1239. Maximum Length of a Concatenated String with Unique Characters Medium Bit Manipulation String Backtracking Array **Leetcode Link** 

### In this problem, you're given an array of strings named arr. Your task is to create the longest possible string s by concatenating some or all strings from arr. However, there's an important rule: the string s must consist of unique characters only.

**Problem Description** 

In other words, you need to pick a subsequence of strings from arr such that when these strings are combined, no character appears more than once. The length of the resulting string s is your main objective, and you must return the maximum possible length. Remember that a subsequence is formed from the original array by potentially removing some elements, but the order of the

remaining elements must be preserved. Intuition

To find the optimal solution for the maximum length of s, we use a bit manipulation technique known as "state compression". This technique involves using a 32-bit integer to represent the presence of each letter where each bit corresponds to a letter in the

alphabet. The intuition behind this approach is that it allows us to efficiently check whether two strings contain any common characters. We can do this by performing an AND operation (&) on their respective compressed states (masks). If the result is zero, it means there

are no common characters.

3. Iterate through each string s in the array arr. For each string, create a bit mask mask that represents the unique characters in the string.

zero), it means we can concatenate this string without repeating any character.

 If the string has duplicate characters, we set mask to zero and skip it since such a string cannot contribute to a valid s. 4. Iterate through the current masks in masks. We use the AND operation to check if the current string's mask has any overlap with mask. If it doesn't (i.e., the result is

○ In such a case, we combine (OR operation |) the current mask with mask and add the new mask to our masks list.

2. Create a list masks with a single element, zero, to keep track of all unique character combinations we've seen so far.

3. Loop through each string s in the input array arr.

to find the corresponding bit position.

still result in a string with all unique characters.

are considered without duplication, leading to an efficient solution.

Let's walk through a small example to illustrate the solution approach.

For u, ord('u') - ord('a') gives us 20. So, mask becomes 0 | (1 << 20).</li>

∘ For n, ord('n') - ord('a') gives us 13. So, mask becomes mask | (1 << 13).

For q, ord('q') - ord('a') gives us 16. So, mask becomes mask | (1 << 16).</li>

form a new mask: 1048576 | 65792 which in binary is 1000010010000, and in decimal is 1111368.

For u, there's already a bit set in the previous mask, so we skip the creation of a new mask.

After processing iq, our mask is 1000000010000 in binary, which is 65792 decimal.

7. The masks array becomes [0, 1048576, 65792, 1111368].

characters we can create by concatenating strings from arr.

def maxLength(self, arr: List[str]) -> int:

if mask >> char\_index & 1:

mask |= 1 << char\_index

# Add the character to the mask

for existing\_mask in masks.copy():

if existing\_mask & mask == 0:

return max\_length # return the maximum length found

for char in string:

mask = 0

public int maxLength(List<String> arr) {

for (String s : arr) {

int bitMask = 0;

// Iterate over each string in the list.

bitMask = 0;

int currentSize = bitMasks.size();

for (int i = 0; i < currentSize; ++i) {</pre>

int combinedMask = bitMasks.get(i);

if ((combinedMask & bitMask) == 0) {

return maxLen; // Return the maximum length found.

int maxLength(std::vector<std::string>& arr) {

// Iterate over all strings in the input vector

std::vector<int> masks = {0};

// Import necessary functions from built—in modules

const popCount = (n: number): number => {

15 const maxLength = (arr: string[]): number => {

// Iterate over all strings in the input array

// Add the current character to the mask

// Create a copy of the current masks to iterate over

import { max } from 'lodash';

let masks: number[] = [0];

for (const ch of str) {

mask |= 1 << bitIndex;</pre>

if (mask === 0) return;

const currentMasks = [...masks];

if ((mask >> bitIndex) & 1) {

arr.forEach(str => {

mask = 0;

break;

let count = 0;

count += n & 1;

while (n) {

n >>= 1;

return count;

10

11

13

16

18

19

20

21

22

24

25

26

27

28

29

30

31

32

33

34

35

36

37

38

39

40

41

42

43

44

52

53

54

55

56

57

58

60

63

59 };

12 };

int max\_length = 0; // to store the max length of unique characters

// masks initially contains only one element: "0", which represents an empty string

// Utility function to count the number of set bits (1s) in the binary representation of a number

// Function to compute the max length of a concatenated string of unique characters

// Masks initially contains only one element: 0, which represents an empty string

// Check if this character has already appeared in the string (mask)

maxLength = max([maxLength, popCount(combinedMask | mask)])!;

