881. Boats to Save People

Greedy Array Two Pointers

Sorting

Problem Description

Medium

In this problem, we are provided with an array called people, where each element represents the weight of a person. We also have an infinite number of boats that can carry a maximum weight of limit. Each boat can carry at most two people at the same time, as long as the total weight of these people doesn't exceed the limit. Our objective is to determine the minimum number of boats required to carry every person.

be able to efficiently pair people.

Intuition To solve this problem, we can use a two-pointer technique. The main idea is to pair the heaviest person left with the lightest person that can fit in the same boat with them, thus optimizing the usage of boat space. We start by sorting the people array to

person left to place on a boat, while j represents the heaviest. We loop until our two pointers meet. In each iteration, we try to place the heaviest person (people[j]) in a new boat and see if we can also fit the lightest person (people[i]) with them without exceeding the limit. • If we can fit both the i person and the j person on the same boat, we increment the i pointer (meaning the i person is now on a boat).

After sorting, we set two pointers: one at the start (i) and one at the end (j) of the array. The i pointer represents the lightest

• Regardless of whether the i person got on the boat or not, we decrement the j pointer, indicating that the j person is now on a boat, and increment the counter ans, which tracks the number of boats used.

needed to carry everyone. **Solution Approach**

We continue this process until every person has been placed on a boat. The counter ans gives us the minimum number of boats

The solution approach for this problem hinges on the efficient use of a two-pointer technique and the algorithm that supports it.

Sorting the Array: We begin by sorting the people array. Sorting is crucial because it allows us to consider the lightest and

3.

Here's a walkthrough of the implementation details:

(alone if not with the i-th person).

every person is considered exactly once when pairing them.

space efficient and has a linear time complexity in this context.

heaviest weights that can possibly be paired together. In Python, this is done with the sort() method, which sorts the array in increasing order. Sorting is a common preprocessing step in many algorithms to facilitate ordered operations.

- Two-Pointer Technique: After sorting, we initialize two pointers: i, pointing to the start, and j, pointing to the end of the array. These pointers will move towards each other as we pair up people into boats. The two-pointer technique is a common pattern used to solve problems that involve arrays, especially when looking for pairs that meet a certain criteria, as it is both
- paired with the person at the j-th position (heaviest remaining) without exceeding the weight limit. If the sum of weights people[i] + people[j] is less than or equal to limit, it means both can share one boat. We then move the i pointer up (incrementing it by 1) to consider the next lightest person for the subsequent iterations.

Iterating and Pairing: As we iterate through the array, we check if the person at the 1-th position (lightest remaining) can be

The j pointer is moved down (decremented by 1) after every iteration since the j-th person is always placed in a boat

number of boats used. **Loop Termination**: The loop continues until i > j, which means all persons have been paired up and placed on boats. At this point, the value of ans represents the minimum number of boats required to carry all persons.

Counting Boats: We have a counter, ans, which is incremented in every iteration of the loop. This counter represents the

- The algorithm uses no additional data structures and operates directly on the input array. Therefore, the space complexity is O(1), as it only uses a fixed amount of extra space. The time complexity, after sorting, is O(n), where n is the number of people, since
- **Example Walkthrough** Let us consider a small example to illustrate the solution approach. Suppose we have an array people given as [3, 5, 3, 4] and the limit of the boats is 5. We want to find out the minimum number of boats needed to carry everyone following the solution

First, we sort the array, which becomes [3, 3, 4, 5].

Step 1: Sorting the Array

approach detailed above.

Step 2: Initializing Two Pointers

We compare the weights at i and j, which are people[i] = 3 and people[j] = 5. Since their sum is 8 which is greater than limit, they cannot go together. We need a boat for people[j], so we decrement j to 2.

Our pointers are now at people[i] = 3 and people[j] = 4. Their sum is 7, which again exceeds the limit. So, we place

We set our two pointers i and j. The pointer i starts at index 0 and j starts at index 3, the last index in the sorted array.

Now people[i] = 3 and people[j] = 3. Their sum is 6, still exceeding the limit. The third boat is used for people[j], and we decrement j to 0.

Step 3: Iterating and Pairing Persons to Boats

people[j] in a new boat and decrement j to 1.

people[i]. **Step 4: Counting Boats**

Finally, the pointers i and j both point to the first element, which is 3. We have no choice but to use a fourth boat for

Step 5: Loop Termination The loop terminates when \mathbf{i} is greater than \mathbf{j} . This happens after the fourth iteration in our example.

used by attempting to pair the lightest and heaviest people on the same boat without surpassing the weight limit.

Using the approach, we determined that the minimum number of boats required to carry everybody in the array [3, 5, 3, 4]

with a limit of 5 is 4. This example demonstrates the efficiency of the two-pointer technique in minimizing the number of boats

Solution Implementation

Python

Continue until all people have been assigned boats.

if people[lightest_index] + people[heaviest_index] <= limit:</pre>

// Method to find out the number of boats necessary to rescue all people.

int numRescueBoats(vector<int>& people, int limit) {

sort(people.begin(), people.end());

int numBoats = 0;

while (i <= j) {

j--;

i++;

numBoats++;

return numBoats;

let numBoats: number = 0;

let j: number = people.length - 1;

let i: number = 0;

while (i <= j) {

j--;

i++;

numBoats++;

return numBoats;

people.sort()

num boats = 0

int j = people.size() - 1;

int i = 0;

// First, sort the list of people by their weights.

