



Problem Description

The problem provides us with two integers n and k. We are required to construct a list of n distinct positive integers, each ranging from 1 to n. The list needs to be such that the absolute differences between consecutive elements form a list that has exactly k distinct integers. This means that if we say our list is answer = [a1, a2, a3, ..., an], then the list formed by calculating the absolute differences |a1 - a2|, |a2 - a3|, |a3 - a4|, ..., |an-1 - an| should contain k unique values.

The task is to find any such list answer that satisfies these conditions and return it. This is an interesting problem as it mixes elements of combinatorics, construction, and the understanding of what patterns can emerge from the difference operations.

Intuition

To understand the solution approach, let's keep in mind what we're aiming for: distinct absolute differences. A key observation here is that the largest difference we can get is n - 1, which happens when you subtract 1 from n. To get k distinct differences, we can start by forming the sequence in such a way that it includes the largest differences first, which can be achieved by starting at 1, then jumping to n, then 2, and so on, alternating between the 'lows' and 'highs'.

For example, if n is 10 and k is 4, you would start with [1, 10, 2, 9...], because the differences are [9, 8, 7...] which covers 3 of the k distinct differences we need.

possible differences and starts to get smaller with each pair added to the list. Once we have created k differences, we continue the pattern in order to meet the list length n, but at this point, we no longer need to create new unique differences, just to maintain the pre-existing pattern.

Notice the alternating pattern in the for-loop where depending on the parity of i, we append either 1 (low end of unused numbers) or

The provided solution alternates between the lowest and highest numbers not yet in the answer, which naturally creates the largest

r (high end of unused numbers). The further for-loop picking up from k to n continues the pattern based on the last number added to ensure we finish with a pattern that still has only k unique differences. Through this process, we're able to construct the desired list, satisfying the condition for k distinct differences, using a simple and

efficient approach.

The implementation provided in the reference solution uses a thoughtful pattern to satisfy the condition of k distinct differences. To

Solution Approach

walk you through it:

ans. This is determined by checking the parity of i, the loop index. If it's even, we append and increment the 1 (the next smallest available integer) to ans. If it's odd, we append and decrement r (the next largest available integer) to ans. This loop effectively creates a "zig-zag" pattern in ans that guarantees the differences between adjacent numbers in ans have k distinct values. 2. Once we have enough distinct differences, the objective of creating k distinct integers has been met, and we only need to fill the

1. The first for-loop iterates k times. During each iteration, it alternates between the lowest and highest numbers not yet added to

- rest of ans with the remaining numbers in a way that doesn't create new distinct differences. This is done with the second forloop which starts iterating from k up to n-1. The appending in this loop continues the established pattern based on the last number added to ans before this loop began. ∘ If k is even, then the pattern must continue with the decreasing order, hence r is appended and decremented.

∘ If k is odd, then the pattern must continue with increasing order, therefore 1 is appended and incremented.

By these steps, a valid ans with the right properties is constructed and ready to be returned as the solution.

Initialize two pointers, 1 and r, to the smallest (1) and largest (n) numbers within the specified range respectively.

- Alternate between appending 1 and r to ans, increasing 1 and decreasing r appropriately, until k distinct differences have been
- created. • Continue filling ans with the remaining numbers, ensuring the previously established pattern is maintained, until ans has a length
- of n. Return ans as the final answer.
- Example Walkthrough

Here is a high-level breakdown of the algorithm:

integers, each between 1 and 5, and the absolute differences of consecutive elements should have 3 distinct values.

2. Start the first for-loop to iterate k times. The goal here is to alternate between 1 and r to get distinct differences.

Let's illustrate the solution approach with a small example. Let's use n = 5 and k = 3. We need to create a list of 5 distinct positive

 \circ For the first iteration (i = 0 is even), append 1 to ans and increment 1. ans = [1], 1 = 2, r remains 5. \circ For the second iteration (i = 1 is odd), append r to ans and decrement r. ans = [1, 5], 1 remains 2, r = 4.

Append 1 to ans and increment 1. ans = [1, 5, 2, 3], 1 = 4, r remains 4.

def construct_array(self, n: int, k: int) -> List[int]:

Initialize pointers for the smallest and largest elements

If i is even, append from the left side (increasing numbers)

// If 'k' is even, decrement from right; otherwise, increment from left

1 // This function creates an array with a unique set of integers that have k different absolute

2 // differences. The array is of length 'n', and the differences range between 1 and k.

