Two Pointers

Hash Table

## Problem Description The task is to create a class, SparseVector, which encapsulates the concept of a sparse vector and implements a method to

Design

Array

Medium

compute the dot product of two sparse vectors. A sparse vector is defined as a vector that contains mostly zeros and therefore should not be stored in a typical dense format as that would waste space. The goal is to store such vectors efficiently and perform operations on them. To efficiently store the sparse vector, we can use a dictionary to hold only the non-zero elements, where the keys are the indices of

these elements, and the values are the elements themselves. This way we aren't storing all the zero values, which can dramatically reduce memory usage for very sparse vectors. The SparseVector class has two methods:

2. dotProduct(vec): This method computes the dot product between the vector represented by the current instance of

comprehension that filters out the zero values.

SparseVector and another sparse vector, vec. The dot product of two vectors is computed by multiplying corresponding entries and summing those products. In the case of sparse

1. SparseVector (nums): The constructor takes a list of integers nums and initializes the sparse vector using a dictionary

entries. The follow-up question asks about efficiently computing the dot product if only one of the two vectors is sparse.

Intuition

For the solution, the idea is to leverage the sparsity of the vectors to optimize the dot product computation. Given that most of the

vectors, most of these products will be zero, because they involve multiplications by zero, so we only need to consider the non-zero

elements in the vectors are zeros, we want to perform multiplications only for the non-zero elements. By converting the vectors into a dictionary structure with non-zero elements, we can quickly identify which elements actually need to be multiplied.

### In the dotProduct method, we iterate over the items in the smaller dictionary (to optimize the number of iterations) and multiply values by the corresponding values in the other dictionary, if they exist. If an index does not exist in the other dictionary, it means

that the value for that index in the other vector is zero and thus does not contribute to the dot product. Therefore, we use the .get method to handle such cases, which allows us to specify a default value of 0 when an index is not found. When dealing with one sparse and one non-sparse vector, the current approach still works efficiently because the dot product will

focus on iterating over the non-zero elements of the sparse vector and lookup the corresponding values in the non-sparse vector.

Solution Approach The implementation of the SparseVector solution makes use of two main aspects: Python dictionaries and the concept of dictionary comprehension for building a structure to represent the sparse vectors.

Algorithm and Data Structure • Dictionary for Sparse Representation: A Python dictionary is an ideal data structure for representing a sparse vector. It allows

storing key-value pairs where the key is the index of a non-zero element in the original vector, and the value is the non-zero

element itself. This structure is memory efficient since we only store entries for non-zero elements.

# We use a dictionary comprehension in the constructor to iterate over nums using enumerate to get both the index i and the

Constructor \_\_init\_\_:

value v together.

 dotProduct Method: We receive another SparseVector object, vec, and we want to compute the dot product with the current sparse vector

The resulting dictionary self.d holds only the elements of the input list that are non-zero, along with their indices.

The condition if v ensures that we're only storing the non-zero values (as zero is considered False in Python).

 We access the internal dictionaries of the current instance (a) and the vec (b) — these dictionaries store the indices and values of the non-zero entries.

instance.

the zero values of the larger vector and only iterate over the potential non-zero counterparts. • We then use a generator expression to iterate over the items of a: for i, v in a.items().  $\circ$  For each element, we calculate the product v \* b.get(i, 0). The get method of the dictionary is very handy in this case, as

By comparison of the lengths of these two dictionaries, we choose to iterate over the smaller dictionary (here represented

as a). This is an optimization step; since the dot product will be zero for all indices not present in both vectors, we can skip

**Pattern Used** 

Efficient Computation with Sparse Representation: By representing the vectors in a sparse form, computations are made more

• Iterating Over a Smaller Set: Choosing to iterate over the smaller set of elements to reduce the number of operations is a

Combining these algorithms and patterns, the SparseVector class efficiently implements the computation of a dot product between

it will return of if the index i doesn't exist in b—a common occurrence with sparse vectors, and also safe considering the

By using a compressed representation for the vectors with dictionaries and strategically leveraging the sparsity, the implementation

To find the dot product of sparseA and sparseB, we invoke the dotProduct method on one of them, let's say

two sparse vectors, considering only the meaningful, non-zero elements, and thus avoiding unnecessary computations.

