums.size(); // `start` is the index to mark the beginning of a new subarray
           // Iterate over the array
           while (start < n) {</pre>
```

int end = start + 1; // `end` is the index for the end of a growing subarray

// Calculate the number of possible subarrays within the current valid range

// Use the arithmetic series sum formula to count subarrays: n \* (n + 1) / 2

while (end < n && nums[end] > nums[end - 1]) {

count += 1ll \* (1 + length) \* length / 2;

int length = end - start; // Length of the current subarray

// Extend the subarray until the current element is not greater than the previous one

#### 21 // Move the start for the next potential subarray 22 23

++end;

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```
start = end;
24
25
            return count; // Return the total count of the subarrays
26
27 };
28
Typescript Solution
   function countSubarrays(nums: number[]): number {
       // Initialize the count of subarrays
       let count = 0;
       // Index 'i' is used to iterate through the array with initialized value of 0
       let i = 0;
       // 'n' stands for the length of the input array 'nums'
       const n = nums.length;
 8
       // Loop over the elements of the array using 'i'
 9
       while (i < n) {
10
           // Initialize 'j' for the inner loop as the next index of 'i'
11
           let j = i + 1;
13
           // Inner loop to find increasing consecutive subarray starting at 'i'
14
           while (j < n \& nums[j] > nums[j - 1]) {
15
               ++j; // Increase 'j' if the current element is greater than the previous
16
17
18
           // Calculate the length of the current increasing subarray
19
           const length = j - i;
20
21
           // Calculate the count of subarrays for this segment using the formula for sum of first 'length' natural numbers
22
```

#### 27 28 29 // Return the total count of increasing consecutive subarrays return count; 30

Time and Space Complexity

i = j;

count += ((1 + length) \* length) / 2;

// Set 'i' to 'j' to look for the next segment

23

24

26

31 }

32

**Time Complexity** The given code consists of a while loop that iterates over the length of the array nums. Inside this loop, there is another while loop that continues as long as the current element is greater than the previous element. This inner loop increments j, effectively counting the length of a monotonically increasing subarray starting at index i. The time complexity of this algorithm depends on the number and size of the monotonically increasing subarrays in nums.

and the inner loop runs only once for each element, thus giving a time complexity of O(n). In the worst-case scenario, when all elements are in increasing order, the first inner loop runs n-1 times, the second n-2 times, and

so on. Therefore, the number of iterations would resemble the sum of the first n-1 integers, which is (n-1)\*n/2, resulting in a time

In the best-case scenario, when all elements are in decreasing order, the outer loop runs n times (where n is the length of the array),

complexity of  $O(n^2)$  for this scenario. However, because each element is visited at most twice (once as the end of a previous subarray and once as the beginning of a new

# subarray), the actual time complexity, in general, is O(n).

**Space Complexity** The space complexity of the provided code is 0(1). This is because the code uses a constant amount of extra space for variables

ans, i, and j, regardless of the input size. There are no additional data structures that grow with the size of the input.