11. Container With Most Water

Medium Greedy Array Two Pointers

Problem Description

You are presented with an integer array called height which represents the heights of vertical lines placed at positions indexed from 1 to n (0-indexed in the array). Imagine that each height[i] is linked to a line on a chart that extends upward from the x-axis to a point (i, height[i]). Your task is to find two lines that, along with the x-axis, enclose the greatest possible area, which represents the maximum water that can be trapped between them without allowing any spillage over the sides of the lines (the container cannot be slanted). The goal is to calculate and return this maximum trapped water area.

Intuition

To solve this problem efficiently, we use a two-pointer technique. We place one pointer at the beginning of the array and the other at the end, and these pointers represent the potential container boundaries. At each step, the trapped water is determined by the distance between the pointers (which is the container's width) and the height of the smaller line (since the water level can't be higher than the smaller of the two boundaries). This is the area that could potentially be the maximum.

To maximize the area, after calculating the trapped water at each step and comparing it to the maximum we've seen so far, we move

the pointer at the shorter line towards the other pointer. This is because keeping the pointer at the taller line stationary and moving the shorter one might lead us to find a taller line and thus a larger area. There's no advantage in moving the taller pointer first, as it would only reduce the potential width without guaranteeing a taller line to increase height. We repeat this process of calculating, updating the maximum water area, and moving the shorter line pointer towards the other pointer until the <u>two pointers</u> meet, at which point we've considered every possible container and the maximum stored water has been found.

By approaching this problem with each step optimized to either maintain or improve the potential maximum area, we are able to

arrive at the solution efficiently, resulting in an algorithm that runs in linear time relative to the number of lines.

Learn more about Greedy and Two Pointers patterns.

Solution Approach

smaller of the two heights at height[i] and height[j].

The implementation of the solution follows the two-pointer approach. Here's a step-by-step guide to how the solution works:

1. Initialize two pointers: i is set to the start of the array (0), and j is set to the end of the array (len(height) - 1).

- 2. Initialize a variable ans to keep track of the maximum area discovered so far. Initially, ans is set to 0.
- 3. Enter a loop that continues as long as i is less than j. This loop allows us to explore all possible combinations of lines from i to j to maximize the area.

If height[i] < height[j], then we increment i (i += 1) to potentially find a taller line.

- 4. Inside the loop, calculate the area trapped between the lines at pointers i and j using the formula: area = (j i) * min(height[i], height[j]). This calculates the width of the container (j i) and multiplies it by the height, which is the
- 5. Update ans with the maximum of its current value and the calculated area. ans = max(ans, area) ensures that ans holds the highest value of trapped water area at each step.
- 6. Determine which pointer to move. We need to move the pointer corresponding to the shorter line since this is the limiting factor for the height of the trapped water. We do this using a conditional statement:
- Else, decrement j (j -= 1) for the same reason from the other end.
 Continue looping until the pointers meet. At this point, ans would have the maximum area that can be trapped between any two
- This solution uses a <u>greedy</u> approach, and its efficiency stems from the fact that at each stage, the move made is the best possible move to increase or at least maintain the potential of the maximum area. By incrementally adjusting the width and height of the

done within the loop.

Example Walkthrough

The algorithm has a linear-time complexity, O(n), as each element is visited at most once, and there's a constant amount of work

Let's illustrate the solution approach using a small example.

1 Ma start with two pair

lines.

1. We start with two pointers: i at the start (0), representing the first line, and j at the end (8), representing the last line. Thus, i points to height [0] which is 1, and j points to height [8] which is 7.

2. We set ans = 0, as we have not calculated any area yet.

3. Now we start our loop where i < j. Since 0 < 8, we enter the loop.

Consider the integer array height = [1, 8, 6, 2, 5, 4, 8, 3, 7].

considered container, it efficiently narrows down to the optimal solution.

- 4. We calculate the area between lines at pointers i and j. The width is j i which is 8 0 = 8, and the height is the smaller of
- 7. Our two pointers now are at i = 1 and j = 8. We will continue this process until i and j meet.

5. We update ans to be the maximum of its current value and the calculated area. So, ans = max(0, 8) = 8.

8. Repeat steps 4-6:

6. Since height[i] is less than height[j], we move the i pointer to the right to potentially find a taller line. Now i becomes 1.

Update ans to be max(8, 49) = 49.
 Since height[1] is greater than height[8], we move j to the left (now j is 7).

• New area at pointers i = 1 and j = 8: area = (8 - 1) * min(8, 7) = 7 * 7 = 49.

two heights at height[i] and height[j], so min(1, 7) = 1. Thus, the area is 8 * 1 = 8.

- 9. Continue iterations:
 - ans remains 49 since 49 > 18.
 height[1] is greater than height[7], so we move j to the left (now j is 6).

