

1582. Special Positions in a Binary Matrix

Easy Array Matrix

[LeetCode Link](#)

Problem Description

In this LeetCode problem, we're given a binary matrix `mat`, which is made up of only `0`s and `1`s. Our task is to count how many 'special positions' are in the matrix. A special position is defined as one where the value at that position is `1` and all other values in the same row and column are `0`. Here, the matrix is indexed starting at `(0,0)` for the top-left element.

Intuition

The intuition behind the solution is to first count the number of `1`s in each row and each column. If a position `(i, j)` has a `1`, and the corresponding counts for row `i` and column `j` are both exactly `1`, then the position `(i, j)` is a special position. Here's the breakdown:

- We initialize two lists, `r` and `c`, to keep track of the count of `1`s in each row and each column, respectively.
- By double looping through the matrix, we update these counts.
- After populating `r` and `c`, we go through the matrix again, checking if a `1` is in a position `(i, j)` such that `r[i]` and `c[j]` are both exactly `1`.
- If the condition from step 3 is met, we increment our `ans` variable, which holds the count of special positions.
- We return the value of `ans` as the final result.

This approach works because for a position with a `1` to be special, it must be the only `1` in its row and column. By counting the `1`s in each row and column first, we have all the information we need to efficiently determine if a position is special during our second pass through the matrix.

Solution Approach

The solution approach follows a straightforward algorithmic pattern that is quite common in matrix-related problems, which includes the following steps:

- Initialize Count Arrays:** The code initializes two arrays `r` and `c` with lengths equal to the number of rows `m` and columns `n` of the input matrix, respectively. These arrays are used to keep track of the sum of `1`s in each row and column, hence initialized to all `0`s.
- Populate Count Arrays:** The solution uses a nested loop where `i` iterates over the rows and `j` iterates over the columns. For each cell in the matrix, if the value `mat[i][j]` is `1`, the sum in the corresponding count arrays `r[i]` and `c[j]` are incremented by `1`. This allows us to accumulate the number of `1`s for each row and each column in their respective counters.
- Identify Special Positions:** With the populated count arrays, we loop through the matrix for the second time. During this iteration, we check if the value at `mat[i][j]` is `1` and if `r[i]` and `c[j]` are both equal to `1`. This condition verifies that the current position `(i, j)` is special as it is the only `1` in its row and column.
- Count Special Positions:** If the condition in the previous step is satisfied, we increment the variable `ans` which is used to count the number of special positions.
- Return the Result:** Once the entire matrix has been scanned during the second iteration, the `ans` variable contains the total count of special positions. This value is returned as the output.

The data structures used are quite simple and effective; we are using two one-dimensional arrays (`r` for rows and `c` for columns) to keep the sums. The algorithmic pattern employed is also straightforward, involving iterations and condition checking. This approach is efficient since each element in the matrix is processed a constant number of times, resulting in a time complexity of $O(m*n)$, where `m` and `n` are the number of rows and columns in the matrix, respectively. The space complexity is $O(m+n)$, which is required for the row and column sum arrays.

Example Walkthrough

Let's consider a 3x4 binary matrix `mat` for our example:

```
1 mat = [  
2   [1, 0, 0, 0],  
3   [0, 0, 1, 0],  
4   [0, 1, 0, 0]  
5 ]
```

Following our algorithmic steps:

- Initialize Count Arrays:** We initialize two arrays `r` with length 3 (number of rows) and `c` with length 4 (number of columns), to all `0`s. So, `r = [0, 0, 0]` and `c = [0, 0, 0, 0]`.
- Populate Count Arrays:** We iterate through the matrix `mat`:
 - For `i=0` (first row), we find `mat[0][0]` is `1`, so we increment `r[0]` and `c[0]` by `1`. Now, `r = [1, 0, 0]` and `c = [1, 0, 0, 0]`.
 - For `i=1` (second row), we find `mat[1][2]` is `1`, so we increment `r[1]` and `c[2]` by `1`. Now, `r = [1, 1, 0]` and `c = [1, 0, 1, 0]`.
 - For `i=2` (third row), we find `mat[2][1]` is `1`, so we increment `r[2]` and `c[1]` by `1`. Now, `r = [1, 1, 1]` and `c = [1, 1, 1, 0]`.After populating the counts arrays, `r` and `c` now accurately reflect the number of `1`s in each row and column.

