1538. Guess the Majority in a Hidden Array Medium Array Math Interactive

In this problem, we're given an array of integers called nums, where every integer is either 0 or 1. Direct access to this array is not permitted; instead, we have access to an API ArrayReader that provides two functions. The query(a, b, c, d) function can be used

to query the array with four different indices (with the condition 0 <= a < b < c < d < ArrayReader.length()) and returns the distribution of the four selected elements as follows: Returns 4 if all four elements are 0's or all are 1's.

 Returns 2 if three elements are the same (either three 0's and one 1, or three 1's and one 0). Returns 0 if there's an even split (two 0's and two 1's).

Problem Description

The length() function returns the size of the array. Our goal is to find the index of any element with the most frequent value, which could be either 0 or 1. In case of a tie, where 0 and 1

are equally frequent, we return -1.

with the first three; if it doesn't match, it's different.

subsets of the array using the query() function.

distribution pattern of the first four elements.

If the return value of this query matches x, we increment counter a;

it's a majority element); otherwise, increment b and update k respectively.

o If a equals b, we conclude there is a tie and return −1;

Let's assume we have a nums array of size 8, and we perform the following steps:

We iterate with a loop for indices 4 to 7 (the rest of the array).

We continue with query(0, 1, 2, 6), returning 4, so we increment a.

At the end of this process, let's assume a is 6, and b is 1. We now decide the majority element:

Initialize the counter for the two possible majorities and an index tracker

minority_index = i # Store the index of the first occurrence in minority

These queries involve the element at index 4 to compare with the baseline value

if reader.query(i, (i + 1) % 3, (i + 2) % 3, 4) == initial_queries_comparison:

minority_index = i # Update the index of the first occurrence in minority

The element at index 3 has a different status compared to the first three elements due to the setup

Hence, if the majority count is greater, the index of the minority is returned; otherwise, 3 is returned

Perform additional queries to determine the first three elements' majority/minority status

The k variable is initialized but not yet set.

To solve this problem, we start with the understanding that the query() function can give us an insight into the majority element by comparing the distribution of 0s and 1s among different subsets of four elements. Since we're allowed to call query() 2 * n times where n is the array length, we have enough queries at our disposal to deduce the majority element's index.

The solution includes querying the first four elements to establish the initial distribution (let's call this the baseline distribution). Afterwards, we loop through the rest of the elements, using query() with the first three indices fixed and the fourth one changing to include each new index from the rest of the array. If the distribution matches the baseline, the new element shares the majority value

The first element not included in the initial query (index 4) is specially treated by checking its distribution with the next 3 consecutive elements. This helps us in confirming whether the initially queried elements were a majority or a split. After looping through all elements, we compare the count of elements that matched the baseline distribution (a) with those that didn't (b). The index that occurs more is the majority. If both counts are equal, we have a tie, and we return -1.

The intuition is based on iteratively narrowing down the possible indices for the majority element by comparing the distribution of

Solution Approach

breakdown of each part of the code and the algorithms, data structures, or patterns used: 1. Initialization: The n variable is initialized with the size of the array using reader.length(). Two counters, a and b, are initialized

The implementation of the solution approach involves using a simple iteration to leverage the ArrayReader API effectively. Here's a

to keep track of the counts of indices that match or do not match the initial baseline distribution. Variable k is initialized to store an index where the value is different from the baseline if such an index is found. 2. Initial Query: We perform the first query(0, 1, 2, 3) to establish a baseline distribution stored in variable x. This tells us the

3. Iterative Comparison: A for loop is used to iterate through the elements starting from index 4 to the last index n-1. In each iteration, we query a subset that includes the first three fixed indices (0, 1, 2) and the current index i.

4. Special Cases: After the loop, we need to verify the initial three elements (which are fixed in the previous query() calls) to

 \circ If the return value doesn't match x, we increment counter b and update k with the current index i.

5. Determine Majority Index: Finally, we determine whether there is a majority by comparing the counts a and b.

index 4. This helps in confirming whether the initially queried indices were a majority. • The results of these queries are compared against a different baseline distribution stored in y which is obtained by query (0, 1, 2, 4).

ensure their distribution. This requires three additional queries, each omitting one of the first three indices alongside the fourth

o If the result of these comparisons is equal to y, increment a since the omitted element matches the initial query (suggesting

∘ If a is greater, we return 3 which was part of the original subset and, therefore, in the majority. ○ If b is greater, the index k is returned, indicating that k is part of the frequent value.

