# Pramod Parajuli Simulation and Modeling, CS-331

Chapter 2
System Studies



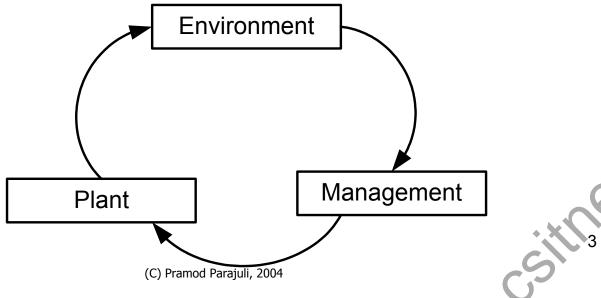
#### **Sub Systems**

- -System consists of interacting *subsystems*
- -Each subsystem has its own inputs and outputs
- -Similarly, a model can also be broken into **submodels**
- -Sometimes, the terms subsystem, sub-model, and blocks are interchangeable



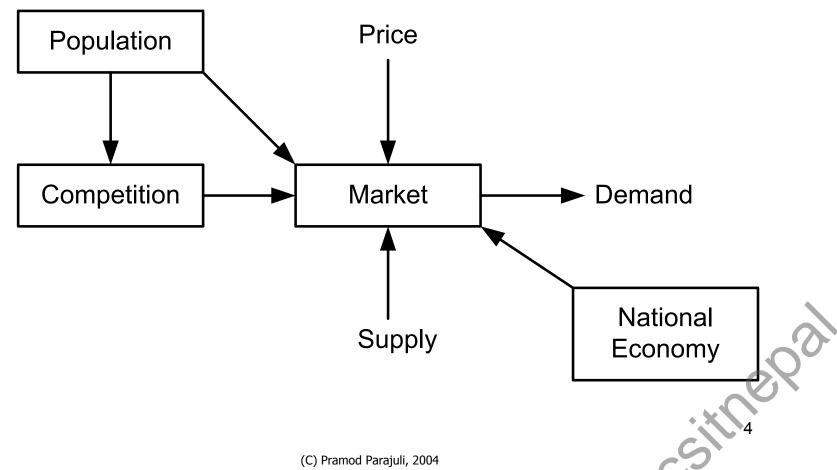
#### **A Corporate Model**

- Model that exhibits the property of a corporation
- 3 essentials
  - Environment: the corporation exists within the environment
  - Management: responsible for all of the planning, risk analysis, scheduling, marketing etc.
  - Plant: the real implementation of the plan and design

