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Practice Questions for Recursion | Set 1

Explain the functionality of following functions.

Question 1

```
int fun1(int x, int y)
{
    if(x == 0)
        return y;
    else
        return fun1(x - 1, x + y);
}
```

Answer: The function fun() calculates and returns $((1 + 2 \dots + x-1 + x) + y)$ which is $x(x+1)/2 + y$. For example if x is 5 and y is 2, then fun should return $15 + 2 = 17$.

Question 2

```
void fun2(int arr[], int start_index, int end_index)
{
    if(start_index >= end_index)
        return;
    int min_index;
    int temp;

    /* Assume that minIndex() returns index of minimum value in
       array arr[start_index...end_index] */
    min_index = minIndex(arr, start_index, end_index);

    temp = arr[start_index];
    arr[start_index] = arr[min_index];
    arr[min_index] = temp;

    fun2(arr, start_index + 1, end_index);
}
```

Answer: The function `fun2()` is a recursive implementation of [Selection Sort](#).

Please write comments if you find any of the answers/codes incorrect, or you want to share more information about the topics discussed above.

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/practice-questions-for-recursion/>

Print all possible strings of length k that can be formed from a set of n characters

Given a set of characters and a positive integer k, print all possible strings of length k that can be formed from the given set.

Examples:

Input:
`set[] = {'a', 'b'}, k = 3`

Output:
aaa
aab
aba
abb
baa
bab
bba
bbb

Input:
`set[] = {'a', 'b', 'c', 'd'}, k = 1`
Output:
a
b
c
d

For a given set of size n, there will be n^k possible strings of length k. The idea is to start from an empty output string (we call it *prefix* in following code). One

by one add all characters to *prefix*. For every character added, print all possible strings with current prefix by recursively calling for k equals to k-1. Following is Java implementation for same.

```
// Java program to print all possible strings of length k
class PrintAllKLengthStrings {

    // Driver method to test below methods
    public static void main(String[] args) {
        System.out.println("First Test");
        char set1[] = {'a', 'b'};
        int k = 3;
        printAllKLength(set1, k);

        System.out.println("\nSecond Test");
        char set2[] = {'a', 'b', 'c', 'd'};
        k = 1;
        printAllKLength(set2, k);
    }

    // The method that prints all possible strings of length k. It is
    // mainly a wrapper over recursive function printAllKLengthRec()
    static void printAllKLength(char set[], int k) {
        int n = set.length;
        printAllKLengthRec(set, "", n, k);
    }

    // The main recursive method to print all possible strings of length k
    static void printAllKLengthRec(char set[], String prefix, int n, int k) {

        // Base case: k is 0, print prefix
        if (k == 0) {
            System.out.println(prefix);
            return;
        }

        // One by one add all characters from set and recursively
        // call for k equals to k-1
        for (int i = 0; i < n; ++i) {

            // Next character of input added
            String newPrefix = prefix + set[i];

            // k is decreased, because we have added a new character
            printAllKLengthRec(set, newPrefix, n, k - 1);
        }
    }
}
```

```
    }  
}
```

Output:

First Test

```
aaa  
aab  
aba  
abb  
baa  
bab  
bba  
bbb
```

Second Test

```
a  
b  
c  
d
```

The above solution is mainly generalization of [this post](#).

This article is contributed by [Abhinav Ramana](#). Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above

Tags: [combinatorics](#), [Java](#), [Recursion](#)

Source

<http://www.geeksforgeeks.org/print-all-combinations-of-given-length/>

Print all possible combinations of r elements in a given array of size n

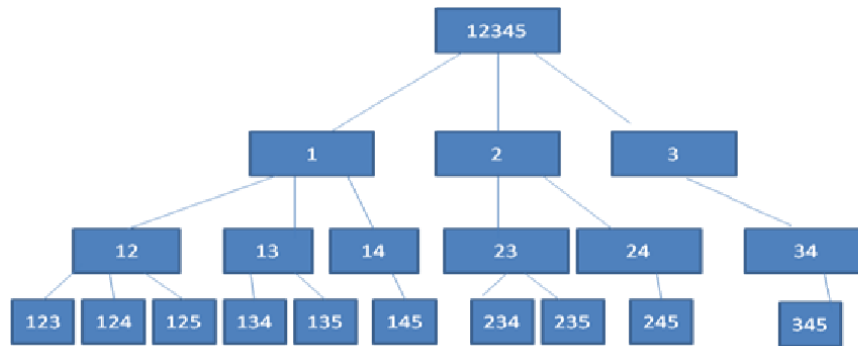
Given an array of size n, generate and print all possible combinations of r elements in array. For example, if input array is {1, 2, 3, 4} and r is 2, then output should be {1, 2}, {1, 3}, {1, 4}, {2, 3}, {2, 4} and {3, 4}.

Following are two methods to do this.

