3011. Find if Array Can Be Sorted

Medium Bit Manipulation Array Sorting

Problem Description

specific operation. The operation allows us to swap any two adjacent elements, but only if those elements have the same number of 1s in their binary representations; this is known as the number of set bits. We can perform this operation as many times as needed, including not at all, if the array is already sorted. In essence, we need to check if, by using the allowed swaps, we can arrange the array in non-decreasing order. If we find it's

In this problem, we are given an array of positive integers called nums, and our task is to determine if we can sort it using a

possible to achieve this, we should return true. Otherwise, we return false if it's impossible to sort the array under these constraints.

The solution hinges on understanding that we cannot change the relative order of elements with different numbers of set bits since they can't be swapped directly based on the rule. Therefore, sorting the array essentially breaks it down into subarrays,

Intuition

each composed of elements with the same number of set bits, which could be ordered in any way since swaps among them are allowed. With this in mind, we can iterate through the array and identify these subarrays. Within each subarray, we keep track of the minimum and maximum value encountered so far. A crucial insight is that if the minimum value in a subarray is less than the maximum value of the previous subarray, it indicates that <u>sorting</u> is impossible. This is because, in a sorted array, all elements in a

previous (and thus lower) subarray should be less than or equal to all the elements in the following subarray. To implement this, we use two pointers as we traverse the array. The first pointer, i, marks the start of a subarray, and the second pointer, j, explores the rest of the array to find the end of this subarray. The while loops ensure that we progress through the array, from one subarray to the next, assessing the minimum and maximum for each set bit count. If we successfully traverse

the entire array without encountering a condition that makes sorting impossible, we return true. Otherwise, we return false as

soon as such a condition is found. Solution Approach The implementation follows a straightforward two-pointer approach to tackle the problem:

Initialize a variable pre_mx to negative infinity. This will keep track of the maximum value of the previous subarray as we

Set up two pointers, i and j, starting from 0 (i) and 1 (j), respectively. Pointer i represents the beginning of the current

progress through nums.

Loop over nums using i to iterate through the array. For each position i, we: a. Find the number of set bits of nums [i], which

subarray, which implies it is impossible to sort the array. Hence, return False.

subarray, while j will be used to find the end of this subarray.

processed subarray for the next iteration.

value of nums [i] which is 3.

- determines the current subarray we're evaluating. This can be done using the .bit_count() method in Python. b. Initialize mi and mx to the value of nums[i]. These will track the minimum and maximum values within the current subarray, respectively.
- While inside the loop, initiate a nested loop that keeps running as long as j is within the bounds of the array and nums[j] shares the same number of set bits as nums [i]. Within this loop: a. Update mi and mx to be the minimum and maximum of the
- current subarray by comparing them to nums[j]. b. Increment j to check the next element. After the nested loop terminates (meaning we reached the end of the current subarray with matching set bits), check if pre_mx is greater than mi. If it is, it means that the previous subarray had a value greater than the smallest value of the current

Update pre_mx with the largest value in the current subarray, mx, because this now becomes the maximum of the last

Set pointer i to j to start the algorithm for the next subarray of elements with equal set bit count. If the algorithm completes the iteration over the array without returning False, it means sorting the array is possible under the given rules, so it returns True.

This approach efficiently applies the rules of the problem to determine if sorting is feasible, relying on the fact that only elements

with the same number of set bits can be adjacent in the final sorted array. It uses python's built-in .bit_count() method to count

Example Walkthrough

set bits and utilizes comparison operations to ensure order within and between identified subarrays.

11, 01, 10, and 100, with set bit counts of 2, 1, 1, and 1, respectively. Initialize pre_mx to negative infinity. Start with i = 0 and j = 1.

At i = 0, nums[i] = 3. Number of set bits in 3 (11 in binary) is 2. Initialize min (mi) and max (mx) of the current subarray to the

Move to j which is 1. Number of set bits in nums[j] (1 in binary) is 1, which is different from the 2 set bits we have for nums[i].

