In this problem, we are given the current state of a Tic-Tac-Toe board represented as an array of strings. Our goal is to determine

Problem Description

whether this board configuration could have been reached in the course of a valid game. The board is of size 3 x 3, and the characters 'X', '0', and ' ' represent the moves by the first player, the second player, and an empty space, respectively. Tic-Tac-Toe is played according to these rules:

 Two players take turns to make their move. The first player uses 'X' and the second player uses '0'.

Players can only place their marks in empty squares (' ').

both or one more 'X' than '0'.

- The game ends either when a player has filled a row, column, or diagonal with their character, or when all the squares are filled, rendering the game over.
- Once the game has ended, no further moves can be made. We must verify if the given board could logically be the result of playing a game following these rules.
- Intuition

To provide a valid solution, a few simple checks must be implemented based on the game's rules.

1. Count the occurrences of 'X' and '0'. Since players alternate turns starting with 'X', there should either be an equal number of

Toe.

2. Check for winners. Since the game stops as soon as a winning condition is met:

- ∘ If 'X' has won, there must be exactly one more 'X' than '0' on the board—because 'X' plays first and would have just played to win the game.
- ∘ If '0' has won, there must be an equal number of 'X' and '0' on the board since '0' would have just played to win the game.
- 3. Understand that both 'X' and '0' cannot win in a single game instance—it would against game rules. The code given first defines a function, win(x), which checks for winning conditions for the character x. It checks all rows, columns,

and both diagonals to see if any of them are filled with the same character. The code then counts the number of 'X's and '0's on

the board. Lastly, it applies the previous two checks: it confirms the counts are appropriate given the rules, and it ensures that only one (or none) of the players could have possibly won the game. If any of these conditions fail, the board state is impossible, and the function returns False. Otherwise, it returns True.

Solution Approach The solution is implemented in Python and uses simple iterative constructs to verify the validity of the given Tic-Tac-Toe board configuration.

By decomposing the problem into these logical steps, we can arrive at a clear solution approach that aligns with the rules of Tic-Tac-

• The solution starts by counting the number of 'X' and '0' characters present on the board utilizing list comprehensions. • It's done by looping through each cell in the board using two nested loops (one for rows and one for columns) and

incrementing the count appropriately for each character. 2. Winning Check Function (win(x)):

• The function win(x) takes a character x as an input and checks if that character has a win condition on the board.

• It checks for a win in each row, in each column, and across both diagonals. The all function is used to simplify the check

After counting 'X's and '0's, the code checks if their counts are valid. According to the rules, there cannot be more '0's

• If any win condition is met, it returns True. Otherwise, it returns False. 3. Game Rules Logic:

within each row, column, or diagonal.

Here are the key components of the solution approach:

1. Counting 'X' and '0' Characters:

4. Final Validation:

Example Walkthrough

1. Counting 'X' and '0' Characters:

• We check if 'X' has a win condition:

Next, we check if '0' has a win condition:

■ So, win('0') would return True.

Toe.

- than 'X's, and 'X's can have at most one more than '0' because they start the game. If these conditions are not met, the function returns False.
- winning move. If there is no such count difference, the function returns False. Similarly, it checks if '0' has won. If '0' has won, the counts of 'X' and '0' must be equal, as '0' would have just played the winning move. If x does not equal o in count, then it returns False.

Lastly, the code ensures that both 'X' and '0' have not won simultaneously. If either 'X' or '0' is winning, their respective

Then, it checks if 'X' has won. If 'X' has won, there must be one more 'X' than '0', as 'X' would have just played the

count checks must also pass, as previously described. An understanding of how a Tic-Tac-Toe game progresses and ends is integral to the solution. The implementation leverages basic

since the problem can be solved with simple list iteration and condition checking.

