938. Range Sum of BST **Binary Search Tree Depth-First Search** Tree Easy

Problem Description

calculate the sum of all the node values in the BST that fall within the inclusive range [low, high]. This means that if a node's value is equal to or greater than low and equal to or less than high, it should be included in our sum. The binary search property of the tree, where left child nodes are less than the parent node and right child nodes are greater, can be used to optimize our search for the range.

The problem provides us with the root node of a binary search tree (BST) and two integer values, low and high. It asks us to

Binary Tree

also be less than low.

Intuition

unnecessary traversal. The steps of the approach are: 1. If the current node is null (we've reached a leaf's child), we can stop traversing this path.

The intuition behind the solution approach is to perform a depth-first traversal of the BST while leveraging the BST property to avoid

- 2. If the current node's value falls within [low, high], we add it to the sum and continue to search both the left and right subtrees as there may be more nodes within the range.
- 3. If the current node's value is less than low, we only need to traverse the right subtree because all values in the left subtree will
- 4. If the current node's value is greater than high, we only need to traverse the left subtree, as all values in the right subtree will be greater than high.
- Using these rules, the search efficiently skips parts of the tree that don't contribute to the range sum, which optimizes our algorithm significantly compared to a naive approach that checks every node.

Solution Approach

The implementation of the solution involves the use of a recursive helper function called search, nested within the main function

rangeSumBST. This is a common design pattern in recursive solutions, allowing the use of helper functions with additional parameters without changing the main function's signature. The algorithm uses this recursive function to perform a modified in-order traversal of

the binary search tree. Here's a breakdown of how the algorithm works, with references to the data structures and patterns used: 1. Initialization: A variable self.ans is initialized to 0. This will accumulate the sum of the node values that are within the range [low, high]. 2. Recursive Function (search): A nested function search is defined, which takes the current node as its parameter. The use of

- recursion is key here, enabling the function to traverse the tree depth-first. 3. Base Case: At the beginning of the search function, there is a check to see if the current node is None. If it is, the function returns
- immediately. This check acts as the base case of the recursion, terminating the traversal at leaf nodes.
- o If the current node's value is within the range [low, high] (inclusive), the value is added to self.ans. As this node is within the range, there might be other nodes within the range both to the left and right, so the function recursively calls itself on

o If the current node's value is less than low, the function calls itself recursively on node. right as all left child nodes of the

current node are guaranteed to be out of the range. If the current node's value is greater than high, the function calls itself recursively on node. left as all right child nodes of

5. **BST Property Utilization**:

both node.left and node.right.

4. Range Check:

- the current node are guaranteed to be out of the range. 6. Starting the Traversal: The recursive search function is first called on the root node to start the depth-first traversal. 7. Returning the Answer: Finally, after the recursive calls have completed, self. ans contains the sum of the values within the
- range, and this value is returned by the rangeSumBST function. The use of a BST's intrinsic properties allows the algorithm to avoid inspecting every single node in the tree, thereby significantly

improving efficiency, especially in cases where the range bounds are far from the minimum and maximum values in the tree. The

space complexity is proportional to the height of the tree (O(H)) due to the recursion stack, and the time complexity is O(N) in the

worst case when the tree is unbalanced, but it could be much less if the tree is balanced and the search prunes branches effectively.

Example Walkthrough Let's illustrate the solution approach using a small example. Consider the following binary search tree (BST) and the range [low, high] = [10, 22]:

Now let's walk through how the solution would process this tree:

3. The search function is now called with node 10. Since 10 is also within the range, we add it to self.ans (15 + 10 = 25), and call search on both of its children (5 and 13).

and the search function will be called on both its left child (10) and right child (20).

1. The rangeSumBST function initializes selflans to 0. This will hold the sum of values within the given range.

we do not call search on its left subtree, and there is no right subtree to explore. 5. The search function is next called with node 13, which falls within the range. Therefore, 13 is added to self.ans (25 + 13 = 38),

and since it has a right child (11) that could be within the range, search is called on node 11.

6. Node 11 is within the range, so its value is added to self.ans (38 + 11 = 49). Node 11 has no children, so no further calls are made here.