Method 1 (Fix Elements and Recur)

We create a temporary array 'data[]' which stores all outputs one by one. The idea is to start from first index (index = 0) in data[], one by one fix elements at this index and recur for remaining indexes. Let the input array be {1, 2, 3, 4, 5} and r be 3. We first fix 1 at index 0 in data[], then recur for remaining indexes, then we fix 2 at index 0 and recur. Finally, we fix 3 and recur for remaining indexes. When number of elements in data[] becomes equal to r (size of a combination), we print data[].

Following diagram shows recursion tree for same input.



Following is C++ implementation of above approach.

```
// Program to print all combination of size r in an array of size n
#include <stdio.h>
void combinationUtil(int arr[], int data[], int start, int end, int index, int r);

// The main function that prints all combinations of size r
// in arr[] of size n. This function mainly uses combinationUtil()
void printCombination(int arr[], int n, int r)
{
    // A temporary array to store all combination one by one
    int data[r];

    // Print all combination using temprary array 'data[]'
    combinationUtil(arr, data, 0, n-1, 0, r);
}

/* arr[] ---> Input Array
   data[] ---> Temporary array to store current combination
   start & end ---> Staring and Ending indexes in arr[]
   index ---> Current index in data[]
   r ---> Size of a combination to be printed */
void combinationUtil(int arr[], int data[], int start, int end, int index, int r)
```

```

{
    // Current combination is ready to be printed, print it
    if (index == r)
    {
        for (int j=0; j<r; j++)
            printf("%d ", data[j]);
        printf("\n");
        return;
    }

    // replace index with all possible elements. The condition
    // "end-i+1 >= r-index" makes sure that including one element
    // at index will make a combination with remaining elements
    // at remaining positions
    for (int i=start; i<=end && end-i+1 >= r-index; i++)
    {
        data[index] = arr[i];
        combinationUtil(arr, data, i+1, end, index+1, r);
    }
}

// Driver program to test above functions
int main()
{
    int arr[] = {1, 2, 3, 4, 5};
    int r = 3;
    int n = sizeof(arr)/sizeof(arr[0]);
    printCombination(arr, n, r);
}

```

Output:

```

1 2 3
1 2 4
1 2 5
1 3 4
1 3 5
1 4 5
2 3 4
2 3 5
2 4 5
3 4 5

```

How to handle duplicates?

Note that the above method doesn't handle duplicates. For example, if input

array is {1, 2, 1} and r is 2, then the program prints {1, 2} and {2, 1} as two different combinations. We can avoid duplicates by adding following two additional things to above code.

- 1) Add code to sort the array before calling combinationUtil() in printCombination()
- 2) Add following lines at the end of for loop in combinationUtil()

```
// Since the elements are sorted, all occurrences of an element
// must be together
while (arr[i] == arr[i+1])
    i++;
```

See [this](#) for an implementation that handles duplicates.

Method 2 (Include and Exclude every element)

Like the above method, We create a temporary array data[]. The idea here is similar to [Subset Sum Problem](#). We one by one consider every element of input array, and recur for two cases:

- 1) The element is included in current combination (We put the element in data[] and increment next available index in data[])
- 2) The element is excluded in current combination (We do not put the element and do not change index)

When number of elements in data[] become equal to r (size of a combination), we print it.

This method is mainly based on [Pascal's Identity](#), i.e. $n_{c_r} = n-1_{c_r} + n-1_{c_{r-1}}$

Following is C++ implementation of method 2.

```
// Program to print all combination of size r in an array of size n
#include<stdio.h>
void combinationUtil(int arr[],int n,int r,int index,int data[],int i);

// The main function that prints all combinations of size r
// in arr[] of size n. This function mainly uses combinationUtil()
void printCombination(int arr[], int n, int r)
{
    // A temporary array to store all combination one by one
    int data[r];

    // Print all combination using temprary array 'data[]'
    combinationUtil(arr, n, r, 0, data, 0);
}

/* arr[] ---> Input Array
```

```

n      ---> Size of input array
r      ---> Size of a combination to be printed
index  ---> Current index in data[]
data[] ---> Temporary array to store current combination
i      ---> index of current element in arr[]      */
void combinationUtil(int arr[], int n, int r, int index, int data[], int i)
{
    // Current combination is ready, print it
    if (index == r)
    {
        for (int j=0; j<r; j++)
            printf("%d ",data[j]);
        printf("\n");
        return;
    }

    // When no more elements are there to put in data[]
    if (i >= n)
        return;

    // current is included, put next at next location
    data[index] = arr[i];
    combinationUtil(arr, n, r, index+1, data, i+1);

    // current is excluded, replace it with next (Note that
    // i+1 is passed, but index is not changed)
    combinationUtil(arr, n, r, index, data, i+1);
}

// Driver program to test above functions
int main()
{
    int arr[] = {1, 2, 3, 4, 5};
    int r = 3;
    int n = sizeof(arr)/sizeof(arr[0]);
    printCombination(arr, n, r);
    return 0;
}

```

Output:

```

1 2 3
1 2 4
1 2 5
1 3 4

```



```
1 3 5
1 4 5
2 3 4
2 3 5
2 4 5
3 4 5
```

How to handle duplicates in method 2?

Like method 1, we can follow two things to handle duplicates.