Let's consider a Tic-Tac-Toe board with the following configuration: 1 ['X', 'X', '0'], 2 ['0', 'X', ' '], 3 ['', '', '0']

control structures and the inherent properties of the game rules to reach a conclusion. There's no use of advanced data structures

By combining these logical steps, the code effectively validates if the final board state can be the result of a valid game of Tic-Tac-

 There are 3 'X' characters and 3 '0' characters on the board. 2. Winning Check Function (win(x)):

Since '0' has a win condition, and the count of 'X' and '0' is equal, this matches the rule that '0' must have won on the

Since only '0' has a win condition and the counts of 'X' and '0' follow the rule associated with '0' winning, the game

game rules. The analysis confirms that this particular board could indeed represent a game of Tic-Tac-Toe that has been played

Diagonals do not have three 'X' either. ■ So, win('X') would return False.

last move.

Python Solution

class Solution:

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3. Game Rules Logic:

However, one diagonal (from the bottom right to the top left) is filled with '0'.

No row or column is entirely filled with 'X'.

No row or column is entirely filled with '0'.

Using the solution approach, we'll walk through the validation process:

4. Final Validation:

correctly according to the standard rules.

board is a possible result of a valid Tic-Tac-Toe game. This illustrates how the code would verify the validity of the given board configuration by applying simple checks that are tied to the

return True

return True

return True

return False

return False

return True

private String[] board;

this.board = board;

return false;

return false;

// or one more 'X' than '0'

Check for the two diagonal wins

if all(board[i][j] == mark for j in range(3)):

if all(board[j][i] == mark for j in range(3)):

return all(board[i][2 - i] == mark for i in range(3))

If '0' has won, the count of 'X' and '0' must be the same

The board is valid if it does not violate any of the above rules

// 'X' goes first so there must be either the same amount of 'X' and '0'

if all(board[i][i] == mark for i in range(3)):

Count the number of 'X's and '0's on the board

count_x = sum(row.count('X') for row in board)

count_o = sum(row.count('0') for row in board)

if has_winner('0') and count_x != count_o:

// Checks if the given Tic-Tac-Toe board state is valid

int countX = count('X'), count0 = count('0');

if (countX != count0 && countX - 1 != count0) {

if (hasWon('X') && countX - 1 != count0) {

// If 'X' has won, there must be one more 'X' than '0'

// Function to check the validity of a tic-tac-toe game board state

// Lambda to check if a given player has won the game

// Check rows and columns for a win condition

// Check both diagonals for a win condition

// Count the number of 'X' and '0' on the board

if (countX != count0 && countX - 1 != count0) return false;

if (checkWin('X') && countX - 1 != count0) return false;

if (checkWin('0') && countX != count0) return false;

// If all rules are satisfied, the board state is valid

// Rule 2: If 'X' has won, there must be one more 'X' than '0'

// Rule 3: If '0' has won, the number of 'X's and '0's must be equal

* @param {string[]} board - An array of strings representing the tic-tac-toe board.

* @return {boolean} - Returns true if the board state is valid, false otherwise.

// Lambda to count occurrences of a provided character ('X' or '0') on the board

for (char cell : row) { // Iterate through each cell in the row

count += cell == character; // Increment count if the cell matches the character

if (board[i][0] == player && board[i][1] == player && board[i][2] == player) return true;

if (board[0][i] == player && board[1][i] == player && board[2][i] == player) return true;

if (board[0][0] == player && board[1][1] == player && board[2][2] == player) return true;

return board[0][2] == player && board[1][1] == player && board[2][0] == player;

// Rule 1: The number of 'X's must either be equal to or one more than the number of 'O's

bool validTicTacToe(vector<string>& board) {

auto checkWin = [&](char player) {

int countX = countCharacter('X');

int count0 = countCharacter('0');

* Checks if a given tic-tac-toe board state is valid.

const validTicTacToe = (board: string[]): boolean => {

const hasWon = (char: string): boolean => {

// Check rows and columns for win

for (let i = 0; i < 3; ++i) {

return true;

return true;

// Check diagonals for win

return true;

// Helper function to check if a player has won the game.

