

Experiment No 3

Aim : Implementation and analysis of RSA cryptosystem and digital signature scheme using RSA.

Lab Outcome :

LO2 : Demonstrate Key management, distribution and user authentication.

Theory :

1. Explain the steps of RSA key generation?

RSA (Rivest-Shamir-Adleman) is a widely used asymmetric cryptographic algorithm that relies on a pair of keys: a public key and a private key. RSA key generation involves a series of steps that ensure secure communication and data encryption. Below, I'll provide a detailed explanation of the key generation process:

1. Choosing Prime Numbers (p and q): The first step in RSA key generation is to select two distinct prime numbers, usually denoted as p and q. These prime numbers are critical to the security of the algorithm. They need to be large and chosen randomly to prevent attackers from factoring the modulus and breaking the encryption.
2. Calculating Modulus (n): The modulus (n) is computed as the product of the two prime numbers: $n = p * q$. The modulus is used in both the public and private keys. It provides the size of the "space" in which the encryption operates, making the encryption stronger with larger values of n.
3. Calculating Euler's Totient Function ($\phi(n)$): Euler's totient function ($\phi(n)$) is calculated as $\phi(n) = (p - 1) * (q - 1)$. This function is crucial for ensuring that the public and private keys are relatively prime. $\phi(n)$ represents the count of numbers less than n that are coprime to n.
4. Selecting Public Exponent (e): The public exponent (e) is a small odd integer that is coprime to $\phi(n)$. A common choice for e is 65537 ($2^{16} + 1$). This choice of e provides good security properties while ensuring efficient encryption and decryption operations.
5. Calculating Private Exponent (d): The private exponent (d) is computed as the modular multiplicative inverse of e modulo $\phi(n)$. In other words, it satisfies the equation $(e * d) \% \phi(n) = 1$. The private exponent d is what allows the decryption of messages encrypted with the public key.

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6. Public Key Generation: The public key consists of the pair (e, n) . It is distributed to anyone who wishes to send an encrypted message to the key owner. The public key is used for encrypting messages, ensuring only the private key holder can decrypt them.

7. Private Key Generation: The private key consists of the pair (d, n) . This key must be kept secret and secure. The private key is used for decrypting messages encrypted with the corresponding public key. Losing the private key could compromise the security of encrypted communications.

The RSA key generation process is fundamental to the security and effectiveness of RSA encryption. It leverages the mathematical properties of prime numbers and modular arithmetic to create a secure communication channel between parties. The strength of RSA lies in the difficulty of factoring large semiprime numbers (the product of two large prime numbers), which makes it practically impossible for attackers to deduce the private key from the public key.

2. Explain the steps of Digital signature generation and verification process:

Digital signatures play a crucial role in ensuring data integrity, authenticity, and nonrepudiation in the digital world. They provide a way to verify that a digital document or message was indeed generated by a specific sender and has not been tampered with during transmission. The process involves two main steps: digital signature generation and digital signature verification.

Digital Signature Generation:

1. Hashing the Message: The sender begins by creating a cryptographic hash of the message they want to sign. A hash function, such as SHA-256, is used to produce a fixed-size digest that uniquely represents the content of the message.
2. Private Key Encryption: The sender then encrypts the hash value using their private key. This encrypted hash forms the digital signature. The use of the private key ensures that only the sender, who possesses the corresponding private key, can create the signature.
3. Attaching the Signature: The encrypted hash (digital signature) is attached to the original message. This combination forms the digitally signed message. Any alteration to the message will result in a different hash, making it evident that the message has been tampered with.

Digital Signature Verification:

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1. Hashing the Received Message: The recipient of the digitally signed message starts by computing the hash value of the received message using the same hash function as the sender. This generates a digest that represents the content of the received message.
2. Public Key Decryption: The recipient then decrypts the digital signature using the sender's public key. This process yields the original hash value that the sender encrypted using their private key during the signature generation.
3. Comparing Hashes: The recipient compares the decrypted hash value with the hash value they calculated from the received message. If the two hash values match, it indicates that the message has not been tampered with and that the signature is valid. A mismatch suggests either tampering or the use of an incorrect signature.

Benefits and Security:

The digital signature process provides several benefits:

- Data Integrity: Any alteration to the message or document will lead to a mismatch between the computed hash and the decrypted hash in the signature.
- Authenticity: The use of the sender's private key ensures that only the sender could have created the signature.
- Non-Repudiation: The sender cannot deny having sent the digitally signed message since the signature is tied to their private key.