Data structures used in this solution are primarily basic integer variables for counting. The pattern used is iterative comparisons with

early stopping as soon as the majority element is confirmed. The algorithm doesn't require complex data structures as it makes

- effective use of the provided API to solve the problem. **Example Walkthrough**
- The array size n is 8 (determined using reader.length()). • We initialize two counters, a and b, to zero. Counter a will track indices matching the baseline distribution, while b tracks the

• We run query (0, 1, 2, 3) and let's say it returns 4. This suggests all elements are the same (all 0s or all 1s), so our baseline distribution x is 4. 3. Iterative Comparison:

• We perform query(0, 1, 2, 4). Assume it returns 4, identical to our baseline, so we increment a.

Next, query(0, 1, 2, 5) might return 2, unlike our baseline. We increment b and set k to 5.

Lastly, query(0, 1, 2, 7) returns 4, incrementing a again. 4. Special Cases:

5. **Determine Majority Index:**

Python Solution

1 class Solution:

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C++ Solution

public:

1 class Solution {

int guessMajority(ArrayReader& reader) {

int arrayLength = reader.length();

// Get the array length

int minorityCount = 0;

int minorityIndex = 0;

} else {

between 0s and 1s, we would return -1.

def guessMajority(self, reader: "ArrayReader") -> int:

Get the length of the array

majority_count, minority_count = 1, 0

majority_count += 1

minority_count += 1

majority_count += 1

minority_count += 1

if majority_count == minority_count:

public int guessMajority(ArrayReader reader) {

// Get the length of the array

int arrayLength = reader.length();

initial_queries_comparison = reader.query(0, 1, 2, 4)

If the counts are the same, we return -1, as there is no majority

return minority_index if majority_count > minority_count else 3

// Initial query to determine the pattern to compare against

n = reader.length()

minority_index = 0

else:

for i in range(3):

return -1

else:

1. Initialization:

others.

2. Initial Query:

 Next, query(0, 2, 3, 4) and if it returns 4, we increment a—let's say it does; • Finally, query(0, 1, 3, 4) and if it returns 4, we increment a—let's assume it also does.

We then create a separate baseline y with query(0, 1, 2, 4) (we have already done this and know it's 4).

• We run query(1, 2, 3, 4) for special case handling, and if it returns 4, we increment a—let's assume it does;

This example confirmed that the majority values were present in the initial subset, and indexes that matched this distribution were in the majority. If b had been greater, we would return k, which in this walkthrough was 5. If a and b were equal, indicating an even split

Since a is greater than b, we return index 3 because it belongs to the subset that matched our initial baseline the most.

Perform the initial query to establish a baseline comparison 10 baseline_query = reader.query(0, 1, 2, 3) 11 12 13 # Iterate through the rest of the array starting from index 4 14 for i in range(4, n): 15 # Query with the new index and compare to the baseline if reader.query(0, 1, 2, i) == baseline_query: 16

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Java Solution
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1 class Solution {

