

We Know What You Want:



Movies & Models

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Executive Summary

This report summarizes the prediction of movie ratings for users based on the recommendation system our team is building. This tests out our recommendation system for implementation on our platform. An accurate recommendation system can effectively improve user experience, prolong user lifespan, broaden our marketing flexibility, and ultimately sustain revenue for our business.

Our recommendation system is fairly mature at this stage. We accurately predicted team members' rating on three movies in 6 out of 8 applicable cases. We achieved this even under data constraints.

Then, we took it to the next level. We made predictions on new users and movies where we have no prior data. These "cold start" cases are particularly tricky in the industry, but our system made it work. We successfully produced rating predictions for new movies based on existing user data, and for brand new users in cases with and without prior data.

Behind the scenes, the core of our success is the method of collaborative filtering. It is a machine learning technique that uses similarities between users and movies simultaneously to make predictions. Think about it this way. We tend to ask for recommendations from friends who have similar taste in movies to our own. Collaborative filtering works the same way. We can get into the details in our next meeting. For now, rest assured that our predictions are as robust as they can be given the data at hand. In our implementation, we took steps to eliminate user bias and item bias that could cloud our predictions.

We're not stopping here though. With more data and testing, we can build a robust and accurate recommendation system that could pinpoint each user's interest and offer a collection of tailor-made films to watch. This will allow us to stay in the game and even edge out competitors in an industry that is ever more reliant on recommendation systems.

Introduction

How often do we waste time trying to pick the best flick to watch over dinner? Ever ended up regretting watching a suggested movie? As a part of MovieRecommender.Inc, our key objective is to provide the best recommendations to our clients. We analyze historic movie ratings from numerous users along with personalized user parameters to deliver the perfect recommendation system.

Problem Formulation

Our goal is to create a recommendation system primarily using collaborative filtering. Both historical data from DMBI and internal employee data are available. For starters we develop a basic model to predict movie rating for team members with both user and item-based filters. We then enhance the model and predict ratings for newly joined customers whom we have no data on. On obtaining initial data on new customers, we feed this data to our system to see if it affects our predictions.

Data Characteristics

We have two datasets – 98 rows of ratings (1 to 5, hate to love) in employee dataset and 280 rows in DBMI dataset on 50 movies (Details in *Appendix 1-4*).

In terms of popularity (i.e., the number of users that rated the movie). The most popular movies are typically Hollywood box office champions such as *Avatar* (84) while the least known titles are about niche cultures such as *Ida* (4). Besides, in terms of public preferences, we compared the average ratings among movies. *Inception* (4.88) received the highest user average adjusted rating while *A Separation* (2.44) was rated the lowest. Also, we found that about 72% of ratings are 5 and 4 and only 2% of ratings are 1. This shows that either the users are lenient overall, or the set of movies is generally critically acclaimed. We also discovered that most users rated about 7 to 20 movies out of 50 with a few movie “fanatics” who have rated more than 40 movies.

Model Development, Predictions and Results

For task one, we developed several models to make predictions and do comparisons.

The picked 3 movies are: *La La Land*, *Gravity* and *The Imitation Game*.

Model 1 - 3: Item-Item Based Collaborative Filters with Original Ratings, Mean Centered, and Z-scores

Starting off, we used Item-Item Collaborative Filtering (IICF) with original movie ratings. To predict ratings for our members. We applied this model to both the class data and the combined data of class and DBMI ratings. Then, we used IICF on normalized movie ratings by centering each rating by the overall average for each team member. To mitigate the impacts of different variances among individuals in Model 1&2, we standardized and replaced the ratings with Z-scores. After that, we calculated the cosine similarity matrix of all movies and got the top 15 neighbors of each movie with the highest similarity rankings. The results are summarized in the table below. (Details in *Appendix 5-7*)

	Actual			Item Item with zscores			Item Item with original scores			Item Item with mean centered		
	La la land	Gravity	The Intimation Game	La la land	Gravity	The Intimation Game	La la land	Gravity	The Intimation Game	La la land	Gravity	The Intimation Game
Fred	4.00	3.00	-	4.04	4.01	4.30	2.27	2.49	2.42	4.00	3.28	2.76
Ajaiy	3.00	1.00	1.00	3.05	2.24	3.44	0.93	1.24	1.03	3.89	2.55	2.08
Sripriya	-	-	-	3.84	3.87	4.27	0.94	0.91	0.89	4.11	3.00	2.50
Jinny	5.00	5.00	3.00	4.01	4.02	4.37	3.54	1.67	1.65	4.00	3.17	2.66

We used the z-score method as one of the potential paths in **task 2**. We still standardized ratings as the first step, but this time we calculated average, standard deviation and cosine based on the DMBI dataset.

Name	Winter's bone	Serious Man	Son of Soul
Fred	2.83	2.70	3.29
Ajaiy	2.02	2.07	2.46
Sripriya	2.75	2.67	3.25
Jinny	2.86	2.77	3.35

Results are in the table above. Besides, we could add new data or more content features as another path, like movie genre, target audience, launch time, box office takings etc. and make classification among movie attributes. Also, user-based methods are useful paths to find similar users and make predictions.

Model 4: User-User Based Collaborative Filters (UUCF) (Appendix 8)

We developed a UUCF model that clusters similar users together. Since user's ratings are subjective, it is essential to normalize the ratings first. Then based on their Pearson correlation method “n” similar users to “user of interest” (say, user A) are identified. With the help of the ratings given by similar users we then predict ratings by user. If a particular movie hasn't been rated by any of the ‘n’ users, the model is unable to generate a predicted rating for user A, this is observed usually when the value of ‘n’ is small. Below are the predicted ratings for the members of our team for 3 movies of our choice. (Question 1) :

Movie Title	La La Land				Gravity				The Imitation Game			
n - value	5	15	30	Actual Rating	5	15	30	Actual Rating	5	15	30	Actual Rating
User 332 - Shaolong	3.85	3.41	3.51	4	3.49	3.53	3.67	3	N/A	4.28	4.26	-
User 342 - Ajaiy	2.4	2.15	1.99	3	0.02	1.03	1.29	1	1.13	1.12	1.14	1
User 362 - Jinny	5	5	5	5	N/A	5	4.92	5	4.33	4.25	4.37	4

As “n” increases the prediction accuracy decreases, as our pool of similar users becomes larger, i.e lowering correlation value threshold. We now make predictions for specific movies of interest (as per Question 2). Here compared to the above case, the values of n are much higher, this is because these movies are much rarely watched as compared to the ones in the previous question. Hence more number of similar users (higher ‘n’ value) are required to make a prediction. This issue can be avoided in the IICF.

Movie Title	Winter's Bone			A Serious Man			Son of Saul		
n - value	100	150	200	100	150	200	100	150	200
User 332 - Shaolong	N/A	4.18	4.18	3.437	3.721	3.721	N/A	N/A	4.005
User 342 - Ajaiy	1.023	1.023	1.023	1.023	1.023	1.023	1.023	1.023	1.023
User 362 - Jinny	4.226	4.226	4.225	4.342	4.432	4.317	4.432	4.432	4.317

In UUCF using Pearson correlation we also observe NaN values of correlation due to variance being 0, hence for a fairly new user or a user with very few number of ratings like Sripriya (4th team member) the ratings cannot be predicted. This issue is also resolved in the IIFC method.

Different users have subjective opinions of ratings, some are harsh while some generous. Using a boxplot of average ratings of every user we observe among our team members that Ajaiy has harshest while Jinny has most lenient ratings.(Appendix 9)

In Task 3, we are predicting the rating of 3 new users (Amy, Camille, and Shachi) on *Avatar*, *Inception*, and *The Wolf of Wall Street*. Having no prior data on new users poses a challenge. We define 3 paths to approach this challenge. The predictions from all three paths are in the table below.

Path	Data	<i>Inception</i>	<i>Avatar</i>	<i>The Wolf of Wall Street</i>
Simple Average (1)	Employee	4.40	3.99	4.17
	Employee + DBMI	4.49	4.02	4.12
IICS of Actual Ratings (2)	Employee	3.99	4.00	3.99
	Employee + DBMI	3.99	3.99	4.00
IICS of Normalized Ratings (3)	Employee	4.05	3.90	3.96
	Employee + DBMI	3.90	3.70	3.91

First, we make predictions based on simple averages of actual ratings for the 3 movies with historical data. We assume that pooling the ratings across the entire dataset, the averages should at least have some generalizability towards typical new users. In our second path, we predict ratings for new users based on

cosine similarity between movies with IICF of prior ratings for 10 films most similar with the 3 targeted movies (*Appendix 10*). We eliminate some bias from the first approach by filtering and predicting based on similar content, but are still exposed to user biases. To eliminate that, in our third path we normalize historical user ratings. Then, we filter for the most similar movies with mean-centered ratings (*Appendix 11*). Eliminating biases, our predictions are getting closer to true ratings.

