2874. Maximum Value of an Ordered Triplet II

Medium <u>Array</u>

Problem Description

In this problem, we are given an array of integers, nums, indexed starting from 0. The task is to find the maximum value that can be obtained from choosing any three different indices (i, j, k) in the array such that i < j < k. The value of a triplet (i, j, k)is calculated using the formula (nums[i] - nums[j]) * nums[k].

If we consider different combinations of three elements from the array, some might yield negative values, while others might yield

positive values or zero. We want to find the maximum positive value, or if all the possible triplets result in a negative value, we return 0. To understand the value of a triplet, let's consider that nums[i] is greater than nums[j], then (nums[i] - nums[j]) will be positive.

In this case, to maximize the value of the triplet, you would want nums [k] to be as large as possible because you are multiplying by nums [k]. If nums [i] is less than nums [j], the difference becomes negative, and a large nums [k] will only lead to a more negative value. In that case, we are not interested in those combinations as our goal is to find the maximum positive value.

The intuition behind the solution is to traverse the array while keeping track of two key values: the maximum value found so far

Intuition

the maximum value of the triplet without having to explicitly check all possible triplet combinations. The maximum prefix value mx represents the largest number we have seen so far as we iterate through the array. This value could potentially be nums [i] of our triplet. As we are looking for i < j < k, any number we see can be a candidate for nums [k].

(mx), and the maximum difference between mx and the current value (mx_diff). These two variables help in efficiently computing

The maximum difference mx_diff represents the highest value obtained from subtracting any previously encountered number from mx. It effectively keeps track of the maximum (nums[i] - nums[j]) that we have seen so far.

While we iterate through the array, for any current number num, we calculate and update ans with max(ans, mx_diff * num). This

step calculates the maximum triplet value for the current number as nums [k] (since num is always the right-most element in the

potential triplet). We ensure to first update ans before updating mx_diff because mx_diff needs to be the result of the prefix, not including the current number. **Solution Approach**

When we start iterating through the array nums, we initialize two variables mx and mx_diff with zero. mx will keep track of the

maximum value we have encountered so far (i.e., the maximum value for nums[i]), and mx_diff will store the maximum difference computed as (nums[i] - nums[j]) during the iteration.

step ensures that we always have the maximum possible product for the current state of the array.

The approach is to cleverly keep track of the necessary values as we iterate through the array, enabling us to calculate the

Update the Answer: For the current value num in nums, we attempt to update the answer, ans, with the maximum of either ans itself or the product of mx_diff and num. The reason behind this calculation is that num will serve as nums [k] (the potential third element in our triplet), and mx_diff represents the maximum difference from previous elements nums[i] and nums[j]. This

ans = max(ans, mx_diff * num)

Hence, it is updated as the maximum of itself or mx - num.

include the current num as mx_diff gets updated only after ans.

maximum triplet value on the fly without the need to consider each triplet individually.

Below are the steps that we perform as we traverse the array nums from left to right:

Update Maximum Value: Next, we update mx to be the maximum of itself or the current value num, because as we move through the array, we need to keep track of the largest value seen so far that could become nums [i] for future triplets. mx = max(mx, num)**Update Maximum Difference**: Finally, we update mx_diff. To maintain the invariant that mx_diff is the maximum difference

for a valid triplet, we must ensure that it is always calculated uptil the elements before num (as num is a candidate for nums [k]).

mx_diff = max(mx_diff, mx - num) Since we always update ans before mx_diff, we can guarantee that the difference applied to the calculation of ans doesn't

This way, as we move forward through the array, we dynamically update and maintain the necessary values to find the maximum

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triplet product based on the constraints given in the problem. The final answer is stored in ans, which by the end of the iteration
of the array contains the maximum value for all the valid triplets (i, j, k) that we were tasked with finding.
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The algorithm leverages two fundamental ideas:

• Dynamic Updates: Instead of considering every triplet separately, it keeps track of the potential maximums dynamically. • Greedy Choice Property: By choosing the best options at each step (maximum value and maximum difference), we ensure the end result is

with linear time complexity O(n) and constant space complexity O(1). **Example Walkthrough**

This concise yet effective approach and the minimal use of extra space (just two variables) contributes to an efficient solution

find the maximum value of (nums[i] - nums[j]) * nums[k] where i < j < k. We start by initializing mx and mx_diff as 0. The variable ans will be used to keep track of the maximum value we find.

1. We begin with the first element 1. mx is updated to 1 (it's the first element). There are no previous elements to consider, so we move to the next

Let's walk through a small example to illustrate the solution approach. Consider the array nums = [1, 5, 6, 3, 7]. We need to

3. Moving to element 6, mx remains at 5. mx_diff is updated to 0 (which was 5 - 5, the only pair we've considered). We can now consider the difference between the current mx and nums[j] which is from previous elements. However, we do not update ans since we still need a k index.

To summarize, the steps were as follows:

• nums[0] = 1: Initialize mx = 1, mx_diff = 0, ans = 0.

Import typing List to specify the type of the input nums.

def maximumTripletValue(self, nums: List[int]) -> int:

Iterate through each number in the input list.

max_number = max(max_number, number)

// ans - to store the maximum product of the triplet.

let [maxProduct, maxNum, maxDifference] = [0, 0, 0];

for (const num of nums) {

maxNum = Math.max(maxNum, num);

// maxNum - to store the maximum number encountered so far.

// the product of maxDifference and the current num.

maxProduct = Math.max(maxProduct, maxDifference * num);

// maxDifference - to store the maximum difference encountered so far.

// Loop through each number in the array to calculate the maximum triplet value.

// Update maxNum with the maximum of current maxNum and the current num.

// Update the maxProduct with the maximum of current maxProduct and

max_difference = max(max_difference, max_number - number)

element.

