Problem Description

1. It is composed only of the first k letters of the English lowercase alphabet.

In this problem, we are dealing with the concept of beautiful strings. A string is considered beautiful if two conditions are met:

- 2. It does not contain any palindromic substring of length 2 or more.
- Given a beautiful string s with a length of n and a positive integer k, the task is to find the next lexicographically smallest beautiful

string that is larger than s. The lexicographic order is like dictionary order - for example, b is larger than a, ab is larger than aa, and so on. If the string contains a letter at some position where it differs from another string and this letter is bigger, the entire string is considered larger in lexicographic order. To solve the problem, we want to:

Increment the string in the minimal way to find the next lexicographically larger string.

that results in a string fulfilling the beauty criteria.

Preserve the "beautiful" characteristic of the string.

Intuition

1. Start from the end of the given string s and move backwards to find the first place where we can increment a character without

Take the following steps:

breaking the beauty rules. 2. Once such a place is found, replace the character at that position with the next possible character that does not create a palindrome with the two previous characters.

The intuitive approach to this problem is to use a greedy strategy. The goal is to find the smallest lexicographical increment possible

- 3. After replacing a character, it is necessary to build the rest of the string from that point onward with the smallest possible characters from the set of allowed first k characters also while avoiding the creation of palindromic substrings.
- 4. If no such position exists, then it is not possible to create a lexicographically larger beautiful string, and an empty string should be returned as per the problem statement.
- This greedy approach ensures that the resulting string is strictly the next lexicographically larger string since only the necessary changes are made starting from the back, and each replacement ensures the smallest viable increment.
- Solution Approach The provided reference solution uses a backwards greedy algorithm to build the lexicographically smallest beautiful string that

comes after the given string s. Here's the step-by-step approach based on the code: 1. We initialize a variable n with the length of the given string s and convert the string to a list of characters, cs.

2. The algorithm then iterates over cs from the last character to the first. For each character, it tries to find the next character in the alphabet that can be placed at that position to make the string lexicographically larger while maintaining the non-palindrome

property. To do this, it converts the character to its numerical equivalent (p = ord(cs[i]) - ord('a') + 1) and iterates from p to k-1 to find a suitable replacement.

3. A replacement is deemed suitable if it isn't the same as the character immediately before it (cs [i - 1]) or the one two positions before (cs[i - 2]). This ensures that substrings of length 2 or 3 are not palindromic.

to n - 1. For this remaining part, the smallest possible character that does not form a palindrome with the previous two

6. If the loop terminates without finding a suitable replacement for any of the positions, it means no lexicographically larger

beautiful string can be formed, and therefore an empty string " is returned.

conversion, providing an efficient means to compare and assign characters.

form bb, which is a palindrome. Therefore, we continue moving backward.

can only use the first 3 letters of the English alphabet: a, b, c).

4. Once a suitable character is found for position i, the code updates cs[i] and moves on to filling the rest of the string from i + 1

- characters is selected. Again, this is checked by comparing against the characters at positions 1 1 and 1 2. 5. When the loop successfully updates the character array cs, the newly formed string is returned by joining the list of characters.
- The above algorithm effectively uses a linear scan of the input string in the worst-case scenario, making the time complexity linear in relation to the length of s. The use of a fixed-size ASCII offset (ord('a')) ensures a constant time operation for character to integer
- In summary, the approach relies on a greedy algorithm that backs up from the end of the string to find the smallest necessary increments while maintaining the string's beauty, taking advantage of character-integer conversions and simple comparisons to enforce the beauty constraints.

Following the solution approach, we perform the following steps: 1. Start from the end of s, which is the character c. We need to find a place where we can increment a character without creating

Let's take a small example to illustrate the solution approach. Imagine we have a beautiful string s = "abac" and k = 3 (meaning we

3. Before a, we have b. We can't increment b to c because that will create the palindrome cac.

beautiful.

lowercase letters of the alphabet.

Get the length of the string

Convert the string to a list for easier manipulation

position = ord(char_list[i]) - ord('a') + 1

for replacement_pos in range(position, k):

If so, skip this replacement

for m in range(k):

continue

continue

string_length = len(s)

palindrome substrings.