// Check the game's rules:

for (int i = 0; i < 3; ++i) {

int count = 0;

return count;

auto countCharacter = [&](char character) {

for (const auto& row : board) {

public boolean validTicTacToe(String[] board) {

def validTicTacToe(self, board: List[str]) -> bool: # Function to check if player with mark 'X' or '0' has won 3 def has_winner(mark): 4 # Check for horizontal and vertical wins 5 for i in range(3): 6

21 # Check for the correct number of 'X's and '0's 22 if count_x != count_o and count_x - 1 != count_o: 23 return False 24 25 # If 'X' has won, 'X' must be one more than '0' if has_winner('X') and count_x - 1 != count_o: 26

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Java Solution
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1 class Solution {

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             // If '0' has won, there must be the same number of 'X' and '0'
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             return !(hasWon('0') && countX != count0);
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         // Checks if the given player has won
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         private boolean hasWon(char player) {
             // Check all rows and columns
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             for (int i = 0; i < 3; ++i) {
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                 if (board[i].charAt(0) == player && board[i].charAt(1) == player && board[i].charAt(2) == player) {
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                     return true;
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                 if (board[0].charAt(i) == player && board[1].charAt(i) == player && board[2].charAt(i) == player) {
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                     return true;
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             // Check both diagonals
             if (board[0].charAt(0) == player && board[1].charAt(1) == player && board[2].charAt(2) == player) {
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                 return true;
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 39
             return board[0].charAt(2) == player && board[1].charAt(1) == player && board[2].charAt(0) == player;
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         // Counts the number of times the given character appears on the board
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 43
         private int count(char character) {
 44
             int count = 0;
             for (String row : board) {
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                 for (char cell : row.toCharArray()) {
 46
 47
                     if (cell == character) {
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                         ++count;
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             return count;
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 54 }
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C++ Solution
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// Iterate through each row of the board

44 return true; 45 46 }; 47

Typescript Solution

1 class Solution {

};

};

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// Helper function to count occurrences of 'X' or '0' on the board. const countOccurrences = (char: string): number => { 8 return board.reduce((accumulator, currentRow) => { 9 return accumulator + [...currentRow].filter(c => c === char).length; 10 11 }, 0);

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};

};

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       // Count occurrences of 'X' and '0'.
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        const xCount = countOccurrences('X');
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        const oCount = countOccurrences('0');
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36
       // Ensure 'X' goes first and there's at most one more 'X' than '0'
37
       if (xCount !== oCount && xCount - 1 !== oCount) {
38
            return false;
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       // Check for a win by 'X'. If 'X' has won, there must be one more 'X' than '0'.
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42
       if (hasWon('X') && xCount - 1 !== oCount) {
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            return false;
44
45
       // Check for a win by '0'. If '0' has won, there must be an equal number of 'X' and '0'.
46
47
       if (hasWon('0') && xCount !== oCount) {
            return false;
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       // If none of the invalid conditions were met, the board is valid.
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if (board[i][0] === char && board[i][1] === char && board[i][2] === char) {

if (board[0][i] === char && board[1][i] === char && board[2][i] === char) {

if (board[0][0] === char && board[1][1] === char && board[2][2] === char) {

return board[0][2] === char && board[1][1] === char && board[2][0] === char;

over the 9 cells of the board a constant number of times to count occurrences of 'X' and 'O', and to check for wins.

Time Complexity

return true;

Time and Space Complexity

To calculate x and o, we have two double loops that go through the 3×3 board, which would normally result in a time complexity of 0(n^2). However, since the board size is constant and does not grow with input, it results in a fixed number of operations that do not depend on any input size variable, so it is 0(1).

The win function is called at most two times (once for 'X' and once for 'O'). Within each call, it goes through each row, each column, and both diagonals to check for a win condition, which again, since the board is a fixed 3×3 size, results in a constant number of operations that are 0(1).

The time complexity of the validTicTacToe function is 0(1) because the size of the board is fixed at 3×3, and the algorithm iterates

Space Complexity

The space complexity of the validTicTacToe function is also 0(1). No additional space is used that grows with the input size. The function only uses a fixed number of variables (x, o, and the board itself) and the space taken by the recursive stack during the calls to win doesn't depend on the input size since the depth of recursion is not affected by the input but by the fixed size of the 3×3 board.