1855. Maximum Distance Between a Pair of Values

Medium Greedy Array Two Pointers Binary Search

Problem Description

such that: 1. i is an index from nums1 and j is an index from nums2.

In this problem, we are given two non-increasing integer arrays, nums1 and nums2. We define a valid pair as a pair of indices (i, j)

- 2. i must be less than or equal to j (i \leftarrow j).
- 3. The value at nums1[i] must be less than the value at nums2[j] (nums1[i] < nums2[j]).
 - possible distance for any valid pair of indices. If there are no valid pairs, we should return 0. Note that an array is non-increasing if each element is less than or equal to the previous element. This implies that the numbers

The distance for a valid pair (i, j) is calculated by the difference j - i. The goal of the problem is to return the maximum

in both nums1 and nums2 are sorted in non-increasing order (from largest to smallest).

The intuition behind the solution involves recognizing that if a pair (i, j) is valid, then any pair (i, k) where k < j is also valid

Intuition

efficiently find the maximum distance. We choose the two-pointer approach here as it simplifies the implementation. We start by initializing two pointers, i and j, at the beginning of nums1 and nums2 respectively. We then iterate through nums1 with i, trying to find the furthest j in nums2 that will form a valid pair. As we go, we keep track of the maximum distance ans.

due to the non-increasing order of the arrays. This property allows us to use a two-pointer or a binary search approach to

The crucial observation is that since both nums1 and nums2 are non-increasing, once we find a j for a particular i such that nums1[i] <= nums2[j], we don't need to reset j back to i for the next i. Instead, we can continue from the current j, because if</pre>

nums1[i] <= nums2[j] and nums1 is non-increasing, then nums1[i + 1] will be less than or equal to nums1[i], and hence also less than or equal to nums2[j]. We keep incrementing j until the condition nums1[i] <= nums2[j] is no longer met.

However, we need to calculate the distance j - i and store the maximum. Since j is incremented in the inner loop until nums1[i]

- nums2[j] is false, at this point j is actually one index past the valid pair, so we compute j - i - 1 to get the correct distance

As a result, the algorithm efficiently calculates the maximum distance of any valid pair by scanning through both arrays only once.

The given reference solution approach indicates using a Binary Search algorithm. However, the provided solution code actually uses a two-pointer technique, which intuitively exploits the sorted nature of the arrays to find the maximum distance. Below, we'll

The code defines a class Solution with a method maxDistance which accepts two arrays, nums1 and nums2.

bounds).

Solution Approach

for considering the current index i.

Initialization: We begin by initializing a few variables: • m, the length of nums1 • n, the length of nums2 o ans, which will keep track of the maximum distance found among valid pairs. It is set to 0 initially.

Finding the Furthest j: For every index **i**, we have an inner while loop that seeks the furthest **j** such that nums1[i] <=

Iterating with Two Pointers: We use a while loop to iterate through nums1 with i as long as i < m (ensuring we don't go out of

remain 0 if no valid pairs existed. This value is then returned as the result of the method.

We want to find the maximum possible distance for any valid pair of indices.

valid pair for i = 0, we increment i to 1 and start over with j = 0.

def maxDistance(self, nums1: List[int], nums2: List[int]) -> int:

Initialize the maximum distance and the indices for nums1 and nums2

For the current idx_nums1, increase idx_nums2 as long as

Update the maximum distance if a larger one is found

// Using two pointers, iterate through both arrays

while (j < nums2Size && nums1[i] <= nums2[j]) {</pre>

for (int i = 0, j = 0; $i < nums1Size; ++i) {$

maxDist = max(maxDist, j - i - 1);

Import the List type from the typing module for type annotations

Initialize the lengths of the two input lists

len_nums1, len_nums2 = len(nums1), len(nums2)

max_distance = idx_nums1 = idx_nums2 = 0

Loop through the elements of nums1

while idx_nums1 < len_nums1:</pre>

idx nums2 += 1

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max distance = max(max distance, idx nums2 - idx nums1 - 1)

Update the maximum distance if a larger one is found

the conditions are satisfied (nums1[idx_nums1] <= nums2[idx_nums2])

while idx_nums2 < len_nums2 and nums1[idx_nums1] <= nums2[idx_nums2]:</pre>

Decrement by 1 because idx_nums2 is increased one more time before the condition fails

++j;

// i is the pointer for nums1 and j is the pointer for nums2

// While j is within the bounds of nums2 and the value at nums1[i]

// Calculate the current distance, and update maxDist if it's greater

// than the current maxDist. Subtract one because j has been incremented

// in the last iteration of the inner loop where the condition was still valid.

// is less than or equal to the value at nums2[j], increment j

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walk through the implementation of the two-pointer solution given in the code.

Two pointers i and j, both set to 0, to iterate through nums1 and nums2 respectively.

- nums2[j]. This loop runs as long as j < n. If the condition is met, j is incremented by 1, moving the second pointer ahead in nums2.
- Incrementing 1: After checking and possibly updating the ans with the maximum distance for the current 1, we increment 1 by 1 and repeat the above steps until all elements of nums1 have been considered. **Returning the Answer**: When the loop terminates, ans will hold the maximum distance of any valid pair (i, j), or it will

far. The -1 is there to correct for the j index that is now at an invalid pair, having just moved past the last valid nums2[j].

