1631. Path With Minimum Effort

You are a hiker preparing for an upcoming hike. You are given heights, a 2D array of size rows x columns, where heights [row] [col] represents the height of cell (row, col). You are situated in the top-left cell, (0, 0), and you hope to travel to the bottomright cell, (rows-1, columns-1) (i.e., **0-indexed**). You can move up, down, left, or right, and you wish to find a route that requires

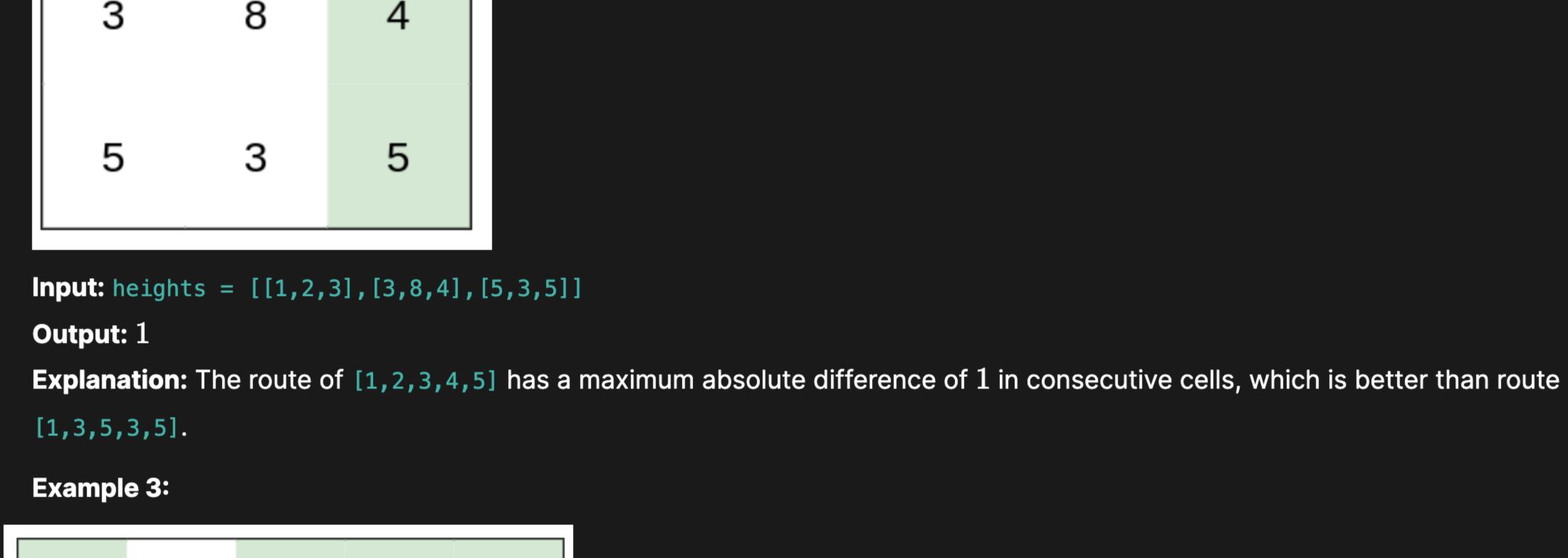
A route's effort is the maximum absolute difference in heights between two consecutive cells of the route.

Return the minimum effort required to travel from the top-left cell to the bottom-right cell. Example 1:

the minimum effort.

```
Input: heights = [[1,2,2],[3,8,2],[5,3,5]]
Output: 2
Explanation: The route of [1,3,5,3,5] has a maximum absolute difference of 2 in consecutive cells. This is better than the route
of [1,2,2,2,5], where the maximum absolute difference is 3.
```

Example 2:



Input: heights = [[1,2,1,1,1],[1,2,1,2,1],[1,2,1,2,1],[1,2,1,2,1],[1,1,1,2,1]]

rows == heights.length columns == heights[i].length

Output: 0

Constraints:

Explanation: This route does not require any effort.

Solution **Brute Force** Our most simple brute force for this problem would be to try all different routes that start from the top-left cell and end in the bottom-right cell. We'll then find the efforts for all these routes and return the smallest.

 $1 \leq \text{rows}, \text{columns} \leq 100$

 $1 \leq \text{heights[i][j]} \leq 10^6$

left cell to the bottom-right cell such that we never travel between cells with a distance that exceeds a. We can accomplish this with a BFS/flood fill algorithm.

above.

Time Complexity

Time Complexity: $\mathcal{O}(RC \log M)$

queue<int> qCol;

vis[0][0] = true;

while (!qRow.empty()) {

continue;

continue;

continue;

continue;

continue;

qRow.add(newRow);

qCol.add(newCol);

return vis[rows-1][columns-1];

int rows = heights.length;

high = mid;

low = mid;

mid = (low + high) / 2;

qRow = collections.deque([0])

curRow = qRow.popleft()

curCol = qCol.popleft()

continue

continue

continue

qRow_append(newRow)

qCol.append(newCol)

process next node

return vis[rows-1][columns-1]

if isValidEffort(heights,mid):

while low + 1 < high:

high = mid

low = mid

mid = (low + high) // 2

newRow = curRow + deltaRow

newCol = curCol + deltaCol

vis[newRow][newCol] = True

vis[0][0] = True

while qRow:

qCol = collections.deque([0]) # BFS starts in top-left cell

check if cell is in boundary

check if distance exceeds limit

for [deltaRow, deltaCol] in [(-1, 0), (0, 1), (1, 0), (0, −1)]:

if (newRow < 0 or newRow >= rows or newCol < 0 or newCol >= columns):

if vis[newRow][newCol] == True: # check if cell has been visited

if (abs(heights[newRow][newCol] - heights[curRow][curCol]) > mid):