Our predictions remain high across the board as the 3 targeted movies are blockbusters. Their popularity can mask the effectiveness of our predictions. Predicting ratings of a diverse set of films could yield more apparent results. In addition, we theorized more ways to predict ratings when we face “cold start” user cases. First, most streaming platforms collect information on preference when a new user lands for the first time. Second, we can use UUCF based on demographic information. Lastly, we can gather data that could indirectly inform user taste: views and clicks when browsing movies could indicate interest.

Earlier we did not have any information on these new customers, but now we have their ratings for 5 movies. In **task 4**, we first calculate the cosine similarity between the movies to be predicted vs the movies whose data we now have for each new customer. We then calculate (*Appendix 12*) the weighted average of the rating by providing a higher weight if the movies are more similar to each other. Customers are more likely to give the same rating to similar movies, hence this can be used for new customers. The employee and full dataset resulted in some decimal differences, but on rounding we got the same results.

User	Inception	Avatar	Wolf of Wall Street
Amy	3 (2.95)	3 (2.9)	3 (2.92)
Shachi	4 (4.17)	4 (4.15)	4 (4.16)
Camille	3 (3.17)	3 (3.16)	3 (3.14)

$$\text{Predicted Rating} = \frac{\sum_1^j \text{CosineSimilarity}_{(i,j)} * \text{Rating}_j}{\sum_1^j \text{CosineSimilarity}_{(i,j)}}$$

Amy’s and Camille’s prediction as compared to that in task 3, has dropped by 1 for all movies, Shachi’s remains the same for all. This change in rating is because earlier we made predictions purely based on the item and no user data, whereas now we have taken into consideration the data of the new users which helps fine tune the model to make a more personalized and accurate prediction.

Value Creation, Recommendations and Implications

Using such recommendation engines in eCommerce and mobile commerce, the search and transaction costs per user could be reduced. As users spend long hours online purchasing, the basket size, retention rates and conversion rates are all improved. For retailers like Walmart, accurate predictions could help the company to adjust the assortment strategy and balance inventory level. With UUCFs, it could analyze preference differences between consumer groups and help targeted promotions. With IICFs, stores could adjust assortment among similar products to grow profits.

Potentially we could improve the methods by adding more dimensions of movie content and customer profiles. Second, benchmarking with public data sources would expose potential opportunities. Besides, objective value functions could be considered to refine the recommendation process. Instead of making predictions simply based on similarity and scores, a weighted objective function considering the relative importance of each movie could be helpful. The importance index could be based on movie popularity (e.g. number of reviews, box office earnings) and sentiments (e.g. Rotten Tomatoes reviews). Thus, popular movies with positive reviews could get higher weights and be recommended to more users.

To improve areas in customer analytics, benchmarking with open industrial data would help understand market trends and changes in customer behaviors before deep-diving in a specific segment. Richer dimensions provide more angles in analyzing customer journeys and where to make interventions in social media. It is suggested to consider relative priorities when conducting customer analytics.

Conclusion

We have made predictions for both existing as well as new users by employing different methods. In case of new users or existing users with few ratings, we are inclined to use the IICF method. But for existing users, UUCF produces better predictions at about 75% accuracy and we would recommend that. Had we collected preliminary data for new users about demographics, or choice of language, genre, actors and so on, we could have attempted a UUCF model as well. On the other hand, for existing users with a significant number of ratings, we can use either UUCF or IICF models.

Appendix

Appendix 1: Count of Non-Zero Rating by Movie

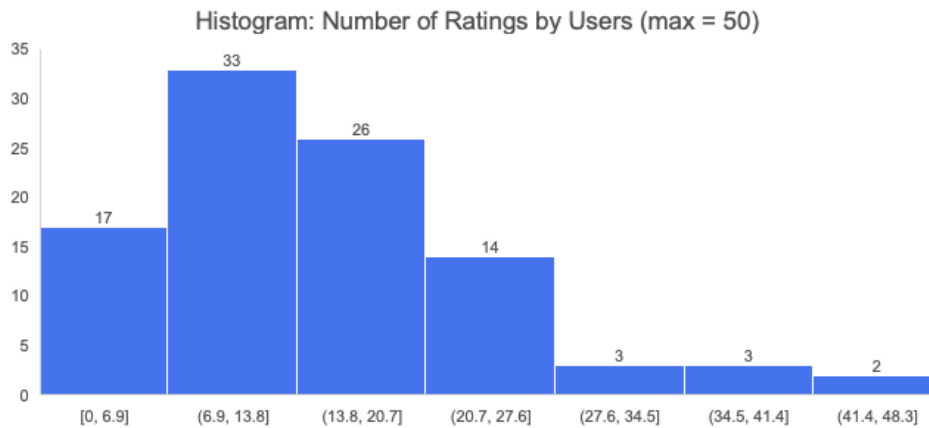
As a note, the employee dataset doesn't include ratings on 3 movies: *Winter's Bone*, *A Serious Man*, and *Son of Saul* as they were not included in the initial survey. "Did Not Watch" or NA is counted as no input.

Movies	Count of Non-0 Rating
[Avatar]	84
[Inception]	82
[The Wolf of Wall Street]	81
[Life of Pi]	69
[La La Land]	67
[Toy Story 3]	65
[Gravity]	58
[The Imitation Game]	56
[Dunkirk]	55
[Black Swan]	51
[The Social Network]	49
[Mad Max: Fury Road]	49
[The Grand Budapest Hotel]	46
[The King's Speech]	39
[Inglourious Basterds]	39
[Zero Dark Thirty]	38
[Arrival]	38
[12 Years a Slave]	35
[Birdman]	33
[Call Me by Your Name]	32
[The Shape of Water]	30
[Hugo]	27
[Argo]	25
[The Descendants]	23
[Spotlight]	22
[Lincoln]	22
[Moonlight]	21
[Boyhood]	19
[Blue is the Warmest Colour]	17
[Manchester by the Sea]	17
[Three Billboards Outside Ebbing, Missouri]	17
[The Fighter]	17
[The Tree of Life]	15
[Up in the Air]	14
[True Grit]	12
[Amour]	10
[The Artist]	10
[Precious]	10
[The White Ribbon]	9
[A Prophet]	8
[A Separation]	7
[Toni Erdmann]	7
[Inside Llewyn Davis]	7
[Leviathan]	6
[Beasts of the Southern Wild]	6
[The Secret in Their Eyes]	5
[Ida]	4

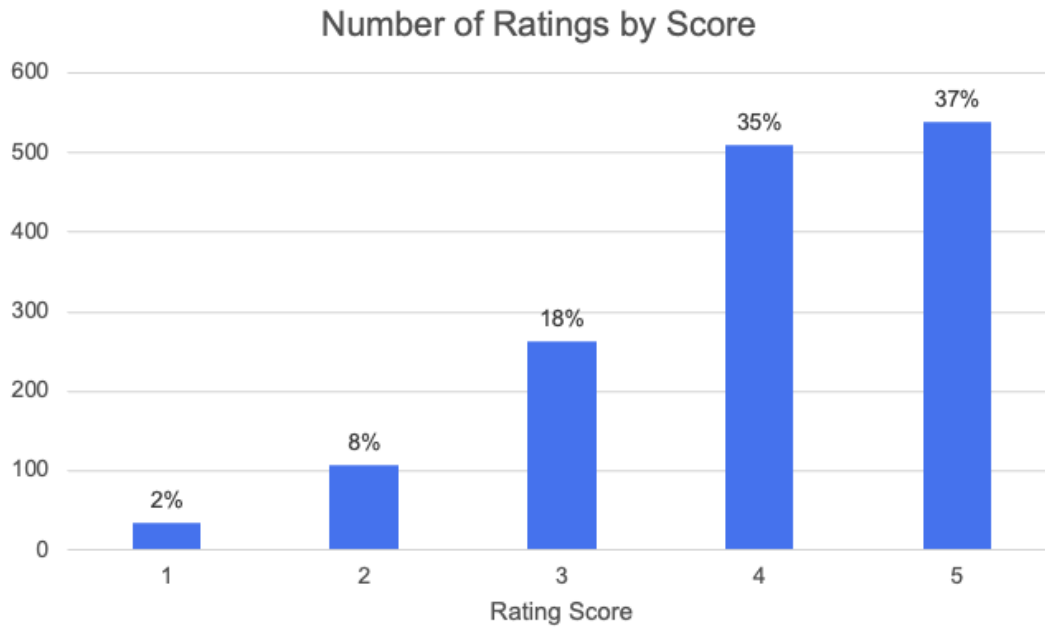
Appendix 2: Average Movie Ratings by Users

