2527. Find Xor-Beauty of Array



Problem Description

This LeetCode problem provides us with an integer array called nums which is 0-indexed. It introduces a concept of effective value for any triplet of indices in the array (i, j, k). The effective value for these indices is calculated as ((nums[i] | nums[j]) & nums[k]) where | represents the bitwise OR operation and & represents the bitwise AND operation. The xor-beauty of the array is the result of performing a bitwise XOR operation on all the effective values of all possible triplets of indices within

the array. The requirement is to calculate and return this xor-beauty value.

• $0 \ll i$, j, $k \ll n$ indicates that each of the indices must be within the bounds of the array.

Important things to note:

- The bitwise OR (|) takes two bit patterns and performs the logical inclusive OR operation on each pair of corresponding bits.
- The bitwise AND (§) takes two bit patterns and performs the logical AND operation on every pair of corresponding bits.

Intuition

effective value and then apply the bitwise XOR operation across these values. However, the provided solution suggests a different approach, which implies that there is an observation or property in the bitwise operations that simplifies the problem significantly. The intuition behind the solution given is that the xor-beauty of the array obtained by computing the effective value for all triplets

When approaching this problem, one might initially consider iterating through all possible triplets of indices to compute each

(i, j, k) can be simplified to just perform the bitwise XOR of all elements in the input array nums. This simplified solution suggests that there must be a property of bitwise OR, AND, and XOR that makes every other value except

the numbers themselves cancel out when considering all possible combinations of triplets. Essentially, it seems that the problem boils down to xoring each number with itself for all positions i, j, and k, which results in the original value. Thus, the solution approach is to take advantage of this property and uses Python's reduce() function combined with the xor

operator from the operator module to iteratively apply the xor operation on all elements in the array, leading to the xor-beauty directly without explicitly calculating the effective values for all triplets. **Solution Approach**

The provided Python code for this problem uses a functional programming style. It employs the use of the reduce function from Python's functools module. The reduce function applies a given function cumulatively to the items of a sequence, from left to

right, so as to reduce the sequence to a single value. The xor operator used here is a binary function that performs the "exclusive or" operation, which is imported from Python's builtin operator module. This operation takes two bits and returns 1 only if exactly one of the bits is 1.

Knowing that the reduce function will apply the xor operator to all elements in the sequence, here is what happens in the given solution:

2. It then iteratively applies the xor operator to the current result and the next element in the nums array. 3. This operation continues for all elements in the nums array until it has been reduced to a single value.

The final result after this process is the xor-beauty of the array, which is the cumulative result of xoring all the numbers together.

1. The reduce function initializes the reduction with the first element of the nums array.

- The use of reduce and xor indicates no specific need for handling each element position or its relationship with other elements;
- no iteration over triples or pairs is performed, and no auxiliary data structures are required. This points to an underlying pattern or property within the bitwise operations that allows for this simplified approach.

The code snippet that implements this solution is as follows: from functools import reduce from operator import xor

