# 2113. Elements in Array After Removing and Replacing Elements

Medium <u>Array</u>

## **Problem Description**

The problem presents an array nums representing a sequence of integers and a dynamic process that alternately removes elements from the beginning of the array and restores them after the array has been emptied. This process repeats indefinitely. Explicitly, each minute, one element from the beginning of the array is removed until the array is empty. Subsequently, each minute, an element is appended to the end of the array in the same order they were removed until nums is restored to its original

state. The problem also provides a set of queries where each query is a pair consisting of a minute time\_j and an index index\_j. The

task is to find out what element, if any, exists at the given index at the specific time. If the index at a given time exceeds the current length of the array (since elements may have been removed or not yet restored), the answer to that query is -1. Intuition

The key to solving this problem lies in recognizing the cyclic nature of changes to the array. The array completes one cycle of

need to determine the state of the array at a given point in this cycle to answer the queries.

## changes every 2 \* length(nums) minutes: half of the cycle for removing elements and the other half for restoring them. Thus, we

Firstly, since the array repeats the same pattern every 2 \* n minutes (n being the initial length of nums), we can simplify each query time t by using the modulus operator t % (2 \* n) to find the equivalent time within the first cycle.

Next, we identify two distinct phases within a cycle: The removal phase: this lasts for the first n minutes of the cycle. In this phase, we can simply check whether the index i

specified in the query is still within the bounds of the array after t elements are removed from the start. The current element

The **restoration phase**: this starts after the removal phase and lasts until the end of the cycle (from minute n to minute 2 \* n).

can be directly accessed as nums[i + t].

- During this phase, we can find out if the element at i has been restored by checking if i < t n (which means that the element at index i has already been appended back). In this case, the element at index i is simply nums [i].
- **Solution Approach** To implement the solution, we must navigate through the queries to determine the values at specific times. Here's a step-by-step approach that is followed by the given solution:

answers to each query. The variable n holds the length of nums, and m holds the number of queries.

Initialization: We initialize an array ans with the same number of elements as queries filled with -1. This array will store the

Query Simplification: For each query consisting of time t and index i, we first reduce t to its equivalent time within the first

cycle by calculating t %= 2 \* n. This is crucial since the array's behavior repeats every 2 \* n minutes. It avoids unnecessary

repetition by focusing on a single cycle. **Handling Queries:** 

- We loop through each query using j as the index and unpack each query into t and i. ∘ We check if the current minute t falls within the removal phase (t < n). If true, we see if the queried index i is valid after removing t elements from the beginning. The check i < n - t assures there is still an element at the index after the removal. If this is the case, we
- retrieve the value nums [i + t]. ∘ If the current minute t falls within the restoration phase (t > n), we perform a different check: i < t - n. This checks if the element at index i has been restored by this minute. If it has, we know that the element at index i is the same as nums [i] since we restore the elements in the same order they were removed.

These steps use simple iterations and conditions to determine each query's answer effectively. The algorithm's time complexity is

O(m), as each query is handled in constant time, given that we have precomputed n (the length of nums). There are no complex

**Example Walkthrough** 

[(3, 1), (0, 2), (5, 0), (10, 1)].

• For the first query (3, 1):

For the second query (0, 2):

For the third query (5, 0):

data structures used apart from an array to store the results.

• We simplify t = 3 % (2 \* 4) = 3. The new query is (3, 1).

 $\blacksquare$  t = 10 % (2 \* 4) = 2. The new query is (2, 1).

Simplification is not needed since t = 0. The query remains (0, 2).

# Determine the length of the 'nums' list and the length of 'queries'.

answers[index] = nums[target\_index + actual\_shift]

\* Finds elements in the array after performing certain query operations.

