2070. Most Beautiful Item for Each Query Medium <u>Array</u> <u>Binary Search</u> <u>Sorting</u>

beauty of all items with a price less than or equal to prices[i].

Problem Description

If no items fit the criteria for a given query (all items are more expensive than the query value), the answer for that query is 0. We are asked to return a list of the maximum beauty values corresponding to each query.

In this problem, we have a list of items, each represented by a pair [price, beauty]. Our goal is to answer a series of queries,

Intuition

each asking for the maximum beauty value among all items whose price is less than or equal to the query value.

for given price limits.

To solve the problem efficiently, we first notice that we can handle the queries independently. So, we want a quick way to find

the maximum beauty for any given price limit. We approach this by sorting the items by price. Sorting the items allows us to employ a binary search technique to efficiently

find the item with the highest beauty below a certain price threshold. After sorting items, we create two lists: prices, which holds the sorted prices, and mx, which holds the running maximum beauty observed as we iterate through the sorted items. This ensures that for each price prices[i], mx[i] is the maximum

bisect_right finds the index j in the sorted prices list such that all prices to the left of j are less than or equal to the query value.

The binary search is carried out by using the bisect_right function from Python's bisect module. For each query,

If such an index j is found and is greater than 0, it means there exists at least one item with a price lower than or equal to the

Otherwise, if no index j is returned because all items are too expensive, we default the answer for that query to 0. This algorithm allows us to answer each query in logarithmic time with respect to the number of items, which is desirable when dealing with a large number of items or queries.

Solution Approach

The solution uses a mix of sorting, dynamic programming, and binary search to efficiently answer the maximum beauty queries

Sorting Items: Start by sorting the items based on their price. This is vital because it allows us to leverage binary search later on. Sorting is done using Python's default sorting algorithm, Timsort, which has a time complexity of O(n log n).

query value. We use j - 1 as the index to get the maximum beauty value from the mx list.

simply the beauty of the first item in the sorted list. **Building a Running Maximum Beauty:** • Iterate through each item, starting from the second one (since the first element's max beauty is already recorded).

Initialize a list mx, which keeps track of the maximum beauty encountered so far as we iterate through the items. The first element of mx is

• For each item, update the mx list with the greater value between the current item's beauty and the last recorded max beauty in mx. This is a

form of dynamic programming, where the result of each step is based on the previous step's result. **Answering Queries with Binary Search:**

Extracting Prices and Initializing Maximum Beauty List (mx):

Here's the step-by-step implementation strategy:

Extract the sorted prices into a list called prices.

- Initialize an answer list ans of the same size as queries, defaulting all elements to 0. • For each query, use the bisect_right function from the bisect module to perform a binary search on prices to find the point where the
- query value would be inserted while maintaining the list's order. • bisect_right returns an index j that is one position past where the query value would be inserted, so a price less than or equal to the

Return the Answer List:

of queries.

Example Walkthrough

• queries = [2, 4, 6]

Following the steps:

Sorting Items:

query must be at an index before j. ∘ If j is not 0, it means an item with a suitable price exists, and the answer for this query is mx[j - 1] - the corresponding max beauty by that price. If j is 0, it means no items are cheaper than the query, and the answer remains 0.

After all queries have been processed, return the answer list ans filled with the maximum beauties for each respective query.

- This approach effectively decouples the item price-beauty relationship from the queries, by pre-computing a list of maximum beauties (mx) that can later be quickly referenced using binary search. This transforms what could be an O(n*m) problem (naively checking n items for each of m queries) into an O(n log n + m log n) problem, where n is the number of items and m the number
- Let's illustrate the solution approach with a small example: Suppose we have the following items and queries: • items = [[3, 2], [5, 4], [3, 1], [10, 7]]

 We sort items by price: sorted_items = [[3, 2], [3, 1], [5, 4], [10, 7]] Extracting Prices and Initializing Maximum Beauty List (mx): Extract prices: prices = [3, 3, 5, 10] • Initialize mx with the maximum beauty of the first item: mx = [2]

 \circ Process the second item: it has the same price but lower beauty, so mx remains the same: mx = [2]

