Force equations 
$$m \begin{cases} \dot{u} + qw - vv \end{cases} = (T_{\alpha_1} + T_{\alpha_2}) - cw - \beta \int \sin \theta + \sigma_2$$

 $D = \frac{1}{2} C_D P A_c V^2$   $S = 1000 \text{kg/m}^3$ ,  $A \rightarrow Prontal area$   $Cd \rightarrow d\text{kg}$  coefficient

$$(X, Y, Z, O, \emptyset, \varphi) \rightarrow \text{output}$$
  
 $(T_{Z_1}, T_{Z_2}, T_{Z_1}, T_{Z_2}) \rightarrow \text{Inputs}$ 

$$\begin{bmatrix} P \\ Q \\ 7 \end{bmatrix} = \begin{bmatrix} 1 & 0 & -sin(0) \\ 0 & (\omega(\phi) & (\omega(0)) \cdot sin(\phi) \\ 0 & -sin(0) & (\omega(0)) \cdot (\omega(\phi)) \end{bmatrix} \begin{bmatrix} \dot{\phi} \\ \dot{\phi} \\ \dot{\psi} \end{bmatrix}$$

L = 
$$p 1_{\pi\pi} + 79 ( P_{22} - P_{44}) = 0 \Rightarrow p = \frac{79 ( 344 - P_{22})}{1_{\pi\pi}}$$

M =  $9 3_{44} + 79 ( P_{22} - P_{42}) \Rightarrow p = \frac{79 ( 944 - P_{22})}{1_{\pi\pi}}$ 

Torque equations

 $9 2_{44} + 79 ( P_{22} + P_{21} ( P_{24} - P_{21})) = (T_{21} + T_{22}) = P_{21} + T_{21} + T_{21} + T_{22} + T_{21} + T_{22} + T_{21} + T_{22} + T_{21} + T_{22} + T_{22} + T_{21} + T_{22} + T_{22} + T_{21} + T_{22} + T_{22} + T_{22} + T_{22} + T_{22} + T_{21} + T_{22} + T_{22$ 

Body have and inestral frame concepts

Consider Body Rome,

Let (A) in the body frame (regnestent allos)

body frame rotating erround 2' and with an omgalas

(01,0). (in)

$$\frac{2\left(\frac{dA_{x}}{de}\right)^{2}+\frac{di}{de}}{\frac{1}{de}}\frac{A_{x}}{A_{x}}+\left(\frac{dA_{y}}{de}\right)^{2}+\frac{di}{de}}{\frac{1}{de}}\frac{A_{y}}{A_{y}}$$

$$+\left(\frac{dA_{z}}{de}\right)^{2}+\frac{di}{de}\frac{A_{z}}{de}$$

consider, is solated to i with with

$$di = di = di = di = di = di$$

direction of  $di = \hat{\omega} \times \hat{i}$ 

so, 
$$d\vec{i} = (do) \cdot \hat{\omega} \times \hat{i}$$

$$\frac{d\vec{i}}{dt} = (do) \cdot \hat{\omega} \times \hat{i}$$

$$\frac{d\vec{i}}{dt} = (do) \cdot \hat{\omega} \times \hat{i}$$

$$\frac{d\vec{i}}{dt} = (do) \cdot \hat{\omega} \times \hat{i}$$

A' in body frame  $\vec{A} = A_{x} + A_{y} + A_{z} + A_{z}$ 

```
%initializations
clear pos x pos y pos z ori phi ori theta ori si
clc
M=20; %mass of 26 Kg
g=9.8; %9.8 m/s2
W=M*g; %Weight of the body
B=196.2; %Bouyancy force
A=0.045; %frontal area
C=0.82; %Drag coefficient
Ro=997; %density of the water
dt=0.2; %time step
zp=0.1; %z coordinate of the propulsive force
1z1=0.1; %
1z2=0.01;
1x1=0.12;
1x2=0.12;
yp=1x1+1x2;
%moments of inertia
Ixx=10;
Iyy=10;
Izz=10;
%Euler angles
theta=0.01;
phi=0.01;
si=0.01;
%input thrust
15];
10];
Tz1=5;
Tz2=5;
%angular velocities in body frame
p=0;
q=0;
r=0;
%velocities in body frame
u = 0;
v=0;
w=0;
%velocities in inertial frame
x_dot=0;
```

```
y_dot=0;
z dot=0;
%pose in inertial frame
x=0;
y=0;
z=0;
for i=1:28
%drag forces
Dx=0.5*C*Ro*A*(u^2);
Dy=0.5*C*Ro*A*(v^2);
Dz=0.5*C*Ro*A*(w^2);
%derivative of velocities in body frame from equation of motion
u dot=(((Tx1(i)+Tx2(i))-(W-B)*sin(theta)-Dx)/M)-(q*w-r*v);
v^{-}dot=(((W-B)*cos(theta)*sin(phi)-Dy)/M)-(r*u-p*w);
w = dot = (((W-B) * cos(theta) * cos(phi) + (Tz1+Tz2) - Dz)/M) - (p*v-q*u);
\mbox{\ensuremath{\mbox{$\%$}}} derivatives of angular velocities in body frame
p dot=((Iyy-Izz)*r*q)/Ixx;
q dot=((Tx1(i)-Tx2(i))*zp+(Tz1*lz1-Tz2*lz2)+r*p*(Izz-Ixx))/Iyy;
r dot=((Tx1(i)-Tx2(i))*yp+(Ixx-Iyy)*p*q)/Izz;
%velocities in body frame
u=u+(u\_dot*dt);
v=v+(v_dot*dt);
w=w+(w dot*dt);
wo=[u;v;w];
%angular velocities
p=p+(p_dot*dt);
q=q+(q\_dot*dt);
r=r+(r_dot*dt);
ao=[p;q;r];
%rotation matrix
R=[\cos(si)*\cos(theta)\cos(si)*\sin(theta)*\sin(phi)-\sin(si)*\cos(phi)]
sin(si)*sin(phi)+cos(si)*cos(phi)*sin(theta);
    sin(si)*cos(theta) cos(si)*cos(phi)+sin(phi)*sin(theta)*sin(si)
sin(theta)*sin(si)*cos(phi)-cos(si)*sin(phi);
    -sin(theta) cos(theta)*sin(phi) cos(theta)*cos(phi)];
%velocites in inertial frame
X dot=R*wo;
x dot=X dot(1);
y = dot = X = dot(2);
z dot=X dot(3);
%rotation matrix for angular velocities
```

```
T=[1 \ 0 \ -\sin(theta);
    0 cos(phi) cos(theta)*sin(phi);
    0 -sin(theta) cos(theta)*cos(phi)];
%for derivative of angular velocities in inertial frame
Ao=inv(T) *ao;
phi_dot=Ao(1);
theta_dot=Ao(2);
si dot=Ao(3);
%euler angles
phi=phi+(phi_dot*dt);
theta=theta+(theta dot*dt);
si=si+(si_dot*dt);
if(phi>180)
    phi=180;
end
if (phi<-180)</pre>
    phi=-180;
end
if (theta>90)
     theta=90;
if (theta<-90)</pre>
     theta=-90;
 end
if(si>360)
     si=360;
end
if(si<0)
    si=0;
 end
%pose in inertial frame
x=x+(x dot*dt);
y=y+(y_dot*dt);
z=z+(z_dot*dt);
pos x(i)=x;
pos_y(i) = y;
pos_z(i)=z;
ori_phi(i)=phi;
ori_theta(i)=theta;
ori si(i)=si;
```

