1404. Number of Steps to Reduce a Number in Binary Representation to One

Medium Bit Manipulation String

The problem presents a scenario where you are given the binary representation of an integer as a string s. Your task is to determine

Problem Description

how many steps it would take to reduce this number to 1 by following two rules: If the current number is even, divide it by 2.

Leetcode Link

The constraint mentioned in the problem is that it's guaranteed that following these rules will always lead you to reach the number 1,

2. If the current number is odd, add 1 to it.

regardless of the starting number.

Intuition

To solve this problem, we need to understand how binary numbers work and how we can apply the given rules to get to '1'. The last digit of a binary number determines if it's even (0) or odd (1). Therefore:

1. If the last digit is '0', we know the number is even, and we need to divide the number by '2'. In binary terms, dividing by '2' is equivalent to simply removing the last digit (which is a '0' in this case).

2. If the last digit is '1', then the number is odd, and we need to add '1' to it. Adding '1' to an odd binary number will flip the last digit

- to '0' and may cause a carry to propagate towards the most significant bit. The key challenge in this problem is handling the carry when incrementing an odd binary number. We must traverse the binary string
- from least significant bit (rightmost) to the most significant bit (leftmost), flipping the bits until we either reach a '0', which does not require a carry, or we reach the beginning of the string, at which point an additional final carry would complete the task.

 If there is no carry and the character is '0' (even), no action is needed, just an additional step is counted. If there is no carry and the character is '1' (odd), we must flip it to '0' and count a step for the flip and another step for adding '1'

If there is a carry and the character is '1', we keep it as '1', maintain the carry, but still count a step.

2. Initialize a counter ans to 0, which will count the number of steps taken to get to '1'.

to make it even (which enables the division by '2').

We iterate over the binary string in reverse, keeping track of carries. For each character:

- Finally, if there is a carry after completing the traversal of the string, we add one final step because the binary number would need to grow by one more significant bit (imagine going from binary '111' to '1000'). The resulting count of steps is our answer.
- Solution Approach

If there is a carry and the character is '0', we flip it to '1', eliminate the carry, count a step for the flip, and move on.

1. Initialize a variable carry to False. This will act as a flag to determine whether we need to carry a '1' when we flip a '0' to a '1' or vice versa.

3. Loop through the binary string's characters in reverse, except for the first character, using for c in s[:0:-1]:. This is because

the first bit (the leftmost) does not directly affect the counting, as the problem assumes that the number will eventually be reduced to '1'.

4. For each iteration, check if there is a carry. If so, and the current bit is a '0', flip it to a '1' and reset the carry to False. If the

to '0' and there is no more carry.

extra step needed to reach '1'.

Example Walkthrough

carry remains False.

'10' in binary.

As a summary of the steps:

current bit is a '1', flip it to a '0' and keep the carry as True.

8. Return the counter ans as the number of steps taken.

The solution provided in Python follows these steps:

- 5. If the current bit is '1', increment the steps by one because '1' represents an odd number which needs to add '1' to become even. Then, set the carry to True. 6. Regardless of the conditions above, increment the steps by one for the division by '2' operation, except when we flip the last '1'
- 7. Finally, outside of the loop, if there is still a carry if carry: after all the flips, which means all bits were '1's, and by adding '1' we overflow into an additional bit (e.g., from '111' to '1000'), increment the steps by one more (ans += 1), since this represents an
- into account how addition and division by '2' affect binary digits. The solution does not use any additional data structures and takes advantage of the property of binary numbers and arithmetic to achieve the intended result efficiently.

The algorithm makes use of a simple simulation of the manual process one might use to add binary numbers on paper while taking

Let's take the binary representation of the integer 13 as an example, which is 1101 in binary. 1. We initialize the carry as False and the step counter ans as 0.

2. We examine the binary string from right to left, starting with the second-to-last digit because the last one determines if we need

• The next-to-last character is '0'. Since there is no carry and it's even, we can divide by '2'. This gives us one step (ans += 1), and

• Since it's '1', it's odd; we add '1' to it, flip it to '0', and add two steps (ans += 2 - one for adding '1' and one for the division by '2').

Now, because we added '1' to a '1', it means we have a carry over.

we need an extra step to account for the overflow (e.g., from '111' to '1000').

3. The next character (moving right to left) is a '1'.

4. We move to the first character, which is also a '1'.

Starting from the second-to-last bit (from the right), our steps will be:

to add one to make it even (if it's a '1') or if we can divide immediately (if it's a '0').

• We flip the '1' to '0', count the step for the flip (ans += 1), but do not add another step for division because that will happen next. 5. After completing the string traversal, we check for carry. There is still a carry which means we had a string of all '1's before, so

• There is still a carry from before. This '1' becomes a '0' due to the carry, but we still have a carry because adding '1' to '1' gives

 Start: 1101 Divide by 2 (remove last '1'): 110, steps = 1

Add 1 (to handle carry from '111'): 1000, steps = 5

Divide by 2 three times (remove ending '0's): 1, steps = 8

Thus, the number of steps taken to reduce the binary string 1101 to 1 is 8.

