1845. Seat Reservation Manager

Heap (Priority Queue) Medium Design

Problem Description

The problem involves designing a system to manage seat reservations for a series of seats that are sequentially numbered from 1 through n, where n is the total number of seats available. The system should support two key operations: reserving a seat and unreserving a seat. When a seat is reserved, it should be the seat with the smallest number currently available. Unreserving will return a previously reserved seat back into the pool of available seats.

Initialization (SeatManager(int n)): The constructor of the system takes an integer n which represents the total number of seats. It should set up the initial state with all seats available for reservation.

In Python, we have access to a min-heap implementation through the heapq module.

The operations that the system needs to support are as follows:

- Reserve (int reserve()): This operation should return the smallest-numbered seat that is currently unreserved, and then reserve it (making it no longer available for reservation).
- Unreserve (void unreserve(int seatNumber)): This function takes an integer seatNumber and unreserves that specific seat, making it available again for future reservations.
- Intuition

The solution to this problem requires an efficient data structure that can constantly provide the smallest-numbered available seat and also allow reserving and unreserving seats in a relatively fast manner. A min-heap is a suitable data structure for this problem

as it can always provide the minimum element in constant time and supports insertion and deletion operations in logarithmic time.

smallest available seat number.

smallest element is at the root, making it easy to access it quickly.

Here's the intuition behind each part of the solution:

Reserve: When reserving a seat, we pop the smallest element from the heap using the heappop function, which gets us the • smallest-numbered seat available. This operation also removes this seat from the pool of available seats. **Unreserve:** To unreserve a seat, we push the seat number back into the min-heap using the heappush function. This means

Initialization: We initialize the state by creating a list of all available seats. We then transform this list into a heap using the

heapify function from the heapq module. This sets up our min-heap, ensuring that we always have quick access to the

- the seat is again counted among the available seats and can be reserved in a future operation. Overall, the min-heap maintains the state of available seats, ensuring the system can efficiently handle the reservation state and
- **Solution Approach**

The solution to the problem uses a priority queue data structure, which is implemented using a heap in Python with the heapq module. The heap is a specialized tree-based data structure that satisfies the heap property — in the case of a min-heap, the

Initialization (__init__ method): We initialize our SeatManager with an array (list) containing all possible seat numbers. This • array is denoted as self.q (representing a queue) and holds integers from 1 to n inclusive. The heapify function is then called

def reserve(self) -> int:

return heappop(self.q)

seat allocations.

smallest element, which will be at index 0. def __init__(self, n: int): self.q = list(range(1, n + 1))heapify(self.q)

returns the smallest element from the heap, which corresponds to the smallest-numbered available seat as per our problem

statement. Since the heap property is maintained after the pop operation, the next smallest element will come to the front.

Unreserve (unreserve method): When a seat needs to be unreserved, the heappush function is used. It takes the seat number

and adds it back to our heap selfig. The heappush function automatically rearranges elements in the heap to ensure the heap

on self.q to transform it into a heap. This operation rearranges the array into a heap structure, so it's ready to serve the

Reserve (reserve method): To reserve a seat, we use the heappop function on our heap self.q. This function removes and

Here's a walkthrough of the algorithm and data structures used in each method of the SeatManager class:

property is maintained after adding a new element. def unreserve(self, seatNumber: int) -> None: heappush(self.q, seatNumber) The key insights in applying a min-heap for this solution are the constant time access to the minimum element and the

logarithmic time complexity for insertion and deletion operations. The way the min-heap self-adjusts after a pop or push

operation ensures that the sequence of available seats is always well-organized for the needs of the reserve and unreserve

Let us consider an example where n = 5, which means that the SeatManager is initialized with 5 seats available.

The SeatManager is set up by calling SeatManager (5).

• The method returns 2, making that seat reserved.

• The self.q is now [3, 4, 5] with 3 at the root.

Next, if another reserve request comes:

• The reserve method then returns this value, so seat 1 is now reserved.

• After applying heapify(self.q), self.q becomes a min-heap but remains [1, 2, 3, 4, 5] since it is already in ascending order and satisfies the heap property (the smallest element is at the root). When a client calls reserve() for the first time:

If we reserve again: • Calling reserve() pops the root, which is now seat 2.

methods.

Example Walkthrough

• The unreserve method calls heappush(self.q, 2), which adds seat 2 back to the heap.

• The heap structure is maintained, and self.q automatically readjusts to [2, 3, 4, 5] as it becomes the root again.

• The reserve method calls heappop(self.q), which removes the root of the heap, the smallest element: seat 1.

• Calling reserve() now would pop 2 from the heap again (even though we put it back earlier). • The reserve method returns 2 once more, reserving it again.

• The self.q state is [3, 4, 5] with seat 3 ready to be the next one reserved.

Initializing a list of seat numbers starting from 1 to n

In a min-heap, the smallest element is always at the root

Releasing a previously reserved seat by adding it back into the heap

The heappush function automatically maintains the heap property

self.available_seats = list(range(1, n + 1))

Reserving the smallest available seat number

return heapq.heappop(self.available_seats)

def unreserve(self, seat_number: int) -> None:

and then rearranging the heap

An example on how to use the SeatManager class

(i.e., popping the root element from the min-heap)

heapq.heappush(self.available_seats, seat_number)

// SeatManager manages the reservation and releasing of seats

// PriorityQueue to store available seat numbers in ascending order

Heapifying the list to create a min-heap

heapq.heapify(self.available_seats)

Now, let's assume a client wants to unreserve seat 2. They call unreserve(2):

• When initialized (__init__), we start with self.q listing seat numbers [1, 2, 3, 4, 5].

• The self.q looks like [2, 3, 4, 5] now, with 2 being the next available seat as the root.

is always at the root and can be reserved or unreserved in a consistent and predictable manner.