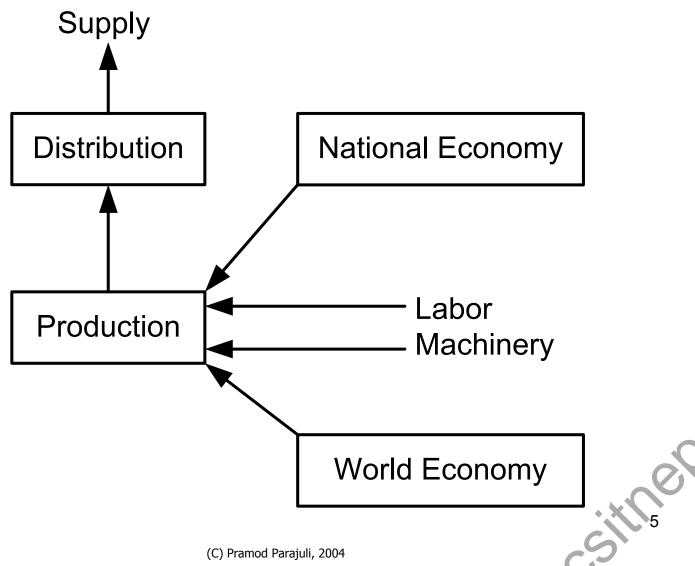


### **Environment**

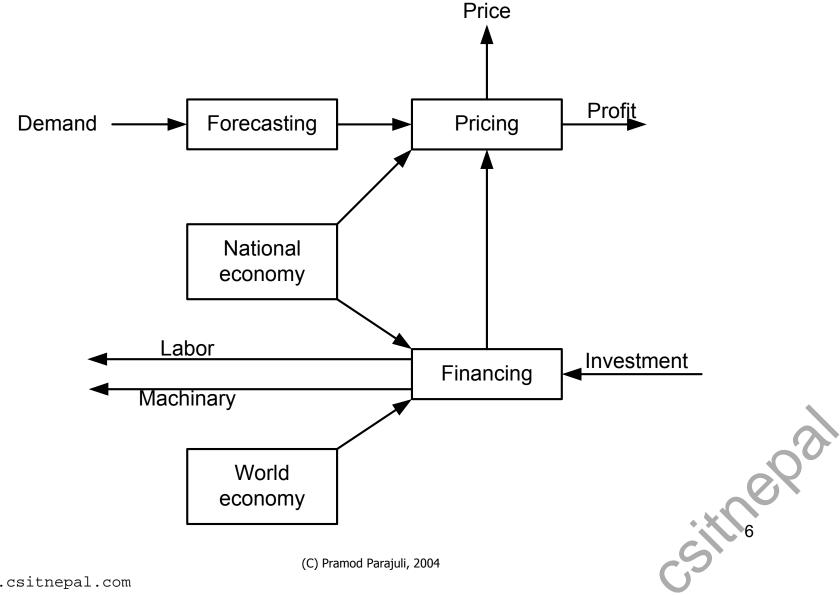
### market model



#### **Production**

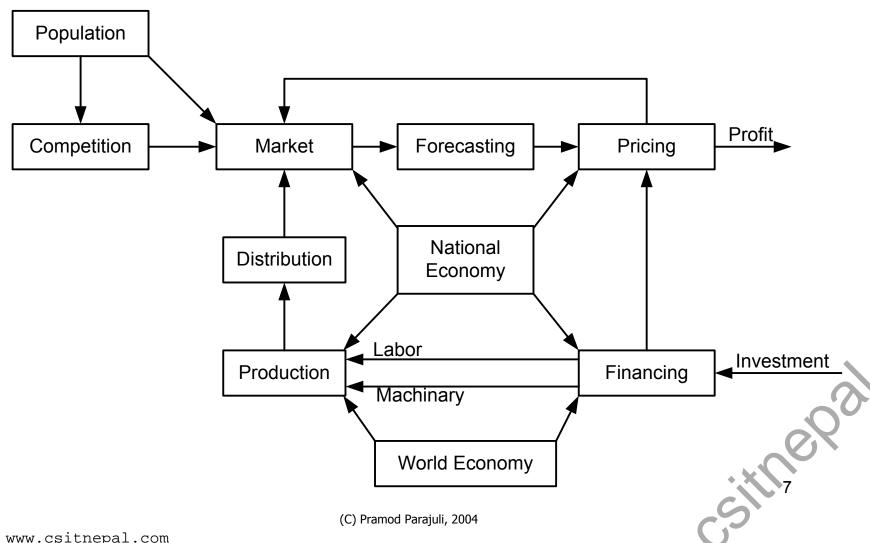


# **Management**



# **Full Corporate Model**

#### Combine



#### **Types of System Studies**

- System analysis
  - understand the system under study
  - focus on system performance
- System design
  - develop the logical objects that meet some specification
  - calculate the performance and compare with the prediction
  - if not satisfied, then redesign and repeat again
- System postulation
  - Characteristic of the way models are employed in other disciplines

#### **System Analysis**

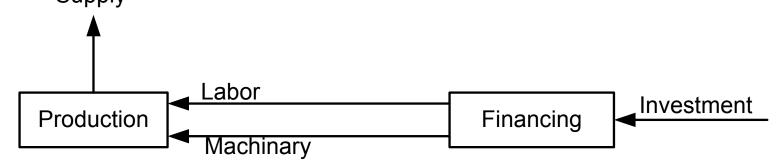
# Considerations;

K Capital investment

L Labor

M Machinery

Supply Supply



$$S = f.L^{a1}.M^{a2}$$

Cobb-Douglas model. For simplicity consider; a1=a2=1

## **System Analysis**

As far as financial model is considered, it is modeled as;