- 1) Add code to sort the array before calling combinationUtil() in printCombination()
- 2) Add following lines between two recursive calls of combinationUtil() in combinationUtil()

```
// Since the elements are sorted, all occurrences of an element
// must be together
while (arr[i] == arr[i+1])
    i++;
```

See [this](#) for an implementation that handles duplicates.

This article is contributed by **Bateesh**. Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above

Tags: [MathematicalAlgo](#), [Recursion](#)

Source

<http://www.geeksforgeeks.org/print-all-possible-combinations-of-r-elements-in-a-given-array-of-size-n/>

Print all increasing sequences of length k from first n natural numbers

Given two positive integers n and k, print all increasing sequences of length k such that the elements in every sequence are from first n natural numbers.

Examples:

Input: k = 2, n = 3

Output: 1 2
 1 3

2 3

Input: k = 5, n = 5

Output: 1 2 3 4 5

Input: k = 3, n = 5

Output: 1 2 3

1 2 4

1 2 5

1 3 4

1 3 5

1 4 5

2 3 4

2 3 5

2 4 5

3 4 5

We strongly recommend to minimize the browser and try this yourself first.

It's a good recursion question. The idea is to create an array of length k. The array stores current sequence. For every position in array, we check the previous element and one by one put all elements greater than the previous element. If there is no previous element (first position), we put all numbers from 1 to n.

Following is C++ implementation of above idea.

```
// C++ program to print all increasing sequences of
// length 'k' such that the elements in every sequence
// are from first 'n' natural numbers.
#include<iostream>
using namespace std;

// A utility function to print contents of arr[0..k-1]
void printArr(int arr[], int k)
{
    for (int i=0; i<k; i++)
        cout << arr[i] << " ";
    cout << endl;
}

// A recursive function to print all increasing sequences
// of first n natural numbers. Every sequence should be
// length k. The array arr[] is used to store current
// sequence.
void printSeqUtil(int n, int k, int &len, int arr[])
```

```

{
    // If length of current increasing sequence becomes k,
    // print it
    if (len == k)
    {
        printArr(arr, k);
        return;
    }

    // Decide the starting number to put at current position:
    // If length is 0, then there are no previous elements
    // in arr[]. So start putting new numbers with 1.
    // If length is not 0, then start from value of
    // previous element plus 1.
    int i = (len == 0)? 1 : arr[len-1] + 1;

    // Increase length
    len++;

    // Put all numbers (which are greater than the previous
    // element) at new position.
    while (i<=n)
    {
        arr[len-1] = i;
        printSeqUtil(n, k, len, arr);
        i++;
    }

    // This is important. The variable 'len' is shared among
    // all function calls in recursion tree. Its value must be
    // brought back before next iteration of while loop
    len--;
}

// This function prints all increasing sequences of
// first n natural numbers. The length of every sequence
// must be k. This function mainly uses printSeqUtil()
void printSeq(int n, int k)
{
    int arr[k]; // An array to store individual sequences
    int len = 0; // Initial length of current sequence
    printSeqUtil(n, k, len, arr);
}

// Driver program to test above functions
int main()

```

```
{
    int k = 3, n = 7;
    printSeq(n, k);
    return 0;
}
```

Output:

```
1 2 3
1 2 4
1 2 5
1 2 6
1 2 7
1 3 4
1 3 5
1 3 6
1 3 7
1 4 5
1 4 6
1 4 7
1 5 6
1 5 7
1 6 7
2 3 4
2 3 5
2 3 6
2 3 7
2 4 5
2 4 6
2 4 7
2 5 6
2 5 7
2 6 7
3 4 5
3 4 6
3 4 7
3 5 6
3 5 7
3 6 7
4 5 6
4 5 7
4 6 7
5 6 7
```

This article is contributed by **Arjun**. Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/print-increasing-sequences-length-k-first-n-natural-numbers/>

Recursive Functions

Recursion:

In programming terms a recursive function can be defined as a routine that calls itself directly or indirectly.

Using recursive algorithm, certain problems can be solved quite easily. [Towers of Hanoi \(TOH\)](#) is one such programming exercise. Try to write an *iterative* algorithm for TOH. Moreover, every recursive program can be written using iterative methods (Refer Data Structures by Lipschutz).

Mathematically recursion helps to solve few puzzles easily.

For example, a routine interview question,

In a party of N people, each person will shake her/his hand with each other person only once. On total how many hand-shakes would happen?

Solution:

It can be solved in different ways, graphs, recursion, etc. Let us see, how recursively it can be solved.

There are N persons. Each person shake-hand with each other only once. Considering N-th person, (s)he has to shake-hand with (N-1) persons. Now the problem reduced to small instance of (N-1) persons. Assuming T_N as total shake-hands, it can be formulated recursively.

$T_N = (N-1) + T_{N-1}$ [$T_1 = 0$, i.e. the last person have already shook-hand with every one]

Solving it recursively yields an arithmetic series, which can be evaluated to $N(N-1)/2$.