end

## For the analysis, first we done the modelling in XY plane (2D analysis)

## Matlab code:

```
%initializations
clear pos_x pos_y ori_si vel_u vel_v
%%for the visualization of an object moving in 2D plane
close(figure(1))
ax = axes('XLim', [-50 50], 'YLim', [-50 50]);
view(2)
grid on;
[x,y] = cylinder([.2 0.2]);
h(1) = surface(y,x,'FaceColor','yellow');
h(2) = surface(y,x,'FaceColor','blue');
grid on
xlabel('X');
ylabel('Y');
t = hgtransform('Parent',ax);
set(h, 'Parent',t)
drawnow
응응
k=1000;
M=20; %mass of 26 Kg
g=9.8; %9.8 m/s2
W=M*g; %Weight of the body
B=196.2; %Bouyancy force
A=0.045; %frontal area
C=0.5; %Drag coefficient
Ro=997; %density of the water
dt=0.1; %time step
lx1=0.12; %length between thruster1 mounted point and centre of mass.
1x2=0.12;
yp=1x1+1x2;
%moments of inertia
Izz=10; %not a calculated value.You need to calculate it :)
%Euler angles
si=0.01;
%input thrust
Tx2=15;
Tx1=15;
%angular velocities in body frame
r=0;
```

```
%velocities in body frame
u=0;
v=0;
%velocities in inertial frame
x dot=0;
y = dot = 0;
%pose in inertial frame
x=0;
y=0;
ti=0;
for i=1:k
%drag forces
Dx=0.5*C*Ro*A*(u^2);
Dy=0.5*C*Ro*A*(v^2);
%derivative of velocities in body frame from equation of motion
u dot=(r*v);
v_{dot} = (((Tx1+Tx2)-Dy)/M)-(r*u);
%derivatives of angular velocities in body frame
r_dot=((Tx1-Tx2)*yp)/Izz;
%velocities in body frame
u=u+(u_dot*dt);
v=v+(v_dot*dt);
wo=[u;v];
%angular velocities
r=r+(r_dot*dt);
ao=r;
%rotation matrix
R=[\cos(si) - \sin(si);
    sin(si) cos(si)];
%velocites in inertial frame
X dot=R*wo;
x_{dot=X_{dot}(1)};
y_dot=X_dot(2);
%for derivative of angular velocities in inertial frame
si dot=r;
%euler angles
```

```
si=si+(si dot*dt);
%pose in inertial frame
x=x+(x_dot*dt);
y=y+(y_dot*dt);
pos x(i)=x;
pos y(i) = y;
vel_u(i)=u;
vel_v(i) = v;
ori si(i)=si;
dragF(i) = Dy;
%for plot in 2D plane
translation=makehgtform('translate',[pos x(i),pos y(i),0]);
zrotational=makehgtform('zrotate', ori si(i));
set(t, 'matrix', translation*zrotational);
pause(0.1)
end
pos_x=pos_x';
pos_y=pos_y';
ori_si=ori_si';
vel_u=vel_u';
vel_v=vel_v';
dragF=dragF';
time=0:0.1:9.9;
figure(2)
plot(time, vel v)
grid on
xlabel('Time');
ylabel('Velocity_v');
figure(3)
plot(time,dragF)
xlabel('Time');
ylabel('Force');
```



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