



INFORMATION THEORY (ELL714)

ASSIGNMENT 2

JOINT TYPICALITY BASED CHANNEL DECODER

Submitted To:

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1 Objective

The aim of this assignment is to check if a good decoding scheme can be performed using AEP in a Binary Symmetric Channel and to verify the coding theorem.

2 Introduction

The joint typicality is described by the following conditions. All three conditions must be satisfied for any two sequences at the input and the output of a channel to be jointly typical

$$A_{\epsilon}^{(n)} = \{(x^n, y^n) \in X^n \times Y^n : \\ \left| \frac{-1}{n} \log(p(x^n) - H(x)) \right| < \epsilon \\ \left| \frac{-1}{n} \log(p(y^n) - H(y)) \right| < \epsilon \\ \left| \frac{-1}{n} \log(p(x^n, y^n) - H(x, y)) \right| < \epsilon \}$$

3 The experiments

1. For each $n \in \{10, 100, 500, 1000, \dots\}$, obtained a random codebook C_n containing $\lceil 2^{nR} \rceil$ codewords. Independently generated binary numbers using an underlying uniform probability mass function $p(x)=0.5$.
2. Using C_n , transmit codewords with uniform distribution over the channel.
3. At the receiver side, observed the binary sequences and then decoded the input message using a decoder based on joint typicality. Pick $\epsilon = 0.01$ when defining joint typicality.
- 4) Through simulations, compute the average probability of error of the decoder. Also, compute how many times the decoder is unable to decode the message?
- 5) Plotted the average probability of error of the decoder against different values of n .
- 6) Commented on the plot change when the value of ϵ was changed.

4 Outputs and observations

Figure 1. shows the typical output terminal. When n was varied from 100 through

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ajey@Cosmos:~/Desktop$ python3 asignment2.py
The Capacity of the channel is:0.029049405545331308bits/s
The Rate chosen is =  $0.5 \cdot C = 0.014524702772665654$ bits/s
Length of a sequence is = 10
Total number of sequences in the codebook: 2

The Random Codebook is:

(0, 1, 1, 0, 0, 0, 0, 1, 1, 0)
(0, 0, 0, 1, 0, 0, 0, 0, 0, 1)

The Recieved output is:

[1 0 1 1 1 0 0 0 0]
[0 0 0 1 0 0 1 0 0 1]
No.of failures = 2
Percentage of failure = 100.0

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Figure 1: A typical output screen

1000, I found the decoder behaving as in Figure.2. It confirms the idea that as n increases, the error possibility of error becomes smaller. Similarly, the observation

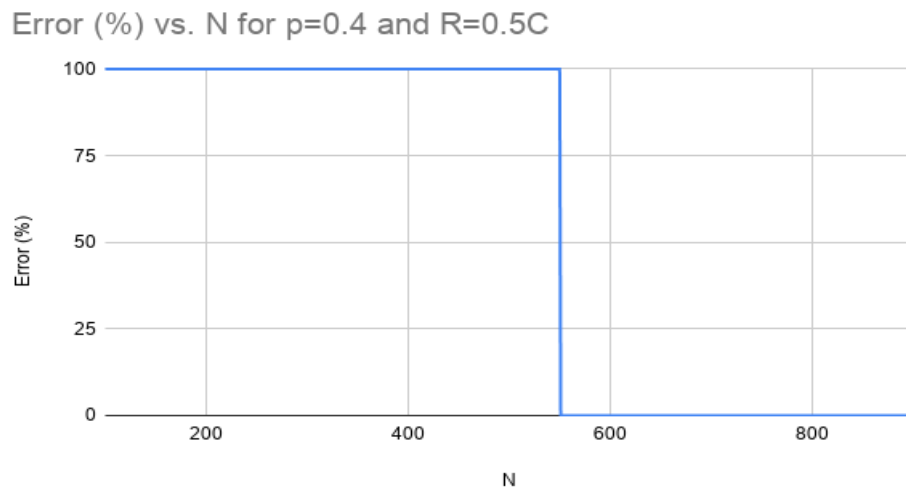


Figure 2: Error Vs N chart, $p=0.4$, $R=0.5C$

plots for when ϵ was changed is shown in Figure 3. for $\epsilon = 0.1$, the change in error rate is shown in blue. for $\epsilon = 0.01$, the change in error rate is shown in yellow. When ϵ is increased, the number of bits required to achieve joint typicality increases.

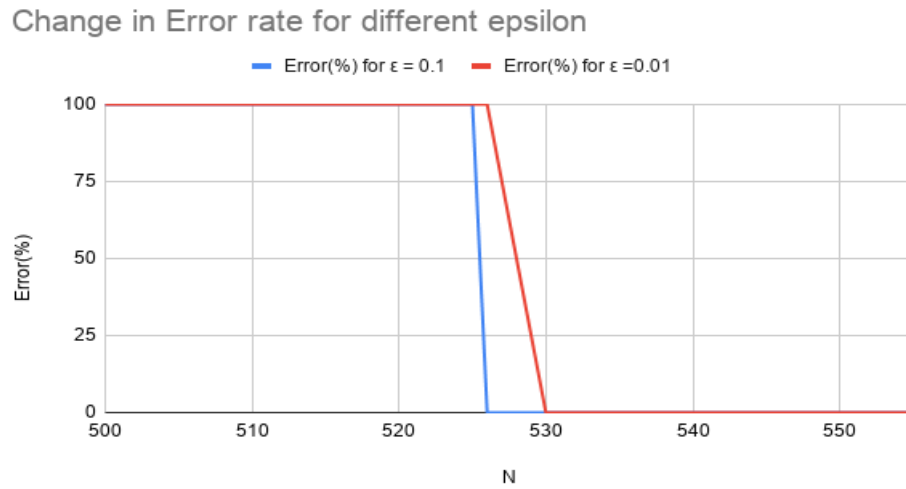


Figure 3: Error Vs N chart for different values of ϵ