# In this problem, we are given an array nums that contains a sequence of unique integers. The sequence may be sorted or not sorted.

**Problem Description** 

element as a pivot, it chooses a random pivot during each iteration. If the pivot matches the target, the function returns true. If the pivot is less than the target, all elements to the left of the pivot (including the pivot itself) are removed from the sequence, and the search continues with the remaining elements. Similarly, if the pivot is greater than the target, all elements to the right of the pivot are removed from the sequence. This continues until either the target is found (and true is returned) or the sequence is empty (and false is returned). The crux of the problem is to find out how many values in the nums array are guaranteed to be found using this function, regardless

We are tasked with implementing an algorithm that simulates a binary search-like process, but instead of choosing the middle

as pivots in each iteration, it will always end up being found if it is indeed in the sequence. Intuition

To solve this problem, we need to identify which elements in the sequence would always be found, regardless of the random

selection of the pivot. To do this, we need to find out whether choosing any pivot would lead to accidentally discarding the target

of which pivots are randomly selected in the process. A "guaranteed" value here means that no matter how the elements are chosen

## element when it shouldn't have been discarded. To be a 'binary search-able' number, a target value in the sequence must never be in the same subsequence as any incorrect pivot (an incorrect pivot being any element that would not be the target and would

mi.

For example, let's say our target is the number 3 in an unsorted sequence. If at any point during the function execution, the number 3 is in a subsequence with a pivot greater than 3, it might get discarded even though it hasn't been evaluated yet. Hence, the process involves two checks: 1. From left to right, we check if any element is smaller than any element to its left. If it is, then in some random pivot selection, it

could be incorrectly disregarded as a pivot. 2. From right to left, we check if any element is greater than any element to its right. If it is, then it could also lead to the same problem but in the opposite direction.

array to 1 (representing 'true'), indicating that we assume all elements are binary search-able.

mistakenly remove the target from consideration).

During the execution, we utilize two variables mx and mi to keep track of the maximum value encountered so far from the left and the minimum value from the right, respectively. Starting from the left of the array, for each element x, if it is smaller than mx, then it

cannot be binary search-able as there exists a larger value to the left. Thus, we set ok[i] to 0 for such an element. We then update

nums [i] is greater than mi, we set ok[i] to 0, indicating that the element can't be guaranteed to be searchable, and then we update

At the end of the process, sum(ok) will yield the total number of elements in the nums array that are guaranteed to be found, which is

We maintain an array, ok, to keep track of whether each element in nums is binary search-able. We initially set all elements in this

mx with the maximum value seen so far. We perform a similar procedure starting from the right of the array, using mi to track the minimum value seen so far. If any element

the solution to the problem. **Solution Approach** 

The solution provided leverages the concept of maintaining two boundary conditions as we iterate over the input array, which is a

common technique in problems involving subarrays or sequence behavior modifications based on certain conditions.

Here is a closer look at the step-by-step approach: 1. Initialize an array ok of the same length as nums, with all elements set to 1. This array will track whether each element in nums

2. Set mx (maximum boundary) to a very small number (the problem uses -1000000 as an initially small value) and mi (minimum

boundary) to a very large number (the problem uses 1000000), ensuring these boundaries will not affect the first comparison.

## 3. Iterate over nums from left to right, updating mx to be the maximum value seen so far. If the current element x is less than mx, it means x had a larger number before it, and thus, x can't be guaranteed to always be searchable. Set ok[i] to 0.

could be binary search-able (1 for yes, 0 for no).

Let's relate the steps with the actual code segments:

• The sum of elements in ok is obtained by return sum(ok).

than mi, it implies that there's a smaller element to its right, so if nums [i] were chosen as a pivot, it would mistakenly discard the smaller number. Set ok[i] to 0 for such cases.

5. Finally, sum up all elements in ok. This sum represents the count of elements that are guaranteed to be binary search-able.

4. Iterate over nums from right to left, updating mi to be the minimum value seen so far. If the current element nums [i] is greater

 The ok array initialization is directly represented by ok = [1] \* n. • Setting the mx and mi boundaries uses mx, mi = -10000000, 10000000.

The two for loops represent the left-to-right and right-to-left iterations with corresponding logic to update ok.

By combining the edge constraints from both ends of the array, we ensure that only those elements that satisfy the conditions for both leftward and rightward iterations are considered binary search-able. The nature of the algorithm is such that it has O(n) time complexity since it passes over the array twice—once from each end—and performs constant-time operations within each iteration.

In terms of algorithmic patterns, this approach can be recognized as a variant of the two-pointer technique where instead of moving

ability condition described in the problem.