- Identify Special Positions:** With the count arrays set up, we go through the matrix once more:
 - Check position `(0,0)`. Since `mat[0][0]` is `1` and both `r[0]` and `c[0]` are exactly `1`, this is a special position.
 - Check position `(1,2)`. Since `mat[1][2]` is `1` and both `r[1]` and `c[2]` are exactly `1`, this is also a special position.
 - Check position `(2,1)`. Since `mat[2][1]` is `1` and both `r[2]` and `c[1]` are exactly `1`, this is a special position as well.Every `1` we encountered is indeed in a special position.
- Count Special Positions:** We increment our variable `ans` for each special position identified. As we found 3 special positions, `ans` would be `3`.
- Return the Result:** Our function would return `ans`, the total count of special positions, which in this case is `3`.

In this straightforward example, our methodical walk-through demonstrates that the provided binary matrix `mat` contains three special positions, as identified using the solution approach. The row and column counts help efficiently pinpoint the special positions in just two scans of the matrix.

Python Solution

```
1 class Solution:  
2     def numSpecial(self, mat: List[List[int]]) -> int:  
3         # Get the number of rows 'm' and columns 'n' of the matrix  
4         num_rows, num_cols = len(mat), len(mat[0])  
5  
6         # Initialize row_sum and col_sum to keep track of the sum of each row and column  
7         row_sum = [0] * num_rows  
8         col_sum = [0] * num_cols  
9  
10        # Calculate the sum of elements for each row and column  
11        for i, row in enumerate(mat):  
12            for j, value in enumerate(row):  
13                row_sum[i] += value  
14                col_sum[j] += value  
15  
16        # Initialize variable 'special_count' to count special positions  
17        special_count = 0  
18  
19        # Check for special positions where the value is 1  
20        # and its row and column sums are both exactly 1  
21        for i in range(num_rows):  
22            for j in range(num_cols):  
23                if mat[i][j] == 1 and row_sum[i] == 1 and col_sum[j] == 1:  
24                    # Increment the count of special positions  
25                    special_count += 1  
26  
27        # Return the final count of special positions  
28        return special_count  
29
```

Java Solution

```
1 class Solution {  
2     public int numSpecial(int[][] mat) {  
3         int numRows = mat.length, numCols = mat[0].length;  
4         int[] rowCount = new int[numRows];  
5         int[] colCount = new int[numCols];  
6  
7         // Calculate the sum of each row and each column  
8         for (int i = 0; i < numRows; ++i) {  
9             for (int j = 0; j < numCols; ++j) {  
10                rowCount[i] += mat[i][j];  
11                colCount[j] += mat[i][j];  
12            }  
13        }  
14  
15        int specialCount = 0;  
16  
17        // Iterate through the matrix to find special elements  
18        // A special element is defined as the element that is the only '1' in its row and column  
19        for (int i = 0; i < numRows; ++i) {  
20            for (int j = 0; j < numCols; ++j) {  
21                // Check if the current element is '1' and its corresponding  
22                // row and column sums are '1' which would mean it's a special element  
23                if (mat[i][j] == 1 && rowCount[i] == 1 && colCount[j] == 1) {  
24                    specialCount++;  
25                }  
26            }  
27        }  
28  
29        // Return the total count of special elements found in the matrix  
30        return specialCount;  
31    }  
32 }  
33
```

