Problem Description

allowed to increment any element by 1 up to k times. The frequency of an element is how many times that element appears in the array. The objective is to find the highest possible frequency of any number in the array after making at most k increments in total.

You are given an integer array nums and an integer k. The task is to find the maximum frequency of any element in nums after you're

Intuition

Starting with the smallest elements on the left, we work towards the right. For each position r (right end of the window), we calculate the number of operations needed to raise all elements from 1 (left end of the window) to r to the value of the element at

calculate how many operations we would need to make all elements in the subarray equal to the rightmost element.

The intuition behind the solution is to first sort the array. By doing this, we can then use a sliding window to check each subarray and

position r. This is done by multiplying the difference between nums [r] and nums [r - 1] by r - 1 (size of the current window minus one). If the total operations required exceed k, we shrink the window from the left by increasing 1, subtracting the necessary operations as we go to keep the window valid (total operations less than or equal to k). Meanwhile, we're always keeping track of the maximum

window size we're able to achieve without exceeding k operations, as this directly corresponds to the maximum frequency. The solution uses a two-pointer technique to maintain the window, expanding and shrinking it as needed while traversing the sorted array only once, which gives an efficient time complexity.

Solution Approach

The algorithm implemented in the given solution follows a sliding window approach using two pointers, 1 and r, which represent the

left and right ends of the window, respectively. The fundamental data structure used here is the list (nums), which is sorted to

facilitate the sliding window logic. Here is a step-by-step breakdown: 1. Sort the Array: The array nums is sorted to allow comparing adjacent elements and to use the sliding window technique

effectively. 1 nums.sort()

- 1 (left pointer) which starts at 0. r (right pointer) which starts at 1 since the window should at least contain one element to make comparisons.
- ans which keeps track of the maximum frequency found. window which holds the total number of operations performed in the current window.

value of nums [r].

1 while window > k:

2 ans = max(ans, r - 1)

1 r += 1

1 return ans

1 l, r, window = 0, 1, 0

- 3. Expand the Window: The algorithm enters a loop that continues until the right pointer r reaches the end of the array.
- 1 while r < len(nums): 4. Calculate Operations: In each iteration, calculate the operations needed to increment all numbers in the current window to the

frequency ans if the current window size (r - 1) is greater than the previous maximum.

2. Initialize Pointers and Variables: Three variables are initialized:

2 ans = 1 # A single element has at least a frequency of 1.

5. Shrink the Window: If window exceeds k, meaning we cannot increment the elements of the current window to match nums [r]

with the allowed number of operations, move 1 to the right to reduce the size of the window until window is within the limit again.

6. Update Maximum Frequency: After adjusting the window to ensure we do not exceed k operations, update the maximum

window -= nums[r] - nums[l]

1 window += (nums[r] - nums[r - 1]) * (r - 1)

7. Return the Result: Once we have finished iterating through the array with the right pointer r, the ans variable holds the maximum frequency that can be achieved, and we return it.

The sliding window technique coupled with the sorted nature of the array allows for an efficient solution. This technique avoids

recalculating the increment operations for each window from scratch; instead, it updates the number of operations incrementally as the window expands or shrinks.

Example Walkthrough

Suppose we have an array nums = [1, 2, 3] and k = 3. First, we sort nums, which in this case is already sorted: [1, 2, 3].

• Since window <= k, we do not need to shrink the window. We then update ans with the new window size, which is r - 1. ans =

$\max(1, 1 - 0) = 1.$

the maximum frequency is 2.

nums.sort()

Python Solution

class Solution:

Increment r and it becomes 2.

Let's consider a small example to illustrate the solution approach in action:

• Initialize the pointers and variables: l = 0, r = 1, window = 0, and ans = 1.

• Enter the loop. nums [r] is 2, and nums [l] is 1. window becomes (2 - 1) * (1 - 0) = 1.

Again, window <= k, so we do not shrink the window. Update ans = max(1, 2 - 0) = 2.

Increment r and it becomes 3. Since r is now equal to len(nums), the loop ends.

Next iteration, nums [2] is 3. We calculate operations needed: window += (3 - 2) * (2 - 0) = 1 + 2 = 3.

Return ans. So the maximum frequency after k increments is 2.

def maxFrequency(self, nums: List[int], k: int) -> int:

Sort the input list in non-decreasing order.

left, right, n = 0, 1, len(nums)

while cumulative_diff > k:

left += 1

- Putting it all together, we found that after incrementing the elements optimally, we can have at least two elements with the same
 - from typing import List

Initialize two pointers for sliding window and the variables needed.

cumulative_diff += (nums[right] - nums[right - 1]) * (right - left)

cumulative_diff -= nums[right] - nums[left]

If the cumulative differences exceed k, shrink the window from the left.

max_freq, cumulative_diff = 1, 0 10 11 12 # Iterate with right pointer over the list to expand the window. 13 while right < n: # Increase the total difference by the difference between the current right element 14 # and its predecessor multiplied by the number of elements in the current window. 15

value in the array [1, 2, 3] by using at most 3 increments (for example: incrementing 1 and 2 to make the array [3, 3, 3]). Thus,

