## **Problem Description** You are tasked with finding the largest '+' shape that can be formed in a binary grid, where '1's represent a potential part of the '+'

are some coordinates provided in the mines array which represent where '0s' will be, thus creating obstacles for forming the '+'. The order of the plus sign is defined as the length from its center to its edge, which means the total size will be related to the order as order\*2 - 1. The goal is to return the highest order of a '+' sign found in this grid. If no '+' can be formed, the function should return 0. Intuition

and '0's represent a space where part of a '+' cannot exist. The grid is n x n in size, and originally it's filled with '1's. However, there

down from that center '1'.

The intuition behind finding the largest plus sign involves assessing each potential center for how far in each of the four directions (up, down, left, and right) we can go before hitting a '0' or the edge of the grid. We use dynamic programming to avoid redundant calculations. A matrix dp of the same dimensions as grid is created. Each element

When tasked with finding the largest axis-aligned plus sign of '1's in a modified binary grid, we need to think about what defines a

plus sign. For a plus sign to exist at any location, there must be uninterrupted sequences of '1's extending to the left, right, up, and

in dp will eventually represent the largest order of a plus sign that can have that cell as its center.

We initialize dp with 'n', representing the maximum possible order for a plus sign in an n x n grid. We then iterate through the indices

Next, we make four passes through the grid for each cell (i, j):

 From left to right: if there's no obstacle, we increase the count left, otherwise we start the count over. We then set dp[i][j] to the minimum of its current value (which will be at least left). From right to left, following the same logic with the variable right.

From top to bottom and bottom to top: the same process follows for the variables up, and down.

- After this process, we know for any cell in dp, it holds the minimum possible extension in all four directions, effectively giving us the order of the largest plus sign centered at that cell.
- Finally, we look for the maximum value in the dp array. This value is the order of the largest axis-aligned plus sign of '1's in the grid.

in the mines array, setting the corresponding dp cell to '0', indicating an obstacle.

To implement the solution for finding the largest plus sign, we utilize the dynamic programming technique that involves creating a 2D

array called dp that serves as a table to store intermediate results. This is crucial because it will help in reducing the complexity by storing the achievable order of a plus sign at each (i, j) position, thus avoiding recomputation.

1. Initialize the dp matrix, with n rows and n columns, setting every cell to n. This pre-population assumes the plus sign can extend

## to the edge of the grid in every direction from any cell.

Here's the step-by-step approach:

or 'down' counters.

constraints in all four directions.

left, right sequence calculations.

Here's a walkthrough of applying the solution step-by-step to this grid:

Right to left pass: Similar to above, but from the right.

Solution Approach

3. To calculate the order of the largest plus sign that can be centered at each cell, iterate over each row and column four times, once for each direction: left, right, up, and down.

is not zero, we increment left or right as appropriate, showing that the arm of the plus can extend in that direction.

For left and rightward checks, we loop through each row, once from left to right and then in the reverse direction. If dp[i] [j]

At each step, we update the dp matrix by assigning the minimum value amongst the current dp value and the 'left', 'right', 'up',

2. Iterate over the mines list, which contains the positions that must be set to '0'. The mines list modifies the dp matrix by setting

dp[x][y] = 0 for every [x, y] pair, showing that no plus sign can be centered at these 'mined' cells.

- Similarly, for upwards and downwards, we loop through each column in both top-to-bottom and bottom-to-top directions, incrementing up or down if dp[j][i] is not zero.
- plus sign that can be found in the grid. The specific data structure used here is a 2D list (list of lists) for the dp table, enabling direct access to each cell for its up, down,

4. After the conclusion of the loops, scan through the dp matrix to find the maximum value. This value is the order of the largest

This process ensures that dp[i][j] holds the order of the largest plus sign for which the cell (i, j) can be the center, considering the

Example Walkthrough

In terms of the algorithm, the solution employs an efficient linear scan of rows and columns, taking O(n^2) time — a significant

optimization over brute force approaches that would require 0(n^3) or greater. It effectively combines the principles of dynamic

programming with those of matrix traversal, effectively reducing the problem to simple arithmetic and comparisons.

Let's say we have a  $3\times3$  grid (n = 3) and the mines array is [[1, 1]], meaning there will be a '0' in the center of the grid.

1. We initialize the dp matrix to represent the maximum possible order of the plus sign in a 3×3 grid:

dp = [[3, 3, 3],[3, 3, 3], [3, 3, 3]]

2. We then apply the mines: since we have a mine at [1, 1], we set dp[1] [1] to 0, indicating no plus can be centered here.