Let's use a small example to illustrate the solution approach. We will walk through both the left-to-right and right-to-left iterations

Consider the array nums = [4, 2, 5, 7, 6, 3, 1] and the target value as 3. We will go through the algorithm to demonstrate how it

two pointers towards each other, we move boundaries in a way that encodes the validity of each element based on the search-

1. Initialize an array ok to [1, 1, 1, 1, 1, 1, 1], i.e., initially assuming all elements are search-able. 2. Set mx to -1000000 and mi to 1000000. **Left-to-Right Check:** 

• Next element is 2. It is less than the current mx (which is 4), so we update ok at index 1 to 0 [1, 0, 1, 1, 1, 1, 1].

# Finally, 1 is less than mx (7), so update ok at index 6 to 0 [1, 0, 1, 1, 0, 0, 0].

Right-to-Left Check:

set mi to 1.

Final Step:

Example Walkthrough

steps to clarify how the ok array gets updated.

 Since ok [5] was already 0, this step does not change the state of ok. Continue to 6, which is greater than the current mi (1), so ok at index 4 could potentially be set to 0, but it's already 0.

Finally, 4 is greater than mi (1), so ok remains as [1, 0, 1, 1, 0, 0, 0].

def binarySearchableNumbers(self, nums: List[int]) -> int:

is\_binary\_searchable = [1] \* num\_elements

for i in range(num\_elements -1, -1, -1):

is\_binary\_searchable[i] = 0

min\_from\_right = nums[i]

42 # result = solution.binarySearchableNumbers([1, 3, 2, 4, 5])

return sum(is\_binary\_searchable)

# it cannot be found using binary search.

# Return the count of elements that are binary searchable.

# This is the sum of the flags indicating binary searchability.

# Update the min value encountered from the right.

if nums[i] > min\_from\_right:

if value < max\_from\_left:</pre>

num\_elements = len(nums) # Number of elements in the input list

# This list holds flags for elements that are binary searchable.

# Initially set all elements as potentially binary searchable (1).

# Initialize the variables to keep track of the maximum value from the left

# Iterate from right to left to check if there's a smaller number after any element.

# If the current value is greater than the min found so far,

# print(result) # Output would be the count of binary searchable numbers in the input list

• Next is 2, which is greater than the current mi (1), and since ok at index 1 is 0, it remains unchanged.

Next element is 3. It's greater than the current mi (1), so we update ok at index 5 to 0 [1, 0, 1, 1, 0, 0, 0].

ensures whether 3 or any other value can be found regardless of the random pivot selections.

Start with the first element (4). Since mx is -10000000, 4 is greater than mx, so we set mx to 4.

Process 6, it is less than mx (7), so we update ok at index 4 to 0 [1, 0, 1, 1, 0, 1, 1].

Move to 3, it is less than mx (7), so update ok at index 5 to 0 [1, 0, 1, 1, 0, 0, 1].

Move to 5, which is greater than mx (4), so we update mx to 5.

Continue to 7, which is greater than mx (5), so we update mx to 7.

• Process 7, it is greater than mi (1), but ok at index 3 is still 1, and it remains 1 as 7 has no smaller element to its right. Move to 5, which is greater than mi (1), ok at index 2 remains 1.

Sum up the values in ok to find the total count of elements guaranteed to be searchable. In this case, sum(ok) equals to 3.

Therefore, 3 elements in the nums array can be guaranteed to be found using our random-pivot-based binary search algorithm. These

elements are 4, 5, and 7. These elements are guaranteed searchable because there are no other values to their left that would cause

• Start with the last element of the current ok state [1, 0, 1, 1, 0, 0, 0] which is 1. Since mi is 1000000, 1 is less than mi, so we

- them to be discarded if they were not chosen first, and similarly, no values to their right that would be incorrectly discarded if these elements were chosen as pivots.
- # and the minimum value from the right encountered so far. 12 max\_from\_left = float('-inf') 13 min\_from\_right = float('inf') 14 15 # Iterate from left to right to check if there's a larger number before any element. 16 for i, value in enumerate(nums):

### # If the current value is less than the max found so far, 19 20 # it cannot be found using binary search. 21 is\_binary\_searchable[i] = 0 22 else: 23 # Update the max value encountered from the left. 24 max\_from\_left = value

40 # Example usage:

**41** # solution = Solution()

else:

Python Solution

class Solution:

