1232. Check If It Is a Straight Line

<u>Math</u>

Problem Description

Geometry

Easy

Array

in the form [x, y]—where x is the x-coordinate and y is the y-coordinate of a point on the XY plane. The task is to determine if all these points lie on a single straight line or not.

The problem presents us with an array called coordinates. Each element within this array is itself an array that represents a point

Intuition

To check if points lie on the same straight line, we need to ensure that the slope between any two points is the same across all points. The slope is a measure of how steep a line is. If pairs of points have different slopes, the points do not lie on a single straight line.

slope is consistent between consecutive points, then all the points are on the same line. In our solution, we take the first two points from coordinates to calculate a reference slope. For computational efficiency and to

To calculate the slope between two points (x1, y1) and (x2, y2), we use the formula slope = (y2 - y1) / (x2 - x1). If the

avoid the potential division by zero error, we check the equality of slopes using a cross-multiplication method. Specifically, instead of directly computing (y2 - y1) / (x2 - x1) == (y - y1) / (x - x1), we check if (x - x1) * (y2 - y1) == (y - y1)

* (x2 - x1) for subsequent points (x, y). If the equality holds for all pairs of points in the coordinates array, the function returns True, which means all points lie on a single straight line. If any pair of points fails the equality test, the function returns False, and we know that not all points are on

The intuition behind this approach is that we're using the properties of slopes in a way that's computationally efficient and avoids possible arithmetic errors when dealing with real numbers.

The algorithm follows a straightforward approach by checking if the slope between any two points is the same across all points. No additional data structures or complex patterns are necessary. The algorithm involves simple arithmetic operations and a for

The algorithm starts by storing the x and y coordinates of the first two points from the coordinates array in x1, y1 and x2, y2. These two points are used to find the reference slope for the line.

return False

straight line.

loop. Here's a step-by-step implementation break down:

The check is made using the following condition:

points do indeed lie on a straight line.

will iterate over just one point: [3, 4].

between point [1, 2] and point [2, 3].

if (4-1)*(3-2)!=(6-2)*(2-1):

if (x - x1) * (y2 - y1) != (y - y1) * (x2 - x1):

Solution Approach

the same line.

coordinates[2:]: loop. Inside the loop, for each point (x, y), the algorithm checks if the cross-product of the differences in coordinates between

The algorithm then iterates over the remaining points in coordinates, starting from the third point, using a for x, y in

- point (x, y) and the first point (x1, y1) equals the cross-product of the differences between the second point (x2, y2)and the first point.
- division by zero, it multiplies the opposite sides and compares them for equality. If the check fails for any point, the function immediately returns False, indicating that the points do not all lie on the same

This expression is derived from the slope equality slope1 = slope2. Instead of dividing the differences, which can cause a

If the loop completes without encountering any point that fails the slope check, the function returns True, signaling that all

- The time complexity of this algorithm is O(n), where n is the number of points, since we have to check the condition for each point once. The space complexity is O(1) since we are using a fixed amount of additional space regardless of the number of
- points. **Example Walkthrough**

Suppose coordinates = [[1, 2], [2, 3], [3, 4]]. We are looking to confirm whether these points fall on a single straight line.

Based on our algorithm, we first take the coordinates of the first two points to calculate the reference slope. So from our

Next, the algorithm will iterate over the remaining points in coordinates. Since we only have three points in this example, it

Now, the algorithm will check if the cross-product of differences with the new point [3, 4], denoted as (x, y), and the first point (x1, y1) equals the cross-product of the differences between the second point (x2, y2) and the first point. This

equation looks like:

which simplifies to:

Solution Implementation

Extract the first 2 points

first point = coordinates[0]

x1, y1 = first_point

x2, y2 = second_point

x, y = point

second_point = coordinates[1]

Coordinates of the first point

Coordinates of the second point

for point in coordinates[2:]:

return False

Check if the subsequent points are in a straight line

if (x - x1) * (y2 - y1) != (y - y1) * (x2 - x1):

if (deltaX1 * deltaY1 != deltaY2 * deltaX2) {

// Function to check if all points lie on a straight line.

bool checkStraightLine(vector<vector<int>>& coordinates) {

int x1 = coordinates[0][0], v1 = coordinates[0][1];

int x2 = coordinates[1][0], y2 = coordinates[1][1];

// we get (x-x1)*(y2-y1) == (y-y1)*(x2-x1)

// All points lie on the same straight line

int x = coordinates[i][0], y = coordinates[i][1];

// Check if the cross product of the vectors is zero

if $((x - x1) * (y2 - y1) != (y - y1) * (x2 - x1)) {$

def checkStraightLine(self, coordinates: List[List[int]]) -> bool:

Check if the subsequent points are in a straight line

// This is a vector algebra way of checking colinearity:

// (x-x1)/(x2-x1) should be equal to (y-y1)/(y2-y1) for all points on the line

// By cross-multiplying to avoid division (and potential division by zero),

// If all the points satisfy the line equation then return true

return false;

#include<vector> // Needed to use std::vector

// Extract the first point (x1,y1)

// Extract the second point (x2,y2)

// Loop through all the remaining points

// Extract the current point (x, y)

for (int i = 2; i < coordinates.size(); ++i) {</pre>

return true;

return true;

using std::vector;

class Solution {

C++

public:

from typing import List

if 3 != 4:

if (3-1)*(3-2)!=(4-2)*(2-1): Simplifying the expressions on each side of the inequality gives:

Let's walk through a small example to illustrate the solution approach:

coordinates, we have x1, y1 = 1, 2 and x2, y2 = 2, 3.

if 2 * 1 != 2 * 1:

In this case, both sides are equal, meaning that the slope between point [1, 2] and point [3, 4] is the same as the slope

Since there are no more points to check, and the equality held true for the third point, the algorithm would return True. This confirms that all the given points in the example line [1, 2], [2, 3], [3, 4] are on the same straight line.

