# **Flywheel**

### • What is the aim of the experiment?

To determine the mass of flywheel.

#### • What is flywheel?

A flywheel is a mechanical device which stores energy in the form of rotational momentum. Torque can be applied to a flywheel to cause it to spin, increasing its rotational momentum.

#### • What is the principle used?

The angular acceleration of a flywheel depends on the couple acting on it. By applying a known couple the angular acceleration and hence moment of inertia is calculated.

#### • Define angular displacement.

When a rigid body rotates about an axis, the angle through which any point on the body rotates is angular displacement.

Denoted by  $\theta$ .

Units: deg, rad, revolutions.

If a point P on the rigid body makes an angle  $\theta$  at an instant of time t then  $\theta(t)$  is the angular displacement at time t. See figure (1).

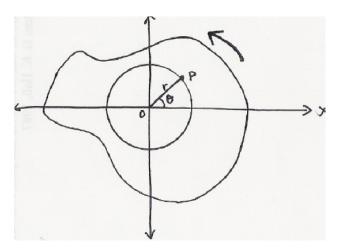


Figure 1: Angular displacement of point P.

### • Define angular velocity.

The rate of change of angular displacement with time is called angular velocity.

Denoted by  $\omega$ .

SI unit:  $rad s^{-1}$ .

If  $\theta(t_1)$  is the angular displacement of a point at time  $t_1$  and  $\theta(t_2)$  is the angular displacement of the same point at time  $t_2$ , then angular velocity is

$$\omega = \frac{\theta(t_2) - \theta(t_1)}{t_2 - t_1}.$$

When  $t_2 - t_1 = \Delta t$  is infinitesimally small, we have instantaneous angular velocity

$$\omega = \frac{\mathrm{d}\theta(t)}{\mathrm{d}t}.$$

## • Define angular acceleration.

The rate of change of angular velocity with time is called angular acceleration.

Denoted by  $\alpha$ .

SI unit:  $rad s^{-2}$ .

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$$\alpha = \frac{\omega(t_2) - \omega(t_1)}{t_2 - t_1}.$$

When  $t_2 - t_1 = \Delta t$  is infinitesimally small, we have instantaneous angular acceleration

$$\alpha = \frac{\mathrm{d}\omega(t)}{\mathrm{d}t} = \frac{\mathrm{d}^2\theta(t)}{\mathrm{d}t^2}.$$

#### • Define moment of inertia.

Quantitatively, it is the product of mass of a particle and square of its distance from the axis of rotation, summed over all particles of the rigid body.

If  $m_i$  is the mass of  $i^{th}$  particle and  $r_i$  is the distance of it from the axis of rotation then moment of inertia of the body about that axis is

$$I = \sum_{i} m_i r_i^2.$$

SI unit: kgm<sup>2</sup>.

• What is the moment of inertia of a circular disc about an axis perpendicular to its plane?

$$I = \frac{MR^2}{2},$$

where M is its mass,

R is its radius.

### • Does moment of inertia change when the axis of rotation is changed?

If mass distribution of the rigid body changes when axis of rotation is changed, then moment of inertia changes.

• Does moment of inertia depend on mass of the rigid body?

Yes.

#### • How is angular acceleration caused to the flywheel?

To cause angular acceleration, we need to apply torque. Torque is applied by attaching load to the flywheel via a thread. As the load is pulled downwards due to gravity, the flywheel accelerates.

• How is the angular acceleration of flywheel calculated?

$$\alpha = \frac{4\pi n}{t^2},$$

where n is the number of rotations completed by the flywheel, t is the time taken to complete n rotations.