Finally, the sum function accumulates all the products to give us the result of the dot product.

efficient since we ignore all zero-product cases which would contribute nothing to the final sum.

default value for any index not in the dictionary would be zero.

common optimization strategy in algorithms involving collection processing.

maximizes efficiency in terms of both time and space complexity.

Let's walk through a small example to illustrate the solution approach.

### **Example Walkthrough**

- Suppose we have two sparse vectors represented as follows: Vector A: [1, 0, 0, 2, 0] Vector B: [0, 3, 0, 4, 0]
- sparseB. When initializing these objects, our dictionary comprehension will filter out the zeroes and store only the non-zero elements and their indices:

sparseA's internal dictionary will have the elements {0: 1, 3: 2}, corresponding to indices and values (index 0 has value 1, and

Using the given solution approach, we first convert these lists into SparseVector objects. Let's call these objects sparseA and

### sparseA.dotProduct(sparseB).

Here's a step-by-step explanation:

called the method on it.

sparseB.

Python Solution

class SparseVector:

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from typing import List

index 3 has value 2).

1. Inside the dotProduct method, we compare the sizes of the internal dictionaries of sparseA and sparseB. Since both have two elements, we can choose either one to iterate over, but for the sake of this example, we will iterate over sparseA because we

dictionary. We have two iterations in our loop:

sum and thus the dot product of A and B is 8.

def \_\_init\_\_(self, nums: List[int]):

SparseVector(int[] nums) {

if (nums[i] != 0) {

for (int i = 0; i < nums.length; ++i) {</pre>

// Return the dotProduct of two sparse vectors

if (largerMap.size() < smallerMap.size()) {</pre>

for (var entry : smallerMap.entrySet()) {

int index = entry.getKey();

// SparseVector v1 = new SparseVector(nums1);

// SparseVector v2 = new SparseVector(nums2);

Map<Integer, Integer> temp = smallerMap;

public int dotProduct(SparseVector vec) {

smallerMap = largerMap;

largerMap = temp;

nonZeroElements.put(i, nums[i]);

Map<Integer, Integer> smallerMap = nonZeroElements;

Map<Integer, Integer> largerMap = vec.nonZeroElements;

# Return the dot product of two sparse vectors

def dotProduct(self, vec: "SparseVector") -> int:

# Store the non-zero elements with their indices as keys

# For efficiency, iterate through the smaller vector

# overlapping elements of the two sparse vectors

else (vec.non\_zero\_elements, self.non\_zero\_elements)

# Calculate the dot product by summing the product of the

self.non\_zero\_elements = {i: v for i, v in enumerate(nums) if v != 0}

if len(self.non\_zero\_elements) < len(vec.non\_zero\_elements) \</pre>

// Constructor to populate the map with non-zero elements from the input array

// Reference to the smaller of the two maps to iterate over for efficiency

// Swap if 'vec's map has fewer elements to iterate over the smaller map

// Iterating through the smaller map and multiplying the matching values

// This map will store the non-zero values of the sparse vector associated with their indices

int productSum = 0; // The result of the dot product operation

smaller\_vector, larger\_vector = (self.non\_zero\_elements, vec.non\_zero\_elements) \

sparseB's internal dictionary will have the elements {1: 3, 3: 4}.

 Second iteration: For index 3 in sparseA, there is a matching index in sparseB which has the value 4. We perform the multiplication 2 (from sparseA) \* 4 (from sparseB) which equals 8. 3. We sum the results of the multiplications. In this example, the only non-zero result came from the second iteration (8), so the

2. We now loop over the items in sparseA's dictionary. For each item, we look up whether the corresponding index is in sparseB's

• First iteration: For index 0 in sparseA, there is no corresponding index in sparseB. When we attempt to multiply 1 (from

sparseA) with sparseB.get(0, 0) (using .get to specify a default value of 0), the result is 0 since index 0 is not present in

approach, taking advantage of the sparse representation by only considering non-zero elements and their indices in the computations.