\* @param queries Instructions for each query, containing two values [t, i]

// n is the size of the nums vector; m is the size of the queries vector

// t is the number of rotations and i is the index for the current query

// and the index is within the bounds after the rotation, get the element

// that means the array has been rotated back to its original position

// and possibly further, we get the element from the original position

// which indicates that the element is not accessible after the rotation

// Since the array rotates back to the original position after n\*2 rotations,

// If the number of rotations is more than size but the index is within bounds,

// Initialize an answer vector with size m and fill it with -1

// we use modulo to simplify the number of rotations

// If the number of rotations is less than the size of nums

 $^{\prime\prime}$  If none of the above conditions meet, the answer remains -1

// t is the number of rotations and i is the index for the current query

// and the index is within the bounds after the rotation, get the element

// that means the array has been rotated back to its original position

// and possibly further, we get the element from the original position

// Since the array rotates back to the original position after n \* 2 rotations,

// If the number of rotations is more than the size but the index is within bounds,

int n = nums.size(), m = queries.size();

int t = queries[j][0], i = queries[j][1];

std::vector<int> ans(m, -1);

for (int j = 0; j < m; ++j) {

**if** (t < n && i < n - t) {

ans[j] = nums[i];

ans[j] = nums[i + t];

else if  $(t >= n \&\& i < t - n) {$ 

// Iterate over each query

t = (n \* 2);

// Iterate over each query

t %= (n \* 2);

for (let j = 0; j < m; ++j) {

let t: number = queries[j][0];

if (t < n && i < n - t) {</pre>

ans[j] = nums[i + t];

else if  $(t >= n \&\& i < t - n) {$ 

const i: number = queries[j][1];

// we use modulo to simplify the number of rotations

// If the number of rotations is less than the size of nums

# Process each query and determine the element at the given index if it exists.

# since a full rotation would bring the array back to the original state.

elif actual\_shift > num\_length and target\_index < actual\_shift - num\_length:</pre>

# The actual shift is the remainder when 'shift' is divided by twice the 'num\_length',

# Case 2: If the shift is greater than the array length and the target index is within

num\_length, query\_count = len(nums), len(queries)

answers = [-1] \* query count

# Initialize the answer list with -1 for each query.

for index, (shift, target\_index) in enumerate(queries):

# the range before the shift, update the answer.

# After processing all queries, return the answers list.

answers[index] = nums[target\_index]

The input array

\* @return Array of elements according to each query

**Initialization**: Initialize an array to store answers ans =  $\begin{bmatrix} -1, -1, -1, -1 \end{bmatrix}$  (since we have four queries). Also, we have n = 4(the length of nums) and m = 4 (the number of queries). **Query Simplification:** 

Let's walk through an example to illustrate the solution approach. Suppose we have an array nums = [1,2,3,4] and the queries

• t = 5 % (2 \* 4) = 5. The new query is (5, 0). • For the fourth query (10, 1):

∘ For (3, 1): We are in the removal phase because 3 < 4. Is index 1 valid after removing 3 elements? 1 < 4 - 3, yes. So ans [0] = nums [1 +

For (5, 0): We are in the restoration phase because 5 > 4. Is index 0 restored after 5 minutes when 1 minute of restoration has passed? 0 <</li>

3] = nums [4], but 4 is outside the index range for nums, hence ans [0] remains -1. For (0, 2): It's the beginning of the cycle. No elements have been removed yet, so ans [1] = nums [2] = 3.

**Handling Queries:** 

```
5 - 4, yes, so ans [2] = nums [0] = 1.
     ∘ For (2, 1): Still in the removal phase as 2 < 4. Is index 1 valid after 2 have been removed? 1 < 4 - 2, yes, so ans [3] = nums [1 + 2] =
       nums[3] = 4.
  Final ans array after evaluating all queries is [-1, 3, 1, 4]. Each element of ans correlates to the results of the respective
  queries, suggesting that at those specific times and indices, these were the correct values in the array.
Solution Implementation
  Python
  class Solution:
      def elementInNums(self, nums: List[int], queries: List[List[int]]) -> List[int]:
```

actual\_shift = shift % (2 \* num\_length) # Case 1: If the shift is less than the array length and the target index is within the range # after the shift, update the answer. if actual\_shift < num\_length and target\_index < num\_length - actual\_shift:</pre>

```
return answers
Java
```

