2679. Sum in a Matrix Medium Array Simulation) Heap (Priority Queue) Matrix Sorting **Leetcode Link**

Problem Description

In this problem, we are provided with a 0-indexed 2D integer array nums, which represents a matrix. The goal is to calculate a score based on specific operations performed on this matrix. We start with a score of 0, and we repeatedly perform the following two-part operation until the matrix is empty:

- 1. From each row in the matrix, select and remove the largest number. If any row has multiple largest numbers (i.e., a tie), any of them can be selected.
- The required output is the final score once there are no more numbers left in the matrix.

2. After removing these numbers from each row, identify the largest number among them and add that number to the score.

It's important to keep track of the largest numbers being selected during each operation and ensuring that the correct value (the

maximum from these selections) is added appropriately to the score.

Intuition

largest number from each row and find the overall maximum to add to the score, sorting the rows can simplify the problem. By

The intuition behind the solution comes from the way the operations on the matrix are defined. Since we always need to select the

sorting each row, we guarantee that the largest number in each row will be at the end. This operation effectively "flips" the matrix so that each row becomes a column. Then, the algorithm iterates through the new "rows" (original columns) and computes the maximum value. This value is the one that should be added to the score since it represents the

largest value that would be selected from the original rows during an iteration. By continuing to sum these maxima for all "new rows," we accumulate the total score. The benefit of this approach is that the whole process takes place with a complexity close to that of the sorting operation itself, which is efficient compared to a naive approach

that might involve multiple iterations for each step. The use of Python's built-in functions like sort(), max(), and map() allows for a concise and efficient implementation of this intuition.

Solution Approach

through each part of the implementation:

for row in nums:

1. Sort each row of the nums matrix. In Python, this can be achieved using the sort() method, which sorts the elements of a list in ascending order. By sorting each row, we ensure that the largest number in each row will be at the end.

The implementation of the solution follows the steps that correspond to its intuitive approach described previously. Let's walk

row.sort() 2. The next step is to find the largest number that was removed from each row and add that to the score. Since the rows are

sorted, we can use the fact that in Python, the max() function can be applied to a list of lists by using the zip(*iterables)

to the sort) become the elements of the new "rows."

This is done with the following line of code:

o This "transposition" and finding the maximum occurs in the following line of code: 1 return sum(map(max, zip(*nums)))

The map() function applies max to each new row (actually a column of the original matrix) and finds the maximum element,

function. The zip(*nums) effectively transposes the matrix, so the last elements of each original row (which are the largest due

which corresponds to the maximum number we removed from the original rows.

a straightforward manner, and sum() to accumulate these values into the final score.

```
    Finally, the sum() function takes the iterable produced by map() (which consists of the largest numbers from each operation)

 and sums them up, thus calculating the final score.
```

- The combination of sort(), max(), zip(), and map() provides an elegant and efficient solution. It uses sorting to rearrange the elements, a matrix transpose operation to work across rows as if they were columns, the max() function to grab the largest values in
- **Example Walkthrough**

Consider the following small matrix for our example: 1 nums = [[1, 2, 9],

Let's walk through the steps of the solution approach using this matrix:

[7, 8, 3]

Before sorting:

1. Sort each row of the nums matrix in ascending order:

```
2 [4, 5, 6],
3 [1, 2, 9],
        [7, 8, 3]
After sorting each row:
```

[4, 5, 6],

[4, 1, 3],

[5, 2, 7],

each row due to sorting).

[1, 2, 9], [3, 7, 8]

The max of the third transposed row is 9

def matrix_sum(self, nums: List[List[int]]) -> int:

16 # Example of using the Solution class to find matrix sum

sum += maxInColumn;

return sum;

[6, 9, 8]

3. For each new row (originally a column), we select the maximum value (which, in this case, would be the originally last item of

2. Using zip(*nums), we transpose the matrix so we can easily access the largest numbers (the last elements of each row):

Largest numbers, which are the maxima of the transposed rows:

Transposed and zipped matrix (effectively "flip" so that each row is now a column):

As per the first step, rows are sorted, and now the largest number in each row is at the end.

```
    The max of the first transposed row is 4

    The max of the second transposed row is 7
```

Python Solution

class Solution:

from typing import List

- 4. Finally, we sum up these maxima to get the final score, which is 4 + 7 + 9 = 20. The sum of these maxima gives us the solution to the problem, which is the final score. In this example, the score is 20.
 - # Sort each row of the matrix in ascending order for row in nums: row.sort() # Transpose the matrix to access columns as rows

```
transposed_matrix = zip(*nums)
10
11
           # Find the max element in each column (since rows are sorted, it is the last element in each row after transposition)
           # And compute the sum of these maximum values
14
            return sum(map(max, transposed_matrix))
```