Exercise: In a party of N couples, only one gender (either male or female) can shake hand with every one. How many shake-hands would happen?

Usually recursive programs results in poor time complexities. An example is Fibonacci series. The time complexity of calculating n-th Fibonacci number using recursion is approximately 1.6^n . It means the same computer takes almost 60% more time for next Fibonacci number. Recursive Fibonacci algorithm has

overlapped subproblems. There are other techniques like *dynamic programming* to improve such overlapped algorithms.

However, few algorithms, (e.g. merge sort, quick sort, etc...) results in optimal time complexity using recursion.

Base Case:

One critical requirement of recursive functions is termination point or base case. Every recursive program must have base case to make sure that the function will terminate. Missing base case results in unexpected behaviour.

Different Ways of Writing Recursive Functions in C/C++:

Function calling itself: (Direct way)

Most of us aware atleast two different ways of writing recursive programs. Given below is towers of Hanoi code. It is an example of direct calling.

```
// Assuming n-th disk is bottom disk (count down)
void tower(int n, char sourcePole, char destinationPole, char auxiliaryPole)
{
    // Base case (termination condition)
    if(0 == n)
        return;

    // Move first n-1 disks from source pole
    // to auxiliary pole using destination as
    // temporary pole
    tower(n-1, sourcePole, auxiliaryPole,
        destinationPole);

    // Move the remaining disk from source
    // pole to destination pole
    printf("Move the disk %d from %c to %c\n", n,
        sourcePole, destinationPole);

    // Move the n-1 disks from auxiliary (now source)
    // pole to destination pole using source pole as
    // temporary (auxiliary) pole
    tower(n-1, auxiliaryPole, destinationPole,
        sourcePole);
}

void main()
{
    tower(3, 'S', 'D', 'A');
}
```

The time complexity of TOH can be calculated by formulating number of moves.

We need to move the first N-1 disks from Source to Auxiliary and from Auxiliary to Destination, i.e. the first N-1 disks requires two moves. One more move of last disk from Source to Destination. Mathematically it can be defined recursively.

$$M_N = 2M_{N-1} + 1.$$

We can easily solve the above recursive relation ($2^N - 1$), which is exponential.

Recursion using mutual function call: (Indirect way)

Indirect calling. Though least practical, a function [funA()] can call another function [funB()] which in turn calls [funA()] former function. In this case both the functions should have the base case.

Defensive Programming:

We can combine defensive coding techniques with recursion for graceful functionality of application. Usually recursive programming is not allowed in safety critical applications, such as flight controls, health monitoring, etc. However, one can use a static count technique to avoid uncontrolled calls (NOT in safety critical systems, may be used in soft real time systems).

```
void recursive(int data)
{
    static callDepth;
    if(callDepth > MAX_DEPTH)
        return;

    // Increase call depth
    callDepth++;

    // do other processing
    recursive(data);

    // do other processing
    // Decrease call depth
    callDepth--;
}
```

callDepth depth depends on function stack frame size and maximum stack size.

Recursion using function pointers: (Indirect way)

Recursion can also be implemented with function pointers. An example is signal handler in POSIX compliant systems. If the handler causes to trigger same event due to which the handler is being called, the function will reenter.

We will cover function pointer approach and iterative solution to TOH puzzle in later article.

Thanks to Venki for writing the above post. Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above.

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/recursive-functions/>

Reverse a stack using recursion

You are not allowed to use loop constructs like while, for..etc, and you can only use the following ADT functions on Stack S:

isEmpty(S)

push(S)

pop(S)

Solution:

The idea of the solution is to hold all values in Function Call Stack until the stack becomes empty. When the stack becomes empty, insert all held items one by one at the bottom of the stack.

For example, let the input stack be

1

First 4 is inserted at the bottom.

4

So we need a function that inserts at the bottom of a stack using the above given basic stack functions.

```
void insertAtBottom(struct sNode** top_ref, int item)
{
    int temp;
    if(isEmpty(*top_ref))
    {
        push(top_ref, item);
    }
    else
    {
```



```

        /* Hold all items in Function Call Stack until we reach end of
        the stack. When the stack becomes empty, the isEmpty(*top_ref)
        becomes true, the above if part is executed and the item is
        inserted at the bottom */
        temp = pop(top_ref);
        insertAtBottom(top_ref, item);

        /* Once the item is inserted at the bottom, push all the
        items held in Function Call Stack */
        push(top_ref, temp);
    }
}

```

//Below is the function that reverses the given stack using insertAtBottom()

```

void reverse(struct sNode** top_ref)
{
    int temp;
    if(!isEmpty(*top_ref))
    {

        /* Hold all items in Function Call Stack until we reach end of
        the stack */
        temp = pop(top_ref);
        reverse(top_ref);

        /* Insert all the items (held in Function Call Stack) one by one
        from the bottom to top. Every item is inserted at the bottom */
        insertAtBottom(top_ref, temp);
    }
}

```

//Below is a complete running program for testing above functions.

```

#include<stdio.h>
#include<stdlib.h>
#define bool int

/* structure of a stack node */
struct sNode
{
    char data;
    struct sNode *next;
};

