248. Strobogrammatic Number III Recursion Array String Hard

number is one that retains its original value when rotated by 180 degrees. Imagine flipping the number upside down; if it still reads the same, it's strobogrammatic. For example, 69 and 88 are strobogrammatic, while 70 is not. Given two string inputs, low and high, which represent the lower and upper bounds of a numeric range, the task is to calculate the

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total count of strobogrammatic numbers that fall within this range, including the bounds themselves. We need to ensure that we convert low and high from strings to integers because we are working with numeric comparisons.

This is a problem that combines counting, string manipulation, and number theory. Solvers must understand the nature of strobogrammatic numbers and devise a strategy to generate and count all valid strobogrammatic numbers within the specified interval.

given the potentially large range. The direct approach of checking each number within the range will be inefficient, especially for large bounds.

Intuition

Here are the critical steps to the algorithm: 1. We observe that strobogrammatic numbers are symmetrical and recursively build them from the middle outwards.

2. For a given length u, we can construct strobogrammatic numbers by placing pairs of strobogrammatic digits at the start and end

To approach this solution, we need to generate strobogrammatic numbers in an efficient way, which requires careful consideration

3. The valid pairs to form strobogrammatic numbers are ('0', '0'), ('1', '1'), ('8', '8'), ('6', '9'), and ('9', '6'). 5. We execute this DFS approach in a loop starting from the length of the low string to the length of the high string, building all

4. We include '0' at the ends only if we are not at the outermost layer, since a number cannot start with '0'.

of an already-formed strobogrammatic number of length u - 2. This uses a depth-first search (DFS) approach.

- possible strobogrammatic numbers of each length. 6. We check if each generated strobogrammatic number falls within the low to high range after converting it to an integer.
- 7. Increment a counter each time we find a valid strobogrammatic number within the range. This approach focuses on generating only potentially valid strobogrammatic numbers rather than searching through the entire range,
- Solution Approach

To do so, a helper function called dfs is used to construct these numbers. Here's a detailed explanation of how the solution operates:

• The dfs function is defined to construct strobogrammatic numbers of a given length u. It has two base cases:

The provided solution involves the use of recursion to generate strobogrammatic numbers with a depth-first search (DFS) approach.

∘ If u == 0, the function returns an empty list containing just an empty string [''], since there are no digits in a zero-length number.

range, the counter ans is incremented.

strobogrammatic numbers exist between 10 and 100.

Example Walkthrough

• 69, which is strobogrammatic.

• 88, which is strobogrammatic.

• 96, which is strobogrammatic.

numbers between 10 and 100.

Python Solution

class Solution:

∘ If u == 1, the function returns a list of single-digit strobogrammatic numbers ['0', '1', '8']. • For other cases, dfs is called recursively on u - 2 to return the list of strobogrammatic numbers that are two digits shorter. We

can sandwich pairs of strobogrammatic digits around each returned number to form new strobogrammatic numbers of length u.

• These digit pairs are added only if the resulting number is not longer than the maximum length (n) being checked. The pairs used are ('1', '1'), ('8', '8'), ('6', '9'), and ('9', '6'). If the length is not the full target length n, we can also use the

pair ('0', '0'), but leading zeros are not added to full-length numbers.

thus reducing the number of necessary checks and improving efficiency.

used to get the length range of strobogrammatic numbers. • The main part of the solution iterates over each length from a to b, inclusive, generating strobogrammatic numbers of that length

After defining the dfs function, the lengths a and b represent the lengths of the low and high strings, respectively, which are

- using the dfs function. • The generated strings are checked to determine if they fall within the specified numeric range [low, high]. This is done by converting the strobogrammatic string to an integer and comparing it against the numeric low and high. If it falls within the
- Throughout the implementation, key algorithmic patterns such as recursion, DFS, and generating combinatorial output based on constraints are used to build an efficient solution for counting strobogrammatic numbers within a given range.

• Finally, the ans value containing the count of strobogrammatic numbers in the specified range is returned.

