#### 2064. Minimized Maximum of Products Distributed to Any Store

Medium Array Binary Search

### Problem Description

number of product types, denoted by an array quantities where each entry quantities [i] represents the amount available for the i-th product type. The objective is to distribute these products to the stores following certain rules:

• Each store can receive at most one product type.

The problem presents a scenario where there is a given number of specialty retail stores, denoted by an integer n, and a certain

- A store can receive any amount of the one product type it is given.
  The goal is to minimize the maximum number of products given to any single store.
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  - This situation is akin to finding the most balanced way of distributing products such that the store with the largest stock has as little product as possible, in order to minimize potential waste or overstock.

In simple terms, you are asked to find the smallest number x which represents the maximum number of products that any store will have after the distribution is completed.

ntuition

The solution involves using a <u>binary search</u> algorithm. The key insight here is that if we can determine a minimum possible x such

## that all products can be distributed without exceeding x products in any store, we have our answer. Here's the reasoning process:

We know that the value of x must be between 1 (if there's at least one store for each product) and the maximum quantity in quantities (if there's only one store).
Using <u>binary search</u>, we can quickly narrow down the range to find the smallest possible x.

• To test if a given x is valid, we check if all products can be distributed to stores without any store getting more than x products. This is done by calculating the number of stores needed for each product type (rounded up) and ensuring the sum does not exceed n.

to be distributed within the n stores.

- calculating the number of stores needed for each product type (rounded up) and ensuring the sum does not exceed n.

  The check function in the provided code snippet helps with this validation by returning True if a given x allows for all the products
- The Python bisect\_left function is used to perform the binary search efficiently. It returns the index of the first element in the

to linear search, especially when there's a large range of possible values for x.

Here is the step-by-step implementation of the solution:

represents the smallest x for which check(x) is True.

repeatedly divides the search interval in half.

cover the maximum possible quantity.

**Helper Function (check):** 

given range that matches True when passed to the check function. This means it effectively finds the lowest number x such that check(x) is true, which is our desired minimum possible maximum number of products per store (x).

By starting the binary search at 1 and going up to 10\*\*6 (an arbitrary high number to ensure the maximum quantity is covered), we guarantee finding the minimum x within the valid range.

Solution Approach

The solution adopts a binary search algorithm to efficiently find the minimum value of x that satisfies the distribution conditions.

Binary search is an optimal choice here because it allows for a significant reduction in the number of guesses needed compared

Binary Search Algorithm:
 The binary search is used to find the minimum x such that all products can be distributed according to the rules. It is efficient because it

○ In this case, the lower and upper bounds for the search are 1 and 10\*\*\*6 respectively. The upper bound is a sufficiently large number to

• A helper function, check, is used during the binary search to validate whether a given x can be used to distribute all the products within the

x and rounding up (since we can't have a fraction of a store). This is done using (v + x - 1) // x for each v in quantities. The rounding up

#### available stores. • For each product type in quantities, the function calculates the number of stores required by dividing the quantity of that product type by

- is achieved by adding x-1 before performing integer division.

  Using bisect\_left:
- The Python function bisect\_left from the bisect module is employed to perform the binary search. The function takes in a range, a target value (True in this case, as check returns a boolean), and a key function (check). The key function is called with each mid-value during the search to determine if x is too high or too low.
   bisect\_left will find the position i to insert the target value (True) in the range in order to maintain the sorted order. Since the key function

effectively turns the range into a sorted boolean array (False for values below our target and True for values at or above it), the position i

Outcome:
 The value of x found by the bisect\_left search is incremented by 1 because the range is 0-indexed, whereas the quantities need to be 1-indexed (since x can't be zero).

This approach of binary search combined with a check for the validity of the distribution ensures that the solution is both

efficient and correct, taking O(log M \* N) time complexity, where M is the range of possible values for x and N is the length of

Let's consider an example where we have n = 2 specialty retail stores and quantities = [3, 6, 14] for the product types.

• The possible values for x start with a lower bound of 1, and an upper bound of 10\*\*6.

quantities.

**Example Walkthrough** 

**Binary Search Initialization:** 

**Adjusting the Search Range:** 

 $\circ$  Continuing the binary search, let's try x = 10.

example, we choose 7.

First Mid-point Check:

Let's pick a mid-point for x during the binary search. Since our bounds are 1 and 10\*\*6, a computationally reasonable mid-point to start could be 500,000. However, for the sake of example, we'll use 5 as it's a more illustrative number.

