76. Minimum Window Substring String Hash Table Sliding Window Hard Leetcode Link

# **Problem Description**

The problem requires us to find the smallest segment (substring) from string s that contains all the characters from string t, including duplicates. This segment or substring must be minimized in length and must contain each character from t at least as many times as it appears in t. If we are unable to find such a segment, we should return an empty string. A key point is that the solution is guaranteed to be unique where applicable.

Intuition To solve this problem, we employ a sliding window technique along with character counting. The main idea revolves around

expanding and shrinking a window on string s to include the characters from t in the most efficient way possible.

comes into play. We also keep a counter for the characters in our current window (window) and the number of characters from t in the window (cnt).

Firstly, we need to know how many of each character from t need to be in our window. This is where need, our character count for t,

Two pointers (i and j) mark the start and end of the current window. As we traverse s, we expand our window by including the current character and check if this character is "necessary" (meaning it's still required to meet the t character count criterion). If it is, we increment cnt.

Whenever cnt reaches the length of t, it means our window potentially includes all characters from t. At this point, we should attempt to shrink the window from the left by incrementing j, all the while making sure the window still contains all characters from t. If during this shrinkage we find a window smaller than our previous smallest (mi), we update our minimum window size (mi) and starting position (k). The process of expanding and shrinking continues until the end of string s. If by the end we haven't found any such window, we

return an empty string. Otherwise, we return the smallest window from s that contains all characters from t, starting at k with length mi.

Solution Approach The solution utilizes a sliding window approach, which dynamically changes its size, along with two hash tables or counters to keep

track of the characters in the sliding window (window) and the characters needed (need). The python Counter from the collections

module has been used for this purpose as it conveniently allows counting the frequency of each character in strings s and t.

## Here's the breakdown of the algorithm:

1. First, we initialize the need counter with the character frequencies of the string t since we want to find a substring of s that contains at least these many characters of t. 2. We also initialize a window counter with no characters, an integer cnt set to 0 to count the "necessary characters," indices j and

k (j for the start of the sliding window and k for the start of the minimum window), and a variable mi representing the minimum

3. We then iterate over the string s with the index i and character c, expanding the window by adding the character c.

expanding and shrinking the size of the window.

length infinity (inf provided by python) of the window.

- 4. If the character c is "necessary," meaning need[c] >= window[c] (it contributes to forming a window that covers t), we increment cnt.
- 5. A while loop starts whenever cnt matches the length of t, indicating that our current window has all the characters needed in string t. Inside this loop:
- We check if the current window size (i j + 1) is smaller than the previously recorded minimum (mi). If it is, we update mi with the new window size and k with the new start position of the window (j).

we expand the window by moving i to the right, otherwise, we continue to shrink the window.

1. We initialize need with the frequencies of character of t: need = {'A': 1, 'B': 1, 'C': 1}.

5. At i = 3, c = B, window becomes {'A': 1, 'B': 1} and cnt now is 2.

11. We continue with the expansion of the window by moving i to the right.

becomes invalid as cnt drops below the length of t.

cnt. Given we are potentially removing a "necessary character," we update the window count for that character. Continue to move j to the right as long as cnt equals the length of t and the condition need[s[j]] >= window[s[j]] holds true.

6. After the loop ends, if cnt does not equal the length of t, it means our current window is missing some characters from t, and

Shrink the window from the left by moving j right. If the character s[j] at the left boundary was "necessary," decrement

7. Once we've traversed all of s, we check if we found a minimum window (by checking if k>=0). If we have, we return the substring s[k:k + mi], otherwise, we return an empty string as per the problem's requirement.

This approach ensures that all characters of t are included in the minimum window in s as efficiently as possible, by appropriately

Example Walkthrough Let's take a small example to illustrate the solution approach. Suppose s = "ADOBECODEBANC" and t = "ABC".

2. Initialize window as an empty counter, cnt as 0, j and k both to 0, and mi as infinity. 3. We start iterating over s with our i pointer starting from the 0th index.

7. Since cnt equals the length of t, we enter the while loop and notice the current window size is smaller than mi (infinity), so we

update mi = 6, and k = 0.

that contains all the characters of t.

from collections import Counter

from math import inf

left = 0

min\_left = -1

min\_size = inf

# Iterate over each character in the source string

# Include current character in the window

min\_size = right - left + 1

# reducing it further would break the window condition

if target\_counter[source[left]] >= window\_counter[source[left]]:

if target\_counter[char] >= window\_counter[char]:

for right, char in enumerate(source):

valid\_char\_count += 1

min\_left = left

valid\_char\_count -= 1

window\_counter[char] += 1

class Solution:

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contains extra characters not needed.

