# 238. Product of Array Except Self

Medium Array **Prefix Sum** 

## **Problem Description**

The problem provided relates to an array transformation challenge. Specifically, you are given an integer array named nums and the task is to generate a new array named answer. For each index i in the new array, answer[i] should be the product of all the elements in nums except for nums[i]. For example, if nums = [1, 2, 3, 4], then answer = [24, 12, 8, 6] because:

- answer[1] should be 1\*3\*4 = 12 • answer[2] should be 1\*2\*4 = 8 • answer[3] should be 1\*2\*3 = 6

• answer[0] should be 2\*3\*4 = 24

- Important constraints to note in this problem include:
- The resultant product of any index will fit within a 32-bit integer, meaning we won't have integer overflow issues for the given range of input.

all numbers to the left of the current index.

to the right of the current index.

- The desired algorithm should run with a time complexity of O(n), which implies a solution should be achievable in a single pass through the array. The division operation cannot be used, which would have been the straightforward approach (multiplying all elements and then
- dividing by each nums[i] for each answer[i]). These constraints guide us to find a more creative solution that involves using multiplication only and finding a way to accumulate
- and distribute the products without dividing.

Intuition The solution to this problem involves accumulating products from both ends of the array. Since we can't use division, we need to

## think about how we can get the product of all elements except for the current one. A smart way to do this is by multiplying two separate products: one accumulated from the beginning of the array up to the element right before the current one, and another

from the end of the array to the element right after the current one. To elaborate: 1. We initialize two variables, left and right, to 1. They will hold the products of elements to the left and right of the current element, respectively.

- 3. We traverse the array from the left; each ans [i] gets the current product on its left (initialized with 1 for the first element as there are no elements to its left), then we update left to include nums[i]. So during this pass, left accumulates the product of
- 4. Next, we traverse the array from the right; we multiply each ans [i] with the current product on its right (again, starting with 1), and after the multiplication, we update right to include nums[i]. During this pass, right accumulates the product of all numbers

2. We create an array ans to store our results, starting with default values (often zeroes).

5. By the end of these two passes, each ans [i] will have been multiplied by both the products of the numbers to its left and right, effectively giving us the product of all other numbers except for nums [i].

This approach cleverly bypasses the need for division and adheres to the time complexity requirement since we are only making two

passes over the array. Solution Approach

The implementation of the solution leverages a single-dimensional array for storage and two variables for the accumulation of products. The algorithm does not use complex data structures or patterns; instead, it builds on the simple principle of accumulation

1. Initialize an array ans to hold our results, filled with zeros, and ensuring that it has the same length as the input array nums.

## 2. Two variables, left and right, are initialized to 1 to hold the running product of the elements to the left and right of the current

element.

and iteration over the input array.

Here's a step-by-step breakdown:

effectively accumulating the product up to the current element.

1 for i, x in enumerate(nums): ans[i] = left left \*= x

3. The first loop iterates over the elements of nums from left to right. For each element at index i, we set ans [i] to the current value

of left since left contains the product of all elements before nums[i]. Then, we update left by multiplying it with nums[i],

4. The second loop iterates over the elements of nums from right to left. We've already captured the products on the left side in the first pass. Now, for each element at index i, we multiply the current value in ans[i] (the left product) with right, which now represents the product of elements after nums[i]. Subsequently, we update right by multiplying it with nums[i], accumulating the product from the end of the array towards the beginning.

By maintaining two pointers that accumulate the product of elements to the left and right of the current index, and by updating our

result array in-place, we manage to get the desired products without ever using division. Moreover, we meet the complexity

constraints by maintaining a linear time complexity O(n) as we traverse the input array exactly twice, no matter its size.

Let's walk through a small example to illustrate the solution approach. Consider the array nums = [2, 3, 4, 5].

ans[0] = left (which is 1 initially).

ans[1] = left (which is 2 now).

ans is updated to [1, 2, 0, 0].

ans[2] = left (which is 6).

ans[3] = left (which is 24).

3. Second Pass (Right to Left):

■ Update left to left \* nums[0], now left = 2.

■ Update left to left \* nums[1], now left = 6.

■ Update left to left \* nums[2], now left = 24.

left is no longer updated since it's the last element.

■ Final ans after the first pass: [1, 2, 6, 24].

The second loop corresponds to the following code snippet:

This first loop is described by the following code snippet:

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Example Walkthrough
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Step-by-Step Walkthrough

1. Initialization:

1 for i in range(n - 1, -1, -1):

ans[i] \*= right

right \*= nums[i]

 Initialize variables left and right with the value 1 to accumulate products from the left and right respectively. 2. First Pass (Left to Right): Iterate over nums from left to right, and calculate the left product excluding the current element.

Initialize the ans array with the same length as nums, in this case, ans = [0, 0, 0, 0] for storing the results.

### ■ ans now becomes [1, 0, 0, 0]. 2. i = 1:

**Iteration details:** 

1. i = 0:

3. i = 2:

So, ans becomes [1, 2, 6, 0]. 4. i = 3:

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    Iterate over nums from right to left, and calculate the right product excluding the current element.