• We run the check function with x = 5. We need one store for the first product type (3/5 rounded up is still 1 store), two stores for the second

product type (6/5 rounded up is 2 stores), and three stores for the third product type (14/5 rounded up is 3 stores).
 In total, we would need 1 + 2 + 3 = 6 stores to distribute the products with each store receiving no more than 5 products. However, we only have 2 stores.
 Since we can't distribute the products without exceeding 5 products in any store with only 2 stores, check(5) returns False.

Since 5 is too small, we adjust our search range. The next mid-point we check is halfway between 5 and 10\*\*6, but again as this is an

 $\circ$  We run the check function with x = 7. This time we would need 1 store for the first product type (3/7 rounded up is still 1 store), 1 store for

#### the second product type (6/7 rounded up is still 1 store), and 2 stores for the third product type (14/7 is exactly 2 stores), totaling 1 + 1 + 2 = 4 stores. This is still more than 2 stores, so check(7) returns False.

Finding the Valid x:

• Running check(10), the first product type requires 1 store (3/10 rounded up is still 1 store), the second product type also requires 1 store (6/10 rounded up is still 1 store), and the third product type requires 2 stores (14/10 rounded up is 2 stores). The total is 1 + 1 + 2 = 4 stores, which is still too many.

have a fraction of a store). The total is 3 stores, which is still more than 2, so check(15) returns False.

Binary Search Conclusion:

Finally, we try x = 20.

Now running check(20), each product type will require only 1 store: (3/20, 6/20, 14/20 all round up to 1). The sum is exactly 2 stores, which

• Since check(20) returns True and we cannot go lower than 20 without needing more stores than we have, 20 is our smallest possible x.

In practice, the binary search would proceed by narrowing down the range between the values where check returns False and

products to the 2 stores in such a way that no store has more than 20 products, thereby minimizing the maximum number of

where check returns True. In our manually stepped-through example, x = 20 is the solution. This means that we can distribute the

However, if we check x = 15, we see that each product type would only require 1 store: (3/15, 6/15, 14/15 all round up to 1 since we can't

# products per store. Solution Implementation

**Python** 

Java

class Solution {

return left;

return left;

let searchStart = 1;

while (searchStart < searchEnd) {</pre>

for (const quantity of products) {

searchStart = middle + 1;

let storeCount = 0;

} else {

return min\_max\_quantity

Time and Space Complexity

**Time Complexity:** 

**}**;

**TypeScript** 

C++

public:

#include <vector>

class Solution {

using namespace std;

matches n = 2.

```
def is_distribution_possible(x):
    # Calculate the total number of stores required if each store can hold up to 'x'
    # items. The expression (quantity + x - 1) // x is used to ceiling divide the quantity
    # by x to find out how many stores are required for each quantity.
```

return min\_max\_quantity

from bisect import bisect\_left

def minimizedMaximum(self, n: int, quantities: List[int]) -> int:

# where the 'is\_distribution\_possible' function returns 'True'.

public int minimizedMaximum(int stores, int[] products) {

// and the highest possible maximum is assumed to be 100000

// Method to find the minimized maximum number of products per shelf

int left = 1; // Start with the minimum possible value per shelf

int minimizedMaximum(int n, vector<int>& quantities) {

# quantity in any store does not exceed 'x'.

return total\_stores\_needed <= n</pre>

# Define a check function that will be used to determine if a specific value of 'x'

total\_stores\_needed = sum((quantity + x - 1) // x for quantity in quantities)

# the items does not exceed the number of stores. We search in the range from 1 to 10\*\*6

# as an upper limit, assuming that the maximum quantity per store will not exceed 10\*\*6.

min\_max\_quantity = 1 + bisect\_left(range(1, 10\*\*6), True, key=is\_distribution\_possible)

# Use binary search (bisect\_left) to find the smallest 'x' such that distributing

# Return the smallest possible maximum quantity that can be put in a store.

# Check if the total number of stores needed does not exceed the available 'n' stores.

# The second argument to bisect\_left is 'True' because we are interested in finding the point

# allows distributing all the quantities within 'n' stores such that the maximum

from typing import List

class Solution:

```
// (based on the problem constraints if given in the problem description).
int left = 1, right = 100000;
// Using binary search to find the minimized maximum value
while (left < right) {</pre>
    // Midpoint of the current search space
    int mid = (left + right) / 2;
    // Counter for the number of stores needed
    int count = 0;
    // Distribute products among stores
    for (int quantity : products) {
        // Each store can take 'mid' amount, calculate how many stores are required
        // for this particular product, rounding up
        count += (quantity + mid - 1) / mid;
   // If we can distribute all products to 'stores' or less with 'mid' maximum product per store,
    // we are possibly too high in the product capacity (or just right) so we try a lower capacity
    if (count <= stores) {</pre>
        right = mid;
    } else {
        // If we are too low and need more than 'stores' to distribute all products,
        // we need to increase the product capacity per store
        left = mid + 1;
```

// 'left' will be our minimized maximum product per store that fits all products into 'stores' stores.