6. At i = 5, c = C, window updates to {'A': 1, 'B': 1, 'C': 1} and cnt increases to 3, which is the length of t. Now we have a potential window "ADOBEC" from index 0 to 5.

8. Next, we move j right to shrink the window while checking if it still contains t fully. The window now can be shrunk because it

4. When i = 0, c = A, we found a necessary character A. We update window to {'A': 1} and increment cnt to 1.

- 9. When j = 3, s[j] = B, which is necessary, we decrement window['B'] and, since need['B'] is still greater, decrement cnt.
- 12. At i = 9, cnt again matches the length of t, indicating another potential window "BECODEBA". 13. Entering the while loop, we successfully shrink this window to "CODEBA" and then to "ODEBA" and finally to "DEBA" before it

10. We exit the while loop because the window is not valid (no longer contains all of t), cnt is no longer equal to the length of t.

14. We continue this process of expansion and shrinkage until we reach the end of s.

15. At the end of traversal, we have a mi of 4 and a k of 9, which corresponds to the window "BANC" which is the smallest window

containing all characters of t. 16. We then return this window s [9:9+4] which equals "BANC".

By following this approach using the sliding window technique and character counting, we efficiently find the smallest segment in s

- **Python Solution**
- def minWindow(self, source: str, target: str) -> str: # Create a counter for the target to keep a record of each character's frequency target\_counter = Counter(target) window\_counter = Counter() # This will keep a count of characters in the current window 8 valid\_char\_count = 0

# Number of characters that meet the target criteria

# If the character at the left pointer is less frequent in the window than in the target,

# Left pointer to shrink the window

# Left boundary index of the minimum window

# Initialize min\_size to positive infinity

# If the current character is needed and the window contains enough of this character

### # If the window has all the characters needed 23 while valid\_char\_count == len(target): 24 # If this window is smaller than the minimum so far, update minimum size and index 25 if right - left + 1 < min\_size:</pre>

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33
                   # Shrink the window from the left
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35
                   window_counter[source[left]] -= 1
36
                    left += 1
37
38
           # If no window meets the criteria, return an empty string
39
           return '' if min_left < 0 else source[min_left:min_left + min_size]</pre>
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Java Solution
  1 class Solution {
         public String minWindow(String source, String target) {
  2
             // Array to store the frequency of characters needed from the target string
             int[] charFrequencyInTarget = new int[128];
             // Array to store the frequency of characters in the current window of the source string
             int[] charFrequencyInWindow = new int[128];
  6
  8
             int sourceLength = source.length();
             int targetLength = target.length();
  9
 10
 11
             // Populate the frequency array for the target string
 12
             for (int i = 0; i < targetLength; ++i) {</pre>
 13
                 charFrequencyInTarget[target.charAt(i)]++;
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             int matchCount = 0; // Count of characters that matches from target
 17
             int windowStart = 0; // The start index of the current window
             int minWindowStart = -1; // The start index of the minimum window
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 19
             int minLength = Integer.MAX_VALUE; // Length of the smallest window
 20
             // Iterate over the source string
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 22
             for (int windowEnd = 0; windowEnd < sourceLength; ++windowEnd) {</pre>
 23
                 // Include the current character in the window
 24
                 charFrequencyInWindow[source.charAt(windowEnd)]++;
 25
 26
                 // If the character is needed and we have not more than needed, increase the match count
 27
                 if (charFrequencyInTarget[source.charAt(windowEnd)] >= charFrequencyInWindow[source.charAt(windowEnd)]) {
 28
                     matchCount++;
 29
 30
 31
                 // When we have all characters from the target in our window
 32
                 while (matchCount == targetLength) {
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int windowLength = windowEnd - windowStart + 1; // Get the current window's length

// The character at window start is going to be removed since window is moving forward

if (charFrequencyInTarget[charAtStart] >= charFrequencyInWindow[charAtStart]) {

// If the character is one that is needed and after removing there are not enough of it, decrease match count

// Update minimum length and starting index if a new minimum is found

if (windowLength < minLength) {</pre>

matchCount--;

minLength = windowLength;

minWindowStart = windowStart;

// Remove the character from the window

char charAtStart = source.charAt(windowStart);