C++ Solution

```
1 class Solution {  
2 public:  
3     // Function to count the number of special positions in a binary matrix.  
4     // A position (i, j) is called special if mat[i][j] is 1 and all other elements in row i and column j are 0.  
5     int numSpecial(vector<vector<int>>& mat) {  
6         int numRows = mat.size();           // Number of rows in the matrix  
7         int numCols = mat[0].size();        // Number of columns in the matrix  
8         vector<int> rowCount(numCols, 0);    // Row count to store the sum of each row  
9         vector<int> colCount(numCols, 0);    // Column count to store the sum of each column  
10  
11        // Fill rowCount and colCount by summing the values in each row and column  
12        for (int i = 0; i < numRows; ++i) {  
13            for (int j = 0; j < numCols; ++j) {  
14                rowCount[i] += mat[i][j];  
15                colCount[j] += mat[i][j];  
16            }  
17        }  
18  
19        int specialCount = 0; // Variable to store the number of special positions found  
20  
21        // Search for special positions. A position (i, j) is special if  
22        // mat[i][j] is 1 and the sum of both row i and column j is 1.  
23        for (int i = 0; i < numRows; ++i) {  
24            for (int j = 0; j < numCols; ++j) {  
25                if (mat[i][j] == 1 && rowCount[i] == 1 && colCount[j] == 1) {  
26                    specialCount++; // Increment count if a special position is found  
27                }  
28            }  
29        }  
30  
31        return specialCount; // Return the total count of special positions  
32    }  
33 };  
34
```

Typescript Solution

```
1 function countSpecialElements(matrix: number[][]): number {  
2     // Get the number of rows and columns from the matrix  
3     const rowCount = matrix.length;  
4     const colCount = matrix[0].length;  
5  
6     // Create arrays to store the sum of elements in each row and column,  
7     // and initialize each element of the arrays to 0  
8     const rowSums = new Array(rowCount).fill(0);  
9     const colSums = new Array(colCount).fill(0);  
10  
11    // First pass: Calculate the number of 1's in each row and column  
12    for (let rowIndex = 0; rowIndex < rowCount; rowIndex++) {  
13        for (let colIndex = 0; colIndex < colCount; colIndex++) {  
14            // If the element at the current position is 1, increment  
15            // the corresponding row and column sums  
16            if (matrix[rowIndex][colIndex] === 1) {  
17                rowSums[rowIndex]++;  
18                colSums[colIndex]++;  
19            }  
20        }  
21    }  
22  
23    // Initialize the result variable which will hold the count of special elements  
24    let specialCount = 0;  
25  
26    // Second pass: Check for special elements, which are the elements  
27    // that are the only 1 in their row and column  
28    for (let rowIndex = 0; rowIndex < rowCount; rowIndex++) {  
29        for (let colIndex = 0; colIndex < colCount; colIndex++) {  
30            // Check if the current element is 1 and if it's the only one  
31            // in its row and column, if so increment the specialCount  
32            if (matrix[rowIndex][colIndex] === 1 && rowSums[rowIndex] === 1 && colSums[colIndex] === 1) {  
33                specialCount++;  
34            }  
35        }  
36    }  
37  
38    // Return the count of special elements  
39    return specialCount;  
40 }  
41
```

Time and Space Complexity

Time Complexity

The time complexity of the code can be analyzed by looking at the number of nested loops and the operations within them.

- The code first initializes the row and column count arrays `r` and `c`, which is $O(m)$ and $O(n)$ respectively, where `m` is the number of rows and `n` is the number of columns in the input `mat`.
- The first nested for loop iterates through all elements of the matrix to populate `r` and `c`, which will be $O(m * n)$ since every element is visited once.
- The second nested for loop also iterates through the entire matrix to count the number of special elements based on the conditions that rely on the previous computations stored in `r` and `c`. This is also $O(m * n)$.

Hence, the overall time complexity is $O(m * n)$ because this dominates the overall performance of the code.

Space Complexity

The space complexity of the code includes the space used for the input and any auxiliary space used:

- The input matrix itself does not count towards auxiliary space complexity as it is given.
- Two arrays `r` and `c` of length `m` and `n` are created to keep track of the sum of each row and column, which gives us $O(m + n)$.

Therefore, the auxiliary space complexity is $O(m + n)$.