 \circ Process the third item: new price with higher beauty, update mx: mx = [2, 4]

\circ Process the fourth item: new price with higher beauty, update mx: mx = [2, 4, 7]**Answering Queries with Binary Search:**

Return the Answer List:

from bisect import bisect_right

items.sort()

class Solution:

 Query 2: 4 is equal to the second price, bisect_right would place it after index 1, so we use mx[0]: ans = [0, 2, 0] Query 3: 6 would fit between indexes 2 and 3, bisect_right returns 3 so we use mx[2]: ans = [0, 2, 4]

Initialize an answer list ans with all zeros: ans = [0, 0, 0]

Query 1: 2 is less than all prices, therefore ans [0] remains 0.

Building a Running Maximum Beauty:

- The final answer list reflecting maximum beauties for each query is: ans = [0, 2, 4] Thus, for the queries [2, 4, 6], the maximum beauty values for items within these price limits are [0, 2, 4], respectively.
- Solution Implementation **Python**

Extract a list of prices for binary search

prices = [price for price, _ in items]

for index in range(1, len(items)):

for i, query in enumerate(queries):

index = bisect right(prices, query)

Return the list of answers to the queries

for (int i = 1; i < items.length; ++i) {</pre>

// Arrav to store the answer for each query

int left = 0, right = items.length;

// The number of queries to process

int[] answers = new int[queryCount];

for (int i = 0; i < queryCount; ++i) {

right = mid;

left = mid + 1;

int queryCount = queries.length;

while (left < right) {</pre>

} else {

if (left > 0) {

return answers;

answers[i] = max_beauty[index - 1]

public int[] maximumBeauty(int[][] items, int[] queries) {

// item has the maximum beauty value at or below its price.

items[i][1] = Math.max(items[i - 1][1], items[i][1]);

// or the maximum beauty of all previous items.

// exceeding the query (price we can spend).

if (items[mid][0] > queries[i]) {

answers[i] = items[left - 1][1];

// Return the array of answers for all the queries

function maximumBeautv(items: number[][], queries: number[]): number[] {

items[i][1] = Math.max(items[i - 1][1], items[i][1]);

let mid = Math.floor((left + right) / 2);

// Preprocess items to keep track of the maximum beauty so far at each price point

// Perform a binary search to find the rightmost item with price less than or equal to the query price

left = mid + 1; // Item is affordable, potentially look for more expensive items

// If search ended with left pointing to an item, take the beauty value of the item to the left of it

// If left is 0, then all items are too expensive, thus the answer for this query is 0 by default

right = mid; // Item is too expensive, reduce the search range

// because the binary search gives us the first item with a price higher than the query

def maximumBeauty(self, items: List[List[int]], queries: List[int]) -> List[int]:

Create a list to store the maximum beauty encountered so far

max_beauty.append(max(max_beauty[-1], items[index][1]))

Process each query to find the maximum beauty for that price

Initialize the answer list for the queries with zeroes

max beauty = [items[0][1]] # initialize with the first item's beauty

Find the rightmost item that is not greater than the query price

Sort the items by price first (since the first item of each sub-list is price)

Update the max beauty list with the maximum beauty seen up to current index

If we found an item, store the corresponding max beauty (if not, zero stays by default)

// Iterate over each query to find the maximum beauty that can be obtained

// Sort items based on their price in ascending order

items.sort((a, b) => a[0] - b[0]);

let numOfQueries = queries.length;

while (left < right) {</pre>

else

if (left > 0) {

from bisect import bisect_right

items.sort()

return answers;

class Solution:

for (let i = 1; $i < items.length; ++i) {$

for (let i = 0: i < numOfOueries: ++i) {</pre>

let left = 0, right = items.length;

if (items[mid][0] > queries[i])

answers[i] = items[left - 1][1];

Extract a list of prices for binary search

prices = [price for price, _ in items]

for index in range(1, len(items)):

for i, query in enumerate(queries):

index = bisect right(prices, query)

answers = [0] * len(queries)

let answers = new Array(numOfQueries).fill(0);

Initialize the answer list for the queries with zeroes answers = [0] * len(queries) # Process each query to find the maximum beauty for that price