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charFrequencyInWindow[charAtStart]--;
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                     windowStart++; // Move the window forward
 52
 53
             // Return the minimum window substring or an empty string if no such window exists
             return minWindowStart < 0 ? "" : source.substring(minWindowStart, minWindowStart + minLength);</pre>
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C++ Solution
  1 class Solution {
  2 public:
         string minWindow(string s, string t) {
             int need[128] = {0}; // Array to store the frequency of characters required from 't'
             int window[128] = {0}; // Array to store the frequency of characters in the current window
             int strLength = s.size(), targetLength = t.size(); // Store the length of the strings 's' and 't'
  6
             // Populate the need array with frequencies of characters in 't'
  8
             for (char& c : t) {
  9
 10
                 ++need[c];
 11
 12
 13
             // Initialize variables for the sliding window technique
 14
             int matches = 0; // Number of characters that match 't' in the current window
             int start = 0; // Start index of the minimum window
 15
 16
             int minStart = -1; // Start index of the overall minimum window found
             int minLength = INT_MAX; // Length of the overall minimum window found
 18
             // Iterate over the string 's' using 'i' as the end index of the window
 19
             for (int i = 0; i < strLength; ++i) {</pre>
 20
 21
                 // Include the character at the current position into the window
 22
                 ++window[s[i]];
 23
                 // If the current character is needed and the window contains enough
 24
                 // instances of it to match 't', then increment the match count
 25
                 if (need[s[i]] >= window[s[i]]) {
 26
                     ++matches;
 27
 28
                 // When all characters from 't' are found in the current window
                 while (matches == targetLength) {
 29
 30
                     // Update minimum window if the current window's length is smaller
 31
                     if (i - start + 1 < minLength) {</pre>
 32
                         minLength = i - start + 1;
 33
                         minStart = start;
 34
 35
                     // Exclude character at the start position from the window
                     if (need[s[start]] >= window[s[start]]) {
 36
 37
                         ---matches;
 38
                     --window[s[start++]];
 39
 40
 41
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 43
             // If no window was found, return an empty string. Otherwise, return the minimum window
             return minStart < 0 ? "" : s.substr(minStart, minLength);</pre>
 44
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    };
 47
```

## 14 15 16 17

which simplifies to 0(m + n).

strings themselves but on the size of the character set, making it O(C).

Typescript Solution

```
function minWindow(source: string, target: string): string {
        // Initialize arrays to keep track of character frequency in `target`
        // and the current window in `source`
        const targetFreq: number[] = new Array(128).fill(0);
         const windowFreq: number[] = new Array(128).fill(0);
  6
         // Populate target character frequencies
         for (const char of target) {
  8
             ++targetFreq[char.charCodeAt(0)];
  9
 10
 11
 12
         let validCharCount = 0; // Keeps track of how many characters match target in current window
 13
         let left = 0; // Left pointer for the sliding window
         let start = -1; // Start index of the min-length window
         let minLength = Infinity; // Length of the smallest window found
        // Iterate over the `source` string to find the minimum window
 18
         for (let right = 0; right < source.length; ++right) {</pre>
             // Include the current character in the window
 19
 20
             const rightCharIndex = source.charCodeAt(right);
             ++windowFreq[rightCharIndex];
 21
 22
 23
            // If the character is needed and window has enough of that character, increase valid count
             if (windowFreq[rightCharIndex] <= targetFreq[rightCharIndex]) {</pre>
 24
 25
                 ++validCharCount;
 26
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 28
            // Try and contract the window from the left if it contains all the required characters
 29
            while (validCharCount === target.length) {
 30
                 if (right - left + 1 < minLength) {</pre>
                     minLength = right - left + 1; // Update the smallest window length
 31
 32
                     start = left; // Update the start index of the smallest window
 33
 34
 35
                 // Decrease the left-most character's frequency and move the left pointer
                 const leftCharIndex = source.charCodeAt(left);
 36
 37
                 if (targetFreq[leftCharIndex] >= windowFreq[leftCharIndex]) {
 38
                     --validCharCount; // If the character was contributing to valid count, decrease the valid count
 39
 40
                 --windowFreq[leftCharIndex];
 41
                 ++left;
 42
 43
 44
 45
         // If `start` is not updated, no valid window is found
        // Otherwise, return the minimum length window from `source`
         return start < 0 ? '' : source.slice(start, start + minLength);
 47
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Time and Space Complexity
```

The time complexity of the provided code is 0(m + n). This is because the code iterates through all characters of string s once which is of length m, and for each character, it performs a constant number of operations. Additionally, it iterates through the characters of string t once which is of length n to fill the need Counter object. The while loop and the inner operations are also constant time because it will at most iterate for every character in string s. Altogether, this gives us two linear traversals resulting in 0(2m + n),

The space complexity of the code is O(C), where C is the fixed size of the character set. In the code, we have two Counter objects:

given that the size of the character set is fixed at 128, the space used by these counters does not depend on the size of the input

need and window. Since the Counter objects will only have as many entries as there are unique characters in strings s and t, and