1508. Range Sum of Sorted Subarray Sums

Binary Search

Leetcode Link

Problem Description

Medium Array

The given problem revolves around finding the sum of a specific subset of a sorted array that contains sums of all non-empty continuous subarrays of the given array nums. The problem requires three inputs: nums - an array of n positive integers.

Sorting

- Left the starting index from which to sum (one-indexed).
- 3. right the ending index up to which to sum (one-indexed).

Two Pointers

Our objective is to compute the sum of all non-empty continuous subarrays, sort these sums, and then calculate the sum of the elements from the left to right indices in the sorted array. The final answer should be returned modulo 10^9 + 7 to handle very

these sums. This can be done by using two nested loops:

2. Use a nested loop to iterate through all possible subarrays:

After adding nums [j] to s, append the new sum to arr.

large numbers which could cause integer overflow situations. To clarify:

 A non-empty continuous subarray is a sequence of one or more consecutive elements from the array. Sorting these sums means arranging them in non-decreasing order.

- Summing from index left to index right implies adding all elements of the sorted sums array starting at index left-1 and ending at index right-1 (since the problem statement indexes from 1, but arrays in most programming languages, including
- Python, are 0-indexed).
- Intuition

The brute force approach to this problem is to generate all possible continuous subarrays of nums, calculate their sums, and then sort

1. The outer loop goes through each element of nums from which a subarray can start.

2. The inner loop extends the subarray from the starting element from the outer loop to the end of nums, calculating the sum for each extension.

This generates an array arr of sums for each subarray. Once we have this array, we sort it. With the sorted array, we now only need

- to sum the numbers from left-1 to right-1 since we're using Python's zero-indexing (the original problem indexes from 1).
- This solution is intuitive but not optimized. It can solve the problem as long as the nums array is not too large since the time complexity would otherwise become prohibitive. For larger arrays, an optimized approach should be considered involving more

force method, being mindful of its limitations. **Solution Approach**

advanced techniques such as prefix sums, heaps, or binary search. However, for the provided solution, we stick to the intuitive brute

The provided solution iterates through each possible subarray of the given array nums and maintains a running sum. To achieve this, the following steps are implemented: Initialize an empty list arr that will hold the sums of all non-empty continuous subarrays.

○ The outer loop, controlled by variable 1, goes from 0 to n-1, where 1 represents the starting index of a subarray.

arr[left - 1 : right].

In summary, the approach uses:

 For each i, initialize a sum variable s to 0, to calculate the sum of the subarray starting at index i. ◦ The inner loop, controlled by variable j, goes from i to n-1. In each iteration of this loop, add the value nums [j] to s. This effectively extends the subarray by one element in each iteration.

- 3. Once all sums are calculated, sort the list arr with the .sort() method. This arranges all the subarray sums in non-decreasing order.
- This is important since the sum of subarray sums could be very large. 6. Return the result.

5. Compute the result modulo 10***9 + 7 to get the output within the specified range and handle any potential integer overflow.

4. Calculate the sum of the elements from index left-1 to right-1 in the sorted list arr. This is done with the slice notation

- Brute force algorithm: to generate all subarray sums. Sorting: to arrange the sums in non-decreasing order.
- The time complexity of this approach is $0(n^2)$ for generating the subarray sums and 0((n*(n+1)/2) * log(n*(n+1)/2)) for sorting, where n is the length of the nums array. The space complexity is 0(n*(n+1)/2) since we are storing the sum of each possible subarray

Iteration breakdown:

• For i = 0:

in arr.

Example Walkthrough

To illustrate the solution approach, let's consider a small example:

 \circ j = 0:s = 0 + nums[0] (add 1), arr becomes [1].

3. Sorting arr: We sort arr, resulting in [1, 2, 3, 3, 5, 6].

 \circ j = 1:s = 1 + nums[1] (add 2), arr becomes [1, 3].

 \circ j = 2:s = 3 + nums[2] (add 3), arr becomes [1, 3, 6].

 \circ j = 1:s = 0 + nums[1] (add 2), arr becomes [1, 3, 6, 2].

 \circ j = 2:s = 0 + nums[2] (add 3), arr becomes [1, 3, 6, 2, 5, 3].

Suppose we have an array nums = [1, 2, 3], with left = 2 and right = 3. We need to find the sum of the sorted subarray sums from the left to right indices, inclusive.

Prefix sum technique: by maintaining a running sum s as we iterate through the array.

Modular arithmetic: to ensure the final sum stays within the specified limits.

2. Iterate using nested loops: The outer loop runs with i from 0 to 2 (the length of nums minus one).

4. Calculate the result: We sum the elements from left-1 to right-1, which corresponds to the second (index 1) and third (index

• For i = 1:

1. Initialize arr: We start with an empty list arr to hold the sums of all non-empty continuous subarrays.

The inner loop starts with j at i, with s initialized to 0 each time the outer loop starts.