If we had a point that did not satisfy the slope equality, for example [4, 5] replaced by [4, 6], the algorithm would compare:

return False.

This inequality is true, indicating that the point [4, 6] does not lie on the same straight line as the others, so the algorithm would

- **Python**
- class Solution: def checkStraightLine(self, coordinates: List[List[int]]) -> bool:

If they are not equal for any point, the points do not form a straight line

If the loop completes without returning False, all points are in a straight line

Use the cross product to determine if three points are on the same line: # (x - x1)/(x2 - x1) should be equal to (y - y1)/(y2 - y1)# Cross-multiplying to avoid division (to handle the case when $x^2 - x^2$ is 0) we get: # (x - x1) * (y2 - y1) should be equal to (y - y1) * (x2 - x1)

return True

```
Java
class Solution {
    /**
     * Checks if all the given points lie on a straight line.
     * @param coordinates Array of point coordinates on a 2D plane.
     * @return true if all points lie on a single straight line, false otherwise.
    public boolean checkStraightLine(int[][] coordinates) {
        // Coordinates of the first point
        int x1 = coordinates[0][0];
        int y1 = coordinates[0][1];
        // Coordinates of the second point
        int x2 = coordinates[1][0];
        int y2 = coordinates[1][1];
        // Loop over the rest of the points starting from the third one
        for (int i = 2; i < coordinates.length; i++) {</pre>
            // Coordinates of the current point
            int currentX = coordinates[i][0];
            int currentY = coordinates[i][1];
            // Check if the current point lies on the line formed by the first two points
            // This is done by using the cross product which should be zero for collinear points
            int deltaX1 = currentX - x1;
            int deltaY1 = v2 - v1:
            int deltaY2 = currentY - y1;
            int deltaX2 = x2 - x1;
            // If current point does not satisfy the line equation then return false
```

};

```
TypeScript
// Necessary import statement when working with arrays in TypeScript
import { Vector } from 'prelude-ts';
// Function to check if all points lie on a straight line.
function checkStraightLine(coordinates: number[][]): boolean {
    // Extract the first point (x1, y1)
    const x1 = coordinates[0][0];
    const y1 = coordinates[0][1];
    // Extract the second point (x2, y2)
    const x2 = coordinates[1][0];
    const y2 = coordinates[1][1];
    // Loop through all the remaining points
    for (let i = 2; i < coordinates.length; i++) {</pre>
        // Extract the current point (x, y)
        const x = coordinates[i][0];
        const y = coordinates[i][1];
        // Check if the cross product of the vectors is zero
        // This is a vector algebra way of checking collinearity:
        // (x-x1)/(x2-x1) should be equal to (y-y1)/(y2-y1) for all points on the line
        // Bv cross-multiplving to avoid division (and potential division by zero),
        // we get (x-x1) * (y2-y1) == (y-y1) * (x2-x1)
        if ((x - x1) * (y2 - y1) !== (y - y1) * (x2 - x1)) {
            return false; // The current point doesn't lie on the straight line defined by the first two points
    // All points lie on the same straight line
```

return false; // The current point doesn't lie on the straight line defined by the first two points

```
x, y = point
# Use the cross product to determine if three points are on the same line:
\# (x - x1)/(x2 - x1) should be equal to (y - y1)/(y2 - y1)
# Cross-multiplying to avoid division (to handle the case when x^2 - x^2 is 0) we get:
\# (x - x1) * (y2 - y1) should be equal to (y - y1) * (x2 - x1)
# If they are not equal for any point, the points do not form a straight line
if (x - x1) * (y2 - y1) != (y - y1) * (x2 - x1):
    return False
```

If the loop completes without returning False, all points are in a straight line

Time Complexity

return True

Time and Space Complexity

return true;

class Solution:

from typing import List

Extract the first 2 points

first point = coordinates[0]

x1, y1 = first_point

x2, y2 = second point

second_point = coordinates[1]

Coordinates of the first point

Coordinates of the second point

for point in coordinates[2:]:

The time complexity of the function checkStraightLine is O(n), where n is the number of coordinate points in the input list coordinates. This is because the function uses a single loop that iterates through the coordinates starting from the third element, and for each iteration, it performs a constant number of mathematical operations to check if the points lie on the same line. These operations do not depend on the size of the input other than the fact that they iterate once for each element beyond the first two. **Space Complexity**

The space complexity of the function is 0(1). The function uses a fixed amount of extra space to store the variables x1, y1, x2, y2, x, and y. The amount of space used does not scale with the size of the input list, meaning that the space usage is constant.