1178. Number of Valid Words for Each Puzzle String Bit Manipulation <u>Trie</u> Hash Table Hard Array

Problem Description

pair of conditions for each puzzle. A word is valid with respect to a puzzle if: 1. The word contains the first letter of the puzzle.

Leetcode Link

Given a list of words and a list of puzzles, the aim is to figure out how many words from the word list are valid according to a specific

2. Every letter of the word is also in the given puzzle.

puzzle) of the puzzle mask and sum their counts in the counter.

2. **Processing the puzzles**: For each puzzle in puzzles, we:

It's important to note that it is not necessary for all letters of the puzzle to be in the word. For example, for the puzzle "abcdefg", words such as "faced", "cabbage", and "baggage" are valid because they include the first letter 'a' of the puzzle and all other letters

in these words are contained within the puzzle. On the other hand, "beefed" and "based" are invalid because "beefed" lacks the letter 'a', and "based" contains the letter 's', which is not present in the puzzle. The output is an array where each element corresponds to the number of valid words for each puzzle.

The intuition behind the solution is based on converting both puzzles and words into binary representations where each bit

efficiently.

Intuition

'a' corresponds to the least significant bit, and 'z' to the most significant bit of a 26-bit integer, since there are 26 letters in the English alphabet. We start by creating masks for the words - a mask is a binary number where a bit is set (i.e., 1) if the corresponding letter is in the

word. We use a counter to keep track of how many times every possible combination (mask) appears in the list of words. This

To represent a set of letters as a binary number, we assign each letter a bit position based on its order in the alphabet. For instance,

corresponds to a letter's presence. To tackle this kind of problem, we use bitwise operations to perform checks and counts

preprocessing is helpful because we need to compare each word with multiple puzzles, and using masks allows us to do these comparisons quickly using bitwise operations. For each puzzle, we also create a mask. We then need to count all valid word masks with respect to the puzzle mask. A word mask is valid if it includes the first letter of the puzzle, and all bits set in the word mask are also set in the puzzle mask. To find these valid

word masks, we iterate over every submask (a mask with some bits possibly turned off, but still containing the first letter of the

This way, we leverage the precomputed frequencies of each word mask to efficiently calculate the number of valid words for each puzzle. **Solution Approach**

and patterns: 1. Counter for masks of words: We create a Counter from the collections module in Python to keep track of all the unique masks created from the words list. To generate a mask, the solution goes through each character in a word and performs an OR | operation between the mask (initialized to zero) and a bit shifted by the alphabetical position of the character (1 << (ord(c) -

characters and allow for fast subset enumeration. Here's the step-by-step approach, highlighted by key algorithms, data structures,

The implementation of the solution involves understanding how bitwise operations can effectively represent unique sets of

ord("a"))). This results in a number where the bits corresponding to letters in the word are set to 1.

Countertox`.

Example Walkthrough

list puzzles = ["chloe", "dolph"].

• e: $1 << (4) \Rightarrow 00010000$

• c: $1 << (2) \Rightarrow 00000100$

• h: 1 << (7) ⇒ 10000000

Perform this process for each word:

 Compute the puzzle's mask in the same way as the word's mask. Store the first letter's position in i because it must be present in each valid word. Initialize x, which will accumulate the count of valid words for this puzzle. 3. Subset enumeration: Enumerate submasks of the puzzle's mask:

The inner while loop does the following: Starting with j as the puzzle mask, we repeatedly find submasks by decrementing

o If the submask contains the first letter of the puzzle (j >> i & 1), we add the count of this mask from our precomputed

j. The expression j = (j - 1) & mask turns off one bit at a time in the submask that is also on in the puzzle's mask.

5. Result assembly: Finally, the counts of valid words (stored in x) for each puzzle are appended to the ans list, which represents the number of valid words for each puzzle. Through this application of bitwise operations, subsets enumeration and using a counter to map set bits to frequencies, we achieve

Mathematically, if |W| is the length of the word list, and |P| is the length of the puzzle list, the algorithm efficiently compresses the

4. Edge case handling: For puzzles that don't even have one word matching, the count would simply be added as zero.

an efficient solution to a problem that might seem combinatorial and complex at first glance.

O(|W| * |P|) brute-force approach into a faster one by using bit masks and counting common patterns.

Step 1: Creating masks for words and initializing Counter:

We iterate through each word in words to create a binary mask. For instance, for "echo" the binary mask would be:

Let's use a small example to illustrate the solution approach. Say our word list is words = ["echo", "hold", "chef"] and our puzzle

OR all the above: mask for echo = 11010100

For puzzle "chloe", we find all the subset masks of the puzzle's mask. The first letter 'c' must be included, so the submask must have

For "dolph", we would do the same. The word "hold" would be the only match since it's the only word containing 'd' and all its letters

The submasks of "chloe" we consider will be (represented as strings for simplicity): "11011101", "11011100", "11011001", ...,

Our Counter would contain the count of the unique masks. From the example words, we have unique masks so each would have a count of 1 in the Counter.