This example demonstrates how a min-heap structure is essential for efficiently managing the smallest seat number reservation

and is perfectly suited to the requirements of the problem described. The ordering of the heap ensures that the smallest number

import heapq # Importing heapq for heap operations

def __init__(self, n: int):

def reserve(self) -> int:

Solution Implementation

Python

class SeatManager:

```
# obj.unreserve(seat_number)
Java
```

obj = SeatManager(n)

seat_number = obj.reserve()

import java.util.PriorityQueue;

public class SeatManager {

```
private PriorityQueue<Integer> availableSeats;
    // Constructor initializes the PriorityQueue with all seat numbers
    public SeatManager(int n) {
        availableSeats = new PriorityQueue<>();
        // Add all seats to the queue, seat numbers start from 1 to n
        for (int seatNumber = 1; seatNumber <= n; seatNumber++) {</pre>
            availableSeats.offer(seatNumber);
    // reserve() method to reserve the seat with the lowest number
    public int reserve() {
       // Polling gets and removes the smallest available seat number
        return availableSeats.poll();
    // unreserve() method to put a seat number back into the queue
    public void unreserve(int seatNumber) {
        // Offering adds the seat number back to the available seats
        availableSeats.offer(seatNumber);
// Example of how the SeatManager might be used:
// SeatManager manager = new SeatManager(n);
// int seatNumber = manager.reserve(); // Reserves the lowest available seat number
// manager.unreserve(seatNumber); // Unreserves a seat, making it available again
C++
```

```
private:
   // Priority queue to manage the available seats. Seats are sorted in ascending order.
    std::priority_queue<int, std::vector<int>, std::greater<int>> seats;
};
```

* // Initialization

/**

#include <queue>

public:

#include <vector>

class SeatManager {

SeatManager(int n) {

int reserve() {

seats.pop();

for (int i = 1; $i \le n$; ++i) {

int allocatedSeat = seats.top();

// Return the reserved seat number.

seats.push(i);

return allocatedSeat;

void unreserve(int seatNumber) {

seats.push(seatNumber);

* use its reserve and unreserve methods.

// Add all seats to the array in ascending order.

// Sort the array to maintain the priority queue behavior.

// Shift the first element from the array and return it,

// representing the reservation of the lowest available seat.

for (let i = 1; i <= n; ++i) {

seatsArray.sort((a, b) => a - b);

seatsArray.push(i);

function reserve(): number {

initializeSeatManager(10);

// Unreserve a specific seat.

unreserve(reservedSeatNumber);

let reservedSeatNumber = reserve();

// Reserve a seat.

```
* SeatManager* seatManager = new SeatManager(n);
* // Reserve a seat
* int reservedSeatNumber = seatManager->reserve();
* // Unreserve a specific seat
* seatManager->unreserve(seatNumber);
* // Remember to free allocated memory if it's no longer needed, to avoid memory leaks
* delete seatManager;
TypeScript
// Initialize variables for seat management.
let seatsArray: number[] = [];
// Function that initializes the seat manager with a given number of seats.
function initializeSeatManager(n: number): void {
   // Ensure the seats array is empty before initialisation.
   seatsArray = [];
```

// This is to ensure the smallest number is always at the start of the array.

// Function that reserves the lowest-numbered seat that is available and returns the seat number.

// Constructor that initializes the seat manager with a given number of seats.

// Reserves the lowest-numbered seat that is available and returns the seat number.

// Get the smallest available seat number from the priority queue.

// Remove the seat from the priority queue as it is now reserved.

// Unreserves a previously reserved seat so it can be used again in the future.

// Add the seat back to the priority queue as it is now available.

* This code snippet shows how to create an instance of the SeatManager and

// Add all seats to the priority queue in ascending order.

```
let allocatedSeat = seatsArray.shift();
    // Return the reserved seat number.
    return allocatedSeat ?? -1; // Returns -1 if no seat is available (in a case where the array is empty).
// Function to unreserve a previously reserved seat so it can be used again in the future.
function unreserve(seatNumber: number): void {
    // Add the seat number back to the array.
    seatsArray.push(seatNumber);
    // Sort the array to re-establish priority queue order.
    seatsArray.sort((a, b) => a - b);
// Usage example:
// Initialize the seat manager with a number of seats.
```

```
// Note: In a real implementation, care should be taken to handle errors
  // or exceptional conditions, such as trying to unreserve a seat that has not been reserved.
import heapq # Importing heapq for heap operations
class SeatManager:
   def __init__(self, n: int):
       # Initializing a list of seat numbers starting from 1 to n
        self.available_seats = list(range(1, n + 1))
       # Heapifying the list to create a min-heap
       # In a min-heap, the smallest element is always at the root
        heapq.heapify(self.available_seats)
   def reserve(self) -> int:
```

obj = SeatManager(n) # seat_number = obj.reserve() # obj.unreserve(seat_number)

Releasing a previously reserved seat by adding it back into the heap

The heappush function automatically maintains the heap property

Reserving the smallest available seat number

return heapq.heappop(self.available_seats)

def unreserve(self, seat_number: int) -> None:

and then rearranging the heap

An example on how to use the SeatManager class

Time and Space Complexity

Time Complexity

(i.e., popping the root element from the min-heap)

heapq.heappush(self.available_seats, seat_number)

• init method: O(n) - Constructing the heap of size n takes O(n) time.

- reserve method: O(log n) Popping the smallest element from the heap takes O(log n) time, where n is the number of unreserved seats. • unreserve method: O(log n) - Pushing an element into the heap takes O(log n) time.
- **Space Complexity**

• The space complexity for the entire SeatManager is O(n) where n is the number of seats. This accounts for the heap that stores the seat numbers.