Movie	Original Ratings	Movie	Ratings Adjusted With User Average
Son of Saul	n/a	Son of Saul	n/a
Winter's Bone	n/a	Winter's Bone	n/a
A Serious Man	n/a	A Serious Man	n/a
Inception	4.40	Inception	4.88
Black Swan	4.29	Ida	4.83
The Imitation Game	4.27	Black Swan	4.61
The Grand Budapest Hotel	4.26	Inglourious Basterds	4.52
Inglourious Basterds	4.26	The Grand Budapest Hotel	4.51
Ida	4.25	The Imitation Game	4.48
Call Me by Your Name	4.25	Call Me by Your Name	4.43
Three Billboards Outside Ebbing, Missouri	4.18	Three Billboards Outside Ebbing, Missouri	4.41
The Wolf of Wall Street	4.17	The Wolf of Wall Street	4.39
The Social Network	4.12	The Social Network	4.28
Life of Pi	4.12	Life of Pi	4.22
Dunkirk	4.05	Dunkirk	4.21
12 Years a Slave	4.00	The Tree of Life	4.14
Argo	4.00	Moonlight	4.12
True Grit	4.00	True Grit	4.10
Avatar	3.99	12 Years a Slave	4.06
Arrival	3.97	Avatar	3.99
The Tree of Life	3.93	Argo	3.96
Up in the Air	3.93	The White Ribbon	3.94
Moonlight	3.90	The Secret in Their Eyes	3.92
The Shape of Water	3.90	Arrival	3.92
Zero Dark Thirty	3.89	Up in the Air	3.91
Gravity	3.88	Zero Dark Thirty	3.88
The King's Speech	3.87	Gravity	3.85
Hugo	3.85	Blue is the Warmest Colour	3.83
La La Land	3.85	The Shape of Water	3.78
The Descendants	3.83	Hugo	3.76
The Secret in Their Eyes	3.80	The Descendants	3.73
Toy Story 3	3.78	A Prophet	3.69
The White Ribbon	3.78	La La Land	3.68
Spotlight	3.77	Toy Story 3	3.62
Blue is the Warmest Colour	3.76	Leviathan	3.61
The Fighter	3.76	The Fighter	3.61
Leviathan	3.67	The King's Speech	3.60
Manchester by the Sea	3.65	Spotlight	3.57
Mad Max: Fury Road	3.63	Amour	3.47
A Prophet	3.63	Precious	3.34
Amour	3.60	Mad Max: Fury Road	3.29
Lincoln	3.59	Manchester by the Sea	3.26
Birdman	3.58	Beasts of the Southern Wild	3.26
The Artist	3.50	Lincoln	3.24
Precious	3.50	The Artist	3.17
Beasts of the Southern Wild	3.50	Birdman	3.13
Toni Erdmann	3.43	Toni Erdmann	3.11
Boyhood	3.42	Boyhood	2.89
Inside Llewyn Davis	3.29	Inside Llewyn Davis	2.88
A Separation	3.14	A Separation	2.44

Appendix 3: Count of Total Ratings by User



Appendix 4: Count of Rating Score Across all User Ratings



Appendix 5: Model 1, Item-Item Collaborative Filters with Original Scores

user	La La Land	Avatar	Life of Pi	Inception	The Wolf of V	Toy Story 3	The King's S	The Grand B	Black Swan	The Social Network
Fred	4	5		5	5		5			
Ajaly	3	2	2	1	2	1				
Sripriya		4	4							
Jinny	5	5		5		4	5	5	3	

	Cosine Similarity									
	Sim(1,2)	Sim(1,3)	Sim(1,4)	Sim(1,5)	Sim(1,6)	Sim(1,7)	Sim(1,8)	Sim(1,9)	Sim(1,10)	
Deno1	7.07	7.07	7.07	7.07	7.07	7.07	7.07	7.07	7.07	
Deno2	8.37	4.47	7.14	5.39	4.12	7.07	5.00	3.00	0.00	
CosineM1	0.7736797	0.749548	0.7193332	0.6840894	0.6710463	0.6621177	0.6547967	0.6451648	0.6082978	
CosineM2	0.7367459	0.6869723	0.6864672	0.6538814	0.6451429	0.6154741	0.6005972	0.59323	0.5857671	
CosineM3	0.7533215	0.7474057	0.727957	0.6962558	0.6930729	0.6718697	0.6708153	0.6460261	0.6166931	

user	Movie 1	Movie 2	Movie 3
Fred	2.30	2.45	2.45
Ajaly	0.94	1.24	1.13
Sripriya	0.99	0.92	0.90
Jinny	3.03	1.63	1.58

Appendix 6: Model 2, Item-Item Collaborative Filters with Mean Centered

user	Movie 1	Precious	The White Ri	Hugo	Inception	Black Swan	Avatar	Toy Story 3	Ida	The Shape of Water
Fred	0	0	0	0	1.333333333	0	1	0	0	0
Ajaib	-1	0	0	0	-2.666666667	0	-2	-1.5	0	0
Sripriya	0	0	0	0	0	0	0	0	0	0
Jinny	1	0	0	0	1.333333333	0	1	1.5	0	0

user	LalaLand	Precious	The White Ri	Hugo	Inception	Black Swan	Avatar	Toy Story 3	Ida	The Shape of Water
Fred	4				5		5			4
Ajaib	3				1		2	1		
Sripriya							4			
Jinny	5				5	3	5	4		
Average	4	#DIV/0!	#DIV/0!	#DIV/0!	3.666666667	3	4	2.5	#DIV/0!	4

	Cosine Similarity									
	Sim(1,2)	Sim(1,3)	Sim(1,4)	Sim(1,5)	Sim(1,6)	Sim(1,7)	Sim(1,8)	Sim(1,9)	Sim(1,10)	
Cosine1	0.075388	0.065263	0.057097	0.046491	0.031059	0.030489	0.030136	0.028905	0.025063	
AbsCosine1	0.075388	0.065263	0.057097	0.046491	0.031059	0.030489	0.030136	0.028905	0.025063	
Cosine2	0.15	0.14	0.08	0.07	0.06	0.02	0.02	0.02	0.02	
AbsCosine2	0.149427466	0.138117955	0.076679892	0.071770284	0.064097584	0.022519338	0.019969038	0.018565304	0.015466986	
Cosine3	0.157533979	0.133486352	0.102798245	0.088306186	0.086229544	0.060527063	0.053826336	0.04507807	0.040924758	
AbsCosine3	0.157533979	0.133486352	0.102798245	0.088306186	0.086229544	0.060527063	0.053826336	0.04507807	0.040924758	

user	Movie 1	Movie 2	Movie 3
Fred	4.24	3.03	2.79
Ajaib	3.41	2.94	2.03
Sripriya	4.00	3.00	2.50
Jinny	4.35	3.03	2.68