} else {

// process next node

public int minimumEffortPath(int[][] heights) {

if (isValidEffort(heights,mid)) {

vis[newRow][newCol] = true;

// check if distance exceeds limit

int columns = heights[0].length; // dimensions for heights

qRow.push(0);

const vector<int> deltaRow = $\{-1, 0, 1, 0\}$;

const vector<int> deltaCol = $\{0, 1, 0, -1\}$;

bool isValidEffort(vector<vector<int>>& heights, int mid) {

qCol.push(0); // BFS starts in top-left cell

Full Solution

<u>search</u>. Why can we binary search this value? Let's say our minimum **good** effort is b. Our binary search condition is satisfied since all values **strictly** less than b are **not good** and all values greater or equal to b are **good**.

Every binary search iteration, we can check whether or not some effort is good by running the BFS/flood fill algorithm mentioned

The minimum effort a that's **good** is the final answer that we return. To find the minimum effort, we can implement a binary

Instead of thinking of finding the efforts of all possible routes, we should think about finding routes that have some specific

A route will have an effort smaller or equal to a if it travels from the top-left cell to the bottom-right cell and all adjacent cells in

the route have a distance that doesn't exceed a. To check if such routes exist, we can check if there exists a path from the top-

effort. Given some effort a, how do we check if there exists a route that has an effort smaller or equal to a?

Let's first denote the distance between two adjacent cells as the absolute difference between their heights.

We'll denote an effort a as **good** if there exists a route with an effort smaller or equal to a.

Let's denote R as number of rows, C as number of colmns, and M as maximum height in heights. Since BFS/flood fill will run in $\mathcal{O}(RC)$ and we have $\mathcal{O}(\log M)$ binary search iterations, our final time complexity will be $\mathcal{O}(RC\log M)$.

// dimensions for heights

if (abs(heights[newRow][newCol] - heights[curRow][curCol]) > mid) { // check if distance exceeds lin

int rows = heights.size(); int columns = heights[0].size(); vector<vector<bool>> vis(rows, vector<bool>(columns)); // keeps track of whether or not we visited a node queue<int> qRow;

C++ Solution

class Solution {

```
int curRow = qRow.front();
qRow.pop();
int curCol = qCol.front();
qCol.pop();
for (int dir = 0; dir < 4; dir++) {</pre>
    int newRow = curRow + deltaRow[dir];
    int newCol = curCol + deltaCol[dir];
    if (newRow < 0 || newRow >= rows || newCol < 0 || newCol >= columns) { // check if cell is in bounda
```

if (vis[newRow][newCol]) { // check if cell has been visited

//We can also use queue<pair<int,int>> to store both the row & col in one queue

```
vis[newRow][newCol] = true;
                qRow.push(newRow);
                qCol.push(newCol);
                // process next node
        return vis[rows - 1][columns - 1];
  public:
   int minimumEffortPath(vector<vector<int>>& heights) {
        int low = -1; // every effort less or equal to low will never be good
        int high = (int)1e6; // every effort greater or equal to high will always be good
        int mid = (low + high) / 2;
        while (low + 1 < high) {
           if (isValidEffort(heights, mid)) {
                high = mid;
           } else {
                low = mid;
           mid = (low + high) / 2;
        return high;
Java Solution
class Solution {
    final int[] deltaRow = \{-1, 0, 1, 0\};
    final int[] deltaCol = \{0, 1, 0, -1\};
   private boolean isValidEffort(int[][] heights, int mid){
        int rows = heights.length;
        int columns = heights[0].length; // dimensions for heights
        boolean[][] vis = new boolean[rows][columns]; // keeps track of whether or not we visited a node
        Queue<Integer> qRow = new LinkedList();
        Queue<Integer> qCol = new LinkedList();
        qRow.add(0);
        qCol.add(0); // BFS starts in top-left cell
        vis[0][0] = true;
        while (!qRow.isEmpty()) {
           int curRow = qRow.poll();
           int curCol = qCol.poll();
            for (int dir = 0; dir < 4; dir++) {</pre>
                int newRow = curRow + deltaRow[dir];
                int newCol = curCol + deltaCol[dir];
                if (newRow < 0 || newRow >= rows || newCol < 0</pre>
                    || newCol >= columns) { // check if cell is in boundary
                    continue;
                if (vis[newRow][newCol]) { // check if cell has been visited
```

int low = -1; // every effort less or equal to low will never be good int high = (int) 1e6; // every effort greater or equal to high will always be good int mid = (low + high) / 2;while (low + 1 < high) {

```
return high;
Python Solution
import collections
class Solution:
    def minimumEffortPath(self, heights: List[List[int]]) -> int:
        rows = len(heights)
        columns = len(heights[0]) # dimensions for heights
        low = -1 # every effort less or equal to low will never be good
        high = 10 ** 6 # every effort greater or equal to high will always be good
        mid = (low + high) // 2
        def isValidEffort(heights, mid):
            vis = [[False] * columns for a in range(rows)]
            # keeps track of whether or not we visited a node
```

if (Math.abs(heights[newRow][newCol] - heights[curRow][curCol]) > mid){

```
Solution Implementation
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Python

Java

C++

return high

else:

```
TypeScript
```