```

```

/* Function Prototypes */
void push(struct sNode** top_ref, int new_data);
int pop(struct sNode** top_ref);
bool isEmpty(struct sNode* top);
void print(struct sNode* top);

/* Driver program to test above functions */
int main()
{
    struct sNode *s = NULL;
    push(&s, 4);
    push(&s, 3);
    push(&s, 2);
    push(&s, 1);

    printf("\n Original Stack ");
    print(s);
    reverse(&s);
    printf("\n Reversed Stack ");
    print(s);
    getchar();
}

/* Function to check if the stack is empty */
bool isEmpty(struct sNode* top)
{
    return (top == NULL)? 1 : 0;
}

/* Function to push an item to stack*/
void push(struct sNode** top_ref, int new_data)
{
    /* allocate node */
    struct sNode* new_node =
        (struct sNode*) malloc(sizeof(struct sNode));

    if(new_node == NULL)
    {
        printf("Stack overflow \n");
        getchar();
        exit(0);
    }

    /* put in the data */
    new_node->data = new_data;

```

```

    /* link the old list off the new node */
    new_node->next = (*top_ref);

    /* move the head to point to the new node */
    (*top_ref) = new_node;
}

/* Function to pop an item from stack*/
int pop(struct sNode** top_ref)
{
    char res;
    struct sNode *top;

    /*If stack is empty then error */
    if(*top_ref == NULL)
    {
        printf("Stack overflow \n");
        getchar();
        exit(0);
    }
    else
    {
        top = *top_ref;
        res = top->data;
        *top_ref = top->next;
        free(top);
        return res;
    }
}

/* Function to print a linked list */
void print(struct sNode* top)
{
    printf("\n");
    while(top != NULL)
    {
        printf(" %d ", top->data);
        top = top->next;
    }
}

```

Please write comments if you find any bug in above code/algorithm, or find other ways to solve the same problem.

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/reverse-a-stack-using-recursion/>

Tail Recursion

What is tail recursion?

A recursive function is tail recursive when recursive call is the last thing executed by the function. For example the following C++ function `print()` is tail recursive.

```
// An example of tail recursive function
void print(int n)
{
    if (n < 0) return;
    cout << " " << n;

    // The last executed statement is recursive call
    print(n-1);
}
```

Why do we care?

The tail recursive functions considered better than non tail recursive functions as tail-recursion can be optimized by compiler. The idea used by compilers to optimize tail-recursive functions is simple, since the recursive call is the last statement, there is nothing left to do in the current function, so saving the current function's stack frame is of no use.

Can a non-tail recursive function be written as tail-recursive to optimize it?

Consider the following function to calculate factorial of `n`. It is a non-tail-recursive function. Although it looks like a tail recursive at first look. If we take a closer look, we can see that the value returned by `fact(n-1)` is used in `fact(n)`, so the call to `fact(n-1)` is not the last thing done by `fact(n)`

```
#include<iostream>
using namespace std;

// A NON-tail-recursive function. The function is not tail
// recursive because the value returned by fact(n-1) is used in
// fact(n) and call to fact(n-1) is not the last thing done by fact(n)
```

```

unsigned int fact(unsigned int n)
{
    if (n == 0) return 1;

    return n*fact(n-1);
}

// Driver program to test above function
int main()
{
    cout << fact(5);
    return 0;
}

```

The above function can be written as a tail recursive function. The idea is to use one more argument and accumulate the factorial value in second argument. When n reaches 0, return the accumulated value.

```

#include<iostream>
using namespace std;

// A tail recursive function to calculate factorial
unsigned factTR(unsigned int n, unsigned int a)
{
    if (n == 0) return a;

    return factTR(n-1, n*a);
}

// A wrapper over factTR
unsigned int fact(unsigned int n)
{
    return factTR(n, 1);
}

// Driver program to test above function
int main()
{
    cout << fact(5);
    return 0;
}

```

We will soon be discussing more on tail recursion.

References:

http://en.wikipedia.org/wiki/Tail_call
<http://c2.com/cgi/wiki?TailRecursion>

Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/tail-recursion/>

Practice Questions for Recursion | Set 2

Explain the functionality of following functions.

Question 1

```
/* Assume that n is greater than or equal to 1 */
int fun1(int n)
{
    if(n == 1)
        return 0;
    else
        return 1 + fun1(n/2);
}
```

Answer: The function calculates and returns $\lfloor \log_2(n) \rfloor$. For example, if n is between 8 and 15 then fun1() returns 3. If n is between 16 to 31 then fun1() returns 4.

Question 2

```
/* Assume that n is greater than or equal to 0 */
void fun2(int n)
{
    if(n == 0)
        return;

    fun2(n/2);
    printf("%d", n%2);
}
```

Answer: The function fun2() prints binary equivalent of n. For example, if n is 21 then fun2() prints 10101.

Note that above functions are just for practicing recursion, they are not the ideal implementation of the functionality they provide.

Please write comments if you find any of the answers/codes incorrect.

