Using Gauss-Jordan elimination, solve the following problems numerically. All the necessary functions will go in your own library (file) while the main code will simply read the input i.e. initialization, call relevant functions and write the solutions.

1. Use Gauss-Jordon elimination to find the solution of the following system of linear equations, [2]

$$x + y + z + w = 13$$

$$2x + 3y - w = -1$$

$$-3x + 4y + z + 2w = 10$$

$$x + 2y - z + w = 1$$

2. Use Gauss-Jordon elimination to find the solution of the following system of linear equations, [3]

$$2y - 3z = -1$$
$$x + z = 0$$
$$x - y = 3$$

3. Find the inverse of the following invertible matrix using Gauss-Jordon elimination. Keep only up to 2 places in decimal. Verify that your solution is indeed the inverse of the given matrix. [3]

$$\left(\begin{array}{ccc}
0 & 2 & 1 \\
4 & 0 & 1 \\
-1 & 2 & 0
\end{array}\right)$$

4. Use Gauss-Jordon elimination to determine the determinant of the matrix, [2]

$$\left(\begin{array}{ccccc}
1 & 4 & 2 & 3 \\
0 & 1 & 4 & 4 \\
-1 & 0 & 1 & 0 \\
2 & 0 & 4 & 1
\end{array}\right)$$