2598. Smallest Missing Non-negative Integer After Operations

Greedy Array Medium Hash Table

Problem Description

(minimum excluded), which represents the smallest non-negative integer not present in the array. We are given an array nums and an integer value. The operation at our disposal allows us to add or subtract value from any element in nums. The goal is to apply this operation as many times as we want to maximize the MEX of the resulting array. Understanding the MEX is crucial as it is the key evaluation metric for the outcome of array manipulations. For instance, in an

This problem presents an optimization challenge with a combination of array manipulation and a novel concept called MEX

array [-1, 2, 3], since 0 and 1 are not present, the MEX is 0, as it is the smallest non-negative integer not in the array. However, if we had [1, 0, 3], the MEX would be 2. What makes this problem interesting is the strategic decision of how to add

or subtract 'value' in order to maximize the MEX. Intuition

To solve the problem, we need a smart way to track the potential MEX without exhaustively enumerating all possible permutations of array changes, which would be computationally infeasible. The intuition here lies in realizing that adding or

subtracting value doesn't affect the remainder when each element of nums is divided by value. Consequently, the remainders form certain 'buckets' that we can only fill up to a certain level - dictated by how many times a remainder appears in the original array. This leads to the insight that we can use the frequencies of these remainders to determine the MEX without iterating through all possible array operations. Specifically, by initializing a counter for the frequency of each remainder (modulo value) present in the

existing remainder frequencies. When the counter for a remainder corresponding to i % value is 0, it signals that we've hit a 'gap', or a value that can't be created through any combination of operations on the current array, since none of the array elements produce a remainder equal to i % value when divided by value. That's our desired maximum MEX. If not, we decrement the count and move to the next

array, we can iterate from 0 and move up to find the smallest non-negative integer (our potential MEX) that doesn't collide with

integer, repeating the process until we find our MEX. **Solution Approach** The solution strategy is built on a counting approach, which significantly simplifies the operation and determination of MEX. Let's

Counting Modulo Frequencies: We realize that the operation of adding or subtracting value from any element in nums

expound on the implementation of the solution:

retains its modulo value. Thus, we store the count of occurrences of each remainder after dividing the elements by value using a Counter data structure. This gives us the frequency distribution of remainders.

Modulo Value as a Key Insight: We use the modulo operation considering value as an invariant in our problem. This insight

solves the optimization problem by allowing us to work with a limited number of remainders (from 0 to value - 1) and their

We check if the count for the current number i modulo value is 0. If it is, no number in nums can be changed through

addition or subtraction operations to get a remainder that matches i % value. Hence, i represents a MEX that cannot be

for the remainder i % value by 1 because, conceptually, we have 'used up' one instance where a number in the array

- counts instead of dealing with potentially large numbers after multiple addition or subtraction operations. Iterating for MEX: We initialize an iteration from 0 upwards, continuing to len(nums) + 1 to cover all potential MEX values. In each iteration:
- obtained through any variant of the **nums** array, and we immediately return it as the maximum MEX. If the count is not 0, it implies that i % value is a possible remainder and thereby not the MEX. We decrement the count

could achieve this remainder. We continue to the next iteration to find the MEX.

This approach avoids brute-force computation and provides an elegant, efficient path to determining the MEX. We rely on the cyclic nature of modulo operation and the Counters that track the possibility of numbers to be fashioned into a specific modulus bucket through the given operation.

The algorithm is optimized as it avoids iterating through all possible operations on the array and instead, operates on a simple

linear search for the smallest non-present modulo within the range, thus optimizing it to a time complexity of O(n).

First, we count the modulo frequencies. The remainders of numbers in nums when divided by value = 3 are:

Let's illustrate the solution with an example. Consider the array nums = [1, 3, 4] and let value = 3. We want to maximize the MEX of the array by adding or subtracting 3 to elements in nums.

• 1 % 3 = 1 • 3 % 3 = 0

• 4 % 3 = 1

Step 1: Counting Modulo Frequencies

Example Walkthrough

So, our frequency distribution (remainder counts) is: • Remainder 0:1 occurrence

For i = 0: The remainder 0 % 3 = 0 has a count of 1 (from the number 3 in nums). This is not our MEX, so we decrement

For i = 2: The remainder 2 % 3 = 2 has a count of 0. This means that we've found a gap here; we can't get a remainder of

This concludes our example. Without performing any operations on the array nums, we have efficiently determined that the

Step 2: Utilizing Modulo Value as an Insight

the count for remainder 0.

Solution Implementation

from collections import Counter

for i in range(len(nums) + 1):

Python

Java

C++

#include <vector>

#include <cstring>

class Solution {

TypeScript

class Solution:

operations:

for (const num of nums) {

count[index]++;

for (let i = 0; ; ++i) {

return i;

class Solution {

• Remainder 1: 2 occurrences

• Remainder 2: 0 occurrences

- **Step 3: Iterating for MEX** Starting from 0, we check the remainder counts:
 - 2 by adding or subtracting 3 from any element in nums. Hence, the MEX is 2.

