ACM/ICPC CheatSheet

Puzzles

Contents

1 STL Useful Tips

1.1 Common libraries

```
#include<iostream>
#include<cstdio>
#include<cmath>
#include<string>
#include<queue>
#include<stack>
#include<vector>
#include<deque> // double ended queue
```

```
#include<priority_queue> // priority queue
#include <functional> // for hash
#include<algorithm>
#include<cstdlib> // random
#include<ctime>
#include<sstream>
#include<climits> // all useful constants
```

1.2 Useful constant

```
INT_MIN
INT_MAX
LONG_MIN
LONG_MAX
LLONG_MIN
LLONG_MAX
(~0u) // infinity (for long and long long)
      // use (~0u)>>2 for int.
```

1.3 Space waster

```
// consider to redefine data types to void data range problem
#define int long long // make everyone long long
#define double long double // make everyone long double

// function definitions

#undef int // main must return int
int main(void)
#define int long long // redefine int

// rest of program
```

1.4 Initialize array with predefined value

```
// for 1d array, use STL fill_n or fill to initialize array
fill(a, a+size_of_a, value)
fill_n(a, size_of_a, value)
// for 2d array, if want to fill in 0 or -1
memset(a, 0, sizeof(a));
  // otherwise, use a loop of fill or fill_n through every a[i]
  fill(a[i], a[i]+size_of_ai, value) // from 0 to number of row.
```

1.5 Modifying sequence operations

```
void copy(first, last, result);
void swap(a,b);
void swap(first1, last1, first2); // swap range
void replace(first, last, old_value, new_value); // replace in range
void replace_if(first, last, pred, new_value); // replace in conditions
  // pred can be represented in function
  // e.x. bool IsOdd (int i) { return ((i%2)==1); }
void reverse(first, last); // reverse a range of elements
void reverse_copy(first, last, result); // copy a reverse of range of elements
void random_shuffle(first, last); // using built-in random generator to shuffle array
```

1.6 Merge

```
// merge sorted ranges
void merge(first1, last1, first2, last2, result, comp);
// union of two sorted ranges
void set_union(first1, last1, first2, last2, result, comp);
// intersection of two sorted ranges
void set_interaction(first1, last1, first2, last2, result, comp);
// difference of two sorted ranges
void set_difference((first1, last1, first2, last2, result, comp);
```

1.7 String

```
// Searching
unsigned int find(const string &s2, unsigned int pos1 = 0);
unsigned int rfind(const string &s2, unsigned int pos1 = end);
unsigned int find_first_of(const string &s2, unsigned int pos1 = 0);
unsigned int find_last_of(const string &s2, unsigned int pos1 = end);
unsigned int find_first_not_of(const string &s2, unsigned int pos1 = 0);
unsigned int find_last_not_of(const string &s2, unsigned int pos1 = end);
// Insert, Erase, Replace
string& insert(unsigned int pos1, const string &s2);
string& insert(unsigned int pos1, unsigned int repetitions, char c);
string& erase(unsigned int pos = 0, unsigned int len = npos);
string& replace(unsigned int pos1, unsigned int len1, const string &s2);
string& replace(unsigned int pos1, unsigned int len1, unsigned int repetitions, char c);
// String streams
stringstream s1;
int i = 22;
s1 << "Hello world! " << i;
cout << s1.str() << endl;
```

1.8 Heap

```
template <class RandomAccessIterator>
  void push_heap (RandomAccessIterator first, RandomAccessIterator last);
template <class RandomAccessIterator, class Compare>
  void push_heap (RandomAccessIterator first, RandomAccessIterator last,
          Compare comp);

template <class RandomAccessIterator>
  void pop_heap (RandomAccessIterator first, RandomAccessIterator last);
template <class RandomAccessIterator, class Compare>
  void pop_heap (RandomAccessIterator first, RandomAccessIterator last,
          Compare comp);

template <class RandomAccessIterator>
  void make_heap (RandomAccessIterator first, RandomAccessIterator last);
template <class RandomAccessIterator, class Compare>
  void make_heap (RandomAccessIterator first, RandomAccessIterator last,
          Compare comp );

template <class RandomAccessIterator>
  void sort_heap (RandomAccessIterator first, RandomAccessIterator last);
```

```
template <class RandomAccessIterator, class Compare>
  void sort_heap (RandomAccessIterator first, RandomAccessIterator last,
          Compare comp);
template <class RandomAccessIterator>
  RandomAccessIterator is_heap_until (RandomAccessIterator first,
                    RandomAccessIterator last);
template <class RandomAccessIterator, class Compare>
  RandomAccessIterator is_heap_until (RandomAccessIterator first,
                    RandomAccessIterator last
                    Compare comp);
```

1.9 Sort

```
void sort(iterator first, iterator last);
void sort(iterator first, iterator last, LessThanFunction comp);
void stable_sort(iterator first, iterator last);
void stable_sort(iterator first, iterator last, LessThanFunction comp);
void partial_sort(iterator first, iterator middle, iterator last);
void partial_sort(iterator first, iterator middle, iterator last, LessThanFunction comp);
bool is_sorted(iterator first, iterator last);
bool is_sorted(iterator first, iterator last, LessThanOrEqualFunction comp);
// example for sort, if have array x, start_index, end_index;
sort(x+start_index, x+end_index);
```

1.10 Permutations

```
bool next_permutation(iterator first, iterator last);
bool next_permutation(iterator first, iterator last, LessThanOrEqualFunction comp);
bool prev_permutation(iterator first, iterator last);
bool prev_permutation(iterator first, iterator last, LessThanOrEqualFunction comp);
```