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# Move the right pointer to the next element in the list.
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                right += 1
25
26
               # Update the maximum frequency using the current window size.
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max_freq = max(max_freq, right - left)
28
29
           # Return the maximum frequency achievable with total operations \leq k.
30
           return max_freq
31
32 # The class and method could be tested with a simple test case as follows:
33 # sol = Solution()
34 # print(sol.maxFrequency([1,2,4], 5)) # Expected output: 3
Java Solution
   class Solution {
       // Function to find the maximum frequency of an element after performing operations
       public int maxFrequency(int[] nums, int k) {
           // Sort the array to group similar elements together
           Arrays.sort(nums);
 6
           int n = nums.length; // Store the length of the array for iteration
           int maxFreq = 1;  // Initialize max frequency as 1 (at least one number is always there)
           int operationsSum = 0; // This will hold the sum of operations used at any point
 9
10
           // Start with two pointers:
11
12
           // 'left' at 0 for the start of the window,
13
           // 'right' at 1, since we'll start calculating from the second element
14
           for (int left = 0, right = 1; right < n; ++right) {</pre>
               // Calculate the total operations done to make all elements from 'left' to 'right' equal to nums[right]
               operationsSum += (nums[right] - nums[right - 1]) * (right - left);
16
17
               // If the total operations exceed k, shrink the window from the left
18
               while (operationsSum > k) {
19
20
                   operationsSum -= (nums[right] - nums[left++]);
22
```

// Calculate the max frequency based on the window size and update it if necessary

maxFreq = Math.max(maxFreq, right - left + 1);

// Return the maximum frequency

int maxFrequency(std::vector<int>& nums, int k) {

// Initialize variables: n is the size of the vector,

for (int left = 0, right = 1; right < n; ++right) {</pre>

// Beginning with the second element as there's nothing to the left of the first.

std::sort(nums.begin(), nums.end());

// ans will hold the maximum frequency.

// Sort the given vector.

int n = nums.size();

int maxFrequency = 1;

return maxFreq;

15 // 'window' represents the total increments needed to make // all elements in the current window equal to the current maximum element. 16 long long window = 0; 17 18 19 // Using two pointers technique: l -> left, r -> right.

C++ Solution

1 #include <vector>

2 #include <algorithm>

class Solution {

public:

```
// Update the 'window' with the cost of bringing the newly included
22
23
               // element nums[right] to the value of nums[right - 1].
               window += 1LL * (nums[right] - nums[right - 1]) * (right - left);
25
26
               // If the total increments exceed k, shrink the window from the left.
27
               while (window > k) {
                    window -= (nums[right] - nums[left]);
28
29
                    left++;
30
               // Calculate max frequency by finding the maximum window size till now.
32
33
               maxFrequency = std::max(maxFrequency, right - left + 1);
34
35
           // Return the maximum frequency found.
36
37
           return maxFrequency;
38
39 };
40
Typescript Solution
   function maxFrequency(nums: number[], k: number): number {
       // Sort the array
       nums.sort((a, b) \Rightarrow a - b);
       // Initialize the answer with a single element frequency
       let maxFrequency = 1;
       // Initialize a variable to keep track of the total sum that needs to be added to make all elements equal during a window slide
       let windowSum = 0;
9
10
       // Get the count of elements in the array
11
       let n = nums.length;
12
13
       // Initialize two pointers for our sliding window technique
14
15
       for (let left = 0, right = 1; right < n; right++) {</pre>
           // Update the window sum by adding the cost of making the right-most element equal to the current right-most element
16
           windowSum += (nums[right] - nums[right - 1]) * (right - left);
17
           // Shrink the window from the left if the cost exceeds the value of k
19
           while (windowSum > k) {
               windowSum -= nums[right] - nums[left];
21
               left++;
```

28 // Return the maximum frequency achieved 29 return maxFrequency; 30 31 } 32

Time and Space Complexity Time Complexity

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• Two-pointer window iteration: The while loop iterates over the sorted list, adjusting the window of elements by incrementing the right pointer and potentially the left pointer. The right pointer makes only one pass over the list, resulting in O(n) operations. The left pointer moves only in one direction and can move at most n times, so it also contributes to O(n) operations.

Combining the sort and the two-pointer iteration results in a time complexity of O(n log n + n), which simplifies to O(n log n) since

• Sorting the list: Sorting takes 0(n log n) time, where n is the number of elements in nums.

// Update the maximum frequency with the current window size if it's greater

maxFrequency = Math.max(maxFrequency, right - left + 1);

n log n dominates n for large n. Therefore, the overall time complexity of the code is $O(n \log n)$.

The provided code first sorts the nums list, and then uses a two-pointer approach to iterate over the list, adjusting the window of

Space Complexity The space complexity of the code depends on the space used to sort the list and the additional variables used for the algorithm.

(Timsort), the sorting can take up to O(n) space in the worst case.

elements that can be made equal by applying up to k operations.

• Sorting the list: The sort operation on the list is in-place; however, depending on the sorting algorithm implemented in Python

- Additional variables: The code uses a few additional variables (1, r, n, ans, window). These require constant space (0(1)). Therefore, considering both the sorting and the additional variables, the space complexity of the code is O(n) in the worst case due
- to the sorting operation's space requirement.