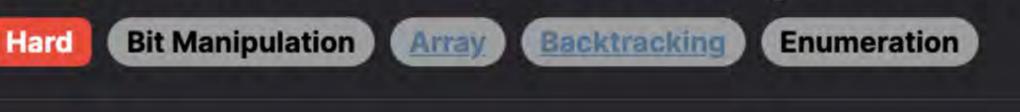
2151. Maximum Good People Based on Statements



Specifically, the input is a 2D integer array statements where:

Problem Description

Leetcode Link

 statements[i][j] = 1 means person i claims person j is good (truthful). statements[i][j] = 2 means person i has not made any claim about person j.

statements[i][j] = 0 means person i claims person j is bad (untruthful).

- Individuals are not permitted to make statements about themselves, thus statements[i][i] is always 2. The objective is to
- determine the maximum number of people that can be considered 'good' based on these statements. A 'good' person always tells the truth, while a 'bad' person may lie or tell the truth.

Intuition

The intuition behind the solution is to utilize a brute-force approach, trying every possible combination of 'good' and 'bad' assignments for the people. Since a 'good' person always tells the truth, their statements can be used to cross-verify which people

then that person cannot be considered good in any combination that includes the first person as a good individual. The solution uses bit masking to represent each combination of 'good' and 'bad' people. Each bit in a mask represents a person, where 1 can denote 'good' and 0 can denote 'bad'. There are 2^n possible combinations (masks) to check, where n is the number of people.

can be good and which cannot. If a 'good' person says another person is good, then both must be good; if they say someone is bad,

The function check (mask) takes a mask as an argument and iterates over all people. It checks the statements of those who are 'good' (bits set to 1) in the current mask. For each 'good' person's statements, it checks whether they align with the current assumption of who's good and bad. For instance, if a 'good' person claims another person is good, but the mask marks them as bad (or vice versa), the current mask is invalid, and the function returns 0. Otherwise, if no conflicts are found, it returns the number of 'good' people in

The main function calls check(mask) for all 2ⁿ combinations and returns the maximum number of good people found among all valid masks that don't lead to contradictions. This brute-force solution works well for smaller n, as it explores all possibilities and ensures that the maximum number of 'good' people is found according to the statements made.

Solution Approach

Here is a step-by-step walkthrough of the solution:

1. Brute Force Enumeration: We generate all possible combinations of each person being 'good' or 'bad' by iterating through

integers from 1 to 2ⁿ - 1, inclusive. Here, n is the number of people. The reason we start from 1 is because 0 would mean that

The implementation is grounded on a bit manipulation strategy. It uses an integer to represent a set of truth assignments to

nobody is good, which is not a valid scenario for us to consider.

i has made about other people (j).

people in this combination.

potential solution when n is within a manageable size.

(where nobody is good) and check 001 to 111.

cannot verify Person 1's truthfulness this way.

[2, 2, 1], // Person 1's statements about Person 0 and 2

[1, 0, 2] // Person 2's statements about Person 0 and 1

the current mask (the count of 1's in the mask).

individuals, where the i-th bit of the integer corresponds to the i-th person.

function is responsible for validating the combination against the statements made. 3. Validating the 'Good' People: Within check(mask), we traverse over each person (i) by examining the current bit in the mask: (mask >> 1) & 1. If this results in 1, the person is assumed 'good' in this particular combination. Then, we check each statement

2. Checking Each Combination: For each combination (represented by mask), we implement a function called check(mask). This

the truthfulness of i's statement against the current combination (mask). If a 'good' i made a statement that contradicts the current assumption about j, the function returns 0, indicating this mask (or combination) is not valid.

4. Statement Verification: If person i has made a definitive statement about person j (i.e., statements [i] [j] is 0 or 1), we check

5. Counting 'Good' People: If no contradictions are found for a 'good' person 1, the count increments, tallying the number of 'good'

number of 'good' people found from all the valid combinations. It uses the built-in Python function max() to find the maximum over all return values from check(mask). By utilizing bit masks to represent sets and checking all possible combinations, the algorithm finds the optimal solution that matches

the problem's constraints. This approach, while not the most time-efficient for large n, ensures accuracy by not overlooking any

6. Finding the Maximum: Finally, the main solution function calls check(mask) for each possibility and keeps track of the maximum

Example Walkthrough Suppose we have a group of 3 people, and we are given the following statements array: 1 statements = [[2, 1, 0], // Person 0's statements about Person 1 and 2

Here's how we would apply the solution approach: 1. Brute Force Enumeration: Since there are 3 people, we have 2^3 = 8 combinations to consider. We will ignore the mask 000

2. Checking Each Combination: Let's consider the mask 011, indicating Person 0 is 'bad' while Persons 1 and 2 are 'good'. We use

3. Validating the 'Good' People: In the check(mask) function, we start with Person 0 being 'bad', so we skip and move to Persons 1

the check(mask) function to determine if this mask is a valid representation of the 'good' people.

assumed them to be 'bad'. Therefore, check(mask) also returns 0 for this mask.