Appendix 7: Model 3, Item-Item Based Collaborative Filters with Z-Scored

(a) Step 1: Standardized Z-score of ratings

	X.The.Social.Network.	X.A.Prophet.	X.Amour.	X.The.King.s.Speech.	X.La.La.Land.	X.Boyhood.	X.Inception.	X.A.Separation.	X.The.Artist.	X.The.White.Ribbon.
1	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.6440915	0.0000000	0.0000000	0.0000000
2	-0.1428571	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.6440915	0.0000000	0.0000000	0.0000000
3	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	-0.4337759	0.0000000	0.4629101	0.0000000
4	1.0238095	0.0000000	0.0000000	0.0000000	-1.6552829	0.0000000	-1.5116433	0.0000000	0.0000000	0.0000000
5	-0.1428571	0.0000000	0.0000000	0.0000000	0.0000000	0.6022941	0.6440915	0.0000000	0.0000000	0.0000000
6	1.0238095	0.0000000	0.0000000	1.0685803	-1.6552829	0.0000000	-0.4337759	0.0000000	0.0000000	0.0000000
7	1.0238095	0.0000000	0.0000000	1.0685803	1.0278773	-0.4380321	-0.4337759	0.0000000	0.0000000	0.0000000
8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
9	0.0000000	0.0000000	0.0000000	0.0000000	1.0278773	0.0000000	0.6440915	0.0000000	0.0000000	0.0000000
10	-0.1428571	0.0000000	0.0000000	0.0000000	0.1334906	0.0000000	-0.4337759	0.0000000	0.0000000	0.0000000
11	-0.1428571	0.0000000	-0.5581563	0.0000000	0.0000000	0.0000000	-0.4337759	0.0000000	0.0000000	0.0000000
12	-0.1428571	0.0000000	0.0000000	-0.8257211	0.1334906	0.0000000	-0.4337759	0.0000000	0.4629101	0.0000000
13	-0.1428571	0.0000000	0.0000000	-0.8257211	-0.7608962	0.0000000	0.6440915	0.0000000	0.0000000	0.0000000
14	0.0000000	0.7245688	0.0000000	0.0000000	-0.7608962	0.0000000	-0.4337759	0.0000000	0.0000000	0.0000000
15	1.0238095	0.0000000	0.0000000	-1.7728718	-0.7608962	0.6022941	0.6440915	1.18019369	0.0000000	0.0000000
16	1.0238095	0.0000000	0.0000000	0.0000000	0.1334906	0.0000000	0.6440915	0.0000000	0.0000000	0.0000000
17	-0.1428571	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	-0.4337759	0.0000000	0.0000000	0.0000000
18	-2.4761905	0.0000000	0.0000000	0.0000000	0.0000000	1.6426202	0.6440915	0.0000000	0.0000000	0.0000000
19	1.0238095	-1.2076147	-0.5581563	-1.7728718	-0.7608962	0.0000000	0.6440915	0.0000000	0.0000000	0.2286648
20	-0.1428571	-1.2076147	0.0000000	-1.7728718	1.0278773	0.0000000	0.6440915	0.0000000	-0.4629101	0.2286648
21	0.0000000	0.0000000	1.3023647	1.0685803	-2.5496697	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
22	-1.3095238	0.0000000	0.0000000	0.0000000	1.0278773	0.0000000	-1.5116433	0.0000000	0.0000000	0.0000000
23	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	-3.6673781	0.0000000	0.0000000	0.0000000
24	0.0000000	0.0000000	0.0000000	0.0000000	-0.7608962	0.0000000	-2.5895107	0.0000000	0.0000000	0.0000000
25	0.0000000	0.0000000	0.0000000	0.0000000	-0.7608962	0.0000000	-0.4337759	0.0000000	0.0000000	0.0000000

(b) Step 2: Similarity matrix (i.e., Cosine matrix) - Sample data

	X.The.Social.Network.	X.A.Prophet.	X.Amour.	X.The.King.s.Speech.	X.La.La.Land.	X.Boyhood.	X.Inception.	X.A.Separation.	X.The.Artist.
X.The.Social.Network.	1.000000000	0.026666032	0.055839910	-0.025873397	-0.191756801	-0.3258071967	0.165821054	-0.009425320	0.0943898830
X.A.Prophet.	0.026666032	1.000000000	0.464233584	0.432650968	0.002999977	0.0294529666	0.010932820	0.043983222	0.1126872339
X.Amour.	0.055839910	0.464233584	1.000000000	0.318117078	-0.009273278	-0.0176082284	0.130794504	-0.066656980	0.1818202630
X.The.King.s.Speech.	-0.025873397	0.432650968	0.318117078	1.000000000	0.022514942	0.1063154462	0.008895721	0.074759596	-0.0413377603
X.La.La.Land.	-0.191756801	0.002999977	-0.009273278	0.022514942	1.000000000	0.1296745355	0.158465758	-0.100605781	0.0238331688
X.Boyhood.	-0.325807197	0.029452967	-0.017608228	0.106315446	0.129674536	1.0000000000	0.052551051	0.514666902	-0.2210436238
X.Inception.	0.165821054	0.010932820	0.130794504	0.008895721	0.158465758	0.0525510509	1.000000000	-0.013316141	0.0367343142
X.A.Separation.	-0.009425320	0.043983222	-0.066656980	0.074759596	-0.100605781	0.5146669021	-0.013316141	1.000000000	-0.2973808571
X.The.Artist.	0.094389883	0.112687234	0.181820263	-0.041337760	0.023833169	-0.2210436238	0.036734314	-0.297380857	0.9999999999
X.The.White.Ribbon.	0.072653421	0.169742853	0.320883647	-0.106858601	0.069874483	-0.1001625046	0.013283600	-0.067417262	0.6362090102
X.Zero.Dark.Thirty.	0.028079601	0.205399513	0.142824820	0.160638077	0.009076173	0.1425718677	0.188436752	0.002943247	0.1783596050
X.Avatar.	0.127667101	0.096270785	0.189165945	0.208058492	0.113009194	-0.0111780889	0.366982959	-0.066284034	0.1292189781
X.Spotlight.	-0.086817831	0.057760015	-0.030584276	0.162432689	0.161347978	0.2305631489	0.033648726	0.179672265	0.1995717947
X.Precious.	0.037068593	0.196931590	0.510829468	0.120531511	0.083140305	0.0759301468	0.061010124	-0.072685476	0.2420910129
X.The.Tree.of.Life.	0.006443851	0.296324595	0.645201657	0.125979043	-0.071161535	0.1571625415	0.087428217	-0.024659297	0.3702156406
X.12.Years.a.Slave.	0.080191628	0.232379001	0.289429146	0.236791769	0.066924644	-0.1387101522	-0.006816131	-0.193932695	0.4364357804
X.Blue.is.the.Warmest.Colour.	0.294082851	0.057298985	0.019463498	-0.017722192	-0.054447947	-0.1387227833	0.054622469	-0.069789988	0.3107365886
X.Up.in.the.Air.	0.001570199	-0.059843917	0.045583928	0.047662483	-0.036493631	0.0002563754	-0.073434107	0.064054590	0.5088387036
X.Inglourious.Basterds.	0.098212510	0.285603890	0.162375254	0.177533422	0.057201451	-0.1535791065	-0.002132869	-0.025748290	0.4550474624
X.Mad.Max..Fury.Road.	0.270839873	-0.166033763	-0.091975838	0.043345410	-0.175350166	0.0759985693	0.045211981	0.271697138	0.0596331010
X.Moonlight.	0.062654926	0.145208350	0.383848308	0.052745452	-0.009231830	-0.0351356937	0.107419351	0.051774092	0.4169450693
X.Birdman.	0.067858515	0.173079205	0.240956152	0.156474878	0.058119197	0.0614893077	0.028265288	0.049698716	0.0894346006
X.Manchester.by.the.Sea.	-0.061572204	-0.083809270	-0.006901477	0.047459080	0.063816465	0.1066362465	0.004002340	0.044337531	-0.0622460935