// Return the maximum length of a string with all unique characters

// console.log(maxLength(["un", "iq", "ue"])); // Should print 4

// If the character repeats, discard this string by setting the mask to 0 and break

// Only proceed if mask is not zero (valid string without any repeating character)

let maxLength = 0; // To store the max length of unique characters

let mask = 0; // Bitmask to represent the current string

let bitIndex = ch.charCodeAt(0) - 'a'.charCodeAt(0);

// Iterate over each character in the current string

// we can combine them into a new mask.

break;

if (bitMask == 0) {

continue;

for (int i = 0; i < s.length(); ++i) {</pre>

if (((bitMask >> bitIndex) & 1) == 1) {

break

**if** mask != 0:

Consider the input array of strings arr as ["un", "iq", "ue"].

combination of characters from both masks. We add this new mask to masks.

Here's a step-by-step breakdown of how we arrive at the solution:

1. Initialize a variable ans to zero. This will hold the maximum length found.

- Update ans with the count of set bits in the new mask, which represents the length of the unique character string formed up to this point. This is done using the built-in bit\_count() method on the new mask. 5. Finally, return the maximum length ans found during the process.
- The use of state compression and bit manipulation makes the solution efficient, as it simplifies the process of tracking which characters are present in the strings and eliminates the need for complex data structures or string operations.
- The algorithm follows these steps: 1. Initialize an integer ans with the value 0, which will track the maximum length of a string with unique characters found during the process.

The solution uses two significant concepts: bit manipulation for state compression and backtracking to explore all combinations.

will have a 1 in the position corresponding to a letter (where a is the least significant bit, and z is the most significant). As we iterate over each character c in the string s, we calculate the difference between the ASCII value of c and that of 'a'

For each string s, we create an integer mask that serves as its unique character identifier. The binary representation of mask

2. We begin with an array masks that starts with a single element, 0, to record the baseline state (the empty string).

# 1 i = ord(c) - ord('a')

1 if mask >> i & 1:

1 if m & mask == 0:

1 masks.append(m | mask)

previous maximum.

Example Walkthrough

our masks to be [0, 1048576].

1 ans = max(ans, (m | mask).bit\_count())

mask = 0

**Solution Approach** 

We then check if the bit at that position is already set. If so, it means the character has appeared before, and we break the

break Otherwise, we set the bit corresponding to the character in the mask. 1 mask |= 1 << i

• For each existing m in masks, we ensure there's no overlap between m and the current mask using the bitwise AND operation.

If there's no overlap, it means that adding the current string's unique characters to the characters represented by m would

In that case, we combine m and mask using the bitwise OR operation. The result is a new mask representing a unique

• If the current string s has any duplicate characters, we disregard this mask and move on to the next string in arr. 4. Next, for each mask computed from the current string, we examine the masks collected so far.

loop, setting mask to 0, as this string cannot be part of the result due to the duplicate character.

 We then calculate the total number of unique characters we have so far with the new mask by counting the number of set bits. In Python, this can be done with the .bit\_count() method. We update our answer ans if this count is greater than the

5. Once we've checked all strings and recorded all possible unique character combinations, we return the value of ans, which

represents the maximum length of a string with all unique characters we can create by concatenating a subsequence of arr.

The use of bit masks elegantly handles the uniqueness constraint, and the iterative approach ensures that all potential combinations

1. Start by initializing ans to 0 and masks to [0]. 2. The first string is un.

4. The next string is iq. For i, ord('i') - ord('a') gives us 8. So, mask becomes 0 | (1 << 8).</li>

5. Check this mask against all in masks. There's no common bit set with 1048576 (previous mask). Therefore, we can combine them to

6. Update ans with the bit count of the new mask. It has 4 bits set, representing 4 unique characters. ans becomes 4.

9. There are no more strings to process. We return the ans, which is 4. This is the maximum length of a string with all unique

3. There are no duplicates in un, so we move on and create a new combination by OR-ing this mask with 0 from masks. We update

# 8. Lastly, we have the string ue.

**Python Solution** 

class Solution:

14

15

16

17

18

19

20

21

22

23

24

25

26

27

28

29

30

31

32

33

9

10

11

14

16

17

18

19

20

22

23

24

25

26

27

28

29

30

31

32

33

34

35

36

37

38

39

40

41

42

44

43 }

from typing import List

This process of using bit masks allows us to efficiently manage and combine the unique characters from various strings without having to deal with actual string concatenation and character counting.

max\_length = 0 # Variable to store the maximum length of unique characters

char\_index = ord(char) - ord('a') # Map 'a'-'z' to 0-25

# If mask is not zero, it means the string had unique characters

int maxLen = 0; // This will hold the maximum length of unique characters.

