2876. Count Visited Nodes in a Directed Graph Dynamic Programming Memoization Hard Graph

## Leetcode Link

# Problem Description In this problem, we are given a directed graph which is represented by a 0-indexed array edges. Each element edges [i] indicates

that there is a directed edge from node i to node edges [i]. The graph consists of n nodes labeled from 0 to n - 1, and n directed edges.

The task is to determine, for each starting node 1, how many distinct nodes can be visited if we follow the directed edges starting from node 1 until we return to any node visited earlier in the same process. This essentially means we're calculating how many unique nodes we encounter before we enter a cycle or revisit any node during traversal which implies the start of a cycle.

# Intuition

Whether or not we've entered a cycle, and if so, the length of that cycle.

To solve this problem, we need to keep track of two key pieces of information:

To do this, we can start at each unvisited node and follow edges to traverse the graph, using an array vis to record the order in

The number of nodes visited in the current traversal, starting from each node i.

which we visited nodes. During the traversal, we do one of two things:

information gained during each traversal and avoiding redundant computations.

We now know the number of nodes outside the cycle that have been visited and also the length of the cycle. For each unvisited node, its answer is then the number of unique nodes visited — which is the sum of the length of the cycle and the path length to the cycle for nodes outside the cycle, or simply the cycle length for nodes inside the cycle.

If we find a node that has already been visited in this traversal (vis[j] is nonzero), we then know that we have entered a cycle.

- If we find a node for which we've already computed an answer, then, for each visited node, its answer is the distance from the current node to this node plus the answer of this node we've already computed. The algorithm involves iterating over each of the nodes of the graph and performing a depth-first traversal. During the traversal, we update the vis array to reflect the visitation order and calculate the necessary counts for the cycle and the path leading to the cycle. Once a traversal from a starting node is completed or we encounter a previously computed answer, we backtrack while updating the
- ans array with the number of nodes that can be visited for each start node.

This method allows us to efficiently compute the number of nodes that can be visited from each starting node by leveraging the

Solution Approach The solution implements a form of depth-first traversal. Here's a breakdown of the approach based on the provided Reference Solution Approach and Python solution:

1. Initialization: Create two arrays, ans and vis. ans will store the final answer for each node (i.e., the number of different nodes visited), and vis will store the visitation order for each node. Both are initially filled with zeros.

2. Outer Loop: Iterate through all the nodes with a for loop, using each node as a starting point for the process.

#### 3. Traversal Initiation: For each starting node, if ans [i] is zero, meaning that we have not computed the answer for this node, we start traversing from this node i.

or outside the cycle.

traversal. For each node j we visit:

4. Inner Loop - Traversing Nodes: In a while loop, continue to follow the directed edges until we encounter a node that we have already visited in this traversal (which implies a cycle) or a node that we have already computed the answer for in a different

 Increment the count (cnt) which keeps track of how many nodes we have visited in this traversal. Update vis[j] with the visitation order cnt. Move to the next node using j = edges[j].

5. Cycle and Path Detection: Once we've either hit an already visited node within this traversal or an already computed node,

6. Backtracking and Answer Update: Once we've hit a node for which an answer was already computed or the start of a cycle has

been determined, loop back through the nodes we just visited to update their answers (ans[j]). The nodes inside the cycle all

- calculate the cycle length if necessary and the total number of nodes visited. If a cycle is detected, the length is determined by the difference between the current cnt value and the visitation order of the node that's part of the cycle (vis[j]).
- have the same answer (the cycle length). 7. Population of Answers: Loop through the previously visited nodes and update their answers based on whether they are inside
- **Data Structures Used:**  One-dimensional lists (ans to store answers for each node, vis to store visitation order). Algorithm Patterns Used:

The implementation uses the max(total, cycle) to ensure the answer for each node is either the total number of nodes visited (for

 Cycle detection and cycle length calculation within a directed graph. Backtracking to propagate the calculated answers to all starting points included in a traversal.

This approach minimizes redundant computations and efficiently calculates the answers for all the nodes in a directed graph that

### Let's illustrate the solution approach using a small example with a directed graph:

 $0 \rightarrow 1 \rightarrow 2$ 

 $3 \rightarrow 4 \rightarrow 5$ 

potentially contains cycles.

Example Walkthrough

Edge from node 0 to node 1

Edge from node 1 to node 2

Edge from node 3 to node 4

Edge from node 4 to node 5

This means we have six nodes, and the directed edges are as follows:

Suppose we have the following directed graph represented by edges = [1, 2, 0, 4, 5, 3].

those outside the cycle) or the length of the cycle (for those inside the cycle).

