2420. Find All Good Indices Medium Array **Dynamic Programming** Prefix Sum **Leetcode Link**

Problem Description In this problem, you are given an array nums of integers and a positive integer k. Your task is to find all the "good" indices in this array.

1. The k elements immediately before index i are in non-increasing order. This means each element is less than or equal to the element before it.

2. The k elements immediately after index i are in non-decreasing order. This means each element is greater than or equal to the

element after it.

An index i is considered "good" if it satisfies two conditions based on the elements around it:

- The problem constraints are such that the "good" indices have to be in the range k <= i < n k, which means you do not need to consider the first k indices and the last k indices of the array. The task is to return all "good" indices in increasing order.
- For example, given nums = [2,1,1,1,3,4,1] and k = 2, index 3 is "good" because the two elements before it [2,1] are in nonincreasing order and the two elements after it [3,4] are in non-decreasing order.

The key to solving this problem lies in efficiently checking the two conditions for "good" indices without repeatedly iterating over k

elements for each potential "good" index. To do this, we can preprocess the array to create two additional arrays:

1. An array decr to keep track of the length of non-increasing sequences ending at each index. decr[i] gives the length of the non-increasing sequence before index i.

2. An array incr to keep record of the length of non-decreasing sequences starting at each index. incr[i] gives the length of the non-decreasing sequence after index i.

- By precomputing these values, we can quickly check whether an index is "good" by simply verifying if decr[i] >= k and incr[i] >= k. The preprocessing is efficient because each element only needs to be compared with its immediate predecessor or successor to update the decr and incr arrays respectively.
- The process is as follows:

• Initialize the decr and incr arrays to be of length n + 1 with all values set to 1. This accounts for the fact that each index is by

default part of a non-increasing or non-decreasing sequence of length 1 (itself). Populate the decr array starting from the second element up to the second to last element by comparing each element with the one before it. • Populate the incr array starting from the second to last element back to the second element by comparing each element with

Iterate over the range k to n - k to collect all "good" indices where both decr[i] >= k and incr[i] >= k hold true.

the one after it.

- The provided solution code correctly implements this approach, thus making the process of finding "good" indices efficient.
- Solution Approach The solution uses a straightforward approach with dynamic programming techniques to keep track of the lengths of non-increasing
- and non-decreasing subsequences around each index. Here's a step-by-step breakdown of how the algorithm and data structures are used:

2. Dynamic Programming - Filling decr Array: The decr array is populated in a forward pass starting from index 2 up to n - 1. For

1. Initialization of Arrays: The decr and incr arrays are initialized to be of size n + 1, with all elements set to 1. These arrays are used to store the lengths of non-increasing and non-decreasing subsequences, respectively. This initial setup caters to the fact

The check nums [i − 1] <= nums [i − 2] confirms that the sequence is non-increasing at the point before i.

By using incr[i], we can efficiently determine if there are k non-decreasing elements after index i.

O(nk)) down to O(n) because each element in nums is processed a constant number of times.

that solitary elements can be considered as subsequences of length one.

every index i, if the current element nums[i - 1] is less than or equal to its previous element nums[i - 2], then decr[i] is updated to be decr[i - 1] + 1, indicating that the non-increasing sequence continues.

>= k.

Example Walkthrough

Step 1: Initialization of Arrays

1, 6] and k = 3. We want to find all "good" indices.

Step 2: Dynamic Programming - Filling decr Array

decr[2] remains 1 (since 5 <= 5 is false).

decr[3] = decr[2] + 1 = 2 (since 4 <= 5 is true).

decr[4] = decr[3] + 1 = 3 (since 3 <= 4 is true).

We populate decr array from the second element to the second to last:

increasing elements before it.

3. Dynamic Programming - Filling incr Array: Similarly, the incr array is filled in a backward pass from index n - 3 to 0. For every index i, if the current element nums[i + 1] is less than or equal to the next element nums[i + 2], then incr[i] is updated to be incr[i + 1] + 1. \circ The condition nums [i + 1] <= nums [i + 2] ensures that the sequence after i is non-decreasing.

