979. Distribute Coins in Binary Tree

Depth-First Search Medium **Binary Tree**

Problem Description

of coins in the tree is equal to the total number of nodes (n). Your task is to redistribute the coins so that every node has exactly one coin. Redistribution is done by moving coins between adjacent nodes (where adjacency is defined by the parent-child relationship). On each move, you can take one coin from a node and move it to an adjacent node. This problem asks you to find the minimum number of moves required to achieve a state where every node has exactly one coin.

You are provided with the root of a binary tree, where each node contains a certain number of coins (node.val). The total number

Intuition

The number of moves for a single node is the number of excess coins it has or needs. When a node has more coins than it needs (more than 1), the excess can be moved to the parent. Conversely, if it needs coins (has less than 1 coin), it requests coins from its parent.

The intuition behind the solution is to use a post-order traversal, which visits the children of a node before visiting the node itself.

To compute the number of moves, call the function recursively on the left and right children. The number of moves required for the left subtree is the absolute value of extra/deficit coins in the left subtree and similarly for the right subtree. The current balance of coins for the node is the node's value plus the sum of moves from left and right (which can be positive, negative, or

zero) minus one coin that is needed by the node itself. If this balance is positive, it means the node has extra coins to pass up to its parent. If it's negative, it needs coins from its parent. The total number of moves is accumulated in a variable, which is the sum of the absolute values of extra/deficit coins from both subtrees. This approach works because it ensures that at each level of the tree, we move the minimum necessary coins to balance out the children before considering the parent. This ensures we don't make redundant moves.

Solution Approach The solution uses a depth-first search (DFS) approach to traverse the binary tree and calculate the balance of coins at each

Here's a step-by-step walkthrough of the implementation:

node.

Define a nested helper function, dfs, which will perform the DFS traversal. This function accepts a single argument: the current node being visited (initially the root of the tree).

node's nonexistent child.

or deficit coins in the left subtree. Do the same for the right child and store the result in right.

The base case of the recursion is to return 0 if the root passed to the function is None, which means you've reached a leaf

Recursively call dfs on the left child of the current node and store the result in left, which represents the number of excess

- The main logic of the solution is encapsulated in these two points:
- The total number of moves required (ans) is increased by abs(left) + abs(right). This represents the total number of moves needed to balance the left and right subtrees of the current node. • The dfs function returns left + right + root.val - 1. This return value represents the balance of the current node after accounting for its

own coin (root.val), and it's meant to be either passed up to the parent (if positive) or requested from the parent (if negative).

The ans variable is defined in the outer function scope but is modified inside the dfs function. This is done using the nonlocal

Initialize ans to 0 before starting the DFS. This variable will accumulate the total number of moves required to balance the

- keyword, which allows the inner function to modify ans that is defined in the non-local (outer) scope.
- tree. After the DFS completes, ans contains the total number of moves, and the function returns this value.
- The algorithm efficiently calculates the required number of moves using a post-order traversal (visit children first, then process the current node), which helps to avoid redundant moves. It does not require any additional data structures beyond the function call stack used for recursion.
- **Example Walkthrough**

Consider this binary tree with 3 nodes:

Here 3, 0, and 0 are the values at each node, respectively, indicating the number of coins they hold. We need to redistribute these

4. Now, the dfs function processes the left child with value 0. Since it needs one coin, the return value of the dfs function will be -1 for this node.

6. With both children processed, we come back to the root node. We use the return values from the left and right child (-1 from each) to calculate

8. The current balance for the root node after these moves is $3 + (-1) + (-1) - 1 = \emptyset$. Since the root now has exactly 1 coin (which is our goal

5. Similarly, dfs is called on the right child, which also has the value 0, and the process is the same as the left child. The return value is -1.