Example Walkthrough

we have to increment b to c, ensuring no direct repetition with its neighboring character. 5. Now we have chac, but we are not allowed to have direct repetitions or create palindromic substrings such as cac. Since c is

already the maximum allowed character for our k, we must convert the subsequential characters to the smallest possible

7. The resulting string is chab which is the smallest lexicographic increment from our original string abac that keeps the string

So, the solution algorithm would output chab as the next lexicographically smallest beautiful string after abac when using the first 3

4. We reach the first character a. We can increment a to b resulting in the string bbac. However, this forms a palindrome bb. Hence,

2. The last character c is already the maximum for k = 3, so we move backward. Before c, there is an a, but increasing a to b would

thus we must place a b instead. 6. Following this pattern, the next characters will be the lowest possible values ensuring no palindromic substrings are created. After b, the smallest allowed character which doesn't create a palindrome is a.

characters (a), ensuring that we do not form a palindrome. However, placing a after c would give us caa, which is a palindrome;

- Python Solution class Solution: def smallestBeautifulString(self, s: str, k: int) -> str:
 - char list = list(s) 8 # Iterate backwards through the character list 9 for i in range(string_length - 1, -1, -1): 10 # Find the position of the current character in the alphabet (1-based) 11

Check if the previous two characters are the same as the potential replacement character

Skip if the character matches any of the previous two characters

Assign and break since the smallest possible character has been found

if (i > 0 and char_list[i - 1] == replacement_char) or (i > 1 and char_list[i - 2] == replacement_char):

if (l > 0 and char_list[l - 1] == next_char) or (l > 1 and char_list[l - 2] == next_char):

Try replacing current character with the next possible beautiful character

Calculate the replacement character based on its position

Assign the replacement character to the current position

replacement_char = chr(ord('a') + replacement_pos)

Iterate over possible characters

char_list[l] = next_char

nextChar = (char) ('a' + m);

// If no valid string can be formed, return an empty string

continue;

return String.valueOf(chars);

break;

chars[l] = nextChar;

// Apply the same rule for the next characters

// Assign the chosen character and break to the next position

// Return the new string after constructing it from the character array

// Function to create the smallest lexicographically string that follows specific rules

 $next_char = chr(ord('a') + m)$

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char_list[i] = replacement_char
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                   # For remainder of the string, place lexicographically smallest possible character
                    for l in range(i + 1, string_length):
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                             break
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                     # Return the modified string after the first replacement
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                     return ''.join(char_list)
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             # Return an empty string if no possibility to make the string beautiful
             return ''
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Java Solution
    class Solution {
         public String smallestBeautifulString(String s, int k) {
             // Length of the input string
             int n = s.length();
             // Convert the input string to a character array for manipulation
             char[] chars = s.toCharArray();
  6
             // Iterating from the end of the character array
             for (int i = n - 1; i >= 0; --i) {
                 // Calculate the numeric position of the current character
 10
                 int position = chars[i] - 'a' + 1;
 11
 12
                 // Iterate through the alphabet starting from the character after the current one
 13
                 for (int j = position; j < k; ++j) {
                     // Convert the numeric position into a character
 14
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                     char nextChar = (char) ('a' + j);
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                     // Check if replacing the current character with the next one obeys the rules
 17
                     // (next character should not be the same as the previous two characters)
 18
                     if ((i > 0 \&\& chars[i - 1] == nextChar) || (i > 1 \&\& chars[i - 2] == nextChar)) {
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                         continue;
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                     // Assign the new character to the current position
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                     chars[i] = nextChar;
 23
                     // Iterate over the remaining characters in the array starting from i+1
 24
                     for (int l = i + 1; l < n; ++l) {
 25
                         // Iterate over all possible characters within the given limit 'k'
 26
                         for (int m = 0; m < k; ++m) {
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if ((l > 0 && chars[l - 1] == nextChar) || (l > 1 && chars[l - 2] == nextChar)) {

string smallestBeautifulString(string s, int k) { int n = s.size(); // Get the length of the input string 6 7 // Iterate backward through the string