• New area at pointers i = 1 and j = 7: area = (7 - 1) * min(8, 3) = 6 * 3 = 18.

10. The process continues in this manner, always moving the pointer at the shorter height until i and j are equal.

amount of water that can be trapped between two lines without spilling.

Calculate the area formed between the two pointers

Update the maximum area if current_area is larger

current_area = (right - left) * min(height[left], height[right])

def maxArea(self, height: List[int]) -> int:

if height[left] < height[right]:</pre>

while left < right:</pre>

Python Solution

Initialize two pointers, one at the beginning and one at the end of the height array

left, right = 0, len(height) - 1
fight = 0,

At the end of these iterations, and holds the maximum area that can be trapped, which in this example, is 49. This is the largest

```
max_area = max(max_area, current_area)

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15  # Move the pointer that points to the shorter line inward,
16  # since this might lead to a greater area
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class Solution {

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public int maxArea(int[] height) {

left++;

right--;

++left;

--right;

} else { // Otherwise, move the right pointer to the left

return maxArea; // Return the maximum area found

} else {

int right = height.length - 1;

// Variable to keep track of the maximum area

maxArea = Math.max(maxArea, currentArea);

if (height[left] < height[right]) {</pre>

// Iterate until the two pointers meet

int left = 0;

int maxArea = 0;

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class Solution:

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left += 1
18
19
               else:
20
                   right -= 1
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22
           # Return the maximum area found
           return max_area
Please note that the type hint List[int] requires importing List from the typing module in Python 3.5+. If you're using Python 3.9+
it's also possible to use built-in list type hints directly like list[int]. If you want to include the necessary import, here's how you
would do that:
1 from typing import List # This line is needed for the type hint (Python 3.5 - 3.8)
   class Solution:
       # ... rest of the code remains the same
Java Solution
```

while (left < right) {
 // Calculate the area with the shorter line as the height and the distance between the lines as the width
 int currentArea = Math.min(height[left], height[right]) * (right - left);
 // Update the maximum area if the current area is larger</pre>

// Move the pointer that points to the shorter line towards the center

// Method to find the maximum area formed between the vertical lines

// Initialize two pointers at the beginning and end of the array

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24
           // Return the maximum area found
27
            return maxArea;
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C++ Solution
   #include <vector>
   #include <algorithm> // Include algorithm for std::min and std::max
   class Solution {
   public:
       int maxArea(vector<int>& heights) {
            int left = 0; // Starting from the leftmost index
           int right = heights.size() - 1; // Starting from the rightmost index
            int maxArea = 0; // Initialize the maximum area to 0
10
           // Continue looping until the left and right pointers meet
11
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           while (left < right) {</pre>
13
               // Calculate the current area with the minimum of the two heights
               int currentArea = std::min(heights[left], heights[right]) * (right - left);
14
               // Update the maximum area if the current area is larger
                maxArea = std::max(maxArea, currentArea);
16
17
               // Move the pointers inward. If left height is less than right height
18
               // then we move the left pointer to right hoping to find a greater height
19
               if (heights[left] < heights[right]) {</pre>
20
```

```
Typescript Solution
   function maxArea(height: number[]): number {
       // Initialize two pointers, one at the start and one at the end of the array
       let leftIndex = 0;
       let rightIndex = height.length - 1;
       // Initialize the variable to store the maximum area
       let maxArea = 0;
       // Iterate until the two pointers meet
8
       while (leftIndex < rightIndex) {</pre>
9
           // Calculate the area with the current pair of lines
10
           const currentArea = Math.min(height[leftIndex], height[rightIndex]) * (rightIndex - leftIndex);
11
           // Update maxArea if the current area is larger
           maxArea = Math.max(maxArea, currentArea);
13
14
           // Move the pointer that's at the shorter line inwards
15
           // If the left line is shorter than the right line
16
           if (height[leftIndex] < height[rightIndex]) {</pre>
17
               ++leftIndex; // Move the left pointer to the right
18
19
           } else {
20
               --rightIndex; // Move the right pointer to the left
21
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24
       // Return the maximum area found
25
       return maxArea;
26 }
27
```

The given Python code implements a two-pointer technique to find the maximum area of water that can be contained between two

The function initializes two pointers at the start and end of the array respectively and iterates inwards until they meet, performing a constant number of operations for each pair of indices. Since the pointers cover each element at most once, the iteration is linear relative to the number of elements n in the height array.

Space Complexity

Time Complexity

Hence, the time complexity is 0(n).

The code uses a fixed number of integer variables (i, j, ans, and t) and does not allocate any additional memory that scales with the

size of the input array.

Thus, the space complexity is 0(1).

Time and Space Complexity

lines, given an array of line heights.