// This ensures that the difference is no more than 'k'

result[i] = (k % 2 == 0) ? right-- : left++;

// Return the constructed array

return result;

1. Initialize two pointers, l = 1 and r = 5 (smallest and largest numbers).

- \circ For the third iteration (i = 2 is even), append 1 to ans and increment 1. ans = [1, 5, 2], 1 = 3, r remains 4.
- 3. Now, ans contains 1, 5, 2. The absolute differences so far are [4, 3]. We have our k = 3 distinct differences, because when we append the next number, it will either be a 3 or a 2, giving us the third difference (which would be 1), without creating a fourth difference.
- 4. Determine the pattern to finish the last part of the list. We've placed 5 and 2, and k is odd, so we continue with this increasing pattern (because the last movement from 5 to 2 was a decrease).
- At this point, appending 1 or r would get the same number (4 in this case), so we can just add the remaining number to the list.

5. You finish with ans = [1, 5, 2, 3, 4]. The absolute differences of consecutive elements are [4, 3, 1, 1] which have three

This example demonstrates how the pattern works by maximizing differences first and then following the pattern to fill the rest of the list without introducing new distinct differences. The final list ans = [1, 5, 2, 3, 4] satisfies the provided conditions.

from typing import List class Solution:

```
# This list will store our answer
           result = []
9
10
           # First phase: creating k distinct differences
```

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Python Solution

distinct values: 4, 3, and 1.

left, right = 1, n

for i in range(k):

if i % 2 == 0:

result.append(left)

```
left += 1
16
               # If i is odd, append from the right side (decreasing numbers)
17
               else:
                    result.append(right)
19
                    right -= 1
20
21
22
           # Second phase: filling up the rest of the array
23
           for i in range(k, n):
               # If k is even, fill the rest of the array with decreasing numbers
               if k % 2 == 0:
26
                    result.append(right)
27
                    right -= 1
               # If k is odd, fill the rest of the array with increasing numbers
28
29
               else:
30
                    result.append(left)
31
                    left += 1
32
33
           # Return the result array
34
           return result
25
36 # Example usage
37 sol = Solution()
   print(sol.construct_array(10, 4)) # This will print an array of size 10 with exactly 4 distinct differences.
Java Solution
 1 class Solution {
       public int[] constructArray(int n, int k) {
           // Initialize left and right pointers to the start and end of the range
           int left = 1, right = n;
           // Create an array to store the result
           int[] result = new int[n];
           // Fill the first part of the array with a 'k' difference pattern
           for (int i = 0; i < k; ++i) {
               // Alternate between the lowest and highest unused numbers
10
11
                result[i] = (i % 2 == 0) ? left++ : right--;
12
           // Complete the rest of the array
14
15
           for (int i = k; i < n; ++i) {
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24 }

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C++ Solution
 1 class Solution {
 2 public:
       vector<int> constructArray(int n, int k) {
           // 'left' and 'right' are used to keep track of the smallest and largest elements remaining
           int left = 1, right = n;
           vector<int> result(n); // This will be our final result array
           // The first part of the sequence should have 'k' distinct differences
           for (int i = 0; i < k; ++i) {
 9
               // If 'i' is even, choose from the smallest values, else choose from the largest
               result[i] = (i % 2 == 0) ? left++ : right--;
11
12
13
14
           // The remaining part of the sequence should be either increasing or decreasing
           for (int i = k; i < n; ++i) {
15
               // If 'k' is even, keep decreasing, else keep increasing.
16
               // This keeps the absolute difference to 1, as required for elements after the initial 'k'
               result[i] = (k % 2 == 0) ? right-- : left++;
19
20
21
           return result; // Return the final constructed array
22
23 };
24
```

Typescript Solution

```
function constructArray(n: number, k: number): number[] {
       let leftNumber = 1;  // Initialize the starting value for the low end
       let rightNumber = n;
                               // Initialize the starting value for the high end
       const answer = new Array<number>(n); // Initialize the answer array with length n
       // Fill the first k elements of the array with the pattern to ensure k unique differences
       for (let i = 0; i < k; ++i) {
           // Alternate between the low and high end numbers to create the different differences
           answer[i] = i % 2 === 0 ? leftNumber++ : rightNumber--;
13
       // Fill the remaining elements of the array
14
       // If k is even, continue decrementing from the rightNumber
       // If k is odd, continue incrementing from the leftNumber
       for (let i = k; i < n; ++i) {
           answer[i] = k % 2 === 0 ? rightNumber-- : leftNumber++;
18
       return answer; // Return the constructed array
   // Example usage:
   // constructArray(10, 4) might return [1, 10, 2, 9, 3, 4, 5, 6, 7, 8] (k unique differences from 1 to 4)
Time and Space Complexity
```

Thus, the space complexity of the function is O(n).

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and runs until n. Therefore, the total number of operations is k + (n - k) = n, which means that every element from 1 to n is visited exactly once. This gives us a time complexity of O(n).

Time Complexity

Space Complexity The space complexity of the function is determined by the space required to store the output list, ans, which contains n elements since the function constructs an array of n unique integers. No additional data structures that grow with the input size are used.

The provided function consists of two for loops. The first loop runs k times, where k is a parameter. The second loop starts from k