4. Find Good Indices: After populating decr and incr, the solution then iterates through the valid range of indices (k to n - k - 1)

and checks whether the conditions for "good" indices are met for each index. An index i is "good" if decr[i] >= k and incr[i]

The decr[i] array captures the length of non-increasing order, which can be utilized later to check if an index i has k non-

5. Result Collection: The indices that satisfy the good condition are added to the resultant list. This is done through a list comprehension that iterates over the valid range and includes the value i if it passes the check. This algorithm effectively reduces the time complexity from what could be a brute-force check using nested loops (which would be

Let's walk through a smaller example to illustrate the solution approach. Assume we have an array nums = [5, 4, 3, 7, 8, 5, 4, 2,

Initial decr: [1, 1, 1, 1, 1, 1, 1, 1, 1, 1] Initial incr: [1, 1, 1, 1, 1, 1, 1, 1, 1, 1]

We initialize decr and incr arrays of length n + 1 (where n is the length of nums, which is 10) and set all values to 1.

Updated decr: [1, 1, 1, 2, 3, 1, 1, 2, 3, 1, 1]

 decr[5] resets to 1 (since 7 <= 3 is false). ... Continue this for the rest of the array.

Applying this solution to larger arrays is efficient because it avoids repeated calculations for each index, instead utilizing the

incr[7] = incr[8] + 1 = 3 (since 4 <= 2 is false). • incr[6] resets to 1 (since 5 <= 4 is false).

• ... Continue this pass for the rest of the array.

Updated incr: [1, 1, 1, 1, 1, 1, 1, 1, 2, 3, 1]

We populate incr array in a backward pass:

Step 3: Dynamic Programming - Filling incr Array

• incr[8] = incr[9] + 1 = 2 (since 2 <= 1 is false).

Step 4: Find Good Indices

We then loop through the range k to n - k and check if both decr[i] >= k and incr[i] >= k:

- i = 3 does not satisfy decr[3] >= 3. • i = 4 satisfies both decr[4] >= 3 and incr[4] >= 3.
- We collect all "good" indices. For our example, the only "good" index we find is 4. Thus, the output is [4].

precomputed decr and incr arrays for quick lookups.

def good_indices(self, nums: List[int], k: int) -> List[int]:

Build the non-increasing sequence length array

increment the length at the current index

increment the length at the current index

public List<Integer> goodIndices(int[] nums, int k) {

// Initialize list to store all the good indices

// and at least k non-decreasing elements after it

// Return the list containing all the good indices found

// Function to find all good indices based on the given conditions

nonIncrLens[i] = nonIncrLens[i - 1] + 1;

// Calculate lengths of non-decreasing subsequences from the end

nonDecrLens[i] = nonDecrLens[i + 1] + 1;

// Iterate through the array to find all the good indices

if (nonIncrLens[i - 1] >= k && nonDecrLens[i + 1] >= k) {

increment a value at the current index based on the previous index.

 \circ This back traversal is done n - 3 times, also yielding a time complexity of O(n).

// Check if the current index i is a good index

for (let i = n - 2; $i \ge 0$; --i) {

// Array to store the good indices

let goodIndicesList: number[] = [];

for (let i = k; i < n - k; ++i) {

goodIndicesList.push(i);

// Return the list of all good indices

if (nums[i] <= nums[i + 1]) {</pre>

// Calculate lengths of non-increasing subsequences from the start

vector<int> goodIndices(vector<int>& nums, int k) {

for (int i = 1; i < n; ++i) {

if (nums[i] <= nums[i - 1]) {</pre>

// Traverse the array and add indices to the list that are good indices

if (decreasingLengths[i] >= k && increasingLengths[i] >= k) {

// A index is good if there are at least k non-increasing elements before it

List<Integer> goodIndices = new ArrayList<>();

for (int i = k; i < n - k; ++i) {

goodIndices.add(i);

return goodIndices;

// Create array to store the lengths of decreasing sequences

// Initialize the length of the array

int[] decreasingLengths = new int[n];

int n = nums.length;

Initialize the length of the 'nums' list

 $non_decreasing_lengths = [1] * (n + 1)$

if nums[i - 1] <= nums[i - 2]:</pre>

if nums[i + 1] <= nums[i + 2]:</pre>

for i in range(2, n - 1):

for i in range(n - 3, -1, -1):

... Continue this for the range.