Let's consider a small example where the low string is "10" and the high string is "100". We need to find out how many

Using the solution approach, we would start by finding strobogrammatic numbers of different lengths within the inclusive range of the lengths of "10" (length 2) and "100" (length 3). We iterate through lengths 2 and 3 since no strobogrammatic number of length 1 falls between 10 and 100.

Next, for length 3 (same as the length of "100"), the possible strobogrammatic numbers would need to have a form such as "x0x",

strobogrammatic number due to the nature of the digit '0' in the middle. As a result, there are no valid 3-digit strobogrammatic

"x1x", or "x8x" (the middle digit can be '0', '1', or '8'). But we quickly realize that none of these forms can create a valid

As such, the total count of strobogrammatic numbers between 10 and 100 is 3.

def strobogrammaticInRange(self, low: str, high: str) -> int:

def generate_strobogrammatic(length):

if length != num_length:

min_length, max_length = len(low), len(high)

if length == 0:

return sub_ans

low, high = int(low), int(high)

Out of these, only 69, 88, and 96 are valid and fall within the given range (10 to 100).

For length 2 (same as the length of "10"), the possible strobogrammatic numbers are:

• 11, which is not strobogrammatic because it doesn't retain its value when flipped.

• 00 is excluded as it's not a valid two-digit number because numbers cannot start with '0'.

In this case, the dfs function would have worked by first generating numbers of length 2 by sandwiching the central parts [''] with all valid pairs except ('0', '0') and then generating numbers of length 3 by sandwiching the central parts ['0', '1', '8'] with valid pairs. However, since all 3-digit combinations fall outside the range, they would not be counted.

The final answer would therefore be 3, representing the strobogrammatic numbers 69, 88, and 96.

Helper function to generate strobogrammatic numbers of length 'length'

Base case for a strobogrammatic number of length 0 is an empty string

Numbers like '060', '080' etc. cannot be at the beginning or end

So we add them only when we're not at the outermost level

sub_ans.append('0' + sub_number + '0')

count = 0 # Counter for strobogrammatic numbers within the range

generate strobogrammatic numbers of length 'num_length'

// Pairs of strobogrammatic numbers that are each other's reflection.

// Public method to count the strobogrammatic numbers in a given range.

public int strobogrammaticInRange(String low, String high) {

if (length != targetLength) {

return result;

#include <functional> // For std::function

10 using std::stoll; // For converting string to long long

12 using ll = long long; // Define 'll' as an alias for 'long long'

int strobogrammaticInRange(string low, string high) {

if (size == 0) return vector<string>{""};

if (size != currentSize) {

4 #include <utility> // For std::pair

int currentSize;

int count = 0;

// Base cases

vector<string> results;

result.add("0" + middle + "0");

private static final int[][] STROBO_PAIRS = {{1, 1}, {8, 8}, {6, 9}, {9, 6}};

Loop through all lengths from min_length to max_length

for num_length in range(min_length, max_length + 1):

return [''] # Base case for length 1 (single digit strobogrammatic numbers) 8 if length == 1: 9 return ['0', '1', '8'] 10 sub_ans = [] 11 12 # Recursive call to get the inner strobogrammatic number for sub_number in generate_strobogrammatic(length - 2): 13 14 # Adding the strobogrammatic pairs to the sub_number for pair in ('11', '88', '69', '96'): 15 sub_ans.append(pair[0] + sub_number + pair[1]) 16

for num_str in generate_strobogrammatic(num_length): 31 # Convert the string to an integer and check if it's within range 32 if low <= int(num_str) <= high:</pre> 33 count += 1

return count # Return the count of strobogrammatic numbers within the range

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Java Solution

1 class Solution {

private int targetLength;

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};

50 }

C++ Solution

1 #include <vector>

2 #include <string>

6 using std::vector;

7 using std::string;

9 using std::pair;

14 class Solution {

15 public:

