

### **Problem Description**

Bit Manipulation

Array

In the given problem, there is an array named arr that contains n non-negative integers which we can't see because it is hidden. This arr array has been transformed into another array named encoded with a length of n - 1. This transformation uses the bitwise XOR operation: each element of encoded is the result of XORing consecutive elements in arr, i.e., encoded[i] = arr[i] XOR arr[i + 1]. The XOR operation is a bitwise operation that outputs 1 only if the input bits are different, and 0 otherwise.

The challenge is to reconstruct the original arr array given the encoded array and the first element of arr (referred to as first or arr[0]). The description assures that there is a unique solution for arr.

### Intuition

Easy

The XOR operation plays a crucial role here because it has a unique property: it's reversible if we know one of the operands. Meaning, if we have a XOR b = c, we can find a by doing c XOR b, and similarly, find b by doing c XOR a. This is because performing XOR twice with the same number cancels out the operation (e.g., a XOR b XOR b is equal to a).

This property makes it possible to recover the arr array starting from the provided first element (arr[0]). The intuition behind the solution is simply to iterate through the encoded array and apply the XOR operation between the last known value of arr and the current element in encoded to find the next value of arr. In essence, given arr[i] and encoded[i], we can solve for arr[i + 1] by calculating arr[i] XOR encoded[i].

By starting with arr[0] as first and iteratively applying the XOR operation with the encoded values, we can decode the entire arr array. The solution process unfolds one element at a time, until all values in arr are revealed.

# **Solution Approach**

The implementation utilizes a simple for loop and the append method on lists in Python. For those unfamiliar with Python, appending to a list adds a new element to the end of the list. The algorithm works as follows:

We then iterate over each element e in the encoded array.

• Initially, the known first element of arr (given as first) is appended to an empty list named ans.

- In each iteration, we XOR the last element of ans with e. In terms of the algorithm, if ans [-1] is the last element of the list ans, then e is XORed with ans [-1], and the result is the next element in arr, which is then appended to ans.
- This method leverages the reversible property of XOR mentioned earlier: encoded[i] = arr[i] XOR arr[i + 1] implies arr[i + 1] = encoded[i] XOR arr[i]. Since arr[i] is the last known element (initially first), we can decode arr[i + 1] using the elements of encoded.

The loop continues until we have reconstructed the entire arr array.

The Solution class and its decode method, provided in the reference solution, are examples of the use of Python's object-oriented programming paradigm. The decode method encapsulates the aforementioned algorithm. There are no specific data structures besides the list used for the result, and no complex patterns -- it's a straight application of XOR to decode each subsequent number in the sequence.

Start by creating a result list ans with the first element first.

Here's an explicit breakdown of the steps in the decode function:

- Iterate over the encoded array using a for loop.
- In each iteration, XOR the last element of ans with the current element in encoded and append the result to ans.
- Continue until all elements in encoded have been used.
- The list ans is now the decoded arr array, which we return from the function.
- Example Walkthrough

### Let's illustrate the solution approach with a small example. Suppose we have the following encoded array and first element:

• encoded = [6, 1, 4]

```
We know that encoded[i] is derived from arr[i] XOR arr[i + 1]. So the original array arr starts with first and has n elements, with
```

first = 5 (which is actually arr[0])

n = len(encoded) + 1.

Step 1: Initialize the result list with first

Now we will use the given solution approach to decode the original array arr.

```
• ans = [5]
```

#### Calculate 5 XOR 6 which equals 3 Append 3 to ans

Step 2: XOR first with the first element of encoded

- ans becomes [5, 3]
- Step 3: XOR the last element of ans (now 3) with the next element of encoded

Append 2 to ans

### • ans becomes [5, 3, 2]

Calculate 3 XOR 1 which equals 2

- Step 4: XOR the last element of ans (now 2) with the next element of encoded
- Calculate 2 XOR 4 which equals 6 Append 6 to ans

ans becomes [5, 3, 2, 6] At this point, we've performed an XOR operation with all elements of the encoded array, and our result list now contains all elements

property of the XOR operation can be utilized to solve this type of decoding problem iteratively.

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of the original array arr.
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The decoded original array arr is [5, 3, 2, 6].

Using the given solution approach, we are able to reconstruct arr from encoded and first. This illustrates how the reversible

## **Python Solution**

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from typing import List

# Return the fully decoded list

\* Decodes an encoded array with the given first element value.

// The length of the decoded array is one more than the length of the encoded array.

decoded.push\_back(first); // Add the first element to the decoded vector

// The next number is found by XORing the current number with the encoded number

public int[] decode(int[] encoded, int first) {

// Decode the rest of the encoded vector

for (int i = 0; i < encoded.size(); ++i) {</pre>

decoded.push\_back(decoded[i] ^ encoded[i]);

return decoded; // Return the fully decoded vector

int[] decodedArray = new int[n + 1];

int n = encoded.length;

return decoded list

class Solution:

**Final Result:** 

```
def decode(self, encoded: List[int], first: int) -> List[int]:
           # Initialize the result list with the first element
           decoded_list = [first]
           # Iterate over the encoded list and decode each element
           for encoded_element in encoded:
               # The next number is found by XORing the last number in the decoded list
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               # with the current encoded element
               decoded_list.append(decoded_list[-1] ^ encoded_element)
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```

#### \* @param encoded The array of integers to be decoded. \* @param first The first element of the decoded array. \* @return The decoded array of integers. 9

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**Java Solution** 

class Solution {

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           // Setting the first element of the decoded array.
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           decodedArray[0] = first;
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           // Iterating through the encoded array to decode it.
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           for (int i = 0; i < n; ++i) {
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               // The current element is obtained by XORing the previous element of the decoded
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               // array with the current element of the encoded array.
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               decodedArray[i + 1] = decodedArray[i] ^ encoded[i];
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           // Returning the decoded array.
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           return decodedArray;
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28 }
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C++ Solution
   #include <vector> // Include the vector header to use std::vector
   class Solution {
   public:
       // Decodes an encoded vector using the first element
       // @param encoded: the encoded vector of integers
       // @param first: the first element to start decoding
       // @return the decoded vector of integers
       std::vector<int> decode(std::vector<int>& encoded, int first) {
           std::vector<int> decoded; // Create an empty vector to store the decoded numbers
```

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Typescript Solution
   // Import the Array type from TypeScript for type annotations
   import { Array } from "typescript";
   // Decode an encoded array using the first element
  // @param encoded — the encoded array of numbers
6 // @param first — the first element to start decoding
7 // @return the decoded array of numbers
   function decode(encoded: Array<number>, first: number): Array<number> {
       let decoded: Array<number> = []; // Create an empty array to store the decoded numbers
       decoded.push(first); // Add the first element to the decoded array
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       // Decode the rest of the encoded array
       for (let i = 0; i < encoded.length; i++) {</pre>
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           // The next number is found by XORing the current number with the encoded number
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           decoded.push(decoded[i] ^ encoded[i]);
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       return decoded; // Return the fully decoded array
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19 }
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```

### result to the ans list. Therefore, since each operation in the loop takes 0(1) time and the loop runs for n iterations, the overall time complexity is O(n).

Time and Space Complexity **Time Complexity** The given Python function decode consists of a single loop that iterates through the encoded list, which has n elements, where n is the length of the encoded list. Within the loop, there is a constant time operation which performs an XOR operation (^) and appends the

Space Complexity The space complexity of the function decode is determined by the ans list which the function populates and returns. Since the ans list will contain exactly n + 1 elements after processing an encoded list of length n, the space complexity is 0(n). The space required grows linearly with the input size, making the space complexity linear as well.