128. Longest Consecutive Sequence

Hash Table

Array

Union Find

Problem Description

Medium

3] is a consecutive sequence, but [1, 3, 4] is not. Our task is to find the longest such sequence in the given array.

The tricky part of this problem is that we need to come up with a solution that has a time complexity of O(n). This means we

sequence of numbers is considered consecutive if every number follows the previous one without any gaps. For example, [1, 2,

The problem asks us to find the length of the longest sequence of consecutive numbers in an unsorted array called nums. A

cannot afford the luxury of sorting the array as it would typically require 0(n * log n) time. Thus, we must find a way to keep track of sequences efficiently, despite the order of elements being arbitrary.

set and if we can extend a consecutive sequence. A hash table, or in Python a set, is an ideal candidate because it allows us to

list to a set.

Intuition

Here's the intuition for the solution approach:

1. Convert the nums array into a set to eliminate duplicates and allow for 0(1) existence checks. It takes 0(n) time to convert the

To solve this problem in O(n) time, we need to think of a data structure that allows us to quickly check if an element exists in the

2. We iterate through each number \mathbf{x} in the original array. For each \mathbf{x} , we have two conditions:

the beginning of its sequence.

query the existence of an element in constant 0(1) time.

- If x 1 is not in the set, x could be the start of a new sequence.
 If x 1 is in the set, x is part of a sequence that started before x and we don't need to check it as it will already be covered when we check
- 3. When we find a number x that is the start of a new sequence (because x 1 is not in the set), we then proceed to check how long this sequence is by continuously incrementing y (initialized as x + 1) as long as y is present in the set.
- 4. Each time we extend the sequence, we update the length of the current sequence and update the answer ans if the current sequence is longer than the previously recorded longest sequence.
- sequence from its beginning, ensuring our algorithm runs in O(n) time.

This approach guarantees we only make a constant number of passes through the array and that we only consider each

Solution Approach

The solution approach can be decomposed into key steps that align with the algorithmic design and utilize data structures such

as hash tables effectively.

Step 1: Building a Set Firstly, we convert the given list nums into a set s. This process removes any duplicate elements and

s = set(nums)

for x in nums:

for.

Step 2: Iteration and Sequence Detection We iterate through each number x in the list nums. For each number, we check if its predecessor (x - 1) is in the set.

facilitates constant time checks for the presence of integers. This is critical as it allows for the linear time algorithm we're aiming

if x - 1 not in s:
 If x - 1 is not in the set, it implies that x could potentially be the start of a new consecutive sequence.
 Step 3: Extension of the Sequence When we find that x could be the start of a sequence, we try to find out where the sequence

ends. We initialize a variable y as x + 1 and while y is in the set, we keep incrementing y by one to extend the sequence. y = x + 1

while y in s:

y += 1

ans = max(ans, y - x)

Step 5: Return the Result Once we've considered each number in the array, we return ans as the answer to the problem, which

sequence is y - x. If this length is greater than any previously found sequences, we update our answer ans.

represents the length of the longest consecutive elements sequence found.

find the longest sequence of consecutive numbers in this array.

Duplications are removed and we can check for existence in constant time.

We iterate through nums. Assume our iteration order is the same as the array's order.

Step 4: Update Longest Sequence Length After we find a sequence starting with x and ending before y, the length of this

and satisfy the problem's constraints.

Example Walkthrough

This approach takes advantage of the hash table pattern via the set s, which provides us with the constant time lookups needed

to achieve an overall O(n) time complexity. Thus, we harness the capability of hash tables to manage our computations efficiently

Let's illustrate the solution approach using a small example. Consider the unsorted array nums = [4, 1, 3, 2, 6]. Our goal is to

We transform the nums array into a set: $s = set([4, 1, 3, 2, 6]) \# s = \{1, 2, 3, 4, 6\}$

We check if 3 (x - 1) is in the set:

Iteration 1: x = 4

Iteration 2: x = 1

while y in s:

Step 1: Building a Set

Since 3 is present, 4 is not the start of a new sequence.

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Since 0 is not present, 1 is a start of a new sequence.
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We check if ∅ (x - 1) is in the set:

Step 2: Iteration and Sequence Detection

if 3 not in s: # False, hence we skip

Step 3: Extension of the Sequence

We extend the sequence from 1 onwards to find its length:

We update ans to the length of this sequence if it is the longest found so far.

Iterations continue with 2, 3, and 6 but no other new sequence is found with a length greater than 3.

if 0 not in s: # True, thus 1 might be a sequence start

We calculate the length of the current sequence 4 - 1 which is 3. ans = max(ans, 4 - 1) # if ans was 0, it becomes 3

def longestConsecutive(self, nums: List[int]) -> int:

Create a set from the list for O(1) lookups

Check if it's the start of a sequence

Iterate over each number in the list

if number - 1 not in num_set:

current_num = number

current_streak = 1

y += 1 # y becomes 3, then 4, stops at 5

The sequence we found is 1, 2, 3, 4.