class Solution {

\* @param nums

/\*\*

\*/

```
public int[] elementInNums(int[] nums, int[][] queries) {
        int numLength = nums.length; // the length of the input array
        int queryCount = queries.length; // the number of queries
        int[] result = new int[queryCount]; // array to store the result elements
       // Loop over each query
        for (int j = 0; j < queryCount; ++j) {</pre>
            result[j] = -1; // initialize the result as -1 (not found)
            int period = queries[j][0], index = queries[j][1]; // extract period (t) and index (i) from the query
            period %= (2 * numLength); // reduce the period within the range of 0 to 2*n
            // Check if the required element falls within the unshifted part of the array
            if (period < numLength && index < numLength - period) {</pre>
                result[j] = nums[index + period]; // set the element after 'period' shifts
            // Check if the required element falls within the shifted part of the array
            else if (period > numLength && index < period - numLength) {</pre>
                result[j] = nums[index]; // set the element without shift as it has cycled back
        return result; // return the result array with elements according to queries
C++
#include <vector>
class Solution {
public:
   // Function to get the elements in nums after applying rotations from queries
   std::vector<int> elementInNums(std::vector<int>& nums, std::vector<std::vector<int>>& queries) {
```

```
// Return the answer vector
       return ans;
};
TypeScript
// Importing array type from Typescript for type annotations
import { Array } from "typescript";
// Function to get the elements in nums after applying rotations from queries
function elementInNums(nums: Array<number>, queries: Array<Array<number>>): Array<number> {
    // n is the size of the nums array; m is the size of the queries array
    const n: number = nums.length;
    const m: number = queries.length;
    // Initialize an answer array with size m and fill it with -1
    let ans: Array<number> = new Array(m).fill(-1);
```

```
ans[j] = nums[i];
          // If none of the above conditions meet, the answer remains -1
          // which indicates that the element is not accessible after the rotation
      // Return the answer array
      return ans;
class Solution:
   def elementInNums(self, nums: List[int], queries: List[List[int]]) -> List[int]:
       # Determine the length of the 'nums' list and the length of 'queries'.
        num_length, query_count = len(nums), len(queries)
       # Initialize the answer list with -1 for each query.
        answers = [-1] * query_count
       # Process each query and determine the element at the given index if it exists.
        for index, (shift, target_index) in enumerate(queries):
           # The actual shift is the remainder when 'shift' is divided by twice the 'num length',
            # since a full rotation would bring the array back to the original state.
            actual_shift = shift % (2 * num_length)
           # Case 1: If the shift is less than the array length and the target index is within the range
            # after the shift, update the answer.
            if actual_shift < num_length and target_index < num_length - actual_shift:</pre>
                answers[index] = nums[target_index + actual_shift]
            # Case 2: If the shift is greater than the array length and the target index is within
            # the range before the shift, update the answer.
            elif actual_shift > num_length and target_index < actual_shift - num_length:</pre>
                answers[index] = nums[target_index]
```

# We'll analyze both the time complexity and space complexity.

# After processing all queries, return the answers list.

The time complexity of the algorithm depends on the number of queries we need to process, as the iterations inside the loop do not depend on the size of the nums list. Since we are iterating over every single query once, the time complexity is 0(m), where m

We do not have any nested loops that iterate over the length of the nums list, and the modulo and if-else operations inside the for

The code provided involves iterating over the list of queries and computing the answer for each query based on given conditions.

loop are all constant time operations. Hence, the overall time complexity is O(m).

return answers

is the number of queries.

**Time Complexity** 

Time and Space Complexity

**Space Complexity** 

## The space complexity is determined by the additional space required by the program which is not part of the input. Here, the main additional space used is the ans list, which contains one element for each query.

We do not use any additional data structures that grow with the size of the input, so there is no further space complexity to consider.

Since we create an ans list of size m, the space complexity is O(m), where m is the number of queries.

Therefore, the overall space complexity is also O(m).