1428. Leftmost Column with at Least a One

Medium Array **Binary Search** Interactive Matrix

Problem Description

smallest column index across all rows.

1's. The task is to find the index of the leftmost column that contains at least one '1'. If there's no such column, we return -1. Access to the matrix is restricted to two operations. One is BinaryMatrix.get(row, col), which returns the value at a specified row

The given problem presents a binary matrix with rows sorted in a non-decreasing order. That means each row transitions from 0's to

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and column, and the other is BinaryMatrix.dimensions(), which returns the number of rows and columns. A key constraint is that any solution must limit the number of calls to BinaryMatrix.get to 1000, making straightforward solutions like

scanning every element inefficient and infeasible. Intuition

The problem is essentially asking us to find the smallest column index that contains the value '1'. Given that each row is sorted, a linear scan from the leftmost column to the rightmost in each row would be wasteful since we might traverse a lot of zeros before

finding a one, especially in large matrices. Instead, the optimal approach is to utilize binary search within each row. Binary search can quickly home in on a '1' in a sorted array by repeatedly halving the search space. For each row, we perform a binary search to find the leftmost '1'. We keep track of the

With the provided solution, we iterate over each row and perform a binary search. If we find a '1', we update the result to be the minimum of the current result and the column index where '1' was found.

The binary search within each row is optimized with the condition while left < right, which keeps narrowing down the range until

left and right converge. When they converge, we check if the leftmost position contains a '1' to consider it as a candidate for our answer.

Since we are only making a couple of calls to BinaryMatrix.get per row (one for each step of the binary search), we stay within the limit of 1000 calls and arrive at an efficient solution.

The solution follows the Binary Search algorithm to narrow down the leftmost column that contains a '1'. Since we know that each row is sorted, this property allows us to use binary search to efficiently find the first occurrence of '1' per row, if it exists.

The process of binary search starts by initializing two pointers, left and right, which represent the range of columns we're

calculated by averaging left and right.

the binary matrix, so we return -1.

Example Walkthrough

the leftmost '1' for that row or there is no '1' in that row.

Solution Approach

We then enter a loop that continues to narrow down the range by checking if the mid position contains a '0' or a '1'. If a '1' is found, it means we should continue our search to the left side of mid to find the leftmost '1', so we set right to mid. If a '0' is found, we move

our search to the right side by setting left to mid + 1. The loop stops once left and right meet, which means we have either found

searching in. At the start, left is set to 0, and right is set to the last column index cols - 1. The middle of the range, mid, is then

A key detail in this implementation is that after the binary search per row, an additional check is done on the left position. If BinaryMatrix.get(row, left) returns '1', then we potentially found a new leftmost '1', and we update the result res accordingly. We use res to store the current smallest index where a '1' was found across all rows processed until that point, initializing it with -1. This step is crucial as it allows us to progressively update the position of the leftmost '1' column, and by the end of the row iterations,

we will have the index of the overall leftmost column with a '1'. If res remains -1 by the end of the loops, it means there were no '1's in

The algorithm efficiently leverages the sorted property of the rows and minimizes reads, ensuring we stay within the 1000_api_calls limit while still achieving a time complexity of O(logN), where N is the number of columns, multiplied by the number of rows M, yielding an overall time complexity of O(MlogN).

Let's illustrate the solution approach with a small example. Consider the binary matrix: [0, 0, 0, 1],

1. We start by getting the dimensions of the matrix. Let's assume dimensions are 4 rows and 4 columns.

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• We recalculate mid = (left + right) / 2, which is now 2. Again, BinaryMatrix.get(0, mid) is 0, so we move left to mid +

that if a '1' exists in this row, it must be to the right. So we move left to mid + 1.

3. We loop through each row and perform a binary search within that row:

Now left is 3, and our loop terminates since left >= right.

The fourth row has no '1's, so it doesn't change res.

