

Problem Description

Given a string s, the task is to calculate the total number of distinct non-empty subsequences that can be formed from the characters of the string. Note that a subsequence maintains the original order of characters but does not necessarily include all characters. Importantly, if the solution is a very large number, it should be returned modulo 10^9 + 7 to keep the number within manageable bounds. This modular operation ensures that we deal with smaller numbers that are more practical for computation and comparison.

Intuition

them down into simpler subproblems. The key insight is to build up the number of distinct subsequences as we iterate through each character of the given string. We maintain an array dp of size 26 (to account for each letter of the alphabet) which keeps track of the contribution of each

The intuition for solving this problem lies in dynamic programming - a method used for solving complex problems by breaking

character towards the number of distinct subsequences so far. The variable ans stores the total count of distinct subsequences at any given point. As we traverse the string:

• We calculate the index i corresponding to the character c (by finding the difference between the ASCII value of c and that of a).

Solution Approach

- The variable add is set to the difference between the current total number of subsequences ans and the old count of subsequences ending with
- the character c (dp[i]). We add 1 to this because a new subsequence consisting of just the character c can also be formed.
- The ans is updated to include the new subsequences introduced by including the character c. The new ans is also taken modulo 10^9 + 7 to handle the large numbers.
- The count of subsequences ending with the character c (dp[i]) is incremented by add to reflect the updated state. This approach ensures that each character's contribution is accounted for exactly once, and by the end of the iteration, ans
- contains the count of all possible distinct subsequences modulo 10^9 + 7.

The implementation of the solution is fairly straightforward once we've understood the intuition behind it. This problem employs dynamic programming and a single array to keep track of the contributing counts. Here's the breakdown of the approach:

• We use a modulus mod set to 10**9 + 7 to ensure we manage the large numbers effectively by returning the number of subsequences modulo this value.

• The data structure dp is an array initialized to size 26 (representing the English alphabet) with all zeroes. This array will store the count of subsequences that end with a particular character.

Iterate Over the String:

Initialize the Modulus and DP Array:

- For each character c in the string s, we do the following steps:
- **Determine the Index for c:** ∘ We calculate an index i by taking the ASCII value of the character c, subtracting the ASCII value of 'a' from it (ord(c) - ord('a')). This
- gives us a unique index from 0 to 25 for each lowercase letter of the alphabet. **Calculate the Additive Contribution:**

Update the DP Array:

for the subsequence consisting solely of the new character c. **Update the Total Count of Subsequences:**

Compute add, which will determine how much the current character c will contribute to the new subsequences count. It is determined by

the current total of distinct subsequences ans minus the previous count stored in dp[i] for that character c. We add one to add to account

Update ans by adding the new contribution from the character c. Applying modulo mod here ensures we handle overflow and large numbers.

o Increase the count in dp[i] by the value of add. This means that any subsequences that now end with the current character c include the

Initialize the Modulus and DP Array:

(initially 0) - dp[0] + 1 = 0 - 0 + 1 = 1.

Determine the Index for 'a': The index is still 0.

old subsequences plus any new subsequences formed due to adding c.

- Using this method, we build up the solution incrementally, considering the influence of each character on the subsequences. The reason we have to subtract the old count of subsequences for the character c before adding it again (after increasing with add) is
- to ensure that we do not double-count subsequences already accounted for by previous appearances of c. The complexity of this solution is O(n), where n is the length of the string since we go through every character of the string once, performing O(1) operations for each.

Example Walkthrough To illustrate the solution approach, let's go through a small example using the string "aba".

We set mod to 10^9 + 7. Our dp array, which has 26 elements for each letter of the English alphabet, is initialized to zeroes.

We begin iterating through the string "aba" character by character.

Iterate Over the String:

First Character - 'a':

Determine the Index for 'a': We calculate the index for 'a' as ∅ (since 'a' - 'a' = ∅).

- Update the Total Count of Subsequences: We set ans = ans + add = 0 + 1 = 1 (the subsequences are now "" and "a"). Update the DP Array: We update dp[0] to dp[0] + add = 0 + 1 = 1.
 - **Second Character 'b':**
 - Determine the Index for 'b': The index for 'b' is 1 ('b' 'a' = 1). ○ Calculate the Additive Contribution: The current total count of distinct subsequences, ans, is 1. add = ans - dp[1] + 1 = 1 - 0 + 1 = 2 (which corresponds to new subsequences "b" and "ab").

○ Update the Total Count of Subsequences: The new ans will be ans + add = 3 + 3 = 6 (the subsequences now are "", "a", "b", "ab", "ba",

• Calculate the Additive Contribution: Since this is the first character, and there are no previous subsequences, we calculate add = ans

• Update the DP Array: We update dp[1] to dp[1] + add = 0 + 2 = 2. Third Character - 'a' (again):

○ Update the Total Count of Subsequences: Now ans = ans + add = 1 + 2 = 3 (the subsequences are "", "a", "b", and "ab").

Calculate the Additive Contribution: We know ans is 3, and since we've encountered 'a' before, we subtract its previous contribution from

ans and add 1: add = ans -dp[0] + 1 = 3 - 1 + 1 = 3 (these are new subsequences: "a", "ba", and "aba").

"aa", and "aba"; note that we don't count subsequences like "aa" as distinct since the order must be maintained).

At the end of this process, the final answer for the total count of distinct non-empty subsequences is 6. However, if ans were larger, we would apply the modulo operation to ensure we obtain a result within the bounded range.