7. The total moves at the root node are abs(-1) + abs(-1) = 2. This is because we need to move one coin to each child.

coins such that each node has exactly one coin.

the number of moves required for the root.

def __init__(self, val=0, left=None, right=None):

right_balance = dfs(node.right)

moves_count += abs(left_balance) + abs(right_balance)

return left_balance + right_balance + node.val - 1

int leftMovesRequired = postOrderTraversal(node.left);

// Return the net balance of coins for this node

TreeNode() : val(0), left(nullptr), right(nullptr) {}

TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}

// Recursive case: solve for left and right subtrees.

totalMoves += abs(leftMoves) + abs(rightMoves);

// Recursively dfs into the left and right subtrees.

return leftExcessCoins + rightExcessCoins + node.val - 1;

totalMoves += Math.abs(leftExcessCoins) + Math.abs(rightExcessCoins);

const leftExcessCoins = dfs(node.left);

// Start the DFS from the root of the tree.

dfs(root);

class Solution:

def dfs(node):

moves_count = 0

return moves_count

dfs(root)

if node is None:

return 0

const rightExcessCoins = dfs(node.right);

int rightMovesRequired = postOrderTraversal(node.right);

return leftMovesRequired + rightMovesRequired + node.val - 1;

// Calculate the total moves needed by adding up the moves required by both subtrees

totalMoves += Math.abs(leftMovesRequired) + Math.abs(rightMovesRequired);

TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}

// Base case: if the current node is null, return 0 since there are no coins to move.

// Because moves from both left and right need to pass through the current node.

// Recurse on the right subtree

// Definition for a binary tree node.

struct TreeNode {

TreeNode *left;

TreeNode *right;

// Constructors

int val;

class Solution {

public:

Return the net balance of coins for the current subtree

Solution Implementation

self.val = val

def dfs(node):

self.left = left

self.right = right

if node is None:

nonlocal moves_count

2. Since the root is not None, we continue by calling dfs on the left child, which has the value 0. 3. The left child has no children, so both calls to its children return 0.

1. Starting at the root, the dfs function is called on the root node which has the value 3.

Let's take a simple binary tree as an example to illustrate the solution approach.

- for every node), it needs no further action. 9. The ans variable gets updated in each recursive call, and after the entire tree is traversed, it holds the value 2, which is the minimum number of
- moves required to redistribute the coins.
- Finally, after the DFS traversal finishes, we find that the minimum number of moves required for this example is 2.
- **Python** # Definition for a binary tree node.

class Solution: def distributeCoins(self, root: Optional[TreeNode]) -> int: # Depth-first search (DFS) function to traverse the tree and redistribute coins

Use nonlocal to modify the ans variable declared in the parent function's scope

and we subtract 1 because the current node should have 1 coin after redistribution

Increment the total moves by the absolute amount of coins to move from/left child and right child

Net balance is the coins to be redistributed, i.e., current node's coin plus left and right balance,

If the current node is None, we do not need to redistribute any coins

```
return 0
# Recursively redistribute coins for the left and right subtrees
left_balance = dfs(node.left)
```

class TreeNode:

```
# Initialize the moves counter to 0
       moves_count = 0
       # Start DFS from the root to distribute coins and calculate the moves
       dfs(root)
       # Return the total number of moves required to distribute the coins
       return moves_count
Java
// Definition for a binary tree node.
class TreeNode {
    int val; // Node's value
    TreeNode left; // Left child
    TreeNode right; // Right child
    // Constructor to create a leaf node.
    TreeNode(int val) {
       this.val = val;
    // Constructor to create a node with specified left and right children.
    TreeNode(int val, TreeNode left, TreeNode right) {
       this.val = val;
       this.left = left;
       this.right = right;
class Solution {
    private int totalMoves; // To track the total number of moves needed
   // Distributes coins in the binary tree such that every node has exactly one coin
    public int distributeCoins(TreeNode root) {
        totalMoves = 0; // Initialize the total moves to 0
       postOrderTraversal(root); // Start post-order traversal from the root
       return totalMoves; // After traversal, totalMoves has the answer
    // Helper function to perform post—order traversal of the binary tree
    private int postOrderTraversal(TreeNode node) {
       // Base case: if current node is null, return 0 (no moves needed)
       if (node == null) {
            return 0;
       // Recurse on the left subtree
```