// Initial search space: the lowest possible maximum is 1 (each store can have at least one of any product),

```
int right = 1e5; // Assume an upper bound for the maximum value per shelf
// Use binary search
while (left < right) {</pre>
    int mid = (left + right) >> 1; // Calculate mid value
    int count = 0; // Initialize count of shelves needed
    // Iterate through the quantities array
    for (int& quantity : quantities) {
        // Calculate and add number of shelves needed for each quantity
        count += (quantity + mid - 1) / mid;
   // If the count of shelves needed is less than or equal to the available shelves
   // there might be a solution with a smaller max quantity, search left side
    if (count <= n) {
        right = mid;
   // Otherwise, search the right side with larger quantities
   else {
        left = mid + 1;
// When left meets right, it's the minimized max quantity per shelf
```

```
// Increment the store count by the number of stores needed for this product.
// We take the ceiling to account for incomplete partitions.
storeCount += Math.ceil(quantity / middle);
}

// If the store count fits within the number of available stores,
// we proceed to check if there's an even smaller maximum.
if (storeCount <= stores) {
    searchEnd = middle;</pre>
```

function minimizedMaximum(stores: number, products: number[]): number {

let searchEnd = 1e5; // Assuming 1e5 is the maximum possible quantity.

// Calculate the middle value of the current search interval.

// Counter to keep track of the total number of stores needed.

// Iterating over each product quantity to distribute among stores.

const middle = Math.floor((searchStart + searchEnd) / 2);

// Binary search to find the minimized maximum number of products per store.

// Define the search interval with a sensible start and end.

```
// The minimized maximum number of products per store that will fit.
      return searchStart;
from bisect import bisect_left
from typing import List
class Solution:
   def minimizedMaximum(self, n: int, quantities: List[int]) -> int:
       # Define a check function that will be used to determine if a specific value of 'x'
        # allows distributing all the quantities within 'n' stores such that the maximum
        # quantity in any store does not exceed 'x'.
        def is_distribution_possible(x):
           # Calculate the total number of stores required if each store can hold up to 'x'
            # items. The expression (quantity + x - 1) // x is used to ceiling divide the quantity
            # by x to find out how many stores are required for each quantity.
            total_stores_needed = sum((quantity + x - 1) // x for quantity in quantities)
            # Check if the total number of stores needed does not exceed the available 'n' stores.
            return total_stores_needed <= n</pre>
```

# Use binary search (bisect\_left) to find the smallest 'x' such that distributing

# Return the smallest possible maximum quantity that can be put in a store.

# the items does not exceed the number of stores. We search in the range from 1 to 10\*\*6

# as an upper limit, assuming that the maximum quantity per store will not exceed 10\*\*6.

min\_max\_quantity = 1 + bisect\_left(range(1, 10\*\*6), True, key=is\_distribution\_possible)

# The second argument to bisect\_left is 'True' because we are interested in finding the point

// Else we need to increase the number of products per store and keep looking.

The given Python code aims to find a value of x that, when used to distribute the quantities of items amongst n stores, results in a minimized maximum number within a store while ensuring all quantities are distributed. This is achieved by using a binary search

via bisect\_left on a range of possible values for x.

# where the 'is\_distribution\_possible' function returns 'True'.

The binary search is performed on a range from 1 to a constant value (10\*\*6), resulting in  $0(\log(C))$  complexity, where C is the upper limit of the search range. Inside the check function, there is a loop which computes the sum with complexity 0(Q) for each check, where Q is the length of the quantities list. Therefore, the time complexity of the entire algorithm is  $0(Q * \log(C))$ .

Space Complexity:

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The code uses a constant amount of additional memory outside of the quantities list input. The check function computes the sum using the values in quantities without additional data storage that depends on the size of quantities or the range of values. Hence, the space complexity is 0(1), as no significant additional space is consumed in relation to the input size.