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/practice-questions-for-recursion-set-2/>

Practice Questions for Recursion | Set 3

Explain the functionality of below recursive functions.

Question 1

```
void fun1(int n)
{
    int i = 0;
    if (n > 1)
        fun1(n-1);
    for (i = 0; i < n; i++)
        printf(" * ");
}
```

Answer: Total numbers of stars printed is equal to $1 + 2 + \dots + (n-2) + (n-1) + n$, which is $n(n+1)/2$.

Question 2

```
#define LIMIT 1000
void fun2(int n)
{
    if (n <= 0)
        return;
    if (n > LIMIT)
        return;
    printf("%d ", n);
    fun2(2*n);
    printf("%d ", n);
}
```

Answer: For a positive n , $\text{fun2}(n)$ prints the values of n , $2n$, $4n$, $8n$... while the value is smaller than LIMIT . After printing values in increasing order, it prints same numbers again in reverse order. For example $\text{fun2}(100)$ prints 100, 200, 400, 800, 800, 400, 200, 100.

If n is negative, then it becomes a non-terminating recursion and causes overflow.

Please write comments if you find any of the answers/codes incorrect, or you want to share more information about the topics discussed above.

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/practice-questions-for-recursion-set-3/>

Practice Questions for Recursion | Set 4

Question 1

Predict the output of following program.

```
#include<stdio.h>
void fun(int x)
{
    if(x > 0)
    {
        fun(--x);
        printf("%d\t", x);
        fun(--x);
    }
}

int main()
{
    int a = 4;
    fun(a);
    getchar();
    return 0;
}
```

Output: 0 1 2 0 3 0 1


```

        fun(4);
        /
        fun(3), print(3), fun(2)(prints 0 1)
        /
        fun(2), print(2), fun(1)(prints 0)
        /
        fun(1), print(1), fun(0)(does nothing)
        /
        fun(0), print(0), fun(-1) (does nothing)

```

Question 2

Predict the output of following program. What does the following fun() do in general?

```

int fun(int a[],int n)
{
    int x;
    if(n == 1)
        return a[0];
    else
        x = fun(a, n-1);
    if(x > a[n-1])
        return x;
    else
        return a[n-1];
}

int main()
{
    int arr[] = {12, 10, 30, 50, 100};
    printf(" %d ", fun(arr, 5));
    getchar();
    return 0;
}

```

Output: 100

fun() returns the maximum value in the input array a[] of size n.

Question 3

Predict the output of following program. What does the following fun() do in general?

```

int fun(int i)
{
    if ( i%2 ) return (i++);
}

```

```

        else return fun(fun( i - 1 ));
    }

    int main()
    {
        printf(" %d ", fun(200));
        getchar();
        return 0;
    }

```

Output: 199

If n is odd then returns n, else returns (n-1). Eg., for n = 12, you get 11 and for n = 11 you get 11. The statement “*return i++;*” returns value of i only as it is a post increment.

Please write comments if you find any of the answers/codes incorrect, or you want to share more information/questions about the topics discussed above.

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/practice-questions-for-recursion-set-4/>

Practice Questions for Recursion | Set 5

Question 1

Predict the output of following program. What does the following fun() do in general?

```

#include<stdio.h>

int fun(int a, int b)
{
    if (b == 0)
        return 0;
    if (b % 2 == 0)
        return fun(a+a, b/2);

    return fun(a+a, b/2) + a;
}

```

```

int main()
{
    printf("%d", fun(4, 3));
    getchar();
    return 0;
}

```

Output: 12

It calculates $a*b$ (a multiplied b).

Question 2

In question 1, if we replace $+$ with $*$ and replace $\text{return } 0$ with $\text{return } 1$, then what does the changed function do? Following is the changed function.

```

#include<stdio.h>

int fun(int a, int b)
{
    if (b == 0)
        return 1;
    if (b % 2 == 0)
        return fun(a*a, b/2);

    return fun(a*a, b/2)*a;
}

int main()
{
    printf("%d", fun(4, 3));
    getchar();
    return 0;
}

```

Output: 64

It calculates a^b (a raised to power b).

Question 3

Predict the output of following program. What does the following `fun()` do in general?

```

#include<stdio.h>

int fun(int n)
{
    if (n > 100)

```

```

        return n - 10;
    return fun(fun(n+11));
}

int main()
{
    printf(" %d ", fun(99));
    getchar();
    return 0;
}

```

Output: 91

```

fun(99) = fun(fun(110)) since 99 > 100
        = fun(100)      since 110 > 100
        = fun(fun(111)) since 100 > 100
        = fun(101)      since 111 > 100
        = 91            since 101 > 100

```

Returned value of fun() is 91 for all integer arguments $n \geq 101$. This function is known as [McCarthy 91 function](#).

Please write comments if you find any of the answers/codes incorrect, or you want to share more information/questions about the topics discussed above.