Get the dimensions of the binary matrix

if binaryMatrix.get(row, left) == 1:

if (binaryMatrix.get(row, left) == 1) {

result = Math.min(result, left);

// Function to find the leftmost column with a 1 in a binary matrix

int result = -1; // Initialize result to -1 to indicate no 1 found

int right = cols - 1; // Ending index of the current row

// Binary search to find the leftmost 1 in the current row

// Starting index of the current row

int leftMostColumnWithOne(BinaryMatrix& binaryMatrix) {

// Retrieve the dimensions of the binary matrix

int cols = dimensions[1]; // Number of columns

int rows = dimensions[0]; // Number of rows

for (int row = 0; row < rows; ++row) {</pre>

int left = 0;

vector<int> dimensions = binaryMatrix.dimensions();

// Iterate through each row to find the leftmost 1

result = left;

return result;

// Update the result with the new found column with a '1'.

if (result == -1) { // If it's the first '1' found in any of the rows.

// Return the result. If no '1' was found, -1 will be returned, indicating such.

} else { // If it's not the first, we take the lesser (more left) of the two columns.

rows, cols = binaryMatrix.dimensions()

left, right = 0, cols - 1

def leftMostColumnWithOne(self, binaryMatrix: 'BinaryMatrix') -> int:

Iterate over each row to find the leftmost column with a 1

Initialize result as -1 to represent no 1's found yet

We need to find the leftmost column that contains a '1'. Here's how we approach the problem:

2. We initialize our result (res) to -1, which would be the final answer if there's no '1' in the matrix.

• After the loop, we check BinaryMatrix.get(0, left), which is 1, meaning we've found a column with a '1'. We update res to left, which is 3, the current smallest index of a found '1'.

 \circ For the first row, we initialize left = 0 and right = 3 (since there are 4 columns, indices start from 0).

- - now res becomes 1. • The third row also leads to updating res to min(res, left) after binary search, but since the leftmost '1' is in column 2, res remains 1.

5. Finally, since we have gone through all rows, res holds the index of the leftmost column containing a '1', which in this example is

• For the second row, our binary search will quickly converge to left = 1, the first '1'. We update res to min(res, left), so

• We calculate the middle, mid = (left + right) / 2, which is initially 1. Since BinaryMatrix.get(0, mid) is 0, we now know

This approach limits the number of calls to BinaryMatrix.get to 2-3 per row, which is well below the limit of 1000 and is efficient

4. We repeat this for the remaining rows:

even for large matrices, with a final time complexity of O(MlogN). **Python Solution**

Perform a binary search to find the leftmost 1 in the current row 10 while left < right:</pre> 11 12 mid = (left + right) // 2 # Use integer division for Python 3 if binaryMatrix.get(row, mid) == 1: 13 right = mid # Move the right pointer to the middle if a 1 is found 14

left = mid + 1 # Move the left pointer past the middle otherwise

If a 1 is found and result is -1 (first 1 found), or if the current column

After exiting the loop, check if the current leftmost index contains a 1

is less than the previously recorded result, update result

22 result = left if result == -1 else min(result, left) 23 # Return the result, which is the index of the leftmost 1 or -1 if no 1 is found 24 return result 25

Java Solution

class Solution:

result = -1

for row in range(rows):

else:

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// Define the solution class implementing the algorithm to find the leftmost column with at least one '1' in a binary matrix.
 2 class Solution {
       // Method to find the leftmost column index with a '1'.
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       public int leftMostColumnWithOne(BinaryMatrix binaryMatrix) {
           // Retrieve the dimensions of the binary matrix.
           List<Integer> dimensions = binaryMatrix.dimensions();
            int rows = dimensions.get(0); // Number of rows in the binary matrix.
            int cols = dimensions.get(1); // Number of columns in the binary matrix.
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           // Initial result is set to -1 (indicating no '1' has been found yet).
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            int result = -1;
13
           // Iterate through each row to find the leftmost '1'.
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            for (int row = 0; row < rows; ++row) {</pre>
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               // Initialize pointers for the binary search.
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                int left = 0;
                int right = cols - 1;
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               // Perform binary search in the current row to find the '1'.
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               while (left < right) {</pre>
22
                    // Calculate middle index.
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                    int mid = left + (right - left) / 2; // Avoids potential overflow.
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                    // Check the value at the middle index and narrow down the search range.
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                    if (binaryMatrix.get(row, mid) == 1) {
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                        // '1' is found, shift towards the left (lower indices).
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                        right = mid;
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                    } else {
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                        // '0' is found, shift towards the right (higher indices).
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                        left = mid + 1;
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// After the loop, 'left' is the position of the leftmost '1' or the first '0' after all '1's in this row.