(c) Step 3: Predicted top 15 neighbors of each movie - Sample data

	V1	V2	V3	V4	V5	V6	V7	V8
X.The.Social.Network.	X.The.Social.Network.	X.Blue.is.the.Warmest.Colour.	X.Dunkirk.	X.Mad.Max..Fury.Road.	X.The.Wolf.of.Wall.Street.	X.Inception.	X.Black.Swan.	X.Avatar.
X.A.Prophet.	X.A.Prophet.	X.Amour.	X.The.King.s.Speech.	X.The.Fighter.	X.The.Tree.of.Life.	X.Inglourious.Basterds.	X.Three.Billboards.Outside.Evansville.	X.Toni.Erdmann.
X.Amour.	X.Amour.	X.The.Tree.of.Life.	X.Precious.	X.A.Prophet.	X.Moonlight.	X.The.Fighter.	X.Ida.	X.The.White.Ribbon.
X.The.King.s.Speech.	X.The.King.s.Speech.	X.A.Prophet.	X.Amour.	X.12.Years.a.Slave.	X.Avatar.	X.Black.Swan.	X.Toni.Erdmann.	X.True.Grit.
X.La.La.Land.	X.La.La.Land.	X.Arrival.	X.Dunkirk.	X.Life.of.Pi.	X.Spotlight.	X.Inception.	X.Boyhood.	X.Ida.
X.Boyhood.	X.Boyhood.	X.A.Separation.	X.The.Descendants.	X.Hugo.	X.True.Grit.	X.Spotlight.	X.Call.Me.by.Your.Name.	X.The.Tree.of.Life.
X.Inception.	X.Inception.	X.Toy.Story.3.	X.Gravity.	X.Dunkirk.	X.Avatar.	X.The.Wolf.of.Wall.Street.	X.The.Imitation.Game.	X.Arrival.
X.A.Separation.	X.A.Separation.	X.Boyhood.	X.Call.Me.by.Your.Name.	X.Inside.Llewellyn.Davies.	X.The.Descendants.	X.Mad.Max..Fury.Road.	X.True.Grit.	X.Toni.Erdmann.
X.The.Artist.	X.The.Artist.	X.Ida.	X.The.White.Ribbon.	X.Beasts.of.the.Southern.Cross.	X.Leviathan.	X.Up.in.the.Air.	X.Inglourious.Basterds.	X.Lincoln.
X.The.White.Ribbon.	X.The.White.Ribbon.	X.Beasts.of.the.Southern.Cross.	X.Ida.	X.The.Secret.in.Their.Eyes.	X.The.Artist.	X.Leviathan.	X.The.Fighter.	X.Moonlight.
X.Zero.Dark.Thirty.	X.Zero.Dark.Thirty.	X.Argo.	X.Toni.Erdmann.	X.The.Fighter.	X.Gravity.	X.Arrival.	X.Ida.	X.Dunkirk.
X.Avatar.	X.Avatar.	X.Gravity.	X.Inception.	X.The.Wolf.of.Wall.Street.	X.Dunkirk.	X.Toy.Story.3.	X.Life.of.Pi.	X.The.King.s.Speech.
X.Spotlight.	X.Spotlight.	X.Inglourious.Basterds.	X.Birdman.	X.True.Grit.	X.The.Grand.Budapest.Hotel.	X.12.Years.a.Slave.	X.Toni.Erdmann.	X.Dunkirk.
X.Precious.	X.Precious.	X.The.Tree.of.Life.	X.Toni.Erdmann.	X.Amour.	X.Ida.	X.The.Fighter.	X.True.Grit.	X.Birdman.
X.The.Tree.of.Life.	X.The.Tree.of.Life.	X.Amour.	X.Precious.	X.The.White.Ribbon.	X.Ida.	X.Beasts.of.the.Southern.Cross.	X.The.Secret.in.Their.Eyes.	X.Moonlight.
X.12.Years.a.Slave.	X.12.Years.a.Slave.	X.Inglourious.Basterds.	X.Toni.Erdmann.	X.Ida.	X.The.Artist.	X.The.Fighter.	X.Birdman.	X.True.Grit.
X.Blue.is.the.Warmest.Colour.	X.Blue.is.the.Warmest.Colour.	X.The.Artist.	X.The.Social.Network.	X.Dunkirk.	X.Beasts.of.the.Southern.Cross.	X.Ida.	X.Leviathan.	X.The.White.Ribbon.
X.Up.in.the.Air.	X.Up.in.the.Air.	X.The.Secret.in.Their.Eyes.	X.The.Artist.	X.The.White.Ribbon.	X.Beasts.of.the.Southern.Cross.	X.Moonlight.	X.Leviathan.	X.Mad.Max..Fury.Road.
X.Inglourious.Basterds.	X.Inglourious.Basterds.	X.12.Years.a.Slave.	X.Toni.Erdmann.	X.The.Artist.	X.True.Grit.	X.The.Fighter.	X.Spotlight.	X.Three.Billboards.Outside.Evansville.
X.Mad.Max..Fury.Road.	X.Mad.Max..Fury.Road.	X.Up.in.the.Air.	X.Dunkirk.	X.Inside.Llewellyn.Davies.	X.A.Separation.	X.The.Social.Network.	X.Gravity.	X.Moonlight.
X.Moonlight.	X.Moonlight.	X.The.Secret.in.Their.Eyes.	X.The.White.Ribbon.	X.Beasts.of.the.Southern.Cross.	X.Ida.	X.Up.in.the.Air.	X.The.Artist.	X.The.Tree.of.Life.
X.Birdman.	X.Birdman.	X.12.Years.a.Slave.	X.Precious.	X.Toni.Erdmann.	X.Black.Swan.	X.Spotlight.	X.The.Fighter.	X.Up.in.the.Air.
X.Manchester.by.the.Sea.	X.Manchester.by.the.Sea.	X.True.Grit.	X.Inside.Llewellyn.Davies.	X.The.Descendants.	X.Call.Me.by.Your.Name.	X.Toni.Erdmann.	X.Three.Billboards.Outside.Evansville.	X.Moonlight.
X.Lincoln.	X.Lincoln.	X.Ida.	X.The.Artist.	X.Beasts.of.the.Southern.Cross.	X.The.White.Ribbon.	X.Leviathan.	X.The.Tree.of.Life.	X.Toni.Erdmann.
X.Hugo.	X.Hugo.	X.Up.in.the.Air.	X.Boyhood.	X.12.Years.a.Slave.	X.The.Descendants.	X.Ida.	X.The.Artist.	X.Lincoln.

(d) R Codes of model 1 - Key highlights

Cosine calculation

```
# create cosine function
getCosine <- function(x,y)
{
  this.cosine <- sum(x*y) / (sqrt(sum(x*x)) * sqrt(sum(y*y)))
  return(this.cosine)
}
```

Similarity matrix

```
for(i in 1:ncol(hw4_new)) {
  # Loop through the columns for each column
  for(j in 1:ncol(hw4_new)) {
    # Fill in placeholder with cosine similarities
    similarity[i,j] <- getCosine(as.matrix(hw4_new[i]),as.matrix(hw4_new[j]))
    absCosine[i,j] <- abs(similarity[i,j])
  }
}
View(similarity)
View(absCosine)
```

Top neighbors selection

```
# get the top 15 neighbors
neighbours <- matrix(NA, nrow=ncol(similarity),ncol=15,dimnames=list(colnames(similarity)))
for(i in 1:ncol(hw4_new))
{
  neighbours[i,] <- t(rownames(head(n=15,as.matrix(similarity[order(similarity[,i],decreasing=TRUE),][,i]))))
}
View(neighbours)
```

Appendix 8: User-User Collaborative Filtering

Structure of Input Data : We have combined both the class data as well as DBMI Data. Totally we have 378 users, starting from user id 0 to 377.

userid	title	rating
0	The Social Network	5
0	The King's Speech	3
0	La La Land	4
0	Inception	5
0	Avatar	5
0	12 Years a Slave	2
0	Up in the Air	5
0	Birdman	4
0	Lincoln	3
0	Hugo	4
0	Gravity	5
0	The Wolf of Wall Street	5
0	Life of Pi	5
1	The Social Network	3
1	The King's Speech	4
1	La La Land	5
1	Boyhood	4
1	Inception	5
1	Avatar	3
1	Up in the Air	3

Step 0 : Inputting and Structuring data

```
df = pd.read_excel("data.xlsx")
df.head()
matrix_data = df.pivot_table(index='userid', columns='title', values='rating')
matrix_data.head()
```

Step 1 : Normalizing the ratings to remove User Bias

We do so by subtracting the average rating from each individual value, this gives a negative rating value for those below average and positive for ones above.

```
mat = matrix_data.subtract(matrix_data.mean(axis=1), axis = 'rows')
mat.head()
```

Step 2 : Defining similarity between users

This is done in two methods, one using Pearson Correlation and the other using Cosine Similarity.

Method 1 : Cosine Similarity : Calculates the cosine of the angle between the two vectors that represent a pair of users.

```
In [5]: # User similarity matrix using cosine similarity
user_similarity_cosine = cosine_similarity(mat.fillna(0))
user_similarity_cosine

Out[5]: array([[ 1.          , -0.0994042 ,  0.04651303, ...,  0.23534666,
                 0.04518771,  0.10963225],
               [-0.0994042 ,  1.          , -0.20246457, ..., -0.07663063,
                 -0.23659147, -0.15111763],
               [ 0.04651303, -0.20246457,  1.          , ...,  0.53785287,
                 -0.15122507,  0.          ],
               ...,
               [ 0.23534666, -0.07663063,  0.53785287, ...,  1.          ,
                 -0.05422456, -0.12677314],
               [ 0.04518771, -0.23659147, -0.15122507, ..., -0.05422456,
                 1.          , -0.10693227],
               [ 0.10963225, -0.15111763,  0.          , ..., -0.12677314,
                 -0.10693227,  1.          ]])
```

The downside of this method is that it cannot accept N/A values, and hence NA values need to be encoded as 0, this would misrepresent the ratings and hence we did not use this method in our predictions, it is only for illustration purposes.