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int initialQueryResult = reader.query(0, 1, 2, 3);
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           // 'sameMajorityCount' is the count of indices following the initial pattern
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           // 'differentMajorityCount' is the count of indices that differ from the initial pattern
            int sameMajorityCount = 1, differentMajorityCount = 0;
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           // 'differentIndex' keeps track of the index where a different pattern was first noticed
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            int differentIndex = 0;
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           // Check rest of the elements with the initial ones except the last three
            for (int i = 4; i < arrayLength; ++i) {</pre>
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                if (reader.query(0, 1, 2, i) == initialQueryResult) {
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                    sameMajorityCount++; // Same pattern detected, increment count
20
                } else {
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                   differentMajorityCount++; // Different pattern detected, increment count and update the index
22
                   differentIndex = i;
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            // Perform queries swapping out one of the first three elements with the fourth one
27
            // This checks the pattern of the last three indices
            int subsequentQueryResult = reader.query(0, 1, 2, 4);
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            for (int i = 0; i < 3; i++) {
                int queryResult = reader.query(i == 0 ? 1 : 0, i == 1 ? 2 : 1, i == 2 ? 3 : 2, 4);
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31
                if (queryResult == subsequentQueryResult) {
32
                    sameMajorityCount++; // Increment count if the same as the subsequent pattern
33
                } else {
34
                   differentMajorityCount++; // Increment different count and update index with the swapped element
35
                   differentIndex = i;
36
37
38
39
           // If counts are equal, no unique majority index exists
           if (sameMajorityCount == differentMajorityCount) {
40
                return -1;
41
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           // Return the index which has the majority pattern (most occurrences)
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           // If the counts of the same pattern is greater, return the constant 3 as per initial result
```

// If counts of the different pattern is greater, return the index where the difference was first noted

int majorityCount = 1; // We start with 1 since we know the first four elements are the baseline

return sameMajorityCount > differentMajorityCount ? 3 : differentIndex;

// Query the first four elements to get a baseline comparison

// Initialize the count for the majority and minority elements

if (reader.query(0, 1, 2, i) == firstQueryResult) {

// Compare the rest of the array elements starting from the fifth element

// If the next element belongs to the majority, increase the majority count

// Otherwise, increase the minority count and update the minorityIndex

// Perform another query with 0, 1, 2 and a known different element (4 in this case)

// If the majority and minority counts are the same, the result is ambiguous

// Check the remaining three elements against the new query to determine if they belong to the majority or minority

int firstQueryResult = reader.query(0, 1, 2, 3);

// Keep track of the latest minority element index

int secondQueryResult = reader.query(0, 1, 2, 4);

if (reader.query(1, 2, 3, 4) == secondQueryResult) {

minorityIndex = 0; // Element 0 is different

if (reader.query(0, 2, 3, 4) == secondQueryResult) {

minorityIndex = 1; // Element 1 is different

for (int i = 4; i < arrayLength; ++i) {</pre>

++majorityCount;

++minorityCount;

++majorityCount;

++minorityCount;

++majorityCount;

++minorityCount;

} else {

} else {

minorityIndex = i;

44 45 if (reader.query(0, 1, 3, 4) == secondQueryResult) { 46 ++majorityCount; 47 } else { 48 ++minorityCount; minorityIndex = 2; // Element 2 is different 49

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             if (majorityCount == minorityCount) {
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                 return -1;
 55
 56
 57
             // If the majority count is greater, the answer is the initial subset index (3)
 58
             // Otherwise, return the index of the minority element
 59
             return majorityCount > minorityCount ? 3 : minorityIndex;
 60
 61 };
 62
Typescript Solution
    function guessMajority(reader: ArrayReader): number {
         // Retrieve the length of the array from the reader
  3
         const arrayLength = reader.length();
  4
  5
         // Perform the initial query on the first four elements
         const firstQueryResult = reader.query(0, 1, 2, 3);
  6
  8
         // Initialize counter for the majority and minority elements, as well as the index of the first different element
         let majorityCount = 1;
  9
         let minorityCount = 0;
 10
 11
         let firstDifferentIndex = 0;
 12
 13
         // Iterate over the rest of the elements, starting from the 5th element
 14
         for (let i = 4; i < arrayLength; ++i) {</pre>
             // Compare each new element with the initial three elements to determine its type
 15
 16
             if (reader.query(0, 1, 2, i) === firstQueryResult) {
 17
                 ++majorityCount;
 18
             } else {
 19
                 ++minorityCount;
 20
                 firstDifferentIndex = i;
 21
 22
 23
 24
         // Perform additional queries by excluding one element from the first four each time
 25
         const secondQueryBase = reader.query(0, 1, 2, 4);
 26
         if (reader.query(1, 2, 3, 4) === secondQueryBase) {
 27
             ++majorityCount;
 28
         } else {
 29
             ++minorityCount;
 30
             firstDifferentIndex = 0;
 31
 32
         if (reader.query(0, 2, 3, 4) === secondQueryBase) {
 33
             ++majorityCount;
         } else {
 34
 35
             ++minorityCount;
 36
             firstDifferentIndex = 1;
 37
 38
         if (reader.query(0, 1, 3, 4) === secondQueryBase) {
 39
             ++majorityCount;
         } else {
 40
             ++minorityCount;
 41
             firstDifferentIndex = 2;
 42
```

Time and Space Complexity

return -1;

if (majorityCount === minorityCount) {

The time complexity of the provided guessMajority function primarily depends on the number of calls made to the reader query method within a loop and outside of it.

Time Complexity

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• There is a fixed number of calls to reader query made outside of the loop for the indices 0, 1, 2, 3, and four additional calls to compare with index 4. • The loop iterates from index 4 to n - 1 (where n is the length of the array), making one call to reader query per iteration.

// If the majority is in the first four elements, we return 3, which points to the index 3 in the initial query

// Otherwise, we return the index of the first element that was different from the initial majority

Space Complexity The space complexity of the code is determined by the variables used in the guessMajority function.

Thus, the total number of query calls is 8 + (n - 4) = n + 4. Given that each query call is assumed to have a constant time

Hence, the number of query calls is 4 (initial) + 4 (comparisons with index 4) + (n − 4) for the loop.

// If there is an equal number of majority and minority elements, there is no majority

// The majority is determined by the element with more occurrences

return majorityCount > minorityCount ? 3 : firstDifferentIndex;

 No additional data structures that grow with the input size are used. Therefore, the space complexity of the guessMajority function is 0(1), which means it requires constant space.

complexity, the time complexity of the guessMajority function is O(n).

Constant extra space is used for the variables a, b, k, x, and y, independent of the input size n.