Depth-First Search (DFS) traversal to explore the graph.

We can visualize the graph like this:

Now, let's walk through the solution steps:

Edge from node 2 to node 0 (forming a cycle with nodes 0, 1, 2)

Edge from node 5 to node 3 (forming a cycle with nodes 3, 4, 5)

3. Traversal Initiation: Set cnt = 1 since we are starting traversal from node 0. Then we set vis[0] = 1 to indicate node 0 is visited

2, increment cnt to 3, and mark vis[2] = 3.

2. Outer Loop: We start with node of and since ans [0] is zero, we begin traversal.

num\_nodes = len(edges) # Determine the total number of nodes

# Traverse all nodes to calculate visit counts

while not visited[current\_node]:

count += 1 # Increase visit count

while not visit\_counts[current\_node]:

public int[] countVisitedNodes(List<Integer> edges) {

if (visitedCount[currentNode] == 0) {

// Loop through each node

int numNodes = edges.size();

if (!visitCount[i]) {

currentNode = i;

return visitCount;

const nodeCount = edges.length;

// Return the visit count for each node.

function countVisitedNodes(edges: number[]): number[] {

// Get the total number of nodes (length of the edges array)

std::vector<int> visitCount(numNodes);

// Iterate through all nodes in the graph.

int currentCount = 0, currentNode = i;

visited[currentNode] = ++currentCount;

currentNode = edges[currentNode];

while (visited[currentNode] == 0) {

if (visitCount[currentNode] == 0) {

while (visitCount[currentNode] == 0) {

currentNode = edges[currentNode];

// If the current node already has a determined visit count, skip it.

cycleSize = currentCount - visited[currentNode] + 1;

// Traverse the graph until a visited node or end of path is found.

int cycleSize = 0, totalVisits = currentCount + visitCount[currentNode];

// Backtrack and assign maximum between total visits and cycle size.

visitCount[currentNode] = std::max(totalVisits--, cycleSize);

// If visitCount at the current node is zero, it means we've found a cycle.

std::vector<int> visited(numNodes);

for (int i = 0; i < numNodes; ++i) {</pre>

int n = edges.size(); // The size of the graph (number of nodes)

for (int currentNode = 0; currentNode < n; ++currentNode) {</pre>

// Only process nodes that have not been counted yet

for node in range(num\_nodes):

if not visit\_counts[node]:

visit\_counts = [0] \* num\_nodes # Initialize list to store visit counts for each node

# Analyze the traversal to distinguish between cycle and path lengths

cycle\_length, total\_length = 0, count + visit\_counts[current\_node]

visit\_counts[current\_node] = max(total\_length, cycle\_length)

current\_node = edges[current\_node] # Move to the next node

int[] visitedCount = new int[n]; // Array to store the count of visits for each node

int[] visitedState = new int[n]; // Array to track the state of each node during traversal

total\_length -= 1 # Reduce total\_length as we move back

count = 0 # Initialize count for counting the nodes visited in this traversal

visited[current\_node] = count # Mark current node as visited with a timestamp

# The visit count at each node is the maximum of total length and cycle length

current\_node = edges[current\_node] # Move to the next node in the sequence

visited = [0] \* num\_nodes # Keep track of visited nodes with a timestamp

# Check if we haven't already calculated the visit count for this node

current\_node = node # Start traversing from the current node

# Traverse nodes until we reach a node we've already visited

current\_node = node # Start again from the initial node

5. Cycle Detection: When we attempt to move from node 2 to node 0, we notice that vis [0] is already marked (indicating a cycle since we've returned to an already visited node within this traversal). The cycle includes nodes 0, 1, and 2. 6. Backtracking and Answer Update: The length of the cycle is cnt - vis[0] = 3 - 1 = 2. We then backtrack, updating ans [0], ans [1], and ans [2] to 2 as they are part of the cycle.

first.

3, 4, and 5, and after backtracking and updating, we'd have ans [3], ans [4], and ans [5] all set to 3.

accurate answer updates.

Python Solution

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update any additional answers.

After processing all nodes, the final ans array is [2, 2, 2, 3, 3, 3], indicating the number of nodes we can visit from each starting node before encountering a cycle or revisiting a node.