Step 5: Result Collection

n = len(nums)# Initialize two lists to track the non-increasing sequence lengths # to the left and non-decreasing sequence lengths to the right of every index $non_increasing_lengths = [1] * (n + 1)$

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Java Solution

class Solution {

Python Solution

class Solution:

from typing import List

27 # Find all 'good' indices, where both the non-increasing sequence on the left 28 # and the non-decreasing sequence on the right are at least 'k' elements long $good_indices = [i for i in range(k, n - k) if non_increasing_lengths[i] >= k and non_decreasing_lengths[i] >= k]$ 30 31 return good_indices

If current and previous elements form a non-increasing sequence,

Build the non-decreasing sequence length array in reverse order

non_increasing_lengths[i] = non_increasing_lengths[i - 1] + 1

non_decreasing_lengths[i] = non_decreasing_lengths[i + 1] + 1

If the next element and the one after it form a non-decreasing sequence,

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// Create array to store the lengths of increasing sequences
            int[] increasingLengths = new int[n];
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            // Initially set lengths of sequences to 1 for all elements
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            Arrays.fill(decreasingLengths, 1);
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           Arrays.fill(increasingLengths, 1);
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           // Calculate lengths of non-increasing sequences to the left of every index
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            for (int i = 1; i < n - 1; ++i) {
                if (nums[i] <= nums[i - 1]) {</pre>
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                    decreasingLengths[i + 1] = decreasingLengths[i] + 1;
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           // Calculate lengths of non-decreasing sequences to the right of every index
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            for (int i = n - 2; i > 0; ---i) {
                if (nums[i] <= nums[i + 1]) {</pre>
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                    increasingLengths[i - 1] = increasingLengths[i] + 1;
```

int n = nums.size(); // Total number of elements in nums // Arrays to keep the lengths of non-increasing and non-decreasing subsequences vector<int> nonIncrLens(n, 1); vector<int> nonDecrLens(n, 1); 11 12

public:

C++ Solution

1 #include <vector>

2 using namespace std;

class Solution {

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           // Calculate lengths of non-decreasing subsequences from the end
           for (int i = n - 2; i >= 0; --i) {
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                if (nums[i] <= nums[i + 1]) {</pre>
                    nonDecrLens[i] = nonDecrLens[i + 1] + 1;
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           // Vector to store the good indices
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           vector<int> goodIndices;
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           // Iterate through the array to find all the good indices
            for (int i = k; i < n - k; ++i) {
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               // Check if the current index i is a good index
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               if (nonIncrLens[i - 1] >= k && nonDecrLens[i + 1] >= k) {
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                    goodIndices.push_back(i);
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           // Return the list of all good indices
           return goodIndices;
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41 };
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Typescript Solution
   // TypeScript doesn't have a direct equivalent to the C++ <vector> library, so we use arrays instead.
   // Function to find all good indices based on the given conditions
    function goodIndices(nums: number[], k: number): number[] {
       const n: number = nums.length; // Total number of elements in nums
       // Arrays to keep the lengths of non-increasing and non-decreasing subsequences
       let nonIncrLens: number[] = new Array(n).fill(1);
        let nonDecrLens: number[] = new Array(n).fill(1);
10
       // Calculate lengths of non-increasing subsequences from the start
       for (let i = 1; i < n; ++i) {
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           if (nums[i] <= nums[i - 1]) {</pre>
                nonIncrLens[i] = nonIncrLens[i - 1] + 1;
15
```

Time Complexity 1. Building the non-increasing prefix array decr:

3. Finding good indices:

0(n).

return goodIndicesList;

Time and Space Complexity

 \circ Each operation is 0(1), and since we do this n-2 times, this part has a time complexity of 0(n). 2. Building the non-decreasing prefix array incr: Similarly, we iterate backward from n − 3 to 0, doing an 0(1) operation each time.

○ We iterate through the range [k, n - k) and check two conditions for each index i, which again takes 0(1) per index.

 \circ We iterate once from the index 2 to n - 1 (one-based indexing). In each iteration, we check a condition and possibly

The given Python code consists of two main parts - first, creating non-increasing (decr) and non-decreasing (incr) prefix arrays, and

second, iterating through the range [k, n - k] to check and collect good indices based on the condition given in the problem.

∘ There are n - 2k such indices, leading this part to have a time complexity of 0(n - 2k). However, since k is at most n, this simplifies to O(n).

Considering all three parts, the overall time complexity combines to:

• 0(n) + 0(n) + 0(n) = 0(3n) which simplifies to 0(n).

- 2. Space used for the output list:
 - \circ In the worst-case scenario, every index from k to n k may be a good index, so this list can take up to n 2k spaces. • The worst case for this list is also when k is very small compared to n, which would make its space complexity approach

 \circ Combined, they utilize 2 * (n + 1) memory space, which simplifies to 0(2n) or just 0(n).

- In conclusion, the time complexity of the code is O(n) and the space complexity is O(n).
- **Space Complexity** 1. Space used by decr and incr arrays: \circ Both arrays have a size of n + 1, so the space taken by each is O(n).
 - Therefore, combining the space complexities from the arrays and the final output list, we get:
 - O(n) + O(n) = O(2n) which simplifies to O(n).