## 3. Next, we make passes to calculate the left, right, up, and down order for each cell:

After the left to right pass:

After the right to left pass:

1 dp = [[1, 2, 3],

[3, 0, 3],

[3, 3, 3]]

dp = [[3, 3, 3],

Left to right pass: We count the number of consecutive '1's from the left for each cell in a row and update the dp value.

2 [1, 0, 3], 3 [1, 2, 3]]

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(We only update if the value of the current cell is greater than the count.)

    Top to bottom pass: We do the same vertically.
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2 [1, 0, 1],

3 [1, 2, 1]]

1 dp = [[1, 1, 1],

each direction from its center.

class Solution:

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41 };

int maxOrder = 0;

return maxOrder;

mines.forEach(mine => {

dpMatrix[mine[0]][mine[1]] = 0;

Typescript Solution

for (auto& row : dpMatrix) {

After bottom to top pass:

[1, 0, 1],

1 dp = [[1, 2, 3],

[1, 0, 1],

[1, 2, 3]]

- After top to bottom pass: 1 dp = [[1, 1, 1],
- [1, 1, 1]]

 $dp = [[n] * n for _ in range(n)]$ 

left = right = up = down = 0

for mine in mines:

for i in range(n):

x, y = mine

dp[x][y] = 0

maximum value which will give us the order of the largest '+'. In our example:

1\*2 - 1 = 1. Hence, the largest plus sign we can form has arms of length 1.

def orderOfLargestPlusSign(self, n: int, mines: List[List[int]]) -> int:

# Calculate the order of the largest plus sign considering mines.

for j, k in zip(range(n), reversed(range(n))):

dp[i][j] = min(dp[i][j], left)

dp[i][k] = min(dp[i][k], right)

dp[k][i] = min(dp[k][i], down)

dp[j][i] = min(dp[j][i], up)

return max(max(row) for row in dp)

// Set cells that are mines to 0

dp[mine[0]][mine[1]] = 0;

int left = 0, right = 0, up = 0, down = 0;

for (int j = 0, k = n - 1; j < n; ++j, --k) {

for (int[] mine : mines) {

for (int i = 0; i < n; ++i) {

# Initialize a 2D DP array with n rows and columns filled with value n.

Bottom to top pass: And finally, from bottom to top.

Python Solution from typing import List

# Initialize counts for the left, right, up, and down arms of the plus sign.

# Iterate over rows and columns in both the forward and reverse direction.

// Iterate over the matrix to find the maximal order of the plus sign at each point

// Count continuous ones from the left to right in a row

right = (dpMatrix[i][k] != 0) ? right + 1 : 0;

up = (dpMatrix[j][i] != 0) ? up + 1 : 0;

down = (dpMatrix[k][i] != 0) ? down + 1 : 0;

dpMatrix[i][j] = min(dpMatrix[i][j], left);

dpMatrix[k][i] = min(dpMatrix[k][i], down);

maxOrder = max(maxOrder, \*max\_element(row.begin(), row.end()));

const dpMatrix: number[][] = Array.from({ length: n }, () => Array(n).fill(n));

// Iterate over the matrix to calculate the arm length of plus signs in all directions

dpMatrix[j][i] = min(dpMatrix[j][i], up);

function orderOfLargestPlusSign(n: number, mines: number[][]): number {

// Setting up the mined locations in the dp matrix to 0

dpMatrix[i][k] = min(dpMatrix[i][k], right);

// Calculate continuous arm length for up and down directions

// The minimum of the 4 directions should be taken for the true arm length

// Find the maximum arm length from the dp matrix, which is the order of the largest plus sign

// Initialize a dp (dynamic programming) matrix filled with 'n', the maximum possible arm length

# If there's no mine, increment counts; else reset to 0.

# This represents the maximum size of the plus sign at each cell assuming no mines are present.

# Set each mine location in the DP array to 0 because these locations cannot be part of a plus sign.

21 left = left + 1 if dp[i][j] else 0 22 right = right + 1 if dp[i][k] else 0 23 up = up + 1 if dp[j][i] else 0 down = down + 1 if dp[k][i] else 0 24 25 26

# Update the DP array with the minimum arm length seen so far for each direction.

# Find the largest value in the DP array, which corresponds to the order of the largest plus sign.

# This ensures that the plus sign is only as long as the shortest arm length.

4. Now dp contains the order of the largest '+' that can be formed with each cell as its center. We scan through dp to find the

• The maximum value in dp is 1, which means the largest possible plus sign order is 1, and the size of this plus sign would be

To summarize, for this 3×3 grid with a mine at the center, the largest '+' sign we can form has an order of 1, extending a single cell in