4. Statement Verification: For Person 1 (who is 'good' in this mask), their statement about Person 2 is that they are 'good' (statements [1] [2] is 1), which aligns with our mask. However, we do not have a statement from Person 1 about Person 0, so we

mask, so check(mask) returns 0.

Python Solution

def maximumGood(self, statements):

class Solution:

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and 2.

Moving to Person 2, they state that Person 0 is 'good' (statements [2] [0] is 1), but our mask assumes Person 0 is 'bad', creating a contradiction. Person 2 also claims that Person 1 is 'bad' (statements [2] [1] is 0), which contradicts our mask where Person 1 is 'good'.

5. Counting 'Good' People: Since there's a contradiction in Person 2's statements, we cannot count any 'good' people under this

6. Finding the Maximum: We perform the same check(mask) for all other combinations. Let's take another example with the mask

101, where Persons 0 and 2 are 'good', and Person 1 is 'bad'. Person 0 claims Person 1 is 'good' which is a contradiction since we

By going through all combinations, we may find that the mask 110 yields the maximum number of 'good' people without contradiction — Person 0 claims Person 2 is 'bad', and Person 2 claims Person 0 is 'good', which both align with this mask. In this scenario, both Persons 0 and 1 can be considered good based on their statements and each other's statements.

Therefore, the final result given by the main function would be 2, as this is the maximum number of 'good' people found across all

valid combinations. The function would iterate through all the masks, evaluate each one using the check(mask) function, and

conclude that the combination 110 presents the maximum number of good people without causing any conflicts.

Helper function to check and count the number of 'good' people based on the given mask

If there is no conflict, increment the count of 'good' people

1 << len(statements) gives the total number of combinations for 'good' / 'bad' assignments

Iterate through this person's statements about others

if value < 2 and ((mask >> jdx) & 1) != value:

return count_good # Return the count of 'good' people for this mask

max_good_people = max(check(mask) for mask in range(1, 1 << len(statements)))</pre>

// Method to find the maximum number of people that can be classified as good

// Check the current subset and update the maximum if applicable

return maxGoodPersons; // Return the maximum number of good persons found

int personCount = statements.length; // The total number of persons

// Iterate over all the statements made by this person

// Return the total number of good persons in this subset if it is valid

// Iterate through all possible subsets of persons using a mask

for (int mask = 1; mask < (1 << statements.length); ++mask) {</pre>

int maxGoodPersons = 0; // Initialize the count of maximum good persons to zero.

maxGoodPersons = Math.max(maxGoodPersons, checkSubset(mask, statements));

// Helper method to check if a given subset of persons is valid and calculate the count

int goodPersonCount = 0; // Initialize the count of good persons in this subset to zero.

// Check if the current person (i) is included in the subset (good) as per the mask

// Iterate over each person to check if they can be classified as good, based on the current subset

int statementValue = statements[i][j]; // Statement about person j made by person i

// If the statement value is less than 2 (0 or 1), check consistency with subset

// If there is an inconsistency, the subset is not valid and we return 0

if (statementValue < 2 && ((mask >> j) & 1) != statementValue) {

for jdx, value in enumerate(statement):

return 0

count_good += 1

public int maximumGood(int[][] statements) {

private int checkSubset(int mask, int[][] statements) {

for (int j = 0; j < personCount; ++j) {</pre>

for (int i = 0; i < personCount; ++i) {</pre>

return 0;

return goodPersonCount;

if (((mask >> i) & 1) == 1) {

def check(mask): count_good = 0 # Initialize count of 'good' people # Iterate through each person's statements for idx, statement in enumerate(statements): # Check if the bit in the mask for this person is set to 1 (indicating 'good') if (mask >> idx) & 1: 9

If the statement is not 'unknown' and conflicts with the mask, return 0

Iterate over all possible combinations of 'good' and 'bad' people and find the max count of 'good' people

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           return max_good_people
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  # The List type need to be imported from typing if you want to use it in type hints
  from typing import List
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27 # Then you could use it as follows:
   class Solution:
       def maximumGood(self, statements: List[List[int]]) -> int:
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           # ... rest of the code remains the same
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Java Solution
1 class Solution {
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34 35 36 // If all statements by person i are consistent, increment the count of good persons ++goodPersonCount; 37 38