Method 2 : Pearson Correlation : Calculated correlation values between pairs of users. Correlation values range from -1 to +1. Higher the value, the more similar the users are.

```
# User similarity matrix using Pearson correlation
user_similarity = mat.T.corr()
user_similarity.head()
```

```
]:
```

	userid	0	1	2	3	4	5	6	7	
userid	0	1.000000	-0.198680	-1.0	-0.316228	0.218218	0.566947	0.577350	-5.222330e-01	0.03
1	-0.198680	1.000000	NaN	-0.174078	0.192308	0.011606	-0.816497	-6.500800e-17	0.20	
2	-1.000000	NaN	1.0	NaN	NaN	NaN	NaN	NaN	NaN	
3	-0.316228	-0.174078	NaN	1.000000	-0.292770	-0.727607	NaN	8.807048e-01	-0.47	
4	0.218218	0.192308	NaN	-0.292770	1.000000	0.785714	NaN	-4.000000e-01	-0.32	

5 rows x 377 columns

Step 3 : Here we identify 'n' users similar to the user of interest

```
In [7]: # Number of similar users
n = 30

# User similarity threshold
user_similarity_threshold = 0.3

# Get top n similar users
similar_users = user_similarity[
    user_similarity[picked_userid]>user_similarity_threshold][picked_userid].sort_values(ascending=False)[:n]

# Print out top n similar users
print(f'The similar users for user {picked_userid} are', similar_users)
```

The similar users for user 362 are userid

377	1.000000
281	1.000000
329	1.000000
192	1.000000
351	1.000000
69	1.000000
49	1.000000
165	1.000000
19	1.000000
288	0.918559
110	0.880705
361	0.880705
352	0.871315
366	0.836660
84	0.790569
218	0.763763
282	0.763763
256	0.725866

Step 4 : Using the similar users list, a movie score is predicted for all movies watched by the similar users based on the similarity index, this score is then used to compute a predicted rating for our user of interest by adding the average rating of the user of interest to movie score.

```
In [11]: # A dictionary to store item scores
item_score = {}

# Loop through items
for i in similar_user_movies.columns:
    # Get the ratings for movie i
    movie_rating = similar_user_movies[i]
    # Create a variable to store the score
    total = 0
    # Create a variable to store the number of scores
    count = 0
    # Loop through similar users
    for u in similar_users.index:
        # If the movie has rating
        if pd.isna(movie_rating[u]) == False:
            # Score is the sum of user similarity score multiply by the movie rating
            score = similar_users[u] * movie_rating[u]
            # Add the score to the total score for the movie so far
            total += score
            # Add 1 to the count
            count += 1
    # Get the average score for the item
    item_score[i] = total / count

# Convert dictionary to pandas dataframe
item_score = pd.DataFrame(item_score.items(), columns=['movie', 'movie_score'])

# Sort the movies by score
ranked_item_score = item_score.sort_values(by='movie_score', ascending=False)

# Select top m movies
m = 50
ranked_item_score.head(m)
```

```
Out[11]:
```

	movie	movie_score
2	A Separation	0.798630
19	La La Land	0.433773
30	The Grand Budapest Hotel	0.406546
17	Inception	0.396069
3	Amour	0.395810
6	Avatar	0.387676
16	Ida	0.363048

```
# Average rating for the picked user
avg_rating = matrix_data[matrix_data.index == picked_userid].T.mean()[picked_userid]

# Print the average movie rating for user 1
print(f'The average movie rating for user {picked_userid} is {avg_rating:.2f}')
```

The average movie rating for user 332 is 4.20

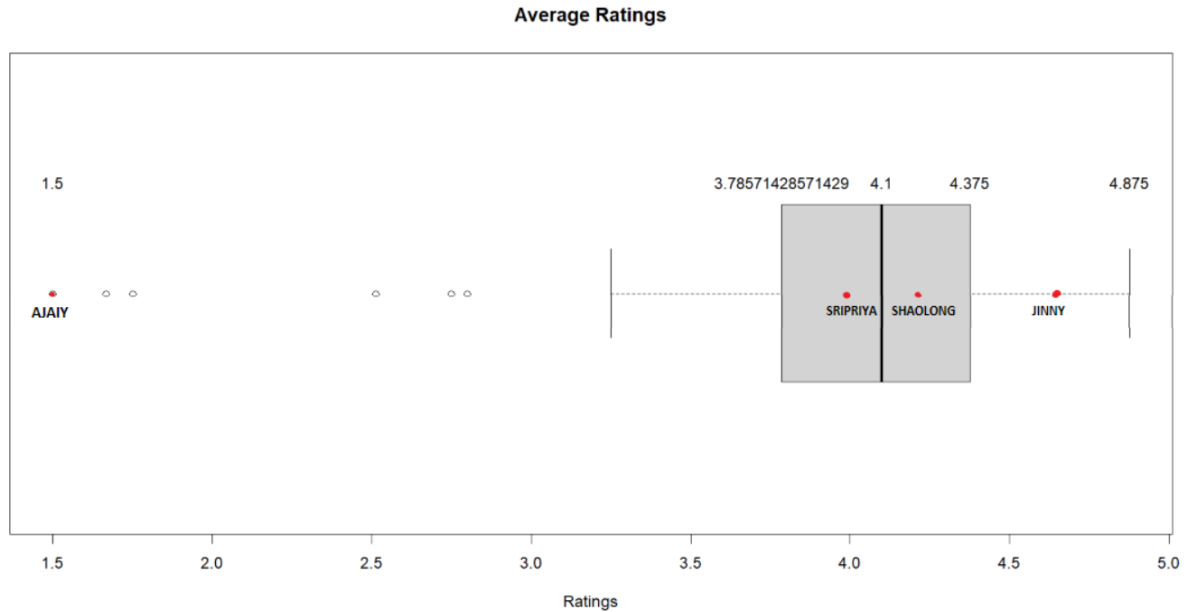
```
# Calculate the predicted rating
ranked_item_score['predicted_rating'] = ranked_item_score['movie_score'] + avg_rating

ranked_item_score.head(m)
```

```
]:
```

	movie	movie_score	predicted_rating
6	The Grand Budapest Hotel	1.285714	5.485714
3	Inception	0.542857	4.742857
0	Avatar	0.309524	4.509524
8	The Wolf of Wall Street	0.285714	4.485714
9	Toy Story 3	0.066667	4.266667
5	Life of Pi	0.042857	4.242857
4	La La Land	-0.200000	4.000000
7	The Shape of Water	-0.433333	3.766667
2	Gravity	-0.714286	3.485714
1	Birdman	-1.714286	2.485714

Appendix 9 : Boxplot for all users average ratings with our team members highlighted to visualize rating leniency.



Appendix 10a: Item-Item Cosine Similarity of Actual Movies Ratings, Class Data (Partial of 50x50)

