1770. Maximum Score from Performing Multiplication Operations **Dynamic Programming** Array **Leetcode Link** Hard

## You are given two arrays nums and multipliers. Array nums is of size n, and multipliers is of size m, with the condition that n >= m.

**Problem Description** 

Each operation consists of the following steps:

You start with a score of 0 and intend to perform exactly m operations to maximize your score.

to your score.

3. Remove x from nums.

and return this maximum score.

state and store it in f[i][j].

1. Select an integer x from either the start or end of the array nums. 2. Multiply x by the corresponding multipliers[i] (where i is the index of the current operation, starting at 0) and add the result

The challenge is to figure out the sequence of operations that leads to the maximum possible score after performing moperations,

Intuition

To solve this problem, we use dynamic programming to keep track of the highest score we can achieve after a certain number of operations. Specifically, we create a 2D array f where f[i][j] represents the maximum score we can achieve by selecting i elements from the start and j elements from the end of nums. The value of k in the code represents the current operation we're on,

# and ans will store our final answer.

Here's the intuition behind the solution step by step: 1. We prepare a 2D DP array f with dimensions  $(m + 1) \times (m + 1)$  where each cell is initially filled with negative infinity (-inf)because we want to calculate the maximum. The +1 ensures we have space for zero selections from both ends.

3. For each possible set of selections from the start and end (represented by i and j respectively), calculate the score for that

4. For the state represented by f[i][j], we consider two possibilities: ∘ f[i - 1][j] + multipliers[k] \* nums[i - 1]: This corresponds to selecting the element x from the start of the array.

2. Set f[0][0] to 0 as the base case, which represents that no operation has been performed yet and the score is zero.

 $\circ$  f[i][j - 1] + multipliers[k] \* nums[n - j]: This corresponds to selecting the element x from the end of the array. 5. Take the maximum of these two values to find the optimal score for that particular operation.

6. If the sum of i and j is equal to m (meaning all operations have been used), update ans to track the highest score found up to

that point.

7. After evaluating all possible combinations of selections from nums, return the maximum score ans. This approach ensures that at every step, we are considering all possible choices and computing the optimal score that can be

Solution Approach The solution approach uses dynamic programming, a method for solving a complex problem by breaking it down into simpler

• Initialization: Create a 2D list f of size (m + 1) x (m + 1), where m is the length of the multipliers array, and set all elements to

• Nested Loops: Two nested loops iterate over all possibilities where i represents the number of elements selected from the start,

and j represents the number of elements selected from the end. Since the problem requires exactly m operations, the outer loop

• If i > 0, meaning we can select from the start, update f[i][j] with the maximum of its current value or the value from

subproblems. It is applicable here because the decision at each step depends on the results of previous steps, and there are

-inf. This represents the maximum possible scores. Additionally, set f[0][0] to 0 as a starting point since no operations mean no score.

Update f[i][j] according to the dynamic programming state transition equation:

achieved given the previous decisions, thereby solving the problem optimally.

### • State Update: For each (i, j) pair: $\circ$ Calculate the index k = i + j - 1, which represents the operation number.

and f[i][j].

Example Walkthrough

1 nums = [1, 2, 3]

1 f = [

2 multipliers = [3, 2]

need to perform 2 operations.

f[0] [0] to 0. The table looks like this:

overlapping subproblems.

The implementation details are as follows:

ranges from 0 to m, inclusive, ensuring  $i + j \ll m$ .

contain the maximum score possible. Hence, return ans.

choosing the start (f[i-1][j] + multipliers[k] \* nums[i-1]). • If j > 0, meaning we can select from the end, update f[i][j] with the maximum of its current value or the value from choosing the end (f[i][j-1] + multipliers[k] \* nums[n-j]). Check if i + j equals m, that is, if we have performed m operations. If so, update ans with the maximum of its current value

• Answer Calculation: After populating the f table with all possible scores, ans, which has been tracking the maximum, will

By storing and updating the maximum score at each state, the solution efficiently computes the maximum score possible after m

operations. This dynamic programming table eliminates the need to recompute overlapping subproblems and ensures each

subproblem is solved only once. The final answer is found by considering all possible ways to perform the moperations.

Let's illustrate the dynamic programming solution approach with a small example. Suppose we have:

Following the solution approach: 1. Initialization: We create a 2D list f with dimensions  $(3 \times 3)$  (since m + 1 = 2 + 1 = 3), initializing all elements to -inf. Then, set

2. Nested Loops: We iterate through all combinations of i (selections from the start) and j (selections from the end). Our loops will

Here, n = 3 (size of nums) and m = 2 (size of multipliers). As per the problem, we have to perform m operations, so in this case, we

## Perform state updates

For j = 0 to 2

1 For i = 0 to 2

[0, -inf, -inf],

[-inf, -inf, -inf],

[-inf, -inf, -inf]

• We can take from the start: f[1][0] gets updated to max(-inf, 0 + 3 \* nums[0]) which is 3.  $\circ$  When i = 0 and j = 1, k = 0:

■ We can take from the end: f[0][1] gets updated to max(-inf, 0 + 3 \* nums[2]) which is 9.