Tracking the Maximum Distance: Once we are either out of bounds in nums2 or the condition is no longer satisfied, the inner

loop breaks and we use the maximum function max(ans, j - i - 1) to update our answer with the largest distance found so

doesn't require additional data structures and runs in linear time, as each pointer only passes through its respective array once. Thus, the implementation uses a methodical two-pointer strategy to measure the maximum distance between valid pairs across

The two-pointer approach is efficient because it leverages the sorted properties of nums1 and nums2 to avoid redundant checks. It

Let's walk through an example to illustrate the solution approach in practice. Suppose we have the following inputs: nums1 = [4, 2, 2] nums2 = [3, 2, 0]

We start with i = 0 in nums1 and j = 0 in nums2, with ans = 0 as we haven't found any valid pairs yet. In the outer loop, i is now at index 0 and nums1[0] is 4. The inner while loop starts iterating j through nums2. nums2[j] is 3,

which is less than nums1[i], so we don't have a valid pair. We continue to the next j without changing ans.

Now, j = 1 and nums2[j] is 2. It's still not greater than nums1[i] = 4, so we move to the next j. At j = 2, we have nums2[j] equal to 0, which is also not greater than 4. Having reached the end of nums2 without finding a

2.

Python

Java

increase over 0, so ans stays at 0.

two sorted arrays.

Example Walkthrough

Now i = 1 and nums1[i] is 2. Starting again from the beginning of nums2, we find that nums2[0] is 3, which is greater than nums1[1]. This is a valid pair (i=1, j=0). Hence, we update ans = max(ans, 0-1-1), but this gives us -2, which is not an

- We increment j to see if there is a pair with a larger distance. Now j is 1 and since nums1[i] = 2 is already less than nums2[j] = 2, we stop the inner while loop and update ans. Now ans = $\max(0, 1 - 1 - 1)$, which remains 0 as the indices are the same.
- case remains 0 as there were no valid pairs that satisfied the condition for a positive maximum distance. This example demonstrates how the two-pointer approach navigates through both arrays, cleverly using the condition of nonincreasing order to find the valid pairs and calculating the maximum possible distance.

After considering all elements of nums1 and finding no valid pair with a positive distance, the function returns the ans, which in this

Finally, we increment i to 2. nums1[i] is still 2, and we try with nums2[j] starting from the beginning. At j = 0, we once again

have a valid pair (i=2, j=0) and update ans to max(0, 0 - 2 - 1), giving us -3, which doesn't increase ans. Since all values

are non-increasing and there's no greater element in nums2 than 3, we can conclude there's no need to iterate j further for i =

Import the List type from the typing module for type annotations from typing import List class Solution:

```
max_distance = max(max_distance, idx_nums2 - idx_nums1 - 1)
    # Move to the next index in nums1
    idx_nums1 += 1
# Return the maximum distance found
```

return max_distance

Solution Implementation

```
class Solution {
    public int maxDistance(int[] nums1, int[] nums2) {
        int lengthNums1 = nums1.length; // length of the first array
        int lengthNums2 = nums2.length; // length of the second array
        int maxDist = 0; // variable to keep track of the maximum distance
        // Initialize two pointers for both arrays
        for (int indexNums1 = 0, indexNums2 = 0; indexNums1 < lengthNums1; ++indexNums1) {</pre>
            // Move the indexNums2 pointer forward as long as the condition holds
            while (indexNums2 < lengthNums2 && nums1[indexNums1] <= nums2[indexNums2]) {</pre>
                ++indexNums2;
           // Update maxDist with the maximum distance found so far
            // We subtract 1 because indexNums2 has moved one step further than the true distance
            maxDist = Math.max(maxDist, indexNums2 - indexNums1 - 1);
        return maxDist; // return the maximum distance found
C++
class Solution {
public:
    int maxDistance(vector<int>& nums1, vector<int>& nums2) {
        int nums1Size = nums1.size(); // Represents the size of the first vector nums1
        int nums2Size = nums2.size(); // Represents the size of the second vector nums2
        int maxDist = 0; // Initialize maximum distance to 0
```

```
return maxDist; // Return the computed maximum distance
};
TypeScript
function maxDistance(nums1: number[], nums2: number[]): number {
    let maximumDistance = 0; // This will store the maximum distance found.
    const nums1Length = nums1.length; // Length of the first array
    const nums2Length = nums2.length; // Length of the second array
    // Start with two pointers, 'i' for array nums1 and 'j' for array nums2
    for (let i = 0, j = 0; i < nums1Length; ++i) {
       // Increment 'j' as long as it's within the bounds of nums2
       // and the element in nums1 is less than or equal to the element in nums2.
       // This ensures that the 'j' finds the furthest distance it can go for each 'i'.
       while (j < nums2Length && nums1[i] <= nums2[j]) {</pre>
            j++;
       // Update the maximum distance. Since 'j' moved one step extra, we subtract 1.
       // i.e., j - i is the total distance from current 'i' to the last valid 'j'
       // but we need to subtract 1 since 'j' has moved one step ahead of valid position.
       maximumDistance = Math.max(maximumDistance, j - i - 1);
    // Return the maximum distance found
    return maximumDistance;
```

Move to the next index in nums1 $idx_nums1 += 1$ # Return the maximum distance found return max distance

Time and Space Complexity

Time Complexity

from typing import List

class Solution:

The time complexity of the given code is 0(m + n). Here, m is the length of nums1 and n is the length of nums2. This is because the two pointers i and j only move forward through their respective arrays, with i incrementing in every outer loop, and j potentially moving forward during each inner loop until nums1[i] <= nums2[j] no longer holds. Since each pointer goes through its</pre> respective array at most once, the time complexity is linear with respect to the sizes of the input arrays.

Space Complexity

The space complexity of the code is 0(1). No additional space is used that grows with the input size. The variables ans, i, j, m, and n each use a constant amount of space.