Python

optimal.

4. At element 3, mx is not updated since 3 is not greater than 5. mx_diff can be updated to 2 (mx which is 5 minus current element 3). The answer ans is now the maximum of 0 and $mx_diff * num$, which is 2 * 3 = 6.

5. Finally, we arrive at element 7. mx is not updated since 7 is not greater than current mx which is 5. We then calculate ans as the maximum of 6 and

 $mx_diff * num, which is 2 * 7 = 14.$ Thus, ans is updated to 14. mx_diff is updated to 4 (since 5 - 3 was less than 5 - 1 which is 4). After the iteration, ans holds the value 14, which is the maximum value for the expression (nums[i] - nums[j]) * nums[k].

2. At element 5, we update mx to 5 (since 5 is greater than mx which was 1). We cannot update mx_diff yet since we do not have a j index.

• nums[1] = 5: Update mx = 5. ans and mx_diff cannot be updated as we need a k. • nums[2] = 6: mx_diff can now be calculated, but remains 0, mx remains 5. • nums[3] = 3: Update mx_diff = 2. Update ans = max(0, 2 * 3) = 6.

The procedure efficiently finds the maximum value by dynamically updating the mx, mx_diff, and ans variables while traversing

the array a single time. The solution did not require examining all possible triplets, thus maintaining a linear time complexity.

• nums[4] = 7: Do not update mx but update ans = max(6, 2 * 7) = 14. Update $mx_diff = max(2, 5 - 3) = 4$.

Solution Implementation

Initialize variables to store the maximum triplet value, the maximum number encountered so far,

Update max_difference which is the maximum difference found between max_number and any number.

and the maximum difference between the maximum number and the current number.

Calculate the maximum triplet value by taking the maximum between the current max_triplet_value # and the product of max_difference and the current number. max_triplet_value = max(max_triplet_value, max_difference * number) # Update max_number if the current number is greater than the max_number seen so far.

max_triplet_value = 0

max_number = 0

max_difference = 0

for number in nums:

from typing import List

class Solution:

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# Return the maximum possible triplet value found.
        return max_triplet_value
Java
class Solution {
    // Method to calculate the maximum triplet value.
    public long maximumTripletValue(int[] nums) {
       // Initialize three variables to store the current maximum value,
       // the maximum difference found so far, and the answer we will return.
        long currentMax = 0;
        long maximumDiff = 0;
        long answer = 0;
       // Iterate through each number in the array.
        for (int num : nums) {
           // Calculate the tentative answer as the current number times the maximum difference,
           // update the answer if the result is greater than the current answer.
            answer = Math.max(answer, num * maximumDiff);
            // Update currentMax if the current number is greater than currentMax.
            currentMax = Math.max(currentMax, num);
           // Update maximumDiff if the difference between currentMax and current number
           // is greater than maximumDiff.
           maximumDiff = Math.max(maximumDiff, currentMax - num);
       // Return the final answer.
       return answer;
```

C++

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#include <vector>
#include <algorithm> // Include necessary headers for vector and max function
class Solution {
public:
    long long maximumTripletValue(std::vector<int>& nums) {
        long long maxTripletValue = 0; // This will hold the maximum value of the triplet found so far
        int maxNum = 0; // This will keep track of the maximum number encountered in the array
        int maxDifference = 0; // This will keep the maximum difference we've found between maxNum and a smaller number
       // Iterate over the elements of nums
        for (int num : nums) {
           // Update the maximum value of any triplet found so far.
           // The maximum triplet value is defined by maxDifference multiplied by the current number.
           maxTripletValue = std::max(maxTripletValue, 1LL * maxDifference * num);
           // Update maxNum if the current number is greater than the previous maxNum.
           maxNum = std::max(maxNum, num);
           // Update maxDifference if the difference between the current maxNum and num is greater
           // than the previous maxDifference.
           maxDifference = std::max(maxDifference, maxNum - num);
        return maxTripletValue; // Return the maximum triplet value found.
};
TypeScript
function maximumTripletValue(nums: number[]): number {
   // Initialize variables:
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// Update maxDifference with the maximum of current maxDifference and
          // the difference between current maxNum and the current num.
          maxDifference = Math.max(maxDifference, maxNum - num);
      // Return the calculated maximum product of a triplet.
      return maxProduct;
# Import typing List to specify the type of the input nums.
from typing import List
class Solution:
   def maximumTripletValue(self, nums: List[int]) -> int:
       # Initialize variables to store the maximum triplet value, the maximum number encountered so far,
       # and the maximum difference between the maximum number and the current number.
       max_triplet_value = 0
       max_number = 0
       max_difference = 0
       # Iterate through each number in the input list.
        for number in nums:
           # Calculate the maximum triplet value by taking the maximum between the current max_triplet_value
           # and the product of max difference and the current number.
           max_triplet_value = max(max_triplet_value, max_difference * number)
           # Update max_number if the current number is greater than the max_number seen so far.
           max_number = max(max_number, number)
           # Update max_difference which is the maximum difference found between max_number and any number.
           max_difference = max(max_difference, max_number - number)
       # Return the maximum possible triplet value found.
        return max_triplet_value
Time and Space Complexity
  The time complexity of the provided code is O(n) because there is a single for loop that iterates through the array nums once.
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Each operation inside the loop, such as updating ans, mx, and mx_diff, is done in constant time, independent of the size of the input array. As the loop runs n times, where n is the length of the array, the overall time complexity is linear. The space complexity of the code is 0(1). The reason for this constant space complexity is that only a fixed number of variables

(ans, mx, and mx_diff) are used. These variables do not depend on the size of the input, hence, the amount of allocated memory stays constant regardless of the input size.