while (left < right) {</pre> 19 20 21 22

C++ Solution

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1 class Solution {

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// Find the middle index
                     int mid = (left + right) / 2; // The '>> 1' has been replaced with '/ 2' for clarity
                     if (binaryMatrix.get(row, mid) == 1) {
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                         // If a 1 is found, narrow the search to the left half
                         right = mid;
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                     } else {
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                         // If a 0 is found, narrow the search to the right half
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                         left = mid + 1;
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                 // After binary search, check if we have found a 1 at the 'left' index
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                 // and update the result accordingly
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                 if (binaryMatrix.get(row, left) == 1) {
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                     // If this is the first 1 found, or if the current index is smaller than previous one
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                     if (result == −1) {
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                         result = left; // update the result with the current index
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                     } else {
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                         result = min(result, left); // update the result with the smaller index
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             // Return the result
             return result;
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    };
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Typescript Solution
  1 // Interface representing the BinaryMatrix's methods for TypeScript type checking
    interface BinaryMatrix {
         get(row: number, col: number): number;
         dimensions(): number[];
  5
    // Variable to hold the leftmost column with a 1 in a binary matrix
     let leftMostColumnResult: number = −1;
    // Function to find the leftmost column with a 1 in a binary matrix
    function leftMostColumnWithOne(binaryMatrix: BinaryMatrix): number {
         // Retrieve the dimensions of the binary matrix
         let dimensions: number[] = binaryMatrix.dimensions();
         let rows: number = dimensions[0]; // Number of rows
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         let cols: number = dimensions[1]; // Number of columns
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         leftMostColumnResult = -1; // Initialize the result to -1 to indicate no 1 has been found
 18
 19
        // Iterate through each row to find the leftmost 1
 20
         for (let row = 0; row < rows; ++row) {</pre>
 21
                               // Starting index of the current row
             let left = 0;
 22
             let right = cols - 1; // Ending index of the current row
 23
```

38 // After binary search, check if we have found a 1 at the 'left' index // and update the result accordingly 39 if (binaryMatrix.get(row, left) === 1) { 40 41 // If this is the first 1 found, or if the current index is smaller than the previously found one if (leftMostColumnResult === -1) { 42 43 leftMostColumnResult = left; // Update the result with the current index

54 // Example usage:

while (left < right) {</pre>

} else {

} else {

// Return the result

return leftMostColumnResult;

// Find the middle index

right = mid;

left = mid + 1;

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// console.log(leftMostColumnWithOne(matrix));

Time and Space Complexity

Time Complexity The provided code loops through each row of the binary matrix to find the leftmost column containing a 1. For each row, the code implements a binary search which has a logarithmic time complexity. Since the binary search is conducted for each of the rows, the

leftMostColumnResult = Math.min(leftMostColumnResult, left); // Update the result with the smaller index

 We iterate over each row once: 0(rows) For each row, a binary search is conducted within cols, which takes O(log(cols))

total time complexity is 0(rows * log(cols)).

Here's the breakdown of the time complexity:

Thus, the combined time complexity is 0(rows * log(cols)).

// Binary search to find the leftmost 1 in the current row

// If a 1 is found, narrow the search to the left half

// If a 0 is found, narrow the search to the right half

if (binaryMatrix.get(row, mid) === 1) {

55 // let matrix: BinaryMatrix = new SomeBinaryMatrixImplementation();

let mid = Math.floor((left + right) / 2); // Use floor to avoid decimal indices

Space Complexity

The space complexity is 0(1) since we are only using a constant amount of extra space. The variables res, left, right, mid, and the loop counter row do not depend on the size of the input and use a fixed amount of space.