Step 2: Processing the puzzles:

mask for "chloe" ⇒ 11011101

"00000100" (which represents just 'c').

So, count for "chloe" is 2.

and "dolph", respectively.

Python Solution

class Solution:

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from collections import Counter

results = []

return results

for (String word : words) {

for char in word:

bitmask_counter[bitmask] += 1

List to store the result for each puzzle

from typing import List

hold: 1000010010010

• echo: 11010100

chef: 10011000

 The mask of "echo" (11010100) is a subset of "chloe" mask, it's valid. • The mask of "hold" (1000010010010) is not a subset since 'd' is not in "chloe".

For each submask, we check if our word masks match.

are in the puzzle "dolph". So, count for "dolph" is 1.

For "chloe", the binary mask would be computed similarly to words. So:

Step 3 & 4: Enumerating subsets and counting the valid words:

Step 5: Result assembly: Finally, we would assemble our results into an array with [2, 1], which indicates the number of valid words for the puzzles "chloe"

Set the bit at the position corresponding to the character

valid_word_count += bitmask_counter[submask]

public List<Integer> findNumOfValidWords(String[] words, String[] puzzles) {

int bitmask = 0; // Initialize bitmask for the current word

// For each character in the word, update the bitmask

// Create a list to store the final count of valid words for each puzzle

int bitmask = 0; // Initialize bitmask for the current puzzle

// Initialize the valid word count for the current puzzle

int firstLetterBitmask = 1 << (puzzle.charAt(0) - 'a');</pre>

// For each character in the puzzle, update the bitmask

// Iterate over all submasks of the puzzle bitmask to find valid words

// Check if the submask includes the first letter of the puzzle

validWordCount += frequencyMap.getOrDefault(submask, 0);

vector<int> findNumOfValidWords(vector<string>& words, vector<string>& puzzles) {

// Map to store the frequency of each unique character mask for the words

mask |= 1 << (ch - 'a'); // Set the bit corresponding to the character

frequency[mask]++; // Increase the count for this bitmask representation of the word

// Populate the frequency map with the bitmask representation of words

int mask = 0; // Initialize bitmask for the current word

for (int submask = bitmask; submask > 0; submask = (submask - 1) & bitmask) {

// Add the count of words matching the submask to the total count

for (int i = 0; i < word.length(); ++i) {</pre>

List<Integer> result = new ArrayList<>();

for (String puzzle : puzzles) {

int validWordCount = 0;

result.add(validWordCount);

unordered_map<int, int> frequency;

for (auto& word : words) {

for (char& ch : word) {

return result;

bitmask |= 1 << (word.charAt(i) - 'a');

frequencyMap.merge(bitmask, 1, Integer::sum);

for (int i = 0; i < puzzle.length(); ++i) {</pre>

// Loop over each puzzle to calculate count of valid words

bitmask |= 1 << (puzzle.charAt(i) - 'a');</pre>

if ((submask & firstLetterBitmask) != 0) {

// Add the calculated count to the result list

// Return the list of valid word counts for each puzzle

Map<Integer, Integer> frequencyMap = new HashMap<>(words.length);

// Create a frequency map to store the number of occurrences of each word's bitmask

// Merge the current bitmask into the frequency map, summing up the counts

// Calculate the bitmask for the first letter of the puzzle (required in all words)

// Loop over each word to calculate the bitmask and update the frequency map

Append the count of valid words for this puzzle to the results list

 $submask = (submask - 1) & puzzle_bitmask$

results.append(valid_word_count)

bitmask |= 1 << (ord(char) - ord('a'))

Increase the count of this specific bitmask

• The mask of "chef" (10011000) is also a valid subset since all bits match and the first letter 'c' is present.

the bit for 'c' set. Then we enumerate by repeatedly removing one bit until 'c' is the only bit left.

def findNumOfValidWords(self, words: List[str], puzzles: List[str]) -> List[int]: # Initialize a counter to keep track of frequency of each unique bitmask bitmask_counter = Counter() for word in words: # Create a bitmask for each word 9 10 bitmask = 0

33 34 35 36 37 # Generate the next submask by 'turning off' the rightmost 'on' bit

Java Solution

class Solution {

19 for puzzle in puzzles: # Create a bitmask for the puzzle 20 puzzle_bitmask = 0 22 for char in puzzle: # Set the bit for each character in the puzzle 23 24 puzzle_bitmask |= 1 << (ord(char) - ord('a'))</pre> 25 26 # Count of valid words for this puzzle 27 valid_word_count = 0 28 # The first character of the puzzle is essential, store its bit position 29 first_char_bit = ord(puzzle[0]) - ord('a') # Start with the puzzle's bitmask and generate all submasks 30 31 submask = puzzle_bitmask 32 while submask: # Check if the submask includes the first character of the puzzle if submask >> first_char_bit & 1: # Add count of words that match this submask