Step 4: Update Longest Sequence Length

After iterating through all numbers, the longest sequence found is from 1 to 4, which has a length of 4. Thus, ans = 4 and is returned as the solution.

Solution Implementation

num_set = set(nums)

longest_streak = 0

for number in nums:

for (int num : nums) {

int longestStreak = 0;

for (int num : nums) {

// Go through each element in the array.

if (!numSet.contains(num - 1)) {

int currentNum = num;

int currentStreak = 1;

currentNum += 1;

currentStreak += 1;

numSet.add(num);

Step 5: Return the Result

Python

class Solution:

Increment the current_num to find the length of the streak
while current_num + 1 in num_set:
 current_num += 1
 current_streak += 1

Initialize the current number as the possible start of a sequence

Update the longest_streak with the maximum streak found

longest_streak = max(longest_streak, current_streak)

// Initialize the variable for the longest consecutive sequence.

// Check if current number is the beginning of a sequence.

// Initialize the current streak length.

while (numSet.contains(currentNum + 1)) {

// Update the longest streak found so far.

// Function to find the length of the longest consecutive elements sequence.

// Check if current number is the beginning of a sequence.

// Update the longest streak if current one is longer.

longestStreak = Math.max(longestStreak, currentStreak);

// Incrementally check consecutive numbers.

// Return the length of the longest consecutive sequence.

def longestConsecutive(self, nums: List[int]) -> int:

Create a set from the list for O(1) lookups

Check if it's the start of a sequence

current_streak += 1

Iterate over each number in the list

if number - 1 not in num_set:

while (numSet.has(currentNum + 1)) {

let longestStreak = 0; // Stores the length of the longest consecutive sequence.

let currentNum = num; // Starting number of the current sequence.

let currentStreak = 1; // Initializing current streak length.

Initialize the current number as the possible start of a sequence

Update the longest_streak with the maximum streak found

longest_streak = max(longest_streak, current_streak)

Return the length of the longest consecutive sequence

// Initialising a set to store unique numbers from the input.

function longestConsecutive(nums: number[]): number {

const numSet: Set<number> = new Set(nums);

// Iterate over each number in the set.

if (!numSet.has(num - 1)) {

currentNum++;

currentStreak++;

for (const num of numSet) {

// Initialize the current number as the potential start of the sequence.

// Expand the current streak if consecutive numbers are found.

longestStreak = Math.max(longestStreak, currentStreak);

```
# Return the length of the longest consecutive sequence
    return longest_streak

Java

class Solution {
    public int longestConsecutive(int[] nums) {
        // Create a hash set to store the unique elements of the array.
        Set<Integer> numSet = new HashSet<>();

        // Add all elements to the set.
```

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// Return the longest streak length.
        return longestStreak;
#include <vector>
#include <unordered_set>
#include <algorithm>
class Solution {
public:
    int longestConsecutive(vector<int>& nums) {
       // Create an unordered set to hold unique elements for constant-time lookups.
       unordered_set<int> numbersSet(nums.begin(), nums.end());
        int longestStreak = 0; // Variable to store the length of the longest consecutive sequence found.
       // Iterate over each element in the vector.
        for (int num : nums) {
            // Check if the current number is the beginning of a sequence by looking for num -1.
            if (!numbersSet.count(num - 1)) {
                // If num is the start of a sequence, look for all consecutive numbers starting with num + 1.
                int currentNum = num + 1;
                // Continue checking for the next consecutive number in the sequence.
                while (numbersSet.count(currentNum)) {
                    currentNum++;
                // Update the longest streak with the length of the current sequence.
                longestStreak = max(longestStreak, currentNum - num);
       // Return the longest length of consecutive sequence found.
       return longestStreak;
};
TypeScript
```

return longest_streak

Time and Space Complexity

The algorithm has two main parts:

return longestStreak;

num_set = set(nums)

longest_streak = 0

for number in nums:

class Solution:

The given code is designed to find the length of the longest consecutive elements sequence in an unsorted array. It utilizes a set to achieve an average time complexity of O(n).

Time Complexity:

2. Looping through each number in the array and extending the consecutive sequence if the current number is the start of a sequence. This part is also 0(n) on average because each number is visited only once during the sequence extension process.

depend on the size of the input are used.

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Combining these two parts still results in a total of O(n) time complexity since other operations inside the loop are constant time on average, such as checking for membership in the set and updating the ans variable.
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1. Creating a set from the list of numbers, which takes O(n) time.

Space Complexity:

The space complexity is O(n) because a set is created to store the elements of the array, and no other data structures that