### public int orderOfLargestPlusSign(int n, int[][] mines) { // Create a DP array and initialize each cell with the maximum size n int[][] dp = new int[n][n]; for (int[] row : dp) { Arrays.fill(row, n);

Java Solution

import java.util.Arrays;

public class Solution {

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                   left = dp[i][j] > 0 ? left + 1 : 0;
23
                   // Count continuous ones from the right to left in a row
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                   right = dp[i][k] > 0 ? right + 1 : 0;
25
                   // Count continuous ones from top to bottom in a column
                   up = dp[j][i] > 0 ? up + 1 : 0;
26
                   // Count continuous ones from bottom to top in a column
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                   down = dp[k][i] > 0 ? down + 1 : 0;
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                   // Update DP for the arms length of the plus sign, consider previous computations too
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                   dp[i][j] = Math.min(dp[i][j], left);
                   dp[i][k] = Math.min(dp[i][k], right);
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                   dp[j][i] = Math.min(dp[j][i], up);
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                   dp[k][i] = Math.min(dp[k][i], down);
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           // Find the largest plus sign order from the DP array
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           int maxOrder = Arrays.stream(dp)
               .flatMapToInt(Arrays::stream)
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41
               .max()
42
               .getAsInt();
43
44
           return maxOrder;
45
46 }
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C++ Solution
  1 class Solution {
  2 public:
         // This function calculates the order of the largest plus sign that can be found
         // in a square binary grid. Mines are represented by zeros in the grid.
         int orderOfLargestPlusSign(int n, vector<vector<int>>& mines) {
             // Initialize a dp (dynamic programming) matrix filled with 'n' which is the maximum possible arm length
  6
             vector<vector<int>> dpMatrix(n, vector<int>(n, n));
  8
             // Setting up the mined locations in the dp matrix to 0
  9
             for (auto& mine : mines) {
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                 dpMatrix[mine[0]][mine[1]] = 0;
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             // Iterate over the matrix to calculate the arm length of the plus sign in all directions
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             for (int i = 0; i < n; ++i) {
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                 int left = 0, right = 0, up = 0, down = 0;
                 for (int j = 0, k = n - 1; j < n; ++j, --k) {
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 18
                     // Calculate continuous arm length for left and right directions
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                     left = (dpMatrix[i][j] != 0) ? left + 1 : 0;
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#### 11 for (let i = 0; i < n; i++) { 12 13 14 15

});

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let left = 0, right = 0, up = 0, down = 0;
             for (let j = 0, k = n - 1; j < n; j++, k--) {
                // Calculate continuous arm length for left and right directions
                left = (dpMatrix[i][j] !== 0) ? left + 1 : 0;
                 right = (dpMatrix[i][k] !== 0) ? right + 1 : 0;
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                // Calculate continuous arm length for up and down directions
 19
                up = (dpMatrix[j][i] !== 0) ? up + 1 : 0;
 20
                down = (dpMatrix[k][i] !== 0) ? down + 1 : 0;
 21
 22
                // The minimum of the 4 directions should be taken for the true arm length
 23
                dpMatrix[i][j] = Math.min(dpMatrix[i][j], left);
 24
                dpMatrix[i][k] = Math.min(dpMatrix[i][k], right);
 25
                dpMatrix[j][i] = Math.min(dpMatrix[j][i], up);
 26
                dpMatrix[k][i] = Math.min(dpMatrix[k][i], down);
 27
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         // Find the maximum arm length from the dp matrix, which is the order of the largest plus sign
         let maxOrder = 0:
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 32
         dpMatrix.forEach((row) => {
 33
             maxOrder = Math.max(maxOrder, Math.max(...row));
         });
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 35
         return maxOrder;
 36
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Time and Space Complexity
Time Complexity
```

# The time complexity of the given code can be analyzed by breaking down each part of the code:

## 2. The first loop to set the mines takes O(m) time, where m is the number of mines. 3. The nested loops to calculate the left, right, up, and down values take 0(n^2) time. For each of the n rows and n columns, the loop runs n times.

- 4. The final nested loops also run in  $O(n^2)$  time, since it involves traversing the dp matrix again to calculate the minimum for each position and also to find the maximum order for plus sign at the end.
- Overall, the time complexity is dominated by the nested loops, so the final time complexity is 0(n^2).
- The space complexity is determined by the extra space used by the algorithm, which is: The dp matrix that requires O(n^2) space.

1. Initializing the dp matrix with the size  $n \times n$  takes  $O(n^2)$  time.

- Thus, the space complexity of the algorithm is  $O(n^2)$ .
- 2. Four variables left, right, up, and down are used but they only add 0(1) space.

Space Complexity