7. Back to the root, the search function is called with the node 20. This node's value is within the range and therefore is sum-up to

2. The search function is called with the root node (15). Since 15 is within the range [10, 22], it is added to self. ans (0 + 15 = 15),

4. When called with node 5, the function does not add its value to self. ans since 5 is outside the range. As 5 is less than low (10),

8. Node 25 is greater than high (22), so we don't add it to self. ans. Also, since its value is greater than high, we do not explore its right subtree (not existing in this case), and because it has no left child, the traversal of this path ends.

self.ans (49 + 20 = 69). Since there is a right child (25) and it is potentially within the range, we call search on it.

With all paths explored, the final sum calculated is self.ans = 69, and the rangeSumBST returns this sum as the answer.

Helper function to perform DFS and accumulate node values within the range [low, high]

If the current node's value is less than the low value of the range

then only search to the right as all left values will also be less

If the current node's value is within the range [low, high], add it to the total sum

This example demonstrates how the algorithm effectively uses the BST properties to skip over irrelevant parts of the tree (for

instance, not exploring left subtrees of nodes with values less than low, and right subtrees of nodes with values greater than high), thus optimizing the search for efficiency.

1 # Definition for a binary tree node 2 class TreeNode: def __init__(self, val=0, left=None, right=None):

if low <= node.val <= high:</pre> 17 self.total_sum += node.val 18 # Continue searching to the left and right as there may still be values 19 20 # within the range [low, high] dfs(node.left)

class Solution:

10

11

13

14

15

16

22

23

24

25

26

Python Solution

self.val = val

def dfs(node):

self.left = left

self.right = right

if not node:

return

dfs(node.right)

dfs(node.right)

elif node.val > high:

elif node.val < low:</pre>

def rangeSumBST(self, root: TreeNode, low: int, high: int) -> int:

If the current node is None, return and do nothing

```
28
                   # If the current node's value is greater than the high value of the range
29
                   # then only search to the left as all right values will also be greater
                   dfs(node.left)
30
31
32
           # Initialize the total_sum as 0 before starting the DFS
33
           self.total_sum = 0
34
           # Start the depth-first search from the root node
35
           dfs(root)
36
           # After DFS, return the total sum of values within [low, high]
37
           return self.total_sum
38
Java Solution
   // Class containing the solution method to calculate the sum of values of all nodes within a range of a BST
  class Solution {
       // This method computes the sum of values falling within the [low, high] range in a BST
       public int rangeSumBST(TreeNode root, int low, int high) {
           // If the current node is null, return 0 since there are no values to add
           if (root == null) {
               return 0;
           // If the value of the current node is within the [low, high] range,
10
           // include its value in the sum, and continue searching in both left and right subtrees
           if (low <= root.val && root.val <= high) {</pre>
13
               return root.val + rangeSumBST(root.left, low, high) + rangeSumBST(root.right, low, high);
14
15
           // If the value of the current node is less than the lower bound,
           // skip the left subtree because all values there will be out of range,
16
           // and only continue searching in the right subtree
           else if (root.val < low) {</pre>
18
               return rangeSumBST(root.right, low, high);
19
20
21
           // If the value of the current node is greater than the upper bound,
22
           // skip the right subtree because all values there will be out of range,
           // and only continue searching in the left subtree
24
           else {
25
               return rangeSumBST(root.left, low, high);
26
```

44 // Constructor for creating a new node with a given value and references to left and right children 45 TreeNode(int val, TreeNode left, TreeNode right) { this.val = val; 46 47

class TreeNode {

int val;

TreeNode() {}

TreeNode(int val) {

this.val = val;

// Definition for a binary tree node.