So we close this subarray here because we cannot form a subarray with different set bit counts. Since we cannot include

We check if $pre_mx > mi$ which means if -inf > 3. This is not true, so we move on and update pre_mx to mx which is 3.

Let's illustrate the solution approach using a small example with the array nums = [3, 1, 2, 4]. The binary representations are

j = 2, nums[j] = 2 which also has 1 set bit. We include nums[j] in the current subarray and update mi to min(mi, nums[j]) (which remains 1) and mx to max(mx, nums[j]) (which becomes 2). Increment j to 3.

j = 3, nums[j] = 4 which also has 1 set bit. We include nums[j] in the current subarray and update mi to min(mi, nums[j])

Since we've reached the end of the array, we've verified that each subarray with the same set bit count is such that its

The result here is that the array can be sorted using the allowed operations: swap 1 and 2 to get [3, 2, 1, 4], which is now in

(which is still 1) and mx to max(mx, nums[j]) (which becomes 4). After this, j is out of bounds (since nums has only four elements), so we exit this nested loop.

We check if $pre_mx > mi$ which means if 3 > 1. This is not true, so we update pre_mx to mx which is now 4.

We set i to j, therefore i is now 1 and increment j to 2 to start evaluating the next subarray.

nums[j] in the current subarray, we skip updating mi and mx and proceed to step 5.

At i = 1, nums [i] is 1. The number of set bits is 1. Initialize mi and mx to 1.

the non-decreasing order. Our algorithm returns True.

def canSortArray(self, nums: List[int]) -> bool:

Iterate through the list of numbers.

current_min = current_max = nums[i]

while j < n and bin(nums[j]).count('1') == bit_count:</pre>

Move to the next segment with a different bit count.

current_min = min(current_min, nums[j])

current_max = max(current_max, nums[j])

// Move 'i' to the start of the next segment.

// If all segments are in the correct order, return true.

Initialize previous maximum to negative infinity.

Initialize index and get the length of the list.

minimum value is not less than the maximum value of the previous subarray.

Python

Initialize the next index and get the bit count of the current number. j = i + 1bit_count = bin(nums[i]).count('1') # Keep track of the minimum and maximum for the current bit count.

Slide through the array to find consecutive numbers with the same bit count.

If the previous maximum number is greater than the current minimum,

```
# the array cannot be sorted based on the conditions, hence return False.
if previous_max > current_min:
    return False
# Update previous maximum for the next iteration.
previous_max = current_max
```

Solution Implementation

previous_max = -inf

i, n = 0, len(nums)

j += 1

while i < n:

from math import inf

class Solution:

```
i = j
       # If we've reached this point, the array can be sorted, therefore return True.
        return True
Java
class Solution {
    public boolean canSortArray(int[] nums) {
       // Initialize the previous maximum value to the lowest possible value.
        int prevMax = Integer.MIN_VALUE;
       // Index 'i' will track the start of each segment with equal bit count.
       int i = 0;
       // 'n' holds the length of the input array.
       int n = nums.length;
       // Loop through the elements of the array.
       while (i < n) {
           // 'j' will track the end of the current segment.
           int j = i + 1;
           // 'bitCount' stores the number of 1-bits in current array element.
           int bitCount = Integer.bitCount(nums[i]);
           // 'min' and 'max' track the minimum and maximum of the current segment.
           int min = nums[i], max = nums[i];
           // Continue to next elements if they have the same bit count.
           while (j < n && Integer.bitCount(nums[j]) == bitCount) {</pre>
                min = Math.min(min, nums[j]);
                max = Math.max(max, nums[j]);
                j++;
           // If the max value of the previous segment is greater than the min of the current, it can't be sorted.
           if (prevMax > min) {
                return false;
           // Update the prevMax to the max value of the current segment.
           prevMax = max;
```

C++

i = j;

return true;

let minElement = nums[i];

let maxElement = nums[i];

if (previousMax > minElement) {

return false;

j++;