$$K = eL + M$$

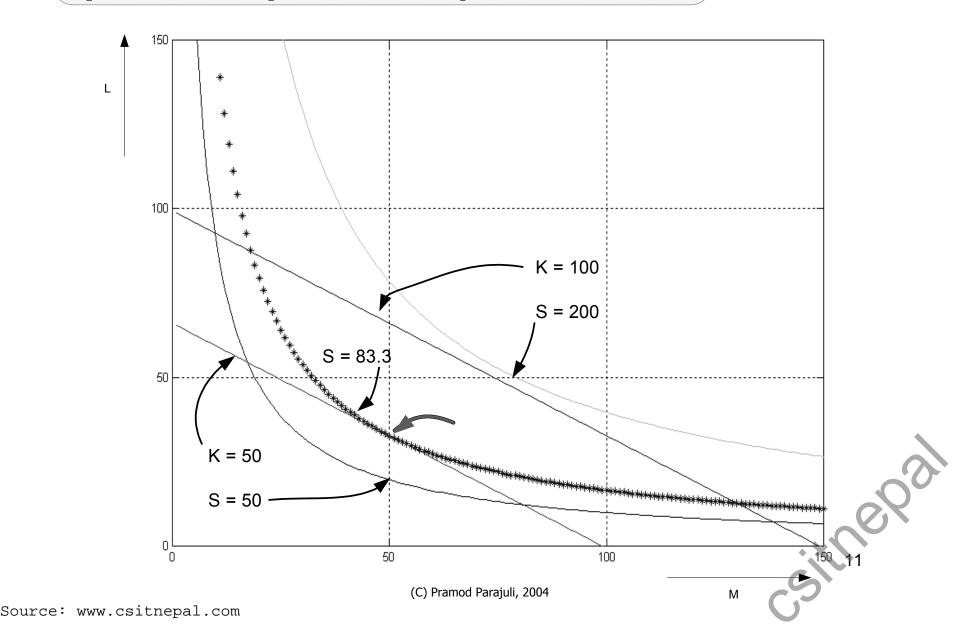
Since the interdependency of K, L, M, and S has been found, can we find an assignment of L and M that maximizes supply for a given investment?

Let's see the graph plot of the relationships.

Let's consider that e = 0.75 and f = 0.1



# **System Analysis – The optimal solution**



## **System Analysis – The optimal solution**

The optimal point is;

$$M = 50$$

$$L = 33.3$$

Depending on the samples taken, the optimal point changes.

Here, only a part of the corporate model is optimized and hence known as **sub-optimization**.

In general, when the system is giving the maximum performance, most of the sub-systems are at their peek performance.

### **System Analysis – The optimal solution**

The example we saw is a static one.

If the market competition, economy influence etc are to be considered, then the system will be dynamic and required even more sophisticated study



# Online computer system

- 'M' number of messages are received in a second
- 'm' number of characters in one message
- A buffer that can hold '**b**' number of characters at a time
- Fraction 'k' of the messages are replied
- The replied messages have 'r' number of characters on the average
- Same buffer used for sending and receiving
- **2,000** instructions are required to process a message
- 10,000 instructions require to generate the reply message
- To read and reply the messages requires **1,000** instructions each

# Online computer system

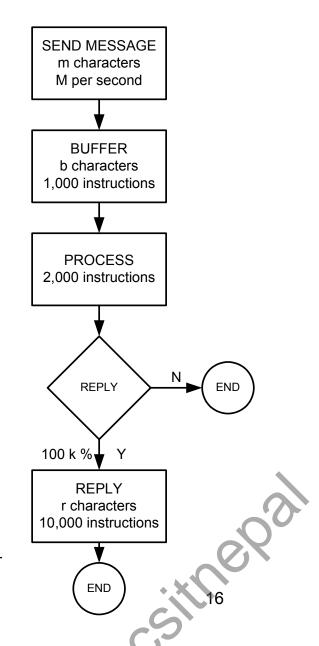
- 3 computer systems,
  - 25,000 instruction per second
  - 50,000 instruction per second
  - 100,000 instructions per second
- Buffer size can be
  - 1 character buffer
  - 2 character buffer
  - 5 character buffer
  - 10 character buffer
- Altogether, 12 different configurations
- Which computer with which buffer size will be the best for the implementation given the price of the systems,

# Here,

- M messages per second
- kM messages replied per second
- (M.m + k.M.r) characters pass thro buffer
- Since the buffer can hold 'b' chars,
   M (m+k.r)/b incomings per second