// The integer value of the node

TreeNode left; // Reference to the left child

TreeNode right; // Reference to the right child

// Constructor for creating a new node without children

// Constructor for creating a new node with a given value

27

29

32

33

34

35

36

37

38

39

40

41

42

43

28 }

```
this.left = left;
           this.right = right;
48
49
50 }
51
C++ Solution
 1 /**
    * Definition for a binary tree node.
    * struct TreeNode {
          int val;
          TreeNode *left;
          TreeNode *right;
          TreeNode() : val(0), left(nullptr), right(nullptr) {}
          TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
          TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}
    * };
10
11
   */
12 class Solution {
   public:
14
       /**
15
        * Computes the sum of values of all nodes with a value in the range [low, high].
        * Utilizes the BST property to prune branches that cannot contain values in the range.
16
17
18
        * @param root Pointer to the root of the binary search tree (BST).
19
        * @param low The lower bound of the range (inclusive).
20
        * @param high The upper bound of the range (inclusive).
21
        * @return The sum of values in the specified range.
22
23
       int rangeSumBST(TreeNode* root, int low, int high) {
24
           if (root == nullptr) {
25
               // Base case: if the current node is null, return sum of 0
26
               return 0;
27
28
29
           // Check if the current node's value is within the range [low, high]
           if (low <= root->val && root->val <= high) {</pre>
30
               // If it is in the range, include the node's value in the sum,
31
32
               // and continue to check both left and right children
33
               return root->val + rangeSumBST(root->left, low, high) + rangeSumBST(root->right, low, high);
34
           } else if (root->val < low) {</pre>
35
               // If current node's value is less than low, no need to check
36
               // the left subtree as all values will be out of range; proceed
               // to check the right child
37
               return rangeSumBST(root->right, low, high);
39
           } else {
               // If current node's value is greater than high, no need to check
40
               // the right subtree as all values will be out of range; proceed
               // to check the left child
               return rangeSumBST(root->left, low, high);
43
44
45
46 };
47
Typescript Solution
```

```
11
    * @param root The root of the binary search tree (BST).
    * @param low The lower bound of the range (inclusive).
    * @param high The upper bound of the range (inclusive).
    * @returns The sum of values within the specified range.
16
    */
   function rangeSumBST(root: TreeNode | null, low: number, high: number): number {
     if (!root) {
       // Base case: if the current node is null, return a sum of 0.
       return 0;
21
22
     // Check if the current node's value is within the range [low, high].
     if (root.val >= low && root.val <= high) {</pre>
       // The node's value falls within the range, so add it to the sum,
       // and continue to check both the left and right subtrees.
       return root.val + rangeSumBST(root.left, low, high) + rangeSumBST(root.right, low, high);
27
      } else if (root.val < low) {</pre>
28
       // The current node's value is less than the low end of the range,
29
       // so there is no need to check the left subtree (all values will be too small).
30
       // Instead, traverse the right subtree only.
       return rangeSumBST(root.right, low, high);
32
33
      } else {
       // The current node's value is greater than the high end of the range,
34
       // so there is no need to check the right subtree (all values will be too large).
35
       // Instead, traverse the left subtree only.
36
       return rangeSumBST(root.left, low, high);
37
38
39 }
40
Time and Space Complexity
The given Python code defines a function rangeSumBST that calculates the sum of values of all nodes with a value in the range [low,
high] within a binary search tree (BST). The function implements a recursive depth-first search strategy.
```

// Typescript representation of a binary search tree node

* Computes the sum of values of all nodes with a value in the range [low, high].

* Utilizes the Binary Search Tree (BST) property to prune branches that cannot contain values in the range.

2 type TreeNode = {

val: number;

left: TreeNode | null;

right: TreeNode | null;

Time Complexity

The time complexity of the function is O(N), where N is the number of nodes in the binary search tree. This is because, in the worstcase scenario, the function may have to visit every node in the tree. However, due to the properties of a binary search tree and the pruning of branches that do not fall within the [low, high] range, the average case will likely be more efficient than this. Nonetheless, the upper bound worst-case remains O(N). **Space Complexity**

The space complexity of the recursion is O(H), where H is the height of the tree. This complexity arises from the call stack that holds the recursive calls during the search process. In the worst-case scenario of a skewed binary search tree where the tree behaves like a linked list, the height of the tree could be N, making the space complexity O(N). For a balanced tree, the height of the tree would be log(N), leading to a space complexity of O(log(N)). It should be noted that this does not take into account the space used to store the binary search tree itself, only the additional space used by the recursion call stack.