	The Social N	A Prophet	Amour	The King's S	La La Land	Boyhood	Inception	A Separatio	The Artist	The White R	Zero Dark T	Avatar	Spotlight	Precious	The Tree of	12 Years a	Blue is the V	Son of Saul	Up in the Air
The Social N	1	0.311725	0.286864	0.456811	0.562902	0.395197	0.70833	0.199984	0.250169	0.270678	0.707969	0.623574	0.47518	0.236087	0.339673	0.548338	0.372221	NA	0.38579
A Prophet	0.311725	1	0.416691	0.166013	0.259349	0.306412	0.301432	0.274247	0.444281	0.530541	0.226652	0.250797	0.221178	0.348977	0.378299	0.152654	0.197238	NA	0.281089
Amour	0.286864	0.416691	1	0.394901	0.280838	0.20774	0.261447	0.230535	0.271151	0.623254	0.310886	0.333358	0.303854	0.565529	0.726503	0.393522	0.32331	NA	0.223398
The King's S	0.456811	0.166013	0.394901	1	0.653784	0.294491	0.556918	0.257086	0.155831	0.311629	0.392281	0.638545	0.476426	0.351618	0.479076	0.578874	0.264809	NA	0.329882
La La Land	0.562902	0.259349	0.280838	0.653784	1	0.404249	0.751457	0.192922	0.222048	0.308465	0.47567	0.769086	0.516463	0.338197	0.371573	0.54804	0.34792	NA	0.304196
Boyhood	0.395197	0.306412	0.20774	0.294491	0.404249	1	0.470078	0.550498	0.258008	0.23296	0.386979	0.39555	0.278364	0.273368	0.26142	0.460945	0.329931	NA	0.41035
Inception	0.70833	0.301432	0.261447	0.556918	0.751457	0.470078	1	0.259842	0.338492	0.294738	0.651036	0.816309	0.441343	0.31776	0.330745	0.536792	0.34281	NA	0.392622
A Separatio	0.199984	0.274247	0.230535	0.257086	0.192922	0.550498	0.259842	1	0.274367	0.402309	0.251397	0.193519	0.291234	0.307408	0.300972	0.357833	0.278261	NA	0.403767
The Artist	0.250169	0.444281	0.271151	0.155831	0.222048	0.258008	0.338492	0.274367	1	0.520479	0.311953	0.309882	0.236172	0.389358	0.439439	0.27844	0.281953	NA	0.452672
The White R	0.270678	0.530541	0.623254	0.311629	0.308465	0.23296	0.294738	0.402309	0.520479	1	0.332756	0.322335	0.425067	0.709682	0.660098	0.399267	0.470177	NA	0.368321
Zero Dark T	0.707969	0.226652	0.310886	0.392281	0.47567	0.386979	0.651036	0.251397	0.311953	0.332756	1	0.597099	0.442594	0.352342	0.334511	0.490999	0.396897	NA	0.456775
Avatar	0.623574	0.250797	0.333358	0.638545	0.769086	0.39555	0.816309	0.193519	0.309882	0.322335	0.597099	1	0.447028	0.349611	0.404168	0.594862	0.340935	NA	0.426835
Spotlight	0.47518	0.221178	0.303854	0.476426	0.516463	0.278364	0.441343	0.291234	0.326172	0.425067	0.442594	0.447028	1	0.330932	0.321492	0.445524	0.385514	NA	0.259179
Precious	0.236087	0.348977	0.565529	0.351618	0.338197	0.273368	0.31776	0.307408	0.389358	0.709682	0.352342	0.349611	0.330932	1	0.779437	0.395697	0.454698	NA	0.424727
The Tree of	0.339673	0.378299	0.726503	0.479076	0.371573	0.26142	0.330745	0.300972	0.439439	0.660098	0.334511	0.404168	0.321492	0.779437	1	0.475317	0.429456	NA	0.453589
12 Years a	0.548338	0.152654	0.393522	0.578874	0.54804	0.460945	0.536792	0.357833	0.27844	0.399267	0.490999	0.594862	0.445524	0.395697	0.475317	1	0.47241	NA	0.363878
Blue is the V	0.372221	0.197238	0.32331	0.264809	0.34792	0.329931	0.34281	0.278261	0.281953	0.470177	0.396897	0.340935	0.385514	0.454698	0.429456	0.47241	1	NA	0.396043
Son of Saul	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	1	NA
Up in the Air	0.38579	0.281089	0.223398	0.329882	0.304196	0.41035	0.392622	0.403767	0.452672	0.368321	0.456775	0.426835	0.259179	0.424727	0.453589	0.363878	0.396043	NA	1

Appendix 10b: Item-Item Cosine Similarity of Normalized Movies Ratings, Class Data (Partial of 50x50)

	The Social N	A Prophet	Amour	The King's S	La La Land	Boyhood	Inception	A Separatio	The Artist	The White R	Zero Dark T	Avatar	Spotlight	Precious	The Tree of	12 Years a	Blue is the V	Son of Saul	Up in the Air
The Social N	1	0.097834	0.045761	-0.06299	-0.1568	-0.33901	0.113245	-0.19216	0.180167	0.218485	-0.05071	0.063951	-0.25115	-0.01139	0.1432	0.013651	0.195703	NA	-0.01497
A Prophet	0.097834	1	0.273392	0.151256	0.015029	-0.1502	0.070455	-0.33862	0.472991	0.18426	0.194351	0.258515	0.022496	0.162155	0.161518	0.192979	0.127401	NA	-0.05526
Amour	0.045761	0.273392	1	0.048932	0.015657	-0.24587	0.051496	-0.41219	0.394309	0.374774	0.081798	0.157896	-0.10853	0.284212	0.348642	0.265267	0.104925	NA	0.128771
The King's S	-0.06299	0.151256	0.048932	1	-0.03096	0.056625	-0.29384	0.008958	0.09502	-0.20809	0.132981	0.162425	0.037461	-0.00742	-0.18775	0.148147	0.008049	NA	0.004471
La La Land	-0.1568	0.015029	0.015657	-0.03096	1	0.055999	-0.02746	-0.12566	0.02276	0.080707	-0.11174	0.041973	-0.03998	0.045124	-0.04551	-0.0373	0.037558	NA	-0.058
Boyhood	-0.33901	-0.1502	-0.24587	0.056625	0.055999	1	-0.2405	0.377385	-0.27493	-0.36282	0.079882	-0.15804	0.273557	-0.05172	-0.15188	-0.16828	-0.28025	NA	-0.16514
Inception	0.113245	0.070455	0.051496	-0.29384	-0.02746	-0.2405	1	-0.31723	0.133582	0.188747	-0.04275	0.011161	-0.18567	0.060548	0.196676	0.007639	0.104624	NA	0.000307
A Separatio	-0.19216	-0.33862	-0.41219	0.008958	-0.12566	0.377385	-0.31723	1	-0.44205	-0.40803	-0.15104	-0.30065	0.327629	-0.26996	-0.49314	-0.43097	-0.36114	NA	-0.34043
The Artist	0.180167	0.472991	0.394309	0.09502	0.02276	-0.27493	0.133582	-0.44205	1	0.435349	0.046381	0.093816	0.005839	0.185571	0.166814	0.339735	0.174047	NA	0.305072
The White R	0.218485	0.18426	0.374774	-0.20809	0.080707	-0.36282	0.188747	0.435349	0.435349	1	-0.11127	0.116821	-0.28413	0.144008	0.482241	0.116499	0.084538	NA	0.37404
Zero Dark T	-0.05071	0.194351	0.081798	0.132981	-0.11174	0.079882	-0.04275	-0.15104	0.046381	-0.11127	1	-0.04537	0.019502	0.035142	-0.0081	0.197545	0.025813	NA	-0.11521
Avatar	0.063951	0.258515	0.157896	0.162425	0.041973	-0.15804	0.011161	-0.30065	0.093816	0.116821	-0.04537	1	-0.23624	0.082609	0.24656	0.037775	0.195354	NA	0.086365
Spotlight	-0.25115	0.022496	-0.10853	0.037461	-0.03998	0.273557	-0.18567	0.327629	0.005839	-0.28413	0.019502	-0.23624	1	-0.12313	-0.45091	-0.06985	-0.1627	NA	-0.21838
Precious	-0.01139	0.162155	0.284212	-0.00742	0.045124	-0.05172	0.060548	-0.26996	0.185571	0.144008	0.035142	0.082609	-0.12313	1	0.632711	0.116229	0.064966	NA	-0.00915
The Tree of	0.1432	0.161518	0.348642	-0.18775	-0.04551	-0.15188	0.196676	-0.49314	0.166814	0.482241	-0.0081	0.24656	-0.45091	0.632711	1	0.107042	0.203744	NA	0.175144
12 Years a	0.013651	0.192979	0.265267	0.148147	-0.0373	-0.16828	0.007639	-0.43097	0.339735	0.116499	0.197545	0.037775	-0.06985	0.116229	0.107042	1	0.191684	NA	0.331063
Blue is the V	0.195703	0.127401	0.104925	0.008049	0.037558	-0.28025	0.104624	-0.36114	0.174047	0.084538	0.025813	0.195354	-0.1627	0.064966	0.203744	0.191684	1	NA	0.152799
Son of Saul	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	1	NA
Up in the Air	-0.01497	-0.05526	0.128771	0.004471	-0.058	-0.16514	0.000307	-0.34043	0.305072	0.37404	-0.11521	0.086365	-0.21838	-0.00915	0.175144	0.331063	0.152799	NA	1

Appendix 11a: Item-Item Cosine Similarity of Actual Movies Ratings, Class + DBMI Data (Partial of 50x50)