1.11 Searching

```
// will return address of iterator, call result as *iterator;
iterator find(iterator first, iterator last, const T &value);
iterator find_if(iterator first, iterator last, const T &value, TestFunction test);
bool binary_search(iterator first, iterator last, const T &value);
bool binary_search(iterator first, iterator last, const T &value, LessThanOrEqualFunction comp);
```

1.12 Random algorithm

```
srand(time(NULL));
// generate random numbers between [a,b)
rand() % (b - a) + a;
// generate random numbers between [0,b)
rand() % b;
// generate random permutations
random_permutation(anArray, anArray + 10);
random_permutation(aVector, aVector + 10);
```

2 Number Theory

2.1 Max or min

```
int max(int a, int b) { return a>b ? a:b; }
int min(int a, int b) { return a<b ? a:b; }
```

2.2 Greatest common divisor — GCD

```
int gcd(int a, int b)
{
  if (b==0) return a;
  else return gcd(b, a%b);
}
```

2.3 Least common multiple — LCM

```
int lcm(int a, int b)
{
  return a*b/gcd(a,b);
}
```

2.4 If prime number

```
bool prime(int n)
{
  for (int i=2;i*i<=n;i++)
    if (n%i==0) return false;
  return true;
}
```

2.5 Leap year

```
bool isLeap(int n)
{
  if (n%100==0)
    if (n%400==0) return true;
    else return false;

  if (n%4==0) return true;
  else return false;
}
```

2.6 $a^b \bmod p$

```
long powmod(long base, long exp, long modulus) {
  base %= modulus;
  long result = 1;
  while (exp > 0) {
    if (exp & 1) result = (result * base) % modulus;
    base = (base * base) % modulus;
    exp >>= 1;
  }
  return result;
}
```

2.7 Factorial mod

```
//n! mod p
int factmod (int n, int p) {
  long long res = 1;
  while (n > 1) {
    res = (res * powmod (p-1, n/p, p)) % p;
    for (int i=2; i<=n%p; ++i)
      res=(res*i) %p;
    n /= p;
  }
  return int (res % p);
}
```

2.8 Generate combinations

```
// n>=m, choose M numbers from 1 to N.
void combination(int n, int m)
{
  if (n<m) return ;
  int a[50]={0};
  int k=0;

  for (int i=1;i<=m;i++) a[i]=i;
  while (true)
  {
    for (int i=1;i<=m;i++)
      cout << a[i] << " ";
    cout << endl;

    k=m;
    while ((k>0) && (n-a[k]==m-k)) k--;
    if (k==0) break;
    a[k]++;
    for (int i=k+1;i<=m;i++)
      a[i]=a[i-1]+1;
  }
}
```

3 Searching Algorithms

3.1 Find rank k in array

4 Dynamic Programming

4.1 Knapsack problems

4.2 Longest common subsequence

```
int dp[1001][1001];

int lcs(const string &s, const string &t)
{
  int m = s.size(), n = t.size();
  if (m == 0 || n == 0) return 0;
  for (int i=0; i<=m; ++i)
    dp[i][0] = 0;
```

```
  for (int j=1; j<=n; ++j)
    dp[0][j] = 0;
  for (int i=0; i<m; ++i)
    for (int j=0; j<n; ++j)
      if (s[i] == t[j])
            dp[i+1][j+1] = dp[i][j]+1;
          else
            dp[i+1][j+1] = max(dp[i+1][j], dp[i][j+1]);
  return dp[m][n];
}
```

4.3 Maximum submatrix

5 Trees

5.1 Tree representation in array

5.2 Tree traversal

6 Graph Theory

6.1 Flood fill algorithm

```
//component(i) denotes the
//component that node i is in
void flood_fill(new_component)
  do
    num_visited = 0
    for all nodes i
      if component(i) = -2
      num_visited = num_visited + 1
      component(i) = new_component

    for all neighbors j of node i
      if component(j) = nil
        component(j) = -2
  until num_visited = 0

void find_components()
  num_components = 0
  for all nodes i
    component(node i) = nil
  for all nodes i
    if component(node i) is nil
      num_components = num_components + 1
      component(i) = -2
      flood_fill(component num_components)
```

6.2 SPFA — shortest path

6.3 Floyd-Warshall algorithm – shortest path of all pairs

```
// map[i][j]=infinity at start
void floyd()
{
  for (int k=1; k<=n; k++)
    for (int i=1; i<=n; i++)
      for (int j=1; j<=n; j++)
```

```
        if (i!=j && j!=k && i!=k)
          if (map[i][k]+map[k][j]<map[i][j])
            map[i][j]=map[i][k]+map[k][j];
}
```

6.4 Prim — minimum spanning tree

```
const int N=500;
unsigned long D[N], Q[N][N];// initial: 4294967295 without linking
bool cmp(int x,int y){return D[x]<D[y];}

unsigned long Prim(void)
{
  int i=N;
  list<int> L;
  for(memcpy(D,Q[0],sizeof(D));--i;L.push_back(i));
  for(list<int>::iterator p;!L.empty();)
  for(p=min_element(L.begin(),L.end(),cmp),i=*p,L.erase(p),p=L.end();L.end()!=++p;D[*p]<?=Q[i][*p]);
  return  accumulate(1+D,N+D,0LU);
}
```

6.5 Eulerian path

6.6 Topological sort