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C++ Solution

1 #include <vector>

2 #include <string>

6 class Solution {

public:

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});

return result;

Time and Space Complexity

2. For each puzzle in the list of puzzles:

const result: number[] = [];

puzzles.forEach(puzzle => {

let puzzleBitmask = 0;

let validWordsCount = 0;

for (const char of puzzle) {

if (subset & firstCharBit) {

result.push(validWordsCount);

// Calculate the number of valid words for each puzzle

average length of the words is L, this operation is O(L).

puzzleBitmask |= 1 << (char.charCodeAt(0) - 'a'.charCodeAt(0));</pre>

const firstCharBit = 1 << (puzzle.charCodeAt(0) - 'a'.charCodeAt(0));</pre>

validWordsCount += frequencyMap.get(subset) || 0;

// Push the count of valid words for this puzzle into the result array

// Use subset generation method to iterate over all subsets of the puzzle bitmask

for (let subset = puzzleBitmask; subset; subset = (subset - 1) & puzzleBitmask) {

// Check if the first character of the puzzle is in the current subset

#include <unordered_map>

using namespace std;

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             // Vector to store the result, one entry for each puzzle
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             vector<int> results;
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             // Process each puzzle and find the number of valid words for it
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             for (auto& puzzle : puzzles) {
 26
                 int mask = 0; // Initialize bitmask for the current puzzle
 27
                 for (char& ch : puzzle) {
                     mask |= 1 << (ch - 'a'); // Set the bit corresponding to each character
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                 int count = 0; // Initialize the valid words count for the current puzzle
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                 int firstCharBit = 1 << (puzzle[0] - 'a'); // Bitmask for the first puzzle character</pre>
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                 // Iterate through all submasks of the puzzle mask
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                 for (int submask = mask; submask; submask = (submask - 1) & mask) {
                     // Check if the submask includes the first character of the puzzle
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 37
                     if (submask & firstCharBit) {
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                         count += frequency[submask]; // If it does, add the word frequency to the count
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                 // Add the count to the results vector
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                 results.push_back(count);
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             // Return the results vector containing the number of valid words for each puzzle
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             return results;
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    };
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Typescript Solution
     function findNumOfValidWords(words: string[], puzzles: string[]): number[] {
         // Create a map to count the frequency of each unique character mask
         const frequencyMap: Map<number, number> = new Map();
         // Generate a bitmask for each word and count their frequency
         words.forEach(word => {
  6
             let bitmask = 0;
             for (const char of word) {
  8
                 bitmask |= 1 << (char.charCodeAt(0) - 'a'.charCodeAt(0));</pre>
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             frequencyMap.set(bitmask, (frequencyMap.get(bitmask) || 0) + 1);
         });
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         // Initialize an array to store the number of valid words for each puzzle
```

1. For each word in the list of words: We iterate through all the characters in the word and create a bitmask representing the unique characters. Assuming the

Time Complexity

combinations in the word counter. In the worst-case scenario, there could be 2^P combinations if each puzzle has distinct letters.

 Since we need to check each of these combinations against our counter, and the first letter of the puzzle must be included, we're looking at 0(2^(P-1)) operations for each puzzle. This is because we iterate through all the subsets of the bitmask that includes the first letter.

• Similar to words, we create a bitmask for the puzzle. Assuming the average length of puzzles is P, this operation is O(P).

The novel part is trying out different combinations of the puzzle's letters represented by the bitmask and checking those

The given algorithm involves two main parts, constructing a bitmask for each word and puzzle and then solving the puzzles.

 \circ However, we perform this operation for all N words. So, the time complexity for this part is O(N * L).

 \circ Performing this for all M puzzles, the total time complexity for solving puzzles is $0(M * 2^{(P-1)})$.

2. The space complexity for storing the answer (ans) is O(M), where M is the number of puzzles.

- Combining the two parts, the total time complexity is $0(N * L + M * 2^{(P-1)})$. Note that L and P usually have upper limits (since the question constrains are such that the length of the words and puzzles would not exceed a certain length e.g., 7 for puzzles), so for very large N and M the dominant term could be either depending on the values of N, M, L, and P.
- **Space Complexity** 1. Counter for words (cnt): This will store the frequency of each unique bitmask for the words. The space used by the counter will be proportional to the number of unique bitmasks rather than the number of words themselves. Since there are at most 26 characters, and each character could be present or absent, we theoretically can have at most 2^26 entries, though in practice, this will be much less due to the constraints of the problem (e.g., if words are of limited length). Therefore, the space complexity

for cnt can be considered 0(26) assuming the length of the word is limited, but in the unconstrained case, it would be 0(2^26).

The total space complexity of the algorithm is, therefore, 0(2^26 + M), but again, assuming a practical limit to the number of unique bitmasks due to constraints on the word length, the space would be more accurately described as 0(26 + M).