// Iterate until all people have been considered.

if (people[i] + people[j] <= limit) {</pre>

// Return the total number of boats needed.

// Initialize the counter for the number of boats needed.

// Iterate until all people have been considered.

if (people[i] + people[j] <= limit) {</pre>

// Return the total number of boats needed.

// Initialize the counter for the number of boats needed.

// "people" is the list of weights of the people, and "limit" is the weight limit of the boat.

// Use two pointers, one at the beginning (lightest person) and one at the end (heaviest person).

// A boat is used for the heaviest person, decrement the pointer to the next heaviest person.

// If the lightest and the heaviest person can share a boat, increment the pointer to the next lightest person.

while lightest_index <= heaviest_index:</pre>

Return the total number of boats needed.

We needed one boat for each step, so the total number of boats used is 4.

def num_rescue_boats(self, people: List[int], limit: int) -> int: # Sort the list of people to organize by weight for optimal pairing. people.sort() # Initialize the count of rescue boats needed. num_boats = 0 # Two pointers to keep track of the lightest and heaviest person not yet on a boat. lightest_index, heaviest_index = 0, len(people) - 1

If the lightest and heaviest person can share a boat, increase the lightest pointer.

lightest_index += 1 # Always decrease the heaviest pointer since the heaviest person gets on a boat. heaviest_index -= 1 # Increment the boat count as either one or two people have been assigned to a boat.

Example usage:

num_boats += 1

return num_boats

from typing import List

class Solution:

```
# solution = Solution()
# print(solution.num_rescue_boats([3, 2, 2, 1], 3)) # Output: 3
Java
import java.util.Arrays; // Import Arrays class to use the sort method
class Solution {
    /**
     * Returns the minimum number of boats required to rescue people.
     * @param people An array representing the weight of each person.
     * @param limit Maximum weight capacity a boat can carry.
     * @return The minimum number of boats required.
     */
    public int numRescueBoats(int[] people, int limit) {
       // Sort the array of people to organize weights in ascending order
       Arrays.sort(people);
       // Initialize the count of boats to 0
        int boatCount = 0;
        // Use two-pointer technique to pair the lightest and heaviest people
        for (int lighter = 0, heavier = people.length - 1; lighter <= heavier; --heavier) {</pre>
            // If the lightest and heaviest persons can share a boat, increment lighter pointer
            if (people[lighter] + people[heavier] <= limit) {</pre>
                lighter++;
            // A boat is used, increment boat count
            boatCount++;
        // Return the total number of boats required after going through all the people
        return boatCount;
```

};

C++

public:

#include <vector>

class Solution {

#include <algorithm>

```
TypeScript
// Function to find out the number of boats necessary to rescue all people.
// `people` is the list of weights of the people, and `limit` is the weight limit of the boat.
function numRescueBoats(people: Array<number>, limit: number): number {
   // First, sort the list of people by their weights in non-decreasing order.
   people.sort((a, b) => a - b);
```

// Use two pointers, one at the beginning (lightest person) and one at the end (heaviest person).

// A boat is used for the heaviest person, decrement the pointer to the next heaviest person.

// Increment the counter for boats as either one or two people have used a boat.

Two pointers to keep track of the lightest and heaviest person not yet on a boat.

If the lightest and heaviest person can share a boat, increase the lightest pointer.

Always decrease the heaviest pointer since the heaviest person gets on a boat.

Increment the boat count as either one or two people have been assigned to a boat.

// If the lightest and the heaviest person can share a boat, increment the pointer to the next lightest person.

// Increment the counter for boats as either one or two people have used a boat.

```
from typing import List
class Solution:
   def num_rescue_boats(self, people: List[int], limit: int) -> int:
       # Sort the list of people to organize by weight for optimal pairing.
```

Initialize the count of rescue boats needed.

while lightest_index <= heaviest_index:</pre>

Return the total number of boats needed.

lightest_index += 1

heaviest_index -= 1

num_boats += 1

return num_boats

lightest index, heaviest index = 0, len(people) - 1

Continue until all people have been assigned boats.

if people[lightest_index] + people[heaviest_index] <= limit:</pre>

```
# Example usage:
# solution = Solution()
# print(solution.num_rescue_boats([3, 2, 2, 1], 3)) # Output: 3
Time and Space Complexity
  The given Python code implements an efficient algorithm to find the minimum number of boats required to rescue people based
  on their weights and the limit of a boat's capacity.
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• The people.sort() operation has a time complexity of O(n log n), where n is the length of the people list. Sorting is typically achieved using algorithms like Timsort in Python, which has this complexity.

• The while loop runs in O(n) time since in the worst case, it could iterate over all elements once (where n is the number of people). Each

The time complexity of the code is determined by the sorting operation and the while loop that is used to pair people onto boats.

```
operation inside the loop (checking condition and incrementing/decrementing counters) is 0(1).
Combining both operations, the overall time complexity of the code is 0(n log n) + 0(n), which simplifies to 0(n log n) as the
```

0(n log n) term dominates 0(n) when n is large.

Time Complexity

- **Space Complexity** The space complexity of the algorithm is mainly due to the additional space required for sorting the people list.
- The people.sort() operation is typically done in-place in Python, meaning that it doesn't require additional space proportional to its input, so it's 0(1) space complexity. • The variables i, j, and ans use a constant amount of extra space 0(1).
- Thus, the overall space complexity of the code is 0(1), indicating that it uses a constant amount of space regardless of the input size.