// Iterate over the characters in the string to create a bitmask.

// set the bitmask to 0 and break out of the loop.

int bitIndex = s.charAt(i) - 'a'; // Convert character to a bitmask index (0-25).

// If the character is already in the bitmask (duplicate character),

bitMask |= 1 << bitIndex; // Add the character into the bitmask.

// If bitmask is 0, the string contains duplicates and should be ignored.

// Iterate over existing masks and combine them with the new mask if possible.

// If there is no collision between the current mask and the new mask,

bitMasks.add(combinedMask | bitMask); // Combine masks by OR operation.

maxLen = Math.max(maxLen, Integer.bitCount(combinedMask | bitMask)); // Update maxLen if necessary.

bitMasks.add(0); // Initialize the list with a bitmask of 0 (no characters).

# If the character is already in the mask, reset mask and break

# Check the new mask with existing masks for no overlap of characters

new\_mask = existing\_mask | mask # Combine the masks

masks.append(new\_mask) # Append the new mask to masks

masks = [0] # List to store the unique character sets as bit masks

# Iterate through each string in the input list for string in arr: mask = 0 # Initialize mask for current string # Check each character in the string

Java Solution class Solution {

List<Integer> bitMasks = new ArrayList<>(); // This list will store unique character combinations using bit masking.

max\_length = max(max\_length, bin(new\_mask).count('1')) # Update max length

```
C++ Solution
```

public:

9

10

11

12

#include <vector>

class Solution {

#include <algorithm>

2 #include <string>

13 for (std::string& str : arr) { 14 15 int mask = 0; // Bitmask to represent the current string 16 17 // Iterate over each character in the current string for (char& ch : str) { 18 19 int bitIndex = ch - 'a'; 20 21 // Check if this character has already appeared in the string (mask) 22 if ((mask >> bitIndex) & 1) { 23 // If the character repeats, discard this string by setting the mask to 0 and break 24 mask = 0;25 break; 26 27 28 // Add the current character to the mask mask |= 1 << bitIndex;</pre> 29 30 31 32 // Only proceed if mask is not zero (valid string without any repeating character) 33 if (mask == 0) continue; 34 35 int currentMasksCount = masks.size(); // Iterate over existing combinations of strings represented by masks 36 37 for (int i = 0; i < currentMasksCount; ++i) {</pre> int combinedMask = masks[i]; 38 39 40 // Check if current mask and combined mask have no characters in common if ((combinedMask & mask) == 0) { 41 // Combine current string with the string represented by combinedMask 43 masks.push\_back(combinedMask | mask); // Update max\_length using the number of unique characters in the new combination 44 45 max\_length = std::max(max\_length, \_\_builtin\_popcount(combinedMask | mask)); 46 47 48 49 50 // Return the maximum length of a string with all unique characters 51 return max\_length; 52 53 }; 54 Typescript Solution

### 45 // Iterate over existing combinations of strings represented by masks currentMasks.forEach(combinedMask => { 46 47 // Check if the current mask and combined mask have no characters in common 48 if ((combinedMask & mask) === 0) { 49 // Combine current string with the string represented by combinedMask 50 masks.push(combinedMask | mask); 51 // Update maxLength using the number of unique characters in the new combination

});

61 // Example usage:

return maxLength;

Time and Space Complexity

});

## inner loop iterating over the set of bitmasks masks. For every character c in each string s, we perform a constant-time operation to check if that character has already been seen by using a bitmask. If it has, we break early and the mask is set to 0. The worst-case scenario for this operation is O(k) where k is the length of the longest string.

**Time Complexity** 

Considering the generation of new masks, for every mask variable generated from string s, the code iterates through the masks list to check if there's any overlap with existing masks (m & mask == 0). In the worst-case scenario, if all characters in arr are unique and n is the length of arr, there could be up to 2<sup>n</sup> combinations as every element in arr could be included or excluded from the combination. The bit count operation (.bit\_count()) is generally considered a constant-time operation, but since it's applied for each newly

The time complexity of the code primarily stems from two nested loops: the outer loop iterating over each string s in arr, and the

Therefore, the overall time complexity is  $0(n * 2^n * k)$ . **Space Complexity** 

worst-case scenario, this could be as large as 2<sup>n</sup> where n is the length of arr. No other data structure in the code uses space that

created mask, it doesn't dominate the time complexity.

scales with the size of the input to the same degree. Therefore, the space complexity of the algorithm is 0(2^n).

The space complexity is dictated by the masks list which stores the unique combinations of characters that have been seen. In the