 \circ j = 2:s = 2 + nums[2] (add 3), arr becomes [1, 3, 6, 2, 5]. • For i = 2:

from typing import List

subarray_sums = []

for i in range(n):

return range_sum

current_sum = 0

for j in range(i, n):

class Solution:

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5. Modular arithmetic: The final step is to take the result modulo 10***9 + 7. Since 5 is already less than 10***9 + 7, the answer remains 5. The method returns the result 5, which is the sum of the second and third smallest sums of non-empty continuous subarrays of nums. In this case, the sums of these subarrays are 2 for the subarray [2] and 3 for the subarrays [3] and [1, 2]. Since [3] appears twice, we only count it once in the specified range. This walkthrough summarizes the steps in the provided solution to compute the sum of subarray sums in a given range after sorting them, thereby displaying the complete process from initialization through to obtaining the final result. Python Solution

def rangeSum(self, nums: List[int], n: int, left: int, right: int) -> int:

Calculate the sum of every contiguous subarray and store it into subarray_sums

subarray_sums.append(current_sum) # Append the current sum to the list

Note: The '-1' adjustment is required because list indices in Python are 0-based

current_sum += nums[j] # Add the current element to the sum

Compute the sum of the elements from the 'left' to 'right' indices

int index = 0; // Index to insert the next sum into subarraySums

int currentSum = 0; // Stores the sum of the current subarray

currentSum += nums[end]; // Add the next element to the currentSum

// Calculate the sum of the subarray sums between indices left-1 and right-1 (inclusive)

answer = (answer + subarraySums[i]) % mod; // Aggregate the sum modulo mod

subarraySums[k++] = currentSum; // Store the sum of the subarray

for (int end = start; end < n; ++end) -

sort(subarraySums.begin(), subarraySums.end());

return answer; // Return the final calculated sum

let subarraySums: number[] = new Array(n * (n + 1) / 2);

let currentSum = 0; // Stores the sum of the current subarray

let index = 0; // Index for inserting into subarraySums

// Calculate the sum of all possible subarrays

for (let end = start; end < n; ++end) {

for (let start = 0; start < n; ++start) {</pre>

const int mod = 1e9 + 7; // The modulo value

for (int i = left - 1; i < right; ++i) {</pre>

int answer = 0; // Variable to store the final answer

// Sort the sums of the subarrays

// Loop over nums array to define starting point of subarray

range_sum = sum(subarray_sums[left - 1 : right]) % mod

Return the computed sum modulo 10^9 + 7

1 import java.util.Arrays; // Import Arrays class for sorting

for (int i = 0; i < n; ++i) {

Initialize an array to store the sum of contiguous subarrays

2) elements in the sorted arr. This gives us the sum of 2 + 3 = 5.

- 15 # Sort the array of subarray sums in non-decreasing order subarray_sums.sort() 16 17 # Define the modulus value to prevent integer overflow issues 18 mod = 10**9 + 719 20
- Java Solution

// This method calculates the sum of values within a given range of subarray sums from nums array

public int rangeSum(int[] nums, int n, int left, int right) { // Calculate the total number of subarray sums int totalSubarrays = n * (n + 1) / 2; // Initialize an array to store all possible subarray sums 10 int[] subarraySums = new int[totalSubarrays]; 11

class Solution {

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int currentSum = 0; // Holds the temporary sum of the current subarray
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               // Loop over nums array to create subarrays starting at index i
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                for (int j = i; j < n; ++j) {
                    currentSum += nums[j]; // Add the current number to the current subarray sum
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                    subarraySums[index++] = currentSum; // Store the current subarray sum and increment index
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           // Sort the array of subarray sums
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           Arrays.sort(subarraySums);
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           int result = 0; // Initialize the result to 0
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           final int mod = (int) 1e9 + 7; // Modulo value to prevent integer overflow
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           // Add the values from position "left" to "right" in the sorted subarray sums
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           for (int i = left - 1; i < right; ++i) {</pre>
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                result = (result + subarraySums[i]) % mod;
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           return result; // Return the computed sum
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35 }
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C++ Solution
1 #include <vector>
   #include <algorithm>
   class Solution {
   public:
       int rangeSum(vector<int>& nums, int n, int left, int right) {
           // Create an array to store the sums of all subarrays, with size based on the number of possible subarrays
           vector<int> subarraySums(n * (n + 1) / 2);
           int k = 0; // Index for inserting into subarraySums
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           // Calculate the sum of all possible subarrays
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           for (int start = 0; start < n; ++start) {</pre>
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Typescript Solution function rangeSum(nums: number[], n: number, left: number, right: number): number { // Calculate the number of possible subarrays and initialize an array to store their sums

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subarraySums[index++] = currentSum; // Store the sum of the subarray
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       // Sort the sums of the subarrays
       subarraySums.sort((a, b) => a - b);
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       let answer = 0; // Variable to store the final answer
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       const MOD = 1e9 + 7; // The modulo value
20
       // Calculate the sum of the subarray sums between indices left-1 and right-1 (inclusive)
21
       for (let i = left - 1; i < right; ++i) {
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           answer = (answer + subarraySums[i]) % MOD; // Aggregate the sum modulo MOD
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       return answer; // Return the final calculated sum
27 }
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Time and Space Complexity
The given Python code computes the range sum of all possible contiguous subarrays sorted in a non-decreasing order and then
returns the sum of the subarray values from the left to right indices (1-indexed). Here is the complexity analysis:

    Time Complexity:
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currentSum += nums[end]; // Add the next element to the current sum

- The outer loop runs n times, where n is the length of the input list nums. The inner loop runs n - i times for each iteration of the outer loop, summing elements and appending the sum to the array
- arr. When i is 0, the inner loop will run n times; when i is n-1, it will run 1 time. On average, it will run n/2 times. The sort operation on the array arr of size n * (n + 1) / 2 (the total number of subarrays) has a time complexity of 0(n^2 * $log(n^2)$) which simplifies to $0(n^2 * log(n))$.
- The sum operation over arr[left 1: right] can be considered O(k), where k is the difference between right and left. However, this is negligible compared to the sorting complexity.
- Combining these, the overall time complexity is dominated by the sort, resulting in $0(n^2 * \log(n))$.
 - results in O(n^2).

Space Complexity:

- \circ The space used by the array arr, which stores the n * (n + 1) / 2 sum values, dominates the space complexity. This No other significant space-consuming structures or recursive calls that would impact the overall space complexity.
- Therefore, the space complexity of the code is $O(n^2)$ and the time complexity is $O(n^2 * log(n))$.