class Solution: def xorBeauty(self, nums: List[int]) -> int:

```
return reduce(xor, nums)
Here, the xorBeauty method is defined inside the Solution class and takes the nums array as input. It simply returns the xor-
beauty, computed by reducing the 'nums' array using bitwise XOR operation.
The key to understanding why this works lies in the properties of bitwise operations, specifically the XOR operation, which
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include the fact that xoring a number with itself results in zero, and xoring any number with zero results in the number itself. These properties seem to eliminate the need to calculate every single triplet's effective value.

Example Walkthrough Let's illustrate the solution approach with a small example using an integer array nums. Imagine that nums is given to us as [3, 5, 7].

Firstly, to follow the problem's statement directly without the optimized solution, we would potentially look at all possible triplets

and calculate their effective values, which would be: • For triplet (i=0, j=0, k=0), the effective value is ((nums[0] | nums[0]) & nums[0]) which equals (3 | 3) & 3 so 3 & 3 which results in 3.

• For triplet (i=0, j=0, k=1), the effective value is ((nums[0] | nums[0]) & nums[1]) which equals 3 & 5 resulting in 1.

• This process would continue for all possible triplets (i, j, k) where i, j, k range from 0 to 2. Considering there are 3 elements, we have 3³ or 27 such triplet combinations. We would then run the bitwise XOR operation on

But according to our given solution, we don't need to do all that work. Let's apply the simplified solution on our example array [3,

5, 7] by performing a cumulative XOR operation on all the elements: 1. We start with the first element, which is 3.

So, using the simplified solution, the xor-beauty of the array [3, 5, 7] is calculated to be 1.

The process used in the simplified solution involves no explicit combinatorial effective value calculation and animates the bitwise

Here is how the aforementioned Python code snippet from the solution approach would execute this example:

from functools import reduce

xor beauty = reduce(xor, nums)

Solution Implementation

from typing import List

Python

all these 27 effective values to get the xor-beauty.

from operator import xor nums = [3, 5, 7]

operations' commutative and associative properties to achieve the same result more efficiently.

2. Next, we apply the xor operator with the second element: 3 xor 5 which gives us 6.

3. Lastly, we xor this result with the third element: 6 xor 7 which gives us 1.

print(f"The xor-beauty of the array {nums} is: {xor_beauty}") The output of this code snippet will be: "The xor-beauty of the array [3, 5, 7] is: 1".

Import 'List' type from 'typing' module for type hinting

class Solution: def xor beauty(self, nums: List[int]) -> int: # Perform a pairwise XOR operation on all elements in `nums` # The `reduce` function applies the `xor` operation cumulatively to the items of `nums`,

from left to right, so as to reduce the iterable `nums` to a single value.

from functools import reduce # Import the 'reduce' function from 'functools' module

from operator import xor # Import 'xor' function from 'operator' module

Here `xor` is used as the binary operation function.

Example usage: # sol = Solution() # result = sol.xor beauty([1, 2, 3, 4]) # print(result) # This would output the cumulative XOR of the array elements

return reduce(xor, nums)

for (int number : nums) {

result ^= number;

function xorBeauty(nums: number[]): number {

return result;

```
Java
class Solution {
    // Method to calculate the XOR beauty of an array
    public int xorBeauty(int[] nums) {
        // Initialize result variable to hold the cumulative XOR
        int result = 0;
```

// Iterate through all elements in the nums array

// XOR the current number with the result so far

// Return the final XOR result which represents the XOR beauty

// The XOR of a single number with itself is 0, and the XOR with 0 is the number itself.

// and each element in the array (from left to right) to reduce it to a single value.

// Hence, the XOR of all numbers in the array gives us the "beauty" of the array.

// @returns {number} - The result of XOR operation on all the elements of the array.

// @param {number[]} nums - An array of numbers to find the XOR "beauty" of.

// The reduce() method applies a function against an accumulator

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#include <vector>
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C++

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class Solution {
public:
    // Function to calculate the "xorBeauty" of given numbers.
    int xorBeauty(vector<int>& nums) {
        int result = 0; // Initialize the result to zero.
        // Iterate over each number in the given vector.
        for (const int& number : nums) {
            result ^= number; // Compute the cumulative XOR of the numbers, storing in result.
        // The result is the XOR of all elements in nums.
        return result;
};
TypeScript
// Function that calculates the XOR of all elements in an array.
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// Here, it starts with an initial value of 0 and applies XOR operation to all elements. return nums.reduce((accumulator: number, current: number) => accumulator ^ current, // XOR operation 0 // Initial value for the accumulator

```
from functools import reduce # Import the 'reduce' function from 'functools' module
from operator import xor # Import 'xor' function from 'operator' module
from typing import List  # Import 'List' type from 'typing' module for type hinting
class Solution:
    def xor beauty(self, nums: List[int]) -> int:
       # Perform a pairwise XOR operation on all elements in `nums`
       # The `reduce` function applies the `xor` operation cumulatively to the items of `nums`,
       # from left to right, so as to reduce the iterable `nums` to a single value.
       # Here `xor` is used as the binary operation function.
       return reduce(xor, nums)
# Example usage:
# sol = Solution()
# result = sol.xor beauty([1, 2, 3, 4])
# print(result) # This would output the cumulative XOR of the array elements
Time and Space Complexity
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Time Complexity

Space Complexity

input size.

The time complexity of the given code is O(n), where n is the length of the nums list. This is because reduce applies the xor operation sequentially to the elements of the list, processing each element exactly once.

The space complexity of the given code is 0(1). The reduce function uses a constant amount of space to apply the xor

operation since it only needs to maintain the cumulative xor result and does not require any additional space that depends on the