8 using std::function;

```
int minLength = low.length(), maxLength = high.length();
 8
            long lowerBound = Long.parseLong(low), upperBound = Long.parseLong(high);
 9
            int count = 0;
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            // Loop through each length from low to high
13
            for (targetLength = minLength; targetLength <= maxLength; ++targetLength) {</pre>
                // Generate all strobogrammatic numbers of the current length.
14
                for (String num : generateStrobogrammaticNumbers(targetLength)) {
15
16
                    long value = Long.parseLong(num);
17
                    // Check if the generated number is within the range, if so, increment the count.
18
                    if (lowerBound <= value && value <= upperBound) {</pre>
19
                        ++count;
20
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23
            return count;
24
25
        // Helper method to generate strobogrammatic numbers of a given length.
26
27
        private List<String> generateStrobogrammaticNumbers(int length) {
28
            // Base case for recursion: if length is 0, return a list with an empty string.
29
            if (length == 0) {
30
                return Collections.singletonList("");
31
32
            // If the length is 1, we can use '0', '1', and '8' as they look same even after rotation.
33
            if (length == 1) {
                return Arrays.asList("0", "1", "8");
34
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36
            List<String> result = new ArrayList<>();
37
            // Get all the strobogrammatic numbers of length minus two.
38
            for (String middle : generateStrobogrammaticNumbers(length - 2)) {
39
                // Surround the middle part with each pair of STROBO_PAIRS.
40
                for (int[] pair : STROBO_PAIRS) {
41
                    result.add(pair[0] + middle + pair[1]);
42
```

// If this is not the outermost layer, we can add '0' at both ends as well.

// Define pairs that are strobogrammatic (they look the same when rotated 180 degrees)

// Depth-First Search function to generate strobogrammatic numbers of a certain size

// Generate smaller strobogrammatic numbers and append new pairs to them

// If not at the outermost layer, we can add '0' at both ends

// Declare the current size of strobogrammatic numbers to generate

if (size == 1) return vector<string>{"0", "1", "8"};

function<vector<string>(int)> generateStrobogrammatic = [&](int size) {

for (auto& smallerStr : generateStrobogrammatic(size - 2)) {

results.push_back(left + smallerStr + right);

for (auto& [left, right] : strobogrammaticPairs) {

results.push_back('0' + smallerStr + '0');

// Initialize counter for valid strobogrammatic numbers within the range

const vector<pair<char, char>> strobogrammaticPairs = {{'1', '1'}, {'8', '8'}, {'6', '9'}, {'9', '6'}};

40 41 return results; **}**; 42 43 44 // Get sizes of the provided range 45 int sizeLow = low.size(), sizeHigh = high.size();

