- Combinatorics
- Permutations
- Permutation : Generic Approach
- Combinations

For question 1, we have two possible outcomes:

- True
- False

Similarly, for question 2 as well.

since we have to solve question 1 AND 2 We will

Instead, if we had to solve question 1 OR 2, we would've

This is because, when considering Event 1 AND Event 2, we are talking about two independent events.

- Solving question 1 is independent from solving question 2
- Hence, we need to multiply to consider their combined effect.

Therefore, we can solve them in 2 \* 2 = 4 ways:

- True, True
- True, False
- False, True

• False, False

## Permutation and Combination

- When talking about permutations, we mean arrangement of objects.
- Therefore, as with arranging objects, the most important thing is order is which they are arranged.

∘ This means that  $(i, j) \neq (j, i)$ 

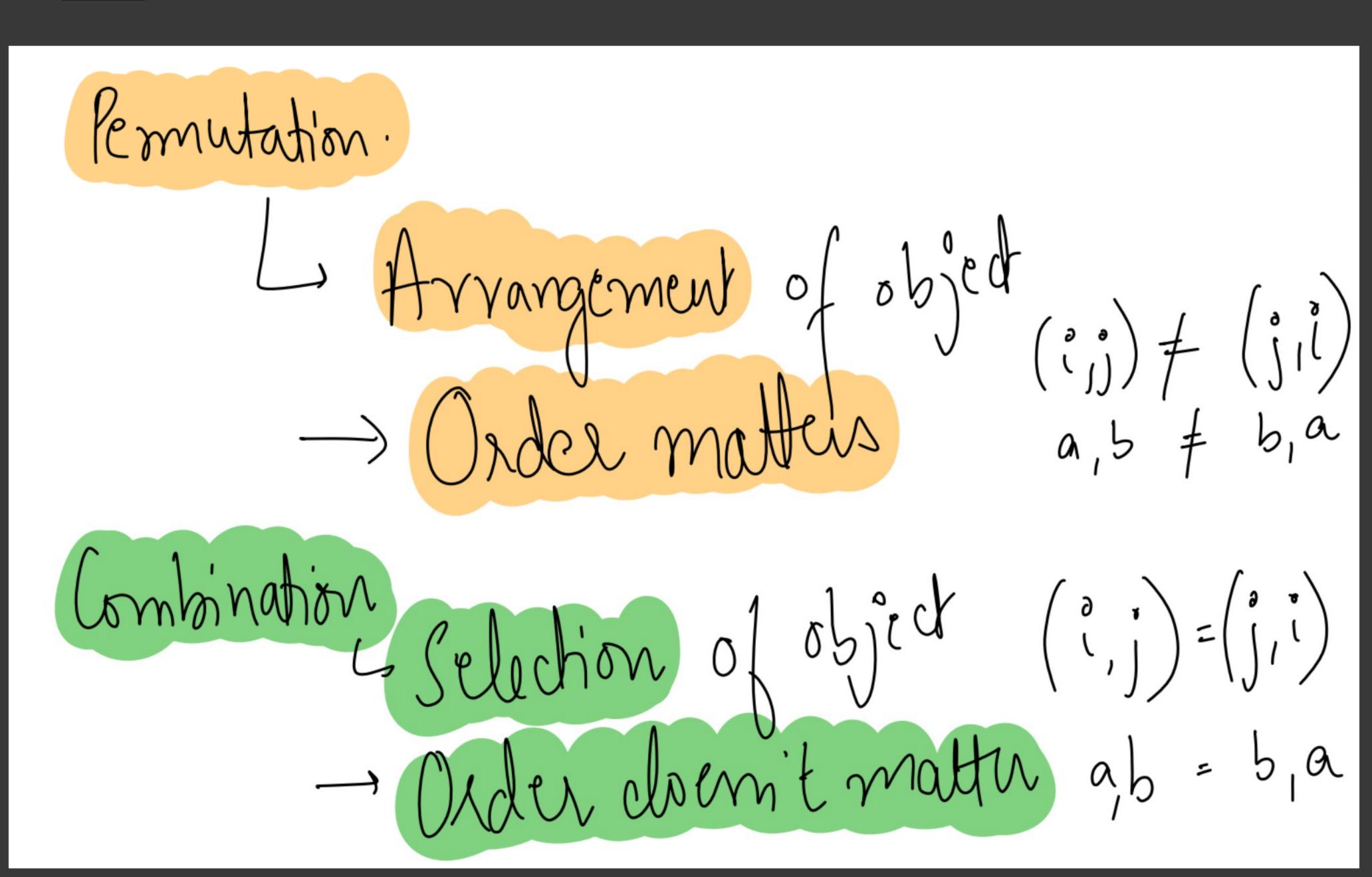
Formal Definition: A permutation is an arrangement of items or elements in a specific order, where the order of the arrangement matters.

The second aspect is **Combinations** 

- Combination is Selection of objects.
- Over here, the order of objects does not matter.

• This means that (i, j) = (j, i)

Formal Definition: A combination is selection of items or elements where the order of the arrangement does not matter.



# Permutation : Generic Formula

Since there are 3 slots for N objects, the no. of ways in which we can arrange them is  $^NP_3$ 

i.e. 
$${}^{N}P_{3} = N.(N-1).(N-2)$$

$$^{N}P_{4} = N.(N-1).(N-2).(N-3)$$

We can observe a pattern between the no. of slots/blanks, and the last term of the above expressions

This can be found using:

$$^{N}P_{k} = N(N-1)(N-2)(N-3)...(N-(k-1)) = N(N-1)(N-2)(N-3)...(N-k+1)$$

Let's re-write this equation by multiplying and dividing by same expression, as:

$${}^{N}P_{k} = N(N-1)(N-2)(N-3)\dots(N-(k-1)) = N(N-1)(N-2)(N-3)\dots(N-k+1) \times \frac{(N-k)(N-k-1)(N-k-2)\dots1}{(N-k)(N-k-1)(N-k-2)\dots1}$$

As we know, we can write this in the form of factorial as:  ${}^{N}P_{k} = \frac{N!}{(N-k)!}$ 

# Combinations

- Combinations, in simple terms, are all the different ways you can choose a certain number of items from a group, where the order in which you pick them doesn't matter.
- It's like making a sandwich with different ingredients the combination is the unique mix of ingredients you choose, regardless of the order you add them.

In the language of combinatorics, this number of ways of selecting is known as Combination.

Similarly, we can write the **general formula** for combinations in terms of permutations as:  ${}^nC_k = \frac{{}^nP_k}{k!}$ 

We can further expand it as:  ${}^{n}C_{k} = \frac{n!}{k!(n-k)!}$