// Keep updating min/max in the group where the bit count is the same

// If the max of the previous group is greater than the min of the current group, return false

while (j < length && bitCount(nums[j]) === bitCountOfCurrent) {</pre>

minElement = Math.min(minElement, nums[j]);

maxElement = Math.max(maxElement, nums[j]);

```
#include <vector>
#include <algorithm>
using namespace std;
class Solution {
public:
    bool canSortArray(vector<int>& nums) {
        int previousMax = -300; // Initial value considering the constraints for possible integer values
        int currentIndex = 0, numSize = nums.size();
        // Loop through all elements in the array
       while (currentIndex < numSize) {</pre>
            int nextIndex = currentIndex + 1;
            int currentPopCount = __builtin_popcount(nums[currentIndex]);
            int currentMin = nums[currentIndex], currentMax = nums[currentIndex];
            // Find subsequence where all elements have the same number of set bits (1s)
            while (nextIndex < numSize && __builtin_popcount(nums[nextIndex]) == currentPopCount) {</pre>
                currentMin = min(currentMin, nums[nextIndex]);
                currentMax = max(currentMax, nums[nextIndex]);
                nextIndex++;
            // If the maximum value from previous segment is greater than minimum of the current,
            // then the array can't be sorted based on the rules given
            if (previousMax > currentMin) {
                return false;
            previousMax = currentMax; // Update previousMax to the max of the current segment
            currentIndex = nextIndex; // Move to the next segment
       // If the loop completes without returning false, it means the array can be sorted
        return true;
};
TypeScript
function canSortArray(nums: number[]): boolean {
    let previousMax = -300; // Initiate the previous maximum to a value lower than any element in nums
    const length = nums.length;
    // Iterate over the array
    for (let i = 0; i < length; ) {</pre>
        let j = i + 1; // Start from the next element
        const bitCountOfCurrent = bitCount(nums[i]); // Get the bit count of the current element
       // Find min and max element within the same bit count group
```

```
// Update the previousMax to the max of the current group
          previousMax = maxElement;
          i = j; // Move to the next group
      // If the entire array can be separate into groups with incremental mins, return true
      return true;
  function bitCount(i: number): number {
      // Apply bit manipulation tricks to count the bits set to 1
      i = i - ((i >>> 1) \& 0 \times 55555555);
      i = (i \& 0x333333333) + ((i >>> 2) \& 0x333333333);
      i = (i + (i >>> 4)) \& 0x0f0f0f0f;
      i = i + (i >>> 8);
      i = i + (i >>> 16);
      return i & 0x3f; // Return the count of bits set to 1
from math import inf
class Solution:
   def canSortArray(self, nums: List[int]) -> bool:
       # Initialize previous maximum to negative infinity.
        previous max = -inf
       # Initialize index and get the length of the list.
        i, n = 0, len(nums)
       # Iterate through the list of numbers.
       while i < n:
            # Initialize the next index and get the bit count of the current number.
            j = i + 1
            bit_count = bin(nums[i]).count('1')
            # Keep track of the minimum and maximum for the current bit count.
            current min = current max = nums[i]
           # Slide through the array to find consecutive numbers with the same bit count.
           while j < n and bin(nums[j]).count('1') == bit_count:</pre>
                current_min = min(current_min, nums[j])
               current_max = max(current_max, nums[j])
                j += 1
           # If the previous maximum number is greater than the current minimum,
           # the array cannot be sorted based on the conditions, hence return False.
            if previous_max > current_min:
                return False
            # Update previous maximum for the next iteration.
            previous_max = current_max
           # Move to the next segment with a different bit count.
           i = j
       # If we've reached this point, the array can be sorted, therefore return True.
        return True
Time and Space Complexity
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Time Complexity

The time complexity of the code is O(n) because there is a single while loop that iterates through each element of the array nums exactly once. Inside the loop, the .bit_count() method is called, which is expected to run in constant time, and basic arithmetic

Space Complexity The space complexity of the code is 0(1) since it uses a fixed amount of extra space: variables pre_mx, i, n, j, cnt, mi, and mx. There is no use of any data structures that grow with the size of the input array nums, which keeps the space complexity constant.

operations and comparisons are performed, which also take constant time per iteration. Even though there is a nested loop, it

does not increase the overall number of iterations; it just continues from where the outer loop left off.