[1, 2, 3],

[4, 5, 6],

[7, 8, 9]

22 # sol = Solution()

17 # matrix = [

21 #]

21

24

25

26

27

29

31

33

32 };

Typescript Solution

28 }

```
# print(sol.matrix_sum(matrix)) # Output: 18
24
Java Solution
1 class Solution {
       // Method to calculate the sum of the maximum elements in each column of the matrix.
       public int matrixSum(int[][] matrix) {
           // Sort each row of the matrix to ensure elements are in non-decreasing order.
           for (int[] row : matrix) {
               Arrays.sort(row);
           // Initialize the sum that will eventually store the answer.
           int sum = 0;
11
12
           // Traverse each column of the sorted matrix to find the maximum element.
           for (int col = 0; col < matrix[0].length; ++col) {</pre>
13
               int maxInColumn = 0; // Variable to keep track of the max element in the current column.
14
15
               // Iterate through each row to find the maximum element for the current column.
16
               for (int[] row : matrix) {
17
                   maxInColumn = Math.max(maxInColumn, row[col]); // Update the max for the column if a larger element is found.
18
19
20
```

// After finding the maximum element in the column, add it to the sum.

// Return the final sum, which is the total of all maximum elements in each column.

```
C++ Solution
1 #include <vector>
2 #include <algorithm> // Include algorithm library for sort and max functions
   class Solution {
   public:
       // Function that calculates the sum of maximum elements in each column after sorting each row
       int matrixSum(vector<vector<int>>& matrix) {
           // Sort each row in ascending order
           for (auto& row : matrix) {
               sort(row.begin(), row.end());
11
12
           int totalSum = 0; // Initialize sum of max elements to 0
13
14
           // Loop through each column
15
           for (int col = 0; col < matrix[0].size(); ++col) {</pre>
16
               int maxElem = 0; // Variable to store the max element in the current column
18
               // Loop through each row to find the max element in the current column
19
               for (auto& row : matrix) {
20
                   // Update maxElem if we find a larger element in current column
21
                   maxElem = max(maxElem, row[col]);
23
24
25
               // Add the max element of the current column to the total sum
26
               totalSum += maxElem;
29
           // Return the total sum of max elements of all columns
30
           return totalSum;
```

```
function matrixSum(matrix: number[][]): number {
       // Sort each row in the matrix to have numbers in ascending order
       for (const row of matrix) {
           row.sort((a, b) => a - b);
       let totalSum = 0; // Initialize a variable to store the sum of maximums from each column
       // Iterate over the columns of the matrix
       for (let columnIndex = 0; columnIndex < matrix[0].length; ++columnIndex) {</pre>
           let maxInColumn = 0; // Initialize a variable to store the maximum value in the current column
           // Iterate over each row to find the maximum value in the current column
13
           for (const row of matrix) {
14
               maxInColumn = Math.max(maxInColumn, row[columnIndex]);
15
16
           // Add the maximum value of the current column to the total sum
           totalSum += maxInColumn;
19
20
21
22
       return totalSum; // Return the computed sum
23 }
Time and Space Complexity
Time Complexity:
```

each column after transposition. 1. Sorting: Each row is sorted individually using row.sort(), which typically uses Tim Sort, an algorithm with a worst-case time

complexity of O(n log n) for sorting a list of n elements. If m represents the number of rows and n represents the number of

24

columns in nums, then the sorting step has a time complexity of $0(m * n \log n)$. 2. Finding max and summing: The zip(*nums) function is used to transpose the matrix, and map(max, ...) is used to find the maximum element in each column. Since there are n columns, and finding the max takes 0(m) time for each column, this step has a time complexity of 0(m * n). The final summing of these values is done in 0(n).

The time complexity of the matrixSum method involves two steps: sorting the rows of the matrix and finding the maximum element of

because 0(m * n log n) is the dominating term. **Space Complexity:**

Combining the two steps, the overall time complexity is $0(m * n \log n) + 0(m * n) + 0(n)$, which simplifies to $0(m * n \log n)$

1. Sorting: Sorting is done in-place for each row, so no additional space is proportional to the size of the input matrix is used.

- Therefore, it does not increase the asymptotic space complexity. 2. Transposing and finding max: The zip function returns an iterator of tuples, which, when combined with map, doesn't create a
- list of the entire transposed matrix but rather creates one tuple at a time. Thus, the space required for this operation is O(n) for storing the maximums of each column.

Thus, the space complexity of the matrixSum method is O(n).