	The Social N	A Prophet	Amour	The King's S	La La Land	Boyhood	Inception	A Separatio	The Artist	The White R	Zero Dark Ti	Avatar	Spotlight
The Social N	1	0.269625	0.216214	0.571513	0.608298	0.383359	0.717668	0.255281	0.320411	0.192774	0.595409	0.67338	0.490684
A Prophet	0.269625	1	0.302771	0.245621	0.250761	0.290441	0.240663	0.389553	0.353563	0.288218	0.208368	0.233489	0.240942
Amour	0.216214	0.302771	1	0.319894	0.237586	0.198899	0.223006	0.231291	0.357973	0.403379	0.232023	0.237028	0.235381
The King's S	0.571513	0.245621	0.319894	1	0.662118	0.402351	0.628466	0.332923	0.362033	0.21659	0.381307	0.644882	0.495078
La La Land	0.608298	0.250761	0.237586	0.662118	1	0.431774	0.719333	0.28155	0.321761	0.215607	0.4122	0.77368	0.446938
Boyhood	0.383359	0.290441	0.198899	0.402351	0.431774	1	0.43786	0.421998	0.314186	0.207583	0.343878	0.411769	0.370961
Inception	0.717668	0.240663	0.223006	0.628466	0.719333	0.43786	1	0.279072	0.321286	0.201837	0.557575	0.851802	0.482852
A Separatio	0.255281	0.389553	0.231291	0.332923	0.28155	0.421998	0.279072	1	0.314457	0.274884	0.238312	0.259016	0.318819
The Artist	0.320411	0.353563	0.357973	0.362033	0.321761	0.314186	0.321286	0.314457	1	0.303997	0.34742	0.291441	0.33704
The White R	0.192774	0.288218	0.403379	0.21659	0.215607	0.207583	0.201837	0.274884	0.303997	1	0.270703	0.213979	0.211352
Zero Dark Ti	0.595409	0.208368	0.232023	0.381307	0.4122	0.343878	0.557575	0.238312	0.34742	0.270703	1	0.495387	0.463023
Avatar	0.67338	0.233489	0.237028	0.644882	0.77368	0.411769	0.851802	0.259016	0.291441	0.213979	0.495387	1	0.473384
Spotlight	0.490684	0.240942	0.235381	0.495078	0.446938	0.370961	0.482852	0.318819	0.33704	0.211352	0.463023	0.473384	1

Appendix 11b: Item-Item Cosine Similarity of Normalized Movies Ratings, Class + DBMI Data (Partial of 50x50)

	The Social Net	A Prophet	Amour	The King's S	La La Land	Boyhood	Inception	A Separatio	The Artist	The White R	Zero Dark Ti	Avatar	Spotlight
The Social Net	1	0.015768	0.004335	-0.12165	-0.16894	-0.18326	-0.00291	-0.08181	0.026013	0.03248	-0.01152	-0.04514	-0.0226
A Prophet	0.015768	1	0.11994	0.077483	0.016389	-0.00022	-0.0814	-0.03353	-0.12647	0.165372	-0.03554	0.076997	-0.031
Amour	0.004335	0.11994	1	0.103091	-0.08541	0.014042	-0.03955	0.070074	-0.02242	0.085667	-0.05407	-0.01584	-0.028
The King's Spe	-0.12165	0.077483	0.103091	1	0.000363	-0.02504	-0.08092	0.06866	0.10043	0.011491	0.013103	-0.01653	0.028386
La La Land	-0.16894	0.016389	-0.08541	0.000363	1	-0.01571	0.046491	-0.02125	-0.06338	0.065263	-0.1128	0.030489	-0.09272
Boyhood	-0.18326	-0.00022	0.014042	-0.02504	-0.01571	1	-0.01992	0.243613	-0.01152	-0.12917	0.013317	-0.10581	0.091607
Inception	-0.00291	-0.0814	-0.03955	-0.08092	0.046491	-0.01992	1	-0.02647	-0.0535	-0.0207	-0.02465	-0.03605	-0.04992
A Separatio	-0.08181	-0.03353	0.070074	0.06866	-0.02125	0.243613	-0.02647	1	-0.13727	-0.1659	-0.07081	-0.17916	0.117388
The Artist	0.026013	-0.12647	-0.02242	0.10043	-0.06338	-0.01152	-0.0535	-0.13727	1	-0.01994	-0.07293	-0.0311	0.012266
The White Ribb	0.03248	0.165372	0.085667	0.011491	0.065263	-0.12917	-0.0207	-0.1659	-0.01994	1	0.002839	0.06902	-0.14789
Zero Dark Thir	-0.01152	-0.03554	-0.05407	0.013103	-0.1128	0.013317	-0.02465	-0.07081	-0.07293	0.002839	1	-0.02482	0.068215
Avatar	-0.04514	0.076997	-0.01584	-0.01653	0.030489	-0.10581	-0.03605	-0.17916	-0.0311	0.06902	-0.02482	1	-0.07358
Spotlight	-0.0226	-0.031	-0.028	0.028386	-0.09272	0.091607	-0.04992	0.117388	0.012266	-0.14789	0.068215	-0.07358	1

Appendix 12: Part 4 Calculations (New User Ratings with Some Data)

	Inception	Avatar	The Wolf of Wall Street
[The Social Network]	0.719116	0.687974	0.75407
[A Prophet]	0.21835	0.228056	0.239612
[Amour]	0.209932	0.195524	0.189689
[The King's Speech]	0.649641	0.646697	0.620413
[La La Land]	0.707379	0.774084	0.670436
[Boyhood]	0.431219	0.418917	0.388716
[Inception]	1	0.863107	0.814106
[A Separation]	0.287574	0.27848	0.300717
[The Artist]	0.317543	0.287278	0.308578
[The White Ribbon]	0.158477	0.162401	0.154672
[Zero Dark Thirty]	0.523176	0.457468	0.530656
[Avatar]	0.863107	1	0.78761
[Spotlight]	0.497648	0.48374	0.494049
[Precious]	0.288566	0.271756	0.311837
[The Tree of Life]	0.275999	0.2395	0.227474
[12 Years a Slave]	0.53044	0.511255	0.516062
[Blue is the Warmest Color]	0.369966	0.337936	0.333582
[Son of Saul]	0.125376	0.103493	0.1483
[Up in the Air]	0.533608	0.471962	0.497787
[Inglourious Basterds]	0.586449	0.56571	0.622727
[Mad Max: Fury Road]	0.664714	0.657573	0.671928
[Moonlight]	0.425366	0.394588	0.385699
[Gravity]		0.718996	0.669188
[Black Swan]		0.634356	0.639194
[Ida]		0.202036	0.175653
[Leviathan]		0.219192	0.192337
[The Wolf of Wall Street]		0.814106	0.78761
[True Grit]		0.317685	0.272438
[The Descendants]		0.359629	0.314313
[The Secret in Their Eyes]		0.215148	0.215984
[Life of Pi]		0.770414	0.786958
[Arrival]		0.6002	0.562826
[Call Me by Your Name]		0.455193	0.474729
[Winter's Bone]		0.103672	0.086387
[The Grand Budapest Hotel]		0.622723	0.620311
[Dunkirk]		0.634139	0.623451
[Inside Llewyn Davis]		0.246369	0.209305
[A Serious Man]		0.101577	0.090687
[Toy Story 3]		0.688166	0.713104
[Beasts of the Southern Wild]		0.169663	0.213227

	Inception	Avatar	Wolf	Amy	Sachi	Camille
	0.28856603	0.27175595	0.311836563	2	4	4
	0.53044034	0.511255	0.51606242	2	5	3
	0.66471372	0.6575727	0.671927793	4	5	4
	0.63982085	0.64593489	0.667147017	3	4	1
	0.68816567	0.71310449	0.660939182	3	3	4
Sum	2.81170661	2.79962303	2.827912976			

Avatar Rating for Amy $2.96 = (0.271*2 + 0.511*2 + 0.657*4 + 0.645*3 + 0.713*3) / 2.811$

$$\text{Predicted Rating} = \frac{\sum_1^j \text{CosineSimilarity}_{(i,j)} * \text{Rating}_j}{\sum_1^j \text{CosineSimilarity}_{(i,j)}}$$

i is the movie, whose rating is to be predicted (Inception, Avatar, Wolf of Wall Street)

j is the ratings of movies in the new data (Precious, 12 Years a Slave, Mad Max Fury Road ,Black Swan & Toy Story 3)