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             // Convert string bounds to long long for numerical comparison
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 51
             ll lowerBound = stoll(low), upperBound = stoll(high);
 52
 53
             // Generate strobogrammatic numbers for sizes within the inclusive range [sizeLow, sizeHigh]
             for (currentSize = sizeLow; currentSize <= sizeHigh; ++currentSize) {</pre>
 54
 55
 56
                 // Generate strobogrammatic numbers of current size
 57
                 for (auto& strobogrammaticNum : generateStrobogrammatic(currentSize)) {
 58
 59
                     // Convert the strobogrammatic string to a number
 60
                     ll value = stoll(strobogrammaticNum);
 61
 62
                     // Check if the number is within the given range
                     if (lowerBound <= value && value <= upperBound) {</pre>
 63
 64
                         ++count;
 65
 66
 67
 68
             // Return the total count of strobogrammatic numbers in the range
 69
             return count;
 70
 71 };
 72
Typescript Solution
  1 // Use the 'bigint' type to handle large integer values in TypeScript
  2 type ll = bigint;
  4 // Define pairs that are strobogrammatic (they look the same when rotated 180 degrees)
  5 const strobogrammaticPairs: Array<[string, string]> = [['1', '1'], ['8', '8'], ['6', '9'], ['9', '6']];
    // Depth-First Search function to generate strobogrammatic numbers of a certain size
    const generateStrobogrammatic = (size: number, maxSize: number): string[] => {
        // Base cases: return arrays of empty string or single strobogrammatic digits
        if (size === 0) return [''];
 10
         if (size === 1) return ['0', '1', '8'];
 11
 12
 13
         let results: string[] = [];
 14
 15
         // Generate smaller strobogrammatic numbers and append new pairs to them
         const smallerNumbers = generateStrobogrammatic(size - 2, maxSize);
 16
         for (const smallerStr of smallerNumbers) {
 17
             for (const [left, right] of strobogrammaticPairs) {
 18
 19
                 results.push(`${left}${smallerStr}${right}`);
 20
 21
             // If not at the outermost layer, we can add '0' at both ends
 22
             if (size !== maxSize) {
 23
                 results.push(`0${smallerStr}0`);
 24
 25
 26
         return results;
 27 };
 28
    // Function that calculates the count of strobogrammatic numbers within a given range
    const strobogrammaticInRange = (low: string, high: string): number => {
         // Initialize counter for valid strobogrammatic numbers within the range
 31
 32
         let count: number = 0;
 33
 34
         // Get sizes of the provided range
 35
         const sizeLow: number = low.length;
 36
         const sizeHigh: number = high.length;
 37
 38
         // Convert string bounds to 'bigint' for numerical comparison
 39
         const lowerBound: ll = BigInt(low);
         const upperBound: ll = BigInt(high);
 40
 41
 42
         // Generate strobogrammatic numbers for sizes within the inclusive range [sizeLow, sizeHigh]
 43
         for (let currentSize: number = sizeLow; currentSize <= sizeHigh; ++currentSize) {</pre>
 44
             // Generate strobogrammatic numbers of the current size
 45
             const strobogrammaticNumbers = generateStrobogrammatic(currentSize, currentSize);
 46
             for (const numStr of strobogrammaticNumbers) {
 47
                 // Convert the strobogrammatic string to a number
 48
                 const value: ll = BigInt(numStr);
 49
 50
```

Time Complexity The time complexity of the solution can be analyzed as follows: • The recursive function dfs(u) generates all strobogrammatic numbers of length u.

Time and Space Complexity

count++;

return count;

• The number of strobogrammatic numbers of length u grows exponentially since every pair of digits can lead to 5 possibilities (including the '00' pair except at the top level). Therefore, approximately, the recursion's time complexity can be described by

The space complexity can be analyzed as follows:

T(u) = 5 * T(u - 2) for u > 1, which indicates exponential growth. • The full search for generating strobogrammatic numbers ranges from length a (len(low)) to length b (len(high)), and the generation complexity would roughly be $0(1) + 0(5^{(a-1)/2}) + \dots + 0(5^{(b-1)/2})$, which is dominated by the largest

term $0(5^{(b-1)/2})$ when b is even or $0(5^{(b/2)})$ when b is odd.

considering zero-padded numbers), where k is the number of results from dfs(u - 2).

For u=0 and u=1, it returns a fixed set of values, so this is constant time, 0(1).

// Check if the number is within the given range

if (lowerBound <= value && value <= upperBound) {</pre>

// Return the total count of strobogrammatic numbers in the range

Considering the final for-loop that iterates over n from a to b inclusive and checks against the range, the overall time complexity would be approximated by $0(b * 5^{(b/2)})$, where b is the length of high. **Space Complexity**

The given code defines a Solution class with a method strobogrammatic InRange to find strobogrammatic numbers within a given

• For u > 1, it recursively calls dfs(u - 2) and then iterates over the result, which we'll call k, prepending and appending pairs of

strobogrammatic digits to each string. Since there are four pairs it can append (except for the first and last digits, for which

there's an additional pair), the number of operations for each recursive call relates to 4 * k + k (when u is not equal to n,

range. A strobogrammatic number is a number that looks the same when rotated 180 degrees (e.g., 69, 88, 818).

 Additionally, the space to store ans increases exponentially with the recursion, similar to time complexity, since every level of recursion generates a list of numbers that grows exponentially. • The space is freed once each recursive call completes, but the maximum held at any time relates to the maximum depth of the

• The recursion dfs(u) will have a maximum stack depth equivalent to b/2 (since each recursive step reduces u by 2).

recursion tree, meaning the space complexity is also dominated by the output size of the deepest recursion call.

Given the above, the space complexity is also $0(5^{(b/2)})$, where b is the length of high.

Problem Description The challenge presented involves identifying a special class of numbers known as "strobogrammatic numbers." A strobogrammatic