2 public:

C++ Solution

1 class Solution {

return "";

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for (int i = n - 1; i >= 0; --i) {
  8
                 int position = s[i] - 'a' + 1; // Convert character to zero-based position
  9
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                 // Try each possible character starting from the current position to k-1
 12
                 for (int j = position; j < k; ++j) {</pre>
 13
                     char c = 'a' + j; // Convert integer position j to its corresponding character
 14
 15
                     // Skip characters that are illegal due to the rules (same as previous one or two)
                     if ((i > 0 \&\& s[i - 1] == c) || (i > 1 \&\& s[i - 2] == c)) {
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                         continue;
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                     s[i] = c; // Set the current character of the string s
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 22
                     // Update the rest of the string after the current position
                     for (int l = i + 1; l < n; ++l) {
 23
                         // Try each character from 'a' to 'a' + (k - 1)
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 25
                         for (int m = 0; m < k; ++m) {
 26
                             c = 'a' + m;
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                             // Apply the same rules, skip if the character is illegal
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                             if ((l > 0 \&\& s[l - 1] == c) || (l > 1 \&\& s[l - 2] == c)) {
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                                 continue;
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                             // Set the next character in the string s
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                             s[l] = c;
 35
                             break; // Break to fill the next position in the string
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                     return s; // Return the updated string once it is built
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             return ""; // Return an empty string if no valid string can be formed
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 45 };
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Typescript Solution
     function smallestBeautifulString(inputString: string, alphabetSize: number): string {
         // Split the input string into an array of characters
         const characters: string[] = inputString.split('');
        // Get the length of the character array
         const length = characters.length;
  6
         // Loop backwards through the characters
  8
         for (let index = length - 1; index >= 0; --index) {
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// Calculate the alphabet position of the current character and increment it by 1 (to find next character)

const currentCharPos = characters[index].charCodeAt(0) - 'a'.charCodeAt(0) + 1;

for (let charCode = currentCharPos; charCode < alphabetSize; ++charCode) {</pre>

let nextChar = String.fromCharCode(charCode + 'a'.charCodeAt(0));

// Check the adjacent characters to avoid consecutive duplicates

(index > 1 && characters[index - 2] === nextChar)) {

if ((index > 0 && characters[index - 1] === nextChar) ||

// Get the character representation of charCode

// Update the current character in the array

characters[nextIndex] = nextChar;

// If no beautiful string could be formed, return an empty string

// Loop over the possible characters (starting from currentCharPos to alphabetSize)

// Check the adjacent characters to avoid consecutive duplicates

if ((nextIndex > 0 && characters[nextIndex - 1] === nextChar) ||

// Convert the array back to a string and return the resultant string

(nextIndex > 1 && characters[nextIndex - 2] === nextChar)) {

// Update the character at nextIndex with the non-repeating character

26 // Fill the rest of the string with non-repeating characters for (let nextIndex = index + 1; nextIndex < length; ++nextIndex) {</pre> 27 28 // Try characters from 'a' to the kth letter in the alphabet for (let nextCharCode = 0; nextCharCode < alphabetSize; ++nextCharCode) {</pre> nextChar = String.fromCharCode(nextCharCode + 'a'.charCodeAt(0));

return '';

continue;

characters[index] = nextChar;

continue;

break;

return characters.join('');

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Time and Space Complexity **Time Complexity** The time complexity of the code is actually not O(n). In the worst case, both of the nested loops could iterate up to k times for each position. The outer loop runs from n-1 down to 0, contributing an 0(n) factor. Inside this loop, we have the second loop iterating through the possible characters less than k, giving a factor of O(k). Similarly, the innermost loop, which resets each character after

the current position, iterates up to k times for each remaining position, leading to a factor of 0(k * (n - i)). Therefore, the worst-

Space Complexity

case time complexity is closer to $0(n * k^2)$.

The space complexity is indeed 0(1), assuming that the space needed for the input string s is not counted as additional space since we're transforming it in-place into a list cs. The only additional space used is for a few variables to store indices and characters,

which does not scale with the input size, hence constant space complexity.