Initialize a counter to track the number of steps

has_carry = False # Carry is consumed

and we keep the carry for the next bit

Iterate over the string in reverse order, excluding the most significant bit

If the current bit is '1', it becomes '0' after adding carry,

If the current bit is '1' and there is no carry, or if we just had a carry,

boolean carry = false; // Initialize carry to keep track of addition carry

// If it's 1, it remains 1 and we also have a carry

// If current bit is 1, we need to flip it which results in a carry

steps++; // Increment the steps for the potential addition (or bit move)

return steps; // Return the total number of steps to convert the binary number to 1

// If a carry is left after processing all bits, an additional step is needed

steps++; // Increment the steps for flipping the bit

// Loop backwards through the binary string (ignoring the MSB at index 0 initially)

// If it's 0, carry turns it to 1 without generating a new carry

int steps = 0; // Initialize steps to count the number of operations

Add 1 (to the odd number): 111, steps = 3

Divide by 2 (remove last '1'): 11, steps = 4

We increment ans by one more step (ans += 1).

class Solution: def numSteps(self, binary_str: str) -> int: # Initialize a boolean to track if there is a carry in binary addition has_carry = False

if bit == '0':

bit = '0'

else:

for bit in binary_str[:0:-1]: # If there is a carry, add it to the current bit if has_carry: # If the current bit is '0', it becomes '1' after adding carry 13

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Java Solution

class Solution {

public int numSteps(String s) {

if (carry) {

} else {

if (c == '1') {

if (carry) {

steps++;

carry = true;

if (c == '0') {

c = '0';

carry = false;

for (int $i = s.length() - 1; i > 0; --i) {$

char c = s.charAt(i); // Get the current bit

// If there is a carry from the previous operation

// Determine the actions based on the current bit

steps_count = 0

Python Solution

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# increment the step count since we would need an additional step to reduce it
    if bit == '1':
        steps_count += 1 # One step to make it '0'
        has_carry = True # A carry is generated for the next bit
    # One step is always needed for each bit, either to add the carry or to divide by 2
    steps_count += 1
# If there is a carry after processing all bits, add an extra step to handle it
if has_carry:
    steps_count += 1
# Return the total number of steps needed to reduce the binary string to '1'
return steps_count
```

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C++ Solution

1 class Solution {

public:

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int numSteps(string s) {
           // Initialize the number of steps to 0
           int steps = 0;
           // The carry variable to handle the addition carry over
           bool carry = false;
           // Traverse the binary string from the least significant bit to the most
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           // Ignoring the most significant bit as we stop when we reach the beginning of the string
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            for (int i = s.size() - 1; i > 0; --i) {
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               // Get the current bit
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               char bit = s[i];
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               // If there's a carry from the previous operation
               if (carry) {
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                   // Flip the current bit due to the carry
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                   if (bit == '0') {
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                        bit = '1';
                        // The carry has been used, reset it to false
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                        carry = false;
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                   } else // If the bit is '1', turning into '0' keeps carry true
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                        bit = '0';
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               // If the bit is '1', we will need a step to make it '0' and create a carry
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               if (bit == '1') {
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                   // Increment steps for the flip to '0'
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                   ++steps;
                   // Set the carry for the next iteration
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                   carry = true;
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               // Regardless of the bit, we do a right shift operation
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               ++steps;
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           // If there's a carry at the end, we need to add one more step to add it to the MSB
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           if (carry) ++steps;
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           // Return the total number of steps
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           return steps;
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43 };
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Typescript Solution
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// If the bit is '1', it will turn into '0' and we keep the carry as true 21 bit = '0'; 23 24 25

steps++;

steps++;

return steps;

if (bit === '1') {

carry = true;

if (carry) steps++;

// Return the total number of steps

} else {

if (carry) {

1 function numSteps(s: string): number {

let steps: number = 0;

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let carry: boolean = false;

// Get the current bit

let bit: string = s[i];

if (bit === '0') {

carry = false;

bit = '1';

// Initialize the number of steps to 0

// The carry variable to handle the addition carry over

for (let i: number = s.length - 1; i > 0; --i) {

// Flip the current bit due to the carry

// Increment steps for the flip to '0'

// Set the carry for the next iteration

// If there's a carry from the previous operation

// Traverse the binary string from the least significant bit to the most

// The carry has been absorbed, so we reset it to false

// Regardless of the bit, we perform a right shift operation

and takes constant time, so the overall time complexity of the code is O(n).

// Ignoring the most significant bit as we stop when we reach the start of the string

// If the bit is '1', we will need a step to make it '0' and generate a carry

// If there's a carry at the end, we need one more step to add it to the MSB

Time and Space Complexity The provided code implements a function to transform a binary number given as a string into the number 1, by applying certain operations and counts the number of steps taken.

possibly incrementing ans, and modifying carry. The loop runs for n - 1 iterations, where n is the length of the input string. Since each iteration takes a constant time, the time complexity of the loop is O(n). The final if block is also executed at most once

To analyze the time complexity, let's look at the loop in the code. It iterates over the string s from the end (excluding the first

character) towards the beginning. For each character c, it performs a constant number of operations, checking the value of c,

Space Complexity:

Time Complexity:

The space complexity is determined by the amount of extra space used by the algorithm besides the input itself. Here, we have a few variables (carry, ans, and c) which only require a constant amount of space.

Hence, the space complexity of the provided code is 0(1), which means it uses a constant amount of additional space regardless of the size of the input.