Find the rightmost item that is not greater than the query price

// The current maximum beauty is either the beauty of the current item

// Process each query to find the maximum beauty for the specified price

// Use binary search to find the rightmost item with a price not

int mid = (left + right) >> 1; // equivalent to (left + right) / 2

// If the mid item's price exceeds the query price, move the right pointer

// Otherwise, move the left pointer to continue searching to the right

// If there's at least one item that costs less than or equal to the query price

// The answer is the maximum beauty found among all the affordable items

// If no such item is found, the default answer of 0 (for beauty) will remain

max beauty = [items[0][1]] # initialize with the first item's beauty

Create a list to store the maximum beauty encountered so far

max_beauty.append(max(max_beauty[-1], items[index][1]))

def maximumBeauty(self, items: List[List[int]], queries: List[int]) -> List[int]:

Sort the items by price first (since the first item of each sub-list is price)

Update the max beauty list with the maximum beauty seen up to current index

If we found an item, store the corresponding max beauty (if not, zero stays by default)

// Sort the items array based on the price in increasing order Arrays.sort(items, (item1, item2) -> item1[0] - item2[0]); // Update the beauty value in the sorted items array to ensure that each

if index:

return answers

Java

class Solution {

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C++
#include <vector>
#include <algorithm>
using namespace std;
class Solution {
public:
    // Function that returns the maximum beauty item that does not exceed the query price
    vector<int> maximumBeauty(vector<vector<int>>& items, vector<int>& queries) {
        // Sort items based on their price in ascending order
        sort(items.begin(), items.end());
        // Preprocess items to keep track of the maximum beauty so far at each price point
        for (int i = 1; i < items.size(); ++i) {</pre>
            items[i][1] = \max(items[i - 1][1], items[i][1]);
        int numOfQueries = queries.size();
        vector<int> answers(num0fQueries);
        // Iterate over each query to find the maximum beauty that can be obtained
        for (int i = 0; i < numOfQueries; ++i) {</pre>
            int left = 0, right = items.size();
            // Perform a binary search to find the rightmost item with price less than or equal to the query price
            while (left < right) {</pre>
                int mid = (left + right) / 2;
                if (items[mid][0] > queries[i])
                    right = mid; // Item is too expensive, reduce the search range
                else
                    left = mid + 1;  // Item is affordable, potentially look for more expensive items
            // If search ended with left pointing to an item, take the beauty value of the item to the left of it
            // because the binary search gives us the first item with a price higher than the query
            if (left > 0) answers[i] = items[left - 1][1];
            // If left is 0, then all items are too expensive, thus the answer for this query is 0 by default
        return answers;
};
TypeScript
// Import necessary functions from 'lodash' for sorting and binary search
import _ from 'lodash';
// Function that returns the maximum beauty item that does not exceed the query price
```

if index: answers[i] = max_beauty[index - 1] # Return the list of answers to the queries return answers

Time and Space Complexity

Sorting the items list: The items.sort() method is called on the list of items, which typically has a time complexity of O(n * log(n)), where n is the number of items. Creating the prices list: This involves iterating over the sorted items list to build a new list of prices, which will take O(n).

Time Complexity

Space Complexity

Creating the mx list: A single for-loop is used to construct the mx list. This also runs in O(n) time as it iterates over n items once.

The time complexity of the provided code can be broken down into the following parts:

4. Answering the queries by binary search: Each query performs a binary search to find the right index in the prices list, which takes O(log(n)). Since this is done for q queries, the total time complexity for this step is O(q * log(n)).

The ans list: Space needed is O(q) for storing the answers for q queries.

Combining these steps, the overall time complexity is 0(n * log(n) + n + n + q * log(n)), which simplifies to 0(n * log(n) + n + n + q * log(n))q * log(n)) because the linear terms are overshadowed by the n * log(n) term when n is large.

The space complexity of the code can be analyzed by considering the additional data structures used:

- The prices list: This consumes O(n) space. The mx list: This also consumes O(n) space.
- Therefore, the overall space complexity is 0(n + n + q) which simplifies to 0(n + q) as we add the space required for the two lists related to items and the space for the answers to the queries.