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from typing import List

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Java Solution
   class Solution {
       public int binarySearchableNumbers(int[] nums) {
            int length = nums.length; // Get the length of the array
           int[] searchable = new int[length]; // Define an array to keep track of searchable numbers
           Arrays.fill(searchable, 1); // Assume all numbers are initially searchable
           int maxLeft = Integer.MIN_VALUE; // Initialize the maximum to the smallest possible integer
           int minRight = Integer.MAX_VALUE; // Initialize the minimum to the largest possible integer
           // Forward pass: Check for each element if there is a larger number on its left
           for (int i = 0; i < length; ++i) {</pre>
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               if (nums[i] < maxLeft) {</pre>
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                   searchable[i] = 0; // If found, mark the element as unsearchable
               maxLeft = Math.max(maxLeft, nums[i]); // Update the max value from the left
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           int count = 0; // Initialize the count of binary searchable numbers
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           // Backward pass: Check for each element if there is a smaller number on its right
19
           for (int i = length - 1; i >= 0; --i) {
20
               if (nums[i] > minRight) {
21
22
                   searchable[i] = 0; // If found, mark the element as unsearchable
23
24
               minRight = Math.min(minRight, nums[i]); // Update the min value from the right
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26
                count += searchable[i]; // Increment count if the current number is searchable
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            return count; // Return the total count of binary searchable numbers
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31 }
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C++ Solution
 1 class Solution {
2 public:
       // Function to count how many numbers in the array are binary searchable
       int binarySearchableNumbers(vector<int>& nums) {
            int n = nums.size(); // Get the size of the array
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vector<int> isBinarySearchable(n, 1); // Initialize a vector to keep track of binary searchable numbers

isBinarySearchable[i] = 0; // If the current element is smaller than the max to the left, it's not searchable

isBinarySearchable[i] = 0; // If the current element is larger than the min to the right, it's not searchable

int maxToLeft = INT\_MIN; // Initialize the maximum to the left with the smallest int

maxToLeft = max(maxToLeft, nums[i]); // Update maxToLeft

int count = 0; // Initialize a count for the binary searchable numbers

minToRight = min(minToRight, nums[i]); // Update minToRight

return count; // Return the total count of binary searchable numbers

int minToRight = INT\_MAX; // Initialize the minimum to the right with the largest int

// Determine which elements are not searchable by traversing the array from left to right

// Determine which elements are not searchable by traversing the array from right to left

count += isBinarySearchable[i]; // Add to count if the number is binary searchable

isBinarySearchable = new Array(n).fill(1); // Initialize an array to keep track of binary searchable numbers

maxToLeft = Number.MIN\_SAFE\_INTEGER; // Initialize the maximum to the left with the smallest safe integer

minToRight = Number.MAX\_SAFE\_INTEGER; // Initialize the minimum to the right with the largest safe integer

### let minToRight: number; let isBinarySearchable: number[]; // Function to determine if a number is binary searchable function binarySearchableNumbers(nums: number[]): number { let n: number = nums.length; // Get the size of the array

Typescript Solution

2 let maxToLeft: number;

1 // Define the global variables

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for (int i = 0; i < n; ++i) {

if (nums[i] < maxToLeft) {</pre>

for (int i = n - 1; i >= 0; --i) {

if (nums[i] > minToRight) {

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30 };

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13
       // Determine which elements are not searchable by traversing the array from left to right
       for (let i = 0; i < n; ++i) {
14
           if (nums[i] < maxToLeft) {</pre>
15
               isBinarySearchable[i] = 0; // If the current element is smaller than maxToLeft, it's not searchable
16
           maxToLeft = Math.max(maxToLeft, nums[i]); // Update maxToLeft with the maximum value so far
18
20
21
       let count: number = 0; // Initialize a count for the binary searchable numbers
       // Determine which elements are not searchable by traversing the array from right to left
22
       for (let i = n - 1; i \ge 0; ---i) {
           if (nums[i] > minToRight) {
24
               isBinarySearchable[i] = 0; // If the current element is larger than minToRight, it's not searchable
26
27
           minToRight = Math.min(minToRight, nums[i]); // Update minToRight with the minimum value so far
           count += isBinarySearchable[i]; // Increment count if the element is binary searchable
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29
30
       return count; // Return the total count of binary searchable numbers
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Time and Space Complexity
Time Complexity
The given Python code performs a single forward pass through the array to identify elements that are not greater than any element
before them, and then performs a single backward pass to identify elements that are not less than any element after them. Each
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pass involves a simple comparison operation for each element of the list. The forward pass processes each element once, marking those elements that are smaller than the maximum element observed so far with a 0. This constitutes O(n) operations where n is the size of the nums list. Similarly, the backward pass also processes each element once, marking those elements that are greater than the minimum

- element observed so far with a 0. This also constitutes 0(n) operations. Finally, the summing operation to count the number of 1s in the ok list also takes O(n).
- **Space Complexity**

The space complexity is determined by the additional space used by the program excluding the input.

• The loop indices and temporary variables used for logic operations also occupy constant space.

Hence the overall time complexity of the code is O(n) + O(n) + O(n) which simplifies to O(n).

# • The code defines a list ok which has the same size as the input list nums. Therefore ok takes O(n) space.

- Variables mx and mi use constant space, so their space complexity contribution is 0(1).
- Thus, the overall space complexity of the code is O(n) due to the ok array. The rest of the variables do not contribute significantly as they are constant space.