For i = 1: The remainder 1 % 3 = 1 has a count of 2. Again, we decrement the count for remainder 1.

We acknowledge that we can deal with numbers in nums only in terms of their remainders when divided by value.

from typing import List class Solution: def findSmallestInteger(self, nums: List[int], value: int) -> int:

maximum MEX achievable is 2 by just iterating through remainders and their counts.

Create a counter to keep track of the frequency of each number modulo 'value'

If there is no number i modulo 'value' in our collection, return i

// Method to find the smallest integer that is not present in the array when modulus with value

// Iterate over each number in nums and increment the count for the corresponding modulus

modulo_counter = Counter(num % value for num in nums)

public int findSmallestInteger(int[] nums, int value) {

countModulo[(num % value + value) % value]++;

Iterate over the numbers from 0 to length of nums (inclusive)

// Create an array to count occurrences of each modulus result

if modulo counter[i % value] == 0: return i # Otherwise, decrease the count of i modulo 'value' by one modulo_counter[i % value] -= 1

```
// Start looking for the smallest integer that is not in the array, by checking modulus occurrences
for (int i = 0; ; ++i) { // no termination condition here since we are guaranteed to find a number eventually
    // Use the i % value to wrap around the countModulo array
   // Check if the current number has a count of zero, which means it's not present in the nums array when modulus with valu
    if (countModulo[i % value] == 0) {
       // If it's not present, this is the smallest number we are looking for
       return i;
    // Otherwise, decrease the count and keep looking
```

countModulo[i % value]--;

int[] countModulo = new int[value];

for (int num : nums) {

```
public:
    int findSmallestInteger(vector<int>& nums, int value) {
       // Create an array to count occurrences of each modulus value
       int countArray[value];
       // Initialize the countArray with zeros
       memset(countArray, 0, sizeof(countArray));
       // Fill the countArray with the count of each modulus value
        for (int num : nums) {
            // Correct negative values using modulo operation, then increment the count
            ++countArray[(num % value + value) % value];
       // Iterate to find the smallest integer not present in nums when modulo `value`
        for (int i = 0; ; ++i) {
           // Calculate the current index modulo value
            int modIndex = i % value;
           // If the count for the current index is zero.
           // it means the integer `i` is not present in nums as mod value
            if (countArray[modIndex] == 0) {
                // Return the smallest integer not present
                return i;
            // Decrement the count for the current index as it is now being used
            --countArray[modIndex];
       // The loop is designed to run indefinitely, will break internally.
};
```

```
// Otherwise, decrement the count at the current index
       count[index]--;
   // The loop is intended to run indefinitely, as it will always return inside the loop body.
from collections import Counter
from typing import List
```

if (count[index] === 0) {

function findSmallestInteger(nums: number[], value: number): number {

const count: number[] = new Array(value).fill(0);

// Initialize a counter array with size 'value' and fill it with 0s.

// Increment the count for each number in nums based on its modulo 'value'

// Iterate to find the smallest integer not in 'nums' after modulo 'value'.

const index = i % value; // Calculate the index in the count array

def findSmallestInteger(self, nums: List[int], value: int) -> int:

modulo_counter = Counter(num % value for num in nums)

Create a counter to keep track of the frequency of each number modulo 'value'

const index = ((num % value) + value) % value; // Handles negative numbers

// If the count at the current index is 0, this is the smallest integer not found in 'nums'

```
# Iterate over the numbers from 0 to length of nums (inclusive)
       for i in range(len(nums) + 1):
           # If there is no number i modulo 'value' in our collection, return i
           if modulo counter[i % value] == 0:
               return i
           # Otherwise, decrease the count of i modulo 'value' by one
           modulo_counter[i % value] -= 1
Time and Space Complexity
  The given Python code defines a method findSmallestInteger meant to find the smallest integer that is not present in the input
  list nums when considering each number modulo value. It manages this by creating a frequency counter for the modulo results
  and then iteratively checking for the smallest index that is not present in the frequency counter.
Time Complexity
```

2. The subsequent for loop runs for n + 1 iterations in the worst case, as it stops as soon as it finds an integer that is not in the counter. Each operation within the for loop (accessing cnt and decrementing the count) is 0(1) thanks to Python's Counter which is a hash map under the hood.

1. Initializing the counter with (x % value for x in nums) has a linear runtime proportional to the size of nums.

complexity remains linear or O(n). **Space Complexity**

The time complexity of the function is O(n), where n is the length of the input list nums. This arises from the following

Therefore, as the initialization of the counter and the for loop are both linear in terms of n and are not nested, the overall time

The space complexity of the algorithm is O(value), where value is the input parameter to the method. This complexity is

attributed to the following points:

[0, value). 2. No other data structures are used that depend on the size of the input or value.

Thus, the space required by the counter is directly proportional to the value, leading to a space complexity of O(value).

1. The counter cnt stores at most value different keys, since each number in nums is taken modulo value, which results in a possible range of