369. Plus One Linked List

Problem Description

Medium Linked List Math

numerical form; it's represented as a <u>linked list</u>, with each node containing a single digit. The head of the linked list contains the most significant digit (MSD), while the tail contains the least significant digit (LSD). For example, the integer 123 would be represented as a linked list 1 -> 2 -> 3. The goal is to add one to this integer and return the resulting <u>linked list</u> following the same MSD to LSD format. The problem must

strings. Intuition

The problem is about incrementing a given non-negative integer by one. However, the integer isn't represented in the traditional

be solved in such a way that the linked list structure is mantained, without converting the entire list to an integer or a series of

To intuitively approach this solution, we need to think about how we generally add one to a number. Starting from the LSD, we add one; if this causes a digit to exceed 9, it rolls over to 0, and we add 1 to the next significant digit, continuing this process until

there are no more rollovers or we've reached the MSD.

need a new node to accommodate the extra digit generated from the rollover (from 999 to 1000, for instance). Here's a step-by-step breakdown of the approach: 1. Use a sentinel (dummy) node at the start of the list to handle cases when a new digit must be added (a new MSD).

one that will potentially increase by one. All digits to the right of it will become zero if there's a rollover. If all digits are 9, we'll

Following this idea in a linked list, we first need to locate the right-most digit that is not a 9. This digit is important because it's the

2. Traverse the linked list to find the rightmost node whose value is not 9. This node is named target. If all digits are 9, target will remain as the dummy node. 3. Increment the target node's value by 1. 4. Set all nodes to the right of target (if any) to 0, as these have been "rolled over".

now contains the new MSD.

- 5. If the dummy node's value is 0, it means no new MSD was added and we can return the original head. Otherwise, return the dummy node as it This approach works due to the linked list's inability to be accessed randomly (we can't go back once we pass a node), making it
- necessary to mark the last non-9 whilst initially traversing the list. This will prevent us from needing a second full traversal.
 - The solution makes use of a simple linked list traversal and manipulation approach. We follow the below steps algorithmically: Initialization:

Create a dummy node (dummy) with 0 as its value, which will precede our original linked list. This helps in scenarios where a carry over might

Using a while loop, we start to traverse the list starting from the head while checking for a condition, head != None. This condition ensures

add an additional digit to the front. dummy next is pointed to the head of the input list. Initialize a variable target to point to the dummy node. This target variable will be used to remember the position in the list where we might later add one. **Traverse the List:**

we stop at the end of the list.

value.

Solution Approach

During traversal, we look for the right-most node that is not a 9. We update target to point to this node each time we encounter a non-9

Increment the Target Value:

• After the traversal, we know the target node is the right-most node that isn't 9. We increment target val by 1. **Handle Rollover:** Move target to its next node. Continue another loop to set all the following values to 0, turning all 9s that come after the incremented value into 0s (as they have been

 If the dummy node's value is still 0, it implies the increment did not add a new digit, so we return dummy next as the head of the updated list. ∘ If the dummy node's value is 1, it implies a new digit has been added due to a carry (for example, from 999 to 1000), so we return the dummy

rolled over).

Return the Modified List:

node itself as it is now the head of the updated list.

In terms of data structures, we simply use the given linked list nodes and a single additional node for the dummy. The space complexity of the algorithm is O(1) since we are modifying the input linked list in place and only using a fixed number of extra

used to simplify operations at the head of the list, allowing us to handle edge cases more gracefully.

Here's a step-by-step walkthrough of the solution approach with this example:

Move to the final node 9. Keep target at 2 as the final node is indeed a 9.

This results in a linked list that represents the initial number incremented by 1.

variables. The time complexity of the algorithm is O(n), where n is the number of nodes in the linked list, since we are potentially traversing the entire list.