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/practice-questions-for-recursion-set-5/>

Practice Questions for Recursion | Set 6

Question 1

Consider the following recursive C function. Let len be the length of the string s and num be the number of characters printed on the screen, give the relation between num and len where len is always greater than 0.

```

void abc(char *s)
{
    if(s[0] == '\0')
        return;

```

```

    abc(s + 1);
    abc(s + 1);
    printf("%c", s[0]);
}

```

Following is the relation between *num* and *len*.

```

num = 2^len-1

s[0] is 1 time printed
s[1] is 2 times printed
s[2] is 4 times printed
s[i] is printed 2^i times
s[strlen(s)-1] is printed 2^(strlen(s)-1) times
total = 1+2+...+2^(strlen(s)-1)
        = (2^strlen(s)) - 1

```

For example, the following program prints 7 characters.

```

#include<stdio.h>

void abc(char *s)
{
    if(s[0] == '\0')
        return;

    abc(s + 1);
    abc(s + 1);
    printf("%c", s[0]);
}

int main()
{
    abc("xyz");
    return 0;
}

```

Thanks to [bharat nag](#) for suggesting this solution.

Question 2

```

#include<stdio.h>
int fun(int count)

```

```

{
    printf("%d\n", count);
    if(count < 3)
    {
        fun(fun(fun(++count)));
    }
    return count;
}

int main()
{
    fun(1);
    return 0;
}

```

Output:

```

1
2
3
3
3
3
3
3

```

The main() function calls fun(1). fun(1) prints “1” and calls fun(fun(fun(2))). fun(2) prints “2” and calls fun(fun(fun(3))). So the function call sequence becomes fun(fun(fun(fun(fun(3))))). fun(3) prints “3” and returns 3 (note that count is not incremented and no more functions are called as the if condition is not true for count 3). So the function call sequence reduces to fun(fun(fun(fun(3)))). fun(3) again prints “3” and returns 3. So the function call again reduces to fun(fun(fun(3))) which again prints “3” and reduces to fun(fun(3)). This continues and we get “3” printed 5 times on the screen.

Please write comments if you find any of the answers/codes incorrect, or you want to share more information/questions about the topics discussed above.

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/practice-questions-for-recursion-set-6/>

Practice Questions for Recursion | Set 7

Question 1 Predict the output of the following program. What does the following fun() do in general?

```
#include <stdio.h>

int fun ( int n, int *fp )
{
    int t, f;

    if ( n <= 1 )
    {
        *fp = 1;
        return 1;
    }
    t = fun ( n-1, fp );
    f = t + *fp;
    *fp = t;
    return f;
}

int main()
{
    int x = 15;
    printf("%d\n",fun(5, &x));

    return 0;
}
```

Output:

8

The program calculates nth Fibonacci Number. The statement `t = fun (n-1, fp)` gives the (n-1)th Fibonacci number and `*fp` is used to store the (n-2)th Fibonacci Number. Initial value of `*fp` (which is 15 in the above program) doesn't matter. Following recursion tree shows all steps from 1 to 10, for execution of `fun(5, &x)`.

```

      (1) fun(5, fp)
      /      \
(2) fun(4, fp)  (10) t = 5, f = 8, *fp = 5
   /      \

```

```

          (3) fun(3, fp)  (9) t = 3, f = 5, *fp = 3
        /      \
      (4) fun(2, fp)  (8) t = 2, f = 3, *fp = 2
    /      \
  (5) fun(1, fp)  (7) t = 1, f = 2, *fp = 1
  /
(6) *fp = 1

```

Question 2: Predict the output of the following program.

```

#include <stdio.h>

void fun(int n)
{
    if(n > 0)
    {
        fun(n-1);
        printf("%d ", n);
        fun(n-1);
    }
}

int main()
{
    fun(4);
    return 0;
}

```

Output

```
1 2 1 3 1 2 1 4 1 2 1 3 1 2 1
```

```

          fun(4)
        /
      fun(3), print(4), fun(3) [fun(3) prints 1 2 1 3 1 2 1]
    /
  fun(2), print(3), fun(2) [fun(2) prints 1 2 1]
  /
fun(1), print(2), fun(1) [fun(1) prints 1]
/
fun(0), print(1), fun(0) [fun(0) does nothing]

```

Please write comments if you find any of the answers/codes incorrect, or you want to share more information/questions about the topics discussed above.

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/practice-questions-for-recursion-set-7/>

Check if a number is Palindrome

Given an integer, write a function that returns true if the given number is palindrome, else false. For example, 12321 is palindrome, but 1451 is not palindrome.

Let the given number be *num*. A simple method for this problem is to first [reverse digits of num](#), then compare the reverse of *num* with *num*. If both are same, then return true, else false.