Python

class Solution:

programming and efficient arithmetic operations, handling each character's contribution exactly once. Solution Implementation

def distinctSubseqII(self, s: str) -> int:

 $last_count = [0] * 26$

total_count = 0

for char in s:

Define the modulo value to handle large numbers

Initialize the total count of distinct subsequences

added_subseq = total_count - last_count[index] + 1

Get the index of the current character in the alphabet (0-25)

Calculate how many new subsequences are added by this character:

It is total_count (all previous subsequences) minus last_count[index]

Iterate over each character in the string

index = ord(char) - ord('a')

 \circ Update the DP Array: We set dp[0] to dp[0] + add = 1 + 3 = 4.

MOD = 10**9 + 7# Initialize an array to keep track of the last count of subsequences # ending with each letter of the alphabet

(which we have already counted with the current character) plus 1 for the character itself

This walkthrough demonstrates how the algorithm incrementally computes the count of distinct subsequences using dynamic

```
# Update the total count of distinct subsequences
           total_count = (total_count + added_subseq) % MOD
           # Update the last count of subsequences for the current character
            last_count[index] = (last_count[index] + added_subseq) % MOD
       # Return the total count of distinct subsequences
       return total_count
Java
class Solution {
   private static final int MOD = (int) 1e9 + 7; // Modulus value for handling large numbers
   public int distinctSubseqII(String s) {
        int[] lastOccurrenceCount = new int[26]; // Array to store the last occurrence count of each character
        int totalDistinctSubsequences = 0; // Variable to store the total count of distinct subsequences
```

// Iterate through each character in the string

int alphabetIndex = s.charAt(i) - 'a';

// Determine the alphabet index of current character

// And add 1 for the subsequence consisting of the character itself.

totalDistinctSubsequences = (totalDistinctSubsequences + newSubsequences) % MOD;

// Update the last occurrence count for this character in the lastOccurrenceCount array

// Update the totalDistinctSubsequences by adding newSubsequences

for (int i = 0; i < s.length(); ++i) {</pre>

function distinctSubseqII(s: string): number {

for (const char of s) {

 $last_count = [0] * 26$

total_count = 0

for char in s:

// Iterate over each character in the string

(runningTotal + currentValue) % MODULO, ∅) + 1;

Initialize the total count of distinct subsequences

added subseq = total count - last count[index] + 1

Update the total count of distinct subsequences

total_count = (total_count + added_subseq) % MOD

Get the index of the current character in the alphabet (0-25)

Calculate how many new subsequences are added by this character:

Update the last count of subsequences for the current character

It is total_count (all previous subsequences) minus last_count[index]

Iterate over each character in the string

index = ord(char) - ord('a')

```
// Since the result can be negative due to the subtraction during the loop,
       // we add MOD and then take the modulus to ensure a non-negative result
       return (totalDistinctSubsequences + MOD) % MOD;
class Solution {
public:
   const int MODULO = 1e9 + 7;
   // Method to calculate the number of distinct subsequences in the string `s`.
   int distinctSubseqII(string s) {
       vector<long> lastOccurrence(26, 0); // Array to store the last occurrence contribution for each character
        long totalCount = 0; // Total count of distinct subsequences
       // Loop through each character in the string
        for (char& c : s) {
            int index = c - 'a'; // Map character 'a' to 'z' to index 0 to 25
            long additionalCount = (totalCount - lastOccurrence[index] + 1 + MODULO) % MODULO; // Calculate the additional count
            totalCount = (totalCount + additionalCount) % MODULO; // Update the total count
            lastOccurrence[index] = (lastOccurrence[index] + additionalCount) % MODULO; // Update the last occurrence contribution
       return (int)totalCount; // Return the total count of distinct subsequences as an integer
};
TypeScript
```

const lastOccurrence = new Array<number>(26).fill(0); // Store the count of distinct subsequences ending with each letter

// Calculate the number to add. This number represents the new subsequences that will be formed by adding the new cha

// Subtract the last occurrence count of this character to avoid counting subsequences formed by prior occurrences or

int newSubsequences = (totalDistinctSubsequences - lastOccurrenceCount[alphabetIndex] + 1 + MOD) % MOD;

lastOccurrenceCount[alphabetIndex] = (lastOccurrenceCount[alphabetIndex] + newSubsequences) % MOD;

```
// Return the sum of all distinct subsequences modulo the defined constant to avoid overflow
      return lastOccurrence.reduce((runningTotal, currentValue) =>
          (runningTotal + currentValue) % MODULO, 0);
class Solution:
   def distinctSubseqII(self, s: str) -> int:
       # Define the modulo value to handle large numbers
       MOD = 10**9 + 7
       # Initialize an array to keep track of the last count of subsequences
       # ending with each letter of the alphabet
```

const MODULO: number = 1e9 + 7; // A constant for the modulo operation to prevent overflow

// Calculate the number of new distinct subsequences ending with the current character

// It is the sum of all distinct subsequences seen so far plus 1 (for the char itself)

lastOccurrence[charIndex] = lastOccurrence.reduce((runningTotal, currentValue) =>

const charIndex: number = char.charCodeAt(0) - 'a'.charCodeAt(0); // Map 'a' to 0, 'b' to 1, etc.

```
last_count[index] = (last_count[index] + added_subseq) % MOD
       # Return the total count of distinct subsequences
       return total_count
Time and Space Complexity
```

(which we have already counted with the current character) plus 1 for the character itself

The key operation is iterating over each character in the input string s. For each character, the algorithm performs a constant amount of work; it updates ans and modifies an element in the dp array, which is of fixed size 26 (corresponding to the lowercase

space does not scale with the input size but is a constant size due to the fixed alphabet size.

The provided code computes the count of distinct subsequences in a string using dynamic programming.

```
English alphabet). The time complexity is therefore O(N), where N is the length of the string s.
```

Time Complexity

Space Complexity The space complexity of the algorithm is defined by the space needed to store the dp array and the variables used. The dp array requires space for 26 integers, regardless of the length of the input string. Hence, the space complexity is O(1) since the required