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C++ Solution
  1 class Solution {
  2 public:
        // Finds the maximum number of people who can be good based on their statements
         int maximumGood(vector<vector<int>>& statements) {
             int maxGood = 0; // Stores the maximum number of 'good' people found
  6
             // Iterate over all possible combinations of 'good' and 'bad' people
             for (int mask = 1; mask < (1 << statements.size()); ++mask) {</pre>
                 // Compare current count with the new count returned by check function
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                 maxGood = max(maxGood, check(mask, statements));
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             return maxGood; // Return the maximum count of 'good' people possible
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         // Checks if a given combination (mask) of 'good' people is consistent with their statements
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         int check(int mask, vector<vector<int>>& statements) {
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             int countGood = 0; // Counter for the number of 'good' people in the current combination
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             int n = statements.size(); // Number of people
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             // Iterate over each person
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             for (int i = 0; i < n; ++i) {
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                 if ((mask >> i) & 1) { // Check if the person is 'good' in the current mask
                     // If the person is 'good', check all of their statements
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                     for (int j = 0; j < n; ++j) {
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                         int statementValue = statements[i][j]; // Statement about person j by person i
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                         // If statementValue < 2, it means person i has made a definitive statement.
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                         // Check if the statement is consistent with our current 'good'/'bad' combination
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                         if (statementValue < 2 && ((mask >> j) & 1) != statementValue) {
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                             return 0; // Inconsistency found; this is not a valid combination
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                     countGood++; // Increment the count of 'good' people for this combination
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             return countGood; // Return the number of 'good' people for this combination if consistent
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 40 };
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Typescript Solution
   // Helper function to count the number of 'good' persons that can be inferred based on the current mask.
2 // The mask represents a set of people we assume to be 'good' (where each bit corresponds to a person).
   function checkValidity(mask: number, statements: number[][], peopleCount: number): number {
       let goodCount = 0; // Track number of 'good' people.
       for (let i = 0; i < peopleCount; ++i) {</pre>
           // If the i-th bit of mask is set, consider the i-th person 'good'.
           if ((mask >> i) & 1) {
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// If a 'good' person makes a definite statement (true or false) about another person,

// check if that statement conflicts with our current assumptions. If it does, return 0 as

for (let mask = 1; mask < (1 << peopleCount); ++mask) { // Update the maximum good count if the current mask leads to a higher number of 'good' people. maxGood = Math.max(maxGood, checkValidity(mask, statements, peopleCount)); 34 35 // Return the maximum number of 'good' people that can be deduced without contradictions. 36 37 return maxGood;

return goodCount;

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for (let j = 0; j < peopleCount; ++j) {</pre>

return 0;

function maximumGood(statements: number[][]): number {

goodCount++;

Time and Space Complexity

const statementValue = statements[i][j];

// Return the total count of 'good' people in this configuration.

const peopleCount = statements.length; // Total number of people.

// Iterate over all possible sets of 'good' people represented by masks.

// this configuration of 'good' people is not possible.

// If we reach here, person 'i' is 'good' without contradictions.

// Main function to find the maximum number of 'good' people based on their statements.

let maxGood = 0; // Keep track of the maximum number of 'good' people found so far.

// (1 << peopleCount) gives us the number of possible masks, as each person can be good or not.

if (statementValue < 2 && ((mask >> j) & 1) != statementValue) {

The provided Python code defines a function maximumGood which finds out the maximum number of people who can be considered "good" based on their statements about themselves and others. The solution employs a brute force approach to check every possible combination of "good" and "bad" people and then validate these combinations against the given statements.

The time complexity of the code is determined by the number of possible combinations of people being good or bad, since we are

iterating over all possible combinations using a bit mask. Given n people, there are 2ⁿ possible combinations (since for each person,

there is a binary decision to be either good or bad). For each combination, we are checking all statements made by all n persons, and

each person makes n statements or observations. This results in a nested loop running n times for each of the 2ⁿ combinations.

Time Complexity

Thus, the time complexity is $0(n * 2^n)$, where n is the number of people. **Space Complexity**

The space complexity of the code is quite straightforward. The only additional space used is for the variable cnt, which is an integer

used to keep count of the number of "good" people in the current combination, and the space used in the recursive process stack. This does not scale with n and hence is O(1). However, it's important to note that the code uses recursive calls to the check function. The maximum depth of this recursion would be n in the worst case (although in the check function there are no recursive calls, it's important to consider for more general cases). Therefore, if we would consider the function call stack in the analysis, the space complexity would be o(n) for the recursion call

stack space. However, since in the provided code check is more of an iterative function, we consider the space complexity to be

In this LeetCode problem, we're given a set of statements made by a group of n people, about each other's trustworthiness.