Altogether, the total number of instructions required;

$$N = 2,000M + 10,000M.k + \frac{1,000M(m+kr)}{b}$$



- If 's' is the number of instructions per second that the computer can execute then, the value of 's' to be able to process the given messages M, must be

$$N \leq s$$

- Let's consider that,

$$M = 5$$

$$M = 5$$
  $m = 15$ 

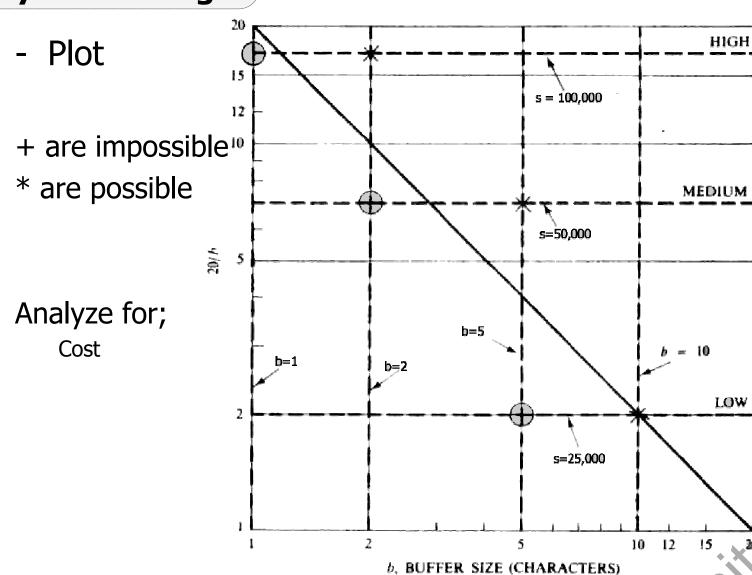
$$k = 0.1$$
  $r = 50$ 

$$r = 50$$

- When simplified, N ≤ s becomes;

$$\frac{20}{b} \le \frac{s}{5,000} - 3$$

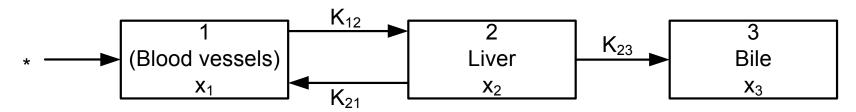
- Plot b against 20/b



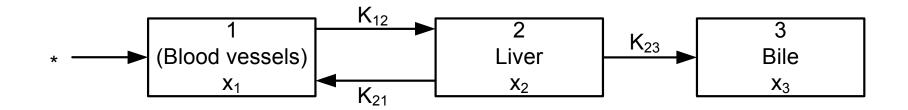
#### **System Postulation**

# Blood filtration in human body

- Bloods from vessels come into the liver
- Liver filters the blood and re-circulates the refined blood to vessels and extracts bile
- The amount of blood filtered and re-circulated can be observed (medical studies) using thyroxine.
- Use of compartments (*compartmental model*) to represent the components



### **System Postulation**



# The overall function can be represented as;

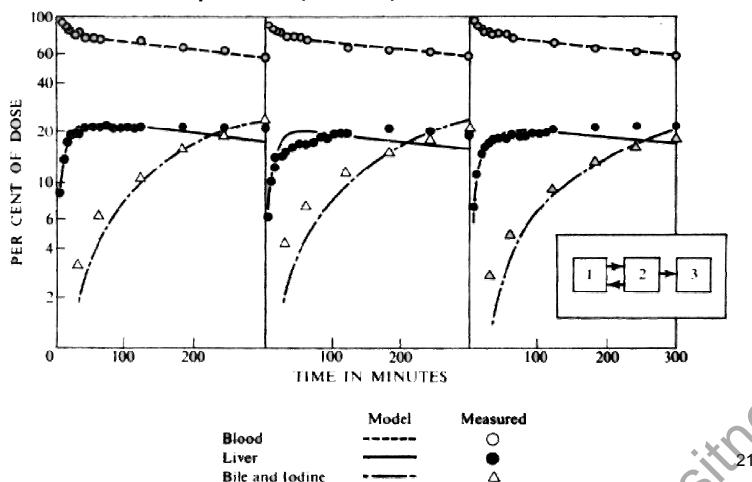
$$\frac{dx_1}{dt} = -k_{12}.x_1 + k_{21}.x_2 \qquad x_1 = C_{11}.e^{-b_1t} + C_{12}.e^{-b_2t}$$

$$\frac{dx_2}{dt} = k_{12}x_1 - (k_{21} + k_{23}).x_2 \qquad x_2 = C_{21}.e^{-b_1t} + C_{22}.e^{-b_2t}$$

$$\frac{dx_3}{dt} = k_{23}.x_2 \qquad x_3 = C_{31} + C_{32}.e^{-b_1t} + C_{33}.e^{-b_2t}$$

#### **System Postulation**

If the real world readings and the output of the models are plotted, then;



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