Example Walkthrough

Initialization:

Increment the Target Value:

Return the Modified List:

def __init__(self, val=0, next_node=None):

Handle Rollover:

Let's consider a linked list that represents the integer 129: 1 -> 2 -> 9

The patterns used in the solution include the two-pointer technique as well as the sentinel node pattern. The two-pointer

technique, in this case, involves the target and head pointers to traverse and modify the input list. The sentinel node pattern is

point to dummy. **Traverse the List:** Start traversing the list: Move to 1. Since 1 is not 9, update target to this node. Move to 2. Since 2 is not 9, update target to this node.

○ target is pointing to the node with value 2. Increment this node's value by 1. The list now temporarily looks like 0 -> 1 -> 3 -> 9.

Check the dummy node. It still has the value 0, so no new MSD has been added. Thus, the head of the updated list is dummy next.

The example illustrates the given steps, showing how to navigate and modify the list without turning it into another data type.

∘ Set all nodes to the right of target to 0. This is just the final node in this example. Now the list looks like 0 → 1 → 3 → 0.

○ Create a dummy node with a value 0 and connect it to the head of the list. The list now looks like 0 -> 1 -> 2 -> 9. Initialize the target to

○ The final resulting list is 1 → 3 → 0, which represents the integer 130.

Python

class ListNode:

self.val = val

self.next = next node

non_nine_node = dummy

if head.val != 9:

head = head.next

non_nine_node.val += 1

current = non_nine_node.next

non_nine_node = head

Increase the value of the last non-nine node by 1

Set all the nodes after the last non-nine node to '0'

current = current.next; // Move to the next node

return dummy.val == 1 ? dummy : dummy.next;

* Definition for singly-linked list.

ListNode(): val(0), next(nullptr) {}

ListNode* plusOne(ListNode* head) {

dummyHead->next = head;

while (head != nullptr) {

head = head->next;

++nonNineNode->val;

if (head->val != 9) {

ListNode(int x) : val(x), next(nullptr) {}

ListNode* dummyHead = new ListNode(0);

ListNode* nonNineNode = dummyHead;

nonNineNode = head;

nonNineNode = nonNineNode->next;

while (nonNineNode != nullptr) {

nonNineNode = nonNineNode->next;

nonNineNode->val = 0;

// Definition for singly-linked list node.

// Function to create a new ListNode.

return { val: val, next: next };

let dummyHead = createListNode(0);

let nonNineNode: ListNode = dummyHead;

ListNode(int x, ListNode *next) : val(x), next(next) {}

// Function to add one to a number represented as a linked list.

// Increment the value of the rightmost non-nine node.

// Otherwise, we return the original head of the list.

return dummyHead->val == 1 ? dummyHead : dummyHead->next;

function createListNode(val: number, next: ListNode | null = null): ListNode {

// Create a dummy head in case we need to add a new head (e.g., from 999 + 1 = 1000).

// 'nonNineNode' will point to the rightmost node that is not a 9, or to the dummy head if all are 9s.

// Move to the next node, which is the first in the sequence of 9s after the incremented digit.

// If the dummy head's value was changed, it means we added a new digit at the start, so return the dummy head.

// Reset all the following 9s to 0s because we have added one to the preceding digit.

// Function to add one to a number represented as a linked list.

function plusOne(head: ListNode | null): ListNode | null {

// Increment the value of the rightmost non-nine node.

// Otherwise, return the original head of the list.

return dummyHead.val === 1 ? dummyHead : dummyHead.next;

Create a dummy node before the head to handle edge cases easily

Traverse the linked list to find the last node that is not a '9'

Make 'current' point to the node right after the incremented node

This variable will keep track of the last node before the sequence of 9's

// Traverse the list to find the rightmost node that is not a 9.

// Move to the next node, which is the first in the sequence of 9's.

* struct ListNode {

class Solution {

int val;

ListNode *next;

// Check if dummy node has the incremented value (meaning carry was there)

// Create a dummy head in case we need to add a new head (e.g., 999 + 1 = 1000).

// 'nonNineNode' will point to the rightmost node that is not a 9 or to the dummy head.

// Reset all the following 9's to 0's because we've already added one to the preceding digit.