In conclusion, the SparseVector class successfully computes the dot product of sparseA and sparseB as 8 using an efficient

- 17 return sum(value \* larger\_vector.get(index, 0) for index, value in smaller\_vector.items()) 19 # Example usage: 20 # v1 = SparseVector(nums1) 21 + v2 = SparseVector(nums2)22 # ans = v1.dotProduct(v2)
- Java Solution import java.util.HashMap; import java.util.Map; class SparseVector { // Using a HashMap to efficiently store non-zero elements and their positions private Map<Integer, Integer> nonZeroElements = new HashMap<>();

### 34 int value = entry.getValue(); 35 productSum += value \* largerMap.getOrDefault(index, 0); 36 37 return productSum; // Return the computed dot product 38 39

C++ Solution

1 #include <vector>

2 #include <unordered\_map>

using namespace std;

6 class SparseVector {

public:

// Example of usage:

// int ans = v1.dotProduct(v2);

// Class to represent a Sparse Vector

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unordered map<int, int> indexToValueMap;
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       // Constructor which takes a vector of integers and populates the indexToValueMap
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       SparseVector(vector<int>& nums) {
            for (int i = 0; i < nums.size(); ++i) {
               if (nums[i] != 0) {
                    indexToValueMap[i] = nums[i];
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       // Return the dot product of this sparse vector with another sparse vector vec
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       int dotProduct(SparseVector& vec)
           // Using references to the internal maps for easier access
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           auto& thisVectorMap = indexToValueMap;
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           auto& otherVectorMap = vec.indexToValueMap;
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           // Optimize by iterating over the smaller map
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           if (thisVectorMap.size() > otherVectorMap.size()) {
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                swap(thisVectorMap, otherVectorMap);
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           int total = 0;
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           // Compute dot product by only considering non-zero elements
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           for (auto& [index, value] : thisVectorMap) {
                if (otherVectorMap.count(index)) {
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                    total += value * otherVectorMap[index];
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           return total;
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  };
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   // Usage example:
  // vector<int> nums1 = { ... };
  // vector<int> nums2 = { ... };
47 // SparseVector v1(nums1);
48 // SparseVector v2(nums2);
   // int product = v1.dotProduct(v2);
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Typescript Solution
   // Object to encapsulate sparse vector data and operations
  2 const sparseVectorOperations = {
         sparseVectorData: new Map<number, Map<number, number>>(),
         // Function to initialize a sparse vector from a given array of numbers
         createSparseVector: function(nums: number[], vectorId: number): void {
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```

### 28 let result = 0; 29 30 // Calculate dot product by iterating through the map with fewer elements 31 for (const [index, value] of smallerMap) { 32 if (largerMap.has(index)) {

// Example usage:

return result;

Time and Space Complexity

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const sparseData = new Map<number, number>();

if (nums[index] !== 0) {

let smallerMap = vec1Data;

smallerMap = vec2Data;

largerMap = vec1Data;

if (vec1Data.size > vec2Data.size) {

42 sparseVectorOperations.createSparseVector([1, 0, 0, 2, 3], 1);

43 sparseVectorOperations.createSparseVector([0, 3, 0, 4, 0], 2);

let largerMap = vec2Data;

for (let index = 0; index < nums.length; ++index) {</pre>

sparseData.set(index, nums[index]);

// Function to calculate the dot product of two sparse vectors identified by their IDs

// Swap if veclData has more elements than vec2Data to minimize iterations

44 const dotProductResult = sparseVectorOperations.calculateDotProduct(1, 2); // Should calculate the dot product

calculateDotProduct: function(vectorId1: number, vectorId2: number): number {

const vec1Data = this.sparseVectorData.get(vectorId1) || new Map();

const vec2Data = this.sparseVectorData.get(vectorId2) || new Map();

result += value \* (largerMap.get(index) || 0);

console.log(dotProductResult); // Outputs the result of the dot product calculation

this.sparseVectorData.set(vectorId, sparseData);

# **Time Complexity:** The constructor \_\_init\_\_ has a time complexity of O(n) where n is the number of elements in nums, as it needs to iterate through all

elements to create the dictionary with non-zero values. The dotProduct function has a time complexity of O(min(k, 1)) where k and 1 are the number of non-zero elements in the two SparseVectors, respectively. This is because the function iterates over the smaller of the two dictionaries (after ensuring a has the

smaller length, swapping if necessary) and attempts to find matching elements in the larger one. The get operation on a dictionary has an average case time complexity of 0(1). **Space Complexity:** The space complexity of the  $_{init}$  function is 0(k), where k is the number of non-zero elements in nums, since the space required

The dotProduct function operates in 0(1) space complexity because it calculates the sum on the fly and does not store intermediate results or allocate additional space based on input size, other than a few variables for iteration and summing.

depends on the stored non-zero elements.