

Roll No. 2182300201

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EW-165**B.E. IIIrd Semester (New Scheme) CSE****Examination, 2021-22****Engineering Mathematics-II****Paper - CS-301****Time : 3 Hours]****[Maximum Marks : 60****Note :-** Attempt all questions: All questions carry equal Marks.

Attempt any two from each question.

1. (a) Solve : $\tan x \cdot \sin^2 y \, dx + \cos^2 x \cdot \cot y \, dy = 0$

(b) Solve : $(D^2 + 4D - 12)y = e^{2x} \cdot (x - 1); D \equiv \frac{d}{dx}$

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(c) Solve: $\frac{dx}{dt} - 7x + y = 0$ and $\frac{dy}{dt} - 2x - 5y = 0$.

2. (a) Solve $x^2y^{11} + xy^1 - y = 0$, given that $x + \frac{1}{x}$ is one integral.

(b) Give working rule for solving second order Linear differential equation by the method of variation of parameters.

(c) Solve: $y^{11} - (2 \tan x) y^1 + 5y = 0$ using normal form.

3. (a) Solve: $p(1+q) = qz$

(b) Solve: $(Dx^2 + Dy^2)z = x^2y^2$

(c) Solve: $p^2 - q^2 = x - y$

4. (a) Show that the function $z/|z|$ is not analytic any where.

(b) Using Cauchy's integral formula, evaluate $\int_C \frac{e^{2z}}{(z+1)^4} dz$,

where C is the circle $|z| = 3$.

(c) Explain the concept of analytic functions and harmonic conjugate. Give suitable examples.

5. (a) Explain the concept of divergence of a vector field. Give its physical interpretation.

(b) Find the directional derivative of $f(x, y) = x^2y^3 + xy$ at $(2, 1)$ in the direction of a unit vector which makes an angle of 60° with the x -axis.

(c) Find the gradient of $f(x, y, z) = xy + 2yz - 8$ at $(3, -2, 1)$.