// The net balance is the sum of left and right balances plus the coins at the node minus one (for the node itself)

```
int distributeCoins(TreeNode* root) {
    int totalMoves = 0; // This will store the total number of moves needed to balance the coins
   // The Depth First Search (DFS) function computes the number of moves required
   // starting from the leaves up to the root of the tree.
   // It returns the excess number of coins that need to be moved from the current node.
    function<int(TreeNode*)> dfs = [&](TreeNode* node) -> int {
```

int leftMoves = dfs(node->left);

int rightMoves = dfs(node->right);

if (!node) {

return 0;

```
// Return the number of excess coins at this node: positive if there are more coins than nodes,
            // negative if there are fewer. A value of -1 means just the right amount for the node itself.
            return leftMoves + rightMoves + node->val - 1;
        };
       // Call the DFS function starting from the root of the tree.
       dfs(root);
        // Return the total number of moves needed to distribute the coins.
        return totalMoves;
};
TypeScript
// Function to distribute coins in a binary tree to ensure each node has exactly one coin.
// Each move allows for a coin transfer between a parent and a child node (either direction).
// The function returns the minimum number of moves needed to achieve this state.
function distributeCoins(root: TreeNode | null): number {
    // Variable to keep track of the total number of moves needed.
    let totalMoves = 0;
    // Helper function for depth-first search (DFS) to compute the number of moves each subtree needs.
    function dfs(node: TreeNode | null): number {
       // If we've reached a null node, return 0 as there are no coins to move.
        if (!node) {
            return 0;
```

// The absolute value is used because it takes the same number of moves whether the coin needs to be moved in or out.

// Since each node should end up with 1 coin, we subtract 1 from the sum of current node value and excess coins from both

// Return the excess number of coins at this node: positive if there are too many coins, negative if not enough.

// The number of moves made at the current node is the sum of absolute values of each subtree's excess coins.

```
// Return the total number of moves calculated using the DFS helper.
      return totalMoves;
# Definition for a binary tree node.
class TreeNode:
   def __init__(self, val=0, left=None, right=None):
        self.val = val
        self.left = left
        self.right = right
```

Depth-first search (DFS) function to traverse the tree and redistribute coins

If the current node is None, we do not need to redistribute any coins

Recursively redistribute coins for the left and right subtrees

Start DFS from the root to distribute coins and calculate the moves

Return the total number of moves required to distribute the coins

// Add the absolute values of excess coins from left and right subtrees to the totalMoves.

```
left_balance = dfs(node.left)
right_balance = dfs(node.right)
# Use nonlocal to modify the ans variable declared in the parent function's scope
nonlocal moves count
# Increment the total moves by the absolute amount of coins to move from/left child and right child
moves_count += abs(left_balance) + abs(right_balance)
# Return the net balance of coins for the current subtree
# Net balance is the coins to be redistributed, i.e., current node's coin plus left and right balance,
# and we subtract 1 because the current node should have 1 coin after redistribution
return left_balance + right_balance + node.val - 1
```

Initialize the moves counter to 0

def distributeCoins(self, root: Optional[TreeNode]) -> int:

Time and Space Complexity The given Python code performs a Depth-First Search (DFS) on a binary tree to distribute coins so that every node has exactly

The time complexity of the DFS function is O(n), where n is the number of nodes in the binary tree. This is because each node in

Time Complexity:

one coin.

the tree is visited exactly once during the DFS traversal. **Space Complexity:**

The space complexity of the DFS function is O(h), where h is the height of the binary tree. This space is used by the call stack during recursion. In the worst case, if the tree is skewed, the height h can be n, making the space complexity O(n). However, in a balanced binary tree, the space complexity would be $O(\log n)$.