Output:

Digital Signature:

The screenshot shows a browser window with multiple tabs open. The active tab is titled "Digital Signatures Scheme" from "Virtual Labs". The page content includes fields for plaintext ("attackpostponed") and hash algorithm ("SHA-1"). The "Hash output(hex)" field contains the value "d1852d8bbfb03f7450fbecdb69742ec9f16af37f3". Below this, there's a section for RSA input with a hex value "31b4ef479d501506cdfed8dcea64037e20ddf844ef32df7f1dc479570d6482111646adf07ed40fe6eaf3b9b6e66fc82df6a2c840928528dafbe13574cd61533e" and an "Apply RSA" button. Further down, there's a "Digital Signature(base64)" field containing "MbTvR51QFQbN/tjcgmQDfiDd+ETvMt9/HcR5Vw1kgHEWRq3wftQP5urzubbmb8gt9qLIQJKFKNr74TV0zWFTPg==". The browser's status bar at the bottom shows the date as 25-08-2023.

This screenshot shows the same digital signatures simulation page. It displays a "Digital Signature(hex)" field with the value "31b4ef479d501506cdfed8dcea64037e20ddf844ef32df7f1dc479570d6482111646adf07ed40fe6eaf3b9b6e66fc82df6a2c840928528dafbe13574cd61533e". Below it is a "Digital Signature(base64)" field with the value "MbTvR51QFQbN/tjcgmQDfiDd+ETvMt9/HcR5Vw1kgHEWRq3wftQP5urzubbmb8gt9qLIQJKFKNr74TV0zWFTPg==". A "Status" field indicates "Time: 4ms". Under the "RSA public key" section, there's a "Public exponent (hex, F4=0x10001)" field with the value "3" and a "Modulus (hex)" field with the value "BC86E3DC782C446EE756B874ACECF2A15E613021EAF1ED5EF295BEC2BED899D26FE2EC896BF9DE84FE381AF67A787CB848D85235E72AB595ABF8FE840D5F8DB". At the bottom, there are buttons for "1024 bit", "1024 bit (e=3)", "512 bit", and "512 bit (e=3)". The browser's status bar at the bottom shows the date as 25-08-2023.

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RSA key generation and decode

Private exponent (hex):
7daf4292fac82d9f44e47af87348a1c0b9440cac1474bf394a1b929d729e5bbc
f482f29a9300e11b478c091f7e5cad3f8edae2effe3164d7e0eeada87ee817b

P (hex):
ef3fc61e21867a900e01ee4b1ba69f5403274ed27656da03ed88d7902cce693f

Q (hex):
c9b9fcc298b7d1af568f85b50e749539bc01b10a68472fe1302058104821cd65

D mod (P-1) (hex):
9f7fd9696baefc6009569edcbd19bf8d576f89e1a439e6ad4905e50ac8899b7f

D mod (Q-1) (hex):
867bfd7107a8bca39b503ce09a30e267d567606f02f7540cac03ab5856bde43

1/Q mod P (hex):
412db551d93ee1bd7dccafc63d7a6d031fc66035ecc630ddf75f949a378cd9d

Decrypted Plaintext (string):
chandrayaanislanded

Status:
Decryption Time: 4ms

RSA private key

1024 bit 1024 bit (e=3) 512 bit 512 bit (e=3) Generate bits = 512

Modulus (hex):
BC86E3DC782C446EE756B874ACECF2A115E613021EAF1ED5EF295BEC2BED899D
26FE2EC896BF9DE84FE381AF67A7B7CB848D85235E72AB595ABF8FE840D5F8DB

Public exponent (hex, F4=0x10001):
3

Private exponent (hex):
7daf4292fac82d9f44e47af87348a1c0b9440cac1474bf394a1b929d729e5bbc
f482f29a9300e11b478c091f7e5cad3f8edae2effe3164d7e0eeada87ee817b

Public-Key Cryptosystems (PKCSv1.5)

Plaintext (string):
chandrayaanislanded

Ciphertext (hex):
714804a48356c44f88d6e546ea716ce84ed9138718330fb914f90922887f9b8d
3afe405eadcd12e8acf21a3043ace8ed37640edc56f2f50cb8b56b924c5ef73b

decrypt

Decrypted Plaintext (string):
chandrayaanislanded

Status:
Decryption Time: 4ms

RSA private key

Modulus (hex):
1024 bit 1024 bit (e=3) 512 bit 512 bit (e=3) Generate bits = 512

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Conclusion:

Learnt about RSA scheme and RSA cryptosystem , explored steps involved in digital key generation and verification , generated and verified digital signature using software and also implemented RSA scheme.

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