 $\circ$  Take from the start: f[1][1] can become max(-inf, f[0][1] + 2 \* nums[0]) which is 9 + 2 \* 1 = 11.

We continue doing this to fill out our table f. After the first set of operations, part of our table looks like this:

cover (i, j) pairs such as (0, 0), (1, 0), (0, 1), and so on, but will not exceed i + j = m:

If i + j <= 2 // This is our operation limit `m`</pre>

3. State Update: We update f[i][j] for each (i, j) pair:

check f[2][0], f[1][1], and f[0][2] to find our answer.

Continuing the update process with i and j values:

After updating all values, our table f looks like this:

• When i = 1 and j = 1, k = 1:

f[1][1] becomes 11.

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**}**;

dp[0][0] = 0;

int maxScore = minInt;

Java Solution

class Solution {

import java.util.Arrays;

[0, 9, -inf],

[3, 11, -inf],

class Solution:

dp[0][0] = 0

max\_score = float('-inf')

if left\_count > 0:

if right\_count > 0:

public int maximumScore(int[] nums, int[] multipliers) {

Arrays.fill(dp[i], Integer.MIN\_VALUE);

for (int i = 0;  $i \le m$ ; i++) {

for (int i = 0;  $i \le m$ ; ++i) {

**if** (left > 0) {

if (i - left > 0) {

int n = nums.length; // The length of the nums array

dp[0][0] = 0; // Base case: no operation gives score of 0

// Outer loop goes through all possible counts of operations

for (int left = 0; left <= m - i; ++left) {</pre>

int right = i + left - 1;

int m = multipliers.length; // The length of the multipliers array

[-inf, -inf, -inf]

• When i = 1 and j = 0, k = 0:

[0, 9, -inf],[3, -inf, -inf], [-inf, -inf, -inf] 4. Answer Calculation: We check f[i][j] values where i + j = m to update ans, the maximum score so far. Since m = 2, we will

 $\circ$  Take from the end: f[1][1] can become max(-inf, f[1][0] + 2 \* nums[2]) which is 3 + 2 \* 3 = 9. Since 11 is greater,

Thus, the final answer is 11; it's the maximum score we can get by performing 2 operations using the given nums and multipliers.

Python Solution from typing import List

dp = [[float('-inf')] \* (multipliers\_length + 1) for \_ in range(multipliers\_length + 1)]

dp[left\_count][right\_count] = max(dp[left\_count][right\_count],

dp[left\_count][right\_count] = max(dp[left\_count][right\_count],

def maximumScore(self, nums: List[int], multipliers: List[int]) -> int:

# The starting score is 0 when no multipliers have been applied

# Initialize the dp (Dynamic Programming) array with negative infinity

# Loop through all the possible combinations of left and right operations

for right\_count in range(multipliers\_length - left\_count + 1):

current\_multiplier\_index = left\_count + right\_count - 1

# Calculate the score if we take the number from the left

# Calculate the score if we take the number from the right

# If we have used all multipliers, update the maximum score

max\_score = max(max\_score, dp[left\_count][right\_count])

int[][] dp = new int[m + 1][m + 1]; // DP array to store the intermediate solutions

int maxScore = Integer.MIN\_VALUE; // Variable to keep track of the maximum score

// Inner loop considers different splits between left and right operations

// Initialize all values in the DP array to a very small number to ensure there's no overcount

// If we can take a left operation, update the DP value considering the left pick

// If we can take a right operation, update the DP value considering the right pick

if left\_count + right\_count == multipliers\_length:

num\_length, multipliers\_length = len(nums), len(multipliers)

# The length of the nums and multipliers arrays

# To accommodate for potential negative scores

# Initialize the answer with negative infinity

for left\_count in range(multipliers\_length + 1):

# The index of the current multiplier

Our maximum score ans is the maximum value in f where i + j = m, which in this case is f[1][1] = 11.