  Iteration details:
    1. i = 3:
         ans [3] is multiplied by right (1 initially), so ans [3] remains 24.
         ■ Update right to right * nums[3], now right = 5.
    2. i = 2:
         ans[2] = ans[2] * right (6 * 5), so ans[2] becomes 30.
         ■ Update right to right * nums[2], now right = 20.
    3. i = 1:
         ans[1] = ans[1] * right (2 * 20), thus ans[1] becomes 40.
         Update right to right * nums[1], which makes right = 60.
    4.i = 0:
         ans[0] = ans[0] * right (1 * 60), resulting in ans[0] being 60.
         right update is not needed since it's the final element.
4. Final Result:

    The resulting ans array after both passes reflects the products of all elements for each position excluding the element itself:
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This walkthrough indicates how the solution approach effectively computes the desired output without the need for division, and it successfully avoids any overflow issues within a 32-bit signed integer range. The time complexity of the solution is O(n), as it passes through the array twice regardless of its size.

# Store the cumulative product in the 'answer' list at the current index 'i'.

# 'right' will represent the cumulative product of elements to the right of the current element.

# Update 'left' to include the product of the current element.

# Update 'right' to include the product of the current element.

# Return the 'answer' list which now contains the products except self.

// Set the current element in the result array to 'leftProduct'

// Multiply the current element in the result array by 'rightProduct'

num\_length = len(nums) # Initialize the answer list with 1's of the same length as 'nums'. answer = [1] \* num\_length # 'left' will represent the cumulative product of elements to the left of the current element.

for i in range(num\_length):

for i in range(num\_length -1, -1, -1):

// Get the length of the input array

// Initialize the answer array with the same length

// Loop through the array from left to right

// Loop through the array from right to left

// Return the final product except self array

vector<int> productExceptSelf(vector<int>& nums) {

// Initialize the left running product as 1

for (int index = 0; index < size; ++index) {</pre>

int size = nums.size(); // Store the size of the input vector

// Calculate the running product from the left for each element

// Backward pass: Calculate the product of all elements to the right of each index

productToRight \*= nums[i]; // Update the productToRight for the previous index

result[i] \*= productToRight; // Multiply with the already stored product to the left

for (let i = length - 1, productToRight = 1;  $i \ge 0$ ; i--) {

return result; // Return the final result array

vector<int> output(size); // Initialize the output vector with the same size as the input

for (int i = length - 1; i >= 0; i--) {

result[i] \*= rightProduct;

rightProduct \*= nums[i];

int length = nums.length;

int leftProduct = 1;

int rightProduct = 1;

int leftProduct = 1;

int[] result = new int[length];

for (int i = 0; i < length; i++) {</pre>

result[i] = leftProduct;

leftProduct \*= nums[i];

answer[i] = left

left \*= nums[i]

answer[i] \*= right

right \*= nums[i]

def productExceptSelf(self, nums: List[int]) -> List[int]:

# Determine the length of the input list 'nums'.

ans = [60, 40, 30, 24].

This matches what we expect as:

 $\blacksquare$  ans [0] = 3 \* 4 \* 5 = 60

 $\blacksquare$  ans [1] = 2 \* 4 \* 5 = 40

 $\blacksquare$  ans [2] = 2 \* 3 \* 5 = 30

 $\blacksquare$  ans [3] = 2 \* 3 \* 4 = 24

**Python Solution** 

class Solution:

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1 from typing import List

left = 1

right = 1

28 return answer 29 Java Solution class Solution { // Method to calculate the product of elements except self public int[] productExceptSelf(int[] nums) {

// Initialize 'leftProduct' to 1, to represent the product of elements to the left of the current index

// Multiply 'leftProduct' by the current element in nums for the next iteration (prefix product)

// Initialize 'rightProduct' to 1, to represent the product of elements to the right of the current index

// Multiply 'rightProduct' by the current element in nums for the next iteration (suffix product)

# Multiply the existing value in 'answer' by the 'right' value which is the product of elements to the right of 'i'.

#### return result; 30 31 32 } 33

C++ Solution

1 class Solution {

public:

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output[index] = leftProduct; // Set the current output element as the product so far from the left
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               leftProduct *= nums[index]; // Update the leftProduct to include the current number
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           // Initialize the right running product as 1
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           int rightProduct = 1;
           // Calculate the running product from the right for each element
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           for (int index = size - 1; index >= 0; --index) {
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               output[index] *= rightProduct; // Multiply the current output element by the product so far from the right
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               rightProduct *= nums[index]; // Update the rightProduct to include the current number
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           return output; // Return the final output vector containing the product of all elements except self for each position
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25 };
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Typescript Solution
   function productExceptSelf(nums: number[]): number[] {
       const length = nums.length; // Total number of elements in input array
       const result: number[] = new Array(length); // Initialize an array to store the result
       // Forward pass: Calculate the product of all elements to the left of each index
       for (let i = 0, productToLeft = 1; i < length; i++) {</pre>
           result[i] = productToLeft; // Set the product (initially 1)
           productToLeft *= nums[i]; // Update the productToLeft for the next index
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Time and Space Complexity
The time complexity of the code is O(n) because there are two separate for-loops that each run through the list of n elements
exactly once. The first loop calculates the product of all elements to the left of the current element, and the second loop calculates
the product of all elements to the right. Since each loop operates independently and sequentially, the procedures do not multiply in
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complexity but rather add, resulting in 2n, which simplifies to 0(n). The space complexity is 0(1), excluding the output array ans. This is because the algorithm uses a constant number of extra variables (left, right, i, x). The space taken by these variables does not scale with the size of the input array nums, hence constant space complexity.