During the entire process, we only traverse the graph starting from each node one time, ensuring an efficient solution that avoids

redundant calculations. The vis array helps to quickly determine the presence of a cycle and the nodes involved in the cycle for

1. Initialization: Create two arrays ans and vis with length 6 (the number of nodes), initializing all values to zero.

4. Inner Loop - Traversing Nodes: We follow the directed edge to node 1. Increase cnt to 2 and mark vis[1] = 2. Next, visit node

7. Population of Answers for Nodes Outside the Cycle: Since there are no nodes outside the cycle for this starting node, we don't

Next, we would proceed with node 3 as the starting node and repeat the steps. Eventually, we would identify the cycle among nodes

from typing import List class Solution: def countVisitedNodes(self, edges: List[int]) -> List[int]:

24 if not visit\_counts[current\_node]: 25 # If the target node hasn't been calculated, we found a cycle 26 cycle\_length = count - visited[current\_node] + 1 27 total\_length = count 28 29 # Now backfill the visit\_counts array with appropriate visit counts

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            return visit_counts # Return the computed visit counts for each node
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```

Java Solution

1 class Solution {

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int count = 0; // Initialize visit count
                   int nextNode = currentNode; // Start traversal from the current node
12
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                   // Traverse the graph until a previously visited node is encountered
14
                   while (visitedState[nextNode] == 0) {
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                       visitedState[nextNode] = ++count; // Increment visit count
16
                       nextNode = edges.get(nextNode); // Move to the next node in the edge list
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                   // Variables to determine the length of the cycle and total visits
                   int cycleLength = 0;
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                   int totalVisits = count + visitedCount[nextNode];
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24
                   // If the node encountered is the start of the cycle
25
                   if (visitedCount[nextNode] == 0) {
                       cycleLength = count - visitedState[nextNode] + 1; // Calculate cycle length
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                   nextNode = currentNode; // Reset traversal starting node
                   // Assign the maximum of total visits or cycle length to each node in the path
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                   while (visitedCount[nextNode] == 0) {
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                       visitedCount[nextNode] = Math.max(totalVisits--, cycleLength);
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                       nextNode = edges.get(nextNode); // Move to the next node in the edge list
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           return visitedCount; // Return the count array for all nodes
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40 }
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C++ Solution
1 #include <vector>
2 #include <algorithm>
   class Solution {
  public:
       // Function to count the number of visited nodes in a directed graph.
       // edges: An array where the i-th element is the node visited after node i.
       std::vector<int> countVisitedNodes(std::vector<int>& edges) {
```

# 42 }; 43

Typescript Solution

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// Initialize the answer array with zeros
       const answer: number[] = new Array(nodeCount).fill(0);
       // Initialize the visited array with zeros to track if a node has been visited
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       const visited: number[] = new Array(nodeCount).fill(0);
       // Iterate over each node
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       for (let currentNode = 0; currentNode < nodeCount; ++currentNode) {</pre>
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           // Only process nodes that have not determined the visited count yet
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           if (answer[currentNode] === 0) {
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                let visitCount = 0; // Counter for number of nodes visited in the current path
                let nodeIndex = currentNode; // Current node index being visited
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               // Traverse the nodes starting from the current node until a visited one is encountered
               while (visited[nodeIndex] === 0) {
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                   visitCount++;
18
                   visited[nodeIndex] = visitCount; // Mark the node as visited with the count
19
                   nodeIndex = edges[nodeIndex]; // Move to the next connected node
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               // Calculate the total visits including the current path and potential prior answers
24
               let cycleLength = 0;
25
                let totalVisits = visitCount + answer[nodeIndex];
26
               // If the next node doesn't have an answer yet, it means we found a cycle
               if (answer[nodeIndex] === 0) {
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29
                   cycleLength = visitCount - visited[nodeIndex] + 1; // Calculate the cycle length
30
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32
               // Reset nodeIndex to the start of the current path
33
               nodeIndex = currentNode;
34
               // Update the answer array with the maximum visits for each node in the current path
35
               while (answer[nodeIndex] === 0)
36
37
                   answer[nodeIndex] = Math.max(totalVisits, cycleLength);
38
                   totalVisits--:
                   nodeIndex = edges[nodeIndex]; // Move to the next node in the path
40
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       // Return the filled answer array with the visit count for each node
44
45
       return answer;
46 }
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Time and Space Complexity
```

The space complexity of the given code is also O(n). This is due to the allocation of two arrays of size n: ans array to store the answer for each node, and the vis array to keep track of the visitation status of each node. There are no additional data structures or recursive calls that would increase the space usage, so it remains linear with respect to the number of nodes n.

The time complexity of the given code is O(n). This is because each node is visited exactly once in a single pass to count the number

of nodes visited before reaching a previously visited node (or itself, forming a cycle). The outer loop runs for each node (n iterations),

and the inner while loops process each node only once, without revisits due to the vis array marking visited nodes.