37 # Return the maximum score after using all multipliers 38 39 return max\_score 40

// This method calculates the maximum score from performing operations on the array `nums` using the `multipliers`.

dp[left\_count - 1][right\_count] + multipliers[current\_multiplier\_index] \* num

dp[left\_count][right\_count - 1] + multipliers[current\_multiplier\_index] \* num

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                   // If we have used all multipliers, update the maximum score if the current one is higher
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                   if (i == m) {
                       maxScore = Math.max(maxScore, dp[left][i - left]);
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           return maxScore; // Return the maximum score found
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40 }
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C++ Solution
  1 class Solution {
  2 public:
         int maximumScore(vector<int>& nums, vector<int>& multipliers) {
             // No need for such a large negative initial value, as scores can be negative.
             // Let's use the minimum possible value for integers.
             const int minInt = numeric_limits<int>::min();
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             // Size of the nums and multipliers arrays.
             int numSize = nums.size(), multiplierSize = multipliers.size();
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             // Initializing a DP table where f[i][j] represents the maximum score possible
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             // using the first i elements from the beginning and the first j elements
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             // from the end of nums, after applying i + j multipliers.
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vector<vector<int>> dp(multiplierSize + 1, vector<int>(multiplierSize + 1, minInt));

// Update the dp value for picking from the beginning of nums.

// Update the dp value for picking from the end of nums.

// If we've used all multipliers, compare with maxScore.

dp[i][j] = max(dp[i][j], dp[i-1][j] + multipliers[k] \* nums[i-1]);

dp[i][j] = max(dp[i][j], dp[i][j-1] + multipliers[k] \* nums[numSize - j]);

// Base case: no elements picked and no multipliers applied.

// Variable to store the final maximum score.

for (int i = 0; i <= multiplierSize; ++i) {</pre>

int k = i + j - 1;

if (i > 0) {

if (j > 0) {

// Return the maximum score found.

return maxScore;

Typescript Solution

.fill(0)

dp[0][0] = 0;

// Loop through all valid combinations of picks.

// The kth multiplier to apply.

if (i + j == multiplierSize) {

function maximumScore(nums: number[], multipliers: number[]): number {

const negativeInfinity = Number.MIN\_SAFE\_INTEGER;

// Base case: if no numbers are picked, score is 0.

// Retrieve the lengths of the input arrays.

const multipliersLength = multipliers.length;

const dp = new Array(multipliersLength + 1)

// This will hold the answer to the problem.

for (let i = 0; i <= multipliersLength; ++i) {</pre>

dp[i][j] = Math.max(

if (i + j === multipliersLength) {

maxScore = Math.max(maxScore, dp[i][j]);

// Return the calculated maxScore after considering all possibilities.

dp[i][j],

const multiplierIndex = i + j - 1;

for (let j = 0; j <= multipliersLength - i; ++j) {</pre>

const numLength = nums.length;

let maxScore = negativeInfinity;

if (i > 0) {

if (j > 0) {

);

Time and Space Complexity

// Initialize a large negative number that will never be reached in the problem.

.map(() => new Array(multipliersLength + 1).fill(negativeInfinity));

// Iterate through all possible counts of elements picked from the beginning and end.

// Calculate the index for the current multiplier based on i and j.

// If an element from the front is picked, update the DP table accordingly.

// If an element from the back is picked, update the DP table accordingly.

dp[i][j-1] + nums[numLength - j] \* multipliers[multiplierIndex]

// If all multipliers have been used, consider the result as a possible max score.

rules. The function maximumScore utilizes dynamic programming with a 2D array f to store intermediate results.

// Initialize a DP table with dimensions of multipliersLength + 1 and fill with negative infinity.

maxScore = max(maxScore, dp[i][j]);

for (int j = 0; j <= multiplierSize - i; ++j) {</pre>

dp[left][i - left] = Math.max(dp[left][i - left], dp[left - 1][i - left] + multipliers[right] \* nums[left - 1]);

dp[left][i - left] = Math.max(dp[left][i - left], dp[left][i - left - 1] + multipliers[right] \* nums[n - (i - left]) + multipliers[right] | \* nums[n - (i - left]) | \* nu

#### dp[i][j] = Math.max(dp[i][j], dp[i - 1][j] + nums[i - 1] \* multipliers[multiplierIndex] );

return maxScore;

complexity is added there.

**Time Complexity:** The time complexity depends on two loops that iterate over the range (m + 1). The outer loop variable i runs from 0 to m, and for each value of i, the inner loop variable j runs up to (m - i). This essentially results in a total of roughly m/2 \* m/2 iterations, which can be approximated to  $O(m^2)$  where m is the length of the multipliers list.

The provided Python code aims to find the maximum score from multiplying elements of nums with multipliers based on specific

Moreover, the updates within the if conditions inside the nested loops also operate in constant time. Therefore, no additional

**Space Complexity:** 

Hence, the overall time complexity of this code is  $0(m^2)$ .

The space complexity is determined by the size of the 2D array f, which has dimensions (m + 1) by (m + 1). So the total space used

is (m + 1) \* (m + 1), resulting in a space complexity of  $0(m^2)$  as well. Thus, the overall space complexity of the algorithm is  $0(m^2)$ .