// If the dummy head's value was changed, it means we added a new digit, so we return the dummy head.

// If dummy val is 1, return the dummy node, else return the original list without the dummy

return dummy if dummy val != 0 else dummy next

while head:

Solution Implementation

class Solution: def plusOne(self, head: ListNode) -> ListNode: # Create a dummy node before the head to handle edge cases easily dummy = ListNode(0) dummy.next = head

This variable will keep track of the last node before the sequence of 9's

Traverse the linked list to find the last node that is not a '9'

Make 'current' point to the node right after the incremented node

If the dummy node's value is '0', it means the linked list doesn't have leading zeros

If the dummy node's value is not '0', the list starts with a '1' followed by zeros

while current: current.val = 0 current = current.next

Java

```
/**
* Definition for singly-linked list.
public class ListNode {
   int val; // Value of the node
   ListNode next; // Reference to the next node
   ListNode() {}
   ListNode(int val) { this.val = val; }
   ListNode(int val, ListNode next) {
       this.val = val;
       this.next = next;
class Solution {
    public ListNode plusOne(ListNode head) {
       // Create a dummy node which initially points to the head of the list
       ListNode dummy = new ListNode(0);
       dummy.next = head; // Connect the dummy node to the head of the list
       ListNode notNine = dummy; // This will point to the last node not equal to 9
       // Traverse the list to find the rightmost not-nine node
       while (head != null) {
           if (head.val != 9) {
               notNine = head; // Update the rightmost not-nine node
           head = head.next; // Move to the next node
       // Increment the value of the rightmost not-nine node
       notNine.val += 1;
        // Set all the nodes right to the increased node to 0
       ListNode current = notNine.next;
       while (current != null) {
            current.val = 0;
```

};

TypeScript

interface ListNode {

next: ListNode | null;

dummyHead.next = head;

head = head.next;

nonNineNode.val++;

nonNineNode = nonNineNode.next;

while (nonNineNode !== null) {

nonNineNode = nonNineNode.next;

def __init__(self, val=0, next_node=None):

def plusOne(self, head: ListNode) -> ListNode:

non_nine_node = head

Increase the value of the last non-nine node by 1

Set all the nodes after the last non-nine node to '0'

nonNineNode.val = 0;

self.val = val

self.next = next_node

dummy = ListNode(0)

non_nine_node = dummy

if head.val != 9:

head = head.next

non_nine_node.val += 1

current = non_nine_node.next

dummy.next = head

while head:

val: number;

C++

/**

* };

public:

// Traverse the list to find the rightmost node that is not a 9. while (head !== null) { if (head.val !== 9) { nonNineNode = head;

class ListNode:

class Solution:

while current: current.val = 0 current = current.next # If the dummy node's value is '0', it means the linked list doesn't have leading zeros # If the dummy node's value is not '0', the list starts with a '1' followed by zeros return dummy if dummy val != 0 else dummy next

Time and Space Complexity

Time Complexity

before a sequence of '9's that needs to be incremented. In the worst case, this traversal looks at every node exactly once, resulting in a time complexity of O(n), where n is the length of the linked list. The second traversal occurs after the increment and only traverses the portion of the list that consists of '9's, turning them into '0's. In the worst case, this could again traverse the entire list (in the case that all nodes are '9's except the first), giving this traversal a time complexity of O(n) as well.

notation and the list is only traversed a constant number of times (specifically, twice).

Space Complexity

The space complexity of the algorithm is dependent on the additional variables defined in the method and not on the input size. The method uses a few constant extra space for pointers (dummy, target, and head), and does not create any additional data structures that grow with the input size. Therefore, the space complexity is 0(1). The dummy node created does not count as extra space since it's only a fixed-size pointer to the existing list (and not extra nodes being created).

The given Python code traverses the linked list twice. In the first traversal, it looks through all the nodes to find the last node

The total worst-case time complexity, combining both traversals, remains O(n) because the constants do not matter for Big O