Following is an interesting method inspired from method#2 of [this post](#). The idea is to create a copy of *num* and recursively pass the copy by reference, and pass *num* by value. In the recursive calls, divide *num* by 10 while moving down the recursion tree. While moving up the recursion tree, divide the copy by 10. When they meet in a function for which all child calls are over, the last digit of *num* will be *i*th digit from the beginning and the last digit of copy will be *i*th digit from the end.

```
// A recursive C++ program to check whether a given number is
// palindrome or not
#include <stdio.h>

// A function that returns true only if num contains one digit
int oneDigit(int num)
{
    // comparison operation is faster than division operation.
    // So using following instead of "return num / 10 == 0;"
    return (num >= 0 && num < 10);
}

// A recursive function to find out whether num is palindrome
// or not. Initially, dupNum contains address of a copy of num.
bool isPalUtil(int num, int* dupNum)
{
    // Base case (needed for recursion termination): This statement
    // mainly compares the first digit with the last digit
    if (oneDigit(num))
        return (num == (*dupNum) % 10);

    // This is the key line in this method. Note that all recursive
    // calls have a separate copy of num, but they all share same copy
```

```

    // of *dupNum. We divide num while moving up the recursion tree
    if (!isPalUtil(num/10, dupNum))
        return false;

    // The following statements are executed when we move up the
    // recursion call tree
    *dupNum /= 10;

    // At this point, if num%10 contains i'th digit from beginning,
    // then (*dupNum)%10 contains i'th digit from end
    return (num % 10 == (*dupNum) % 10);
}

// The main function that uses recursive function isPalUtil() to
// find out whether num is palindrome or not
int isPal(int num)
{
    // If num is negative, make it positive
    if (num < 0)
        num = -num;

    // Create a separate copy of num, so that modifications made
    // to address dupNum don't change the input number.
    int *dupNum = new int(num); // *dupNum = num

    return isPalUtil(num, dupNum);
}

// Driver program to test above functions
int main()
{
    int n = 12321;
    isPal(n)? printf("Yes\n"): printf("No\n");

    n = 12;
    isPal(n)? printf("Yes\n"): printf("No\n");

    n = 88;
    isPal(n)? printf("Yes\n"): printf("No\n");

    n = 8999;
    isPal(n)? printf("Yes\n"): printf("No\n");
    return 0;
}

```

Output:

Yes
No
Yes
No

This article is compiled by [Aashish Barnwal](#). Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above.

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/check-if-a-number-is-palindrome/>

Practice questions for Linked List and Recursion

Assume the structure of a Linked List node is as follows.

```
struct node
{
    int data;
    struct node *next;
};
```

Explain the functionality of following C functions.

1. What does the following function do for a given Linked List?

```
void fun1(struct node* head)
{
    if(head == NULL)
        return;

    fun1(head->next);
    printf("%d ", head->data);
}
```

fun1() prints the given Linked List in reverse manner. For Linked List 1->2->3->4->5, fun1() prints 5->4->3->2->1.

2. What does the following function do for a given Linked List ?

```

void fun2(struct node* head)
{
    if(head== NULL)
        return;
    printf("%d  ", head->data);

    if(head->next != NULL )
        fun2(head->next->next);
    printf("%d  ", head->data);
}

```

fun2() prints alternate nodes of the given Linked List, first from head to end, and then from end to head. If Linked List has even number of nodes, then fun2() skips the last node. For Linked List 1->2->3->4->5, fun2() prints 1 3 5 5 3 1. For Linked List 1->2->3->4->5->6, fun2() prints 1 3 5 5 3 1.

Below is a complete running program to test above functions.

```

#include<stdio.h>
#include<stdlib.h>

/* A linked list node */
struct node
{
    int data;
    struct node *next;
};

/* Prints a linked list in reverse manner */
void fun1(struct node* head)
{
    if(head == NULL)
        return;

    fun1(head->next);
    printf("%d  ", head->data);
}

/* prints alternate nodes of a Linked List, first
from head to end, and then from end to head. */
void fun2(struct node* start)
{
    if(start == NULL)
        return;
    printf("%d  ", start->data);
}

```

```

        if(start->next != NULL )
            fun2(start->next->next);
        printf("%d ", start->data);
    }

/* UTILITY FUNCTIONS TO TEST fun1() and fun2() */
/* Given a reference (pointer to pointer) to the head
   of a list and an int, push a new node on the front
   of the list. */
void push(struct node** head_ref, int new_data)
{
    /* allocate node */
    struct node* new_node =
        (struct node*) malloc(sizeof(struct node));

    /* put in the data */
    new_node->data = new_data;

    /* link the old list off the new node */
    new_node->next = (*head_ref);

    /* move the head to point to the new node */
    (*head_ref) = new_node;
}

/* Drier program to test above functions */
int main()
{
    /* Start with the empty list */
    struct node* head = NULL;

    /* Using push() to construct below list
       1->2->3->4->5 */
    push(&head, 5);
    push(&head, 4);
    push(&head, 3);
    push(&head, 2);
    push(&head, 1);

    printf("\n Output of fun1() for list 1->2->3->4->5 \n");
    fun1(head);

    printf("\n Output of fun2() for list 1->2->3->4->5 \n");
    fun2(head);
}

```

```
    getchar();  
    return 0;  
}
```

Please write comments if you find any of the answers/explanations incorrect, or you want to share more information about the topics discussed above.

Tags: [Recursion](#)

Source

<http://www.geeksforgeeks.org/practice-questions-for-linked-list-and-recursion/>